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THE MAGNETOSPHERE OF JUPITER AS OBSERVED WITH PIONEER 10. PARTS I, II, AND III
J. A. Van Allen, et al

Iowa University

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May 1974

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THE MAGNETOSPIIERE OF JUPITER AS OBSERVED WITHI PIONEER 10
Part I: Instrument and Principal Findings
J. A. VAN ALLEN, D. N. BAKER, B. A. RANDALL, and D. D. SENTMAN

## 20. Abstract

This paper reports on the first in situ observations of energetic electrons of energy $E_{e}>0.06 \mathrm{NeV}$ in the magnetosphere of Jupiter during
November-December 1973. The outer magnetosphere has the form of a thin disclike, quasi-trapping regiun extending from about 20 to over 100 RJ (planetary radii). This magnetodisc is confined near the magnetic equatorial plane and has epproximate axial symetry about the magnetic axis of the planet. The observations inside a radial cistance of $12 \mathrm{R}_{J}$ are well organized by a centered dipolar model of the planet's magnetic field :ith a tilt of $9: 5 \pm 0: 5$ to the rotational axis and with pole at a System III longitude of $230^{\circ} \pm 3^{\circ}$. Absolute omnidirectional intensities of electrons within the stable trapping region inside $20 \mathrm{R}_{J}$ are given for four energy ranges $E_{e}>0.06,>0.55,>5.0,>21$, and $>31 \mathrm{MeV}$. One exanple is

$$
J\left(E_{e}>21 \mathrm{MeV}\right)=3.0 \times 10^{8} \exp (-L / 1.45)\left(\frac{\cos ^{6} \Lambda}{\sqrt{4-3 \cos ^{2} \Lambda}}\right)^{m / 2}
$$

for $3.5<L<12 R_{J}$, where $J$ is in electrons $/ \mathrm{cm}^{2} \mathrm{sec}$, $L$ is the magnetic shell parameter in units $0: R_{J}$, and $\Lambda$ is the magnetic latitude. The pitch angle parameter $m=3.5+(3.86 / L)^{8}$. Marked depletion of perticle intensities at the orbits of Io, Buropa, and Ganymece is observed in the lower energy ranges.

Part II: Non-Rigid Eotation of the Nagnetodisc
C. K. GOERTZ, T. G. NOATTiROP, and M. F. THOMSEN

## 20. Abstract

The maximum count rates of energetic particles are observed earlier on the inbound pass and leter on the outbound pass than one woild expect if the Jovian maenetodisc rotated rigidly with the planet. This lead and lag cennot be explained by the observed aziruthal distortion of the Jovian ragnetic rield elone. The foot of a masnetic field in the ionosphere must slip with respect to Jupiter's surface. The rate of slippage and tine electric field necessary for this is estimated. Tre electric field may be as large as 2 volts/meter in the Jovian polar ionoschere.

Part III: Jovian Synchrotron Padiation at 10.4 cm as Deduced from Observed Electron Fluxes
T. G. NORTHEOP and T. J. BIN.INGHAM

## 20. Abstract

Synchrotron radiation at 10.4 cm wavelength between 2.9 and 5.0 Jovian radii has been calculsted from the electron fiuxes observed by the Iowa Pioneer 10 detectors. This calculated cmissivity (watts $/ \mathrm{m}^{3} \times \mathrm{Hz} \times$ steradian) exceeds the Beard-Luthev [197j] spatial resolution of the Eerge [1966] interfcrometer measurements by about a factor of 2 at 3 Jovian radii. The calculated emiscivity is quite insensitive to the enerey spectral index. It is only moderately sensitive to the equatorial ancular distribution. The disacrecment would be only about $30 \%$ if Eeard and Luthey had used the Iowa ancular distribution. A factor of 2 would represent a ecnuine disaisreement, but $30 \%$ would not exceed the combined uncertainties of our analysis and the Beard-luthey analysis.

## Part I: Instrument and Principal Findings <br> J. A. VAN ALLEN, D. N. BAKER, B. A. RANDALL,

 and D. D. SENTMANPart II: Non-Rigid Rotation of the Magnetodisc
C. K. GOERTZ, T. G. NORTHROP, and M. F. THOMSEN

Part III: Jovian Synchrotron Radiation at 10.4 cm as Deduced from Observed Electron Fluxes
T. G. NORTHROP and T. J. BIRMINGIAM

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Department of Fhysics and Astronomy The University of Iowa Iowe City, Iowa 52242

May 1974

The University of Iowa instrument on Pioneer 10 is a modified version of one proposed in November 1968. The original design was simplified and revised in accordance with constraints specified by the National Aeronautics and Space Administration at the time of acceptance of the experiment in early 1909.

Among the several observational objectives of our experiment, the principal onc was to make an exploratory survey of the absolute intersities, energy spectra, and angular distributions of energetic electrons and protons as a function of position along the trajectory of the spacecraft through the magnctosphere of Jupiter, giving primary emphasis to electrons of energy $E_{e}>0.06 \mathrm{MeV}$ and secondary emphasis to protons of energy $E_{p}>6.6 \mathrm{MeV}$.

A preliminary report of our Jovian encounter measurements has been published [Van Allen et al., 1974a, 1974b]. The present paper is based on a thorough re-analysis of detector calibrations and of the observational data.

## DESCRIPTION OF INSTRUMENT

At the time of design of the experiment a valued reference was a paper of Chang and Davis [1962] giving estimates of the distribution and absolute intensities of relativistic electrons in the magnetosphere of Jupiter that would yield the well-observed decimetric radio emission [Carr and Gulkis, 1969]. The most pertinent previous experience in observing such high intensities of relativistic electrons in space was that obtained following the 196 migh-altiture nuclear explosion (Starfish) in Earth's magnetosphere [0'Brien et al., 1962] [Van Allen et al., 1963] [Van Allen, 1906]. That experience served as a guide for instrunent design. Other basic considerations in addition to the NASA constraints were simplicity, ruggedness, internal redundancy, large dynamic range, reliability over lonc flight periods, and insensitivity to radiation damage and temperature.

Seven miniature Geiger-Mucller tubes are used as basic detectors. Four of these ( $A, B, C$, and $G$ ) are EON Corporation endwindow type 6213 which have logged over 700,000 detector hours of reliable operation in University of Iowa instrunents on a wide variety of earth-orbiting and planetary missions of lone duration. Many individual tubes have locged over $10^{10}$ counts and a few, over $10^{11}$ counts. The three other tubes (D, F, F) are fon Corporation
type $) 10$ f tubes, which had not been flown before but had proved, after sbrincent wection and testing, to have excellent reliability and a considerably lesser dead-time than do the 6213's. The seven tubes were placed in a variety of physical arrangements.
$A, C$, and $B$ are mounted in a single block as shown in Figure 1. The central tube $C$ is shielded omnidirectionally. $A$ and B arc similarly shielded except for thinner window, unidirectional collimators in the $+X$ direction. The individual cuunting rates of the thre tubes are telemetered separately; also double coincidences $A B$ and triple coincidences $A B C$ with a resolving time of $1 \mu s$ are formed and telemetered.

The second assembly comprises an onmidirectionally shielded, triangular array of three miniature, cylindrical tubes as shown in Figure $?$ The rate of $D$ and the triple coincidence rate DEF are telemetered.

The third assembly (Figure 3) uses a thin mica-window 6213 ( $1.3 \mathrm{mg} / \mathrm{cm}^{2}$ ) (G) in scatter geometry with a gold-plated elbow as the entrance apcrture. The purpose of the scatter arrangement is to admit low energy electrons ( $\mathrm{E}_{\mathrm{e}}>0.060 \mathrm{MeV}$ ) but discriminate stroncly against protons, $\mathrm{E}_{\mathrm{p}}<20 \mathrm{Mev}$.

I'he overall physical arrangement is sketched in Figure 4. Ihe $\%$-axis of the instrument is parallel to the axis of rotation of the spacecraft. The +X axis points outward into free space from the rim of the .astrument compartment of the spacecraft. The
magnetometer and a portion of the magnetometer-boom subtiend a trivial fraction of the fields of viow of the collimators of $\Lambda, B$, and $G$; otherwise there is no physical obstruction within the fields of view.

The instrument uses 12 bits ( 4 words) in each 19-bit main science frame (MSF) of the spacecraft's telemetry format (i.e., $6.25 \%$ of science telemetry) in science formats A or B. Quasilogarithmic data compression is used to maintain $1 \%$ accuracy at all possible counting rates. All outputs are digital. A complete cycle of University of Iowa data comprises eleven MSF's as follows: Sync Word, $G, A, B, G, A B, A B C, C, D, A B C$, and DEF. Thus the individual accumulation duty cycles are $9.1 \%$ for $A, B, C, D, A B$, and DEF, and $18.2 \%$ for $G$ and $A B C$.

Counts from each detector channel are accumulated for a period of time in seconds equal to $192 / \mathrm{b}$, where b is the telemetry rate in bits/second for the entire spacecraft ( $b=16,32$, $64,128,256,512,1024$, or 2048 , as selected by ground conmand).

During the Jovian encounter the prevailing value of b was 1024 bits/second and the telemetry format was mainly D/B with some segments in format $B$ (as sketched above). In format $D / B$ the duty cycles of our detectors are the same as in formats $A$ or $B$ but the sampling time is doubled. Hence, each data sample corresponded to an accumulation time of 0.375 second, or to a rotational angle of 10.7 the prevailing spacecraft rotational period of 1 . 6 .
seconds. Successive samples from each channel are taken at intervals of 4.125 seconds or $118^{\circ}$ of rotational angle. The rotational axis $(+7)$ of the spacecraft is pointed continuously at the earth with an error of less than $1^{\circ}$ and therefore lies approximately in the ecliptic pisne. Angular distributions of particle intensities as a function of roll angle in the equatorial plane of the spacecraft are assembled as a soft-ware operation using attitude data supplied by the Anes Research Center. In our analyses the roll angle is measured from the ascending node of the spacecraft's equator on the ecliptic to the $+X$-axis of the instrument (Figures 1, 2, 3, and 4) at the mid-time of the sample. It is noted that the Z-axis of the $\mathrm{s} / \mathrm{C}$ is approximately orthogonal to the $\vec{B}$ vector of the planet during the central portion of the encounter. Hence a nearly complete scan of particle pitch angles is obtained. (This is not true in the outer portion of the planet's magnetosphere.) A useful angular distribution can be assembled for each detector channel for each minute and a nearly complete one for each 3.6 minutes of total observational time.

All data transmission during the encounter was in real-time except for a period of 64 minutes during which the spacecraft was occulted by the planet; during this period data were stored for 51.2 minutes at 16 bits/second in Format B in a 49,152 bit accumulator and subsequently played back.

Our instrument is designed to operate continuous.ly throughout flight in a single mode as described above. Two completely redundant logic packages are provided internal to the instrument. Command switching from "main" to "standby" processor is the only mode change provided other than "power on", "power off" commands. No malfunctions of any kind in the University of Iowa instrument have been detected during some 2.6 months of continuous in-flight operation, including the Jovian encounter and the post-oncounter period to date of writing. The instrument temperature during encounter was $+4^{\circ} \mathrm{C}$, comfortably near the center of the range for proper operation $-20^{\circ} \mathrm{C}$ to $+40^{\circ} \mathrm{C}$.

The total mass of the instrument is 1.64 kg and the total power required 0.76 watt.

## PHYSICAL CALIBRATION OF CHIE DETECTORS

The original design of the instrument was done principally on a calculational basis. Following completion of the prototype and flight instruments an extensive serios of physical calibrations (in addition to standard environmental qualification tests) was made with the following radiation sources:
(a) Variety of $\beta$ sources ( $\mathrm{C}^{3.4}, \mathrm{Ni}^{63}, \mathrm{Tc}^{99}, \mathrm{Sr}^{90}, \mathrm{TI}^{205}$ ) (U. of Iowa)
(b) 5000 curie $\mathrm{Co}^{60}$ source of gamma rays
(U. of Iowa)
(c) 30-230 kV d.c. x-ray machine
(U. of Iowa)
(d) $0.3-1.8 \mathrm{MeV}$ Van de Graaff accelerator for protons

> (U. of Iowa)
(e) 1-6 MeV Van de Graaff accelerator for protons (U. of Iowa)
(f) $\quad \beta-$ ray spectrometer ( $\sim 50-600 \mathrm{keV}$ )
(U. of Iowa)
(g) Van de Graaff accelerator for electrons $0.2-1.6 \mathrm{MeV}$ (GSFC)
(h) $0-300 \mathrm{kV}$ d.c. electron accelerator

> (U. of Iowa)
(i) Variable energy cyclotror for protons $15-100 \mathrm{MeV}$ (U. of Maryiand)
(j) Linac for electrons $5-40 \mathrm{MeV}$
(Argonne Cancer Research Hospital)
(k) Linac for electrons $20-100 \mathrm{MeV}$
(Gulf Radiation Technology Laboratory, now Intelcom Rad Tech)
(l) Synchrocyclotron for protons $\sim 100-570 \mathrm{MeV}$
(Space Radiation Effects Labcratory)
The full body of calibration data has been assembled and analyzed by Baker [1973]. A re-analysis and further digest of "unit response functions" for monoenergetic beams are summarized in Figure 5 for electrons and in Figure 6 for protons. It is noted that the ordinate in each case is in absolute units -- namely count/sec for an isotropic beam of monoenergetic particles having an omnidirectional intensity of one particle $/ \mathrm{cm}^{2} \mathrm{sec}$. Inasmuch as all calibrations were done with actual particle beams, effects of locally produced bremsstrahlung, stc. are automatically included in the response functions.

The only significant shortcomings of Figures 5 and 6 are the assumption of particle isotropy and the omission of the influence of the spacecraft, on the outer edge of which our instrument is mounted. For a continuously rotating spacecraft, the assumption of isotropy causes an error of the order of $25 \%$ or less for the types of angular distributions actually observed. This error can be
reduced by iteration, when worthwhile to do so. The spacecraft end its contents (mostly low Z-material) subtend an effective solid angle of about $30 \%$ of the unit sphere centered on the detectors. On the one hand this mass of material acts as an absorber, thus tending to decrease counting rates. On the other hand, it acts as a generator of multiple particle events via bremsstrahlung, pair production, etc., thus tending to increase counting rates.

For protons $E_{p}<100 \mathrm{MeV}$ and electrons $\mathrm{E}_{\mathrm{e}}<20 \mathrm{MeV}$, the absorption effect probably dominates; for electrons, $E_{e}>20 \mathrm{MeV}$, the production of secondaries probably dominates. Observed multiple coincidence rates during high energy electron tests in the laboratory and during the Jovian encounter are sufficiently low to suggest that the multiplicative effects in the spacecraft are not important. Lacking a thoroughly definitive test of this matter we have adopted Figures 5 and 6 without any correction for spacecraft influence. The overall uncertainty in the absolute intensities quoted hereafter is probably of the order of $50 \%$.

Using the monoenergetic, unit response functions of Figures 5 and 6 we have subjected each detector, calculationally, to isotropic beams of electrons and protons (separately) having continuous power-law or exponential spectra with arbitrary differential spectral index $\gamma$ or e-folding energy $E_{0}$, respectively.

The resulting absolute geometric factor ( $\mathrm{cm}^{2}$ ) is then a function of $\gamma$, or $E_{o}$, and of the assumed threshold energy. These calculations yield "bow-tie" diagrams such as those shown for electrons in Figure 7. The approximately coincident crossing-points of the several curves in each diagram enable one to assign a single pair of effective values of absolute geometric factor and threshold that are approximately independent of spectral form. Our adopted values are tabulated in Table 1.

The differences in counting rates ( $G-C$ ), $(B-C)$, and ( $A-C$ ) are attributed to particles entering the collimators of $G, B$, and A, respectively, on the assumptions that the omnidirectional shielding of G, A, B, and C is identical and that the individual tubes are identical. During most of the Jovian enrounter the ratios (G-C)/C, etc. are substantially greater than unity and inaccuracies in these assumptions produce no significant error. However, near periapsis the several ratios shrink to near unity and the formally inferred values of the intensities of electrons $\mathrm{E}_{\mathbf{e}}<21 \mathrm{MeV}$ are subject to considerable uncertainty. Otherwise stated, the problem is one of differencing two large and somewhat uncertain counting rates and ascribing the difference to a collimator whose solid angle is a small fraction of $4 \pi$ (Table 1). Appropriate qualifications are repeated at relevant points later in the paper.

A valuable overall validation of the detector calibrations was obtaineci from observations during traversal of Earth's outer
radiation belt and magnetosheath by Pioneer 10 on March 3, 1972 in the range $5.2 \leq L \leq 6.2$ and $8<L<29$ earth radii. Angular distributions and absolute intensitics of electrons $\mathrm{E}_{\mathrm{e}}>60 \mathrm{keV}$ and $>550 \mathrm{keV}$ were in good agreement with well established values [Van Allen, 1972 ].

The dynamic range of the individual $G M$ tubes extends to at least $10^{7}$ counts/sec in the manner illustrated in Figure 8. Such $r$ vs $R$ curves were run repeatedly and over a wide range of temperature $\left(-20^{\circ} \mathrm{C}\right.$ to $\left.+25^{\circ} \mathrm{C}\right)$ for each detector in the completed flight unit using a d.c. x-ray machine and a 5000 curie $\mathrm{Co}^{60}$ source of $\gamma$-rays. They were also checked at the maximum with protons and electrons. The $r$ vs $R$ curves for all detectors are generally similar though they differ among themselves in detailed shape. Dependence on temperature has been virtually eliminated during development of the associated electronics. As will be seen later, the operating points of detectors $A, B, C$, and $G$ (but not D) moved up to and beyond the peaks of their $r$ vs $R$ curves during traversal of the central part of the Jovian magnetosphere. Near the peak of the curve, $d r / d R$ is approximately zero and the apparent (observed) rate is insensitive to changes in the true rate. To the right of the peak, a reasonably accurate determination of $R$ again becomes possible. The basic ambiguity between the left and right hand branches of the curve can be resolved by distinctively different statistical fluctuations in the apparent counting rate
of an individual detector and by the general run of data from the several different detectors.

A specific problem in the near-periapsis data occurred. The maximum observed rates of $A, B, C$, and $G$ were all significantly greater (by 1400-2100 counts/second) than those of the laboratory calibration curves. After eliminating a number of conceivable causes fC: this discrepancy, we have concluded that the most likely cause was slight upward drifts in the voltage of the gas-filled corona regulator tubes (Victoreen GVIA) which control the high voltage supplied to the GM tubes. The effect is simulated by changing the nominal 700 volts by $1-2 \%$. The manufacturer advises us that aging drifts of this magnitude occur commonly in longterm bench tests of operating GVIA's.

After examination of data from the Jovian encounter (the only in-flight episode that has or probably ever will exercise the detectors to the peaks of their $r$ vs $R$ curves) we ran families of $r$ vs $R$ curves as a function of voltage for similar tubes. We then selected a menber of the family that closely resembled the preflight curve for each detector and then the corresponding member at such a higher voltage as to exhibit the same peak value of $r$ as observed on that detector during the encounter. The latter was then adopted as the basis for converting apparent rates to true rates. Figure 8 illustrates the adopted solution to the problem for detector G, a typical case.

No one of the individual GM tubes can distinguish elertrons from protons. However, combinations of detectors have useful (and in some cases conclusive) diagnostic properties for determining the particle species that is dominantly responsible for a given set of observed counting rates. These methods rely on ratios and differences of individual counting rates and on multiple coincidence rates. One such ratio is DEF/D. Its laboratory value for electrons is shown in Figure 5, with a maximum of $2 \times 10^{-2}$ at $\mathrm{E}_{\mathrm{e}} \approx 70 \mathrm{MeV}$, whereas for protons $E_{p}<150 \mathrm{MeV}$ it is less than $10^{-5}$ and for protons $150<\mathrm{E}_{\mathrm{p}}<500 \mathrm{MeV}$ it is $\leqslant 2 \times 10^{-3}$ (Figure 6). In the inner magnetosphere of Jupiter the observed ratio was $\approx 10^{-2}$, thus showing that the response of $D$ was attributable primarily to electrons $\mathrm{E}_{\mathbf{e}}>20 \mathrm{MeV}$.

Another simple diagnostic relating to high energy particles is the ratio of the counting rates of $C$ and $D . C$ and $D$ have essentially the seme proton energy threshold but markedly different electron energy thresholds (Table 1). For a pure proton beam of any spectral form, $C / D \approx 2.8$. For electrons, $C / D$ depends on the form of the spectrum and ranges from $\approx 3.4$ for $\gamma_{e}=1.5$ to $\approx 14.5$ for $\gamma_{e}=5.0(\gamma=$ differential spectral index). The values of $C / D$ obscrved throughout the Jovian magnetosphere lie primarily in the range 4.0-7.0. These values correspond to electrons being the primary contributor to the counting rates of both $C$ and $D$.

For lower energy particles, the ratio of the counting rates of detectors $G$ and $B$ provide the best species identification. By comparing the electron and proton response functions (Figures 5 and 6) of these two detectors one sees that $G$ responds almost negligibly to protons $\mathrm{E}_{\mathrm{p}}<20 \mathrm{MeV}$. B , however, has a threshold of unidirectional response to protons of $\mathrm{E}_{\mathrm{p}}=6.6 \mathrm{MeV}$. For electrons, the order of the thresholds is reversed with G's threshold at $E_{e} \approx 0.040 \mathrm{MeV}$ and $\mathrm{B}^{\prime} \mathrm{s}$ at $\mathrm{E}_{\mathrm{e}} \approx 0.20 \mathrm{MeV}$. The effect of these relations is that $G / B$ is markedly $>1$ when the lower energy particles are predominantly electrons and is $<1$ when protons dominate (and when $1.0<\gamma_{p} \leqslant l .5$ ). In all but isolated regions, throughout encounter, $G / B>1$. Specifically for $r \leqslant 20 R_{J}$, G/B is $\not \geqslant 1.5$. Thus, lower energy protons contribute much less than do electrons to the counting rates of $G$ and $B$ in this region.

It appears that the responses of $A, C$, and $D$ are caused dominantly by electrons at all times during the Jovian encounter. Within a radius of $20 R_{J}$, the responses of $G$ and $B$ are also caused dominantly by electrons. During isolated segments of data in the outer magnetosphere, low energy protons contribute signiricantly to the responses of $G$ and $B$.

Our internal identification analysis is consistent with data from other Pioneer 10 experiments [Simpson et al., 1974] [Trainor et al., 1974] [Fillius and McIlwain, 1974].

## ENCOUNTER TRAJECTORY

In order to understand the run of observations, it is valuable to have at hand a general view of the encounter trajectory. One such diagram in planet-centered inertially oriented coordinates is Figure 9, a projection on the ecliptic plane of the hyperbolic trajectory of the spacecraft and of the orbits of the four inner satellites of Jupiter. The inclination of the planet's orbital plane to the ecliptic plane is $1: 3$ and of its equatorial plane to its orbital plane is $3^{\circ} 1$. Also the orbital planes of the inner satellites are nearly coincident with the planet's equatorial plane. Hence the three basic reference planes are interchangeable for approximate purposes.

A second diagram of essential importance is one showing the time-trace of the spacecraft in magnetic polar coordinates. Any such trace is, of course, dependent on the assumed model of the external magnetic field of the planet. An example of such a diagram is Figure 10. The pargmeters of the model of the magnetic field as shown in Figure 10 arise from analysis of our particle data as described in a later section.

In order to maintain consistency within the Pioneer 10 project, the JPL/ARC value of $71,372 \mathrm{~km}$ has been adopted as
"the radius of Jupiter" ( $=1 \mathrm{R}_{J}$ ). Geometric distances and values of the McIlwain L-parameter are expressed in terms of this unit. The above value is within $0.3 \%$ of the best current value of the planet's equatorial radius.

## NOTE ON TIME-LABELING

Throughout this paper, we time-label observed data with the Greenwich Mean Time at which the data were received at the earth ("Earth Received Time" or ERT). Also, the position of the spacecraft is time-labeled with the ERT of the data that were being observed at the position so labeled. During the encounter, the time-of-flight of an electromagnetic signal from the spacecraft to the earth varied from 41.3 minutes at periapsis passage minus 10 days to 47.0 minutes at periapsis passage plus 10 days. A constant value of 46 minutes is of adequate accuracy for approximate purposes. For example, if one imagines that the spacecraft carries a Greenwich Mean Time clock which reads 0202 at a position $P$, this position is time-labeled 0248 , as are the data observed at P .

## NOTES ON COORDINATE SYSTEMS AND <br> KINDRED MATTERS

Three different, planet-centered, rotating coordinate systems (I, II, and III) are in cormon use for specifying identifiable physical features of Jupiter. All measure latitude from the equatorial plane. The three different longitudes are measured from different meridians, but all increase westward, i.e., in the sense opposite to the sense of rotation of the planet. Each of the systems corresponds to a different period of rotation. Hence the relationships among the three longitude values ( $\lambda_{I}, \lambda_{I I}, \lambda_{I I I}$ ) of a given object are time dependent; also the relationships are a function of the distance of the object, if time at the object is used. A sparse tabulation of System I and System II (but not System III) longitudes of the central meridian of the planet as viewed by a terrestrial observer (at particular values of ERT) is given routinely in the annual American Ephemeris and Nautical Almanac. Also given are accurate but sparse data on the ephemerides of the satellites for the use of terrestrial observers (See also Explanatory Supplement to the Astronomical Fphemeris and Nautical Almanac, 1961, and the Supplement to the A.E. 1968, 1966.)
[Peek, 1958] [Marth, 1896]. The Pioneer 10 trajectory as supplied
to experimenters by the Ames Research Center tabulates longitude of the spacecraft (at "spacecraft time") as the negative of $\lambda_{I}$ according to the Jet Propuision Laboratory convention [Melbourne et al., 1968]. A valuable digest of all of the above has been made by Mead [1973], who gives the following conversion formulae as applicable at Jupiter (or approximately to a nearby spacecraft):

$$
\begin{aligned}
& \lambda_{I I I}(1957.0)=\lambda_{I I}+0.27432(J-2435839.5) \\
& \lambda_{I I}=\lambda_{I}-7.63(J-2435839.5)-70.78 \\
& \lambda_{I I I}(1957.0)=\lambda_{I}-7.35568(J-2435839.5)-70.78
\end{aligned}
$$

where all longitudes are in degrees and $J$ is the Julian date, at Jupiter.

The System III or "magnetospheric" longitude [I.A.U. Info. Bull. No. 8, 1962] is based on radio astronomical measurements and is the one presumably most relevant to the present investigation. We have converted the longitude of the spacecraft to System III (1957.0) using the above formulae.

Further, according to Mead's [19/3] digest of radio astronomical data, the tilt of a centered dipole (representing the external magnetic field of the planet) is about $10^{\circ}$ to the rotational axis and the System III (1957.0) longitude of its pole is about $224^{\circ}$ as extrapolated to 1973.9.

Accurate ephemerides of the five inner satellites of Jupiter were kindly supplied to us by M. Helton of the Jet Propulsion Laboratory.

## REVIEN OF ENCOUNTER OBSERVATIONS

The first durable encounter with the magnetosphere of Jupiter occurred at 2024 ERT on November 26, 1973 (Figure 11). At that time the radial distance of the spacecraft from the center of the planet was $109 \mathrm{R}_{\mathrm{J}}\left(7.8 \times 10^{6} \mathrm{~km}\right)$ and its local time was 9.7 hours. The counting rates of our lowest energy threshold detectors $G$ and $B$ (cf. Table 1) began a clear and progressive increase above interplanetary rates. The causative particles are primarily electrons $\mathrm{E}_{\mathrm{e}}>0.060 \mathrm{MeV}$. Also at that time a weak but characteristic bow shock signature appeared in data from both the magnetometer [Smith et al., 1974] and plasma analyzer [Wolfe et al., 1974]. During the 24-hour period 1200/November 25 to 1200/November 26 the fluctuating interplanetary magnetic vector had an average cone angle of $116^{\circ}$ (polar angle from +Z-axis of spacecraft, which was earthpointed), an average clock angle (rotational angle measured from the ascending mode of the spacecraft's equatorial plane on the ecliptic plane to $\vec{B}$ ) of $18^{\circ}$ (i.e., slightly northward-pointing relative to the ecliptic), and an average magnitude of $0.67 \gamma$ (gamma). Beginning at about 1200/November 26 the cone angle changed discontinuously to $\approx 140^{\circ}$, the clock angle crept upwards
toward a value of $\approx 60^{\circ}$, and the magnitude changed to an erratic but lower value of about $0.3 \gamma$. This general region is labeled "pre-shock" in Figure 11. In the magnetosheath the magnetic vector was quite irregular in direction and magnitude with an average macnitude of 2 to 3 times its interplanetary value. At 2038/November 27 both magnetometer and plasma analyzer data identified a magnetopause signature. Also, the counting rates of our particle detectors (including the heavily shielded ones) began a distinctive and discontinuous increase, though less abruptly than did the magnitude of the magnetic vector.

After passage through the magnetopause (Figure 12) there were generally rising counting rates on all detectors. The most distinctive feature of this period was a regular periodic variation, more or less colierently on all detectors, with a period of about 10 hours. This period is identified with the planet's System III rotational period of 9.9249 hours [Carr, 1971]. The regular pattern of variability was interrupted by a 6-hour "drop-out" to interplanetary values in the counting rates of all channels during the period 0500 to 1100 on December 1. Thereafter, the generally upward trend of counting rates of all detectors resumed as though the drop-out had not occurred and the periodicity reappeared. However, for the first cycle following the drop-out, the counting rates of lower energy detectors $G$ and $B$ were out-of-phase with those of the higher energy detectors $A, C$, and $D$ by about $180^{\circ}$.

This phase-shift disappeared and coherence was reestablished by midday of December 2.

Beginning at about $0800 /$ December $3\left(r=19 R_{J}\right)$, all counting rates began a strong upward climb of several orders of magnitude (Figure 13) and reached their greatest values at 0215/December 4, about an hour before periapsis passage at 0315 at $r=2.84 \mathrm{R}_{\mathrm{J}}$. The rates then declined to a deep minimum at 1545 ( $r=13.4 \mathrm{R}_{\mathrm{J}}$ ).

Thereafter the periodic, coherent variation of counting rates resumed, with broader minima and flatter maxima than on the Inbound leg of the trafectory, and with generally declining values (Figure 14). This pattern persisted until late on December 9 $\left(x \approx 88 \mathrm{R}_{J}\right)$. Then for about a day, the pattern of variability more nearly resembled that of the inbound leg of the trajectory. At about $1300 /$ December $10\left(r=98 \mathrm{R}_{\mathrm{J}}\right)$ an abrupt, coherent cut-off in all counting rates occurred and they all dropped to interplanetary values. However, sporadic activity resumed (rigure 15) abcut 20 hours later and persisted through at least December 16 ( $\mathbf{r}=170 \mathrm{k}_{J}$ ). Isolated bursts of particles, presumably from Jupiter, continued to occur for many days thereafter.

THE MAGNETODISC

The pervasive $10-\mathrm{hr}$ periodicity (or modulation) in the counting rates of all detectors in the outer magnetosphere of the planet on both the sunward (inbound) and dawn (outbound) sides is identified with the rotational period of the planet. The System III (sidereal) rotational period derived from radio (e.g., magnetospheric) emissions (both decametric and decimetric) is $9 \mathrm{hr} 55 \mathrm{~min} 29.75 \pm 04 \mathrm{sec}=9.9249 \mathrm{hr}$ [Carr, 1971].

We consider that our particle observations taken together with the magnetic field observations [Smith et al., 1974] and rudimentary theoretical considerations make it virtually conclusive that the outer magnetosphere of Jupiter has the physical shape of an immense, relatively-thin disc. We have adopted a suggestion by William Dixon that this portion of the Jovian magnetosphere be referred to as the magnetodisc.

In our earlier paper [Van Allen et al., 1974a], we showed that a thin, tilted, rigid disc attached to the planet and having, as observed, a radially distended magnetic field and an accompanying population of confined, or quasi-trapped, energetic particles gives a good first order representation of the observations. It was further supposed that the basic cause of the distention of the
field is thermal plasma (not directly observed) corotating with the planet and subject to an approximate balance of forces -- gravitational, pressure gradient, magnetic, and centrifugal. It is of interest to note that at $100 \mathrm{R}_{\mathrm{J}}$ the circumferential velocity of a corotating parcel of plasma is $1250 \mathrm{~km} / \mathrm{sec}$, over three times as great as a typical solar wind velocity.

Indirect evidence for the presence of thermal plasma is provided by the approximate "nulls" and strong fluctuations in direction of the magnetic vector $\vec{B}$ that occur at or near the centers of our charged particle peaks. This phenomenon is especially clear on the outbound leg of the trajectory (dawn side). One of the best of many examples is shown in Flgure 16.

Some authors have argued that the magnetodisc is comprised of outward streaming particles. Although it is difficult to exclude this possibility completely, we conilinue to favor the view that the energetic particle population in the magnetodisc is quasi-trapped, though no clear basis for estimating residence times has yet occurred to us. A variety of evidence having various levels of persuasiveness is as follows:
(a) The magnetodisc is thin in its axial dimension ( $\leqslant 10 R_{J}$ ) and has sha:p boundaries ( $\approx 1 R_{J}$ ). Such sharpness is compatible wi.th magnetic confinement of electrons of the energies observed. For example, electrons of $E_{e}=0.1,1.0$, and 10 MeV have gyro-radil in a $5 \%$ magnetic field of $0.003,0.013$, and 0.098 $\mathbf{R}_{\mathbf{J}}$, respectively.
(b) Our angular distribution studies exclude unidirectional streaming along magnetic field lines. Indeed the predominant form of angular distribution in the magnetodisc is approximate isotropy with noteworthy exceptions in which the distribution has pronounced and equal maxima along both $+\vec{B}$ and $-\vec{B}$ ("dumbbell" distribution) or orthogonal to $\vec{B}$ ("pancake" distribution), clearly requiring quasitrapping for times long compared to a latitudinal bounce period.
(c) The persistent $10-\mathrm{hr}$ periodicity out to $\approx 100 \mathrm{R}_{\mathrm{J}}$ suggests closed rather than open magnetic field lines in order that the diurnal wobbling of the dipole be transmitted to the point of observation.
(d) An approximate integral of the magnetic flux through the magnetodisc outside of $20 \mathrm{R}_{J}$ (magnetic latitude $\approx 77^{\circ}$ ) suggests that there is little or no "polar cap" of cpen, unpopulated field lines.
(e) The particle intensities decline, in general, with increasing radial distance. This fact might be consistent with either outward streaming or quasi-trapping but the outer boundary is relatively sharply defined (Figures 12, 14, and 15), thus favoring confinement.
(f) Approximate axial symmetry of particle populations in the magnetodisc over some five hours of local time suggests residence times comparable to or greater than a rotational period (10 hr).

It should be noted (Figure 9) that the angle between the magnetic vector (approximately radial) and the spin axis of the spacecraft is markedly different on inbound and outbound legs of the trajectory in the outer magnetosphere. On the inbound leg our low energy detectors make only a partial scan of particle pitch angles relative to local magnetic vector, almost never reaching pitch angles near $0^{\circ}$ or $180^{\circ}$, whereas relatively complete scans of pitch angles are usual on the outbound leg. This fact may account, in part, for the difference in the modulation pattern of counting rates on the inbound and outbound legs of the trajectory, as is evident by comparing Figure 12 with Figure 14. Another, and perhaps more significant, reason is suggested by noting that the modulation pattern on the outbound leg from 2100/December 9 to 1300/December 10 (Figure 14) and from 0000/December 13 to 2000/December 14 closely resembles that of the inbound leg. Both of these periods occurred before magnetopause crossings. Hence, buffeting by the solar wind on the sunward side of the magnetodisc and on its outer fringe on the dawn side may tend to destroy the well ordered geometric form that it has at lesser radii on the dawn side. Such a line of thought is also compatible with the disorderly and more orderly nature of the magnetic field in the respective regions.

One feature of special interest is the drop-out of particle intensities on December 1. The plasma analyzer experimenters
[Wolfe et al., 1974] suggest that this is caused by a dramatic Inward movement of the sunward magnetopause, caused by an impulsive Increase in solar wind pressure. For the sake of discussion, we adopt a competing view, namely that a plasma instability developed In the outer magnetodisc, that field line interconnection occurred at $\approx 50 \mathrm{R}_{\mathrm{J}}$, and that a "bubble" of magnetized plasma "spun off" Into interplanetary space, carrying a quasi-trapped population of energetic particles with it [Gold, 1964 [Dungey, 1958]. SupportIng evidence for this view is provided by the subsequent observation of a passing bubble of energetic particles by our instruments on Pioneer 11 (Figure 17), which was nearly along the same radial line from the sun as was Jupiter and at a distance of 2.1 A.U. closer to the sun. The apparent group velocity of this bubble based on time between drop-out and passage of maximum intensity is $1,140 \mathrm{~km} / \mathrm{sec}$, a value similar to the circumferential velocity of the outer edge of the magnetodisc. The time profile of the event is quite different than those of solar energetic particle (SEP) events for similar particle energies and is in fact similar to other Jovian energetic particle (JEP) events observed as "precursors" and "post-cursors" by other Pioneer 10 experimenters [Simpson et al., 1974] [Trainor et al., 1974] and confirmed by us.

One is reminded of the body of pulsar evidence on the time variability of dispersion measure (the columnar integral of electron
density between pulsar and Earth) which is most plausibly attributed to spin-off of plasma from the rotating pulsar [Rankin and Roberts, 1971] [Rankin and Counselman, 1973]. Indeed, there appears to be a certain descriptive validity in thinking of Jupiter as a pulsarlike object, though the relevant physical parameters are of enormously different magnitude in the respective cases.

The existence of "switching anisotropies" (rapid transitions from unidirectional streaming in one direction to unidirectional streaming in the opposite direction) in the magnetodisc early on December 6 has been reported by Simpson et al. [1974]. We have examined our data for the same period at the same time resolution and confirm the rapid fluctuations and strong anisotropies. However, we find the angular distributions to be bi-directional (dumbbell) in form and not unidirectional thus contradicting their interpretation of close-by local acceleration.

The most common angular distribution of particle intensity In the magnetodisc ( $r>25 \mathrm{R}_{\mathrm{J}}$ ) is one of approximate isotropy. Significant exceptions occur as illustrated by four examples in Figure 18. Soon after the inbound crossing of the magnetopause on November 27 a weak but persistent pancake distribution appeared (upper left, Figure 18). At about 0500/November 28 this distribution changed over to one of dumbbell form and remained so (lower left, Figure 18) until 0600/November 29, after which time it became isotropic. Significant departure from isotropy was
observed again late on December 1 and early on December 2 (upper right, Figure 18) following the drop-out early on December 1 (Figure 12). The distribution was of pancake form at that time; by $0400 /$ December 2 , it had changed to dumbill form, then moved slowly to isotropy. The signature of the angular distribution history during this epoch resembles that following the first crossing of the magnetopause and thus tends to confirm the magneto-pause-like character of the recovery from the drop-out in mid-day of Decenken 1. Such evidence does not distinguish between the competitive hypotheses of impulsive spin-off or impulsive compression of the outer portion of the magnetodisc on December 1. A transition from pancake to dumbbell form occurred in less than one hour at about $1700 /$ December 2 , near a crossing of the magnetic equator.

On the outbound leg, nearly isotropic distributions predominate. Noteworthy exceptions occur, particularly on December 6, when strong dumbbeli distributions appear. An example is given in the lower right panel of Figure 18.

No periods of unidirectional streaming have been identified during either inbound or outbound traversals of the magnetodisc.

A detailed study of the periodic fluctuations in counting rates in the magnetodisc has yielded significant modifications to the first-order rigid disc model proposed earlier [Van Allen et al., [1974a] and has suggested some illuminating implications. The times
of minima in detector $C$ on the inbound leg of the trajectory and of maxima in detector $G$ on the outbound leg have been measured carefully on large scale working plots (of the nature of Figures 12, 14, and 15). These two different detectors were selected as giving the best definition on the respective legs of the trajectory. The System III longitude of the spacecraft ( $\lambda_{\text {III }}$ ) at those times is plotted as a function of radial distance in Figure 19. If the disc were rigid with its pole at $\lambda_{I I I}=224^{\circ}$ all points would lie along the line labeled $44^{\circ}$. It is seen that this expectation is, in fact, fulfilled out to $r \approx 25 R_{J}$. Beyond this radial distance the inbound and outbound curves curl markedly away from the rigid-disc line and in opposite senses. This effect is presumed to be one of local time. The inbound points (pre-noon) lead the line and the outbound points (pre-dawn) lag the line. The effect is interpreted in more detail by Goertz et al. [1974] in an accompanying paper as resulting from a composite of disc-flapping by the mechanism of transverse Alfvén waves and of local-time-and-latitudedependent slipping of the feet of magnetic field lines in the ionosphere of the planet. The latter feature of the interpretation yields provisional estimates of ionospheric electric fields at high latitudes.

THE INNER MAGNETOSPHERE

Our discussion of the inner magnetosphere ( $r \leqslant 20 \mathrm{R}_{J}$ ) of Jupiter centers around the observations presented in Figure 13. Of companion importance are the magnetic field observations [Smith et al., 1974]. The regular dipolar magnetic field at radial distances $r \leqslant 10 R_{J}$ undergoes a progressive transition to a markedly distended and often irregular form in the magnetodisc within about the same range of radial distance as that within which the distributions of energetic particles undergo a qualitative change in character.

The curves of Figure 13 give absolute omnidirectional intensities of electrons whose energy exceeds five different energy thresholds as show (cf. Table 1). The bases for going from raw counting rate data to these curves have been discussed in detail in the section entitled Physical Calibration of Detectors. Briefly, the procedure is as follows:
(a) Each individual counting rate sample from each detector is corrected for dead-time using the appropriate, renormalized r vs R curve (as Figure 8, for example). Either the rising or falling branch of the curve is used as decided from a careful, earlier examination of the uncorrected data. This decision is an individualized one for each different detector.
(b) The corrected ("true") counting rates for the omnidirectionally shielded detectors $C$ and $D$ are corrected to absolute intensities by the summary data of Table 1.
(c) For the directional detectors $G, B$, and $A$, the three differences of corrected, rotationally averaged counting rates ( $G-C$ ), ( $B-C$ ), and ( $A-C$ ) are found for each interval of time. Each of these differences is assumed to correspond to a proper average over the unit sphere of the unidirectional intensity in the appropriate energy range. The quantities (G-C), (B-C), and (A-C) are then converted to absolute omnidirectional intensities by means of Table 1 , the factor $4 \pi$ having already been incorporated into the listed values of reciprocal geometric factor.
(d) Finally, the respective intensity values from step (c) for $0.060<\mathrm{E}_{\mathrm{e}}<21 \mathrm{MeV}, 0.55<\mathrm{E}_{\mathrm{e}}<21 \mathrm{MeV}$, and $5.0<\mathrm{E}<2.1 \mathrm{McV}$ are added to those of detector $C\left(E_{e}>21 \mathrm{MEV}\right)$ as obtained in step (b). The three resulting curves as shown in Figure 13 are labeled $E_{e}>0.060,>0.55$, and $>5.0 \mathrm{MeV}$, respectively.

Solid lines in Figure 13 represent data that we consider worthy of a high level of confidence.

Dashed portions of the three upper curves are uncertain on the grounds discussed at length in the section entitled Physical Calibration of the Detectors. Further work is being done on this portion of the data to reduce uncertainties in effective omnidirectional shielding and in dead-time corrections. Nonetheless,
the dashed portions of the three upper curves represent our best efforts to date and deserve provisional consideration.

The principal features of Figure 13 are as follows:
(a) All intensities tend generally upward to maximum values at about an hour before periapsis passage, then decline. The position of maximum intensities and the absence of symmetry in the curves are considered to be understood in terms of the nature of the trajectory in magnetic coordinates (Figure 10), as will be shown later.
(b) Detailed features in the curves (especially the upper three) appear to be plausibly associated with traversal of magnetic shells swept through by the three inner Galilean satellites (Figure 10).
(c) The two lowest energy channels show marked breaks in their upward climbs and a great deal of detailed structure in the vicinity of the inbound, near-equatorial crossing of the orbit of Ganymede. On the outbound, high-latitude crossing, there is a large and rapid decline in intensities of electrons of all energies. Only a small fraction of this decline can be attributed to "normal" latitude dependence of intensity (see later).
(d) There are clear and unequivocal notches in the upper two curves and a local plateau in the next lower curve at the inbound crossing of the orbit of Europa, at relatively high magnetic latitude. On the outbound crossing (nearer the
magnetic equator) there are clear plateaus and considerable structure in the upper three curves.
(e) At both inbound and outbound crossings of the orbit of Io there are similar notches in the upper three curves. These two crossings are at similar magnetic latitudes.
(f) Satellite effects in the lower two, higher energy curves are weak or indiscernible, except for the marked Ganymede dip on the outbound traversal of its magnetic shell.
(g) Although not shown in Figure 13, we have found no effects associated with either crossing of the orbit of Callisto, probably because its orbit ( $r=26.38 R_{J}$ ) lies outside of the wellordered magnetic field of the planet.
(h) In a later paragraph it is suggested that Amalthea, whose orbit (of radius $2.54 \mathrm{R}_{\mathrm{J}}$ ) is slightly interior to the periapsis of Pioneer 10, may have a significant sweeping effect on the population of energetic particles.

Our measurements of particle intensities can yield, at best, only a crude estimate of the magnitude of the magnetic moment of the planet. On this point, the direct magnetometer measurements are far superior. However, the particle measurements provide an independent and perhaps superior determination of the orientation of the axis of the moment. For an initial treatment we have concentrated on the use of the data from detectors C and D.

The procedure is an attempt to find, by trial-and-error, values of the tilt and system III longitude of the pole of a centered dipole such that the inbound and outbound intensity data are coincident when plotted as a function of the magnetic shell parameter $L$. The further, essential parometer is the form of the pitch angle distribution of unidirectional intensity at the magnetic equator, which may be a function of $L$. This process of three parameter minimization of inbound vs. outbound residuals has not yet been carried out in a sophisticated way. But the results of a rough minimization are considered quite illuminating and worthy of being reported at this stage.

The process is illustrated by a series of plots. A preliminary analysis [Van Allen et al., 1974a] showed that the angular distribution of intensity in the inner magnetosphere is of pancake form. For analytical convenience we have adopted the form

$$
j(\alpha) \propto \sin ^{m} \alpha
$$

wherein $j$ represents the unidirectional intensity and $\alpha$ the local pitch angle. In a quasi-time-stationary trapping situation, this angular distribution, if true at the magnetic equator for particles of a given species and energy, is true at every other point on the same L-shell for the same class of particles. Also the omnidirectional intensity $J$ varies with the ratio of the magnitude of
the local magnetic field $B$ to its magnitude at the equator $B_{o}$ as follows:

$$
\frac{J(B)}{J\left(B_{0}\right)}=\left(\frac{B_{0}}{B}\right)^{m / 2} .
$$

For a dipolar magnetic field

$$
\frac{J(B)}{J\left(B_{0}\right)}=\left(\frac{\cos ^{6} \Lambda}{\sqrt{4-3 \cos ^{2} \Lambda}}\right)^{m / 2}
$$

or

$$
\frac{J(\Lambda)}{J(0)}=\left(\frac{\cos ^{6} \Lambda}{\sqrt{4-3 \cos ^{2} \Lambda}}\right)^{m / 2}
$$

wherein $\Lambda$ is the magnetic latitude.
The first step in the process is shown in Figure 20. Here we assumed the Smith et al [1974] displaced dipole model and sought the best value of $m$ independent of $L$. The model was relatively unsuccessful for any value of $m$, though $m=4$ produced about the best results.

We then tried centered dipoles with arbitrary values of tilt, longitude of pole, and values of $m$. For $m$ independent of $L$, this search yielded a tilt of $9.5^{\circ}, \lambda_{\text {III }}$ of the pole $=230^{\circ}$, and $m=4$ as a set of parameters that produced excellent closure in
the range $4.3<L<11 R_{J}$ (Figure 21). We have found it impossible to produce closure for $L>11 \mathrm{R}_{\mathrm{J}}$ with any dipolar model.

Examination of fanilies of diagrams such as Figire 10 suggested that the open loop for $L<4.3 R_{J}$ might simply be a manifestation of a rapid monotonic increase of $m$ as $L$ diminishes. Figure 22 shows the results of adopting a simple dependence of $m$ on $L$, keeping the tilt and longitude of the pole as before. This figure represents our most successful effort thus far on detector $C$, for electrons $E_{e}>21 \mathrm{MeV}$. A similar effort on data from detector $D$ for electrons $E_{e}>31 \mathrm{MeV}$ yields Figure 23.

Thus for both energy ranges, we achieved excellent closure of inbound and outbound data in the range $2.9<L<l e$ with a centered dipole having tilt of $9.5^{\circ}$ to the rotational axis of the planet and with its pole at $\lambda_{\text {III }}(1957.0)=230^{\circ}$. Changes of these values by more then $\pm 0^{\circ}: 5$ or $\pm 3^{\circ}$, respectively, produce a discernible deterioration in closure.

For C: $m=3.5+(3.86 / L)^{8}$
For D: $\quad m=4.0+(3.567 / L)^{8}$

Both of these empirical formula are for $L>2.9 R_{J}$. There is no assurance that they are valid for lesser values of $L$.

By least squares fitting to the data of Figures 22 and 23 in the range $3.5<L<12 R_{J}$ and use of Table 1 , we find
$J\left(E_{e}>21 \mathrm{MeV}\right)=3.0 \times 10^{8} \exp (-L / 1.45)\left(\frac{\cos ^{6} \Lambda}{\sqrt{4-3 \cos ^{2} \Lambda}}\right)^{\mathrm{m} / 2}$
and
$J\left(E_{e}>31 \mathrm{MeV}\right)=9.9 \times 10^{7} \exp (-L / 1.51)\left(\frac{\cos ^{6} \Lambda}{\sqrt{4-3 \cos ^{2} \Lambda}}\right)^{m / 2}$
with $J$ the omnidirectional intensity in absolute units electrons $/ \mathrm{cm}^{2}$ sec, $L$ in units of $R_{J}$, and $\Lambda$ the magnetic latitude in the dipolar model previously described. The values of $m$ are given in an immediately preceding paragraph for $C$ and $D$, respectively.

It is tempting to attribute the roll-over of both curves at low $L$ values to a sweeping effect of Amalthea. A diffusional analysis will be useful in assessing the validity of this suggestion. Also, the follow-on mission Pioneer 11 is now targeted for a periapsis of $1.6 \mathrm{R}_{\mathrm{J}}$. Its data should contribute to knowledge of this matter.

For $\mathrm{L}>12 \mathrm{R}_{\mathrm{J}}$ is appears hopeless to match inbound and outbound data with any magnetic source entirely interior to the planet. The general failure to accomplish closure is presumably attributable to a system of external magnetospheric currents, such as those so obviously necessary to account for the magnetodisc. A special
feature of the lack of closure is the great notch in the outbound pass in the vicinity of $\mathrm{L}=15 \mathrm{R}_{\mathrm{J}}$ (Figures 22 and 23 ). By
reference to Figure 10, it is noted that the inbound traversal of this magnetic shell is near the equator whereas the outbound pass is at a latitude of about $22^{\circ}$. We attribute this notch to Ganymede. The value of $m$ required to produce closure in this region is about 12. Such a thin pancake distribution is qualitatively compatible with the expectations of inward aiffusion of particles past a satellite [Mead and Hess, 1973] [Birmingham et al., 1974]. A comparable, though less pronounced, effect at the two crossings of the orbit of Europa has been noted earlier in the low energy but not the high energy channels.

During most of the traversal of the magnetodisc and the inner magnetosphere there is no simple power law or exponential spectrum in energy that gives a good representation of the data over the full energy range provided by our five basic detectors. We have adopted a two-part power law fit

$$
\frac{d J}{d E} \propto E_{e}^{-\gamma_{1}}
$$

in the energy range $0.06<\mathrm{E}_{\mathrm{e}}<5 \mathrm{MeV}$ and

$$
\frac{d J}{d E} \propto E_{e}^{-\gamma_{2}}
$$

in the energy range $E_{e}>5 \mathrm{MeV}$.
In the magnetodisc, typical values are $1.6<\gamma_{1}<2.0$ and $3.0<\gamma_{2}<4.5$.

In the region $2.9<\mathrm{L}<7.0 \mathrm{R}_{\mathrm{J}}$, values of $\gamma_{2}$ as inferred from C/D ratios are shown in Figure 24.

In the region $8<L<18 \mathrm{R}_{\mathrm{J}}$, provisional values of both $\gamma_{1}$ and $\gamma_{2}$ are plotted in Figure 25.

REMARKS

A retrospective assessment of the ziature of the Pioneer 10 encounter trajectory confirms the wisdom of its choice for a first reconaissance. But, as with any single planetary fly-by, there are obv. us deficiencies in coverage. From the standpoint of magnetospheric physics, there is a clear need for (a) observations at lesser radial distances (from which nost of the decimetric radio noise emission occurs), (b) a survey of the inner magnetosphere at higher latitudes, (c) observations on the evening side of the planet at large radial distances, and (d) observations on the anti-solar side of the planet at radial distances of hundreds of planetary radii to search for magnetotail phenomena.

The targeting of the follow-on mission Pioneer 11 (periapsis passage on 3 December 1974) is designed to remedy several of these deficiencies as well as to provide a subsequent fly-by of Saturn. Also Pioneer 11 carries a considerably improved version of our experiment.

In March-April 1976, Pioneer 10 will cross the radial line from the sun through Jupiter. A search for magnetotail phenomena will be made at that time, though the Jupiter-spacecrart distance will then be 4.7 A.U. (astronomical units) or $9900 \mathrm{R}_{\mathrm{J}}$.

If it is assumed that the magnetodisc of Jupiter extends to as great a distance on the dusk side as it has been observed to do on the dawn side, then its diameter perpendicular to the sun-planet line is at least $2.4 \times 10^{7} \mathrm{~km}$. Such a distance subtends 203 as Jupiter is viewed from the earth at opposition.

In addition to its overall intrinsic interest, the magnetosphere of Jupiter offers the following features which are distinctively different than that of Earth:
(a) Because of the great value of Jupiter's magnetic moment $1.45 \times 10^{30}$ gauss $\mathrm{cm}^{3}$ [Smith et al., 1974] or $1.8 \times 10^{4}$ times that of Earth, the physical scale of the Jovian magnetosphere is very much greater. By the same token the intensities and characteristic energies of inward-diffusing electrically-charged particles are also much greater.
(b) At the same planetocentric distance as measured in the respective planetary radii the centrifugal force on a parcel of plasma in the equatorial plane of Jupiter is 65 times as great as that at Earth. For this reason, the great magnetodisc of Jupiter has no terrestrial counte:.part; rather it gives Jupiter a certain physical resemblance to a pulsar.
(c) The spin-off of plasma and energetic particles from the outer magnetodisc is a new planetary phenomenon (at least quantitatively). It provides an important new tool for investigation of the interplanetary propagation of energetic particles in the outer solar system, free of the complexities of the solar environment.
(d) Ihe Moon's orbit lies outside of the central magnetosphere of Earth. No discernible effect of the Moon thereon has ever been shown to exist. In contrast, the four inner satellites of Jupiter produce massive sweeping effects on trapped particle populations especially in the lower energy ranges as demonstrated herein. A more refined study of these effects promises significant numerical results on both L-shell and pitch angle diffusion coefficients and hence on the basic dynamics of the magnetosphere.

In a companion paper Northrop and Birmingham [1974] have calculated the decimetric radiation implied by our observational data on energetic electrons.

The detail in our low energy electron data is inadequate to assess the proposal of Gurnett and collaborators [Gurnett, 1972] [Hubbard et al., 1974] that the Jovian satellites act as sources of energetic particles.

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## Table 1. Adopted Energy Thresholds and Geometric Factors for Ploneer 10 Detectors

## Electrons

## Detector

frective
Energy Range
$\mathrm{G}-\mathrm{C}$
$\mathrm{B}=\mathrm{C}$
$\mathrm{A}-\mathrm{C}$
$0.06 \mathrm{MeV}<\mathrm{E}_{\mathrm{e}}<21 \mathrm{MeV}$

C
D
$0.55 \mathrm{MeV}<\mathrm{E}_{\mathrm{e}}<21 \mathrm{MeV}$
$5 \mathrm{MeV}<\mathrm{E}_{\mathrm{e}}<21 \mathrm{MeV}$

$$
\begin{aligned}
& \mathrm{E}_{\mathrm{e}}>21 \mathrm{MeV} \\
& \mathrm{E}_{\mathrm{e}}>31 \mathrm{MeV}
\end{aligned}
$$

Effective Inverse Omnidirectional
Geometric Factors ( $1 / Q$ )
\(\left.\begin{array}{l}2600 \mathrm{~cm}^{-2} <br>
830 <br>
600 <br>
23.0 <br>

63.0\end{array}\right\}\)\begin{tabular}{c}
Primarily <br>

| Directional |
| :---: |
| Detectors | <br>

omnidirectional
\end{tabular}

*Approximately valid for electron spectra with power law spectral indices $1.5 \leqslant \gamma_{e} \leqslant 4.0$.

## Protons

$$
\begin{gathered}
B-C \\
A-C \\
C \\
D \\
G-C
\end{gathered}
$$

$6.6 \mathrm{MeV} \leq \mathrm{E}_{\mathrm{p}} \leq 77.5 \mathrm{MeV} \quad 620 \mathrm{~cm}^{-2}$
$30 \mathrm{MeV} \leq \mathrm{E}_{\mathrm{p}} \leq 77.5 \mathrm{MeV} \quad 675$ $E_{p}>77.5 \mathrm{MeV}$
$\mathrm{E}_{\mathrm{p}}>77.5 \mathrm{MeV}$
For $\gamma_{p} \leqslant 3.5$, protons of energy $E_{p} \leqslant 25 \mathrm{MeV}$ make a negligible contribution. For such a spectrum ( $G-C$ ) is sensitive for $25 \leqslant E_{p} \leqslant 77.5 \mathrm{MeV}$ with $I / Q \approx 125 \mathrm{~cm}^{-2}$.

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## CAPIIONG FOR FIGURES

Figure 1. Cut-away view of one system of detectors. A, C, and $B$ are miniature, end-window EON 6213 Geiger-Mueller tubes. The Z-axis is parallel to the rotational axis of the spacecraft.

Figure 2. Crossmsectional view of the heavily shielded triangular array of miniature, cylindrical EON 5107 Geiger-Mueller tubes $D, E$, and $F$.

Figure 3. Cut-away view of the arrangenent of the single EON 6213 Geiger-Mueller tube G. Low energy particles enter the end-window of the tube only after being scattered from the inner walls of the gold-plated elbow.

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Figure 5. Unit response functions of the several detectors for monoenergetic electrons. See text for identity of the accelerators used in determining these curves and for other details.

Figure 6. Unit response functions of the several detectors for monoenergetic protons.

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Figure 9. Projection on the ecliptic plane of the hyperbolic encounter trajectory of Pioneer 10 and the orbits of the four inner Jovian satellites. The numbers 1 and? on the orbits of JI, JII, and JIII show the positions of each of these satellites at the time that the spacecraft crossed the L-shell of that satellite, inbound and outbound respectively. The number 3 shows the position of JV at the time that the spacecraft was at periapsis, marked P. $\boldsymbol{\gamma}_{2}$ designates Jupiter's vernal equinox and $\gamma_{\oplus}$ designates Earth's vernal equinox. The ephemerides are courtesy of M. Helton of the Jet Propulsion Laboratory. Note that the spacecraft spin axis is parallel to the planet-earth line throughout the encounter.

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Figure 22. An improved version of Figure 21, assuming a simple L-dependence of $m$ in the angular distribution $j \propto \sin ^{m} \alpha$.

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Figure 24. The L-dependence of the differential spectral index $\gamma$ in a power law spectrum as derived from the counting rate ratio C/D. The abscissa is based on a $9.5^{\circ}$ tilt of the dipole toward longitude $\lambda_{\text {III }}=230^{\circ}$.
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$58^{<}$

A-670-316-1


Figure 1
$59^{<}$


Figure 2


Figure 3


Figure 4


Figure 5.

63<


Figure 6


Figure 7


$66<$

Figure - 9
\&

PIONEER 10 ENCOUNTER
MAGNETIC MERIDIAN PLANE PROJECTION


Figure 10


Figure 11


Figure 12

## $70^{<}$



Figure 13


Figure 14


Figure 15


$74<$

Figure 17


Figure 18

$76^{<}$

Figure 19

77<


Figure

78<


Figure 21

79<


Figure 22
$80^{\circ}$


Figure 23


Figure 24

$82<$

Figure 25

## $83^{<}$

# The Magnetosphere of Jupiter as Observed with Pioneer 10. Part II: Non-Rigid Rotation of the Magnetodisc 

by

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## ABSTRACT

The maximum courit rates of energetic particles are observed earlier on the inbound pass and later on the outbound pass than one would expect if the Jovian magnetodisc rotated rigidly with the planet. This lead and lag cannot be explained by the observed azimuthal distortion of the Jovian magnetic fleld alone. The foot of a magnetic field in the ionosphere must slip with respect to Jupiter's surface. The rate of slippage and the electric field necessary for this is estimated. The electric field may be as large as 2 volts/meter in the Jovian polar ionosphere.

## INTRODUCTION

The 10-hour particie-fiux modulation exhibited by the energetic particle measurements aboard Pioneer 10 [Van Allen et al., 1974a; Simpson et al., 1974; I'rainor et al., 1974; and Filius and McIlwain, 1974] have been interpreted by those authors as being due to a confinement of the energetic particles near the magnetic equatorial plane, which oscillates above and below the rotational equatorial plane. This oscillation is caused by the tilt between Jupiter's magnetic dipole axis and spin axis.

The maximum count rates should then occur when the magnetic latitude of Pioneer 10 is a minimum, i.e., when it is at a Jovian longitude $\lambda$ III $\approx 230^{\circ}$ on the inbound pass and at $\lambda$ III $\approx 50^{\circ}$ on the outbound pass, based on the model of the Jovian magnetic field described by Smith et al. [1974]. Van Allen et al. [1974b], however, report that the maximum count rates are observed when the spacecraft is at a longitude $\lambda$ III $<230^{\circ}$ on the inbound pass and at $\lambda$ III $>50^{\circ}$ on the outbound pass, i.e., earlier than one would expect on the inbound pass and later on the outbound pass. Figure 1 shows a polar plot of the position of count-rate maxima for the inbound and outbound pass as well as the positions of count rate minima.

The deviations $\alpha$ apparently indicate an azimuthal distortion of the magnetic field from a meridional plane, as indicated in Figure 2. And, indeed, Smith et al. [1974] have reported a systematic sweep back of the magnetic field from meridional planes, as illustrated in Figure 2.

In the following we will show that this is incompatible with Van Allen's observations if we assume that the foot of a field line is tied to the planet, and therefore conclude that it slips.

## MAGNETIC FIELD DISTORTION

In the following we will carry out our calculations in a coordinate system having the $z$-axis along the magnetic dipole; $\hat{\rho}$ is a radial unit-vector in the dipole's equatorial plane and $\hat{\varphi}$ completes a cylindrical coordinate system. A displacement of the outer parts of a field line merely parallel to the magnetic equatorial plane of the dipole cannot account for Van Allen's observations. The displacement must have a component in the rotational equatorial plane. Figure 2 indicates that this requires a displacement not only in the $\hat{\varphi}$ direction of the magnetic coordinate system but also in the $\hat{\rho}$ direction.

The motion of a field line can be thought of as a superposition of a rotation about Jupiter's rotation axis and an up and down motion due to the motion of the dipole with respect to the rotational axis. The outer ends of a field will not immediately adjust to the motion of the dipole but will follow with a time delay $\Delta t$

$$
\begin{equation*}
\Delta t=\int_{\text {Jupiter }}^{\text {Pioneer }} \frac{d s}{g} \tag{1}
\end{equation*}
$$

where $g$ is the group velocity of an Alfven wave and the integral
is taken along the field line passing through Pioneer 10. The group velocity of an Alfvén wave in the non-rotating system is:

$$
\begin{equation*}
\overrightarrow{\mathbf{g}}=\overrightarrow{\mathbf{w}}+\mathbf{v}_{A} \vec{B} / B \tag{2}
\end{equation*}
$$

where $\vec{W}$ is the magnetohydrodynamic drift velocity of a blob of plasma tied to the magnetic field. In a time $\Delta t$ the foot of the field line moves by $(\Delta \varphi)_{0}=\left(g_{\varphi}\right)_{0} \Delta t / \rho_{0}$, provided $B_{\varphi}$ vanishes at the foot of the field line. The outer end lags behind by $\Delta \lambda$ where

$$
\begin{equation*}
\Delta \lambda=\frac{\left(g_{\varphi}\right)_{0}}{\rho_{0}} \Delta t-\varphi \tag{3}
\end{equation*}
$$

where $\varphi$ is the angular motion of the outer end in the time $\Delta t$ and

$$
\begin{equation*}
\frac{d \Delta \lambda}{d \rho}=\frac{\left(g_{\varphi}\right)_{0}}{\rho_{0}} \frac{d \Delta t}{d \rho}-\frac{d \varphi}{d \rho}=\frac{\left(\varepsilon_{\varphi}\right)_{0}}{\rho_{0}} \frac{d \Delta t}{d \rho}-\frac{1}{\rho} \frac{g_{\varphi}}{g_{\rho}} \tag{4}
\end{equation*}
$$

For a conducting plasma we have (in the non-rotating frame):

$$
\begin{equation*}
\nabla \times(\vec{W} \times \vec{B})=\partial \vec{B} / \partial t \tag{5}
\end{equation*}
$$

In the magnetic frame the $\varphi$ derivatives of the components of $\vec{B}$ vanish and a solution of Equation (5) is

$$
\begin{align*}
& w_{\rho}=k B_{\rho}, \quad w_{z}=k B_{z}, \quad w_{\varphi}-k B_{\varphi}=a \rho, \\
& \frac{\partial \vec{B}}{\partial t}=-\vec{B} \frac{\partial a}{\partial \varphi} \tag{6}
\end{align*}
$$

if the change of magnetic field $\partial \vec{B} / \partial t$ can be attributed to rotation of the source of $\vec{B}$ with the planet. $k$ is a function of position and a is constant along a field line. $k$ represents mass flow away from the planet. At the $\mathrm{f}_{\mathrm{not}}\left(\mathrm{B}_{\varphi}\right)_{0}=0$ and thus:

$$
a(\varphi) \rho_{0}=\left(w_{\varphi}\right)_{0} .
$$

Since

$$
\Delta t=\int_{\rho_{0}}^{\rho} \frac{d \rho^{\prime}}{g_{\rho}}
$$

and

$$
\begin{aligned}
g_{\varphi} & =w_{\varphi}+v_{A} \frac{{ }^{\frac{\varphi}{~}}}{B}=\frac{\rho}{\rho_{0}}\left(w_{\varphi}\right)_{0}+k B_{\varphi}=v_{A} \frac{B_{\varphi}}{B} \\
& =\frac{\rho}{\rho_{0}}\left(w_{\varphi}\right)_{0}+w_{\rho} \frac{B_{\varphi}}{B_{\rho}}+v_{A} \frac{B_{\varphi}}{B},
\end{aligned}
$$

$$
\begin{align*}
\frac{d \Delta \lambda}{d \rho} & =\frac{\left(g_{\varphi}\right)_{0}}{\rho_{0}} \frac{1}{g_{p}}-\frac{\left(w_{\varphi}\right)_{0}}{\rho_{0}} \frac{1}{g_{p}}-\frac{1}{\rho} \frac{w_{0}}{g_{\rho}} \frac{B_{\varphi}}{B_{p}}-v_{A} \frac{B_{\varphi}}{B_{g_{p}}} \frac{1}{\rho} \\
& =-\frac{1}{\rho} \frac{B_{\varphi}}{B_{p}}\left[w_{\rho}+v_{A} \frac{B_{g}}{B}\right] \frac{1}{E_{p}}=-\frac{1}{\rho} \frac{B_{\varphi}}{B_{\rho}} \tag{7}
\end{align*}
$$

This is the equation of a magnetic field line in the magnetic coordinate system. The result (7) is obvious if there is rigid co-rotation and no mass flow, but we have now established its general validity.

We have analyzed the magnetic field data given to us by Smith. Figure 3 shows the radial and azimuthal magnetic field components as well as the ratio $B_{\varphi} / \rho B_{\rho}$, all measured in a (tilted) magnetic frame, with a tilt angle of $15^{\circ}$. A positive value for $B_{\phi} / \rho B_{\rho}$ indicates a lead. $B_{\phi} / \rho B_{\rho}$, however, is predominantly negative both on the outbound and inbound pass. The occasional positive value is most likely due to numerical uncertainties in the calculations. This result confirms that the outer parts of a magnetic field line always lag the foot of the field line. The data show that $B_{\varphi} / B_{p}$ is not a strongly varying function of $z$, at least in the outer parts of the magnetosphere. Using the smooth curve for ${ }_{B_{\varphi}} / \rho B_{\rho}$ in Figure 3 we can easily calculate $\Delta \lambda(\rho)$. The result is shown by the dashed curve in Figure 1. It is quite obvious that this is not sufficient to explain Van Allen's observations. The treatment so far has only
dealt with a difference in longitude between the foot of a field line and the outer parts. Figure 1, however, shows the relative azimuthal deviation of the outer parts of a field line from the surface of Jupiter. Apparently the foot of a field line moves relative to the surface of Jupiter in such a way that it leads the surface on the inbound pass and lags on the outbound pass. In other words, the foot of a magnetic field line is not strictly tied to the planet. It is known that "line-tying" is also only partially effective in the earth's ionosphere (see, e.g., Axford, 1969). The magnetic field data indicate a general lag of the outer parts with respect to the foot of a field line. Thus the observed deviation is

$$
\begin{equation*}
\alpha=\Delta \lambda+\beta=-\int_{\rho_{0}}^{\rho} \frac{1}{\rho^{\prime}} \frac{\stackrel{B}{\varphi}_{B_{\rho}}}{\mathrm{B}_{\rho}} d \rho^{\prime}+\beta, \tag{8}
\end{equation*}
$$

where $\beta$ is due to a slipping of the foot of a field line with respect to the planet's surface.

INTERPRETATION

The fact that the foot of a field line leads or lags the surface of the planet must be due to the existence of an electric field in the rotation frame of Jupiter because at Jupiter all but the most energetic particles ( $\mathrm{E}>10^{2} \mathrm{MeV}$ ) move together with the magnetic field at a drift velocity

$$
\begin{equation*}
\vec{v}_{D}=\frac{\vec{E} \times \vec{B}}{B^{2}} \tag{9}
\end{equation*}
$$

If the ionosphere represented a perfect short circuit across the field lines the shorting currents would resist any motion of field lines relative to the planet and the only electric fields which could exist would be due to a $\partial \overrightarrow{\mathrm{B}} / \partial \mathrm{t}$ [Axford, 1969]. Birmingham and Jones [1968] show that the $\partial \vec{B} / \partial t$ due to the rotation of the planet is precisely that required for corotation. Thus the obscrved deviation from corotation of the feet of field lines with Jupiter must either be due to a steady electric field or a $\partial \vec{B} / \partial t$ not associated with the rotation of Jupiter.

Although we have no a priori reason to believe that the motion is not due to a $\partial \vec{B} / \partial t$, the persistence of the forward motion of the field lines throughout the 6.5 days of the inbound pass seems to
rule out an electric field associated with a $\partial \vec{B} / \partial t$. Since the forward motion is quite large ( $\beta$ changes from 0 to $90^{\circ}$ between the early morning and noon) we must require a considerable electric field which, one would imagine, is difficult to achieve with a $\partial \vec{B} / \partial t$ of the order of magnitude produced by Jupiter's rotation. Thus we assume steady state. We can estimate the steady electric field in the following way. From

$$
\int_{\rho_{0}}^{\rho} d_{\rho}^{\prime} \frac{B_{\varphi}}{\rho^{\prime} B_{\rho}}
$$

we know that the foot of the fi.eld line with Pioneer 10 crossed at a distance $r$ leads the spacecraft by $\Delta \lambda^{\circ}(r)$ on the outbound and $\Delta \lambda^{i}(r)$ on the inbound pass. Assuming that Pioneer 10 crosses essentially the same field lines at a distance $r$ on the inbound and outbound passes (i.e., assuming that the field line is convected around Jupiter with little distention in the radial direction), we find that the foot has moved through an angle of $\beta^{\circ}(r)-\beta^{i}(r)$ whereas the surface has only moved through an angle $\gamma-\left(\alpha^{0}-\alpha^{i}\right)$ ( $\gamma$ being the angle between the inbound and outbound passes) in the same time (see Figure 4). The surface moves with an angular velocity $\Omega_{J}=1.76 \times 10^{-4} \mathrm{~s}^{-1}$ whereas the field line moves with

$$
\begin{equation*}
\Omega=\Omega_{J} \frac{\beta^{0}-\beta^{i}}{\gamma-\left(\alpha^{0}-\alpha^{i}\right)} \tag{10}
\end{equation*}
$$

relative to the surface. Then

$$
\begin{equation*}
E \approx \Omega \mathrm{~B}(\mathrm{r}) \tag{11}
\end{equation*}
$$

It is clear that this crude estimate is only justified as long as there is no appreciable stretching of the field lines in the radial direction during their motion from the early morning to noon side of the Jovian magnetosphere, which is probably orly true for those field lines which the spacecraft crossed at distances $r<60 R_{J}$. The electric field in the rotating frame of Jupiter calculated from Equations (10) and (11) is of the order of $10^{-2} \mathrm{~V} / \mathrm{m}$. This corresponds to a typical electric field of $2 \mathrm{~V} / \mathrm{m}$ in the Jovian polar ionosphere. The total potential drop across the polar ionosphere and thus across the Jovian magnetosphere may easily be as large as several MeV. Although we do not know what physical mechanism is responsible for electric fields of this magnitude it is tempting to associate it with the magnetic field line merging and recomection similar to that active in the earth's magnetosphere (see, e.g., Axford, 1909). Then the potential drop across the Jovian magnetosphere is a measure of the maximum energy that can be given to solar wind particles accelerated in the field line reconnection process. This process may explain the relatively large fluxes of energetic particles just inside the magnetosphere which, if they are of solar wind origin, must have gone through an accelerating region.

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## FIGURE CAPTIONS

Figure 1 Polar plot of the positions of count-rate maxima and minima on the inbound and outbound pass.

Figure 2 The azimuthal distortion of a magnetic field line. Figure 3 The radial ( $B_{\rho}$ ), azimuthal ( $B_{\varphi}$ ) magnetic field components, and ${ }^{B} / \rho B_{\rho}$ as a function of radial distance $\rho$ from the magnetic dipole axis. The dipole axis is inclined $15^{\circ}$ with respect to the rotational axis.

Figure 4 The geometry of the magnetic field distortion and slippage. The heavy lines indicate the projection of the distorted field lines on the ecliptic plane.

## 99<



Figure 1


Figure 2

$101<$
A-G74-345


Figure 4

## $103<$

The Magnetosphere of Jupiter as Observed with Pioneer 10.<br>Part III: Jovian Symchrotron Radiation at 10.4 cm as Deduced from Observed Electron Fluxes<br>T. G. Northrop*<br>Department of Physics and Astronomy, University of Iowa, Iowa City, Iowa 52242<br>and<br>T. J. Birmingham<br>Theoretical Group, Goddard Space Flight Center, Greenbelt, Maryland 20771

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#### Abstract

Synchrotron radiation at 10.4 cm wavelength between 2.9 and 5.0 Jovian radii has been calculated from the electron fluxes observed by the Iowa Pioneer 10 detectors. This calculated emissivity (watts $/ \mathrm{m}^{3} \times \mathrm{Hz} \times$ steradian) exceeds the Beard-Luthey [1973] spatial resolution of the Berge [1966] interferometer measurements by about a factor of 2 at 3 Jovian radii. The calculated emissivity is quite insensitive to the energy spectral index. It is only moderately sensitive to the equatorial angular distribution. The disagreement would be only about $30 \%$ if Beard and Luthey had used the Iowa angular distribution. A factor of 2 would represent a genuine disagreement, but $30 \%$ would not exceed the combined uncertainties of our analysis and the Beard-Luthey analysis.


## INTRODUCTION

The University of Iowa detectors on Pioneer 10 give electron energy and angular distributions as functions of distance from Jupiter [Van Allen, et al., 1974]. We have used these measured distributions to calculate the emissivity (in watts $/ \mathrm{m}^{3} \times \mathrm{Hz} \times$ steradian) of 10.4 cm wavelength radiation from the Jovian magnetic equatorial plasma. The emissivity is then compared to the radio astronomical observations from earth.

Berge [1966] has observed the decimetric synchrotron radiation at 10.4 cm as a function of distance from the planet. These measurements are unavoidably integrated along the line of sight through the Jovian magnetosphere. The emissivity per unit volume varies with radius, because both the magnitude of the field and the electron distribution vary. Beard and Luthey [1973] have resolved the Berge observations to give the volume emissivity of radiation polarized parallel to the magnetic dipole plane from a unit volume in the plane. Figure 1 shows their curve as well as the result of our calculations from the Iowa electron fluxes. Because Pioneer 10 did not penetrate to closer than $2.9 R_{J}$ (Jovian radii) the calculated curve does not extend inside of that radius. The discrepancy that appears between the Beard-Luthey curve and our calculation exceeds known possible errors in the data and calculations. At the end of
this paper we suggest a reason for the discrepancy
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## RADIATION PER ELECTRON

The radiation emitted per steradian at right angles to the magnetic field $\vec{B}$ from harmonics in frequency range $\Delta f\left(\begin{array}{l}\text { ertz }\end{array}\right)$ and


and polarized parallel to $\vec{B}$ is

$$
\Delta f \frac{e^{2} \omega_{i, 1}^{2}}{4 \pi \varepsilon_{0} \omega_{0}} \beta_{0}^{2} J_{m}^{2}(x)
$$

where $\omega_{0}=\frac{e B}{m_{0} \gamma}, m_{0}=$ electron rest mass, $\gamma=\left(1-\beta^{2}\right)^{-\frac{1}{2}}, \omega=$ angular observation frequency ( $\frac{\text { radians }}{\sec }$ ), $m=\frac{\omega}{\omega_{0}}, x=\frac{\omega \beta_{1}}{\omega_{0}}, \beta_{11}=\beta \cos \delta$, $\beta_{1}=\beta \sin \delta, \delta$ being the electron's pitch angle, and $J_{m}^{\prime}(x)$ is the derivative with respect to $x$ of the Bessel function $J_{m}(x)$. It has been assumed that there are many harmonics within $\Delta \mathrm{f}$, a good approxamation at 10.4 cm .

Usually $m \gg 1 ; m \geqslant 100$ for Jupiter and 10.4 cm wavelength. When $m$ is large there is an approximation to the Borsel Anctitons of
high order [Watson, 1922]

$K_{1 / 3}$ being the Bessel function of imaginary argument. For $\alpha<1$, the exponent in (3) is $-m\left[\frac{\alpha^{5}}{5}+o\left(\alpha^{7}\right)\right] ; \alpha$ is $\operatorname{sech}^{-1} \beta_{\perp}$ in (1) and (2). For the energies that contribute detectably to the radiation, $\gamma$ turns out to be greater than 10 ( $\sim 5 \mathrm{Mev}$ electrons) in the range of 2.9 to 5 Jovian radil. Because the half width of the radiation beam of an electron is $\sim \frac{1}{2 \gamma}$, electrons with pitch angles less than about $\frac{\pi}{2}-\frac{1}{2 \gamma}$ do not contribute to radiation perpendicular to $\vec{B}$. Thus, $\beta_{1} \cong 1-\frac{3}{4 \gamma^{2}}$ and $\alpha \cong \frac{1}{\gamma}$. Thus, $\frac{-m \alpha^{5}}{5} \cong \frac{-m}{5 \gamma^{5}}$ is very small and the exponential is unity for the purposes of this calculation.

Differentiation of (3) gives the expression for $J_{m}^{\prime}(x)$ to be used in expression (1), which then becomes

$$
\Delta f \frac{e^{2} \omega^{2} \beta^{4} \sin ^{4} \delta\left(\cos ^{2} \delta+\gamma^{-2} \sin ^{2} \delta\right)^{2}}{12 \pi^{3} \varepsilon_{0} c \omega_{0}} K_{2 / 3}^{2}\left[\frac{\omega \gamma}{\left(e B / m_{0}\right)} \frac{\left(\cos ^{2} \delta+\gamma^{-2} \sin ^{2} \delta\right)^{3 / 2}}{3}\right]
$$

for the power radiated per steradian perpendicular to $\vec{B}$ and polarized perpendicular to है.

The omnidirectional flux of particles of energy greater than $E$ was thus assumed to be (at the equator)

$$
\begin{equation*}
J(>E)=k(L) E^{-\Gamma(L)}, \tag{5}
\end{equation*}
$$

where $L$ is the number of Jovian radii from the center. The differential (in energy and pitch angle) flux corresponding to (5) is (in particles $/ m^{2} \times$ sec $\times$ steradian $x$ Mev)

$$
\begin{equation*}
j(\delta, E, L, \lambda)=\frac{k(L) \Gamma(L)}{2 \pi S(n)} E^{-(\Gamma+1)_{\sin ^{2}} n\left(E_{\delta} L\right)} \tag{6}
\end{equation*}
$$

where

$$
\begin{equation*}
S(n)=\int_{0}^{\pi} d \delta \sin ^{n+1} \delta \cong \sqrt{\frac{2 \pi e}{n}}\left(\frac{n}{n+1}\right)^{\frac{n+1}{2}} \tag{7}
\end{equation*}
$$

the approximation being Stirling's and in error by less than $2 \%$ for $\mathrm{n}>3$. As indicated by the notation, the pitch angle distribution can in principle be a function of energy as well as of the radial distance, although the data obtained from only two passes through Jupiter's magnetosphere is insufficient to determine the dependence. Van Allen et al. [1974] have taken

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$$
\begin{align*}
& n_{C}=3.5+(3.86 / \mathrm{L})^{8} \\
& n_{D}=4.0+(3.57 / L)^{8} \tag{8}
\end{align*}
$$

for the $C$ and $D$ detectors, respectively, as giving good closure between the inbound and outbound count rates (Figures 2 and 3). Because these detectors are energy integrating, $\mathrm{n}_{\mathrm{C}} \neq \mathrm{n}$ ( $21 \mathrm{Mev}, \mathrm{L}$ ) and $n_{D} \neq n(31 \mathrm{Mev}, \mathrm{L})$, but are averages of some sort. We have used the average $\bar{n}(L)$ of $n_{C}(L)$ and $n_{D}(L)$ in the radiation calculation, and kept $n$ independent of energy. Use of $\bar{n}$ does not introduce much error. Firstly, $S(n)$ in (6) varies roughly as $\frac{1}{\sqrt{n}}$, as can be seen in (7) for $n$ large. Secondly, the radiation integral (13) is totally Insensitive to $n$, since the integrand goes to zero very rapidly away from $\delta=\frac{\pi}{2}$ because of the angular dependence of the $K_{2 / 3}^{2}$ factor, not because of the angular dependence of $\sin ^{n+5} \delta$. The rapid cutoff by the $K_{2 / 3}^{2}$ is the mathematical manifestation of the narrow radiation beam of a relativistic electron. $\bar{n}$ decreases from 11.3 to 3.9 over the range $L=2.9$ to 5.0 .

The spectral index $\Gamma(L)$ is shown in Figure 4 and the coefficient $k(L)$ in Figure 5. They were obtained from the C and $D$ detector count rates as follows. Let

$$
\begin{equation*}
I(\Gamma)=\frac{\int_{0}^{\infty} d E R_{C}(E) E^{-(\Gamma+1)}}{\int_{0}^{\infty} d E R_{D}(E) E^{-(\Gamma+1)}} \tag{9}
\end{equation*}
$$

$R_{C}$ and $R_{D}$ being the count rates of the respective detectors per unit incident omnidirectional flux of electrons of energy E. Then $C(L) / D(L)=I[\Gamma(L)]$ is an integral equation to be solved for $\Gamma(L)$. $I(\Gamma)$ turns out to be given by $I(\Gamma)=2.818 \mathrm{e}^{0.4032 \Gamma}$ and therefore

$$
\begin{equation*}
\Gamma(L)=5.711 l_{E_{10}}[C(L) / D(L)]-2.570 \tag{10}
\end{equation*}
$$

The coefficient $k(L)$ is aetermined as follows: fram (5)

$$
\begin{equation*}
-\frac{\mathrm{d} J(>E)}{d E}=k(L) \Gamma(L) E^{-(\Gamma+1)} \tag{11}
\end{equation*}
$$

is the differential in energy flux. But

$$
\begin{equation*}
C(L)=\int_{0}^{\infty} d E R_{C}(E) \frac{-d J}{d E}=k(L) \Gamma(L) \int_{0}^{\infty} d E R_{C}(E) E^{-(\Gamma+1)} \tag{12}
\end{equation*}
$$

and $k(L)$ is determined because the integral is known from the detector calibration.

The curve $\Gamma(L)$ in Figure 4 indicates that the electron spectrum hardens as one comes in from $L=5$, reaches a maximum hardness at about $L=3.6$ and then softens. (The hump at $L=3.2$ may be only an artifact of exactly how the $C$ and $D$ curves turn over inside $\mathrm{L}=3.5$.) The qualitative physical interpretation could be that of
a hardening of the spectrum caused by energizing of the electrons as they diffuse inward, followed by a selective sapping of the more energetic electrons as the radiation region is entered at about 3.5. In any case the radiated power is remarkably insensitive to $\Gamma$, as will be discussed below.

THE RADIATION

Multiplication of the radiation per particle (1) by the particle density $j / c$ from (6) and integration over angle $\delta$ and energy E gives the total radiation from a unit volume per steradian at right angles to $\vec{B}$ and polarized $\perp \vec{B}$ :
$P$ (watts polarized $\perp \mathrm{B} / \mathrm{m}^{3} \times$ steradian $\left.\times \mathrm{Hz}\right)=$

$$
\begin{equation*}
\frac{e^{2} \omega^{2} \Gamma(L) k(L)(0.511)^{-\Gamma}}{12 \pi^{3} \varepsilon_{0} c^{2} S[n(L)]\left(e B / m_{0}\right)} \int_{0}^{\infty} d \gamma \gamma^{-\Gamma} \int_{0}^{\pi} d \delta \sin ^{n+5} \delta\left(\cos ^{2} \delta+\gamma^{-2} \sin ^{2} \delta\right)^{2} \tag{13a}
\end{equation*}
$$

$=\frac{e^{2} \omega 2 C(L)(0.511)^{-1}}{12 \pi^{3} \epsilon_{0} c^{2}\left[e B(L) / m_{0}\right] S[n(L)]} \frac{\int_{0}^{\infty} d E E^{-(\Gamma+1)} E \int_{0}^{\pi} d \delta \sin ^{n+5} \delta\left(\cos ^{2} \delta+0.261 E^{-2} \sin ^{2} \delta\right)^{2} K_{2 / 3}^{2}[\ldots]}{\int_{0}^{\infty} d E E^{-(\Gamma+1)} R_{C}(E)}$
the latter form upon substitution of $k(L)$ from (12). The radiation integral in (13a) has been evaluated numerically. The Jovian dipole moment was taken as 4.0 gauss $R_{J}^{3}$ [Smith, et al., 1974]. Westfold's [1959] table of $K_{2 / 3}(x)$ was used with appropriate interpolation. Table 1 gives the $\%$ contribution to the total radiation of electrons in various energy ranges ( $E \cong 0.511 \gamma \mathrm{Mev}$ ). The maximum contribution at each $L$ is underlined. Clearly the contribution of electrons between 5 and 21 Mev is negligible except around $L=2.9$, and even there the contribution cannot account for the discrepancy in Fisure 1. The calculated radiation is insensitive to the extrapolation via $\mathrm{E}^{-\Gamma}$ to energies below the C detector threshold of 21 Mev .

Table 2 illustrates the remarkable insensitivity to $\Gamma$. At each of the tabulated $L$ 's, the midale column is the radiation normalized to unity calculated for the "correct" $\Gamma$ of Figure 4. The other two columns show how the cilculated radiation would change for the same $C(L)$, but increased or decreased $\Gamma$. Although the double integral in (13a) is very sensitive to $\Gamma$, so is the coefficient in a conpensating sense. The explanation for the insensitivity is most easily visible in (13b), where all of the $\Gamma$ dependence is in the integrals. If the ratio $E \int_{0}^{\pi} d \delta \ldots / R_{C}(E)$ were independent of $E$, the radiation would be independent of $\Gamma$. With the use of Table 1 , it can be seen that at $L=2.9, E \int_{0}^{\pi} d \delta \ldots$ increases from zero at about 10 Mev to a maximum at about 56 Mev and then falls off gently out
to $\gamma=400$. On the other hand [Van Allen, et al., 1974] $R_{C}(E)$ increases in almost exactly the same fashion from zero at 10 Mev to a maximum at 60 Mev and remains constant at this maximum. The slight dependence on $\Gamma$ at $L=2.9$ arises from the slow fall off $E \int_{0}^{\pi} d \delta \ldots$ above its maximum. At $L$ greater than 2.9 , the $\Gamma$ dependence increases because the maximum of the $E \int_{0}^{\pi} d \delta \ldots$ curve shifts to higher energies, as can be seen in Table 1.

CONCLUSIONS

In conclusion, it seems impossible to find enough latitude in the parameters of our calculation to reduce our results by the necessary factor of 2 or more to obtain agreement with the Beard-Luthey curve. However, about half of the disagreement would have disappeared if they had used our equatorial angular distributions (8). Lacking better information at that time, they assumed an isotropic distribution in pitch angle from $6=48^{\circ}$ to $132^{\circ}$. Distribution (8) is more concentrated in the equatorial plane than this, hence, produces more radiation from the equator. If they had used angular distribution (8), their resolved curve would have been inigher by $\int_{4 e^{\circ}}^{132^{\circ}} d \delta \sin \delta / S(n)=1.34 / S(n)$. At $I=2.9$ this factor is 1.92 , while at $L=3.5$ it is 1.42. This leaves our calculation some $30 \%$ above their result at $L=3$, the \% discrepancy increasing with $L$. We consider this much disagreement acceptable in view of the uncertainty

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in their resolution of the low emission region at $L>3$, and of uncertainties in our calculation. Pioneer 11 will penetrate the mpre intense region near $L=1.7$ and permit a comparison where the Beard-Luthey curve is more reliable.

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## Table 1

The $\%$ Contribution to the Total Radiation of Various Electron Energy Ranges ( $\mathrm{E} \cong 0.5 \gamma \mathrm{MeV}$ )

| L | 5-20 | 20-40 | 40-60 | $60-80$ | 80-100 | 100-120 | 120-140 | 140-160 | 160-180 | 180-200 | 300-320 | 380-400 | $\leftarrow \gamma$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.9 | 0.01 | 13.6 | 32.6\% | 22.0 | 12.2 | 6.9 | 4.1 | 2.6 | 1.7 | 1.2 | 0.2 | 0.1 |  |
| 3.5 | 0.00 | 2.0 | 18.4 | 23.6\% | 17.6 | 11.7 | 7.7 | 5.2 | 3.6 | 2.6 | 0.5 | 0.2 |  |
| 4.0 | 0.00 | 0.3 | 8.5 | $\underline{19.7}$ | $\underline{19.2}$ | 14.6 | 10.3 | 7.2 | 5.1 | 3.7 | 0.8 | 0.4 |  |
| 5.0 | 0.00 | 0.0 | 0.8 | 7.3 | 14.8 | $\underline{16.3}$ | 14.1 | 11.2 | 8.5 | 6.4 | 1.4 | 0.7 |  |

Table 2
Sensitivity of the Radiation to $\Gamma$

| L | Using <br> $\Gamma-0.2$ | Radiation <br> Using <br> Correct $\Gamma$ | Using <br> $\Gamma+0.2$ |
| :---: | :---: | :---: | :---: |
| 2.9 | 0.97 | 1 | 0.97 |
| 3.5 | 1.05 | 1 | 0.94 |
| 4.0 | 1.09 | 1 | 0.88 |
| 5.0 | 1.18 | 1 | 0.83 |

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## FIGURE CAPTIONS

Figure 1. Emissivity of 10.4 cm radiation polarized parallel to the magnetic equator, as calculated from the electron fluxes and as deduced by Beard and Luthey from the Barge interferometer measurements.

Figure 2. Counting rate of the Iowa $C$ electron detector (energies > 21 MeV ) corrected to the magnetic equator for the inbound and outbound passes.

Figure 3. Counting rate of the Iowa D electron detector (energies > 31 Mev ) corrected to the magnetic equator for the inbound and outbound passes.

Figure 4. The integral (in energy) power law spectral index $\Gamma$. Figure 5. The coefficient $k(L)$ appearing in the integrated (in energy and angle) flux k(L) $\mathrm{E}(\mathrm{Mev})^{-\Gamma(L)}$.


Figure - 1

122<
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Figure 2

1 23 <


Figure 3

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Figure 4


Figure 5

