# NASATECHNICAL MEMORANDUM 

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## EFFECT OF GYRO VERTICALITY ERROR ON <br> LATERAL AUTOLAND TRACKING PERFORMANCE FOR AN INERTIALLY SMOOTHED CONTROL LAW

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# EFFECT OF GYRO VERTICALITY ERROR ON 

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## SUMMARY

This report presents the results of a simulation study performed to determine the effects of gyro verticalıty error on the simulated lateral autoland tracking and landing performance of a small twin-jet short-haul commercial transport. A vertical gyro error model was used to generate the roll attitude signal which was used with the inertially smoothed control law in a small perturbation simulation. The influence of initial angular gyro tilt errors ( $2^{\circ}, 3^{\circ}, 4^{\circ}$, and $5^{\circ}$ ) introduced prıor to localizer capture for a $1.05^{\circ}$ per mınute gyro erection rate was investigated. These errors were used to simulate deviations which may occur in the attitude sensor as a result of the cumulative effects of maneuverinduced spin-axis misalinement and drift. Results showed that for a $5^{\circ}$ initial tilt error, the lateral "ON COURSE" autoland control logic was not satisfied and thereby localizer beam path integration was precluded and unacceptable beam standoff at touchdown occurred.

## INTRODUCTTION

Throughout the evolution of automatic landing systems for alrcraft, it became apparent to designers that landing decision heights could be decreased by means of increased navigation data accuracy. The current impetus toward reduced cıvil alrcraft landing minima has sharply brought into focus the demand for such noise-free highly accurate navigation information in the form of vehicle attitude, position, velocity, and acceleration. The introduction of the mıcrowave landing system (MLS) promises to provide accurate position data. Because of this system, the potential exists for obtaining accurate estimates of position, velocity, and acceleration information for guldance and control by processing MLS data with relatively low-cost onboard sensors such as bodymounted accelerometers and standard attitude gyros. If this potential can be achieved, acceptable automatic landing performance may be attained by using the MLS and low-cost onboard sensors in lieu of high-cost inertial platforms. However, because of new flight technıques for approach to landing which may consist of much terminal area maneuvering, a general concern has arisen as to the effects of maneuver-induced errors of conventional sensors on automatic control systems.

Although it is true that inertial systems have fulfilled the data accuracy requirements, expensive purchasing and maintenance costs are discouraging to alroraft operators to say the least. Thus, a simulation study was undertaken
to investigate the lateral performance of an inertially smoothed control law by using a conventional vertical gyro which simulated maneuver-induced tilt errors. It was assumed in this study that other guidance data such as lateral position, velocity, and acceleration information were accurately obtained. In other words, no error models were incorporated for these data in the simulation.

The purpose of this paper is to present the results of a study showing the influence of simulated maneuver-induced gyro verticality error on the lateral tracking performance of an automatic landing system of a small twin-jet shorthaul commercial transport (fig. 1). Reference 1 provides detalled information on this control law. This class of error occurs in attitude gyros subjected to low-frequency oscillations associated with preapproach maneuvering during curved or decelerating approaches. In particular, tests were directed toward determining the effects of various initial gyro tilt errors ( $2^{\circ}, 3^{\circ}, 4^{\circ}$, and $5^{\circ}$ ) for a vertical gyro erecting at $1.05^{\circ}$ per minute. This erection rate is typical of many of the present-day comercially available vertical gyros. Particular attention was devoted to the lateral tracking performance while on a short 8334 m ( $4.5 \mathrm{n} . \mathrm{mi}$.$) approach. The tilt errors and erection rate were simulated$ by the use of a first-order vertical gyro error model.

## SYMBOLS

Values are presented in both SI and U.S. Customary Units. Calculations were made in U.S. Customary Unıts.

| c | local level acceleration, g units |
| :---: | :---: |
| g | acceleration constant due to gravity, m/sec ${ }^{2}$ ( $\mathrm{ft} / \mathrm{sec}^{2}$ ) |
| h | altıtude, m (ft) |
| $\mathrm{h}_{\mathrm{R}}$ | radio altıtude, m (ft) |
| $\mathrm{K}_{\mathrm{n}}$ | filter gain |
| $\mathrm{K}_{\psi_{\mathrm{G}}}$ | gain on ground heading through transient-force gain changer |
| s | Laplace transform |
| V | total airspeed, m/sec ( $\mathrm{ft} / \mathrm{sec}$ ) |
| $\mathrm{V}_{\mathrm{G}}$ | total groundspeed, $\mathrm{m} / \mathrm{sec}(\mathrm{ft} / \mathrm{sec}$ ) |
| $\mathrm{X}, \mathrm{Y}$ | X - and y -coordinates in X and Y Earth axes, m (ft) |
| $\dot{\mathrm{Y}}$ | cross-track velocity, m/sec (ft/sec) |
| $\beta$ | glideslope error, deg |
| $\delta_{a}$ | aileron position, deg |



Dots (•) over symbols indicate differentiation with respect to the independent varlable time.

A caret (^) over a symbol denotes output of minımum value discriminator.

## SIMULATION PROGRAM

A block diagram of the simulation program is shown in figure 2 and consists of the inertially smoothed control laws and servo dynamics into which thrust, aileron, and elevator commands were input. Linear aircraft equations of motion in perturbed state form were written in order to determine vehicle position, velocity, acceleration, and attitude information. These equations were written to form the vehicle model used in the flight critical control laws to compute errors from the desired flight. This study was conducted by use of a digital simulation of a small twin-jet research aırcraft whose systems are described in references 2 and 3. The trajectory for this study was a $61.73 \mathrm{~m} / \mathrm{sec}$ ( $120-\mathrm{knot}$ ), $3^{\circ}$ descent to touchdown. Based on these deviations from this trajectory, control commands were introduced to the respective servos of the vehicle control system. Utilızation of roll attitude feedback was made after being corrupted by the vertical gyro error model. Shown in flgure 2 are the blocks representing the longitudinal and lateral autoland systems. Spoiler input was formulated by a 1.73 gain on the aileron signal. First-order lag models were used to describe engine thrust response. The control signals thus derived together with the yaw damper output were introduced into the aircraft perturbation equations of motion which were written in state varlable form.

The perturbation states in vehicle stability axes were pitch attitude $\theta$, normalized inertial velocity $u^{\prime}$, angle of attack $\alpha$, pitch rate $q$, bank angle $\phi$, heading $\psi$, sideslip $\beta$, roll rate $p$, and yaw rate $r$. The control vector consisted of perturbed elevator position $\delta_{e}$, perturbed stabilizer position $\delta_{s t a b}$, perturbed thrust $\delta_{t}$, perturbed alleron position $\delta_{a}$, perturbed spoiler position $\delta_{s p}$, and perturbed rudder position $\delta_{r}$. Aerodynamic data were obtained by use of a data program package at the Langley Research Center for the aircraft in the landing configuration, that is, gear down, flaps $40^{\circ}$ down, $61.73 \mathrm{~m} / \mathrm{sec}(120 \mathrm{knots})$ alrspeed, and a weıght of $400 \mathrm{kN}(90000 \mathrm{lb})$.

Gyro Error Model
Figure 3 is a block diagram showing the fundamental elements of the single degree of freedom vertical gyro error model. The errors associated with a conventional vertical gyro (ref. 4) are a result of three distinct effects:
(1) Cumulatıve drıft effects: Because of mass unbalance, bearing frıction, Earth rotation rate, and coriolis acceleration, the gyro spin axis becomes misalined with the true local vertical.
(2) Maneuver-induced spin-axis alınement with a false vertical: During perıods of accelerated flight (forward or centripetal acceleration present), the gimbal-mounted electrolytic bubble sensors cause the gyro to be alined with a false vertical. This false or apparent vertical is the vector addition of vehicle acceleration and gravity.
(3) Propogation error in turns: This effect predominantly occurs in alrcraft turns during which time the gyro spin axis tefids to maintain a fixed spatial orientation as the arplane and gimbals rotate about the gyro. The result
of this phenomena is that any existing pitch error while on a northern heading translates to a roll error when heading is changed to east or west.

The fundamental components of the gyro model (fig. 3) are the erection rate limiter and cutout and the torque motor. The cutout threshold for these tests was set to a lateral acceleration corresponding to a $6^{\circ}$ bank angle. In other words, whenever the apparent lateral acceleration sensed by the roll bubble exceeded the acceleration corresponding to $6^{\circ}$ roll, erection cutout occurred. The angular position error is then formed by the addition of the drift and the erection signal from the torque motor. Finally, this error was added to the true attitude for formulation of the measured roll attitude signal.

## Tests

The initial setup for this study is shown in figure 4. A relatively short straight-in final approach was used after the aircraft was started at capture in straight and level flight but offset by 365.76 m ( 1200 ft ). It was also given a $20^{\circ}$ localızer intercept angle. Initial condition errors between the spin axis and the local vertical (see fig. 3) were injected prior to commencing the problem. All these gyro tilt errors $\left(2^{\circ}, 3^{\circ}, 4^{\circ}\right.$, and $5^{\circ}$ ) were positive, that 1 s , right wing down which simulates a worse case situation. Also, gyro drift and Earth rates were assumed to be positive. Vehicle automatic tracking performance was monitored through touchdown for each tilt error and the selected erection rate. Wind velocity was consldered to be zero in these tests.

## RESULTS AND DISCUSSION

The lateral autoland tracking performance was examined for a gyro erection rate of $1.05^{\circ}$ per minute after initial gyro tilt errors were induced prior to locallzer capture. Figure 5 shows the lateral tracking performance when the inertial roll attitude feedback that would be expected from a stabilized platform is used. It is realized that because of preapproach maneuvering, maximum roll attitude errors of the order of $0.1^{\circ}$ are possible with stabilized platforms, but in the context of this paper they were considered to be insignificant. In other words, the inertial platform attitude signal was deemed to be perfect. Figures 6 to 9 show the effect of the various tilt errors on the final approach trajectory. Tracking and overshoot errors observed in figures 6 to 8 are due to the initial gyro tilt errors which are not completely eliminated by erection. The lower plot gives the varıation of tilt error with respect to time. It should be noted that although the induced lateral displacement errors (due to initial $2^{\circ}, 3^{\circ}$, and $4^{\circ}$ gyro tilt) at touchdown are small, they are systematic and may be significant percentagewise when compared with the influence of other environmental and landing system errors. For the $5^{\circ}$ tilt error (fig. 9), unacceptable standoff and divergence from the runway center line were observed. The lateral touchdown dispersion for $2^{\circ}, 3^{\circ}$, and $4^{\circ}$ tilt errors are plotted in figure 10 and vary from $-0.45 \mathrm{~m}(-1.47 \mathrm{ft})$ to $-0.53 \mathrm{~m}(-1.74 \mathrm{ft})$. For the $5^{\circ}$ tilt error where the control logic was not satisfied, the lateral deviation at touchdown was $101.98 \mathrm{~m}(334.57 \mathrm{ft})$ and is unacceptable.

The behavior of figure 9 can be understood if the lateral autoland control loop (fig. 11) is studied. Three logic criteria must be satisfied in order to acquire the "ON COURSE" state. In order to satisfy all criteria ("ON COURSE" set to true in the simulation), the localizer beam angle must be less than $\eta_{\text {lim }}$ (see insert (A) in fig. 11) and the beam rate less than $0.027^{\circ}$ per second. Also, the bank angle must be less than $3^{\circ}$. When all criterıa are satisfied, "ON COURSE" is set to true and the appropriate switch closures result. Of these three criterıa, the last two are readily satısfied; however, the first requirement depends on beam deviation and may or may not be satisfied depending on the tilt error encountered at localizer capture. Because the beam acceptance limit $\eta_{l ı m}$ is a function of altıtude and decreases rapidly relative to tilt error reduction, it was found that the localizer angular displacement $\eta$ did not become sufficiently small compared with $\eta_{l ı m}$ for the $5^{\circ}$ tilt error. As a result, the localizer beam integration loop whose primary function is to reduce the steady-state beam displacement error to zero is never incorporated into the control law. Also, the high loop gains (inserts (C) and (D) in fig. 11) are not attained; thereby less precise tracking and unacceptable beam standoff at touchdown result.

## CONCLUDING REMARKS

The results of this study indicate that vertical gyro tilt errors, which may be substantial because of terminal area maneuvering and gyro imperfections, can degrade lateral autoland tracking performance measurably. In addition, for the control law examined, there is an error threshold which, if exceeded, precludes localızer capture because the "ON COURSE" logic crıterıa could not be satisfied.

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May 6, 1977

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Figure 1.- Dimensions of simulated aircraft.


Figure 2.- System block diagram.
True roll attitude, $\phi$

Figure 3.- Lateral degree of freedom vertical gyro model.


Figure 4.- Test situation and sign convention.



Figure 5.- Lateral tracking performance using inertial roll attitude feedback.
$105^{\circ}$ per minute erection rate




Figure 6.- Lateral tracking performance for a $2^{0}$ vertical gyro tılt error prior to localizer capture.
$105^{\circ}$ per minute erection rate




Figure 7.- Lateral tracking performance for a $3^{\circ}$ vertical gyro tilt error prior to localizer capture.


Figure 8.- Lateral tracking performance for a 40 vertical gyro tilt error prior to localızer capture.

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105^{\circ} \text { per minute erection rate }
$$





Figure 9.- Lateral tracking performance for a $5^{\circ}$ vertical gyro tilt error prior to localızer capture.


Lateral dispersion from runway center line at touchdown, ft
Figure 10.- Touchdown dispersions for various initial gyro verticality errors.

Figure 11.- Lateral autoland system.

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