

NASA CONTRACTOR REPORT

NASA CR-150777

ANALYSIS OF WIND BIAS CHANGE WITH RESPECT TO TIME AT CAPE KENNEDY, FLORIDA, AND VANDENBERG AFB, CALIFORNIA

By Stanley I. Adelfang
Science Applications, Inc.
2109 W. Clinton Avenue, Suite 800
Huntsville, Alabama 35805

(NASA-CR-150777) ANALYSIS OF WIND BIAS
CHANGE WITH RESPECT TO TIME AT CAPE KENNEDY,
FLORIDA, AND VANDENBERG AFB, CALIFORNIA;
(Science Applications, Inc., Huntsville,
Ala.) 87 p HC ACS/MF ACT

770-3764

Incl: 1
CRRL 041 63/47 30264

August 1978



Prepared for

NASA - George C. Marshall Space Flight Center
Marshall Space Flight Center, Alabama 35812

TECHNICAL REPORT STANDARD TITLE PAGE

1. REPORT NO. NASA CR-150777	2. GOVERNMENT ACCESSION NO.	3. RECIPIENT'S CATALOG NO.
4. TITLE AND SUBTITLE Analysis of Wind Bias Change with Respect to Time at Cape Kennedy, Florida, and Vandenberg AFB, California		5. REPORT DATE August 1978
6. PERFORMING ORGANIZATION CODE		7. AUTHOR(S) Stanley I. Adelfang
8. PERFORMING ORGANIZATION REPORT #		9. PERFORMING ORGANIZATION NAME AND ADDRESS Science Applications, Inc. 2109 W. Clinton Avenue, Suite 800 Huntsville, Alabama 35805
10. WORK UNIT NO.		11. CONTRACT OR GRANT NO. NAS8-32226
12. SPONSORING AGENCY NAME AND ADDRESS National Aeronautics and Space Administration Washington, D. C. 20546		13. TYPE OF REPOR. & PERIOD COVERED Contractor
14. SPONSORING AGENCY CODE		

15. SUPPLEMENTARY NOTES

Prepared under the technical monitorship of the Atmospheric Sciences Division, Space Sciences Laboratory, NASA/Marshall Space Flight Center

16. ABSTRACT

This report presents a statistical analysis of the temporal variability of wind vectors at 1 km altitude intervals from 0 to 27 km altitude after applying a digital filter to the original wind profile data sample.

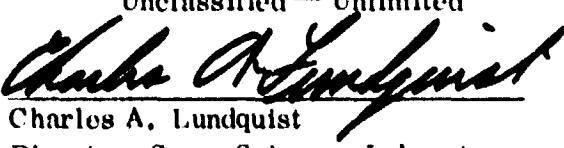
17. KEY WORDS	18. DISTRIBUTION STATEMENT Unclassified — Unlimited  Charles A. Lundquist Director, Space Sciences Laboratory		
19. SECURITY CLASSIF. (of this report)	20. SECURITY CLASSIF. (of this page)	21. NO. OF PAGES	22. PRICE
Unclassified	Unclassified	87	NTIS

TABLE OF CONTENTS

<u>Section</u>	<u>Page</u>
I INTRODUCTION	1
II TECHNICAL BACKGROUND	2
A. Introduction	2
B. Data	2
C. Digital Filter	3
D. Definitions	33
E. Statistics	6
III ANALYSIS	8
A. Introduction	8
B. Wind Bias Component Change With Respect to Time	8
C. Joint Distribution of Wind Bias Component Changes With Respect to Time	22
D. Modulus of Vector Wind Bias Change With Respect to Time .	25
E. Conditional Vector Wind Bias Ellipses	32
IV CONCLUSIONS	39
V REFERENCES	41
Appendix	41

LIST OF ILLUSTRATIONS

<u>Figure</u>		<u>Page</u>
1	Wind Bias Profile Calculated from a Rawinsonde Profile and an Artificial Profile Composed of Monthly Means for the Period 1956-67 at KSC	5
2	Zonal and Meridional Wind Bias Component Autocorrelation During April at 6, 12 and 18 km at Cape Kennedy (1956-70)	10
3	Zonal and Meridional Wind Bias Component Autocorrelation During January at 6, 12 and 18 km at Vandenberg AFB (1965-74)	11
4	Constants b and c of Equations 18 and 19 for Cape Kennedy During April (1956-70)	14
5	Constants b and c of Equations 18 and 19 for Vandenberg AFB During January (1965-74)	15
6	Theoretical (Straight Lines) and Observed (Plotted Points) Cumulative Probability Distribution of Zonal Wind Bias Component Change, Δu , with Respect to Time Increment, τ , During April at 12 km Over Cape Kennedy (1956-70)	18
7	Theoretical (Straight Lines) and Observed (Plotted Points) Cumulative Probability Distribution of Meridional Wind Bias Component Change, Δv , with Respect to Time Increment, τ , During April at 12 km Over Cape Kennedy (1956-70)	19
8	Theoretical (Straight Lines) and Observed (Plotted Points) Cumulative Probability Distribution of Zonal Wind Bias Component Change, Δu , with Respect to Time Increment, τ , During January at 12 km Over Vandenberg AFB (1965-74)	20
9	Theoretical (Straight Lines) and Observed (Plotted Points) Cumulative Probability Distribution of Meridional Wind Bias Component Change, Δv , with Respect to Time Increment, τ , During January at 12 km Over Vandenberg AFB (1965-74)	21
10	Observed λ_e as a Function of Theoretical λ_e for a Bivariate Normal Distribution of Wind Bias Component Changes (Δu , Δv) with Respect to Time at 12 km During April (1956-70) at Cape Kennedy	23
11	Observed λ_e as a Function of Theoretical λ_e for a Bivariate Normal Distribution of Wind Bias Component Changes (Δu , Δv) with Respect to Time at 12 km During January (1965-74) at Vandenberg AFB	24
12	Joint Distribution of 95 Percent Wind Bias Component Changes with Respect to Time at 6, 12 and 18 km During April at Cape Kennedy (1956-70) and January at Vandenberg (1965-74) . . .	26
13	April Theoretical Percentiles of Modulus, R, of Vector Wind Bias Change with Respect to Time Interval, τ , at 12 km Over Cape Kennedy (1956-70)	28

LIST OF ILLUSTRATIONS (Con.)

<u>Figure</u>		<u>Page</u>
14	January Theoretical Percentiles of Modulus, R, of Vector Wind Bias Change with Respect to Time Interval, t_1 , at 12 Km Over Vandenberg AFB (1965-74)	29
15	April Conditional 95 Percent Wind Bias Ellipses at 12 km for Time Increments of 12, 24, 36, 48, 60 and 72 Hours at Cape Kennedy (1956-70)	33
16	January Conditional 95 Percent Wind Bias Ellipses at 12 km for Time Increments of 12, 24, 36, 48, 60 and 72 Hours at Vandenberg AFB (1965-74)	34
17	Wind Direction Characteristics of a Vector Probability Ellipse . .	38

LIST OF TABLES

<u>Table</u>		<u>Page</u>
1	Filter Weights and Effective Response Function of an 11-Point Martin-Graham Low Pass Filter with a Nominal Cutoff Frequency of $.04 \text{ km}^{-1}$ and a Termination Frequency of $.20 \text{ km}^{-1}$	4
2	Constants b and c of Equations 18 and 19 at Altitudes from 5 to 22 km During January at VAFB (1965-74) and During April at Cape Kennedy (1956-70)	13
3	Calculated [Eqs. 22 and 23] and Observed $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ from Wind Bias Profiles During April at Cape Kennedy at 6, 12, and 18 km	16
4	Calculated [Eqs. 22 and 23] and Observed $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ from Wind Bias Profiles During January at Vandenberg AFB at 6, 12 and 18 km	17
5	Theoretical and Observed Modulus, R(m/sec), of Vector Wind Bias Change with Respect to Time Interval, τ , During April (1956-70) at 12 km Over Cape Kennedy	30
6	Theoretical and Observed Modulus, R(m/sec), of Vector Wind Bias Change with Respect to Time Interval, τ , During January (1965-74) at 12 km Over Vandenberg AFB	31
7	Wind Direction (Degrees) Characteristics of 95 Percent Conditional Vector Wind Bias Ellipses at 12 km Over Cape Kennedy During April for an Elapsed Time, τ , of 12 Hours	36
8	Wind Direction (Degrees) Characteristics of 95 Percent Conditional Vector Wind Bias Ellipses at 12 km Over Vandenberg AFB During January for an Elapsed Time, τ , of 12 Hours	37

I. INTRODUCTION

A typical wind model used for ascent vehicle wind biasing consists of the monthly mean wind at each altitude. Such a model does not contain the small scale perturbations normally found in Rawinsonde profiles. The smoothness of the wind profile model is not considered to be a serious deficiency because wind biasing is with respect to the predominant large scale perturbation in the profile. Thus, even if a single Rawinsonde profile obtained a few hours prior to launch is used as the basis for wind biasing, the small scale perturbations in the profile would be removed before implementation. Nevertheless, filtered profiles can still differ greatly from the monthly mean profile; therefore, individual filtered wind profiles that are representative of the wind conditions associated with a particular launch would be the most desirable basis for wind biasing of launch vehicles. The monthly mean wind profile is almost never representative of launch conditions.

The development of a pre-launch wind monitoring scheme to provide data for wind biasing will require knowledge of the change of smoothed wind profiles with respect to time. This report describes wind bias change with respect to time that has been calculated from the VAFB (1965-74) and KSC (1956-70) twice daily Rawinsonde series. Each profile in the series was filtered before calculation of wind change statistics. The filtering process removed the small scale perturbations. Wind change at KSC and VAFB for unfiltered profiles has been described in previous reports [1,2]. The methodology used in this study is basically the same; wind bias change for time intervals from 0 to 72 hours at altitudes from 5 to 22 km is calculated for selected months. Wind bias change is presented in terms of statistical summaries of wind bias component change and the modulus of vector wind bias change; the parameters of theoretical probability distribution functions representing the wind bias change variables are also presented. The validity of the theoretical distributions is established by comparing them with the observed distributions. These distribution functions can be utilized to obtain statistical predictions of wind change with respect to time.

This report consists of a brief statement of technical background (Section II), an analysis of wind change statistics calculated from filtered data (Section III) and conclusions (Section IV); the calculated statistics of wind bias change with respect to time for selected months 1 km altitude increments from 5 to 22 km to KSC and VAFB are listed in the appendix.

II. TECHNICAL BACKGROUND

A. INTRODUCTION

The large sample of wind profiles obtained at VAFB is suitable for calculation of an equally large sample of wind bias change data. In order to readily abstract information on wind bias change from these data, it is necessary to perform a second series of calculations which provide statistical summaries of wind bias change. The choice of statistical parameters for description of wind bias change is based in part on the need to specify the parameters of theoretical distributions of wind change. These theoretical distribution functions are described in detail by Smith [3]. The basic distribution of the four variables consisting of the zonal and meridional components of the wind bias vector at an initial time and after an elapsed time, Δt , is quadravariate normal. The conditional distribution of the wind bias components at a specified future time, given the wind bias components at an initial time, is bivariate normal. The modulus of the wind bias change vector is Rayleigh and the distribution of either the zonal or meridional wind bias component change is univariate normal. A significant portion of the analytical discussion in Section III of this report is the presentation of observed distributions of wind bias change and comparison with the theoretical distributions of wind bias change variables. Succeeding paragraphs of this section are concerned with a description of the wind bias profile data, the filtering of the data and the definition of statistical parameters of wind bias change used in the various theoretical distribution functions.

B. DATA

The basic winds aloft data are recorded in terms of wind direction, θ and magnitude, W . The wind vector is expressed in the standard meteorological coordinate system in which the direction from which the wind is blowing is measured in degrees clockwise from true north. The zonal component, u , of wind vector is positive for a west (west to east) wind ($\theta=270^\circ$) and negative for an east (east to west) wind ($\theta=90^\circ$); the meridional component, v , is positive for a south (south to north) wind ($\theta=180^\circ$) and negative for a north (north to south) wind ($\theta=0^\circ$); u and v are obtained from θ and W according to:

$$u = -W \sin \theta, \quad 0 \leq \theta \leq 360^\circ \quad (1)$$

$$v = -W \cos \theta, \quad (2)$$

The relation between θ defined above and the angle defined in standard mathematical polar form s :

$$\theta = 270 - \theta_{\text{Math}} \quad (3)$$

C. DIGITAL FILTER

Wind profiles suitable for wind biasing of launch vehicles (defined here as wind bias profiles) are calculated by application of an 11-point symmetrical Martin-Graham digital low-pass filter to Rawinsonde profiles. The filter removes the small scale perturbations in the wind profile without the addition of phase shift to the data. The filter gain and weighting functions are listed in Table 1. The effect of the filter on a particular profile is illustrated in Figure 1. Application of the filter to a wind profile originally containing data at 1 km intervals from 0 to 27 km produces a somewhat abbreviated filtered profile extending from 5 to 22 km. The mathematical background and computer code for calculation of the filter gain and weighting functions are described by Demandel and Krivo (4).

The typically large deviation of individual filtered and unfiltered Rawinsonde profiles from the artificial profile composed of the monthly mean at each altitude is also illustrated in Figure 1.

D. DEFINITIONS

The subscript 0 is used to denote the initial value of a variable, and the subscript 1 denotes the variable after an elapsed time, Δt . Thus:

$$\Delta u = u_1 - u_0 \quad (4)$$

$$\Delta v = v_1 - v_0 \quad (5)$$

Where Δu and Δv are the components of the wind bias change for a specified Δt . The modulus, R , of the wind bias change with respect to time is given by:

$$R = \sqrt{(\Delta u)^2 + (\Delta v)^2} \quad (6)$$

Table 1. Filter Weights and Effective Response Function of an 11-Point Martin Graham Low Pass Filter with a Nominal Cutoff Frequency of $.04 \text{ km}^{-1}$ and a Termination Frequency of $.20 \text{ km}^{-1}$

Filter Weights, h_i	Response Function, $G(f)$	
	$f(\text{km}^{-1})$	$G(f)$
h_0	.22658165	.01 .996 .02 .985
$h_{+1,-1}$.20033538	.03 .966 .04 .940
$h_{+2,-2}$.13609867	.05 .905 .06 .863
$h_{+3,-3}$.06181594	.07 .813 .08 .756
$h_{+4,-4}$.00628003	.09 .693 .10 .624
$h_{+5,-5}$.01832084	.15 .251 .20 -.002 .30 .023 .40 -.023 .50 .023 .60 -.023 .70 .023 .80 -.023

ORIGINAL PAGE IS
OF POOR QUALITY

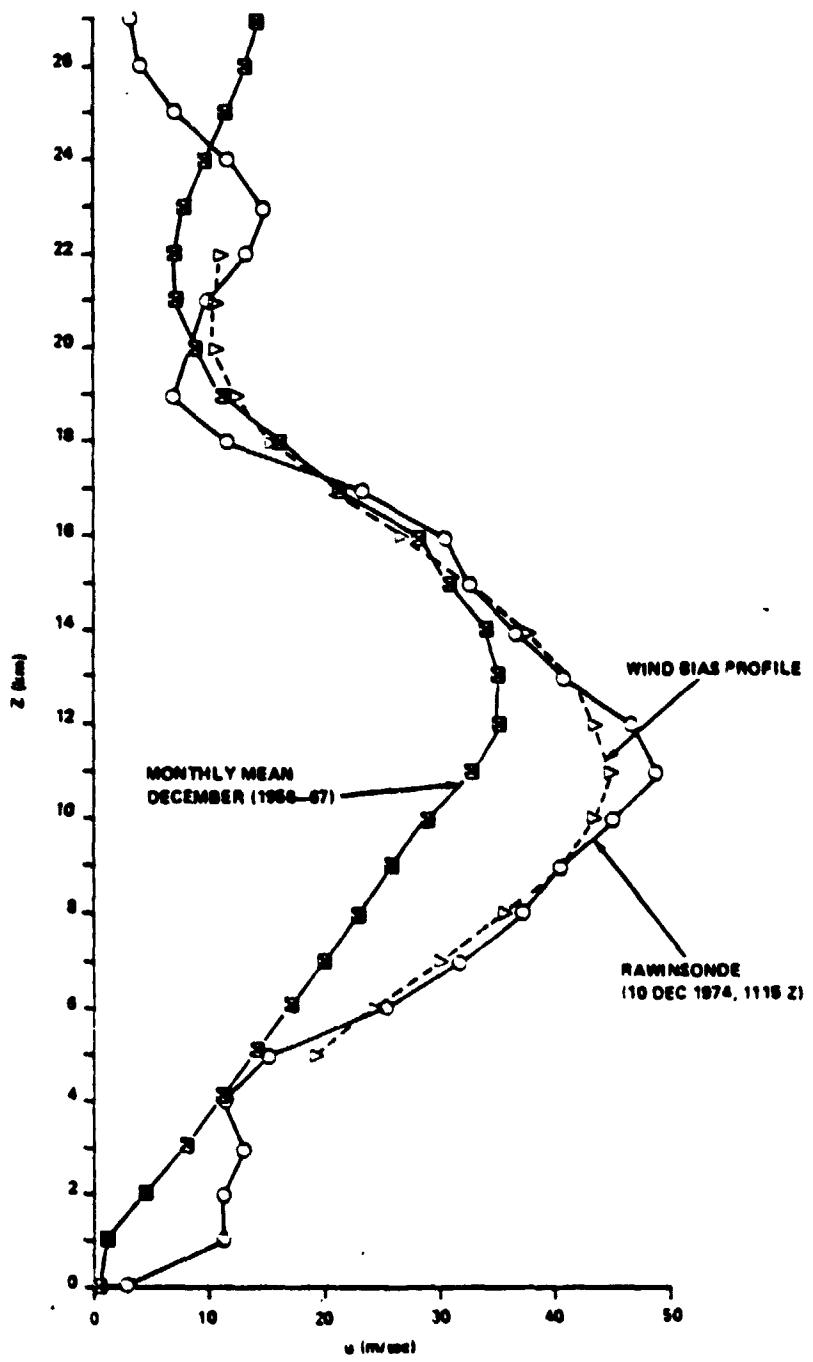


Figure 1. Wind Bias Profile Calculated from a Rawinsonde Profile and an Artificial Profile Composed of Monthly Means for the Period 1956-67 at KSC

The statistical means are denoted by an overbar, the standard deviations and the correlation coefficients are denoted by σ_x and $R(X, Y)$, respectively, with X and Y replaced with the notation appropriate to the variable of interest.

E. STATISTICS

The wind vector measurements at an initial time and after an elapsed time are treated in this investigation as a sample from a quadravariate normal distribution defined by the fourteen statistics listed below:

MEANS

$$\bar{u}_0, \bar{v}_0, \bar{u}_1, \bar{v}_1$$

STANDARD DEVIATIONS

$$\sigma_{u_0}, \sigma_{v_0}, \sigma_{u_1}, \sigma_{v_1}$$

CORRELATION COEFFICIENTS

$$R(u_0, v_0), R(u_0, u_1)$$

$$R(v_0, v_1), R(u_1, v_1)$$

$$R(u_1, v_0), R(v_1, u_0)$$

The fourteen statistics of the quadravariate normal distribution of vector wind difference with respect to time consist of the five bivariate normal statistics of vector wind at an initial time ($\bar{u}_0, \bar{v}_0, \sigma_{u_0}, \sigma_{v_0}$ and $R(u_0, v_0)$) and the nine statistics involving component differences which can be calculated from the quadravariate statistics listed above according to the following equations:

MEANS

$$\Delta u = \bar{u}_1 - \bar{u}_0 = \bar{u}_1 - \bar{u}_0 \quad (7)$$

$$\Delta v = \bar{v}_1 - \bar{v}_0 = \bar{v}_1 - \bar{v}_0 \quad (8)$$

STANDARD DEVIATIONS

$$\sigma_{\Delta u} = \sqrt{\sigma_{u_1}^2 + \sigma_{u_0}^2 - 2\sigma_{u_1}\sigma_{u_0} R(u_1, u_0)} \quad (9)$$

$$\sigma_{\Delta v} = \sqrt{\sigma_{v_1}^2 + \sigma_{v_0}^2 - 2\sigma_{v_1}\sigma_{v_0} R(v_1, v_0)} \quad (10)$$

Where $R(x,y)$ is the correlation coefficient of variables x and y .

CORRELATION COEFFICIENTS

$$R(u_0, \Delta u) = \frac{\sigma_{u_1} R(u_0, u_1) - \sigma_{u_0}}{\sigma_{\Delta u}} \quad (11)$$

Where, $\sigma_{\Delta u}$ is obtained from Equation 9

$$R(v_0, \Delta v) = \frac{\sigma_{v_1} R(v_0, v_1) - \sigma_{v_0}}{\sigma_{\Delta v}} \quad (12)$$

Where, $\sigma_{\Delta v}$ is obtained from Equation 10

$$R(\Delta u, v_0) = \frac{\sigma_{u_1} R(v_0, u_1) - \sigma_{u_0} R(u_0, v_0)}{\sigma_{\Delta u}} \quad (13)$$

$$R(\Delta v, u_0) = \frac{\sigma_{v_1} R(u_0, v_1) - \sigma_{v_0} R(u_0, v_0)}{\sigma_{\Delta v}} \quad (14)$$

$$R(\Delta u, \Delta v) = \frac{(\sigma_{u_1} \sigma_{v_1} R(u_1, v_1) - \sigma_{u_1} \sigma_{v_0} R(u_1, v_0)) + (\sigma_{u_0} \sigma_{v_1} R(u_0, v_1) + \sigma_{u_0} \sigma_{v_0} R(u_0, v_0))}{\sigma_{\Delta u} \sigma_{\Delta v}} \quad (15)$$

III. ANALYSIS

A. INTRODUCTION

The analysis of wind bias profile change with respect to time follows the approach taken in previous studies of vector wind change at KSC and VAFB [1,2]. The vectors under consideration have been modified by the filtering process described in the previous section. Since the component of wind change associated with small scale perturbations in the profile has been removed, the calculated wind change is expected to be smaller for wind bias profiles. The objective of this analysis is the establishment of a theoretical basis for estimation of wind bias change. This is accomplished by comparison of theoretical probability distributions which contain wind bias change sample statistics as parameters (from the appendix of this report), to observed probability distributions of wind bias change. Wind bias change with respect to time is analyzed herein in terms of wind component change, unconditional and conditional joint distributions of wind component change, and the modulus of vector wind change.

B. WIND BIAS COMPONENT CHANGE WITH RESPECT TO TIME

The theoretical probability distribution of wind component change with respect to time is univariate normal with zero mean and standard deviation given by Equations 9 and 10; the assumption of zero means of component differences is verified by the sample statistics given in the appendix. The theoretical normal distribution of component differences can be derived by using either the standard deviations of component differences given in the appendix or an estimate which can be obtained from the standard deviation of the components if it is assumed that:

$$\sigma_{u_0}' = \sigma_{u_1} = \sigma_u$$

$$\sigma_{v_0}' = \sigma_{v_1} = \sigma_v$$

Equations 9 and 10 reduce to

$$\sigma_{\Delta u} = \sqrt{2} \sigma_u \sqrt{1 - R(u_1, u_0)} \quad (16)$$

$$\sigma_{\Delta v} = \sqrt{2} \sigma_v \sqrt{1 - R(v_1, v_0)} \quad (17)$$

The wind component autocorrelation functions, $R(u_1, u_0)$ and $R(v_1, v_0)$ can be represented by a negative exponential function of time increment, τ ; i.e.,

$$R(u_1, u_0) = \text{EXP}(-b\tau) \quad (18)$$

$$R(v_1, v_0) = \text{EXP}(-c\tau) \quad (19)$$

where b and c are computed according to

$$b = - \frac{\sum \tau_i \ln R_i(u_1, u_0)}{\sum \tau_i^2} \quad (20)$$

$$c = - \frac{\sum \tau_i \ln R_i(v_1, v_0)}{\sum \tau_i^2} \quad (21)$$

Examples of the decay of the autocorrelation function at 6, 12 and 18 km during April at Cape Kennedy and January at VAFB are illustrated in Figures 2 and 3, respectively; the lines in the figure represent the decay rate predicted by Equations 18 and 19.

Substitution of Equations 18 and 19 into 16 and 17, respectively, yields a simple expression for $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ in terms of σ_u and σ_v , respectively.

$$\sigma_{\Delta u} = \sqrt{2} \sigma_u \sqrt{1 - \text{EXP}(-b\tau)} \quad (22)$$

$$\sigma_{\Delta v} = \sqrt{2} \sigma_v \sqrt{1 - \text{EXP}(-c\tau)} \quad (23)$$

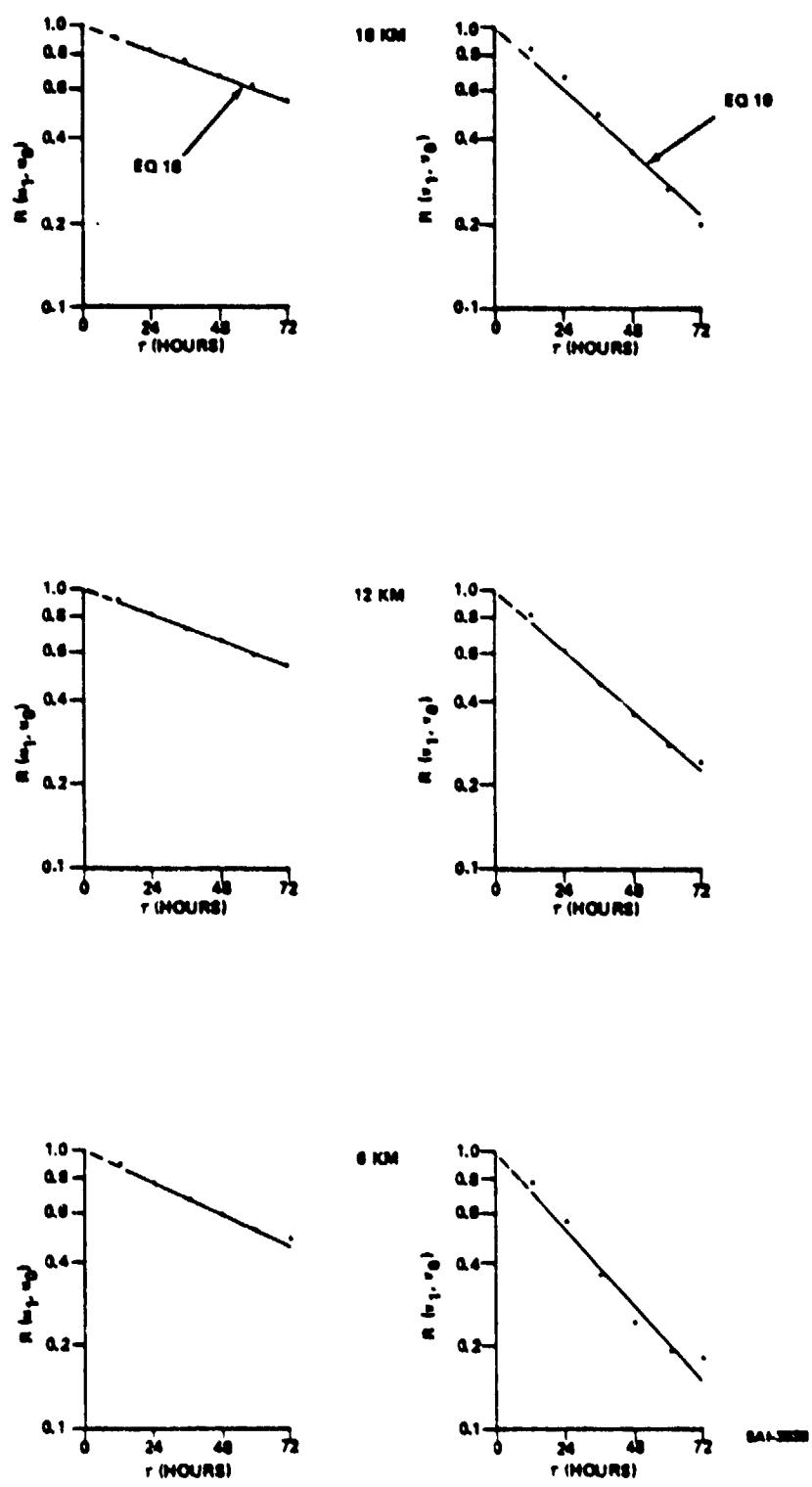


Figure 2. Zonal and Meridional Wind Bias Component Autocorrelation During April at 6, 12, and 18 km at Cape Kennedy (1956-70)

ORIGINAL PAGE IS
OF POOR QUALITY

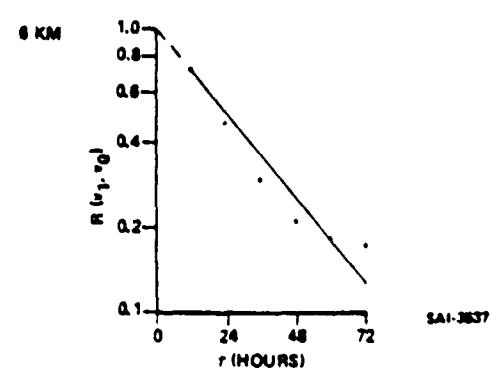
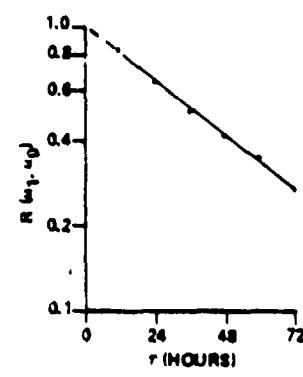
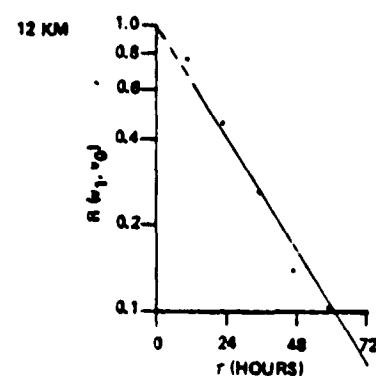
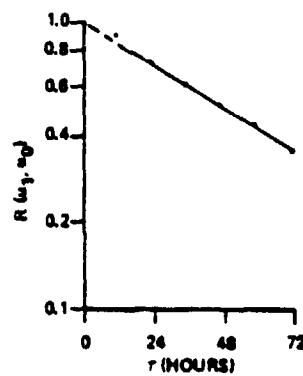
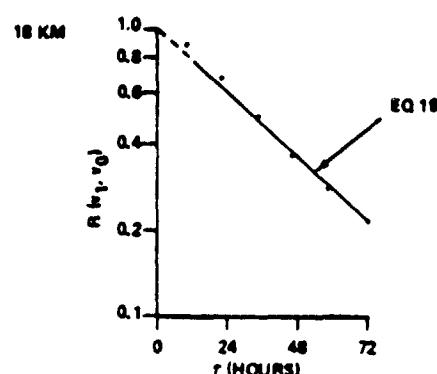
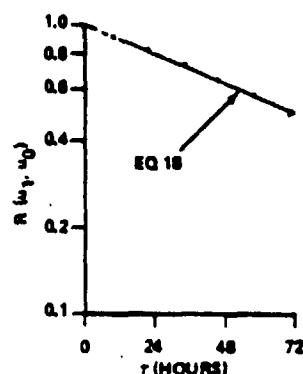


Figure 3. Zonal and Meridional Wind Bias Component Autocorrelation During January at 6, 12 and 18 km at Vandenberg AFB (1965-74)

Equations 22 and 23 indicate that $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ are asymptotic to $\sqrt{2} \sigma_u$ and $\sqrt{2} \sigma_v$ for large values of τ . Therefore, estimates of the extreme value of $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ are obtained by setting τ equal to ∞ in equations 22 and 23.

The calculated values of b and c at altitudes from 5 to 22 km over KSC in April and VAFB during January listed in Table 2 are also plotted in Figures 4 and 5. At both locations at altitudes from 5 to 22 km the decay rate of the meridional wind bias component autocorrelation is larger than the decay rate for the zonal component. The variation of the decay rate for the meridional component as a function of altitude differs at the two locations. Maximum decay for the meridional component occurs at 12 - 13 km over VAFB during January; in contrast, at KSC during April, the maximum occurs at the extremes of altitude range (near 5 and 22 km) and is a minimum at 15 km. The decay of zonal component autocorrelation decreases steadily with altitude at VAFB during January. At KSC during April the decay also decreases with altitude but at a very rapid rate and within a restricted altitude range (5 - 15 km); above 15 km the decay increases.

The calculated and observed values of $\sigma_{\Delta u}(\tau)$ and $\sigma_{\Delta v}(\tau)$ at 6, 12, and 18 km during April at KSC and January at VAFB are listed in Tables 3 and 4. The estimated extreme values of $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$, ($\sqrt{2} \sigma_u$ and $\sqrt{2} \sigma_v$, respectively), are listed at the bottom of each column of calculated values. The comparisons in Tables 3 and 4 indicate that $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ can be accurately estimated by application of Equations 22 and 23, respectively. General application of this estimation technique at other locations would require a more adequate knowledge of the form of the autocorrelation function than is presently available.

The theoretical distribution of wind bias component differences has been derived from sample estimates of $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ and $\bar{\Delta u}$ and $\bar{\Delta v}$ (given in the appendix) for the intervals of 12, 24, 36 and 48 hours at 12 km during April at KSC and January at VAFB; the theoretical normal distributions are plotted as straight lines in Figures 6 through 9; the plotted symbols represent the observed distributions of Δu and Δv . It is indicated that the observed distribution of bias component changes is accurately represented

Z (km)	VAFB (JANUARY)		KSC (APRIL)	
	$10^2 b (\text{hr}^{-1})$	$10^2 c (\text{hr}^{-1})$	$10^2 b (\text{hr}^{-1})$	$10^2 c (\text{hr}^{-1})$
5	1.79	2.72	1.17	2.96
6	1.80	2.83	1.08	2.64
7	1.80	2.99	1.04	2.43
8	1.78	3.16	1.02	2.32
9	1.72	3.33	1.02	2.26
10	1.63	3.49	0.99	2.21
11	1.52	3.64	0.96	2.15
12	1.41	3.74	0.89	2.06
13	1.32	3.77	0.85	1.97
14	1.25	3.87	0.81	1.89
15	1.21	3.42	0.80	1.86
16	1.18	3.04	0.80	1.89
17	1.09	2.67	0.82	1.99
18	0.96	2.11	0.84	2.14
19	0.81	1.76	0.86	2.38
20	0.70	1.60	0.90	2.79
21	0.65	1.37	0.98	3.71
22	0.63	1.34	1.10	3.34

SAI 3818

Table 2. Constants b and c of Equations 18 and 19 at Altitudes from 5 to 22 km During January at VAFB (1965-74) and During April at Cape Kennedy (1956-70)

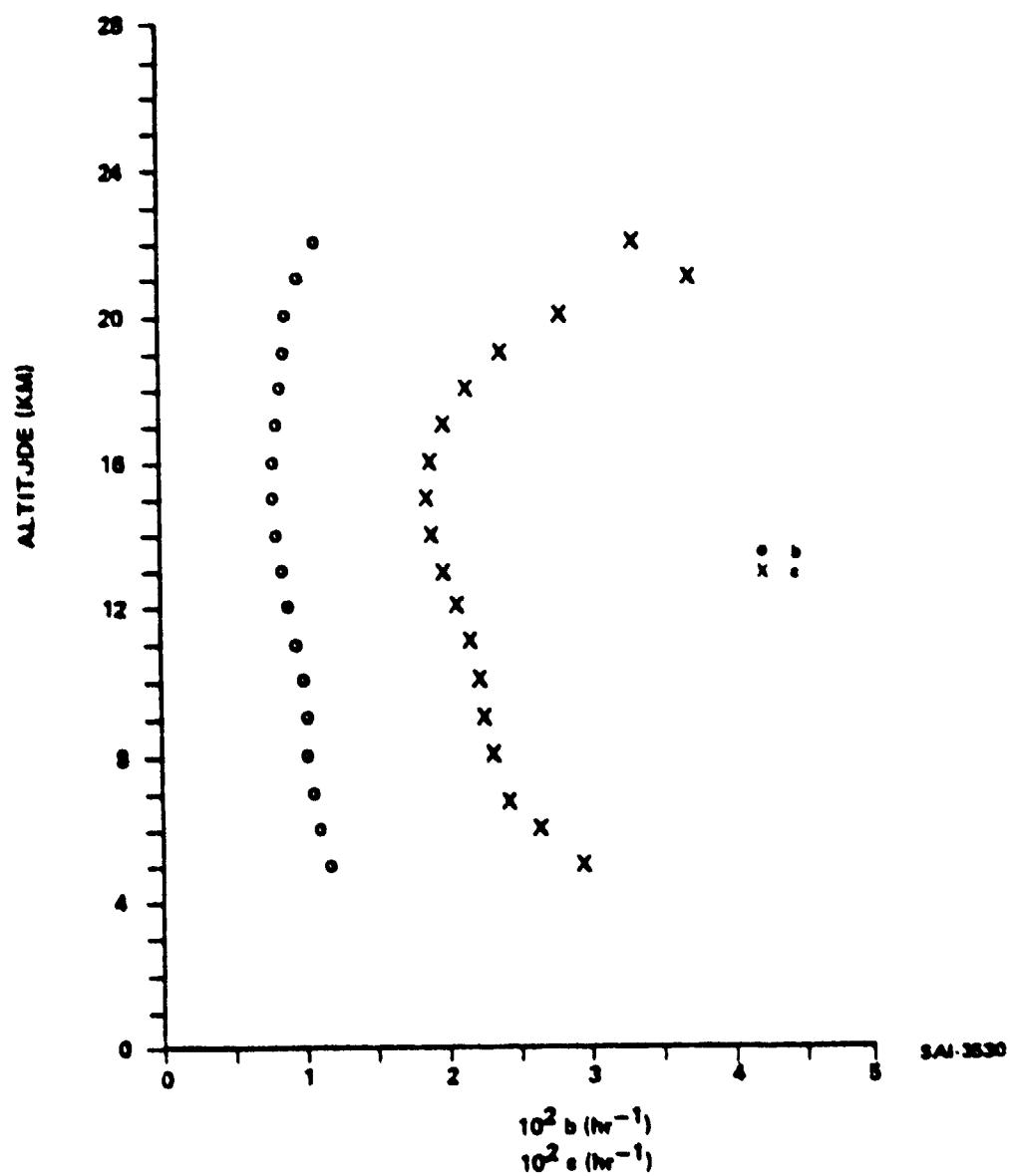


Figure 4. Constants b and c of Equations 18 and 19 for Cape Kennedy During April (1956-70)

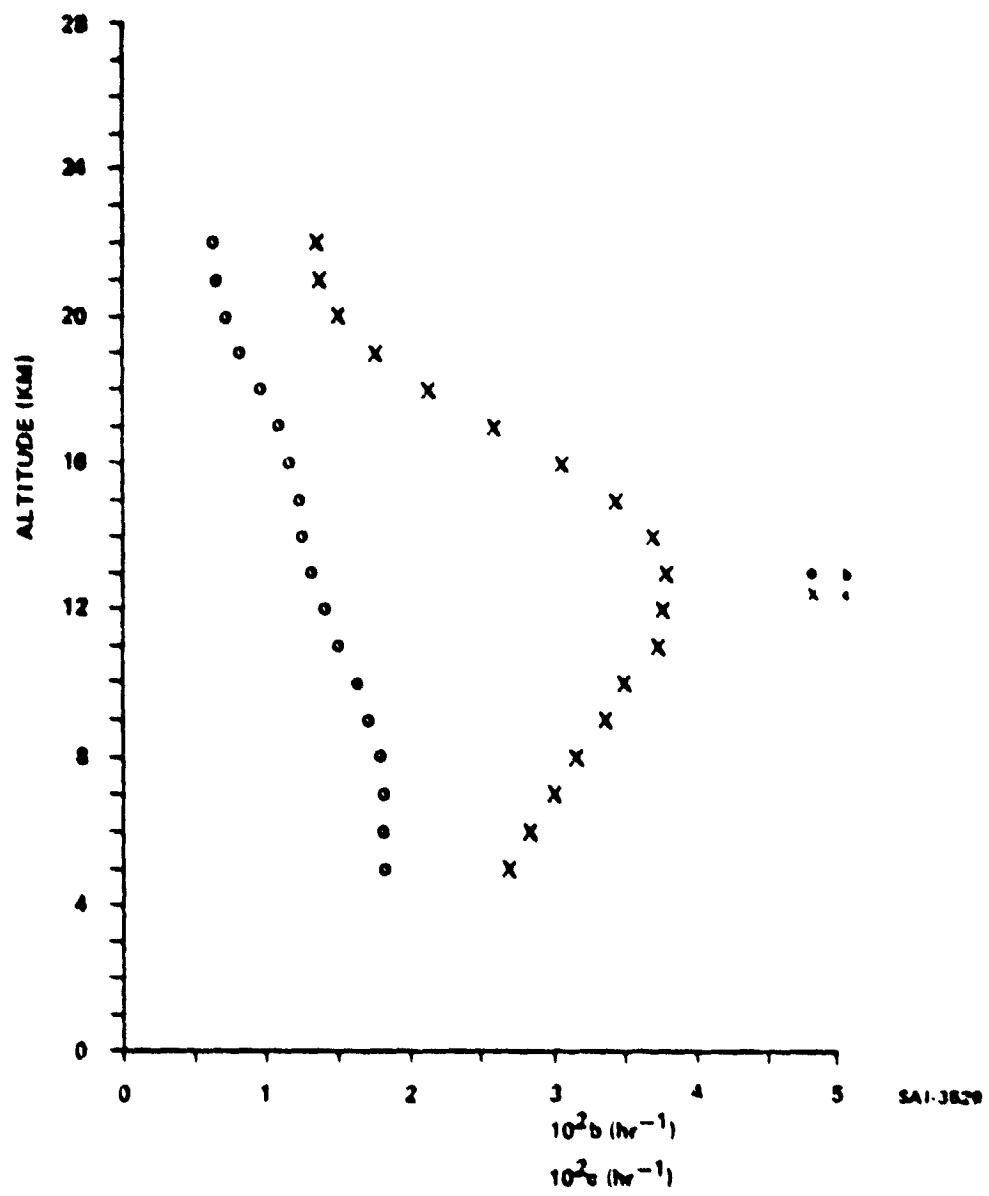


Figure 5. Constants b and c of Equations 18 and 19 for Vandenberg AFB During January (1965-74)

ALTITUDE (KM)	t (HOURS)	$\sigma_{\Delta u}$		$\sigma_{\Delta v}$	
		CALCULATED	OBSERVED	CALCULATED	OBSERVED
18	12	3.11	3.17	3.20	2.60
	24	4.29	4.13	4.26	3.89
	36	5.13	5.04	4.92	4.78
	48	5.78	5.70	5.38	5.33
	60	6.32	6.24	5.71	5.72
	72	6.78	6.59	5.95	5.99
	∞	10.04	—	—	—
12	12	7.00	6.23	7.89	7.28
	24	9.65	9.28	10.53	10.35
	36	11.52	11.50	12.20	12.34
	48	12.97	12.94	13.36	13.44
	60	14.16	14.05	14.20	14.23
	72	15.14	14.92	14.82	14.65
	∞	—	—	—	—
6	12	6.12	4.74	5.11	4.75
	24	7.01	7.04	6.72	6.59
	36	8.33	8.53	7.69	7.83
	48	9.34	9.38	8.32	8.52
	60	10.14	10.03	8.75	8.76
	72	10.79	10.54	9.05	8.82
	∞	14.68	—	—	—

SAI-3816

Table 3. Calculated [Eqs. 22 and 23] and Observed $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ from Wind Bias Profiles During April at Cape Kennedy at 6, 12, and 18 km

ALTITUDE (KM)	T (HOURS)	$\sigma_{\Delta u}$		$\sigma_{\Delta v}$	
		CALCULATED	OBSERVED	CALCULATED	OBSERVED
18	12	3.20	2.97	3.58	2.86
	24	4.40	4.08	4.75	4.42
	36	5.24	5.03	5.49	5.44
	48	6.89	5.75	6.01	6.07
	60	6.42	6.48	6.38	6.43
	72	6.85	7.03	6.65	6.65
	∞	9.72	--	7.52	--
12	12	9.18	8.12	12.23	9.91
	24	12.43	12.16	15.65	15.04
	36	14.64	14.66	17.49	17.56
	48	16.27	16.17	18.57	18.83
	60	17.63	17.33	19.23	19.16
	72	18.53	18.61	19.63	19.40
	∞	23.19	--	20.34	--
6	12	7.62	8.96	9.00	8.88
	24	10.23	10.13	11.78	12.22
	36	11.93	11.89	13.41	14.06
	48	13.14	12.94	14.47	14.79
	60	14.04	13.78	15.17	14.97
	72	14.73	14.62	16.65	16.13
	∞	17.28	--	16.79	--

SA1381

Table 4. Calculated [Eqs. 22 and 23] and Observed $\sigma_{\Delta u}$ and $\sigma_{\Delta v}$ from Wind Bias Profiles During January at Vandenberg AFB at 6, 12 and 18 km

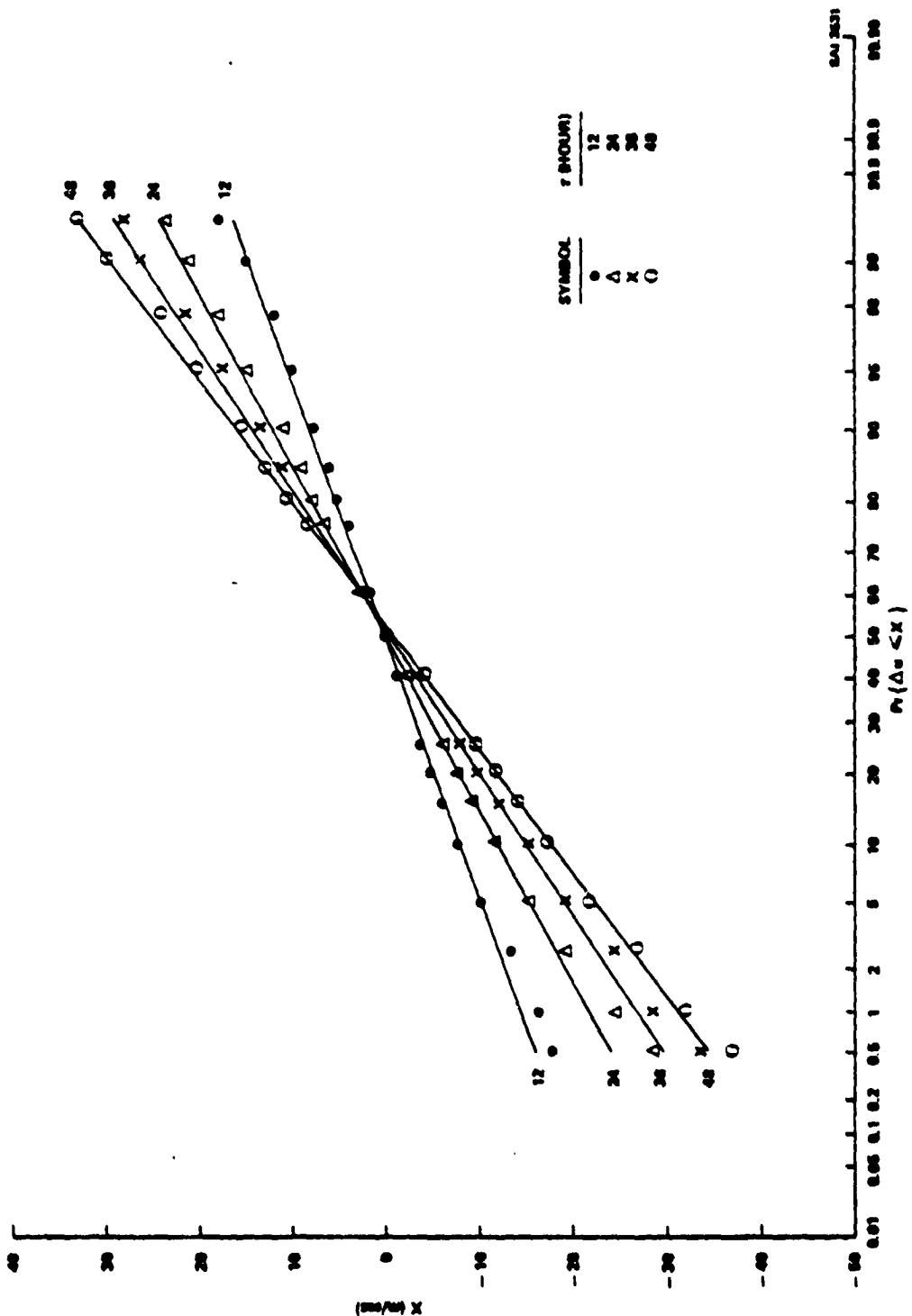


Figure 6. Theoretical (Straight Lines) and Observed (Plotted Points) Cumulative Probability Distribution of Zonal Wind Bias Component Change, Δu , with Respect to Time Increment, τ , During April at 12 km Over Cape Kennedy (1956-70)

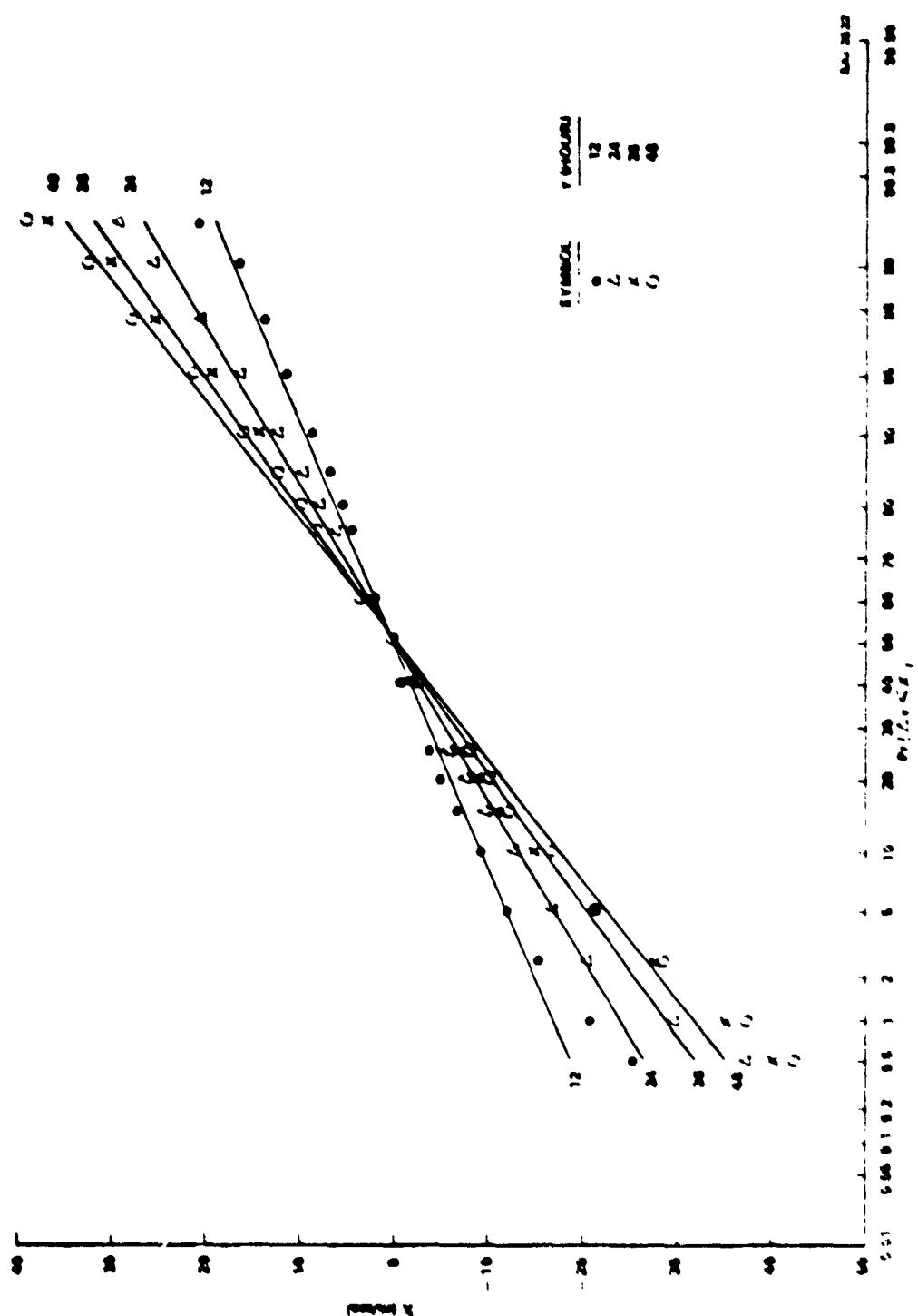


Figure 7. Correspondence between time (hours) and distance (miles) and illustrated by straight lines passing through the origin.

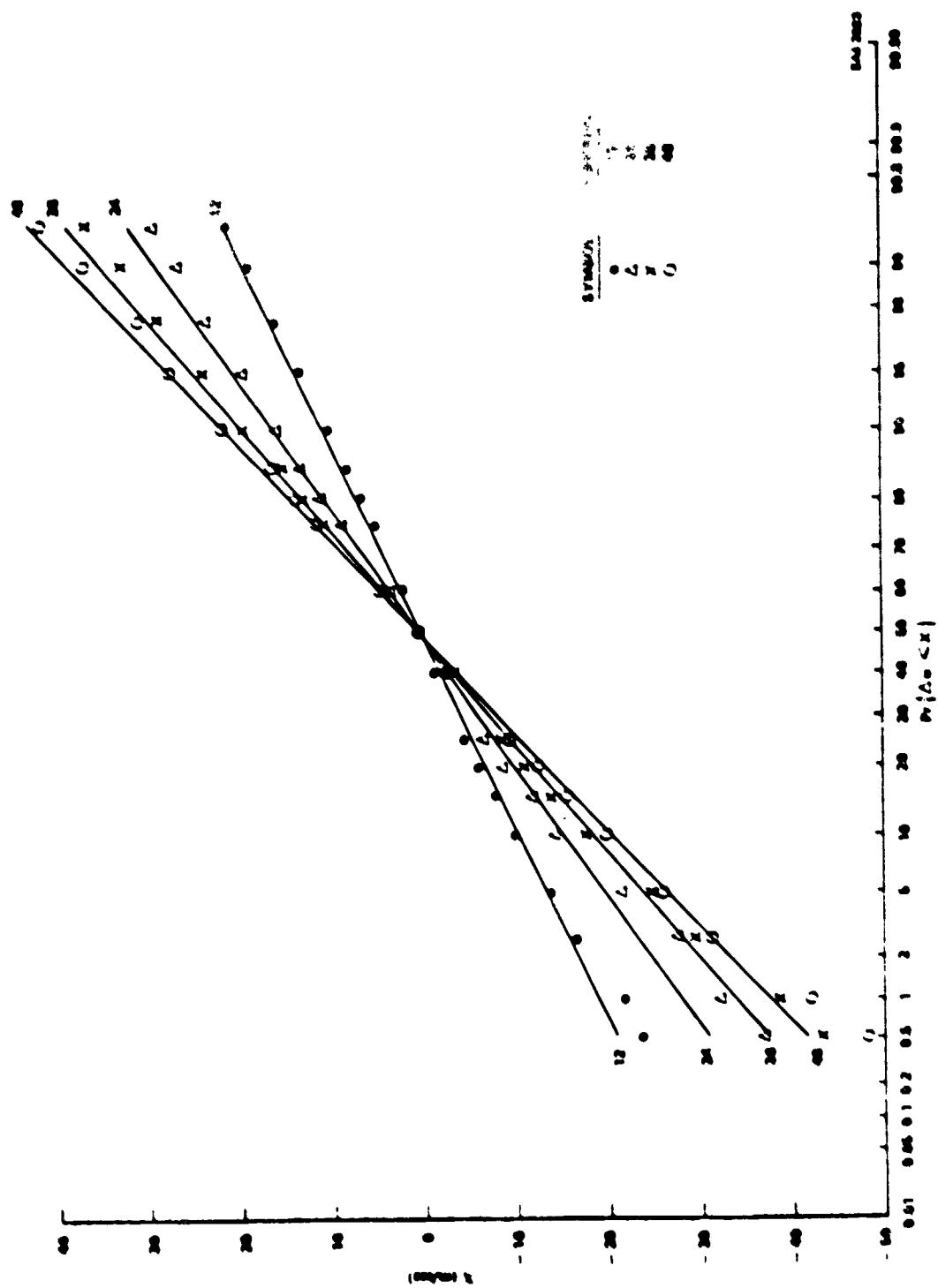


Figure 8. Theoretical (straight lines) and Observed (Plotted Points) Cumulative Probability Distribution of Zonal Wind Bias Component Change, Δu , with Respect to Time Increment, τ , During January at 12 km Over Vandenberg AFB (1965-74)

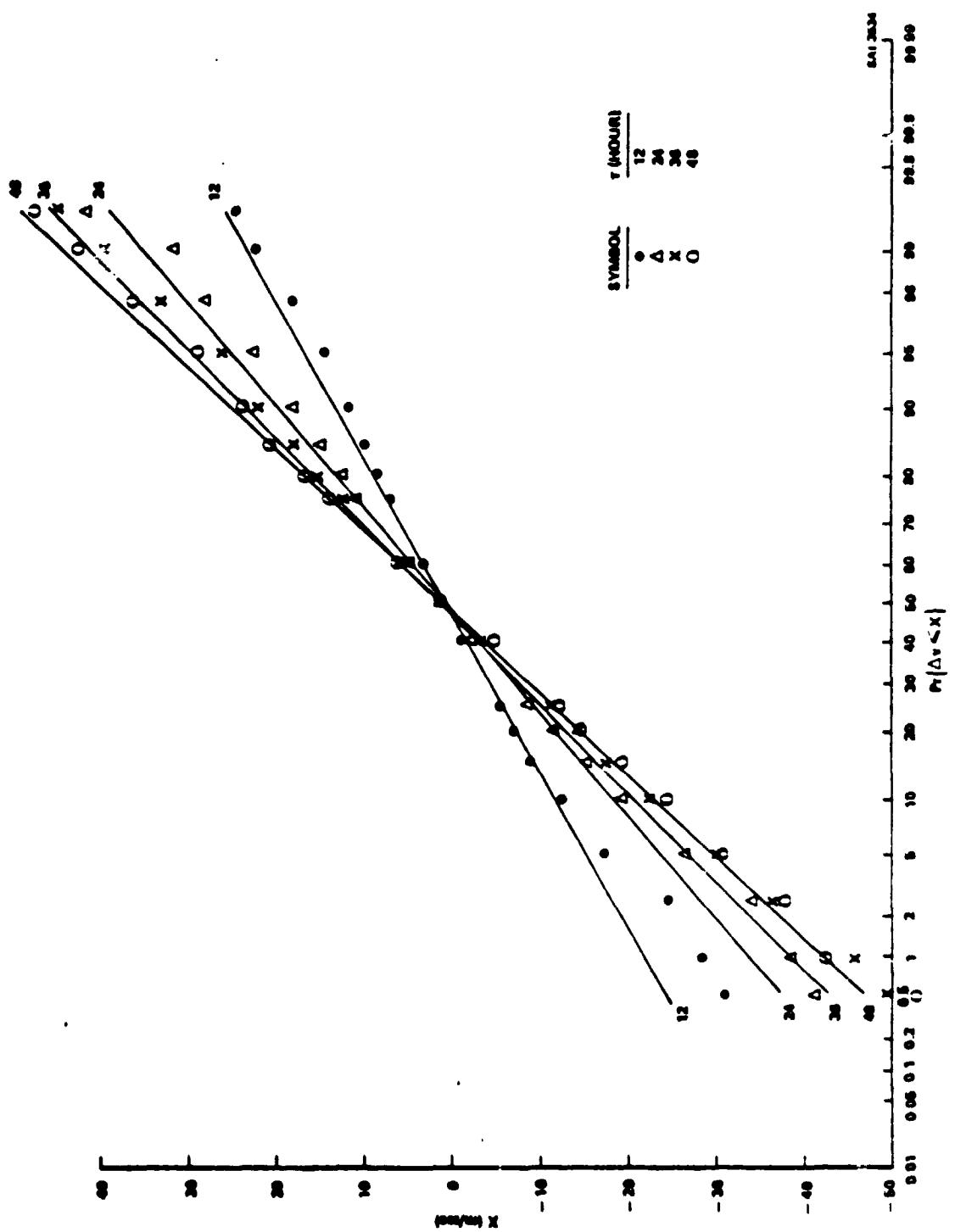


Figure 9. Theoretical (Straight Lines) and Observed (Plotted Points) Cumulative Probability Distribution of Meridional Wind Bias Component Change, Δv , with Respect to Time Increment, t , During January at 12 km Over Vandenberg AFB (1965-74)

ORIGINAL PAGE IS
OF POOR QUALITY

by the theoretical normal distribution for a large range of probabilities; the deviation of the observed distribution from the theoretical distribution at the extreme probabilities is attributed to the small sample of observations and errors in the Rawinsonde data.

C. JOINT DISTRIBUTION OF WIND BIAS COMPONENT CHANGES WITH RESPECT TO TIME

The joint distribution of zonal and meridional wind bias component change with respect to time (Δu and Δv) can be approximated by a bivariate normal distribution. A useful property of such a distribution is that an ellipse can be calculated which contains the end points of a specified percent of vectors having components Δu and Δv . A detailed description of the derivation of probability ellipses and plotting methodology is given by Smith [3]. The five parameters of the bivariate normal distribution of Δu and Δv , calculated for each monthly reference period at KSC and VAFB at 1 km altitude intervals from 5 to 22 km are listed in the appendix.

The degree of approximation of the bivariate normal distribution to the observed distribution can be evaluated by comparison of the observed percentage of vectors which are contained within the ellipse to that predicted by the ellipse at a specified probability level. For example, for a sample of 1,000 vectors, 950 of the vectors should terminate within the 95 percent (theoretical $P = .95$) ellipse calculated from the bivariate statistics of the 1,000 vectors; however, a plot of the 1,000 vectors could indicate that only 945 vectors (observed $p=.945$) terminate within the 95 percent ellipse. For illustration on a linear graph comparison of the theoretical to the observed P is given in terms of the parameter λ_e given by

$$\lambda_e = \sqrt{2} \sqrt{-\ln(1-P)} \quad (24)$$

A comparison of theoretical and observed values of λ_e at 12 km during April at KSC and January at VAFB for time intervals of 12, 24, 36 and 48 hours is illustrated in Figures 10 and 11. Perfect agreement between theoretical and observed λ_e is represented by a line drawn from the origin with a slope, B , equal to 1. The calculated least squares slopes are given in the figure legend. The plots indicate a tendency for the theoretical λ_e to exceed the

ORIGINAL PAGE IS
OF POOR QUALITY

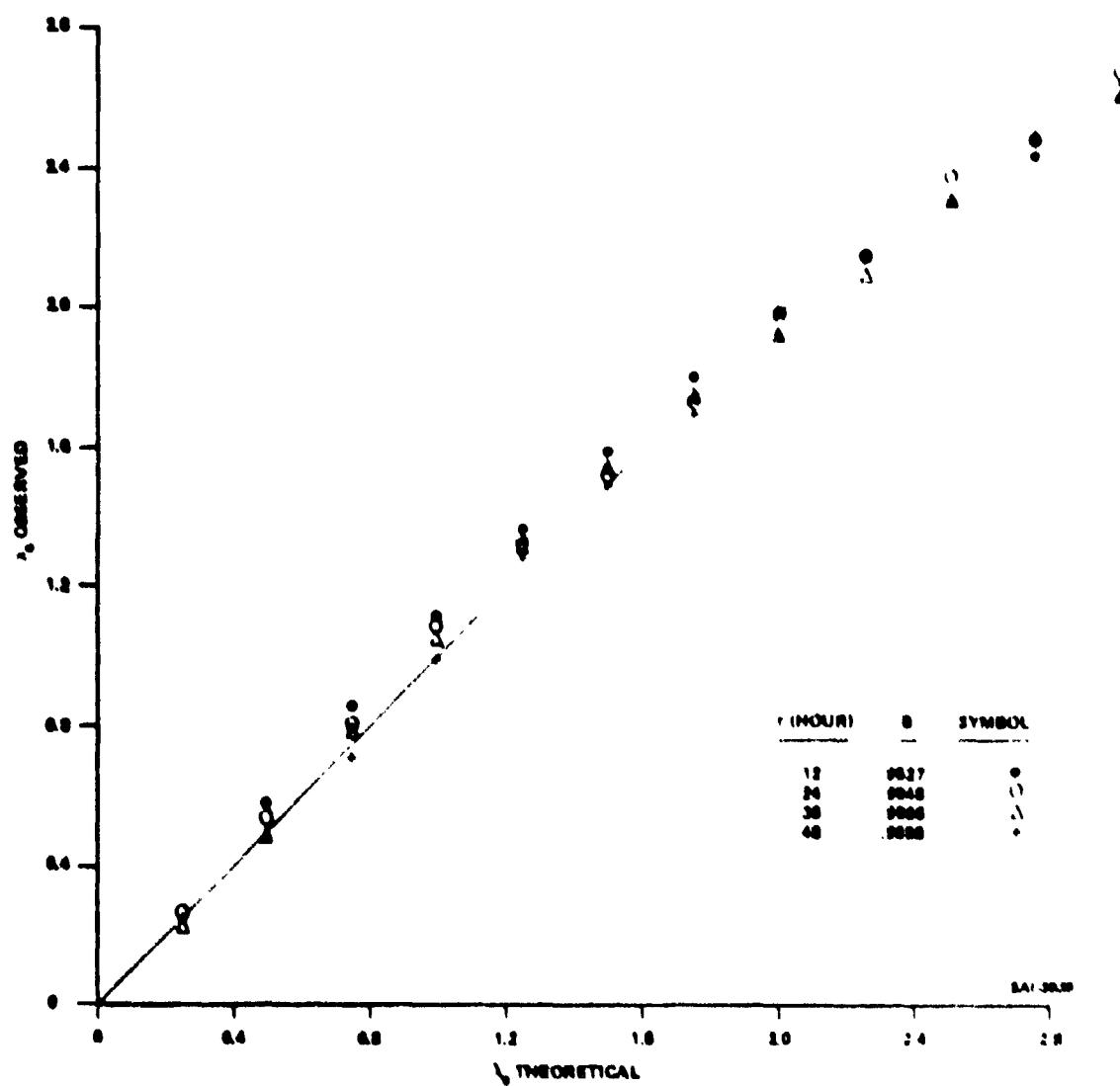


Figure 10. Observed λ_c as a Function of Theoretical λ_c for a Bivariate Normal Distribution of Wind Bias Component Changes ($\Delta u, \Delta v$) with Respect to Time at 12 km During April 1956-70 at Cape Kennedy

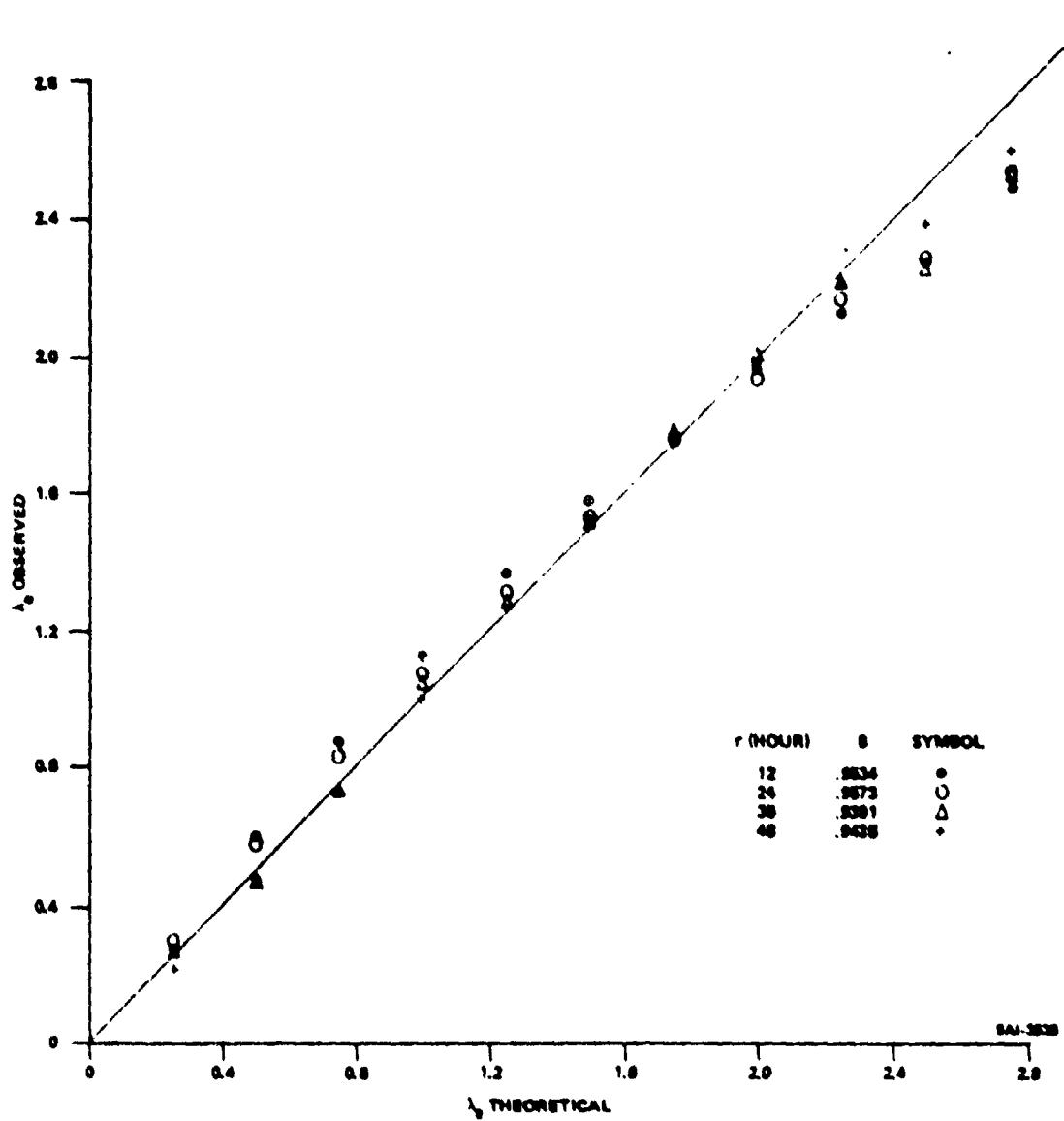


Figure 11. Observed λ_e as a Function of Theoretical λ_e for a Bivariate Normal Distribution of Wind Bias Component Changes ($\Delta u, \Delta v$) with Respect to Time at 12 km During January (1965-74) at Vandenberg AFB

observed λ_e for large values of λ_e . The interpretation of this result is that for extreme probabilities the theoretical distributions predict fewer wind change vectors terminating outside the ellipse than is observed. These results may have to be taken into consideration if engineering application of theoretical wind change statistics beyond 95 percent level is required.

The 95 percent probability ellipses for the joint distribution of wind bias component changes with respect to time at 6, 12, and 18 km during April at KSC and January at VAFB are illustrated in Figure 12; the relatively large changes with respect to time at 12 km is clearly illustrated at both locations.

D. MODULUS OF VECTOR WIND BIAS CHANGE WITH RESPECT TO TIME

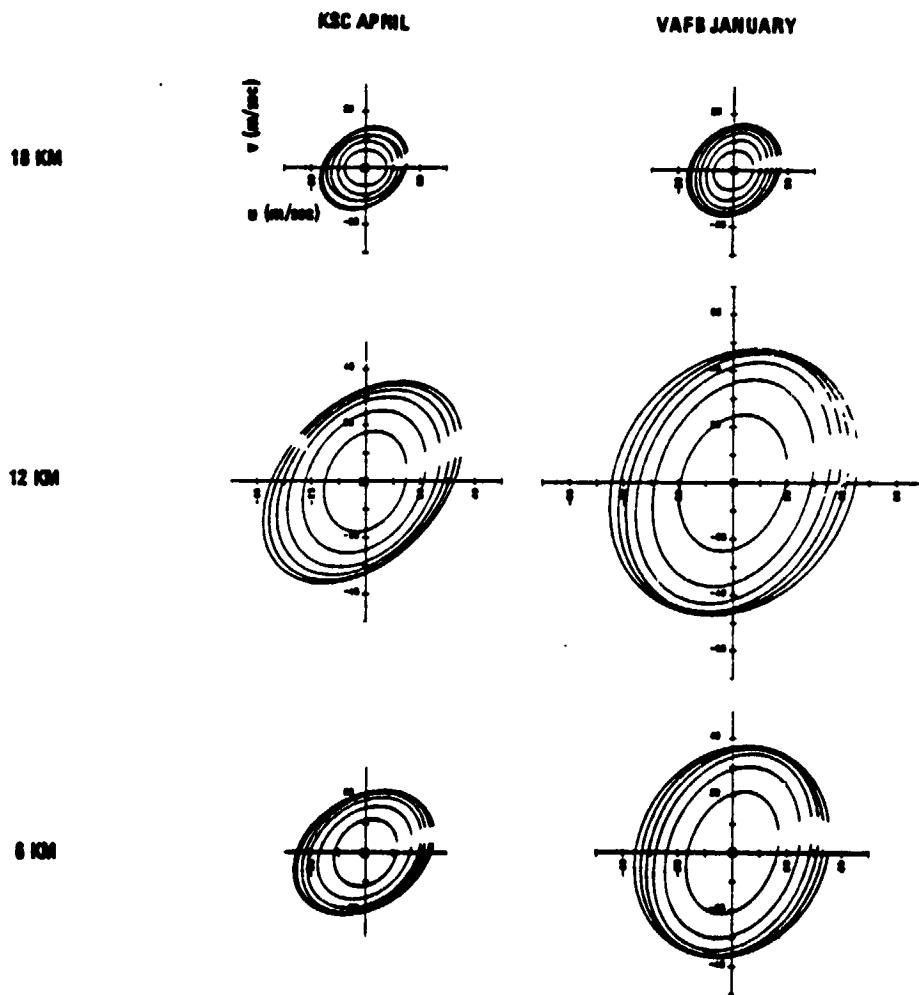
If wind bias change with respect to time has a distribution which is bivariate normal, the modulus R , of the wind bias change vector (defined by Equation 5) has a Rayleigh distribution. Since the Rayleigh distribution cannot be integrated in closed form, numerical integration is required to obtain the cumulative probability distribution. Derivation of the Rayleigh distribution, given the five bivariate normal distribution statistics, requires summation involving products of the modified Bessel function of the first kind. Smith [3] summarizes the basic equations for the Rayleigh distribution derived by Wier [5] and extended by Yadavalli [6] to include the condition for correlated variables. The Rayleigh distribution reduces to the integrable classical form if it is assumed that the components of the vector wind change are independent and that they have zero means and equal standard deviations; the classical Rayleigh probability density function is

$$f(R) = \frac{R}{\sigma^2} \exp(-R^2/2\sigma^2) \quad R \geq 0 \quad (25)$$

Integration of Equation 25 from zero to a specified value of R yields the cumulative probability that $R \leq R^*$ where,

$$\Pr\{R \leq R^*\} = 1 - \exp(-R^2/2\sigma^2) \quad R \geq 0 \quad (26)$$

where $\sigma = \sigma_{\Delta u} = \sigma_{\Delta v}$



THE SIX ELLIPSES FOR EACH ALTITUDE AND MONTH ARE FOR TIME INCREMENTS AT 12-HOUR INTERVALS FROM 12 TO 72 HOURS; THE AREA OF THE ELLIPSES INCREASES WITH INCREASING TIME INTERVAL.

SAI-3846

Figure 12. Joint Distribution of 95 Percent Wind Bias Component Changes with Respect to Time at 6, 12 and 18 km During April at Cape Kennedy (1956-70) and January at Vandenberg (1965-74)

ORIGINAL PA
OF POOR QU

Since the standard deviation of the component difference can be expressed as a function of the standard deviation of the components (Equations 22 and 23) it follows that

$$\Pr \{R \leq R^*\} = 1 - \text{EXP} \left[- \frac{R^2}{4\sigma_k^2 [1 - \text{EXP}(-k\tau)]} \right] \quad (27)$$

where σ_k and k correspond to either σ_u and b or σ_v and C given in Equations 22 and 23.

An expression for R given a particular probability, $\Pr \{R \leq R^*\}$, is obtained by solution of Equation 27 to obtain

$$R = \sqrt{2} \lambda_e \sigma_k \sqrt{1 - \text{EXP}(-k\tau)} \quad (28)$$

where λ_e is derived from Equation 24 denoting $\Pr \{R \leq R^*\}$ by P

The choice of $\sigma_k = \sigma_v$ and $k = c$ (from Equation 23) at 12 km during April at KSC and January at VAFB yields the most accurate approximation of the cumulative Rayleigh distribution obtained by numerical integration of Equation 28 in Reference 1. Comparisons of the 99, 95, and 50 percentile modulus of the wind change vector with respect to time based on the Rayleigh (Equation 28, Reference 1) and the classical Rayleigh (Equation 27) are illustrated in Figures 13 and 14; the rather good agreement between the distributions for time intervals from 12 to 72 hours is attributable to the accuracy of the simplifying assumptions described above. There is a slight tendency, especially for time intervals ≤ 36 hours for the classical Rayleigh to be larger than the Rayleigh.

The remaining question is: How well do these theoretical distributions compare with observed observations? Comparisons of observed and theoretical values of R for time intervals of 12, 24, 36 and 48 hours at 12 km during November, December and January at VAFB are given in Tables 5 and 6; column II of the tables contains R calculated according to the classical Rayleigh distribution with σ equal to the monthly value of σ_v at 12 km and k equat to the decay constant, c, in the monthly exponential least squares

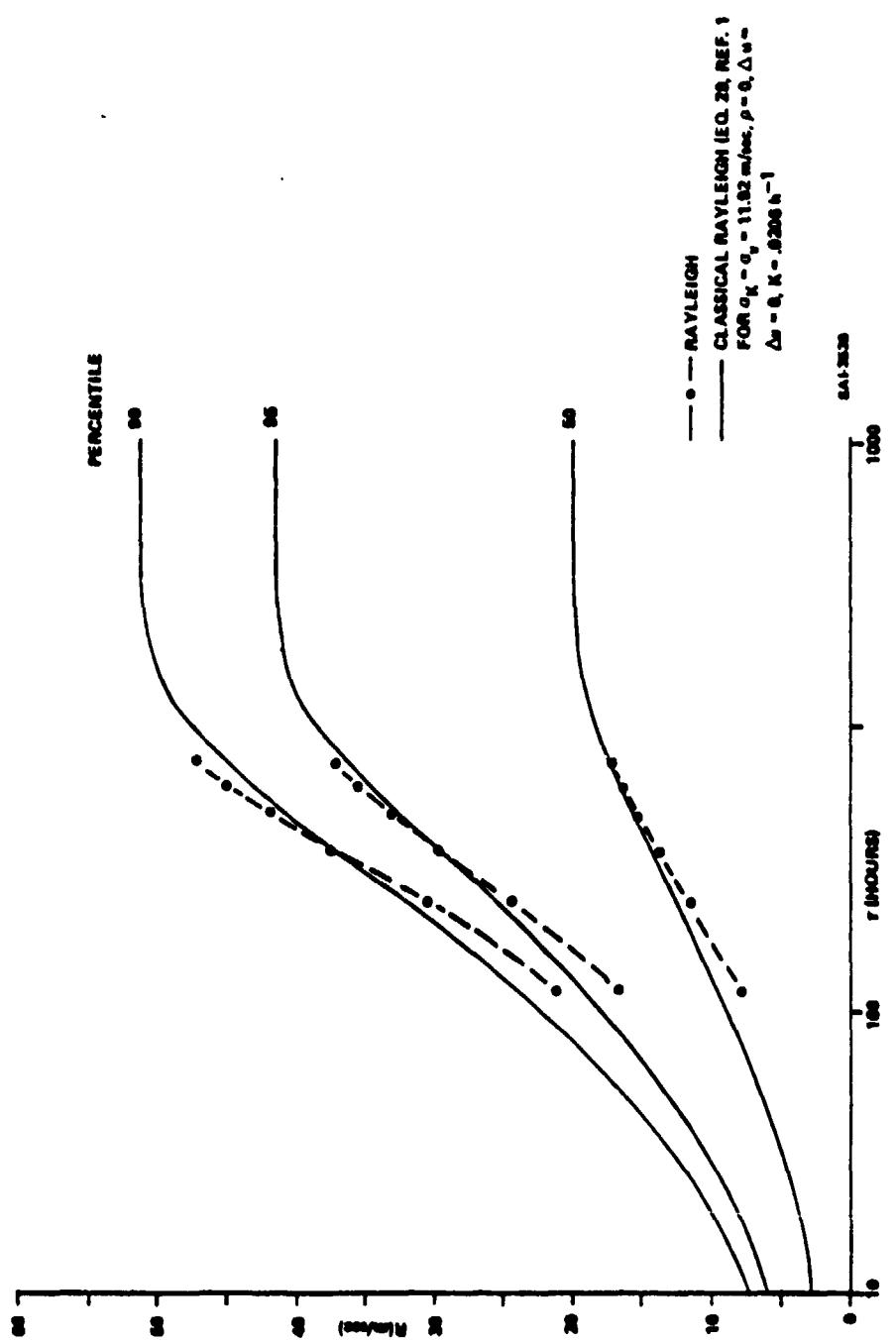


Figure 13. April Theoretical Percentiles of Modulus, P , of Vector Wind Bias Change with Respect to Time Interval, τ , at 12 km Over Cape Kennedy (1956-70)

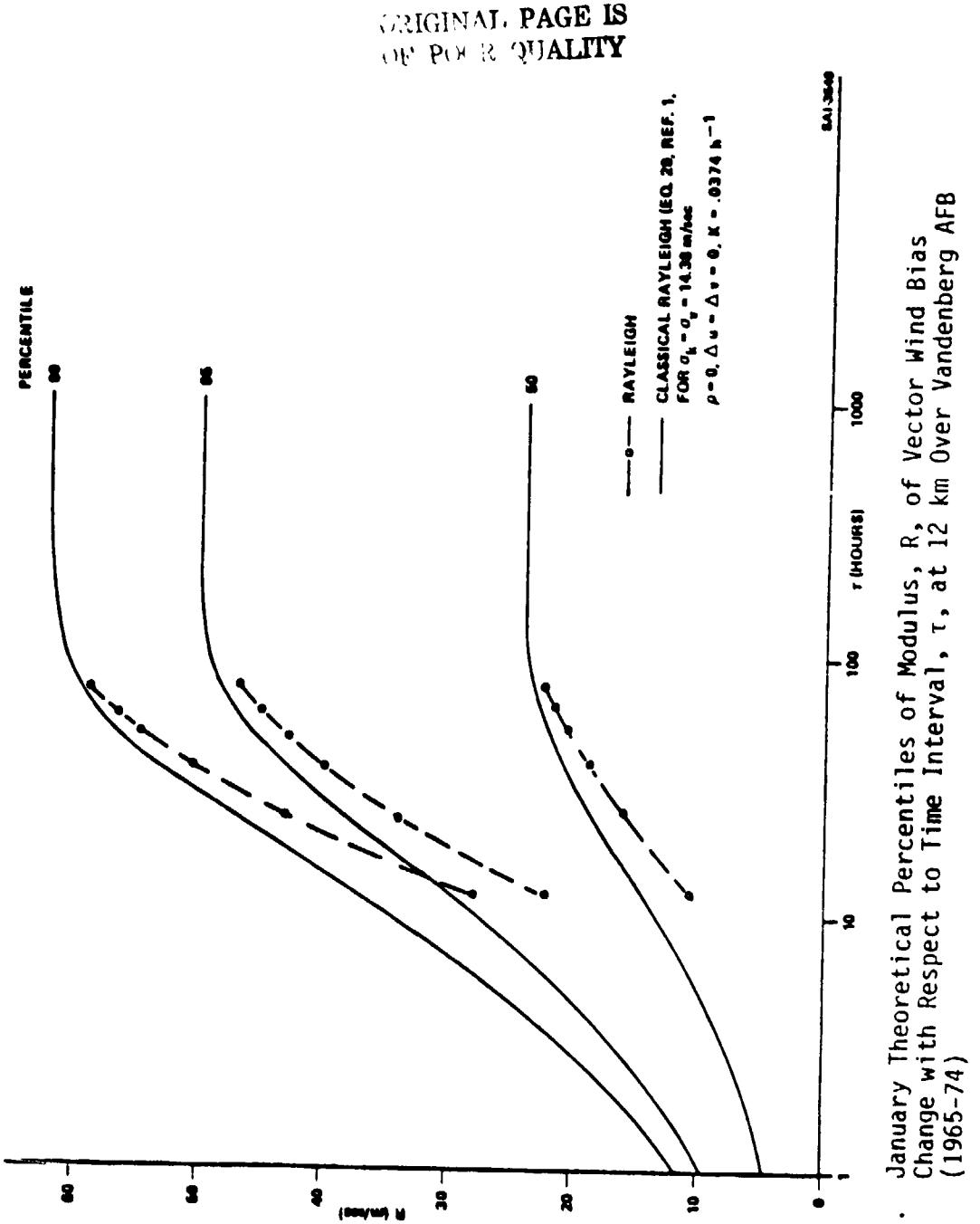


Figure 14. January Theoretical Percentiles of Modulus, R , of Vector Wind Bias Change with Respect to Time Interval, τ , at 12 km Over Vandenberg AFB (1965-74)

τ (HOURS)	$P_r\{R < R^*\}$	12		24		36		48				
		I	II	OBSERVED	I	II	OBSERVED	I	II	OBSERVED		
.50	7.89	9.29	7.01	11.41	12.40	10.08	13.80	14.36	12.68	15.20	15.73	14.21
.60	9.09	10.68	8.11	13.16	14.25	11.80	15.92	16.51	14.60	17.56	18.08	16.52
.75	11.25	13.14	10.34	16.28	17.53	15.71	19.73	20.31	18.86	21.78	22.24	20.85
.80	12.14	14.15	11.47	17.59	18.89	17.30	21.33	21.89	20.48	23.57	23.97	22.56
.84134	13.00	15.14	12.56	18.86	20.20	18.46	22.88	23.41	22.35	25.31	25.63	24.41
.86	13.22	15.37	12.81	19.15	20.51	18.71	23.25	23.76	22.87	25.73	26.02	24.80
.90	14.63	16.93	15.05	21.21	22.51	21.36	25.77	26.18	26.57	28.55	28.67	28.00
.95	16.78	19.31	17.80	24.39	25.77	25.50	29.68	29.86	31.37	32.93	32.70	33.20
.97502	18.74	21.43	21.38	27.26	28.60	30.36	33.24	33.14	36.88	36.93	36.29	39.70
.97725	18.96	21.70	21.88	27.63	28.96	30.65	33.70	33.55	37.76	37.46	36.75	40.26
.98734	20.51	23.32	25.87	29.85	31.12	34.54	36.46	36.06	41.40	40.57	39.49	48.30
.99000	21.06	23.94	26.40	30.73	31.95	37.00	37.53	37.02	42.00	41.77	40.54	51.00
.99500	22.73	25.68	27.50	33.15	34.27	42.75	40.54	39.71	48.60	45.16	43.49	59.75

COLUMN I: CALCULATIONS OF R BASED ON Eqs. 28a AND 28b OF REF. 1 AND NUMERICAL INTEGRATION OF THE RAYLEIGH PROBABILITY DENSITY FUNCTION.

COLUMN II: CALCULATIONS OF R BASED ON EQ.30 OF THIS TEXT AND ASSUMING $\sigma_v = \sigma_u = 11.92$ m/sec, K = C = .0206 hr⁻¹ AND $\Delta u = \Delta v = 0$.

Table 5. Theoretical and Observed Modulus, R(m/sec), of Vector Wind Bias Change with Respect to Time Interval, τ , During April (1956-70) at 12 km Over Cape Kennedy

SAI-3619

τ (HOURS)	12			24			36			48			
	$P_r\{H < R^*\}$	I	II	OBSERVED									
.50	10.52	14.39	9.47	15.82	18.43	14.76	18.73	20.59	18.25	20.38	21.86	19.91	
.60	12.13	16.55	11.22	18.25	21.18	17.74	21.61	23.67	21.42	23.49	25.14	23.55	
.75	17.99	20.36	14.35	22.60	26.06	21.88	26.74	29.12	25.93	29.04	30.92	28.53	
.80	16.20	21.93	15.62	24.43	28.00	23.89	28.90	31.38	28.17	31.37	33.31	30.58	
.84134	17.38	23.46	16.68	26.21	30.03	26.23	31.00	33.56	30.47	33.64	35.63	33.08	
.850	17.65	23.81	16.95	26.63	30.48	27.00	31.50	34.07	30.92	34.17	36.17	33.75	
.900	19.64	26.23	20.18	29.50	33.58	30.60	34.87	37.53	34.50	37.81	39.85	37.60	
.95	22.45	29.92	24.86	33.84	38.31	35.33	40.12	42.81	41.50	43.44	45.45	42.40	
.97502	25.06	33.21	28.10	37.98	42.51	40.17	44.88	47.51	46.51	48.55	50.44	48.76	
.97725	25.42	33.63	28.38	38.52	43.05	40.63	45.50	48.11	47.30	49.18	51.08	50.45	
.98134	27.47	36.14	32.15	41.66	46.26	44.79	49.19	51.70	51.15	53.14	54.89	56.58	
.99	28.25	37.10	33.40	42.87	47.49	45.80	50.62	53.08	52.80	54.67	56.35	57.80	
.995	30.49	39.80	35.90	46.30	50.84	49.90	54.65	56.93	59.90	58.96	60.44	60.90	

COLUMN I. CALCULATIONS OF R BASED ON Eqs. 28a AND 28b OF REF. 1 AND NUMERICAL INTEGRATION OF THE RAYLEIGH PROBABILITY DENSITY FUNCTION.

COLUMN II: CALCULATIONS OF R BASED ON EQ. 30 OF THIS TEXT AND ASSUMING $v = v_0 = 14.38$ m/sec, $K = C = .0374 \text{ hr}^{-1}$ and $f_{u,v} = L_{u,v} = 0$.

SAI-3618

Table 6. Theoretical and Observed Modulus, R(m/sec), of Vector Wind Bias Change with Respect to Time Interval, τ , During January (1965-74) at 12 km Over Vandenberg AFB

fit to the v component autocorrelation function (Equation 23); Column I was obtained by numerical integration of the Rayleigh distribution. It is indicated that the observed cumulative distribution agrees fairly well with the theoretical distribution for probabilities less than .95 to .975. For large probabilities, there is a consistent tendency for the theoretical distribution to underestimate the observed distribution. This tendency is attributable to the small sample of data available at the extreme probabilities and errors in the Rawinsonde data.

E. CONDITIONAL VECTOR WIND BIAS ELLIPSES

Prior knowledge that environmental constraints necessary to assure the success of a space vehicle launch will be satisfied implies that there is a capability for prediction of environmental parameters; the prediction can be based on knowledge of conditions prior to launch. With regard to winds aloft, prior conditions are typically based on Rawinsonde or Jimsphere wind profiles. A typical question that could be posed before launch is: Given a measurement of the wind bias vector 12 prior to launch at 12 km, will the wind bias vector at launch time be within 95 percent reference month wind ellipse? A question of this type can be answered if the distribution of vector wind bias components at an initial time, T_0 , and at a future time, T_1 , can be approximated by a quadravariate normal distribution. Given the components of the bias vector at T_0 , the conditional distribution of the bias vector at T_1 is bivariate normal. Smith [1] describes the derivation of the conditional bivariate normal distribution and documents the computer program used in this investigation for calculation of these distributions. Figures 15 and 16 illustrate the 95 percent conditional bivariate normal distributions at 12 km that have been calculated for time increments of 12, 24, 36, 48, 60 and 72 hours for the month of April at KSC and January at VAFB. Five vectors were selected as given initial conditions for calculations of the conditional ellipses. The components of the vectors are defined below:

1. Monthly bias component means
2. Maximum zonal wind bias and the corresponding meridional wind bias from the monthly 95 percent vector wind bias ellipse.
3. Minimum zonal wind bias and the corresponding meridional wind bias from the monthly 95 percent vector wind bias ellipse.

ORIGINAL PAGE IS
OF POOR QUALITY

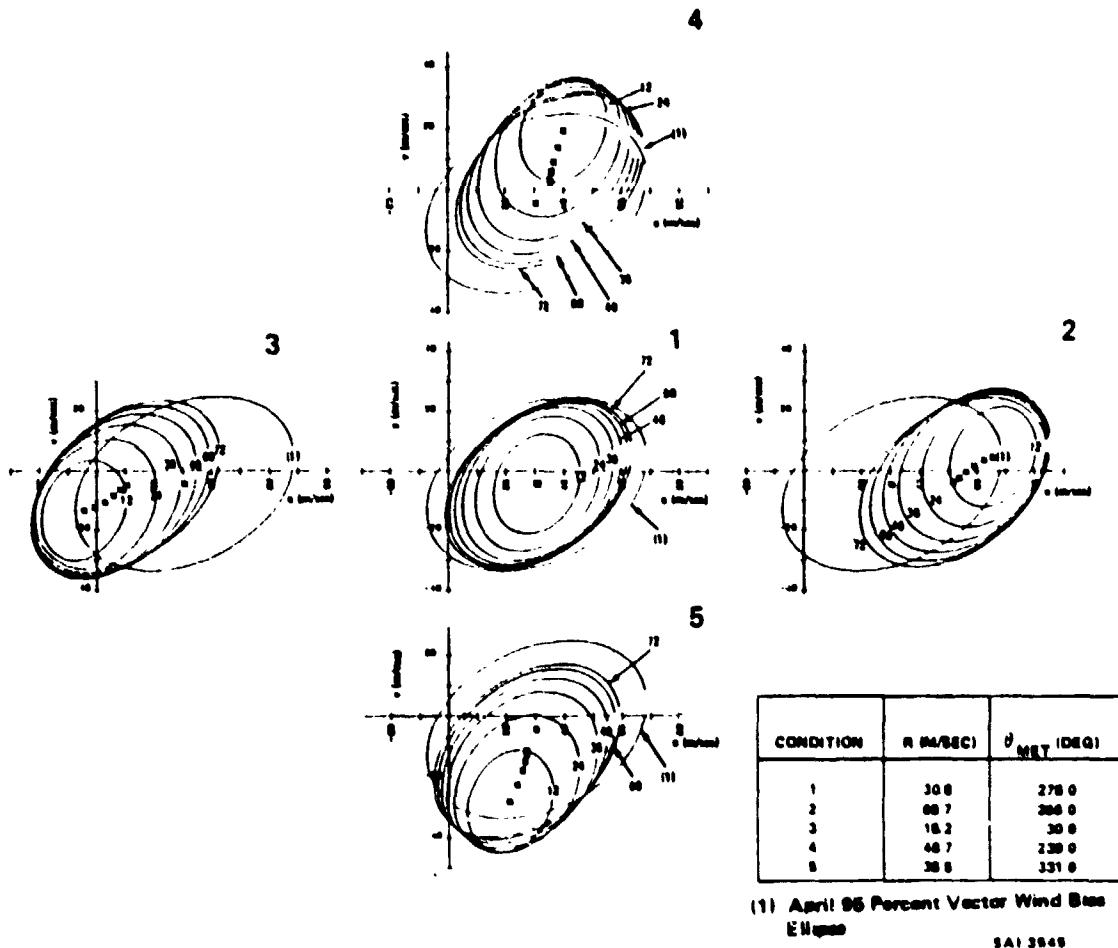


Figure 15. April Conditional 95 Percent Wind Bias Ellipses at 12 km for Time Increments of 12, 24, 36, 48, 60 and 72 Hours at Cape Kennedy (1956-70)

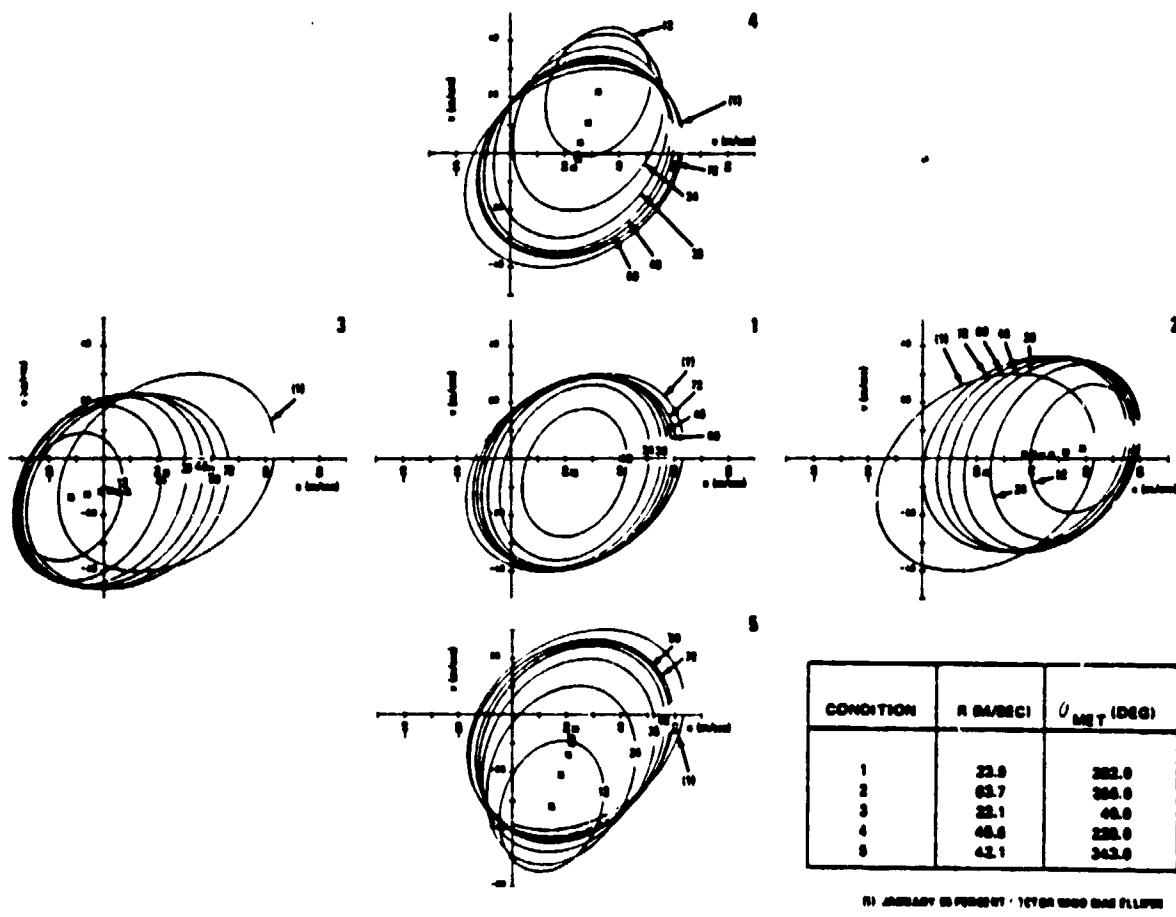


Figure 16. January Conditional 95 Percent Wind Bias Ellipses at 12 km for Time Increments of 12, 24, 36, 48, 60 and 72 Hours at Vandenberg AFB (1965-74)

4. Maximum meridional wind bias and the corresponding zonal wind bias from the monthly 95 percent vector wind bias ellipse.
5. Minimum meridional wind bias and the corresponding zonal wind bias from the monthly 95 percent vector wind bias ellipse.

The given vectors are specified in the inset of Figures 15 and 16 (polar form, at 12 km) and in Tables 7 and 8 (component form, at 6, 12, 18 km).

The conditional ellipses illustrated at the center of Figures 15 and 16 show that if the observed wind vector has components equivalent to the monthly mean bias components (condition 1) then 95 percent of the wind vectors after elapsed times as large as 72 hours will fall within the monthly 95 percent ellipse. Therefore, satisfaction of a launch constraint which states that the wind bias vector must be included within the 95 percent monthly ellipse would be assured for periods as long as 72 hours following an observation of a wind vector having components which correspond to the monthly means. The conditional ellipses based on selection of given wind bias vectors that terminate on the monthly 95 percent ellipse (conditions 2 through 5) have a significant proportion of their area lying outside the monthly 95 percent ellipse; as the time increment increases this proportion decreases but remains significant for a time increment as large as 72 hours. This implies that a significant proportion of wind bias vectors will not satisfy a launch constraint based on the 95 percent wind bias ellipse for periods as long as 72 hours (or longer if these calculations are extended) following an observation of a wind bias vector which terminates on the 95 percent ellipse.

The wind direction characteristics of a wind bias ellipse can be described in terms of the angles associated with wind bias vectors constructed between the origin and the center of the ellipse (at the component means) and between the origin and the two tangent positions to the ellipse. The three vectors constructed in this manner and the angles θ_A , θ_B , θ_E and $\Delta\theta$ are illustrated in Figure 17, the range of wind angles, θ_R , is θ_A to θ_B . The angles θ_R , θ_E , $\Delta\theta$ calculated from five 95 percent conditional ellipses for April at KSC and January at VAFB at 6, 12 and 18 km are listed in Tables 7 and 8.

CONDITION (°)	θ_e	θ_A	θ_B	$\Delta\theta$
1	278	248	313	65
2	268	252	281	39
3	20	•	•	•
4	244	225	268	41
5	323	293	349	56

- (*) THE FIVE CONDITIONAL DISTRIBUTIONS ARE BASED ON THE FIVE GIVEN WIND VECTORS LISTED BELOW. CONDITION 1 IS BASED ON MONTHLY MEAN WIND BIAS COMPONENTS FOR THE PERIOD 1956-70; CONDITIONS 2 THRU 5 ARE FROM THE 95 PERCENT VECTOR WIND BIAS ELLIPSE AT 12 KM THAT WAS CALCULATED FROM TWICE DAILY FILTERED RAWINSONDE DATA DURING THE PERIOD 1956-70.
- 95 PERCENT CONDITIONAL ELLIPSE COVERS ALL QUADRANTS.

CONDITIONS	M/SEC		
1	u, v	30.44	- 4.35
2	u _{max} , v	68.53	4.46
3	u _{min} , v	- 7.65	- 13.16
4	u, v _{max}	41.94	24.83
5	u, v _{min}	18.94	- 33.63

SAI-3627

Table 7. Wind Direction (Degrees) Characteristics of 95 Percent Conditional Vector Wind Bias Ellipses at 12 km Over Cape Kennedy During April for an Elapsed Time, τ , of 12 Hours

ORIGINAL PAGE IS
OF POOR QUALITY

CONDITION(*)	θ_0	θ_A	θ_B	M
1	282	229	343	114
2	266	246	290	44
3	41	-	-	-
4	236	208	272	64
5	336	293	8	76

- (*) THE FIVE CONDITIONAL DISTRIBUTIONS ARE BASED ON THE FIVE GIVEN WIND VECTORS LISTED BELOW. CONDITION 1 IS BASED ON MONTHLY MEAN WIND BIAS COMPONENTS FOR THE PERIOD 1966-74; CONDITIONS 2 THRU 5 ARE FROM THE 95 PERCENT VECTOR WIND BIAS ELLIPSES AT 12 KM THAT WERE CALCULATED FROM TWICE DAILY FILTERED RAWINSONDE DATA DURING THE PERIOD 1966 -74.
- 95 PERCENT CONDITIONAL ELLIPSE COVERS ALL QUADRANTS.

CONDITION		M/SEC	
1	u, v	23.36	- 4.96
2	u_{max}, v	63.50	4.47
3	u_{min}, v	- 16.78	- 14.37
4	u, v_{max}	34.11	30.26
5	u, v_{min}	12.61	- 40.16

SAI JB28

Table 8. Wind Direction (Degrees) Characteristics of 95 Percent Conditional Vector Wind Bias Ellipses at 12 km Over Vandenberg AFB During January for an Elapsed Time, t , of 12 Hours

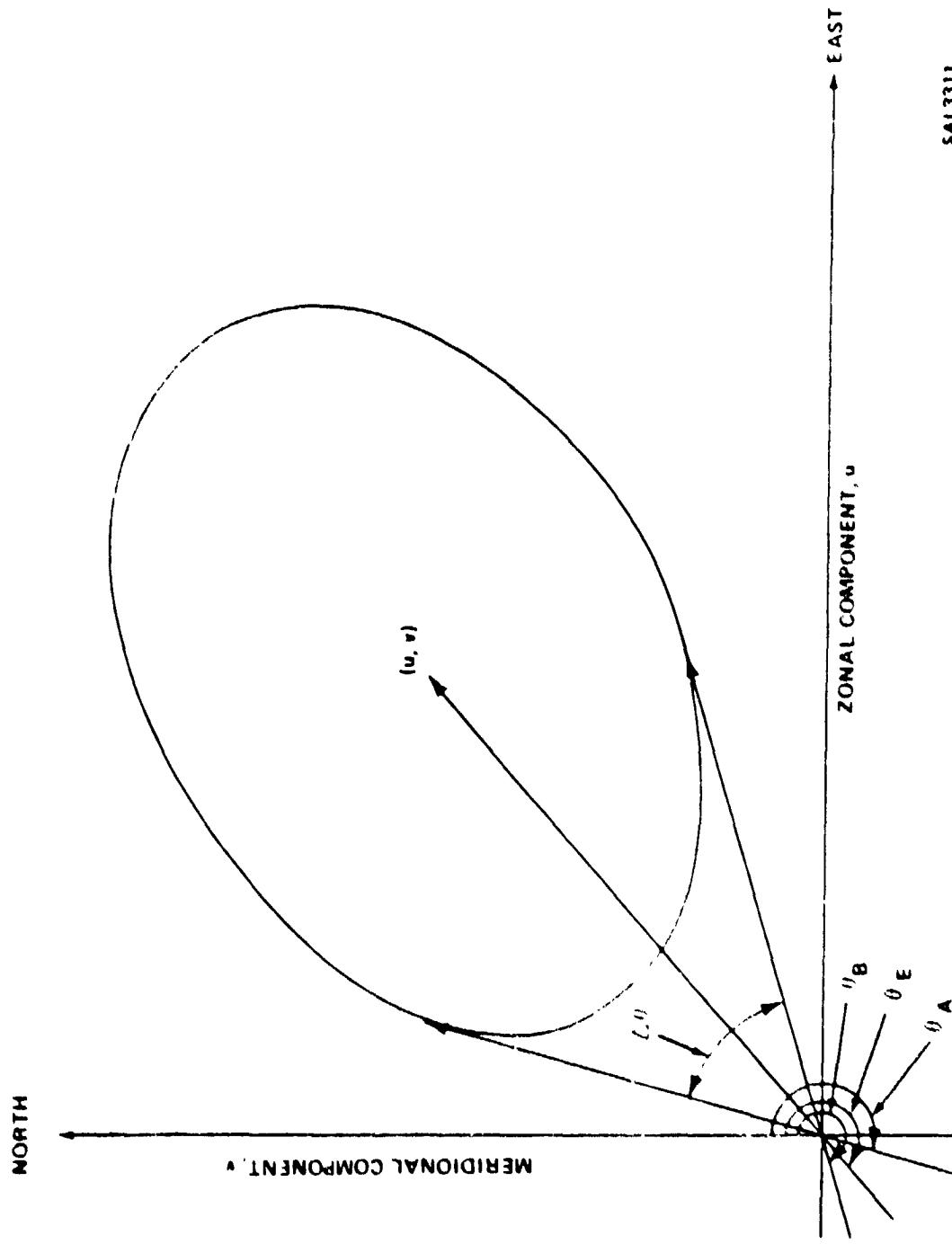


Figure 17. Wind Direction Characteristics of a Vector Probability Ellipse

IV. CONCLUSIONS

The analysis presented in the preceding section for selected months and altitudes illustrates how various theoretical distribution functions can be used for calculation of wind bias change with respect to time at Cape Kennedy, Florida and Vandenberg AFB, California. The calculations can be made by utilization of the statistics given in the appendix for any reference month at 1 km altitude increments from 0 to 27 km. It also has been shown that the techniques originally used to describe wind change observed in unfiltered Rawinsonde profiles can also be applied with equivalent accuracy to describe wind bias change.

The basic underlying assumption for the calculation of the distributions of wind bias change is that the joint distribution of the four variables represented by the components of the wind bias vector at any initial time and after a specified elapsed time is quadravariate normal. If the wind bias vector is specified at an initial time, then the conditional joint distribution of the wind bias components at a future time is bivariate normal. Since each of the variables of the quadravariate normal distribution is normal and the difference of two normal distributions is normal, it follows that wind bias component change is also normal and the joint distribution of zonal and meridional wind bias change is bivariate normal. The modulus of bivariate normally distributed variables has a Rayleigh distribution. Therefore, the modulus of vector wind bias change with respect to time is Rayleigh.

Sample distributions based on reference month Rawinsonde data obtained during January 1965-74 at Vandenberg AFB and April 1956-70 at Cape Kennedy agree reasonably well with the aforementioned theoretical distributions.

The standard deviation of wind bias component change with respect to time is the only statistic required for determination of the theoretical probability distribution (normal with zero mean) of wind bias component change. It has been shown than over a large range of altitudes that this statistic can be estimated from wind bias component standard deviation and the decay constant of the component theoretical autocorrelation function (Table 1). The assumption of exponential decay of the autocorrelation function is reasonably accurate in most instances to time increments as large as 72 hours at both locations.

The observed modulus of vector wind bias change with respect to time is systematically larger than the predicted modulus (Section III.C) for extreme probabilities. This may be attributable to inadequacy of the theory or inaccuracies of the data which affect the observed distribution at the extreme probabilities. If the theoretical distribution at extreme probabilities is to be used in engineering applications, it will be necessary to explain these systematic differences.

V. REFERENCES

1. Adelfang, S. I.: Analysis of Vector Wind Change with Respect to Time for Cape Kennedy, Florida. Science Applications, Inc., Report SAI-78-552-HU, prepared for NASA-Marshall Space Flight Center under Contract NAS8-32226, 14 April 1977.
2. Adelfang, S. I.: Analysis of Vector Wind Change with Respect to Time for Vandenberg Air Force Base, California. Science Applications, Inc., Report SAI-78-668-HU, prepared for NASA-Marshall Space Flight Center under Contract NAS8-32226, 1 December 1977.
3. Smith, O. E.: Vector Wind and Vector Wind Shear Models 0-27 km Altitude for Cape Kennedy, Florida, and Vandenberg AFB, California. NASA TMX-73319, July 1976.
4. DeMandel, R. E. and Krivo, S. J.: Selecting Digital Filters for Application to Detailed Wind Profiles. NASA CR-61325.
5. Weil, H.: The Distribution of Radial Error. Ann. of Mathematical Statistics, Vol. 25, 1954, pp. 168-170.
6. Yadavalli, S. V.: On Applications of Some Results Related to Bivariate Gaussian Density Distribution Functions. Int. J. of Control. 1st Series, Vol. 5, No. 2, 1967, pp. 191-194.

APPENDIX

This appendix contains two sets of reference month quadravariate and conditional bivariate normal statistics of variables X, Y, XP and YP, at 1 km intervals from 5 to 22 km. The statistics were calculated from serially complete twice daily wind bias profiles calculated from Rawinsonde profiles obtained during the period 1965-74 at VAFB and 1956-70 at KSC. The notation for the variable given in Section II of this report differs from the notation established for the computer output given herein; the notations are compared in Table A-1.

TABLE A-1. NOTATION OF VARIABLES

Computation Set		A		B	
Variable		Text (Sect. II)	Computer Output	Text (Sect. II)	Computer Output
X		u_0	$u(\text{at } T)$	u_0	$u(\text{at } T)$
Y		v_0	$v(\text{at } T)$	v_0	$v(\text{at } T)$
XP		u_1	$u(\text{at } T+DT)$	$u_1 - u_0$ $= \Delta u$	$u(\text{at } T+DT)$ $-u(\text{at } T)$
YP		v_1	$v(\text{at } T+DT)$	$v_1 - v_0$ $= \Delta v$	$v(\text{at } T+DT)$ $-v(\text{at } T)$

Table A-1 shows that the quadravariate statistics of computation set "A" are for wind bias components at an initial time and after a specified time increment; the statistics for set "B" are for wind bias components at an initial time and wind bias component change after a specified time increment. The reference month quadravariate normal statistics at a particular altitude for six time increments (12, 24, 36, 48, 60 and 72 hours) are listed in the lower left of each page of computer listing; the six sets of conditional bivariate normal statistics corresponding to the six time increments are listed in the lower right. The data were conditioned on monthly means for the entire data sample. The derivation of the conditional bivariate normal statistics for any other given vector involves recalculation of the

conditional means according to equations A-1 and A-2; the standard deviations and correlation coefficients do not have to be recalculated because they are independent of the given wind vector.

$$\bar{x}_c |_{xp^*=\bar{x}} + \frac{[(R(x,xp) - R(x,yp) R(xp,yp)) (xp^* - \bar{x}) (\sigma_x/\sigma_{xp})] + [(R(x,yp) - R(x,xp) R(xp,yp)) (yp^* - \bar{y}) (\sigma_x/\sigma_{yp})]}{1 - [R(xp,yp)]^2} \quad (A-1)$$

$$\bar{y}_c |_{yp^*=\bar{y}} + \frac{[(R(y,xp) - R(y,yp) R(xp,yp)) (xp^* - \bar{x}) (\sigma_y/\sigma_{xp})] + [(R(y,yp) - R(y,xp) R(xp,yp)) (yp^* - \bar{y}) (\sigma_y/\sigma_{yp})]}{1 - [R(xp,yp)]^2} \quad (A-2)$$

where, \bar{x}_c and \bar{y}_c are the mean components of the conditional distribution, xp^* and yp^* are the components of the given vector and $\sigma_x, \sigma_y, \sigma_{xp}$ and σ_{yp} are equivalent to S.D.x, S.D.y, S.D.xp and S.D.yp, respectively given in the computer listings.

QUADRATIC

AND

CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP

STATION (128181) - CAFE KENNEDY

MONTH OF RECORD - APRIL

PLANE OF REFERENCE - 1/56 - 12/70

ALTAIA ANGLE - 90.0

ALTITUDE (KFM)

QUADRATIC NORMAL STATISTICS OF X,Y,XP,YP

	MEAN X XP	S.D. X XP	R (X,XP)	MEAN Y YP	S.D. Y YP	R (Y,YP)	MEAN R (XP,YP)	S.D. R (XP,YP)	R (YP,X)	MEAN R (YP,X)	S.D. R (YP,X)	MEAN R (XP,YP)	S.D. R (XP,YP)	MEAN R (YP,XP)	S.D. R (YP,XP)
1	11.29	9.40	.1510	-1.58	6.34	6.00	-.0000	0.00	-.0000	11.29	1.58	11.29	1.58	11.29	1.58
2	11.21	9.37	.9889	-1.68	6.34	7.646	-1.528	2.740	-1.046	11.35	1.06	11.71	-1.53	3.96	3.96

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR XP AND YP

	MEAN X XP	S.D. X XP	R (X,XP)	MEAN Y YP	S.D. Y YP	R (Y,YP)	MEAN R (XP,YP)	S.D. R (XP,YP)	R (YP,X)	MEAN R (YP,X)	S.D. R (YP,X)	MEAN R (XP,YP)	S.D. R (XP,YP)	MEAN R (YP,XP)	S.D. R (YP,XP)
1	12	11.06	9.33	.7499	-1.67	6.33	.5268	.1491	.2656	-1.1415	11.43	5.73	.1545	-1.51	5.26
2	12	10.94	9.28	.6298	-1.70	6.32	.3587	.1449	.2339	-1.1735	11.47	6.85	.1551	-1.51	5.89
3	12	10.83	9.22	.5542	-1.74	6.28	.2069	.1371	.1232	-1.1563	11.51	7.50	.1564	-1.52	6.17
4	12	10.76	9.16	.4938	-1.68	6.25	.1522	.1336	.0753	-1.266	11.54	7.96	.1694	-1.55	6.26
5	12	10.73	9.11	.4448	-1.65	6.24	.1396	.1290	.0479	-1.075	11.58	8.26	.1740	-1.56	6.28

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR XP AND YP

	MEAN X XP	S.D. X XP	R (X,XP)	MEAN Y YP	S.D. Y YP	R (Y,YP)	MEAN R (XP,YP)	S.D. R (XP,YP)	R (YP,X)	MEAN R (YP,X)	S.D. R (YP,X)	MEAN R (XP,YP)	S.D. R (XP,YP)	MEAN R (YP,XP)	S.D. R (YP,XP)
1	19.01	10.36	.1781	-2.00	6.94	6.00	-.0000	0.00	-.0000	19.01	-2.00	19.01	-2.00	19.01	-2.00
2	19	10.36	.8954	-2.04	6.94	7.657	.1813	.2786	.0181	14.09	4.36	.1337	-1.96	9.35	9.35
3	19	10.32	.7649	-2.08	6.93	.5451	.1778	.2637	-.0601	14.20	6.73	.1767	-1.92	9.69	9.69
4	19	10.28	.6590	-2.11	6.92	.3611	.1724	.2015	-.1287	14.27	7.38	.1936	-1.92	6.40	6.40
5	19	10.22	.5869	-2.16	6.86	.2364	.1692	.1112	-.1249	14.32	8.07	.2001	-1.93	6.71	6.71
6	19	10.16	.5226	-2.10	6.83	.1721	.1582	.0729	-.1041	14.35	8.63	.2147	-1.96	6.81	6.81
7	19	10.11	.4711	-2.07	6.82	.1796	.1537	.0191	-.0659	14.38	9.00	.2206	-1.98	6.83	6.83

CHIARAVARIATE AND
STATION (12560)
- CAPE MELVILLE
MONTH OF RECORD - APRIL
PERIOD OF RECORD - 1/56 - 12/70
ALPHA ANGLE - 90.0

ALTITUDE (km) - 7

QUADRATIC NORMAL STATISTICS OF X,Y,XP,YP

DT	MEAN XP	S.D. XP	R (X,YP)	M.FAN Y ₀	S.D. Y ₀	R (Y,YP)	M.FAN (XP,YP)	R (XP,Y ₀)	M.FAN (YP,Y ₀)	R (YP,YP)	M.FAN XP	S.D. XP	M.FAN YP	S.D. YP
12	16.71	11.46	.8272	-2.39	7.67	.7702	.2027	.2651	.7656	*	16.90	6.88	.1223	2.31
24	16.50	11.47	.7775	-2.44	7.65	.5617	.1995	.2639	.0276	*	17.04	6.89	.1175	6.23
36	16.32	11.38	.6743	-2.47	7.64	.3788	.1934	.2734	.0784	*	17.13	6.07	.2141	2.27
48	16.16	11.31	.6021	-2.51	7.57	.2536	.1857	.1205	.0789	*	17.19	6.05	.2106	2.27
60	16.07	11.28	.5271	-2.47	7.55	.2237	.1789	.0692	.0732	*	17.21	6.97	.2482	7.31
72	16.01	11.19	.4823	-2.47	7.54	.2089	.1745	.0290	.0645	*	17.21	6.90	.2573	7.50

QUADRATIC NORMAL STATISTICS OF X,Y,XP,YP

DT	MEAN XP	S.D. XP	R (X,YP)	M.FAN Y ₀	S.D. Y ₀	R (Y,YP)	M.FAN (XP,YP)	R (XP,Y ₀)	M.FAN (YP,Y ₀)	R (YP,YP)	M.FAN XP	S.D. XP	M.FAN YP	S.D. YP
12	19.61	12.65	.8956	-2.79	8.59	.7757	.2746	.2891	.1060	*	19.81	7.47	.1294	2.71
24	19.27	12.61	.7819	-2.64	8.56	.5689	.2214	.2669	.0204	*	20.00	7.66	.1648	6.25
36	19.16	12.57	.6918	-2.57	8.54	.3910	.2156	.2767	.0354	*	20.10	8.77	.2268	7.93
48	18.99	12.57	.6059	-2.92	8.46	.2840	.2066	.1717	.0470	*	20.16	9.83	.2750	8.21
60	18.86	12.47	.5413	-2.87	8.45	.2432	.2019	.0655	.0375	*	20.16	10.44	.2767	7.71
72	18.91	12.34	.4859	-2.65	8.44	.2237	.1972	.0176	.0359	*	21.12	10.94	.2699	6.33

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND
STATION (120661) - CAPE HENNEPIN
MONTH OF RECORD - APRIL
PERIOD OF RECORD - 1/56 - 12/70
ALPHA ANGLE - 90.0

CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
X = V1AT 1
Y = V1AT 1
XP = V1AT 1
YP = V1AT 1

• • • • • ALTITUDE (MM) - 9

• • • • • QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, YP

DT	MEAN X	S.D. XP	R (X, XP)	MEAN Y	S.D. YP	R (Y, YP)	MEAN (XP, YP)	S.D. (XP, YP)	R (XP, YP)	MEAN (YR, YP)	S.D. (YR, YP)	R (YR, YP)	MEAN XP	S.D. XP	R (XP, YP)	MEAN YP	S.D. YP	R (XP, YP)
12	22.66	13.89	.8972	-3.27	9.71	.7783	.2456	.2935	.1622	22.89	6.04	.1091	-3.18	6.00	.2054	-2.054	-3.13	.784
24	22.38	13.88	.7886	-3.52	9.67	.5730	.2430	.2480	.0672	23.04	6.85	.2054	-3.13	7.84	.2433	-3.12	.81	.2755
36	22.15	13.80	.6845	-3.35	7.64	.4621	.378	.2078	.0147	23.19	7.92	.2433	-3.13	8.81	.2755	-3.13	9.22	.2755
48	21.95	13.75	.6070	-3.40	9.54	.3720	.2314	.1519	.0003	23.27	10.88	.2755	-3.13	9.36	.3011	-3.18	9.36	.3011
60	21.83	13.63	.5833	-3.58	9.55	.2529	.2248	.0612	.0003	23.29	11.56	.3011	-3.18	9.36	.3011	-3.22	9.36	.3011
72	21.74	13.54	.4663	-3.05	9.54	.2287	.0003	.0024	.0003	23.29	12.05	.3011	-3.18	9.36	.3011	-3.22	9.36	.3011

• • • • • ALTITUDE (MM) - 10

• • • • • QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, YP

DT	MEAN X	S.D. XP	R (X, XP)	MEAN Y	S.D. YP	R (Y, YP)	MEAN (XP, YP)	S.D. (XP, YP)	R (XP, YP)	MEAN (YR, YP)	S.D. (YR, YP)	R (YR, YP)	MEAN XP	S.D. XP	R (XP, YP)	MEAN YP	S.D. YP	R (XP, YP)
12	25.68	14.96	.9116	-3.77	10.86	.7031	.2654	.0767	.1761	25.96	6.92	.1675	-3.65	6.96	.2206	-3.61	6.74	.2206
24	25.39	14.91	.7422	-3.03	10.81	.5811	.2632	.0763	.1123	26.17	7.73	.2206	-3.61	7.73	.2615	-3.60	9.79	.2615
36	25.15	14.86	.6219	-3.87	10.76	.4164	.2590	.2049	.0701	26.30	11.68	.2615	-3.60	11.72	.2965	-3.61	10.26	.2965
48	24.93	14.79	.6161	-3.92	10.67	.3191	.2525	.1792	.0562	26.38	11.72	.2965	-3.61	12.04	.3233	-3.66	10.47	.3233
60	24.80	14.67	.5501	-3.91	10.59	.2589	.2457	.0657	.0562	26.41	12.04	.3233	-3.66	12.04	.3411	-3.72	10.53	.3411
72	24.69	14.56	.4949	-3.86	10.67	.2787	.0007	.0007	.0007	26.42	12.04	.3411	-3.72	10.53	.3411	-3.72	10.53	.3411

QUADRIVARIATE BMII CONDITIONAL MULTIVARIATE NORMAL STATISTICS OF X, Y, ZP, VP
 STATION 41286.81 - CAMP MURKIN
 MAXIMUM OF DIFFERENCE - APRIL
 PERCENT OF ERROR - 17.56 - 12.70
 ALPHAS AMGLT - 91.00
 VP = VARIOUS - 0.01

Altitude 1600 - 11

QUADRIVARIATE NORMAL STATISTICS OF X, Y, ZP, VP

CONDITIONAL MULTIVARIATE NORMAL STATISTICS
FOR VP AND VP

	MEDIAN	S.D.	P	MEDIAN	S.D.	P	MEDIAN	S.D.	P	MEDIAN	S.D.	P
	VP	VP	(X,Y)	VP	VP	(X,Y)	VP	VP	(X,Y)	VP	VP	(X,Y)
12	26.57	15.62	.2846	-4.12	11.67	.900						
16	29.56	15.62										
20	26.57	15.62										
24	26.57	15.62										
28	27.82	15.62										
32	27.82	15.62										
36	27.82	15.62										
40	27.82	15.62										
44	27.82	15.62										
48	27.82	15.62										
52	27.82	15.62										
56	27.82	15.62										
60	27.82	15.62										
64	27.82	15.62										
68	27.82	15.62										
72	27.82	15.62										

Altitude 1600 - 17

QUADRIVARIATE NORMAL STATISTICS OF X, Y, ZP, VP

CONDITIONAL MULTIVARIATE NORMAL STATISTICS
FOR VP AND VP

	MEDIAN	S.D.	P	MEDIAN	S.D.	P	MEDIAN	S.D.	P	MEDIAN	S.D.	P
	VP	VP	(X,Y)	VP	VP	(X,Y)	VP	VP	(X,Y)	VP	VP	(X,Y)
12	27.26	15.62	.2846	-4.12	11.67	.900						
16	27.26	15.62										
20	27.26	15.62										
24	27.26	15.62										
28	27.26	15.62										
32	27.26	15.62										
36	27.26	15.62										
40	27.26	15.62										
44	27.26	15.62										
48	27.26	15.62										
52	27.26	15.62										
56	27.26	15.62										
60	27.26	15.62										
64	27.26	15.62										
68	27.26	15.62										
72	27.26	15.62										

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL multivariate normal statistics of x , y , xp , yp
 STATION 112M61 - CAMP KENNEDY
 ELEVATION = 1011 ft
 PROVINCE OF NELSON - ARKANSAS
 PERIOD OF RECORD - 1/56 - 12/70
 ALTIMA SOURCE - 90.0
 ALTITUDE (ft) = 117

QUADRIVARIATE NORMAL STATISTICS OF x,y,xp,yp

DT	MEAN xp	S.D. xp	MEAN x, xp	S.D. xp	MEAN y	S.D. y	MEAN xp, yp	S.D. xp, yp	MEAN xp	S.D. xp	MEAN xp	S.D. xp
12	35.77	16.77	49.76	11.53	11.65	8.57	31.61	12.06	26.91	11.15	5.50	22.55
24	30.87	19.69	46.59	10.53	11.50	8.55	31.49	12.37	20.88	9.78	9.78	28.66
36	30.20	14.56	47.58	9.60	11.6	9.27	31.51	12.70	16.13	10.53	9.88	32.68
48	30.00	16.99	46.66	10.67	11.6	9.60	31.63	12.95	16.92	10.75	9.16	30.56
60	29.85	16.34	45.99	9.60	11.6	9.80	31.69	13.06	16.49	10.55	9.22	32.22
72	29.73	16.24	45.95	9.67	11.39	9.256	31.69	13.19	16.66	11.78	10.23	31.78

ALTITUDE (ft) = 117

QUADRIVARIATE NORMAL STATISTICS OF x,y,xp,yp

DT	MEAN xp	S.D. xp	MEAN x, xp	S.D. xp	MEAN y	S.D. y	MEAN xp, yp	S.D. xp, yp	MEAN xp	S.D. xp	MEAN xp	S.D. xp
12	29.76	13.58	43.56	9.07	10.49	9.00	30.74	10.76	29.76	9.17	7.11	22.05
24	29.29	13.24	46.69	8.21	10.45	8.27	31.07	12.78	30.17	8.91	7.51	28.91
36	29.03	13.16	47.55	8.35	10.91	8.72	31.33	12.94	30.51	8.76	8.86	33.58
48	28.84	13.09	46.75	8.42	10.37	8.91	32.62	12.68	31.73	9.39	9.02	33.02
60	28.71	12.96	46.10	8.53	10.58	9.14	31.21	12.87	30.87	10.55	9.51	33.95
72	28.59	12.86	45.94	8.63	10.56	9.26	31.62	12.23	31.49	10.49	9.88	33.50

ORIGINAL PAGE IS
OF POOR QUALITY

CHIEF PLATEAU AND
VALLEY CLOUDS
NUMBER OF CLOUDS
PERCENT OF CLOUDS -
AT EACH PLATEAU

411110.01 1971

CHIEF PLATEAU AND VALLEY CLOUDS

COMPUTATIONAL MEAN STATISTICS FOR 1971 AND VP
CONDITIONAL MEAN AND VARIANCE

MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.
26.074	11.48	26.069	-3.62	30.97	100	26.76	-3.67	26.76	101	26.76	101
01	16.90	2.00	18.801	1.6	17.701	1.6	17.701	1.6	17.701	1.6	
12	26.76	11.59	26.776	-2.71	30.82	0.675	31.010	0.786	26.78	0.754	
24	26.93	11.54	26.859	-3.80	30.83	0.703	31.021	0.779	27.18	0.746	
36	26.05	11.97	27.954	-3.88	30.69	0.7569	31.941	0.797	27.27	0.753	
48	25.92	11.59	26.971	-3.74	30.72	0.712	31.012	0.749	27.19	0.745	
60	25.80	11.79	26.166	-3.96	30.71	0.7166	31.003	0.737	27.31	0.714	
72	25.69	11.37	26.940	-3.94	30.721	0.7000	31.026	0.769	27.36	0.704	

411110.01 1971

CHIEF PLATEAU AND VALLEY CLOUDS

COMPUTATIONAL MEAN AND VARIANCE
CONDITIONAL MEAN AND VARIANCE

MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.
22.31	9.96	22.40	1.07	22.40	1.07	22.40	1.07	22.40	1.07	22.40	1.07
01	16.90	2.00	18.801	1.6	17.701	1.6	17.701	1.6	17.701	1.6	
12	22.11	9.45	22.21	0.6	22.21	0.6	22.21	0.6	22.21	0.6	
24	21.90	9.81	21.89	0.67	21.89	0.67	21.89	0.67	21.89	0.67	
36	21.71	9.71	21.70	0.68	21.70	0.68	21.70	0.68	21.70	0.68	
48	21.53	9.69	21.52	0.69	21.52	0.69	21.52	0.69	21.52	0.69	
60	21.50	9.69	21.50	0.70	21.50	0.70	21.50	0.70	21.50	0.70	
72	21.56	9.69	21.56	0.70	21.56	0.70	21.56	0.70	21.56	0.70	

QUADRATIC AND CONDITIONAL BIVARIATE NORMAL STATISTICS FOR X, Y, Z, VP
 STATION ELEVATION - CAMP MOUNTAIN
 NUMBER OF RECORDS - 4096
 PERCENT OF ERROR - 11.56 - 12.70
 ALPHA LEVEL - .050

ALTITUDE (ft)

- 17

CONDITIONAL BIVARIATE NORMAL STATISTICS OF X,Y,VP,VP

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR X AND YP

N	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	
12	16.86	0.32	-9128	-2.56	6.05	0.652	-2675	0.793	-2401	1.19	3.90	0.577	-2.05
24	16.69	0.26	0.398	-2.61	4.06	0.695	-3777	0.874	-6259	1.37	6.67	1.195	-2.35
36	16.52	0.23	0.751	-2.67	6.01	0.5209	-3668	0.475	-1653	1.02	5.67	1.21	-2.15
48	16.49	0.15	0.679	-2.71	5.29	0.3617	-3899	0.3606	-1526	1.06	6.17	1.251	-2.10
60	16.30	0.07	0.608	-2.73	5.99	0.2936	-3664	0.2795	-1439	1.09	6.62	1.287	-2.35
72	16.22	7.98	0.5513	-2.73	6.00	0.2216	-3620	0.2246	-1359	1.09	6.98	1.3145	-2.17

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR X AND VP

N	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	MEAN	S.D.	
12	16.86	0.32	-9128	-2.56	6.05	0.652	-2675	0.793	-2401	1.19	3.90	0.577	-2.05
24	16.69	0.26	0.398	-2.61	4.06	0.695	-3777	0.874	-6259	1.37	6.67	1.195	-2.35
36	16.52	0.23	0.751	-2.67	6.01	0.5209	-3668	0.475	-1653	1.02	5.67	1.21	-2.15
48	16.49	0.15	0.679	-2.71	5.29	0.3617	-3899	0.3606	-1526	1.06	6.17	1.251	-2.10
60	16.30	0.07	0.608	-2.73	5.99	0.2936	-3664	0.2795	-1439	1.09	6.62	1.287	-2.35
72	16.22	7.98	0.5513	-2.73	6.00	0.2216	-3620	0.2246	-1359	1.09	6.98	1.3145	-2.17

ORIGINAL PAGE
OF POOR QUALITY

QUADRAVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 1128681 - CAPE KENNEDY
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/56 - 12/70
 ALMA ANGLE - 90.00

ALTITUDE (MM) - 19

CUADRABIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

DT HR	MEAN		S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
	X	XP	(X,XP)	Y	(Y,YP)	XP	(XP,YP)	Y	(Y,P)	YP	(YP,X)	XP	(XP,X)	Y	(Y,P)	YP	(YP,YP)	XP	(XP,YP)
12	6.81	5.93	.98669	-1.60	3.78	.81559	.3695	.9502	.2761	7.03	2.75	- .0087	-1.55	2.08					
24	6.70	5.91	.81199	-1.62	3.74	.67115	.3831	.4609	-.2251	7.12	3.38	- .0319	-1.52	2.73					
36	6.60	5.85	.73607	-1.65	3.70	.44443	.3907	.4694	.2046	7.18	4.02	.0727	-1.49	3.12					
48	6.51	5.81	.66077	-1.67	3.67	.33221	.3953	.4197	.1854	7.22	4.47	.1531	-1.47	3.13					
60	6.44	5.76	.5906	-1.66	3.66	.2267	.3884	.3793	.1770	7.23	4.83	.1910	-1.46	3.04					
72	6.39	5.71	.5912	-1.66	3.66	.1711	.3821	.3338	.1561	7.24	5.03	.2313	-1.47	3.52					

ALTITUDE (MM) - 20

CUADRABIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

DT HR	MEAN		S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
	X	XP	(X,XP)	Y	(Y,YP)	XP	(XP,YP)	Y	(Y,P)	YP	(YP,X)	XP	(XP,X)	Y	(Y,P)	YP	(YP,YP)	XP	(XP,YP)
12	3.15	3.09	.3274	-1.26	3.01	.3274	-1.26	3.01	.3274	3.00	3.10	-1.26							
24	3.02	3.05	.9808	-1.27	3.01	.7053	.3341	.3274	.2598	3.17	2.90	.0036	-1.24	1.95					
36	2.93	2.95	.81163	-1.28	3.00	.5481	.3457	.4197	.2068	3.25	2.91	.0512	-1.22	2.33					
48	2.86	2.99	.7335	-1.30	2.96	.3750	.3509	.4151	.1955	3.26	3.44	.0664	-1.20	2.64					
60	2.78	2.95	.6527	-1.31	2.93	.2990	.3542	.3763	.1705	3.31	3.64	.1341	-1.19	2.74					
72	2.73	2.92	.5769	-1.31	2.92	.1632	.3462	.3745	.1677	3.32	3.16	.1631	-1.18	2.81					

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 9120681 - CAPE HENNEPIN
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/56 - 12/70
 ALMA ANGLE - 90.0

UNIVARIATE NORMAL STATISTICS OF X, Y, Z, P, VP

MEAN		S.D.		R		MEAN		S.D.		R		MEAN		S.D.		R		MEAN		S.D.		
X	Y	Xp	Yp	(X,Y)	Y	Xp	Yp	(X,Yp)	Yp	(Xp,Yp)	Y	Xp	Yp	(Xp,Y)	Y	Xp	Yp	(Xp,Yp)	Yp	(Xp,Y)	Y	
.36	.498	.7572	-1.02	.7572	-1.02	.255	.900	.255	.900	.255	.900	.36	.498	.36	.498	.36	.498	.36	.498	.36	.498	
01	12	.30	.66	.8795	-1.03	.754	.6653	.7599	.7833	.7140	.61	2.13	.692	-1.01	1.68	12	.30	.66	.8795	-1.03	.754	.6653
12	29	.23	.66	.6127	-1.03	.553	.5497	.6660	.2980	.11730	.47	2.60	.0774	-1.00	2.09	12	.30	.66	.8795	-1.03	.754	.6653
36	56	.16	.64	.7263	-1.04	.5302	.5322	.6689	.2823	.1624	.69	1.07	.0951	-1.99	2.17	36	.30	.67	.8814	-1.04	.754	.6653
48	60	.13	.63	.6331	-1.03	.298	.2666	.2698	.2756	.1375	.51	3.46	.1231	-1.99	2.90	48	.30	.67	.8814	-1.04	.754	.6653
60	72	.10	.62	.5497	-1.03	.247	.0781	.2644	.2498	.1278	.51	3.74	.1464	-1.98	2.97	60	.30	.67	.8814	-1.04	.754	.6653
72	72	.03	.61	.5976	-1.02	.247	.0589	.2614	.2792	.0955	.51	3.93	.1725	-1.98	2.98	72	.30	.67	.8814	-1.04	.754	.6653

卷之三

ORIGINAL PAGE IS
OF POOR QUALITY

BIVARIATE NORMAL STATISTICS OF NOV

STATION (117868) - CAMP HUMBLEY

X = Year To
Y = Year To

MONTH	PER. OF REC.	ALT. MM.	ALPHA DEG.	MEAN X	S.D. X	R X,Y	MEAN Y	S.D. Y
1/56	- 12/70	5	90.0	11.79	9.60	.1510	-1.58	6.36
1/56	- 12/70	6	90.0	16.01	10.78	.1761	-2.00	6.24
1/56	- 12/70	7	90.0	16.61	11.47	.1969	-7.15	7.67
1/56	- 12/70	8	90.0	19.73	12.17	.2273	-2.75	6.59
1/56	- 12/70	9	90.0	22.77	11.92	.2464	-3.22	6.70
1/56	- 12/70	10	90.0	25.83	15.70	.2652	-3.71	10.44
1/56	- 12/70	11	90.0	29.56	15.62	- .2846	-9.12	11.67
1/56	- 12/70	12	90.0	32.44	15.76	.1920	-6.35	11.92
1/56	- 12/70	13	90.0	30.97	16.77	.3193	-6.13	11.96
1/56	- 12/70	14	90.0	29.76	17.38	.3356	-6.07	17.60
1/56	- 12/70	15	90.0	26.76	11.64	.3490	-3.62	6.97
1/56	- 12/70	16	90.0	22.20	9.76	.3583	-3.07	7.45
1/56	- 12/70	17	90.0	17.03	8.42	.3626	-2.51	6.01
1/56	- 12/70	18	90.0	11.69	7.10	.3652	-2.00	6.75
1/56	- 12/70	19	90.0	6.93	6.00	.3697	-1.58	3.74
1/56	- 12/70	20	90.0	3.10	5.09	.3274	-1.26	3.01
1/56	- 12/70	21	90.0	0.36	4.49	.2572	-1.02	2.55
1/56	- 12/70	22	90.0	-1.35	0.22	.1958	-0.98	2.26

QUADRATIC AND CONDITIONAL BIVARIATE NORMAL	STATISTICS OF X, Y, Z, XP, YP
STATION (12668) - CAPE KENNEDY	X = UCAT 11
MONTH OF RECORD - APRIL	Y = UCAT 11
PERIOD OF RECORD - 1/56 - 12/70	Z = UCAT 11
ALPHA ANGLE - 90.0	XP = UCAT 11 + UCAT 11 YP = UCAT 11 - UCAT 11

ECUADOR VARIATE NOMINAL STATISTICS OF H.Y.-NP-Y.P

CONDITIONAL BIVARIATE NORMAL STATISTICS

54

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR NP AND VP

DT	MEAN X	S.D. X	MEAN Y	S.D. Y	MEAN (X,Y)		MEAN (Y,X)		MEAN (XP,YP)		MEAN (YP,XP)		MEAN (XP,YP)		MEAN (YP,XP)	
					MEAN XP	S.D. XP	MEAN YP	S.D. YP	MEAN (Y,YP)	S.D. (Y,YP)	MEAN (XP,YP)	S.D. (XP,YP)	MEAN (YP,XP)	S.D. (YP,XP)	MEAN (XP,YP)	S.D. (XP,YP)
12.01	10.38	-17.81	-2.00	6.14	9.00	11.01	-2.00	11.01	6.14	9.00	12.01	10.38	12.01	10.38	12.01	10.38
12	-0.9	4.74	-2.313	-0.5	4.75	-3.18	2.007	-2.191	-2.317	4	6.92	9.90	-18.03	5.24	6.20	5.24
24	-2.7	7.05	-3.666	-0.8	6.59	-6.72	2.679	-1.239	-2.716	4	6.38	6.54	-15.90	2.93	5.83	2.93
36	-4.2	8.55	-4.223	-1.2	7.83	-5.670	2.986	-0.262	-2.275	4	9.27	9.27	-16.66	1.58	5.54	1.58
48	-5.6	9.36	-4.681	-1.6	8.52	-6.228	3.002	-0.513	-2.458	4	7.27	7.10	-12.23	.58	5.34	.58
60	-6.5	10.03	-5.052	-1.1	8.76	-6.630	2.955	-1.104	-2.222	4	6.82	6.92	-11.26	-1.10	5.24	-1.10
72	-6.9	10.54	-5.110	-0.7	8.82	-6.481	2.889	-1.379	-2.075	4	6.67	6.76	-10.78	-0.74	5.24	-0.74

ORIGINAL PAGE 15
OF POOR QUALITY

QUADRATIC AND CONDITIONAL BI-VARIATE NORMAL STATISTICS OF X, Y, VP, VD
 STATION 1128681 - TYPE II
 NUMBER OF RECORDS 156 - APRIL
 PERIOD OF RECORDS - 1/56 - 12/70
 ALPHA FACTOR - 90.0

ALTITUDE (FTMS) - 7

QUADRATIC NORMAL STATISTICS OF X, Y, VP, VD

MEAN	S.D.	μ_x^2	μ_y^2	μ_{xy}	μ_{vp}	μ_{vd}	$\mu_{vp, vd}$	$\mu_{vp, xv}$	$\mu_{vd, xv}$	MEAN	S.D.	μ_x^2	μ_y^2	μ_{xy}	μ_{vp}	μ_{vd}	$\mu_{vp, vd}$	$\mu_{vp, xv}$	$\mu_{vd, xv}$
10.481	11.67	.1999	-2.35	7.67	900	11.681	-2.35	11.681	-2.35	10.73	11.67	.1999	-2.35	11.681	-2.35	11.681	-2.35	11.681	-2.35
12	-10	5.20	-2286	-0.04	5.20	-1582	1767	-1831	-1680	10.18	10.01	-2081	5.21	6.97	6.95	2.95	2.95	6.95	6.95
22	-31	7.66	-3595	-0.08	7.17	-6764	-2614	-0.45	-2432	7.80	10.5	-1955	1.64	1.64	1.64	1.64	1.64	1.64	1.64
36	-50	9.22	-6119	-1.11	8.53	-5558	-3051	-0.025	-2549	9.31	10.5	-1660	1.52	1.52	1.52	1.52	1.52	1.52	1.52
68	-66	10.16	-6508	-1.16	9.25	-6188	-3180	-0.026	-2588	8.70	10.11	-1685	1.52	1.52	1.52	1.52	1.52	1.52	1.52
90	-75	10.93	-6571	-1.11	9.71	-6509	-3157	-0.027	-2620	8.24	10.11	-162	1.52	1.52	1.52	1.52	1.52	1.52	1.52
72	-80	11.75	-6525	-1.06	11.53	-6373	-3208	-0.028	-2110	7.96	9.71	-1265	1.52	1.52	1.52	1.52	1.52	1.52	1.52

CONDITIONAL BI-VARIATE NORMAL STATISTICS

MEAN	S.D.	μ_x^2	μ_y^2	μ_{xy}	μ_{vp}	μ_{vd}	$\mu_{vp, vd}$	$\mu_{vp, xv}$	$\mu_{vd, xv}$	MEAN	S.D.	μ_x^2	μ_y^2	μ_{xy}	μ_{vp}	μ_{vd}	$\mu_{vp, vd}$	$\mu_{vp, xv}$	$\mu_{vd, xv}$
19.73	12.67	.2223	-2.75	8.59	900	19.73	-2.75	19.73	-2.75	19.73	11.67	.1999	-2.35	19.73	-2.75	19.73	-2.75	19.73	-2.75
12	-12	5.76	-2352	-0.04	5.76	-3363	1704	-1761	-1713	11.52	12.21	-2127	6.93	7.90	7.90	7.90	7.90	7.90	7.90
24	-35	8.37	-452	-0.08	7.96	-4079	-1212	-0.12	-3216	11.7	11.7	-1982	1.52	1.52	1.52	1.52	1.52	1.52	1.52
36	-56	10.08	-5079	-1.12	9.45	-5027	-3259	-0.07	-4067	10.7	11.7	-1781	1.52	1.52	1.52	1.52	1.52	1.52	1.52
68	-76	11.17	-5562	-1.17	10.20	-5020	-3259	-0.07	-4067	10.7	11.7	-1781	1.52	1.52	1.52	1.52	1.52	1.52	1.52
90	-84	12.02	-6950	-1.13	10.48	-6667	-2126	-0.12	-5367	9.53	10.99	-1635	1.52	1.52	1.52	1.52	1.52	1.52	1.52
72	-91	12.68	-5263	-1.10	10.61	-6515	-2085	-0.20	-6209	9.8	11.6	-1629	1.52	1.52	1.52	1.52	1.52	1.52	1.52

CONDITIONAL BI-VARIATE NORMAL STATISTICS
 19.73 VP AND VP

CONDITIONAL BI-VARIATE NORMAL STATISTICS OF X, Y, VP, VD

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, VP
 STATION (12868) - CAPE KENNEDY
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/56 - 12/70
 ALPHA ANGLE - 90.0

ALTITUDE (KMH) - 9

QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, VP

CONDITIONAL BIVARIATE NORMAL STATISTICS

MEAN X	S.D. X	R (X,Y)	MEAN			S.D. Y	MEAN			S.D. XP	MEAN			S.D. VP
			X	Y	XP		X	Y	XP		Y	XP, YP	XP, VP	
22.77	13.92	.2466	-3.22	-	9.70	9.00	-	-	-	22.77	-	-3.22	-	
DT	MEAN XP	S.D. XP	MEAN Y	S.D. Y	MEAN (X,YP)	R (Y,VP)	MEAN (XP,YP)	R (XP,Y)	MEAN (XP,VP)	R (XP,VP)	MEAN XP	S.D. XP	MEAN VP	S.D. VP
HR	MEAN XP	S.D. XP	MEAN Y	S.D. Y	MEAN (X,YP)	R (Y,VP)	MEAN (XP,YP)	R (XP,Y)	MEAN (XP,VP)	R (XP,VP)	MEAN XP	S.D. XP	MEAN VP	S.D. VP
12	-1.13	6.30	-2313	.05	6.46	-.3333	-1807	.1071	-1532	.1345	12.92	13.45	4.58	9.00
24	-4.40	9.11	-3360	.10	8.95	-4.646	-2514	.0336	-1923	.1502	12.46	13.02	2.69	8.45
36	-6.62	11.01	-4066	.13	10.57	-5.5509	-2993	-.0486	-2108	.1201	12.65	12.65	2.29	8.01
48	-8.82	12.26	-4560	.18	11.37	-5.5995	-3287	-.1300	-2087	.1138	12.36	12.36	2.09	7.73
60	-9.94	13.17	-4949	.16	11.76	-6.6191	-1951	-.2013	-2013	.1076	12.09	12.09	1.22	7.61
72	-11.03	13.89	-5262	.12	11.95	-6.6292	-2383	-.2003	-2003	.1033	11.84	11.84	1.22	7.56

ALTITUDE (KMH) - 10

QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, VP

CONDITIONAL BIVARIATE NORMAL STATISTICS

MEAN X	S.D. X	R (X,Y)	MEAN			S.D. Y	MEAN			S.D. XP	MEAN			S.D. VP
			X	Y	XP		X	Y	XP		Y	XP, YP	XP, VP	
25.83	15.00	.2852	-	-3.71	-	10.84	-	9.00	-	25.83	-	-3.71	-	
DT	MEAN XP	S.D. XP	MEAN (X,YP)	R (Y,VP)	MEAN (XP,YP)	R (XP,Y)	MEAN (XP,VP)	R (XP,VP)	MEAN XP	S.D. XP	MEAN VP	S.D. VP	MEAN VP	S.D. VP
HR	MEAN XP	S.D. XP	MEAN (X,YP)	R (Y,VP)	MEAN (XP,YP)	R (XP,Y)	MEAN (XP,VP)	R (XP,VP)	MEAN XP	S.D. XP	MEAN VP	S.D. VP	MEAN VP	S.D. VP
12	-1.15	6.65	-2280	-.06	7.14	-3265	.1921	.0691	-1316	.1418	14.18	14.55	2.75	4.06
24	-4.44	9.64	-3316	.12	9.91	-4.595	.2545	-.0011	-1675	.1568	14.09	14.09	2.71	4.54
36	-6.68	11.72	-4029	.16	11.67	-5.644	.3012	-.0797	-1872	.1323	13.69	13.69	2.56	9.04
48	-8.90	13.09	-4526	.21	12.55	-5.5921	.3343	-.1580	-1900	.1259	13.36	13.36	2.37	8.72
60	-10.04	14.08	-4925	.20	13.10	-6.6160	.3606	-.2222	-1893	.1192	13.06	13.06	2.16	8.54
72	-11.14	14.86	-5244	.17	13.36	-6.6286	.3777	-.2670	-1897	.1142	12.77	12.77	1.97	8.42

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
STATION (12868) - CAPE KENNEDY
MONTH OF RECORD - APRIL
PERIOD OF RECORD - 1/56 - 12/70
ALPHA ANGLE - 90.0

ALTITUDE (KM) - 11

QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, YP

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR XY AND YP

N	MEAN			S.D.			MEAN			S.D.			MEAN			S.D.		
	X	XP	YP	(X, Y)	MEAN	S.D.	XP	YP	(X, YP)	MEAN	S.D.	XP	YP	(X, Y)	MEAN	S.D.	XP	YP
28.56	15.62	-2846	-6.12	-11.67	900					15.19	15.20	-12939	3.26		11.01			
12	-17	6.62	-2201	-0.8	7.49	-3159	-2039	.0351	-1115	15.19	15.20	-12939	3.26					
24	-4.8	9.72	-3229	-1.5	10.47	-4490	-2643	-0.339	-1669	14.69	14.75	-2912	1.15	10.38				
36	-7.5	11.92	-3952	-2.0	12.36	-5366	-3106	-1.094	-1686	14.24	14.33	-2791	-2.27	9.84				
48	-9.6	13.35	-4450	-2.5	13.35	-5832	-3463	-1.855	-1757	13.59	13.99	-2603	-1.64	9.48				
60	-1.11	15.62	-4867	-2.5	16.04	-6111	-3727	-2.660	-1800	12.89	13.65	-2397	-2.69	9.24				
72	-1.23	15.26	-5197	-2.2	14.39	-6269	-3863	-2.891	-1807	12.33	13.34	-2206	-3.46	9.08				

ALTITUDE (KM) - 12

QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, YP

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR XY AND YP

N	MEAN			S.D.			MEAN			S.D.			MEAN			S.D.		
	X	XP	YP	(X, Y)	MEAN	S.D.	XP	YP	(Y, YP)	MEAN	S.D.	XP	YP	(X, Y)	MEAN	S.D.	XP	YP
30.44	15.56	.3020	-6.35	-11.92	900					15.77	15.19	.3097	2.44	11.34				
12	-19	6.23	-2103	-0.9	7.28	-2985	-2209	.0085	-0.978	15.77	15.19	.3097	2.44					
24	-50	9.28	-3121	-1.8	10.35	-4323	-2816	-0.0593	-1343	15.31	14.76	.3077	.51	10.72				
36	-76	11.50	-3856	-2.6	12.34	-5205	-3272	-1.5227	-1583	14.85	14.93	.2972	-86	10.17				
48	-98	12.94	-4558	-3.0	13.44	-5721	-3636	-2.071	-1686	14.19	14.00	.2791	-2.26	9.78				
60	-114	14.05	-4789	-3.1	14.23	-6036	-3852	-2.6269	-1741	13.67	13.66	.2606	-3.31	9.50				
72	-126	14.92	-5136	-2.8	14.65	-6229	-3941	-3.025	-1755	12.92	13.34	.2433	-4.09	9.30				

QUADRIVARIATE AND CONDITIONAL DIVARIATE NORMAL STATISTICS OF X, Y, XP, VP
 STATION (192B65) - CAPE KENNEDY
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/56 - 12/70
 ALPHA ANGLE - 90.0
 N = UNIT 1
 Y = UNIT 1
 A = UNIT 1
 XP = UNIT 1 + DP1 = UNIT 1
 VP = UNIT 1 + DP1 = UNIT 1

ALTITUDE (KMH) - 15

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,VP

	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
DP	MEAN	S.D.	(X,XP)	MEAN	S.D.	(Y,YP)	MEAN	S.D.	(XP,VP)	MEAN	S.D.	(X,YP)	MEAN	S.D.	(Y,VP)
NA	30.97	16.77	.3193	-6.53	11.46	.900									
NA	30.97	16.77	(X,XP)	MEAN	S.D.	(Y,YP)	MEAN	S.D.	(XP,VP)	MEAN	S.D.	(X,YP)	MEAN	S.D.	(Y,VP)
NA	12	-20	5.61	-2024	-10	6.56	-2768	2344	-0000	-0359	15.71	-11.44	-3259	2.17	10.99
NA	24	-50	8.45	-3019	-20	9.54	-4119	2993	-0680	15.61	-15.61	-3253	-4.40	10.63	
NA	36	-76	10.58	-3773	-27	11.56	-5041	3490	-1428	15.67	-15.67	-3152	-1.01	9.89	
NA	48	-97	11.95	-6278	-34	12.72	-5598	3824	-2162	16.22	13.35	-2983	-2.40	9.50	
NA	60	-112	13.05	-2223	-35	13.55	-5950	3963	-2696	13.51	13.01	-2853	-3.68	9.20	
NA	72	-124	13.92	-3088	-33	14.03	-6177	4017	-3059	12.97	12.70	-2681	-4.23	8.99	

ALTITUDE (KMH) - 16

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,VP

	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
DP	MEAN	S.D.	(X,XP)	MEAN	S.D.	(Y,YP)	MEAN	S.D.	(XP,VP)	MEAN	S.D.	(X,YP)	MEAN	S.D.	(Y,VP)
NA	29.76	13.38	.3356	-6.07	10.40	.900									
NA	29.76	13.38	(X,XP)	MEAN	S.D.	(Y,YP)	MEAN	S.D.	(XP,VP)	MEAN	S.D.	(X,YP)	MEAN	S.D.	(Y,VP)
NA	12	-20	4.94	-2008	-10	5.57	-2562	2226	-0155	-1013	15.10	-13.09	-3434	2.91	10.02
NA	24	-48	7.42	-2956	-20	8.28	-3918	3064	-0507	-1403	14.89	-12.77	-3429	1.19	9.53
NA	36	-73	9.16	-5728	-27	10.19	-4804	3583	-1317	-1640	14.23	-12.61	-3156	-6.43	9.06
NA	48	-92	10.60	-1232	-35	11.47	-5487	3962	-2058	-1771	13.61	-12.12	-3207	-1.81	8.69
NA	60	-106	11.63	-1690	-36	12.19	-5874	4027	-2582	-1780	12.90	-11.62	-3091	-2.90	8.41
NA	72	-117	12.46	-3071	-35	12.69	-6129	4074	-2961	-1803	12.37	-11.53	-2959	-7.72	8.20

ORIGINAL PAGE IS
OF POOR QUALITY

UNIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION (1266) - CAPE KENNEDY
 MONTH OF RECORD - APRIL
 PERIOD OF RECORDS - 1956 - 1970
 ALPHA ANGLE - 90.0

UNIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 ALITUDE (km) - 15

CONDITIONAL BIVARIATE NORMAL STATISTICS
 FOR XP AND YP

DI	MEAN	S.D.	X	MEAN	S.D.	Y	MEAN	S.D.	XP	MEAN	S.D.	YP	MEAN	S.D.
HR	MEAN	XP	(X,XP)	MEAN	Y	(Y,Y)	MEAN	XP	(XP,XP)	MEAN	Y	(Y,YP)	MEAN	XP
HR	MEAN	XP	(X,XP)	MEAN	Y	(Y,Y)	MEAN	XP	(XP,XP)	MEAN	Y	(Y,YP)	MEAN	XP
12	-2.20	6.36	-2070	-0.9	6.60	-2429	-1918	0.583	-1182	13.62	11.39	.5621	6.25	8.65
24	-6.45	6.36	-2951	-18	6.95	-3789	2657	-0.025	-1550	15.56	11.13	.3647	2.62	6.24
36	-0.67	8.03	-3725	-25	8.64	-5786	3489	-0.931	-1746	12.85	10.83	.3599	7.53	7.84
48	-2.24	9.13	-6226	-32	9.73	-5427	3874	-1709	-1859	12.29	10.58	.3479	7.52	7.52
60	-0.96	10.06	-6696	-34	10.69	-5800	3960	-2278	-1826	11.62	10.31	.3389	7.28	7.28
72	-1.07	10.80	-5087	-36	10.97	-6116	4030	-2696	-1966	11.11	10.06	.3275	7.09	7.09

ALITUDE (km) - 16

CONDITIONAL BIVARIATE NORMAL STATISTICS
 FOR XP AND YP

DI	MEAN	S.D.	X	MEAN	S.D.	Y	MEAN	S.D.	XP	MEAN	S.D.	YP	MEAN	S.D.
HR	MEAN	XP	(X,XP)	MEAN	Y	(Y,Y)	MEAN	XP	(XP,XP)	MEAN	Y	(Y,YP)	MEAN	XP
HR	MEAN	XP	(X,XP)	MEAN	Y	(Y,Y)	MEAN	XP	(XP,XP)	MEAN	Y	(Y,YP)	MEAN	XP
12	-1.19	5.67	-2200	-0.7	3.79	-2414	1332	1.131	-1304	11.31	9.66	.3814	4.86	7.14
24	-4.2	5.65	-3016	-14	5.76	-3779	2510	0.662	-1676	11.31	9.45	.3903	3.54	6.79
36	-6.40	6.84	-3710	-21	7.18	-6788	3067	-0.297	-1822	10.78	9.20	.3893	1.69	6.47
48	-7.75	7.77	-4265	-27	8.10	-5463	3531	-1129	-1706	10.33	9.00	.3807	-4.62	6.22
60	-6.85	8.57	-759	-29	8.75	-5750	3680	-1766	-1887	9.77	8.77	.3735	-7.72	6.02
72	-6.95	9.19	-5125	-29	9.18	-6157	3762	-2236	-1202	9.33	8.56	.3437	-1.65	5.87

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, VP, VP
 STATION (112868) - CAPE KENNEDY
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/156 - 12/70
 ALPHA ANGLE - 90.0

ALTITUDE (KFM) - 17

QUADRIVARIATE NORMAL STATISTICS OF X, Y, VP, VP

	MEAN	S.D. X	S.D. Y	MEAN	S.D. VP	MEAN	S.D. (X, VP)	MEAN	S.D. (Y, VP)	MEAN	S.D. (VP, X)	MEAN	S.D. (VP, Y)	MEAN	S.D. (VP, VP)
NP	MEAN VP	S.D. X, VP	S.D. Y, VP	MEAN VP	S.D. VP	MEAN VP	S.D. (X, VP)	MEAN VP	S.D. (Y, VP)	MEAN VP	S.D. (VP, X)	MEAN VP	S.D. (VP, Y)	MEAN VP	S.D. (VP, VP)
17.03	17.03	8.42	.3626	-2.51	6.01	9.00									
	17.03	8.42	.3626	-2.51	6.01	9.00									
12	-17	3.50	-2.353	-0.05	3.13	-2.691	.0784	-16.06	-15.52	6.64	-8.10	-3980	4.09	5.72	
24	-34	4.72	-3.126	-0.10	4.75	-3.879	-1.567	-13.68	-17.18	8.50	-7.93	-4175	3.25	5.61	
36	-51	5.85	-3.850	-0.16	5.88	-4.692	-2.532	-0.660	-18.03	8.21	-7.73	-4226	1.81	5.15	
48	-64	6.64	-4.943	-0.20	6.62	-5.554	-2.877	-0.617	-18.50	7.91	-7.56	-4177	.79	4.95	
60	-73	7.30	-5.606	-0.22	7.13	-5.960	-3.114	-0.1092	-18.46	7.54	-7.38	-4118	.07	4.80	
72	-81	7.78	-5.167	-0.23	7.49	-6.248	-3.303	-0.1620	-18.60	7.20	-7.20	-4033	.65	4.66	

ALTITUDE (KFM) - 18

QUADRIVARIATE NORMAL STATISTICS OF X, Y, VP, VP

	MEAN	S.D. X	S.D. Y	MEAN	S.D. VP	MEAN	S.D. (X, VP)	MEAN	S.D. (Y, VP)	MEAN	S.D. (VP, X)	MEAN	S.D. (VP, Y)	MEAN	S.D. (VP, VP)
NP	MEAN VP	S.D. X, VP	S.D. Y, VP	MEAN VP	S.D. VP	MEAN VP	S.D. (X, VP)	MEAN VP	S.D. (Y, VP)	MEAN VP	S.D. (VP, X)	MEAN VP	S.D. (VP, Y)	MEAN VP	S.D. (VP, VP)
11.69	11.69	7.10	.3652	-2.00	6.75	9.00									
	11.69	7.10	.3652	-2.00	6.75	9.00									
12	-16	3.17	-2.496	-0.03	2.60	-2.654	.017	-18.42	-15.82	6.03	-6.80	-4101	2.43	4.49	
24	-28	4.13	-3.224	-0.06	3.89	-4.051	.0978	-18.13	-16.90	5.82	-6.65	-4404	4.21	4.21	
36	-41	5.06	-3.920	-0.11	4.78	-5.071	-1.562	-10.86	-16.99	5.62	-6.49	-4550	1.20	5.00	
48	-53	5.70	-4.417	-0.14	5.33	-5.696	-2.163	-0.192	-17.20	5.43	-6.35	-4532	.52	5.84	
60	-61	6.24	-4.856	-0.16	5.72	-6.107	-2.988	-0.1419	-17.19	5.22	-6.20	-4517	.01	3.73	
72	-68	6.59	-5.190	-0.16	5.99	-6.373	-2.654	-0.0966	-17.53	5.01	-6.07	-4433	-.35	3.63	

ORIGINAL PAGE IS
OF POOR QUALITY

UNIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION (12868) - CAPE KENNEDY
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/56 - 12/70
 ALPHA ANGLE - 90.0

ALTITUDE (km) - 19

UNIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

DT	MEAN	S.D.	\bar{x}	\bar{y}	MEAN	S.D.	\bar{x}	\bar{y}	MEAN	S.D.	\bar{x}	\bar{y}	MEAN	S.D.	\bar{x}	\bar{y}
12	-1.1	2.86	-2.588	-0.02	2.27	3.006	-0.0104	-1.790	-1.552	3.64	5.74	-4.097	.88	3.50		
24	-1.25	3.57	-3.256	-0.04	3.21	-2.4292	-0.0772	-1.882	-1.580	3.52	5.61	-4.426	.89	3.27		
36	-1.32	4.31	-3.928	-0.07	3.92	-3.5542	-0.1030	-1.553	-1.509	3.33	5.47	-4.692	.43	3.08		
48	-1.24	4.86	-4.438	-0.08	4.24	-3.5879	-0.1647	-0.053	-1.558	2.21	5.35	-6.687	.07	2.97		
60	-1.69	5.32	-4.870	-0.10	4.60	-6.5221	-0.1722	-0.063	-1.523	1.10	5.22	-6.770	-.19	2.86		
72	-1.54	5.61	-5.189	-0.10	4.76	-6.5229	.2053	-.0467	-1.614	2.98	5.11	-6.670	-.35	2.81		

ALTITUDE (km) - 20

UNIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

DT	MEAN	S.D.	\bar{x}	\bar{y}	MEAN	S.D.	\bar{x}	\bar{y}	MEAN	S.D.	\bar{x}	\bar{y}	MEAN	S.D.	\bar{x}	\bar{y}
12	-1.08	2.68	-2.596	-0.01	2.15	-3.581	-0.036	-1.375	-0.951	1.68	4.90	-3.721	-.08	2.78		
24	-1.17	3.07	-3.224	-0.02	2.73	-4.6575	-0.061	-1.643	-1.341	1.65	6.79	-3.954	-.01	2.62		
36	-1.24	3.68	-3.892	-0.04	3.34	-5.6687	-0.043	-1.097	-1.225	1.50	4.67	-4.295	-.18	2.43		
48	-1.31	4.19	-4.438	-0.06	3.52	-6.6051	-0.134	-0.494	-1.378	1.44	4.55	-4.289	-.28	2.36		
60	-1.37	4.61	-4.885	-0.05	3.86	-6.6601	-0.1271	0.0171	-1.291	1.37	4.53	-4.688	-.38	2.26		
72	-1.41	4.88	-5.221	-.05	3.91	-6.726	.1625	-.0234	-1.466	1.33	4.33	-4.363	-.42	2.21		

QUADRATIC AND CUBIC NORMAL STATISTICS OF R, V, RP, VP
 STATION (12868)
 MONTH OF RECORD - APRIL
 PERIOD OF RECORD - 1/56 - 1/270
 ALPHA ANGLE - 90.0

ALTITUDE (ftm) - 127

QUADRATIC NORMAL STATISTICS OF R, V, RP, VP

COMBINED NORMAL STATISTICAL STATISTICS

	MEAN	S.D.	R	V	RP	VP	MEAN	S.D.	R	V	RP	VP	MEAN	S.D.	R	V	RP	VP
R	.36	.478	.2572	-1.02	2.55	.900	.36	.36	.36	.36	.36	.36	.36	.36	.36	.36	.36	.36
V																		
RP																		
VP																		

ORIGINAL PAGE
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL MULTIVARIATE NORMAL STATISTICS OF X, Y, XP, VP
STATION 195214 - WINDSHIELD
MOMN OF RECORD - JANUARY
MOMN OF RECORD - 2/65 - 11/70
ALPHA SOURCE - 90.0

Altitude (ftm) - 6

QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, VP

ui	mean \bar{x}	s.d. s_x	n (x,y)	mean \bar{y}	s.d. s_y	n	mean \bar{xp}	s.d. s_{xp}	n (xp,y)	mean \bar{vp}	s.d. s_{vp}	n (vp,x)	mean \bar{xp}	s.d. s_{xp}	n (xp,yp)	mean \bar{vp}	s.d. s_{vp}	n (vp,xp)	
12	10.54	.9373	-3.57	10.56	.7697	-2.56	.3119	.0975	•	10.67	.668	-2.02	-1.67	.687	•	10.54	.691	-1.71	4.07
13	10.69	.6472	-3.52	10.69	.6617	-2.59	.3177	.0231	•	10.65	.617	-1.65	-1.71	.607	•	10.75	.637	-1.71	9.86
14	10.57	.5165	-3.53	10.52	.6126	-2.47	.2832	.0024	•	10.62	.62	-0.02	-1.70	.675	•	10.77	.637	-1.71	10.01
15	10.31	.9229	-3.96	10.45	.2270	-2.21	.2921	.0040	•	10.67	.557	-1.877	-1.877	.677	•	10.74	.693	-1.64	10.03
16	10.82	.3523	-3.37	10.41	.1987	-2.57	.3096	.0104	•	10.74	.74	-1.014	-1.014	.657	•	10.75	.74	-1.014	10.14
17	10.69	.2689	-3.26	10.62	.1757	-2.99	.2807	.0508	•	10.77	.75	-2.087	-2.087	.665	•	10.74	.75	-2.087	10.14

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 93249 - VANDENBERG
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 2/65 - 11/79
 ALPHA ANGLE - 90.0

Altitude (km) - 7

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR XP AND YP

DT HR	MEAN		S.D.		R		MEAN		S.D.		R		MEAN		S.D.	
	X	XP	(X,XP)	Y	(Y,Y)	R _{XY}	R _{YP}	(X,Y)	R _{XP}	R _{YP}	(XP,Y)	R _{XY}	R _{XP}	(XP,YP)	R _{XP}	R _{YP}
12	14.97	15.65	.8310	-0.13	12.01	.7167	.2740	.3138	.1302	14.81	7.49	.2867	-0.25	9.71	9.71	
24	15.10	15.69	.6951	-0.06	12.94	.9488	.2651	.2885	.1069	14.75	10.35	.2332	-0.29	11.57	11.57	
36	15.16	15.94	.5176	-0.05	12.95	.2698	.2555	.2499	.0171	14.75	11.66	.2399	-0.28	12.58	12.58	
48	15.13	15.35	.4208	-0.96	12.61	.1869	.2633	.2591	.0218	14.80	12.95	.2289	-0.28	12.50	12.50	
60	15.01	13.97	.3860	-0.87	12.62	.1696	.2658	.2842	.0072	14.87	12.83	.2226	-0.26	12.50	12.50	
72	14.86	15.67	.2665	-0.79	12.86	.1557	.2605	.2594	.0213	14.90	13.75	.2389	-0.23	12.60	12.60	

Altitude (km) - 8

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

DT HR	MEAN		S.D.		R		MEAN		S.D.		R		MEAN		S.D.	
	X	XP	(X,XP)	Y	(Y,Y)	R _{XY}	R _{YP}	(X,Y)	R _{XP}	R _{YP}	(XP,Y)	R _{XY}	R _{XP}	(XP,YP)	R _{XP}	R _{YP}
12	16.96	15.26	.2852	-0.55	14.23	.620	-0.55	14.96	.055	15.96	-0.55	14.96	.055	15.96	-0.55	15.96
24	17.05	15.10	.9318	-0.98	16.15	.7083	.2711	.2932	.1421	16.89	9.38	.2558	-0.61	9.93	9.93	
36	17.21	15.60	.6405	-0.41	14.95	.4337	.2606	.2460	.0721	16.82	11.50	.2438	-0.68	12.62	12.62	
48	17.25	16.93	.5176	-0.40	14.09	.2558	.2514	.2101	.0211	16.82	12.91	.2476	-0.63	13.54	13.54	
60	17.29	16.90	.4230	-0.29	14.01	.1697	.2576	.2329	.0135	16.87	13.65	.2352	-0.63	13.74	13.74	
72	17.13	14.98	.3560	-0.21	11.95	.1526	.2596	.2160	.0156	16.93	10.17	.2251	-0.62	13.66	13.66	

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL PIVARIATE NORMAL STATISTICS FOR X, Y, XP, YP
 STATION 193210 - VAILDBERG
 MONTHS RECORDED - JANUARY
 PERIOD OF RECORD - 2/25 - 11/78
 ALTA ANGLE - 90.0

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP
 ALTITUDE (ft) - 15
 QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP
 ALTITUDE (ft) - 15

UT HR	MEAN XP	S.D. XP	MEAN Y	S.D. Y	NORMAL STATISTICS OF X, Y, XP, YP				NORMAL STATISTICS OF X, Y, XP, YP			
					MEAN YP	S.D. YP	MEAN (XP, YP)	S.D. (XP, YP)	MEAN (XP, Y)	S.D. (XP, Y)	MEAN YP	S.D. YP
12.08	16.68	.2741	-9.78	15.08	6.20	-	-	-	-	-	10.06	.6666
12	19.16	16.39	-8.551	-4.82	7.120	.2642	2.697	.1566	19.02	.900	25.49	.61
24	19.32	16.27	-6.520	-4.76	6.096	.6304	.2536	.2417	12.15	.2815	24.93	.66
36	19.38	16.19	-5.124	-6.74	16.96	.2498	.2498	.2102	15.87	.2472	16.92	.62
48	19.79	16.18	-6.125	-6.64	16.89	.1574	.2490	.2113	16.97	.2341	16.65	.66
60	19.53	16.27	-3.665	-4.55	16.82	.1369	.2515	.2467	16.94	.1522	22.13	.96
72	19.16	16.28	-2.900	-4.87	16.87	.1171	.2470	.2285	15.75	.2373	23.93	.55

UT HR	MEAN XP	S.D. XP	MEAN Y	S.D. Y	NORMAL STATISTICS OF X, Y, XP, YP				NORMAL STATISTICS OF X, Y, XP, YP			
					MEAN YP	S.D. YP	MEAN (XP, YP)	S.D. (XP, YP)	MEAN (XP, Y)	S.D. (XP, Y)	MEAN YP	S.D. YP
21.08	17.21	.2673	-5.11	15.47	7.211	.2633	2.713	.2191	21.03	.1114	21.03	.16
21	21.19	17.15	-8.453	-5.15	17.42	.2748	.2569	.2907	21.03	.1114	21.03	.16
24	21.22	17.04	-6.621	-7.07	15.37	.4336	.2473	.2191	21.03	.1114	21.03	.17
35	21.17	16.96	-5.374	-6.78	15.37	.2465	.2570	.1259	21.03	.1114	21.03	.17
48	21.80	16.97	-4.507	-4.69	15.20	.1884	.2432	.1221	21.03	.1114	22.00	.10
60	21.33	17.07	-3.660	-4.79	15.22	.1279	.2447	.2278	21.03	.1114	21.03	.16
72	21.22	17.07	-3.66	-4.71	15.76	.0799	.2410	.2183	21.03	.1114	21.03	.16

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 193284 - VANDENBERG
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 2/65 - 3/74
 ALPHA ANGLE - 90.0

ALTITUDE (KMH) - 11

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
 FOR XP AND YP
 GIVEN X
 Y

MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
X	XP	XP	Y	YP	YP	XP	YP	XP	YP	XP	YP	XP	YP	YP
22.62	17.21	.2640	-5.13	15.25	6.20	-	-	-	-	22.62	-5.13	-	-	-
12	22.66	17.16	.9605	-5.09	15.20	.7426	.2537	.1921	.2258	.876	.2317	-5.16	10.18	
24	22.79	17.07	.6493	-5.06	15.17	.4409	.2458	.2762	.1096	.2250	.12.31	-5.18	13.60	
36	22.89	17.00	.5651	-5.04	15.16	.2493	.2361	.1924	.0198	.22.47	14.05	-5.19	14.64	
48	22.99	17.01	.4777	-4.94	15.10	.1415	.2419	.1791	.4705	.72.48	.14.97	-5.20	14.92	
60	22.91	17.11	.4112	-4.83	15.02	.1106	.2431	.2034	.5084	.22.53	.15.58	-5.20	14.90	
72	22.79	17.11	.3309	-4.75	15.04	.0855	.2299	.1969	.0220	.22.59	.16.21	-5.18	14.94	

ALTITUDE (KMH) - 12

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
 FOR XP AND YP
 GIVEN X
 Y

MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
X	XP	XP	Y	YP	YP	XP	YP	XP	YP	XP	YP	XP	YP	YP
23.36	16.01	.2677	-4.95	16.34	6.20	-	-	-	-	23.36	-4.95	-	-	-
12	23.39	16.35	.8770	-4.92	16.34	.7620	.7595	.2395	.2133	.23.33	.7.98	.2270	-4.97	9.29
24	23.50	16.27	.7220	-4.90	16.33	.9516	.2537	.2061	.1104	.23.26	.11.28	.2391	-4.98	12.76
36	23.61	16.22	.5962	-4.87	14.52	.2513	.2469	.1795	.4455	.23.21	.13.06	.2385	-4.99	13.81
48	23.67	16.21	.5044	-4.78	14.27	.1364	.2505	.1737	.0220	.23.21	.14.01	.2267	-5.00	14.10
60	23.67	16.30	.4378	-4.66	14.19	.1106	.2509	.1915	.0171	.21.25	.14.66	.2158	-5.03	14.12
72	23.56	16.31	.3526	-4.58	14.18	.0356	.2481	.0783	.0372	.23.30	.15.32	.2213	-4.99	14.02

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 1932143 - VAMPURSES
 MONTH OF MARCH - JANUARY
 PLANE OF REFERENCE - 2/65 - 111/70
 ALPHA ANGLE - 90.0

ALTITUDE (MM) - 11

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

01 01 01 01
 142 23.67 16.90 .7824 -6.19 12.99 620
 142 23.10 14.85 .9914 -.456 12.96 .7805 .2761 .2576 .2362 .23.04 6.75 .2134 -.60 6.10
 24 23.16 14.76 .7696 -.456 12.97 .466n .2721 .2711 .1576 .22.95 .6.62 24.51 -.61 11.40
 35 23.30 14.75 .6267 -.456 12.95 .2556 .2668 .1485 .4817 .22.92 .11.54 24.62 -.62 12.46
 46 23.37 14.73 .5383 -.456 12.91 .1352 .2702 .1798 .7549 .22.91 .12.48 24.68 -.64 12.73
 60 23.39 14.79 .9619 -.33 12.95 .0942 .2695 .1016 .753 .22.94 .13.16 24.82 -.65 12.74
 72 23.32 14.87 .5717 -.425 17.62 .0759 .27669 .1989 .7541 .22.94 .13.01 .2343 -.63 12.75

ALTITUDE (MM) - 14

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

01 01 01 01
 142 21.7C 12.99 .2051 -6.13 11.51 620
 142 21.79 12.94 .9075 -.614 11.29 .7071 .3G12 .2901 .75A1 .21.66 .5.64 .20793 -.13 6.67
 28 21.81 12.99 .7712 -.455 11.31 .4946 .27U9 .1810 .1610 .21.67 .9.74 .2451 -.14 5.67
 56 21.91 12.87 .6512 -.413 11.27 .2661 .2750 .2120 .1129 .21.51 .7.81 .2554 -.15 10.74
 88 21.96 12.94 .5612 -.404 11.26 .1914 .2786 .1994 .903 .21.54 .10.70 .2510 -.16 11.04
 92 22.72 12.97 .4770 .4566 .2766 .2765 .1767 .1767 .11.55 .11.55 .2553 -.20 11.06
 72 21.76 12.95 .3651 -.384 11.16 .1724 .2938 .2013 .0811 .21.67 .11.96 .2561 -.19 11.27

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 1932180 - WANDMERSG
 NORTH OF RECORD - JANUARY
 PERIOD OF RECORD - 2/65 - 11/74
 ALMA ANGLE - 90.0

Altitude (km) - 15

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
 FOR XP AND YP

	MEAN X	S.D. XP	R (X,XP)	MEAN Y	S.D. YP	R (Y,YP)	MEAN XP, YP	S.D. (XP, YP)	R (XP, YP)	MEAN YP	S.D. (YP)
DT HR	19.43	11.00	-	3342	-3.69	-	9.57	6.20	-	19.43	-3.69
12	19.48	10.95	.903	-3.70	7.56	.8116	3304	.3316	.2163	19.30	6.71
24	19.54	10.91	.7652	-3.70	9.57	.5129	3290	.3269	.2037	19.34	6.78
36	19.63	10.91	.6679	-3.70	9.56	.2907	3267	.2515	.1529	19.29	6.15
48	19.69	10.88	.5758	-3.62	9.55	.1623	3259	.2259	.1250	17.24	8.96
60	19.73	10.91	.8811	-3.52	9.50	.1126	3275	.2175	.1072	19.26	9.60
72	19.72	10.92	.3926	-3.46	9.46	.0986	3242	.2217	.1059	19.32	10.11

Altitude (km) - 16

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
 FOR XP AND YP

	MEAN X	S.D. XP	R (X,XP)	MEAN Y	S.D. YP	R (Y,YP)	MEAN XP, YP	S.D. (XP, YP)	R (XP, YP)	MEAN YP	S.D. (YP)
DT HR	16.54	9.21	-	3613	-3.33	-	7.94	6.20	-	16.54	-3.33
12	16.59	9.17	.9023	-3.36	7.99	.8259	.546	.3750	.2949	16.45	3.96
24	16.65	9.16	.7969	-3.36	7.95	.5515	.1562	.1542	.2271	16.45	5.56
36	16.73	9.16	.5812	-3.36	7.98	.3353	.1566	.3151	.1804	16.61	6.72
48	16.78	9.16	.5066	-3.24	7.92	.2036	.3599	.2477	.1519	16.60	7.42
60	16.82	9.17	.4970	-3.21	7.90	.1459	.3562	.2912	.1352	16.61	8.01
72	16.82	9.17	.4133	-3.15	7.88	.1247	.1528	.2657	.1269	16.63	8.43

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL multivariate normal statistics of x, y, xp, yp
 STATION 1932181 - WADDEMBURG
 MONTH OF RECORD - JANUARY
 PERIOD OF PLENDID - 2/6, - 11/70
 ALTIMA SOURCE - 96.0

ALTITUDE (MM) - 17

QUADRIVARIATE NORMAL STATISTICS OF x, y, xp, yp

CONDITIONAL multivariate normal statistics FOR xp AND yp

MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
X	XP	Y	XP, YP	YP	Y	XP, Y	YP	XP	XP, YP	YP	Y
13.37	7.91	.2669	-5.09	6.51	6.20						
01	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.
12	13.42	7.79	.9023	-5.00	6.51	.9409	.3839	.9148	.3114	.332	.346
28	13.49	7.79	.8066	-5.10	6.52	.6013	.3637	.3055	.2452	1.27	.549
36	13.54	7.80	.7010	-5.09	6.51	.0401	.1816	.3634	.2034	1.24	.555
48	13.59	7.80	.6121	-5.04	6.50	.2685	.3840	.3447	.1807	1.23	.616
60	13.62	7.81	.5168	-2.97	6.49	.1996	.3799	.3291	.1618	1.29	.669
72	13.64	7.82	.4313	-2.95	6.46	.1660	.3766	.3097	.1519	1.25	.705

ALTITUDE (MM) - 18

QUADRIVARIATE NORMAL STATISTICS OF x, y, xp, yp

MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
X	XP	Y	XP, YP	YP	Y	XP, Y	YP	XP	XP, YP	YP	Y
10.17	6.87	.3905	-2.96	5.37	6.20						
01	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.
12	10.22	6.87	.7065	-2.96	5.73	.8556	.9003	.8797	.1250	10.12	.284
28	10.29	6.88	.8235	-2.97	5.34	.6559	.1994	.6111	.2610	10.04	.186
36	10.34	6.90	.7331	-2.95	5.74	.4760	.3962	.4779	.2322	10.04	.464
48	10.37	6.91	.6511	-2.92	5.33	.3504	.1973	.3691	.2344	10.04	.2140
60	10.40	6.92	.5581	-2.69	5.72	.2699	.3753	.3760	.1867	10.04	.549
72	10.43	6.93	.4916	-2.46	5.71	.2173	.2406	.3438	.1780	10.04	.2671

QUADRAVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 193214 - VANDENBERG
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 2/65 - 11/74
 ALPHAS A-FIVE - 90.0

ALTITUDE (MM) - 19

QUADRAVARIATE NORMAL STATISTICS OF X,Y,XP,YP

MEAN XP yp	S.D. X Y	R (X,Y)	MEAN R YP	S.D. R YP	R (XP,YP)	R (YP,X)	MEAN R (XP,Y)	S.D. R XP	R (XP,YP)	MEAN R YP	S.D. R YP
7.15	6.37	.3965	-2.91	3.61	620						
7.15	6.37	.3965	-2.91	3.61	620						
7.15	6.37	.3965	-2.91	3.61	620						
7.15	6.37	.3965	-2.91	3.61	620						

ALTITUDE (MM) - 20

QUADRAVARIATE NORMAL STATISTICS OF X,Y,XP,YP

MEAN XP yp	S.D. X Y	R (X,Y)	MEAN R YP	S.D. R YP	R (XP,YP)	R (YP,X)	MEAN R (XP,Y)	S.D. R XP	R (XP,YP)	MEAN R YP	S.D. R YP
9.48	6.30	.3791	-2.92	3.61	620						
9.48	6.30	.3791	-2.92	3.61	620						
9.48	6.30	.3791	-2.92	3.61	620						
9.48	6.30	.3791	-2.92	3.61	620						

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

MEAN X Y	S.D. X Y	GIVEN X Y	MEAN Y X	S.D. Y X	GIVEN Y X
7.15	6.37	620	7.15	6.37	-2.91
7.15	6.37	620	7.15	6.37	-2.91
7.15	6.37	620	7.15	6.37	-2.91
7.15	6.37	620	7.15	6.37	-2.91

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

MEAN X Y	S.D. X Y	GIVEN X Y	MEAN Y X	S.D. Y X	GIVEN Y X
7.15	6.37	620	7.15	6.37	-2.91
7.15	6.37	620	7.15	6.37	-2.91
7.15	6.37	620	7.15	6.37	-2.91
7.15	6.37	620	7.15	6.37	-2.91

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND
STATION 1932161 - WANDENBERG
MONTH OF RECORD - JANUARY
PERIOD OF RECORD - 2/65 - 11/74
ALPHA ANGLE - 90.0

ALTITUDE (KMI) - 21

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

DT HR	MEAN XP	S.D. XP	R (X,XP)	MEAN Y _P	S.D. Y _P	R (Y,PY)	R (XP,YP)	R (YP,X)	R (YP,Y)	MEAN GIVEN X		MEAN GIVEN Y		S.D. YP	
										N	MEAN XP	S.D. XP	R (XP,YP)	MEAN YP	
20.20	2.25	6.57	.3556	-2.92	3.46	620					2.29		-2.92		
24	2.35	6.63	.9260	-2.91	3.49	6616	.3875	.3163	.223	2.48	.0451	-2.93	1.74		
29	2.42	6.67	.6734	-2.92	3.49	6747	.3526	.4524	.2865	3.20	.0820	-2.93	2.27		
36	2.48	6.72	.8087	-2.92	3.50	6350	.3491	.3725	.2561	2.19	.1568	-2.79	2.63		
48	2.51	6.75	.7497	-2.90	3.51	5376	.3486	.3896	.2336	2.13	.1959	-2.95	2.67		
60	2.55	6.76	.6729	-2.88	3.51	4382	.3498	.2996	.7151	2.12	.086	-2.96	3.79		
72	2.60	6.80	.6097	-2.86	3.51	3517	.3517	.2668	.1928	2.10	.521	-2.96	3.21		

ALTITUDE (KMI) - 22

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

DT HR	MEAN XP	S.D. XP	R (X,XP)	MEAN Y _P	S.D. Y _P	R (Y,PY)	R (XP,YP)	R (YP,X)	R (YP,Y)	MEAN GIVEN X		MEAN GIVEN Y		S.D. YP	
										N	MEAN XP	S.D. XP	R (XP,YP)	MEAN YP	
62	6.62	7.12	.3523	-2.91	3.36	620					.62		-2.91		
12	6.69	7.19	.9325	-2.91	3.37	8629	.3523	.3716	.3251	5.56	.257	-2.92	1.64		
29	7.76	7.23	.6816	-2.90	3.38	7499	.3497	.4507	.2865	4.16	.1166	-2.92	2.19		
36	8.83	7.29	.6191	-2.70	3.39	6479	.3474	.3497	.2769	4.45	.1646	-2.93	2.53		
48	8.87	7.31	.7516	-2.60	3.40	5696	.3401	.3188	.2511	4.48	.2176	-2.94	2.77		
67	9.01	7.31	.6784	-2.67	3.40	4465	.3500	.4621	.2747	5.73	.2730	-2.94	2.99		
72	9.06	7.34	.6145	-2.87	3.41	3586	.3525	.2199	.3042	4.41	.662	-2.94	3.12		

BIVARIATE NORMAL STATISTICS FOR X, Y

STATION 1932141 - VANCOUVER

X = VINT T₁Y = VINT T₂

MONTH	PER. OF REC.	ALT. MM.	ALPHA DEG.	MEAN		S.D. X	MEAN (X, Y)	S.D. Y	N
				X	Y				
1	-	2/65 - 11/74	5	90.0	10.74	10.65	126.18	-3.61	620
	2/65 - 11/74	6	90.0	12.45	12.22	27.78	-3.90	11.67	620
	2/65 - 11/74	7	90.0	10.88	13.77	24.68	-6.70	13.10	620
	2/65 - 11/74	8	90.0	16.06	15.26	28.52	-6.55	16.23	620
	2/65 - 11/74	9	90.0	19.08	16.49	27.81	-4.88	15.78	620
	2/65 - 11/74	10	90.0	21.08	17.21	26.93	-5.11	15.47	620
	2/65 - 11/74	11	90.0	22.62	17.51	26.80	-5.13	15.75	620
	2/65 - 11/74	12	90.0	23.36	16.90	26.77	-4.95	14.18	620
	2/65 - 11/74	13	90.0	23.07	16.20	28.24	-6.59	12.99	620
	2/65 - 11/74	14	90.0	21.70	12.99	30.91	-6.13	11.11	620
	2/65 - 11/74	15	90.0	19.43	11.00	35.82	-2.69	9.57	620
	2/65 - 11/74	16	90.0	16.26	9.21	31.64	-3.13	7.94	620
	2/65 - 11/74	17	90.0	15.37	7.91	38.54	-3.00	6.11	620
	2/65 - 11/74	18	90.0	10.17	6.81	39.95	-2.92	5.32	620
	2/65 - 11/74	19	90.0	7.15	5.37	39.25	-2.91	6.51	620
	2/65 - 11/74	20	90.0	4.98	6.30	37.81	-2.92	5.61	620
	2/65 - 11/74	21	90.0	2.29	6.47	35.58	-2.92	3.98	620
	2/65 - 11/74	22	90.0	.62	7.12	35.23	-2.91	3.36	620

ORIGINAL PAGE IS
OF POOR QUALITY

STATION 1912141 - WANNENG
MONTH OF RECORD - JANUARY
PERIOD OF RECORD - 2/65 - 11/79
ALPHA ANGLE - 90.0

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
X = V1AT 1
Y = V1AT 1
XP = V1AT 1 + D11 - V1AT 11
YP = V1AT 1 + D11 - V1AT 11

ALITUDE (KM) - 5

QUADRIVARIATE NORMAL STATISTICS OF X,Y,XP,YP

MEAN X	S.D. X	R (X,Y)	MEAN Y	S.D. Y	N	MEAN XP	S.D. XP	R (XP,YP)	MEAN YP	S.D. YP	R (YP,XP)
15.74	1C.65	.2639	-3.63	10.64	620	17.74	.3463	.2344	6.75	9.98	.2695

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

DT HR	MEAN XP	S.D. XP	R (X,XP)	MEAN YP	S.D. YP	R (Y,YP)	MEAN R (XP,YP)	R (YP,XP)	MEAN XP	S.D. XP	R (XP,YP)
12	.018	.648	-.3522	.66	7.50	-.3627	.2272	.1130	6.75	9.98	.2695
28	.15	.603	-.4955	.11	10.76	-.5168	.2780	.0552	6.62	9.60	.2845
36	.23	.513	-.5131	.16	12.49	-.5028	.1939	.0120	5.87	9.74	.2859
48	.19	.1127	-.5583	.17	13.10	-.6298	.1723	.0169	5.77	8.74	.3795
63	.07	.11.95	-.5859	.26	12.32	-.6632	.1602	.0331	5.72	8.53	.3364
72	-.16	.12.72	-.6176	.35	13.52	-.6512	.1680	.0160	5.59	8.31	.3447

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

DT HR	MEAN XP	S.D. XP	R (X,XP)	MEAN YP	S.D. YP	R (Y,YP)	MEAN R (XP,YP)	R (YP,XP)	MEAN XP	S.D. XP	R (XP,YP)
17	.17	.676	-.3126	.05	9.66	-.3750	.2544	.0761	7.85	11.5	.2816
28	.19	.11.12	-.4932	.12	12.22	-.5281	.2380	.0217	7.18	10.82	.2878
36	.26	.11.89	-.5131	.12	14.15	-.6119	.2349	.0193	7.66	10.76	.2872
48	.22	.12.94	-.5579	.21	14.79	-.6364	.2197	.0126	7.36	11.14	.3108
67	.11	.13.75	-.5862	.36	16.97	-.6887	.1691	.0196	6.93	9.79	.3338
72	-.04	.14.62	-.6180	.39	15.13	-.6536	.1508	.0128	6.71	9.13	.3556

CONDITIONAL BIVARIATE NORMAL STATISTICS
FOR XP AND YP

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, Z, W, V
 STATION 1972141 - VANDENBERG
 Month of RECORD - JULY 1970
 PERIOD OF RECORD - 2/65 - 12/70
 ALPHA ANGLE - 0°.0

Altitude (km) - 7

QUADRIVARIATE NORMAL STATISTICS OF X, Y, Z, W, V

CONDITIONAL BIVARIATE NORMAL STATISTICS FOR Xp AND Yp

	MEAN X	S.D. Xp	MEAN Y	S.D. Yp	MEAN Z	S.D. Zp	MEAN W	S.D. Wp	MEAN V	S.D. Vp
No.										
12	.06	7.92	.00	3.92	0.16	9.9	-0.38	9.6	.2689	.0018
25	.22	11.49	.00	3.92	0.16	13.72	-0.2556	9.59	.2568	.0016
36	.26	15.46	-.51	2.49	15.74	-6.12	-0.7527	0.16	11.74	.2625
42	.25	19.92	0.25	5.67	2.55	-0.2659	-0.7854	0.11	10.03	.2624
65	.13	15.53	0.23	5.67	1.67	-0.5654	-0.7854	0.11	9.68	.2624
72	-.02	16.99	0.23	5.67	1.67	-0.5654	-0.7854	0.11	9.74	.2624

	MEAN xp	S.D. xp	MEAN Yp	S.D. Yp	MEAN Zp	S.D. Zp	MEAN Wp	S.D. Wp	MEAN Vp	S.D. Vp
No.										
12	.06	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
25	.22	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
36	.26	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
42	.25	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
65	.13	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
72	-.02	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201

	MEAN xp	S.D. xp	MEAN Yp	S.D. Yp	MEAN Zp	S.D. Zp	MEAN Wp	S.D. Wp	MEAN Vp	S.D. Vp
No.										
12	.06	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
25	.22	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
36	.26	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
42	.25	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
65	.13	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201
72	-.02	13.71	.7868	-.0070	15.10	6.20	14.98	-.0201	16.98	-.0201

QUADRIVARIATE NORMAL STATISTICS OF X, Y, Z, W, V
 CONDITIONAL BIVARIATE NORMAL STATISTICS FOR Xp AND Yp
 MEAN Xp: 16.98 S.D. Xp: 4.55
 MEAN Yp: 16.98 S.D. Yp: 4.55
 MEAN Zp: 16.98 S.D. Zp: 4.55
 MEAN Wp: 16.98 S.D. Wp: 4.55
 MEAN Vp: 16.98 S.D. Vp: 4.55

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRATIC AND CUMULATIVE BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 193261 - VANCOUVER
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 2/65 - 11/74
 ALPHAS ANGLE - 07.0
 ALTITUDE (KMI) - 6

ALTITUDE (KMI) - 6

QUADRATIC NORMAL STATISTICS OF X, Y, XP, YP

CONDITIONAL BIVARIATE NORMAL STATISTICS

FOR XP AND YP

DT HR	MEAN XP	S.D. XP	R X, YP	MEAN YP	S.D. YP	MEAN		S.D.		MEAN		S.D.	
						X	Y	X	Y	X	Y	X	Y
12	.74	.94	-.2961	.07	.11.42	-3.3949	.2666	-.0173	.1616	12.68	15.68	.2737	.57
24	.23	13.66	-.4370	.13	16.03	-5.192	.2682	-.0983	.2128	10.49	16.79	.2694	12.61
36	.30	16.02	-.5462	.15	16.61	-6.167	.2748	-.1732	.2413	10.41	14.13	.2614	11.76
48	.51	17.40	-.5452	.24	19.46	-6.549	.2531	-.0670	.2404	10.36	13.71	.2759	11.30
60	.21	18.95	-.5707	.33	19.65	-6.645	.2059	-.0228	.2254	10.34	13.41	.3047	11.16
72	.07	19.52	-.6297	.41	19.90	-6.6704	.1796	-.0643	.2102	10.19	13.06	-.3215	11.00

ALTITUDE (KMI) - 6

QUADRATIC NORMAL STATISTICS OF X, Y, XP, YP

CONDITIONAL BIVARIATE NORMAL STATISTICS

FOR XP AND YP

DT HR	MEAN XP	S.D. XP	R X, YP	MEAN YP	S.D. YP	MEAN		S.D.		MEAN		S.D.	
						X	Y	X	Y	X	Y	X	Y
12	.76	.95	-.2886	.06	.11.96	-.3757	.2510	-.0178	.1373	11.39	16.67	.2661	.54
24	.21	13.93	-.4168	.17	16.41	-5.165	.2641	-.0649	.1692	11.57	15.48	.2637	13.10
36	.29	16.83	-.4923	.12	19.91	-6.154	.2734	-.1621	.2279	11.57	16.20	.2531	12.11
48	.42	17.91	-.5336	.22	21.79	-6.773	.2522	-.1766	.2729	11.36	16.96	.2641	11.57
60	.25	19.51	-.5593	.32	21.93	-6.641	.2197	-.0441	.2175	11.42	16.16	.2694	11.55
72	.12	21.15	-.5926	.49	21.62	-6.964	.1816	-.0510	.1914	11.47	16.79	.2167	11.34

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, XP, YP
 STATION 99219 - VANCOUVER
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 2/65 - 1/78
 ALPHA ANGLE - QU. 15°

ALTITUDE (KMI) - 11

QUADRIVARIATE NORMAL STATISTICS OF X, Y, XP, YP

CONDITIONAL BIVARIATE NORMAL STATISTICS

	MEAN	S.D.	\bar{x}	MEAN	S.D.	\bar{y}	MEAN	S.D.	\bar{xp}	MEAN	S.D.	\bar{yp}	MEAN	S.D.	\bar{xp}	MEAN	S.D.	\bar{yp}
01	MEAN XP	S.D. XP	(X,XP)	MEAN YP	S.D. YP	(Y,YP)	MEAN (XP,YP)	S.D. (XP,YP)	(XP,YP)	MEAN YP	S.D. YP	(YP,YP)	MEAN (XP,YP)	S.D. (XP,YP)	(XP,YP)	MEAN YP	S.D. YP	(YP,YP)
02	22.62	17.21	.2696	-5.15	15.25	6.20	22.62	5.11										
03	.04	.08	-.2697	.78	10.92	1.3620	.2329	.0116	-.1111	.11.82	.0556	.2631	-.1.15	.0.27				
04	.17	.10	-.3597	.07	16.18	.25321	.2568	.0763	-.1649	.15.74	.0589	.2589	-.78	.12.88				
05	.27	.15	-.4765	.19	16.63	.26015	.2600	.1908	-.2058	12.114	.0507	.2521	-.76	.11.96				
06	.32	.19	-.5166	.19	19.18	.26593	.2655	.0857	-.2066	12.015	.0668	.2621	-.76	.11.90				
07	.29	.17	-.5066	.37	20.16	.26732	.2123	.0572	-.2027	12.16	.0533	.2826	-.65	.11.20				
08	.17	.05	-.5017	.39	20.68	.26616	.0619	.0591	-.1804	11.93	.0194	.213	-.13	.11.11				
09	23.36	16.00	.2677	-4.95	14.39	6.70												
10	MEAN XP	S.D. XP	(X,XP)	MEAN YP	S.D. YP	(Y,YP)	MEAN (XP,YP)	S.D. (XP,YP)	(XP,YP)	MEAN YP	S.D. YP	(YP,YP)	MEAN (XP,YP)	S.D. (XP,YP)	(XP,YP)	MEAN YP	S.D. YP	(YP,YP)
11	.12	.12	-.2534	.05	9.91	-.3088	.2175	.0582	-.0797	.11.97	.0585	.2445	-.64	.13.40				
12	.14	.16	-.2813	.05	15.14	-.5763	.2413	.0581	-.1472	.12.08	.0516	.2662	-.69	.12.21				
13	.25	.16	-.0584	.05	17.56	.6141	.2612	.01108	-.1707	.12.23	.0553	.2030	-.91	.11.32				
14	.11	.17	-.5045	.16	19.13	-.6604	.2478	.0973	-.1879	.12.24	.0112	.2793	-.85	.10.76				
15	.31	.13	-.5342	.22	19.16	-.6762	.2176	.0731	-.1693	.12.11	.0251	.2895	-.78	.10.59				
16	.22	.22	18.61	.37	19.84	-.6848	.1975	.0749	-.1712	.12.24	.0361	.3375	-.13	.10.45				

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, VP, VP
STATION 193211 - VANGUARD
MONTH OR RECRUIT - JANUARY
POSITION OF AERONAUT - 11/6 - 11/78
ALPHA ANGLE - 90.0

ALTITUDE (MM)

QUADRIVARIATE NORMAL STATISTICS OF X, Y, VP, VP

CONDITIONAL BIVARIATE NORMAL STATISTICS

01	MEAN VP	S.D. VP	R (X, Y)	MEAN VP	S.D. VP	R (X, VP)	R (Y, VP)	R (X, Y)	MEAN VP	S.D. VP	R (X, VP)	R (Y, VP)	R (X, Y)
12	.09	.2395	.01	.060	.3245	.2195	.655	.0796	.01	.061	.1646	.2864	.1556
20	.11	.3635	.07	.1341	.5196	.2505	.6096	.1280	.1176	.1376	.2897	.1170	.1170
36	.22	.3635	.07	.1643	.5117	.2632	.6116	.1116	.1191	.1375	.2860	.1026	.1026
49	.10	.0894	.03	.0672	.2522	.0169	.1737	.0195	.1267	.1267	.2966	.090	.0933
60	.22	.5238	.025	.1739	.6775	.2258	.6591	.1776	.1212	.1212	.3282	.110	.052
72	.25	.1645	.03	.1745	.6849	.1982	.6096	.1667	.1202	.1202	.3282	.110	.052

CONDITIONAL BIVARIATE NORMAL STATISTICS

01	MEAN VP	S.D. VP	R (X, Y)	MEAN VP	S.D. VP	R (X, VP)	R (Y, VP)	R (X, Y)	MEAN VP	S.D. VP	R (X, VP)	R (Y, VP)	R (X, Y)
12	.10	.579	.238	.109	.171	.3210	.6048	.0010	.109	.1215	.1011	.1071	.073
20	.11	.875	.7486	.111	.1347	.575	.5222	.0069	.111	.1116	.1116	.1116	.091
36	.21	.1761	.4277	.137	.1347	.6167	.7665	.-1155	.1354	.1173	.1173	.1173	.044
49	.24	.1210	.4177	.140	.1679	.6576	.2576	.-1160	.1661	.1174	.1174	.1174	.050
60	.17	.1327	.5169	.071	.113	.6757	.2725	.-1179	.1779	.1189	.1189	.1189	.031
72	.27	.1435	.5587	.07	.1521	.6961	.1963	.-1265	.1678	.1191	.1191	.1191	.025

QUADRAVARIATE AND CONDITIONAL MULTIVARIATE NORMAL STATISTICS OF X, Y, VP, VP
 STATION 191216 - VANDENBERG
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 7/65 - 11/74
 ALPHAS ANGLF - Q10,J

ALTITUDE (KM) - 16

QUADRAVARIATE NORMAL STATISTICS OF X, VP, VP

	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}
DI	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}
12	11.73	.11	-2.295	-0.11	5.07	.3072	-0.087	-0.016	10.67	.1571	-0.18	.014
20	11.78	.11	-3.378	-0.01	9.04	.0928	-0.2516	-0.054	10.34	.1553	-0.18	.014
36	11.73	.09	-0.0155	-0.01	11.39	.0571	-0.2645	-0.1472	-15.25	.1006	9.99	.062
69	11.78	.09	-0.6693	.07	12.36	.0685	-0.2568	-0.1975	10.33	.0707	-0.59	.065
67	11.73	.13	-5.133	.17	12.70	.0666A	-0.2305	-0.1775	10.13	.062	-0.927	.0707
72	12.78	.29	-0.5555	.23	12.79	-0.6757	-0.2212	-0.1988	-0.1774	.073	-0.67	.0707

ALTITUDE (KM) - 16

QUADRAVARIATE NORMAL STATISTICS OF X, Y, VP, VP

	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}
DI	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}	MEAN	S.D.	X _{VP}	Y _{VP}
12	11.73	.11	-2.293	-0.11	5.07	.3075	-0.297	-0.1126	10.67	.1571	-0.18	.014
20	11.78	.11	-3.378	-0.01	9.04	.0923	-0.2456	-0.0786	10.34	.1553	-0.18	.014
36	11.73	.09	-0.0155	-0.01	11.39	.0570	-0.2677	-0.1522	-15.25	.1007	9.99	.062
69	11.78	.09	-0.6693	.07	12.36	.0685	-0.2568	-0.1975	10.33	.0707	-0.59	.065
67	11.73	.13	-5.133	.17	12.70	.0666A	-0.2305	-0.1775	10.13	.062	-0.927	.0707
72	12.78	.29	-0.5555	.23	12.79	-0.6757	-0.2212	-0.1988	-0.1774	.073	-0.67	.0707

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, KP, VP
 STATION 193214 - VANDENBURG
 MONTH OF RECORD - JANUARY
 PLATO OF RECORD - 2/65 - 11/70
 ALPHA ANGLE - 90.0

ALITUDE (MM) - 17

QUADRIVARIATE NORMAL STATISTICS OF X, Y, KP, VP

MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
X	KP	(X, KP)	Y	VP	(Y, VP)	KP	VP	(KP, VP)	Y	VP	(Y, VP)
12	.05	.345	-.2267	.357	.367	-.2914	.1717	.0652	-.1570	.764	.0532
29	.12	.905	-.3100	.01	.582	-.5896	.2310	.0159	-.1551	.739	.150
36	.18	.618	-.1886	.079	.715	-.5469	.2362	.07286	-.1657	.731	.76
49	.22	.614	-.8925	.05	.717	-.6159	.2266	.01965	-.1691	.723	.514
67	.25	.710	-.4526	.07	.623	-.6341	.2196	.0567	-.1777	.723	.515
72	.27	.838	-.5534	.14	.6496	.2170	.0703	-.0703	-.1813	.721	.509

ALITUDE (MM) - 18

QUADRIVARIATE NORMAL STATISTICS OF X, Y, KP, VP

MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R	MEAN	S.D.	R
X	KP	(X, KP)	Y	VP	(Y, VP)	KP	VP	(KP, VP)	Y	VP	(Y, VP)
11.17	6.97	.3995	-2.96	5.12	5.20	-2.96	5.12	5.20	10.17	-2.96	5.12
12	.75	2.97	-.2165	.07	.84	-.2657	.1512	.0930	-.1374	.6218	.4205
26	.12	4.34	-.2930	-.011	.482	-.4116	.2168	.0147	-.1657	.653	.432
36	.17	5.03	-.3596	-.07	.584	-.5584	.2184	.0192	-.1716	.591	.449
49	.20	5.75	-.6115	.04	.617	-.5646	.2126	.0193	-.1749	.623	.4686
67	.23	6.44	-.6934	.07	.645	-.6042	.2149	.0153	-.1744	.573	.4413
72	.26	7.11	-.5574	.10	.655	-.6267	.2152	.01515	-.1775	.571	.4491

CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF X, Y, R, S, P, D, B
CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF U, V, W, Z, Q, T, F, G

	MEAN	MEDIAN	SD	S.E.M.	MIN	MAX	CONF. INT.				
U	5.66	5.76	1.28	0.10	-0.50	11.72	5.00	5.00	5.00	5.00	5.00
V	4.55	4.48	0.65	0.04	3.25	5.85	4.00	4.00	4.00	4.00	4.00
W	2.89	2.80	0.26	0.02	2.35	3.43	2.60	2.60	2.60	2.60	2.60
Z	0.85	0.79	0.24	0.02	-0.05	1.80	0.60	0.60	0.60	0.60	0.60
X	2.48	2.45	0.09	0.00	2.25	2.70	2.30	2.30	2.30	2.30	2.30
Y	0.69	0.68	0.12	0.01	-0.05	1.50	0.50	0.50	0.50	0.50	0.50
R	3.40	3.30	0.11	0.01	2.45	4.40	3.30	3.30	3.30	3.30	3.30
S	2.74	2.73	0.12	0.01	1.80	3.80	2.60	2.60	2.60	2.60	2.60
T	2.15	2.13	0.08	0.01	1.40	3.00	2.00	2.00	2.00	2.00	2.00
F	0.45	0.45	0.08	0.01	-0.05	1.00	0.30	0.30	0.30	0.30	0.30
G	1.65	1.65	0.10	0.01	0.00	3.50	1.00	1.00	1.00	1.00	1.00
P	2.40	2.40	0.08	0.01	1.50	3.40	2.20	2.20	2.20	2.20	2.20
D	0.13	0.13	0.05	0.00	-0.10	0.50	0.00	0.00	0.00	0.00	0.00
B	0.40	0.40	0.05	0.00	-0.10	1.00	0.00	0.00	0.00	0.00	0.00

	MEAN	MEDIAN	SD	S.E.M.	MIN	MAX	CONF. INT.				
U	5.66	5.76	1.28	0.10	-0.50	11.72	5.00	5.00	5.00	5.00	5.00
V	4.55	4.48	0.65	0.04	3.25	5.85	4.00	4.00	4.00	4.00	4.00
W	2.89	2.80	0.26	0.02	2.35	3.43	2.60	2.60	2.60	2.60	2.60
Z	0.85	0.79	0.24	0.02	-0.05	1.80	0.60	0.60	0.60	0.60	0.60
X	2.48	2.45	0.09	0.00	2.25	2.70	2.30	2.30	2.30	2.30	2.30
Y	0.69	0.68	0.12	0.01	-0.05	1.50	0.50	0.50	0.50	0.50	0.50
R	3.40	3.30	0.11	0.01	2.45	4.40	3.30	3.30	3.30	3.30	3.30
S	2.74	2.73	0.12	0.01	1.80	3.80	2.60	2.60	2.60	2.60	2.60
T	2.15	2.13	0.08	0.01	1.40	3.00	2.00	2.00	2.00	2.00	2.00
F	0.45	0.45	0.08	0.01	-0.05	1.00	0.30	0.30	0.30	0.30	0.30
G	1.65	1.65	0.10	0.01	0.00	3.50	1.00	1.00	1.00	1.00	1.00
P	2.40	2.40	0.08	0.01	1.50	3.40	2.20	2.20	2.20	2.20	2.20
D	0.13	0.13	0.05	0.00	-0.10	0.50	0.00	0.00	0.00	0.00	0.00
B	0.40	0.40	0.05	0.00	-0.10	1.00	0.00	0.00	0.00	0.00	0.00

CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF X, Y, R, S, P, D, B
CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF U, V, W, Z, Q, T, F, G

CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF X, Y, R, S, P, D, B
CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF U, V, W, Z, Q, T, F, G

CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF X, Y, R, S, P, D, B
CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF U, V, W, Z, Q, T, F, G

CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF X, Y, R, S, P, D, B
CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF U, V, W, Z, Q, T, F, G

CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF X, Y, R, S, P, D, B
CONFIDENCE INTERVALS FOR THE MEAN STATISTICS OF U, V, W, Z, Q, T, F, G

ORIGINAL PAGE IS
OF POOR QUALITY

QUADRIVARIATE AND CONDITIONAL BIVARIATE NORMAL STATISTICS OF X, Y, VP, TP
 STATION 0972141 - WINDENBERG
 MONTH OF RECORD - JANUARY
 PERIOD OF RECORD - 1/65 - 11/74
 ALPHA ANGLF - 20.0 JU

ALTITUDE (KMH)

QUADRIVARIATE NORMAL STATISTICS OF X, Y, VP, TP

	MEDIAN	S.D.	E_x	MEDIAN	S.D.	E_y	MEDIAN	S.D.	E_{xy}	MEDIAN	S.D.	E_{xp}	MEDIAN	S.D.	E_{yp}
1	1.69	1.17	2.54	-0.177	0.1	1.93	-0.2776	0.615	0.006	-0.7731	2.31	6.86	-0.747	-1.16	3.35
2	1.24	1.14	3.33	-0.2224	0.14	2.09	-0.3539	0.701	0.043	-0.7956	1.97	6.37	-0.638	-1.18	3.23
3	1.19	1.19	4.41	-0.2759	0.17	2.07	-0.4224	0.7422	0.048	-0.893	1.97	6.30	-0.569	-1.25	3.14
4	1.09	1.22	4.76	-0.3244	0.15	2.36	-0.4748	0.7945	0.1265	-0.923	2.21	6.72	-0.320	-1.29	3.05
5	1.06	1.26	5.02	-0.3742	0.18	2.71	-0.5245	0.8216	0.1578	-0.963	2.45	6.18	-0.262	-1.15	2.96
6	1.02	1.32	5.91	-0.4179	0.25	2.52	-0.5638	0.8556	0.1689	-0.981	2.67	5.98	-0.261	-1.16	2.87

ALTITUDE (KMH)

QUADRIVARIATE NORMAL STATISTICS OF X, Y, VP, TP

	MEDIAN	S.D.	E_x	MEDIAN	S.D.	E_y	MEDIAN	S.D.	E_{xy}	MEDIAN	S.D.	E_{xp}	MEDIAN	S.D.	E_{yp}
1	1.67	1.12	2.12	-0.1523	0.11	1.73	-0.2575	0.6417	0.002	-0.7775	2.37	6.91	-0.691	-1.14	3.42
2	1.25	1.15	3.05	-0.2143	0.13	2.05	-0.3453	0.7527	0.043	-0.8255	2.07	6.52	-0.527	-1.42	3.35
3	1.21	1.19	3.34	-0.2674	0.17	2.04	-0.4177	0.7943	0.1017	-0.8747	2.07	6.51	-0.394	-1.44	3.27
4	1.07	1.23	3.72	-0.3161	0.15	2.31	-0.4855	0.8212	0.1355	-0.9213	2.26	6.97	-0.326	-1.29	3.18
5	1.04	1.24	4.19	-0.3770	0.19	2.71	-0.5163	0.8553	0.1725	-0.961	2.44	7.04	-0.264	-1.16	2.96
6	1.04	1.34	4.64	-0.4313	0.25	2.95	-0.5745	0.8812	0.1642	-0.981	2.67	7.04	-0.222	-1.45	2.79