$\mathbb{D}_{\mathbf{Z}}$ 

# N78-32468

#### NASTRAN COMPUTER RESOURCE

MANAGEMENT FOR THE MATRIX DECOMPOSITION MODULES

Charles W. Bolz Computer Sciences Corporation

#### SUMMARY

Detailed computer resource measurements of the NASTRAN matrix decomposition spill logic were made using a software input/output monitor. These measurements showed that, in general, job cost can be reduced by avoiding spill. The results indicated that job cost can be minimized by using dynamic memory management. A prototype memory management system is being implemented and evaluated for the CDC CYBER computer.

#### INTRODUCTION

The early large structural analysis programs were designed for secondgeneration computer systems that were severely core-limited, requiring structural programmers to develop ingenious strategies for using mass storage to extend the range of solvable problems. It was for such a computer that NASTRAN was initially developed, and the matrix decomposition code with its efficient spill logic was a singular achievement in numerical analysis software. As NASTRAN was implemented on third generation computers which allowed multiprogramming, such as the UNIVAC 1108 and the CDC 6000 series, it remained expedient to use as little central memory as possible in order to maximize overall system efficiency. However, present day computers such as the CDC CYBER 175 and the UNIVAC 1110 have very large, fast, low-cost semiconductor memories, and excessive mass storage usage can rapidly degrade overall system efficiency and increase job cost. It therefore becomes important for the user to select an optimum memory region size for his problem.

In order to accurately assess the effects of memory region size on  $I/\emptyset$  utilization and job cost, a software monitor was developed to measure  $I/\emptyset$  volumes by file on CDC CYBER computers. Spill volume statistics were accumulated for the SDCØMP and CDCØMP matrix decomposition modules using NASTRAN Level 17.0.0 on the CDC CYBER 175 under the NØS 1.2 operating system. These statistics were interpreted using job cost accounting relations typical of CDC and UNIVAC systems. The results suggested that a dynamic memory management system designed to avoid spill would be cost effective, and a prototype system is being implemented on the CDC CYBER.

Matrices to be decomposed by NASTRAN are normally sparse banded matrices with relatively few terms away from the band. During the decomposition, it is desirable to have all the non-zero terms of a row, and all the non-zero terms of the triangular factor generated by reduction of that row, in main memory. If this is possible for each row, then the matrix need be read in from secondary storage only once during the decomposition, and the factorized matrix written out. If insufficient memory is allocated, however, intermediate results must be stored on spill files. Numerous passes through the spill files may be required to perform the decomposition.

The matrix decomposition and spill logic is described in detail in references 1 and 2.

#### JOB COST ACCOUNTING ALGORITHMS

The astute NASTRAN user interprets computer resource utilization guidelines in terms of job cost, as assessed by his installation accounting algorithm. Results presented in this study are interpreted in terms of two accounting algorithms: one used commonly at CDC installations, and the second at UNIVAC sites.

Many factors go into an accounting algorithm, but for NASTRAN execution only central memory used (CM), central processor-unit time (CPU), and mass storage input/output transfers  $(I/\emptyset)$  are important. In terms of these resources, the CDC accounting formula may be generalized as

$$Cost = (1 + C_1 CM) (C_2 CPU + C_3 I/\emptyset)C_A$$

and the UNIVAC relation as

$$Cost = CM (C_2 CPU + C_3 I/\emptyset)C_4$$

where  $C_2$  and  $C_3$  are functions of the CPU and mass transfer device speeds. The constant  $C_1$  is set by the CDC NØS operating system at 0.007 per 512-word block. The dollar multiplier,  $C_4$ , is installation dependent, so all matrix decomposition costs presented in this study are normalized to the no-spill case.

IBM accounting formulas vary with installation and operating system, so the IBM user should interpret the results presented in terms of his particular system.

### THE I/Ø MONITOR

The basic utility for this study is a software monitor which was originally developed by the author for analyzing the  $I/\emptyset$  usage of programs running under the CDC SCØPE operating system. The monitor decodes all  $I/\emptyset$  requests and records, by data block, the type of request and the number of physical records transferred between central memory and mass storage. The record is printed at the end of each module, as shown in Figure 1.

As adapted for the CDC version of NASTRAN, the  $I/\emptyset$  monitor is called from XIØRTNS, which is the interface between GINØ (General input/output) and the operating system (ref. 3). The monitor was validated by checking the total  $I/\emptyset$  volume printed out against accounting log (dayfile) statistics for each NASTRAN run. Since the monitor itself occupies only 350 words of CYBER 175 memory, and uses about 20 microseconds of central processor time per  $I/\emptyset$  request, it has negligible impact on the job environment.

### THE COMPUTER RESOURCE UTILIZATION STUDY

#### Complex Decomposition

Two problems were chosen for study. The first is a complex eigenvalue analysis of a gas-filled, thin elastic cylinder (NASTRAN Demonstration Problem 7-2-1 of reference 4). This case requires decomposition of an order 390 complex matrix, and can be solved by NASTRAN in a reasonable memory region only by using the determinant method. This particular problem was the impetus of the present study. When it was run on an IBM S/360-95 under the Multiple Variable Tasking (MVT) operating system with a memory region of 410000 bytes, an  $I/\emptyset$  timeout resulted after twenty minutes  $I/\emptyset$  time. When the region size was increased to 500000 bytes, the  $I/\emptyset$  time was less than five minutes.

Computer resource requirements for this problem are shown in figure 2, and dramatically illustrate the effect of spill on resource utilization. As long as memory region size is small enough to require spill,  $I/\emptyset$  volume and CPU time are steep inverse functions of open core (scratch memory) size and job cost (as measured by the CDC accounting algorithm) is decreased by increasing core. But once sufficient open core is provided to avoid spill, CPU and  $I/\emptyset$  utilization remain constant, and job cost increases with increasing memory size.

Real Symmetric Decomposition

The second problem chosen is the static analysis of a long, narrow orthotropic plate, based on NASTRAN Demonstration Problem 1-4-1 of reference 4. This problem is useful for study because data can be readily generated for a broad range of grid sizes. Problem sizes ranging from 128 to 1100 active columns were studied. (For a given memory region, spill is closely related to the number of active columns.) These were produced by grids of from 300 to 2100 points, generating matrices of order 760 to 4990, respectively.

A problem size of 277 average active columns, generated by a grid of 660 points, resulting in a matrix of order 1660 was selected for detailed investigation. This problem has spill characteristics typical of large user problems commonly analyzed using NASTRAN. The grid is comparatively small; however for problems of similar spill behavior, CPU and  $I/\emptyset$  resource utilization are linearly proportional to matrix order for a constant memory region.

Results for this case are shown in figure 3 in non-dimensional form, normalized to the conditions at the open core size where spill is no longer required. The outstanding feature of figure 3 is the  $I/\emptyset$  required by spill. At an open core size of 50% of that required for in-core reduction,  $I/\emptyset$  volume is seven times that required for in-core reduction. The CPU time curve illustrates that, refined as the symmetric decomposition spill logic is, considerable computer time is used processing spill  $I/\emptyset$ . And the cost curve shows that the cost penalty incurred by using more open core is more than compensated for by the reduced  $I/\emptyset$  and CPU resource requirements.

To lend perspective, a cost curve was developed for a typical UNIVAC 1110 system, where cost is directly proportional to memory used, and  $I/\emptyset$  is relatively less expensive. This curve is not as dramatic as the CDC curve, but still shows the importance of increasing open core to minimize spill.

### DYNAMIC MEMORY MANAGEMENT

When matrix decomposition dominates a NASTRAN problem, the foregoing discussion indicates that computer resource utilization can be minimized by requesting sufficient core to avoid spill, if possible. For typical problems, however, matrix decomposition is only part of the solution procedure. This is illustrated by the problem described in Table 1. The decomposition of the order 7000 matrix without spill would require a memory region of 160,000 decimal words on a CYBER 175, which is 30,000 words more than is available to a single program. But the decomposition step is only about 40% of the computational effort. Another 50% of the computation can be performed in 50,000 words core, and the remainder in 70,000.

This suggests that an ideal strategem to reduce computer costs would be to dynamically manage memory to give each module only the core it needs. Direct implementation of this idea would present a formidable task - 160 NASTRAN modules to be modified. However, the results presented in Table 1 indicate that most of these modules - input, sort, geometry processing, element matrix assembler and generator, etc; require a small memory region, and suggest the following three-phase memory management scheme.

(1) Execution of each module is attempted in a small memory region.

- (2) Modules which can be expected to have large memory requirements compute and request the needed core.
- (3) Any other module which runs out of core while executing has its memory region expanded to a predetermined intermediate size.

CDC IMPLEMENTATION OF DYNAMIC MEMORY MANAGEMENT

The dynamic memory management scheme described above is being implemented on the CDC CYBER 175 as follows.

- The user specifies to NASTRAN an initial and a nominal memory region size.
- (2) Before invoking each module, the link driver (XSEM) routine calls a subroutine MEMMGR (memory manager) to reset the memory region to its initial value.
- (3) The matrix decomposition routines call MEMMGR to obtain the open core needed to execute without spill. If insufficient memory exists, all available memory is obtained.
- (4) Modules that run out of open core normally issue an error abort call to subroutine MESAGE. This call is intercepted by MEMMGR, the nominal memory region is assigned, and control returned to the calling module. (Note that this requires that the call to MESAGE be an inline call).

This scheme is being tested using the cases of figures 1 and 2 and Table 1. The predicted cost savings are shown in figure 2. These cases indicate that dynamic memory management to avoid spill can reduce job costs significantly.

### CONCLUSION

An input/outout monitor was developed for the CDC version of NASTRAN which allows detailed analysis of computer resource utilization of the matrix decomposition modules. This analysis shows that for typical accounting algorithms, job costs can be reduced by avoiding spill in the decomposition. Analysis of a typical problem indicates that dynamic memory management could further reduce overall job cost.

#### REFERENCES

- 1. The NASTRAN Programmer's Manual, NASA SP-222(03), July, 1976.
- 2. The NASTRAN Theoretical Manual, NASA SP-221(03), March, 1976.

- Brown, W. K., and Schoellmann, W. F., "Study of the NASTRAN Input/Output Subsystems," <u>Sixth NASTRAN Users' Colloquium</u>, NASA CP-2018, October, 1977.
- 4. The NASTRAN Demonstration Problem Manual, NASA SP-224(03), July 1976.

## TABLE 1

## THERMAL STABILITY STUDY

## Order of Matrix = 7215 Average Active Columns = 238 Maximum Active Columns = 505 Three Spill Groups

Operation	CPU, seconds	I/O, 10 <sup>3</sup> PRU <sup>(1)</sup>	Memory Region (60 bit words)
Input Processing	49	16	52000
Geometry Processing	14	20	52000
Element Matrix Processing	140	81	52000
Constraint Elimination	183	25	52000
Decomposition	307	157	98000 <sup>(</sup> ~)
Static Solution Generation	70	81	66000
Totals	736	380	

- (1) One PRU = Sixty-four 60 bit words
- (2) The decomposition would require 160000 words without spill

## TABLE 2

# NASTRAN DYNAMIC MEMORY MANAGEMENT ON THE CYBER 175 EXPECTED RESOURCE UTILIZATION AND COST SAVINGS

Problem	Memory Region (10 <sup>3</sup> word)	CPU (seconds)	I/Ø (103pRU)(1)	Cost Savings (Percent)
Demo Problem 7-2-1	52 74	45.3 242.8	12.4 49.2	2.5%
Demo Problem 1-4-1	52 94	49.6 66.3	34.7 26.9	12.7%
Thermal Stability Study	52 66 98 <sup>(2)</sup>	386 70 307	142 81 157	14.3%

(1) One PRU = sixty-four 60 bit words

(2) The decomposition would require 160,000 words without spill

## ORIGINAL PAGE IS OF POOR QUALITY

105 RBHG2 END

VUUL      11      131      11      14      0        NT-AN      19      1134      60      19      0        NGGX      9      134      60      19      0        NGGX      9      134      9      0      0        SCRAICHI      3      30      9      0      0        SCRAICHI      3      30      9      0      0        SCRAICHI      3      30      9      0      0        SCRAICHI      2      20      10      2      0        SCRAICHI      2      20      10      2      0        SCRAICHI      2      20      10      2      0        SCRAICHI      40      13      4      0      0        SCRAICHI      5      1407      23      0      0        HDD. HUTAL      67      1407      13      0      0      0        SCRAICHI      3      14      9      2      0      0      0	FILE POSTIION O D D
SCRAICHA  999  16333  16  998  0    GRAICHI  2  13  9  4  0    KGAI  2703  9.741  16  572  0    SCRAICHA  6013  106537  16  5006  0    SCRAICHA  6013  106537  16  5006  0    SCRAICHA  10157  240131  16  5006  0    GRAND SUM  15167  240131  16  5006  0    III  SSGAI  FRANSFERRED  DATA IRANSFER  READ/WRITES  DPEN/CLUSE    YUUL  11  131  11  11  0  0    HT-LAN  19  133  6  0  0  0    CALL 22  PPCALLS  FRANSFERRED  DATA IRANSFER  READ/WRITES  DPEN/CLUSE    YUUL  11  131  10  0  0  0    CSCRAICH3  30  10  4  0  0    SCRAICH3  313  9  4  0  0    SCRAICH3  313  9  4  0  0    SCRAICH3  313  10  2  0  0    SCRAICH3  313 <td>0</td>	0
SCRAICHT      1	
NGGL  3783  9784  16  9786    SCRAICH3  5131  100517  16  5306  0    ADD. 10TAL  13351  226449  16  5306  0    GRAIND SUM  15167  240131  16	i
ADD.  TDTAL  LIG  LIG    GRAND SUM  13167  240131  16    111  SSG1  END    CALL  22  PRUS  AVERAGE    FILE  PPCALLS  TRANSFERED  DATA    JUUL  11  131  11    NT-XN  19  1324  0    AGGX  9  34  9    SCALTCHI  3  30  9    SCATCHI  2  20  13    SCATCHI  2  20  13    SCATCHI  2  20  14    SCATCHI  2  20  14    SCATCHI  3  16  9    SCATCHI  3  10  9    SCATCHI  3  10  9    SCATCHI  3  10  9    SCATCHI  3  10	. 0 7
GRAND SUN  15167  240131  16    111 SSG1  END    CALL 22  PRUS  AVERAGE    716E  PPCALLS  TRANSFERED  DATA TRANSFER  READ/VRITES  DPEN/CLDSE    700L  11  131  11  10  0    111  131  11  11  0    111  131  11  10  0    111  131  11  10  0    111  131  11  10  0    111  131  10  0  0    111  131  10  0  0    111  131  11  0  0    111  131  10  0  0    111  131  10  0  0    111  131  10  0  0    111  131  10  0  0    111  131  10  0  0    111  131  10  0  0    111  12  10  10  10    111  14  0  2  0    111  11  11  10  0    111	7
111 SSG1    END      CALL 22 FILE    PCALLS    PRUS TRANSFERED    AVERAGE DATA JRANSFER    READ/MRIJES    DPEN/CLDSE      VOUL NT-AN    19    1131    11	
111 SSG1      END        CALL 22      PCALLS      TRANSFERED      DATA JRANSFER      READ/WRIJES      DPEN/CLDSE        VOUL      Y      131      11      11      11      11        NT-AN      19      135      60      19      0        SGS7      9      6      0      0      0        SGS7      9      6      0      0      0        SGS7      9      6      0      0      0      0        SGS7      9      6      0      0      0      0      0        SGRATCH1      3      30      7      4      0      0      0        SCRATCH3      318      7      4      0      <	······································
CALL 22      PRUS FILE      AVERAGE TRANSFERRED      DATA JPANSFER      READ/VRIJES      DPEN/CLDSE        200L      11      131      11      11      11      0      17      0        AGGX      9      34      9      6      0      0      0        AGGX      9      34      9      6      0      0      0        CALL 20      9      34      9      6      0      0      0      0      0        CALL 21      0      0      10      4      0	· · · · · · · · · · · · · · · · · · ·
FILE      PPCALLS      TRANSFERRED      DATA TRANSFER      READ/WRITES      DPEN/CLOSE        VOUL      131      131      11      131      11      11        NT-AN      19      134      60      19      0        SGR      9      34      9      6      0        SGR      9      34      9      6      0        SGR      9      34      9      6      0        SGRATCHIA      3      30      7      4      0        SCRATCHIA      3      30      7      4      0        SCRATCHIA      3      30      7      4      0        SCRATCHIA      3      10      7      23      0      0        GRAND JUM      152.14      249730      16      MPYAONULL MATRIX PRODUCT      0      0        CALL 20      PRUS      AVERAGE      0      0      0      0        FILE      PPCALLS      TRANSFERKED      DATA TRANSFER      READ/WRITES      0      0	• • • •
GGG  9  34  9  6  0    SLJ  6  60  10  4  0    SCRATCHL  30  17  4  0    SCRATCHL  30  7  4  0    SCRATCHL  2  20  10  2    PG  2  10  2  0    SCRATCHL  67  1607  23    GRAND JUM  15214  249730  16    PUUL  9  2  0    FILE  PPCALLS  TRANSFERRED  DATA TRANSFER    PUUL  4  40  112    NTRAM  40  112  6    ASS  3  10  9    SCRATCHLA  3  10  9    SCRATCHLA <t< td=""><td>FILE POSITION</td></t<>	FILE POSITION
223 ECC  0  00  10  4  0    CASECC  5  10  10  4  0    SCRATCHL  3  10  7  4  0    SCRATCHL  5  10  7  4  0    SCRATCHL  67  10  2  0  0    PG  2  10  7  2  0    GRAND JUM  152.14  249730  16  10  7    GRAND JUM  152.14  249730  16  0  0    FILE  PPCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES  0PEN/CLUSE    FUOL  9  4  0  12  8  0  0    NTRAA  3  10  9  2  0  0    SCRATCHA  10  9  2  0  0    SCRATCHA  10  9  2  0  0    VEX  10  9  2  0  0    SCRATCHA	2
SCRATCHI  5  30  9  4  0    SCRATCHI  5  10  9  4  0    SCRATCHI  6  10  2  0  0    SCRATCHI  67  1007  23  0  0    GRAND JUM  152.14  249730  10  10    AUD.  101AL  67  1007  23  0    CALL 20  PRUS  AVERAGE  0  10  10    FILE  PCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES  0PEN/CLUSE    PUOL  9  5  10  10  9  2  0    NTRAM  10  10  9  2  0  0    NTRAM  10  9  2  0  0    NSS  3  10  9  2  0    NGCT  3  10  9  2  0    NGGX  3  10  9  2  0    NGGX  3	. Ŭ .
SCRATCH3  5  36  9  4  0    DGPD1  4  54  13  4  0    SIL  2  20  10  2  0    P6  2  18  9  2  0    P6  2  18  9  2  0    GRAMD 3UM  15234  249730  16  HYAONULL HATRIX PRODUCT    CALL 20  PRUS  AVERAGE  NUL HATRIX PRODUCT    FILE  PPCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES  OPEN/CLUSE    PUUL  9  4  0  10  4  0    NTRAM  3  18  9  2  0    SCRATCHA  1  18  9  2  0    SCRATCHA  1  18  9  2  0    SCRATCHA  1  10  9	0 1
Sil  2  20  10  2  0    PG  2  10  9  2  0    GRAND JUM  15214  249730  16  16    FILE  PPCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES    PUDL  9  40  10  4    WTRAA  0  10  4  0    NTRAA  0  10  4  0    SERATCHA  1  18  9  2  0    VUV  1  10  9  2  0    VUV  1  10  9  2  0    VS  1  10  9  2  0    VVV  1  10  9  2 <td< td=""><td>_ <u>1</u></td></td<>	_ <u>1</u>
HOD.  LOTAL  67  LOT  23    GRAND  JUM  LS214  249730  L6    HPYAONULL  HATRIX  PRODUCT    CALL  20  PRUS  AVERAGE    FILE  PPCALLS  TRANSFERRED  DATA  TRANSFER  READ/WRITES  OPEN/CLOSE    PUOL  4  40  10  4  0    NTRAN  4  10  112  6  0    NTRAN  4  10  9  2  0    NTRAN  10  9  2  0    NTRAN  10  9  2  0    NTRAN  10  9  2  0    Star  3  11  9  2  0    SCRATCHA  10  9  2  0    RGGX  3  16  9  2  0    VLV  3  16  9  2  0    VSS  3  10  9  2  0    VLV  3  10  9  2  0    VSS  3  10  9  2  0    VSS  3  10  9  2  0    NIBA	0 0
GRAND JUM  152.14  24.973.0  16    CALL 20  PRUS  AVERAGE    FILE  PPCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES  OPEN/CLUSE    PUOL  9  90  10  4  0  0    NTRAA  0  10  4  0  0  0    NTRAA  0  10  4  0  0    KSS  3  10  9  2  0    KSS  3  10  9  2  0    PG  3  18  9  2  0    KGGX  3  16  9  2  0    VV  1  10  9  2  0    VISET  3  16  9  2  0    HOD, TOTAL  49  1130	
CALL 20  PRUS  AVERAGE    FILE  PPCALLS  TRANSFERED  DATA TRANSFER  READ/VRTTES  OPEN/CLUSE    PRUL  4  0  10  4  0    NTRAM  4  112  6  0    NTRAM  4  112  6  0    NTRAM  4  112  6  0    NTRAM  4  97  12  6    NTRAM  4  97  2  0    SERATCHA  1  18  9  2  0    SERATCHA  1  14  9  2  0    NDICT  3  16  9  2  0    VV  3  16  9  2  0    VV  3  10  9  2  0    VV  3  10  9  2  0    VS  3  10  9  2    VS  3  113D	
PIDL  Q  Q  Q  Q  Q    NTRAA  A  A98  112  A  A    NTRAA  A  A98  2  O  O    SCRATCHA  A  A18  9  2  O    SCRATCHA  A  A18  9  2  O    NTRAA  A  A9  2  O  O    NTS  A  A18  9  2  O    VLV  A  10  9  2  O    VLV  A  10  9  2  O    VSET  J  10  9  2  O    NTAN  L52  271A98  AYERAGE  PEN/CLOSE    F1L5  PP	
PHOL  4  0  10  4  0  0    NTRAA  0  898  112  0  0  0    NTRAA  0  18  9  2  0    KSS  3  18  9  2  0    SCRATCHA  10  9  2  0  0    SCRATCHA  10  9  2  0    VUV  1  10  9  2  0    ULV  1  10  9  2  0    VSET  1  10  9  2  0    VSET  1  10  9  2  0    NTAL  43  1130  25  0    GRAND SUH  16523  271098  16  10    VITAL  13  152  76  15  0    NTRAN	
KELH    3    16    9    2    0      KSS    3    10    9    2    0      SCRATCHA    2    10    9    2    0      KGGX    3    16    9    2    0      KGGX    3    16    9    2    0      KGGX    3    16    9    2    0      VLV    3    10    9    2    0      VSS    3    10    9    2    0      VSS    3    10    9    2    0      MOD. TOTAL    49    1130    25    0    1130      I37 SDR2    END    1130    25    0    0      I37 SDR2    END    1130    2    0    0      I37 SDR2    END    1152    76    15    0 <td>FILE POSITION</td>	FILE POSITION
SCRATCHA  SCRAT	
PG  1  1H  9  2  0    XDICT  3  1A  9  2  0    XGGX  1  1A  9  2  0    XGGX  1  1A  9  2  0    YS  3  10  9  2  0    VLV  3  10  9  2  0    VS  3  10  9  2  0    VS  3  10  9  2  0    VST  3  10  9  2  0    KFS  3  16  9  2  0    HDOL YOTAL  49  133  271498  16    I37 SDRZ  END  1136  2  0    CAUL 29  PRUS  AVERAGE  READ/WRITES  0PEN/CLOSE    POQL  4  60  10  4  0    NTRAN  15  1152  76  15  0    NTRAN  15  1152  76  <	······································
KGGX  1  1  1  1    PS  1  16  9  2  0    ULV  1  10  9  2  0    VS  3  10  9  2  0    USET  3  10  9  2  0    VST  1130  25  0  0    RAND SUH  16523  271898  16  16    VST  STSDR2  END  10  4  0    VST  STSDR2  END  10  4  0    NTRAN  15  1152  76  15  0    NTRAN  15  1152  76  15  0    KELA  A  18  9  2  0    SCRATCH6  3  18  9  2	
ULV  1  10  9  2  0    YS  1  10  9  2  0    USET  1  10  9  2  0    WGO. YOTAL  49  1136  25  0    GRAND SUM  16523  271898  16    I37 SDR2  END  16  1    I37 SDR2  END  16    VALL  29  PRUS  AVERAGE    F1LE  PPCALLS  TRANSFERRED  DATA TRANSFER    READ/WRITES  OPEN/CLOSE    POQL  4  0    NTRAN  15  1152    T6  15  0    KELM	
USET  J  10  9  2  0    NFS  J  10  9  2  0    NOO. TOTAL  49  1136  25    GRAND SUH  1623  271898  16    L37 SDR2  END  16    CALL 29  PRUS  AVERAGE    F1LE  PPCALLS  TRANSFERRED  DATA TRANSFER    READ/WRITES  OPEN/CLOSE    POQL  4  0    NTRAN  15  1152    READ  16  9    READ  0    NTRAN  15  1152    READ  9  2    QCALCA  4  0    NTRAN  15  1152    READ  9  2    QCALCA  4  0    NTRAN  15  10    NTRAN  15  0    NTRAN  15  0    RES  3  18    9  2  0    SCRATCH6  3  18    9  2  0    KDICT  7  22  0	1
KFS  3  16  9  2  0    MOD. YOTAL  49  113A  25  0    GRAND SUM  16523  271898  16    L37 SDR2  END  16    CALL 29  PRUS  AVERAGE    F1LE  PPCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES  OPEN/CLOSE    POQL  4  0  10  4  0    NTRAN  15  1152  76  15  0    KELM    9  2  0    KSS  3  18  9  2  0    SCRATCH6  3  18  9  2  0    K01C1  7  52  10  5  0	
GRAND SUM  16523    L37 SDR2  END    CALL 29  PRUS    FILE  PPCALLS    TRANSFERRED  DATA TRANSFER    READ/WRITES  OPEN/CLOSE    POOL  4    40  10	ī
L37 SDR2    END      CALL 29    PRUS    AVERAGE      FILE    PPCALLS    TRANSFERRED    DATA TRANSFER    READ/WRITES    OPEN/CLOSE      POOL    4    0    10    4    0      NTRAN    15    1152    T6    15    0      KELM      18    9    2    0      KSS      18    9    2    0      SGAATICH6      18    9    2    0      K01C1	·····
L37 SDR2      END        CALL 29      PRUS      AYERAGE        FILE      PFCALLS      TRANSFERRED      DATA      TRANSFER      READ/WRITES      OPEN/CLOSE        POOL      4      40      10      4      0        NTRAN      L5      1152      76      15      0        NTRAN      L5      1152      76      15      0        KELM       18      9      2      0        KSS      3      18      9      2      0        READ/WRITES      0      15      0         KELM       18      9      2      0        KOLCI      7      52      10      5      0	· · · · · · · · · · · ·
CALL 29  PRUS  AVERAGE    FILE  PPCALLS  TRANSFERRED  DATA TRANSFER  READ/WRITES  OPEN/CLOSE    POOL  4  0  10  4  0    NTRAN  L5  1152  76  15  0    KELM  .3  .18  9  2  0    KSS  .3  .18  .9  2  0    SCRATCH6  .3  .18  .9  .2  0    KDLCT  .7  .52  .10  .5  0	
KSS  1  18  9  2  0    SCRATCH6  3  18  9  2  0    PG  3  18  9  2  0    KDICT  7  52  10  5  0	
KSS  1  18  9  2  0    SCRATCH6  3  18  9  2  0    PG  3  18  9  2  0    KDICT  7  52  10  5  0	FILE POSITION
KSS  1  18  9  2  0    SCRATCH6  3  18  9  2  0    PG  3  18  9  2  0    KDICT  7  52  10  5  0	
SCRATCHO  3  10  4  2  0    PG  3  10  3  2  0    κθ1ct  7  52  10  5  0	ang tana si anang kanang katalan 🗛 sa sa kanang ka
PG	
KGGX 190 7191 16 196 0	· · · <u>1</u> ·
	2
	<b>.</b>
YS . 9 84 12 7 0 USET 3 18 9 2 .0	2
	ĩ
10 <u>1</u> 19H	
EST 19 309 16 19 0 EVEXIN 7 91 13 7 0	0
KLL 2 20 10 2 0	Ō
UGV 8 108 13 8 0 809. TOTAL 311 5389 17	0
GRAND SUH 10834 277247 16	بالمحمور بالانتها

Figure 1. Output from the NASTRAN I/Ø Monitor (typical).

21

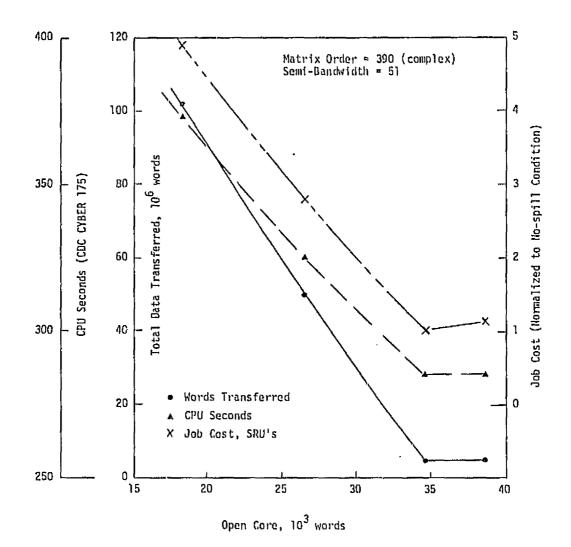
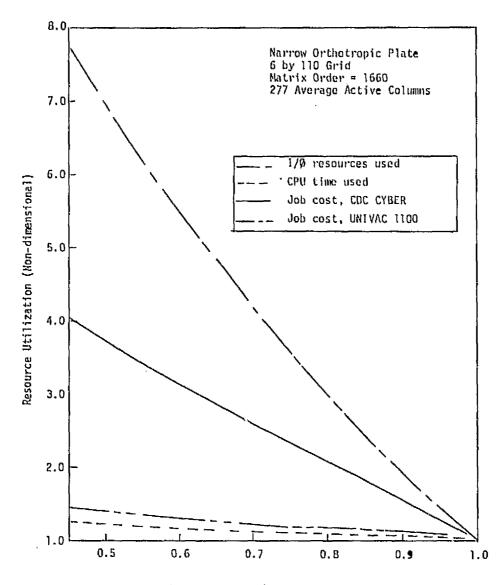


Figure 2. Resource Analysis vs. Open Core Eigenvalue Analysis of a Thin Elastic Cylinder.

# ORIGINAL PAGE IS OF POOR QUALITY



Open Core Size (Non-dimensional)

Figure 3. Resource Utilization for Symmetric Decomposition Normalized to No-spill Values.