

# GOODYEAR AEROSPACE

(NASA-CR-120261) USERS MANUAL: DYNAMICS  
OF TWO BODIES CONNECTED BY AN ELASTIC  
TETHER, SIX DEGREES OF FREEDOM FOREBODY  
AND FIVE DEGREES OF (Goodyear Aerospace  
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# GOODYEAR AEROSPACE CORPORATION

AKRON 15, OHIO

## USERS MANUAL

DYNAMICS OF TWO BODIES CONNECTED

BY AN ELASTIC TETHER - SIX DEGREES OF FREEDOM FOREBODY

AND FIVE DEGREES OF FREEDOM DECELERATOR

(REF. NASA CONTRACT NAS8-29144 S/A1)

BY

GEORGE R. DOYLE, JR.

&

JAMES W. BURBICK

GER-16047

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## ABSTRACT

One important aspect to recovering a body falling through the atmosphere, is to decelerate and stabilize it. This is usually accomplished by means of a parachute. The design of the recovery system necessitates a knowledge of the dynamics and loads during parachute deployment and inflation. In many cases, a pitch plane analysis will provide adequate information. However, if the body is in a general tumbling motion, it is necessary to analyze its motion in three dimensions.

This report contains the equations of motion and a computer program for the dynamics of a six degree of freedom body joined to a five degree of freedom body by a quasilinear elastic tether. The forebody is assumed to be a completely general rigid body with six degrees of freedom; the decelerator is also assumed to be rigid, but with only five degrees of freedom (symmetric about its longitudinal axis). The tether is represented by a spring and dashpot in parallel, where the spring constant is a function of tether elongation. Lagrange's equation is used to derive the equations of motion with the Lagrange multiplier technique used to express the constraint provided by the tether. A computer program is included which provides a time history of the dynamics of both bodies and the tension in the tether.

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NOMENCLATURE

The following is a list of variables used in the computer program and in the derivation of the equations as discussed in this report. A brief description and associated units are included.

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
A	a	Distance along the longitudinal axis of the forebody ( $X_b$ ) from the intersection of the body axes to the tether-forebody confluence point, positive towards the nose	(m)	ft
AA(6,4)		Dummy variables used to express incremental velocities of the forebody in the Runge-Kutta integration	(m/sec)	ft/sec or rad/sec
AALPDE(8)		An array of eight variables signifying angle-of-attack of the forebody used with damping coefficients		deg
AALPFE(16)		An array of sixteen variables signifying angle-of-attack of the forebody used with force coefficients		deg
AALPME(16)		An array of sixteen variables signifying angle-of-attack of the forebody used with moment coefficients		deg
AALPPE(8)		An array of eight variables signifying angles of attack of the decelerator		deg
AAM(8)		An array of eight variables signifying Mach number of the forebody used with force and moment coefficients		
AAMD(8)		An array of eight variables signifying Mach number of the forebody used with damping coefficients		
AAMP(8)		An array of eight variables signifying Mach number of the decelerator		
AERATO		Suspension Line AE Ratio (AERATO = $AE/AE_{Nylon}$ )		

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<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
AIPHI		Number of elements in PPHIE array ( = 2 to 8)		
AIPHID		Number of elements in PPHIDE array ( = 2 to 8)		
AJALPD		Number of elements in AALPDE array ( = 8)		
AJALPF		Number of elements in AALPFE array ( = 8 or 16)		
AJALPM		Number of elements in AALPME array ( = 8 or 16)		
AKAM		Number of elements in AAM array ( = 2 to 8)		
AKAMD		Number of elements in AAMD array ( = 2 to 8)		
ALPE	$\alpha$	Angle-of-attack of the forebody		deg
ALPPE	$\alpha_p$	Angle-of-attack of the decelerator		deg
AM		Mach number of the forebody		
AMAX1		Larger ordinate of two points on the longitudinal added mass versus $D_o$ log log plot	kg	slug
AMAX2		Smaller ordinate of two points on the longitudinal added mass versus $D_o$ log log plot	kg	slug
AMAY1		Larger ordinate of two points on the lateral added mass versus $D_o$ log log plot	kg	slug



<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
AMAY2		Smaller ordinate of two points on the lateral added mass versus $D_o$ log log plot	kg	slug
AMP		Mach number of the decelerator		
AP	$a_p$	Distance along the longitudinal axis of the decelerator ( $X_{pb}$ ) from the c.g. to the tether-decelerator confluence point	(m)	ft
AX		Exponent of longitudinal added mass equation (MPAL = RH000 * BX * DS ** AX)		
AY		Exponent of lateral added mass equation (MPAS = RH000 * BY * DS ** AY)		
B	b	Distance along the lateral axis of the forebody ( $Y_b$ ) from the intersection of the body axes to the tether-forebody confluence point, positive towards the left wing	(m)	ft
BB(5,4)		Dummy variables used to express incremental velocities of the decelerator in the Runge-Kutta integration	(m/sec)	ft/sec or rad/sec
BX		Coefficient of longitudinal added mass equation (MPAL = RH000 * BX * DS ** AX)		
BY		Coefficient of lateral added mass equation (MPAS = RH000 * BY * DS ** AY)		
C	c	Distance along the vertical axis of the forebody ( $Z_b$ ) from the intersection of the body axes to the tether-forebody confluence point, positive up	(m)	ft

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CA	$C_A$	Axial force coefficient of forebody		
CAP	$C_{AP}$	Axial force coefficient of decelerator		
CC(3,3)	$C_{ij}$	Elements of transformation matrix from inertial coordinates to body coordinates of the forebody		
CAA(8,16,8)		A three dimensional array of variables signifying axial force coefficients of the forebody corresponding to AAM(8), AALPFE(16), and PPHIE(8)		
CCAP(8,8)		A two dimensional array of 64 variables signifying axial force coefficients of the decelerator with respect to angle of attack corresponding to AAMP(1) thru AAMP(8)		
CCHI	$C_\chi$	$\cos(\chi)$		
CCHIP	$C_{\chi_p}$	$\cos(\chi_p)$		
CCLL(8,16,8)		A three dimensional array of variables signifying rolling moment coefficients of the forebody corresponding to AAM(8), AALPME(16), and PPHIE(8)		
CCLLP(8,8,8)		A three dimensional array of variables signifying roll damping coefficients of the forebody corresponding to AAMD(8), AALPDE(8), and PPHIDE(8)		
CCLM(8,16,8)		A three dimensional array of variables signifying pitching moment coefficients of the forebody corresponding to AAM(8), AALPME(16), and PPHIE(8)		

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CCLMQ(8,8,8)		A three dimensional array of variables signifying pitch damping coefficients of the forebody corresponding to AAMD(8), AALPDE(8), and PPHIDE(8)		
CCLN(8,16,8)		A three dimensional array of variables signifying yawing moment coefficients of the forebody corresponding to AAM(8), AALPME(16), and PPHIE(8)		
CCLNR(8,8,8)		A three dimensional array of variables signifying yaw damping coefficients of the forebody corresponding to AAM(8), AALPDE(8), and PPHIDE(8)		
CCN(8,16,8)		A three dimensional array of variables signifying normal force coefficients of the forebody corresponding to AAM(8), AALPFE(16), PPHIE(8)		
CCM(8,8)		A two dimensional array of 64 variables signifying the pitching moment coefficients of the decelerator with respect to angle of attack corresponding to AAMP(1) thru AAMP(8)		
CCNP(8,8)		A two dimensional array of 64 variables signifying the normal force coefficient of the decelerator with respect to angle of attack corresponding to AAMP(1) thru AAMP(8)		
CCP(3,3)	$C_{pij}$	Elements of transformation matrix from inertial coordinates to body coordinates of the decelerator		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CCRIT		c/cr = damping ratio = 0.06		
CCY(8,16,8)		A three dimensional array of variables signifying side force coefficients of the forebody corresponding to AAM(8), AALPFE(16), and PPHIE(8)		
CDAP		Drag area of decelerator	(m <sup>2</sup> )	ft <sup>2</sup>
	c.g.	Center of gravity		
CGAM	C <sub>γ</sub>	Cos(γ)		
CGAMP	C <sub>γ<sub>p</sub></sub>	Cos(γ <sub>p</sub> )		
CHIE	χ	Flight path angle of forebody in horizontal plane, measured from X axis toward Y axis		deg
CHIPE	χ <sub>p</sub>	Flight path angle of decelerator in horizontal plane, measured from X axis toward Y axis		deg
CLL	C <sub>l</sub>	Rolling moment coefficient of the forebody		
CLLP	C <sub>l<sub>p</sub></sub>	Rolling damping coefficient of the forebody		
CLM	C <sub>m</sub>	Pitching moment coefficient of the forebody		
CLMQ	C <sub>m<sub>q</sub></sub>	Pitch damping coefficient of the forebody		
CLN	C <sub>n</sub>	Yawing moment coefficient of the forebody		
CLNR	C <sub>n<sub>r</sub></sub>	Yaw damping coefficient of the forebody		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
CN	$C_N$	Normal force coefficient of the forebody		
CNP	$C_{Np}$	Normal force coefficient of the decelerator		
COM(20)		Input variable used to define computer simulation - up to eighty figures		
CPHI	$C_\phi$	$\text{Cos } (\phi)$		
CPHII	$C_{\phi_i}$	$\text{Cos } (\phi_i)$		
CPHIPI	$C_{\phi_{pi}}$	$\text{Cos } (\phi_{pi})$		
CPSI	$C_\psi$	$\text{Cos } (\psi)$		
CPSIP	$C_{\psi_p}$	$\text{Cos } (\psi_p)$		
CS	$C_s$	Damping coefficient of tether	$\frac{\text{N-sec}}{\text{m}}$	$\frac{\text{lb}_f\text{-sec}}{\text{ft}}$
CSIGP		Cosine of one half the apex angle of the cone formed by the suspension lines		
CTHE	$C_\theta$	$\text{Co } (\theta)$		
CTHEP	$C_{\theta_p}$	$\text{Cos } (\theta_p)$		
CY	$C_Y$	Side force coefficient of forebody		
D	d	Aerodynamic reference length of forebody	(m)	ft
D <sub>i</sub> (6,6)		A two dimensional array of variables signifying the coefficients of the second derivatives in the equations of motions	(kg) (kg-m <sup>2</sup> )	slug or slug-ft <sup>2</sup>
DDP(3,3)		A two dimensional array of variables signifying the coefficients of the second derivatives in the equations of motion of the decelerator	(kg) (kg-m <sup>2</sup> )	slugs or slug-ft <sup>2</sup>
DELSX		Total suspension line deflection array	m	ft

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DELTX		Total tether line deflection array	m	ft
DLTO		Initial elongation of tether beyond unstretched length. DLTO is negative if the forebody and decelerator confluence points are closer together than LTO	(m)	ft
DLTX		Tether deflection component in array element (DLX(I) associated with load PX(I)	m	ft
DLX		Effective spring deflection array	m	ft
DMD		Rate of change of longitudinal added mass	kg/sec	slug/sec
DP	$d_p$	Aerodynamic reference length of decelerator	(m)	ft
DPR		Degress per radian - 57.2957795		
DS		Parachute diameter associated with SP	m	ft
DSP		Parachute projected diameter associated with DS	m	ft
DSX1		Larger abscissa of two points on the longitudinal added mass versus $D_o$ log log plot	m	ft
DSX2		Smaller abscissa of two points on the longitudinal added mass versus $D_o$ log log plot	m	ft
DSY1		Larger abscissa of two points on the lateral added mass versus $D_o$ log log plot	m	ft

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
DSY2		Smaller abscissa of two points on the lateral added mass versus $D_0$ log log plot	m	ft
DT		Integration increment		sec
DTP		Number of integrations between data output		
DTF1		Number of integrations between data output when $T \leq TDTC$		
DT1		Integration increment when $T \leq TDTC$		sec
DTT		Estimated parachute system period/12	sec	sec
DYPR	q	Dynamic pressure of forebody	(N/m <sup>2</sup> )	lb <sub>f</sub> /ft <sup>2</sup>
DYPRP	q <sub>p</sub>	Dynamic pressure of decelerator	(N/m <sup>2</sup> )	lb <sub>f</sub> /ft <sup>2</sup>
EE(6)		An array signifying the nonhomogeneous terms in the six equations of motion of the forebody	(N/m) (N)	ft-lb <sub>f</sub> or lb <sub>f</sub>
EPL		Suspension line strain array	m/m	ft/ft
EPS		Number used to check for inconsistent equations in PIVERT Subroutine, $10^{-13}$		
EPSI		Number used to check if $\theta$ is approaching a singular point $\theta = \frac{2n+1}{2}\pi$ . If $\theta$ is approaching a singular point, the accelerations are kept fixed until this region is passed. EPSI = 0.0000061 freezes the accelerations if $\theta$ is within $0.2^\circ$ of a singular point.		
EPT		Tether line strain array	m/m	ft/ft

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ETA1		Number which controls DT if $\theta$ is near a singular point. ETA1 = 0.00061 sets $DT = DT1/5$ , if $\theta$ is within $2^\circ$ of a singularity		
FF(5)		An array signifying the accelerations of the decelerator	(m/sec)	ft/sec or rad/sec
FREQP		Estimated parachute system frequency	1/sec	1/sec
FSULT		Ultimate design factor of safety for parachute		
FX	$F_x$	Generalized force on forebody in X direction	(N)	lb <sub>f</sub>
FXB	$F_{xb}$	Body force in direction of $X_b$ due to aerodynamics	(N)	lb <sub>f</sub>
FXP	$F_{xp}$	Generalized force on decelerator in X direction	(N)	lb <sub>f</sub>
FXPB	$F_{xpb}$	Body force in direction of $X_{pb}$	(N)	lb <sub>f</sub>
FY	$F_y$	Generalized force on forebody in Y direction	(N)	lb <sub>f</sub>
FYB	$F_{yb}$	Body force in direction of $Y_b$ due to aerodynamics	(N)	lb <sub>f</sub>
FYP	$F_{yp}$	Generalized force on decelerator in Y direction	(N)	lb <sub>f</sub>
FYPB	$F_{ypb}$	Body force in direction of $Y_{pb}$	(N)	lb <sub>f</sub>
FZ	$F_z$	Generalized force on forebody in Z direction	(N)	lb <sub>f</sub>
FZB	$F_{zb}$	Body force in direction of $Z_b$ due to aerodynamics	(N)	lb <sub>f</sub>



<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
FZP	$F_{zp}$	Generalized force on decelerator in Z direction	(N)	lb <sub>f</sub>
FZPB	$F_{zpb}$	Body force in direction of $Z_{pb}$	(N)	lb <sub>f</sub>
G	g	Acceleration of gravity at Z	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
GAME	$\gamma$	Flight path angle of forebody in vertical plane		deg
GAMPE	$\gamma_p$	Flight path angle of decelerator in vertical plane		deg
GLOAD		Limit design load factor of forebody		
GO		Acceleration of gravity at earth's surface, 32.17	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
HHH		Altitude below which simulation is ended	(m)	ft
ICXO		Canopy roll moment of inertia about its C.M.	kg-m <sup>2</sup>	slug-ft <sup>2</sup>
ICYO		Canopy pitch moment of inertia about its C.M.	kg-m <sup>2</sup>	slug-ft <sup>2</sup>
IERSW		Variable signifying whether or not the equations being solved in subroutine PIVER are consistent		
ILXO		Parachute lines roll moment of inertia about its C.M.	kg-m <sup>2</sup>	slug-ft <sup>2</sup>
ILYO		Parachute lines pitch moment of inertia about its C.M.	kg-m <sup>2</sup>	slug-ft <sup>2</sup>
IXB	$I_{xb}$	Moment of inertia about $X_b$ axis	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
IXPB	$I_{xpb}$	Apparent moment of inertia about $X_{pb}$ axis	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
IXYB	$I_{xyb}$	Product of inertia associated with $X_b$ and $Y_b$ axes	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
IXZB	$I_{xzb}$	Product of inertia associated with $X_b$ and $Z_b$ axes	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
IYB	$I_{yb}$	Moment of inertia about $Y_b$ axis	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
IYPB	$I_{ypb}$	Apparent moment of inertia about $Y_{pb}$ axis	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
IYZB	$I_{yzb}$	Product of inertia associated with $Y_b$ and $Z_b$ axes	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
IZB	$I_{zb}$	Moment of inertia about $Z_b$ axis	(kg-m <sup>2</sup> )	slug-ft <sup>2</sup>
KS	$K_s$	Tether spring constant	(N/m)	lb <sub>f</sub> /ft
LS		Suspension line length	m	ft
LSCL		Distance along parachute centerline between the confluence point and the projected diameter plane	m	ft
LT	$L_T$	Tether length - distance between confluence points	(m)	ft
LTD	$\dot{L}_T$	Time rate of change of tether length	(m/sec)	ft/sec
LTO	$L_{TO}$	Unstretched tether length	(m)	ft
M	m	Mass of forebody	(kg)	slugs
MP	$m_p$	Real mass of decelerator	(kg)	slugs
MPAL		Added mass of the decelerator along $X_{pb}$ axis	(kg)	slugs

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<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
MPAS		Added mass of the decelerator along $Y_{pb}$ or $Z_{pb}$ axis	(kg)	slugs
MPL	$m_{pl}$	Apparent longitudinal ( $X_{pb}$ ) mass of decelerator	(kg)	slugs
MPS	$m_{ps}$	Apparent side ( $Y_{pb}$ or $Z_{pb}$ ) mass of decelerator	(kg)	slugs
NS		Number of parachute suspension lines		
NT		Number of tether lines		
OMETRC		Option variable: if OMETRC = 1., Input and Output are in the metric system. If OMETRC = 0.0 Input and Output are in the English system.		
OMXBE	$w_{xb}$	Angular velocity about $X_b$ axis		deg/sec
OMYBE	$w_{yb}$	Angular velocity about $Y_b$ axis		deg/sec
OMZBE	$w_{zb}$	Angular velocity about $Z_b$ axis		deg/sec
OPAM		Option variable: if OPAM = 1., added mass of the decelerator $\neq 0$ ; if OPAM = 0., added mass of decelerator = 0		
OPDA		Option variable: if OPDA = 1., damping moment coefficients of the forebody are read in as arrays; if OPDA = 0., damping moment coefficients are read in as constants		
OPOS		Option variable: if OPOS = 1., at least one of the c.g. offsets or products of inertia of the forebody $\neq 0$ .; if OPOS = 0., all c.g. offsets and products of inertia = 0.		

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
OPPLOT		Option variable: if OPPLOT = 1., a plot tape can be made; if OPPLOT = 0., no plot tape is made.		
OPPRIN		Option variable: if OPPRIN = 1., all aerodynamic coefficient arrays are printed out; if OPPRIN = 0., no aerodynamic coefficient arrays are printed out		
OPDT		Option for automatic DT determination (OPDT = 1)		
OPSP		Option for automatic parachute area calculations (OPSP = 1)		
OPSYM		Option variable: if OPSYM = 1., the forebody is aerodynamically symmetric such that $C_y = C_m = 0$ ; if OPSYM = 0., the forebody is not symmetric		
PCT01		Parachute overinflation at reefed stage (I). (percent/100)		
PCT01		Parachute overinflation at reefed stage 1. (percent/100)		
PCT02		Parachute overinflation at reefed stage 2. (percent/100)		
PCT03		Parachute overinflation at reefed stage 3. (percent/100)		
PHIAE		Aerodynamic roll angle of forebody, $0 \leq \text{PHIAE} \leq 180^\circ$		deg
PHIDDE	0	Angular acceleration about $X_b$ axis		deg/sec <sup>2</sup>
PHIDE	0	Angular velocity about $X_b$ axis		deg/sec <sup>2</sup>

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
PHIE	$\theta$	Euler angle rotation about $X_b$ axis		deg
PHIIE	$\theta_i$	Aerodynamic roll angle of forebody, $-180^\circ \leq \theta_i \leq 180^\circ$		deg
PHIPI	$\theta_{pi}$	Aerodynamic roll angle of decelerator, $-180^\circ \leq \theta_{pi} \leq 180^\circ$		deg
POROS		Parachute porosity. Use POROS = 0.15		
PPHIDE(8)		An array of eight variables signifying forebody roll angle used with damping coefficients		deg
PPHIE(8)		An array of eight variables signifying forebody roll angle used with force and moment coefficients		deg
PSIDDE	$\ddot{\psi}$	Angular acceleration of forebody about -Z axis		deg/sec <sup>2</sup>
PSIDE	$\dot{\psi}$	Angular velocity of forebody about -Z axis		deg/sec
PSIE	$\psi$	Euler angle rotation of forebody about -Z axis		deg
PSIPDE	$\dot{\psi}_p$	Angular velocity of decelerator about -Z axis		deg/sec
PSIPE	$\psi_p$	Angular rotation of decelerator about -Z axis		deg
PSPDDE	$\ddot{\psi}_p$	Angular acceleration of decelerator about -Z axis		deg/sec <sup>2</sup>
PULAN		Angle between tether and forebody centerline	deg	deg
PS		Suspension line load array	N	lb <sub>f</sub>

<u>FORTTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
PSX		Total suspension line load array	N	lb <sub>f</sub>
PT		Tether line load array	N	lb <sub>f</sub>
PTX		Total tether line array	N	lb <sub>f</sub>
PX		Effective spring load array	N	lb <sub>f</sub>
QMAXPB		Parachute load due to rate of change of mass of the parachute times the relative velocity, XPBDR	N	lb <sub>f</sub>
QPHI	$Q_{\theta}$	Generalized force about $X_b$ axis	(m-N)	ft-lb <sub>f</sub>
QPSI	$Q_{\psi}$	Generalized force of forebody about -Z axis	(m-N)	ft-lb <sub>f</sub>
QPSIP	$Q_{\psi p}$	Generalized for of decelerator about -Z axis	(m/N)	ft/lb <sub>f</sub>
QTHE	$Q_{\theta}$	Generalized force of forebody about negative line of modes	(m/N)	ft/lb <sub>f</sub>
QTHEP	$Q_{\theta p}$	Generalized force of decelerator about negative line of modes	(m/N)	ft/lb <sub>f</sub>
RATIO		Nondimensional length used in the decelerator's body torque expressions		
RE		Radius of earth - 20,926,435.	(m)	ft
RHO		Density of atmosphere at Z (1962 Standard)	(kg/m <sup>2</sup> )	slug/ft <sup>2</sup>
RHOOO		Air density ratio (RHO/RHOO)		
S	S	Aerodynamic reference area of forebody	(m <sup>2</sup> )	ft <sup>2</sup>
SCHI		sin ( $\chi$ )		
SCHIP		sin ( $\chi_p$ )		
SGAM		sin ( $\gamma$ )		

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
SGAMP		$\sin(\chi_p)$		
SP		Parachute drag area	m <sup>2</sup>	ft <sup>2</sup>
SPD		Time rate of change of parachute drag area	m <sup>2</sup> /sec	ft <sup>2</sup> /sec
SPHI	S $\theta$	$\sin(\theta)$		
SPHII	S $\theta_i$	$\sin(\theta_i)$		
SPHIPI	S $\theta_{pi}$	$\sin(\theta_{pi})$		
SPRQ		Initial parachute area	m <sup>2</sup>	ft <sup>2</sup>
SPR1		First reefed stage parachute drag area	m <sup>2</sup>	ft <sup>2</sup>
SPR2		Second reefed stage parachute drag area	m <sup>2</sup>	ft <sup>2</sup>
SPR3		Third reefed stage parachute drag area	m <sup>2</sup>	ft <sup>2</sup>
SPRL		Parachute drag area associated with reefed stage (I-1)	m <sup>2</sup>	ft <sup>2</sup>
SPRU		Parachute drag area associated with reefed stage (I)	m <sup>2</sup>	ft <sup>2</sup>
SPSI	S $\psi$	$\sin(\psi)$		
SPSIP	S $\psi_p$	$\sin(\psi_p)$		
SSP(16)		An array of sixteen variables signifying aerodynamic reference area of the decelerator corresponding to TTIP(16)	(M <sup>2</sup> )	ft <sup>2</sup>
STHE	S $\theta$	$\sin(\theta)$		
STHEP	S $\theta_p$	$\sin(\theta_p)$		
T		Flight time		sec
TENS		Tension in tether	N	lb <sub>f</sub>
THEDDE	' $\theta$ '	Angular acceleration of forebody about negative line of nodes		deg/sec <sup>2</sup>

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
THEDE	$\dot{\theta}$	Angular velocity of forebody about negative line of nodes		deg/sec <sup>2</sup>
THEE	$\theta$	Euler angle rotation of forebody about negative line of nodes		deg
THEPDE	$\dot{\theta}_p$	Angular velocity of decelerator about negative line of nodes		deg/sec
THEPE	$\theta_p$	Euler angle rotation of decelerator about negative line of nodes		deg
THPDDE	$\ddot{\theta}_p$	Angular acceleration of decelerator about negative line of nodes		deg/sec <sup>2</sup>
TFI		Parachute inflation time from Stage (I) to Stage (I + 1)	sec	sec
TINF		Time when inflated area first equals SPRU	sec	sec
TINT		Time at start of inflation of reefed stage (I)	sec	sec
TNINY		Total time spent in region where (1-ABS(SIN(TH E))). LT.EPSI)	sec	sec
TO		Initial time	sec	sec
TOIF		One half the time spent in the over- inflation of stage I	sec	sec
TOTRO		Time at start of inflation of first reefed stage	sec	sec
TOTR1		Time at start of inflation of second reefed stage	sec	sec
TOTR2		Time at start of inflation of third reefed stage	sec	sec



<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
TOTR3		Time at end . third reefed stage	sec	sec
TPD		Total tether load (tension + damping)	N	lb <sub>f</sub>
TPDRB		Component of tether load normal to forebody centerline	N	lb <sub>f</sub>
TPDXB		Tether load component along forebody XB axis	N	lb <sub>f</sub>
TPDYB		Tether load component along forebody YB axis	N	lb <sub>f</sub>
TPDZB		Tether load component along forebody ZB axis	N	lb <sub>f</sub>
TRO		Time from "TO" to start of inflation of first stage	sec	sec
TR1		Time from "TO" to start of inflation of second stage	sec	sec
TR2		Time from "TO" to start of inflation of third stage	sec	sec
TR3		Time from "TO" to end of third stage (TR3 > TTT)	sec	sec
TTIP(16)		An array of sixteen variables signifying inflation time events		sec
TXB	T <sub>xb</sub>	Torque about X <sub>b</sub> axis due to aerodynamics	(m-N)	ft-lb <sub>f</sub>
TTT		Flight time at which simulation is ended		sec
TYB	T <sub>yb</sub>	Torque about Y <sub>b</sub> axis due to aerodynamics	(m-N)	ft-lb <sub>f</sub>
TYPB	T <sub>ypb</sub>	Torque about X <sub>pb</sub> axis due to aerodynamics	(m-N)	ft-lb <sub>f</sub>
TZB	T <sub>zb</sub>	Torque about Z <sub>b</sub> axis due to aerodynamics	(M-N)	ft-lb <sub>f</sub>

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
TZPB	$T_{zpb}$	Torque about $Z_{pb}$ axis due to aerodynamics	(m-N)	ft-lb <sub>f</sub>
V		Total velocity of forebody	(m/sec)	ft/sec
VP		Total velocity of decelerator	(m/sec)	ft/sec
VS		Speed of sound at Z	(m/sec)	ft/sec
WT		Weight of forebody	(N)	lb
WTC		Parachute canopy weight	kg·m/sec <sup>2</sup>	lb
WTCM		Mass of parachute canopy	kg	slug
WTL		Parachute suspension lines weight	kg·m/sec <sup>2</sup>	lb
WTCM		Mass of parachute suspension lines	kg	slug
WTP		Weight of decelerator	(N)	lb
X	X	Down range inertial axis or displacement of forebody	(m)	ft
	$X_b$	Longitudinal body axis or displacement of forebody	(m)	ft
XBAR	$\bar{X}$	c.g. offset along $X_b$ axis	(m)	ft
XBD	$X_b$	$X_b$ body axis velocity	(m/sec)	ft/sec
X	$\dot{X}$	Down range velocity of forebody	(m/sec)	ft/sec
XDD	$\ddot{X}$	Down range acceleration of forebody	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
XP	$X_p$	Down range displacement of decelerator	(m)	ft
XPBD	$\dot{X}_{pb}$	$X_{pb}$ body axis velocity of decelerator	(m/sec)	ft/sec
XPBDR		Velocity of air entering or exiting the parachute relative to the parachute velocity	m/sec	ft/sec

<u>FOPIRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
XPBDI		Parachute velocity, XPBD, at T = TINT. It is used to calculate fill time	m/sec	ft/sec
XPB	$\dot{X}_p$	Down range velocity of decelerator	(m/sec)	ft/sec
XPDD	$\ddot{X}_p$	Down range acceleration of decelerator	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
Y	Y	Cross range inertial axis or displacement of forebody	(m)	ft
	$Y_b$	Lateral body axis or displacement of forebody	(m)	ft
YBAR	$\bar{Y}$	c.g. offset along $Y_b$ axis	(m)	ft
YBD	$\dot{Y}_b$	$Y_b$ body axis velocity	(m/sec)	ft/sec
YD	$\dot{Y}$	Cross range velocity of forebody	(m/sec)	ft/sec
YDD	$\ddot{Y}$	Cross range acceleration of forebody	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
YP	$Y_p$	Cross range inertial displacement of decelerator	(m)	ft
YPBD	$\dot{Y}_{pb}$	$Y_{pb}$ body axis velocity of decelerator	(m/sec)	ft/sec
YPD	$\dot{Y}_p$	Cross range velocity of decelerator	(m/sec)	ft/sec
YPDD	$\ddot{Y}_p$	Cross range acceleration of decelerator	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
Z		Vertical inertial axis or displacement of forebody	(m)	ft
	$Z_b$	Vertical body axis or displacement of forebody	(m)	ft

<u>FORTRAN</u>	<u>STANDARD</u>	<u>DESCRIPTION</u>	<u>METRIC UNITS</u>	<u>ENGLISH UNITS</u>
ZBAR	$\bar{Z}$	c.g. offset along $Z_b$ axis	(m)	ft
ZBD	$\dot{Z}_b$	$Z_b$ body axis velocity	(m/sec)	ft/sec
ZD	$\dot{Z}$	Vertical velocity of forebody	(m/sec)	ft/sec
ZDD	$\ddot{Z}$	Vertical acceleration of forebody	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>
ZP	$Z_p$	Vertical inertial displacement of decelerator	(m)	ft
ZPBD	$\dot{Z}_{pb}$	$Z_{pb}$ body axis velocity of decelerator	(m/sec)	ft/sec
ZPD	$\dot{Z}_p$	Vertical velocity of decelerator	(m/sec)	ft/sec
ZPDD	$\ddot{Z}_p$	Vertical acceleration of decelerator	(m/sec <sup>2</sup> )	ft/sec <sup>2</sup>

CHAPTER I - INTRODUCTION

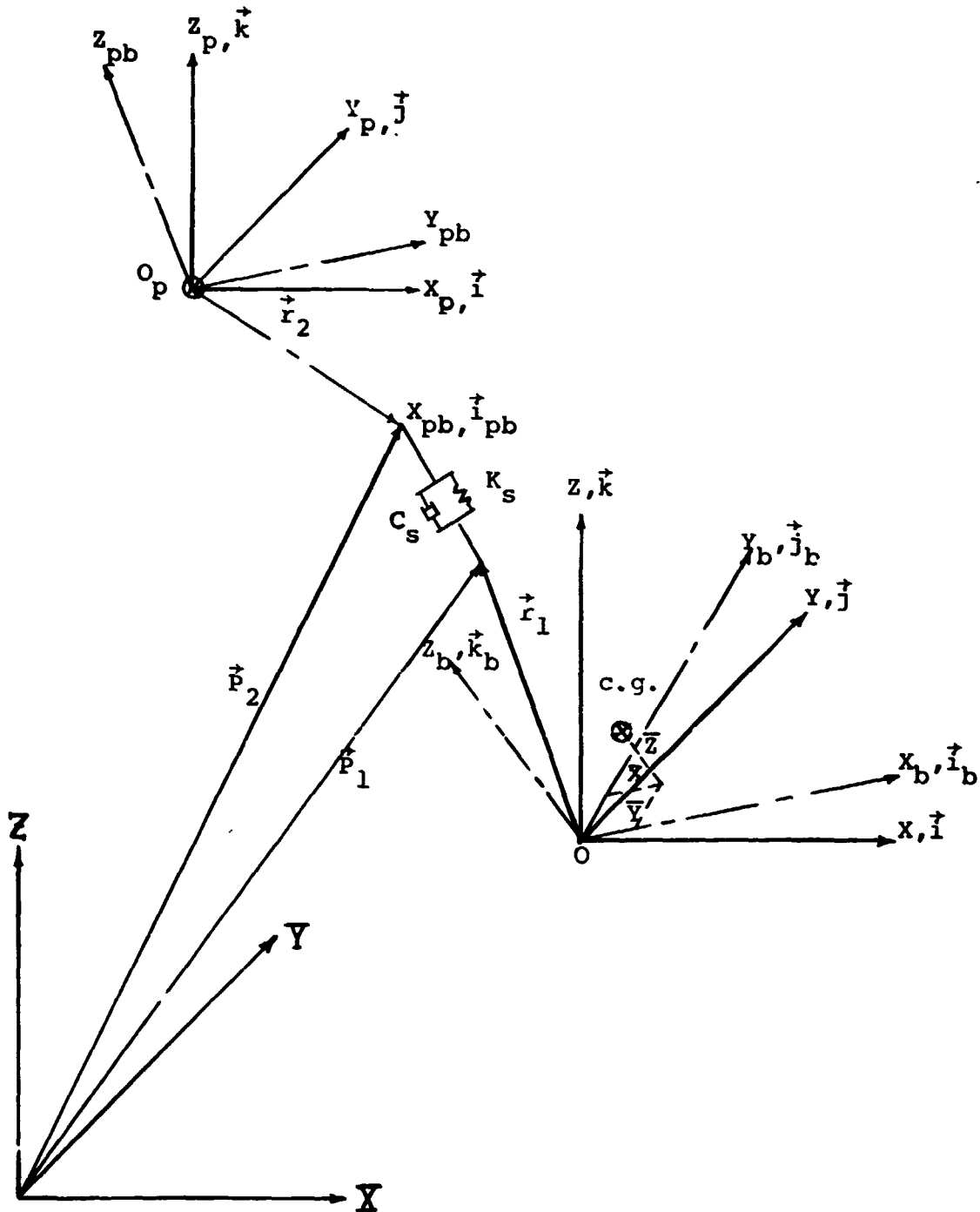
The system to be simulated is two rigid bodies joined by an elastic tether. The forebody may have a completely general shape and mass characteristics, and will be free to move with six degrees of freedom (three translational, three rotational). The decelerator is assumed to be symmetric in shape and mass characteristics about its longitudinal (roll) axis, and will be free to move with five degrees of freedom (three translational, two rotational). A frictionless swivel is assumed at the decelerator-tether confluence point. Thus the roll motions of the forebody will not couple with the decelerator. The tether is simulated by a spring and dashpot in parallel. Damping coefficients for tether lines are difficult to obtain; but spring constants for a tether can be found from experimental stress strain curves. Consequently; the damping coefficient is assumed constant, while the spring constant is assumed to be a function of elongation in the computer program, thereby introducing a quasilinear spring.

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REF: EOI 380

CHAPTER II DERIVATION OF EQUATIONS OF MOTION

SECTION 1 - COORDINATE SYSTEM

Figure 1 shows the different coordinate systems used to derive the equations of motion.  $\bar{X}\bar{Y}\bar{Z}$  is an inertial orthogonal coordinate system attached to a flat non-rotating earth.  $XYZ$  and  $X_p Y_p Z_p$  are orthogonal axes fixed to the forebody and decelerator at "O" and "O<sub>p</sub>" respectively. Coordinate systems  $XYZ$  and  $X_p Y_p Z_p$  translate with the bodies but do not rotate, always remaining parallel to corresponding inertial axes. The displacements  $X, Y, Z, X_p, Y_p,$  and  $Z_p$ , as measured from the origin of  $\bar{X}\bar{Y}\bar{Z}$ , are the six translational degrees of freedom of the two bodies. The reference forebody body axes, longitudinal ( $X_b$ ), lateral ( $Y_b$ ), and vertical ( $Z_b$ ), intersect at "O", the origin of the aerodynamics load system of the forebody. The reference decelerator body axes, longitudinal ( $X_{pb}$ ), lateral ( $Y_{pb}$ ), and vertical ( $Z_{pb}$ ) intersect at "O<sub>p</sub>", the c.g. of the decelerator. The variables  $\bar{X}, \bar{Y}, \bar{Z}$  are the distances from "O" to the c.g. of the forebody measured positively in the direction of the positive body axes  $X_b, Y_b, Z_b$  respectively. For orientation purposes, the reader should position himself as a pilot in an airplane. In this position,  $X_b$  is positive toward the nose,  $Y_b$  is positive toward the left wing and  $Z_b$  is positive up.  $\vec{r}_1$  is the vector distance from the intersection of the longitudinal, lateral, and vertical axes of the forebody ("O") to the tether confluence point of the forebody.  $\vec{r}_2$  is the vector distance from the c.g. of the decelerator ("O<sub>p</sub>") to the tether confluence point of the decelerator;  $\vec{r}_2$  lies along  $X_{pb}$ .



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FIGURE 1 - COORDINATE SYSTEMS

**SECTION 2 - EULER ANGLE TRANSFORMATION**

In order to specify the angular orientation of a body with reference to a non-rotating coordinate system (X, Y, Z), three successive rotations are made as shown in Figure 2. The first rotation is in the direction, -OZ, such that OX and OY are rotated through an angle  $\psi$  into Oa and ON respectively. The second rotation is in the direction, -ON, such that Oa and OZ are rotated through an angle  $\theta$  into  $OX_b$  and Ob respectively. The final rotation is about  $OX_b$  such that ON and Ob are rotated through an angle  $\phi$  into  $OY_b$  and  $OZ_b$  respectively. The three angular rotations ( $\psi, \theta, \phi$ ) specify the orientation of the body axes ( $X_b, Y_b, Z_b$ ) with respect to the inertial axes ( $X, Y, Z$ ). Again, from a pilots viewpoint, a positive  $\psi$  is a nose to the right yaw; a positive  $\theta$  is a nose up pitch; and a positive  $\phi$  is a right wing down roll.

The transformation matrix between the body axes and inertial axes is now found by considering one rotation at a time and then combining. The first rotation is given by:

$$\begin{Bmatrix} Oa \\ ON \\ OZ \end{Bmatrix} = \begin{bmatrix} C\psi & -S\psi & 0 \\ S\psi & C\psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{Bmatrix} OX \\ OY \\ OZ \end{Bmatrix} \quad (1)$$

where  $S\psi = \sin\psi$  and  $C\psi = \cos\psi$ .

The second rotation is:

$$\begin{Bmatrix} OX_b \\ ON \\ Ob \end{Bmatrix} = \begin{bmatrix} C\theta & 0 & S\theta \\ 0 & 1 & 0 \\ -S\theta & 0 & C\theta \end{bmatrix} \begin{Bmatrix} Oa \\ ON \\ OZ \end{Bmatrix} \quad (2)$$



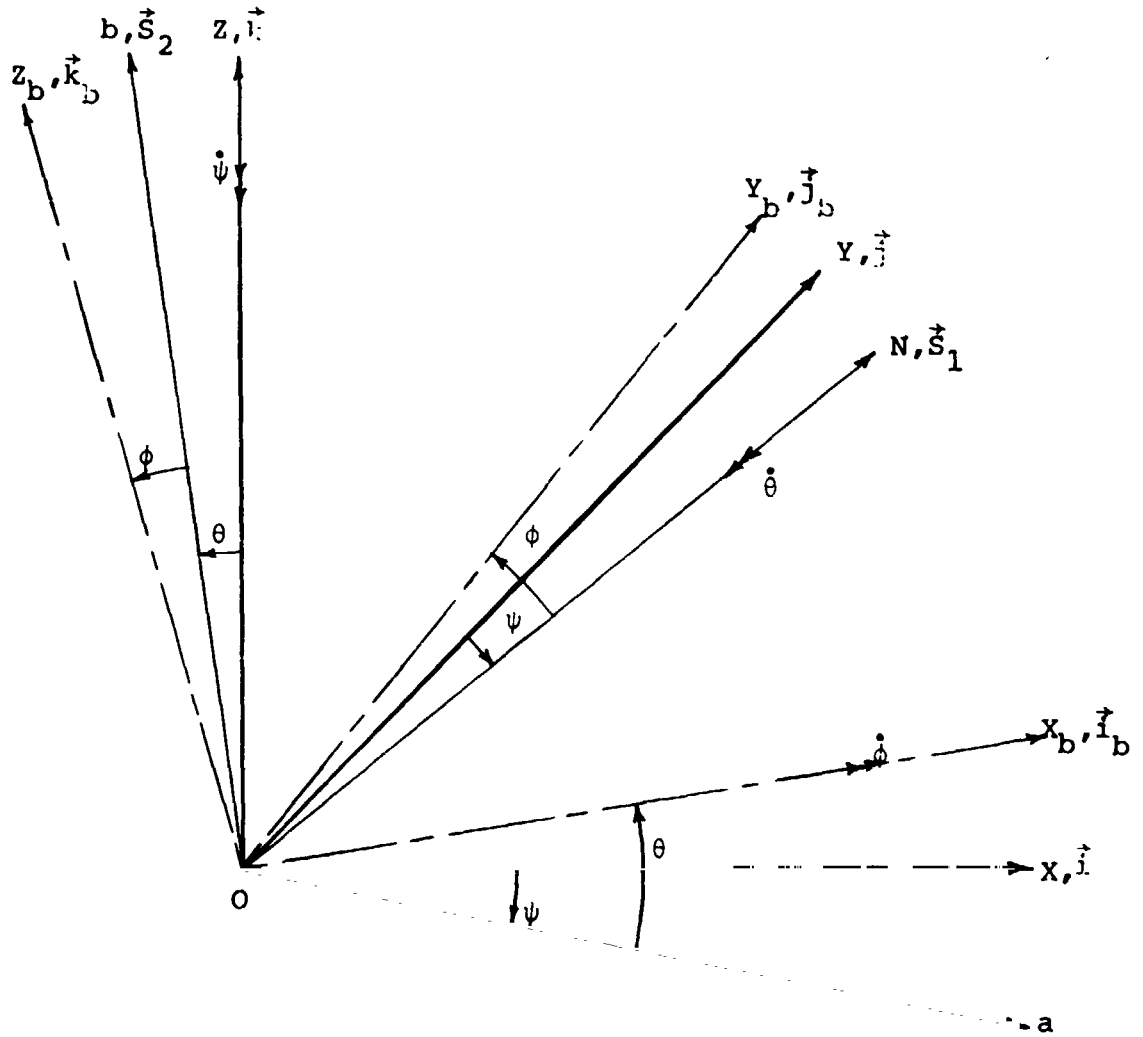


FIGURE 2 - EULER ANGLE ROTATIONS

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The final rotation is:

$$\begin{Bmatrix} OX_b \\ OY_b \\ OZ_b \end{Bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\phi & S\phi \\ 0 & -S\phi & C\phi \end{bmatrix} \begin{Bmatrix} OX_b \\ ON \\ Ob \end{Bmatrix} \quad (3)$$

By substituting Equation (1) into (2) and (2) into (3), the transformation matrix [C] is formed

$$\begin{Bmatrix} OX_b \\ OY_b \\ OZ_b \end{Bmatrix} = \begin{bmatrix} C\psi C\theta & -S\psi C\theta & S\theta \\ -C\psi S\theta S\phi + S\psi C\phi & S\psi S\theta S\phi + C\psi C\phi & C\theta S\phi \\ -C\psi S\theta C\phi - S\psi S\phi & S\psi S\theta C\phi - C\psi S\phi & C\theta C\phi \end{bmatrix} \begin{Bmatrix} OX \\ OY \\ OZ \end{Bmatrix} \quad (4)$$

Since [C] is a linear orthogonal ( $\sum_{i=1}^3 C_{ij} C_{ik} = \delta_{jk}$ ;  $j, k = 1, 2, 3$ ) transformation, its inverse is equal to its transpose. (1). Therefore,

$$\begin{Bmatrix} OX \\ OY \\ OZ \end{Bmatrix} = \begin{bmatrix} C\psi C\theta & -C\psi S\theta S\phi + S\psi C\phi & -C\psi S\theta C\phi - S\psi S\phi \\ -S\psi C\theta & S\psi S\theta S\phi + C\psi C\phi & S\psi S\theta C\phi - C\psi S\phi \\ S\theta & C\theta S\phi & C\theta C\phi \end{bmatrix} \begin{Bmatrix} OX_b \\ OY_b \\ OZ_b \end{Bmatrix} \quad (5)$$

For the decelerator, there is no rotation about the longitudinal axis. Consequently, the transformation matrix in (4) is simplified by letting  $\phi = 0$ . The result is  $[C_p]$ .

$$\begin{Bmatrix} OX_{pb} \\ OY_{pb} \\ OZ_{pb} \end{Bmatrix} = \begin{bmatrix} C\psi_p C\theta_p & -S\psi_p C\theta_p & S\theta_p \\ S\psi_p & C\psi_p & 0 \\ -C\psi_p S\theta_p & S\psi_p S\theta_p & C\theta_p \end{bmatrix} \begin{Bmatrix} OX_p \\ OY_p \\ OZ_p \end{Bmatrix} \quad (6)$$

The total angular velocity of the forebody is given by:

$$\vec{\omega} = \dot{\psi} \vec{k} - \dot{\theta} \vec{s}_1 + \dot{\phi} \vec{i}_b \quad (7)$$

From the inverse of (3):

$$\vec{s}_1 = c\phi \vec{j}_b - s\phi \vec{k}_b \quad (8)$$

$$\vec{s}_2 = s\phi \vec{j}_b + c\phi \vec{k}_b \quad (9)$$

From the inverse of (2)

$$\vec{k} = s\theta \vec{i}_b + c\theta \vec{s}_2 \quad (10)$$

Substituting (8), (9), and (10) into (7):

$$\vec{\omega} = [-\dot{\psi}(s\theta) + \dot{\phi}] \vec{i}_b + [-\dot{\psi}(c\theta s\phi) - \dot{\theta}(c\phi)] \vec{j}_b + [-\dot{\psi}(c\theta c\phi) + \dot{\theta}(s\phi)] \vec{k}_b \quad (11)$$

The components of angular velocity for the forebody are:

$$\omega_{xb} = -\dot{\psi}(s\theta) + \dot{\phi} \quad (12)$$

$$\omega_{yb} = -\dot{\psi}(c\theta s\phi) - \dot{\theta}(c\phi) \quad (13)$$

$$\omega_{zb} = -\dot{\psi}(c\theta c\phi) + \dot{\theta}(s\phi) \quad (14)$$

Likewise, for the decelerator, the angular velocities are:

$$\omega_{xpb} = -\dot{\psi}_p (s\theta_p) \quad (15)$$

$$\omega_{ypb} = -\dot{\theta}_p \quad (16)$$

$$\omega_{zpb} = -\dot{\psi}_p (c\theta_p) \quad (17)$$

SECTION 3 - KINETIC ENERGY

The kinetic energy of the system is due to the translational and rotational velocities of the forebody and the decelerator. The forebody is completely general in shape, and products of inertia and c.g. offsets will effect the kinetic energy. On the other hand, the decelerator is assumed to be symmetric about the longitudinal axis and the aerodynamic loads are referenced to the c.g. Therefore, all products of inertia and c.g. offsets are zero. The expression for kinetic energy is: (2)

$$\begin{aligned}
 T = & \frac{1}{2} m [\dot{X}^2 + \dot{Y}^2 + \dot{Z}^2] + \frac{1}{2} [I_{xb} \omega_{xb}^2 + I_{yb} \omega_{yb}^2 + I_{zb} \omega_{zb}^2] \\
 & - [I_{yzb} \omega_{yb} \omega_{zb} + I_{xzb} \omega_{xb} \omega_{zb} + I_{xyb} \omega_{xb} \omega_{yb}] \\
 & + m [\dot{X}_b (\omega_{yb} \bar{Z} - \omega_{zb} \bar{Y}) + \dot{Y}_b (\omega_{zb} \bar{X} - \omega_{xb} \bar{Z}) + \dot{Z}_b (\omega_{xb} \bar{Y} - \omega_{yb} \bar{X})] \\
 & + \frac{1}{2} m_{pl} [\dot{X}_{pb}^2] + \frac{1}{2} m_{ps} [\dot{Y}_{pb}^2 + \dot{Z}_{pb}^2] \\
 & + \frac{1}{2} [I_{xpb} \omega_{xpb}^2 + I_{ypb} \omega_{ypb}^2 + I_{zpb} \omega_{zpb}^2] \tag{18}
 \end{aligned}$$

In Equation (18),  $m_{pl}$  and  $m_{ps}$  include directional mass terms due to the air enclosed in the canopy,  $I_{xpb}$ ,  $I_{ypb}$ , and  $I_{zpb}$  are apparent mass moments of inertia.

SECTION 4 - POTENTIAL ENERGY

The potential energy of the system is due to the gravitational potential of both bodies and the elastic potential of the tether.

$$V = mg[Z + \bar{X}(S\theta) + \bar{Y}(C\theta S\phi) + \bar{Z}(C\theta C\phi)] + m_p g Z_p + \frac{1}{2} K_s [L_T - L_{T_0}]^2 \quad (19)$$

$L_{T_0}$  is the unstretched length of the tether; and  $L_T$  is the stretched length of the tether as given by the geometry of the system. Referring to Figure 1:

$$L_T = |\vec{P}_2 - \vec{P}_1| \quad (20)$$

$\vec{P}_1$  and  $\vec{P}_2$  are the vectors from the inertial coordinate system ( $\bar{X} \bar{Y} \bar{Z}$ ) to the confluence points of the forebody and decelerator respectively. For the forebody,

$$\vec{P}_1 = x\vec{i} + y\vec{j} + z\vec{k} + \vec{r}_1 \quad (21)$$

$$\vec{r}_1 = a\vec{i}_b + b\vec{j}_b + c\vec{k}_b \quad (22)$$

a, b, and c are measured along positive body axes  $X_b$ ,  $Y_b$ , and  $Z_b$  respectively. Using the coordinate transformation matrix (4):

$$\begin{aligned} \vec{P}_1 = & [X+a(C\psi C\theta)+b(-C\psi S\theta S\phi+S\psi C\phi) + c(-C\psi S\theta C\phi-S\psi S\phi)] \vec{i} \\ & + [Y+a(-S\psi C\theta)+b(S\psi S\theta S\phi+C\psi C\phi)+ c(S\psi S\theta C\phi-C\psi S\phi)] \vec{j} \\ & + [Z+a(S\theta)+ b(C\theta S\phi)+ c(C\theta C\phi)] \vec{k} \end{aligned} \quad (23)$$

Similarly for the decelerator:

$$\vec{p}_2 = x_p \vec{i} + y_p \vec{j} + z_p \vec{k} + \vec{r}_2 \quad (24)$$

$$\vec{r}_2 = a_p \vec{i}_{pb} \quad (25)$$

Substituting (25) into (24) and using matrix Equation (6),

$$\vec{p}_2 = [x_p + a_p (C\psi_p C\theta_p)] \vec{i} + [y_p + a_p (-S\psi_p C\theta_p)] \vec{j} + [z_p + a_p (S\theta_p)] \vec{k} \quad (26)$$

$$L_T = [L_T \cdot L_T]^{1/2} \quad (27)$$

$$L_T = \{ [x_p + a_p (C\psi_p C\theta_p) - X - a (C\psi C\theta) - b (-C\psi S\theta S\phi + S\psi C\phi) - c (-C\psi S\theta C\phi - S\psi S\phi)]^2 \\ + [y_p + a_p (-S\psi_p C\theta_p) - Y - a (-S\psi C\theta) - b (S\psi S\theta S\phi + C\psi C\phi) - c (S\psi S\theta C\phi - C\psi S\phi)]^2 \\ + [z_p + a_p (S\theta_p) - Z - a (S\theta) - b (C\theta S\phi) - c (C\theta C\phi)]^2 \}^{1/2} \quad (28)$$

Define the variables  $\bar{A}$ ,  $\bar{B}$ , and  $\bar{C}$  such that:

$$L_T = \{ [\bar{A}]^2 + [\bar{B}]^2 + [\bar{C}]^2 \}^{1/2} \quad (29)$$

Further on in the derivation it will be necessary to know the total time derivative of  $L_T$  and the partial derivatives of  $\bar{A}$ ,  $\bar{B}$ , and  $\bar{C}$  with respect to the generalized coordinates.

$$\dot{L}_T = [\bar{A} \dot{\bar{A}} + \bar{B} \dot{\bar{B}} + \bar{C} \dot{\bar{C}}] / L_T \quad (30)$$

$$\begin{aligned} \dot{\bar{A}} &= \dot{x}_p + a_p [\dot{\psi}_p (-S\psi_p C\theta_p) + \dot{\theta}_p (-C\psi_p S\theta_p)] - \dot{x} - a [\dot{\psi} (-S\psi C\theta) + \dot{\theta} (-C\psi S\theta)] \\ &\quad - b [\dot{\psi} (S\psi S\theta S\phi + C\psi C\phi) + \dot{\theta} (-C\psi C\theta S\phi) + \dot{\phi} (-C\psi S\theta C\phi - S\psi S\phi)] \\ &\quad - c [\dot{\psi} (S\psi S\theta C\phi - C\psi S\phi) + \dot{\theta} (-C\psi C\theta C\phi) + \dot{\phi} (C\psi S\theta S\phi - S\psi C\phi)] \end{aligned} \quad (31)$$

$$\begin{aligned} \dot{\bar{B}} &= \dot{y}_p + a_p [\dot{\psi}_p (-C\psi_p C\theta_p) + \dot{\theta}_p (S\psi_p S\theta_p)] - \dot{y} - a [\dot{\psi} (-C\psi C\theta) + \dot{\theta} (S\psi S\theta)] \\ &\quad - b [\dot{\psi} (C\psi S\theta S\phi - S\psi C\phi) + \dot{\theta} (S\psi C\theta S\phi) + \dot{\phi} (S\psi S\theta C\phi - C\psi S\phi)] \\ &\quad - c [\dot{\psi} (C\psi S\theta C\phi + S\psi S\phi) + \dot{\theta} (S\psi C\theta C\phi) + \dot{\phi} (-S\psi S\theta S\phi - C\psi C\phi)] \end{aligned} \quad (32)$$

$$\begin{aligned} \dot{\bar{C}} &= \dot{z}_p + a_p [\dot{\theta}_p (C\theta_p)] - \dot{z} - a [\dot{\theta} (C\theta)] - b [\dot{\theta} (-S\theta S\phi) + \dot{\phi} (C\theta C\phi)] \\ &\quad - c [\dot{\theta} (-S\theta C\phi) + \dot{\phi} (-C\theta S\phi)] \end{aligned} \quad (33)$$

$$\frac{\partial \bar{A}}{\partial X} = \frac{\partial \bar{B}}{\partial Y} = \frac{\partial \bar{C}}{\partial Z} = -1 \quad (34)$$

$$\frac{\partial \bar{A}}{\partial X_p} = \frac{\partial \bar{B}}{\partial Y_p} = \frac{\partial \bar{C}}{\partial Z_p} = 1 \quad (35)$$

$$\begin{aligned} \frac{\partial \bar{A}}{\partial Y} &= \frac{\partial \bar{A}}{\partial Z} = \frac{\partial \bar{A}}{\partial Y_p} = \frac{\partial \bar{A}}{\partial Z_p} = 0 \\ \frac{\partial \bar{B}}{\partial X} &= \frac{\partial \bar{B}}{\partial Z} = \frac{\partial \bar{B}}{\partial X_p} = \frac{\partial \bar{B}}{\partial Z_p} = 0 \end{aligned} \quad (36)$$

$$\frac{\partial \bar{C}}{\partial X} = \frac{\partial \bar{C}}{\partial Y} = \frac{\partial \bar{C}}{\partial X_p} = \frac{\partial \bar{C}}{\partial Y_p} = 0$$

$$\frac{\partial \bar{A}}{\partial \psi} = a (S\psi C\theta) - b (S\psi S\theta S\phi + C\psi C\phi) - c (S\psi S\theta C\phi - C\psi S\phi) \quad (37)$$

$$\frac{\partial \bar{A}}{\partial \theta} = a (C\psi S\theta) + b (C\psi C\theta S\phi) + c (C\psi C\theta C\phi) \quad (38)$$

$$\frac{\partial \bar{A}}{\partial \phi} = b (C\psi S\theta C\phi + S\psi S\phi) - c (C\psi S\theta S\phi - S\psi C\phi) \quad (39)$$

$$\frac{\partial \bar{A}}{\partial \psi_p} = a_p (-S\psi_p C\theta_p) \quad (40)$$

$$\frac{\partial \bar{A}}{\partial \theta_p} = a_p (-C\psi_p S\theta_p) \quad (41)$$

$$\frac{\partial \bar{B}}{\partial \psi} = a (C\psi C\theta) - b (C\psi S\theta S\phi - S\psi C\phi) - c (C\psi S\theta C\phi + S\psi S\phi) \quad (42)$$

$$\frac{\partial \bar{B}}{\partial \theta} = a (-S\psi S\theta) - b (S\psi C\theta S\phi) - c (S\psi C\theta C\phi) \quad (43)$$

$$\frac{\partial \bar{B}}{\partial \phi} = -b (S\psi S\theta C\phi - C\psi S\phi) + c (S\psi S\theta S\phi + C\psi C\phi) \quad (44)$$

$$\frac{\partial \bar{B}}{\partial \psi_p} = a_p (-C\psi_p C\theta_p) \quad (45)$$

$$\frac{\partial \bar{B}}{\partial \theta_p} = a_p (S\psi_p S\theta_p) \quad (46)$$

$$\frac{\partial \bar{C}}{\partial \psi} = 0 \quad (47)$$

$$\frac{\partial \bar{C}}{\partial \theta} = a (-C\theta) + b (S\theta S\phi) + c (S\theta C\phi) \quad (48)$$



$$\frac{\partial \bar{C}}{\partial \phi} = b(-C\theta C\phi) + c(C\theta S\phi) \quad (49)$$

$$\frac{\partial \bar{C}}{\partial \psi_p} = 0 \quad (50)$$

$$\frac{\partial \bar{C}}{\partial \theta_p} = a_p(C\theta_p) \quad (51)$$

#### SECTION 5 - RALEIGH'S DISSIPATION FUNCTION

If the viscous damping force is proportional to the velocity of the particle at which the force acts, an expression analogous to the potential energy of a spring may be used. This function,  $F$ , is known as Rayleigh's dissipation function, and is defined as <sup>(1)</sup>

$$F = \frac{1}{2} \sum_{i=1}^n C_i \dot{q}_i^2 \quad (52)$$

For this problem, Rayleigh's damping is considered only in the tether.

$$F = \frac{1}{2} C_s \dot{L}_T^2$$

#### SECTION 6 - LAGRANGE'S EQUATION

The Lagrange equation for a non-conservative (aerodynamic forces) system with a holonomic (can be expressed as an algebraic expression), scleronomous (independent of time) constraint and Rayleigh's dissipation function (damping in the elastic tether) can be written as: <sup>(1)</sup>

$$\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} - \lambda \frac{\partial \bar{q}}{\partial q_i} + \frac{\partial F}{\partial \dot{q}_i} = Q_i \quad (54)$$

In Equation (54), the term  $\lambda \frac{\partial \bar{q}}{\partial q_i}$  expresses the generalized force exerted by the tether on the  $i^{\text{th}}$  degree of freedom. The constraint equation is:

$$\bar{q} = \{ [\bar{A}]^2 + [\bar{B}]^2 + [\bar{C}]^2 \}^{1/2} - L_T = 0 \quad (55)$$

$Q_i$  is the generalized force due to the aerodynamics.

$\frac{\partial F}{\partial \dot{q}_i}$  is the force due to damping in the tether.

The Lagrangian is equal to the total kinetic energy of the system (Equation (18)) minus the total potential energy of the system (Equation (19)). With substitutions from Equations (4), (6) and (12) to (17), the Lagrangian is:

$$\begin{aligned} L = & \frac{1}{2} m [\dot{X}^2 + \dot{Y}^2 + \dot{Z}^2] + \frac{1}{2} m_{pl} [\dot{X}_p (C\psi_p C\theta_p) + \dot{Y}_p (-S\psi_p C\theta_p) + \dot{Z}_p (S\theta_p)]^2 \\ & + \frac{1}{2} m_{ps} \{ [\dot{X}_p (S\psi_p) + \dot{Y}_p (C\psi_p)]^2 + [\dot{X}_p (-C\psi_p S\theta_p) + \dot{Y}_p (S\psi_p S\theta_p) + \dot{Z}_p (C\theta_p)]^2 \} \\ & + \frac{1}{2} I_{xb} [-\dot{\psi}(S\theta) + \dot{\phi}]^2 + \frac{1}{2} I_{yb} [-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)]^2 + \frac{1}{2} I_{zb} [-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)]^2 \\ & - \{ I_{yzb} [-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)] [-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)] + I_{xzb} [-\dot{\psi}(S\theta) + \dot{\phi}] [-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)] \} \\ & + I_{xyb} [-\dot{\psi}(S\theta) + \dot{\phi}] [-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)] \} \end{aligned}$$

$$\begin{aligned}
 & + \frac{1}{2} I_{xpb} [-\dot{\psi}_p^2 (S^2 \theta_p) + \frac{1}{2} I_{ypb} [\dot{\theta}_p^2 + \dot{\psi}_p^2 (C^2 \theta_p)]] \\
 & + m \{ [\dot{X}(C\psi C\theta) + \dot{Y}(-S\psi C\theta) + \dot{Z}(S\theta)] [\bar{Z}(-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi)) - \bar{Y}(-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi))] \\
 & + [\dot{X}(-C\psi S\theta S\phi + S\psi C\phi) + \dot{Y}(S\psi S\theta S\phi + C\psi C\phi) + \dot{Z}(C\theta S\phi)] [\bar{X}(-\dot{\psi}(C\theta C\phi) + \dot{\theta}(S\phi)) - \bar{Z}(-\dot{\psi}(S\theta) + \dot{\phi})] \\
 & + [\dot{X}(-C\psi S\theta C\phi - S\psi S\phi) + \dot{Y}(S\psi S\theta C\phi - C\psi S\phi) + \dot{Z}(C\theta C\phi)] [\bar{Y}(-\dot{\psi}(S\theta) + \dot{\phi}) - \bar{X}(-\dot{\psi}(C\theta S\phi) - \dot{\theta}(C\phi))] \} \\
 & - mg [Z + \bar{X}(S\theta) + \bar{Y}(C\theta S\phi) + \bar{Z}(C\theta C\phi)] - m_p g z_p - \frac{1}{2} K_s [L_T - L_{T0}]^2 \tag{56}
 \end{aligned}$$

Note:  $I_{ypb} = I_{zpb}$  due to decelerator symmetry.

#### SECTION 7 - GENERAL EQUATIONS OF MOTION

Equation (56) displays all of the generalized coordinates explicitly except those appearing in  $L_T$ . The terms to be substituted into Equation (54) are now developed.

#### X Equation

$$\begin{aligned}
 \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{X}} \right) & = \ddot{X}\{m\} + \ddot{\psi}\{m[\bar{X}(-S\psi C\theta) + \bar{Y}(S\psi S\theta S\phi + C\psi C\phi) + \bar{Z}(S\psi S\theta C\phi - C\psi S\phi)]\} \\
 & + \ddot{\theta}\{m[\bar{X}(-C\psi S\theta) + \bar{Y}(-C\psi C\theta S\phi) + \bar{Z}(-C\psi C\theta C\phi)]\} \\
 & + \ddot{\phi}\{m[\bar{Y}(-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z}(C\psi S\theta S\phi - S\psi S\phi)]\} \\
 & + \dot{\psi}\dot{\theta}\{m[\bar{X}(2S\psi S\theta) + \bar{Y}(2S\psi C\theta S\phi) + \bar{Z}(2S\psi C\theta C\phi)]\}
 \end{aligned}$$

$$\begin{aligned}
 & +\ddot{\psi}\dot{\phi}\{m[\bar{Y}(2S\psi S\theta C\phi-2C\psi S\phi)+\bar{Z}(-2S\psi S\theta S\phi-2C\psi C\phi)]\} \\
 & +\dot{\theta}\dot{\phi}\{m[\bar{Y}(-2C\psi C\theta C\phi)+\bar{Z}(2C\psi C\theta S\phi)]\} \\
 & +\dot{\psi}^2\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\} \\
 & +\dot{\theta}^2\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi)+\bar{Z}(C\psi S\theta C\phi)]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\}
 \end{aligned} \tag{57}$$

$$\frac{\partial L}{\partial X} = 0 \tag{58}$$

$$\frac{\partial \bar{g}}{\partial X} = \frac{-\bar{A}}{L_T} \tag{59}$$

$$\frac{\partial F}{\partial X} = 0 \tag{60}$$

Y Equation

$$\begin{aligned}
 \frac{d}{dt}\left(\frac{\partial L}{\partial \dot{Y}}\right) & = \ddot{Y}\{m\} + \ddot{\psi}\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\} \\
 & + \ddot{\theta}\{m[\bar{X}(S\psi S\theta)+\bar{Y}(S\psi C\theta S\phi)+\bar{Z}(S\psi C\theta C\phi)]\} \\
 & + \ddot{\phi}\{m[\bar{Y}(S\psi S\theta C\phi-C\psi S\phi)+\bar{Z}(-S\psi S\theta S\phi-C\psi C\phi)]\} \\
 & + \dot{\psi}\dot{\theta}\{m[\bar{X}(2C\psi S\theta)+\bar{Y}(2C\psi C\theta S\phi)+\bar{Z}(2C\psi C\theta C\phi)]\}
 \end{aligned}$$

$$\begin{aligned}
 & +\ddot{\psi}\phi\{m[\bar{Y}(2C\psi S\theta C\phi+2S\psi S\phi)+\bar{Z}(-2C\psi S\theta S\phi+2S\psi C\phi)]\} \\
 & +\ddot{\theta}\phi\{m[\bar{Y}(2S\psi C\theta C\phi)+\bar{Z}(-2S\psi C\theta S\phi)]\} \\
 & +\dot{\psi}^2\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\} \\
 & +\dot{\theta}^2\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi)+\bar{Z}(-S\psi S\theta C\phi)]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\}
 \end{aligned} \tag{61}$$

$$\frac{\partial L}{\partial \dot{Y}} = 0 \tag{62}$$

$$\frac{\partial \bar{q}}{\partial \dot{Y}} = -\frac{\bar{B}}{L_T} \tag{63}$$

$$\frac{\partial F}{\partial \dot{Y}} = 0 \tag{64}$$

Z Equation

$$\begin{aligned}
 \frac{d}{dt}\left(\frac{\partial L}{\partial \dot{Z}}\right) & = \ddot{Z}\{m\}+\ddot{\theta}\{m[\bar{X}(C\theta)+\bar{Y}(-S\theta S\phi)+\bar{Z}(-S\theta C\phi)]\} \\
 & +\ddot{\phi}\{m[\bar{Y}(C\theta C\phi)+\bar{Z}(-C\theta S\phi)]\} \\
 & +\dot{\theta}\dot{\phi}\{m[\bar{Y}(-2S\theta C\phi)+\bar{Z}(S\theta S\phi)]\} \\
 & +\dot{\theta}^2\{m[\bar{X}(-S\theta)+\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\}
 \end{aligned} \tag{65}$$

$$\frac{\partial L}{\partial Z} = -mg \quad (66)$$

$$\frac{\partial \bar{q}}{\partial Z} = -\frac{C}{L_T} \quad (67)$$

$$\frac{\partial F}{\partial \dot{Z}} = 0 \quad (68)$$

X<sub>p</sub> Equation

$$\begin{aligned} \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{X}_p} \right) &= \dot{X}_p \{ m_{pl} [C^2 \psi_p C^2 \theta_p] + m_{ps} [S^2 \psi_p + C^2 \psi_p S^2 \theta_p] \} \\ &+ \ddot{Y}_p \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S 2 \psi_p C^2 \theta_p] \} \\ &+ \ddot{Z}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} C \psi_p S 2 \theta_p] \} \\ &+ \dot{X}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] [-S 2 \psi_p C^2 \theta_p] \} \\ &+ \dot{X}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [-C^2 \psi_p S 2 \theta_p] \} \\ &+ \dot{Y}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] [-C 2 \psi_p C^2 \theta_p] \} \\ &+ \dot{Y}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} S 2 \psi_p S 2 \theta_p] \} \\ &+ \dot{Z}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S \psi_p S 2 \theta_p] \} \\ &+ \dot{Z}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [C \psi_p C 2 \theta_p] \} \end{aligned} \quad (69)$$

$$\frac{\partial L}{\partial \dot{X}_p} = 0 \quad (70)$$

$$\frac{\partial \bar{q}}{\partial \dot{X}_p} = \frac{\bar{A}}{L_T} \quad (71)$$

$$\frac{\partial F}{\partial \dot{X}_p} = 0 \quad (72)$$

Y<sub>p</sub> Equation

$$\begin{aligned} \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{Y}_p} \right) &= \ddot{X}_p \{ [m_{p\ell} - m_{ps}] [-\frac{1}{2} S 2\psi_p C^2\theta_p] \} \\ &+ \ddot{Y}_p \{ m_{p\ell} [S^2\psi_p C^2\theta_p] + m_{ps} [C^2\psi_p + S^2\psi_p S^2\theta_p] \} \\ &+ \ddot{Z}_p \{ m_{p\ell} - m_{ps} \} [-\frac{1}{2} S\psi_p S 2\theta_p] \} \\ &+ \dot{X}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] [-C 2\psi_p C^2\theta_p] \} \\ &+ \dot{X}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [\frac{1}{2} S 2\psi_p S 2\theta_p] \} \\ &+ \dot{Y}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] [S 2\psi_p C^2\theta_p] \} \\ &+ \dot{Y}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [-S^2\psi_p S 2\theta_p] \} \\ &+ \dot{Z}_p \dot{\psi}_p \{ [m_{p\ell} - m_{ps}] [-\frac{1}{2} C\psi_p S 2\theta_p] \} \\ &+ \dot{Z}_p \dot{\theta}_p \{ [m_{p\ell} - m_{ps}] [-S\psi_p C 2\theta_p] \} \end{aligned} \quad (73)$$

$$\frac{\partial L}{\partial \dot{Y}_p} = 0 \quad (74)$$

$$\frac{\partial \bar{q}}{\partial \dot{Y}_p} = \frac{\bar{B}}{L_T} \quad (75)$$

$$\frac{\partial F}{\partial \dot{Y}_p} = 0 \quad (76)$$

Z<sub>p</sub> Equation

$$\begin{aligned} \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{z}_p} \right) = & \ddot{X}_p \{ [m_{pl} - m_{ps}] \left[ \frac{1}{2} C\psi_p S2\theta_p \right] \} \\ & + \ddot{Y}_p \{ [m_{pl} - m_{ps}] \left[ -\frac{1}{2} S\psi_p S2\theta_p \right] \} \\ & + \ddot{z}_p \{ m_{pl} [S^2\theta_p] + m_{ps} [C^2\theta_p] \} \\ & + \dot{X}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] \left[ -\frac{1}{2} S\psi_p S2\theta_p \right] \} \\ & + \dot{X}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [C\psi_p C2\theta_p] \} \\ & + \dot{Y}_p \dot{\psi}_p \{ [m_{pl} - m_{ps}] \left[ -\frac{1}{2} C\psi_p S2\theta_p \right] \} \\ & + \dot{Y}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [-S\psi_p C2\theta_p] \} \\ & + \dot{z}_p \dot{\theta}_p \{ [m_{pl} - m_{ps}] [S2\theta_p] \} \end{aligned} \quad (77)$$



$$\frac{\partial L}{\partial \dot{z}_p} = -m_p g \quad (78)$$

$$\frac{\partial \bar{q}}{\partial \dot{z}_p} = \frac{\bar{C}}{L_T} \quad (79)$$

$$\frac{\partial F}{\partial \dot{z}_p} = 0 \quad (80)$$

$\psi$  Equation

$$\begin{aligned} \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{\psi}} \right) = & \ddot{\psi} \{ I_{x_b} (S^2 \theta) + [I_{y_b} (S^2 \phi) + I_{z_b} (C^2 \phi)] (C^2 \theta) + I_{y_z b} (-C^2 \theta S 2 \phi) \\ & + [I_{x_z b} (C \phi) + I_{x_y b} (S \phi)] (-S 2 \theta) \} \\ & + \ddot{\theta} \{ [(I_{y_b} - I_{z_b}) \left( \frac{1}{2} S 2 \phi \right) - I_{y_z b} (C 2 \phi)] (C \theta) + [I_{x_z b} (S \phi) - I_{x_y b} (C \phi)] (S \theta) \} \\ & + \ddot{\phi} \{ I_{x_b} (-S \theta) + [I_{x_z b} (C \phi) + I_{x_y b} (S \phi)] (C \theta) \} \\ & + \ddot{X} \{ m [\bar{X} (-S \psi C \theta) + \bar{Y} (S \psi S \theta S \phi + C \psi C \phi) + \bar{Z} (S \psi S \theta C \phi - C \psi S \phi)] \} \\ & + \ddot{Y} \{ m [-\bar{X} (C \psi C \theta) - \bar{Y} (-C \psi S \theta S \phi + S \psi C \phi) - \bar{Z} (-C \psi S \theta C \phi - S \psi S \phi)] \} \\ & + \dot{\psi} \dot{\theta} \{ [I_{x_b} - I_{y_b} (S^2 \phi) - I_{z_b} (C^2 \phi) + I_{y_z b} (S 2 \phi)] (S 2 \theta) - [I_{x_z b} (C \phi) + I_{x_y b} (S \phi)] (2 C 2 \theta) \} \\ & + \dot{\psi} \dot{\phi} \{ [(I_{y_b} - I_{z_b}) (S 2 \phi) - I_{y_z b} (2 C 2 \phi)] (C^2 \theta) + [I_{x_z b} (S \phi) - I_{x_y b} (C \phi)] (S 2 \theta) \} \\ & + \dot{\theta} \dot{\phi} \{ [-I_{x_b} + (I_{y_b} - I_{z_b}) (C 2 \phi) + I_{y_z b} (2 S 2 \phi)] (C \theta) \} \end{aligned}$$

$$\begin{aligned}
 & +\dot{\theta}^2 \{ [(I_{yb} - I_{zb}) (-\frac{1}{2} S 2\phi) + I_{yzb} (C 2\phi)] (S\theta) + I_{xzb} (C\theta S\phi) - I_{xyb} (C\theta C\phi) \} \\
 & +\dot{\phi}^2 \{ I_{xyb} (C\theta C\phi) - I_{xzb} (C\theta S\phi) \} \\
 & +\dot{X}\dot{\psi} \{ m [-\bar{X} (C\psi C\theta) - \bar{Y} (-C\psi S\theta S\phi + S\psi C\phi) - \bar{Z} (-C\psi S\theta C\phi - S\psi S\phi)] \} \\
 & +\dot{X}\dot{\theta} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\
 & +\dot{X}\dot{\phi} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) - \bar{Z} (S\psi S\theta S\phi + C\psi C\phi)] \} \\
 & +\dot{Y}\dot{\psi} \{ m [-\bar{X} (-S\psi C\theta) - \bar{Y} (S\psi S\theta S\phi + C\psi C\phi) - \bar{Z} (S\psi S\theta C\phi - C\psi S\phi)] \} \\
 & +\dot{Y}\dot{\theta} \{ m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \} \\
 & +\dot{Y}\dot{\phi} \{ m [-\bar{Y} (-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z} (-C\psi S\theta S\phi + S\psi C\phi)] \}
 \end{aligned} \tag{81}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \psi} & = \dot{X}\dot{\psi} \{ m [-\bar{X} (C\psi C\theta) - \bar{Y} (-C\psi S\theta S\phi + S\psi C\phi) - \bar{Z} (-C\psi S\theta C\phi - S\psi S\phi)] \} \\
 & +\dot{X}\dot{\theta} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\
 & +\dot{X}\dot{\phi} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) - \bar{Z} (S\psi S\theta S\phi + C\psi C\phi)] \} \\
 & +\dot{Y}\dot{\psi} \{ m [-\bar{X} (-S\psi C\theta) - \bar{Y} (S\psi S\theta S\phi + C\psi C\phi) - \bar{Z} (S\psi S\theta C\phi - C\psi S\phi)] \} \\
 & +\dot{Y}\dot{\theta} \{ m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \} \\
 & +\dot{Y}\dot{\phi} \{ m [-\bar{Y} (-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z} (-C\psi S\theta S\phi + S\psi C\phi)] \}
 \end{aligned} \tag{82}$$

$$\frac{\partial \bar{G}}{\partial \psi} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \psi} + \bar{B} \frac{\partial \bar{B}}{\partial \psi} \} / L_T \tag{83}$$

$$\frac{\partial F}{\partial \psi} = 0 \tag{84}$$

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θ Equation

$$\begin{aligned}
 \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{\theta}} \right) = & \ddot{\psi} \{ [(I_{yb} - I_{zb}) \left( \frac{1}{2} S^2 \phi \right) - I_{yzb} (C^2 \phi)] (C\theta) - [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (S\theta) \} \\
 & + \ddot{\theta} \{ I_{yb} (C^2 \phi) + I_{zb} (S^2 \phi) + I_{yzb} (S^2 \phi) \} \\
 & + \ddot{\phi} \{ I_{xyb} (C\phi) - I_{xzb} (S\phi) \} \\
 & + \ddot{X} \{ m [\bar{X} (-C\psi S\theta) + \bar{Y} (-C\psi C\theta S\phi) + \bar{Z} (-C\psi C\theta C\phi)] \} \\
 & + \ddot{Y} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\
 & + \ddot{Z} \{ m [\bar{X} (C\theta) + \bar{Y} (-S\theta S\phi) + \bar{Z} (-S\theta C\phi)] \} \\
 & + \dot{\psi} \dot{\theta} \{ [(I_{yb} - I_{zb}) \left( -\frac{1}{2} S^2 \phi \right) + I_{yzb} (C^2 \phi)] (S\theta) + [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (-C\theta) \} \\
 & + \dot{\psi} \dot{\phi} \{ [(I_{yb} - I_{zb}) (C^2 \phi) + I_{yzb} (2S^2 \phi)] (C\theta) + [I_{xyb} (S\phi) + I_{xzb} (C\phi)] (S\theta) \} \\
 & + \dot{\theta} \dot{\phi} \{ [I_{yb} - I_{zb}] (-S^2 \phi) + I_{yzb} (2C^2 \phi) \} \\
 & + \dot{\phi}^2 \{ -I_{xyb} (S\phi) - I_{xzb} (C\phi) \} \\
 & + \dot{X} \dot{\psi} \{ m [\bar{X} (S\psi S\theta) + \bar{Y} (S\psi C\theta S\phi) + \bar{Z} (S\psi C\theta C\phi)] \} \\
 & + \dot{X} \dot{\theta} \{ m [\bar{X} (-C\psi C\theta) + \bar{Y} (C\psi S\theta S\phi) + \bar{Z} (C\psi S\theta C\phi)] \} \\
 & + \dot{X} \dot{\phi} \{ m [\bar{Y} (-C\psi C\theta C\phi) + \bar{Z} (C\psi C\theta S\phi)] \} \\
 & + \dot{Y} \dot{\psi} \{ m [\bar{X} (C\psi S\theta) + \bar{Y} (C\psi C\theta S\phi) + \bar{Z} (C\psi C\theta C\phi)] \}
 \end{aligned}$$

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$$\begin{aligned}
 & +\dot{Y}\dot{\theta}\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi)+\bar{Z}(-S\psi S\theta C\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Z}\dot{\theta}\{m[-\bar{X}(S\theta)-\bar{Y}(C\theta S\phi)-\bar{Z}(C\theta C\phi)]\} \\
 & +\dot{Z}\dot{\phi}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\}
 \end{aligned} \tag{85}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \theta} = & \dot{\psi}\dot{\theta}\{[I_{zb}-I_{yb}]\left(\frac{1}{2}S\theta S2\phi\right)+[-I_{xyb}(C\phi)+I_{xzb}(S\phi)](C\theta)+[I_{yzb}](S\theta C2\phi)\} \\
 & +\dot{\psi}\dot{\phi}\{[I_{xb}](-C\theta)+[I_{xzb}(C\phi)+I_{xyb}(S\phi)](-S\theta)\} \\
 & +\dot{\psi}^2\{[I_{xb}-I_{yb}(S^2\phi)-I_{zb}(C^2\phi)+I_{yzb}(S2\phi)]\left(\frac{1}{2}S2\theta\right)-[I_{xzb}(C\phi)+I_{xyb}(S\phi)](C2\theta)\} \\
 & +\dot{X}\dot{\psi}\{m[\bar{X}(S\psi S\theta)+\bar{Y}(S\psi C\theta S\phi)+\bar{Z}(S\psi C\theta C\phi)]\} \\
 & +\dot{X}\dot{\theta}\{m[\bar{X}(-C\psi C\theta)+\bar{Y}(C\psi S\theta S\phi)+\bar{Z}(C\psi S\theta C\phi)]\} \\
 & +\dot{X}\dot{\phi}\{m[\bar{Y}(-C\psi C\theta C\phi)+\bar{Z}(C\psi C\theta S\phi)]\} \\
 & +\dot{Y}\dot{\psi}\{m[\bar{X}(C\psi S\theta)+\bar{Y}(C\psi C\theta S\phi)+\bar{Z}(C\psi C\theta C\phi)]\} \\
 & +\dot{Y}\dot{\theta}\{m[\bar{X}(S\psi C\theta)+\bar{Y}(-S\psi S\theta S\phi)+\bar{Z}(-S\psi S\theta C\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Z}\dot{\theta}\{m[\bar{X}(-S\theta)+\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \\
 & +\dot{Z}\dot{\phi}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\} \\
 & -mg[\bar{X}(C\theta)+\bar{Y}(-S\theta S\phi)+\bar{Z}(-S\theta C\phi)]
 \end{aligned} \tag{86}$$

$$\frac{\partial g}{\partial \theta} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \theta} + \bar{B} \frac{\partial \bar{B}}{\partial \theta} + \bar{C} \frac{\partial \bar{C}}{\partial \theta} \} / L_T \quad (87)$$

$$\frac{\partial F}{\partial \dot{\theta}} = 0 \quad (88)$$

φ Equation

$$\begin{aligned} \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{\phi}} \right) = & \dot{\psi} \{ I_{xb} (-S\theta) + I_{xyb} (C\theta S\phi) + I_{xzb} (C\theta C\phi) \} \\ & + \ddot{\theta} \{ I_{xyb} (C\phi) - I_{xzb} (S\phi) \} + \ddot{\phi} \{ I_{xb} \} \\ & + \dot{X} \{ m [\bar{Y} (-C\psi S\theta C\phi - S\psi S\phi) + \bar{Z} (C\psi S\theta S\phi - S\psi C\phi)] \} \\ & + \dot{Y} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) + \bar{Z} (-S\psi S\theta S\phi - C\psi C\phi)] \} \\ & + \dot{Z} \{ m [\bar{Y} (C\theta C\phi) + \bar{Z} (-C\theta S\phi)] \} \\ & + \dot{\psi} \dot{\theta} \{ I_{xb} (-C\theta) + [I_{xyb} (S\phi) + I_{xzb} (C\phi)] (-S\theta) \} \\ & + \dot{\psi} \dot{\phi} \{ [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (C\theta) \} \\ & + \dot{\theta} \dot{\phi} \{ -I_{xyb} (S\phi) - I_{xzb} (C\phi) \} \\ & + \dot{X} \dot{\psi} \{ m [\bar{Y} (S\psi S\theta C\phi - C\psi S\phi) + \bar{Z} (-S\psi S\theta S\phi - C\psi C\phi)] \} \\ & + \dot{X} \dot{\theta} \{ m [\bar{Y} (-C\psi C\theta C\phi) + \bar{Z} (C\psi C\theta S\phi)] \} \\ & + \dot{X} \dot{\phi} \{ m [\bar{Y} (C\psi S\theta S\phi - S\psi C\phi) + \bar{Z} (C\psi S\theta C\phi + S\psi S\phi)] \} \end{aligned}$$

$$\begin{aligned}
 & +\dot{Y}\dot{\psi}\{m[\bar{Y}(C\psi S\theta C\phi+S\psi S\phi)+\bar{Z}(-C\psi S\theta S\phi+S\psi C\phi)]\} \\
 & +\dot{Y}\dot{\theta}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\} \\
 & +\dot{Z}\dot{\theta}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\}+\dot{Z}\dot{\phi}\{m[\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \quad (89)
 \end{aligned}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \phi} = & \dot{\psi}\dot{\theta}\{[(I_{yb}-I_{zb})(C2\phi)+I_{yzb}(2S2\phi)](C\theta)+[I_{xyb}(S\phi)+I_{xzb}(C\phi)](S\theta)\} \\
 & +\dot{\psi}\dot{\phi}\{[I_{xyb}(C\phi)-I_{xzb}(S\phi)](C\theta)\} \\
 & +\dot{\theta}\dot{\phi}\{-I_{xyb}(S\phi)-I_{xzb}(C\phi)\} \\
 & +\dot{\psi}^2\{[(I_{yb}-I_{zb})(\frac{1}{2}S2\phi)-I_{yzb}(C2\phi)](C^2\theta)+[I_{xzb}(S\phi)-I_{xyb}(C\phi)](\frac{1}{2}S2\theta)\} \\
 & +\dot{\theta}^2\{(I_{yb}-I_{zb})(-\frac{1}{2}S2\phi)+I_{yzb}(C2\phi)\} \\
 & +\dot{X}\dot{\psi}\{m[\bar{Y}(S\psi S\theta C\phi-C\psi S\phi)+\bar{Z}(-S\psi S\theta S\phi-C\psi C\phi)]\} \\
 & +\dot{X}\dot{\theta}\{m[\bar{Y}(-C\psi C\theta C\phi)+\bar{Z}(C\psi C\theta S\phi)]\} \\
 & +\dot{X}\dot{\phi}\{m[\bar{Y}(C\psi S\theta S\phi-S\psi C\phi)+\bar{Z}(C\psi S\theta C\phi+S\psi S\phi)]\} \\
 & +\dot{Y}\dot{\psi}\{m[\bar{Y}(C\psi S\theta C\phi+S\psi S\phi)+\bar{Z}(-C\psi S\theta S\phi+S\psi C\phi)]\} \\
 & +\dot{Y}\dot{\theta}\{m[\bar{Y}(S\psi C\theta C\phi)+\bar{Z}(-S\psi C\theta S\phi)]\} \\
 & +\dot{Y}\dot{\phi}\{m[\bar{Y}(-S\psi S\theta S\phi-C\psi C\phi)+\bar{Z}(-S\psi S\theta C\phi+C\psi S\phi)]\}
 \end{aligned}$$

$$\begin{aligned}
 & +\dot{Z}\dot{\theta}\{m[\bar{Y}(-S\theta C\phi)+\bar{Z}(S\theta S\phi)]\} \\
 & +\dot{Z}\dot{\phi}\{m[\bar{Y}(-C\theta S\phi)+\bar{Z}(-C\theta C\phi)]\} \\
 & -mg[\bar{Y}(C\theta C\phi)-\bar{Z}(C\theta S\phi)]\}
 \end{aligned} \tag{90}$$

$$\frac{\partial \bar{g}}{\partial \phi} = \{ \bar{A} \frac{\partial \bar{A}}{\partial \phi} + \bar{B} \frac{\partial \bar{B}}{\partial \phi} + \bar{C} \frac{\partial \bar{C}}{\partial \phi} \} / L_T \tag{91}$$

$$\frac{\partial F}{\partial \dot{\phi}} = 0 \tag{92}$$

$\psi_p$  Equation

$$\begin{aligned}
 \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{\psi}_p} \right) &= \ddot{\psi}_p \{ I_{xpb} (S^2 \theta_p) + I_{ypb} (C^2 \theta_p) \} \\
 &+ \dot{\psi}_p \dot{\theta}_p \{ [I_{xpb} - I_{ypb}] S 2\theta_p \}
 \end{aligned} \tag{93}$$

$$\begin{aligned}
 \frac{\partial L}{\partial \psi_p} &= \dot{x}_p^2 \{ [m_{p\ell} - m_{ps}] [-\frac{1}{2} S 2\psi_p C^2 \theta_p] \} \\
 &+ \dot{y}_p^2 \{ [m_{p\ell} - m_{ps}] [\frac{1}{2} S 2\psi_p C^2 \theta_p] \} \\
 &+ \dot{x}_p \dot{y}_p [m_{p\ell} - m_{ps}] [-C 2\psi_p C^2 \theta_p] \\
 &+ \dot{x}_p \dot{z}_p \{ [m_{p\ell} - m_{ps}] [-\frac{1}{2} S \psi_p S 2\theta_p] \} \\
 &+ \dot{y}_p \dot{z}_p [m_{p\ell} - m_{ps}] [-\frac{1}{2} C \psi_p S 2\theta_p]
 \end{aligned} \tag{94}$$

$$\frac{\partial \bar{g}}{\partial \psi_p} = \left\{ \bar{A} \frac{\partial \bar{A}}{\partial \psi_p} + \bar{B} \frac{\partial \bar{B}}{\partial \psi_p} \right\} / L_T \quad (95)$$

$$\frac{\partial F}{\partial \dot{\psi}_p} = 0 \quad (96)$$

$\theta_p$  Equation

$$\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{\theta}_p} \right) = I_{ypb} \ddot{\theta}_p \quad (97)$$

$$\begin{aligned} \frac{\partial L}{\partial \theta_p} = & \dot{x}_p^2 \{ [m_{pl} - m_{ps}] [-\frac{1}{2} C^2 \psi_p S 2\theta_p] \} \\ & + \dot{y}_p^2 \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S^2 \psi_p S 2\theta_p] \} \\ & + \dot{z}_p^2 \{ [m_{pl} - m_{ps}] [\frac{1}{2} S 2\theta_p] \} \\ & + \dot{x}_p \dot{y}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} S 2\psi_p S 2\theta_p] \} \\ & + \dot{x}_p \dot{z}_p \{ [m_{pl} - m_{ps}] [C \psi_p C 2\theta_p] \} \\ & + \dot{y}_p \dot{z}_p \{ [m_{pl} - m_{ps}] [-S \psi_p C 2\theta_p] \} \\ & + \dot{\psi}_p^2 \{ [I_{xpb} - I_{y pb}] [\frac{1}{2} S 2\theta_p] \} \end{aligned} \quad (98)$$

$$\frac{\partial \bar{g}}{\partial \theta_p} = \left\{ \bar{A} \frac{\partial \bar{A}}{\partial \theta_p} + \bar{B} \frac{\partial \bar{B}}{\partial \theta_p} + \bar{C} \frac{\partial \bar{C}}{\partial \theta_p} \right\} / L_T \quad (99)$$

$$\frac{\partial F}{\partial \dot{\theta}_p} = 0 \quad (100)$$



L<sub>T</sub> Equation

$$\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{L}_T} \right) = 0 \quad (101)$$

$$\frac{\partial L}{\partial L_T} = -K_S (L_T - L_{T0}) \quad (102)$$

$$\frac{\partial \bar{q}}{\partial L_T} = -1 \quad (103)$$

$$\frac{\partial F}{\partial \dot{L}_T} = C_S \dot{L}_T \quad (104)$$

Substituting Equations (101) to (104) into (54) yields:

$$\lambda = -[K_S (L_T - L_{T0}) + C_S \dot{L}_T] \quad (105)$$

The value of  $\lambda$  in Equation (54) is now defined and is expressed in terms of the eleven generalized coordinates and their time derivatives. The eleven simultaneous, nonlinear, coupled differential equations of motion are then written as:

1. X Equation

$$\begin{aligned} & \ddot{X}\{m\} + \ddot{\psi}\{m[\bar{X} C_{12} + \bar{Y} C_{22} + \bar{Z} C_{32}]\} \\ & + \ddot{\theta}\{m[\bar{X}(-C\psi S\theta) + \bar{Y}(-C\psi C\theta S\phi) + \bar{Z}(-C\psi C\theta C\phi)]\} + \ddot{\phi}\{m[\bar{Y}C_{31} - \bar{Z}C_{21}]\} \\ & = \dot{\psi}\dot{\theta}\{-2m[\bar{X}(S\psi S\theta) + \bar{Y}(S\psi C\theta S\phi) + \bar{Z}(S\psi C\theta C\phi)]\} + \dot{\psi}\dot{\phi}\{-2m[\bar{Y}C_{32} - \bar{Z}C_{22}]\} \end{aligned}$$

$$\begin{aligned}
 & +\ddot{\theta}\dot{\phi}\{2m[\bar{Y}(C\psi C\theta C\phi)-\bar{Z}(C\psi C\theta S\phi)]\}+\dot{\psi}^2\{m[\bar{X}C_{11}+\bar{Y}C_{21}+\bar{Z}C_{31}]\} \\
 & +\dot{\theta}^2\{m[\bar{X}C_{11}+\bar{Y}(-C\psi S\theta S\phi)+\bar{Z}(-C\psi S\theta C\phi)]\}+\dot{\phi}^2\{m[\bar{Y}C_{21}+\bar{Z}C_{31}]\} \\
 & +[K_s(L_T-L_{TO})+C_s\dot{L}_T][\bar{A}/L_T]+F_x
 \end{aligned} \tag{106}$$

2. Y Equation

$$\begin{aligned}
 & \ddot{Y}\{m\}+\ddot{\psi}\{-m[\bar{X}C_{11}+\bar{Y}C_{21}+\bar{Z}C_{31}]\} \\
 & +\ddot{\theta}\{m[\bar{X}(S\psi S\theta)+\bar{Y}(S\psi C\theta S\phi)+\bar{Z}(S\psi C\theta C\phi)]\}+\ddot{\phi}\{m[\bar{Y}C_{32}-\bar{Z}C_{22}]\} \\
 = & \dot{\psi}\dot{\theta}\{-2m[\bar{X}(C\psi S\theta)+\bar{Y}(C\psi C\theta S\phi)+\bar{Z}(C\psi C\theta C\phi)]\}+\dot{\psi}\dot{\phi}\{2m[\bar{Y}C_{31}-\bar{Z}C_{21}]\} \\
 & +\dot{\theta}\dot{\phi}\{-2m[\bar{Y}(S\psi C\theta C\phi)-\bar{Z}(S\psi C\theta S\phi)]\}+\dot{\psi}^2\{m[\bar{X}C_{12}+\bar{Y}C_{22}+\bar{Z}C_{32}]\} \\
 & +\dot{\theta}^2\{m[\bar{X}C_{12}+\bar{Y}(S\psi S\theta S\phi)+\bar{Z}(S\psi S\theta C\phi)]\}+\dot{\phi}^2\{m[\bar{Y}C_{22}+\bar{Z}C_{32}]\} \\
 & +[K_s(L_T-L_{TO})+C_s\dot{L}_T][\bar{B}/L_T]+F_y
 \end{aligned} \tag{107}$$

3. Z Equation

$$\begin{aligned}
 & \ddot{Z}\{m\}+\ddot{\theta}\{m[\bar{X}(C\theta)+\bar{Y}(-S\theta S\phi)+\bar{Z}(-S\theta C\phi)]\}+\ddot{\phi}\{m[\bar{Y}C_{33}-\bar{Z}C_{23}]\} \\
 = & \dot{\theta}\dot{\phi}\{2m[\bar{Y}(S\theta C\phi)-\bar{Z}(S\theta S\phi)]\}+\dot{\theta}^2\{m[\bar{X}C_{13}+\bar{Y}C_{23}+\bar{Z}C_{33}]\} \\
 & +\dot{\phi}^2\{m[\bar{Y}C_{23}+\bar{Z}C_{33}]\}+[K_s(L_T-L_{TO})+C_s\dot{L}_T][\bar{C}/L_T]-mg+F_z
 \end{aligned} \tag{108}$$

4. X<sub>p</sub> Equation

$$\begin{aligned}
 & \ddot{X}_p \{m_{p\ell} [c^2\psi_p c^2\theta_p] + m_{ps} [s^2\psi_p + c^2\psi_p s^2\theta_p]\} \\
 & + \ddot{Y}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}s^2\psi_p c^2\theta_p]\} + \ddot{Z}_p \{[m_{p\ell} - m_{ps}] [\frac{1}{2}c\psi_p s^2\theta_p]\} \\
 = & [m_{p\ell} - m_{ps}] \{\dot{X}_p \dot{\psi}_p [s^2\psi_p c^2\theta_p] + \dot{X}_p \dot{\theta}_p [c^2\psi_p s^2\theta_p] + \dot{Y}_p \dot{\psi}_p [c^2\psi_p c^2\theta_p] \\
 & + \dot{Y}_p \dot{\theta}_p [-\frac{1}{2}s^2\psi_p s^2\theta_p] + \dot{Z}_p \dot{\psi}_p [\frac{1}{2}s\psi_p s^2\theta_p] + \dot{Z}_p \dot{\theta}_p [-c\psi_p c^2\theta_p]\} \\
 & - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{A}/L_T] + F_{xp} \tag{109}
 \end{aligned}$$

5. Y<sub>p</sub> Equation

$$\begin{aligned}
 & \ddot{X}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}s^2\psi_p c^2\theta_p]\} + \ddot{Y}_p \{m_{p\ell} [s^2\psi_p c^2\theta_p] + m_{ps} [c^2\psi_p + s^2\psi_p s^2\theta_p]\} \\
 & + \ddot{Z}_p \{[m_{p\ell} - m_{ps}] [-\frac{1}{2}s\psi_p s^2\theta_p]\} \\
 = & [m_{p\ell} - m_{ps}] \{\dot{X}_p \dot{\psi}_p [c^2\psi_p c^2\theta_p] + \dot{X}_p \dot{\theta}_p [-\frac{1}{2}s^2\psi_p s^2\theta_p] + \dot{Y}_p \dot{\psi}_p [-s^2\psi_p c^2\theta_p] \\
 & + \dot{Y}_p \dot{\theta}_p [s^2\psi_p s^2\theta_p] + \dot{Z}_p \dot{\psi}_p [\frac{1}{2}c\psi_p s^2\theta_p] + \dot{Z}_p \dot{\theta}_p [s\psi_p c^2\theta_p]\} \\
 & - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{B}/L_T] + F_{yp} \tag{110}
 \end{aligned}$$

6. z<sub>p</sub> Equation

$$\begin{aligned}
 & \ddot{x}_p \{ [m_{pl} - m_{ps}] [\frac{1}{2} S \psi_p S 2\theta_p] \} + \ddot{y}_p \{ [m_{pl} - m_{ps}] [-\frac{1}{2} S \psi_p S 2\theta_p] \} \\
 & + \ddot{z}_p \{ m_{pl} [S^2 \theta_p] + m_{ps} [C^2 \theta_p] \} \\
 = & [m_{pl} - m_{ps}] \{ \dot{x}_p \dot{\psi}_p [\frac{1}{2} S \psi_p S 2\theta_p] + \dot{x}_p \dot{\theta}_p [-C \psi_p C 2\theta_p] + \dot{y}_p \dot{\psi}_p [\frac{1}{2} C \psi_p S 2\theta_p] \\
 & + \dot{y}_p \dot{\theta}_p [S \psi_p C 2\theta_p] + \dot{z}_p \dot{\theta}_p [-S 2\theta_p] \} \\
 & - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{C}/L_T] - m_p g + F_{zp} \tag{111}
 \end{aligned}$$

7. ψ Equation

$$\begin{aligned}
 & \ddot{\psi} \{ I_{xb} (S^2 \theta) + [I_{yb} (S^2 \phi) + I_{zb} (C^2 \phi)] (C^2 \theta) + I_{yzb} (-C^2 \theta S 2\phi) \\
 & + [I_{xzb} (C \phi) + I_{xyb} (S \phi)] (-S 2\theta) \} + \ddot{\theta} \{ [(I_{yb} - I_{zb}) (\frac{1}{2} S 2\phi) - I_{yzb} (C 2\phi)] (C \theta) \\
 & + [I_{xzb} (S \phi) - I_{xyb} (C \phi)] (S \theta) \} + \ddot{\phi} \{ -I_{xb} C_{13} + I_{xyb} C_{23} + I_{xzb} C_{33} \} \\
 & + \ddot{x} \{ m [\bar{X} C_{12} + \bar{Y} C_{22} + \bar{Z} C_{32}] \} + \ddot{y} \{ -m [\bar{X} C_{11} + \bar{Y} C_{21} + \bar{Z} C_{31}] \} \\
 = & \dot{\psi} \dot{\theta} \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi) + I_{yzb} (S 2\phi)] (-S 2\theta) + [I_{xzb} (C \phi) \\
 & + I_{xyb} (S \phi)] (2C 2\theta) \} + \dot{\psi} \dot{\phi} \{ [(I_{yb} - I_{zb}) (S 2\phi) - I_{yzb} (2C 2\phi)] (-C^2 \theta) \\
 & + [I_{xzb} (S \phi) - I_{xyb} (C \phi)] (-S 2\theta) \} + \dot{\theta} \dot{\phi} \{ [I_{xb} - (I_{yb} - I_{zb}) (C 2\phi) - I_{yzb} (2S 2\phi)] (C \theta) \} \\
 & + \dot{\theta}^2 \{ [(I_{yb} - I_{zb}) (\frac{1}{2} S 2\phi) - I_{yzb} (C 2\phi)] (S \theta) - I_{xzb} C_{23} + I_{xyb} C_{33} \}
 \end{aligned}$$

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$$\begin{aligned}
 & +\dot{\phi}^2 \{-I_{xyb} C_{33} + I_{xzb} C_{23}\} \\
 & - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi} + \bar{B} \frac{\partial \bar{B}}{\partial \psi}] / L_T + Q_\psi
 \end{aligned} \tag{112}$$

8.  $\theta$  Equation

$$\begin{aligned}
 & \ddot{X}\{m[\bar{X}(-C\psi\theta) + \bar{Y}(-C\psi C\theta S\phi) + \bar{Z}(-C\psi C\theta C\phi)]\} \\
 & + \ddot{Y}\{m[\bar{X}(S\psi\theta) + \bar{Y}(S\psi C\theta S\phi) + \bar{Z}(S\psi C\theta C\phi)]\} \\
 & + \ddot{Z}\{m[\bar{X}(C\theta) + \bar{Y}(-S\theta S\phi) + \bar{Z}(-S\theta C\phi)]\} \\
 & + \ddot{\psi}\{[(I_{yb} - I_{zb}) \frac{1}{2} S^2\phi - I_{yzb} (C^2\phi)] (C\theta) + [I_{xyb} (C\phi) - I_{xzb} (S\phi)] (-S\theta)\} \\
 & + \ddot{\theta}\{I_{yb} (C^2\phi) + I_{zb} (S^2\phi) + I_{yzb} (S^2\phi)\} + \ddot{\phi}\{I_{xyb} (C\phi) - I_{xzb} (S\phi)\} \\
 = & \dot{\psi}\dot{\phi}\{[I_{xb} + (I_{yb} - I_{zb}) (C^2\phi) + I_{yzb} (2S^2\phi)] (-C\theta) + [I_{xzb} (C\phi) + I_{xyb} (S\phi)] (-2S\theta)\} \\
 & + \dot{\theta}\dot{\phi}\{(I_{yb} - I_{zb}) (S^2\phi) - I_{yzb} (2C^2\phi)\} \\
 & + \dot{\psi}^2\{[I_{xb} - I_{yb} (S^2\phi) - I_{zb} (C^2\phi) + I_{yzb} (S^2\phi)] (\frac{1}{2} S^2\theta) + [I_{xzb} (C\phi) \\
 & + I_{xyb} (S\phi)] (-C^2\theta)\} + \dot{\phi}^2\{I_{xyb} (S\phi) + I_{xzb} (C\phi)\} - mg[\bar{X}(C\theta) + \bar{Y}(-S\theta S\phi) + \bar{Z}(-S\theta C\phi)] \\
 & - [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta} + \bar{B} \frac{\partial \bar{B}}{\partial \theta} + \bar{C} \frac{\partial \bar{C}}{\partial \theta}] / L_T + Q_\theta
 \end{aligned} \tag{113}$$

9.  $\phi$  Equation

$$\begin{aligned}
 & \ddot{X}\{m[\bar{Y}C_{31} - \bar{Z}C_{21}]\} + \ddot{Y}\{m[\bar{Y}C_{32} - \bar{Z}C_{22}]\} + \ddot{Z}\{m[\bar{Y}C_{33} - \bar{Z}C_{23}]\} \\
 & + \ddot{\psi}\{-I_{xb} C_{13} + I_{xyb} C_{23} + I_{xzb} C_{33}\} + \ddot{\theta}\{I_{xyb} (C\phi) - I_{xzb} (S\phi)\} + \ddot{\phi}\{I_{xb}\}
 \end{aligned}$$

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$$\begin{aligned}
 &= \dot{\psi} \dot{\theta} \{ [I_{x_b} + (I_{y_b} - I_{z_b}) (C2\phi) + I_{y_z b} (2S2\phi)] (C\theta) + [I_{x_{yb}} (S\phi) + I_{x_z b} (C\phi)] (2S\theta) \} \\
 &+ \dot{\psi}^2 \{ [(I_{y_b} - I_{z_b}) (\frac{1}{2}S2\phi) - I_{y_z b} (C2\phi)] (C^2\theta) + [I_{x_z b} (S\phi) - I_{x_{yb}} (C\phi)] (\frac{1}{2}S2\theta) \} \\
 &+ \dot{\theta}^2 \{ (I_{y_b} - I_{z_b}) (-\frac{1}{2}S2\phi) + I_{y_z b} (C2\phi) \} - mg [\bar{Y}C_{33} - \bar{Z}C_{23}] \\
 &- [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \phi} + \bar{B} \frac{\partial \bar{B}}{\partial \phi} + \bar{C} \frac{\partial \bar{C}}{\partial \phi}] / L_T + Q_\phi \tag{114}
 \end{aligned}$$

10.  $\psi_p$  Equation

$$\begin{aligned}
 &\ddot{\psi}_p \{ I_{x_{pb}} (S^2\theta_p) + I_{y_{pb}} (C^2\theta_p) \} \\
 &= \dot{\psi}_p \dot{\theta}_p \{ (I_{x_{pb}} - I_{y_{pb}}) (-S2\theta_p) \} + [m_{p\ell} - m_{ps}] \{ \dot{x}_p \dot{y}_p [-C2\psi_p C^2\theta_p] \\
 &+ \dot{x}_p \dot{z}_p [-\frac{1}{2}S\psi_p S2\theta_p] + \dot{y}_p \dot{z}_p [-\frac{1}{2}C\psi_p S2\theta_p] + \dot{x}_p^2 [-\frac{1}{2}S2\psi_p C^2\theta_p] + \dot{y}_p^2 [\frac{1}{2}S2\psi_p C^2\theta_p] \} \\
 &- [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi_p} + \bar{B} \frac{\partial \bar{B}}{\partial \psi_p}] / L_T + Q_{\psi_p} \tag{115}
 \end{aligned}$$

11.  $\theta_p$  Equation

$$\begin{aligned}
 &\ddot{\theta}_p \{ I_{y_{pb}} \} \\
 &= \dot{\psi}_p^2 \{ (I_{x_{pb}} - I_{y_{pb}}) (\frac{1}{2}S2\theta_p) \} + [m_{p\ell} - m_{ps}] \{ \dot{x}_p \dot{y}_p [\frac{1}{2}S2\psi_p S2\theta_p] + \dot{x}_p \dot{z}_p [C\psi_p C2\theta_p] \\
 &+ \dot{y}_p \dot{z}_p [-S\psi_p C2\theta_p] + \dot{x}_p^2 [-\frac{1}{2}C^2\psi_p S2\theta_p] + \dot{y}_p^2 [-\frac{1}{2}S^2\psi_p S2\theta_p] + \dot{z}_p^2 [\frac{1}{2}S2\theta_p] \} \\
 &- [K_S (L_T - L_{T0}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta_p} + \bar{B} \frac{\partial \bar{B}}{\partial \theta_p} + \bar{C} \frac{\partial \bar{C}}{\partial \theta_p}] / L_T + Q_{\theta_p} \tag{116}
 \end{aligned}$$

SECTION 8 - SIMPLIFIED EQUATIONS OF MOTION

Equations (106) to (116) are for the most general situation possible, and as a result, are quite lengthy. Under some circumstances, these equations can be simplified. If this can be accomplished, a significant decrease in computer time will be realized. The first simplification occurs if the forebody's aerodynamic (body) reference axes are principal axes. In this case  $\bar{X} = \bar{Y} = \bar{Z} = 0$  and  $I_{xyb} = I_{xzb} = I_{yzb} = 0$ . Equations (106), (107), (108), (112), (113), and (114) become:

$$\ddot{X}\{m\} = [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{A}/L_T] + F_x \quad (117)$$

$$\ddot{Y}\{m\} = [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{B}/L_T] + F_y \quad (118)$$

$$\ddot{Z}\{m\} = [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{C}/L_T] - mg + F_z \quad (119)$$

$$\begin{aligned} & \ddot{\psi} \{ I_{xb} (S^2 \theta) + [I_{yb} (S^2 \phi) + I_{zb} (C^2 \phi)] (C^2 \theta) \} + \ddot{\theta} \{ (I_{yb} - I_{zb}) (\frac{1}{2} C \theta S 2 \phi) \} + \dot{\phi} \{ -I_{xb} C_{13} \} \\ & = \dot{\psi} \dot{\theta} \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi)] (-S 2 \theta) \} + \dot{\psi} \dot{\phi} \{ (I_{yb} - I_{zb}) (-C^2 \theta S 2 \phi) \} \\ & + \dot{\theta} \dot{\phi} \{ [I_{xb} - (I_{yb} - I_{zb}) (C 2 \phi)] (C \theta) \} + \dot{\theta}^2 \{ (I_{yb} - I_{zb}) (\frac{1}{2} S \theta S 2 \phi) \} \\ & - [K_S (L_T - L_{TO}) + C_S \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi} + \bar{B} \frac{\partial \bar{B}}{\partial \psi}] / L_T + Q_\psi \end{aligned} \quad (120)$$

$$\begin{aligned} & \ddot{\psi} \{ (I_{yb} - I_{zb}) (\frac{1}{2} C \theta S 2 \phi) \} + \ddot{\theta} \{ I_{yb} (C^2 \phi) + I_{zb} (S^2 \phi) \} \\ & = \dot{\psi} \dot{\phi} \{ [I_{xb} + (I_{yb} - I_{zb}) (C 2 \phi)] (-C \theta) \} + \dot{\theta} \dot{\phi} \{ (I_{yb} - I_{zb}) (S 2 \phi) \} \\ & \dot{\psi}^2 \{ [I_{xb} - I_{yb} (S^2 \phi) - I_{zb} (C^2 \phi)] (\frac{1}{2} S 2 \theta) \} \end{aligned}$$

$$-[K_S(L_T-L_{TO})+C_S\dot{L}_T][\bar{A}\frac{\partial\bar{A}}{\partial\theta}+\bar{B}\frac{\partial\bar{B}}{\partial\theta}+\bar{C}\frac{\partial\bar{C}}{\partial\theta}]/L_T+Q_\theta \quad (121)$$

$$\begin{aligned} & \ddot{\psi}\{-I_{xb}C_{13}\}+\ddot{\phi}\{I_{xb}\} \\ = & \dot{\psi}\dot{\theta}\{[I_{xb}+(I_{yb}-I_{zb})(C2\phi)](C\theta)\}+\dot{\psi}^2\{(I_{yb}-I_{zb})(\frac{1}{2}C^2\theta S2\phi)\} \\ & +\dot{\theta}^2\{(I_{yb}-I_{zb})(-\frac{1}{2}S2\phi)\} \\ & -[K_S(L_T-L_{TO})+C_S\dot{L}_T][\bar{A}\frac{\partial\bar{A}}{\partial\phi}+\bar{B}\frac{\partial\bar{B}}{\partial\phi}+\bar{C}\frac{\partial\bar{C}}{\partial\phi}]/L_T+Q_\phi \quad (122) \end{aligned}$$

The above six equations of motion have not only been shortened, but they also have been uncoupled in the translational accelerations making them easier to solve. The second simplification involves the decelerator degrees of freedom. If the added masses of the decelerator are ignored ( $m_{pl} = m_{ps} = m_p$ ), Equations (109), (110), (111), (115), and (116) become:

$$\ddot{X}_p\{m_p\} = -[K_S(L_T-L_{TO})+C_S\dot{L}_T](\bar{A}/L_T) + F_{xp} \quad (123)$$

$$\ddot{Y}_p\{m_p\} = -[K_S(L_T-L_{TO})+C_S\dot{L}_T](\bar{B}/L_T) + F_{yp} \quad (124)$$

$$\ddot{Z}_p\{m_p\} = -[K_S(L_T-L_{TO})+C_S\dot{L}_T](\bar{C}/L_T) - m_p g + F_{zp} \quad (125)$$



$$\ddot{\psi}_p \{I_{xpb} (S^2 \theta_p) + I_{ypb} (C^2 \theta_p)\} = \dot{\psi}_p \dot{\theta}_p \{(I_{xpb} - I_{ypb}) (-S2\theta_p)\} \\ - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \psi_p} + \bar{B} \frac{\partial \bar{B}}{\partial \psi_p}] / L_T + Q_{\psi p} \quad (126)$$

$$\ddot{\theta}_p \{I_{ypb}\} = \dot{\psi}_p^2 \{(I_{xpb} - I_{ypb}) (\frac{1}{2} S2\theta_p)\} \\ - [K_s (L_T - L_{T0}) + C_s \dot{L}_T] [\bar{A} \frac{\partial \bar{A}}{\partial \theta_p} + \bar{B} \frac{\partial \bar{B}}{\partial \theta_p} + \bar{C} \frac{\partial \bar{C}}{\partial \theta_p}] / L_T + Q_{\theta p} \quad (127)$$

Like the simplified equation for the forebody, the decelerator equations have also shortened. Furthermore, they have completely uncoupled in the second derivatives making numerical integration easy.

SECTION 9 - GENERALIZED FORCES - AERODYNAMICS

The nonconservative forces acting on the forebody are due to aerodynamics. The aerodynamics and the convention used in this report apply to the Space Shuttle Solid Rocket Booster (S.R.B.). If a different body is to be simulated, the aerodynamic coefficients and possibly the convention used to define them, would change.

For the S.R.B., the aerodynamics are a function of roll angle, angle-of-attack, and Mach number. The angle-of-attack is measured from the total velocity vector to the positive longitudinal axis ( $X_b$ ) as shown in Figure 3.

$$\alpha = \tan^{-1} \left[ \frac{(\dot{y}_b^2 + \dot{z}_b^2)^{1/2}}{\dot{x}_b} \right] \quad (128)$$

The normal force coefficient,  $C_N$ , is in the plane formed by the velocity vector and the longitudinal axis, and is perpendicular to the longitudinal axis ( $X_b$ ). The roll angle,  $\phi_i$ , is then measured from the normal force coefficient to the  $Z_b$  body axis. The axial force coefficient is defined as usual, positive in the negative  $X_b$  direction. Finally, the side force coefficient is perpendicular to the  $X_b$  body axis and to the normal force, such that the directions of  $C_A$ ,  $C_N$ ,  $C_Y$  form a right-handed orthogonal coordinate system. Mathematically, the aerodynamics roll angle is given by:

$$\phi_i = \tan^{-1} [-\dot{y}_b / -\dot{z}_b] \quad (129)$$

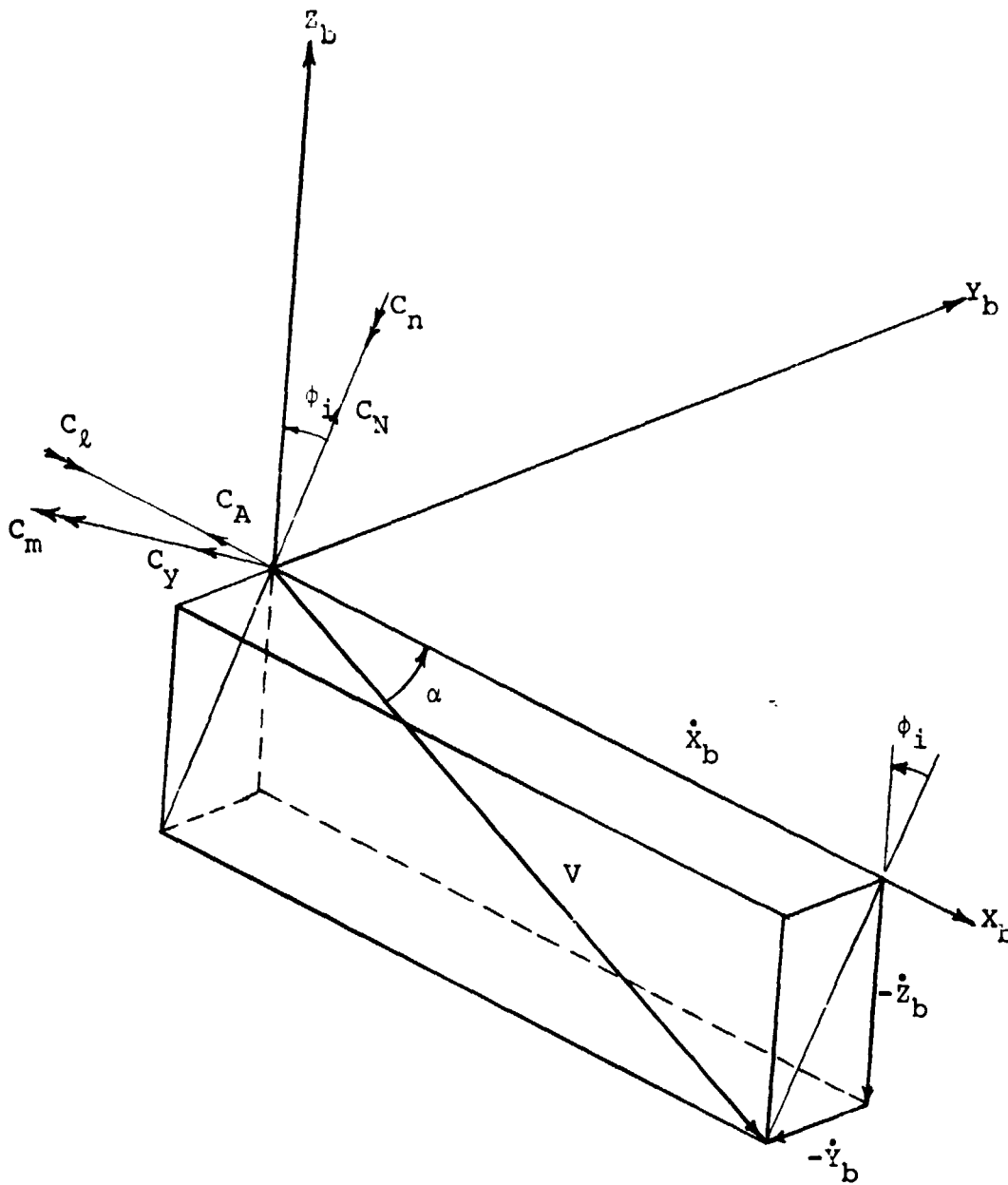


FIGURE 3 - AERODYNAMIC COORDINATE SYSTEM

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The positive directions of the moment coefficients are shown in Figure 3 as double arrows. Damping moment coefficients are about the body axes ( $X_b, Y_b, Z_b$ ). Aerodynamic body axes forces are given as:

$$F_{xb} = -q S C_A \quad (130)$$

$$F_{yb} = qS[-C_Y C\phi_i + C_N S\phi_i] \quad (131)$$

$$F_{zb} = qS[C_Y S\phi_i + C_N C\phi_i] \quad (132)$$

The body axes forces are converted to inertial axes force using the elements of [C], Equation 4.

$$F_x = F_{xb} C_{11} + F_{yb} C_{21} + F_{zb} C_{31} \quad (133)$$

$$F_y = F_{xb} C_{12} + F_{yb} C_{22} + F_{zb} C_{32} \quad (134)$$

$$F_z = F_{xb} C_{13} + F_{yb} C_{23} + F_{zb} C_{33} - mg \quad (135)$$

Body axes torques are:

$$T_{xb} = gSd[C_\ell + C_{\ell p} \left(\frac{\omega_{xb}^d}{2V}\right)] \quad (136)$$

$$T_{yb} = qSd[-C_m C\phi_i - C_n S\phi_i + C_{m_q} \left(\frac{\omega_{yb}^d}{2V}\right)] \quad (137)$$

$$T_{zb} = qSd[C_m S\phi_i - C_n C\phi_i + C_{n_r} \left(\frac{\omega_{zb}^d}{2V}\right)] \quad (138)$$

The body axis torques are transformed to generalized torques using Equations (5) and (1) and noting sign conventions.

$$Q_{\psi} = -[T_{xb} C_{13} + T_{yb} C_{23} + T_{zb} C_{33}] \quad (139)$$

$$Q_{\theta} = -T_{yb} C_{\phi} + T_{zb} S_{\phi} \quad (140)$$

$$Q_{\phi} = T_{xb} \quad (141)$$

The aerodynamics of a decelerator (parachute) are not well known because a parachute is not a rigid body, and does not lend itself to easily obtainable test data, especially under dynamic conditions. Consequently the aerodynamics of a symmetric decelerator tend to be relatively simple due to a lack of better understanding rather than the inability to use available information. If better aerodynamic data is attainable, it is a simple matter to alter the body forces and torques appropriately.

For this report, the decelerator body forces and torques are:

$$F_{xpb} = -q_p S_p C_{Ap} \quad (142)$$

$$F_{ypb} = q_p S_p C_{NP} S_{\phi_{pi}} \quad (143)$$

$$F_{zpb} = q_p S_p C_{Np} C_{\phi_{pi}} \quad (144)$$

$$T_{ypb} = -q_p S_p d_p (C_{MP} - 0.1 * \dot{\theta}_p * D_p / V_p) C_{\phi_{pi}} \quad (145)$$

$$T_{zpb} = q_p S_p d_p (C_{MP} - 0.1 * \dot{\theta}_p * D_p / V_p) S_{\phi_{pi}} \quad (146)$$

$$\phi_{pi} = \tan^{-1} [-\dot{y}_{pb} / -\dot{z}_{pb}] \quad (147)$$

The generalized forces for the decelerator are:

$$F_{xp} = F_{xpb} C_{p11} + F_{ypb} C_{p21} + F_{zpb} C_{p31} \quad (148)$$

$$F_{yp} = F_{xpb} C_{p12} + F_{ypb} C_{p22} + F_{zpb} C_{p32} \quad (149)$$

$$F_{zp} = F_{xpb} C_{p13} + F_{zpb} C_{p33} - m_p g \quad (150)$$

$$Q_{\psi p} = -T_{zpb} C_{p33} \quad (151)$$

$$Q_{\theta p} = -T_{ypb} \quad (152)$$

CHAPTER III COMPUTER PROGRAM

SECTION 1 - FEATURES OF THE COMPUTER PROGRAM

The computer program contains the following features.

1. The program has many options which simplify the input of data or decrease the program run time. Use of the options are contained in the listing of the program as comment cards. These options are:
  - a. Options are included which change the dimensions of the aerodynamic coefficient arrays as dictated by input requirements.
  - b. An option is provided (OPDT = 1.0) which automatically determines the magnitude of the integration time interval, DT.
  - c. An option is provided (OPSP = 1.0) which calculates the parachute drag area (SP) time history. If this option is not used the drag area versus time is input into the program in the form of look-up arrays.
  - d. An option for including longitudinal and lateral added air mass effects on the parachute (OPAM = 1.0) is included in the program.
  - e. A provision is made to use simplified equations of motion (OPOS = 0.0) to reduce run time, if all the forebody products of inertia and center of mass offsets are equal to zero.
  - f. An option (OPPLOT = 1.0) for making a plot tape is available.
  - g. English or metric systems may be used for data input and out by equating METRC to 0.0 or 1.0 respectively.
2. All aerodynamic coefficients are read into the program as functions of angle of attack, roll angle, and mach number in the form of three dimensional look-up arrays.

3. The initial start conditions for the forebody and aft body are completely general.
4. The stacking of design cases is possible.
5. The attachment location of the tether to the forebody is completely general.
6. The tether load and the angle it makes with the centerline of the forebody are program outputs.
7. All load and trajectory data are output at pre-selected times.
8. Termination of a design case occurs at a predetermined time or altitude.
9. The program calculates the effective system spring constant.
10. The program calculates the parachute physical properties as the parachute inflates as a function of time.
11. The parachute may have three stages of reefing, if the automatic drag area versus time option is chosen.
12. As the parachute inflates, the drag area versus time follows a second degree curve ( $y = ax^2$ ).



SECTION 2 - INPUT

Except for the variable COM, all inputs are read in under the format statement 8F10.0. COM is an 80 column header card. All of the following variables are defined in the nomenclature.

<u>INPUT ITEM</u>	<u>VARIABLE</u>	<u>NUMBER OF CARDS</u>
a)	AIPHI, AIPHID, AJALPF, AJALPM, AKAM, AKAMD, OPSYM, OPDA	1 card
b)	PPHIE	1 card
c)	AALPFE	1 or 2 cards
d)	AALPME	1 or 2 cards
e)	AAM	1 card
f)	CCA	4 to 128 cards
g)	CCN	4 to 128 cards
h)	CCLM	4 to 128 cards
i)	CCY	0 or 4 to 128 cards
j)	CCLL	0 or 4 to 128 cards
k)	CCLN	0 or 4 to 128 cards
l)	CLLP, CLMQ, CLNR	0 or 1 card
m)	PPHIDE	0 or 1 card
n)	AALPDE	0 or 1 card
o)	AAMD	0 or 1 card
p)	CCLLP	0 or 4 to 64 cards
q)	CCLMQ	0 or 4 to 64 cards
r)	CCLNR	0 or 4 to 64 cards
s)	AALPPE	1 card
t)	AAMP	1 card
u)	CCAP	2 to 8 cards
v)	CCNP	2 to 8 cards
w)	CCMP	2 to 8 cards

<u>INPUT ITEM</u>	<u>VARIABLE</u>	<u>NUMBER OF CARDS</u>
x)	PS, PT, EPL, EPT	1 card
y)	X, Y, X, V, GAME, CHIE, EPSI, ETAI	1 card
z)	WT, LXB, IYB, IZB, IXYB, IXZB, IYZB	1 card
aa)	S, D, XBAR, YBAR, ZBAR, OPPRIN, OPLOT, OPOS	1 card
bb)	PSIE, THEE, PHIE, OMXBE, OMYBE, OMZBE	1 card
cc)	A, B, C, OPAM, OMETRC	1 card
dd)	PSIPE, THEPE, PSIPDE, THEPDE, VP, GAMPE, CHIPE	1 card
ee)	LS, LTO, DLTO, NS, NT, DP, CCRIT	1 card
ff)	AMAX1, AMAX2, DSX1, DSX2, AMAY1, AMAY2, DSY1, DSY2	1 card
gg)	WTC, WTL, OPSP, OPDT IF (OPSP.EQ.0.0) GO TO ITEM kk)	
hh)	TRO, TR1, TR2, TR3	1 card
jj)	SPRO, SPR1, SPR2, SPR3, PCT01, PCT02, PCT03, POROS	1 card
kk)	TTIP, SSP IF (OPDT.EQ.0.0) GO TO ITEM mm)	4 cards
ll)	GLOAD, FSULT, AERATO, TO, DTP1, TTT, HHH	1 card
mm)	DT1, TO, DTP1, TTT, HHH	1 card
nn)	COM	1 card

The values of the variables read in input item "a" determine, in part, the sizes of the aerodynamic arrays. The axial and moment coefficients have the option of using either eight or sixteen angles-of-attack (one or two cards). If, for example, five or eleven angles-of-attack are needed, one or two cards are needed respectively. The roll and Mach number arrays may vary from two to eight. As an example consider the array CCA where the value of  $C_A$  depends on five roll angles ( $\phi_i$ ), eleven angles-of-attack ( $\alpha$ ) and seven Mach numbers (AM). The array PPHIE would be read in on one card containing five distinct roll angles, the last three fields of ten digits would be blanks. The array AALPFE would be read in on two cards. The first card would contain eight distinct angles-of-attack, and the second card would contain three distinct angles-of-attack and five blank fields of ten digits. The array AAM would be read in on one card containing seven distinct Mach numbers and one blank field of ten digits. The first element in each of the above arrays should start at zero and increase numerically until it is highest

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possible value expected to be encountered is specified. In this particular example, the array size used will be CCA(5, 16, 7). The proper read sequence is to first read two cards containing the values of  $C_A$  at eleven angle -of-attack, the initial roll angle (zero) and the initial Mach number (zero). These cards are followed by two cards containing values of  $C_A$  at eleven angles-of-attack, the second roll angle and the initial Mach number. This is continued for five roll angles at the initial Mach number. After these ten cards, the same procedure is followed for the second Mach number, and the third, etc. up to seven sets of ten cards.

All the aerodynamic coefficient arrays are read similarly. However, notice that the angle-of-attack array associated with the moment coefficients is different than that associated with the force coefficients. Also, the damping moment coefficient arrays (input items "p", "q", and "r") may not be read in at all, depending on the value of OPDA. Instead, input item "l" can be used if the damping coefficients are constant. Finally, the damping coefficients correspond to the arrays read in input items "m", "n", and "o".

Figure 4 helps to clarify the meaning of the input parameters associated with the added air mass on the parachute (Ref. Input Item ff).

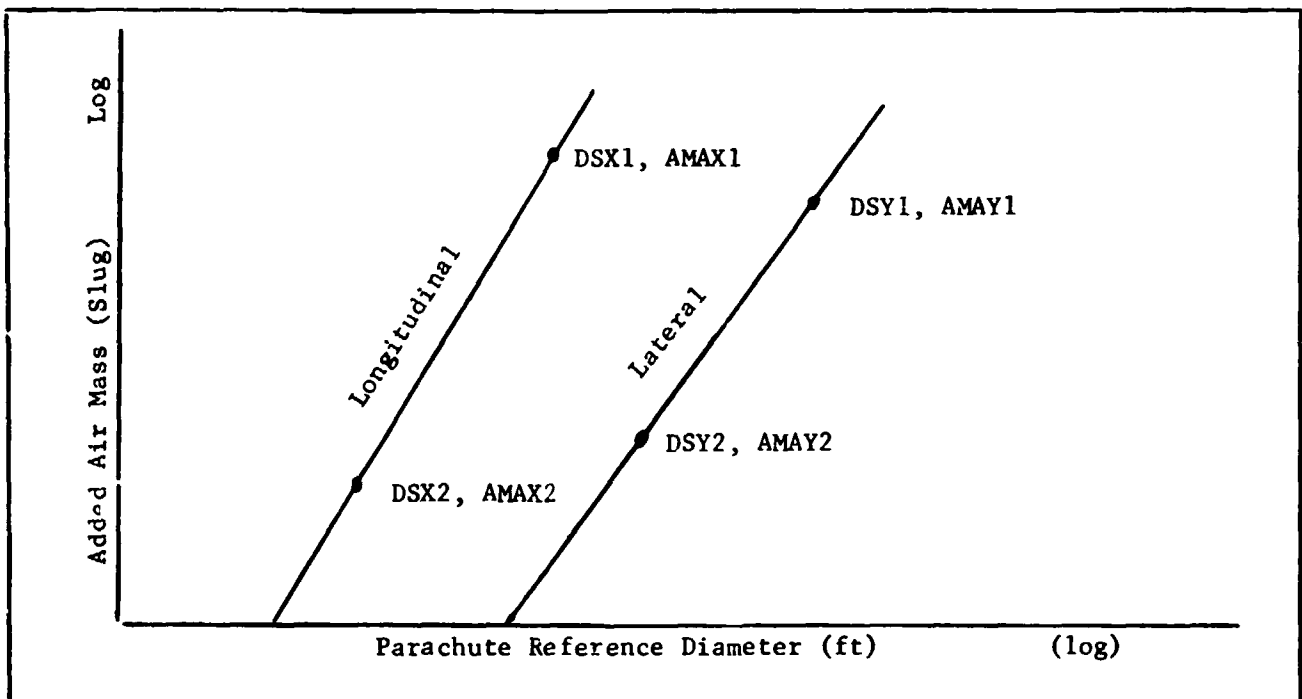


Figure 4. Input Parameters for Parachute Added Air Mass

Figure 5 helps to clarify the meaning of the parameters associated with OPSO = 1.0 which directs the program to calculate the parachute area time history as time advances (Reference Input Items hh and jj).

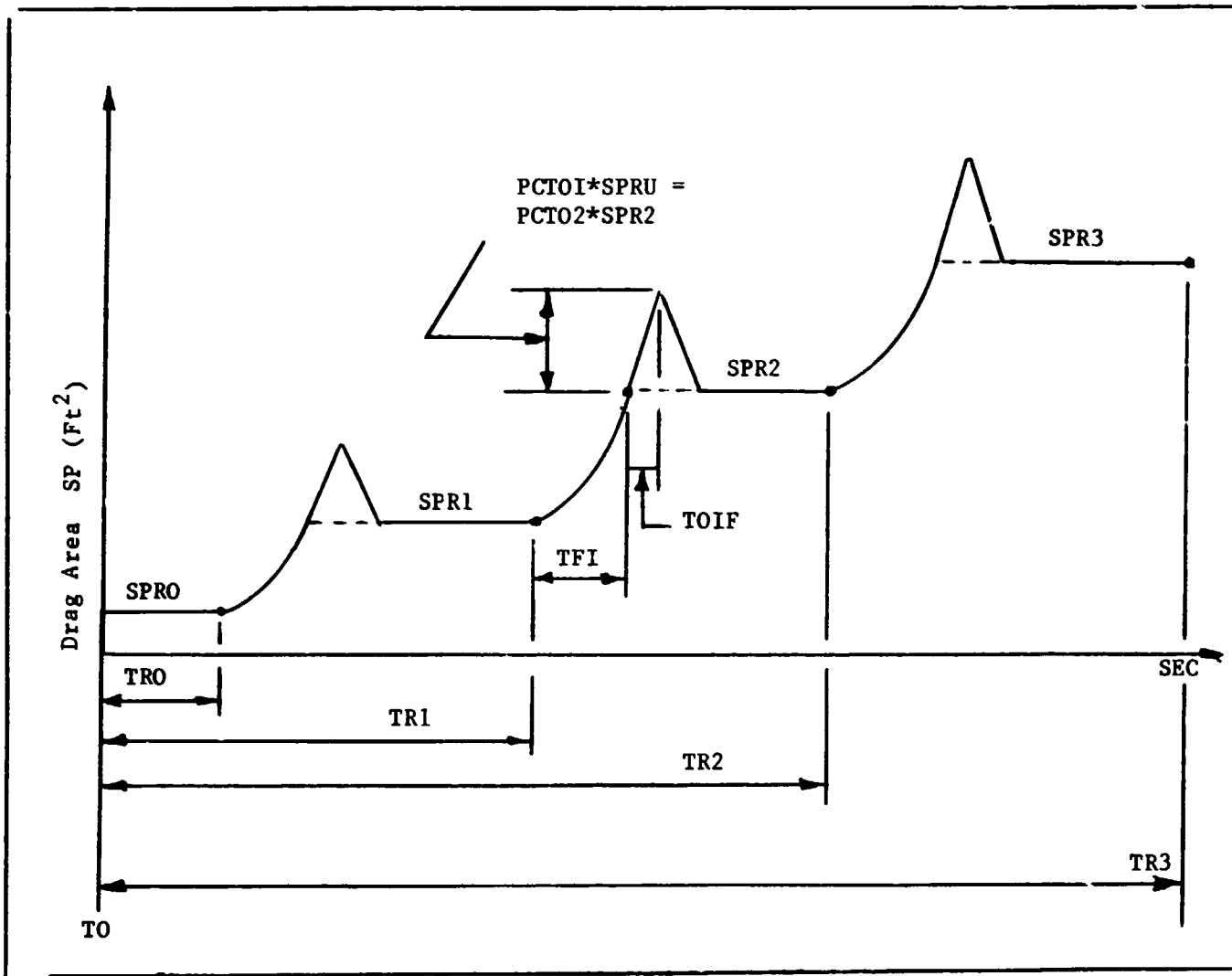


Figure 5. Parameters for Program Calculated Parachute Drag Area Time History

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SECTION 3 - OUTPUT

All output variables are defined in the nomenclature. Before beginning the simulation, the following variables, specifying the characteristics of the rigid body and initial parameters, are printed out.

Line 1. COM  
 Line 2. IXB, IXYB, XBAR, S, CLIP, OPPRIN, OPSYM, AIPHI, AIPHID, DT1 EPSI  
 Line 3. IYB, IXZB, YBAR, D, CLMQ, OPPLLOT, OPDA, AJALPF, AJALPM, AJALPD,  
 TTT, ETA1  
 Line 4. IZB, IYZB, ZBAR, WT, CLNR, OPOS, OMETRC, AKAM, AKAMD, HHH

If CLLP, CLMQ, and CLNR are constants for the simulation, their values are printed out in the appropriate place. If the damping coefficients are found from interpolation of three dimensional arrays, CLLP, CLMQ, and CLNR are set equal to zero for this printout only. Several variables dealing with the decelerator are then printed out.

Line 5. A, LTO, LS, AMAX1, AMAX2, AMAY1, AMAY2, AP, GLOAD, FREQP, OPAM,  
 PCTO1  
 Line 6. B, NT, NS, DSK1, DSK2, DSY1, DSY2, CHIPE, FSULT, POROS, OPDT,  
 PCTO2  
 Line 7. C, DLTO, DP, WTC, WTL, WTP, CCRIT, VP, AERATO, TO OPSO, PCTO3  
 Line 8. TRO, TR1, TR2, TR3, SPRO, SPR1, SPR2, SPR3

The parachute suspension line load and strain arrays are printed out next on Lines 9 and 10.

Line 9. PS(I)  
 Line 10. EPL(I)

The tether line load and strain arrays are printed out next on Lines 11 and 12.

Line 11. PT(I)  
 Line 12. EPT(I)

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The parachute inflation time history array and drag area array are printed out next. If the option (OPSP = 1.0) the arrays are set equal to zero because they are not known before initial time T0.

Line 13. TTIP(I)

Line 14. SSP(I)

The computer program then checks the option variable OPPRIN. If OPPRIN = 1., all the aerodynamic data is listed as follows:

PPHIE(I)  
AALPFE(J)  
AALPME(J)  
AAM(K)  
  
CCA(I,J,K)  
CCN(I,J,K)  
CCLM(I,J,K)

If OPSYM = 0., the following aerodynamic data is listed

CCY(I,J,K)  
CCLL(I,J,K)  
CCLN(I,J,K)

In the above aerodynamic coefficient arrays, AALPFE(J) is associated with CCA, CCN, and CCY; AALPME(J) is associated with CCLM, CCLL, and CCLN.

If OPDA = 1., the damping aerodynamics is listed.

PPHIDE(I)  
AALPDE(J)  
AAMD(K)  
  
CCLLP(I,J,K)  
CCLMQ(I,J,K)  
CCLNR(I,J,K)

E-ID-15(7-71)  
REF: EOI 380

The aerodynamic arrays associated with the decelerator then follow.

AALPPE(I)

AAMP(I)

CCAP(I)

CCNP(I)

CCMP(I)

After the listing of the input data, the computer program begins numerically integrating. At  $T = T_0$  and at predetermined time increments, the following data is printed out.

Line 1. T, X, XD, XDD, FX, CA, V, TENS, XP, XPD, XPDD, FXP, CDAP, CMP  
 Line 2. TXB, Y, YD, YDD, FY, CN, AM, LT, YP, YPD, YPDD, FYP, CNP, AMP  
 Line 3. TYB, Z, ZD, ZDD, FZ, CY, DYPR, TPD, ZP, ZPD, ZPDD, FZP, TYPB, DYPRP  
 Line 4. TZB, PSIE, PSIDE, PSIDDE, QPSI, CLN, ALPE, OMXBE, PSIPE, PSIPDE,  
 PSPDDE, QPSIP, TZPB, ALPPE  
 Line 5. GAME, THEE, THEDE, THEDDE, QTHE, CLM, PHIE, OMYBE, THEPE,  
 THEPDE, THPDDE, QTHEP, TPDXB, GAMPE  
 Line 6. CHIE, PHIE, PHIDE, PHLDDDE, QPHI, CLL, PHIAE, OMZBE, KS, CLLP,  
 CLMQ, CLNR, TYPDRB, PULAN  
 Line 7. MPAL, MPAS, DMD, QMAXPB, IXPB, IYPB, SPD, SP, SPRU, SPRL, TINT,  
 TNINY, TFI, XPBDI

When the simulation reaches HHH or TTT, the computer will write out "RUN ENDED BY CONSTRAINTS". It will then attempt to read in more data cards, to initialize for another simulation, starting with input item "y". If there are no data cards available, the program will CALL EXIT.

SECTION 4 - NUMERICAL SOLUTION

For the most general type rigid body, there are six second order differential equations, coupled in the acceleration terms. These six equations can be written as:

$$\sum_{i=1}^6 D_{ij} \ddot{U}_i = v_j \quad j = 1, 2, \dots, 6 \quad (153)$$

and solved simultaneously using the PIVERT subroutine. PIVERT uses Gauss elimination with complete pivoting to obtain the largest diagonal elements. After solving for the accelerations ( $\ddot{U}_i$  in equation (153)), the results are numerically integrated using Runge-Kutta, fourth order techniques<sup>(3)</sup>.

If the forebody has the properties that  $\bar{X} = \bar{Y} = \bar{Z} = I_{xyb} = I_{xzb} = I_{yzb} = 0.$ , the equations of motion greatly simplify for the forebody. In the case of integrating the Euler angles, three equations remain coupled in the acceleration terms, and are separated using PIVERT. The three translational accelerations are already in a suitable form to integrate immediately. A simpler situation occurs if the added masses of the decelerator are neglected. All five equations of motion are uncoupled in the second derivative and are easily integrated by 4th order Runge-Kutta.



SECTION 5 - PLOTTING ROUTINE

If OPLOT = 1., eleven variables are saved in arrays. At the end of the simulation, any or all of these variables are plotted by calling PLTRAJ and setting the appropriate arguments. PLTRAJ was originally written for use on a CALCOMP 563 plotter and 750 tape drive. It has been modified for use at M.S.F.C. where a SC 4020 plotter is the preferred plotter. The original PLTRAJ will plot up to 4 variables versus time on one graph for each call to PLTRAJ. The modified PLTRAJ for the SC 4020 plotter plots only one variable versus time per plot; therefore four plots will be made instead of one for each call to PLTRAJ. Two hundred data points are plotted on each graph per variable.

SECTION 6 - ENGLISH TO METRIC CONVERSION

The computer program operates in either English or Metric units. The program input and output is in English units unless the option parameter, OMETRC, is set equal to 1. If OMETRC = 1. the input and output is in the Metric System. A conversion table from English to Metric is given below for commonly used engineering parameters.

ENGLISH TO METRIC CONVERSION

REFERENCE NASA SP 7012

\*EXACT

FORCE	(LB) X 4.4482216152605* = (1) NEWTON	N
LENGTH	(FT) X .30480060 * = (1) METER	m
MASS	(SLUG) X 14.5939029 = (1) KILOGRAM	kg
SPEED	(FT/SEC) X .3048 = (1) METERS SEC	m/sec
PRESSURE	(LB/FT <sup>2</sup> ) X 47.880258 = (1) NEWTON/METER <sup>2</sup>	N/m <sup>2</sup>
volume	(FT <sup>3</sup> ) x .028316846592* = METERS <sup>3</sup>	m <sup>3</sup>
AREA	(FT <sup>2</sup> ) X .09290304* = METERS <sup>2</sup>	m <sup>2</sup>
ACCELERATION	(FT/SEC <sup>2</sup> ) X .3048* = METER/SEC <sup>2</sup>	m/sec <sup>2</sup>
INERTIA	(SLUG-FT <sup>2</sup> ) X 1.355817945= KILOGRAM-METER <sup>2</sup>	kg-m <sup>2</sup>
TORQUE	(FT-LB) X 1.355817948 = METER - NEWTON	m-N
DENSITY	(SLUG/FT <sup>3</sup> ) X 515.379 = KILOGRAM/METER <sup>3</sup>	kg/m <sup>3</sup>
viscosity	(SIUG/FT-SEC) X 47.880258 = NEWTON SEC/METER <sup>2</sup>	(N-sec)/m <sup>2</sup>
SPRING CONSTANT	(LB/FT) X 14.59390293 = NEWTON/METER	N/m

\* Exact Numbers - No round offs

SECTION 7 - CONCLUSIONS AND RECOMMENDATIONS

The following conclusions and recommendations are made for use of the 6+5 D.O.F. computer program.

1. The (6+5) DOF loads assessment computer program should be used primarily to analyze the loads induced on a wobbling or spinning body when the body is stabilized by the deployment of a drogue parachute.
2. After the body has been stabilized by the drogue, further parachute deployments (main chutes) should be analyzed using the planar (3+3) DOF computer program. The (3+3) program should be used because of the following reasons:
  - a. The (3+3) program is faster and easier to use than the (6+5) program.
  - b. Terminal descent with the forebody pitch angle equal to  $\pm 90^\circ$  presents no mathematical solution problem using the (3+3) DOF program.
3. It should be noted here that the (6+5) DOF program has a mathematical singularity point at a forebody pitch angle of  $\pm 90^\circ$ . To permit passage through this point the six forebody accelerations are frozen at their last value when the pitch angle is in the region of  $89.8^\circ < \theta < 90.2^\circ$ . This induces some error in the translational coordinates and attitude of the forebody, but it has been shown to be small for normal velocity passes through this point. A time count (TNINY) for the time spent in this region is a program output.

CHAPTER IV - PROGRAM LISTING AND SAMPLE COMPUTER RUN

The following program listing is for the Univac 1108 at M.S.F.C. and adapted from the IBM 360 listing used by Goodyear Aerospace Corporation.

The sample problem, SRB Stabilization by 54' Drogue Parachute, represents the deployment of a 54' drogue from a SRB which is wobbling and flying broadside to the wind vector. The trajectory of the SRB is nearly vertical. The drogue is starting to inflate and is stretched out normal to the SRB centerline. The drogue has one stage of reefing (0.82 of full open area).

Some of the more important initial conditions are given in the table below.

Altitude	Ft	19,000.
Velocity	Ft/Sec	553.
Angle of Attack	Deg.	90.
Flight Path Angle	Deg.	- 85.
Body Axis Rates		
Pitch	Deg/Sec	- 1.0
Yaw	Deg/Sec	0.0
Roll	Deg/Sec	0.0

The output from the sample problem starts on Page 57, and selected portions of the trajectory are found starting on page 107.

E-ID-1517 71)  
REF: EOI 38C



```

00110 9 WICM,WLTM,CCRIT,LS,NS,NT,TO,TRD,TKI,THZ,TH3,SPRO,SPKI,SPR2,SPR3
00111 A ,PCTO1,PCTO2,PCTO3,POROS,LOAD,FSULT,ALNATO,FREQP,XPBDM,DTI
00112 B ,SPNU,SPRL,TINT,TINF,TFL,XPBD1,TCROU,TCRI,TOH2,TOIR3,OPSP,TMINY
00113 I FORMAT(10,0)
00114 Z FORMAT(13A6,A2)
00115 50 FORMAT(11I,5X,TIME,5X,X,8A,XD,7A,XUD,6X,FX,7X,CA,7X,
00116 'V,AX,TEMS,5X,AP,7X,XPB,6X,XPDD,5X,FXP,6X,CDAP,5X,
00117 2'CP,
00118 '6X,TXB,6X,Y,6X,YD,7A,YDD,6X,YFY,7X,CN,7X,AM,7X,LT,
00119 '7X,YP,7A,YP,6X,YPD,5X,FPY,6X,CNP,6X,AMP,
00120 56X,ITYB,6X,Z,8A,ZD,7X,ZDD,6X,FZ,7X,CY,7X,ODYPR,5X,
00121 6'TPD,6X,7P,7X,2PD,6X,2PDD,5X,FPZ,6X,TPB,5X,DPMP,
00122 76X,TZB,6X,PSIE,5X,PSIOE,4X,PSIOO,3A,OPSI,5A,CLM,6X,
00123 8'ALPE,5A,OMXBE,4X,PSIPE,4X,PSIPE,3X,PSPODE,3X,UPSIP,
00124 9'X,TPB,5X,ALPPE,
00125 AX,GAME,5X,THEE,5X,THEDE,4X,THEDE,3X,OTHE,5X,CLM,6X,
00126 0'PHIE,4X,OMYBE,4X,THEPE,4X,THEPOL,3A,TPODE,3X,OTHEP,
00127 CX,TPDXB,4X,GAMPE,
00128 0AX,CHIE,5X,PHIE,5X,PHIOE,4X,PHIOE,3X,OPHI,5X,CLL,6X,
00129 E'PHIAE,4X,OMZBE,4X,KS,7X,CLLP,5X,CLMQ,5X,CLMR,
00130 F 5X,TPORB,4X,PULAN,6X,MPAL,5X,MPAS,5X,DMD,6X,QMAAPB,
00131 G 3X,IXPB,5X,IYPB,5X,SPD,6X,SP,7X,SPRU,5X,SPRL,5A,
00132 H 'TINT,4X,TNINY,5X,TFI,6X,XPB01,
00133 51 FORMAT(3X,F9.4,F9.0,2F9.3,F9.0,F9.3,F9.2,2F9.0,2F9.0,F9.3,
00134 1F9.3/
00135 23X,2F9.0,2F9.3,F9.0,3F9.3,F9.0,2F9.2,F9.0,2F9.3/
00136 33X,2F9.0,2F9.3,F9.0,F9.3,F9.2,2F9.0,2F9.2,2F9.0,F9.2/
00137 43X,F9.0,3F9.3,F9.0,6F9.3,2F9.0,F9.3/
00138 53X,4F9.3,F9.0,6F9.3,F9.0,F9.0,F9.3/
00139 6 3X,4F9.3,F9.0,3F9.3,F9.0,3F9.3,2F9.0/
00140 7 3X,2F9.1,F9.2,4F9.1,3F9.2,3F9.5,F9.2/
00141 C
00142 C ALPHA IS THE NO. OF ELEMENTS IN PPHIE ARRAY (2. TO 8.)
00143 C ALPHAID IS THE NO. OF ELEMENTS IN PPHIDE ARRAY (2. TO 8.)
00144 C AJALPF IS THE NO. OF ELEMENTS IN AALPFE ARRAY (8. OR 16.)
00145 C AJALPM IS THE NO. OF ELEMENTS IN AALPME ARRAY (8. OR 16.)
00146 C AKAM IS THE NO. OF ELEMENTS IN THE AAM ARRAY (2. TO 8.)
00147 C AKAMD IS THE NO. OF ELEMENTS IN THE AAMD ARRAY (2. TO 8.)
00148 C
00149 C OPSYM EQUAL 1. IF BODY IS SYMMETRIC SUCH THAT CY=CELL=CLM=0.
00150 C OPSYM EQUAL 0. IF BODY IS NOT SYMMETRIC
00151 C
00152 C OPDA EQUAL 1. TO READ AMPING COEFFICIENTS AS A FUNCTION OF
00153 C ROLL ANGLE, ANGLE-OF-ATTACK, AND MACH NUMBER
00154 C OPDA EQUAL 0. TO READ AMPING COEFFICIENTS AS CONSTANTS
00155 C
00156 CALL PHARG(1,66,1,4,1,2,1)
00157 IIN = 5
00158 IOUT = 6
00159 IUSED = 0
00160 READ(IIN,1) ALPHA,ALPHAID,AJALPF,AJALPM,AKAM,AKAM,OPSYM,OPDA
00161 IPHI=ALPHI
00162 IPHID=ALPHID
00163 JALPF=AJALPF
00164 JALPM=AJALPM
00165 AJALP=0.
00166
00167
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00446 1400
00457 1410
00465 1420
00477 1430
00510 1440
00527 1450
00532 1460
00541 1470
00552 1480
00563 1490
00575 1500
00603 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00603 1510 IF(OPSP.EQ.O) GO TO 91
00605 1520 READ(IIN,1)TRC,TRI,TR2,TR3
00613 1530 READ(IIN,1)SPRO,SPRI,SPR2,SPR3,PCT01,PCT02,PCT03,POR05
00625 1540 DO 64 I=1,16
00630 1550 TTIP(I)=0.0
00631 1560 SSP(I)=0.0
00633 1570 CONTINUE
00634 1580 GO TO 92
00635 1590 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00641 1600 READ(IIN,1) TTIP,SSP
00642 1610 TR0=0.0
00643 1620 TRI=0.0
00644 1630 TR2=0.0
00645 1640 TR3=0.0
00646 1650 SPR1=0.0
00647 1660 SPR2=0.0
00650 1670 SPR3=0.0
00651 1680 PCT01=0.0
00652 1690 PCT02=0.0
00653 1700 PCT03=0.0
00654 1710 POR05=0.0
00655 1720 CONTINUE
00656 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00656 1730 IF(OPDT.EQ.O) GO TO 93
00660 1740 READ(IIN,1)GLOAD,FSULT,4ERATO,TO,DTPI,TTT,MMH
00671 1750 GO TO 94
00672 1760 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00701 1770 READ(IIN,1)DTI,TO,DP1,TTT,MMH
00702 1780 GLOAD=0.0
00703 1790 FSULT=0.0
00704 1800 4ERATO=0.0
00705 1810 CONTINUE
00710 1820 READ(IIN,2)COM
00711 1830 N=0
00712 1840 WTP= WTL+ WTC
00713 1850 T = TO
00714 1860 TOTR0= TO+TRC
00715 1870 TOTR1= TO+TRI
00716 1880 TOTR2= TO+TR2
00716 1890 TOTR3= TO+TR3
00716 1900 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00717 1910 IF(OPDT.EQ.1) GO TO 60
00721 1920 GO TO 63

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0722 1930 60 DTT=.04735*SQR((LS*WTP)/(GLOAD*WTSULT*AERATO))
0723 1940 FREQP=1./(112.*DTT)
0724 1950 YY=DTT
0725 1960 I=0
0726 1970 NN=YY
0727 1980 IF(NN.GE.1) GO TO 62
0731 1990 I=I+1
0732 2000 YY=YY*10.
0733 2010 GO TO 61
0734 2020 DT1=NN/10.**1
0735 2030 63 CONTINUE
0736 2040 GO=32.*17
0737 2050 RHO0=.002378
0740 2060 ME=.0926435.
0741 2070 *DIAGNOSTIC. THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
0743 2080 IF(OMTRC.EQ.1.) GO TO 140
0744 2090 GO TO 141
0745 2100 RE=6378377.
0746 2110 RHO0=.22557
0747 2120 GO=9.8054160
0750 2130 DPR=57.2957795
0751 2140 M=WT/GO
0752 2150 MP=WTP/GO
0753 2160 WTCM= WTC/32.17
0754 2170 WTLM= WTL/32.17
0755 2180 LSCLO= SQR((LS*LS-.10176*DP*DP)
0756 2190 AP= (WTC*(.1595*DP+LSCLO)+.5*LSCLO*WTL)/(WTC+WTL)
0757 2200 AX= (ALOG10(AMAX1))-ALOG10(AMAX2))/(ALOG10(DSX1))-ALOG10(DSX2))
0760 2210 AY= (ALOG10(AMAY1))-ALOG10(AMAY2))/(ALOG10(DSY1))-ALOG10(DSY2))
0761 2220 BY= AMAY1/(DSY1*AY)
0762 2230 PSI=PSIE/DPR
0763 2240 THE=THEE/DPR
0765 2250 PHI=PHIE/DPK
0766 2260 PSIP=PSIPE/DPR
0767 2270 THEP=THEPE/DPK
0770 2280 OMXB=OMXBE/DPK
0771 2290 OMYB=OMYBE/DPR
0772 2300 O'ZB=O'ZBE/DPR
0773 2310 THEPD=THEPOE/DPR
0774 2320 PSIPD=PSIPOE/DPR
0775 2330 GAM=GAME/DPR
0776 2340 CHI=CHIE/DPR
0777 2350 GAMP=GAMPE/DPR
0780 2360 CHIP=CHIPE/DPR
0781 2370 SGAM=SGAM(GAM)
0782 2380 CGAM=CGAM(GAM)
0783 2390 SCHI=SCHIE(CHI)
0784 2400 CCMI=CCOS(CHI)
0785 2410 SGAMP=SGAMP(GAMP)
0786 2420 CGAMP=CGAMP(GAMP)
0787 2430 SCHIP=SCHIP(CHIP)
0788 2440 CCPIP=CCOS(CHIP)
0789 2450 XD=V*CGAM*CHI
0790 2460 YD=V*CGAM*SCHI
0791 2470 ZD=V*SGAM

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01013 2480 XPD=VPCGAMP*CCHIP
01014 2490 YPD=VPCGAMP*SCHIP
01015 2500 ZPD=VPC*SGAMP
01016 2510 SPSI=SIN(SNGL(PSI))
01017 2520 STHE=SIN(SNGL(THE))
01020 2530 SPHI=SIN(SNGL(PHI))
01021 2540 SPSTP=SIN(SNGL(PSIP))
01022 2550 STHEP=SIN(SNGL(THEP))
01023 2560 CPSI=COS(SNGL(PSI))
01024 2570 CTHE=COS(SNGL(THE))
01025 2580 CPHI=COS(SNGL(PHI))
01026 2590 CPSIP=COS(SNGL(PSIP))
01027 2600 CTHEP=COS(SNGL(THEP))
01030 2610 CC(1,1)=CPSI*CTHE
01031 2620 CC(1,2)=-SPSI*CTHE
01032 2630 CC(1,3)=STHE
01033 2640 CC(2,1)=-CPSI*STHE*SPHI+SPSI*CPHI
01034 2650 CC(2,2)=SPSI*STHE*SPHI+CPSI*CPHI
01035 2660 CC(2,3)=CTHE*SPHI
01036 2670 CC(3,1)=-CPSI*STHE*CPHI-SPSI*SPHI
01037 2680 CC(3,2)=SPSI*STHE*CPHI-CPSI*SPHI
01040 2690 CC(3,3)=CTHE*CPHI
01041 2700 CCP(1,1)=CPSI*CTHEP
01042 2710 CCP(1,2)=-SPSI*CTHEP
01043 2720 CCP(1,3)=STHEP
01044 2730 XP=X+A*CC(1,1)+B*CC(2,1)+C*CC(3,1)-(LTO*DLTO*AP)*CCP(1,1)
01045 2740 YP=Y+A*CC(1,2)+B*CC(2,2)+C*CC(3,2)-(LTO*DLTO*AP)*CCP(1,2)
01046 2750 ZP=Z+A*CC(1,3)+B*CC(2,3)+C*CC(3,3)-(LTO*DLTO*AP)*CCP(1,3)
01047 2760 PSTO=-L*ONYB*SPHI+OMZB*CPHI//CTHE
01050 2770 THED=-L*ONYB*CPHI+OMZB*SPHI
01051 2780 PHID=OMXB*STHE+ONYB*SPHI+OMZB*CPHI//CTHE
01052 2790 DT=DTI
01053 2800 TNJNY=0*0
01054 2810 DTP=DTPI
01055 2820 IYH2B=IYB-12B
01056 2830 DTPC=0.
01057 2840 CONSTR=-1.
01060 2850 JJJ=1
01061 2860 JJ=1
01061 2870
01061 2880
01061 2890
01062 2900
01064 2910
01064 2920
01065 2930
01070 2940
01071 2950
01073 2960
01073 2970
01073 2980
01073 2990
01073 3000
01073 3010
01074 3020
01074 3030

```

C WRITE OUT BODY CHARACTERISTICS AND CONTROL VARIABLES  
C

```

WRITE(10,14)
14 FORMAT(1H,5X,'TRAJECTORY OF A RIGID BODY WITH 6 D.O.F. CONNECTED
1 TO A RIGID PARACHUTE WITH 5 D.O.F. BY AN ELASTIC TETHER',//)
WRITE(10,13) COM
31 FORMAT(23X,13A6,A2//)
WRITE(10,11)
11 FORMAT(7X,1XB,7X,1YB,8X,1XBAR,6X,1S,9X,1CLLP,6X,1OPPRIN,
14X,1OPSYM,5X,1ALPHI,15X,1ALPHID,4X,1DTI,7X,1EPSI,7
27X,1YB,7X,1X2B,8X,1YBAR,6X,1D,9X,1CLM,6X,1OPLOT,4A,
3*OPDA,6X,1AJALPF,4X,1AJALPH,4X,1AJALPD,4X,1TTT,7X,1ETA1,7
47X,1I2B,7X,1Y2B,8X,1ZBAR,6X,1WEIGHT,4X,1CLNR,6X,1OPUS,6X,
5*OMETPC,4X,1AKAM,16X,1AKAMD,5X,1MHM,7)
WRITE(10,13) 1XB,1YB,1XBAR,5,1CLLP,1OPPHIN,1OPSYM,1ALPHI,1ALPHID,DTI,
1EPSI,1YB,1X2B,1YBAR,1D,1CLM,1OPLOT,1OPDA,1AJALPF,1AJALPH,1AJALPD,1TTT,

```

```
01074 ZETAJ,I,ZL :YEB,ZBAN,WT,CLNR,OPOS,OMETRC,AKAM,AKAMD,MHM
01137 13 FORMAT(2X,F10.1,2X,F10.1,3F10.3,4X,3IF4.0,6X)10X,F4.0,2X,F10.4,
01137 IF10.6/2X,F10.1,2X,F10.1,3F10.3,4X,4IF4.0,6X)10X,F4.0,2X,F10.4,3F10.6/
01137 22X,F10.1,2X,F10.1,3F10.3,4X,F4.0,6X,F4.0,6X,F4.0,6X,F4.0
01137 316X,F4.0,2X,F10.1)
01140 WRITE(IOUT,18)
01142 18 FORMAT(///,6X,'A',9X,'LTO',7X,'LS',6X,'AMAX1',5X,'AMAX2',5X,
01142 '1'AMAY1',5X,'AMAY2',2X,'AP',5X,'GLOAD',5X,'FNEW',6X,'UPAM',
01142 'A',6X,'PTOT',/)
01142 2 10X,'NT',7X,'MS',7X,'DSX1',6X,'DSX2',6X,'DSY1',6X,
01142 3 10X,'CHIPE',5X,'FSULT',5X,'OROS',6X,'OPDI',5X,'PCTO2',/
01142 4 10X,'3X,'DLTO',7X,'DP',8X,'MTC',7X,'MTL',7X,'MTP',5X,'CCRIT',/
01142 5 10X,'TRD',7X,'TR1',7X,'TR2',7X,'TR3',6X,'SPR0',6X,'SPR1',6X,
01142 6 'SPR2',6X,'SPR3',/)
01142 WRITE(IOUT,19) A,LTO,LS,AMAX1,AMAX2,AMAY1,AMAY2,AP,
01143 1 GLOAD,FRECP,UPAM,PC OI,R,NT,NS,DSX1,DSX2,DSY1,DSY2,CHIPE,FSULT,
01143 2 POROS,CPDT,PCTO2,C,DLTO,DP,MTC,MTL,MTP,CCRIT,VP,AERATO,TD,UPSP,
01143 3 PCTO3,TRD,TR1,TR2,TR3,SPRO,SPR1,SPR2,SPR3
01143 19 FORMAT(6X,12F10.3/6X,12F10.3/6X,12F10.3/6X,12F10.3/
01142 WRITE(IOUT,2) PS,EPL,PT,EPT
01142 12 FORMAT(//,5X,'PARACHUTE SUSPENSION LINE LOAD AND STRAIN ARRAYS'
01142 1// 9X,'PS(8)',2X,8F10.2/8X,'EPL(8)',1X,8F10.4//
01142 2 15X,'TETHER LINE LOAD AND STRAIN ARRAYS',/9X,'PT(8)',2X,
01142 3 8F10.2/8X,'EPT(8)',1X,8F10.4//)
01142 WRITE(IOUT,21) TTIP,SSP
01142 21 FORMAT(//,20X,'PARACHUTE INFLATION TIME HISTORY ARRAY,TTIP',//
01142 1 2X,16.8,4//,20X,'PARACHUTE AERODYNAMIC REF. AREA ARRAY, SSP',//
01142 2 2X,16.8,1//)
C
01142 C
01142 C
01142 C
01142 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01142 IF(OPPRIN,EG,2.) GO TO 46
01142 WRITE(IOUT,15)
01142 15 FORMAT(11I30,' AERODYNAMIC COEFFICIENTS OF FOREBODY',/)
01142 WRITE(IOUT,5)
01142 5 FORMAT(10X,'PHIE (R LL ANGLE-DEGREES)',/)
01142 WRITE(IOUT,10) (PPHIE(I),I=1,1PHI)
01142 WRITE(IOUT,4)
01142 4 FORMAT(10X,'AALPFE (ANGLE OF ATTACK-DEGREES)',/)
01142 WRITE(IOUT,10) (AALPFE(J),J=1,JALPFF)
01142 10 FORMAT(1X,16F8.3/)
01142 WRITE(IOUT,7)
01142 7 FORMAT(10X,'AALPME (ANGLE OF ATTACK-DEGREES)',/)
01142 WRITE(IOUT,10) (AALPME(J),J=1,JALPHE)
01142 WRITE(IOUT,6)
01142 6 FORMAT(10X,'AAM (MACH NUMBER)',/)
01142 WRITE(IOUT,10) (AAM(K),K=1,KAM)
01142 40 40 K=1,KAM
01142 WRITE(IOUT,14)
01142 14 FORMAT(///,40X,'CA (AXIAL COEF. ARRAY (PHI),JALPFF,'AMI)',/)
01142 WRITE(IOUT,1) (AAM(K))
01142 17 FORMAT(40X,'MACH NO. ',F6.3//)
01142 40 40 I=1,1PHI
01142 90 WRITE(IOUT,10) (CCA(I,J,K),J=1,JALPFF)
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01335 3590 DO 41 K=1,KAM
01340 3600 WRITE(10UT,20)
01342 3610 20 FORMAT(//,40X,'CN (NORMAL COEF. ARRAY(IPHI,JALPF,KAM))')
01343 3620 WRITE(10UT,17) AAM(K)
01344 3630 DO 41 I=1,IPHI
01351 3640 41 WRITE(10UT,10) (CCN(I,J,K),J=1,JALPF)
01361 3650 DO 44 K=1,KAM
01364 3660 WRITE(10UT,26)
01367 3670 26 FORMAT(//,40X,'CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))')
01372 3680 WRITE(10UT,17) AAM(K)
01375 3690 DO 44 I=1,IPHI
01375 3700 44 WRITE(10UT,10) (CCLM(I,J,K),J=1,JALPM)
01405 3710 *DIAGNOSTIC*
01405 3710 THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01407 3720 IF(OPSYM.EQ.1.) GO TO 95
01412 3730 DO 42 K=1,KAM
01412 3730 WRITE(10UT,22)
01414 3740 22 FORMAT(//,40X,'CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))')
01415 3750 WRITE(10UT,17) AAM(K)
01420 3760 DO 42 I=1,IPHI
01423 3770 42 WRITE(10UT,10) (CCY(I,J,K),J=1,JALPF)
01433 3780 DO 43 K=1,KAM
01436 3790 WRITE(10UT,24)
01440 3800 24 FORMAT(//,40X,'CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))')
01441 3810 WRITE(10UT,17) AAM(K)
01444 3820 DO 43 I=1,IPHI
01447 3830 43 WRITE(10UT,10) (CCLL(I,J,K),J=1,JALPM)
01457 3840 DO 45 K=1,KAM
01462 3850 WRITE(10UT,28)
01464 3860 25 FORMAT(//,40X,'CLN (YAW MOM. COEF. ARRAY(IPHI,JALPM,KAM))')
01465 3870 WRITE(10UT,17) AAM(K)
01470 3880 DO 45 I=1,IPHI
01473 3890 45 WRITE(10UT,10) (CCLN(I,J,K),J=1,JALPM)
01503 3900 *DIAGNOSTIC*
01503 3900 THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01504 3910 IF(OPDA.EQ.1.) GO TO 39
01506 3920 GO TO 38
01507 3930 39 CONTINUE
01510 3940 WRITE(10UT,8)
01512 3950 8 FORMAT(1H,10X,'PPHIDE (ROLL ANGLE-DEGREES)')
01513 3960 WRITE(10UT,10) (PPHIDE(I),I=1,IPHID)
01521 3970 WRITE(10UT,9)
01523 3980 9 FORMAT(//,10X,'AALPDE (ANGLE OF ATTACK-DEGREES)')
01524 3990 WRITE(10UT,10) (AALPDE(J),J=1,JALPD)
01532 4000 WRITE(10UT,65)
01534 4010 65 FORMAT(//,10X,'AAMD (MACH NUMBER)')
01535 4020 WRITE(10UT,10) (AAMD(K),K=1,KAMD)
01543 4030 DO 47 K=1,KAMD
01544 4040 WRITE(10UT,30)
01550 4050 30 FORMAT(//,30X,'CLF (ROLL DAMPING MOM. COEF. ARRAY(IPHID,JALPD,KA
01550 4060 IMD))')
01551 4070 WRITE(10UT,17) AAMD(K)
01554 4080 DO 47 I=1,IPHID
01557 4090 47 WRITE(10UT,34) (CCLF(I,J,K),J=1,JALPD)
01567 4100 34 FORMAT(1X,8F15.3/)
01570 4110 DO 48 K=1,KAMD
01573 4120 WRITE(10UT,33)

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01575 4130
01576 4140
01577 4150
01601 4160
01604 4170
01614 4180
01617 4190
01621 4200
01621 4210
01622 4220
01625 4230
01630 4240
01640 4250
01642 4260
01643 4270
01652 4280
01652 4290
01652 4300
01652 4310
01652 4320
01653 4330
01654 4340
01656 4350
01660 4360
01662 4370
01664 4380
01665 4390
01667 4400
01670 4410
01671 4420
01673 4430
01675 4440
01675 4450
01675 4460
01675 4470
01676 4480
01677 4490
01700 4500
01701 4510
01702 4520
01703 4530
01704 4540
01705 4550
01706 4560
01707 4570
01710 4580
01711 4590
01712 4600
01713 4610
01714 4620
01715 4630
01716 4640
01717 4650
01720 4660
01721 4670
01722 4680

33 FORMAT(///,30X,CLHQ (PITCH DAMPING MOM. COEF. ARRAY(1PHI),JALPD,K
1AMD))//
WRITE(IOUT,17) AAMD(K)
DO 48 I=1,1PHID
48 WRITE(IOUT,34)(CCLHQ(I),J,K),J=1,JALPD)
DO 49 K=1,KAMD
WRITE(IOUT,32)
32 FORMAT(///,30X,CLNR (YAW DAMPING MOM. COEF. ARRAY(1PHI),JALPD,KAMD
1))//
WRITE(IOUT,17) AAMD(K)
DO 49 I=1,1PHID
49 WRITE(IOUT,34)(CCLNR(I),J,K),J=1,JALPD)
38 WRITE(IOUT,66)
66 FORMAT(///,30X,AE DYNAMICS OF PARACHUTE'////)
WRITE(IOUT,67) AALPPE,AAMP,CCAP,CCNP,CCMP
67 FORMAT(20X,'ANGLE OF ATTACK ARRAY (AALPPE(8))'//,10X,8F10.3//,
A2CX,'MACH NUMBER ARRAY(AAMP(8))'//,10X,8F10.3//,
120X,'AXIAL COEFF. ARRAY (CCAP(8,8))'//,8(10X,8F10.3)////,
220X,'NORMAL COEFF. ARRAY (CCNP(8,8))'//,8(10X,8F10.3)////,
320X,'PITCH MOM. COEFF. ARRAY (CCMP(8,8))'//,8(10X,8F10.3)//)
46 CONTINUE
WRITE(IOUT,50)
100 IF(Z.LT.HHM) CONSTR=0.
IF(T.GT.TT) CONSTR=0.
IF(JJ.EQ.1) GO TO 101
DTPC=DTPC*I.
IF (DTPC.LT.DTP) GO 0 110
JJ=JJJ+1
DTPC=0.
IF(JJJ.LE.6) GO TO 101
WRITE(IOUT,50)
JJJ=1
C CALCULATE AND WRITE OUTPUT
C
C 101 CALL SUBR
PSIE=PSI*OPR
THEE=THE*OPR
PHIE=PHI*OPR
PSIPE=PSIP*OPR
THEPE=THEP*OPR
PSIDE=PSID*OPR
THEDE=THED*OPR
PHIDE=PHID*OPR
PSIPDE=PSIPD*OPR
THEPDE=THEPD*OPR
PSIDDE=EE(1)*OPR
THEDEE=EE(2)*OPR
PHIDDE=EE(3)*OPR
XDD=EE(4)
YDD=EE(5)
ZDD=EE(6)
PSPDDE=FF(1)*OPR
THPDDE=FF(2)*OPR
XPDDE=FF(3)
YPDDE=FF(4)

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01723          ZPDD=FF(5)
01724          CHIE=ATAN2(SNGL(YD), NGL(XD))0PR
01725          GAM=ATAN2(SNGL(ZD), SORT(SNGL(XD002+YD002)))
01726          IF(XD.LT.0.) GAM=3.14159265-GAM
01730          GAMP=ATAN2(SNGL(ZPD), SORT(SNGL(XPD002+YPD002)))
01731          IF(XPD.LT.0.) GAMP=3.14159265-GAMP
01733          GAME=GAM0DPR
01734          ALPPE=ALPP0DPR
01735          GAMPE=GAMP0DPR
01736          OMXBE=OMXB0DPR
01737          OMYBE=OMYB0DPR
01740          OMZBE=OMZB0DPR
01741          CDAP=CAP0SP
01742          VD=SQR(XDD002+YDD002+ZDD002)
01743          VPD=SQR(XPDD002+YPDD002+ZPDD002)
01744          TPD RB=SQR(TP0YB002+TPDZB002)
01745          IF(LT.YT.) GO TO 3
01747          PULAN= ATAN2(TPDRB, TPDAB)0DPR
01750          GO TO 54
01751          53 PULAN= 180.
01752          54 CONTINUE
01753          WRITE(10UT,51)T,X,XD,XDD,FX,CA,V,TENS,XP,XPD,XPDD,FXP,CDAP,CMP,
01753          ITR,Y,YD,YDD,FY,CN,AMLT,YP,YPD,YPDD,FYP,CNP,AMP,
01753          2TYR,Z,ZD,ZDD,FZ,CY,DYPR,TPD,ZP,ZPD,FZP,TPPB,DYPRP,
01753          3TYR,PSIE,PSUE,PSIODE,OPSI,CLN,ALPE,OMXUE,PSIPE,PSIPDE,PSPDUE,
01753          4QPSIP,TZPE,ALPPE,
01753          5GAME,THEE,THEDE,THEDE,OTHE,CLM,PHIIE,OMYBE,THEPE,THEPE,TPPDE,
01753          6OTHEP,TPDXR,GAMPE,
01753          7CHIE,PHIE,PHIDE,PHIDE,OPHI,CLL,PHIAE,OMZBE,KS,CLLP,CLMQ,CLNR
01753          8.TPD RB,PULAN,MPAL,MPAS,DMO,QMAXPB,IYPB,IYB,SPD
01753          9. SP,SPRU,SPRL,TINT,TINY,TFI,XPBD)
02117          JU=2
02117          C SPECIFY VARIABLES FOR LOT TAPE
02117          C
02120          *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
02120          IF (OPPLOT.EQ.0.) GO TO 110
02122          N=NI+1
02123          XA(N)=T
02124          YI(N)=PSIE
02125          Y2(N)=THEE
02126          Y3(N)=PHIE
02127          Y4(N)=ALPE
02130          Y5(N)=Z
02131          Y6(N)=AM
02132          Y7(N)=GAME
02133          Y8(N)=DYPR
02134          Y9(N)=TPD
02135          Y10(N)=ALPPE
02136          5-7 (CONSTRI)11J,111,111
02141          111 WRITE(10UT,52)
02143          52 FORMAT(1/5X,'RUN ENDED BY CONSTRAINTS./)
02144          520 IF (OPPLOT) 99,99,112
02147          521 IF (N.LE.1) GO TO 99
02151          IRET = 0
02152          GO TO 116

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02153 5240
02156 5250
02161 5260
02162 5270
02163 5280
02164 5290
02165 5300
02166 5310
02167 5320
02167 5330
02167 5340
02167 5350
02177 5360
02175 5370
02175 5370
02177 5380
02200 5390
02203 5400
02205 5410
02210 5420
02212 5430
02213 5440
02214 5450
02215 5460
02216 5470
02217 5480
02220 5490
02221 5500
02222 5510
02223 5520
02224 5530
02225 5540
02226 5550
02227 5560
02230 5570
02231 5580
02231 5590
02233 5600
02234 5610
02235 5620
02236 5630
02237 5640
02240 5650
02241 5660
02242 5670
02243 5680
02244 5690
02245 5700
02246 5710
02247 5720
02250 5730
02251 5740
02252 5750
02253 5760
02254 5770
02255 5780

113 IF (OPLOT)100,103,114
114 IF (N -200)103,115,115
115 IRET = 1
116 IUSED = 1
CALL PLTRAJIXA,Y1,Y2,Y3,Y4,N,10,2,3,4,5,COM)
CALL PLTRAJIXA,Y5,Y6,Y7,Y8,N,10,1,6,7,8,COM)
CALL PLTRAJIXA,Y9,Y10,Y3,Y4,N,10,9,11,0,0,COM)
N = 0
IF (IRET) 99, 99,103

C RUNGE KUTTA INTEGRATION (4TH ORDER)
103 00 74 J=1,N
THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
IF (J.EQ.1.AND.DTPC.EQ.0.) GO TO 77
CALL SUBR
77 00 75 I=1,6
75 A(I),J=EE(I)0DT
DO 76 I=1,5
76 88(I,J)=FF(I)0DT
GO TO (71,72,73,74),J
71 PSI=PSI+S*PSID0DT
THE=THE+S*THED0DT
PHI=PHI+S*PHID0DT
XX=X+S*XD0DT
YY=Y+S*YD0DT
Z=Z+S*ZD0DT
PSI=PSI+S*PSIPD0DT
THE=THE+S*THEPD0DT
XP=XP+S*XPD0DT
YP=YP+S*YPD0DT
ZP=ZP+S*ZPD0DT
PSID=PSID+S*AA(1,I)
THED=THED+S*AA(2,I)
PHID=PHID+S*AA(3,I)
XD=XD+S*AA(4,I)
YD=YD+S*AA(5,I)
ZD=ZD+S*AA(6,I)
PSIPD=PSIPD+S*88(1,I)
THEPD=THEPD+S*88(2,I)
XPD=XPD+S*88(3,I)
YPD=YPD+S*88(4,I)
ZPD=ZPD+S*88(5,I)
T=T+S*DT
GO TO 74
72 FSI=PSI+S*25*AA(1,I)0DT
THE=THE+S*25*AA(2,I)0DT
PHI=PHI+S*25*AA(3,I)0DT
XX=X+S*25*AA(4,I)0DT
YY=Y+S*25*AA(5,I)0DT
ZZ=Z+S*25*AA(6,I)0DT
PSIP=PSIP+S*25*88(1,I)0DT
THEP=THEP+S*25*88(2,I)0DT
XP=XP+S*25*88(3,I)0DT
YP=YP+S*25*88(4,I)0DT
ZP=ZP+S*25*88(5,I)0DT

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5790 PSID=PSID+.5\*(AA(1,2)-AA(1,1))  
 5800 THED=THED+.5\*(AA(2,2)-AA(2,1))  
 5810 PHID=PHID+.5\*(AA(3,2)-AA(3,1))  
 5820 XD=XD+.5\*(AA(4,2)-AA(4,1))  
 5830 YD=YD+.5\*(AA(5,2)-AA(5,1))  
 5840 ZD=ZD+.5\*(AA(6,2)-AA(6,1))  
 5850 PSIPD=PSIPD+.5\*(BB(1,2)-BB(1,1))  
 5860 THEPD=THEPD+.5\*(BB(2,2)-BB(2,1))  
 5870 XPD=XPD+.5\*(BB(3,2)-BB(3,1))  
 5880 YPD=YPD+.5\*(BB(4,2)-BB(4,1))  
 5890 ZPD=ZPD+.5\*(BB(5,2)-BB(5,1))  
 GO TO 74  
 73 PSI=PSI+DT\*(.5\*PSID+.25\*(AA(1,2)-AA(1,1)))  
 74 THE=THE+DT\*(.5\*THED+.25\*(AA(2,2)-AA(2,1)))  
 75 PHI=PHI+DT\*(.5\*PHID+.25\*(AA(3,2)-AA(3,1)))  
 76 X=X+DT\*(.5\*XD+.25\*(AA(4,2)-AA(4,1)))  
 77 Y=Y+DT\*(.5\*YD+.25\*(AA(5,2)-AA(5,1)))  
 78 Z=Z+DT\*(.5\*ZD+.25\*(AA(6,2)-AA(6,1)))  
 79 PSIP=PSIP+DT\*(.5\*PSIPD+.25\*(BB(1,2)-BB(1,1)))  
 80 THEP=THEP+DT\*(.5\*THEPD+.25\*(BB(2,2)-BB(2,1)))  
 81 XP=XP+DT\*(.5\*XPD+.25\*(BB(3,2)-BB(3,1)))  
 82 YP=YP+DT\*(.5\*YPD+.25\*(BB(4,2)-BB(4,1)))  
 83 ZP=ZP+DT\*(.5\*ZPD+.25\*(BB(5,2)-BB(5,1)))  
 84 PSIO=PSIO+.5\*(AA(1,2)+AA(1,3))  
 85 THEC=THEC+.5\*(AA(2,2)+AA(2,3))  
 86 PHIO=PHIO+.5\*(AA(3,2)+AA(3,3))  
 87 XD=XD+.5\*(AA(4,2)+AA(4,3))  
 88 YD=YD+.5\*(AA(5,2)+AA(5,3))  
 89 ZD=ZD+.5\*(AA(6,2)+AA(6,3))  
 90 PSIPD=PSIPD+.5\*(BB(1,2)+BB(1,3))  
 91 THEPD=THEPD+.5\*(BB(2,2)+BB(2,3))  
 92 XPD=XPD+.5\*(BB(3,2)+BB(3,3))  
 93 YPD=YPD+.5\*(BB(4,2)+BB(4,3))  
 94 ZPD=ZPD+.5\*(BB(5,2)+BB(5,3))  
 T=1+.5\*DT  
 74 CONTINUE  
 PSIO=PSIO-AA(1,3)  
 THEC=THEC-AA(2,3)  
 PHIO=PHIO-AA(3,3)  
 XD=XD-AA(4,3)  
 YD=YD-AA(5,3)  
 ZD=ZD-AA(6,3)  
 PSIPD=PSIPD-BB(1,3)  
 THEPD=THEPD-BB(2,3)  
 XPD=XPD-BB(3,3)  
 YPD=YPD-BB(4,3)  
 ZPD=ZPD-BB(5,3)



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02347 635  V=Z-DT*(ZPD+5*BB(4,2))
02350 636  ZP=Z-DT*(ZPD+5*BB(5,2))
02351 637  PSI=PSI-DT*(PSID+AA(1,1)+AA(1,2)+AA(1,3))/6.
02352 638  THE=THE-DT*(THED+AA(2,1)+AA(2,2)+AA(2,3))/6.
02353 639  PHI=PHI-DT*(PHID+AA(3,1)+AA(3,2)+AA(3,3))/6.
02354 640  X=X-DT*(XD+AA(4,1)+AA(4,2)+AA(4,3))/6.
02355 641  Y=Y-DT*(YD+AA(5,1)+AA(5,2)+AA(5,3))/6.
02356 642  Z=Z-DT*(ZD+AA(6,1)+AA(6,2)+AA(6,3))/6.
02357 643  PSIP=PSIP-DT*(PSIPD+BB(1,1)+BB(1,2)+BB(1,3))/6.
02360 644  THEP=THEP-DT*(THEPD+BB(2,1)+BB(2,2)+BB(2,3))/6.
02361 645  XPD=XPD-DT*(XPD+BB(3,1)+BB(3,2)+BB(3,3))/6.
02362 646  YPD=YPD-DT*(YPD+BB(4,1)+BB(4,2)+BB(4,3))/6.
02363 647  ZPD=ZPD-DT*(ZPD+BB(5,1)+BB(5,2)+BB(5,3))/6.
02364 648  PSI=PSI-DT*(PSID+AA(1,1)+AA(1,2)+AA(1,3))/6.
02365 649  THE=THE-DT*(THED+AA(2,1)+AA(2,2)+AA(2,3))/6.
02366 650  PHI=PHI-DT*(PHID+AA(3,1)+AA(3,2)+AA(3,3))/6.
02367 651  X=X-DT*(XD+AA(4,1)+AA(4,2)+AA(4,3))/6.
02370 652  Y=Y-DT*(YD+AA(5,1)+AA(5,2)+AA(5,3))/6.
02371 653  Z=Z-DT*(ZD+AA(6,1)+AA(6,2)+AA(6,3))/6.
02372 654  PSIP=PSIP-DT*(PSIPD+BB(1,1)+BB(1,2)+BB(1,3))/6.
02373 655  THEP=THEP-DT*(THEPD+BB(2,1)+BB(2,2)+BB(2,3))/6.
02374 656  XPD=XPD-DT*(XPD+BB(3,1)+BB(3,2)+BB(3,3))/6.
02375 657  YPD=YPD-DT*(YPD+BB(4,1)+BB(4,2)+BB(4,3))/6.
02376 658  ZPD=ZPD-DT*(ZPD+BB(5,1)+BB(5,2)+BB(5,3))/6.
02377 659  IF(ABS(SIN(SNGLE(T(1)))*LT(5.41)) DT=DT/5.
02401 660  IF(ABS(SIN(SNGLE(T(1)))*GT(5.41)) DT=DT*
GO TO 100
02403 661  1000 CONTINUE
02404 662
02405 663  IF(IUSED.EQ.0) GO TO 1010
02405 664  C   END ALL PLOTTING BEFORE EXIT
02407 665  CALL ENDJOB
02410 666  1010 STOP
02411 667  END

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END OF COMPILATION: 18 DIAGNOSTICS.

CF-7  
FOR US SUBR  
MSD 11A -03/27/74-00119:12 (0.1)

SUBROUTINE SUBR ENTRY POINT 006176

STORAGE USED: CODE(1) 0062101 DATA(0) 0005761 BLANK COMMON(2) 020174

EXTERNAL REFERENCES (BLOCK, NAME)

- 0003 DENS
- 0004 DENSM
- 0005 INTERP
- 0006 PIVERT
- 0007 SIN
- 0010 COS
- 0011 SQRT
- 0012 ATAN2
- 0013 MPOUS
- 0014 NIOZS
- 0015 NSTOP5
- 0016 XPRR
- 0017 MERR38

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

Block	Type	Relative Location	Name
0001	000346	10L	000563 100L
0001	001551	104L	001640 110L
0001	000555	15L	001652 111L
0001	001193	163L	001047 161L
0000	000354	196F	001421 174L
0001	001675	211L	001663 210L
0001	002405	301L	001373 300L
0001	005311	41L	001362 401L
0001	002054	501L	004042 500L
0001	003207	61L	002077 601L
0001	003203	676G	003254 67L
0001	002337	801L	002325 800L
0001	002145	901L	004133 900L
0002	R 000155	A	002316 97L
0002	R 000324	AAH	000217 66L
0002	R 020154	AERATO	003162 665G
0000	R 000231	ALPPE	000637 80L
0002	017764	AMAX2	000721 84L
0000	R 000260	AMSL	002313 98L
0000	R 000100	BBAR	000264 98L
0002	R 000107	CA	000264 98L
0002	R 000344	CCA	000277 80L
0002	R 015344	CCLM9	003162 665G
0002	R 017470	CCLM9	000637 80L
0002	R 000114	CLL	000721 84L
0002	R 000121	CLNR	002313 98L
0000	R 000270	CPM11	000264 98L
0001	000346	10L	000575 101L
0001	001652	111L	001640 110L
0001	001047	161L	001652 111L
0001	001421	174L	001373 170L
0001	001663	210L	001414 198L
0001	001373	300L	002026 215L
0001	001362	401L	00162 40L
0001	004042	500L	00430 1JL
0001	002077	601L	00341 52F
0001	003254	67L	003221 62L
0001	002325	800L	002110 700L
0001	004133	900L	002675 81L
0001	002316	97L	000707 82L
0002	R 000155	A	002471 96L
0002	R 000324	AAHPPE	000334 AALPDE
0002	R 020154	AERATO	000334 AAHD
0000	R 000231	ALPPE	000177 ALPE
0002	017764	AMAX2	000252 ALPPSL
0000	R 000260	AMSL	017767 AMAY1
0000	R 000100	BBAR	002160 AP
0002	R 000107	CA	000303 BBAHD
0002	R 000344	CCA	000115 CAP
0002	R 015344	CCLM9	0002 R 013344 CCLL
0002	R 017470	CCLM9	0002 R 016341 CCLNR
0002	R 000114	CLL	0002 R 020131 CCR1T
0002	R 000121	CLNR	0002 R 000112 CLM
0000	R 000270	CPM11	0002 R 000110 CN
0001	000346	10L	000575 102L
0001	001652	111L	001640 110L
0001	001047	161L	001652 111L
0001	001421	174L	001421 174L
0001	001663	210L	001431 200L
0001	001373	300L	003306 30L
0001	001362	401L	00250 400L
0001	004042	500L	000627 50L
0001	002077	601L	002065 600L
0001	003254	67L	003162 665G
0001	002325	800L	000637 80L
0001	004133	900L	000721 84L
0001	002316	97L	002313 98L
0002	R 000155	A	000264 98L
0002	R 020154	AERATO	000277 80L
0000	R 000231	ALPPE	000277 80L
0002	017764	AMAX1	000166 AM
0000	R 000260	AMSL	000167 AMP
0000	R 000100	BBAR	017775 AY
0002	R 000107	CA	017776 BY
0002	R 000344	CCA	000304 CBAND
0002	R 015344	CCLM9	000344 CCLM
0002	R 017470	CCLM9	000231 CCN
0002	R 000114	CLL	000344 CCY
0002	R 000121	CLNR	000120 CLM
0000	R 000270	CPM11	000116 CNP
0001	000346	10L	000641 103L
0001	001652	111L	00054 19L
0001	001047	161L	00105 162L
0001	001421	174L	001361 195L
0001	001663	210L	001663 210L
0001	001373	300L	001373 300L
0001	001362	401L	001362 401L
0001	004042	500L	004042 500L
0001	002077	601L	002077 601L
0001	003254	67L	003254 67L
0001	002325	800L	002325 800L
0001	004133	900L	004133 900L
0001	002316	97L	002316 97L
0002	R 000155	A	000264 98L
0002	R 020154	AERATO	000277 80L
0000	R 000231	ALPPE	000277 80L
0002	017764	AMAX1	000166 AM
0000	R 000260	AMSL	000167 AMP
0000	R 000100	BBAR	017775 AY
0002	R 000107	CA	017776 BY
0002	R 000344	CCA	000304 CBAND
0002	R 015344	CCLM9	000344 CCLM
0002	R 017470	CCLM9	000231 CCN
0002	R 000114	CLL	000344 CCY
0002	R 000121	CLNR	000120 CLM
0000	R 000270	CPM11	000116 CNP
0001	000346	10L	000641 103L
0001	001652	111L	00054 19L
0001	001047	161L	00105 162L
0001	001421	174L	001361 195L
0001	001663	210L	001663 210L
0001	001373	300L	001373 300L
0001	001362	401L	001362 401L
0001	004042	500L	004042 500L
0001	002077	601L	002077 601L
0001	003254	67L	003254 67L
0001	002325	800L	002325 800L
0001	004133	900L	004133 900L
0001	002316	97L	002316 97L
0002	R 000155	A	000264 98L
0002	R 020154	AERATO	000277 80L
0000	R 000231	ALPPE	000277 80L
0002	017764	AMAX1	000166 AM
0000	R 000260	AMSL	000167 AMP
0000	R 000100	BBAR	017775 AY
0002	R 000107	CA	017776 BY
0002	R 000344	CCA	000304 CBAND
0002	R 015344	CCLM9	000344 CCLM
0002	R 017470	CCLM9	000231 CCN
0002	R 000114	CLL	000344 CCY
0002	R 000121	CLNR	000120 CLM
0000	R 000270	CPM11	000116 CNP

0000 K 000334 CPSIP2  
0000 R 000172 CTMEP2  
0000 M 000270 C152  
0000 R 000176 CZTMEP  
0000 R 000315 DADPSP  
0000 M 000317 DADPSP  
0000 M 000324 DCDTME  
0000 M 000247 DELSPO  
0002 K 000114 DLX  
0002 M 017757 OS  
0002 D 017772 DSY2  
0002 R 000040 EE  
0002 R 000034 EPT  
0000 M 000271 FXB  
0002 K 000213 FYP  
0000 K 000276 FZPB  
0000 R 000002 ICXO  
0002 K 017745 I1YPB  
0002 R 000124 I1B  
0002 R 000125 I1B  
0000 I 000251 J  
0002 R 000132 LS  
0002 R 000147 LTO  
0002 R 000144 HP  
0002 R 020133 NS  
0002 R 000206 OMBZ  
0002 R 000135 OPSYM  
0002 D 000004 PHI  
0002 K 000202 PHIE  
0002 R 000314 PPHIE  
0002 D 000000 PSI  
0000 R 000152 PSIPDZ  
0002 K 000104 PK  
0002 R 000223 QTHE  
0002 R 017761 RH000  
0000 R 000245 SPDINF  
0000 M 000244 SPOI  
0002 K 020144 SPR2  
0002 K 017721 SSP  
0000 K 000204 SIC2C3  
0000 R 000206 S2C3  
0000 M 000175 S2THERP  
0000 M 000242 TFMTI  
0002 D 000052 THEPD  
0000 R 000237 TOIF  
0000 R 000230 TPOY  
0002 020134 TRO  
0002 R 017701 T1PB  
0002 R 000221 T2PB  
0002 K 020171 TOTR3  
0000 M 000221 VS  
0002 D 000006 X  
0000 R 000225 XPB0  
0000 R 000344 XPDPD  
0002 K 000153 YBAR  
0002 D 000044 YPD

0002 R 000123 CS  
0000 R 000170 CT E2  
0000 R 000211 C152C3  
0000 R 000337 CZTMEP  
0000 R 000315 DADTME  
0000 R 000322 DADPSP  
0000 D 000324 DCDTME  
0002 R 020064 DELSK  
0000 R 000312 DLXSL  
0002 R 020022 OSP  
0000 D 000056 DT  
0000 D 000137 EEP  
0002 D 000074 FF  
0002 R 000212 FXP  
0000 R 000275 FY#B  
0000 R 000217 G  
0000 R 000301 ICYO  
0000 R 000004 ILKO  
0002 R 000142 I1MYPB  
0002 R 000141 I1MZB  
0000 I 000263 JJ  
0000 R 000243 KSLC  
0002 R 000143 M  
0002 R 017756 MPAL  
0002 R 020134 NT  
0000 R 000134 OPAM  
0002 R 000235 PC OI  
0002 R 000230 PHIAF  
0000 R 000232 PHIPI  
0000 R 000223 PR  
0002 D 000144 PS D  
0002 R 000204 PSX  
0002 R 020071 QMAXPB  
0002 R 000226 QT EP  
0002 R 000173 S  
0000 R 000155 SPH1  
0002 R 020161 SPAL  
0002 R 020145 SPR3  
0000 R 000154 STME  
0000 R 000174 SZPHI  
0002 D 000054 T  
0002 D 000022 THE  
0002 R 020163 TIMF  
0000 R 000236 TOIR  
0002 R 017356 TPOYB  
0002 020137 TH1  
0002 R 000215 T1B  
0002 R 020135 TO  
0002 R 000164 V  
0002 020124 WTC  
0002 R 000152 XBAR  
0000 R 020165 XPB01  
0000 R 000340 XPD2  
0000 R 000223 YB0  
0000 R 000345 YPDZPB

0000 R 000161 CTME  
0000 R 000213 C1C2C3  
0000 R 000177 CZPMI  
0000 R 000314 DADPMI  
0000 R 000311 DAMP  
0000 D 000115 DDP  
0000 R 000308 DLT  
0002 R 000176 DP  
0002 R 017766 DSK2  
0002 R 000170 DYPK  
0000 D 000145 EPS  
0002 R 000153 FSULT  
0002 R 000210 FY  
0000 R 000273 FZB  
0002 R 000163 GD  
0002 000271 I1M  
0000 00045 I1NJP5  
0002 R 000127 I1YB  
0002 R 000131 I1ZB  
0002 R 017741 KKS  
0002 R 000146 LT  
0002 R 017742 MNPAL  
0002 R 000200 MPL  
0002 R 000204 OMBX  
0002 R 000133 OPOS  
0002 R 020147 PCTU2  
0000 R 000151 PH1U2  
0002 R 020141 POROS  
0000 R 000215 P5DPHD  
0002 D 000036 P5IP  
0002 R 020054 PTK  
0002 R 000222 QPSI  
0002 R 000172 RHO  
0002 R 017760 SPD  
0000 R 000254 SPHIPI  
0002 R 020142 SPRC  
0000 R 000156 SPSIP  
0000 R 000167 STHEL2  
0000 R 000202 S1S2C3  
0000 R 000205 S2S3  
0002 R 000161 TENS  
0000 R 000150 THEU2  
0002 R 020173 TNINY  
0000 R 000327 TPOX  
0002 R 017357 TPO4B  
0002 020141 TR3  
0002 R 000220 TYPB  
0002 R 020167 TOTM1  
0000 R 000255 VPXB  
0002 020125 WTL  
0002 D 000022 XD  
0002 D 000042 XPD  
0000 R 000346 XPPSPU  
0002 D 000024 YD  
0000 R 000341 YPD2

0000 M 000164 CTMEP  
0000 K 000212 C1C2S3  
0000 M 000336 CZPSIP  
0000 M 000312 DADPSI  
0000 M 000321 DADPMI  
0000 M 000325 DCDPMI  
0000 M 000246 DELSP  
0000 M 000307 ULTX  
0002 M 000203 UPR  
0002 017771 U571  
0002 000171 UYHP  
0002 M 000227 U5PSI  
0002 M 000207 YX  
0000 K 000272 FYB  
0002 M 000214 FZP  
0000 I 000233 I  
017744 I1XPA  
0002 I 000232 I1UUT  
0002 K 000130 I1ZB  
0002 M 000146 I2B  
0002 M 000151 I2S  
0002 M 000180 LTO  
0002 017743 MNPAS  
0002 M 000201 MPS  
0002 M 000205 OMBX  
0002 M 020172 O1SP  
0002 M 020180 PCTO3  
0000 M 000256 PHT1  
0002 K 017344 PPHIDE  
0000 M 000214 P5DTU  
0002 U 000050 P5IPU  
0000 M 000306 PTKSL  
0002 K 000225 UPSIP  
0002 M 017762 MH00  
0000 K 000241 SPOEL  
0000 M 000166 SPH12  
0002 M 020143 SPRI  
0000 M 000333 SPSIP2  
0000 M 000165 STME2  
0000 M 000201 S1S2S3  
0002 M 000173 S2TME  
0002 K 020164 TFI  
0002 U 000204 TRU  
0002 M 000234 TSL  
0002 K 000217 T2B  
0002 K 020170 TOTM2  
0000 M 000230 VPXPB  
0002 M 020130 WTLM  
0002 U 000030 XP  
0000 M 000343 XPDPD  
0002 D 000010 Y  
0000 M 000226 YPB  
0000 M 000351 YPTMFD

0002 D 000012 Z      0002 R 000154 ZBAR      0000 R 000224 ZBD      0002 D 000026 ZD      0002 U 000034 ZP  
 0000 R 000227 ZPBD      0002 D 000046 ZPD      0000 R 000342 ZPDZ      0000 M 000352 ZPSPD      0000 M 000353 ZPTMPD

00000 \*DIAGNOSTIC\*      THE NAME IZXR APPEARS IN A DIMENSION OR TYPE STATEMENT BUT IS NEVER REFERENCED.  
 00000 \*DIAGNOSTIC\*      THE NAME IXYA APPEARS IN A DIMENSION OR TYPE STATEMENT BUT IS NEVER REFERENCED.

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00101 SUBROUTINE SUBR
00102 REAL M,IXB,IYB,IZB,IXZB,IYZB,IYXZB,IZMAB,IXMYB
00103 1,MP,MPAL,MPAS,MPL,MPS,MLMHP,LT,LTO,LTDO,KS,IXPB,IYPB,IXMYPB
00104 2,LSCL,LSNS,NT,LSLCO,LYO,IXKO,ILYO,ILXO
00105 DOUBLE PRECISION PSI,THE,PHI,X,Y,Z,PSID,THEU,PHID,XD,YD,ZD,AP,YP,
00106 IZP,PSIP,THEP,XPD,YPD,ZPD,PSIPD,THEPD,EE(6),FF(5),T,UT
00107 2,DD(6,6),DDF(3,3),EEP(3),EPS
00108 COMMON PSI,THE,PHI,X,Y,Z,PSID,THEU,PHID,XD,YD,ZD,AP,YP,
00109 IZP,PSIP,THEP,XPD,YPD,ZPD,PSIPD,THEPD,T,UT,EE,FF
00110 COMMON ALPH,CA,CM,CY,CLM,CLN,CLL,CAP,CHP,CHM,CLMQ,CLNK,CLLP,CS,
00111 2,IXB,IYB,IZB,IXZB,IYZB,IXPB,OPAS,OPAM,OPSYM,OPDA,OMETRC,
00112 3,IYPB,IYXZB,IXMYPB,M,MP,MLMHP,LT,LTO,LTU,KS,XBAR,YBAR,ZBAR,A,B,
00113 4C,AP,TEMS,RE,GO,V,VP,AM,AMP,DYPR,DYPRP,KMO,S,SP,D,DP,ALPE,MPL,MPS,
00114 6PHIE,DPR,OMXB,OMYB,M75,FX,FY,FZ,FAP,FPY,FPZ,FXB,TYB,IZB,IYPB,
00115 7TZPB,QPSI,QTHE,QPHI,QPSIP,QTHER,EPST,PHIAE,IIN,IOUT
00116 COMMON CC(3,3),AALPFE(16),AALPME(16),AALPDE(8),PPHIE(8),AAM(8)
00117 1,AAMD(8),CCA(8,16,8),CCN(8,16,8),CCY(8,16,8),CCLL(8,16,8),CCLM(8,16,8),
00118 2CCL(8,16,8),CCLN(8,16,8),CCLP(8,8,8),CCLM(8,8,8),
00119 3CCLNR(8,8,8),PPHIDE(8),TPD,TPUXB,TPDYB,TPUZH
00120 4,AAMP(8),CCAP(8,8),CCNP(8,8),CCMP(8,8),CCPI(3,3),TTIP(16),SSP(16),
00121 5 KKS,MMPAL,MMPAS,IIXPB,IYYPB,IYXZPB,IYXZPB,IYXZPB,IYXZPB,IYXZPB,IYXZPB,
00122 6,DS,SPD,RH00,RH00,AMAX1,AMAX2,OSK1,OSK2,AMAY1,AMAY2,DST1,DST2,
00123 7 AX,AX,AY,RY,HPAS,OMD,QMAXPB,DSP,CSIGP,PS(8),PT(8),EPL(8),EPT(8),
00124 8 PSX(8),PTX(8),DELSX(8),DELTA(8),PX(8),DLX(8),MTC,WL,LSLCO
00125 9 WTCM,WTLH,CCRIT,LS,NS,NT,TO,TRQ,TRI,TR2,TR3,SPRU,SPH1,SPR2,SPR3
00126 A ,PCTO1,PCTO2,PCTO3,POROS,GLOAD,FSULT,AERATO,AREG,XPBOR,DT1
00127 B,SPRU,SPRL,TINT,YINF,TFI,XPBD1,TOTR0,TOTR1,TOTR2,TOTR3,OPSP,TMINY
00128 EPS=.1D-12
00129 PS1D=PS1D**2
00130 THE2=THE**2
00131 PH1D=PH1D**2
00132 PS1D2=PS1D**2
00133 SP1=STN(SNGL(PS1))
00134 STHE=STN(SNGL(THE))
00135 SPH1=STN(SNGL(PH1))
00136 SP1P=STN(SNGL(PS1P))
00137 STHEP=STN(SNGL(THEP))
00138 CPS1=COS(SNGL(PS1))
00139 CTHE=COS(SNGL(THE))
00140 CPH1=COS(SNGL(PH1))
00141 CPSIP=COS(SNGL(PSIP))
00142 CTHEP=COS(SNGL(THEP))
00143 STHE2=STHE**2
00144 SPH12=SPH1**2
00145 STHEP2=STHEP**2
00146 CTHE2=CTHE**2
00147 CPH12=CPH1**2
00148 CTHEP2=CTHEP**2

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 P0220  
 P0221

S2THE=7\*STHE\*CTHE  
 S2PHI=2\*SPHI\*CPHI  
 S2THEP=2\*STHEP\*CTHEP  
 C2THE=CTHE2-STHE2  
 C2PHI=CPHI2-SPHI2  
 S1S2=SPSI\*STHE  
 S1S2S3=SPSI\*STHE\*SPHI  
 S1S2C3=SPSI\*STHE\*CPHI  
 S1C2S3=SPSI\*CTHE\*SPHI  
 S1C2C3=SPSI\*CTHE\*CPHI  
 S2S3=STHE\*SPHI  
 S2C3=STHE\*CPHI  
 C1S2=CPSI\*STHE  
 C1S2S3=CPSI\*STHE\*SPHI  
 C1S2C3=CPSI\*STHE\*CPHI  
 C1C2S3=CPSI\*CTHE\*SPHI  
 C1C2C3=CPSI\*CTHE\*CPHI  
 PSDTD=PSID\*THED  
 PSDPHD=PSID\*PHID  
 TOPHD=THED\*PHID

C  
 C  
 C  
 CALCULATE TRANSFORMATION MATRICES

CC(1,1)=CPSI\*CTHE  
 CC(1,2)=SPSI\*CTHE  
 CC(1,3)=STHE  
 CC(2,1)=C1S2S3\*SPSI\*CPHI  
 CC(2,2)=S1S2S3\*CPSI\*CPHI  
 CC(2,3)=CTHE\*SPHI  
 CC(3,1)=C1S2C3\*SPSI\*SPHI  
 CC(3,2)=S1S2C3\*CPSI\*PHI  
 CC(3,3)=CTHE\*CPHI  
 CCP(1,1)=CPSIP\*CTHEP  
 CCP(1,2)=SPSIP\*CTHEP  
 CCP(1,3)=STHEP  
 CCP(2,1)=SPSIP  
 CCP(2,2)=CPSIP  
 CCP(3,1)=CPSIP\*STHEP  
 CCP(3,2)=SPSIP\*STHEP  
 CCP(3,3)=CTHEP  
 G=GDIRE/(Z\*RE)\*\*2  
 IF(DIAGNOSTIC) THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.  
 IF(DIAGNOSTIC) GO 0 10  
 CALL DENSIZ,PR,RHO,VS  
 GO TO 11  
 10 CALL DENSIZ,PR,RHO, S1  
 11 CONTINUE  
 V=SQRT(SMGL(XD\*2+YD\*2+ZD\*2))  
 VP=SQRT(SMGL(XPD\*2+YPD\*2+ZPD\*2))  
 AM=V/VS  
 AMP=VP/VS  
 DYPR=.5\*RHO\*V\*2  
 DYPRP=.5\*RHO\*VP\*2  
 XBD=XD\*CC(1,1)+YD\*CC(1,2)+ZD\*CC(1,3)  
 YBD=YD\*CC(2,1)+YD\*CC(2,2)+ZD\*CC(2,3)  
 ZBD=XD\*CC(3,1)+YD\*CC(3,2)+ZD\*CC(3,3)

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00222 1040 XPRD=XPDC*CCP(1,1)+YPC*CCP(1,2)+ZPC*CCP(1,3)
00223 1050 YPRD=XPDC*CCP(2,1)+YPC*CCP(2,2)
00224 1060 ZPRD=XPDC*CCP(3,1)+YPC*CCP(3,2)+ZPC*CCP(3,3)
00225 1070 VPXPR=SQRT(YPC**2+ZPC**2)
00226 1080 ALPP=ATAN2(VPXPR,XPBD)
00227 1090 ALPPE = ALPP*OPR
00230 1100 IF (VPXPR) 13,13,14
00233 1110 13 PHIPI = 0.
00234 1120 GO TO 15
00235 1130 14 PHIPI = ATAN2(-YPC,-ZPC)
00236 1140 15 CONTINUE
00237 1150 C
00238 1160 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00239 1170 IF(OPSP.EQ.0) GO TO 103
00241 1180 C
00242 1190 I=2
00243 1200 100 IF(Y.LE.YTIP(I)) GO 0 101
00244 1210 I=I+1
00245 1220 GO TO 100
00246 1230 101 TSL=(Y-TTIP(I-1))/(TTIP(I)-TTIP(I-1))
00247 1240 SP=SSP(I-1)+(SSP(I)-SSP(I-1))*TSL
00248 1250 SPD= (SSP(I)-SSP(I-1))/(TTIP(I)-TTIP(I-1))
00249 1260 XPBDR= XPBD
00250 1270 IF(SPD.LY.0) GO TO 50
00251 1280 GO TO 151
00252 1290 50 XPBDR= 0.0
00253 1300 151 CONTINUE
00254 1310 GO TO 200
00255 1320 103 CONTINUE
00256 1330 IF(I.GT.TOTR) GO TO 80
00257 1340 GO TO 84
00258 1350 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00259 1360 IF(PTOI.EQ.0) GO 0 84
00260 1370 IF(T.GE.TINF.AND.T.LY.TOIR) GO TO 82
00261 1380 81 IF((TFI/DT).LE.2.) DT= DT/2.
00262 1390 GO TO 84
00263 1400 82 IF((TOIF/DT).LE.2.) DT= DT/2.
00264 1410 GO TO 84
00265 1420 84 CONTINUE
00266 1430 IF(T.LE.TOTR.AND.T.GE.TO) GO TO 160
00267 1440 IF(T.LE.TOTR1.AND.T.GT.TOTR) GO TO 161
00268 1450 IF(T.LE.TOTR2.AND.T.GT.TOTR1) GO TO 162
00269 1460 IF(T.LE.TOTR3.AND.T.GT.TOTR2) GO TO 163
00270 1470 SP=SPRO
00271 1480 SPD= 0.0
00272 1490 TINF= 0.0
00273 1500 PCTOI= 0.0
00274 1510 XPBDI= 0.0
00275 1520 TFI= 0.0
00276 1530 SPRU= 0.0
00277 1540 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00278 1550 IF(T.LE.TOTR.AND.T.GT.(TOTR-OT)) XPBDI=XPBD
00279 1560 GO TO 200
00280 1570 161 TINT = TOTR

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00326      SPRL = SPR0
00327      SPRU = SPR1
00330      PCT01 = PCT01
00331      TRU = TOTR1
00332      IF (T.LE.TOTR1.AND.T.GT.(TOTR1-0T)) XPBD1=XPBD
00334      GO TO 190
00335      TINT = TOTR1
00336      SPRU = SPR1
00337      SPRU = SPR2
00340      PCT01 = PCT02
00341      TRU = TOTR2
00342      IF (T.LE.TOTR2.AND.T.GT.(TOTR2-0T)) XPBD1 = XPBD
00345      TINT = TOTR2
00346      SPRU = SPR2
00347      SPRU = SPR3
00350      PCT01 = PCT03
00351      TRU = TOTR3
00352      GO TO 190
00353      SPOEL = SPRU-SPRL
00354      TFI = 45.01284*(SURT(SPOEL))*POROS/XPBD1
00355      TINF = TINT+TFI
00356      TFMTI = TINF-TINT
00357      TOIF = 5.0PCT01*TFMTI
00360      TOIR = TINF+TOIF
00361      TOIR = TINF+2.0*TOIF
00362      SPOI = PCT01*SPOEL
00363      SPDINF = 2.0*SPOEL/TFMTI
00364      IF ((TRU-TOIR).LT.0.0) GO TO 194
00370      IF (T.LE.TINF.AND.T.GT.TINT) GO TO 191
00372      IF (T.LE.TOI.AND.T.GT.TINF) GO TO 195
00374      IF (T.LE.TOIR.AND.T.GT.TOI) GO TO 197
00400      DELSP = (SPOEL*(T-TINT)**2)/TFMTI**2
00401      SP = SPRL + DELSP
00402      XPDR = XPBD
00403      GO TO 200
00404      DELSPO = SPDINF*(T-TINF)
00405      SP = SPRU + DELSPO
00406      SPD = SPDINF
00407      XPDR = XPBD
00410      GO TO 200
00411      DELSPO = SPOI - SPDINF*(T-TOI)
00412      SP = SPRU + DELSPO
00413      SPD = -SPDINF
00414      XPDR = 0.0
00415      GO TO 200
00416      SP = SPRU
00417      SPD = 0.0
00420      XPDR = 0.0
00421      GO TO 200
00422      FORMAT(//,2X, 'TERMINATION REQUESTED BY PROGRAM , TRU=,IX,F10.4
00423      I ,2X,'GIVES NEGATIVE TIME ON REEFED STAGE',/))

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DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.

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00424 2130 194 WRITE(J,194) TRU
00427 2140 STOP
00430 2150 CONTINUE
00431 2160 IF((1-ABS(STHE))<.LT.EPSI) TMINY=TMINY-DY
00433 2170 DS= SQRT(1.2732405P)
00434 2180 DSP= .6380DS
00435 2190 LSCL= SORT(LS*LS-.250DSP0DSP)
00436 2200 CSIGP= LSCL/LS
00437 2210 RH000= RHO/RH00
00440 2220 MPAL= RH000*BX0DS0AX
00441 2230 MPAS= RH000*BY0DS0AY
00442 2240 QMAXPB= DMD*XPBDR
00444 2260 *DIAGNOSTIC THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00446 2270 IF(OPAM<EQ.0.C) GO TO 102
00447 2280 GO TO 104
00450 2290 102 MPAL= 0.0
00451 2300 MPAS= 0.0
00452 2310 MPL=MPAL*MP
00453 2320 MFS=MPAS*MP
00454 2330 MLMHSP=MPL-MPS
00455 2340 ICY0= .104167*WTCH0D P00SP
00456 2350 ICX0= .625*ICYO
00457 2360 ILY0= WTLH*(.C8333*LS*LS+.03125*DSP0DSP)
00460 2370 ILX0= .125*WTLH*DSP0DSP
00461 2380 IYP0= ICY0+ILY0+WTLH*(AP+.5*LS*CSIGP)*.02+(MPAS*WTCH0)
00462 2390 IXP0= ICX0+ILX0
00463 2410 IXMPB=IXPB-IYPB
00464 2420 I=2
00465 2430 110 IF(AMP*LE.AAMP(1)) GO TO 111
00467 2440 I=I+1
00470 2450 111 AMPSL=(AMP-AAMP(I-1))/(AAMP(I)-AAMP(I-1))
00471 2460 J=J
00472 2470 210 IF(ALPPE*LE.AALPPE(J)) GO TO 211
00473 2480 J=J+1
00475 2490 GO TO 210
00476 2500 211 ALPSSL= (ALPPE-AALPPE(J-1))/(AALPPE(J)-AALPPE(J-1))
00477 2510 CAP=(CCAP(I,J-1)-CCAP(I-1,J-1))/AMPSSL+CCAP(I-1,J-1)/(CCAP(I,J)-
00500 2520 ICCAP(I-1,J))/AMPSSL+C AP(I-1,J)/(CCAP(I,J-1)-CCAP(I-1,J-1))/AMPSSL+
00500 2530 2CCAP(I-1,J-1))/ALPSSL
00501 2540 CNP=(CCNP(I,J-1)-CCNP(I-1,J-1))/AMPSSL+CCNP(I-1,J-1)/(CCNP(I,J)-
00501 2550 ICCNP(I-1,J))/AMPSSL+CCNP(I-1,J)/(CCNP(I,J-1)-CCNP(I-1,J-1))/AMPSSL+
00501 2560 2CCNP(I-1,J-1))/ALPSSL
00502 2570 CMP=(CCMP(I,J-1)-CCMP(I-1,J-1))/AMPSSL+CCMP(I-1,J-1)/(CCMP(I,J)-
00502 2580 ICCMP(I-1,J))/AMPSSL+CCMP(I-1,J)/(CCMP(I,J-1)-CCMP(I-1,J-1))/AMPSSL+
00502 2590 2CCMP(I-1,J-1))/ALPSSL
00503 2610 CMP= CMP+(CNP*AP/DP)
00504 2620 CPHIPI=COS(PHIPI)
00505 2630 SPHIPI=SIN(PHIPI)
00506 2640 VPXB=SQRT(YB0**2+ZB0**2)
00507 2650 ALPE=ATAN2(VPXB,XB0)*OPR
00510 2660 IF (VPXB) 213,213,214
00513 2670 213 PHI= 0.

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00514 2680 GO TO 215
00515 2690 214 PH11 = ATAN2(-Y60,-Z60)
00516 2700 215 CONTINUE
00517 2710 PH11E=PH11*DP
00520 2720 PH1AE=PH1E
00521 2730 IF(PH1E.LT.0.) PH1AE=-PH1E
C
00521 2740 THE ABOVE STATEMENT SHOULD BECOME A COMMENT CARD IF THERE IS NO
C 2750 AERODYNAMIC PLANE OF SYMMETRY
C
00521 2760
C
00521 2770 AERODYNAMICS
C
00521 2780
C
00523 2800 K=2
00524 2810 500 IF(AM.LE.AAM(K)) GO TO 501
00526 2820 K=K+1
00527 2830 GO TO 500
00530 2840 501 AMSL=(AM-AAM(K))/(AAM(K)-AAM(K-1))
00531 2850 J=2
00532 2860 600 IF(ALPE.LE.AALPFE(J)) GO TO 601
00534 2870 J=J+1
00535 2880 GO TO 600
00536 2890 601 ALPFSL=(ALPE-AALPFE(J-1))/(AALPFE(J)-AALPFE(J-1))
00537 2900 I=2
00540 2910 700 IF(PH1AE.LE.PPH1E(I)) GO TO 701
00542 2920 I=I+1
00543 2930 GO TO 700
00544 2940 701 PH1SL=(P11AE-PPH1E(I-1))/(PPH1E(I)-PPH1E(I-1))
00545 2950 JJ=2
00546 2960 900 IF(ALPE.LE.AALPME(JJ)) GO TO 901
00550 2970 JJ=JJ+1
00551 2980 GO TO 900
00552 2990 901 ALPMSL=(ALPE-AALPME(JJ-1))/(AALPME(JJ)-AALPME(JJ-1))
C
00552 3000
C
00552 3010 THE FIFTH, SIXTH, AND SEVENTH ARGUMENTS OF SUBROUTINE 'INTERP'
C 3020 MUST AGREE WITH THE DIMENSIONS OF THE FIRST ARGUMENT
C
00552 3030 CALL INTERP(CCA,AMSL,ALPFSL,PH1SL,8,16,8,1,J,K,CF)
00553 3040 CA=CF
00554 3050 CALL INTERP(CCN,AMSL,ALPFSL,PH1SL,8,16,8,1,J,K,CF)
00555 3060 CN=CF
00556 3070 CALL INTERP(CCLM,AMSL,ALPMSL,PH1SL,8,16,8,1,J,K,CF)
00557 3080 CLM=CF
00560 3090
*DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00561 3100 IF(OPSYN.EQ.1.) GO TO 98
00563 3110 CALL INTERP(CCY,AMSL,ALPFSL,PH1SL,8,16,8,1,J,K,CF)
00564 3120 CY=CF
00565 3130 CALL INTERP(CCLL,AMSL,ALPMSL,PH1SL,8,16,8,1,J,K,CF)
00566 3140 CLL=CF
00567 3150 CALL INTERP(CCLN,AMSL,ALPMSL,PH1SL,8,16,8,1,J,K,CF)
00570 3160 CLN=CF
00571 3170 GO TO 99
00573 3180 98 CY=0.
00574 3190 CLL=0.
00574 3200 CLN=0.
00575 3210 99 CONTINUE
*DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00576

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00576 3220
00600 3230
00601 3240
00602 3250
00604 3260
00605 3270
00606 3280
00607 3290
00610 3300
00612 3310
00613 3320
00614 3330
00615 3340
00616 3350
00620 3360
00621 3370
00622 3380
00623 3390
00624 3400
00625 3410
00626 3420
00627 3430
00630 3440
00631 3450
00632 3460
00632 3470
00632 3480
00632 3490
00633 3500
00634 3510
00635 3520
00636 3530
00637 3540
00640 3550
00641 3560
00642 3570
00643 3580
00644 3590
00645 3600
00646 3610
00647 3620
00650 3630
00651 3640
00652 3650
00653 3660
00654 3670
00654 3680
00654 3690
00655 3700
00655 3710
00655 3720
00656 3730
00656 3740
00657 3750
00640 3760
00661 3770

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IF(OPDA.EQ.1.) GO TO 97
GO TO 96
97 J=2
800 IF(ALPE.LE.AALPDE(J)) GO TO 801
J=J+1
GO TO 800
901 ALPSL=(ALPE-AALPDE(J-1))/(AALPDE(J)-AALPDE(J-1))
K=2
900 IF(AH.LE.AAMD(K)) GO TO 901
K=K+1
GO TO 900
901 AMSL=(AH-AAMD(K-1))/(AAMD(K)-AAMD(K-1))
I=2
300 IF(PHIAE.LE.PPHIDE(I)) GO TO 301
I=I+1
GO TO 300
301 PHISL=(PHIAE-PPHIDE(I))/(PPHIDE(I)-PPHIDE(I-1))
CALL INTERP(CCLP,AMSL,ALPSL,PHISL,0,0,0,I,J,K,CF)
CCLP=CF
CALL INTERP(CCLM,AMSL,ALPSL,PHISL,0,0,0,I,J,K,CF)
CLM=CF
CALL INTERP(CCLNR,AMSL,ALPSL,PHISL,0,0,0,I,J,K,CF)
CLNR=CF
96 SPHII=SIN(PHII)
CPHII=COS(PHII)
C CALCULATE GENERALIZED FORCES
C
FXB=-OYPR*CA
FYB=OYPR*S(CN*SPHII-CY*CPHII)
FZB=OYPR*S(CN*CPHII+CY*SPHII)
OMXB=PHID*PSID*CC(1,3)
OMYB=THED*CPHI*PSID*CC(2,3)
OMZB=THED*SPI*PSID*CC(3,3)
TXB=OYPR*S(D*CLL+CLLP*OMXB*O/(2.0*V))
TYB=OYPR*S(D*CLM*CPHII-CLN*SPHII+CLM*OMYB*O/(2.0*V))
TZB=OYPR*S(D*CLN*SPHII-CLM*CPHII+CLN*OMZB*O/(2.0*V))
FXPB=-OYPR*SP*CAP-HA*PB
FYPB=OYPR*SP*CPN*SPHII
FZPB=OYPR*SP*CPN*CPHII
TYPB=OYPR*SP*OP*(CMP-.1)*THEPD*OP/VPI*CPHII
TZPB=OYPR*SP*OP*(CMP-.1)*THEPD*OP/VPI*SPHII
ABARXP=AP*CCP(1,1)-X*ACC(1,1)-B*CC(2,1)-C*CC(3,1)
BBARYP=AP*CCP(1,2)-Y*ACC(1,2)-B*CC(2,2)-C*CC(3,2)
CBARZP=AP*CCP(1,3)-Z*ACC(1,3)-B*CC(2,3)-C*CC(3,3)
ABARDXPD=AP*PSIPD*CCP(1,2)+THEPD*CCP(3,1)-XD+A*(PSID*
CC(1,2)-THED*CL12)-B*(PSID*CC(2,2)+PHID*CC(3,1)-THED*CL2S3)
ZC*(PSID*CC(3,2)-PHID*CC(2,1)-THED*CL2C3)
BBARDYPD=AP*PSI*CCP(1,1)-THEPD*CCP(3,2)-YD+A*(PSID*
CC(1,1)-THED*SL12)-B*(PSID*CC(2,1)+PHID*CC(3,2)+THED*SL2S3)
ZC*(PSID*CC(3,3)-PHID*CC(2,1)+THED*SL2C3)
CBARDZPD=AP*THEPD*CTHEP*ZD-A*THEPD*CTHEP*B*(-THED*SL2S3+PHID*
CC(3,3))+C*(THED*SL2C3+PHID*CC(2,3))
LTSORT(ABAR*2+BBAR*2+CBAR*2)
LTD=(AHAR*ABAR+BBAR*BBAR+CBAR*CBAR)/LT
DLT=LT-LTO

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00662 3780
00662 3790
00662 3800
00662 3810
00664 3820
00667 3830
00670 3840
00671 3850
00672 3860
00673 3870
00675 3880
00700 3890
00701 3900
00702 3910
00704 3920
00705 3930
00704 3940
00707 3950
00710 3960
00711 3970
00713 3980
00714 3990
00716 4000
00717 4010
00720 4020
00721 4030
00722 4040
00723 4050
00724 4060
00725 4070
00726 4080
00727 4090
00730 4100
00731 4110
00732 4120
00733 4130
00734 4140
00735 4150
00736 4160
00737 4170
00740 4180
00741 4190
00742 4200
00743 4210
00744 4220
00745 4230
00746 4240
00747 4250
00750 4260
00751 4270
00752 4280
00753 4290
00754 4300
00755 4310
00756 4320
00757 4330

IFILT,LT,LTO) GO TO 0
C
C SPRING CONSTANT AS A FUNCTION OF ELONGATJUN
C
DO 40 I=1,8
PSX(I)=PS(I)*NS*CSIGP
PTX(I)=PT(I)*NT
DELSX(I)=EPL(I)*LS*CSIGP
DELTX(I)=EPT(I)*LTO
60 CONTINUE
DO 45 J=1,8
PX(J)=PSX(I)
J=2
61 IF(PX(I).LE.PTX(J)) GO TO 62
J=J+1
62 PTXSL=(PX(I)+PTX(J))/(PTX(J)-PTX(I)-1)
DLTX=DELTX(J)+DELTX(I)-PTXSL
DLX(I)=DELSX(I)+DLTX
65 CONTINUE
I=2
66 IF(DLX(I).LE.DLX(I)) GO TO 67
I=I+1
67 DLXSL=(DLT-DLX(I-1))/(DLX(I)-DLX(I-1))
TENS=PX(I-1)+PX(I)-PX(I-1)*DLXSL
KS=TENS/DLT
CS=2*CCCRIT*SQRT(KS*OMPL)
DAMP=CS*LT
60 TO 31
30 TENS=0.
DAMP=0.
31 FX=FXB*CC(1,1)+FYB*CC(2,1)+FZB*CC(3,1)
FY=FYB*CC(1,2)+FYB*CC(2,2)+FZB*CC(3,2)
FZ=FZB*CC(1,3)+FYB*CC(2,3)+FZB*CC(3,3)-M*G
FXP=FXB*CCP(1,1)+FYPB*CCP(2,1)+FZPB*CCP(3,1)
FYP=FXB*CCP(1,2)+FYPB*CCP(2,2)+FZPB*CCP(3,2)
FZP=FXB*CCP(1,3)+FZPB*CCP(3,3)-M*P*G
QPSI=(TXB*CC(1,3)+TYB*CC(2,3)+TZB*CC(3,3))
QTHE=TYB. PHI+TZB*SPH
QPHI=TXB
QPSIP=TZPR*CCP(3,3)
QTHEP=TYPB
DADPSI=-A*CC(1,2)-B*CC(2,2)-C*CC(3,2)
DADTHE=A*CI2+B*CI253+C*CI2C3
DADPHI=-B*CC(3,1)+C*CC(2,1)
DADSP=AP*CCP(1,2)
DADTMP=AP*CCP(3,1)
DADPSI=A*CC(1,1)+B*CC(2,1)+C*CC(3,1)
DADTHE=-A*S12-B*S1C253-C*S1C2C3
DADPHI=-B*CC(3,2)+C*CC(2,2)
DADSP=AP*CCP(1,1)
DADTMP=AP*CCP(3,2)
DCDTHE=-A*CIHE+B*S253+C*S2C3
DCDPHI=-B*CC(3,3)+C*CC(2,3)
DCDTMP=AP*CCP(3,3)

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00760 4340 TPDS=TENS+DAMP
00761 4350 TPDX=TPD*ARAR/LT
00762 4360 TPDY=TPD*BRAR/LT
00763 4370 TPDZ=TPD*CRAR/LT
00764 4380 TPDXB=TPDX*CC(1,1)+TPDY*CC(1,2)+TPDZ*CC(1,3)
00765 4390 TPYB=TPDX*CC(2,1)+TPDY*CC(2,2)+TPDZ*CC(2,3)
00766 4400 TPZB=TPDX*CC(3,1)+TPDY*CC(3,2)+TPDZ*CC(3,3)
00767 *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
00767 4410 IF(TPOS.EQ.1.) GO TO 40
00767 4420 C
00767 4430 C
00767 4440 C
00771 4450 IF(1.-ABS(STHE)).LT.(EPS1) GO TO 43
00773 4460 DD(1,1)=IXR*STHE2+(IYB*SPH12+IZB*CPH12)*CTHE2
00774 4470 DD(1,2)=CTHE*IYMZB*.5*S2PH1
00774 4480 DD(1,3)=-IXB*CC(1,3)
00774 4490 DD(2,1)=DD(1,2)
00777 4500 DD(2,2)=IYB*CPH12+IZB*SPH12
00777 4510 DD(2,3)=0.
01000 4520 DD(3,1)=DD(1,3)
01001 4530 DD(3,2)=0.
01003 4540 DD(3,3)=IXB
01004 4550 EE(1)=PSD*TD*(IXB-IYB*SPH12-IZB*CPH12)*(-S2THE)+PSDPHD*IYMZB
01004 4560 I1=CTHE2*S2PH1+TDPHD*(CTHE*(IXB-IYMZB*CPH1)+THE2*.5*STHE*IYMZB
01004 4570 I2=PH1-TPD*(ABAR*ADDP51+BBAR*DBDP51)/LT+FPS1
01005 4580 EE(2)=PSDPHD*CTHE*(IXB-IYMZB*CPH1)+TDPHD*IYMZB*S2PH1+PSID2*.5
01005 4590 I2*THE*(IXB-IYB*SPH12-IZB*CPH12)-TPD*(ABAR*ADATHE+BBAR*DBDTHE+
01005 4600 ZCBAR*DCDTHE)/LT+QTHE
01004 4610 EE(3)=PSD*TD*CTHE*(IXB-IYMZB*CPH1)+PS1D2*(CTHE2*IYMZB*.5*S2PH1)+
01004 4620 I1*THE2*(-.5*S2PH1*IYMZB)-TPD*(ABAR*ADDPH1+BBAR*DBDPH1+CBAR*DCDPH1)/
01006 4630 ZLT*QPH1
01007 4640 CALL PIVERT(DD,EE,3,6,1,EPS,IERSW)
01010 4650 IF(IERSW.EQ.0) GO TO 43
01012 4660 WRITE(10,5) IERSW
01015 4670 S1 FORMAT(/,SX,INCONSISTENT EQUATIONS ON FOREBODY,/,20X,*,IERSW=*,{2)
01016 4680 STOP
01017 4690 43 EE(4)=(FX+TPD*ABAR/LT)/M
01020 4700 EE(5)=(FY+TPD*BBAR/LT)/M
01021 4710 EE(6)=(FZ+TPD*CBAR/LT)/M
01022 4720 GO TO 41
01023 4730 40 CONTINUE
01023 4740 C
01023 4750 C
01023 4760 C
01024 4770 EQUATIONS OF MOTION FOR GENERAL FOREBODY
01026 4780 IF(1.-ABS(STHE)).LT.(EPS1) GO TO 41
01026 4790 DD(1,1)=STHE2*IXB+CTHE2*(IYB*SPH12+IZB*CPH12-IY2B*S2PH1)
01026 4800 I-S2THE*(IYB*SPH1+IX2B*CPH1)
01027 4810 DD(1,2)=CTHE*(IYMZB*.5*S2PH1-IY2B*CPH1)-IXYB*S2C3+IX2B*S2S3
01030 4820 DD(1,3)=-IXB*CC(1,3)+IXYB*CC(2,3)+IXZB*CC(3,3)
01031 4830 DD(1,4)=M*(IXAR*CC(1,2)+YBAR*CC(2,2)+ZBAR*CC(3,2))
01032 4840 DD(1,5)=M*(YBAR*CC(1,1)-YBAR*CC(2,1)-ZBAR*CC(3,1))
01033 4850 DD(1,6)=0.
01034 4860 DD(2,1)=DD(1,2)
01034 4870 DD(2,2)=IYB*CPH12+IZB*SPH12+IY2B*S2PH1
01034 4880 DD(2,3)=IXYB*CPH1-IX2B*SPH1
01037 4890 DD(2,4)=M*(XBAR*CC(1,2)-YBAR*CC(2,2)+ZBAR*CC(3,2))

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01040 489. DD(2,5)=M*(ZBAR*S1S2+YBAR*S1C2S3+ZBAR*S1C2C3)
01041 490. DD(2,6)=M*(ZBAR*CTHE-YBAR*S2S3-ZBAR*S2C3)
01042 491. DD(3,1)=DD(1,3)
01043 492. DD(3,2)=DD(2,3)
01044 493. DD(3,3)=IXB
01045 494. DD(3,4)=M*(YBAR*CC(3,1)-ZBAR*CC(2,1))
01046 495. DD(3,5)=M*(YBAR*CC(3,2)-ZBAR*CC(2,2))
01047 496. DD(3,6)=M*(YBAR*CC(3,3)-ZBAR*CC(2,3))
01050 497. DD(4,1)=DD(1,4)
01051 498. DD(4,2)=DD(2,4)
01052 499. DD(4,3)=DD(3,4)
01053 500. DD(4,4)=M
01054 501. DD(4,5)=0.
01055 502. DD(4,6)=0.
01056 503. DD(5,1)=DD(1,5)
01057 504. DD(5,2)=DD(2,5)
01060 505. DD(5,3)=DD(3,5)
01061 506. DD(5,4)=0.
01062 507. DD(5,5)=M
01063 508. DD(5,6)=0.
01064 509. DD(6,1)=0.
01065 510. DD(6,2)=DD(2,6)
01066 511. DD(6,3)=DD(3,6)
01067 512. DD(6,4)=0.
01070 513. DD(6,5)=0.
01071 514. DD(6,6)=M
01072 515. EE(1)=PSD(0,1)=S2*(ME)+(IXB-1YB*SPI2-1ZB*CPH12+1YZB*S2PH1)
01072 516. 1+2*(C2THE*(1YB*SPI+1XZB*CPH1)+PSDPHD(1-CTHE2)*(S2PH1+1YMZB
01072 517. 2-1YZB*2*(S2PH1)+(S2T*E)*(1YB*CPH1-1XZB*SPI))+TOPHD(CTHE*(1XZB
01072 518. 3-1YMZB+C2PH1-1YZB*2*(S2PH1))+THE2*(STHE*(1YMZB)+.5*S2PH1
01072 519. 5+1XZB*CPH1)+1XZB*CC(3,3)-1XZB*CC(2,3))+PHID2*(-1YB*CC(3,3)
01073 520. EE(2)=PSDPHD(CTHE*(1XZB-1YMZB*CPH1)+BBDPS)/LT+QPSI
01073 521. 1XZB*SPI+1XZB*CPH1)+TOPHD(1YMZB*S2PH1-1YZB*2*(C2PH1)+PSI2*(
01073 522. 2+5*S2TME*(1XZB-1YB*SPI2-1ZB*CPH12+1YZB*S2PH1)-C2THE*(1XZB*SPI
01073 523. 3+1XZB*CPH1)+.5*(2*(1YB*SPI+1XZB*CPH1)-DD(6,2))*G
01073 524. 4+TPD*(ABAR*DDT*E+BBAR*DDTME+CBAR*DDTME)/LT+QTHE
01074 525. EE(3)=PSD(0,CTHE*(1XZB+1YMZB*CPH1)+2*(1YZB*S2PH1)+2*(S2TME*(
01074 526. 1XZB*SPI+1XZB*CPH1)+PSI2*(CTHE2*(1YMZB+.5*S2PH1-1YZB*CPH1)
01074 527. 2+.5*S2TME*(1XZB*CPH1-1XZB*SPI))+THE2*(1-2*(S2PH1+1YMZB+
01074 528. 3C2PH1)-DD(6,3))*G+TPD*(ABAR*DDPSI+BBAR*DDPSI)+CBAR*DDPSI)/LT+QPHI
01075 529. EE(4)=2*(PSD(0,DD(5,2)+PSUPHD(5,3))-PSI2*DD(5,1))+M(2*(
01075 530. 1TOPHD*(YBAR*CC(2C3)-ZBAR*CC(2S3))+THE2*(XBAR*CC(1,1)-YBAR*CC(1S2S3
01075 531. 2-ZBAR*CC(1S2C3))+PHID2*(YBAR*CC(2,1)+Z*AP*CC(3,1)))+FX*TPD*ABAR/LT
01076 532. EE(5)=2*(PSD(0,DD(4,2)+PSDPHD(DD(4
01076 533. 1TOPHD*(-YBAR*CC(2C3)+ZBAR*CC(2S3))+T*E) AN*CC(1,2)+YBAR*CC(1S2S3
01076 534. 2+ZBAR*CC(1S2C3))+PHID2*(YBAR*CC(2,2)+ZBA
01077 535. EE(6)=M(2*(TOPHD*(YBAR*CC(2C3)-ZBAR*CC(2S3))+1*E2*(XBAR*CC(1,3)
01077 536. 1+YBAR*CC(2,3)+ZBAR*CC(3,3))+PHID2*(YBAR*CC(2,3)+ZBAR*CC(3,3))+FZ
01077 537. 2+TPD*CBAR/LT
01077 538. CALL PIVERT(DD,EE,6,6,1,EPS,IERSW)
01100 539. IF(IERSW.EQ.0) GO TO 41
01101 540. WRITE(10UT,51) IERSW
01104 541. STOP
01107 542. *DIAGNOSTIC* THE TEST FOR EQUALITY BETWEEN NON-INTEGERS MAY NOT BE MEANINGFUL.
01107 543. 41 IF(10PAN.EQ.1.) GO TO 42

```

01107	5440	C	EQUATIONS OF MOTION IF NO ADDED MASS IS INCLUDED ON PARACHUTE
01107	5450	C	
01107	5460	C	
01111	5470	C	FF(1,1)=(-PSIPD*STHEP2+S2THEP*(XMYPB-TPD*(ABAR*DAOPSP+BBAR*DBOPSP)/
01111	5480	C	1LY*QPSI)/(IXPB*STHEP2+IYPB*CTHEP2)
01112	5490	C	FF(1,2)=(PSIPD2*5+S2T EP*(XMYPB-TPD*(ABAR*DAOPSP+BBAR*DBOPSP)/
01112	5500	C	ICBAR*DCDTHP)/LT+QTHEP)/IYPB
01113	5510	C	FF(1,3)=(-TPD*ABAR/LT+FXP)/MP
01114	5520	C	FF(1,4)=(-TPD*BBAR/LT+FYF)/MP
01115	5530	C	FF(1,5)=(-TPD*CBAR/LT+FZP)/MP
01116	5540	C	RETURN
01117	5550	C	42 CONTINUE
01117	5560	C	
01117	5570	C	EQUATIONS OF MOTION IF ADDED MASS IS INCLUDED ON PARACHUTE
01117	5580	C	
01120	5590	C	SPI2=SPI2+2
01121	5600	C	CPSIP2=CPSIP2+2
01122	5610	C	S2SPI2=2*S2SPI2+CPSIP
01123	5620	C	C2SPI2=CPSIP2-S2SPI2
01124	5630	C	C2THEP=CTHEP2-STHEP2
01125	5640	C	XP2=XPD+2
01126	5650	C	YP2=YPD+2
01127	5660	C	ZP2=ZPD+2
01130	5670	C	XPDYD=XPD*YD
01131	5680	C	YDZPD=YD*ZPD
01132	5690	C	YDZPD=YD*ZPD
01133	5700	C	XPPSD=XPD*PSIPD
01134	5710	C	XPTPD=XPD*THEP
01135	5720	C	YPPSD=YPD*PSIPD
01136	5730	C	YPTPD=YPD*THEP
01137	5740	C	ZPPSD=ZPD*PSIPD
01140	5750	C	ZPTPD=ZPD*THEP
01141	5760	C	DDP(1,1)=MPL*CTHEP2+CPSIP2+MPS*(SPSIP2+STHEP2+CPSIP2)
01142	5770	C	DDP(1,2)=MLMSP*5+S2PSIP*CTHEP2
01143	5780	C	DDP(1,3)=MLMSP*5+S2THEP*CPSIP
01144	5790	C	DDP(2,1)=DDP(1,2)
01145	5800	C	DDP(2,2)=MPL*CTHEP2+PSIP2+MPS*(CPSIP2+S2PSIP2+STHEP2)
01146	5810	C	DDP(2,3)=MLMSP*5+PSIP2+STHEP
01147	5820	C	DDP(3,1)=DDP(1,3)
01150	5830	C	DDP(3,2)=DDP(2,3)
01151	5840	C	DDP(3,3)=MPL*STHEP2+MPS*CTHEP2
01152	5850	C	EEP(1,1)=2*XPPSD*DDP(1,2)-ZPPSD*DDP(2,3)+MLMSP*(XPTPD+S2THEP
01152	5860	C	1-CPSIP2+YPPSD*C2SPI2-C2SPI*CTHEP2-YPTPD*5+S2THEP*S2PSIP-ZPTPD
01152	5870	C	2C2THEP*CPSIP)-TPD*ABAR/LT+FXP
01153	5880	C	EEP(1,2)=YPPSD*DDP(1,2)+ZPPSD*DDP(1,3)+MLMSP*(XPPSD+C2PSIP
01153	5890	C	1-CTHEP2-XPTPD*5+S2THEP*S2PSIP+YPTPD*S2THEP-S2PSIP2-ZPTPD
01153	5900	C	2S2SPI2+C2THEP1-TPD*BBAR/LT+FYF
01154	5910	C	EEP(3,1)=XPPSD*DDP(2,3)+YPPSD*DDP(1,3)+MLMSP*(-XPTPD+CPSIP
01154	5920	C	1-CTHEP+YPTPD*SPSIP2+C2THEP-ZPTPD*S2THEP1-TPD*CBAR/LT+FXP
01155	5930	C	FF(1,1)=(-PSIPD*STHEP2+S2THEP*(XMYPB-TPD*(ABAR*DAOPSP+BBAR*DBOPSP)/
01155	5940	C	IXPDZPD*DDP(2,3)-YDZPD*DDP(1,3)+XP2-YD2)*DDP(1,2)
01155	5950	C	2-TPD*(ABAR*DAOPSP+BBAR*DBOPSP)/LT+QPSIP)/(IXPB*STHEP2+IYPB*CTHEP2)
01155	5960	C	FF(1,2)=(PSIPD2*5+S2T EP*(XMYPB-TPD*(ABAR*DAOPSP+BBAR*DBOPSP)/
01156	5970	C	1-XPDZPD*DDP(2,3)-YDZPD*DDP(1,3)+XP2-YD2)*DDP(1,2)
01156	5980	C	2-C2THEP-YDZPD*SPSIP2+C2THEP)-TPD*(ABAR*DAOPSP+BBAR*DBOPSP)/
01156	5990	C	YDZPD*DDP(2,3)-YDZPD*DDP(1,3)+XP2-YD2)*DDP(1,2)

```

01157 600* CALL PIVERT(DDP,EEP,3,3,1,EPS,IERSM)
01160 601* IF(IERSM.NE.0) WRITE(10UT,52)
01163 602* IF(IERSM.NE.0) STOP
01165 603* 52 FORMAT(/5X,'INCONSISTENT EQUATIONS ON PARACHUTE',//20X,'IERSM=',
01166 604* 112)
01168 605* FF(3)=EEP(1)
01167 606* FF(4)=EEP(2)
01170 607* FF(5)=EEP(3)
01171 608* RETURN
01172 609* END

```

END OF COMPILATION: 11 DIAGNOSTICS.





```

00110 310
00112 0DIAGNOSTIC THE LIST CONTAINS AN ILLEGAL ITEM.
00112 DATA FLOY
00112 330
00112 0DIAGNOSTIC A LIST IN THE ABOVE STATEMENT IS TOO LONG.
00114 DATA LABELS /ALTI TU DE M
00114 340
00114 350
00114 360
00114 370
00114 380
00114 390
00114 400
00114 410
00114 420
00114 430
00114 440
00114 0DIAGNOSTIC A LIST IN THE ABOVE STATEMENT IS TOO LONG.
00114 DATA I TIME/O/
00114 450
00120 460
00120 470
00125 480
00126 490
00126 500
00126 510
00130 520
00131 530
00132 540
00133 550
00134 560
00137 570
00140 580
00141 590
00142 600
00143 610
00144 620
00145 630
00150 640
00151 650
00152 660
00153 670
00154 680
00155 690
00156 700
00161 710
00162 720
00163 730
00164 740
00165 750
00166 760
00167 770
00172 780
00173 790
00174 800
00175 810
00176 820
00177 830

1
2
3
4
5
6
7
8
9
A
B

DATA I TIME/O/
IF (I,X .LE. 0) GO TO 900
IF (I TIME) GO TO 150
100 CALL IDENT(9,ADARY)
150 I TIME = I TIME + 1

ISYM = 34
FLOX(1) = LABELS(1,IX)
FLOX(2) = LABELS(2,IX)
FLOX(3) = LABELS(3,IX)
FLOX(4) = LABELS(4,IX)
IF (IY1) 550,55C,510
510 CONTINUE
FLOY(1) = LABELS(1,IY1)
FLOY(2) = LABELS(2,IY1)
FLOY(3) = LABELS(3,IY1)
FLOY(4) = LABELS(4,IY1)
CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y1)
IF (IY2) 550,55C,520
520 CONTINUE
FLOY(1) = LABELS(1,IY2)
FLOY(2) = LABELS(2,IY2)
FLOY(3) = LABELS(3,IY2)
FLOY(4) = LABELS(4,IY2)
CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y2)
IF (IY3) 550,55C,530
530 CONTINUE
FLOY(1) = LABELS(1,IY3)
FLOY(2) = LABELS(2,IY3)
FLOY(3) = LABELS(3,IY3)
FLOY(4) = LABELS(4,IY3)
CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y3)
IF (IY4) 550,55C,540
540 CONTINUE
FLOY(1) = LABELS(1,IY4)
FLOY(2) = LABELS(2,IY4)
FLOY(3) = LABELS(3,IY4)
FLOY(4) = LABELS(4,IY4)
CALL QUIK3V(1,ISYM,FLOX,FLOY,N,X,Y4)

```

00200 84 550 CONTINUE  
00201 85 C  
00202 86 900 CONTINUE  
00203 87 RETURN  
00204 88 END

END OF COMPILATION; 9 DIAGNOSTICS.

0FOP,US INTERP  
MSD 11A -03/27/77-0(119128 (0,1))

SUBROUTINE INTERP ENTRY POINT 000113

STORAGE USED: CODE(1) 000125; DATA(0) 0000171 BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

0003 WERR3S

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0000 R 000000 CFI 0000 R 000001 CF2 0000 000002 INJP'S

```
00101 1* SUBROUTINE INTERP(CF,AMSL,ALPSL,PHISL,I,J,J,K,K,I,J,K,CF)
00101 2* C
00101 3* C THREE DIMENSIONAL LINEAR INTERPOLATION TO FIND AERO. COEFF.
00101 4* C
00103 5* DIMENSION CCF(I,J,K,K)
00104 6* CFI=(CCF(I,J-1,K)-CCF(I-1,J-1,K))*PHISL+CCF(I-1,J-1,K)
00104 7* I+(CCF(I,J,K)-CCF(I-1,J,K))*PHISL+CCF(I-1,J,K)-((CCF(I,J-1,K)
00104 8* 2-CCF(I-1,J-1,K))*PHISL+CCF(I-1,J-1,K))*ALPSL
00105 9* CF2=(CCF(I,J-1,K-1)-CCF(I-1,J-1,K-1))*PHISL+CCF(I-1,J-1,K-1)+
00105 10* I+(CCF(I,J,K-1)-CCF(I-1,J,K-1))*PHISL+CCF(I-1,J,K-1)-((CCF(I,
00105 11* 2J-1,K-1)-CCF(I-1,J-1,K-1))*PHISL+CCF(I-1,J-1,K-1))*ALPSL
00106 12* CF=AMSL*(CF1-CF2)+CF2
00107 13* RETURN
00110 14* END
```

END OF COMPILATION! NO DIAGNOSTICS.

FOR US PIVERT  
MSD 11A -03/27/74-00:19:30 (0,1)

SUBROUTINE PIVERT ENTRY POINT 050640

STORAGE USED: CODE(1) 000705; DATA(0) 000111; BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

0003 NERR39

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001	000064	1166	0001	000240	120L	0001	000367	1216	0001	000123	1376	0001	000416	150L	
0001	000205	1576	0001	000232	1766	0001	000451	190L	0001	000275	2056	0001	000371	2176	
0001	000605	220L	0001	000376	2236	0001	000610	230L	0001	000423	2406	0001	000464	2546	
0001	000537	2616	0001	000567	2666	0001	000133	30L	0001	000137	70L	0001	000021	I	
0000	I	000025	11	0000	I	000026	111	0000	I	000016	11	0000	I	000017	12
0000	I	000022	J	0000	I	000020	K	0000	I	000024	K1	0000	I	000014	L1
0000	I	000015	L2	0000	D	000002	ONE	0000	I	000023	L	0000	I	000014	L1
0000	D	000012	TOL	0000	D	000000	ZE O	0000	D	000004	PIV1	0000	D	000010	TB

SUBROUTINE PIVERT(A,R,M,MD,N,EPS,IER)

TO SOLVE A GENERAL SYSTEM OF SIMULTANEOUS LINEAR EQUATIONS. GELG 70  
SOLUTION IS DONE BY MEANS OF GAUSS-ELIMINATION WITH GELG 470  
COMPLETE PIVOTING. GELG 480

DESCRIPTION OF PARAMETERS  
A = THE M BY M COEFFICIENT MATRIX. (DESTROYED)  
R = THE M BY N MATRIX OF RIGHT HAND SIDES. (DESTROYED) GELG 150  
M = ON RETURN R CONTAINS THE SOLUTION OF THE EQUATIONS. GELG 130  
MD = THE NUMBER OF EQUATIONS IN THE SYSTEM. GELG 140  
N = THE DIMENSION OF A GELG 160  
EPS = THE NUMBER OF RIGHT HAND SIDE VECTORS. GELG 170  
IER = AN INPUT CONSTANT WHICH IS USED AS RELATIVE GELG 180  
TOLERANCE FOR TEST ON LOSS OF SIGNIFICANCE. GELG 190  
IER=0 = NO ERROR, GELG 200  
IER=1 = NO RESULT BECAUSE OF M LESS THAN I OR GELG 210  
PIVOT ELEMENT AT ANY ELIMINATION STEP GELG 220  
EQUAL TO 0. GELG 230  
IER=K = WARNING DUE TO POSSIBLE LOSS OF SIGNIFI- GELG 240  
CANCE INDICATED AT ELIMINATION STEP K+1. GELG 250  
WHERE PIVOT ELEMENT WAS LESS THAN OR GELG 260  
EQUAL TO THE INTERNAL TOLERANCE EPS TIMES GELG 270  
ABSOLUTELY GREATEST ELEMENT OF MATRIX A. GELG 280  
GELG 290  
GELG 300  
GELG 310

REMARKS

00101 10  
00101 20  
00101 30  
00101 40  
00101 50  
00101 60  
00101 70  
00101 80  
00101 90  
00101 100  
00101 110  
00101 120  
00101 130  
00101 140  
00101 150  
00101 160  
00101 170  
00101 180  
00101 190  
00101 200  
00101 210  
00101 220  
00101 230  
00101 240  
00101 250  
00101 260  
00101 270

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280 00101      THIS IS A MODIFICATION OF GELG (FROM IBM-SSP)
290 00101      INPUT MATRICES M AND A ARE ASSUMED TO BE STORED COLUMNWISE
300 00101      THE PROCEDURE GIVES RESULTS IF THE NUMBER OF EQUATIONS M IS
310 00101      GREATER THAN O AND PIVOT ELEMENTS AT ALL ELIMINATION STEPS
320 00101      ARE DIFFERENT FROM O. HOWEVER WARNING IER=K - IF GIVEN -
330 00101      INDICATES POSSIBLE LOSS OF SIGNIFICANCE. IN CASE OF A WELL
340 00101      SCALED MATRIX A AND APPROPRIATE TOLERANCE EPS, IER=K MAY BE
350 00101      INTERPRETED THAT MATRIX A HAS THE RANK K. NO WARNING IS
360 00101      GIVEN IN CASE M=1.
370 00101      .....GELG 410
380 00101      .....GELG 420
390 00101      .....GELG 500
400 00101      .....GELG 510
410 00104      DIMENSION A(MD,M),R(MD,N)
420 00105      DOUBLE PRECISION A,R,EPS,ZERO,ONE,PIV,PIV1,TB,TOL
430 00110      DATA ZERO,ONE/0.000,1.000/
440 00110      IF(M)230,230,10
450 00110      SEARCH FOR GREATEST ELEMENT IN MATRIX A
460 00113      C 10 IER = 0
470 00114      PIV = ZERO
480 00115      DO 30 L1=1,M
490 00120      DO 30 L2=1,M
500 00123      TB = DABS(A(L1,L2))
510 00124      IF(TB - PIV)30,30,20
520 00127      20 PIV = TB
530 00130      11 = L1
540 00131      12 = L2
550 00132      30 CONTINUE
560 00135      TOL = EPS*PIV
570 00135      C
580 00135      A(L1) IS PIVOT ELEMENT. PIV CONTAINS THE ABSOLUTE VALUE OF A(L1).
590 00135      GELG 700
600 00135      START ELIMINATION LOOP
610 00136      DO 170 K=1,M
620 00136      C
630 00136      TEST ON SINGULARITY
640 00141      IF(PIV)230,230,40
650 00144      40 IF(IER)70,50,70
660 00147      50 IF(PIV - TOL)60,60,70
670 00152      60 IER = K-1
680 00153      70 PIV1 = ONE/A(L1,L2)
690 00154      J = 11-K
700 00155      I+K IS ROW-INDEX, J+K COLUMN-INDEX OF PIVOT ELEMENT
710 00155      GELG 860
720 00155      PIVOT ROW REDUCTION AND ROW INTERCHANGE IN RIGHT HAND SIDE R
730 00155      DO 80 L=1,N
740 00156      TB = PIV1*R(L1,L)
750 00161      R(L1,L) = R(K,L)
760 00162      80 R(K,L) = TB
770 00163      GELG 870
780 00163      GELG 880
790 00163      C
800 00165      IS ELIMINATION TERMINATED
810 00165      IF(K-M)90,180,180
820 00165      GELG 950
830 00170      COLUMN INTERCHANGE IN MATRIX A
840 00170      CONTINUE
850 00170      GELG 980

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PC171 840
PC174 850
PC175 860
PC200 870
PC201 880
PC202 890
PC202 900
PC207 910
PC204 920
PC207 930
PC210 940
PC211 950
PC211 960
PC211 970
PC213 980
PC213 990
PC213 1000
PC214 1010
PC215 1020
PC216 1030
PC221 1040
PC222 1050
PC225 1060
PC226 1070
PC227 1080
PC232 1090
PC233 1100
PC234 1110
PC235 1120
PC237 1130
PC242 1140
PC245 1150
PC245 1160
PC245 1170
PC245 1180
PC247 1190
PC252 1200
PC253 1210
PC256 1220
PC257 1230
PC260 1240
PC263 1250
PC264 1260
PC265 1270
PC270 1280
PC272 1290
PC273 1300
PC274 1310
PC274 1320
PC274 1330
PC277 1340
PC300 1350
PC301 1360

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IF(J)120,170,190
100 CONTINUE
DO 110 L=K,M
TB = A(L,K)
A(L,K) = A(L,12)
110 A(L,12) = TB
C
C ROW INTERCHANGE AND PIVOT ROW REDUCTION IN MATRIX A
120 DO 130 L=K,M
TB = PIV(A(11),L)
A(11,L) = A(K,L)
130 A(K,L) = TB
C
C SAVE COLUMN INTERCHANGE INFORMATION
A(K,K) = J
C
C ELEMENT REDUCTION AND NEXT PIVOT SEARCH
PIV = ZERO
KI = K+1
DO 160 I=KI,M
PIV = -A(II,K)
DO 150 L=KI,M
A(II,L) = A(II,L) + PIV*A(K,L)
TB=DABS(A(II,L))
IF(TB - PIV)152,150,140
140 PIV = TB
II = I
I2 = L
150 CONTINUE
DO 160 L=I,M
140 R(II,L) = R(II,L) + PIV*R(K,L)
170 CONTINUE
C
C END OF ELIMINATION LOOP
C
C BACK SUBSTITUTION AND BACK INTERCHANGE
180 IF(M-1)230,225,190
190 CONTINUE
DO 210 I=2,M
II = M+1 - I
L = A(II,II) + .F
DO 210 J=I,M
TB = R(II,J)
III = II+1
DO 200 K=III,M
200 TB = TB - A(III,K)*R(K,J)
210 R(II,J) = R(II,J) - TB
220 RETURN
C
C ERROR RETURN
230 JER = .F
RETURN
END

```

6EL61080

6EL61150

6EL61180

6EL61380

6EL61410

6EL61620

END OF COMPILATION; NO DIAGNOSTICS.

OFOR,US DENS  
MSD 11A -03/27/74-00119134 (0.1)

SUBROUTINE DENS ENTRY POINT 000106

STORAGE USED(1) 0001211 DATA(0) 000 011 BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

0003 EXP  
0004 XPRR  
0005 SORT  
0006 MERR33

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001	000011	1216	0001	000022	2L	0001	000050	3L	0001	000060	4L	0000	K	000102	A			
0000	R	000130	B	0000	R	000160	0M	0000	R	000166	M	0000	I	000167	I			
0000	000170	INJPS	0000	R	000026	P8	0000	R	000162	T	0000	R	000054	T8	0000	R	000161	TEMP

00101 SUBROUTINE DENS(Z, P, RHO, CS)  
00102 DOUBLE PRECISION Z  
00103 DIMENSION HB(22), PD(22), TB(22), A(22), B(22)  
00104 DATA HB/0.,.36789239,65616.798,10496.68,15419.48,170603.67,  
00105 1 200131.23,259186.35,291153.40,323032.75,354753.59,386406.39,  
00106 2 480781.04,512046.16,543215.48,655268.46,728243.91,939894.75,  
00107 3 1234619.4,152799.4,1798726.4,268776.6/  
00108 DATA PD/2116.217,472.67922,114.34505,116.12852,2.3162994,  
00109 1 1.2322512,36032173.,021672818.,0034331482.,0062812953,  
00110 2 00015359986.,00005264807.,00010571582.,0000077157071,  
00111 3 000005832472.,0000035196139.,0000145371.,39343987E-6,  
00112 4 84176667E-7,22884174E-7,7205836E-8,24891264E-8/  
00113 DATA TB/28A.15,2216.65,228.65,2270.65,2270.65,252.65,2.180.65,210.65,  
00114 1 260.65,362.65,960.65,1110.65,1210.65,1350.65,1550.65,1830.65,  
00115 2 2150.65,2420.65,2590.65,2700.65/  
00116 DATA A/-.6R755856E-5,0.,.14068775E-5,.37325169E-5,0.,  
00117 -.225230554E-5,.,.M8256481E-5,G.,.52141408E-5,.74757236E-5,  
00118 2 1212079E-4,17.28281E-4,49941997E-5,.28886537E-5,  
00119 3 18635746E-5,1204117E-5,.85314774E-6,.6116347E-6,  
00120 4 42048419E-6,2526889E-6,20.1572315E-6/  
00121 DATA B/5.255886.,.48063102E-4,34.163232,12.201179,.,.38473567E-4,  
00122 1 17.081627,8.540804,.,.57641135E-4,11.055224,.,.6127901,  
00123 2 3.2961763,1.6390858,.,.2174464,3.245879,.,.4.6156949,  
00124 3 6.4033868,7.8733154,.,.9.3039039,11.4627,.,.17.025198,  
00125 4 20.25.562133/  
C

H = 2085531.E02/(2085531.E0 + Z)  
DO 1 I = 2, 22  
IF(H-MB(I),2,1)

```

00126      1      CONTINUE
00130      1 = 23
00131      2 1 = 1 - 1
00132      DH = H - HB(1)
00133      TEMP = 1. + A(1) * DH
00134      T = TB(1) * TEMP
00135      IF(A(1) > 3.613
00140      6 TEMP = EXP(B(1) * DH)
00141      GO TO 4
00142      3 TEMP = TEMPOOB(1)
00143      4 P = PB(1) * TEMP
00144      RHO = .3236414E-3 * P / T
00145      CS = 65.770322E0 * SQRT(1)
00146      RETURN
00147      END

```

END OF COMPILATION: NO DIAGNOSTICS.



0708,US DENSM  
MSD 11A -03/27/79-00119:37 (0.1)

SUBROUTINE DENSM ENTRY POINT 0C9111

STORAGE USED: CODE(1) 000124I DATA(0) 000 061 BLANK COMMON(2) 000000

EXTERNAL REFERENCES (BLOCK, NAME)

- 0003 EXP
- 0004 XPRR
- 0005 SORT
- 0006 MEMR3S

STORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

0001 000C13 1226 0001 00C024 2L 0001 000-52 3L 0001 U00062 4L 000J M 00G104 A  
 0000 R 000132 B 0000 R 000162 DM 0000 R 0C0160 M 0000 R 0C0002 MB  
 0000 000175 INJPS 0000 R 00C030 PB 0000 R 0C0164 Y 0000 R 000056 TB  
 0000 D 000000 Z 0000 R 0C0163 TEMP

00101 1\* SUBROUTINE DENSM(I2, P, RHO, CS)  
 00103 DOUBLE PRECISION L,Z1  
 00104 DIMENSION HB(22), PB(22), TB(22), A(22), B(22)  
 00105 DATA HB/0.,.36289,239.65616,798,104986.88,154199.48,170603.67,  
 00105 2 200131.23,259186.35,291153.40,32302.75,354753.59,386406.39,  
 00105 3 480781.04,512046.16,543215.48,605268.46,6728243.91,939894.75,  
 00105 4 1234619.4,1526799.4,1798726.4,2068776.6/  
 00107 DATA PR/2116.217,472.67922,114.34505,18.128852,2.3162994,  
 00107 1 1.2322512,236032173.,021672818.,0034331482.,00062812953,  
 00107 2 .00015359986.,00005266807.,000010571582.,0000077157071,  
 00107 3 .0000058324672.,0000035196139.,0000145371.,39343987E-6,  
 00107 4 .84176667E-7,22884174E-7,72058936E-8,24891264E-8/  
 00111 DATA TR/28A,15.2,216.65,228.65,2270.65,252.65,2\*180.65,210.65,  
 00111 1 260.65,360.65,960.65,1110.65,11210.65,1350.65,1550.65,1800.65,  
 00111 2 2160.65,2420.65,2590.65,2700.65/  
 00113 DATA A/-.68755056E-5,0.,.14068775E-5,.37325169E-5,0.0,  
 00113 1 -.22523554E-5,4825481E-5,0.,.521440E-5,.74757236E-5,  
 00113 2 .12120769E-4,.17 28281E-4,.49941997E-5,.28886537E-5,  
 00113 3 .18635746E-5,.1204172E-5,.85314774E-6,.6116347E-6,  
 00113 4 .42048419E-6,.25268899E-6,20.1572315E-6/  
 00115 DATA B/5.255886,48063102E-4,-34.163232,-12.201179,.38473567E-4,  
 00115 1 17.081627,0.540804,-57641135E-4,-11.055226,-6.6127901,  
 00115 2 -3.2961763,-1.6390858,-2.1704464,-3.2456979,4.6156949,  
 00115 3 -6.4033868,-7.8733159,-9.3039039,-11.4627,-17.025198,  
 00115 4 20.25.562133/  
 00117 C  
 00117 Z = 2103.28084  
 00120 M = 2085531.E0+2/(2085531.E0 + Z)

```

00121 290 00 1 1 = 2, 22
00124 300 IF(M-NB(1))2,1,1
00127 310 CONTINUE
00131 320 1 = 23
00132 330 2 1 = 1 - 1
00133 340 DM = M - NB(1)
00134 350 TEMP = J. + A(1)*DM
00135 360 T = TB(1)*TEMP
00136 370 IF(A(1))3,6,3
00141 380 4 TEMP = EXP(B(1)*DM)
00142 390 GO TO 4
00143 400 3 TEMP = TEMP*B(1)
00144 410 4 P = PB(1)*TEMP*47.88025
00145 420 RHO = .003483647*P/T
00146 430 CS = 20.04679*SQRT(T)
00147 440 RETURN
00150 450 END
    
```

END OF COMPILATION: NO DIAGNOSTICS.

DEPT,T  
FURPUR 24HI-03/27-00:19

1HNT5V443021\*TPFS ELEMENT TABLE

D NAME	VERSION	TYPE	DATE	TIME	SEN #	SIZE-PRE,ICAT	(CYCLE WORD)	PSRNUDE	LUCATION
PL6DOF		FOR SYMB	27 MAR 74	00:17:00	1	168	5	0	1792
PL6DOF		RELOCATABLE	27 MAR 74	00:17:16	2	204	5	0	1960
SUBR		FOR SYMB	27 MAR 74	00:17:20	3	147	5	0	2166
SUBR		RELOCATABLE	27 MAR 74	00:17:31	4	2	5	0	2313
PLTRAJ		FOR SYMB	27 MAR 74	00:17:33	5	24	5	0	2491
PLTRAJ		RELOCATABLE	27 MAR 74	00:17:35	6	1	5	0	2515
INTERP		FOR SYMB	27 MAR 74	00:17:36	7	5	5	0	2529
INTERP		RELOCATABLE	27 MAR 74	00:17:37	8	5	5	0	2534
PIVERT		FOR SYMB	27 MAR 74	00:17:55	9	41	5	0	2540
PIVERT		RELOCATABLE	27 MAR 74	00:17:58	10	25	5	0	2581
DENS		FOR SYMB	27 MAR 74	00:18:01	11	14	5	0	2607
DENS		RELOCATABLE	27 MAR 74	00:18:03	12	10	5	0	2621
DENSM		FOR SYMB	27 MAR 74	00:18:18	13	14	5	0	2632
DENSM		RELOCATABLE	27 MAR 74	00:18:19	14	11	5	0	2646
A		MAP SYMB	27 MAR 74	00:18:20	15	1	5	0	2650
CHUTE		ABSOLUTE	27 MAR 74	00:18:37	16	868	5	1	2659
PL6DOF		FOR SYMB	27 MAR 74	00:19:03	17	168	5	1	2659
PL6DOF		RELOCATABLE	27 MAR 74	00:19:12	18	204	5	1	3527
SUBR		FOR SYMB	27 MAR 74	00:19:15	19	147	5	1	3695
SUBR		RELOCATABLE	27 MAR 74	00:19:25	20	176	5	1	3901
PLTRAJ		FOR SYMB	27 MAR 74	00:19:26	21	24	5	1	4048
PLTRAJ		RELOCATABLE	27 MAR 74	00:19:27	22	13	5	1	4226
INTERP		FOR SYMB	27 MAR 74	00:19:28	23	5	5	1	4250
INTERP		RELOCATABLE	27 MAR 74	00:19:30	24	5	5	1	4264
PIVERT		FOR SYMB	27 MAR 74	00:19:31	25	41	5	1	4275
PIVERT		RELOCATABLE	27 MAR 74	00:19:34	26	25	5	1	4316
DENS		FOR SYMB	27 MAR 74	00:19:35	27	14	5	1	4342



TRAJECTORY OF A RIGID BODY WITH 6 D.O.F. CONNECTED TO A RIGID PARACHUTE WITH 5 D.O.F. BY AN ELASTIC TETHER

54-FT. DROGUE DEPLOYMENT

IX8	IXY8	XBAR	S	CLLP	OPPRIN	OPSYM	ALPHI	AIPNID	DTI	EPSI
IX9	IXZ8	YBAR	D	CLMQ	OPPLOT	OPDA	AJALPF	AJALPD	TTY	ETAJ
IX6	IXZ8	ZBAR	WEIGHT	CLNR	OPOS	OMETRC	AKAM	AKAMD	HMM	
171149.0	.0	-2.000	116.260	.000	1.	0.	2.	2.	.0100	.0000084
8539000.0	.0	.000	12.1e7	.000	0.	0.	16.	8.	5.0000	.000610
8539000.0	.0	.000	143300.00	.000	1.	0.	6.2	2.	10000.0	

A	LTO	LS	AMAX1	AMAX2	AMAX3	AMAY1	AMAY2	AP	GLOAD	OPAM	PCT01
B	NT	NS	DSX1	DSX2	DSY1	DSY2	CHIPE	CHIPE	FSULT	OPDT	PCT02
C	DLTO	UP	WTC	WTL	WTP	CCRIT	VP	VP	AERATO	OPSP	PCT03
TR0	TR1	TR2	TR3	SPR0	SPR1	SPR2	SPR3				
83.800	6.500	100.000	660.000	16.500	720.000	11.500	63.819	3.000	7.234	1.000	.100
.000	3.000	56.000	150.000	43.000	210.000	52.000	.000	3.000	.100	1.000	.000
.000	.010	54.000	219.000	651.000	870.000	.000	552.303	1.000	.000	1.000	.000
.000	13.000	100.000	100.000	8.000	1879.100	2290.203	.000				

PARACHUTE SUSPENSION LINE LOAD AND STRAIN ARRAYS

PS(18)	.00	1000.00	2000.00	4000.00	6000.00	10000.00	12000.00	12900.00
EPL(18)	.0000	.0230	.0560	.0890	.1090	.1370	.1600	.1800
PT(18)	.00	20000.00	35000.00	60000.00	80000.00	120000.00	160000.00	200000.00
EPT(18)	.0000	.0250	.0500	.0750	.0900	.1100	.1200	.1370

TETHER LINE LOAD AND STRAIN ARRAYS

PARACHUTE INFLATION TIME HISTORY ARRAY, TTIP

.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------

PARACHUTE AERODYNAMIC REF. AREA ARRAY, SSP

.00	.00	.00	.00	.00	.00	.00	.00	.00	.00	.00	.00
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

AERODYNAMIC COEFFICIENTS OF FOREBODY

PPHIE (ROLL ANGLE-DEGREES)

.000 360.000

AALPFE (ANGLE OF ATTACK-DEGREES)

.000 30.000 60.000 80.000 85.000 90.000 95.000 100.000 120.000 150.000 180.000 .000 .000 .000 .000 .000

JALPME (ANGLE OF ATTACK-DEGREES)

.000 30.000 60.000 80.000 85.000 90.000 95.000 100.000 120.000 150.000 180.000 .000 .000 .000 .000 .000

AAM (MACH NUMBER)

.000 .400 .600 .900 1.200 1.960

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .000

.800 .750 .200 .200 .350 .250 .050 -.200 -1.550 -2.400 -.800 .000 .000 .000 .000 .000  
 .800 .750 .200 .200 .350 .250 .050 -.200 -1.550 -2.400 -.800 .000 .000 .000 .000 .000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .400

.800 .750 .200 .200 .350 .250 .050 -.200 -1.550 -2.400 -.800 .000 .000 .000 .000 .000  
 .800 .750 .200 .200 .350 .250 .050 -.200 -1.550 -2.400 -.800 .000 .000 .000 .000 .000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .600

.800 .750 .250 .300 .300 .100 -.350 -1.450 -2.500 -1.350 .000 .000 .000 .000 .000 .000  
 .800 .750 .250 .300 .300 .100 -.350 -1.450 -2.500 -1.350 .000 .000 .000 .000 .000 .000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .900

1.000	.900	.150	.600	.650	.600	.400	.200	-1.400	-2.600	-1.550	.000	.000	.000	.000	.000	.000
1.000	.900	.150	.600	.650	.600	.400	.200	-1.400	-2.600	-1.550	.000	.000	.000	.000	.000	.000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= 1.200

1.550	1.400	.500	.600	.450	.250	.050	-.200	-1.500	-2.850	-2.100	.000	.000	.000	.000	.000	.000
1.550	1.400	.500	.600	.450	.250	.050	-.200	-1.500	-2.850	-2.100	.000	.000	.000	.000	.000	.000

CA (AXIAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= 1.960

1.100	1.200	1.100	.600	.450	.250	.050	-.150	-1.300	-2.700	-2.300	.000	.000	.000	.000	.000	.000
1.100	1.200	1.100	.600	.450	.250	.050	-.150	-1.300	-2.700	-2.300	.000	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .000

.000	3.200	7.600	5.800	5.700	5.700	5.700	5.800	8.200	3.200	.000	.000	.000	.000	.000	.000	.000
.000	3.200	7.600	5.800	5.700	5.700	5.700	5.800	8.200	3.200	.000	.000	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY (IPHI,JALPF,KAM))

MACH NO.= .400

.000	3.200	7.600	5.800	5.700	5.700	5.700	5.600	9.200	3.200	.000	.000	.000	.000	.000
.000	3.200	7.600	5.800	5.700	5.700	5.700	5.800	9.200	3.200	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY(IPHI,JALPF,KAM))  
MACH NO.= .600

.000	3.500	9.600	10.800	10.800	10.700	10.600	10.500	9.500	3.600	.000	.000	.000	.000	.000
.000	3.500	9.600	10.800	10.800	10.700	10.600	10.500	9.500	3.600	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY(IPHI,JALPF,KAM))  
MACH NO.= .900

.000	4.600	14.200	17.400	18.100	18.300	17.900	17.200	13.700	4.300	.000	.000	.000	.000	.000
.000	4.600	14.200	17.400	18.100	18.300	17.900	17.200	13.700	4.300	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY(IPHI,JALPF,KAM))  
MACH NO.= 1.200

.000	5.800	16.500	20.400	20.800	21.000	20.700	20.300	15.900	6.000	.000	.000	.000	.000	.000
.000	5.800	16.500	20.400	20.800	21.000	20.700	20.300	15.900	6.000	.000	.000	.000	.000	.000

CN (NORMAL COEF. ARRAY(IPHI,JALPF,KAM))  
MACH NO.= 1.760

.000	7.200	16.100	20.200	20.600	20.800	20.500	20.000	15.700	6.100	.000	.000	.000	.000	.000
.000	7.200	16.100	20.200	20.600	20.800	20.500	20.000	15.700	6.100	.000	.000	.000	.000	.000

CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .800

.000	5.100	10.000	5.200	4.300	2.500	.200	-2.100	-8.200	-3.600	.000	.000	.000	.000	.000	.000	.000
.000	5.100	10.000	5.200	4.300	2.500	.200	-2.100	-8.200	-3.600	.000	.000	.000	.000	.000	.000	.000

CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	5.100	10.000	5.700	4.300	2.500	.200	-2.100	-8.200	-3.600	.000	.000	.000	.000	.000	.000	.000
.000	5.100	10.000	5.700	4.300	2.500	.200	-2.100	-8.200	-3.600	.000	.000	.000	.000	.000	.000	.000

CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .600

.000	4.700	12.900	10.700	9.200	7.100	4.900	2.600	-8.300	-3.000	.000	.000	.000	.000	.000	.000	.000
.000	4.700	12.900	10.700	9.200	7.100	4.900	2.600	-8.300	-3.000	.000	.000	.000	.000	.000	.000	.000

CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	7.600	23.100	14.000	11.200	8.200	5.300	.800	-9.500	-3.300	.000	.000	.000	.000	.000	.000	.000
.000	7.600	23.100	14.000	11.200	8.200	5.300	.800	-9.500	-3.300	.000	.000	.000	.000	.000	.000	.000

CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.200

.000	8.000	19.000	12.100	10.700	9.400	7.700	6.000	-2.900	-5.700	.000	.000	.000	.000	.000	.000	.000
.000	8.000	19.000	12.100	10.700	9.400	7.700	6.000	-2.900	-5.700	.000	.000	.000	.000	.000	.000	.000



CLM (PITCH MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.960

.000	7.400	10.800	11.400	10.600	9.600	8.400	7.000	2.800	-1.300	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	7.400	10.800	11.400	10.600	9.600	8.400	7.000	2.800	-1.300	.000	.000	.000	.000	.000	.000	.000	.000	.000

CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))

MACH NO.= .000

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))

MACH NO.= .400

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))

MACH NO.= .600

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))

MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

.000 .000

CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))

MACH NO.= 1.200

.000 .000

CY (LATERAL COEF. ARRAY(IPHI,JALPF,KAM))

MACH NO.= 1.960

.000 .000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .000

.000 .000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))

MACH NO.= .400

.000 .000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))  
MACH NO.= .600

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))  
MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))  
MACH NO.= 1.200

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLL (ROLL MOM. COEF. ARRAY(IPHI,JALPM,KAM))  
MACH NO.= 1.960

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN IYAN MOM. COEF. ARRAY(IPHI,JALPM,KAM))  
MACH NO.= .000

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= .600

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= .900

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.200

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

CLN (YAW MOM, COEF, ARRAY(IPHI,JALPM,KAM))

MACH NO.= 1.960

.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000

.000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000  
 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000

### AERODYNAMICS OF PARACHUTE

#### ANGLE OF ATTACK ARRAY (AALPPE(B))

.000 10.000 40.000 90.000 140.000 170.000 180.000 .000

#### MACH NUMBER ARRAY (AAMP(B))

.000 10.000 .000 .000 .000 .000 .000 .000

#### AXIAL COEFF. ARRAY (CCAP(B,B))

.550 .550 .000 .000 .000 .000 .000 .000  
 .500 .500 .000 .000 .000 .000 .000 .000  
 .300 .300 .000 .000 .000 .000 .000 .000  
 .100 .100 .000 .000 .000 .000 .000 .000  
 -.300 -.300 .000 .000 .000 .000 .000 .000  
 -.500 -.500 .000 .000 .000 .000 .000 .000  
 -.550 -.550 .000 .000 .000 .000 .000 .000  
 .000 .000 .000 .000 .000 .000 .000 .000

#### NORMAL COEFF. ARRAY (CCNP(B,B))

.000 .000 .000 .000 .000 .000 .000 .000  
 .050 .050 .000 .000 .000 .000 .000 .000  
 .320 .320 .000 .000 .000 .000 .000 .000  
 1.000 1.000 .000 .000 .000 .000 .000 .000  
 .320 .320 .000 .000 .000 .000 .000 .000  
 .050 .050 .000 .000 .000 .000 .000 .000  
 .000 .000 .000 .000 .000 .000 .000 .000  
 .000 .000 .000 .000 .000 .000 .000 .000

#### PITCH MOM. COEFF. ARRAY (CCMP(6,B))

.000 .000 .000 .000 .000 .000 .000 .000  
 -.050 -.050 .000 .000 .000 .000 .000 .000  
 -.320 -.320 .000 .000 .000 .000 .000 .000  
 -1.000 -1.000 .000 .000 .000 .000 .000 .000

10

-.320	-.320	.000	.000	.000	.000	.000	.000
-.050	-.050	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000
.000	.000	.000	.000	.000	.000	.000	.000



TIML	X	XD	XDD	FX	CA	V	TENS	XP	XPD	XPDD	FAP	CDAP	CMP
TR8	Y	YU	Y00	FY	CN	AM	LT	YP	YD	YPOD	FYP	CNP	AMP
TR9	Z	ZU	Z00	FZ	CL	DYPR	TPD	ZP	ZPD	ZPOD	FZP	TYPB	DYPRP
TR9	PSIE	PSIDE	PSI0DE	GPSI	CLM	ALPE	OMKBE	PSIPE	PSI0PDE	PSP0UDE	GPSIP	TZPB	ALPPE
GAME	THEE	THEDE	THE0DE	QTHE	CLM	PHITE	OHYBE	THEPE	THEPDE	TMPODE	GTHEP	TPDXB	GAMPE
CHIE	PHIE	PHIDE	PHI0DE	GPHI	CLL	PHIAE	OMZBE	K5	CLLP	CLMQ	CLNR	TPDRB	PULAM
MPAL	MPAS	DND	OMAXPB	IXPB	IYPB	SPD	SP	SPRU	SPRL	TINT	TINNY	TFI	XPB0I
.4200	20.	45.876	-7.625	-27309.	.049	545.28	113529.	96.	41.38	-13.98	-10339.	631.144	.000
0.	0.	.000	.000	.000	8.749	.523	12.471	0.	.00	.00	.000	.000	.469
-1195181.	18770.	-543.346	32.453	34862.	.000	196.37	116745.	18857.	-487.00	120.36	120362.	-2364.	157.77
0.	.000	.000	.000	0.	.000	92.710	.000	.000	.000	.000	0.	0.	.031
-85.174	7.536	15.705	77.686	1145181.	4.123	.000	-15.705	274.884	-1.108	-6.814	2364.	5494.	-85.143
.000	.000	.000	.000	0.	.000	.000	.000	19014.	.000	.000	.000	116616.	87.
6.5	2.6	45.21	22097.3	1768.5	37907.0	5427.9	1147.66	1879.10	8.00	.00000	.00000	.53811	552.30
.4300	20.	45.799	-8.117	-27659.	.043	544.94	124111.	97.	41.31	-1.42	-10798.	661.388	.000
0.	0.	.000	.000	.000	8.739	.523	12.803	0.	.00	.00	.000	.000	.469
-1121099.	18765.	-543.011	34.627	34358.	.000	196.16	127302.	18852.	-486.56	-26.00	125964.	-2538.	157.51
0.	.000	.000	.000	0.	.000	92.876	.000	.000	.000	.000	0.	0.	.024
-85.179	7.697	16.512	83.593	1121099.	4.041	.000	-16.512	274.877	-1.173	-6.216	2538.	6363.	-85.147
.000	.000	.000	.000	0.	.000	.000	.000	19692.	.000	.000	.000	127143.	87.
6.9	2.8	47.34	23116.0	1853.1	38360.0	5557.1	1202.78	1879.10	8.00	.00000	.00000	.53811	552.30
.4400	21.	45.716	-8.400	-28024.	.036	544.58	134125.	97.	41.34	7.03	-11317.	692.350	.000
0.	0.	.000	.000	.000	8.728	.523	13.116	0.	.00	.00	.000	.000	.469
-1095795.	18759.	-542.654	36.639	33821.	.000	195.93	137143.	18847.	-487.37	-126.36	132299.	-2710.	158.06
0.	.000	.000	.000	0.	.000	93.051	.000	.000	.000	.000	0.	0.	.016
-85.184	7.867	17.375	89.076	1095795.	3.954	.000	-17.375	274.864	31.234	-5.921	2710.	7284.	-85.151
.000	.000	.000	.000	0.	.000	.000	.000	20272.	.000	.000	.000	136950.	87.
7.4	2.9	49.51	24217.8	1939.7	38832.1	5686.4	1259.00	1879.10	8.00	.00000	.00000	.53811	552.30
.4500	21.	45.631	-8.667	-28405.	.029	544.20	143220.	98.	41.44	11.10	-11882.	724.029	.000
0.	0.	.000	.000	.000	8.716	.522	13.401	0.	.00	.00	.000	.000	.471
-1069230.	18754.	-542.279	38.423	33255.	.000	195.69	145961.	18842.	-488.93	-178.32	139207.	-2890.	159.10
0.	.000	.000	.000	0.	.000	93.235	.000	.000	.000	.000	0.	0.	.008
-85.190	8.045	18.291	93.956	1069230.	3.863	.000	-18.291	274.852	-1.294	-6.171	2890.	8240.	-85.154
.000	.000	.000	.000	0.	.000	.000	.000	20752.	.000	.000	.000	145728.	87.
7.9	3.1	51.74	25386.3	2028.3	39323.8	5815.6	1316.51	1879.10	8.00	.00000	.00000	.53811	552.30
.4600	22.	45.543	-8.916	-28804.	.021	543.80	151200.	99.	41.55	11.04	-12474.	756.418	.000
0.	0.	.000	.000	.000	8.704	.522	13.651	0.	.00	.00	.000	.000	.473
-1041376.	18748.	-541.687	39.948	32663.	.000	195.44	153608.	18837.	-490.78	-185.40	146485.	3137.	160.33
0.	.000	.000	.000	0.	.000	93.429	.000	.000	.000	.000	0.	0.	.000
-85.196	8.233	19.252	98.149	1041376.	3.767	.000	-19.252	274.839	-1.374	-16.085	-3137.	9220.	-85.161
.000	.000	.000	.000	0.	.000	.000	.000	21143.	.000	.000	.000	163331.	87.
8.5	3.4	54.01	26601.1	2118.9	39835.8	5944.8	1375.31	1879.10	8.00	.00000	.00000	.53811	552.30
.4700	22.	45.452	-9.148	-29221.	.014	543.39	158017.	98.	41.65	8.06	-13073.	789.406	.000
0.	0.	.000	.000	.000	8.692	.521	13.865	0.	.00	.00	.000	.000	.474
-1012217.	18743.	-541.481	41.213	32047.	.000	195.18	160081.	18833.	-492.51	-155.75	153906.	3796.	161.49
0.	.000	.000	.000	0.	.000	93.632	.000	.000	.000	.000	0.	0.	.009
-85.202	8.430	20.252	101.653	1012217.	3.666	.000	-20.252	274.824	-1.545	-16.043	-3796.	10212.	-85.167
.000	.000	.000	.000	0.	.000	.000	.000	21456.	.000	.000	.000	15755.	86.
9.0	3.6	56.33	27841.4	2211.8	40368.4	6074.1	1435.41	1879.10	8.00	.00000	.00000	.53811	552.30





TIME	X	Y	Z	PSIL	TREE	PHIE	MPAL	XD	YD	ZD	KDD	FX	CA	V	TENS	XP	KPD	XPDD	FXP	CDAP	P
TXB	YB	ZB	PSIB	TREB	PHIB	MPALB		XD	YD	ZD	KDD	FX	CA	V	TENS	XP	KPD	XPDD	FXP	CDAP	P
-5400	25							44.761	-10.585	-32649	-0.057	540.20	186387	101	40.80	-29.56	-16473	1039.559			.000
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.469
-7697.19	18705	-538.404	46.123					-537.940	46.785	2666.0	0.000	192.89	191451	18793	-483.92	295.58	203051	17431	13934	154.23	
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.197
-85.255	10.395	29.074	117.408					29.074	117.408	728879	2.671	-0.00	-29.074	274.636	-3.183	-22.372	-12431	19376			.85.217
.000	.000	.000	.000					.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.84
143	5.7	74.94	36393.7					74.94	36393.7	3022.4	45434.6	6954.3	1961.77	1879.10	8.00	.00000	.00000	.00000	.53811		552.30
.5600	26							44.545	-11.019	-33726	-0.086	539.31	194009	102	40.50	-30.96	-16763	1077.331			.000
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.464
-728879	18700	-537.940	46.785					-537.940	46.785	25972	0.000	192.58	195500	18788	-480.96	294.18	207261	13934			156.11
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.197
-85.255	10.395	29.074	117.408					29.074	117.408	728879	2.671	-0.00	-29.074	274.636	-3.183	-22.372	-12431	19376			.85.217
.000	.000	.000	.000					.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.84
143	5.7	74.94	36393.7					74.94	36393.7	3022.4	45434.6	6954.3	1961.77	1879.10	8.00	.00000	.00000	.00000	.53811		552.30
.5600	26							44.545	-11.019	-33726	-0.086	539.31	194009	102	40.18	-31.74	-17028	1175.474			.000
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.463
-686607	18694	-537.468	47.499					-537.468	47.499	25972	0.000	192.58	195500	18788	-480.96	294.18	207261	13934			154.23
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.192
-85.270	11.001	31.462	121.307					31.462	121.307	642887	2.364	-0.00	-31.462	274.568	-3.669	-24.910	-15124	22571			.85.234
.000	.000	.000	.000					.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.84
15.1	6.0	76.21	36782.6					76.21	36782.6	3129.6	46156.4	724.3	2031.32	1879.10	8.00	.00000	.00000	.00000	.53811		552.30
.5700	27							44.434	-11.244	-34294	-0.101	538.82	198155	103	40.00	45.76	-13740	1115.348			.000
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.462
-642887	18689	-536.970	48.206					-536.970	48.206	25268	0.000	192.27	195336	18784	-479.75	-692.20	169743	15124			153.48
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.198
-85.270	11.001	31.462	121.307					31.462	121.307	642887	2.364	-0.00	-31.462	274.568	-3.669	-24.910	-15124	22571			.85.234
.000	.000	.000	.000					.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.84
15.1	6.0	76.21	36782.6					76.21	36782.6	3129.6	46156.4	724.3	2031.32	1879.10	8.00	.00000	.00000	.00000	.53811		552.30
.5800	27							44.321	-11.414	-34882	-0.117	538.33	200315	103	40.47	48.12	-13795	1076.945			.000
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.469
-597733	18684	-536.507	48.268					-536.507	48.268	24556	0.000	191.95	200600	18779	-487.02	-750.37	168932	16147			158.19
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.221
-85.278	11.321	32.677	121.519					32.677	121.519	597733	2.201	-0.00	-32.677	274.530	-3.956	-30.489	-16147	13971			.85.250
.000	.000	.000	.000					.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.84
14.3	5.7	74.94	36782.6					74.94	36782.6	3022.4	45434.6	6954.3	1962.02	1879.10	8.00	.00000	.00000	.00000	.53811		552.30
.5900	27							44.206	-11.528	-35491	-0.134	537.85	199456	103	40.94	44.81	-13633	1038.552			.000
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.474
-551209	18678	-536.027	47.661					-536.027	47.661	23843	0.000	191.64	198581	18774	-494.52	-738.12	167987	17243			163.12
0								.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.244
-85.286	11.654	33.886	119.947					33.886	119.947	551209	2.033	-0.00	-33.886	274.487	-4.280	-34.301	-17248	25052			.85.267
.000	.000	.000	.000					.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.000	.83
13.6	5.4	73.72	36782.6					73.72	36782.6	2915.7	44736.2	6954.3	1892.47	1879.10	8.00	.00000	.00000	.00000	.53811		552.30



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