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# **NASA Contractor Report 145362**

**A COMPUTER PROGRAM FOR CALCULATING AERODYNAMIC  
CHARACTERISTICS OF LOW ASPECT-RATIO WINGS WITH  
PARTIAL LEADING-EDGE SEPARATION**

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**Langley Research Center**  
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### LIST OF SYMBOLS

<u>Symbols</u>	<u>Description</u>	<u>Dimensions</u>
b	Wing span	m (ft)
c	Local chord	m (ft)
$C_R$	Root chord	m (ft)
M	Number of spanwise strips plus one	
N	Number of bound elements	
x,y,z	Wing rectangular coordinate system with x in the streamwise direction and y to the right	m (ft)
<u>Greek</u>		
$\alpha$	Angle of attack	deg
<u>Subscripts</u>		
cp	Control point	
i	Chordwise bound element number	
j	Spanwise strip number	
k	Chordwise bound element number	
$\ell$	Leading-edge	

## 1. INTRODUCTION

This document describes in detail the necessary information for using a computer program to predict distributed and total aerodynamic characteristics for low aspect-ratio wings with partial leading-edge separation. This program is based on the numerical method developed in reference 1. The flow is assumed to be steady and inviscid. The wing boundary condition is formulated by the Quasi-Vortex-Lattice method. The leading-edge separated vortices are represented by discrete free vortex elements which are aligned with the local velocity vector at mid-points to satisfy the force free condition. The wake behind the trailing-edge is also force free. The flow tangency boundary condition is satisfied on the wing, including the leading- and trailing-edges.

The program is restricted to delta wings with zero thickness and no camber. It is written in Fortran language and runs on CDC 6600 Computer.

## 2. COMPUTER PROGRAM DESCRIPTION

### 2.1 PROBLEM DEFINITION

In steady symmetric flight at a high angle of attack, the flow over a thin low aspect-ratio highly sweptback wing separates along the leading-edge and the tips. In the following, only delta wings are considered. The wing can be represented by a bound vortex sheet, across which there exists a pressure difference, and the separated flow along leading-edges by force free vortex sheets, across which there is no pressure difference. In the present method, the Quasi-Vortex-Lattice method (reference 2) is used to simplify the induced velocity expressions due to the bound vortex sheet and discrete force free vortex elements for separated vortex sheets. The following boundary conditions are imposed on the flow model:

- a. The flow must be tangential to the wing surface.
- b. The leading-edge boundary condition and the trailing-edge Kutta condition are to be satisfied.
- c. The vortex elements over the wing and wake behind the trailing-edge are force free.

This is a non-linear problem because the strengths of the wing bound vortices and free vortices, and the locations of the free vortex elements are unknown. Thus, the problem is solved by an iterative method.

### 2.2 PROGRAM CAPABILITIES

This computer program provides a theoretical method for determining the aerodynamic characteristics of low aspect-ratio thin delta wings without camber, with partial leading-edge separation. The following is a list of the aerodynamic characteristics the program calculates:

- a. Spanwise and chordwise  $\Delta C_p$  distributions

- b. Spanwise distribution of sectional lift, induced-drag and pitching moment coefficients.
- c. Total lift, induced-drag, pitching-moment and leading-edge thrust coefficients.

### 2.3 GEOMETRY DESCRIPTION

The origin of the rectangular coordinate system is at the wing apex. The wing lies in the x-y plane and the x-axis is taken along the wing center-line. The wing span is given by b and the surface area S.

#### 2.3.1 WING GEOMETRY

The location of bound- and trailing-vortex elements for a typical case are shown in figure 1. The x-location of bound elements is given by the cosine law and is illustrated in figure 1.

$$x_i = x_l + \frac{c}{2} (1 - \cos(\frac{2i-1}{2N} \pi)), \quad (1)$$

$$i = 1, 2, \dots, N$$

where  $x_l$  is the leading-edge x-coordinate, c is the chord and N is the number of bound elements in a chordwise direction. The spanwise location of trailing elements is given by,

$$y_j = \frac{b}{4} (1 - \cos(\frac{2j-1}{2M} \pi)), \quad (2)$$

$$j = 1, 2, \dots, M$$

where b is the span and M is the number of legs of trailing vorticity, which is one higher than the number of spanwise strips of bound elements. The locations of control points are given by,

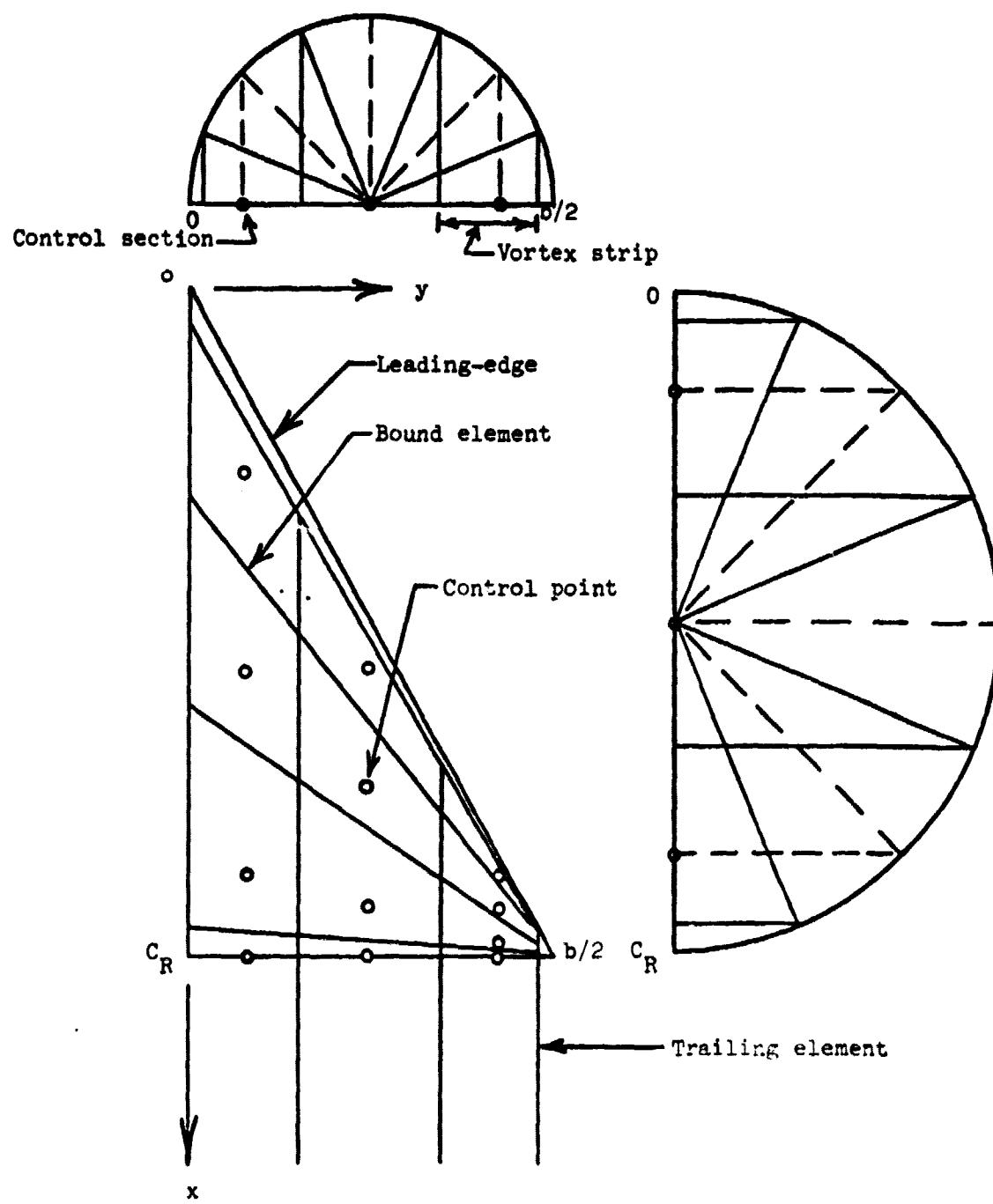


Figure 1. Wing geometry without leading-edge vortex system

$$x_{cp_k} = x_{l_j} + \frac{c_j}{2} (1 - \cos(\frac{\pi k}{N})) , \quad (3)$$

$$k = 0, 1, 2, \dots, N$$

$$y_{cp_j} = \frac{b}{4} (1 - \cos(\frac{\pi j}{M})) , \quad (4)$$

$$j = 1, 2, \dots, (M - 1)$$

where  $x_{l_j}$  and  $c_j$  are the leading-edge x-coordinate and chord at  $y_{cp_j}$  respectively.

It has been found numerically that the aerodynamic characteristics depended on the number of spanwise strips, i.e. M of equation (2). Therefore, a parametric study has been made to find a relation between the aspect ratio and the number of spanwise strips for reasonably accurate results (Fig. 2) (Section 3 of ref. 1). It is to be noted that as the aspect ratio is decreased, the number of spanwise strips has to be increased. This is due to the fact that the spanwise variation of aerodynamic characteristics, such as pressure coefficient and thrust coefficient, is large for small aspect ratio wings. This study was performed by matching the lift coefficients obtained by using the present method to those obtained by using suction analogy (ref. 3) at one angle of attack.

### 2.3.2 LEADING-EDGE VORTEX SYSTEM GEOMETRY

The leading-edge vortex system is superimposed on the regular quasi-vortex-lattice grid. A typical vortex element is shown by points A through J in figure 3. These points are connected by a series of short straight segments. The initial location of these segments is shown by dashed lines and final

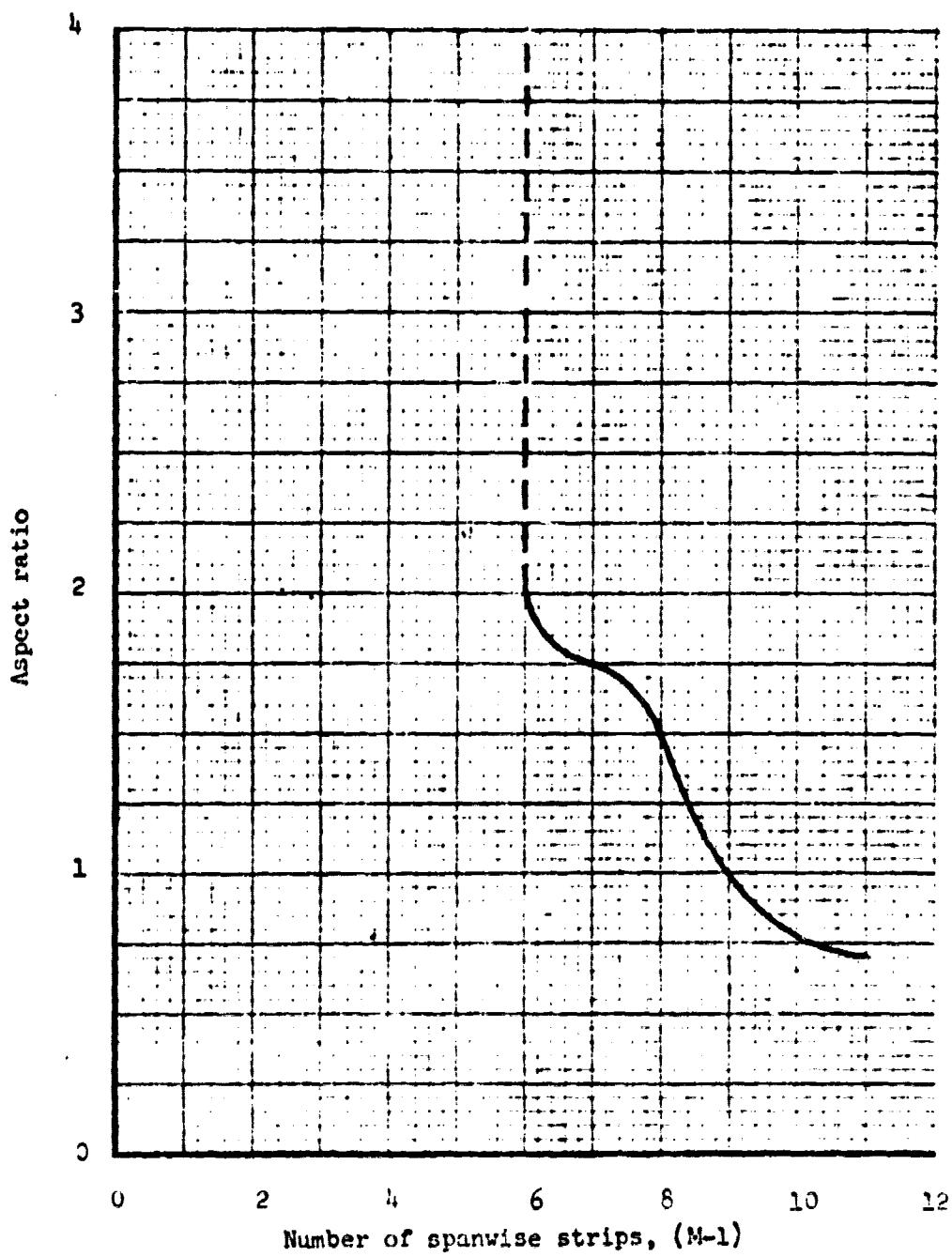


Figure 2. Variation of number of spanwise strips with aspect ratio

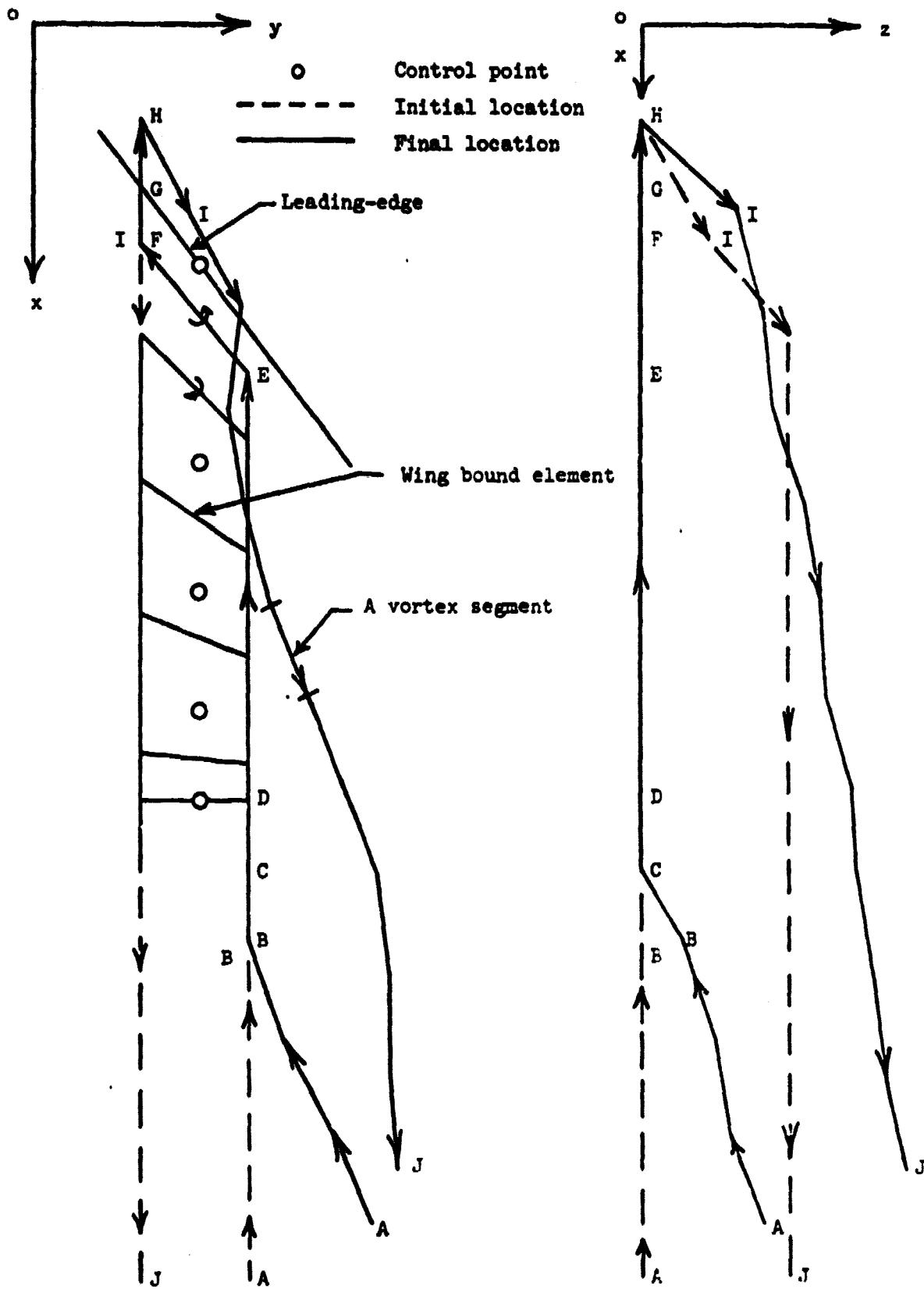


Figure 3. A typical vortex element of leading-edge vortex system

location by solid lines. These segments have the following characteristics;

- a. Points A through E lie along a wing trailing vortex element.

Initially point A is one root chord away from the trailing-edge in the downstream direction and the line segments between A and D are parallel to the axis of symmetry. The line segments between points A and B are of equal length. In the final converged position these segments are aligned in the direction of the local velocity vector. The segments B-C and C-D are  $0.1 C_R$  long. B-C is allowed to move only in the vertical direction whereas C-D is fixed in the wing plane because the flow is tangential to the trailing-edge.

Segment D-E is also fixed in the wing plane.

- b. Points E, F, G and H also lie in the wing plane. The location of segment E-F is ahead of the wing first bound element and is given by,

$$x_E = x_{l_E} + \frac{c_E}{2} \left(1 - \cos\left(\frac{\pi}{2(N+1)}\right)\right) \quad (5.a)$$

$$x_F = x_{l_F} + \frac{c_F}{2} \left(1 - \cos\left(\frac{\pi}{2(N+1)}\right)\right) \quad (5.b)$$

where the subscripts E and F refer to the points under consideration. The above two equations are similar to equation (1). It is to be noted that segment E-F is located at the first bound element for a grid of  $(N+1)$  bound elements in a chordwise direction. The segments F-G and G-H are of the same length and point G lies on the leading-edge. The segment G-H is fixed in the wing plane due to the leading-edge boundary condition.

c. The initial location of point I is given by,

$$x_I = x_F \quad (6.a)$$

$$y_I = y_F \quad (6.b)$$

$$z_I = 0.1 C_R \tan(22.5 - 0.5\alpha) \text{ for } \alpha \leq 15^\circ \quad (6.c)$$

$$\text{or } z_I = 0.1 C_R \tan \alpha \quad \text{for } \alpha > 15^\circ \quad (6.d)$$

where  $C_R$  is the root chord and  $\alpha$  is the angle of attack.

Initially point J is one root chord away from the trailing-edge.

The segments between point I and J are of equal length and lie in a plane parallel to x-z plane. These segments are approximately at a height of  $0.1 \cdot C_R$  above the wing plane. In the final converged position all the segments between points H and J are aligned in the direction of the local velocity vector.

d. The semi-infinite segments from points A to infinity and J to infinity are straight and are parallel to the undisturbed free-stream direction.

#### 2.4 SOLUTION PROCEDURE

The basic unknowns of the problem are the bound vortex density on the wing, and the strengths and the locations of the elements of the leading-edge vortex system and the wake. The problem is nonlinear because the locations of the leading-edge vortex system and the wake are unknown a priori. Therefore, the problem is solved by the iterative process described below;

- a. Prescribe the vortex lattice for the wing surface, and the initial locations of the free elements over the wing and in the wake.
- b. By satisfying the wing boundary condition, obtain the bound vortex density of the wing and the strengths of free elements.
- c. Calculate all the aerodynamic characteristics.
- d. Calculate the forces acting on the free elements over the wing surface.
- e. Adjust the free elements of the leading-edge vortex system and the wake in the local velocity vector direction.
- f. Repeat steps b through e until a converged solution is obtained.

The initial locations of the free vortex elements are assumed by letting them leave the leading-edge in the undisturbed free-stream direction up-to a height of about ten percent of the root chord beyond which the elements are parallel to the wing plane. Initially, all the elements of the wake lie in the plane of the wing. In the iteration process, the force free condition is satisfied on the free elements from the root to the tip in the down-stream direction. The elements over the wing are adjusted before the elements of the wake. In the first iteration the segments over the wing are moved 100 percent according to the velocity computed at their mid-points. This movement is gradually reduced in steps of 90, 80 and 75 percent in the next three iterations, after which it remains at 75 percent (Section 2.5.2 of ref. 1). The segments in the wake are moved only 50 percent in each iteration. Thus, exact force free condition is not enforced because whenever the free elements come close to each other they induce unreasonably large velocities because viscous effects are not included in the present theory. These large velocities increase the forces on the segments and induce fluctuations in their locations.

The solution is assumed to have converged if in two consecutive iterations the difference between the total strengths of leading-edge free vortex elements is less than one percent and the absolute force acting on the free elements is in the neighborhood of a minimum. Thus, an exact force free condition is not enforced as discussed in the previous paragraph.

### **3. INPUT DATA FORMAT**

The following is the description of input data cards for this program.

#### **Card 1. Format (16A5)**

TTL            Any title identifying the case to be run. END in first  
               three columns terminates the job.

#### **Card 2. Format (6I5)**

NCW            Number of chordwise lines (limited to nine)

NSW            Number of spanwise lines (one higher than number of  
               spanwise strips of panels, limited to twenty). It  
               depends on aspect-ratio and is determined by using  
               figure 2.

NBRR           Number of constant x-locations where  $\Delta C_p$ 's are to be  
               interpolated (limited to twenty-five).

NCONTS        = 0, Initial locations of free elements will be  
               calculated in the program.

               = 1, Initial locations of free elements will be read  
               from data cards.

MITER          Maximum number of iterations to be performed  
               (usually between 10 and 15)

IPUNCH        = 0, Coordinates of free elements will not be punched  
               out after last iteration.

               = 1, Coordinates of free elements will be punched out  
               after last iteration.

#### **Card 3. Format (6F10.5)**

XXL(1)        Leading-edge x-coordinate of the root chord.

XXT(1)	Trailing-edge x-coordinate of the root chord.
YL(1)	y-coordinate of the root chord
XXL(2)	Leading-edge x-coordinate of the tip chord.
XXT(2)	Trailing-edge x-coordinate of the tip chord.
YL(2)	y-coordinate of the tip chord.

Card 4. Format (7F10.5)

ALPHA	Angle of attack (in degrees).
AMACH	Mach number.
DELTA	Length of a segment of leading-edge free vortex elements (may be taken as $0.15 C_R$ ).
DL	Length of a segment of wake elements (may be taken as $0.15 C_R$ ).
XEND	x-coordinate beyond which free elements of leading-edge and wake system are represented by a single element going to infinity.
CBAR	Reference chord.
AREA	Total reference wing area.

Card 5. Format (8F10.5)

XBRR(I),	Constant x-locations where
I = 1, NBRR	$\Delta C_p$ 's are to be interpolated.

Card 6. Format (8F10.5)

CTT(I),	Sectional leading-edge thrust coefficients for
I = 1, (NSW-1)	spanwise strips. All these values are set equal to zero for complete leading-edge separation.

\*\*\* If NCONTS = 0, go back to card number 1 \*\*\*

**Card 7. Format (10I2)**

NELM(I), One higher than the number of segments for each leading-edge free vortex element (numbered from root to tip).  
I = 1,(NSW-1) edge free vortex element (numbered from root to tip).

**Card 8. Format (8F10.5)**

XE(K) x-coordinates of the end-points of segments of Ith  
K = 1,NELM(I) leading-edge free vortex element.

**Card 9. Format (8F10.5)**

YE(K), y-coordinates of the end-points of segments of Ith  
K = 1,NELM(I) leading-edge free vortex element.

**Card 10. Format (8F10.5)**

ZE(K) z-coordinates of the end-points of segments of Ith  
K = 1,NELM(I) leading-edge free vortex element.

\*\*\*Cards 8 thru 10 are repeated (NSW-1) times.\*\*\*

**Card 11. Format (10I2)**

NNELM(I), One higher than the number of segments for each wake  
I = 1,NSW element (numbered from root to tip).

**Card 12. Format (8F10.5)**

XXE(K) x-coordinates of the end-points of segments of Ith  
K = 1,NNELM(I) trailing wake element.

**Card 13. Format (8F10.5)**

YYE(K) y-coordinates of the end-points of segments of Ith  
K = 1,NNELM(I) trailing wake element.

**Card 14. Format (8F10.5)**

ZZE(K), z-coordinates of the end-points of segments of Ith  
K = 1,NNEM(I) trailing wake element.

\*\*\* Cards 12 thru 14 are repeated NSW times.\*\*\*

\*\*\* Go back to card number 1.\*\*\*

Note: The punched data cards obtained by running this program with IPUNCH = 1,  
can be directly used for cards 7 thru 14 for further iterations.

#### 4. OUTPUT DATA FORMAT

All the input data cards for each case are listed at the beginning of the output. The output data at each iteration step is as follows:

The title card (input data card number 1) is printed-out as it is inputted. The angle-of-attack (in degrees), Mach Number and iteration number are also listed. The end-point locations of the leading-edge free elements are listed next. The first row of numbers in each group are the x-coordinates, second row the y-coordinates and third row the z-coordinates. The end-point locations of the wake elements are listed in the similar manner. On the next two pages, x-y and y-z digital plots for leading-edge free-elements are made. It is to be noted that the leading-edge elements lying in the plane of the wing and along center line are not plotted. So, the elements next to the center line are represented by "1". When similar numbers are connected by straight lines, they represent the path of a free vortex element. A "+" sign represents a duplicate point. In these two plots there are (NSW-2) rows of free elements. The digital plots for wake elements are made on next two pages. The elements along center line are again not plotted. There are (NSW-1) elements.

Some of the intermediate variables are listed under following labels:

X/C	Percent chord location
2Y/B	Percent span location
GAMAY	Bound vortex density over the wing ( $\gamma_y$ ) at the given (X/C, 2Y/B)
CAPGAMA	Strength of leading-edge free element ( $\Gamma$ ) at the given 2Y/B
DELTA-CP	The total $\Delta C_p$ at the given (X/C, 2Y/B)

The sectional properties are listed under the following labels:

I	Spanwise station number (numbered from root to tip)
CLI	The sectional lift coefficient
CMI	The sectional pitching moment coefficient about the y-axis
CDI	The sectional induced drag coefficient
CTI	The sectional leading-edge thrust coefficient.

The total lift, pitching moment, induced drag and leading-edge thrust coefficients are listed after sectional properties. The spanwise pressures at constant x-locations are listed under following labels:

Y	y-coordinate
2Y/B(LOCAL)	Percent span location based on local span
DELTA-CP	The total $\Delta C_p$ at the given (x,y)

The last item listed for each iteration is the absolute force acting on leading-edge free elements.

The last page of the output is the "Summary Sheet", which is used to pick up final converged solution. It has the following format:

The title (input data card number 1) is printed again. The angle of attack (in degrees) and Mach Number are also listed. The other variables listed are,

ITERATION	Iteration number
CL	The total lift coefficient
CM	The total pitching moment coefficient about y-axis
CD	The total induced drag coefficient
CT	The total leading-edge thrust coefficient
GMSUM	Total sum of the strengths of leading-edge free vortex elements, except the one at the center line.

PERR	Percent change in GNSUM values of two consecutive iterations
TFARS	Total absolute force acting on leading-edge free elements

This program has not yet been completely automated and the converged solution is to be picked by the user, from the Summary Sheet, by using the following criteria:

The solution is assumed to have converged if in two consecutive iterations the difference between the total strengths of leading-edge free vortex elements is less than one percent and the absolute force acting on the free elements is in the neighborhood of a minimum.

## **5. REFERENCES**

1. Mehrotra, S. C. and Lan, C. E., "A Theoretical Investigation of the Aerodynamics of Low-Aspect-Ratio Wings with Partial Leading-Edge Separation", NASA CR-145304, January 1978.
2. Lan, C. E., "A Quasi-Vortex-Lattice Method in Thin Wing Theory", Journal of Aircraft, Vol. 11, No. 9, pp. 518-527, Sept. 1974.
3. Lamar, J. E. and Gloss, B. B., "Subsonic Aerodynamic Characteristics of Interacting Lifting Surfaces with Separated Flows around Sharp Edges Predicted by a Vortex Lattice Method", NASA TN D-7921, Sept. 1975.

## 6. APPENDICES

### 6.1 APPENDIX A: EXAMPLE INPUT AND OUTPUT

The following is an example of delta wing of aspect-ratio 2 at an angle-of-attack of 30 degrees. The flow is assumed to be completely separated from the leading-edge and so sectional leading-edge thrust coefficients are set to zero on card number 6. Listing of input data cards is given below:

#### Listing of Input Data Cards

CARD NUMBER	COLUMN NUMBER									
	1	2	3	4	5	6	7	8	9	10
1	ASPECT RATIO = 2.0									
2	0.	7.	5.	0.	10.	0.				
3	0.	4.	5.	0.	4.	4.	2.			
4	30.	0.	0.	0.6	0.6	7.5	2.			
5	1.	8.	5.	1.	3.5	3.75				
6	0.	0.	0.	0.	0.	0.	0.			
7	END									

Output data is listed on the following pages. An inspection of the "Summary Sheet" suggests that the converged solution has been reached at 8th iteration.

**INPUT DATA CARDS**

ASPECT RATIO = 2.0

6	7	5	0	10	0
0.00000	4.00000	0.00000	4.00000	4.00000	2.00000
30.00000	0.00000	6.00000	6.00000	7.50000	2.00000
1.00000	2.00000	3.00000	3.50000	3.75000	0.00000
0.00000	0.00000	0.00000	0.00000	0.00000	0.00000

FND OF INPUT DATA

ORIGINAL PAGE IS  
POOR QUALITY

ASPECT RATIO = 2.0 MACH NUMBER = 0.000 ITERATION NUMBER = 0

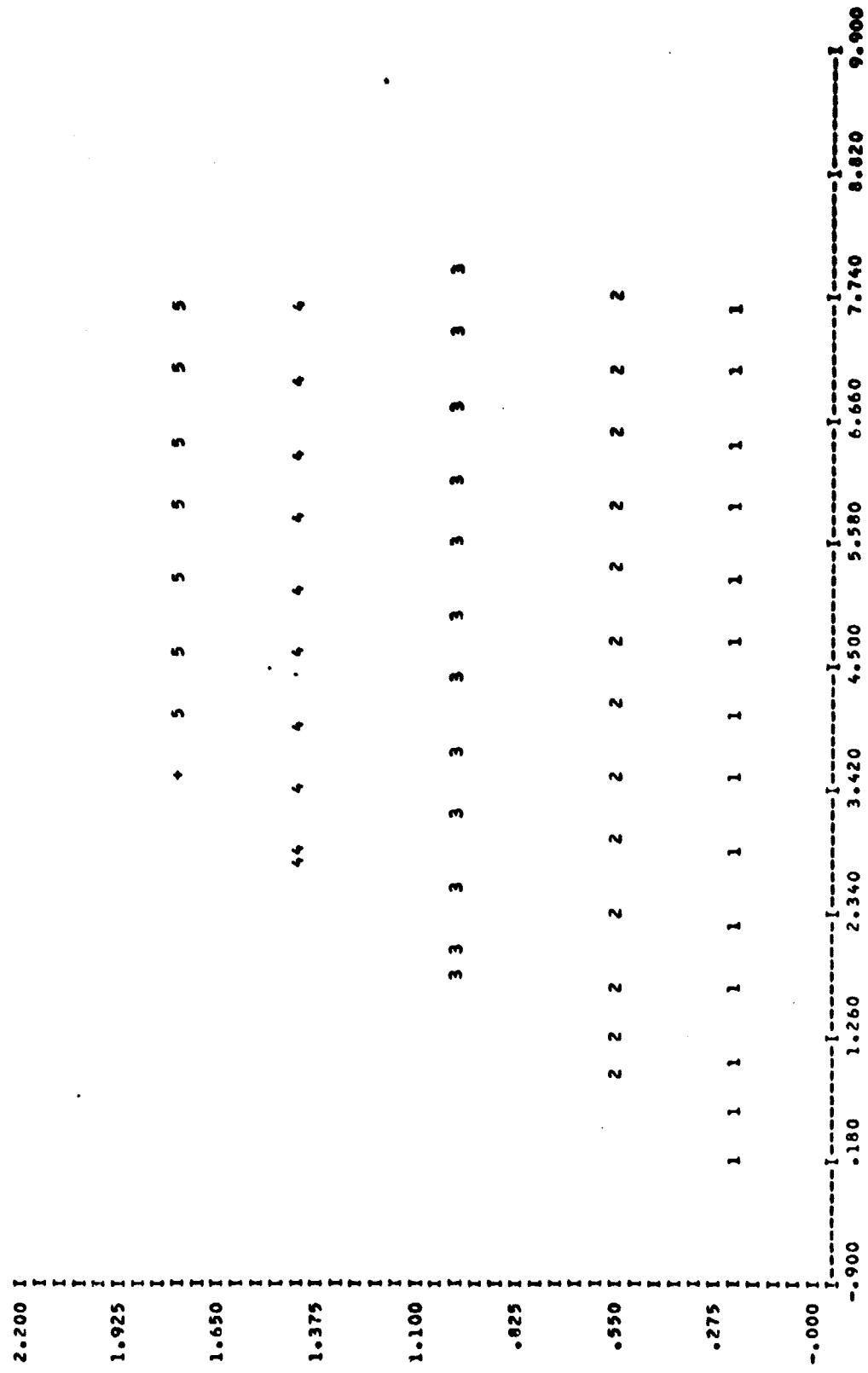
LEAVING EDGE ELEMENTS

22

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SHAKE ELEMENTS

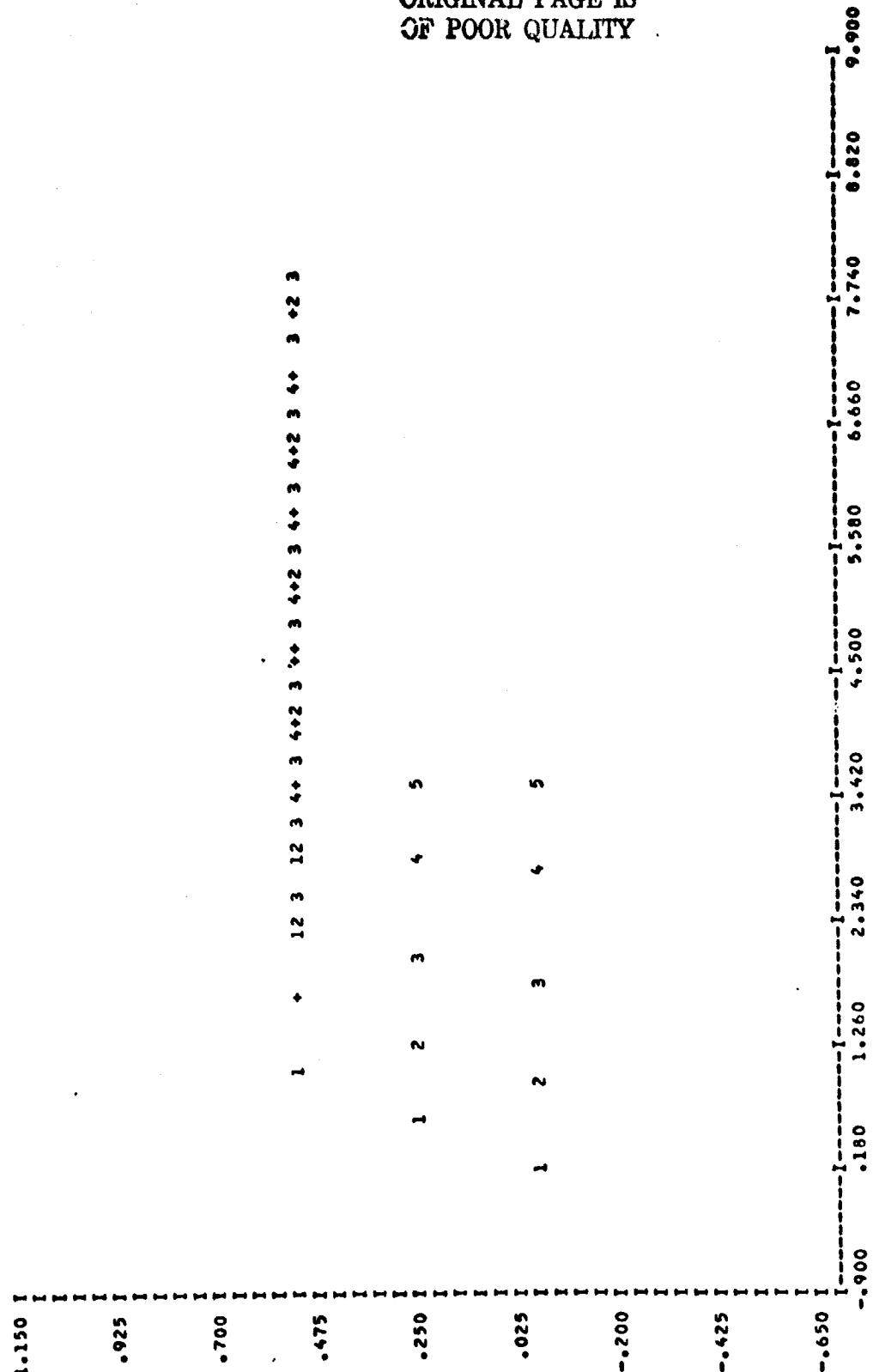
X VS Y (LEADING-EDGE ELEMENTS)



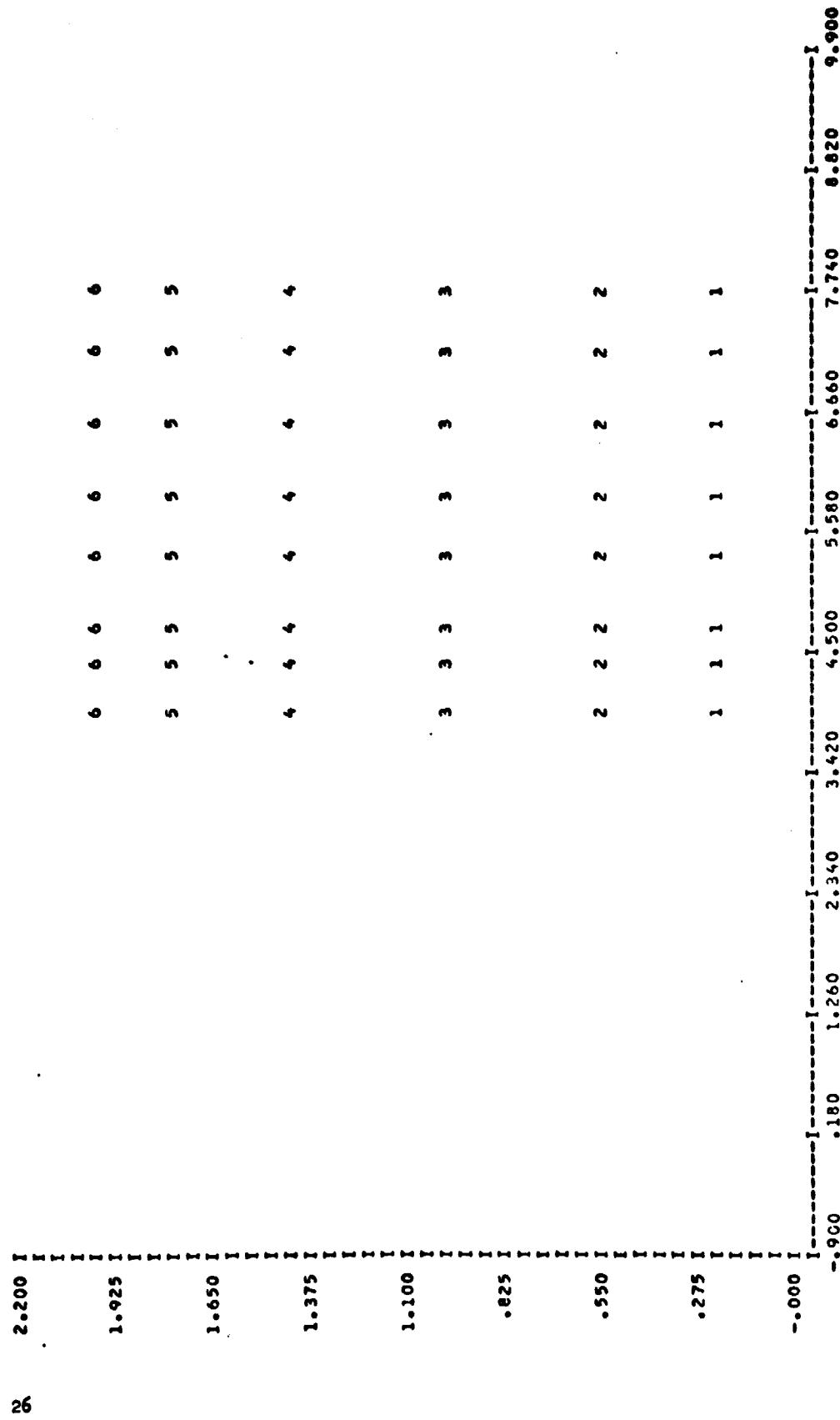
25

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OF POOR QUALITY

X VS Z (LEADING-EDGE ELEMENTS)

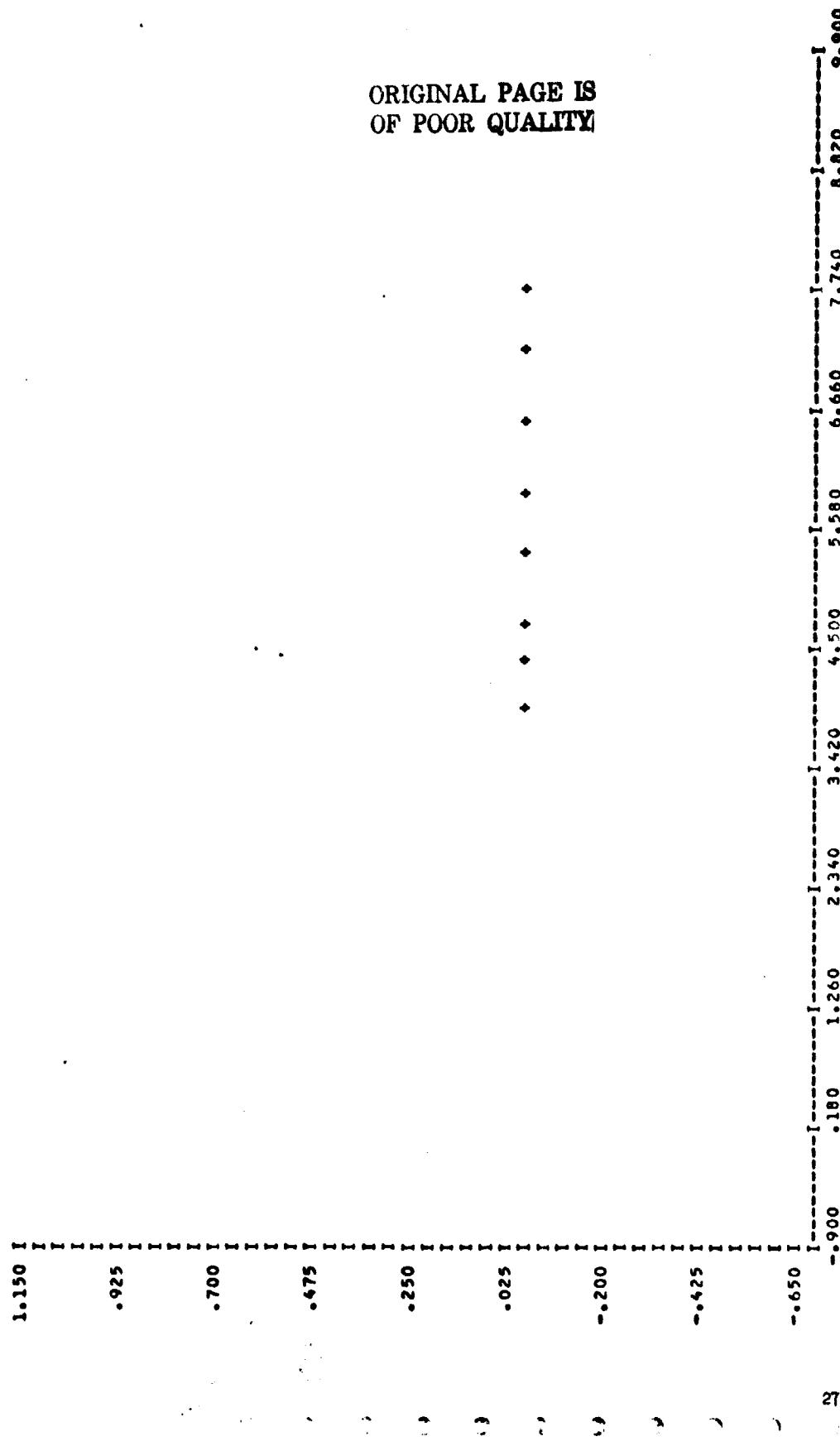


X VS Y (WAKE ELEMENTS)



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X VS TIME ELEMENTS)



## LEADING-EDGE OPTIMISTICS

2Y/8 CAPGAMA

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\*\*\*\*\*  
\* \* \* \* \*  
.04952 1.59529  
.040 1.00432  
.18826 .89376  
.38974 .71560  
.61126 .46288  
.81174 .18600  
.95048

30

DOELTA-CP OISTRIEUNIC

SECTIONAL PROPERTIES

	CLI	CMI	CDI	CTI
*	***	***	***	***
1	1.92967	-1.25424	1.11352	0.00000
2	1.70269	-1.71973	.98305	0.00000
3	1.62912	-2.27566	.94057	0.00000
4	1.22177	-2.08599	.70539	0.00000
5	.98222	-1.95844	.56708	0.00000
6	.79862	-1.77019	.46108	0.00000

TOTAL LIFT COEFFICIENT = 1.55805  
 TOTAL PITCHING MOMENT COEFFICIENT = -1.83185  
 TOTAL DRAG COEFFICIENT = .89954  
 TOTAL THRUST COEFFICIENT = 0.00000

SPANWISE PRESSURES AT CONSTANT X = 1.00000  
 Y 2Y/B(LOCAL) DELTA-CP  
 •09903 •09903 1.55729  
 •37651 •37651 1.55929  
 •77748 •77748 2.62486

SPANWISE PRESSURES AT CONSTANT X = 2.00000  
 Y 2Y/B(LOCAL) DELTA-CP  
 •09903 •06602 0.54461  
 •37651 •25101 1.11094  
 •77748 •51832 1.37594  
 1.22252 •81501 1.05633

SPANWISE PRESSURES AT CONSTANT X = 3.00000  
 Y 2Y/B(LOCAL) DELTA-CP  
 •09903 •05659 •50101  
 •37651 •21515 •89194  
 •77748 •44427 1.22321  
 1.22252 •69858 •98009  
 1.62313 •92771 1.03461

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OF POOR QUALITY

SPANWISE PRESSURES AT CONSTANT X = 3.75000  
Y 2Y/A(LOCAL) DELTA-CP

* .09903	* .05282	* .79304
* .37651	* .20081	* .86444
* .77748	* .41466	* .91482
* 1.22252	* .65201	* .73136
* 1.62149	* .86596	* .59463

TOTAL ABSOLUTE FORCE ACTING ON LEADING-EDGE FREE ELEMENTS = 1.28618

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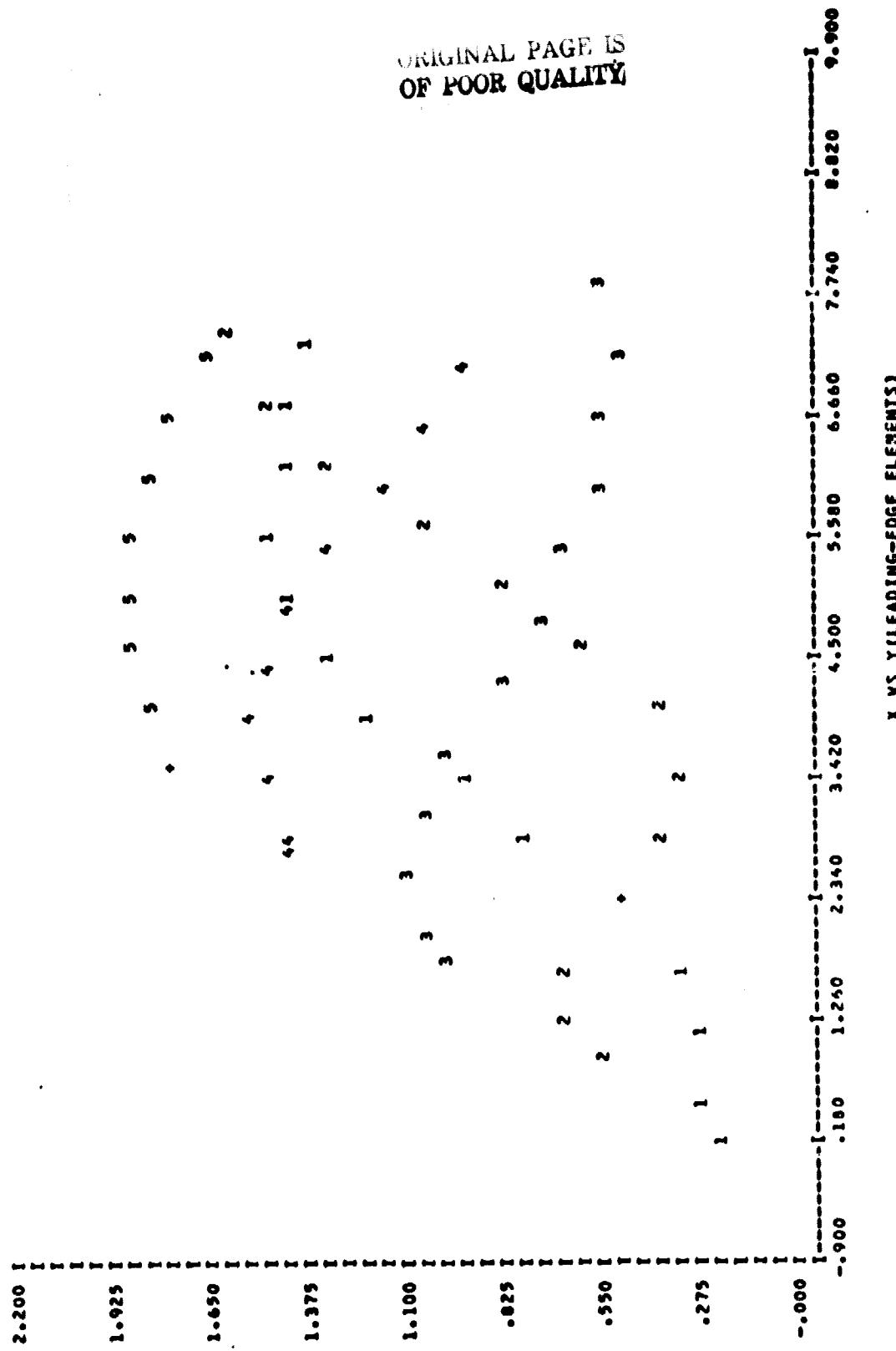
ALPHA(0EG.)=30.000 ASPECT RATIO = 2.0 MACH NUMBER= 0.000 ITERATION NUMBER = 1

LEADING EDGE EVENTS

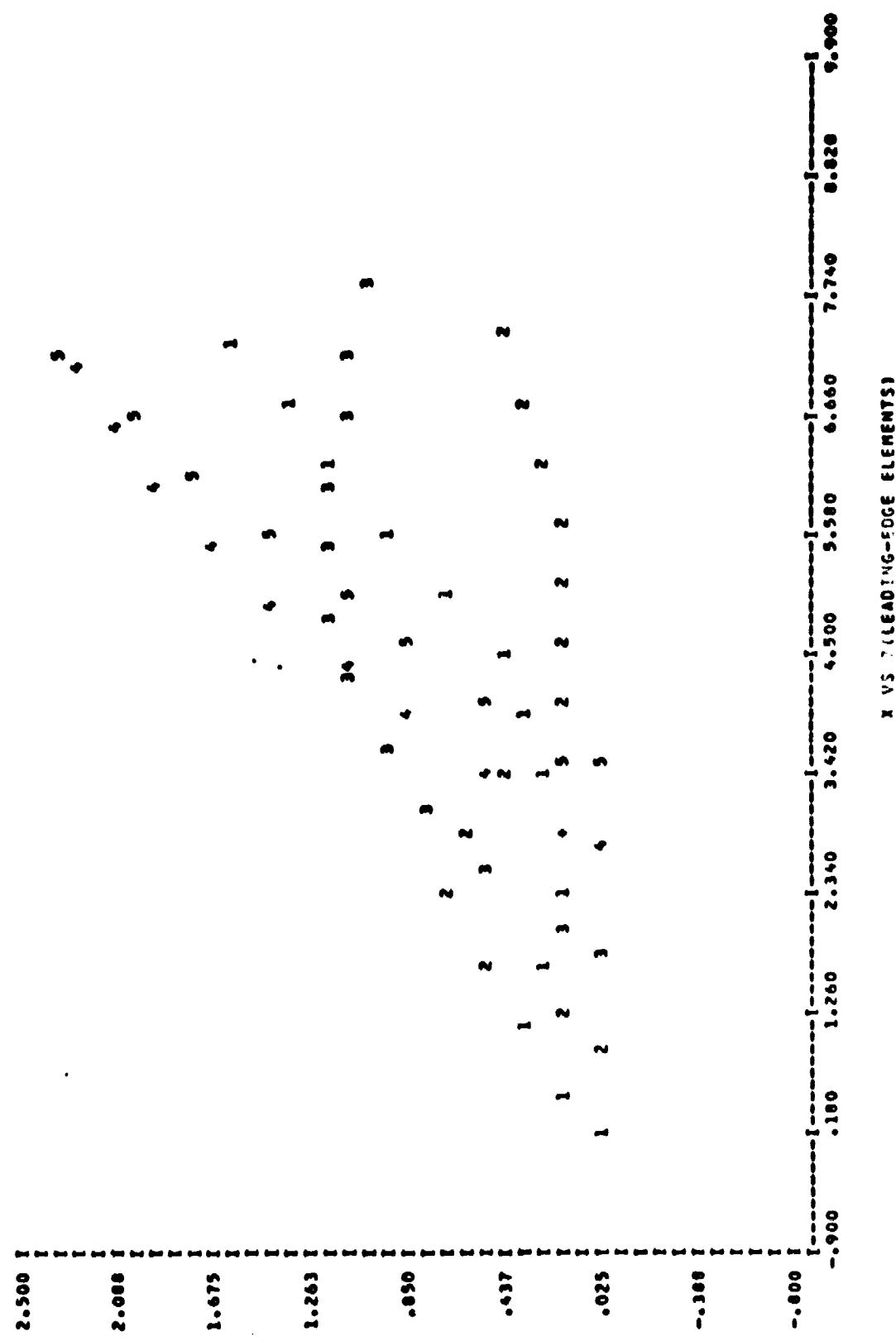
## MAKE ELEMENTS

*** 1***	4.0000	4.4000	4.8000	5.4000	6.0000	6.6000	7.2000	7.8000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
*** 2***	4.0000	4.4000	4.7966	5.3953	5.9940	6.5920	7.1890	7.7847
0.0000	0.0000	0.2578	0.3015	0.3359	0.3660	0.3956	0.4263	0.4623
0.0000	0.0000	-0.0295	-0.0380	-0.0191	0.0188	0.0711	0.1362	0.1362
*** 3***	4.0000	4.4000	4.7766	5.3421	5.9134	6.4944	7.0814	7.6696
0.0000	0.0000	0.5661	0.7009	0.9010	1.0842	1.2337	1.3542	1.4563
0.0000	0.0000	-0.0047	-0.0174	-0.0124	-0.0047	0.0257	0.0859	0.0859
*** 4***	4.0000	4.4000	4.7883	5.3637	5.9220	6.4620	7.0440	7.6423
1.0000	1.0000	1.0935	1.2481	1.4221	1.5050	1.3919	1.3901	1.3901
0.0000	0.0000	0.0225	0.0931	0.2274	0.4753	0.5674	0.5224	0.5224
*** 5***	4.0000	4.4000	4.7857	5.3673	5.9494	6.5284	7.1000	7.6664
1.4339	1.4339	1.4339	1.5302	1.6578	1.7672	1.8530	1.9251	1.9971
0.0000	0.0000	0.0000	0.0440	0.1164	0.2137	0.3459	0.5135	0.6979
*** 6***	4.0000	4.4000	4.7877	5.3675	5.9425	6.5136	7.0814	7.6665
1.7918	1.7918	1.9458	1.9526	2.0615	2.1512	2.2193	2.2745	2.2745
0.0000	0.0000	0.0000	0.0750	0.1666	0.3185	0.4793	0.6607	0.8546
*** 7***	4.0000	4.4000	4.7740	5.3114	5.8961	6.4717	7.0506	7.6294
1.9749	1.9749	2.0235	2.0791	2.0785	2.0702	2.0623	2.0566	2.0566
0.0000	0.0000	0.0000	0.1334	0.3483	0.5509	0.7203	0.8778	1.0359

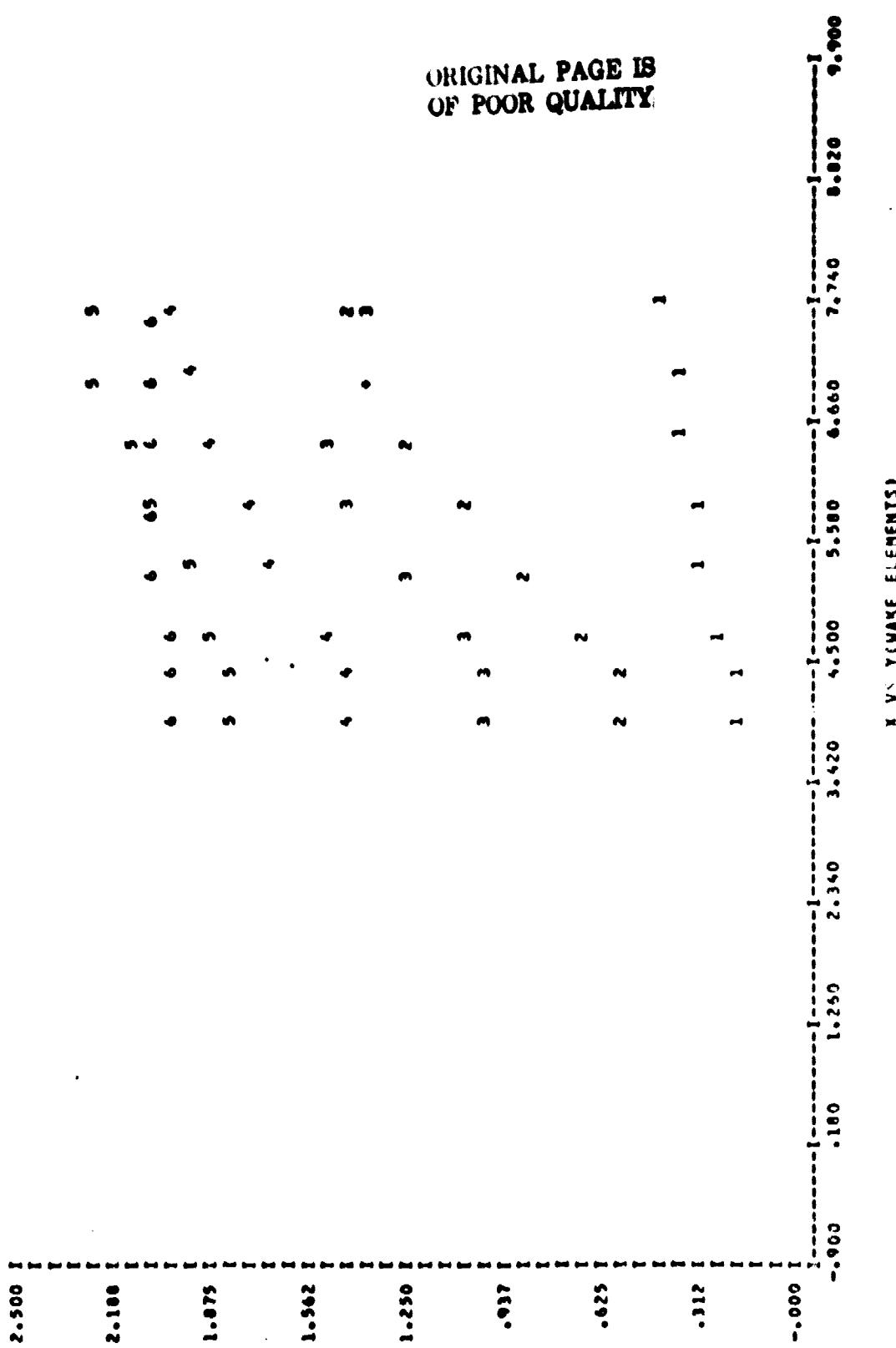
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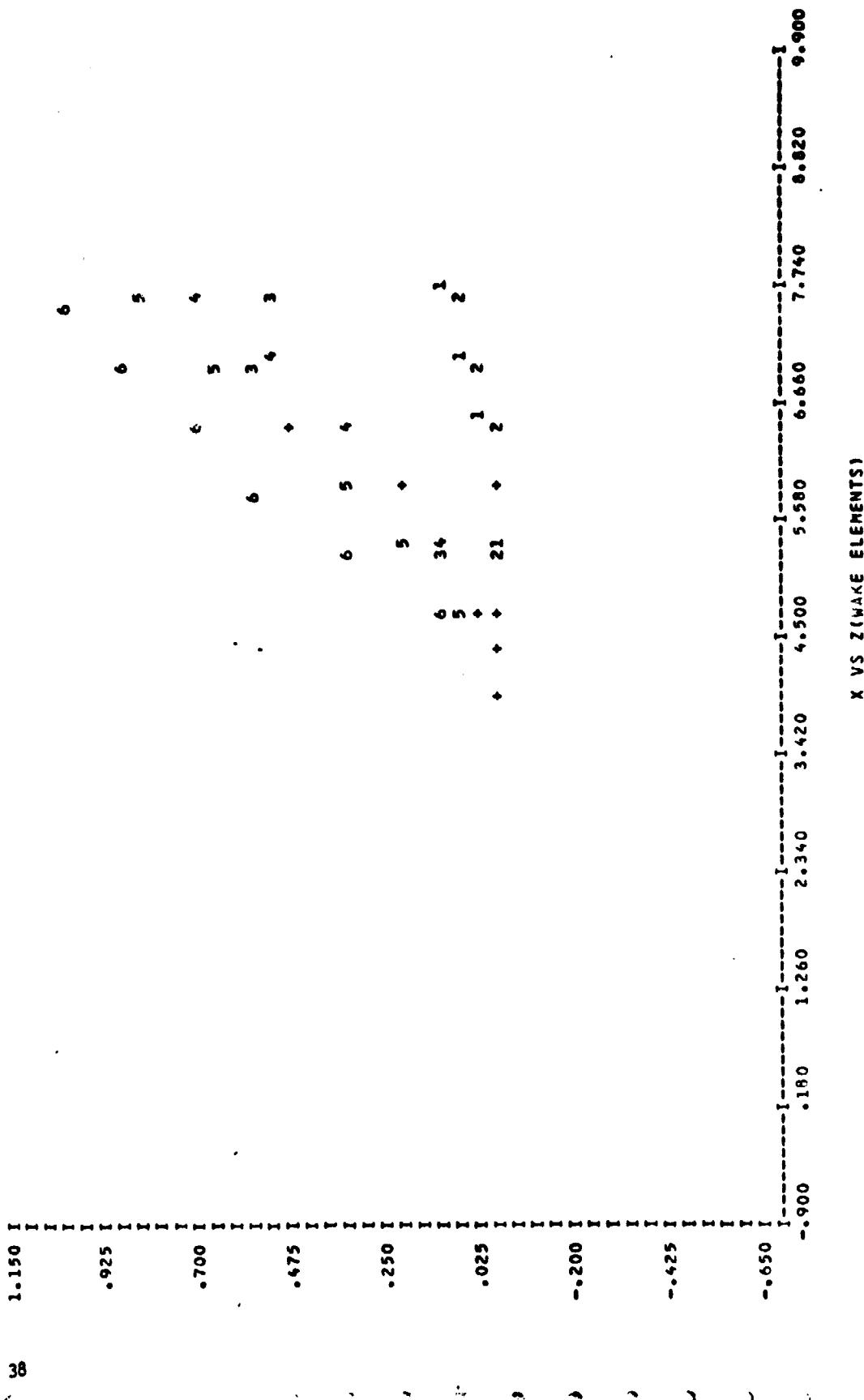


X VS Y(LEADING-EDGE ELEMENTS)



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WING VORTEX STRENGTHS

X/C	2Y/B	GAMA Y
* * *	* * *	* * *
*01704	*04952	8.25052
*14645	*04952	1.36627
*37059	*04952	.61192
*62941	*04952	.51188
*85355	*04952	.22160
*98296	*04952	.03334
*01704	*14626	5.80367
*14645	*18826	1.10192
*37059	*18826	*47379
*62941	*18826	*46969
*85355	*18826	.29190
*98296	*18826	*03814
*01704	*38874	7.13406
*14645	*38874	1.02614
*37059	*38874	*61492
*62941	*38874	*11650
*85355	*38874	*30132
*98296	*38874	*13724
*01704	*61126	8.92539
*14645	*61126	1.04178
*37059	*61126	*75280
*62941	*61126	*40170
*85355	*61126	*08733
*98296	*61126	-.00273
*01704	*81174	11.70835
*14645	*81174	1.22415
*37059	*81174	*80887
*62941	*81174	*53281
*85355	*81174	*27362
*98296	*81174	*08046
*01704	*95048	17.57687
*14645	*95048	1.78459
*37059	*95048	1.09015
*62941	*95048	*76081
*85355	*95048	*43806
*98296	*95048	*13460

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OF POOR QUALITY

LEADING-EDGE VORTICES STRENGTHS

2Y/B GAMA

\*\*\*\*\*  
\* \* \* \* \*  
• 04952 1.58978  
• 18826 • 96851  
• 38874 • 91597  
• 61126 • 73407  
• 81174 • 46763  
• 95048 • 18480

DELTA-CP DISTRIBUTION

X/C	2Y/B	DELTA-CP
***	***	***
001254	.04952	9.566653
010908	.04952	4.96700
028306	.04952	1.65211
050000	.04952	1.42061
711694	.04952	.79068
89092	.04952	.52909
98746	.04952	.24339
01254	.16826	8.81633
10908	.18826	2.68645
28306	.18826	1.96220
50000	.18826	1.82361
711694	.18826	1.35237
89092	.18826	.90122
98746	.18826	.65134
01254	.38874	5.57613
10908	.38874	3.48906
28306	.38874	2.25933
50000	.38874	1.84106
711694	.38874	1.93991
89092	.38874	1.54343
98746	.38874	1.23947
01254	.61126	4.02855
10908	.61126	2.83133
28306	.61126	1.32986
50000	.61126	1.00104
711694	.61126	1.23559
89092	.61126	.90902
98746	.61126	.97263
01254	.81174	3.29553
10908	.81174	2.57849
28306	.81174	1.22989
50000	.81174	.66425
711694	.81174	.38255
89092	.81174	.14927
98746	.81174	-.14288
01254	.95048	2.58105
10908	.95048	2.40211
28306	.95048	1.07138
50000	.95048	.69590
711694	.95048	.11024
89092	.95048	-.21056
98746	.95048	-.78007

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SECTIONAL PROPERTIES  
\*\*\*\*\*

	CLI	CMI	CDI	CTI
*	***	***	***	***
1	1.79394	-1.20941	1.03573	0.00000
2	1.77886	-1.91614	1.02703	0.00000
3	1.99753	-2.92693	1.15327	0.00000
4	1.31320	-2.30045	.75818	0.00000
5	.87826	-1.74180	.50706	0.00000
6	.68555	-1.51759	.39580	0.00000

TOTAL LIFT COEFFICIENT = 1.66094  
TOTAL PITCHING MOMENT COEFFICIENT = -2.07341  
TOTAL DRAG COEFFICIENT = .95894  
TOTAL THRUST COEFFICIENT = 0.00000

SPANWISE PRESSURES AT CONSTANT X= 1.00000  
Y 2Y/B(LOCAL) DELTA-CP  
.09903 .19806 2.52115  
.37651 .75302 3.26689

SPANWISE PRESSURES AT CONSTANT X= 2.00000  
Y 2Y/B(LOCAL) DELTA-CP  
.09903 .09903 1.40684  
.37651 .37651 1.92070  
.77748 .77748 2.89741

SPANWISE PRESSURES AT CONSTANT X= 3.00000  
Y 2Y/B(LOCAL) DELTA-CP  
.09903 .06602 .69986  
.37651 .25101 1.41881  
.77748 .51832 1.89848  
1.22252 .81501 1.03833

SPANWISE PRESSURES AT CONSTANT X= 3.50000  
Y 2Y/B(LOCAL) DELTA-CP  
.09903 .05659 .47866  
.37651 .21515 1.01330  
.77748 .44427 1.84657  
1.22252 .69858 1.23071  
.62340 .92771 .99452

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SPANWISE PRESSURES AT CONSTANT X = 3.075000

Y	2Y/B (LOCAL)	DELTA-CP
.09903	.05282	.64341
.37651	.20081	.81792
.77748	.41466	1.51332
1.22252	.65201	1.05705
1.62349	.86586	.46002

TOTAL ABSOLUTE FORCE ACTING ON LEADING-EDGE FREE ELEMENTS = .42133

Similar type of output data is printed for iterations 2 through 7.

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ASPECT RATIO = 2.0  
ALPHA(DEG.)=30.000 MACH NUMBER= 0.000 ITERATION NUMBER= 8

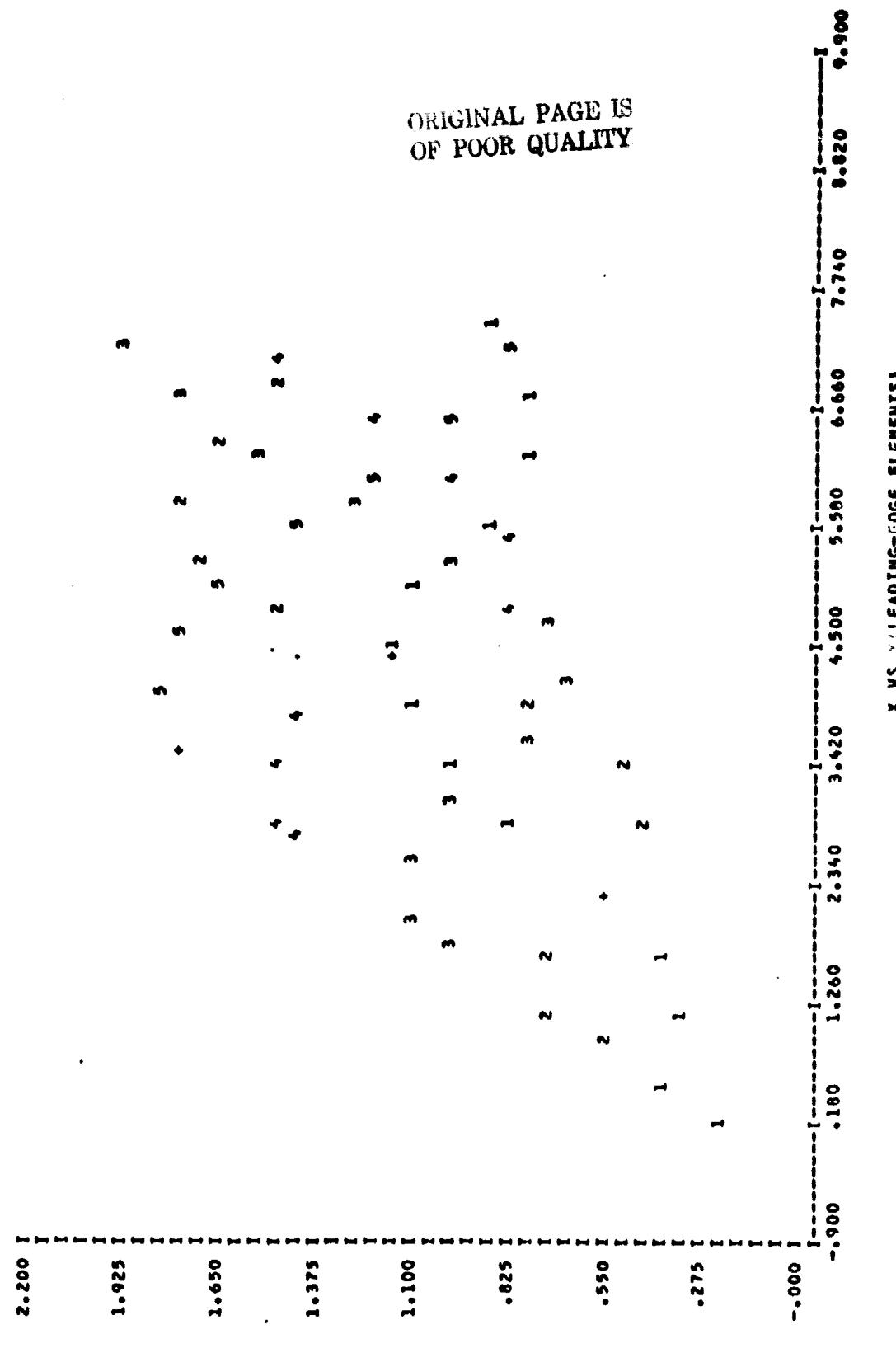
LEADING EDGE ELEMENTS

****	1****	2****	3****	4****	5****
4.0000	.4810	.0501	0.0000	-2000	.7196
.2192	.2182	0.0000	0.0000	0.0000	0.0000
0.0000	0.0000	0.0000	0.0000	.2309	.5309
4.0000	1.1682	.4610	.4353	.2582	.5650
5.6629	6.2497	6.3483	7.4432	.2182	.3602
.5661	.5661	.2182	.8710	0.0000	.3285
.9362	.7887	.7942	0.0000	.2309	.3558
0.0000	0.0000	1.1069	1.1172	0.0000	.3103
1.1773	1.1488	1.1322	.9988	1.2219	1.7408
4.0000	2.0251	1.1682	1.1322	2.3013	2.8852
5.8736	6.3455	6.9060	.5661	.7332	.7057
1.0000	1.0000	.5661	.5661	.5427	.4330
1.7523	1.6634	1.4875	1.0000	1.1134	1.1207
0.0000	0.0000	0.0000	0.0000	.2309	.5309
1.0342	1.3142	1.5679	0.0000	0.0000	.6696
4.0000	2.9820	2.0251	2.0000	1.9000	2.0647
6.7251	7.2906	1.4339	1.0000	1.0000	1.1207
1.4339	1.4339	1.0000	0.0000	0.0000	.9813
1.7940	1.6033	0.0000	0.0000	0.0000	.7925
0.0000	0.0000	0.0000	0.0000	0.0000	.8654
1.2452	1.5452	0.0000	0.0000	0.0000	.7505
4.0000	3.5691	2.6820	2.8578	2.8112	2.9160
1.7515	1.7918	1.4339	1.4339	1.4766	1.4982
0.0000	0.0000	0.0000	0.0000	0.2309	.5309
4.0000	3.9505	3.5691	3.5637	3.5418	3.5838
1.9749	1.9749	1.7618	1.7818	1.7618	1.7988
0.0000	0.0000	0.0000	0.0000	.2309	.5309

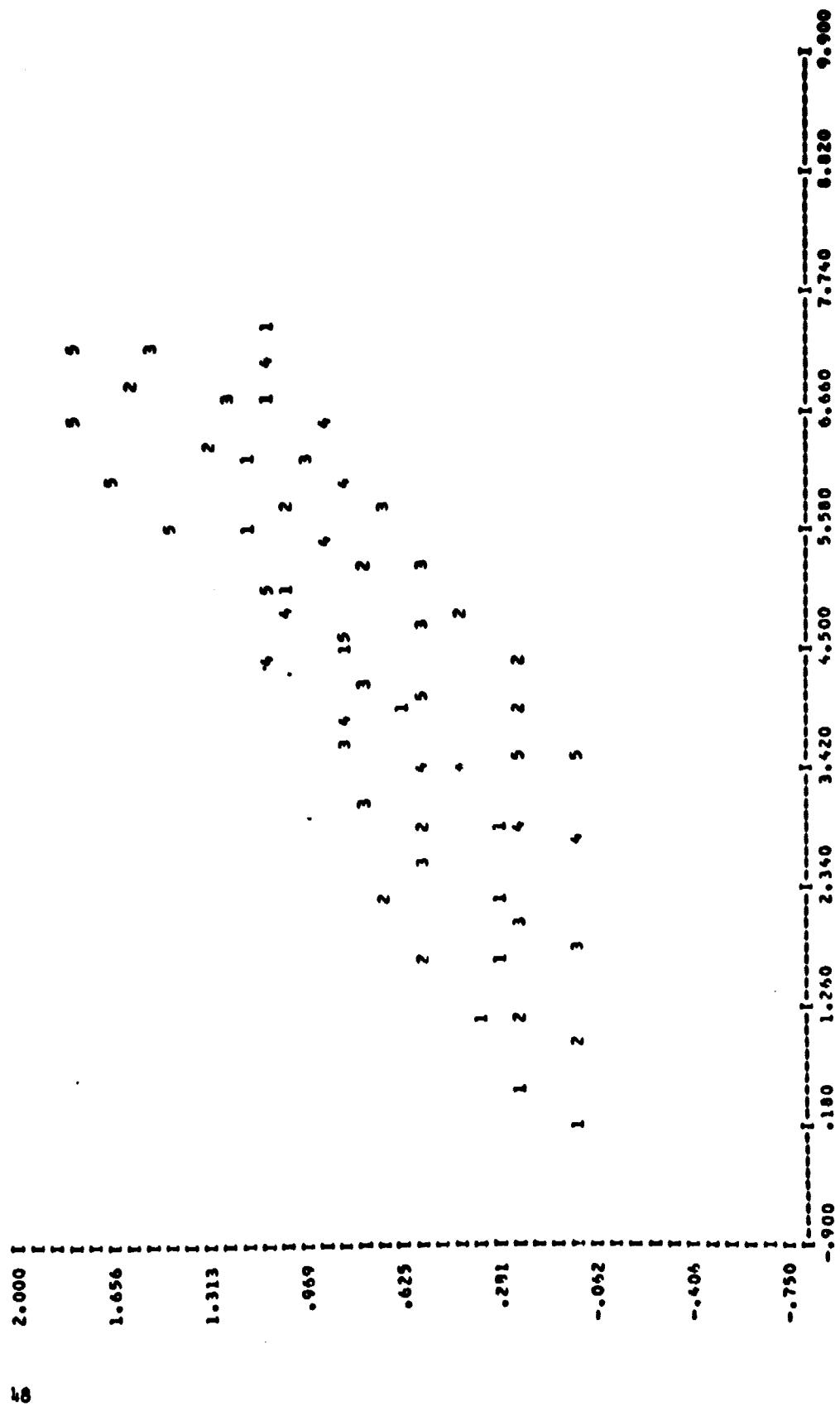
## WAKE ELEMENTS

*** 1***	4.0000	4.4000	4.8000	5.4000	6.0000	6.6000	7.2000	7.8000
0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
*** 2***	4.0000	4.4000	4.7950	5.3837	5.9691	6.5489	7.1210	7.6835
0.2182	* 2182	* 2762	* 3919	* 4978	* 6256	* 7667	* 9161	
0.0000	0.0000	0.0241	.0720	.1345	.2209	.3340	.4778	
*** 3***	4.0000	4.4000	4.7722	5.3152	5.8277	6.3064	6.7535	7.2188
0.5661	* 5661	* 7118	* 3591	1.2379	1.5255	1.7972	2.0284	
0.0000	0.0000	-0.0152	.0480	.1880	.4030	.6998	.9998	
*** 4***	4.0000	4.4000	4.6777	5.1049	5.5289	6.0000	6.4677	6.9853
1.0000	1.0000	1.2874	1.6665	1.9858	2.2392	2.4657	2.4202	
0.0000	0.0000	.0154	.1994	.4791	.7509	1.0509	1.3509	
*** 5***	4.0000	4.4000	4.7294	5.2543	5.7812	6.2922	6.7917	7.3062
1.4339	1.4339	1.6403	1.9193	2.0575	2.1515	2.2946	2.3672	
0.0000	0.0000	.0943	.1759	.4275	.7275	1.0275	1.3275	
*** 6***	4.0000	4.4000	4.7569	5.2122	5.7156	6.2566	6.8245	7.3461
1.7918	1.7918	1.9106	2.1609	2.2897	2.4232	2.3237	2.3229	
0.0000	0.0000	.1267	.4267	.7267	.9837	1.1639	1.4639	
*** 7***	4.0000	4.4000	4.7409	5.2573	5.7463	6.2053	6.7249	7.2717
1.9749	1.9749	2.0367	1.9795	2.2496	2.4932	2.5000	2.5000	
0.0000	0.0000	.2000	.5000	.7168	1.0168	1.3188	1.5658	

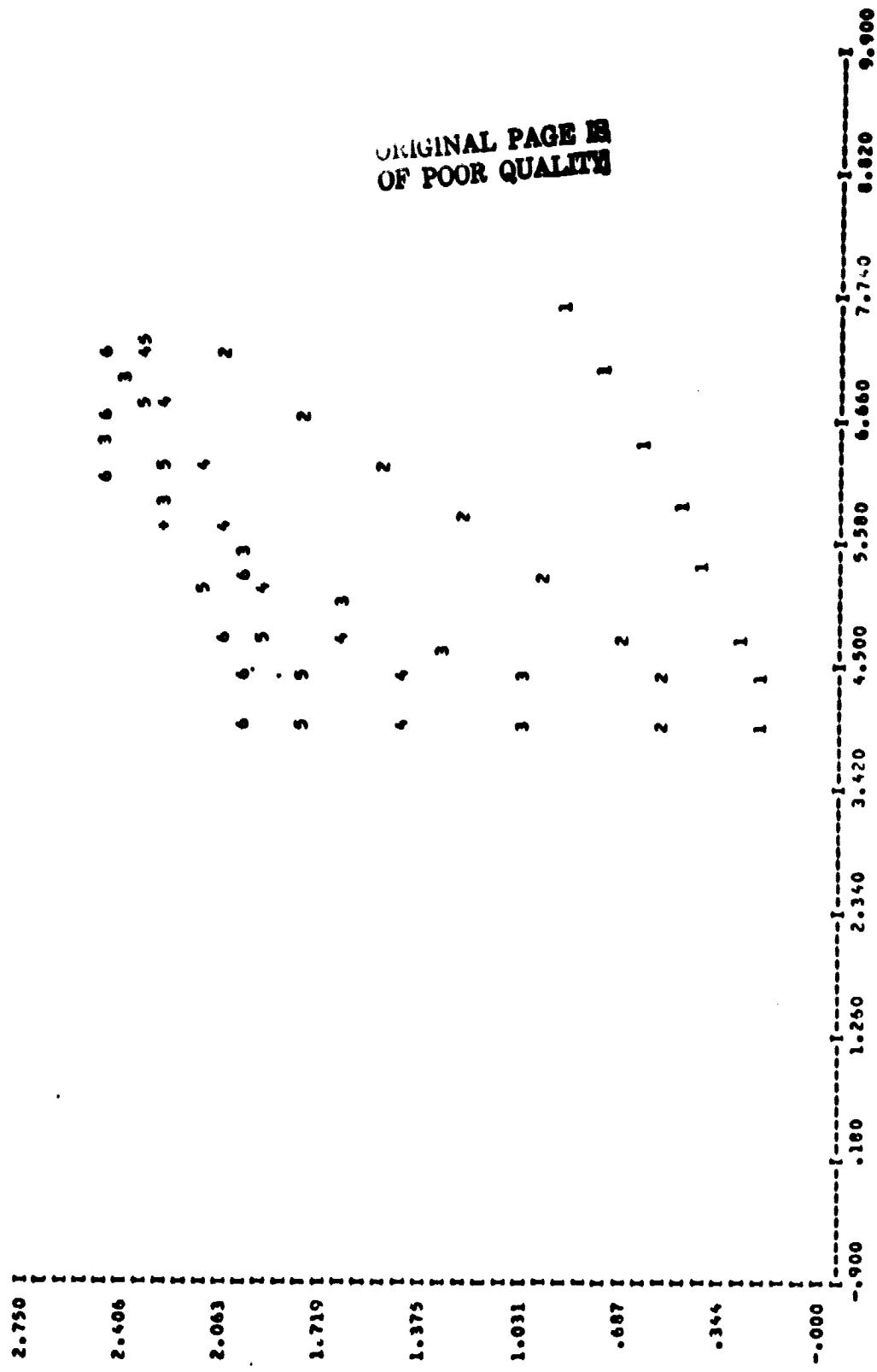
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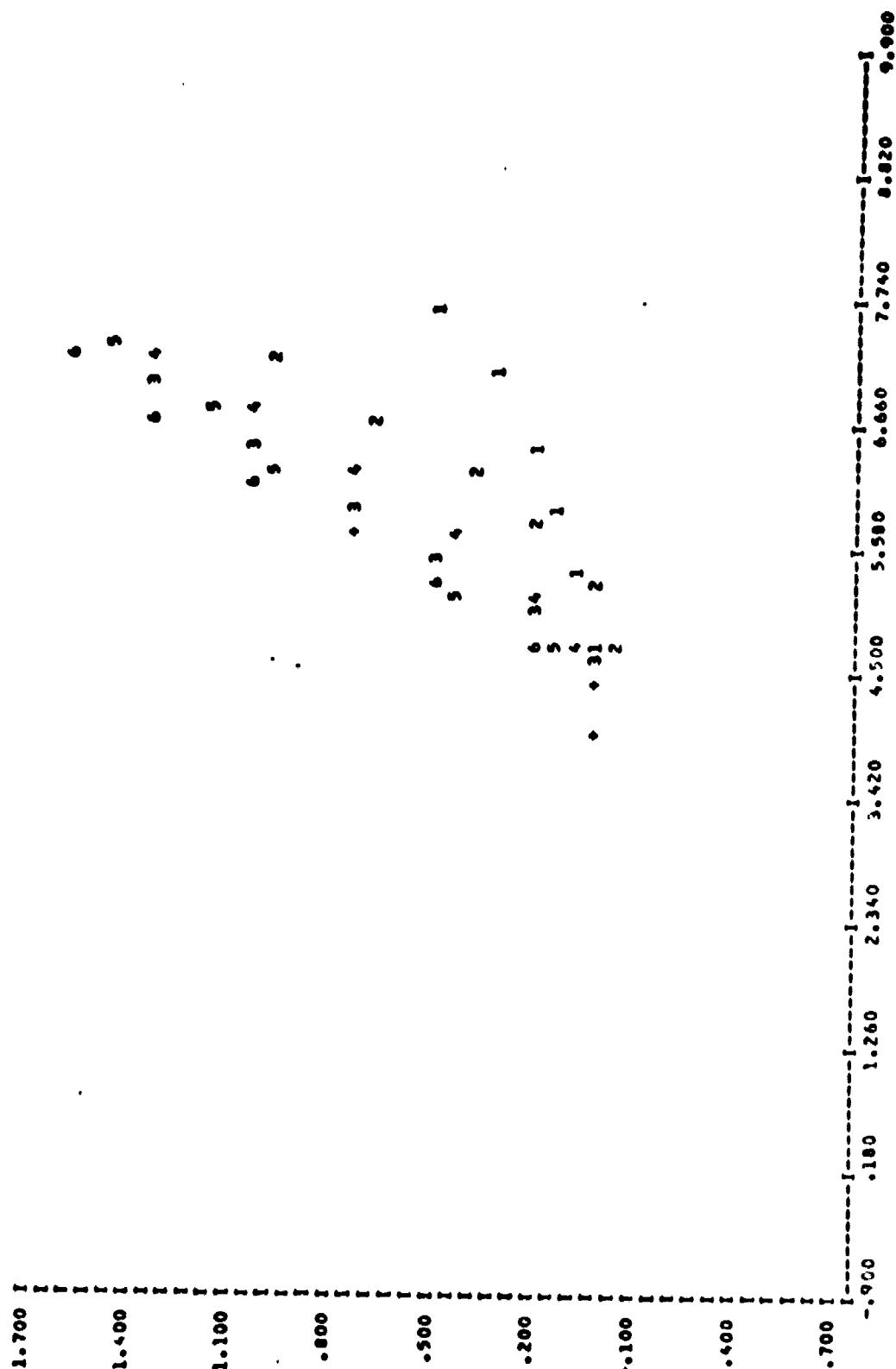
X VS Z (LEADING-EDGE ELEMENTS)



X VS Y(MAKE ELEMENTS)



X VS Z(WAKE ELEMENTS)



卷之三

LEARNING-EDGE VARIETIES OF STATE NARRATIVES

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WING VORTEX STRENGTHS

\*\*\*\*\*  
• 04952 1.60568  
• 1A826 • 90490  
• 38874 • 86239  
• 61126 • 71020  
• 81174 • 46124  
• 95048 • 18644

DELTA-CP DISTRIBUTION	X/C	2Y/B	DELTA-CP
*****	*****	*****	*****
*01254	.04952	7.61337	
*10908	.04952	4.55513	
*28306	.04952	1.52432	
*50000	.04952	1.29977	
*71694	.04952	.66802	
*89092	.04952	.36277	
*98746	.04952	.15258	
*01254	.18826	6.34274	
*10908	.18826	2.29859	
*28306	.19826	1.73239	
*50000	.18826	1.58317	
*71694	.18826	1.21872	
*89092	.19826	.77920	
*98746	.16826	.50958	
*01254	.38874	4.33651	
*10908	.38874	2.91581	
*28306	.38874	1.97543	
*50000	.38874	1.63405	
*71694	.38874	1.76146	
*89092	.38874	1.44152	
*98746	.38874	1.15567	
*01254	.61126	3.55946	
*10908	.61126	2.62342	
*28306	.61126	1.33923	
*50000	.61126	.97921	
*71694	.61126	1.18459	
*89092	.61126	.90131	
*98746	.61126	.86762	
*01254	.81174	3.13069	
*10908	.81174	2.47576	
*28306	.81174	1.27152	
*50000	.81174	.73556	
*71694	.81174	.48107	
*89092	.81174	.22523	
*98746	.81174	-.11281	
*01254	.95048	2.63992	
*10908	.95048	2.47422	
*28306	.95048	1.11563	
*50000	.95048	.74813	
*71694	.95048	.15061	
*89092	.95048	-.18024	
*98746	.95048	-.76758	

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SECTIONAL PROPERTIES

54

	CLL	CMH	CDI	CTI
1	1.56797	-1.04769	.90527	0.00000
2	1.49362	-1.04737	.86234	0.00000
3	1.73731	-2.58121	1.00304	0.00000
4	1.25071	-2.16754	.72210	0.00000
5	.90756	-1.80656	.52399	0.00000
6	.72602	-1.60937	.41917	0.00000

TOTAL LIFT COEFFICIENT= 1.45997  
 TOTAL PITCHING MOMENT COEFFICIENT = -1.86231  
 TOTAL DRAG COEFFICIENT = .84292  
 TOTAL IMPUST COEFFICIENT = 0.00000

X	Y	Z	SPANWISE PRESSURES AT CONSTANT X=
2Y/B(LOCAL)	DELTA-CP		1.00000
.09903	.09903	1.9806	2.34285
.37651	.37651	1.66734	
.37651	.75302	.68275	

X	Y	Z	SPANWISE PRESSURES AT CONSTANT X=
2Y/B(LOCAL)	DELTA-CP		2.00000
.09903	.09903	1.9806	2.34285
.37651	.37651	1.66734	
.77748	.77748	.67956	

X	Y	Z	SPANWISE PRESSURES AT CONSTANT X=
2Y/B(LOCAL)	DELTA-CP		3.00000
.09903	.09902	.57516	
.37651	.25101	1.27410	
.77748	.51832	1.69580	
1.22252	.81501	1.06014	

X	Y	Z	SPANWISE PRESSURES AT CONSTANT X=
2Y/B(LOCAL)	DELTA-CP		3.50000
.09903	.09903	.57516	
.37651	.21515	1.69582	
1.22252	.69858	1.17457	
1.62349	.92771	1.05241	

SPANWISE PRESSURES AT CONSTANT X = 3.075000  
Y 2Y/B (LOCAL) DELTA-CP

• 09903	• 05282	• 47436
• 37651	• 20081	• 68765
• 77748	• 41466	1.41464
1.22252	• 65201	1.03999
1.62349	• 86586	• 55153

TOTAL ABSOLUTE FORCE ACTING ON LEADING-EDGE FREE ELEMENTS •

• 17432

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Similar type of output data is printed for iterations 9 and 10.

SUMMARY SHEET  
\*\*\*\*\*

ASPECT RATIO = 2.0

ALPHA(DEG.) = 30.000 MACH NUMBER = 0.000

ITERATION	CL	CM	CD	CT	GMSUM	PERR	TFABS
*****	**	**	**	**	*****	*****	*****
0	1.5581	-1.8319	.8995	0.0000	3.2626	1.2862	
1	1.6609	-2.0734	.9589	0.0000	3.2710	.4213	
2	1.5024	-1.9132	.8674	0.0000	3.1577	3.5233	.3423
3	1.4260	-1.8073	.8233	0.0000	3.1057	1.6609	.3454
4	1.4328	-1.8182	.8272	0.0000	3.1027	.0976	.2999
5	1.4558	-1.8541	.8405	0.0000	3.1204	.5712	.2140
6	1.4632	-1.8670	.8448	0.0000	3.1257	.1698	.1865
7	1.4648	-1.8697	.8457	0.0000	3.1292	.1117	.1858
8	1.4600	-1.8673	.8429	0.0000	3.1252	.1308	.1743
9	1.4598	-1.8618	.8428	0.0000	3.1260	.0263	.1754
10	1.4598	-1.8614	.8429	0.0000	3.1270	.0318	.1732

ALL CASES COMPLETED

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**6.2 APPENDIX B: COMPUTER PROGRAM LISTING**

A listing of the computer program is given on the following pages.

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OVERLAY (LEVSP,0,0)  
PROGRAM LEVSP(INPUT,OUTPUT,TAPE1,TAPE2,TAPE3,TAPE5=INPUT,TAPE6=OUTLEV  
INPUT,PUNCH,TAPE4,TAPE7)  
LEV 10  
LEV 20  
LEV 30  
LEV 40  
LEV 50  
LEV 60  
LEV 70  
LEV 80  
LEV 90  
LEV 100  
LEV 110  
LEV 120  
LEV 130  
LEV 140  
LEV 150  
LEV 160  
LEV 170  
LEV 180  
LEV 190  
LEV 200  
LEV 210  
LEV 220  
LEV 230  
LEV 240  
LEV 250  
LEV 260  
LEV 270  
LEV 280  
LEV 290  
LEV 300  
LEV 310  
LEV 320  
LEV 330  
LEV 340  
LEV 350  
LEV 360  
LEV 370  
LEV 380  
LEV 390  
LEV 400

AERODYNAMICS OF LOW ASPECT-RATIO WINGS WITH PARTIAL LEADING-EDGE  
SEPARATION (LEADING-EDGE VORTEX SEPARATION PROGRAM)  
BY - SUDHIR C. MEFHOTRA AND C. EDWARD LAN  
UNIVERSITY OF KANSAS

THIS PROGRAM IS RESTRICTED TO DELTA AND ARROW WINGS

PROGRAM IS DIVIDED INTO FIVE OVERLAYS.  
OVERLAY (1,0) READS ALL THE DATA CARDS AND SETSUP INETIAL GEOMETRY  
OF THE WING AND THE FREE ELEMENTS  
OVERLAY (2,0) PLOTS FREE ELEMENTS OVER THE WING AND IN THE WAKE ONLEV  
THE LINE PRINTER OUTPUT  
OVERLAY (3,0) SOLVES FOR THE STRENGTHS OF WING AND LEADING-EDGE  
VORTEX SYSTEM  
OVERLAY (4,0) COMPUTES THE AERODYNAMIC CHARACTERISTICS  
OVERLAY (5,0) COMPUTES THE NEW LOCATIONS OF THE LEADING-EDGE AND  
TRAILING-EDGE VORTICES  
AS THE PROBLEM IS NONLINEAR, IT IS SOLVED BY ITERATION. ITERATION  
IS PERFORMED OVER OVERLAYS (2,0) THRU (4,0) TO OBTAIN THE FINAL  
CONVERGFD SOLUTION.

THE DIMENSIONS OF THE FOLLOWING VARIABLES MUST BE CHECKED BEFORE  
RUNNING THE PROGRAM.

-D- APPEARS IN BLANK COMMON OF MAIN LINE (OVERLAY(0,0))  
MUST BE DIMENSIONED MAXIMUM OF THE FOLLOWING VARIARLFS.  
N1=2286  
N2=3\*NMAX\*(NSW-1)+NSW  
N3=3\*NSW\*(INNMAX+2)+NSW+1  
N4=(NCPTTL+1)\*\*2/4+10\*NWNG+10\*NSW+3\*NCW-6  
N5=29\*NWNG+25\*NSW+10\*NCW-14  
N6=21\*NWNG+14\*NSW+NCW-9

-W- APPEARS IN PROGRAM LOADS (OVERLAY (4,0))  
MUST BE DIMENSIONED AT LEAST ((N\*NCW+3)\*(NWNG+NCW+4))

```

C -E- APPEARS IN PROGRAM NEWSHAP (OVERLAY(5,0))
C MUST BE DIMENSIONED AT LEAST (3*NSW*(NMAX+NNMAX)-3*NNMAX+1)
C
C WHERE, NMAX = MAXIMUM NUMBER OF END-POINTS IN ANY ONE FREE
C LEADING-EDGE VORTEX ELEMENT
C NNMAX = MAXIMUM NUMBER OF END-POINTS IN ANY ONE WAKE
C ELEMENT
C NCW = NUMBER OF CHORDWISE LINES (ONE HIGHER THAN
C NSW = NUMBER OF SPANWISE LINES (ONE HIGHER THAN
C NCPTTL = TOTAL NUMBER OF SPANWISE ROWS OF PANELS)
C INCLUDING THOSE AT THE LEADING-EDGE ((NCW+1)*
C (NSW-1))
C NWNG = TOTAL NUMBER OF CONTROL POINTS OVER THE WING
C EXCLUDING THOSE AT THE LEADING-EDGE (NCW*
C (NSW-1))
C
C COMMON D(3000)
COMMON /ALL1/ NSW, NSWI, NCW, NWNG, NCPTTL, MITER, IPUNCH
COMMON /ALLRA/ TTL(16), ALPHA, SINR, COSA, SWPLE, BETA2, TANPH1, B7PLEV
1H1, BSQD4P, D4, CON, PI, D4SQ2, CBAR, HALF8, AREA
COMMON /ALLRA/ XE(40), YE(40), ZE(40), XXE(30), YYE(30), ZZE(30), ZMIN, NLEV
IELM(11), NNELM(12)
COMMON /XPLOT/ XMN, YMN, ZMN, XMX, YMX, ZMX
COMMON /GM/ ITER, L1, L2, L3, L4, L5, L6, L7, L8
COMMON /XSTN/ XBPR(25), NBRK
CALL OVERLAY (SHLEVSP, 1, 0)
ITER=0
CONTINUE
ALP=ALPHA+180./PI
AMACH=SORT(1.-BETA2)
WRITE FREE ELEMENTS LOCATIONS
WRITE (6,100) TTL, ALP, AMACH, ITER
REWIND 4
DO 30 I=1,NSW1
***** ****
C READ (4) K, (XE(J),YE(J),ZE(J),J=1,K)
C ***** ****
C WRITE (6,150) I
C
LEV 410
LEV 420
LEV 430
LEV 440
LEV 450
LEV 460
LEV 470
LEV 480
LEV 490
LEV 500
LEV 510
LEV 520
LEV 530
LEV 540
LEV 550
LEV 560
LEV 570
LEV 580
LEV 590
LEV 600
LEV 610
LEV 620
LEV 630
LEV 640
LEV 650
LEV 660
LEV 670
LEV 680
LEV 690
LEV 700
LEV 710
LEV 720
LEV 730
LEV 740
LEV 750
LEV 760
LEV 770
LEV 780
LEV 790

```

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```
SUBROUTINE SKIPR (NT,NR)
C      SKIPS NR-RECORDS OF TAPE NT
      DO 10 I=1,NR
      READ (NT)
      RETURN
10      END
```

```
10
SKP 20
SKP 30
SKP 40
SKP 50
SKP 60
```

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C FUNCTION ARCCOS (X)  
C CALCULATES ARC-COSINE OF X  
ARCOS=0.  
IF (X.EQ.1.) RETURN  
IF (X.EQ.(-1.)) GO TO 10  
XX=X/(SQR(1.-X\*X))  
ARCOS=1.5707963-ATAN(XXX)  
RETURN  
ARCOS=3.1415976  
RETURN  
END

10  
ARC 10  
ARC 20  
ARC 30  
ARC 40  
ARC 50  
ARC 60  
ARC 70  
ARC 80  
ARC 90  
ARC 100  
ARC 110-

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```
10 DOT 10
20 DOT 20
30 DOT 30
40 DOT 40
50 DOT 50
60 DOT 60
70 DOT 70
80 DOT 80

SUBROUTINE DOTPRO (A,B,SUM)
C   CALCULATES DOT-PRODUCT OF TWO VECTORS
C   DIMENSION A(3), B(3),
SUM=0.
DO 10 I=1,3
      SUM=SUM*A(I)*B(I)
10   RETURN
      END
```

```
SUBROUTINE CROSPRD (A,B,C)
C
C      CALCULATES CROSS-PRODUCT OF TWO VECTORS
DIMENSION A(3), B(3), C(3)
C(1)=A(2)*B(3)-A(3)*B(2)
C(2)=A(3)*B(1)-A(1)*B(3)
C(3)=A(1)*B(2)-A(2)*B(1)
RETURN
END
```

C

```
CRS 10
CRS 20
CRS 30
CRS 40
CRS 50
CRS 60
CRS 70
CRS 80-
```

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```
10
SUBROUTINE VOTWNG (C,THETP,XX,YY,ZZ,XN,YN,XTE,YTE,CONS,CON1,CON2,CON3,
1,CONJ1,CONJ2,CONJ3,CONK1,CONK2,CONK3,CONI,CONJ,CONK,SIN,SW1,NCH,NWNG
20
2NG)
C EVALUATES INFLUENCE COEFFICIENTS FOR CALCULATION OF INDUCEON
C VELOCITY DUE TO WING ELEMENTS
COMMON /ALL1/ NSW
COMMON /ALLRA/ XXX(30), YYE(30), ZZE(30)
COMMON /NCTT/ NCT,NCN
COMMON /XIYZI/ XI,YI,ZI
DIMENSION THFTD(1), C(1), CONS(1), XTE(1), YTE(1), SI(1), CON1(1)WNG 100
1, CONI3(1), CONJ1(1), CONJ2(1), CONJ3(1), CONK1(1), CONK2(1), CONKWG 110
23(1), CONI(1), CONJ(1), CONK(1), XN(NWNG,2), YN(NWNG,2), R(3), D(3)WNG 120
3) WNG 130
C DIMENSIONS OF FJ1,FJ2,FJ3-(2*NSW) ** SEE GEOM **
C DIMENSIONS OF FJ2,FJ3-(2*NCPTTL) ** SEE GEOM **
C DIMENSION FJ1(40), FJ2(40), FJ3(40), F12(418), F13(418)
XI=XX
YI=YY
ZI=ZZ
NC1=NWNG+NCW
NC2=NWNG-NCW
C VELOCITY DUE TO ROUND ELEMENTS
DO 10 I=1,NSW1
DO 10 J=1,NCW
NP=(I-1)*NCW+
CALL INFEL2 (XN(NP,1),YN(NP,1),0.,0.,XN(NP,2),YN(NP,2),0.,0.,B1)
A1=-YN(NP,1)
A2=-YN(NP,2)
CALL INFEL2 (XN(NP,1),A1,0.,XN(NP,2),A2,0.,0.,D)
CONI(NP)=CONS(I)*(R(1)-D(1))
CONJ(NP)=CONS(I)*(R(2)-D(2))
CONK(NP)=CONS(I)*(R(3)-D(3))
C 10 VELOCITY DUE TO TRAILING ELEMENTS ON THE WING SURFACE
DO 20 I=1,NSW1
DO 20 J=1,NCW
NP=(I-1)*NCW+
CALL INFEL2 (XN(NP,1),YN(NP,1),0.,0.,XTE(I),YN(NP,1),0.,0.,B1)
F12(NP)=B(2)
F13(NP)=B(3)
AYN=-YN(NP,1)
```

```

WNG 410
WNG 420
WNG 430
WNG 440
WNG 450
WNG 460
WNG 470
WNG 480
WNG 490
WNG 500
WNG 510
WNG 520
WNG 530
WNG 540
WNG 550
WNG 560
WNG 570
WNG 580
WNG 590
WNG 600
WNG 610
WNG 620
WNG 630
WNG 640
WNG 650
WNG 660
WNG 670
WNG 680
WNG 690
WNG 700
WNG 710
WNG 720
WNG 730
WNG 740
WNG 750
WNG 760
WNG 770
WNG 780
WNG 790

NO=NC1+NPF
CALL INFL2 (XN(NP,1),AYN,0.,XTE(1),AYN,0.,B)
F12(NO)=B(2)
F13(NQ)=B(3)
CONTINUE
DO 30 J=1,NCW
NP1=NWNC+j
NP2=NC1+NP1
NP=NC2+j
CALL INFL2 (XN(NP,2),YN(NP,2),0.,XTE(NSW),YN(NP,2),0.,B)
FT2(NP1)=R(2)
FI3(NP1)=R(3)
AYN=YN(NP,2)
CALL INFL2 (XN(NO,2),AYN,0.,XTE(NSW),AYN,0.,B)
FT2(NP2)=R(2)
FI3(NP2)=R(3)
CONTINUE
DO 40 I=1,NSW1
NC 40 J=1,NCW
NP=(I-1)*NCW+J
I1=NP+NC1
I2=NP+NCW
I3=I1+NCW
CONJ2(NP)=C0NS(I)*(FI2(I1)-FI2(NP)+FI2(I2)-FI2(I3))
CONK2(NP)=C0NS(I)*(FI3(I1)-FI3(NP)+FI3(I2)-FI3(I3))
VELOCITY DUE TO TRAILING ELEMENTS BEYOND TRAILING EDGE
*****C*****
REWIND 4
CALL SKTPR (4,NSW)
DO 80 I=2,NSW
READ (4) KK,XXE(J),YYE(J),ZZE(J),J=1,KK
*****C*****
FJ1(I)=0.
FJ2(I)=0.
FJ3(I)=0.
IF (I.EQ.NCT) GO TO 60
DO 50 J=2,KK
CALL INFL2 (XXE(J-1),YYE(J-1),ZZE(J-1),XXE(J),YYE(J),ZZE(J),B)
FJ1(I)=FJ1(I)+B(I)

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FJ2(I)=FJ2(I)+B(2)
FJ3(I)=FJ3(I)+B(3)
CONTINUE
CALL FUNA (XXE(KK),YYE(KK),ZZE(KK),B(1),B(2),B(3))
FJ1(I)=FJ1(I)+B(1)
FJ2(I)=FJ2(I)+B(2)
FJ3(I)=FJ3(I)+B(3)
CONTINUE
IN=I+NSW
FJ1(IN)=0.
FJ2(IN)=0.
FJ3(IN)=0.
DO 70 J=2,MK
AYT1=-YYE(J-1)
AYT2=-YYE(J)
CALL INFL? (XXE(J-1),AYT1,ZZE(J-1),XXE(J),AYT2,ZZE(J),B)
FJ1(IN)=FJ1(IN)+B(1)
FJ2(IN)=FJ2(IN)+B(2)
FJ3(IN)=FJ3(IN)+B(3)
CONTINUE
AYT2=-YYE(KK)
CALL FUNA (XXE(KK),AYT2,ZZE(KK),B(1),B(2),B(3))
FJ1(IN)=FJ1(IN)+B(1)
FJ2(IN)=FJ2(IN)+B(2)
FJ3(IN)=FJ3(IN)+B(3)
CONTINUE
FJ1(I)=0.
FJ2(I)=0.
FJ3(I)=0.
FJ1(NSW+1)=0.
FJ2(NSW+1)=0.
FJ3(NSW+1)=0.
DO 90 I=1,NSW
I1=I+1
I2=I+NSW
I3=I2+1
EFJ1=CONS(I)*(FJ1(I2)-FJ1(I)+FJ1(I1)+FJ2(I2)-FJ2(I1)+FJ2(I1)-FJ3(I2)+FJ3(I1)-FJ3(I1))
EFJ2=CONS(I)*(FJ2(I2)-FJ2(I1)+FJ2(I1)-FJ3(I2)+FJ3(I1)+FJ3(I1)-FJ3(I1))
EE,I3=CONS(I)*(FJ3(I2)-FJ3(I1)+FJ3(I1)-FJ3(I1))

```

```

DO 90 J=1,NCW
NP=(I-1)*NCW+J
CONI3(NP)=EFJ1
CONJ3(NP)=EFJ2
CONK3(NP)=FFJ3
90          C TOTAL INDUCED VELOCITY
I=1
DO 100 J=1,NWNG
CONI(J)=(CONI(J)+CONI3(J))*SI(I)
CONJ(J)=(CONJ(J)+CONJ2(J)+CONJ3(J))*SI(I)
CONK(J)=(CONK(J)+CONK2(J)+CONK3(J))*SI(I)
I=I+1
IF (I.GT.NCW) I=1
CONTINUE
RETURN
END
100

```

SUBROUTINE VDTFRE (X,Y,Z,CJ,CK,NSW1,BSQD4P,XLE,YLE)  
 C EVALUATES INFLUENCE COEFFICIENTS FOR CALCULATION OF INDUCED  
 C VELOCITY DUE TO FREE ELEMENTS  
 COMMON /ALLPR/ XE(40),YE(40),ZE(40),XXE(30),YYE(30),ZZE(30)  
 COMMON /NCTT/ NCT,NCON  
 COMMON /XYIZI/ XI,YI,ZI  
 DIMENSION CI(1), CJ(1), CK(1), XLE(1), YLE(1), ZLE(1)  
 DIMENSION NF VTDL-(NSW1,3) \*\* SEE GEOM \*\*  
 DIMENSION VTDL(19,3)  
 XI=X  
 YI=Y  
 ZI=Z  
 NCT1=0  
 \*\*\*\*  
 C REWIND 4  
 C 10 \*\*\*\*  
 DO 60 I=1,NSW1  
 V(1)=0.  
 V(2)=0.  
 V(3)=0.  
 FJ1=0.  
 FJ2=0.  
 FJ3=0.  
 \*\*\*\*  
 C READ (4) KK, XF(J), YE(J), ZE(J), J=1,KK  
 C \*\*\*\*  
 K=KK-1  
 C VELOCITY DUE TO FREE ELEMENTS AHEAD OF TRAILING-EDGE AND THOSE  
 C OVER THE WING  
 DO 20 J=1,K  
 IF (I.EQ.NCON.AND.J.GT.4.AND.YI.GT.0.) GO TO 20  
 CALL INFLL (XF(J)),YE(J),ZE(J),XE(J+1),YE(J+1),ZE(J+1),VVV  
 V(1)=V(1)+VVV(1)  
 V(2)=V(2)+VVV(2)  
 V(3)=V(3)+VVV(3)  
 20 CONTINUE  
 IF (I.EQ.NCON.AND.YI.GT.0.) GO TO 30  
 CALL FUNA (XE(K+1),YE(K+1),ZE(K+1),FJ1,FJ2,FJ3)  
 VTDL(I,1)=V(1)+FJ1  
 VTDL(I,2)=V(2)+FJ2  
 VTDL(I,3)=V(3)+FJ3

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VTDL(I,3)=V(3)+FJ3
FJ1=0.          FRE 410
FJ2=0.          FRE 420
FJ3=0.          FRE 430
I1=I+1          FRE 440
* * * * *          FRE 450
* * * * *          FRE 460
* * * * *          FRE 470
* * * * *          FRE 480
* * * * *          FRE 490
* * * * *          FRE 500
IF (I1.EQ.NCT1.AND.YI.GT.0.) GO TO 50
C VELOCITY DUE TO WAVE ELEMENTS          FRE 510
DO 40 J=?,IT          FRE 520
CALL INFL2 (XXE(J-1),YYE(J-1),ZZE(J-1),XXE(J),YYE(J),ZZE(J),VI)          FRE 530
FJ1=FJ1+V(1)          FRE 540
FJ2=FJ2+V(2)          FRE 550
FJ3=FJ3+V(3)          FRE 560
CONTINUE          FRE 570
CALL FUNA (XXE(I1),YYE(I1),ZZE(I1),VI(1),VI(2),VI(3))          FRE 580
FJ1=FJ1+V(1)          FRE 590
FJ2=FJ2+V(2)          FRE 600
FJ3=FJ3+V(3)          FRE 610
CONTINUE          FRE 620
VTDL(I,1)=VTDL(I,1)-FJ1          FRE 630
VTDL(I,2)=VTDL(I,2)-FJ2          FRE 640
VTDL(I,3)=VTDL(I,3)-FJ3          FRE 650
* * * * *          FRE 660
REWIND 4          FRE 670
CALL SKIPR (6,I)          FRE 680
* * * * *          FRE 690
CONTINUE          FRE 700
YI=-YI          FRE 710
NCT1=NCT1+1          FRE 720
IF (NCT1.GT.I1) GO TO 80
DO 70 I=1,NSW1          FRE 730
C(I)=VTDL(I,1)
CJ(I)=VTDL(I,2)
CK(I)=VTDL(I,3)
70 CONTINUE          FRE 740
          FRE 750
          FRE 760
          FRE 770
          FRE 780
          FRE 790
GO TO 10

```

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FRE 800  
FRE 810  
FRE 820  
FRE 830  
FRE 840  
FRE 850  
FRE 860-

C      TOTAL INDUCED VELOCITY  
      DO 90 I=1,NSW1  
      CI(I)=8\$004P\*(CI(I)+VIDL(I,1))  
      CJ(I)=8\$004P\*(CJ(I)-VIDL(I,2))  
      CK(I)=8\$004P\*(CK(I)+VIDL(I,3))  
      RETURN  
      END  
90

```

SUBROUTINE FUNA (XT, YT, ZT, FJ1, FJ2, FJ3)
C
C INDUCED VELOCITY DUE TO A VORTEX ELEMENT OF UNIT STRENGTH TRAILINGFUN 20
C FROM (XT, YT, ZT) TO INFINITY FUN 30
COMMON /ALLRA/ AA(21),BETA2,TANPH1,B2PH1,AB,D4,AC(2),D4S02 FUN 40
COMMON /XIVIZI/ XI,YI,ZI FUN 50
DIMENSION A(3), B(3), C(3) FUN 60
A(1)=XT-XI FUN 70
A(2)=YT-YI FUN 80
A(3)=ZT-ZI FUN 90
B(1)=XT+1-XI FUN 100
B(2)=YT-YI FUN 110
B(3)=ZT+TANPH1-ZI FUN 120
CALL CRSPPD (A,B,C)
CC=SOR(T(C(1)*C(1)+C(2)*C(3)*C(3)))
IF (CC.LE.(1.E-10)) GO TO 10
D5=2.*((R2PH1*(ZT-ZI-XT*TANPH1)-XI)
D6=XI*X1+RETA2*((YI-YT)**2+(ZT-ZI-XT*TANPH1)**2)
Q=4.*D4*D6-D5*D5
IF (0.LE.(1.E-10)) GO TO 10
RR=SQR(T(D4*XT*XT+D5*XT+D6))
FJ4=2.*((D4S02-(2.*D4*XT*D5)/RR)/Q
FJ1=(YT-YI)*TANPH1*FJ4
FJ2=(ZT-ZI*(XI-XT)*TANPH1)*FJ4
FJ3=-(YT-YI)*FJ4
RETURN
FJ1=0.
FJ2=0.
FJ3=0.
RETURN
END

```

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```
SUBROUTINE INFL2 (X1,Y1,Z1,X2,Y2,Z2,VACL)
  INDUCED VELOCITY DUE TO A VORTEX ELEMENT OF UNIT STRENGTH LYING
  BETWEEN (X1,Y1,Z1) AND (X2,Y2,Z2)
  COMMON /ALLRA/ AA(20),BETA
  COMMON /XYIZI/ XI,YI,ZI
  DIMENSION VAI(3),VL(3),VAP(3),VBP(3),VLP(3),VACL(3),VAPCLP(3)
  INF 10
  INF 20
  INF 30
  INF 40
  INF 50
  INF 60
  INF 70
  INF 80
  INF 90
  INF 100
  INF 110
  INF 120
  INF 130
  INF 140
  INF 150
  INF 160
  INF 170
  INF 180
  INF 190
  INF 200
  INF 210
  INF 220
  INF 230
  INF 240
  INF 250
  INF 260
  INF 270
  INF 280
  INF 290
  INF 300
  INF 310
  INF 320
  INF 330
  INF 340
  INF 350
  INF 360
  INF 370
  INF 380
  INF 390
  INF 400
C
C
  VAI(1)=X1-X1
  VAI(2)=Y1-Y1
  VAI(3)=Z1-Z1
  VL(1)=X2-X1
  VL(2)=Y2-Y1
  VL(3)=Z2-Z1
  VAP(1)=VAI(1)
  VAP(2)=BETA*VAI(2)
  VAP(3)=BETA*VAI(3)
  VBP(1)=X2-X1
  VBP(2)=BETA*(Y2-Y1)
  VBP(3)=BETA*(Z2-Z1)
  VLP(1)=VL(1)
  VLP(2)=BETA*VL(2)
  VLP(3)=BETA*VL(3)
  CALL CRSPRD (VAI,VL,VACL)
  CALL CRSPRD (VAP,VLP,VAPCLP)
  CALL DOTPRD (VAPCLP,VAPCLP,DAPCLP)
  IF (AABS(DAPCLP).LT.(1.E-10)) GO TO 10
  CALL DOTPRD (VBP,VBP,DBPLP)
  BPLPD= SORT(DBPLP)
  CALL DOTPRD (VAP,VAP,DAPLP)
  DAPLP=DAPLP/APMND
  CONST=(DAPLP-DAPLP)/DAPCLP
  GO TO 20
  CONST=0.
  CONTINUE
  VACL(1)=VACL(1)*CONST
  VACL(2)=VACL(2)*CONST
  VACL(3)=VACL(3)*CONST
  10
  20
```

**RETURN  
END**

**INF 410  
INF 420-**

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SUBROUTINE NEWVEL (C, THETP, XEE, YEE, ZEE, XTE, YTE, COMS, DUMMY, COVEL
INI, CONJ, CONK, SI, NSW1, NCW, NWNG, CI, CJ, CK, XLE, UU, VV, WW, CPCW1, XCP, YCP, VEL
2GAMA, YMA)
C
C EVALUATES TOTAL VELOCITY AT POINT (XEE, YEE, ZEE)
COMMON /ALLRA/ AA(17), SINAA, COSA, AB(15), BS004P
COMMON /GM/ ITER, L1, L2, L3, L4, L5, L6, L7, LB
DIMENSION DUMMY(11), CONI(11), CONK(11), CONL(11), CII(11), CJ(11), CPCW1(11), YEL
1, C(11), THETP(11), XTÉ(11), XLE(11), YLE(11), SI(11), CPCW1(11), VEL
2, XCP(11), YCP(11), GAMAI(11), YM(11), XNWNG(21), YNWNG(21), NP(4), VEL
3U(4,3), V(3)1
C
C IF POINT IS IN THE WING PLANE, THE REGULAR METHOD FOR VELOCITY
C EVALUATION IS USED.
IF (ZEE .LE. 0.00001) GO TO 110
IF (YEE .GT. YM(NSW1)) GO TO 110
CH1=XTE(11)-XLE(11)
CH2=XTE(21)-XLE(21)
XY=XLE(11)*(YEE-YLE(11))*(CH2-CH1)/(YLE(21)-YLE(11))
CHY=CH1+(YEE-YLE(11))*(CH2-CH1)/(YLE(21)-YLE(11))
XC=(XEE-XLY)/CHY
IF ((XC .LT. 0.0 .OR. XC .GT. 1.0)) GO TO 110
ZC=ZEE/CHY
C
C IF THE POINT (XEE, YEE, ZEE) IS AT Z(CSOLCA) LESS THAN ZTOL, THE
C VELOCITY IS OBTAINED BY LINEAR INTERPOLATION OF THE VELOCITIES
C CALCULATED ABOVE FOUR WING CONTROL POINTS AMONG WHICH THE POINT ISVEL
C LOCATED. BY NUMERICAL EXPERIMENTATION ZTOL HAS BEEN OBTAINED TO BEVEL
C 0.2.
ZTOL=0.2
IF ((ZC .GE. ZTOL)) GO TO 110
I=1
DO 10 I=I+1
IF (I .LT. NSW1) GO TO 10
IF (YEE .LE. YYM(I)) GO TO 20
IF (YEE .GT. YYM(I).AND. YEE .LE. YYM(I+1)) GO TO 20
IF ((C .LT. NCW) GO TO 30
IF ((C .GT. CPCW1(I))) GO TO 50
IF ((C .GT. CPCW1(J)).AND. XC .LE. CPCW1(J+1)) GO TO 40
NP(1)=I-1+NCW+j
NP(2)=NP(1)+1
J=J+1
10 VEL 300
VEL 310
VEL 320
VEL 330
VEL 340
VEL 350
VEL 360
VEL 370
VEL 380
VEL 390
VEL 400

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OVERLAY (LEVSP,1,0)
PROGRAM GEOM
DEFINES THE WING AND FREE ELEMENT GEOMETRY
C MAXIMUM VALUES
C NCW = 9
C ** NNCW = NCW+1 = 10
C ** NSW = 20
C ** NSW1 = NSW-1 = 19
C ** NWNG = NNCW+NSW1 = 190
C ** NCPTTL = (NNCW+1)*NSW1 = 209
COMMON XXL(2),XXT(2),YL(2),CPCWL(10),CPCW1(10),SI(10),SN(10),SNN(10)
10),SWP(10),SLOPE(10),XL(2,10),C(19),THETP(19),CONS(19),CPWSW1(19),XGE
2LM(19),XTM(19),YLM(19),CTT(19),CPWSW1(20),XLE(20),YLE(20),XTE(20),Y
3AVWNG(190),YAVWNG(190),XN(190,2),YN(190,2),XCP(209),YCP(209),R(10),G
420),Y(10,20)
COMMON /ALLRA/,ALLRA,TTL(16),ALPHA,SINA,COSA,SMPLE,BETA,BETAZ,TANPH1,82PG
1H1,BSQD4P,D4,CON,PI,D4SQ2,CBAR,HALFB,AREA
COMMON /XSTN/,XARR(25),NBRR
THEND=SHEND
***** ****
C READ (5,130) TTL
IF (TTL(1).EQ.THEND) GO TO 120
READ (5,160) NCW,NSW,NBRR,NCONTS,MITER,IPUNCH
NSW1=NSW-1
READ (5,150) (XXL(I),XXT(I),YL(I),I=1,2)
READ (5,150) ALPHA,AMACH,DELTA,DL,XEND,CBAR,AREA
READ (5,150) (YBRR(I),I=1,NBRR)
READ (5,150) (CTT(I),I=1,NSW1)
***** ****
C WRITE (6,170) TTL
WRITE (6,160) NCW,NSW,NBRR,NCONTS,MITER,IPUNCH
WRITE (6,150) (XXL(I),XXT(I),YL(I),I=1,2)
WRITE (6,150) ALPHA,AMACH,DELTA,DL,XEND,CBAR,AREA
WRITE (6,150) (YBRR(I),I=1,NBRR)
WRITE (6,150) (CTT(I),I=1,NSW1)
NCW=NCW
NCW=NNCW+1
C NPRCY=0, USED FOR BOUND ELEMENTS = (NCW+1)
C NPRCY=1, USED FOR BOUND ELEMENTS = NCW
C

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```
      WRITE (1) (CTT(I), I=1,NSW1)
      WRITE (1) (CPCL(I), I=1,NCW)
      CALL FRELM (XXL,XXT,YL,XLE,XTE,YLE,PI,NCWL,NSW1,XEND,DELTA,ALPHA,DGE01250
      IL,NCNTS)
      RETURN
      WRITE (6,140)
      STOP
C
      120 FORMAT (6,140)
      130 FORMAT (16A5)
      140 FORMAT (1H1,/,10X,19HALL CASES COMPLETED)
      150 FORMAT (8F10.5)
      160 FORMAT (10I5)
      170 FORMAT (1H1,/,17W INPUT DATA CARDS/,16A5)
      END
      GEO1190
      GEO1200
      GEO1210
      GEO1220
      GEO1230
      GEO1240
      GEO1250
      GEO1260
      GEO1270
      GEO1280
      GEO1290
      GEO1300
      GEO1310
      GEO1320
      GEO1330
      GEO1340
      GEO1350
      GEO1360-
```

```

C          SUBROUTINE PNLWNG (NSW,LPANEL,NCW)
C          GENERATES THE GRID OF BOUND AND TRAILING VORTEX ELEMENTS
COMMON XXL(2),XXT(2),YL(2),CPCWL(10),CPCWL(110),SI(10),SN(10),SNN(10),
10, SWP(10),SLNPE(10),XL(2,10),C(19),THETP(19),CONS(19),CPSW1(19),XPNL
2LM(19),XTM(19),YLM(19),CTT(19),CPSWL(20),XLE(20),XTE(20),YLE(20),XPNL
3AWNG(190),YAWNG(190),XN(190,2),YN(190,2),XCP(209),YCP(209),X(10,PNL
420),Y(10,20)
DO 10 I=1,2
D=XXT(I)-XXL(I)
DC 10 J=1,NCW
XL(I,J)=XXL(I)+CPCWL(J)*D/100.
SPAN=YL(2)-YL(1)
DO 20 I=1,NCW
SLNPE(I)=(XL(2,I)-XL(1,I))/SPAN
SWP(I)=ATAN(SLNPE(I))
DO 30 K=1,NSW
YK=CPSWL(K)*SPAN/100.
YL1=YL(1)+YK
DO 30 J=1,NCW
Y(J,K)=YL1
X(J,K)=XL(1,J)+SLOPE(J)*YK
NSW1=NSW-1
XLE(1)=XXL(1)
XT(1)=XXT(1)
YLE(1)=Y(1,1)
DLE=(XXL(2)-XXL(1))/SPAN
DTE=(XXT(2)-XXT(1))/SPAN
DO 40 I=2,NSW
YLE(I)=Y(1,I)
YLM(I-1)=YLE(1)+CPSW1(I-1)*SPAN/100.
DLE=DLE*(Y(I,I)-Y(I,I-1))
DTE=DTE*(Y(I,I)-Y(I,I-1))
XLE(I)=XLE(I-1)+DLE
XT(I)=XT(I-1)+DTE
XLM(I-1)=XLE(1)+CPSW1(I-1)*DLE/100.
XTM(I-1)=XT(1)+SPAN*CPSW1(I-1)*DTE/100.
DO 50 K=1,NSW1
NP=(K-1)*NCW
CC=XTM(K)-XLM(K)
DO 60 J=1,NCW

```

```

10
PNL 20
PNL 30
PNL 40
PNL 50
PNL 60
PNL 70
PNL 80
PNL 90
PNL 100
PNL 110
PNL 120
PNL 130
PNL 140
PNL 150
PNL 160
PNL 170
PNL 180
PNL 190
PNL 200
PNL 210
PNL 220
PNL 230
PNL 240
PNL 250
PNL 260
PNL 270
PNL 280
PNL 290
PNL 300
PNL 310
PNL 320
PNL 330
PNL 340
PNL 350
PNL 360
PNL 370
PNL 380
PNL 390
PNL 400

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NPANEL=NP+J
XCP(INPANEL)=XL M(K)+CC*CPCWL(J)/100.
YCP(INPANEL)=YL M(K)
XAVNG(INPANEL)=XL M(K)+CC*CPCWL(J)/100.
YAVNG(INPANEL)=YL M(K)
DO 50 I=1,2
KI=K+I-1
XN(INPANEL,I)=X(J,KI)
YN(INPANEL,I)=Y(J,KI)
CONTINUE
LPANEL=NPANEL
DO 70 K=1,NSW1
NP=LPANEL+K
XCP(NP)=XL M(K)
YCP(NP)=YL M(K)
RETURN
END
50
60
70
```

```

SUBROUTINE FRELN (XXL,XXT,YL,XLE,XTE,YLE,PI,NCW1,NSW1,XEND,DELTA,AFLM
1  ALPH,OL,NCONT)
C   FINDS THE INERTIAL COORDINATES OF FREE VORTEX ELEMENTS
COMMON /ALLR/ XE(40),YE(40),XXE(30),YYE(30),ZZE(30),ZMIN,NFLM
1ELM(11),NNELM(12)
COMMON /XPLOT/ XMN,YMN,XMN,YMX,ZMX
DIMENSION XXL(1), XXT(1), YL(1), XLE(1), XTE(1), YLE(1)
AHP1=ALPHA
ALP=ALPHA*180./PI
IF (ALP.LE.15.) AHP1=(22.5-0.5*ALP)*PI/180.
NSW=NSW1+1
THT1=PI/(FLOAT(2*NCW1))
CPC=0.5*(1.-COS(THT1))
ZMIN=.XTE(1)-XLE(1)*TAN(AHP1)/10.
SAHPI=SIN(AHP1)
CAHPI=COS(AHP1)
REWIND 2
REWIND 4
C   EVALUATION OF COORDINATES OF LEADING-EDGE ELEMENTS
DO 30 I=1,NSW1
XE(1)=XTE(I+1)
YE(1)=YLE(I+1)
ZE(1)=0.
XE(2)=XLE(I+1)+CPC*(XTE(I+1)-XLE(I+1))
YE(2)=YLE(I+1)
ZE(2)=0.
XE(3)=XLE(I)+CPC*(XTE(I)-XLE(I))
YE(3)=YLE(I)
ZE(3)=0.
XE(4)=XLE(I)
YE(4)=YLE(I)
ZE(4)=0.
XE(5)=XLE(I)-0.05*(XTE(I)-XLE(I))
IF (I.EQ.1) XMN=XE(5)
YE(5)=YLE(I)
ZE(5)=0.
XE(6)=XE(4)+0.05*(XTE(I)-XLE(I))
YE(6)=YLE(4)
ZE(6)=ZMIN
J=6

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```

FLM 410
FLM 420
FLM 430
FLM 440
FLM 450
FLM 460
FLM 470
FLM 480
FLM 490
FLM 500
FLM 510
FLM 520
FLM 530
FLM 540
FLM 550
FLM 560
FLM 570
FLM 580
FLM 590
FLM 600
FLM 610
FLM 620
FLM 630
FLM 640
FLM 650
FLM 660
FLM 670
FLM 680
FLM 690
FLM 700
FLM 710
FLM 720
FLM 730
FLM 740
FLM 750
FLM 760
FLM 770
FLM 780
FLM 790

XE(7)=XE(6)+DELTA*CAHPI
YE(7)=YE(6)
ZE(7)=ZE(6)+DELTA*SAHPI
IF ((I.EQ.1)) GO TO 20
J=7
    XE(J+1)=XE(J)+DELTA
    YE(J+1)=YE(J)
    ZE(J+1)=ZE(J)
    IF (XE(J+1).GE.XEND) GO TO 20
    J=J+1
    GO TO 10
10   NELM(I)=J+1
    K=NELM(I)
    C
    IF (NCONT.NE.0) WRITE (2) (XE(J),YE(J),ZE(J),J=1,5)
    WRITE (4) K,(XE(J),YE(J),ZE(J),J=1,K)
    C
    NMAX=0
    DO 40 I=1,NSW1
    IF (NMAX.LT.NELM(I)) NMAX=NELM(I)
    EVALUATION OF COORDINATES OF WAKE ELEMENTS
    40  0 70 I=1,NSW
        XE(I)=XTE(I)
        YE(I)=YTE(I)
        ZE(I)=0.
        XXF(2)=XXE(1)+(XXT(1)-XXL(1))/10.
        YYE(2)=YYE(1)
        ZZEE(2)=ZZE(1)
        XXE(3)=XXE(2)+(XXT(1)-XXL(1))/10.
        YYE(3)=YYE(2)
        ZZEE(3)=ZZE(2)
        J=3
        IF (XXE(I).GE.XEND) GO TO 60
        XXE(I+1)=XXE(I)+DL
        YYE(I+1)=YYE(I)
        ZZEE(I+1)=ZZE(I)
        J=J+1
        GO TO 50
      NELM(I)=J

```

```

C          K=J
C          IF (NCONTS.NE.0) WRITE (2) (XXE(J),YYE(J),ZZE(J),J=1,2)
70        WRITE (4) K,(XXE(J),YYE(J),ZZE(J),J=1,K)
C          NNMAX=0
DO 80 I=1,NSW1
  IF (NNMAX.LT.NNELM(I)) NNMAX=NNELM(I)
C          WRITE (4) NNMAX,NNMIN,ZMIN,NCONTS
C          XINT=XEND-XMN
XMX=XEND
XMM=XEND+0.20*XLNT
YMN=0.
YMX=YL(2)
ZMN=-YL(2)/4.
ZMX=YL(2)/2.
IF (NCONTS.EQ.0) GO TO 130
      READS LOCATION OF LEADING-EDGE ELEMENTS FROM INPUT DATA CARDS
C          *****
C          REWIND 2
REWIND 2
READ (5,160) (NNELM(I),I=1,NSW1)
DO 90 I=1,NSW1
  K=NNELM(I)
  READ (5,150) ((X1,J=1,5),(YE(J),J=6,K))
  READ (5,150) ((Y1,J=1,5),(ZE(J),J=6,K))
  READ (5,150) ((Z1,J=1,5),(ZE(J),J=6,K))
  READ (2) ((XE(J),YE(J),ZE(J),J=1,5))
  WRITE (4) K,(XE(J),YE(J),ZE(J),J=1,K)
90        READS LOCATION OF WAKE ELEMENTS FROM INPUT DATA CARDS
READ (5,160) (NNELM(I),I=1,NSW1)
DO 100 I=1,NSW
  K=NNELM(I)
  READ (5,150) (((X1,J=1,2),(XXE(J),J=3,K)))
  READ (5,150) (((Y1,J=1,2),(YYE(J),J=3,K)))
  READ (5,150) (((Z1,J=1,2),(ZZE(J),J=3,K)))
  READ (2) (XXE(J),YYE(J),ZZE(J),J=1,2)

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100  WRITE (6, K, (XXF(J), YYE(J), ZZE(J)), J=1,K)
      WRITE (6, NMAX, NMAX, ZMIN, NCNTS)
      REWIND 4
      WRITE (6, 160) (NELM(I), I=1,NSWI)
      DO 110 I=1,NSWI
      READ (6, 160) (XEM(J), YEM(J), ZEM(J), J=1,K)
      WRITE (6, 140) (XXE(J), YYE(J), ZZE(J), J=1,K)
      WRITE (6, 140) (YE(J), J=1,K)
      WRITE (6, 140) (ZE(J), J=1,K)
      WRITE (6, 140) (ZEM(J), J=1,K)
      WRITE (6, 160) (NELM(I), I=1,NSWI)
      DO 120 I=1,NSW
      READ (6, K, (XXE(J), YYE(J), ZZE(J)), J=1,K)
      WRITE (6, 140) (XXE(J), J=1,K)
      WRITE (6, 140) (YYE(J), J=1,K)
      WRITE (6, 140) (ZZE(J), J=1,K)
      WRITE (6, 170)
110   C *****
      RETURN
      C
120   C
130   C
140   FORMAT (14F9.4)
150   FORMAT (10F8.4)
160   FORMAT (10I2)
170   FORMAT (18H END OF INPUT DATA, //)
      END
```

```

OVERLAY (LEVSP,2,0)
PROGRAM PLOT
SETS UP DIMENSIONS FOR PLOTTING LEADING-EDGE AND WAKE ELEMENTS
COMMON DIL1
COMMON /ALLI/ NSW,NSW1
***** *****
REWIND 4
NN=NSW1+NSW
CALL SKIPR (4,NN)
READ (4) NMAX,NMAXX,ZMIN,NCOUNTS
***** *****
MXE=1
MYE=MXE+NNSW1+NMAX
MZE=MYE+NNSW1+NMAX
MNELM=MZE+NNSW1+NMAX
MNEXT=MNELM+NSW1
MNEXT=3*NNSW+NMAX-3*NMAX+NNSW
CALL PLOTT (D(MXE),0(MYE),D(MZE),D(MNELM),NSW1)
MXE=1
MYE=MXE+NNSW*(NNMAX+2)
MZE=MYE+NNSW*(NNMAX+2)
MNELM=MZZE+NNSW*(NNMAX+2)
MNEXT=MNELM+NSW
MNEXT=3*NSW*(NNMAX+2)+NSW+1
CALL PLOTT (D(MXE),0(MYE),D(MZE),D(MNELM),NSW1)
RETURN
END

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SUBROUTINE PLOTIT (XE,YE,ZE,NNM,NS)
C MANIPULATES LEADING-EDGE AND WAKE ELEMENTS COORDINATES IN A FORM
C SUITABLE FOR PLOTTING
COMMON /ALLI/ NSW,NSU,1
COMMON /XPLOT/ YMN,YNM,ZMN,XMX,YMX,ZMX
DIMENSION NNM(11), XE(NNS), YE(NNS), ZE(NNS), LABZ(11), PTT 20
DATA LABY/6*6H ,6HX V$ Y,6*6H ,2H /
DATA LABZ/6*6H ,6HX V$ Z,6*6H ,2H /
***** PTT 30
***** PTT 40
***** PTT 50
***** PTT 60
***** PTT 70
***** PTT 80
***** PTT 90
***** PTT 100
***** PTT 110
***** PTT 120
***** PTT 130
***** PTT 140
***** PTT 150
***** PTT 160
***** PTT 170
***** PTT 180
***** PTT 190
***** PTT 200
***** PTT 210
***** PTT 220
***** PTT 230
***** PTT 240
***** PTT 250
***** PTT 260
***** PTT 270
***** PTT 280
***** PTT 290
***** PTT 300
***** PTT 310
***** PTT 320
***** PTT 340
***** PTT 350
***** PTT 360
***** PTT 370
***** PTT 380
***** PTT 390
***** PTT 400

REWIND 4
IF (NS=50,NSU) GO TO 20
DO 10 I=1,NSW
READ (4) KK,(XF(I,J),YE(I,J),ZE(I,J),J=1,KK)
NNM(I)=KK
NC=4
LABY(8)=6H(LEAD)
LABY(9)=6HNG-FDG
LABY(10)=6HE ELEM
LABZ(11)=6HENTS1
LABZ(9)=6HLEAM1
LABZ(10)=6HNG-FDG
LABZ(11)=6HE ELEM
LABZ(11)=6HENTS1
GO TO 50
DO 30 I=1,NSU1
READ (4)
DO 40 I=1,NSW
READ (4) KK,(XF(I,J),YE(I,J),ZE(I,J),J=1,KK)
NNM(I)=KK
10
20
30
40
50

```

```

I=1
K=NNM(L)-NC
00 60 J=1,K
K=J+NC
XE(I,J)=XE(I,L,K)
XE(I,J+1)=XMN
YE(I,J)=YF(I,L,K)
ZE(I,J)=ZEN
ZE(I,K+1)=ZMN
XE(I,K+2)=XMK
YE(I,K+2)=YMX
ZE(I,K+2)=ZMX
NNM(I)=K+2
NS1=NS-1
CALL LNPL01 (XE,YE,NNM,NS1,NS,LAB81)
CALL LNPL01 (XE,ZE,NNM,NS1,NS,LAB82)
RETURN
END
PTT 410
PTT 420
PTT 430
PTT 440
PTT 450
PTT 460
PTT 470
PTT 480
PTT 490
PTT 500
PTT 510
PTT 520
PTT 530
PTT 540
PTT 550
PTT 560
PTT 570
PTT 580
PTT 590

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50   IF (TOP.GE.ZMAX) GO TO 60
      TOP=TOP+RANGE
      GO TO 50
      CONTINUE
50     IF (KEY.EQ.2) GO TO 70
      KEY=2
      ZMAX=YMAX
      ZMIN=YMIN
      YINC=0.01*(TOP-ROTTOP)
      XINC=YINC*SCALE
      XROT=BOTTOM*SCALE
      GO TO 20
20     CONTINUE
      YINC=0.0125*(TOP-BOTTOM)
      YLOW=TOP+YINC
      YHIGH=YLOW-YINC
      WRITE (6,160)
      KEY=5
      CONTINUE
80     DO 90 IJ=2,101
      90   ALINE(IJ)=BLANK
      YHIGH=YLOW
      YLOW=YHIGH-YINC
      YHS=SCALE*YHIGH
      YLS=SCALE*YLOW
      DO 110 I=1,M
      N=NELM(I)-2
      DO 110 J=1,N
      IF ((Y(I,J).GT.YHS.OR.Y(I,J).LE.YLS)) GO TO 110
      INDEX=(X(I,J)-XBOT)/XINC
      INDEX=INDEX+1
      IF (INDEX.GT.101) INDEX=101
      IF (ALINE(INDEX).NE.BLANK) GO TO 100
      ALINE(INDEX)=SYM(I)
      GO TO 110
100   ALINE(INDEX)=PLUS
      CONTINUE
110   ALINE(1)=UP
      IF (KEY.NE.5) GO TO 120

```

```

TPP=TOP*SCALE
WRITE (6,170) TPP,ALINE
GO TO 130
WRITE (6,180) ALINE
120  CONTINUE
KEY=KEY-1
IF (KEY.EQ.0) KEY=5
TOP=TOP-YINC
IF (TOP.GE.BOTTOM) GO TO 80
IF (KEY.NE.4) GO TO 80
WRITE (6,210) YAXIS
XINC=10.0*XINC
ALINE(1)=XBOT
DO 140 I=2,11
ALINE(I)=ALINE(I-1)+XINC
WRITE (6,190) (ALINE(I),I=1,11)
C   WRITE (6,200) (LABEL(I),I=1,14)
150  RETURN
C
160  FORMAT (1HL,/ )
170  FORMAT (F10.3,1X,10IA1)
180  FORMAT (11X,10IA1)
190  FORMAT (5X,11F10.3)
200  FORMAT (//,20X,13A6,A2)
210  FORMAT (11X,10IA1)
END
LNP1060-

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```

OVERLAY FILESPR,3,0)
PROGRAM SOLN
SETS UP DIMENSIONS FOR SOLVING THE STRENGTHS OF WING AND LEADING-
EDGE VORTEX SYSTEM
COMMON D(11) COMMON /ALL1/ NSW,NSW1,NCHW,NWNG,NCPTTL
LC=1 LTHTETP=LCPML+NSW1
LXTE=LTHETP+NSW1
LXLE=LXTE+NSW
LYLE=LXLE+NSW
LCNS=LXLE+NSW
LCTT=LCONS+NSW1
LCPML=LCTT+NSW1
LCPSW=LCPML+NSW
LSI=LCPSW+NSW1
LSN=LSI+NSW
LXN=LCP+NCPTTL
LYCPL=LYC+NCPTTL
LYCPL=LYC+NWNG
LCON=LCONJ+NWNG
LCOK=LCONK+NWNG
LCI=LCOK+NWNG
LCJ=LCI+NWNG
LCK=LCK+NWNG
LDUMY=LCK+NWNG
LNEXT=LNEXT+1)*#2/4
MNEXT=LNEXT+1)*#2/4+10*NWNG+10*NSW+3*NCHW-6
MNEXT=MNEXT+(NCPTTL+1)*#2/4+10*NWNG+10*NSW+3*NCHW-6
MNEXT=(NCPTTL+1)*#2/4+10*NWNG+10*NSW+3*NCHW-6
CALL AERODN (NWNG,D(LC),DLTHETP),DLXTE),DLRXL(E),DLCONSI),DLCONI),DLCONJ),DLCONK),DLCPML),DLCPWT),
1,DLISI),DLISN),DLXCD),DLXCP),DLYCD),DLYCP),DLYCN),DLYN),DLXN),DLYH),DLCH),DLCK),DLCLCJ),DLCLCTT),DLCLPSW),
2CONK),DLCLCJ),DLCLCTT),DLCLPSW),DLCLPSW),DLCLPSW),DLCLPSW),DLCLPSW),DLCLPSW),DLCLPSW),DLCLPSW),
RETURN
END

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SUBROUTINE AERODN (NHNG,C,THETP,XTE,XLE,YLE,CONS,SI,SN,XCP,YCP,XN,AER
10
1YN,CONI,CONJ,CONK,CJ,CK,DUMMY,CT,CP,JL,CPSW1) AER
20
C   SOLVES FOR THE STRENGTHS OF WING AND LEADING-EDGE WATERTEX SYSTEM    AER
30
COMMON /ALLI/ NSW,NSW1,NCW,NWCPT1L AER
40
COMMON /ALLRA/ AA(17),SINAP,AD(6),BSQD4P AER
50
COMMON /GM/ ITER,L1,L2,L3,L4,L5,L6,L7,L8 AER
60
COMMON /NCTT/,NCT,NCON AER
70
DIMENSION C(1),THETP(1),XTE(1),YLE(1),CONS(1),SI(1),AER
80
1SN(1),XCP(1),YCP(1),DUMMY(1),CONI(1),CONJ(1),CPSW1(1),YN(WNG,2),AER
90
2 C(1),CK(1),CT(1),CPCW(1),CPSW1(1),YN(WNG,2),AER
100
C ****
REWIND 1
REWIND 2
REWIND 3
CALL SKIPR (1,5)
READ (1) (C(1),I=1,NSW1)
READ (1) (THETP(1),I=1,NSW1)
READ (1) (XTE(1)*YLE(1),I=1,NSW1)
CALL SKIPR (1,1)
READ (1) (CONS(1),I=1,NSW1)
READ (1) (SI(1),SN(1),I=1,NCW)
READ (1) (XCP(1),YCP(1),I=1,NCPT1L)
READ (1) ((XN(1),J1,YN(1),J2),I=1,2),I=1,NCW
READ (1) (CT(1),I=1,NSW1)
READ (1) (CPCW(1),I=1,NCW)
CALL SKIPR (1,2)
READ (1) (CPSW1(1),I=1,NSW1)
READ (1) (L1=L1+NWN
C   INFLUENCE COEFFICIENT INITIALIZATION 3270
L1=L1+NWN
L2=L2+NWN
L3=L3+NWN
L4=L4+NWN
L5=L5+NWN
L6=L6+NWN
L7=L7+NWN
L8=L8+NWN
L9=L9+NWN
NCN=0
NCT=0
DO 13 I=1,NCPT1L
      
```

```

AER 410
ZCP=0.
CALL VDTWNG (C,THETP,XCP(I),YCP(I),ZCP(I),ZC2,XN,YN,XTE,YLE,CONS,DUMMY(LLAER 420
1),DUMMY(L2),DUMMY(L3),DUMMY(L4),DUMMY(L5),DUMMY(L6),DUMMY(L7),DUMMAER 430
2Y(L9),CONI,CONJ,CONK,SIN,NSWI,NCW,NWNG)
WRITE (2) (CONK(J),J=1,NWNG)
CALL VDTFRE (XCP(I),YCP(I),ZCP(I),ZC2,CJ,CK,NSWI,BSOD4P,XLE,YLE)
WRITE (3) (CK(J),J=1,NSWI)

10 CONTINUE
      C GAMA-EVALUATION
      REWIND 2
      REWIND 3
      READ (2) (CONI(I),I=1,NWNG)
      NWNG1=NWNG+1
      NWNB=NWNG+NSWI
      NWNB1=NWNB+1
      READ (3) (CONI(I),I=NWNG1,NWNB)
      CONI(NWNB1)=SINA
      IJ=1
      DO 20 I=1,NWNB
      CJ(I)=-CONI(I+1)/CONI(I)
      IJ=2
      NJ=NWNB-1
      CONTINUE
      READ (2) (CONI(I),I=1,NWNG)
      READ (3) (CONI(I),I=NWNG+1,NWNB)
      CONI(NWNB1)=SINA
      IF ((IJ.GT.NWNG) .AND. (IJ.LT.NWNB)) THEN
      CALL VNSEQN (NJ,IJ,CONI,CJ,CONK)
      IJ=IJ+1
      NJ=NJ-1
      IF ((IJ.LE.NWNB) .AND. (IJ.GT.NWNG))
      WRITE (6,80)
      DO 40 I=1,NSWI
      DO 40 J=1,NCW
      N2=(I-1)*NSWI+J
      WRITE (6,100)
      DO 50 I=1,NSWI
      J=NWNG+I

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```

50      WRITE (6,901) CPSW1(1),CJ(1)
      C      EVALUATION OF SECTIONAL LEADING-EDGE THRUST
      CALL THRST (CJ,CONI,CONJ)
      NERR=0
      DO 60 I=1,NSWI
      IF (ABS(CONJ(I)-CT(I)).GE.(1.0E-10)) NERR=1
      IF (NERR.EQ.1) WRITE (6,110)
      GMSUM=0.
      DO 70 I=2,NSWI
      KS=NWNGB+I
      GMSUM=GMSUM+CJ(IKS)
      C      ..... .
      REWIND 2
      WRITE (2) (CJ(I),I=1,NWNB)
      WRITE (7) GMSUM
      C      ..... .
      RETURN
      C
      60      FORMAT (1H1, //, 22H WING VORTEX STRENGTHS,/, 22H ****
      1***, /, 29H X/C 2Y/3 SAMAY, /, 29H ****
      2 ***)
      70      FORMAT (3F10.5)
      80      FORMAT (1//, 32H LEADING-EDGE VORTEX STRENGTHS, /, 31H ****
      1***, /, 29H CAPSANA, /, 29H ****, /, 29H ****)
      90      FORMAT (1//, 34H ERROR IN SECTIONAL CALCULATION, /, 10F10.5)
      100     END
      110

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SUBROUTINE VMSEON (NC1,K,AA,CA)
C   SOLVES A SYSTEM OF SIMULTANEOUS EQUATIONS
C   DIMENSION AA(11), CA(11), AI(11)
NC=K*NC1
SUM1=0.
K1=K-1
JJ=1
DO 10 J=1,K1
    SUM1=SUM1+AA(J)*A(JJ)
    DO 30 I=1,NC1
        SUM2=SUM2+AA(I)*A(JI)
        JJ=JJ+NC1+1
        DO 20 J=1,K1
            SUM2=SUM2+AA(J)*A(JJ)
            KJ=JJ+NC1+1
            KK=K+I
            SUM2=SUM2+AA(KK)
            CA(I)=-(SUM2/SUM1)
            M=1
            L=0
            KNC=(K-1)*NC1
            DO 60 I=1,NC
                IF (II.GT.KNC) GO TO 50
                MM=(M-1)*NC1+1
                IF (II.EQ.MM) GO TO 70
                KK=KK+1
                II=II+L
                AI(I)=CA(KK)*BASE+AI(II)
                GO TO 60
            50   II=I-KNC
                AI(II)=CA(II)
            60   CONTINUE
                GO TO 80
            70   II=M-K-1
                BASE=A(II)
                K=K+1
                M=M+1
                L=L+1
                GO TO 10
        20   CONTINUE
        30   CONTINUE
    10   CONTINUE

```

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VHS 410  
VHS 420  
VHS 430  
VHS 440-

GO TO 40  
CONTINUE  
RETURN  
END

90

```

SUBROUTINE THRST (SGN,CONK,CT)
C
EVALUATES SECTIONAL LEADING-EDGE THRUST COEFFICIENTS
COMMON /ALLI/ NSW,NWNG,NCH,NWNG
COMMON /ALLRA/ AA(17),SINA,COSA,SINL,COSL,AL3,BETA2,AC15),PI
DIMENSION SGM(1), CONK(11), CT(11)
AM2=1-BETA2
FCOS=COS(SHPL)
FTAN=TAN(SHPL)
VARI=FLDAT(NCW)+SORT(FTAN*FTAN+BETA2)
VAR2=SORT(1.-AM2*FCOS*FCOS)
REWIND 2
REWIND 3
CALL SKIPR (2,NWNG)
CALL SKIPR (3,NWNG)
DO 30 I=1,NSW1
WL=0.
READ (2) (CONK(J),J=1,NWNG)
DO 10 J=1,NWNG
WL=WL+CONK(J)*SGM(J)
10 READ (3) (CONK(J),J=1,NSW1)
DO 20 J=1,NSW1
JJ=NWNG+J
WL=WL+CONK(J)*SGM(J)
20 THRT1=(WL+SINA)/VAR1
CT(1)= (PI/2.)*VAR2*THRT1*THR1/FCOS
30 RETURN
END

```

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## **OVERLAY (LEVSP,4,0) PROGRAM LOADS SETS UP DIMENSIONS FOR EVALUATING AERODYNAMIC CHARACTERISTICS**



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```
60      GML(I)=GAMA(NGI)*SURA/C(I)          COF 800
C      .....                                     COF 810
      REWIND 3          (GML(I),I=1,NSW1)      COF 820
      WRITE (3) (GML(I),I=1,NSW1)      COF 830
C      .....                                     COF 840
      TNSP=TAN(OSWP(I))      COF 850
      DO 70 II=1,NSW1      COF 860
      XEE=XAVWNA(I)      COF 870
      YEE=YAVWNA(I)      COF 880
      CALL NEWVEL(C,THETP,XEE,YEE,ZEE,XN,YN,XTE,YLE,CONS,DUMMY,CONI,CONC)DF 890
      1J,CONK,SI,NSW1,NCW,NWNG,C1,CJ,CK,XLE,UU,VV,WW,ADUM,BDUM,CDUM,GAMA,COF 900
      2YLM)      COF 910
      NWNGII=NWNG+II      COF 920
      GMY(NWNGII)=GML(II)*(UU-VV*TNSP)      COF 930
      CONTINUE      COF 940
      CALCULATION OF DCP-VALUES FOR WING POINTS      COF 950
      PN=PI/(FLOAT(NCW))      COF 960
      DO 80 I=1,NCW      COF 970
      W(I)=0.      COF 980
      WX(I)=XN(I,1)      COF 990
      WY(I)=YN(I,1)      COF1000
      DO 150 I=1,NSW1      COF1010
      DO 140 J=1,NCW      COF1020
      NP=(I-1)*NCW+J      COF1030
      VYY=VY(NP)      COF1040
      CPG=0.      COF1050
      CPH=0.      COF1060
      CPI=0.      COF1070
      DO 100 JJ=1,J      COF1080
      NPIN=(I-1)*NCW+JJ      COF1090
      IF (J.EQ.JJ) GO TO 130      COF1100
      CPG=CPG+GAMA(NPIN)*SI(JJ)
      GO TO 100      COF1110
      CPG=CPG+0.5*GAMA(NPIN)*SI(JJ)
      CONTINUE      COF1120
      130      COF1130
      CPI=0.      COF1140
      DO 100 JJ=1,J      COF1150
      NPIN=(I-1)*NCW+JJ      COF1160
      IF (I.EQ.NSW1) GO TO 130      COF1170
      DO 120 JJ=1,J      COF1180
      NPOT=I*NCW+JJ
```

```

IF (J.EQ.JJ) GO TO 110
CPH=CPH+GAMA(NPOT)*SI(JJ)
GO TO 120
CPH=CPH+0.5*GAMA(NPOT)*SI(JJ)

110 CONTINUE
CPH=CPH*PN*C(I+1)*VYY
CP1=2.*GAMA(NWNG*I)*VYY
N=(NP+NCW)=CPG+CPH+CP1
WX(NP+NCW)=XN(NP,2)
WY(NP+NCW)=YN(NP,2)
CONTINUE
120 CONTINUE
N3=NWNG+NCW+3
CALL SURFSET (N3,WX,WY,WN,C1)
DO 170 K=1,NCW
DO 160 J=1,NSW1
NP=(J-1)*NCW+K
DCP1=2.*GMY(NP)
XEE=XAWNG(NP)
YEE=YAWNG(NP)
CALL SURFORD (W,XEE,YEE,VV,VV,N3)
DCPD=VV/VLE(J)-VLE(J)
DCP(NP)=DCP1+DCPD
CONTINUE
140 CONTINUE
150 CONTINUE
N3=NWNG+NCW+3
CALL SURFSET (N3,WX,WY,WN,C1)
DO 170 K=1,NCW
DO 160 J=1,NSW1
NP=(J-1)*NCW+K
DCP1=2.*GMY(NP)
XEE=XAWNG(NP)
YEE=YAWNG(NP)
CALL SURFORD (W,XEE,YEE,VV,VV,N3)
DCPD=VV/VLE(J)-VLE(J)
DCP(NP)=DCP1+DCPD
CONTINUE
160 CONTINUE
170 CONTINUE
C CALCULATION OF INDUCED VELocities AT END-POINTS OF SOUND ELEMENTS
C NEAR LEADING-EDGE
C CPC=0.5*(1-COS(SINT(1,1)))
DO 180 I=2,NSW
XEE=EXLE(I)+CPG*(XTE(I)-XLE(I))
YEE=YLE(I)
CALL NEWVEL (C,THEIT2,THEET2,ZEE,XN,YN,XTE(YL),CNS,DUMM,Y,CNNI,CONCOF1500
1,J,CNX,S1,NSW1,NCW,NWNG,C1,XLE,I,DCP1+DCPD)
2YLM)
180 YL(I)=VV
C DC? -INTERPOLATION FOR SOUND ELEMENTS OF YING
C CALL INTGMY (NCW,NSW1,DCP,SNN,DCDEF,DUMM(I,1),DUMMY(INNCW))
C CALCULATION OF DECREASE IN DCP-VVALUES AT THE LEADING-EDGE
DCPA(I)=0.

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DCPA(NSW)=0.  
DO 190 I=2,NSW1  
DCPA(I)=2.*GAMA(NMNG+I)*VY(I)  
190 CONTINUE  
DO 200 I=1,NSW1  
CNC(I)=-2.*GMN(MNWG+I)  
200 CONTINUE C FINAL DCP-VALUES AT LARGER WING GRID  
DO 230 I=1,NSW1  
DO 220 J=1,NNCW  
NP=(I-1)*NNCW+J  
GMNW(NP)=CDEF(I,K+1)  
DO 210 K=1,NCW  
FK=K  
AM1=COS(FK*THT(J))  
AM2=AM1*CDEF(I,K+1)  
GMNW(NP)=GMNW(NP)/(SIN(THT(J)))  
IF (J.NE.1) GD TO 220  
NGI=NWNG+I  
GMNW(NP)=GMNW(NP)+CNC(I)  
210 CONTINUE  
220 CONTINUE NGI=NWNG+I  
DO 240 I=1,NMW  
DCP(I)=GMNW(I)  
PI=P1/12.*FLOAT(NNCW)  
WRITE(6,370)  
DO 250 I=1,NSW1  
DO 250 J=1,NNCW  
N2=(I-1)*NNCW+J  
C251=0.5*(1.-C3512.*FLOAT(I-1,)*P1J)  
230 CONTINUE  
240 CONTINUE  
250 WRITE(6,380) C251,C3512,C52111,DCP(NP)  
250 C252(J)=CDS((12.*FLOAT(I,J)-1.)*P1J)  
250 CL=0.  
CM=0.  
CD=0.  
C EVALUATION OF SECTIONAL AND TOTAL AERODYNAMIC CHARACTERISTICS  
COF1580  
COF1590  
COF1600  
COF1610  
COF1620  
COF1630  
COF1640  
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COF1670  
COF1680  
COF1690  
COF1700  
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COF1870  
COF1880  
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COF1900  
COF1910  
COF1920  
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COF1960
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CTT=0.          COF1970
DO 280 I=1,NSW1
SECCL(I)=0.      COF1980
SECCM(I)=0.      COF1990
PHII=PI*FLOAT(I)/FLOAT(NSW1)    COF2000
DO 270 J=1,NNCW   COF2010
NP=(I-1)*NNCW+J  COF2020
SECCL(I)=SECCL(I)+DCP(INP)*QI(J)  COF2030
SECCM(I)=SECCM(I)-DCP(INP)*QI(J)  COF2040
              COF2050
1R           COF2060
              COF2070
              COF2080
              COF2090
              COF2100
              COF2110
              COF2120
              COF2130
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              COF2180
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              COF2200
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              COF2220
              COF2230
              COF2240
              COF2250
              COF2260
              COF2270
              COF2280
              COF2290
              COF2300
              COF2310
              COF2320
              COF2330
              COF2340
              COF2350

270 CONTINUE
SECCL(I)=SECCL(I)*PI/(2.*FLOAT(NNCW))
SECCM(I)=SECCM(I)*PI/(2.*FLOAT(NNCW))
SECCD(I)=SECCD(I)*SINA-CT(I)*COSA
SECCL(I)=SECCL(I)*COSA+CT(I)*SINA
CL=CL+SECCL(I)*C(I)*SIN(PHI)
CM=CM+SECCM(I)*C(I)*SIN(PHI)
CD=CD+SECCD(I)*C(I)*SIN(PHI)
CTT=CTT+CT(I)*SIN(PHI)
CL=CONST*CL
CM=CONST*CM
CD=CONST*CD
CTT=CONST*CTT
C
      WRITE (7) CL,CM,CD,CTT
      WRITE (6,340) (I,SECCL(I),SECCM(I),SECCD(I),CTT),I=1,NSW1
      WRITE (6,350) CL,CM,CD,CTT
      NNCW1=NNCW+1
      CALL INTGMY (NNCW,NSW1,DCP,CNN,CDEF,DUMMY(1),DUMMY(NNCW1))
      REWIND 1
      CALL SKIPR (1,B)
      READ (1) (XL1(I),CI(I),I=1,NSW1)
      C
      EVALUATION OF DCP AT CONSTANT X LOCATIONS
      DO 330 K=1,NARR
      XBR=XARR(K)
      KY=1
      IF ((X3R.LT.XLM(KY)) GO TO 300
      KY=KY+1

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IF (KY.LE.NSW1) GO TO 290  
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SUBROUTINE INTGMY (INCW,NSW1,SGM,SNN,COEF,F,THETA)
C
SETS UP COEFFICIENTS OF A MATRIX FOR OCP-INTERPOLATION
DIMENSION SGM(11), SNN(11), F(11), THETA(11), COEF(NSW1,1)
PI=3.14159265
N1=NCW+1
FN=NCW
DO 40 I=1,NSW1
DO 10 J=1,NCW
NK=(I-1)*NCW+J
FJ=j
THETA(J)=(2.*FJ-1.)*PI/(2.*FN)
10   F(J)=SGM(NK)*SNN(J)
DO 30 J=1,N1
COEF(I,J)=0.
FJ=j
DO 20 K=1,NCW
COEF(I,J)=COEF(I,J)+F(K)*COS((FJ-1.)*THETA(K))
20   IF (J.EQ.1) COEF(I,J)=COEF(I,J)/FN
      IF (J.NE.1) COEF(I,J)=COEF(I,J)*2./FN
      CONTINUE
30   CONTINUE
40   RETURN
END
INT 10
INT 20
INT 30
INT 40
INT 50
INT 60
INT 70
INT 80
INT 90
INT 100
INT 110
INT 120
INT 130
INT 140
INT 150
INT 160
INT 170
INT 180
INT 190
INT 200
INT 210
INT 220
INT 230-

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C SUBROUTINE SURFSET (N3,X,Y,W,IWK)  
C SET UP PROGRAM FOR SURFACE SPLINE  
C WRITTEN BY - ROBERT N. DESMARais, STRUCTURES AND DYNAMICS DIV.  
C LANGLEY RESEARCH CENTER, HAMPTON, VA. 23665  
C DIMENSION X(1), Y(1), W(N3,1), IWK(1)  
E=1.E-10  
N2=1  
N=N3-3  
N1=N+1  
N2=N+2  
N4=N3+1  
RN=1./N  
N3Z=N3+N2  
N23=N2+3  
C COMPUTE SCALING PARAMETERS, UB,UX,UY,VB,VX,VY  
XB=0.  
YB=0.  
PXX=0.  
PXY=0.  
PYY=0.  
TH=0.  
DO 10 I=1,N  
XB=XB+X(I)  
YB=YB+Y(I)  
PXX=PXX+X(I)\*X(I)  
PXY=PXY+X(I)\*Y(I)  
PYY=PYY+Y(I)\*Y(I)  
XB=RN\*XB  
YB=RN\*YB  
PXX=RN\*PXX-X3\*Y3  
PXY=RN\*PXY-X3\*Y3  
PYY=RN\*PYY-Y3\*Y3  
IF (PXY.NE.0) TH=.5+ATAN2(2.+PXY,PXY-PXX)  
CT=COS(TH)  
ST=SIN(TH)  
C2=CT\*CT  
CS=2.\*CT\*ST  
S2=ST\*ST  
SU=1./SQRT(PXX+C2-PXY\*CS+PYY\*CS2)  
SY=1./SQRT(PXY+S2+PXY\*CS+PYY\*CS2)

10

SRF 10  
SRF 20  
SRF 30  
SRF 40  
SRF 50  
SRF 60  
SRF 70  
SRF 80  
SRF 90  
SRF 100  
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SRF 130  
SRF 140  
SRF 150  
SRF 160  
SRF 170  
SRF 180  
SRF 190  
SRF 200  
SRF 210  
SRF 220  
SRF 230  
SRF 240  
SRF 250  
SRF 260  
SRF 270  
SRF 280  
SRF 290  
SRF 300  
SRF 310  
SRF 320  
SRF 330  
SRF 340  
SRF 350  
SRF 360  
SRF 370  
SRF 380  
SRF 390  
SRF 400

```

UX=SU*CST          SRF 410
UY=-SU*SST         SRF 420
VX=SV*CST          SRF 430
VY=SV*SST          SRF 440
UB=-(UX*X*B+UY*Y*B) SRF 450
VB=-(VX*X*B+VY*Y*B) SRF 460
PUT Z INTO ITS W LOCATION
IZ=N*NZ            SRF 470
DO 30 J=N4,N32      SRF 480
DO 20 I=1,3          SRF 490
W(I,J)=0            SRF 500
SRF 510
SRF 520
SRF 530
SRF 540
SRF 550
SRF 560
SRF 570
SRF 580
SRF 590
SRF 600
SRF 610
SRF 620
SRF 630
SRF 640
SRF 650
SRF 660
SRF 670
SRF 680
SRF 690
SRF 700
SRF 710
SRF 720
SRF 730
SRF 740
SRF 750
SRF 760
SRF 770
SRF 780
SRF 790

C
IZ=IZ-1
W(I,J)=0
DO 30 I=4,N3
W(I,N3Z+N4-J)=W(IZ+1)
I2=IZ-1
PUT U,V (SCALED X,Y) INTO THEIR W LOCATIONS
DO 40 J=N1,N3
DO 40 I=1,3
W(I,J)=0
DO 50 J=1,N
JA=N4-J
W(JA,N1)=W(1,J)
W(2,J)=UB+UX*X(J)+UY*Y(J)
W(JA,N2)=W(2,J)
W(3,J)=VB+VX*X(J)+VY*Y(J)
W(JA,N3)=W(3,J)
DO 60 J=1,N
JB=N4-J
COMPUTE H MATRIX IN W
DO 60 I=4,JB
IB=N4-I
R2=(W(2,J)-W(2,IB))**2+(W(3,J)-W(3,IB))**2
W(I,J)=R2+ALOG(R2+E)
W(J3,IB)=W(I,J)
MATTINV IS THE SYSTEM LIBRARY ROUTINE FOR SOLVING LINEAR EQUATIONS
N31=N3+1
CALL MATTINV (N3,N3,W,1,W(1,N31),1,DET,ISC,INWK,INWK(N4))
PUT S,U,V IN LOW W
N(1,1)=N3*(1.0+N2)

```

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SRF 800
SRF 810
SRF 820
SRF 830
SRF 840
SRF 850
SRF 860
SRF 870
SRF 880
SRF 890
SRF 900
SRF 910
SRF 920
SRF 930
SRF 940
SRF 950
SRF 960
SRF 970
SRF 930-
W(2,1)=N
W(3,1)=E
DO 70 I=1,N
W(I+3,1)=0
W(I,2)=UB+UX*X(I)+UY*Y(I)
W(I,3)=VB+VX*X(I)+VY*Y(I)
70
W(N1,2)=UR
W(N2,2)=UX
W(N3,2)=UY
W(N1,3)=VR
W(N2,3)=VX
W(N3,3)=VY
IF (NZ.EQ.0) RETURN
DO 90 J=4,NZ
DO 80 I=1,N3
      LEFT SHIFT A,B MATRICES N COLUMNS
      W(I,J)=W(I,N+J)
80      RETURN
      END
```

70

C  
80

```

C          SUBROUTINE SURFORD (W,XP,YP,ZP,M3)
C          SURFACE SPLINE INTERPOLATION (COORDINATES)
C          WRITTEN BY - ROBERT N. DESHARAS, STRUCTURES AND DYNAMICS DIV.
C          LANGLEY RESEARCH CENTER, HAMPTON, VA. 23665
C          DIMENSION W(M3,1)
C          N=M3-3
C          N1=N+1
C          N2=N+2
C          N3=N+3
C          N4=N+4
C          U=W(N1,2)+W(N2,2)*XP+W(N3,2)*YP
C          V=W(N1,3)+W(N2,3)*XP+W(N3,3)*YP
C          ZP=W(N1,4)+W(N2,4)*U+W(N3,4)*V
C          DO 10 I=1,N
C          R2=(U-W(I,2))*#2+(V-W(I,3))*#2
C          ZP=ZP+W(I,4)*R2*ALNG(IR2+W(3,I))
C          RETURN
C          END

```

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```
      SUBROUTINE MATINV (MAX,N,A,B,IOP,DETERM,ISCALE,IPIVOT,TWK)
      MATRIX INVERSION WITH ACCOMPANYING SOLUTION OF LINEAR EQUATIONS
      PROVIDED BY - ANALYSIS AND COMPUTATION DIVISION
      LANGLEY RESEARCH CENTER
      HAMPTON, VA. 23665
      DIMENSION IPIVOT(N), A(MAX,N), B(MAX,N), WK(MAX,2)
      EQUIVALENCE (IROW,JROW), (ICOLUMN,JCOLUMN), (AMAX,T,SWAP)
      C
      C      INITIALIZATION
      C
      ISCALE=0
      R1=10.0**100
      R2=1.0/R1
      DETERM=1.0
      DO 10 J=1,N
      IPIVOT(J)=0
      DC 370 I=1,N
      C      SEARCH FOR PIVOT ELEMENT
      C
      AMAX=0.0
      DC 60 J=1,N
      IF (IPIVOT(J)-1) 20,60,20
      20  DO 50 K=1,N
          IF (IPIVOT(K)-1) 30,50,410
          30  IF (ABS(AMAX)-ABS(A(IJ,K))) 40,50,50
              IROW=J
              ICOLUMN=N
              AMAX=A(IJ,K)
              40  CONTINUE
              50  CONTINUE
              60  IF (AMAX) 80,70,80
                  70  DETERM=0.0
                  1SCALE=0
                  GO TO 410
                  410  IPIVOT(ICOLUMN)=IPIVOT(ICOLUMN)+1
                  80  IF (IROW-ICOLUMN) 90,130,90
                  90  INTERCHANGE ROWS TO PUT PIVOT ELEMENT ON DIAGONAL
                  C
                  C      IF (IROW-ICOLUMN) 90,130,90
                  C
      MAT 10
      MAT 20
      MAT 30
      MAT 40
      MAT 50
      MAT 60
      MAT 70
      MAT 80
      MAT 90
      MAT 100
      MAT 110
      MAT 120
      MAT 130
      MAT 140
      MAT 150
      MAT 160
      MAT 170
      MAT 180
      MAT 190
      MAT 200
      MAT 210
      MAT 220
      MAT 230
      MAT 240
      MAT 250
      MAT 260
      MAT 270
      MAT 280
      MAT 290
      MAT 300
      MAT 310
      MAT 320
      MAT 330
      MAT 340
      MAT 350
      MAT 360
      MAT 370
      MAT 380
      MAT 390
      MAT 400
```

```

90      DETERM=-DETERM
        DO 100 L=1,N
        SWAP=A(IRROW,L)
        A(IRROW,L)=ANICOLUM,L)
        ANICOLUM,L)=SWAP
        IF (1) 130,130,110
        100    A(ICOLUM,L)=SWAP
        IF (1) 130,130,110
        110    DO 120 L=1,M
        SWAP=q(IRROW,L)
        B(IRROW,L)=B(ICOLUM,L)
        B(ICOLUM,L)=SWAP
        120    IWK(i,1)=IRROW
        IWK(1,2)=ICOLUM
        PIVOT=ANICOLUM,ICOLUM)
        IF (102.EQ.1) GO TO 270
        IF (PIVOT) 140,70,140
        130

C      SCALE THE DETERMINANT
C
140    PIVOTT=PIVOT
        IF (ABS(DETERM)-R1) 170,150,150
        150    DETERM=DETERM/R1
        ISCALE=ISCALE+1
        IF (ABS(DETERM)-R1) 200,160,160
        160    DETERM=DETERM/R1
        ISCALE=ISCALE+1
        GO TO 200
        170    IF (ABS(DETERM)-R2) 130,130,200
        180    DETERM=DETERM*R1
        ISCALE=ISCALE-1
        IF (ABS(DETERM)-R2) 170,190,200
        190    DETERM=DETERM*R1
        ISCALE=ISCALE-1
        IF (ABS(PIVOTT)-R1) 230,210,210
        200    PIVOTT=PIVOTT/R1
        210    ISCALE=ISCALE+1
        IF (ABS(PIVOTT)-R1) 250,220,220
        220    PIVOTT=PIVOTT/R1
        ISCALE=ISCALE+1
        GO TO 240

```

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230 IF (ABS(PIVOTT)-R2) 240,240,260
240 PIVOTT=PIVOTT+R1
      ISCALE=ISCALE-1
      IF (ABS(PIVOTT)-R2) 250,250,260
250 PIVOTT=PIVOTT+R1
      ISCALE=ISCALE-1
      DETERM=DETERM+PIVOTT
C
C      DIVIDE PIVOT ROW BY PIVOT ELEMENT
C
270 IF (PIVOTT) 280,70,280
280 A(ICOLUMN,ICOLUMN)=1.0
      DO 290 L=1,N
      A(ICOLUMN,L)=A(ICOLUMN,L)/PIVOTT
290 IF (L) 320,320,300
      IF (L) 310,320,300
      DO 310 L=L+1,N
      B(ICOLUMN,L)=B(ICOLUMN,L)/PIVOTT
310
C      REDUCE NON-PIVOT ROWS
C
320 DO 370 L=1,N
      IF ((L-1)COLUMN) 330,370,330
330 T=A(L,L)
      A(L,L,COLUMN)=0.0
      DO 340 L=L+1,N
      A(L,L)=A(L,L)-A(ICOLUMN,L)*T
      IF (N) 370,370,350
      DO 360 L=L+1,N
      B(L,L)=B(L,L)-B(ICOLUMN,L)*T
      360 CONTINUE
370
C      INTERCHANGE COLUMNS
C
380 DO 400 I=1,N
      L=N+1-I
      IF (IWK(L,1)-IWK(L,2)) 390,400,330
      JACOM=IWK(L,1)
      JCOLUMN=IWK(L,2)
      DO 390 K=1,N

```

```
SWAP=A(K,JROW),
A(K,JROW)=A(X,JCOLUMN)
A(K,JCOLUMN)=SWAP
CONTINUE
CONTINUE
RETURN
END
```

390  
400  
410

```
MAT1190
MAT1200
MAT1200
MAT1210
MAT1220
MAT1230
MAT1240
MAT1250-
```

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```
OVERLAY (LEVSP,5,0)
PROGRAM NEWSHAP
SETS UP DIMENSIONS FOR COMPUTING THE NEW LOCATIONS OF LEADING-EDGE NSP 10
AND TRAILING-EDGE VORTICES BY MAKING THOSE FORCE-FREE NSP 20
COMMON D(1) NSP 30
COMMON /ALLI/ NSW,NSW1,NCH,NWNG,NCPTTL NSP 40
DIMENSION E(2400) NSP 50
***** NSP 60
REWIND 4 NSP 70
NN=NSW1+NSW NSP 80
CALL SKTPR (4,NN) NSP 90
READ (4) NMAX,NNMAX,ZMIN,NCNTS NSP 100
***** NSP 110
LC=1 NSP 120
LTHTP=LC+NSW1 NSP 130
LXN=LTHETP+NSW1 NSP 140
LYN=LXN+2*NWNG NSP 150
LXT=LXN+2*NWNG NSP 160
LXLE=LXTE+NSW NSP 170
LYLE=LXLE+NSW NSP 180
LCNS=LYLE+NSW NSP 190
LSI=LCNS+NSW NSP 200
LXCP=LSI+NSW NSP 210
LYCP=LYCP+NCPTTL NSP 220
LCI=LYCP+NCPTTL NSP 230
LCJ=LCI+NWNG NSP 240
LCK=LCK+NWNG NSP 250
LCONI=LCONI+NWNG NSP 260
LCONJ=LCONJ+NWNG NSP 270
LCONK=LCONK+NWNG NSP 280
LDUMY=LDUMY+8*NWNG NSP 290
LNELM=LNELM+NSW1 NSP 300
LGAMA=LNELM+NSW1 NSP 310
LGML=LGAMA+NCPTTL NSP 320
L'LM=LGML+NSW1 NSP 330
LCPW=LCPW+NSW1 NSP 340
LNEXT=LNEXT+NSW1 NSP 350
LNEXT=21*NWNG+14*NSW+NCW-9 NSP 360
MXE=1 NSP 370
NSP 380
NSP 390
NSP 400
```

C

```

MYE=MXE+NSW1*NMAX
MZE=MYE+NSW1*NMAX
MXE=MZE+NSW1*NMAX
MYE=MXE+NSW1*NMAX
MZE=MYE+NSW1*NMAX
MNEXT=MZE+NSW1*NMAX
MNEXT=3*NSW*NMAX-3*NMAX+3*NSW*NMAX+1
CALL NEWELM(0(LC1),0(LCX1),0(LCN1),0(LCNELM),0(LCPCW))
3(MYE),E(MZE),NSW,NCW,ZMIN,NMAX,NNMAX,NNMAX,NNMAX
2CONJ),D(LCONK),D(LDUMY),NNG,NCP TTL,E(MYE),E(MZE),E(MYE),E(MZE)
1,D(LCNS1),D(LS1),D(LXCP),D(LC1),D(LCJ),D(LCA),D(LCONI),D(LRN)
4NTS,D(LGAMA),D(LGM1),D(LYL1),D(LYLW),D(LCPCW))
RETURN
END
NSP 410
NSP 420
NSP 430
NSP 440
NSP 450
NSP 460
NSP 470
NSP 480
NSP 490
NSP 500
NSP 510
NSP 520
NSP 530
NSP 540-

```

C



```

ATL=1.-0.1*FLOAT(ITER)
IF (NCONTS.NE.0) ATL=0.75
IF (ATL.LT.0.75) ATL=0.75
BTL=1.-ATL
EVALUATION OF FORCE ACTING ON LEADING-EDGE ELEMENTS
C
TFABS=0.
TLNTH=0.
NCT=0
DO 40 I=2,NSW1
NCON=I
K=NELM(I)-1
ALNTH=0.
FABS=0.
DO 30 J=5,K
XEE=(XE(I,J)+XF(I,J+1))/2.
YEE=(YE(I,J)+YE(I,J+1))/2.
ZEE=(ZE(I,J)+ZE(I,J+1))/2.
CALL NEWVEL(C,THETP,XEE,YEE,ZEE,XN,YN,XTE,YLE,CONS,DUMMY,CONI,CONNL
1J,CONK,SI,NSW1,NRW,NWNG,CJ,CX,XLE,UU,VV,WW,CPCW1,XCP,YCP,GAMA,YNLH
2LM)
GMA=GAMA(NWNG+I)
A(1)=XE(I,J+1)-XE(I,J)
A(2)=YE(I,J+1)-YE(I,J)
A(3)=ZE(I,J+1)-ZE(I,J)
AAA=SORT(A(1)*A(1)+A(2)*A(2)+A(3)*A(3))
A(1)=A(1)*GMA/AREA
A(2)=A(2)*GMA/AREA
A(3)=A(3)*GMA/AREA
B(1)=UU
B(2)=VV
B(3)=WW
CALL CRSPRD(A,B,F)
FABSI=SORT(F(1)*F(1)+F(2)*F(2)+F(3)*F(3))
FABS=FABSI+FABSI
ALNTH=ALNTH+AAA
CONTINUE
TFABS=TFABS+FABS
TLNTH=TLNTH+ALNTH
CONTINUE
30
40

```

```

TAVRG=TFABS/TLNTH
WRITE (6,170) TFABS
C
C      WRITE (7) TFABS, TAVRG, TLNTH
C
C      CALCULATION OF THE COORDINATES OF LEADING-EDGE ELEMENTS BY
C      SATISFYING FORCE-FREE CONDITION
DO 110 J=5,NMAX
DO 110 I=2,NSW1
NCON=1
K=NELM(I)-1
IF (J.GT.K) GO TO 110
XXX=XE(I,J+1)
YY=YE(I,J+1)
ZZ=ZE(I,J+1)
DLS=SORT((XE(I,J+1)-XE(I,J))**2+(YE(I,J+1)-YE(I,J))**2+(ZE(I,J+1)-ZE(I,J))**2)
1ZE(I,J)**2)
XEE=(XE(I,J)+XE(I,J+1))/2.
YEE=(YE(I,J)+YE(I,J+1))/2.
ZEE=(ZE(I,J)+ZE(I,J+1))/2.
CALL NEWVEL (C,THETP,XEE,YEE,ZEE,XN,YN,XTE,YLE,CONS,DUMMY,CONI,CONNLM1000
1J,CONK,S1,NSW1,NCW,NWNG,C1,C2,CK,XLE,UU,VV,W,W,CPCW1,XCP,YCP,GAMA,YML1010
2LM)
UVW=SORT(UU*UU+VV*VV+WW*WW)
IF (J.EQ.5) GO TO 50
VVA=ATL*VV/UUVW
WWA=ATL*WW/UUVW
DLY=VVA*DLS+BTL*(YE(I,J+1)-YE(I,J))
DLZ=WWA*DLS+BTL*(ZE(I,J+1)-ZE(I,J))
GO TO 60
CONTINUE
VVA=0.5*VVV/UVW
WWA=0.5*WWW/UUVW
DLY=VVA*DLS+0.5*(YE(I,J+1)-YE(I,J))
DLZ=WWA*DLS+0.5*(ZE(I,J+1)-ZE(I,J))
GO TO 70
CONTINUE
IF ((DLZ/DLS).GT.SINA) DLZ=DLS+SINA
CONTINUE

```

30 50 70



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J2=J+2
KP=K+1
IF (J2.GT.KP) GO TO 130
DO 120 JK=J2,KP
XXE(I,JK)=XXE(I,JK)+DX
YYE(I,JK)=YYE(I,JK)+DY
ZZE(I,JK)=ZZE(I,JK)+DZ
120 CONTINUE
C      ..... NLM2050
C      ..... NLM2060
REWIND 4
DO 140 L=1,MSW1
KS=NELM(L)
140 WRITE (6) KS,(XE(L,M),YE(L,M),ZE(L,M),M=1,KS)
DO 150 L=1,MSW
KS=NNELM(L)
150 WRITE (6) KS,(XXE(L,M),YYE(L,M),ZZE(L,M),M=1,KS)
WRITE (6) NMAX,NNMAX,ZMIN,NCNTS
C      ..... NLM2140
C      ..... NLM2150
160 CONTINUE
RETURN
C      ..... NLM2160
NLM2170
C      ..... NLM2180
170 FORMAT (//,59H TOTAL ABSOLUTE FORCE ACTING ON LEADING-EDGE FREE ELEMENTS,,F10.5)
      END
      NLM2190
      NLM2200-

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