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A SECOND-ORDER BUDYKO-TYPE PARAMETERIZATION OF LANDSURFACE HYDROLOGY

BY STEFANOS A. ANDREOU and

PETER S. EAGLESON

1982



Report No. 280

Prepared under the Support of The National Aeronautics and Space Administration

Grant NAG 5-134

June 1982

(NASA-CR-169432)A SECOND-ORDER BUDKYO-TYPEN83-10472PARAMETERIZATION OF LANDSURFACE HYDROLOGYSemiannual Progress Report (MassachusettsInst. of Tech.)143 p HC••••BAD CAPSUnclasLANGUAGE••••[en1[A07/MF[en1] A01CSCL 08H G3/4335576

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and

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RALPH M. PARSONS LABORATORY

HYDROLOGY AND WATER RESOURCE SYSTEMS

Report Number 280

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1

June 1982

ACKNOWLEDGEMENTS

This work was completed with the support of the National Aeronautics and Space Administration (NASA) under Grant NAG 5-134.

The work was performed by Stefanos A. Andreou, research assistant in Civil Engineering at MIT, and constitutes his thesis presented in partial fulfillment of the requirements for the degree of Master of Science in Civil Engineering. This study was supervised by Peter S. Eagleson, Professor of Civil Engineering, who also provided the theoretical background material on which it is based.

Thanks also are due to Dr. Chris P. Milly, who provided many helpful suggestions and comments, and to Antoinette DiRenzo, who performed all the necessary typing.

ABSTRACT

This work develops a simple, second-order parameterization of the water fluxes at a landsurface for use as the appropriate boundary condition in general circulation models of the global atmosphere. The derived parameterization incorporates the high non-linearities in the relationship between the near-surface soil moisture and the evaporation, runoff and percolation fluxes.

Based on the one-dimensional statistical-dynamic derivation of the annual water balance developed by Eagleson (1978), it makes the transition to shortterm prediction of the moisture fluxes, through a Taylor expansion around the average annual soil moisture.

A comparison of the suggested parameterization is made with other existing techniques and available measurements.

A thermodynamic coupling is applied in order to obtain estimations of the surface ground temperature.

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NOTATION

Symbols	Definition and Dimensions	
A	albedo	[-]
A _o	gravitational infiltration rate as modified by capillary ris from water table.	se [LT ⁻¹]
B p	biomass production	$[ML^{-2}T^{-1}]$
с _н	coefficient for the sensible heat transfer.	[-]
с _w	coefficient for the water vapor transfer	[-]
c p	specific heat of water vapor at constant pressure	$[L^2T^{-2}deg^{-1}]$
c	pore disconnectedness index	[-]
с s	specific heat of soil-water system	$[L^2T^{-2}deg^{-1}]$
D _{ij}	moisture transfer coefficient between layers i and j	[LT ⁻¹]
d ₁ '	depth to which the diurnal moisture cycle extends	[L]
d ₁	a soil depth influenced by the diurnal soil-moisture cycle	[L]
d	diffusivity index of soil	[-]
d ₂	a soil depth influenced by the annual temperature cycle	[L]
Ea	drying power of the air	$[\mathrm{FL}^{-1}\mathrm{T}^{-1}]$
E _{pA}	annual potential evapotranspiration	[L]
E _T A	annual actual evapotranspiration	[L]
Er	annual storm surface retention	[L]
E	exfiltration parameter	[-]
ē	average annual actual evapotranspiration rate	[LT ⁻¹]
ēp	average annual potential evapotranspiration rate	[LT ⁻¹]
eT	actual evapotranspiration rate	[LT ⁻¹]
e. p	potential evapotranspiration rate	[LT ⁻¹]
e _T v	transpiration rate from vegetation	[LT ⁻¹]

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6	soil evaporation rate	[LT ⁻¹]
e	saturation vapor pressure at surface temperature	[FL ⁻²]
e	vapor pressure of the air at screen height	$[FL^{-2}]$
fe	exfiltration capacity of soil	$[LT^{-1}]$
f	infiltration capacity of soil	[LT ⁻¹]
G	heat flux into the soil	[FL ⁻¹]
G	gravitational infiltration parameter	[-]
Н	sensible heat	$[FL^{-1}]$
Hs	sensible heat	[FL ⁻¹]
I	infiltration on soil surface	[LT ⁻¹]
Is	infiltration under vegetated surfaces	[LT ⁻¹]
i	rainfall rate	[LT ⁻¹]
J	evapotranspiration efficiency	[-]
K(1)	saturated hydraulic conductivity	$[LT^{-1}]$
ĸ	hydraulic conductivity between layers i and j	[LT ⁻¹]
K _a	atmospheric heat conductance	$[\mathrm{FT}^{-1}\mathrm{deg}^{-1}]$
K	surface heat conductance	$[\mathrm{FT}^{-1}\mathrm{deg}^{-1}]$
k(1)	saturated intrinsic permeability	[L ²]
k	plant coefficient	[-]
k	soil thermal diffusivity	$[L^2 T^{-1}]$
L	latent heat of vaporization	$[L^2 T^{-2}]$
L	Monin-Obukhov length	[L]
М	vegetal canopy density	[-]
м	equilibrium vegetal canopy density	[-]
m _T	rainy season length	[T]

^m tb	mean time between storms	[T]
^m P _A	mean annual precipitation	[L]
m _v	mean number of storms per year	[-]
^m i	mean storm intensity	[LT ⁻¹]
^m H	mean storm depth	[L]
m	pore size distribution index of soil	[-]
ne	effective porosity of the soil	[-]
n	effective porosity of the soil	[-]
P _A	annual precipitation	[L]
- P	mean storm intensity	[LT ⁻¹]
Pa	atmospheric pressure	[FL ⁻²]
q*	saturated atmospheric specific humidity	[-]
ц а	specific humidity of the atmosphere at screen elevatio	n[-]
q _{ij}	soil moisture flux between layer i and j	[LT ⁻¹]
(R _i) _B	bulk Richardson number	[-]
R g _A	annual groundwater runoff	[L]
^R SA	annual surface runoff	[L]
Rn	net radiation at the surface	[FLT ⁻¹]
R	gas constant	$[L^2T^{-2}deg^{-1}]$
ra	atmospheric diffusion resistance	$[L^{-1}T]$
r _i	surface diffusion resistance	$[L^{-1}T]$
Se	exfiltration "desorptivity"	[LT ^{-1/2}]
s _i	infiltration "sorptivity"	$[LT^{-1/2}]$
S s	relative humidity at the evaporating surface	[-]
Sg	saturation ratio of the surface atmosphere	[-]

8	average soil moisture at the surface layer	[-]
°o	average annual soil moisture at the surface layer	[-]
^s k	soil moisture concentration at time k	[-]
^s k	critical value of soil moisture	[-]
ī _a	average annual atmospheric temperature	[deg]
Ta	air temperature at screen height	[deg]
Т	one year	[T]
۲ 8	ground temperature at the surface	[deg]
ro	surface temperature	[deg]
Τ ₁	soil temperature at the depth of the vapor source	[deg]
т2	mean soil temperature of layer of depth d2	[deg]
t _o	time when the surface becomes saturated after a precipitation	[T]
t _o	time when the surface becomes dry during an evaporation period	[T]
^t r	storm duration	[T]
t _b	time between storms	[T]
U	moisture uptake by plants	[LT ⁻¹]
Ua	wind speed	[LT ⁻¹]
w	upward capillary rise velocity from the water table	[LT ⁻¹]
Wg	surface soil moisture	[-]
Wmax	maximum value of soil moisture for which surface runoff is equa	al to zero [-]
Y	total yield	[L]
уg	percolation rate	[LT ⁻¹]
ӯ _g	average annual percolation rate	[LT ⁻¹]
У _В	surface runoff rate	[LT ⁻¹]
, y _s	average annual surface runoff rate	[LT ⁻¹]
у	total yield rate	[LT ⁻¹]
^z r	surface layer thickness 13	[L]

Z	distance above the soil surface	[L]
z _a	screen height	[L]
2 ₀	surface roughness	[L]
α	reciprocal of average storm intensity m _i	$[L^{-1}T]$
β	reciprocal of average time between storms t	[T ⁻¹]
γ	the psychrometric constant	$[FL^{-2}deg^{-1}]$
Δ	slope of the saturation vapor pressure-temperature curve	$[FL^{-2}deg^{-1}]$
δ	reciprocal of average storm duration t	[T ⁻¹]
η	reciprocal of mean storm depth m _H	[L ⁻¹]
Э	volumetric moisture content	[-]
⊖ _f c	field capacity	[-]
к	shape factor of Gamma-distributed rainstorm depths	[-]
λ	parameter of Gamma-distributed storm depth	[-]
Ξ	potential humidity	[-]
ρ _α	mass density of air	$[\mathrm{FL}^{-4}\mathrm{T}^2]$
ρ _w	mass density of water	$[FL^{-4}T^2]$
ρ _s	density of soil-water system	$[\mathrm{FL}^{-4}\mathrm{T}^{2}]$
σ	capillary infiltration parameter	[]
τ ₁	one day	[T]
ф _е	dimensionless desorption diffusivity of soil	[-]
φ _i	dimensionless sorption diffusivity of soil	[-]
Ψg	soil matrix head	[L]
Ψ	soil matrix head	[L]
Ω	groundwater recharge potential	[-]

CHAPTER 1

Introduction

1.1 Background

Current global atmospheric general circulation models use very complex numerical techniques to solve the hydrodynamic and thermodynamic equations of motion in the atmosphere, but they generally treat the land surface thermal and moisture boundary conditions in a rather simplistic way. This study attempts to provide an improved land surface boundary condition that increases the physical fidelity while maintaining computational practicality.

There are many difficulties involved in such a parameterization. First, there are problems related to inhomogeneities of the system's inputs, such as precipitation and of the system parameters, such as soil properties. Because of the great difficulty in defining the interactions of the microscale and the macroscale dynamics and representing these in a computationally efficient way, the problem of spatial variability is treated by considering a lumped onedimensional system, having effective areal parameters. A second problem is that of formulating the appropriate differential equations, which will account for the exchange of water and heat between the soil and the atmosphere. Special problems that arise here are those concerning the time scales of the physical processes, the number of parameters used and the selection of conceptual models representative of the real processes.

1.2 Objectives

The objectives of this work are:

1. To derive analytical expressions for the evaporation and yield rates which can be applied in dynamic mass balance equations for short term prediction of the soil moisture in the root zone.

2. To minimize the number of parameters necessary to implement this parameterization and to determine the inputs and observations required to operate the model.

3. To compare the results with those obtained from other models, which use either detailed numerical techniques or different types of parameterization.

4. To perform sensitivity analyses with respect to the critical soil parameters.

5. To estimate the ground surface temperature.

It must be noted, that the presence of snow is not taken into account in this research.

CHAPTER 2

Literature Review

2.1 Landsurface Parameterization

According to Eagleson [1981], there are six basic elements of the hydrothermal system at the earth surface, which must be parameterized:

1. The rate of potential evapotranspiration e_p , which is a function of the incoming short and long wave radiation to the system, the wind speed, the surface roughness, the vapor pressure of the air, the temperature of the air and of the ground. The dependence of e_p on the ground temperature generates a feedback between the soil and the atmosphere, and becomes a major coupling factor between the heat and moisture fluxes. Because of the creation of an atmospheric boundary layer due to the air flow close to the surface, e_p becomes also a function of the extent of the upwind evaporating surface.

2. The actual evapotranspiration rate e_T , which is a function of the available soil moisture, the soil properties and the vegetation cover. The value of e_T is limited from above by the value of e_p , i.e., the capacity of the atmosphere to remove vapor from the surface. The following general expression relates e_T with e_p :

$$J = \frac{e_T}{e_p} = f(s, e_p, t; soil and vegetation), J \leq 1$$

where J is called the "evaporation efficiency".

3. The water yield rate y, which is divided into two components, the surface runoff rate y_g and the percolation to the water table y_g . The yield rate is functionally related to the following parameters: y = f(s, precipitation input, t; soil properties and storage capacity of the surface layer). 17 4. The surface temperature T_g , which is dynamically related to the net radiation R_n , the latent and sensible heat losses from the soil, and the heat storage capacity of the surface soil layer.

5. The surface moisture retention capacity e_r , which can become important for certain types and density of vegetation cover and also under very arid conditions.

6. The soil moisture layer thickness Z_r , which consists of the portion of the soil close to the surface, where changes in moisture and heat content are concentrated. This zone is usually taken equal to one meter, but in fact it should be determined by the root-zone depth and by the soil and climatic properties of the area under investigation.

An overview of the methodologies proposed by prior investigators to model the above elements, will now be made following that of Eagleson (1981).

1. Potential Evapotranspiration rate ep

The concept of potential evapotranspiration, first introduced by Thornthwaite [1948], refers to the capacity of the atmosphere to remove vapor, under given meteorological conditions, when there is unlimited water supply from the soil and the ground surface is wet.

The basis of the recent approaches for estimating e is Penman's [1948] equation in the modified form:

$$\rho_{w} L.e_{p} = \frac{\Delta(R_{n}-G)}{\Delta+\gamma} + \gamma \frac{E_{a}(x)}{\Delta+\gamma}$$
(2.1)

where

$$E_a = \frac{{}^{o_a L}_a}{r_a} [q^*(T_a) - q_a]$$

and

 $R_n = net radiation near the surface.$

G = net heat flux into the ground.

Δ

 (de*/dT), the slope of the saturation vapor pressure-temperature curve.

 γ = the psychrometric constant.

L = latent heat of vaporization

E = the "drying power" of the air

 $q^*(T_a) =$ saturated atmospheric specific humidity at air temperature $q_a =$ specific humidity of the atmosphere at screen elevation $r_a =$ atmospheric diffusion resistance.

Equation (2.1) was applied in many theoretical and experimental studies by investigators such as Penman and Schofield, 1951; Penman, 1956; Tanner and Petton, 1960; Slatyer and McIlroy, 1961; Monteith, 1965, 1973; Rijtema, 1965; Van Bavel, 1966; Kohler and Parmele, 1967; Thom and Oliver, 1977.

The two-term structure of Equation (2.1) helps to point out the influence of large-scale advection. The first term corresponds to a lower limit to evaporation from a moist surface under steady-state conditions. When such conditions have been established, the value of q_a tends to reach the saturation value. This can happen in the downwind direction of a wet surface of infinite extent, where evaporated moisture will be advected. The second term of Equation (2.1) represents the drying power of the air $E_a(x)$. It takes it's maximum value at the beginning of the uniform surface (x=0), where the air is dryest. It was found by McNaughton [1976], that $E_a(x)$ decreases exponentially with distance x.

2. The Actual Evaporation Rate er

When the limiting factor for evaporation is not the available energy supplied to the system, but is the amount of soil moisture within the surface layer, then evaporation control passes to the soil. In this case, the evapotranspiration rate becomes dependent on the value of soil moisture, the soil properties and the vegetation cover, which together influence the capacity of the soil to deliver moisture upwards. Thus we can write: $e_T = f(e_p, s; soil, vegetation)$. The methods developed in order to determine this function can be categorized as follows:

a. Empirical parameterizations

Those involve long-term average relationships between precipitation and evaporation, which are derived from simple water balance equations applied to various catchments, by equating the total streamflow at the end of the catchment to the total yield produced in the basin. Such empirical relations are of no importance if one is interested in understanding the dynamics that govern the physical process, the interaction between the system's elements and their response to different hydrological and atmospheric conditions. As references one can mention the works by Schreiber [1904], Ol'dekop [1911], Tara [1954], Budyko [1956], Pike [1964], Budyko [1971].

b. Divergence of Atmospheric Vapor Flux

Rasmussen [1977]; derived a steady-state long-term regional atmospheric water balance over an area in space, by considering horizontal water vapor fluxes measured with probes well distributed in space. He used surface precipitation observations to close the water balance and estimate the long-term spatially-averaged actual evapotranspiration.

c. Advection-Aridity Approach

Brutsaert and Stricker [1979] assumed that the second term of Equation (2.1) represents the effect of larger-scale advection. They also used the concept of symmetry between potential and actual evapotranspiration introduced by Bouchet [1963] and the corresponding value of e_p for conditions of minimal advection suggested by Priestley and Taylor [1972], to derive:

$$\frac{e_{T}}{e_{p}} = \frac{\alpha(R_{n} - G)}{R_{n} - G + \frac{\gamma}{\Delta}E_{a}} -1$$
(2.2)

where $\alpha \sim 1.26$

This methodology is called the "advection-aridity" approach. The time scale in Equation (2.2) is arbitrary, although they found it to work satisfactorily for daily values. It must be noted that difficulties are encountered in estimating the wind function which enters into the calculation of E_a and also advection effects were assumed to be generated only due to the regional shortage of moisture supply at the surface. d. Soil Moisture Surrogate

Attempts have been made to derive equations for the actual evapotranspiration rate, by introducing a soil-moisture related surface parameter. All equations of this type are of the general form:

$$\frac{e_{T}}{e_{p}} = \frac{1}{1 + \frac{\gamma}{\Delta + \gamma}B}$$
(2.3)

where

i. $B = K_a/K_s$, Slatyer and McIlroy [1961] $K_a, K_s =$ atmospheric and surface heat conductances.

ii. $B = r_c/r_a$, Monteith [1965]

 $r_a = atmospheric diffusion resistance$ $r_c = surface diffusion resistance, which was related to the$ evaporation rate and to the difference between the vapor pressure at the leaf surface and it's saturated value at leaf surface temperature.

iii. $B = (1-S_{c})/S_{c}$, Barton [1979]

where $S_s =$ relative humidity at the evaporating surface, which for non saturated surfaces can be very different from the relative humidity at the ground surface.

A special difficulty encountered in expressions such as Equation (2.3) is that they are not designed to represent effective areally averaged values for the atmospheric temperature and the value of b.

Tanner and Fuchs [1968] derived a more general equation for e_T, which does not assume any particular diffusion model for the leaf or other surface and does not include internal resistance to heat diffusion. The model they used is:

$$E = \frac{E_{p} - [\rho C_{p} \Delta / (\Delta + \gamma)] (T_{o} - T_{i}) / r_{a}}{1 + [\gamma / (\Delta + \gamma)] (r_{i} / r_{a})}$$
(2.4)

where

- T_{o} = surface temperature [°K]
- T₁ = soil temperature at the boundary between the dry and moist layer in the soil, where the vapor source is.

There are also studies which derived expressions for the transpiration from plants. A category of these assumes knowledge of plant physiology, which can reduce their applicability for macroscale parameterizations, due to their inability to capture dynamic interelationships among the various spatially variable system components. Studies of this type include those by Van de Honert [1948], Cowan [1965], Rijtema [1965], and Federer [1977].

Assuming the same albedos from the vegetation and the wet bare soil, Shuttleworth [1979] proposed a relationship similar to Equation (2.3), where he replaced e_T by e_{T_V} , the transpiration rate from the plant.

Eagleson [1981] applied ecological optimality hypotheses to water-limited Natural Soil-Vegetation systems, to derive the following equation for the average evapotranspiration efficiency:

$$\frac{e_{T}}{\bar{e}_{p}} = \begin{cases} 0.11 + 2.22M_{o} - 1.87M_{o}^{2} + 0.54M_{o}^{3} , k_{v} = 1 \\ 0.11 + 1.25M_{o} + 0.27M_{o}^{2} - 0.63M_{o}^{3} , k_{v} = 0.7 \end{cases}$$
(2.5)

where

 $M_{o} = \text{percentage of vegetation cover}$ and $k_{v} = \frac{e_{Tv}}{e_{p}} = \text{plant coefficient.}$ e. Moisture Accounting Models

Most of the atmospheric general circulation models currently in use, apply a surface boundary conditions which incorporates an evaporation-soilmoisture relationship of the linear Thornthwaite-Budyko type. This relation has the form:

$$\frac{\mathbf{e}_{\mathrm{T}}}{\mathbf{e}_{\mathrm{p}}} = \begin{cases} 1 & \Theta > \Theta_{\mathrm{f}_{\mathrm{c}}} \\ \Theta / \Theta_{\mathrm{f}_{\mathrm{c}}} & 0 \le \Theta \le \Theta_{\mathrm{f}_{\mathrm{c}}} \end{cases}$$
(2.6)

where Θ_{f_c} is the soil field capacity, i.e., the upper limit of soil moisture for which water can be stored in the soil without drainage due to gravity.

A major difficulty encountered in formulations such as Equation (2.6) is the definition of the field capacity Θ_{f_c} , since there is no rigorous justification for the correct value of this parameter.

As it is pointed out by other investigators (Philip, 1957; Hillel, 1971; Lowry, 1959), the relation between evapotranspiration and soil moisture can be highly non-linear, due to the influence of soil properties and vegetation cover, which play a dominant role during the exfiltration process. This nonlinear relation was also theoretically supported and verified by Eagleson [1978], and it is the one used for the purposes of the present study.

Eagleson [1978] used the probability distributions of the independent climatic variables to obtain the derived distributions of the dependent elements of the water-balance, through a physically-based model of the natural process. With this statistical-dynamic approach he derived an expression of the long-term annual average evapotranspiration efficiency $\frac{\overline{e}_T}{\overline{e}_p}$ as a function of the long-term averages of soil moisture and climatic parameters, soil properties and vegetation cover. This relationship will be presented with more details in Chapter 3.

3. Water Yield Rate y

There are empirical equations which relate the long-tern average annual yield with annual precipitation and potential evaporation (Lettau, 1969).

Another way of estimating the total long-term yield is by equating it with the long-term time integral of the streamflow in the catchment. This assumption can lead to errors especially under very arid conditions, where the groundwater flow does not appear as streamflow.

Empirical models developed by Budyko [1971], and Arakawa [1972], estimate the short-term yield as a function of soil moisture, precipitation, potential evapotranspiration, soil porosity, and surface layer thickness Z_r .

4. Surface Temperature T_g

The ground temperature T_g is an important parameter for determining sensible and latent heat fluxes from the soil to the atmosphere. Complicated numerical models exist, which solve the coupled moisture and heat transport equations in porous media. Recent studies include the work by Philip and DeVries [1957], Sasamori [1971], Rosema [1975], Benoit [1976], and Milly [1980].

For application in GCM's, more simplified methods for estimating T are g needed. The most commonly used among those method.logies as presented by Deardorff [1978] are:

$$R_n(T_g,t) - H(T_g,c) - \rho_w L e_T(T_g,t) = G$$
(2.7)
must be solved for T_g , given that the other elements of the equation
are known.

b. Dependence of G on the sensible heat H. Kasahara and Washington [1971] assumed $G = \frac{1}{3}H$ and solved Equation (2.7) for T_g .

c. Dependence of G on the net radiation R_n . Nickerson and Smiley [1975] assumed G = -0.19 R_n , when $R_n < 0$ (down) and G = -0.32 R_n , when $R_n > 0$ (up) and solved Equation (2.7) for T_p .

d. Bottom-insulated single soil layer. Arakawa [1972], Corby [1972], and Rowntree [1975] applied the following equation:

$$\frac{\partial \mathbf{T}}{\partial \mathbf{t}} = \pi^{\frac{1}{2}} G/(\rho_{g} c_{g} d_{1})$$
(2.8)

where

and
$$d_1 = (k_s \tau_1)^{b_1}$$

where

$$k_g = soil thermal diffusivity$$

 $\tau_1 = one day$

e. Force-restore method. Bhumralkar [1975] and Blackadar [1976] developed a formula that contains the deep soil temperature T_2 of the following form:

$$\alpha \frac{\partial T_g}{\partial t} = 2\pi^{\frac{1}{2}} G/(\rho_s c_s d_1) - 2\pi (T_g - T_2)/\tau_1$$
(2.9)

where

$$\alpha = 1 + \frac{2\delta}{d_1 \pi^{-\frac{1}{2}}} \text{ and } T_g = T(\delta, t), \quad \delta = 1 \text{ cm}$$

Deardorff [1978] considered the case where $\delta \rightarrow 0$ and Lin [1980] considered the δ layer thickness effect to be weaker than that of Bhumralkar [1975] by setting: $\alpha=1 + \frac{\delta}{d_1 \pi^{-\frac{1}{2}}}$

Tests performed by Deardorff [1978] and Lin [1980], proved that the force-restore method gives reasonably accurate results for estimating the ground surface temperature.

Sasamori [1970], developed a model by using the thermodynamic equilibrium relation: 26

$$S_{g} = \exp\left[g\psi_{g}(0)/RT_{g}\right]$$
(2.10)

wher@

 $s_g = saturation ratio of the surface atmosphere$ $<math>\psi_g(0) = soil matrix head as a function of 0$ R = gas constant

That way he provided a coupling between the energy and mass conservation equations and the local thermodynamic equilibrium of temperature and humidity. Equation (2.10) could be solved for T_g in the case of soil controlled evaporation given that the other terms are known. A special difficulty could occur when the surface is saturated.

Then T should be approximated by the temperature above the evapora-

5. Surface retention capacity

There is a volume of precipitation moisture which is retained at the surface due primarily to the surface texture. There are empirical relations for estimating that capacity and a collection of them is given by Wigham [1975], Blake [1975], and others. It should be noted that this water loss must depend also on the amount of precipitation, it's intensity and the duration of interstorm periods.

6. Thickness of Soil Moisture Layer Z_r

This layer represents the depth from the surface within which big changes in soil moisture and heat content can occur due to forcing from the atmosphere. By using Philip's [1969] infiltration theory, Eagleson [1978] showed that this capillary penetration depth is of the order of one meter. Clearly, this depth would be a function of the soil-type, the timing of precipitation events and the depth of the root-zone system. The diurnal thermal penetration depth has been found to be of the same order of magnitude.

Budyko assigned a value of $Z_r = 1m$ and Arakawa assumed $nZ_r = 10cm$. Gates et al. [1977] suggested $\Theta_{f_c}Z_r = 30$ cm and Shukla suggested $\Theta_{f_c}Z_r = 10cm$.

Clearly, a rigorous justification of the appropriate value of Z_r does not exist and it's value is chosen rather arbitrarily. A sensitivity analysis is needed, in order to define the critical parameters that influence Z_r .

2.2 Water Balance Models

The existing water balance models can be divided into three categories:

a. Empirical (Thornthwaite and Mather, [1955]; Lettau, [1969]).

b. Phenomenological ("The Stanford Watershed Model", Crawford and Linsley [1966]; Holtan et al. [1974]; Peck [1976]).

c. Dynamic (Eagleson [1978]).

For short-term predictions of soil moisture the Deardorff [1978] and Lin [1979] models are mentioned here, since results from their methodologies are compared with those obtained in this work.

Deardorff [1978] applied the "Force-restore" method to determine surface moisture and temperature. He used a value of the bulk soil moisture in the upper half-meter of the soil and wrote an equation of the form:

$$\frac{\partial W_{g}}{\partial t} = -C_{1} \frac{(e_{T}-i)}{\rho_{w}d_{1}} - C_{2} \frac{(W_{g}-W_{b})}{\tau} , \quad 0 \le W_{b} \le W_{max}$$
(2.11)

where

i = storm intensity

W_g = surface soil moisture

$$C_1 = f(W_q/W_{max})$$

 $C_2 = constant$

 $\tau = 1 \, day$

 $d_1' = depth$ to which the diurnal moisture cycle extends.

W = maximum value of soil moisture for which surface runoff is equal to zero.

Transpiration from vegetation was included by using a generalization of the Monteith and Szeicz [1962] function for evaporation, which incorporates parameters related to plant physiology. The complicated representation of vegetation can make this approach difficult to apply in an actual situation. Gravity is ignored and actual evaporation is derived from a Budyko type linear relation.

Lin [1979] developed a deterministic model to be dynamically coupled with a GCM and the groundwater zone. The ground is represented by a surface layer of 10cm depth, an intermediate 40cm layer and a deep layer which contains the groundwater zone.

The equations describing the system's dynamics are given by: Surface layer d1:

 $d_{1}(d\Theta_{1}/dt) = (I_{s} - e_{s}/\rho_{w})(1-M) + (I_{c} - U_{1})M - q_{12}$ (2.12)

Intermediate layer d2:

$$d_2(d\Theta_2/dt) = -U_2M + q_{12} - q_{23}$$
(2.13)

Deep layer:

 $\Theta_3 = f(t)$, with very slow variations with time.

where

I_s,I_c = infiltration on soil and under vegetated surfaces
e_s = soil evaporation rate
M = percentage of vegetation cover
U₁,U₂ = moisture uptake by plants
q_{ij} = moisture flux from layer i to j

The potential evapotranspiration is derived from an aerodynamic equation and the actual evapotranspiration as a refinement of Budyko's parameterization, by using the value of the field capacity, wilting point and some empirical constants. The surface retention capacity of the soil and vegetation is ignored. The infiltration capacity is estimated by applying Holtan's [1974] method, where $I_i = A\Theta_i^B$. The soil moisture flux q_{ij} , between adjacent layers is given by:

$$q_{ij} = D_{ij}(\Theta_j - \Theta_j) + K_{ij}$$
 (2.14)

where

D_ij = moisture transfer coefficients
K_i = hydraulic conductivity of the soil

From numerical experiments, he derived reasonable results of hydrologic variables such as soil moisture, evapotranspiration and surface temperature, for various regions of the earth. He distinguished between the variables that can be obtained from remote sensing and which are Θ_1 , M, and T_g and those which cannot. The time and space varying parameters K_{ij} and D_{ij} create a special difficulty to implement in the model, since very often large scale measurements of those parameters do not exist.

CHAPTER 3

Review of the Water Balance

3.1 Introduction

The theoretical background of this work is drawn from Eagleson's (1978 a, b, c, d, e, f, g) water balance model. The physical model is one-dimensional and only vertical fluxes of water are considered in the soil column. The inputs to the system are of two types:

a. Climatic variables, which are treated as independent random variables and are seven in total number.

b. Soil properties, which are represented by three independent parameters considered to be deterministic.

The effect of vegetation is explicitly considered in the model through two parameters, the percentage of v getation cover M_0 , and the plant water use coefficient, k_v . Vegetation is modeled to act as a uniformly distributed sink throughout the entire surface layer of thickness Z_r , which continuously extracts moisture during the evapotranspiration period, at a rate regulated by the value of k_v .

The use of natural selection hypotheses and possible observations of the percentage of vegetation cover and total water yield from the basin, can significantly reduce the number of necessary input parameters to the model. Those techniques will be referenced with details in Chapter 5.

Uncertainty in the model is introduced through the probability distributions of several climatic variables. Precipitation events are simulated as independent and identically distributed rectangular intensity pulses having Poisson distributed arrivals. The corresponding storm depth: h, are assumed as gamma distributed. The interstorm periods t_b and storm durations t_r , are 31

taken to be exponentially distributed. The rate of potential evapotranspiration e_p and the air temperature T_a , are set equal to their annual average values. The system dynamics for soil moisture movement are represented by Philip's (1969) infiltration and exfiltration equations. The averaged outputs from the system, i.e., the actual evaporation E_{T} , the surface runoff R_{c} and the groundwater runoff R_{g} are calculated through the use of derived distributions. More details for the model's assumptions are described by Eagleson (1978 a).

The mean annual water balance equation [Eagleson, 1978e] is given by:

$$E[P_{A}] \left\{ 1 - e^{-G-2\sigma} \Gamma(\sigma+1)\sigma^{-\sigma} \right\} = E[E_{P_{A}}^{*}]J(E,M,K_{v}) + m_{t}K(1)s_{o}^{c} - Tw$$
(3.1)

where

E[] = expectation operatorPA = annual precipitation ^Ер_А = annual potential evapotranspiration ^Ет_А = annual actual evapotranspiration = $E_{T_A}/E_{P_A}^*$ = evapotranspiration efficiency. J Ε exfiltration parameter G = gravitational infiltration parameter capillary infiltration parameter σ m_T = rainy season length K(1) = saturated hydraulic conductivity. average annual soil moisture at the surface layer s_ Ē = pore disconnectedness index С Т = 1 year = upward capillary rise velocity from the water table. 32W

3.2 The Separate Elements of the Water Balance

The basic elements of the water balance, which will be of use in the current landsurface parameterization are the following:

a. Evapotranspiration

Eagleson (1978d) derived the total evapotranspiration during an interstorm period by using an exfiltration analogy of Philip's [1969] infiltration equation of the following form:

$$f_e = \frac{1}{2} S_e^{-\frac{1}{2}} - M \cdot e_v + W$$
 (3.2)

where

M = vegetation fraction of surface

e, = vegetation transpiration rate

w = velocity of capillary rise from the water table

$$S_{e} = 2s_{o}^{1+d/2} \left[\frac{n_{e}^{K(1)\psi(1)\phi_{e}(d)}}{\pi m} \right]^{\frac{1}{2}}$$
(3.3)

where

ne	=	effective porosity of the soil
K(1)	п	saturated effective hydraulic conductivity
ψ(1)	=	saturated matrix potential of soil
φ _e (1)		dimensionless desorption diffusivity of soil
d	=	diffusivity index of soil
m	=	pore size distribution index of soil
so	=	initial soil moisture, constant throughout the surface boundary
		layer

The boundary conditions associated with the exfiltration equation are interpreted as follows:

In the beginning of the interstorm period, the surface soil moisture s_1 will take a value $s_1 = 1$, so that the exfiltration rate f_e will be equal to the potential evaporation rate e_p from a wet surface. We denote by t* the time it takes for the surface retention to evaporate and by t_o the time it takes for the surface to become completely dry. When $t > t* + t_o$, then $f_e < e_p$, and f_e will be given by Equation (4.1). Evaporation ceases at the time when $f_e = 0$, or when a new storm begins. Transpiration from the vegetated surface assuming unstressed conditions, will take place at a constant rate e_v , which will be given by: $e_v = k_v e_p$, where $k_v =$ plant water use coefficient and $e_p =$ bare soil potential evaporation.

The time t , after which control passes to the soil was found to be equal to:

$$t_{o} = \frac{s_{e}^{2}}{2\bar{e}_{p}^{2}(1+Mk_{v}-w/\bar{e}_{p})} \cdot \left(1 - M + \frac{M^{2}k_{v} + 1(1-M)w/\bar{e}_{p}}{2(1+Mk_{v}-w/\bar{e}_{p})}\right)$$
(3.4)

Assuming exponential distribution of the time between storms t_b and a constant potential evapotranspiration rate \bar{e}_p equal to it's annual average value, Eagleson [1978b] derived the following expression for the average annual evapotranspiration efficiency J(E, M, K_v):
$$J = \frac{\tilde{e}_{T}}{\tilde{e}_{p}} = 1 - \left[\frac{1 - M}{1 - M + Mk_{v}}\right] \cdot \left\{ \left[1 + Mk_{v} + (2B)^{\frac{1}{2}}E\right] e^{-BE} - \left[Mk_{v} + (2C)^{\frac{1}{2}}E\right] e^{-CE} - (2E)^{\frac{1}{2}} \left[\gamma\left(\frac{3}{2}, BE\right)\right] \right\}$$
(3.5)

where

 \bar{e}_{T} = actual annual average rate of evapotranspiration

$$B = \frac{1 - M}{1 + Mk_v - w/\bar{e}_p} + \frac{M^2k_v + (1 - M)w/\bar{e}_p}{2(1 + Mk_v - w/\bar{e}_p)^2}$$

$$C = \frac{1}{2}/(Mk_v - w/\bar{e}_p)^2$$
and
$$E = \frac{2\beta n K(1)\psi(1)\phi_e}{\pi m\bar{e}_p^2} s_o^{d+2}$$

b. Surface Runoff

Assuming uniform intensity i(t) during a rainstorm Eagleson [1978e] applied Philip's [1969] infiltration equation, to represent the infiltration rate by:

$$f_{i} = \frac{1}{2} S_{i} t^{-\frac{1}{2}} + A_{o}$$
(3.5)

for a saturated surface,

$$A_{o} = \frac{1}{2} K(1) (1+s_{o}^{c}) - w$$

and

$$S_{i} = 2(1-s_{o}) \{ [5nK(1)\psi(1)\Phi_{i}(d,s_{o})]/3m\pi \}^{5}$$

where

$$S_i = infiltration sorptivity$$

 $\Phi_i(d,s_o) = dimensionless sorption diffusivity of soil$

When the surface is saturated $(s_1=1)$, f_i becomes maximum and equal to the infiltration capacity f_i^* .

If the depth of surface retention is represented by h_0 , then infiltration into the soil will start if $t_r > h_0/i$. The initial infiltration rate will be equal to the storm intensity i. The continuous rise in the internal soil moisture will cause an increase of the surface moisture. When the surface becomes saturated, at time $t_0 + h_0/i$, the infiltration rate will be given from Equation (3.6). Thus, for $t_r > t_0 + h_0/i$, $i > f_1$ and surface runoff is produced. It is found that:

$$t_{o} = \frac{S_{i}^{2}}{2i(i-A_{o})} \left[1 + \frac{A_{o}}{2(i-A_{o})} \right]$$
(3.7)

By solving the linearized diffusion equation with constant flux boundary condition, a similar expression can be obtained for t_o (Carslaw and Jaeger, 1959), where the coefficient 1/2 is replaced by $\pi^2/16$.

By assuming the value of s_0 to be constant at it's time-averaged value, Eagleson [1978e] approximated the expected annual surface runoff R_{s_A} with the following function.

$$\frac{E[R_{S_A}]}{E[P_A]} = e^{-G-2\sigma} \Gamma(\sigma+1)/\sigma^{\sigma} - E[E_r]/m_{H}$$
(3.8)

where

 $\sigma = \left[\frac{5n\eta^{2}K(1)\psi(1)(1-s_{o})^{2}\phi_{i}(d,s_{o})}{6\pi\delta m}\right]^{1/3}$

$$G = [\alpha K(1)/2][1+s_0^c] - \alpha W$$

 $E_r = \text{storm surface retention}$

- η = reciprocal of mean storm depth m_{μ}
- δ = reciprocal of average storm duration t_r
- α = reciprocal of average storm intensity m 36

c. Percolation to the Water Table

The average annual groundwater runoff is given by [Eagleson, 1978f):

$$E[R_{g_A}] = m_{\tau} K(1) s_0^{c} - Tw \qquad (3.9)$$

where

$$m_{\tau}$$
 = mean rainy season length

T = one year

CHAPTER 4

The Short-Term Water Balance Model

The purpose of this model is to make short-term predictions of the soil moisture level within the surface layer, by taking into account the atmospheric boundary conditions at the surface.

We assume that high moisture concentrations occur within a depth Z_r from the surface. That implies that a portion of the infiltrated water during precipitation will be stored within that layer of thickness Z_r . Below that depth Z_r , water will percolate downwards due to gravitational forces. If the surface reaches saturation during the precipitation period, then runoff will be produced at a rate depending on the value of the internal moisture within the layer Z_r . During evapotranspiration, the actual evaporation rate from the bare soil will be determined from the amount of available moisture within this layer and will be limited from above by the potential evapotranspiration rate e_p . Vegetation is assumed here to transpire at the potential rate under unstressed conditions, which will be independent of the level of soil moisture within the layer Z_r .

We consider a vertical soil column in contact with the atmosphere and define as the moisture state variable s_0 , the concentration of soil moisture in the vegetation root zone Z_r . In a one-dimensional representation, where only vertical fluxes are considered, the conservation of water mass equation can be written:

$$nZ_{r} \frac{ds}{dt} = i - e_{T} - y \qquad (4.1)$$

where

 e_{T} = evapotranspiration rate = $f_{1}(s; climate, soil, vegetation)$ (4.2) 38 y = yield rate = f₂(s; climate, soil)

r = effective porosity of soil in vegetation root zone

 Z_{μ} = thickness of vegetation root zone (cm)

- i = rainfall rate (cm/sec)
- e_{m} = evapotranspiration rate (cm/sec)
- y = yield rate (surface runoff plus percolation below the root zone)
 (cm/sec)

(4.3)

Equations (4.2) and (4.3) establish a non-linear relation between e_T , y, and s. In order to make the transition from the long-term time averaged values \bar{e}_T and \bar{y} to their short-term values, e_T and y vary linearly around their long-term averages, with respect to the value of s. Thus, the non-linearities in the relations between e_T , y, and s will be incorporated into the model through a Taylor expansion of those functions, around the annual average soil moisture s_0 . By performing that expansion, a transition is made from the longterm average values of those rates as they appear in the water balance derived by Eagleson [1978], to their short-term values.

The water balance can be written in the following form, which is more convenient for this purpose:

$$1 = EJ + e^{-G-2\sigma} \Gamma(\sigma+1)\sigma^{-\sigma} = \Omega s_{\sigma}^{c}$$
(4.4)

where

$$E = \text{potential humidity} = E[P_A]/E[E_P_A]$$

$$\Omega = \text{groundwater recharge potential} = m_T K(1)/E[P_A]$$

$$J = \text{evapotranspiration efficiency} = \frac{\overline{e_T}}{\overline{e_p}}$$

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To a first-order approximation, we assume that the actual evapotranspiration rate e_T at anytime will vary linearly with changes in the soil moisture concentrations, s. Thus, we expand J around s_o and obtain:

$$\frac{\mathbf{e}_{\mathrm{T}}}{\overline{\mathbf{e}}_{\mathrm{p}}} = \frac{\overline{\mathbf{e}}_{\mathrm{T}}}{\overline{\mathbf{e}}_{\mathrm{p}}} + \frac{\partial J}{\partial s} (s - s_{\mathrm{o}}) + \dots$$
(4.5)

From the definition of J (Equation 3.4) we can find:

$$C_{1} = \frac{\partial J}{\partial s} = \left[\frac{1 - M}{1 - M + Mk_{v}}\right] \cdot \left[\left\{-(1 + Mk_{v})B + (2B)^{\frac{1}{2}} - B(2B)^{\frac{1}{2}}E\right] \cdot \left(e^{-BE}E(1)(d+2)s_{o}^{d+1}\right\} - \left\{\left[-k_{v}C + (2C)^{\frac{1}{2}} - C(2C)^{\frac{1}{2}}E\right] \cdot \left(e^{-CE}E(1)(d+2)s_{o}^{d+1}\right\} - \left\{\sqrt{2E(1)}\left(\frac{d}{2}+1\right)s_{o}^{d/2}\left[\gamma\left(\frac{3}{2},CE\right) - \gamma\left(\frac{3}{2},BE\right)\right] + (2E)^{\frac{1}{2}}s_{o}^{\left(\frac{3d}{2}+2\right)}(d+2) E(1)^{\frac{3}{2}}\left[C^{\frac{3}{2}}e^{-CE(1)s_{o}^{d+2}} - B^{\frac{3}{2}}e^{-BE(1)s_{o}^{d+2}}\right]\right\}\right]$$

Then Equation (4.5) is:

$$\frac{e_{T}}{\bar{e}_{p}} = J(s_{0}) + C_{1}(s-s_{0})$$
(4.7)

The following relation holds for the annual expected value of the surface runoff R : s.

$$e^{-G-2\sigma}\Gamma(\sigma+1)\sigma^{-\sigma} = \frac{E[R_{S_A}]}{E[P_A]}$$
(4.8)

At this point, we assume that the surface runoff occurs only during the storm duration. In order to obtain an expression for the average annual surface runoff rate \bar{y}_s we can write:

$$\frac{E[R_{s_A}]}{E[P_A]} = \frac{\overline{y}_s}{\overline{p}}$$
(4.9)

where

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 $\overline{p} = {}^{m} P_{A} / {}^{m} v {}^{m} t_{r} = \text{mean storm intensity} = {}^{m} n_{i}$ and $\overline{y}_{s} = E[R_{s_{A}}] / {}^{m} v {}^{m} t_{r}$

Here again, a first-order approximation is made and the surface runoff function is expanded in Taylor-series around the mean s.

In order to accomplish this, the derivative of the surface runoff function, with respect to s, should be derived. In attempting to evaluate the derivative of the runoff function, $e^{-G-2\sigma}\Gamma(\sigma+1)\sigma^{-\sigma}$, a difficulty is encountered because the derivative of the gamma function cannot be given in closed form. This difficulty was overcome by approximating the function $\xi = e^{-2\sigma}\frac{\Gamma(\sigma+1)}{\sigma^{\sigma}}$ by the polynomial:

$$\log \xi = -0.806 - 1.766(\log \sigma) - 0.980(\log \sigma)^2$$
 (4.10)

It is believed that this approximation represents satisfactorily the runoff function (Figure 1).

We can now evaluate the derivative of $\frac{y_s}{\bar{p}} = e^{-G-2\sigma}\Gamma(\sigma+1)\sigma^{-\sigma}$ with respect to s.

We find that:

$$C_{2} = \frac{d(y_{s}/\bar{p})}{ds}\Big|_{s=s_{0}} = e^{-G} \cdot \xi \left[\frac{-\alpha K(1) c s_{0}^{C-1}}{2} + U\right]$$
(4.11)

where

$$U = \frac{\Lambda}{\sigma} \left[-1.766 - 1.96(\log \sigma) \right]$$

and $\Lambda = \left| \frac{5\pi \eta^2 K(1)\psi(1)}{6\pi \delta m} \right|^{1/3} \cdot \frac{1}{3} \cdot (1 - s_0)^{-4/3}$.

$$\cdot \underbrace{\begin{bmatrix} -2(1-s_0)[d(1-s_0)^{1.425-0.0375d} + 5/3] - (1-s_0)^{2.425-0.0375d} d(1.425-0.0375d) \\ [d(1-s_0)^{1.425-0.375d} + 5/3]^{4/3} \\ 41 \end{bmatrix} }_{41}$$

2

in Bain



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SURFACE RUNOFF FUNCTION

FIGURE 1

Plotted points represent:

$$(\log \xi) = -0.806 - 1.766(\log \sigma) - 0.980(\log \sigma)^2$$

The following relation holds for the annual expected value of the ground-water runoff R : g_{\star}

$$\Omega s_{o}^{c} = \frac{E[R_{gA}]}{E[P_{A}]}$$
(4.12)

We assume that percolation to the water table occurs during the entire rainy season of length m_{χ} . Thus, in order to derive a representative rate \bar{y}_g for the percolation, the following normalization is applied:

$$\Omega s_{o}^{c} = \frac{E[R_{gA}]}{E[P_{A}]} = \frac{\overline{y}_{g}}{m_{P_{A}}/m_{\tau}} = \frac{\overline{y}_{g}}{\overline{p}} \cdot \frac{m_{\tau}}{m_{v}m_{t}}$$
(4.13)

By taking the derivative of \bar{y}_g/\bar{p} with respect to s, we obtain:

$$C_{3} = \frac{d(y_{g}/\bar{p})}{ds} \bigg|_{s=s_{o}} = \frac{m_{v}m_{t_{r}}K(1) c s_{o}^{c-1}}{m_{P_{A}}}$$
(4.14)

We also expand the groundwater runoff rate y around it's long_term average value. Thus, finally we can write to the the first approximation:

$$\frac{y_{s}}{\bar{p}} = \frac{\bar{y}_{s}}{\bar{p}} + C_{2}(s-s_{o})$$
 (4.15)

$$\frac{y}{p} = \frac{y}{p} + C_3(s-s_0)$$
(4.16)

In order for the model to be applicable for both bare soil and for the presence of vegetation cover, the value of $C_1 \frac{dJ}{ds}$ for the case of bare soil is also evaluated.

For bare soil, the value of J (Eagleson, 1978) leads to:

and

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$$C_{1} = \frac{dJ}{ds} = \left[\sqrt{2} e^{-E} + \left[1 + \sqrt{2} E \right] e^{-E} + \Gamma \left(\frac{3}{2}, E \right) \sqrt{2} \cdot \frac{1}{2} \cdot E^{-\frac{1}{2}} - (2E)^{\frac{1}{2}} (E^{\frac{1}{2}} e^{-E}) \right] \cdot \frac{2\beta\eta K(1)\psi(1)\Phi_{e}(d)(d+2)s_{o}}{\pi m e_{p}^{2}}$$

$$(4.17)$$

According to the above linearizations, the conservation of water mass, Equation (4.1), can be written in the following finite difference form:

(i) Rain $(t \le t_r)$ $nZr \frac{\Delta s}{\Delta t} = i - y_s - y_g$ (4.18)

Since surface sumoff will start to be produced after time t > t_0 from the beginning of the storm, where t_0 is the time when the surface gets saturated (Equation 3.7), we must account for y_s in Equation (4.18) only when $t_r > t > t_0$.

It also seems reasonable to assume that the percolation below the depth 2_r will not only be a function of the soil moisture s_k in the surface layer at time k but also of the soil moisture s_0 below that layer. That is $y_g = f(s_k, s_0)$. In order to keep the equations simple, we will assume that y_g will vary with respect to the average value $\frac{s_k + s_0}{2}$.

Thus, finally we have:

For $t < t_{o}$

$$nZr\left(\frac{s_{k+1}-s_k}{\Delta t}\right) = i - \left[\overline{y}_g + C_3 \overline{p}\left(\frac{s_k+s_o}{2} - s_o\right)\right]$$
(4.19)

For $t > t_0$

$$nZr\left(\frac{{}^{8}k+1-{}^{8}k}{\Delta t}\right) = i - \left[\overline{y}_{s} + C_{2} \overline{p}\left(s_{k}-s_{o}\right)\right] - \left[\overline{y}_{g} + C_{3} \overline{p}\left(\frac{s_{k}+s_{o}}{2}\right)\right]$$

$$(4.20)$$

(ii) <u>No rain</u> (interstorm period) $t \leq t_{b}$

$$nZr\left(\frac{s_{k+1}-s_k}{\Delta t}\right) = -\left[\bar{e}_T + C_1 \bar{e}_p(s_k-s_o)\right] - \left[\bar{y}_g + C_3 \bar{p} \left(\frac{s_k+s_o}{2} - s_o\right)\right]$$
(4.21)

The limiting value for $e_T = \bar{e}_T + C_1 \bar{e}_p (s_k - s_0)$ will be the value of the potential rate of evapotranspiration e_p . That implies that e_T will be replaced by e_p until the time when the surface gets dry.

The above equations were solved explicitey with respect to s_{k+1} . The time step Δt was taken equal to 30 minutes, i.e., we update the soil moisture every 30 minutes. The time step was chosen to be of this order of magnitude both for reasons of numerical accuracy of the solutions and because this is the necessary time scale for conjunctive operation of the model with a GCM of the atmosphere. All other parameters appearing in Equations (4.19) through (4.21) are treated as known inputs in the model.

Two catchments were selected to test the model, Clinton, Massachusetts and Santa Paula, California. They represent two contrasting climates, the first corresponding to a humid and the second to a se____arid region and have been well-studied elsewhere (Eagleson, 1978 a,b,c,d,e,f,g). The appropriate selection of parameters and necessary inputs in order to implement the model are presented in the next chapter.

CHAPTER 5

Selection of the Appropriate Model Parameters

5.1 Introduction

The parameters necessary to implement the model can be divided into the following categories:

a. Climatic Variables:

^m P _A	•	mean annual precipitation [cm]
^m t _b	8	mean time between storms [days]
^m tr	E	mean storm duration [days]
m _τ		average rainy season length [days]
ĸ	8	shape factor of gamma-distributed rainstorm depths
τ _a	=	average annual atmospheric temperature [°C]
^m i	-	mean storm intensity [cm/day]
e	8	potential evapotranspiration rate [cm/day]

The values of m_{P_A} , m_{t_b} , m_{t_r} , m_i , m_{τ} , and κ are derived using the statistical properties of the rainfall events (Eagleson 1978b). The value of \overline{T}_a is taken from measurements of the air temperature close to the surface during the year. The value of \overline{e}_p , as it was developed in Chapter 2, is a function of solar climatic and surface characteristics. Here, it will be evaluated using a Penman-type equation. For the applications at Clinton, Massachusetts and Santa Paula, California, it will be set equal to its annual average value. In a later application, at Phoenix, Arizona this assumption will be relaxed and diurnal changes of e_p will be considered.

b. Soil parameters

Three independent soil parameters are used in the model. These are:

1

n = effective porosity of the soil

k(1) = saturated intrinsic permeability [cm²]

c = pore disconectedness index.

By applying ecological optimality conditions (Eagleson 1982) it is possible, given the porosity, to estimate the appropriate values for k(1) and c of natural surfaces. Those conditions are described in paragraph (5.2).

c. Vegetation parameters

Vegetation is represented in the model by the percentage of vegetation cover M_0 and the water use coefficient k_v . It will again be shown how the value of M_0 is selected by applying ecological optimality hypotheses. Another way of obtaining M_0 is through observations, sometimes by using remote sensing techniques. If this is the case, then that can help to determine more accurately the parameter k_v , as it will be shown later. d. Surface layer thickness Z_r

The surface layer thickness Z_r is treated in the model as an independent variable, although we know that it is a function of the root zone depth, and the soil and climatic characteristics of the region. Since the exact value of this parameter is not known and the purpose of its existence is to provide us with a simple conceptual model of the physical process which accounts for some storage of water close to the surface, it will be possible to fit the value of this parameter either using available observations or solutions of more accurate numerical models. Sensitivity analysis will be performed in order to investigate the influence of Z_r on the various fluxes within the soil column, and to test the assumption of many investigators, that Z_r must be taken equal to lm.

5.2 Ecological Optimality Hypotheses

Eagleson (1982) derived several equilibrium conditions, which he hypothesized to hold in the long-term for a natural, water-limited soil-vegetation system.

In a natural soil-vegetation system equilibrium stages can be considered to occur at different time scale.

In the short-term it is assumed that the system tends to minimize waterdemand stress, so, the canopy density and the plant species will take such values that maximize the soil moisture. That implies that the following relations must hold for a given climate and soil:

$$\left(\frac{\partial s_{o}}{\partial M}\right)_{k_{v}} = 0 , M = M_{o}$$
 (5.1)

$$\frac{\partial s_{o}}{\partial k_{v}} \bigg|_{M} = 0 , k_{v} = k_{v}$$
(5.2)

where

s_o = average soil moisture concentration in the root zone
M_o = short-term equilibrium canopy density
k_{v_o} = short-term equilibrium plant coefficient

Equations (5.1) and (5.2) define the "complete vegetal equilibrium". It was shown by Eagleson [1982], that for canopy densities $M_0 > 0.42$ complete equilibrium is not possible because Equation (5.2) cannot be satisfied. He further hypothesized that for a moist climate the canopy will always satisfy Equation (5.1) but that the species will only be in a quasi-equilibrium, so that the following condition is satisfied:

$$\begin{pmatrix} \frac{\partial M}{\partial E} \\ \frac{\partial E}{\partial E} \end{pmatrix}_{k} = 0$$
 (5.3)

where

E = dimensionless climate-soil parameter

It was hypothesized that in long-term there is a synergistic symbiotic development of both the soil properties and the vegetation canopy which tends to maximize biomass production, B_p . For water limited systems, B_p will be proportional to the water utilization by the plants, i.e.,

$$B_{p} \sim M_{o} k_{v} \bar{e}_{p}$$
(5.4)

For a given climate and constant k_v , B_p is maximized, according to Equation (5.4), when M_o is maximized. The conditions for this equilibrium then, are:

$$\left(\frac{\partial M_{o}}{\partial c}\right)_{k(1)} = 0 , M_{o} = M_{o}^{*}$$
(5.5)

$$\left(\frac{\partial M_{o}}{\partial k(1)}\right)_{c} = 0 , M_{o} = M_{o}^{*}$$
(5.6)

The third soil property, the effective porosity n, is assumed constant during this optimization procedure.

For two contrasting climates, those of Clinton, Massachusetts and Santa Paula, California, and with the climatic and soil parameters given in Table 5.1 contours of constant M_0 for different combinations of k(1) and c were drawn. (Figure 2 and 3). Each contour corresponds also to a constant value of E and of the actual evapotanspiration E_{T_A} . From those contours, the optimum value of the canopy density, M_0^* , can be derived. That peak value of M_0 , defines a unique pair of values of k(1) and c. Thus, under the previously developed hypotheses the only soil parameter that is needed to be known is the porosity n.

Eagleson and Tellers [1982] provide encouraging tests of the above hypotheses for different catchments. They also suggest algorithms for fitting 49





the values of k_v and n, if observations of the canopy density and the total water yield exist.

Also shown in Figure 2 and 3 are curves of constant s_0 . It is noticed that the locus of optimum (maximum) s_0 does not coincide with the peak value of M_0 . The basic reason for that is that in the long-term evolution, the dominant factor is the maximization of the biomass production. Thus, although the system is locally optimized with respect to s_0 , maximization of s_0 is not the primary condition to be fulfilled. A more detailed discussion of this point is given by Eagleson [1982]. TABLE 5.1

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Clint	on,	Massachusetts	Santa Paula, California
Mo	8	0.912	M _o = 0.424
ēp	8	0.150 cm/day	ē = 0.274 cm/day
mt.	-	3 days	m _t ⊏ 10.42 days b
^m t _r	a	0.32 days	$m_t = 1.43$ days
m _τ	8	365 days	m _τ ≕ 212 days
w/e	8	0	w/e ^p = 0
m V	e	109	m _V = 15.7
^m PA	8	94 cm	$m_{pa} = 54 \text{ cm}$
k v	8	1	$k_v = 1$
ī _a	8	8.4°C	T _a = 13.8°C
к	-	0.50	κ = 0.25
λ	8	0.578	$\lambda = 0.0732$
k(1)	•	$5.57 \times 10^{-11} \cdot cm^2$	$k(1) = 12.27 \times 10^{-11} \text{ cm}^2$
с	=	4.75	c ¤ 5.25

[The values of M_0 , k(1), and c were set equal to those corresponding to peak climatic values, according to the vegetal equilibrium hypothesis and the ecological optimality hypothesis, as they are described by Eagleson (1982).]

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CHAPTER 6

6.1 Simulation of the Rainfall Process

In order to test the model, rainfall inputs were generated, which possessed the statistical characteristics derived from historical records. Under the assumption of independently distributed rainfall depths, storm durations, and times between storms, we generated those variables with the following characteristics:

Storm depth h:

It was considered as Gamma distributed with parameters κ and λ . The corresponding pdf was

$$f_{\rm H}(h) = \frac{\lambda(\lambda^{\rm h}) e}{\Gamma(k)}$$
(6.1)

with $m_{H} = \kappa / \lambda$, $\sigma_{H}^{2} = \kappa / (\lambda)^{2}$

Storm duration t_r:

It was taken as exponentially distributed with pdf of the form

$$f_{t_r}(t_r) = \delta e^{-\delta t_r}, \quad t_r > 0$$
 (6.2)

where

$$\delta = m_{t_r}^{-1}$$

Time between storms th:

It was also taken as exponentially distributed with pdf

$$f_{t_b}(t_b) = \beta e^{-\beta t_b}, t_b > 0$$
 (6.3)

where

 $\beta = m_{t_b}^{-1}$

The above distributions for h, t_r , and t_b were chosen, because it is shown by Eagleson [1978b] that they can adequately represent the rainfall process.

The generated variables, i.e., h, t_r , and t_b preserved the above-defined statistics. For their generation the IMSL library subroutine GGAMR was used. This subroutine was incorporated into the main program "Taylor. Fortran", which also calculates the statistics of the generated variables in order to check for consistency with the historical values. (Gamma and exponentially distributed variables, can both be generaged with this subrountine, by making some slight modification of the parameters used.)

The storm intensity was assumed uniform during the rain and thus was derived just by dividing the value of the generated h with the corresponding value t_r . Since the storm magnitudes and storm durations were assumed independently distributed, the matching was performed arbitrarily by using the values of h and t_r in the sequence they were generated from the random number generator. Of course, such a matching could give rise to unrealistic values of i, in the extremes where independence is most invalid. However, at this stage, this fact will not be taken into account in testing the model, although its inpact should be kept in mind during the interpretation of the results.

The statistics of the generated rainstorm characteristics for Clinton, Massachusetts and Santa Paula, California are presented in Table 6.1.

The observed differences are reasonable, since the generated variables which were tested, corresponded to many fewer events than the historical values derived from five years of observations. We also observe that the generated series at Clinton, Massachusetts gives an average storm depth considerably less than the average of five years, so we expect that to reflect in a smaller soil moisture on the average than the average annual soil moisture corcorponding to five years of data.

TABLE 6.1

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Clinton, Massachusetts

	Historical (5 years)	Generated	(1 year)
Storm depth	E[h] = 0.86	E[h] =	0.73
[cm]	Var[h] = 1.50	Var[h] =	0.73
Storm duration	$E[t_r] = 0.32$	n[t _r] =	0.34
[days]	$Var[t_r] = 0.10$	Var[t _r] =	0.13
Time between	$E[t_b] = 3$	E[h] =	3.18
[days]	$Var[t_r] = 9$	Var[t _b] =	10.88
	Santa Paula, California		
	Historical (5 years)	Generated	(l year)
Storm depth	E[h] = 3.41	E[h] =	3.83

Storm depth	E[h] = 3.41	E[h] = 3.83
[cm]	Var[h] = 46.65	Var]h] = 20.16
Storm duration	$E[t_r] = 1.43$	$E[t_r] = 2.34$
[days]	$Var[t_r] = 2.04$	$Var[t_r] = 4.69$
Time between	$E[t_{b}] = 10.42$	$E[t_b] = 11.90$
[days]	$Var[t_b] = 108.57$	$Var[t_b] = 66.30$

CHAPTER 7

Presentation of Results

7.1 The Evapotranspiration, Surface Runoff, and Percolation Functions

Before applying the model described in Chapter 4 for simulating the soilmoisture concentration during the rainy season, it is essential to present the rate functions of evapotranspiration e_T , surface runoff y_s , and percolation y_g , which will be linearized around the average annual soil moisture, s_o .

The actual evapotranspiration rate e_T is given by Equation(3.6), where it appears through the expression of evapotranspiration efficiency J, i.e., normalized with the value of the average annual (seasonal) potential evaporation rate \tilde{e}_p . By using the climatic variables and the soil and vegetation parameters derived under climatic climax conditions and shown in Table 5.1, for the catchments of Clinton, Massachusetts and Santa Paula, California, the evapotranspiration efficiency J can be plotted as a function of the soil-moisture, s.

Figure 4 shows the J(s) function for the bare soil case ($M_0 = 0$) and Figure 5 shows J(s) when the presence of vegetation is taken into account. Also, shown in Figure 4 is the evaporation efficiency function that is used by Manabe [1969] in his GCM. This follows a linear Budyko-Type parameterization for which J = 1 if $s > s_k$ and $J = \frac{s}{s_k}$ if $s < s_k$, where s_k is a critical value of s defined by $s_k = 0.75 \times s_f$ and s_f is the degree of soil saturation within a soil layer from the surface to 1m depth, corresponding to the field capacity Θ_f . The value of the field capacity used in Manabe's General Circulation Model is held uniform over all areas of the Earth and is set equal to 15 cm.

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Evapotranspiration Efficiency Function (M = 0)

FIGURE 4

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The difference in the J(s) functions for Clinton and Santa Paula can be explained by the different climatic and soil properties of the two catchments. Clearly, Manabe's J(s) function overestimates the evapotranspiration in both cases. In Figure 5 we observe the apparent influence of the vegetation cover M on the evaporation efficiency. In this case according to the assumptions developed in Chapter 3, the limiting value of e_{T} becomes $M_{k} e_{p}$. For the humid climate of Clinton, we expect that the deviations of s around the average annual value s, will not be very high and thus we will always operate in the region where J = 1. Otherwise, the linearization procedure described in Chapter 4 will not give accurate results. With a value of $s_0 = 0.72$, as derived from the annual water balance, the above assumption is very reasonable for the humid climate. For the semi-arid climate of Santa Paula, we observe that the function J(s) is very close to a linear form, for values of s in the neighborhood of $s_0 = 0.55$. That implies, that the use of a linearized function of J around s, will give accurate results for this case. It must be pointed out that when a constant value of e is used, equal to its annual average value e, then the actual evapotranspiration rate e_{T} will tend to \bar{e}_{p} as s increases above the value of s_0 . Thus, this function is expected to give fairly accurate results when applied in a real case of successive rainy and dry periods, if e is supposed to be held constant. But if e is changing, as would be the case in reality, then the value of $\boldsymbol{e}_{_{\boldsymbol{T}}}$ obtained from this function will tend to the value of \overline{e}_{n} whenever the surface becomes saturated and not to the actual value of e_p . Thus, if a changing value of e_p is to be used, the time t from the beginning of the interstorm period until the surface gets dry must first be calculated. Before that time, evaporation will occur at the actual potential rate $e_{_{D}}$ and after that time control will pass to the soil and the value of $e_{_{T}}$

obtained through the previously described linearization procedure will be used.

The average annual surface runoff rate \overline{y}_s is given by:

$$\overline{y}_{g} = e \Gamma(\sigma+1)\sigma^{-\sigma}m_{P_{A}}/m_{v}m_{t_{r}}$$
(7.1)

In Figure 6 \bar{y}_s is plotted versus s, for the catchments of Clinton and Santa Paula.

The average annual percolation rate \bar{y}_{g} to the water table is given by:

$$\bar{y}_{g} = K(1)s^{c}$$
 (7.2)

The function \overline{y} versus s is shown in Figure 7 for both Clinton and Santa Paula.

The functions $\bar{y}_{g}(s)$ and $\bar{y}_{g}(s)$ indicate high non-linearities between those fluxes and the soil moisture s. Thus, we must expect that a linearization around the corresponding average soil moisture s_{0} , for each climate, can introduce errors in the estimation of those rates, especially when the deviations from the average value become high. This fact should be considered with attention to the interpretation of the results. That is, since those functions appear in this case to be convex, we expect to underestimate the surface runoff and percolation rates, whenever $s > s_{0}$ and overestimate them when $s < s_{0}$.



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Surface Runoff Function $y_{s}(s)$

FIGURE 6



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7.2 Simulation of Soil-Moisture Concentration During the Rainy Season Using

a Constant Value of $e_p = \overline{e}_p$

Equations (4.14) and (4.16) were solved for each time step ($\Lambda t = 30$ minutes), with respect to s_{k+1} , using the generated rain storm events. The depth of the surface layer Z_r which accounts for storage was treated as an independent variable, i.e., many simulation runs were performed with different values of Z_r in order to observe the sensitivity of the fluxes with respect to that parameter. The capillary rise from the water table was taken equal to zero, assuming that the water table was deep enough that it did not have any impact on the fluxes occuring close to the surface. The climate and soil properties for Clinton and Santa Paula were those presented in Table 5.1 which were derived using ecological optimality hypotheses (Eagleson 1982).

The computer program named "TAYLOR.FORTRAN" was set up to perform a simulation of the soil-moisture concentration in the surface layer. A complete description of this program is given in Appendix 2.

The soil-moisture concentration, s, as a function of time, for Clinton, Massachusetts is shown in Figure 8. Two different cases are presented; one with $Z_r = 100$ cm and one with $Z_r = 50$ cm. As is expected for the case where Z_r is smaller, the soil moisture fluctuates over a larger range. The results shown in Figure 9 correspond to a vegetation cover $M_o = 0.912$, which is the climatic climax value (Eagleson and Tellers, 1982). When bare soil was assumed (M = 0), there was no change in the results, because in the humid climate of Clinton, evaporation from the bare soil occurs at the potential level (climate controlled) and because we have taken $k_v = 1$, its optimum value (Eagleson and Tellers, 1982).

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Simulation of Soil Moisture During the Rainy Season (Clinton, Massachusetts)

FIGURE 8

Analogous results of s versus time for Santa Paula, California and $Z_r = 100$ cm and $Z_r = 50$ cm, are shown in Figure 9. We observe that at Santa Paula we have larger deviations of s around the mean s_0 compared to those at Clinton. This is due to the much longer interstorm periods and longer storm durations of the climate of Santa Faula. The results shown in Figure 10 correspond to a vegetation cover $M_0 = 0.424$ (optimum value). When M was set equal to zero (bare soil), small differences occured in the soil-moisture concentration. This was due to the fact that here also the evaporation from the bare soil is, on the average, rather high $(J(s_0) = 0.84)$ and again $k_r = 1$.

A sensitivity analysis was performed for the humid climate of Clinton and the semi-arid climate of Santa Paula, with respect to the value of the parameter Z_r . The results are shown in Figure 10. The horizontal axis corresponds to values of Z_r ranging from 20 cm to 120 cm. On the vertical axis, the cumulative yield and cumulative evaporation at the end of the rainy season are plotted. For Santa Paula, California, it is interesting to observe that there is a range of values of Z_r from approximately 60-120 cm, where those fluxes are insensitive to the value of Z_r . When Z_r becomes small enough, evaporation is rapidly reduced. This is due to the fact that soil moisture is exhausted very fast during the interstorm period, the surface becomes dry faster and control passes to the soil earlier than before. On the contrary, yield increases rapidly with small values of Z_r , because in that case, during the rain, the soil-moisture concentration in the surface layer increases very fast and the surface becomes saturated at earlier times. Thus, surface runoff is produced more frequently and at earlier times during the rain.

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FIGURE 9

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FIGURE 10 68

For Clinton, Massachusetts, the cumulative yield does not seem to become very sensitive to the value of Z_r , when the latter becomes small. For values of Z_r ranging from 0.4-lm, there is a maximum change of 3cm in the cumulative yield. The rate of chango becomes much smaller when Z_r exceeds lm. Cumulative evaporation was found to remain constant for all values of Z_r , indicating that the exfiltration process was always under climate control. At this point, it must be noted that, because of the model's structure, this sensitivity analysis becomes invalid for the humid climate of Clinton when Z_r is low and the value of s is such that control must pass to the soil. That is, the linearization around the value of the average annual soil roisture s_0 , is not valid in this case of $e_T << e_p$. However, for a humid climate, we can say apriori that Z_r should not be very low and so assume that soil control does not occur. Otherwise, it would be necessary to change the linearization procedure, and thus reduce the general applicability of the model.

It must be noted that in all cases examined for both climates, the moisture in the surface layer was never completely exhausted. would be exhausted however, if even smaller values of Z_r are assumed. However, such Z_r are physically unrealistic because Z_r is defined to include all exchangeable moisture.

We also observe that, because of earlier passage to soil-control when $M \neq 0$, the cumulative evaporation is greater when M = 0, for most values of Z_r .

7.3 Comparison With A Numerical Model

In order to test the predictive capability of the model developed in this study, the soil-moisture concentration and the water fluxes obtained from it, were compared to those obtained by an "exact" numerical model. The numerical model used was that developed by Milly and Eagleson [1980]. This model assumes a one-dimensional representation of the physical system and solves the coupled, non-linear partial differential equations governing mass and heat transport in the soil, using the Galerkin finite element method. In the present comparison, an isothermal version of the model was applied. The vertical soil column was taken equal to 5m and the influence of the water table was considered to be negligible. A constant flux (K(Θ_0) = constant) boundary condition was assumed at the bottom. The surface boundary condition was changed according to the surface moisture state. During precipitation, infiltration takes place at the precipitation rate, until the soil surface reaches saturation. After that happens, ponding of water on the surface occurs, thus producing surface relations. During evaporation, the evaporation rate is equal to the potential value until the surface becomes completely dry and control passes to the soil. After this time, evaporation proceeds according to the exfiltration capacity of the soil. The values for the precipitation intensities, storm durations, and interstorm periods used were those obtained from the simulated rainstorm events, as described in Chapter 6. The value of the potential evapotranspiration was assumed constant throughout the simulation period and equal to it's annual average value, and thus, as discussed in Section 7.1 it was not necessary to calculate a time to during the evaporation period.

The computer program SPLASH.FORTRAN developed by Milly [1980] was used in order to obtain the numerical solution. Many runs were performed, varying $\frac{70}{70}$
the number of finite elements within the soil column and several other parameters, in order to achieve convergence of results. This procedure is described with more details in Appendix 2. The results from this comparison are shown in Figure 11-16, and correspond to solutions of the numerical model where convergence was achieved. Figures 11-13 show the storage change, the total yield (surface runoff and percolation) and evaporation flux respectively, for Santa Paula, California and for 10 consecutive simulation periods. Each simulation period corresponds to either a storm or an interstorm period, with intensities and durations as generated by the procedure described in Chapter 6. The storage change represents the deviation from the initial soil-moisture concentration. From the results of the numerical model, it was found that the surface became dry at the eighth simulation period which implies that control passed to the soil at that time.

It is observed that the differences between the two models are not big and never exceed 1 cm of storage. The analytical model follows the numerical solution very faithfully. The water fluxes outside the surface layer are shown in Figure 12. Again, the differences between the two models are very small. The evaporation flux is shown in Figure 13. The differences here do not exceed 0.5 cm.

Figure 14-16 show the same comparison for Clinton, Massachusetts, and for 20 simulation periods, generated as discussed before. From Figure 14, we observe that the storage change is consistantly referestimated by the analytical model, but again the differences between the two are relatively small and never exceed 0.6 cm of storage. In Figure 15, the total yield at each simulation period is plotted and the agreement between the two models is considered as very satisfactory. Evaporation fluxes are shown in Figure 16. For the humid climate





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FIGURE 12

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FIGURE 13

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FIGURE 14

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of Clinton, evaporation was always at the potential level and thus there is no difference between the two models. Thus, all differences in storage change can be explained by the differences occuring in the prediction of the yield.

In general, it should be noted that the solution obtained by the analytical model is in very satisfactory agreement with the numerical solution for both climates. Of course, it must be kept in mind that the tested version of the numerical model was a simplified one, since isothermal conditions were assumed.

7.4 Comparison with Manabe's [1969] Parameterization

Manabe's [1969] landsurface parameterization was also compared with the model developed in this study.

Manabe [1969] uses the concept of field capacity s_{f_c} in his soil-moisture model. He assumes a surface layer of lm and defines a critical value of soilmoisture s_k given by: $s_k = 0.75 \times s_f$. Then he assumes the following equations to hold for the water and vapor fluxes at the surface:

i. Evaporation

if $s > s_k$, $e_T = e_p$ if $s < s_k$, $e_T = e_p$. $\frac{s}{s_k}$

where

e is estimated from an aerodynamic type equation ii. Soil moisture if s = s and i > e, $\frac{\partial s}{\partial t} = 0$ and y = i - e and if s < s f, $\frac{\partial s}{\partial t} = i - e_T$

The value of the field capacity chosen by Manabe for all applications was 15cm, which for a soil layer of 1m and a porosity of 0.35 corresponds to a soil-moisture concentration given by $s_{f_c} = 0.42$.

Using the same initial condition ($\odot = \odot_{f_c}$) for both models, the storage change versus the simulation period, is shown in Figures 17 and 18 for Santa Paula, California and Clinton, Massachusetts. It is observed that there is a big difference between the two, which is on the order of 4cm for Santa Paula and 3cm for Clinton. Since the first simulation period corresponds to a storm and the initial condition of soil moisture is set equal to the field capacity, it is expected that Manabe's model will not produce a storage change during that period because according to his assumption, soilmoisture cannot exceed the value of field capacity. If the first simulation period was an interstorm period, the storage changes produced by both models would not have so much difference. But big differences in storage will occur later on, when a precipitation event comes and soil-moisture reaches the value of the field capacity.

Since good agreement between the presently developed analytical model and the "exact" numerical model has already been established, it appears that Manabe's model does not represent the system very well. His model fails to capture the time variations of yield. This is shown for Clinton, Massachusetts in Figure 19. Values of the yield for Santa Paula obtained using Manabe's model are not shown graphically here. It was found, however, that a total yield of 8.7 cm was predicted for Santa Paula during the first simulation period by this model, while the yield was zero for all other simulation periods. As is shown in Figure 12, this is much different from the value predicted by both the numerical model and the analytical model developed here. Better results could possibly be obtained if a different value for the field capacity was chosen for Manabe's model, but what means can be used to evaluate this field capacity a priori?



FIGURE 17









In general, the analyti.al model suggested in this study seems to be an improvement to the landsurface parameterization, mainly because it is simple, physically based and gives consistent and accurate results when compared to numerical solutions.

7.5 Soil Moisture Simul on with Changing Value of ep

The model was also tested with real measurements of soil-moisture concentrations obtained from an experimental field at Phoenix Airport, Arizona. Values of the meteorological variables were available every half-hour, so that is was possible to estimate a changing value of e, using either a Penman-type equation or an aerodynamic equation. More precisely, the following measured aata were available: Net radiation R_n at the surface, Air Temperature T_a, wind speed U_a, and vapor pressure e at screen height, surface temperature T_{σ} at depth of 1 cm and average soil-moisture concentration in three layers below the surface (from 0 - 10cm, from 10 - 50cm, and from 50 - 100cm). The data corresponded to seven days of measurements from 5 March - 11 March, 1971. Details of the experimental field and measurement procedures are given by Jackson [1976]. Briefly, the soil consisted of Adelanto Loam, was reasonably uniform to about 100cm and had been cultivated numercus times during past years. The soil properties for the Adelanto Loam and the climatic variables at Phoenix Airport, are given on Table 7.1. A graph of hydraulic conductivity and diffusivity as a function of soil moisture \odot is given by Jackson [1976]. Before the experiment took place, the field was irrigated and during the sevenday period of measurements, no precipitation was measured by rain gages at the Phoenix Airport, although some traces did occur.

In order to compare the results of the model with the measured values of soil-moisture, the latter were averaged over the lm surface layer depth.

TABLE 7.1

Phoenix Airport - Arizona 0.263 cm/day ē ^mt_b 7.27 days z ^mtr 0.11 days = 365 days m_ = 0.50 κ w/ē_p ≃ 0 ī, = 21.3 °C m , = 45 19.35 cm mp = A 0.35 (assumed) n == $2.68 \times 10^{-9} \text{ cm}^2$ k(1) =6.5 с =

[The climatic variables shown in this table were derived by using the computer programs HODCOP and RAINSTAT developed by Restrepo and Eagleson (1978) for the interpretation and analysis of NOAA hourly precipitation data tapes. The soil properties for the Adelanto loam are given by Jackson (1965, 1979) and Mualem (1976).]

The value of the potential evaporation rate e_p was first estimated from a Penman-type equation, as described in Chapter 2, where the surface heat flux was neglected and the surface roughness was taken equal to 0.03cm.

As is also mentioned by Jackson [1976], the surface became dry after the fourth day of the experiment. This implies that after that time, flux control passed to the soil. Since the model used accounts only for soil moisture within the bulk volume and since it uses an evaporation efficiency function derived using the value of the annual (or seasonal) average evapotranspiration rate \tilde{e}_p , it cannot accurately locate this change, especially when e_p is much higher than \tilde{e}_p , as it was also discussed in Section 7.1. To surmount this problem, it was necessary to calculate apriori the average time t_o , until the surface becomes dry. This time is given by: (Eagleson, 1978d)

$$t_{o} = \frac{s_{e}^{2}}{2\bar{e}_{p}^{2}}$$
(7.3)

where S_{μ} is the exfiltration "desorptivity" defined for a dry surface by:

$$S_{e} = 2s_{o}^{1+d/2} \left[\frac{nK(1)\psi(1)\Phi_{e}(d)}{\pi m} \right]^{\frac{1}{2}}$$
(7.4)

and M was assumed equal to zero.

Using the values of the parameters as defined in Table 7.1, it was found that $t_0 = 3.92$ days, which is very close to the value of four days mentioned by Jackson.

Equation (4.16) was now solved as before. The results for the soilmoisture concentration in the layer of lm, are shown in Figures 20 and 21, evaluated using two different values of $\frac{1}{2}$ (the annual average value $\frac{1}{2} = 0.263$ p_A (the average value $\frac{1}{2} = 0.263$)





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as expected, the fitting is better when \overline{e}_p is the actual average for the sevenday period.

Some of the small discrepancies in these comparisons may be due to the ungaged (trace) precipitation that occured during this period.

In order to perform the simulation described above, the computer program ARIZ.FORTRAN was prepared. It uses as an input file the available meteorologic and soil-moisture characteristics, obtained every half-hour.

It must be noted that the ecological optimality hypotheses were not applied for soil-parameterization in the Arizona experiment for two reasons. First, because the field has b.en cultivated and is thus not in its natural state, and second, because soil properties were available from measurements.

Evaluation of the soil moisture concentration and the evaporation fluxes during the seven-day period will be shown in the following Section 7.6, where the thermodynamic coupling will be applied.

7.6 The Thermodynamic Coupling

The developed soil-moisture model was operated conjunctively with a thermal balance model, in order to estimate the surface temperature T_g . Two methods were tested, using the Arizona data. One used the force-restore method [Deardorff, 1978] and another used the thermodynamic equilibrium equation [Edlefsen and Anderson, 1963].

a. The force-restore method.

The force-restore method was described in Chapter 2, but the basic equations used are repeated here for convenience. Written in finite difference form, as they were solved in the present study, those equations take the form:

$$\frac{T_{g}^{k+1} - T_{g}^{k}}{\Delta t} = \frac{2G\pi^{\frac{1}{2}}}{\rho_{s}c_{s}d_{1}} - \frac{2\pi}{\tau_{1}} (T_{g}^{k} - T_{2}^{k})$$
(7.5)

$$G = R_n - H_s - LE$$
 (7.6)

and

$$\frac{T_2^{k+1} - T_2^k}{\Delta t} = G/(\rho_s c_s d_2)$$
(7.7)

where

T k = ground temperature at the surface (°K) = heat flux into the soil [cal/cm².sec] G R_n net radiation at the surface [ly/sec] = sensible heat flux [cal/cm².sec] Hs = water vapor flux [g/cm²sec] Е 86400 sec τ₁ T2^k = mean soil temperature over layer of depth d₂(°K) latent heat of vaporization [cal/g] L 8 = specific heat of soil [cal/g.°K] C s = density of soil [g/cm³] ρ d₁ soil depth influenced by the diurnal temperature cycle [cm] = d_2 soil depth influenced by the annual temperature cycle [cm] = The value of a_1 is given by: $d_1 = (k_s \tau_1)^{\frac{1}{2}}$, where k_s is the soil ther-

mal diffusivity. Assuming a soil porosity n = 0.35, the volumetric heat capacity of the soil $\rho_s c_s$ is estimated by (DeVries, "Heat Transfer in Soils").

$$\rho_{\rm s}c_{\rm s} = (1-n) 2 \times 10^6 + \Theta (4.2) \times 10^6 + (n-\Theta)c_{\rm s}$$

where

- 0 = volumetric water content

Using the Arizona data, we obtain:

$$\rho_{\rm s}c_{\rm s} = (1 - 0.35)2 \times 10^6 + 0.0805 \times 4.2 \times 10^6 + 0.269 \times 1.25 \times 10^3 = 1.6384369 \times 10^6 \, \text{J/m}^3 \, \text{K}$$

or $\rho_{ss} \simeq 0.39 \text{ cal/cm}^{3} \text{K}$

The thermal conductivity of the soil λ is obtained using the value given by deVries for loam and for n = 0.35. It is found that $\lambda = 1.44 \text{ cal.cm}^{-1} \text{sec }^{\circ}\text{C}^{-1}$ Thus, the soil thermal diffusivity will be given by:

$$k_s = \frac{\lambda}{\rho_s c_s} = 0.013 \text{ cm}^2/\text{sec.}$$

and

$$d_1 = (0.0 \pm 3 \times 86400)^2 = 33.51 \text{ cm}.$$

This value is close to the value of 31.89 applied by Lin [1980] for the same experimental field.

The value of d_2 is given by: $d_2 = (365 \text{ k}_s \tau_1)^{\frac{1}{2}} = 640.21 \text{ cm}$

The sensible heat flux H was evaluated from the equation suggested by Anderson [1976]:

$$H_{s} = \rho_{a} c_{p} \cdot C_{H} \cdot U_{a} (T_{g} - T_{a}) \left[\frac{cal}{c_{m}^{2} sec} \right]$$
(7.8)

Under climate-controlled conditions where $E = E_p$, the water vapor flux was evaluated by the aerodynamic relation:

$$E_{p} = \frac{\rho_{a} \times 0.622}{P_{a}} \cdot C_{w} U_{a} (e_{s} - e_{a}) \left[\frac{B}{cm^{2} \sec}\right]$$
(7.9)

In these equations:

 $e_s = saturation vapor pressure at surface temperature$ $<math>e_a = vapor pressure of the air at screen height$ $U_a = wind speed at screen height$ $T_a = air temperature (°K) at screen height$ $<math>\rho_a = density of air$ $c_p = specific heat of dry air$ $P_a = atmospheric pressure$

 C_{H} and C_{w} are coefficients equivalent to the drag coefficient for sensible heat and water vapor flux respectively. Under neutral conditions those are given by (Anderson 1976):

$$(C_{\rm H})_{\rm N} = (C_{\rm W})_{\rm N} = \frac{k^2}{[ln \frac{Z_{\rm a}}{Z_{\rm o}}]^2}$$
 (7.10)

where

k = Von Karman's constant (0.4)

Z = screen height

 $Z_{o} = surface roughness$

Deardorff [1968] computed the ratio of each of those coefficients to its value under neutral conditions, and his results are described by:

$$\frac{C_{\rm H}}{(C_{\rm H})_{\rm N}} = \frac{C_{\rm w}}{(C_{\rm H})_{\rm N}} = \left[1.0 - (\ln\frac{Z_{\rm a}}{Z_{\rm o}})^{-1} \cdot \left[\ln(\frac{1+x^2}{2}) + 2\ln(\frac{1+x}{2}) - 2\tan^{-1}(x) + \frac{\pi}{2}\right]\right]^{-1} \cdot \left[1 - 2\ln(\frac{Z_{\rm a}}{Z_{\rm o}})^{-1} \cdot \ln(\frac{1+x^2}{2})\right]^{-1}$$
(7.11)

where

 $x = (1 - 16 \frac{Z}{L})^{1/4}$

and L is the Monin-Obukhov length which can be related to the bulk Richardson number $(R_i)_R$ through the relation:

$$\frac{Z_{a}}{L} = \frac{k \cdot C_{H} / (C_{H})_{N} \cdot (R_{i})_{B}}{(C_{H})_{N}^{l_{2}} \cdot [1 - (ln\frac{Z_{a}}{Z_{o}})^{-1} [ln(\frac{1+x}{2}) + 2ln(\frac{1+x}{2}) - 2tan^{-1}(x) + \frac{\pi}{2}]^{-3}}$$
(7.12)

where

$$(R_{i})_{B} = \frac{2g \cdot Z_{a}(T_{a} - T_{g})}{(T_{g} + T_{a}) \cdot U_{a}^{2}}$$
(7.13)

Using equations (7.10), (7.11), and (7.12), a table of corresponding values of the ratio of bulk transfer coefficients C_H and C_w to their neutral value for different Richardson numbers $(R_i)_B$ and for different values of surface roughness Z_o , can be constructed. Such a table is shown by Anderson [1976, page 19]. That kind of table was used in the analysis performed here in order to determine the transfer coefficients to be used.

Equations (7.5), (7.6), and (7.7) were solved simultaneously with the soil-moisture Equation (4.16). At each time-step, which was equal to 30 minutes, new values of T_g^{k+1} for the surface temperature and of s_{k+1} for the soil-moisture, were estimated. The parameters of the surface roughness Z_o and of the initial deep soil temperature T_2 were varied in order to obtain the best fit with the measurements of surface temperature and soil moisture.

The changing value of e was evaluated through the use of the aerodynamic Equation (7.9). This value is used until control passes to soil.

The results are shown in Figures 22 through 29. In Figure 22 the surface temperature is plotted and compared with the solid line which represents the measured values. The transfer coefficient was set equal to $(C_H)_N = 0.00277$ and the initial deep soil temperature was set equal to $T_2 = 11^{\circ}C$. The fitting can be considered as satisfactory, although we observe that for the firs'. 60 hours the surface temperature is overestimated by the model at the peaks and after that point it is underestimated at the peaks.

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Surface Temperature by Force-Restore Method ($Z_0 = 0.05$ cm, $T_2 = 11^{\circ}$ C, e_p calculated from the aerodynamic equation). FIGURE 22

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In Figure 26, the daily evaporation rate obtained from the model is compared with that measured by lysimeter (Jackson, 1976). It is seen that the calculated evaporation from the first day is less than the measured one. That could explain the overprediction of surface temperature observed in Figure 22, at the first day. That is, the higher actual evaporation makes the surface cooler than that predicted from the model.

Another fact that must be mentioned is that the measurements of surface temperature are at a depth of 1cm below the surface. Since the model assumed evaluates the temperature exactly at the surface, a discrepancy between the two could be justified. J. D. Lin (1980) mentions that high temperature gradients, as high as a difference of 20°C in 2cm, can occur near the ground surface during most of the daytime, which supports what was said before.

Figures 24 and 25 show the results obtained using the same value for the transfer coefficient $(C_H)_N \approx 0.00277$ as before, but with a different initial value for the deep temperature $T_{2_1} \approx 14^{\circ}C_{\circ}$. We observe that soil-moisture concentration is not predicted as well as before.

It has been argued by Bhumralkar (Deardorff, 1978) that T_2 can be estimated as the average air temperature during the previous 24 hours. If this argument is correct, it is possible that an initial value of $T_2 = 11^{\circ}$ C, although it seems low for the Phoenix climate (where the annual average air temperature is about 21°C) could indeed have occured.

Figures 27 and 28 show the results of the comparison, when a larger transfer coefficient $(C_H)_N = 0.0057$ is assumed. Clearly, for this high value of $(C_H)_N$ the soil-moisture concentration (Figure 28) is very much underpredicted by the model.



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Average Daily Evaporation Rate

FIGURE 26

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Surface Temperature by the Force-Restore Method $(Z_0 = 0.5 \text{cm}, T_2 = 14^{\circ}\text{C}, e_p \text{ calculated from transformed from transformed for the second sec$

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FIGURE 28 100 A complete sensitivity analysis of the errors in the predictions of soil moisture and surface temperature with the values of surface roughness and initial deep soil temperature is shown in Table 7.2. It seems that a value of $Z_0 = 0.05$ cm and of $T_{2_1} = 11^{\circ}$ C gives us results which predict fairly accurately both surface temperature and soil moisture. This can be confirmed both from Table 7.2 and from Figures 22 and 23. From Table 7.2, it is observed that combinations of Z_0 and T_{2_1} with even smaller errors do exist, but the differences are very small compared with the errors obtained when $Z_0 = 0.05$ cm and $T_{2_1} = 11^{\circ}$ C are selected. The problem of a priori selection of Z_0 and T_{2_1} remains however.

It should be specially noted that when control passes to the soil (after the fourth day), the prediction of surface temperature is very accurate, which implies that the analytical model developed here for soil moisture fluxes, gives reasonable estimates of the actual rate of evaporation.

Manabe's model cannot be compared to the analytical model developed here for the Pheonix, Arizona experiment because the value of the soil field capacity, s_f, is not known.

b. The thermodynamic equilibrium equation.

The thermodynamic equilibrium equation is given by:

$$\frac{e}{e_{s}(T_{g})} = \exp\left[\frac{g(s,T_{g})}{R_{g}}\right]$$

where e is the vapor pressure at the soil surface.

Equation (7.14) was developed by Edlefsen and Anderson (1943) and implies that the water and vapor are in thermodynamic equilibrium. It has the attraction of involving only known variables and thus does not require esti-

TABLE 7.2

Fhoenix, Arizona

Surface roughness Z _o (cm)	Initital deep soil temper- ature T ₂ (°C)	Cumulative Error of Soil moisture predictions $337 \text{ MES}_{i} - s_{i}^{CAL}$ i=0	Cumulative Error of surface Temperature predictions 337 MES - $T_{g_1}^{CAL}$ $\underline{i=0}$ $T_{g_1}^{MES}$ - $T_{g_1}^{CAL}$
0.5	13	4.898	563.78
	11	3.815	629.19
	9	2.738	683.88
	7	1.935	1008.22
	5	1.063	1327.97
	3	0.457	1696.69
0.05	15	1.300	724.60
	13	0.541	610.21
	11	0.582	571.49
	9	1.373	628.97
	7	2.155	824.57
	5	2.790	1135.92
0.1	15	2.339	639.97
	13	1.422	561.12
	11	0.535	550.40
	9	0.547	627.94
	7	1.381	842.12
	5	2.016	1162.72
0.25	15	4.510	539.42
	13	3.250	519.76
	11	2.253	565.17
	9	1.278	685.42
	7	0.474	920.04
	5	0.550	1254.45

mates such as T_2 and C_H of the force-restore method. In order to apply it during the exfiltration process, it must be assumed that a quasi-steady state thermodynamic condition is reached at each time-step, when e_T is calculated. It must also be noted that Equation (7.14) ignores the influence of the adsorptive force-field, which can become important for a dry soil. In order to apply Equation (7.14), the dependence of ψ on T_g was ignored, assuming that the influence of T_g on ψ is not important and that the primal variability of ψ comes from variations in soil moisture.

Also (7.14) was applied only for the case where the surface is dry. When the surface is wet, the surface termperature was estimated by using again the force-restore method. If instead of doing so, it was set equal to the air temperature, a big discrepancy between the measurements and predictions would have been observed.

At each time step a value of the actual evaporation was determined by the model. By using the aerodynamic equation, a value for the vapor pressure e at the surface was calculated. From the soil-moisture model, the value of ψ was estimated by using the current value of s. The value of the surface temperature T_g^k of the previous time step k was used to evaluate (RT_g^k) since this factor is not very institute to changes at T_g . Then, Equation (7.14) was solved for T_g^{k+1} , since the only unknown now was $e_s(T_g^{k+1})$, which is a function of T_g^{k+1} .

The results are shown in Figures 29 and 30. It does not seem that the surface termperature is well estimated compared to the results of the forcerestore method. After the fourth day when the surface dries and the thermodynamic equation starts to apply, the surface temperature is systematically underpredicted.

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Surface Temperature by the Thermodynamic Equilibrium Equation

FIGURE 29 104 ORIGINAL MALLA



Soil Moisture Concentration (Temperature Calculated by the Thermodynamic equilibrium Equation)

> FIGURE 30 105

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CHAPTER 8

Summary, Conclusions, and Recommendations for Further Research

8.1 Summary

In this study, a simple analytical model was formulated to parameterize the water fluxes at the landcurface. A short-term water balance equation was solved during precipitation and interstorm periods, assuming all exchange of moisture to take place within a single surface layer. The evaporation and yield fluxes were assumed to vary linearly around their annual average values, as given by Eagleson (1978).

Successive rainstorm events and interstorm periods were generated in order to test the model. Soil-moisture concentration, within the surface layer was predicted every half-hour. The storage change and the evaporation and yield fluxes obtained from the analytical model during long simulation periods, were compared with those obtained from a numerical model (Milly 1980) and with a simple parameterization model (Manabe 1969) currently used in GCM's. This was done for two contrasting climates, those of Clinton, Massachusetts and Santa Paula, California.

Finally, the analytical model developed here for soil-moisture fluxes was operated conjunctively with thermal balance models, in order to predict the surface temperature. Results of the obtained soil-moisture concentration and surface temperature for this latter case, were compared with available measurements.

Two cases, one in which the potential evapotranspiration rate e_p was held constant at its annual average value and one in which e_p was allowed to change with time, were considered and the necessary modifications of the model for each case were discussed.
Sensitivity analysis was performed with respect to the depth of exchangeable moisture within the soil and also with respect to the surface roughness and deep soil temperature, when the thermodynamic coupling was considered.

For the catchments of Clinton, Massachusett, and Santa Paula, California, the soil and vegetation properties used were those obtained from the application of ecological optimality hypotheses (Eagleson 1982). According to these hypotheses only effective soil porosity n and the climate are necessary in order to determine k(1), c and the optimum vegetation properties M_o and k_v .

In order to apply the analytical model developed here to determine the landsurface boundary condition for use in GCM's of the atmosphere, the following steps should be followed:

1. Obtain at each grid point on the landsurface the representative climatic and soil parameters necessary to implement the model. Those parameters are described in Chapter 4 and the use of ecological optimality hypotheses, in order to reduce their number is also discussed.

2. Make an estimate of the surface layer thickness.

3. Estimate the average storm intensity and average potential evaporation rate every half-hour (or appropriate Δt) according to whether it is a precipitation or an interstorm period, respectively. If there is a precipitation period, calculate the time t_0 until the surface becomes saturated and let surface runoff be produced after that time if rain continues. If there is an interstorm period, calculate the time t_0 until the surface becomes dry and calculate evaporation before that time by setting it equal to the value of the (changing) potential evaporation rate.

4. Solve the linearized Equations (4.14) and (4.15) if a storm has occured, or Equation (4.16) if it is an interstorm period, every time period. Thus, an updated value of soil-moisture concentration will be obtained. Updated values of actual evaporation rate and of yield rate will also be obtained.

5. If the surface temperature is to be calculated, Equations (4.14)-(4.16) can be solved conjunctively with the equations of the force-restore method. In order to do that, estimates of the surface roughness and the initial deep soil temperature are necessary. In addition, knowledge of several meteorological variables at each time step will be necessary in order to estimate the changing value of e_p , which influences the thermal and water balance equations at the surface.

8.2 Conclusions

The model was tested using simulated rainstorm events for two contrasting climates and in both cases it was found to agree reasonably well with the solution of the numerical model. It was also tested against real measurements of soil-moisture during an evaporation period, and again it was found that it made very accurate predictions.

Thus, from the results obtained in this research, it can be stated that a simple second-order Budyko-type parameterization of the landsurface, compares favorably with "exact" numerical solutions for exchanges of water through the surface. Also, the parameterization suggested here is an improvement over the first-order Budyko-type model of Manabe (1969).

A range of depths of the soil-moisture layer was found for both tested climates, within which the cumulative evaporation and yield fluxes were rather insensitive to the layer depth. This range appears to include the actual root-zone depth.

In order to estimate the surface temperature, it was found that the forcerestore method is superior to the application of the thermodynamic equilibrium equation, but again difference with real measurements, although small, d'i exist. It must also be pointed out that in order to apply the force-restore method conjunctively with the analytical soil-moisture model developed here, parameters such as the surface roughness and the initial dee, soil temperature must be either known or fitted apriori to available data.

It should also be said that the very good agreement between analytical and numerical solutions for Santa Paula and for Clinton was obtained using soil properties derived from ecological optimality hypotheses. This provides one more indication of the applicability of these hypotheses.

8.3 Suggestions for Further Research

Using as a basis the simple landsurface parameterization developed in this study, the following additional studies should be carried out:

1. Test the model at other catchments particularly under soil-controlled conditions and for longer simulation periods.

2. Compare the model with other simple parameterizations in addition to the one suggested by Manabe (1969).

3. Investigate cases where $k_v \neq 1$ and possibly test the analytical model with more accurate numerical models which include vegetation.

4. Investigate the relation between the soil-moisture layer thickness and the soil properties k(1) and c for different climates.

5. Further investigate the sensitivity of the force-restore method with respect to the surface roughness coefficient and the deep soil temperature..

6. Use the short-term water balance model developed in this study conjunctively with measurements of soil moisture (obtained for example by

remote sensing). Thus, one equation representing system dynamics and one vector of observations will be available to apply optimal linear estimation techniques (linear filtering) and to make predictions of soil moisture.

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APPENDIX 1

FORTRAN PROGRAMS FOR SIMULATING SOIL-MOISTURE

AT THE SURFACE LAYER

1. PROGRAM TAYLOR, FORTRAN

ORIGINAL PACE IS OF POOR QUALITY

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C THIS PROGRAM GENERATES RAINSTORM EVENTS, STORM DURATIONS
C AND INTERSTORM PERIODS WHICH PRESERVE THE HISTORICAL STATISTICS.
C IT CALCULATES THE SOIL MOISTURE OVER A DEPTH CLOSE TO THE SURFACE
C EVERY HALF HOUR .IT PLOTS THE EVAPOTRANSPIRATION
C FUNCTION, THE SURFACE RUNOFF AND PERCOLATION FUNCTIONS.IT ALSO
C PLOTS THE DAILY SOIL MOISTURE DURING THE RAINY SEASON LENGTH.
C IT CALCULATES THE TOTAL STORAGE CHANGE, THE CUMULATIVE C EVAPORATION AND YIELD AT THE END OF EVERY RAINY OR
C INTERSTORM PERIOD
C IT HAS THE OPTION OF USING MANABE'S MODEL
C TO CALCULATE THE MOISTURE FLUXES
C THE VALUE OF THE POTENTIAL EVAPOTRANSPIRATION RATE
C IS SET EQUAL TO ITS ANNUAL AVERAGE VALUE
C ****
C CLIMATIC AND SOIL VARIABLES
c epr=average annual evapotranspiration rate(cm/day)
c mtb=mean time between storms(days)
c mtr=mean storm duration(days)
c mpa=mean annual precipitation(cm)
c mtau=mean rainy season length(days)
c ta=average annual air temperature(C)
c mnu=mean number of storms per year
c n=soil porosity
c k1=saturated intrinsic permeability(cm2)
c c=pore disconectedness index
c Zr=surface layer tkickness(cm)
c Mosvegetation cover
c Ky=plant coefficient
c k=parameter of gamma distibuted storm depths
c Lamda=parameter of gamma distributed storm depths
C ****
real min, mo, m, n, nu, k1, mtb, mtr, mh, in
real sjk(20), yi(20), soj(20), a77(20), b77(20), b78(20)
real da(365), SKP(315), st(365), b79(20), a79(20), ys(20), yg(20)
real a78(20), day(365
 fii(d, ;o)=1./(d*(1.~sc)**(1.45-.0375*d)+5./3.)
external plot_$setup (descriptors)
external plot_$scale (descriptors)
 external plot (descriptors)
character*10.xaxis,yaxis
 fi(em)=10.**(.66+.55/em+.14/em**2.)
 k11#1
 ran=1.
 print, 'To use Manabes parameterization type 2 , otherwise 1'
 input, mnb
 if(mnb.eq.1) go to 3020
 print, 'Input the initial soil moisture so'
 input, so
 go to 3021
  3020 print, 'Input the average annual soil moisture so'
 input.so
 print,'Input Time step (in days) '
 input.tis
 C NR=Number of rainstorm events you want to generate
```

```
3021 print, 'Input NR'
input,NR
print, 'Input storm properties k and Lamda'
input, xk, aml
if(mnb.eq.2) go to 3040
print, 'For daily fluxes type 1, for half hour fluxes type 2 '
input,fl
print, 'To plot S(t) type 2, otherwise 1'
input, lot
print, 'For cumulative fluxes after each storm and interstorm period type 2, otherwise 1'
input,ucu
print, 'To plot S(t) for different values of Zr type 2 , otherwise i'
input, szr
print, 'To print the cumulative fluxes only at the end of the rainy season type 2 , otherwise i'
input,fcu
3040 print, 'To print the rainstorm events type 2 , otherwise 1'
input, rae
11=1
3003 print, 'epr, mtb, mtr, mpa, mtau, ta, mnu, n'
input,epr,mtb,mtr,mpa,mtau,ta,mnu,n
if(mnb.eq.2) go to 3022
2020 print, 'Mo,Kv,k1,c,Zr'
input, vg, vk, k1, cs, zr
if(vg.eq.1) stop
if(ran.eq.2) go to 3004
if(dif.eq.2) go to 3004
C J(s)=evapotranspiration efficiency function
C Ys(s)=surface runoff function
C Yg(s)=ground water percollation function
1000 print, 'To plot J(s) and y(s) type 2 , otherwise 1'
input, p1
if(pl.eq.1) go to 3004
if(k11.eq.2) go to 3004
print, 'To draw different curves for J(s) for different climates type 2, otherwise 1'
input, dif
 double precision sumi, meani, mean2, mean3, B28
double precision sum2
double precision sum3
3004 if(ran.eq.2) go to 807
3022 if(rae.eq.1) go to 42
print.'STORM DEPTH STORM DURATION TIME BETWEEN '
print,
          (cm)
                        (days)
                                       (days) '
 42 11=1
C GENERATION OF RAISTORM EVENTS
C R1(I)=storm depth(cm)
 C R2(I)=storm duration(days)
 C R3(I)=interstorm duration(days)
 real R(500), WK(1000), R1(500), R2(500), R3(500)
 double precision DSEED
 DSEED=123765.0D0
 A=xk
 B-1./aml
  call ggamr(DSEED,A,NR,WK,R)
```

do 5 I=1,NR R(I) = B + R(I)5 continue do 41 I=1,NR R1(I)=R(I) 41 continue DSEED=3478758.0D0 A¤1. 8=mtr call ggamr(DSEED,A,NR,WK,R) do 7 I#1,NR R(I)=B*R(I) 7 continue do 21 I=1.NR R2(I)=R(I) 21 continue DSEED=649853.0D0 Ant. B#mtb call ggamr(DSEED,A,NR,WK,R) do 9 I=1,NR R(I) = B * R(I)9 continue do 30 I=1,NR R3(I)=R(I)30 continue if(ran.eq.2) go to 807 if(rae.eq.1) go to 3023 go to 3024 3023 if(mnb.eq.2) go to 3025 go tu 807 3024 dc 11 I=1,NR write(6,17) R1(I),R2(I),R3(I) 17 format(f10.6,4x,f10.6,4x,f10.6) 11 continue 807 m=2./(cs-3.) d=cs-1./m-1 dE=2.+1./m fied=fie(dE) C COMPUTE WATER CONSTANTS Gall WATCN(ta,sut,nu,gamsw) C COMPUTE CLIMATIC PARAMETERS delta=1./mtr mh=mpa/(mtau/(mtb+mtr)) amnu=mtau/(mtb+mtr) mi≊mh/mtr eta=1./mh alpna=1./mi p1=3,14159 beta=1./mtb C COMPUTE DERIVATIVE OF J WITH RESPECT TO SO

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H

den=(1.425-0.0375+d) if(pl.eq.1) go to 802 k=0 50°0. 805 30=50+0.05 go to 802 862 ds*(1.-so)*+den dds=ds+d deno=dds+(5./3.) denom = deno = (4./3.)500*1.-50 501=500++(-4./3.) denos=2+soo+deno dt=(2.425-0.0375+d) 502#500##dt deos1=so2+d+den nom=-denos-deos1 nom1=nom+so1 der=nom1/(denom+3) fic=fi(m) sil=sqrt(n/(k1+fic))+sut/gamsw si11=si1=so++(-1./m) bk1=k1+gamsw/nu sigc=n+eta++2.+bk1+s11/(pi+m+delta)+72000. sigc1=sigc++0.33333333 dersig=sigci=der sia=5+n+bk1+86400+s11/(3+m+p1) sigma=(sigc/deno+(1.-so)++2.)++.333333 g=alpha+bk1+86400+.5+(1.+so++cs) gl=alog10(sigma) xp=(1.766+g1)+(0.980+(g1++2.)) xp1=-.806-xp CSI=10. ++xp1 xp2=(1.96+g1)+1.766 U=-dersig+xp2/sigma co=alpha+86400+bk1/2.*cs+so++(cs-1.) col=U-co C2=co1+CSI+exp(-g) C38=mtau+86400+bk1+cs/mpa+so++(ca-1.) C3ºC.8/2. if(vg.eq.0) go to 80 go to 90 80 E=2.*beta*n*bk1*si1*fied/(p1*m*epr**2.)*86400*so**(d+2.) if(E.ge.88.) E=88. z1=(1.+E+sqrt(2.))+exp(-E) z2=gamma(1.5)-gamt(1.5,E) z2=z2+sqrt(2.*E) sj=1.-z1+z2 if(pl.eq.1) go to 803 k=k+1 sjk(k)=sj if(k.eq.20) go to 804 go to 805 803 ag=gamma(1.5)-gamt(1.5,E) gimexp(-E)*sqrt(2.) g2=E+sqrt(2.)+1. g2=g2=exp(-E)

```
g3=ag+sqrt(2.)/(2.+sqrt(E))
g4=exp(-E)*sqrt(E)*sqrt(2*E)
gg=-g1+g2+g3-g4
Eli=2.*beta+n*bk1+si1+fied/(pi+m+epro+2.)+86400
E12=(d+2.)+50++(d+1.)
der1j=gg+E11+E12
 Cisderij
if(C1.1e.0) C1=0.0
go to 100
90 B=(1.-vg)/(1.+(vg+vk))
B=B+(vk+vg++2.)/(2.+(1.+(vg+vk))++2.)
 C=1./(2.*(vg*vk)**2.)
E1=2.*beta*n*bk1*si1*fied/(pi*m*epr**2.)*86400
E=2.*beta*n*bk1*si1*fied/(pi*m*epr**2.)*86400*so**(d+2.)
o1=B+((vg+vk)+1)
01=-01+sqrt(B+2.)
o11=B*E*sqrt(2.+B)
01=01-011
o1=o1+exp(-B+E)
01=01+E1+(d+2.)
o1=o1+(so++(d+1.))
o2=-vg+vk+C
02=02+sqrt(2+C)
02=02-(C+sqrt(2+C)+E)
 C88=C+E
if(C88.ge.88) C88=88.
02=02+exp(.C88)*E1*(d+2.)
02*02*(50**(d+1.))
 CE=U+E
8E*8*E
at=(vg+vk)+1.
a2=E*sqrt(2.*B)
a3=a1+a2
 if(BE.ge.88.) BE=88.
a3=a3*exp(-BE)
a4=vg+vk
84=a4+(E*sqrt(2.*C))
 1f(CE.ge.88.) CE=88.
 a4=a4=exp(-CE)
 a5=gamt(1.5,CE)-gamt(1.5,BE)
 a5=a5*sqrt(2.*E)
 a6=a3-a4-a5
 a6=a6*(1, vg)/(1, -vg+(v_{9}*vk))
 sj=1.-a6
 if(pl.eq.1) go to 806
 k=k+1
 sjk(k)=sj
 if(k.eq.20) gu to 804
 go to 805
 806 o3=gamt(1.5,CE)-gamt(1.5,BE)
 03=03+sqrt(2.+E1)
 03*(1.+d/2.)*03*(so**(d/2.))
 031=-C+E1+(so++(d+2,))
 031=(C++1.5)+exp(031)
 O32=-B*E1*(so**(d+2.))
 o32=(B**1.5)*exp(o32)
 033=031-032
 033=033*(E1++1.5)
 033=033*(2.+d)
```

```
o33=o33*(so**((1.5+d)+2.))
033=033+sqrt(2.+E)
03=03+033
derj=01-02-03
deri=derj+(1.-vg)
derj=-derj/((vg+vk)+1.-vg)
Clederj
1f(C1.1e.0) C1=0.0
B28=mtau+bk1+86400/mpa+so++cs
C **********
                                      ***********************
C DimDerivative of J with respect to s
C2=Derivative of Ys with respect to s
C C38=Derivative of Yg with respect to s
C sjed(so)
C sillepsi evaluated at so
C bkissaturated hydraulic conductivity (cm/sec)
100 print101,C1,C2,C38,5j,5111,bk1
101 format(3hC1=,f10.6,4x,3hC2=,f10.6,4x,3hC3=,f10.6,4x,2hJ=,f10.6,4x,3hHH=,f10.2,4x,f20.10)
SK=so
804 p=mpa/(mnu+mtr)
 C1=C1+epr
B1=sj+epr
if(pl.eq.1) go to 808
50=0.
k=0
811 so=so+0.05
ds=d+(1.-so)++den
deno=ds+(5./3.)
sigma=(sigc/deno+(1.-so)++2.)++.333333
808 B22=sigma++(-sigma)
sigmesigma+1.
B22=B22*gamma(sigm)
B2=B22+exp(-g-(2+sigma))
B28=mtau+bk1+86400/mpa+so++cs
84=82+p
85=828+p+mnu+mtr/mtau
if(pl.eq.1) go to 809
k=k+1
ys(k)=84
yg(k)∘B5
soj(k)¤so
 if(k.eq.20) go to 810
go to 811
809 if(ucu.eq.2) go to 1816
 print,' S(t)
                  i(cm/day)
                                 Et(cm/day)
                                                yieid(cm/day)
                                                                   DAY '
go to 1815
C ****
                                              *************
                ********************
C CALCULATE THE SOIL MOISTURE CONCENTRATION AND THE
C CUMULATIVE EVAPORATION AND YIELD AT THE END OF
C EVERY RAISTORM AND INTERSTORM PERIOD
 1816 print, 'SOIL, MOIST, CUM, EVAP, CUM, YIELD'
 1815 1f(p1.eq.1) go to 812
810 1f(k11.eq.2) go to 3001
```

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```
C PLOT J VERSUS H
call plot $setup(' '.'s','J',1,0,0,0)
call plot $seale(0.,1.,0.,1.)
3001 1-0
K11=2
do 813 j+1,20
1=1+1
b77(1)+sjk(j)
a/7(1) *soj(j)
813 continue
call plot (#77,677,20,1,1 1)
if(dif,eq.1) go to 3002
00 to 3003
3002 read(8,)
C *********
                      C PLOT YO AND YO VERSUS 8
call plot $setup(' ', 'SOIL MOISTURE', 'SURFACE RUNDER', 1,0,0,0)
 call plot $8cale(0.,1.,0.,2.)
1=0
do 814 j=1,20
1=1+1
b78(1)=ys(j)
a78(1)+soj(j)
814 continue
eall plot_(a78, b78, 20, 1, ' ')
read(b,)
 call plot_$setup(' ','SOIL MOISTURE','GROUNDWATER RUNDEF', 1,0,0,0)
 call plot $scale(0.,1.,0.,2.)
1.40
do 834 j#1,20
1+1+1
b79(1)=yg(1)
a79(1)=Boj(j)
834 continue
call plot_(a79, b79, 20, 1, ' ')
po to 1000
812 17(821.00.1) po to 817
do 2001 11+1,2
print, 'Input Zr(em)'
Input, gr
817 a=n+zr
Dt*tis
K=O
KP+0
1=0
LM+O
SK3+0.0
SK2*0.0
LMM*O
yialder0.0
evepe*0.0
400 If (ueu, eq. 1) go to 401
 If (szr.eq. 2) go to 401
```

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if(fcu.eq.2) go to 40i
write(6,1701)SK,evapc,yieldc 1701 format(f8.5,4x,f8.5,4x,f8.5) C ******* ******* C CALCULATE THE VALUE OF SOIL MOISTURE EVERY HALF HOUR C DURING A PRECIPITATION EVENT ****** C ************** 401 Dt1=0. yt=0.0 sial=sia+fii(d,SK) sia2=2*(1.-SK)*sqrt(sia1) Ao=bk1+86400/2. 1f(SK.1e.0) go to 215 ao1=Ao*(1.+(SK**cs)) go to 216 215 ao1=Ao 216 I=I+1 r2=R2(I) in=R1(I)/r2 To1=2+in+(in-ao1) to2=s1a2++2./To1 to3=2.*(1n-ao1) to4=1.+(ao1/to3) To=to2+to4 300 Dt1=Dt1+Dt if(Dt1.ge.r2) go to 200 LM=LM+1 if(Dti.ge.To) yt=1 if(SK2.it.SK3) yt=0.0 SK1=SK+(in-p*((B2*yt)+(B28*mnu*mtr/mtau))-p*(SK-so)*((C2*yt)+(C3*mnu*mtr/mtau)))*Dt/a SK2=SK1 SK3=SK if(SK1.ge.0.999) go to 211 go to 212 211 SK1=0.999 vield*in yieldc=yieldc+(in*tis) go to 213 212 yield=p*((B2*yt)+(B28*mnu*mtr/mtau))+p*(SK-so)*((C2*yt)+(C3*mnu*mtr/mtau)) yieldc=yieldc+(yield*tis) 213 SK=SK1 if(fl.eq.1) go to 250 if(szr.eq.2) go to 300 write(6,210) SK,in,yield 210 format(f8.5,4x,f8.5,22x,f8.5) go to 300 250 tiss=1./tis if(LM.ge.tiss) go to 251 go to 300 251 LM=0 LMM¤LMM+1 if(LMM.gt.mtau) go to 900 KP=KP+1 SKP(KP)≈SK da(KP)=LMM if(vcu.eq.2) go to 300 if(szr.eq.2) go to 300 write(6,252) SK,in,yield,LMM

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oncease the IS OF POOR QUALITY 252 format(f8.5,4x,f8.5,22x,f8.5,9x,15) go to 300 200 if(ucu.eq.1) go to 201 if(fcu.eq.2) go to 201 write(6,1700) SK,yieldc,yt 1700 format(#8.5,16x,f8.5,4x,f3.1) ************ C CALCULATE THE VALUE OF SOIL MOISTURE EVERY HALF HOUR C DURING AN INTERSTORM PERIOD C **** 201 Dt1=0. 500 Dt1=Dt1+Dt r3=R3(1) if(Dti.ge.r3) go to 400 LM=LM+1 evap=B1+(C1*(SK-so)) if(evap.ge.epr) go to 600 evapp=evap/epr if(evapp.le.vg) go to 701 SK1=SK-(evap+(B2G*p*mnu*mtr/mtau)+(C3*p*mnu*mtr*(SK-so)/mtau))*Dt/a evapc=evapc+(evap*tis) go to 700 600 evap∍epr evapc=evapc+(evap*tis) SK1=SK-(epr*Dt/a)-((B28*p*mnu*mtr/mtau)+(C3*p*mnu*mtr*(SK-so)/mtau))*Dt/a go to 700 701 evap*epr*vg evapc=evapc+(evap*tis) SK1=SK-(evap*Dt/a)-((B28*p*mnu*mtr/mtau)+(C3*p*mnu*mtr*(SK-so)/mtau))*Dt/a 700 yield=(B28*p*mnu*mtr/mtau)+(C3*p*mnu*mtr*(SK-so)/mtau) if(yield.le.0.0000001) yield=0.0000001 yieldc=yieldc+(yield*tis) SK=SK1 if(f1.eq.1) go to 750 if(szr.eq.2) go to 757 write(6,220) SK,evap,yield 220 format(f8.5,16x,f8.5,10x,f8.5) 757 K=K+1 if(K.ge.1000) stop go to 500 750 tiss=1./tis if(LM.ge.tiss) go to 751 go to 500 751 LM=0 LMM=LMM+1 if(LMM.le.mtau) go to 901 write(6,905) SK,evapc,yieldc 905 format(f8.5,4x,f8.5,4x,f8.5) go to 900 901 KP=KP+1 SKP(KP)=SK da(KP)=LMM if (ucu.eq.2) go to 500 if(szr.eq.2) go to 500 write(6,752) SK,evap,yield,LMM 752 format(f8.5,16x,f8.5,10x,f8.5,9x,15) go to 500 900 if(szr.eq.2) go to 2008 if(ran.eq.2) go to 2031

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C ***
                                                ********
C CALCULATE THE STATISTICAL PROPERTIES OF THE GENERATED
C RAINSTORM EVENTS
*******
print, 'Statistical properties of the simulated rainstorm characteristics'
sum1≈0.0D0
sum2=0.0D0
sum3=0.0D0
do 1001 IL=1.I
sum1=sum1+R1(IL)
sum2=sum2+R2(IL)
sum3=sum3+R3(IL)
1001 continue
mean1=sum1/(float(I))
mean2=sum2/(float(I))
mean3=sum3/(float(I))
var1=0.0
var2=0.0
var3=0.0
do 1002 IL=1,I
vari=vari+((Ri(IL)-meani)**2.)
var2=var2+((R2(IL)-mean2)**2.)
var3=var3+((R3(IL)-mean3)**2.)
1002 continue
vari1=var1/float(I-1)
vari2=var2/float(I-1)
vari3=var3/float(I-1)
print,'AVER.h(cm)
                     AVER.tr(days)
                                     AVER.tb(days) '
write(6,1003) mean1, mean2, mean3
1003 format(f10.6,6x,f10.6,6x,f10.6)
print,' VAR.h
                     VAR.tr
                                     VAR.tb'
print 1004, varii, vari2, vari3
1004 format(f8.2,4x,f8.2,10x,f8.2)
ran=2.
2031 if(lot.eq.2) go to 2030
go to 2020
2030 read(5,)
2008 if(i1.gt.1) go to 2003
C PLOT THE SOIL MOISTURE CONCENTRATION WITHIN THE
C LAYER OF THICKNESS Zr VERSUS TIME DURING THE
C RAINY SEASON LENGTH
 C **
                       *******
  call plot_$setup(' ','DAYS','SOIL MOISTURE',1,0,0,0)
 call plot_$scale(1.,220.,0.,1.)
 2003 1=0
 do 910 j=1,LMM
 1=1+1
 st(1)=SKP(1)
 day(1)=da(j)
 910 continue
 if(il.eq.1) go to 2004
 if(il.eq.2) go to 2005
 2005 call plot_(day,st,mtau,3,'.')
 go to 2001
 2004 call plot_(day,st,mtau,1,' ')
 if(szr.eq.1) go to 2000
```

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2001 continue
C *
C CALCULATE THE MOISTURE FLUXES USING MANABE'S PARAMETERIZATION
3025 if(mnb.eq.1) go to 2000
print, 'S(t)
              CUM.EVAP.
                          CUM.YIELD'
SK=so
Dt=1./48.
I=0
yieldc=0.0
evapc=0.0
Dt11=0.0
3031 write(6,3033) SK,evapc,yieldc
3033 format(f8.5,4x,f8.5,4x,f8.5)
Dt1=0.0
I=I+1
r2=R2(I)
in=R1(I)/r2
3028 Dt1=Dt1+Dt
Dt11=Dt11+Dt
if(SK.ge.0.42) go to 3029
SK1=SK+1n+Dt/(n+100)
SK=SK1
if(Dti.ge.r2) go to 3027
go to 3028
3029 yield=(in-epr)+Dt
yieldc=yieldc+yield
if(Dt1.ge.r2) go to 3027
go to 3028
3027 write(6,3030) SK,evapc,yieldc
3030 format(f8.5,4x,f8.8,4x,f8.5)
Dt1=0.0
r3=R3(I)
3032 Dt1=Dt1+Dt
Dt11=Dt11+Dt
evap=epr
 if(SK.1t.0.315) evap=epr+SK/0.315
 SK1=SK-evap+Dt/(n+100)
evapc=evapc+(evap*Dt)
 SK=SK1
 if(Dt11.ge.mtau) stop
 if(Dt1.ge.r3) go to 3031
 go to 3032
2000 read(5,)
 stop
 end
 subroutine WATCN(ta,sut,nu,gamsw)
 real nu, nut
 dimension sutt(11), nut(11), gamst(11)
 data sutt/75.6,74.9,74.2,73.5,72.80,72.1,71.4,70.7,70.0,69.3,68.6/
 data nut/17.93e-3,15.18e-3,13.09e-3,11.44e-3,10.08e-3,8.94e-3,
 & 8.e-3,7.2e-3,6.53e-3,5.97e-3,5.94e-3/
 data gamst/0.99987,0.99999999,0.99973,0.99913,0.99823,0.99708,
```

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8 0.99568.0.99406.0.99225.0.99025.0.98807/
if(ta.gt.50.)go to 10
ita=ifix(ta+.2)+1
frac=ta-float(5+(ita-i))
ita1=ita+i
sut=(sutt(ita1)-sutt(ita))+0.2+frac+sutt(ita)
nu=(nut(ita1)-nut(ita))+0.2+frac+nut(ita)
gamsw=((gamst(ita1)-gamst(ita))*.2*frac+gamst(ita))*980.
return
10 sut=sutt(11)
nu=nut(11)
gamsw=gamst(11)
return
end
C **
       ********
c this function computes the gamma incomplete function
C *
                                                  . . . . . . . . . . . .
function gamt(a,x)
if(x.eq.0)go to 40
if(x.gt.100)go to 50
sum=1./a
an=1.0
oldesum
33 old=old+x/(a+an)
lf(01d/sum-1.e-6)20,10,10
10 an=an+1.
sum=sum+old
if (an-300.)33,33,12
12 continue
20 xxx=(a+alog(x)+alog(sum)-x)
if(xxx.1t.-80.)go to 40
gamt=(exp(xxx))
go to 60
40 gamt#0.0
go to 60
50 gamt=gamma(a)
60 return
end
C +++
              c This function computes the gamma function by a Stirling approx.
function gamma(y)
x=y+1.
 p1=3.14159
 stir1=1./(12.+x)
 stir2=1./(288.+x++2.)
 stir3=-139./(51R+0.*x*+3.)
stir4=-571./(2488320.*x*+4.)
 stir=1+stir1+stir2+stir3+stir4
 gamma=exp(-x)*x**(x-.5)*sqrt(2.*pi)*stir/y
 end
 function fie(d)
 dimension y(6)
 data y/0.18,0.11,0.077,0.056,0.044,0.034/
 if(d.gt.7.)go to 10
 x=d-1.
 i=ifix(x)
 frac=x-float(i)
 y_{1=alog(y(1))}
 y_{2=alog}(y(i+1))
```

fie¤exp((y2-y1)*frac+y1) return 10 fie¤.034 return end ORIGINAL FAGLES OF POOR QUALINY

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2. PROGRAM ARIZ.FORTRAN

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C ...............
C THIS PROGRAM CALCULATES THE AVERAGE SOIL MOISTURE CONCENTRATION C OVER 1m DEPTH EVERY HALF HOUR , DURING AN EVAPORATION PERIOD WITH
C A CHANGING VALUE OF THE POTENTIAL EVAPORATION RATE.
C IT ALSO CALCULATES THE SURFACE TEMPERATURE USING THE FORCE-
C RESTORE METHOD OR THE THERMODYNAMIC EQUILIBRIUM EQUATION.
C THE POTENTIAL EVAPORATION RATE IS CALCULATED EITHER USING
C PENMAN'S EQUATION OR THE AERODYNAMIC EQUATION.
C ATMOSPHERIC INSTABILITY CRITERIA ARE USED.
  THE SHORT-TERM WATER AND THERMAL BALANCES CAN BE SOLVED SIMULTANEOUSLY
C AND THE SOIL MOISTURE CONCENTRATION AND SURFACE TEMPERATURE
C CAN BE CALCULATED AND PLOTED
C THIS PROGRAM READS FROM FILE 31 THE METEOROLOGIC
C VARIABLES AND THE SOIL MOISTURE CONCENTRATION MEASUREMENTS.
C WHICH ARE GIVEN EVERY HALF HOUR.
C ************
C THE CLIMATIC VARIABLES AND SOIL PARAMETERS USED AS INPUTS
C TO THIS MODEL ARE DESCRIBED BELOW.
c epr#annual average potential evaporation rate(cm/day)
c mpa=mean annual precipitation(cm)
c mtr=mean storm duration(days)
c mtaummean rainy season length(days)
c mnu=mean number of storms per year
c J=evapotranspiration efficiency
c C1=derivative of J with respect to s
c C3=derivative of percolation rate with respect to s
c somaverage annual soil moisture
c SK=initial soil moisture at 1m depth
c n≃porosity
c Zr=surface layer thichness
c K(1)=saturated hydraulic conductivity (cm/sec)
c capore disconactedness index
c a(1,1)=net radiation(ly/min)
c a(1,2)=air temperature(C)
c a(1,3)=water vapor pressure of air (mb)
c a(1,4)=wind speed(cm/sec)
c a(1,5)=average soil moisture content in O-10cm
c a(1,6) average soil moisture content in 10-50cm
c a(1,7)=average soil moisture content in 50-100cm
c a(1,8)=ground temperature at 1cm (C)
 c Tg=calculated surface temperature(C)
c T2=deep soil temperature(C)
 c (cH)n=drag coefficient under neutral conditions
 real a(337,8),ep1(337),hr(337),ASK(337)
 real epp(337),hrr(337)
real AsK(337),SK2(337),hr1(337),SK3(337),hr2(337)
 real AsK1(337), TgCC(337), TgC1(337), TgKK(337)
 real ToCM(337)
 external plot_$setup (descriptors)
 external plot_$scale (descriptors)
external plot_(descriptors)
 real mpa, mtau, mtr, mnu, k1, m
 fi(em)=10.**(.66+.55/em+.14/em**2.)
 dcuble precision B,ga,gd,gd1,bet,deno,T,es,dif,H,nom,ep,B28
```

```
print, 'epr, mpa, mtr, mtau, mnu, J, C1, C3, so, SK, n, Zr, K(1), c'
input,epr,mpa,mtr,mtau,mnu,sj,C1,C3,so,SK,un,zr,bk1,cs
read(31,) ((a(1,j), i=1,337), j=1.8)
print, 'To print file31 type2, otherwise type 1'
input, ty
print, 'To plot ep type i,otherwise type 2'
input, pr
print, 'To print ep write 2 ,otherwise 1'
input.pr1
print, 'To print soil moisture type 2 ,otherwise1'
input.pt
print, To calculate the surface temperature type 2, otherwise 1'
input, tmr
if(tmr.eq.1) go to 200 print, 'Input the initial surface temperature Tg, T2 (in degrees Celcius) and (CH)n'
input, TgC, T2, cHn
print, 'To solve simultaneously the equations for soil moisture
& and temperature using the aerodynamic equation and
& the instability criteria type 2 . otherwise 1'
input, aer
print, 'To use the thermodynamic equation type 2 , otherwise 1'
input, thm
if(thm.eq.1) go to 305
print, 'Input k(1), Ta'
input, k1, ta
m=2./(cs-3.)
fic=fi(m)
C ****
           **************
C COMPUTE WATER CONSTANTS
call WATCN(ta,sut,nu,gamsw)
si1=sqrt(un/(k1+fic))+sut/gamsw
305 T2=T2+273.16
TgK=TgC+273.16
TgF = (9. * TgC/5.) + 32.
TgKK(1)=TgK
200 if(ty.eq.1) go to 41
do 40 1=1,337
write((6, 20) a((1, 1), a((1, 2), a((1, 3), a((1, 4), a((1, 5), a((1, 6), a((1, 7), a((1, 8))
20 format(f10.4,2x,f10.4,2x,f10.4,2x,f10.4,2x,f10.4,2x,f10.4,2x,f10.4,2x,f10.4,2x,f10.4)
40 continue
41 h=-0.5
sum=0.0
                              .
 do 46 1=1,337
c CALCULATE ep USING PENMAN'S EQUATION
C ******
              ************
                                    *************
ga=(a(1,2)+0.013)+0.42
                                                                        .
gd1=1./ga
gd×gd1-1.
deno=597.*gd1
bet=200./0.03
bet=alog(bet)
bet=bet#+2.
B=10.++(-7)
B=1.222+B
B=B+a(1,4)+60.
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B=B/bet
T=273.16+a(1,2)
es=273.16/T
es=1.-es
es=es+(5.00650+19.83923)
es=exp(es)
es1=(273.16/T)++5.00650
es=(is+es1+6.11
dif#es-a(1,3)
H=597.+B+dif+gd
nom=H+a(1,1)
64 ep=nom/deno
ep=ep+60.+24.
h=h+0.5
ep1(1) ep
hr(i)=h
sum=sum+epi(i)
if(pri.eq.1) go to 46
write(6,45) ep
45 format(f10.4)
46 continue
avep=sum/337.
write(6,60) avep
60 format(2x, f10, 4)
 if(pr.eq.2) go to 61
call plot_$setup('Potential Evaporation','Hours','ep',1,0,0,0)
 call plot_$scale(0.,168.,-0.15,2.)
61 1=0
do 51 j=1,337
 1=1+1
epp(i)=epi(j)
hrr(i)=hr()
51 continue
 if(pr.eq.2) go to 63
-----
                                          ************************
C CALCULATE THE UPDATED SOIL MOISTURE
C ********
                                           ******************
            ********
 63 al=un=zr
 hr8=-0,5
 p=mpa/(mnu+mtr)
 B28=mtau+bk1+86400./mpa+so++cs
 Dt=1./48.
 C33=C3/2.
 do 100 1=1,337
 ASK(1)=(0.10*a(1,5))+(0.40*a(1,6))+(0.50*a(1,7))
 B1=sj*epr
 ci=C1+epr
 yt¤0.0
 evap=B1+(c1+(SK-so))
 if(1.1e.196) go to 108
 if(evap.lt.epi(i)) go to 107
 108 evap=epi(1)
 yt¤1.0
 107 A#K(1)=ASK(1)/0.35
 ASKK#/ sk(1)
 SK2(1)=SK
 hr1(1)-br8+0.5
 SK1=SK-(evap+(B28+p*mnu*mtr/mtau)+(C33+p*mnu*mtr*(SK-so)/mtau))*Dt/a1
```

```
if(pt.eq.1) go to 102
write(6,101) ASKK,SK,yt
101 format(f10.4,4x,f10.4,4x,f3.1)
102 SK#SK1
hr8=hri(1)
100 continue
if(tmr.eq.2) go to 290
                  C ************
C PLOT THE CALCULATED AND MEASURED SOIL MOISTURE CONCENTRATION
C AT DEPTH OF 1m . USING PENMAN'S EQUATION TO CALCULATE op
C .....
 call plot_$setup(' ','HOURS','SOIL MOISTURE',1,0,0,0)
 call plot_$scale(0.,170.,0.62,0.70)
1=0
do 110 j=1,337
1=1+1
AsK1(1)=AsK(1)
SK3(1)=SK2(j)
hr2(1) * hr1(j)
110 continue
call plot_ (hr2,5K3,337,3,'.')
call plot_ (hr2,AsK1,337,1,'')
290 Dt=1800.
if(tmr.eq.i) go to 210
Ev1=-10.
SUM=0.0
L=1
print, 'Average Daily Evaporation Rate(cm/day)'
SK=SK2(1)
****
C CALCULATE OP USING THE AERODYNAMIC EQUATION AND THE
C ATMOSPHERIC INSTABILITY CRITERIA(surface roughness 0.05cm)
C ***
                                                             *****
 do 250 1=1,337
TgA=a(1,2)+273.16
SK2(1)=SK
est=6.11+(0.339*(TgF-32.))
if(i.le.196) go to 260
Ev11=B1+(c1+(SK2(i)-so))
 Ev1=Ev11/86400
 260 R1*2.*981*100.*(TgA-TgK)/((TgA+TgK)*(a(1,4)**2.))
 if(Ri.ge.0.2) rat=0.0
 if(Ri.it.O.2.and.Ri.ge.O.1) ret=(-2.+Ri)+O.4
 if(Ri.lt.O.1.and.Ri.ge.O.O) rat=(-8.*Ri)+1.
 if(R1.1t.0.0.and.R1.ge.-0.1) rat=1.30
 if(Ri.lt.-0.1.and.Ri.ge.-0.2) rat=1.8
if(Ri.lt.-0.2.and.Ri.ge.-0.3) rat=2.2
 if(R1.1t.-0.3.and.R1.ge.-0.4) rat=2.45
 if(Ri.lt.-0.4) rat=2.7
  cH°cHn*rat
  Ev*cH*(730.5e-9)*a(1,4)*(est-a(1,3))
 if(1.1e.196) go to 262
 if(Ev.ge.Ev1) Ev=Ev1
 if(thm.eq.1) go to 262
 1f(Ev.1t.Ev1) go to 262
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*************
C **
                   C CALCULATE THE SURFACE TEMPERATURE USING THE C THERMODYNAMIC EQUILIBRIUM EQUATION
                                   C *
est1=Ev1/(cH+(730.5e-9)*a(1,4))
est=est1+a(1,3)
sit1=si1+SK++(-1./m)
ex=981.*5111/((2.876e+6)*ToK)
rh#exp(ex)
TgF1=est-(rh+6.11)+(0.339+32.*rh)
TgF=TgF1/(0.339+rh)
j=1+1
TgKK(j)=(5.+(TgF-32.)/9.)+273.16
TgK=TgKK(j)
262 if(aer.eq.1) go to 261
SK1=SK-((Ev+86400.)+(B28+p+mnu*mtr/mtau)+(C33+p+mnu*mtr+(SK-so)/mtau))/(48.*a1)
SK#SK1
if(Ev.1t.Ev1) go to 261
if(1.1e.196) go to 261
if(thm.eq.2) go to 250
261 Hs=cH+(285.48e-6)+a(1,4)+(TgK-TgA)
Le=597.3-(0.57+TgC)
G=(a(i,i)/60.)-Hs-(Le*Ev)
j≈i+i
                                ********
C ***************************
C COMPUTE SURFACE TEMPERATURE
             C ***
TgKK(j)=TgKK(1)+(2.+G+Dt/7.37)-((72.720-6)+Dt+(TgKK(1)-T2))
TgC=TgKK(j)-225.16
 TgF = (9. * TgC/5.) + 32.
TgK=TgKK(j)
 T2=T2+(G*Dt/249.68)
 SUM=SUM+(Ev+86400.)
 L=L+1
 if(L.1t.48) go to 250
 AEv=SUM/48.
 write(6,400) AEV
 400 format(2x, f8.4)
 L=1
 SUM=0.0
 250 continue
                                              .................
 C PLOT CALCULATED AND MEASURED SURFACE TEMPERATURE
 C USING THE AERODYNAMIC EQUATION
                           *******
 C #8#
  call plot_$setup(' ','HOURS','SURFACE TEMPERATURE',1,0,0,0)
  call plot_$scale(0.,170.,-2.,40.)
 do 270 1=1,337
 TgCC(1)=TgKK(1)-273.16
 270 continue
 1≃0
 do 280 j=1,337
 1=1+1
 TgCM(1)=a(1.8)
 TgC1(1)=TgCC(j)
```

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hr2(1) + hr1(j)
280 continue
call plot (hr2,TgC1,337,3,'.')
call plot (hr2,TgCM,337,1,'')
if(aer.eq.1) go to 210
read(5,)
 call plot_$setup(' ','HOURS','SOIL MDISTURE',1,0,0,0)
call plot_$scale(0.,170.,0.61,0.70)
1=0
do 300 j=1,337
1=1+1
SK3(1)=SK2(J)
AsK1(1)=AsK(j)
hr2(1)=hr1(j)
300 continue
C ***
                                                            ******
C PLOT CALCULATED AND MEASURED SOIL MOISTURE DERIVED BY
C USING THE AERODYNAMIC EQUATION FOR ESTIMATING op
C ********
                                                       ***********
 call plot_ (hr2,5K3,337,3,'.')
call plot_ (hr2,AsK1,337,1,'')
210 stop
end
C ********
                 subroutine WATCN(ta,sut,nu,gamsw)
real nu, nut
dimension sutt(11), nut(11), gamst(11)
date sutt/75.6,74.9,74.2,73.5,72.80,72.1,71.4,70.7,70.0,69.3,68.6/
data nut/17.93e-3,15.18e-3,13.09e-3,11.44e-3,10.02e-3,8.94e-3,
& 8.e-3,7.2e-3,6.53e-3,5.97e-3,5.94e-3/
data gamst/0.99987,0.9999999999,0.99973,0.99913,0.99823,0.99708,
& 0.99568,0.99406,0.99225,0.99025,0.98807/
if(ta.gt.50.) go to 10 ita=ifix(ta+.2)+1
frac=ta-float(5*(ita-1))
1ta1=ita+1
sut=(sutt(ita1)-sutt(ita))*0.2*frac+sutt(ita)
nu=(nut(ita1)-nut(ita))*0.2*frac+nut(ita)
gamsw=((gamst(itai)-gamst(ita))*.2*frac+gamst(ita))*980.
return
 10 sut=sutt(11)
nu=nut(11)
gamsw=gamst(11)
return
```

end

APPENDIX 2

DOCUMENTATION OF THE COMPUTER PROGRAM SPLASH

Documentation of the Computer Program SPLASH

A complete documentation of the computer program SPLASH.FORTRAN is given by Milly and Eagleson (1980). Here, only the procedure to achieve convergence of the results will be described and the way of attaching a file to it, including the boundary conditions of the area under investigation.

Two parameters were varied in order to achieve convergence. Those were:

1. XERR

The parameter XERR represents the maximum allowed change of soil-moisture at every node and at every time-step. That is,

$$XERR = \max_{nodes i} \left[|\Theta_{i}(t+\Delta t) - \Theta_{i}(t)| \right].$$

As this parameter decreases, the accuracy of calculations increases. In studying the catchments of Santa Paula and Clinton, it was found that convergence of the results occurs when XERR = 0.0005.

2. ZRAT

The parameter ZRAT is given by:

$$ZRAT = \frac{(length of top element) \times (number of elements)}{(total column length)}$$

For a fixed number of nodes, the value of ZRAT was varied until satisfactory convergence was achieved. The results for Clinton, Massachusetts and Santa Paula, California are shown in Figures 31 and 32, respectively.

It was found that satisfactory convergence is achieved for Clinton, when XERR = 0.0005, ZRAT = 0.01 and n = 21. For Santa Paula it was found that convergence can be considered achieved when XERR = 0.0005, ZRAT = 0.01, and n = 41.

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Convergence Experiments (Clinton, Massachusetts) FIGURE 31



OF POOR QUALLE

Inputs for SPLASH

First the program "input" described by Milly and Eagleson (1980) must be run, in which the number of nodes and the manner of setting up the nodes is established, and also the parameters XERR and initial $\psi(s)$ are defined.

By running "input" File 98 is created. This file must then be combined with a file including the soil properties and the atmospheric boundary conditions of the area under investigation. This file is also described with details by Milly and Eagleson (1980). By combining those two files, File 15 is created.

Then, the program SPLASH.FORTRAN is ready to run, using as input File 15.