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A STUDY OF DIGITAL GYRO COMPENSATION LOOPS

Final Report  
April 1975

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## ABSTRACT

The primary objective of this program was to demonstrate the feasibility of replacing existing state-of-the-art analog gyro compensation loops with digital computations. This objective was realized during the course of the program.

A breadboard design was established in which one axis of a Teledyne tuned-gimbal TDF gyro was caged digitally while the other was caged using conventional analog electronics. The digital loop was designed analytically to closely resemble the analog loop in performance. The breadboard was subjected to various static and dynamic tests in order to establish the relative stability characteristics and frequency responses of the digital and analog loops. Several variations of the digital loop configuration were evaluated. The results were very favorable - it appears that digital caging is indeed a practical approach.

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## I. INTRODUCTION

### Background

In January 1974 Teledyne Systems Company completed under contract to NASA Langley Research Center an "Investigation of the Application of Two-Degree-of-Freedom Dry Tuned-Gimbal Gyroscopes to Strapdown Navigation Systems"\*. During the course of that study an entirely new approach to the control and compensation of the TDF gyro, as well as accelerometers, was suggested and studied. This technique was based upon the use of "all-digital" sensor compensation loops and control functions.

An analysis of the hardware content and costs of present day inertial navigation systems showed that a significant portion, on the order of 30%, of the system, consists of analog and computer interface electronics. The advent of newly available, versatile, digital microcomputers and high-speed analog-to-digital and digital-to-analog converters now makes it practical to replace essentially all of the analog electronics by functionally equivalent digital computations.

Figure 1 shows a functional block diagram of a conventional strapdown inertial navigation system mechanization. Both the sensor compensation functions and the spin motor and pickoff excitations are generated by analog electronics which operate independently of the digital processor. The sensor torquing currents are fed through precision resistances to develop voltages which are proportional to angular rates and accelerations. These voltages are then converted into digital numbers for use in the navigation and attitude equations which must be solved by the computer.

Figure 2 shows the corresponding block diagram for a strapdown system employing digital sensor control and compensation. Here all of the compensation loop servo functions are mechanized as digital computations in the processor. The basic inputs to the A/D converter are the sensor pickoff signals rather than the restoring signals. The torquing signals are computed as digital numbers, converted to analog signals and, after power amplification, used to restore the sensors. These same digital torquing quantities may be used directly in the strapdown attitude and navigation computations as well. (In an optional configuration the actual torquing signals are also passed through the A/D converter for use in the attitude and navigation equations.)

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\*The final report of this study was published as NASA CR-132419

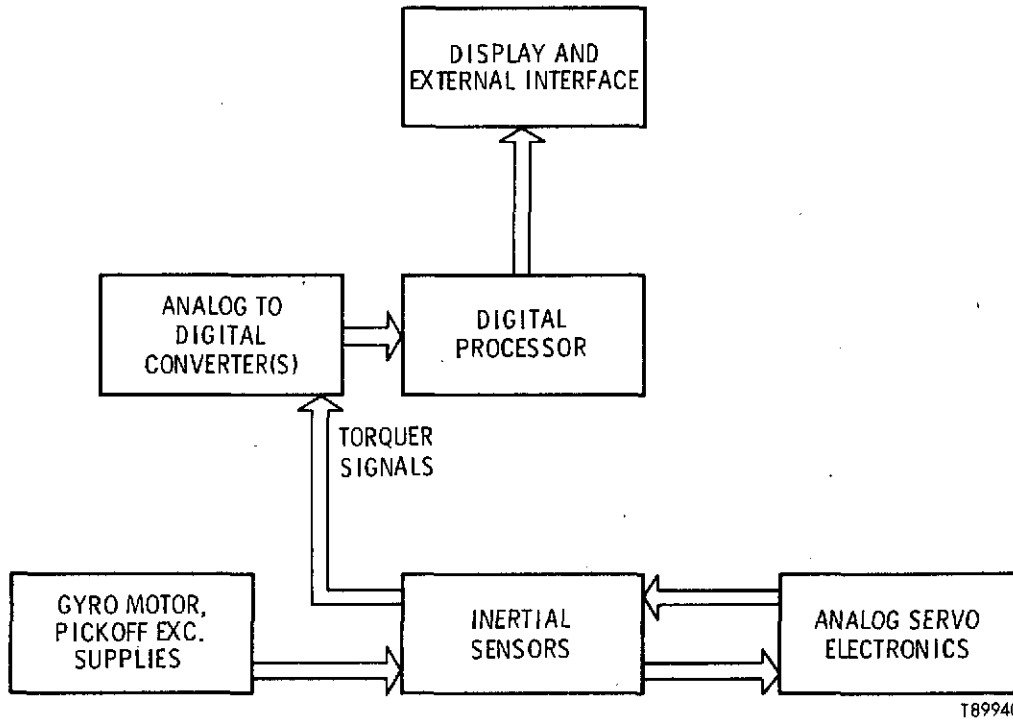


Figure 1. Functional Block Diagram of Conventional Strapdown Mechanization

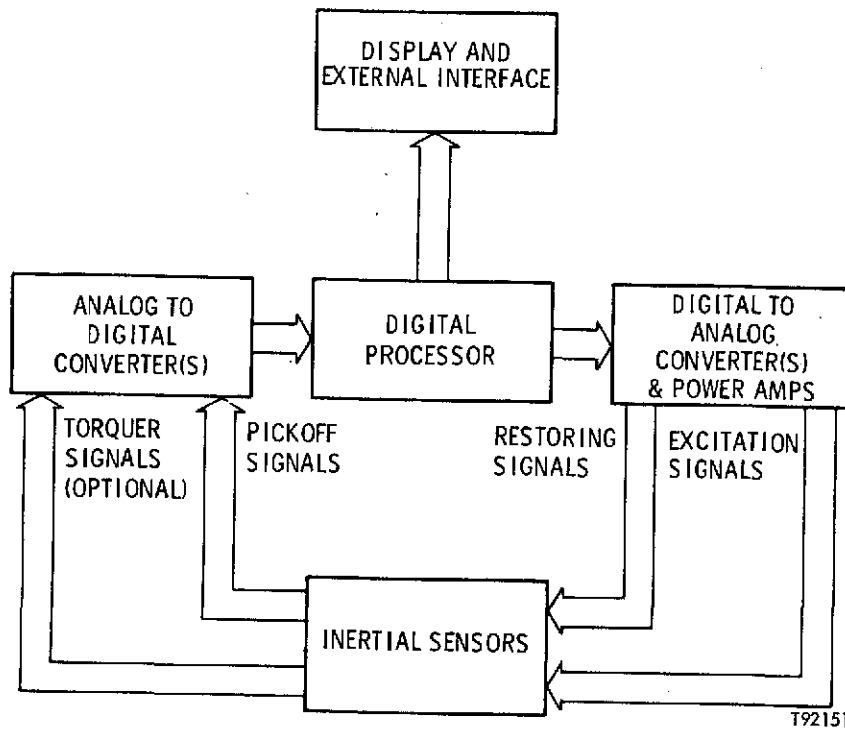


Figure 2. Functional Block Diagram of "All-Digital" Strapdown Mechanization

What is gained by such an "all-digital" approach is that the presently cumbersome and necessarily specialized analog and digital interface electronics can be virtually eliminated, being replaced by digital computations (software) performed in the computer hardware which is, in any case, required for the attitude and navigation computations. This results in substantial savings in cost, size, weight, and power consumption while simultaneously increasing the reliability of the system by reducing the component count.

### Objective

The objective of this program was to determine the feasibility of replacing present state-of-the-art analog circuits in strapdown tuned-gimbal gyro compensation circuits with their digital counterparts. This was accomplished by designing appropriate compensation loops for the dry tuned TDF gyro, selecting appropriate data conversion and processing techniques and algorithms, and, using existing laboratory equipment, breadboarding the design for laboratory evaluation.

The principal area of engineering design involved in the program was the determination of the specific software requirements for closing the instrument loops and performing the required compensation. Specific requirements relative to processing rate, word length, computer time and memory utilization were established in order that corresponding requirements for a full complement of strapdown sensors may be readily extrapolated. Additionally, appropriate analog-to-digital and digital-to-analog conversion designs were established and techniques selected which were capable of meeting these requirements.

An available dry tuned-gimbal two-degree-of-freedom gyroscope was utilized together with an electronic circuit breadboard and existing laboratory hardware to implement the digital control loop. Selection of hardware and techniques was based on the anticipated availability of proven hardware in the late 1970's. The breadboard design was evaluated using standard test and evaluation procedures.

This final report summarizes the test configuration and the program results which were obtained.

## II. ANALYSIS

The breadboard design which was established for this study, consisted of a dry-tuned two-degree-of-freedom (TDF) gyroscope with one axis being caged in a conventional manner using simplified existing "state-of-the-art" analog compensation. The second axis was caged using a digital compensation loop designed to emulate the performance of the analog compensation. Figure 3 shows a simplified block diagram of the breadboard design. An analysis of the two caging techniques employed in the design is presented in the following paragraphs.

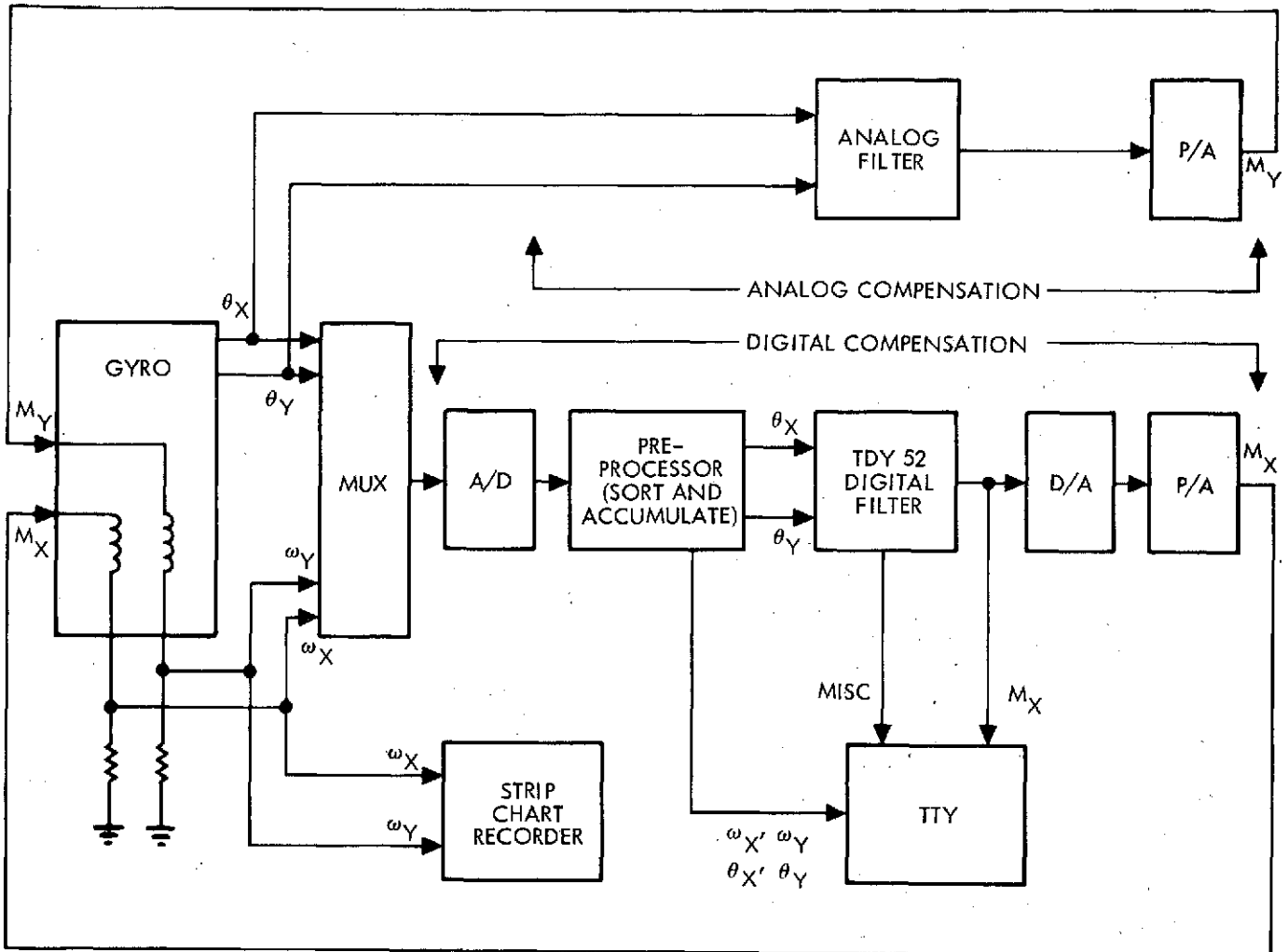
### Analog Compensation Design

The general Teledyne gyro caging loop configuration for conventional analog compensation is shown in the simplified block diagram of Figure 4. Observe that both direct and cross axis compensation is employed in this design in order to increase the loop bandwidth and reduce the rotor hangoff during acceleration inputs. In this block diagram  $\theta_X$  and  $\theta_Y$  represent the gyro pickoff angles,  $T_X$  and  $T_Y$  the gyro torques,  $P_X$  and  $P_Y$  the precessional torques resulting from rate inputs  $\omega_X$  and  $\omega_Y$ , and  $M_X$  and  $M_Y$  the rebalance torques provided by the compensation loops.

A more detailed block diagram of the compensation portions of the loop for the current Teledyne design is shown in Figure 5. This block diagram shows the actual transfer functions which are implemented in the analog electronics as well as the pickoff and torquer transfer characteristics. A derivation and analysis of this compensation design is included in NASA CR-132419. The pole-zero locations for the compensation electronics using this design are shown in Figure 6.

Concurrently with the digital loop demonstration program Teledyne has been involved in an extensive redesign effort on its conventional analog compensation electronics. This effort has as its goals improved loop performance and simpler loop design. Although work is continuing in this area, it has been found that excellent performance can be obtained with relatively simple analog transfer functions. The pole-zero configuration for one such simple loop is shown in Figure 7. This configuration provides a baseline for much of the digital loop design work which was performed during the program.





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Figure 3. Block Diagram of the System Used in the Digital Gyro-Caging Study

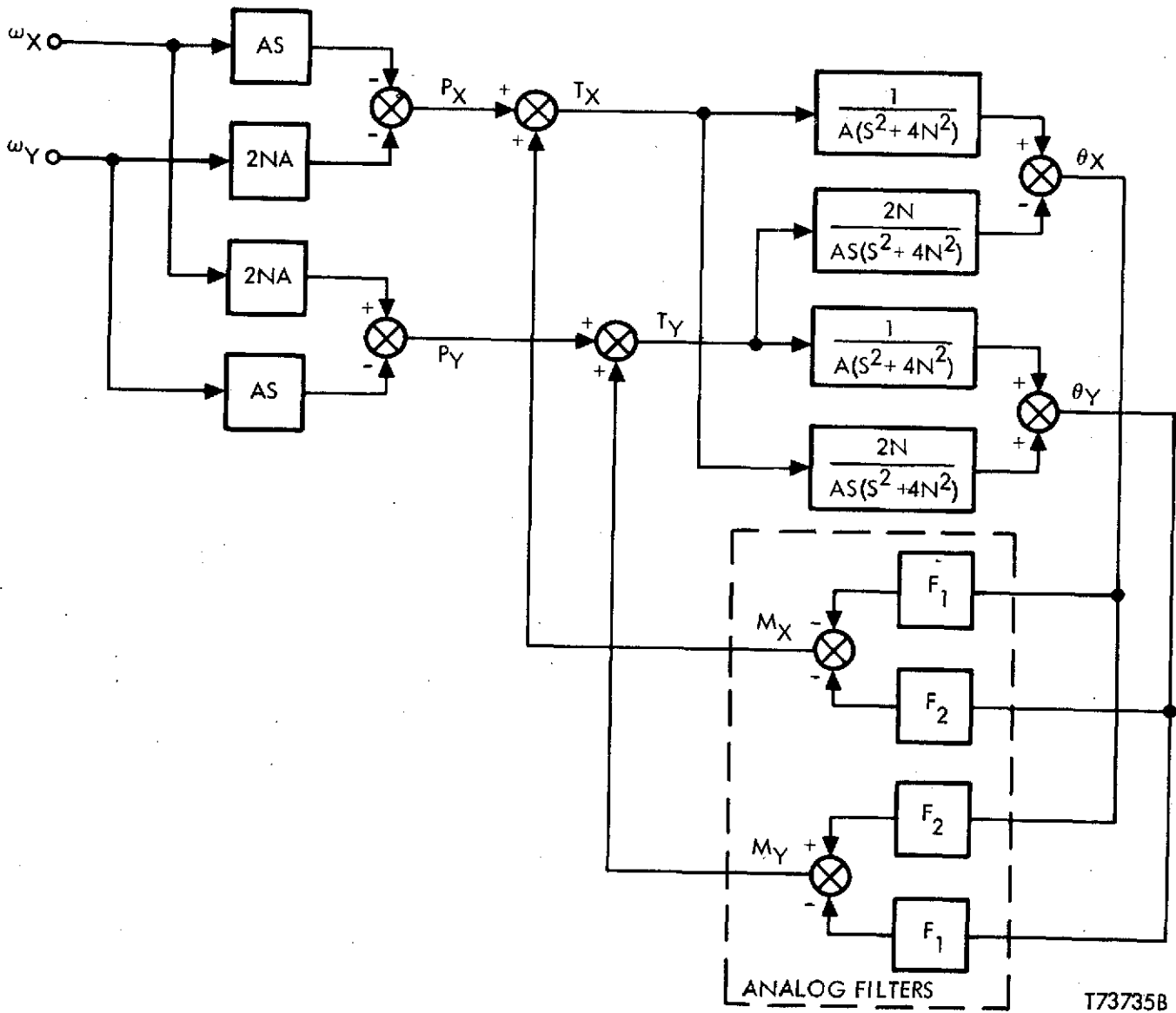
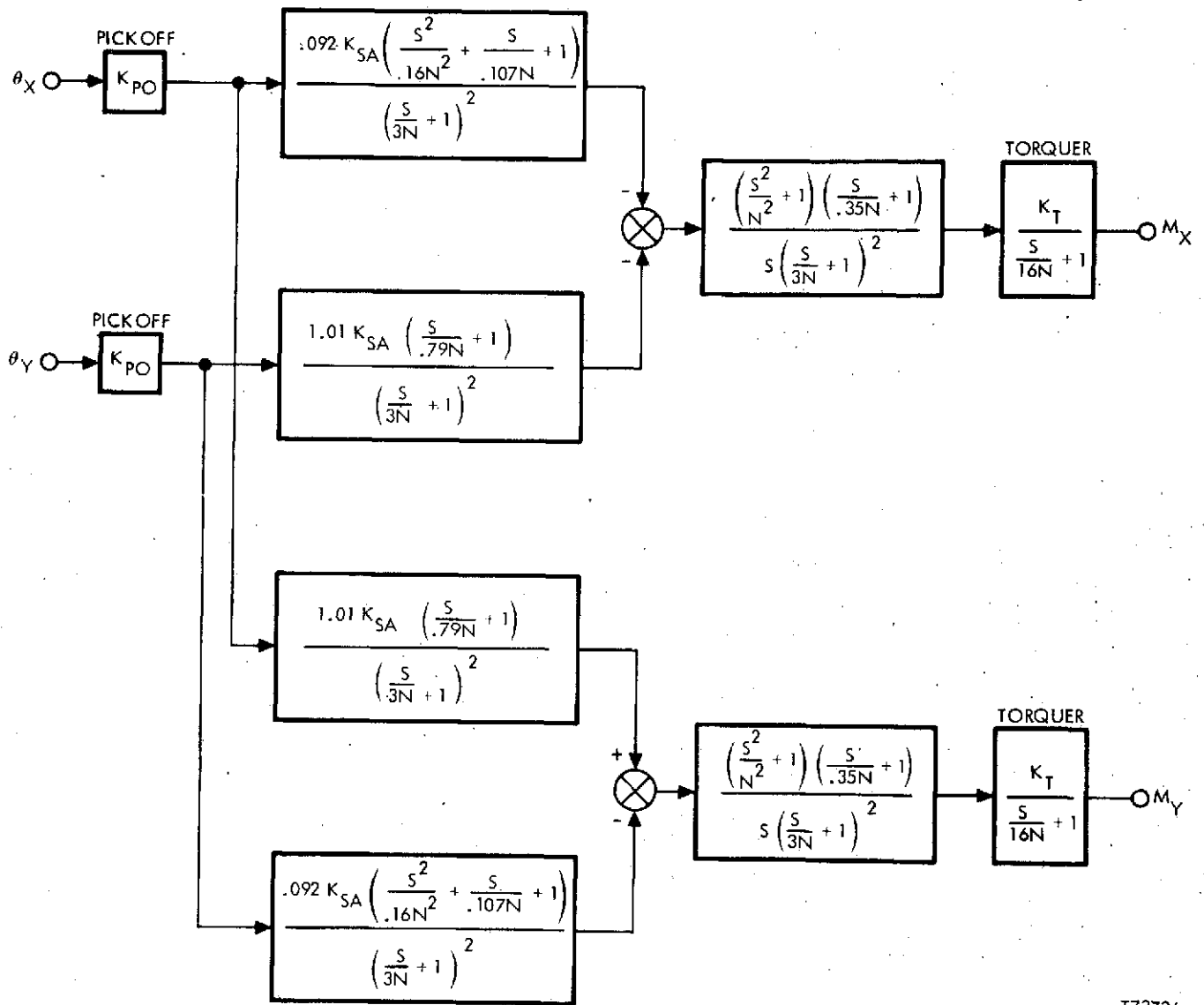


Figure 4: Block Diagram of Gyro and Caging Electronics



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Figure 5. Caging Loop Mechanization

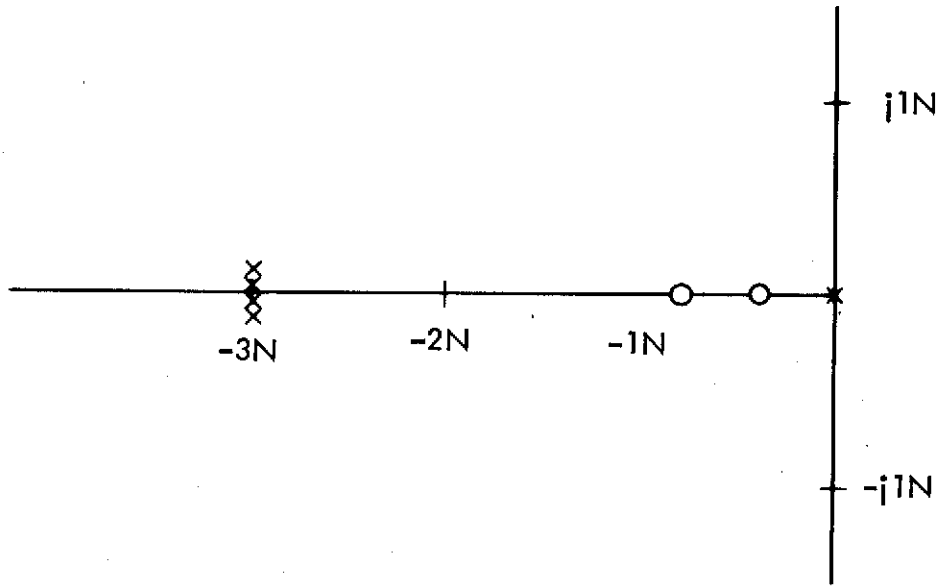


Figure 6a. Pole-Zero Locations for Cross Axis-Current Design

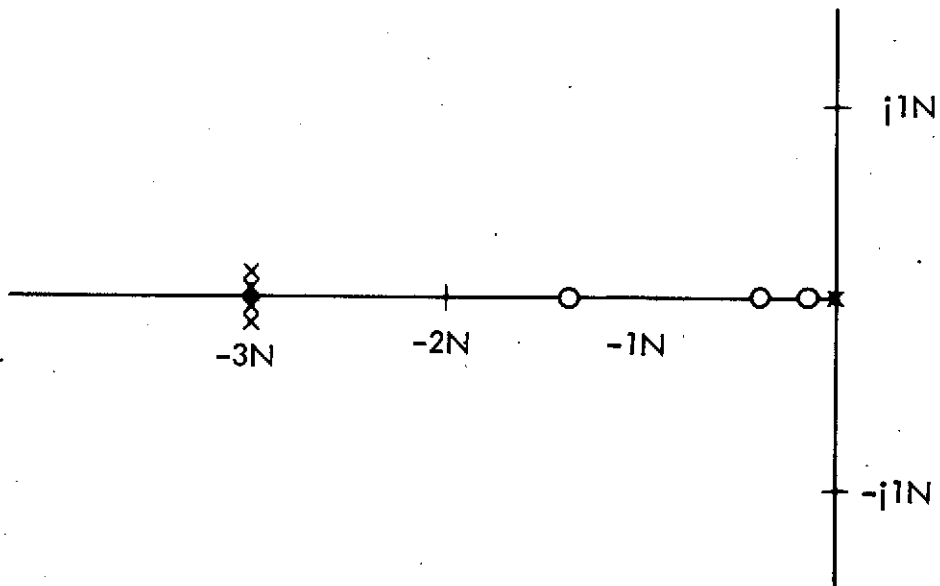


Figure 6b. Pole-Zero Locations for Direct Axis-Current Design

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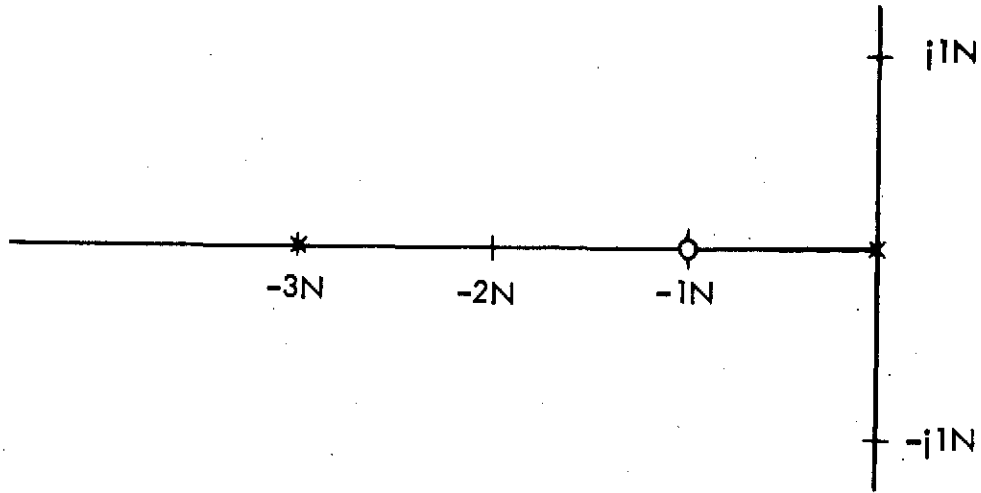
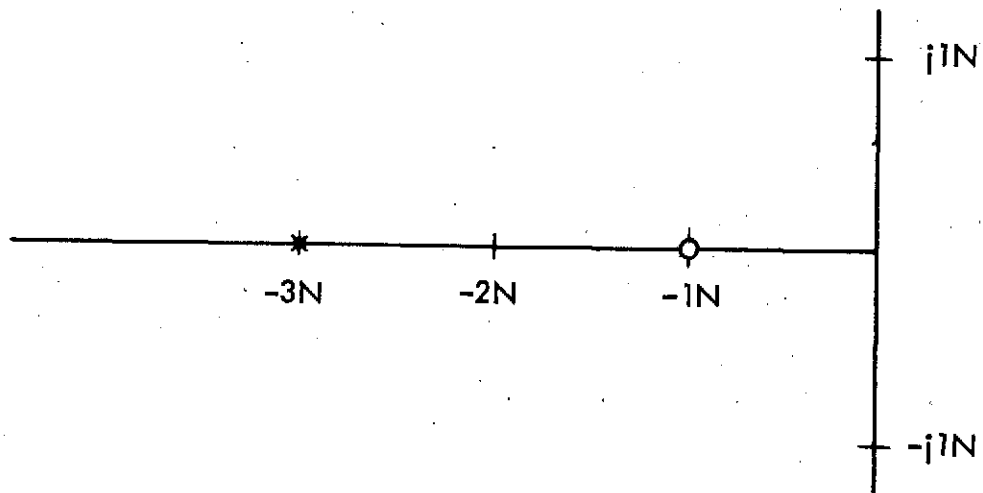


Figure 7a. Pole-Zero Locations for Cross Axis - New Design



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Figure 7b. Pole-Zero Locations for Direct Axis - New Design

## Digital Compensation Analysis

Figure 8 shows a simplified block diagram of the digital gyro caging loop. This figure should be compared with Figure 4. One of the primary objectives of the program was to design digital filters which would emulate the performance of the existing analog filter design.

The study of digital filters and digital servos has progressed rapidly in the past decade and an extensive literature now exists with regard to these subjects. Rabiner and Rader\*, for example, provides both theoretical and practical coverage of digital filtering as well as extensive bibliographies. The large variety of digital filters and the subtleties (e.g., the aliasing effect) which arise in their implementation, however, serve to maintain digital filtering as more of an art than a science.

Some "cookbook" approaches exist for obtaining digital equivalents to analog filters. Some of these have been analyzed, aided where required by simulation, in order to determine their applicability to the digital compensation loop design. In selecting a practical approach, particular attention was paid to the impact on the computer with regard to memory and time utilization. As an example, it was desirable to synthesize digital filters whose coefficients are integer powers of two, since this allows the replacement of multiply instructions with less time consuming shift instructions.

As one simple example of using the cookbook approaches, consider the bilinear transformation approach using the transformation

$$s \rightarrow \frac{1-z^{-1}}{1+z^{-1}}$$

The transfer function

$$H(s) = \frac{\frac{s}{.79N} + 1}{\left(\frac{s}{3N} + 1\right)^2}$$

appearing in Figure 5 is seen to have a zero at  $\omega_1 = .79N = 496$  rad/sec and a double pole at  $\omega_2 = 3N = 1884$  rad/sec. In order to synthesize a digital filter with these characteristics we first derive an analog filter with a zero at

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\*Rabiner, L.R. and C.M. Rader, Digital Signal Processing, IEEE Press, New York, 1972.

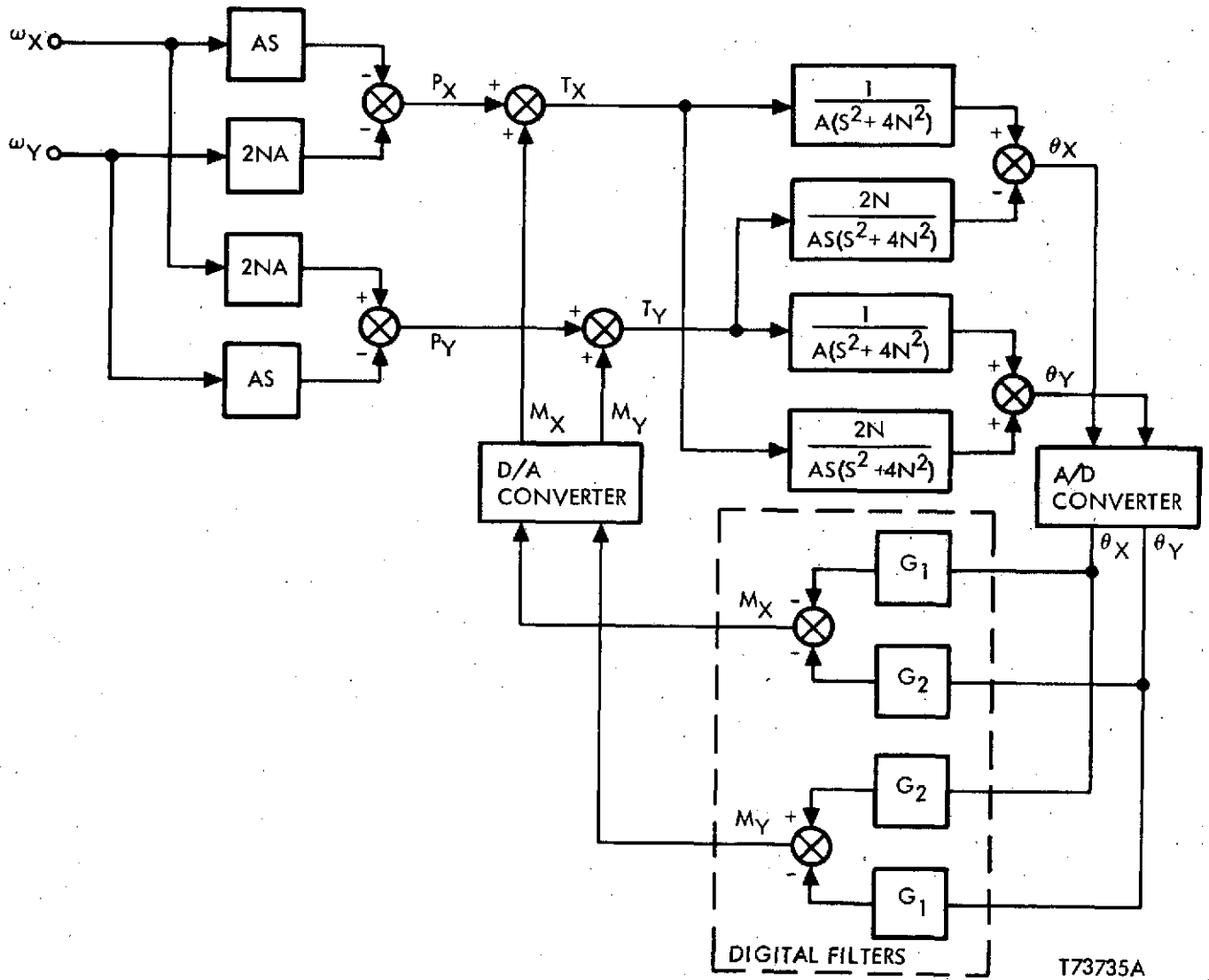


Figure 8. Block Diagram of Digital Compensation Loop

$$\omega'_1 = \tan \frac{\omega_1 \tau}{2}$$

and a double pole at

$$\omega'_2 = \tan \frac{\omega_2 \tau}{2}$$

where  $\tau$  is the computer iteration interval. Assuming, for example, an iteration rate of 200 Hz,  $\tau$  is 5 milliseconds and

$$\omega'_1 = \tan \frac{(496)(.005)}{2} = 2.91$$

$$\omega'_2 = \tan \frac{(1884)(.005)}{2} = 418.59$$

so that the "dummy" analog transfer function is

$$H'(s) = \frac{\frac{s}{2.91} + 1}{\left(\frac{s}{418.59} + 1\right)^2}$$

Finally, the digital transfer function is found by introducing the transformation

$$s \rightarrow \frac{1-z^{-1}}{1+z^{-1}} \text{ so that}$$

$$\begin{aligned} H(z) &= \frac{\frac{1}{2.91} \frac{(1-z^{-1})}{(1+z^{-1})} + 1}{\left(\frac{1}{418.59} \frac{(1-z^{-1})}{(1+z^{-1})} + 1\right)^2} \\ &= \frac{\left[\frac{1}{2.91} (1-z^{-1}) + (1+z^{-1})\right] [1+z^{-1}]}{\left[\frac{1}{418.59} (1-z^{-1}) + (1+z^{-1})\right]^2} \end{aligned}$$



$$= \frac{\left(1 + \frac{1}{2.91}\right) + 2z^{-1} + \left(1 - \frac{1}{2.91}\right)z^{-2}}{\left(1 + \frac{2}{418.59} + \frac{1}{(418.59)^2}\right) + 2\left(1 - \frac{1}{(418.59)^2}\right)z^{-1}}$$


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$$+ \left(1 - \frac{2}{(418.59)} + \frac{1}{(418.59)^2}\right)z^{-2}$$

The bracketed groups in this expression are fixed constants. Thus an exact mechnaization of this filter requires 6 multiplies and 4 adds per iteration of the computer. Observe, however, that one of these multiplications is by the number two. Thus for this operation a shift may replace a multiply instruction resulting in a substantial saving in computer time since a simple shift requires only a small fraction of the time needed for execution of a multiply instruction.

Further simplifications may be possible in this transfer function. For example, consider approximating the factor  $(1 + 1/2.91) = 1.34$  by

$$1.375 = 1 + \frac{1}{4} + \frac{1}{8}$$

Then the multiplication (of the current input) by this factor may be accomplished by a double shift, a single shift, and two additions, again effecting a substantial saving in computer time. Such approximations must be carefully analyzed, however. Working "backward" through the preceding derivation it is seen that this approximation has the effect of shifting the zero of the transfer function from  $\omega_1 = 496$  rad/sec to

$$\omega_1 = \frac{2}{\tau} \tan^{-1} (2.67)$$

$$= \frac{2}{.005} (1.21) = 485 \frac{\text{rad}}{\text{sec}}$$

In this case the effect on the filter response is probably negligible. This is not the case for all approximations which appear on the surface to be reasonable, however.

Initial efforts in designing the digital compensation filters concentrated on emulating existing "old design" analog filters as used in previous strapdown systems. The transfer functions of these analog filters are shown in the block diagram of Figure 4 and their pole-zero locations in Figure 5.

Consider first the cross axis transfer function relating  $M_Y$  to  $\theta_X$ , i. e. the y-axis torquer output to the x-axis pickoff angle. The analog transfer function is

$$\frac{M_Y(s)}{\theta_X(s)} = \frac{1.01 K_{sa} K_{po} K_T \left( \frac{s}{.79N} + 1 \right) \left( \frac{s}{.35N} + 1 \right) \left( \frac{s^2}{N^2} + 1 \right)}{s \left( \frac{s}{16N} + 1 \right) \left( \frac{s}{3N} + 1 \right)^4}$$

Since the pickoff and torquer transfer functions will exist in the digital loop in any case, they do not have to be implemented digitally. The gain factor ( $1.01 K_{sa}$ ) may also be neglected in the digital design as the gain may be provided by the power amplifier. Thus the digital transfer function to be mechanized should be equivalent to

$$H(s) = \frac{\left( \frac{s}{.35N} + 1 \right) \left( \frac{s}{.79N} + 1 \right) \left( \frac{s^2}{N^2} + 1 \right)}{s \left( \frac{s}{3N} + 1 \right)^4}$$

Using the bilinear transformation technique and assuming now an 800 Hz update rate, the dummy analog breakpoints are computed

$$\omega'_1 = \tan \frac{(2\pi)(35)}{(2)(800)} = .13832$$

$$\omega'_2 = \tan \frac{(2\pi)(79)}{(2)(800)} = .32058$$

$$\omega'_3 = \tan \frac{(2\pi)(100)}{(2)(800)} = .41421$$

$$\omega'_4 = \tan \frac{(2\pi)(300)}{(2)(800)} = 2.41421$$

Making the substitution

$$s \rightarrow \frac{1 - z^{-1}}{1 + z^{-1}}$$

the digital transfer function is found (after much arithmetic manipulation) to be

$$H(z) = 57.8787 \frac{1 - 1.68566z^{-1} + .50190z^{-2} + 1.36534z^{-3} - 1.43278z^{-4} + 3.8945z^{-5}}{1 + .65685z^{-1} - .62742z^{-2} - .74517z^{-3} - .25483z^{-4} - .02944z^{-5}}$$

In order to obtain a rough estimate of computer timing requirements for implementation of the digital loop, the numerator of  $H(z)$  was considered. The numerator was first approximated in order to eliminate the need for multiplications. Thus

$$1.68566 \approx 1 + 2^{-1} + 2^{-3} + 2^{-4} = 1.6875$$

$$.50190 \approx 2^{-1} = .500$$

$$1.36534 \approx 1 + 2^{-2} + 2^{-3} = 1.375$$

$$1.43278 \approx 1 + 2^{-2} + 2^{-3} + 2^{-4} = 1.4375$$

$$.38945 \approx 2^{-2} + 2^{-3} + 2^{-6} = .390625$$

so that the numerator is implemented as

$$\begin{aligned} \theta_x(k) - (1 + 2^{-1} + 2^{-3} + 2^{-4}) \theta_x(k-1) + (2^{-1}) \theta_x(k-2) + (1 + 2^{-2} + 2^{-3}) \theta_x(k-3) \\ - (1 + 2^{-2} + 2^{-3} + 2^{-4}) \theta_x(k-4) + (2^{-2} + 2^{-3} + 2^{-6}) \theta_x(k-5) \end{aligned}$$

(Working "backward" as before, these approximations resulted in analog breakpoints of .519N, .749N and .711N  $\pm$  j.706N, a reasonable agreement with the original transfer function.) Using the TDY-52B/IMP-16 instructions, a simple program was written to implement the equation above. The instruction breakdown was as follows

Instruction	Number	Time Per Instruction	Time (μsec)
Load	6	7.7	46.20
Store	5	9.1	45.50
Reg. Copy	1	8.75	8.75
Reg. Add	10	4.55	45.50
Add/Sub	5	7.7	38.50
Shift Rt. 1	3	10.1	30.30
Shift Rt. 2	5	14.3	71.50
Shift Rt. 3	1	17.5	17.50
			303.75 μsec

Assuming that each transfer function numerator and denominator is of roughly the same complexity, the total time required to implement the four transfer functions is

$$(303.75) \times 2 \times 4 = 2.43 \text{ msec}$$

which is approximately twice the available time for an 800 Hz update rate. Since this estimate does not include I/O processing, scaling, executive, control, etc. it was clear that much simpler processing would be required if the digital compensation loop were to be successfully implemented with the TDY-52B computer.

Fortunately, as described in Section II, efforts were underway concurrent to the digital loop program to simplify and improve analog compensation techniques. This work resulted in the designs described in the preceding section, and showed that very simple analog transfer functions could be used to obtain the desired servo loop response characteristics. Furthermore, it was decided to mechanize one axis of the gyro in an analog loop in order to more accurately compare the analog loop and digital loop responses, thus reducing the digital computations which were required. These two factors resulted in a digital loop design which could be implemented with a TDY-52B even though the update rate was increased to 1200 Hz.

The "first cut" at implementing the new transfer functions started with the analog functions whose pole-zero locations are shown in Figure 7.

$$F_1(s) = \frac{s + N}{s + 3N}$$

$$F_2(s) = \frac{s + N}{s(s + 3N)}$$

where  $F_1(s)$  is the direct axis transfer function and  $F_2(s)$  is the cross axis transfer function. Using a 1200 Hz update, the dummy breakpoint frequencies were computed to be

$$\omega'_1 = \tan \frac{(2\pi)(100)}{(2)(1200)} = .26795$$

$$\omega'_2 = \tan \frac{(2\pi)(300)}{(2)(1200)} = 1.0000$$

so that

$$F_1(z) = \frac{\frac{(z-1)}{(z+1)} + .26795}{\frac{(z-1)}{(z-1)} + 1.0000} = \frac{1.26795z - .73205}{2z} = .63398(1 - .57735z^{-1})$$

$$F_2(z) = \frac{\frac{(z-1)}{(z+1)} + .26795}{\frac{(z-1)}{(z+1)} \left[ \frac{z-1}{z+1} + 1.000 \right]} = .63398 \frac{(1 + .42265z^{-1} - .57735z^{-2})}{(1-z^{-1})}$$

Since the constant gain term can be readily implemented in the analog portion of the loop, it may be neglected. The transfer functions were further simplified to

$$G_1(z) = (1 - .5z^{-1})$$

$$G_2(z) = \frac{(1 + .5z^{-1} - .5z^{-2})}{(1-z^{-1})}$$

for easier digital implementation. This has the effect of changing  $\omega'_1$  to .333 and  $\omega_1$  (the analog loop zero) to 1.23N instead of N.

The comparison of analog and digital frequency responses is shown in Figures 9a and 9b for this configuration. It is seen that the breakpoints and low - frequency asymptotics are identical, with variations occurring at intermediate points. The high frequency performance of the digital loop is, of course, different from the analog response due to the "fold-over" effect. For this reason, the filter update rate must be sufficiently high that the deleterious effects of this phenomenon are countered by attenuation in the analog portions of the loop. (Test results indicate that 1200 Hz is the minimum update frequency required to obtain the desired response and that higher frequencies are desirable.)

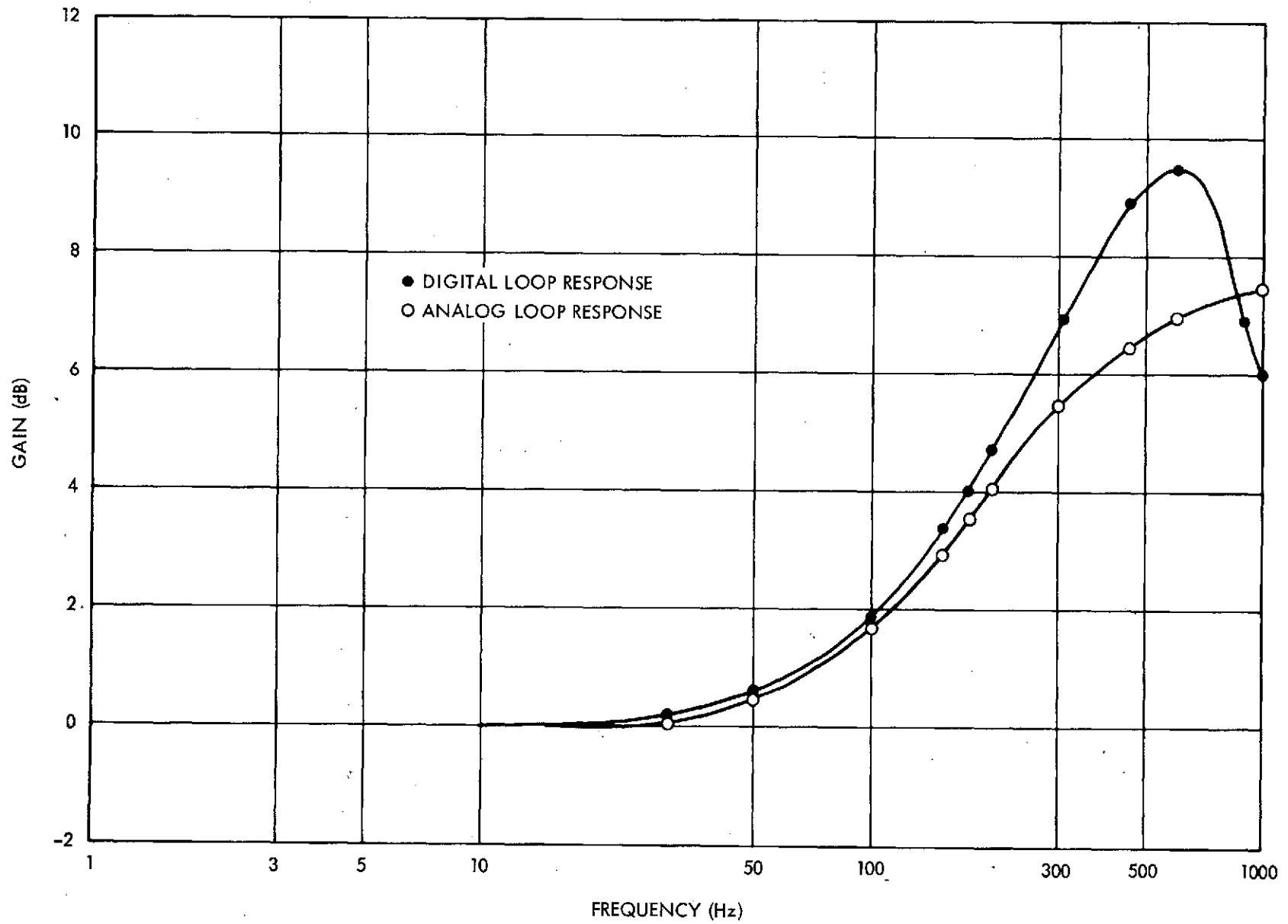


Figure 9a. Direct Axis Frequency Response

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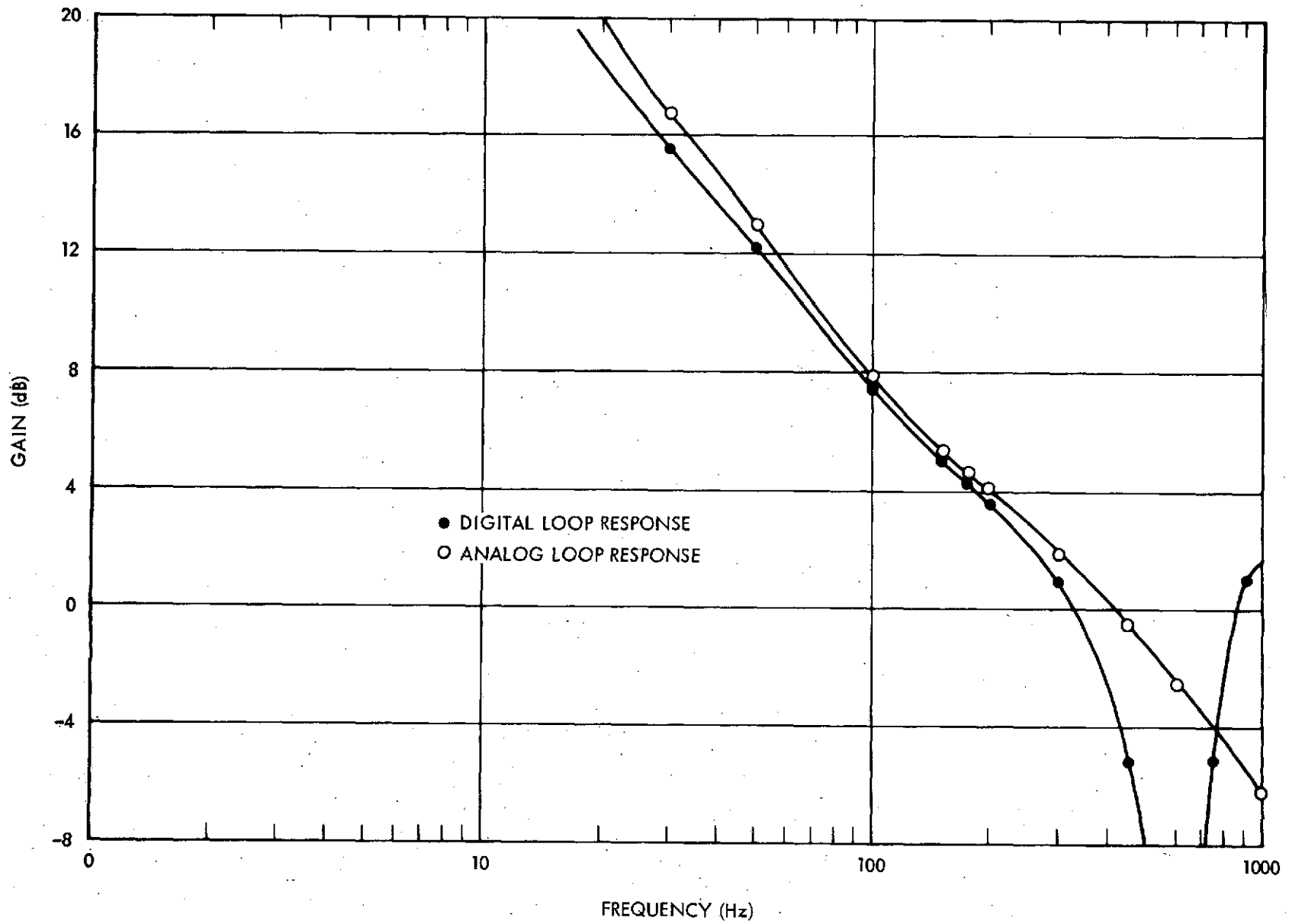


Figure 9b. Cross Axis Frequency Response

Several variations of parameters were tested within the constraints of the basic filter configurations described by  $G_1(z)$  and  $G_2(z)$  above. It was found that the transfer functions

$$G_1(z) = (1 - \frac{15}{16} z^{-1})$$

$$G_2(z) = \frac{1 + \frac{1}{16} z^{-1} - \frac{15}{16} z^{-2}}{1 - z^{-1}}$$

provided reasonably optimal performance for the digital loop\*. Most of the results described in the report reflect this configuration. Thus the equations which were mechanized in the computer were

$$M_x(k) = M_x(k-1) + \theta_x(k) + (2^{-4}) \theta_x(k-1) - (1-2^{-4}) \theta_x(k-2)$$

$$M_y(k) = \theta_y(k) - (1-2^{-4}) \theta_y(k-1)$$

$$M(k) = M_x(k) - M_y(k)$$

where  $M(k)$  is the computed gyro torque at the  $k^{\text{th}}$  iteration.

The digital number  $M(k)$  is converted by the digital-to-analog converter and, after power amplification, used to torque the gyro. In the absence of errors,  $M(k)$  represents the true torque input and is, therefore, proportional to the angular rate of the gyro case. This is precisely the information which is desired for attitude computation in a strapdown navigator. Any errors introduced by the D/A converter therefore propagate directly into attitude errors. For this reason it is necessary to use an accurate D/A converter in the digital loop.

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\*This corresponds to moving the zero locations in Figure 6 from 100 Hz to approximately 12.7 Hz.



The analog-to-digital conversion requirements are much less stringent. Due to the closed-loop nature of the digital compensator, errors in the A/D converter are of relatively minor importance to the accuracy of rate measurement (just as pickoff measurement errors are unimportant in a conventional analog loop mechanization).

The test results indicate that a 16 bit computer word length is sufficient for mechanization of the digital loop. The D/A converter should be an accurate device with excellent (or, at least, well compensatable) bias and scale factor characteristics. The A/D converter can be less accurate without seriously compromising torque measurement accuracy. The digital loop was mechanized using a 12 bit A/D converter and a 13 bit D/A converter. These resolutions are not critical, however, for the reasons outlined above. As long as the analog torque applied accurately represents the (quantized) digital torque, no net error will result in the computation of attitude due to the D/A converter resolution.

### III. COMPUTER

The computer used in the breadboard is an IMP-16P (National Semiconductor), which is electrically and functionally interchangeable with the TSC hybrid packaged TDY-52B. Although these two machines are functionally the same, they are vastly different physically. The CPU of each consists of four 4-bit NS (National Semiconductor) GPC/P RALU slices. The microprogram of each is contained in a set of two Control Read Only Memories (CROMs) that implement the NS IMP-16 computer repertoire. Input/Output and other hardware details are also similar. The IMP-16P and TDY-52B are thus, basically, the same machine.

The most obvious difference between the IMP-16P and TDY-52B is one of size. Teledyne has packaged the heart of the IMP-16P into a small hybrid unit that is only two inches on a side and .2" thick. The IMP-16P computer, including a convenient control panel and 4K of 16-bit RAM memory, occupies a box with a frontal dimension of about 10 1/2" x 17" and a depth of about 24".

The IMP-16P was selected for the digital loop demonstration primarily because its control panel feature facilitated the operation and modification of the breadboard. The results which were obtained are, however, equally applicable to the TDY-52B.

Table 1. TDY-52B/IMP-16 Instruction Repertoire (Sheet 1 of 2)

MNEMONIC	INSTRUCTION NAME	FUNCTION	FORMAT	EXECUTION TIME IN MICROSECONDS
<b>LOAD AND STORE</b>				
LD	LOAD	$(EA) \rightarrow (ACr)$ , IF INDIRECT $((EA) \rightarrow (ACr))$	2	7.0, 9.8 IF INDIRECT
LDB	LOAD BYTE	$(1/2 EA) \rightarrow (ACO \text{ LESS SIGNIFICANT BYTE})$	5	16.8 TO 28.0
LI	LOAD IMMEDIATE	$D \rightarrow (ACr)$	4B	4.2
ST	STORE	$(ACr) \rightarrow (EA)$ , IF INDIRECT $(ACr) \rightarrow ((EA))$	2	8.4, 11.2 IF INDIRECT
STB	STORE BYTE	$(ACO \text{ LESS SIGNIFICANT BYTE}) \rightarrow (1/2 EA)$ $0 \rightarrow (SEL)$	5	23.8 TO 32.2
RXCH	REGISTER EXCHANGE	$(SR) \rightarrow (DR)$ , $(DR) \rightarrow (SR)$	6	11.2
RCPY	REGISTER COPY	$(SR) \rightarrow (DR)$	6	8.4
<b>LOGICAL</b>				
RXOR	REGISTER EXCLUSIVE OR	$(SR) \oplus (DR) \rightarrow (DR)$	6	8.4
RAND	REGISTER AND	$(SR) \text{ "AND" } (DR) \rightarrow (DR)$	6	8.4
AND	AND	$(R01) \text{ "AND" } (EA) \rightarrow (R01)$	3	7.0
OR	OR	$(R01) \text{ "OR" } (EA) \rightarrow (R01)$	3	7.0
<b>ARITHMETIC</b>				
RADD	REGISTER ADD	$(SR) + (DR) \rightarrow (DR)$ OV, CY	6	4.2
ADD	ADD	$(ACr) + (EA) \rightarrow (ACr)$ OV, CY	2	7.0
SUB	SUBTRACT	$(ACr) - (EA) \rightarrow (ACr)$ OV, CY	2	7.0
MPY	MULTIPLY	$(EA) * (AC1) \rightarrow \{(ACO, (AC1))\}$ L 0 $\rightarrow (SEL)$	5	148.4 TO 170.8
DIV	DIVIDE	$\{(ACO), (AC1)\} \rightarrow (EA) \rightarrow (ACO) \text{ QUOTIENT}$ 0 $\rightarrow (SEL)$ OV, L $\{(AC1) \text{ REMAINDER}\}$	5	177.8 TO 222.6
DADD	DOUBLE PRECISION ADD	$\{(ACO), (AC1)\} + \{(EA), (EA+1)\} \rightarrow \{(ACO), (AC1)\}$ 0 $\rightarrow (SEL)$ OV, CY	5	16.8
DSUB	DOUBLE PRECISION SUBTRACT	$\{(ACO), (AC1)\} - \{(EA), (EA+1)\} \rightarrow \{(ACO), (AC1)\}$ 0 $\rightarrow (SEL)$ OV, CY	5	16.8
CAI	COMPLEMENT AND ADD IMMEDIATE	$\sim (ACr) + D \rightarrow (ACr)$	4B	4.2
<b>SHIFT</b>				
ROL	ROTATE LEFT	$2 (ACr) \rightarrow (ACr)$ IF SEL = 0, (BIT 15) $\rightarrow$ (BIT 0) IF SEL = 1, (BIT 15) $\rightarrow$ (L), (L) $\rightarrow$ (BIT 0) } D TIMES	4B	5.6 + 4.2D
ROR	ROTATE RIGHT	$1/2 (ACr) \rightarrow (ACr)$ IF SEL = 0, (BIT 0) $\rightarrow$ (BIT 15) IF SEL = 1, (BIT 0) $\rightarrow$ (L), (L) $\rightarrow$ (BIT 15) } D TIMES	4B	5.6 + 4.2D
SHL	SHIFT LEFT	$2 (ACr) \rightarrow (ACr)$ 0 $\rightarrow$ (BIT 0) } D TIMES IF SEL = 1, (BIT 15) $\rightarrow$ (L)	4B	5.6 + 4.2D
SHR	SHIFT RIGHT	$1/2 (ACr) \rightarrow (ACr)$ IF SEL = 0, 0 $\rightarrow$ (BIT 15) IF SEL = 1, (L) $\rightarrow$ (BIT 15), 0 $\rightarrow$ (L) } D TIMES	4B	5.6 + 4.2D
<b>SINGLE BIT</b>				
SETST	SET STATUS BIT	1 $\rightarrow$ (STATUS FLAG N)	9	18.2 TO 44.8
CLRST	CLEAR STATUS BIT	0 $\rightarrow$ (STATUS FLAG N)	9	18.2 TO 44.8
SETBIT	SET BIT	1 $\rightarrow$ (ACO BIT N)	9	18.2 TO 44.8
CLRBIT	CLEAR BIT	0 $\rightarrow$ (ACO BIT N)	9	18.2 TO 44.8
CMPBIT	COMPLEMENT BIT	$(ACO \text{ BIT } N) \rightarrow (ACO \text{ BIT } N)$	9	18.2 TO 44.8

T92170-1A

Table 1. TDY-52B/IMP-16 Instruction Repertoire (Sheet 2 of 2)

MNEMONIC	INSTRUCTION NAME	FUNCTION	FORMAT	EXECUTION TIME IN MICROSECONDS
<u>JUMP</u>				
JMP	JUMP	EA → (PC), IF INDIRECT (EA) → (ACr)	4A	4.2, 7.0 IF INDIRECT
JMPP	JUMP THROUGH POINTER	(100 <sub>16</sub> + N) → (PC)	9	9.8
JINT	JUMP INDIRECT TO LEVEL 0	(PC) → (STK), 0 → (IEF) (120 <sub>16</sub> + N) → PC	9	9.8
BOC	BRANCH ON CONDITION	IF CONDITION CC IS TRUE, (PC) + D → (PC)	1	5.6, 7.0 IF BRANCH
JSR	JUMP TO SUBROUTINE	(PC) → (STK) EA → (PC), IF INDIRECT (EA) → (PC)	4A	5.6, 8.4 IF INDIRECT
JSRI	JUMP TO SUBROUTINE IMPLIED	(PC) → (STK) FF80 <sub>16</sub> + C → (PC)	8	5.6
JSRP	JUMP TO SUBROUTINE THROUGH POINTER	(PC) → (STK) (100 <sub>16</sub> + C) → (PC)	8	11.2
RTS	RETURN FROM SUBROUTINE	(STK) + C → (PC)	8	5.6
RTI	RETURN FROM INTERRUPT	(STK) + C → (PC) 1 → (IEF)	8	7.0
<u>SKIP</u>				
AISZ	ADD IMMEDIATE AND SKIP IF ZERO	(ACr) + D → (ACr) OV, CY IF (ACr) = 0, (PC) + 1 → (PC)	4B	5.6, 7.0 IF SKIP
SKAZ	SKIP IF "AND" IS ZERO	IF (R01) "AND" (EA) = 0, (PC) + 1 → (PC)	3	8.4, 9.8 IF SKIP
ISZ	INCREMENT AND SKIP IF ZERO	(EA) + 1 → (EA) IF (EA) = 0, (PC) + 1 → (PC)	4B	9.8, 11.2 IF SKIP
DSZ	DECREMENT AND SKIP IF ZERO	(EA) - 1 → (EA) IF (EA) = 0, (PC) + 1 → (PC)	4B	11.2, 12.6 IF SKIP
SKG	SKIP IF GREATER THAN	IF (ACr) > (EA), (PC) + 1 → (PC)	2	11.2 TO 14.0
SKNE	SKIP IF NOT EQUAL	IF (ACr) ≠ (EA), (PC) + 1 → (PC)	2	8.4
SKSTF	SKIP IF STATUS FLAG TRUE	IF (STATUS FLAG N) = 1, (PC) + 1 → (PC) 0 (SEL)	9	18.2 TO 44.8
SKBIT	SKIP IF BIT TRUE	IF (AC0 BIT N) = 1, (PC) + 1 → (PC) 0 (SEL)	9	18.2 TO 44.8
<u>STACK</u>				
PUSHF	PUSH STATUS FLAGS ONTO STACK	(SF) → (STK)	8	5.6
PULLF	PULL STATUS FLAGS FROM STACK INTO FLAG REGISTER	(STK) → (ACr)	8	7.0
PUSH	PUSH ONTO STACK	(ACr) → (STK)	4B	4.2
PULL	PULL FROM STACK	(STK) → (ACr)	4B	4.2
XCHRS	EXCHANGE REGISTER AND STACK	(ACr) → (STK) (STK) → (ACr)	4B	7.0
<u>INPUT/OUTPUT</u>				
RIN	REGISTER INPUT	(AC3) + C → (IO ADDR) (IO DATA) → (AC0)	8	9.8
ROUT	REGISTER OUTPUT	(AC3) + C → (IO ADDR) (AC0) → (IO DATA)	8	9.8
SFLG	SET FLAG	C → (IO ADDR), 1 → (CONTROL FLAG FC)	7	5.6
PFLG	PULSE FLAG	C → (IO ADDR), 1 → (CONTROL FLAG FC)	7	5.6
ISCAN	INTERRUPT SCAN	1/2 (AC1) → (AC1) UNTIL 1 SHIFTED OUT (AC2) + NUMBER OF SHIFTS → (AC2)	9	8.4 TO 100.8
HALT	HALT	PROCESSOR HALTS	8	—

## Notation Used in Instruction Descriptions

Notation	Meaning
ACr	Denotes a specific working register (AC0, AC1, AC2, or AC3), where <i>r</i> is the number of the accumulator referenced in the instruction.
AR	Denotes the address register used for addressing memory or peripheral devices.
cc	Denotes the 4-bit condition code value for conditional branch instructions.
ctl	Denotes the 7-bit control-field value for flag, input/output, and miscellaneous instructions.
CY	Indicates that the Carry flag is set if there is a carry due to the instruction (either an addition or a subtraction).
disp	Stands for displacement value and it represents an operand in a nonmemory reference instruction or an address field in a memory reference instruction. It is an 8-bit, signed twos-complement number except when base page is referenced; in the latter case, it is unsigned.
dr	Denotes the number of a destination working register that is specified in the instruction-word field. The working register is limited to one of four: AC0, AC1, AC2, or AC3.
EA	Denotes the effective address specified by the instruction directly, indirectly, or by indexing. The contents of the effective address are used during execution of an instruction. See table 3-1.
fc	Denotes the number of the referenced flag (see table 3-20 under 3.6.10, Input/Output, Halt, and Flag Instructions).
INTEN	Denotes the Interrupt Enable control flag.
IOREG	Denotes an input/output register in a peripheral device.
L	Denotes 1-bit link (L) flag.
OV	Indicates that the overflow flag is set if there is an overflow due to the instruction (either an addition or a subtraction).
PC	Denotes the program counter. During address formation, it is incremented by 1 to contain an address 1 greater than that of the instruction being executed.
r	Denotes the number of a working register that is specified in the instruction-word field. The working register is limited to one of four: AC0, AC1, AC2, or AC3.
SEL	Denotes the Select control flag. It is used to select the carry or overflow for output on the carry and overflow (CYOV) line of the CPU, and to include the link bit (L) in shift operations.
sr	Denotes the number of a source working register that is specified in the instruction-word field. The working register is limited to one of four: AC0, AC1, AC2, or AC3.
xr	When not zero, this value designates the number of the register to be used in the indexed and relative memory-addressing modes.

Notation Used in Instruction Descriptions (Continued)

Notation	Meaning
( )	Denotes the contents of the item within the parentheses. (ACr) is read as "the contents of ACr." (EA) is read as "the contents of EA."
[ ]	Denotes "the result of."
~	Indicates the logical complement (ones complement) of the value on the right-hand side of ~.
→	Means "replaces."
←	Means "is replaced by."
@	Appearing in the operand field of an instruction, denotes indirect addressing.
∧	Denotes an AND operation.
∨	Denotes an OR operation.
∇	Denotes an exclusive OR operation.

## IV. SOFTWARE

### Introduction

The intent of this study was not to demonstrate the particular processor which was used but rather to demonstrate how the program was mechanized for this particular computer in such a manner that the software could be mechanized for any given computer with equivalent characteristics. The reader should have some knowledge, however, of the computer in which the equation set was mechanized in order to fully understand the work performed. An example of how the flow charts reflect the instruction repertoire of the processor is in the handling of negative quantities. The TDY-52B/IMP-16 has a logical shift only, so that when a multiplication by  $1/16$  is to be performed it is necessary to handle negative quantities in a different manner than positive quantities where the multiplication can be performed by a shift of 4 bit positions.

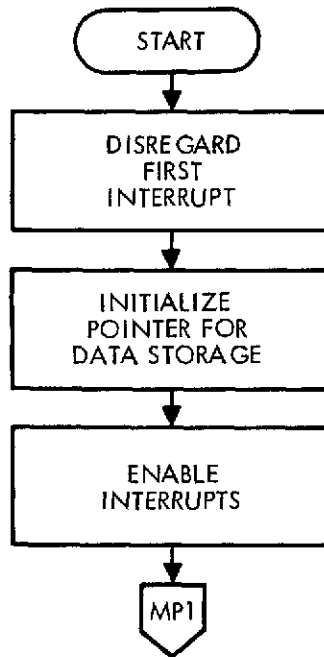
In order to give a better understanding of the digital computer used in this study a summary of instructions was included in Section III. Should the reader have further interest in this processor including the interrupt system, push-pull stack operation, logic mechanization, etc., complete descriptive manuals can be obtained from Teledyne Systems Company.

### Power On Processing

Upon recognition of Power being applied to the unit, coding is performed to disregard the initial multiplexer interrupt. This is done to allow the program to become synchronized with the timing base of the multiplexer so that after the initial interrupt the timing base of approximately 104 microseconds between interrupts is established for the remaining processing. The next task is to initialize a pointer within the processor so that whenever data is generated for storage the starting point for this storage is established.

The interrupts are then enabled so that the processor is ready to recognize interrupts from the multiplexer. Finally a transfer is made to the Main Processing Loop. As the processor used in this study turns on with Random Access Memory (RAM) set to an all one's condition, the initial iterations of the Main Processing do not have the proper data for use as a priori iteration data so that the data generated for the first two iterations of the Main Processing Loop is not precise.

POWER ON INITIALIZATION



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Main Programming Loop

The Main Programming Loop is where the majority of calculations are performed. This routine is coded to run continuously, i. e. from Power On the calculation process is repeatedly performed with the only interruptions being the X peak and Y peak Interrupts where data from the analog to digital converter is input. Once the data has been input within either of these interrupt routines, program control is transferred back to the Main Programming Loop at the point the program was interrupted.

Essentially the processing within this software module consists of solving the equations below:

$$M_x(K) = M_x(K-1) + U_x(K) + 1/16 U_x(K-1) - 15/16 U_x(K-2)$$

$$M_y(K) = U_y(K) - 15/16 U_y(K-1)$$

$$M_z(K) = U_x(K) - U_y(K)$$



where:

$M_x$  = filtered digital quantity from X axis pickoff

$M_y$  = filtered digital quantity from Y axis pickoff

$M$  = total digital torque output to D/A

Index (k) designates quantity input or calculated on current program iterations.

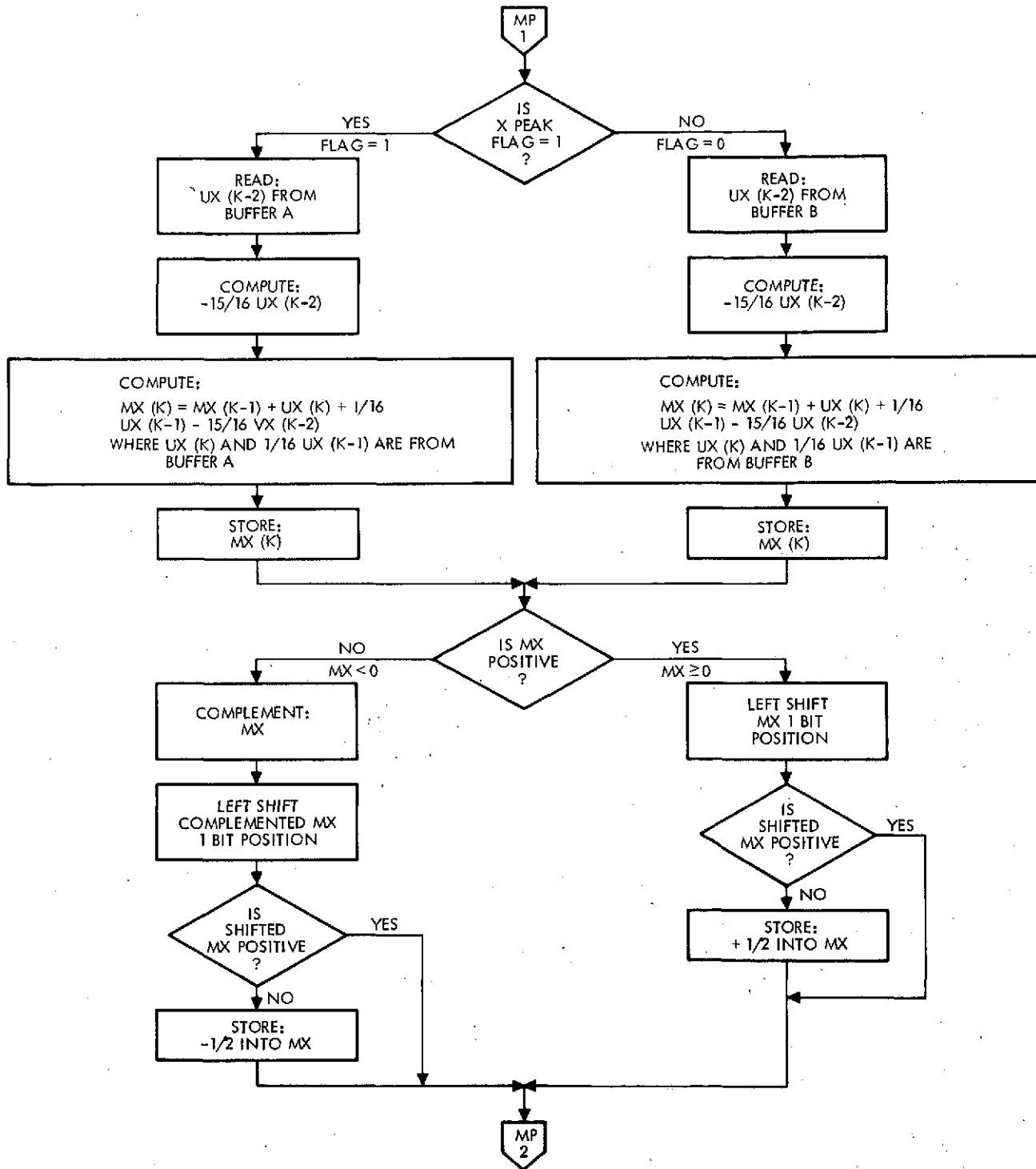
Index (k-1) designates quantity input or calculated on previous iteration

Index (k-2) designates quantity input or calculated two iterations previous

The other calculations performed in this loop and shown on the flow diagrams for the Main Processing Loop is the interrogation of two software flags, X peak flag and Y peak flag, to properly correlate the data from the storage buffers and to transform the data from its 2's complement form for the sign magnitude digital to analog convertor.

Following is the flow chart for the Main Processing Loop. (Figure 10.)

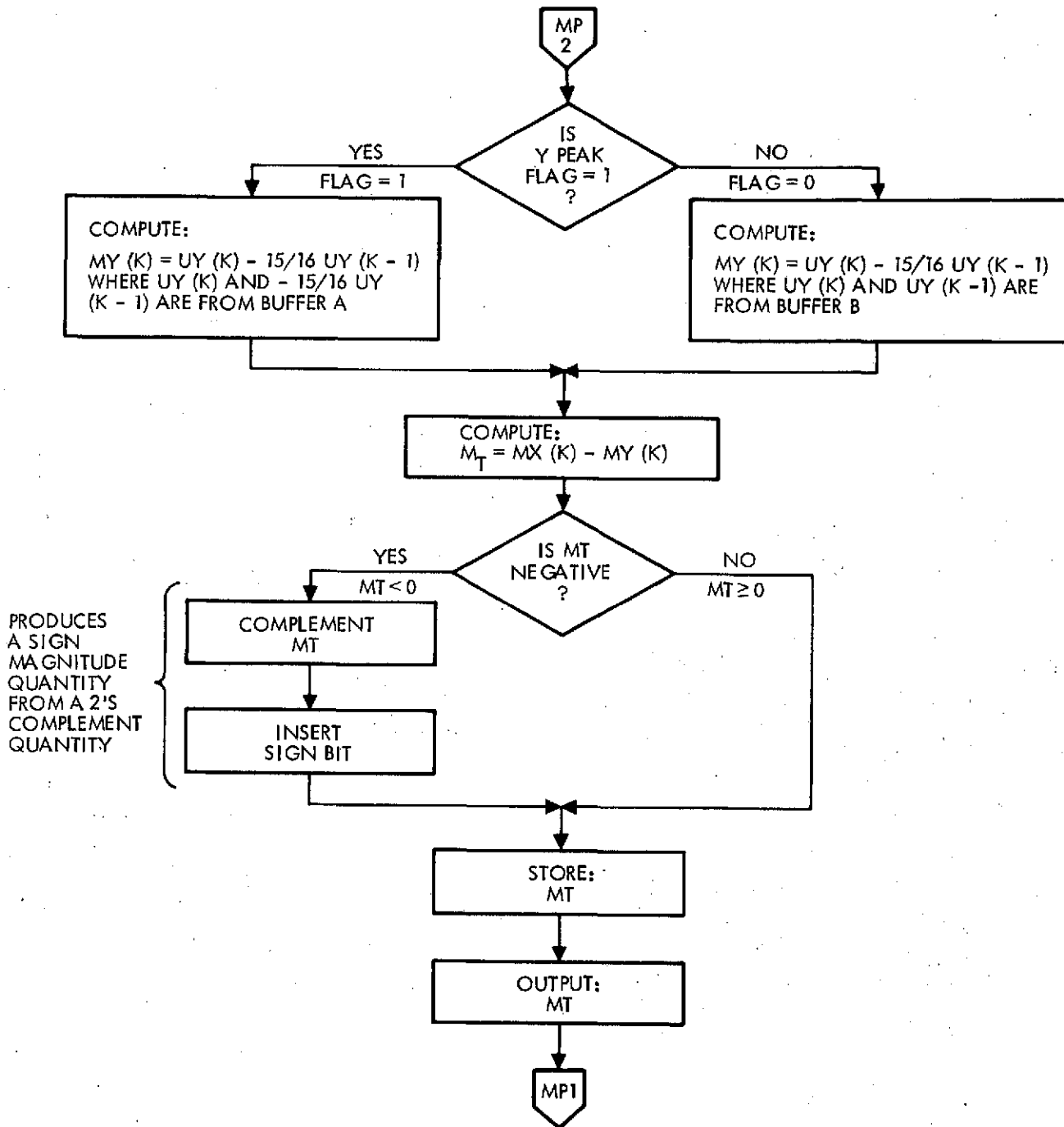
MAIN PROGRAMMING LOOP



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Figure 10. Main Programming Loop

MAIN PROGRAMMING LOOP

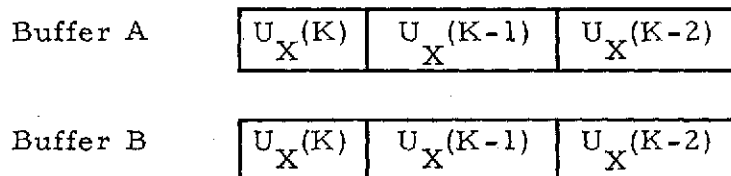


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Figure 10. Main Programming Loop (Continued)

## X Peak Interrupt Servicing

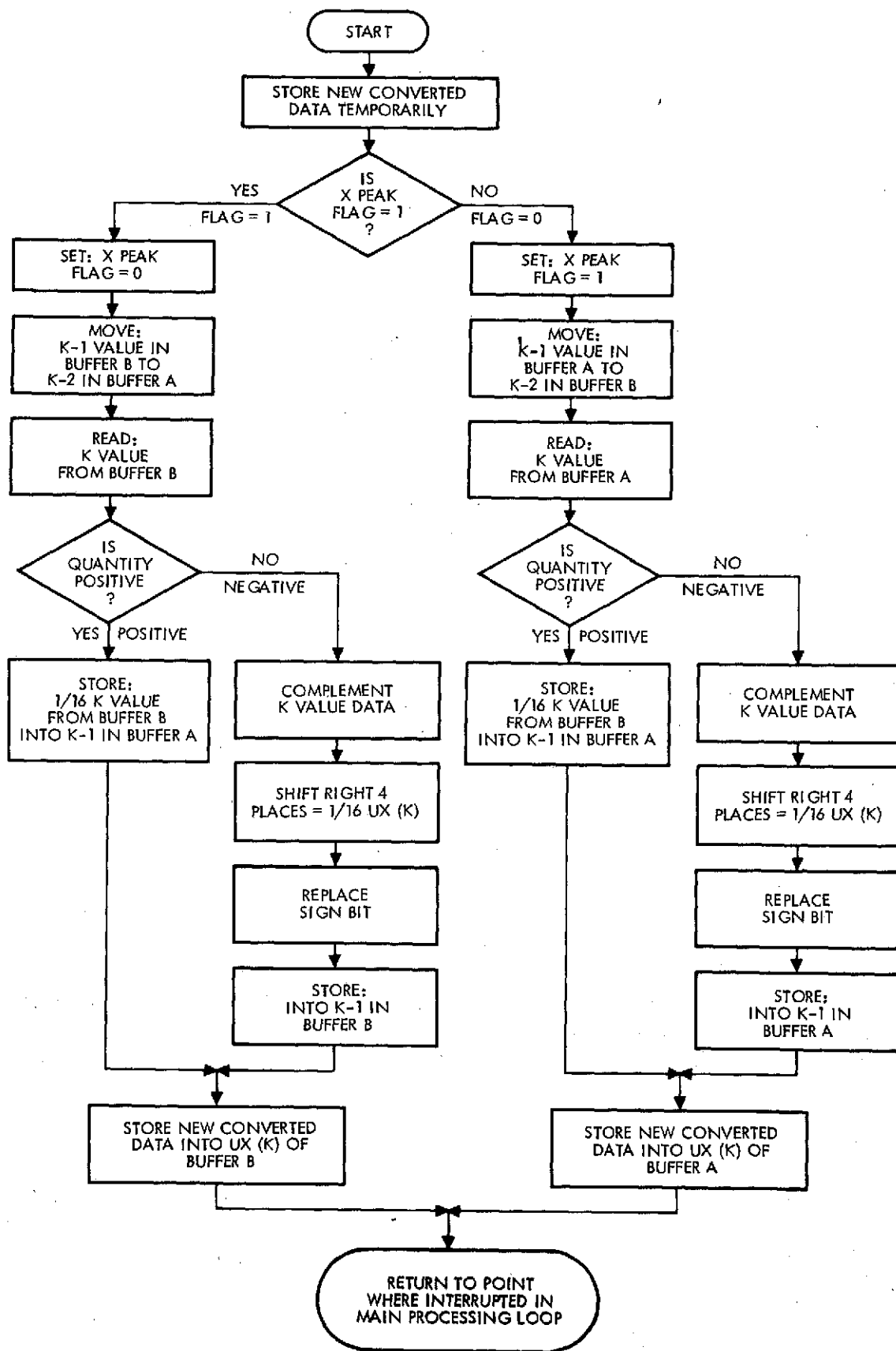
Upon recognition by the processor that sample data from the X axis pickoff is available, the Main Processing Loop is interrupted at the end of the instruction it is performing and the program is transferred to the X Peak Interrupt Servicing routine. The purpose of this routine is to accept the digitized X axis pickoff data for the computation to be performed by the Main Processing Loop. In order to keep the data being computed in the Main Programming Loop correlated it was necessary to mechanize two buffer areas which are merely memory cells set aside for temporary data storage and retrieval. At any given point of time one of the buffer areas is set for reading by the Main Processing Loop and the other buffer area is set for writing or storage by the X Peak Interrupt Servicing routine. The purpose of these buffers is to ensure that the data being computed is indeed from successive iterations. A memory cell is used as a flag (X Peak Flag in flow charts) to indicate how the buffers are currently being utilized. This same flag is again interrogated in the Main Processing Loop for the same purpose. A graphic illustration of the storage areas referred to as 'swinging buffers' will perhaps clarify this coding concept. At the time the X Peak Interrupt is entered by the program assume that the two buffers are as shown below



and further assume that the flag (X Peak Flag) indicates that Buffer A is the area that should be used to store data. The cell from Buffer B containing  $U_X(K-1)$  must first be moved to Buffer A as it now becomes two iterations old, i. e.  $U_X(K-2)$ . In the same manner the Buffer B cell containing  $U_X(K)$  is moved to Buffer A and is now one iteration old, i. e.  $U_X(K-1)$ . The digitized X axis pickoff data input during the current iteration is then stored in Buffer A as  $U_X(K)$ . Buffer A then contains data from three successive inputs. The process is reversed the next iteration such that Buffer B contains current data. The last task of the X Peak Interrupt processing is to divide the data from the previous iteration by 16 (accomplished by a right shift of 4 places) before storing to relieve the Main Processing Loop of this computational burden. Once these tasks are performed the program is returned to the Main Processing Loop to the point at which the interrupt occurred.

Following is the flow charts for the X Peak Interrupt Processing.  
(Figure 11.)

X PEAK INTERRUPT SERVICING FLOWS



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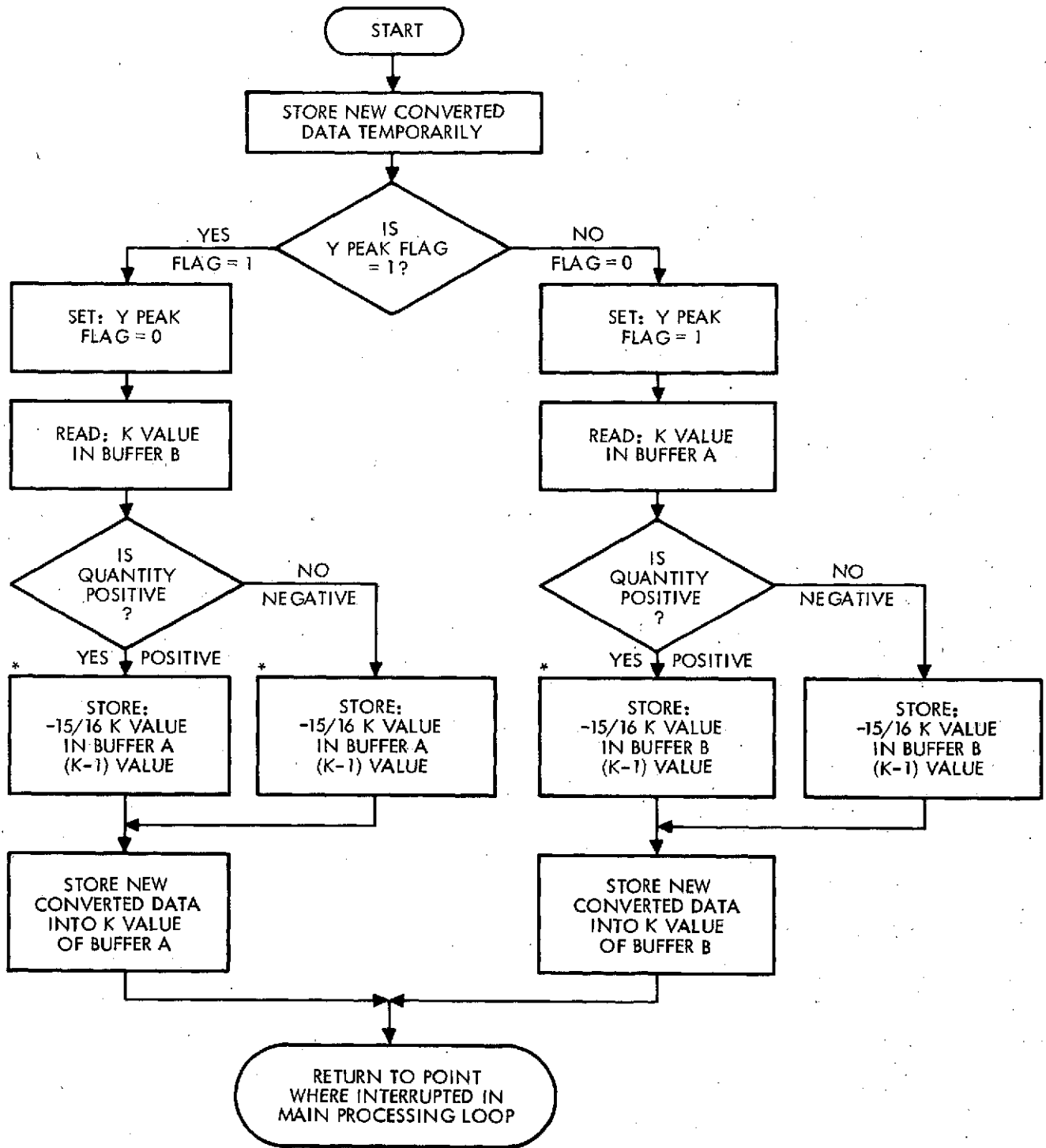
Figure 11. X Peak Interrupt Servicing Flow

## Y Peak Interrupt Servicing

Upon recognition by the processor that sample data from the Y axis pickoff is available the Main Processing Loop is interrupted at the end of the instruction it is performing and the program is transferred to the Y Peak Interrupt Servicing routine. The purpose of this routine is to accept the digitized Y axis pickoff data for the computation to be performed by the Main Processing Loop. This data is correlated in much the same manner as previously explained in the X Peak Interrupt Servicing in that a flag (Y Peak Flag) is used to determine which data is time correlated and buffers are used to determine read and write areas. In this process the last iteration Y axis pickoff data  $U_Y(K-1)$  is multiplied by 15/16 as a time saving step to the Main Processing Loop. Again, as in the X Peak Interrupt Processing, a return is made to the point in the Main Processing Loop where processing was interrupted.

Following is the flow charts for the Y Peak Interrupt Processing.  
(Figure 12.)

Y PEAK INTERRUPT SERVICING FLOWS



\*  $-15/16 UY (K-1) = -1 + 1/16 UY (K-1)$

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Figure 12. Y Peak Interrupt Servicing Flow

## V. ANALOG INTERFACE

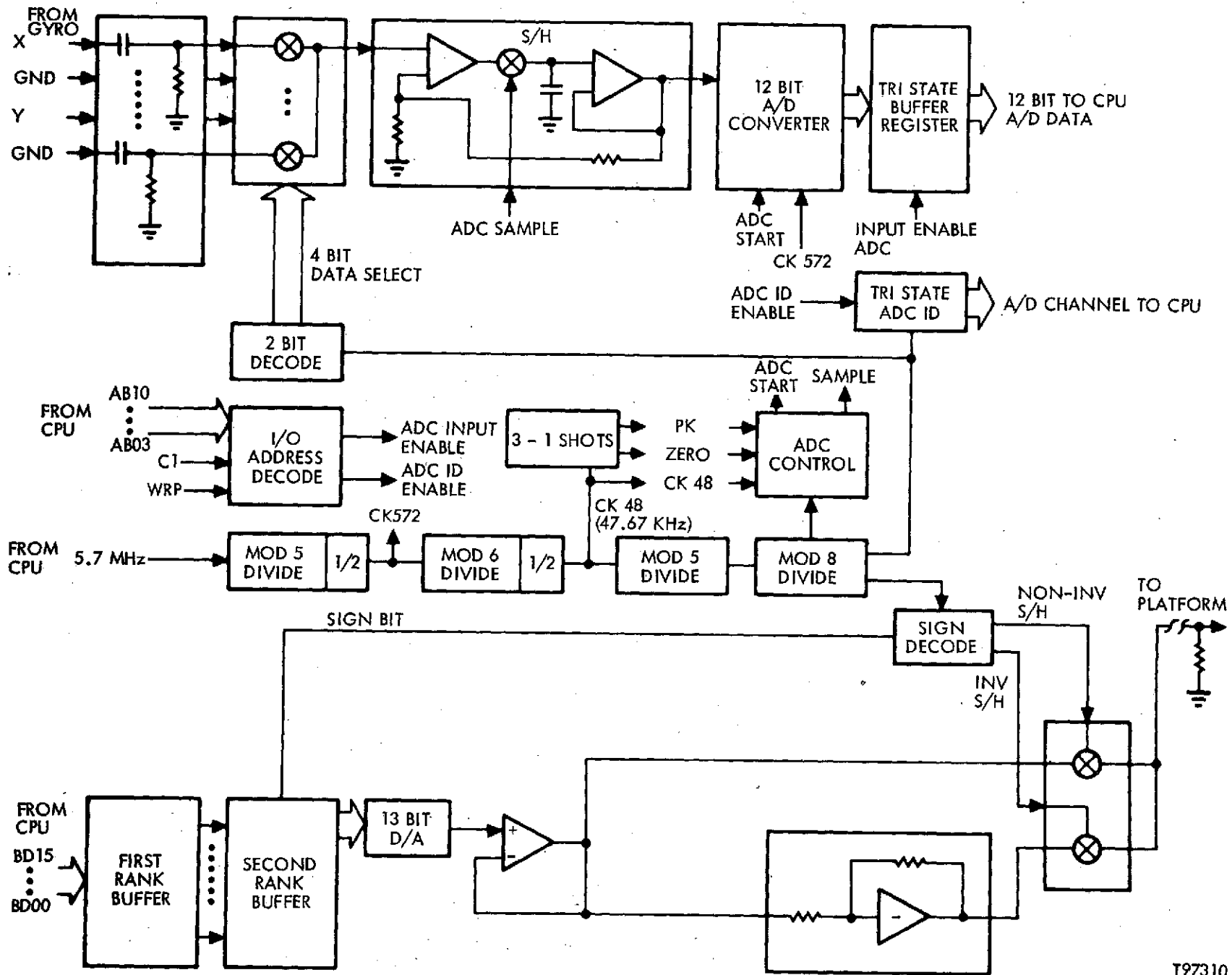
The analog interface for the IMP 16 computer consists of an A/D converter, a D/A converter, and the control logic for the two converters. A block diagram of the interface is shown in Figure 13.

The A/D converter section, shown in Figure 14, consists of an input multiplex switch, a sample and hold, a 12-bit converter, and a tri-state buffer register. The input multiplex selects an input channel which may be a peak, zero, or ground input from one of the gyros. This input depends on which channel is selected by the computer and logic decode. The input is applied to the sample and hold circuit, which will hold the input signal value until the A/D performs a conversion. The A/D start command and clock are supplied by the control logic. The tri-state buffer holds the A/D conversion and outputs it to the CPU until the next input enable allows the data to update.

The D/A converter accepts a 13-bit sign-magnitude word from the CPU and converts it to a + or - DC output to drive the gyro torquer amplifier. This converter consists of a  $\pm$  DC reference, a 12-bit ladder network, plus  $\pm$  output buffer amplifiers. The control logic decodes the input data word and outputs a sign bit so that the proper polarity is applied to the ladder network. The control logic also applies a 12-bit word to the ladder network to determine amplitude. The signal from the ladder network is applied to output buffer amplifiers. The control logic enables either a + or - sample switch which applies the respective output signal to the hold capacitor located on the torquer amplifier on the platform.

The control logic of the analog interface receives the 5.72 MHz CPU clock and divides it by 10 and 12 successively to provide basic square waves of 572 KHz and approximately 48 KHz. The 48 KHz clock is used to generate periodically four sequential analog select signals, each spanning an interval of 32 clock periods. Two successive analog-to-digital conversions are made during an analog select interval, one in the first half-interval and one in the second half-interval. The 48 KHz bit times of each half-interval are designated  $T_0$  through  $T_{15}$ . Analog sampling signals are enabled during  $T_1$  of each half-interval such that an analog peak signal is sampled in the first half-interval and an analog zero crossing is sampled in the second half-interval. Analog to digital conversion is accomplished during  $T_2$  and  $T_3$  of each half cycle. An interrupt request is then sent to the CPU at  $T_4$ . The converted 12-bit analog data may be input to the computer by the command,  $R_{IN}(0070)_{16}$ . The analog data is identified by a three-bit code which is inputted to the computer by the command,  $R_{IN}(0078)_{16}$ .





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Figure 13. A/D - D/A Control Block Diagram

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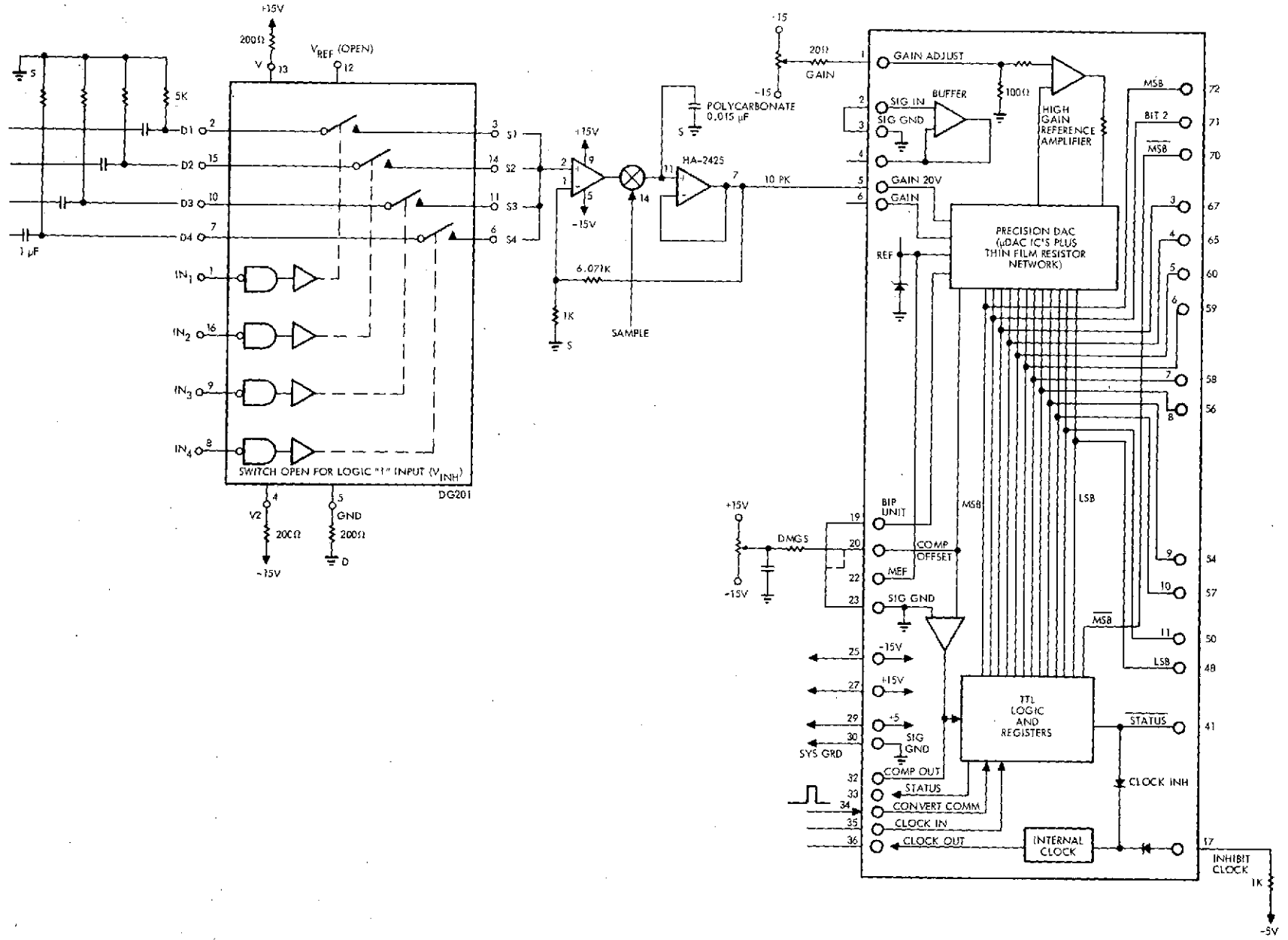


Figure 14. A/D Converter

The CPU outputs a 13-bit word in sign-magnitude format for conversion to analog by the command,  $R_{OUT} (0078)_{16}$ . The data word is latched in a 1st rank buffer from which it is transferred to a 2nd rank buffer at bit time  $T_0$  of a continuous 8-bit cycle of the 48 KHz square wave. The conversion is accomplished during each  $T_0$ . Also, sampling of the converted output is disabled during  $T_0$ .

## VI. TEST RESULTS

### Test Description

Figures 15 through 17 illustrate the general test setup. In this test configuration, the gyro was mounted on the rate table such that the input rates would be about the gyro x axis.

The x and y gyro pickoff signals were fed to both the digital servo and the analog servo. The digital servo controlled only the y torquer, and the analog servo controlled only the x torquer.

The rate table was driven by the oscillator portion of the wave analyzer with a constant voltage applied to the rate table.

The wave analyzer was used to measure the torquer signals and pickoff signals. The x axis (direct) pickoff signal was also measured in the open loop condition. The open loop and closed loop measurements were used to calculate the gains that are plotted in Figures 18 and 19.

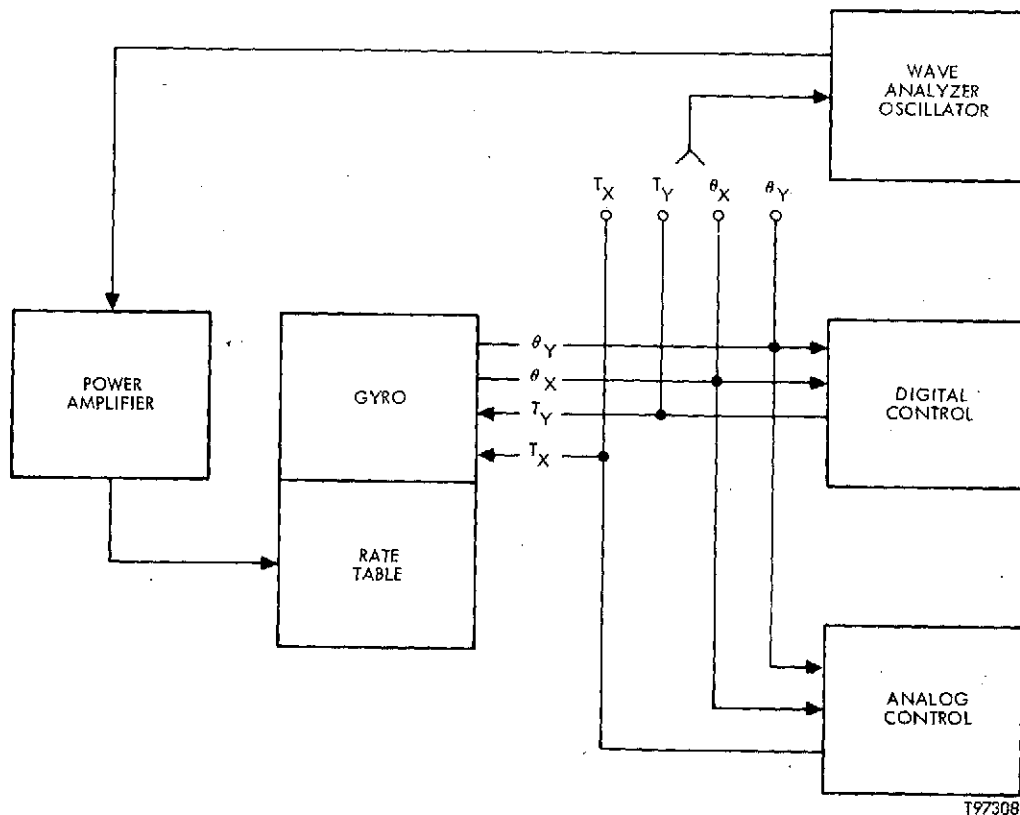
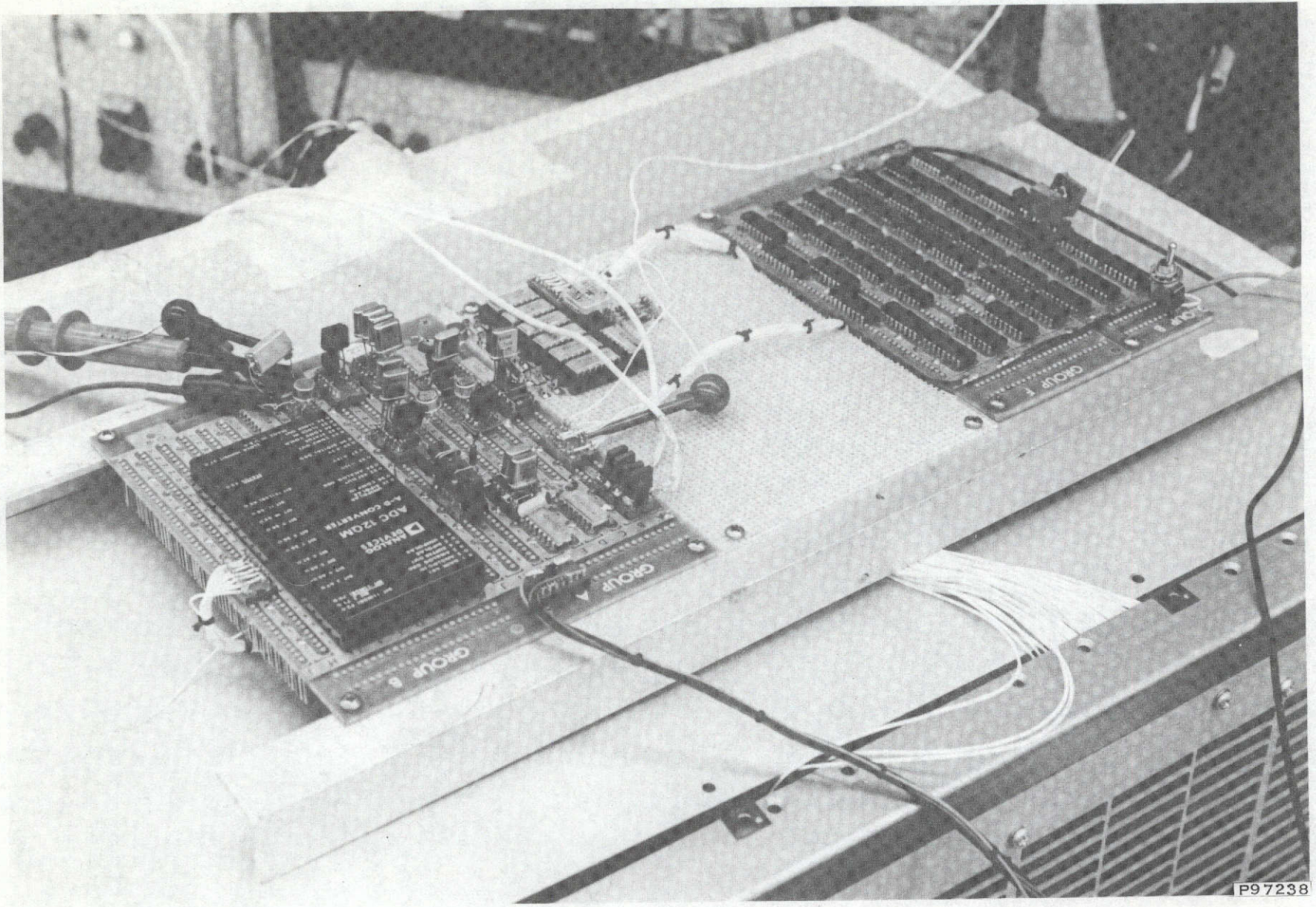


Figure 15. Block Diagram, Test Set Up

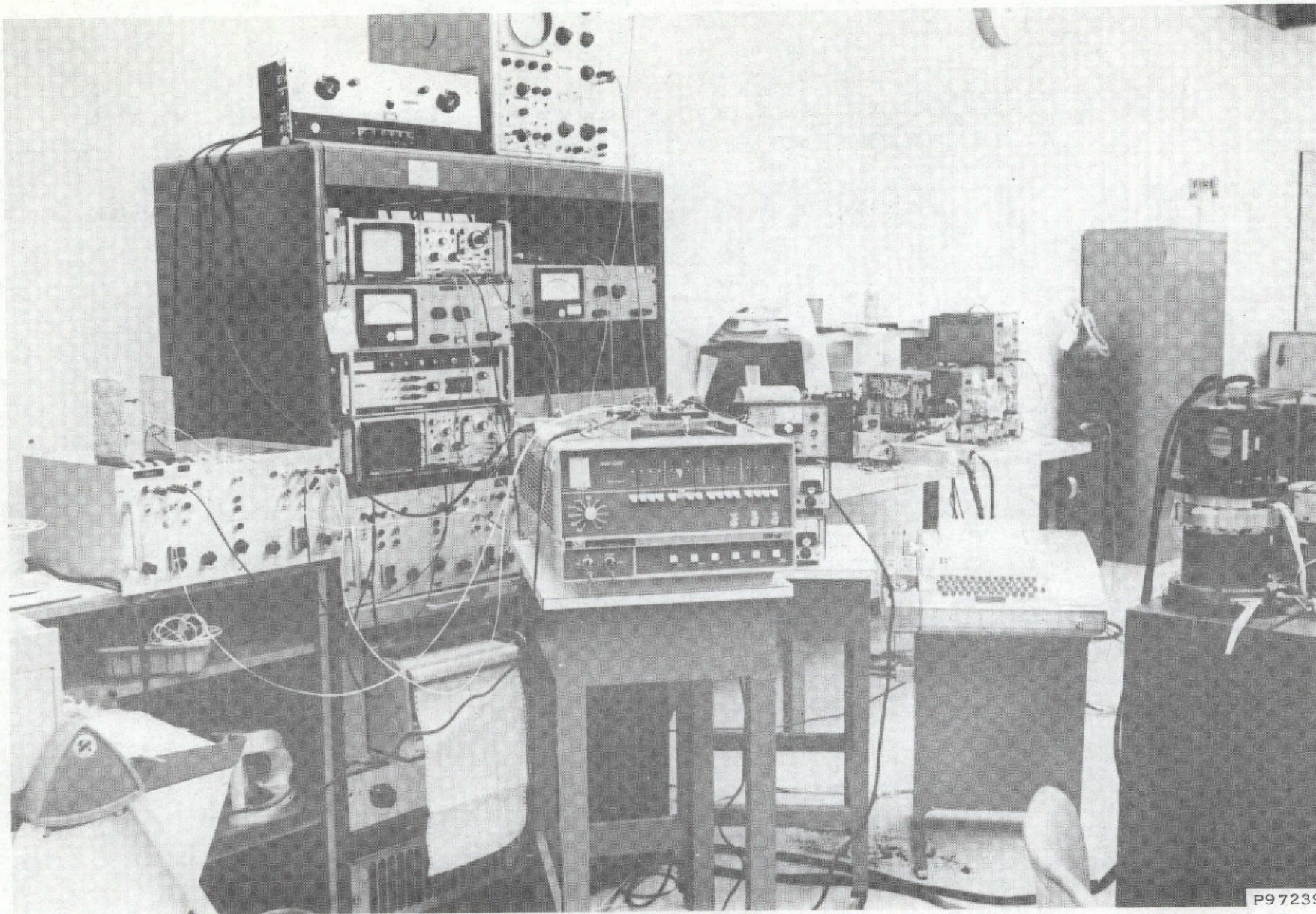




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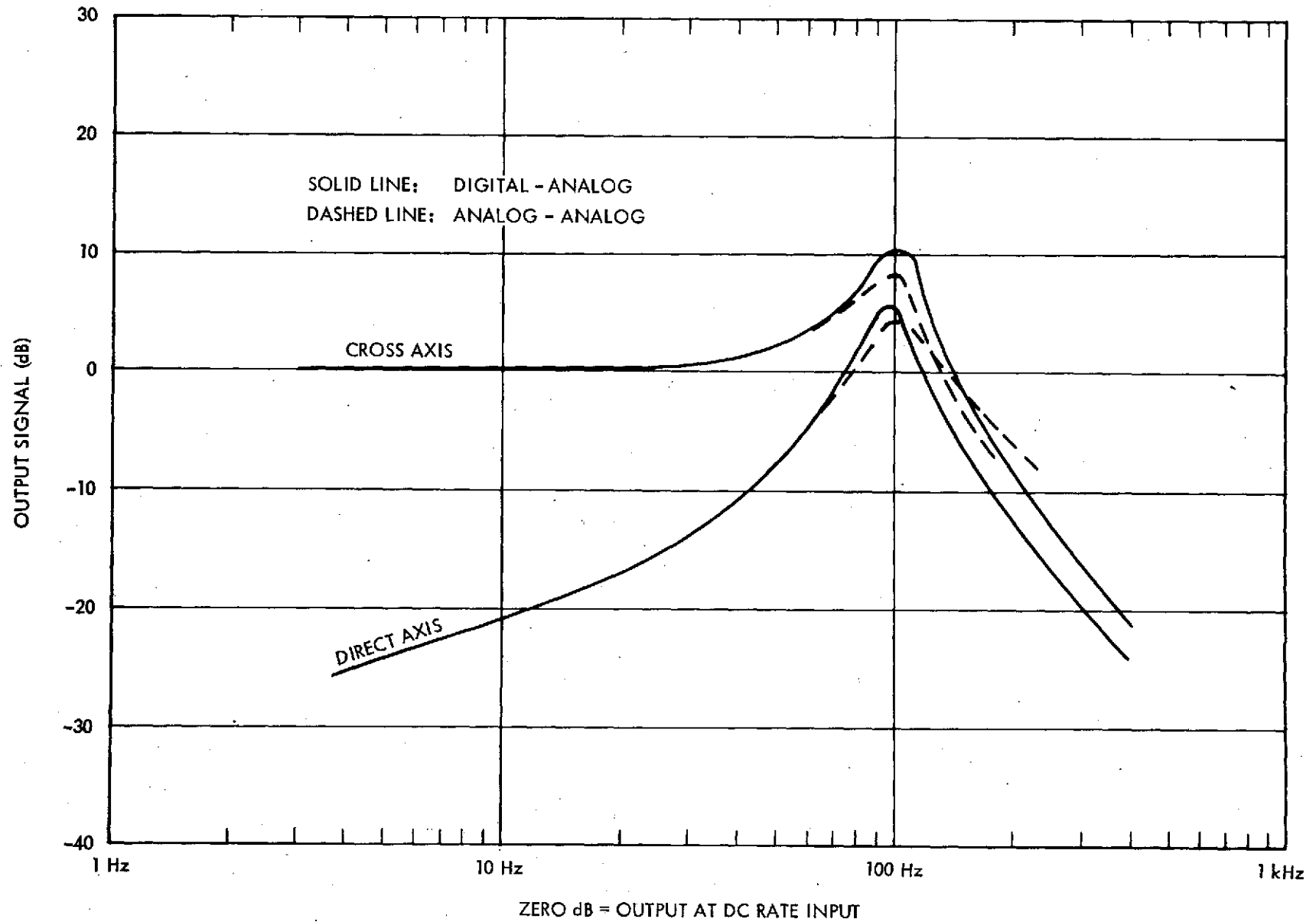
Figure 16. Test Set-Up for Digital Compensation Loop Feasibility Study





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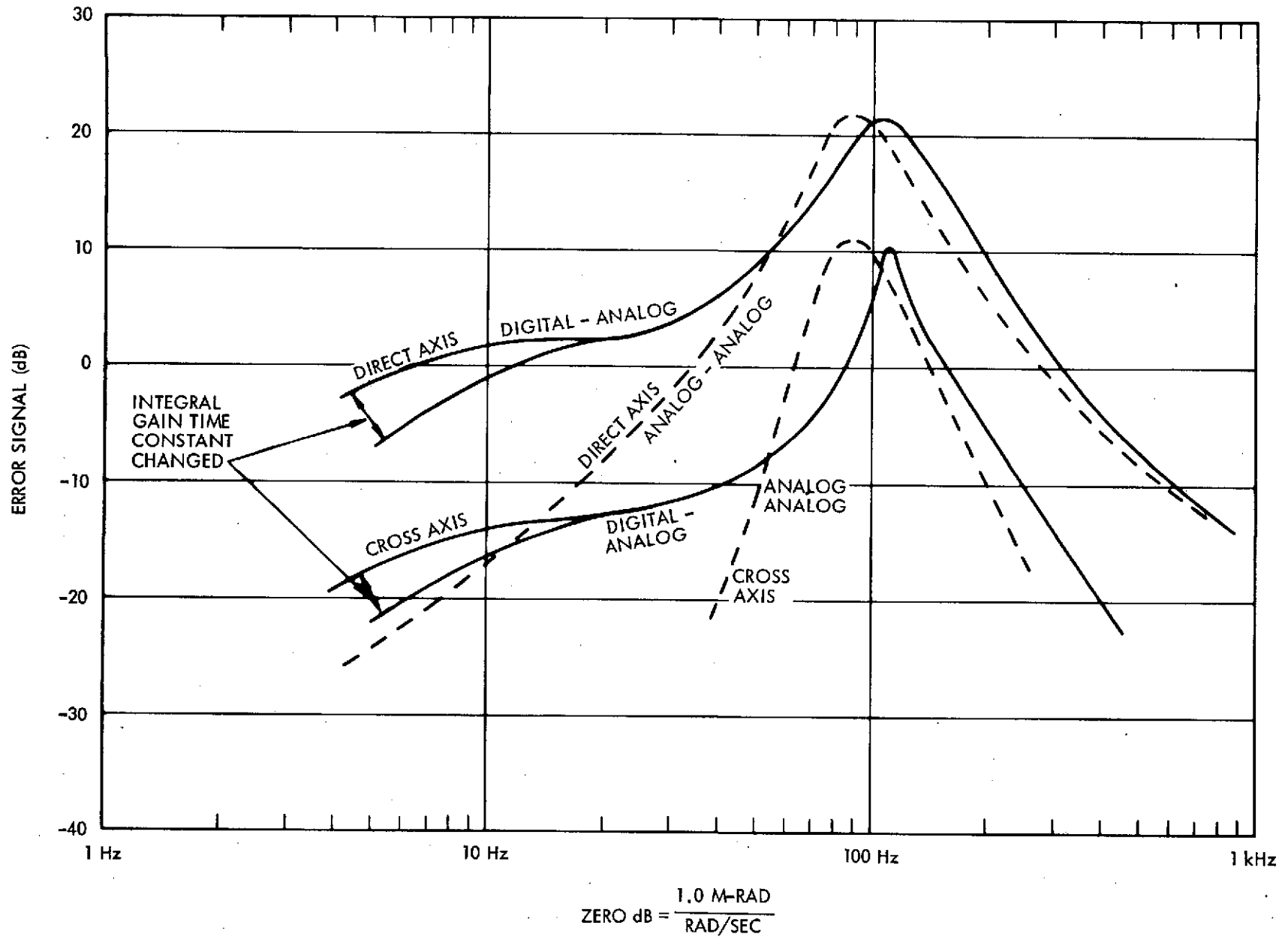
Figure 17. Test Set-up of Converters and Interface for Digital Compensation Loop System



DATA TAKEN 8.2.74 TMW

Figure 18. Output Signal (Torquer Voltage) vs Frequency  
Digital-Analog Loop ~ 100 Hz Bandwidth

T97307



DATA TAKEN 8.2.74 TMW

Figure 19. Error Signal (Pickoff Angle) vs Frequency  
Digital-Analog Loop ~ 100 Hz Bandwidth

T97306



The rate table drive frequency was varied from 10 Hz to 1 KHz with 3 to 5 measurements taken per decade depending on how rapidly the data was changing with frequency.

The integral gain time constant in the digital servo was modified (software modification) and the test repeated. There were no modifications to the analog servo.

### Discussion of Test Results

The test setup described above provided a means for one-to-one comparison of the performance of the digital and analog caging loops. In order to obtain such a comparison, however, it was necessary to match the gains of the two loops since the digital computations, as described in Section 2, assumed that the gain would be adjusted on the analog level, i. e., in the power amplifier. The criterion used to match the gain (applied torque vs pickoff angle) of the digital loop to that of the analog loop was to operate each servo 6 db below its marginal stability level. Using this criterion it was found that the digital loop gain was approximately 10 db below that of the analog loop.

Frequency response data was taken for both the digital and analog loops. Figure 20 shows the output signal (i. e., the torquer voltage) response versus frequency. Figure 21 shows the error signal (i. e., pickoff angle) versus frequency. These figures are actually families of responses showing variations resulting from adjusting the "integral gain time constant" in the digital loop. This time constant is directly related to the location of the zero of the digital transfer functions described in Section 2. The range or variation corresponds to varying this zero location between 123 Hz and 12.7 Hz.

It is apparent from Figure 18 that the closed loop response of the digital loop compares very favorably with that of the analog loop in terms of the torquer output versus frequency. This quantity is, of course, of primary interest as it is the ultimate measure of gyro rate.

Figure 19 indicates that the gyro pickoff angles are substantially larger for the digital loop than for the analog loop for low frequency inputs. This is attributable to the lower gain in the digital loop which was established by the gain matching criterion described above.

The primary reason that the marginal stability gain for the digital loop is lower than for the analog loop is the effective phase shift introduced by the finite computer iteration rate. Thus as the computational frequency is increased it is expected that the digital loop gain established by the gain matching procedure would be increased and the pickoff angle versus frequency response of the digital loop would more closely approximate the corresponding analog response. Unfortunately this conclusion could not readily be verified due to computer timing limitations.

The primary ramifications of the lower loop gain in the digital loop is a lowering of the bandwidth of the caging loop which would occur in a gyro with both axes mechanized digitally. Subsequent analysis indicates that the effective bandwidth of such an all-digital gyro would be approximately 25 Hz for the configuration which was tested (i. e., 1200 Hz digital processing). This corresponds closely with the 30 Hz bandwidth used in Teledyne's current analog caging loops. This bandwidth can be further increased by increasing the computational frequency and can be expected to approach the 100 Hz of the new analog design with very high speed processing.

In summary, then, the test results were in general concert with expectations and the feasibility of using digital filtering in place of conventional analog caging loops for the TDF tuned-gimbal gyroscope was demonstrated.

## VII. SUMMARY AND CONCLUSIONS

The primary objective of this program was to demonstrate the feasibility of replacing existing state-of-the-art analog gyro compensation loops with digital computations. This objective was realized during the course of the program.

A breadboard design was established in which one axis of a Teledyne tuned-gimbal TDF gyro was caged digitally while the other was caged using conventional analog electronics. The digital loop was designed analytically to closely resemble the analog loop in performance. The breadboard was subjected to various static and dynamic tests in order to establish the relative stability characteristics and frequency responses of the digital and analog loops. Several variations of the digital loop configuration were evaluated. The results were very favorable - it appears that digital caging is indeed a practical approach.

The primary limitation to the digital compensation loop approach appears to be the requirement for high processing rates. The tests which were performed indicate that the minimum processing rate for acceptable loop performance is approximately 1200 Hz. Using the general purpose IMP-16 on TDY-52B computers essentially all of the available computer time was required to perform the digital caging loop functions for a single gyro axis at this rate. (These functions include all timing, control, sampling, etc., as well as the implementation of the actual digital filters.) For this reason it appears desirable to consider a special purpose digital processor for the digital caging loop task. Such a processor could be quite simple in concept since the only arithmetic functions required to implement the digital filters which were derived during the program are adds, subtracts, and shifts.

The primary advantages of using digital caging loops in place of conventional analog loops are reduction of cost, size, weight, and power, increased reliability, and simplified maintenance, resulting from the elimination of a substantial amount of hardware from the IMU Electronics. The electronics which are eliminated using the digital technique include pickoff demodulators, caging electronics, spin supplies, clock and timing functions, and pickoff excitation generation. New functions which must be performed with the digital loop are digital-to-analog conversion and, optionally, the special purpose digital processing. Since both of these functions may be multiplexed to handle all sensor axes, the hardware required is minimal. A preliminary design analysis has indicated the hardware requirement to perform these two

functions is of the order of 5 to 20% of that required for the analog functions which they replace depending upon the level of redundancy which is employed in the system. The resulting savings in direct acquisition cost for a fail-op/fail-op redundant strapdown navigator is projected to be approximately \$4000 per system in quantities of 150 systems.

The performance of a system using digital caging loops is expected to be virtually identical to that using conventional analog technology. This is particularly true if a special purpose processor is employed, since the processing rate can be increased beyond the 1200 Hz which was used in the demonstration. Higher rates will provide digital loop performance which matches the analog loop performance even more closely than described in this report.

Other than the limitations imposed by computational speed, the digital loop which was breadboarded during the program appears to be suitable for use in a practical system design without any significant modifications. The general design philosophy, filtering algorithms, computer word length, A/D and D/A converter accuracies and resolutions, etc., which were employed in the breadboard design are all suitable for use in a production design.

APPENDIX A  
PROGRAM LISTING

This is the assembly language gyro program as assembled on Teledyne unspecialized assembler TUMPA. Assembled code was punched out in special loading format on mylar teletype tape for loading via teletype into the IMP-16P. This program will also run on the TDY-52B.

\*\*\*\*\* TELEDYNE UNSPECIALIZED MACRO ASSEMBLER

- B PAD LITERAL INITIAL CHARACTER
- D OTHER THAN OCTAL DIGIT
- D DECIMAL CHARACTER IN OCTAL FIELD
- K TOO MANY CHARACTERS IN FIELD
- P PROGRAM COLLATER PROBLEM
- S MEANINGLESS PAD LINE
- D MACRO NOT IN TABLE
- D MACRO TOO DEEPLY NESTED

```
C001 $.C/ GYRD PROGRAM VERSION 1.7 TAPE 987
C002 $.PC,20,1/
C003 $.PCIF,2,LDB,2/
C004 $.PCIF,2,STB,2/
C005 $.PCIF,2,DADD,2/
C006 $.PCIF,2,OSLB,2/
C007 $.PCIF,2,HPY,2/
C008 $.PCIF,2,DIV,2/
C009 $.TRAN,3,2/
C010 $.TRAN,4,2/
C011 $.TRAN,3,1/
C012 $.TRAN,4,1/
C013 $.TRAN,3,1/
C014 $.BDDL,2,R0,0/
C015 $.BDDL,2,R1,1/
C016 $.BDDL,2,R2,2/
C017 $.BDDL,2,R3,3/
C018 $.BDDL,2,ACC,0/
C019 $.BDDL,2,AC1,1/
C020 $.BDDL,2,AC2,2/
C021 $.BDDL,2,AC3,3/
C022 $.BDDL,2,BASE,0/
C023 $.BDDL,2,PC,1/
C024 $.BDDL,2,XR2,2/
C025 $.BDDL,2,XR3,3/
C026 $.BDDL,2,XMIT,4/
C027 $.BDDL,2,LNK,17/
C028 $.BDDL,2,OV,16/
C029 $.BDDL,2,CY,15/
C030 $.BDDL,2,IE,1/
C031 $.BDDL,2,SEL,2/
C032 $.BDDL,2,REAR,3/
C033 $.BDDL,2,XHIT,4/
C034 $.BDDL,2,JC14,16/
C035 $.BDDL,2,JC1,1/
C036 $.BDDL,2,JC2,2/
C037 $.BDDL,2,JC3,3/
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TUMPA PAGE 11112

C038 \$.BOCL,2,JC4,4/  
C039 \$.BOCL,2,JC5,5/  
C040 \$.BOCL,2,JC6,10/  
C041 \$.BOCL,2,JC9,11/  
C042 \$.BOCL,2,JC10,12/  
C043 \$.BOCL,2,JC11,13/  
C044 \$.FEED/

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C045 $.ORG,1/
C046 $.C/ INTERRUPT EXECUTIVE
00001 C047  ,PUSH,ACC/
00002 C048  ,PUSH,AC3/
00003 C049  ,LI,AC3,0/
00004 C050  ,RIN,170/
00005 C051 XX,RCPY,ACC,AC3/
00005 C052  ,JMP,AC3,C/
C053 $.ORG,10/
C054 $.C/ X PEAK BUFFERS
00010 C055 XP1,DCT,C/ FLAG1
00011 C056 XP2,DCT,C/ CELL2
00012 C057 XP3,DCT,C/ CELL3
00013 C058 XP4,DCT,C/ CELL4
00014 C059 XP5,DCT,C/ FLAG2
00015 C060 XP6,DCT,C/ CELL5
00016 C061 XP7,DCT,C/ CELL6
00017 C062 XP8,DCT,C/ CELL7
00020 C063 C10,DCT,40000/
00021 C064 C14,DCT,140000/
00022 C065 MT,DCT,0/
C066 $.ORG,30/
C067 $.C/ Y PEAK BUFFERS
00030 C068 YP1,DCT,C/ FLAG1
00031 C069 YP2,DCT,C/ CELL1
00032 C070 YP3,DCT,C/ CELL2
00033 C071 YP4,DCT,C/ FLAG2
00034 C072 YP5,DCT,C/ CELL3
00035 C073 YP6,DCT,C/ CELL4
C074 $.ORG,40/
00040 C075 XX1,RCPY,ACC,AC3/
00041 C076 XX2,JMP,BASE,FGD/
00042 C077 FGD,LD,ACC,BASE,XX1/
00043 C078  ,ST,ACC,BASE,XX/
00044 C079  ,PULL,AC3/
00045 C080  ,PULL,ACC/
00046 C081  ,RIJ,0/
C082 $.ORG,100/
C083 $.C/ DATA STORAGE POINTER
00100 C084 DSPC,DCT,4000/
00101 C085 DSP,DCT,C/
00102 C086 SIGN,DCT,100000/
C087 $.C/ GYRE MAIN
00103 C088 MX,DCT,0/
00104 C089 M,DCT,0/
C090 $.ORG,1000/
C091 $.C/ X PEAK INTERRUPT SERVICE
01000 C092  ,LI,AC3,0/
01001 C093  ,RIN,160/
01002 C094  ,PUSH,ACC/
01003 C095  ,LD,ACC,BASE,XP1/

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01004 C096 ,BCC*,1,XPEAK2/
01005 C097 ,LI,ACC,0/
01005 C098 ,ST,ACC,BASE,XP1/
01007 C099 ,LD,ACC,BASE,XP7/
01010 C100 ,ST,ACC,BASE,XP4/
01011 C101 XPEAK4,LD,ACC,BASE,XP6/
01012 C102 ,BCC*,2,XPEK4/
01013 C103 ,CAI,ACC,1/
01014 C104 ,SHR,ACC,4/
01015 C105 ,CAI,ACC,1/
01016 C106 ,ST,ACC,BASE,XP3/
01017 C107 ,JMP*,XPEK5/
01020 C108 XPEK4,SHR,ACC,4/
01021 C109 ,ST,ACC,BASE,XP3/
01022 C110 XPEK5,PULL,ACC/
01023 C111 ,ST,ACC,BASE,XP2/
01024 C112 ,PULL,ACC/
01025 C113 ,PULL,ACC/
01026 C114 ,RTI,0/
01027 C115 XPEAK2,LI,ACC,1/
01030 C116 ,ST,ACC,BASE,XP1/
01031 C117 ,LD,ACC,BASE,XP3/
01032 C118 ,ST,ACC,BASE,XP8/
01033 C119 XPEAK6,LD,ACC,BASE,XP2/
01034 C120 ,BCC*,2,XPEAK7/
01035 C121 ,CAI,ACC,1/
01036 C122 ,SHR,ACC,4/
01037 C123 ,CAI,ACC,1/
01040 C124 ,ST,ACC,BASE,XP7/
01041 C125 ,JMP*,XPEAK8/
01042 C126 XPEAK7,SHR,ACC,4/
01043 C127 ,ST,ACC,BASE,XP7/
01044 C128 XPEAK8,PULL,ACC/
01045 C129 ,ST,ACC,BASE,XP6/
01046 C130 ,PULL,ACC/
01047 C131 ,PULL,ACC/
01050 C132 ,RTI,0/
C133 ,CRC,1200/
C134 ,C/ Y PEAK INTERRUPT SERVICE
01200 C135 YPEAK,LI,ACC,0/
01201 C136 ,RIN,100/
01202 C137 ,PUSH,ACC/
01203 C138 ,LD,ACC,BASE,YP1/
01204 C139 ,BCC*,1,YPEAK2/
01205 C140 ,LI,ACC,0/
01206 C141 ,ST,ACC,BASE,YP1/
01207 C142 ,LD,ACC,BASE,YP5/
01210 C143 ,BCC*,2,YPEAK3/
01211 C144 ,CAI,ACC,1/
01212 C145 ,SHR,ACC,4/
01213 C146 ,CAI,ACC,4/

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01214 C147 ,SUB,ACC,BASE,YP5/
01215 C148 ,ST,ACC,BASE,YP3/
01216 C149 ,JMP*,YPEAK4/
01217 C150 YPEAK3,SHR,ACC,4/
01220 C151 ,SUB,ACC,BASE,YP5/
01221 C152 ,ST,ACC,BASE,YP3/
01222 C153 YPEAK4,PULL,ACC/
01223 C154 ,ST,ACC,BASE,YP2/
01224 C155 ,PULL,ACC3/
01225 C156 ,PULL,ACC/
01226 C157 ,RTI,0/
01227 C158 YPEAK2,LI,ACC,1/
01230 C159 ,ST,ACC,BASE,YP1/
01231 C160 ,LD,ACC,BASE,YP2/
01232 C161 ,BCC*,2,YPEAK5/
01233 C162 ,CAI,ACC,1/
01234 C163 ,SHR,ACC,4/
01235 C164 ,CAI,ACC,1/
01236 C165 ,SUB,ACC,YP2/ ,SUB,ACC, BASE, YP2/
01237 C166 ,ST,ACC,BASE,YP6/
01240 C167 ,JMP*,YPEAK6/
01241 C168 YPEAK5,SHR,ACC,4/
01242 C169 ,SUB,ACC,BASE,YP2/
01243 C170 ,ST,ACC,BASE,YP6/
01244 C171 YPEAK6,PULL,ACC/
01245 C172 ,ST,ACC,BASE,YP5/
01245 C173 ,PULL,ACC3/
01247 C174 ,PULL,ACC/
01250 C175 ,RTI,0/
C176 $.ORG,1500/
C177 $.C/ DATA STORAGE INTERRUPT SERVICE
01500 C178 DS,LD,ACC,BASE,DSP/
01501 C179 ,SHR,ACC,14/
01502 C180 ,BDC*,3,DS6/
01503 C181 ,LD,ACC,BASE,XP1/
01504 C182 ,BDC*,1,DS2/
01505 C183 ,LD,ACC,BASE,XP6/
01506 C184 ,JMP*,DS3/
01507 C185 DS2,LD,ACC,BASE,XP2/
01510 C186 DS3,LD,ACC3,BASE,DSP/
01511 C187 ,ST,ACC,ACC3,0/
01512 C188 ,LI,ACC,1/
01513 C189 ,RADD,ACC,ACC3/
01514 C190 ,LD,ACC,BASE,YP1/
01515 C191 ,BCC*,1,DS4/
01516 C192 ,LD,ACC,BASE,YP5/
01517 C193 ,JMP*,DS5/
01520 C194 DS4,LD,ACC,BASE,YP2/
01521 C195 DS5,ST,ACC,ACC3,0/
01522 C196 ,LI,ACC,1/
01523 C197 ,RADD,ACC,ACC3/

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01524 C198 ,LD,ACC,BASE,MT//
01525 C199 ,ST,ACC,AC3,0//
01526 C200 ,LI,ACC,1/
01527 C201 ,RADD,ACC,AC3/
01530 C202 ,ST,AC3,BASE,DSP/
01531 C203 DS6,PULL,AC3/
01532 C204 ,PULL,ACC/
01533 C205 ,RTI,0/
C206 $,ORG,2000/
C207 $.C/ GYPD MAIN PROGRAM
02000 C208 MAIN,LD,ACC,BASE,XX2/
02001 C209 ,ST,ACC,BASE,XX/
02002 C210 ,LI,AC3,0/
02003 C211 ,LD,ACC,BASE,DSPC/
02004 C212 ,ST,ACC,BASE,DSP/
02005 C213 ,LI,ACC,0/
02006 C214 ,ST,ACC,BASE,MX/
02007 C215 ,SFLG,IEN,0/
02010 C216 RET,LD,ACC,BASE,XP1/
02011 C217 ,BCC*,1,MAIN2/
02012 C218 ,LD,ACC,BASE,XP8/
02013 C219 ,SHL,ACC,4/
02014 C220 ,CAI,ACC,1/
02015 C221 ,ADD,ACC,BASE,XP8/
02016 C222 ,ADD,ACC,BASE,XP6/
02017 C223 ,ADD,ACC,BASE,XP7/
02020 C224 ,ADD,ACC,BASE,MX/
02021 C225 ,ST,ACC,BASE,MX/
02022 C226 ,JMP*,MAIN3/
02023 C227 MAIN2,LD,ACC,BASE,XP4/
02024 C228 ,SHL,ACC,4/
02025 C229 ,CAI,ACC,1/
02026 C230 ,ADD,ACC,BASE,XP4/
02027 C231 ,ADD,ACC,BASE,XP2/
02030 C232 ,ADD,ACC,BASE,XP3/
02031 C233 ,ADD,ACC,BASE,MX/
02032 C234 ,ST,ACC,BASE,MX/
02033 C235 MAIN3,BCC*,2,MAIN4/
02034 C236 ,CAI,ACC,1/
02035 C237 ,SHL,ACC,1/
02036 C238 ,RDC*,2,MAIN5/
02037 C239 ,LD,ACC,BASE,C14/
02040 C240 ,ST,ACC,BASE,MX/
02041 C241 ,JMP*,MAIN5/
02042 C242 MAIN4,SHL,ACC,1/
02043 C243 ,RDC*,2,MAIN5/
02044 C244 ,LD,ACC,BASE,C10/
02045 C245 ,ST,ACC,BASE,MX/
02046 C246 MAIN5,LD,ACC,BASE,YP1/
02047 C247 ,BCC*,1,MAIN6/
02050 C248 ,LI,ACC,0/

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02051 0249 ,ADD,ACO,BASE,YP5/
02052 0250 ,ADD,ACO,BASE,YP6/
02053 0251 ,ST,ACO,BASE,H/
02054 0252 ,JMP*,MAIN7/
02055 0253 MAIN6,LI,ACO,0/
02056 0254 ,ADD,ACO,BASE,YP2/
02057 0255 ,ADD,ACO,BASE,YP3/
02060 0256 ,ST,ACO,BASE,H/
02061 0257 MAIN7,LD,ACO,BASE,Hx/
02062 0258 ,SUB,ACO,BASE,H/
02063 0259 ,ST,ACO,BASE,H/
02064 0260 MAIN10,REC#,2,MAIN11/
02065 0261 ,CAI,ACO,1/
02064 0262 ,OR,ACO,BASE,SIGN/
02067 0263 MAIN11,LI,AC3,0/
02070 0264 ,RCUT,170/
02071 0265 ,ST,ACO,BASE,HT/
02072 0266 ,JMP*,RET/
0207 0267 $.C/ PROGRAM SECTION DUMP
02073 0268 DUMP,LD,AC3,BASE,OSPC/
02074 0269 DP2,RCPY,AC3,ACO/
02075 0270 ,SHR,ACO,14/
02076 0271 ,BCC#,3,DP2/
02077 0272 ,LD,ACO,AC3,0/
02100 0273 ,SHR,ACO,10/
02101 0274 ,LD*,AC2,PUTC./
02102 0275 ,JSR,AC2,0/
02103 0276 ,LD,ACO,AC3,0/
02104 0277 ,AND*,ACO,MASK/
02105 0278 ,LD*,AC2,PUTC./
02106 0279 ,JSR,AC2,0/
02107 0280 ,LI,ACO,1/
02110 0281 ,RAUU,ACO,AC3/
02111 0282 ,JMP*,DP2/
02112 0283 PUTC.,DCT,77131/
02113 0284 MASK,DCT,377/
0285 $.END/
0286 $.FEED/

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CROSS REFERENCE TABLE LISTING

C10 00020 C2044  
 C14 00021 C2037  
 DP2 02074 C2076 02111  
 DS 01500  
 DS2 01507 C1504  
 DS3 01510 C1506  
 DS4 01520 C1515  
 DS5 01521 C1517  
 DS6 01531 C1502  
 DSP 00101 C1500 01510 01530 02004  
 DSPC 00100 C2003 02073  
 DLMP 02073  
 FGD 00042 C0041  
 H 00104 C2053 02060 02062 02063  
 MAIN 02000  
 MAIN10 02064  
 MAIN11 02067 C2064  
 MAIN2 02023 C2011  
 MAIN3 02033 C2022  
 MAIN4 02042 C2033  
 MAIN5 02046 C2036 02041 02043  
 MAIN6 02055 C2047  
 MAIN7 02061 C2054  
 MASK 02113 C2104  
 MT 00022 C1524 02071  
 MX 00103 C2006 02020 02021 02031 02032 02040 02045 02061  
 PLTC. 02112 C2101 02105  
 RET 02010 C2072  
 SIGN 00102 C2066  
 XP1 00010 C1003 01006 01030 C1503 02010  
 XP2 00011 C1023 01033 01507 02027  
 XP3 00012 C1016 C1021 01031 02030  
 XP4 00013 C1010 02023 02026  
 XP5 00014  
 XP6 00015 C1011 01045 01505 02016  
 XP7 00016 C1007 01040 01043 02017  
 XP8 00017 C1032 02012 02015  
 XPEAK2 01027 C1004  
 XPEAK4 01011  
 XPEAK6 01032  
 XPEAK7 01042 C1024  
 XPEAK8 01044 C1041  
 XPEAK4 01023 C1012  
 XPEAK5 01022 C1017  
 XX 00005 C0043 02001  
 XX1 00040 C0042  
 XX2 00041 C2000  
 YP1 00030 C1203 01206 01230 C1514 02046  
 YP2 00031 C1223 01231 01236 01242 01520 02056  
 YP3 00032 C1215 01221 02057

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YP4 00033  
YP5 00034 C1207 01214 01220 C1245 01516 02051  
YP6 00035 C1237 01243 02052  
YPEAK 01200  
YPEAK2 01227 C1204  
YPEAK3 01217 C1210  
YPEAK4 01222 C1216  
YPEAK5 01241 C1232  
YPEAK6 01244 C1240  
C288 \$.FEED/

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C289 \$.C/ THESE CARDS SPECIFY WORD ASSEMBLY  
 C290 \$.IF,2,LD/  
 C291 \$.SETC,6,10/  
 C292 \$.JUMP,A/  
 C293 \$.IF,2,LI/  
 C294 \$.SETC,5,23/  
 C295 \$.JUMP,R/  
 C296 \$.IF,2,LIN/  
 C297 \$.SETC,5,23/  
 C298 \$.SETC,6,0/  
 C299 \$.SUB,6,4,4/  
 C300 \$.JUMP,R/  
 C301 \$.IF,2,LDI/  
 C302 \$.SETC,6,11/  
 C303 \$.JUMP,A/  
 C304 \$.IF,2,LDR/  
 C305 \$.SETC,5,2300/  
 C306 \$.JUMP,K/  
 C307 \$.IF,2,ST/  
 C308 \$.SETC,6,12/  
 C309 \$.JUMP,A/  
 C310 \$.IF,2,STI/  
 C311 \$.SETC,6,13/  
 C312 \$.JUMP,A/  
 C313 \$.IF,2,STB/  
 C314 \$.SETC,5,2320/  
 C315 \$.JUMP,K/  
 C316 \$.IF,2,RXCH/  
 C317 \$.SETC,5,34/  
 C318 \$.JUMP,D/  
 C319 \$.IF,2,RCPY/  
 C320 \$.SETC,5,35/  
 C321 \$.JUMP,D/  
 C322 \$.IF,2,PLSH/  
 C323 \$.SETC,4,20/  
 C324 \$.JUMP,C/  
 C325 \$.IF,2,PULL/  
 C326 \$.SETC,4,21/  
 C327 \$.JUMP,C/  
 C328 \$.IF,2,XCHRS/  
 C329 \$.SETC,4,25/  
 C330 \$.JUMP,C/  
 C331 \$.IF,2,PLSHF/  
 C332 \$.SETC,3,1/  
 C333 \$.JUMP,L/  
 C334 \$.IF,2,PULLF/  
 C335 \$.SETC,3,5/  
 C336 \$.JUMP,L/  
 C337 \$.IF,2,ADD/  
 C338 \$.SETC,6,14/  
 C339 \$.JUMP,A/

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C340 \$.IF,2,DADD/  
 C341 \$.SETC,5,224C/  
 C342 \$.JUMP,K/  
 C343 \$.IF,2,CAI/  
 C344 \$.SETC,5,24/  
 C345 \$.JUMP,B/  
 C346 \$.IF,2,RAND/  
 C347 \$.SETC,5,30/  
 C348 \$.JUMP,D/  
 C349 \$.IF,2,SUB/  
 C350 \$.SETC,6,15/  
 C351 \$.JUMP,A/  
 C352 \$.IF,2,DSUB/  
 C353 \$.SETC,5,2260/  
 C354 \$.JUMP,K/  
 C355 \$.IF,2,MPY/  
 C356 \$.SETC,5,2200/  
 C357 \$.JUMP,K/  
 C358 \$.IF,2,DIV/  
 C359 \$.SETC,5,2220/  
 C360 \$.JUMP,K/  
 C361 \$.IF,2,AND/  
 C362 \$.SETC,6,14/  
 C363 \$.JUMP,G/  
 C364 \$.IF,2,RAND/  
 C365 \$.SETC,5,37/  
 C366 \$.JUMP,D/  
 C367 \$.IF,2,OR/  
 C368 \$.SETC,6,19/  
 C369 \$.JUMP,G/  
 C370 \$.IF,2,RXOR/  
 C371 \$.SETC,5,36/  
 C372 \$.JUMP,D/  
 C373 \$.IF,2,SETBIT,3/  
 C374 \$.SETC,4,162/  
 C375 \$.JUMP,J/  
 C376 \$.IF,2,CLRBIT,4/  
 C377 \$.SETC,4,163/  
 C378 \$.JUMP,J/  
 C379 \$.IF,2,CMPBIT,13/  
 C380 \$.SETC,4,166/  
 C381 \$.JUMP,J/  
 C382 \$.IF,2,SETST/  
 C383 \$.SETC,4,160/  
 C384 \$.JUMP,J/  
 C385 \$.IF,2,CLRST/  
 C386 \$.SETC,4,161/  
 C387 \$.JUMP,J/  
 C388 \$.IF,2,AISZ/  
 C389 \$.SETC,5,22/  
 C390 \$.JUMP,R/

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C391 \$.IF,2,ISZ/  
C392 \$.SETC,5,36/  
C393 \$.JUMP,B/  
C394 \$.IF,2,DSZ/  
C395 \$.SETC,5,37/  
C396 \$.JUMP,B/  
C397 \$.IF,2,SKG/  
C398 \$.SETC,6,16/  
C399 \$.JUMP,A/  
C400 \$.IF,2,SKHE/  
C401 \$.SETC,6,17/  
C402 \$.JUMP,A/  
C403 \$.IF,2,SKAZ/  
C404 \$.SETC,6,16/  
C405 \$.JUMP,G/  
C406 \$.IF,2,SKBIT/  
C407 \$.SETC,4,165/  
C408 \$.JUMP,J/  
C409 \$.IF,2,SKSTF/  
C410 \$.SETC,4,164/  
C411 \$.JUMP,J/  
C412 \$.IF,2,ISCAN/  
C413 \$.SETC,3,2420/  
C414 \$.JUMP,UCT/  
C415 \$.IF,2,JMP/  
C416 \$.SETC,5,10/  
C417 \$.JUMP,B/  
C418 \$.IF,2,JMPI/  
C419 \$.SETC,5,11/  
C420 \$.JUMP,B/  
C421 \$.IF,2,JMPP/  
C422 \$.SETC,4,120/  
C423 \$.JUMP,J/  
C424 \$.IF,2,BCC/  
C425 \$.SETC,5,1/  
C426 \$.JUMP,F/  
C427 \$.IF,2,HALT/  
C428 \$.SETC,3,9/  
C429 \$.JUMP,L/  
C430 \$.IF,2,JSR/  
C431 \$.SETC,5,12/  
C432 \$.JUMP,B/  
C433 \$.IF,2,JSRP/  
C434 \$.SETC,4,6/  
C435 \$.JUMP,H/  
C436 \$.IF,2,JSRI/  
C437 \$.SETC,5,13/  
C438 \$.JUMP,B/  
C439 \$.IF,2,JSRIP/  
C440 \$.SETC,4,7/  
C441 \$.JUMP,H/

C442 \$.IF,2,JINTC/  
 C443 \$.SETC,4,122/  
 C444 \$.JUMP,J/  
 C445 \$.IF,2,JINT/  
 C446 \$.SETC,4,122/  
 C447 \$.JUMP,J/  
 C448 \$.IF,2,RTS/  
 C449 \$.SETC,4,4/  
 C450 \$.JUMP,H/  
 C451 \$.IF,2,RTI/  
 C452 \$.SETC,4,2/  
 C453 \$.JUMP,H/  
 C454 \$.IF,2,RDL/  
 C455 \$.SETC,5,26/  
 C456 \$.JUMP,B/  
 C457 \$.IF,2,RLR/  
 C458 \$.SETC,5,26/  
 C459 \$.JUMP,BK/  
 C460 \$.IF,2,SHL/  
 C461 \$.SETC,5,27/  
 C462 \$.JUMP,R/  
 C463 \$.IF,2,SHR/  
 C464 \$.SETC,5,27/  
 C465 \$.JUMP,BR/  
 C466 \$.IF,2,RIN/  
 C467 \$.SETC,4,10/  
 C468 \$.JUMP,H/  
 C469 \$.IF,2,RDUT/  
 C470 \$.SETC,4,14/  
 C471 \$.JUMP,H/  
 C472 \$.IF,2,SFLG/  
 C473 \$.SETC,5,2/  
 C474 \$.JUMP,E/  
 C475 \$.IF,2,PFLG/  
 C476 \$.SETC,5,3/  
 C477 \$.JUMP,E/  
 C478 \$.IF,2,LC\*/  
 C479 \$.SETC,5,10/  
 C480 \$.JUMP,APC/  
 C481 \$.IF,2,LDI\*/  
 C482 \$.SETC,5,11/  
 C483 \$.JUMP,APC/  
 C484 \$.IF,2,ST\*/  
 C485 \$.SETC,5,12/  
 C486 \$.JUMP,APC/  
 C487 \$.IF,2,STI\*/  
 C488 \$.SETC,5,13/  
 C489 \$.JUMP,APC/  
 C490 \$.IF,2,ADD\*/  
 C491 \$.SETC,5,14/  
 C492 \$.JUMP,APC/

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C493 \$.IF,2,SUB\*/  
 C494 \$.SETC,5,13/  
 C495 \$.JUMP,APC/  
 C496 \$.IF,2,AND\*/  
 C497 \$.SETC,5,14/  
 C498 \$.JUMP,GPC/  
 C499 \$.IF,2,DR\*/  
 C500 \$.SETC,5,15/  
 C501 \$.JUMP,GPC/  
 C502 \$.IF,2,SKG\*/  
 C503 \$.SETC,5,16/  
 C504 \$.JUMP,APC/  
 C505 \$.IF,2,SKNE\*/  
 C506 \$.SETC,5,17/  
 C507 \$.JUMP,APC/  
 C508 \$.IF,2,SKAZ\*/  
 C509 \$.SETC,5,16/  
 C510 \$.JUMP,GPC/  
 C511 \$.IF,2,JMP\*/  
 C512 \$.SETC,4,10/  
 C513 \$.JUMP,BPC/  
 C514 \$.IF,2,JMP1\*/  
 C515 \$.SETC,4,11/  
 C516 \$.JUMP,APC/  
 C517 \$.IF,2,BCC\*/  
 C518 \$.SETC,5,1/  
 C519 \$.JUMP,FPC/  
 C520 \$.IF,2,JSR\*/  
 C521 \$.SETC,4,12/  
 C522 \$.JUMP,APC/  
 C523 \$.IF,2,JSRI\*/  
 C524 \$.SETC,4,13/  
 C525 \$.JUMP,BPC/  
 C526 \$.IF,2,RTS\*/  
 C527 \$.SETC,4,4/  
 C528 \$.JUMP,HPC/  
 C529 \$.IF,2,RT1\*/  
 C530 \$.SETC,4,2/  
 C531 \$.JUMP,HPC/  
 C532 \$.IF,2,RIN\*/  
 C533 \$.SETC,4,10/  
 C534 \$.JUMP,HPC/  
 C535 \$.IF,2,ROUT\*/  
 C536 \$.SETC,4,14/  
 C537 \$.JUMP,HPC/  
 C538 \$.IF,2,ISZ\*/  
 C539 \$.SETC,4,36/  
 C540 \$.JUMP,BPC/  
 C541 \$.IF,2,OSZ\*/  
 C542 \$.SETC,4,37/  
 C543 \$.JUMP,BPC/

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C544 \$.IF,2,0CT/  
 C545 \$.SPCT,0CT/  
 C546 \$.MOVE,3,0,20,0/  
 C547 \$.WORD,1/  
 C548 \$.RET/  
 C549 \$.IF,2,JMPP-/  
 C550 \$.SETC,4,120/  
 C551 \$.SETC,5,400/  
 C552 \$.ADD,3,5,3/  
 C553 \$.JUMP,J/  
 C554 \$.IF,2,JSRP-/  
 C555 \$.SETC,4,6/  
 C556 \$.SETC,5,400/  
 C557 \$.ADD,3,5,3/  
 C558 \$.JUMP,H/  
 C559 \$.IF,2,JINT-/  
 C560 \$.SETC,4,122/  
 C561 \$.SETC,5,440/  
 C562 \$.ADD,3,5,3/  
 C563 \$.JUMP,J/  
 C564 \$.IF/ \*\*DEFAULT\*\*  
 C565 \$.MOVE,1,0,20,0/  
 C566 \$.WORD,1/  
 C567 \$.RET/  
 C568 \$.SPCT,A/  
 C569 \$.MOVE,6,0,4,14/  
 C570 \$.MOVE,3,0,2,12/  
 C571 \$.MOVE,4,0,2,10/  
 C572 \$.MOVE,5,0,10,0/  
 C573 \$.WORD,1/  
 C574 \$.RET/  
 C575 \$.SPCT,BK/  
 C576 \$.SETC,6,0/  
 C577 \$.SUB,6,4,4/  
 C578 \$.SPCT,B/  
 C579 \$.MOVE,5,0,6,12/  
 C580 \$.MOVE,3,0,2,10/  
 C581 \$.MOVE,4,0,10,0/  
 C582 \$.WORD,1/  
 C583 \$.RET/  
 C584 \$.SPCT,C/  
 C585 \$.MOVE,4,0,6,12/  
 C586 \$.MOVE,3,0,2,10/  
 C587 \$.WORD,1/  
 C588 \$.RET/  
 C589 \$.SPCT,0/  
 C590 \$.MOVE,5,3,4,14/  
 C591 \$.MOVE,5,2,1,7/  
 C592 \$.MOVE,5,0,2,0/  
 C593 \$.MOVE,3,0,2,12/  
 C594 \$.MOVE,4,0,2,10/

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C595 \$.WORD,1/  
 C596 \$.RET/  
 C597 \$.SPCT,E/  
 C598 \$.MOVE,5,1,1,13/  
 C599 \$.MOVE,5,0,1,7/  
 C600 \$.MOVE,3,0,3,10/  
 C601 \$.MOVE,4,0,7,0/  
 C602 \$.WORD,1/  
 C603 \$.RET/  
 C604 \$.SPCT,F/  
 C605 \$.MOVE,5,0,4,14/  
 C606 \$.MOVE,3,0,4,10/  
 C607 \$.MOVE,4,0,10,0/  
 C608 \$.WORD,1/  
 C609 \$.RET/  
 C610 \$.SPCT,G/  
 C611 \$.MOVE,6,0,5,13/  
 C612 \$.MOVE,3,0,1,12/  
 C613 \$.MOVE,4,0,2,10/  
 C614 \$.MOVE,5,0,10,0/  
 C615 \$.WORD,1/  
 C616 \$.RET/  
 C617 \$.SPCT,H/  
 C618 \$.MOVE,4,0,4,7/  
 C619 \$.MOVE,3,0,7,0/  
 C620 \$.WORD,1/  
 C621 \$.RET/  
 C622 \$.SPCT,J/  
 C623 \$.MOVE,4,0,14,4/  
 C624 \$.MOVE,3,0,4,0/  
 C625 \$.WORD,1/  
 C626 \$.RET/  
 C627 \$.SPCT,K/  
 C628 \$.MOVE,5,0,20,0/  
 C629 \$.MOVE,3,0,2,10/  
 C630 \$.WORD,1/  
 C631 \$.MOVE,4,0,20,0/  
 C632 \$.WORD,1/  
 C633 \$.RET/  
 C634 \$.SPCT,L/  
 C635 \$.MOVE,3,0,4,7/  
 C636 \$.WORD,1/  
 C637 \$.RET/  
 C638 \$.SPCT,APC/  
 C639 \$.CPC,6/  
 C640 \$.SFTC,7,1/  
 C641 \$.MOVE,5,0,4,14/  
 C642 \$.MOVE,3,0,2,12/  
 C643 \$.MOVE,7,0,1,10/  
 C644 \$.ADD,6,7,7/  
 C645 \$.SUB,4,7,4/

C646 \$.MOVE,4,0,10,0/  
 C647 \$.WORD,1/  
 C648 \$.RET/  
 C649 \$.SPCT,APC/  
 C650 \$.CPC,5/  
 C651 \$.SETC,6,1/  
 C652 \$.MOVE,4,0,6,12/  
 C653 \$.MOVE,6,0,2,10/  
 C654 \$.ADD,5,6,6/  
 C655 \$.SUB,3,6,3/  
 C656 \$.MOVE,3,0,10,0/  
 C657 \$.WORD,1/  
 C658 \$.RET/  
 C659 \$.SPCT,FPC/  
 C660 \$.CPC,6/  
 C661 \$.SETC,7,1/  
 C662 \$.MOVE,5,0,4,14/  
 C663 \$.MOVE,3,0,4,10/  
 C664 \$.ADD,6,7,7/  
 C665 \$.SUB,4,7,4/  
 C666 \$.MOVE,4,0,10,0/  
 C667 \$.WORD,1/  
 C668 \$.RET/  
 C669 \$.SPCT,6PC/  
 C670 \$.CPC,6/  
 C671 \$.SETC,7,1/  
 C672 \$.MOVE,5,0,5,13/  
 C673 \$.MOVE,3,0,1,12/  
 C674 \$.MOVE,7,0,2,10/  
 C675 \$.ADD,6,7,7/  
 C676 \$.SUB,4,7,4/  
 C677 \$.MOVE,4,0,10,0/  
 C678 \$.WORD,1/  
 C679 \$.RET/  
 C680 \$.SPCT,HPC/  
 C681 \$.CPC,5/  
 C682 \$.SETC,6,1/  
 C683 \$.MOVE,4,0,11,7/  
 C684 \$.ADD,5,6,6/  
 C685 \$.SUB,3,6,3/  
 C686 \$.MOVE,3,0,7,0/  
 C687 \$.WORD,1/  
 C688 \$.RET/  
 C689 \$.ASM/

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ASSEMBLED MACHINE LANGUAGE LISTING

000001	00000040000	000002	00000041400	000003	00000047400	000004	00000002170	000005	000000031601
000005	00000021400	000010	00000000000	000011	00000000000	000012	00000000000	000013	00000000000
000014	00000000300	000015	00000000000	000016	00000000000	000017	00000000000	000020	000000040000
000021	00000014000	000022	00000000000	000030	00000000000	000031	00000000000	000032	000000000000
000033	00000000000	000034	00000000000	000035	00000000000	000040	000000031601	000041	000000020042
000042	000000100040	000043	000000120005	000044	000000043400	000045	000000042000	000046	000000004000
000100	000000004000	000101	000000000000	000102	000000100000	000103	000000000000	000104	000000000000
001000	000000047400	001001	000000002160	001002	000000004000	001003	000000100010	001004	00000010422
001005	000000046000	001006	000000120010	001007	000000100016	001010	000000120013	001011	000000100015
001012	000000011005	001013	000000050001	001014	000000056374	001015	000000050001	001016	000000120012
001017	000000020402	001020	000000056374	001021	000000120012	001022	000000042000	001023	000000120011
001024	000000043400	001025	000000042000	001026	000000000400	001027	000000044001	001030	000000120010
001031	000000100012	001032	000000120017	001033	000000100011	001034	000000011005	001035	000000050001
001036	000000056374	001037	000000050001	001040	000000120016	001041	000000020402	001042	000000056374
001043	000000120016	001044	000000042000	001045	000000120015	001046	000000043400	001047	000000042000
001050	000000000400	001200	000000047400	001201	000000002160	001202	000000004000	001203	000000100030
001204	00000010422	001205	000000046000	001206	000000120030	001207	000000100034	001210	000000011006
001211	000000050001	001212	000000056374	001213	000000050004	001214	000000150034	001215	000000120032
001216	000000020403	001217	000000056374	001220	000000150034	001221	000000120032	001222	000000042000
001223	000000120031	001224	000000043400	001225	000000042000	001226	000000000400	001227	000000046001
001230	000000120030	001231	000000100031	001232	000000011006	001233	000000050001	001234	000000056374
001235	000000050001	001236	000000150400	001237	000000120035	001240	000000020403	001241	000000056374
001242	000000150031	001243	000000120035	001244	000000042000	001245	000000120034	001246	000000043400
001247	000000042000	001250	000000000400	001500	000000100101	001501	000000056354	001502	000000011426
001503	000000100010	001504	000000010402	001505	000000100015	001506	000000020401	001507	000000100011
001510	000000106101	001511	000000121400	001512	000000045001	001513	000000031400	001514	000000100030
001515	00000010402	001516	000000100034	001517	000000020401	001520	000000100031	001521	000000121400
001522	000000046001	001523	000000031400	001524	000000100022	001525	000000121400	001526	000000046001
001527	000000031400	001530	000000126101	001531	000000043400	001532	000000042000	001533	000000000400
002000	000000100041	002001	000000120005	002002	000000047400	002003	000000100100	002004	000000120101
002005	000000046000	002006	000000120103	002007	000000004400	002010	000000100010	002011	000000010411
002012	000000100017	002013	000000056004	002014	000000050001	002015	000000140017	002016	000000140015
002017	000000140016	002020	000000140103	002021	000000120103	002022	000000020410	002023	000000100013
002024	000000056004	002025	000000050001	002026	000000140013	002027	000000140011	002030	000000140012
002031	000000140103	002032	000000120103	002033	000000011006	002034	000000050001	002035	000000056001
002036	000000011007	002037	000000100021	002040	000000120103	002041	000000020404	002042	000000056001
002043	000000011002	002044	000000100020	002045	000000120103	002046	000000100030	002047	000000010405
002050	000000046000	002051	000000140034	002052	000000140035	002053	000000120104	002054	000000020404
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002062	000000150104	002063	000000120104	002064	000000011002	002065	000000050001	002066	000000064102
002067	000000047400	002070	000000003170	002071	000000120022	002072	000000020715	002073	000000106100
002074	000000036201	002075	000000056364	002076	000000011775	002077	000000101400	002100	000000056370
002101	000000104410	002102	000000025000	002103	000000101400	002104	000000060406	002105	000000104404
002106	000000025000	002107	000000046001	002110	000000031400	002111	000000020762	002112	000000077131
002113	000000000377								

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## APPENDIX B

### LIST OF SYMBOLS

A	Gyro rotor moment of inertia normal to spin axis
$F_1(s), F_2(s)$	Direct-axis and cross-axis analog transfer functions
$F_1(z), F_2(z)$	Direct-axis and cross-axis digital transfer functions
$G_1(z), G_2(z)$	Mechanized direct-axis and cross-axis digital transfer functions
H(s)	General analog transfer function
H(z)	General digital transfer function
H'(s)	Dummy analog transfer function
k, K	Iteration index
$K_{PO}$	Pickoff gain factor
$K_{SA}$	Compensation gain factor
$K_T$	Torquer gain factor
M(k)	Total digital torque
$M_x, M_y$	Components of computer digital torque resulting from X- and Y- pickoff signals
$M_X, M_Y$	Analog rebalance torques
N	Gyro spin speed
$P_X, P_Y$	Precessional torques
s, S	Laplace Operator
$T_X, T_Y$	Total torques
$U_X, U_Y$	Digitized gyro pickoff angles
$X_{peak}$	Sampled X-axis pickoff angle
$Y_{peak}$	Sampled Y-axis pickoff angle



$z^{-1}$	Delay operator
$\theta_x, \theta_y$	Digitized gyro pickoff angles
$\theta_X, \theta_Y$	Gyro pickoff angles
$\tau$	Iteration period
$\omega_X, \omega_Y$	Angular rate inputs
$\omega_i, i = 1, 2, \dots$	Analog filter break frequencies
$\omega'_i, i = 1, 2, \dots$	Dummy analog filter break frequencies