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# CREEP-RUPTURE DATA ANALYSIS -

ENGINEERING APPLICATION OF REGRESSION TECHNIQUES

by

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A thesis submitted to the Graduate Faculty of North Carolina State University at Raleigh in partial fulfillment of the requirements for the Degree of Doctor of Philosophy

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#### ABSTRACT .

RUMMLER, DONALD ROBERT. Creep-Rupture Data Analysis -Engineering Application of Régression Techniques (Under the direction of HAYNE PALMOUR III).

The creep and rupture behavior of materials can control the design of structures which operate at elevated temperatures. In lieu of an adequate fundamental understanding, current design practice makes use of a variety of empirical techniques to predict creep behavior.

The results of investigations to apply regression techniques to the development of methodology for creep-rupture data analysis are presented. Regression analysis techniques are applied to the explicit description of the creep behavior of materials for space shuttle thermal protection systems. A regression analysis technique is then compared to five parametric methods for analyzing three simulated and twenty real data sets. Finally, a computer program for the efficient evaluation of creep- rupture data with five parametric methods is presented.

### BIOGRAPHY

Donald R. Rummler was born **provided** in **provide**, , the son of a master tailor. He received his elementary and secondary education in Cheraw, South Carolina and Belmont, North Carolina, graduating from Belmont Abbey Preparatory School in 1955.

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The author also expresses heartfelt thanks to his parents who stimulated and encouraged his curiosity. Finally, the author expresses his thanks to his wife, Mary, and children, Mark, Kathy, and Karen, for their patience and constant support.

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# GENERAL INTRODUCTION

The creep-rupture behavior of materials can and does control the design of many structural components. Designers and analysts in the nuclear power generation, aerospace turbine, and chemical processing industries, for example, are required to design structural components which must operate reliably for periods up to forty years in complex, high temperature environments. Unfortunately, the current state of our understanding of the creep process does not allow the use of "first principles" for sizing components and predicting their service behavior. Consequently, the creep-rupture design techniques used today can at best be called "enlightened. empiricism." There is no generally accepted method of analysis for the prediction of creep-rupture behavior. In fact, a method which works well for one material very often will not work well for a different material.

The purpose of the investigations reported herein was to explore the application of regression analysis techniques to the analysis of creep-rupture data of interest in aerospace applications. They constitute a part of a continuing effort, begun in 1970, to provide the materials related methodology necessary to design efficient aerospace vehicles.

The first paper deals with the application of regression analysis to the creep of space shuttle materials. Regression

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techniques are used as a tool (1) to assess the effects of sheet thickness and oxygen partial pressure on the steady-state creep behavior, (2) to analytically describe the low creep strain behavior, and (3) to assess the effects of data scatter for materials where data are limited.

The third paper describes the development and use of a computer program for parametric analysis of creep rupture data. The program includes provisions for the analysis of five different parameter methods. Sample problems to aid the user in setting- up a problem are presented.

# APPLICATION OF REGRESSION ANALYSIS TO CREEP OF

# SPACE SHUTTLE MATERIALS<sup>1</sup>

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<sup>&</sup>lt;sup>1</sup>Published in proceedings of International Conference on Creep and Fatigue in Elevated Temperature Applications, Philadelphia, PA, September 1973 and Sheffield UK, April 1974; Conference publication 13, Institution of Mechanical Engineers.

#### APPLICATION OF REGRESSION ANALYSIS TO CREEP OF

#### SPACE SHUTTLE MATERIALS

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#### ABSTRACT

Regression analysis techniques were used to assess the effects of sheet thickness and oxygen partial pressure and to develop constitutive creep equations. Application of prediction intervals is emphasized.

## 1 SYNOPSIS

Metallic heat shields for Space Shuttle thermal protection systems must operate for many flight cycles at high temperatures in low-pressure air and use thin-gage ( $\leq 0.65$  mm) sheet. Available creep data for thin sheet under those conditions are inadequate. To assess the effects of oxygen partial pressure and sheet thickness on creep behavior and to develop constitutive creep equations for small sets of data, regression techniques are applied and discussed.

> 2 SYMBOLS  $\epsilon$  = creep strain t = time, hours th = sheet thickness, mm T = temperature, K  $\sigma$  = stress, MN/m<sup>2</sup> x, y, z, D,  $\phi$  = dummy variables

#### 3 INTRODUCTION

Recent Space Shuttle technology research and development studies ((1)<sup>\*</sup> and (2)) have indicated that the creep behavior of high-temperature alloys may control the design and reusability of metallic heat shields for radiative thermal protection systems (TPS). The heat shields function as lightly loaded aerodynamic surfaces, and they must efficiently utilize thin-gage sheet to avoid weight penalties. Loads are applied at high temperature, when the local partial pressure of oxygen is low. In general, creep strains must be limited to less than 0.005 to avoid excessive panel deflections.

The creep data which exist for candidate superalloys are for steady-state creep tests run on relatively thick specimens at atmospheric pressure. These data are presented as time to a given strain level for various combinations of stress and temperature (see, for example, Refs. (3) and (4)). Attempts to use this type of data to predict the cyclic creep deformation of simple tensile specimens or for the preliminary design of heat shields underestimated the experimental creep strains by as much as a factor of 10 ((1) and (2)). These predictions typically utilized one of the parameter methods (5) combined with a life fraction approach to sum the cyclically accumulated strains. This failure to predict the experimental creep strains could be the result of one or both of the following:

(1) The data upon which calculations were based were for the creep of relatively thick specimens at atmospheric pressure, and may not be applicable to thin specimens at low pressure.

<sup>\*</sup> References are given in Appendix 1.

(2) No analytic expression was available which could account for both the nonlinear primary and linear secondary creep stages.

The purpose of this paper is to present the results of an investigation to determine the applicability of regression analysis techniques to predict creep behavior when data are limited. Three applications of regression techniques which address the aforementioned shuttle TPS creep problems are discussed. Regression techniques are used as a tool (1) to assess the effects of sheet thickness and oxygen partial pressure on steady-state creep behavior, (2) to analytically describe the low creep strain behavior, and (3) to assess the effects of data scatter for materials when data are limited.

#### 4 ANALYSIS PROCEDURES

## 4.1 Development

To evaluate trends in creep data and to predict creep behavior, explicit expressions for the mean and the expected upper and lower bounds for creep strain data as a function of stress, temperature, and time were desired. Little information is available about the form of these expressions for the candidate materials at low levels of creep strain. Consequently, two computer programs were written and applied to develop the desired expressions. Both programs utilize standard linear regression techniques (6). One program was of the form:

$$w = b_0 + b_1 \mu$$
(1)  

$$w = \log (\text{stress})$$
  

$$u = \log (\text{time})^{\prime}$$

where

This program was used to generate coefficients, mean value estimates, and 95 percent prediction intervals<sup>\*</sup> for data at specific values of strain and temperature.

The second program was used to develop models for creep strain as a function stress, temperature, and time. For this multiple regression program, the equation form assumed was:

$$f(y) = g\left\{ \left( a_{1}x_{1}^{2} + b_{1}x_{1} + c_{1} \right) \left( a_{2}x_{2}^{2} + b_{2}x_{2} + c_{2} \right) \left( a_{3}x_{3}^{2} + b_{3}x_{3} + c_{3} \right) \right\}$$
(2)

where y,  $x_1$ ,  $x_2$ , and  $x_3$  are, respectively, functions of creep strain, stress, temperature, and time.

Provision for transformation of y,  $x_1$ ,  $x_2$ , and  $x_3$  was included in the program. The transformations, which included many of those found useful for analysis of creep data (7) were as follows:

<sup>&</sup>lt;sup>\*</sup>The prediction interval (6) is used to make a statement about the anticipated value of the dependent variable (y) for a future single observation at a specific value of the independent variable (x) or variables  $(x_i, x_j, x_k \dots)$ ; for example, y will be between 2 and 6 for 95 percent of all future single observations taken at x = 3. The more familiar confidence interval, on the other hand, is used to make statements about the true mean value of y; for example, there is a 95-percent probability that the true mean value of y at x = 3 is between 3 and 5. The prediction interval limits are wider since these include both the sampling errors and the uncertainties in estimating the mean value of y.

Transformation Code (TCj)	Transformation $(0 \le i \le 3)$
0	$x_i = z_i$
1	$x_i = \log (z_i)$
2 ′	$x_i = 1/z_i$ .
3	$x_{i} = \log (1/z_{i})$
4	$x_i = ln(z_i)$
· 5	$x_{i} = (z_{i})^{1/2}$
ę	$\mathbf{x}_{i} = \mathbf{z}_{i} + 1.0$
7	$x_{i} = \log (z_{i} + 1.0)$
8`	$x_{i} = (z_{i})^{1/3}$

where the  $z_i$  are specific values of stress, temperature, or time. Similar functional transformations (y = f(D)) were used for strain. Each transformation combination was assigned a four-digit transformation number where the digits are the transformation code values for y,  $x_1$ ,  $x_2$ , and  $x_3$ , respectively.

Thus transformation 1025 used the following transformations:

y = log D = log (c) x<sub>1</sub> = z<sub>1</sub> =  $\sigma$ x<sub>2</sub> = 1/z<sub>2</sub> = 1/T. x<sub>3</sub> = (z<sub>3</sub>)<sup>1/2</sup> = (t)<sup>1/2</sup>

Creep data sets usually include a wide range of times, typically three orders of magnitude, whereas the ranges for creep strain, stress, and temperature are seldom in excess of one order of magnitude. Early analysis of nultiple regression computer runs revealed that the combination of the wide range in the variables associated with creep data sets and equation forms which include terms that can be highly colinear, such as x and  $x^2$ , led to ill-conditioned normal equations which were subject to significant round-off errors during a matrix inversion operation. In order to minimize these errors, the data were scaled from 1 to 10 after transformation of the primary variables (y,  $x_1$ ,  $x_2$ ,  $x_3$ ) as follows:

$$y_{i} = 9.0 (y_{i} - y_{min}) / (y_{max} - y_{min}) + 1$$
$$x_{ij} = 9.0 (x_{ij} - x_{i min}) / (x_{i max} - x_{i min}) + 1$$

where  $y_{\min}$  and  $y_{\max}$  are the minimum and maximum values of the transformed strain. The x and x have similar definitions as they apply to the transformed values of stress, temperature, and time.

After transforming and scaling the primary variables, Equation (2) was expanded and new independent variables, defined as follows, were introduced:

$$y = a_{1}a_{2}a_{3}\left(x_{1}^{2}x_{2}^{2}x_{3}^{2}\right) + a_{1}a_{2}b_{3}\left(x_{1}^{2}x_{2}^{2}x_{3}\right) + \dots = \sum_{j=1}^{k} \phi_{j}z_{j}$$
(3)

This procedure results in an equation with 27 terms having linear coefficients  $(\phi_i)$ .

Some values of  $\phi_j$  were set equal to zero so that, in Equation (3), the order (degree of interaction) for the number of terms in the regression analysis could be reduced as follows:

k	Order	(Allowed term types)
23	4th	$\left(x_{l}x_{m}x_{n}^{2}$ and $x_{l}^{2}x_{m}^{2}\right)$
17	3rd	$(x_{l}x_{m}x_{m} \text{ and } x_{l}^{2}x_{m})$
10	2nd	$(x_2 x_m)$
4	lst	(x <sub>l</sub> )

(Note that the reduced form can no longer be factored back to Equation (2).)

## 4.2 Application

To perform a multiple regression analysis using Equation (3), the order of the equation (k value) was selected first. Next, the transformations to be used on the primary variables were selected. Each observation of the data set was transformed, then scaled. The transformed and scaled values for strain, stress, temperature, and time were then used to generate values for the additional variables in Equation (3). This data set was then used in the regression analysis. The mean values of creep strain were calculated from the coefficients derived during a multiple regression analysis. Explicit functions for the upper and lower bounds (95 percent prediction intervals) were calculated by treating either the upper or lower prediction limit calculated for each observed value of strain during the initial regression as another set of observed strain values; two additional regression analyses provided the desired coefficients. The residual mean square (RMS) for the prediction interval "data" sets were always extremely small ( $\approx 10^{-7}$  times that of the original data set analysis). This suggests that the errors involved in these approximations for the original prediction intervals were not large.

After a regression analysis was performed, all variables and residuals were descaled and back-transformed. Several quasi-statistical parameters were then calculated to aid model development and "best-equation" selection. These parameters are described as they are introduced.

#### 5 RESULTS AND DISCUSSION

The following examples illustrate how regression techniques were applied to three areas of creep behavior which are of interest in Space Shuttle TPS creep studies. These areas are typical of those which can occur during the preliminary design phases of any program when extensive creep data are not available.

## 5.1 Use of Simple Regression (Equation (1))

Haynes alloy H-188 is a cobalt base alloy which has excellent oxidation resistance and moderate elevated temperature strength. It is a candidate material for TPS application up to 1250 K. The creep data base consists primarily of the work reported in (4). This work includes creep tests on H-188 sheet from 10 production heats and for thicknesses ranging from 0.51 to 2.03 mm. All creep tests were run in air at standard pressure.

Figure 1 presents the data at 1144 K at a strain level of 0.002. A regression analysis was performed on the data set with sheet thickness  $\leq 0.84$  mm. These data will be defined herein as the "standard data," against which data from future observations will be compared. The regression line and the 95-percent prediction interval for the standard data are also shown on the figure. The results shown in Figure 1 allow the following statements to be made:

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(1) Ninety-five (95) percent of all future observations made under the same test conditions are expected to fall within the prediction interval for sheet thicknesses between 0.51 and 0.84 mm. If creep data from tests at lifferent test conditions generally fall outside of the prediction interval, shen the new test conditions have probably changed the creep behavior of the naterial.

(2) Most of the data for the > 0.84 mm fall well within the prediction interval for the "standard data." Thus, the  $\epsilon = 0.002$  creep strength of laynes alloy H-188 at 1144 K is not significantly different for sheet thicklesses from 0.51 to 2.03 mm. This is in contrast to the results presented in (4) where creep rupture strengths of sheet  $\leq 1.27$  mm thick were lower than those for sheets >1.27 mm thick.

The prediction interval and mean line from Figure 1 for the "standard lata" are shown in Figure 2. Also shown in Figure 2 are the results of preep tests run in another laboratory on thin-gage H-188 at both standard and reduced pressures of air. The focus provided by the prediction interval indipates that the  $\epsilon = 0.002$  creep strength of H-188 for sheet thicknesses between 0.51 and 0.64 mm both at standard atmospheric and reduced pressures was not significantly different from that previously established for 0.51 to 0.84 mm sheet at standard atmospheric pressure. However, for thinner sheet (0.254 mm) at reduced pressure creep, strength was significantly higher as indicated by the many test data points (open circles) above the prediction interval. Similar results were observed for other strain leyels at 1144 K.

The conclusions drawn from Figure 2 could have been reached with far fewer tests (as few as 2 or 3 for any of the test conditions shown). The use of prediction intervals data appears to be an efficient technique to explore

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the effects of "nonstandard" creep conditions and to compare creep data from different sources. This is particularly useful during the preliminary design phases of a program when the consequences of "nonstandard" conditions, such as thin gage or low air pressure, must be assessed rapidly and maximum use of existing data base for thicker material at atmospheric air pressure is necessary.

# 5.2 Use of Multiple Regression (Equation (3))

To explore the effects of primary creep and various hardening rules, such as strain hardening, on the accumulation of cyclic creep strain, it is useful to have a constitutive relationship for steady-state creep strain. This is particularly true when the data base is limited and does not include a large number of test stresses and temperatures.

The data set (8) for René sheet (solution treated at 1450 K and aged at 1172 K) was selected to demonstrate the application of multiple-regression techniques to develop a constitutive creep equation. Creep tests were conducted at 1005, 1089, and 1172 K. Tests were not replicated. For this study, 142 strain-time data points (observations) with strain levels from 0.0005 to 0.005 were selected as input for the multiple regression analyses.

In addition to a normal regression analysis, the program numerically solved the resulting equation to estimate the time  $(t_{\epsilon})$  required to reach each input strain level. To assure compatibility with a strain-hardening cyclic-creep analysis, all equation forms which did not permit efficient solutions (less than 500 iterations) for all  $t_{\epsilon}$  were rejected. The program also rejected all equation forms which calculated either a negative strain or time. Early computer runs revealed that the multiple correlation coefficient square  $(R^2)$  and the residual mean squared error (MSE), commonly used (7) to

rapidly evaluate a large number of equation alternatives were poor discriminators for this data set and these variable transformations. The following parameters were determined from the descaled and back-transformed calculated values of strain and time:

- EMSE (strain mean squared error)
- E/TO (maximum calculated strain at t = 0.001 h)
- T/EO (maximum calculated time at  $\epsilon = 0.000001$ )
- AE (average strain error)
- ATP (average time error, percent)

These parameters have recognizable consequences in the preliminary design sense and were considered useful discriminators for the selection of a "best" equation. Numerous variable transformations were evaluated in a single computer run. Typically, 200 different transformations were examined in a single 600-second computer run.

Analysis of several "best" equations during early computer runs indicated that the equations were often unstable near time = zero. This unstable behavior is illustrated in Figure 3 for typical values of stress and temperature. This failure to predict  $\epsilon = 0$  at t = 0 was eliminated by assuming an unrecorded data point ( $\epsilon = 0.000001$ , t = 0.001 h) for each creep test reported in (8). These assumed data points were added to the initial data set to yield the 167 data points and were included in all further regressions. The dashed line in Figure 3 shows that a typical predicted creep curve using the additional assumed points is reasonable, although the fit to the original data (open circular symbols) is not as good.

Even with the addition of the assumed data points, none of the variable transformations yielded a satisfactory prediction equation for the k = 27

version of Equation (3). The model was unstable when projected on log-stress, log-time plots. At the lowest test temperature (1005 K) and short test times ( $\approx$  10 h) these equation forms began to predict longer times for a particular level of creep strain as the stress was increased. For this particular data set, run 4124 with k = 23 produced the "best" model equation. This run produced the lowest values of EMSE, AE, and ATP and computed  $E/TO \leq 0.000001$ and  $T/EO \leq 0.01$  hr. The use of fewer terms in the model (k < 23) significantly increased the EMSE, AE, and ATP values calculated with the original 142 observations. This is illustrated in the following table:

	23	$\frac{k}{10}$	_7
emse (× 10 <sup>7</sup>	6,71	7.25	9.14
AE (× 10 <sup>3</sup> )	550	622	730
ATP (0/0)	33	37	74

Thus for this data set, the inclusion of the higher order interaction terms in the model significantly improved the model's ability to fit the data.

The degree of fit typically provided by "best" model equation is illustrated in Figure 4 for  $\epsilon = 0.002$ . The symbols are the data taken from (8), the solid lines are the mean stress and the 95-percent prediction interval calculated from a regression of log time on log stress using only those data points shown for each temperature. The dashed lines are the mean stress values and the 95-percent prediction intervals calculated by run 4124, k = 23 which included all of the 167 data points available in the data set. Agreement between the two calculated mean stress values is considered good. More importantly, however, this figure illustrates that the calculated 95-percent prediction intervals from run 4124, k = 23 are consistent with those obtained from the linear regressions on the data for each temperature. This indicates that the model is probably as good as the data scatter warrant and that the consequences of this scatter can be adequately assessed in a steady-state creep analysis by utilizing the coefficients determined by run 4124 to calculate mean creep strains and the coefficients determined for the lower bounds of the prediction interval shown in Figure 4 to calculate maximum creep strains. For instance, a "best" model equation could be used to calculate creep strains at intermediate values of temperature to compare with other creep data obtained by other investigators.

Figure 5 illustrates some typical mean creep curves calculated with the coefficients determined for the "best" equation. The shapes of these curves are consistent with those obtained by fairing through the original data points. More importantly, the curvilinear nature of the creep curves demonstrate that the model equation applies even when creep strain does not accumulate linearly as a function of time. Therefore, the model is functionally capable of accounting for the effects of primary stage creep in a strain-hardening analysis of cyclic creep.

To further assess the applicability of the regression analysis, the standard deviations for the average percentage time error for strain levels 0.001, 0.0015, and 0.002 were calculated. These standard deviations were compared to similar results obtained from three optimized "C" value Larson-Miller analyses (5) of the data at these strain levels with the following results.

Comparison of Standard Deviation of Percent Time Errór

	Larson-Miller	Run 4124, $k = 23$
0.001	44.2	20.4
0.0015	46.7	20.8
0.002	36.3	33.5

This comparison suggests that the "best" regression equation, which includes all strain levels, predicts the observed creep behavior at least as well as the family of Larson-Miller curves which would be required to cover a similar range of strain levels.

Multiple regression techniques can also be applied to fit "faired" data to estimate mean values for creep strain. This is illustrated in Figure 6. First, linear regressions of log time on log stress (Eq. (1)) were run on the original data set (8) for each level of strain and temperature. The results of several of these regressions are shown as solid lines in the figure. Next, the mean times to a given level of strain were calculated from the regression equations of the solid lines. Finally, these calculated mean times and the appropriate values of creep strain, stress, and temperature were used as input data for a multiple regression analysis (Eq. (3)). The dashed lines in Figure 6 were calculated from the results of a run 4121, k = 27, using these calculated mean times as input data. The k = 27 version of Equation (3) was not unstable with the "faired" data set, whereas, as noted before, this version was unstable with the "raw" data.

Often creep data are presented in the literature as families of faired curves for specific levels of strain and temperature. No individual creep curves are available for the material of interest.

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As can be seen from this example, multiple regression techniques can be used to obtain a single equation which will coalesce families of curves. However, a prediction interval is no longer applicable because the calculations are no longer based on scattered data.

### 6 CONCLUDING REMARKS

Frequently, creep data are limited during the preliminary design phases of a program such as the design of Space Shuttle thermal protection systems. The examples presented herein illustrate the applicability of regression techniques for (1) evaluating the effects of "nonstandard" creep conditions such as sheet thickness or low oxygen partial pressure on creep behavior and (2) developing analytical expressions to predict creep behavior from limited data. The use of prediction intervals to evaluate the design consequences of the data scatter has been discussed.

### 7 ACKNOWLEDGMENTS

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#### APPENDIX 1

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Fig. 2. Effect of sheet thickness and test pressure on creep strength of H-188 at 1144 K, e = 0.022



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Fig. 3. Effect of 'zero' data points on a typical calculated creep curve for René 41



Symbols: experimental (8)

------ : linear regression at each temperature, mean and 95 per cent prediction interval

---: run 4124, k = 23, mean and 95 per cent prediction interval

Fig. 4. Comparison of experimental and calculated creep strength for Rene 41, *e* = 0.002



Fig. 5. Typical calculated creep curves for Rene 41, run 4124, k = 23

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Fig. 6. Comparison of experimental and calculated mean creep strengths for René 41

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STRESS-RUPTURE DATA CORRELATION -GENERALIZED REGRESSION ANALYSIS AN ALTERNATIVE TO PARAMETRIC METHODS<sup>1</sup>

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# STRESS-RUPTURE DATA CORRELATION -GENERALIZED RECESSION ANALYSIS AN ALTERNATIVE TO PARAMETRIC METHODS

By ' Donald R. Rummler

ABSTRACT: The applicability of multiple regression analysis techniques to stress-rupture data correlation has been investigated. A generalized interacting variable (GIVAR) method of data correlation is proposed and evaluated. The GIVAR method is compared to six parameter methods of data correlation on three sets of simulated data and twenty sets of real data. In all cases, the GIVAR method provided the best data correlation. Application of prediction intervals and correlating variables in addition to temperature and stress is also discussed.

# INTRODUCTION

Since 1952 when the first paper [1] introducing the concept of a time-temperature parameter (TTP) was published, the need to correlate and extrapolate stress-rupture data has continued unabated. The importance of stress-rupture data analysis has led to a large number of papers which either propose new parametric approaches [2-5], offer detailed comparisons of analysis techniques [5-7], and/or provide state-of-the-art surveys [8-12]. Although the development of some parametric methods can be related to creep behavior and fundamental processes, most parametric methods have been empirically derived. Most also make the assumption that there is a simple functional relationship between temperature and time-to-rupture which will yield a constant value of the parameter at a given level of applied stress. Consequently, the selection of a particular parameter to use for data analysis imposes rigid requirements on the nature of the allowable interactions between time-to-rupture, applied stress, and temperature. Methods for the selections of a particular parameter for the analysis of data sets are given in the previously cited survey papers. The application of these methods to real data sets is often difficult. Often the analyst is required to use data sets which are inadequate in terms of stress or temperature range to allow a clear selection of the parametric method best suited for data correlation. Data scatter further compounds the difficulty of selecting an analysis technique and often forces the analyst to "smooth" or approximate

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his data in order to conform reasonably to the functional requirements of a particular parametric representation.

An attempt to overcome some of the difficulties has led to the concept of minimum commitment [7, 10, 13]. This method (MCM) proposes the use of a general time-temperature functional relationship. The MCM method has recently been evaluated during an investigation concerned primarily with its extrapolative characteristics [7]. Although the MCM showed promise during the evaluation, its clear superiority over other forms of parametric analysis was not demonstrated. In addition, in its present form, the MCM does not provide the analyst with an explicit form of parametric representation directly nor is it completely general in the allowed functional interactions between the primary variables of time-to-rupture, stress, and temperature.

The empirical nature of the data analysis techniques currently available is the direct result of the lack of understanding of the stress-rupture process particularly in complex engineering alloys. Until better theoretical models of creep-rupture behavior are developed, the engineer or analyst is faced with the task of establishing a functional relationship which will describe and correlate the data at hand. Regression analysis has been found to be a useful tool for the analysis of multifactor data particularly when the physical factors which control the response to be predicted are understood only in general terms. Such is currently the case in the analysis of stressrupture data.
The purpose of this paper is to present the results of an investigation to determine the applicability of multiple regression analysis techniques to stress-rupture data correlation. The particular regression techniques developed are first compared to several parametric methods using both simulated and real stress-rupture data sets. The potential of the developed regression techniques is further explored by subjecting a large number of real data sets to a preliminary analysis designed to select the functional form of an equation to be used for detailed analysis. These results are also compared to several parametric methods.

#### DATA FOR ANALYSIS

Both simulated and real data sets were used to assess the capabilities of multiple regression analysis techniques for stress-rupture data correlation.

#### Simulated Data

Simulated data sets were derived from data for Timken 35-15 stainless steel taken from reference [8]. These data were fitted by the method of least squares to transformations of the following parametric expressions:

Larson-Miller

 $T(C + \log t_r) = b_0 + b_1 \log \sigma$ Örr-Sherby-Dorn

 $\log t_r - \Delta H/2.3RT = b_0 + b_1 \log \sigma$ . Rabotnov

$$\sigma(1 + A t_r^b) = b_0 + b_1/T + b_2/T^2$$

where R = universal gas constant t<sub>r</sub> = time to rupture T = temperature σ = stress C. AH. A. b. b. b. b. = con

C,  $\Delta H$ , A, b, b<sub>0</sub>, b<sub>1</sub>, b<sub>2</sub> = constants determined by least squares

The Larson-Miller [1] and the Orr-Sherby-Dorn [2] expressions are familiar time-temperature parameters which assume that the parameter (left side of equation) is constant for a given stress. The parameter can be considered a temperature compensated time. The Rabotnov [12, 14] expression is a time-stress parameter which assumes that the value of the parameter (left side of equation) is a constant for a given temperature. The parameter represents a time compensated stress. Although the Rabotnov expression was originally developed for correlation of creep data, its use for creep-rupture correlation has been suggested [12] as an alternative to TTP methods.

The values of the constants determined by the regression analysis for each parametric expression were used with the experimental stress and temperature levels to calculate "exact" times for each simulated data set. The simulated data sets are referred to as L-M Exact, O-S-D Exact, and RAB Exact. Additional details of the fitting procedures and tabulation of the real and simulated data are presented in Appendix A.

#### Real Data

All real data were taken from a recent evaluation of para-

metric methods for extrapolation [7]. Careful attention was paid to the adequacy of the data in terms of range of stress and temperature exposure and long times to rupture. The data included a wide range of materials. The material types and number of observations in each data set are shown in Table 1. The data set numbering in reference [7] has been retained in this investigation. Tables 2 and 3 present the data for the two data sets (4 and 16) which are analyzed in detail. Reference [7] lists the data for the other data sets analyzed.

#### ANALYSIS PROCEDURES

The three types of analysis techniques used during this investigation (1) parametric, (2) minimum commitment (MCM), and (3) Generalized Iteracting Variables (GIVAR) are discussed in this section

#### Parametric Methods

A number of different parametric techniques have been suggested for correlating stress-rupture data. The equation forms used for multiple regression analysis of the parametric techniques selected for this investigation were as follows:

Larson-Miller (L-M)

$$Y = \log t_{r} = b_{0} + b_{1}/T_{R} + b_{2}S/T_{R} + b_{3}S^{2}/T_{R} + b_{4}S^{3}/T_{R} + b_{5}S^{4}/T_{R} + b_{6}S^{5}/T_{R}$$

$$\frac{Drr-Sherby-Dorn (0-S-D)}{Y = \log t_{r} = b_{0} + b_{1}/T_{K} + b_{2}S + b_{3}S^{2} + b_{4}S^{3} + b_{5}S^{4} + b_{6}S^{5}$$

$$\frac{Manson-Succop (M-S)}{Y = \log t_{r} = b_{0} + b_{1}T_{F} + b_{2}S + b_{3}S^{2} + b_{4}S^{3} + b_{5}S^{4} + b_{6}S^{5}$$

$$\frac{\text{Manson-Haferd (M-H)}}{\text{Y} = \log t_r = b_0 + b_1 T_0 + b_2 T_0 S + b_3 T_0 S^2 + b_4 T_0 S^3 + b_5 T_0 S^3 + b_6 T_0 S^4 + b_6 T_0 S^5}$$

$$\frac{\text{Rabotnov (RAB)}}{\text{Y} = t_r^a = b_0 + b_1 / \sigma T_F + b_2 / \sigma T_F^2 + b_3 / \sigma T_F^3 + b_4 / \sigma T_F^4 + b_5 / \sigma T^5}$$
where
$$t_r = \text{time to rupture, hours}$$

 $t_r = time to rupture, nours$   $S = \log \sigma$   $\sigma = applied stress, ksi$   $T_F = temperature, {}^{O}F$   $T_K = temperature, Kelvin$   $T_R = temperature, Rankin$  $T_O = offset temperature = T_F - T_A$ 

 $b_i$ ,  $T_A$ , a = constants estimated by method of least squares. Both the M-H and RAB techniques required the use of iterative, non-linear multiple regression techniques to estimate all of the constants.

In all cases, some function of time to rupture was considered the dependent variable whose variance was minimized. High order polynomials which are functions of stress have often been used to correlate stress-rupture data [7, 8]. Although a sufficiently high order polynomial can approximate any function, it can also result in unrealistic waviness in plots of the dependent variable versus any one of the independent variables. For these reasons, the parametric model equation forms were also analyzed in functional forms which included only second or third order

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polynomials in the stress function.

In addition to estimating the required constants and predicted values of log time to rupture, the parametric analysis procedures produced the following summary values to aid data correlation and parameter comparison:

$$\overline{RMS} = \left(\frac{\Sigma(OTR - PTR)^2}{N}\right)^{1/2}$$

$$\overline{STD} = \left(\frac{\Sigma(OTR - PTR)^2}{N - K - 1}\right)^{1/2}$$

$$\overline{DPAVG} = \frac{\Sigma(PIMAX - PIMIN)}{N}$$

DPMAX = maximum value of PIMAX - PIMIN where

OTR = observed log time to rupture PTR = predicted log time to rupture N = number of observations in data set K = number of constants in regression model PIMAX, PIMIN = upper and lower bounds of 95% prediction

interval for each observation in a data set

The root mean square (RMS) provides an overall comparison of data correlation including both random error and functional bias. It does not, however, reflect the increases in the regression standard deviation which can occur when high order polynomial terms are included in the model equation. The added high order terms may be highly correlated with the other independent variables already in the equation and consequently may not reduce the residual sum of squares enough to account for the loss in degrees of freedom [15]. For all regressions which used log time to rupture as the dependent variable the calculated value of STD

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is equivalent to the standard deviation of the regression.

The average width (DPAVG) and the maximum width (DPMAX) of the 95% prediction interval are considered useful indicators of the expected scatter for a future observation taken from the same material under the same testing conditions. The prediction interval [16, 17] is used to make a statement about the expected value of the dependent variable (log time to rupture) for a single future observation at specific values of the independent variables (functions of stress and temperature). The prediction interval is wider than the more familiar confidence interval on the mean, since it includes both sampling errors and the uncertainties in estimating the mean value of the dependent variable.

#### Minimum Commitment Method

The minimum commitment method (MCM) of parametric analysis [7, 10] was developed to minimize the dependence of the data analyst on the particular model equation forms of the generally used parameter methods. The MCM concept is to utilize a parameter model equation general enough to encompass most of the popular parameter methods. The parametric equation chosen has the form:

 $\log t (1 + AP) + P = G$ 

where

t = time to rupture

A = constant

P = function of temperature

G = function of stress

The functions P and G are "station functions" which are defined by their values at selected levels of temperature and stress. Since it is not necessary for P and G to be explicitly expressed, there is no commitment on the part of the analyst to a particular parametric form. MEGA (Manson-Ensign Generalized Analysis) is the computer program developed to implement the MCM [13]. The particular version of MEGA used during this investigation utilized three stations of temperature to define P and three stations of stress to define G. In addition, the first and second derivatives of the G function at the mid station were included in the analysis. The analysis, therefore, involved the calculation of eight constants [7].

The parametric equation form which has been selected for the MCM does not readily lend itself to a least squares method of solution with log of time to rupture as the dependent variable. Consequently, the MEGA computer program in its current form does not yield least squares statistics such as the standard deviation of the solution (regression). The lack of appropriate statistics necessitated the use of RMS as the evaluator when comparing the MCM method to other methods of stress-rupture data correlation. Generalized Interacting Variables Method

Development - The basic concept for the generalized <u>interacting variables (GIVAR) method of data correlation was</u> developed for the analysis and correlation of creep data [18]. Simply stated, it is assumed that the functional relationship between the dependent variable and independent variables can be

described by a low order polynomial in each independent variable. For stress-rupture data correlation, this concept leads to a model response equation of the general form:

 $f(y) = g[(a_1 + b_1X_1 + c_1X_1^2)(a_2 + b_2X_2 + c_2X_2^2 + d_2X_2^3)]$ where y, X<sub>1</sub>, and X<sub>2</sub> are respectively functions of time to rupture, temperature, and stress. Because complex interactions between time, temperature, and stress are known to occur during the creep-rupture process, the model equation is completely general and allows all interaction terms which result from the combination of the low order polynomials specified for each independent variable. Additional independent variables can be readily introduced into the general model form by the inclusion of additional low order polynomials,

f(y) = g[(A) (B) (C) (D)]where A, B, C, D are low order polynomials of the independent correlating variables.

The computer program to implement the GIVAR method includes provision for transformation of y and  $X_i$ . For this investigation, the majority of data correlations were performed with the following transformations

Variable	Allowed Transformations
У	log t
xl	T, 1/T, log T
х <sub>2</sub>	$\sigma$ , $\sigma^{1/3}$ , log $\sigma$
where t,	T, $\sigma$ are respectively time to rupture, temperature, and

stress. After transformation of the primary variables, the model

equation form is expanded and new independent variables, defined as follows, are introduced to yield a response equation for a multiple regression analysis:

 $y = a_1a_2a_3 + b_1X_1 + b_2X_2 + b_1b_2X_1X_2 - - - = \sum_{j=1}^{k} \phi_jZ_j$ The resulting model equation form for the multiple regression analysis is linear in the coefficients  $(\phi_j)$  and is simply an extension of equation forms which have been used to determine optimum conditions in multifactor environments [19], for example, to determine the conditions necessary to maximize the output of a chemical process.

Application - To perform a GIVAR correlation of stress rupture data, the orders of the independent variable polynomials were selected and the general equation form expanded. A second order polynomial in temperature and a fifth order polynomial in stress were used for the majority of data correlations. When a  $\sigma^{1/3}$  transformation was selected, a sixth order polynomial in stress was used. Temperature and stress interaction terms above third order  $(X_1^2X_2)$  were deleted from the polynomial expansions. Next, the transformations of each prime variable which would be allowed were selected. The computer program, using these control inputs plus the original data set, then analyzed all combinations of the variable transforms and printed out summary results for each analysis. The variable transforms which produced the lowest standard deviation of the regression were then resubmitted and the number of terms in the regression model was reduced using a technique known as a tki-directed search [15].

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When there are M potential variables in a regression model, there are  $2^{M}$  possible regression equations. The  $t_{k,i}$  directed search technique has been proposed as an alternative to stepwise regression techniques [16] to reduce the number of variables in a regression model. The  $t_{k,i}$  directed search uses the ratio of each  $b_{i}$  to its standard error as follows:

$$t_{k,i} = \frac{b_i}{S(b_i)}$$

where  $b_i$  and  $S(b_i)$  are the values of the coefficient and the standard error for ith variable. Following a regression on the full model equation, the variables in the full regression model are arranged in decreasing order of their  $t_{k,i}$  values. Successive regressions reduce the number of variables until a "basic set" is found. The program then analyzes all model equations which can be constructed including all of the basic set of variables plus all possible combinations of the previously dropped variables. The "best" equation is selected on the basis of the lowest standard deviation of the regression.

Finally, the "best" reduced variable regression equation was analyzed in detail to verify its adequacy. If the model was to be used for significance tests or if a statistical interval such as the prediction interval were to be used, verification included careful examination of residual plots [15, 16, 20] to assess departures from the assumptions of the linear regression model. RESULTS AND DISCUSSION

### Simulated Data

The purpose of the simulated data sets was to assess the functional capability of the GIVAR method and its associated computer program without the confusing influence of the large scatter normally associated with stress-rupture data.

The results of the simulated data set analyses are summarized in Table 4 which shows the calculated values of STD for each of the six methods of data correlation for the three simulated data sets. For each data set, the generalized interacting variables method (GIVAR) produced the lowest value of STD. Of equal importance to the significantly better correlation was the fact that the GIVAR computer program selected the most correct of the prime variable transformations for the L-M and O-S-D Exact data The tki search quickly reduced the original nine term sets. model equations to the correct three term equations. The value of STD calculated for these two cases is due primarily to rounding off the calculated exact times for these data sets. For the RAB Exact data, log t, log T, and log  $\sigma$  were selected as the best prime variable transformations. In this case, the original eleven term model equation was reduced to nine terms during the t<sub>k.i</sub> search.

Table 4 also illustrates the general futility of adding higher order polynomial terms to improve correlation for the restricted models. For the four commonly used parameters, no significant improvement can be seen when expanding the model equation from four terms to seven terms (from a second order to a fifth order equation in stress). A similar lack of correlation improvement

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has been reported on real data [5].

The correlations produced by the M-H and GIVAR methods for the RAB Exact data are shown in Fig. 1. The GIVAR method correlation is noticeably better than the M-H correlation. It is important to remember that in both analyses, log time to rupture was the dependent variable and consequently, minimization of differences between observed and calculated times to rupture was the regression criteria. For these data, neither of the two methods shown had model equation forms which would exactly duplicate the governing equation for the RAB Exact data generation. This is a comparable situation to most real data where correlation models seldom represent a material's behavior exactly. Since for most real data either correlation would probably be considered . satisfactory, the calculation of a statistical interval such as the prediction interval to assess uncertainty about a future observation would be a natural extension of these correlations.

The residuals of the M-H and GIVAR correlations for the RAB Exact data are presented in Fig. 2. The M-H residuals clearly exhibit curvature as a function of the predicted log time to rupture. The residuals are not randomly distributed with respect to the dependent variable (predicted log time to rupture). This type of behavior indicates that the regression model is inadequate and needs additional terms. What has happened is that the M-H model equation, even with a fifth order polynomial in stress, was functionally incapable of correctly approximating the Rabotnov expression which was used to generate these data. The

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random distribution of the GIVAR correlation which includes interaction terms does not suggest any functional inadequacy. An examination of the cumulative normal distribution of the residuals for the GIVAR correlation failed to indicate that the residuals were not normally distributed. Since the GIVAR correlation equation of these data does not appear to violate any of the basic regression assumptions, the calculation and use of a statistical interval would be in order [16].

#### Real Data

The results of the GIVAR correlation on alloy 4 (a plain carbon steel) are presented in Fig. 3. As for all GIVAR correlations, log time to rupture was the dependent variable. The prime variable transformations selected by the computer program are shown. The original eleven term model equation was reduced to seven terms during the  $t_{k,i}$  search. The GIVAR mean fit seems to satisfactorily correlate this complex behavior. The STD value of the GIVAR correlation for these data was 40 percent lower (0.103 versus 0.146) than a third order M-H model which was the best of the parameter models.

To minimize the computer time, the 95% prediction interval about each observation is normally calculated during the computer run which performs the regression on the model equation. The upper and lower bounds of the 95% prediction are listed along with the calculated time to rupture. For these data, the calculated prediction interval called attention to a possible outlier, i.e., an atypical observation. This data point is shown

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with the filled symbol. Examination of the residual plot with respect to predicted log time to failure (Fig. 4) suggested that the residuals were randomly distributed, had a mean of zero, and exhibited constant variance with the single exception of the residual for the possible outlier. The cumulative normal distribution plot of these residuals (Fig. 5) also appeared normal with the exception of the single suspect data point. Although there are many schemes for outlier rejection [21, 22], the present purpose is to demonstrate that the prediction interval provided a useful tool for focusing attention on a possible outlier which may have otherwise been overlooked. For other data sets, the calculated prediction interval has called attention to data transcription errors which had gone undetected because of large data scatter. It should be pointed out that the use of the prediction interval to provide a focus for possible outliers is not strictly correct in the statistical sense. Its proper use is to make estimates of the bounds which can be expected from a single future observation from the same population. Dismissing the outlier for the moment, we can say that 95% of the time a future single observation will fall within the bounds shown in Fig. 3. The implications of this kind of statement for acceptance testing, quality control, or determining the significance of a new test variable are obvious.

Temperature and stress are usually considered the prime variables for stress rupture correlation. Some authors [5], however, have been able to improve correlation by the use of an

additional variable such as elastic modulus to normalize stress. Table 5 summarizes the results of correlation analyses on alloy 16 (a nickel base alloy) to evaluate the effect of additional variables. The listing includes the analysis method, the prime variable transformations, and the calculated values for STD, DPAVG and DPMAX. The units of DPAVG and DPMAX are log (time to rupture, hours). For these data, the M-S and M-H methods were the best (lowest STD) of the parameter methods. However, the use of elastic modulus (E) to normalize stress did not significantly improve the fit in either case. Using just temperature and stress, the GIVAR method resulted in a significantly lower value of STD than the best parameter method. When second order polynomial expressions for elastic modulus and ultimate tensile strength at the test temperature were incorporated into a generalized interacting model equation, a significant further correlation improvement was achieved. The significance of the better correlation provided by the GIVAR method is more easily appreciated when it is realized, that within the average prediction interval bounds, the predicted time to rupture varies by a factor of 3 for the best parameter method and by a factor of 1.6 for the GIVAR method. For the maximum width of the prediction intervals, these values are 4.5 and 1.8, respectively. It should be pointed out that the GIVAR model equation did not allow interactions to occur between elastic modulus or ultimate tensile strength and temperature, since they are both highly correlated with temperature. In this case, the original 21 term

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model equation was reduced to 13 terms during the tk,i search.

The best M-H and GIVAR correlations of the alloy 16 data are presented graphically in Fig. 6. The GIVAR fit is noticeably superior. Even with a fifth order polynomial in log stress, the M-H model equation appears to be functionally inadequate to correlate the complex behavior of alloy 16. This functional inadequacy is further demonstrated in Fig. 7 which presents the residuals as a function of the predicted log time to failure. The M-H residuals are not randomly distributed and definitely display a curvilinear tendency suggesting the need for interaction terms. The GIVAR residuals appear to be randomly distributed and do not suggest any inadequacies in the model equation form. The cumulative normal distribution of the residuals for the GIVAR solution (not shown) did not reveal any gross departures from normalcy. Since none of the basic assumptions of the linear regression appear to have been violated, the making of significance statements or the calculation of statistical intervals for this solution would be in order.

In order to further assess the generality of the GIVAR method, all of the data sets of reference [7] were correlated with the five parameter methods, the MCM method and the GIVAR method. The independent variables for these analyses were limited to functions of temperature and stress. For the parameter methods, second, third, and fifth order model equation forms were examined. The lowest RMS values for the five parameter methods,

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MCM and GIVAR methods are tabulated in Table 6 and presented graphically in Fig. 8. RMS was selected as the basis of comparison in order to include the MCM analyses. Additional details and other summary values for these analyses are presented in Appendix B.

In Fig. 8, a range band is shown for the five parameter methods. The MCM and GIVAR method are shown with symbols. For each of the twenty data sets analyzed, the GIVAR method produced the lowest value of RMS. The GIVAR method on the average porduced a 19% lower RMS value than the MCM which was on the average the best of the other methods examined. Examination of Table 6 reveals that the GIVAR solution in several cases required less terms in the model equation than the best parameter model equation. The MEGA computer program used to implement the MCM required the determination of eight constants. Table 6 also shows that the Rabotnov method was in all cases the worst of the parametric methods. It should be pointed out, however, that a polynomial in 1/T was the only function of temperature investigated and that other functions of temperature might provide better correlations. With the exception of the GIVAR method, none of the other methods consistently produced the lowest RMS value for all twenty alloys. The failure of any single method to be consistently superior was also observed in reference [7] where the primary emphasis was on the extrapolative characteristics of the various parametric methods with these sets of data.

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#### CONCLUSIONS

An investigation has been made to assess the applicability of a generalized interacting variable (GIVAR) multiple regression analysis method for the correlation of stress-rupture data. The GIVAR method was compared to six other methods of stress-rupture data correlation on twenty sets of data. The following conclusions are made from the analyses presented herein.

1. For all data sets examined, the GIVAR method produced the best correlation (lowest RMS value).

2. It was shown that the GIVAR method has the functional generality to satisfy criteria necessary for the calculation of statistical intervals.

3. The GIVAR method readily accepts the inclusion of correlating variables in addition to stress and temperature.

4. The prediction interval was shown to be useful for the detection of possible data outliers.

#### APPENDIX A

Parametric Analysis to Establish Simulated Data Sets

The purpose of simulated data sets was to evaluate the functional capabilities of the various correlation methods without the confounding influences of the large scatter normally associated with real data. Creep rupture data are seldom the result of a statistically designed experiment. The data are seldom balanced in variable space. In addition, temperature and stress are often highly correlated. Because of testing economics, low stresses are usually associated with high temperatures and high stresses are usually associated with low test temperatures. In order to include this type of inbalance in the simulated data sets, the data for Timken 35-15 stainless steel [8] were fitted to a first order Larson-Miller and Orr-Sherby-Dorn expressions and to a second order Rabotnov expression by the method of least squares. The equation forms and the fitted coefficients were as follows:

Larson-Miller

 $(Tx10^{-4}) (C + \log t_r) = b_0 + b_1 \log \sigma$ where T = test temperature, <sup>O</sup>R C = iteratively determined constant = 13  $t_r$  = time to rupture, hours  $b_0 = 6.39038$  $b_1 = -0.90584$  $\sigma$  = stress, psi

Orr-Sherby-Dorn  
log 
$$t_r - \frac{\Delta H_R}{2.3RT} = b_0 + b_1 \log \sigma$$
  
where  
 $t_r$  = time to rupture, hours  
 $\Delta H_R$  = apparent activation energy, iteratively calculated =  
58000  
R = universal gas constant = 1.986  
T = temperature, K  
 $b_0$  = 4.46410  
 $b_1$  = -4.60029  
 $\sigma$  = stress, psi  
Rabotnov  
 $t^a = b_0 + b_1/\sigma T + b_2/\sigma T^2$   
where  
t = time to rupture, hours  
a = constant iteratively determined = 0.3637  
 $b_0$  = -1.62434  
 $b_1$  = -2.44083 x 10<sup>5</sup>  
 $\sigma$  = stress, ksi  
T = temperature, <sup>O</sup>F  
 $b_2$  = 4.88958 x 10<sup>8</sup>

The rupture times which were calculated for each of the three solution methods were substituted for the experimental times to rupture to form the "exact" simulated data sets. These calculated times and the original data for the Timken 35-15 stainless steel are presented in Table 7.

#### APPENDIX B

Supplementary Analysis of Correlation Methods

The purpose of this appendix is to supplement the correlation method comparison presented in the main body of the paper on the twenty real sets of data.

The results of the parametric correlations are summarized for the L-M, O-S-D, M-S, M-H and RAB in tables 8 through 12, respectively. The tables present values of RMS, STD, DPAVG and DPMAX which were calculated for each level of polynomial model equation which was evaluated. For the L-M, O-S-D, M-S, and M-H methods, second, third, and fifth order expressions in stress required 4, 5, and 7 terms, respectively. The RAB method required 3, 4, or 6 terms to develop second, third, and fifth order expressions. Table 13 presents a summary of the GIVAR method for these twenty data sets.

Parametric methods

In all cases for the L-M, O-S-D, M-S, and M-H methods, a fifth order expression produced the lowest value of RMS for a given alloy. In some cases, however, the high correlation of the power terms in stress resulted in ill-conditioned solutions which were not reliable (see Table 8, alloy 14, for example). Such was not the case for the RAB solutions (Table 12) where third order expansions (4 terms) of temperature fit better than fifth order in a number of cases (alloys 4, 6, 8, 11A, 11B, 17A).

The calculated values of STD, which for the L-M, O-S-D, M-S, and M-H methods were equivalent to the standard deviation of the

regression, did not follow the trend of better correlation with increasing degree of stress polynomial. The increased STD values reflect the fact that added variables did not reduce the residual sum of squares enough to account for the loss in degrees of freedom. These cases included the following:

Alloy	Method(s)
1	Ľ.⊷M
4	L-M, O-S-D, M-S, M-H
б	L-M, O-S-D, M-S, M-H
8	L-M, M-S, M-H
11A	L-M, O-S-D, M-S, M-H
11B	L-M, O-S-D, M-S
12	L-M, O-S-D, M-S, M-H

This behavior, larger values of STD with a higher order polynomial, was also exhibited for several of the alloys during the RAB method correlations (Table 12). The poorer correlation provided by the higher order polynomials can be better appreciated when we recall that the units of DPAVG and DPMAX are log time. Taking the best parametric method correlation in terms of RMS for alloy 4 (Table 11), we see that the average predicted time within the 95% prediction interval varies by a factor of 4.9 for a seven term equation and by 4.5 for a five term equation. The comparable values for the maximum width of the prediction interval are 6.4 and 5.4. In this case the use of a fifth order expression has significantly degraded the correlation. In addition to providing more sensitivity to

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changes in the "goodness" of correlation, the values of DPAVG and DPMAX as preliminary evaluators of correlation have the feature of allowing all methods to be compared on an equal basis. Values of DPAVG and DPMAX can be backtransformed and averaged if necessary to accommodate different transforms of the dependent variable. They can thus provide the analyst with a "feeling" for the scatter and uncertainty in the data and its correlation.

It is beyond the scope of this paper to summarize the results of all of the analyses which were performed by the GIVAR method on the real data. Table 13 summarizes the "best" model equation results for each alloy. In most cases, the "best" equation was selected after the examination of summary computer results for nine different model equation forms. Log T and  $\sigma^{1/3}$ transformations of temperature and stress were selected for several of the alloys (Table 13). These transformations are not suggested by any of the standard parametric methods. As expected, not only did the GIVAR method produce the lowest value of RMS for each of the alloys, but it also produced the lowest value of the other preliminary correlation evaluators STD, DPAVG, and DPMAX (Tables 8 through 13).

It is rare that stress-rupture data have the replicated observations that are necessary to provide an internal estimate of data scatter. The data for alloy 13 [7] was such an exception. There were seventeen experimental conditions which were replicated. These replicated observations had an average standard deviation of 0.232 with a spread of from 0.024 to 0.476,

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in terms of log time. The best GIVAR correlation of these data (Table 13) had a standard deviation of 0.280 indicating that the fit was comparable to the data scatter. This value is somewhat lower than the best (M-H) parameter method STD of 0.293 (Table 11).

#### Summary

1. Higher order polynomial model equations do not always provide the best correlations of stress-rupture data.

2. The standard deviation of the regression (STD) is a better correlation evaluator than RMS.

3. The average and maximum width of the 95% prediction interval (DPAVG and DPMAX) are sensitive preliminary evaluators for stress-rupture data correlations.

TABLE 1---Real data sets examined.

ALLOY	MATERIAL	NUMBER OF
	:	OBSERVATIONS
	,	
1	1100-0 ALUMINUM	64
2	5454-0 ALUMINUM	, <b>7</b> 5
<b>4</b>	PLAIN CARBON STEEL	. 26
5	lCr-1Mo STEEL	33
6	lCr-lMo- 0.25 V STEEL	26
7	304 STAINLESS STEEL	. 52
8	304 STAINLESS STEEL	39
9	316 STAINLESS STEEL	. 38
11A, 11B	347 STAINLESS STEEL	42,44
12	A286 IRON-NICKEL	24.
13	INCO 625 IRON-NICKEL	99
<u>1</u> 4	INCO 718 NICKEL-BASE	26
15	RENÉ 41 NICKEL-BASE	37
16	ASTROLOY R NICKEL-BASE	. 33
17A, 17B	UDIMET 500 NICKEL-BASE	103,105
18A, 18B	L-605 COBALT-BASE	100,104
19	6061-T651 ALUMINUM	99

TOTAL = 20 DATA SETS •

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Temperature <sup>O</sup> F	Stress <u>ksi</u>	Time to Rupture <u>Hours</u>
752	40.3	752
752	38.1	1696
752	35.8	3973
752	33.6	6134 ·
752	31.4	10422
752	29.1	20227
842	33.6	65
842	31.4	441
842	26.9	1341
842	24.6	3023
842	22.4	3934
842	17.9	12985
842	15.7	18648
842	13.4	34753-
932	22.4	63
932	20.2	247
932	17.9	430
932	15.7	1317
932	13.5	2958
932	11.2	3202
932	9.0	7558
932	6.7	22707
1022	13.5	43
1022	11.2	142
1 <u>022</u>	9.0	<sup>4</sup> 96
1022	6.9	1935

# TABLE 2--Stress-rupture data for alloy 4.

Temperature	Stress	Time to Rupture	Tensile Strength <sup>(a)<sup>.</sup></sup>	Elastic Modulus <sup>(b)</sup>
° <sub>F</sub>	ksi	. • Hours	ksi	10 <sup>-6</sup> psi
-				
*	*	•	۰,	
1400	101.0	12.8	150	25.80
1400	86.0	59.0	150	25.80
1400	80.0	176.6	150	25.80
1400	74.0.	400.7	150	25.80
1400	. 70.0.	- 577.0	150	25.80
1400	61.0	2279.8	150	25.80
- 1400	55.0	4,063.2	150	25.80
1500	75.0	30.5	130	25.05
1500	64.0	142.2	130	25.05
1500	,50.0	351.3	130	25.05
1500	-52.0 Mrr 0	712.0	130	25.05
1500	45.0		130	25.05
1500	39.0	222(•4 11202 h	120	25.05
1500	31.U	• 4393•4	130	25.05
1600	04.U 56 5	10.5	110	24.50
1000	50.5 h6 F	20.0 1/15 8	011	24.00
1600	40.5 Jun 0	252 0	13.0	24.50
1600	41.U	200+0 525 7	110	24.00 DH ED
1600	21 0	888 0	110	24.50
1600	うエ•O う上 - F	2800 7	110	24.50
1600		. 6331 0	11.0	24.50
1700	41.0	11.5	80	23,30
1700	33.5	44. 2	-80	23,30
1700	29.0	120.9	· 80	23.30
1700	24.0	342.7	80	23.30
1700	21.0	746.7	80	23,30
1700	17.5	1768.7	80	23,30
1700	14.5	2838.7	80	23.30
1800	29.5	6.1	40	22,15
1800	20.5	49.3	40	22.15
1800	17.0	174.0	40	. 22.15
1800	14.5	340.7	40	22.15

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TABLE 3--Stress rupture data for alloy 16.

(a) Estimated from reference [23](b) From reference [5]

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Dat Set	5 <b>8</b> .	No. of equation terms	4	ь—м 5	7	4	0-5-D	7	Para 4	meter M-S 5	Method 7	s 4	м-н 5	7	3	RAB 4	5	Gene: GIVAR	valized Interacti No. of varia- bles in "best" equation	ng Variables Prime variable transformations
0-6 Exe	S-D		.045	.045	.045				-092	.095	.096	.027	.023	.024	.317	.046	.003	.00003	3	log t, 1/T, log s
L-l	Mact					.046	•047	.047	.052	.054	.055	.027	.024	.025	.202	.052	.051	.00002	3	log t, 1/T, log σ
RA: Ex	B act		<b>.11</b> 7	.118	.119	.145	.149	.150	.083	.084	.085	.044	.042	.044				.010	<b>9</b> ,	log t, log Τ, log σ

TABLE 4--Comparison of STD values for simulated data.

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	TABLE	5Effect	of	additional	variables	on	correlation
•		-			$\sim$		

alloy 16 - Astroloy®

ANALYSIS METHOD	PRIME VARIABLES	STD	PREDICTION AVERAGE	INTERVAL MAXIMUM
ĮM	l/T <sub>R</sub> , log σ	.142	.631	•756
0-S-D	l/T <sub>K</sub> , log σ	.148	.661	.824
M-S	Τ <sub>F</sub> , log σ	,118	.527	,657
M-S	Τ <sub>F</sub> , log σ/E	.114	.506	.648
M-H	T <sub>F</sub> , T <sub>A</sub> log σ	.116	•517	.660
M-H	T <sub>F</sub> , T <sub>A</sub> , log σ/E	.110	.489	.652
RAB	l/T <sub>F</sub> , σ	•373	1.159	4.140
GIVAR	.l/T <sub>F</sub> , σ	.061	.279	•353
GIVAR	$\log T_F, \frac{1}{\sigma_{TU}}, \sigma^{1/3}, 1/E$	.044	.213	.256
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	Number of Data	т	M	0-5	<b>_</b> D	м_	q	M	ч	PA	в	мс	м	CTU	<b>A D</b>
Alloy	Points	Terms	RMS	Terms	RMS	Terms	RMS	Terms	RMS	Terms	RMS	A	RMS	Terms	RMS
ı	64	7	.159	7	.139	7	.220	7	.153	6	.209	0	.127	9	.106
2	75	7	.082	7	.086	7	.160	7	.074	6	.245	0	.077	11	,055
4	26	7	.161	7	.149	7	.161	7	,128	4	.247	15	.109	· 7	.088
5	33	7	.063	7	.050	7	.089	7	.054	3	.304	0	.054	9	.043
6	26	7	.097	7	.057	7	.124	7	.045	4	.298	05	.043	6	.042
7A	52	7	.140	7	.131	7	.179	7	,121	6	.256	0	.131	10	.091
8	39	7	.178	7	.131	7	.233	7	.137	4	.291	05	.115	10	074
9	38	7	.111	7	.094	7	.141	7	.111	6	.148	.15	.078	8	.068
11A	42	7	.134	7	.142	7	.122	7	.113	4	.179	10	.109	7	.100
11B	44	7	.132	7	.139	7	.122	7	.111	. 4	.218	05	.111	9	.099
12	24	7	.183	7	.191	7	.178	7	.178	• 6	.385	10	.175	6	.166
13	95	7	.288	7	.291	7	.291	7 .	.282	6	.363	05	.290	8	.268
14	26	5 <sup>a</sup>	.064	5 <sup>a</sup>	.074	5 <sup>a</sup>	.073	5 <sup>a</sup>	.059	6	.293	0	.056	10	.037
15	37	7	.088	7	.092	7	.100	7	.088	~ 6	.321	0	.096	7	.068
16	33	7	.126	7	.132	7	.105	7	.103	• 6	.344	15	.072	9	.052
17A	103	7	202	7	.232	7	.201,	7 '	.200	4	.461	0	.198	9	.191
17B	105	7	.200	7	.228	7	.201	7	.198	4	.477	0	.201	- 7	.196
18A	100	7	.216	7	.251	7	.182	7	.182	6	.381	0	.186	8	.173
18B	104	7	214	7	.252	7	.180	7	.180	6.,	.410	0	.187	8	.171
19	100	7	.265	7	.253	, <b>7</b>	•308	7	.276	6	.452	0	.350	10	.225
Average	•		.155		.156		.169		.140		314		.138		.116

#### TABLE 6---Summary of <u>RMS</u> comparisons.

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<sup>a</sup>Evidence of ill-conditioned solution for seven term model.

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	Experimenta	1	Calculated	l time to rup	ture, hours
$\operatorname{Temp}_{F}$ .,	Stress, ksi	Time to Rupture Hours	L-M Exact	0-S-D Exact	RAB Exact
1200 1200 1200 1200 1300 1300 1300 1300 1400 1400 1400 1500 1500 1500 1500 1600 1600 1600 1600 1800 1800 1800 1800	21.0 19.0 18.0 13.0 16.0 13.0 11.0 7.5 8.5 7.0 6.0 6.0 4.9 3.5 6.0 4.0 3.0 2.5 3.0 2.0 1.5 1.3	120     170     300     975     60     160     300     120     400     900     120     300     120     300     120     300     120     300     120     100     100     1000	81.36 140.47 188.67 1114.10 46.89 136.51 322.53 2315.56 166.00 427.33 905.32 138.89 354.14 1676.99 25.56 152.03 538.66 1200.88 21.84 110.91 351.35 623.51	149.16 236.38 303.14 1354.55 52.16 135.58 292.38 1702.62 122.73 299.80 - 609.27 .96.32 .244.54 1149.68 18.21 117.62 441.81 1022.11 24.58 158.75 596.31 1151.78	77.21 110.82 134.11 401.32 71.44 150.14 265.00 910.22 228.84 434.31 711.23 252.30 490.24 1409.44 73.96 302.83 765.48 1349.54 30.82 139.88 369.08 585.77

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## TABLE 7--Experimental and calculated stress-rupture data for Timken 35-15 stainless steel.

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## TABLE 8--Summary of Larson-Miller method correlations.

	71/2					9 T			DPAYG		DPMAX			
Number	of	terms	4	нла 5	7	4	5	7	4	5	7	4	5	7
	All	оу	c 1960	6 16 10	0 1546	6 1903	0.1671	0.1680	0.7937	0,7020	6.7159	0.8455	0.7960	0.9100
		1	1 1042	0.1004	0.1007	0 1514	0.0921	0.0858	P.6287	0.3849	0.3632	0.6633	0.4218	0.4410
		2	0 1 7 7 5	0.1490	0 1604	6 1952	n.1811	0.1882	0.8497	9.8029	0.1654	0,9488	0.9214	1.0204
		4	0.1790	0.1620	0.0000	0.1278	0 0795	0.0704	0.3750	0.3443	0.3131	n,4068	0.4077	0.4036
		5	0.0823	0.0752	0.0070	0 1100	0 1097	0 1135	0.5153	0.4818	0.5223	0.5700	0.5662	0.6494
		6	0 1000	0.0977	0.0970	0.1070	0 1001	0 1609	0 7714	0.6797	0.6497	0.0091	0.7370	0.7530
		7	0.1709	6.1257	0.1404	0.1007	9.1000	0.1962	n 6009	n 4219	0.8597	0.2631	0.9337	1.0632
		8	0 1791	0.1791	0.1777	0,1841	0,1914	0,1933	0 4214	0 5631	0.5410	0.7412	0.7294	1.7116
		ā.	0.1387	0,1224	0.1114	0,1466	0,1515	0.1203	0 6 7 1 9 7	0 4176	0.6386	0.6664	0.6786	0.7051
	11	á	0.1395	0.1358	6.1337	0.1467	0.1447	0.1464	0.6170	0.61/0	0.6000	0.7014	0.7087	0.7229
	- î î	R	6.1397	0.1340	0.1317	0.1465	0,1424	0.1436	(1.01/9	0.0750	1 0142	1 4289	1,2125	1.2280
		2	0,2356	0,1861	n,1833	0.2581	0.2091	0.2175	1,1520	0,9339	1 0510	1 5049	1 5613	1 6586
		2	0.3313	0.305?	0.2681	0,3385	n.3137	0.2993	1,3945	1.2985	1.02	0 7570	0 3772	-a
		-) 1	0.0677	0.0643	a	(+,0736	ካ.በ716	a	0.3201	0.3172			0.5772	0 5750
	1	.4	0.1497	0.0996	r.167r	0,1585	0,1072	0,0973	0.6729	0.4606	0.4282	0.7275	0.0277	0.0000
	-	2	0.1663	0.1342	0.1257	0.1774	n.1457	0.1417	0.7577	0.6309	0,6303	0,404	0.7362	0.0062
	1	10	0 2374	0.2064	3.2020	0.2426	0.2116	0.2092	n.9951	0.8725	C.8711	1,0364	0.9428	1.0415
	- 17	A	0 2526	0 2046	0.1999	0.2575	0.2090	Panš.0	1.0554	0.8607	0.8602	1,1363	1.0042	1,1186
	17	B	0 2304	0 2245	0 2161	0.2356	0.2303	0.2241	0.9679	0,9510	0.9344	1,0056	1.0292	1,1236
	18	3a	0.2007	0.0061	0 21 30	0 2327	6.2338	0.2215	0.9541	0,9631	0.9212	1,0288	1.1120	1,1542
	18	3B	0.720	1 arci		6 4485	0 7628	0.2751	1_8096	1.4981	1.1473	1.003	1.5931	1.2681
		19	0.4516	1.9225	H. SC00	0,440	<b>.</b>				-			

<sup>a</sup>Evidence of 111-conditioned solution.

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#### TABLE 9 --- Summary of Orr-Sherby-Dorn method correlations.

	RMS					STD			DPAVG		DPMAX		
Number	of terms	4	5	7	4	5	7	4	5	7	4	5	7
					-					•			
	Alloy												
	l	0.1892	0.3417	0.1387	0.1954	0.1476	0.1470	0.8149	0.6202	0,6264	0.8619	0.6899	0.7806
	2	0.2025	0.1072	0,0860	(+2081	0.1109	0.0903	0.8643	0.4636	0.3823	0.9103	0.4950	0.4450
	4	0.1819	0.1510	0.1493	0.1978	0,1680	0.1746	0.8608	C.7452	0.8036	0.9502	0.8133	0.9189
	5	0.6818	0.0611	n.0495	0.0872	0.0663	0.0557	0.3727	0.2876	0.2482	0.3975	0.3029	0.3043
	ē	0.0661	0.0574	0.0566	0.0718	0.0639	0.0662	0.3128	0.2834	0.3045	0.3282	0.3110	0,3688
	7	0.1582	0.1456	0,1306	0.1647	0,1531	0.1404	0,6907	0,6480	0,6048	0,7184	0,6680	0,6624
	ė	0.1389	0.1374	0.1308	0.1466	0,1472	0.1444	0,6209	0,6308	0.6329	0 6616	0,6944	0,7589
	ġ.	0.1204	0.1077	0.0935	0 1337	0.1156	0.1035	0.5668	0.4962	0.4541	0.5925	0.5693	0.5902
	llÁ	0.1511	0.1437	0.1424	0.1582	0.1531	0.1560	0.6707	0.6539	0,6803	0.7124	0.6901	0.7378
	118	0.1568	0.1413	0.1393	0.1644	0,1501	0.1519	0,6930	0,6393	0,6605	0,7803	0.7149	0,7542
	12	0.2689	0.1940	0.1914	0.2945	0.2180	0.2275	1.2931	0.9767	1,0607	1.4279	1.1902	1.3414
	13	0.3420	0.3193	0,2910	0,3503	0,3281	0.3023	1.4425	1.3578	1.2643	1.5942	1.6033	1,5184
	ĩ4	0.0873	6.0738	a	0.0949	0.0821	a	n.4131	0.3642	a	0.4261	0.3991	a
	15	0.1742	0.0990	0,0923	0.1844	°.1073°	0.1025	0,7830	0.4614	0,4516	0.8225	0.4857	0.5349
	īć	0.1797	0.1416	0,1317	Õ 1917	0,1537	0.1484	10,8191	0.6661	0,6605	0.8540	0.7447	0.8237
	17A	0.2864	0.2370	0.2322	0.2921	0,2429	0.2405	1,1982	1.0016	1.0013	1,2249	1.0250	1,1031
	17B	0.3181	0.2329	0,2284	0 3243	0.2387	0.2364	1,3290	0.9830	0,9830	1,3996	1.0309	1,1771
	18A	0.2658	0.2650	0.2505	0.2713	0.2719	0.2597	1.1145	1,1226	1,0832	1,1424	1,1523	1,2127
	18B	0 2702	0,2661	9,2520	0.2755	0,2727	0.2609	1,1297	1.1238	1.0855	1,1678	1.1764	1.2777
	19	0.5102	0.4067	0.2533	0:5207	0.4173	0.2627	2.1390	1.7232	1.0957	2,1995	1.7714	1,1595

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# <sup>a</sup>Evidence of ill-conditioned solution.

		RMS				STD			DPAVG		DPMAX		
Number of	terms	4	5	7	4	5	7	4	5	7	4	5	7
Allo	у												
1		0,2417	0.2256	0.2204	0.2496	0,2350	0.2335	1.0412	0.9873	0,9951	1.1062	1.0916	1.2462
2		6.2042	0,1679	0,1602	0.2098	0.1738	0.1682	0.8714	0.7264	0.7119	0.9425	0.8035	0.8258
4		0.1776	0.1628	0.1610	0,1930	0.1812	0.1883	0.8404	0.8036	0.8666	0.4913	0.8661	0.9908
5		0.1055	0.0941	0.0886	0.1126	0,1022	0.099A	0,4809	0.4429	0,4446	0.4988	0,4680	0.5449
6		0.1264	0.1239	0.1235	0.1376	0.1378	0.1445	0,5990	0.6111	0.6647	0.6761	0.6824	0.8050
7		0.2025	0.1830	0.1788	0.2105	0,1925	0.1922	0.8830	0.8145	0.8279	0,9291	0.8500	0,9079
8		0.2329	0.2339	0.2330	0.2469	0.2505	0.2572	1,0455	1.0735	1,1276	1,1286	1,1731	1,3518
ŏ		0.1639	0.1516	0 1409	0,1733	0,1627	0.1559	0,7348	0,6981	0.6844	0.7706	0,7975	0,8895
114		0.1302	0.1241	0 1219	0.1369	0.1322	0.1336	0 5779	0.5646	0,5826	0.6197	0,5990	0,6316
118		0.1317	0.1249	0 1217	0.1381	0.1327	0.1329	0.5822	0.5652	0.5778	0.6514	0.6310	0.6609
10		0.235	0.1821	0.1779	0.2579	0.2046	0.2114	1.1325	0.9167	0.9858	1,2058	1.1163	1,2468
13		0.3492	0.3056	0.2914	0.356A	0.3140	0.3027	1.4688	1.2996	1.2661	1.6739	1,5537	1.5409
10		0.6885	6.0728	a	0.0875	0.0810	a	0.3810	0.3591	a	0.3928	0.3936	a
15		0.1673	0.1153	0.0999	0.1771	0.1240	0.1110	0.7520	0.5331	0.4889	0.7838	0.5629	0.5796
10		1559	6.1157	0.1051	0.1663	0.1256	0.1184	6.7106	0.5443	0.5268	0.7567	0.6055	0.6570
174		6 26.55	6 2184	0 2012	6.2736	n 2239	0.2085	1,1222	0.9231	0.8679	1 1497	0 9447	0.9559
175		0 2745	0 2205	0 2007	0.2849	0.2260	0.2077	1.1677	0.9307-	0.8637	1,2206	0.9689	1.0323
184		0 1944	0 1942	0 1022	0 1989	0.1992	0.1889	0.8171	0.8227 -	0.7878	0.8378	0.8482	0.8827
104		0 1987	0 1954	0 1805	0 2027	0.2003	0.1567	0.8309	0.8253	0.7768	0.8621	0.8620	0.9142
100		6 4141	6 3640	0 3076	0 4 2 4 7	0.3735	0.3192	1.7446	1.5423	1.3313	1.8299	1.6135	1.4131
19		0.416)	0,0040		0.7277	0.0100	V. 01 /r			~			

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#### TABLE 10---Summary of Manson-Succop method correlations.

<sup>a</sup>Evidence of ill-conditioned solution.

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TABLE 11	Summary	of	Manson-Haferd	method	correlations.
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			RMS				STD			DPAVG		DPMAX			
Number	of	terms	4	5	7	4	5	7	4	5	7	4	5	7	
	A1)	Loy												•	
		1	0,2122	0.1653	0,1533	0,2192	0.1722	0.1624	0.9144	0.7235	0.6921	0.9716	0.7998	0.8466	
		2,	0.1893	0.1145	0.0741	0.1946	0.1185	0.0779	0.8040	0,4954	0.3295	9 P668	0.5535	0.3452	
		4	0.1722	0.1312	0.1284	6,1872	0.1460	0.1502	P. 814A	0.6472	0.6908	0.9018	€0.7294	0.8072	
		5	0,0930	0.0597	0.0541	0.0992	0.0649	0.0610	0.4239	0.2809	0.2712	0.4677	0.3406	0.3510	
		6	0,0481	0.0455	0.0448	0.0523	0.0507	0.0525	0.2277	0.2247	0.2413	0.2468	0.2594	0.2988	
		7	0.1475	0.1294	0,1212	0.1535	0.1361	0.1303	0.6437	0.5759	0.5608	0.6907	0.6429	0.6534	
		8	0,1524	0.1390	0,1365	0.1609	0.1489	0.1507	0.6813	0.6380	0.6605	0.7561	0.7468	0.8061	
		9	0.1476	0,1299	0.1111	0.1560	0.1394	0.1231	0.6611	0.5975	0.5397	0.8048	0.7819	0.7105	
	11	A	0,1248	0.1143	0,1128	0.1312	0,1217	0.1235	0 5540	0.5196	0.5388	0.5985	0.5721	0.5898	
	11	в	0,1287	0.1144	0.1111	0.1350	0.1215	0.1212	0.5689	0.5172	0.5266	0.6492	0.6060	0.6095	
	1	2	0.2176	0,1821	0.1779	0.2384	0.2046	0.2114	1.0455	0.9157	0.9847	1.3147	1.1877	1.2502	
	'ī	3	0.3448	0,3041	0.2819	0.3523	0.3124	0.2929	1,4505	1.2929	1.2244	1.6561	1.5899	1.6379	
	1	4	0,0773	0,0587	a	0.0840	0.0654	а	0.3655	0.2896	a	P.4131	0.3481	a	
	้า	5	0.1673	0.1015	0.0883	0.1771	0.1091	0.0980	0.7520	0.4690	0.4315	0.8203	0.5505	0.5441	
	ī	6	0.1557	0.1148	0,1032	0,1660	0.1247	0.1162	0 7093	0.5398	0.5172	0.7821	0.6419	0.6600	
	17	'A	0.2677	0.2170	0.1998	0.2730	0.2224	0.2069	1.1199	0.9170	0.8614	1.1706	0.996Å	1.0388	
	17	'B -	0.2758	0,2179	0.1984	0.2012	0.2232	0.2054	1.1525	0.9193	0.8537	1.2466	1.0843	1 1137	
	īġ	Ā	0,1946	0,1936	0.1822	0,1986	0.1986	0.1889	0.8158	0.8200	0.7878	0.0540	0.0953	0 9548	
	- 18	B	0,1967	0.1948	0,1804	0,2006	0.1997	0.1868	r.8224	0.8226	0.7769	0.8926	0.9539	0 9775	
	ĩ	.9	0,4129	0.3619	0,2760	0.4214	0.3713	0.2862	1,7310	1,5331	1,1934	1.0026	1.6363	1.3242	

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<sup>a</sup>Evidence of ill-conditioned solution.

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. TABLE 12--Summary of Rabothov method correlations.

		RMS				STD			DPAVG			DPMAX		
Number	of terms	3	4	6	.3	4	6	3	4	6	3	4	6	
	Alloy			natu "	• •	-								
	1	0.4387	0.2185	0,2091	0.4494	0.2257	0.2178	0.0000	0.0000	0.9158	0_0000	0.0000	1,0270	
	2	0.3800	0.245ė	0.2452	0.3879	0,2526	0,2538	1,8936	1,0257	1.0269	3,5595	1.6010	1.6469 .	
	4	0.3033	0.2473	0.2644	0.3225	0.2688	0.2942	1,4867	1,4262	1,4309	3,4359	3.8611	5.3300	
	5	0.3040	0.3053	0,3132 `	0,31'88	0.3257	0.3400	1.7321	1.6602	1.7328	3,1460	2,9195	3.2385	
	6	0.3228	0.2975	0,3425	0.3432	0.3235	0.3811	1.6292	1.6693	1.6632	4.3534	4.2000	4 4432	
	7	0.4090	0,2674	0.2561	0:4214	0.2783	0,2694	1,9803	1.3364	1,3095	6.4589	4.1598	3.6349	
	8 .~	0,5865	0.2912	0.3257	0.6105	0.3074	0.3489	2,9696	1.6791	1,9132	12,1315	3,4606	5.8765	
	9	0,2364	0,1523	0,1478	0;2464	0.1610	0,1611	1,0881	0.7106	0,7195	1.3500	1.0488	1.1497	
	<b>1</b> 1A	0,5037	0,1791	0,1915	0.5227	0,1882	0,2040	1.4762	0.8855	0,9193	3,7275	2.4518	2.8222	
	11B ·	0.4127	0,2180	0.2326	0.4276	0.2287	0.2471	1.8748	1.0452	1,0775	4,8993	3,7546	4.5071	
	12	0.4197	0;3891	0.3854	0.4487	0.4262	0.4332	• 2.4168	1,8572	1,9490	6.8192	3,1121	3,1838	
	13	0.8140	0,3982	0.3626	0.8272	0.4068	0.3746	3,7109	2.0841	1,9390	7,4721	5,0910	3.7243	
	14 -	0,3240	0.2945	~0 <b>;2927</b>	0.3445	0.3202	0.3257	· 0.0000	1.4057	1,4524	0,0000	1.5688	1.5985	
	15	0.3249	0,3306	0.3210 -	0.3389	0.3501	0.3451	1,6262	1,6262	1.4666	3.4998	5,7345	4.5364	
	16	0.5893	0,3604	0.3438 .	0,6181	0,3845	0.3732	1,2650	1.1264	1,1590	6,0260	3.8238	4.1400	
	17A	JO.4785	0,4608	0.4638	0.4857	_0, <b>,</b> 4700	0.4755	2,8635	2,2600	2.3512	13.3286	7.2185	8.4388	
	17B	0.4892	0,4770	0.4770	0.4963	0.4863	0.4887	2.8288	2.4270	2.4692	13,1340	10.3149	10.8394	
	18A	0,3896	0,3921	0.3807	0.3955	0.4002	0.3906	1.7884	-1.8021	1.8257	5.3525	5.8298	11.8130	
	18B	0.4168	0,4116	0.4101	0.4229	0.4198	0.4203	1.9422	1.7542	1.8609	16,9520	5.7573	14.9843	
	19	0.6105	0,4668	0.4516	0.6196	0.4764	0,4634	3,4160	2.0914	2.0226	10,1529	3.4808	3,1542	

<sup>a</sup>Based upon backtransformed log time values.

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-	• •	· ,	TABLE 1	3Summary	of GIV	JAR method co	rřelatior	15.		
	Alloy .	No. of Observ.	Prime V Transfo <u>Temp.</u>	ariable rmation <u>Stress</u>	No. of <u>Start</u>	Variables <u>"Best"</u>	RMS	<u>st</u> d	DPAVG	DPMAX
	1 ,	64	1/T	<sub>0</sub> 1/3	12	9	.1060	.1130	.4921	.6387
	2	• 75	log T	<sub>0</sub> 1/3	12	J]	.0551	.0592	.2548	.3099
	4	26	1/T	<sub>0</sub> 1/3	12	7	.0883	.1033	.4754	•5273 <i>,</i>
	5	33	log T	σ	11	9	.0426	.0499	•2284	.2799
	6	26,	1/T	log σ	9	б	.0418	.0476	,2150	.2485
	7	52	log T	$\sigma^{1/3}$	12	10	.0910	.1013	.447ı	,5155
	8	39	1/T ·	σ	11	10	.0744	,0863	.3910.	.4971-
	9	38	log T	σ	11	8	•0677	.0762	•3384	.4169
	11A	42	1/T	<sub>d</sub> 1/3	12	7	.0997	.1092	.4764	•5360
40	11B	44	1/T	σ.	11	9	.0985	.1104	.4894	•5686
	12	24	1/T	σ	11	б	.1664	<b>.</b> 1921	.8784	1.0377
	13	95	1/T .	log σ	11	8	.2677	•2797	1,1756	1.4435
	14 ·	26	log T	$\sigma^{1/3}$	12	10	•0368	.0456	,2218	.2547
	15	37	log T	σ	lļ	7	.0683	.0758	3337	. <u>4</u> 185
	16	33	1/T	σ	11	. 9	.0520	.0610	.2788	•35 <u>2</u> 9
	17A	103	1/T	σ	11	9.	.1913	.2002	, <sup>8</sup> 417	.9649
	17B	105	1/T	$\sigma^{1/3}$	12	7	.1963	.2032	<b>.</b> 8450	.9053
,	18A	100	l/T	σ,	11	8 ,	.1726	.1799	•754l	.8583
	18B	104	1/T	σ <sup>1/3</sup>	12	8	.1712	.1782	•7451	.8174
64	19	100	1/T	$\sigma^{1/3}$	12	10	.2248	•2369	1.0028	1.0978

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Fig. 1-Correlation of Rabotnov simulated data set.



Fig. 2---Comparison of regression residuals for Rabotnov simulated data set.

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Fig. 4--Regression residuals for alloy 4, GIVAR analysis.

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Fig. 6-Comparison of M-H and GIVAR correlations for alloy 16.



Fig. 7---Comparison of regression residuals for alloy 16.

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Fig. 8-RMS values for various methods of analysis.

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# COMPUTER PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA<sup>1</sup>

By , ,

Donald R. Rummler

<sup>1</sup>This manuscript will be submitted to the National Aeronautics and Space Administration for publication as a Technical Memorandum.

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## COMPUTER PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA<sup>1</sup>

Bу

Donald R. Rummler

#### ABSTRACT

A computer program which uses several parametric model equations to analyze creep-rupture data is presented in detail. The model equations include the Larson-Miller, Orr-Sherby-Dorn, Manson-Succop, Manson-Haferd, and Rabotnov parameter methods. Standard multiple regression techniques are used to analyze data with respect to each model equation. In addition to the usual regression statistics, the program calculates statistical intervals including confidence and prediction intervals. Graphical output includes a residual plot with respect to the dependent variable and a cumulative distribution of the residuals. The computer input and output, in printed and plotted form, for sample problems are presented to aid the user in setting up and running the program.

#### SUMMARY

A computer program which uses several parametric model equations to analyze creep-rupture data is presented in detail. The model equations include the Larson-Miller, Orr-Sherby-Dorn, Manson-Succop, Manson-Haferd, and Rabotnov parameter methods. Standard multiple regression techniques are used to analyze data with respect to each model equation. In addition to the usual regression statistics, the program calculates statistical intervals including confidence and prediction intervals. Graphical output includes a residual plot with respect to the dependent variable and a cumulative distribution of the residuals. The program, its subroutines and their variables are listed and defined. The computer input and output, in printed and plotted form, for sample problems are presented to aid the user in setting-up and running the program. The development of the parameter model equations and the use of statistical intervals is discussed. , • \*

### INTRODUCTION

The importance of creep-rupture data analysis has led to a large number of papers which either propose new parametric analysis approaches (refs. 1, 2, 3, and 4, for example) or offer detailed comparisons of different parametric methods (refs. 4, 5, and 6). Most parametric methods for creep-rupture data analysis are empirical. Consequently, it is common practice for the data analyst to fit the creep-rupture data at hand to a variety of parametric model equations to select the most appropriate analysis method.

Although several analysis methods have been presented in general terms (ref. 6, for example), there is no widely used, efficient computer program tailored specifically to the parametric analysis of creep-rupture data. In addition, most methods do not include generation of statistical intervals to aid in the selection of the "best" parametric model equation for a particular set of data.

This paper describes the development and use of a computer program for the parametric analysis of creep-rupture data. The program includes provisions for the analysis of five different parameter methods. The parametric equations used and the statistical quantities calculated are discussed. The computer program input and output, in printed and plotted form, for three sample problems are presented to aid the user in setting up and running a problem with the program.

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#### PROGRAM DESCRIPTION

The computer program (PARAM) was developed to analyze and correlate creep-rupture data utilizing a variety of parametric method model equations. For each model equation, a function of the time to a particular creep event (such as time to 0.005 strain) is the dependent variable. Functions of stress and temperature are the only correlating independent variables. The major features of the program are as follows:

(1) The method of least squares is used to establish the coefficients for the parametric model equation selected for analysis.

(2) Provisions are made for analysis with four widely used time-temperature methods (Larson-Miller, Orr-Sherby-Dorn, Manson-Succop, and Manson-Haferd) and one time-stress (Rabotnov) method.

(3) Polynomial forms of the parametric model equations up to the fifth order are included.

(4) Multiple analyses can be accomplished during a single computer run.

(5) In addition to the usual regression statistics, the program calculates the maximum and minimum value of each independent variable, as well as its range and average value.

(6) The program also calculates the relative influence, contribution to the sums of squares, and warns of coefficient solution errors for each independent variable.

(7) Listings are made of the observed and fitted values of

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the dependent variable in both regression and real variable coordinates.

(8) Two statistical intervals, the 95 percent confidence and the 95 percent prediction, are approximated and calculated for each observation.

(9) Residual plots are made to indicate how the regression residuals are distributed over all of the fitted values of the dependent variable and whether they are normally distributed.

PARAM was written in FORTRAN IV language for the Control Data 6000 series digital computer under the SCOPE 3.0 operating system. The program is dimensioned for a maximum of 5 input variables, a maximum of 10 derived independent variables and a maximum of 200 observations for each data set. It requires approximately 60,000 octal locations of core storage. A source listing of the main program and its subroutines is presented in appendix A. A detailed description of the matrix equation solution subroutine MATINV and the plotting subroutines PSEUDO, DDIPLT and CALPLT are presented in appendix B.

#### ANALYSIS

The analysis utilizes standard least squares multiple regression analysis techniques (refs. 7 and 8) to solve parametric equations of the following form:

 $Y = b_0 + b_1 X_1 + b_2 X_2 + --- + b_1 X_1$ (1) where Y = fitted value of dependent variable

 $X_1, X_2$  . . . ,  $X_i$  = independent variables

 $b_0 = estimated Y intercept when all <math>X_i = 0$ 

b<sub>1</sub>, b<sub>2</sub>, - - - b<sub>i</sub> = estimated coefficients of independent variables

Specifically, the equation forms chosen for each of the parametric methods selected are as follows:

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$$\begin{split} \mathbf{T}_{\mathrm{F}} &= \mathrm{temperature, }^{\mathrm{O}}\mathbf{F} \\ \mathbf{T}_{\mathrm{K}} &= \mathrm{temperature, Kelvin} \\ \mathbf{T}_{\mathrm{R}} &= \mathrm{temperature, Rankine} \\ \mathbf{T}_{\mathrm{O}} &= \mathrm{offset \ temperature = } \mathbf{T}_{\mathrm{F}} - \mathbf{T}_{\mathrm{A}} \\ \mathbf{b}_{1}, \ \mathbf{T}_{\mathrm{A}}, \ \mathbf{a} &= \mathrm{constants \ estimated \ by \ method \ of \ least \ squares.} \end{split}$$

Both the M-H and RAB techniques require the use of iterative, non-linear multiple regression techniques to estimate all of the constants.

Each parametric equation can be analyzed in truncated form since the number of equation terms (LLO) is selected with input case control cards.

The development of each of the parametric method model equations is presented in appendix C.

#### PROGRAM USAGE

To submit a problem, information is normally entered on punched cards. Four types of information cards (option, case control, data set identification, and data) are the only input required. Output includes listings and plots.

## Input

The option card controls both the printed and graphic output of the program. It also establishes the initial values to be used for the iteratively modified constants for the Manson-Haferd and Rabotnov parametric analyses. The case control cards determine the parametric equation forms to be evaluated and their

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degree of truncation. A data identification card and the data cards complete the deck set up. The input card order, format, permitted values and comments follow:

<u>Option</u>	card	(215, 2	F10.0)		
Column	FORTRAN Variable	Val	ue	Co	omments
5	INPUT	(	No	listing of	input cards
1		-	Li	st data set	I.D., option,
			an	d case conti	rol cards
		, ,	Li	st l + data	observa-
			ti	ons	
		-	Li	st 2 + regre	ession varia-
			bl	es for first	t five
`			ob	servations	
10	OUTPUT	(	No	listing of	residuals
,		:	. Li	st regression	on residuals
			1	+ list back	transformed
			re	siduals	
			2	+ regression	n residual .
			pl	ots	
ll to 2	20 TA		In	itial value	for constant
			in	non-linear	M-H equation;
			_		

3 2 + regression residual plots Initial value for constant in non-linear M-H equation; A value of -5000.0 is recommended Initial value for constant in non-linear RAB equation; A value of 0.2 is recommended.

21 to 30

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Column	FORTRAN Variable	Value	Comments
5	NPAM(I)		Parametric expression to
			be evaluated
		l	Larson-Miller
		2	Orr-Sherby-Dorn
		3	Manson-Succop
		4	Manson-Haferd
		5	Rabotnov
10	LLO(I)	2to6	Number of coefficients to
			be determined for parametric
			expression selected, see
			ANALYSIS section of
			paper.

The program is dimensioned for a maximum of 20 case control cards. During a single computer run, a data set can be evaluated with 20 different parametric model equation forms. A blank card must follow the last case control card.

Blank Card

Column

Data	identification	card	(8A10)
			<pre></pre>

FORTRAN Variable

Comment ·

l to 80 TYPE

Data I.D. Any characters in columns 1 to 80. This title is included in all listed output

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Data cards	(3F12.0)	
Column	FORTRAN Variables	Comments
1-12	RS(I,1)	Time to a particular creep event
13 <b>-</b> 24	RS(I,3)	Temperature, <sup>O</sup> F
25 <b>-</b> 36	RS(I,2)	Applied stress

The program is dimensioned for a maximum of 200 observations in a data set. Round-off errors can be minimized by limiting the range of the variables. This range reduction is helpful since most creep-rupture data is ill-conditioned (see refs. 7 and 8). Last data card must be followed by a blank card.

### Blank card

More than one set of data may be analyzed with a single set up of the option and case control cards. To analyze additional data sets during a single computer run, assemble the deck as follows:

### Option card

Case control cards

Blank card

First data set

### Data identification card

Data cards

Blank card

## Data identification card

Data cards Second data set
Blank card

### Data identification card

<u>Data cards</u>

Third data set

Blank card

As many data sets as desired may be analyzed during a single computer run with this type of deck setup.

#### Output.

Examples of printed and plotted output are presented in the discussion of sample problems. Most of the output headings are self-explanatory or standard statistical terms (refs. 7 and 8). Some headings are abbreviations of standard terms and/or require additional description. These headings and brief descriptions, in the order of their appearance for the printed output are as follows:

<u>Heading</u> <u>Description</u> STANDARD ERROR Standard error of estimate is square root of residual mean square, sometimes called residual root mean square

MULT. CORREL.

COEFF. SQUARED The multiple correlation coefficient squared, sometimes called coefficient of determination

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MIN	The minimum value of indicated variable;
	independent variables are in tabular form
MAX	The maximum value of indicated variable
Y	Tabulated values of independent variable
Xl-X(L2)	Tabulated values of independent variables;
	L2 is number of variables in case
VARIABLE	Transformation required for parametric
	method being evaluated
COEF. P.I.	Calculated coefficients for the fitted
	equation, indexed by I starting with b
S.E. COEF.	Estimated standard error of the coeffi-
·	cient
Т	COEF.P(I)/S.E. COEF.
RAN X(I)	Range of independent variable
RINF(I)	Relative influence of independent
	variable, $\frac{(COEF.P(I)(RANX(I))}{Y RANGE}$
PSUM	The fraction of the total sums
	of squares explained by an inde-
	pendent variable; corrected for
	those independent variables which
	preceed it in the listing

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CERR .	The percentage difference
	between MATINV and Gaussian
	elimination solutions for
	coefficient; values in excess
	of 0.01 suggest round-off
	errors due to ill-conditioned
	normal equations

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95 PERCENT	The 95 percent prediction interval for
PREDICTION	a single future observation is estimated
INTERVAL	for each observation in regression
STATISTICS	variable space; these values are back
	transformed into log time space to calcu-
	late average and maximum values; values
	for the t distribution are approximated
	with a third order polynomial in log
REAL TIME FACTOR	(degrees of freedom) 10. <sup>(WIDTH)</sup>

RESIDUALS -	Values listed under this heading are
REGRESSION	in terms of the regression dependent
SPACE	variable coordinates
RESIDUAL	Observed value of dependent variable-cal-
	culated value of dependent variable
PCTERR	(100)(RESIDUAL) Y

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ORDER	The rank order of the residual in regression
	coordinates; the rank order of the
	PCTERR in real space coordinates;
	ordered with respect to the largest
	absolute value.
CIMIN	Estimated lower limit of 95% confidence
	interval for the mean
CIMAX	Estimated upper limit of the 95%
	confidence interval for the mean
PIMIN	Estimated lower limit of 95% prediction
	interval for a single future observation
PIMAX	Estimated upper limit of the 95%
	prediction interval for a single future
	observation

TVALUE =  $(10.0)^{T1}$ 

where

T1 =  $0.86186 - 0.98427 \text{ DF} + 0.58495(\text{DF})^2$ -  $0.11594(\text{DF})^3$ 

DF = residual degrees of freedom for regression.

The graphical output of the program includes a plot of the residuals with respect to the calculated value of the dependent variable (FITTED Y) and a cumulative normal distribution of the residuals (ZP NORMAL). For the ZP NORMAL plot, the plotting points for the abscissa, P, are in terms of the inverse of the standardized normal distribution and are calculated in the following manner:

for FZ = 0  $\neq$  0.5 ZP<sub>1</sub> = 1.0451 + 4.3598XP + 3.4606(XP)<sup>2</sup> + 1.9088(XP)<sup>3</sup> + 0.5446(XP)<sup>4</sup> + 0.0608(XP)<sup>5</sup>

where XP = log FZ

, . -3. FZ = (j - 3/8)/(N + 1/4)

j = 1, 2, - - N when the residuals are arranged in order of increasing magnitude.

for FZ =  $0.5 \Rightarrow 1.0^{-1}$ 

$$XP = \log (1-FZ)$$
$$ZP_2 = -ZP_1$$

The ZP expression approximates the inverse of the standard normal distribution.

### SAMPLE CASES

Three sample cases are presented to illustrate operation of the computer program and a method for rapidly selecting the most applicable parametric equation for a single set of creep-rupture data. The data are for a type 316 stainless steel (ref. 5). The three sample cases described in this section required a total of 10.9 seconds of CDC 6600 CPU time to compile and run.

## Case 1

For this case, all five parametric methods in second degree form were used to correlate the data. The purpose of this case was to quickly scan the parametric models to select a single parameter for further study. Output was minimized by using INPUT = 1 and IOUT = 0. The program input and output for case 1 are presented in Figures 1 and 2, respectively.

When compared to the other four parameter methods, the O-S-D method had the highest MULT. CORREL. COEF. SQUARED, the lowest AVERAGE and MAXIMUM WIDTH of the 95% prediction interval. It also had the lowest STANDARD ERROR of the four time-temperature parameters.

#### Case 2

Based upon the results of case 1, the Orr-Sherby-Dorn parameter (NPAM = 2) was selected for further evaluation. The purpose of this case was to quickly determine the degree of the O-S-D expression which would provide the best correlation of the data. Once again, output was minimized (INPUT = 0, IOUT = 0).

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The program input and output for case 2 are presented in Figures 3 and 4, respectively.

With respect to MULT. CORREL. COEF. SQUARED, there is no appreciable improvement in the correlation produced by increasing the degree of the polynomial expression. However, the STANDARD ERROR shows a steady decrease as additional variables are added up to the fifth order expression where it increases slightly. The T values for this fifth order expression clearly illustrate the inflation of the standard error of the coefficients which this high level of co-linearity produces. The CERR value for I = 2 (X(I) = LOG STRESS) suggests that the solution matrix was ill-conditioned because the two methods of solution do not agree.

The RESIDUAL SUMS OF SQUARES for the fourth order expression is approximately 30 percent lower than the third order expression. Although significant differences between the other correlation indications are not apparent, the fourth order expression is selected for further evaluation.

#### Case 3

Final verification of the fourth order expression selected in case 2 requires the full output capabilities of the program (INPUT = 3, IOUT = 3). The input and output for this case are presented in figures 5 and 6. The output includes a listing of the first 5 values of the regression variables, residuals and statistical intervals in regression and back transformed coordinates and plots of residuals with respect to the

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calculated dependent variable (Y FITTED) and with respect to the normal cumulative distribution. The most important part of the verification of the fourth order expression is the examination of the residual plots. These plots suggest that the residuals have a zero mean and are randomly distributed with respect to the FITTED Y and that their cumulative distribution is normal. These two characteristics of the residuals are necessary for the calculation of valid statistical intervals.

The method selected for determining the "best" parametric equation for a set of data was used primarily to demonstrate the capabilities of the computer program PARAM. For other methods see references 4, 5, and 6. For a further discussion of the use of statistical intervals, the reader is referred to references 7 and 11.

#### CONCLUDING REMARKS

A computer program specifically developed for the parametric analysis of creep-rupture data has been discussed. The equations used for the analysis of five parametric methods and the computer program used to implement the analysis are given.

The computer program is versatile, allows rapid assessment of parametric methods for creep-rupture data, and has a relatively small core storage requirement. In addition to the statistics which are usually calculated and output by multiple regression programs, the program outputs the 95% confidence interval on the mean and the 95% prediction interval for a

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future observation. Residual plots are provided to assess the validity of the calculated statistical intervals.

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## APPENDIX A

## SOURCE LISTING OF PROGRAM PARAM

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	PROGRAM PARAM(INPUT+OUTPUT+PUNCH+TAPE5=INPUT+TAPE6=OUTPUT+ 1TAPE7=PUNCH)	00000001 00000002
С	PARAM	0000003
Ć	PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA	00000004
С	COEFFICIENTS FOR PARAMETRIC MODEL EQUATIONS ARE DETERMINED BY	00000005
С	METHOD OF LEAST SQUARES	00000006
С	Y= B0+B1X1+B2X2	00000007
С	PARAMETRIC METHODS INCLUDE	0000008
с	LARSON-MILLER(L-M)	0000009
С	ORR-SHERBY-DORN(0-S-D)	00000010
с	MANSON-SUCCOP (M-S)	00,000011
с	MANSON-HAFERD (M-H)	00000012
с	RABOTNOV (RAB)	00000013
с	DONALD R. RUMMLER	
С	NASA-LANGLEY RESEARCH CENTER . HAMPTON . VA 1976	•
Ć C	ARRAYS WHICH DEPEND ON NUMBER OF OBSERVATIONS IN DATA SET (L1)	00000016
	DIMENSION AA( 200)CY( 200).CIMAX( 200).CIMIN( 200)	00000017
	DIMENSION ERRPER( 200), F( 200,10), IPERM( 200), PYMAX( 200)	00000018
	DIMENSION PYMIN( 200), RIS( 200), RS( 200,5), TEMP( 200), Y( 200	)00000019
	DIMENSION ZP (200)-	00000020
С	ARRAYS WHICH DEPEND ON NUMBER OF VARIABLES IN REGRESSION MODEL	00000021
С	NUMBÈR OF INDEPENDENT VARIABLES (L2)	00000022
	DIMÉNSION CERR'(10) + PAR(10)	0000023
	DIMENSION PAR1(10), SB(10); SSR(10), SUMA(10), SUMB(10)	00000024
	DIMENSION, SUMP2(10,10), SUMX(10), SUMXY(10,10), SUMX1(10,10)	00000025
	DIMENSION _ SUMX2(10), T(10), XMAX(10), XMIN(10), XRAN(10)	00000026
	DIMENSION XMEAN(10)	00000027
С	NUMBER OF COEFFICIENTS DETERMINED (L3)	00000028
	DIMENSION $D(11,11) + DD(11,11) + E(11,1) + G(11,1) + INDEX(11,2)$	0000029
	DIMENSION IPIVOT(11) X(11)	00000030
С	NUMBER OF COEFFICIENTS +1 (N3)	00000031
	DIMENSION A(12,12), B(12,12)	00000032
С	ARRAYS WHICH DEPEND UPON OTHER FACTORS	00000033
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· · ·	0000034
NUMBER OF CASES	0000035
DIMENSION LLO(20) · NPAM(20)	0000036
MISC NAR(20) DAM(5)	
DIMENSION TYPE (8) IN (2) VAR (3()) PAM (3)	0000038
DATA ( $PAM(I) \cdot I = 1 \cdot 5$ )/ 3HL-M · 5HO-S+U · 3HM-S · 5HM-H · 5HS+A/T ·	0000039
DATA(VAR(I),I=1,30)/3H1/T,3H5/1,5H5**2/1,6H5**3/1,6H5**4/1,	0000040
16HS**5/T •	00000041
23H1/T+1HS+4HS**2+4HS**3+4HS**4+4HS**5+	00000042
31HT,1HS,4HS**2,4HS**3,4HS**4,4HS**5,	00000043
42HDT+4HDT*S+7HDT*S**2+7HDT*S**3+7HDT*S**4+7HDT*S**5+	00000046
55H1/L*T+8H1/L*T**2+9H1/L*T**3+9H1/L*T**4+8H1/L*T**5+9H1/L*T**6	0000045
L1 = NUMBER OF OBSERVATIONS IN DATA SET	00000045
LI IS DETERMINED BY PROGRAM	0000043
L2 = NUMBER OF VARIABLES INPARAMETRIC EQUATION SELECTED	0000047
L3 = NUMBER OF COEFFICIENTS TO BE DETERMINED, INCLUDES BU	00000048
L3 = L2+1	00000049
CALL PLOT VECTOR FILE ONLY WHEN OUTPUT INCLUDES PLOTTING	0000085
CALL PSEUDO	и <b>ж</b>
CALL LEROY	
COMPLETE DATA DECK SETUP INCLUDING OPTION AND CASE CONTROL CARDS	** •
FOR EACH DATA SET ARE REQUIRED IF 1 - CONTINUE CARD IS HERE	
1 CONTINUE	00000081
READ INPUT AND OUTPUT OPTIONS AND	,
INITIAL VALUES OF M-H AND RAB CONSTANTS	
IPUT = INPUT LISTING OPTIONS	00000053
0 - NO INPUT LISTING	
1 - CASE CONTROL VARIABLES	
2 - + DATA SET OBSERVATIONS	
3 + TRANSFORMED REGRESSION VARIABLES FOR FIRST	
FIVE OBSERVATIONS	
OUTPUT = OUTPUT OPTIONS	0000058
0 - NO RESIDUALS	
1 - RESIDUALS REGRESSED SPACE	0000060
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с		2 - 1 + REAL SPACE RESIDUALS	00000061
č		3 - 2 + RESIDUAL PLOT IN REGRESSED SPACE	00000062
		READ(5,4) INPUT, IOUT, TA,RA	00000051
	4	FORMAT(215+2F10+0)	00000052
		IF(EOF+5)900+9	
	9	CONTINUE	
с		READ CASE CONTROL CARDS	00000063
с		PUT BLANK CARD AFTER LAST CASE CARD	00000064
с		LLO = TOTAL NUMBER OF VARIABLES FOR CASE	00000069
c		NPAM = PARAMETRIC EXPRESSION TO BE EVALUATED	00000070
с		1 - LARSON-MILLER (LM)	00000071
с		2 - ORR-SHERBY-DORN (OSD)	00000072
с	c	- MANSON-SUCCOP (MS)	00000073
с		4 - MANSON-HAFERD (MH)	00000074
с		, 5 - RABOTNOV (RAB)	00000075
		I3=1 ·	00000067
	3	READ (5.2) NPAM(13).LLO(13)	00000068
		IF(LL0(13)) 7.8.7	00000076
	7	Ì3=I3+1	00000077
-		GO TO 3	00000078
	2	FORMAT (215)	00000079
	8	13=13-1	00000080
С		ONLY ONE SETUP OF OPTION AND CASE CONTROL CARDS ARE REQUIRED	
с		FOR MANY DATA SETS IF 1 - CONTINUE CARD IS HERE	
с	1	CONTÎNUE	
С		READ DATA SET IDENIFICATION (TYPE)	00000082
		READ(5,777)(TYPE(I),I=1.8)	00000083
	777	FORMAT (BA10)	00000084
		IF(EOF+5) 900+6	00000085
	6	1=1	00000086
с		READ IN OBSERVATIONS	00000088
С		IF NUMBER OF CORRELATING VARIABLES CHANGES.	
С		CHANGE STATEMENTS 5 AND 10	
С		RS(I,1) = RUPTURE TIME	00000091
С		RS(1,2)= APPLIED STRESS,PSI	00000092
С		RS(1,3) = TEST TEMPERATURE, DEGREES F	00000093
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С		PUT BLANK CARD BEHIND LAST DATA CARD	00000089
	10	READ(5+5) RS(1+1)+ RS(1+3)+ RS(1+2)	00000090
		IF(E0F.5) 900,901	00000094
	901	CONTINUE	00000095
		IF (RS(I+1)-0+) 11+12+11	00000096
	11	I = I + 1	0000097
		GO TO 10	00000098
	5	FORMAT(3F12.0)	00000099
	12	L1 = I - 1	00000100
		IF(INPUT-1)301,300,300	00000101
С		INPUT = 1 LISTING	00000102
	300	WRITE(6+414)	00000103
		WRITE(6,220)	00000104
		WRITE(6+221)	00000105
		WRITE(6,502)(TYPE(I),I=1,8)	00000106
	302	FORMAT( 10x+*DATA SET*/10x+ BA10/)	00000107
		WRITE(6,299)	00000108
	299	FORMAT(* OPTION CARD*)	00000109
		WRITE(6,303)INPUT,IOUT, TA,RA	00000110
	303	FORMAT (* INPUT= *+11/* IOUT= * +11/* TA= *+F10+0/* RA= *+F10+4/)	00000111
		WRITE(6+304)	00000112
	304	FORMAT(* CASE CONTROL CARDS*/5X+* PARAMETER CODE*+5X+	00000113
	1	1*NO. COEFFICIENTS*/)	00000114
		WRITE(6,305)(NPAM(I),LLO(I),I=1,I3)	00000115
	305	FORMAT(10X+15+15X+15)	00000116
	301	CONTINUE	00000117
С		INPUT = 2 LISTING	00000118
		IF(INPUT-2) 309,308,308	00000119
	308	WRITE(6,414)	00000120
		WRITE(6,306)	00000121
			+

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		306	FORMAT(5X,*INPUT DATA OBSERVATIONS*/ 3X.*NO.*.14X.* TIME*. 5X.	00000122
			1 *STRESS*, 5X,*TEMPERATURE*)	00000123
			WRITE(6+307)(I+RS(I+1)+RS(I+2)+RS(I+3) + I=1+L1)	00000124
		307	FORMAT(15+10x+F10+2, F8+0 + 4X+F10+C)	00000125
		309	CONTINUE	00000126
	С		START CASE LOOP (I3)	00000127
	С		13 = NUMBER OF CASES (PARAMETRIC EQUATIONS) TO BE EXAMINED	
	Ç		FOR EACH DATA SET	00000130
			DO 350 KK = 1 • 13	00000130
				00000131
				00000132
				00000133
			LAST=0	00000134
			BMSE= 1000000.	00000135
				00000136
				00000137
			1FG=0	00000138
40			L = NPAM(KK)	00000139
			IF (L-4)22,21,20	00000140
	_	20	CONTINUE	00000141
	С		RABOTNOV CONSTANTS	00000142
			C=RA	00000143
			DEL =0.1	00000144
	,		DELMIN=0.001	00000145
-			GO TO 23	00000146
	С		MANSON-HAFERD CONSTANTS	00000147
•		21	CONTINUE	00000148
			C=TA	00000149
			DEL = 1000.0	00000150
			DELMIN=10.	00000151
			GO TO 23	00000152
		22	LAST=2	00000153
		23	CONTINUE	00000154
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	57	CONTINUE		00000155
С		SELECT PARAMETRIC FORM FOR REC	GRESSION	00000156
		L=NPAM(KK)		00000157
		GO TO (61.62.63.64.65).L		00000158
	61	CALL LM(Y+RS+F+L1)		00000159
		GO TO 66		00000160
	62	CALL OSD(Y+RS+F+L1)		00000161
		GO TO 66		00000162
	63	CALL MS(Y+RS+F+L1)		00000163
		GO TO 66		00000164
	64	CALL MH( Y+RS+F+L1+C )		00000165
		GO TO 66		00000166
	65	CALL RAB (Y+RS+F+L1+C)		00000167
	66	CONTINUE		00000168
	,	SSER=0.0		00000169
С		ZERO'A+B+SUMX1 ARRAYS		00000170
		DO 473 M=1+12		00000171
		DO 473 J=1.12		00000172
		A(M,J)=0.0		00000173
		B(M+J)=0+0		00000174
	473	SUMX1 (M+J)=0+0		00000175
		DO 105 MF1+L2		00000176
		SUMX(M)=0.0		00000177
		D0105I=1+L1		00000178
	105	SUMX(M) = SUMX(M) + F(I + M)		00000179
		DO 106 M=1+L2		00000180
		DO 106 J=1+L2		00000181
		SUMP2(M+J)=0+0		00000182
		D0106I = 1 + L1		00000183
	106	SUMP2(M+J)=SUMP2(M+J)+F(I+M)*F	F(I+J)	00000184
		SUMY=0.0		00000185
		SUMY2=0.0		00000186
		D0107I=1.L1		00000187
				+

	SUMY=SUMY+Y(I)
107	SUMY2=SUMY2+Y(I)**2
	DO 108 M=1+L2
	SUMXY(M)=0.0
	D0108I=1+L1
108	$SUMXY(M)=SUMXY(M)+F(I \cdot M)*Y(I)$
	DO 109 M=1+L2
	DO 109 J=1.L2
109	SUMX1(M,J)=SUMP2(M,J)-(SUMX(M)*SUMX(J))/XN
	DO 110 M=1.L2
110	SUMX1(M+L3)=SUMXY(M)-(SUMX(M)*SUMY)/XN
	SUMX1(L3+L3)=SUMY2-(SUMY**2)/XN
	D042M=1+L3
42	$SUMX1(L3 \cdot M) = SUMX1(M \cdot L3)$
	N3=L3+1
	D0161=1.L3
	SUMX1(I+N3)=0+0
	D016M=1,L3
16	$SUMX1(I \cdot N3) = SUMX1(I \cdot N3) + SUMX1(I \cdot M)$
•	D017J=1.N3
17	A(1,J)=SUMX1(1,J)
	SUMB(1)=C.O
	DO1EJ=1+N3
	B(1+J)=A(1+J)/A(1+1)
18	$SUMB(1) = SUMB(1) + B(1 \cdot J)$
	SUMB(1) = SUMB(1) - B(1, N3)
	D0115I=2+L3
	D0115J=1.N3
	NIX=I-1
	TEMP=0.0
	D011611=1+NIX
116	TEMP=-A(I1+I)*B(I1+J)+TEMP
	A(I,J)=TEMP+SUMX1(I,J)

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115	$B(I \bullet J) = A(I \bullet J) / A(I \bullet I)$	00000221
	D029I=1.L2	00000222
29	SSR(I) = A(I + L3) + B(I + L3)	00000223
	REGSS=SUMX1(L3,L3)-A(L3,L3)	00000224
	SSER=A(L3+L3)	00000225
	CORC=REGSS/SUMX1(L3+L3)	00000226
	XN1 = L1 - L2 - 1	00000227
	XMSFR=SSER/XN1	00000228
	ZIP=XMSER	00000229
	STD=SQRT(XMSER)	00000230
	XMRSS=RFGSS/L2	0000231
	ETDSS=XMRSS/XMSER	00000232
	$TOTSUM=SUMX1 (I 3 \cdot I 3)$	0000233
c	ITERATE ON LOWEST 1-CORC FOR RABOTNOV SOLUTION	00000234
C.	TF(NPAM(KK) + FQ + 5) ZIP=1 + 0-CORC	00000235
C	LOOP AROUND ITERATION FOR L-M.O-S-D. AND M-S SOLUTIONS	00000236
C	$I = ND\Delta M (KK)$	00000237
	I = (1 - 1 - 4) = 0 = 1439	00000238
	17(1.05T+1) = 51.52.1439	00000239
<b>E</b> 1		00000240
51	CALL ITER(C +CBEST+ZIP +BMSE+IEG+ICT+ DEL+DELMIN+LIM+LAST)	00000241
	CALC ITER(C) + COES(C) = C + C + C + C + C + C + C + C + C + C	00000242
50		00000243
52		0000,0244
		00000245
		. 00000246
		00000247
1439		00000248
		00000249
		00000250
		00000251
		00000252
11-	= SUMR(x) = SUMR(x) + R(x) +	00000253
114		+

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		D0801=1+12	0000254
		D080J=1+L2	00000255
	80	$D(1 \cdot J) = SUMX1(1 \cdot J)$	<u>00000256</u>
	00	DD(1+1) = L1	00000257
		0072 M=1+L2	00000258
		I = M + 1	00000259
	72	$DD(I \bullet I) = SUMX(M)$	00000260
		D073 K=1.12	00000261
		J=K+1	00000262
	73	DD(1+J) = SUMX(K)	00000263
		D074 M=1+L2	00000264
		I ≈ M + 1	00000265
		D074 K=1+12	00000266
		J=K+1	00000267
	74	$DD(I_{\bullet}I) = D(M_{\bullet}K)$	00000268
c	сни	INGE 19 WHEN YOU REDIMENSION PROGRAM	00000269
C	011		00000270
		CALL MATINV(19.L3.DD.0.G.1.DETERM.ISCALE.IPIVOT.INDEX)	00000271
		D0811#1+1.2	00000272
	81	$F(I \cdot I) = SUMX1(I \cdot L3)$	00000273
		CALL MATINV(L9.L2.D ,1.E.1.DETERM.ISCALE.IPIVOT.INDEX)	00000274
		PAR(1) = B(1,2,1,3)	00000275
		M3=1 2	00000,276
		K3=L2	00000277
		D0113I=2+L2	00000278
		$MI \times = I - I$	00000279
		M3=M3-1	00000280
		TEMP1=0.0	00000281
		D0114I1=1+MIX	00000282
		TEMP1=-PAR(I1)*B(M3+K3)+TEMP1	00000283
	114	K3=K3~1	00000284
		PAR(I) = TEMP1 + B(K3) + B(K3)	00000285
	113	K3=L2	00000286 '
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		D047M=1.L2	00000287
	47	SUMX2(M)=SUMX(M)/XN	00000288
		SUMY3=SUMY/XN	00000289
		K4=L2	00000290
		D0216I=1+L2	00000291
		PAR1(K4)=PAR(I)	00000292
	216	K4=K4-1	00000293
		PARO=0.0	00000294
		D0217I=1+L2	00000295
	217	PARO=PARO-PAR1(1)*SUMX2(1)	00000296
		PARO=PARO+SUMY3	00000297
		N5=L1-L2-1	00000298
		XN1 = N5	00000299
		XMSER=SSER/XN1	00000300
		IF (XMSER .GT. 9.0E+100) GO TO 350	00000301
N		D049I=1+L2	00000302
9		1F(D(I,I)+LT+0+0)WRITE(6+1100)(I+D(I+1))	00000303
		IF(D(I.I).LT.0.0) NEGSB=NEGSB+1	00000304
•	С	AVOID MODE 2 DUMP ABORT CASE 3/3/76	00000305
		IF(D(I+I)+LT+ 0+0) GO TO 350	00000306
	1100	FORMAT(//+5X+****NEGATIVE SB(I)+I=*+I3+*DI=*+E20+8)	00000307
	49	SB(I)=SQRT(ABS(D(I,I) *XMSER))	00000308
		D0118I=1.L2	00000309
		T(I) = PARI(I) / SB(I)	00000310
	118	T(I) = ABS(T(I))	00000311
	C	CY(I)= SOLUTION IN REGRESSION SPACE	00000312
		D01221=1.L1	00000313
		SUMCY =00	00000314
		TEM=Q•O	00000315
		-D0123M=1+L2	00000316
	123	TEM=TEM+PAR1(M)*F(I+M)	00000317
		SUMCY ≓SUMCY+TĘM	00000318
	122	CY(I)=SUMCY +PARO	00000319
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CALL MINMAXYMIN, YMAX, YRAN, YMEAN, Y,L1)       00000321         D0 95 K=1+L1       00000323         96 X(K)=F(K,1)       00000324         CALL MINMAX(XMIN(1), XMAX(1), XRAN(1), XMEAN(1), XXL1)       00000326         95 CONTINUE       00000327         95 CONTINUE       00000326         95 CONTINUE       00000327         WRITE(6,220)       00000328         WRITE(6,221)       00000330         220 FORMAT(5x+X LAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT(5x+X ANALYSIS OF CREEP-RUPTURE DATA*)       00000333         WRITE(6,526)       00000335         502 FORMAT(7* REGRESSION VALUES*)       00000336         WRITE(6,502)(TYPE(1),IE1+8)       00000337         WRITE (6,506)/DAM(MM)       00000337         WRITE (6,507)(L1)       *,1X,8A10)       00000337         WRITE (6,506)(L2)       00000337         WRITE (6,506)(L2)       00000341         S06 FORMAT(* NO. OF INDEPENDENT VARIABLES *, 8X, 14)       00000342         S08 FORMAT(* NO. OF INDEPENDENT VARIABLES *, 8X, 14)       00000342         S08 FORMAT(* RESIDUAL DEGREES OF FREEDOM *, 8X, F4)       00000344         S09 FORMAT(* RESIDUAL DEGREES OF FREEDOM *, 8X, F4)       00000345         WRITE(6,545)(XNSER)       00	С		CALCULATE MIN. MAX. RANGE, MEAN			00000320
D0 95 1=1.L2       00000322         D0 95 K=1.L1       00000323         95 X(K)=F(K:I)       00000324         CALL MINMAX(XMIN(I), XMAX(I), XRAN(I),XMEAN(I),X.L1)       00000326         95 CONTINUE       00000326         c       PRINT REGRESSION STATISTICS       00000327         wRITE(6.414)       00000326         wRITE(6.221)       00000326         220 FORMAT( 5X.* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT( 5X.* LEAST-SQUARES REGRESSION VALUES*)       00000335         wRITE(6.526)       00000335         526 FORMAT(* A NALYSIS OF CREEP-RUPTURE DATA*)       00000336         wRITE(6.502)(TYPE(I)+I=1+8)       00000336         526 FORMAT(* DATA SET       *.1X.8A10)       00000336         526 FORMAT(* NO. OF OBSERVATIONS       *.8X.14)       00000337         wRITE(6.507)(L1)       00000338       00000339         wRITE(6.508)(L2)       00000344       00000344         507 FORMAT(* NO. OF INDEPENDENT VARIABLES       *.8X.14)       00000344         508 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X.F4)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X.F4)       00000345         504 FORMAT(* RESIDUAL MEAN SQUARE       *.E12.4)       00000347	Ť		CALL MINMAX (YMIN, YMAX, YRAN, YMEAN, Y	+L1)		00000321
D0 96 K=1,L1 0000323 96 X(K)=F(K,I) 00000324 CALL MINMAX(XMIN(I), XMAX(I), XRAN(I),XMEAN(I),X+L1) 00000325 95 CONTINUE 00000326 95 CONTINUE 00000326 WRITE(6,414) 00000327 WRITE(6,220) 00000329 WRITE(6,221) 00000330 220 FORMAT( 5X+& LAAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*) 00000331 221 FORMAT( 5X+& ANALYSIS OF CREEP-RUPTURE DATA*) 00000332 WRITE(6,526) 00000335 526 FORMAT( X REGRESSION VALUES*) 00000335 527 FORMAT( A REGRESSION VALUES*) 00000335 528 FORMAT(* DATA SET *.1X+8A10) 00000335 529 FORMAT(* DATA SET *.1X+8A10) 00000336 WRITE(6,506)PAM(MM) 00000337 WRITE(6,506)PAM(MM) 00000337 S06 FORMAT(* NO. OF OBSERVATIONS *.8X, 14) 00000340 WRITE(6,508)(L2) 0000340 WRITE(6,509)(XN1) 00000341 WRITE(6,509)(XN1) 00000341 WRITE(6,514)(FTRSS) 00000342 S08 FORMAT(* RESIDUAL DEGREES OF FREEDOM *.8X, F4) 00000343 WRITE(6,514)(FTRSS) 00000344 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,545)(MSER) 00000347 WRITE(6,547)(SER) + E12.41) 00000347 WRITE(6,547)(SER) + C12.41) 00000350 546 FORMAT(* RESIDUAL MEAN SQUARE *. E12.41) 00000347 WRITE(6,547)(SER) + C12.41) 00000351 WRITE(6,547)(SER) + C12.41) 00000351 WRITE(6,547)(SER) + C12.41) 00000352			DO 95 I=1+L2			00000322
96 X(K)=F(K,1)       00000324         CALL MINMAX(XMIN(1), XMAX(1), XRAN(1), XMEAN(1), X,L1)       00000325         95 CONTINUE       00000326         C       PRINT REGRESSION STATISTICS       00000328         WRITE(6,414)       00000328         WRITE(6,220)       00000329         WRITE(6,221)       00000330         220 FORMAT(Sx,* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT(S,* LEAST-SQUARES REGRESSION VALUES       00000333         wRITE(6,526)       00000335         502 FORMAT(/*       REGRESSION VALUES       00000335         502 FORMAT(* DATA SET       *,1X,8A10)       00000336         mm=NPAM(KK)       00000336       00000337         wRITE(6,502)(TYPE(1),1=1,8)       00000337       00000337         S06 FORMAT(* DATA SET       *,1X,8A10)       00000336         mm=NPAM(KK)       00000337       00000337         wRITE(6,506)(L2)       00000334       00000334         S06 FORMAT(* NO. OF DBSERVATIONS       *, 8X, 14)       00000340         S07 FORMAT(* NO. OF INDEPENDENT VARIABLES       *, 8X, 14)       00000342         S08 FORMAT(* NO. OF INDEPENDENT VARIABLES       *, 8X, F4)       00000343         wRITE(6,514)(FTRS)       00000345			D0 95 K=1+L1			00000323
CALL MINMAX(XMIN(1), XMAX(1), XMAN(1), XMEAN(1), X,L1)       00000325         95 CONTINUE       00000326         C       PRINT REGRESSION STATISTICS       00000327         WRITE(6,414)       00000329         WRITE(6,220)       00000330         220 FORMAT(5X:* ANALYSIS OF CREEP-RUPTURE DATA*)       00000331         221 FORMAT(5X:* ANALYSIS OF CREEP-RUPTURE DATA*)       00000332         WRITE(6,526)       00000333         526 FORMAT(*/**)       00000334         WRITE(6,502)(TYPE(1),I=1+8)       00000335         502 FORMAT(*/* DATA SET       *.1X.8A10)         MRINPAM(KK)       00000337         WRITE (6,506)PAM(MM)       00000336         504 FORMAT(* NO. OF OBSERVATIONS       *. 7X. A8)       00000334         507 FORMAT(* NO. OF INDEPENDENT VARIABLES       *. 8X. 14)       00000342         508 FORMAT(* NO. OF INDEPENDENT VARIABLES       *. 8X. 14)       00000342         509 FORMAT(* ROSIL) L2       00000345       00000345         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *. 8X. F4)       00000345         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *. 8X. F4)       00000345         514 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *. 82.41       00000345         514 FORMAT(* RESIDUAL MEAN SQUARE       *. E1		96	$X(K) = F(K \cdot I)$			000 <b>00324</b>
95 CONTINUE       00000326         C       PRINT REGRESSION STATISTICS       00000327         WRITE(6,414)       00000328         WRITE(6,220)       00000329         WRITE(6,221)       00000330         220 FORMAT( 5X:* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT( 5X:* ANALYSIS OF CREEP-RUPTURE DATA*)       00000332         WRITE(6.526)       00000333         526 FORMAT( /* REGRESSION VALUES*)       00000336         502 FORMAT(* DATA SET *.1X:8A10)       00000336         MM=NPAM(KK)       00000337         WRITE (6.502)(TYPE(1):1=1:8)       00000336         502 FORMAT(* DATA SET *.1X:8A10)       00000336         503 FORMAT(* PARAMETER SELECTED *.1X:8A10)       00000337         WRITE (6.507)(L1)       00000337         504 FORMAT(* NO: OF OBSERVATIONS *.8X, 14)       00000341         WRITE(6.508)(L2)       00000342         505 FORMAT(* NO: OF INDEPENDENT VARIABLES *.8X, 14)       00000343         WRITE(6.514)(FTRSS )       00000345         504 FORMAT(* RESIDUAL DEGREES OF FREEDOM *.8X, F4)       00000344         509 FORMAT(* F - VALUE *.F12:1)       00000345         504 FORMAT(* RESIDUAL MEAN SQUARE *.F12:4)       00000347         505 FORMAT(* RESIDUAL MEAN SQUARE *.E12			CALL MINMAX(XMIN(I) + XMAX(I) + XRAN	(I) + XMEAN(I	) • X • L 1 )	00000325
C       PRINT REGRESSION STATISTICS       00000327         WRITE(6+414)       00000328         WRITE(6+220)       00000330         220 FORMAT( 5X+* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT( 5X+* LEAST-SQUARES REGRESSION VALUES 0000332       00000332         WRITE(6+526)       00000333         526 FORMAT( /* REGRESSION VALUES*)       00000336         502 FORMAT(* DATA SET *.1X+8A10)       00000336         504 FORMAT(* DATA SET *.1X+8A10)       00000337         WRITE(6+506)FAM(MM)       00000337         505 FORMAT(* NO+ OF OBSERVATIONS *.1X+8A10)       00000339         WRITE(6+508)( L2)       00000341         507 FORMAT(* NO+ OF INDEPENDENT VARIABLES *.8X, 14)       00000342         508 FORMAT(* NO+ OF INDEPENDENT VARIABLES *.8X, 14)       00000343         WRITE(6+509)(XN1)       00000343         WRITE(6+514)( FRSS )       00000343         S08 FORMAT(* RESIDUAL DEGREES OF FREEDOM *.8X, F4)       00000344         S09 FORMAT(* RESIDUAL DEGREES OF FREEDOM *.8X, F4)       00000345         S09 FORMAT(* RESIDUAL DEGREES OF FREEDOM *.8X, F4)       00000347         WRITE(6+545)(XMSER)       00000346         S45 FORMAT(* RESIDUAL MEAN SQUARE *. F12•1)       00000347               WRITE(6+546)( STD)		95	CONTINUE			00000326
WRITE(6+414)       00000328         WRITE(6+220)       00000320         WRITE(6+221)       00000330         220 FORMAT(5X+* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT(5X+* LEAST-SQUARES REGRESSION VALUE DATA*)       00000332         WRITE(6+526)       00000333         526 FORMAT(* DATA SET       *.1X+8A10)         WRITE(6+502)(TYPE(1)+1=1+8)       00000336         502 FORMAT(* DATA SET       *.1X+8A10)         WRITE(6+502)(TYPE(1)+1=1+8)       00000337         WRITE(6+502)(TYPE(1)+1=1+8)       00000336         502 FORMAT(* DATA SET       *.1X+8A10)         WRITE(6+502)(TYPE(1)+1=1+8)       00000337         WRITE(6+502)(TYPE(1)+1=1+8)       00000338         506 FORMAT(* DATA SET       *.1X+8A10)         WRITE(6+507)(L1)       00000338         506 FORMAT(* PARAMETER SELECTED       *.7X+A8)       00000341         WRITE(6+508)(L2)       00000341         508 FORMAT(* NO+ OF INDEPENDENT VARIABLES       *.8X, 14)       00000342         508 FORMAT(* NO+ OF INDEPENDENT VARIABLES       *.8X+F4)       00000345         WRITE(6+514)(FTRSS)       00000345       00000345         WRITE(6+545)(XMSER)       00000345       00000346         545 FORMAT(* RESIDUA	с		PRINT REGRESSION STATISTICS			00000327
WRITE(6,220)       00000329         WRITE(6,221)       00000330         220 FORMAT(5x:* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT(5x:* ANALYSIS OF CREEP-RUPTURE DATA*)       00000332         WRITE(6,526)       00000333         526 FORMAT(7* REGRESSION VALUES*)       00000335         502 FORMAT(* DATA SET       *.1X:8A10)       00000336         504 FORMAT(* DATA SET       *.1X:8A10)       00000336         505 FORMAT(* PARAMETER SELECTED       *.7X: A8)       00000339         WRITE(6:507)(L1)       00000340       00000340         507 FORMAT(* NO. OF OBSERVATIONS       *.8X: 14)       00000341         WRITE(6:508)(L2)       00000341       00000342         508 FORMAT(* NO. OF INDEPENDENT VARIABLES       *.8X: 14)       00000342         508 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X: F4)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X: F4)       00000345         WRITE(6:5451)(KMSER)       00000345       00000345         S45 FORMAT(* RESIDUAL MEAN SQUARE       *. E12.4)       00000349         WRITE(6:546)(STD)       00000351       00000351         S46 FORMAT(* STANDARD ERROR       *. E12.4)       00000351         WRITE(6:547)(SSER) </td <td>Ŭ</td> <td></td> <td>WRITE(6+414)</td> <td></td> <td></td> <td>00000328</td>	Ŭ		WRITE(6+414)			00000328
WRITE(6,221)       00000330         220 FORMAT( 5x,* LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT( 5x,* ANALYSIS OF CREEP-RUPTURE DATA*)       00000332         wRITE(6,526)       00000333         526 FORMAT( /* REGRESSION VALUES*)       00000335         502 FORMAT(* DATA SET       *.1X.8A10)       00000336         mm=NPAM(KK)       00000337         wRITE(6,506)PAM(MM)       00000337         S06 FORMAT(* PARAMETER SELECTED       *.7X, A8)       00000339         wRITE(6,507)(L1)       00000341       00000342         S08 FORMAT(* NO. OF INDEPENDENT VARIABLES       *.8x, 14)       00000343         wRITE(6,509)(XN1)       00000344       00000345         S09 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8x, F4)       00000345         wRITE(6,5514)(FTRSS)       *.912.1)       00000346         S14 FORMAT(* R ESIDUAL DEGREES OF FREEDOM       *.8x, F4)       00000347         wRITE(6,545)(XMSER)       00000347       00000347         S45 FORMAT(* RESIDUAL MEAN SQUARE       *. E12.4)       00000349         wRITE(6,546)( STD)       00000350       00000351         S46 FORMAT(* STANDARD ERROR       *. E12.4)       00000351         wRITE(6,547)( SSER)       *. E12.4) <t< td=""><td></td><td></td><td>WRITE(6,220)</td><td></td><td></td><td>00000329</td></t<>			WRITE(6,220)			00000329
220 FORMAT( 5X** LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC*)       00000331         221 FORMAT( 5X** ANALYSIS OF CREEP-RUPTURE DATA*)       00000332         WRITE(6+526)       00000333         526 FORMAT( /* REGRESSION VALUES*)       00000335         502 FORMAT(* DATA SET       *+1X*8A10)         MM=NPAM(KK)       00000336         WRITE(6+502)(TYPE(1)*I=1*8)       00000337         502 FORMAT(* DATA SET       *+1X*8A10)         MM=NPAM(KK)       00000336         WRITE(6+506)PAM(MM)       00000337         506 FORMAT(* NO* OF OBSERVATIONS       *+ 7X* A8)       00000339         WRITE(6*507)(L1)       00000340         507 FORMAT(* NO* OF OBSERVATIONS       *+ 8X* 14)       00000341         WRITE(6*508)(L2)       00000343       00000343         S08 FORMAT(* NO* OF INDEPENDENT VARIABLES       *+ 8X* 14)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *+ 8X* F4)       00000345         WRITE(6*509)(XN1)       00000347       00000347         S08 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *+ 8X* F4)       00000345         S09 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *+ 8X* F4)       00000347         WRITE(6*545)(XMSER)       00000347       00000347         S45 FORMAT(* RESIDUAL MEAN			WRITE(6.221)			00000330
221       FORMAT( 5X,* ANALYSIS OF CREEP-RUPTURE DATA*)       00000332         wRITE(6,526)       00000333         526       FORMAT( /* REGRESSION VALUES*)       00000334         wRITE(6,502)(TYPE(1),II=1,8)       00000335         502       FORMAT(* DATA SET *,1X+8A10)       00000336         mm=NPAM(KK)       00000336         wRITE (6,506)PAM(MM)       00000337         sofe FORMAT(* DATA SET *,1X+8A10)       00000336         mm=NPAM(KK)       00000337         wRITE (6,506)PAM(MM)       00000338         506       FORMAT(* NO. OF OBSERVATIONS *, 8X, 14)       00000340         507       FORMAT(* NO. OF INDEPENDENT VARIABLES *, 8X, 14)       00000341         wRITE(6,509)(XN1)       00000341       00000343         swRITE(6,509)(XN1)       00000344       00000345         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM *, 8X, F4)       00000344         509       FORMAT(* F - VALUE *, F12.1)       00000345         wRITE(6,545)(XMSER)       00000347         545       FORMAT(* RESIDUAL MEAN SQUARE *, E12.4)       00000349         wRITE(6,546)( STD)       00000351         546       FORMAT(* STANDARD ERROR *, E12.4)       00000351         wRITE(6,547)( SSER)       00000351		220	FORMAT( 5X+*   FAST-SQUARES REGRESS	ION PROGRAM	FOR PARAMETRIC*)	00000331
WR ITE (6,526)       00000333         526 FORMAT( /* REGRESSION VALUES*)       00000334         WR ITE (6,502) (TYPE (1), I=1,8)       00000335         502 FORMAT(* DATA SET *.1X+8A10)       00000336         MM=NPAM(KK)       00000337         WR ITE (6,506)PAM(MM)       00000337         S06 FORMAT(* PARAMETER SELECTED *.7X+ A8)       00000339         WR ITE (6,507) ( L1)       00000340         507 FORMAT(* NO+ OF OBSERVATIONS *. 8X, I4)       00000342         S08 FORMAT(* NO+ OF INDEPENDENT VARIABLES *. 8X, I4)       00000342         S08 FORMAT(* RESIDUAL DEGREES OF FREEDOM *. 8X, F4)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM *. 8X, F4)       00000345         WR ITE (6,514) ( FTRSS )       00000347         WR ITE (6,545) (XMSER)       00000347         S45 FORMAT(* RESIDUAL MEAN SQUARE *. E12.4)       00000347         WR ITE (6,546) ( STD)       00000347         WR ITE (6,546) ( STD)       00000351         S46 FORMAT(* STANDARD ERROR *. E12.4)       00000351         WR ITE (6,547) ( SSER)       4		221	FORMAT( 5X+* ANALYSIS OF CREEP-RUP	TURE DATA*)		00000332
526       FORMAT( /* REGRESSION VALUES*)       00000334         WRITE(6,502)(TYPE(1),I=1,8)       00000335         502       FORMAT(* DATA SET *,1X,8A10)       00000336         MM=NPAM(KK)       00000337         WRITE (6,506)PAM(MM)       00000338         506       FORMAT(* PARAMETER SELECTED *, 7X, A8)       00000339         WRITE (6,507)( L1)       00000340         507       FORMAT(* NO. OF OBSERVATIONS *, 8X, 14)       00000341         WRITE(6,508)( L2)       00000342         508       FORMAT(* NO. OF INDEPENDENT VARIABLES *, 8X, 14)       00000344         S09       FORMAT(* RESIDUAL DEGREES OF FREEDOM *, 8X, F4)       00000345         WRITE(6,514)( FTRSS )       00000345       00000345         514       FORMAT(* RESIDUAL MEAN SQUARE *, F12.1)       00000347         WRITE(6,546)( STD)       00000349       00000349         545       FORMAT(* RESIDUAL MEAN SQUARE *, E12.4)       00000350         546       FORMAT(* STANDARD ERROR *, E12.4)       00000351         WRITE(6,547)( SSER)       00000351			WRITE (6.526)			00000333
WRITE(6.502)(TYPE(I))I=1.8)       00000335         502       FORMAT(* DATA SET       *.1X.8A10)       00000336         MM=NPAM(KK)       00000337       00000337         WRITE(6.506)PAM(MM)       00000338         506       FORMAT(* PARAMETER SELECTED       *.7X.AB)       00000339         WRITE(6.507)(L1)       00000340         507       FORMAT(* NO. OF OBSERVATIONS       *.8X.14)       00000342         508       FORMAT(* NO. OF INDEPENDENT VARIABLES       *.8X.14)       00000342         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X.F4)       00000345         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X.F4)       00000345         S09       FORMAT(* RESIDUAL DEGREES OF FREEDOM       *.8X.F4)       00000345         S14       FORMAT(* RESIDUAL MEAN SQUARE       *.F12.1)       00000348         S45       FORMAT(* RESIDUAL MEAN SQUARE       *.E12.4)       00000349         WRITE(6.546)( STD)       00000350       00000350         546       FORMAT(* STANDARD ERROR       *.E12.4)       00000351         WRITE(6.547)( SSER)       00000351       00000351		526	FORMAT( /* REGRESSION V	ALVES	~- <u>-</u> +* }	00000334
502       FORMAT (* DATA SET       *.1X.8A10)       00000336         MM=NPAM(KK)       00000337         WRITE (6.506)PAM(MM)       00000338         506       FORMAT (* PARAMETER SELECTED       *.7X.A8)       00000399         WRITE (6.507) (L1)       00000340         507       FORMAT (* NO.OF OBSERVATIONS       *.8X.14)       00000341         wRITE (6.508) (L2)       00000342         508       FORMAT (* NO.OF INDEPENDENT VARIABLES       *.8X.14)       00000342         508       FORMAT (* RESIDUAL DEGREES OF FREEDOM       *.8X.F4)       00000343         wRITE (6.514) (FTRSS)       00000345       00000346         514       FORMAT (* F - VALUE       *.F12.1)       00000347         wRITE (6.545) (XMSER)       00000347       00000347         545       FORMAT (* RESIDUAL MEAN SQUARE       *.E12.4)       00000349         wRITE (6.546) (STD)       00000350       546       GOMAT (* STANDARD ERROR       *.E12.4)       00000351         546       FORMAT (* STANDARD ERROR       *.E12.4)       00000351       00000351         wRITE (6.547) (SSER)       wRITE (6.547) (SSER)       *.       00000351		520	WRITE(6+502)(TYPE(1)+I=1+8)			00000335
MM=NPAM(KK)       00000337         WRITE (6.506)PAM(MM)       00000338         506 FORMAT(* PARAMETER SELECTED       *, 7x, A8)       00000339         WRITE(6.507)(L1)       00000340         507 FORMAT(* NO. OF OBSERVATIONS       *, 8x, 14)       00000341         WRITE(6.508)(L2)       00000342         508 FORMAT(* NO. OF INDEPENDENT VARIABLES       *, 8x, 14)       00000343         WRITE(6.509)(XN1)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000346         514 FORMAT(* F - VALUE       *, F12.1)       00000348         WRITE(6.545)(XMSER)       00000348       00000349         S45 FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6.546)(STD)       00000350       546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351       00000352       *		502	FORMAT (* DATA SET *	,1X,8A10)		00000336
WRITE (6,506)PAM(MM)       00000338         505       FORMAT(* PARAMETER SELECTED       *, 7x, A8)       00000339         WRITE(6,507)(L1)       00000340         507       FORMAT(* NO* OF OBSERVATIONS       *, 8x, 14)       00000341         WRITE(6,508)(L2)       00000342         508       FORMAT(* NO* OF INDEPENDENT VARIABLES       *, 8x, 14)       00000343         WRITE(6,509)(XN1)       00000344       00000345         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000345         WRITE(6,514)(FTRSS)       00000346       00000347         S14       FORMAT(* F - VALUE       *, F12+1)       00000348         WRITE(6,545)(XMSER)       00000348       00000349         S45       FORMAT(* RESIDUAL MEAN SQUARE       *, E12+4)       00000349         WRITE(6,546)(STD)       00000350       00000350         S46       FORMAT(* STANDARD ERROR       *, E12+4)       00000351         WRITE(6,547)(SSER)       00000351       00000352			MM=NPAM (KK)		·	00000337
506       FORMAT(* PARAMETER SELECTED       *, 7x, AB)       00000339         WRITE(6,507)(L1)       00000340         507       FORMAT(* NO. OF OBSERVATIONS       *, 8x, 14)       00000341         WRITE(6,508)(L2)       00000342         508       FORMAT(* NO. OF INDEPENDENT VARIABLES       *, 8x, 14)       00000343         WRITE(6,509)(XN1)       00000344         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000345         WRITE(6,514)(FTRSS)       00000346         514       FORMAT(* F - VALUE       *, F12.1)       00000347         WRITE(6,545)(XMSER)       00000348         545       FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000350         546       FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6,547)(SSER)       00000351       00000352			WRITE (6,506)PAM(MM)			00000338
WRITE(6,507)(L1)       00000340         507 FORMAT(* NO. OF OBSERVATIONS       *. 8x. 14)       00000341         WRITE(6,508)(L2)       00000342         508 FORMAT(* NO. OF INDEPENDENT VARIABLES       *. 8x. 14)       00000343         WRITE(6,509)(XN1)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *. 8x. F4)       00000345         WRITE(6,514)(FTRSS)       00000345         514 FORMAT(* F - VALUE       *. F12.1)       00000347         WRITE(6,545)(XMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       *. E12.4)       00000349         WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *. E12.4)       00000351         WRITE(6,547)(SSER)       00000352         *       ************************************		506	FORMAT (* PARAMETER SELECTED	*,	7X, A8)	00000339
507       FORMAT(* NO• OF OBSERVATIONS ** Bx, 14)       00000341         WRITE(6*508)(L2)       00000342         508       FORMAT(* NO• OF INDEPENDENT VARIABLES **, 8x, 14)       00000343         WRITE(6*509)(XN1)       00000344         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM **, 8x, F4)       00000345         WRITE(6*514)(FTRSS)       00000345         514       FORMAT(* F - VALUE ** F12*1)       00000348         545       FORMAT(* RESIDUAL MEAN SQUARE ** E12*4)       00000349         WRITE(6*546)(STD)       ** E12*4)       00000350         546       FORMAT(* STANDARD ERROR ** E12*4)       00000351         WRITE(6*547)(SSER)       00000351			WRITE(6,507)( L1)	ę		00000340
WRITE(6,508)(L2)       00000342         508 FORMAT(* NO* OF INDEPENDENT VARIABLES       *, 8x, 14)       00000343         WRITE(6,509)(xN1)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000345         WRITE(6,514)(FTRSS)       00000345         S14 FORMAT(* F - VALUE       *, F12*1)       00000347         WRITE(6,545)(xMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       *, E12*4)       00000349         WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12*4)       00000351         WRITE(6,547)(SSER)       00000352         +       *       *		507	FORMAT (* NO. OF OBSERVATIONS	*•	8x. 14)	00000341
508       FORMAT(* NO. OF INDEPENDENT VARIABLES       *, 8x, 14)       00000343         WRITE(6.509)(xN1)       00000344         509       FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000345         WRITE(6.514)(FTRSS)       00000346         514       FORMAT(* F - VALUE       *, F12.1)       00000347         WRITE(6.545)(XMSER)       00000348         545       FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6.546)(STD)       00000350       00000351         546       FORMAT(* STANDARD ERROR       *, E12.4)       00000352         WRITE(6.547)(SSER)       4       00000352       +			WRITE(6,508)( L2)			00000342
WRITE(6,509)(XN1)       00000344         509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000345         WRITE(6,514)(FTRSS)       00000346         514 FORMAT(* F - VALUE       *, F12.1)       00000347         WRITE(6,545)(XMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6,547)(SSER)       00000352         +       +       +		508	FORMAT (* NO. OF INDEPENDENT VARIA	BLES *,	8x, 14)	00000343
509 FORMAT(* RESIDUAL DEGREES OF FREEDOM       *, 8x, F4)       00000345         WRITE(6,514)(FTRSS)       00000346         514 FORMAT(* F - VALUE       *, F12.1)       00000347         WRITE(6,545)(XMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6,547)(SSER)       00000352			WRITE(6,509)(XN1)		•,	00000344
WRITE(6,514)(FTRSS)       00000346         514 FORMAT(* F - VALUE       *, F12.1)       00000347         WRITE(6,545)(XMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6,547)(SSER)       00000352		509	FORMAT (* RESIDUAL DEGREES OF FREE	DOM *,	8X, F4)	00000345
514 FORMAT(* F - VALUE       ** F12*1)       00000347         WRITE(6*545)(XMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       ** E12*4)       00000349         WRITE(6*546)( STD)       00000350         546 FORMAT(* STANDARD ERROR       ** E12*4)       00000351         WRITE(6*547)( SSER)       00000352			WRITE(6,514)(FTRSS)		•	00000346
WRITE(6,545)(XMSER)       00000348         545 FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6,547)(SSER)       00000352		514	FORMAT(* F - VALUE	*•	F12+1)	00000347
545 FORMAT(* RESIDUAL MEAN SQUARE       *, E12.4)       00000349         WRITE(6.546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6.547)(SSER)       00000352         +       +			WRITE(6,545)(XMSER)	،		00000348
WRITE(6,546)(STD)       00000350         546 FORMAT(* STANDARD ERROR       *, E12.4)       00000351         WRITE(6,547)(SSER)       00000352         +       +		545	FORMAT (* RESIDUAL MEAN SQUARE	¥.	E12+4)	00000349
546 FORMAT(* STANDARD ERROR *+ E12+4) 00000351 WRITE(6+547)( SSER) 00000352 +			WRITE(6,546)( STD)			00000350
WRITE(6,547)( SSER) 00000352 +		546	FORMAT (* STANDARD ERROR	<del>×</del> •	E12.4)	00000351
+			WRITE(6,547)( SSER)			00000352
						+

	547	FORMAT(* RESIDUAL SUM OF SQUARES	*• F12.4)	00000353
		WRITE(6, 548)(TOTSUM)		00000354
	548	FORMAT (* TOTAL SUMS OF SQUARES	*• E12•4)	00000355
		WRITE(6, 549)(CORC)		00000356
	549	FORMAT(* MULT. CORREL. COEF. SQUARED	*• F12•4/)	00000357
с		WRITE(6,320)		00000358
-	320	FORMAT(/)		00000359
		IF (MM.EQ.4) WRITE (6.432) CBEST	•	00000360
		IF (MM.EQ.5) WRITE (6.433) CBEST		00000361
	432	FORMAT (* MANSON - HAFERD CONSTANT (TA) =*.F	10+1/)	00000362
	433	FORMAT(* RABOTNOV CONSTANT (RA) =*.F10.5/)		00000363
		WRITE(6,492)(YMIN,YMAX,YRAN,YMEAN)		00000364
	492	FORMAT (5 X * MIN Y =* E11.2.3X * MAX Y =*.	E11.2,3X,* Y RANGE =*.	00000365
		E11.2.3X* MEAN Y =*.E11.2/)		00000366
С		INPUT= 3 LISTING		00000367
-		IF (INPUT-3)311,310,311		00000368
	310	WRITE(6,312)		00000369
	312	FORMAT (/ 5X. *FIRST 5 OBSERVATIONS - TRANSF	ORMED VARIABLES*/	00000370
		$15X_{*}Y_{*}18X_{*}X_{1} - X(L^{2}) *)$		00000371
		DO 313 I=1+5		00000372
		DO 315 J=1,L2		00000373
	315	TEMP(J) = F(I,J)		000 <b>0</b> 0374
		WRITE(6+314)(Y(I)+(TEMP(J)+J=1+L2))		00000375
	313	CONTINUE		00000376
	314	FORMAT(8E15.5)		00000377
		WRITE(6,320)		00000378
	311	CONTINUE		00000379
		WRITE(6,422)		0 <b>00003</b> 80
	422	FORMAT(3X,* I *,2X,*VARIABLE*, 4X,*COEF	•P(I)*•3X• *S•E•COEF•*•	00000381
		1 4X, *T*, 5X, *MEAN X(I)*, 3X,	*MIN X(I)*+ 3X+*MAX X(I	00000382
	2	2*•3X• *RAN X(I)*• 4X•*RINF*• 3X• *PSUM*• 3	X•*CERR*)	00000383
		WRITE(6,535)(PARO)		00000384
	535	FORMAT(6x,*0*,11x,E14.4)		00000385
				+

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00000386
     M = NPAM(KK) * 6 - 6
                                                                           00000387
     DO 420 I=1+L2
                                                                           00000388
     CERR(I)=100.0*((PAR1(I)-E(I))/PAR1(I))
                                                                           00000389
     RINF=(XRAN(I)*PAR1(I)+1.0E-30) /YRAN
                                                                           00000390
     SSRR=SSR(I)/REGSS
     WRITE(6+421)(I+WAR(I+M)+PAR1(I)+ SB(1)+T(I)+XMEAN(I)+
                                                                           00000391
    1 XMIN(I), XMAX(I), XRAN(I), RINF, SSRR, CERR(I))
                                                                           200000392
                                                                           00000393
 420 CONTINUE
                                                                           00000394
                  17. 4X.A8.1X. E12.4. E11.2. F7.2.
 421 FORMAT(
                                                                           00000395
             E13.3, 3E11.2, F8.2, F7.3, F7.2)
                                                  5
     1
                                                                           00000396
      WRITE(6+424)
 424 FORMAT( /* VARIABLE CODE*/10X,*S=LOG STRESS*/10X,*T=TEMPERATURE*
                                                                           00000397
                                                                           00000398
     1/10x,*DT=T-TA*/10X,*L=STRESS*/)
                                                                           00000399
      CUMERR=0.0
                                                                           00000400
      RR15=0.0
                                                                           00000401
      SRIS2=0.0
                                                                           00000402
      EMAx=0.0
                                                                           00000403
      EMAXP=0.0
                                                                           00000404
      NZERO=0
                                                                           00000405
      SDP=0.0
                                                                           00000406
      SSDP=0.0
                                                                           00000407
      DPMAX = -10.0
                                                                           00000408
       XDF=ALOG10(XN1)
      T6=0.8618559 -0.9842715*XDF+0.5849466*XDF**2-.1159365*XDF**3
                                                                           00000409
                                                                           00000410
      T6=10+**T6
                                                                           00000411
CCCC **** START 333 LOOP*****
                                                                           00000412
      D0333M=1+L1
                                                                           00000413
      X(1) = 1 \cdot 0
                                                                           00000414
      DO 92 K=1.L2
                                                                           00000415
      I = K + 1
                                                                           00000416
      X(I)=F(M+K)
  92
                                                                           00000417
      DO 100 J =1.L3
                                                                           00000418
        TEMP(J) = 0.0
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	$00,100,1,\pm1.13$	00000419
•	$TEMP(J) = TEMP(J) + X(1) * DD(1 \cdot J)$	00000420
100	CONTINUE	00000421
	ANS =0.0	00000422
	DO 200 J=1.L3	00000423
	ANS= ANS +TFMP(J)*X(J)	0000424
200	CONTINUE	00000425
	XMER = XMSER	00000426
	XMER= ABS(XMER)	00000427
	ANS = ABS(ANS)	00000428
.C	CALCULATE 95 PERCENT STATISTICAL INTERVALS	00000429
	DELTA=T6*SQRT(XMER*ANS)	00000430
	CIMAX(M)=CY(M)+DELTA	00000431
	CIMIN(M) = CY(M) - DELTA	00000432
	DELTA=T6*SQRT(XMER*(1+ANS))	00000433
	PYMAX(M)=CY(M)+DELTA	00000434
	PYMIN(M)=CY(M)-DELTA <sup>-</sup>	00000435
	RIS(M) = CY(M) - Y(M)	00000437
С	AVOID DUMP WHEN Y=0 2/25/76	00000438
	IF(Y(M)+EQ+0+0) Y(M)=0+000001	00000439
	$ERRPER(M) = RIS(M)/Y(M) \times 100$	00000440
	IF ( $ABS(RIS(M)) \bullet GT \bullet ABS(EMAX))EMAX = RIS(M)$	00000441
	RIS2 =RIS(M)**2	00000442
	SRIS2=SRIS2+RIS2	00000443
	RRIS=RRIS+ABS(RIS(M))	00000444
	$IF(ABS(ERRPER(M)) \cdot GT \cdot ABS(EMAXP)) FMAXP = FRRPER(M)$	00000445
	CUMERR=CUMERR+ABS(ERRPER(M))	00000446
333	CONTINUE	00000447
CCCC	***** END 333 LOOOP \$\$\$\$**	00000448
с	FIND OBSERVATIONS OUTSIDE OF 95 PERCENT PREDICTION INTERVAL	00000449
401	FORMAT(/* OBSERVATIONS OUTSIDE OF 95 PERCENT PREDICTION INTERVAL*	/00000450
	15x,*0BS.*, 5x,*CALC Y*, 5x,*PYMIN*, 5x,*PYMAX* /)	00000451
	IBAD=0	00000452
	•	+

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			00000050
		IF(CY(I)-PYMIN(I)) 402,399,399	00000454
	399	CONTINUE	00000455
		IF(CY(I)-PYMAX(I)) 400,400,402	00000456
	402	IBAD=IBAD+1	00000457
		IF(IBAD+EQ+1) WRITE(6+401)	00000458
		WRITE(6+403)( I+ CY(I)+PYMIN(I)+PYMAX(I) )	00000459
	400	CONTINUE	00000460
	403	FORMAT ( 15,3E16.6)	00000461
С		DETERMINE DP STATISTICS IN TERMS OF LOG TIME TO RUPTURE	00000462
-		DPSUM=0.0	00000463
		DPMAX = -100.0	00000464
		IF (NPAM(KK)-5) 404,406,404	00000465
	404	DO 405 I=1.L1	00000466
		DP=PYMAX(I)-PYMIN(I)	00000467
		IF (DP.GT.DPMAX) DPMAX=DP	00000468
		DPSUM= DPSUM+DP	00000469
	405	CONTINUE	00000470
		GO TO 408	. 00000471
с		RABOTNOV DP	00000472
-	406	DO 407 I=1+L1	00000473
С		AVOID NEGATIVE PY DUMP	00000474
-		$IF(PYMIN(I) \bullet LT \bullet 0 \bullet 0) PYMIN(I) = 1 \bullet 0$	00000475
		$IF(PYMAX(I) \bullet LT \bullet 0 \bullet 0) PYMAX(I) = 1 \bullet 0$	, 00000476
		PP1 = PYMAX(1) * * (1.0/CHEST)	00000477
		RP2=PYMIN(I)**(1,0/CBEST)	00000478
		DP = ALOG10(RP1) - ALOG10(RP2)	00000479
		IF (DP+GT+DPMAX)DPMAX=DP	00000480
		DPSUM=DPSUM+DP	00000481
	407	CONTINUE	00000482
	408	DPAVE = DPSUM/L1	00000483
			000004Ř4
		RP2=10.***DPMAX	00000485

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DO 400 I=1+L1

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WRITE(6+410)	00000486
410 FORMAT( 5X+* 95 PERCENT PREDICTION INTERVAL STATISTICS*/25X+	00000487
1*LOG TIME*,10X,*REAL TIME FACTOR (ANTILOG WIDTH)*/)	00000488
WRITE(6,409)(DPAVE, RP1, DPMAX, RP2)	00000489
409 FORMAT (* AVERAGE WIDTH *, 5x, F10.3,19x, F10.1/* MAXIMUM WIDTH*,	00000490
1 6X • F10 • 3 • 19X • F10 • 1 )	00000491
C ORDER RESIDUALS - LARGEST TO SMALLEST	00000492
L1NEG = -L1	00000493
DO 2100 1=1+L1	00000494
TEMP(I) = 0.0	00000495
2100 TEMP(I)= ABS(RIS(I))	00000496
CALL AORDER(TEMP + L1NEG, IPERM)	00000497
DO 1202 I=1.L1	00000498
J = IPERM(I)	00000499
TEMP(J) = I	00000500
1202 CONTINUE	00000501
C OUTPUT = 1 OR GREATER	00000502
C RESIDUALS IN REGRESSED SPACE	00000503
IF(IOUT -1) 413,412,412	00000504
412 CONTINUE	00000505
WRITE(6+414)	0000506
WRITE(6,415)	00000507
414 FORMAT(1H1)	00000508
415 FORMAT(* RESIDUALS - REGRESSION SPACE*/)	00000509
WRITE(6,416)	00000510
WRITE(6,417)(I,Y(I),CY(I),RIS(I),ERRPER(I), TEMP(I),	00000511
1 $CIMAX(I) \cdot CIMIN(I) \cdot PYMIN(I) \cdot PYMAX(I) \cdot I = 1 \cdot L1)$	00000512
417 FORMAT(15, 1X, 3E12.3, , F10.1, 8X, F5, 4X, 4E12.3)	00000513
416 FORMAT( 2X+*OBS*+ 7X+*Y OBS*+ 6X+*Y CALC*+5X+ *RESIDUAL*+6X+	00000514
1 *PCTERR *, 1x,*ORDER*,7X ,*CIMIN*, 7X,*CIMAX*,7X,	00000515
2 *PIMIN*,7X ·*PIMAX*/)	00000516
413 CONTINUE	00000517
XMRSS=REGSS/L2	00000518
······································	· +

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 $\frac{\omega}{5}$ 

```
00000519
      FTRSS=XMRSS/XMSER
                                                                          00000520
      DPAVE= SDP/L1
                                                                          00000521
      DPSIG=(L1*SSDP-SDP**2)/(L1*(L1-1•0))
                                                                          00000522
      DPSIG=SQRT(DPSIG)
                                                                          00000523
      STD=SQRT(XMSER)
                                                                          00000524
      PLOTTING ROUTINE
С
                                                                          00000525
      PLOT RESIDUALS WITH VARIAN ON LINE PLOTTER
С
                                                                          00000526
      IF (IOUT -3)445,440,440
                                                                          00000527
  440 CONTINUE
                                                                          00000528
      IN(1) = 5HPARAM
                                                                          00000529
      IN(2) = 4HPLOT
                                                                          00000530
      N=L1
                                                                          00000531
      ISYMD=12
                                                                          00000532
      IEC=1
                                                                          00000533
      CALL MINMAX(YL,YH,YRAN,YMEAN,RIS,L1)
                                                                          00000534
      YL=1.8*YL
                                                                          00000535
      YH=1.8*YH
                                                                          00000536
      XL=0.0
                                                                          00000537
      XH=0.0
                                                                          00000538
      NXM = 1
                                                                          00000539
      NYM = 1-
                                                                          00000540
      YNOTE= 10H RESIDUAL
                                                                          00000541
      XNOTES = 10HZP NORMAL
                                                                          00000542
      XNOTE6= 10H FITTED Y
                               .
      CALL VDIPLT(IEC, IN, N, CY(1), RIS(1), XL,XH,YL,YH,NXM,
                                                                          00000543
                                                                          00000544
     1 XNOTEG. NYM. YNOTE. ISYMD)
                                                                          00000545
      CALL AORDER(RIS+L1+IPERM)
                                                                          00000546
      DO 430 I=1.L1
                                                                          00000547
      J=IPERM(I)
                                                                          00000548
      TEMP(I) = RIS(J)
                                                                          00000549
      XI = I
                                                                          00000550
      FZ=(X1-.375)/(L1+.25)
                                                                          00000551
      IF(FZ-0.5)570.570.571
```

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5	ZP(I) = 1.04505 + 4.35979*XX + 3.46057*XX**2+ 1.90878*XX**3 1 + 0.54456*XX**4+ 0.0608*XX**5 GO TO 572 571 XX=ALOG10(1.0-FZ) ZP(I) = 1.04505 + 4.35979*XX + 3.46057*XX**2+ 1.90878*XX**3 1 + 0.54456*XX**4+ 0.0608*XX**5 ZP(I) = -ZP(I) 572 CONTINUE 530 CONTINUE	00000553 00000554 00000555 00000556 00000557 00000558 00000559
5	1 + 0.54456*XX**4+ 0.0608*XX**5 G0 T0 572 571 XX=ALOG10(1.0-FZ) ZP(I)= 1.04505 + 4.35979*XX + 3.46057*XX**2+ 1.90878*XX**3 1 + 0.54456*XX**4+ 0.0608*XX**5 ZP(I)=-ZP(I) 572 CONTINUE 530 CONTINUE	00000554 00000555 00000556 00000557 00000558 00000559
5	GO TO 572 GO TO 572 ZP(I)= 1.04505 + 4.35979*XX + 3.46057*XX**2+ 1.90878*XX**3 1 + 0.54456*XX**4+ 0.0608*XX**5 ZP(I)=-ZP(I) G72 CONTINUE G72 CONTINUE	00000555 00000556 00000557 00000558 00000559
5 4	571 XX=ALOG10(1.0-FZ) ZP(I)= 1.04505 + 4.35979*XX + 3.46057*XX**2+ 1.90878*XX**3 1 + 0.54456*XX**4+ 0.0608*XX**5 ZP(I)=-ZP(I) 572 CONTINUE 530 CONTINUE	00000556 00000557 00000558 00000559
5	<pre>ZP(I)= 1.04505 + 4.35979*XX + 3.46057*XX**2+ 1.90878*XX**3 1 + 0.54456*XX**4+ 0.0608*XX**5 ZP(I)=-ZP(I) 572 CONTINUE 50 CONTINUE 50 CONTINUE</pre>	00000557 00000558 00000559
5	1 + 0.54456*XX**4+ 0.0608*XX**5 ZP(I)=-ZP(I) 572 CONTINUE 530 CONTINUE	00000558 00000559
5	ZP(I) = -ZP(I) 572 CONTINUE 530 CONTINUE	00000559
5	572 CONTINUE	
4	130 CONTINUE	00000560
		00000561
	$YI = 0 \bullet 0$	00000562
	YH=0.0	00000563
	CALL VDIPLT(IFC, IN, N, ZP(1), TEMP(1), XL, XH, YL, YH, NXM,	0000564
	1 XNOTES, NYM, YNOTE, ISYMD)	00000565
4	45 CONTINUE	00000566
с	OUTPUT. = 2 OR GREATER	00000567
C	REAL SPACE RESIDUAL OUTPUT	0000568
37 37	BACKTRANSFORM SOLUTION AND PREDICTION INTERVALS	00000569
-	MX=NPAM (KK)	00000571
	DO 441 $M=1 + L^{1}$	00000572
	GO TO(201,201,201,201,203),MX	00000573
2	201 CY(M) = 10.0**CY(M)	00000574
	PYMAX'(M)=10.0**PYMAX(M)	00000575
-	PYMIN(M)=10.0**PYMIN(M)	00000576
	$CIMAX(M) = 10 \cdot 0 * * CIMAX(M)$	0000577
٠	CIMIN(M)=10.0**CIMIN(M)	0000578
	GO TO 205	00000579
2	203 CONTINUE	00000580
С	AVOID NEGATIVE TO A POWER DUMP	00000581
	$IF(PYMIN(M) \bullet LE \bullet 0 \bullet 0) PYMIN(M) = 1 \bullet 0$	00000582
	IF(PYMAX(M)+LE+ 0+0) PYMAX(M)=1+0	0000583
	$IF(CIMAX(M) \bullet LE \bullet 0 \bullet 0) CIMAX(M) = 1 \bullet 0$	00000584
	$IF(CIMIN(M) \bullet LE \bullet 0 \bullet 0) CIMIN(M) = 1 \bullet 0$	00000585
		+

	$IE(CY(M) \rightarrow E \rightarrow 0 \rightarrow 0) CY(M) = 1 \rightarrow 0$	00000586
	$CY(M) = CY(M) * (1 \cdot 0 / CBEST)$	00000587
	PYMAX(M) = PYMAX(M) * * (1.0/CBEST)	0000588
	$PYMIN(M) = PYMIN(M) * * (1 \cdot 0 / CBEST)$	00000589
	$CIMAX(M) = CIMAX(M) * (1 \cdot 0 / CBEST)$	00000590
	$CIMIN(M) = CIMIN(M) * * (1 \cdot 0 / CBEST)$	00000591
	205 CONTINUE	00000592
	RIS(M) = RS(M+1) - CY(M)	00000593
	$FRPPFR(M) = (RIS(M)/RS(M \cdot 1)) * 100 \cdot$	00000594
	441 CONTINUE	00000595
	C ORDER REAL SPACE RESIDUALS	00000596
	$DO 425 I=1 \cdot L1$	00000597
	TEMP(I)=0.0	00000598
	425 TEMP(I)=ABS(ERRPER(I))	00000599
	CALL AORDER (TEMP+LINEG, IPERM)	00000600
8	DO 1203 I=1+L1	00000601
	J=IPERM(1)	00000602
	TEMP(J)=I	00000603
	1203 CONTINUE	00000604
	IF(IOUT+LT+2) GO TO 350	00000605
	WRITE(6,414)	0000606
	WRITE(6,431)	0000607
	431 FORMAT (* BACKTRANSFORMED RESIDUALS - REAL SPACE*/)	00000608
	WRITE(6+416)	00000609
	WRITE(6,417)(I,RS(I,1),CY(I),RIS(I),ERRPER(I),TEMP(I),	00000610
	1 CIMIN(I), CIMAX(I), PYMIN(I), PYMAX(I), I=1,L1)	00000611
	350 CONTINUE	00000612
	GO TO 1	00000613
	900 CONTINUE	00000614
	C CALL CALPLT ROUTINE ONLY WHEN PLOTTING	00000615
	IF(IOUT •GE•3) CALL CALPLT(0,0,999)	00000616
	STCP	00000617
	END	
~	SUBROUTINE AORDER (AA+N+IPERM)	00000610
~		· <b>T</b>

	C	THIS SUBROUTINE ORDERS VALUES IN AA AND STORES ORDER IN IPERM	00000619
		IN IS NUMBER OF VALUES IN AA	00000621
		IPERM IS ORDERED WITH RESPECT TO ECCATION OF VALUES IN SA	0000000
		IPEDM(N) HAS LOCATION OF LARGEST VALUE IN AA	00000623
		IPERMIN HAS EVENTION OF EAROLOF VALUE IN SH	00000624
	C c	IF N IS NEGATIVE IPERM IS ORDERED BY EDGATION OF EAROEST TO	00000625
	C	SMALLEST VALUES IN AA	00000626
	C	ARRAY AA IS NUT CHANGED	00000627
		DIMENSION AA(I), IPERM(I)	00000628
		LOGICAL SWITCH	00000629
		NABS = IABS(N)	00000629
	100	DU 100 I=I+NADS	000000531
	100	IPERM(I) = I	00000632
	000	IF ( NADS (LI)) REFURN	00000633
	200	SWITCH = •FALSE•	00000634
		DUBUU I- ZINADS	00000000
		I = IPERM(I = 1)	00000636
39		JJ = IPERM(I)	00000637
		1F( NOLID US GO TO 400	00000000
	200	IF (AA(II) • LE • AA(55)) 60 (0 500	000000639
	300	I[EMP=IPERM(I=1)]	00000839
		IPERM(I=I) = IPERM(I)	00000640
			00000041
		SWIICH = •IRVE•	00000642
			00000643
	400	$\frac{1}{2} \left( \frac{1}{2} \left( \frac{1}{2} \right) + \frac{1}{2} \left( \frac{1}{2} \right) \right) = \left( \frac{1}{2} \right) $	000000645
	500	CUNTINUE	00000045
	000	DETUDN	00000647
•	900	RETURN	00000047
			00000648
	~	SUBROUTINE LM (1+RS+F+LI)	00000049
		CONVERTS TIMETSTRESSTAND TEMPERATURE TO FORMAT REQUIRED	00000651
	C	FUR LINEAR SULUTION OF LARSON-MILLER EXPRESSION	10000001
1			•

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		C.	SOLUTION ALLOWS FIFTH ORDER EXPANSION OF LOG STRESS	00000652
		C	Y = B0 + B1(X1) + B2(X2) B6(X6)	00000653
		С	WHERE Y = LOG(RUPTURE TIME)	00000654
		С	S = APPLIED STRESS IN PSI	COOO0655
		С	T = TEST TEMPERATURE IN DEGREES F	00000656
		С	X1 = 1/(T+460)	00000657
		С	X2 = LOG(S)/(T+460) = S/TK	00000658
		С	X3= S**2/TK	00000659
		С	X4= S**3/TK	00000660
		С	X5= S**4/TK	00000661
		С	X6= S**5/TK	00000662
		С	C.BO-B6 = CONSTANTS DETERMINED BY LINEAR LEAST SQUARES METHOD	00000663
		С	BO= OPTIMUM L-M CONSTANT (C)	00000664
	•		DIMENSION Y(200), RS(200,5), F(200,10)	00000665
			DO 10 I=1+L1	00000666
	4		Y(I) = ALOG10(RS(I+1))	00000667
	0		S = ALOG10(RS(1+2))	00000668
			T = (RS(1+3)+460+0)	00000669
			$F(I_{\bullet}I) = 1_{\bullet}O/T$	00000670
			F(I,2) = S/T	00000671
			F(1,3) = S**2/T	00000672
			F(I,4) = S**3/T	00000673
			F(1,5) = S**4/T	00000674
	•		F(I,6) = S**5/T	00000675 /
•			10 CONTINUE	00000676
			RETURN	00000677
			END	00000678
			SUBROUTINE OSD(Y,RS,F,L1)	00000679
		с	CONVERTS TIME, STRESS, AND TEMPERATURE TO FORMAT REQUIRED	00000680
		с	FOR LINEAR SOLUTION OF ORR-SHERBY-DORN EXPRESSION	00000681
		С	SOLUTION ALLOWS FIFTH ORDER EXPANSION OF. LN STRESS	00000682
		С	WHERE Y = LOG(TIME TO CREEP EVENT)	
		c	S = APPLIED STRESS IN PSI	00000684

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			0000685
	С	T = TEST TEMP IN DEGREES F	0000686
	Ċ	X1 = 1/TK	0000687
	C	X2=LN(S) = SL	0000688
	C	X3= SL**2	0000689
	С	X4= SL**3	0000690
	С	X5= SL**4	00000691
	С	X6= SL**5	00000692
	С	BO-B6= CONSTANTS, DETERMINED BY LINEAR LEAST SQUARES METHOD	0000693
	С	B1= DELH/R	00000694
	С	DELH= APPARENT ACTIVATION ENERGY	00000000
	C	R= UNIVERSAL GAS CONSTANT	0000696
		DIMENSION Y(200), RS(200,5), F(200,10)	00000697
		DO 10 I=1+L1	00000698
		Y(I) = ALOGIO(RS(I,I))	0000699
		S = ALOG10(RS(1,2))	00000700
4		T = (5 + 79 + ) * (RS(1 + 3) - 32 + ) + 273 +	00000701
сці с		F(I,1) = 1.07	00000702
		$F(1 \cdot 2) = S$	00000703
		F(1,3) = 5 * * 2	0000704
		$F(1 \cdot 4) = S \cdot * \cdot 3$	00000705
		F(1,5) = 5**4	0000706
		F(1,6) = 5**5	0000707
		10 CONTINUE	0000708
		RETURN	00000709
			00000710
	_	SUBROUTINE MS(Y)RS)F(L)	00000711
	С	CONVERTS TIME STRESS AND TEMPERATORE TO FORMAN RECOVIDED	00000712
	С	FOR LINEAR SOLUTION OF MANSON-SOCCOP EXTRESPON	00000713
	C	SOLUTION ALLOWS FIFTH ORDER EXPANSION OF EUG STREED	00000714
	С	BI = OPTIMOM M=3 CONSTRUCT(C)	00000715
		DIMENSION Y(200) RS(200) DIA T(200)	00000716
		DO I 0 I=I+LI	00000717
		Y(1) = ALUGIO(RS(1))	+

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с с с с с с с с с с	10	<pre>S= ALOG10(RS(I,2)) T= RS(I+3) F(I,1)=T F(I,2)= S F(I,3)= S**2 F(I,4)= S**3 F(I,5)= S**4 F(I,6)= S**5 CONTINUE RETURN END SUBROUTINE MH(Y+RS+F+L1+CMH) FOR NONLINEAR SOLUTION OF MANSON-HAFERD EXPRESSION CMH = TEMPERATURE OFFSET (TA)</pre>	00000718 00000720 00000721 00000723 00000723 00000724 00000725 00000725 00000726 00000727 00000728 00000729 00000730 00000731 00000732 00000733 00000735 00000735 00000736 00000737 00000738 00000739 00000740 00000740 00000742
с С		X4= DT*S**3 X5= DT*S**4	00000735
С		X6= DT*S**5	00000738
С	,	SOLUTION IS ITERATED TO FIND CMH WHICH PRODUCES BEST FIT	00000739
		DIMENSION Y(200), RS(200,5), P(200,10)	00000740
		$\frac{1}{2} \frac{1}{2} \frac{1}$	00000741
		$S = \Delta \log \log (RS(1+2))$	00000742
		DT = RS(1,3) - CMH	00000743
		F(I,I) = DT	00000744
		F(I,2) = DT*S	00000745
		F(1,3)= DT*S**2	00000746
		F(1+4)= DT*S**3	00000747
		F(I+5)= DT*S**4	00000748
		F(1+6)= DT*S**5	00000749
-	10	CONTINUE	+

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		00000751
		00000752
	SUBROUTINE ITER(C, BC,X,PBX,IFG,ICT, DEL, DELMIN, LIM,LAST)	00000753
c	ITERATES CONSTANT (C) TO MINIMIZE VALUE (X)	00000754
ĉ	BC = VALUE OF CONSTANT ASSOCIATED WITH LOWEST (BEST) X VALUE	00000755
	DEV- REST PREVIOUS VALUE OF X	00000756
ć	JEG TELAG TO CONTROL INCREASING OR DECREASING C FOR NEXT ITERAT	ION0000757
	DEC -CONTROLS SIZE OF C INCREMENT	00000758
	LOT TALLOWS O TO INCREMENT BEYOND BC BEFORE CHANGING	
	INCOMMENT SIZE. ITERATION STOPS WHEN DEL .LE. DELMIN	
C	INCREMENT SIZET FRENTION STOLD WHEN DED TEMPET	00000761
C	LIM = COURTER FOR TTERATIONS	00000762
С	LASTEEND TTERATION FLAG	00000763
_		00000764
С	INCREASING C	00000765
	5 LIM = LIM+1	00000766
С	NEXT CARD PREVENTS NEGATIVE X PROMIBEING DEDITA VALOU	00000767
		· 00000768
	IF (PBX +G1 + X) BC=C	00000769
	IF (PBX •GI• X) PBX=X	00000770
	IF (PBX •EQ• X) ICT=U	0000771
	$IF(X \circ GT \circ PBX) = ICI=ICI+I$	00000772
	IF (DEL •LE•DELMIN) GO TO 40	00000773
С	IF(ICT+LT+2) GO TO IO	00000774
	IF( ICT+LT+10) GO TO 10	00000775
	DEL = 0.3*DEL	00000776
	ICT=0	00000777
С		00000778
		00000779
		00000780
		00000781
		00000782
	GO TO SU	00000783
С	DECREASING CONSTANT	+

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	30	LIM =LIM+1	0000784
	С	NEXT CARD PREVENTS NEGATIVE X FROM BEING BEST X VALUE	00000785
		IF(X.LE. 0.0) GO TO 35	0000787
		IF(PBX •GT• X) BC=C	00000787
		IF(PBX •GT• X) PBX=X	00000788
		IF (PBX +EQ+ X) ICT=0	00000789
		IF(X •GT• PBX) ICT=ICT+1	00000790
		IF(DEL.LE.DELMIN) GO TO 40	00000791
		IF( ICT+LT+10) GO TO 35	00000792
		DEL=0.3*DEL	00000793
		ICT=0	00000794
		C=BC-5.0*DEL	00000795
		IFG=0	00000796
	35	C=C-DEL	00000797
•		GO TO 50	00000798
	40		00000799
	50	CONTINUE	00000800
4		RETURN	00000801
-+	-	END	00000802
	·e-•	SUBROUTINE RAB(Y,RS,F,L1,A)	00000803
·	c,	FOR NONLINEAR SOLUTION OF RABOTNOV EXPRESSION	00000804
	c	SOLUTION ALLOWS FIFTH ORDER EXPANSION OF TEMPERATURE FUNCTION	00000805
	č	WHERE Y= RUPTURE TIME **A	0000806
	Č.	T= TEST TEMPERATURE IN DEGREES F	00000807
-	č	$x_1 = 1/ST$	00000808
	č	A= ITERATED CONSTANT	00000809
<u>,</u>	Č	S= STRESS IN PSI	00000810
	Ŭ	DIMENSION Y(200), RS(200,5), F(200,10)	00000811
			00000812
		$Y(1) = (RS(1 \cdot 1)) * * A$	00000813
		$S = RS(1 \cdot 2)$	00000814
		$T = RS(1 \cdot 3)$	00000815
		F(1,1) = 1,0/(S*T)	00000816
			+

		00000817
	$F(1,3) = 1 \cdot ((S*T**3))$	00000818
	$F(1, 0) = 1 \cdot ((S + T + 2 \cdot 0))$	00000819
		0000820
		00000821
		00000822
10		00000823
	REIURN	00000824
		0000825
	SUBROUTINE MINMAX (CMIN, CMAX, CRAIN, CMEAN, CONT,	00000826
	CALCULATES MINIMUM, MAXIMUM, RANGE, AND MEAN OF COTT	0000827
	WHERE N= NUMBER OF OBSERVATIONS	00000828
	DIMENSION C(I)	00000829
	CMAX=-1.0E+100	00000830
	CMIN=1+0E+100	00000831
	CSUM=0.0	00000832
	DO 5. I=1•N	00000833
	CSUM=CSUM+C(I)	0000033
	, IF( C(I)-CMIN) 2.3.3	00000834
. 2	2 CMIN=C(I)	00000835
	3 IF( C(I)-CMAX)5+5+4	00000836
4	4 CMAX=C(I)	00000837
4	5 CONTINUE ···	0000838
	CMEAN=CSUM/N	00000839
	CRAN=CMAX-CMIN	00000840
	7 CONTINUE	00000841
	RETURN <sup>1</sup> - 1	00000842
	END	00000843
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# APPENDIX B LANGLEY RESEARCH CENTER SYSTEM SUBROUTINES

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SUBROUTINE MATINV

LANGUAGE :	FORTRAN	· •
PURPOSE:	To invert a re equation AX = and by an opti	al square matrix A, solve the matrix B, where B is a matrix of constant vectors, on evaluate the determinant.
USE:	CALL MATINV(MA	X,N,A,M,B,IOP,DETERM,ISCALE,IPIVOT,IWK)
	MAX	An input integer specifying the maximum order of A as stated in the dimension statement of the calling program.
	N	An input integer specifying the order of A; $l \leq N \leq MAX$ .
	A	An input/output two-dimensional array of the coefficients. On return to the calling program, $A^{-1}$ is stored in A. A must be dimensioned in the calling program with first dimension MAX and second dimension at least N. The original A matrix is destroyed.
	М	An input integer specifying the number of column vectors in B. $M = 0$ signals that the subroutine is used solely for inversion; however, in the call statement an entry

corresponding to B must be present.

An input/output two-dimensional array of the constant vectors. On return to the calling program, the solution X is stored in B. B should have its first dimension MAX and its second dimension at least M. The original B matrix is destroyed.

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ISCALE

IOP Compute the determinant option. IOP = 0, Compute the determinant. IOP = 1, Do not compute the determinant.

DETERM For IOP = 0, in conjunction with ISCALE, represents the value of the determinant of • A as follows:

DET(A) = (DETERM)10<sup>100</sup>(ISCALE)

For IOP=1, the determinant is set to 1. The determinant is set to zero for a singular matrix, for both IOP = 0 or 1 option. Upon return from MATINV, DETERM should be tested or written out in the calling program.

(See Other Coding Information)

For IOP = 0, the scale factor is computed by the subroutine to avoid overflow or underflow in the computation of the quantity, DETERM. For IOP = 1, ISCALE may be a dummy argument.

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IPIVÓT ,

A one-dimensional array used by the subprogram to store pivotal information. It should be dimensioned at least N. In general the user does not need to make use of this array.

IWK

An integer array of temporary storage, dimensioned at least 2 x N.

METHOD: Jordan's method is used to reduce a matrix A to the identity matrix I through a succession of elementary transformations:  $l_n, l_{n-1}, \dots, l_1$ . A = I. If these transformations are simultaneously applied to I and to a matrix B of constant vectors, the results are  $A^{-1}$  and X where AX = B. Each transformation is selected so that the largest element is used in the pivotal position.

ACCURACY: Total pivotal strategy is used to minimize the rounding errors; however, the accuracy of the final results depends upon how well-conditioned the original matrix is. A return with DETERM  $\neq$  0 does not guarantee accuracy in the solutions or inverse.

REFERENCE: Fox, L., An Introduction to Numerical Linear Algebra. Oxford University Press, New York, 1965.

STORAGE: 516<sub>8</sub> locations

## SUBROUTINE DDIPLT

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LANGUAGE:	FORTRAN	
PURPOSE:	To provide routine wa the DD80 p to use on <u>be used on</u> plays shou	a one-call method of preparing plotting. This s originally designed for recording plots on lotter only; however, it has been redesigned any plotter. This one-call routine should not any new jobs; new jobs requiring one-call dis- ld use INFOPLT.
	These disp figures.	lays will not meet specifications for final
USE:	CALL DDIPI	T(IEC, IN, N, XDATA, YDATA, XMIN, XMAX, YMIN, YMAX, NXM, XM, NYM, YM, ISYMD)
	where	is the code for terminating the frame
	•	0 frame incomplete 1 frame complete with this data. The frame change is built in and the plotter will be spaced for the next frame.
	IN	is a two-word array. Each word contains 10 Hollerith characters for plot identification.
	N;	is the number of points to be plotted.
	XDATA	is the name of the array containing the floating point values of X to be plotted.
	YDATA	is the name of the array containing the floating point values of Y to be plotted.
	XMIN	is the minimum value for X.
	XMAX	is the maximum value for X.
	YMIN	is the minimum value for Y.

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YMAX is the maximum for Y.

The routine checks for the first call only to determine if either (XMAX-XMIN) or (YMAX-YMIN) is equal to zero. When either is zero, the routine will scan the X and/or Y array to determine the limits. For multiple curves per display, the limits must be specified on the first call to include all curves since the limits from the first call will be used for all curves.

If any data falls outside the limits, it will be eliminated; but a count will be kept of all points dropped and written at top of the plot.

Minimum/maximum values are next checked to see that the range is not zero. When it is, the specified values are adjusted by 10 percent of the minimum or set equal to ±1.0 in cases where minimum and maximum are equal to zero.

NXM	is the number of central memory words in the
	message for the horizontal annotation. Maxi-
	mum number of words is 13; each word contains
	10 characters. If NXM and NYM are both neg-
	ative, tic marks will be generated instead of
	grid.

- XM is the name of array containing the label for the horizontal annotation.
- NYM is the number of words in the message for the vertical annotation. Maximum number of words is 13.
- YM 'is the name of array containing the label for the vertical annotation.
- ISYMD is the integer code specifying the symbol or mode to be used for plotting the data values.

ŀ	Circle	0	8	Fan	Q
2	Square	Õ	9	Long diamond	$\diamond$
3	Diamond	$\diamond$	10	House	$\triangle$
4	Triangle	Δ	11	Circled dot	$\odot$
5	Right Triangle	$\nabla$	1.2	Х	
6	Quadrant	Δ	13	Dot	
7	Dog House	$\square$	14	Vectors	

RESTRICTIONS:	The following arrays must be spe	cified in	a DIMENSIC	N
	statement of the calling program	1: IN(2),	XDATA(N),	YDATA(N),
	XM(NXM), YM(NYM).			

Each curve on a display requires a separate entry to the routine. X and Y coordinates for plotting must be in separate arrays of single precision, floating point data. Frame control is specified by the IEC code in the calling sequence for the routine.

METHOD: Data are scaled and plotted; axes are drawn and annotated, and grid lines or tic marks are generated.

> Minimum/maximum values are adjusted to provide a range when all values of an array are equal. Adjustment is also made where needed to improve the appearance of the plot.

ACCURACY: Approximately three significant figures may be read in either direction.

REFERENCES:

STORAGE: 3021<sub>A</sub> locations

SUBPROGRAMS USED: CALPLT, NOTATE, NUMBER, PNTPLT, NFRAME

OTHER CODING A call to PSEUDO (1.4.1) must precede the first call INFORMATION: A call to PSEUDO (1.4.1) must precede the first call to DDIPLT. An entry called VDIPLT with the same parameters as DDIPLT is available which packs 8 6" x 6" plots per frame for the Varian postprocessor.

#### SUBROUTINE PSEUDO

#### LANGUAGE: COMPASS

PURPOSE: To create and write an appropriately named Plot Vector File. Through linkages set up by an initial call to PSEUDO, all subsequent graphics data generated by the user will be routed through one of the PSEUDO entry points and written on the Plot Vector File. The PSEUDO processor is designed for use with the frame dependent postprocessors described in Section 1.3, Volume IV, of the Computer Programing Manual.

use:

### CALL PSEUDO

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or

CALL PSEUDO(FN)

file name left-justified with zero fill. Default file name is SAVPLT.

Example:

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### CALL PSEUDO

This will establish a Plot Vector File named SAVPLT.

CALL PSEUDO(6LMYFILE)

This will establish a Plot Vector File named MYFILE.

- NOTE: The Plot Vector File (or Files) will usually be written to disk (as opposed to tape) and may be postprocessed following user program termination via appropriate specification of one or more PLOT control cards (see Section 1.3, Volume IV, Computer Programing Manual).
- RESTRICTIONS: (1) An initializing call to PSEUDO (with or without a file name argument) must be made prior to any calls to CALPLT or any other graphics output routine.

- (2) Every Plot Vector File should be terminated with a 999 pen code, CALL CALPLT(0.0,0.0,999). The transmission of the 999 code will cause an EOF write on the Plot Vector File, and the file will temporarily be closed. Thus, any given Plot Vector File will contain only one 999 pen code and/or one EOF.
- (3) To continue plotting execution following transmission of a 999 code to a current Plot Vector File, the user program must call the PSEUDO processor to create new Plot Vector File (i.e., CALL PSEUDO(6LMYFIL2)).

METHOD: In addition to entry PSEUDO, this processor contains two other entry points, namely PLT9999 and PLT9998. An initializing call to PSEUDO will set PLT9999 into the processor switching mechanism (PLOTSW). Subsequent plot data generation will then be routed via CALPLT, PLOTSW, and PLT9999 and written on the Plot Vector File. The entry PLT9998 is used to record special purpose data from routines NFRAME and PLTSTOP.

ACCURACY:

REFERENCES: See Section 1.3, Volume IV, Computer Programing Manual.

STORAGE: 2155<sub>8</sub> locations total for direct subprograms

SUBPROGRAMS USED: NUMARG, PLOTSW

### APPENDIX C

## DEVELOPMENT OF PARAMETRIC MODEL EQUATIONS

This appendix presents the development of the parametric model equations used in the computer program PARAM. The Larson-Miller, Orr-Sherby-Dorn, Manson-Succop, and Manson-Haferd expressions are familiar time-temperature parameters. These parameters assume that the value of the parameter (a function of stress) is a constant for each value of the temperature compensated time parameter. The Rabotnov parameter (refs. 9 and 10) is a time-stress parameter which assumes that the value of the parameter (a function of temperature) is a constant for each value of the time compensated stress parameter. Time to a given creep event and a polynomial in the parameter function (stress or temperature) were respectively the dependent and independent variables all regression model equation forms used in PARAM. The following presents the development of these five equation forms:

Larson-Miller Parameter

 $P = T_{R} (\log t + C) = f (\sigma)$   $T_{R}(\log t + C) = b_{1} + b_{2} \log \sigma + b_{3}(\log \sigma)^{2} + b_{4}(\log \sigma)^{3} + b_{5}(\log \sigma)^{4} + b_{6}(\log \sigma)^{5}$ assuming  $b_{o} = -C$  $\log t = b_{o} + b_{1}/T_{R} + b_{2} \log \sigma/T_{R} + b_{3} (\log \sigma)^{2}/T_{R} + b_{4} (\log \sigma)^{3}/T_{R} + b_{5} (\log \sigma)^{4}/T_{R} + b_{6} (\log \sigma)^{5}/T_{R}$ 

where P = the Larson-Miller parameter  $T_{R} = temperature, ^{O}R$ t = time to a particular creep event C = Larson-Miller constant  $\sigma$  = applied stress  $b_0 - - b_6 = coefficients$  estimated by method of least squares. Orr-Sherby-Dorn Parameter  $P = t \exp(-\Delta H/RT_{K}) = g(\sigma)$  $\log t - K (\Delta H/RT_K) = f (\log \sigma)$ assuming  $b_1 = K\Delta H/R$  $\log t = b_0 + b_1/T_K + b_2 \log \sigma + b_3 (\log \sigma)^2 + b_4 (\log \sigma)^3$  $+ b_5 (\log \sigma)^4 + b_6 (\log \sigma)^5$ where P = Orr-Sherby-Dorn parameter t = time to a particular creep event  $\Delta H$  = apparent activation energy R = universal gas constant  $T_{K}$  = temperature, Kelvin  $\sigma$  = applied stress  $b_0 - b_6 = coefficients$  estimated by method of least squares. Manson-Succop Parameter  $P = \log t + CT_F = f(\sigma)$  $\log t = -C T_F + f (\sigma)$ assuming  $b_1 = -C$ 

$$\begin{split} \log t &= b_0 + b_1 T_F + b_2 \log \sigma + b_3 (\log \sigma)^2 + b_4 (\log \sigma)^3 \\ &+ b_5 (\log \sigma)^4 + b_6 (\log \sigma)^5 \end{split}$$
 where P = Manson-Succop parameter  
t = time to a particular creep event  
C = Manson-Succop constant  
T\_F = temperature, <sup>O</sup>F  
 $\sigma$  = applied stress  
 $b_0 - b_6$  = coefficients estimated by method of  
least squares.

## Manson-Haferd Parameter

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$$\begin{split} P &= (\log t - \log t_{a})/(T_{F} - T_{A}) = f(\sigma) \\ \log t &= \log t_{a} + (T_{F} - T_{A}) f(\sigma) \\ \text{assuming } b_{o} &= \log t_{a} \\ D &= T_{F} - T_{A} \\ \log t &= b_{o} + b_{1}D + b_{2} D \log \sigma + b_{3} D (\log \sigma)^{2} \\ &+ b_{4} D (\log \sigma)^{3} + b_{5} D (\log \sigma)^{4} + b_{6} D (\log \sigma)^{5} \\ \text{where } P &= \text{Manson-Haferd parameter} \\ t &= time to a particular creep event \\ t_{a} &= offset time \\ T_{F} temperature, ^{O}F \\ T_{A} &= offset temperature, ^{O}F \\ \sigma &= applied stress \\ b_{o} &= b_{6} &= coefficients estimated by method of \\ &= least squares which iteratively searched values \\ &= of T_{A} to determine best fit. \end{split}$$

Rabotnov Parameter

$$\begin{split} \mathbf{P} &= \sigma(\mathbf{1} + \mathbf{A}\mathbf{t}^{\alpha}) = \mathbf{f}(\mathbf{T}) \\ \mathbf{t}^{\alpha} &= -\mathbf{1}/\mathbf{A} + \mathbf{1}/\mathbf{A}\sigma \ [\mathbf{C}_{\mathbf{1}} + \mathbf{C}_{2}/\mathbf{T} + \mathbf{C}_{3}/\mathbf{T}^{2} + \mathbf{C}_{4}/\mathbf{T}^{3} + \mathbf{C}_{5}/\mathbf{T}^{4} \\ &+ \mathbf{C}_{5}/\mathbf{T}^{5} + \mathbf{C}_{6}/\mathbf{T}^{6}] \\ \text{assuming } \mathbf{b}_{0} &= -\mathbf{1}/\mathbf{A} \\ &\mathbf{b}_{\mathbf{i}} &= \mathbf{C}_{\mathbf{i}}/\mathbf{A} \\ \mathbf{t}^{\alpha} &= \mathbf{b}_{0} + \mathbf{b}_{\mathbf{1}}/\sigma\mathbf{T} + \mathbf{b}_{2}/\sigma\mathbf{T}^{2} + \mathbf{b}_{3}/\sigma\mathbf{T}^{3} + \mathbf{b}_{4}/\sigma\mathbf{T}^{4} + \mathbf{b}_{5}/\sigma\mathbf{T}^{5} \\ &+ \mathbf{b}_{6}/\sigma\mathbf{T}^{6} \\ \text{where } \mathbf{P} &= \text{Rabotnov parameter} \\ \sigma &= \text{applied stress} \\ \mathbf{A}, \alpha &= \text{constants} \\ \mathbf{t} &= \text{time to a particular creep event} \\ \mathbf{T} &= \text{temperature, } ^{O}\mathbf{F} \\ \mathbf{b}_{0} - \mathbf{b}_{6} &= \text{coefficients estimated by method of least} \\ &= \text{squares which iteratively searched values of } \alpha \\ &= \text{to determine best fit.} \end{split}$$

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  - York, Nov. 1969.

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2	4	•			-	
3	4					
. 4	4					
5	3					
	g	316	s st		SS S	STEEL
3142	.90	1	175.	00		25.00
74	.60	12	200.	00		30.00
213	•00	. 12	200•	.00		28.00
656	•20	12	200+	00		25.00
3476	•10	12	200•	00		22.00
6825	•30	12	200•	00		20.00
10076	•50	12	200•	00		18.50
15790	<b>.</b> 80	12	200•	00		17.00
290	•90	12	225•	00		25.00
186	•50	12	250•	00		25.00
81	.50	12	275•	00		25.00
36	• 50	1.	300• 200	00		23.00
104	• 10	1.		00		20.00
220	• 20	1-	300.	00		19.00
200	.00	1.	300	00		18.00
377	•50 <sup>/</sup>	13	300	.00		17.00
753	.70	1	300.	00		16.00
785	.30	1.5	300.	00		16.50
1232	•50	1	300-	00		15.00
185,4	•60	10	300.	00		13.60
2421	•00	13	300•	00		13.00
4078	•30	13	30 <b>0</b> •	00		12.00
6258	•10	13	300.	00		11:00
- 21	50ء	2 13	325.	00		25.00
· · 9	•90	13	350.	00		25.00
2	•70	14	100.	00		25+00
. 83	.30	14	10 <b>0</b> •	00		15.00
· 251	•20	14	100.	00		12.00
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רי ה	-00 -00	1.4	50 <b>0</b> •	00		16.40
ر ۵۵	•60 <sup>°</sup>	· 19	500	00		12.50
87	90	1 1	500	00		10.00
170	40	- 14	500	oð.		9.00
614	.90	19	500	00		7.00
28	• 70	1	ō50.	00		10.00

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Figure 1.-Input data for Case 1.

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ΟΔΤΔ	SFT		ALLOY 9	316 STAINLESS STEEL
OPT I ON	CARD		,	•
INPUT=	1			•
IOUT=	0			
TA=	-5000			
R A=	•2000			
CASE C	ONTROL CARDS			
Р	ARAMETER CODE	NO. C	COEFFICIENTS	
	1		4	•
	2		4	
•	3		4	
	4		4	
	5		3	

Figure 2.-Output for Case 1.

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LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ----- REGRESSION VALUES \_\_\_\_ ALLOY DATA SET 9 316 STAINLESS STEEL PARAMETER SELECTED L-M NO. OF OBSERVATIONS 38 NO. OF INDEPENDENT VARIABLES 3 RESIDUAL DEGRE S OF FREEDOM 34 F - VALUE 476.8 RESIDUAL MEAN SQUARE 2.1495E-02 1.4661E-01 STANDARD ERROR 7.30836-01 RESIDUAL SSUM OF SQUARES 3.1476E+01 TOTAL SUN'S OF SQUARES .9768 MULT. CORREL. COEF. SQUARED 4.20E+00 MEAN Y = 2.45E+00 MIN Y = 4.31F-01 MAX Y = Y RANGE = 3.775+00 CERR MIN X(1) MAX X(I) RAN XELL RINE PSUM COEF.P(I) S.E.COEF. Ŧ MEAN X(1) VARIABLE Ŧ -1.8792E+01 0 6.12E-04 1.145-04 1.44 .335 .00 4.988-04 1/T 4.7642E+04 2.98E+03 16.00 5-613E-04 1 -.46 4.315-04 8-905-04 4.596-04 .663 .00 6.9295-04 S/T -3.7957E+03 4.14E+03 .92 2 9.50E-04 -.83 .003 -.00 1.31E-03 8.6898-04 3.64E-04 3 S\*\*2/T -3.29796+03 1.69E+03 1.95 VARIABLE CODE S=LOG STRESS T=TEMPERATURE DT=T-TA L=STRESS 95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) LOG TIME AVERAGE WIDTH .621 4.2 MAXIMUM WIDTH .741 5.5

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Figure 2.-Continued.

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LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ALLOY. 9 316 STAINLESS, STEEL ALLOY. 9 DATA SET . . 0-S-D ~ • • PARAMETER SELECTED -- 38 ND. OF OBSERVATIONS .- -~ 3 NO. OF INDEPENDENT VARIABLES RESIDUAL DEGREES OF FREEDOM F - VALUE + 34 \*\*\***3**\*\*, \*\* \* 575.9 -1.7867E-02 RESIDUAL MEAN SQUARE STANDARD ERROR 4~ ' 1.3367E-01 °6.0748E-01 RESIDUAL SUM OF SQUARES . Al-3.1476E+01 TOTAL SUMS OF SQUARES. ۰ د .9807 MULT. CORREL. COEF. SQUARED - 1 2.45E+00 MEAN Y = Y RANGE = 3.77E+00 4.205+00 HAX Y = MIN Y = + 4.31-01 • . RINF. PSUM CERR RAN X(I) MAX X(I) MEAN X(1) MIN X(I) COEF-P(I) - S.E.COEF. т VARIABLE 1 \_\_\_1.5630E+01 --+00 .333 . . 1.15 Ð 2.06E-04 1.10E-03 8.965-,04 5.27F+02 1.0116-03 40.07 2:1117E+04 1/T .00 1 . •25 .658 6.32E-01 1.48E+00 8.455-01 1.2288+00 2+02F+00 .75 1.5077E+00 2. 36E-01 S . ' -1.30 .009 .00 2 2+18E+00 1.47E+00 7.14E-01 1.5336+00 3.99 -3.3333E+00 3 S\*\*2 VAPIABLE CODE S=LOG STRESS T=TEMPERATURE DT=T-TA ' L=STRESS 95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) UHIGINAL PAGE IS OF POOR QUALITY LOG TIME 3.7 .567 AVERAGE WIDTH 3.9 .593 MAXIMUM WIDTH

Figure 2.-Continued.

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LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC
DATA SET REGRESSION VALUES
PARAMETER SELECTED M-S
NO. OF OBSERVATIONS 38
NO. OF INDEPENDENT VARIABLES 3
RESIDUAL DEGREES OF FREEDOM 34
KESIDAL MEAN SQUARE J. 7326E-01
AFSTDUAL SUM OF SQUARES 1.0206E+00
TOTAL SUMS OF SQUARES 3.1476 E+01
NULT. CORREL. COEF. SQUARED .9676
MIN Y = 4.31E-01 MAX Y = 4.20E+00 Y RANGE = 3.77E+00 MEAN Y = 2.45E+00
I VARIABLE COEF.P(I) S.E.COEF. T MEAN X(I) MIN X(I) MAX X(I) RAN X(I) RINF PSUM CER
0 2.2556E+01 
1
3 S**2 -2.3794E+00 1.09E+00 2.19 1.533E+00 7.14E-01 2.18E+00 1.47E+0093 .0050
VARIABLE CODE S=LOG STRESS T=TEMP" RATURE DT=T-TA L=STRESS
95 PERCENT PREDICTION INTERVAL STATISTICS Log time real time factor (antilog width)
AVERAGE WIDTH .735 5.4 MAXIMUM WIDTH .771 5.9

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Figure 2.-Continued.

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## LEAST-SQUAPES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA

----- REGRESSION VALUES ------316 STAINLESS STEEL ALL OY 9 DATA SET M-H PARAMETER SELECTED 38 ND. OF OBSERVATIONS NO. OF INDEPENDENT VARIABLES 3 34 RESIDUAL DEGREES OF FREEDOM 419.8 F - VALUE RESIDUAL MEAN SQUARE 2.4334E-02 STANDARD ERROR 1.5599E-01 8.2737E-01 RESIDUAL SUM OF SQUARES 3.1476E+01 TOTAL SUMS OF SQUARES MULT. CORREL. COEF. SQUARED +9737

.805

MANSON - HAFERE CONSTANT(TA) = 302.0

2.45E+00 3.77E+00 MEAN Y = Y RANGE = MINY = 4.31E-01MAX Y = 4-20E+00 . CERR RAN X(I) RINF PSUM MEAN X(I) MIN X(I) MAX X(I) S.E.COEF. COEF.P(I) Т VARIABLE I 1.4509E+01 0 8.75E+02 1.01E+03 3.75E+02 -1.06 .328 -.00 1.25E+03 -1.0686E-02 8+48 1.028E+03 DT. 1.26E-03 ł .68 •651 -.00 1.54E+03 5.24E+02 2.15E-03 1.251E+03 DT\*S 4-8648E-03 2.26 2 .021 -1.59 -.00 2.15E+03 1.29E+03 8.57E+02 9.028-04 5.13 1.548E+03 DT\*S\*\*2 -4.6243E-03 3

VAPIABLE CODE

MAXIMUM WIDTH

S=LOG STRESS T=TEMPERATURE DT=T-TA L=STRESS

95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) LOG TIME .661 4.6 AVERAGE WIDTH 6.4

Figure 2.-Continued.

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LEAST-SQUARES REGRESSION PRCGRAN FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA • ----- REGRESSION VALUES -----ALL OY 9 **316 STAINLESS STEEL** DATA SET PARAMETER SELECTED RAB 38 ND. OF OBSERVATIONS 2 NO. OF INDEPENDENT VARIABLES RESIDUAL DEGREES OF FREEDOM 35 . 220.4 F - VALUE RESIDUAL MEAN SQUARE STANDARD ERROR 2.1137E-03 . 4.59758-02 RESIDUAL SUM OF SQUARES 7.39796-02 1.0058E+00 TOTAL SUMS OF SQUARES MULT. CORREL. COEF. SQUARED •9264 RABOTNOV CONSTANT (RA) = .05630 1.72E+00 Y RANGE = 6.66E-01 MEAN Y = 1.38E+00 MAX Y = MIN Y = 1.06E+00CERR RAN X(I) RINF PSUM MAX X(I) COEF.P(I) S-E-COEF. MEAN X(I) MIN X(I) 1 VARIABLE Т 8.7594E-01 Э -3.74 0.00 2.06E+03 17.94 4.693E-05 2.78E-05 9.52E-05 6.758-05 +092 -3.6886E+04 1 1/L\*T 2.046-08 6.356-08 4.31E-08 4.13 .908 0.00 3.505E-08 3.19E+06 20.01 2 1/1\*T\*\*2 6.3869E+07 VAP TABLE CODE S=LOG STRESS T=TEMPERATURE DT=T-TA L=STRESS 95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIMÉ FACTOR (ANTILOG WIDTH) LOG TIME 12.3 AVERAGE WIDTH 1.088 22.4 MAXIMUM WIDTH 1.350

URIGINAL PAGE IS OF POOR QUALITY

Figure 2.-Concluded.

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ALLOY	9	316 STAIN	ESS STEEL	
3142	90	1175.00	25.00	
74.	60	1200.00	30.00	
213	00	1200.00	28.00	-
656	20	1200.00	25.00	
3476.	10	1200.00	22.00	
6825	30	1200.00	20.00	
10076.	50	1200.00	18.50	
15790.	80	1200.00	17.00	
290.	,90	1225.00	25.00	
186.	50	1250.00	25.00	
81.	50	1275.00	25.00	
36.	50	1300+00	25.00	
104•	10	1300.00	22.00	
228.	20	1300.00	20.00	
258.	10	1300.00	19.00	
319.	00	1300.00	18.00	
377.	50	1300+00	17.00	
753	70	1300.00	16.00	
785	,30	1300.00	16.50	
1232.	,50	1300+00	15.00	
1854.	60	1300.00	13.60	
2421.	00	1300.00	13.00	
4078	,30	1300+00	12.00	
6258.	.10	1300.00	11.00	
21.	50	1325+00	25.00	
9. 2	70	1350.00	25.00	
2 • 8 2 •	30	1400.00	25.00	
261	20	1400-00	12.50	
201 e	00	1400+00	10.00	
27.	90	1450.00	15.00	
75.	20	1450.00	12.50	
10. 5-	00	1500+00	16+40	
40	60	1500.00	12.50	
87.	90	1500.00	10.00	
170.	40	1500.00	9.00	
614-	90	1500+00	7.00	
28.	70	1550.00	10.00	

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Figure 3.-Input data for Case 2.

LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ----- REGRESSION VALUES -----316 STAINLESS STEFL ALLOY 9 DATA SET 0-S-D PARAMETER SELECTED . -38 NO. OF OBSERVATIONS 2 NO. OF INDEPENDENT VARIABLES 35 RESIDUAL DEGREES OF FREEDOM 600.Í F - VALUÉ 2.54816-02 PESIDUAL MEAN SQUARE . " 1.5963E-01 STANDARD ERROR 8.9183E-01 RESIDUAL SUM OF SQUARES 3.1476E+01 TOTAL SUMS OF SQUARES .9717 MULT. CORREL. COEF. SQUARED 4.20E+00 . Y RANGE = 3.77E+00 MEAN Y = 2.45E+00 MIN Y = 4.31E-01MAX Y = MIN X(I) MAX X(I) RAN X(I) RINF PSUM CERR MÉAN'X(I) S.E.COEF. ٠T VARIABLE COEF.P(I) I -1.1091E+01 Э, 0.00 .336 8.96E-04 1.10E-03 8.45E-01 1.48E+00 2.06E-04 1.16 1.011E-03 6.26E+02 34.09 2.1335E+04 1 1/1 -1-10 .664 -00 6.32E-01 2.316-01 28.22 1.228E+00 -6.5279E+00 2 S . VAFTABLE CODE S=LOG STRFSS T=TEMPFRATURE DT=T-TA . L=STRESS 95 PERCENT PPEDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) LOG TIME 4.7 •66B AVERAGE WIDTH 5.0 MAXIMUM WIDTH .703

Figure 4.-Continued.

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LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ----- REGRESSION VALUES -----316 STAINLESS STEPL ALLOY 9 DATA SET 0-5-0 - PARAMETER SELECTED . NO. OF OBSERVATIONS 38 NO. OF INDEPENDENT VARIABLES 3 34 RESIDUAL DEGRERS OF FREEDOM 575.9 F - VALUE 1,78678-02 PESIDUAL MEAN SQUARE 1.3367E-01 STANDARD ERROR RESIDUAL SUM OF SQUARES 6.0748E-01 TOTAL SUMS DE SQUARES 3.1476E+01 - MULT. CORREL. COFF. SQUARED .9807 MEAN Y = 2.45E+00Y RANGE = 3.77E+00 MAX Y = 4.20E+00MTN Y = 4.31E-01 PSUM GERR MIN X(I) MAX X(I) RAN X(I) RINF S.E.COEF. Ť MEAN X(I) VAR LABLE COEF.P(I) 1 -1.5630E+01 - 0 1.15 .333 -.00 1.10E-03 2.06E-04 1.0119-03 8.965-04 1/T 2.1117E+04 5.278+02 40.07 1 +00 6.328-01 .25 .658 1.48E+00 8.458-01 2.028+00 .75 1.22BE+00 1.5077E+00 S 2 .009 +00 2.18É+00 -1.30 1.5339+00 7.14E-01 1.47E+00 8.36F-01 3.99 -3.3333E+00 3 S\*\*2 VAPIABLE CODE S=LOG STRESS T=TEMPERATURE DT=T-TA L=STRFSS 95 PERCENT PREDICTION INTERVAL STATISTICS RÉAL TIME FACTOR (ANTILOG WIDTH) LOG TIME 3.7 .567 AVERAGE WIDTH 3.9 . .593 MAXIMUM WIDTH

Figure 4.-Continued.

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LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ----- REGRESSION VALUES ------316 STAINLESS STEEL ALLOY 9 DATA SET PARAMETER SELECTED 0-8-0 NO. OF OBSERVATIONS 38 NO. OF INDEPENDENT VARIABLES 4 33 RESIDUAL DEGREES OF FREEDOM 580.4 F - VALUE RESIDUAL MEAN SQUARE 1.3367E-02 1.1562F+01 STANDARD ERROR RESIDUAL SUM OF SQUARES 4.4113F-01 3.1476E+01 TOTAL SUMS OF SQUARES . .9860 MULT. CORREL. COEF. SQUARED 2.45 2+00 Y RANGE = 3.77E+00 MEAN Y = 4-205+00 MIN Y = 4.31E-01 MAX Y = RINE PSUM CERR MIN X(I) MAX X(I) RAN X(1) MEAN X(1) VARIABLE COEF.P(I) S.F.COEF. Т I 6.7051E+00 0 .331 2.065-04 1.14 .00 45.87 1.011E-03 8.965-04 1.10E-03 4.57E+02 1/T 2.0982E+04 1 6.32E-01 -.00 8.455-01 1.48E+00 -9.60 .654 3.42 1-228E+00 1.67E+01 2 S '-5.7228E+01 7.14E-01 2.185+00 1-47E+00 18.58 .009 -.00 1.533E+00 1.45E+01 3.29 4.7687E+01 3 S\*\*2 -.00 3.225+00 2.62E+00 -10.13 .005 6.048-01 -1.4563E+01 4.13F+00 3.53 1.942E+00 4 S\*\*3 VARIABLE CODE S=LOG STRESS T=TEMPERATURE DT=T-TA L=STRESS 95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) LOG TIME 3.1 AVERAGE WIDTH .496 3.7 MAXIMUM WIDTH .569

OF POOR QUALITY

Figure 4.-Continued.

LEAST-SQUARFS REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ----- REGRESSION VALUES ------316 STAINLESS STEEL ALLOY 9 DATA SET . Ŋ−S−D PARAMETER SELECTED ~ -38 NO. OF OBSERVATIONS • 5 NO. OF INDEPENDENT VARIABLES RESIDUAL DEGREES OF FREEDOM . 32 **بر**م 594.8 F - VALUE 1.0472E-02 RESIDUAL MEAN SQUARE . . 1.0233E-01 STANDARD ERROR 3.3509E-01 RESIDUAL SUM OF SQUARES 3.1476E+01 TOTAL SUMS OF SQUARES - .9894 MULT. CORREL. COEF. SQUARED MEAN Y = 2.45E+00 MIN Y = 4.31E-01 MAX Y = 4.20E+00 Y RANGE = 3.77E+00 MEAN X(I) MIN X(I) MAX X(I) RAN X(I) CERR RINE PSUM VARIABLE COEF.P(I) S.E.COEF. T Ť -1.0736E+02 O. 2.06E-04 1.15 .330 -.00 8.965-04 1.105-03 4.09E+02 51.77 1.0116-03 17T 2.11615+04 1 .652 -.00 8.45E-01 1.48E+00 6.326-01 58.47 1.2285+00 1.286+02 2.72 3-4852E+02 2 S -.00 2.18E+00 1.47E+00 -190.05 +009 7.14E-01 2.89 1.533E+00 1.69F+02 S\*\*2 -4.8780E+02 3 2.625+00 205.77 .005 -.00 6.045-01 3.22E+00 1.9425+00 9.76E+01 3.03 2.95926+02 4 S\*#3 4.255+00 -75.36 .003 **~.**00 2.492E+00 5.108-01 4.76E+00 2.10E+01 3.18 -6.6787E+01 5 S\*\*4 ٠ VARIABLE CODE S=LOG STRESS T=TEMPERATURE DT=T-TA L=STRFSS 95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) LOG TIME 2.8 .444 AVERAGE WIDTH 3.6 MAXIMUM HIDTH .560

Figure 4.-Continued.

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OF POOR QUALITY LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA ----- REGRESSION VALUES -----316 STAINLESS STEEL DATA SET 9 ALLOY 0-S-D PARAMETER SELECTED 38 NO. OF OBSERVATIONS NO. OF INDEPENDENT VARIABLES 6 PESIDUAL DEGREES OF FREEDOM 31 484.8 F - VALUE 1.0708E-02 PESIDUAL MEAN SQUARE 1.0348E-01 STANDARD FRRDR 3.31946-01 PESIDUAL SUM OF SQUARES TOTAL SUMS OF SQUAPES 3.1476E+01 MULT. CORRTL. COEF. SQUARED .9895 MEAN Y = 2.45E+00 Y RANGE 👳 3.77E+00 4.205+00 MAX Y = MIN Y = 4.315-01 CERR MAX X(1) RAN X(I) RINE PSUM S.E.COEF. MEAN X([) MIN X(I) T VARIABLE COEF.P(I) T 4.7690E+01 ٦ .330 .00 2.068-04 1.16 1.10E-03 4-15E+02 51.03 1.011E-03 8.96E-04 2.11815+04 1 :/T 6.32E-01 -56.65 .652 .01 1.48E+00 1.2285+00 8.45E-01 1-27E+03 .27 ~3.3766E+02 2 S 1.47E+00 278.50 .009 +00 1.533E+00 7.148-01 2.18E+00 7.1482F+02 2.22E+03 .32 S\*\*2 3 .005 .00 ( 04E-01 3.22E+00 2.62E+00 -520.10 1.9426+00 -7.47985+02 1.93E+03 .39 4 S\*\*3 4.25E+00 431.24 .003 .00 2.4926+00 5.10E-01 4.76E+00 8.28E+02 •46 5 S\*\*4 3.82185+02 .000 .00 4.31E-01 7.03E+00 6.60E+00 -134.18 .54 3.2352+00 -7.6572E+01 1.41E+02 6 S\*\*5 VAPIABLE CODE S=LOG STRESS T=TEMPFRATURE DT=T-TA L=STRESS 95 PERCENT PREDICTION INTERVAL STATISTICS REAL TIME FACTOR (ANTILOG WIDTH) LOG TIME 2.8 AVEPAGE WIDTH .454 .590 3.9 MAXIMUM WIDTH

Figure 4.-Concluded.

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3	з	-5000.0	0.2	1
2	6			
ALL	OY S	9 316 STA	INLESS STE	EL
31	42.90	1175+0	0 25	• 00
	74.60	1200•0	0 30	• 00
2	13.00	1200.0	0 28	• 00
6	56.20	1200+0	0 25	•00
34	76.10	1200+0	22	•00
68	25.30	1200+0	10 20	•00
100	76.50	1200+0		• 50
15/	90.80	1200.0		•00
2	90.90	1225+0	25	•00
1	86.50	1250+0	0 25	•00
	81.50	1275•0	25	•00
. <b>.</b>	36.50	1300+0	0 25	•00
1		1300+0		•00
2		1300+0		•00
2	28.10	1300+0		•00
3	19.00 77.50	1300+0	10 17	•00
		1300+0	10 16	•00
7		1300+0		•50
12	32.50	1300-0	10 10 10' 15	•00
18	52.50	1300+0	10 13	•60
24	21.00	1300+0	i 13	• 00
40	78.30	1300.0	10 12	•00
62	58.10	1300•0	0 11	•00
	21.50	1325.0	0 25	.00
	9.90	1350+0	0 25	•00
	2.70	1400.0	0 25	•00
	83.30	1400+0	0 15	•00
2	51.20	1400+0	0 12	•50
9	21.00	1400+0	10 10	•00
	27.90	1450.0	0 15	•00
	75.20	1450.0	12 00	• 50
	5.00	1500•0	10 16	•40
	40.60	1500+0	0 12	•50
1	87.90	1500+0	10	•00
1	70.40	1500•0	9	•00
6	14.90	1500•0	0 7	•00
:	28,70	1550.0	0 10	•00

Figure 5.-Input data for Case 3.

## LEAST-SQUARES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA 316 STAINLESS STEEL ALLOY 9 DATA SET OPTION CARD INPUT= 3 10UT = 3 TA= -5000 **-**2000 R A= CASE CONTROL CARDS PARAMETER CODE NO. COEFFICIENTS

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Figure 6.-Output for Case 3.

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INPUT	DATA	OBSERVATIONS		
NO.		TIME	STRESS	TEMPERATURE
1		3142.90	25	1175
2		74.60	30	1200
3		213.00	28	1200
4		656.20	25	1200
5		3476.10	22	1200
6		6825.30	20	1200
7		10076.50	18	1200
8		15790.80	17	1200
9		290.90	25	1225
10		186.50	25	1250
11		81.50	25	1275
12		36.50	25	1300
13		104.10	22	1300
14		228.20	20	1300
15		258.10	19	1300
16		319.00	18	1300
17		377.50	17	1300
18-		753.70	16	1300
19		785.30	16	1300
20		1232.50	15	1300
21		1854.60	14	1300
22		2421.00	13	1300
23		4078.30	12	1300
24		6258.10	11	1300
25		21,50	25	1325
26		9,90	25	1350
27		2.70	25	1400
28		83.30	15	1400
29		251.20	13	1400
30		921.00	10	1400
31		27.90	15	1450
32		75.20	13	1450
· <b>3</b> 3		5.00	16	1500
34		40.60	13	1500
35		87.90	10	1500
36		170.40	9	1500
37		614.90	7	1500
38.		28.70	10	1550

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Figure 6.-Continued.

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LFAST-SQUAPES REGRESSION PROGRAM FOR PARAMETRIC ANALYSIS OF CREEP-RUPTURE DATA

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DATA SE PARAMETI NO. OF ND. OF RESIDUA F - VALI REŞIDUA STANDARI SESIDUA TATAL S MULT. C	- REGR T SELE OBSERVA INDEPEN L DEGRE L H=AN D ERROR L SUM UMS OF ORREL-	FSSION VALUES ALL TIONS DENT VARIABLES ES OF FREEDOM SQUARE OF SQUARES SOUARES COEF. SQUARED	 GY 9 316 0-5 1.0472E- 1.0233E- 3.3509E- 3.1476E- .99	STAIN -D 38 5 -2 -32 -02 -01 -01 -01 -01 -01 -01 -01 -01	LESS STEEL						
MIN	Υ =	4.315-01 MAX Y	= . 4.20F+0	Y 00	RANGE = 3	.77E+00 ME	AN Y = 2	•45E+00			
FIRS Y 3.497 1.872 2.328 2.817 3.541	T 5 NBS 337+00 74:+00 385+00 045+00 09-+00	FRVATIONS - TRANS X1 - X(L 1.101325-03 1.08473E-03 1.38473E-03 1.08473E-03 1.98473E-03 1.98473E-03	FOR MED VAR 12 1.39794E+00 1.47712E+00 1.44716E+00 1.39794E+00 1.34242E+00	ABLES 1. 2. 2. 1. 1. 1. 1.	95424 <b>6+00</b> 181896+00 094276+00 954246+00 802106+00	2.7319LE+00 3.2229LE+00 3.03073E+00 2.7319LE+00 2.41918E+00	3.81904 4.76063 4.38595 3.81904 3.24756	E+00 E+00 E+00 E+00 E+00			
I	VARIA	BLE COEF.P(I)	S.E.COEF.	۲	MEAN X(I)	MIN X(I)	MAX XEED	RAN XEI I	RINF	PSUM	CERR
0		-1.0736E+02	6 005402	E1 77	1 0115-03	8 965-04	1.305-03	2 - 06E÷04	1.15	-330	00
1	1/1	2-11616+04	4.096+02	21.11	1 2205400	0.455-01	1 495+00	6.325-01	58.47	-652	00
2	S	3-4852-+02	1-205+02	2+16	1 5225400	7.145-01	2.185+00	1-47E+00	-190-05	-009	00
د	5442	~4+8780E+02	1.075+02	2.07	1 0425+00	6.04E-01	3.22E+00	2+62E+00	205.77	-005	00
4	6**C A**2	2+9594=+02	2.105+01	3.18	2.4925+00	5.108-01	4.76E+00	4.25E+00	-75.36	.003	00
VAPIABLE	CODE S=LOG T=TEMF DT=T-1 L=STRE	STRESS PERATURE IA ESS	TATIST	ICS							
40	FERGEN	LOG TIME	R	EAL TIM	E FACTOR (AN	TILOG WIDTH)					

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AVERAGE WIDTH	•444	2.8
MAXIMUM WIDTH	.560	3.6

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Figure 6.-Continued.

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SESIDUALS - REGRESSION SPACE

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'n۲	Y OBS	Y CALC	RESIDUAL	PCTERR	ORDER	CIMIN	CIMAX	PIMIN	PIMAX
,	3 4075+00	3 3665+00	-7.3126-01		2	3.334E+00	3.199F+00	3.0468+00	3.486E+00
. 1	1.8735+00	1.879F+00	6.4058-03	.3	32	2.024E+00	1.735E+00	1.625E+00	2.133E+00
5	2 2295+00	2 2215400	2.6875-03	-1	36	2+426E+00	2.236E+00	2.102E+00	2.561E+00
,	2.020-100	2.0165.00	0 7005-02	3.5	11	2.975E+00	2.855E+00	2.6976+00	3.1338+00
4	2.5415400	3.4025+00	-1.391E-01	-3.9	6	3.467E+00	3.3378+00	3.183E+00	3.621E+00
ż	3 9345400	3 6885+00	-1.462E-01	-3.8	5	3.758E+00	3.6185+00	3.468E+00	3.908E+00
7	4 0035+00	3.8925+00	-1.109F-01	-2.8	7	3.965E+00	3.820E+00	3.6712+00	4.114E+00
8	4 1985+00	4.098E+00	-1.004E-01	-2.4	LÓ	4.173E+00	4.0235+00	3.876E+00	4.320E+00
c c	2.464E+00	2.5745+00	1-106E-01	4.5	8	2.6305+00	2.518E+00	2.358E+00	2.791E+00
۰ <u>،</u>	2.2712+00	2.2445+00	- 2. 704E-02	-1.2	23	2.298E+00	2.189E+00	2.028E+00	2.460E+00
11	1.9115+00	1.922F+00	1-130E-02	.6	30	1_978F+00	1,8675+00	1.706E+00	2.139E+00
12	1 5625+00	1.6105+00	4.811E-02	3.1	18	1.670E+00	1.5510+00	1.393E+30	1.828E+00
12	2.317E+00	2.0975+00	7.9909-02	4.0	13	2.1556+00	2.040F+00	1.8815+00	2.314E+00
14	2.3585+00	2.383E+00	2.501E-02	1.1	26	2.440E+00	2.326F+00	2-167E+00	2.6005+00
15	2.4125+00	2.5205+00	1-082E-01	4.5	9	2.5758+00	2.465E+00	2-304E+00	2.736E+00
16	2.5045+00	2-656F+00	1.5195-01	6.1	4	2+708E+00	2.603E+00	2.440E+00	2.8715+00
17	2.5775+00	2-7935+00	2.1655-01	8.4	3	2.844E+00	2.743E+00	2.578E+00	3.0098+00
18	2-8775+00	2-9375+00	5-943E-02	2.1	15	2.9876+00	2.887E+00	2.722E+00	3.1528+00
10	2.895=+00	2.8645+00	~ 3- 0935-02	-1.1	21	2.914E+00	2.814E+00	2.6496+00	3.079E+00
21	3,0915+10	3.0895+00	-1.443E-03	0	37	3.142E+00	3.037E+00	2.874E+00	3.305E+00
21	3,2685+00	3.328E+00	5.9575-02	1.8	14	3,.388E+00	3.268E+00	3.110E+00	3.545E+00
22	3.384E+00	3.4425+00	5.778E-02	1.7	16	3.506E+00	3.377E+00	3.223E+00	3.661E+00
22	3.6105+00	3.651=+00	4.073E-02	1.1	19	3.724E+00	3.578E+00	3.430E+00	3.873E+00
22	3.7966+00	3.8885+00	9-1955-02	2.4	12	3.971E+00	3.8066+00	3.664E+00	4-113E+00
2=	1.3325+00	1.3075+00	-2.534E-02	-1.9	25	1.372E+00	1.242E+00	1.088E+00	1.526E+00
26	9.956F-01	1.012F+00	1.6545-02	1.7	28	1.084E+00	9.4005-01	7.910E-01	1.233E+00
27	4-314=-01	4.461E-01	1.475E-02	3.4	29	· 5.344E-01	3.578E-01	2.192E-01	6.730E-01
2.4	1.9215+00	1,9255+00	4.402E-03	•2	33	1.981E+00	1.869E+00	1.709E+30	2.141E+00
20	2-400F+00	2.379E+00	-2.108E-02	9	27	2.437E+00	2.321E+00	2.162E+00	2.596E+00
30	2.964F+00	2.990F+00	2.6115-02	.9	24	3.062E+00	2.919E+00	2.7705+00	3.211E+00
31	1.446F+00	1.3895+00	-5.697E-02	-3.9	17	1.457E+00	1.320E+00	1.169E+00	1.609E+00
32	1.876 +00	1.8435+00	-3.369E-02	-1.8	20	1.907E+00	1.778E+00	1.624E+00	2.061E+00
33	6.990E-01	6.687E-01	- 3.0285-02	-4.3	22	7.6028-01	5.7728-01	4.405E-31	8.969E-01
- 4	1.609F+00	1.333E+00	-2.750F-01	-17.1	1	1.408E+00	1.259E+00	1.111E+00	1.5562+00
25	1.9445+00	1.945E+00	9.2715-04	•0	38	2.018E+00	1.872E+00	1.723E+00	2.166E+00
34	2.2317+00	2.235 +00	3.8316-03	.2	34	2.319E+00	2.152E+00	2.010E+00	2.460E+00
ŝ,	2.789-+00	2.7805+00	-8.500E-03	~.3	31	2.966E+00	2.594E+00	2.500E+00	3.0602+00
38	1.458 +00	1.461E+00	3.328E-03	• 2	35	1.543E+00	1.380E+00	1.237E+00	L.686E+00

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Figure 6.-Continued.

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PCTERF 79S Y 085 Y CALC RESIDUAL ORDER. CIMEN CIMAX P IMIN PIMAX L 3.143F+03 1.846=+03 1+297F+03 41.3 4 L-580E+03 2.156E+03 1.1138+03 3.061E+03 ž 7.460\*+01 7.5716+01 -1-108E+00 -1+5 32 5+4282+01 1.056E+02 4.217E+01 1.359E+02 2.1305+02 2.143 +02 -1.322E+00 -.6 1.7235+02 36 2-665E+02 1.264E+02 3.635E+02 -25.3 5 6.562F+02 8-2235+02 7-1558+02 9.451E+02 -1+661=+02 4.982E+02 1.357E+03 3-476F+03 8 2.174E+03 2+5235+03 9-5275+02 2.928E+03 1.525E+03 4.176E+03 6.825F+^3 28.6 4.875-+03 1.951F+03 6 4.153E+03 5.7225+03 2.935E+03 8.0965+03 L.008F+04 7.8065+03 22.5 6-GI1E+03 2.2705+03 11 9.218E+03 4.691E+03 1.2998+04 . я. īž 1+053E+04 1.5795+04 1+2535+04 3.258 +03 20.6 1.4915+04 7.513E+33 2.091E+04 ç 2.909=+02 3.753=+02 -8.4385+01 -29.0 5 3.300E+02 4.268E+02 2.280E+02 6.1765+02 1.8655+02 1.752E+02 1.1265+01 6.0 24 ·1.547E+02 1.986E+02 1.066E+02 10 2.881E+02 -2.6 -11.7 11 8.1505+01 8.365E+01 30 9.508E+01 5.083E+01 -2-1495+00 7.359E+01 1.376E+02 3-5565+01 1-096E+02 3.650F+01 12 4.078E+01 ~4.2762+00 18 4.676E+01 2.4728+01 6.726E+01 1.4285+02 1.041=+~2 13 1.251E+02 -2.103E+01 -20.2 13 7.595E+01 2.0615+02 -5.9 14 2.282=+02 2.4175+02 -1.3535+01 25 2.121E+02 2.755E+02 1.468E+02 3-9815+02 3.311E+02 7 2.917E+02 4.009E+02 15 2.5815+92 -7+304E+01 -28.3 2.J13E+02 3.759E+02 5.447E+02 3.190F+02 4.526E+02 -1.336E+02 -41.9 14 5.1092+02 3 2.755E+02 7.435E+02 6.982E+02 9.699E+02 17 3.775-+02 6.2155+02 -2.4405+02 -64.6 5-532E+02 3.7875+02 1.0205+03 ~1.1055+02 7.701E+02 7.5375+32 8.642=+92 -14.7 18 15 5.268E+02 1.418E+03 1 . 7.853=+02 7.3135+02 5.399E+01 6.9 21 6.517E+02 8.207E+02 4.458E+J2 1+2005+03 2-1.2325+33 1,228#+03 4.0875+00 • 3 37 1:089E+03 1.385E+03 7.479E+02 2.018E+03 1.8555+03 2.127F+03 -14+7 21 -2.7275+02 14 1.852E+03 2-443E+03 1.289E+03 3.510E+03 2.421=+03 -14-2 -9-8 2-383E+03 3-210E+03 22 2.7665+03 -3.445F+02 16 1.671E+03 4.577E+03 4.479=+03 -4.010E+02 23 4.0785+03 19 3.7848+03 5.302E+03 2.6905+03 7-459E+03 24 6.258=+33 7.7345+03 -1.4765+03 -23.6 10 6.399E+03 9.347E+03 4.610E+03 1+2976+04 5.7 ~3.9 2 = 2.150 +01 1.745E+01 8.709E+00 2.028=+01 1.219E+00 26 28 2.357E+01 1.225E+01 3.358E+01 1.214E+01 <sup>~</sup>6 9.900 +00 1.028=+01 -3.842--01 6.180E+00 1.7116+01 2.279E+00 7.397E+01 27 2.700 +00 2.793=+00 -9.325E-02 -3.5 29 3.423E+00 1.656E+00 4.710=+00 33 27 8.330=+01 8.415 +01 -1.0 9-572E+01 28 -8,4875-01 5.113E+01 1.3855+02 29 2.512-+-2 2+3935+)2 1.1900+01 4.7 2.094E+02 2.734E+02 1.452E+02 3-9435+02 23 17 9.210=+02 9.781-+02 -5.7078+01 -6-2 30 8.302E+02 1.152E+03 5.882E+02 1.626E+03 12-3 31 2.790=+71 2,4475+91 3.4305+00 2.089F+01 2.866E+01 1.474E+01 4.061E+01 7.520"+01 5.9595+01 5.614E+00 7.5 20 22 6.0045+01 8.064E+01 1.151E+02 32 4.206E+01 33 5.000=+00 3-777E+00 4.663E+00 3.367E-01 6.7 5.757E+00 2.757E+00 7.8875+00 1.813E+01 7.442E+01 4.060=+01 46.9 2 2.1555+01 1.905E+01 34 2.561E+01 1.2928+01 3-5945+01 35 8.790=+31 8.8095+01 -1.8785-01 -.2 38 1.043E+02 5.2906+01 1.467E+02 ~.9 36 1.794-+32 1.7195+02 -1.5105+00 34 1.418E+02 2.083E+02 1.0248+02 2.887E+02 1.9 -.8 37 6.149=+02 6.0305+02 1.1925+01 31 3.9282+02 9-257E+02 3.165E+02 1.149E+03 38 2.870F+01 2.8929+01 -2.2088-01 2.398E+01 35 3.488E+01 1.725E+01 4.848E+01

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BACKTRANSFORMED RESIDUALS - REAL SPACE

Figure 6.-Continued.





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Figure 6.-Concluded.