## SAO LASER REPORT NO. 6

## PHOTORECEIVER EFFICIENCY MEASUREMENTS

C. G. Lehr

(NASA-CR-142070) PHOTORECEIVER EFFICIENCY N75-15975 MEASUREMENTS (Smithsonian Astrophysical
observatory) $41 \mathrm{pHC} \$ 3.75 \quad \operatorname{CSCL} 20 \mathrm{~F}$
Unclas
 $\qquad$ 63/36 08988

January 1975

Center for Astrophysics
Harvard College Observatory and Smithsonian Astrophysical Observatory Cambridge, Massachusetts 02138

## TABLE OF CONTENTS

Section Page
ABSTRACT ..... v
1 INTRODUCTION ..... 1
2 QUANTITIES MEASURED ..... 3
3 TECHNIQUE USED ..... 5
4 DESCRIPTION OF THE PHOTORECEIVER ..... 7
5 CALCULATIONS ..... 11
6 PROCEDURE ..... 17
7 COMPUTATIONS ..... 19
8 RESULTS ..... 21
9 ACKNOWLEDGMENTS ..... 25
10 REFERENCES ..... 27
Appendix
A BRIGHT STARS USED FOR RECEIVER EFFICIENCY MEASUREMENTS. ..... A-1
B STATION COORDINATES ..... B-1
C FORTH PROGRAM; SAMPLE INPUT AND OUTPUT DATA FOR COMPUTING PMT PARAMETERS ..... C-1
D FORTH PROGRAM AND SAMPLE OUTPUT FOR RECEIVER EFFICIENCY COMPUTATIONS ..... D-1
PRECEDING PAGE BLANK NOT FILMED


#### Abstract

The efficiency and other related parameters of Smithsonian Astrophysical Observatory's four laser receivers were measured at the observing stations by using equipment already available at the stations. If the efficiency is defined as the number of photoelectrons generated by the photomultiplier tube divided by the number of photons entering the aperture of the receiver, its measured value is about $1 \%$ for the laser wavelength of 694 nm . This value is consistent with the efficiency computed from the specified characteristics of the photoreceiver's optical components.


# PHOTORECEIVER EFFICIENCY MEASUREMENTS 

C. G. Lehr

## 1. INTRODUCTION

Laser systems as used for satellite tracking are different from other laser tracking systems (Lehr, 1974). In some ways they are simpler, because:
A. The objects tracked are in stable orbits.
B. Output data are not required immediately.

In other ways, they have requirements that are particularly stringent; for example, they must track objects at megameter ranges with decimeter accuracies. Furthermore, the currently shifting emphasis in application from geodesy to geodynamics, along with the launch of spherical satellites such as Lageos and Starlette, will require both increased range and increased accuracy (Kaula, 1969).

Currently, all laser systems for satellite tracking are pulsed systems (Halme, 1973), whose performance is characterized by the amount of energy in the received signal. This energy is low and is usually expressed in photon counts per pulse or, when a photomultiplier tube (PMT) is used, in photoelectrons per pulse. It is important to be able to calculate and measure $N$, the number of electrons in a return, for two reasons: In the first place, $N$ must be at least unity for the return to be detected, and in the second, the accuracy of a single return increases with $N$. To see this, consider a pulse of width t ns. Assuming the return has the shape of a normal probability density function, the error associated with a return of a single electron is

$$
\begin{equation*}
\sigma_{t}=\frac{t}{2(2 \ln 2)^{1 / 2}} \mathrm{~ns} \tag{1a}
\end{equation*}
$$

[^0]or
\[

$$
\begin{equation*}
\sigma_{R}=\frac{7.5 t}{(2 \ln 2)^{1 / 2}} \mathrm{~cm} \tag{lb}
\end{equation*}
$$

\]

where, for example, $\sigma_{R}=127 \mathrm{~cm}$ when $t=20 \mathrm{~ns}$. However, when $N>1$, we have

$$
\begin{equation*}
\sigma_{\mathrm{N}}=\frac{\sigma_{\mathrm{R}}}{\mathrm{~N}^{1 / 2}} \tag{2}
\end{equation*}
$$

which, for $N=300$, a value just below the point where PMT saturation begins to set in for the RCA 7265 PMT, is

$$
\sigma_{\mathrm{N}}=\frac{127}{300^{1 / 2}}=7 \mathrm{~cm}
$$

In calculating and measuring N values, we also determine the laser receiver's efficiency and related quantities. Then we can do the following:
A. Observe any decrease in receiver efficiency with time.
B. Compare one laser receiver with another.
C. Measure atmospheric extinction at the laser wavelength.

## 2. QUANTITIES MEASURED

The receiver efficiency is the principal result of the measurements described in this report. It is defined herein as the number of photoelectrons generated by the PMT divided by the number of photons reaching the aperture of the receiving telescope. The most important factor in the receiver efficiency is the quantum efficiency of the PMT, but transmission losses in the receiving telescope are also significant. These losses include the aperture blocking of the secondary mirror and its supporting spider, along with absorption in the reflector, lenses, and narrow-band filter. The central wavelength of the measurement is that of the laser, 694 nm , but the measured efficiency is an integrated value over the receiver's bandwidth (several angstroms) rather than over the spectral width $(<1 \AA$ ) of the transmitted laser energy.

Other quantities are obtained along with the measurement of the receiver's efficiency. Of these, the value of the PMT gain is useful because it influences the noisefigure and gain requirements of the video amplifier that follows the PMT. The singleelectron distribution of the PMT is important in distinguishing weak returns from the noise background. The receiver-threshold level can be set lower when this distribution is narrow than when it is wide. The area of a single electron allows the number of electrons in the received pulse to be calculated from the area under the received pulse. The duration of a single-electron pulse is a measure of the overall response time of the receiving system.

## 3. TECHNIQUE USED

Measuring receiver efficiency is similar to measuring the quantum efficiency of a PMT. A technique commonly used at present for the latter requires a calibrated light source for the input and a discriminator and counter for the gain and output measurement (Klobuchar et al., 1974). The procedure is complicated for the general case because it is necessary to consider the wavelength and intensity of the input light as well as the distribution of the light beam over the photocathode. However, certain simplifications result from the limited nature of the present situation. Our measurements are made only for the ruby-laser wavelength of 694 nm , for intensities below the saturation level of the PMT, and for a light beam that covers the photocathode.

The technique described herein uses only equipment already available at an observing station. The input light flux $F$ and the PMT anode current ${ }^{*} I_{A}$ are measured simultaneously. The gain G of the PMT is measured shortly before or after the measurement of $F$ and $I_{A}$. The cathode current $I$ is $I_{A} / G$. If $F$ is in photons per second and $I$ in electrons per second, the efficiency of the receiver is

$$
\begin{equation*}
\eta=\frac{\mathrm{I}}{\mathrm{~F}} . \tag{3}
\end{equation*}
$$

Bright stars are used as sources of input light, with values of F computed from tables of narrow-band photometric data. The PMT gain is determined by dividing the average measured output charge of a single-electron pulse by the electronic charge, $q=1.602 \times 10^{-19}$ Coulomb. The output charge is found by measuring and averaging the areas under single-electron pulses in the anode current. These pulses are displayed on a fast oscilloscope and photographed. The charge, in Coulombs, is the area under one of these pulses when the vertical scale is in amperes and the horizontal scale is in seconds.

[^1]A number of measured pulse areas are averaged to reduce the statistical variation introduced by the dynode amplifiers of the PMT. We use oscilloscope photography because that equipment is already available at the Smithsonian Astrophysical Observatory (SAO) observing stations; there are other less time-consuming possibilities, but they would require additional equipment or modification of components now in use. If a discriminator and frequency counter were available, the cathode current could be measured directly in photoelectrons per second. Or if the "lock-out" feature of the laser system's time-interval counter could be made temporarily inoperative, the cathode current could be obtained by averaging measured intervals between successive electron pulses in the anode current. The cathode current is the reciprocal of this average value.

## 4. DESCRIPTION OF THE PHOTORECEIVER

A block diagram of the laser receiving system as set up for range measurements (Lehr et al., 1971) is shown in Figure 1. The transmitted and received pulses are displayed on a Tektronix type 454 oscilloscope, whose bandwidth is 150 MHz . Figure 2 is a block diagram for receiver efficiency measurements. The PMT's dc anode current is measured by a microvoltmeter connected across a 100 -ohm resistor, and singleelectron pulses in the anode current are displayed on the fast oscilloscope. Figure 3 is an optical diagram of the Cassegrain receiving telescope (Gates, 1970), whose characteristics are given in Table 1. A transmission curve for a typical narrow-band filter is reproduced in Figure 4. Pertinent characteristics of the RCA 7265 photomultiplier, taken from the manufacturer's data sheet (RCA, 1968), are listed in Table 2.

Using Tables 1 and 2, we can estimate values to be expected in our measurements. The receiver efficiency should be the quantum efficiency of the PMT times the reflectances of the two mirrors times the transmissions of the three lenses times the transmission of the narrow-band filter, or

$$
\eta=0.025(0.88)^{2}(0.999)^{3}(0.625) \times 100=1.2 \%
$$

We can also estimate the background current due to the light from the dark night sky:

$$
\begin{equation*}
I_{B}=N_{\lambda} \cdot A_{R} \cdot \Omega_{R} \cdot \Delta \lambda \cdot \eta \cdot q \cdot G, \tag{4}
\end{equation*}
$$

where
$N_{\lambda}=$ the spectral radiance of the sky,
$A_{R}=$ the area of the receiver aperture,
$\Omega_{R}=$ the field of the receiver (solid angle),
$\Delta \lambda=$ the bandwidth of the filter,
$\eta$ = the receiver efficiency,


Figure 1. Block diagram for range measurements.


Figure 2. Block diagram for receiver efficiency measurements.


Figure 3. Optical diagram of the photoreceiver.


Figure 4. Transmission curve of narrow-band optical filter.
$q=$ the electronic charge,
$\mathrm{G}=$ the gain of the PMT.
For the dark night sky, $N_{\lambda}$ is approximately $10^{13}$ photons $\mathrm{s}^{-1} \mathrm{~m}^{-2} \mathrm{sr}^{-1} \mu_{\mathrm{m}}{ }^{-1}$ (Lehr, 1974; see Table IV). The other quantities are $A_{R}=0.2 \mathrm{~m}^{2}, \Omega_{R}=10^{-6} \mathrm{sr}$ for a field of 4 arcmin, $\Delta \lambda=8 \times 10^{-3} \mu \mathrm{~m}, \eta=1.2 \%, \mathrm{q}=1.6 \times 10^{-19}$ Coulomb, and $\mathrm{G}=4.8 \times 10^{7}$. We obtain $I_{B}=0.1 \mathrm{nA}$, which is negligible compared with the specified dark current of 50 nA . It should be noted, however, that for the most part in our tests, the dark current was only a few nanoamperes.

Table 1. Optical characteristics of the photoreceiver.
Primary Mirror
$0.508-\mathrm{m}$ diameter
f/4
parabolic
$88 \%$ reflectance
Secondary Mirror
$0.146-\mathrm{m}$ diameter
flat
$88 \%$ reflectance

## Lenses

$99.9 \%$ transmission at 694 nm

Table 2. Specified characteristics of the RCA 7265 photomultiplier tube.

| Operating voltage | 2400 V |
| :--- | :--- |
| Quantum efficiency (at 694 nm ) | $2.5 \%$ |
| Gain | $4.8 \times 10^{7}$ |
| Dark current (at $22^{\circ} \mathrm{C}$ ) | 50 nA |
| Pulse rise time ( 10 to $90 \%$ of peak) | 2.7 ns |
| Maximum anode current | 1 mA |

*The equivalent pulse width for a gaussian pulse is 3.8 ns .

## 5. CALCULATIONS

The first task in calculating the receiver efficiency is to determine F, the input light flux at the laser wavelength. To do so, we must have spectral flux densities for the stars used in the measurements. These are taken from the published results of Mitchell and Johnson (1969) on 1000 bright stars in 13 narrow-wavelength bands. Of use to us is band 72, whose central wavelength is 724 nm and whose effective rectangular bandpass is $8.1 \%$ or ( $695 \mathrm{~nm}, 753 \mathrm{~nm}$ ). The ruby-laser wavelength, 694 nm , is at the edge of this band, but adjacent band 63 appears to be less suitable, having a central wavelength of 635 nm and an effective bandwidth of $5.1 \%$ or ( $619 \mathrm{~nm}, 651 \mathrm{~nm}$ ).

The stars measured by Mitchell and Johnson are brighter than 5th visual magnitude and north of $-20^{\circ}$ declination. This declination limit eliminates some bright southern stars (such as Achernar, Antares, Canopus, and Fomalhaut) from the tables. The stars are listed according to their bright-star numbers, found in the Yale Catalog (Hoffleit, 1964). The photometric data are referenced by A0 V stars of zero magnitude. An A 0 V star is a main-sequence star whose color index, $\mathrm{B}-\mathrm{V}$, is zero. Table 2 of Mitchell and Johnson gives an absolute calibration of $1.73 \times 10^{-12} \mathrm{~W} \mathrm{~cm}^{-2} \mu^{-1}$ in filter band 72 for a zero-magnitude A0 V star.

The spectral irradiance of a given star is found by using the absolute calibration from above along with Table 7 of Mitchell and Johnson. This table is entered with the star's bright-star number. Two magnitude values are selected: the one headed 52 , which we call $x$, and the one from the column headed $52-72$, which we designate by $y$. Since $x$ is the magnitude of the star in spectral band 52 and $y$ is the magnitude difference between bands 72 and band 52, we have the following relation:

$$
\begin{equation*}
\log _{10} \frac{\ell_{0}}{\ell}=0.4(\mathrm{x}-\mathrm{y}) \tag{5}
\end{equation*}
$$

where $\ell_{0}$ and $\ell$ are, respectively, the spectral irradiance values for the $A 0 \mathrm{~V}$ reference star and for the star in question. Using the given value for $\ell_{0}$, we have

$$
\begin{align*}
\ell & =1.73 \times 10^{-12} \times 10^{-0.4(x-y)} \mathrm{W} \mathrm{~cm}^{-2} \mu \mathrm{~m}^{-1}  \tag{6a}\\
& =6.05 \times 10^{10} \times 10^{-0.4(x-y)} \text { photons } \mathrm{s}^{-1} \mathrm{~m}^{-2} \mu \mathrm{~m}^{-1}, \tag{6b}
\end{align*}
$$

where in equation (6b) we used the fact that $h \nu=2.86 \times 10^{-19}$ Joule for the laser wavelength, 694 nm . The value of $\ell$ given by equation (6) is that outside the earth's atmosphere. In computing the light flux entering the aperture of the receiver, we must correct for atmospheric extinction, for which we use

$$
\begin{equation*}
T=e^{-T / \sin a} . \tag{7}
\end{equation*}
$$

Here, $a$ is the star's altitude angle and $\tau$ is given by Kaula (1962), as follows:

$$
\begin{equation*}
\tau=\int_{h_{0}}^{\infty}\left(\frac{0.00114}{\lambda^{4}} e^{-0.126 h}+0.145 e^{-0.65 h}\right) d h \tag{8}
\end{equation*}
$$

where $h_{0}$ is the station height in kilometers and $\lambda$ is the wavelength in micrometers. The first term in the integrand comes from molecular scattering, with a scale height of 7.9 km . The second term is due to water-vapor absorption, which has a scale height of only 1.5 km and hence is affected significantly by the station's $h_{0}$ value. For a ruby laser with $\lambda=0.694 \mu \mathrm{~m}$, equation (8) becomes

$$
\begin{equation*}
\tau=0.0389 \mathrm{e}^{-0.126 \mathrm{~h}_{0}}+0.223 \mathrm{e}^{-0.65 \mathrm{~h}_{0}} \tag{9}
\end{equation*}
$$

We can compute a from the epoch of the observation and the coordinates of the star and the station (see Appendices A and B) from the following (Sidgwick, 1971, p. 509):

$$
\begin{equation*}
\sin a=\sin \delta \sin \phi+\cos \delta \cos \phi \cos H, \tag{10}
\end{equation*}
$$

where H and $\delta$ are the star's hour angle and declination and $\phi$ is the station's latitude. The hour angle is

$$
\begin{equation*}
H=L S T-R A \tag{11}
\end{equation*}
$$

where RA is the right ascension of the star and LST, the local sidereal time, is

$$
\begin{equation*}
\mathrm{LST}=(1.002738) \mathrm{U} \mathrm{~T}+\lambda+\mathrm{ST}, \tag{12}
\end{equation*}
$$

in which UT is the universal time, $\lambda$ is the east longitude of the station, and ST is the hour angle of the equinox for $0^{h}$ UT on the day of the measurement. LST, UT, $\lambda$, and ST in equation (12) can be expressed in either hours or degrees. The conversion factor is $15^{\circ}$ per hour.

We now calculate the input flux F for a given star:

$$
\begin{equation*}
F=\ell \cdot A_{R} \cdot \Delta \lambda \cdot T \text { photons } s^{-1} \tag{13}
\end{equation*}
$$

where $\ell$ and T are given by equations (6b), (7), (9) and (10); $\Delta \lambda$ is the width in micrometers of the narrow-band filter, and $A_{R}$ is the aperture area of the receiving telescope in square meters. The $S A O$ receiving telescope has an aperture diameter of 0.508 m , for which $A_{R}=0.203 \mathrm{~m}^{2}$. The value of $\Delta \lambda$ varies from one filter to another between $7 \times 10^{-4}$ and $9 \times 10^{-4} \mu \mathrm{~m}$. The cathode current $I$ is

$$
\begin{equation*}
\mathrm{I}=\frac{\mathrm{I}_{\mathrm{s}}-\mathrm{I}_{\mathrm{b}}}{\left\langle 1.602 \times 10^{-19}\right\rangle \mathrm{G}} \text { photoelectrons } \mathrm{s}^{-1} \tag{14}
\end{equation*}
$$

where $I_{S}$ is the anode current in amperes with the star in the receiver's field of view, $I_{b}$ is the background current with the star out of the receiver's field, and $G$ is the measured gain of the PMT. At the SAO stations, the PMT output current is measured as a voltage across a 100 -ohm resistor. Hence, $I_{s}=\left(V_{S} / 100\right) \times 10^{-6}$ and $I_{b}=\left(V_{b} / 100\right) \times 10^{-6}$, where $\mathrm{V}_{\mathrm{s}}$ and $\mathrm{V}_{\mathrm{b}}$ are voltages in microvolts. Equations (3), (13), and (14) give the efficiency of the receiver.

For an idea of the $I_{S}$ values we might expect from various stars, we assume a station at sea level, a star altitude of $45^{\circ}$, a filter bandwidth of 0.7 nm , a receiver
efficiency of $1.2 \%$, and a PMT gain of $4.8 \times 10^{7}$. For zero background current, we obtain the following expression for $I_{S}$ from equations (3), (13), and (14):

$$
\begin{equation*}
I_{S}=9.041 \times 10^{-3} \ell \cdot \mu \mathrm{~A} \tag{15}
\end{equation*}
$$

Estimated $I_{S}$ values are given in Table 3 for the 18 bright stars selected for the photometric measurements (see Appendix A). The criteria for their selection were as follows:
A. The star must have a name. It was felt that a named star could be easily identified by an observer, who would then check that the proper star was in the field of the telescope.
B. The star must not be variable.
C. The computed PMT current must be $\sim 0.2 \mu \mathrm{~A}$ or more so as to be well above the background current.

No attempt was made to track stars during the photometric measurements. The telescope's direction was fixed and the star drifted through. If the telescope's field is f arcmin, the star will be within this field for at least 4 f s. Hence, for a field of several arcminutes, there is enough time to make the measurement.

Table 3. Characteristics of the 18 stars used for photoreceiver measurements.

|  | Bright- <br> star <br> number | x <br> $(52)$ | y <br> $(52-72)$ | $\ell$ <br> Name | (photons $\left.\mathrm{s}^{-1} \mathrm{~m}^{-2} \mu^{-1}\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Aldebaran | 1457 | 1.333 | 1.797 | Estimated <br> PMT anode <br> current, $\mathrm{I}_{\mathrm{S}}$ <br> $(\mu \mathrm{A})$ |  |
| Algeiba | $4057 / 8$ | 2.303 | 1.198 | $2.185 \times 10^{10}$ | 0.84 |
| Alphard | 3748 | 2.384 | 1.452 | $2.563 \times 10^{10}$ | 0.20 |
| Altair | 7557 | 0.799 | 0.236 | $3.600 \times 10^{10}$ | 0.23 |
| Arcturus | 5340 | 0.243 | 1.321 | $1.632 \times 10^{11}$ | 0.32 |
| Capella | 1708 | 0.243 | 0.859 | $1.066 \times 10^{11}$ | 1.5 |
| Deneb | 7924 | 1.309 | 0.185 | $2.148 \times 10^{10}$ | 0.96 |
| Dubhe | 4301 | 2.068 | 1.072 | $2.416 \times 10^{10}$ | 0.19 |
| Eltanin | 6705 | 2.662 | 1.675 | $2.436 \times 10^{10}$ | 0.22 |
| Hamal | 617 | 2.315 | 1.181 | $2.128 \times 10^{10}$ | 0.22 |
| Kochab | 5563 | 2.479 | 1.525 | $2.511 \times 10^{10}$ | 0.19 |
| Menkar | 911 | 2.951 | 1.969 | $2.447 \times 10^{10}$ | 0.23 |
| Mirach | 337 | 2.510 | 1.873 | $3.363 \times 10^{10}$ | 0.22 |
| Pollux | 2990 | 1.388 | 1.025 | $4.327 \times 10^{10}$ | 0.30 |
| Procyon | 2943 | 0.462 | 0.485 | $6.176 \times 10^{10}$ | 0.39 |
| Rigel | 1713 | 0.172 | 0.080 | $5.554 \times 10^{10}$ | 0.56 |
| Sirius | 2491 | -1.421 | 0.009 | $2.257 \times 10^{11}$ | 0.50 |
| Vega | 7001 | 0.039 | 0.008 | $5.876 \times 10^{10}$ | 2.0 |
|  |  |  |  | 0.53 |  |

## 6. PROCEDURE

Receiver efficiency measurements are currently made at least once every 6 months at each of the four observing stations. Before the measurements are started, coordinates in azimuth and altitude for those stars (from Appendix A) that will be more than $20^{\circ}$ above the horizon during the period of observation are sent to the station for epochs 5 min apart. Predictions are made for each night over a period of a week to a month by using appropriate subroutines from the satellite-prediction program.

The actual measurements are made on clear nights, and measurements are conducted on several stars, preferably those at high altitudes where the atmospheric correction is minimal. PMT current readings are taken with a high-impedance voltmeter across a $5 \% 100$-ohm resistor that carries the anode of the PMT. The telescope field is set to 4 arcmin, so at least 16 s will be available for the measurement.

The PMT is turned on 10 min before the transit of the first star, and the anode voltage is set to the desired value and measured. The PMT current is read as each star passes through the field, and the background current is read before and after the passage of the star.

Single-electron measurements, needed to find the gain and other relevant parameters of the PMT, are made shortly before or after the star measurements. If desired, an artificial light source can be used. The amount of light entering the PMT is adjusted to give an anode current of $100 \mu \mathrm{~A}$, a value that turns out to be convenient for oscilloscope photographs. Expanded pulses, taken with a sweep speed of 5 ns per division (see Figure 5), are used to find the width of a single-electron pulse, and compressed pulses, photographed with a sweep of 200 ns per division, are used to measure the pulse amplitudes. If the gain of the PMT is the specified value, $4.8 \times 10^{7}$, there should be about 26 compressed pulses on the photograph (see Figure 6). Since the amplitudes have large variations, at least five photographs are taken for a good representation of the distribution.

One of the uses of the single-electron measurements is to calculate the number of electrons in the return from a satellite or from a fixed reflector on the ground. This number can be obtained from measuring the area under a single-electron pulse. For the SAO systems, the return pulses are displayed after a video amplification of 31 dB , the voltage gain for the Avantek AV-5 amplifier for input signals of 300 mV or less. To take account of video amplification, the pulse areas derived from PMT anodecurrent measurements are multiplied by $10^{31 / 20}=35.5$.


Figure 5. Single-electron pulses: 20 mV per division; 5 ns per division.


Figure 6. Single-electron pulses: 20 mV per division; 200 ns per division.

## 7. COMPUTATIONS

Although we have already presented the basic formulas for computing the quantities described in Section 2, a few more details should now be supplied.

The amplitude distribution of single electrons is computed from the measured pulse heights of photographs like Figure 6; the average amplitude is the mean of this distribution. The average pulse width is determined from photographs like Figure 5. The average single-electron area is assumed to be the area under a curve having the shape of a normal distribution with an amplitude equal to the average amplitude and a width equal to the average width. The width of the single-electron pulse is the full width between half-amplitude points. Some pulses, however, are unsymmetrical, having marked changes in slope on their trailing edges, which often occur near the half-amplitude points. For this reason, the pulse width is not measured directly; instead, we measure the area of the pulse and its amplitude. Then the width is taken to be that for a curve having these area and amplitude values and the shape of a normal distribution. If the pulse height is H and the area is A , this width is

$$
\begin{equation*}
\mathrm{W}=\frac{2 \mathrm{~A}}{\mathrm{H}}\left(\frac{\ln 2}{\pi}\right)^{1 / 2}=0.9394 \frac{\mathrm{~A}}{\mathrm{H}} . \tag{16}
\end{equation*}
$$

If $W_{a v}$ is the average value of $W$ computed from photographs similar to Figure 5 and $\mathrm{H}_{\mathrm{av}}$ is the average amplitude from photographs like Figure 6, the average electron area of the pulse before video amplification is

$$
\begin{equation*}
\mathrm{A}_{\mathrm{av}}=\frac{1}{2}\left(\frac{\ln 2}{\pi}\right)^{-1 / 2} \mathrm{H}_{\mathrm{av}} \mathrm{~W}_{\mathrm{av}} \tag{17}
\end{equation*}
$$

In principle, $A_{\text {av }}$ could have been found by averaging the area under several hundred pulses, but in practice, it is not convenient to do so, because many time-consuming area measurements would have to be made. The method actually used takes advantage of the fact that the pulse shape is fairly stable from pulse to pulse, although the pulse amplitudes change markedly.

Two programs were written for the Data General Nova minicomputer in the language Forth (Collins and Cherniack, 1974): the first for computing PMT parameters from single-electron-pulse photographs, and the second for computing receiver efficiency from measurements on the stars. These are given in Appendices C and D.

## 8. RESULTS

Table 4 summarizes the results of recent photoreceiver measurements at the four SAO stations, and Figure 7 gives plots of single-electron distributions.

The measured values of the efficiency are close to the expected value of $1.2 \%$ obtained in Section 4. Errors for the efficiency are sample standard deviations computed from the efficiency values obtained with different stars as references. The single-electron pulse widths are larger than the specified value for the PMT given in Table 2; this stretching may be due to the video circuitry and the oscilloscope that follows the PMT. The PMT gain is consistent with the specified value in Table 2. The broad single-electron distributions shown in Figure 7 are as expected for a tube (such as the RCA 7265) that was not designed to resolve single electrons. Pearl (1967) also found a wide distribution for the RCA 7265.

## (MV)

> 0
> 10 XX
> 2g Xxxxxxxxxxxxxxxxxxxxx
> 30 XXXXXXXXXXXXXXXXXXXX
> 40 XXXXXXXXXXXXXXXXXXXX
> 50 XXXXXXXXXXXXXXXXXX
> 60 Xxxxxxxxxxxxxxxxxxxxxxxx
> 76 XXXXXXXXXXXXXXXXXXXXXXX
> 80 XXXXXXXXXXXXXXXXXXX
> 99 XxXXXXXXXXXXXXXXXXXXXXXX
> 100 XXXXXXXXXXXXXXXXXX
> 110 Xxxxxxx
> 120 XXXXX
> 130
> 140
> 150

Figure 7. Single-electron distribution. (a) South Africa, July 8, 1974; PMT S24439.
(N.V)

0
10 $X \times X \times X X X X X X X X X X X X X X$
20 KXXXXXXXXXXXXXXXXXXXXXXXXXXXX
30 K KXXXXXXXXXXXXXXXXXXKXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX

50 KXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
60 KXXXXXXXXXXXXXXXXXXXXXXXXX
70 KXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
צD $X X X X X K X X X X X X X X X X X X X X X X X X ~$
90 KXXXXXXXXXXXXXXXXKX
$100 \times X \times X X X X X$
$110 \times \times \times \times X X X$
120 $\times x \times \times \times \times \times \times \times \times \times \times \times \times \times$
130
140
150
Figure 7. Single-electron distribution. (b) Peru, August 1, 1974; PMT S24245.

```
(MV)
    0
    10 XXXXXXXXXXXX
    20 XXXX
    30 XXXXXXXXXXXXXXXX
    40 XXXXXXXXXXXXXXXXXX
    50 XXXXXXXXXXXXXXXXXXXX
    60 XXXXXXXXXX
    70 XXXXXXXXXXXX
    80 xXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
    90 XXXXXXXXXXXXXXXXXXX
    100 XXXXXXXXXXXXXXXX
    110 XXXXXXXX
    120 XX
    130 x XXXXXXXXXXXXXXXXXXXXXXXXXXXX
    140 XXXXXXXXXXXXXX
    150 XXXXXXXXXXXXXX
    160 XXXXXX
    170 XXXXXX
    180 XXXXXXXXXXXXXXXXXXXXXXXXX
    190 XXXXXX
    200 XXXX
    210 XXXX
    220 xxxxXX
    230 XXXXXX
    240 XX
    250 XX
    260 XXXX
    270 XX
    280 XXXX
    290
    300 XX
    310
    320
    33C
    34e
    350
```

Figure 7. Single-electron distribution. (c) Arizona, July 10, 1974; PMT S24244.
(MV)

```
    0
    10x
    20
    30 XXXXXXXXXXXXXXXXXX
    40 XXXXXXXXXXXXXX
    50 XXXXXXXXXXXX
    60 XXXXXXX
    70 XXXXXXXXXXXXXXXXXX
    80 XXXXXXXXXXXXXXXXXXXXXX
    90 XXXXXXXX
    100 XXXXXXXXXXXXX
    110 XXXXXXXXXXXXXXXXXXX
    120 XX
    130 XXXXXXXXXXXXXXX
    140 XXXXXXX
    150 XX
    160 X
    170 XXXXX
    180 XXXXXX
    190 XX
    206 X
    210
    220
    230
    240
    250 X
    260
    270
    280
    290
    300
    310 x
    320
    330
    340
    350
```

Figure 7. Single-electron distribution. (d) Brazil, July 13, 1974; PMT S24240.

Table 4. Results of photoreceiver efficiency measurements at the four SAO stations.

| Station | Date of <br> measurement | Receiver <br> efficiency (\%) | Average <br> electron <br> amplitude $(\mathrm{mV})$ | Average <br> electron <br> duration (ns) | Area of <br> single <br> electron (V ns) | PMT <br> gain |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| South Africa | July 8, 1974 | $1.0 \pm 0.2$ | 63 | 6.5 | 15.4 | $5.4 \times 10^{7}$ |
| Peru | Aug. 1, 1974 | $0.8 \pm 0.1$ | 55 | 5.9 | 12.2 | $4.3 \times 10^{7}$ |
| Arizona | July 10, 1974 | $1.0 \pm 0.1$ | 116 | 6.3 | 27.5 | $9.7 \times 10^{7}$ |
| Brazil | July 13, 1974 | $1.3 \pm 0.2$ | 92 | 7.1 | 24.6 | $8.7 \times 10^{7}$ |

## 9. ACKNOWLEDGMENTS

I thank Dr. Michael R. Pearlman for his support of this work, which required a commitment of time and manpower at the four stations. I also thank Jakob Wohn and Charles R. H. Tsiang for their helpful advice on many occasions. It is a pleasure to acknowledge the contribution of Jerome R. Cherniack, who patiently taught me Forth and guided me through the writing of the minicomputer programs. The assistance of the observers at the tracking stations is greatly appreciated; the successful outcome of the measurements depended on their skill and resourcefulness.

COLLINS, P. L., and CHERNIACK, J. R.
1974. SAO Forth-A primer. Smithsonian Astrophys. Obs., Cambridge, Massachusetts, October, 102 pp .
GATES, G. M.
1970. Telescope photoreceiver manual. Tinsley Laboratories, Inc., Berkeley, California.
HALME, S. J.
1973. Workshop on satellite laser systems. Lagonissi 22-25.5.1973, Helsinki Univ. Technology, 40 pp .
HOFFLEIT, D.
1964. Catalogue of Bright Stars. 3rd rev. ed., Yale Univ. Obs., New Haven, Connecticut, 415 pp.
KAULA, W. M.
1962. Celestial geodesy. Tech. Note, NASA TN D-1155, March, pp. 72-73.
1969. The Terrestrial Environment: Solid-Earth and Ocean Physics (Chairman). Report of a Study at Williamstown, Massachusetts, NASA CR-1579, 147 pp.
KLOBUCHAR, R. L., AHUMADA, J. J., MICHAEL, J. V., and KAROL, P. J.
1974. An accurate method of photomultiplier gain determination. Rev. Sci. Instr., vol. 45, pp. 1071-1072.
LEHR, C. G.
1974. Laser tracking systems. In Laser Applications, vol. 2, ed. by M. Ross, Academic Press, New York, pp. 1-52.
LEHR, C. G., PEARLMAN, M. R., MENDES, G. M., and TSIANG, C. R. H.
1971. The laser network of the Smithsonian Astrophysical Observatory. Presented at the XVth General Assembly of the IUGG, Moscow, August.
MITCHELL, R. I., and JOHNSON, H. L.
1969. Thirteen-color narrow-band photometry of one thousand bright stars. Comm. No. 132, Lunar Planet. Lab., Univ. Arizona, vol. 8, part 1, 49 pp.

## PEARL, P. R.

1967. Single-electron response of the RCA 7265 photomulitplier. Journ. Sci. Instr., vol. 44, p. 797.
RADIO CORPORATION OF AMERICA
1968. RCA-7265 photomultiplier tube. RCA Electronics Components, Harrison, New Jersey, 8 pp.

SIDGWICK, J. B.
1971. Amateur Astronomer's Handbook. Faber and Faber, London.

## APPENDIX A

BRIGHT STARS USED FOR RECEIVER EFFICIENCY MEASUREMENTS*

| Name of star |  | Visual magnitude | Right ascension | Declination |
| :---: | :---: | :---: | :---: | :---: |
| Aldebaran | a Tau | 1.1 | 68.621 | $+16 \% 460$ |
| Algeiba | $\gamma$ Leo | 2.6 | 154.649 | +19.969 |
| Alphard | a Hyd | 2.2 | 141.590 | - 8.549 |
| Altair | a Acq | 0.9 | 297.390 | + 8.801 |
| Arcturus | a Boo | 0.2 | 213.630 | +19.312 |
| Capella | a Aur | 0.2 | 78.710 | +45.974 |
| Deneb | a Cyg | 1.3 | 310.145 | +45. 190 |
| Dubhe | a UMa | 1.9 | 165.549 | +61.886 |
| Eltanin | $\gamma$ Dra | 2.4 | 269.006 | +51.491 |
| Hamal | a Ari | 2.2 | 31.440 | +23.345 |
| Kochab | $\beta$ UMi | 2.2 | 222.690 | +74.258 |
| Menkar | a Cet | 2.8 | 45.242 | + 3.992 |
| Mirach | $\beta$ And | 2.4 | 17.082 | +35.488 |
| Pollux | $\beta$ Gem | 1.2 | 115.947 | +28.088 |
| Procyon | a CMi | 0.5 | 114.498 | + 5.290 |
| Rigel | $\beta$ Ori | 0.3 | 78.334 | - 8.229 |
| Sirius | a CMa | -1.6 | 101.012 | -16.681 |
| Vega | a Lyr | 0.1 | 279.023 | +38.759 |

[^2]
## APPENDIX B

## STATION COORDINATES*

| Station | Height <br> $(\mathrm{km})$ | Latitude | East Longitude |
| :--- | :---: | :---: | :---: |
| South Africa (7902) | 1.544 | -259.959 | 28.248 |
| Peru (7907) | 2.452 | -16.465 | 288.508 |
| Arizona (7921) | 2.383 | 31.684 | 249.122 |
| Brazil (7929) | 0.046 | -5.928 | 324.836 |

${ }^{*}$ From Gaposchkin, E. M., editor, 1973 Smithsonian Standard Earth (Щ), Smithsonian Astrophys. Obs. Spec. Rep. No. 353; see especially pp. 339-341.

## APPENDIX C

FORTH PROGRAM; SAMPLE INPUT AND OUTPUT DATA FOR COMPUTING PMT PARAMETERS

## Forth Program

299

* 45 LOAD START 3DO LOAD DONE I
* ; S

45

* ( COMPUTATION OF PMT PARAMETERS FROM PULSE HEIGHTS AND UIDTHS ) 1
* DISCARD REMEMBER DI SCARD 2
* 3 D ! 3
* (H-SCALE MV/DIV IS FOR COMPACT PULSES P-SCALE IS FOR PLOT ) 4
* ( W-SCALE NS/DIV IS FOR EXPANDED PULSES ) 5
* (IN: \#BINS, P-SCALE. H-SCALE, W-SCALE ) 6
* ( $W:$ AREA DIV SQ, HEIGHT DIV ) 7
* (H: HEIGHT DIU ) 8
* 40 LOAD 41 LOAD 42 LOAD 43 LOAD 9
* ; S


## 40

* "AVE. ELECTRON AMPLITUDE (MU) $="$ MESSAGE AVH-M
* " X" MESSAGE M 2
* " AVE. ELECTRON DURATION (NS) $=$ " MESSAGE AUH-M 3
* "AREA OF SINGLE ELECTRON (V-NS) = "MESSAGE AREA-M 4
* " PLOT OF SINGLE-ELECTRON DISTRIBUTION: "MESSAGE 5
* PLOT-M . 6
* " (MV)" MESSAGE UNITS-M . 7
* "PMT GAIN = "MESSAGE GAIN-M 8
* ( CONTINUED ON BLOCK 41)
* ; S

```
    4!
    * 36 INTEGER #BINS & INTEGER P-SCALE &
* 0. .VAR H-SCALE Ø. OVAR WOSCALE 2
* 1 [ #BINS ] ARRAY BIN 3
* 0. .VAR H-SCALE De oVAR WOSCALE &
* 0. .VAR KOUNT 0. .VAR K 0. .VAR Y 5
* 0. .VAR SUM-H D. UAR W-SUM 6
* 0. .VAR X D. .VAR A O INTEGER NX 
* : START CR CR 20 SPACES [ ] BIN MCLEAR Do KOUNT O! . &
* D. K .! D. SUN-H .! b. W-SUM !! ; 9
* : PUTINBIN 10. ./ .5.4.FIX & BIN &0
* DUP © 1 + SWAP ! ; &!
* ( CONTINUED ON BLOCK 42 ) &2
* ;5
```

2

* : H Ø DO KOUNT 1. $\ddagger$ KOUNT $\cdot$ ! H-SCALE * DUP
3
* PUTINBIN SUM-H * SUM-H \& LOOP ;
4

5
* W-SUM + + W-SUM •! LOOP ;
6
* : AVH CR CR AVH-M SUM-H KOUNT •/ DUP
* Y •! .. ; ..... 7
* : AVW CR AUW-M W-SUM K . / DUP X . ! . : ..... 8
* : AREA CR AREA-M Y X 1.06447 .* ** •DUP ..... 9
* A .! • ©3548 1 **... ; ..... 10
* ( CONTINUED ON BLOCK 43 ) ..... 81
* S

```
4 2
```

4 2

* : IN N-SCALE ! H-SCALE ! OFIX PoSCALE ! ofIX \#BINS ! ;

```
* : IN N-SCALE ! H-SCALE ! OFIX PoSCALE ! ofIX #BINS ! ;
```

43

```* : GAIN CR GAINm A 50. ./ \(1.6021 \mathrm{Mo7} / 100 \%\)1
```

* 4 F ! ..... 2
* $\quad$ INTEGER $X^{\prime} S$ ..... 3
* XXXXXXXXXXXXXXXXXXXXYXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXRXX ..... 4
* X'S ! ..... 5
* : P X'S O COUNT DROP NX © DUP IF TYPE ELSE DROP DROP THEN ; ..... 6
* : PLOT CR CR PLOT-M CR CR UNITS×M CR \{ BINS ..... 7
 ..... 8
* NX ! P LOOP ; ..... 9
* " ELECTRON AMPLITUDES UERE MEASURED" MESSAGE E-M ..... 10
* : ELECTRONS KOUNT . E EM ; ..... 11
* : DONE AVH AVW AREA GAIN PLOT CR CR ELECTRONS: ..... $\$ 2$

Notes: A. \# BINS controls the number of $10-\mathrm{mV}$ intervals that will appear in the plot of the single-electron distribution.
B. H-SCALE (mV/div) and W-SCALE (ns/div) are, respectively, the vertical oscilloscope setting for the compact pulses and the sweep speed for the expanded pulses.
C. $\mathbf{P}$ is a constant that can be increased to prevent the plot of the singleelectron distribution from going off scale.

## Sample Input Data



```
301
* [6. 2.2 4. 4. 3.1 2.9.9 5.3 1.7.6 ] H l
* [3.1.5 3.1 1.6 1.2.6 3.4 1. 3. ] H 2
* [1.4 1.4 3. 5.6 2.9 3.4 2.1 1.7 1.8 3.4 ] H 3
* [1.5 2.9 4.3 1.8 4.8 5.8 2.4 3.8 .9 ] H
* [1.9 1.6.04 1. 6. 1.6 3.7 1.8 3.9 3.4 ] H 5
* [llllllll.3 4.1 1.9 4.6 1.9 1.2 4.3 2.3 ] H 6
* [ 1.8 3.7 2.8 2.6.5 5.1 5.8 1.7 4.5 3.6 ] H % 7
* [ 3.5 1.4 3.4 1.5 2. 6. 1.7 2.2 .4 ] H & 8
* [ 5.4 1. 3. 2. 4.6 1.7 1.2.5 4. 1.6 ] H $
* [1.9 3.8 3.4 1.8 3.6 1.6 2.7 6. 4.2 ] H 10
* 1. 4.8 3.9 2.4 5.4 2.4 1.4 4.5 1.5 . 4 ] H il 
* [4.7 1.2 3.7 4.5 3.6 1. 4.3 4. 3.2 ] H 12
* 302 LOAD 13
* ;S
```

```
302
```



```
* [4.2 3. 2.7 3.8.6 3.4 .7 3.8 1.5 2.5 6. 2.7 ] H
* [1. . 6 4.6 4.5 4.8 3.6 3.7 1.6 3.7 2.7 1.6 .5 ] H
* [1.2.7 1. 1.5 2.9 1.9 .6 5.2 1.6 4.2 4. 1. ] H 4
```



```
* [1.9 2.7 3.3 3.3 3. 3.9 4.4 1. 4.4 1.6 3.6 1.7 ] H
* [ 3.7 4.6 6. .5.2.3 1.2 1.7 3.4 1.3 4.2 3.2 1.8 ] H 7
* [ 3.4 2. 2 2.4 4.6 2. 6. 1.6 . 8 1.1 3.6 1.7 1.6 ] H & &
* [4.4 2. 4 1.2 4.8 . 8 2. 2.3 3. 1.1 5.4 2.4 3.8 ] H 9
* [ 1.5 2.1 . 5 3.5 1.4 2.7 1.5 ] H
```

299 LOAD
PERU 1 AUG 74 PMT S24245
AVE. ELECTRON AMPLITUDE (MV) = 5.478E+1
AVE. ELECTRON DURATION (NS) = 5.917E+\emptyset
AFEA OF SINGLE ELECTRON (V-NS) = 1.224E+1
PMT GAIN = 4.307E+7
PLOT OF SINGLE-ELECTRON DISTRIBUTION:
(MV)
0
10 XXXXXXXXXXXXXXXXXX
20 XXXXXXXXXXXXXXXXXXXXXXXXXXXXX
30 XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
40 XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
50 XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
60 XXXXXXXXXXXXXXXXXXXXXXXXXXX
70 XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
80 XXXXXXXXXXXXXXXXXXXXXXXXX
90 XXXXXXXXXXXXXXXXXXX
100 XXXXXXXX
110 XXXXXXX
120 XXXXXXXXXXXXXXXX
130
140
150
3.070E+2 ELECTRON AMPLITUDES WERE MEASURED

```

\section*{APPENDIX D}

\section*{FORTH PROGRAM AND SAMPLE OUTPUT FOR}

\section*{RECEIVER EFFICIENCY COMPUTATIONS}

Forth Program
23
* (STELLAR PHOTOMETRY ) ..... 1
* DI SCARD REM EMBER DI SCARD ..... 2
* 22 LOAD 24 LOAD 25 LOAD 26 LOAD ..... 3
* 27 LOAD 28 LOAD 29 LOAD 33 LOAD ..... 4
* 3 D !* \(\operatorname{S}\)
22
" MESSAGE Mø ..... 1
* " EFFICIENCY (\%) ALTITUDE (DEG) " MESSAGE M1 ..... 2
* " AVERAGE EFFICIENCY (\%) = " MESSAGE M2 ..... 3
* " ESTIMATED ERROR \(="\) MESSAGE M3 ..... 4
* : HEADING CR M \(\emptyset\) MI CR ; ..... 5
* : MA CR CR M2 ; ..... 6
* : MS CR M3 ; ..... 7
* ( CONTINUED ON BLOCK 24 ) ..... 8
* ; S
24* Ø. . Var filter o. . Var gain o. . Var C1
* D. . Var lat D. . Var long ..... 2
* 0. . VAR L Ø. . VAR ST D. .VAR UT ..... 3
* 0. - var sv 0. . var bV 0. . var ra ..... 4
* 0. VAR DEC D. VAR E-S 0. VAR E-SQ ..... 5
* Ø. . Var n 0. . Var E-aV 0. . Var E ..... 6
* : ZERO Ø. E-S •! Ø. E-SQ . ! Ø. N .! ; ..... 7
* : DEGREES 36DD. . / . SWAP 60. ./ . + . + 15. .* ; ..... 8
* : RAD 57. 2958 ./ ; ..... 9
* 1 CONSTANT SAFRICA 2 CONSTANT PERU ..... 10
* 3 CONSTANT ARIZONA 4 CONSTANT BRAZIL ..... 11
* (CONTINUED ON BLOCK 25 ) ..... 12
* ; S
25
* 43 MATRIX STATION-APRAY ..... 1
* : Q 41 DO DUP 4 J - 2 STATION-ARRAY ! L LOOP DROP ; ..... 2
* . 1138-25.959 28.248 1 0 ..... 3
*.07387-16.465 288.508 \(2 Q\) ..... 4
*.07616 31.684 249.122 \(3 Q\) ..... 5
*. 2557-5.928 324.836 4 Q ..... 6
* 1.CONSTANT ALDEEARAN 2 CONSTANT ALGEIBA ..... 7
* 3 CONSTANT ALPHARD 4 CONSTANT ALTAIR ..... 8
* 5 CONSTANT ARCTURUS 6 CONSTANT CAPELLA ..... 9
* 7 CONSTANT DENEB 8 CONSTANT DUBHE ..... 10
* 9 CONSTANT ELTANIN 10 CONSTANT HAMAL ..... 11
* 11 CONSTANT KOCHAB 12 CONSTANT MENKAR ..... 12
* 13 CONSTANT MIRACH 14 CONSTANT POLLUX ..... 13
* 15 CONSTANT PROCYON 16 CONSTANT RIGEL ..... 14
* ( CONTINUED ON BLOCK 26 ) ..... 15
* ; 5
26
* 17 CONSTANT SIRIUS 18 CONSTANT VEGA ..... 1
* 183 MATRIX STAR-ARRAY ..... 2
* : R 4 l DO DUP 4 J - 2 STAR-ARRAY !! LOOP DPOP ; ..... 3
* 265.268 .62116 .460 R ..... 4
* 62.52 154.649 19.969 2 R ..... 5
* 73.32 141.590-8.549 3 R ..... 6
* 103. 297.3908.801 4 R ..... 7
* 466.9213 .63019 .3125 R ..... 8
* 305.178 .71045 .9746 R ..... 9
* 61.44 310.145 45.1907R ..... 10
* 69.13 165.549 61.886 8 R ..... 11
* 69.7 269.006 51.491 9 R ..... 12
* 60.83 31.440 23.345 10 R ..... 13
* ( CONTINUED ON BLOCK 27 ) ..... 14
* : S
27
* 71.85 222.69074.258 11 R ..... 1
* 70.02 45.242 3.992 12 R ..... 2
* 96.22 17.082 35.488 13 R ..... 3
* \(123.8 \quad 115.947 \quad 28.088 \quad 14 \mathrm{R}\) ..... 4
* 176.7114 .4985 .29015 R ..... 5
* \(153.978 .334-8.22916 \mathrm{R}\) ..... 6
* 645.7 101.012-16.681 17 R ..... 7
* 168.1279 .02338 .75918 R ..... 8
* : STATION GAIN •! FILTER •! [ DUP 1 ] STATION-ARRAY ..... 9
* C ! ! [ DUP 2 ] STATION-ARRAY LAT •! [ DUP 3 ] ..... 10
* STATION-ARRAY LONG •! DROP HEADING ; ..... 11
* ( CONTINUED ON BLOCK 28 ) ..... 12
* ; S
28
* : LST UT 1.002738 •* LONG . + ST . + ; ..... 1
* : HA LST RA . - ; ..... 2
* : S DEC RAD SIN LAT RAD SIN .* DEC RAD COS ..... 3
* LAT RAD COS HA RAD COS ** •* •+ ; ..... 4
* : A S . DUP . DUP •* .MINUS 1. •+ SQRT ./ ; ..... 5
* : ALTR a atan ; ..... 6
* : ALT ALTR 57.2958 .*... CR ; ..... 7
* : X C .MINUS ALTR SIN ./ ; ..... 8
* ( CONTINUED ON BLOCK 29 ) ..... 9
* ; S
29
* : ATTEN X EXP ;1
* : CURRENT SU BU ..... 2
* : FLUX 7084.5 L FILTER ATTEN .* •* •* ; ..... 3
* : KOUNT N 1. .+ N . ! ; ..... 4
* : E-SUM E-S E.+ E-S .! ; ..... 5
* : E-SQ-SUM E. .DUP .* E-SQ .+ E-SQ .! ; ..... 6
* : AVE KOUNT E-SUM E-SO-SUM ; ..... 7
* : EFFICIENCY CURRENT FLUX ./ 100. .* .DUP E.! .. AVE ; ..... 8
* : STAR BU .! SU •! DEGREES UT .! DEGREES ST .! ..... 9
* [ DUP 1.] STAR-ARRAY L .! [ DUP 2 ] STAR-ARRAY ..... 10
* RA - I [ DUP 3 ] STAR-ARRAY DEC •! DROP ..... 11
* EFFICIENCY ALT ; ..... 12
* ( CONTINUED ON BLOCK 33 ) ..... 13
* ; S
```

* : AV E-S N ./ . DUP E-AU . 1 .. ;
* : STD MS E-AU .DUP .* N .* .MINUS E-SQ o+ ..... 2
* N 1. .. . ${ }^{\prime}$ SQRT .. ZERO ; ..... 3
* : TEST N 1. $=$ IF ZERO ELSE STD THEN : ..... 4
* : average ma av test ; ..... 5
* ; S

Notes: A. The $3 \times 4$ matrix "station array" contains each station's location (latitude and longitude), along with its constant $\tau$ for atmospheric extinction.
B. The $18 \times 3$ matrix "star array" contains each star's location (right a scension and declination), along with a constant that gives its spectral intensity at 694 nm .

| HAMAL | 20. | 32 | 56. | D | 15 | 02. | 17 |  | STAR | 8.644E-1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| MI RACH | 20. | 32. | 56. | 07 | 40 | $\emptyset 2$ | 24 | 1.50 | STAR | $7.829 \mathrm{E}-1$ | 3.289E+1 |
| MENKAR | 20. | 32. | 56. | 07 | 45 | 00. | 16. | 1.50 | STAR | $6.889 \mathrm{E}-1$ | 3.47 |
| ALTAIR | 20 | 32. | 56. | 08 | 05 | ) | 27 | 1.55 | STAR | 8.621 | 2 |
| MI RACH | 20. | 32. | 56. | 08 | 10 | 02. | 24. | 1.40 | STAR | 7.796E-1 | 3.54 |
| MENKAR | 20. | 32. | 56 | 08 | 15 | 0 | 18 | 1.50 | STAR | 7.697E-1 | 4.158 |
| HAMAL | 20. | 32. | 56. | 08 | 40 | 02 | 17 | 1.50 | STAR | 8.281E-1 | 4.363 |
| MENKAR | 20. | 32. | 56. | 08. | 45 | 02. | 18. | 1.55 | STAR | $7.581 \mathrm{E}-1$ | 4.820 |
| HAMAL | 20. | 32. | 56. | 89 | , | 02. | 18. | 1.55 | STAR | 8.736E-1 |  |
| AL DEBARAN | 20. | 32. | 56. | 09 | 15 | 02. | 62. | 1.60 | STAR | 7.772 E | 2. |

AVERAGE
AVERAGE EFFICIENCY (\%) $=7.985 \mathrm{E}-1$
ESTIMATED ERROR $=5.817 \mathrm{E}-2$

Notes: A. The computation is started by entering the name of the station followed by the bandwidth of the filter (in angstroms), the PMT gain (with the factor $10^{-7}$ omitted), and the word STATION.
B. The photometric observations are entered by the name of the star followed by ST (hours, minutes, seconds) for the date of the observation, UT (hours, minutes, seconds), two readings of the microvoltmeter (with the star in and out of the field), and the word STAR.
C. The average efficiency and the estimated error are obtained by entering the word AVERAGE.


[^0]:    This work was supported in part by Grant NGR 09-015-002 from the National Aeronautics and Space Administration.

[^1]:    ${ }^{*}$ Actually, $\mathrm{I}_{\mathrm{A}}$ is the measured anode current less the background current that exists when $\mathrm{F}=0$.

[^2]:    The star positions are for 1975.0 (from The American Ephemeris and Nautical Almanac for the Year 1975, U.S. Govt. Printing Office, Washington, D.C., 1973).

