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Radar Cross Sections of Standard and Complex Shape Targets

Final Report

1 September 1973 to 30 November 1974

NGL44-033-017

M. S. Sohel, Ph. D. Associate Professor Electrical Engineering Department College of Engineering Prairie View A&M University

Mr. Pat Rozas, EE-6

Lyndon B. Johnson Space Center

Houstón, Texas 77058

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## A Final Report

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## RADAR CROSS SECTIONS OF STANDARD AND COMPLEX SHAPED TARGETS

Research Project: NGL44-033-017

Principal Investigator: M.S. Sohel, PhD.

#### Submitted to

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National Aeronautics and Space Administration

## ACKNOWLEDGEMENTS

I very gratefully acknowledge the cooperation and guidance received from Mr. Pat Rozas, supervisor of this project, Lyndon B. Johnson Space Center, Houston, Texas. Thanks are also due to my students for their contritutions in the completion of this report. I am deeply indepted to Dean Austin E. Greaux, P. E., College of Engineering, Prairie View A&M University, for his kind support and encourgement.

Special thanks are also due to National Aeronautics and Space Administration for providing the fininancial assistance, under Grant No. NGL44-033-017, to conduct this research. My secretaries Ms. Jackie Kimble and Ms. Annie Johnson deserve special thanks for their typing services. ABSTRACT

This study presents in a systematic form the theoretical, analytical, and experimental results of radar-cross-sections of targets of different shapes. This report is designed to give the engineer a feel for the gross features of the target and the resulting radar-cross-section to be expected. This will heip him then to begin a detailed analysis inorder to obtain a better prediction of the true RCS of the target. Various techniques useful to predict RCS are given. RCS of finite standard targets is presented. Then a presentation of techniques used to predict the RCS of complex targets is made. Finally, RCS of complex shapes is given. This report will be very helpful to accomplish National Aeronautics and Space Administration goal of predicting the RCS of candidate target?

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## CONTENTS

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1.	Cover Sheet	1.
2.	Acknowledgements	2.
3.	Astract	3.
4.	Introduction	4.
5.	RCS of Standard Targets a. Finite Cones and Disks b. Flat Plates c. Frustum d. Finite Rectangular Cylinders e. Blunted Cone Tips f. Spherical Shell Segment g. Dielectric or Plasma Scatterers h. Cross Polarization Diagnostics	11. 20. 26. 35. 39. 45. 52. 57.
6.	RCS of Complex Targets By Various Techniques a. Scattering Center Theory b. RCS of Complex Shapes c. Computerized Ray Optics Method d. Microwave and Optical Simulation Techniques	65. 72. 79. 84.
7.	Bibliography	87.

3-a

## Introduction

Radars were developed by independent efforts of several countries during the early twentieth century. Basically speaking, it is an electronic eye useful:

- To detect and locate targets which are obscured to the naked eye because of distance or environmental conditions.
- (2) To determine the physical shape of a target, from the knowledge of the incident energy and reflected energy.
- (3) To determine the speed of the moving target.
- (4) To determine the type of material the target is made of.
- (5) To guide airplanes when the pilot is not able to see due to bad weather conditions.

#### RADAR-CROSS-SECTION

In order for a radar to determine the physical shape of an object, the utilization of the radar-cross-section is employed. Radar-Cross-Section or RCS is defined as 4 times the ratio of the back solution power per unit solid angle to the incident power per unit area. It maybe noted here that radar-cross-section has units of area and is generally denoted by (**T**).

# back scattered power/unit solid angle incident power/unit area

-5-

In other words, the reflectivity of the target at which a radar signal is incident is expressed by the radar-cross-section, which includes eddects of area, configuration, size and material of the target.

## METHODS OF DETERMINING THE RADAR-CROSS-SECTION

Research on RCS dates as far as 1949. Some of the methods found in the earlier research were used in World War II to determine targets of interest to the United States Military. Some of the earlier methods are:

- Using pulse signals and measuring the electric field strength.
- (2) Using continious wave (cw) signals and measuring the standing wave distribution or measuring the doppler shift (shifts caused by the effect of target or medium motion with relative to each other.)
- (3) Method.
- (3) Methods using frequency modulated continious wave signals in frequency modulated radars.

Today, there are techniques such as:

- (1) Physical Optics
- (2) Geometrical Theory of Diffraction
- (3) Creeping Wave Analysis
- (4) Impulse Response Theory

Physical optics is used to calculate the radar-cross-section for perfectly conducting bodies. This theory explains the behavior of light and takes into account the phasing between scatters. The physical optics theory arises from the radiation integral which assumes that the surface current is the same attany point as it would be at that point on an infinite plane tangent to the body at that point and assumes further the existence of a sharp shadow boundary, beyond which surface current is identically zero, Unfortunately, the approximation is poor at just those parts of the surface of the body that are most important in determining the value of the integral. Therefore, physical optics frequently give poor results.

This theory has certain limitations such as:

- When the theory is applied to bistatic cases (transmitter and reciever in different places) it yields results that do not conform to the principles of reciprocity.
- (2) Polarization dependence of backscattering cannot be obtained from using this method.
- (3) Physical optics is unable to account for effects for arising from diffraction or creeping-wave progation into the shadow region of a body.

However, physical optics is still used despite it limitations. It is used because in some cases it gives good results such as for perfectly conducting bodies and most of the time can tell in advance for which cases these results can be obtained.

The physical-optics cross section for backscattering of a body' is given by this expression: (Ross, 1966)

$$\sigma^{-} = 4\pi |g(k)|^{2}$$

$$g(k) = \frac{-jk}{a\pi} \int dz \frac{da}{dz} e^{jkz}$$

Where:

 $k = wave number = 2\pi | \lambda$ 

- $\lambda = radar wavelength$
- z = coordinate along the radar line of sight
- A = area of intercept of body with plane perpendicular to radar.

line of sight

However, the expression just sited to give poor results for bistatic scattering. Various methods have been suggested for the modification of physical optics so that it will yield better results. Such suggestions as: modifying the assumed surface currents, or the method used by S. Adachi, which was to continue the integration over the total surface instead of over just the illiminated portion. However, Adachi (1965) method proved rather odd results.

Physical Optics can lead to serious error, mainly because it assumes that the current distribution on a surface is the same at each point.

The most practical of the asymptotic techniques that have been developed so far is the geometrical theory of diffraction, developed principally by J. B. Keller (1960). This theory takes: into account diffracted; as well as reflected rays. Geometrical diffraction theory assumes localization of the scattering at points defined by stationary phase arguments or by abrupt geometric discontinuities. Also, the current distribution of a scattering center is obtainable from that of a known case of similar geometry. Then based on similar known problems a diffraction coefficient is assigned to each center. This coefficient is the function of a phaser proportional to the distance along a ray projected from the scattering center to the radar.

Even though, this theory is practical for many targets it is not yet related to Maxwell's equations. Also, the prediction of cross section near grazing incidence is a problem for the geometrical theory of diffraction. The results from this theory approaches

-7-

infinity near edge on aspect angles due to singularities contained in terms describing multireflections. The effect of multireflections issnot discussed in this study, because radar-crossrsection of the target to be considered in this study can be predicted by the scattering centers in term of single diffraction.

Moreover, the geometrical theory of diffraction has been applied to predict RCS of such bodies as spheres, rectangular flat plates and cones. The theory provides good results except for the nose on aspect angles.

The creeping wave theory is concerned with the waves that passes around the rear of a smooth body. This theory is of importance mainly for small bodies, generally in the resonance region, or for bodies specifically constructed to have low radar-cross-section. The theory is valid for the resonance region mainly because the creeping wave tends to become very small after progating a few wavelengths. The creeping-wave contributions to cross-sections are generally small, ther are usually important for bodies that do not have large scatters on them.

There are two methods for computing the creeping-wace contributions to radar scattering. First, one can perform an asymptotic expansion of the exact solution of the scattering problem and recognize the creeping-wave contributions in the answer through the phase expressions that appear in the answer. However, here one needs the exact solution do the scattering. Second, one can use the geometrical theory of diffraction approach. This method uses

-8;--

the diffraction and decay coefficients so obtained from the geometrical theory of diffraction to calculate the contribution from the creeping-wave.

The impulse-response technique was developed by Kennaugh (1965). This method considers the scattering of a short pulse, an impulse, a step function, or a ramp function rather than the continious wave or short oscillatory pulse normally considered. The method is similar to the impulse-response method used in the investigations of the transient behavior of physical systems such as servomechnisms.

It is noted here that an impulse function can only be approximated and the ideal impulse is not normally generated. Therefore, the hypothetical impulse is not oscillatory, so the entire surface of the body contributes to the scattering. Frim linear systems analsis, it is known that convolution techniques can be used to derive continious waves or short oscillatory pulses from the impulse response.

The impulse-response technique is capable of bridging the gap between Rayleigh scattering and high frequency results into the lower-frequency region, physical optics and geometrical diffraction theory results can thus be made to hold quite well in the resonance region. The impulse-response theory also takes into account combinations of simple shapes and the distortion of a simple shape into a more complex one. This technique permits the use of different computational techniques for diffrent parts of the body, since the impulse response for each region of the body can be added together.

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-9-

The advantages of the impulse-response technique are:

- 1) Its ability to treat scattering in the resonance region
- 2) The simple pictures it gives of scattering
- 3) The ease in which computational methods dan be used
- 4) Its experimental results can be used to improve the results of analytical techniques.

The geometrical theory of diffraction produces good results for many bodies. It has been applied to such bodies as; flat plates, right circular cones, cylinder, frustrums and other bodies. The theory also provides good results for complex and composite bodies.

Moreover, the radar-cross-section of composite bodies such as service satellites, missles and other such bodies are of great concern. This paper will present the radar-cross-section of a missle, by the use of the geometrical theory of diffraction.

#### APPLICATION OF GEOMETRICAL DIFRACTION THEORY TO SCATTERING FROM CONES AND DISKS

The study compares the previous analytical results, obtained by geometrical theory of diffraction for perfectly conducting cones and disks, with experimental results for both horizontal and vertical polarization cases. Presentation is made for cones ranging from 0.98 to 2.87 wavelengths in diameter at the base and having half angles of 4<sup>o</sup>, 15<sup>o</sup>, and 90<sup>o</sup>, the latter corresponds to a disk.

#### TARGET GEOMETRY AND COORDINATE SYSTEM

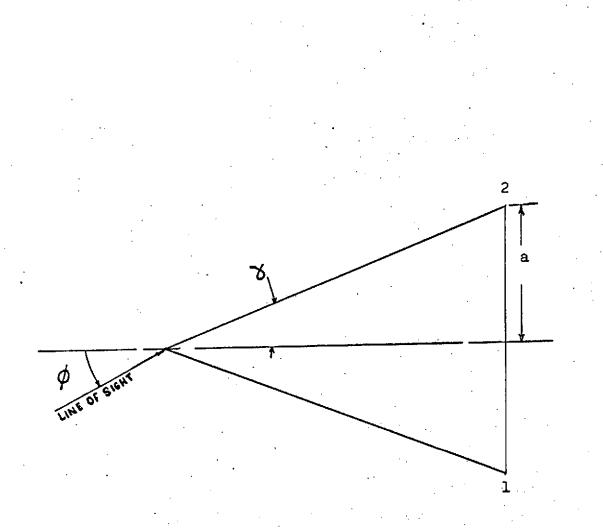
The target geometry and coordinate system used is presented in Figure 1.

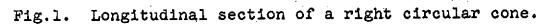
## ANALYTICAL AND/OR EXPERIMENTAL PLOTS

The analytical and experimental results are plotted in Figures 2. through 13.

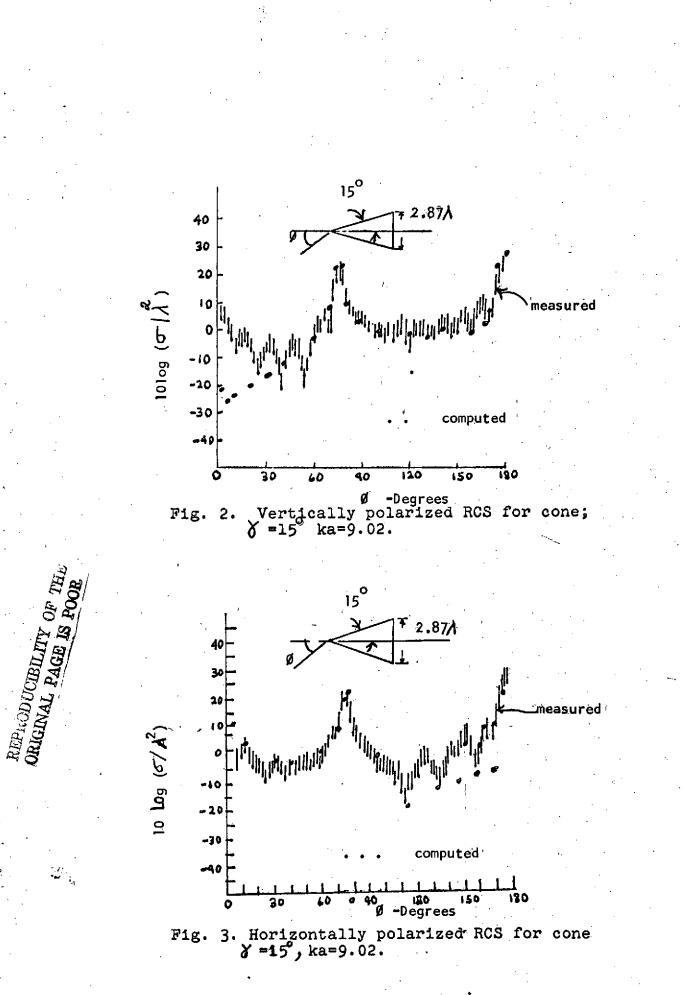
#### INTERPRETATION OF RESULTS

The results seem to agree well. Futhermore, for cones having normalized base circumference (ka) of 8 or 9, the predicted and measured RCS agree well except when the cone is observed within about 30° of nose-on for vertical polarization, in which case large errors occur for some as yet unknown reason. For smaller cones having diameters about equal to the wavelength (ka around 3), the computed RCS is generally predicted within 5dB, but the form of RCS is not predicted very accurately. Baskscattering from a disk of the same diameter for viewing angles within  $60^{\circ}$  of the normal to the base.

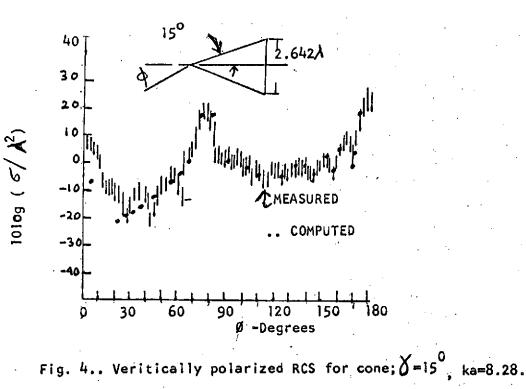


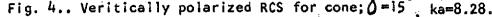


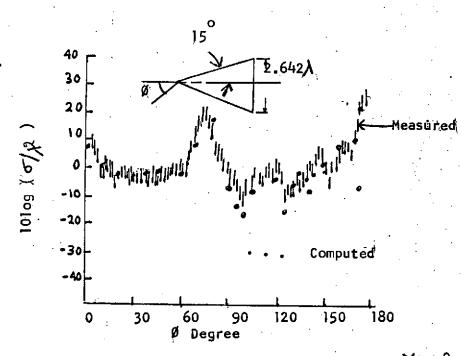
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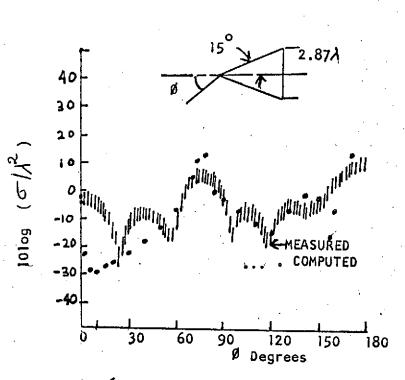




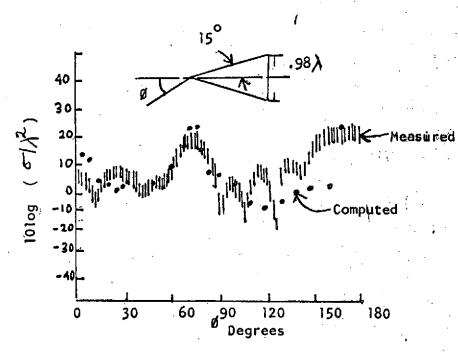
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Horizonitally polarized RCS for cone;  $\mathcal{Y} = 15^{\circ}$ , ka=8.28. Fig. 5.







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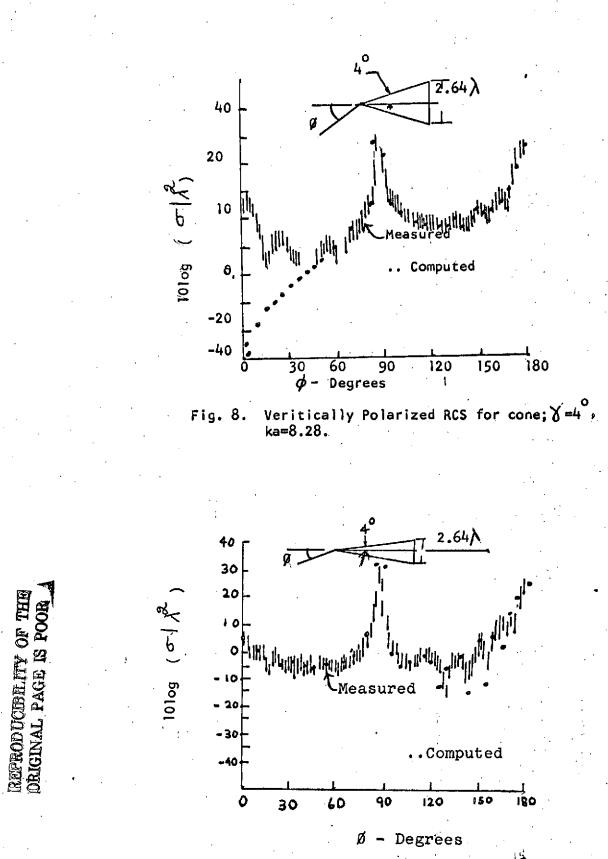
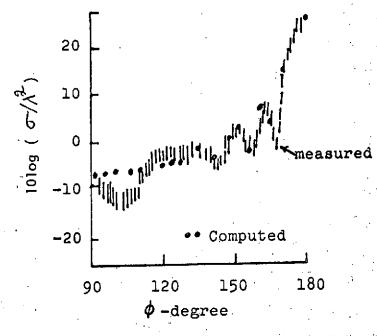
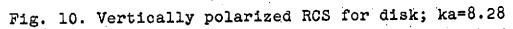
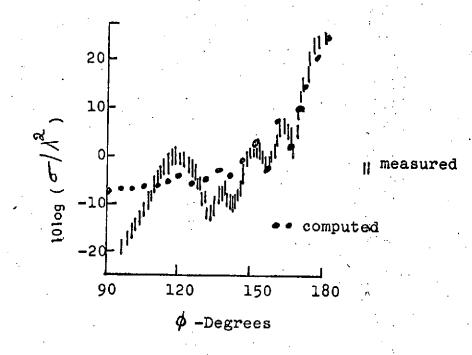


Fig. 9. Horizontally polarized RCS for cone;  $\gamma = 4$ , ka=8.28.

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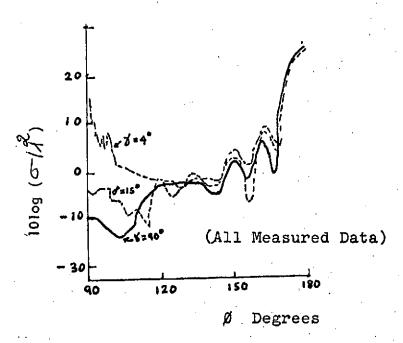


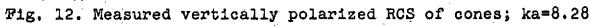


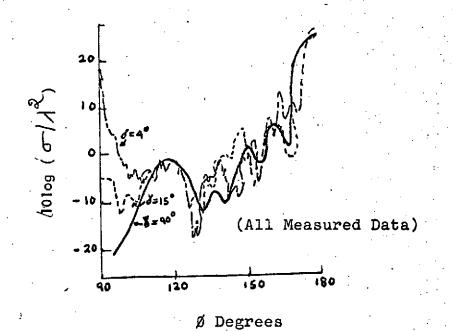


Fig, 11. Horizontally polarized RCS for disk; ka=8.28.

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Fig. 13. Measured horizontally polarized RCS of cones; ka=8.28

## RADAR-CROSS-SECTION OF RECTANGULAR FLAT PLATES AS A FUNCTION OF ASPECT ANGLE

This study investigates the scattering from flat perfectly conducting plates. Radar-Cross-Section results are presented, based upon both theoretical as well as experimental studies. RCS expressions based upon physical optics theory for near specular returns are presented. Geometrical theory of diffraction gives good results for non-specular cases except for edge on case. Based upon experimental measurements, an analytical expression is derived from this data for edge-on case.

## TARGET AND COORDINATE SYSTEM

The target (perfectly conducting rectangular flat plate) and coordinate system used is shown in Fig. 1.

#### ANALYTICAL EXPRESSIONS

Based upon optics theory, an expression of the RCS, for both horizontal and vertical polarization may be written as:

Futhermore, based upon geometric diffraction theory, the RCS expressions may be written:

For the vertical polarization case:

$$\begin{aligned} \nabla \nabla_{g:d.} &= \frac{4b^2}{\pi} \left[ Cod Rha sin \phi - \frac{j sin Rha sin \phi}{sin \phi} \right] \\ &- \frac{i ka - j\pi/4}{\sqrt{R\pi} (2ka)^3/2} \left[ \frac{1}{csp} + \frac{e}{4\sqrt{R\pi} (2ka)^3/2} \left( \frac{(1+sin\phi)e}{(1-sin^2\phi)} + \frac{j 2ka sin \phi}{(1-sin^2\phi)} \right) \right] \\ &- \frac{e}{\sqrt{R\pi} (2ka)^3/2} \left[ \frac{1}{csp} + \frac{e}{4\sqrt{R\pi} (2ka)^3/2} \left( \frac{(1+sin\phi)e}{(1-sin^2\phi)} + \frac{i 4ka - j\pi/2}{8\pi (2ka)^3} \right) \right] \\ &- \frac{(1-sin\phi)e}{(1+sin^2\phi)} \left( \frac{1}{(1+sin^2\phi)} \right) \right] \times \left[ 1 - \frac{e}{8\pi (2ka)^3} \right] \left[ \frac{2}{R} \right] \\ &- \frac{i 2ka + j\pi/4}{R} \left[ Cod R ka sin \phi + \frac{j sin R ka sin \phi}{sin \phi} \right] - \frac{4e}{\sqrt{R\pi} (2ka)^{3/2}} \\ &- \frac{i 2ka + j\pi/4}{\sqrt{R\pi} (2ka)^{3/2}} \left[ \frac{1}{(2ka)^{3/2}} \left( \frac{e}{1-sin\phi} + \frac{e}{(1+sin\phi)} \right) \right] \times \\ &- \left[ \frac{1}{2\pi (2ka)^{3/2}} \left( \frac{e}{1-sin\phi} + \frac{e}{(1+sin\phi)} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^{3/2}} \left[ \frac{1}{2\pi (2ka)^{3/2}} \left( \frac{e}{2\pi (2ka)^{3/2}} + \frac{e}{(1+sin\phi)} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^{3/2}} \left[ \frac{1}{2\pi (2ka)^{3/2}} \left( \frac{e}{(1-sin\phi)^2} + \frac{e}{(1+sin\phi)^2} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{e}{2\pi (2ka)^3} + \frac{e}{(1+sin\phi)^3} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} \left( \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right) \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} + \frac{1}{2\pi (2ka)^3} \right] \\ &- \frac{1}{2\pi (2ka)^3} \left[ \frac{1}{2\pi (2ka)^3$$

EXPER

Three targets (aluminum material) are fabricated for monostatic measurements on the Cornell Aeronautical Labs X-band CW radar range at 1.28 inches wavelength. The dimensions of the plate are shown in the respective figures.

## ANALYTICAL AND/OR EXPERIMENTAL PLOTS

Figures 2 and 3 show the plots obtained from the measured 3 and analytical data.

Futhermore, experiment was carried out to measure RCS at grazing indidence ( $\oint$ =90°). Results are shown in figure  $\frac{4}{7}$ .

An analytical fit to the experimental data show the following accurate expression:

$$\nabla \left( 4 = 90^{\circ} \right) = \frac{\alpha}{\lambda} \frac{b^{2}}{b^{2}} \left[ \left( 1 + \frac{\pi}{\lambda} \frac{1}{\lambda} + \frac{1}{\lambda} \frac{1}{\lambda} + \frac{1}{\lambda} \frac{1}{\lambda} \right)^{2} \right] \\
 + \left( 1 - \frac{\pi}{2} \frac{1}{\lambda} \frac{1}{\lambda} + \frac{1}{\lambda} \frac{1}{\lambda} \right)^{2} \cos \left( 4 \frac{1}{k^{2}} - \frac{3\pi}{5} \right)^{2} \right]$$

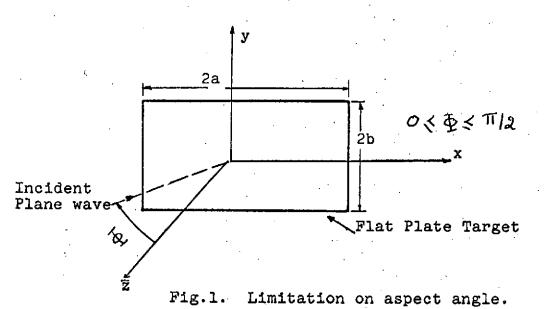
for the vertical polarization case and

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for the horizontal polarization case.

## INTERPRETATION OF RESULTS

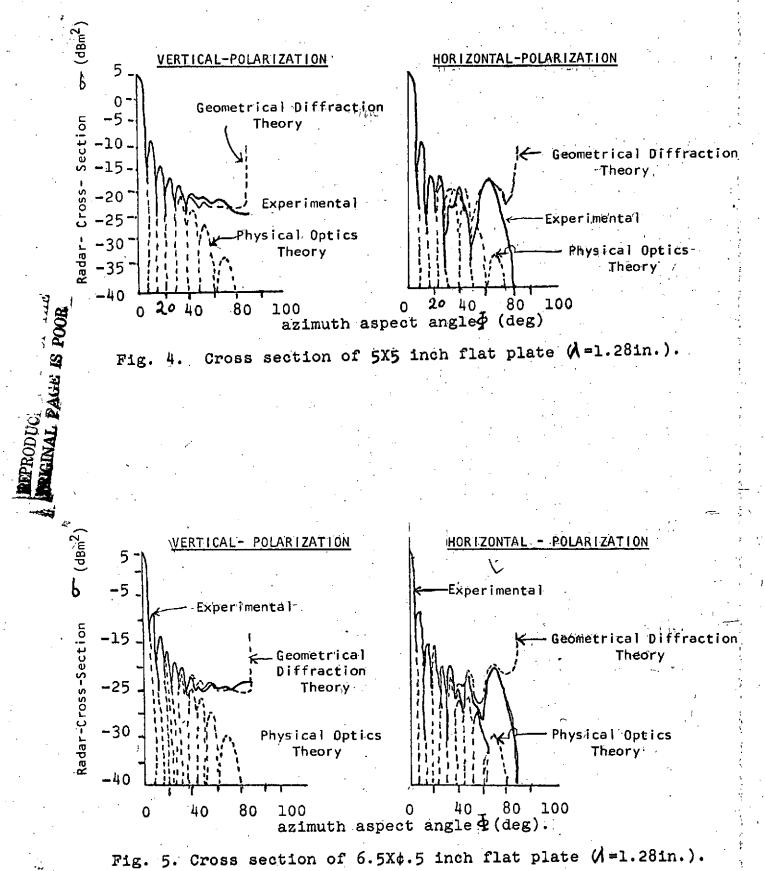
A comparasion of the results shows that physical optics theory is valid for a near specular aspect angle incident, whereas geometrical theory of diffraction is valid for  $3^{\circ} \leq \Phi \leq 8^{\circ}$ but fails for grazing incidence, i. e., for  $\Phi \geq 78^{\circ}$ . An empirical formular obtained from the expremental results shows good fit for grazing incidents on a flat finite rectangular plate. Futher work needs to be done in the area of deriving modified diffraction coefficients at near grazing incidents.



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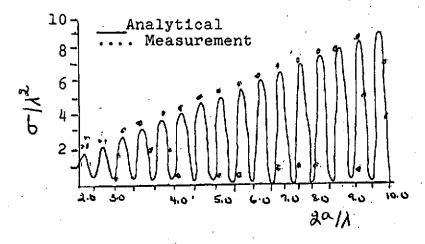
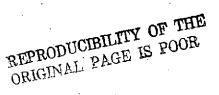


Fig.4. Comparision of analytical fit with measurement data, vertical polarization



BISTATIC SCATTERING MATRIX FOR A FRUSTUM

Keller's geometrical theory of diffraction is applied to derive theoretically the radar-cross-section expressions of a frustum as a function of frequency, aspect angle and bistatic angle. The calculated results from these expressions are in good agreement with the bistatic measurement data.

#### TARGET AND COORDINATE SYSTEM

The target ( perfectly conducting frustrum ) and the coordinate system used is shown in Fig. 1.

#### ANALYTICAL EXPRESSIONS

Symmetry of the problem shows that there are four scattering centers, and the radar-cross-section expressions for them may be written as:

$$\sqrt{\sigma} = \frac{i}{2} \sqrt{\sigma_2} e^{i t}$$
(1)

where  $\sigma$  = RCS and  $\beta$  = phase of the scattered field. Futhermore

$$\sqrt{\sigma_{1}} = \begin{cases} \frac{\sin(\pi/n_{1})}{n_{1}} \sqrt{\frac{\alpha_{1}\cos\phi}{k\cos(\alpha_{1}|2)}} \left[ \left\{ \cos(\pi/n_{1}) - \cos(\frac{\pi+2\phi}{n_{1}}) \right\} \right] \\ + \left[ \cos(\pi/n_{1}) - \cos(\frac{\beta_{1}}{n_{1}}) \right] , \quad \text{if } \in \pi - \alpha - \beta_{2} \end{cases}$$

$$\Phi \gg \pi - \alpha - \beta_{2} / 2$$

$$\sqrt{\sigma_{2}} = \begin{cases} \frac{\sin(\pi/n_{1})}{m_{2}} \sqrt{\frac{a_{2} \csc\phi}{k \cos(R_{-1})}} \left[ \left\{ \cos(\pi/n_{2}) - \cos(\frac{3\pi - 2\phi}{n_{2}}) \right] \right] \\
 + \left\{ \cos(\pi/n_{2}) - \cos(R/2) \right\}^{-1} \right], \quad \Phi_{7} - \alpha + \frac{\beta_{a}}{2} \\
 0, \quad \Phi_{7} - \alpha + \beta_{a}/2. 
 (3)$$

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$$\begin{split} & \sum_{n=1}^{\infty} \frac{(\pi/n_{2})}{n_{2}} \sqrt{\frac{a_{2} \csc \phi}{\beta_{1} \cos(\beta_{1}/2)}} \left[ \left\{ \cos(\pi/n_{2}) - \cos(\frac{3\pi + 2\phi}{n_{2}}) \right\} \right] \\ & \mp \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/n_{2}) \right\} - \cos(\frac{3\pi + 2\phi}{n_{2}}) \right\} \\ & \mp \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/n_{2}) \right\} - \frac{\phi}{\gamma} \approx - \beta_{1}/2 \\ & = \frac{\pi/2}{n_{2}} + \frac{\beta_{1}/2}{n_{2}} = \frac{\phi}{\gamma} \approx - \frac{\beta_{1}/2}{\gamma} \\ & = \frac{\sin(\pi/n_{2})}{n_{2}} \sqrt{\frac{a_{2} \csc \phi}{\beta_{1} \cos(\beta_{1}/2)}} \left[ \left\{ \cos(\pi/n_{2}) - \cos(-\frac{\pi + 2\phi}{n_{2}}) \right\} \right] \\ & \mp \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} - \frac{1}{\gamma} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\beta_{1}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) - \cos(\pi/n_{2}/2) \right\} \\ & = \frac{1}{2} \left\{ \cos(\pi/n_{2}/2) - \cos(\pi/n$$

And the phase referenced to the base of the frustum are given by:

$$\beta_1 = -\lambda k \cos(\beta a_{12}) [a_1 \sin \phi + \lambda h \cos \phi] + \pi / 4$$

$$f_a = -aka_2 \sin\phi \cos(\beta u/a) + \pi/4$$

$$f_3 = + 2k \cos(\beta n/2) [a_1 \sin \phi - 2h \cos \phi] - \pi/L$$

$$J_4 = +2ka_2 sin \phi \cos(\beta a_{2}) - \pi / 4$$

where lpha is the frustum angle in radians.

$$d = \tan^{-1}\left(\frac{a_2 - a_1}{2h}\right)$$

$$\eta_1 = \frac{3}{2} - \frac{\alpha}{\pi}$$

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 $\mathcal{M}_2 = \frac{3}{2} + \frac{2}{7}$ k = 271/2

Upper sign in above equations correspond to vertical polarization and lower sign corresponds to horizontal polarization.

Also using small approximation, at and near the nose-on axial aspects, one obtains:

At and near the tail-on aspect ( $( \mathbf{p} = \mathbf{N} )$  small angle approximation of equations (2) -(5) yield :

$$\sqrt{T} e = 2 \int \pi \left[ \left( \frac{1}{k} \cos \left( \frac{\beta a}{2} \right) \right) a_2^2 \frac{J_1 \left( \frac{a}{k} \frac{k a_2 \sin \phi \cos \left( \frac{\beta a}{2} \right) \right)}{\left( \frac{a}{k} \frac{k a_2 \sin \phi \cos \left( \frac{\beta a}{2} \right) \right)} e} \right]$$

$$\frac{t}{2} a_2 \frac{\sin(\pi | n_2)}{n_2} \frac{J_2 \left(2 k a_2 \sin \varphi \cos \beta a_{/2}\right)}{\left(\cos(\pi | n_2) - \cos(\beta a_{/2})\right)} \right]$$

REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR For  $\mathfrak{F} = \pi_{l_{\mathcal{A}}} - \mathfrak{R}$ , the expression for the radar-cross-section, using physical optics theory, may be written as:

$$\sigma(\phi = \pi \gamma_2 - \alpha) = \frac{8\pi}{9\lambda} \left[ \frac{a_2^{3/2}}{a_2^2} - \frac{a_1^{3/2}}{a_1^2} \right]^2 \cos\left(\frac{\beta_2}{2}\right) \right]$$
[Sin²q G3q]

## EXPERIMENTAL DETAILS

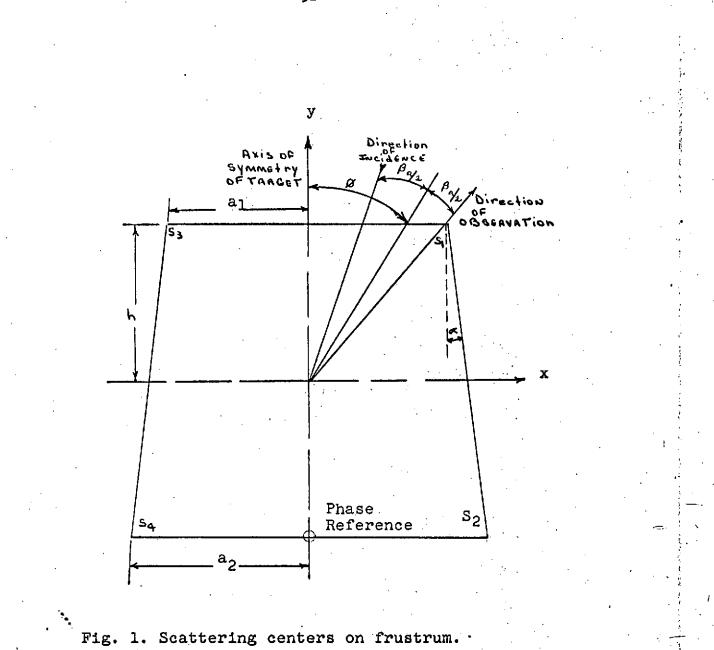
The experiment was conducted by General Dynamics at Forth Worth, Texas. Operating frequency of 6 050 GHz was used. All other details are listed in the respective diagrams.

## ANALYTICAL AND/OR EXPERIMENTAL PLOTS

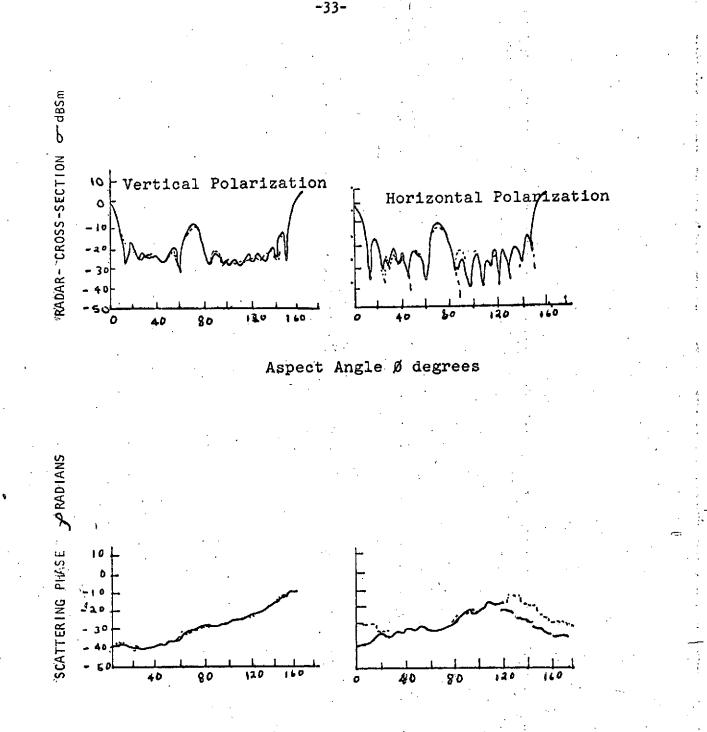
These results are ploted in Figs. 2 and 3.

## INTERPRETATION OF RESULTS

The general agreement between theory and experiment is very good. Generalization of formulas in terms of an unrestricted bistatic parameter  $\beta$  (where  $\beta$  is the projection of  $\beta$  in the azimuth plane) is straight forwarded. Therefore, the theory is suitable for scintillation, doppler spectrum and coherent radar studies, as well as for grosser aspects of RCS investigations.



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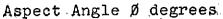
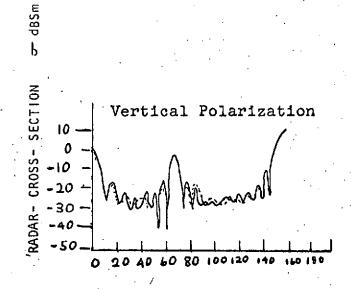
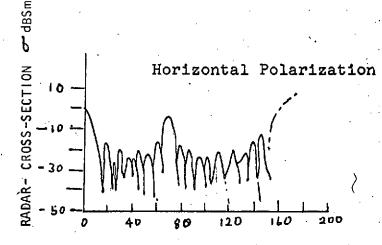


Fig.2. Bistatic scattering matrix for frustrum.  $2a_1=2.507$ ,  $2a_2=3.239$ , 2h=2.083,  $\beta_q$  =30.0 degrees. Dotted line indicates geometrical diffraction theory (single diffraction); solid line indicates experimental.





Aspect Angle Ø degrees

Fig.3. Bistatic radar cross section of frustrum for vertical and horizontal polarizations.  $2a_1=2.510$ ,  $2a_2=3.844$ , 2h=3.804,  $\psi_{\rm C}=30.0$  degrees. Dotted line indicates geometrical diffraction theory (single diffraction); solid line indicates experimental.

-34-

RADAR-CROSS-SECTION OF A FINITE RECTANGULAR CYLINDER

Keller's Geometrical Theory of Diffraction, with scattering centers concept, is applied to investigate the high frequency scattering from a finite rectangular cylinder. Theoretical expressions of RCS as a function of frequency and aspect angle are derived. Experimental work is also reported to compare the results for the mono-static case.

## TARGET AND COORDINATE SYSTEM

The target geometry and coordinate system used is shown in Fig. 1.

#### ANALYTICAL EXPRESSIONS

Based upon this theory, there will be three scattering centers and the final expression for the mono-static radar-cross-section may be written as:

 $= \left[ \sqrt{\sigma_1} \exp j \beta_1 + \sqrt{\sigma_2} \exp j \beta_2 + \sqrt{\sigma_3} \exp j \beta_3 \right]^2$ 

with the amplitude of the contribution reradiated from each center given by

$$\sqrt{\overline{\sigma_{1}}} = \frac{46}{3\sqrt{\pi}} \sin\left(\frac{2\pi}{3}\right) \left[ \left\{ \cos\left(\frac{2\pi}{3}\right) - \cos\left(\frac{2}{3}\pi + \frac{4}{3}\phi\right) \right\}^{2} + \left\{ \cos\left(\frac{2\pi}{3}\right) - 1 \right\}^{2} \right]$$

$$\int \overline{\sigma_{2}} = \frac{4b}{3\sqrt{\pi}} \sin\left(a\pi_{3}\right) \left[ \left\{ \cos\left(2\pi_{3}\right) - \cos\left(4\psi_{3}\right) \right\}^{2} + \left\{ \cos\left(2\pi_{3}\right) - 1\right\}^{2} \right]$$

$$\sqrt{\sigma_{3}} = \frac{4b}{3\pi} \sin\left(\frac{2\pi}{3}\right) \left[ \left\{ \cos\left(\frac{2\pi}{3}\right) - \cos\left(\frac{2\pi}{3}\right) - \cos\left(\frac{2\pi}{3}\right) \right\} \right]$$

$$= \left\{ \cos\left(\frac{2\pi}{3}\right) - 1 \right\} \right]$$

and with the phase of contrubution reradiated from each center given by:

$$S_1 = -2k(a \sin \phi + c \cos \phi) + \pi/4$$

 $f_2 = -2k(a\sin\phi - c\cos\phi) + \pi/4$ 

 $f_3 = 2k(asin\phi - c \cos\phi) + \pi/\gamma$ 

 $k = 2\pi / \lambda$  :  $\lambda$  = wavelength.

These equations were programmed on computer for 0.5°  $< \oint < 89.5^{\circ}$ 

## EXPERIMENTAL DETAILS

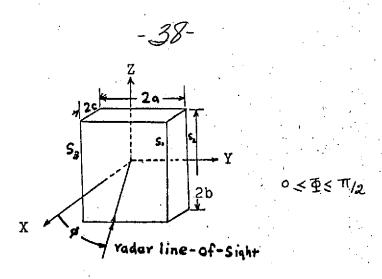
Experiment was conducted at Cornell Aeronautical Labs, to measure the mono-static radar-cross-section of the rectangular cylinder using ka band pulsed-radar range with operating frequency 34.85 GHz. The model dimensions used are:  $2a = 14.763 \lambda$ ;  $2b = 171716 \lambda$ ;  $2c = 2.26 \lambda$ .

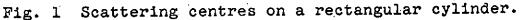
# ANALYTICAL AND/OR EXPERIMENTAL PLOTS

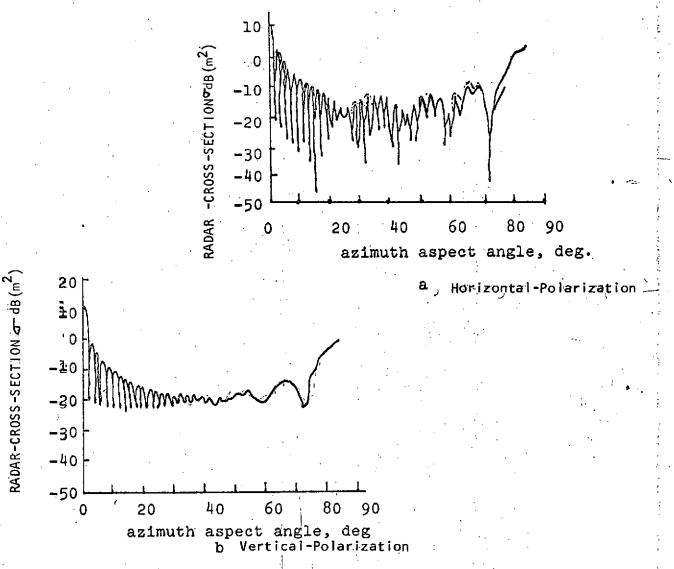
The results are plotted in Figs. 2a and 2b.

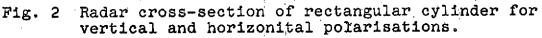
## INTERPRETATION OF RESULTS

There seems to be a good agreement at all aspect angles in both cases between theory and experiment. It will improve for long cylinders and when the effect of multiple diffractions terms are also taken into account. The present analysis can be extended to handle bistatic and specular cases. The espressions valid for arbitrary aspect angles are yet to be developed.









Experimental

Theoretical (Single-diffraction terms only)

# RADAR SCATTERING FROM BLUNTED CONE TIPS

In this study radar-cross-section expressions are developed by using exact electromagnetic theory for:

- 1. Ball-point tip cone
- 2. Round-tip cone
- 3. Concave-tip cone

Results obtained from these expressions are further compared with the results obtained by Physical Optics Theory and the so called "Crude Model Theory," which approximates blunt cone as a combination of pointed cone plus sphere.

## TARGET AND COORDINATE SYSTEM

1. Ball-point tip semi-infinite cone is shown in Fig. 1a. where r = a for  $o \leq \theta \leq \pi - d$ 

 $\theta = \pi - \alpha$  for 27a

2. Round-tip semi-infinite cone is shown in Fig. 1b.

where  $r = -R \sec(\sqrt{\Gamma} \cos \theta + \sqrt{\cos^2 \theta - \cos^2 \alpha})$ 

for

 $R = a \cot \alpha$ 

3. Concave-tip semi-infinite cone is shown in Fig. lc.

where r = R

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# ANALYTICAL EXPRESSIONS

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1. Using exact theory, the radar-cross-section of a ballpoint tip cone may be written as:

$$\sigma = \pi/k^{2} \left[ \sum_{y} \frac{y(y+i)}{N_{y}} \exp(iy\pi) - \sum_{h} \frac{\mu(h+i)}{N_{h}} \exp(j\mu\pi) \right] - 2j \left[ \sum_{y} \frac{y(y+i)}{N_{y}} \exp(iy\pi) \frac{J_{y}/n_{y}}{n} - \sum_{h} \frac{\mu(\mu+i)}{N_{h}} \exp(i\mu\pi) \frac{J_{h}/n_{h}}{n} \right] + jJ_{y}/n_{y} \mu - \sum_{h} \frac{\mu(\mu+i)}{N_{h}} \exp(i\mu\pi) \frac{J_{h}/n_{h}}{n} + \frac{J_{h}/n_{h}}{n} \right] + \frac{\gamma(n+i)}{2} \left[ 1 + J_{h} (\alpha/2) + \psi(n+i) + \psi(n+i) + \psi(n+i) - 2\psi(i) \right] + 2n(n+i)^{2} \left[ 1 + J_{h} (\alpha/2) + \psi(n+i) + \psi(n+i) + \psi(n+i) - 2\psi(i) \right] + 2n(n+i)^{2} + 4n(n+i)/3 + 3(n-i) + n(n+i)(n+2)/2 \left] \alpha^{4}/n_{h}$$

$$\frac{\mu_n s}{n+\frac{n(n+1)}{4}} \frac{q^2}{4} + \left\{ \frac{n^2 (n+1)^2 \left[ 1+2 \left[ n(q/2) + \psi(n+1) \right] + \psi(n+1) - \frac{n(n-1)(n+1)}{2} + n(n+1)(2n+1) - n(n-1)(n+1) + \frac{n(n+2)}{2} - n(n+1)/3 \right\} \frac{q^4}{16}$$

$$\begin{bmatrix} N_{y_n} \\ N_{\mu_n} \end{bmatrix} = a_n(n+1)/a_{n+1} \left\{ 1 \pm \alpha^2 a_n(n+1)/a_{(a_n+1)} \right\}$$

These approximations are valid, provided that れぺくくえ 11. Using exact theory, radar-cross-section expressions for a round-tip and concave-tip cones may be written as:

$$\sigma = \pi j k^{2} \left\langle x^{2} j_{2} - 2j \sum_{n,m} j^{m+n} (2m+1) n(n+1) / m(m+1) x \right.$$

$$\left[ \frac{A_{n, \gamma_{m}} - j C_{n, \mu_{n}}}{B_{n, \gamma_{m}}} - \frac{C_{n, \mu_{m}} + j \tilde{A}_{n, \gamma_{m}}}{D_{n, \mu_{n}}} \right]^{2}$$

111. Using physical optics theory, for nose-on incidences, the back-scattering cross-section for the concave tip is: (neglecting the cone termination at infinity)

$$\sigma = 4\pi k^2 R^4 \left[ \frac{(ajkR-1)exp(ajkR)}{(akR)^2} - \frac{(ajkR\omega_3 a-1)exp(ajkR\omega_3 a)}{(akR\omega_3 a-1)exp(ajkR\omega_3 a)} \right]^2$$

IV. Using physical optics theory, the backscattering-cross section may be written as:

$$\overline{\sigma} = \pi a^{2} \left\{ 1 - \frac{\sin \left[ 2ka(1 - \sin \alpha) \right]}{ka \cos^{2} \alpha} + \frac{1 + \cos^{4} \alpha}{4 (ka)^{2} \cos^{4} \alpha} - \frac{\cos \left[ 2ka(1 - \sin \alpha) \right]}{2 (ka)^{2} \cos^{2} \alpha} \right\}$$

V. RCS for round-tip cone, using crude model, may be written as:

 $\sigma = \sigma_{cone +} \sigma_{sphere}$ Futhermore, Table 1 shows scaling of  $(\sigma / \pi a^2)$  min. as a function of  $\alpha$ .

-47-

Tip Shape	(び /  a <sup>2</sup> ) min	Location (ka)
<b>∫</b> Exact	0.7 < <sup>2</sup>	0.8 X
ounded) (Physical (Optics	0.8 ∝ <sup>2</sup>	0.8 X
Exact	0.6 x <sup>2</sup>	0.9 ×
oncave (Physical Optics	م <sup>2</sup>	0.75X
Exact	1.6 x 8/3	0.5 x 2/3
all-Point Crude Model	1.6 × <sup>8/3</sup>	$0.5 \propto^{2/3}$

# Scaling of $(\frac{\sigma}{\pi}a^2)$ min As a Function of $\alpha$

TABLE 1

## ANALYTICAL AND/OR EXPERIMENTAL PLOTS

The above equations are programmed on a computer and results are plotted in Figures 2, 3, 4, and 5.

## INTERPRETATION OF RESULTS

For the ball-point tip case, exact theory agrees very closely with the crude model ( $\mathbf{T} = \mathbf{T}$  cone +  $\mathbf{T}$  sphere) results. The RCS of rounded and concave tips were calculated by means of exact theory and by using physical optics theory. These results show close agreement. The agreement is better for the rounded tip is probably due to the smooth tip cone join, wereas crude model failed miserably in cases of round and concave tip cones.

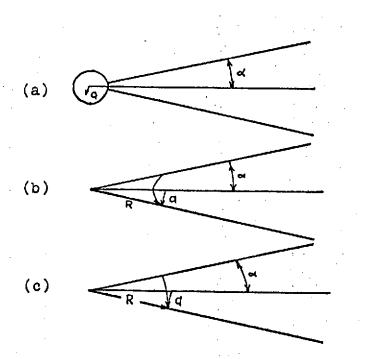
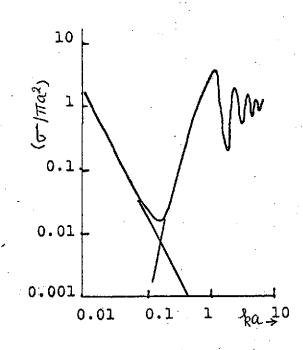
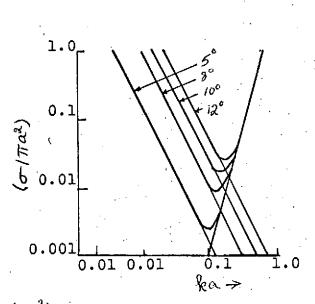


Fig. 1. (a) Ball-point tip. (b) Rounded tip. (c) Concave tip.



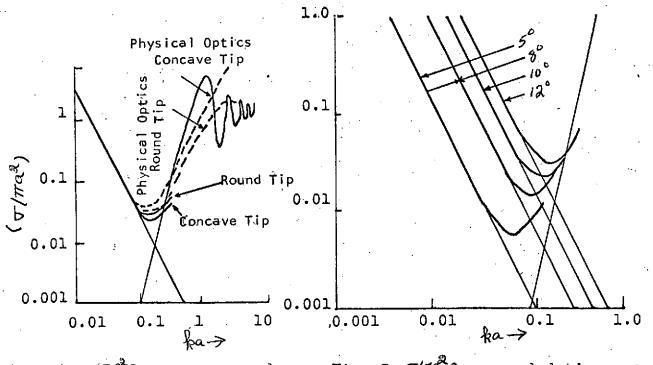
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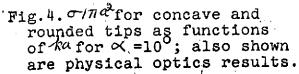
Fig. 2.  $\sigma/\pi a^2$  for ball-point tip as a function of kafor  $\alpha = 10^{\circ}$ ; as a shown lightly are the curves for a pointed cone and an isolated sphere.

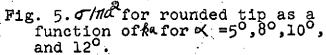


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Fig. 3. $(\sigma/\pi a^2)$  for ball-point tip as a function of  $k^a$  for  $\alpha = 5^\circ$ ,  $8^\circ$ ,  $10^\circ$ , and  $12^\circ$ ; curves for pointed cones and an isolated sphere are shown lightly.







RADAR CROSS SECTION OF SPHERICAL SHELL SEGMENTS

This study derives the far-field backscatter radar cross section of a spherical shell for nose-on and near nose-on aspects for the high frequency case. The theoretical expressions are derived by first computing specular contributions by physical optics method and then adding to it the edge diffracted term. The sommerfield half-plane solution is modified to give the edge contribution. This technique involves deriving a correction factor, based on phase considerations, which takes into account the differences between the basic two dimensional problem considered and the three dimensional problem of interest here. Analytical results are compared with the experimental results.

# TARGET GEOMETRY AND COORDINATE SYSTEM

The target geometry and coordinate system used is shown in Figs. 1, 2, and 4.

#### ANALYTICAL EXPRESSION

Using technique of adding specular terms by physical optics and the edge diffraction term by sommerfield theory; the expression for the RCS, for the nose-on case, may be written as:

= 41 at sin ka (1 - cos 8)

-45-

For the case of a near nose-on aspects, or in a region such that  $\sin\theta \not\ni \frac{1}{2 \text{ kb}}$  (where  $b = 1 \sin \gamma$ ). Furthermore,  $\theta < \gamma$ this region is characterized by the following:

- 1. Specular reflection is present.
- 2. All of the edge is in "lit" region.
- 3. The entire edge is not in phase at any angle.

RCS is given by:

$$\sigma \begin{pmatrix} V \\ H \end{pmatrix} = \pi \alpha^{2} \Big[ 1 - \sqrt{\frac{\sin Y}{4\pi \frac{\pi}{8} a \sin \theta}} \Big]^{2} \\ \left\{ e^{j\eta_{1}} \Big[ \frac{1}{\frac{\sin (\delta - \theta)}{\pi}} + 1 \Big] + e^{j\eta_{2}} \Big[ \frac{1}{\frac{\sin (\delta - \theta)}{\pi}} + 1 \Big] \right\} \Big]^{2}$$

where

$$\mathcal{M}_{i} = a \left[ a \left[ 1 - \cos(\gamma - \theta) \right] + \pi / 4$$

$$n_2 = a ka [1 - cos(8+0)] - \pi/4$$

#### EXPERIMENTAL DETAILS

To compare the theoretical results for nose-on case, experimental data obtained by Blore and Musal (1960 is used. But for the case of near-nose-on aspect, two models are made from this walled copper and measured at the Conduction Corpotation Radar Cross Section Measuring Range. Measurements were made at frequencies of 9.00 KMC and 10.23 KMC, and for both horzontal and vertical polarizations.

#### TABLE I

Dimensions of Models

Model	Radius of Curvature (a)	8	Ring Radius (b)
A	4.44 cm	4810	3.32 cm
' B `	4.44 cm	48½° 60½°	3.32 cm 3.87 cm

#### ANALYTICAL AND/OR EXPERIMENTAL PLOTS

Theoretical and experimental results for both cases are shown in Figures 2, 5, 6, 7, and 8.

# INTERPRETATION OF RESULTS

It may be seen that results obtained are valid when kb>> 1 (where b is the edge radius), for segments smaller than a hemisphere. For nose-on incidence, it is shown that the edge contribution has the same value as the well known specular contribution. An important consequence of this is strong interferences between these two contributors. Comparasion of this result with experiment shows that it is in good agreement. It is found to be much more accurate than the ordinary physical optics results.

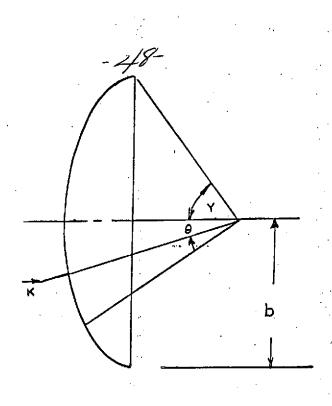
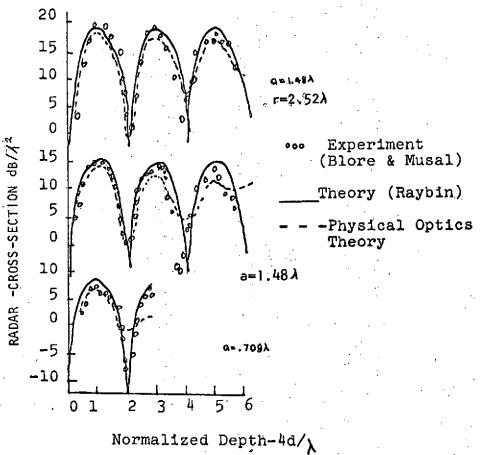
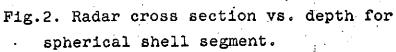
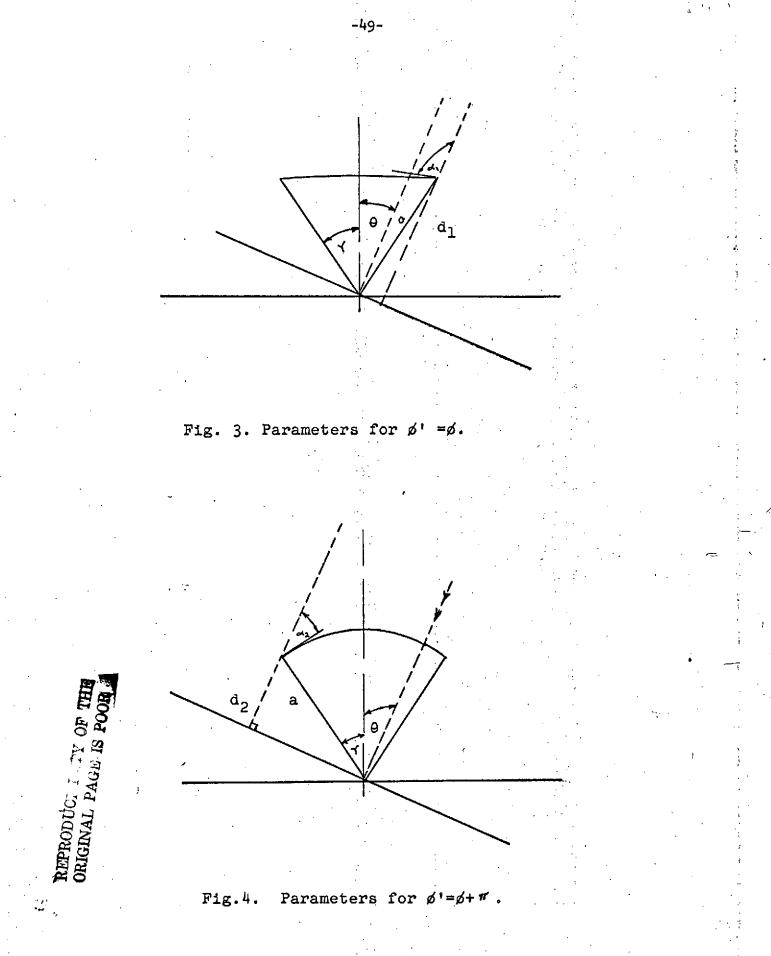


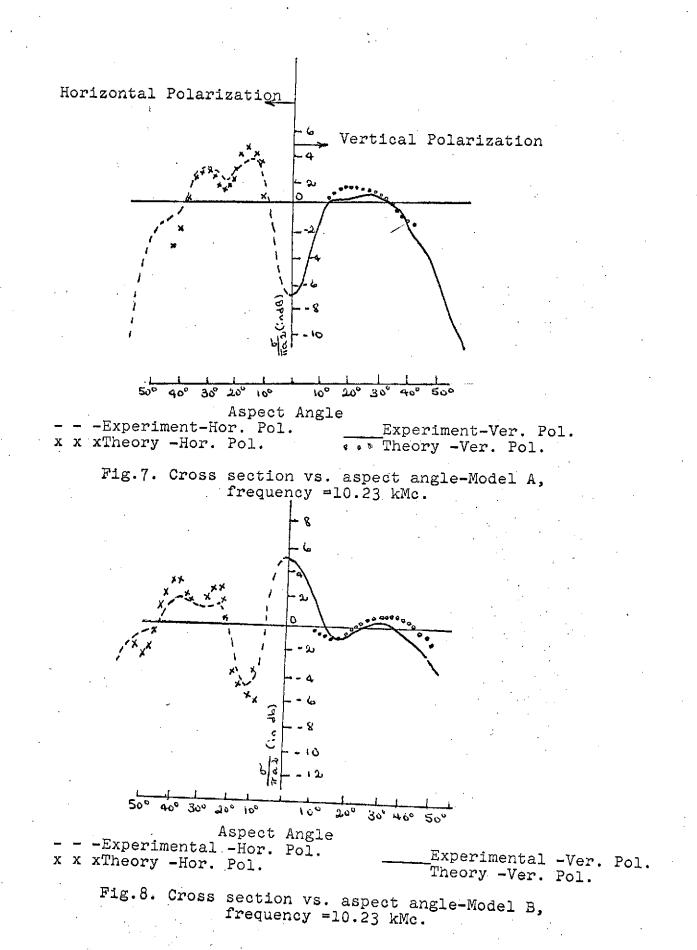
Fig. 1. Spherical shell segment.



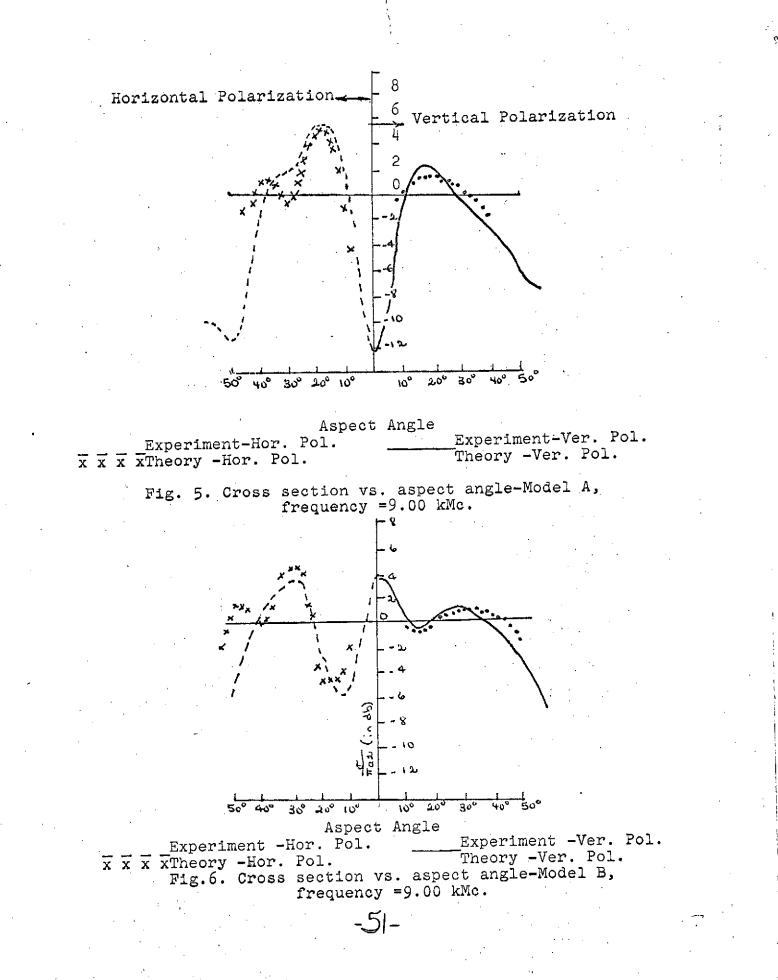




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## APPROXIMATIONS FOR DIELECTRIC OR PLASMA SCATTERERS

The study deals with the calculations of radar-crosssection of non-conducting bodies. Two approximate methods are proposed: The method of super-position approximation, for calculating the RCS of a concentric dielectric-clod sphere. This approximation treats scattering by outer and inner bodies separately; refraction at the free space/dielectric interface are introduces to modify the size of the inner body. This technique is easily applicable but requires that the properties of inner and outer body be known separately. This technique valid prococircied

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where  $r_1 r_2$  are the radii of inner and outer shells.

Second technique called, "the modified geometrical optics theory", is applied to calculate the RCS of dielectric bodies. The basis of this modified geometrical optics methods is ray tracing. The wwave fronts, which are normal to the rays, can be determined by tracing individual paths for a number of rays adjacent to the stationary ray and glory ray.

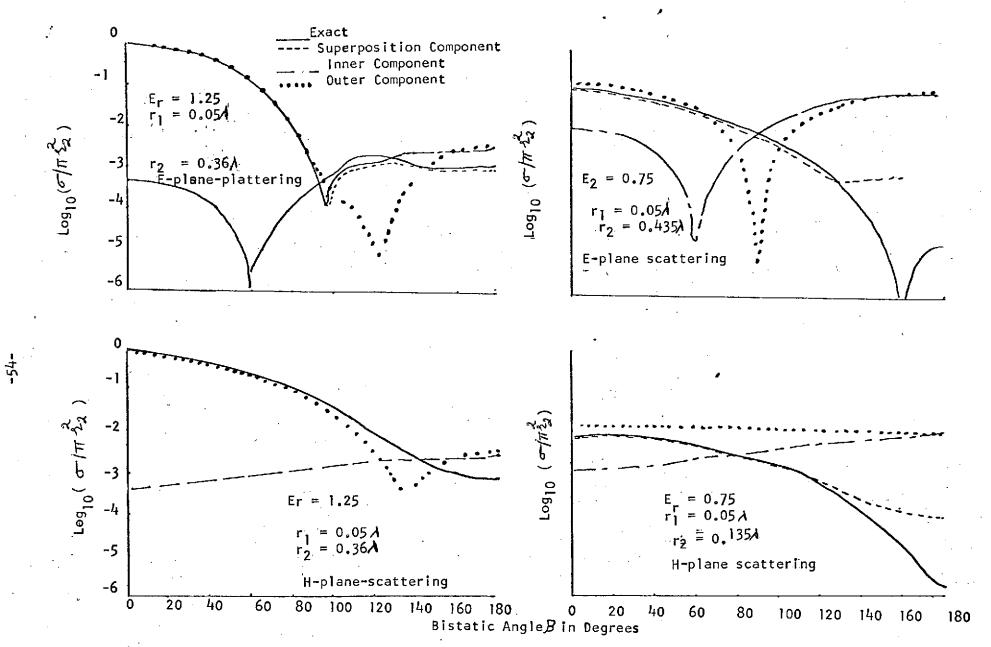
Finally, results obtained by these two methods are compared against the results obtained by exact theory.

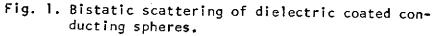
# ANALYTICAL AND/OR EXPERIMENTAL RESULTS

Results obtained by Supperposition, Modified Geometric Theory, and exact theory, techniques are shown in Figures 1, 2, 3, 4, and 5.

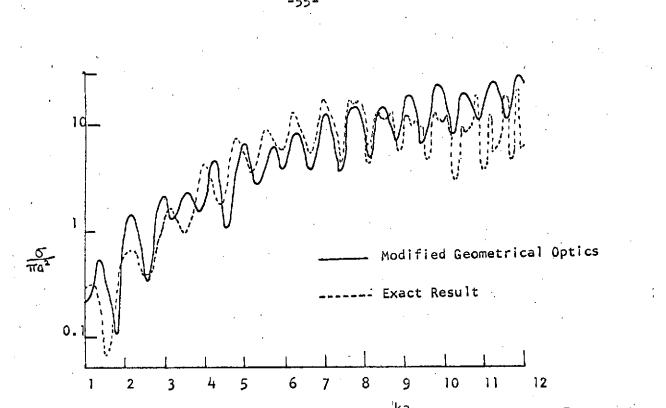
## INTERPRETATION OF RESULTS

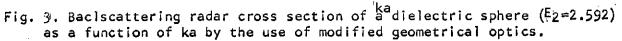
The analysis shows that superposition gives excellent results when the radius of the conducting body is less than  $0.5 \lambda$ . This method fails to predict the depth of the nulls accurately for extremely deep nulls and for bodies with larger inner radius but predicts the maxima for such cases with reasonable accuracy. The modified geometrical optics theory should be used for larger inner bodies if the depth of the nulls is of interest. The results obtained from these studies seem to be in good agreement with theory.





# Fig. 2. Bistatic scattering of dielectric coated conducting spheres.





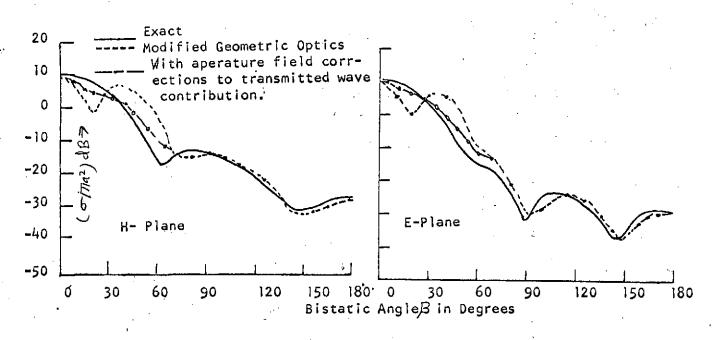
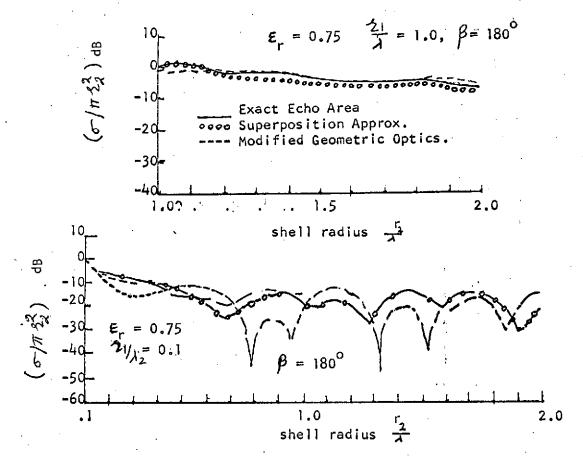
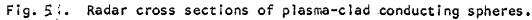


Fig. 4 Bistatic cross section of a plasma sphere with  $\epsilon$ =0.74 and a $\lambda$ =0.75.





## CROSS POLARIZATION DIAGNOSTICS

When a body is illuminated by an electromagnetic wave, the backscattered field usually includes direct and cross-polarization components. Historically, the former has been more widely studied because it is the component typically sensed by nomostatic radars and since it contains all specular contributions, it tends to be larger of the two. In contrast, the cross-polarized return is produced by more subtle contrubutions which elementary theories cannot predict.

Because of this depedence on the finer details of the object, the cross polarized return contains information about the scatter that is not readily obtainable from the direct return. The relationship of the transverse body dimensions and severity of any edges to the cross polarized RCS is shown.

#### ANALYTICAL EXPRESSIONS

Based upon geometrical theory of diffraction, for a right circular cone with half-angle  $\mathcal{X}$ , an expression for cross-polarized RCS ( $\mathcal{X}_{cr}$ ) may be written as:

$$\frac{\sigma_{cr}}{\lambda^2} = \frac{1}{\pi} \left\{ A ka J_2(\xi) \right\}^2$$

-57-

where  $A = n^{-1} \cot \pi I(2n)$ ;  $n = \frac{3}{2} + \frac{3}{2}I\pi$ ,  $\xi = 2Ka$ . Sin Ø and  $J_2(\xi)$  is the bessel function of second order. Equation 1 reduces to an expression for the disk for n = 2 but is relatively insensitive to cone angle. Similarly, an expression for a cone-sphere may be written as:

 $\frac{f_{cr}}{\lambda^{2}} = \frac{1}{4\pi} \left\{ \frac{\cos^{2} r \cos \psi}{\cos 2r + \cos 2\psi} \right\}^{2} \left\{ J_{2}^{2}(\xi) + t_{an}^{2} r t_{an}^{2} \psi J_{1}^{2}(\xi) \right\}$ 

where  $\xi = 2$  ka cos  $\delta' \sin \phi' = \phi'$  aspect angle.

## EXPERIMENTAL DETAILS

The -S- and -X- band measurements of the backscattering for four axially symmetric bodies: thin disks, right circular cones, cones with rounded edges and cone-spheres, are undertaken. The transmitted and received polarizations are inclined  $\pm 45^{\circ}$  to the horizontal, and the resulting patterns were recorded over an angular range  $-30^{\circ} \leq 5 \leq 30^{\circ}$  about the axis.

#### ANALYTICAL AND/OR EXPERIMENTAL PLOTS

The analytical and experimental results obtained are shown in Fig. 1.

# INTERPRETATION OF RESULTS

The analysis shows that disks and sharply edged cones have the strongest returns, cone-spheres the weakest, and cones with rounded edges have intermediate values. The difference between cones and cone-sphere is as much as 30dB for ka = 20. The agreement between theory and experiment is of the order of 1dB for disks and narrow cones. In case of cone-sphere, agreement with the experiment is reasonable in view of the extreme by low level measures, but the systematic discrepancy for small (ka) suggests that there may be another source of depolarization, such as creeping waves.

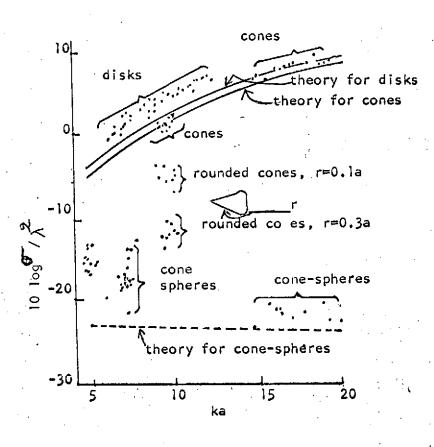


Fig. 1. Cross polarized radar cross sections.

THE BACKSCATTERING RADAR CROSS SECTION OF LONG THIN DIELECTRIC BODIES OF REVOLUTION ON A METAL PLANE

Approximate theoretical expressions are developed for a thin dielectrix body of revolution on a perfectly conduction plane and surrounded by free space. In particular cases of circular sylinder and cone are treated. The development is based upon image theory.

#### TARGET AND COORDINATE SYSTEM

The target and coordinate system is shown in Fig. 1.

## ANALYTICAL EXPRESSIONS

<u>Case 1</u>- For the case of a circular cylinder, f = a, and the RCS expression may be written as:

$$\sigma = \hat{k}^{4} \sqrt{2} \left( A \cos^{2} \alpha + B \sin^{2} \alpha \right)$$
(1)

where  $k = 2\pi / \lambda$  is the free space wave number,  $V = \pi \ell \alpha^2$  is the volume of the cylinder, and

$$A = A(\epsilon, \beta) = \frac{\sin^{4}\beta}{\pi} \left(\frac{\epsilon-1}{\epsilon+1}\right) \left\{ \left(\epsilon+1\right)^{2} + 4\epsilon^{2} \left(\epsilon^{2}\beta\right) \right\}$$
(2)

$$B = B(\epsilon, \beta) = \frac{\sin^{4}\beta}{\pi} \left(\frac{\epsilon-i}{\epsilon+i}\right)^{2} \left\{1 + \frac{\sin^{2}\beta}{\epsilon-\cos^{2}\beta}\right\}^{2} (3)$$
$$-\frac{6}{6}$$

Equation (1) is valid if the following assumptions are made:

$$\frac{\ell}{\lambda}$$
 77 1 (4)

$$ka\sqrt{(e-as^2\beta)} \ll 1$$
 (5)

$$2klas\beta = 71$$
 (6)

<u>Case 11</u>- For the case of a right circular cone, whose lateral surface is defined as:

$$S = \alpha(1 - (z/\ell)), \quad 0 \le z \le \ell$$

۰f

a/e <<1

the RCS expressions are given by equations (1), (2), and (3), where now  $V = \pi \ell^{\alpha^2}/3$ , volume of cone. Assumptions (4) - (8) also apply in this case.

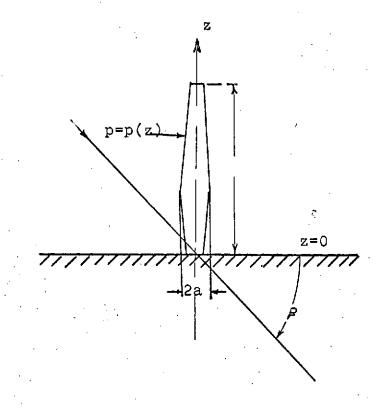
## INTERPRETATION OF RESULTS

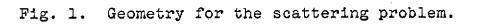
The expressions of RCS derived here are valid for all bodies of revolution satisfying the restrictions outlined and such that on their lateral surface f = f(z):

 $\left| \left( dS \middle| dz \right) \right| << 1$ 

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for oszel





## PREDICTION OF RADAR CROSS SECTION OF A COMPOSITE TARGET USING SCATTERING CENTER THEORY

-65

The radar-cross-section of a composite body consisting of sections of a sphere, cone, cylinder, flare and frustrum is predicted. The theoretical expressions predicted are programmed on a computer and the results are plotted. The cattering center concept is used and such a target will have eight scattering centers.

## TARGET GEOMETRY COORDINATE SYSTEM

The target geometry and coordinate system used is shown in Figures 1 and 2.

## ANALYTICAL EXPRESSIONS

A detailed derviation of scattering center contributions is not required for the composite body. Using Geometrical theory of diffraction, one may write by inspection

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$$\sqrt{\overline{T}_{2}} = \frac{\sin \overline{T}/n_{2}}{n_{2}} \sqrt{\frac{a_{1}csc\phi}{R}} \left\{ \left[ \cos \overline{T}_{12} - \cos \frac{2\pi - 2\phi}{n_{2}} \right]^{1} + \left[ \cos \overline{T}_{12} - 1 \right]^{1} \right\}$$

$$= o; \phi > \phi_{2}$$

$$\sqrt{\overline{T}_{3}} = \frac{\sin \pi/n_{3}}{n_{3}} \sqrt{\frac{a_{1}csc\phi}{R}} \left\{ \left[ \cos \frac{\pi}{n_{3}} - \cos \frac{2\phi}{n_{3}} \right]^{1} + \left[ \cos \frac{\pi}{n_{3}} - 1 \right]^{1} \right\}$$

$$= o; \phi > \phi_{2}$$

$$\sqrt{\overline{T}_{3}} = \frac{\sin \pi/n_{3}}{n_{3}} \sqrt{\frac{a_{1}csc\phi}{R}} \left\{ \left[ \cos \frac{\pi}{n_{3}} - \cos \frac{2\pi - 2\phi}{n_{3}} - 2x F_{2}} \right]^{1} + \left[ \cos \frac{\pi}{n_{3}} - 1 \right]^{1} \right\}$$

$$= o; \phi > \phi_{2}$$

$$\sqrt{\overline{T}_{4}} = \frac{\sin \pi/n_{4}}{n_{4}} \sqrt{\frac{a_{2}csc\phi}{R}} \left\{ \left[ \cos \frac{\pi}{n_{4}} - \cos \frac{2\pi - 2\phi - 2xF_{2}}{n_{4}} \right]^{1} + \left[ \cos \frac{\pi}{n_{4}} - 1 \right]^{1} \right\}$$

$$\sqrt{\overline{T}_{5}} = \frac{\sin \pi/n_{4}}{n_{4}} \sqrt{\frac{a_{1}csc\phi}{R}} \left\{ \left[ \cos \pi/n_{2} - \cos \frac{2\pi + 2\phi}{n_{2}} \right]^{1} + \left[ \cos \frac{\pi}{n_{4}} - 1 \right]^{1} \right\}$$

$$\begin{split} \sqrt{\sqrt{7}} &= \frac{\sin^{-1}\sqrt{7}_{14}}{\sqrt{7}_{14}} \sqrt{\frac{\alpha_{2}\cos\phi}{k}} \left\{ \begin{bmatrix} \cos^{-1}/7_{14} - \cos^{\frac{2\pi+2\theta+2\chi_{F_{2}}}{\gamma_{14}}} \end{bmatrix}^{-1} \mp \begin{bmatrix} \cos^{-1}/7_{24} \end{bmatrix}^{-1} \end{bmatrix} \\ &= \circ ; \quad \overline{\Psi}_{7} \leq \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} \leq \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \frac{2\pi+2\theta+2\chi_{F_{2}}}{\gamma} ; \quad \overline{\Psi}_{8} = \frac{\pi}{4} - 2\pi\pi^{2}\frac{1}{2}\pi^{-1} ; \quad \overline{\Psi}_{8} \leq \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \overline{\Psi} \leq \overline{\Psi}_{8} \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \frac{2\pi+2\theta+2\chi_{F_{2}}}{\gamma} ; \quad x_{F_{1}} = r_{1}\sigma ; \quad \overline{\Psi}_{8} = \pi^{-1}\frac{1}{4} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \overline{\sigma} + 2h_{2}\cos\phi \right] \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \frac{2\pi+2\theta+2\chi_{F_{2}}}{\gamma} ; \quad x_{F_{1}} = r_{2}\sigma ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \overline{\sigma} + 2h_{2}\cos\phi \right] \\ s &= \sigma ; \quad \overline{\Psi}_{7} < \frac{2\pi+2\theta+2\chi_{F_{2}}}{\gamma} ; \quad x_{F_{2}} = r_{2}\sigma ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \overline{\Phi}_{9} \right] \\ s &= \pi^{-1} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad x_{F_{2}} = r_{2}\sigma ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} = \pi^{-1} + 2\pi\pi^{2} \left[ c_{0}\sigma ; \frac{\alpha_{1}-\alpha_{1}}{\gamma} ; \quad \overline{\Psi}_{9} =$$

At a near nose on aspect angles scattering centers  $\rm S_2$  and  $\rm S_5$  (and  $\rm S_4$  and  $\rm S_7)$  expand to form a ring discontinuity. The RCS may be given by:

$$\begin{bmatrix} \int \overline{\sigma_{2}} \, \mathcal{C} \, + \, \int \overline{\sigma_{5}} \, \mathcal{C} \, \end{bmatrix} (\phi = 0) = \frac{\sin \pi / n_{2}}{n_{2}} \, 2a \int \overline{\pi} \, \mathcal{C} \, \int \mathcal{C} \, \frac{1}{n_{2}} \, \frac{\partial \mathcal{L}}{\partial n_{2}} \, \int \mathcal{L} \, \frac{\partial \mathcal{L}}{\partial n_{2}} \,$$

$$\begin{bmatrix} \sqrt{5} \frac{3}{4} + \sqrt{5} \frac{3}{4} \frac{5}{4} \end{bmatrix} (4 \times 10) = 2\sqrt{\pi} \alpha \frac{\sin \pi}{2} \frac{3}{2} \frac{4 k h_3 \cos \phi}{2} \\ \begin{bmatrix} \sqrt{5} \frac{3}{4} + \sqrt{5} \frac{3}{4} \frac{5}{4} \end{bmatrix} \times \frac{3\sqrt{2} \frac{3}{4} \frac{3}{2} \frac$$

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At the tail-on and near tail-on axail aspect, scattering centers  $S_4$  and  $S_7$  again expand to form a ring discontinuity. Then one may have:

$$\begin{bmatrix} J \sigma_{4} e + J \sigma_{7} e \end{bmatrix} (\phi_{2} \pi) = 2 J \pi \alpha \frac{\sin \pi / n_{4}}{n_{4}} e^{-j k_{4} h_{3} c_{4} \phi} \\ = \chi \\ \begin{bmatrix} J \sigma_{4} e + J \sigma_{7} e \end{bmatrix} (\phi_{2} \pi) = 2 J \pi \alpha \frac{\sin \pi / n_{4}}{n_{4}} e^{-j k_{4} h_{3} c_{4} \phi} \\ = \chi \\ \begin{bmatrix} C \cos \pi / n_{4} - C \cos \frac{2 \times F_{2}}{n_{4}} \end{bmatrix}^{-1} \\ X = J_{0} \left( 2 k \alpha_{2} \sin \phi \right) - j \frac{\frac{2 \times F_{2}}{n_{4}} t \cos \phi}{(C \cos \pi / n_{4} - C \cos \frac{2 \times F_{2}}{n_{4}})^{2}} \\ J_{1} \left( 2 k \alpha_{2} \sin \phi \right) \pm \left\{ \cos \pi / n_{4} - i \right\}^{-1} J_{2} \left( 2 k \alpha_{2} \sin \phi \right) \end{bmatrix}$$

For the broadside case ( $\emptyset = \pi/2$ ), the RCS expression may be written as

$$\begin{bmatrix} \overline{y}_{2} e^{j} f_{3} \\ + \sqrt{e} e^{j} e^{j} \end{bmatrix} (4^{\frac{3}{2}} \pi/2) = \begin{bmatrix} -\sqrt{k}a_{1} 2h_{2} \\ \frac{\sin(2kh_{2}c_{0}\phi)}{(2kh_{2}c_{0}\phi)} e^{j} \\ e^{j} f_{4} \end{bmatrix} (4^{\frac{3}{2}} \pi/2) = \begin{bmatrix} -\sqrt{k}a_{1} 2h_{2} \\ \frac{\sin\pi}{h_{2}} + \frac{\sin\pi}{h_{2}} \\ \frac{\sin\pi}{h_{2}} \end{bmatrix} x$$

$$-j2ka_{1}sin\phi$$

## ANALYTICAL PLOTS

The RCS expressions were run on a digital computer with a target dimensions (in inches) for test calculations shown as below:

-67-

 $a_1 = .90'', a_2 = 1.70''$ and  $\lambda = 1.70^{2}$ 

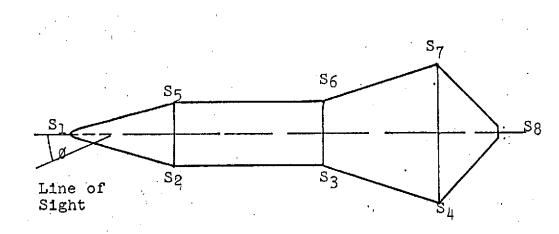
These results are plotted in figures 3, and 47.

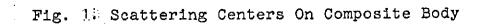
#### INTERPRETATION OF RESULTS

The observed dincontinuties in the predicted RCS indicate aspects for which further modification of geometrical diffraction theory is required. The discontinuity observed for  $\emptyset = 5.6$ degrees is due to the shadowing of ring discontinuity by the contribution due the scattering center S4 and S7 of Figure **2**. For  $\emptyset = 75.6$  degrees, one may replace the return from this ring discontinuity by the contribution due to scattering center  $S_{4}$ , according to equations 14-and 24. The discontinuity observed for  $\emptyset = 10$  degrees is due to the shadowing of scattering center  $S_{E}$ . Multiple diffraction consideration will allow smooth transition here. Two singularities remain in the formulation sue to the use of unmodified geometrical diffraction theory in describing specular scattering by conical surfaces. The effects of these singularities are the two spikes occuring at  $\emptyset = 74.5$ degrees (due to the cone specular) and at  $\emptyset = 70$  degrees (the specular from the flare). Since the theory fails gracefully for conical speculars, physical optics estimates may be introduced in a small angular region centered about specular aspect. The remaining discontinuity occurs at  $\emptyset = 117$  degrees, at which aspect, the return from the ring singularity

is introduced. In actual fact, this ting contribution is valid for aspect with 15 degrees of the tail-on axail aspect since it is based upon small angle approximation.

-68-





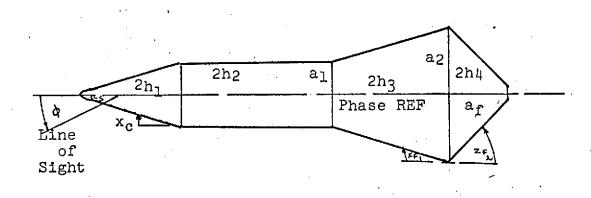
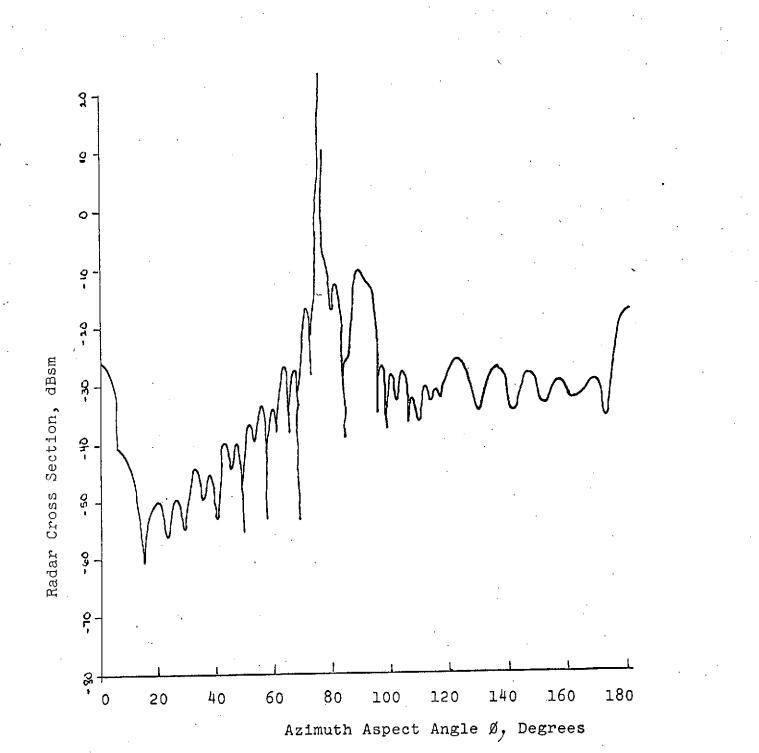
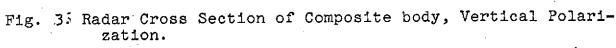


Fig. 2. Composite Geometry





-70-

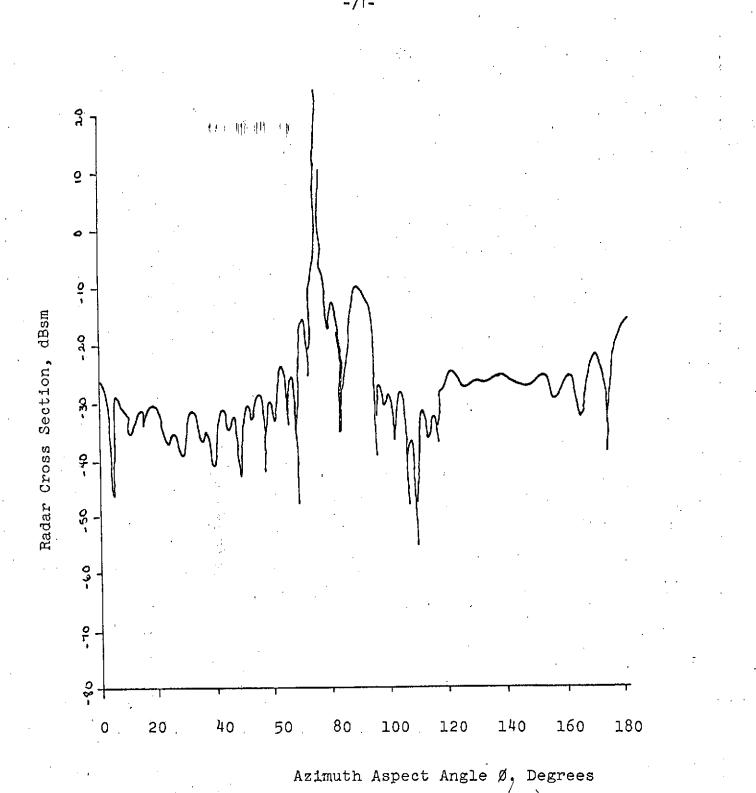


Figure 4, Radar Cross Section Of Composite Body, Horizontal Polarization

-71-

RADAR CROSS SECTION ESTIMATION FOR COMPLEX SHAPES

This study presents a method for estimating RCS of complex shapes such as an aircraft, missle, and satellite. It is based upon methods already developed for simple shapes. The theoretical method for estimating the RCS of complex shapes utilizes the following steps.

- 1. The complex shape is resolved into an ensamble of components each of which can be geometrically approximated by a simple shape in such a way that the RCS of simple shape approximates the RCS of the component it replaces.
- RCS values are computed for the approximations to the components (simple shapes) derived in step (1).
- 3. Steps (1) and (2) are then combined to yield an estimate of the RCS of entire body.

Two methods i. e. "relative phase method" and "random phase method" are proposed. Furthermore, theoretical results are compared against the experimental results.

#### TARGET AND COORDINATE SYSTEM

Two targets are investigated:

A missle model is shown in Fig. T.

An aircraft model is shown in Fig. 2.

#### ANALYTICAL EXPRESSIONS

<u>Relative Phase Method</u> - For any given combination of aspect angle, wave length, and polarization, N components for which RCS values have been computed, e. g., the set of values.

One of the methods of combination involves the consideration of the relative plase angle between the returns from these N scatters. Therefore, the RCS of the entire body may be written as:

$$\sigma_{p} = \left| \sum_{j=1}^{N} (\sigma_{j})^{2} \exp(j \Phi_{j}) \right|^{2}$$

where  $\mathbf{J} =$  the RCS of the *j*th component and  $\mathbf{F}_{j} =$  the relative phase angle associated in the *j*th component.

<u>RANDOM PHASE METHOD</u>- In case where  $\Phi_j$  are randomly distributed, then upon averaging over the  $\Phi_j$ , one obtains the expressions:

$$E[\sigma] = \sum_{j=1}^{N} \sigma_{j}.$$

$$E[\sigma] \pm S$$

$$S^{2} = \left(\sum_{j=1}^{N} \sigma_{j}\right)^{2} - \sum_{j=1}^{N} \sigma_{j}.$$

#### ANALYTICAL AND/OR EXPERIMENTAL PLOTS

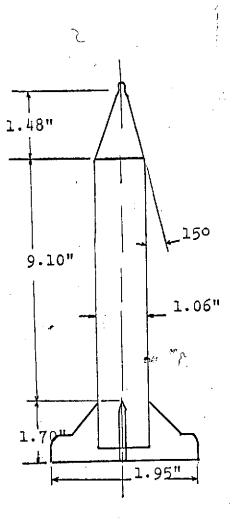
For the case of a Missle, results are shown in Figs. 2,

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23, and 24, and for the case of a large jet-aircraft, results are shown in Figures 36 and 75.

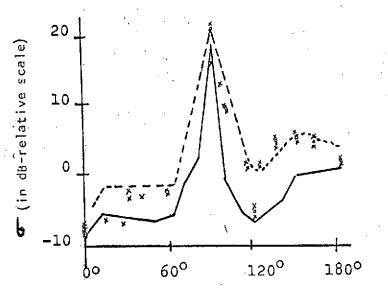
# INTERPRETATION OF RESULTS

It may be noted that relative phase method is not good for large aircrafts at small wavelengths. In such cases random phase method should be used. Techniques discussed here are most effective tools with which to describe modification, and even the design of RCS characteristics of complex shapes.



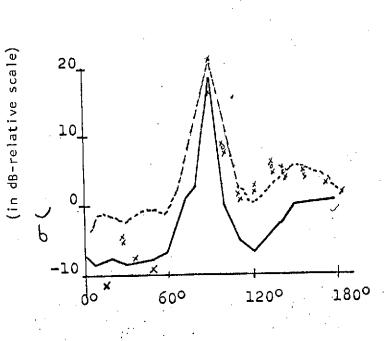


Sketch of missile model.

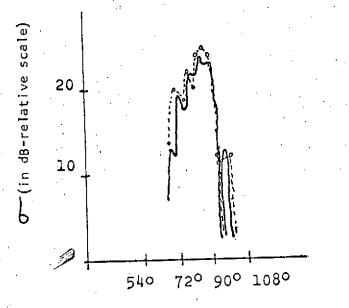


# ASPECT ANGLE

g<sub>2</sub>). Missile with fins — theory and experiment for vertical polarization (E vector normal to plane in which aspect is measured, two of the fins contained in Fig.2/. 



ASPECT ANGLE



# ASPECT ANGLE

F16.3. Missile with fins\_, theory and experiment for E vector slanted at a 45° angle to the plane in which aspect is measured (two fins located in that plane). X X Experimental points;----theory (in-phase estimation);\_\_\_\_\_theory (random phase estimation).

Fig. 4. RCS for a missile near broadside. \_\_\_\_\_ Experimental data; . . theory (relative phase).

-76-

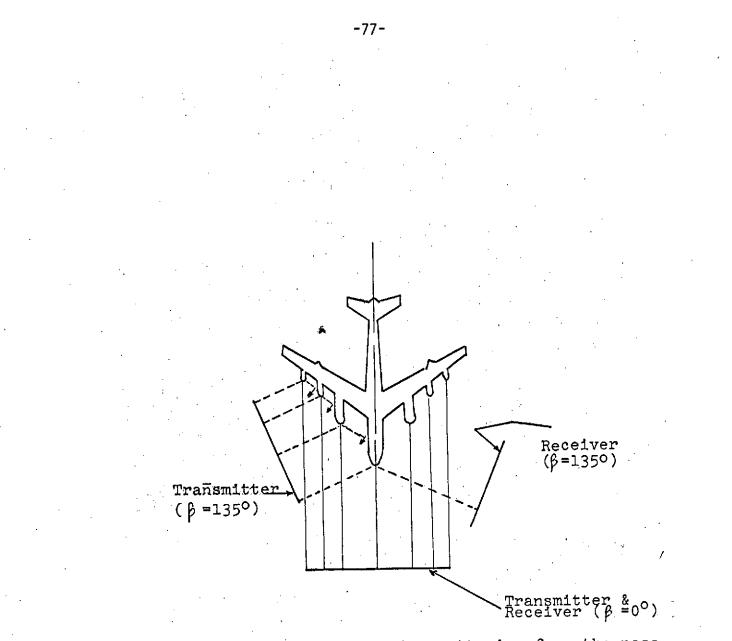
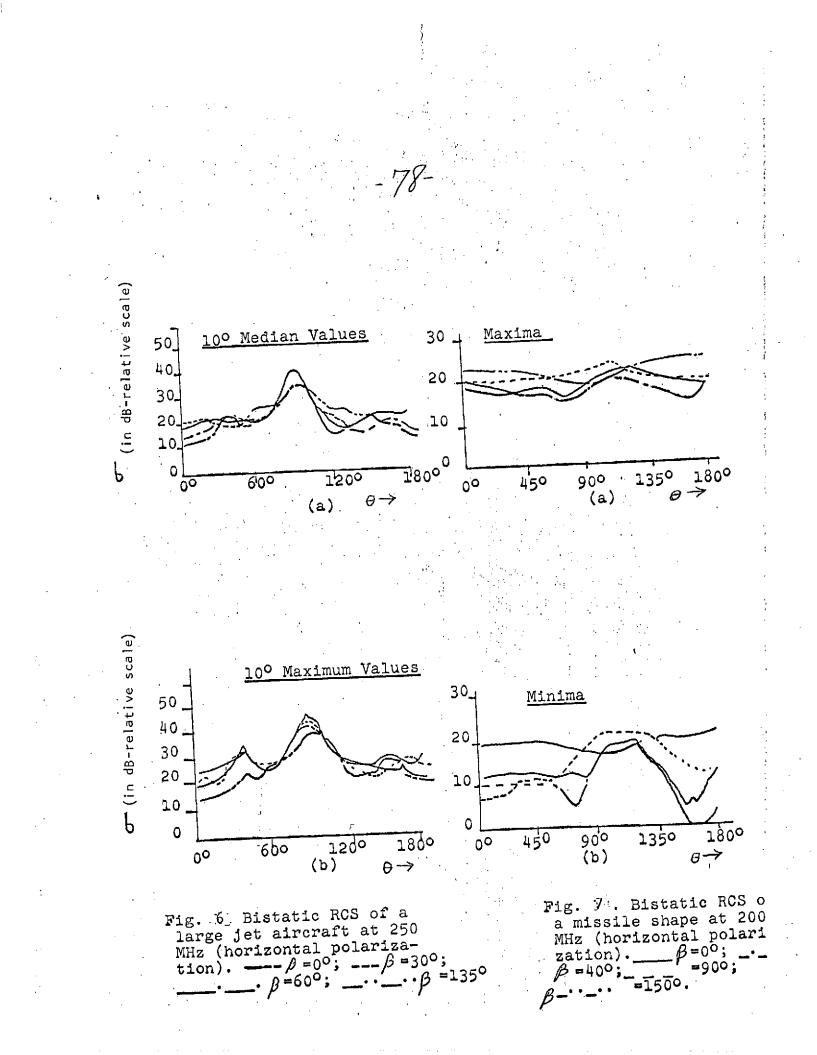


Fig. 5?. Monostatic and bistatic scattering from the nose of a large aircraft (the  $\theta=0^\circ$  case for  $\beta=0^\circ$  and  $\beta=135^\circ$ ).



## COMPUTERIZED RAY OPTICS METHOD OF CALCULATING AVERAGE VALUE RADAR-CROSS-SECTION

In order to estimate the RCS of airborne vehicles, it is often necessary to consider the average values of radar returns. A method providing the quick estimate of the average static radar cross section of the vehicle components would ve useful. This study extends a method of ray optics called computerized ray optics method to determine the RCS of a body of arbitrary shape, and which may be concave and/or convex on which double reflection and depolarization can occur. The reason for this method can be used here on an arbitrary body is that rather than finding an expression for the RCS, a large number ' of rays are simply "thrown" at the body. The reflection boundary conditions for a perfect conductor (Etangential = 0, and Dnormal are continuous) collected at the receiver and summed (vector-wise and phase-wise). Analytical results are compared against the experimented results.

### TARGET GEOMETRY AND/OR CONDUCTIVE SYSTEM

The explanation of the target and coordinate system used is shown in Figs. 1, 2, and 多.

#### ANALYTICAL EXPRESSIONS

The bistatic radar cross section is defined as:

$$(\Theta_{nom}, \phi_{nom}) = (P_{\Theta} (\Theta_{nom}, \phi_{nom}) | dSL) | (P_{N} | 4\pi)$$

-79-

$$J = \frac{4\pi \sqrt{\left[\sum_{ALL,RAYS}^{N} Re(P_0)\right]^2 + \left[\sum_{ALL,RAYS}^{N} Im(P_0)\right]^2}}{(d D_2)(N)(P_2)}$$

$$\mathbf{\nabla \phi} = \frac{4\pi \int \left[\sum_{A \in L, RAYS} Re(P_{\phi})\right]^{2} + \left[\sum_{A \in L, RAYS} Im(P_{\phi})\right]^{2} }{\left[d \cdot \Omega_{L}\right](N)(P_{2})}$$

where

 $P\theta = Re (P\theta) + j Im (P\theta)$  $P\emptyset = Re (P\emptyset) + j Im (P\emptyset)$ 

P<sub>2</sub> is the power in the 2nd incident ray and is equal to unity and N is the number of rays per square meter.

#### EXPERIMENTAL DETAILS

An experimental body is shown in Fig. 3. It is composed of an ogive "O", a cylinder "C", a hemisphere "S", and a winglike body "W". It was is to test the method of computerized ray optics to calculate average values of RCS of bodies that can display 1) interference phenomena, 2) double reflections, and 3) depolarization.

#### ANALYTICAL AND/OR EXPERIMENTAL PLOTS

The analytical and experimental plots are shown in Fig. 4.

#### INTERPRETATION OF RESULTS

The analysis shows that agreement between measured and calculated results in generally good and within  $\pm 2dB$ , except at  $\theta = 0$ ,  $\emptyset = 0$ , where a crepting wave was identified experimentally. The angles at

which large creeping wave will be excited can be predicted by observing the angles of glancing incidence at a discontinuity of the surface.

-8,L-

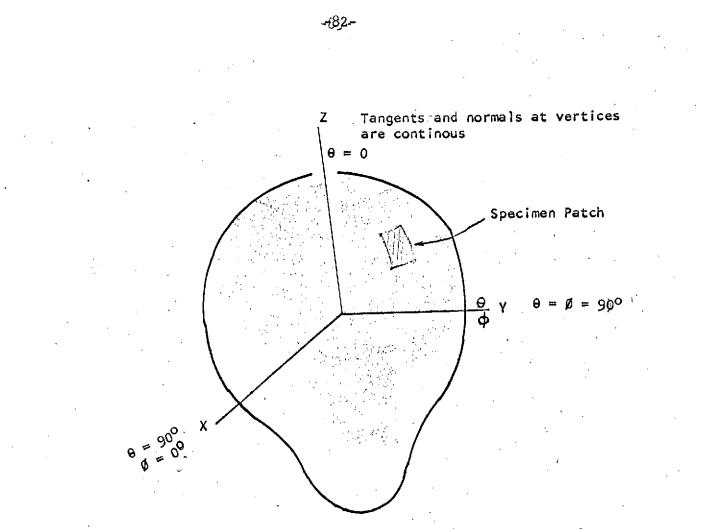


Fig. E. Arbitrary body defined by patchwork surface.

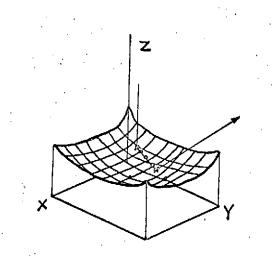
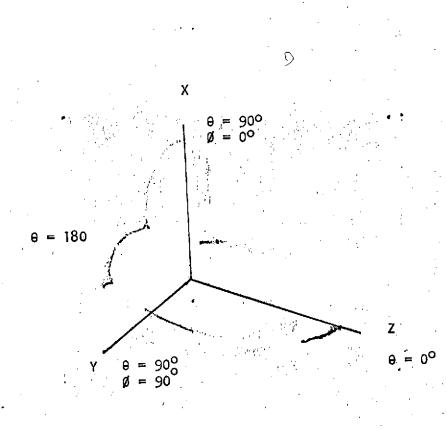
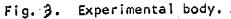
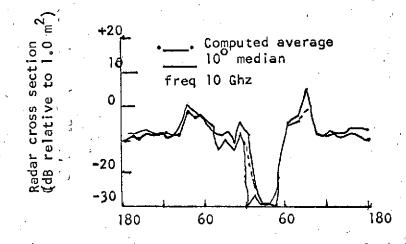


Fig. 2. Double reflection.

\* Ray Hits Block Ray above surface Block Hit Ray below Surface









- 83-

# COMPARASION OF RCS BY MICROWAVE AND OPTICAL SIMULATION TECHNIQUES

Radar cross section of a jet aircraft is obtained using microwave and optical simulation techniques.

## TARGET AND COORDINATE SYSTEM

 $(\frac{1}{4})$  scale model of a modern jet aircraft is used.

## EXPERIMENTAL DETAILS

Mictowave measurement are undertaken using a (cw) balancedbridge RCS measurement system at 4.4 GHz, and  $(\frac{1}{4})$  scale model of a modern jet aircraft model to simulate quasi-monostatic RCS measurements at 8.6 GHz of the full scale aircraft.

The optical simulation measurements are conducted using a monostatic optical simulation system and  $(\frac{1}{4}/35)$  scale model of the same aircraft. The model was loaded with vacum deposit aluminium producing a mirror like surface.

#### EXPERIMENTAL PLOTS

The results obtained from both these techniques are plotted in Fig. 1.

# INTERPRETATION OF RESULTS

The mean radar-cross-sections are considered to be valid for frequencies between 3GHz and 24 GHz. Results of measurement agree with in an average of 3.5 dB and that both techniques can be used to obtain RCS at microwave frequencies of complex shapes such as aircraft.

0

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-10

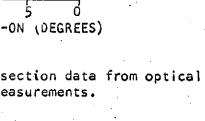
+20 +15 +10 +5

·66-

MICROWA

20 15 10 25 5 Ó AZIMUTH ANGLE FROM NOSE-ON (DEGREES)

Fig. 1. Comparison of radar cross-section data from optical simulation and microwave measurements.



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