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ANALYSIS OF EDGE IMPACT STRESSES IN COMPOSITE PLATES

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applied to the study of oth	er stress wave pro	opagation problems	in a half space.						
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The in-plane edge impact of composite plates, with or without a protection strip, is investigated in this work. A computational analysis based on the Fast Fourier Transform technique is presented. The particular application of the present method is in the understanding of the foreign object damage problem of composite fan blades. However, the method is completely general, and may be applied to the study of other stress wave propagation problems in a half space. Results indicate that for the protective strip to be effective in reducing impact stresses in the composite the thickness must be equal or greater than the impact contact dimension. Also large interface shear stresses at the strip - composite boundary can be induced under impact.

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INTRODUCTION

This report is part of a continuing effort by NASA to understand the basic mechanics of foreign object impact of composite materials of particular interest are damage resistant designs of jet engine fan blades under hail or bird impact. In previous reports the central or normal impact response of composite plates was examined [1]. In this report the mechanics of edge impact of composite plates are examined. This is schematically illustrated in Figure 1.

The basic approach to the study of impact of composite plates in this program has been to examine the stress waves generated by the impact forces. For central impact of plates it has been shown that in addition to wave propagation across the plate thickness, bending and extensional waves propagate away from the impact site. The stresses associated with these waves have been studied without considering the effect of boundaries such as the free or clampled edges of a fan blade. This simplification has been made on the premise that -4 for short impact times e.g. less than 10 sec. few edge reflections have taken place, and that the highest stresses occur at the impact site. However, for edge impact, the boundary conditions greatly affect the nature of the wave mechanics.

Edge waves in solids have been studied extensively in seismology. The principal phenomenon is the entrapment of wave energy in a layer near the surface. This surface wave is known as a Rayleigh wave and travels at a velocity below the shear velocity for isotropic solids. For plates, however, two types of edge waves can occur as shown in Figure 2a. For impact transverse to the plate, flexural edge waves can occur. For in-plane, Rayleigh type edge waves are generated. In this report only in-plane edge waves will be discussed.

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Wave type solutions to the equations of elastodynamics of an orthotropic plate which exponentially decay away from the edge (X direction) and pro-3 pagate along the edge (X direction) can be found provided the edge wave 1 velocity satisfies the equation (Reference 9).

$$\rho v^{2} + \begin{bmatrix} C & -\rho v^{2} \\ \frac{55}{C} & C & (C & -\rho v^{2}) \\ 33 & 55 & 11 \end{bmatrix}^{1/2} \begin{bmatrix} 2 & C & (C & -\rho v^{2}) \\ 13 & 33 & 11 \end{bmatrix}^{1/2} = 0$$

where ρ is the massdensity of the plate and C_{ij} are the effective plate elastic constants (denoted by \widehat{C} in Reference 1). It can be shown that ij one real root lies in the interval

$$0 < \rho v^2 < C$$
55

Thus, the edge or Rayleigh wave speed is less than the shear speed in this direction $\left[C_{55}/\rho\right]^{1/2}$.

Changing the layup angle will affect the elastic constants C and hence, ij change the value of the edge wave velocity. The results of this calculation are shown in Figure ^{2b} where the C are obtained from Reference 7. The ij edge wave speed seems to obtain a maximum between <u>+</u> 15 and <u>+</u> 30[°] layup angle ^{which} is below the extentional wave speeds labelled "dilational" and "shear" in Figure 2b and which is greater than the bending wave velocity. In order to prevent damage to composite fan blades under foreign object impact leading edge protection has been used. (See e.g. Ref. (8)). This usually consists of a strip of metal attached to the leading edge of the fan blade. To model the effects of this impact protection strip, the in-plane edge impact of an anisotropic plate, with a beam-strip attached to the impact edge, has been studied (see Figure 1). It will be shown later that the strip will decrease the tensile stress along the edge while producing shear stress between the strip and the plate edge.

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Let the plate be the half-space $x_3 > 0$. The equations of motion are given by [1] as:

$$C_{11} u_{1,11} + C_{55} u_{1,33} + (C_{13} + C_{55}) u_{3,13} = \rho u_{1}, tt$$

$$(1.1)$$

$$C_{33} u_{3,33} + C_{55} u_{3,11} + (C_{13} + C_{55}) u_{1,13} = \rho u_{3,tt}$$

here we have employed C_{11} , C_{13} , C_{33} ... to denote C_{11} , C_{13} , C_{33} ... of [1]. The in-plane motion is assumed to be independent of the bending deformation. With the loading condition shown in Figure 1, the boundary conditions are (without protection strip):

$$t_{13}(x_1,0,t) = C_{55}(u_1+u_3,1)\Big|_{x_2=0} = 0$$

(1.2)

$$t_{33}(x_1,0,t) = \begin{bmatrix} C & u & + C & u \\ 33 & 3,3 & 13 & 1,1 \end{bmatrix} \Big|_{x_2=0} = p f(x_1) g(t)$$

The following nondimensional parameters are used;

$$C_{11}^{*} = C_{11}^{\prime}/C_{66}^{\prime}, C_{13}^{*} = C_{13}^{\prime}/C_{66}^{\prime}, C_{33}^{*} = C_{33}^{\prime}/C_{66}^{\prime}, C_{55}^{*} = C_{55}^{\prime}/C_{66}^{\prime}, P_{66}^{*} = p/C_{66}^{\prime}$$
(1.3)

$$u_1^* = u_1/\ell, \quad u_3^* = u_3/\ell, \quad x_1^* = x_1/\ell, \quad x_3^* = x_3/\ell, \quad t^* = t \sqrt{C_{66}/\rho}/\ell \quad (1.4)$$

 ℓ is a length parameter. C is a typical elastic constant. In what follows the equations will be assumed to be nondimensionalized using (1.3) and (1.4).

To obtain the solution, we employ transform methods. Define:

$$F(f) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-ik_1 x_1} f(x_1) dx_1$$

as the Fourier transform of f(x) where we assume that

$$\mathbf{f}(\mathbf{x}_{1})\Big|_{-\infty}^{\infty} = \frac{\partial}{\partial \mathbf{x}_{1}}\mathbf{f}(\mathbf{x}_{1})\Big|_{-\infty}^{\infty} = 0$$

Then

$$F(\frac{\partial}{\partial x_1} f) = ik F(f), \qquad F(\frac{\partial}{\partial x_1^2} f) = -k_1^2 F(f)$$

Also define

$$\mathcal{L}(f) = \int_0^\infty e^{-st} f(t) dt$$

as the Laplace transform. The initial conditions are assumed to be,

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$$u_{1}(x_{1}, x_{3}, 0) = \frac{\partial}{\partial t} u_{1}(x_{1}, x_{3}, 0) = 0$$

$$u_{3}(x_{1}, x_{3}, 0) = \frac{\partial}{\partial t} u_{3}(x_{1}, x_{3}, 0) = 0$$
(1.5)

Letting $\iint F(u_1) = \bar{u}_1(k,x_3,s), \iint F(u_3) = \bar{u}_3(k,x_3,s)$, we have the following transformed equation:

$$C_{11}(-k_{1}^{2})\bar{u}_{1} + C_{55}\bar{u}_{1,33} + (C_{13}+C_{55})(ik_{1})\bar{u}_{3,3} = +s^{2}\bar{u}_{1}$$

$$(1.6)$$

$$C_{33}\bar{u}_{3,33} + C_{55}(-k_{1}^{2})\bar{u}_{3} + (C_{13}+C_{55})(ik_{1})\bar{u}_{1,3} = +s^{2}\bar{u}_{3}$$

and at
$$x_{3} = 0$$
, the transformed boundary conditions become
 $\tilde{u}_{1,3} + ik_{1}\tilde{u}_{3} = 0$

$$C_{33}\tilde{u}_{3,3} + C_{13}ik_{1}\tilde{u}_{1} = -p_{0}\overline{f(k_{1})g(s)}$$
(1.7)

Since we are expecting surface wave propagation, we seek the solution of (1.6), (1.7) in the forms:

$$\begin{bmatrix} \tilde{u}_{1} \\ \tilde{u}_{3} \end{bmatrix} = \begin{bmatrix} \phi_{1} \\ \phi_{2} \end{bmatrix} e^{-p(k,s)x}_{3}$$
(real (p) ≥ 0)
(1.8)

Therefore, the equations for ϕ_1, ϕ_2 are:

$$\begin{bmatrix} -s^{2} - C_{11} k_{1}^{2} + p^{2} C_{55} & -ik_{1} p(C_{13} + C_{55}) \\ -ik_{1} p(C_{13} + C_{55}) & -s^{2} - k_{1}^{2} C_{55} + p^{2} C_{33} \end{bmatrix} \begin{bmatrix} \phi_{1} \\ \phi_{2} \end{bmatrix} = 0$$
(1.9)

or for a non-trivial solution,

$$det = C_{33} C_{55} p^{4} + [C_{33} (-s^{2} - C_{11} k_{1}^{2}) + C_{55} (-s^{2} - C_{55} k_{1}^{2}) + k_{1}^{2} (C_{13} + C_{55})^{2}] p^{2} + (s^{2} + C_{11} k_{1}^{2}) (s^{2} + C_{55} k_{1}^{2}) = 0$$

$$(1.10)$$

We will choose the p's with positive real parts to ensure the decay in x_{3} direction of the surface wave. Let the solutions be $p = p_{1}, p_{2}$, therefore, we have

$$p \neq \mathbf{p}_{1}: \phi_{1}^{(1)} \equiv C_{1}(k_{1},s), \phi_{2}^{(1)} = -\frac{i[-s^{2}-C_{11}k_{1}^{2} + C_{55}p_{1}^{2}]}{k_{1}p_{1}(C_{13} + C_{55})} \phi_{1}^{(1)} \equiv \psi_{31}C_{1}$$
(1.11)

$$p = p_{2}: \phi_{1}^{(2)} \equiv C_{2}(k_{1},s), \phi_{2} = \psi_{32+2} \equiv -\frac{i[-s^{2}-C_{11}k_{1}^{2} + C_{55}p_{2}^{2}]}{k_{1}p_{2}(C_{13}+C_{55})} \phi_{1}^{(2)}$$

Therefore, the displacements have the forms:

$$\begin{bmatrix} \tilde{u}_{1} \\ \tilde{u}_{3} \end{bmatrix} = C_{1}(k_{1}, s) \begin{bmatrix} 1 \\ \psi_{31} \end{bmatrix} e^{-p_{1}x_{3}} + C_{2}(k_{1}, s) \begin{bmatrix} 1 \\ \psi_{32} \end{bmatrix} e^{-p_{2}x_{3}}$$
(1.12)

 C_1 , C_2 are determined from the boundary conditions (1.7), or

$$\begin{bmatrix} -p_{1} + ik_{1}\psi_{31} & -p_{2} + ik_{1}\psi_{32} \\ -p_{1}C_{33}\psi_{31} + ik_{1}C_{13} & -p_{2}C_{33}\psi_{32} + ik_{1}C_{13} \end{bmatrix} \begin{bmatrix} C_{1} \\ C_{2} \end{bmatrix} = \begin{bmatrix} 0 \\ -p_{0} & \overline{fg} \end{bmatrix}$$
(1.13)

Here, the determinant, $\Delta(p_1,s)$, given by,

$$\Delta = (ik_{1} \psi_{31} - p_{1}) (ik_{1} C_{13} - p_{2} C_{33} \psi_{32})$$

$$-(ik_{1}\psi_{32} - p_{2})(ik_{1}C_{13} - p_{1}C_{33}\psi_{31})$$
(1.14)

must be non-zero to ensure a solution. (Δ =0 gives the Rayleigh poles of the system, which correspond to a free surface). Therefore,

$$C_{1} = \frac{1}{\Delta} \begin{bmatrix} ik_{1} \psi_{32} - p_{2} \end{bmatrix} \overline{fg} p_{0}$$

$$(1.15)$$

$$C_{2} = \frac{1}{\Delta} \begin{bmatrix} p_{1} - ik_{1} \psi_{31} \end{bmatrix} \overline{fg} p_{0}$$

and the physical displacements $u_1(x_1,x_2,t)$, $u_1(x_1,x_2,t)$ are obtained by inverting their transforms.

From the stress-strain relations

$$t_{13} = C_{55}(u_{1,3} + u_{3,1}), \quad t_{11} = C_{11}u_{1,1} + C_{13}u_{3,3},$$
$$t_{33} = C_{33}u_{3,3} + C_{13}u_{1,1}$$
(1.16)

we obtain the transforms of the stresses

...

$$\bar{t}_{13} = C_{55} \{ (-p_1 + ik_1 \psi_{31}) C_1 e^{-p_1 x_3} + (-p_2 + ik_1 \psi_{32}) C_2 e^{-p_2 x_3} \}$$

$$\bar{t}_{13} = (C_{11} ik_1 - C_{13} p_1 \psi_{31}) C_1 e^{-p_1 x_3} \qquad (1.17)$$

$$+ (C_{11} ik_1 - p_2 \psi_{32} C_{13}) C_2 e^{-p_2 x_3}$$

 $\vec{t}_{33} = (-p_1\psi_{31}C_3 + ik_1C_1)C_1e^{-p_1X_3}$

+ $(-p_2\psi_{32}C_{33}+C_{13}ik_1)C_2e^{-p_2x_3}$,

and the physical stresses can be obtained by inversion.

The particular forcing function employed is

$$f(x_{1}) g(t) = \left[1 - \left(\frac{1}{a}\right)^{2}\right] \sin \frac{\pi t}{\tau_{0}} \qquad 0 < t < \tau_{0} \qquad |x_{1}| \le a$$

$$= \left[1 - \left(\frac{k}{a}\right)^{2} x_{1}^{*2}\right] \sin \left(\pi t^{*}/\tau_{0}^{*}\right) \qquad (1.18)$$

where
$$\tau^*_{O} \equiv \ell/\sqrt{C_{O}/\rho}$$
.

Here a is a length measuring the impact area, and τ_0 is the contact time [1]. The transform of this particular forcing function, in non-dimensional form becomes,

$$\overline{fg} = + \frac{4}{k_1^2 (a/\ell)^2} \left[-\frac{a}{\ell} \cos k_1 (\frac{a}{\ell}) + \sin k (\frac{a}{\ell}) / k \right] \frac{\pi \tau_0^* (1 + e^{-S \tau_0^*})}{\pi^2 + \tau_0^{*2} s^2}.$$
(1.19)

II. EDGE IMPACT OF PLATE WITH EDGE PROTECTION

To prevent failure of composite fan blades under impact forces, leading edge protective strips have been employed. In practice, these strips of stainless steel are wrapped around the leading edge. To model this device, we consider a beam bonded to the edge of an anisotropic plate (Figure 1). The effect of the beam will be to thwart the force of impact, thereby decreasing the normal stresses in the composite. However, we shall show that with such a reduction in normal stress, sizeable interface shear stresses can be induced.

With the introduction of a beam of thickness b on the edge of the composite plate, the Rayleigh wave behavior will depend on the ratio of the wavelength to thickness ratio of each Fourier component in the x_1 direction. Thus one should expect the Rayleigh wave speed to vary with b/a, the thickness to impact footprint ratio. In addition the Rayleigh wave will become distorted as it propagates.

To solve the edge strip problem the solution in the composite plate follows the same procedure as the no-strip case except for the boundary conditions on the edge. In place of the zero stress conditions on the edge we relate the edge stresses t_{33} , t_{13} to the motion of the beam strip. If one considers a small element of the beam-strip along the x_1 direction, the momentum balance equations in the x_1 , x_3 directions become, (for a plate of unit thickness)

$$\rho b \frac{\partial^2 U}{\partial t^2} = Eb \frac{\partial^2 U}{\partial x_1^2} + t_{13}$$
(2.1)

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$$\rho b \frac{\partial^2 W}{\partial t^2} = -EI \frac{\partial^4 W}{\partial x_1^4} + I_\rho b \frac{\partial^4 W}{\partial x_1^2 \partial t^2} + \frac{b}{2} \frac{\partial t_{13}}{\partial x_1} + t_{33} + p_o^f g \qquad (2.2)$$

In these equations U, W are the x_1 , x_3 displacements of the beam element at the half thickness, and t_{33} , t_{13} are the interface stresses.

We choose the compatibility conditions between the beam and plate displacements

$$W = u_{2}, \text{ on } x_{2} = 0.$$
 (2.3)

$$U = u_1 + \frac{b}{2} \frac{\partial u_3}{\partial x_1}, \text{ on } x_3 = 0$$
(2.4)

In the above equations b is the depth of the strip, E, I, Ip are respectively the Young's modulus, moment of inertia and rotary inertia. Also p f(t) $g(x_1)$ is the edge loading now applied to the outer protective strip surface.

The equations for the plate remain as in the free edge case and a solution is obtained by taking a Laplace transform on time and a Fourier transform on the space variable x_1 . With nondimensionalization the solution in the plate is assumed in the form of (1.12). The transform of the plate displacements are

$$\begin{bmatrix} \overline{u}_1 \\ \overline{u}_3 \end{bmatrix} = C_1 \begin{bmatrix} 1 \\ \psi_{31} \end{bmatrix} e^{-p_1 x_3} + C_2 \begin{bmatrix} 1 \\ \psi_{32} \end{bmatrix} e^{-p_2 x_3}$$
(2.5)

where p_1 , p_2 are defined in (1.10) and ψ_{31} , ψ_{32} are given in (1.11). C_1 , C_2 are determined from the edge boundary conditions. However, in place of the free edge conditions (1.2) we use the equations of motion for the strip (2.1),

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(2.2). C_1 , C_2 are then solutions to the algebraic equations

$$\begin{bmatrix} G_1 & H_1 \\ G & H \end{bmatrix} \begin{bmatrix} C_1 \\ C_2 \end{bmatrix} = \begin{bmatrix} 0 \\ -p_o^* \overline{fg} \end{bmatrix}$$

where

$$G_{1} = -k^{2}Ew + p_{1}C_{55} - \rho ws^{2} - \psi_{31}(ik^{2}w^{2}E/2 + ikC_{55} + \rho w^{2}s^{2}ik/2)$$

$$H_{1} = -k^{2}Ew + p_{2}C_{55} - \rho ws^{2} - \psi_{32}(ik^{3}w^{2}E/2 + ikC_{55} + \rho w^{2}s^{2}ik/2)$$

$$G = -ikC_{13} + ikwp_{1}C_{55}/2 + \psi_{31}(p_{1}C_{33} + Ew^{2}k^{4}/12 + wk^{2}C_{55}/2 + k^{2}s^{2}\rho w^{3}/2 + \rho ws^{2})$$

$$H = -ikC_{13} + ikwp_{2}C_{55}/2 + \psi_{32}(\rho_{2}C_{33} + Ew^{2}k^{4}/12 + wk^{2}C_{55}/2 + k^{2}s^{2}\rho w^{3}/12 + \rho ws^{2})$$
(2.7)

where $w = b/\ell$, ρ , E, are nondimensionalized quantities and p_1 , p_2 , ψ_{31} , ψ_{32} are defined in (1.11).

(2.6)

III. NUMERICAL INVERSION

The inversions are accomplished by the Fast Fourier Transform (FFT) techniques [2], which consists of a transformation from Laplace to Fourier transforms, and a two-dimensional numerical inversion using the usual FFT alogarithm. Notice the Laplace inversion formula

$$f(t) = \frac{1}{2\pi i} \int_{\Gamma}^{C+i\infty} f(s) e^{st} ds$$

$$\Gamma$$

Set $s = C + i\alpha$

$$f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(C+i\alpha) e^{Ct} e^{i\alpha t} d\alpha \qquad (3.1)$$

where C and α are both real, and C is greater than the largest real part of all singularities of f(s). Numerically, the double Fourier transform (or inversion) has the following form [1]:

$$\mathbf{f}(\mathbf{x},\mathbf{t}) \cong \frac{\mathbf{K}_{\mathbf{X}}\mathbf{K}_{\mathbf{t}}}{\pi^{2}NM} = \frac{-\mathbf{i}\left[\mathbf{K}_{\mathbf{X}}(1-\frac{\mathbf{L}}{N})\mathbf{x} + \mathbf{K}_{\mathbf{t}}(1-\frac{\mathbf{L}}{M})\mathbf{t}\right] \times \mathbf{M}}{\mathbf{\Sigma} \times \mathbf{\Sigma}} \frac{\mathbf{X}}{\mathbf{f}(\mathbf{I},\mathbf{J})} = \frac{2\pi\mathbf{i}\left[\frac{(\mathbf{I}-\mathbf{I})\mathbf{x}}{N} + \frac{(\mathbf{J}-\mathbf{I})}{M}\mathbf{t}\right]}{\mathbf{I}=\mathbf{I}}$$

(3.2)

where N, M are the number of points in x and t direction respectively, and K_x , K_t are the corresponding half-frequency range.

For the present problem, the determination of C is through the following considerations:

The form of inversion integrals are, in general,

$$I = \frac{1}{2\pi i} \int_{C-i\infty}^{C+i\infty} \frac{F(k_1,s)}{\Delta(k_1,s)} e^{-px} e^{st} ds \qquad p = p(k_1,s), Re(p) \ge 0$$

$$C-i\infty \qquad (3.3)$$

and \triangle is given by (1.14). It is easy to see the singularities of the integral of (2.3) are:

a) Poles at
$$\Delta = 0$$
,

$$\Delta = (p_2 - p_1) ik_1 (C_{13} - \psi_{31} \psi_{32} C_{33}) + (\psi_{32} - \psi_{31}) (k_1^2 C_{13} + p_1 p_2 C_{33}) = 0$$
(34)

implies

$$(p_2-p_1)[C_{13}k_1^2p_1p_2(C_{13}+C_{55})^2 + C_{33}(C_{55}p_1^2-s^2-C_{11}k_1^2)(C_{55}p_2^2-s^2-C_{11}k_1^2)]$$

$$= 0 \qquad (3.5)$$

Interpretation of this condition is best understood for the particular case of an isotropic material, i.e. for

$$C_{11} = \lambda + 2\mu = C_{33}, \quad C_{13} = \lambda, \quad C_{55} = \mu,$$

choose $C_{66} = C_{55} = \mu$
It is easy to see that from (1.10), (1.11)

$$det = [\mu p^{2} - (\mu k_{1}^{2} + \rho s^{2})] \{ (2\mu + \lambda) p^{2} - [(\lambda + 2\mu) k_{1}^{2} + \rho s^{2}] \}$$

$$p_{1}^{2} = (\mu k_{1}^{2} + \rho s^{2})/\mu, \qquad p_{2}^{2} = [(\lambda + 2\mu) k^{2} + \rho s^{2}]/(\lambda + 2\mu)$$

$$\psi_{31} = ik_{1}/p_{1}, \qquad \psi_{32} = -p_{2}/ik_{1},$$

Here $[\mu/\rho]^{1/2} \equiv v_s$, is the shear wave speed and $[(\lambda+2\mu)/\rho]^{1/2} v_p$, is the longitudinal or pressure wave speed for isotropic materials.

Thus for the isotropic case that, $\Delta = 0$ implies

$$4\mu p_{2} + (p_{1} + \frac{k^{2}}{p_{1}}) \left[\lambda + \frac{p_{2}^{2}}{k^{2}} (\lambda + 2\mu)\right] = 0$$
(3.6)

where p_1 , p_2 are defined above. This is the equation for the Rayleigh wave speed $v_R \equiv (is /k)^{1/2}$ which is found as a real root of (3.6) (see e.g.[3]). For the case $\lambda = \mu$ (Poissons ratio = 0.25), $v_R = 0.919 v_s$.

For the anisotropic case a computational scheme to calculate the zeroes of (3.5) has been written, (Figure 2).

b) Branch points: The branch points of the integrand in(3.3) are the same as those of the functions $p_1(k_1,s)$, $p_2(k_1,s)$, they are:

i)
$$p = 0$$
, or $p = 0$ which implies $(C_{11}k^2 + \rho s^2) (C_{55}k^2 + \rho s^2) = 0$
i.e., $k/s = \pm i\sqrt{\rho/C_{55}}$, $\pm i\sqrt{\rho/C_{11}}$ pure imaginary.

These correspond to longitudinal and shear wave speeds for an isotropic material

ii)
$$p_{1,2} = \pm \sqrt{-B} \pm \sqrt{B^2 - 4AC/2A}$$
 (3.7)

with $A = C_{33} C_{55} > 0$

$$B = -\rho s^{2} (C_{33} + C_{55}) + k^{2} [(C_{13} + C_{55})^{2} - C_{11} C_{33} - C_{55}^{2}]$$

$$C = (C_{11} k^{2} + \rho s^{2}) (C_{55} k^{2} + \rho s^{2})$$

These branch points are those values of s/k which render B - 4AC = 0, and are branch points of second order.^[4] The distribution of these points is shown in Figure 3. It has been shown [5] that the contribution of these branch points to the value of the integrals (3.3) is important only when one considers the multi-reflected and refracted waves in layered media, or when the position of interest is very close to the impact origin. In this study we were more concerned with how the energy is propagated away from the impact point, which is mainly associated with surface waves, thus we ignored the contribution of these branch points.^[5]

The contour of integration for the Laplace inversion is as shown in Figure 3. Notice the branch cuts are extended to negative infinity, in accordance with the requirement that $C > \max$ real part of the singularities. The requirement that real $(p) \ge 0$ also determines the correct sheet of the Riemann surfaces. Numerically, since the branch points are located at s/k = constant as k gets large C should be large, and the factor e^{ct} in the Laplace inversion expression will rise sharply to an unmanageable size. Since, in the last paragraph, we have noticed the contribution of the branch points is unimportant, a path Γ_2 is chosen to replace Γ_1 by the Cauchy's integral theorem. Notice the advantage of integration along Γ_2 is that C_0 is a positive constant independent of k. The determination of optimal C_0 is discussed in [2]. Here, in order to minimize the aliasing and round off errors in numerical computations simultaneously, we choose

$$C_{o} = \frac{2}{3M\lambda_{t}} \qquad \ln (\hat{g}/\hat{r}) \qquad (3.9)$$

where $\hat{g} = p_0/C_{65}$, $\hat{r} = 10^{-6} \times \frac{1}{\lambda_t}$. λ_t is a small time interval, less than the impact contact time. Further details are given in Appendix A.

IV. RESULTS

A computer program has been written to calculate the stresses in a plate with an elastic beam on one edge under a transient impact load distribution along the edge. A program description, flow charts, input data formats, and sample printout of the program are contained in the appendices to this report. In this section we will summarize some of the results obtained from this computer program. These results were calculated for an anisotropic plate with effective elastic constants of 55% graphite fiber/epoxy matrix composite obtained from Reference 7 and summarized in the Table.

No-strip case:

The Rayleigh wave can be seen in the stress t_{11} on the edge as shown in Figures 4, 5 for a graphite fiber-epoxy composite for layup angles 0, + 15°. After the initial contact time, the stress is observed to propagate with little change at a speed near the calculated Rayleigh speed (Figure 2). This wave can be observed in the computed output in the space-time $(x_1, -t)$ plane Figure 7, as a band of non-zero values along a diagonal from the upper left to the lower right corner of the x_1^{-t} , -t plane. Caution is urged in using this program since spurious waves can enter the calculations due to the periodic nature of the finite numerical Fourier Transform. These spurious waves are data bands which lie along diagonals from upper right to lower left. In other words, only disturbances emanating from the impact source in the upper left corner of the x_1 -t plane of Figure 7 should be valid. A computer map of the space time history of the edge impact stress is shown in Figure 6. A contact time of 35 µsec and contact length 2 cm was used in these calculations.

- 20 -

As is characteristic of surface wave effects, the stresses due to impulsive loading on the edge decrease with distance from the edge. This is shown in Figure 8 for two different layup angles. The normal stress t_{33} appears to decrease to about 1/4 of its value on the surface at a depth equal to one half of the loading length a. The rate of decay from the edge depends on the layup angle. Another characteristic of edge impact is the development of tension in the normal stress t_{33} under the impact point. This is shown in Figure 9. Thus while the compression part decreases with distance from the edge <u>a tension tail developes in the wave</u>.

The effect of layup angle on the impact stresses can be seen in Figures 10, 11. The stress t_{11} at the edge is larger than the impact pressure and decreases as the layup angle goes from 0[°] to + 45[°] (Figure 10).

Below the surface or edge, the peak normal stress t_{33} at $x_1 = 0$ is a minimum for layup angles near $\pm 30^{\circ}$, while the shear stress t_{13} increases as the fiber angle goes from 0° to $\pm 45^{\circ}$ (Figure 10).

An unexpected result is the shift of the maximum normal stress t_{33} to points off the impact axis $x_1 = 0$ for layup angles greater than about + 30. A pronounced peak in t_{33} versus $x_{1/}$ beyond the impact pressure foot print, can be seen in Figure 11 for + 45° layup angle.

Impact protection strip case:

The effect of bonding an edge impact protection strip to the half plane is shown in Figures 12-16. In Figures 12, 13, the increase in the thickness of a steel strip produces a decrease in the interface stresses

- 21 -

 t_{11} , t_{33} but creates an interface shear stress at the strip-composite interface. This shear stress reaches a maximum for strip thickness less than the impact footprint length and decreases for greater strip thicknesses. Thus, if the strip is too thin, <u>debonding can occur under im-</u> pact due to induced interface shear.

In Figure 14 one can see that increasing the strip thickness decreases the peak normal stress t_{33} and redistributes the load over a longer length under the strip. However, while the peak compression stress is decreased by the strip, tension is created which could also produce debonding of the strip from the composite.

For the no-strip case a Rayleigh wave was seen to propagate along the edge relatively unperturbed (Figures 4, 5). With the strip present, (Fig.15) this wave becomes distorted as time increases. In fact, the beam-strip boundary conditions introduce dispersion in the edge waves which make the Rayleigh edge wave velocity dependent in the effective wave length of the disturbance.

Finally in Figure16 shear stress distributions along the stripcomposite interface are shown for a thickness near the shear peak (b/a = 0.25) and another for b/a = 2.0. In the latter case the shear is distributed over a larger length resulting in a lower peak stress. Also the strip delays the time of maximum shear from 1/2 to 3/4 T_a

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Summary of Results

An analytical-numerical method has been developed to solve the response of a composite plate with a bonded edge strip to in-plane impact type forces on the edge. Results of computer simulations reveal the following:

- 1) Rayleigh edge waves can propagate away from the impact site with tension and compression up to values of the impact pressure, depending on layup angle.
- 2) Normal to the edge, the initial peak compression pulse decreases as it propagates into the plate but a tension tail develops as it propagates away from the impact site.
- 3) The edge stress t_{11} under impact is decreased as the fiber layup angle goes from 0° to $\pm 45^{\circ}$.
- Protection strips of thickness less than half the impact length can develop large interface shear under impact.
- 5) The normal and edge stresses t_{33} , t_{11} at the edge can be decreased significantly by protection strips of thickness greater than the half impact length.

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TAPLE I. - STRESS-STRAIN COEFFICIENTS FOR 55 PERCENT GRAPHITE

FIBER-EPOXY MATRIX COMPOSITE

0 ⁰ Layup					±15 ⁰ Layup							
27.95	0.3957	0.3957	0	0	0	24.56	0.4000	1.986	0	0	0	
i.	1.170	0.4601	0	0	0		1.170	0.4558	0	0	0	
		1.170	0	0	0			1.374	0	0	0	
			0.3552	0	0				0.3552	0	0	
		,		0.7197	0					2.310	0	
					0.3552						0.3552	
±30 ⁰ Layup					±45 ⁰ Layup							
16.48	0.4118	5.167	0	0	0	8.197	0.4279	6.758	0	0	0	
	1.170	0.4400	0	0	0		1.170	0.4279	. 0	0	0	1
		3.093	0	0	0			8.179	0	0	0,	
			0.3552	0	0				0.3552	0	0	
				5.491	0					7.082	0	
					0.3552						0.3552	

[All constants to be multiplied by 10^6 psi; data obtained from ref. 7.]

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APPENDIX A

The Determination of Parameter C

Consider the Laplace inversion of a function g(t) as

$$g(t) = \frac{1}{2\pi i} \int_{C_0^{-i\infty}}^{C_0^{+i\infty}} \bar{g}(s) e^{st} ds \qquad (A.1)$$

and let $s = C_0 + i\omega$, C_0 and ω are real. We can change (A.1) into the Fourier inversion formula

$$g(t) = \frac{1}{2\pi} e^{C_0 t} \int_{-\infty}^{\infty} \tilde{g}(C_0 + i\hat{w}) e^{i\omega t} d\omega = e^{C_0 t} \mathbf{x}(t) \quad (A.2)$$

which is then inverted by the Fast Fourier Transform technique. In the FFT scheme, a continuous function $\bar{g}(C_0+i\omega)$ is discretized and the infinite interval of integration is truncated. The error due to truncation depends on each problem but doesn't depend on C_0 , thus in the determination of C_0 , we will assume the truncation error is negligible. It is shown [2] that the discretizing of the transform in one domain will cause aliasing error in the other domain, e.g. sampling \bar{g} at N points in a frequency interval, $0 < \infty < \Omega$, will produce a transformed function $x_p(t)$ which is periodic and which differs substantially from x(t) for large enough t. For even x(t) this difference can be shown [2] to be given by,

$$x_n(t) \simeq x(t) + x(t-T)$$

for 0 < t < T/2 where $T = N/\Omega$.

It has been shown [2] also that the aliasing error is approximated + $C_0(T-2t)$ by $E_a(t) = e$ g(T-t) for the Laplace inversion (A.2).

Notice the aliasing error is a decreasing function of C_0 .

The other source of error is of course the round off error in compu- C_{ot} tation. Since we multiply the resulting x(t) by e to get g(t), the rounding error is of the form

$$Er(t) = e^{C_0T}r(t).$$

The error bounds are then

$$\varepsilon_{1} = |Max Ea(t)| = e^{-C_{0}(T-2\tau)} Max|g(T-t)|$$

$$\varepsilon_{2} = |Max Er(t)| = e^{C_{0}\tau} Max|r(t)|$$

$$0 \le t \le \tau$$

Equating ε_1 and ε_2 , the optimal C is then

$$C_{o} = \frac{\ln (Max g(T-t)/Max r(t))}{T-\tau}$$

Chosing $\tau = T/4$, therefore

 $C_{o} = \frac{4}{3T} \ln(\hat{g}/\hat{r})$, $\hat{g} \equiv Max g(T-t)$, $\hat{r} \equiv Max r(t)$

Notice, empirically, $\hat{r} \approx 2 \frac{N}{T} 10^{-6}$ on single precision IBM 360 systems.

- 28 -APPENDIX B

- A FLOW CHART OF THE PROGRAM
- 1. Main Program



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APPENDIX C

NOTES ON COMPUTER PROGRAM

The choice of scales is very essential to the success of the present computational method. It is noticed that the accuracy depends on the number of points employed and the range of frequency spectra covered. Considering limitations of both computer storage and time, a time-space grid of 32 x 64 points was chosen for t > 0, $x_1 > 0$. Thus, the nondimensionalization of all equations and quantities are both necessary and important to the obtaining of meaningful data from the limited grid size.

The numerical inaccuracies introduced have several origins: 1. Theoretically, error has been introduced by the neglecting of the outer branch points contributions. It has been shown, for isotropic cases, the contributions of these branch points behaved like r^{-2} at large distance from a delta function loading at the origin r = 0. Compared with the $r^{-\frac{1}{2}}$ decreases of the contribution of the residue. Thus, for small r, or near the origin, the errors might be significant. An asymptotic form of the behavior of small r has been deduced for a simple delta loading at origin on an isotropic half-space []. It is shown the error thus introduced is of the order of 5% maximum response in stress.

2. The aliasing error introduced through the periodizing of the functions. 3. The round-off error in Laplace inversion along with aliasing error. have been discussed in the determination of C_{0} (Appendix A). It is

- 30 -

found that error 3 is more serious of the two. Hence in calculations the maximum non-dimensionalized time should be restricted to below 6 or 8 for reasonably good results.

4. Errors due to reflections at the boundary. Since the space grid is finite, it has been observed that whenever a wave hit the boundary of chosen space, a sizable numerical error will start propagating in, as if the wave were reflected from the boundary. The basic reason is due to the periodization of the space (x_1) domain. In computation, this error should be avoided. To correctly determine the extent of the space (x_1) domain, a priori recognization of significant wave speed (at which most of the energy travels) is important. Usually an estimation will be sufficient. Then the proper nondimensionalizing constants can be chosen.

APPENDIX D PROGRAM INPUT AND OUTPUT

Α. Method: FFT alogarithm for numerical inversion Input Data Cards: Β, Card 1. NTEST, NSTRIP, NP (315) 1 A test program for FFT (2-D) (beam). NTEST = The present program 0 NSTRIP = 1 With strip No strip 0 Calculate: u only NP = 1 2 u, u u, u, t 3 u, u, t, t, t 1 3 33, 11 4 u, u, t, t, t i 3, 33, 11, t 5 Card 2. CC(I) I = 1,9, RHO, ANGLE (8E10,4) CC(I=1,9) Material constants of composite, in the order $C_{11}, C_{22}, C_{33}, C_{44}, C_{55}, C_{66}, C_{12}, C_{13}, C_{23}$ (psi) Density of composite (g/cm³) RHO ANGLE (degrees) lay-up angle Card 3. VEL , DM, E1, ANU, DEN (8E10.4) VEL - Velocity of incoming particle m/sec DM - Diameter of impacting object cm - Youngs Modulus of impacting object (psi) E1 ANU - Poissons ratio of impacting object DEN - Density of impacting object (gm/cc)

- Card 4. NSTRES, NK3, DX3 (215, F10,3) NSTRES = 1Number of steps in x_3 direction NK3: $\Delta x_3/\ell$, step size in x_3 direction DX3: Photo elastic fringe order computer map in the x-t plane. . . RO, W, ES (3E10,4) Card 5. density of strip beam (g/cm^3) RO: depth of strip beam (cm) W: Young's modulus of strip beam (psi) ES:
- C. Output:
 - 1. Test problem: Appendis III
 - 2. Values of displacements $1 : u_1$ $2 : u_3$ (stress) $3 : t_{33}$ $4 : t_{13}$ $5 : t_{11}$
 - 3. Relative magnitude computer maps of displacements and stresses.



FORTRAN IV G LEVEL 21

C****** PROGRAM TO CALCULATE STRESSES DUE TO EDGE IMPACT OF A PLATE* С C THIS PROGRAM CALCULATES THE ELASTIC RESPONSE OF A N С ANISOTROPIC PLATE TO AN IN-PLANE EDGE IMPACT FORCE ON X3=0.0 С WHEN NSTRIP =1 , THE PROGRAM PLACES AN IMPACT PROTECTION STRIP С , OR BLASTIC BEAM ON THE EDGE. THE IMPACT FORCE IS A HALF SINE ¢ FUNCTION IN TIME AND IS NON ZERO FOR O<T<TO, (MICROSEC). THE С FORCE IS DISTRIBUTED ALONG THE EDGE AS PO(1-X1**2), WHERE C X1 IS NORMALIZED BY THE HALF WIDTH OF THE IMPACT CONTACT С LENGTH. ¢ THE METHOD EMPLOYS A POURIER TRANSFORM IN THE EDGE DIRECTION Ç X1, AND A LAPLACE TRANSFORM IN THE TIME DIMENSION. THE TRANSFORM C OF THE FORCING FUNCTION IS GIVEN IN THE SUBROUTINE CALCUL AND С THE SOLUTION IS OBTAINED USING A 2-DIMENSIONAL FAST FOURIER С INVERSION ROUTINE CALLED *POURT*. С THE OUTPUT FOR A GIVEN DEPTH.X3 CONSISTS OF DISPLACEMENTS Ċ U1, U3, AND STRESSES T33, T11, T13, IN THE X1-TIME PLANE . С THE STRESSES ARE NORMALIZED BY THE PLASTIC CONSTANT C(6,6). С С IMPACT FORCE С I С I C I С I С v Ι ٧ С VIV С VIV С V С С * * * * * * * * * * * * * <<< STRIP STRIP >>> * * С c С С ----> X1 C С С 1 С С COMPOSITE C 1 С С С 1 С C С HALF SPACE ł С C C V Ċ С C X3 С С INPUT DATA С NN(1) -- 2.0* MAX X1 DISTANCE, NN(2) -- MAX NO. OF TIME UNITS Ċ NSTRIP=0,NO STRIP,...NSTRIP=1,WITH STRIP c c NP=1,--,5, CALCULATES U1,U3,T33,T11,T13,IN THAT ORDER NP=6, CALCULATES DISPL. OF A BEAM ON AN ELASTIC FOUNDATION С CC(9), ELASTIC CONSTANTS OF PLATE IN THE ORDER С C11, C22, C33, C44, C55, C66, C23, C13, C12, IN PSI С RHO, DENSITY OF PLATE IN UNITS GM/CC С ANGLE--LAYUP ANGLE OF COMPOSITE PLATE, DEG., FOR INFO ONLY С VEL, VELOCITY OF INCOMING OBJECT METERS/SEC С DN, DIAMETER OF IMPACTING OBJECT -CM. С E1, ANU, YOUNG'S MODULUS AND POISSON'S RATIO FOR IMPACTING BODY С DENSITY OF IMPACTING BODY DEN, С NSTRESS=1 С NK3, NO.OF DEPTHS X3, (FOR NK3=1, X3=0) С DX3, INCREMENT IN DEPTH X3 (NORMALIZED BY AO) С DENSITY OF PROTECTIVE STRIP GE/CC RO.

* This program has two extra cards to override the Hertz contact time and contact length calculation. Remove cards #51, 52.

```
DATE = 74186
                                                                                  11/28/29
FORTRAN IV G LEVEL
                     21
                                         MAIN
                       W, THICKNESS TO WIDTH RATIO OF BEAM
             С
             С
                       ES, YOUNG'S MODULUS FOR BEAM
                       WI--FOURIER WAVELENGTH (CM) OF THE ORDER OF AO OB LESS
WI--FOURIER WAVE PERIOD (SEC) OF THE ORDER OF TO OR LESS
             С
             С
                           CHOICE OF WL, WT DETERMINES DX, DT--DX=WL/2, DT=WT/2
             С
                            TRANSFORM OF NORMALIZED FORCING FUNCTION F(X1)*G(T)
             С
                       FG,
                            THIS IS PROVIDED IN PROGRAM BUT CAN BE CHANGED BY THE USER
             С
             С
             С
                       OUTPUT DATA
                       TO,TC CONTACT TIME (SEC, 1. E-6 SEC ) (PROM HERTZ THEORY)
             С
             С
                       AC.A.
                              HALF THE IMPACT CONTACT LENGTH , CM
                       FO, MAX IMPACT FORCE FROM HERTZ THEORY , NEWTONS
             С
                            WAVE SPEED IN PLATE SQRT (C66/RHO)
             С
                         OR WAVE SPEED IND BEAM STRIP, SQRT(E1/DEN) UNITS CM/SEC
             С
                       CL=SORT (C11/RHO) LONGITUDINAL WAVE SPEED ALONG EDGE IN PLATE
             С
                       CS=SQRT (C55/RHO), SHEAR SPEED ALONG EDGE OF PLATE, CM/SEC
             C
                       CR, RAYLEIGH WAVE SPEED ALONG FREE EDGE OF PLATE
             С
             С
                       DX, DT SPACE TIME INCREMENTS IN X1-T SPACE UNITS--CM AND SEC
             С
                       DATA(I,J) ,NORMALIZED TRANSFORM OF ONE OF DISPL. OR STRESSES
             С
                        --BEFORE CALL FOURT, AFTER CALL FOURT DATA IS A 2 DIM MATRIX OF
             С
                           DISPL. OR STRESSES IN X1-T SPACE.DEPENDING ON VALUE OF K
             С
                           IN THE LOCP 'DO 4 K=1, NP'
             С
                       U1, U3, NORMALIZED DISPL. IN PLANE OF PLATE (E.G. U1/A0)
             Ċ
              С
                       T33,T11,T13, NORM. STRESSES (E.G. T33/C66)
                           --NOTE-- T33 ON X3=0 SHOULD REPRODUCE THE FORCING FUNCTION
              С
              С
                                     WHEN THERE IS NO STRIP
              С
                           --NOTE-- AS A CHECK T13=0 ON X3=0 WHEN THERE IS NO STRIP
              С
                       THE FRINGE ORDER MAP PLOTS THE DIFF IN PRINCIPAL STRESSES AND
              с
                         MAY BE USED TO COMPARE WITH PHOTOELASTIC EXPERIMENTS OR TO
              С
                           LOOK FOR POINTS OF MAX IN PLANE SHEAR STRESSES
              С
                       ******
              С
                       THIS PROGRAM HAS BEEN WRITTEN BY F.MOON AND C-K KANG UNDER
              С
                         A GRANT TO PRINCETON UNIVERSITY FROM THE NASA LEWIS RESEARCH
              С
                         LAB.
              С.
                       *****
                       --NOTE TO THE USER-- IN THE OUTPUT MAPS OF STRESSES OR DISPL.,
              С
              С
                       YOU WILL NOTICE BANDS OF SIMILAR NUMBERS RUNNING PROM THE
              С
                       UPPER LEFT CORNER TO THE LOWER RIGHTCORNER -- THESE ARE WAVES
              C
                       WHICH EMINATE FROM THE IMPACT POINT--HOWEVER- WAVES RUNNING
              С
                       FROM RIGHT UPPER TO LEFT LOWER CORNER ARE SPURIOUS DUE TO THE
              С
                       DESCRETENESS OF THE NUMERICAL FOURIER INVERSION PROGRAM
              С
                       --ALSO DATA FOR TIMES NEAR TMAX AT THE BOTTOM OF THE MAPS ARE
              С
                       USUALLY SPURIOUS AND SHOULD NOT BE USED
              С
 0001
                    COMMON /MMC/ D, DK1
 0002
                    COMMON /MC/DK2, FG1, T0, C11, C13, C33, C55, RH0, R0, W, ES, NSTRLP, A0
 0003
                  DIMENSION DATA (128,32), NM (40), CC (9)
 0004
                    DIMENSION NN(2)
 0005
                    DIMENSION RDATA (40)
 0006
                    DIMENSION CIDATA(40)
 0007
                    DIMENSION FRNGE (64,32)
 0008
                    DIMENSION T11(64,32),T33(64,32),T13(64,32)
 0009
                    COMPLEX DATA,S
 00 10
                    CCMPLEX P1, P2, S1, S2, C1, C2, B, C, D, SI
 0011
                    COMPLEX DK2, FG, SLAP, DK1
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FORTRAN	IV	G	LEVEL	21	MIAN	DATE	= 74186	11/28,
0012				COMP	.EX*16 BS			
0013				NN(1	=128			
0014				NN(2	= 32			
		C]***	READ	IN AND WRITE OUT DATA AND P	ARAMETERS		
			- [***	RHO.	0.TO MUST BE IN C.G.S. UNIT	S. PO NUST	BE CONSIST	ENT WITH CC
0015			-	CALL				
0016				READ	(5.102) NTEST NSTRIP.NP			
0017				READ	(5,100) CC. RHO. ANGLE		· .	
0018			•	UPTT'	(6,490) CC			
0019				- ህዝግጥ	(6,491) RHO. ANGLE			
0020				PFAD	S 100) VEL. DH. EL.AND. DEN			
0021			•	P0=C				
0022				C11=	CC (1) = CC (7) ++2 / CC (2)			
0023				C11-	$(33 \pm 0013) = 0019 \times 2700127$			
0023				C12-	cc(9) = cc(3) = cc(9) + cc(2)			
0025				013-	CC(0) = CC(1) = CC(3) = CC(2)			
0025				C33-			•	
0028				51±				
6629					KNU/0.090+1.5-4			
0028				KEAU	(5, IUI) NSTRES, NK3, DK3			
0029				WR.	TE (6,504) NSTRES, NK3, DK3			
0030				51	CEPLX(U., 1.)			
		9		****	CALCULATE THE IMPACT CONTAC	T TIDE , RAI	JIN2"UN NU	1233UKE
0024			<u>_</u> *****		BASED ON HERTZ CONTACT THEO	RI		
0031				8=08, 5-55	2.0			
0032				K=K±				
0033				E I = E	*6895.0			
0034				E 2 = C	(2) *6895.0			
0035				DEN =	EN*1.0E3			
0036				A MA S	=4./3.*PI*R**3*DEN			
0037				AK2=	./3.*SQRT (R) *E1/ ((1.0-A NU*A	NU) +E 1/E2)		
0038				ALP =	./4.*AMASS*VEL*VEL/AK2			
0039				ALF=	(ALF) **0.4			
0040				TC=2	943*ALF/VEL			
0041				F0=1	14*AMASS*VEL*VEL/ALP			
0042				A=SQ	T (ALP*R)			
0043			•	A=1.	122*A			
0044				TC=T	*1.0E6			
0045				WRIT	(6,710) VEL,TC,A,FO			
			****	*****	******	*		
		(]***	CALC	LATE THE NON-DIMENSIONAL PA	RAMETERS		
0046				EE=	C (6)			
0047				E≈ S	RT (EE/RHO)			
0048				RE≠ _	HO			
		(3	D	FINE TRANSPORE SPACE AND DI	STANCE-TIME	SPACE	
		(]***	UNIT	DISTANCE CM.			
0049				A 0= A				
0050				T0=T	*1.E-6			
			C		TEST CASE TO== 35E-	6, A0=1 CN		
0051				A 0 = 1	0	-		
0052				T0=35	.E-6			
0053				AL=A				
		(:***	UNIT	TIMESEC.			
0054				TE=A	/E			
~~~~		(	***	SMAL	EST WAVELENGTHS	•		
0055		•		WL=A	/1.5			
0000				97=T)	/10.0			
0000					····			

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FORTRAN IV G LEVEL 21

11/28/21

	C*** DIMENSIONS OF TRANSFORM SPACE
0057	XK=2.0*PI*AL/WL
0058	TK=2.0*PI*TE/WT
	C*** NCNDIMENSIONALIZE CONSTANTS
0059	AO = AO / AL
0060	TO = TO/TE
0061	
0062	$D_{x} = W I / 2 \cdot 0$
0063	
0000	MRIII (0,021) — «,, ma, ing an
0060	C CALCULATE RAILEIGG WAVE SPEED
0004	
0005	x2= C55
0066	
0067	DO 90 I=1,100
0068	N = N + 1
0069	X = (X1 + X2) / 2.0
0070	D1 = (C55 - X) / (C11 - X)
0071	D 1= SQRT (D 1)
0072	D2= (C13) **2-C33* (C11-X)
0073	D3=C55*C33
0074	D3 = SQRT(D3)
0075	F=D1*D2/D3
0076	F=X+P
0077	IF(F) 81.82.83
0078	81 X 1=X
0079	GO TO 92
0080	82 60 70 91
0081	83 ¥2=¥
0082	92 CONTINUE
0083	
0084	$\mathbf{F} \mathbf{F} \mathbf{F} \mathbf{F} \mathbf{A} \mathbf{F} \mathbf{C} \mathbf{F} \mathbf{D} 1 = 1  \mathbf{O} \mathbf{F} \mathbf{D}$
0085	
0005	
0000	
0007	7 I CUNTINUS UNTERVE 7011 011 011 011
0000	
0083	701 FORMAT (//, 10X, 6H C11 =, E12.4, 6H C33 $\pm$ , E12.4, 6H C55 $\pm$ , E12.4,
0000	10H C I 3 = , E 12, 4, 7
0090	CL=C11/RHO
0091	CL=SQRT (CL)
0092	CS=C55/RHO
E600	CS=SQRT (CS)
0094	CR=X/RHO
0095	CR = SQRT(CR)
0096	RDS=CR/CS
0097	WRITE(6,702) CL,CS,CR,RDS,N
0098	702 FORMAT(//, 10X, 12HLONG. SPEED =, E12.4, 13H SHEAR SPEED =, E12.4
	1 //, 10X, 16 HRAYLEIGH SPEED =, E12.4, BR CR/CS =, P10.5, 5X, 15)
	C * * * * * * * * * * * * * * * * * * *
	C*** CONSTANTS FOR STRIP CASE
0099	READ (5, 100) RO.W.ES
0100	WRITE (6.521) RO.W.ES
0101	$RO = RO/6, 895 \pm 1, E-4$
0102	IF (RO) 51.51.50
0103	50 CONTINUE
0104	E= SORT (FS/RO)
	2 PART (PS/40)

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PORTRAN IV G LEVEL 21

0105	WRITE (6,510) E
0106	51 CONTINUE
0107	RO = RO/RE
0108	ES= ES/EE
0109	W= W/AO/AL
	C*************************************
0110	205 CONTINUE
0111	C11 = C11/BE
0112	C13= C13/BE
0113	C33= C33/EE
0114	C55= C55/BE
0115	PO = PO / FE
0116	RHO = RHO/RE
0117	RG1 = P0 + T0
0118	
0110	
0120	a. 1117)
0120	л- лици. С+++ салантати тик тартаси TNVRRSTON PARAMETRR
0404	UTTT CALCULAID INE DATMACE INTENSION FRANCESS. UM-DEARD
0121	
0122	
0123	CH= 2./3./M/WT* ALUG (KR)
0124	CLAP= CH
<del>.</del>	C*** CALCULATE THE SECOND UNDER DRANCH FUINIS
0125	A = RHO* (C33-C55) ** 2*RHO (C31-C55) ** 2*RHO (C
0126	E= -2.*RHO*((CJJ+C55)*(CIJ+CIJ+CIJ+CIJ+CJJ+CJJ+CJJ+CJJ)*2.**CJJ+CJJ
0127	$\mathbf{F} = (C13 + C13 + 2 + C13 + C55 - C11 + C33) + + 2 - 4 + + C11 + C33 + C55 + C55$
0128	BS= 1.D0*E*E-1.D0*4.*A*F
0129 🕓	D= CDSQRT (BS)
0130	P1= →5/A*(+E+D)
0131	$P2=F/P1/\lambda$
0132	P1= CSQRT (P1)
0133	P2=CSQRT(P2)
0134	WRITE (6,509)
0135	WRITE (6,506) P1,P2
0136	204 WRITE (6,508) CLAP
0137	$N_{2} = N_{2} + 1$
0138	M2= M/2+1
0139	IF (NTEST.EQ.1) GO TO 211
0140	211 IF (NSTRIP.EQ.1) WRITE (6,514)
<b>U</b> • • • •	C*** GENERATE THE TRANSFORMED EXPRESSIONS
0141	REWIND 2
0142	DO 1 I = 1, N
0103	DK1 = 2. * XK / N* (I5) - XK
0140	DO 1 J = 1.0
0144	DK2F=2. *TK/N* (J+.5) -TK
0145	SLAP= CMPLX (CLAP, DK2F)
0140	DK2 = -SI * SLAP
0147	TF (NTEST.NE. 1) GO TO 201
0140	PG= PT*(1.+CEXP(-SLAP))/(SLAP*SLAP+PI*PI)*
0149	105TW/DK11/DK1#(1, +DK1+DK1/(PT+PT-DK1+DK1))
	TOUTH (NY FIZURA CONTRACTOR STATES AND CONTRACTOR S
A - F -	$\frac{1}{1} = \frac{1}{1} = \frac{1}$
0150	μαια της του
0151	GU TU F
0152	ZUT CALL CALCUL(U)
0153	T CONTINUE

· .

FORTRAN	IV	GL	EVEL	21	MAIN		DATE = 74186	11/28/2
0154 0155				IF (NT) WRTTE	EST.NE.1) GO TO 202			
0156				CALL	(0,007) OHRT/DATA NN 2 1 1 AL			
0157					KT = 1 N2			4
0158				9 <del>-</del> -ST	α Ξ =			
0159				DO 15	P = 1 H			
0160					NUデー 1 g 印 本DT /M本 /W二 4 1 年 / V コー 4 1			
0161				$\tau = -51$	-PI/G-(G-1)+(KJ-1) FF*(F1-1)			
0162				- 1 - EI/J - DAWA (KI	LAT (AUTI) LAT (AUTI)			<b>.</b>
0163			15	DATA (K)	L # NU ) - DATA (NL # NU) * X N N	+TK/PI/PI/N	VERCEXP(B) *CEX	P(C)
0164			15	- DALA (A) - Sotas	LANDJE DATA(KLAKU)*EX (6 606) (/Dimi/T t)	P(CLAP+T)	4	
0165		~	ل سار سار سار ا	GO TO 2	203	J= 1,01), 1=	₹, N2)	
		- C1	******	*******	******			
0166		<u>ر</u> ،	202	DALN LU	DOP FOR DIFFERENT DEP	TAS X3		
0160			202	UU D K.	3= 1,NK3			
0107		~	لم بد با	X 3= (K.	3-1) *DX3			
0168		C,	~ ~ ~	LOOP FC	JR CALCULATING DISPLA	CEMENTS AND	STRESSES AT A	GIVEN DEPTH
0160				DO 4 K=	= I,NP			
0109				WRITE (C	0,680) (C. 50,41 m.)			
0170				WRI1E (	(5,501) X3			
0170				REWIND	2			
0172					= ], N			
0175				DO / J=				
0175				READ (2	<pre>4) P1, P2, C1, C2, S1, S2,</pre>	DK1, DK2		
0175				B= CEXE	?(=X3#21)			
V170		<b>C H</b>	. س	C= CEXE	? (~X3¥P2)			
0177		U.+		DISPLAC	BRENTS			
0178				15 (N.C	(Q, 1) DATA $(I, J) = C1 * B$	+C2*C		
0170		<b>C *</b>	r ate aiu	IF (N.F	$Q \cdot Z$ DATA $(I, J) \neq C I \neq S$	1*B+C2*S2*C		
0179			• •	JINESSE				
••••			1	ገር ቢለቀድ በአጥል /ተ	-1\ = (C13+CT+D21.033+)			
0180			•	TP /V E	O #1	6 1+2 1) +C 1+B	+(CT3*SI*DK1-C3	3*P2*S2) *C2*C
			1	ገር (ጠቀይ በአቆጥል /ፕ	(V·7) - T) - (C11*ST*DV1_C12+:			
0181			•		30 = (CIT+3I+DRT+CI3+)	r 1+2 i) +C 1+Bi	+{C11*ST*0K1+C1	3*P2*S2) *C2*C
			• 1	ግግ በግግ ግግ ለማስጠ	(2 + 3) = (-55 + 1) + - 51 + - 5 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + - 52 + 52 + - 52 + - 52 + 52 + 52 + 52 + 52 +	+		
0182			•	TR /R T	Φ 6/ CO MO 7	*5 I) *C I≭8+ (-	+ 2+S1 * 0K 1*S2) *	C2*C)
		C*	**	17 (N.D	POP & PRAMON AN DIA			
0183				FF=0 1	FOR A BEAM ON AN ELAS	STIC FOUNDAY	LION	
		C*	**	FORCING				
0184		•		FG= DT+	FG1+/1 +CFYD/_CT±NF2	*****		• •
			1	14. / (DK 1		- 10) ) / (BT+51	L - U & Z * U & Z * T U * T U	) *
0185			•		*DK1/12  D*/25*U=0 = DE	1 * DE 1 - RO * CCC	15 (UN ITAU) ) 15 (UN ITAU) )	+
			1	+EP	· DR1/12:0+(E3+#+#+DR	1+DV1-RO+M+A	*DKZ*DKZ)-HO*W	*DK2*DK2
0186			•	TPINE	0.6)			
			1	DATA (T.	$11 \pm 8C/D$			
0187			7	CONTINU	C) - 1 C) D			
0188			•	CALL FO	☆   111日〒/DAITA NN つ 1 1 (A)			
0189				DO 3 KT	= 1.02			
0190				B = -ST *	PT/N + (N - 1) + (VT - 1)			
0191								
0192				C = -ST *				
0193				T= PT/T	××××××××××××××××××××××××××××××××××××			
0194				DATA (KT	$\mathbf{F}_{\mathbf{A}} = \mathbf{D}_{\mathbf{A}} \mathbf{T}_{\mathbf{A}} \mathbf{F}_{\mathbf{A}} $		M /Nw (DWD / D) +	NB (0)
0195				E= CLAP	**************************************		UNUTOPYN(R) *CR	76 (C)
0196			3	DATAIKT		D / R)		
			-		A A A			

.

ORTRAN	IV G	LEVEL	21	MAIN	DATE = 74186	
		~***	() S T C 11 1 2 M 12	THE DROTORIASTIC PRING	E ORDER	
0197		6.444	DA 200 T=			
0137			-1 002 00	1 32		
0190			10 230 0-	3)		
0 2 0 0			TE (0.000.	$\frac{1}{1} = \frac{1}{1} = \frac{1}$	. J)	
0200			TE (N.EU.	$= \frac{1}{1} + $		
0201			1F (K+EQ+	(2) 1 2 (1 2 0) - KEVT (DV 1 V (1	<b>1011</b>	
0202			TL (V°EA.	5) 60 10 280	1	
0203			GO TO 290		•	
0204		280	CONTINUE		117 T 11 # T12 (T 1)	
0205			FNGE = (T11)	(I,J)-T33(I,J))++2+4+0+	E 15 (190) + (15 (190)	
0206			FRNGE (I, J	I) =5QET (FNGE)		
0207		290	CONTINUE	· · · · · · · · · · · · · · · · · · ·		
0208		214	WRITE (6,	,511) K		
		C***	FIND THE	MAXIMUM VALUE		
0209			RS = 1.E - 3			
0210			DO 14 I=1	1,,40		
0211			DO 14 J=	1,32		
0212			S= DATA (1	(J)		
0213			TP= REAL	(S) /RS		
0214			TF (ABS/1	(P), LT. 1.) GO TO 14		
0215			RS= REAL	(S)		
0216		14	CONTINUE	· · · · · · · · · · · · · · · · · · ·		
0210		17	WRITE (6.	516) RS		
02.17		c	WELL (O)	PRINT REAL PART OF	DISPL. AND STRESSE	S
0210		C.				
0210			NT 3 = 10			
0219			010-10 DO 310 T-	- 1 мт т		
0220				- 1, (11)		
0221				(00) T1		
0222			WRITE (0, C			
0223			DO 300 J=	$= 1_{\mu} J \mathcal{L}^{-1}$		
0224			SR=RLAL (I	UATA (I, J) ) / RS		
0225			SING=AIN/	AG (DATA (1,J))/RS		
0226			RDATA(J)=	=SR		
0227		_	CIDAIA(J)	=SIAG		
0228		300	CONTINUE		×	
0229			WRITE(6,	620) (RDATA(L),L=1,8)		
0230			BRITI(6,6	650)		
0231			BRITE(6,	620) (CIDATA(L),L=1,11)		
0232		310	CONTINUE			
0233			HRITE(6,	580)	•	
0234			IF (K.EQ.	.1) WRITE(6,630)		
0235			IF (K.EQ.	.2) WRITE (6,631)		
0236			IF (K.EQ	.3) WRITE(6,632)		
0237			IF (K.EO	.4) WRITE(6,633)		
0238			IF (K.EO.	.5) WRITE (6,634)		
0230			IF (K.EO.	.6) WRITE (6.635)		
0239			WRTTE (6.	640) DX.DT		
V 4 4 V		C 🕸 🕸 🕷	PLOT THE	RELATIVE VALUES		
0.24.4		• • • •	DO 12 J=	1.M		
0241			- T C 12 J-	1.40		
0242			- DO 13 1-	1 / T 11		• •
0243			S- DAIA (.	577 (C) /DC # 100		
0244		13	( 88 (1) = R)	5451 SM	•	
0245			WRITE (D	, בוכי		
0246		12	CONTINUE		T ODDED	
		C***	PLOT A M.	AP OF PHOTUELASTIC FRING	P OTARK	
0247			IF (K.LT	°2} GO TO 4		

FORTRAN IV G LEVEL 21

.

0248	RS=1.E-3
0249	DO 312 I=1,20
0250	DO 312 J=1,20
0251	SS=FRNGE(I,J)
0252	TP=SS/RS
0253	IF (ABS (TP).LT.1.) GO TO 312
0254	RS=SS
0255	312 CONTINUE
0256	WRITE (6,680)
0257	WRITE(6,516) RS
0258	WRITE (6,690)
0259	DO $320 J=1,32$
0260	DO 315 I=1,40
0261	SS=PRNGE(I,J)
0262	315 MM(I)=SS/RS*100
0263	WRITE(6,515) MM
0264	320 CONTINUE
0265	4 CONTINUE
0266	6 CONTINUE
0267	100 FORMAT (8E10.4)
0268	101 FORMAT (215,3F10.3)
0269	102 FORHAT (315)
0270	490 FORMAT (5X, 55H BLASTIC CONSTANTS C11, C22, C33, C44, C55, C66, C12, C13, C3
	12,/9E12.4,/)
0271	491 FORMAT (5X, 25H DENSITY OF PLATE GH/CC, F10.4, 5X, 20H FIBER LAYUP AN
•	1GLE,F10.4)
0272	500 PORMAT (2F12.4,4E15.4)
0273	501 FORMAT (5H X3= F10.4)
0274	502 PORMAT (10H STRESSES T3/(BE15 7))
	247 rought (100 010000 13/(0113:11)
0275	503 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7)
0275 0276	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/)
0275 0276 0277	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES )
0275 0276 0277 0278	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7)
0275 0276 0277 0278 0279	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST )
0275 0276 0277 0278 0279 0280	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4)
0275 0276 0277 0278 0279 0280 0281	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCNE ORDER BRANCH POINTS )
0275 0276 0277 0278 0279 0280 0281 0281 0282	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= P10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= P12.4) 509 FORMAT (28H SECCNE ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,P12.3,7H CM/SEC)
0275 0276 0277 0278 0279 0280 0281 0282 0283	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCNE ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0283 0284	503 FORMAT (304 DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I )
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0285	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (8F15.8)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0285 0286 0287	503 FORMAT (505 DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (8F15.8) 514 FORMAT (/50X 10HWITH STRIP)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0284 0285 0286 0287 0288	503 FORMAT (104 DIAMADEN 15, 10, 10, 10, 10, 10, 10, 10, 10, 10, 10
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0284 0285 0286 0287 0288	503 FORMAT (104 DIAMASHS 15) (0019.1) 503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (8E15.7) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (8F15.8) 514 FORMAT (750X 10HWITH STRIP) 515 FORMAT (24,40I3) 516 FORMAT (16H MAXIMUM VALUE= E15.7)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0284 0285 0286 0287 0288 0289	503 FORMAT (104 DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (15H THIS IS A TEST ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECONE ORDER BRANCH POINTS ) 510 FORMAT (28H SECONE ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (24,40I3) 515 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0284 0285 0286 0287 0288 0289	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (15H THIS IS A TEST ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,P12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (27,40I3) 515 FORMAT (24,40I3) 516 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (/,5X,23H IMPACT PRESSURE (PSI) = ,E12.4,5X,25H 1/2 CONTACT LE 1NGTH (CH) = ,P12.4,5X,23H IMPACT DURATION (SEC) = ,E12.4,/)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0284 0285 0286 0287 0288 0289 0290	<pre>503 FORMAT (505 DATA, 150 (00574)) 503 FORMAT (505 DATA, 150 (00574)) 504 FORMAT (505 DATA, 150 (00574)) 505 FORMAT (507 DATA, 1500) 506 FORMAT (14H SIMPLE POLES ) 506 FORMAT (15H THIS IS A TEST ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (500, 000, 000, 000, 000, 000, 000, 000</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0286 0287 0288 0289 0290	503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (8E15.7) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCNL ORDER BRANCH POINTS ) 510 FORMAT (28H SECCNL ORDER BRANCH POINTS ) 510 FORMAT (5X,27H LONG.WAVE SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (24,40I3) 515 FORMAT (24,40I3) 516 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT(/,5X,23H IMPACT PRESSURE(PSI) = ,E12.4,5X,25H 1/2 CONTACT LE 1NGTH (CH) = ,F12.4,5X,23H IMPACT DURATION (SEC) = ,E12.4,/) 521 FORMAT(/,5X,18H DENSITY OF BEAM= ,F12.4,5X,17H NORM.THICKNESS= , 1F12.4,5X,15H BEAM MODULUS= ,E12.4)
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0286 0287 0288 0289 0290	<pre>503 FORMAT (500 DATA, 1500 DATA, 1400 DATA, 1400 DATA, 1500 DATA, 1400 DATA, 1400 DATA, 1400 DATA, 1500 DATA, 1400 DATA, 1500 DATA, 1400 DATA, 1400 DATA, 1400 DATA, 1500 DATA, 1400 DATA, 1500 DATA, 1400 DATA, 1500 D</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0286 0287 0288 0289 0290 0290	<pre>503 FORMAT (5X5H DATA, 15X10HCONSTANTS ,20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (15H THIS IS A TEST ) 507 FORMAT (16H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7) 521 FORMAT (17, 5X, 23H IMPACT PRESSURE(PSI)= , E12.4, 5X, 25H 1/2 CONTACT LE 1NGTH(CM)= , F12.4, 5X, 23H IMPACT DURATION (SEC)= , E12.4, /) 521 FORMAT (/, 5X, 18H DENSITY OF BEAM= , F12.4, 5X, 17H NORM.THICKNESS= , 1F12.4, 5X, 15H BEAM MODULUS= , E12.4) 600 FORMAT (1, 20X, 18HNORMALIZED DIST.= , I4) 621 FORMAT (11710.5) 631 HORMAT (15Y 200 DURATION (SEC) = 200 DURAT(11F10.5) 631 HORMAT (15Y 200 DURATED DURATION (SEC) = 200 DURAT(11F10.5) 631 HORMAT (16Y 200 DURATED DURATION (SEC) = 200 DURAT(11F10.5) 631 HORMAT (16Y 200 DURATED DURATE</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0286 0287 0288 0289 0290 0290	<pre>503 FORMAT (5X5H DATA, 15X10HCONSTANTS, 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X8HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= F10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (15H THIS IS A TEST ) 507 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 511 FORMAT (24H RAYLEIGH SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 515 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 516 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (7,5X, 23H IMPACT PRESSURE(PSI) = ,E12.4,5X,25H 1/2 CONTACT LE 1NGTH (CH) = ,F12.4,5X,23H IMPACT DURATION (SEC) = ,E12.4,/) 521 FORMAT (7,5X, 18H DENSITY OF BEAM= ,F12.4,5X,17H NORM.THICKNESS= , 1F12.4,5X,15H BEAM MODULUS= ,E12.4) 600 FORMAT (11F10.5) 621 FORMAT (11F10.5) 621 FORMAT (5X,20H WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #14 for for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #14 for WAVELEN (TIME-SEC) = ,E12.4,5X,20H WAVELEN (DIST-CM )= 1 #12 #14 for WAVELEN (DIST-CM )= 1 #14 for WAVELEN (DIST-CM )= 1 #15 #15 for WAVELEN (DIST-CM )= 1 #15 #15 for WAVELEN (DIST-CM )= 1 #15 #15 for WAVELEN (DIST</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0288 0289 0290 0290 0291 0292 0293	<pre>503 FORMAT (5X5H DATA, 15X10HCONSTATS , 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (14H SIMPLE POLES ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (15H THIS IS A TEST ) 508 FORMAT (20H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (20H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (20H LAPLACE INVERSION PARAMETER= F12.3,7H CM/SEC) 511 FORMAT (24H RAYLEIGH SPEED IN BEAM = ,F12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (450X 10HWITH STRIP) 515 FORMAT (25X,23H IMPACT PRESSURE (PSI) = ,E12.4,5X,25H 1/2 CONTACT LE 1NGTH (CH) = ,F12.4,5X,23H IMPACT DURATION (SEC) = ,E12.4,/) 521 FORMAT (/,5X,18H DENSITY OF BEAM = ,F12.4,5X,17H NORM.THICKNESS= , .1F12.4,5X,15H BEAM MODULUS= ,E12.4) 600 FORMAT (/, 20X, 18HNORMALIZED DIST.= ,I4) 620 FORMAT (11F10.5) 621 FORMAT (5X,20H WAVELEN (TIME-SEC) = ,E12.4,5X,23H MAX WAVE NO (NC 20 NDTH) = ,F12.4,5X,23H MAX FREQ NO (NON DIN) = ,F12.4,5X,23H MAX WAVE NO (NC</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0288 0289 0290 0290 0291 0292 0293	<pre>503 FORMAT (5x5H DATA, 15x10HCONSTANTS , 20x10HPARAMETERS /8E15.7) 504 FORMAT (5x5H DATA, 15x10HCONSTANTS , 20x10HPARAMETERS /8E15.7) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (14H SIMPLE POLES ) 506 FORMAT (14H SIMPLE POLES ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= P12.4) 509 FORMAT (20H SECOND ORDER BRANCH POINTS ) 510 FORMAT (20H SECOND ORDER BRANCH POINTS ) 510 FORMAT (24H RAYLEIGH SPEED IN BEAM = ,P12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (8P15.8) 515 FORMAT (25X,23H IMPACT PRESSURE (PSI) = ,E12.4,5X,25H 1/2 CONTACT LE 1NGTH (CM) = ,P12.4,5X,23H IMPACT DURATION (SEC) = ,E12.4,/) 521 FORMAT (1,5X,18H DENSITY OF BEAM= ,F12.4,5X,17H NORM.THICKNESS= , 1F12.4,5X,15H BEAM MODULUS= ,E12.4) 600 FORMAT (1, 20X,18HNORMALIZED DIST.= ,I4) 620 FORMAT (11F10.5) 621 FORMAT (5X,23H MAX FREQ NO(NON DIN) = ,F12.4,5X,23H MAX WAVE NO(NC 2N DIM) = ,F12.4,7)</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0288 0289 0290 0290 0291 0292 0293	<pre>503 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 505 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (18H SIMPLE POLES ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (24H RAYLEIGH SPEED IN BEAM = , P12.3, 7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (3615.8) 514 FORMAT (50X 10HWITH STRIP) 515 FORMAT (27, 40I3) 516 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (7, 5X, 23H IMPACT PRESSURE(PSI) = , E12.4, 5X, 25H 1/2 CONTACT LE 1NGTH (CM)= , P12.4, 5X, 23H IMPACT DURATION (SEC) = , E12.4, /) 521 FORMAT (7, 5X, 18H DENSITY OF BEAM= , F12.4, 5X, 17H NORM.THICKNESS= , .1F12.4, 5X, 15H BEAM MODULUS= , E12.4) 600 FORMAT (1, 20X, 18HNORMALIZED DIST.= , I4) 620 FORMAT (11F10.5) 621 FORMAT (5X, 20H WAVELEN (TIME-SEC) = , E12.4, 5X, 20H WAVELEN (DIST-CM )= 1, F12.4, /, 5X, 23H MAX FREQ NO (NON DIN) = , F12.4, 5X, 23H MAX WAVE NO (NC 2N DIM) = , P12.4, /) 630 FORMAT (30X, 16H DISPLACEMENT U1,/) 631 FORMAT (30X, 16H DISPLACEMENT U1,/)</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0288 0289 0290 0290 0290 0291 0292 0293	<pre>503 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (14H SIMPLE POLES ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= F12.4) 509 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 510 FORMAT (28H SECCND ORDER BRANCH POINTS ) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (50X 10HWITH STRIP) 515 FORMAT (16H MAXIMUM VALUE= E15.7) 520 FORMAT (7.5X, 23H IMPACT PRESSURE(PSI) = , E12.4, 5X, 25H 1/2 CONTACT LE 1NGTH (CH) = , F12.4, 5X, 23H IMPACT DURATION (SEC) = , E12.4, /) 521 FORMAT (/, 5X, 18H DENSITY OF BEAM= , F12.4, 5X, 17H NORM.THICKNESS= , .1F12.4, 5X, 15H BEAM MODULUS= , E12.4) 600 FORMAT(/, 20X, 18HNORMALIZED DIST.= , I4) 600 FORMAT(/, 20X, 18HNORMALIZED DIST.= , I4) 600 FORMAT(/, 20X, 18HNORMALIZED DIST.= , I4) 600 FORMAT(/, 5X, 23H MAX FREQ NO (NON DIM) = , F12.4, 5X, 23H MAX WAVE NO (NC 2N DIM) = , F12.4, /) 631 FORMAT (30X, 16H DISPLACEMENT U1, /) 631 FORMAT (30X, 16H DISPLACEMENT U3, /) 632 FORMAT (30X, 16H DISPLACEMENT U3, /) 633 FORMAT (30X, 16H DISPLACEMENT U3, /) 634 FORMAT (30X, 16H DISPLACEMENT U3, /) 635 FORMAT (30X, 16H DISPLACEMENT U3, /) 637 FORMAT (30X, 16H DISPLACEMENT U3, /) 638 FORMAT (30X, 16H DISPLACEMENT U3, /) 639 FORMAT (30X, 16H DISPLACEMENT U3, /) 630 FORMAT (30X, 16H DISPLACEMENT U3, /) 631 FORMAT (30X, 16H DISPLACEMENT U3, /) 632 FORMAT (30X, 16H DISPLACEMENT U3, /) 633 FORMAT (30X, 16H DISPLACEMENT U3, /) 634 FORMAT (30X, 16H DISPLACEMENT U3, /) 635 FORMAT (30X, 16H DISPLACEMENT U3, /) 634 FORMAT (30X, 16H DISPLACEMENT U3, /) 635 FORMAT (30X, 16H DISPLACEMENT U3, /) 634 FORMAT (30X</pre>
0275 0276 0277 0278 0279 0280 0281 0282 0283 0284 0285 0286 0287 0286 0287 0288 0289 0290 0290 0291 0292 0293	<pre>503 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X5H DATA, 15X10HCONSTANTS , 20X10HPARAMETERS /8E15.7) 504 FORMAT (5X6HNSTRESS= I3,5X4HNX3= I4,5X4HDX3= P10.4,/) 505 FORMAT (14H SIMPLE POLES ) 506 FORMAT (15H THIS IS A TEST ) 507 FORMAT (15H THIS IS A TEST ) 508 FORMAT (30H LAPLACE INVERSION PARAMETER= P12.4) 509 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (28H SECOND ORDER BRANCH POINTS ) 510 FORMAT (24H RAYLEIGH SPEED IN BEAM = ,P12.3,7H CM/SEC) 511 FORMAT (14H DISPLACEMENTS I4) 512 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 513 FORMAT (24H RAYLEIGH SPEED CS/CR*I ) 514 FORMAT (45X, 23H IMPACT PRESSURE(PSI) = ,E12.4,5X,25H 1/2 CONTACT LE 1NGTH (CM) = ,P12.4,5X,23H IMPACT DURATION (SEC) = ,E12.4,/) 521 FORMAT (/,5X,23H IMPACT PRESSURE(PSI) = ,E12.4,5X,17H NORM.THICKNESS= , IP12.4,5X,15H BEAM MODULUS= ,E12.4) 600 FORMAT(/, 20X,18H DENSITY OF BEAM= ,P12.4,5X,17H NORM.THICKNESS= , IP12.4,5X,15H BEAM MODULUS= ,E12.4) 620 FORMAT(/, 20X,18HNORMALIZED DIST.= ,I4) 620 FORMAT(/, 20X,18HNORMALIZED DIST.= ,I4) 621 FORMAT (5X,23H MAX FREQ NO(NON DIN) = ,F12.4,5X,23H MAX WAVE NO(NC 2N DIM) = ,P12.4,/) 631 FORMAT (30X,11H STRESS T33,/) 633 FORMAT (30X,11H STRESS T33,/) 633 FORMAT (30X,11H STRESS T33,/) 634 FORMAT (30X,11H STRESS T33,/) 63</pre>

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## ORTRAN IV G LEVEL 21

0298	634 FORMAT (30X, 11H STRESS T13,/)
0299	635 FORMAT (30X,41H TEST-DISPL.OF BEAR OR DESTING TO A DAY 28 L / 20X
0300	640 PORMAT (20X, 14H>> X1, $DX = P(2, 4, 7, 20X, 2H) = P(2, 4, 7, 20X, 2H)$
I	1 2H 1./,20X,2H V./,20X,2H V./,20X,9HTLHE,DT= ,212.4,//)
0 30 1	650 FORMAT(10H INAG PART)
0.302	680 FORMAT (181)
0303	690 FORMAT (/, 20X, 17H FRINGE ORDER MAP, /, 20X, 31H SQRT ((TTT-135) * 2141*
	1T13*T13))
0304	710 FORMAT( 5X,6H VEL= ,F12.4,5X,5H TO= ,F12.4,5X,4H A= ,F12.4,5X,
	15H PO= ,F12.4,/)
0305	203 STOP
0306	END

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0001	SUBROUTINE CALCUL (NPOLE)
0002	COMMON ZMMCZ D. DK1
0003	COMMON /NC/DK2_PG1.TO_C11_C13_C33_C55_RHO_RO_R_PS_NSTRID_AO
0004	CONFIET A1 B2
0005	COMPTER GO.GO1.HO.HO1 G10 G11 H10 H11
0006	
0007	COMPLEX DEL DEL DEL DEL SE SE CEL CO SE DI CI MERINE
0008	CONTLEX DRIPDREFEIPEZIGIJSZICIJCZISLIBICID JEG
0009	DT = 3 44150265
0010	ST = CNDTY(0 - 1)
0011	b = c 33 * c 55
0012	B = (C33 + (RHO + DK) + DK) + (C11 + DK1 + DK1) + (C55 + (DHO + DK) + DK) - (C55 + DK1 + DK1) + (C55 + (DHO + DK) + DK) + (C55 + (DHO + DK) + DK) + (C55 + (DHO + DK) + (DK) +
***	1D81*D81*(C13+C55)**2
0013	C = (RHO * D K 2 + D K 2 + D K 1 + D K 1 + D K 1) + (RHO * D K 2 + D K 2 + C 5 5 + D K 1 + D K 1)
0014	BS = 1, D0 + B + B - 1, D0 + 4, + 8 + C
0015	D = CLSORT(BS)
0016	$P_{1} = .5/A + (-B+D)$
0017	P2=C/P1/A
0018	P1 = CSORT(P1)
0019	IF $(REAL(P1), LT, 0, 0, AND, NPOLE, NE, 2)$ $P1 = -P1$
0020	P2=CSQRT(P2)
0021	IF (REAL(P2).LT.O.O.AND.NFOLE.NE.2) $P2=-P2$
0022	S1 = -SI/DK1 /P1/(C13+C55) * (RHO*DK2*DK2-C11*DK1*DK1+C55*P1*P1)
0023	52= -SI/DK1 /P2/ (C13+C55) * (RHO*DK2*DK2-C11*DK1*DK1+C55*P2*P2)
0024	IF (NFOLE.EQ.2) GO TO 201
	C*** PORCING FUNCTION
0025	FG= PI*FG1*(1.+CEXP(-SI*DK2*T0))/(PI*PI-DK2*DK2*T0*T0)*
	14./ (DK1*A0) **2* (CSIN (DK1*A0) /DK1-A0*CCOS (DK1*A0) )
0026	201 IF (NSTRIP.EQ.1) GO TO 202
0027	D= (SI*DK1*S1-P1)*(SI*DK1*C13-P2*C33*S2)-(SI*DK1*S2-P2)*(SI*DK1*
	1C13-P1*C33*S1)
0028	IF (NPOLE.EQ.2) RETURN
0029	206  C1 = FG/D * (SI * D K1 * S2 + P2)
0030	C2 = FG/D*(P1-SI*DK1*S1)
0031	GO TC 203
0032	202 CONTINUE
0022	C*** MATRIX FOR STRIP PROBLEM
0033	B 1=W*W*(ES*DK1*DK1-RO*DK2*DK2) *DK1*DK1/12.0-RO*DK2*DK2 B 1= H+D 1
0034	C (= N+C) 20Ve (SC+0K1+0K1, DO+DK0+DK0)
0035	$DZ = \pi \tau (LO + DK + DK + DKZ + DKZ)$ $C 10 = C 55 + (C + DK + C + DKZ + DKZ)$
0037	$u_1 u = c_5 \varepsilon_1 (c_1 + c_1 + c_2 + c_1)$
0038	$\frac{1}{1} = \frac{1}{1} = \frac{1}$
0039	$H_{1} = h_{2} + (1 + 0 + 0 + 1 + 0 + 1 + 0 + 1 + 0 + 1 + 0 + 0$
0040	$\frac{1}{2} = \frac{1}{2} = \frac{1}$
0041	90(01-01-01-00+00+00-00) H0=-/ST*DE1*01-0-00+00-00
0042	$= G \hat{\Omega}^{+} = - S \hat{\Gamma} * D \hat{X}^{+} C \hat{\Gamma} \hat{\Omega}^{+} \hat{\Sigma}^{+} \hat{\Omega} \hat{\Omega}^{+} \hat{\Omega}^{$
0043	HO 1 = ST = DRT + ST = T = DT = ST
0044	$H_1 = H_10 + H_11$
0045	G1=G10+G11
C046	G=G0+G01
0047	H=HO+HO1
0048	$D = G10 \times H0 = G0 \times H10 + (H0 \times G11 + H01 \times G10 - G0 \times H11 - G01 \times H10) \times (H01 + G11 - H11 \times G01)$
	1)
0049	IF (NPOLE.EQ.2) RETURN

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FORTRAN IV G LEVEL 21

0050		C1= -FG/D+H1	
0051		C2=FG/D*G1	_
0052	203	WRITE (2) P1, P2, C1, C2, S1, S2, DK1, DK	2
0053		RETUFN	
0054		END	

ELASTIC CONSTANTS C11,C22,C33,C44,C55,C66,C12,C13,C32, 0.2456E 08 0.1170E 07 0.1374E 07 0.3552E 06 0.2310E 07 0.3552E 06 0.4000E 06 0.1986E 07 0.4558F 06 1.4400 DENSITY OF PLATE GM/CC--FIBER LAYUP ANGLE-- 15.0000 NSTRESS= 1 NX 3= 1 DX3 = 1.000087.3169* A= 1.3342* FO= 1042938.7500 VEL= 300.0000 T0= WAVELEN (TIME-SEC) = 0.3500E-05WAVELEN (DIST-CM ) = 0.6667 MAX WAVE NO (NON DIN) = 9.4248 MAX FREQ NO(NON DIN) = 13.7654 $C11 = 0.2442E \ 08 \ C33 = 0.1196E \ 07 \ C55 = 0.2310E \ 07 \ C13 = 0.1830E \ 07$ LCNG.SPEED = 0.1081E 07SHEAR SPEED = 0.3326E 0612 **RAYLEIGH SPEED = 0.3020E \ 06 \ CR/CS = 0.90800** 0.5000 2.7000 BEAM MODULUS= 0.1124E 08 DENSITY OF BEAM= NORM.THICKNESS= LONG. WAVE SPEED IN BEAM = 535757.750 CM/SEC SECOND ORDER ERANCH POINTS

+ 45 -

0.1997043E 02 0.0 0.0 0.2266004E 01 LAPLACE INVERSION PARAMETER= 0.5948

#### WITH STRIP

* This program has test cards (#51, 52) to override the Hertz calculation  $T0=3510^{-6}$  s A=1 cm.

STRESS T33



n. Û Ö Û 3. Ô. 14 12 Ō. Û Ω 27 23 15 - 1 41 36 24 - 1 54 49 34 17 -3 - 3 -2 -1 Û -1 67 61 44 23 -3 Ø Û Û - 2 ~5 -3 78 71 52 29 12 -2 -5 -6 87 80 59 34 16 -5 -4 -2 -1 - 4 -6 -6 -4 -3 -6 94 86 64 39 20 - 3 n -7 -7 -6 -5 -3 - 1 98 90 68 42 23 10 -1 -6 -7 -7 -6 -5 -3 -2 100 91 70 44 25 13 -6 -3 -5 -5 -4 -2 98 91 70 45 26 15 -6 -7 -7 -7 n -6 -4 -3 -1 95 87 68 44 27 16 -1 -3 +5 -6 -7 -7 -7 -7 -6 -5 -3 89 82 64 43 27 17 10 -1 - 3 -5 - 6 -7 -7 -6 -5 -4 - 2 -7 80 74 59 40 26 17 11 -6 -2 -7 -7 -5 -4 -6 -6 70 65 52 36 25 17 12 - 3 -4 ~6 -7 -7 -4 -3 -1 57 53 43 31 22 16 12 -5 -6 -7 Э - 1 -3 ~4 -6 -5 -3 -2 -4 -5 -6 -7 -7 -7 43 41 34 26 19 15 ß -7 -6 -5 -2 -7 -7 -4 -2 -3 -5 -6 28 27 24 19 16 13 12 10 -7 -6 - 4 - 3 -1 -7 -7 13 13 13 12 12 11 11 10 -4 -6 -7 -7 -6 -5 -3 - 1 -7 -3 - 11 -5 -6 9 10 -2 -7 -7 -7 -6 -5 -4 -5 -6 -1 -2 - 4 -4 -3 -5 -7 -7 -7 -6 -4 - 3 -1 -3 -7 -6 -7 - 6 -5 - 3 -2 -6 -7 -7 -7 -7 -6 ~5 -3 -1 б -3 -4 -7 - 3 -6 -4 -7 -5 -6 -7 -7 -4 -3 -2 -7 -7 -6 — U -4 ~ 5 ~6 -7 -7 ~7 ü, -4 -2 -6 -6 -- 6 - 5 -5 -2 -3 -4 -6 -6 -7 -7 -7 -6 -2 -4 -6 -6 -5 -5 -6 -7 -7 -7 З -1 -3 -4 - 3 - 3 -7 -7 0 -1 -2 -4 -5-6 ш -2 -1 -5 -5 - 4 -- U - 4 0 -1 -2 -3 -5 -6 -7 - 1 -3 -3 -1 -1 -2 -3 - 3 3 2 -2 -3 -4 -5 9 10 - 3 -3 -2 -5 -4 -4 - 3 -3 - 7 - 3 - 3 - 7

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X3= 0.0 DISPLACEMENTS 3 MAXIMUM VALUE= -0.7104896E 00

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	1	NORMATIZED	DIST. =	n						-
0.00050	0.03979	0.14142	0 27084	<u>0 / 118/</u>	0 54907	0 67705	0 70744	0 07700	0 04077	0.00577
1.00000	0.98948	0.95134	0 99048	0.90461	0.70005	0.07703	0.10714 0.0083	0.00000	0.94377	0.98577
-0.04267	-0.07263	-0 07276	-0.07738	-0.060407	-0.06257	0 0 20 20 20 20 20 20 20 20 20 20 20 20	0.43933	0.20094	0.13502	0.01142
THAC DART	0.01203	9.07270	~0.07730	-0.00042	-0.00357	-0.03010	-0.05201	-0.01223	-0.05377	
0 00000	-0.0000	0 00000	0.00000	0 00000	0 00004	0 00004				
0.00000	-0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00002	0,00001	0.00002	0.00003
	` N	NORMALIZED	DIST.=	1						-
0.00052	0.03504	0.12364	0.23925	0.36748	0.49373	0.61244	0.71537	0 90093	0 96363	0.00001
0.91968	0.91198	0.87880	0.82442	0.74692	0.65225	0 53970	0 61292	0,00000	0.00.002	0.01004
-0.03628	-0.06768	-0.07048	-0.07543	-0.06060	-0.05251	-0.02075	-0 05050	-0.01540	0.13423	0.01894
THAG PART			0101243	0.00000	0.00201	-4.43243	-0.00009	-0.01542	-0.04908	
0.00000	-0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00002	0.00001	0.00002	0.00003
										••••••
	Ň	ORMALIZED	DIST.=	2						
0.00046	0.02177	0.07726	0.15621	0.24997	0.34647	0.44004	0.52356	0.59467	0.64909	0.68662
0.70461	0.70446	0.68451	0.64749	0.59235	0.52308	0.43886	0.34489	0.24037	0.13188	0.03829
-0.01809	-0,05320	-0.06323	-0.06962	-0.06054	-0,06012	-0.04359	-0.04736	-0.02317	-0.04079	0100023
IMAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00002	0.00002
	N		DTST =	7						
0.00028	0.00689	0.02688	0.06236	0 11326	0 17235	0 22827	0 20226	0 34664	0 20024	0 40373
0.44479	0.45370	0 44958	0.00250	0.11520	0.26662	0.23427	0.27330	0.34651	0.39036	0.42373
0.00870	-0.03042	-0.00000	-0 06009	-0.05957	-0 06702	0.31700	0.20100	0.19681	0.12822	0.06182
THAG PART	0103042	0+04000	-0.00009	-0.03037	-0.05702	-0.04745	-0.04482	-0.03114	-0.03385	
0.00000	0 00000	0 00000	0 00000	0 00000	0.00000	0 00000				
		0.00000	0.00000	0.00000	0.00000	0.00000	0.0001	0.00001	0.00001	0.00001
	N	ORMALIZED	DIST.=	4						
0.00030	0.00089	0.00200	0.00749	0.02457	0.05280	0.08844	0.12718	0.16551	0.20047	0.23014
0.25300	0.26837	0.27564	0.27493	0.26619	0.25006	0.22685	0.19759	0.16280	0.12382	0 08191
0.03868	-0.00176	-0.03008	-0.04672	-0.05288	-0.05368	-0.04925	-0.04457	-0.03642	-0.03159	0.00101
IMAG PART							0000000	VIV.0042	0+00103	
0.00000	0.00000	-0.00000	-0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001
	**		ртол —	<i>r</i>						
0 00022	0.0000	-0 00067		5						
0.00032 0.13309	0.16100	-0.00267	-0.01052	-0.01476	-0.00909	0.00649	0.02920	0,05590	0.08350	0.10982
0.13430 0 04544	0.10198	0.00000	0.37462	0.1//71	0.17551	0.16799	0.15576	0.13895	0.11848	0.09467
V.V0340	0.02911	-0.00428	-0.02892	-0.04250	-0.04904	-0.04829	-0.04595	-0.03865	-0.03469	
LBAG PART	A 00000		A							
0.00000	0.00000	-0.00000	-0.00000	-0.00000	-0.00000	-0.00000	0.00000	0.00000	0.00000	0.00000
	•									

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STRESS T11

0.3333 --->> X1, DX= V 0.1750E-05 TIME, DT=

Û Ó. Û. **n** Ũ Ú 0 --2 5 10 Q 8 18 16 -5 -1 Ô -2 - 1 -4 0 12 26 24 - 15 2 -1 -4 -4 -3 4 19 34 30 -5 -6 -6 -5 -2 6 11 27 43 37 23 11 2 -2 Û. 2 -4 -8 -9 -9 -9 -7 -4 -1 15 20 37 53 45 27 12 n 2 -6-10-12-13-12-11 -9 -6 -3 25 30 47 63 53 33 15 3 -7-13-16-17-16-15-13-11 -8 -5 -2 35 40 57 73 61 39 18 5 -6-14-19-20-20-19-17-15-13-10 -7 -4 -1 45 50 67 82 69 45 23 9 -4-13-20-23-24-24-22-20-17-15-12 -9 -6 -3 0 54 59 75 89 76 51 28 61 66 82 95 82 57 33 14 0-11-19-24-26-27-27-25-22-19-16-14-11 -8 -5 -2 ñ 68 72 86 98 85 61 38 19 4 -7-16-23-27-29-30-29-27-24-21-18-15-13-10 -7 -4 -1 72 76 89100 87 64 43 24 9 -2-12-19-25-29-31-32-31-29-26-23-20-17-14-11 -8 -5 -3 - 1 75 78 89 98 87 66 47 29 15 3 -6-15-21-26-30-32-33-33-31-28-25-22-19-16-13-10 -7 -4 -2 0 - 1 - 175 78 87 94 84 66 49 34 20 9 0 -9-16-22-27-31-33-34-34-33-30-27-24-21-18-15-12 -9 -6 -3 -1 0 - 1 - 1 74 76 83 88 79 65 50 37 26 15 6 -2-10-16-22-27-31-34-35-35-34-32-29-26-23-19-16-13-10 -8 -5 -3 -1 -1 -1 71 72 76 79 73 61 50 40 30 21 13 4 -2-10-16-22-27-31-34-36-36-35-33-31-28-24-21-18-15-12 -9 -7 -4 -3 -2 66 66 68 68 64 56 49 41 34 26 19 12 4 -2 -9-15-21-26-31-34-36-36-36-35-32-29-26-23-19-16-14-11 -8 -6 -4 59 59 58 56 53 50 46 42 37 31 25 19 12 5 -1 +7-14-20-25-30-33-36-37-37-36-34-31-28-24-21-18-15-13-10 -8 51 50 48 45 43 43 42 41 38 35 30 25 19 13 7 0 -6-12-18-24-29-33-35-37-37-37-35-32-29-26-23-20-17-14-12 39 39 39 38 38 38 38 39 39 38 35 31 26 21 15 8 2 -4-11-17-23-28-32-35-37-38-38-36-34-31-28-25-22-19-16-25 26 28 30 32 34 35 37 38 39 39 36 33 28 22 17 10 4 -2 -9-15-21-26-31-34-37-38-38-37-36-33-30-27-24-21-15 16 18 22 25 29 31 34 36 38 40 40 39 35 30 25 19 12 6 0 -7-13-19-25-30-34-37-39-39-39-37-35-32-29-26-8 10 13 17 22 27 30 33 35 37 39 40 40 38 33 28 21 15 8 1 -5-11-18-24-29-33-36-39-40-40-38-36-34-30-7 11 15 19 24 29 32 35 37 38 39 40 39 35 30 24 18 11 4 -2 -9-16-22-27-32-36-38-40-40-39-37-34-2 4 8 13 18 22 27 31 34 36 38 39 39 39 36 32 26 20 14 7 0 -6-12-19-25-30-34-37-39-39-39-37--1 -1 - 4 6 10 15 20 25 29 33 35 36 38 39 39 37 34 29 22 16 10 4 -2 -9-15-21-27-31-34-37-38-38-.3 -4 -4 -2**1** 8 13 17 22 27 31 34 36 37 38 39 38 36 32 26 19 13 7 1 -5-11-17-23-28-32-35-36-1 5 -6 -6 -4 -1 -4 -3 -4 -3 0 2 6 11 16 21 25 29 33 36 38 39 39 39 37 34 29 23 16 9 3 -2 -8-14-20-25-29-32--8 -7 -5 -5 -6 -9-11-10 -7 -4 -2 -1 1 4 8 14 19 25 29 32 35 37 39 40 40 39 36 32 26 19 12 6 0 -5-12-18-23-27-

 X3= 0.0 DISPLACEMENTS 4 MAXIMUM VALUE= -0.1169061E 01

	1	NORMALIZED	DIST.=	0						,
0.00258	0.00591	-0.02645	-0.05231	-0.04372	-0.00204	0.06720	0.15474	0.25280	0.35369	0.45160
0.54124	0.61882	0.68126	0.72641	0.75286	0.75988	0.74715	0.71530	0.66481	0.59890	0.51992
0.39153	0.25986	0.15272	0.07511	0.01861	-0.01623	-0.04614	-0.05638	-0.08178	-0-05544	
IMAG PART								-,,		
0.00000	0.00000	0.00000	-0.00000	-0.00000	-0.00000	0.00000	0.00000	0.00000	0.00001	0.00001
	1	ORMALIZED	DIST.=	1						
0.00200	0.00707	-0.00660	-0.01783	-0.00073	0.04631	0.11913	0.20892	0.30838	0.40951	0.50684
0.59461	0.66947	0.72778	0.76810	0.78838	0.78875	0.76829	0.72861	0.66949	0.59492	0.50860
0.39149	0.26578	0.16154	0.08150	0.02557	-0.01399	-0.04097	-0.05868	-0.07437	-0.06856	J. 30007
IMAG PART								•••••	0100000	
0.00000	0.00000	0.00000	-0.00000	-0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00002
	N	ORMALIZED	DIST.=	2						
0.00095	0.01745	0.05203	0.08323	0.12706	0.19085	0.27497	0.37173	0.47550	0.57739	0.67297
0.75508	0.82171	0.86766	0.89339	0.89515	0.87552	0.83186	0.76861	0,68362	0.58354	0.48166
0.39022	0.28142	0.18630	0.10048	0.04569	-0.00618	-0.02674	-0.06290	-0.05665	-0.09664	
INAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00002
	N	ORMALIZED	DIST.=	3						
0.00057	0.03187	0.10966	0.18732	0.26129	0.34028	0.43188	0.53084	0.63438	0.73316	0.82397
0.89837	0.95550	0.98870	1.00000	0.98414	0,94583	0.88079	0.79607	0.68776	0.56538	0.45448
0.38626	0.30196	0.22148	0.13213	0.07587	0.01127	-0.00827	-0.06039	-0.04181	-0.11182	
IMAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00002	0.00003
	N	ORNALIZED	DIST.=	4						
0.00019	0.01996	0.08833	0.16952	0.24197	0.30671	0.37709	0.45380	0.53712	0.61997	0.69932
0.76750	0.82278	0.85892	0.87669	0.87127	0,84603	0.79712	0.73005	0.64180	0.53914	0.43862
0.38149	0.32254	0.25902	0.17532	0.11222	0.04213	0.01049	-0.04408	-0.03756	-0.10398	
IMAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00002	0.00002
	N	CRMALIZED	CIST.=	5						
0.00069	0.00496	0.04046	0.09727	0.15250	0.19436	0.23295	0.27765	0.33095	0.39123	0.45436
0.51583	0.57109	0.61642	0.64875	0.66607	0.66710	0.65118	0,61852	0.56999	0.50604	0.43337
0.38097	0.34064	0,29211	0.22508	0.15284	0.08553	0.03096	-0.01399	-0.04177	-0.07016	
INAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00001	0.00002

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#### STRESS T13

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### --->> X1, DX= 0.3333 v 0.1750E-05 TIME.DT=

û Э Ó **O** Ð 0 0 Ω 0 10 15 10 0 - 2 - 2 - 1Ö Ũ. Ō 0 20 31 24 7 -2 -6 -5 -3 -1 3 -6 -9 -8 -5 -2 0 30 48 41 19 0 39 63 56 31 12 -1 -9 - 12 - 11 -7 -30 47 76 70 43 22 6 -4-11-14-13-10 -5 -1 Ω 0 52 86 80 52 30 14 2 -6-11-15-14-12 -7 -2 G 0 57 93 88 59 37 20 0 -6-12-14-15-13 -9 -4 Ô **î** 0 59 98 93 64 41 25 14 5 0 -6-11-14-15-14-11 -6 -1 -1 Ð 0 61100 95 66 44 28 18 10 4 -1 -6-10-13-15-15-12 -8 -3 -1 σ 0 60 99 95 67 45 30 21 14 8 3 0 -5 -9-12-15-15-13-10 -5 -1 0 - 1- 1 0 58 96 92 65 45 31 22 16 12 7 4 0 -4 -8-11-14-15-14-11 -7 -2 1 0 -1 -1 0 54 90 87 62 43 30 23 17 14 10 8 4 1 -2 -6-10-13-15-14-12 -8 -4 0 0 50 82 80 57 40 29 22 18 15 12 10 8 5 2 -1 -5 -9-12-14-14-13-10 -5 -1 -2 -1 0 43 72 70 51 36 27 21 17 15 14 12 10 8 6 3 0 -4 -8-11-13-14-14-11 -7 -2 0 0 - 1 - 2 - 10 36 60 59 43 31 24 19 17 15 14 13 12 11 9 7 4 0 -2 -6-10-12-14-14-12 -8 -4 -2 -2 0 28 47 46 34 26 20 17 15 14 14 13 13 12 11 10 7 5 2 -1 -5 -8-12-13-14-13-10 -6 -1 - 1 0 20 33 33 25 19 16 14 13 13 13 13 13 13 12 12 10 8 6 3 0 -4 -7-10-13-14-13-11 -7 -3 0 0 10 18 18 15 13 12 11 11 12 12 13 13 13 13 13 12 11 9 7 4 0 -2 -6 -9-12-13-13-12 -8 -4 0 З 2 3 5 6 9 10 11 12 12 13 13 13 13 13 12 11 10 5 2 -1 -5 -8-11-13-14-12-10 -6 -2 0 -6 -9 -9 -5 -1 2 9 10 11 12 13 13 13 13 13 12 10 8 6 3 0 -4 -7-10-13-14-13-11 -7 -3 0 0 -7-12-15-14-10 -4 0 3 6 9 10 11 12 12 13 13 13 13 12 11 9 7 4 0 -3 -6 -9-12-13-13-12 -9 -5 0 -5-11-15-17-16-13 -7 -1 2 5 9 10 11 12 13 13 13 13 12 11 9 7 4 1 -1 -5 -8-11-13-13-12-10 0 -3 -7-11-15-18-18-15 -9 -3 2 5 - 8 9 10 11 12 13 13 13 12 11 10 8 5 2 0 -4 -7-10-12-13-13-0 -2 -5 -8-11-14-17-18-16-12 -6 0 5 7 9 10 11 11 12 12 13 12 12 11 9 0 -2 -6 -9-11-13-9 10 11 12 12 12 12 12 11 0 - 1 - 2 - 4 - 7 - 10 - 13 - 16 - 17 - 17 - 14 - 8 - 2- 3 2 - 1 - 4 - 8 - 10 -8 9 9 9 10 11 12 12 13 13 12 11 10 0 - 1 - 2 - 4 - 6 - 9 - 12 - 15 - 17 - 17 - 15 - 10 - 43 0 -3 -6 0 0 -2 -3 -5 -7-10-13-16-17-16-12 -7 0 5 8 10 9 9 10 11 13 13 13 13 13 13 12 11 0 -2 0 0 0 -2 -4 -7-10-12-15-16-15-13 -9 -3 3 8 10 10 10 10 10 12 13 14 14 13 12 11 10 1 2 1 0 -1 -2 -5 -7 -9-12-15-16-15-11 -6 0 4 9 11 11 10 10 10 12 13 14 14 13 13 11 10 0 - 1 - 1

Ω   X3= 0.0 DISPLACEMENTS 5 MAXIMUM VALUE= ~C.4623035E 00

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	ļ	NORMALIZED	DIST.=	0						
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	-0.00000	-0.00000	-0.00000	-0.00000
-0.00000	-0.00000	+0.00000	-0.00000	-0.00000	-0.00000	-0.00000	0.00000	0.00000	0.00000	0.00000
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	-0.00000	-0.00000	-0.00000	
IMAG PART		-			• • •					
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000
	1	NORMALIZED	DIST.=	1						
-0.00043	0.02068	0.10175	0.20639	0.30728	0.39631	0.47093	0.52964	0.57264	0.59915	0.61001
0.60465	0.58452	0.54925	0.50110	0.43993	0.36875	0.28784	0.20073	0.10784	0.01335	-0.06204
-0.07283	-0.05896	-0.03786	-0.02592	-0.01095	-0.00946	0.00347	-0.00564	0.01473	-0.01847	
INAG PART										
0.00000	-0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00001	0.00002
	· 1	ORMALIZED	DIST.=	2						
-0.00013	0.03502	0.15215	0.31697	0.48494	0.63521	0.76207	0.86189	0.93521	0.98069	1.00000
0.99229	0.96012	0.90298	0.82454	0.72472	0.60842	0.47603	0.33347	0.18134	0.02696	-0.09592
-0.12971	-0.11354	-0.07743	-0.05318	-0.02567	-0.01857	0.00226	-0.00719	0.01974	-0.01810	
INAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00002	0.00002	0.00002	0.00003
		-		·		-				
	1	NORMALIZED	DIST.=	3 .						
-0.00001	0.02103	0.10073	0.24333	0.41035	0.56703	0.70144	0.80789	0.88641	0.93621	0.95909
0.95511	0.92661	0.87394	0.80010	0.70587	0.59526	0.46931	0.33299	0.18781	0.03946	-0.09051
-0.15673	-0.15637	-0.11853	-0.08225	-0.04707	-0.02788	-0.00646	-0.00410	0.01312	-0.00197	
IMAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00002	0.00002	0.00002	0.00003
•										
	1	NOR MALIZED	DIST.=	4						
-0.00004	-0.00297	0.00997	0.07754	0.19345	0.31982	0.43364	0.52662	0.59598	0.64235	0.66643
0.67025	0.65479	0.62217	0.57325	0.51049	0.43492	0.34924	0.25488	0.15515	0.05108	-0.05597
-0.14683	-0.17773	-0.15636	-0.11319	-0.07501	-0.04060	-0.02147	-0.00133	0.00071	0.01812	
IMAG PART										
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00002	0.00002
	N	<b>ORMALIZED</b>	DIST.=	5				•		
0.00030	-0.00548	-0.02595	-0.02357	0.03348	0.12663	0.22238	0.30661	0.37192	0.41857	0,44612
0.45759	0.45334	0.43645	0.40685	0.36774	0.31856	0.26281	0.19987	0.13350	0.06310	-0.01262
-0.10517	-0.16989	-0.18071	-0.14489	-0.10571	-0.06167	-0.03831	-0.00752	-0.00720	0.02622	
IMAG PART										
0.00000	0.00000	-0.00000	-0.00000	0.00000	0.00000	0.00001	0.00001	0.00001	0.00001	0,00002
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	-									

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FRINGE ORDER MAP SQBT((T11-T33)**2+4.0*T13*T13)

																													-	-	-	-	÷	-
0	0	0	0	0	0	0	0	0	0	0	0	0.	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	2	2	3	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
11	11	12	12	8	4	:2	1	0	0	0	0	0	0	0	0	0	0	Q	0	0	0	0.	0	0	0	0	0	0	0	0	0	0	0	0
21	23	25	24	17	10	6	4	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
29	33	38	37	27	16	10	8	7	4	2	0	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
33	40	50	50	37	22	12	8	10	9	7	4	1	1	2	2	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
34	45	60	62	47	28	14	6	8	11	12	10	7	3	1	2	2	2	, <b>2</b>	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0
32	47	68	73	56	35	18	5	5	10	13	14	13	10	6	2	1	2	2	2	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0
28	48	74	81	64	41	22	8	2	8	13	15	16	15	12	8	- 4	2	2	2	2	1	1	1	2	2	1	1	1	0	0	0	0	0	0
21	48	79	89	71	47	27	12	5	9	13	16	17	18	17	14	11	7	3	2	2	2	2	1	1	1	2	2	2	1	1	1	1	0	0
14	48	83	94	76	52	31	16	9	11	14	17	18	19	19	18	16	13	9	5	3	2	2	2	1	1	0	1	1	2	2	2	2	1	1
6	47	85	98	81	56	35	19	11	12	16	19	20	21	21	21	20	18	15	11	7	4	2	2	2	1	1	0	0	1	1	1	1.	. 1	2:
1	47	85	100	83	59	38	22	13	13	17	20	22	23	23	23	22	21	20	17	13	9	6	- 4	2	1	1	1	1	0	0	1	1	1	1.
10	47	84	99	84	62	41	24	14	13	16	20	23	25	25	25	25	24	23	21	19	15	12	8	5	3	2	1	1	1	1	0	1	1	1
18	47	82	97	84	63	43	27	16	12	15	19	23	25	27	27	27	26	25	24	23	20	17	14	10	.7	4	2	1	0	1	1	1	0	1
26	48	78	92	81	62	45	30	18	12	13	17	21	24	27	28	29	28	28	27	25	24	22	19	16	12	9	6	4	2	0	1	2	2	1
33	48	73	86	77	61	45	32	21	14	11	14	18	22	25	28	29	30	30	29	28	27	25	23	21	17	14	10	8	5	3	1	0	2	2
39	49	67	78	71	58	46	34	24	16	11	11	14	18	22	26	28	30	31	31	30	29	28	26	24	22	19	16	12	9	7	4	2	0	1
44	50	61	69	64	54	44	35	27	20	14	11	11	14	18	22	26	29	30	31	31	31	30	29	27	26	23	21	17	14	11	8	6	4	1
48	50	55	58	55	49	43	36	30	24	18	13	10	11	14.	18	22	26	28	30	32	32	32	31	30	28	27	25	22	19	16	13	10		5
51	51	50	48	46	43	40	36	32	27	22	18	13	10	11	13	17	21	25	28	30	32	32	32	32	31	29	28	26	24	21	18	14	12	9
51	49	46	42	39	37	36	35	33	30	26	22	19	14	11	10	12	16	20	24	27	30	32	33	33	32	31	30	29	27	25	23	19	16	13 :
41	41	41	40	37	35	33	33	34	33	30	27	23	19	15	11	10	11	15	19	23	26	29	31	33	33	33	32	31	30	29	27	24	21	18
30	31	32	34	35	34	33	33	33	34	33	32	28	25	20	16	12	10	11	14	18	22	26	29	31	33	34	34	33	33	31	30	28	26	23
19	20	23	26	30	32	33	33	32	32	34	35	34	31	27	22	18	13	10	10	12	16	21	25	28	31	33	34	35	34	34	33	31	30	28
12	12	14	18	22	26	30	33	33	32	32	33	35	35	3.3	29	25	20	15	11	9	11	15	19	24	27	31	33	34	35	35	35	34	32	31
-5	6	8	11	15	19	24	28	31	33	33	32	32	34	35	34	32	27	22	17	12	10	10	1.3	18	22	26	30	32	34	.35	35	35	34	33
2	2	3	- 5	8	12	17	22	26	29	32	32	32	32	33	34	34	33	.29	24	19	15	11	10	12	16	20	24	28	31	33	34	35	34	34
2	1	0	2	4	6	- 9	14	19	24	28	31	32	32	31	32	33	34	34	31	26	21	16	13	11	11	13	17	22	25	29	31	32	33	33
2	2	3	3	1	1	5	8	12	16	21	25	29	31	32	32	31	32	34	34	33	29	24	18	14	12	11	12	15	19	22	26	28	30	32
7	6	4	2	1	1	1	2	5	10	14	19	24	27	30	31	32	32	33.	34	35	34	32	27	21	16	13	11	11	13	17	20	23	26	28
2	4	7	9	8	5	2	0	1	4	7	12	17	22	27	29	31	32	32	33	34	35	35	33	29	24	19	14	12	11	12	15	19	,22	24

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المراجعين المستحا يتحقق المحالي المراجع

ار ارتباع بار میدوند. استان استان با مستقد و به دارند در در از معرف اینده در و از ایند به دستان از معرفینی از این ارتباع باری باری باری استان استان استان این این از مارد در این معرف اینده در و از اینده می در معرف از مع

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JOB	0350	7/5/74	IBM 360-91
	EXECUTI	ON TIME	34 SEC.
			25 PAGES
		CORE	150 K

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# GEOMETRY OF IN-PLANE EDGE IMPACT OF A COMPOSITE PLATE WITH PROJECTION STRIP







FIGURE 2a

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LAYUP ANGLE

## FIGURE 2b

Comparison of In-plane plate edge wave speed with body wave speeds versus fiber layup angle for 55% graphite fiber/epoxy matrix composite.





Poles, Branch Points and Integration Contours in the complex Plane for the Numerical Solution.



Edge Stress t₁₁ Surface Wave for  $0^{\circ}$  Fiber layup Angle: 55% graphite fiber/epoxy matrix composite



Edge Stress t₁₁ Surface Wave for <u>+</u> 15° Fiber Layup Angle: 55% Graphite fiber/expoxy matrix composite.

Computer Map of Edge Impact Pressure t₃₃ Impact Time 87 µsec.

FIGURE 6

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- 7	1	1	0	<b>0</b>	0	0	- O -	0	0	0	Ð	0	0	0	0	0	ີ0ີ	0	0	0	0	0	0	0	0	0	Ū Ū	0	0	- 0	0	<b>0</b>
1	5	13	8	1	0	0	0	0	Û	Û	ŋ	0	0	0	0	0	0	0	0	·0	0	0	0	0	0	0	0	0	0	0	0	0
3	Û	27	17	2	0	0	0	0	0	0	0	Ũ	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	Ü 0
4	5	40	24	3	0	0	0	· 0	υ υ	<u>0</u>	υ	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	<b>0</b> .
5	8	52	32	3	0	0	0	Û	0	0	0	0	0	0	0	0	. 0	0	0	0	0	0	0	0	0.	θ	0	0	0	0	0	0
7	0	63	38	4	0	C	0	U	0	0	0	0	0	0	0	0	0	0	0	0	U	0	0	0	0	0	0	0	0	0	0	0
- 8	0	72	44	5	0	0	ົບ	- 0	്റ്	ΰŰ	Ŭ	0	<u></u> 0	0		Ö 0	0	0	Ö	0	0 Î	0	0	0	0	0	: 0 T	ΟŪ	0	Ō	0	0
8	9	79	48	6	0	0	0	0	0	0	Э	Ü	Ũ	0	-0	0	0	0	0	0	0	0	Ó	0	0	0	0	0	0	Ō	Ō	0
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STRESS T33

0.4366E-05

STRESS  $t_{11}$  ,  $0^{\circ}$  LAYUP

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SPURIOUS DATA

FIGURE 7

Computer Map of Edge Stress  $t_{11}$  Surface Wave in the Space-Time  $(x_1, t)$  Domain



FIGURE 8 Decrease of Stress  $t_{33}$  with Distance from the Impact Edge.



Stress  $t_{33}$  versus Time at Different Distances from the Edge under the Contact Point.



Maximum Stresses versus Layup angle for 55% Graphite Fiber/epoxy Matrix Composite.



Distribution of Stress  $t_{33}$  Along the Edge for Fiber Layup angles  $0^{\circ}$ ,  $\pm 30$ ,  $\pm 45^{\circ}$ .


DATA FOR 55% GRAPHITE FIBER/EPOXY MATRIX ± 15° LAYUP - STEEL STRIP

FIGURE 12a

Effect of Edge Strip Thickness on Interface Stresses.





Effect of Edge Strip Thickness on Interface Stresses.



FIGURE 13 Effect of Edge Strip Thickness on Interface Stresses.



FIGURE 14 Effect of Edge Strip Thickness on Stress t₃₃ Distribution Along the



Effect of Edge Strip Thickness on the Rayleigh Edge Wave Shape.



Effect of Edge Strip Thickness of Interface Shear Stress t₁₃ Distribution Along the Edge.