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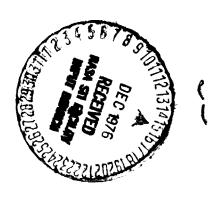
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# ANALYSIS OF EPITAXIAL DRIFT FIELD N ON P SILICON SOLAR CELLS



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#### ANALYSIS OF EPITAXIAL DRIFT FIELD N ON P SILICON SOLAR CELLS

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#### SUMMARY

Performance of epitaxial drift field silicon solar cell structures having a variety of impurity profiles has been calculated. These structures consist of a uniformly doped P-type substrate layer, and a P-type epitaxial drift field layer with a variety of field strengths. Several N-layer structures were modeled. A four layer solar cell model was used to calculate efficiency, open circuit voltage and short circuit current. The effect on performance of layer thickness, doping level, and diffusion length was determined. The results show that peak initial efficiency of 18,1% occurs for a drift field thickness of about 30 μm with the doping rising from 1017 atoms/cm3 at the edge of the depletion region to 1018 atoms/cm3 in the substrate. Stronger drift fields (narrow field regions) allowed very high performance (17% efficiency) even after irradiation to 3×10<sup>14</sup> 1 MeV electrons/cm2.

#### INTRODUCTION

Methods of improving silicon solar cell performance include incorporating back surface fields (BSF) (1-4) and drift fields (DF) (5-7) into the structure. The back surface field is an abrupt (i. e., several orders of magnitude) doping level change in a short (i. e., a few microns) distance. The drift field solar cell is usually made by epitaxial deposition in which doping level changes occur over longer distances.

The epitaxial BSF cell has been reported previously (4). It was shown that the BSF can be made by epitaxial deposition, that the substrate diffusion length can influence performance and that low-high junction theory can be used to predict cell performance. Experimental results on epitaxial drift field structures have also been reported (5). It was shown that reproducible good quality junctions can be made. Intentionally graded epitaxial drift field layers resulted in high (0,636 V) open circuit voltages. While these results are promising, a more comprehensive evaluation of doping profiles and epitaxial layer thickness ranges is needed to pinpoint optimum structures. Because the number of possible combinations of cell construction features and materials properties is great, an experimental evaluation would be time consuming and expensive.

The present work explores analytically the performance of a wide range of epitaxial drift field N on P solar cell structures. The purpose is to identify the cell design feature producing highest performance. A four layer solar cell model was used in these calculations. This model has been used previously (8, 9) to calculate solar cell performance with good agreement with experiment. Cell performance

calculated with this model includes short circuit current density,  $J_{SC}$ , open circuit voltage,  $V_{OC}$ , and efficiency. The influence on performance of field strength, substrate doping level, epitaxial layer width, diffusion length, and N-layer profile was determined. In all cases, the limits of present technology were used to determine achievable ranges and values for the modeling parameters so that the calculated performance would be realistic.

#### MODELING OF THE EPITAXIAL DRIFT FIELD CELL

#### Theoretical Model

The cell model used has been described elsewhere (8,9). It is based on a four layer, homojunction semiconductor device in which region widths, impurity concentrations, and material properties such as diffusion length, mobility, and reflectivity can be specified. A schematic of the cell model is shown in Fig. 1. Only exponential impurity distributions are assumed, resulting in constant drift field strengths within each layer.

The model was derived by solving the continuity equation using the current transport equation and appropriate boundary conditions to solve for the diode saturation current density ( $J_0$ ) and for  $J_{sc}$ . The  $V_{oc}$ , maximum power ( $P_{max}$ ) and air mass zero (AMO) efficiency (eff) were calculated from the following expressions:

$$V_{oc} = \frac{kT}{q} \ln \left( \frac{J_{sc}}{J_0} + 1 \right)$$
 (1)

$$P_{\text{max}} = CF V_{\text{oc}} J_{\text{sc}}$$
 (2)

$$EFF = \left(\frac{P_{max}}{135.3}\right) \times 100\% \tag{3}$$

where k is Boltzmann's constant, T is temperature, q is electronic charge, CF is curve factor which was calculated as previously described (8). The curve factor assumes unity diode quality factor (n = 1) and zero series resistance. For most cells, series resistance leads to about a 3% loss in power and curve factor. However, these data were not adjusted for that loss. The AMO solar constant used was 135, 3 mW/cm<sup>2</sup>.

Figure 2 shows the expected value of diffusion length as a function of doping level before radiation damage (10) and after a radiation fluence of  $3\times10^{14}$  1 MeV electrons/cm<sup>2</sup> (end of life, EOL) (11). Even though a ping level was assumed to vary exponentially in the epitaxial layer, only single values of diffusion length and mobility in each layer are possible

with the model used. The values chosen for modeling were based on the impurity concentration at the center of the epitaxial layer.

The four layer solar cell model has been used previously to calculate performance of epitaxial BSF cells (4), drift field lithium cells (8), and alloyed BSF cells (9). Agreement between calculated and experimental results was good. Thus extension of this model to the present study can be done with confidence.

#### P-Layer Data

The range of values for the doping level in the uniformly doped substrate,  $N_{sub}$ , and at the depletion region edge,  $N_{epi}$ , the width of the epitaxial layer,  $W_{epi}$ , and the diffusion length in the epitaxial layer,  $L_{epi}$ , are shown in Table I. The doping level combinations were constrained such that  $N_{epi} \leq N_{sub}$ . The field strength in the epitaxial layer,  $E_{epi}$ , can be calculated using these parameters and the equation

$$E_{epi} = \frac{kT}{qW_{epi}} \ln \left( \frac{N_{sub}}{N_{epi}} \right)$$
 (4)

The order of magnitude difference between the  $N_{\mbox{sub}}$  and  $N_{\mbox{epi}}$  doping concentration is defined as:

$$\Delta = \log_{10} \frac{N_{sub}}{N_{epi}}$$
 (5)

### N-Layer Data

The principal criterion for the design of the N-layer is that it yield high conversion efficiency, high short wavelength (0.4  $\mu m$ ) collection efficiency, and high  $V_{\rm OC}$ . There are a large number of N-layer constructions and an even larger number of possible P-layer configurations. In order to limit the number of calculations, guidelines were used to reduce the number of N-layer profiles evaluated to six.

These guidelines were that: (1) junction depth,  $X_j$ , be shallow ( $\leq 1~\mu$ m) for good collection efficiency, (2) carrier concentrations be high for good  $V_{OC}$  but no higher than  $10^{19}$  atoms/cm<sup>3</sup> to avoid heavy doping effects (13, 14), and (3) present epitaxial technology limits doping level changes to about two orders of magnitude and layer widths to a minimum of 1 micron. In addition, surface reflectivity of 3% (12) and a front surface recombination velocity of  $10^3$  cm/sec were used. A diffusion length of  $3~\mu$ m was used in the N-layer. This value is comparable to those measured on bulk material doped to this level.

With these guidelines, the N-layer profiles shown in Fig. 3 were used in the calculations. The A and B profiles could be made by epitaxial deposition of a uniformly doped N-layer with subsequent diffusion of a more heavily doped, N-type profile. The C and D profiles are typical of those obtained by diffusion, however, a 0.25 µm layer thickness may be too thin for epitaxial deposition. These layers were included in the evaluation for comparison to more conven-

tional N-layer profiles. The E and F profiles could be made by epitaxial deposition directly.

#### RESULTS AND DISCUSSION

## N-Layer Effects

The sensitivity of cell performance to N-layer profile was investigated. Calculations were made for two P-layer profiles with each N-layer profile shown in Fig. 3. The P-layer profiles were  $N_{sub} = 10^{18} \text{ cm}^{-3}$ ,  $N_{epi} = 10^{17} \text{ cm}^{-3}$ , and  $N_{sub} = 10^{17} \text{ cm}^{-3}$ ,  $N_{epi} = 10^{16} \text{ cm}^{-3}$ .

Table II shows collection efficiency, Voc and conversion efficiency for each N-layer profile. The performance is high even for the 1 micron junction depth profiles. This is due to the good N-layer parameters used and shows that shallow junctions are not needed if 3 µm diffusion length in the Nlayer is achieved. Profiles C and D are less desirable because the 0,25 micron junction depth may not be attainable by epitaxial methods. Profiles A and B have somewhat lower performance than profile E. Note that although the difference in collection efficiency between C and E seems high, there is only 0.1 percent difference in efficiency. Although profile F has a higher collection efficiency (due to its higher field strength), the Voc is lower because of the lower impurity concentration at the depletion region edge. This leads to a lower efficiency. Profile E has a high overall performance and can also be fabricated with existing epitaxial technology. Therefore, based on these results, profile E was used for the remaining calculations with the Player.

#### P-Layer Effects - Initial Performance

Using the expected values of  $L_{epi}$  shown in Fig. 2, each of the P-layer cases has a maximum efficiency at some value of  $N_{epi}$  and  $W_{epi}$ . The highest of these maxima (called the peak efficiency) for each value of  $N_{sub}$  is shown in Fig. 4. The  $N_{sub} = 10^{18} \, \mathrm{cm}^{-3}$  case has the best overall efficiency, 18.1%. For higher or lower values of  $N_{sub}$ , efficiency drops.

In Fig. 5, the importance of N  $_{\rm epi}$  in achieving high efficiency is shown. Maximum efficiency for each case is plotted against N  $_{\rm sub}$  with N  $_{\rm epi}$  as a parameter. Note that Fig. 4 was derived from Fig. 5 by plotting the upper envelope of efficiency at each N  $_{\rm sub}$  doping level. The overall highest efficiency, 18.1%, is for the N  $_{\rm sub}$  = 10  $^{18}$  cm  $^{-3}$ , N  $_{\rm epi}$  = 10  $^{17}$  cm  $^{-3}$ ,  $\Delta$  = 1 case. The next closest efficiencies of about 17.8% are for the uniformly doped 10  $^{17}$  cm  $^{-3}$  and 10  $^{18}$  cm  $^{-3}$  cases. Thus these three cases define the area of greatest interest to the solar cell designer.

The uniformly doped  $10^{17}~{\rm cm}^{-3}$  case gives the highest  $J_{\rm sc}$  (43.8 mA/cm²) because of its high diffusion length. The uniformly doped  $10^{18}~{\rm cm}^{-3}$  case gives the highest  $V_{\rm oc}$  (0.703 V) because of its high doping levels at the depletion region edge. However the efficiencies in these cases are

somewhat lower than the  $N_{sub} = 10^{18}$  cm<sup>-3</sup>,  $N_{epi} = 10^{17}$  cm<sup>-3</sup> case. This latter case is a better compromise between the uniformly doped cases because high voltage (0.671 V) is attained without significantly reducing  $J_{sc}$  (43.5 mA/cm<sup>2</sup>). The doping level, diffusion length and drift field aided collection combine to give best performance in this case. Thus moderate drift fields do offer a performance advantage at beginning of life.

High doping level differences ( $\Delta$  > 2) are not an advantage. For example at N<sub>sub</sub> =  $10^{19}$  cm<sup>-3</sup>, the highest efficiency of 16.75% is for N<sub>epi</sub> =  $10^{17}$  cm<sup>-3</sup>,  $\Delta$  = 2. Higher values of doping level difference ( $\Delta$  > 2) do not result in the highest maximum efficiency. At N<sub>sub</sub> =  $10^{19}$  cm<sup>-3</sup>, maximum efficiency at N<sub>epi</sub> =  $10^{16}$  cm<sup>-3</sup>,  $\Delta$  = 3 is below that for the N<sub>epi</sub> =  $10^{17}$  cm<sup>-3</sup>,  $\Delta$  = 2 case.

Figure 5 also shows that for  $N_{sub} \le 10^{17}~cm^{-3}$ , peak efficiency is for a nonfield, conventional cell, i.e.,  $N_{sub} = N_{epi}$ ,  $\Delta = 0$ . Thus for lightly doped substrates, the drift field epitaxial cell has no advantage. The  $V_{oc}$  achieved with high  $N_{epi}$  makes a greater contribution to performance than that due to the high field strengths which result from low  $N_{epi}$ .

Figure 6 shows the variation of efficiency with width of the epitaxial layer for the  $N_{\rm epi}=10^{17}~{\rm cm}^{-3},~N_{\rm sub}=10^{18}~{\rm cm}^{-3}$  and  $10^{19}~{\rm cm}^{-3}$  cases. Maximum efficiency of 18.1% for  $N_{\rm sub}=10^{18},~N_{\rm epi}=10^{17},~\Delta=1$  case is at  $W_{\rm epi}\approx30$  microns. Equation (4) shows that this corresponds to a field strength of about 20 V/cm. This peak is due to a balance between increasing  $V_{\rm oc}$  and decreasing  $J_{\rm sc}$  as  $W_{\rm epi}$  decreases. This effect is shown more fully in Fig. 7. These data are for the  $N_{\rm sub}=10^{18}~{\rm cm}^{-3},~N_{\rm epi}=10^{17}~{\rm cm}^{-3}, \Delta=1$  case. Maximum efficiency of 18.1% occurs at about  $W_{\rm epi}=30$  microns. The increase of  $V_{\rm oc}$  as  $W_{\rm epi}$  decreases is due to increasing field strength and to the decrease of the ratio of  $W_{\rm epi}$  to  $L_{\rm epi}$ . This decreasing ratio leads to a decrease in the calculated reverse saturation current and thus increasing  $V_{\rm oc}$ .

The effect of epitaxial layer diffusion length on efficiency for the  $N_{\rm sub}=10^{18}~{\rm cm}^{-3}$ ,  $N_{\rm epi}=10^{17}~{\rm cm}^{-3}$  case is shown in Fig. 8. The 18.1% efficiency discussed above occurs at a  $L_{\rm epi}=60~\mu{\rm m}$  value obtained from Fig. 2 for this substrate doping level. If epitaxial technology cannot produce material with this diffusion length, then peak efficiency will be reduced. Conversely, if epitaxial methods can produce higher diffusion length materials at these doping levels, higher peak efficiencies appear possible.

#### P-LAYER EFFECTS - END OF LIFE PERFORMANCE

In Fig. 9, peak efficiency is plotted against  $N_{sub}$  for the end of life (EOL)  $L_{epi}$  values shown in Fig. 2. The initial peak efficiency curve from Fig. 4 is included for reference. After a fluence of  $3\times10^{14}~{\rm cm}^{-2}$  the highest peak effi-

ciency of 17.1% is still for the  $N_{sub} = 10^{18} \text{ cm}^{-3}$ , and  $N_{epi} = 10^{17} \text{ cm}^{-3}$  case. Higher and lower values of  $N_{sub}$  have EOL efficiencies below 17%.

Figure 10 shows efficiency against  $W_{epi}$  for the  $N_{sub}$  =  $10^{18}$  cm<sup>-3</sup>,  $N_{epi}$  =  $10^{17}$  cm<sup>-3</sup> case for several values of  $L_{epi}$ . The maximum efficiency point shifts from  $W_{epi}$  =  $30~\mu m$  (field strength of 20 V/cm) to  $W_{epi} \approx 8~\mu m$  (field strength of 75 V/cm) as  $L_{epi}$  decreases. This shows the importance of field strength in achieving high EOL efficiencies. Note that the initial and EOL peak efficiency values do not occur for the same cell structure. However, by altering layer thickness to about 15  $\mu m$ , a nearly optimum performance can be achieved. In this case, initial efficiency is about 18% while EOL efficiency is 17.1%. Another design choice would be to minimize decrease in performance with radiation fluence. In that case, an  $8~\mu m$  thick layer would have an initial efficiency of 17.2%.

#### CONCLUSIONS

The P-region doping levels of greatest interest to the solar cell designer have been identified as ranging between  $10^{17}~{\rm cm}^{-3}$  and  $10^{18}~{\rm cm}^{-3}$ . Within this range tradeoffs between  $V_{\rm OC}$  and  $J_{\rm SC}$  plus use of drift fields combine to give the highest efficiency. Drift fields slightly improve solar cell beginning of life performance within this range. A peak initial efficiency of 18.1% was calculated for the substrate doping level of  $10^{18}~{\rm cm}^{-3}$ , epitaxial layer doping level of  $10^{17}~{\rm cm}^{-3}$ , epitaxial layer width of  $30~\mu{\rm m}$ , field strength of  $20~{\rm V/cm}$  P-layer case. Diffusion length of  $60~\mu{\rm m}$ , the drift field and good solar cell properties combine to yield this efficiency,

High values of field strength in the epitaxial layer (i.e., above approximately 100 V/cm) do not result in the highest efficiencies. The cell structures that produced the highest efficiencies for substrate doping levels  $\leq 10^{17}~{\rm cm}^{-3}$  were nonfield, iniformly doped structures. This is because the open circuit voltages achieved with high values of epitaxial layer doping level are greater than those obtained in the high field case where this value is necessarily low.

High collection efficiencies (i. e., above 0.95) and high conversion efficiencies are possible with deep (1  $\mu$ m) junction depths if high (3  $\mu$ m) diffusion lengths are assumed,

The highest efficiency for end of life  $(3\times10^{14}~{\rm e/cm^2})$  was 17.2%. This occurs for a substrate doping level of  $10^{18}~{\rm cm^{-3}}$  epitaxial layer doping level of  $10^{17}~{\rm cm^{-3}}$ , and epitaxial layer width of 8  $\mu$ m. Field strength is an important parameter for achieving high EOL efficiency. Thin epitaxial layers and high field strengths give the best EOL efficiencies. Change of  $W_{\rm epi}$  to 15  $\mu$ m results in near optimum initial and EOL performance. This yields a cell with initial efficiency of 18.0% and an EOL efficiency of 17.1%. This represents a tradeoff between highest initial and EOL efficiency.

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TABLE I. - RANGE OF PARAMETERS
USED TO MODEL DRIFT FIELD
SOLAR CELL

Parameter	Range		
N <sub>sub</sub>	10 <sup>14</sup> to 10 <sup>19</sup> atoms/cm <sup>3</sup> 10 <sup>14</sup> to 10 <sup>19</sup> atoms/cm <sup>3</sup>		
W <sub>epi</sub>	8 to 178 μm		
L <sub>epi</sub>	10 to 100 μm		
E <sub>epi</sub>	0 to 372 V/cm		
Δ	1 to 5		

TABLE II. - SUMMARY OF PERFORMANCE OF CELL WITH DIFFERENT N-LAYER PROFILES

N-layer profile	Junction depth, µm	Collection efficiency, at 0.4 μm	v <sub>oc'</sub>	Efficiency,
A	1	0,912	0.675	17.3
В	1	. 944	. 620	15.9
C	. 25	. 992	. 691	18, 1
D	. 25	. 996	. 679	17.8
E	1	.958	. 689	18.0
F	1	. 979	.662	17.3

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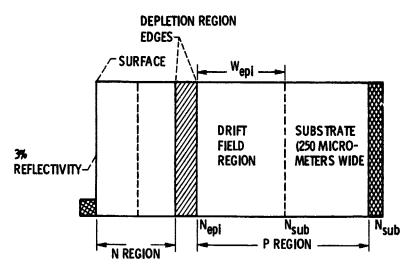


Figure 1. - Cross section of drift field cell model.

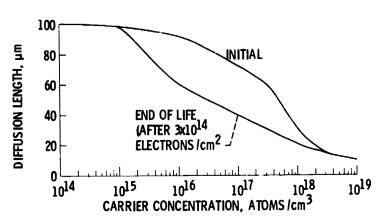
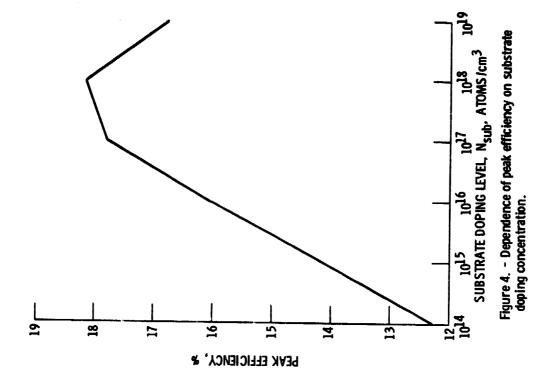
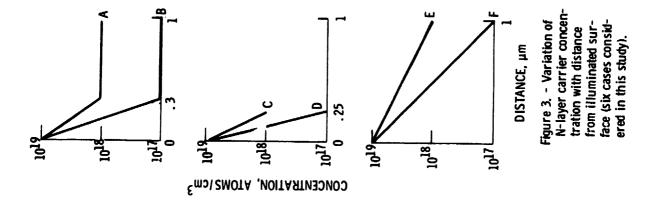


Figure 2. - Variation of diffusion length with carrier concentration before and after electron irradiation.





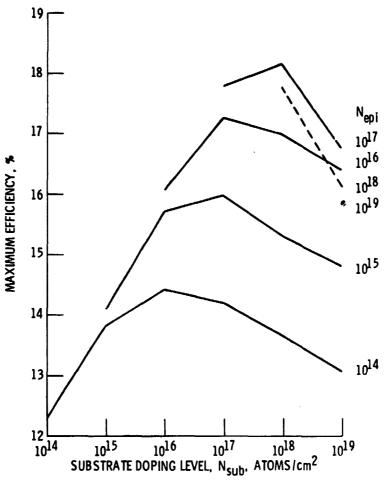
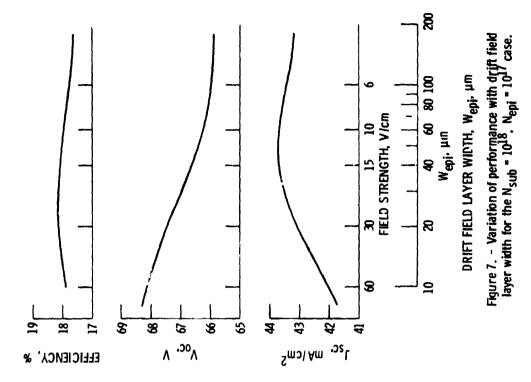


Figure 5. - Variation of maximum efficiency with substrate doping level for values of epitaxial level.



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Figure 6. - Dependence of efficiency on urift field layer width for two doping level cases.

8

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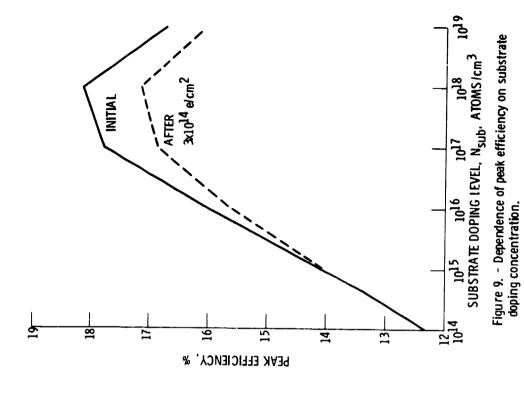
EFFICIENCY, №

N<sub>sub</sub> N<sub>epi</sub> ∆

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81

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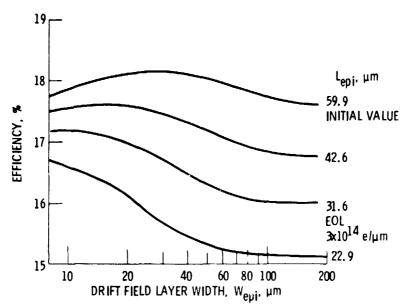


Figure 10. - Variation of efficiency with drift field layer width for values of diffusion length.