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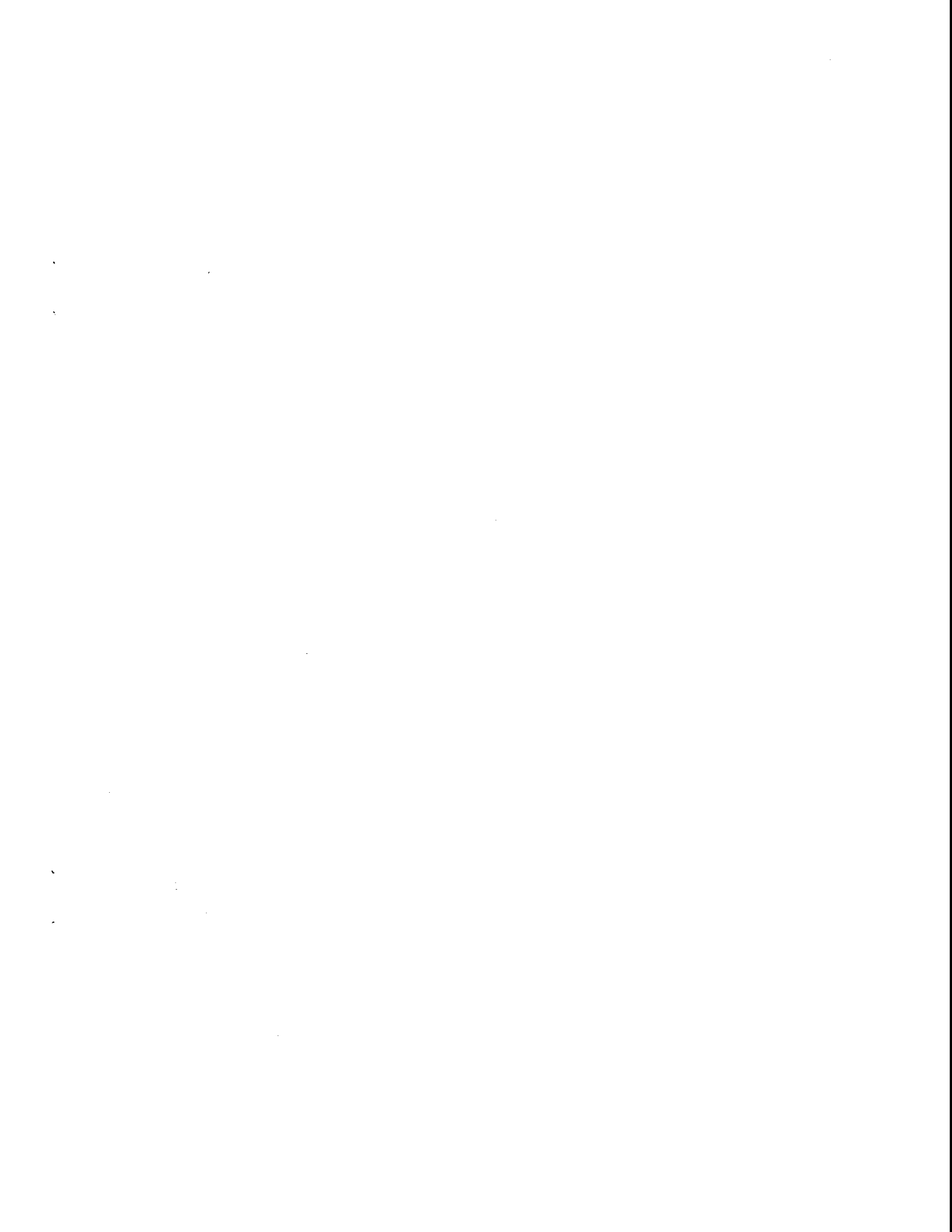
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**LONGITUDINAL RESIDUAL STRESSES  
IN BORON FIBERS**

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16. Abstract <p>A method of measuring the longitudinal residual stress distribution in boron fibers is presented. The residual stresses in commercial CVD boron on tungsten fibers of 102, 142, and 203 <math>\mu\text{m}</math> (4, 5.6, and 8 mil) diameters were determined. Results for the three sizes show a compressive stress at the surface [-800 to -1400 <math>\text{MN}/\text{m}^2</math> (-120 to -200 ksi)], changing monotonically to a region of tensile stress within the boron. At <math>\sim 25</math> percent of the original radius, the stress reaches a maximum tensile [600 to 1000 <math>\text{MN}/\text{m}^2</math> (90 to 150 ksi)] and then decreases to compressive near the tungsten boride core. The core itself is under a compressive stress of <math>\sim -1300</math> <math>\text{MN}/\text{m}^2</math> (-190 ksi). The effects of surface removal on core residual stress and core-initiated fracture are discussed.</p>			
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# LONGITUDINAL RESIDUAL STRESSES IN BORON FIBERS

D. R. Behrendt

Modern boron fibers are produced by chemical vapor deposition (CVD) of boron from a  $\text{BCl}_3\text{-H}_2$  gas mixture on a tungsten wire at high temperatures 1223 to 1573<sup>o</sup>K (1742 to 2372<sup>o</sup>F). At these temperatures, the boron diffuses into the tungsten, forming a core of several of the tungsten borides surrounded by a boron sheath. The tensile fracture strength of a brittle material such as the boron fiber depends on the size and distribution of flaws and on the residual stresses at these flaws. The high strength of boron fibers are due in part to the fact that the primary flaws are located at the surface and in the tungsten boride core, where residual stresses have been found to be compressive [1, 2, 3].

The residual stresses in Refs 1 and 3 were calculated from the radius of curvature of longitudinally split fibers by assuming a linear relation between stress and radius in the boron sheath. The compressive nature of the core stress was deduced from the decrease in the radius of curvature upon removal of the core by etching. In Ref 2, measurements of the change in length of a fiber upon etching of the surface along with the assumption that this change in length varied as the square of the radius were used to calculate the residual stresses. The purpose of the research reported here was to make continuous and more accurate determinations of the residual stress distributions in boron fibers with the goal of using the better understanding to show the way to produce stronger and more uniform fibers.

## Experimental Test Apparatus

The experimental apparatus was designed so that continuous measurements could be made of the length changes of a boron fiber specimen as the surface of the fiber was removed by electropolishing. From these axial strains, the axial residual stress distribution could be calculated. As indicated in the schematic representation of the experimental apparatus (shown in Fig. 1),

the specimen is mounted between an inner and an outer quartz tube. The inner tube is free to slide within the outer tube in teflon bearings. The boron fiber to be tested is cemented with conducting epoxy between the bottom of the outer tube and a sleeve connected to the inner tube. The fiber test section is about 1 cm long. The center plate of a three-plate capacitor is attached to the top of the inner tube. The other two plates are insulated from each other and attached to the top of the outer tube. Thus, any changes in length of the specimen produced an equal change in the position of the center plate with respect to the outer plates. The relative position of the center plate is detected by applying a -100V peak-to-peak 3000 Hz voltage to the outer plates and feeding the resulting signal from the center plate into a high impedance (10 meg  $\Omega$ ) pre-amplifier and then to a lock-in amplifier. A strip chart recorder was connected to the output of the lock-in amplifier so that a continuous recording of length vs. time could be made.

The surface of the boron is removed by electropolishing at room temperature by placing the lower portion of the apparatus in a low conductivity solution made by dissolving 0.5 gm of NaOH in 30 cc of H<sub>2</sub>O and adding this to 150 cc of glycerin. A current of 4 ma per centimeter of fiber length is maintained between the boron fiber and a concentric stainless steel cathode. By direct measurement of the fiber diameter at intervals during preliminary tests, it was established that the rate of mass removal from the fiber is constant for a given current and independent of fiber diameter. For a current of 4 ma/cm at  $\sim$  25 V, the mass removal rate was  $6.3 \times 10^{-8}$  gm/cm/sec. Using this information in an actual run, the fiber diameter for any time during the run could be calculated to an accuracy of 3% from a measurement of the final diameter and total time of electropolishing at constant current. This allowed the apparatus to be undisturbed during an actual run since physical

diameter measurements during the run were not necessary.

The advantages in using electropolishing instead of chemical etching are: (1) the electropolishing is done at room temperature whereas the chemical etching of boron usually requires temperatures near  $373^{\circ}\text{K}$  ( $212^{\circ}\text{F}$ ) to obtain sufficiently large etching rates, (2) the electropolishing method produces a more uniform removal of the surface. A scanning electron microscope was used to examine the surfaces of boron fibers in the as-received, lightly electropolished, and lightly etched [two parts nitric acid to one part water at  $363^{\circ}\text{K}$  ( $194^{\circ}\text{F}$ )] conditions. The as-received fibers had the usual nodular or corn cob appearance. After removal of  $13\ \mu\text{m}$  (0.5 mils) off the diameter by electropolishing, examination of the surface showed it to be smooth with little evidence of the nodules left. In contrast, the nitric acid-etched surfaces, after removal of a similar amount, were considerably rougher with the nodules clearly evident.

#### Specimen Description

The specimens tested were 102, 142, and  $203\ \mu\text{m}$  (4, 5.6, and 8 mil) boron on tungsten fibers made by Avco Systems Division. The 102 and  $142\ \mu\text{m}$  fibers were made in a single-pass  $\text{BCl}_3\text{-H}_2$  reactor using resistive heating of the fiber. The  $203\ \mu\text{m}$  fibers were also made in a single pass  $\text{BCl}_3\text{-H}_2$  reactor with addition of VHF heating to supplement the resistive heating. A  $12.7\ \mu\text{m}$  (0.5 mil) diameter tungsten precursor was used to make the three fiber sizes. The maximum deposition temperature was near  $1573^{\circ}\text{K}$  ( $2372^{\circ}\text{F}$ ). The as-received tensile fracture strengths for these fibers were measured by Smith [4] and are shown in Table 1.

Table 1

Tensile Fracture Stresses of As-Received Boron Fibers [4]

Fiber Diameter		Average Fracture Stress		Coefficient of Variation
$\mu\text{m}$	(mils)	$\text{MN/m}^2$	(ksi)	%
102	(4.0)	3310	(480)	9.4
142	(5.6)	2880	(418)	13.5
203	(8.0)	3590	(521)	23.5

Analysis of the Data

From measurement of the change in length of the fiber with time of electropolishing of the fiber under test, the axial strain  $\epsilon_z$  as a function of fiber radius  $r$  could be calculated. We assume that the mechanical properties of the boron do not depend on radius, that is, that both Young's modulus  $E$  and Poisson's ratio  $\nu$  are constant, but we do allow the tungsten boride core to have properties different from the boron sheath. Witucki [1] has treated the case of equal moduli for both the core and sheath. We also assume that the axial strains are produced only by axial stresses. This means we have neglected the effects of  $\sigma_r$  and  $\sigma_\theta$  stresses on the axial strain  $\epsilon_z$  during the electropolishing process. The stress at a position in the as-received fiber of radius  $r_0$  is derived in the Appendix and is given by

$$\sigma(r_0, r) = - \left[ (E_c - E_b) \frac{r_0^2}{r^2} + E_b \right] \kappa \left[ \frac{r}{2} \frac{d\epsilon_z(r)}{dr} + \epsilon_z(r) \right] \quad (1)$$

where

$E_c$  = Young's modulus of core

$E_b$  = Young's modulus of boron sheath

$r_c$  = radius of core

$r$  = radius of electropolished fiber

$\epsilon_z(r)$  = the axial strain at a fiber radius  $r$  with  $\epsilon_z(r_0) = 0$



DiCarlo [5] has shown that the core of the 203  $\mu\text{m}$  (8 mil) fiber consists of two parts: a  $\text{W}_2\text{B}_5$  inner core  $\sim 12.8 \mu\text{m}$  (0.5 mils) in diameter and a  $\text{WB}_4$  outer core 17  $\mu\text{m}$  (0.67 mils) in diameter. He reports average Young's moduli of the core borides and boron sheath to be 669  $\text{GN/m}^2$  ( $97 \times 10^6$  psi) for the  $\text{W}_2\text{B}_5$ , 407  $\text{GN/m}^2$  ( $59 \times 10^6$  psi) for the  $\text{WB}_4$ , and 393  $\text{GN/m}^2$  ( $57 \times 10^6$  psi) for the boron sheath. In Eq (1), we consider the outer core of  $\text{WB}_4$  and the boron to have the same Young's moduli, thus

$$E_c = 669 \text{ GN/m}^2 \text{ (} 97 \times 10^6 \text{ psi)}$$

$$E_b = 393 \text{ GN/m}^2 \text{ (} 57 \times 10^6 \text{ psi)}$$

$$r_c = 6.4 \mu\text{m} \text{ (} 0.25 \text{ mils)}$$

#### Experimental Results

Measurements were made on ten or more specimens of each of the three sizes of fibers. Fig. 2 is the plot of the raw data, that is, the strain along the fiber axis  $\epsilon_z$  versus radius  $r$  for a 102  $\mu\text{m}$  (4 mil) diameter fiber. This plot is typical of most of the runs except that most fibers broke before the core was reached. The fiber initially contracts as the surface is removed, then elongates, becoming longer than its original length. The test was terminated at a radius of 8.1  $\mu\text{m}$  (0.32 mils) which is the approximate radius of the  $\text{WB}_4$  the outer boride of the core. The electropolishing method used was not nearly as effective in removing the tungsten borides as it was in removing the boron sheath as indicated by a reduction in polishing current at the core diameter. From these data and Eq (1), the longitudinal stress  $\sigma(r_o, r)$  at radius  $r$  for the as-received fiber at radius  $r_o$  could be calculated. Fig. 3 shows the results for the data of Fig. 2. The dashed portion of the curve indicates the average stress within the core. Details of how the stress varies with radius in the core region could not be obtained because the tungsten borides were ineffectively removed by the electropolishing

solution. Figs. 4 and 5 show the results for typical  $142\ \mu\text{m}$  (5.6 mil) and  $203\ \mu\text{m}$  (8 mil) boron fibers respectively. For both of these curves, the fibers broke before the core diameter was reached. For other runs for the 102, 142, and  $203\ \mu\text{m}$  (4.0, 5.6, and 8.0 mil) diameter fibers the shape of the curves were similar with variations of up to  $\pm 15\%$  in the compressive stresses at the surfaces and the maximum tensile stresses near the core.

#### Discussion

The three sizes of boron fibers investigated show similar residual stress distributions; i.e., compressive at the surface, tensile near the core, and for the  $102\ \mu\text{m}$  (4 mil) fiber compressive again in the core. It is expected that the  $142\ \mu\text{m}$  (5.6 mil) and  $203\ \mu\text{m}$  (8 mil) fibers also would show compressive core stresses. Measurements made in Refs 6 and 7 of the curvature of split fibers  $102\ \mu\text{m}$  (4 mils) and smaller before and after removal of the tungsten boride core have shown the core to be in compression. Witucki [1] considers three sources of the residual stresses in the boron fibers: (1) the CVD process itself in which the boron is deposited with a biaxial deposition stress (such a stress might arise, for example, from surface tension or nodule growth effects), (2) the volume increase of the core due to the formulation of the tungsten borides, and (3) the difference in the thermal expansion between the boride core and the boron sheath. Other effects which contribute to the residual stresses are annealing of the disorder produced when the boron is deposited and creep and anelastic deformation [8] which would tend to relax the residual stresses. Considering only the deposition stress and assuming the core and sheath to be completely elastic with the same elastic constants, the axial stress is given by [1]

$$\sigma_z(r) = \sigma_d \left(1 - 2/n \frac{r_0}{r}\right) \quad (2)$$

where

$\sigma_z(r)$  = axial stress at radius r

$\sigma_d$  = deposition stress

$r_0$  = radius of boron fiber

r = radius at which stress is given

In Eq (2) if we let  $\sigma_d = -1300 \text{ MN/m}^2$  (-190 ksi), a surface stress typical of those measured in this investigation,  $\sigma_z(r)$  increases much more rapidly with decreasing r than our measurements indicate. Such large stresses as predicted by Eq (2) will most certainly be relaxed due to creep in the boron sheath and possibly in the tungsten boride core at the temperature of CVD of the boron. We are, at present, investigating a model in which the stresses produced by the deposition process are allowed to relax by creep of boron sheath and boride core.

As the diameter of these fibers is reduced by etching or electropolishing, the fibers contract along their axis as a result of the removal of the compressive layers. This is shown in Fig. 2 for a  $102 \mu\text{m}$  (4 mil) fiber. This contraction increases the compressive stress in the core. The tensile strength of fibers whose fracture is controlled by flaws in the core should thus show an equal increase in the core fracture stress upon etching. Smith [4] has measured the average tensile fracture strength of etched  $203 \mu\text{m}$  (8 mil) boron derived from the same spool of material as was used in this investigation. He has shown that etching produces fibers which fracture in essentially all cases from core flaws. In Table 2 are shown the stresses calculated for the core at fracture using UTS data reported by Smith for various etched diameters. The Young's modulus for the core is the same as

that used in Eq (1). Also shown in Table 2 are the axial strains along with the resulting changes in the stresses at the core produced by electropolishing the  $203\mu\text{m}$  (8 mil) fiber whose stress distribution was shown in Fig.

4. We can compare the core fracture stress of Smith's work to the increase in core stress from this investigation by assuming the core fracture stress at zero strain to be  $7.74\text{ GN/m}^2$  (1122 ksi). This core fracture stress for as-received fibers is larger than the value  $7.21\text{ GN/m}^2$  (1045 ksi) derived from Smith's work. The lower value found by Smith can be attributed to surface flaws and to effects caused by the rough nodular surface at the as-received fibers. Fig. 6 is a plot of the diameter dependence of the core fracture stress as derived from Ref 4 and from the axial strain measured in this investigation. The close agreement between Smith's fracture stress data and the data of this investigation supports Smith's argument that the increase in UTS is due to the increase in the compressive stress at the core produced by the fiber contraction during surface removal.

Table 2

Core Fracture Stresses of Etched and Electropolished 203  $\mu\text{m}$  (8 mil) Boron Fibers

Etched Dia. (2r) $\mu\text{m}$ (mils)	Fiber Stress at Fracture $[\sigma_f]$ (ksi) $\text{GN}/\text{m}^2$	Core Stress at Fracture $[\sigma_c]$ (ksi) $\text{GN}/\text{m}^2$	Axial Strain ( $\epsilon_z$ ) mm/m	Change in Core Stress ( $\Delta\sigma_c$ ) $\text{GN}/\text{m}^2$ (ksi)	Calc. Core Fracture Stress ( $\sigma_c^2$ calc.) $\text{GN}/\text{m}^2$ (ksi) <sup>2</sup>
203 (8.00)	4.25 (616)	7.21 (1045)	0	0	7.74 (1122)
188 (7.42)	4.71 (683)	7.99 (1159)	-0.373	-0.25 (-36)	7.98 (1158)
174 (6.86)	4.79 (694)	8.12 (1177)	-0.690	-0.46 (-67)	8.20 (1189)
164 (6.45)	4.92 (714)	8.34 (1210)	-0.887	-0.59 (-86)	8.33 (1208)
138 (5.45)	5.03 (730)	8.52 (1235)	-1.260	-0.84 (-122)	8.58 (1244)
114 (4.50)	5.23 (759)	8.83 (1281)	-1.512	-1.01 (-147)	8.75 (1269)
90 (3.55)	5.30 (768)	8.89 (1290)	-1.685	-1.12 (-163)	8.86 (1285)

$$(1) \sigma_c = E_c \sigma_f / [E_c r_c^2 / r^2 + E_b (1 - r_c^2 / r^2)]$$

(2) The strains are those measured in this investigation for the 203  $\mu\text{m}$  (8 mil) fiber after electropolishing.

$$(3) \Delta\sigma_c = \epsilon_z E_c$$

$$(4) \sigma_c^{\text{calc.}} = 7.74 + |\Delta\sigma_c| \text{ CM}/\text{m}^2$$

An expression is derived which is used to calculate the longitudinal residual stress  $\sigma(r_0, r)$  at radius  $r$  for an as-received fiber of radius  $r_0$  from measurements of the axial strain produced by removal of the surface by electropolishing. In deriving this expression, we neglect the effects due to radial and tangential stresses. The original fiber is considered to consist of a core of radius  $r_c$  and sheath with Young's moduli  $E_c$  and  $E_b$ , respectively. Consider the fiber to be electropolished to a radius of  $r$ , then the stress in the surface layer will be  $\sigma_s(r)$ . If a layer of thickness  $\Delta r$  is removed by electropolishing, a force  $\Delta F$  is removed from the remaining fiber or

$$\Delta F = - \sigma_s(r) 2\pi r \Delta r \quad (A1)$$

This force produces an axial strain of  $\Delta \epsilon$ , or

$$\Delta \epsilon = \frac{\Delta F}{E_c \pi r_c^2 + E_b \pi (r^2 - r_c^2)} \quad (A2)$$

Combining Eqs (A1) and (A2) and solving for  $\sigma_s(r)$  we have

$$\sigma_s(r) = - \frac{\Delta \epsilon}{\Delta r} \times \frac{E_c r_c^2 + E_b (r^2 - r_c^2)}{2r} \quad (A3)$$

When  $r = r_0$ , we let  $\epsilon = 0$ . The stress  $\sigma_s(r)$  is the stress derived from the stress distribution  $\sigma(r_0, r)$  of the as-received fiber plus the stress produced in the remaining fiber by the strain  $\epsilon$  or

$$\sigma_s(r) = \sigma(r_0, r) + \epsilon \left[ \frac{E_c r_c^2 + E_b (r^2 - r_c^2)}{r^2} \right] \quad (A4)$$

Combining Eqs (A4) and (A3), we have

$$\sigma(r_0, r) = - \left[ (E_c - E_b) \frac{r_c^2}{r^2} + E_b \right] \times \left[ \frac{r}{2} \frac{d\epsilon}{dr} + \epsilon \right]. \quad (A5)$$

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- [2] Faughnan, K. A., Proceedings of the Twenty-Ninth Annual Conference of the Wide World of Reinforced Plastics, Society of the Plastics Industry, Inc., New York, 1974, pp. 4-B,1 to 4-B,10.
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- [8] DiCarlo, J. A., "Composite Materials: Testing and Design," (Fourth Conference), American Society for Testing and Materials, Philadelphia, 1976.

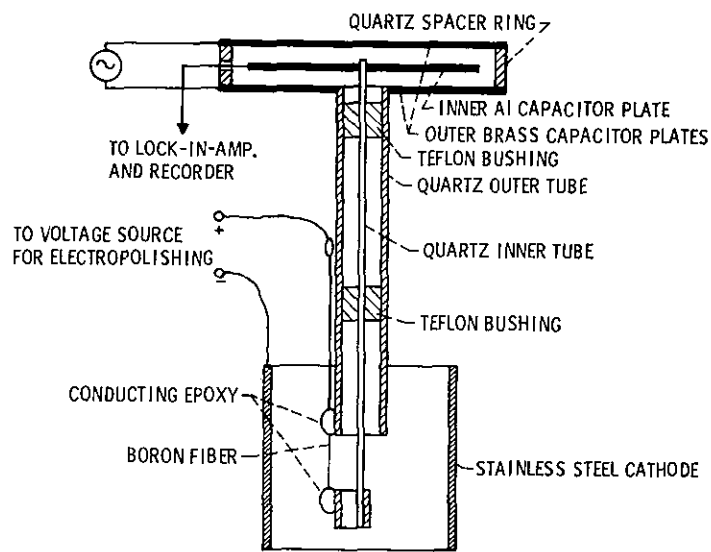


Figure 1. - Quartz gauge used to measure length change of a boron fiber specimen.

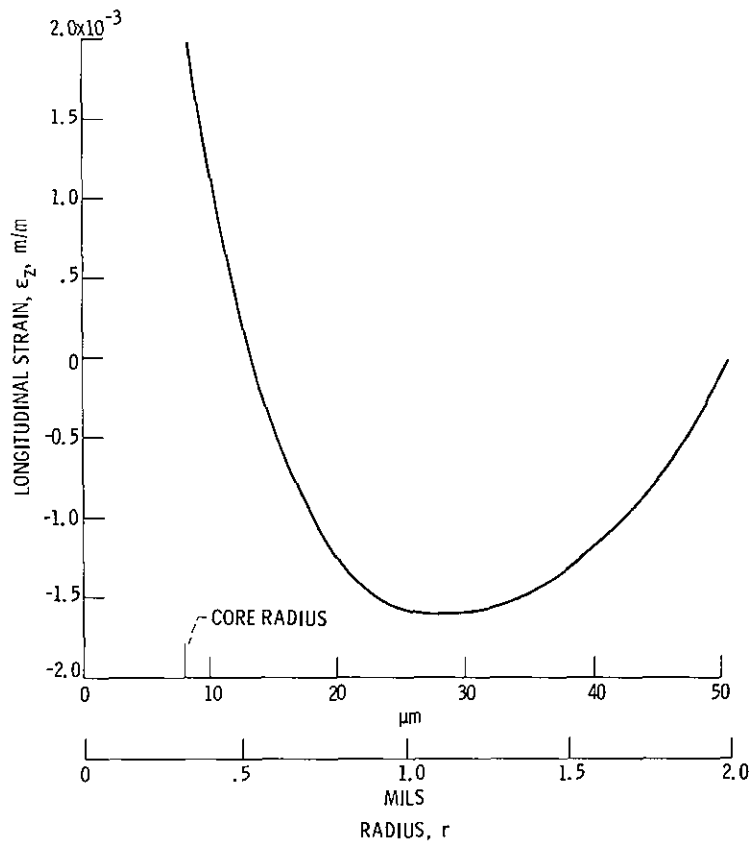


Figure 2. - Longitudinal strain versus electropolished radius of 102 μm (4 mil) diameter B/W fiber.



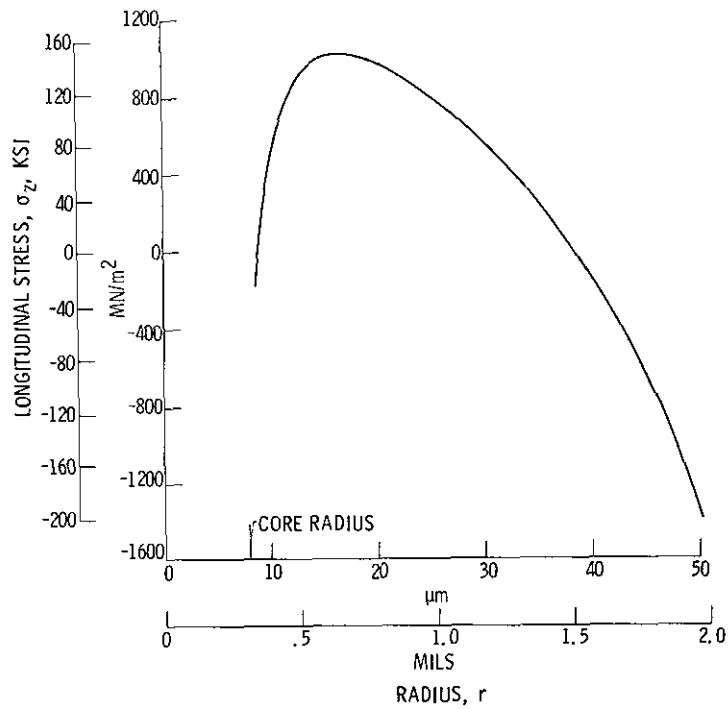


Figure 3. - Longitudinal residual stress distribution in 102 μm (4 mil) diameter B/W fiber.

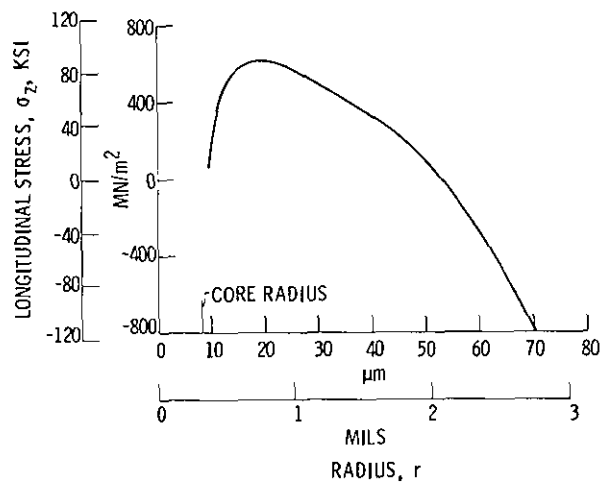


Figure 4. - Longitudinal residual stress distribution in 142 μm (5.6 mil) diameter B/W fiber.

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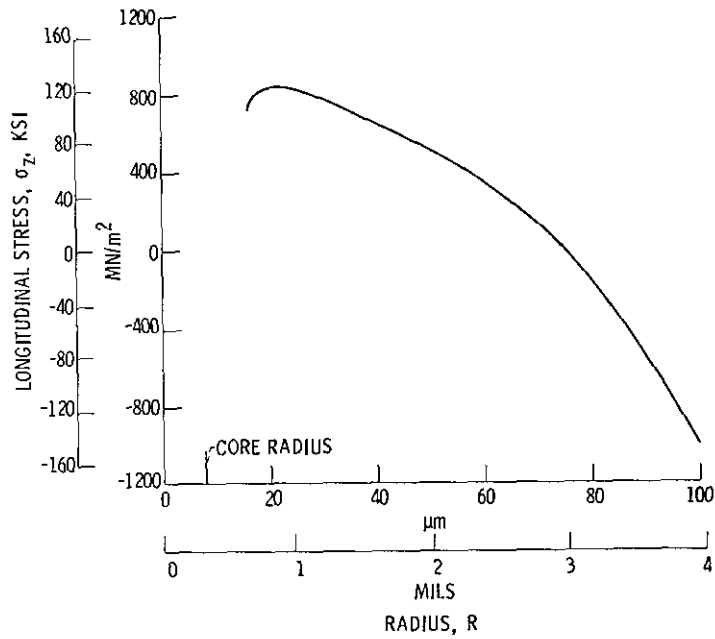


Figure 5. - Longitudinal residual stress distribution in 203  $\mu\text{m}$  (8 mil) diameter B/W fiber.

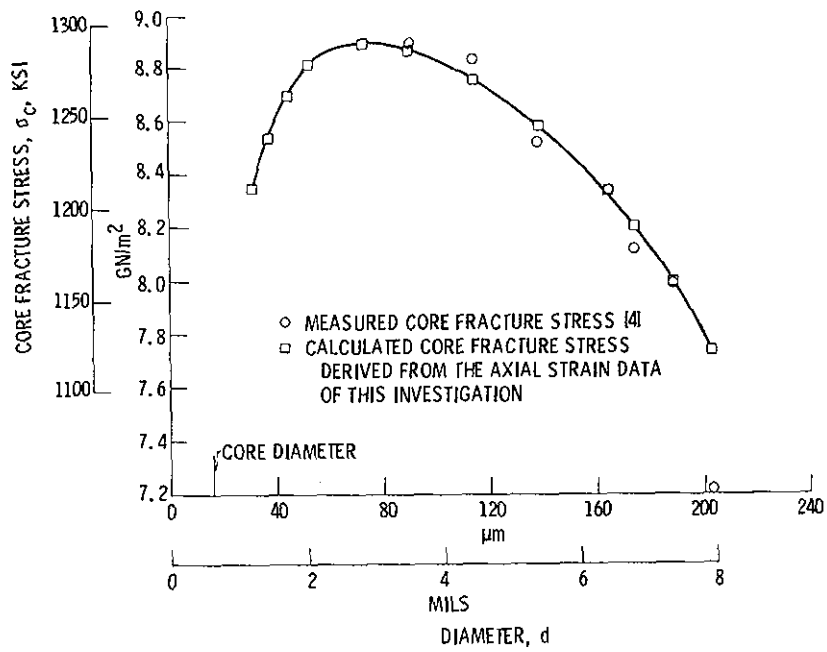


Figure 6. - Diameter dependence of the core fracture stress of 203  $\mu\text{m}$  (8 mil) B/W fiber derived from Smith's UTS data [4] and from the axial strain measurement of this investigation.