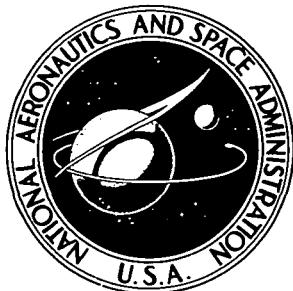


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MEMORANDUM



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A HYBRID COMPUTER PROGRAM  
FOR RAPIDLY SOLVING FLOWING  
OR STATIC CHEMICAL KINETIC  
PROBLEMS INVOLVING MANY  
CHEMICAL SPECIES

*Allen G. McLain and C. S. R. Rao*

*Langley Research Center  
Hampton, Va. 23665*



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16. Abstract A hybrid chemical kinetic computer program has been assembled which provides a rapid solution to problems involving flowing or static, chemically reacting, gas mixtures. The computer program uses subroutines from the program of NASA TN D-6586 for problem setup, initialization, and preliminary calculations and incorporates the stiff ordinary differential equation solution technique of C. W. Gear.			
A number of the check cases presented in NASA TN D-6586 were recomputed with the hybrid program and the results were almost identical to the results published in NASA TN D-6586. The computational time saving is demonstrated with a propane-oxygen-argon shock tube combustion problem involving 31 chemical species and 64 reactions. This case yielded comparable results and a computational time almost an order of magnitude lower than that for the program of NASA TN D-6586. Information is presented in the appendixes to enable potential users to prepare an input data deck for the calculation of a problem.			
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A HYBRID COMPUTER PROGRAM FOR RAPIDLY SOLVING FLOWING  
OR STATIC CHEMICAL KINETIC PROBLEMS  
INVOLVING MANY CHEMICAL SPECIES

Allen G. McLain and C. S. R. Rao\*

Langley Research Center

SUMMARY

A hybrid chemical kinetic computer program has been assembled which provides a rapid solution to problems involving flowing or static, chemically reacting, gas mixtures. The computer program makes use of subroutines from the program of NASA TN D-6586 for problem setup, initialization, and preliminary calculations. However, the method of solution of the resulting ordinary differential equations is that presented by C. W. Gear. The Gear numerical solution technique uses a highly efficient strategy in altering step size and order in combination with an extensive history array to achieve a stable, rapid solution to a problem involving a number of stiff simultaneous differential equations. Therefore, the chief advantage of using the hybrid program of this paper instead of the program of NASA TN D-6586 is realized when the reacting system contains more than 15 different chemical species, although the use of the program for a smaller number of reacting species does not penalize the user with respect to computational time.

A number of the check cases presented in NASA TN D-6586 were recomputed with the hybrid program and the results were almost identical to the results published in NASA TN D-6586. The saving in computational time is demonstrated with a propane-oxygen-argon shock tube combustion problem which involves 31 chemical species and 64 reactions. This case yielded comparable results between the hybrid program and the program of NASA TN D-6586; however, the computational time for the program of this paper was almost an order of magnitude lower than that for the program of NASA TN D-6586.

INTRODUCTION

Recent interest in problems associated with energy conservation and pollution abatement has led to increased use of computer codes to study kinetically controlled chemical reactions in the combustion processes of static and flowing hydrocarbon fuel. In energy-associated research, if a set of realistic kinetic steps is given, simulation of combustion

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\*Old Dominion University, Norfolk, Virginia.

processes could be studied by a variation of input parameters to find the conditions that would provide optimum extraction of energy from a fuel. In pollution research, the conditions where pollutant levels would be reduced could be studied with some insurance that the predicted changes would actually result. Sets of kinetic steps, or reaction mechanisms, which adequately describe the chemical processes appear to grow longer as the fuels increase in molecular weight. At present, only the reaction mechanism for the oxidation of the smallest hydrocarbon, methane, is understood sufficiently to allow a reliable prediction of product distribution during combustion. A recently published reaction mechanism for methane (ref. 1) contains over 20 reactions and approximately 15 species. Higher molecular weight hydrocarbons, such as propane and eventually heptanes, octanes, and other constituents of present fuels, will require many more species and reactions to describe their combustion behavior. Each additional species adds to the computational difficulties associated with solving the differential equations in the mathematical model of the reacting system.

The differential equations become "stiff" because so many of their terms change very rapidly at the same time other terms are hardly changing at all. This stiffness is a local situation and may occur in some regions of the independent variable but not in other regions. The stiffness causes many finite-difference solution procedures to fail unless the increment of the independent variable is reduced significantly in size. The reduced step size, although needed only in certain regions of the independent variable, increases the computational time for a solution over the entire range of the independent variable. Therefore, most computer programs using finite-difference techniques automatically vary increment size in regions where the equations become stiff. The chemical kinetic computer program of reference 2 uses such a strategy for varying increment size to achieve a more efficient use of computer time. However, as the number of equations increase, the strategy and numerical technique used by the program of reference 2 become less efficient and the computational time increases dramatically. For these reasons, a solution technique which was derived specifically for stiff systems of equations was sought.

A hybrid chemical kinetic computer program has been assembled which provides a rapid solution to problems associated with flowing or static, chemically reacting, gas mixtures. The program is designated as hybrid because it combines the desirable portions of two existing and well-documented computer programs. The program uses subroutines from the computer program of reference 2 for problem setup, initialization, and preliminary calculations with the solution technique presented in references 3 and 4. The listing of the resulting computer program is presented in this report. Several of the check cases presented in reference 2 have been computed with the program of this report and the computed results and computational times are compared. To illustrate the savings in computational time for a calculation involving a large number of chemical species, the computed results for the stoichiometric combustion of a propane, oxygen, and argon

mixture in a shock tube obtained by using the hybrid program and the program of reference 2 are compared. Information is presented to enable possible users to calculate a specific problem.

#### SYMBOLS

A	area, m <sup>2</sup>
$\mathcal{A}$	species production function described in equation (5), sec <sup>-1</sup>
$\mathcal{B}$	enthalpy production function described in equation (6), sec <sup>-1</sup>
C <sub>p</sub>	specific heat at constant pressure
f <sub>i</sub>	$= \frac{dy_i}{dt}$
h <sub>i</sub>	enthalpy of species i
M	Mach number, $\sqrt{\frac{V^2 M_w}{\gamma R T}}$
M <sub>w</sub>	molecular weight
p	pressure of gas mixture, atm
R	universal gas constant
T	temperature, K
t	time
t <sub>0</sub>	initial time
V	velocity
w <sub>i</sub>	net species production rate, moles/vol-sec
y	general dependent variable
y <sub>0</sub>	initial value of dependent variable

$\gamma$	specific heat ratio, $\frac{C_p}{C_p - \frac{R}{M_w}}$
$\rho$	density
$\sigma_i$	concentration, moles of species $i$ per unit mass of mixture

### DIFFERENTIAL EQUATIONS FOR CHEMICALLY REACTING, FLOWING OR STATIC SYSTEM

The computer program of this paper, as indicated, is a hybrid combination of two existing and well-documented computer programs. This hybrid program uses the subroutines of reference 2 for setting up the system of differential equations for a specific flowing or static, chemically reacting problem. The system of differential equations is then solved by using subroutines from reference 3 based on the methods developed in reference 4.

The system of equations may be derived with respect to either time or distance and may have either assigned area or pressure profiles. For example, the differential equations which must be solved with respect to time for a one-dimensional steady-state flow through an arbitrary assigned area profile would be

$$\frac{d\sigma_i}{dt} = \frac{w_i}{\rho} \quad (i = 1, 2, \dots, N) \quad (1)$$

$$\frac{dV}{dt} = \frac{V}{M^2 - 1} \left( \frac{1}{A} \frac{dA}{dt} - \mathcal{A} \right) \quad (2)$$

$$\frac{dp}{dt} = -p \left[ \frac{M^2}{M^2 - 1} \left( \frac{1}{A} \frac{dA}{dt} - \mathcal{A} \right) + \mathcal{A} \right] \quad (3)$$

$$\frac{dT}{dt} = -T \left[ \frac{(\gamma - 1)M^2}{M^2 - 1} \left( \frac{1}{A} \frac{dA}{dt} - \mathcal{A} \right) + \mathcal{B} \right] \quad (4)$$

where

$$\mathcal{A} = \frac{RT}{p} \sum_{i=1}^N w_i - \mathcal{B} \quad (5)$$

and

$$\mathcal{B} = \frac{1}{p} \left( \frac{\gamma - 1}{\gamma} \right) \sum_{i=1}^N h_i w_i \quad (6)$$

This relationship represents a system of  $N + 3$  equations with  $N + 3$  unknowns (where  $N$  is the number of species in the system). Problems with distance as the independent variable would yield a similar system of  $N + 3$  equations. If the assigned variable were pressure,  $N + 3$  equations with respect to time or distance would also be possible. Reference 2 offers a complete derivation of the different systems of equations.

### SOLUTION OF DIFFERENTIAL EQUATIONS

The system of equations derived for the particular problem described in the previous section forms a nonlinear, coupled set of differential equations which can be represented in the following form:<sup>\*</sup>

$$\frac{dy_i}{dt} = f_i(t, y_1, \dots, y_N) \quad (i = 1, 2, \dots, N) \quad (7)$$

The equations in this form can be solved by using a numerical solution technique. The subroutine package from reference 3 provides the user with two basically different methods for the solution of such a system of equations. The two basic methods are (1) the Adams implicit methods and (2) the stiffly stable, linear multistep methods of Gear. If the system of equations is not considered to be excessively stiff, the Adams methods may be used to solve the problem efficiently. However, if the problem is judged to be stiff (a condition which may be aggravated by considering a large number of additional equations inherent with the consideration of additional chemical species), the Gear methods should be used. With these methods, the incremental step size is restricted to small values, because of accuracy requirements, only where the solution is active. In this region accuracy is achieved by varying both step size and order of the method of solution. The step sizes in regions of stiffness are unrestricted because of small time constants until the terms become active again. This condition requires that the method be implicit and a system of generally nonlinear equations be solved at each step. For a detailed discussion of the mathematical derivation of this solution technique, reference 4 should be obtained. Reference 3 provides additional information about the method of Gear and is linked directly to the developed subroutine package.

Since the subroutines presented in reference 3 are user-oriented, a reiteration of the mathematical development is not believed to be justified. If equations (1) to (4) are given in the general form of equation (7) with an initial value of the vector  $y(t_0) = y_0$  and

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<sup>\*</sup>(Here  $i$  refers to a particular dependent variable  $y$ , and  $N$  is the total number of equations in which the variable  $y$  changes with the independent variable  $t$ . Specifically,  $y_1$ ,  $y_2$ , and  $y_3$  are  $V$ ,  $\rho$ , and  $T$ , respectively, and  $y_4$  to  $y_N$  are the total number of chemical species.)

a subroutine for the calculation of  $f_i$  values, the subroutine package of reference 3 computes a numerical solution at values of the independent variable  $t$  in intervals desired by the user.

Although the package of subroutines of reference 3 was obtained primarily for the stiffly stable methods of Gear, both the Adams methods and the Gear methods are functional in this program. Comparative calculations which will be performed later in this paper utilize the method of Gear with the internal approximation of the Jacobian by finite differences. The user accessibility to all the methods available with this program is presented in appendix A.

### PROGRAM DESCRIPTION

The computer program described in reference 2 has been altered to allow the solution of the differential equations by the methods described in reference 4. The program organization is still very similar to that presented in reference 2. Table I lists the subroutines of the program of reference 2 and describes the type of changes, if any, which were affected.

An overall schematic diagram of the computer program is shown in figure 1 with the Gear package of reference 3 enclosed by the dashed line. The direction of the arrows indicates calls from one routine to another with normal returns from the called routine after completion of its task. The three subroutines numbered (1) GPAK, (2) KINP, and (3) DRIVES indicate the general order followed during the solution of any of the problems which the program can handle. The program starts in subroutine GPAK and calls KINP for reading the input data (reactions, inert species, third body reactants, and namelists), storing thermodynamic data, initializing variables, and performing initial calculations. The equilibrium property calculations are also obtained in the subroutine. This can be seen by observing the subroutines at the left of figure 1. The return to GPAK is followed by printout of preliminary data. Subroutine DRIVES (ref. 3) is then called and control is maintained by DRIVES until the desired interval of the independent variable is achieved.

The flow diagrams for the main program GPAK and the control subroutine DRIVES are presented in figures 2 and 3, respectively. The flow diagram for subroutine STIFF is shown in figure 4 as it appeared in reference 3 to allow the reader to follow its logic. Subroutine DRIVES calls subroutine STIFF to obtain a solution for the system of differential equations for each increment of the independent variable. After each successful step, DRIVES regains control and calls for output of the calculated data. If printout is desired at specific locations of the independent variable, subroutine YOUT is called for calculation of the dependent variables at the print location through interpolation of the history array.

TABLE I.- SUBROUTINES OF PROGRAM OF REFERENCE (2)  
AND DESCRIPTION OF ALTERATIONS

Subroutines from program of reference (2)	Alteration performed
GCKP	1. All monitoring of integration removed. 2. Calls for output removed. 3. Problem control yielded to subroutine DRIVES of reference 3 for looping and error treatment coding. 4. Subroutine renamed GPAK.
KINP CIMAGE NAMBLK BLCK INIT OUTP	Minor modifications as to variable initialization and printout scheme setup. In OUTP printing format changed to conserve paper.
COMB SHOK SHOCKS ELEMNT EQLBRM MATRIX GAUSS SPOUT	No changes made.
PRED DERV	Combined and renamed DIFFUN. Internal changes made for updating dependent variables at print location without altering array values for continuation of problem after printing.
PARD	Renamed PEDERV.
THRM CUBS	No changes made.
INTE CASM LESV ERROR PERR AUTO SEARCH	These subroutines completely removed and replaced with sub- routines of reference 3. The subroutines used are YOUT COSET YOUTD DECOMP DRIVES SOLVE STIFF

The flow diagram for subroutine YOUT is shown in figure 5. Flow diagrams of subroutines DIFFUN (which is a combination of routine PRED and DERV) and PEDERV (which is basically subroutine PARD) can be seen in reference 2.

The resulting modified program is presented in appendix B. Obvious changes in the computer program made to facilitate its use with the Control Data Corporation 6000 Series computers are not enumerated specifically.

The details of program input and error messages are shown in appendix A. The format is the same as that described in reference 2 and its related bulletin.

## RESULTS OF CALCULATIONS

Several of the check cases presented in reference 2 were calculated by using the modified program of this paper. For ease of comparison, the results of these calculations for check cases 1, 5, 6, and 8 of reference 2 are shown in appendix C alongside results obtained from the program of reference 2. The comparison for check case 1, which is bromine decomposition in a shock tube, is shown first in appendix C. The input card image and the first page of computer output are shown for the modified program alone to show the similarity with output information shown in appendix E of reference 2. The remaining printout for check case 1 enables the reader to see the closeness of the computed results for species concentrations, temperatures, velocities, densities, etc. The one parameter which shows a difference worth mentioning is the dependent variable (time) for this particular case. An explanation as to the reason for this difference is presented to prevent concern by the reader.

The difference is caused by the fact that the selected step sizes are not the same for both programs. This difference is more easily understood by considering the equation by which the dependent variable is calculated by either program.

Time as dependent variable: For time as a dependent variable,

DVAR      dependent variable, initially zero but previous value in subsequent steps

$V_1$       velocity after previous step

$V_2$       velocity after present step

Present step size is in distance units

$$DVAR = DVAR + \frac{2(\text{present step size})}{V_1 + V_2}$$

It is apparent that increments of larger or smaller step size influence the summed DVAR since the average velocity computed is different. Both the program of reference 2 and this program based on different strategies increase the step size automatically. Achieving identical results in DVAR between the two programs is therefore practically impossible.

Distance as dependent variable: For distance as a dependent variable,

$$DVAR = DVAR + \frac{V_1 + V_2}{2} \times (\text{Present step size})$$

Present step size in time units

Similarly, a different average velocity would have an effect in this dependent variable.

For this one reaction system involving three chemical species, the time for computation is presented at the end of the case in appendix C. The comparison for this case is very close.

Check cases 5 and 6 from reference 2 were run together to test the repeat option. The comparison of the output information is shown in appendix C. As can be seen, the computed times, distances, areas, flow, and chemical properties were very close to the computed quantities obtained by using the program of reference 2. The computational time using the program of this report was roughly one half the time for the program of reference 2. This is presented at the end of both cases in appendix C.

Check case 8 from reference 2 was also computed with both programs and the results are also compared in appendix C. The results were again comparable. The computational time was reduced slightly by using the program of this paper.

The results of the comparisons obtained by computing check cases 1, 5, 6, and 8 of reference 2 by the program of this paper and the program of reference 2 indicate that even for as few as eight species, computational time was reduced. The memory required for the program of this paper was  $71100_8$  as compared with  $66700_8$  for the program of reference 2. The memory for the program of this report can be reduced somewhat if subroutine PEDERV is made a dummy routine. However, if partial derivatives are to be calculated in PEDERV (an option used if the second digit of MF equals 1), care must be taken to restore the subroutine's computational ability.

As was shown, the program of this report reduced the usage of computer time for systems with few reacting species. Significantly larger savings in computer time can be expected for kinetic problems involving a very large number of chemical species. This is illustrated by the case shown in appendix D. This case involves the shock tube combustion of propane. The mechanism illustrated in appendix D contains 31 different chemical species in 64 reactions. The bulk of this reaction mechanism is from reference 5 by Chinitz and Bauer. The steps for methane combustion were taken from reference 1 and substituted for the appropriate steps in reference 5. This was done primarily because of the correlation of this methane mechanism with experimental shock tube results. Reaction number 2 in the list of reactions was input to cause some rapid changes in the species concentrations, since it was found that the basic reaction mechanism from reference 5 caused the combustion of propane to proceed very slowly. The thermochemical

data used for the species involved with propane combustion were taken from reference 6 and used in the form of polynomial coefficients presented in reference 7. The computations for the two outputs shown in appendix D were for the stoichiometric combustion of propane and oxygen diluted with argon when subjected to a shock wave traveling at 1.67 km/sec. The calculated results obtained from the computer program of this paper and that from reference 2 are very close at all the printout stations. The comparative time shown at the end of the printout of such program illustrates the advantage of using the Gear solution technique. The computer time required for the calculation using the program of this report was almost an order of magnitude less.

The reaction mechanism presented for the combustion of propane was used merely to illustrate the savings in time for a reaction system involving a large number of chemical species. The need for such an extensive list of chemical species and reactions to describe the combustion of a hydrocarbon similar to those in fuels presently used is evident. The trends established in the studies of methane, ethane, ethylene, and acetylene indicate that extensive reaction mechanisms with numerous chemical species will have to be considered.

#### CONCLUDING REMARKS

A hybrid computer program for solving flowing or static chemical kinetic problems has been assembled from subroutines of NASA TN D-6586 and the subroutine package of the Lawrence Livermore Laboratory Computer document UCID-30001 based on the solution methods presented by C. W. Gear. The resulting computer program has been used to calculate check cases presented in NASA TN D-6586. Comparisons of the check-case results obtained by using the computer program of this paper with those calculated by the program of NASA TN D-6586 have shown a reduction in computer time for equivalent results. For a calculation involving 31 chemical species and 64 reactions, the computer time for using the program of this report was almost an order of magnitude less.

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National Aeronautics and Space Administration  
Hampton, Va. 23665  
June 2, 1976

## APPENDIX A

### DETAILS OF PROGRAM INPUT AND ERROR MESSAGES

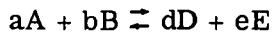
#### Input

The first card of an input data deck instructs the computer to read a thermodynamic data file. The word, CARDS or TAPE, indicates where the thermodynamic data are located. The thermodynamic data are read from the input location (cards or tape) and stored on tape unit for subsequent use by the computer program. The first record of the thermodynamic data set specifies the temperature range limits. The rest of the thermodynamic data is composed of four card sets for each chemical species. The first card contains the species name, the names of its chemical elements, their stoichiometric coefficients, and reference information. The remaining three cards contain the curve-fitted polynomial coefficients for the upper and lower temperature ranges. The upper temperature range runs from 1000 K to 5000 K and the lower range runs from 300 K to 1000 K.

The data cards in the order that they appear in the data deck are described in the following sections.

(1) Title – The first card contains a description of the type case to be run. All 80 locations on one card may be used. The title data are read with an alphanumeric format and appear on the first page of output.

(2) Reactions – Chemical reactions are listed one per card. Each card describes the reaction of the type



where the lower case letters, a, b, d, and e are stoichiometric coefficients between 1 and 9 and the capital letters, A, B, D, and E, refer to chemical species. To the right of each card, the rate constant parameters are presented. Species A or E may be omitted to specify reactions of the types:

- (a) Unimolecular decomposition to one or two products
- (b) Third-body influenced reactions (where one or two reactants form one or two products with the aid of a third body)
- (c) Two reactants forming one product.

The photochemical irreversible decomposition as described in the bulletin of reference 2 can also be used. It is of the form



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The format for the reaction cards as reprinted from the bulletin of reference 2 is:

<u>Card column</u>	<u>FORTRAN format</u>	<u>Content</u>
1	I1	Stoichiometric coefficient of first reactant – default is one
2		Blank (not read)
3 to 10	A8	(a) Name of first reactant (left justified) (b) M for third body collision (c) HNU for photochemical reaction
11		Not read
12	I1	Stoichiometric coefficient of second reactant (left justified) or first reactant for decomposition
13		Not read
14 to 21	A8	Name of second reactant (left justified) – first reactant for decomposition
22 to 24		Not read
25	I1	Stoichiometric coefficient for first product
26		Not read
27 to 34	A8	Name of first product (left justified)
35		Not read
36	I1	Stoichiometric coefficient of second product
37		Not read
38 to 45	A8	(a) Name of second product (left justified) (b) M if thick body recombination

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<u>Card column</u>	<u>FORTRAN format</u>	<u>Content</u>
46 to 49		Not read
50 to 60	E11.4	A factor of rate equation $K = AT^{N-E/RT}$
61 to 62		Not read
63 to 70	F8.4	N factor of rate equation
71 to 72		Not read
73 to 80	F8.4	E, activation energy, cal/mole

The end of the reaction list is signaled by a blank card. The program listed in appendix B is limited to 50 reactions. The dimensions of the program at Langley can be altered quickly, however, by the use of one card with the Control Data UPDATE program management system.

(3) Inert species - A species may be declared inert by placing the species name or names in column 1, 17, 33, or 49 on the next card. A blank card indicates no inert species desired and a blank field after a species name indicates the end of the inert species list.

(4) Version and units - One card specifies the independent variable (time or distance) and the assigned variable (area or pressure). The input and output units may also be specified on this card.

The card punch locations are as follows (from ref. 2):

<u>Columns</u>	<u>Contents</u>	<u>Explanation</u>
1 to 8	Time	Time fundamental variable
	Distance	Distance fundamental variable
11 to 18	Pressure	Pressure is assigned variable
	Area	Area is assigned variable
	(Blank)	Velocity zero (static case)
21 to 23	cgs	Input in internal cgs units

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<u>Columns</u>	<u>Contents</u>	<u>Explanation</u>
	(Blank)	Input in internal units cgs
	fps	Input in fps units
	SI	Input in SI units
31 to 33	cgs	Output in cgs units
	(Blank)	Output in cgs units
	fps	Output in fps units
	SI	Output in SI units

(5) Controls – The controlling variables are input in NAMELIST PROB and are listed below. Default options are underlined. Most of the variables are the same as listed in reference 2. The variable names followed by (✓) will be found only in the program of this paper. The variables deleted from the program are shown as deleted.

<u>Name</u>	<u>Value</u>	<u>Explanation</u>
HMIN	.....	Minimum step size in cm or sec
	<u>0.0001</u>	cm (if DISTANCE on version card)
	<u><math>5.0 \times 10^{-8}</math></u>	Seconds (if TIME on version card)
HMAX	.....	Maximum step size
	<u>0.1000</u>	cm (if DISTANCE version)
	<u><math>5.0 \times 10^{-5}</math></u>	Seconds (if TIME version)
HINT	.....	No longer input (assumes value of HMIN initially)
EMAX	<u>0.0001</u>	Maximum error acceptable (becomes EPS in Gear package)

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<u>Name</u>	<u>Value</u>	<u>Explanation</u>
ALLM1	<u>TRUE</u>	Third body efficiencies equal to 1. None input
	<u>FALSE</u>	Third body efficiencies to be input. Those not input remain equal to one
ELIM	.....	Deleted
CONC	<u>TRUE</u>	Concentration output as molar concentrations if SI or fps output designated
	<u>FALSE</u>	Mass fractions output if SI or fps output designated
ITPSZ	1	An area or pressure table input
	2	Area or pressure specified by polynomial equation
	3	LSUBM and ETA will be input for area equation
	4	D, VISC, BETA, and ETA will be input for area equation
	5	Zero velocity, no assigned pressure
IPRCOD	1	Distance against area profile given
	2	Distance against pressure profile given
	3	Time against area profile given
	4	Time against pressure profile given
XTB	.....	Array for time or distance portion of profile, must be in correct user units
ATB	.....	Array for area or pressure profile, must be in user units

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<u>Name</u>	<u>Value</u>	<u>Explanation</u>
NTB	.....	Total entries in area or pressure table, must be less than or equal to 40
CX3	.....	Coefficient of cubed component of pressure/area polynomial equation
CX2	.....	Coefficient of squared component of pressure/area polynomial equation
CX1	.....	Coefficient of pressure/area to the first power in polynomial equation
CX0	.....	Constant term in pressure/area polynomial equation
LSUBM	.....	Characteristic shock tube reaction length for special area equation (see ref. 2)
ETA	.....	Dimensionless exponent in special area equation for boundary layer (see ref. 2)
D	.....	Hydraulic diameter of shock tube
VISC	.....	Viscosity coefficient
BETA	.....	Dimensionless boundary-layer parameter used to calculate LSUBM
END	.....	Changed from reference 2, must always be input
DELP	.....	Deleted (from ref. 2)
PRINT	.....	Deleted (from ref. 2)
APRINT	.....	Deleted (from ref. 2)
NPRNTS	.....	Deleted (from ref. 2)

## APPENDIX A

<u>Name</u>	<u>Value</u>	<u>Explanation</u>
EVSTEP	.....	Deleted (from ref. 2)
DEBUGØ	<u>FALSE</u>	Changed, prints output parameters in more concise format
	TRUE	Prints format same as reference 2 with exception of derivatives, increment, and relative error information
PAPS(✓)	<u>FALSE</u>	Program prints at every (5) iterations or number specified by IPRIT
	TRUE	Prints at specific stations specified by END and IDEL or a TPRINT table
IDELO(✓)	.....	Number of increments derived (50 maximum)
IPRIT(✓)	<u>5</u>	Number specifying integration steps between printing
TPRINT(✓)	.....	Table of 50 values for specifying printing location (filled automatically by specifying IDEL)
NPRINT(✓)	.....	Number of values in TPRINT table
MF(✓)	22	Positive integer specifying method to be used in solving the problem. Composed of two digits 1st digit – 1 Adams Methods 2 Gear Methods 2nd digit – 0 functional iteration 1 chord method where Jacobian supplied by subroutine PEDERV 2 chord method where Jacobian approximated internally by finite differences 3 chord method where Jacobian replaced by diagonal matrix

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(See ref. 3 for extensive explanation of mathematics involved in different methods.)

<u>Name</u>	<u>Value</u>	<u>Explanation</u>
COMBUS	TRUE	Perform equilibrium combustion calculation
	<u>FALSE</u>	Do not perform equilibrium combustion calculation
SHOCK	TRUE	Perform frozen and equilibrium shock calculations
	<u>FALSE</u>	Do not perform shock calculation
TCON	TRUE	Hold temperature constant
	<u>FALSE</u>	Do not hold temperature constant
RHOCON	TRUE	Hold volume (density) constant
	<u>FALSE</u>	Do not hold volume (density) constant

(6) Third-body efficiencies – To input third-body efficiencies ALLM1 in NAMELIST PROB must be set to FALSE; otherwise, all efficiencies are equal to one and no cards are needed in this section. The third-body efficiency card format is as follows (from bulletin of ref. 2):

<u>Card column</u>	<u>FORTRAN format</u>	<u>Content</u>
1 to 45		Reaction as written in section (2) of this appendix for inputting reactions
46 to 48		Not read
49 to 56	A8	Name of species to be assigned third body ratio other than unity
57		Not read
58 to 63	F6.3	Efficiency ratio for species in columns 49 to 56
64 to 65		Not read

## APPENDIX A

<u>Card column</u>	<u>FORTRAN format</u>	<u>Content</u>
66 to 73	A8	Name of species to be assigned third body ratio other than unity
74		Not read
75 to 80	F6.3	Efficiency ratio for species in columns 66 to 73

The end of the list of third-body efficiencies is signaled by a blank card following the last efficiency card.

(7) Initial conditions – The initial conditions for a problem are input through NAMELIST START. The parameters are as follows:

<u>Name</u>	<u>Value</u>	<u>Explanation</u>
Time	.....	Time in seconds
	<u>0.</u>	For default
X	.....	Distance
	<u>0.</u>	For default
MACH	.....	Mach number
	0.	For default
U	.....	Velocity
RHO	.....	Density
T	.....	Temperature
Area	.....	Area for a flow calculation
MDOT	.....	Mass flow rate for a flow calculation
MM Hg	TRUE	Pressure input in mm of mercury
	<u>FALSE</u>	Pressure input in user's choice of input units

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<u>Name</u>	<u>Value</u>	<u>Explanation</u>
MOLEF	<u>TRUE</u>	Mole fractions input
	<u>FALSE</u>	Mass fractions input

The starting mixture is input as mole fraction or mass fraction of the individual component species. The sum of the individual species mass fractions or mole fraction must be one.

(8) Permanently neglected species - The program of this paper does not neglect species from error consideration, and no cards from this section are necessary.

(9) Final card - The word FINIS in columns 1 to 5 designates that the input data list for a particular case is complete.

As can be seen there are very few new input variables and the input data deck structure is very near that described in reference 2. Multiple cases can be run as described in reference 2.

### Error Messages

The error messages built into the program are listed in the following section; their meanings are indicated.

The subroutine where the error was printed is also indicated. There are 16 remaining from the original program of reference 2 and 6 from the Gear package of reference 3. They are as follows:

#### Main Program GPAK:

(1) End of this case - read data for next case.

Normal end of case reached.

(2) A fatal error has occurred - case terminated.

Indicates that an unrecoverable error has occurred during the call to subroutine KINP and the logical variable NEXT has been set true. This message will be preceded by message from subroutine KINP and the subroutines KINP calls.

#### Subroutine KINP:

(3) The input reaction list does not contain the reaction (- + - = - + -).

Indicates error made in specifying third-body ratio information or during multiple case execution.

(4) The master species list does not contain the species . . . .

Indicates that the printed species is not in the master species list, ALSP in BLOCK DATA.

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(5) The input species list does not contain the species . . . .

Indicates an error in entering third-body efficiencies.

(6) Invalid input composition Sum = x.xxxx.

Indicates input composition does not sum to one.

### Subroutine SHOCKS:

(7) Equilibrium shock calculation failed.

Indicates iteration of equilibrium shock equations failed to converge.

(8) Frozen shock calculation failed.

Indicates iteration of frozen shock equations failed to converge.

### Subroutine EQLBRM:

(9) Derivative matrix singular.

Indicates a singular derivative matrix encountered during an equilibrium calculation.

(10) Singular matrix.

Indicates a singular matrix encountered in an equilibrium calculation.

(11) XX iterations did not satisfy convergence requirements.

Indicates iteration of equilibrium equations failed to converge.

(12) Restart.

Indicates equilibrium calculation restarted.

### Subroutine OUTP:

(13) Invalid composition.

Indicates that mass fractions do not sum to one.

### Subroutine DIFFUN:

(14) Warning Mach number - x.xxx is approaching 1.0.

Indicates that for assigned area calculations numerical problems could be encountered if the Mach number is between 0.9 and 1.1.

### Subroutine THRM:

(15) Error T = xxxx.xx is out of range.

Indicates a temperature above the range of the thermodynamic data has been submitted to THRM for calculation of properties.

(16) Warning T = xxxx.xx is out of range extrapolated values returned.

Indicates a temperature below the range of the thermodynamic data has been submitted to THRM for calculation of properties.

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A number of error messages may be printed if an error condition is encountered in subroutine STIFF. These messages are output as follows from Hollerith format contained in DRIVES.

(17) KFLAG = -1 from STIFF at T = xxxx.xx

Error test failed with ABS (H) = HMIN

H has been reduced to 0.xxxx and STEP will be retried.

This message is encountered often at the start of a problem if HMIN (which is the initial step size) is too large. After 10 reductions of 10 orders of magnitude in step size, and the error condition still exists, the next message is printed.

### PROBLEM APPEARS UNSOLVABLE WITH GIVEN INPUT

At this point, the user may elect to retry the problem with a much smaller HMIN.

(18) KFLAG = -2 from STIFF at T = xxxx.xx H = 0.xxxx

The requested error is smaller than can be handled.

At this point, subroutine YOUTD is called and intermediate printout can be used to enable the user to decide on his next course of action – perhaps relax the relative error requirements. Subroutine YOUTD may be changed by the user to provide the variables he wishes to view.

(19) KFLAG = -3 from STIFF at T = xxxx.xx

Corrector convergence could not be achieved.

This error message will be followed by the messages in section 1 and ultimately the user may be required to alter the program internally if a solution with the present input is desired.

(20) Illegal Input EPS · LE · 0

Indicates the maximum error is zero or negative.

(21) Illegal Input N · LE · 0

Indicates the number of equations to be solved is zero or negative.

(22) Illegal Input (TO - TLAST) \* HO · GE · 0.

Indicates that initial time or distance is greater or equal to final time or distance

or

initial step to be taken in a negative direction

or

the final time is negative.

Error messages (20), (21), and (22) are the results of faulty input and may be corrected easily by retyping the pertinent variable value on the input cards.

## APPENDIX B

### HYBRID PROGRAM LISTING

The entire hybrid program listing is contained herein.

```
PROGRAM GPAK(INPUT,OUTPUT,TAPES=INPUT,TAPE6=OUTPUT,TAPE4,TAPE7)
C***** THIS PROGRAM HAS BITKERS INPUT AND OUTPUT WITH THE GEAR
C*** PACKAGE USED FOR INTEGRATION.
C***** LOGICAL NEXT
LOGICAL KTCON
LOGICAL KUP
DIMENSION Y(28,13),YDOT(56)
COMMON/GJUNK/TLAST
COMMON/COND/DUM1(5),X(28),DUM2(2),NEXT
COMMON/STCOM1/N,T,H,HMIN,HMAX,EPS,MF,KFLAG,JSTART
COMMON/CONT/KTCON
COMMON/UPDT/KUP
C READ AND CONVERT INPUT, PERFORM PRE-KINETIC CALCULATIONS
CALL RINP
1 IF (NEXT) GO TO 1000 .
C PRINT REACTIONS, ASSIGNED VARIABLE PROFILE, INTEGRATION CONTROLS
CALL OUT1
C COMPUTE (NON-INPUT) INITIAL CONDITIONS
DO 17 I=1,56
YDOT(I)= 0.
17 CONTINUE
METH = MF/10
DO 15 I=1,28
DO 15 J=1,13
Y(I,J)=0.
15 CONTINUE
DO 20 I=1,N
Y(I,1) = X(I)
20 CONTINUE
IFN = 0
NPEDV = 0
KUP = .FALSE.
IF(METH .EQ. 1) GO TO 23
K2=6
23 GO TO 24
24 CONTINUE
K2=13
CALL DIFFUN(N,T,Y,YDOT,IFN,NPEDV,K2)
KTCON=.TRUE.
25 CONTINUE
KTCON=.TRUE.
CALL DRIVES(N,T,TLAST,Y,HMIN,EPS,MF,KFLAG,K2)
IF(KFLAG .EQ. -4) NEXT = .TRUE.
IF (NEXT) GO TO 1000

CALL DRIVES(N,T,TLAST,Y,HMIN,EPS,MF,KFLAG,K2)
IF(KFLAG .EQ. -4) NEXT = .TRUE.
IF (NEXT) GO TO 1000

100 WRITE (6,101)
101 FORMAT (7H0(GCKP),5X,44HEND OF THIS CASE - READ DATA FOR NEXT CA
*SE)
GO TO 13

1000 WRITE (6,1001)
1001 FORMAT (7H0(GCKP),5X,46HA FATAL ERROR HAS OCCURRED - CASE TERMIN
*ATED)

13 CONTINUE
CALL RINP
GO TO 1
END
```

## APPENDIX B

### SUBROUTINE KINP

```

C INPUT CAN BE ACCEPTED IN (1) INTERNAL (CGS) UNITS, (2) FPS UNITS,
C (3) SI UNITS

C THE FOLLOWING UNITS ARE USED INTERNALLY
C * DISTANCE      CM      *
C * AREA          CM**2    *
C * MASS FLOW RATE GM/SEC   *
C * PRESSURE      ATM     *
C * TIME          SEC     *
C * VELOCITY      CM/SEC   *
C * DENSITY       GM/CC    *
C * TEMPERATURE   DEG K    *
C * CONCENTRATION MOLE(I)/MASS  *

C INTERNAL CORRESPONDENCE
C * DVAR - DEPENDENT VARIABLE *
C * IVAR - INDEPENDENT VARIABLE *
C * AVAR - ASSIGNED VARIABLE *

C THE FOLLOWING LOGICAL TAPE UNITS ARE REQUIRED
C * LTHM (6) - FOR THERMODYNAMIC DATA *
C * LDAT (7) - FOR TEMPORARY STORAGE OF DATA CARDS *
C LOGICAL TAPE UNIT ASSIGNMENTS ARE SPECIFIED IN #NAMBLK#
```

C THE STOICHIOMETRIC COEFFICIENT OF A  
 C REACTANT (LEFT HAND SIDE) IS NEGATIVE  
 C PRODUCT (RIGHT HAND SIDE) IS POSITIVE

```

LOGICAL ALLMI,CONC,DBUGO,EXCHR,MOLEF,MMHG,NEXT
LOGICAL COMBUS,RHOCON,SHOCK,TCON
LOGICAL PAPS

INTEGER STOIC

REAL MDOT,IVAR,M,MH,N,LSUBM,MIXMH,M2,NEW

DIMENSION Istoic(4)
DIMENSION lss(25),tbr(3),thmc(7,2)
DIMENSION sp(4),dsp(4),spp(2),dspv(2),spnm(28),dpsnm(28)
DIMENSION lmt(4),subs(4),c(25),cx(4)
DIMENSION cja(2),fja(2),sua(2),cup1(2),cup2(2),fup(2),sup(2)

COMMON/LTUS/LTHM,LDAT,NTHRD,NBLANK,NPHOTO
COMMON/OPTS/VERSI,TIMEV,VERSA,AREAV,TCON,RHOCON,IPRCOD
COMMON/COND/AREA,MDUT,P,IVAR,V,RHO,T,SIGMA(25),LS,LSP3,NEXT
COMMON/REAC/LSR(4,50),XX(50),RATE(50),LKEQ(50),DLKEQ(50),MM(50),LR
COMMON/RRAT/A(50),V(50),EACT(50),B(50),M(25,50),ALLM1
COMMON/AFUN/CN(4),ITPSZ,LSUBM,ETA,D,VISC,BETA
COMMON/SPEC/ SNAM(31),MW(25),W(25),STOIC(25,50),OMEGA(25,50)
COMMON/STCON/NOTD,H,HMIN,HMAX,EMAX,MF,KFLAG,JSTART
COMMON/TCOF/TC(7,2,25),TLow,Tmid,Thi
COMMON/XVSA/XTB(60),ATB(40),NT,XU,AU(2),CX3,CX2,CXL,CX0
COMMON/SNMW/DALSP(75),ALMW(75)
COMMON/KOUT/TITLE(20),UNIT0,UNIT0,CONC,EXCHR,DELH(50),FPS,SI,DBUGO
COMMON/GHSC/GRT(25),HRT(25),SR(25),CPR(25),DCPR(25)
COMMON/NECC/RR,MIXMH,M2,GAMMA,TCPR,R
COMMON/MISC/TT,PP,CPR,HRO,ENN,SUMN,ENNL,LLMT(15),B0(15)
COMMON/INDX/TP,HP,NLM,NS,IQ1,CONVG,KMAT,IMAT
COMMON/STCS/STOIC(4,50),EQUIL(50)
COMMON/SNOB/CXTB(40),CATB(40),NZ
COMMON/GJUNK/TLAST
COMMON/STCOM/TPRIT,PAPS
COMMON/PRIN/TPRINT(50),NPRI,NCO

EQUIVALENCE (C,SIGMA),(SPNM,DPSNM),(SP,DSP),(SPP,DSPP),(SPT,SP)
EQUIVALENCE (SPNM,SNAM(4)),(EFFM,SPNM(26)),(BLANK,SPNM(27))
EQUIVALENCE (HNH,SPNM(28))
EQUIVALENCE (CX3,CX)

DATA CU,FU,SU/2HCH,2HFT,2HM /
DATA CUA/4HCM**1,LH2/,FUA/4HFT**1,LH2/,SUA/4HM**2,LH /
DATA CUP1/4HMMHG,LH /,CUP2/3HATM,LH /,FUP/4HLB/F,4HT**2/,SUP/4HN/H
**2H**2/
DATA NEW,CHANGE,REPEAT/3HNEW,4HCHAN,4HREPE/
DATA TAPEND,CARDS/3HENd,4HCARD/

NAMELIST/PROB/HMIN,HMAX,EMAX,ALLMI,CONC,EXCHR,END,DBUGO,
* IPRCOD,ITPSZ,XTB,ATB,NTB,CX3,CX2,CXL,CX0,LSUBM,ETA,D,VISC,BETA
*,COMBUS,RHOCON,SHOCK,TCON,IPRIT
*,TPRIT
*,TPRINT,NPRI,NCO,PAPS,IDEI

C THERMODYNAMIC DATA WILL BE INPUT FROM ##UNIT##
REWIND LTHM
READ (5,991) UNIT
99 FORMAT (20A4)
IF (UNIT .NE. CARDS) GO TO 3

REWIND LTHM
READ (5,981) TLow,Tmid,Thi
98 FORMAT (3F10.3)
WRITE (LTHM,981) TLow,Tmid,Thi
1 READ(5,971) SPT,(LMT(I),SUBS(I),I=1,4)
97 FORMAT(A8,16X,4(A2,F3.0))
C ##END## CARD SIGNALS END OF THERMODYNAMIC DATA
IF(SPT .EQ. TAPEND) GO TO 2

```

## APPENDIX B

```

      WRITE(LTHM,97) SPT,(LMT(I),SUBS(I),I=1,4)
      READ(5,96) ((THMC(K,I),K=1,7),I=1,2)
96 FORMAT(5E15.8)
      WRITE(LTHM,96) ((THMC(K,I),K=1,7),I=1,2)
      GO TO 1
2 WRITE(LTHM,97) SPT
      REWIND LTHM

3 CALL CIMAGE
C   READ OUTPUT TITLE
C   READ (LDAT,99) TITLE
C   ACTION = NEW
C   GO TO 4

      ENTRY RINP
      NCD = 0
      IDEL = 1
      PAPS=.FALSE.
      NEXT = .FALSE.
      CALL CIMAGE
C   READ NEW OUTPUT TITLE
C   READ (LDAT,99) TITLE
C   READ ACTION SWITCH
C   READ (LDAT,99) ACTION

      IF (ACTION .NE. NEW) GO TO 9
C   SET STANDARD OPTIONS
4 CONC = .TRUE.
      EXCHR = .FALSE.
      COMBUS = .FALSE.
      SHOCK = .FALSE.
      TCON = .FALSE.
      RHOCON = .FALSE.
      DBUGO = .FALSE.
      MF=22
      NCD = 0
      IDEL = 1
      PAPS = .FALSE.
      IPRIT = 5
      EMAX = 0.0001
      ITPSZ = 5
      ALLMI = .TRUE.
      DO 5 I=1,25
      DO 5 J=1,50
5 M(I,J) = 1.

C   INITIALIZE
      NEXT = .FALSE.
      NLM = 0
      NS = 0
      LS = 0
      LR = 0
      NT = 0
      DO 6 I=1,40
      XTB(I) = 0.
      CXTB(I) = 0.
      ATB(I) = 0.
6 CATB(I) = 0.
      UNCEND = 0.
      CEND = 0.
      NP = 0
      DO 8 J=1,50
      DO 801 I=1,4
801 NSTOIC(I,J) = 0
      DO 802 I=1,25
802 STOIC(I,J) = 0
8 CONTINUE
      LSUBM = 0.
      ETA = 0.
      D = 0.
      VISC = 0.
      BETA = 0.
      CX3 = 0.
      CX2 = 0.
      CX1 = 0.
      CX0 = 0.
      GO TO 14

9 IF (ACTION .NE. CHANGE) GO TO 13
C   READ REACTION AND (CHANGED) REACTION RATE
10 READ(LDAT,95) (ISTOIC(I),SP(I),I=1,4),TA,TN,TEA
95 FORMAT(2(1X,A8,1X),2X,2(1X,A8,1X),3X,E11.4,2(2X,F8.4))
C   BLANK CARD SIGNALS END OF CHANGE REACTION LIST
IF(SP(2) .EQ. BLANK) GO TO 12
C   ADJUST STOICHIOMETRIC COEFFICIENTS
      DO 510 I=1,4
      IF (ISTOIC(I) .NE. 0) GO TO 510
      IF (SP(I) .EQ. EFFM .OR. SP(I) .EQ. BLANK .OR. SP(I) .EQ. HNU) GO TO 510
      ISTOIC(I) = 1
510 CONTINUE
      ISTOIC(1) = -ISTOIC(1)
      ISTOIC(2) = -ISTOIC(2)
C   SEARCH INPUT REACTION LIST
      DO 511 J=1,LR
      DO 511 I=1,4
      NN = LSR(I,J)
      IF (DSPNN(NN) .NE. DSP(I) .OR. NSTOIC(I,J) .NE. ISTOIC(I))
* GO TO 11
511 CONTINUE

```

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```

A(J) = TA
N(J) = TN
EACT(J) = TEA
GO TO 10
11 CONTINUE
C   ERROR MESSAGE - NO MATCH FOUND
    ISTDIC(1) = -ISTOIC(1)
    ISTDIC(2) = -ISTOIC(2)
    WRITE(6,101) (ISTOIC(I),SP(I),I=1,4)
101 FORMAT (7HO(KINP),5X,55HTHE INPUT REACTION LIST DOES NOT CONTAIN T
*HE REACTION ,I1,1H*,AB,3H + ,I1,1H*,AB,3H = ,I1,1H*,AB,3H +
* I1,1H*,AB)
    NEXT = .TRUE.
    GO TO 10
12 READ (LDAT,99) ACTION
13 IF (ACTION .EQ. REPEAT) GO TO 33

14 LSOLD = LS
    LROLD = LR
C   READ (NEW OR ADDED) REACTION AND REACTION RATE
15 READ(LDAT,95) (ISTOIC(I),SP(I),I=1,4),TA,TN,TEA
C   BLANK CARD SIGNALS END OF NEW OR ADD REACTION LIST
    IF(SP(2) .EQ. BLANK) GO TO 21
C   ADJUST STOICHIMETRIC COEFFICIENTS
    DO 515 I=1,4
    IF (ISTOIC(I) .NE. 0) GO TO 515
    IF(SP(I) .EQ. EFFM .OR. SP(I) .EQ. BLANK .OR. SP(I) .EQ. HNU
    * ) GO TO 515
    ISTDIC(I) = 1
515 CONTINUE
    ISTDIC(1) = -ISTOIC(1)
    ISTDIC(2) = -ISTOIC(2)
    LR = LR + 1
    A(LR) = TA
    N(LR) = TN
    EACT(LR) = TEA
    DO 20 I=1,4
    NSTDIC(I,LR) = ISTDIC(I)
    IF (I .EQ. 2 .OR. I .EQ. 3) GO TO 215
    IF(SP(I) .EQ. EFFM) GO TO 19
    IF(SP(I) .EQ. BLANK) GO TO 219
    IF(SP(I) .EQ. HNU) GO TO 319
215 IF (LS .EQ. 0) GO TO 17
C   MATCH INPUT SPECIES AGAINST INPUT SPECIES LIST
    DO 16 II=1,LS
    IF (DOSPM(II) .NE. DSP(II)) GO TO 16
    LSR(I,LR) = II
    STOIC(II,LR) = STOIC(II,LR) + ISTDIC(I)
    GO TO 20
16 CONTINUE

C   MATCH INPUT SPECIES AGAINST MASTER SPECIES LIST
17 DO 18 II=1,75
    IF (DALSP(II) .NE. DSP(II)) GO TO 18
    LS = LS + 1
    LSR(I,LR) = LS
    STOIC(LS,LR) = ISTDIC(I)
    SPNM(LS) = SP(I)
    MW(LS) = ALMW(II)
    ISS(LS) = II
    GO TO 20
18 CONTINUE
C   ERROR MESSAGE - NO MATCH FOUND
    WRITE(6,102) SP(I)
102 FORMAT (7HO(KINP),5X,54HTHE MASTER SPECIES LIST DOES NOT CONTAIN T
*HE SPECIES ,AB)
C ** RUN TERMINATED - ERROR IN INPUT REACTION LIST
    STOP

19 LSR(I,LR) = NTHRD
    GO TO 20

219 LSR(I,LR) = NBLANK
    GO TO 20

319 IF (II .EQ. 1) GO TO 320
    ISTDIC(1) = -ISTOIC(1)
    ISTDIC(2) = -ISTOIC(2)
    WRITE(6,106) (ISTOIC(I),SP(I),I=1,4)
106 FORMAT (7HO(KINP),5X,42HIMPROPER FORMAT FOR PHOTOCHEMICAL REACTION
*2X,I1,1H*,AB,3H + ,I1,1H*,AB,3H = ,I1,1H*,AB,3H + ,I1,1H*,AB)
    STOP
320 LSR(I,LR) = NPHOTO
20 CONTINUE
    GO TO 15

21 IF (ACTION .NE. NEW) GO TO 25
C   READ INSERT SPECIES (4 PER CARD)
22 READ(LDAT,94) (SP(I),I=1,4)
94 FORMAT(4(A8,BX))
    DO 24 I=1,4
    BLANK FIELD SIGNALS END OF INSERT SPECIES LIST
    IF(SP(I) .EQ. BLANK) GO TO 25
C   SEARCH MASTER SPECIES LIST
    DO 23 II=1,75
    IF (DALSP(II) .NE. DSP(II)) GO TO 23
    LS = LS + 1
    SPNM(LS) = SP(I)
    MW(LS) = ALMW(II)

```

## APPENDIX B

```

1SS(LS) = 11
GO TO 24
23 CONTINUE
C   ERROR MESSAGE - NO MATCH FOUND
    WRITE(6,102) SP(I)
    NEXT = .TRUE.
    LS = LS + 1
    MW(LS) = 1.
24 CONTINUE
GO TO 22

25 IF (LS .EQ. LSOLD) GO TO 30
C   GET THERMODYNAMIC COEFFICIENTS FROM TAPE
    LS = LSOLD + 1
    II = LSOLD
    READ (LTHM,98) TLOW,TMID,THI
26 READ(LTHM,97) SPT
    IF(SPT .EQ. TAPEND) GO TO 29
    READ (LTHM,96) (ITHMC(K,II),K=1,7),I=1,2
    DO 28 I=LSP,LS
    IF (DSPNM(I) .NE. DSP(I)) GO TO 28
    DO 27 KK=1,2
    DO 27 K=1,7
27   TC(K,KK,I) = THMC(K,KK)
    II = II + 1
    IF (II .LT. LS) GO TO 26
    GO TO 230
28 CONTINUE
GO TO 26
C   ERROR MESSAGE - END OF THERMO TAPE REACHED
29 WRITE (6,103)
103 FORMAT (7HO(KINP),5X,42HEND OF THERMO TAPE - NOT ALL SPECIES FOUND
*)
    NEXT = .TRUE.
230 REWIND LTHM

30 LRP = LR0LD + 1
C   GET SPECIES ENTHALPY AT REFERENCE T
    TREF = 298.15
    CALL THRM (TREF,0.)
    TRAL = TREF*1.987165
C   COMPUTE HEAT OF REACTION
    DO 32 J=LRP,LR
    DELH(J) = 0.
80 READ (LDAT,PROB)
    H = HMIN
    IF(.NOT. PAPS) GO TO 1001
    IF(IDEI .EQ. 1) GO TO 1001
    PRINC = END/IDEI
    DO 1000 I=1,IDEI
    TPRINT(I) = PRINC*I
1000 CONTINUE
    NPRIN = IDEI
1001 CONTINUE
    IF (.NOT. ALLMI) GO TO 36
    DO 77 I=1,25
    DO 77 J=1,50
    77 M(I,J) = 1.
    GO TO 40
C   READ THIRD BODY RATIOS
36 READ(LDAT,91) (ISTOIC(I),SP(I),I=1,4), (SPP(I),TBR(I),I=1,2)
91 FORMAT(2(I,LX,A8,LX),2X,2(I,LX,A8,LX),2(2X,A8,LX,F6.3))
C   BLANK CARD SIGNALS END OF THIRD BODY RATIO LIST
    IF(SP(2) .EQ. BLANK) GO TO 40
C   ADJUST STOICHIOMETRIC COEFFICIENTS
    DO 536 I=1,4
    IF (ISTOIC(I) .NE. 0) GO TO 536
    IF(SP(I).EQ.EFFM.OR.SP(I).EQ.BLANK.OR.SP(I).EQ.MNU) GO TO 536
    ISTOIC(I) = 1
536 CONTINUE
    ISTOIC(1) = -ISTOIC(1)
    ISTOIC(2) = -ISTOIC(2)
C   SEARCH INPUT REACTION LIST
    DO 39 J=1,LR
    DO 539 I=1,4
    NN = LSR(I,J)
    IF (DSPNM(NN) .NE. DSP(I) .OR. NSTOIC(I,J) .NE. ISTOIC(I))
    * GO TO 39
539 CONTINUE
    DO 38 I=1,2
    IF(SPP(I) .EQ. BLANK) GO TO 38
C   SEARCH INPUT SPECIES LIST
    DO 37 II=1,LS
    IF (DSPNM(II) .NE. DSPP(I)) GO TO 37
    M(II,J) = TBR(I)
    GO TO 38
    DO 532 I=1,4
    NN = LSR(I,J)
    IF (NN .GT. LS) GO TO 532
    STOC = NSTOIC(I,J)
    DELH(IJ) = DELH(J) + STOC*MRT(NN)
532 CONTINUE
    32 DELH(J) = DELH(J)*TRAL
    LSP3 = LS + 3
C   RESET STANDARD OPTIONS

```

## APPENDIX B

```

33 MOLEF = .TRUE.
      MHHG = .FALSE.

C   INITIALIZE
      END = 0.
      NTB = 0.
      AREA = 0.
      MDOT = 0.
      P = 0.
      V = 0.
      RHO = 0.
      T = 0.

C   READ NAME OF INDEPENDENT VARIABLE, NAME OF ASSIGNED VARIABLE,
C   INPUT UNITS, OUTPUT UNITS
      READ (LOAT,92) VERSI,VERSA,UNITI,UNITO
92 FORMAT (4A4,6X)
      IF (VERSA .EQ. BLANK) VERSA = AREAV

      IF (ACTION .NE. NEW) GO TO 80
C   INITIALIZE STEP SIZE LIMITS
      IF (VERS1 .EQ. TIMEV) GO TO 78
      HMIN = 0.0001
      HMAX = 0.1000
      IPRCOD = 2
      GO TO 79
78 HMIN = 0.500E-07
      HMAX = 0.500E-04
      IPRCOD = 4
79 IF (VERSA .EQ. AREAV) IPRCOD = IPRCOD - 1

C   READ INTEGRATION CONTROLS, PROFILE OPTIONS,
C   PRINT OPTIONS, SPECIALTY SWITCHES
37 CONTINUE
C   ERROR MESSAGE - NO MATCH FOUND
      WRITE(6,104) SPP(I)
104 FORMAT (7H0(KINP),5X,53HTHE INPUT SPECIES LIST DOES NOT CONTAIN TH
      *E SPECIES ,AB)
      NEXT = .TRUE.
38 CONTINUE
      GO TO 36
39 CONTINUE
C   ERROR MESSAGE - NO MATCH FOUND
      ISTOIC(1) = -ISTOIC(1)
      ISTOIC(2) = -ISTOIC(2)
      WRITE(6,101) (ISTOIC(I),SP(I),I=1,4)
      NEXT = .TRUE.
      GO TO 36

C   GET INITIAL CONDITIONS
40 CALL INIT (ISS,MHHG,MOLEF)

C   CHECK INPUT COMPOSITION
      CSUM = 0.
      DO 47 I=1,LS
47 CSUM = CSUM + C(I)
      IF (ABS(I,-CSUM) .LE. .001) GO TO 48
      WRITE(6,105) CSUM,(SPNM(I),C(I),I=1,LS)
105 FORMAT (7H0(KINP),5X,33HINVALID INPUT COMPOSITION SUM = ,F11.6//
      *(12X,A8,E20.5))
      NEXT = .TRUE.
      RETURN

C   SET INITIAL STEP SIZE
48 IF (ITPSZ .GT. 2) GO TO 53
      IF (ITPSZ .EQ. 1 .AND. NTB .EQ. 0) GO TO 53
      IF (NTB .NE. 0) NT = NTB
      NZ = NTB
      CONV = 1.
      CON2 = 1.
      IF (VERSA .NE. AREAV) GO TO 203
      XU = CU
      AU(1) = CUA(1)
      AU(2) = CUA(2)

C   CONVERT AREA PROFILE TO INTERNAL UNITS
      IF (UNITI .NE. FPS) GO TO 201
      XU = FU
      AU(1) = FUA(1)
      AU(2) = FUA(2)
      CONV = 30.48
      GO TO 202
201 IF (UNITI .NE. SI) GO TO 206
      XU = SU
      AU(1) = SUA(1)
      AU(2) = SUA(2)
      CONV = 100.
202 CON2 = CONV*CONV
      GO TO 206

203 XU = CU
      AU(1) = CUP2(1)
      AU(2) = CUP2(2)

C   CONVERT PRESSURE PROFILE TO INTERNAL UNITS
      IF (UNITI .NE. FPS) GO TO 204
      XU = FU
      AU(1) = FUP(1)

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## APPENDIX B

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AU(2) = FUP(2)
CONV = 30.48
CON2 = L./2116.2
GO TO 205
204 IF (UNIT1 .NE. SI) GO TO 205
XU = SU
AU(1) = SUP(1)
AU(2) = SUP(2)
CONV = 100.
CON2 = L./1.01325E+05
205 IF (.NOT. MMHG) GO TO 206
AU(1) = CUP1(1)
AU(2) = CUP1(2)
CON2 = L./760.
206 IF (VERSI .EQ. TIMEV) CONV = 1.
IF (ITPSZ .EQ. 2) GO TO 208
DO 207 I=1,NTB
CXTB(I) = XTB(I)*CONV
207 CATB(I) = ATB(I)*CON2
GO TO 53
208 DO 209 I=1,6
209 CN(I) = CX(I)*CON2

53 CONTINUE

59 IF (ITPSZ .EQ. 1) CALL CUBS (CXTB,CATB,NT)

      IF (UNIT1 .NE. FPS) GO TO 63
C   CONVERT FROM FPS UNITS TO INTERNAL (CGS) UNITS
      IF (VERSI .NE. TIMEV) GO TO 60
      DVAR = DVAR*30.48
      GO TO 61
60 IVAR = IVAR*30.48
61 IF (MMHG) P = P*2.7845
P = P/2116.2
AREA = AREA*929.0304
MDOT = MDOT*453.59237
V = V*30.48
RHO = RHO/62.43
T = T/1.8
IF (VERSI .EQ. TIMEV) GO TO 68
CEND = UNCEND*30.48
GO TO 68
63 IF (UNIT1 .NE. SI) GO TO 67
C   CONVERT FROM SI UNITS TO INTERNAL (CGS) UNITS
      IF (VERSI .NE. TIMEV) GO TO 64
      DVAR = DVAR*100.
      GO TO 65
64 IVAR = IVAR*100.
65 IF (MMHG) P = P*133.3224
P = P/1.01325E+05
AREA = AREA*10000.
MDOT = MDOT*1000.
V = V*100.
RHO = RHO*.001
IF (VERSI .EQ. TIMEV) GO TO 68
CEND = UNCEND*100.
GO TO 68
67 CEND = UNCEND
IF (MMHG) P = P/760.

68 MIXMW = 0.

      IF (.NOT. MOLEF) GO TO 71
C   MOLE FRACTION TO MOLES(I)/MASS(MIXTURE)
      DO 69 I=1,LS
69 MIXMW = MIXMW + C(I)*MW(I)
      DO 70 I=1,LS
70 SIGMA(I) = C(I)/MIXMW
      GO TO 73

C   MASS FRACTION TO MOLES(I)/MASS(MIXTURE)
71 DO 72 I=1,LS
SIGMA(I) = C(I)/MW(I)
72 MIXMW = MIXMW + SIGMA(I)
MIXMW = L./MIXMW

C   UNIVERSAL GAS CONSTANT IN ATM-CC/MOLE-DEG K
73 RR = 82.056
C   UNIVERSAL GAS CONSTANT IN ERGS/MOLE-DEG K
R = 8.3143E+07

      IF (M2 .EQ. 0. .AND. .NOT. (COMBUS .OR. SHOCK)) GO TO 81
      CALL THRM (T,1.)
      CPRO = 0.
      DO 74 I=1,LS
74 CPRO = CPRO + CPR(I)*SIGMA(I)
GAMMA = CPRO/(CPRO - 1./MIXMW)
      IF (V .NE. 0.) GO TO 81
V = SQRT(M2*R/MIXMW*GAMMA*T)

81 IF (P .EQ. 0.) GO TO 82
      RHO = P*MIXMW/(RR*T)
      GO TO 75
82 IF (RHO .EQ. 0.) GO TO 83
P = RHO*RR*T/MIXMW
      GO TO 75

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## APPENDIX B

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83 IF (IPRCOD .GT. 2) GO TO 84
X = IVAR
IF (VERSI .EQ. TIMEV) X = DVAR
CALL CINPICATB,CXTB,NT,X,AVAR,DUM1,DUM2)
GO TO 85
84 TIME = DVAR
IF (VERSI .EQ. TIMEV) TIME = IVAR
CALL CINPICATB,CXTB,NT,TIME,AVAR,DUM1,DUM2)
85 IF (VERSA .EQ. AREAV) GO TO 86
P = AVAR
GO TO 81
86 AREA = AVAR
RHO = MDOT/(AREA*V)
GO TO 82

75 IF (MDOT .EQ. 0.) MDOT = RHO*AREA*V
TO=IVAR
NO=LSP3
TLAST=END

IF (.NOT. (COMBUS .OR. SHOCK)) RETURN
HRO = 0.
DO 76 I=1,LS
76 HRO = HRO + HRT(I)*SIGMA(I)
HRO = HRO*T
M2 = V/R*V/T*MIXMW/GAMMA

C EQUILIBRIUM COMBUSTION
IF (COMBUS) CALL COMB

C EQUILIBRIUM AND FROZEN SHOCK
IF (SHOCK) CALL SHOK

RETURN
END

```

```

BLOCK DATA
C ALPHANUMERIC DATA FOR TESTING AND OUTPUT
COMMON/LTUS/LTHM,LDAT,NTHRD,NBLANK,NPHOTO
COMMON/OPTS/DUM1,TIME,DUM2,AREA,DUM(3)
COMMON/SPEC/SNAM(3),DUM4(25),EFFM,BLANK,HNU,DUM5(25,102)
COMMON/KOUT/DUM6(74),FPS,SI,DUM7

C LOGICAL TAPE UNIT ASSIGNMENTS
DATA LTHM,LDAT/4,7/

C SPECIES SUBSCRIPTS FOR M,BLANK, AND HNU
DATA NTHRD,NBLANK,NPHOTO/26,27,28/

C ALPHANUMERIC DATA
DATA TIME,AREA/6TIME,6AREA/
DATA SNAM,EFFM,BLANK/1HV,3HRHO,1HT,1HM,1H /
DATA HNU/3HHNU/
DATA FPS,SI/3FPS,2HSI/

END

```

```

BLOCK DATA
C SPECIES NAMES AND MOLECULAR WEIGHTS
COMMON/SNMM/ALSP(75),ALMW(75)

DATA ALSP/
* BHAR      , 8HC6H6   , 8HC6H11  , 8HC6H12  , 8HC2H6CD  ,
* 8HC2H5CD  , 8HC2H5OH , 8HC3CHO , 8HC3DM  , 8HC3CD  ,
* 8HC2H4OH  , 8HC2HDM , 8MHND3   , 8HBR    , 8H8R2   ,
* 8HC       , 8HC6H13   , 8HC6H14  , 8HC    , 8HC2H   ,
* 8HCCH3    , 8HCCH4   , 8HCN    , 8HC0    , 8HC02   ,
* 8HC2H3O   , 8HC2H    , 8HC2H2   , 8HC2M4  , 8HC2N   ,
* 8HC8H16   , 8HC8H17   , 8HC3H7   , 8HC3H6  , 8HC3H4  ,
* 8HC2H5   , 8HM     , 8HHCN   , 8HHCL   , 8HMF    ,
* 8HHO2    , 8HH2     , 8HH2O   , 8HH2O2  , 8HHE    ,
* 8HN      , 8HC8H18   , 8HC7H14  , 8HC7H15  , 8HNH2   ,
* 8HNH3    , 8HNU     , 8HN02   , 8HN2    , 8HN2H4  ,
* 8HN2O    , 8HN2O4   , 8HC7H16  , 8HO     , 8HOH    ,
* 8HO2     , 8HMNO   , 8HC2    , 8HXE    , 8HNH    ,
* 8HHC0    , 8HC2H20  , 8HC9H18  , 8HC2H3  , 8HC3H8  ,
* 8HC9H19  , 8HC9H20  , 8HC2H6   , 8HQ3    , 8HN03  ,

DATA ALMW/
* 39.948,    78.114,    83.154,    86.162,    58.081,
* 57.073,    66.070,    64.054,    32.042,    43.046,
* 45.062,    31.035,    63.013,    79.909,    159.820,
* 12.0112,   85.170,    86.170,    13.019,    14.027,
* 15.035,    16.043,    26.018,    28.011,    44.010,
* 43.046,    25.030,    26.038,    28.054,    38.029,
* 112.212,   113.224,   43.089,    42.081,    40.065,
* 29.062,    1.00797,   27.026,    36.461,    20.006,
```

## APPENDIX B

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* 33.005,    2.0159,    18.014,    34.014,    4.0026,
* 14.007,    114.232,   98.189,    99.197,    16.023,
* 17.031,    30.006,    46.006,    28.013,    32.045,
* 44.012,    92.009,    100.205,   15.9994,   17.007,
* 31.997,    31.014,    24.022,    131.300,   15.015,
* 29.0186,   30.026,    126.243,   27.0463,   44.097,
* 127.251,   128.259,   30.070,    47.9982,   62.0049/
END

SUBROUTINE THRM (T,HONLY)
C THIS ROUTINE CALCULATES (DIMENSIONLESS) THERMODYNAMIC PROPERTIES
C FROM POLYNOMIAL CURVE FITS

LOGICAL NEXT

COMMON/COND/DUM(33),LS,LSP3,NEXT
COMMON/GHSC/GRT(25),HRT(25),SR(25),CPR(25),DCPR(25)
COMMON/TCOF/C(7,2,25),TLow,TMid,Thi

F(T) = A1+T*(A2+T*(A3+T*(A4+T*A5)))

IF (T .EQ. 298.15) TPREV=0.
IF (T .EQ. TPREV) RETURN

IF (0.35*TLow .LE. T .AND. T .LE. Thi) GO TO 3
IF (T .LE. 1.20*Thi) GO TO 2

WRITE (6,100) T
100 FORMAT (7HO[THRM],5X,5HERROR,3X,3HT =,F8.2,16H IS OUT OF RANGE)
NEXT = .TRUE.
RETURN

2 WRITE (6,101) T
101 FORMAT (7HO[THRM],5X,7HWARNING,3X,3HT =,F8.2,16H IS OUT OF RANGE,
* 4X,28HEXTRAPOLATED VALUES RETURNED)

C LOCATE PROPER TEMPERATURE RANGE
3 K = 2
IF (T .GT. TMid) K = 1

DO 4 I=1,LS

C COMPUTE H/(R*T)
A1 = C(1,K,I) + C(6,K,I)/T
A2 = C(2,K,I)/2.
A3 = C(3,K,I)/3.
A4 = C(4,K,I)/4.
A5 = C(5,K,I)/5.
4 HRT(I) = F(T)
IF (HONLY .EQ. 0.) RETURN
TPREV = T
DO 5 I=1,LS

C COMPUTE G/(R*T)
A1 = C(1,K,I)*(1.-ALOG(T)) + C(6,K,I)/T - C(7,K,I)
A2 = -C(2,K,I)/2.
A3 = -C(3,K,I)/6.
A4 = -C(4,K,I)/12.
A5 = -C(5,K,I)/20.
GRT(I) = F(T)

C COMPUTE S/R
A1 = C(1,K,I)*ALOG(T) + C(7,K,I)
A2 = C(2,K,I)
A3 = C(3,K,I)/2.
A4 = C(4,K,I)/3.
A5 = C(5,K,I)/4.
SR(I) = F(T)

C COMPUTE CP/R
A1 = C(1,K,I)
A2 = C(2,K,I)
A3 = C(3,K,I)
A4 = C(4,K,I)
A5 = C(5,K,I)
CPR(I) = F(T)

C COMPUTE (DCP/DT)/R
A1 = C(2,K,I)
A2 = 2.*C(3,K,I)
A3 = 3.*C(4,K,I)
A4 = 4.*C(5,K,I)
A5 = 0.
5 DCPR(I) = F(T)

RETURN
END

```

## APPENDIX B

```

SUBROUTINE CUBS(X,Y,N,XI,YI,DY,D2Y)
C THIS ROUTINE IS USED TO CALCULATE VALUES OF THE ASSIGNED VARIABLE
C AND ITS DERIVATIVES
REAL LSUBM
DIMENSION X(N),Y(N)
DIMENSION D(40),S(40),T(40),U(40),V(40)
DIMENSION A3(40),A2(40),A1(40),A0(40)
COMMON/AFUN/C3,C2,C1,C0,ITPSZ,LSUBM,ETA,DIAM,VISC,BETA
EQUIVALENCE (S,A3),(T,A2),(U,A1),(V,A0)
G(A) = 1./{1. - A**ETA)
DG(B) = ETA/LSUBM*TERM***(ETA - 1.)*B*B
D2S(C,D,E) = C*(ETA - 1. + 2.*ETA*TERM**ETA*D)/E

C COMPUTE CUBIC SPLINE COEFFICIENTS FROM INPUT TABLE
C THIS ROUTINE WILL ACCEPT END CONDITIONS OF THE FORM
C   F#*(X(1)) = ALPHAI*F#*(X(2)) + BETAI*F#*(X(3)) + GAMMAI
C   F#*(X(N)) = ALPHAN*F#*(X(N-1)) + BETAN*F#*(X(N-2)) + GAMMAN
C THE CURRENT END CONDITIONS GIVE A PARABOLIC RUNDOUT
C   F#*(X(1)) = F#*(X(2))
C   F#*(X(N)) = F#*(X(N-1))

C CONSTRUCT (TRIDIAGONAL) COEFFICIENT MATRIX
C   S=DIAGONAL, T=SUPERDIAGONAL, U=SUBLIDIAGONAL, V=CONSTANTS
DXIM = X(2) - X(1)
DYIM = Y(2) - Y(1)
DIM = DYIM/DXIM
DXI = X(3) - X(2)
DYI = Y(3) - Y(2)
DI = DYI/DXI
BETAI = 0.
ALPHAI = 1.
GAMMAI = 0.
S(2) = (ALPHAI + 2.)*DXIM + 2.*DXI
T(2) = BETAI*DXIM + DXI
V(2) = (DI - DIM) - (GAMMAI/6.)*DXIM
U(3) = DXI
NM = N - 1
DO 2 I=3,NM
DXIM = DXI
DYIM = DYI
DIM = DI
DXI = X(I+1) - X(I)
DYI = Y(I+1) - Y(I)
DI = DYI/DXI
IF (I .EQ. NM) GO TO 3
S(I) = 2.*(DXIM + DXI)
T(I) = DXI
U(I+1) = T(I)
2 V(I) = DI - DIM
3 BETAN = 0.
ALPHAN = 1.
GAMMAN = 0.
S(NM) = 2.*DXIM + (2. + ALPHAN)*DXI
U(NM) = DXIM + BETAN*DXI
V(NM) = (DI - DIM) - (GAMMAN/6.)*DXI

NM2 = N - 2
DO 4 I=2,NM2
T(I) = T(I)/S(I)
V(I) = V(I)/S(I)
II = I + 1
S(II) = S(II) - U(II)*T(I)
4 V(II) = V(II) - U(II)*V(I)
V(NM) = V(NM)/S(NM)

D(NM) = V(NM)
DO 5 J=2,NM2
I = N - J
5 D(I) = V(I) - T(I)*D(I+1)
GET D(I) AND D(N) FROM END CONDITIONS
D(I) = ALPHAI*D(2) + BETAI*D(3) + GAMMAI/6.
D(N) = ALPHAN*D(NM) + BETAN*D(NM2) + GAMMAN/6.

C COMPUTE CUBIC SPLINE COEFFICIENTS
DO 6 I=1,NM
II = I + 1
DXI = X(II) - X(I)
DYI = Y(II) - Y(I)
DI = D(II)
DIM = D(I)
A3(I) = (DI - DIM)/DXI
DI = DI*X(II)
DIM = DIM*X(II)
A2(I) = -3.*{(DI - DIM)/DXI}
DI = DI*X(II)
DIM = DIM*X(II)
B = DYI/DXI - (D(II) - D(I))/DXI + B
A1(I) = 3.*{(DI - DIM)/DXI} + B
DI = DI*X(II)
DIM = DIM*X(II)

```

## APPENDIX B

```

6 A0(I) = -(DI - DIM)/DXI + Y(I) - D(I)*DXI*DXI - B*X(I)
RETURN

ENTRY CINP
NM=N-1
GO TO (7,10,11,11,13),ITPSZ

C COMPUTE Y, DY/DX, D2Y/DX2 FROM CUBIC SPLINE COEFFICIENTS
7 DO 8 I=1,NM
  II = I
  IF ((X(I) - XII)*(XI - X(I+1)) .GE. 0.) GO TO 9
  B CONTINUE
  WRITE (6,100) XI,X(I),X(N)
100 FORMAT (7H0,CINP),5X,3HXI=,F13.5,17H IS OUT OF RANGE/10X,5HX(1)=,
* F13.5,5X,5HX(N)=,F13.5)

  9 YI = ((A3(I)*XI + A2(I)*XI + A1(I)*XI + A0(I))
  DY = (3.*A3(I)*XI + 2.*A2(I)*XI + A1(I))
  D2Y = 6.*A3(I)*XI + 2.*A2(I)
  RETURN

C COMPUTE Y, DY/DX, D2Y/DX2 FROM INPUT POLYNOMIAL
10 YI = ((C3*XI + C2)*XI + C1)*XI + C0
  DY = (3.*C3*XI + 2.*C2)*XI + C1
  D2Y = 6.*C3*XI + 2.*C2
  RETURN

C COMPUTE Y, DY/DX, D2Y/DX2 FROM INPUT SPECIAL FUNCTION
C EXCEPTIONAL CASE AT X=0
11 IF (XI .EQ. 0.) GO TO 12
  TERM = XI/LSUBM
  YI = G(TERM)
  DY = DG(YI)
  D2Y = D2G(DY,YI,XI)
  RETURN

12 YI = 1.

C FIT A CUBIC THROUGH THE POINTS (0.,Y1),(.05,Y2#),(.05,Y2##), AND
C (.10,Y3##) IN ORDER TO FIND Y1# AND Y1##
13 TERM = .05/LSUBM
  Y2 = G(TERM)
  Y2P = DG(Y2)
  Y2PP = D2G(Y2P,Y2,.05)
  TERM = .10/LSUBM
  Y3 = G(TERM)
  Y3P = DG(Y3)
  Y3PP = D2G(Y3P,Y3,.10)

  DY = (.05*(Y3PP - Y2PP)/(.10 - .05)/2. - Y2PP)*.05 + Y2P
  D2Y = Y2PP - .05*(Y3PP - Y2PP)/(.10 - .05)
  RETURN

C V=0 CASE - ASSIGNED AREA IS NOT REQUIRED
13 YI = 1.
  DY = 0.
  D2Y = 0.
  RETURN

END

SUBROUTINE INIT (ISS,MMHG,MOLEFS)

C READ INITIAL CONDITIONS
LOGICAL MMHG,MOLEF,MMHGS,MOLEFS

REAL IVAR,MDDT,M2,MACH
REAL N,NF,NF2,NF3,NH2,NH3,NO,NO2,N2,N2H4,N2O,N2O4,NE,KR,NH,NOP,NO3
DIMENSION ISS(25),TINP(75)

COMMON/LTJS/LTHM,LDAT,NTHR,D,NBLANK,NPHOTO
COMMON/OPTS/VERSL,TIMEV,DUM1(5)
COMMON/COND/DVAR,AREA,MDDT,P,IVAR,V,RHO,T,CONC(25),LS,DUM2(2)
COMMON/NECC/DUM3(2),M2,DUM4(3)
COMMON/FAKE/
* AR     ,   C6H6    ,   C6H11    ,   C6H12    ,   C2H6CO    ,
* C2H5CO ,   C2H5OH   ,   C2H5CHO  ,   C2H5OH   ,   C2H5CO   ,
* C2H4OH ,   C2H2OH   ,   HNO3     ,   BR       ,   BR2      ,
* C     ,   C6H13    ,   C6H14    ,   CH       ,   CH2      ,
* CH3    ,   CH4      ,   CN       ,   CO       ,   CO2      ,
* C2H3O  ,   C2H      ,   C2H2    ,   C2H4    ,   C2N      ,
* C8H16  ,   C8H17    ,   C3H7    ,   C3H6    ,   C3H4    ,
* C2H5  ,   H        ,   HCN     ,   HCL     ,   HF      ,
* HO2   ,   H2      ,   H2O     ,   H2O2   ,   HE      ,
* N     ,   C8H18    ,   C7H14    ,   C7H15    ,   NH2      ,
* NH3   ,   NO      ,   NO2     ,   N2      ,   N2H4    ,
* N2O   ,   N2O4    ,   C7H16    ,   O       ,   OH      ,
* O2    ,   HNO     ,   C2       ,   XE      ,   NH      ,
* HCO   ,   CH2O    ,   C9H18    ,   C2H3    ,   C3H8    ,
* C9H19 ,   C9H20    ,   C2H6    ,   O3      ,   NO3

```

## APPENDIX B

EQUIVALENCE (TINP(1),AR)

```

NAMELIST/START/X,AREA,MDOT,P,TIME,V,RHO,T, MACH, MMHG,MOLEF,
* AR , C6H6 , C6H11 , C6H12 , C2H6CO ,
* C2H5CO , C2H5OH , CH3CHO , CH3OH , CH3CO ,
* C2H4OH , CH2OH , HNO3 , BR , BR2 ,
* C , C6H13 , C6H14 , CH , CH2 ,
* CH3 , CH4 , CN , CO , CO2 ,
* C2H3O , C2H , C2H2 , C2H4 , C2N ,
* C8H16 , C8H17 , C3H7 , C3H6 , C3H4 ,
* C2H5 , H , HCN , HCL , HF ,
* HO2 , H2 , H2O , H2O2 , HE ,
* N , C8H18 , C7H14 , C7H15 , NH2 ,
* NH3 , NO , NO2 , N2 , N2H4 ,
* N2O , N2O4 , C7H16 , O , OH ,
* O2 , HNO , C2 , XE , NH ,
* HCO , CH2O , C9H18 , C2H3 , C3H8 ,
* C9H19 , C9H20 , C2H6 , O3 , NO3

X = 0.
TIME = 0.
MACH = 0.
DO 1 I=1,75
1 TINP(I) = 0.
MMHG = MMHGS
MOLEF = MOLEFS

READ (LDAT,START)

MMHGS = MMHG
MOLEFS = MOLEF
IF (VERS1 .EQ. TIMEV) GO TO 2
IVAR = X
OVAR = TIME
GO TO 3
2 IVAR = TIME
OVAR = X

3 M2 = MACH*MACH
DO 4 I=1,LS
JJ = ISS(I)
4 CONC(I) = TINP(JJ)

RETURN
END

```

SUBROUTINE CIMAGE

```

C THIS ROUTINE READS EACH DATA CARD, PRINTS A CARD IMAGE, AND STORES
C THE IMAGE FOR LATER FORMATTED INPUT

DIMENSION CARD(20)

COMMON/LTUS/LTHM,LDAT,NTHRD,NBLANK,NPHOTO

EQUIVALENCE (WORD,CARD)

DATA FINIS,BLANK/4HFINI,1H /

READ (5,101) CARD
101 FORMAT (20A4)
IF (EOF,5) 998,999
998 STOP
999 CONTINUE
REWIND LDAT

WRITE (6,100)
100 FORMAT (1H1,56X,18H** DATA CARDS **//37X,1H1,9X,1H2,9X,1H3,9X,
* 1H4,9X,1H5,9X,1H6,9X,1H7,9X,1H8/24X,5HCC 1,8X,8(1H0,9X)//)
GO TO 2

1 READ (5,101) CARD
2 DO 3 I=1,20
  IF (CARD(I) .NE. BLANK) GO TO 4
3 CONTINUE
  WRITE (6,102)
102 FORMAT (60X,16H- BLANK CARD -)
  GO TO 5
4 WRITE (6,103) CARD
103 FORMAT (28X,20A4)
  IF (WORD .EQ. FINIS) GO TO 6
5 WRITE (LDAT,101) CARD
  GO TO 1

6 REWIND LDAT

RETURN
END

```

## APPENDIX B

```

SUBROUTINE OUTP
C   OUTPUT CAN BE GIVEN IN  (1) INTERNAL (CGSI) UNITS, (2) FPS UNITS
C   (3) SI UNITS

LOGICAL ALLM1,CONC,DBUGO,EXCHR,NEXT,RHOCON,TCON

REAL MDOT,IVAR,N,M,MW,MIXMW,M2,MACH,LSUBM

DIMENSION SPNM(28),PRC(25),PRX(50),XXH(50),ESP(25)

COMMON/DERV3/TDERV
CU*MON/LTUS/THM,LDAT,NTHRD,NBLANK,NPHOTO
COMMON/DPTS/VERSI,TIMEV,VERSA,AREAV,TCON,RHOCON,IPRCOD
COMMON/COND/AREA,MDOT,P,IVAR,V,RHD,T,SIGMA(25),LS,LSP3,NEXT
COMMON/STCOM1/DUM(2),HINT,HMIN,HMAX,EMAX,MF,KFLAG,JSTART
COMMON/NECC/RR,MIXMW,M2,GAMMA,TCPR,R
COMMON/KOUT/ITLE(20),UNIT1,UNITO,CONC,EXCHR,DELH(50),FPS,SI,DBUGO
COMMON/REAC/LSR(4),XX(50),RATE(50),LKEQ(50),DLKEQ(50),MH(50),LR
COMMON/RRAT/A(50),N(50),EACT(50),B(50),M(25,50),ALLM1
COMMON/AFUN/CN(4),ITPSZ,LSUBM,ETA,D,VISC,BETAL
COMMON/SPEC/SNAM(31),MW(25),N(25),STOIC(25,50),OMEGA(25,50)
COMMON/XVA/XTB(60),ATB(40),NTB,XU,AU(2),CX(4)
COMMON/GHSC/GRT(25),HRT(25),SRI(25),CPR(25),DCPR(25)
COMMON/STCS/NSTOIC(4,50),EQUIL(50)

EQUIVALENCE (SPNM,SNAM(4))
EQUIVALENCE (PRX(1),XXH(1))

ENTRY OUT1

C ** TITLE PAGE
  IF (VERSI .EQ. TIMEV) GO TO 98
  I = 2
  GO TO 99
98 I = 4
99 IF (VERSA .EQ. AREAV) I = I - 1
  GO TO (100,200,300,400),I
100 WRITE (6,101)
101 FORMAT (1H1,14X,21HDISTANCE-AREA VERSION)
  GO TO 3
200 WRITE (6,201)
201 FORMAT (1H1,12X,25HDISTANCE-PRESSURE VERSION)
  GO TO 3
300 WRITE (6,301)
301 FORMAT (1H1,16X,17HTIME-AREA VERSION)
  GO TO 3
400 WRITE (6,401)
401 FORMAT (1H1,14X,21HTIME-PRESSURE VERSION)
  3 WRITE (6,102) (TITLE(I),I=1,20)
102 FORMAT(1H,*GENERAL CHEMICAL KINETICS PROGRAM*,9X,*NASA Langley Research Center*/39X,*Langley Version of Lewis Program (TN D-658
26)* USING STIFF ODE*/42X,*SOLUTION TECHNIQUE DEVELOPED BY C.W. GEAR
3 */*26X,20A4,/*5X,*REACTION*,31X,*REACTION*,42X,*REACTION RATE VA
4RIABLES*/6X,*NUMBER*,7BX,LHA,16X,1HN,9X,*ACTIVATION*/119X,*ENERGY*
5)

C PRINT REACTION INFORMATION
  DO 6 J=1,LR
  N1 = LSR(1,J)
  N2 = LSR(2,J)
  N3 = LSR(3,J)
  N4 = LSR(4,J)
  NSTOC2 = -NSTOIC(2,J)
  WRITE(6,103) J,NSTOC2,SPNM(N2),NSTOIC(3,J),SPNM(N3),A(J),N(J),
  EACT(IJ)
103 FORMAT(8X,12,25X,11,1H*,A8,2X,1H=,2X,11,1H*,A8,25X,E12.5,5X,
  * F10.4,5X,F10.2)
  IF (N1 .EQ. NBLANK) GO TO 4
  IF (N1 .LE. LS) GO TO 203
  WRITE(6,105) SPNM(N1)
105 FORMAT(1H+,21X,A8,2X,1H+)
  GO TO 4
203 NSTOC1 = -NSTOIC(1,J)
  WRITE(6,204) NSTOC1,SPNM(N1)
204 FORMAT(1H+,19X,11,1H*,A8,2X,1H+)
  4 IF (N4 .EQ. NBLANK) GO TO 6
  IF (N4 .LE. LS) GO TO 304
  WRITE(6,106) SPNM(N4)
106 FORMAT(1H+,61X,1H+,4X,A8)
  GO TO 6
304 WRITE(6,305) NSTOIC(4,J),SPNM(N4)
305 FORMAT(1H+,61X,1H+,2X,11,1H*,A8)

C   CONVERT ACTIVATION ENERGY TO B-FACTOR
  6 B(IJ) = EACT(IJ)/1.987165

  IF (.NOT. ALLM1) GO TO 7
  WRITE (6,106)
106 FORMAT (//41X,50HALL THIRD BODY RATIOS ARE 1.0)
  GO TO 13

  7 WRITE (6,107)
107 FORMAT (//41X,50HALL THIRD BODY RATIOS ARE 1.0 EXCEPT THE FOLLOWING
  *NG//)
  K = 0
  DO 12 I=1,LS
  DO 12 J=1,LR

```

## APPENDIX B

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IF (M(I,J) .EQ. 1.) GO TO 12
K = K + 1
IF (K .EQ. 5) K = 1
GO TO (8,9,10,11),K
8 WRITE(6,108) SPNM(I),J,M(I,J)
108 FORMAT(5X,2HM(,A8,1H,,I2,3H) =,F10.5)
GO TO 12
9 WRITE(6,109) SPNM(I),J,M(I,J)
109 FORMAT(1H*,36X,2HM(,A8,1H,,I2,3H) =,F10.5)
GO TO 12
10 WRITE(6,110) SPNM(I),J,M(I,J)
110 FORMAT(1H*,68X,2HM(,A8,1H,,I2,3H) =,F10.5)
GO TO 12
11 WRITE(6,111) SPNM(I),J,M(I,J)
111 FORMAT(1H*,100X,2HM(,A8,1H,,I2,3H) =,F10.5)
12 CONTINUE

13 IF (VERSI .EQ. TIMEV) GO TO 14
  WRITE (6,112) HMIN,HMAX,HINT,EMAX
112 FORMAT (//56X,20HINTEGRATION CONTROLS//15X,17HMINIMUM STEP SIZE,
 * E14.5,3H CM,33X,17HMAXIMUM STEP SIZE,E14.5,3H CM//15X,17HINITIAL
 *STEP SIZE,E14.5,3H CM,33X,22HMAXIMUM RELATIVE ERROR,F10.5)
  GO TO 15
14 WRITE (6,113) HMIN,HMAX,HINT,EMAX
113 FORMAT (//56X,20HINTEGRATION CONTROLS//15X,17HMINIMUM STEP SIZE,
 * E14.5,4H SEC,32X,17HMAXIMUM STEP SIZE,E14.5,4H SEC//15X,17HINITIAL
 *L STEP SIZE,E14.5,4H SEC,32X,22HMAXIMUM RELATIVE ERROR,F10.5)

C ** SECOND PAGE
15 WRITE (6,114)
114 FORMAT (1H1,50X,31H** ASSIGNED VARIABLE PROFILE **//)
  GO TO (16,18,19,19,20),ITPSZ

16 GO TO (116,216,316,416),IPRCOD
C ASSIGNED VARIABLE TABLE
116 WRITE (6,117) XU,AU
117 FORMAT (34X,64HTHE AREA IS CALCULATED BY INTERPOLATION FROM THE FO
 *LLOWING TABLE//36X,7HSTATION,10X,17HXIAL DISTANCE (,A2,1H),10X,
 *7HAREA (,A4,A1,1H))
  GO TO 516
216 WRITE (6,217) XU,AU
217 FORMAT (32X,68HTHE PRESSURE IS CALCULATED BY INTERPOLATION FROM TH
 *E FOLLOWING TABLE//36X,7HSTATION,10X,17HXIAL DISTANCE (,A2,1H),
 * 9X,11HPRESSURE (,2A4,1H))
  GO TO 516
316 WRITE (6,317) AU
317 FORMAT (34X,64HTHE AREA IS CALCULATED BY INTERPOLATION FROM THE FO
 *LLOWING TABLE//36X,7HSTATION,14X,11HTIME (SEC),16X,7HAREA (,A4,
 * A1,1H))
  GO TO 516
416 WRITE (6,417) AU
417 FORMAT (32X,68HTHE PRESSURE IS CALCULATED BY INTERPOLATION FROM TH
 *E FOLLOWING TABLE//36X,7HSTATION,14X,11HTIME (SEC),15X,11HPRESSUR
 *E (,2A4,1H))
516 DO 17 I=1,NTB
 17 WRITE (6,616) I,XTB(I),ATB(I)
616 FORMAT (38X,I2,14X,1PE12.5,15X,E12.5)
  GO TO 21

18 GO TO (218,318,418,518),IPRCOD
C ASSIGNED VARIABLE POLYNOMIAL
218 WRITE (6,219) AU,CX
219 FORMAT (40X,52HTHE AREA IS CALCULATED FROM THE FOLLOWING POLYNOMIA
 *L//23X,6HAREA (,A4,A1,5H) = (,1PE12.5,9H)X**3 + (,E12.5,9H)X**2 +
 * (,E12.5,6H)X + (,E12.5,1H))
  GO TO 21
318 WRITE (6,319) AU,CX
319 FORMAT (38X,56HTHE PRESSURE IS CALCULATED FROM THE FOLLOWING POLYN
 *OMIAL//20X,10HPRESSURE (,2A4,5H) = (,1PE12.5,9H)X**3 + (,E12.5,9H)
 *X**2 + (,E12.5,6H)X + (,E12.5,1H))
  GO TO 21
418 WRITE (6,419) AU,CX
419 FORMAT (40X,52HTHE AREA IS CALCULATED FROM THE FOLLOWING POLYNOMIA
 *L//23X,6HAREA (,A4,A1,5H) = (,1PE12.5,9H)T**3 + (,E12.5,9H)T**2 +
 * (,E12.5,6H)T + (,E12.5,1H))
  GO TO 21
518 WRITE (6,519) AU,CX
519 FORMAT (38X,56HTHE PRESSURE IS CALCULATED FROM THE FOLLOWING POLYN
 *OMIAL//20X,10HPRESSURE (,2A4,5H) = (,1PE12.5,9H)T**3 + (,E12.5,9H)
 *T**2 + (,E12.5,6H)T + (,E12.5,1H))
  GO TO 21

C SPECIAL AREA FUNCTION
19 WRITE (6,118) LSUBM,ETA
118 FORMAT (41X,50HTHE AREA IS CALCULATED FROM THE FOLLOWING FUNCTION/
 *46X,16H/AREA = 1 - (X/F10.3,4H)***(F10.5,1H))
  IF (ITPSZ .EQ. 4) WRITE (6,1118) D,VISC,BETAL
1118 FORMAT (//6X,20HHYDRAULIC DIAMETER =,F8.4,3H CM,7X,23HVISCOSITY COE
 *FFICIENT =,E12.4,10H GM/CM-SEC,7X,6HΒΕΤΑ =,F7.4)
  GO TO 21

C ZERO VELOCITY - ASSIGNED VARIABLE NOT REQUIRED
20 WRITE (6,119)
119 FORMAT (36X,60HTHIS IS A V=0 PROBLEM - AN ASSIGNED VARIABLE IS NOT
 * REQUIRED)
  GO TO 21

21 CONTINUE

```

## APPENDIX B

```

228 IF (RHOCON) WRITE (6,1126)
1126 FORMAT (//38X,56HTHE VOLUME (DENSITY) WILL BE HELD CONSTANT FOR T
 *HIS CASE)
   IF (TCON) WRITE (6,2126)
2126 FORMAT (//40X,51HTHE TEMPERATURE WILL BE HELD CONSTANT FOR THIS C
 *ASE)
   RETURN

   ENTRY OUT2

C   INITIAL CONDITIONS
   WRITE (6,127)
127 FORMAT (1H1,52X,26H** INITIAL CONDITIONS **//)
   GO TO 29

   ENTRY OUT3

C   GENERAL OUTPUT
   WRITE (6,128)
128 FORMAT (1H1)

29 MACH = SQRT(M2)
MAX = MAX0(LS,LR)

TENT = 0.
CSUM = 0.
PMLOG = ALOG(P*MIXMW)
C   TOTAL ENTRUPY AND MASS FRACTION SUM
DO 30 I=1,L5
IF(SIGMA(I) .LE. 0.) GO TO 30
TENT = TENT + SIGMA(I)*(SR(I)) - ALOG(SIGMA(I)) - PMLOG
30 CSUM = CSUM + SIGMA(I)*MW(I)
TENT = TENT*1.987165

TXMH = 0.
C   ENERGY EXCHANGE RATES
DO 31 J=1,LR
XXH(JJ) = XX(JJ)*DELH(J)
31 TXMH = TXMH + XXH(JJ)

IF (IVERSI .EQ. TIMEV) GO TO 32
TIME = DVAK
X = IVAR
GO TO 33
32 TIME = IVAR
X = DVAR

33 IF (UNIT0 .NE. FPS) GO TO 48

C   CONVERT FROM INTERNAL (CGS) UNITS TO FPS UNITS
X = X/30.48
AREAA = AREA/929.0304
DDTM = MDT/453.59237
PP = P*2116.2
VV = V/30.48
RHOO = RHO*62.43
TT = T*1.8

WRITE(6,129) TIME,AREAA,X,PP,     VV,      RHOO,
* TT,OUTM,TENT,      MACH,GAMMA
129 FORMAT(16X,*TIME*,E14.5,* SEC*,14X,*AREA*,E14.5,* SQ FT*,
1 14X,*AXIAL POSITION*,E14.5,* FT//20X,*FLOW PROPERTIES*,45X,
2 *INTEGRATION INDICATORS*/22X,*PRESSURE*,E22.5,30X,
3 *STEPS FROM LAST PRINT*,13X/23X,* (LB/FT-21)*22X,*VELOCITY*,
4 E22.5,30X,*AVERAGE STEP SIZE*/23X,* (FT/SEC)*22X,*DENSITY*,
5 E22.5,30X,*CONTROLLING VARIABLE*/23X,* (LB/FT-31)*
6 22X,*TEMPERATURE*,E19.5/23X,* (DEG R)*22X,*MASS FLOW RATE*,
7 E16.5/23X,* (LB/SEC)*22X,*ENTROPY*,E23.5,30X,*RELATIVE ERROR*/
8 23X,* (BTU/LB/DEG R)*22X,*MACH NUMBER*,E19.5//22X,*GAMMA*,E25.5)

34 WRITE (6,131)
131 FORMAT (//56X,19HCHEMICAL PROPERTIES//)

CONV = 0.02883
IF (ICONC .OR. EXCHR) GO TO 36

C   PRINT MASS FRACTIONS AND REACTION CONVERSION RATES
   WRITE (6,132)
132 FORMAT (1X,7HSPECIES,4X,13HMASS FRACTION,3X,13HMOLE FRACTION,3X,
* 27HNET SPECIES PRODUCTION RATE,5X,8HREACTION,3X,28HNET REACTION C
*ONVERSION RATE,2X,14HNET RATE/POSI-)
   WRITE (6,133)
133 FORMAT (50X,16H(MOLE/FT**3/SEC),11X,6HNUMBER,7X,22H(MOLE-FT**3/LB
**2/SEC),6X,13HTIVE DIR RATE)
   DO 35 J=1,LR
35 PRX(JJ) = XX(JJ)
CONV = 1./62.43
GO TO 37

36 IF (ICONC .OR. (.NOT. EXCHR)) GO TO 39

C   PRINT MASS FRACTIONS AND ENERGY EXCHANGE RATES
   WRITE (6,134)
134 FORMAT (1X,7HSPECIES,4X,13HMASS FRACTION,3X,13HMOLE FRACTION,3X,
* 27HNET SPECIES PRODUCTION RATE,5X,8HREACTION,5X,24HNET ENERGY EXC
*HANGE RATE,4X,14HNET RATE/POSI-)
   WRITE (6,135)

```

## APPENDIX B

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135 FORMAT (50X,16H(MOLE/FT**3/SEC),11X,6HNUMBER,8X,21H(BTU-FT**3/LB**
 *2/SEC),6X,13HTIVE DIR RATE)

C COMPUTE MASS FRACTIONS
37 DO 38 I=1,LS
38 PRC(I) = SIGMA(I)*MW(I)
GO TO 44
39 IF (.NOT. CONC .OR. EXCHR) GO TO 41

C PRINT MOLAR CONCENTRATIONS AND REACTION CONVERSION RATES
WRITE (6,136)
136 FORMAT (1X,7HSPECIES,4X,13HCCONCENTRATION,3X,13HMOLE FRACTION,3X,
 * 27HNET SPECIES PRODUCTION RATE,5X,8HREACTION,3X,28HNET REACTION C
 *ONVERSION RATE,2X,14HNET RATE/POSI-)
WRITE (6,137)
137 FORMAT (12X,13H(MOLES/FT**3),25X,16H(MOLE/FT**3/SEC),11X,6HNUMBER,
 * 7X,22H(MOLE-FT**3/LB**2/SEC),6X,13HTIVE DIR RATE)
DO 40 J=1,L
40 PRX(J) = XX(J)
CONV = 1./62.43
GO TO 42

C PRINT MOLAR CONCENTRATIONS AND ENERGY EXCHANGE RATES
41 WRITE (6,138)
138 FORMAT (1X,7HSPECIES,4X,13HCCONCENTRATION,3X,13HMOLE FRACTION,3X,
 * 27HNET SPECIES PRODUCTION RATE,5X,8HREACTION,5X,24HNET ENERGY EXC
 *HANGE RATE,4X,14HNET RATE/POSI-)
WRITE (6,139)
139 FORMAT (12X,13H(MOLES/FT**3),25X,16H(MOLE/FT**3/SEC),11X,6HNUMBER,
 * BX,21H(BTU-FT**3/LB**2/SEC),6X,13HTIVE DIR RATE)

C COMPUTE MOLAR CONCENTRATIONS
42 DO 43 I=1,LS

43 PRC(I) = SIGMA(I)*RHOO
44 DO 47 IJ=1,MAX
IF (IJ .GT. LS .OR. IJ .LT. LR) GO TO 45
FMOL = SIGMA(IJ)*MIXMH
WW = W(IJ)*62.43
XXX = PRX(IJ)*CONV
WRITE(6,140) SPNM(IJ),PRC(IJ),FMOL,WW,IJ,XXX,EQUIL(IJ)
140 FORMAT(2X,A8,2X,E12.5,E16.5,7X,E16.5,15X,I3,10X,E16.5,7X,E16.5)
GO TO 47
45 IF (IJ .GT. LS) GO TO 46
FMOL = SIGMA(IJ)*MIXMW
WW = W(IJ)*62.43
WRITE(6,141) SPNM(IJ),PRC(IJ),FMOL,WW
141 FORMAT(2X,A8,2X,E12.5,E16.5,7X,E16.5)
GO TO 47
46 XXX = PRX(IJ)*CONV
WRITE (6,142) IJ,XXX,EQUIL(IJ)
142 FORMAT(78X,13,10X,E16.5,7X,E16.5)
47 CONTINUE
TXMH = TXMH*0.02883
WRITE (6,143) MIXMH,TXMH,CSUM
143 FORMAT ( /4X,24HMIXTURE MOLECULAR WEIGHT,F13.5,5X,26HTOTAL ENERGY
 *EXCHANGE RATE,1PE15.5,7X,17HMASS FRACTION SUM,OPF14.8)
WRITE (6,144)
144 FORMAT (49X,21H(BTU-FT**3/LB**2/SEC))
GO TO 78

48 IF (UNIT0 .NE. SII) GO TO 63

C CONVERT FROM INTERNAL (CGS) UNITS TO SI UNITS
X = X*.01
AREAA = AREA*.0001
DOTM = MDOT*0.001
PP = P*1.01325E+05
VV = V*.01
RHOO = RH0*1000.
TENT = TENT*4184.0

WRITE(6,145) TIME,AREAA,X,PP, VV, RHOO,
 * TIME,DDOT,TENT, MACH,GAMMA
145 FORMAT(16X,*TIME*,E14.5,* SEC*,14X,*AREA*,E14.5,* SQ M*,
 1 14X,*AXIAL POSITION*,E14.5,* M */20X,*FLOW PROPERTIES*,45X,
 2 *INTEGRATION INDICATORS*/22X,*PRESSURE*,E22.5,30X,
 3 *STEPS FROM LAST PRINT*,13X/23X,*N/M-2 *)/22X,*VELOCITY*,
 4 E22.5,30X,*AVERAGE STEP SIZE*/23X,* (M/SEC )/22X,*DENSITY*,
 5 E23.5,30X,*CONTROLLING VARIABLE*/23X,* (KG/M-3 )*/,
 6 22X,*TEMPERATURE*,E19.5/23X,* (DEG K)*/22X,*MASS FLOW RATE*,
 7 E16.5/23X,* (KG/SEC)*/22X,*ENTROPY*,E23.5,30X,*RELATIVE ERROR*,
 8 23X,* (J/DOULE/(KG-K))*/22X,*MACH NUMBER*,E19.5//22X,*GAMMA*,E25.5)

49 WRITE (6,131)

CONV = 4.1840
IF (CONC .OR. EXCHR) GO TO 51

C PRINT MASS FRACTIONS AND REACTION CONVERSION RATES
WRITE (6,132)
132 FORMAT (1X,7HSPECIES,4X,13HMNUMBER,7X,21H(MOLE-M**3/KG**2
 */SEC),7X,13HTIVE DIR RATE )
DO 50 J=1,L
50 PRX(J) = XX(J)
CONV = 0.001
GO TO 52

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## APPENDIX B

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51 IF (CONC .OR. (.NOT. EXCHR)) GO TO 54
C   PRINT MASS FRACTIONS AND ENERGY EXCHANGE RATES
    WRITE (6,136)
    WRITE (6,147)
147 FORMAT (50X,15H(MOLE/M**3/SEC),12X,6HNUMBER,7X,22H(JOULE-M**3/KG**2/SEC),6X,13HTIVE DIR RATE)
C   COMPUTE MASS FRACTIONS
52 DO 53 I=1,LS
53 PRC(I) = SIGMA(I)*MW(I)
GO TO 59

54 IF ((.NOT. CONC) .OR. EXCHR) GO TO 56
C   PRINT MOLAR CONCENTRATIONS AND REACTION CONVERSION RATES
    WRITE (6,136)
    WRITE (6,148)
148 FORMAT (12X,12H(MOLES/M**3),26X,15H(MOLE/M**3/SEC),12X,6HNUMBER,7X
      *,21H(MOL-E-M**3/KG**2/SEC),7X,13HTIVE DIR RATE)
    DO 55 J=1,LR
55 PRX(IJ) = XX(J)
    CONV = 0.001
GO TO 57

C   PRINT MOLAR CONCENTRATIONS AND ENERGY EXCHANGE RATES
56 WRITE (6,138)
    WRITE (6,149)
149 FORMAT (12X,12H(MOLES/M**3),26X,15H(MOLE/M**3/SEC),12X,6HNUMBER,7X
      *,22H(JOULE-M**3/KG**2/SEC),6X,13HTIVE DIR RATE)

C   COMPUTE MOLAR CONCENTRATIONS
57 DO 58 I=1,LS

58 PRC(I) = SIGMA(I)*RHOD
59 DO 62 IJ=1,MAX
  IF (IJ .GT. LS) .OR. IJ .GT. LR) GO TO 60
  FMOL = SIGMA(IJ)*MIXMH
  WW = W(IJ)*1000.
  XXX = PRX(IJ)*CCNV
  WRITE(6,140) SPNM(IJ),PRC(IJ),FMOL,WW,IJ,XXX,EQUIL(IJ)
  GO TO 62
60 IF (IJ .GT. LS) GO TO 61
  FMOL = SIGMA(IJ)*MIXMH
  WW = W(IJ)*1000.
  WRITE(6,141) SPNM(IJ),PRC(IJ),FMOL,WW
  GO TO 62
61 XXX = PRX(IJ)*CCNV
  WRITE (6,142) IJ,XXX,EQUIL(IJ)
62 CONTINUE
  TXMH = TXMH*4.1840
  WRITE (6,143) MIXMH,TXXH,CSUM
  WRITE (6,150)
150 FORMAT (48X,22H(JOULE-M**3/KG**2/SEC))
  GO TO 78

C   PRINT OUTPUT IN INTERNAL (CGS) UNITS
63 WRITE(6,151) TIME,AREA,X,P, V, RHO,
  * T,MDOT,TENT,
  * MACH,GAMMA
151 FORMAT(16X,*TIME*,E14.5,* SEC*,*AREA*,E14.5,* SQ CM*,*
  14X,*AXIAL POSITION*,E14.5,* CM//20X,*PRESSURE,ATM   *=,
  2 F22.4,20X,*VELOCITY,CM/SEC *=,F22.2//20X,*DENSITY,GM/CC  *=,
  3 E22.5,20X,*TEMPERATURE,K *=,F22.5//20X,*FLOW RATE,GM/SEC *=,
  4 E22.5,20X,*ENTRCFY,CAL/GM-K *=,F22.5//20X,*MACH NUMBER *=,
  5 F22.5,20X,*GAMMA   *=,F22.5)

64 WRITE (6,131)
  IF(.NOT. DEBUG) GO TO 700
  IF (CONC .OR. EXCHR) GO TO 66

C   PRINT MASS FRACTIONS AND REACTION CONVERSION RATES
    WRITE (6,132)
    WRITE (6,152)
152 FORMAT (50X,16H(MOLE/CM**3/SEC),11X,6HNUMBER,7X,22H(MOLE-CM**3/GM**2/SEC),6X,13HTIVE DIR RATE)
    DO 65 J=1,LR
65 PRX(IJ) = XX(J)
GO TO 67
66 IF (CONC .OR. (.NOT. EXCHR)) GO TO 69

C   PRINT MASS FRACTIONS AND ENERGY EXCHANGE RATES
    WRITE (6,134)
    WRITE (6,153)
153 FORMAT (50X,16H(MOLE/CM**3/SEC),11X,6HNUMBER,8X,21H(CAL-CM**3/GM**2/SEC),6X,13HTIVE DIR RATE)

C   COMPUTE MASS FRACTIONS
67 DO 68 I=1,LS
68 PRC(I) = SIGMA(I)*MW(I)
GO TO 74

69 IF ((.NOT. CONC) .OR. EXCHR) GO TO 71
C   PRINT MOLAR CONCENTRATIONS AND REACTION CONVERSION RATES
    WRITE (6,136)
    WRITE (6,154)
154 FORMAT (12X,13H(MOLES/CM**3),25X,16H(MOLE/CM**3/SEC),11X,6HNUMBER,
      * 7X,22H(MOLE-CM**3/GM**2/SEC),6X,13HTIVE DIR RATE)
    DO 70 J=1,LR

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## APPENDIX B

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70 PRX(J) = XX(J)
GO TO 72

C   PRINT MOLAR CONCENTRATIONS AND ENERGY EXCHANGE RATES
71 WRITE(6,138)
    WRITE(6,155)
155 FORMAT(12X,13H(MOLES/CM**3),25X,16H(MOLE/CM**3/SEC),11X,6HNUMBER,
      * 8X,21H(CAL-CM**3/GM**2/SEC),6X,13HTIVE DIR RATE)

C   COMPUTE MOLAR CONCENTRATIONS
72 DO 73 I=1,LS
73 PRC(I) = SIGMA(I)*RHO
    PROD = PRC(I) * PRC(3)

74 DO 77 IJ=1,MAX
    IF (IJ .GT. LS .CR. IJ .GT. LR) GU TO 75
    FMOL = SIGMA(IJ)*MIXMW
    WRITE(6,140) SPNM(IJ),PRC(IJ),FMOL,W(IJ),IJ,PRX(IJ),EQUIL(IJ)
    GU TO 77
75 IF (IJ .GT. LS) GO TO 76
    FMOL = SIGMA(IJ)*MIXMW
    WRITE(6,141) SPNM(IJ),PRC(IJ),FMOL,W(IJ)
    GU TO 77
76 WRITE(6,142) IJ,PRX(IJ), EQUIL(IJ)
77 CONTINUE
GO TO 705
700 CONTINUE
    WRITE(6,701)
701 FURMAT(1X,*SPECIES*,4X,*MASS FRACTION*,3X,*MOLE FRACTION*,3X,
  1 *MOLAR CONCENTRATION*,3X,* SIGMA *,3X,*NET SPECIES PRODUCT*
  20N RATE*)
    WRITE(6,702)
702 FURMAT(47X,* (MOLES/CM--3)*,6X,* (MOL(I)/MASS)*,7X,* (MOLES/CC-SEC)*)
DO 703 I=1,LS
    FMOL = SIGMA(I)*MIXMW
    PRC(I)=SIGMA(I)*RHO
    PRCF = SIGMA(I)*MW(I)
    WRITE(6,704) SPNM(I),PRCF,FMOL,PRC(I),SIGMA(I),W(I)
704 FURMAT(2X,A8,2X,E12.5,E16.5,7X,E12.5,7X,E12.5,9X,E12.5)
703 CONTINUE
    PROD = PRC(I)*PRC(3)
    DCOU = PRC(3)*W(1) + PRC(1)*W(3)
    IF(SPNM(1) .NE. 8FCG ) GO TO 705
    WRITE(6,706) DCOU
706 FORMAT(3X,* (D)XC(CO) + (CO)XD(D) = *,E15.5)
705 CONTINUE
    WRITE(6,2000) PROD
2000 FURMAT(3X,6DH PRODUCT OF SPECIES 1 AND SPECIES 3 MOLAR CONCENTRAT
  *IONS = 1PE12.5/ )
    WRITE(6,163) MIXMW,TXXM,CSUM
    WRITE(6,156)
156 FURMAT(49X,21H(CAL-CM**3/GM**2/SEC))
    WRITE(6,159) TDERV
159 FURMAT(/5X,*DTMP/DIVAR = *,E16.5)

78 CONTINUE

82 IF (ABS(1.-CSUM) .LE. .001) RETURN
    WRITE(6,163)
163 FORMAT(7HO(OUTP),5X,19HINVALID COMPOSITION)
    NEXT = .TRUE.
    RETURN

END

```

SUBROUTINE DIFFUN(NI, TI, Y, YDOT, IFN, NPEDV, K2)

C PERFORM ALL NECESSARY PRE-DERIVATIVE CALCULATIONS

```

LOGICAL ALLMI,TCON,NEXT,RHOCON
LOGICAL KTCON
LOGICAL KUP

INTEGER STOIC

REAL IVAR,MDDOT,LKEQ,MM,N,M,MIXMW,M2
DIMENSION Y(NI,K2),YDOT(56)

COMMON/DERV3/TDERV
COMMON/STCMB/TPREV,HNI
COMMON/STCON9/KTCON
COMMON/CONT/KTCON
COMMON/UPDT/KUP
COMMON/LTUS/LTHM,LJAT,NTHRD,NBLANK,NPHOTO
COMMON/OPTS/VERSI,TIMEV,VERSA,AREAV,TCON,RHOCON,IPRCOD
COMMON/COND/DVAR,AREA,MDDOT,P,IVAR,V,RHO,T,SIGMA(25),LS,LSP3,NEXT
COMMON/SPEC/SNAM(31),MW(25),W(25),STOIC(25,50),OMEGA(25,50)
COMMON/REAC/LSR(6,50),XX(50),RATE(50),LKEQ(50),DLKEO(50),MM(50),LR
COMMON/RRAT/A(50),V(50),EACT(50),B(50),M(25,50),ALLMI
COMMON/GHSC/GRT(25),HRT(25),SR(25),CPR(25),DCPR(25)
COMMON/NECC/RR,MIXMW,M2,GAMMA,TCPR,R
COMMON/STCS/NSTOIC(4,50),EQUIL(50)
COMMON/SNO8/CXTB(40),CATB(40),NZ
COMMON/DERN/F(28)

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## APPENDIX B

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COMMON/SARC/S1,S2,AA,BB,TERM
EQUIVALENCE (DV,F(1))
DZADT?D2) = V*V*D2 + DV/V*DA
DZADY?D2) = (D2/V - DV*DA)/V

I*RHO = 0
V=Y(1)
RHO=Y(2)
T=Y(3)
NN 200 I=1,LS
II=I+3
SIGMA(I)=Y(II)
200 CONTINUE
IF(KTCOM) GO TO 400
ENTRY DIFF1
IF (TCOM) GO TO 5
400 CONTINUE
MWARN = 0
C   THERMODYNAMIC PROPERTIES
    CALL THRM (T,1.)
ALOGRT = ALOG(RR*T)
NN 4 J=1,LP
C   REACTION RATE CONSTANT
RATE(J) = A(J)*T**N(J)*EXP(-B(J)/T)

C   LN KFO AND D(LN KFO)/DT
DELSTC = 0.
DELG = 0.
DELH = 0.
NN 2 I=1,A
NN = LSP(I,J)
TF (NN .GT. LS) GO TO 2
STOC = NSTOC(I,J)
DELSTC = DELSTC + STOC
DELG = DELG + STOC*GRT(NN)
DELH = DELH + STOC*HRT(NN)
2 CONTINUE
LKFO(IJ) = -DELG - DELSTC*ALOGRT
NLKFO(IJ) = (DELH - DELSTC)/T
4 CONTINUE

C   MIXTURE MOLECULAR WEIGHT
5 DPL = 0.
NN 6 I=1,LS
6 DPL = DPL + SIGMA(I)
SSUM = DPL
MTMMW = 1./SSUM

C   ***** UPDATE INDEPENDENT AND DEPENDENT VARIABLES
TF(KUP) GO TO 600
TVAR = TI
600 CONTINUE
IF(VERS1 .EQ. TIMEV) GO TO 700
Y = TVAR
TF(KTCOM) TIME = DVAR
IF(.NOT. KUP) .AND. (.NOT. KTCOM) TIME=DVAR+2.*((TI-TPREV)/(VOLD+
Y(1)))
IF(KUP) TIME = DVAR
GO TO 701
700 CONTINUE
TIME = TVAR
TF(KTCOM) X = DVAR
TF(.NOT. KUP) .AND. (.NOT. KTCOM) X=DVAR+(TI-TPEV)*(VOLD+Y(1))
1/2.
IF(KUP) X = DVAR
701 CONTINUE
C   ASSIGNED VARIABLE
IF (TPPCON .GT. 2) GO TO 7
CALL CINPIC(XTB,CATB,NZ,X,AVAR,DA,DZA)
GO TO 8
7 CONTINUE
CALL CINPIC(XTB,CATB,NZ,TIME,AVAR,DA,DZA)

C   CALCULATED VARIABLE
8 IF (VERSA .EQ. AREAV) GO TO 9
P = AVAP
IF (V .NE. 0.) AREA = MDOT/(RHO*V)
GO TO 10
9 AREA = AVAP
P = RHO*PD*T/MIXMW
C   MASS FLOW RATE
MDOT = P*AREA*V
10 NN 20 J=1,LR
N1 = LSP(I,J)
N2 = LSQ(I,J)
N3 = LSQ(3,J)
N4 = LSQ(4,J)

IF (N1 .EQ. NPHOTO) GO TO 15
C   THRD BODY FACTOR
MM(I) = 0.
IF (N1 .NE. NTHRD .AND. N4 .NE. NTHRD) GO TO 12
IF (ALLMI) GO TO 12
NN 11 I=1,LS
11 MM(I) = PM(I) + M(I,J)*SIGMA(I)
GO TO 13

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## APPENDIX B

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12 MM(J) = SSUM
13 IF (LKEQ(J) .GT. 0.) GO TO 14
  EXP3 = EXP(-LKEQ(J)/3.)
  EXP1 = RATE(J)*EXP3
  GO TO 15
14 EXP1 = EXP(ALOG(RATE(J)) - LKEQ(J))
  EXP3 = 1.

C   NET REACTION CONVERSION RATE
15 SIGMA1 = 0.
  IF (N1 .LE. LS) SIGMA1 = SIGMA(N1)
  SIGMA4 = 0.
  IF (N4 .LE. LS) SIGMA4 = SIGMA(N4)
  NC = -(NSTOIC(1,J) + NSTOIC(2,J)) - 2
  DP1 = POWER(RHO,NC)*RATE(J)*POWER(SIGMA1,-NSTOIC(1,J))*  

* POWER(SIGMA(N2),-NSTOIC(2,J))
  IF (N1 .EQ. NPHOTO) GO TO 18
  NC = (NSTOIC(3,J) + NSTOIC(4,J)) - 2
  DP2 = EXP3*POWER(RHO,NC)*EXP3*POWER(SIGMA(N3),NSTOIC(3,J))*  

* POWER(SIGMA4,NSTOIC(4,J))*EXP1
  XX(J) = DP1 - DP2
  IF (N1 .EQ. NTHRD) .OR. N4 .EQ. NTHRDJ XX(J) = MM(J)*RHO*XX(J)
  IF (XX(J).NE. 0.) GO TO 29
  EQUIL(J) = 0.
  GO TO 20
29 IF (XX(J).LT. 0.) GO TO 30
  EQUIL(J) = XX(J)/DP1
  IF (N1 .EQ. NTHRD) .OR. N4 .EQ. NTHRDJ EQUIL(J)=EQUIL(J)/(MM(J)*RHO)
  GO TO 20
30 EQUIL(J) = ABS(XX(J)/DP2)
  IF (N1 .EQ. NTHRD) .OR. N4 .EQ. NTHRDJ EQUIL(J)=EQUIL(J)/(MM(J)*RHO)
  GO TO 20
18 XX(J) = DP1
  EQUIL(J) = 1.0
20 CONTINUE

  RHO2 = RHO*RHO
  TCPR = 0.
  DO 22 I=1,LS

C   TOTAL CP/R
C   NET SPECIES PRODUCTION RATE
  TCPR = TCPR + CPR(I)*SIGMA(I)
  DP1 = 0.
  DO 21 J=1,LR
    STOC = STOIC(I,J)
    OMEGA(I,J) = RHO2*STOC*XX(J)
21 DP1 = DP1 + OMEGA(I,J)
  W(I) = DP1
22 CONTINUE

C   GAMMA (FROZEN)
  GAMMA = TCPR/(TCPR - 1./MIXMW)

C   MACH NUMBER SQUARED
  M2 = V/R*/V/T*MIXMW/GAMMA

  IF (VERSA .NE. AREAV .OR. (M2 .LT. 0.9025 .OR. M2 .GT. 1.1025))  

* GO TO 23
  WMACH = SQRT(M2)
  WRITE (6,101) WMACH
101 FORMAT (7HO(PRED),5X,7HWARNING,3X,13HMACH NUMBER =,F8.4,19H IS APP  

*ROACHING 1.0)
  MWARN = MWARN + 1
  IF (MWARN .LT. 5) GO TO 23
  WRITE (6,102)
102 FORMAT (7HO(PRED),5X,24H5 WARNINGS HAVE OCCURRED)
  NEXT = .TRUE.
  RETURN

23 CONTINUE
C   COMPUTE DERIVATIVES WRT THE INDEPENDENT VARIABLE
C

  DPS1 = 0.
  DPS2 = 0.
  DO 1 I=1,3
    F(I) = 0.
1 CONTINUE

  DENM = RHO
  IF (VERSI .NE. TIMEV) DENM = RHO*V
  DO 50 I=1,LS

C   DSIGMA/DIVAR
    II = I + 3
    F(II) = W(II)/DENM

C   S1 FOR AA
    DPS1 = DPS1 + F(II)
C   S2 FOR BB
50 DPS2 = DPS2 + HRT(I)*F(II)

  S1 = MIXMW*DPS1
  S2 = MIX4W*DPS2

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## APPENDIX B

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C      GAM1 = GAMMA - 1.
C      RB FOR DERIVATIVES
C      BB = GAM1/GAMMA*S2
C
C      AA FOR DERIVATIVES
C      AA = S1 - RB
C
C      DAVAP/DIVAP
C      IF (VEPSI .EQ. TIMEV .AND. IPRCOD .LE. 2) DA = V*DA
C      IF (VEPSI .NE. TIMEV .AND. IPRCOD .GE. 3) DA = DA/V
C
C      T(VERSAL .NE. AREA) GO TO 51
C      ASSIGNED AREA EQUATIONS
C      ED = GAM1*(S2 - S1)
C      TF (RHOCON .AND. V .LEQ. 0. .AND. .NOT. TCON) IRHO = 2
C      DTERM = DA/AREA - AA
C      T1 = 1./((ED + 1.)*
C      T2 = 42*T1
C
C      DIV/DIVAP
C      F(1) = V*T1*DTERM
C
C      DPHD/DIVAP
C      IF (.NOT. PHOCON) F(2) = -RHO*(T2*DTERM + AA)
C
C      DT/DIVAP
C      IF (.NOT. TCON) F(3) = -T*(GAM1*T2*DTERM + BB)
C      IF (RHO .EQ. 2) F(3) = -T*ED
C
C      DARFA/DIVAP WRT IVAR
C      IF (VEPSI .EQ. TIMEV .AND. (IPRCOD .EQ. 1 .AND. V .NE. 0.)) D2A =
C      * D2ADT2(D2A)
C      IF (VEPSI .NE. TIMEV .AND. IPRCOD .EQ. 3) D2A = D2ADX2(D2A)
C
C      T3 = (D2A - DA*DA/AREA)/AREA
C      GO TO 52
C      ASSIGNED PRESSURE EQUATIONS
C      S1 DTERM = DA/P
C      T2 = -1./GAMMA
C
C      DV/DIVAP
C      IF (V .NE. 0.) F(1) = -DA/(RHO*V)*1.01325E+06
C
C      DPHD/DIVAP
C      IF (.NOT. PHOCON) F(2) = -RHO*(T2*DTERM + AA)
C
C      DT/DIVAP
C      IF (.NOT. TCON) F(3) = -T*(GAM1*T2*DTERM + BB)
C
C      DP/DIVAP WRT IVAR
C      IF (VEPSI .EQ. TIMEV .AND. IPRCOD .EQ. 2) D2A = D2ADT2(D2A)
C      IF (VEPSI .NE. TIMEV .AND. IPRCOD .EQ. 4) D2A = D2ADX2(D2A)
C
C      T3 = (D2A - DA*DA/P)/P
C
52 CONTINUE
      TDFPV = F(3)
      IEF(KID) RETURN
      DO 500 I=1,LSP3
      IT=I+IFN
      YDT(I)=F(I)
500 CONTINUE
      RETURN
      END

      SUBROUTINE PEDERVINO(TO,Y,BETA,NO,NPEDV,K2)
C
C      COMPUTE ALL MIXED PARTIAL DERIVATIVES
C
      LOGICAL TCON,RHOCON
C
      INTEGER STCIC
C
      REAL LKE0,MM,N,M,MIXMN,42
      REAL MMPPD0
C
      DIMENSION PXXRH0(50),PXXT(50),PXXSIG(50,25),PGSIG(25),PM2SIG(25),
      * PSISIG(25),PS2SIG(25),PAASIG(25),PRHSIG(25)
      DIMENSION BFTAIN(PEDV),VPEFV,Y(Y0,Y2)
      COMMON//SAHS/S1,S2,A1,BB,UTERM
      COMMON//LTUS/LDAT,NTMPD,NBLANK,NPHOTC
      COMMON//RPTS/RSI,TIMEV,VERSA,AREA,V,RCN,RHOCON,IPRCOD
      COMMON//CDND/IVAR,AREAV,MDOT,P,IVAR,V,RHO,T,SIGMA(25),S,LSP3,NEXT
      COMMON//SPEC/SNAM(31),W(25),W(25),STOC(25,50),OMEGA(25,50)
      COMMON//RAC(LSK(4,50),X(50),RATE(50),LKE0(50),ULKE0(50),MM(50),LR
      COMMON//RRAT/A(50),NISU),FACT(50),U(50),M(25,50),ALLM1
      COMMON//G4SC/GRT(25),PRT(25),SR(25),CPR(25),DCPR(25)
      COMMON//NECC/29,MIXMN,42,GAMMA,TCPR,R
      COMMON//DERN/F(28)
      COMMON//STC3/NSTD(14,50),FQUIL(50)
      V=Y(1)
      RHO=Y(2)
      T=Y(3)
      DO 50 I=1,LSP3

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## APPENDIX B

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      IT=I+3
      SIGMA(I)=Y(II)
50  CONTINUE
      DO 1 I=1,LSP3
      DO 1 K=1,LSP3
      1 RETA(I,K) = 0.

      IRHO = 0
      IF(RHODCN .AND. V .EQ. 0. .AND. .NOT. TCON) IRHO = 2
      DO 2 J=1,L
      DO 2 I=1,L
      2 PXXSTG(J,I) = 0.

C     XX(J) WRT RHO,T,SIGMA(I)
      DO 9 J=1,L
      N1 = LSR(1,J)
      N2 = LSP(2,J)
      N3 = LSR(3,J)
      N4 = LSR(4,J)

      TF (N1 .EQ. NPHOTO) GO TO 7
      TF (LKF0(J) .GT. 0.) GO TO 3
      EXP3 = FXP1-LKEQ(J)/3.
      EXP1 = RATE(J)*EXP3
      GO TO 4
3    EXP1 = EXP(ALOG(RATE(J)) - LKEQ(J))
      EXP3 = 1.

4    SIGMA1 = 0.
      IF (N1 .LE. LS) SIGMA1 = SIGMA(N1)
      SIGMA4 = 0.
      IF (N4 .LE. LS) SIGMA4 = SIGMA(N4)
      NPI = -(NSTOIC(1,J) + NSTOIC(2,J)) - 2
      C1 = NC1
      NC2 = (NSTOIC(3,J) + NSTOIC(4,J)) - 2
      C2 = NC2
      PXXPHD(J) = C1*POWER(RHO,NC1-1)*RATE(J)*POWER(SIGMA1,-NSTOIC(1,J))
      * POWER(SIGMA(N2),-NSTOIC(2,J)) - C2*EXP3*POWER(RHO,NC2-1)*EXP3*
      * POWER(SIGMA(N3),NSTOIC(3,J))*POWER(SIGMA4,NSTOIC(4,J))*EXP1
      PXXT(J) = EXP3*POWER(RHO,NC2)*EXP3*POWER(SIGMA(N3),NSTOIC(3,J))*
      * POWER(SIGMA4,NSTOIC(4,J))*EXP1*LKEQ(J)
      IF (N1 .LE. LS) PXXSIG(J,N1) = FLOAT(-NSTOIC(1,J))*POWER(RHO,NC1)*
      * PATE(J)*POWER(SIGMA1,-NSTOIC(1,J)-1)*POWER(SIGMA(N2),-NSTOIC(2,J))
      * PATE(J)
      PXXSIG(J,N2) = FLOAT(-NSTOIC(2,J))*POWER(SIGMA(N1),-NSTOIC(1,J))
      * PATE(J)
      PXXSIG(J,N3) = -FLOAT(STOIC(N3,J))*EXP3*POWER(RHO,NC2)*EXP3*
      * POWER(SIGMA(N3),NSTOIC(3,J)-1)*POWER(SIGMA4,NSTOIC(4,J))*EXP1
      IF (N4 .LE. LS) PXXSIG(J,N4) = -FLOAT(STOIC(N4,J))*EXP3*POWER(RHO,
      * NC2)*EXP3*POWER(SIGMA(N3),NSTOIC(3,J))*POWER(SIGMA4,
      * NSTOIC(4,J)-1)*EXP1
      IF (N1 .EQ. NTHRD) GO TO 8
      IF (N4 .EQ. NTHRD) GO TO 8
      GO TO 9

7    NC1 = -NSTOIC(2,J) - 2
      C1 = NC1
      PXXPHD(J) = C1*POWER(RHO,NC1-1)*RATE(J)*POWER(SIGMA(N2),
      * -NSTOIC(2,J))
      PXXT(J) = 0.
      PXXSTG(J,N2) = FLOAT(-NSTOIC(2,J))*POWER(RHO,NC1)*RATE(J)*
      * POWER(SIGMA(N2),-NSTOIC(2,J)-1)
      GO TO 9

8    MMRHO = MM(J)*RHO
      PXXPHD(J) = MMRHO*((C1+1.)*POWER(RHO,NC1-1)*RATE(J)*
      * POWER(SIGMA(N2),-NSTOIC(2,J)) - (C2+1.)*EXP3*POWER(RHO,NC2-1)*
      * EXP3*POWER(SIGMA(N3),NSTOIC(3,J))*POWER(SIGMA4,NSTOIC(4,J))*EXP1)
      PXXT(J) = MMRHO*PXXT(J)
      PXXSTG(J,N2) = MMRHO*PXXSIG(J,N2) + XX(J)/MM(J)*M(N2,J)
      PXXSTG(J,N3) = MMRHO*PXXSIG(J,N3) + XX(J)/MM(J)*M(N3,J)
      TF (N4 .LE. LS .AND. N4 .NE. N3) PXXSIG(J,N4) = MMRHO*
      * PXXSTG(J,N4) + XX(J)/MM(J)*M(N4,J)
      GO TO 9

88   MMRHO = MM(J)*RHO
      PXXPHD(J) = MMRHO*((C1+1.)*POWER(RHO,NC1-1)*RATE(J)*
      * POWER(SIGMA1,-NSTOIC(1,J))*POWER(SIGMA(N2),-NSTOIC(2,J)) -
      * (C2+1.)*EXP3*POWER(RHO,NC2-1)*EXP3*POWER(SIGMA(N3),NSTOIC(3,J))*
      * EXP1)
      PXXT(J) = MMRHO*PXXT(J)
      IF (N1 .LE. LS .AND. N1 .NE. N2) PXXSIG(J,N1) = MMRHO*
      * PXXSTG(J,N1) + XX(J)/MM(J)*M(N1,J)
      PXXSTG(J,N2) = MMRHO*PXXSIG(J,N2) + XX(J)/MM(J)*M(N2,J)
      PXXSTG(J,N3) = MMRHO*PXXSIG(J,N3) + XX(J)/MM(J)*M(N3,J)
      9   PXXT(J) = PXXT(J) + XX(J)*(N(J) + B(J)/T)/T

      GTGM1 = GAMMA*(GAMMA - 1.)
      PGAMT = 0.
C     GAMMA WRT SIGMA(I) AND MACH NUMBER SQUARED WRT SIGMA(I)
      DO 10 I=1,L
      PGSIG(I) = GTGM1*(MIXMW - CPR(I)/TCPR)
      PM2SIG(I) = -M2*(MIXMW + PGSIG(I)/GAMMA)
      10 PGAMT = PGAMT + SIGMA(I)*DCPR(I)

C     GAMMA WRT T
      PGAMT = -GTGM1/TCPR*PGAMT

C     MACH NUMBER SQUARED WRT V
      PM2V = 2.*V*MIXMW/(GAMMA*R*T)

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## APPENDIX B

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C MACH NUMBER SQUARED WRT T
PM2T = -M2*(1./T + PGAMT/GAMMA)

TERM = RHO
IF (VERSI .EQ. TIMEV) GO TO 12
TERM = RHO/V
C DSIGMA/DIVAR WRT V
DO 11 II=4,LSP3
II BETAI(II,1) = -F(II)/V

C DSIGMA/DIVAR WRT RHO AND DSIGMA/DIVAR WRT T
12 DO 14 II=4,LSP3
I = II - 3
DO 13 J=1,LR
STOC = STOC(II,J)
BETA(II,2) = BETA(II,2) + STOC*PXXRHO(J)
13 BETA(II,3) = BETA(II,3) + STOC*PXXT(J)
BETA(II,2) = F(II)/RHO + TERM*BETA(II,2)
14 BETA(II,3) = TERM*BETA(II,3)

C DSIGMA(II)/DIVAR WRT SIGMA(K)
DO 16 II=4,LSP3
I = II - 3
DO 16 KK=4,LSP3
K = KK - 3
DO 15 J=1,LR
STOC = STOC(II,J)
15 BETA(II,KK) = BETA(II,KK) + STOC*PXXSIG(J,K)
16 BETA(II,KK) = TERM*BETA(II,KK)

C S1 WRT V,RHO,T,SIGMA(II) AND S2 WRT V,RHO,T,SIGMA(II)
PSIV = 0.
PSIRHO = 0.
PSIT = 0.
PS2V = 0.
PS2RHO = 0.
PS2T = 0.
DO 18 II=4,LSP3
I = II - 3
PSIV = PSIV + BETA(II,1)
PSIRHO = PSIRHO + BETA(II,2)
PSIT = PSIT + BETA(II,3)
PS2V = PS2V + HRT(II)*BETA(II,1)
PS2RHO = PS2RHO + HRT(II)*BETA(II,2)
PS2T = PS2T + HRT(II)*BETA(II,3) + CPR(II)*F(II)/T
PSISIG(II) = 0.
PS2SIG(II) = 0.
DO 17 KK=4,LSP3
K = KK - 3
PSISIG(II) = PSISIG(II) + BETA(KK,II)
17 PS2SIG(II) = PS2SIG(II) + HRT(KK)*BETA(KK,II)
PSISIG(II) = MIXMW*(PSISIG(II) - S1)
18 PS2SIG(II) = MIXMW*(PS2SIG(II) - S2)
PSIV = MIXMW*PSIV
PSIRHO = MIXMW*PSIRHO
PSIT = MIXMW*PSIT
PS2V = MIXMW*PS2V
PS2RHO = MIXMW*PS2RHO
PS2T = MIXMW*PS2T - S2/T

GMIDG = [GAMMA - 1.]/GAMMA
S2DG2 = S2/[GAMMA*GAMMA]
C BB WRT V
PBBV = GMIDG*PS2V
C BB WRT RHO
PBBRHO = GMIDG*PS2RHO
C BB WRT T
PBBT = GMIDG*PS2T + S2DG2*PGAMT

C AA WRT V
PAAV = PSIV - PBBV
C AA WRT RHO
PAARH0 = PSIRHO - PBBRHO
C AA WRT T
PAAT = PSIT - PBBT

C BB WRT SIGMA(II) AND AA WRT SIGMA(II)
DO 19 I=1,LS
PBBSIG(II) = GMIDG*PS2SIG(II) + S2DG2*PGSIG(II)
19 PAASIG(II) = PSISIG(II) - PBBSIG(II)

IF (VERSA .NE. AREA9) GO TO 24
C ASSIGNED AREA EQUATIONS
T1 = 1./(M2 - 1.)
GAM1 = GAMMA - 1.
C DV/DIVAR WRT V
BETAI(1,1) = T1*(DTERM - F(1)*PM2V - V*PAAV)
C DV/DIVAR WRT RHO
BETAI(1,2) = -V*T1*PAARH0
C DV/DIVAR WRT T
BETAI(1,3) = -T1*(V*PAAT + F(1)*PM2T)
C DV/DIVAR WRT SIGMA(II)
DO 20 II=4,LSP3
I = II - 3
20 BETAI(1,II) = -T1*(V*PAASIG(II) + F(1)*PM2SIG(II))

IF (RHCON) GO TO 22
C DRHO/DIVAR WRT V

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## APPENDIX B

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C      RETA(2,1) = RHO*T1*(PAAV + T1*DTERM*PM2V)
C      DPHD/DIVAR WRT RHO
C      RETA(2,2) = RHO*T1*PAARHO + F(2)/RHO
C      DPHD/DIVAR WRT T
C      RETA(2,3) = RHO*T1*(PAAT + T1*DTERM*PM2T)
C      DPHD/DIVAR WRT SIGMA(I)
C      DO 21 TI=4,LSP3
C      T = TI - 3
21     RETA(2,TT) = RHO*T1*(PAASIG(I) + T1*DTERM*PM2SIG(I))

22 IF(TCON) GO TO 300
C      DT/DIVAR WRT V
C      RETA(3,1) = T*(GAM1*T1*(M2*PAAV + T1*DTERM*PM2V) - PBBV)
C      DT/DIVAR WRT RHO
C      RETA(3,2) = T*(GAM1*M2*T1*PAARHO - PBBRHO)
C      DT/DIVAR WRT T
C      RETA(3,3) = T*(T1*(GAM1*(M2*PAAT + T1*DTERM*PM2T) - M2*DTERM*PGAMT
* ) - PBBT) + F(3)/T
C      T*(T0H,E0,2) BETA(3,3)=BETA(3,3)+T*GAM1* PAAT +T*AA*PGAMT
C      DT/DIVAR WRT SIGMA(I)
C      DO 23 TI=4,LSP3
C      T = TI - 3
C      RETA(3,TT) = T*(T1*(GAM1*(M2*PAASIG(I) + T1*DTERM*PM2SIG(I)) - M2*
* DTERM*PGSIG(I)) - PBBSIG(I))
C      T*(T0H,E0,2)BETA(3,II)=BETA(3,II)+GAM1*T*PAASIG(I)+T*AA*PGSIG(I)
23 CONTINUE

GO TO 300
C      ASSIGNING PRESSURE EQUATIONS
24 TI = 1. / (GAMMA * GAMMA)

C      DV/DIVAR WRT V
C      IF (V .NE. 0.) BETA(1,1) = -F(1)/V
C      DV/DIVAR WRT RHO
C      RETA(1,2) = -F(1)/RHO
C      DV/DIVAR WRT T
C      RETA(1,3) = 0.

C      DV/DIVAR WRT SIGMA(I)
C      DO 25 TI=4,LSP3
25     RETA(1,TT) = 0.

      IF (PHDCON) GO TO 27
C      DPHD/DIVAR WRT V
C      RETA(2,1) = -RHO*PAAV
C      DPHD/DIVAR WRT RHO
C      RETA(2,2) = F(2)/RHO - RHO*PAARHO
C      DPHD/DIVAR WRT T
C      RETA(2,3) = -RHO*(PAAT + T1*DTERM*PGAMT)
C      DPHD/DIVAR WRT SIGMA(I)
C      DO 26 TI=4,LSP3
C      T = TI - 3
26     RETA(2,TT) = -RHO*(PAASIG(I) + T1*DTERM*PGSIG(I))

27 IF(TCON) GO TO 300
C      DT/DIVAR WRT V
C      RETA(3,1) = -T*PBBV
C      DT/DIVAR WRT RHO
C      RETA(3,2) = -T*PBBRHO
C      DT/DIVAR WRT T
C      RETA(3,3) = BB - T*(PBBT - T1*DTERM*PGAMT) + F(3)/T
C      DT/DIVAR WRT SIGMA(I)
C      DO 28 TI=4,LSP3
C      T = TI - 3
28     RETA(3,TT) = -T*(PBBSIG(I) - T1*DTERM*PGSIG(I))
300 CONTINUE
      RETURN
      END

      FUNCTION POWER (X,N)

C      PASE X TO THE NTH POWER

C      THIS FUNCTION DEFINES 0**0=1 AND 0**N=0 FOR ALL NON-ZERO N

      POWER = 1.
      IF (N .EQ. 0) RETURN
      IF (X .NE. 0.) GO TO 2
      POWER = 0.
      RETURN
2     IF (N .NE. 1) GO TO 3
      POWER = X
      RETURN
3     POWER = X**N
      RETURN
      END

      SUBROUTINE COMB

C      FOULTRUM COMBUSTION CALCULATIONS

      LOGICAL TP,HP

```

## APPENDIX B

```

COMMON/COND/DVAR,AREA,MDOT,P,IVAR,V,RHO,T,SIGMA(25),LS,LSP3,NEXT
COMMON/SPEC/DUM1(3),SPNM(28),DUM2(25,102)
COMMON/SPECES/EN(25),ENLN(25),DELN(25),A(15,25)
COMMON/INDX/TP,HP,DUM3(6)
COMMON/MISC/TT,PP,CPR0,HRO,ENN,DUM4(32)

TP = .FALSE.
HP = .TRUE.

CALL ELEMNT (LS,SPNM,SIGMA)
ENI = 0.1/FLOAT(LS)
ENIL = ALOG(ENI)
DO 3 I=1,LS
EN(I) = ENI
3 ENLN(I) = ENIL
ENN = 0.1

TT = 3800.
PP = P
CALL EQLBRM

CALL ECOUT

RETURN
END

```

SUBROUTINE SHOK

C EQUILIBRIUM AND FROZEN SHOCK CALCULATIONS

```

LOGICAL TP,HP,EQL .
REAL MIXMW

COMMON/COND/DVAR,AREA,MDOT,P,IVAR,V,RHO,T,SIGMA(25),LS,LSP3,NEXT
COMMON/NECC/RR,MIXMW,M2,GAMMA,TCPR,R
COMMON/SPEC/DUM1(3),SPNM(28),DUM2(25,102)
COMMON/SPECES/EN(25),ENLN(25),DELN(25),A(15,25)
COMMON/POINTS/DLVTP,DLVPT,GAM,WM
COMMON/INDX/TP,HP,DUM3(6)
COMMON/MISC/TT,PP,CPR0,HRO,ENN,DUM4(32)

```

C INITIALIZE
TP = .TRUE.
HP = .FALSE.

C EQUILIBRIUM SHOCK
CALL ELEMNT (LS,SPNM,SIGMA)
GAM = GAMMA
ENI = 0.1/FLOAT(LS)
ENIL = ALOG(ENI)
DO 2 I=1,LS
EN(I) = ENI
2 ENLN(I) = ENIL
ENN = 0.1
EQL = .TRUE.
CALL SHOCKS (EQL)
CALL ESOUT

C FROZEN SHOCK
WM = MIXMW
DLVTP = 1.
DLVPT = -1.
GAM = GAMMA
DO 3 I=1,LS
3 EN(I) = SIGMA(I)
EQL = .FALSE.
CALL SHOCKS (EQL)
CALL FSOUT

RETURN
END

SUBROUTINE SHOCKS (EQL)

C SHOCK EQUATIONS

LOGICAL EQL,NEXT

REAL MIXMW,M2

DIMENSION A(2,3),Y(3)

```

COMMON/COND/DVAR,AREA,MDOT,P,IVAR,V,RHO,T,DUM1(25),LS,LSP3,NEXT
COMMON/NECC/RR,MIXMW,M2,DUM2,TCPR,R
COMMON/GHSC/GRT(25),HRT(25),SRT(25),CPR(25),DCPR(25)
COMMON/SPECES/SIGMA(25),ENLN(25),DELN(25),AAA(15,25)
COMMON/POINTS/DLVTP,DLVPT,GAMMA,WM
COMMON/MISC/TT,PP,CPR0,HRO,DUM3(33)

```

## APPENDIX B

```

C INITIAL ESTIMATE OF PRESSURE AND TEMPERATURE RATIOS
P21 = (Z.*GAMMA*M2 - GAMMA + 1.)/(GAMMA + 1.)
T21 = P21*(Z./M2 + GAMMA - 1.)/(GAMMA + 1.)
IF (.EQL .AND. T*T21 .GT. 2000.) T21 = 0.7*T21 + 600./T

CONST = MIXMW*V/R*V/T
P21L = ALOG(P21)
T21L = ALOG(T21)

C ITERATE ON PRESSURE AND TEMPERATURE RATIOS
C ***** ITERATIONS SET AT 99 ARBITRARILY BY AGM *****
DO 4 K=1,99
IF( K .GT. 8) GO TO 8795
GO TO 8796
8795 WRITE (6,8797) K
8797 FORMAT(16X,I5,* ..... ITERATIONS ..... *)
8796 CONTINUE
PP = P21*P
TT = T21*T
IF (.EQL) CALL EQLBRM
CALL THRM (TT,1.)
IF (.NEXT) GO TO 5
TCPR = 0.
THR = 0.
DO 2 I=1,LS
TCPR = TCPR + CPR(I)*SIGMA(I)
2 THR = THR + HRT(I)*SIGMA(I)
THR = THR*TT
RHO12 = T21/P21*MIXMW/WM

AA = RHO12*CONST
A(1,1) = -AA*DLVTP - P21
A(1,2) = -AA*DLVTP
A(1,3) = P21 - 1. + CONST*(RHO12 - 1.)
AA = (V*RHO12)**2/R
A(2,1) = -AA*DLVTP + TT*(DLVTP - 1.)/WM
A(2,2) = -AA*DLVTP - TT*TCPR
A(2,3) = THR - HRO - V*V*(1. - RHO12*RHO12)/(2.*R)

Y(3) = A(1,1)*A(2,2) - A(1,2)*A(2,1)
Y(2) = (A(1,1)*A(2,3) - A(2,1)*A(1,3))/Y(3)
Y(1) = (A(1,3)*A(2,2) - A(2,3)*A(1,2))/Y(3)

Y1 = ABS(Y(1))
Y2 = ABS(Y(2))
IF (Y2 .GT. Y1) Y1 = Y2
IF (Y1 .LT. 0.5E-04) RETURN
Y1 = Y1/0.4056652
IF (Y1 .LE. 1.) GO TO 3
Y(1) = Y(1)/Y1
Y(2) = Y(2)/Y1

3 P21L = P21L + Y(1)
T21L = T21L + Y(2)
P21 = EXP(P21L)
T21 = EXP(T21L)
4 CONTINUE

5 IF (.NOT. .EQL) GO TO 6
WRITE (6,100)
100 FORMAT (9H0(SHOCKS),5X,36HEQUILIBRIUM SHOCK CALCULATION FAILED)
NEXT = .FALSE.
RETURN

6 WRITE (6,101)
101 FORMAT (9H0(SHOCKS),5X,31HFROZEN SHOCK CALCULATION FAILED)
NEXT = .TRUE.
RETURN

END

SUBROUTINE ELEMNT (LS,DSPEC,SIGMA)

C COLLECT ELEMENT DATA FOR EQUILIBRIUM SHOCK OR COMBUSTION

DIMENSION DSPEC(25),SIGMA(25),LMT(4),SUBS(4)

COMMON/LTUS/LTHM,LDAT,NTHRO,NBLANK,NPHOTO
COMMON/SPECES/EN(25),ENLN(25),DELN(25),A(15,25)
COMMON/MISC/DUM1(7),LLMT(15),B0(15)
COMMON/INDX/TP,HP,NLM,NS,IQ1,DUM2(3)

EQUIVALENCE (DSP,SP)

IF (LS .EQ. NS) GO TO 10

C CONSTRUCT LIST OF ELEMENTS PRESENT
READ (LTTHM,99) DUMMY
NSP = NS + 1
2 READ(LTHM,99) SP,(LMT(K),SUBS(K),K=1,4),DUMM1,DUMM2,DUMM3
99 FORMAT(A8,16X,4(A2,F3.0)/A1/A1/A1)
DO 8 I=NSP,LS
IF (DSPEC(I) .NE. DSP) GO TO 8
DO 3 L=1,15
3 A(L,I) = 0.
IF (NLM .NE. 0) GO TO 4
NLM = 1

```

## APPENDIX B

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LLMT(NLM) = LMT(1)
4 DO 6 K=1,6
  IF (SUBS(K) .EQ. 0.) GO TO 7
  DO 5 L=1,NLM
    IF (LLMT(L) .NE. LMT(K)) GO TO 5
    A(L,I) = SUBS(K)
    GO TO 6
5 CONTINUE
  NLM = NLM + 1
  LLMT(NLM) = LMT(K)
  A(NLM,I) = SUBS(K)
6 CONTINUE
7 NS = NS + 1
  IF (NS .LT. LS) GO TO 2
  GO TO 9
8 CONTINUE
  GO TO 2
9 REWIND LTHM

C   COMPUTE ELEMENT CONCENTRATION IN GM-ATOMS/GM
10 DO 11 L=1,NLM
    BO(L) = 0.
    DO 11 I=1,LS
      11 BO(L) = BO(L) + A(L,I)*SIGMA(I)
      IQ1 = NLM + 1

      RETURN
      END

      SUBROUTINE EQLBRM

C   CALCULATE EQUILIBRIUM COMPOSITION AND PROPERTIES

      LOGICAL CONVG,ISING,LOGV,TP,NEXT
      DIMENSION PROW(18)

      COMMON/POINTS/DLVPT,DLVPT,GAMMA,WM
      COMMON/SPECES/EN(25),ENLN(25),DELN(25),A(15,25)
      COMMON/MISC/TT,PP,CPRO,HSUB0,ENN,SUMN,ENNL,LLMT(15),BO(15)
      COMMON/INDX/TP,HP,NLM,NS,IQ1,CONVG,KMAT,IMAT
      COMMON/GHSC/GRT(25),HKT(25),SR(25),CPR(25),DCPR(25)
      COMMON/MATX/G(128*28),X(28)
      COMMON/NECC/DUM1(4),CPSUM,DUM2
      COMMON/COND/DUM3(35),NEXT

C   INITIALIZE
      SMALNO = 1.0E-06
      SMNOL = -13.815511
      SIZE = 18.5
      SIZEF = 0.
      CONVG = .FALSE.
      ISING = .FALSE.
      LOGV = .FALSE.
      ITN = 300
      ITNUMB = ITN
      SUMN=ENN
      IAGM = 0
      TLN = ALOG(ITT)
      TM = ALOG(PP/ENN)
      ENNL = ALOG(ENN)
      CALL THRM (TT,1.)
      CPSUM = 0.
      DO 2 I=1,NS

C   BEGIN ITERATION
      2 CPSUM = CPSUM + CPR(I)*EN(I)
      3 CALL MATRIX
      NUMB = ITN- (ITNUMB - 1)
      IAGM = IAGM + 1
      IQ2 = IQ1 + 1
      IF (.NOT. CONVG) GO TO 67
      IF (LOGV) GO TO 63
      DO 182 L=1,NLM
        182 PROW(L) = G(IQ1,L)
        GO TO 72

C   LOGV = .TRUE. --- SET UP MATRIX TO SOLVE FOR DLVPT
      63 G(IQ1,IQ2) = ENN
      IQ = IQ1 - 1
      DO 777 I=1,IQ
        777 G(I,IQ2) = G(I,IQ1)
      72 IMAT = IMAT - 1
      67 ITST = IMAT
      CALL GAUSS
      IF (ITST .NE. IMAT) GO TO 774
      IF (.NOT. CONVG) GO TO 85
      IF (LOGV) GO TO 171
      SUM = 0.
      DO 175 L=1,NLM
        175 SUM = SUM + PROW(L)*X(L)
        DLVPT = 1. + (G(IQ2,IQ1) - SUM)/ENN - X(IQ1)
        CCPR = G(IQ2,IQ2)
        DO 176 I=1,IQ1

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## APPENDIX B

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176 CCPR = CCPR - G(IQ2,I)*X(I)
    LOGV = .TRUE.
    GO TO 43

C   SINGULAR MATRIX
774 IF (.NOT. CONVG) GO TO 871
    WRITE (6,172)
172 FORMAT (9HO(EQLBRM),5X,26HDERIVATIVE MATRIX SINGULAR)
    GO TO 1171
871 WRITE (6,74)
74 FORMAT (9HO(EQLBRM),5X,15HSINGULAR MATRIX)
    IF (ISING) GO TO 873
    ISING = .TRUE.
    DO 970 I=1,NS
    IF (EN(I)) .NE. 0.) GO TO 970
    EN(I) = SMALNO
    ENLN(I) = SMNL0
970 CONTINUE
    WRITE (6,776)
776 FORMAT (9HO(EQLBRM),5X,7HRESTART)
    GO TO 43

     85 ITNUMB = ITNUMB - 1
C   OBTAIN CORRECTIONS TO THE ESTIMATES
    IF (TP) X(IQ2) = 0.
    DLNT = X(IQ2)
    SUM = X(IQ1)
    DO 101 I=1,NS
    DELN(I) = HRT(I)*DLNT - HRT(I) + (SR(I) - ENLN(I) - TM) + SUM
    DO 99 L=1,NLM
99    DELN(I) = DELN(I) + A(L,I)*X(L)
101 CONTINUE
    AMBDA = 1.
    AMBDAL = 1.
    SUM = ABS(X(IQ1))
    IF (ABS(DLNT) .GT. SUM) SUM = ABS(DLNT)
    DO 917 I=1,NS
    IF (EN(I)) .GT. 0. .AND. DELN(I) .GT. SUM) SUM = DELN(I)
    IF (EN(I)) .NE. 0. .OR. DELN(I) .LE. 0.) GO TO 917
    SUM1 = (-9.212 - ENLN(I) + ENNL)/(DELN(I) - X(IQ1))
    SUM1 = ABS(SUM1)
    IF (SUM1 .LT. AMBDAL) AMBDAL = SUM1
917 CONTINUE
    IF (SUM .GT. 2.) AMBDA = 2./SUM
    IF (AMBDAL .LT. AMBDA) AMBDA = AMBDAL

C   APPLY CORRECTIONS TO ESTIMATES
    SUM = 0.
    DO 113 I=1,NS
    ENLN(I) = ENLN(I) + AMBDA*DELN(I)
    EN(I) = 0.
    IF ((ENLN(I) - ENNL + SIZE) .LE. 0.) GO TO 113
    EN(I) = EXP(ENLN(I))
    SUM = SUM + EN(I)
113 CONTINUE
    SUMN = SUM
    IF (TP) GO TO 115
    TLN = TLN + AMBDA*DLNT
    TT = EXP(TLN)
    CALL THRM (TT,1.)
    CPSUM = 0.
    DO 3 I=1,NS
3 CPSUM = CPSUM + CPR(I)*EN(I)
    115 ENNL = ENNL + AMBDA*X(IQ1)
    ENN = EXP(ENN)
    TM = ALOG(PP/ENN)

C   TEST FOR CONVERGENCE
    IF (ITNUMB .EQ. 0) GO TO 13
    IF (AMBDA .LT. 1.) GO TO 43
    SUM = (ENN - SUMN)/ENN
    SUM = ABS(SUM)
    IF (SUM .GT. 0.5E-05) GO TO 43
    DO 130 I=1,NS
    AA = ABS(DELN(I)/SUMN)*EN(I)
    IF (AA .GT. 0.5E-05) GO TO 43
130 CONTINUE

     13 CONVG = .TRUE.
    IF (ITNUMB .NE. 0) GO TO 160
    WRITE (6,973) ITN
973 FORMAT (9HO(EQLBRM),4X,I3,* ITERATIONS - NO CONVERGENCE*)
    GO TO 873
160 IF (.NOT. (TP .AND. CONVG)) GO TO 143
    CALL THRM (TT,1.)
    CPSUM = 0.
    DU 4 I=1,NS
    4 CPSUM = CPSUM + CPR(I)*EN(I)
143 ITNUMB = ITN
    GO TO 43

C   CALCULATE EQUILIBRIUM PROPERTIES
1171 DLVTP = -1.
    DLVTP = 1.
    CCPR = CPSUM
    GO TO 199
171 SUM = 0.
    DO 179 L=1,NLM

```

## APPENDIX B

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179 SUM = SUM + PROW(L)*X(L)
    DLVPT = -2. + SUM*ENN + X(IQ1)
199 GAMMA = -1./DLVPT + DLVPT*DLVPT*ENN/CCPR
    WM = 1./ENN
    DO 872 I=1,NS
872 EN(I) = EXP(ENLN(I))
    RETURN
873 WRITE (6,900)
900 FORMAT (9H0(EQLBRM),5X,34HEQUILIBRIUM CALCULATIONS ABANDONED)
    NEXT = .TRUE.
    GO TO 171
    END

SUBROUTINE SPOUT

C SPECIAL OUTPUT

LOGICAL FROZ

REAL MIXMW,M2,MACH1,MACHF,M21,LSUBM

COMMON/KOUT/DUM1(21),UNITO,DUM2(52),FPS,SI,DBUGO
COMMON/COND/DVAR,MDOT,P,IVAR,V,RHO,T,SIGMA(25),LS,LSP3,NEXT
COMMON/GNCC/RR,MIXMW,M2,GAMMA1,TCPR,R
COMMON/GHSC/GRT(25),HRT(25),SR(25),CPR(25),DCPR(25)
COMMON/SPEC/DUM3(3),SPNM(28),DUM4(25,102)
COMMON/AFUN/CX3,CX2,CXL,CXO,ITPSZ,LSU8M,ETA,D,VISC,BETA
COMMON/MISC/TF,PF,CPR,HRO,ENN,DUM5(32)
COMMON/SPECS/EN(25),ENLN(25),DELN(25),A(15,25)
COMMON/POINTS/DLVPT,DLVPT,GAMMAF,WM

ENTRY Ecout
C EQUILIBRIUM COMBUSTION OUTPUT
    WRITE(6,101)
101 FORMAT (1H1,50X,30H** EQUILIBRIUM COMBUSTION **)
    VI = 0.
    GO TO 2

ENTRY ESDUT
C EQUILIBRIUM SHOCK OUTPUT
    WRITE(6,102)
102 FORMAT (1H1,47X,37H** EQUILIBRIUM SHOCK CALCULATION **)

    VI= V
2 PI= P
    RH0I= RHO
    TI= T
    P2I= PF/PI
    T2I= TF/TI
    RH02I= P2I/T2I*WM/MIXMW
    FROZ = .FALSE.
    GO TO 3

ENTRY FSOUT

C FROZEN SHOCK OUTPUT
    WRITE(6,103)
103 FORMAT (1H1,49X,32H** FROZEN SHOCK CALCULATION **)
    PI=P
    VI= V
    RH0I= RHO
    TI=T
    P2I= PF/PI
    T2I= TF/TI
    RH02I= P2I/T2I
    P= PF
    V= VI/RH02I
    RHO= RH0I*RH02I
    T= TI*T2I
    GAMMAF= TCPR/(TCPR - 1./MIXMW)
    FROZ = .TRUE.

3 CALL THRM (TI,1.)
    PMLOG = ALOG(PI*MIXMW)
    S=0.
    DO 4 I=1,LS
    IF (SIGMA(I) .EQ. 0.) GO TO 4
    S = S + SIGMA(I)*(SR(I) - ALOG(SIGMA(I)) - PMLOG)
4 CONTINUE
    S = S*1.987165
    MACH1= SQRT(M2)

    VF = VI/RH02I
    RH0F= RH0I*RH02I
    CALL THRM (TF,1.)
    PMLOG = ALOG(PF*WM)
    SF= 0.
    DO 5 I=1,LS
    IF(EN(I)) .EQ. 0.) GO TO 5
    SF = SF + EN(I)*(SR(I) - ALOG(EN(I)) - PMLOG)
5 CONTINUE
    SF = SF*1.987165
    MACHF= SQRT(VF/R*VF/TF*WM/GAMMAF)

    S2I= SF/S
    G2I= GAMMAF/GAMMA1

```

## APPENDIX B

```

IF (VI .EQ. 0.) GO TO 205
SVI= VI/MACHI
SVF= VF/MACHF
V2I= VF/VI
M2I= MACHF/MACHI
SV2I= SVF/SVI
GO TO 305

205 MACHI = 0.
SVI = 0.
SVF = 0.
V2I = 0.
M2I = 0.
SV2I = 0.

305 IF (.NOT. FROZ .OR. ITPSZ .NE. 4) GO TO 405
C   CALCULATE L(M) FOR KINETIC AREA FUNCTION
PST = 1.
ROSVST = (GAMMAI/SVI)*1.01325E+06
LSUBM = (1./PF)*(RHO2I/(RH02I-1.))*(ROSVST/(PST*V1SC)*MACHI)**((1.
* -ETA)/ETA)*(D*PI/(4.*BETA))**((1./ETA)

405 WRITE (6,104)
104 FORMAT (/4LX,13HINITIAL STATE,17X,11HFINAL STATE,17X,19HFINAL/INIT
* IAL RATIO//)

      IF(UNIT0 .NE. FPS) GO TO 6
C   CONVERT FROM INTERNAL (CGS) UNITS TO FPS UNITS
PI= PI*2116.2
PF= PF*2116.2
VI= VI/30.48
VF= VF/30.48
RHOI= RH0I*62.43
RHOF= RHOF*62.43
TI= TI*1.8
TF= TF*1.8
SVI= SVI/30.48
SVF= SVF/30.48
WRITE(6,105) PI,PF,P2I,VI,WF,V2I,RHOI,RHOF,RHO2I,TI,TF,T2I,S,SF,
* S2I,MACHI,MACHF,M2I,GAMMAI,G2I,SVI,SVF,SV2I
105 FORMAT (10X,BHPRESSURE,1PE35.5,E29.5,E32.5/11X,10H(LB/FT**2)/10X,
* BHELOCITY,E35.5,E29.5,E32.5/11X,8H(FT/SEC)/10X,7HDENSITY,E36.5,
* E29.5,E32.5/11X,10H(LB/FT**3)/10X,11HTEMPERATURE,E32.5,E29.5,
* E32.5/11X,7H(DEG R)/10X,7HENTRTOPY,E36.5,E29.5,E32.5/11X,14H(BTU/L
* B/DEG R)/10X,11HMACH NUMBER,E32.5,E29.5,E32.5//10X,5HGAMMA,E38.5,
* E29.5,E32.5//10X,14HSonic VELOCITY,E29.5,E29.5,E32.5/11X,8H(FT/SE
*C)
GU TO 8

6 IF (UNIT0 .NE. SI) GO TO 7
C   CONVERT FROM INTERNAL (CGS) UNITS TO SI UNITS
PI= PI*1.01325E+05
PF= PF*1.01325E+05
VI= VI*0.01
VF= VF*0.01
RHOI= RH0I*1000.
RHOF= RHOF*1000.
S= S*4184.0
SF= SF*4184.0
SVI= SVI*0.01
SVF= SVF*0.01
WRITE(6,106) PI,PF,P2I,VI,WF,V2I,RHOI,RHOF,RHO2I,TI,TF,T2I,S,SF,
* S2I,MACHI,MACHF,M2I,GAMMAI,G2I,SVI,SVF,SV2I
106 FORMAT (10X,BHPRESSURE,1PE35.5,E29.5,E32.5/11X,8H(N/M**2)/10X,8HVE
* LCDITY,E35.5,E29.5,E32.5/11X,7H(M/SEC)/10X,7HDENSITY,E36.5,E29.5,
* E32.5/11X,9H(KG/M**2)/10X,11HTEMPERATURE,E32.5,E29.5,E32.5/11X,
* 7H(DEG K)/10X,7HENTRTOPY,E36.5,E29.5,E32.5/11X,16H(JOULE/KG/DEG K)
*/10X,11HMACH NUMBER,E32.5,E29.5,E32.5//10X,5HGAMMA,E38.5,E29.5,
* E32.5//10X,14HSonic VELOCITY,E29.5,E29.5,E32.5/11X,7H(M/SEC))
GO TO 8

C   PRINT OUTPUT IN INTERNAL (CGS) UNITS
7 WRITE(6,107) PI,PF,P2I,VI,WF,V2I,RHOI,RHOF,RHO2I,TI,TF,T2I,S,SF,
* S2I,MACHI,MACHF,M2I,GAMMAI,G2I,SVI,SVF,SV2I
107 FORMAT (10X,BHPRESSURE,F35.4,F28.4,F32.4/11X,5H(ATM)/10X,8HVELOCIT
* Y,F33.2,F28.2,F34.4/11X,8H(CM/SEC)/10X,7HDENSITY,1PE36.5,E28.5,
* DPF32.4/11X,10HIGH(CM**3)/10X,11HTEMPERATURE,F30.2,F28.2,F34.4/
* 11X,7H(DEG K)/10X,7HENTRTOPY,F36.4,F28.4,F32.4/11X,14H(CAL/GM/DEG
*K)/10X,11HMACH NUMBER,F32.4,F28.4,F32.4//10X,5HGAMMA,F38.4,F28.4,
* F32.4//10X,14HSonic VELOCITY,F27.2,F28.2,F34.4/11X,8H(CM/SEC))

8 WRITE (6,108)
108 FORMAT (/67X,7HSPECIES,5X,13HMOLE FRACTION)
DO 9 I=1,LS
EN(I)= EN(I)*WM
WRITE(6,109) SPNM(I),EN(I)
109 FORMAT(168X,A8,E15.5)
9 CONTINUE
WRITE(6,110) WM,DLVTP,DLVPT
110 FORMAT (/10X,24HMIXTURE MOLECULAR WEIGHT,36X,F12.5//10X,22H(D LOG V
* (OLUME)/D(LOG T)),E49.4/14X,*AT CONSTANT P//10X,*D(LOG VOLUME)/D(L
* G P)*,E49.4/14X,*AT CONSTANT T*)

RETURN
END

```

## APPENDIX B

### SUBROUTINE MATRIX

LOGICAL TP,HP,CONVG

```
COMMON/SPECES/EN(25),ENLN(25),DELN(25),A(15,25)
COMMON/MISC/TT,PP,CPRD,HSUB0,ENN,SUMN,ENNL,LLMT(15),BO(15)
COMMON/INDEX/TP,HP, L ,NS,IQ1,CONVG,KMAT,IMAT
COMMON/GHSC/GRT(25),HRT(25),SR(25),CPR(25),DCPR(25)
COMMON/MATX/G(28,28),X(28)
COMMON/HECC/DUM1(4),CPSUM,DUM2
```

```
IQ2 = IQ1 + L
IQ3 = IQ2 + 1
KMAT = IQ3
IF(.NOT.CONVG.AND.TP) KMAT = IQ2
IMAT = KMAT - 1
```

C CLEAR MATRIX STORAGES TO ZERO

```
DO 211 I=1,KMAT
DO 211 K=1,KMAT
G(I,K) = 0.
211 CONTINUE
SSS = 0.
HSUM = 0.
```

C BEGIN SET UP OF ITERATION MATRIX

```
KK = L
TM = ALOG(PP/ENN)
DO 65 J=1,NS
H = HRT(J)*EN(J)
F = (HRT(J) - SR(J) + ENLN(J) + TM)*EN(J)
SS = H-F
TERM1 = H
IF (KMAT .EQ. IQ2) TERM1 = F
DO 55 I = 1, L
```

C CALCULATE THE ELEMENTS R(I,K)

```
IF (A(I,J) .EQ. 0.) GO TO 55
TERM = A(I,J)*EN(J)
DO 15 K=1, L
G(I,K)= G(I,K) + A(I,J)*TERM
15 CONTINUE
```

```
G(I,IQ1)=G(I,IQ1)+TERM
G(I,IQ2)=G(I,IQ2)+(I,J)*TERM1
```

```
IF (CONVG .OR. TP) GO TO 55
G(I,IQ3)= G(I,IQ3)+A(I,J)*F
55 CONTINUE
IF (KMAT .EQ. IQ2) GO TO 64
IF (CONVG.DR.HP) GO TO 59
G(IQ2,IQ1) = G(IQ2,IQ1) + SS
G(IQ2,IQ2) = G(IQ2,IQ2) + HRT(J)*SS
G(IQ2,IQ3) = G(IQ2,IQ3) + (SR(J) - ENLN(J) - TM)*F
GO TO 62
```

```
59 G(IQ2,IQ2) = G(IQ2,IQ2) + HRT(J)*H
IF (CONVG) GO TO 66
G(IQ2,IQ3) = G(IQ2,IQ3) + HRT(J)*F
```

```
62 G(IQ1,IQ3)=G(IQ1,IQ3)+F
64 G(IQ1,IQ2)=G(IQ1,IQ2)+TERM1
```

65 CONTINUE

```
SSS = SSS + G(IQ2,IQ1)
HSUM = HSUM + G(IQ1,IQ2)
G(IQ1,IQ1) = SUMN - ENN
```

C REFLECT SYMMETRIC PORTIONS OF THE MATRIX

```
ISYM = IQ1
IF(HP,DR,CONVG) ISYM=IQ2
DO 102 I=1,ISYM
DO 102 J=I,ISYM
G(J,I)=G(I,J)
102 CONTINUE
```

C COMPLETE THE RIGHT HAND SIDE

```
IF(CONVG) GO TO 175
DO 145 I=1,L
145 G(I,KMAT) = G(I,KMAT) + BO(I) - G(I,IQ1)
G(IQ1,KMAT) = G(IQ1,KMAT)+ENN-SUMN
```

C COMPLETE ENERGY ROW AND TEMPERATURE COLUMN

```
IF (KMAT .EQ. IQ2) RETURN
IF (HP) ENERGY = HSUB0/TT - HSUM
G(IQ2,IQ3)=G(IQ2,IQ3)+ ENERGY
175 G(IQ2,IQ2)= G(IQ2,IQ2)+CPSUM
```

```
RETURN
END
```

## APPENDIX B

```

SUBROUTINE GAUSS

C      SOLVE ANY LINEAR SET OF UP TO 20 EQUATIONS

DIMENSION COEFX(28)
COMMON/MATX/G(28,28),X(28)

COMMON/INDX/TP,HP,NLM,NS,IQ1,CONVG,KMAT,IUSE
DATA BIGNO/1.E+38/

C      BEGIN ELIMINATION OF NNTH VARIABLE

IUSE1=IUSE+1
6 DO 45 NN=1,IUSE
IF (NN-IUSE) 8,83,8
83 IF(G(NN,NN))31,23,31

C      SEARCH FOR MAXIMUM COEFFICIENT IN EACH ROW

8 DO 18 I=NN,IUSE
COEFX(I) = BIGNO
IF(G(I,NN).EQ.0.) GO TO 18
COEFX(I) = 0.
DO 10 J>NN,IUSE1
SUM = G(I,J)
IF(SUM.LT.0.) SUM=-SUM
IF(J.NE.NN) GO TO 9
Z = SUM
GO TO 10
9 IF(SUM.GT.COEFX(I)) COEFX(I)=SUM
10 CONTINUE
COEFX(I) = COEFX(I)/Z
18 CONTINUE
TEMP = BIGNO
I=0
20 DO 22 J>NN,IUSE
IF (COEFX(J)-TEMP) 87,22,22
87 TEMP=COEFX(IJ)
IJ=J
22 CONTINUE
IF(I) 28,23,28

C      INDEX I LOCATES EQUATION TO BE USED FOR ELIMINATING THE NTH
C      VARIABLE FROM THE REMAINING EQUATIONS

C      INTERCHANGE EQUATIONS I AND NN

28 IF(NN-I) 29,31,29
29 DO 30 J>NN,IUSE1
Z=G(I,J)
G(I,J)=G(NN,J)
G(NN,J)=Z
30 CONTINUE

C      DIVIDE NTH ROW BY NTH DIAGONAL ELEMENT AND ELIMINATE THE NTH
C      VARIABLE FROM THE REMAINING EQUATIONS

31 K = NN + 1
DO 36 J = K, IUSE1
IF(G(NN,NN).EQ.0.) GO TO 23
G(NN,J) = G(NN,J)/G(NN,NN)
36 CONTINUE
IF(K-IUSE1) 88,45,88
88 DO 44 I = K,IUSE
40 DO 44 J = K, IUSE1
G(I,J) = G(I,J) - G(I,NN)*G(NN,J)
44 CONTINUE
45 CONTINUE

C      BACKSOLVE FOR THE VARIABLES

K = IUSE
47 J = K + 1
X(K) = 0.
SUM = 0.0
IF(IUSE - JJ) 51,48,48
48 DO 50 I = J,IUSE
SUM = SUM + G(K,I)*X(I)
50 CONTINUE
51 X(K) = G(K,IUSE1) - SUM
K = K - 1
IF (K) 47,151,47
23 IUSE = IUSE-1
151 RETURN
END

SUBROUTINE YOUT(N0,TLAST,Y,NQ,K2)
C ***** PRINT OUT INFORMATION
C
C      IN NAMELIST PROB THE PRINTING VARIABLES ARE
C
C      1 PAPS - SET TRUE IF PRINTING AT SPECIFIC STATIONS DESIRED
C      2 TPRINT - A TABLE OF PRINT STATIONS INPUT 50 VALUES AT MOST
C      3 NPRINT - THE NUMBER OF PRINT STATIONS

```

## APPENDIX B

```

C   * IDEL - INCREMENT FOR AUTOMATIC CALCULATION OF AT MOST 50 PRINT
C       STATIONS. IDEL NOT INPUT - A TABLE OF TPRINTS MUST BE
C       INPUT IF PAPS = TRUE
C       IF PAPS = FALSE IPRIT INPUT WILL CAUSE PRINTING EVERY IPRIT
C       ITERATIONS
C       END MUST ALWAYS BE SPECIFIED
C ****
LOGICAL KUP
LOGICAL TCON,RHOCON
LOGICAL DVUDT
REAL IVAR
DIMENSION Y(NO,K2),YPRINT(28)
COMMON/PRIN/TPRINT(50),NPRIN,NCO
COMMON/STCOM1/N,T,H,HMIN,HMAX,EP51,MFI,KFLAG1,JSTART
COMMON/COND/DVAR,AREA,M00T,P,IVAR,V,RHO,Z,SIGMA(25),LS,LSP3,DUM1
COMMON/UPDT/KUP
COMMON/STCOM8/TPREV,HNI
COMMON/STCOM9/VOLD
COMMON/OPTS/VERSI,TIMEV,DUM2(2),TCON,RHOCON,DUM3
DVUDT = .FALSE.
IF(NCO .EQ. 1) GO TO 11
INT=1
NCO=1
11 CONTINUE
IF((T-H).LT. TPRINT(INT) .AND. TPRINT(INT).LE. T) GO TO 10
IF(DVUDT) GO TO 13
ENTRY YOUT1
IF(RHOCON) GO TO 16
IF(VERSI .EQ. TIMEV) GO TO 12
DVAR = DVAR + 2.* (T - TPREV)/(VOLD + Y(1))
GO TO 15
12 CONTINUE
DVAR = DVAR + (T - TPREV)*(VOLD + Y(1))/2.
GO TO 15
13 CONTINUE
IF(RHOCON) GO TO 16
IF(VERSI .EQ. TIMEV) GO TO 17
DVAR = DVAR + (T - IVAR)*2./(VOLD + Y(1))
JC TO 16
17 CONTINUE
DVAR = DVAR + (T - IVAR)*((VOLD + Y(1))/2.)
16 CONTINUE
RETURN
10 CONTINUE
IF(TPRINT(INT) .EQ. T) GO TO 300
S = (TPRINT(INT) - T)/H
DO 1 I=1,N
YPRINT(I) = Y(I)
1 CONTINUE
P=1.
L= NO + 1
DO 3 J=2,L
P = P*S
DO 2 I=1,N
YPRINT(I) = YPRINT(I) + Y(I,J)*P
2 CONTINUE
3 CONTINUE
V = YPRINT(1)
PH0 = YPRINT(2)
Z = YPRINT(3)
DO 200 I=1,LS
II = I+3
SIGMA(I) = YPRINT(II)
200 CONTINUE
IF(RHOCON) GO TO 15
IF(VERSI .EQ. TIMEV) GO TO 14
HOLD1 = TPRINT(INT) - TPREV
IF(DVUDT) HOLD1 = TPRINT(INT) - IVAR
DVAR = DVAR + 2.*HOLD1/(V + VOLD)
GO TO 15
14 CONTINUE
HOLD1 = TPEINT(INT) - TPREV
IF(DVUDT) HOLD1 = TPRINT(INT) - IVAR
DVAR = DVAR + HOLD1*(V + VOLD)/2.
15 CONTINUE
DVUDT = .TRUE.
VOLD = V
IVAR = TPRINT(INT)
KUP = .TRUE.
CALL DIFF1
KUP = .FALSE.
GO TO 400
300 CONTINUE
IF(RHOCON) GO TO 400
IF(VERSI .EQ. TIMEV) GO TO 301
DVAR = DVAR + 2.* (T - TPREV)/(VOLD + Y(1))
GO TO 400
301 DVAR = DVAR + (T - TPREV)*(VOLD + Y(1))/2.
400 CONTINUE
CALL OUT3
INT = INT + 1
IF(INT .LE. NPRIN) GO TO 11
RETURN
END

```

## APPENDIX B

```

SUBROUTINE YOUTD (Y,NQ)
DIMENSION Y(28,6)
WRITE(6,7)
7 FORMAT(5X,*KFLAG NOT EQUAL TO 0*)
RETURN
END

SUBROUTINE DRIVES(N0,T0,TLAST,Y,HO,EPS,MF,KFLAG,K2)
LOGICAL PAPS
COMMON//STCOM1/N,T,H,HMIN,HMAX,EPS1,MF1,KFLAG1,JSTART
COMMON//STCOM8/TPREV,HN1
COMMON//STCOM2/YMAX(28)
COMMON//STCOM3/ERROR(28)
COMMON//STCOM5/FSAVE(56)
COMMON//STCOM6/PRIT,PAPS
DIMENSION Y(N0,K2),YDOT(56),TNIS4(812)
DO 9999 I=1,812
TNIS4(I)=0.
9999 CONTINUE
LOUT=6
IF (EPS.LE.0.) GO TO 400
IF (N0.LE.0) GO TO 410
IF((T0-TLAST)*HO.GE.0.) GO TO 420
N = N0
T = T0
H = HO
HMIN = ABS(HO)
HMIN = AMIN1(HMIN,.1*HMAX)
EPS1 = EPS
MF1 = MF
JSTART = 0
KHFLAG = 0
C
NCOUNT=0
NIS4 = N0*(N0+1)
10 CONTINUE
HN1 = H
TPREV = T
CALL STIFF(Y,N0,TNIS4,NIS4,K2)
NQ = JSTART
C
KGO = 1 - KFLAG1
GO TO ( 20,10,200,300 ),KGU
C KFLAG1 = 0, -1, -2, -3
C
20 CONTINUE
IF(PAPS) GU TO 9998
CALL YOUT1
NCOUNT = NCOUNT + 1
IF(NCOUNT .NE. IPRIT) GO TO 888
CALL OUT3
NCOUNT = 0
888 CONTINUE
GO TO 9997
9998 CONTINUE
CALL YOUT(N0,TLAST,Y,NQ,K2)
9997 CONTINUE
IF ((T-TLAST)*H.LT.0.) GO TO 10
*****C*****C*****C*****C*****C*****C*****C*****C*****C*****
C* THE PROBLEM IS FINISHED. HERE CALL YOUT AND/OR OTHER ROUTINES
C* TO OUTPUT DESIRED FINAL RESULTS.
*****C*****C*****C*****C*****C*****C*****C*****C*****C*****
CALL OUT3
GO TO 500
C
100 WRITE (LOUT,105) T
105 FORMAT(//30H KFLAG = -1 FROM STIFF AT T = ,E16.8/
1 38H ERROR TEST FAILED WITH ABS(H) = HMIN//)
110 IF (KHFLAG.EQ.10) GO TO 150
KHFLAG = KHFLAG + 1
HMIN = HMIN*.1
H = H*.1
WRITE (LOUT,115) H
115 FORMAT(24H H HAS BEEN REDUCED TO ,E16.8,
1 26H AND STEP WILL BE RETRIED//)
JSTART = -1
GO TO 10
C
150 WRITE (LOUT,155)
155 FORMAT(//44H PROBLEM APPEARS UNSOLVABLE WITH GIVEN INPUT//)
*****C*****C*****C*****C*****C*****C*****C*****C*****C*****
C* HMIN HAS BEEN CUT BY 10 ORDERS OF MAGNITUDE WITH NO SUCCESS.
C* AT THIS POINT, OUTPUT INFORMATION NEEDED FOR DEBUGGING.
*****C*****C*****C*****C*****C*****C*****C*****C*****C*****
CALL YOUTD(Y,NQ)
GO TO 500
C
200 WRITE (LOUT,205) T,H
205 FORMAT(//30H KFLAG = -2 FROM STIFF AT T = ,E16.8,5H H =,E16.8/
1 52H THE REQUESTED ERROR IS SMALLER THAN CAN BE HANDLED//)
C* AT THIS POINT, OUTPUT INFORMATION NEEDED FOR DEBUGGING.
CALL YOUTD(Y,NQ)

GO TO 500
C

```

## APPENDIX B

```

300 WRITE (LOUT,305)
305 FORMAT(//30H KFLAG = -3 FROM STIFF AT T = ,E16.8/
      1 45H CORRECTOR CONVERGENCE COULD NOT BE ACHIEVED/)
      GO TO 110
C
400 WRITE (LOUT,405)
405 FORMAT(//26H ILLEGAL INPUT.. EPS.LE.0.//)
      KFLAG = -4
      RETURN
C
410 WRITE (LOUT,415)
415 FORMAT(//23H ILLEGAL INPUT.. N.LE.0.//)
      KFLAG = -4
      RETURN
C
420 WRITE (LOUT,425)
425 FORMAT(//38H ILLEGAL INPUT.. (T0-TLAST)*HO .GE. 0.//)
      KFLAG = -4
      RETURN
C
500 KFLAG = KFLAG1
      T0 = T
      HO = H
      RETURN
***** END OF DRIVES *****
END

SUBROUTINE STIFF(Y,NO,PW,NIS4,K2)
DIMENSION PW(NIS4),Y(NO,K2),EL(13),TQ(4)
COMMON/STCOM1/N,T,H,HMIN,HMAX,EPS,MF,KFLAG,JSTART
COMMON/STCOM9/VOLD
COMMON/STCOM2/YMAX(28)
COMMON/STCOM3/ERROR(28)
COMMON/STCOM5/FSAVE(56)
DATA (ANOISE = 1.E-14)
VOLD = Y(1)
NPEDV = NO
KFLAG = 0
TOLD = T
IF (JSTART.GT.0) GO TO 200
IF (JSTART.NE.0) GO TO 120
*****  

C* ON THE FIRST CALL, THE ORDER IS SET TO 1 AND THE INITIAL  

C* DERIVATIVES ARE CALCULATED. YMAX IS INITIALIZED USING THE INITIAL  

C* Y AND YDOT. IF BOTH ARE INITIALLY ZERO IN ANY COMPONENT, THE DEFAULT  

C* VALUE IS 1. RMAX IS THE MAXIMUM RATIO BY WHICH H CAN BE INCREASED  

C* IN A SINGLE STEP. IT IS INITIALLY 1.E4 TO COMPENSATE FOR THE SMALL  

C* INITIAL H, BUT THEN IS NORMALLY EQUAL TO 10. IF A FAILURE  

C* OCCURS (IN CORRECTOR CONVERGENCE OR ERROR TEST), RMAX IS SET AT 2  

C* FOR THE NEXT INCREASE. EPSJ IS USED AS THE RELATIVE INCREMENT  

C* TO Y WHEN GETTING PARTIALS BY FINITE DIFFERENCING.
*****  

NSQ = NO*NO
NSQ1 = NSQ + 1
NI = NO + 1
CALL DIFUNIN,T,Y,FSAVE,D,NPEDV,K2
DO 110 I = 1,N
      Y(I,2) = FSAVE(I)*H
      AYI = ABS(Y(I))
      IF (AYI.EQ.0.) AYI = ABS(Y(I,2))
      IF (AYI.EQ.0.) AYI = 1.
110   YMAX(I) = AYI
NQ = 1
L = 2
RMAX = 1.E4
EPSJ = SQRT(ANOISE)
CRATE = 1.
OLDLO = 1.
RC = 0.
MFULD = 0
METH = 0
MITER = 0
HOLD = H
*****  

C* IF THE CALLER HAS CHANGED METH, OR IF JSTART = 0, COSET IS CALLED  

C* TO SET THE COEFFICIENTS OF THE METHOD. IF THE CALLER HAS CHANGED  

C* EPS OR METH, THE CONSTANTS E, EDN, EUP, AND BND MUST BE RESET.  

C* E IS A COMPARISON FOR ERRORS OF THE CURRENT ORDER NO. EUP IS  

C* TO TEST FOR INCREASING THE ORDER, EDN FOR DECREASING THE ORDER.  

C* BND IS USED TO TEST FOR CONVERGENCE OF THE CORRECTOR ITERATES.  

C* IF THE CALLER HAS CHANGED H, Y MUST BE RESCALED.  

C* IF H OR METH HAS BEEN CHANGED, IDOUB IS RESET TO L + 1 TO PREVENT  

C* FURTHER CHANGES IN H FOR THAT MANY STEPS. ALSO, RC IS RESET.  

C* RC IS THE RATIO OF NEW TO OLD VALUES OF THE COEFFICIENT L(0)*H.  

C* WHEN RC DIFFERS FROM 1 BY MORE THAN 30 PERCENT, OR THE CALLER HAS  

C* CHANGED MITER, IWEVAL IS SET TO MITER TO FORCE THE PARTIALS TO BE  

C* UPDATED, IF PARTIALS ARE USED.
*****  

120 IF (MF.EQ.MFOLD) GO TO 150
      MF = METH
      MIO = MITER
      MF = MF/10
      MITER = MF - 10*METH
      MFOLD = MF

```

## APPENDIX B

```

IF (MITER.NE.MIO) IWEVAL = MITER
IF (METH.EQ.MEO) GO TO 150
IODOUB = L + 1
IRET = 1
130 CALL COSET(METH,NQ,EL,TQ,MAXDER)
RC = RC*EL(1)/OLDLO
OLDLO = EL(1)
140 EDN = (TQ(1)*EPS)**2
E = (TQ(2)*EPS)**2
EUP = (TQ(3)*EPS)**2
BND = (TQ(4)*EPS)**2
GO TO ( 160 , 170 , 200 ), IRET
150 IF (EPS.EQ.EPSOLD) GO TO 160
IRET = 1
GO TO 140
160 LMAX = MAXDER + 1
EPSOLD = EPS
IF (H.EQ.HOLD) GO TO 200
RH = H/HOLD
H = HOLD
170 RH = AMAX1(RH,HMIN/ABS(H))
RH = AMIN1(RH,HMAX/ABS(H),RMAX)
R1 = 1.
DO 180 J = 2,L
    R1 = R1*RH
    DO 180 I = 1,N
        Y(I,J) = Y(I,J)*R1
    H = H*RH
    RC = RC*RH
    IODOUB = L + 1
    IF (T.NE.TOLD) GO TO 690
C***** THIS SECTION COMPUTES THE PREDICTED VALUES BY EFFECTIVELY
C* MULTIPLYING THE Y ARRAY BY THE PASCAL TRIANGLE MATRIX.
C***** 200 IF(ABS(RC-1.)>T.O.3) IWEVAL = MITER
    T = T + H
    DO 210 J1 = 1,NQ
        DO 210 J2 = J1,NQ
            J = NQ - J2 + J1
            DO 210 I = 1,N
                Y(I,J) = Y(I,J) + Y(I,J+1)
C***** UP TO 3 CORRECTOR ITERATIONS ARE TAKEN. CONVERGENCE IS TESTED
C* BY REQUIRING CHANGES TO BE LESS THAN BND, WHICH IS DEPENDENT ON
C* EPS, IN EUCLIDEAN NORM. THE SUM OF THE CORRECTIONS IS ACCUMULATED
C* IN THE VECTOR ERROR(I). IT IS APPROXIMATELY EQUAL TO THE L-TH
C* DERIVATIVE OF Y MULTIPLIED BY H**L/FACTORIAL(L-1)*EL(L), AND IS
C* THUS PROPORTIONAL TO THE ACTUAL ERRORS TO THE LOWEST POWER OF
C* H PRESENT (H**L).
C* THE Y ARRAY IS NOT ALTERED IN THE CORRECTION LOOP. THE UPDATED
C* Y VECTOR IS STORED TEMPORARILY IN FSAVE. THE NORM OF THE
C* ITERATE DIFFERENCE IS STORED IN D.
C***** 220 DO 230 I = 1,N
    230   ERROR(I) = 0.
    M = 0
    CALL DIFFUN(N,T,Y,FSAVE,N,NPEDV,K2)
    IF (IWEVAL.LE.0) GO TO 340
C***** IF NECESSARY, THE PARTIALS ARE REEVALUATED PRIOR TO STARTING THE
C* CORRECTOR ITERATION. IWEVAL IS THEN SET TO 0 AS AN INDICATOR
C* THAT THIS HAS BEEN DONE.
C* IF MITER = 1 OR 2, THE MATRIX P = I - L(0)*H*JACOBIAN IS STORED
C* IN PW AND SUBJECTED TO LU DECOMPOSITION, WITH THE RESULTS ALSO
C* STORED IN PW. IF MITER = 3, THE MATRIX USED IS P = I - L(0)*H*D,
C* WHERE D IS A DIAGONAL MATRIX.
C***** GO TO ( 240 , 260 , 310 ),MITER
240 CALL PEDERV(N,T,Y,PW,NO,NPEDV,K2)
    R = -EL(1)*H
    DO 250 I = 1,NSQ
    250   PW(I) = PW(I)*R
    GO TO 300
260 D = 0.
    DO 270 I = 1,N
    270   D = D + FSAVE(I+NO)**2
    RO = ABS(H)*SQRT(D)*1.E03*ANDISE
    J1 = -NO
    DO 290 J = 1,N
        J1 = J1 + NO
        YJ = Y(J)
        R = EPSJ*YMAX(J)
        R = AMAX1(R,RO)
        Y(J) = Y(J) + R
        D = -EL(1)*H/R
        CALL DIFFUN(N,T,Y,FSAVE,O,NPEDV,K2)
        DO 280 I = 1,N
            PW(I+J1) = (FSAVE(I) - FSAVE(I+NO))*D
    280   Y(J) = YJ
    290   DO 305 I = 1,N
    305   PW(I*NI-NO) = PW(I*NI-NO) + 1.
    IWEVAL = 0
    RC = 1.
    CALL DECOMP(NO,N,PW,PW(NSQ1),FSAVE,IER)
    IF (IER.NE.0) GO TO 420
    GO TO 360

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## APPENDIX B

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310 R = EL(1)*1
DO 320 I = 1,M
  PW(I) = Y(I) + P*(FSAVE(I+NO)*H - Y(I,2))
CALL DIFFUN(N,T,PW,FSAVE,0,NPDEV,K2)
DO 330 I = 1,N
  RO = PW(I) - Y(I)
  PW(I) = 1.
C*****+
410 IF (M.NE.0) CRATE = AMAX(.9*CRATE,D/D1)
IF ((DAMINI(1.,2.*CRATE)).LE.BND) GO TO 450
D1 = D
M = M + 1
IF (M.EQ.3) GO TO 420
CALL DIFFUN(N,T,FSAVE,FSAVE,N,NPDEV,K2)
GO TO 340
C*****+
C* THE CORRECTOR ITERATION FAILED TO CONVERGE IN 3 TRIES. IF PARTIALS
C* ARE INVOLVED BUT ARE NOT UP TO DATE, THEY ARE REEVALUATED FOR THE
C* NEXT TRY. OTHERWISE THE Y ARRAY IS RETRACTED TO ITS VALUES
C* BEFORE PREDICTION, AND H IS REDUCED, IF POSSIBLE. IF NOT, A
C* NO-CONVERGENCE EXIT IS TAKEN.
C*****+
420 IF (IWEVAL.EQ.-1) GO TO 440
T = TOLD
RMAX = 2.
DO 430 J1 = 1,NQ
  DO 430 J2 = J1,NQ
    J = NQ - J2 + J1
    DO 430 I = 1,N
      Y(I,J) = Y(I,J) - Y(I,J+1)
    IF (ABS(YH)).LE.(HMIN*1.00001) GO TO 680
    RH = .25
    GO TO 170
440 IWEVAL = MITER
GO TO 220
C*****+
C* THE CORRECTOR HAS CONVERGED. IWEVAL IS SET TO -1 IF PARTIAL
C* DERIVATIVES WERE USED, TO SIGNAL THAT THEY MAY NEED UPDATING ON
C* SUBSEQUENT STEPS. THE ERROR TEST IS MADE AND CONTROL PASSES TO
C* STATEMENT 500 IF IT FAILS.
C*****+
450 D = 0.
DO 460 I = 1,N
  D = D + (ERROR(I)/YMAX(I))**2
  IF (MITER.NE.0) IWEVAL = -1
  IF (D.CT.E) GO TO 500
C*****+
C* AFTER A SUCCESSFUL STEP, UPDATE THE Y ARRAY AND YMAX.
C* CONSIDER CHANGING H IF IDOUB = 1. OTHERWISE DECREASE IDOUB BY 1.
C* IF IDOUB IS THEN 1 AND NQ .LT. MAXDER, THEN ERROR IS SAVED FOR
  D = RO - EL(1)*H*(FSAVE(I) - FSAVE(NO+I))
  FSAVE(I) = RO/R
  IF (ABS(RO).EQ.0.) GO TO 330
  IF (D.EQ.0.) GO TO 420
  PW(I) = RO/D
  FSAVE(I) = FSAVE(I)*PW(I)
330 CONTINUE
  IWEVAL = 0
  RC = 1.
  GO TO 380
340 IF (MITER.NE.0) GO TO ( 360 , 360 , 400 ), MITER
C*****+
C* IN THE CASE OF FUNCTIONAL ITERATION, UPDATE Y DIRECTLY FROM
C* THE RESULT OF THE LAST DIFFUN CALL.
C*****+
  D = 0.
DO 350 I = 1,N
  R = H*FSAVE(I+NO) - Y(I,2)
  D = D + ( (R-ERR3R(I))/YMAX(I) )**2
  FSAVE(I) = Y(I) + EL(1)*R
350 ERROR(I) = R
GO TO 410
C*****+
C* IN THE CASE OF THE CH3RD METHOD, COMPUTE THE CORRECTOR ERROR,
C* F SUB (M), AND SOLVE THE LINEAR SYSTEM WITH THAT AS RIGHT-HAND
C* SIDE AND P AS COEFFICIENT MATRIX, USING THE LU DECOMPOSITION
C* IF MITER = 1 OR 2.
C*****+
360 DO 370 I = 1,N
  FSAVE(I+NO) = FSAVE(I+NO)*H - Y(I,2) - ERROR(I)
CALL SOLVE(NO,N,PW,FSAVE(NL),FSAVE,PW(NSQ))
380 D = 0.
DO 390 I = 1,N
  ERROR(I) = ERROR(I) + FSAVE(I)
  D = D + (FSAVE(I)/YMAX(I))**2
390 FSAVE(I) = Y(I) + EL(1)*ERROR(I)
GO TO 410
400 DO 405 I = 1,N
405 FSAVE(I) = PW(I)*(FSAVE(I+NO)*H - Y(I,2) - ERROR(I))
GO TO 380
C*****+
C* TEST FOR CONVERGENCE. IF M.GT.0, AN ESTIMATE OF THE CONVERGENCE
C* RATE CONSTANT IS STORED IN CRATE, AND THIS IS USED IN THE TEST.
C* USE IN A POSSIBLE ORDER INCREASE ON THE NEXT STEP.
C* IF A CHANGE IN H IS CONSIDERED, AN INCREASE OR DECREASE IN ORDER
C* BY ONE IS CONSIDERED ALSO. A CHANGE IN H IS MADE ONLY IF IT IS BY A
C* FACTOR OF AT LEAST 1.1. IF NOT, IDOUB IS SET TO 10 TO PREVENT
C* TESTING FOR THAT MANY STEPS.

```

## APPENDIX B

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*****+
KFLAG = 0
DO 470 J = 1,L
    DO 470 I = 1,N
        Y(I,J) = Y(I,J) + EL(IJ)*ERROR(I)
    DO 480 I = 1,N
480   YMAX(I) = AMAX1(YMAX(I),ABS(Y(I)))
    IF (IDOUB.EQ.1) GO TO 520
    IDOUB = IDOUB - 1
    IF (IDOUB.GT.1) GO TO 700
    IF (INQ.EQ.MAXDER) GO TO 700
    DO 490 I = 1,N
490   Y(I,LMAX) = ERROR(I)
    GO TO 700
*****
C* THE ERROR TEST FAILED. KFLAG KEEPS TRACK OF MULTIPLE FAILURES.
C* RESTORE T AND THE Y ARRAY TO THEIR PREVIOUS VALUES, AND PREPARE
C* TO TRY THE STEP AGAIN. COMPUTE THE OPTIMUM STEP SIZE FOR THIS OR
C* ONE LOWER ORDER.
*****
500   KFLAG = KFLAG - 1
      T = TOLD
      DO 510 J1 = 1,NQ
          DO 510 J2 = J1,NQ
              J = NQ - J2 + J1
              DO 510 I = 1,N
510     Y(I,J) = Y(I,J) - Y(I,J+1)
      RMAX = 2.
      IF (ABS(H).LE.(HMIN*1.00001)) GO TO 660
      IF (KFLAG.LE.-3) GO TO 640
      PR3 = 1.E+20
      GO TO 540
*****
C* REGARDLESS OF THE SUCCESS OR FAILURE OF THE STEP, FACTORS
C* PRI, PR2, AND PR3 ARE COMPUTED, BY WHICH H COULD BE DIVIDED
C* AT ORDER NQ - 1, ORDER NQ, OR ORDER NQ + 1, RESPECTIVELY.
C* IN THE CASE OF FAILURE, PR3 = 1.E20 TO AVOID AN ORDER INCREASE.
C* THE SMALLEST OF THESE IS DETERMINED AND THE NEW ORDER CHOSEN
C* ACCORDINGLY. IF THE ORDER IS TO BE INCREASED, WE COMPUTE ONE
C* ADDITIONAL SCALED DERIVATIVE.
*****
520   PR3 = 1.E+20
      IF (INQ.EQ.MAXDER) GO TO 540
      D1 = 0.
      DO 530 I = 1,N
530     D1 = D1 + ((ERROR(I) - Y(I,LMAX))/YMAX(I))**2
      ENQ3 = 0.5/FLOAT(L+1)
      PR3 = ((D1/EJP)**ENQ3)*1.4 + 1.4E-6
540   ENQ2 = 0.5/FLOAT(L)
      PR2 = ((D/E)**ENQ2)*1.2 + 1.2E-6
      PR1 = 1.E+20
      IF (INQ.EQ.1) GO TO 560
      D = 0.0
      DO 550 I = 1,N
550     D = D + (Y(I,L)/YMAX(I))**2
      ENQ1 = 0.5/FLOAT(NQ)
      PR1 = ((D/ENQ1)**ENQ1)*1.3 + 1.3E-6
560   IF (PR2.LE.PR3) GO TO 570
      IF (PR3.LT.PR1) GO TO 590
570   IF (PR2.GT.PR1) GO TO 580
      NEWQ = NQ
      RH = 1./PR2
      GO TO 620
580   NEWQ = NQ - 1
      RH = 1./PR1
      GO TO 620
590   NEWQ = L
      RH = 1./PR3
      IF (RH.LT.1.1) GO TO 610
      DO 600 I = 1,N
600     Y(I,NEWQ+1) = ERROR(I)*EL(I)/FLOAT(I)
      GO TO 630
610   IDOUB = 10
      GO TO 700
620   IF ((KFLAG.EQ.0).AND.(RH.LT.1.1)) GO TO 610
*****
C* IF THERE IS A CHANGE OF ORDER, RESET NQ, L, AND THE COEFFICIENTS.
C* IN ANY CASE H IS RESET ACCORDING TO RH AND THE Y ARRAY IS RESCALED.
C* THEN EXIT FROM 690 IF THE STEP WAS OK, OR REDO THE STEP OTHERWISE.
*****
630   NQ = NEWQ
      L = NQ + 1
      IRET = 2
      GO TO 130
*****
C* CONTROL REACHES THIS SECTION IF 3 OR MORE FAILURES HAVE OCCURED.
C* IT IS ASSUMED THAT THE DERIVATIVES THAT HAVE ACCUMULATED IN THE
C* Y ARRAY HAVE ERRORS OF THE WRONG ORDER. HENCE THE FIRST
C* DERIVATIVE IS RECOMPUTED, AND THE ORDER IS SET TO 1. THEN
C* H IS REDUCED BY A FACTOR OF 10, AND THE STEP IS RETRIED.
C* AFTER A TOTAL OF 7 FAILURES, AN EXIT IS TAKEN WITH KFLAG = -2.
*****
640   IF (KFLAG.EQ.-7) GO TO 670
      RH = .1
      RH = AMAX1(HMIN/ABS(H),RH)
      H = H*RH
      CALL DIFFUN(N,T,Y,FSAVE,O,NPEDV,K2)

```

## APPENDIX B

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DO 650 I = 1,N
650   Y(I,2) = H*FSAVE(I)
IWEVAL = MITER
100UB = 10
IF (NQ.EQ.1) GO TO 200
NQ = 1
L = 2
IRET = 3
GO TO 130
C***** ALL RETURNS ARE MADE THROUGH THIS SECTION. H IS SAVED IN HOLD
C* TO ALLOW THE CALLER TO CHANGE H ON THE NEXT STEP.
C***** KFLAG = -1
660   KFLAG = -1
GO TO 700
670   KFLAG = -2
GO TO 700
680   KFLAG = -3
GO TO 700
690   RMAX = 10.
700   HOLD = H
JSTART = NQ
RETURN
C***** END OF STIFF *****
END

```

```

SUBROUTINE COSET(METH,NQ,EL,TQ,MAXDER)
C***** COSET IS CALLED BY STIFF AND SETS COEFFICIENTS FOR USE THERE.
C* THE VECTOR EL, OF LENGTH NQ + 1, DETERMINES THE BASIC METHOD.
C* THE VECTOR TQ, OF LENGTH 3, IS INVOLVED IN ADJUSTING THE STEP SIZE
C* IN RELATION TO TRUNCATION ERROR. ITS VALUES ARE GIVEN BY THE
C* PERTST ARRAY.
C* THE VECTORS EL AND TQ DEPEND ON METH AND NQ.
C* COSET ALSO SETS MAXDE, THE MAXIMUM ORDER OF THE METHOD AVAILABLE.
C* CURRENTLY IT IS 12 FOR THE ADAMS METHODS AND 5 FOR THE GEAR METHODS.
C* LMAX = MAXDER + 1 IS THE NUMBER OF COLUMNS IN THE Y ARRAY.
C* THE MAXIMUM ORDER USED MAY BE REDUCED SIMPLY BY CHANGING THE
C* THE NUMBERS IN STATEMENTS 1 AND 2 BELOW.
C*
C* THE COEFFICIENTS IN PERTST NEED BE GIVEN TO ONLY ABOUT
C* ONE PERCENT ACCURACY. THE ORDER IN WHICH THE GROUPS APPEAR BELOW
C* IS... COEFFICIENTS FOR ORDER NQ - 1, COEFFICIENTS FOR ORDER NQ,
C* COEFFICIENTS FOR ORDER NQ + 1. WITHIN EACH GROUP ARE THE
C* COEFFICIENTS FOR THE ADAMS METHODS, FOLLOWED BY THOSE FOR THE
C* GEAR METHODS.
C***** DIMENSION PERTST(12,2,3),EL(13),TQ(4)
DIMENSION PERTST(12,2,3),EL(13),TQ(4)
DATA (PERTST = 1.1,2.,1.,.3158,.07407,.01391,.002182,
      1     .0002945,.00003492,.000003692,.0000003524,
      1     1.,1.,.5,.1667,.04167,1.,1.,1.,1.,1.,1.,
      1     2.,12.,24.,37.,89.,53.,33.,70.,08.,87.,97.,106.,9,
      1     126.,7,147.,4,168.,8,191.,0,
      1     2,0,4,5,7,333,10,42,13,7,1.,1.,1.,1.,1.,1.,
      1     12,0,24,0,37,89,53,33,70,08,87,97,106,9,
      1     126,7,147,4,168,8,191,0,1.,
      1     3,0,6,0,9,167,12,5,1.,1.,1.,1.,1.,1.,1.)
EL(2) = 1.0
GO TO (1,2),METH
1   MAXDER = 12
GO TO (101,102,103,104,105,106,107,108,109,110,111,112),NQ
2   MAXDER = 5
GO TO (201,202,203,204,205),NQ
C***** THE FOLLOWING COEFFICIENTS SHOULD BE DEFINED TO
C* MACHINE ACCURACY. FOR EACH ORDER NQ, THEY CAN BE CALCULATED
C* FROM THE GENERATING POLYNOMIAL,
C*   L(T) = EL(1) + EL(2)*T + ... + EL(NQ+1)*T**NQ.
C* FOR THE IMPLICIT ADAMS METHODS, L(T) IS GIVEN BY
C*   DL/DT = (T+1)*(T+2)* ... *(T+NQ-1)/K,    L(-1) = 0,
C* WHERE          K = FACTORIAL(NQ-1).
C* FOR THE GEAR METHODS,
C*   L(T) = (T+1)*(T+2)* ... *(T+NQ)/K,
C* WHERE          K = FACTORIAL(NQ)*(1 + 1/2 + ... + 1/NQ).
C*
C* THE ORDER IN WHICH THE GROUPS APPEAR BELOW IS..
C* IMPLICIT ADAMS METHODS OF ORDERS 1 TO 12,
C* STIFFLY STABLE GEAR METHODS OF ORDERS 1 TO 5.
C***** 101 EL(1) = 1.0
101 EL(1) = 1.0
GO TO 900
102 EL(1) = 0.5
EL(3) = 0.5
GO TO 900
103 EL(1) = 4.1666666666667E-01
EL(3) = 0.75
EL(4) = 1.66666666666667E-01
GO TO 900
104 EL(1) = 0.375
EL(3) = 9.16666666666667E-01
EL(4) = 3.333333333333E-01
EL(5) = 4.1666666666667E-02
GO TO 900
105 EL(1) = 3.4861111111111E-01
EL(3) = 1.0416666666667

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## APPENDIX B

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EL(4) = 4.8611111111111E-01
EL(5) = 1.0416666666667E-01
EL(6) = 8.3333333333333E-03
GO TO 900
106 EL(1) = 3.2986111111111E-01
EL(3) = 1.1416666666667
EL(4) = 0.625
EL(5) = 1.7708333333333E-01
EL(6) = 0.025
EL(7) = 1.3888888888889E-03
GO TO 900
107 EL(1) = 3.1559193121693E-01
EL(3) = 1.225
EL(4) = 7.5185185185185E-01
EL(5) = 2.5520833333333E-01
EL(6) = 4.8611111111111E-02
EL(7) = 4.8611111111111E-03
EL(8) = 1.9841269841270E-04
GO TO 900
108 EL(1) = 3.0422453703704E-01
EL(3) = 1.2964285714286
EL(4) = 8.6651851851852E-01
EL(5) = 3.3576388888889E-01
EL(6) = 7.7777777777778E-02
EL(7) = 1.0648148148148E-02
EL(8) = 7.9365079365079E-04
EL(9) = 2.4801587301587E-05
GO TO 900
109 EL(1) = 2.9486800044092E-01
EL(3) = 1.3589285714286
EL(4) = 9.7655423280423E-01
EL(5) = 0.4171875
EL(6) = 1.1135416666667E-01
EL(7) = 0.01875
EL(8) = 1.9345238095238E-03
EL(9) = 1.1160714285714E-04
EL(10)= 2.7557319223986E-06
GO TO 900
110 EL(1) = 2.8697544662857E-01
EL(3) = 1.4144841269841
EL(4) = 1.0772156084656
EL(5) = 4.9856701940035E-01
EL(6) = 0.1484375
EL(7) = 2.9060570987654E-02
EL(8) = 3.7202380952381E-03
EL(9) = 2.9968584656085E-04
EL(10)= 1.3778659611993E-05
EL(11)= 2.7557319223986E-07
GO TO 900
111 EL(1) = 2.8018959644394E-01
EL(3) = 1.4644841269841
EL(4) = 1.1715145502646
EL(5) = 5.7935819033527E-01
EL(6) = 1.8832286155203E-01
EL(7) = 4.1430362654321E-02
EL(8) = 6.2111441798942E-03
EL(9) = 6.2520667989418E-04
EL(10)= 4.0417401528513E-05
EL(11)= 1.5156525573192E-06
EL(12)= 2.5052108385442E-08
GO TO 900
112 EL(1) = 2.7426554003160E-01
EL(3) = 1.5099386724387
EL(4) = 1.2602711660212
EL(5) = 6.5923418209877E-01
EL(6) = 2.3045800254550E-01
EL(7) = 5.5697246105232E-02
EL(8) = 9.4394841269841E-03
EL(9) = 1.1192749669312E-03
EL(10)= 9.0939153439153E-05
EL(11)= 4.8225308661975E-06
EL(12)= 1.5031265031265E-07
EL(13)= 2.0876756987866E-09
GO TO 900
201 EL(1) = 1.0
GO TO 900
202 EL(1) = 6.6666666666667E-01
EL(3) = 3.3333333333333E-01
GO TO 900
203 EL(1) = 5.4545454545455E-01
EL(3) = EL(1)
EL(4) = 9.0909090909091E-02
GO TO 900
204 EL(1) = 0.48
EL(3) = 0.7
EL(4) = 0.2
EL(5) = 0.02
GO TO 900
205 EL(1) = 4.3795620437956E-01
EL(3) = 8.2116788321168E-01
EL(4) = 3.1021897810219E-01
EL(5) = 5.4744525567445E-02
EL(6) = 3.6496350354964E-03
C*
900 DO 910 K=1,3

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## APPENDIX B

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910 TQ(K)=PERTST(NQ,METH,K)
      TQ(4) = .5*TQ(2)/FLOAT(NQ+2)
      RETURN
C***** END OF COSET *****
      END

      SUBROUTINE DECOMP(NDIM, N, LU, IPS, SCALES, IER)
C
C     LINEAR SYSTEMS SUBROUTINE
C
C     DECOMPOSE THE N X N MATRIX A INTO TRIANGULAR L AND U SO THAT
C     L * U = P * A FOR SOME PERMUTATION MATRIX P.
C
C     NDIM    THE NUMBER OF ROWS IN THE DIMENSION STATEMENT FOR THE
C             MATRIX A IN THE CALLING PROGRAM.
C     N       THE NUMBER OF ROWS OR COLUMNS IN THE MATRIX
C     LU      ON INPUT, THE MATRIX A TO BE DECOMPOSED.
C             ON OUTPUT, THE ARRAY WHERE L AND U ARE STORED.
C     IPS     THE ROW PIVOT VECTOR, GIVING THE PERMUTATION MATRIX P.
C     IER     THE ERROR RETURN FLAG. IT IS 1 FOR ALL ZERO ELEMENTS
C             IN A ROW, 2 FOR A ZERO PIVOT, AND 0 FOR NO ERROR.
C
C     REAL LU(NDIM,N)
C     DIMENSION IPS(N),SCALES(N)
C     INTEGER PIVROW
C
C     INITIALIZE IER,IPS,LU,SCALES
C
C     IER=0
DO 5 I = 1, N
      IPS(I) = I
      ROWNRM = 0.0
DO 2 J = 1, N
      ROWNRM = AMAX1(ROWNRM, ABS(LU(I, J)))
2   CONTINUE
C
C     TEST FOR MATRIX WITH ZERO ROW.
C
      IF (ROWNRM .EQ. 0.0) GO TO 95
      SCALES(I) = 1.0 / ROWNRM
5   CONTINUE
C
C     GAUSSIAN ELIMINATION WITH PARTIAL PIVOTING
C
C     NM1 = N - 1
DO 17 K = 1, NM1
      BIG = 0.0
      DO 11 I = K, N
        IP = IPS(I)
        SIZE = ABS(LU(IP, K)) * SCALES(IP)
        IF (SIZE .LE. BIG) GO TO 11
      10   BIG = SIZE
          PIVROW = I
11   CONTINUE
C
C     TEST FOR ZERO PIVOT
C
      IF (BIG .EQ. 0.0) GO TO 96
C
C     INTERCHANGE ROW IF NECESSARY
C
      IF (PIVROW .EQ. K) GO TO 15
      J = IPS(K)
      IPS(K) = IPS(PIVROW)
      IPS(PIVROW) = J
15   KP = IPS(K)
      PIVOT = LU(KP, K)
      PIVOT = 1. / PIVOT
      LU(KP, K) = PIVOT
      KP1 = K + 1
DO 16 I = KP1, N
      IP = IPS(I)
      EM = LU(IP, K) * PIVOT
      LU(IP, K) = EM
      DO 16 J = KP1, N
        LU(IP, J) = LU(IP, J) - EM * LU(KP, J)
16   CONTINUE
17 CONTINUE
C
C     TEST FOR LAST PIVOT
C
      IP = IPS(N)
      PIVOT = LU(IP, N)
      IF (PIVOT .EQ. 0.0) GO TO 96
      LU(IP, N) = 1. / PIVOT
      RETURN
C
C     ALL ZERO ELEMENTS IN A ROW
C
95 IER = 1
      RETURN
C
C     ZERO PIVOT
96 IER = 2
      RETURN
C
      END

```

## APPENDIX B

```
C SUBROUTINE SOLVE(NDIM, N, LU, B, X, IPS)
C
C     LINEAR SYSTEM PACKAGE
C     SOLVE A X = B USING L U FROM SUBROUTINE DECOMP.
C
C     SEE DECOMP FOR DESCRIPTION OF PARAMETERS
C
C     DIMENSION B(N),X(N),IPS(N)
C     REAL LU(NDIM, N)
C
C     NPI = N + 1
C
C         FORWARD SUBSTITUTION - SOLVE L * Z = B
C
C     IP = IPS(1)
C     X(1) = B(IP)
C     DO 2 I = 2, N
C         IP = IPS(I)
C         IM1 = I - 1
C         SUM = 0.0
C         DO 1 J = 1, IM1
C             SUM = SUM + LU(IP, J) * X(J)
C 2       X(I) = B(IP) - SUM
C
C     IP = IPS(N)
C     X(N) = X(N) * LU(IP, N)
C
C         BACKWARD SUBSTITUTION - SOLVE U * X = Z, WHERE L * Z = B.
C
C     DO 4 IBACK = 2, N
C         I = NPI - IBACK
C         I GOES FROM (N-1) TO 1 BY -1
C         IP = IPS(I)
C         IP1 = I + 1
C         SUM = 0.0
C         DO 3 J = IP1, N
C             SUM = SUM + LU(IP, J) * X(J)
C 4       X(I) = (X(I) - SUM) * LU(IP, I)
C
C     RETURN
C     END
```

## APPENDIX C

### CHECK CASE OUTPUT COMPARISONS

Check case output comparisons are made in this appendix. The output from the program of this paper is always on the left-hand side of the page and the output from the program of NASA TN D-6586 is always on the right-hand side of the page.

#### Card Input Images

```

** DATA CARDS **

CC 1      1      2      3      4      5      6      7      8
          0      0      0      0      0      0      0      0

          BROMINE DISSOCIATION IN A SHOCK TUBE           CASE 1
M + BR2 = BR + BR  6.49E+11 .5  35500.
          - BLANK CARD -
XE
DISTANCE AREA
$PROB ITPSZ=3,L$UBM=32200.,ETA=0.5U, SHOCK=.TRUE., END=10.,
IDEL=20, PAPS=.TRUE.,
ALLM1=.FALSE., SEND
M + BR2 = BR + BR  8R2  3.80
          - BLANK CARD -
$START P=0.1227, MACH=3.2646, T=299.9, BR2=0.01,XE=0.99, SEND
FINIS

```

```

** DATA CARDS **

CC 1      1      2      3      4      5      6      7      8
          0      0      0      0      0      0      0      0

          METHANE - AIR COMBUSTION (ASSIGNED AREA - TIME INTEGRATION) CASE 6
CH4 + O2 = CH3 + H  3.00E+14 0.  103000.
H + O2 = HO2 + M  1.00E+13 0.  63000.
CO + O2 = CO2 + O  1.59E+15 0.  -1000.
CH3 + C2 = CH2O + OH  1.60E+13 0.  41000.
H + CH4 = CH3 + H2  7.50E+10 0.  0.
O + CH4 = CH3 + OH  6.90E+13 0.  11800.
OH + CH4 = CH3 + H2O  2.00E+13 0.  9200.
H + O2 = OH + O  7.20E+13 0.  5900.
O + H2 = OH + H  1.25E+14 0.  16300.
H2 + OH = H2O + H  2.96E+13 0.  9800.
CO + OH = CO2 + H  2.10E+13 0.  5100.
CH3 + C = CH2O + H  4.20E+11 0.  1000.
CH2O + H = HCO + H2  1.90E+13 0.  0.
CH2O + OH = HCO + H2O  1.00E+13 0.  2000.
CH2O + O = HCO + OH  7.00E+10 .70  1000.
HCO + O = CO + OH  4.00E+11 .60  4000.
HCO + OH = CO + H2O  1.80E+11 .50  0.
HCO + H = CO + H2  1.10E+11 .50  0.
H + HCO = H + CO  1.50E+12 .50  0.
HCO + O2 = CO + HO2  2.00E+13 .50  28600.
HCO + O2 = CO + HO2  1.00E+11 .50  5400.
HO2 + HO2 = H2O2 + O2  1.80E+12 0.  0.
H + HO2 = OH + OH  7.00E+13 0.  0.
O + HO2 = OH + O2  6.00E+12 0.  0.
OH + HO2 = H2O + O2  6.00E+12 0.  0.
M + HO2 = OH + OH  1.17E+17 0.  45500.
M + OH = H2O + M  7.50E+23 -2.60  0.
M + O2 = O + OH  2.75E+19 -1.  118700.
O + H2O = OH + OH  5.75E+13 0.  18000.

N2
TIME      AREA
$PROB ITPSZ=1, IPRCND=1,4MIN=6.25E-10,
HMAX=1.25E-6,
EMAX=.0001,
PAPS=.TRUE.,
END=2.6615E-4,
TPPINT=6.35273E-5,1.2/C555E-4,1.90582E-4,2.22346E-4,2.34109E-4,
2.6615E-4, NPIV=6,
COMHUS=.FALSE., ALLM1=.FALSE.,
XTB=0,5,10,15,20,25,30,35,36,37,38,39,40,40,5,41,42,
ATB=1300,1000,45,1002,02,1004,83,1009,24,1016,16,1028,32,1057,02,
1068,70,1085,55,1112,40,1163,57,1296,59,1371,48,1384,47,
```

## APPENDIX C

```

1400.45, NTB=16,
$END
H + O2 = HO2 + M CH4 5.0 O2 2.0
H + O2 = HO2 + M N2 2.0 H2O 32.5
H + O2 = HO2 + M CO 2.0 CO2 7.5
H + O2 = HO2 + M H2 5.0
H + H2O2 = OH + OH O2 .78 H2O2 6.6
H + H2O2 = OH + OH H2O 6.0
H + OH = H2O + M N2 1.6 H2O 20.
H + OH = H2O + M O2 1.6
- BLANK CARD -
$START P=1.730, V=157412.62, T=1645.,
CH4=0.049768, O2=0.199072, N2=0.75116,
$END
FINIS

```

	** DATA CARDS **							
CC 1	1	2	3	4	5	6	7	8
	0	0	0	0	0	0	0	0

```

METHANE-AIR COMBUSTION AT CONSTANT P (ONE UNIMOLECULAR REACTION) CASE 5
REPEAT
DISTANCE PRESSURE
$PROB ITPSZ=2, CX0=1.730, HMN=1.0E-4, HMAX=20., EMAX=.0001,
COMBUS=.TRUE., ALLMI=.FALSE.,
END=42.,
PAPS=.TRUE.,
TPRINT=5.0 10.0, 25.0, 35.0, 38.0, 39.5, 40.0, 40.5, 41.0, 42.0, NPRIN=10,
IPRIT=4, MF=22,
$END
- BLANK CARD -
$START AREA=1000., MACH=2., T=1645.,
CH4=0.049768, O2=0.199072, N2=0.75116,
$END
FINIS

```

	** DATA CARDS **							
CC 1	1	2	3	4	5	6	7	8
	0	0	0	0	0	0	0	0

```

H2-O2 LOW TEMPERATURE REACTION AT CONSTANT VOLUME (ADJUSTED RATES) C-8
H2 + C2 = H + HO2 1.00E+14 0. 67000.
H2 + CH = H2O 2.10E+13 0. 5100.
H + O2 = OH 1.25E+14 0. 16300.
O + H2 = CH 2.96E+13 0. 9800.
H + O2 = HO2 8.50E+14 0. -1000.
H + HO2 = OH 7.00E+13 0. 0.
M + H2O2 = OH 1.17E+17 0. 45500.
HO2 + HO2 = H2O2 1.00E+12 0. 0.
H2O2 + H2 = H2O2 4.50E+12 0. 24000.
H + H2O2 = H2O 3.18E+14 0. 9000.
OH + H2O2 = H2O 1.00E+13 0. 1800.
H + H2O = OH 5.75E+13 0. 18000.
- BLANK CARD -
- BLANK CARD -

```

```

TIME
$PRCB HMN=5.0E-5, HMAX=.1, EMAX=.0003, ALLMI=.FALSE.,
END=120.,
RHOCN=.TRUE., TCIN=.TRUE., CONC=.FALSE.,
TPRINT=.75, 1.25, 5.0, 10.0, 20.0, 30.0, 40.0, 50.0, 55.0, 60.0, 65.0, 75.0, 85.0, 95.0,
105.0, 120.0, NPRIN=16,
PAPS=.TRUE.,
$END
H + C2 = HO2 + M H2 5. 02 2.
H + O2 = HO2 + M H2O 32.5 O2 .78
M + H2O2 = CH + OH H2O 6. O2 .78
M + H2O2 = OH + OH H2O2 6.6 H2 2.3
- BLANK CARD -
$START MMHG=.TRUE., P=500., T=773.15, H2=.86, O2=.14, $END
FINIS

```

## Check Case 1

DISTANCE-AREA VERSION

GENERAL CHEMICAL KINETICS PROGRAM ITN U-636 USING STIFF ODE  
LANGLEY VERSION SOLUTION TECHNIQUE DEVELOPED BY C.W. GEAR

BROMINE DISSOCIATION IN A SHOCK TUBE

CASE 1

REACTION NUMBER	REACTION	A	REACTION RATE VARIABLES
1	$\text{M} + \text{Br}_2 \rightleftharpoons \text{Br} + \text{Br}$	$6.99000E+11$	N ACTIVATION ENERGY 3500.00

ALL THIRD BODY RATIOS ARE 1.0 EXCEPT THE FOLLOWING

M/BR2 = 1.1 = 3.80000

INTEGRATION CONTROLS

MINIMUM STEP SIZE 1.00000E-04 CM

INITIAL STEP SIZE 1.00000E-04 CM

MAXIMUM STEP SIZE 1.00000E-01 CM

MAXIMUM RELATIVE ERROR .00010

\*\* ASSIGNED VARIABLE PROFILE \*\*

THE AREA IS CALCULATED FROM THE FOLLOWING FUNCTION

$$1/\text{AREA} = 1 - (\text{X}/32200.000) * ( -50000 )$$

\*\* EQUILIBRIUM SHOCK CALCULATION \*\*

INITIAL STATE FINAL STATE FINAL / INITIAL RATIO

PRESSURE (ATM)	* 1.227	1.6130	1.31460
VELOCITY (CM/SEC)	51875.78	18108.11	* 3129
DENSITY (GM/CM**3)	65.69921E-05	20.96952E-04	3.1961
TEMPERATURE (DEG K)	299.90	1231.22	4.1054
ENTROPY (CAL/GM/DEG K)	* 3421	* 3576	1.0451
MACH NUMBER	3.2646	* 1.171	* 1.584
GAMMA	1.6586	1.5731	* 9485
SONIC VELOCITY (CM/SEC)	17728.29	* 35015.45	1.9751

SPECIES	MOLE FRACTION
BR2	8.12229E-03
BR	3.71805E-03
XE	9.88160E-01

MIXTURE MOLECULAR WEIGHT 131.3405d

## APPENDIX C

DLOG VOLUME//DLOG T)  
AT CONSTANT P  
DLOG VOLUME//DLOG P)  
AT CONSTANT T

\*\* FROZEN SHOCK CALCULATION \*\*  
 INITIAL STATE FINAL STATE  
 FINAL/INITIAL RATIO

PRESSURE	*1227	1.0017	1.0535
(ATM)	57075.78	18410.72	*3181
VELOCITY	(CM/SEC)		
DENSITY	65.60921E-05	20.62485E-04	3.436
(GM/CM**3)			
TEMPERATURE	299.90	1245.31	4.1524
(DEG K)			
ENTROPY	*3421	*3575	1.0449
(CAL/GM/DEG K)			
MACH NUMBER	3.2646	*5098	*1.562
GAMMA	1.6586	1.0577	*.9994
SONIC VELOCITY	(CM/SEC)	36115.84	2.0372

SPECIES MOLE FRACTION  
 BR2 1.00000E-02  
 BR 0.  
 XE 9.90000E-01

MIXTURE MOLECULAR WEIGHT  
 DLOG VOLUME//DLOG T)  
AT CONSTANT P  
DLOG VOLUME//DLOG P)  
AT CONSTANT T

TIME SEC  
 AXIAL POSITION CM  
 AREA SQ CM

TIME SEC  
 AXIAL POSITION CM  
 AREA SQ CM

TIME SEC  
 AXIAL POSITION CM  
 AREA SQ CM

## APPENDIX C

FLOW PROPERTIES  
 PRESSURE 1.6017 ATM  
 VELOCITY 18410.72 CM/SEC  
 TEMPERATURE 1245.31346 K  
 DENSITY 2.06245E-03 GM/CC  
 FLOW RATE 3.79718E+01 GM/SEC  
 ENTROPY \*35751 CAL/GM-K  
 MACH NUMBER \*50977  
 GAMMA 1.65767

CHMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
BR2	1.00000E-02	-3.66699E-05	BR2	1.00000E-02	-3.66695E-05
BR	0.	7.33390E-05	BR	0.	7.33390E-05
XE	9.90000E-01	0.	XE	9.90000E-01	0.

MIXTURE MOLECULAR WEIGHT 131.58520

FLOW PROPERTIES  
 PRESSURE 1.6017 ATM  
 VELOCITY 18410.72 CM/SEC  
 TEMPERATURE 1245.31346 K  
 DENSITY 2.06248E-03 GM/CC  
 FLOW RATE 3.79718E+01 GM/SEC  
 ENTROPY \*35751 CAL/GM-K  
 MACH NUMBER \*50977  
 GAMMA 1.65767

CHMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
BR2	1.00000E-02	-3.66699E-05	BR2	1.00000E-02	-3.66695E-05
BR	0.	7.33390E-05	BR	0.	7.33390E-05
XE	9.90000E-01	0.	XE	9.90000E-01	0.

MIXTURE MOLECULAR WEIGHT 131.58520

## APPENDIX C

TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	3.97333E+05	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	3.97333E+05
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000
TIME AXIAL POSITION AREA	2.72634E-05 SEC 5.00000E-01 CM 1.00396E+00 SQ CM	TIME AXIAL POSITION AREA	2.72461E-05 SEC 5.00000E-01 CM 1.00396E+00 SQ CM
MASS FRACTION SUM		MASS FRACTION SUM	

FLOW PROPERTIES		FLOW PROPERTIES	
PRESSURE	1.6058 ATM	PRESSURE	1.6053 ATM
VELOCITY	18301.52 CM/SEC	VELOCITY	18314.71 CM/SEC
TEMPERATURE	1245.9681 K	TEMPERATURE	1246.01850 K
DENSITY	2.06652E-03 GM/CC	DENSITY	2.06614E-03 GM/CC
FLOW RATE	3.79702E+01 GM/SEC	FLOW RATE	3.79903E+01 GM/SEC
ENTROPY	.35752 CAL/GM-K	ENTROPY	.35752 CAL/GM-K
MACH NUMBER	.50659	MACH NUMBER	.50698
GAMMA	1.65772	GAMMA	1.65772

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
BR2	9.93544E-03	-3.68318E-05	BR2	9.93549E-03	-3.6752E-05
BR	1.28945E-04	7.36637E-05	BR	1.27737E-04	7.35059E-05
XE	9.89937E-01	0.	XE	9.89937E-01	0.
<b>MIXTURE MOLECULAR WEIGHT</b> 131.57678					
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	3.97533E+05	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	3.96829E+05		
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000		

TIME AXIAL POSITION AREA	3.31019E-04 SEC 6.00000E+00 CM 1.01384E+00 SQ CM	TIME AXIAL POSITION AREA	3.30915E-04 SEC 6.00000E+00 CM 1.01384E+00 SQ CM
MASS FRACTION SUM		MASS FRACTION SUM	

FLOW PROPERTIES		FLOW PROPERTIES	
PRESSURE	1.0184 ATM	PRESSURE	1.0180 ATM
VELOCITY	17969.51 CM/SEC	VELOCITY	17972.92 CM/SEC
TEMPERATURE	1243.66331 K	TEMPERATURE	1243.654007 K
DENSITY	2.08531E-03 GM/CC	DENSITY	2.08499E-03 GM/CC
FLOW RATE	3.79716E+01 GM/SEC	FLOW RATE	3.79903E+01 GM/SEC
ENTROPY	.35756 CAL/GM-K	ENTROPY	.35756 CAL/GM-K
MACH NUMBER	.49737	MACH NUMBER	.49773
GAMMA	1.65824	GAMMA	1.65873

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
BR2	9.27260E-03	-3.03571E-05	BR2	9.2748E-03	-3.0319E-05
BR	1.44040E-03	6.07152E-05	BR	1.4370E-03	6.06389E-05
XE	9.89287E-01	0.	XE	9.89299E-01	0.
<b>MIXTURE MOLECULAR WEIGHT</b> 131.49043					

### MIXTURE MOLECULAR WEIGHT

131.49065

131.49043

## APPENDIX C

TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	3.21779E+05	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	3.21488E+05
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000
TIME	4.42637E-04 SEC	TIME	4.42332E-04 SEC
AXIAL POSITION	8.00000E+00 CM	AXIAL POSITION	8.00000E+00 CM
AREA	1.01601E+00 SQ CM	AREA	1.01601E+00 SQ CM
FLOW PROPERTIES		FLOW PROPERTIES	
PRESSURE	1.6210 ATM	PRESSURE	1.6210 ATM
VELOCITY	17890.27 CM/SEC	VELOCITY	17890.27 CM/SEC
TEMPERATURE	124.57201 K	TEMPERATURE	124.57201 K
DENSITY	2.09008E-03 GM/CC	DENSITY	2.09008E-03 GM/CC
FLOW RATE	3.79714E+01 GM/SEC	FLOW RATE	3.79714E+01 GM/SEC
ENTROPY	*35756 CAL/GM-K	ENTROPY	*35756 CAL/GM-K
MACH NUMBER	*49520	MACH NUMBER	*49520
GAMMA	1.65839	GAMMA	1.65839
CHEMICAL PROPERTIES		CHEMICAL PROPERTIES	
SPECIES	MOLE FRACTION	SPECIES	MOLE FRACTION
BR2	9.06919E-03	BR2	9.07118E-03
BR	1.83118E-03	BR	1.83924E-03
XE	9.89088E-01	XF	9.89080E-01
MIXTURE MOLECULAR WEIGHT	131.46393	MIXTURE MOLECULAR WEIGHT	131.46619
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	2.84313E+05	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	2.84212E+05
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000
TIME	5.54739E-04 SEC	TIME	5.54356E-04 SEC
AXIAL POSITION	1.01794E+00 SQ CM	AXIAL POSITION	1.00000E+31 SQ CM
AREA		AREA	1.01794E+00 SQ CM
FLOW PROPERTIES		FLOW PROPERTIES	
PRESSURE	1.6237 ATM	PRESSURE	1.6237 ATM
VELOCITY	17817.93 CM/SEC	VELOCITY	17817.93 CM/SEC
TEMPERATURE	124.7136 K	TEMPERATURE	124.7136 K
DENSITY	2.04959E-03 GM/CC	DENSITY	2.04959E-03 GM/CC
FLOW RATE	3.77909E+01 GM/SEC	FLOW RATE	3.77909E+01 GM/SEC
ENTROPY	*35757 CAL/GM-K	ENTROPY	*35757 CAL/GM-K
MACH NUMBER	*49330	MACH NUMBER	*49330
GAMMA	1.65853	GAMMA	1.65853
CHEMICAL PROPERTIES		CHEMICAL PROPERTIES	
SPECIES	MOLE FRACTION	SPECIES	MOLE FRACTION
BR2	8.09013E-03	BR2	8.09235E-03
BR	2.19775E-03	BR	2.19370E-03
XE	9.88912E-01	XE	9.88914E-01
MIXTURE MOLECULAR WEIGHT	131.44060	MIXTURE MOLECULAR WEIGHT	131.44089

## APPENDIX C

TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GHZ/SEC)	2.46251E+05	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GHZ/SEC)	2.46209E+05
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000
<pre> 11/28/75 LRC LCOPS INDEPNUT 6639B-13IK 01/21/750 15.53.30.GT05619.          LKC COMPUTER COMPLEX 15.53.31.JOB,1.00300,120000.002000. A4409 R 15.53.37.3274 100681 B-1250 15.53.31.USER. ALLEN G. MCCLAIN. 0005 15.53.31.89803N 64730 15.53.31.MA1G0. PLEASE RUN ON 6600 ONLY 15.55.24.GO. 15.55.25.LINECN(10000) 15.55.26.FETCH(A4409,BINAY) 15.55.38.TIME BG ATTACH 15.56.41.*TIME ED ATTACH 15.56.42.END FETCH 15.56.43.UPDATE(LQ,C-TAPE4,P-BNFIL,E,D,8) 15.56.44.READING INPUT 15.57.03.UPDATE COMPLETE 15.57.03.UPDATE(Q,P-BNFIL) 15.57.11.READING INPUT 15.57.28.UPDATE COMPLETE 15.57.29.RUN(S,,COMPILE) 15.58.20.SETINDF. 15.58.21.LGO. 15.59.14.MEMORY 01100 CM 15.59.14.RFL 0000638 U/S CALLS 15.59.14.RFL CPU 29.169650 SEC. 15.59.31.STOP 15.59.32.SPRINT(OUTPUT,3) 15.59.35. 0000701 U/S CALLS 15.59.35.CPU 36.633872 SEC. → 15.59.35.PPU 182.190000 SEC. 15.59.37.COST OF THIS JOB HAS \$ 10 15.59.37.KMH 2.02 KILOMORD HOURS 17.02.09. GT05679. 7067 LINES PRINTED. LP20 </pre>			
<pre> 11/04/75 LRC LCOPS INDEPNUT 66000-13IK 01/21/750 13.48.27.GT05661.          LRC COMPUTER COMPLEX 13.48.27.1008,1.00300,120000.002000. A4409 R 13.48.27.3274 100681 B-1250 13.48.27.USER. ALLEN G. MCCLAIN. 0005 13.48.27.9803N 64730 13.48.28.LINECN(10000) 13.48.29.FETCH(A4409,BINAY) 13.49.15.TIME FG ATTACH 13.49.16.END FETCH 13.49.16.UPDATE(Q,-TAPE4,P-BNFIL,E,D,8) 13.49.20.READING INPUT 13.49.36.UPDATE COMPLETE 13.49.37.UPDATE(Q,P-BNFIL) 13.49.41.*READING INPUT 13.49.44.*UPDATE COMPLETE 13.49.48.RUN(S,,COMPILE) 13.50.20.SETINDF. 13.50.21.LGO. 13.50.47.MEMORY 066700 CM 13.50.47.RFL 0000517 O/S CALLS 13.50.47.RFL CPU 27.119152 SEC. 13.51.03.STOP 13.51.05.SPRINT(OUTPUT,3) ← 13.51.07. 0000580 O/S CALLS 13.51.07.CPU 35.07925 SEC. 13.51.07.RFL 139.53432 SEC. 13.51.08.O/S CALLS OF THIS JOB WAS \$ 10 13.51.08.KWH 2.49 KILOMORD HOURS 14.42.06. GT05661. 6337 LINES PRINTED. LP21 </pre>			

## Check Case 5

GENERAL CHEMICAL KINETICS PROGRAM  
DISTANCE-PRESSURE VERSION  
LANGLEY VERSION OF LEWIS PROGRAM (TN D-586)  
SOLUTION TECHNIQUE DEVELOPED BY C.W. GEAR  
NASA LANGLEY RESEARCH CENTER  
METHANE-AIR COMBUSTION AT CONSTANT P (ONE UNIMOLECULAR REACTION) CASE 5

REACTION NUMBER	REACTION	A	REACTION RATE VARIABLES	N	ACTIVATION ENERGY
1	$1\text{*CH}_4$	$3\text{-}80000\text{E+14}$	$1\text{*H}$	$0\text{.0000}$	$103000\text{.00}$
2	$1\text{*CH}_4$	$1\text{*C}_2$	$1\text{*CH}_3$	$1\text{*H}$	$630000\text{.00}$
3	$1\text{*H}$	$1\text{*O}_2$	$1\text{*CH}_2$	$\text{H}$	$-10000\text{.00}$
4	$1\text{*CO}$	$1\text{*O}_2$	$1\text{*CO}$	$1\text{*O}$	$41000\text{.00}$
5	$1\text{*CH}_3$	$1\text{*O}_2$	$1\text{*CH}_2\text{O}$	$1\text{*OH}$	$0\text{.0000}$
6	$1\text{*H}$	$1\text{*O}$	$1\text{*CH}_3$	$1\text{*H}$	$0\text{.0000}$
7	$1\text{*CH}_4$	$1\text{*CH}_4$	$1\text{*CH}_3$	$1\text{*H}$	$11800\text{.00}$
8	$1\text{*O}_2$	$1\text{*CH}_4$	$1\text{*CH}_3$	$1\text{*H}$	$92000\text{.00}$
9	$1\text{*H}$	$1\text{*O}_2$	$1\text{*CH}_3$	$1\text{*H}$	$5900\text{.00}$
10	$1\text{*O}$	$1\text{*H}_2$	$1\text{*OH}$	$1\text{*O}$	$16300\text{.00}$
11	$1\text{*H}_2$	$1\text{*OH}$	$1\text{*H}_2\text{O}$	$1\text{*H}$	$9800\text{.00}$
12	$1\text{*CO}$	$1\text{*OH}$	$1\text{*CO}_2$	$1\text{*H}$	$5100\text{.00}$
13	$1\text{*CH}_3$	$1\text{*OH}$	$1\text{*CH}_2\text{O}$	$1\text{*H}$	$1000\text{.00}$
14	$1\text{*CH}_2\text{O}$	$1\text{*H}$	$1\text{*HCO}$	$1\text{*H}$	$0\text{.0000}$
15	$1\text{*CH}_2\text{O}$	$1\text{*H}$	$1\text{*HCO}$	$1\text{*H}$	$2000\text{.00}$
16	$1\text{*CH}_2\text{O}$	$1\text{*O}$	$1\text{*HCO}$	$1\text{*OH}$	$0\text{.0000}$
17	$1\text{*HCO}$	$1\text{*O}$	$1\text{*CO}$	$1\text{*OH}$	$4000\text{.00}$
18	$1\text{*HCO}$	$1\text{*OH}$	$1\text{*CO}$	$1\text{*H}$	$0\text{.0000}$
19	$1\text{*HCO}$	$1\text{*H}$	$1\text{*CO}$	$1\text{*H}$	$0\text{.0000}$
20	$\text{M}$	$1\text{*HCO}$	$1\text{*CO}$	$1\text{*H}$	$28600\text{.00}$
21	$1\text{*HCO}$	$1\text{*O}_2$	$1\text{*CO}$	$1\text{*H}$	$5400\text{.00}$
22	$1\text{*HCO}_2$	$1\text{*H}_2$	$1\text{*H}_2\text{O}_2$	$1\text{*H}_2\text{O}$	$0\text{.0000}$
23	$1\text{*H}$	$1\text{*H}_2$	$1\text{*OH}$	$1\text{*OH}$	$0\text{.0000}$
24	$1\text{*O}$	$1\text{*H}_2$	$1\text{*OH}$	$1\text{*H}_2$	$0\text{.0000}$
25	$1\text{*OH}$	$1\text{*H}_2$	$1\text{*H}_2\text{O}$	$1\text{*H}_2$	$0\text{.0000}$
26	$\text{M}$	$1\text{*H}_2\text{O}_2$	$1\text{*OH}$	$1\text{*H}_2\text{O}$	$45500\text{.00}$
27	$1\text{*H}$	$1\text{*H}_2$	$1\text{*OH}$	$\text{M}$	$0\text{.0000}$
28	$\text{M}$	$1\text{*CO}$	$1\text{*O}$	$1\text{*OH}$	$-2\text{.6000}$
29	$1\text{*O}$	$1\text{*H}_2\text{O}$	$1\text{*OH}$	$1\text{*OH}$	$118700\text{.00}$
					$0\text{.0000}$

ALL THIRD BODY RATIOS ARE 1.0 EXCEPT THE FOLLOWING

M1CH <sub>4</sub>	M1CO	M1CO <sub>2</sub>	M1H <sub>2</sub> O	M1O <sub>2</sub>	M1H <sub>2</sub>	M1H <sub>2</sub> O <sub>2</sub>	M1O <sub>2</sub>	M1H <sub>2</sub> O	M1N <sub>2</sub>	M1O <sub>2</sub>	M1H <sub>2</sub> O	M1N <sub>2</sub>	M1O <sub>2</sub>	M1H <sub>2</sub> O	M1N <sub>2</sub>	
$1\text{*3)$	$5\text{.00000}$	$2\text{.00000}$	$1\text{.00000E-04}$	$2\text{.00000}$	$7\text{.50000}$	$1\text{.26)$	$7\text{.80000}$	$5\text{.00000}$	$1\text{.3)$	$1\text{.02)$	$1\text{.27)$	$1\text{.60000}$	$1\text{.3)$	$1\text{.02)$	$1\text{.27)$	$1\text{.3)$
$1\text{*31)$	$2\text{.00000}$	$1\text{.00000E-04}$	$1\text{.00000E-04}$	$1\text{.00000}$	$20\text{.00000}$	$1\text{.26)$	$6\text{.60000}$	$1\text{.00000}$	$1\text{.26)$	$1\text{.00000}$	$1\text{.26)$	$1\text{.00000}$	$1\text{.26)$	$1\text{.00000}$	$1\text{.26)$	$1\text{.00000}$
$1\text{*26)$	$6\text{.00000}$	$1\text{.00000E-04}$	$1\text{.00000E-04}$	$1\text{.00000}$	$271\text{.0}$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$	$1\text{.26)$
$1\text{*271)$	$1\text{.60000}$															

## INTEGRATION CONTROLS

MINIMUM STEP SIZE    2.00000E+01 CM  
INITIAL STEP SIZE    1.00000E+04 CM  
MAXIMUM RELATIVE ERROR    .00010

\*\*\* ASSIGNED VARIABLE PROFILE \*\*\*

PRESSURE (ATM)    1 = 1.0.    1X\*\*3 + 1.0.    1X\*\*2 + 1.0.    1X + (1.730000E-01)

\*\* INITIAL CONDITIONS \*\*

## APPENDIX C

TIME SEC	TIME SEC	TIME SEC
AXIAL POSITION CM	AXIAL POSITION CM	AXIAL POSITION CM
AREA SQ CM	SQ CM	SQ CM
0.	0.	0.
1.00000E+03	1.00000E+03	1.00000E+03

### FLOW PROPERTIES

PRESSURE	1.17300	ATM
VELOCITY	1.57412	.62 CM/SEC
TEMPERATURE	1.645	.0000 K
DENSITY	3.01559E-04	GM/CC
FLOW RATE	5.69139E+04	GM/SEC
ENTROPY	2.13077	CAL/GM-K
MACH NUMBER	2.00000	
GAMMA	1.27772	

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CH4	4.97680E-02	-5.08397E-06	CH4	4.97680E-02	-5.08397E-06
CH3	0.	5.08397E-06	CH3	0.	5.08397E-06
H	0.	5.01454E-06	H	0.	5.01454E-06
O2	1.99072E-01	-6.05166E-08	O2	1.99072E-01	-6.05166E-08
H2O	0.	6.94238E-08	H2O	0.	6.94238E-08
CO	0.	0.	CO	0.	0.
CO2	0.	0.	CO2	0.	0.
D	0.	1.85618E-10	D	0.	1.85618E-10
CH2O	0.	0.	CH2O	0.	0.
OH	0.	0.	OH	0.	0.
H2	0.	0.	H2	0.	0.
H2O	0.	0.	H2O	0.	0.
HCO	0.	0.	HCO	0.	0.
H2O2	0.	7.51160E-01	H2O2	0.	7.51160E-01
N2	0.	0.	N2	0.	0.

### MIXTURE MOLECULAR WEIGHT

28.21038

### FLOW PROPERTIES

TIME SEC	TIME SEC	TIME SEC
AXIAL POSITION CM	AXIAL POSITION CM	AXIAL POSITION CM
AREA SQ CM	SQ CM	SQ CM
1.05133E+06	1.05133E+06	1.05133E+06

### MASS FRACTION SUM

1.00000

TIME SEC	TIME SEC	TIME SEC
AXIAL POSITION CM	AXIAL POSITION CM	AXIAL POSITION CM
AREA SQ CM	SQ CM	SQ CM
1.03161E+03	1.03161E+03	1.03161E+03

PRESSURE	1.59919E-04	ATM
VELOCITY	1.57412	.62 CM/SEC
TEMPERATURE	1.611	.2161 K
DENSITY	4.55813E-04	GM/CC
FLW RATE	5.69139E+04	GM/SEC

### FLOW PROPERTIES

PRESSURE	1.57412	.62 CM/SEC
VELOCITY	1.671	.27425 K
TEMPERATURE	3.55909E-03	GM/CC
DENSITY	5.69139E+04	GM/SEC
FLW RATE	1.01616E+03	GM/SEC

## APPENDIX C

ENTROPY  
MACH NUMBER  
GAMMA

2.13913 CAL/GM-K  
1.98449  
1.27713

ENTROPY  
MACH NUMBER  
GAMMA

2.13913 CAL/GM-K  
1.98449  
1.27713

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CH4	4.58362E-02	-8.26286E-04	CH4	4.59385E-02	-8.26221E-04
CH3	3.25902E-04	6.90444E-05	CH3	3.23845E-04	6.89711E-05
H	1.29144E-06	5.10105E-07	H	1.29170E-06	5.10177E-07
O2	1.95297E-01	-8.03038E-04	O2	1.95297E-01	-8.03038E-04
HO2	2.62066E-05	1.01754E-05	HO2	2.62165E-05	1.01572E-05
CO	1.36761E-04	0.13838E-05	CO	1.36765E-04	0.13672E-05
CO2	6.82819E-07	3.55544E-07	CO2	6.82914E-07	3.55336E-07
O	2.29273E-06	7.29443E-07	O	2.29276E-06	7.29269E-07
C+20	2.46017E-05	6.94931E-04	C+20	2.46055E-03	6.94911E-04
OH	8.42844E-06	2.01349E-06	OH	8.42595E-06	2.01184E-06
H2	6.67891E-05	2.19615E-05	H2	6.67894E-05	2.19610E-05
H2O	3.81395E-03	8.25422E-04	H2O	3.81434E-03	8.25414E-04
HO	1.20770E-06	5.67770E-07	HO	1.20775E-06	5.67552E-07
N2	9.35077E-09	6.77955E-09	N2	9.35205E-09	6.78315E-09
	7.51024E-01	0.		7.51024E-01	0.

MIXTURE MOLECULAR WEIGHT  
TOTAL ENERGY EXCHANGE RATE  
(CAL-CM3/GM2/SEC)

28.20528  
-4.05011E+08  
1.00000

TIME  
AXIAL POSITION  
AREA

2.41404E-04 SEC  
3.80000E+01 CM  
1.11238E+03 SQ CM

MIXTURE MOLECULAR WEIGHT  
TOTAL ENERGY EXCHANGE RATE  
(CAL-CM3/GM2/SEC)

28.20528  
-4.04996E+08  
1.00000

TIME  
AXIAL POSITION  
AREA

2.41404E-04 SEC  
3.80000E+01 CM  
1.11238E+03 SQ CM

FLOW PROPERTIES

PRESSURE  
1.7300 ATM  
VELOCITY  
1818.32008 CM/SEC  
TEMPERATURE  
3.42042E-04 K  
DENSITY  
5.69139E+04 GM/CC  
FLOW RATE  
2.18611 GM/SEC  
ENTROPY  
1.89111 CAL/GM-K  
MACH NUMBER  
GAMMA

1.41404E-04 SEC  
3.80000E+01 CM  
1.11238E+03 SQ CM

MIXTURE MOLECULAR WEIGHT  
TOTAL ENERGY EXCHANGE RATE  
(CAL-CM3/GM2/SEC)

28.20528  
-4.04996E+08  
1.00000

TIME  
AXIAL POSITION  
AREA

2.41404E-04 SEC  
3.80000E+01 CM  
1.11238E+03 SQ CM

CL-0, PROPERTIES

PRESSURE  
1.7300 ATM  
VELOCITY  
1818.32008 CM/SEC  
TEMPERATURE  
3.42042E-04 K  
DENSITY  
5.69139E+04 GM/CC  
FLOW RATE  
2.18611 GM/SEC  
ENTROPY  
1.89111 CAL/GM-K  
MACH NUMBER  
GAMMA

1.41404E-04 SEC  
3.80000E+01 CM  
1.11238E+03 SQ CM

CL-0, PROPERTIES

PRESSURE  
1.7300 ATM  
VELOCITY  
1818.32008 CM/SEC  
TEMPERATURE  
3.42042E-04 K  
DENSITY  
5.69139E+04 GM/CC  
FLOW RATE  
2.18611 GM/SEC  
ENTROPY  
1.89111 CAL/GM-K  
MACH NUMBER  
GAMMA

1.41404E-04 SEC  
3.80000E+01 CM  
1.11238E+03 SQ CM

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CH4	2.38776E-02	-1.27534E-02	CH4	2.38636E-02	-1.26732E-02
CH3	4.39133E-03	3.49235E-03	CH3	4.39105E-03	3.49521E-03
H	1.41780E-04	2.19200E-04	H	1.417844E-04	2.48755E-04
O2	1.72822E-01	-1.32944E-02	O2	1.72374E-01	-1.32319E-02
HO2	5.85550E-06	2.37251E-04	HO2	5.89297E-04	2.48904E-04
CO	7.01090E-03	8.30221E-03	CO	7.01015E-03	8.26889E-03
CO2	7.94553E-05	1.23307E-04	CO2	7.85705E-04	1.23826E-04
O	1.01175E-04	1.51401E-04	O	1.00510E-04	1.49584E-04
CH2O	1.30766E-02	6.75384E-04	CH2O	1.30997E-02	7.00694E-04
OH	2.72138E-04	3.96634E-04	OH	2.70305E-04	4.28220E-04
H2	2.38166E-03	2.30961E-03	H2	2.39499E-03	2.29438E-03
H2O	4.82445E-02	1.67788E-02	H2O	4.25105E-02	1.66884E-02
H2O2	1.28555E-04	1.59223E-04	H2O2	1.29155E-04	1.60529E-04
H2O2	1.61195E-06	1.74454E-07	H2O2	1.43660E-06	1.80371E-07
N2	7.46422E-01	0.	N2	7.46422E-01	0.

## APPENDIX C

MIXTURE MOLECULAR WEIGHT	28.03246	MIXTURE MOLECULAR WEIGHT	28.03260
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	-7.9731E+09	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	-7.9414E+09
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000
TIME	2.50933E-04 SEC	TIME	2.50933E-04 SEC
AXIAL POSITION	3.93000E+01 CM	AXIAL POSITION	3.96000E+01 CM
AREA	1.21292E+03 SQ CM	AREA	1.21277E+03 SQ CM
FLOW PROPERTIES			
PRESSURE	1.7300 ATM	PRESSURE	1.7100 ATM
VELOCITY	157412.62 CM/SEC	VELOCITY	157412.62 CM/SEC
TEMPERATURE	1960.5918E+ K	TEMPERATURE	1952.49182 K
DENSITY	2.9088E-04 GM/CC	DENSITY	2.9088E-04 GM/CC
FLOW RATE	5.69139E+04 GM/SEC	FLOW RATE	5.69139E+04 GM/SEC
ENTROPY	2.23128 CAL/GM-K	ENTROPY	2.23122 CAL/GM-K
MACH NUMBER	1.81528	MACH NUMBER	1.81583
GAMMA	1.27872	GAMMA	1.27873
CHEMICAL PROPERTIES			
SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CM <sup>2</sup> /SEC)	NET SPECIES PRODUCTION RATE (MOLES/CM <sup>2</sup> /SEC)
CH <sub>4</sub>	8.31137E-03	-2.03435E-02	1.32395E-13
CH <sub>3</sub>	7.99733E-03	9.97817E-04	8.00794E-03
H	8.20001E-04	2.33859E-03	9.12235E-04
O <sub>2</sub>	1.50991E-01	-3.91860E-02	1.51050E-01
HO <sub>2</sub>	6.193219E-04	-6.21122E-04	5.54066E-04
CO	2.24805E-02	3.327116E-02	2.24335E-02
CO <sub>2</sub>	5.09655E-06	1.65068E-03	5.06334E-04
O	6.18034E-04	2.21144E-03	6.47055E-04
CH <sub>2</sub> O	9.23084E-03	-1.32438E-02	0.26502E-03
DH	1.76113E-03	5.98944E-03	1.73996E-03
H <sub>2</sub>	5.59512E-03	4.181617E-03	5.58113E-03
H <sub>2</sub> O	5.26082E-02	4.98817E-02	5.25606E-02
HCO	3.12930E-06	3.18212CE-04	3.17364E-04
H <sub>2</sub> O <sub>2</sub>	6.04933E-07	-1.25814E-07	6.14553E-07
N <sub>2</sub>	7.38107E-01	0.	7.38142E-01
MIXTURE MOLECULAR WEIGHT	27.7216	MIXTURE MOLECULAR WEIGHT	27.72146
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	-3.07243E+10	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	-3.04127E+10
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000
TIME	2.54109E-04 SEC	TIME	2.54109E-04 SEC
AXIAL POSITION	4.00000E+01 CM	AXIAL POSITION	4.00000E+01 CM
AREA	1.29115E+03 SQ CM	AREA	1.29673E+03 SQ CM
FLOW PROPERTIES			
PRESSURE	1.7300 ATM	PRESSURE	1.7300 ATM
VELOCITY	157412.62 CM/SEC	VELOCITY	157412.62 CM/SEC
TEMPERATURE	2018.62431 K	TEMPERATURE	2016.51071 K
DENSITY	2.18732E-04 GM/CC	DENSITY	2.18844E-04 GM/CC
FLOW RATE	5.61139E+04 GM/SEC	FLOW RATE	5.61139E+04 GM/SEC
ENTROPY	2.26361 CAL/GM-K	ENTROPY	2.26315 CAL/GM-K
MACH NUMBER	1.75419	MACH NUMBER	1.75515
GAMMA	1.28042	GAMMA	1.29042

## APPENDIX C

### CHEMICAL PROPERTIES

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CH <sub>4</sub>	2.18565E-03	-1.39210E-02	C <sub>H</sub> <sub>4</sub>	2.20104E-03	
CH <sub>3</sub>	5.66219E-03	-1.88386E-02	C <sub>H</sub> <sub>3</sub>	6.71294E-03	
H	2.02894E-03	5.75116E-03			-1.37531E-12
O <sub>2</sub>	1.33922E-01	-6.41515E-02			-1.92221E-12
H <sub>2</sub>	2.02510E-04	-9.40159E-04	N <sub>2</sub>	2.00954E-03	5.66629E-03
CO	3.47166E-02	4.2808E-02	C <sub>O</sub>	1.34219E-01	-6.43431E-02
CO <sub>2</sub>	1.59060E-03	6.65321E-03	C <sub>O</sub> <sub>2</sub>	2.86585E-24	-9.50611E-14
O	2.37701E-03	1.15801E-02			4.25523E-02
CH <sub>2</sub> O	4.28719E-03	-1.65838E-02			3.42691E-02
OH	5.43216E-03	1.91430E-02			1.57501E-03
H <sub>2</sub>	6.34510E-03	-1.44710E-03	N <sub>2</sub>	4.32195E-03	2.33263E-03
H <sub>2</sub> O	6.94000E-02	6.11915E-02			1.97101E-02
HCO	3.33470E-04	-4.80585E-04			-1.35412E-03
H <sub>2</sub> O <sub>2</sub>	7.26137E-07	2.12739E-06			6.07855E-02
N <sub>2</sub>	7.31730E-01	0.			-6.75137E-04

### MIXTURE MOLECULAR WEIGHT

MIXTURE MOLECULAR WEIGHT	27.48066	MIXTURE MOLECULAR WEIGHT	27.48292
TOTAL ENERGY EXCHANGE RATE (CAL-C <sub>13</sub> /GM <sub>2</sub> /SEC)	-5.20843E+10	TOTAL ENERGY EXCHANGE RATE (CAL-C <sub>13</sub> /GM <sub>2</sub> /SEC)	-5.17694E+10
MASS FRACTION SUM	1.00000	MASS FRACTION SUM	1.00000

## Check Case 6

TIME-AREA VERSION      GENERAL CHEMICAL KINETICS PROGRAM      NASA LAWNLEY RESEARCH CENTER  
 LANGLEY VERSION OF LEWIS PROGRAM (TN D-6-861) USING STIFF ODE  
 SOLUTION TECHNIQUE DEVELOPED BY G.C.W. GEAR  
 METHANE - AIR COMBUSTION (ASSIGNED AREA - TIME INTEGRATION)      CASE 6

REACTION NUMBER	REACTION		REACTION RATE VARIABLES	
	A	N	ACTIVATION ENERGY	
1	$\text{CH}_4$	$\text{CH}_3$	$3.80000E+14$	0.0000
2	$\text{CH}_4$	$\text{CH}_3$	$1.00000E+13$	103000.00
3	$\text{H}$	$\text{H}_2$	$1.59200E+15$	63000.00
4	$\text{CO}$	$\text{CO}_2$	$0.0000$	-1000.00
5	$\text{CH}_3$	$\text{CH}_2\text{C}$	$1.60300E+13$	41000.00
6	$\text{H}$	$\text{CH}_3$	$1.5000E+10$	0.00
7	$\text{O}$	$\text{CH}_3$	$6.90000E+13$	11800.00
8	$\text{OH}$	$\text{CH}_3$	$2.00000E+13$	9200.00
9	$\text{H}$	$\text{H}_2$	$7.20000E+13$	5900.00
10	$\text{O}$	$\text{H}$	$0.0000$	16300.00
11	$\text{H}_2$	$\text{OH}$	$1.25000E+14$	16300.00
12	$\text{CO}$	$\text{CO}_2$	$2.90000E+13$	9800.00
13	$\text{CH}_3$	$\text{CH}_2\text{O}$	$2.10000E+13$	5100.00
14	$\text{CH}_2\text{O}$	$\text{H}$	$4.20000E+11$	1000.00
15	$\text{CH}_2\text{O}$	$\text{H}$	$1.90000E+13$	0.00
16	$\text{CH}_2\text{O}$	$\text{H}$	$1.00000E+13$	0.00
17	$\text{CH}_2\text{O}$	$\text{H}$	$7.00000E+10$	2000.00
18	$\text{H}_2\text{O}$	$\text{H}$	$7.00000E+10$	1000.00
19	$\text{H}_2\text{O}$	$\text{H}$	$1.80000E+11$	0.00
20	$\text{H}_2\text{O}$	$\text{H}$	$4.00000E+11$	0.00
21	$\text{H}_2\text{O}$	$\text{H}$	$4.00000E+11$	0.00
22	$\text{H}_2\text{O}$	$\text{H}$	$4.00000E+11$	0.00
23	$\text{H}_2\text{O}$	$\text{H}$	$4.00000E+11$	0.00
24	$\text{H}_2\text{O}$	$\text{H}$	$4.00000E+11$	0.00
25	$\text{H}_2\text{O}$	$\text{H}$	$4.00000E+12$	0.00
26	$\text{H}_2\text{O}$	$\text{H}$	$6.00000E+12$	0.00
27	$\text{H}_2\text{O}$	$\text{H}$	$1.17000E+17$	45500.00
28	$\text{H}_2\text{O}$	$\text{H}$	$7.50000E+23$	0.00
29	$\text{H}_2\text{O}$	$\text{H}$	$-2.60000$	118700.00
			$2.75000E+19$	
			$-1.00000$	
			$5.75000E+13$	

ALL THREE BODY RATIOS ARE 1.0 EXCEPT THE FOLLOWING

MICHA	$^{31}$	5.00000	M102	$^{31}$	2.00000	M102	$^{26}$	78000	M102	$^{27}$	1.60000
MICO	$^{31}$	2.00000	M102	$^{31}$	7.50000	M1H2	$^{31}$	5.30000	M1H2	$^{31}$	32.50000
M1H2	$^{26}$	1.60000	M1H20	$^{27}$	2.00000	M1H20	$^{26}$	6.60000	M1N2	$^{31}$	2.00000
M1N2	$^{27}$	1.60000									

### INTEGRATION CONTROLS

MINIMUM STEP SIZE	6.25000E-10 SEC	MAXIMUM STEP SIZE	1.25000E-06 SEC
INITIAL STEP SIZE	6.25000E-10 SEC	MAXIMUM RELATIVE ERROR	.000010

\*\* ASSIGNED VARIABLE PROFILE \*\*

THE AREA IS CALCULATED BY INTERPOLATION FROM THE FOLLOWING TABLE

STATION	AXIAL DISTANCE (CM)	AREA (CM $^2$ )
1	0.	10.00000E-02
2	50.00000E-01	10.00050E-02
3	10.00000E+00	10.03020E-02
4	15.00000E+00	10.04930E-02

## APPENDIX C

5	20.00000E+00
6	25.00000E+00
7	30.00000E+00
8	35.00000E+00
9	36.00000E+00
10	37.00000E+00
11	38.00000E+00
12	39.00000E+00
13	40.00000E+00
14	40.50000E+00
15	41.00000E+00
16	42.00000E+00

\*\* INITIAL CONDITIONS \*\*

TIME SEC	TIME SEC	TIME SEC
AXIAL POSITION CM	AXIAL POSITION CM	AXIAL POSITION CM
AREA SQ CM	AREA SQ CM	AREA SQ CM
0.	0.	0.
1.00000E+03	1.00000E+03	1.00000E+03

FLOW PROPERTIES

PRESSURE	1.7300	ATM
VELOCITY	1574.12.62	CM/SEC
TEMPERATURE	1645.0000	K
DENSITY	3.61550E-04	GM/CC
FLOW RATE	5.69139E+04	CM/SEC
ENTROPY	2.13077	CAL/GM-K
MACH NUMBER	2.00000	
GAMMA	1.27772	

FLOW PROPERTIES

PRESSURE	1.7300	ATM
VELOCITY	1574.12.62	CM/SEC
TEMPERATURE	1645.0000	K
DENSITY	3.61550E-04	GM/CC
FLOW RATE	5.69139E+04	CM/SEC
ENTROPY	2.13077	CAL/GM-K
MACH NUMBER	2.00000	
GAMMA	1.27772	

CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	MIXTURE PRODUCTION RATE (MOLES/CC-SEC)	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CH4	4.97680E-02	-5.08370E-06	4.97630E-02	-5.08339E-06
Cr3	0.	5.08390E-06	0.	5.08397E-06
H	0.	5.01444E-06	0.	5.01454E-06
C2	1.99072E-01	-6.95166E-08	1.99072E-01	-6.95166E-08
H2	0.	6.94238E-08	0.	6.94238E-08
CG	0.	0.	0.	0.
CO2	0.	0.	0.	0.
O	0.	1.85618E-10	0.	1.85619E-10
Cr2O	0.	0.	0.	0.
CH	0.	0.	0.	0.
H2	0.	0.	0.	0.
H2O	0.	0.	0.	0.
HCO	0.	0.	0.	0.
H2O2	0.	0.	0.	0.
N2	7.51160E-01	0.	7.51160E-01	0.

MIXTURE MOLECULAR WEIGHT	28.21038
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	4.05133E+06
MASS FRACTION SUM	1.00000

MIXTURE MOLECULAR WEIGHT	28.21038
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)	4.05133E+06
MASS FRACTION SUM	1.00000

## APPENDIX C

TIME	1.90582E-04	SEC		TIME	1.90582E-04	SEC	
AXIAL POSITION	3.0000E+01	CN		AXIAL POSITION	3.0000E+01	CN	
AREA	1.02832E+03	SQ CM		AREA	1.02832E+03	SQ CM	
<b>FLOW PROPERTIES</b>							
PRESSURE	1.7300	ATM		PRESSURE	1.7300	ATM	
VELOCITY	1574.13	CM/SEC		VELOCITY	1574.13	CM/SEC	
TEMPERATURE	1.690.19471	K		TEMPERATURE	1.690.19471	K	
DENSITY	3.1600E-04	GM/CC		DENSITY	3.1600E-04	GM/CC	
FLOW RATE	5.69139E+04	GM/SEC		FLOW RATE	5.69139E+04	GM/SEC	
ENTROPY	2.14503	CAL/GM-K		ENTROPY	2.14503	CAL/GM-K	
MACH NUMBER	1.97302			MACH NUMBER	1.97302		
GAMMA	1.27678			GAMMA	1.27678		
<b>CHEMICAL PROPERTIES</b>							
SPECIES	MOLE FRACTION			NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)			
CH4	4.29476E-02			-1.57163E-03			
CH3	0.12561E-04			1.85626E-04			
H	4.13952E-06			2.21811E-06			
O2	1.92442E-01			-1.53445E-03			
H2O	7.36540E-05			3.21742E-05			
CO	4.44440E-04			2.21395E-04			
CO2	2.60442E-06			1.45027E-06			
O	5.91879E-06			2.56913E-06			
CH2O	5.73320E-03			1.16009E-03			
OH	1.77416E-05			1.03174E-05			
H2	1.72616E-04			7.46127E-05			
H2O	6.72031E-03			1.60801E-03			
HCO	4.41962E-06			2.46606E-06			
H2O2	6.21163E-08			4.84032E-08			
N2	7.50818E-01			0.			
<b>MIXTURE MOLECULAR WEIGHT</b>							
TIME	2.19754						
TOTAL ENERGY EXCHANGE RATE	-7.76338E+08						
(CAL-CM3/GM2/SEC)							
MASS FRACTION SUM	1.00000						
<b>FLOW PROPERTIES</b>							
PRESSURE	1.7300	ATM		PRESSURE	1.7300	ATM	
VELOCITY	1735.80559	CM/SEC		VELOCITY	1735.80559	CM/SEC	
TEMPERATURE	1.735.80559	K		TEMPERATURE	1.735.80559	K	
DENSITY	3.42056E-04	GM/CC		DENSITY	3.42056E-04	GM/CC	
FLOW RATE	5.69139E+04	GM/SEC		FLOW RATE	5.69139E+04	GM/SEC	
ENTROPY	2.15903	CAL/GM-K		ENTROPY	2.15903	CAL/GM-K	
MACH NUMBER	1.94640			MACH NUMBER	1.94640		
GAMMA	1.27628			GAMMA	1.27628		
<b>CHEMICAL PROPERTIES</b>							
SPECIES	MOLE FRACTION			NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)			
CH4	3.61125E-02			-4.42845E-03			
<b>FLOW PROPERTIES</b>							
PRESSURE	1.7300	ATM		PRESSURE	1.7300	ATM	
VELOCITY	1735.80559	CM/SEC		VELOCITY	1735.80559	CM/SEC	
TEMPERATURE	1.735.80559	K		TEMPERATURE	1.735.80559	K	
DENSITY	3.42056E-04	GM/CC		DENSITY	3.42056E-04	GM/CC	
FLOW RATE	5.69139E+04	GM/SEC		FLOW RATE	5.69139E+04	GM/SEC	
ENTROPY	2.15903	CAL/GM-K		ENTROPY	2.15903	CAL/GM-K	
MACH NUMBER	1.94640			MACH NUMBER	1.94640		
GAMMA	1.27628			GAMMA	1.27628		
<b>CHEMICAL PROPERTIES</b>							
SPECIES	MOLE FRACTION			NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)			
CH4	3.61128E-02			-4.42845E-03			

## APPENDIX C

CH3	1.68287E-03						
H	2.33464E-05	8.61069E-04	1.68332E-03	2.33357E-05	8.59903E-04	2.20172E-05	
O2	1.85538E-01	2.02245E-05	-4.38417E-03	1.85367E-01	-4.38435E-03		
H2O	2.56555E-04	4.38417E-03	1.7689E-04	2.5729E-04	1.3579E-04		
CO	1.97045E-03	1.3782E-03	1.3782E-03	1.6726E-03	1.37822E-03		
CO2	1.39398E-05	1.13446E-05	1.67788E-05	1.39728E-05	1.13664E-05		
C2H	2.39028E-05	1.67788E-05	2.15669E-03	1.39815E-05	1.67628E-05		
CH2O	9.87650E-03	5.91814E-05	3.90675E-05	9.83311E-03	2.15736E-03		
OH	6.72523E-04	4.20292E-04	4.87361E-03	6.73021E-04	4.41865E-04		
H2O	1.38855E-02	4.87361E-03	2.15298E-05	1.38925E-02	4.85830E-03		
CO	2.13047E-07	4.30475E-07	7.15225E-01	2.10936E-05	4.10711E-07		
H2O2	5.15225E-07	4.30475E-07	0.	5.18036E-07	4.10711E-07		
N2	7.49862E-01	0.	7.49862E-01	0.	0.		
MIXTURE MOLECULAR WEIGHT							
		28.16162				28.16158	
TOTAL ENERGY EXCHANGE RATE							
		-2.26827E+09	(CAL-CM3/GM2/SEC)			-2.26866E+09	
MASS FRACTION SUM							
		1.00000				1.00000	
TIME							
		2.54109E-04	SEC			2.54109E-04	SEC
AXIAL POSITION							
		4.00003E-01	CM			1.9995E+01	CM
AREA							
		1.29664E+03	SQ CM			1.29655E+03	SQ CM
FLOW PROPERTIES							
PRESSURE	1.7311	ATM				1.7357	ATM
VELOCITY	157368.41	CM/SEC				157350.54	CM/SEC
TEMPERATURE	2076.68536	K				2092.84429	K
DENSITY	2.78821E-04	GM/CC				2.79232E-04	GM/CC
FLOW RATE	5.69139E04	GM/SEC				5.69245E+04	GM/SEC
ENTROPY	2.26347	CAL/GM-K				2.26412	CAL/GM-K
MACH NUMBER	1.75375					1.75375	
GAMMA	1.28038					1.28038	
CHEMICAL PROPERTY RATES							
SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE	SPECIES	MOLE FRACTION
CH4	2.21248E-03	-1.40216E-02	CH4	2.10663E-03	2.10663E-03	CH4	5.58011E-03
CH3	5.65544E-03	-1.79905E-02	CH3	5.79923E-03	-1.35265E-02	CH3	2.04811E-03
H	2.01047E-03	5.74300E-03	H	2.04865E-03	2.04865E-03	C2	1.33636E-03
O2	1.30044E-01	-6.45030E-02	O2	1.27716E-01	-6.54155E-02	O2	2.77514E-01
CO2	2.83884E-04	-9.62762E-06	CO2	3.45761E-02	4.2269E-02	CO2	1.61267E-02
CO	3.40586E-02	4.25487E-02	CO	1.61267E-02	6.93361E-03	C2H	1.21891E-02
C2	1.57981E-03	6.57912E-03	C2H	2.41513E-03	4.20929E-02	C2H	4.20929E-03
O	2.36793E-03	1.15102E-02	O	2.41513E-03	-1.65466E-02	O	5.501819E-03
CH2O	4.31781E-03	-1.66202E-02	CH2O	4.20929E-03	2.04519E-02	CH2O	7.27519E-03
OH	5.30042E-03	1.97998E-02	OH	6.33614E-03	-1.65495E-03	OH	6.10209E-02
H2	6.34734E-03	-1.41261E-03	H2	6.33614E-03	6.10209E-02	H2	3.79473E-03
H2O	6.92203E-02	6.10209E-02	H2O	6.97039E-02	-6.10209E-02	H2O	7.27519E-03
CO	3.87689E-04	-6.84237E-04	CO	3.79473E-03	2.57139E-06	CO	1.31633E-01
H2O2	7.11304E-07	2.44901E-06	H2O2	7.27519E-07	1.31633E-01	H2O2	0.
MIXTURE MOLECULAR WEIGHT							
		27.48257				27.47702	
TOTAL ENERGY EXCHANGE RATE							
		-5.16937E+10	(CAL-CM3/GM2/SEC)			-5.16904E+10	
MASS FRACTION SUM							
		1.00000				1.00000	

## APPENDIX C

## Check Case 8

TIME-AREA VERSION      GENERAL CHEMICAL KINETICS PROGRAM      NASA Langley Research Center  
 Langley Version of Lewis Program (TN D-6386) Using stiff ODE  
 Solution Technique Developed by C. W. Gear

## H2-O2 LOW TEMPERATURE REACTION AT CONSTANT VOLUME (ADJUSTED RATES) C-8

REACTION NUMBER	REACTION	A	REACTION RATE VARIABLES
1	1*H2 + 1*O2 = 1*OH + 1*H2O	1.0000E+14	0.0000 ACTIVATION ENERGY
2	1*H2 + 1*O2 = 1*OH + 1*H2O	2.10000E+13	67000.00
3	1*H + 1*O = 1*OH + 1*H	1.25000E+14	5100.00
4	1*O + 1*O = 2*OH	2.96000E+13	16300.00
5	1*H + 1*O2 = 1*HO2 + 1*H	8.50000E+14	9800.00
6	1*H + 1*HO2 = 1*OH + 1*OH	7.00000E+13	-1000.00
7	1*H + 1*HO2 = 1*OH + 1*OH	1.17000E+17	0.0000
8	1*H2O2 + 1*H2O = 1*H2O2 + 1*H2	1.00000E+12	45500.00
9	1*H2O2 + 1*H2 = 1*H2O2 + 1*H	1.00000E+12	0.0000
10	1*H2O2 + 1*OH = 1*H2O + 1*OH	3.18000E+14	24000.00
11	1*H2O2 + 1*OH = 1*H2O + 1*OH	1.00000E+13	9000.00
12	1*H2O2 + 1*OH = 1*H2O + 1*OH	5.75000E+13	18000.00

ALL THIRD BODY RATIOS ARE 1.0 EXCEPT THE FOLLOWING

M(H2)	* 5) =	5.000000	M(H2)	* 7) =	2.300000	M(O2)	* 5) =	2.000000	M(O2)	* 7) =	.78000
M(H2O)	* 5) =	32.500000	M(H2O)	* 7) =	6.000000	M(H2O2)	* 7) =	6.000000	M(H2O2)	* 7) =	5.750000

## INTEGRATION CONTROLS

MINIMUM STEP SIZE      5.00000E-05 SEC  
 INITIAL STEP SIZE      5.00000E-05 SEC

MAXIMUM STEP SIZE      1.000000E-01 SEC  
 MAXIMUM RELATIVE ERROR      .00030

\*\* ASSIGNED VARIABLE PROFILE \*\*

THIS IS A V=0 PROBLEM - AN ASSIGNED VARIABLE IS NOT REQUIRED

THE VOLUME (DENSITY) WILL BE HELD CONSTANT FOR THIS CASE

THE TEMPERATURE WILL BE HELD CONSTANT FOR THIS CASE

## APPENDIX C

\*\* INITIAL CONDITIONS \*\*

## APPENDIX C

TIME AXIAL POSITION AREA	0. 0. 1.00000E+00	SEC CM SQ CM	TIME AXIAL POSITION AREA	0. 0. 1.00000E+00	SEC CM SQ CM
<b>FLOW PROPERTIES</b>					
PRESSURE	*6579	ATM	PRESSURE	.6579	ATM
VELOCITY	0.00	CM/SEC	VELOCITY	0.00	CM/SEC
TEMPERATURE	773.15000	K	TEMPERATURE	773.15000	K
DENSITY	6.44320E-05	GM/CC	DENSITY	6.44320E-05	GM/CC
FLOW RATE	0.	GM/SEC	FLOW RATE	0.	GM/SEC
ENTROPY	6.76838	CAL/GM-K	ENTROPY	6.76838	CAL/GM-K
MACH NUMBER	0.00000		MACH NUMBER	0.00000	
GAMMA	1.38099		GAMMA	1.38099	
<b>CHEMICAL PROPERTIES</b>					
SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
H2	8.60000E-01	-1.48936E-16	H2	8.60000E-01	-1.48936E-16
O2	1.40000E-01	-1.48936E-16	O2	1.40000E-01	-1.48936E-16
H	0.	1.48936E-16	H	0.	1.48936E-16
HO2	0.	1.48936E-16	HO2	0.	1.48936E-16
OH	0.	0.	OH	0.	0.
H2O	0.	0.	H2O	0.	0.
O	0.	0.	O	0.	0.
H2O2	0.	0.	H2O2	0.	0.
MIXTURE MOLECULAR WEIGHT					
		6.21325			6.21325
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/CM2/SEC)					
		2.04835E-03			2.04835E-03
MASS FRACTION SUM					
		1.00000			1.00000
<b>FLOW PROPERTIES</b>					
PRESSURE	*6579	ATM	PRESSURE	.6579	ATM
VELOCITY	0.00	CM/SEC	VELOCITY	0.00	CM/SEC
TEMPERATURE	773.15000	K	TEMPERATURE	773.15000	K
DENSITY	6.44320E-05	GM/CC	DENSITY	6.44320E-05	GM/CC
FLOW RATE	0.	GM/SEC	FLOW RATE	0.	GM/SEC
ENTROPY	6.76838	CAL/GM-K	ENTROPY	6.76838	CAL/GM-K
MACH NUMBER	0.00000		MACH NUMBER	0.00000	
GAMMA	1.38099		GAMMA	1.38099	
<b>FLOW PROPERTIES</b>					
PRESSURE	*6579	ATM	PRESSURE	.6579	ATM
VELOCITY	0.00	CM/SEC	VELOCITY	0.00	CM/SEC
TEMPERATURE	773.15000	K	TEMPERATURE	773.15000	K
DENSITY	6.44320E-05	GM/CC	DENSITY	6.44320E-05	GM/CC
FLOW RATE	0.	GM/SEC	FLOW RATE	0.	GM/SEC
ENTROPY	6.76838	CAL/GM-K	ENTROPY	6.76838	CAL/GM-K
MACH NUMBER	0.00000		MACH NUMBER	0.00000	
GAMMA	1.38099		GAMMA	1.38099	

CHEMICAL PROPERTIES					
SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
H2	8.5000E-01	-1.2246E-14	H2	9.6000E-01	-1.4170E-14
O2	1.0000E-01	-1.2392E-14	O2	1.4000E-01	-1.4321E-14
H	1.0108E-14	3.8057E-19	H	1.17015E-14	4.36892E-19
HO2	7.1522E-11	2.68112E-15	HO2	0.27395E-11	3.8676E-15
OH	3.3946E-17	1.37390E-21	OH	2.9766E-17	4.54205E-21
H2O	5.0003E-11	2.38470E-15	H2O	6.12511E-11	2.79077E-15
Q	1.0105E-16	3.08825E-21	Q	1.16771E-16	4.38231E-21
H2O2	2.0016E-10	8.51919E-15	H2O2	2.35896E-10	9.83962E-15
MIXTURE MOLECULAR WEIGHT					
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)		-9.67218E-02	MIXTURE MOLECULAR WEIGHT		6.21325
MASS FRACTION SUM		1.00000	TIME ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)		-1.12233E-01
TIME AXIAL POSITION AREA	5.50000E+01	SEC CM SQ CM	TIME AXIAL POSITION AREA	5.50000E+01	SEC CM SQ CM
TIME AXIAL POSITION AREA	0.00000E+00	1.00000E+00	MASS FRACTION SUM	1.00000	
FLOW PROPERTIES					
PRESSURE	* 6444	ATM	PRESSURE	* 6443	ATM
VELOCITY	0.00	CM/SEC	VELOCITY	0.00	CM/SEC
TEMPERATURE	773.1500	K	TEMPERATURE	773.1500	K
DENSITY	6.44320E-05	GM/CC	DENSITY	6.44320E-05	GM/CC
FLOW RATE	0.	GM/SEC	FLOW RATE	0.	GM/SEC
ENTROPY	6.72769	CAL/GM-K	ENTROPY	6.72737	CAL/GM-K
MACH NUMBER	0.00000		MACH NUMBER	0.00000	
GAMMA	1.37565		GAMMA	1.37562	
CHEMICAL PROPERTIES					
SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
H2	8.3738E-01	-1.29231E-08	H2	8.37240E-01	-1.29193E-08
O2	1.2204E-01	-6.40021E-09	O2	1.21906E-01	-6.46455E-09
H	9.2753E-01	-5.38189E-14	H	9.27814E-09	-6.75851E-12
HO2	6.9193E-06	5.26911E-14	HO2	6.91917E-06	6.82906E-12
OH	1.7985E-10	5.00423E-14	OH	1.79881E-10	1.72275E-12
H2O	3.49376E-02	1.29598E-08	H2O	3.96297E-02	1.29224E-08
Q	8.29587E-11	-1.05702E-15	Q	8.29334E-11	3.82336E-18
H2O2	1.21796E-03	-2.80672E-12	H2O2	1.21758E-03	-4.01829E-12
MIXTURE MOLECULAR WEIGHT					
TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)		-1.79930E+05	MIXTURE MOLECULAR WEIGHT		6.34396
MASS FRACTION SUM		1.00000	TIME ENERGY EXCHANGE RATE (CAL-CM3/GM2/SEC)		-1.79944E+05
TIME AXIAL POSITION AREA	7.50000E+01	SEC CM SQ CM	TIME AXIAL POSITION AREA	7.50000E+01	SEC CM SQ CM

## APPENDIX C

### FLCW PROPERTIES

PRESSURE	-6362	ATM
VELOCITY	0.0	CM/SEC
TEMPERATURE	773.15000	K
DENSITY	6.44320E-05	GM/CC
FLOW RATE	0.	CM/SEC
ENTROPY	6.69235	CAL/GM-K
MACH NUMBER	0.00000	
GAMMA	1.37253	

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
H2	8.22418E-01	-1.27922E-08
O2	1.10740E-01	-6.38349E-09
H	9.33698E-09	-9.88363E-15
H02	7.00003E-06	-2.54685E-14
OH	1.88848E-10	9.62671E-15
H2O	6.56383E-02	1.28195E-08
O	7.71320E-11	1.27307E-16
H2O2	1.19672E-03	-2.72307E-11

### MIXTURE MOLECULAR WEIGHT

6.42463  
TOTAL ENERGY EXCHANGE RATE -1.78257E+05  
(CAL-CM3/GM2/SEC)

MASS FRACTION SUM 1.00000

TIME	1.20000E+02	SEC
AXIAL POSITION	0.	CM
AREA	1.00000E+00	SQ CM

### FLCW PROPERTIES

PRESSURE	* 6187	ATM
VELOCITY	0.00	CM/SEC
TEMPERATURE	773.15000	K
DENSITY	6.44320E-05	GM/CC
FLOW RATE	0.	CM/SEC
ENTROPY	6.60429	CAL/GM-K
MACH NUMBER	0.00000	
GAMMA	1.36576	

### FLOW PROPERTIES

PRESSURE	8.22279E-01	ATM
VELOCITY	1.10635E-01	CM/SEC
TEMPERATURE	9.33808E-09	K
DENSITY	6.99833E-06	GM/CC
FLOW RATE	1.16801E-10	CM/SEC
ENTROPY	6.59827E-02	CAL/GM-K
MACH NUMBER	1.28115E-06	
GAMMA	1.19593E-03	

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
H2	7.88804E-01	-1.17383E-08
O2	8.55376E-02	-5.84890E-09
H	9.62950E-09	1.10515E-14
H02	6.92048E-06	-1.06095E-13
OH	1.90355E-10	4.28070E-14
H2O	1.24502E-01	1.17790E-08
O	6.40241E-11	-2.61371E-15
H2O2	1.06983E-03	-4.04054E-11

PRESSURE	7.88763E-01	ATM
VELOCITY	8.54473E-02	CM/SEC
TEMPERATURE	9.63284E-09	K
DENSITY	6.9198E-06	GM/CC
FLOW RATE	1.90633E-10	CM/SEC
ENTROPY	1.26714E-01	CAL/GM-K
MACH NUMBER	6.39881E-11	
GAMMA	1.06893E-03	

### MIXTURE MOLECULAR WEIGHT

6.60670

### MIXTURE MOLECULAR WEIGHT

6.42538

### MIXTURE MOLECULAR WEIGHT

6.60736

## APPENDIX C

TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GH2 SEC)	-1.63667E+05	TOTAL ENERGY EXCHANGE RATE (CAL-CM3/GH2 SEC)	-1.63589E+05
MASS FRACTION SUM	.99999	MASS FRACTION SUM	.99999
11/19/75 LRC ICOPS INDEPDNT 66000-131K C1/21/750 17.42.09. GTO2854. LRC COMPUTER COMPLEX 17.42.09. JOB,1,00300,129000,002000. A440Y R 17.42.09. 3274 100611 8-1250 17.42.09. USER. ALLEN G. MCCLAIN 0005 17.42.09. 89803N 64301 17.42.09. WAITGO. PLEASE RUN ON 6600 ONLY 17.42.13. GO. 17.42.13. LINECNT(10000) 17.42.14. FECHTA4409.,BINARY) 17.42.19. T ME BG ATTACH 17.42.55. T ME ED ATTACH 17.42.56. END FECH 17.42.57. UPDATE(IQ,C=APF4,p=HNFFILE,D,9) 17.43.00. READING INPUT 17.43.09. UPDATE COMPLETE 17.43.10. UPDATE(IQ,p=BFILE) 17.43.13. READING INPUT 17.43.19. UPDATE COMPLETE 17.43.20. RUN(SA,COMPILE) 17.43.43. SETINDF. 17.43.44. LGC. 17.44.52. MEMORY 071100 CM 17.44.52. QDUS557 O/S CALLS 17.44.52. REL CPU 21.758539 SEC 17.45.21. STOP 17.45.25. SPRINT(OUTPUT,3) 17.45.26. QDUS636 O/S CALLS 17.45.26. CPU 46.955029 SEC. → 17.45.26. PPU 125.710336 SEC. 17.45.27. COST OF THIS JOB WAS \$ 11 17.45.27. KILOWORD HOURS 2.74 20.38.21. GTO2854. 6513 LINES PRINTED. LP24		11/17/75 LRC ICOPS INDEPDNT 6630B-131K 01/21/750 19.56.31. LRC COMPUTER COMPLEX 19.56.31. JOB,1,00300,129000,002000. A4409 R 19.56.31.3274 100631 B-1250 19.56.31. USER. ALLEN G. MCCLAIN 0005 19.56.31. 89803N 64301 19.56.31. LINECNT(10000) 19.56.32. FECHTA4409.,BINARY) 19.56.38. TIME BG ATTACH 19.58.25. TIME ED ATTACH 19.58.26. END FECH 19.58.27. UPDATE(IQ,C=APF4,p=BFILE,D,9) 19.58.31. READING INPUT 19.58.41. UPDATE COMPLETE 19.58.42. UPDATE(IQ,p=BFILE) 19.58.47. READING INPUT 19.58.52. UPDATE COMPLETE 19.58.53. RUN(SA,COMPILE) 19.59.44. SETINDF. 19.59.45. LGO. 20.00.15. MEMORY 066700 CM 20.00.15. REL 0000539 O/S CALLS 20.00.15. REL CPU 27.098794 SEC. 20.01.30. STOP 20.01.30. SPRINT(OUTPUT,3) 20.01.32. 0000578 O/S CALLS 20.01.32. CPU 67.0982836 SEC. ← 20.01.32. PPU 204.13464 SEC. 20.01.32. COST OF THIS JOB WAS \$ 12 20.01.32. KWH 2.99 KILOWORD HOURS 21.05.33. GTO5666. 6288 LINES PRINTED. LP24	

## APPENDIX D

# STOICHIOMETRIC PROPANE-OXYGEN-ARGON SHOCK TUBE COMBUSTION CASE COMPARISON

Comparison of the stoichiometric propane-oxygen-argon shock tube combustion cases is presented in this appendix. The output from the program of this paper is on the left-hand side of each page and the output from the program of NASA TN D-6586 is on the right-hand side.

**GENERAL CHEMICAL KINETICS PROGRAM** NASA LANGLEY RESEARCH CENTER  
**LANGLEY VERSION OF LEWIS PROGRAM (TN D-6586) USING STIFF ODE**  
**SOLUTION TECHNIQUE DEVELOPED BY C.W. GEAR**

\*\*\*\*\* PROpane REACTIONS BY CHINITZ - BAURER 64 RXNS - 31 SPECIES \*\*\*\*\*

REACTION NUMBER	REACTION					REACTION RATE VARIABLES		
	A	B	C	D	E	F	G	H
1	1*CO	+	1*O2	=	1*O	+	1*CO2	1.60000E+13
2	H	+	1*C3H8	=	1*C2H5	+	1*CH3	1.00000E+15
3	1*O4	+	1*H2	=	1*H2O	+	1*H	2.20000E+13
4	1*O	+	1*H2	=	1*OH	+	1*H	1.80000E+10
5	1*H	+	1*OH	=	1*H2O	+	M	7.50000E+23
6	1*C	+	1*H2O	=	1*OH	+	1*OH	5.80000E+13
7	1*H	+	1*H	=	1*H2	+	M	1.00000E+18
8	1*H2	+	1*O2	=	1*OH	+	1*OH	1.70000E+13
9	1*CO	+	1*O	=	1*CO2	+	M	4.00000E+13
10	1*H	+	1*O2	=	1*OH	+	1*O	2.20000E+14
11	1*O4	+	1*CO	=	1*CO2	+	1*H	5.60000E+11
12	M	+	1*O2	=	1*O	+	1*O	2.60000E+19
13	M	+	1*CH4	=	1*CH3	+	1*H	4.00000E+17
14	1*CH4	+	1*O	=	1*OH	+	1*CH3	2.03000E+13
15	1*CH4	+	1*H	=	1*CH3	+	1*H2	6.90000E+13
16	1*CH4	+	1*OH	=	1*CH3	+	1*H2O	2.80000E+13
17	1*CH3	+	1*O	=	1*CH2O	+	1*H	1.95000E+13
18	M	+	1*CH2O	=	1*H2	+	1*CO	2.10000E+16
19	1*HCJ	+	1*OH	=	1*CO	+	1*H2O	2.00000E+13
20	M	+	1*HCO	=	1*H4	+	1*CO	2.00000E+12
21	1*CH2D	+	1*OH	=	1*CO	+	1*H2O	2.00000E+13
22	1*CH3	+	1*O2	=	1*C42O	+	1*O4	1.20000E+12
23	1*C3H8	+	1*OH	=	1*C3H7	+	1*H2O	1.00000E+11
24	1*C3H8	+	1*O	=	1*C2H6	+	1*CH2O	1.00000E+12
25	1*C3H8	+	1*H	=	1*C3H7	+	1*H2	3.60000E+12
26	1*C3H7	+	1*O	=	1*C2H6CO	+	1*H	8.80000E+11
27	1*C3H7	+	1*O	=	1*C3H6	+	1*OH	9.80000E+11
28	1*C347	+	1*OH	=	1*C3H6	+	1*H2O	9.80000E+17
29	1*C3H7	+	1*O2	=	1*C2H5CO	+	1*OH	1.00000E+11
30	1*C346	+	1*O2	=	1*CH3CHO	+	1*CH2O	9.80000E+13
31	1*C3H6	+	1*OH	=	1*CH3CHO	+	1*CH3	8.10000E+17
32	1*C3H6	+	1*O	=	1*C3H4	+	1*H2O	8.10000E+11
33	1*C3H6	+	1*O	=	1*C42O	+	1*CH24	8.10000E+11
34	1*C3H4	+	1*O2	=	1*CH3CO	+	1*HCO	1.00000E+11
35	1*C246	+	1*O	=	1*C2H5	+	1*O4	9.80000E+11
36	1*C246	+	1*OH	=	1*C2H5	+	1*H2O	8.90000E+10
37	1*C2H6	+	1*H4	=	1*C2H5	+	1*H2	2.00000E+12
38	1*C246CO	+	1*OH	=	1*C2H5CO	+	1*H2O	9.60000E+13
39	1*C2H6CO	+	1*H	=	1*C2H5CO	+	1*H2	3.50000E+12
40	1*C2H5CO	+	1*O	=	1*C2H5	+	1*CO2	9.00000E+11
41	1*C2H5CO	+	1*OH	=	1*C2H5OH	+	1*CO	9.00000E+13
42	1*C2H5CO	+	1*O2	=	1*C2H4OH	+	1*CO2	1.00000E+11
43	1*C2H5CO	+	1*H	=	1*C2H5	+	1*HCO	3.33000E+12
44	1*C2H5OH	+	1*H	=	1*C2H5	+	1*H2O	3.00000E+12
45	1*C2H4OH	+	1*H	=	1*C2H5	+	1*OH	3.00000E+12
46	1*C2H5	+	1*O2	=	1*CH3CHO	+	1*OH	1.10000E+11
47	1*C2H5	+	1*O	=	1*C2H4	+	1*OH	8.80000E+11
48	1*C2H5	+	1*O	=	1*CH3CHO	+	1*H	8.80000E+11
49	1*C2H5	+	1*OH	=	1*C2H4	+	1*H2O	8.90000E+10
50	1*CH3CHO	+	1*OH	=	1*CH3CO	+	1*H2O	6.50000E+10
51	1*CH3CHO	+	1*H	=	1*CH3CO	+	1*H2	2.40000E+12
52	1*CH3CO	+	1*	=	1*CH3	+	1*CO2	6.10000E+11
53	1*CH3CO	+	1*O2	=	1*CH2O	+	1*CO2	7.90000E+13
54	1*CH3CO	+	1*OH	=	1*CH3O	+	1*CO	6.20000E+12
55	1*CH3CO	+	1*	=	1*C43	+	1*HCO	2.20000E+12
56	1*CH3OH	+	1*H	=	1*CH3	+	1*H2O	2.30000E+12
57	1*CH2OH	+	1*H	=	1*CH3	+	1*O4	2.20000E+12
58	1*C2H4	+	1*O	=	1*CH3	+	1*HCO	3.00000E+13
59	1*C2H4	+	1*OH	=	1*C2H2	+	1*H2O	3.00000E+13
60	1*C2H4	+	1*OH	=	1*CH3	+	1*CH2O	1.00000E+11
61	1*C2H2	+	1*O	=	1*C2H	+	1*OH	3.40000E+15

## APPENDIX D

62	1*C2H2	+	1*OH	=	1*C2H	+	1*H2O		2.20000E+14	0.0000	7000.00
63	1*C2H	+	1*O2	=	1*CH	+	1*CO2		1.00000E+14	0.0000	23000.00
64	1*CH	+	1*O2	=	1*CO	+	1*OH		8.10000E+10	.5000	0.00

ALL THIRD BODY RATIOS ARE 1.0

### INTEGRATION CONTROLS

MINIMUM STEP SIZE	1.00000E-05 CM	MAXIMUM STEP SIZE	1.00000E-02 CM
INITIAL STEP SIZE	1.00000E-05 CM	MAXIMUM RELATIVE ERROR	.00010

\*\* ASSIGNED VARIABLE PROFILE \*\*

THE AREA IS CALCULATED FROM THE FOLLOWING FUNCTION

$$1/AREA = 1 - (X/ 136.700) * (.50000)$$

### \*\* EQUILIBRIUM SHOCK CALCULATION \*\*

INITIAL STATE	FINAL STATE	FINAL/INITIAL RATIO
---------------	-------------	---------------------

PRESSURE (ATM)	.0526	1.6543	31.4503
VELOCITY (CM/SEC)	167000.00	52127.85	.3121
DENSITY (GM/CM**3)	84.59816E-06	27.10239E-05	3.2037
TEMPERATURE (DEG K)	300.00	2855.91	9.5197
ENTROPY (CAL/GM/DEG K)	1.1175	1.2897	1.1541
MACH NUMBER	5.2328	.5877	.1123
GAMMA	1.6167	1.2721	.7869
SONIC VELOCITY (CM/SEC)	31913.93	88698.65	2.7793

SPECIES	MOLE FRACTION
CO	1.77123E-02
O2	8.88239E-03
O	4.89909E-03
CO2	1.13792E-02
C3H8	8.87498E-45
C2H5	1.87969E-29
CH3	7.14781E-15
OH	7.72594E-03
H2	5.87368E-03
H2O	2.61112E-02
H	5.88176E-03
CH4	3.09820E-16
CH20	9.73995E-11
HCO	1.54604E-08
C3H7	1.68281E-43
C2H6	1.42840E-30
C2H6CO	3.11108E-38
C3H6	6.63878E-38
CH3CHO	2.95174E-24
C3H4	1.71713E-32
C2H4	3.13129E-24
CH3CO	2.19280E-22
C2H5CO	1.11779E-36
C2H5OH	1.08320E-31
C2H4OH	7.53468E-30
CH2OH	6.14808E-16
CH3OH	9.98426E-18
C2H2	1.48022E-18
C2H	2.37942E-18
CH	3.59896E-14
AR	9.11534E-01

MIXTURE MOLECULAR WEIGHT	38.39300
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D(LOG VOLUME)/D(LOG T) AT CONSTANT P	1.1484E+00
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D(LOG VOLUME)/D(LOG P) AT CONSTANT T	-1.0069E+00
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## APPENDIX D

** FROZEN SHOCK CALCULATION **		FINAL STATE		FINAL/INITIAL RATIO	
INITIAL STATE					
PRESSURE (ATM)	.0526		1.8090		36.3915
VELOCITY (CM/SEC)	161000.00		41032.16		*245T
DENSITY (GM/CM**3)	84.59816E-06		34.43127E-05		4.0700
TEMPERATURE (DEG K)	300.00		2535.02		8.4501
ENTROPY (CAL/GM/DEG K)	1.1175		1.2342		1.1044
MACH NUMBER	5.2328		*54.1		.0868
GAMMA	1.6167		1.5338		*94.86
SODIC VELOCITY (CM/SEC)	31913.93		90362.15		2.8314
SPECIES MOLE FRACTION					
CO	0.	CO2	5.00000E-02		
O	0.	O2	0.		
C2H5	0.	C3H8	1.00000E-02		
CH3	0.	OH	0.		
H2	0.	H2O	0.		
H	0.	H+	0.		
CH4	0.	CH2O	0.		
HCO	0.	HCO	0.		
C3H7	0.	C2H6	0.		
C2H6CO	0.	C2H6CO	0.		
C3H6	0.	C3H5OH	0.		
C3H4	0.	C2H4	0.		
C2H3CO	0.	C2H5CO	0.		
C2H5OH	0.	C2H4OH	0.		
CH2OH	0.	CH2OH	0.		
CH3OH	0.	C2H2	0.		
C2H	0.	CH	0.		
AR	0.	Ar	9.40000E-01		
MIXTURE MOLECULAR WEIGHT	39.39194				
DLOG(VOLUME)/DLOG T	1.00000E+00				
AT CONSTANT P					
DLOG(VOLUME)/DLOG P	-1.00000E+00				
AT CONSTANT T					
** INITIAL CONDITIONS **					
TIME	0.	SFC	0.	SEC	
AXIAL POSITION	0.	CM	0.	CM	
AREA	1.00000E+00	SQ CM	1.00000E+00	SQ CM	

## APPENDIX D

### FLOW PROPERTIES

PRESSURE	1.9090 ATM
VELOCITY	4.10216 CM/SEC
TEMPERATURE	2535.01510 K
DENSITY	3.44310E-04 GM/CC
FLOW RATE	1.41279E+01 GM/SEC
ENTROPY	1.23416 CAL/GM-K
MACH NUMBER	4.5419
GAMMA	1.53362

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CO	7.	0.	-2.6365E-07
O2	5.07019E-02	0.	5.20739E-07
CO2	7.	0.	0.
C3H8	1.03000E-02	-2.43867E+00	-2.43867E+00
C2H5	7.	2.43867E+00	2.43867E+00
CH3	7.	2.43867E+00	2.43867E+00
H2	7.	0.	0.
H2O	0.	0.	0.
H	0.	0.	0.
CH4	0.	0.	0.
CH2O	0.	0.	0.
HCO	0.	0.	0.
C3H7	0.	0.	0.
C2H6	0.	0.	0.
C2H5CO	0.	0.	0.
C3H6	0.	0.	0.
CH3CHO	0.	0.	0.
C3H4	0.	0.	0.
C2H4	0.	0.	0.
CHC1	0.	0.	0.
C2H5CO	0.	0.	0.
C2H5OH	0.	0.	0.
CH2OH	0.	0.	0.
CH3OH	0.	0.	0.
C2H2	0.	0.	0.
C2H	0.	0.	0.
AR	0.	0.	0.

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION						
CO	7.	CO	0.	C2	5.00000E-02	CO2	0.
O2	5.07019E-02	C2	5.00000E-02	C2	5.00000E-02	C2H	0.
CO2	7.	C2	0.	C2H	0.	C3H8	1.00000E-02
C3H8	1.03000E-02	C2H	0.	C3H8	1.00000E-02	C2H5	0.
C2H5	7.	C3H8	0.	C2H5	0.	C2H5	0.
CH3	7.	C2H5	0.	CH3	0.	CH3	0.
H2	7.	CH3	0.	H2	0.	H2	0.
H2O	0.	H2	0.	H2C	0.	H2C	0.
H	0.	H2C	0.	CH4	0.	CH4	0.
CH4	0.	CH4	0.	CH2O	0.	CH2O	0.
CH2O	0.	CH2O	0.	HCO	0.	HCO	0.
C3H4	0.	HCO	0.	C3H7	0.	C3H7	0.
C2H4	0.	C3H7	0.	C2H6	0.	C2H6	0.
CHC1	0.	C2H6	0.	C2H5CO	0.	C2H5CO	0.
C2H5CO	0.	C2H5CO	0.	C3H6	0.	C3H6	0.
C2H5OH	0.	C3H6	0.	CH3CHO	0.	CH3CHO	0.
CH2OH	0.	CH3CHO	0.	C3H4	0.	C3H4	0.
CH3OH	0.	C3H4	0.	C2H4	0.	C2H4	0.
C2H2	0.	C2H4	0.	CH3CO	0.	CH3CO	0.
C2H	0.	CH3CO	0.	C2H5CO	0.	C2H5CO	0.
AR	0.	C2H5CO	0.	C2H5OH	0.	C2H5OH	0.
				CH2OH	0.	CH2OH	0.
				CH3OH	0.	CH3OH	0.
				C2H2	0.	C2H2	0.
				C2H	0.	C2H	0.
				CH	0.	CH	0.
				AR	9.40000E-01	AR	0.

### MIXTURE MOLECULAR WEIGHT

39.59194

### TOTAL ENERGY EXCHANGE RATE

1.6911E+12

### TOTAL ENERGY EXCHANGE RATE

{CAL-CM3/SEC}

### MASS FRACTION SUM

1.00000

### MIXTURE MOLECULAR WEIGHT

39.59194

### TOTAL ENERGY EXCHANGE RATE

{CAL-CM3/SEC}

### MASS FRACTION SUM

1.00000

### MIXTURE MOLECULAR WEIGHT

39.59194

TIME	AXIAL POSITION	TIME	AXIAL POSITION
1.26165E-05 SEC	5.00000E-02 CM	1.26106E-06 SEC	5.00000E-02 CM

### FLOW PROPERTIES

PRESSURE	1.8212 ATM
VELOCITY	4016.24 CM/SEC
TEMPERATURE	2518.32089 K
DENSITY	3.45100E-04 GM/CC
FLOW RATE	1.41294E+01 GM/SEC

## APPENDIX D

ENTROPY 1.24807 CAL/GM-K  
MACH NUMBER 4.4053  
GAMMA 1.55452

ENTROPY  
MACH NUMBER  
GAMMA

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CM <sup>2</sup> /SEC)	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CM <sup>2</sup> /SEC)
CO	1.01573E-03	1.23255E-02	CO	1.01431E-03
O2	4.00427E-02	-2.39274E-02	Q2	4.00440E-02
N	9.90509E-04	5.57039E-03	0	9.90190E-04
CO2	3.25137E-04	5.41066E-03	CO2	3.25511E-04
C3H6	1.33708E-06	-3.96444E-05	C3H8	1.33491E-06
C2H5	2.63119E-06	-7.22278E-03	C2H5	2.82779E-04
CH3	9.69471E-03	-1.16297E-02	CH3	8.69581E-03
DH	4.66332E-03	-1.21242E-02	DH	4.66509E-03
H2	1.24394E-03	1.25166E-02	H2	1.22303E-03
H20	2.28866E-03	1.85570E-02	H20	2.36719E-03
H	6.45316E-06	9.63028E-04	H	6.49247E-04
CH4	7.80496E-05	6.45130E-04	CH4	7.79931E-05
CH20	7.16395E-06	1.13777E-05	CH20	7.16611E-06
HCO	5.55127E-05	4.19527E-04	HCO	5.24862E-05
C3H7	7.60844E-07	-1.49437E-05	C3H7	7.61687E-07
C2H6	4.19672E-05	-5.91205E-06	C2H6	4.19711E-05
C2H6CO	4.49355E-06	7.58625E-06	C2H6CO	4.49867E-06
C3H6	9.36581E-06	1.15961E-05	C3H6	9.36510E-06
CH3CHO	1.17600E-03	-2.17636E-03	CH3CHO	7.17721E-03
C3H4	9.89536E-07	1.34747E-05	C3H4	9.87568E-07
C2H4	5.53151E-06	-1.34729E-03	C2H4	5.53490E-04
CH3C	4.50524E-04	2.16492E-03	CH3C	4.50378E-04
C2HCO	2.80989E-07	1.30143E-06	C2HCO	2.80859E-07
C2H5OH	5.05896E-07	1.346437E-06	C2H5OH	5.06019E-07
C2H4OH	7.89298E-06	2.25980E-05	C2H4OH	7.89420E-04
CH2OH	6.11641E-24	6.15439E-03	CH2OH	6.70968E-04
CH3OH	3.21562E-05	4.55611E-04	CH3OH	3.21083E-05
C2H2	4.30351E-05	4.19218E-04	C2H2	4.29866E-04
C2H	3.44361E-05	6.89609E-04	C2H	3.43544E-05
CH	2.02095E-06	7.52362E-05	CH	2.55421E-06
AR	9.29836E-01	0.	AR	9.29837E-01

### MIXTURE MOLECULAR WEIGHT

39.16384

TOTAL ENERGY EXCHANGE RATE  
(CAL-CM<sup>3</sup>/GM<sup>2</sup>/SEC)

-1.83772E+10

MASS FRACTION SUM

1.00000

### MIXTURE MOLECULAR WEIGHT

39.16389

TOTAL ENERGY EXCHANGE RATE  
(CAL-CM<sup>3</sup>/GM<sup>2</sup>/SEC)

-1.83695E+10

MASS FRACTION SUM

1.00000

TIME 1.17734E-05 SEC  
AXIAL POSITION 5.00000E-01 CM  
DISTANCE 1.06437E+00 SQ CM

TIME 1.17734E-05 SEC  
AXIAL POSITION 5.00000E-01 CM  
AREA 1.06437E+00 SQ CM

### FLOW PROPERTIES

TIME 1.17734E-05 SEC

AXIAL POSITION 5.00000E-01 CM

AREA 1.06437E+00 SQ CM

PRESSURE 1.7556 ATM  
VELOCITY 45051.41 CM/SEC  
TEMPERATURE 2804.2803 K  
DENSITY 2.94654E-04 GM/CC  
FLOW RATE 1.41291E+01 GM/SEC  
ENTROPY 1.27982 CAL/GM-K  
MACH NUMBER 4.6314  
GAMMA 1.56828

## CHEMICAL PROPERTIES

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## CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/C-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CO	1.49385E-02	0.28944E-03	CO	1.49333E-02	-6.30954E-03
CO2	1.71184E-22	-1.2570E-02	CO2	1.7925E-02	-1.2563E-02
O	3.20110E-23	2.04744E-23	O	3.2885E-03	2.03228E-03
O2	7.10253E-23	3.2855E-03	CO2	7.1000E-03	3.28691E-03
C2H2	2.65612E-09	-1.15644E-03	C3H8	2.6620E-09	-1.02469E-08
C3H8	9.77335E-06	-2.65171E-05	C2H5	9.79437E-06	-2.1036E-05
C2H5	3.11591E-03	-2.66055E-03	CH3	3.11898E-03	-2.66081E-03
CH3	6.24316E-03	2.77515E-03	OH	6.24055E-03	2.76287E-03
OH	4.65949E-03	3.82491E-04	H2	4.65922E-03	3.83339E-04
H2	2.93192E-12	1.11044E-22	H2O	2.03104E-02	1.11139E-02
H2O	2.66794E-23	2.82676E-03	H	2.66649E-03	2.64289E-03
H	1.45874E-04	-1.02195E-04	CH4	1.46036E-04	-1.27125E-04
CH4	3.65746E-06	1.37619E-05	CH2U	3.66702E-06	4.6910E-06
CH2O	8.31757E-05	-4.25016E-05	HC0	2.84415E-05	-4.69254E-05
HC0	1.02144E-09	-3.42221E-02	C3H7	1.02627E-05	3.4415E-09
C3H7	3.87016E-06	-9.49078E-06	C2H6	3.87300E-06	-9.9490E-06
C2H6	1.59176E-07	-7.61833E-07	C2H6CO	1.58899E-07	-7.5944E-07
C2H6CO	5.42093E-07	-2.05667E-06	C3H6	5.42401E-07	-2.07958E-06
C3H6	7.16770E-04	-2.25229E-03	C2H3CO	7.17622E-04	-2.25206E-03
C3H6	1.17761E-05	-1.77513E-06	C3H6	1.12931E-06	1.78721E-06
C2H4	1.13833E-05	-2.82555E-05	C2H4	1.13904E-05	2.3119E-05
C2H4	1.59292E-04	-3.99399E-04	C3H5	1.59935E-04	4.2625E-04
C2H5CO	3.51151E-09	-1.43995E-07	C2H5CO	3.51172E-07	1.452779E-07
C2H5CO	1.31051E-07	-3.76917E-07	C2H5OH	1.31332E-07	3.77019E-07
C2H5OH	5.74011E-05	-2.13018E-04	C2H4OH	5.74418E-05	2.12801E-04
C2H2O	1.67496E-03	-2.62318E-03	CH2OH	1.67701E-03	2.21546E-03
CH3OH	5.03166E-05	-1.26633E-04	CH3CH	5.04129E-05	1.26538E-04
CH2O	4.69266E-15	-2.10887E-05	C2H2	4.70228E-05	2.1142E-05
C2H2	4.66566E-05	-3.92245E-05	C2H	7.47389E-05	3.91730E-05
C2H	3.02408E-25	-9.67407E-06	AR	3.02434E-05	-9.68076E-06
AR	2.16129E-01	0.	AR	9.16716E-01	0.

MIXTURE MOLECULAR WEIGHT 38.61176  
TOTAL ENERGY EXCHANGE RATE -9.60115E+09  
(CAL-Cv3 GM2/SLC)  
MASS FRACTION SUM 1.00000

TIME 2.271133E-15 SEC  
AXIAL POSITION AREA 1.000001E+00 CM  
PRESSURE 1.000001E+00 CM  
TEMPERATURE 1.000001E+00 K  
DENSITY 1.000001E+00 GM/CC  
FLOW RATE 1.41201E+11 GM/SEC  
ENTROPY 1.29916 CAL/DM-K  
MACH NUMBER 4.5002 CAL/GM-K  
GAMA 1.57343

## FLUID PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/C-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CO	1.97936E-22	2.898687010E-02	CO	1.90793E-02	2.88669411E-02
O2	0.71334E-03	-3.62111E-04	O2	9.71627E-03	-3.60972E-04

## CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/C-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTION RATE (MOLES/CC-SEC)
CO	1.97936E-22	2.898687010E-02	CO	1.90793E-02	2.88669411E-02
O2	0.71334E-03	-3.62111E-04	O2	9.71627E-03	-3.60972E-04

## APPENDIX D

## APPENDIX D

C <sub>02</sub>	5.01222E-03	2.69692E-04	5.00146E-03	2.70800E-04
C <sub>3H8</sub>	9.70141E-03	5.2912E-04	9.6991E-03	9.4122E-04
C <sub>2H5</sub>	5.3035E-14	-5.1302E-12	4.0839E-14	3.50322E-13
C <sub>3H</sub>	5.18170E-09	-2.94837E-09	5.17872E-09	5.03411E-08
H	1.39104E-09	-4.07892E-04	1.39799E-04	1.09711E-04
H <sub>2</sub>	5.53020E-03	1.39179E-04	7.91284E-03	1.97361E-04
H <sub>20</sub>	2.06244E-02	3.46123E-04	5.62936E-03	3.49584E-04
H	6.95146E-02	6.24745E-04	2.60633E-02	7.15334E-05
C <sub>4H</sub>	7.29652E-06	6.24745E-04	5.00894E-03	6.26475E-04
C <sub>2H20</sub>	2.05724E-01	-7.31485E-07	-2.13472E-05	-2.13472E-05
H <sub>20</sub>	1.03220E-07	-3.93032E-07	-6.02122E-07	-6.02122E-07
C <sub>3H7</sub>	1.39104E-13	3.49930E-14	3.97791E-07	3.97791E-07
C <sub>2H6</sub>	1.40720E-08	-6.56428E-08	-2.77126E-13	-2.77126E-13
C <sub>2H16</sub>	2.06644E-12	-1.91254E-11	6.83328E-08	6.83328E-08
C <sub>2H4C0</sub>	2.06644E-12	-1.82104E-11	-1.76119E-11	-1.76119E-11
C <sub>3H6</sub>	1.67692E-11	-2.12454E-05	-1.00441E-11	-1.00441E-11
C <sub>3H10</sub>	4.06401E-07	-2.56403E-06	-2.56171E-06	-2.56171E-06
C <sub>3H4</sub>	2.25143E-09	-6.38217E-08	-6.00151E-08	-6.00151E-08
C <sub>2H8</sub>	7.68685E-09	-4.24136E-08	-4.23398E-08	-4.23398E-08
C <sub>3H7C0</sub>	1.35568E-07	-9.36921E-07	1.35622E-07	1.35622E-07
C <sub>2H12C0</sub>	6.55662E-13	-5.26937E-12	-5.27691E-12	-5.27691E-12
C <sub>2H20H</sub>	4.97656E-11	-2.15935E-10	-2.27188E-10	-2.27188E-10
C <sub>2H20H</sub>	9.41386E-09	-6.45613E-08	-6.37541E-08	-6.37541E-08
C <sub>2H30H</sub>	2.36002E-05	-9.44401E-05	-9.48842E-05	-9.48842E-05
C <sub>2H2</sub>	2.98407E-07	-9.47310E-07	-9.0132E-07	-9.0132E-07
C <sub>2H</sub>	1.96614E-05	-1.17322E-05	1.96894E-05	1.96894E-05
C <sub>H</sub>	3.10424E-05	-1.89541E-05	3.11009E-05	3.11009E-05
AR	1.65338E-05	-8.20404E-06	1.65446E-05	1.65446E-05
	9.11042E-01	0.	9.11044E-01	0.

### MIXTURE MOLECULAR WEIGHT

39.31227

TOTAL ENERGY EXCHANGE RATE  
(CAL-CM<sup>3</sup>/GM<sup>2</sup>/SEC)

-6.32030E+08

MASS FRACTION SUM

1.00000

TIME	3.38104E-05 SEC
AXIAL POSITION	1.50220E+00 CM
AREA	1.11701E+00 SQ CM

39.31227

TIME

AXIAL POSITION

AREA

1.00000

MIXTURE MOLECULAR WEIGHT  
TOTAL ENERGY EXCHANGE RATE  
(CAL-CM<sup>3</sup>/GM<sup>2</sup>/SEC)

3.37939E-05 SEC

TIME AXIAL POSITION AREA

1.50000E+00 CM

1.11701E+00 SQ CM

### FLOW PROPERTIES

PRESSURE	4407.55 ATM
VELOCITY	4407.55 CM/SEC
TEMPERATURE	2899.6116 K
DENSITY	2.942.00E-14 GM/CC
FLOW RATE	1.412711E+01 GM/SEC
ENTROPY	1.25943 CAL/GM-K
MACH NUMBER	4.4766
GAMMA	1.5733

PRESSURE

4407.55 ATM

VELOCITY

4407.55 CM/SEC

TEMPERATURE

2899.6116 K

DENSITY

2.942.00E-14 GM/CC

FLOW RATE

1.412711E+01 GM/SEC

ENTROPY

1.25943 CAL/GM-K

MACH NUMBER

4.4766

GAMMA

1.5733

### CHEMICAL PROPERTIES

SPECIES	MOLE FRACTION	NFT SPECIES PRODUCTN RATE (MOLES/CC-SEC)	SPECIES	MOLE FRACTION	NET SPECIES PRODUCTN RATE (MOLES/CC-SEC)
C <sub>O</sub>	1.84453E-02	-2.78412E-04	CO	1.86458E-02	-2.78863E-04
O <sub>2</sub>	9.15566E-13	-1.35476E-04	O <sub>2</sub>	9.15610E-03	-1.35799E-04
O	5.15440E-13	3.16533E-05	O	5.15533E-03	3.75375E-05
C <sub>O2</sub>	1.05732E-12	3.12059E-04	C <sub>O2</sub>	1.05727E-02	3.12779E-04
C <sub>3H8</sub>	2.00474E-16	-7.96691E-14	C <sub>3H8</sub>	1.53334E-11	-1.21523E-18
C <sub>2H5</sub>	2.51005E-12	3.94418E-12	C <sub>2H5</sub>	2.15577E-12	-1.06579E-11
C <sub>H3</sub>	1.33312E-01	-4.23114E-06	C <sub>H3</sub>	1.34424E-06	-4.27187E-16
OH	9.05170E-05	4.01336E-05	OH	8.03688E-03	4.02440E-05
H <sub>2</sub>	5.92662E-03	9.32311E-05	H <sub>2</sub>	5.90019E-03	9.34522E-05

## APPENDIX D

H	2.53055E-22	-1.5174E-04	H2O	2.58065E-02
C1H	6.01715E-23	-1.1390E-04	H	6.0176E-03
C1H2	C-5.9135E-09	-2.2247E-07	CH4	1.14219E-04
C1H2O	2.08615E-09	-6.1341E-09	CH2O	2.10054E-09
C1CO	1.77175E-09	-1.16173E-09	HC0	7.02074E-08
C3+1	9.44669E-17	1.06192E-15	C3H7	-6.35214E-09
C2+6	1.00906E-11	-4.96505E-11	C2H6	1.07755E-08
C2H6C0	1.04469E-11	-9.19391E-14	C2H6C0	1.20666E-19
C3H6	3.42003E-14	-9.62055E-13	C3H6	9.94139E-12
C3H6	6.46282E-11	-4.11778E-10	C3H6	1.12158E-18
C1CHU	3.50101E-10	-9.37265E-10	C1CH0	1.96659E-18
C2H4	*.30197E-11	-2.06204E-11	C2H4	7.87116E-16
C1CH0	6.67069E-11	-1.29422E-10	C1CH0	-2.1709E-15
C2H5C0	1.37017E-15	2.2599E-14	C2H5C0	-1.84939E-10
C2H5C0	2.23918E-14	-1.81255E-13	C2H5C0	9.91091E-10
C2H4O4	**.8679E-12	-3.40359E-11	C2H4O4	3.66455E-10
C1HOH	2.42361E-07	-7.81098E-07	C1HOH	1.25320E-11
C1HOH	2.39584E-09	-7.66633E-09	C1HOH	1.82277E-11
C2H2	8.11955E-06	-4.72616E-06	C2H2	4.98701E-11
C2H4	1.31919E-05	-7.51433E-05	C2H4	5.50762E-19
C1H	7.45668E-06	-4.10055E-06	C1H	4.17255E-18
AR	Q.10873E-01	0.	AR	7.92508E-14

MIXTURE MOLECULAR WEIGHT                    39.36516  
 TOTAL ENERGY EXCHANGE RATE                -9.05479E+01  
 (CAL-CM3/GM2/SEC)

MASS FRACTION SUM                          1.00000

MIXTURE MOLECULAR WEIGHT                    38.36518  
 TOTAL ENERGY EXCHANGE RATE                -8.07790E+07  
 (CAL-CM3/GM2/SEC)

MASS FRACTION SUM                          1.00000

11/26/75 LRC ICOPS INDEPNDT 6400A-131K 01/21/750  
 20.16.33. G10581. LRC COMPUTER COMPLEX  
 20.16.33. .008. ,01000.165000.002000. A4409 R  
 20.16.34. .3274 10068.1 8-1250 0005  
 20.16.34. USER. ALLEN G. MCCLAIN  
 20.16.34. 89803N 64730  
 20.16.34. WAITGO. PLEASE RUN ON 6400 ONLY  
 20.16.45.00.  
 20.16.46. LINECAT(10000)  
 20.16.46. FETCH(A4409) B6 ATTACH  
 20.17.03. TIME      B6 ATTACH  
 20.17.46. TIME      ED ATTACH  
 20.17.46. UPDATE(Q=C-TAPE4,P=BNFILE,D,B)  
 20.17.50. READING INPUT  
 20.17.50. UPDATE COMPLETE  
 20.18.00. UPDATE COMPLETE  
 20.18.00. UPDATE(Q=P=BNFILE)  
 20.18.04. READING INPUT  
 20.18.20. UPDATE COMPLETE  
 20.18.21. RUN(S,,COMPILE)  
 20.19.25. SETINDF.  
 20.19.26. LG0.  
 20.19.50. MEMORY 135400 CM  
 20.19.50. BNFILE 0000822 O/S CALLS  
 20.19.50. BNFILE 50.147417 SEC.

20.29.32. STOP  
 20.29.33. SPPRINT(OUTPUT,3)  
 20.29.34. 0000820 O/S CALLS  
 20.29.34. CPU 286.074664 SEC. ←  
 20.29.34. CPU 127.32160 SEC. ←  
 20.29.35. COST OF THIS JOB WAS \$ 27  
 20.29.35. KWH 0.66 KILOWATT HOURS  
 21.17.33. G105681. 8377 LINES PRINTED. LP25

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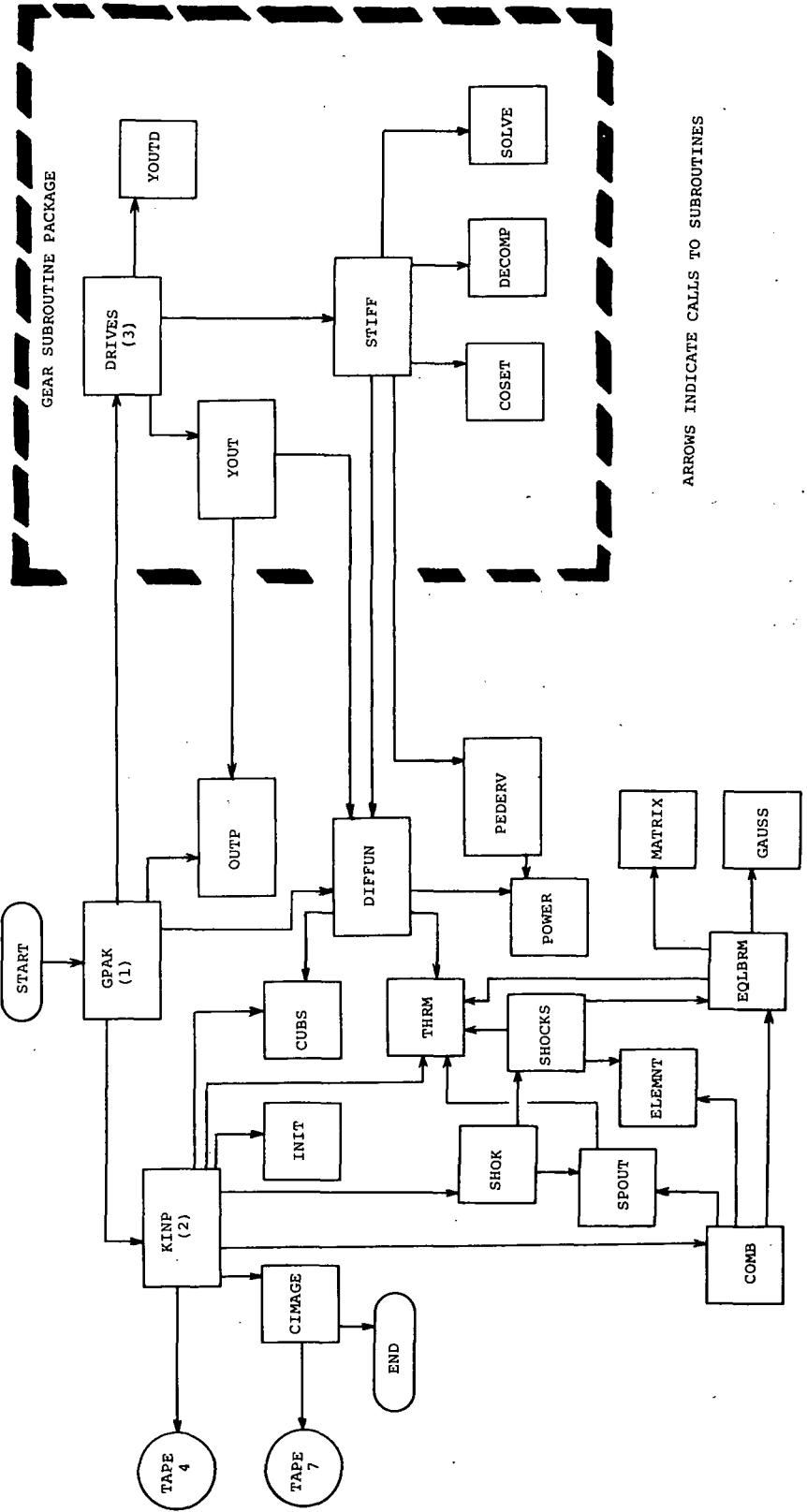


Figure 1.- Overall schematic of the hybrid computer program.

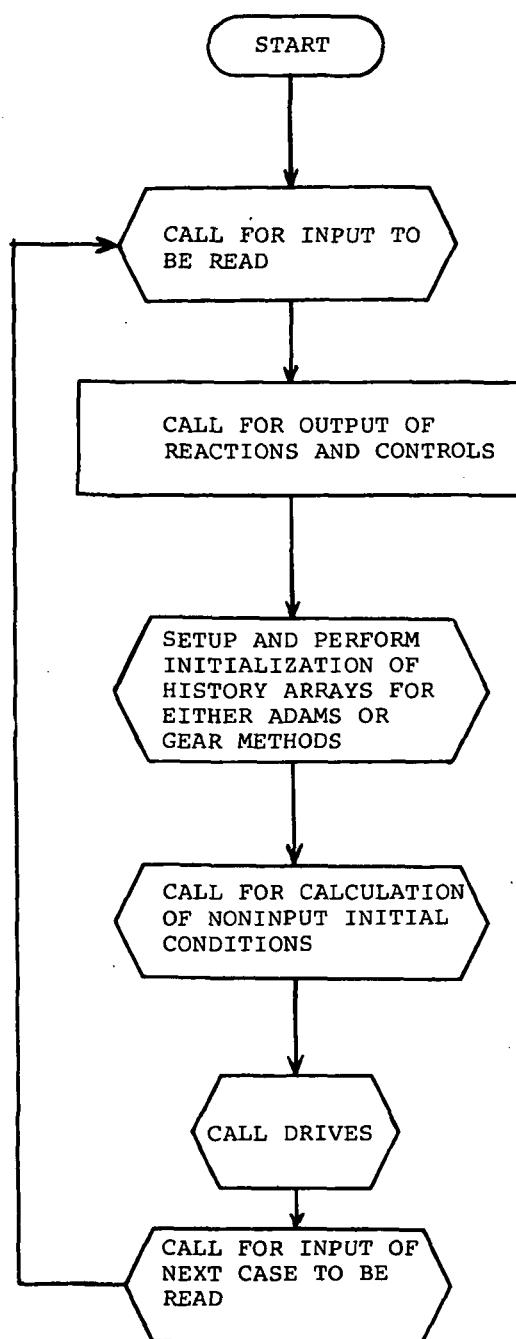


Figure 2.- Flow diagram for main program GPAK.

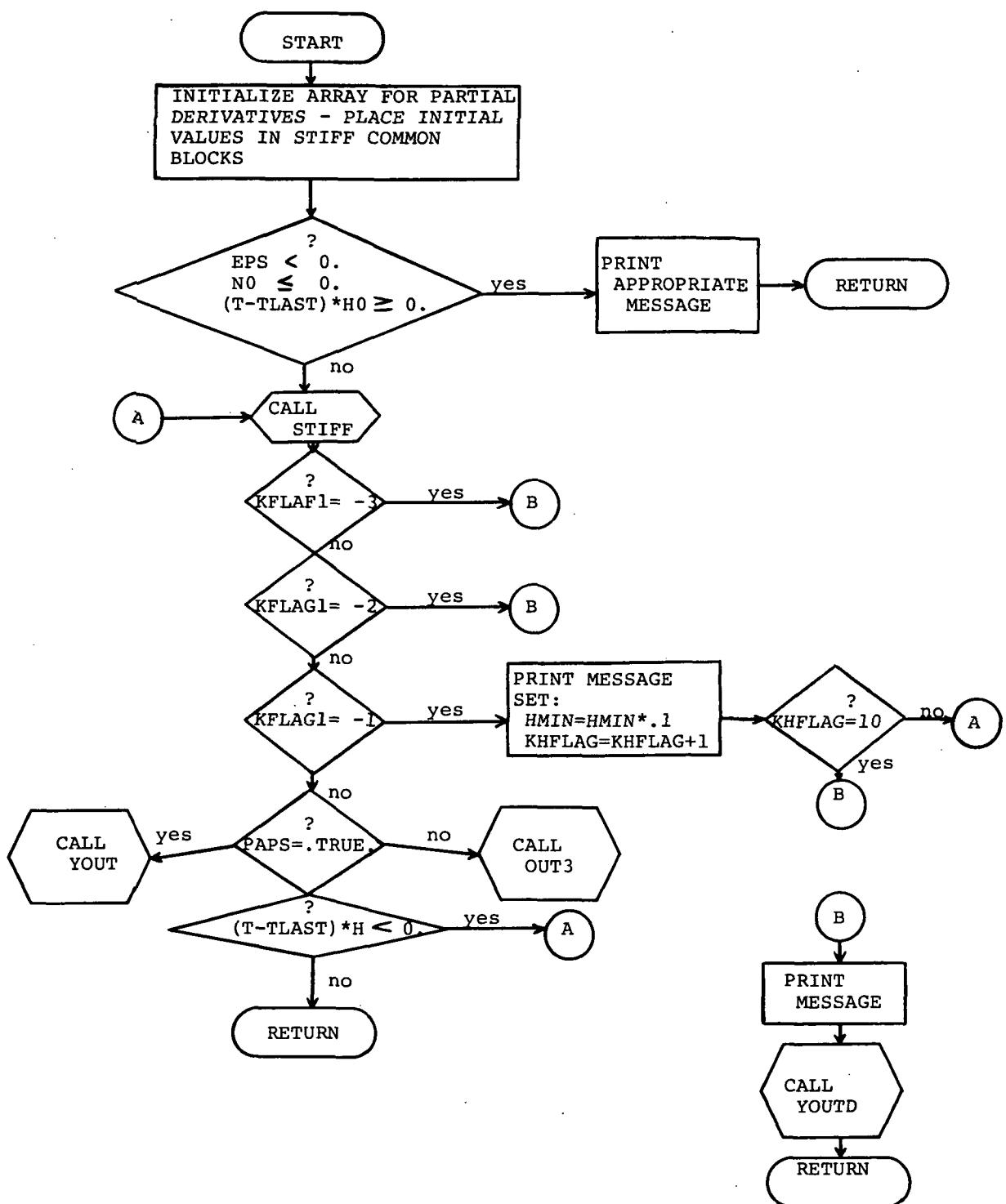


Figure 3.- Flow diagram for subroutine DRIVES.

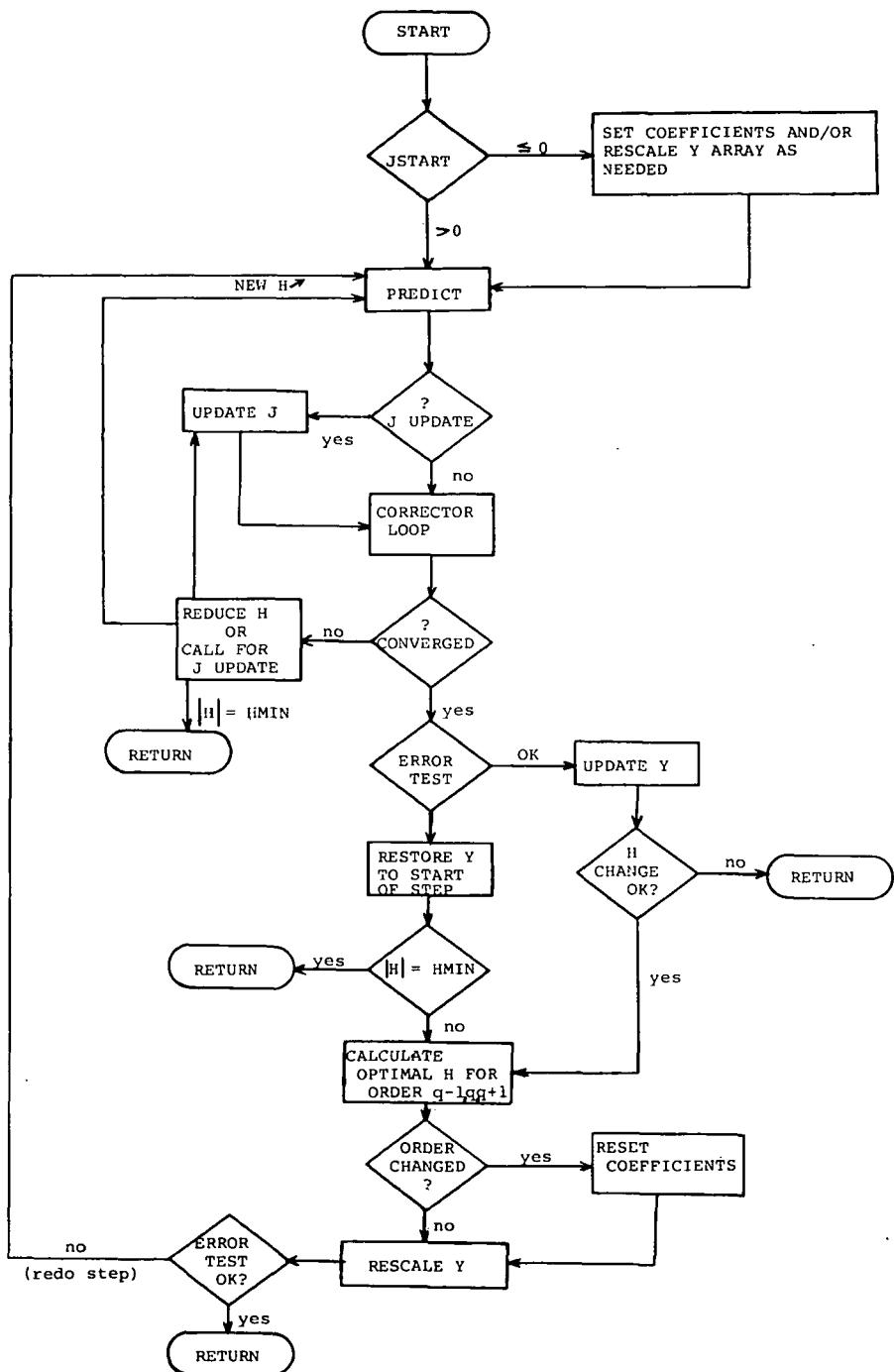


Figure 4.- Flow diagram of subroutine STIFF (from ref. 3).

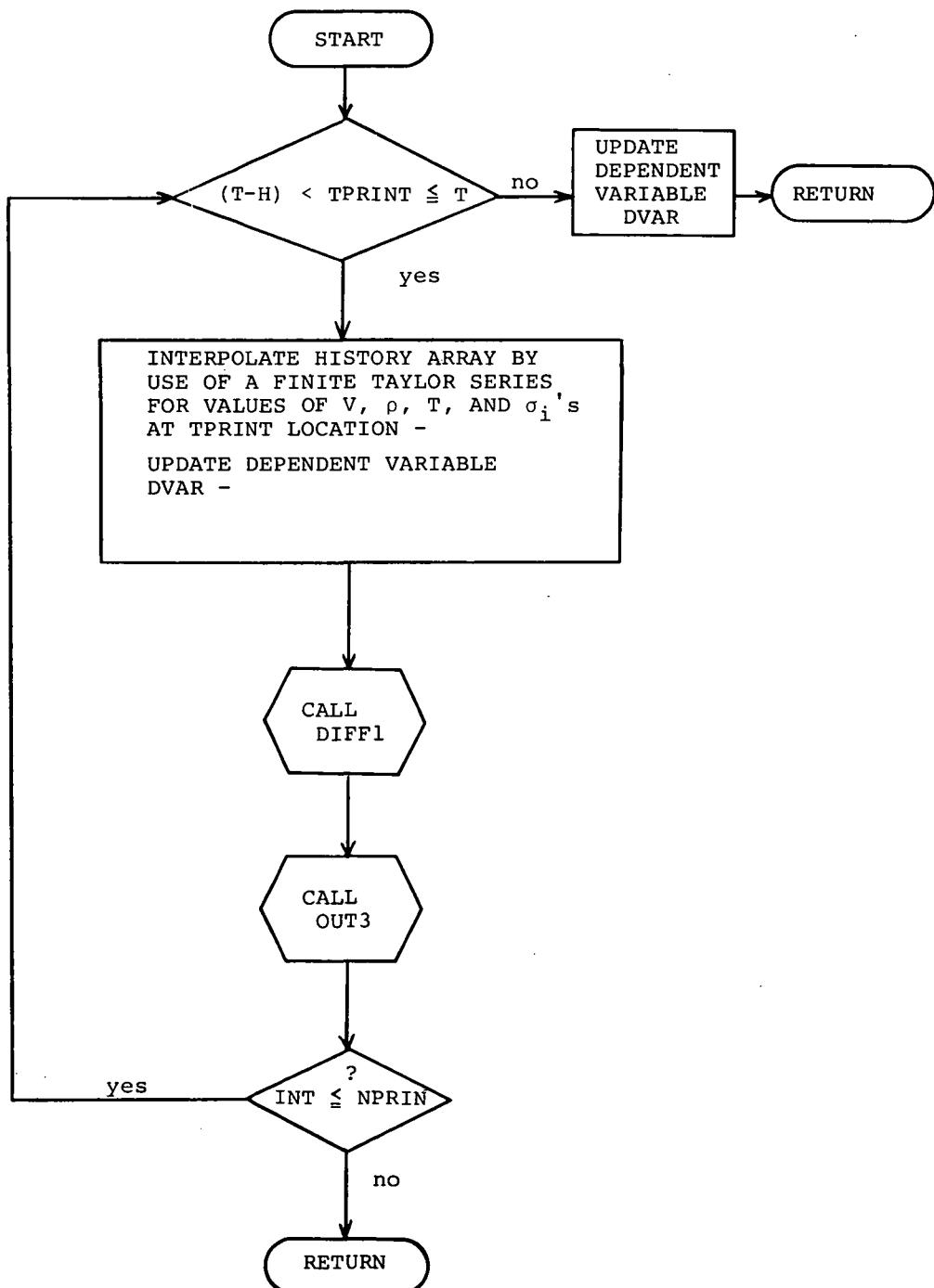


Figure 5.- Flow diagram for subroutine YOUT.

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