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# JOINT INSTITUTE FOR AERONAUTICS AND ACOUSTICS STANFORD UNIVERSITY

## Final Report

### MULTI-CALCULATION RATE SIMULATIONS

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Simulation Sciences Division  
Moffett Field, Ca 95035

#### By

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NSG-2250

November 1977



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## I. INTRODUCTION

Real time simulations of aerospace systems have been developed at several NASA centers for the purpose of providing a testbed for numerous studies involving use of cockpit mockups, visual displays, pilot/astronauts, and vehicle motion. It is common in real-time simulations of large systems to separate the high and low frequency subsystems within the simulation and perform the integrations of the subsystems at different calculation rates. This is done to strike a balance between accuracy of calculation and capacity of the digital computer. Questions arise as to the accuracy of this structure compared to single calculation rates and if any interactions arise that cause errors that are worse than those expected from an analysis of the subsystem above.

This report describes a study that was done on a linear aircraft model that investigates the questions above. Since actual simulations are much more complex with many nonlinearities, these results cannot be applied directly; however, the study does show where the problems are and gives guidelines for selection of sample rates for multiple rate simulations.

### III. BACKGROUND

The particular system simulations in question typically have a fast mode (aircraft short period, dutch roll) and a slow mode (phugoid, roll divergence) which can differ by an order of magnitude in the respective natural frequencies. These kind of problems are referred to as "stiff" differential equations in numerical analysis circles although special techniques to solve stiff equations are not absolutely necessary until frequency multiples on the order of 100 or more exist.

Many different techniques have been reported [1,2,3,4,5] but none use different calculation rates for the different modes of the system. The reason for the lack of literature (and lack of interest by numerical analysts) on multi-calculation rate techniques appears to be due to the difficulty in separating systems into fast and slow modes. Numerical integration procedures are never limited to linear systems which are really the only ones that can be cleanly separated.

In aircraft simulations, system descriptions are sufficiently close to linear so as to allow separation based on our knowledge of the approximate linear version. Furthermore, since the differential equations arise from known physical phenomenon which are similar for all vehicles and flight conditions, once the separation has been determined for one case, it is applied successfully for most others.

On the other hand, the general problem of analyzing a linear discrete system with multiple sample rates has been studied extensively [6,7,8,9,10]. Since any numerical integration procedure can be reduced to a set of difference equations, and will be linear if the differential equations being integrated are linear, these methods are applicable. Unfortunately, the methods are very tedious to apply and require large amounts of algebra before going to a computer. Application of these methods to the aircraft simulation were studied for simple integration procedures but judged to be beyond the scope of the study for the more realistic and complex integration procedures.

### III. METHOD OF ANALYSIS

To provide a common yardstick for comparing the various algorithms, it was decided to use the frequency response of the aircraft simulations. In particular, the transfer function of the longitudinal mode of a DC-8, from elevator command to vehicle attitude was selected for study. Two methods were employed;

- 1) discrete analysis using z-transforms of the single calculation rate cases, and
- 2) numerical simulation of the multi-calculation rate cases.

#### A. The Selected Example

A DC-8 in approach configuration was selected for study. The transfer function between elevator and attitude for this case is [11]:

$$\frac{\theta(s)}{\delta_e(s)} = -1.338 \frac{(s+0.0605)(s+0.535)}{(s^2 + 1.69s + 2.67)(s^2 + 0.0198s + 0.0267)} \quad (1)$$

which results in the short period and phugoid characteristics as shown in Table I. Note the 10:1 difference between the frequencies of the fast

Table I: EXAMPLE CHARACTERISTICS

	Natural Frequency	Damping
Short Period	1.62 r/sec (.258Hz)	0.522
Phugoid	0.164 r/sec (.0261Hz)	0.0606

and slow modes.

The magnitude and phase of (1) was determined analytically and has been included in all the following graphs for comparison (labeled "continuous system"). Since this represents the response of an actual aircraft with varying frequency of input commands, the goal of all digital approximations of this aircraft is to match the continuous response as closely as possible.

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### B. Discrete Analysis of the Single Rate Case

The transfer function in (1) can be written as a set of differential equations:

$$\begin{bmatrix} \dot{y}_1 \\ \dot{y}_2 \\ \dot{y}_3 \\ \dot{y}_4 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -a_0 & -a_1 & -a_2 & -a_3 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} + K \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} (\ddot{\delta}_e + b_1 \dot{\delta}_e + b_0 \delta_e) \quad (2)$$

where for this example:

$$a_3 = 1.7.00522$$

$$y_1 = \theta$$

$$a_2 = 2.6813872$$

$$y_2 = \dot{\theta}$$

$$a_1 = 0.09712526$$

$$y_3 = \ddot{\theta}$$

$$a_0 = 0.07006953$$

$$y_4 = \dddot{\theta}$$

$$K = -1.338$$

$$b_1 = 0.5955$$

$$b_0 = 0.0323675$$

#### 1. Euler's Integration:

Euler's integration [12] can be simply stated by:

$$y(n+1) = y(n) + T[\dot{y}(n)] \quad (3)$$

Combining (2) and (3) and using first differences to generate  $\ddot{\delta}_e$  and  $\dot{\delta}_e$  yields:

$$\frac{\theta(z)}{\delta_e(z)} = KT^2 \frac{z^2 + n_1 z + n_0}{z^4 + m_3 z^3 + m_2 z^2 + m_1 z + m_0} \quad (4)$$

where

$$T = \text{sample time}$$

$$K = -1.338$$

$$n_0 = b_0 T^2 - b_1 T + 1$$

$$n_1 = b_1 T - 2$$

$$m_0 = a_3 T^4 - a_2 T^3 + a_1 T^2 - a_0 T + 1$$

$$m_1 = a_2 T^3 - 2a_1 T^2 + 3a_0 T - 4$$

$$m_2 = a_1 T^2 - 3a_0 T + 6$$

$$m_3 = a_0 T - 4$$

The frequency response of this discrete transfer function can be determined by evaluating (4) with  $z$  taking on values around the unit circle. The computer code for doing this is contained in Appendix A and the results are contained in the following section for  $T$ 's ranging from 0.05 sec to 0.5 sec.

## 2. First Order Adams Integration [13]:

The algorithm is:

$$y(n+1) = y(n) + \frac{T}{2} [3f(n) - f(n-1)] \quad (5)$$

where  $f(n) = y(n)$  from (2).

This algorithm makes use of one past value of the derivative function and therefore increases the order of the discrete system.

The discrete transfer function of (5) is:

$$\frac{\theta(z)}{\delta_e(z)} = K \frac{B_8 z^8 + B_7 z^7 + B_6 z^6 + B_5 z^5 + B_4 z^4 + B_3 z^3 + B_2 z^2 + B_1 z + B_0}{C_{10} z^{10} + C_9 z^9 + C_8 z^8 + C_7 z^7 + C_6 z^6 + C_5 z^5 + C_4 z^4 + C_3 z^3 + C_2 z^2 + C_1 z + C_0} \quad (6)$$

where the coefficients are defined in Appendix B along with the computer code to evaluate the frequency response for (6).

## 3. Second Order Adams Integration [13]:

The algorithm is:

$$y(n+1) = y(n) + \frac{T}{12} [23f(n) - 16f(n-1) + 5f(n-2)] \quad (7)$$

which yields:

$$\frac{\theta(z)}{\delta_e(z)} = K \frac{B_{14} z^{14} + B_{13} z^{13} + \dots + B_1 z + B_0}{C_{16} z^{16} + C_{15} z^{15} + \dots + C_1 z + C_0} \quad (8)$$

where the coefficients are defined in Appendix C.

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### C. Simulation of the Multi-Rate Case

An alternate way of expressing (1) and (2) is also given by Teper [11]:

$$\begin{bmatrix} \dot{u} \\ \dot{w} \\ \dot{q} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} -0.0291 & 0.0629 & 0 & -32.2 \\ -0.251 & -0.628 & 243 & 0 \\ -7.7^{-6} & -8.7^{-3} & -0.792 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} u \\ w \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} 0 \\ -10.2 \\ -1.35 \\ 0 \end{bmatrix} \delta_e \quad (9)$$

The separation of these equations into fast and slow modes can be done in several ways. The ideal manner would be to transform the equations into their normal modes which would then produce two coupled 2nd order systems, one with pure short period characteristics and one with pure phugoid characteristics. Each could be integrated at sample rates suitable to that mode. In practice, this is difficult due to the non-linear terms in the equations. Furthermore, transforming to and from another state definition takes cpu time and may result in higher cpu loading than the more straightforward methods described next.

#### 1. The $1 \times 3$ Separation

If a normal mode analysis of an aircraft is performed, we find that the short period consists primarily of  $\alpha$ ,  $q$ , and  $\theta$  motion with insignificant effect on  $u$ . The phugoid consists of  $u$ ,  $q$ , and  $\theta$  with little effect on  $\alpha$ . Therefore, since  $u$  is the only state that does not involve "fast" behavior, it is the only state that can be safely calculated at the slow calculation rate. The " $1 \times 3$ " separation recognizes this fact and partitions accordingly. The equations are:

##### Fast Loop -

$$\begin{bmatrix} \dot{w} \\ \dot{q} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} -0.628 & 243.5 & 0 \\ -0.0087 & -0.792 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} w \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} -10.2 \\ -1.35 \\ 0 \end{bmatrix} \delta_e + \begin{bmatrix} -0.251 \\ -0.0000077 \\ 0 \end{bmatrix} u \quad (10)$$

Slow Loop -

$$\dot{\begin{bmatrix} u \\ w \end{bmatrix}} = -0.0291U + [0.0629 \quad -32.2] \begin{bmatrix} w \\ \theta \end{bmatrix} \quad (11)$$

2. The 2 X 2 Separation

Another natural separation is based on fast calculation of orientation,  $q$  and  $\theta$ , and slow calculation of translation,  $u$  and  $w$ . It is attractive because a larger portion of the calculations are done at a slower rate, hence more cpu time savings appear achievable. The equations are as follows.

Fast Loop -

$$\dot{\begin{bmatrix} q \\ \theta \end{bmatrix}} = \begin{bmatrix} -.792 & 0 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} q \\ \theta \end{bmatrix} + \begin{bmatrix} -1.35 \\ 0 \end{bmatrix} \delta_e + \begin{bmatrix} -.77 \times 10^{-5} & -.0087 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u \\ w \end{bmatrix} \quad (12)$$

Slow Loop -

$$\dot{\begin{bmatrix} u \\ w \end{bmatrix}} = \begin{bmatrix} -.0291 & .0629 \\ -.251 & -.628 \end{bmatrix} \begin{bmatrix} u \\ w \end{bmatrix} + \begin{bmatrix} 0 \\ -10.2 \end{bmatrix} \delta_e + \begin{bmatrix} 0 & -32.2 \\ 243.5 & 0 \end{bmatrix} \begin{bmatrix} q \\ \theta \end{bmatrix} \quad (13)$$

3. Simulation Procedures

The frequency response of each separation was determined using Euler's Integration (3) and the 1st order Adams Integration (5). It was evaluated at calculation rate ratios (IR) varying between 1 and 20. Since  $IR = 1$  is the single rate case, these calculations could be checked by comparing with the analytical evaluations described in III-B.

The frequency response was determined by evaluating equations (10) and (11) or (12) and (13) using the integration formulas with  $\delta_e$  equal to a sine wave of magnitude = 1. After an initial transient settling delay the resulting sine wave magnitude and phase was assumed to be the desired frequency response. The short period portion of the transient response was quite short; however, the phugoid transient response was unduly long to wait for settling. Therefore, the procedure calculated the phugoid transient response based on the continuous system

(1) using inverse Laplace transforms and subtracted this from the numerical evaluations before determining amplitude and phase. Appendix D contains a listing of the computer code.

#### IV. RESULTS

Table II contains a summary of the figures which represent the results of this study. In the simulations, all IR's between 1 and 20 were evaluated. Those cases not shown in the figures were found to be unstable.

TABLE II: SUMMARY OF FIGURES

Figure	Analytical	Simulated	Integration Algorithm	$T_{\text{fast}}$	IR	Separation
1	X		E	.05-.5	1	---
2	X		A1	.05-.5	1	---
3	X		A2	.05-.5	1	---
4	X		E,A1,A2	.05	1	---
5	X		E,A1,A2	.1	1	---
6	X		E,A1,A2	.2	1	---
7		X	E	.05	1-20	$1 \times 3$
8		X	E	.1	1-10	$1 \times 3$
9		X	E	.2	1-5	$1 \times 3$
10		X	E	.05	1-10	$2 \times 2$
11		X	E	.1	1-5	$2 \times 2$
12		X	E	.2	1-3	$2 \times 2$
13		X	A1	.05	1-20	$1 \times 3$
14		X	A1	.1	1-10	$1 \times 3$
15		X	A1	.1	1-5	$1 \times 3$
16		X	A1	.05	1-10	$2 \times 2$
17		X	A1	.1	1-5	$2 \times 2$
18		X	A1	.2	1-3	$2 \times 2$

The most significant result is the difference between the two separations. This can be seen by comparing the deviations from the continuous curves in Figs. 7, 8 and 9 with those in 10, 11 and 12 respectively for Euler's Integration and similarly Figs. 13, 14 and 15 with 16, 17 and 18. For both integration methods, the  $1 \times 3$  separation is decidedly superior. This is no doubt due to the fact that the  $2 \times 2$  separation solves the  $w$  (or  $\alpha$ ) equation at the slow rate while this state is important to the short period dynamics.

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The first order Adams integration appears to be the best choice of integration methods. Its advantage over Euler's method and small disadvantage compared to a second order Adams is best illustrated in the Fig. 6b phase plot; however, examination of the magnitude in Fig. 6a shows the Euler method's error arising at a lower frequency but remaining smaller at the higher frequencies. The same kind of behavior is exhibited at the faster sample rates (Figs. 4 and 5) but is more difficult to see due to the greater accuracy.

The sample rate requirement for aircraft simulation with a first order Adams integration is dependent on the desired input frequency to be adequately simulated. Examination of Figs. 13, 14 and 15 indicate that one should select the fast sample rate at approximately 10 times the input frequency to be followed and that a slow rate at one-tenth this rate yields no degradation. In other words, to follow a 2 Hz input, one should solve the short period equations at 20 Hz and the phugoid at 2 Hz.

## V. CONCLUSIONS

For a linear model of longitudinal aircraft motion, separation of the equations of motion into slow and fast calculation rate groups is best accomplished by performing  $u$  integration at the slow rate and  $w, q, \theta$  at the fast rate. A separation with  $u$  and  $w$  as the slow variables and  $q$  and  $\theta$  as the fast gave substantially less accuracy.

A first order Adams integration procedure appeared to be a good choice for real time aircraft simulations.

For the example used ( $\omega_{\text{short period}} \approx 0.25 \text{ Hz}$ ,  $\omega_{\text{phugoid}} = 0.025 \text{ Hz}$ ), the fast sample rate should be selected at approximately 10 times the maximum input frequency for which accurate aircraft simulated response is desired. A slow rate of one-tenth the fast rate yielded no degradation over the single rate case.

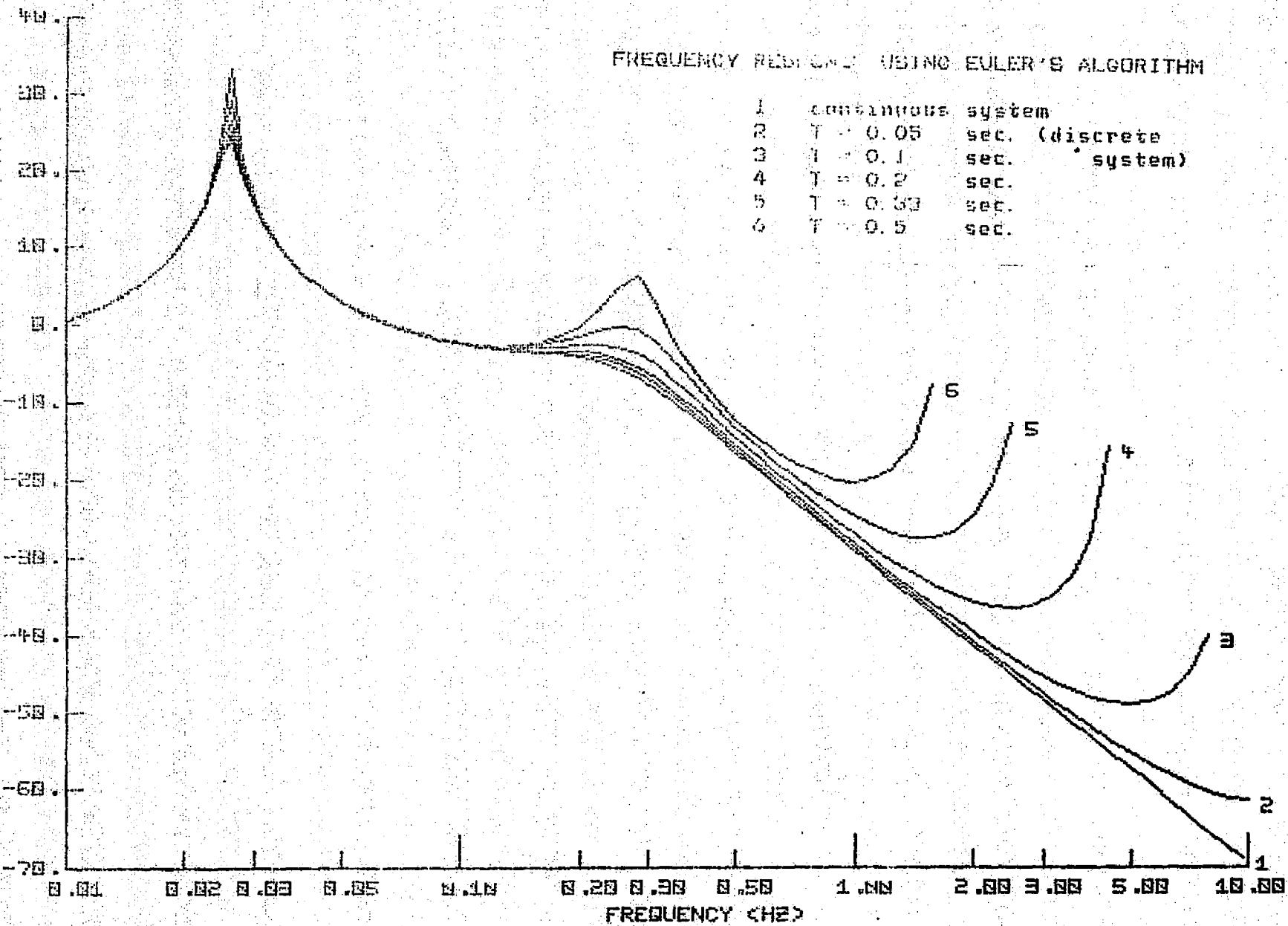


FIGURE 1a

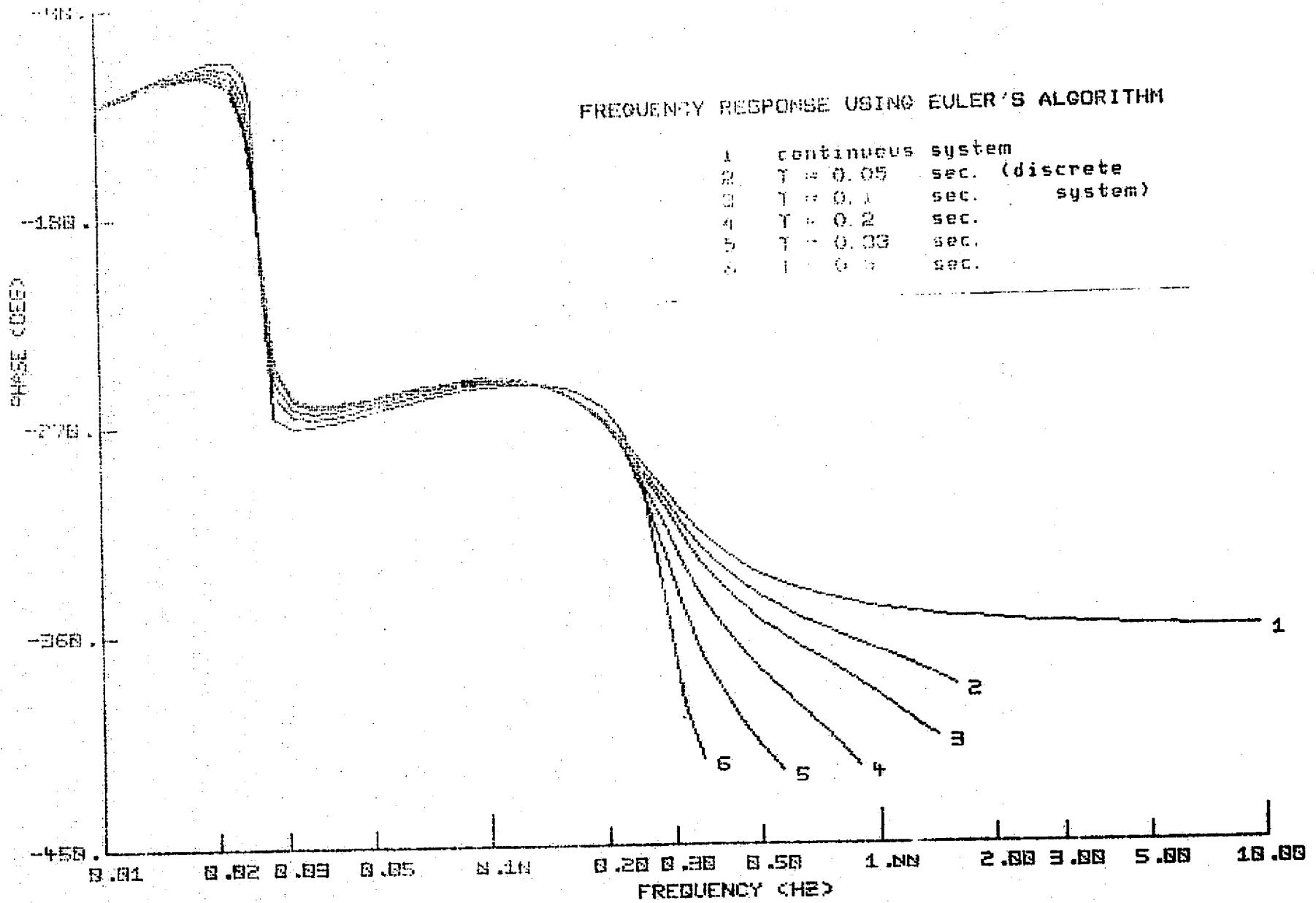


FIGURE 1b

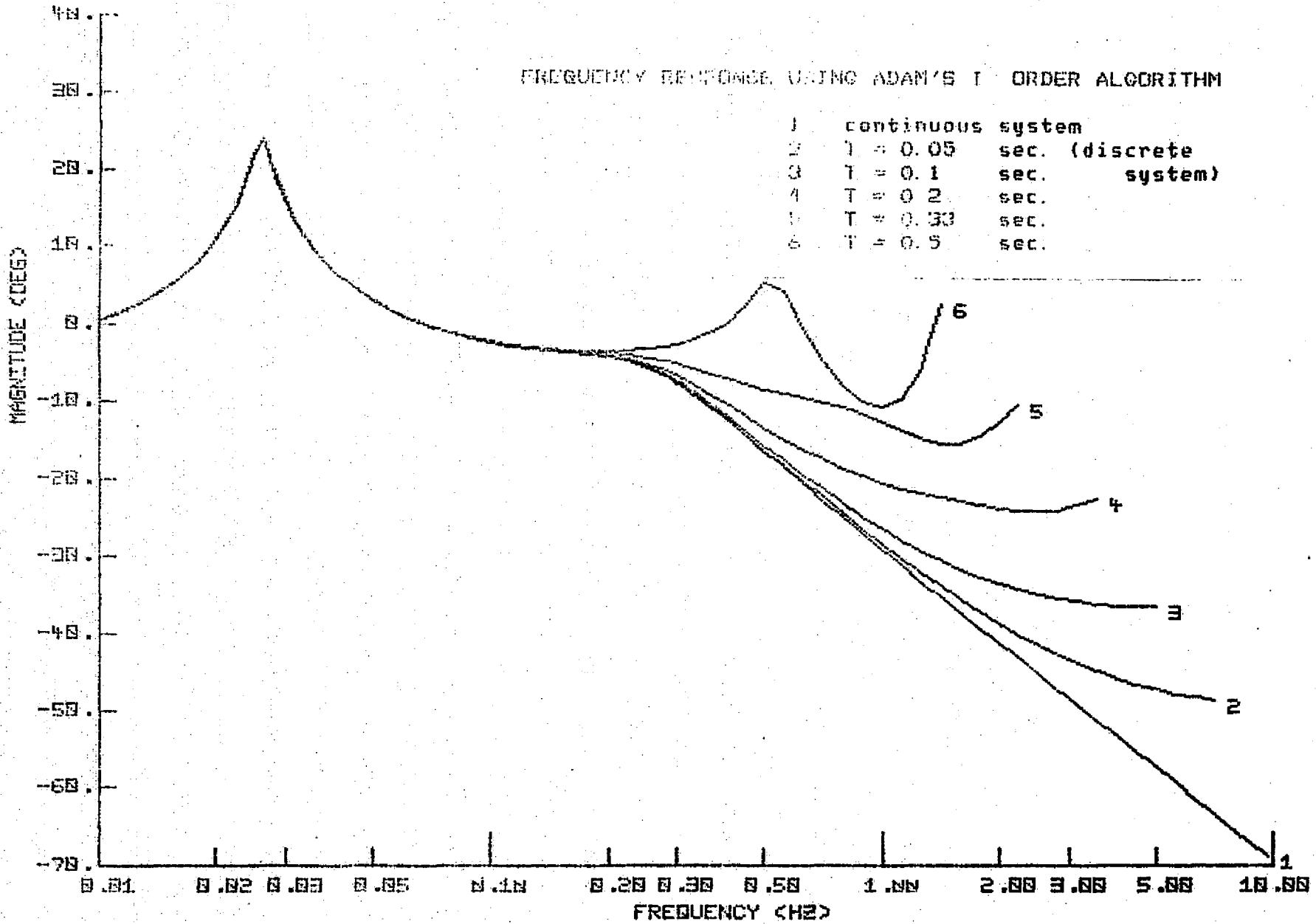


FIGURE 2a

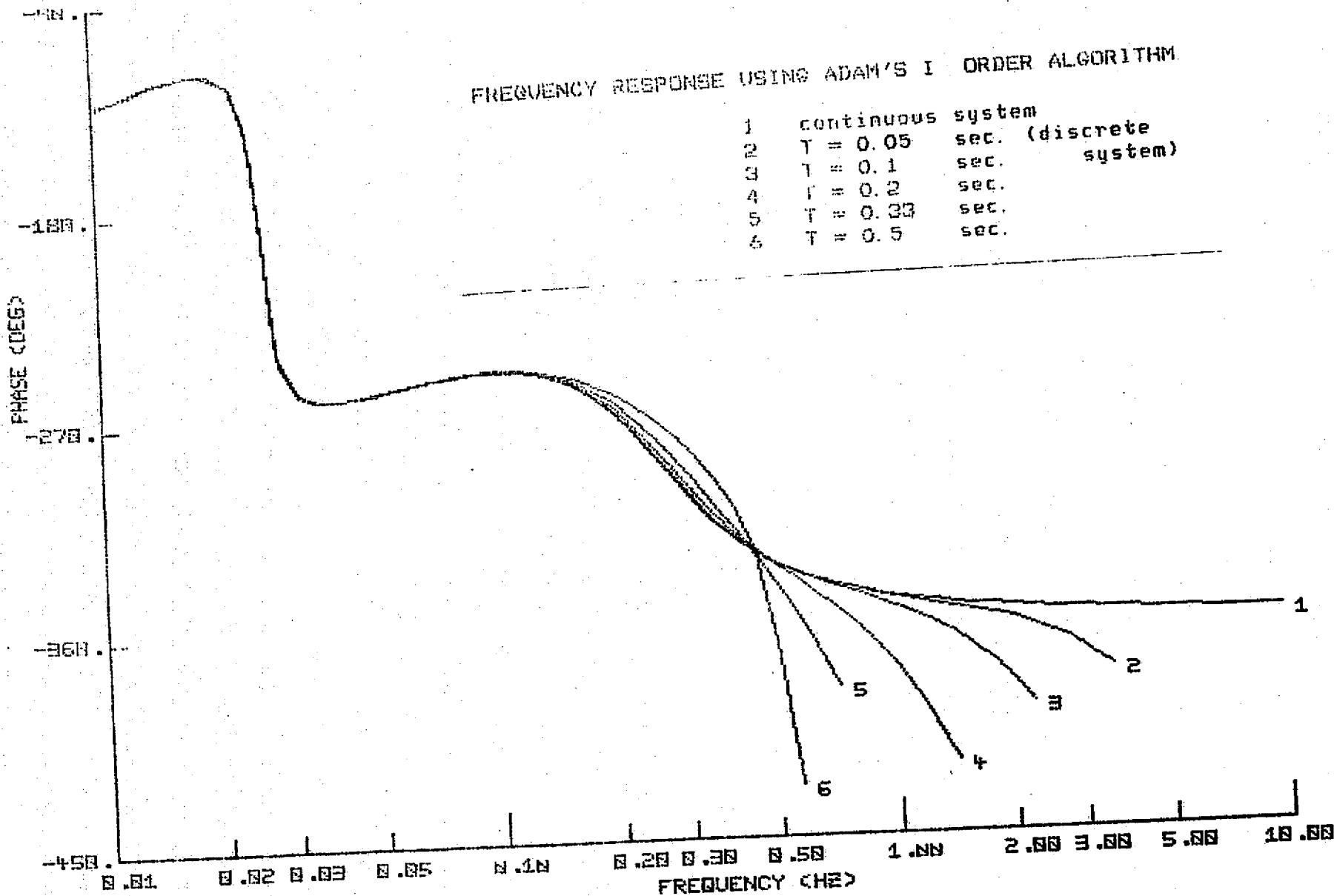


FIGURE 2b.

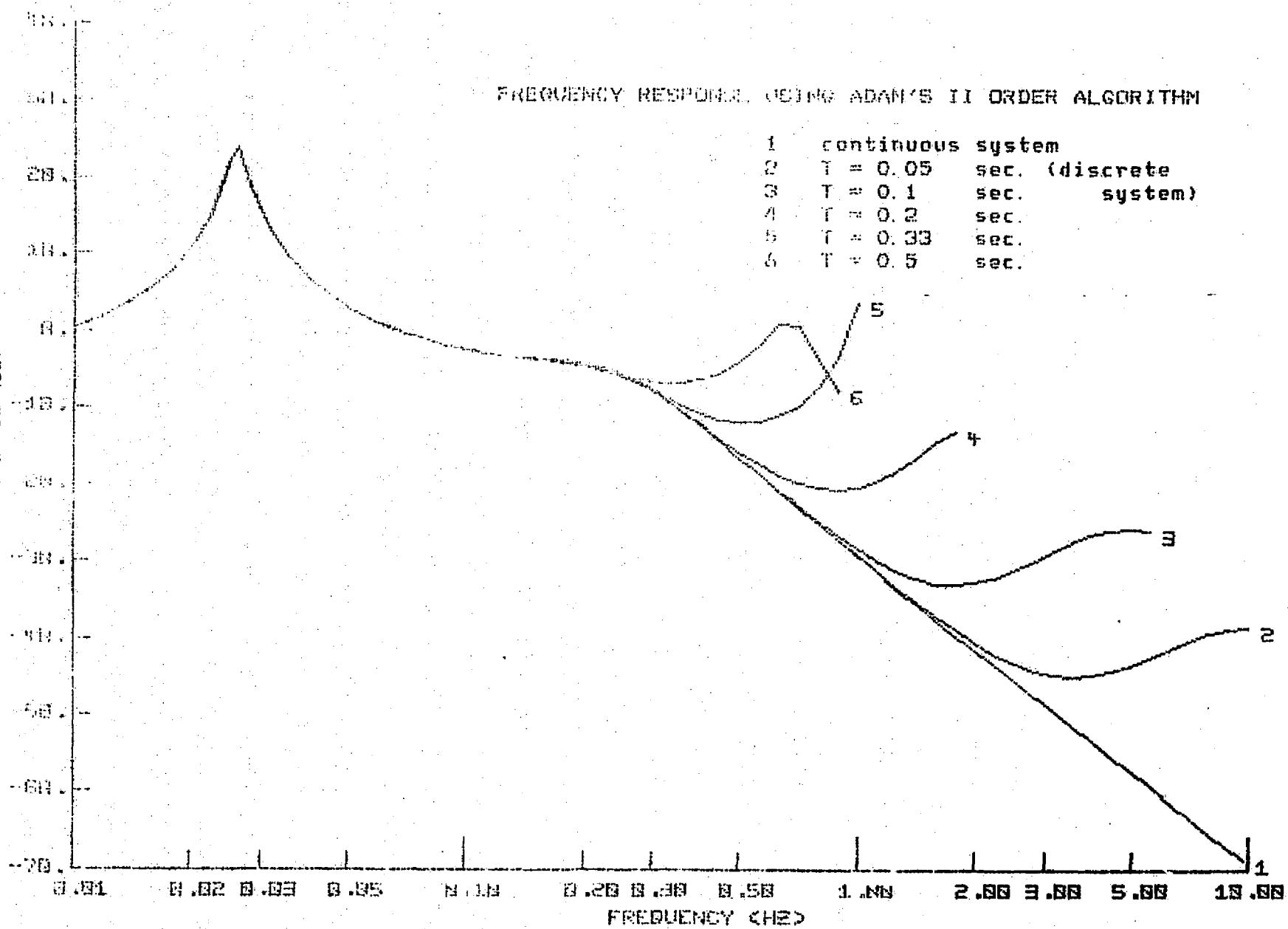


FIGURE 3a

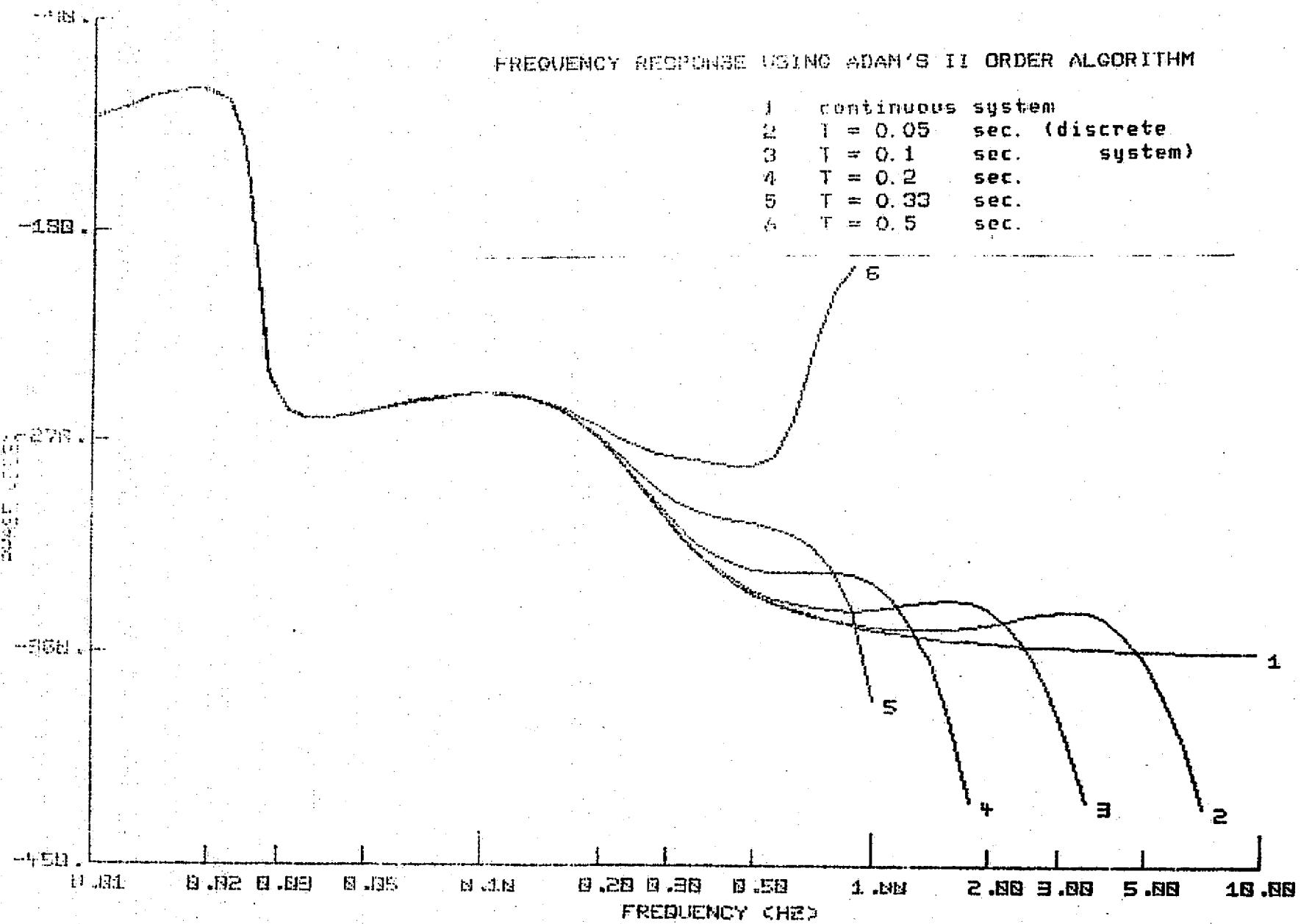


FIGURE 3b

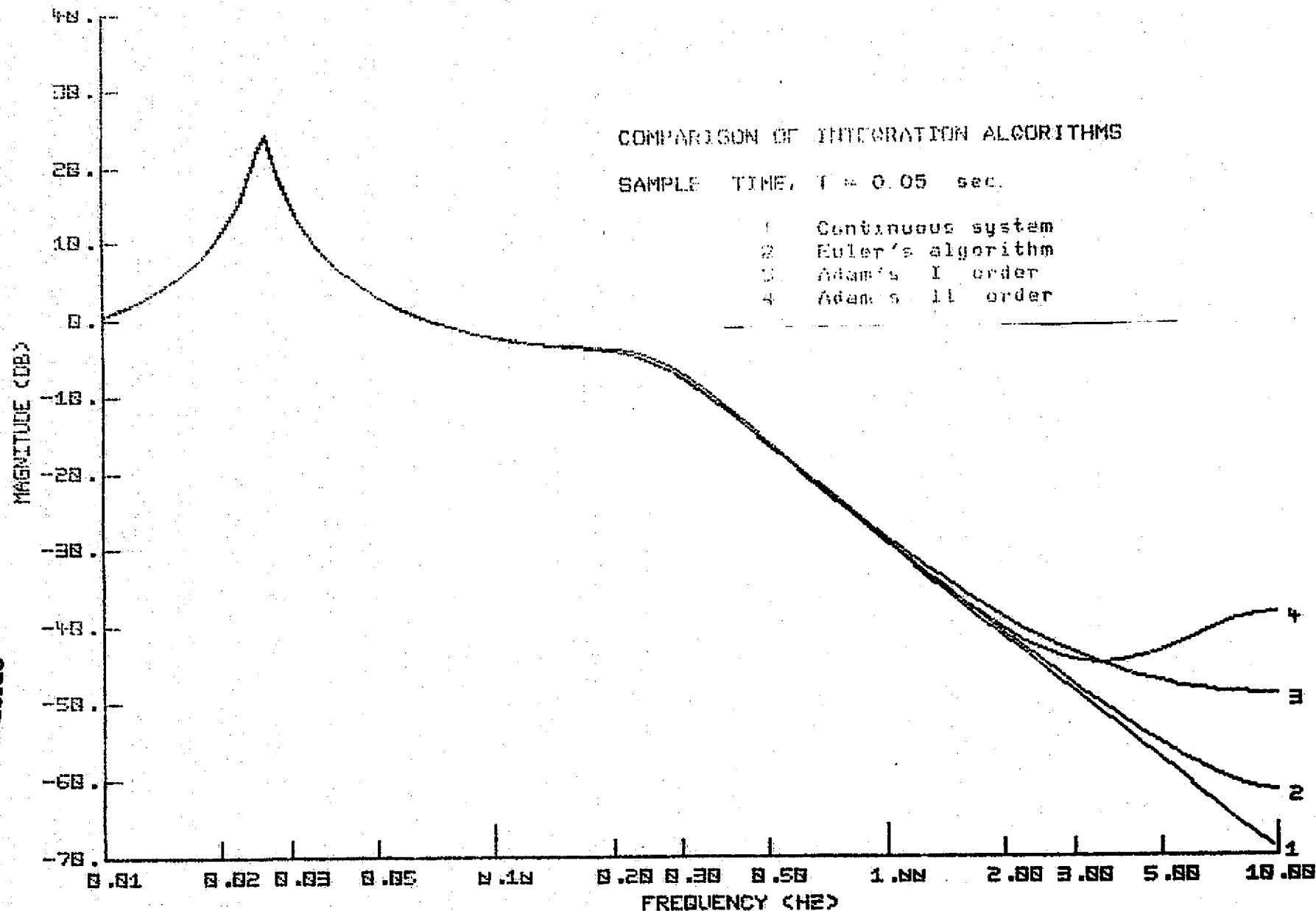


FIGURE 4a

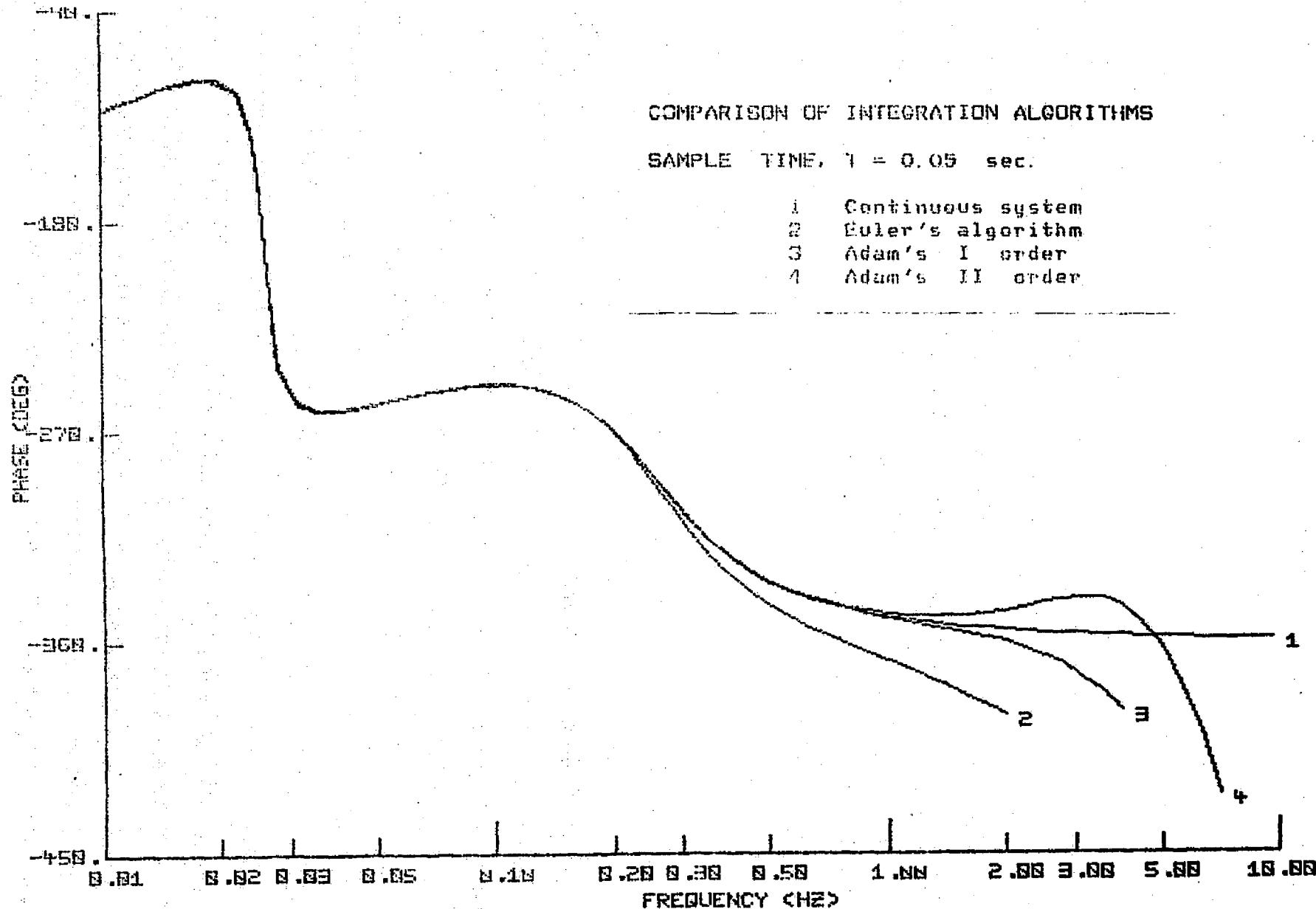


FIGURE 4b

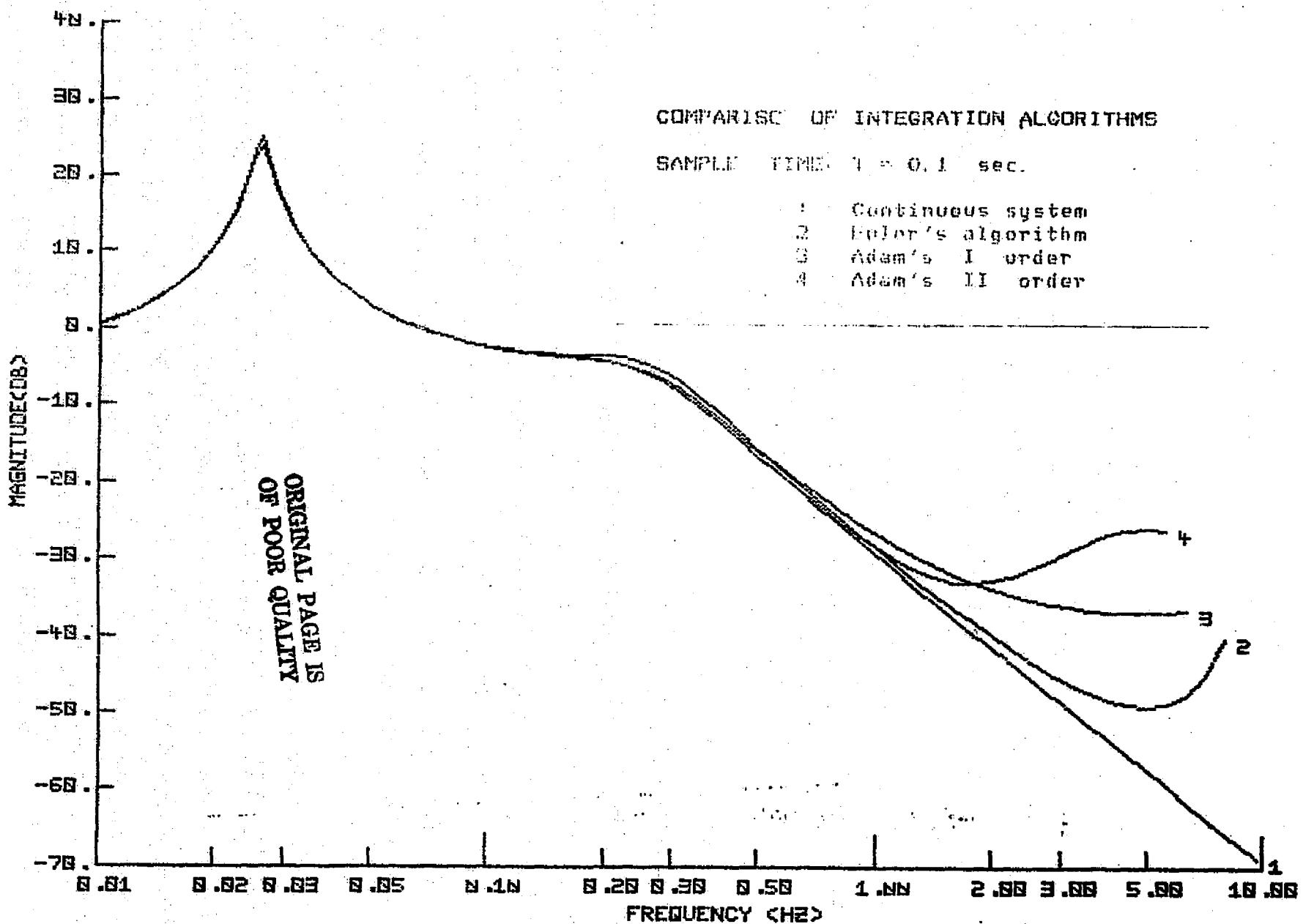


FIGURE 5a

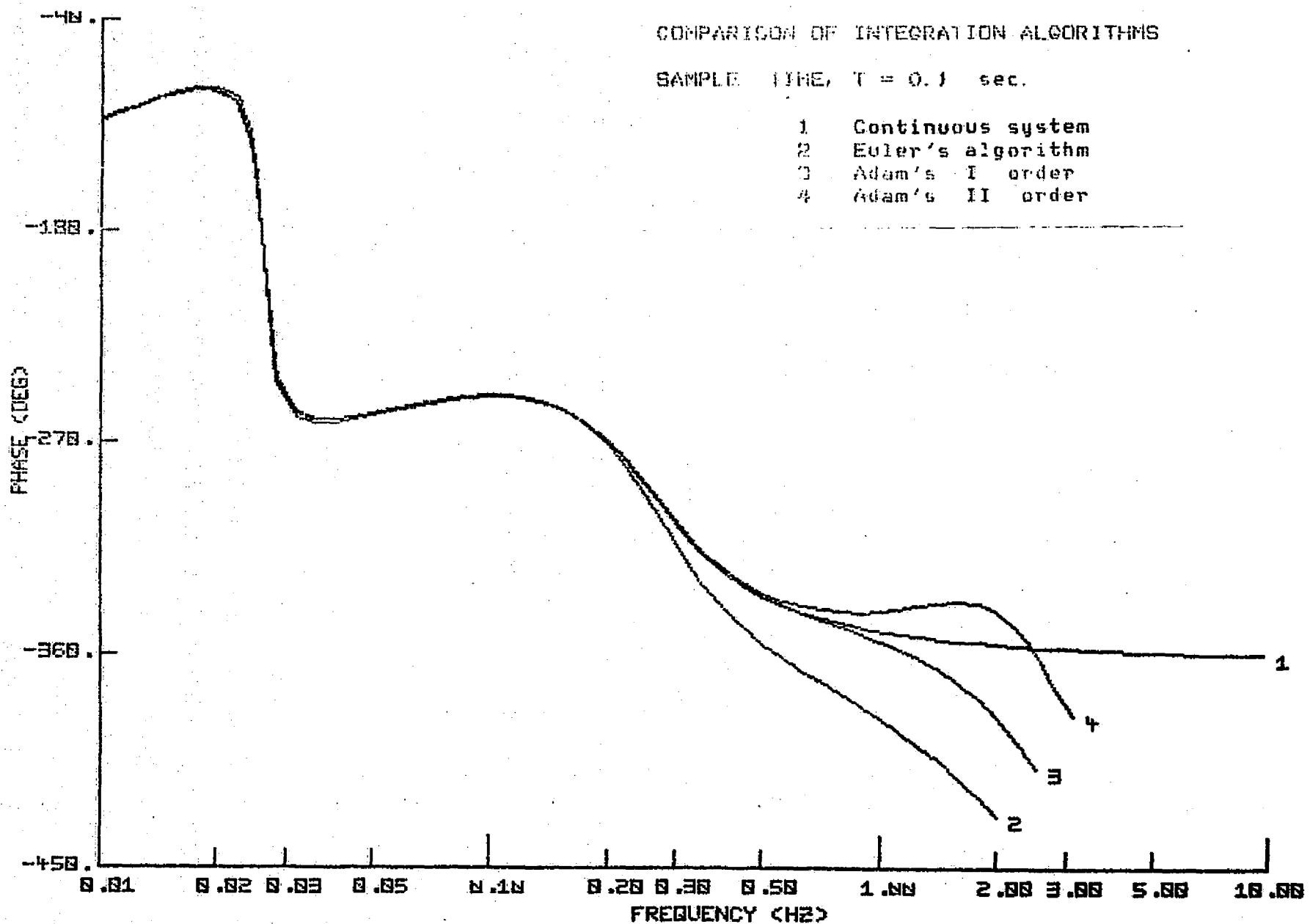


FIGURE 5b

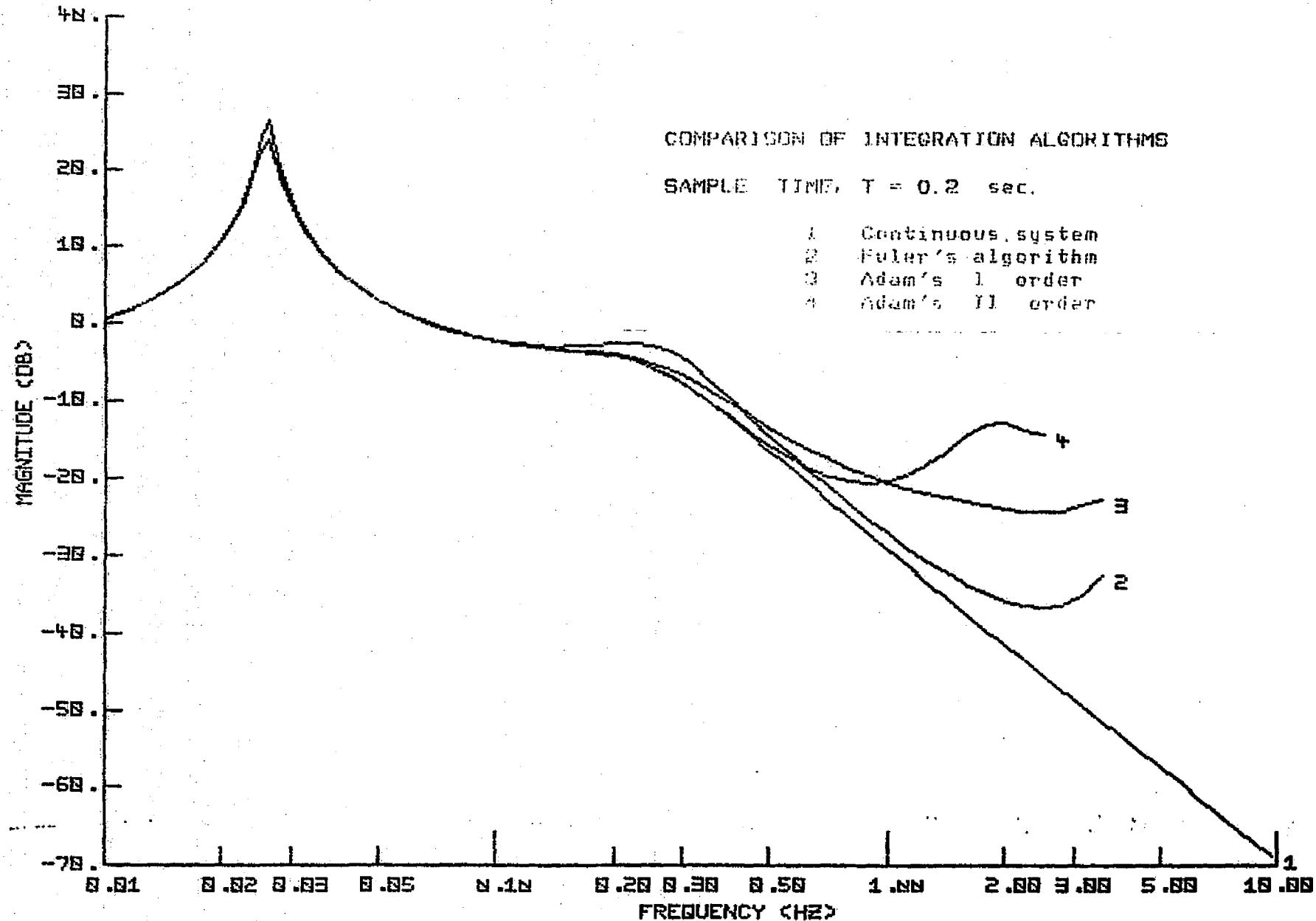


FIGURE 6a

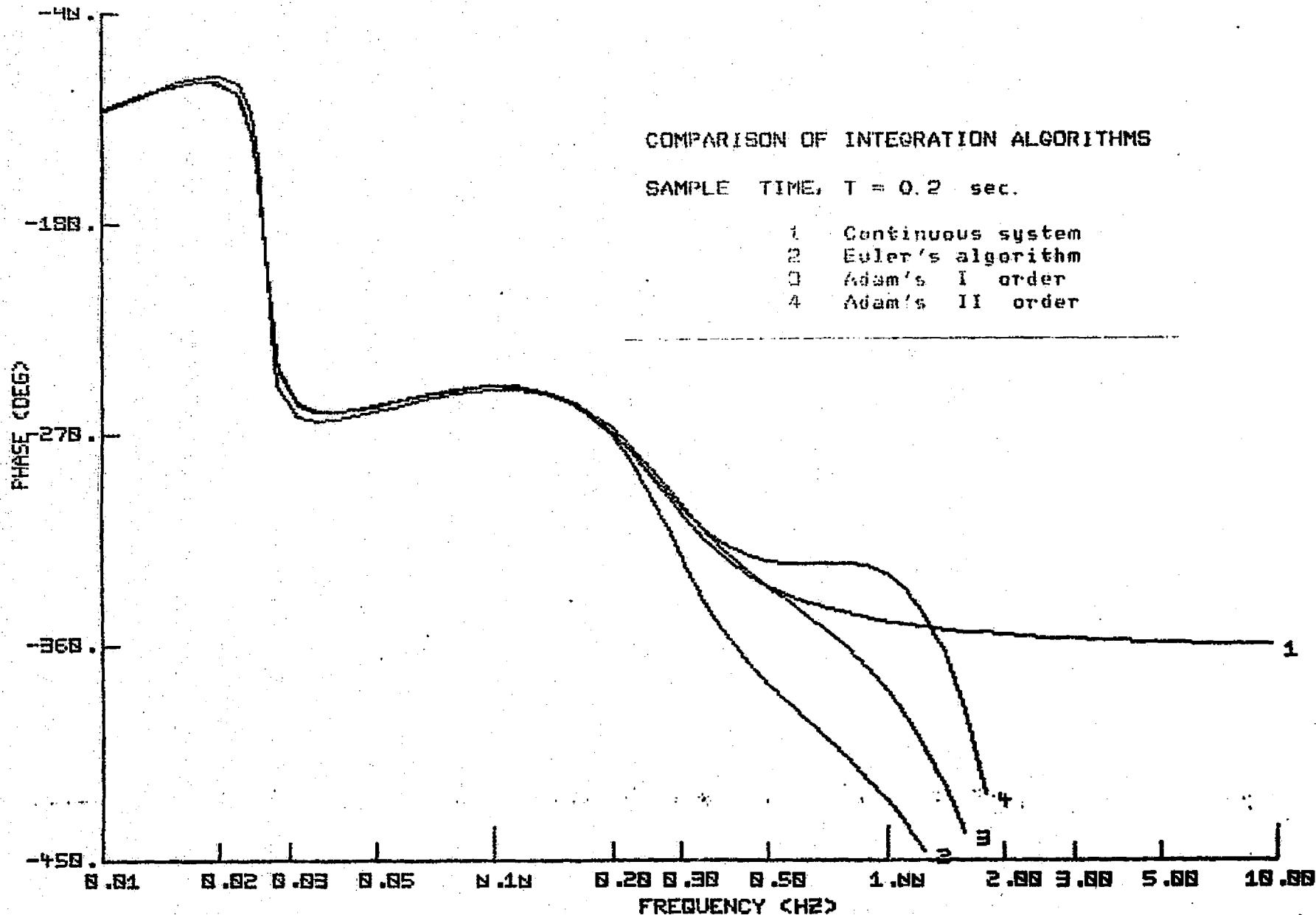


FIGURE 6b

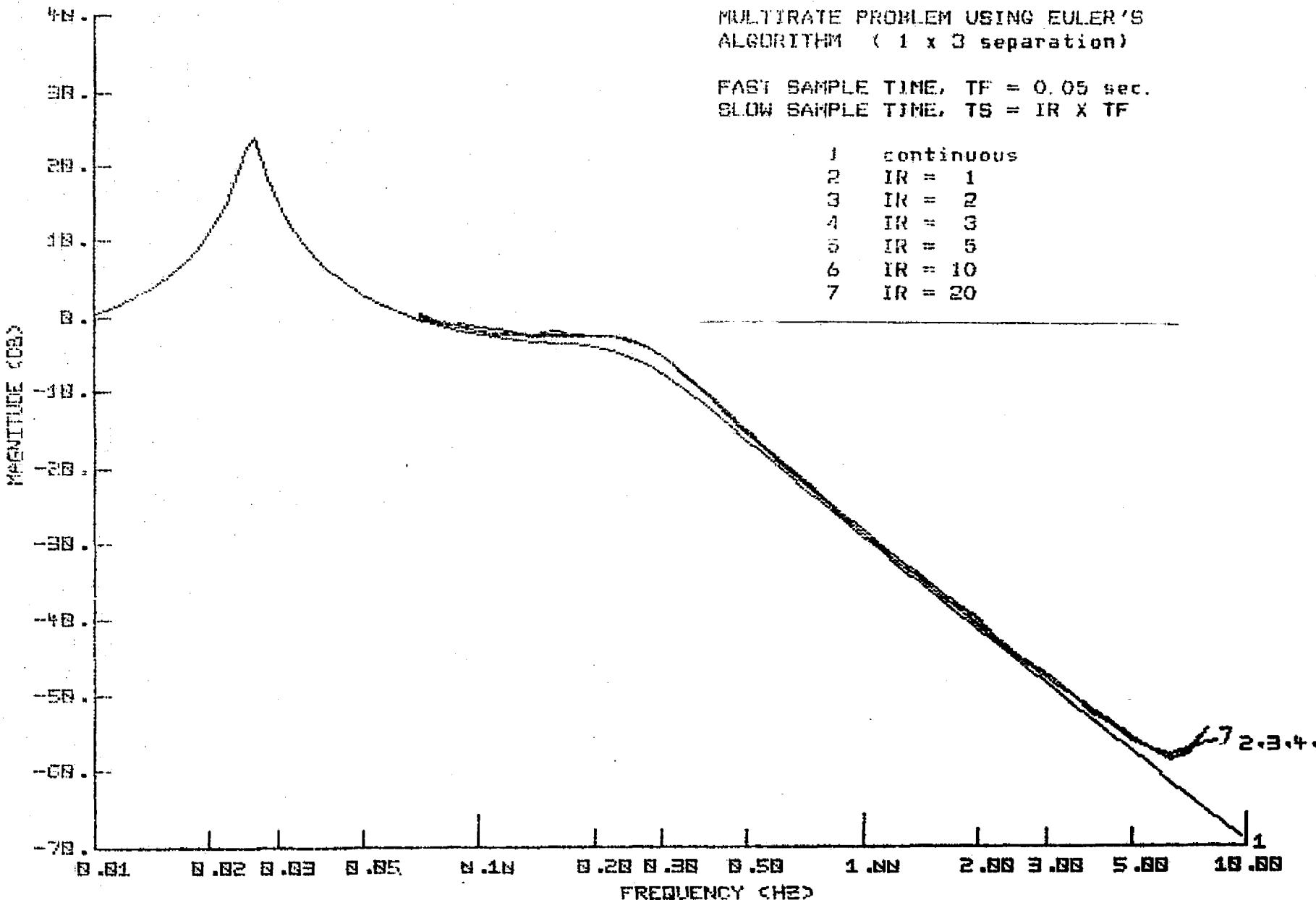


FIGURE 7a

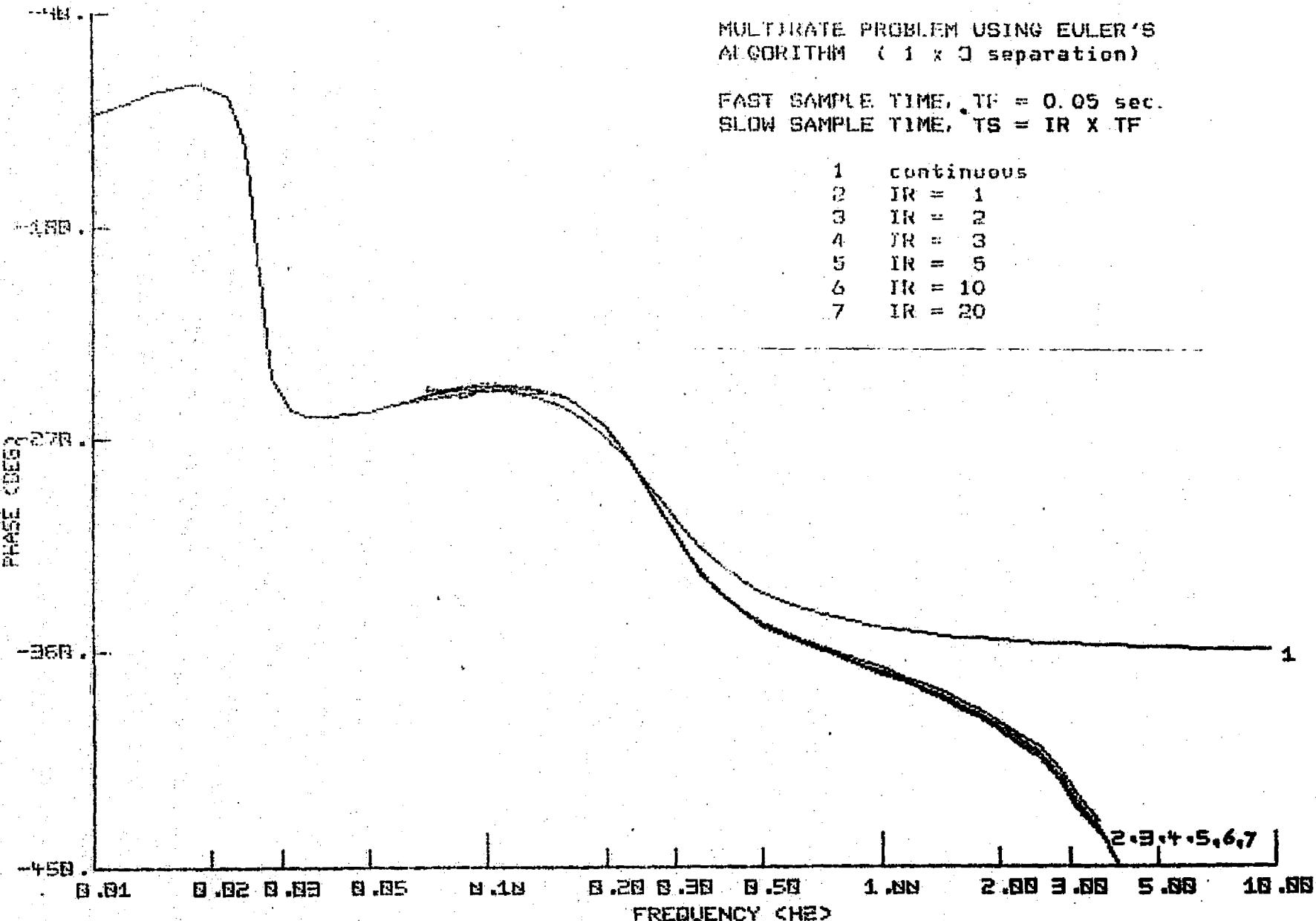


FIGURE 7b

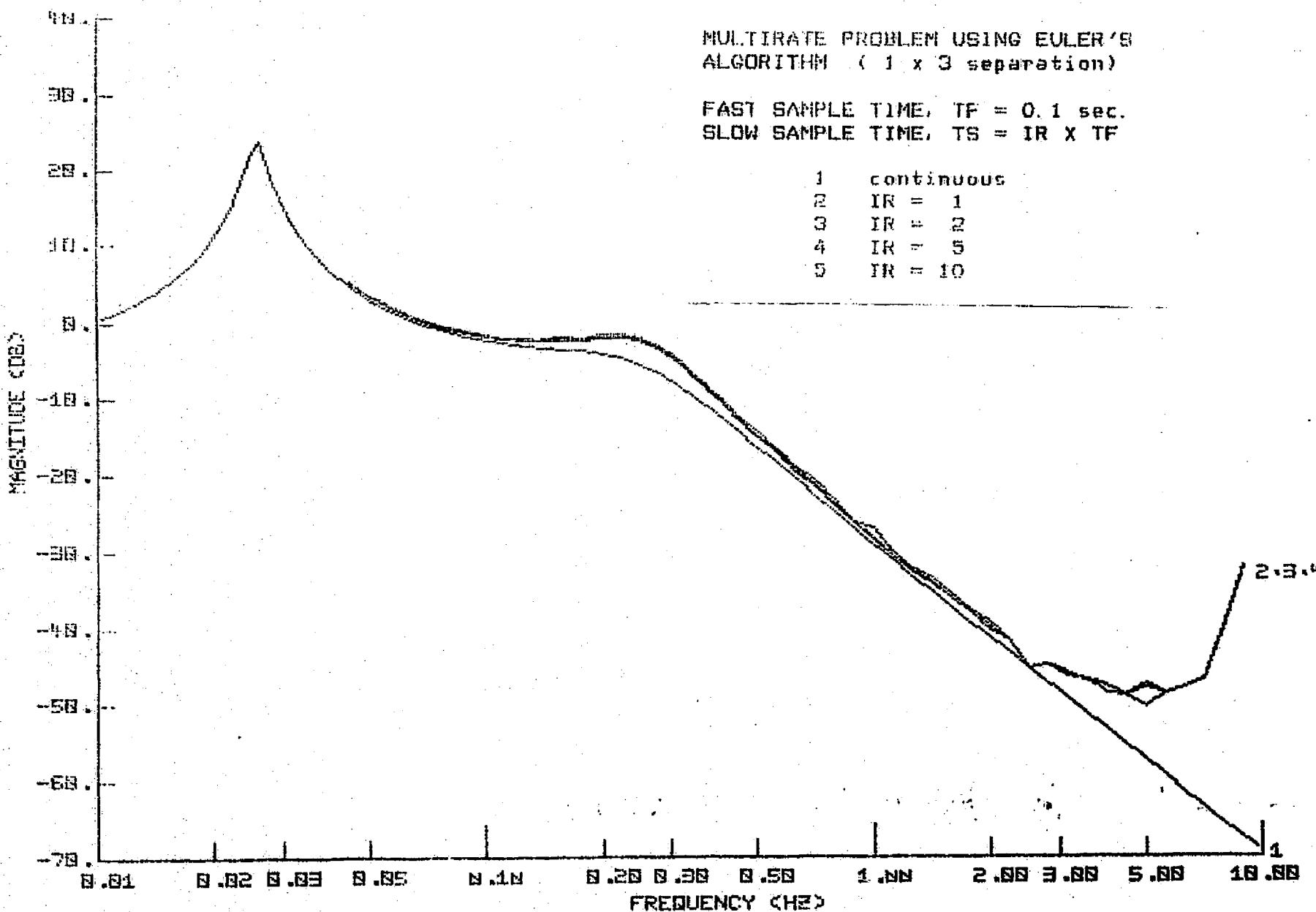


FIGURE 8a

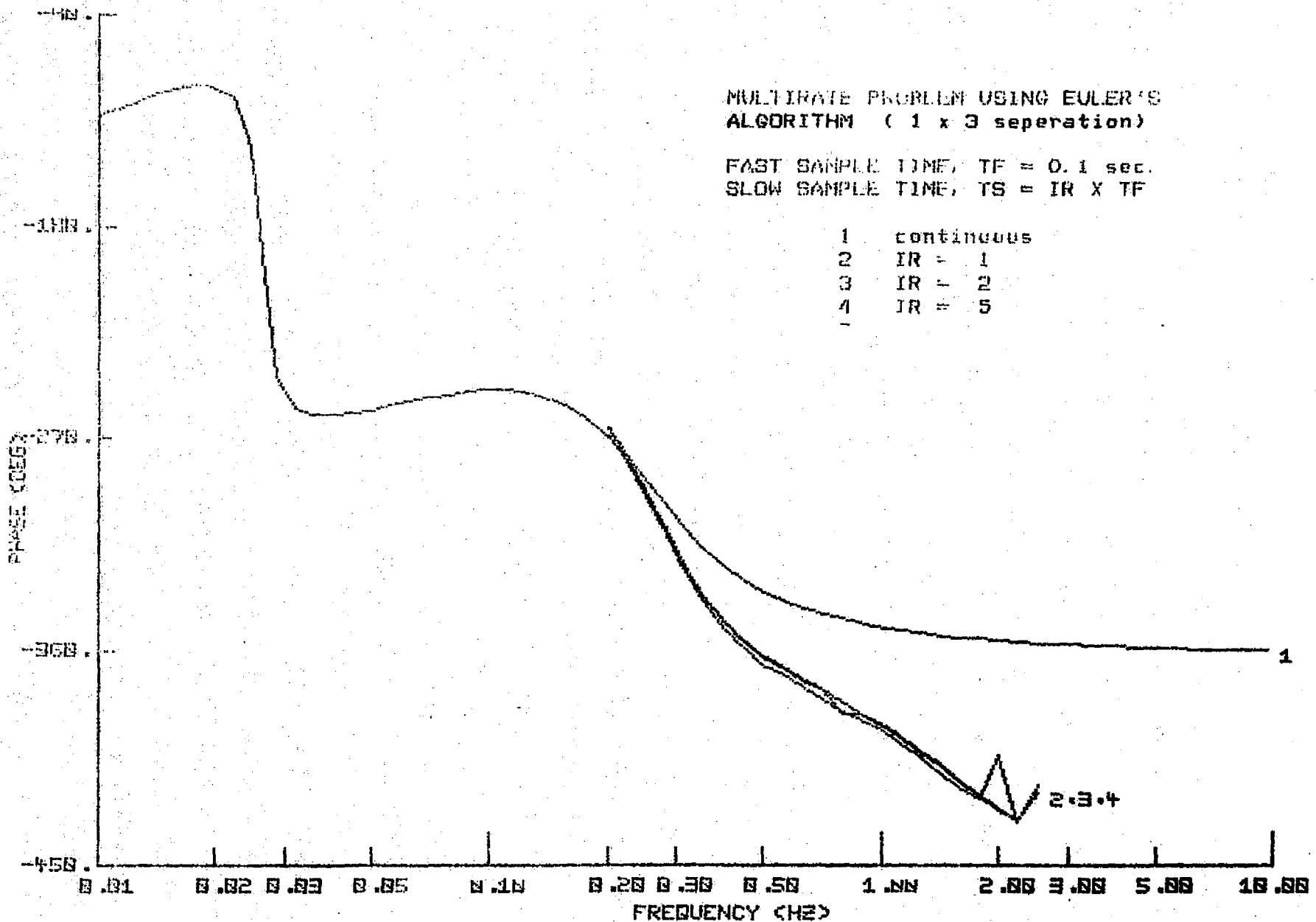


FIGURE 8b

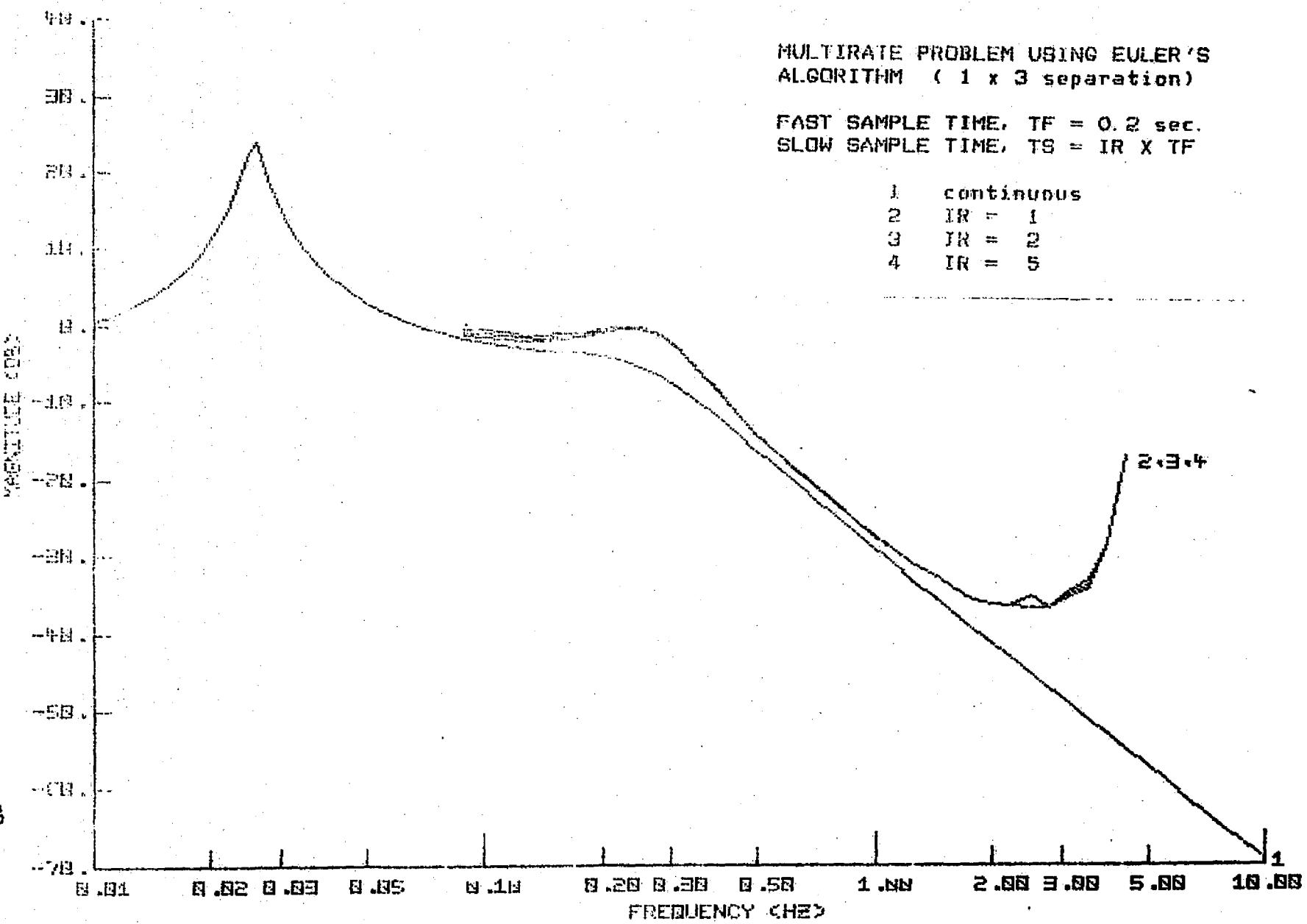


FIGURE 9a

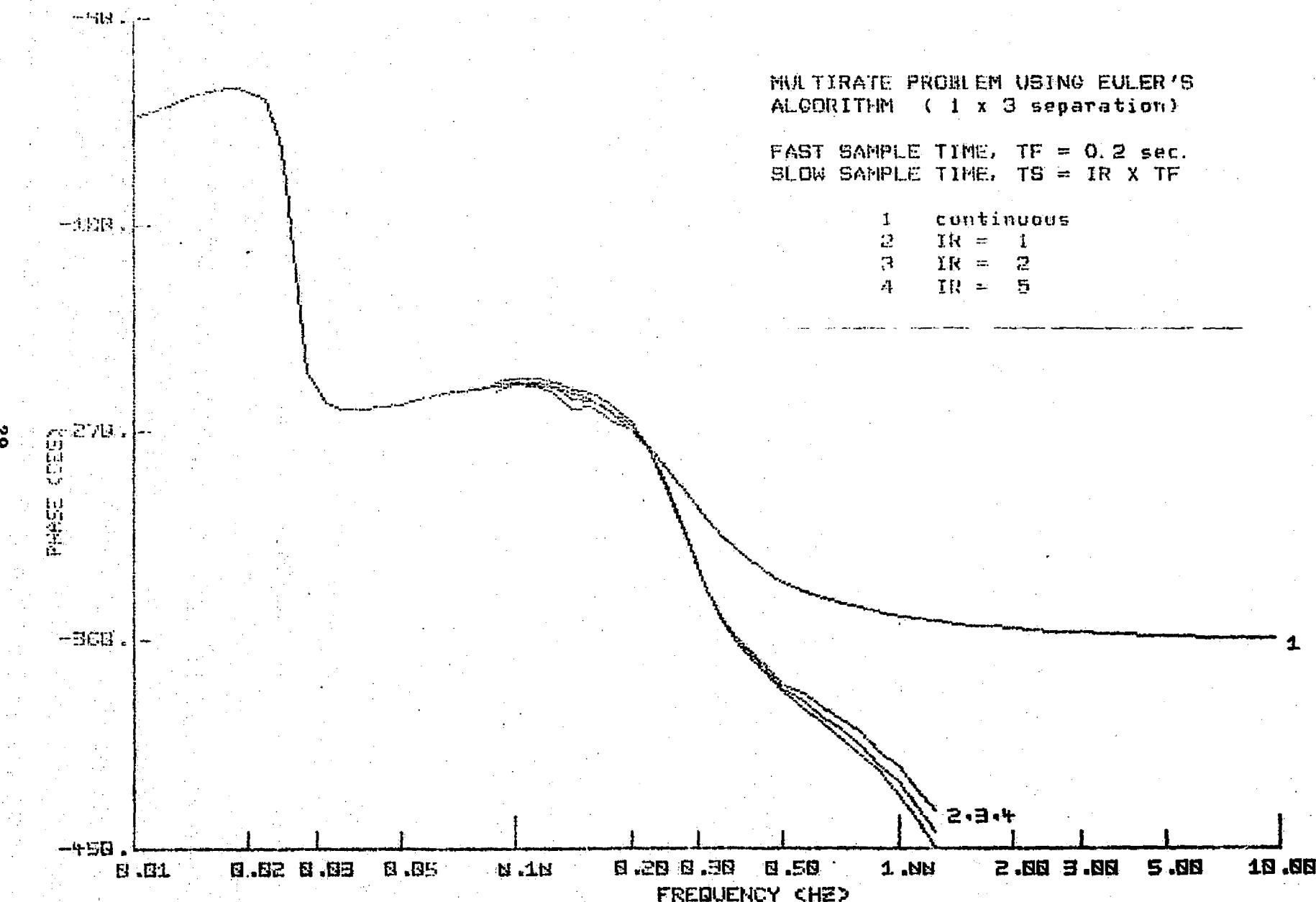


FIGURE 9b

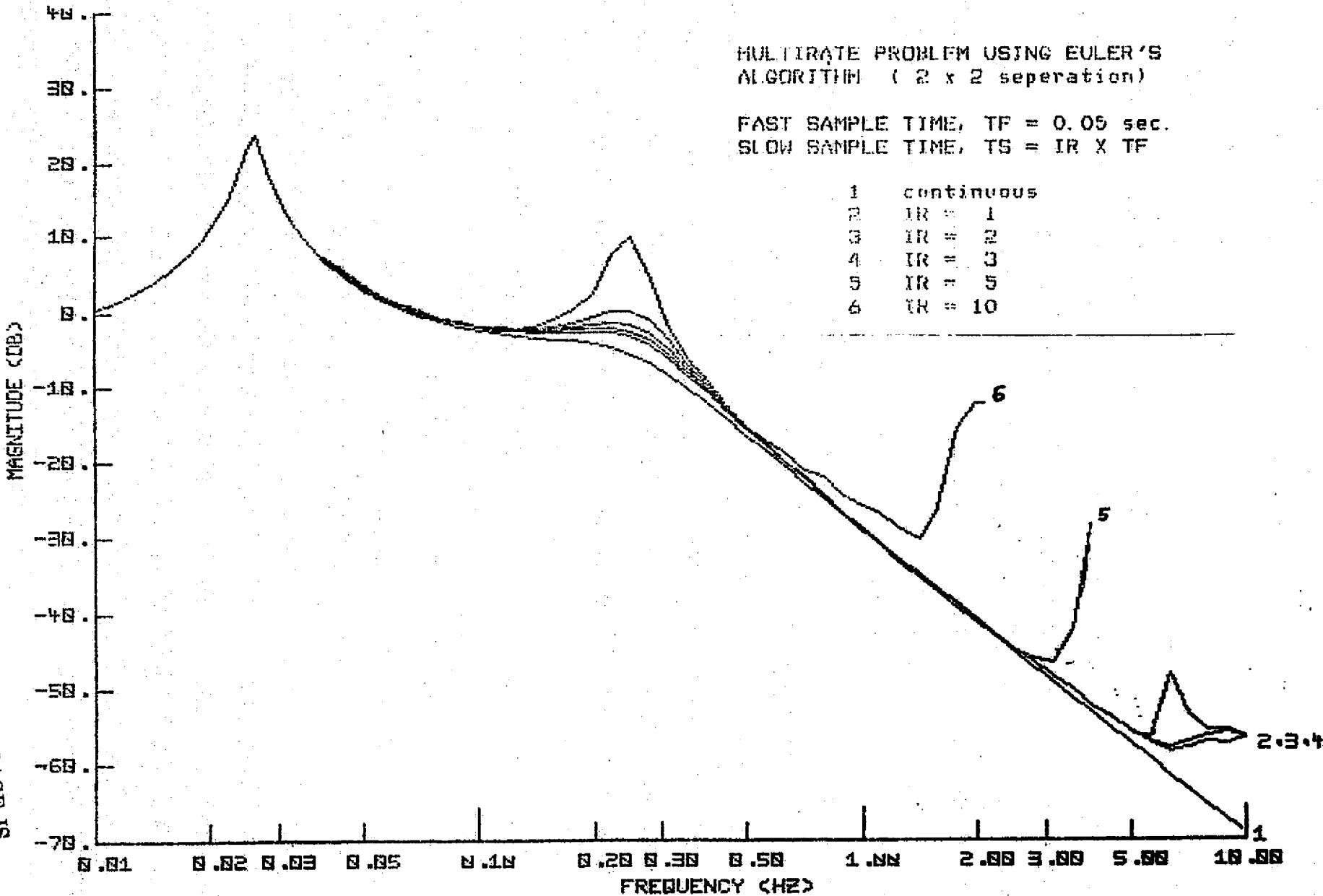


FIGURE 10a

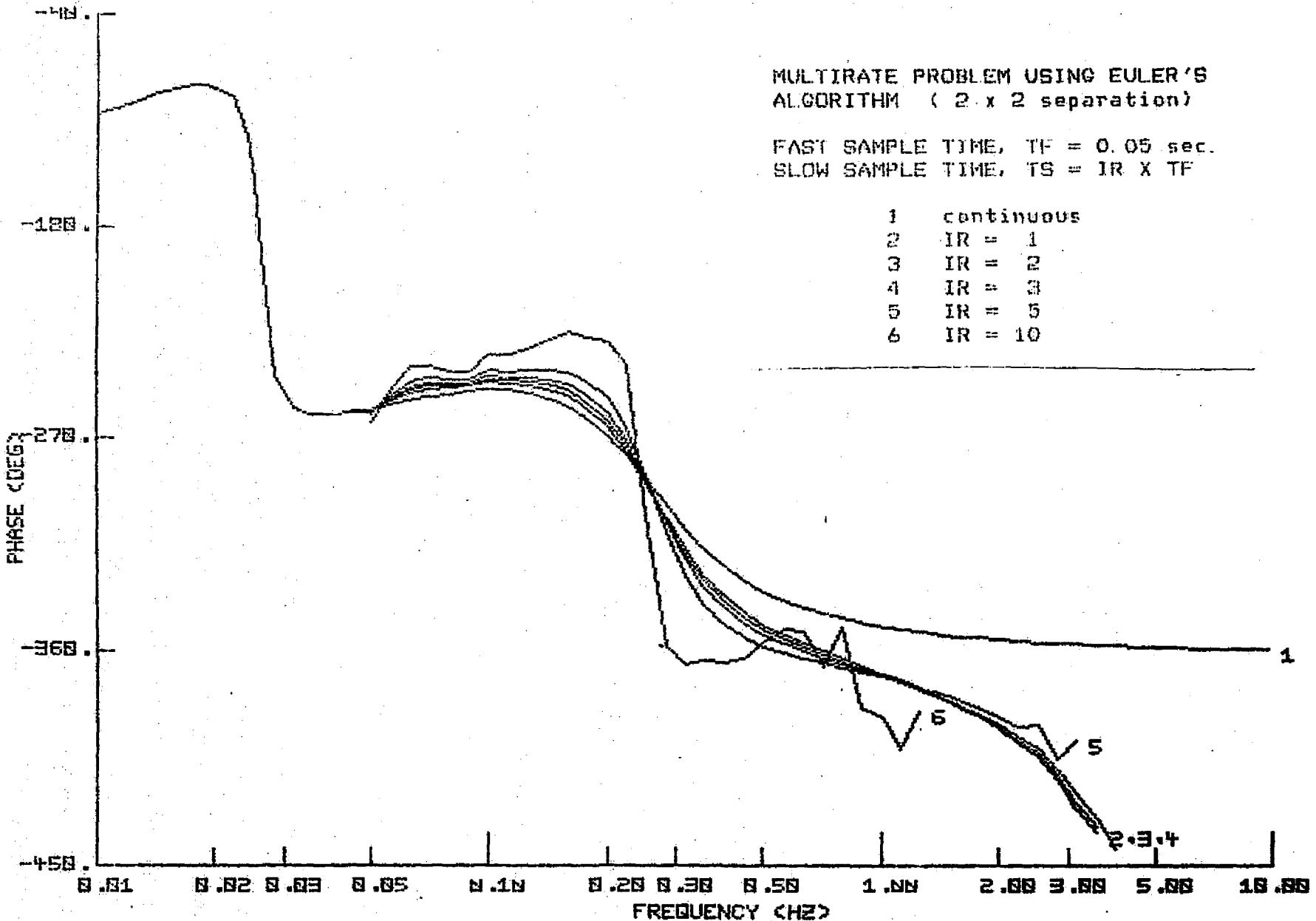


FIGURE 10b

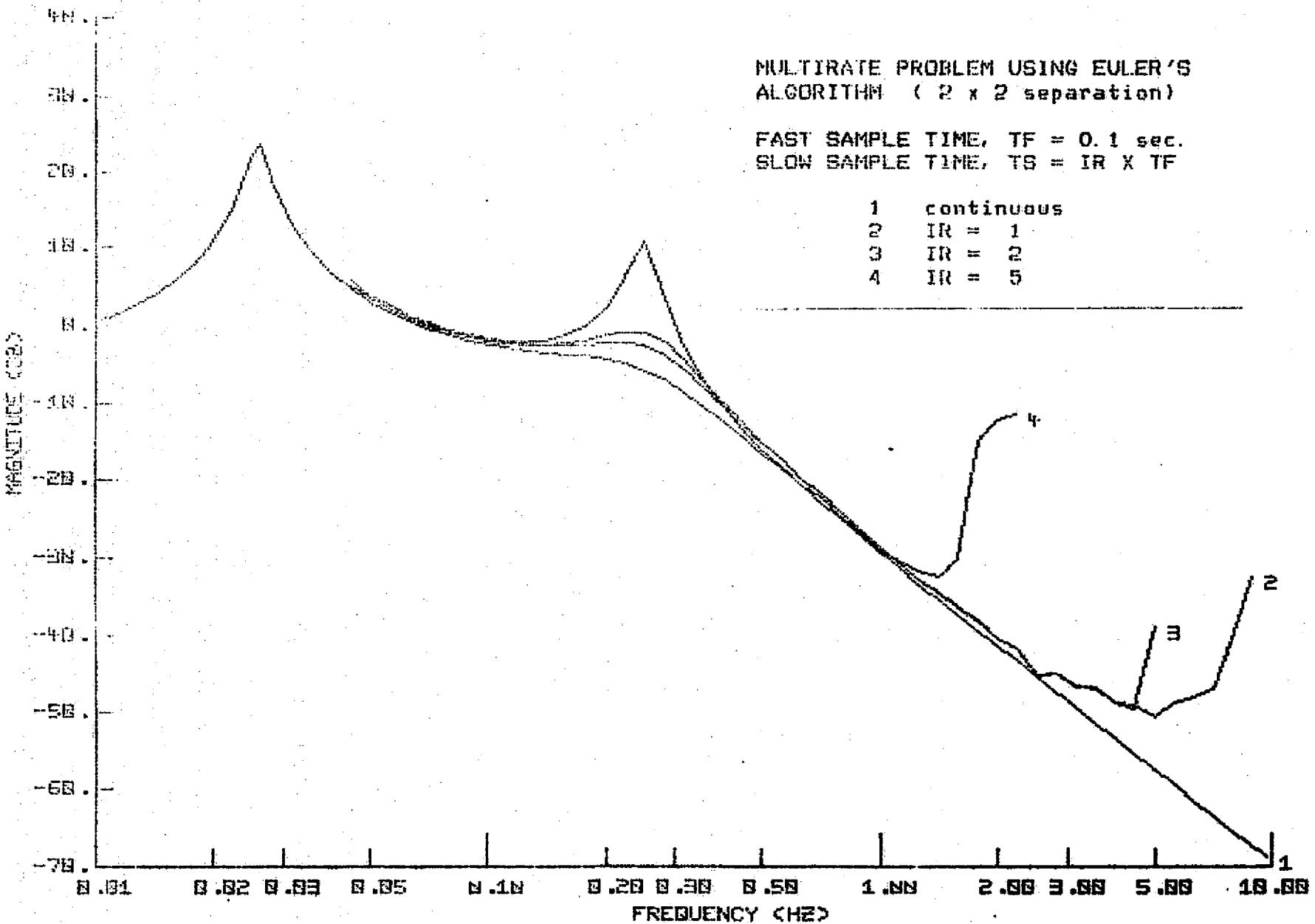


FIGURE 11a

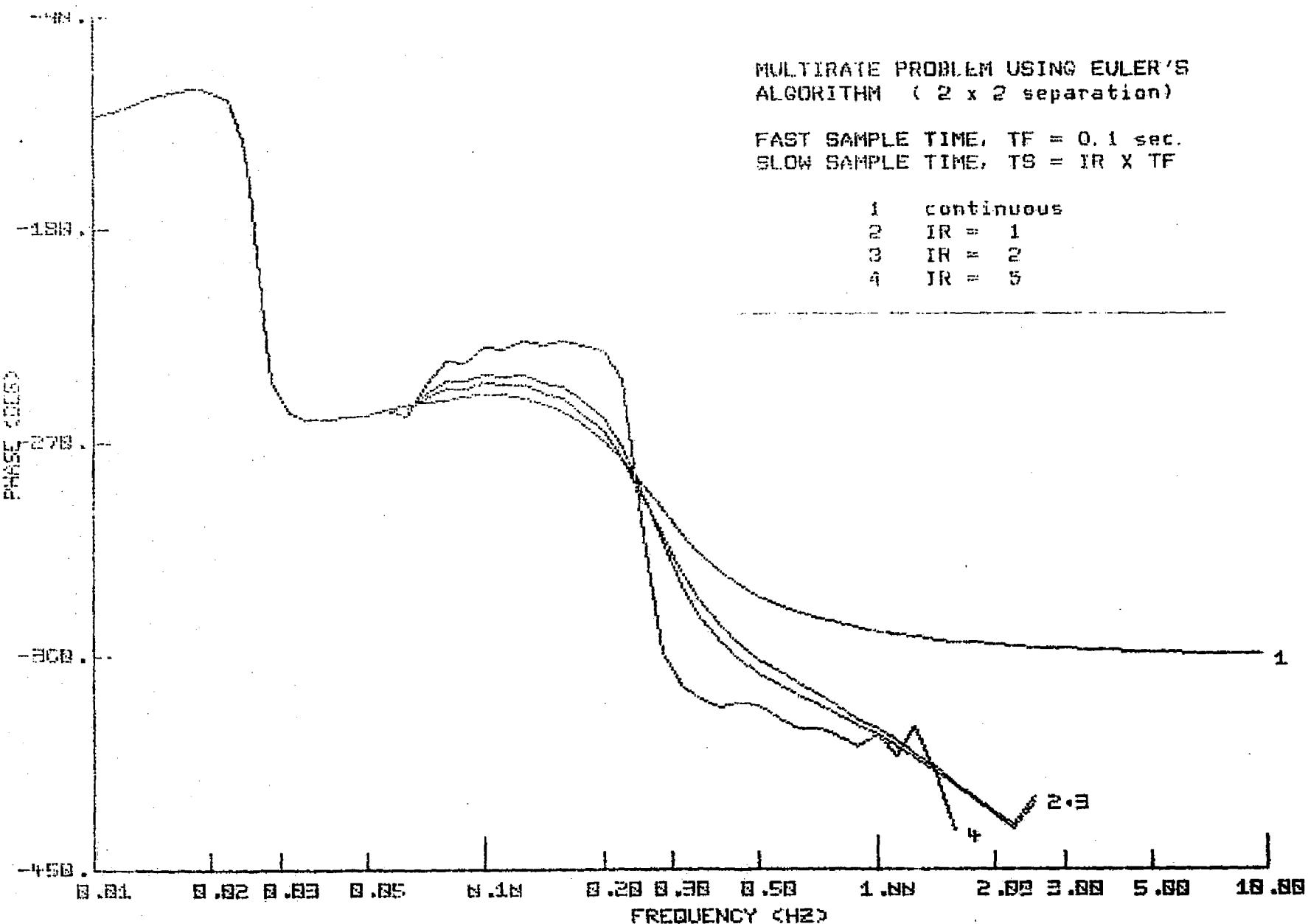


FIGURE 11b

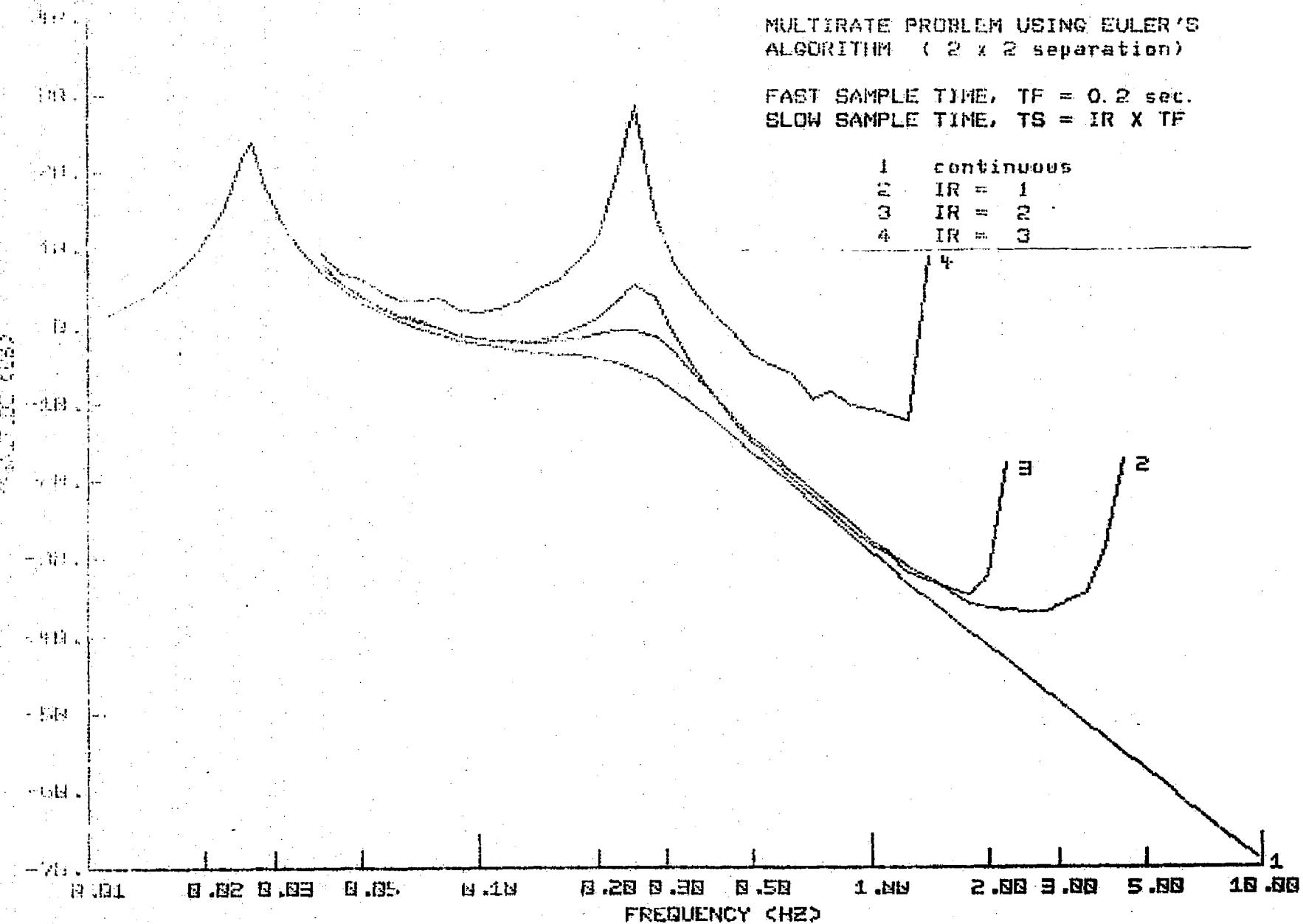


FIGURE 12a

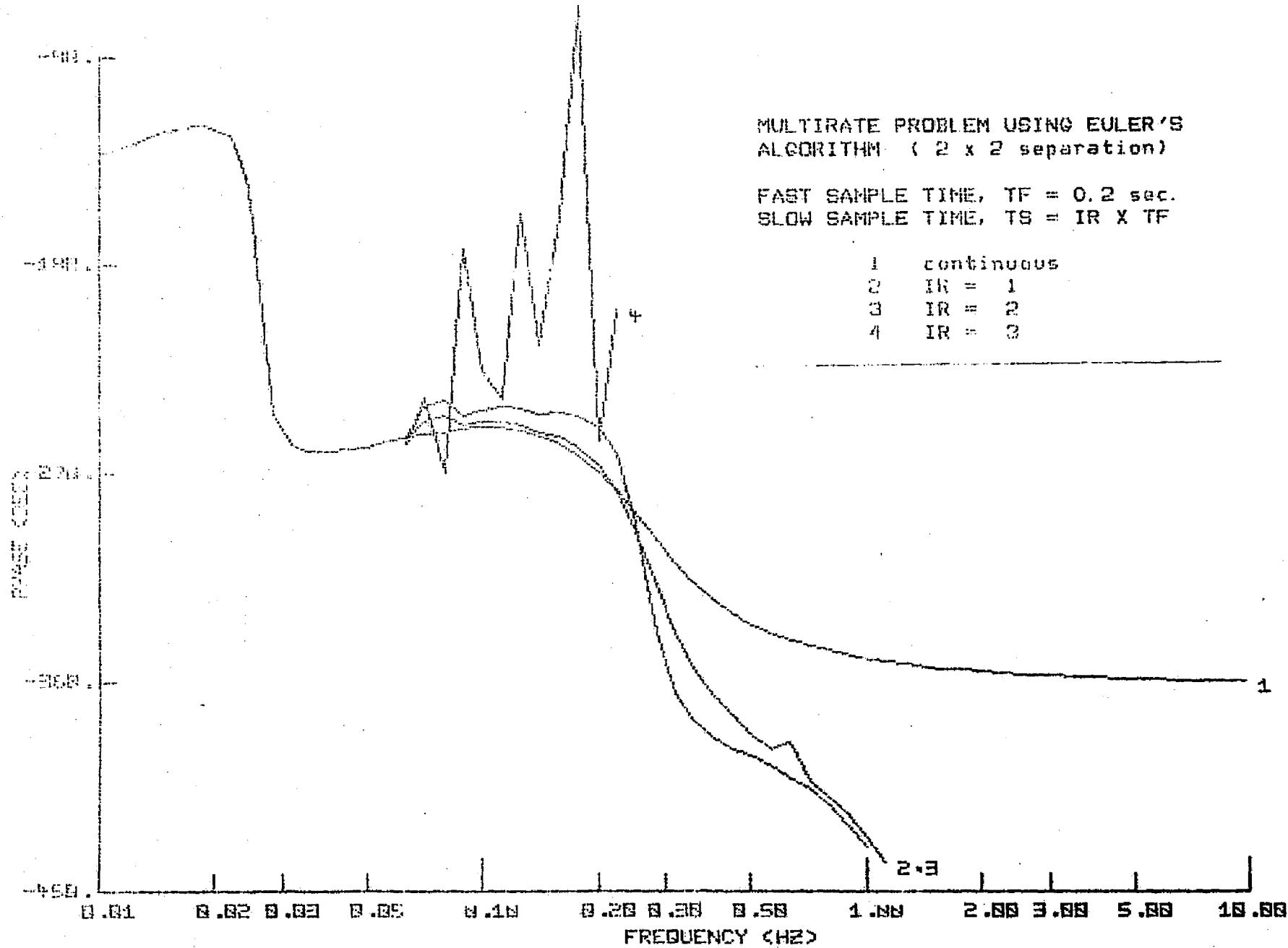


FIGURE 12b

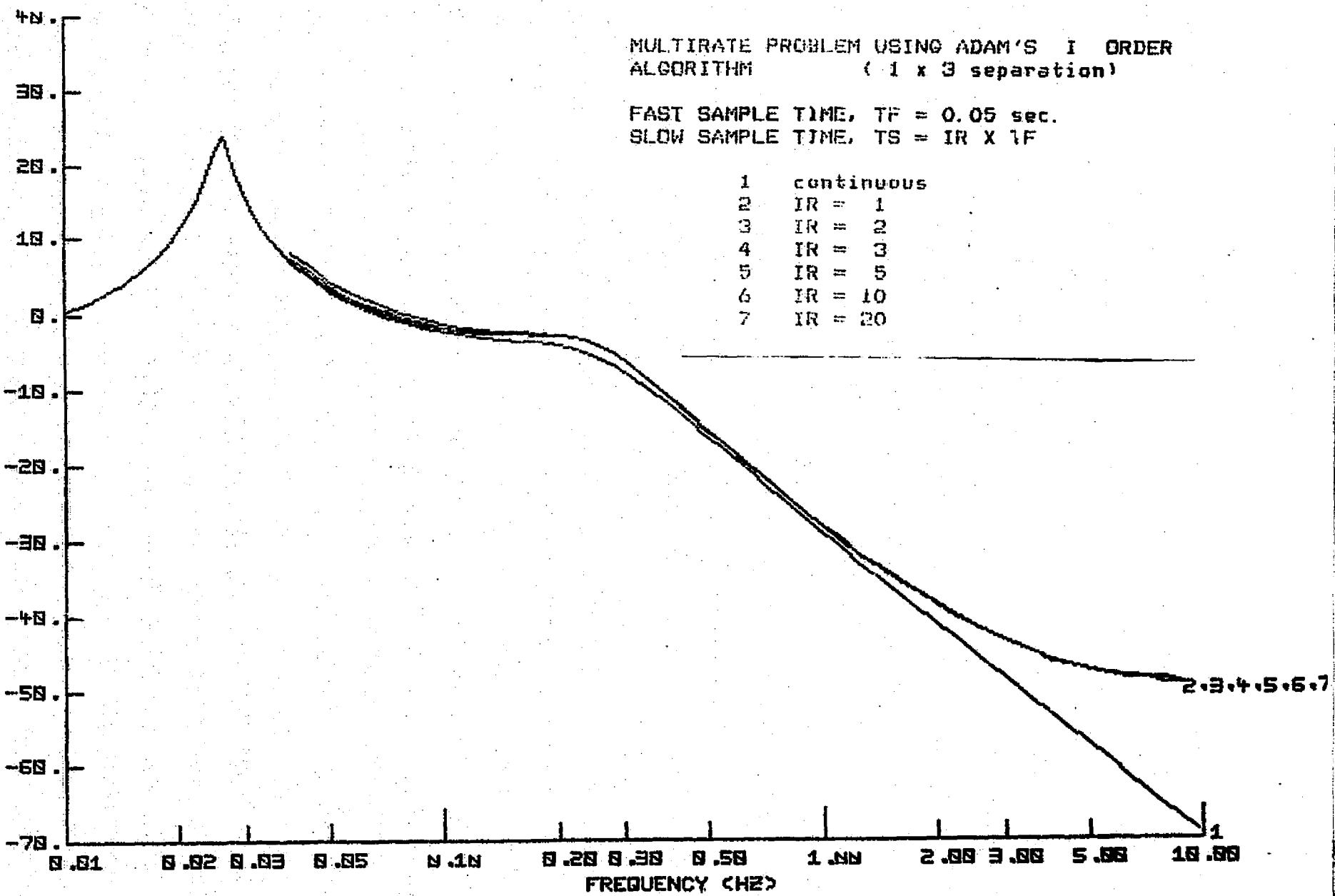


FIGURE 13a

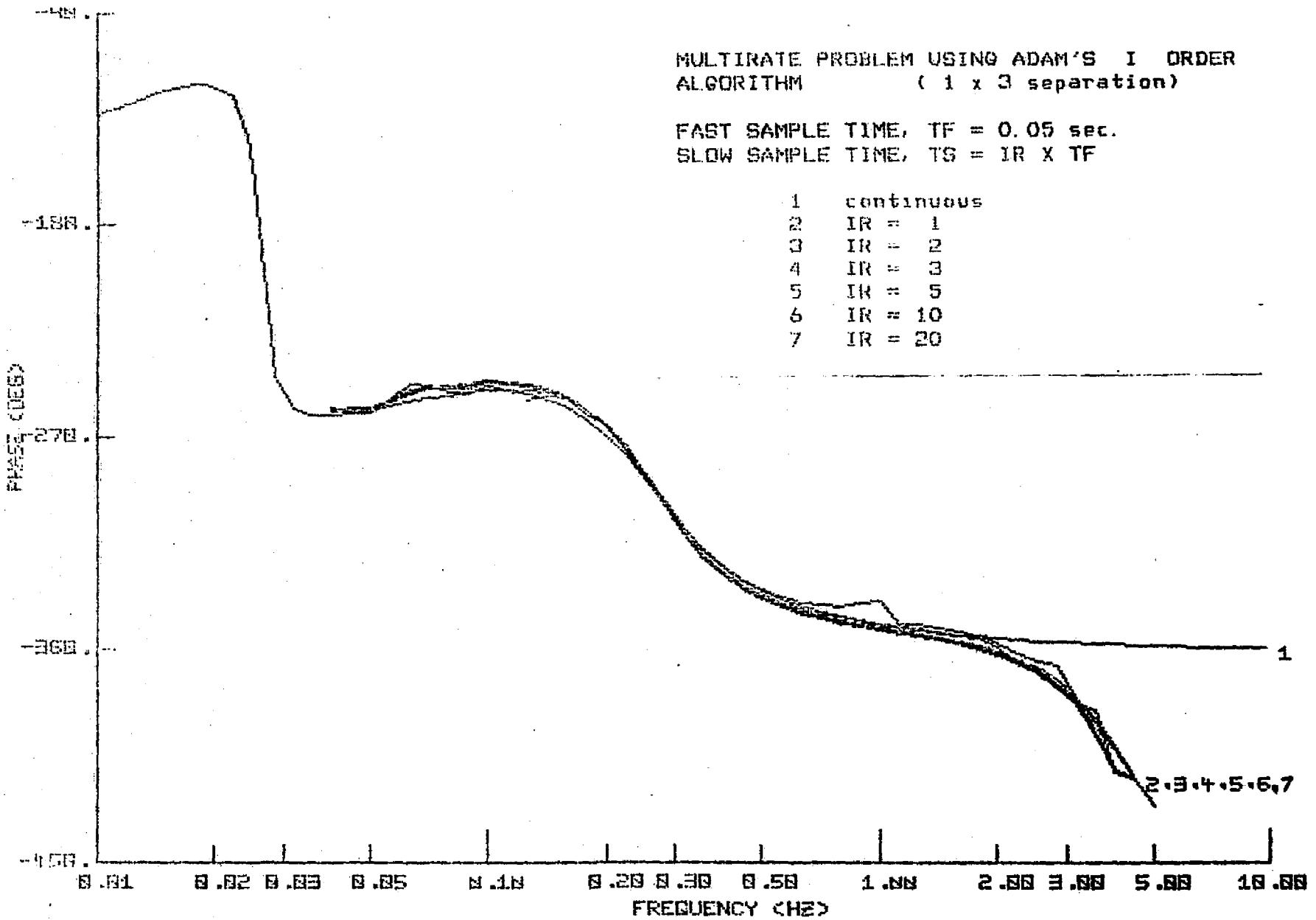


FIGURE 13b

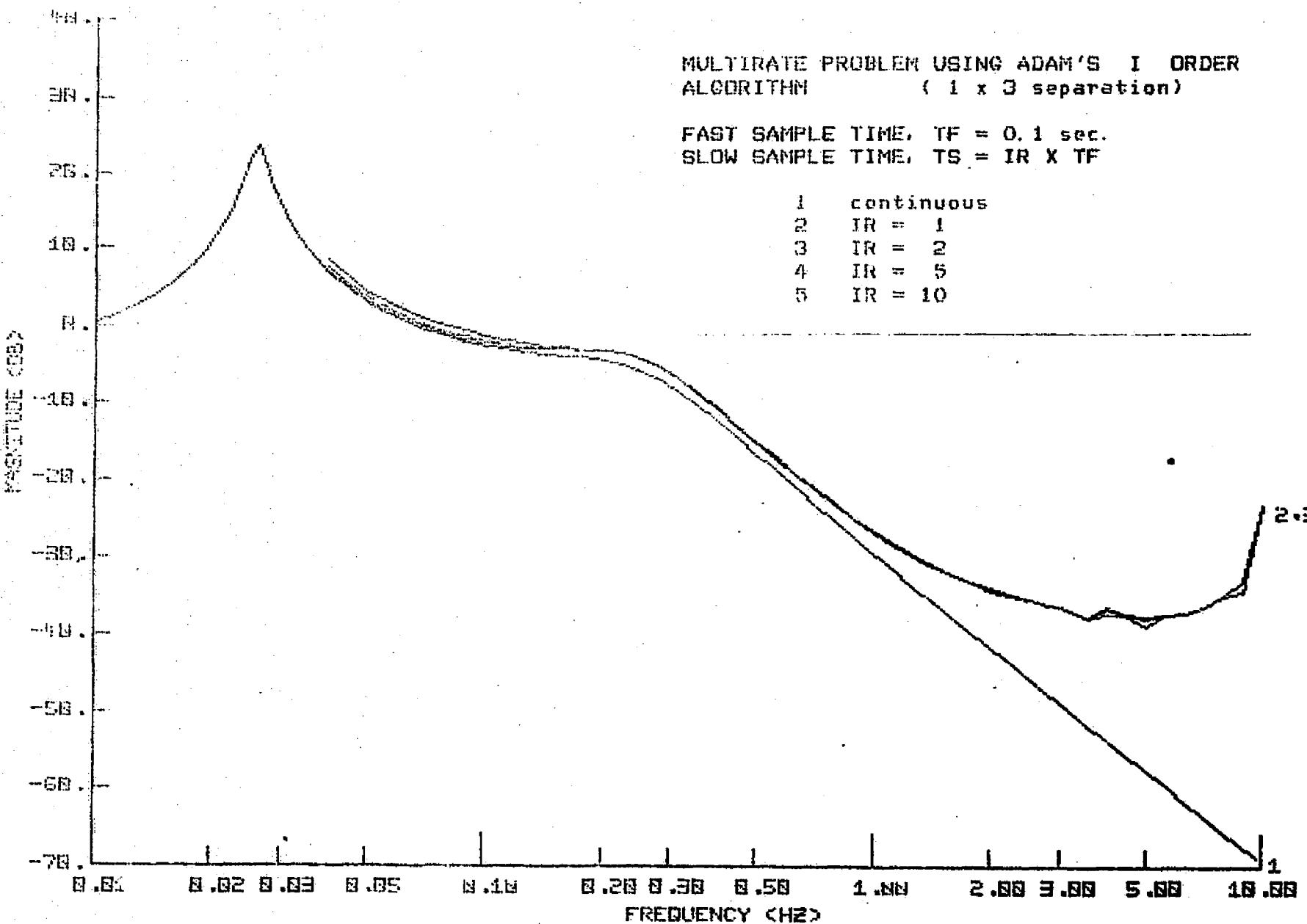


FIGURE 14a

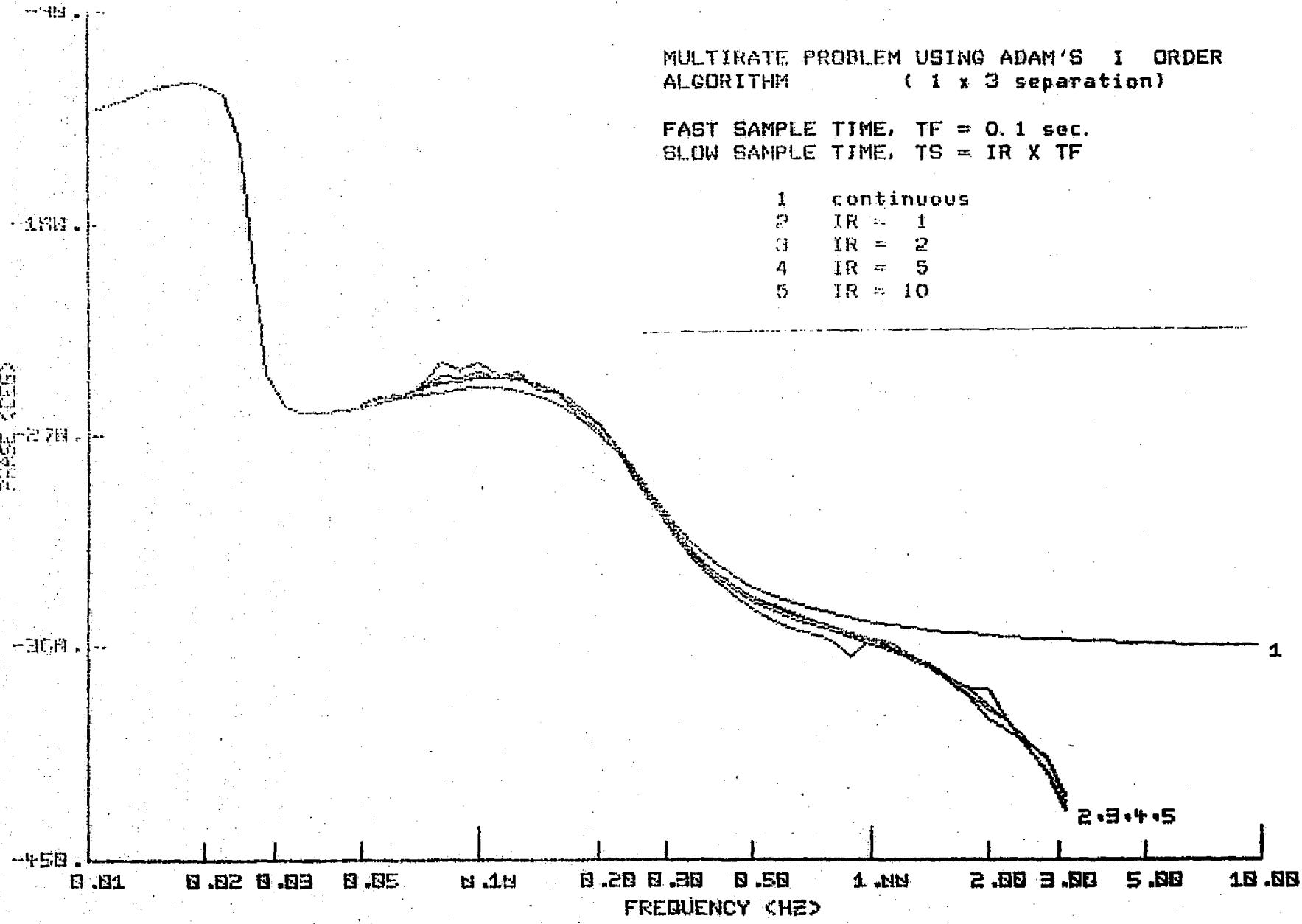
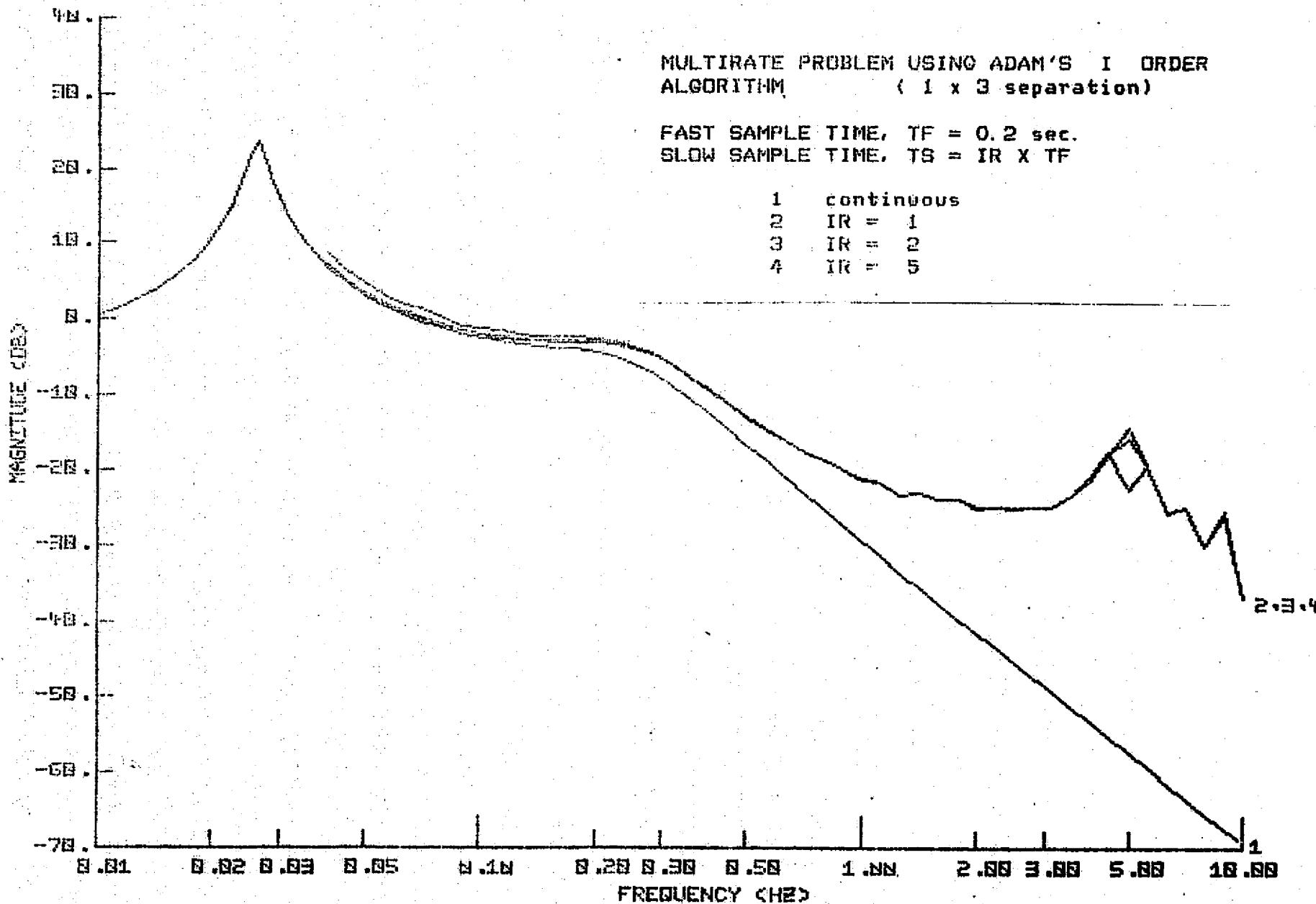


FIGURE 14b



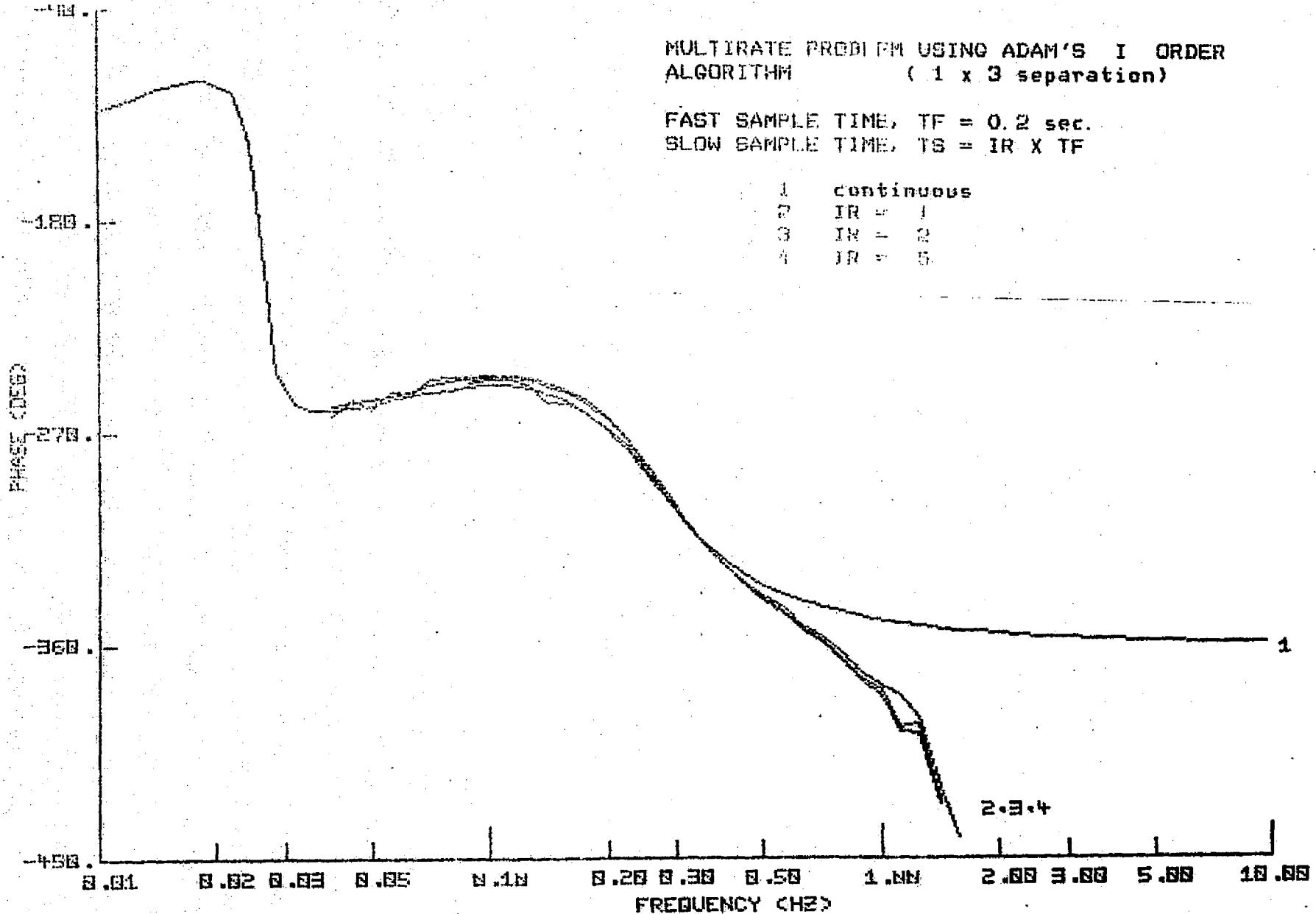


FIGURE 15b

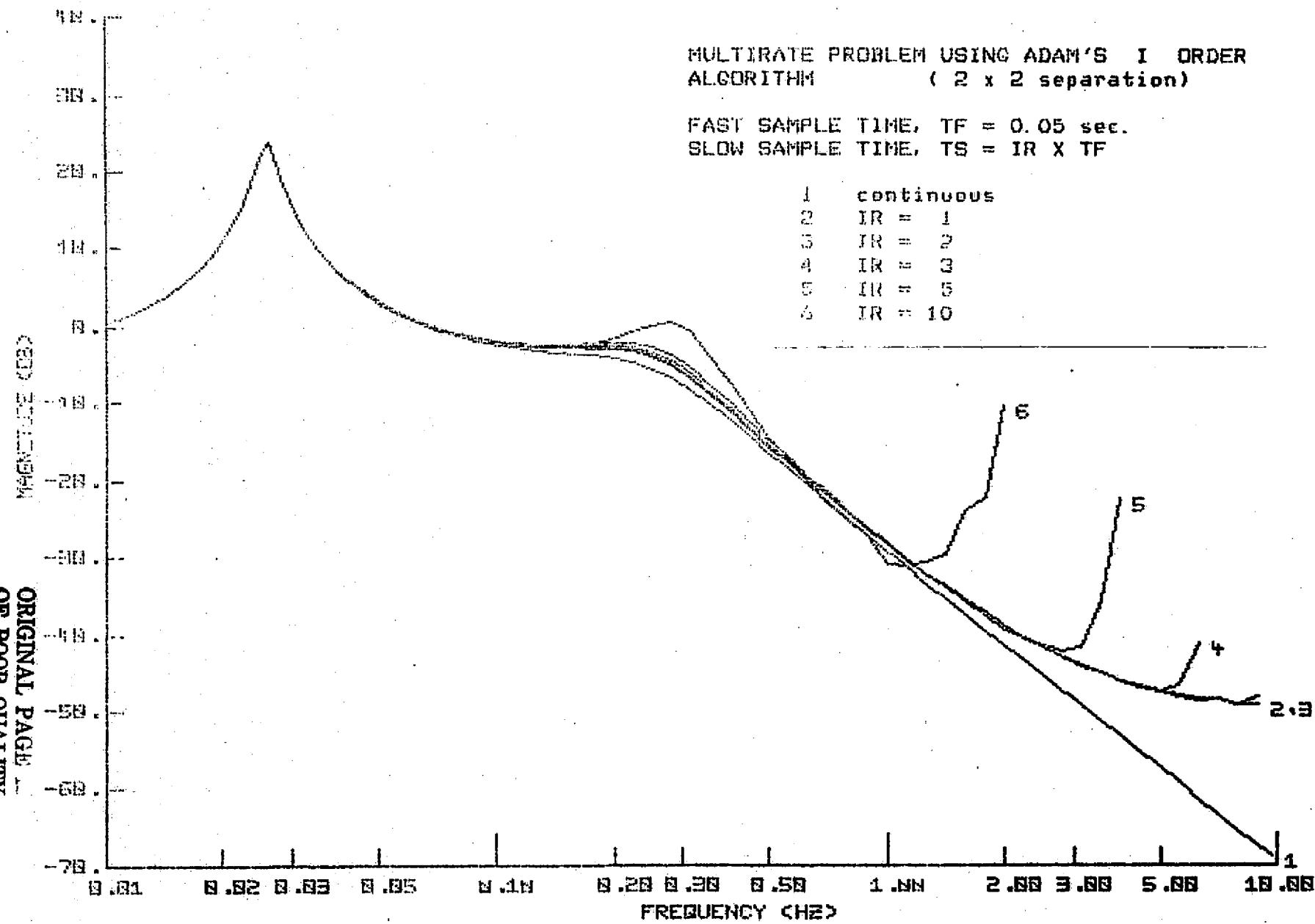


FIGURE 16a

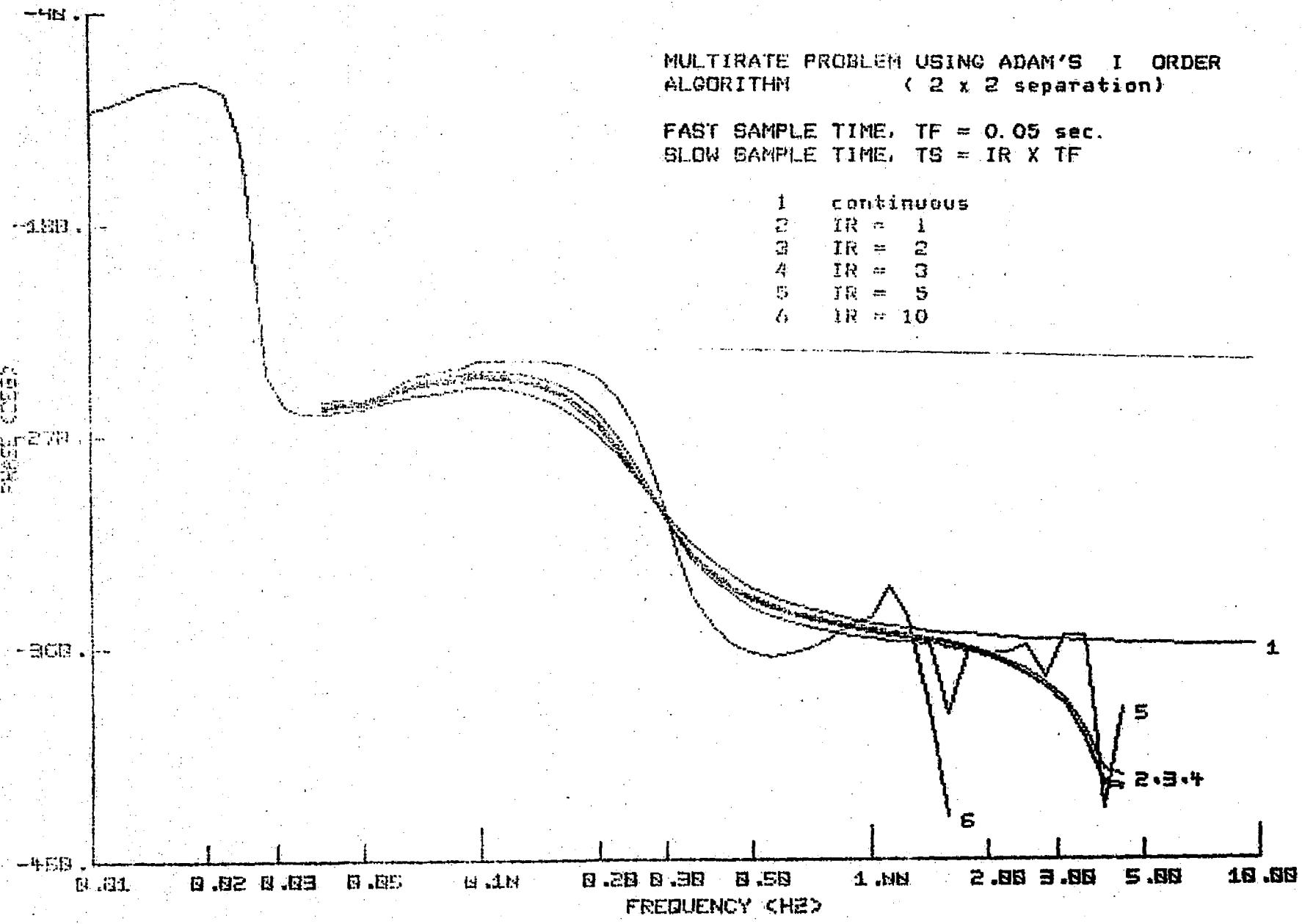


FIGURE 16b

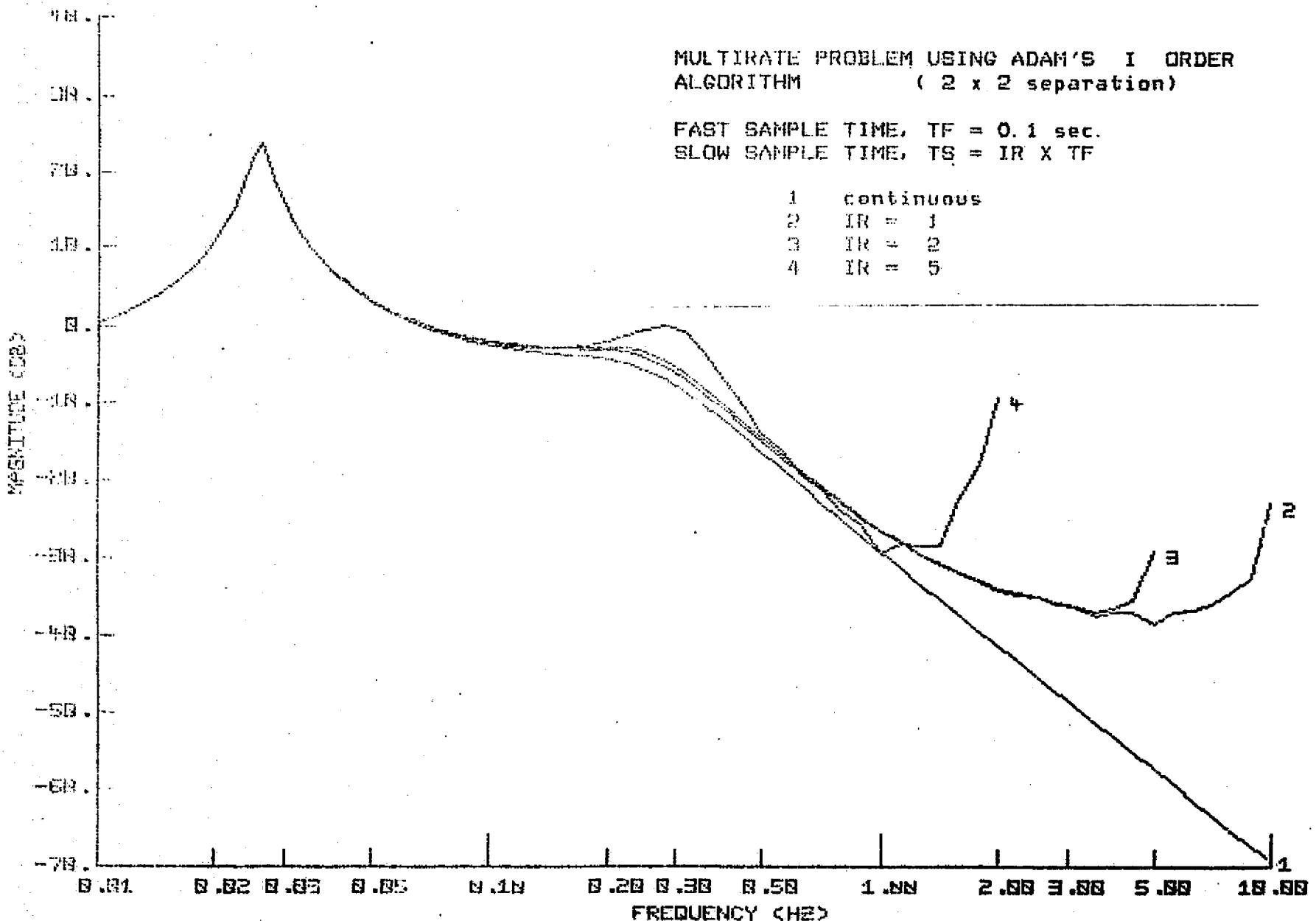


FIGURE 17a

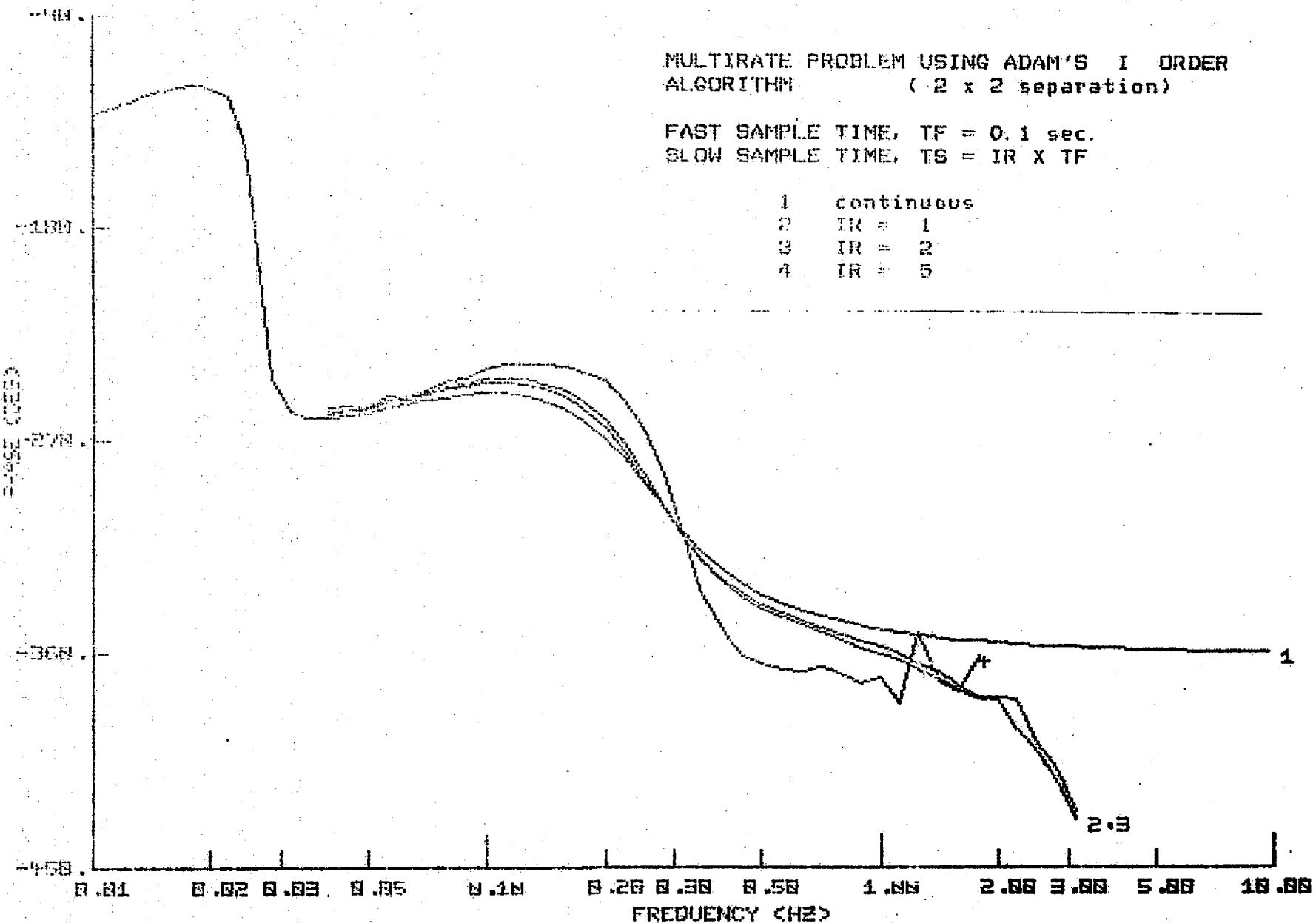


FIGURE 17b

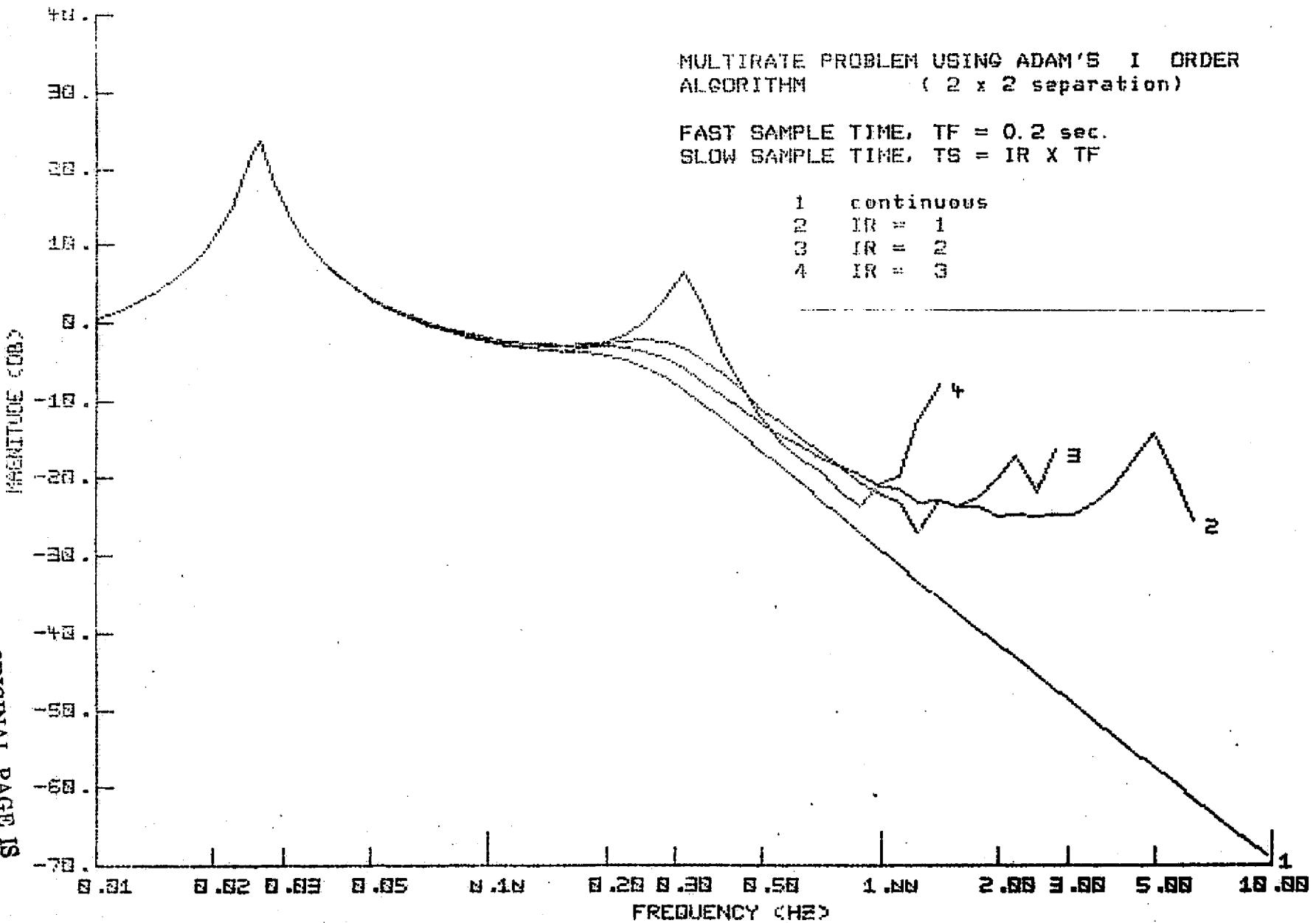


FIGURE 18a

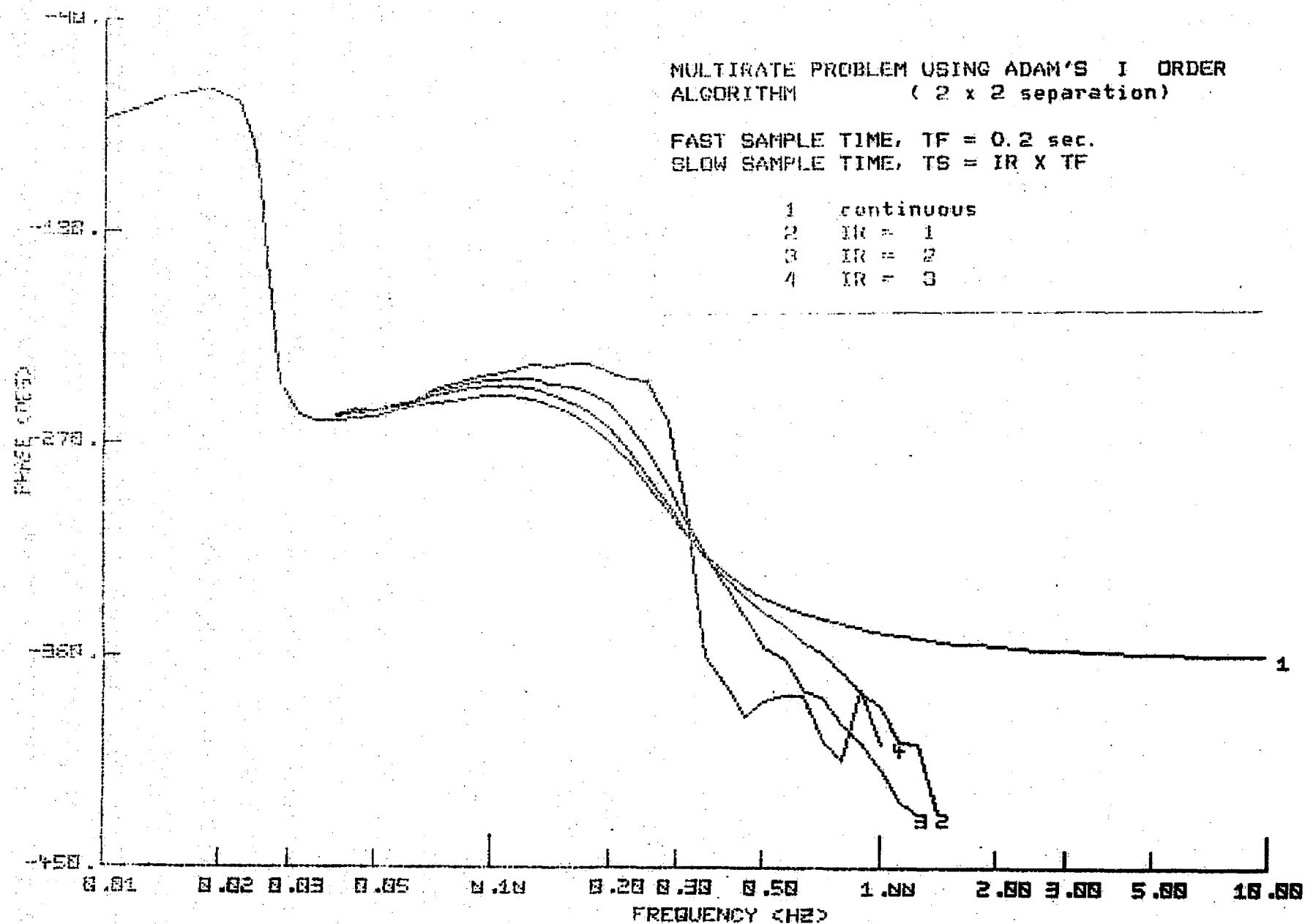


FIGURE 18b

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## APPENDIX A

### FREQUENCY RESPONSE EVALUATION OF EQUATION (4) (EULER'S INTEGRATION)

The following computer code was used to analytically evaluate a  $G(z)$  by letting  $z$  take on values around the unit circle. The coefficients stored  $A_1, A_2, \dots$  and  $B_1, B_2$  are for the continuous transfer function, equation (1) that represents the example described in this report. Lines 21 through 29 compute the coefficients required for an Euler integration of the continuous system.

```

!NATIVE
C GIVEN A TRANSFER FUNCTION IN THE Z-PLACE IN THE FOLLOWING FORM
C
C      M          N-1          N-2
C      B(N) Z + B(N-1) Z + B(N-2) Z + ..... + B(1) Z + B0
C      H(Z) = B(N) Z + B(N-1) Z + B(N-2) Z + ..... + B(1) Z + B0
C
C      N          N-1          N-2
C      C(N) Z + C(N-1) Z + C(N-2) Z + ..... + C(1) Z + C0
C
C THIS PROGRAM CALCULATES, TABULATES AND PLOTS THE FREQUENCY RESPONSE
C OF THE SYSTEM WHOSE TRANSFER FUNCTION IS GIVEN IN THE ABOVE FORM.
C
1      INTEGER OS2,3DP,NDP,CDP
2      REAL F(12),PNCD(25),SAMP(500),NAC(500),PHASE(500)
3      REAL+S,SAKKE,Z,B4,CB,A4,G1,G2
4      REAL+S A1,A2,A3,A4,G1,G2
5      REAL+S C1,C2,C3,C4,C5,C6,C7,C8,C9,C10,C11,C12,C13,C14,C15
6      REAL+D D11,D12,E1,E2,E3,E4,E5,E6,E7,E8,E9,E10,E11,E12,E13,E14,E15
7      LOGICAL LUSE(27),LORD(12)
8      DATA A1,A2,A3,A4/1.716922600,2.861367200,6.8971292600,3.070369500/
9      DATA B2,B1/C,0.032316750,0.533561/
10     READ(5,11)OS2,NDP
11     11 FORMAT(1Z12)
12     RUNG=0.
13     30 READ(5,12) SAMP,FAM,PHAM
14     12 FORMAT(F10.5,Z1(1K,F10.7))
15     1E-(SAMP-E..0+J*GL(3)-900
16     KNS=S-IUN5-1.
17     IF(RNS5.EQ.1) GO TO 53
18     WRITE(6,55)
19     55 FORMAT(1H1)
20     50 T = SAMP
C CONS IS THE CONSTANT (DE-AB) IN THE TRANSFER FUNCTION.
C THE COEFFICIENTS B0, B(I), C0, C(I) ARE THE COEFFICIENTS OF THE
C POLYNOMIALS IN THE TRANSFER FUNCTION OF (PHETA/DELTA)(s) I AS
C CALCULATED BY THE BY USING THE EULER'S METHOD. C'S ARE THE
C DENOMINATOR COEFFS. AND N'S ARE THE NUMERATOR COEFFS.
21     CONS = -1.338 * T ** 2
22     B0 = B2*T**2+B1*T+1
23     B(1) = B1*T**2
24     B(2) = 1.
25     C0 = A4*T**5+A3*T**3+A2*T**2+A1*T+E4
26     C(1) = A3*T**3+A2*T**2+A1*T+E4
27     C(2) = A2*T**2+A1*T+E4
28     C(3) = A1*T+E4
29     C(4) = 1.
30     WRITE(6,70) SAMP
31     14 FORMAT(//,T1,SAMPLE,EHE,E..,E12.5,/)
32     WRITE(6,65) B3
33     65 FGSHAF(' B0 = ',E21.6//)
34     DO 10 I=1,NDP,4
35     WRITE(5,13) 1,B(1),I+1,B(I+1),I+2,B(I+2),I+3,B(I+3)
36     13 FGSHAF(' B(I+1) = ',E18.6//)
37     10 CONTINUE
38     FGSHAF(' C0 = ',E21.6//)
39     75 FORMAT(' C0 = ',E21.6//)
40     DO 15 I=1,NDP,4
41     WRITE(5,15) 1,C(1),I+1,C(I+1),I+2,C(I+2),I+3,C(I+3)
42     15 FGSHAF(' C(I+1) = ',E18.6//)
43     15 CONTINUE

```

```

C
C
C   COMPUTE THE AREA OF FIRE VEHICLES FOR HIRE (LOS SCALE . . .)
44   133 CONTINUE
45       FEISLG = ALDG10 (VALM)
46       LGEMIN = FEISLG
47       IF ( FMIN .LT. 1. ) LGEMIN = LSPMIN = 1
48       IDEC = LGEMIN
49       ED_131_I = 1, 20
50       LGEND(I) = .FALSE.
51   131 FNOR(I) = 10, ** ((I-1)/20, )
52       LGEND(1) = .FALSE.
53       LGEND(7) = .TRUE.
54       LGEND(15) = .TRUE.
55       NE = 1
56       I = (FEISLG - LSPMIN)*20 + 1,5
57   133 FACT = 10, ** IDEC
58   135 X(MF) = PIACTMAGE(MF)
59       LGEND(MF) = LGEND(I)
60       IF ( F(MF) .GE. FAIR ) GOTO 137
61       I = 1, 20
62       MF = MF + 1
63       IF ( I .LE. 20 ) GOTO 135
64       I = 1
65       IDEC = IDEC + 1
66       GO TO 133
67   137 KBFQ = MF - NE
C
C
68       F(69) = C.0241916
69       E(10) = D.0261010
70       NBFQ = NBFQ + 2
C
71   CALL PGNAME(OHP,1DP,B,C,C033,B1,E)
72   CALL UNICIE(OHP,OHP,B,C,C033,SMPV,F,00,C0,SAIM,PIASE)
73   I1=75
74   RANGE M,I1
75   GO TO 30
76   990 CONTINUE
77   STOP
78   END
C
79   SUBROUTINE FOLWEL(OHP,1DP,B,C,C033,1D,CD)
C
80   INTEGER OHP,1DP,C033,B,C,C033,1D,CD
81   REAL = B(1D),C(1D),B(3D),C(3D)
82   CHARACTERS B(1)*1*(23)/20**1/,B(2)*15(20)/20**1/,/
83   A(1)*1*B(2)*2(21)/20**1/,B(3)*15(20)/20**1/,/
84   B(4)*1.00001(21)/20**1/,B(5)*15(20)/20**1/,/
85   A(6)*1.6,200
86   200 FOPEN(11,'TRANSFER FORCFLN : ','')
87   IF (OHP.EQ.1) GO TO 233
88   WRITE (6,201) CONS
89   231 FORMAT(1X,A12.5/' B(1) = ',1X,A12.5/' ')
90   GO TO 215
91   205 TOMP = CD9
92   K1CEP = CD9 + 1
93   IF (OHP.EQ.1) GO TO 212
94   DO 210 I = 1, OHP
95   WRITE (OHP(1),231) TOMP
96   211 FORMAT(12)
97   IF (B(1OHP).LT.0.) GO TO 250
98   WRITE (OHP(1),231) B(1OHP)
99   231 FOPEN(11,A12.5,'X1',1X)
100  250 GO TO 152
101  230 FORMAT(1X,A12.5,'X2',1X)
102  252 TOMP = TOMP - 1
103  210 CONTINUE
104  212 WRITE (OHP(1),231) TOMP
105  271 FORMAT(12)
C
106  623 M = 1
107  K82 = 6
108  DO 225 J = 1, OHP, 6
109  K1CE1(6,255) = B(1CE1(KJ)), KN = 1, K1CE1(KJ)
110  255 FORMAT(20A1,6(1X,A2))
111  K1CE2(6,270) = B(1CE2(KJ)), KN = K1CE1(KJ),K1CE2(KJ)
112  270 FORMAT(20X,6A16/)
113  K1CE1 = K1CE1 + 6
114  225 K82 = K82 + 6
115  K1CE2 = 5,250,1,CD,5
116  290 FORMAT(' H(2) = ',A12.5,'*',100(' '))
117  215 TOMP = OHP
118  TOMP = OHP + 1
119  IF (OHP,EQ.1) GO TO 245
120  DO 240 I = 1, OHP
121  WRITE (OHP(1),231) TOMP
122  285 FORMAT(12)
123  IF (C(230P).LT.0.) GO TO 237
124  K1CE1(LUPN(1),232) = B(1CE1(KJ))
125  232 FORMAT(A1,A12.5,'*',4D,1X)
126  GO TO 238
127  207 WRITE (LUPN(1),230) C(230P)
128  208 TOMP = TOMP - 1
129  240 CONTINUE
130  206 WRITE (BUPN(CMDDP),271) CD
131  254 FORMAT(25X)
132  254 FORMAT(25X)
C

```

```

133      KN1 = 1
134      KN2 = 6
135      DC,235 = 1,202, 6
136      4E12(6,255) DURKY, (DUF)(KN), KN = KN1,KN2)
137      4E12(6,270) (DUF)(KN), KN = KN1,KN2)
138      KN1 = KN2 = 6
139      235 KN2 = KN2 + 6
140      RETURN
141      END

142      SUBROUTINE USECIF(DNP,DNP,B,C,CDNS,SAMP,SYFF2,F,87,C),
      GAI8,SAU,PHASE)
      C
      C
143      INTEGER,CFP,DNP,CFP8
144      REAL GAIN(500),M13(30),FDNS(5),F(121)
145      REAL*B 80,LC,SAMP,CDNS,B(30),C(30)
146      REAL*D XT,YZ,DL3G12,DL3A12,MOL2
147      COMPLEX ICRES
148      COMPLEX*16 DCMPLEX,CNU1,COSN,CNS,LA,CA,CD
149      PI = 3.1415926

150      TPI = 2*PI*SAMP
151      DEGPI = 180. / PI
152      LD_1CD_1 = 1, MFLG
153      100 PHASE(J) = C
154      127 (CCNS,SE,0) GO TO 185
155      LD_1CD_1 = 1, MFLG
156      190 PHASE(J) = -180.
157      185 *XITE(6,125)
158      125 201=1//,2LY,1E4AUXCY(KN) 1,14X,1E187,15X,1E187,15X,1E187,15X,
      111,*PHASE(DNP)*,//
      X
159      LD_100_MF = 1, MFLG
160      CDNA = DCMPLEX(B0,1,DCD)
161      CDEN = DCMPLEX(CC,1,DCD)
162      OMEGAT = F2PI * Y(N)
163      AT = DULE(CLS(D,REGD))
164      VT = DULE(CLH(D,REGD))
165      Z = DCMPLEX(AT,VT)
166      IL_(OMA+OMA-B) = 0.23*PI
167      CN = Z
168      DO 110 I = 1,302
169      CN=CN*(B(I)-V,CN)
170      CN = CN + Z
171      110 CONTINUE
172      105 PE(GD2,EG,0) GO TO 113
173      CD = 2
174      DO 120 I = 1,302
175      CDSD = CDEN*I + CD
176      CD = CD + Z
177      120 CONTINUE
178      115 ICRES = CN*CD / CD2
179      CRCS = CGNS = (CN*CD/CDEN)
180      GAIA(MF) = CDNS(CRCS)
181      RAG(MF)=23.4E0312*(CDNS(CRCS))
182      PHASE(SF)=PHASE(SF)+1E-12*PI*ATAN2((ALIAS(ICRES),REAL(2CRCS)))
183      WRITE(6,150) MF,I(LP),I(17),I(18),I(19),I(20),PHASE(SF)
184      150 FORMAT(3X,12,9X,F12.5,1(12,X,F12.7))
185      100 CONTINUE
186      RETURN
187      END

```

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## APPENDIX B

FREQUENCY RESPONSE EVALUATION OF EQUATION(6)  
(1st ORDER ADAMS)

The computer code in Appendix A was modified by replacing lines 21 through 29 with the following coefficient evaluations.

```

21      CONS = -1.338
22      C1 = 81*T**3
23      C2 = -168*T**4
24      C3 = 54*T**4
25      C4 = -12*T**4
26      C5 = T**3
27      D1 = 16.
28      D2 = 24*A1*T-54
29      D3 = 36*A2*T**2-80*A1*T+96
30      D4 = 50*A3*T**3-96*A2*T**2+36*A1*T-54
31      D5 = 81*A4*T**4-103*A3*T**3+68*A2*T**2-48*A1*T+16
32      D6 = -108*A4*T**5+55.72*A3*T**4-3-32*A2*T**3+6*A1*T
33      D7 = 54*A4*T**4-20*A3*T**3+4*A2*T**2
34      D8 = -12*A4*T**4+2*A3*T**3
35      D9 = 14*T**4
36      G1 = 4.
37      G2 = 6*B1*T-8
38      G3 = 9*B2*T**2-3*B1*T+4
39      G4 = -6*B2*T**2+2*B1*T
40      G5 = B2*T**2
41      K1 = 9*T**2
42      K2 = -6*T**2
43      K3 = T**2
44      B0 = C5*G5
45      B(1) = C4*G5+C5*G4
46      B(2) = C3*G5+C4*G4+C5*G3
47      B(3) = C2*G5+C3*G4+1.3*C5*G2
48      B(4) = C1*G5+C2*G4+C3*G3+C0*G2+C5*G1
49      B(5) = C1*G4+C2*G3+C3*G2+C4*G1
50      B(6) = C1*G3+C2*G2+C3*G1
51      B(7) = C1*G2+C2*G1
52      B(8) = C1*G1
53      C0 = D8*K3
54      C(1) = D8*K3+D9*K2
55      C(2) = D7*K3+D8*K2+D9*K1
56      C(3) = D6*K3+D7*K2+D8*K1
57      C(4) = D5*K3+D5*K2+D7*K1
58      C(5) = D4*K3+D5*K2+D6*K1
59      C(6) = D3*K3+D9*K2+D5*K1
60      C(7) = D2*K3+D3*K2+D4*K1
61      C(8) = D1*K3+D2*K2+D3*K1
62      C(9) = -0.1*K2+D2*K1
63      C(10) = D1*K1

```

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## APPENDIX C

### FREQUENCY RESPONSE EVALUATION OF EQUATION (8) (2nd ORDER ADAMS)

The computer code of Appendix A was modified by replacing lines 21 through 29 with the following coefficient evaluations.

```

21      C0BS = -1.338
22      C1 = 275.941*1**4
23      C2 = -776688*1**3
24      C3 = 1755804*1**3
25      C4 = -884672*1**3
26      C5 = 498156*1**3
27      C6 = -192320*1**3
28      C7 = 49303*1**3
29      C8 = -800041*1**3
30      C9 = 625*1**3
31      D0 = 2(736.
32      D1 = .32744*1**2-82.949
33      D2 = 76.176*1**2-146.800*A1*T+120.115
34      D3 = 146.004*A3**3-238.135*A2*T**2+213.615*A1*T-829.94
35      D4 = 273.84194*1**4-452.703*A3*T**3+353.123*A2*T**2-13.6603*A1*T
36      D5 = -778688*A0*T**4+451.169.2*A3*T**3-26.692*A2*T**2+53568*A1*T**2
37      D6 = -10555864*A4*T**4-12082.1*A3*T**3+115634*A2*T**2-35542*A1*T**2
38      D7 = -684672*A4*T**3+246412*A3*T**3-32243*A2*T**2
39      D8 = 498156*A4*T**4-81160*A3*T**3+3.01*A2*T**2
40      D9 = -192320*A4*T**3+1329.253*A3*T**3
41      D10 = 49303*A4*T**4-1530*A3*T**3
42      D11 = -60304*A4*T**4
43      D12 = .25*1**4
44      G1 = 144
45      G2 = 276*81*T-280
46      G3 = .529*82*T**2-468*11*T+108
47      G4 = -736*82*T**2+2329.81*T
48      G5 = 486*82*T**2-60*81*T
49      G6 = 160*82*T**2
50      G7 = 25*82*T**2
51      K1 = 57.9*1**2
52      K2 = -72.6*T**2
53      K3 = 48.6*T**2
54      K4 = -15.0*1**2
55      K5 = .25*T**2
56      K6 = C5*G7
57      B(1)=C6*G7+C8*G5+C9*G6
58      B(2)=C7*G7+C8*G5+C9*G6
59      B(3)=C6*G7+C7*G5+C8*G6+C9*G6
60      B(4)=C5*G7+C9*G6+C7*G5+C8*G6+C9*G6
61      B(5)=C4*G7+C1*G6+C5*G5+C6*G4+C7*G3+C8*G2+C9*G1
62      B(6)=C3*G7+C4*G6+C5*G5+C6*G4+C7*G3+C8*G2+C9*G1
63      B(7)=C2*G7+C3*G6+C4*G5+C5*G4+C6*G3+C7*G2+C8*G1
64      B(8)=C1*G7+C2*G6+C3*G5+C4*G4+C5*G3+C6*G2+C7*G1
65      B(9)=C1*G6+C2*G5+C1*G4+C4*G3+C5*G2+C6*G1
66      B(10)=C1*G5+C2*G4+C3*G3+C4*G2+C5*G1
67      B(11)=C1*G4+C2*G3+C3*G2+C4*G1
68      B(12)=C1*G3+C2*G2+C3*G1
69      B(13)=C1*G2+C2*G1
70      B(14)=C1*G1
71      G8 = D12*K3
72      C(1)=D11*K5*D12*K4
73      C(2)=D11*K5*D11*K4*D12*K3
74      C(3)=D5*K5*D10*A1*D11*T*X3*D12*K2
75      C(4)=D8*K5*D9*A1*D10*T*X3*D11*K2+D12*K1
76      C(5)=D7*K5*D8*K4*D7*K3*D10*A2*D11*K1
77      C(6)=D5*K5*D7*K4*D7*K3*D6*K2*D11*K1
78      C(7)=D5*K5*D5*K4*D7*K3*D6*K2*D9*K1
79      C(8)=D5*K5*D5*K4*D6*K3*D7*K2*D8*K1
80      C(9)=D3*K5*D4*K4*D5*K3*D6*K2*D7*K1
81      C(10)=D2*K5*D3*K4*D4*K3*D5*K2*D6*K1
82      C(11)=D1*K5*D2*K4*D3*K3*D4*K2*D5*K1
83      C(12)=C5*K5*D1*K4*D2*K3*D3*K2*D4*K1
84      C(13)=C7*K4*D1*K3*D2*K2*(2*D3*K1
85      C(14)=C3*K2*D1*K1
86      C(15)=C7*K2*D1*K1
87      C(16)=C6*K1

```

## **APPENDIX D**

# SIMULATION FOR FREQUENCY RESPONSE EVALUATIONS IN THE MULTI-RATE CASES

The following code performs the calculations using Euler's integration. Note that lines 107 through 112 are shown twice, once for the  $1 \times 3$  separation and once for the  $2 \times 2$  separation.

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```

72      00 200 T = 1.0 NHEFO
73      W = 0.00
74      O = 0.00
75      THETA = 0.00
76      U = 0.00
77      PHONOT = 0.00
78      PHOMPH = 0.00
79      NJ = 1
80      H = 0.00 + (3.0216E11*T)
81      THAX = 0.00
82      THIN = 0.00
83      TI = 0.00
84      C = (-0.65107610-0.00101412112D04120H13*E11)*E03 / (0.81758120-03
85      S = -0.65031650-018120H13*E02 * 1.15004450E11*E04 / (0.81758120-03
86      D = (0.72146720-11-2120H13*E02 * 1.15004450E11*E04) / (-0.81758120-03
87      A = 1.02214840-01420H13*E02 - 1.00000000E11*E04
88
89      Z = 0 / C
90      PHASPL = DATAN (0.163104500/(-0.0000000000))
91      CF = CONGACT(CP1*10000000T11/-0.0000000000+0.16310450010000)
92      S = CF*CP1 / (0.163104500+0.0000000000)
93      PHX = CP1 + H
94      PHY = CF * EXP (-A.990480-02*T1) + CFIN (0.163104500 + TI
95      PHUG = CF * EXP (-A.990480-02*T1) + CFIN (0.163104500 + TI
96      THMPH = THETA + PHUG
97      SET1(J) = TI
98      SET2(J) = THMPH
99      IND = J
100     IF (J<LT,300, GO TO 210
101     IF (THMPH,LT,THAX) GO TO 220
102     IF (THMPH,GT,THIN) GO TO 230
103     THEN = THMPH
104     210
105     C
106     O = PRO + TF * (-0.770-0.000200*PPR-0.70001*PRO
107     S = PPR + TF * (-0.25100*PPR-0.62200*PPR*E241.500+200
108     THETA = PRO + TF + PRO
109     IF (J,NG,TRN1) GO TO 255
110     U = PRO + TS * PHONOT
111     PROOT = -0.0291000*U + 0.062900*W - 32.200*THETA
112     255
113     TI = TI + TF
114     CONTINUE
115
116     GAIN(1) = ((THMAX-THIN) / 2.0001
117     MAG(1) = 20 + 0.021(GAIN(1))
118     300
119     IF (SET1(IND),LT,0, GO TO 302
120     IF (SET2(IND),LT,0,1 GO TO 303
121     IND = IND + 1
122     GO TO 302
123     303
124     M3 = F11 * SET1(IND)
125     PH1 = Z + PI * (F11 * (SET1(IND) - M3)
126     PHAS1(1) = (DARSIN(SET2(IND))/GAIN(1))-PH1 + 180.00 * PI
127     WRITE(6,200) T,N,F11,GAIN(1),M3(1),PHAS1(1)
128     200
129     FORMAT ('11.10X,16.10X,F12.4,3(10X,F15.7)')
130     CONTINUE
131     RETURN
132     END

```

DATA

```

106      TF (3.0216E11*T) GO TO 265
107      W = 0.00 + TS * PHONOT
108      O = PRO + TS * PHONOT
109      PPR00T = -0.0291000*W - 0.062900*W + 24.25000
110      S = 10.20142911(0.224811*TF11+(F11*TS))
111      PHONOT = -0.0291000*W + 0.062900*W - 32.200*THETA
112      265
113      TI = TI + TF

```

] 2x2

The modifications to the previous code so as to use first order Adams integration are shown below.

```

53      00 200 T = 1.0 NHEFO
54      CT11 = -1.37407
55      NJ = 1
56
57      C
58      O = (-0.65107610-0.00101412112D04120H13*E11)*E03 / (0.81758120-03
59      S = -0.65031650-018120H13*E02 * 1.15004450E11*E04 / (0.81758120-03
60      D = (0.72146720-11-2120H13*E02 * 1.15004450E11*E04) / (-0.81758120-03
61      A = 1.02214840-01420H13*E02 - 1.00000000E11*E04
62
63      Z = 0 / C
64      PHASPL = DATAN (0.163104500/(-0.0000000000))
65      CF = CONGACT(CP1*10000000T11/-0.0000000000+0.16310450010000)
66      S = CF*CP1 / (0.163104500+0.0000000000)
67
68      SINCE ADAMS FORMULA IS NOT SELF-STARTING, THE VALUE OF THETA AT
69      THE FIRST INTERVAL IS FOUND BY EULER'S ALGORITHM USING THE FOLLOW-
70      ING SUBROUTINE
71
72      CALL START (F,IR,NHPRO,NJ,T1,TF,TS,HO00T,HO00T,W1,O1,TH1,U1,CF,
73      PHASE1)
74
75      THE FOLLOWING SUBROUTINE FINDS THE DERIVATIVES AT EACH INTERVAL
76      AND FINDS THE VALUE OF THETA,PHUG00. THEN SUBTRACTS THE VALUE
77      OF THE PHUG00 FROM THETA,TJ ELIMINATE THE PHUG00 COMPONENT
78      AND PRINTS OUT THE VALUES.
79
80      CALL DERIV (F,IR,NHPRO,NJ,T1,TF,TS,HO00T,HO00T,W1,O1,TH1,
81      U1,I,CF,PHASE1)
82
83      200
84      CONTINUE
85      GO TO 30
86      300
87      CONTINUE
88      STOP
89      END

```

```

70      SUBROUTINE START (F,IR,I,N1,T1,TF,TS,WDDOT,0003T,0000T,W1)
71      REAL*8 F(121),PI,TF,TS,WDDOT,0003T,0000T,W1
72      REAL*8 TH1,U1,CF,PHASE1
73      REAL*8 W1,00,THETA0,00,UI,01,TH1,U1,DSIN,DEXP
74      INTEGER IR,I,N1
75      PI = 3.14159265D0
76      UI = 0.00
77      W1 = 0.00
78      THETA0 = 0.00
79      U0 = 0.00
80      UI = U0
81      WDDOT = 0.00
82      T1 = 0.00
83      PHUG = CF * DEXP (-0.99381D-02*T1) * DSIN (0.163199500
84      * T1 + PHASE1)
85      C
86      WDDOT = -0.25100*U0 - 0.52600*W1 + 243.5D0*U1 - 10.230*
87      DSIN(2.00*PI+F1*T1)
88      C
89      WDDOT = -0.770+05*U0 - 0.870-02*W1 - 0.79234*U1 - 1.35004
90      DSIN(2.00*PI+F1)*T1
91      C
92      M1 = W1 + TF + WDDOT
93      Q1 = U1 + TF + 0000T
94      TH1 = THETA0 + TF + 00
95      IF (IR.NE.1) GO TO 205
96      UDDOT = -0.2910-01*U1 + 0.6290-01*W1 - 32.203*THETA0
97      UI = U1 + TS * WDDOT
98      NI = NI + 1
99      205   T1 = T1 + TF
100      PHUG = CF * DEXP (-0.99381D-02*T1) * DSIN (0.163199500
101      * T1 + PHASE1)
102      THMPH = TH1 - PHUG
103      RETURN
104      END
105
106      SUBROUTINE DERIV (F,IR,NBER0,M1,T1,TF,TS,WDDOT,0003T,0000T,W1,
107      O1,T1,U1,I,CF,PHASE1)
108      REAL*8 F(121),GAIN(150),HAG(150),PI,TF,TS,CF,PHASE1
109      REAL*8 WDDOT,0003T,0000T,00,01,01,TH1,U1,V2,02,TH2,U2
110      REAL*8 DSIN,0LUG19,DEXP
111      INTEGER I,N1,IR,NJFRQ
112      PI = 3.14159265D0
113      THMAX = 0.00
114      THMIN = 0.0D3
115      Q1 = 0.00
116      Q2 = 0.00
117      U2 = 0.00
118      N = 353 + (3.2/(F1*TF))
119      DO 210 J = 2, N
120      C
121      WDDOT = -0.2310*U1 - 0.61800*W1 + 243.5D0*Q1 - 10.230*
122      DSIN(2.00*PI+F1*T1)
123      Q1DQT = -0.770-05*U1 - 0.870-02*W1 - 0.79234*Q1 - 1.35004
124      DSIN(2.00*PI+F1)*T1
125      C
126      Q2 = W1 + TH + (3.00 * WDDOT - WDDOT) / 2.00
127      Q2 = Q1 + TF + (3.00 * Q1DQT - Q1DQT) / 2.00
128      TH2 = TH1 + TF + (3.00 * Q1 - Q1) / 2.00
129      C
130      IF (J.NE.19+1) GO TO 220
131      Q2 = Q1 + TS + (3.00 * Q1DQT - Q1DQT) / 2.00
132      NI = NI + 1
133      T1 = T1 + TF
134      C
135      PHUG = CF * DEXP (-0.99381D-02*T1) * DSIN (0.163199500
136      * T1 + PHASE1)
137      THMPH = TH2 - PHUG
138      TF = (J-1)*01 GO TO 230
139      TH = (THMPH+THMAX) GO TO 230
140
141      THMAX = THMPH
142      TF = (THMPH,ST,THMIN) GO TO 230
143      THMIN = THMPH
144      C
145      CONTINUE
146      C
147      WDDOT = WDDOT
148      Q1DQT = Q1DQT
149      Q1 = Q1
150      WDDOT = WDDOT
151      M1 = M2
152      O1 = Q2
153      NI = U2
154      TH1 = TH2
155      CONTINUE
156      GAIN(1) = ((THMAX-THMIN) / 2.00)
157      HAG(1) = 20 + LOG10(GAIN(1))
158      WRITE(6,200) I,N1,F1,GAIN(1),HAG(1)
159      FORMAT (1,13,0X,1,13X,12,6,210X,F15,7)
160      RETURN
161      END
162
163      SDATA
164
165      IF (IR.NE.1) GO TO 225
166      WDDOT = -0.25103*U1 - 0.62600*W1 + 243.5D2401 - 10.23004
167      DSIN(2.00*PI+F1*T1)
168      C
169      UDDOT = -0.2910-01*U1 + 0.62600-01*W1 - 32.203*TH1
170      C
171      CONTINUE

```

1x3

2x2

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