CORE

AUBURN UNIVERSITY

STUDY OF EFFECTS OF UNCERTAINTIES ON COMET AND ASTEROID ENCOUNTER AND CONTACT GUIDANCE REQUIREMENTS

FINAL REPORT

PART I. GUIDANCE AND NAVIGATION STUDIES

Prepared for

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

GEORGE C. MARSHALL SPACE FLIGHT CENTER

Under Contract NAS8-27664

December 15, 1973

AUBURN UNIVERSITY
AUBURN, ALABAMA 36830

ENGINEERING

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Aerospace Engineering Department Auburn University Auburn, Alabama 36830

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Project Director

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AND ASTEROID ENCOUNTER AND CONTACT

GUIDANCE REQUIREMENTS

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PROJECT SUMMARY

At the start of our work in June 1971, three principal tasks were assigned. Slightly restated, these tasks were:

- (i) Develop a deterministic algorithm for guidance to rendezvous with comets and asteroids that can handle expected large target ephemeris errors.
- (ii) Define the problem of determination of rotational state of a tumbling asteroid or cometary nucleus and develop possible schemes for this determination.
- (iii) Investigate possible contact rendezvous schemes including the "harpoon" technique.

During the first year, a detailed investigation of a rendezvous guidance technique based on "encounter theory" was conducted. The definition and formulation of the tumbling problem was made and several possible algorithms phrased. A first investigation of the harpoon problem was conducted and frequencies and acceleration levels identified.

Early in the second year work, a successful deterministic rendezvous guidance algorithm based on optimal control theory was developed. The altorithm was considered sufficiently important that, with agreement of NASA, more emphasis was placed on the rendezvous investigation. To accommodate this work, the harpoon study was set aside. An effort was initiated on the rendezvous navigation problem wherein measurements are made and statistically processed onboard the spacecraft to provide the relative state information required

for input to the guidance algorithm. Expenditures on the contract were low enough so that in June 1972 a no-cost extension of the work to September 1973 was possible. At this time the changes in objective were formalized and principal tasks were restated to include the navigation work (and eliminate the contact-rendezvous and harpoon investigation).

In September 1973, delays caused by installation of a new computing machine at the University prevented generation of final data. The contract completion date was again extended, at no cost, to December 15, 1973, to allow time for this data generation and report preparation.

The final report of our work is presented in two volumes:

Part I. Guidance and Navigation Studies

Part II. Tumbling Problem Studies

Each of these volumes presents the technical details of the analyses conducted, the principal conclusions made, and listing of the computer programs employed, including descriptions of the operation of the programs. Technical abstracts of the work are included in each volume. In Part I, the body of the report reproduces a paper prepared for the AIAA 10th Electric Propulsion Conference entitled "Solar Electric Propulsion for Terminal Flight to Rendezvous with Comets and Asteroids." (AIAA Paper No. 73-1062). The title was changed for inclusion in this report and a few typographical errors were corrected.

STUDY OF EFFECTS OF UNCERTAINTIES ON COMET AND ASTEROID ENCOUNTER AND CONTACT GUIDANCE REQUIREMENTS

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STUDY OF EFFECTS OF UNCERTAINTIES ON COMET AND ASTEROID ENCOUNTER AND CONTACT GUIDANCE REQUIREMENTS

PART I. GUIDANCE AND NAVIGATION STUDIES

Abstract

A guidance algorithm that provides precise rendezvous in the deterministic case while requiring only relative state information is developed. A navigation scheme employing only onboard relative measurements is built around a Kalman filter set in measurement coordinates. The overall guidance and navigation procedure is evaluated in the face of measurement errors by a detailed numerical simulation. Results indicate that onboard guidance and navigation for the terminal phase of rendezvous is possible with reasonable limits on measurement errors.

I. Introduction

Solar electric propulsion (SEP) has been identified as the most promising means of attaining the high dynamical energies that are required for missions to comets and asteroids. However, the continuous nature of SEP complicates trajectory dynamics and introduces difficulties in guidance and navigation of the spacecraft. Handling these difficulties will require formulations that are different from those used for the impulsively corrected ballistic trajectories employed for planetary missions to date. Errors in SEP level and direction will be an important concern also because the errors occur over the whole trajectory and will be difficult or impossible to determine in advance or by direct measurement during flight.

Another problem is that the ephemerides of asteroids, and especially comets, are not as well known as those for the planets. Advance knowledge of the position of a comet such as Encke may be in error by 100,000 km. or more. One reason for this is that comets and asteroids are not observed over their full orbits or in as much detail as are planetary bodies. And the orbits of comets and asteroids of interest are more complex than those of the planets because of perturbative effects along their extended, eccentric orbits. Also, comets are acted upon by non-gravitational solar radiation pressure and electromagnetic force.

The spacecraft may proceed along a nominal path for many months or a few years and when the target can be viewed, it is found that the target is not where it is expected to be. Assuming sufficient control authority to correct for this error, there is then the navigation problem of determining the relative position and velocity of the spacecraft

and target for the generation of terminal guidance commands. While transponders allow the spacecraft to be tracked from the earth with good accuracy, the accuracy of earth-based tracking of the target is much less accurate and relative state cannot be determined with sufficient precision by differencing such earth-based data. It will be necessary to make relative measurements of some kind from onboard the spacecraft to insure successful rendezvous.

So, a central problem is determination of types of onboard measurements that can or need be made. But, this problem is tied to the details of the guidance and navigation algorithms to be used and the two questions must be handled together.

Our investigations have led to a terminal guidance algorithm that gives accurate rendezvous in the deterministic case while employing a knowledge of relative state only. With sufficiently accurate relative state estimation and control, rendezvous is possible without use of ground based measurements. And if onboard systems that fit accuracy, weight, power, and cost requirements are available, a fully autonomous guidance and navigation system is possible. Such a system would eliminate signal delay for deep space targets or time-critical terminal maneuvers and relieve a heavy work load for ground based tracking systems. Very frequent measurements would be available and the accuracy of attainment of terminal conditions improved. There is, of course, the important question of availability of necessary onboard measurement and computation systems. Preliminary considerations indicate that required equipment is probably within the capabilities of present technology. A more definitive enswer to this question can be given after evaluation of possible guidance and navigation schemes has been made and specific system requirements identified.

The objective of this paper is to present an approach to the onboard terminal guidance and navigation problem and some first results that indicate the approach does not require unreasonable onboard equipment.

II. The Guidance Algorithm

Simplicity is a first criteria for an onboard guidance scheme. And second, for comet and asteroid missions, the scheme must be broadly adaptable to off-nominal situations because of expected

ephemeris errors. It would be desirable if the scheme is not based on linearization about a nominal, but could proceed from any state point to the desired terminal conditions.

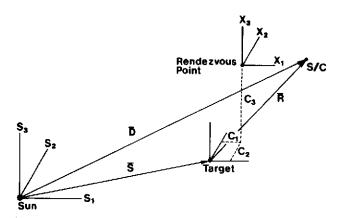


Fig. 1. Rendezvous Geometry.

The geometry and variables used to phrase the rendezvous problem are defined in Figure 1. The mass of most asteroids and certainly of comets is so small that it can be neglected in approach to rendezvous. Appropriate to onboard guidance, the equations of motion are set in coordinates relative to the target:

$$\frac{4}{R} = \bar{F} + GM \left(\frac{\bar{S}}{S^3} - \frac{\bar{D}}{D^3} \right)$$
 (1)

where \bar{F} is the SEP thrust acceleration and G is the universal gravitational constant. The problem is to determine F given the state of the spacecraft and target. An important simplification would be had if F could be specified knowing only the relative state of spacecraft and target. Of course, the dynamics of the problem are not fully specified by just relative state, but as will be found, this simplification is possible in a practical sense. The size of the sun's gradient effect as expressed in the second term on the right of Eq. (1) is the critical factor. In general, this term is larger the farther the spacecraft is from the target and the closer the target is to the sun. If we consider a target position of about 1 to 1.5 a.u. from the sun and a spacecraft position of 1.5 \times 106 to 2.0 \times 106 km. from the target at rendezvous, then the gradient force is of order 10^{-5} to 10^{-6} g's. Expected maximum SEP levels are about 10-4 g's. So, it is not unreasonable to ignore the gradient effect as a first approximation. The gradient effect could, of course, be included as a thrust separately calculated from approximate knowledge of the target ephemeris. In either case, the guidance problem reduces to free space and can be

handled by a number of available mathematical approaches. These ideas are not new, having been previously employed by Cherry for lunar orbits.(3)

Written out in rectangular coordinates centered at the rendezvous point, the equations of motion are

$$\dot{x}_{1} = x_{4}$$

$$\dot{x}_{2} = x_{5}$$

$$\dot{x}_{3} = x_{6}$$

$$\dot{x}_{4} = F_{1} + \frac{GM}{S^{3}} [S_{1} - D_{1} (S/D)^{3}]$$

$$\dot{x}_{5} = F_{2} + \frac{GM}{S^{3}} [S_{2} - D_{2} (S/D)^{3}]$$

$$\dot{x}_{6} = F_{3} + \frac{GM}{S^{3}} [S_{3} - D_{3} (S/D)^{3}]$$

where the subscripts indicate components in the corresponding coordinate directions. M is the mass of the sun. In the spirit of approximation discussed above, the gravitational gradient terms on the right of the last three of Eqs. (2) are dropped. The remaining equations are linear, describing just a free space motion under the action of controls F1, F2, F3. With SEP thrust, a most meaningful criteria for choosing these controls is to minimize their time integrated square.

$$J = \int_{T_0}^{T_f} (F_1^2 + F_2^2 + F_3^2) dt = minimum$$
 (3)

With this starting point, the solution was determined by Abercrombie. (4) The method was essentially the same as employed by several others on related problems, and is a standard procedure from optimal control theory. (5) The result is

$$\begin{split} F_1 &= \left[\frac{6}{\tau_o^2} \left(1 - \frac{2\tau}{\tau_o}\right)\right] x_{10} + \left[\frac{2}{\tau_o} \left(1 - \frac{3\tau}{\tau_o}\right)\right] x_{10} \\ F_2 &= \left[\frac{6}{\tau_o^2} \left(1 - \frac{2\tau}{\tau_o}\right)\right] x_{20} + \left[\frac{2}{\tau_o} \left(1 - \frac{3\tau}{\tau_o}\right)\right] x_{50} \\ F_3 &= \left[\frac{6}{\tau_o^2} \left(1 - \frac{2\tau}{\tau_o}\right)\right] x_{30} + \left[\frac{2}{\tau_o} \left(1 - \frac{3\tau}{\tau_o}\right)\right] x_{60} \end{split}$$
 (4)

where the X_{10} , etc., are the initial conditions and τ = T_f - T is the time to go. Note that the thrust components vary in a simple linear way with time.

The guidance algorithm expressed in Eq. (4) was evaluated with double precision digital simulation. Assuming a deterministic situation in which state is known initially, the full equations of motion, Eqs. (2), were integrated for a period (the guidance interval) with controls specified by Eq. (4). Because of the approximations made in obtaining the free space equations, the true state differs from the free space solution. At the end of the

guidance interval, perfect navigation is assumed, the algorithm is updated with the new, true state, and another period flown. This procedure is repeated until rendezvous is obtained or the path diverges. Simulations were run for typical missions to comets Encke, D'Arrest, and Kopff. Initial conditions were taken from mission studies made by Friedlander.(6) Update periods from continuous to 5 days were employed. The singularity in the algorithm when time to go becomes zero was avoided by pushing time to go ahead two guidance intervals at the end of the trajectory. The time to go push was continued after rendezvous in the case of Encke to examine station-keeping properties of the algorithm. The initial conditions were varied over ranges of 10 degrees in direction of relative velocity, 10 percent in magnitude of relative velocity, and 100,000 km. in position to represent initial target ephemeris errors.

In no case was divergence of the trajectory found. The trajectories were essentially straight line approaches to the rendezvous point. Because of the crude time to go push, there were overshoots of the rendezvous points, but accurate rendezvous was obtained within one or two days of the prespecified time (40 days). In later computer runs, the overshoot has been completely eliminated by reduction of the guidance interval to 0.1 day and the time to go push to one such guidance interval. The spacecraft then performed small oscillations about the rendezvous point that increased slightly as target periapsis was approached and decreased after periapsis. For Encke, with a guidance update of 0.5 days, an overshoot of about 40 km. was obtained for a rendezvous standoff distance of 100 km. in each coordinate direction. After 40 days from guidance initiation, slow oscillations of a few meters amplitude near the rendezvous point occurred. The amplitude increased to somewhat less than 500 meters near periapsis at 100 days and decreased to a few meters by 165 days. Better time to go management would improve these results. The thrust levels during station keeping were extremely low; smaller than 0.5×10^{-8} g's. Fig. 2 shows typical thrust histories for the approach phase for the three comets. It was concluded that the free space optimal control algorithm performed well enough deterministically to warrant investigation with simulation of a realistic navigation scheme.

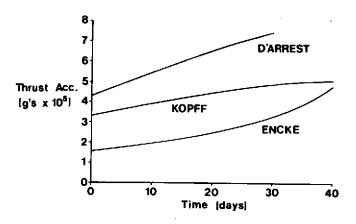


Fig. 2. Rendezvous thrust histories.

III. Navigation Scheme

A Kalman filter was chosen for forming state estimates from onboard measurements. Among the difficulties of practical use of the Kalman filter are two problems that arise because of the linear nature of the Kalman formulation. First, linearization of the system equations leads to a modeling error and it is possible that the first estimate of a new state based on linear propagation from a previous state may not be good enough for the procedure to find a good statistical correction to the first estimate. Second, the formulation requires a linear relation between the physical quantities measured and the system state. Such linear relation is not the usual case and direct linearization of the true relations can lead to serious errors especially when state is not close to estimated values. Either of these problems can produce unsatisfactory performance or divergence of the filter. The problems have been discussed extensively in the literature and there are many ways of handling them.(7,8) We will focus on an approach that is simple from the computational point of view.

The question of modeling error was first examined. A filter in which the measurements were taken as the state variables themselves was programmed for digital computation. Numerical simulation exhibited strong divergence. This was attributed to the usual fact that the filter rapidly reduces the state covariances and thus essentially ignores new measurements as they are made. At this point, one standard fix is to insert noise into the basic system equations. We took an even simpler approach and froze the state covariance matrix after 5 to 10 guidance cycles. This technique worked extremely well. Starting with gross initial errors of 10 percent of the relative state elements (200,000 km, and 150 m/sec.), rendezvous was attained with position errors of about 5 km. and velocity errors of about 0.1 m/sec. This was accomplished with the previous, crude, two-step time-to-go push. We concluded modeling error would be manageable even if requiring a more sophisticated approach in a final formulation.

A method of Mahra(⁹) was chosen to handle the state-measurement relation problem. In his approach, the filtering process is carried out directly in what we term measurement variables. The system state is transformed from the rectangular coordinates used for the guidance problem to new variables, some of which are the measurement quantities themselves. A one-to-one relation between state description and measurements then exists. However, this approach does, as we will see, introduce certain other approximations into the statistics, but, as results show, these are not critical.

The measurement variables vector is taken as $y = (R u v \dot{R} \dot{u} \dot{v})^T$, where u and v are the direction cosines for X_1 and X_2 . The transformation from state variables y = g(X) is

$$R = [(x_1 + c_1) + (x_2 + c_2) + (x_3 + c_3)]^{\frac{\pi}{2}}$$

$$u = (x_1 + c_1)/R$$

$$v = (x_2 + c_2)/R$$

$$\dot{R} = [(x_1 + c_1)x_{l_1} + (x_2 + c_2)x_5 + (x_3 + c_3)x_6]/R$$

$$\dot{u} = (x_{l_1} - \dot{R}u)/R$$

$$\dot{v} = (x_5 - \dot{R}v)/R$$
(4)

The inverse transformation X = l(y) is

$$X_{1} = uR - C_{1}$$
 $X_{2} = vR - C_{2}$
 $X_{3} = wR - C_{3}$
 $X_{4} = R\dot{u} + \dot{R}u$
 $X_{5} = R\dot{v} + \dot{R}v$
 $X_{6} = R\dot{w} + \dot{R}w$
(5)

where, $w^2 = 1 - u^2 - v^2$

Any desirable subset of y can be chosen as the actual measurements: range R; direction cosines u and v; range rate R, etc. The filter process then proceeds as follows. Starting with a best state estimate $\hat{X_k}$ at time T_k , a first estimate X^\dagger at time T_{k+1} is formed by a linear extrapolation through the state transition matrix ϕ for the linearized system

$$\mathbf{x}_{k+1}^{\dagger} = \phi_k \, \hat{\mathbf{x}}_k \tag{6}$$

where,

$$\phi_{k} = \begin{bmatrix} \alpha_{k} & 0 & 0 & \beta_{k} & 0 & 0 \\ 0 & \alpha_{k} & 0 & 0 & \beta_{k} & 0 \\ 0 & 0 & \alpha_{k} & 0 & 0 & \beta_{k} \\ \gamma_{k} & 0 & 0 & \delta_{u} & 0 & 0 \\ 0 & \gamma_{k} & 0 & 0 & \delta_{k} & 0 \\ 0 & 0 & \gamma_{k} & 0 & 0 & \delta_{k} \end{bmatrix}$$

$$(7)$$

and

$$\alpha_{k} = \frac{\tau_{k+1}}{\tau_{k}} \left[3(\frac{\tau_{k+1}}{\tau_{k}}) - 2(\frac{\tau_{k+1}}{\tau_{k}})^{2} \right]$$

$$\beta_{k} = \tau_{k+1} \left[(\frac{\tau_{k+1}}{\tau_{k}}) - (\frac{\tau_{k+1}}{\tau_{k}})^{2} \right]$$

$$\gamma_{k} = -\frac{6}{\tau_{k}} \left[(\frac{\tau_{k+1}}{\tau_{k}}) - (\frac{\tau_{k+1}}{\tau_{k}})^{2} \right]$$

$$\delta_{k} = 3(\frac{\tau_{k+1}}{\tau_{k}})^{2} - 2(\frac{\tau_{k+1}}{\tau_{k}})$$
(8)

with the time to go given by

$$\tau_{k} = T_{F} - T_{k}$$
, $\tau_{k+1} = T_{F} - T_{k+1}$ (9)

We then transfer to the measurement variables with Eq. (4) in the form

$$y^{\dagger} = g(x^{\dagger}), \text{ (nonlinear)}$$
 (10)

The best estimate of the state at T_{k+1} is then given by Kalman's relation

$$\hat{y}_{k+1} = y_{k+1}^{\dagger} + K_{k+1} \left(z_{k+1} - H y_{k+1}^{\dagger} \right)$$
 (11)

where z_{k+1} are the actual measurements, H is a rectangular matrix of ones and zeros that picks from the y_{k+1}^+ vector those elements that correspond to the actual measurements, and K_{k+1} is the Kalman gain (yet to be calculated). We then transform back to the state variables with Eq. (5) in the form

$$\hat{\mathbf{x}}_{k+1} = \mathbf{t}(\hat{\mathbf{y}}_{k+1}), \quad (nonlinear)$$
 (12)

The Kalman gain is calculated by

$$K_{k+1} = M_{k+1/K} H^{T} (H M_{k+1/k} H^{T} + N)^{-1}$$
 (13)

where N is a diagonal square matrix of the variances of the measurement errors and $M_{k+1/k}$ is the transferred covariance matrix of measurement variables calculated by

$$\mathbf{M}_{\mathbf{k}+\mathbf{1}/\mathbf{k}} = \psi_{\mathbf{k}} \ \mathbf{M}_{\mathbf{k}/\mathbf{k}} \ \psi_{\mathbf{k}}^{\mathbf{T}} \tag{14}$$

where, ψ_k is the state transition matrix for the measurement variables and $\text{M}_k/_k$ is the measurement variables covariance matrix at T_k . (Note that no state disturbance has been included) It is here in the construction of ψ_k that approximations are made. Mahra observed that

$$\psi_{\mathbf{k}} = \langle \begin{array}{c} \frac{\partial \mathbf{y}_{\mathbf{k}+1}}{\partial \ \mathbf{y}_{\mathbf{k}}} \end{array} \rangle \langle \begin{array}{c} \frac{\partial \mathbf{y}_{\mathbf{k}}}{\partial \mathbf{x}_{\mathbf{k}}} \end{array} \rangle \langle \begin{array}{c} \frac{\partial \mathbf{x}_{\mathbf{k}}}{\partial \mathbf{y}_{\mathbf{k}+1}} \end{array} \rangle$$

or,

$$\psi_{k} = \left(\frac{\partial g}{\partial x}\right)_{k+1} \Phi_{k} \left(\frac{\partial \ell}{\partial y}\right)_{k} \tag{15}$$

The matrices ($\partial L/\partial y$) and Φ_k are available from the best estimate of state at T_k . To form $(\partial g/\partial x)_{k+1}$, we use the first estimates at T_{k+1} obtained by linear extrapolation from T_k . The matrices $(\partial L/\partial y)$ and $(\partial g/\partial x)$ are not written out here. They can be found in Mahra's paper. (9) All that remains is to propagate the covariances to the next time and this is done with the usual relation

$$M_{k+1/k+1} = (I - K_{k+1} H) M_{k+1/k}$$
 (16)

IV. Guidance and Navigation Evaluation Procedure

Performance evaluation of the overall guidance and navigation scheme requires accurate numerical simulation. A covariance analysis alone will not suffice because of the nonlinearities of the basic dynamics. Fig. 3 is a schematic of the procedure

employed. Starting at a time T_k , an estimate of the state \hat{x}_k is presumed available. For evaluation, the exact state x_k is also specified at this time. The estimate \hat{x}_k is put into the guidance law

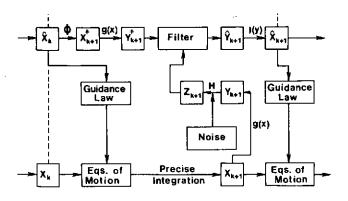


Fig. 3. Evaluation Scheme

to generate the SEP thrusting to be used. The equations of motion including the full effect of the sun and Keplerian motion of the target are then integrated accurately (fourth-order Runge-Kutta) to a time T_{k+1} when measurements will be available. The integrated state x_{k+1} is then transformed to measurement variables and appropriate noise added to simulate actual measurements \mathbf{z}_{k+1} . To represent the onboard computations, the state \hat{x}_k is propagated to time T_{k+1} through the transition matrix Φ_k . The nonlinear transformation g(x) to measurement variables is then made to give a first estimate y[†]. The Kalman gain is then calculated with Eqs. (13), (14), (15). The filtered estimate \hat{y}_{k+1} is then made with Eq. (11). This estimate is then transformed nonlinearly with $\ell(y)$ to obtain the new state estimate \hat{x}_{k+1} . And so on. The computer program for these computations has been given the acronym GANDER for Guidance and Navigation Development and Evaluation Routine.

V. Results

The computations for deterministic evaluation of the guidance algorithm were initiated at ranges as large as 2 × 106 km. However, such ranges are not possible for onboard range and range rate measurement with equipment that fits reasonable weight or power requirements. We could find no information that gives specific distance and accuracy limits for various weight and power allotments except at ranges less than 2000 km.(10) Several discussions led us to believe that 50,000 km. range and 10 measurements per day are conservative limits. At 50,000 km., optimal trajectory studies (6) and our deterministic investigations indicate relative velocity of 20,000 km/day is appropriate. The 50,000 km. range and 20,000 km/day relative velocity correspond to a point in time about 5 days before rendezvous.

Since specific accuracies could not be identified, we conducted evaluations with two assumed measurement error sets representing accurate and rough measurements. Angular measurements from onboard science TV gives accuracies of about 20 arc seconds.(1,2) To allow for onboard implementation, we chose twice this level of error for the angular measurements (.0002 radians or 41.3 arc sec). This and other error levels used are shown in Table 1.

Table 1. Measurement error sets

| SET I | SET II |
|--------------|--------------|
| 41.3 arc sec | 41.3 arc sec |
| .002 Range | .03 Range |
| 4.63 cm/sec | 1.15 m/sec |
| | 41.3 arc sec |

The remaining information necessary before evaluations can be made is the error in relative state information between spacecraft and target. It is obvious if final phase of terminal guidance is initiated at 50,000 km., that an ephemeris error of 100,000 km. (such as for Encke) cannot be tolerated. A preliminary study of onboard prefinal phase orbit determination indicates an improvement of relative position knowledge by as much as a factor of 20 by use of onboard relative angular measurements only. This result was obtained on the basis that the principal error in target ephemeris is time of periapsis passage. We assumed half of the estimated improvement and used 10,000 km. error in each position component. An error of 1000 km/day (11.5 m/sec) was assumed in each velocity component. The initial state covariance was constructed using these values as the standard deviations.

In initial computer runs, a gross filter divergence was found as expected. The divergence is obviously due to the modeling error introduced by approximations in the system dynamics. The covariance matrix rapidly decreased in size and new measurements were not weighted enough. One method of handling this problem is to introduce process noise directly into the differential equations. This has worked quite successfully before (1,2) but does introduce additional complexity in filter computations. A constant or adjustable matrix could also be added to the covariance matrix to control size of the principal elements. A nearly equivalent procedure was decided upon. After several guidance cycles, the covariance matrix had reduced in size considerably and we simply "froze" the matrix at this point. Results showed that a "freeze" after 10 guidance cycles or one day gave reasonable results. Certainly, this procedure is conservative. Of course, a procedure for better management should be developed for any actual system. But, our objective is a first evaluation and if reasonable results can be obtained with the crude freeze, then only improvement can be expected with further development.

The navigation errors for the two data sets are shown in Figs. 4 and 5. A standard computer routine was used to generate noise to simulate

actual measurements. Different error sequences were used for each data type. Three different groups of the two runs for the accurate and rough data sets were investigated. There were no great differences in the results for the three groups. All groups were targeted at a point 100 km. in each coordinate from the target.

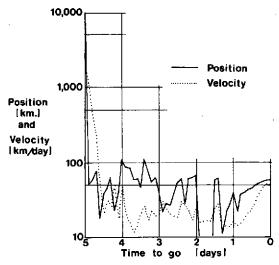


Fig. 4. Navigation Errors for Data Set I

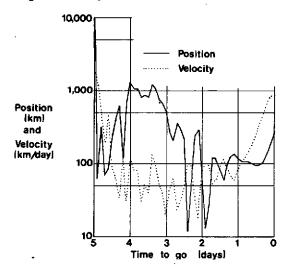


Fig. 5. Navigation Errors for Data Set II

For the accurate data Set I, the terminal rendezvous errors were about 58 km. and 50 km/day (0.58 m/sec). For the rough data Set II, the corresponding numbers were 280 km. and 860 km/day (10.0 m/sec). An exemination of the error histories indicates, however, that much better results could be obtained with better statistical management. After initiation of the procedure at 5 days time to go, there is a rapid decrease in error from the initial values of 17,320 km. and 1732 km/day. It would seem that a better freeze time than 1 day could have been chosen. But, again, we were not interested in forcing the results. By a time of about one day before rendezvous, the errors settled down to about 15 km. and 25 km/day for the accurate Set I and to about 100 km. and 100 km/day for the rough Set II. After this time there is what appears to be a filter divergence to the final values. Examination of the differences in the

extrapolated first state values and the filtered estimates confirm this is the case. No serious attempt was made to correct this divergence since the freezing procedure would probably not be used in any actual implementation.

The SEP thrust accelerations required for the two data sets are given in Fig. 6. The levels do not exceed values that are reasonable for proposed SEP systems. For the accurate Set I, the thrust is essentially constant over the whole period with deviations of only about the 5% error that may be expected from the SEP thrustors. For the rough SET II the deviations are larger but not extreme. The initial lower value arises because on the first few guidance cycles the vehicle does not know where it is. The increase during the last half day also

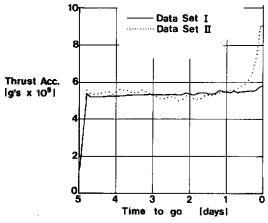


Fig. 6. Thrust Histories

arises because of navigation error. Examination of the detailed trajectories shows that the vehicle is on track to rendezvous. The filter problem near rendezvous discussed in the previous paragraph is the cause of thrust increase. In the sample data form in which the guidance equations are written, there is no numerical singularity except at rendezvous. In the case of the rough data Set II, fixing the thrust at a constant value of about 5.5×10^{-6} actually leads to more accurate rendezyous than following the incorrect filter estimates during the last half day, indicating the terminal point control problems may be helped by reducing frequency of guidance updates near the end of the trajectory so as to avoid small corrections in very small time. The nearly constant SEP level over most of the path also indicates a reduced guidance update frequency may be possible or desirable there as well.

VI. Conclusions

The filtering procedure used was certainly not the best that can be envisioned. Addition of process noise, or a basic improvement in the extrapolation of estimated state would give major improvement of results. Also, the study did not include errors in the SEP thrust level. But thrust level changes due to navigation errors were as large or larger than the 5% expected with the SEP thrustors. Of course, the SEP errors must be included in any more detailed analysis. We

conclude that onboard navigation is possible without unreasonable accuracy requirements for onboard measuring equipment. But further investigation is clearly necessary to obtain definitive results.

For further study we suggest that the following be done:

- 1. Investigate methods of reducing modeling error with emphasis on ease of onboard implementation.
- 2. Include SEP thrust errors and a constraint for constant thrust level and direction rather than the linearly varying model now employed. Errors may be handled as noise or perhaps estimated as new state variables in the filtering process.
- 3. Investigate methods of thrust level control not only at the end point, but during the whole terminal phase. While excessive thrust was never encountered in our investigation, other missions may have to contend with gross off-nominal conditions that can call for excessive thrust unless an automatic control is incorporated in the procedure.
- 4. Investigate onboard methods of target orbit determination that will reduce the target ephemeris uncertainties.
- 5. Investigate the possibility of dispensing with some of the measurements used here with the objective of simplifying onboard systems.
- 6. Determine instrument capabilities, power requirements, weight, etc., for onboard measurements up to ranges of at least 50,000 km. and further, if possible.

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APPENDIX - COMPUTER PROGRAM GANDER

General Program Description

The GANDER Program is written in FORTRAN IV and used with the IBM 370/155. The program is a research tool, not a developed production routine. The steps in the simulation and the names of the subroutines that carry out these steps are as follows.

A fourth order Runge-Kutta subroutine, RUNKUT, is used to integrate the dynamic forces in GOFZ\$ over subintervals of length DT, at each time step (DELT), observations are taken in OBSERV and the filter is used to predict the state in FILTER. The information generated is then put out on Unit 6 and terminal conditions are checked in CYCLOT. Program sequencing and execution is controlled by subroutine CYCLE. Subroutine TARGET is used to generate the comet's position. The name, NOISE, is a dummy name for the functions URAND (Uniformly distributed random numbers) and GRAND (Gaussian distributed random numbers). Ten (10) independent noise channels are shared by these two functions.

Subroutine Names and Descriptions

- MAIN · Reads in system data and calls CYCLE.
- CYCLE · Controls sequence of operation and transfer of data between XT and SP.
- RUNKUT Fourth Order Runge-Kutta Integrator.

 Dynamics are provided by DOFX\$ and
 guidance by GOFX\$. Called by CYCLE.

 Performs N integrations of step size
 DT at each call.
 - Entries:
 RKINIT called by CYCLE.
 Initialize internal variables and read in XT.
- DOFX\$ Compute contribution of dynamics to X.

 J is the index of the components of
 XT.

Entries:

DOFX\$: Compute data to be used by all components.

DOFX: Compute each component.

DXINIT: Initialize internal constants and read in comet data.

SPECIAL - Calls target for comet position.

- GOFX\$ Same as DOFX\$ except XP is used as variable. May call GRAND.
- FILTER User supplied algorithm to calculate XP. (Basic Kalman filter used in present listing)
 - Entries: FLINIT: Used to initialize arrays.

SPECIAL: Variable ICMT is used to bypass covariance update section after preselected number of cycles. Calls MINV

OBSERV . Generates ZT; may call GRAND.

CYCLOT • Outputs data and checks for end of run.

• Entries:

CYCLOT: Output data

TERMIN: Check for end conditions satisfied.

RECAP: If end conditions satisfied; output minimum normed distance, velocity and associated times.

CYINIT: Initialize internal constants.

- TARGET . Comet's position by solution of Kepler's Equation.
- MINV Gaussian elimination inversion routine.

 SPECIAL writes square (nxn) matrix as a vector of length n². (Modified TBM SSP)
- GRAND Generates Gaussian distributed random noise with given mean (RMEAN) and standard deviation (STDDEV).
- ISCNT · Noise channel number. Calls URAND.
- URAND Generates random numbers over the interval [0,1]. (Modified IBM SSP).

BLOCK DATA initializes seed numbers for URAND

Variable Names and Definitions

XT True state vector.

XP Predicted state vector (loaded in GXINIT)

XE XT-XP error in state

ZT True observations

ZP Predicted observations

ZE ZT-ZP error in observations (RESIDUALS)

L\$L One BYTE logical array used to control sequencing of simulator (partially implemented).

L\$E One BYTE logical array for use by error monitor (Experimental program control, not implemented).

DT Integration stepsize (true position).

DELT Guidance update stepsize (predicted position) must be an INTEGRAL multiple

| n | DELT/DT (an integer (exactly)) |
|-------|---|
| TI | Integration start time |
| IF | Integration end time |
| ISLEN | Number of elements in the state vector (XT and XP). |
| IOLEN | Number of elements in the observation vector (ZT and ZP). |
| C | Rendezvous stand-off distance. |
| A | Target semi-major axis |
| RN | Target mean motion. |
| EPS | Target eccentricity. |
| EO | Target eccentric anomaly. |
| TSTAR | Guidance initiation time. |

Input Data

| ARD NO | . CONTENTS | FORMAT | READ BY |
|--------|----------------------------------|--------------|-------------|
| | REQUIRED SYSTE | M DATA | |
| ı | Title Card | 5 A 8 | Main |
| 2 | Run Time Logical Flags (L\$E) | 80L1 | Main |
| 3 | Run Time Error Flags | 80L1 | Main |
| 14 | N. ISLEN, IOLEN | 813 | <u>Main</u> |
| 5 | TI, TF, DT, DELT | 8F10.0 | Main |
| | USER DA | [A | |
| 6 | XT (initial condi- tions) | - 8F10.0 | RKINIT |
| 7 | A,RN,EPS,EO,TSTAR | 8F10.0 | DXINIT |
| Ė | C | 8F10.0 | DXINIT |

Subroutine Initialization Entries

| SUBROUTINES A | ND |
|---------------------------|--|
| LINE NUMBERS | ENTRY |
| GXINIT(J) 34, 35, 36 | Initial position error, kilometers. |
| 37, 38, 39 | Initial velocity error, km/day. |
| FLINIT | Initial covariance matrix (diagonal |
| | elements only in present listing). |
| OVINIT 61 | Standard deviation of angular measurement error (EANG) |
| 62, 63 | Fix logical if statements. Do not change (RMIN and RDMIN). |
| OBSERV | |
| 16, 17, 28, 34, 40, 46 | Mean, St'd. Dev., noise channel (To generate rendom numbers form GRAND). Ten noise channels available. |
| 27, 45 | Range error Std. dev. RFRAF(1) |
| 33, 39 | Range rate error, std. dev. RFRAF RFRAF(4). |
| FILTER 141 | Number of guidance steps before covariance freeze (10 steps in present listing). Remove card for no freeze. |

GANDER Program Listing

| FORTRAN IV | G LEVEL 2L MAIN | |
|--------------|--|---|
| 0001 | IMPLICIT REAL*8 (A-H,O-Z) | |
| 0002 | LUGICAL*1 L\$L,L\$E,LMON,LF,LT | |
| 0003 | CUMMDN/V\$RBLE/XT(6),XP(6),XE(6),ZT(6),ZP(6),ZE(6) | • |
| 0004 | COMMON/T&MER/DELT.DT.TIME.TI.TF.N.ISLEN.IOLEN | |
| 0005 | COMMON/SYSTEM/LSL(40); LSE(10) | |
| J006 | COMMONATIFICE TO COMMON TO | |
| 0007 | COMMUNINUISE/IRAN(10),DG(10),RFRAF(6) | |
| 3008 | COMMUN/JFFSET/C(3) | |
| บังเวิร | DIMENSION &(4,6),RN(4,4),T6(4,4) | |
| 0010 | DATA LF,LT/F,T/ | |
| 0011 | 502 FORMAT(BOL1) | |
| 0012 | 5u3 FORMAT(5A8) | |
| 0013 | 504 FORMAT(813) | |
| 0014 | 505 FORMAT(8F10.0) | |
| 0015 | 602 FORMAT(1HO, BOLL) | |
| 0016 | 603 FORMAT(1H0,5AB) | |
| 3017 | 604 FORMAT(LHO, INPUT CARD LIST) | |
| 0018 | 606 FCRMAT(1H ,///) | |
| 0019 | 607 FURMAT(1H0,815) | |
| 0020 | 6G8 FCRMAT(1H0,1P6D12.5) | |
| 0021 | WRITE(6,004) | |
| 0022 | READ(5,503)TITLE | |
| 0023 | WRITE(6,603)TITLE | |
| 0024 | kEAD(5,502)L&L | |
| u J 25 | WRITE(6,602)L%L | |
| () ú 2 ö | READ(5,502)L\$E | |
| 0J27 | WRITE(6,602)L\$E | |
| U Ú28 | READ(5,5U4)N,ISLEN,IOLEN | |
| 0) 29 | write(o,oG7)n, islen, iolen | |
| 0030 | RFAD(5,505)TI,TF,DT,DELT | |
| 0031 | wRITE(6,608)TI,TF,DT,DELT | |
| 0032 | WRITE(6,606) | |
| 0033 | CALL CYCLE | |
| 0034 | STOP | |
| 0035 | END | |

| FORTRAN IV | G LEVEL 21 CYCLE | |
|--------------|---|--|
| 0001 | SUBHOUTINE CYCLE | |
| 0002 | IMPLICIT REAL*8 (A-H,O-Z) | |
| 0003 | LOGICAL*1 L\$L,L\$E,LMON,LF,LT | |
| 0004 | CGMMON/V&RBLE/XT(6),XP(6),XE(6),ZT(6),ZP(6),ZE(6) | |
| J005 | CUMMGN/TSMER/DELT,DT,TIME,TI,TF,N,ISLEN,IGLEN | |
| 0006 | CUMMON/SYSTEM/LSL(40);LSE(10) | |
| 0007 | COMMUN/MSNITR/LMON(20) | |
| 000 8 | CCMMJN/NOI\$E/IRAN(10),DG(10),RFRAF(6) | |
| 0009 | CCMMGN/OFFSET/C(3) | |
| 0010 | CATA LF,LT/F,T/ | |
| J011 | CIMENSION B(4,6),RN(4,4),T6(4,4) | |
| | C **** INITIALIZE SUBROUTINES **** | |
| 0012 | CALL RKINIT | |
| 00 13 | CUM = OXINIT(1) | |
| 0014 | CUY = GXINIT(1) | |
| 0015 | DUM = UF INIT(1) | |
| J016 | CALL CYINIT | |
| 0017 | CALL FLINIT | |
| 0018 | CALL OVINIT | |
| | C **** COMPUTE TRAJECTORIES **** | |
| 0019 | 1 CALL PUNKUT | |
| 3020 | IF(L\$L(2))60 TO 2 | |

| 0021 | CALL OBSERV | |
|--------------|-------------------------------|--|
| 0021 | | |
| 0022 | CALL FILTER(8,RN,T6) | the same of the sa |
| 0023 | GO TO 3 | |
| 0024 | 2 DG 4 I=1,ISLEN | The state of the s |
| 0025 | 4 XP(1)=XT(1) | |
| | C **** DUTPUT CYCLE DATA **** | |
| 0026 | 3 CALL CYCLOT | |
| | C **** MUNITOR SECTION **** | |
| 0027 | CALL TERMIN | |
| 002B | IF(L\$L(2))GO TO 5 | |
| J 029 | IF(L\$L(3))GO TO 5 | |
| 0030 | IF(L\$L(6))GD TO I | |
| 0031 | GO TO 7 | |
| 0032 | 5 CO 6 I=1, ISLEN | |
| 0033 | 6 XP([)=XT([) | |
| 0034 | IF(L\$L(6))GO TO 1 | |
| | C **** OUTPUT SECTION **** | |
| 0035 | 7 CALL RECAP | |
| 0036 | RETURN | |
| 0037 | END | |

| FORTRAN IV G | LEVEL 21 TARGET |
|--------------|--|
| 1000 | SUBROUTINE TARGET(S,T) |
| 0002 | IMPLICIT REAL*8 (A-H+O-Z) |
| 0003 | DIMENSION S(3) |
| 0004 | COMMON/VAR1/A.RN,EPS.ET.TSTAR.DET |
| 0005 | 601 FORMAT(1HO, CONVERGENCE -, 1PD12.5, KEPEQ) |
| 0006 | EO=ET |
| 0007 | ET=ET+DET |
| 3308 | DO A I=1,100 |
| 0009 | SINET=DSIN(ET) |
| 0010 | COSET=DCOS(ET) |
| 0011 | F=RN*(T+TSTAR)-ET+EPS*SINET |
| 0012 | DF=EPS*CGSET-1.000 |
| 0013 | ET=ET-F/DF |
| 0014 | CIF=DABS(F/DF) |
| 0015 | IF(DIF-LT-1-00-10)G0 TO 2 |
| 0016 | 1 CONTINUE |
| 0017 | WRITE(6,601)DIF |
| 0018 | 2 DET=ET-EO |
| 0019 | S(1)=A*(COSET -EPS) |
| 0020 | S(2)=A*DSÿRT(1.0D0-EPS*EPS *SINET |
| 0021 | S(3)=0.0D0 |
| 0022 | RETURN |
| 0023 | END |

| FORTRAN IV | G LEVEL 21 RUNKUT | |
|--------------|--|-----------|
| 0001 | SUBROUTINE RUNKUT | —. |
| 0002 | IMPLICIT REAL*8 (A-H;0-Z) | |
| 0003 | LOGICAL*1 L\$L,L\$E,LMON,LF,LT | |
| 0004 | LOGICAL*1 LS1,LS2 | |
| 0005 | CUMMON/V\$RBLE/XT(6),XP(6),XE(6),ZT(6),ZP(6),ZE(6) | |
| 0006 | COMMON/TSMER/DELT, DT, TIME, TI, TF, N, ISLEN, TOLEN | |
| 0007 | COMMON/SYSTEM/LSL(40).LSE(10) | |
| 0008 | COMMON/M\$NITR/LMON(20) | |
| 0009 | COMMON/NOISE/IRAN(10),DG(10),RFRAF(6) | |
| 0010 | COMMON/OFFSET/C(3) CIMENSION XINT(6),JUM(6) | _ |
| 0011 | | |
| 3013 | CATA LF,LT/F,T/ L\$L(12)=LT | |
| 0014 | DD 1 ICYCLE=1.N | |
| 0015 | CO 33 I=1,ISLEN | <u></u> - |
| 0016 | 33 SUM(I)=0.0D0 | |
| 0017 | L\$L(10)=LT | _ |
| 0018 | CO 10 11=1,4 | |
| 0019 | LS1=[1.EQ.2. OR.]1.EQ.3 | *** |
| 0020 | LS2=I1.EQ.4 | |
| 0021 | L\$L(11)=I1.EQ.3 | • |
| 0022 | F=F1 | |
| 0023 | FS=F5 | _ |
| 0024 | IF(LS1)F=F2 | |
| 3025 | 1F(LS1)FS=F3 | |
| J026 | IF(LS2)FS=F4 | |
| 0027 | TS=TIME+DT*FS | - |
| 0028 | DO 20 1=1,ISLEN | |
| 0029 | 20 | |
| 0030 | CC 31 I=1,NP1 | |
| 0031 | J=I-1 | |
| 2ذ00 | IF(J.GT.O) GD TD 2 | |
| 0033 | CUM = DOFX\$(J,TS) | |
| 0034 | CU4=GOFX\$(J.TS) | _ |
| 0035 | L\$L(12)=LF | |
| 0036 0037 | GO TO 31 2 XINT(J)=DT*(DDFX(J)+GOFX(J)) | <u></u> |
| 0038 | 2 | |
| 0039 | 31 CONTINUE | |
| 0040 | 4.\$L (10)=LF | |
| 0041 | 10 CONTINUE | |
| 0041 | TIME=TIME+DT | |
| 0043 | DO 11 I=1, ISLEN | — |
| 0044 | 11 XT(1)=XT(1)+SUM(1) | |
| 0045 | 1 CONTINUE | |
| 0046 | RETURN | |
| 0047 | ENTRY RKINIT | _ |
| 0048 | READ(5,501)(XT(I),I=1,ISLEN) | |
| 0049 | WRITE(6,601)(XT(I),I=1,ISLEN) | |
| 0050 | 501 FORMAT(8F10.0) | |
| 0051 | 601 FOR MAT(1HO, 1P8012.5) | |
| 0052 | F1=1.0D0/6.0D0 | |
| 0053 | F2=2.000*F1 | |
| 0054 | F3=1.0D0/2.0D0 | |
| 0055 | F4=1.0D0 | |
| 0056 | F5=0.000 | |
| J057 | TIME=TI | |
| 0058 | NP1 = I St EN+1 | |

| FORTRAN I | V G LEVEL | 21 . | RUNKUT | <u></u> | |
|-----------|-----------|-----------------|--------|---------|--|
| 0059 | | DO 32 1=1.ISLEN | | | |
| 0060 | 32 | (I)TX=(I)TVIX | | | |
| 0061 | | RETURN | | | |
| 0062 | | END | | | |

| FORTRAN I | G LEVEL 21 DOFX\$ | |
|--------------------|---|-------|
| 0001 | FUNCTION DOFX\$(J,TS) | |
| 0002 | IMPLICIT REAL*8(A-H,O-Z) | |
| 0003 | LOGICAL*1 L\$L,L\$E,LMON,LF,LT | ***** |
| 0004 | COMMON/V\$RBLE/XT(6),XP(6),XE(6),ZT(6),ZP(6),ZE(6) | |
| 0005 | CGMMON/TSMER/DELT, DT, TIME, TI, TF, N, ISLEN, IOLEN | |
| _0006 | COMMON/SYSTEM/LSL(40),LSE(10) | |
| 0007 | COMMON/M\$NITR/LMON(20) | |
| 8000 | COMMON/NOISE/IRAN(10),DG(10),RFRAF(6) | |
| 0009 | COMMON/VAR1/A.RN.EPS.EO.TSTAR.DET | |
| 0010 | COMMON/OFFSET/C(3) | |
| 0011 | DIMENSION D(3),S(3) | |
| 0012 | DATA LF,LT/F,T/ | |
| 0013 | 99601 FORMAT(1HO, 14, "IMPROPER INDEX *DOFX") | |
| 0014 | If(NOT-L\$L(11))CALL TARGET(S,TS) | |
| 0015 | \$2=0.000 | |
| 0016 | D2= 0.0D0 | |
| 0017 | DO 1 I=1,3 | |
| 9018 | D(I) = S(I) + C(I) + x + T(I) | |
| 0019 | D2=D2+D(I)*#2 | |
| 0020 | 1 | |
| 0021 | DN=DSQRT(D2) | |
| 0022 | SN=DSQRT(S2) | |
| 0023 | RATI=GM/(SN*SN*SN) | |
| 0024 | RAT 2=(SN/DN) **3 | |
| 0025 | DCF X \$= 0.000 | |
| 0026 | IF(TF-TIME.GT.DELT)RETURN | |
| 0027 | IFI.NOT.LSL(10))RETURN | |
| 0028 | WKITE(6,602)TIME,XT | |
| 0029 | 602 FORMAT(1HO, END STATE ,2X, TIME= ,FLO.3/1H ,1P6D12.5) | |
| 0030 | RETURN | |
| 0031 | ENTRY DOFX(J) | |
| 0032 | L, (89999, 89999, 99999, 99998, 99998) U1 00 | |
| 0033 | WRITE(6,99601)J | |
| 0034 | DOFX=0.0D0 | |
| 0035 | LSE(2)=LY | |
| 0036 | RETURN | |
| 0037 | 99959 COFX=XT(J+3) | |
| 0038 | RETURN | |
| 0039 | 99998 DOFX=PATI*(S(J-3)+D(J-3)*RAT2) | |
| 0040 | RETURN | |
| - · · - | ENTRY DXINIT(J) | |
| 0042 | READ(5,501)A,RN,EPS,ED,TSTAR | _ |
| 0043 0044 | EO=RN*TSTAR | |
| 0044 | WRITE(6,601)A,RN,EPS,EO,TSTAR | |
| | 501 FURMAT(8F10.0) | |
| 0046 0047 | 601 FOR MAT(1H0,1P8012.5) READ(5,501)C | |
| | | |
| 0048 | WRITE(6,601)C GM=9,90549D2O | |
| 0049 | | |
| 0050 | DET=1.0D-3 | |
| | DXINIT=0.0D0 | |
| 0052 | RETURN END | |

| FORTRAN I | V G LEVEL | 21 GOFX\$ | |
|--------------|---------------------------------------|--|---|
| 0001 | | FUNCTION GOFX\$(J.TS) | |
| 0002 | | IMPLICIT REAL*8(A-H,O-Z) | |
| 0003 | | LOGICAL*1 L\$L,L\$E,LMON,LF,LT | |
| 0004 | | COMMON/V \$RBLE/XT(6), XP(6), XE(6), ZT(6), ZP(6), ZE(6) | |
| 0005 | | COMMON/TAMER/DELT, DT, TIME, TI, TF, N, ISLEN, IOLEN | |
| JU 06 | | COMMON/SYSTEM/L\$L(40),L\$E(10) | |
| 0007 | " | COMMON/MINITR/LMON(20) | |
| 8000 | | COMMON/NOISE/IRAN(10),DG(10),RFRAF(6) | |
| 0009 | • | COMMON/FORCE/F(3) | |
| 0010 | | COMMON/OFFSET/C(3) | |
| 3011 | | DATA LF, LT/F, T/ | |
| JU12 | 99601 | FORMAT(1HO,14, "IMPROPER INDEX *GOFX") | |
| 0013 | | IF(L\$L(12))TIM1=TS | |
| 0014 | | TAUO=TF+TIM1 | |
| 0015 | | TAU=TF-TS | |
| 0016 | | TRAT1=(6.000/TAU0*#2)*(1.000-2.000*(TAU/TAU0)) | · |
| 0017 | | TRAT2=(2.0D0/TAU0)*(1.0D0-3.0D0*(TAU/TAU0)) | |
| 0018 | | GOFX\$=0.0D0 | |
| 0019 | | RETURN | |
| 0020 | | ENTRY GOFX(J) | |
| 0021 | | GO TO (99999,99999,99999,9998,9998),J | |
| 0022 | | WRITE(6,99601)J | |
| 0023 | | L\$E(3)=LT | |
| 0024 | | GOF X=0.0D0 | |
| 0025 | | RETURN | |
| 0026 | 99999 | GGF X=0.0D0 | |
| 0027 | • | RETURN | |
| 0028 | 99998 | F(J-3)=TRATL*XP(J-3)+TRAT2*XP(J) | |
| 0029 | • • | GOFX=F(J-3) | |
| 0030 | | RETURN | |
| 0031 | · · · · · · · · · · · · · · · · · · · | ENTRY GXINIT(J) | |
| 0032 | | DO 90001 I=1,1SLEN | |
| 0033 | 90001 | XP(I)=XT(I) | |
| 0034 | | XP(1)=XP(1)+10000 | |
| 0035 | • | XP(2)=XP(2)+10000. | |
| 0036 | | XP(3)=XP(3)+10000. | |
| 0037 | | XP(4)=XP(4)+1000. | |
| 0038 | | XP(5)=XP(5)+1000. | |
| 0039 | | XP(6)=XP(6)+1000. | |
| 0040 | • | GXINIT=0.0D0 | |
| 0041 | | RETURN | |
| 0042 | | END | |

| FORTRAN IV | G LEVEL 21 FILTER |
|--------------|---|
| 0001 | SUBROUTINE FILTER(B,RN,T6) |
| 0002 | IMPLICIT REAL*8(A-H,O-Z) |
| 0003 | LOGICAL*1 L\$L,L\$E,LMON,LF,LT |
| 0004 | COMMUN/V\$RBLE/XT(6), XP(6), XE(6), ZT(6), ZP(6), ZE(6) |
| 0005 | COMMON/TAMER/DELT,DT,TIME,TI,TF,N,ISLEN,IOLEN |
| 0006 | COMMON/SYSTEM/L\$L(40),LSE(10) |
| 0007 | COMMON/M\$NITR/LMON(20) |
| 8000 | COMMON/NOISE/IRAN(10),DG(10),RFRAF(6) |
| 0009 | COMMON/KALMAN/RM(6,6),FILT(6,4),U(6) |
| 0010 | CUMMON/OFFSET/C(3) |
| 0011 | DIMENSION T1(6), YL(6), Y(6), T2(6,6), T3(6,6), T4(6,6), QP(6,6), |
| | 18(10LEN,6),RN(10LEN,10LEN),T5(6,6),T6(10LEN,10LEN),PH1(6,6) |
| 0012 | DIMENSION LE(6).MM(6) |
| 0013 | CATA LF,LT/F,T/ |
| 0014 | WRITE(6, 80) IOLEN |
| 0015 | 80 FURMAT(20X, *IDLEN=*, I2) ICNT=ICNT+1 |
| | |
| 0017 0018 | 00 38 I=1,IOLEN CO 32 J=1.IOLEN |
| 0019 | 32 RN(I,J)=0.0D0 |
| 0020 | DO 38 J=1,1SLEN |
| 3021 | 38 B(1,J)=0.000 |
| 0022 | IF(IJLEN.EQ.21GD TD 34 |
| 3023 | IF(L\$L(20).AND.10LEN.EQ.3)GD TO 37 |
| 0024 | CG 33 1=1,3 |
| 0025 | 33 B(I,L)=1,000 |
| 0026 | IF(IDLEN.EU.4)B(4,6)=1.000 |
| 0027 | GC TO 36 |
| 0028 | 37 B(1,2)=1.0D0 |
| 0029 | 8(2,3)=1.000 |
| 0030 | B(3,6)=1.0D0 |
| 0031 | DU 39 I=1,3 |
| 0032 | 39 RN(I,I)=RFRAF(I+1)**2 |
| 0033 | GO TO 35 |
| 0034 | 34 B(1,2)=1.0D0 |
| 00 35 | 8(2,3)=1.000 |
| 0036 | RN(1,1)=RFRAF(2)**2 |
| 0037 | RNL 2, 2) = RFRAF(3) **2 |
| 0038 | GO TO 35 |
| 0039 | 36 00 30 I=1,IOLEN |
| 0040 | 30 RN(1,1)=RFRAF(1)**2 |
| 0041 | 35 TAUKI=TF-TIME |
| 0042 | TAUK=TAUK1+DELT |
| 0043 | RAT=TAUK1/TAUK |
| 0044 | RAT 2=RAT*RAT |
| 0045 | RAT3=RAT2*RAT |
| 0046 | A=3.000*RAT2-2.0D0*RAT3 |
| 0047 | DIF=RAT-RAT2 |
| 0048 | F=TAUK1*DIF |
| 0049 | D=3.0D0*RAT2=2.0D0*RAT |
| | E=-6.0D0*DIF/TAUK |
| 0051 | 00 31 I=1,3 PHI(I,I)=A |
| 0053 | PHI(1,1,3)=F |
| 0054 | PHI(1+3+1)=E |
| 0055 | PHI(1+3,1+3)=0 |
| 0056 | 31 CONTINUE |
| 0000 | C PREDICT X STATE |
| | O TREESON ROTATE |

| FORTRAN IV | G LEVEL 21 FILTER |
|--------------|---|
| 0057 | DD 10 I=1,1SLEN |
| <u> </u> | T1(I)=0.0D0 |
| 0059 | CO 10 J=1.ISLEN |
| 0060 | 10 T1(1)=T1(1)+PHI(1,J)*XP(J) |
| 00/1 | C TRANSFORM TO Y SYSTEM Y(1)=DSQRT((T1(1)+C(1))**2+(T1(2)+C(2))**2+(T1(3)+C(3))**2) |
| 0061 0062 | Y(2)=(T1(1)+C(1))/Y(1) |
| 0062 0063 | Y(3)=(T1(2)+C(2))/Y(1) |
| 0064 | W = (T1(3) + C(3))/Y(1) |
| 0065 | Y(4)=({T1(1)+C(1)}*T1(4)+(T1(2)+C(2))*T1(5)+(T1(3)+C(3))*T1(6)) |
| | */Y(1) |
| 0066 | Y(5) = (T1(4) - Y(4) + Y(2))/Y(1) |
| 0067 | Y(6}=(T1(5)-Y(4)*Y(3))/Y(1) |
| 0068 | WD=(T1(6)-Y(4)*W)/Y(1) |
| | C COMPUTE LEFT PARTIAL DERIVATIVE |
| 0069 | T2(1,1)=Y(2) |
| 0070 | T2(1,2)=Y(3) |
| J071 | T2(1,3)=W |
| 0072 | T2(2,1)=(1.0D0-Y(2)**2)/Y(1) |
| 0073 | T2(2,2)=-Y(2)*Y(3)/Y(1) |
| JJ 74 | 12(2,3)=-Y(2)*W/Y(1) |
| 0075 | T2(3,1)=T2(2,2) |
| 0076 | T2(3,2)=(1.0D0-Y(3)**2)/Y(1) |
| 0077 | T2(3,3) = -(Y(3) * W)/Y(1) |
| 0078 | DO 11 I=1,3 |
| 0379 | 00 11 J=1,3 |
| 0080 | 11 T2(I+3,J+3)=T2(I,J) |
| 0081 | T2(4,1)=Y(5) |
| 0082 | T2(4,2)=Y(6) |
| 0083 | T2(4,3)=WD T2(5,1)=-(2,000*Y(2)*Y(5)+(1,000-Y(2)**2)*Y(4)/Y(1))/Y(1) |
| 0084 | T2(5,2)=-(Y(3)*Y(5)+Y(2)*Y(6)-Y(2)*Y(3)*Y(4)/Y(1))/Y(1) |
| 0085 0086 | $T_2(5,3) = -(w*Y(5)+Y(2)*WD-Y(2)*W*Y(4)/Y(1))/Y(1)$ |
| | T2(6,1)=T2(5,2) |
| 0087 0088 | T2(6,2)=-(2.0D0*Y(3)*Y(6)+(1.0D0-Y(3)**2)*Y(4)/Y(1))/Y(1) |
| 0089 | T2(6,3)=-(W*Y(6)+Y(3)*WD-Y(3)*W*Y(4)/Y(1))/Y(1) |
| 0007 | C COMPUTE RIGHT PARTIAL DERIVATIVE |
| 3090 | T3(1,1)=YL(2) |
| 0091 | T3(4,4)=YL(2) |
| 0092 | T3(1,2)=YL(1) |
| 0093 | T3(4,5)=YL(1) |
| 0094 | T3(2,1)=YL(3) |
| J045 | T3(5,4)=YL(3) |
| 0096 | T3(2,3)=YL(1) |
| 0097 | T3(5,6)=YL(1) |
| 0098 | T3(3,1)=WL |
| Ju 99 | T3(6,4)=WL |
| 0100 | T3(3,2)=-YL(2)*YL(1)/WL |
| 0101 | T3(6,5)=T3(3,2) |
| 0102 | T3(3,3)=-YL(3)+YL(1)/WL |
| 0103 | T3(6,6)=T3(3,3) |
| 0104 | T3(6,1)=\DL . |
| 0105 | T3(6,2)=-(XP(4)/WL)+YL(1)*YL(2)*WDL/WL**2 |
| 0106 | T3(6,3)=-{XP(5)/WL)+YL(1)*YL(3)*HDL/WL**2 |
| 0107 | C COMPUTE PSI |
| 0107 | DD 12 I=1, ISLEN DD 12 J=1, ISLEN |
| 0108 | T4(I,J)=0.0D0 |
| 0109 | (4(1))(-0.000 |

| FORTRAN | IV G LEVEL ZI FILTER |
|--------------|---|
| 0110 | DO 12 K=1,ISLEN |
| 0111 | . 00 12 L=1,1SLEN |
| 0112 | 12 T4(I,J)=T4(I,J)+T2(I,K)*PHI(K,L)*T3(L,J) |
| | C PREDICT COVARIANCE |
| 0113 | DO 13 1=1,1SLEN |
| 0114 | 00 13 J=1,1SLEN |
| 0115 | T5(I,J)=QP(I,J) |
| 0116 | CO 13 K=1,ISLEN DO 13 L=1,ISLEN |
| 0118 | |
| 0110 | 13 T5(I,J)=T5(I,J)+T4(I,K)*RM(K,L)*T4(J,L) C COMPUTE THE FILTER |
| 0119 | 00 14 I=1, IQLEN |
| 0120 | DO 14 J=1, IOLEN |
| 0121 | T6(I,J)=RN(I,J) |
| 0122 | DO 14 K=1.ISLEN |
| 0123 | CO 14 L=1,ISLEN |
| 0124 | 14 TG(I,J)=TG(I,J)+B(I,K)*T5(K,L)*B(J,L) |
| 0125 | CALL MINV(T6,IOLEN,16,LL,MM,D) |
| 0126 | DU 15 1=1,1SLEN |
| 0127 | DC 15 J=1,IOLEN |
| 0128 | F1LT(1,J)=0.000 |
| 0129 | Du 15 K=1,ISLEN |
| 0130 | DC 15 L=1,IOLEN |
| 0131 | 15 FILT(1,J)=FILT(I,J)+T5(I,K)*B(L,K)*T6(L,J) |
| | C CUMPUTE PREDICTED OBSERVATIONS |
| 0132 | DC 16 1=1.IOLEN |
| 0133 | ZP(1)=0.0D0 |
| 0134 | DG 16 J=1. I SLEN |
| 0135 | 16 ZP(I)=ZP(I)+8(I,J)*Y(J) |
| 0136 | C COMPUTE THE ERRUR IN OBSERVATIONS OF 17 I=1,10LEN |
| 0130 | 17 ZE(I)=ZT(I)-ZP(I) |
| OIJ! | C UPCATE Y |
| 0138 | DG 18 I=1.ISLEN |
| 0139 | T1(1)=Y(1) |
| 0140 | 00 18 J=1,10LEN |
| 0141 | 18 T1(I)=T1(I)+F1LT(I,J)*ZE(J) |
| | C UPDATE COVARIANCE |
| 0142 | IF(ICNT.GT.10.AND.ICNT.LT.32)GD TO 99 |
| 0143 | IF(ICNT.GT.40) GO TO 99 |
| 0144 | DO 19 I=1.ISLEN |
| 0145 | CG 19 J=1,ISLEN |
| 0146 | T4(1,J)=0.000 |
| 0147 | CU 19 K=1.IOLEN |
| 3148 | 19 T4(1,J)=T4(1,J)+FILT(1,K)*8(K,J) |
| 0149 | DD 20 I=1,ISLEN |
| 0150 0151 | CG 20 J=1, ISLEN |
| 0151 | T4(I,J)=-T4(I,J) IF(I,EQ,J)T4(I,J)=T4(I,J)+1,000 |
| 0152 | 20 CONTINUE |
| 0154 | 00 21 I=1+ISLEN |
| 0155 | Dù 21 J=1,1SLEN |
| 0156 | FM(1,J)=0.000 |
| 0157 | DC 21 K=1.ISLEN |
| 0156 | 21 RM(I,J)=RM(I,J)+T4(I,K)*T5(K,J) |
| 0159 | 59 CUNTINUE |
| | C SAVE Y(K+1,K+1) |
| 0160 | DG 22 I=1.ISLEN |
| 0100 | DO 22 I=1,ISLEN |

| FURTRAN I | V G LEVEL 21 FILTER |
|--------------|--|
| 0161 | 22 YL(1)=TL(1) |
| | C CONVERT TO X |
| 0162 | XP(1)=YL(2)*YL(1)-C(1) |
| 0163 | XP(2)=YL(3)*YL(1)-C(2) |
| 0164 | XP(4)=YL(1)*YL(5)+YL(4)*YL(2) |
| 0165 | XP(5)=YL(1)*YL(6)+YL(4)*YL(3) |
| 0166 | XP(3)=DSORT(YL(1)**2-(XP(1)+C(1))**2-(XP(2)+C(2))**2)-C(3) |
| 0167 | xP(6) = (YL(1) * YL(4) - (XP(1) + C(1)) * XP(4) - (XP(2) + C(2)) * XP(5)) / (XP(3) |
| | 6C(3)) |
| 0168 | wL=(XP(3)+C(3))/YL(1) |
| 0169 | WDL = (XP(6) - YL(4) + WL) / YL(1) |
| 0170 | (6,912)(XP(J),J=1,0) |
| 0171 | 912 FORMAT(5D12.5//) |
| 0172 | RETURN |
| 0173 | ENTRY FLINIT |
| | C ZERO ARRAYS |
| 0174 | DC. 101 I=1.ISLEN |
| 0175 | CO 102 J=1.ISLEN |
| 0176 | T2(I,J)=0.000 |
| 0177 | T3(I,J)=0.0D0 |
| 0178 | RM(I,J)=0.000 |
| 0179 | PHI(1,J)=0.0D0 |
| 0180 | 102 QP(I,J)=0.0D0 |
| 0181 | 00 101 J=1,IOLEN 101 FILT(I,J)=0.000 |
| 3182 | |
| 0 183 | C INITIALIZE VARIABLES YL(1)=DSQRT((XP(1)+C(1))**2+(XP(2)+C(2))**2+(XP(3)+C(3))**2) |
| 0184 | YL(2)=(XP(1)+C(1))/YL(1) |
| 0185 | $Y_{L}(3) = (XF(2) + C(2)) / Y_{L}(1)$ |
| 0185 | WL=(XP(3)+C(3))/YL(1) |
| 0187 | $\frac{1}{Y(4) = ((XP(1) + C(1)) \times XP(4) + (XP(2) + C(2)) \times XP(5) + (XP(3) + C(3)) \times XP(6)}{(XP(3) + C(3)) \times XP(6)}$ |
| 010. | */YL(1) |
| 0188 | YL(5)=(XP(4)-YL(4)*YL(2))/YL(1) |
| 0169 | YL(6) = (XP(5) - YL(4) + YL(3)) / YL(1) |
| 0190 | RM(1,1)=1.008 |
| 0151 | RM(2,2)=4.00-02*(1-YL(2)**2) |
| 0192 | RM(3,3)=4.00-02*(1-YL(3)**2) |
| 0193 | RM(4,4)=1.006 |
| 0194 | RM(5,5)=1.0D-05*YL(2)**2 |
| 0195 | RM(6,6)=1.00-05*YL(3)**2 |
| 0196 | WOL = (XP(6)-YL(4)+WL)/YL(1) |
| 0197 | ICNT=0 |
| 0196 | RETURN |
| 0199 | END |

| FORTRAN IV | G LEVEL 21 OBSERV |
|--------------|---|
| 0001 | SUBROUTINE OBSERV |
| 0002 | IMPLICIT REAL #8(A-H, O-Z) |
| 0003 | LOGICAL*1 L\$L,L\$E,LMON,LF,LT |
| 0004 | CG4MDN/V\$RBLE/XT(6),XP(6),XE(6),ZT(6),ZP(6),ZE(6) |
| 0005 | COMMONAT SMERADELT, DT, TIME, TI, TF, N, ISLEN, IOLEN |
| 0006 | COMMUN/SYSTEM/LSL(40),LSE(10) |
| J007 | CGMMON/M\$NITR/LMON(20) |
| 3008 | COMMON/NOISE/IRAN(10),DG(10),RFRAF(6) |
| 0009 | COMMUN/OFFSET/C(3) |
| 0010 | DATA_LF,LT/F,T/ |
| | C OBSERVATIONS |
| | C RFRAF(1 TO 4) = STODEV FOR ZT(1 TO 4) RESPECTIVELY |
| 0011 | RANGE=DSQRT((XT(1)+C(1))**2+(XT(2)+C(2))**2+(XT(3)+C(3))**2) |
| 0012 | ZT(2)=(XT(1)+C(1))/RANGE |
| 0013 | ZT(3)=(XT(2)+C(2))/RANGE |
| 0014 | UAC=DARCOS(ZT(2)) |
| ა015 | VAC=DARCOS(ZT(3)) |
| 0016 | DG(2) = GRAND(0.0D0.EANG, 2) |
| 0017 | CG(3)=GRAND(0.0D0,EANG,3) |
| 0018 | UAC=UAC+DG(2) |
| 0019 | VAC = VAC+DG(3) |
| 0020 | ZT(2)=DCUS(UAC) |
| 0021 | ZT(3)=DCOS(VAC) |
| 0022 | RFRAF(2)=DSQRT(EANG**2*(1.0D0~ZT(2)**2)) |
| 0023 | RFRAF(3)=DSQRT(EANG**2*(1.0D0-ZT(3)**2)) |
| J024 | IF(L\$L(20)) GO TO 10 |
| 0025 | IF(RANGE.GT.RMIN)GO TO 2 |
| J026 | ZT(1)=RANGE |
| 0027 | RFR AF(1)=DABS(ZT(1)*3.00-02) |
| 0928 | DG(1)=GRAND(0.0D0,RFRAF(1),1) |
| 0029 | ZT(1) = ZT(1) + DG(1) |
| 0030 | IF(RANGE-LT-RMIN-AND-RANGE-GT-RDMINIGO TO 3 |
| 1031 | IGLEN=4 |
| 0032 | ZT(4)=((XT(1)+C(1))*XT(4)+(XT(2)+C(2))*XT(5)+(XT(3)+C(3))*XT(6) |
| | */21(1) |
| J033 | RFRAF(4)=1.0002 |
| 0034 | DG(4)=GRAND(0.0DQ.RFRAF(4).4) |
| 0035 | ZT(4)=ZT(4)+DG(4) |
| 0036 | GO TO 5 |
| 3037 | 10 IF(RANGE.GT.ROMIN) GO TO 2 |
| 0038 | 2T(4)=((XT(1)+C(1))*XT(4)+(XT(2)+C(2))*XT(5)+(XT(3)+C(3))*XT(6) |
| | */RANGE |
| 0039 | RFR AF (4)=1.0002 |
| 0040 | OG(4)=GRAND(0.0D0,RFRAF(4),4) |
| 0041 | ZT(4)=ZT(4)+DG(4) |
| 0042 | IF(RANGE.LT.ROMIN.AND.RANGE.GT.RMIN) GO TO 6 |
| 0043 | ICLEN=4 |
| 0044 | ZT(1)=RANGE |
| 0045 | RFRAF(1)=DABS(ZT(1)*3.00-02) |
| 0046 | DG(1)=GRAND(0.0D0,RFRAF(1).1) |
| 0047 | ZT(1)=ZT(1)+DG(1) |
| 0047 | GU TO 5 |
| 0049 | 2 WRITE(6,1)(DG(LSCNT),LSCNT=2,3) |
| | · · · · · · · · · · · · · · · · · · · |
| 0050 | IOLEN=2 |
| 0051 | GO TO 4 |
| 0052 | 3 IULEN=3 |
| 0053 0054 | 5 WRITE(6,1)(DG(LSCNT),LSCNT=1,IOLEN) |
| | 1 FGR MAT(///,1UX,'NOISE',5X,1P4D12.5) |

| FORTRAN IV | EVEL 21 OBSERV |
|------------|-----------------------------------|
| 0055 | GO TO 4 |
| 0056 | 6 WRITE(6,1)(OG(LSCNT),LSCNT=2,4) |
| 0057 | IOLEN=3 |
| 0058 | 4 RETURN |
| 0059 | ENTRY OVINIT |
| 0060 | A=0.0D0 |
| 0061 | EAVG=.0002 |
| 0062 | RMIN=1.0D20 |
| 0063 | RDMIN=1.0D20 |
| 0064 | RETURN |
| 0065 | END |

| FURTRAN I | G LEVEL 21 GRAND |
|---------------|--|
| 1000 | FUNCTION GRAND (RMEAN, STDDEV, ISLCT) |
| 0002 | IMPLICIT REAL*8(A-H,O-Z) |
| | C PURPOSE |
| | C COMPUTES A NORMALLY DISTRIBUTED RANDOM NUMBER WITH A GIVEN |
| | C MEAN AND STANDARD DEVIATION |
| 0003 | A=0.000 |
| 0004 | DC 50 I=1,12 |
| 0005 | 50 A=4+URAND(ISLCT) |
| 0006 | GRAND=(A-6.0D0)*STDDEV+RMEAN |
| 0007 | FETURN |
| 3 00 8 | FND |

| ORTRAN IV G | G LEVEL 21 URANO | |
|--------------|--|--|
| 0001 | FUNCTION URAND(ISLCT) | |
| J 002 | IMPLICIT REAL*8(A-H,O-Z) | |
| 0003 | CCMM IN/NOISE/IRAN(10).DG(10).RFRAF(6) | |
| 0004 | IY= IRAN(ISECT) *65539 | |
| 0005 | IF(IY)5,6,6 | |
| 300 6 | 5 1Y=IY+2147483647+1 | |
| 0007 | 6 URAND=DFLUAT(IY)*4.656613D-10 | |
| 000B | IRAN(ISLET)=IY | |
| 0009 | RETURN | |
| 0010 | ENTRY URINIT(ISLCT) | |
| J011 | URAND=0.000 | |
| 0012 | UKINIT=0.000 | |
| 0013 | RETURN | |
| 0014 | END | |

| ORTRAN IV G | LEVEL 21 BLK DATA |
|-------------|---|
| 0001 | BLOCK DATA |
| 0002 | IMPLICIT REAL*8 (A-H,G-Z) |
| J003 | COMMON/NUI\$E/IRAN(10).DG(10).RFR4F(6) |
| 0004 | DATA IRAN/69800661,54218059,51070625,15239339,75892237, |
| | *10418327,81767867,59847821.52031357,26256073/ |
| 0005 | CN3 |

| FORTRAN | IV G LEVEL 21 CYCLOT |
|---------------|--|
| 0001 | SUBROUTINE CYCLOT |
| 0002 | IMPLICIT REAL*8(A-H.O-Z) |
| 0003 | LOGICAL*1 L\$L,L\$E,LMON,LF,LT |
| 0004 | COMMON/V\$RBLE/XT(6),XP(6),XE(6),ZT(6),ZP(6),ZE(6) |
| 0005 | COMMUNITAMER/DELT.DT.TIME.TI.TF.N.ISLEN.IOLEN |
| J006 | COMMON/SYSTEM/L\$L(40),L\$E(10) |
| 0007 | COMMON/M\$NITR/LMON(20) |
| 0008 | COMMON/NOISE/IRAN(10),DG(10),RFRAF(6) |
| 0009 | COMMUN/KALMAN/ P(6,61,FILT(6,4),U(6) |
| 0010 | COMMON/FORCE/F(3) |
| 0311 | COMMON/OFFSET/C(3) |
| 0012 | DATA LF,LT/F,T/ |
| 0013 | 601 FURMAT(1H ,3X, TRUE STATE VECTOR 1/4X, 1P6D12.5) |
| J J14 | 603 FURMAT(1H ,*TIME=*,1PD12.5) |
| 0015 | 604 FUR MAT(1H , 'NORMED DISTANCE=',1PD12.5,3X,'NORMED VELOCITY=', |
| | 11P012.5,3X, 'NURMED FORCE=',1PD12.5} |
| 0016 | 605 FORMAT(1HO, *\$\$\$ RENDEZVOUS \$\$\$*) |
| 0017 | 606 FORMAT(1HO, MINIMUM NOFMED DISTANCE= , 1PD12.5, 3X, AT TIME= , |
| | 1 12012.5) |
| 8100 | 607 FOR MAT(1HO, *MINIMUM NORMED VELOCITY = *,1PD12.5,3X,*AT TIME=*, |
| | 1 12012.5) |
| 0019 | 608 FORMAT(////) |
| 0020 | 609 FORMAT(1HO, ***** DUT OF TIME ****) |
| 0021 | 610 FORMAT(1HO, FORCE VECTOR ./.1H .1P3D12.5) |
| 0022 | 611 FURMATITHU, 3X, PREDICTED STATE VECTOR (4X, 1P6D12.5) |
| 0023 | 612 FGRMAT(1HO, 3X, *ERROR IN STATE VECTOR*/4X.1P6D12.5) |
| 0023 | 613 FURMAT(1HO, 3X, *TRUE OBSERVATIONS*/4X, 1P6D12.5) |
| | 614 FORMAT(1HO, 3X, *PREDICTED OBSERVATIONS*/4X, 1P6D12.5) |
| 0025 | |
| 0026 | 615 FURMAT(1HO, 3X, 'RESIDUAL ERROR'/4X, 1P6D12.5) |
| 3027 | 617 FURMAT(1HD,3X,*COVARIANCE MATRIX*) |
| 0028 | 61E FORMAT(1H ,6X,1P6D12.5) |
| 0029 | 619 FORMAT(1H1,10X,* SIMULATION RESULTS*,///) |
| 0030 | IF(L\$L(1))WRITE(6,619) |
| 0031 | 620 FORMAT(1H ,3X, NORMED POSITION ERROR = 1,191012.5,5X, NORMED VEL |
| | \$ITY ERROR = *,1P1D12.5) |
| 0032 | FT=0.000 |
| 0033 | T1=0.000 |
| 3034 | 12=0.000 |
| 0035 | 00 l I=1,3 |
| J J 56 | F(I)=F(I)+CF1 |
| 0037 | FT=FT+F(I)**2 |
| 0038 | T1=T1+XT(I)*XT(I) |
| 0039 | 1 T2=T2+XT(I+3)*XT(I+3) |
| 0040 | FT=DSQRT(FT) |
| 0041 | XS=DSQRT(T1) |
| 0042 | XV=DSQRT(T2) |
| 0043 | 1F(1\$L(9))GD TO 2 |
| 0044 | 1F(XS.GT.XO)GO TO 3 |
| 0045 | XU= XS |
| 0046 | TXS=TIME |
| 0047 | 3 IF(XV.GT.XVO)GO TO 2 |
| 0048 | VX=CVX |
| 0049 | TXV=TIME |
| | 2 WRITE(6,603)TIME |
| 0050 | WRITE(6,604)XS,XV,FT |
| 0050 | |
| 0051 | |
| | CHK =DABS(TF-TIME) IF(CHK-LT-DT)TF=TF+DELT |

| FORTRAN IV | G LEVEL 21 CYCLOT | |
|--------------|--|---|
| 0055 | DO 99901 I\$=1,ISLEN | |
| 3056 | 99901 XE(s =XT(s -XP(s) | |
| 0057 | PNDRM=DSQRT(XE(1)**2+XE(2)**2+XE(3)**2} | |
| 0058 | VNJRM=DSQRT(XE(4)**2+XE(5)**2+XE(6)**2) | |
| 0059 | WRITE(6,610)F | |
| 0060 | WRITE(6,601)XT | |
| 0061 | WEITE(6,611)XP | |
| 0062 | WRITE(6,612)XE | |
| 0063 | WRITE(6,620)PNORM,VNORM | |
| 0064 | WRITE(6,613)ZT | |
| 0065 | WRITE(6,c14)ZP | |
| 0066 | WF1TE(6,615)ZE | |
| 0067 | WRITE(6,617) | |
| 0068 | DG 6 1=1,1SLEN | |
| 0069 | 6 White(6,618)(P(1,J),J=1,1SLEN) | |
| 0070 | WRITE(0,608) | |
| 0)71 | 99902 L\$L(1)=LF | |
| 0072 | RETURN | |
| J073 | ENTRY TERMIN | |
| J074 | 1F(XS.LT.1.0D-2.AND.XV.LT.1.0D-41G0 TO 4 | |
| 0 075 | IF(TIME.GE.TF)GD TO 5 | |
| JJ 76 | RETURN | |
| 0077 | 4 WRITE(6,605) | |
| J Q78 | L\$L(6)=LF | |
| 0379 | RETURN | |
| 0000 | 5 WRITE(0,609) | |
| 0081 | L \$L (6)=LF | |
| 0082 | RETUKN | |
| 53 00 | ENTRY RECAP | |
| 0084 | WKITE(6,606)XO,TXS | |
| JO 85 | WFITE(6,607)XVO,TXV | |
| 0086 | RETURN | |
| 0087 | ENTRY CYINIT | |
| 38800 | X0=1.0D40 | |
| 0089 | XVD=1.0040 | _ |
| 0090 | CF1=1.0D0/(9.80665D-3*8.64D4**2) | |
| 0091 | RETURN | |
| 0092 | END | |

| 0001 | SUBROUTINE MINV(A,N,NSO,L,M,BIGA) |
|----------------------|--|
| 0002 | IMPLICIT REAL*8 (A-H+O-Z) |
| 0003 | DIMENSION A(NSQ), L(6), M(6) |
| | C DESCRIPTION OF DADAMSTERS |
| | C DESCRIPTION OF PARAMETERS C A - INPUT MATRIX, DESTROYED IN COMPUTATION AND REPLACED BY |
| | |
| | |
| | |
| | |
| | C L - WORK VECTOR OF LENGTH N C M - WORK VECTOR OF LENGTH N |
| | C |
| 0004 | NK=-N |
| 0005 | OU 190 K=1,N |
| 0000 | NK=NK+N |
| 0007 | L(K)=K |
| 9009 | M(<)=K |
| 0008 | KK=NK+K |
| 0009 0010 | BIG4=A(KK) |
| | DC 30 J=K,N |
| 0011 | IZ=N*(J-1) |
| 0012 | DG 30 I=K.N |
| 0013 | IJ= I7+ I |
| 0014 | 10 IF(DABS(BIGA)-DABS(A(IJ))) 20,30,30 |
| 3015 | 20 b164=4(1J) |
| 0016 | |
| 0017 | L(K)=1 M(K)=J |
| 0018 | 30 CONTINUE |
| 0019 | |
| | C INTERCHANGE ROWS |
| p | C INTERCHANGE ROWS |
| 0030 | · |
| 0020 | J=L(K) IF(J-K) 60,60,40 |
| 0021 | |
| 0022 | 40 KI=K-N DC 50 I=1,N |
| 0023 | |
| 0024 | K 1= K 1 + N HOL D= - A (K I) |
| 0025 | |
| 0026 | JI=KI-K+J A(KI)=A(JI) |
| 0027 | 50 A(JI) =HOLD |
| 0028 | \$\(\text{A}(\text{J}) = \text{A}(\text{D}) \\ \(\text{C} \) |
| | · · · · · · · · · · · · · · · · · · · |
| | C INTERCHANGE CULUMNS G |
| 0020 | • |
| 0029 | 60 I=4(K) IF(I-K) 90,90,70 |
| 0030 | |
| 3031 | 70 JP=N*(I-1) DO 80 J=1,N |
| 0032 | |
| 0033 | JK=NK+J |
| J034 | J]=JP+J |
| 0035 | HOLD=-A(JK) A(JK)=A(JI) |
| 0036 | |
| 0037 | 80 A(JI) =HOLD |
| | C DIVIDE COLUMN BY MINUS PIVOT (VALUE OF PIVOT ELEMENT IS |
| | |
| | CONTAINED IN BIGAL |
| | 6 |
| 0038 003 9 | 90 IF(BIGA) 110,100,110 100 RETUAN |
| | |

| FURTRAN IV G LEVEL | 21 MINV |
|--------------------|--|
| 0040 110 0041 | DO 130 I=1.N IF(I-K) 120.130.120 |
| | [K=NK+] |
| 0043 | A(1K)=A(1K)/(-BIGA) |
| | CONTINUE |
| | CONTINUE |
| <u>C</u> | NEW COLUMN TO THE COLUMN TO TH |
| C | REDUCE MATRIX |
| C | |
| 0045 | DU 16U I=1,N |
| <u> </u> | IK=NK+I IJ=I-N |
| | 00 1/3 4-1 1 |
| 0048 0049 | DO 160 J=1,N IJ=IJ+N |
| | |
| 0050 | IF(I-K) 140,160,140 IF(J-K) 150,160,150 |
| | |
| | KJ=IJ-I+K |
| 0053 | A(IJ)=A(IK)*A(KJ)+A(IJ) |
| | CONTINUE |
| Ç | NAMES OF THE PROPERTY OF THE P |
| <u> </u> | DIVIDE ROW BY PIVOT |
| | W. L. W. A. |
| 3055 | KJ=K-N |
| 0056 | DO 180 J=1.N |
| 3057 | KJ=KJ+N |
| JU58 | IF(J-K) 170,180,170 |
| | A(KJ)=A(KJ)/BIGA |
| | CONTINUE |
| <u> </u> | |
| <u> </u> | REPLACE PIVOT BY RECIPROCAL |
| C | |
| 0061 | A(<k)=1.0 biga<="" th=""></k)=1.0> |
| | CUNTINUE |
| č | STAND SOLVAND COLUMN INTERCHANCE |
| <u>``</u> | FINAL ROW AND COLUMN INTERCHANGE |
| - | k and |
| 0063 | K=N K=(K-1) |
| 0064 200 0065 | IF(K) 270,270,210 |
| | I=L(K) |
| 0067 | IF(1-K) 240,240,220 |
| | JQ=N*(K-1) |
| 0069 | Jk=N*(I-1) |
| 0070 | 00 230 J=1,N |
| 0071 | 7K=70+7 |
| 0072 | HULD=A(JK) |
| 0073 | JI=JR+J |
| 0074 | A(JK)=-A(JI) |
| | A(JI) =HOLD |
| | J=M(K) |
| 0077 | 1F(J-K) 200,200,250 |
| | K I = K - N |
| 0079 | CU 260 I=1,N |
| 00 80 | KI=KI+N |
| 0081 | HOLD=A(KI) |
| 0082 | JI=KI-K+J |
| 0083 | A(KI) = -A(JI) |
| | A(JI) =HOLD |
| 0085 | GD TU 200 |
| | 00 10 200 |

| FORTRAN IV | G LEVEL | 21 | MINV | _ |
|--------------|---------|--------|------|---|
| J U86 | 270 | RETURN | | ٠ |
| 0087 | | FND | | |