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# SHAKE TEST OF ROTOR TEST APPARATUS IN THE

# 40- BY 80-FOOT WIND TUNNEL

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16. Abstract				
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# SHAKE TEST OF ROTOR TEST APPARATUS IN THE 40- BY 80-FT WIND TUNNEL

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#### SUMMARY

A shake test was conducted to determine the dynamic characteristics of a Botor Test Apparatus on two strut systems in the Ames 40- by 80-ft wind tunnel. The rotor-off hub transfer function (acceleration per unit force as a function of frequency) was measured in the longitudinal and lateral directions, using a combination of broadband and discrete frequency excitation techniques. The dynamic data is summarized for the configurations tested, giving the following properties for each mode identified: the natural frequency, the hub response at resonance, and the fixed system damping. The complete transfer functions are presented, and the detailed test results are included as an appendix. Finally, the report discusses the data analysis techniques developed to obtain on-line measurements of the system modal properties, including the damping coefficient and the damping ratio.

### INTRODUCTION

A shake test was conducted to establish the dynamic characteristics of a Rotor Test Apparatus (RTA) in the Ames 40- by 80-ft wind tunnel (figure 1). Of interest were potential resonances at the 1/rev and 4/rev frequencies of rotors likely to be tested on the RTA, and potential ground resonance instabilities.

The shake test was performed on the RTA module, without a rotor, on two strut systems in the wind tunnel, to determine the principle frequencies and damping of the structure. The rotor-off hub transfer function was

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measured in the longitudinal and lateral directions: longitudinal, inplane acceleration of the hub due to longitudinal, inplane force; and lateral, inplane acceleration of the hub due to lateral, inplane force. With the hub transfer functions it is possible to evaluate potential ground resonance and vibration problems of rotors to be tested on the BTA. The frequency ranges of interest are: 0-5 Hz for ground resonance, 3-7.5 Hz for 1/rev vibration, and 12-30 Hz for 4/rev vibration (based on a rotor speed range of 180-450 rpm). The information required for each mode of the system is the natural frequency and the amplitude of the hub response, and for potential ground resonance modes we must know the fixed system damping as well.

## SYSTEM

The system tested consisted of the RTA module, without a rotor, on the struts and balance frame in the 40- by 80-ft wind tunnel. The RTA module included the rotor hub, with the transmission locked, and two 1500-HP electric motors installed (one of the motors was replaced by a dummy weight for this test). The total module weight was 30400 lb.

Two strut/tip configurations were tested: a short strut system (8-ft struts with 5-ft tips) and a long strut system (15-ft struts with 6-in tips). The short struts gave softer support of the module because of the flexibility of the tips. In the basic configuration the balance was free, with the scale system operating. The shake tests were also conducted with the balance locked, in order to obtain the cantilever strut modes. Finally, the system was tested with strut dampers installed, consisting of an extensible strut from the top of each main strut down to the rear of the balance frame, with a total of eight automotive shock absorbers as dampers.

## TEST APPARATUS

A hydraulic shaker was attached to the blade grip of the rotor hub to excite the module by application of an inplane force, in the longitudinal or lateral direction. The other end of the shaker was attached to an

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11600 lb reaction ...ss suspended from a crane. Figure 2 shows the shake test configuration, for lateral excitation. For longitudinal excitation, the shaker was attached to the forward blade grip, with the reaction mass over the module nose. The shaker servo control was operated in a stroke feedback mode.

A load cell between the shaker and hub measured the applied force. Accelerometers on the hub measured the longitudinal and lateral response. Data were recorded for other accelerometers on the module and balance frame, but only the results for the hub response are presented in this report.

The applied force and resulting hub acceleration data were analyzed on-line to determine the dynamic characteristics of the system, using the Dynamic Analysis System (DAS, shown in figure 3). The DAS is basically a time series analyzer and computer, utilizing Fast Fourier Transform techniques and associated software, and programs specific to this shake test.

## TEST PROCEDURE

The frequency ranges investigated were 0-9 Hz for ground resonance and 1/rev vibration modes, and 0-35 Hz for N/rev vibration modes. Broadband random input to the shaker was used, with a bandpass filter to shape the input spectrum. The low cutoff frequency was set at 0.5 Hz to avoid excitation of the reaction mass pendulum modes, and the high cutoff frequency was set at either 9 or 35 Hz to restrict the energy input to the frequency range of interest.

The basic test plan, for each strut/module/balance configuration, excited in the longitudinal and lateral directions, was as follows.

- Random excitation, bandwidth .5-9 Hz; nominal force amplitude \$200 and \$400 lb (\$400 lb point usually repeated).
- 2) Random excitation, bandwidth .5-35 Hz; nominal force amplitude ±100 and ±200 lb.

3) Sinusoidal (discrete frequency) excitation at various force levels, at the low frequency resonances identified in #1; usually points were taken at frequencies near the resonance as well.

There was some variation between runs of course. For future work, the use of narrow-band random excitation at each resonance would seem preferable to a sequence of (nominally) discrete frequency points as was the practice in this test. Narrow-band excitation offers the possibility of obtaining the data over the entire frequency range near the resonance in a single measurement. The reason for the narrow-band excitation is to concentrate the input energy into a particular mode, so for the highest force levels it may be necessary to narrow it down to essentially discrete excitation again. Still, the data from this test indicate that an accurate estimate of the system damping may be obtained from the single frequency point. even if it is not quite at the resonant peak (see the discussions below).

The following six configurations were tested, with longitudinal and lateral excitation for each:

- 1) Short struts.
- 2) Short struts, balance locked.
- 3) Short struts, with strut dampers (8 shocks).
- 4) Long struts.
- 5) Long struts, balance locked.6) Long struts, with strut dampers (8 shocks).

## ANALYSIS

The data for the force applied to the hub and the resulting hub acceleration were analyzed on-line, utilyzing the DAS. The input signal f (force) and output signal a (acceleration) were sampled (digitized) at rate r, taking a total of N samples. The discrete Fourier transforms of f and a were calculated, and converted to engineering units using input conversion factors (lb/volt and g/volt). The products of the transforms gave the cross spectrum  $S_{io} = \overline{F} * A$ , and the input autospectrum  $S_{ii} = \overline{F} * F$ . Sin and Sii were averaged over K data records. Finally the transfer function of the hub response was calculated, from H = acceleration/force = averaged Sto/averaged Sti.

The computer searched the magnitude of the transfer function for resonant peaks. Then it calculated and printed for each peak the following quantities: the resonant frequency  $(\Delta)$  (Hz); the magnitude of the force and acceleration at that frequency; the magnitude of the hub response [H] (g/1000 lb and in/1000 lb); the phase of the response,  $\angle$  H (deg); the fixed system damping coefficient C<sub>S</sub> (lb/fps), calculated from H at the resonant frequency; the damping coefficient, modal mass, and damping ratio (C<sub>S</sub>, M, and  $\int$ ), calculated from integrals of H through the resonant peak; and the damping ratio  $\int$ , calculated by a least-squared-error parameter identification technique from the data for H near the peak. In addition, ground resonance parameters (critical rotor speed and required lag damping) were calculated, for a particular rotor.

The magnitude of the transfer function, |H| vs.  $\omega$ , was displayed on a CRT. A picture was taken as a record of the complete transfer function.

The discrete frequency excitation points were analyzed in the same manner. However, the response was only evaluated at the single line corresponding to the input frequency.

Further details of the analysis techniques are given in appendices: a discussion of the discrete Fourier transform (Appendix A); the local maximum discriminator (Appendix B); calculation of the fixed system damping from the transfer function (Appendix C); LSE parameter identification of the damping ratio (Appendix D); and calculation of the damping from integrals of the transfer function (Appendix E).

The following parameters were used for the analysis of the data in this test:

> Ground resonance and 1/rev dynamics (0-9 Hz): sample rate r = 20.48/sec, number of samples N = 512, number of records K = 10; total sample time T = 250 sec, spectrum frequency increment = .04 Hz.

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2) N/rev dynamics (0-35 Hz): sample rate r = 81.92/sec, number of samples N = 256, number of records K = 20; total sample time T = 62.5 sec, and spectrum frequency increment A = .32 Hz.

For future work, it would probably be better to take more records for the 35 Hz bandwidth excitation, to further reduce the noise in the data; K = 40 (hence T = 125 sec) should be about right. The use of Hanning to smooth the data is usually recommended (see the references of Appendix A), but it was only occasionally used in this test.

#### RESULTS

The results of this test are the dynamic characteristics of the six configurations investigated, specifically, the frequencies and response amplitudes of the principal modes identifiable in the hub transfer functions.

Figure 4 demonstrates the repeatibility of the transfer function measurements. It shows three separate measurements of the longitudinal response on the short struts. There is excellent correlation between the three points. Figures 5 through 10 present the transfer functions for the six configurations tested. The lateral and longitudinal hub responses are shown, in the 9 and 35 Hz excitation ranges for each. The abscissas in the figures are frequency, from 0 to 10 or 50 Hz, and the ordinates are the magnitude of the transfer function in g/1000 lb.

Tables 1 and 2 summarize the dynamic characteristics of the six configurations tested. The tables give the following quantities for each of the longitudinal and lateral modes identified: the resonant frequency  $\omega$  (Hz); the magnitude of the hub response H (g/1000 lb and in/1000 lb); and, for the potential ground resonance modes, the fixed system damping coefficient C<sub>s</sub> (lb/fps). The hub response and damping coefficient data for the long struts, lateral shake, balance free and balance locked (runs 17 and 18) are somewhat uncertain because of a problem with the accelerometer calibration. However, the conversion factor (g/volt) used for these two runs was certainly within 25% of the correct factor. The frequency and damping ratio data are nof affected by this problem.

		Longitudinal Mode	al Modes						Lateral	Modes		
		3	H /•	H / u t	ບຶ				3	Н /2	Н /ч;	లో
Mode		Hz	1000 lb	1000 15	1b/fps		Mode		ZH	1000 15	10001	lb/fps
					SHORT	RT STRUT						
balance	6	1.66	.21	65.	1300-1500		balance	side	2.10	.36		10011-0021
strut		3.04	.38	. 04.	800-1200		balance	уан	2.24	75.	-67	500-600
balance	ertical	7.32	.15	U3			strut		3.52	17.	ł	1400-1600
module	<b>tertical</b>	10.0	- 06.	9			mast		23.2	2.9	50.	
X-beam	<b>tertical</b>	14.1	.70	03			mast		27.7	2.3	03	
mast		25.5	3.1	.05								
		28.5	1.5	-02								
		31.2	1.7	•02								
		35.0	2.0	- 02								
				1	SHURT STRUTS.	1	BALANCE LCCKEI					
strut		2.27	.78	1.47	0111		strut		2.45	07.1	2.2R	300
module	<b>fertical</b>	10.0	.80	•08			mast		23.7	2.0	.03	
Х-bean	tertical	15.3	•50	•02			mast		27.7	1.9	.02	
mast		25.5	2.5	<del>1</del> 0.								
		31.2	1.3	.01								
		35.0	1.5	10.								
				SHOR	SHORT STRUTS	UITH ST	STRUT DAMPIRS	RS				
balance	¢)	1.70	8.		3200-3600		balance	side	1.9	•20	• 20 1	1500-2000
damper	trut	4.9	.15		4000-000		balance	уан	2.2	92 <b>.</b>	1 24.	1900-2100.
strut		5.8	.12	ま	4000-8000		strut		3.52	.22	.18 2	2900-3200
balance	e vertical	2.60	8	.01			mast		23.2	3.5	- 06	
module	<b>vertical</b>	10.7	0%.	-02			mast		27.7	<u></u>	to.	
X-beam	<b>fertical</b>	15.5	•55	-02								
mast		25+5	3.2	•02								
		28.5	1.5	.02								-
		31.2	1.7	-02								
		35.0	2.0	.02								

TABLE 1. Summary of Dynamic Characteristics: Short Struts

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TABLE 2. Summary of Dynamic Characteristics: Long Struts

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	Long1 tud1	Longitudinal Modes	Ŧ					Lateral Modes	Modes H	×	
	3	u /2	1n/	ບິ				3	u /6	r /ut	ບ້
	Hz	1000 lb	1000 lb			Mode		Яz	1000 lb	1000 1b	1b/fps
				м	NG STRUT	2					
balance	1.62	60 <b>°</b>	.32	3400-380		balance	side	2.32	12.	1.86.	1600-2000
	4.02	.85	.51	600-800		halance	уан	2.67	.18	.25 2	2600-3000
balance vertica	7.20	60.	•02			strut		4.50	1.24	1	550-650
<b>vertical</b>	10.6	04.	90.			mast		23.2	1.0	-02	
<b>vertical</b>	14.1	•65	.03			mast		27.7	2.5	03	
	25.5	2.5	さ								
	28.5	1.6	.02								
	31.2	1.4	.01								
	35.0	1.5	.01								
				LUNG STRUTS,	1	BALANCE LOCKE					
	3.00	1.15	1.25	500		strut		3.46	1.55	1.27	280
fertical		•85	•08			mast		23.2	1.5	0	
<b>fertical</b>		•60	•03			mast		27.7	2.2	.03	
	25.5	2.1	•03								
	31.2	1.2	•01								
	35.0	1.4	10.								
			<b>LON</b>	LONC STRUTS	IS HIIM	STRUT DAMPERS	IRS				
balance	1.61	-02	[	3600-4200		balance	side	2.32	ti2.	ŧ.	1400-1800
damper strut	3.61	.10	60.	5000-6400		balance	уам	3.2	.02	.02	
	5.48	.31		3200-4600		strut		4.65	.31	14 2	2800-3000
balance vertica		-02	(			mast		23.2	2.0	đ	
module vertical		-80	-02			mast		27.7	2.6	:03	
X-beam fertical		.65	6								
	25.5	2.5	ъ.								
	28.5	1.4	•02								
	31.2	1.4	•01								
	35.0	1 7.1	.01								

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In the lateral response on the short struts (balance free, no dampers) we observe two close modes at the lower resonance, around 2 Hz. These are the balance side and balance yaw modes, involving considerable module yaw and side motion as well for this case. Figure 11 shows the details of the two modes, expanding the magnitude and phase of the transfer function in the range 1-3 Hz. The detailed test data are given in Appendix G, Table G1. The dynamic situation is as follows. For the short strut configuration, the uncoupled balance lateral modes and cantilever strut side mode have about the same frequency, around 2.4 Hz (see Tables 1 and 2). Thus there is considerable coupling of the balance and module motion for the complete system, with the typical behavior that the frequencies of the coupled modes are driven apart. The balance mode frequencies are decreased, the strut mode frequency is increased, and the damping for the balance modes is reduced. For the long strut configuration, the lateral cantilever strut mode frequency is around 3.5 Hz, well above the balance mode frequencies (see Table 2). Therefore the balance mode frequencies are not lowered significantly for this configuration (note that the balance side mode frequency is expected to be about  $\sqrt{2}$  times the balance longitudinal mode frequency, since there are two side force scales and one drag force scale in the balance system).

The test data show a nonlinear behavior for the damping of the balance modes. The damping for high excitation level and high response amplitude consistently was significantly lower than the damping measured at low levels (the data in Tables 1 and 2 are the values for low excitation level). Figure 12 shows the general trend, for all the configurations tested. The ratio of the balance mode damping to its value at low excitation levels correlates well with the rms value of the exciting force. The linear range extends up to 30 or 40 lb (rms), and at high excitation the damping levels off at about 40 to 50% of the low excitation value. The detailed test data are given in Appendix G. A correlation between the excitation level (broadband and discrete) and the balance drag scale motion for the longitudinal balance mode is also given in Appendix G (run 11, Table G1).

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From the frequencies of the modes we may identify 1/rev and N/rev resonances for the operating range of a particular rotor, and with the data on the magnitude of the hub response assess the vibration potential of these modes. From the frequency and fixed system damping we may assess the ground resonance stability of articulated and soft-inplane hingeless rotors on this Rotor Test Apparatus. A simple ground resonance stability criterion, giving the critical rpm ranges and the lag damping required for stability, is discussed in Appendix F. More detailed calculations of the dynamic stability are recommended however.

The tables of Appendix G present in detail the shake test data for the six configurations investigated.

# DISCUSSION OF ANALYSIS TECHNIQUES

Several methods were used to calculate the modal parameters from the measured transfer function. The quantities required are: the natural frequency  $\omega_n$ , damping coefficient  $C_s$ , damping ratio  $\int$ , and modal mass M (note that these parameters are related by  $C_s = 2 \int \omega_n M$ ).

The natural frequency was estimated using three points around the experimental peak (Appendix D). This technique gave satisfactory results.

The damping coefficient was calculated from the transfer function at a single frequency point (Appendix C), and from integrals of the transfer function through the peak (Appendix E; this method was used only for runs 17 and 18, Tables G4 and G5). Both methods worked well, and the two techniques gave comparable estimates. The experimental data (Appendix G) for the singlepoint calculation of  $C_g$  during discrete frequency sweeps near a resonance demonstrate that this method gives an estimate of the damping which is indeed relatively insensitive to frequency, i.e. roughly constant in the vicinity of each peak (see Appendix C). The integral method of calculating  $C_g$  is less sensitive to noise in the transfer function data, but for very close modes one must watch that the limits of integration cover only one

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resonant peak. With discrete or very narrow-band excitation, only the singlepoint estimate of  $C_s$  is applicable of course. The use of both methods is recommended to obtained the best extimate of the damping coefficient.

To calculate the damping ratio and modal mass ( $\int$  and M), the LSE parameter identification techniques described in Appendix D were used, with four iterations after the initial estimate of the parameters, and either 5 or 10 points for the curve fit around the resonant peak. For an ideal transfer function (no noise in the data) these techniques worked well, especially the two-parameter algorithms. For real data however, i.e. an experimental transfer function measurement including noise, the methods of Appendix D were not satisfactory. The one-parameter algorithm ( $\int$  from |H|) did no better than the initial estimate of  $\int$  from three points. The two-parameter algorithms ( $\int$  and M from either |H| or H) either gave little improvement over the initial estimate, or simply did not converge. The difficulty is probably due to the fact that the derivatives in the iteration formulas are singular at  $\int = 0$ . There is the possibility of better success using an algorithm to identify  $C_g$  and M from the transfer function.

The damping ratio and modal mass ( $\int$  and M) were also calculated (for runs 17 and 18, Table G4 and G5) from integrals of the transfer function, as described in Appendix E. This technique worked well, and its continued use is recommended.

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# APPENDIX A

# The Discrete Fourier Transform

# 1. References

Bendat, Julius., and Piersol, Allan G., <u>Measurement and Analysis</u> of Random Data, John Wiley & Sons, Inc., New York, 1966 Jenkins, Gwilym M., and Watts, Donald G., <u>Spectral Analysis and its</u> <u>Applications</u>, Holden-Day, San Francisco, 1969

# 2. Definition and Application

The input signal (force, f) and output signal (acceleration, a) are sampled (digitized) at rate r, until the total number of samples N is collected. The result is a discrete time series of data, at  $t = n \Delta t$ , n = 0...N-1 ( $\Delta t = 1/r$ , with sampling period T = N/r). The discrete Fourier transforms of the input and output are calculated, using Fast Fourier Transform (FFT) techniques, according to the expression:

$$X(k) = \frac{1}{N} \sum_{n=0}^{N-1} x(n) e^{-i 2\pi k n / N}$$

The result is a discrete spectrum, at the N/2 frequencies  $\omega = k \Delta \omega$ , k = 0...(N/2-1) ( $\Delta \omega = r/N = 1/T$  Hz, with a maximum frequency -- spectrum bandwidth -- of  $\omega_{max} = r/2$  Hz).

The input and output transforms are multiplied then to obtain the cross-spectrum  $S_{io} = \overline{F} * A$  and the input autospectrum  $S_{ii} = \overline{F} * F$ . The spectra  $S_{io}$  and  $S_{ii}$  are averaged over a total of K records of data. Then the system transfer function is calculated as:

$$H = a/f = average S_{io}/average S_{ii}$$

# 3. Relation to Continuous Fourier Transform

The Fourier transform of a continuous, non-periodic time function x(t) is defined as

$$X(w) = \frac{1}{2\pi} \int_{-\infty}^{\infty} x(t) e^{-iwt} \partial t$$

The discrete Fourier transform makes two approximations: first, a finite length record of data is transformed; and secondly, a finite number of samples are taken during the record.

With a finite length record, it is assumed that the data is periodic outside the record; hence we calculate the Fourier transform of a periodic function:

$$X_{1}(\omega) = \frac{1}{T} \int_{0}^{T} x(t) e^{-i\omega \tau} Q \tau$$

at the discrete harmonics  $\omega = 2\pi k/T$ . This may be considered the Fourier transform of x(t) times the window w(t) which is open only for t = 0 to T, so

$$X_{1}(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} x(t)w(t) e^{-i\omega t} dt$$
$$= \int_{-\infty}^{\infty} X(\omega^{*}) W(\omega - \omega^{*}) d\omega^{*}$$

(using the convolution theorem). The time window is

$$w = \begin{cases} \frac{2\pi}{T} & 0 < t < T \\ 0 & \text{otherwise} \end{cases}$$

so the frequency window (the Fourier transform of w) is:

$$W = \frac{\sin \omega T/2}{\omega T/2} e^{-i\omega T/2}$$

which has amplitude 1 and bandwidth  $\Delta \omega = 2\pi T/T$ . Thus

$$X_1(\omega) \cong \int_{\omega - \Delta \omega/2}^{\omega + \Delta \omega/2} X(\omega^*) \partial \omega^*$$

This  $\Delta \omega$  is the same as the frequency increment in the discrete spectrum. So each line in the discrete transform may be viewed as the integral of the continuous transform over the interval  $\omega - \Delta \omega/2$  to  $\omega + \Delta \omega/2$ .

With only a finite number of samples in the record, we calculate as an approximation to  $X_1$  the discrete transform:

# $X_2(k) = \frac{\Delta t}{T} \sum_{n}^{E} \chi(n) e^{-i2\pi kn \Delta t/T}$

(the summation being the discrete approximation of the integral). Since  $\Delta t/T = 1/N$ , this is identical to X(k) defined in section 2 above. The finite length record means that only the discrete harmonics  $\omega = k \Delta \omega$  of the transform are calculated. The finite number of samples means that the maximum frequency of the spectrum is  $\omega = N/2 * \Delta \omega = r/2$  (the Nyquist frequency). It is necessary to filter the analog input and output signals with a low-pass cutoff frequency at or below  $\omega_{max}$ , in order to avoid aliasing of the discrete spectrum by harmonics above the Nyquist frequency, which can not be discerned by sampling at the discrete rate r.

# 4. Noise

Bacause of process and measurement noise, we do not calculate a deterministic spectrum, but rather a statistical estimator of the spectrum. In order to reduce the noise in the estimate of the spectrum, it is necessary to average the data. Thus we take K records, and calculate the average spectrum

$$\overline{S} = \frac{1}{K} \varepsilon S_{K}$$

This sample spectrum has an unbiased mean, and a variance of

$$\frac{V_{\text{or}} \cdot \vec{S}}{S^2} = \epsilon^2 \stackrel{\simeq}{=} \frac{1}{K}$$

The standard deviation is thus inversely proportional to  $K^{\frac{1}{2}}$  (compare with the similar result for the standard deviation of a sample mean). The total sample time is  $KT = K / \Delta \omega$ , so for a given time it is necessary to compromise between the accuracy of the data and the frequency increment in the spectrum. Bendat and Piersol suggest using a minimum of K = 10 records. The statistics of the transfer function H (the ratio of the average cross spectrum to the average input autospectrum) are more complex (the reader is directed to the references given above), but the  $K^{-\frac{1}{2}}$  behavior of the spectra is sufficient for the present purposes.

# 5. Choice of Parameters

The parameters r, N, and K are required to define the sampling and averaging process in the analysis of the data. For a given bandwidth of the data, the sample rate r suggested is

# r = 2.5 \* bandwidth data

 $( \Box_{\max} = r/2 = 1.25 * bandwidth)$ . A low pass filter on the signal is also required, to avoid aliasing in the discrete transform. The number of samples N is then chosen from r and the required frequency increment in the spectrum  $\Delta \omega$ , as  $N = r/\Delta \omega$  (FFT routines used require also that N be a power of 2). We choose  $\Delta \omega$  to define the resonant peaks sufficiently, from  $\Delta \omega \cong \int \omega_{\infty}/2$  (which gives about 5 points covering the  $\frac{1}{2}$  power bandwidth of the peak;  $\Box_{\infty}$  is the natural frequency and  $\int$  the damping ratio of the mode). Finally, the number of records K is chosen for the desired accuracy (noise level) of the spectrum. At least 6 to 10 records are desired; the principle restriction of the number of records is the total sample time KN/r.

# APPENDIX B Local Maximum Discriminator

# 1. Problem

It is necessary to identify the resonant peaks (i.e. the natural frequencies) of the experimental transfer function. The experimental transfer function has measurement and process noise however, so it is not possible to identify the peaks by simply searching for all the local maxima of the data. An algorithm must be developed which will discriminate the true peaks from the spurious local maxima due to noise.

## 2. The Algorithm

We have the data for the magnitude of the transfer function, which may be written  $H_e = H + h$ , where H is the true value and h is random noise in the measurement. Assume h has a normal distribution with zero mean and standard deviation  $\nabla$ , hence probability distribution:

$$f = \frac{1}{\sigma \sqrt{2\pi^2}} e^{-\sqrt{2}/2\sigma^2}$$

Assume  $\P = H/K^{\frac{1}{2}}$ , where K is the number of records of data in the average of the cross spectrum and input autospectrum calculated to find H (see Appendix A).

Consider then the probability of a peak at a certain frequency  $\omega_N$ , i.e. the probability that  $H_N - H > 0$  for all nearby frequencies. This is the probability that  $h > h_N - \Delta H_e$ , where  $\Delta H_e = H_{e_N} - H_e$ ; which is:

$$Pr = \int_{-\infty}^{\infty} \int_{N}^{\infty} f(h) f(h_N) \partial h \partial h_N$$
  
$$= \frac{1}{\sigma^2 2\pi r} \int_{-\infty}^{\infty} e^{-(h^2 + h_N^2)/2\sigma^2} \partial h \partial h_N$$
  
$$= \frac{1}{\sqrt{2\pi r'}} \int_{-\infty}^{\infty} e^{-y^2/2} \partial y$$

This integral may be expressed in terms of the error function.

The product of the probability Pr evaluated at several points around  $\omega_N$  is the probability that all local values of H are less than the H at  $\omega_N$ . Therefore we take as a discriminator of the local maxima the parameter

C is evaluated at all frequencies of the transfer function. If C is above a certain confidence level for any frequency, we consider that point a resonant peak of the transfer function.

The parameter C has the following properties. For a local maximum, C  $\cong$  1, while C is near 0 for a local minimum. If  $\Delta H_e = 0$  for all points (i.e. the experimental data constant), then C =  $\frac{1}{2}$ . Finally, with  $\Delta H_e/\sigma = 1$ , 2, or 3 we obtain C = .76, .92, and .98.

## 3. Application

For on-line evaluation of the data (locating the resonant peaks of the transfer function and calculating the system properties there), it is better to use a rather low confidence level on the discriminator (so a few false peaks are located, which are easily discarded by the engineer), rather than to use a high confidence level which will occasionally miss a true peak because of excessive noise. It is also found that the parameter C is a more sensitive discriminator of the peaks if many points are used to evaluate C for each frequency.

For the present test, a confidence level of 65 to 70 (C above the confidence level considered an indication of a resonant peak) was satisfactory. The parameter C was calculated using 12 points ("m" in the definition of C above) around each frequency.

#### APPENDIX C

## Fixed System Damping from Transfer Function

To evaluate the ground resonance stability of a rotor on a flexible support, it is necessary to know the damping coefficient of the modes. This may be obtained from the hub impedance by the following method. Consider the mass/spring/damper system:  $M\ddot{x} + C_s \dot{x} + M\dot{a} \dot{x} = f$ . The response of the hub acceleration to the applied force is the transfer function

$$H = \frac{a}{f} = \frac{-\omega^2}{M(\omega_n^2 - \omega^2) + C_s i \omega}$$

where  $\Theta_{\infty}$  is the natural frequency, M the generalized mass of the mode, and C<sub>s</sub> the damping coefficient. It follows that

$$C_{\rm S} \equiv \frac{\omega \, dm H}{|H|^2}$$

or

$$C_{S} = 195.4 \frac{\omega J_{mH}}{1HI^{2}}$$

with the dimensions  $[\omega] = Hz$ , [H] = g/1000 lb,  $[C_s] = 1b/fps$ . This is the expression used to calculate the damping of the rotor support, from the experimental measurement of the hub response.

At the resonant frequency ( $\omega = \omega_n$ ) this result becomes  $C_s = \omega/|H|$ . In general the previous form is preferable however, since it holds for all  $\omega$ , not just at the peak. Thus it is possible to evaluate  $C_s$  even though the calculation is not performed exactly at the peak (for multimode systems it is necessary to be at least close to the peak of course). The experimental data (Appendix G) shows that the damping calculated by this expression is quite consistent in the vicinity of the resonance of each mode.

# APPENDIX D Least Squared Error (LSE) Parameter Identification of Damping Ratio from Transfer Function

# 1. LSE Parameter Identification

It is desired to fit an analytic function  $H(\omega, u_i)$  -- where  $\omega$  is the frequency,  $u_i$  are free parameters (e.g. the damping ratio  $\int$ ), and H may be either a complex transfer function or the magnitude -- to experimental data  $H_e(\omega_k)$  at the discrete frequency points  $\omega_k$ . We shall find the parameters  $u_i$  to minimize the squared error

$$\epsilon = \sum_{k} |H(w_k) - H_e(w_k)|^2$$

For complex H, this error is the sum of the distances between H and H on the complex plane (Re H vs. Im H, i.e. the phase plane). The minimum  $\epsilon$  is given by the solution of:

$$\frac{\partial \varepsilon}{\partial n_i} = \varepsilon \frac{\partial}{\partial n_i} \left[ H - H \varepsilon \right]^2 = 0$$

If H is linear in the parameters, the above is a set of linear algebraic equations which may be solved directly for the parameters  $u_i$ . In the present case however, H is not a linear function of  $u_i$ , so a solution by numerical methods is necessary; we shall use Newton's method. From

$$\frac{\partial f}{\partial u_i} \cong \frac{\partial f}{\partial u_i} |_{u_i}^{(m)} + \frac{\xi}{j} (u_j^{(m+i)} - u_j^{(m)}) \frac{\partial^2 f}{\partial u_i \partial u_j} |_{u_i}^{(m)}$$

it follows that the iterative solution of  $\partial f/\partial u_i = 0$  is

$$\vec{n}^{(n+1)} = \vec{n}^{(n)} - \left[\frac{\partial^2 f}{\partial n; \partial n_j}\right]^{-1} \left\{\frac{\partial f}{\partial n_i}\right\}$$

where u is a vector of the parameters  $u_i$  (nth iteration), and the derivatives of f are evaluated using  $u_i^{(n)}$ .

Here  $f = \sum_{k} |H - H_{e}|^{2}$ , hence the solution of the parameter identification problem is:

$$\vec{n}^{(n+1)} = \vec{n}^{(n)} - \left[ \sum_{k} \frac{\partial^{2}}{\partial u_{i} \partial u_{j}} \left[ H - H_{e} \right]^{2} \right]^{-1} \left\{ \sum_{k} \frac{\partial}{\partial u_{i}} \left[ H - H_{e} \right]^{2} \right\}$$

# 2. Transfer function

We shall fit the measured transfer function in the neighborhood of a resonant peak to the theoretical transfer function of a mass/spring/ damper system. Considering the acceleration response to an applied force, the transfer function is  $\frac{7}{100}$ 

$$H = \frac{\omega}{f} = \frac{-\omega^{2}/m}{\omega_{n}^{2} - \omega^{2} + i 2\zeta \omega_{n}}$$

Note that in general the parameter m (mass) is a complex number, because it accounts for the influence of other modes of the system in the vicinity of any particular resonance. The magnitude of H is:

$$|H| = \frac{\omega^{2}/m}{\sqrt{(\omega^{2} - \omega_{x}^{2})^{2} + (2 \int \omega \omega_{x})^{2}}}$$

Fitting H to the experimental data around a peak requires the identification of four parameters then: the damping ratio 5, the natural frequency  $\omega_{n}$ , the mass  $|w_{n}|$ , and the phase angle  $\angle w$  (only the first three are involved in fitting the magnitude of H to the experimental data).

Because of limitation of computer core and language, we consider only the identification of one or two parameters. The following cases will be considered in detail: fitting |H| to  $|H_e|$  by identifying  $\int$ ; fitting |H| to  $|H_e|$  by identifying  $\int$  and |W|; and fitting H to  $H_e$  by identifying  $\int$  and |W|. An initial estimate of the parameters is required to start the iterative LSE solution. It is assumed that the initial estimate of the parameters not corrected by the LSE solution (in particular the natural frequency  $\omega_m$ ) is satisfactorily accurate.

# 3. Initial Estimate of Parameters

Assume that a resonant frequency  $\Theta_P$  has been found (a local maximum of  $|H_e|$ ; see Appendix B). An initial estimate of the parameters may be obtained from the experimental data at the three points  $\Theta_P$ ,  $\omega_L = \omega_P - \Delta \omega$ , and  $\omega_R = \omega_P + \Delta \omega$ . For small 5 and small  $\omega - \omega_n$  (the usual case of interest), the transfer function is approximately

$$|H| \cong \frac{1}{2 \operatorname{Im} \sqrt{5^2 + (\frac{1}{2m} - 1)^2}}$$

From this approximation the parameters of H may be estimated as:

$$\Delta \omega_{n} = \Delta \omega \frac{R_{R} - R_{L}}{2(R_{R} + R_{L} - 2R_{R}R_{L})}$$

$$\omega_n = \omega_p + \Delta \omega_n$$

$$5^{2} = \frac{R_{L}(\Delta \omega + \Delta \omega_{n})^{2} - (\Delta \omega_{n})^{2}}{(1 - R_{L})\omega_{n}^{2}}$$

$$\frac{1}{m} = -H_{ep}\left(\frac{\omega \tilde{n}}{\omega p^2} - 1 + i 25 \frac{\omega n}{\omega p}\right)$$

where

$$R_{L} = |H_{eL}/H_{eP}|^{2}$$

$$R_{R} = |H_{eR}/H_{eP}|^{2}$$

4. Damping ratio from |H|

The LSE iterative solution is

Snew = 
$$5010 + \frac{\xi}{\xi} \frac{\partial}{\partial \zeta} (H - He)^2}{\frac{\xi}{\xi} \frac{\partial^2}{\partial \zeta^2} (H - He)^2}$$

or

where

$$r = \frac{\xi_{0}^{2}}{\xi_{0}^{2}} \frac{(H-H_{e})^{2}}{(H-H_{e})^{2}} - 5 \frac{\partial^{2}}{\partial 5^{2}} \frac{(H-H_{e})^{2}}{(H-H_{e})^{2}}$$

$$= \frac{\sum_{k} \omega^{4} D^{-3/2} (H_{e} - H)}{\sum_{k} \omega^{6} (12 \int_{0}^{2} \omega_{n}^{2}) D^{-5/2} (H_{e} - \frac{4}{3}H)}$$

$$b = (\omega^2 - \omega_n^2)^2 + (2 \int \omega \omega_n)^2$$
$$H = \frac{\omega^2}{m} b^{-\frac{1}{2}}$$

5. Damping ratio and Mass from |H|With  $\mu = 1/|m|$  and  $D = (\omega^2 - \omega_n^2)^2 + (2 \int \omega \omega_n)^2$ , we have  $H = \omega^2 D^{-\frac{1}{2}}$ . The derivatives required are:

$$A = \sum_{k} \frac{\partial}{\partial 5} (H - He)^{2} = \sum_{k} (He - H) \mu \omega^{2} \Delta^{-3/2} \frac{\partial \Delta}{\partial 5}$$
$$B = \sum_{k} \frac{\partial}{\partial \mu} (He - H)^{2} = \sum_{k} (He - H) (-2\omega^{2} \Delta^{-\frac{1}{2}})$$

$$\alpha = \sum_{k} \frac{\partial^{2}}{\partial \zeta^{2}} (H_{e} - H)^{2}$$

$$= \sum_{k} \left[ (H_{e} - H) \mu \omega^{2} D^{-3/2} \frac{\partial^{2} D}{\partial \zeta^{2}} - (H_{e} - \frac{4}{3}H) \mu \omega^{2} \frac{3}{2} D^{-\frac{4}{2}} (\frac{\partial \Phi}{\partial \zeta})^{2} \right]$$

$$\Theta = \sum_{k} \frac{\partial^{2}}{\partial \mu^{2}} (H_{e} - H)^{2} = \sum_{k} 2 \omega^{4} D^{-1}$$

$$c = \sum_{k} \frac{\partial^{2}}{\partial \mu^{2}} (H_{e} - H)^{2} = \sum_{k} (H_{e} - 2H) \omega^{2} D^{-\frac{3}{2}} \frac{\partial \Phi}{\partial \zeta}$$

and the LSE iterative solution is:

$$\begin{pmatrix} 5 \\ \mu \end{pmatrix}_{new} = \begin{pmatrix} 5 \\ \mu \end{pmatrix} - \begin{bmatrix} a & c \\ c & \theta \end{bmatrix}^{-1} \begin{pmatrix} A \\ B \end{pmatrix}$$
$$= \begin{pmatrix} 5 \\ \mu \end{pmatrix} - \frac{1}{ab-c^2} \begin{pmatrix} Ab-Bc \\ Ba-Ac \end{pmatrix}$$

6. Damping ratio and Mass from H

Using the initial estimate of  $\leq m$  and  $\omega_{\infty}$ , we shall match the experimental data  $H_e^{i \leq m}$  to the complex transfer function

 $H = -\mu \omega^2 D^{-1} (\omega_n^2 - \omega^2 - i 25 \omega \omega_n)$ 

where  $D = (\omega^2 - \omega_n^2)^2 + (2 \int \omega \omega_n)^2$  and m = 1/|m|. Then the squared error is

$$\mathcal{E} = \mathcal{E} [H - He]^2 = \mathcal{E} \left[ \mu (\alpha + \mu \omega^4 + \beta 5) \delta^{-1} + [He]^2 \right]$$

where

$$\alpha = 2 \operatorname{ReHe} \omega^2 (\omega_n^2 - \omega^2)$$
  
$$\beta = 2 \operatorname{JmHe} \omega^2 (-2\omega\omega_n)$$

The derivatives required are:  

$$A = \sum_{k} \frac{\partial}{\partial \zeta} |H - H_{e}|^{2} = \sum_{k} \left[ \mu(\alpha + \mu \omega^{4} + \beta \zeta) \left( -\frac{b^{2}}{\partial \zeta} \frac{\partial b}{\zeta} \right) + \beta \mu \delta^{-1} \right]$$

$$B = \sum_{k} \frac{\partial}{\partial \mu} |H - H_{e}|^{2} = \sum_{k} (\alpha + 2\mu \omega^{4} + \beta \zeta) D^{-1}$$

$$a = \sum_{k} \frac{\partial^{2}}{\partial \zeta^{2}} |H - H_{e}|^{2}$$

$$= \sum_{k} \left[ \mu(\alpha + \mu \omega^{4} + \beta \zeta) \left( 2b^{-3} \left( \frac{\partial b}{\partial \zeta} \right)^{2} - b^{-2} \frac{\partial^{2} b}{\partial \zeta^{2}} \right) - \beta \mu^{2} 2b^{-2} \frac{\partial b}{\partial \zeta} \right]$$

$$b = \sum_{k} \frac{\partial^{2}}{\partial \mu^{2}} |H - H_{e}|^{2} = \sum_{k} 2\omega^{\mu} b^{-1}$$

$$c = \sum_{k} \frac{\partial^{2}}{\partial \mu^{2}} |H - H_{e}|^{2} = \sum_{k} \left[ (\alpha + 2\mu \omega^{4} + \beta \zeta) \left( -b^{-2} \frac{\partial b}{\partial \zeta} \right) + \beta b^{-1} \right]$$

,

and the LSE iterative solution is:

$$\binom{5}{m}_{new} = \binom{5}{m} - \frac{1}{\alpha b - c^2} \binom{Ab - Bc}{Ba - Ac}$$

## APPENDIX E

# Damping Ratio from Integral of Transfer Function

The damping ratio, mass, and damping coefficient may be calculated from integrals of the system transfer function. This method is an alternative to the single point or curve fit techniques described above (Appendices C and D). Assuming a single mode transfer function:

$$H = \frac{\alpha}{f} = \frac{-\omega^2/m}{\omega_n^2 - \omega^2 + i 2 \int \omega_n}$$

it may be shown that the damping coefficient and mass are given by:

$$C_{S} \approx \frac{\int_{0}^{\infty} \frac{J_{m}H}{\omega} R_{m}}{\int_{0}^{\infty} \frac{|H|^{2}}{\omega^{2}} d\omega}$$

$$m = \frac{\pi/2}{\int_0^{bo} \int_{W}^{h} dw}$$

and then the damping ratio is  $\int C_s/2m\omega_n$ .

To apply this result to experimental data, the transfer function is integrated through each mode from  $0.8\omega_n$  to  $1.2\omega_n$ . Correcting for the finite limits, we obtain:

$$m = \frac{1510}{\int_{-80}^{1.200} \int_{-100}^{100} H} \partial w$$

$$5 = \frac{.33}{\omega_n} \frac{\left(\int_{-\frac{1}{2}\omega_n}^{\frac{1}{2}\omega_n} \frac{J_m H}{\omega} \frac{\Omega_n}{\omega}\right)^2}{\int_{-\frac{1}{2}\omega_n}^{\frac{1}{2}\omega_n} \frac{IHI^2}{\omega} \frac{\Omega_n}{\omega}}$$

$$C_{s} = 195.4 \qquad \frac{\int_{-1.2\omega_{u}}^{1.2\omega_{u}} \int_{-1.2\omega_{u}}^{1.2\omega_{u}} \int$$

with dimensions  $[H] = g/1000 \text{ lb}, [\omega] = Hz, [m] = lb, and [C_g] = lb/fps.$ Note that the result for C<sub>g</sub> is independent of the limits of integration; compare with the expression in Appendix C. For extremely close modes it may be necessary to integrate over a smaller range around  $\omega_n$ ; the above limits were satisfactory for the present test however. The natural frequency  $\omega_n$  may be obtained from the three-point curve fit around a local maximum, as described in Appendix D, part 3.

By calculating the system parameters from integrals of the transfer function, the effect of noise in the experimental data is reduced. However, the above expressions are not unbiased estimators of  $\int$  and  $C_s$ . With the factor  $|H|^2$  in the denominator, the calculation of  $\int$  and  $C_s$  in the presence of noise will underestimate the true values. The error in the estimate will be of the order  $K^{-1}$ , where K is the number of data records over which the spectra are averaged (see Appendix A). The estimate is conservative at least, and for the present cases the error is only 5 to 10%. If desired, the calculations of  $\int$  and  $C_s$  may be multiplied by (K+1)/K as an approximate correction for the bias error.

## APPENDIX F

# Ground Resonance Stability Criterion

# 1. References

Coleman, Robert P., and Feingold, Arnold M., "Theory of Self-Excited Mechanical Oscillations of Helicopter Rotors with Hinged Blades," NACA Rept. 1351, 1958

Deutsch, M.L., "Ground Vibrations of Helicopters," <u>Journal of the</u> <u>Aeronautical Sciences</u>, vol. 13, no. 5, May 1946

# 2. Ground resonance

Ground resonance is a mechanical instability involving the coupled dynamics of the rotor lag and hub inplane motion. An instability is possible at the resonance of the low frequency lag mode (frequency  $\Omega(1-\vartheta_{5})$ ) and a fixed system mode (frequency  $\omega_{x}$ ), if the product of the fixed system damping and the rotor blade lag damping is below a critical level dependent on the blade inertia and lag frequency.

## 3. Approximate stability criterion

The critical rotor speed for resonance is

 $SC_{crit} = \omega_{x}/(1-v_{g})$ 

and the system damping required at resonance is

$$\left(\frac{C_{x}}{\omega_{x^{2}}}\right)\left(\begin{array}{c}\frac{C_{y}}{\frac{N}{4}} \\ \frac{S_{y}^{2}}{S_{y}^{2}} \\ \frac{1-v_{y}}{v_{y}}\end{array}\right) > 1$$

where

 $\omega_x$  = support natural frequency

- $C_x = support damping$
- > = blade lag frequency (rotating)
- $C_{\mathbf{r}} = \log \operatorname{damping}$

N = number of blades

S<sub>5</sub> = first moment of blade mass about lag hinge (i.e. mass \* radial C.G. location) With dimensions  $[\Omega] = rpm$ ,  $[\omega_x] = Hz$ ,  $[v_5] = per rev$ ,  $[C_x] = lb/fps$ ,  $[C_5] = ft-lb/rad/sec$ , and  $[S_5] = slug-ft$ , the stability criterion is:

$$S_{crit} = \left(\frac{60}{1-\vartheta_{5}}\right) \omega_{x}$$

$$C_{5} > \frac{K}{C_{x}/\omega_{x}^{2}}, \quad k = 39.4 \frac{N}{4} S_{5}^{2} \frac{1-\vartheta_{5}}{\vartheta_{5}}$$

Usually the required lag damping for stability ( $C_{5}$ ) is increased by a margin of 30 to 50% to obtain an engineering estimate of the stability boundary.

This criterion is based on the assumption of a small ratio of blade mass to the rotor support mass, which is usually quite true. For extremely small fixed system damping this approximate criterion may not be conservative however. In general a detailed analysis of ground resonance stability is recommended.

## APPENDIX G

Rotor Test Apparatus Shake Test Data

The tables of this appendix present the data for the resonant frequencies of the hub transfer functions (lateral acceleration due to lateral force, and longitudinal acceleration due to longitudinal force). The following configurations were tested:

Table G1.	Short struts
Table G2.	Short struts, balance locked
Table G3.	Short struts, with strut dampers (8 shocks)
Table G4.	Long struts
Table G5.	Long struts, balance locked
Table G6.	Long struts, with strut dampers (8 shocks)

The following quantities are given in the tables: the resonant frequency  $\boldsymbol{\omega}$  (Hz); the amplitude of the hub response H (g/1000 lb and in/1000 lb); the phase of the response  $\boldsymbol{\lambda}$ H (degrees); the fixed system damping of the mode C<sub>s</sub> (lb/fps); the damping ratio  $\boldsymbol{\zeta}$  (per-cent of critical damping); and the amplitude of the exciting force F (rms lb, with "D" indicating discrete frequency excitation). Several sweeps of discrete frequency excitation in the vicinity of resonances were made, and the data are given for the entire sweep as well as for the peak.

The hub response and damping coefficient data for the long struts, lateral shake, balance free and locked (runs 17 and 18, Tables G4 and G5) are somewhat uncertain because of a problem with the accelerometer calibration. However, the conversion factor (g/volt) used for these two runs was certainly within 25% of the correct factor. The frequency and damping ratio data are not affected by this problem.

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anc	3	×	Ŧ	H N	്	\$	F rms 1b	<b></b>	<u>-</u>
Ъ.	Hz	g/1000 1b	1n/1000 lb	deg	1b/f <b>ps</b>	% critical	D=discrete	·	
	lateral m	modes							
3/2	2.06	- 61		27	300		b 38		
11	2.08	.52		29	286		b 24		
ľ,	2.10	-84		44	334		5 3L		
บั	21.2	1.14		29	tzΓ		82 Q		
25	41.2	1.37		81	300		<b>Δ30</b>		
Ē	91.2	1.20		و =	3) e		<b>b</b> 30		
72	81.2	1.05		135	286		6 34		
5	2.20	14.		153	276		D 30		
21	22.2	.60		157	282		538		
23	2-24	.46		163	272		D 34		
ЗI	م2.2	.40		165	288		D 46		
3/30	2.06	·59		31	348		<b>A 8</b> 0		
21	2.08	.70		39	366		D 70		
14	2.10	56.		53	352		D 62		
ال	21.2	61.1		ዓዛ	348		D c4		
72	2-14	1.12		511	338		D 70		
18	2.16	86.		126	44 M		D 68		
28		<b>،</b> 6		136	055		D 62		
20		:15		145	326		D 72		
22		99. •		152	310		DJL		
సే	2.24	٠5٩		158	<b>9</b> 82		D 74		
32		. 48		163	266		P-D		
AHC 167	17							0 	G P O 74 794 585/5956

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				Table G1.	<pre>31. (concluded)</pre>	led)				
Run/	3	н	Н	( <b>1</b> ,		/uni:	3	н	н	i <b>.</b>
<b>د</b> بن	Чz	£/1000 lb	1n/1000 1	n rms lb		д ——	Hz	g/1000 lb	1n/1000 lb	rms lb
	longitudi	longitudinal modes					lateral	ral modes		
14	10.0	1.06	11.	86		3/8	و 23.0	2.93	. o5	40
ر		• • •	,06	24			6	2.95	So.	60
		.92	.10	62			10	2-94	ъ°.	78
2/4	14.1	69.	·04	98		3/8	g 27.3	2.49	.03	40
د		ا <del>ن</del>	40.	24			٩	2.31	£0.	60
7		:15	40	62		-	10	2.19	.03	78
214	25.2	3.28	So.	86						
و		2.97	40.	24						
٢		3.05	So.	62						
34										
2/4	28.5	1.54	-02	98						
و		1.50	20.	24						
		1.40	202	62						
2/4	31.0	1.69	.02	86						
و		16.1	-02	24						
7		1.45	.02	62						
2/4	35.0	2.10	20、	26						
و		2.22	20.	24						
		1.52	20.	62						
LYL JAT	2								94,5	42G P O 74 794 585/5956

72G P O 74 794 585/5956

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			_				 			 		_				 Ŏ	F I	200	)R	<u>ຊ</u> ບ 	AL	<u></u>		<u></u>		
																										☆GFO *4 *94 585/5956
. ted.	rms lb	D=discrete		156	150	130	156	150	130			89	146	142	D 72											
Short struts, balance locked.	3	🦗 critical		6.1	1.5	2.3	1.2	1.5	1.7				9.1	1.9												
ort struts,	ບ້	lb/fps		540	444	814	3404	4158	4832			384	282	176	290											
Table G2. Sh	ЧH	de <u>ខ</u>		-23	-52	- 46	-154	- 145	141-				76	153	151											
Tal	n:	in/1000 lb		، اون	1.50	1.44	. o3	503	50.			2.03	2.63	2.01	19:1											
	н	g/1000 1b	al modes	.33	.79	っし.	61.	12 .	. 20		modes	1.25	1.63	1.26	62.											
	3	Hz	longitudihal modes	2.32	2.27	2.26	29.T	2.9.1	1.97		lateral mo	2.45	2.45	2.46	2.45						-					
	Run			10/8	σ	5	8/01	σ	51			1/6	2	η	و											ABC 167

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	- <b>X</b> -	s lb		0		٩	٩															565/585 162 12 DAUS
		rms (		36	76	36	96	 											   			12 04:
	н	1n/1000 lb		. o 3	₽o.	20.	20.															
	н	g/1000 1b	modes	1.78	2.22	1.92	: 85															
	3	Hz	lateral I	23.4	23.0	28.5	6.92															
	fun/	rt.		۹/۴	ы	٩ / 4	ហ															
(ed)						ř		 		 					 							
G2. (concluded)																						
. Table G2.	<u>`</u> 4	rms lb		28	<u></u> So	28	80	28	80	82	80		28	80								
	щ	1n/1000 1b		.08	.o7	20,	20-	40.	40.	20.	20-		10.	10.								
	н	g/1000 1b	Mal modes	.90	.74	.52	84,	2.42	2.48	1.30	1. 29		1.47	1.50								
	3	Hz	longitulinal modes	10.1	10.0	15.4	15.3	26.2	25.3	31.5	31.2		35.0	35.2								
	/ung	, ,		9/Q	۲	10/01	-	9/01	5	10/6	r		5 10/6	7								LJL VAL

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3	н	Н	Ч н	ບິ	Ś	н Пара	
Ηz	g/100C 1b	in/1000 lb	deg	1b/fps	5 critical	D = discrete	
long1tu	longitudinal modes						
59.1	60 ·	.32	-105	3442	4.4	64	
1.68	,0 <b>1</b>	、30	-102	3652	4.0	132	
0L. 1	٩o.	٠30	- 9 Z	3702	5.4	104	
1.70	01·	·35	-135	2298		D 38	
1.70	۲٥.	42.	-135	3308		869	
1.70	80.	92.	-132	261S		D160	
4.96	.25	01.	-11-	3476	1.2	64	
4.81	51.	<b>9</b> 0.	<u> ე</u> - ე _	6318	1.1	132	
5.0	ما ا .	وه.		6100		104	
5.00	-29	-12	-110	3138		82 q	
5.00	-12	40.	1 <b>6</b>	8634		D 100	
5.00	٩٥.	٤٥.	- 89	10900		D134	
S %	· Z3	.07	-103	4790	σ	उ	
5.70	51.	·04	-109	8486	で	132	
5.70	.13	、04	- 1:5	7948	٩	104	
5.80	.27	.0 <b>%</b>	-111	3906		<b>D42</b>	
5.80	21.	40.	- 11	99 66		<b>D100</b>	
7.56	80.	20.	-112	16556		64	
7.64	0];	.02	0 41-	8632		132	
	-						

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				Table G3.	. (continue <sup>d</sup> )	( <sub>2</sub> i			
/un <sub>4</sub>	3	r.	н	КH	ບິ	5	F rms lb		
		g/1000 lb	dI 0001/n1	deg	lb/fps	Z critical	D=discrete		
	longitud1	longitudipal modes							
61/21	9 5.08	.12		- 80	8390		D 102		
8		51.		- 86	8344		D 102		
13		51·		-91	8634		D 100		
1		12		-94	8130		D 100		
ふ		.13		-94	7436		5 94		
5	ļ	511		-13	7192		۵۹۵		
~		13		86	68 So		2 b Q		
23		41 ~		76-	Liez		44 Q		
ね		41.		-105	6364		260		
25		hi.		80 1	たいての		D at		
えが		41,		-113	5766		5 90		
12/12	2 5.00	۰۲۹		- 110	3138		D18		
L2		•19		- 164			<b>D27</b>		
12/14	H 5.00	٩٥.		-88	109 10		D67		
12/28		٩٥		-88	104 66		577		
ARC 167	167							-     	·····································

1 modes	H In/1000 11 10/1000 11 10/1000 11 10/1000 11 10/1000 11 10/1000 11 10/1000 11	LH deg J2 60	cs Ib/fps 1952 2120 1856 1856 1856 1856 1856 1380 2120 2540 2540 2040 2100	S critical 3.9	rms <sup>1b</sup> rms <sup>1b</sup> D= discrete 64 156 122 122 126 126 134 166	
Hz lateral mo lateral mo l.95 l.95 l.95 l.88 l.88 l.88 l.88 l.88 l.88 l.88 l.8	╌╪╉╌╂╶╋╌╉╶╋╶╉╴╢╴╫╌┾╌┾╌┾╴		1952 1952 2120 1856 1856 1918 1380 1380 2120 2540 2040 2040 2040 2040	3.9 3.9	D= discrete 64 156 134 166 122 122 134 166	
		12 50 60	1952 2120 1856 1856 1380 1380 1380 1380 2520 2540 2040 2040 2040	<del>د</del> ب	64 156 156 166 122 030 134 166	
		12 60	1952 2120 1856 1918 1918 1380 1380 752 2540 2040 2100 1954	Ŀ	64 156 134 166 122 230 64 156 134 166	
		72	2120 1856 1918 1918 1380 752 752 2720 2720 2720 2100 1954	б. М	156 134 166 122 122 64 136 134 166	
		72 60	1856 1918 1380 1380 2520 2040 2040 2040 2100	e. Έ	134 166 122 122 0 30 64 156 134 166	
		72 60	1918 1380 752 2720 2040 2040 2100	б- М	166 122 122 0 30 64 136 134 166	
		72 60	1380 752 2720 2040 2040 2100	<del>د</del> .	122 D 30 64 156 134 166	
		ŝ	752 2720 2040 2100 1954		D 30 64 156 134 166	
			2720 2040 2100 1954		64 156 134 166	
			2720 2040 2100 1954		64 -56 134 166	
			2040 2100 1954		156 134 166	
			2100		134	
			1954		166	
	94.					
	.39		04.22		122	
2.32 .14	, 25	146	1360		b So	
3.54 .22	81.	108	8682	8.1	156	
3.53 .23	8(.	101	2956	2.4	134	
3.6 .21	91.		3258		166	
352 .18	<del>4</del> -	123	32.08	2.3	122	
3.58 .13	01.	135	3654		D54	

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Pt Stand								
	7.	H	۲H	ى <sup>م</sup>	5	.∺ Mrs 1b		
Hz	g/1000. 1b	41 0001/ui	deg	lb/fps	or critical	Drdiscrete		
lateral	mpdes							
12 1.84	-31		41	758		0 Z C		
13 1.88	56.		60	752		A 30		
	-31		68	1202		242		
151 151	92.		109	1380		4t 4		
<b></b>	.22		119	9851		₽ 50		
1	-11		121	1836		D 54		
	<b>н</b> .		141	1362		D 54	-	
	21.		139	4422		<b>b</b> 58		
20 2.16	01.		150	2(22		D 54		
	<b>5</b> .		141	8262				
	01.		134	774		D 60		
	1.		138	2772		<b>b</b> 52		
	51.		94(	1860				
	21.		185			D 58		
8/27 3.50	4.		119	5514		b 50		
	.12		130	4206		D 50		
	.13		135	2654				
	.12		131	4444		550		
							~	

					Table Gu.		Long struts.		
Hz $g/100(1.1)$ in/1000 1b         deg $1b/fps$ $o$ critical           longituital moles. $3.3$ $77$ $3.544$ $3.2$ l-56 $0.8$ $3.3$ $77$ $3.544$ $3.2$ l-b7 $0.8$ $3.3$ $77$ $3.544$ $3.2$ l-b7 $0.8$ $3.3$ $91$ $3766$ $2.3$ l-b7 $0.9$ $3.5$ $91$ $3744$ $3.2$ l-b7 $0.9$ $3.5$ $91$ $3744$ $3.2$ l-b7 $0.9$ $3.344$ $1.2$ $3.94$ $3.2$ l-b7 $0.9$ $3.7$ $3.94$ $3.2$ $3.94$ $3.2$ $4.04$ $7.5$ $.78$ $.417$ $126$ $802$ $2.5$ $4.05$ $1.90$ $.97$ $122$ $0.7$ $3.7$ $2.5$ $0.7$ $3.94$ $1.3$ $4.05$ $1.96$ $.92$ $2.32$ $0.532$ $1.3$	Run/ Ft	3	н	н	H 🖌	ບ <sup>ຜ</sup>	م	H Tms lb	
Jongituation         Jongituation           1-56 $\cdot \circ 8$ $\cdot 33$ 77 $3 \leq 44$ $3.2$ $44$ 1-b7 $\cdot \circ 8$ $\cdot 35$ $31$ $3144$ $111$ $111$ 1-b7 $\cdot \circ 8$ $\cdot 35$ $47$ $3144$ $111$ $111$ 1-b3 $\cdot \circ 7$ $\cdot 57$ $47$ $1246$ $53$ $11$ 1-b3 $\cdot \circ 7$ $\cdot 57$ $47$ $1246$ $53$ $1344$ $513$ 1-b3 $\cdot 32$ $\cdot 78$ $95$ $1226$ $513$ $4$ 1-b3 $\cdot 47$ $1266$ $877$ $100$ $532$ $12$ $4 \cdot \circ 5$ $1 \cdot 406$ $\cdot 877$ $100$ $532$ $13$ $4$ $4 \cdot \circ 5$ $1 \cdot 406$ $\cdot 87$ $100$ $532$ $13$ $4$ $4 \cdot \circ 5$ $1 \cdot 406$ $532$ $122$ $532$ $132$ $4$ $4 \cdot \circ 5$ $1 \cdot 406$ $532$ $523$		Ηz	g/100( 15	in/1000 lb		1b/fps		D = discrete	
$1 \in L_{0}$ $\cdot \circ R$ $\cdot 33$ $77$ $3 \leq 44$ $3 \cdot 2$ $41$ $1 \cdot \upsilon 7$ $\cdot \circ R$ $\cdot 2 R$ $31$ $3144$ $3 \cdot 2$ $11$ $1 \cdot \upsilon 7$ $\cdot \circ R$ $\cdot 3 \leq 7$ $\cdot 3 \leq 7$ $3344$ $3 \cdot 2$ $11$ $1 \cdot \upsilon 7$ $\cdot \odot 7$ $\cdot 5 7$ $48$ $1344$ $6 \cdot 0$ $11$ $1 \cdot 3 +$ $\cdot \cdot 1 = 7$ $\cdot \cdot 1 = 7$ $\cdot \cdot 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$ $-1 - 1 = 7$		longitudi	hal mode.						
1.67 $.08$ $.28$ $91$ $3966$ $2.3$ $12$ $1.63$ $.07$ $.35$ $3344$ $11$ $1.84$ $.20$ $.57$ $48$ $1346$ $b1$ $1.984$ $.20$ $.57$ $48$ $1346$ $b1$ $1.98$ $.32$ $.78$ $95$ $11220$ $b1$ $1.98$ $.32$ $.78$ $95$ $1220$ $b1$ $4.04$ $.75$ $.47$ $126$ $802$ $2.5$ $12$ $4.05$ $1.07$ $.65$ $67$ $12$ $4$ $4.05$ $1.07$ $.65$ $67$ $12$ $11$ $4.05$ $1.07$ $.65$ $67$ $12$ $4$ $7.20$ $.01$ $.01$ $25$ $6536$ $13$ $4$ $7.20$ $.01$ $.01$ $252$ $676$ $13$ $4$ $7.20$ $.01$ $.01$ $.02$ $.01$ $232$ $44$ $7.20$ $.01$ $.01$ <td>13/6</td> <td>1. S lo</td> <td>80.</td> <td>.33</td> <td>トト</td> <td>3544</td> <td>3.2</td> <td>44</td> <td></td>	13/6	1. S lo	80.	.33	トト	3544	3.2	44	
$1.63$ $\cdot \cdot \circ q$ $\cdot 35$ $3344$ $111$ $1.84$ $\cdot 20$ $\cdot 57$ $48$ $1346$ $b11$ $1.98$ $\cdot 32$ $\cdot 37$ $95$ $1220$ $b1$ $4.04$ $\cdot 32$ $\cdot 47$ $126$ $802$ $233$ $14$ $4.05$ $\cdot 78$ $\cdot 47$ $126$ $892$ $233$ $111$ $4.05$ $\cdot 78$ $\cdot 47$ $126$ $892$ $233$ $111$ $4.05$ $1.97$ $\cdot 653$ $61$ $613$ $613$ $111$ $4.05$ $1.94$ $\cdot 87$ $100$ $532$ $133$ $4$ $7.20$ $\cdot 09$ $\cdot 01$ $25$ $250$ $686$ $51$ $51$ $7.20$ $\cdot 09$ $\cdot 01$ $233$ $270$ $636$ $51$ $51$ $3.94$ $\cdot 38$ $70$ $523$ $51$ $51$ $51$ $51$ $3.94$ $\cdot 38$ $70$ $523$ $446$ $51$ $51$ $51$ $51$	r	1.67	.08	·28	٩I	3966	2.3	120	
1.84 $.20$ $.51$ $48$ $1.346$ $b1$ $1.98$ $.32$ $.78$ $95$ $1220$ $D1$ $4.04$ $.75$ $.45$ $142$ $648$ $1.3$ $4$ $4.04$ $.75$ $.47$ $126$ $802$ $2.5$ $12$ $4.05$ $1.07$ $.65$ $67$ $78$ $11$ $11$ $4.05$ $1.07$ $.65$ $67$ $78$ $12$ $4$ $4.05$ $1.07$ $.65$ $67$ $532$ $26$ $51$ $4$ $4.05$ $1.46$ $.87$ $100$ $532$ $1.3$ $4$ $7.20$ $.09$ $.01$ $25$ $666$ $51$ $51$ $4$ $7.20$ $.09$ $.01$ $25$ $656$ $51$ $51$ $4$ $7.20$ $.09$ $.01$ $25$ $656$ $51$ $51$ $51$ $7.20$ $.01$ $25$ $26$ $686$ $51$ $51$ $51$	8	1.63	60.	·35		3344		811	
$1.98$ $\cdot .32$ $.78$ $95$ $1220$ $13$ $4$ $4.04$ $.75$ $.475$ $142$ $648$ $13$ $4$ $4.02$ $.78$ $.47$ $126$ $802$ $2.5$ $13$ $4.02$ $.78$ $.47$ $126$ $802$ $2.5$ $13$ $4.01$ $1.07$ $.653$ $01$ $01$ $01$ $01$ $4.01$ $1.07$ $.653$ $013$ </td <td>26</td> <td>481</td> <td>.20</td> <td>.57</td> <td>847</td> <td>1346</td> <td></td> <td>\$ 100</td> <td></td>	26	481	.20	.57	847	1346		\$ 100	
$4.04$ $\cdot 75$ $\cdot 47$ $142$ $643$ $1.3$ $1.1$ $4.02$ $\cdot 78$ $\cdot 47$ $126$ $802$ $2.5$ $12$ $4.01$ $1.07$ $\cdot 653$ $61$ $1.3$ $11$ $4.05$ $1.46$ $\cdot 87$ $100$ $532$ $2.5$ $12$ $4.05$ $1.46$ $\cdot 87$ $100$ $532$ $1.3$ $4$ $7.20$ $\cdot 09$ $\cdot 01$ $2.5$ $656$ $1.3$ $4$ $7.20$ $\cdot 09$ $\cdot 01$ $2.5$ $666$ $513$ $4$ $7.20$ $\cdot 09$ $\cdot 01$ $2.5$ $666$ $513$ $4$ $7.20$ $\cdot 09$ $\cdot 01$ $2.5$ $666$ $513$ $4$ $7.20$ $\cdot 09$ $\cdot 01$ $2.5$ $20$ $686$ $513$ $3.94$ $\cdot 38$ $-25$ $220$ $686$ $513$ $513$ $4.01$ $1.44$ $\cdot 88$ $70$ $528$ $516$ $516$ $4.04$ $1.32$ $100$ $532$ $446$ $516$ $516$ $4.04$ $1.32$ $100$ $532$ $446$ $516$ $516$ $4.04$ $1.32$ $100$ $532$ $446$ $516$ $516$ $4.04$ $1.32$ $100$ $532$ $446$ $516$ $516$ $4.04$ $1.32$ $100$ $532$ $446$ $516$ $516$ $4.04$ $1.32$ $107$ $532$ $446$ $516$ $516$ $4.04$ $1.32$ $100$ $512$ $446$ $516$ <td< td=""><td>45</td><td>85.1</td><td>55.</td><td>81:</td><td>95</td><td>1220</td><td></td><td>8819</td><td></td></td<>	45	85.1	55.	81:	95	1220		8819	
$4.04$ $\cdot 75$ $\cdot 45$ $142$ $648$ $1.3$ $1.1$ $4.02$ $\cdot 78$ $\cdot 47$ $126$ $802$ $2.5$ $12$ $4.01$ $1.07$ $\cdot 653$ $67$ $1.3$ $11$ $4.05$ $1.07$ $\cdot 653$ $67$ $1.3$ $11$ $4.05$ $1.46$ $\cdot 87$ $100$ $532$ $2.9$ $5$ $7.20$ $\cdot 07$ $\cdot 01$ $25$ $653$ $1.3$ $4$ $7.20$ $\cdot 07$ $\cdot 01$ $25$ $676$ $51$ $3.34$ $\cdot 38$ $\cdot 25$ $20$ $686$ $51$ $3.34$ $\cdot 38$ $\cdot 70$ $528$ $50$ $51$ $4.06$ $1.44$ $\cdot 88$ $70$ $528$ $5$ $4.04$ $1.32$ $\cdot 37$ $132$ $1446$ $0$ $4.04$ $1.32$ $\cdot 32$ $100$ $532$ $0$ $4.04$ $1.32$ $\cdot 32$ $105$ $51$ $0$ $4.08$ $\cdot 146$ $\cdot 32$ $100$ $532$ $0$ $4.04$ $1.32$ $\cdot 32$ $105$ $528$ $0$ $4.04$ $1.32$ $\cdot 32$ $105$ $532$ $0$ $4.04$ $1.32$ $1.32$ $1.46$ $0$ $4.04$ $1.32$ $1.32$ $1.49$ $0$ $4.04$ $1.32$									
$4, o 2$ $\cdot 78$ $\cdot 47$ $126$ $8o 2$ $2 \cdot 5$ $12$ $4, o 1$ $1: o 7$ $\cdot 65$ $u 7$ $b 7$ $1: 3$ $11$ $4, o 3$ $1: 4 b$ $\cdot 87$ $1o 0$ $532$ $b 7$ $b 0$ $7: 2o$ $\cdot 07$ $\cdot 01$ $25$ $b 532$ $b 1$ $b 1$ $7: 2o$ $\cdot 07$ $\cdot 01$ $25$ $b 532$ $b 1$ $7: 2o$ $\cdot 07$ $\cdot 01$ $25$ $b 26$ $b 1$ $7: 2o$ $\cdot 07$ $\cdot 01$ $25$ $b 26$ $b 1$ $3: 34$ $\cdot 38$ $\cdot 25$ $220$ $686$ $b 1$ $3: 34$ $\cdot 38$ $\cdot 25$ $220$ $686$ $b 1$ $3: 34$ $\cdot 38$ $\cdot 25$ $220$ $686$ $b 1$ $3: 34$ $\cdot 38$ $\cdot 25$ $220$ $686$ $b 1$ $3: 34$ $\cdot 38$ $70$ $526$ $b 1$ $b 1$ $3: 34$ $\cdot 32$ $1.49$ $\cdot 252$ $220$ $686$ $b 1$ $4: o 1$ $1: 44$ $\cdot 88$ $70$ $5226$ $b 1$ $4: o 1$ $1: 44$ $\cdot 88$ $70$ $5226$ $b 1$ $4: o 4$ $1: 32$ $1: 97$ $1: 32$ $1: 44$ $b 1$ $4: o 4$ $1: 32$ $1: 90$ $532$ $4 44_6$ $b 1$ $4: o 4$ $1: 32$ $1: 90$ $532$ $4 44_6$ $b 1$ $4: o 4$ $1: 32$ $1: 90$ $532$ $4 44_6$ $b 1$ $4: o 4$ $1: 32$ $1: 90$ $1: 32$ $1: 90$ <td>13/6</td> <td>4.04</td> <td>15 15</td> <td>-45</td> <td>142</td> <td>849</td> <td>1.3</td> <td>цц</td> <td></td>	13/6	4.04	15 15	-45	142	849	1.3	цц	
4.01 $1.07$ $.65$ $67$ $1.3$ $1.3$ $1.1$ $4.05$ $1.446$ $.87$ $100$ $532$ $b.0$ $7.20$ $.09$ $.01$ $25$ $b53$ $b.3$ $7.20$ $.09$ $.01$ $25$ $b53$ $b.1$ $7.20$ $.09$ $.01$ $25$ $b53$ $b.1$ $7.20$ $.09$ $.01$ $25$ $b65$ $b1$ $7.20$ $.09$ $.01$ $25$ $b65$ $b1$ $3.84$ $.38$ $.25$ $20$ $686$ $b1$ $3.92$ $.51$ $.38$ $27$ $686$ $b1$ $3.92$ $.76$ $528$ $b26$ $b1$ $3.92$ $.76$ $528$ $70$ $526$ $b1$ $4.01$ $1.32$ $.79$ $5226$ $b1$ $b1$ $4.04$ $1.32$ $.79$ $5226$ $b1$ $b1$ $4.04$ $1.32$ $.79$ $1.32$ $1.446$ $b1$ $4.04$ $1.32$ $.79$ $1.32$ $1.49$ $b1$ $4.04$ $1.32$ $1.32$ $1.49$ $b1$ $b1$ $4.04$ $1.32$ $1.49$ $51$ $51$ $51$ $4.04$ $1.32$ $1.49$ $51$ $51$ $51$ $4.04$ $1.32$ $1.41$ $51$ <td< td=""><td>7</td><td>4.02</td><td>8 L.</td><td>.47</td><td>921</td><td>802</td><td>2.5</td><td>120</td><td></td></td<>	7	4.02	8 L.	.47	921	802	2.5	120	
$4.05$ $1.446$ $\cdot 87$ $100$ $532$ $b.3$ $b.3$ $7:20$ $.09$ $.01$ $25$ $6530$ $1.3$ $4$ $7:20$ $.09$ $.01$ $25$ $6530$ $1.3$ $4$ $3.84$ $.38$ $.25$ $220$ $686$ $D_1$ $3.84$ $.38$ $.25$ $220$ $686$ $D_1$ $3.94$ $.38$ $.25$ $220$ $686$ $D_1$ $3.92$ $.76$ $.686$ $D_1$ $4.01$ $1.44$ $.88$ $70$ $526$ $D$ $4.03$ $1.32$ $.79$ $122$ $446_0$ $D$ $4.04$ $1.32$ $.79$ $122$ $446_0$ $D$ $4.04$ $1.32$ $.79$ $122$ $446_0$ $D$ $4.08$ $.54$ $.32$ $169$ $D$ $4.08$ $.54$ $.32$ $169$ $D$	∞	4.01	1.07	و الا الا	69	819	1.3	811	
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$7.20$ $.01$ $.01$ $25$ $6530$ $1.3$ $4$ $3.34$ $.38$ $.25$ $20$ $686$ $D1$ $3.34$ $.38$ $.25$ $20$ $686$ $D1$ $3.72$ $.51$ $.38$ $.25$ $20$ $686$ $D1$ $3.94$ $.38$ $.25$ $20$ $686$ $D1$ $3.95$ $.76$ $686$ $D1$ $D1$ $4.01$ $1.34$ $.83$ $70$ $526$ $D1$ $4.01$ $1.34$ $.83$ $70$ $526$ $D$ $4.04$ $1.32$ $.76$ $522$ $D$ $D$ $4.04$ $1.32$ $.70$ $522$ $D$ $D$ $4.04$ $1.32$ $.74$ $524$ $D$ $D$ $4.04$ $1.32$ $.74$ $52$ $D$ $D$ $4.04$ $00$ $532$ $D$ $D$ $D$ $4.04$ $1.32$ $1.32$ $1.44_0$ $D$ $D$									
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3:34 $:38$ $:25$ $20$ $686$ $D1$ $3:72$ $:51$ $:38$ $:25$ $20$ $686$ $D1$ $3:72$ $:51$ $:38$ $:27$ $686$ $D1$ $3:72$ $:51$ $:38$ $27$ $686$ $D1$ $3:72$ $:51$ $:38$ $27$ $686$ $D1$ $4:01$ $:144$ $.88$ $70$ $528$ $D$ $D$ $4:01$ $:144$ $.88$ $70$ $522$ $D$ $D$ $4:04$ $1:32$ $.79$ $522$ $4446$ $D$ $4:04$ $1:32$ $.79$ $122$ $4446$ $D$ $4:08$ $.54$ $.32$ $167$ $D$ $D$ $4:08$ $.54$ $.32$ $167$ $D$ $D$									
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3.84 $.38$ $.25$ $20$ $686$ $01$ $3.72$ $.51$ $.38$ $.25$ $20$ $686$ $01$ $3.96$ $.76$ $.38$ $27$ $686$ $01$ $4.00$ $1.36$ $.83$ $70$ $538$ $01$ $01$ $4.01$ $1.44$ $.88$ $70$ $526$ $01$ $01$ $4.01$ $1.44$ $.88$ $70$ $526$ $01$ $01$ $4.03$ $1.446$ $.98$ $70$ $526$ $01$ $01$ $4.04$ $1.32$ $.79$ $1.32$ $.446$ $01$ $01$ $4.04$ $1.32$ $.79$ $1.32$ $1.46$ $01$ $01$ $4.08$ $.54$ $.32$ $1.09$ $01$ $01$ $01$ $01$									
3.92 $.51$ $.38$ $29$ $(-51)$ $.38$ $29$ $(-52)$ $(-51)$ $(-$	13/47	3.84	38	. 25	20	ବଃଚ		D102	
3.9b $.7b$ $.47$ $40$ $686$ $D$ $4.0c$ $1.3u$ $.83$ $70$ $538$ $D$ $4.0c$ $1.44$ $.88$ $7c$ $526$ $D$ $4.0j$ $1.44$ $.88$ $7c$ $526$ $D$ $4.0j$ $1.46$ $.98$ $7c$ $526$ $D$ $4.0j$ $1.32$ $.79$ $100$ $532$ $D$ $4.0j$ $1.32$ $.79$ $132$ $446$ $D$ $4.09$ $54$ $.32$ $169$ $132$ $446$ $D$ $4.08$ $.54$ $.32$ $169$ $132$ $446$ $D$	48	3.92	:51	38.	29	229		D 100	
$4. \infty$ $1:34$ $83$ $70$ $538$ $D$ $4.01$ $1.44$ $.88$ $7L$ $526$ $D$ $4.03$ $1.44$ $.88$ $7L$ $526$ $D$ $4.04$ $1.32$ $.779$ $132$ $446$ $D$ $4.08$ $.54$ $.32$ $167$ $446$ $D$ $4.08$ $.54$ $.32$ $167$ $446$ $D$	49	3.96	9L.	-47	40	989			
4.01       1.44       .88       76       526       D         4.03       1.46       .98       100       532       D         4.04       1.32       .79       132       446       D         4.04       1.32       .79       132       446       D         4.08       .54       .32       169       9       D         4.08       .54       .32       169       9       0	5	4.00	1.36	.83	70	538			
4.03       1.46       .98       100       532       0         4.04       1.32       .79       132       446       0         4.08       .54       .32       169       0       0         4.08       .54       .32       169       0       0	53	4.01	1.44	88.	مر	526			
4.04 1.32 .79 132 446 D 4.08 .54 .32 169 D	Ţ	4.03	1.46	86.	100	532			
4.08 ·54 ·32 169 D	5I	4.04	1.32	62.	132	446			
	52		·54	• 32	169				

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				Table G4.	. (continued)	[ [ ]		
/un,_	3	н	Н	Чн М	ບິ	5	F rms lb	
Εt	Ηz	g/1000 1b	1n/1000 1b	deg	1b/fps	🌾 critical	D=discrete	
	long1 tudi	longitudinal modes						
13/18	1.52	.05	.22	17	1690		86 9	
19	1.56	.05	22.	17	1594		D 114	
ని	09.1	و ۱۰	.26	19	1528		D loc	
12	1.64	.08	•31	25	8951		D 88	
22	5.68	-10	·34	29	1592		D 92	
23	1.72	11.	<b>1</b> 8.	30	1562		D 112	
24	96.1	13	24.	3 ه	1 50 2		D 10Z	
52		ه ( ۲	84.	40	1404		401 A	
26		-19	15.	48	1346			
34	1.85	.08	.23	148	2352		D 82	
27		90.	81.	154	2442		D 100	
30		·05	۰۱ ۲	156	2950		86 Q	
33		20.					D 100	
31	1.12	£0.	•10	159	3608		811 <b>T</b>	
36	1.93	.02						
29		201	50.	158	7220		b 124	
32	2.00	10.					801 V	
R		10.					D 96	
13/39	1.80	-12	.36	42	1318		061 Q	
37	1.84	15	.43	31	1240		P 184	
41	1.88	-18	·52	38	1204		D 170	
42	26.1	.25	ر <i>م</i> ا.	53	1186		D 188	
43	96·1	.31	08.	<b>[</b> [	1180		D 182	
44	2.00	61.	.46	139	1348		D 168	
45		、32	& <i>L</i> :	95	1224		D 188	
<b>9</b> 4	2.04	50.	.11	٥٩١	2840		<u>5</u> 236	
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	Nodal Vass v	lb		74500	74800			52800	58600	37600	40000	37900										
	ت. م ا	1)= discrete		. 29		D 86	D 44	62	116	62	116	D 38	D 64		 D 44	D 40	D 38	D 44	b 64			
ued) –	5	1 cal		5.5	5.8			4.6	4.6	8.	6.	0.1				4	2					
G4. (continued)	ບິ	1b/fps		1658	2082	1010	1640	2378	3358	534	616	672	936		ها اه	682	672	606	936			
Table C4.	<b>Α</b> H	deg		-126.5	- 107	-122	- 112	- 70	-96	-89	-109	18 -	- 85		-137	001 -	18 -	-55	10 20 1			
	н	in/1000 1b		.40	££.	49.	.45	.28	.22	29.	.58	.62	.45		.47	.62	29.	·57	.45			
	н	g/1000 lb	modes	.22	.20	.41	.26	.20	<b>یا</b> د	1. 29	81.1	1.30	2P.		•8¢	1-27	1.30	1.19	·13			
	3	Hz	lateral m	2.31	2.32	2.52	2.38	2.68	2.66	4.51	4.47	4.50	4.48		4.44	4.48	4.50	4.52	4.48			
	/une	Pt.		17/1	7	1	25	リノレリ	2	1/41	2		77 44		17/33	82	32	62	26			

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Pun/								
. ,	3	<b>n</b> :	7:	КH	റ <b>ാ</b>	5	rms lb	
I t		g/100% lb	1n/1000 lb	deg	1b/fps	h critical	D=discrete	
	lateral m	mþdes						
17/6	2.12	80.	81.	- ادد	1246		D 100	
7	2.20	11.	22.	-163	181		86 0	
<b>D</b> *	2.24	21.	.25	- 160	1168		N 94	
5-	\$ 2.2	51-	.28	- 157	2611		4 44	
<u> </u>	2.32	-17	.30	- 155	1132		D 100	
=	2.36	• 2 •	.35	- 149	2 6 1 1		P 94	
2	04.2	-22	٩٤.	941-	1234		1 98	
ñ	2.44	.25	14.	- 144	8011		A 106	
21	2.48	•30	.47	-135	1144		D 104	
14	2.52	-42	.64	-122	1010		18 V	
1	2.53	<b>6</b> 0.	51.	- 45	3630			
2	2.56	• 0رو	.12	-59			D 94	
17/64	2.32	.20	.38	-139	1404		D 50	
22	2.36	.23	.42	-119	1706		8+ Q	
25	2·38	2 ک	.45	-112	1640		D 44	
81	2.40	.25	.43	-96	1281		D 46	
24	24.2	61.	.30	- 51	2222		P 44	
5	2.44	21.	.20	-52	3092		87 J	
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3 5	;							
~n	×.	5.		 /un <sub>d</sub>	3	r.	¥	ír,
311	g.'100f lb	in/1000 lb	the lb	 2	Ηz	g/1000 1b	1n/1000 1b	JTES 10
long1 tu <sup>A</sup> 1	longitudihal modes				lateral	E		
<u>اه ل</u>	.62	.05	42	 17/3	22.7	1.01	20.	3•
	:15	و ، 0	52					
14.1	20.	50.	24	 17/3	28.8	2.51	<b>£</b> 0.	30
	19.	:03	52	 				
25.9	2.37	.04	42					
	2.50	40.	S2	 				
28.0	9.1	20.	42					
	ه، ۱	201	52					
31.4	1.38	20.	42.	 				
31.0	1.47	20.	SZ					
35.2	1.58	10.	42					
	1.50	10.	52	 				

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							<b></b>			 						г— <b>т</b>	DC	RIC	AU BO	AL )R	P/ Ql	AGI JAI	3					
	Modal Mass M	lb																		32000	27400	26300						
	F This lb	D= discrete		106	154	0 70		106	154		D86	D 68	D 70	84 Q	D 82					64	118	D22		A 32	D 22	22 0	6 28 A	<b>b</b> 30
balance locked.	2	🖗 critical		1.6	1.0															ۍ و	8.	1.0			T	Φ	4	
Long struts, 1	ເທ	1b/fps		912	804	<i>h</i> S4		10160	6760		422	442	454	4 8 C	432					272	286	292		298	286	292	290	262
Table G5. Lu	<b>A</b> H	deg		118	135	83			49		33	64	83	102	130					- 24	- 46	- 56		- 16	-135	- 56	- 31	0 M I
Ta	Н	11/1000 lb		.60	1.07	l. 39		-02	.02		-82	1.30	1.39	1. 30	1.11					ا الاہ	l. 35	ا. او ه		0 9	1.40	1. 60	1.22	1.04
	н	g/1000 15	mal moder	.58	1.04	1.28		IS	91.		<i>۹۲</i> ،	61.1	1.28	1. 20	50.1				mþdes	1.44	1.63	- 90		۲0.	1.62	1.90	1.47	1.26
	3	Hz	longitudihal moder	3.09	3.07	3.00		8.1	Er.F		<b>مام</b> 2.2	2.99	3.00	10.5	3.04				lateral m	3.48	3.44	3.40		3. 3o	3,36	3.40	3.42	3.44
	Run/	- -		14/1	3	6		1/41	ຕ		14/11	13	σ	21 47	01					1/81	2	2		ا 8/گ	6	7	=	10

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"un/ Pt     H     H     H       Pt     Hz     g/1000 lb     In/1000 lb       18/3     Z4.4     1.35     .02       18/3     Z8.2     2.45     .03       18/3     Z8.2     2.45     .03
Hz       g/1000 lb         lateral modes       24. L         27.1       1.35         28.2       2.45         28.2       2.45         28       1.75
lateral modes         24. L       1. 30         22.1       1. 35         22.1       1. 35         28.2       2.45         28.2       1. 75         28       1. 75
24.4 1.30 22.1 1.35 28.2 2.65 28.2 1.75 28 1.75
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			Table G6.	G6. (continued)	nuec)		
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2.32	-12		- 113	3360		298	
2.40	-16		-111	2610		260	
2.48	.23		-105	2030		D 100	
2.49	52.		- 104	1932		D lot	
2.5.2	-10		-10			2 96	
2-49	. 25		122	1676		D 154	
2.52	. 29		511-	1546		D 156	
2.56	.35		66-	1430			
2.60	.o7		- 22	2480		D 166	

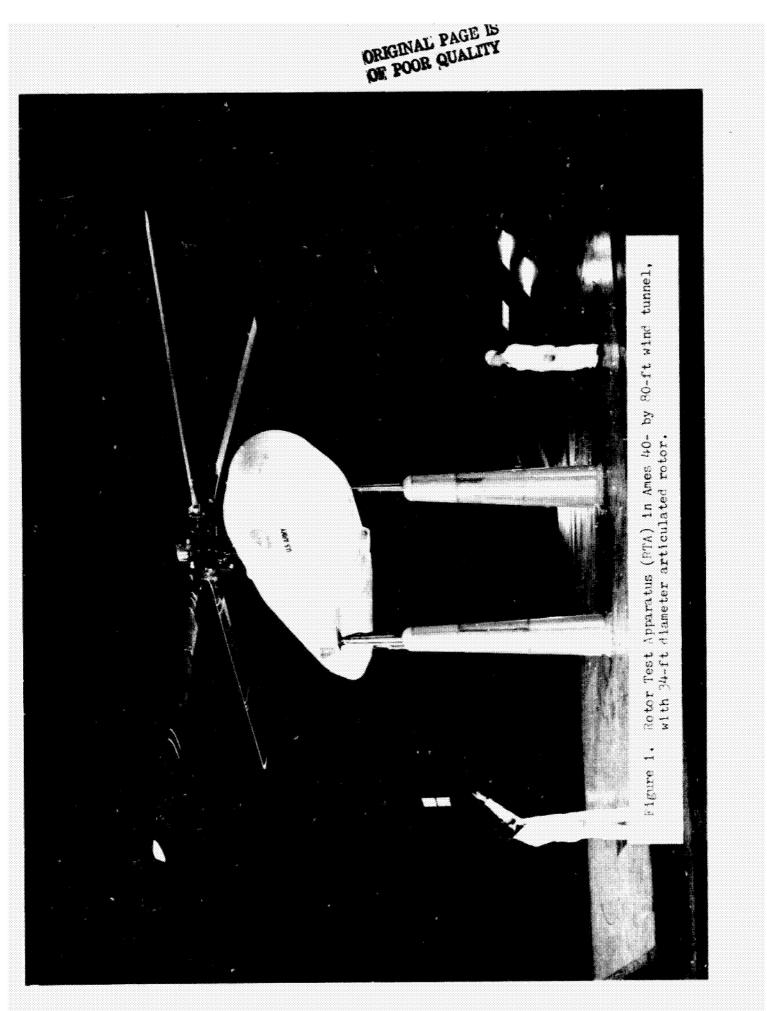
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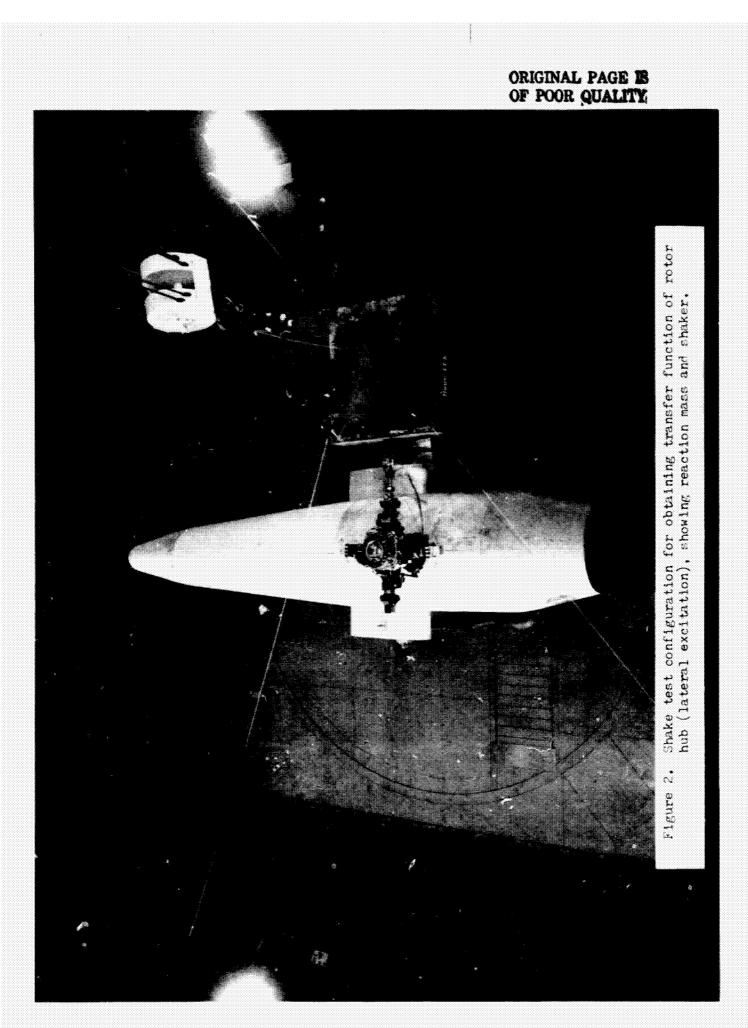
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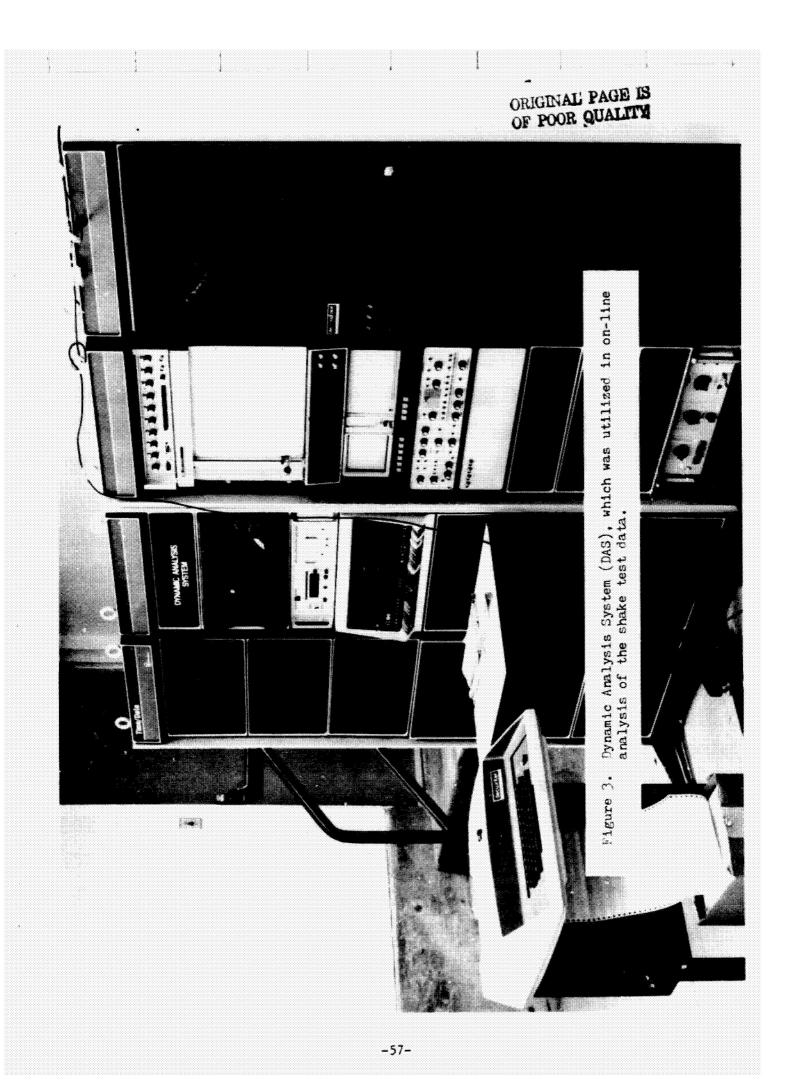
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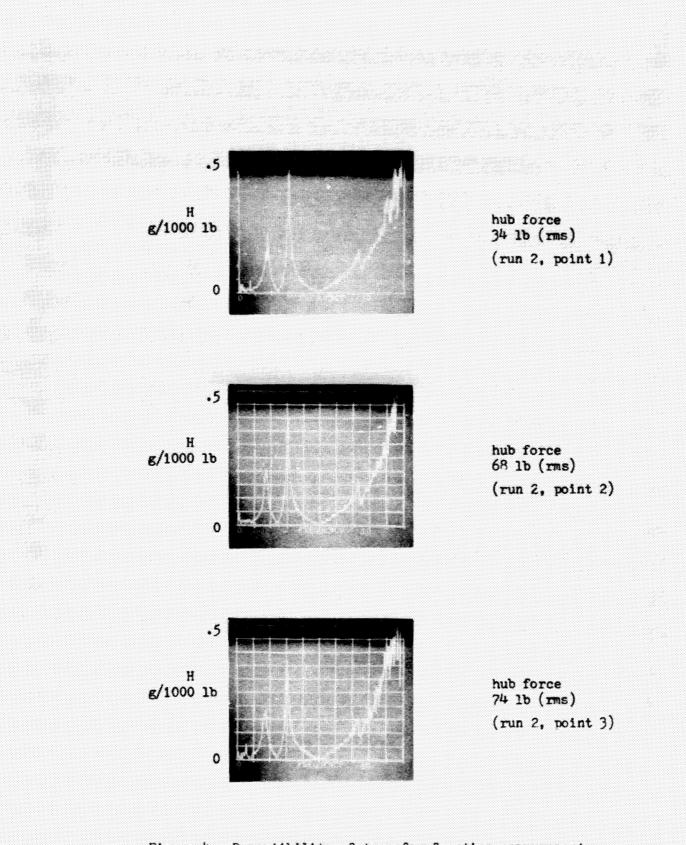
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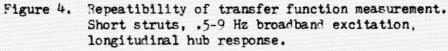
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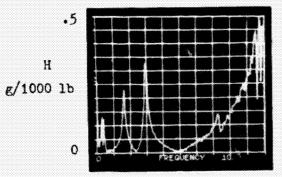




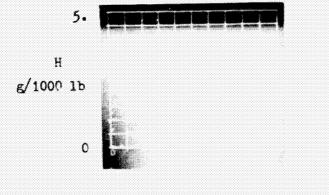








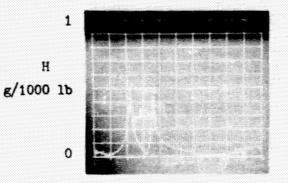
.5-9 Hz broadband excitation, longitudinal hub response (run 11, point 1)



.5-35 Hz broadband excitation, longitudinal hub response

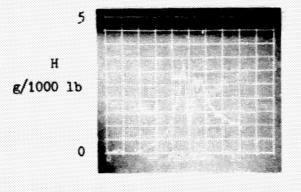
(run 2, point 7)

Figure 5. Short struts.



.5-9 Hz broadband excitation, lateral hub response

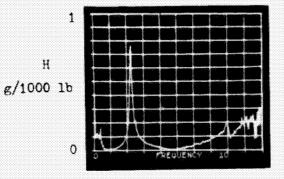
(run 3, point 2)



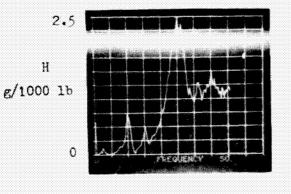
.5-35 Hz broadband excitation, lateral hub response

(rt: 3, point 9)

## Figure 5. (concluded)

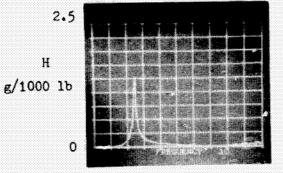


.5-9 Hz broadband excitation, longitudinal hub response (run 10, point 13)

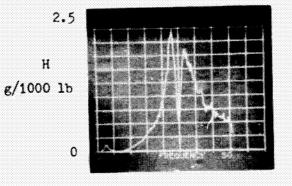


.5-35 Hz broadband excitation, longitudinal hub response (run 10, point 7)

Figure 6. Short struts, balance locked.



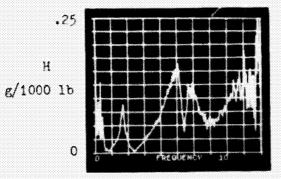
.5-9 Hz broadband excitation, lateral hub response (run 9, point 3)



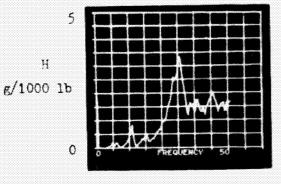
.5-35 Hz broadband excitation, lateral hub response (run 9, point 5)



(concluded).

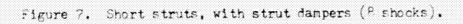


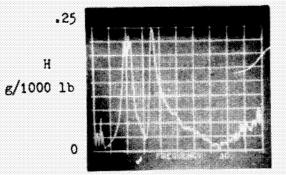
.5-9 Hz broadband excitation, longitudinal hub response (run 12, point 3)



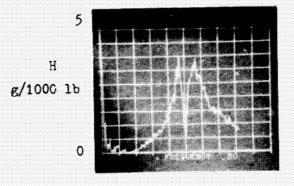
.5-35 Hz broadband excitation, longitudiral hub response

(run 12, point R)





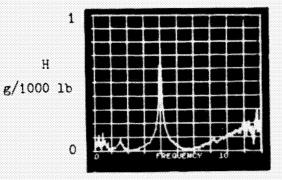
.5-9 Hz broadband excitation, lateral hub response (run 8, point 3)



.5-35 Hz broadband excitation, lateral hub response (run 8, point 8)

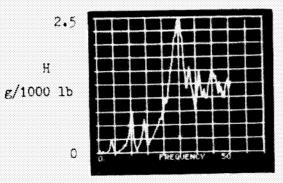


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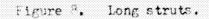
.5-9 Hz broadband excitation, longitudinal hub response

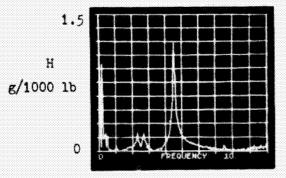
(run 13, point 6)



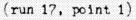
.5-35 Hz broadband excitation, longitudinal hub response

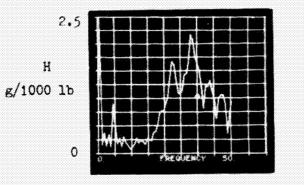
(run 13, point 10)





.5-9 Hz broadband excitation, lateral hub response



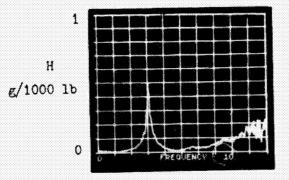


.5-35 Hz broadband excitation, lateral hub response

(run 17, point 4)

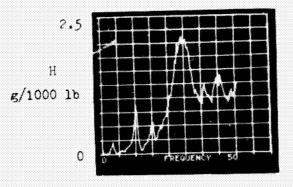


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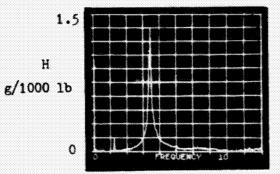
.5-9 Hz broadband excitation, longitudinal hub response

(run 14, point 2)



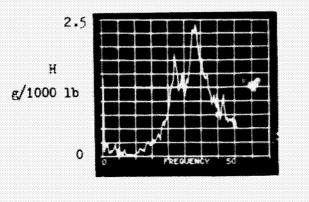
.5-35 Hz broadband excitation, longitudinal hub response (run 14, point 5)

Figure 9. Long struts, balance locked.



.5-9 Hz broadband excitation, lateral hub response

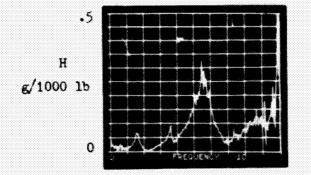
(run 1<sup>8</sup>, point 2)



.5-35 Hz broadband excitation, lateral hub response (run 18, point 4)



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.5-9 Hz broadhand excitation, longitudinal hub response

(run 15, point 1)

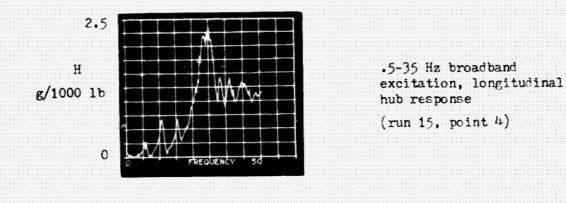
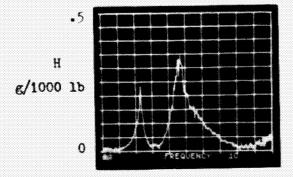
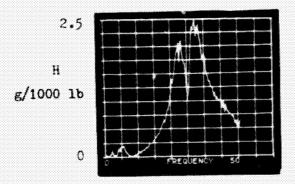


Figure 10. Long struts, with strut dampers (8 shocks).

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.5-9 Hz broadband excitation, lateral hub response (run 16, point 2)



.5-35 Hz broadband excitation, lateral hub response (run 16, point 35)



