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Measurements in the Wake of an 'Infinite' Swept Airfoil

Iowa Inst. of Hydraulic Research, Iowa City

Prepared for

National Aeronautics and Space Administration Washington, DC

Apr 82

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C. J. Novak, and B. R. Ramaprian.

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IIHR Report No. 240

Iowa Institute of Hydraulic Research The University of Iowa Iowa City, Iowa 52242

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ABSTRACT

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TABLE OF CONTENTS

			Page
LIST OF TABLES			vi
LIST OF FIGURES	5		iii
LIST OF SYMBOLS	i		xi
CHAPTER			
I	INT	RODUCTION	1
	1.	The Problem Introduced	1
		ELOPMENT OF THREE-DIMENSIONAL HOT-WIRE TRUMENTATION	5
	1.	Problem Description and Quantities Requiring Measurement	5
:	2.	Available Techniques and a Relative Assessment	5
		<pre>2.1 Method A 2.2 Method B 2.3 Method C 2.4 Description of the Probe 7 </pre>	7 9 11 12
		 Signal Processing: Hardware and Software Accuracy of the Software Triaxial Hot Wire Probe Calibration Validation Tests of Hot Wire Anemometry Test Results Accuracies 	13 14 15 16 18 19
III	DES	CRIPTION OF AIRFOIL EXPERIMENTS	21
	1.	Coordinate System	22
:	2.	Pressure Measurements on the Airfoil	23
	3.	Flow Angle Measurement and Calibration	24
	4.	Experimental Conditions	24
1	5	Experimental Procedure	25

IV	RESULTS AND DISCUSSION	27
	1. General	27
	2. Mean Flow Measurements	27
	3. Integral Parameters	28
	 Growth and Decay of the Velocity Defect and Wake Width 	30
	5. Self-Similar Velocity Profiles	32
	6. Turbulent Stress Measurement	32
	7. Self-Preservation of the Turbulence Profiles	33
	8. Eddy Viscosity Results	34
	9. The Structure Parameter	35
	10. Conclusions	36
REFERENCES		38
APPENDIX	TALBE OF EXPERIMENTAL DATA	91

Î

LIST OF TABLES

Table		Page
1 Boundary Layer and W	lake Traverse Stations	40
Al Symmetric Flat Plate IIHR Probe	Wake Data (x = 177.8) using	94
A2 Airfoil Boundary Lay (central plane)	rer Data at x/L =220	95
A3 Airfoil Boundary Lay (central plane)	ver Data at $x/L =124$	96
A4 Airfoil Boundary Lay (-6" plane)	ver Data at $x/L =124$	97
A5 Airfoil Boundary Lay (+6" plane)	er Data at $x/L =124$	98
A6 Airfoil Boundary Lay (far side)	ver Data at x/L =014	99
A7 Airfoil Boundary Lay (near side)	er Data at $x/L =014$	100
A8 Airfoil Wake Data at	x/L = .014 (central plane)	101
A9 Airfoil Wake Data at	x/L = .027 (central plane)	103
AlO Airfoil Wake Data at	x/L = .027 (-6" plane)	104
All Airfoil Wake Data at	x/L = .027 (+6"`plane)	105
Al2 Airfoil Wake Data at	x/L = .041 (central plane)	106
Al3 Airfoil Wake Data at	x/L = .055 (central plane)	107
Al4 Airfoil Wake Data at	x/L = .138 (central plane)	112
Al5 Airfoil Wake Data at	x/L = .225 (central plane)	117
Al6 Airfoil Wake Data at	x/L = .399 (central plane)	122
Al7 Airfoil Wake Data at	x/L = .661 (central plane)	123
Al8 Airfoil Wake Data at	x/L = .661 (+6" plane)	126
Al9 Airfoil Wake Data at	x/L = .661 (-6" plane)	127

A20	Airfoil Wake Data at x/L = .992 (central plane)	128
A21	Airfoil Wake Data at x/L = 1.928 (central plane)	129

•

-.

.

LIST OF FIGURES

Figure		Page
1.	Sensor coordinate system and sensor direction cosines	47
2.	Hot-wire probe	42
3.	Instrumentation block diagram	43
4.	Distribution of uv in the flat plate boundary layer at -76.3 mm	- 44
5.	Distribution of u' and v' in flat plate boundary layer at -76.3 mm	45
6.	Distribution of uv in the flat plate wake at 177.8 mm	46
7.	Distribution of u' in the flat plate wake at 177.8 mm	47
8.	Distribution of v' in the flat plate wake at 177.8 mm	48
9.	Distribution of w' in the flat plate wake at 177.8 mm	49
10.	Airfoil cross-section (dimensions ir mm)	50
11.	Airfoil in tunnel with measurement station locations	51
12.	Coefficient of pressure variation on both sides of wing	52
13.	Coefficient of pressure variation on both sides of wing on a spanwise basis	53
14.	Yaw probe description and calibration	54
15.	Static pressure variation across trailing edge and wake	55
16.	Boundary layer profiles at x/L =014 and220	56
17.	Boundary liver profiles at various spanwise locations	57

18.	Variation of mean longitudinal velocity in the wake	58
19.	Variation of mean longitudinal velocity at different spanwise locations	59
20.	Variation of crossflow angle in the wake	60
21.	Variation of θ_{11} in the boundary layer and wake	61
22.	Variation of θ_{21} in the boundary layer and wake	62
23.	Variation of _{دا} in the boundary layer and wake	63
24.	Variation of shape factor in the boundary layer and wake	64
25.	Defect velocity w _{xo} vs. x/0 _f	65
26.	Half-width b _x vs. x/0 _f	66
27.	Defect velocity w_{zo} vs. x/θ_{f} in log-log coordinates	67
28.	Half-width b _z vs. x/A _f	68
29.	Self-similar streamwise velocities	69
30.	Self-similar spanwise velocities	70
31.	Variation of u' across the wake	71
32.	Variation of v' across the wake	72
32,	Variation of w' across the wake	73
34.	Variation of uv across the wake	74
35.	Variation of \overline{vw} across the wake	75
36.	Variation of uw across the wake	76
37.	Variation of $\frac{\nabla w_{max}}{UV_{max}}$ with x/θ_{f}	77
38.	Decay rates of u', \overline{vv} and \overline{vw} with respect to x/θ_{f}	78
39.	u' in self-preserving coordinates	79
40.	uv in self-preserving coordinates	80
41.	vw in self-preserving coordinates	81

ix

42.	Eddy viscosity ε_x in self preserving coordinates	82
43.	Eddy viscosity ε_y in self preserving coordinates	83
44.	Recalculation of \overline{uv} using ε_x compared to \overline{uv} as determined experimentally: $x/L = .055$	84
45.	Recalculation of \overline{uv} using ε_x compared to \overline{uv} as determined experimentally: x/L = 1.928	85
46.	Recalculation of \overline{vw} using ε_{x} and ε_{z} compared to \overline{vw} as determined experimentally: $x7L = 0.55$	86
47.	Recalculation of \overline{vw} using ε_x and ε_z compared to \overline{vw} as determined experimentally: $x/L = 1.928$	87
48.	Structure parameter as calculated from Eqn. (34) (symbols as in figure 43)	88
49.	Comparison of structure parameter as calculated from Eqn. (33) and Eqn. (35)	89
50.	Recalculated value of \overline{vw} with a = .15 compared to \overline{vw} obtained experimentally at x/L = .138	90

LIST OF SYMBOLS

.

a _i ,b _i ,c _i	Sensor direction cosines i = 1,2,3
A _{2d}	Bradshaw structure parameter as calculated in two- dimensional case
A _{3d}	Bradshaw structure parameter as calculated in three- dimensional case
A',B'	Constants in King's Law
b _x	Half width of longitudinal velocity in the wake
b _z	Half width of spanwise velocity in the wake
C,L	Airfoil chord length = 922 mm
C _p	Pressure coefficient
A _i ,B _i ,C _i	Variables used in hot wire data analysis, i = 1,2,3
a_4, b_4, c_4 d_4, e_4, f_4	Constants used in hot wire data analysis
E	Hot wire mean voltage output
н	Shape factor (₈₁ /0 _f)
k	Sensitivity correction factor = .1
n	Exponent in King's Law
$\overline{q}_1, \overline{q}_2, \overline{q}_3$	Effective mean velocities of sensors 1, 2, and 3, respectively
۹ ₁ ,۹ ₂ ,۹ ₃	Fluctuating effective velocities of sensors 1, 2, and 3
Q ₁ ,Q ₂ ,Q ₃	Instantaneous effective velocities of sensors 1, 2, and 3
Ū,V,W	Mean velocities in the x,y, and z directions
U,V,W	Instantaneous velocities in x,y, and z directions
u',v',w'	Root mean squares of u,v, and w
U.,U _∞ '	Constant freestream velocity

W _{c1}	W at the centerline
wx	Defect velocity in the longitudinal or chordwise direction
Wz	Defect velocity in the spanwise or crossflow direction
w _{xo}	w_{χ} at the centerline of the wake
₩ zo	w _z at the centerline of the wake
е	Fluctuating hot-wire voltage output
u _t	Friction velocity
5	Boundary layer thickness
x,y,Z	Streamwise (longitudinal or chordwise), normal and spanwise (crossflow) coordinates
ε _x	Eddy viscosity, as calculated from the gradient of U
٤z	Eddy viscosity, as calculated from the gradient of W
θ	Sensor orientation in the x-z plane
ų,	Sensor orientation in the y-z plane
^θ f	Final station momentum thickness (2-D definition)
θt	Trailing edge momentum thickness (2-D definition)
ⁿ x	y/b _x
'nz	y/b _x
٥	$\int_{-\infty}^{\infty} (1 - \frac{U}{U_{\infty}}) dy$
^ô 2	$\int_{-\infty}^{\infty} (1 - \frac{W}{U_{\infty}}) dy$
۱۱ ^θ	$\int_{-\infty}^{\infty} \frac{U}{U_{\infty}} \left(1 - \frac{U}{U_{\infty}}\right) dy$
^θ 22	$\int \frac{W}{U_{\infty}} \left(1 - \frac{W}{U_{\infty}}\right) dy$

$$\theta_{12} \qquad \int \frac{U}{U_{\infty}} (1 - \frac{W}{U_{\infty}}) dy$$

$$\theta_{21} \qquad \int \frac{W}{U_{\infty}} (1 - \frac{W}{U_{\infty}}) dy$$

Y Angle between the velocity vector and the x-direction in the case of the swept air foil

Sweep angle of the airfoil

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CHAPTER I

INTRODUCTION

1. The Problem Introduced

There is a growing interest, in recent years, in the development of calculation methods of three dimensional turbulent shear flows such as boundary layers and wakes. This is largely because of their application in aerodynamics and ship hydrodynamics. Calculation of the drag on the swept wing of an aircraft is a typical example. This problem presents many complexities (especially in the trailing edge and near-wake regions) such as viscid-inviscid interaction, three dimensionality and the modeling of turbulence. Computational techniques capable of handling these complexities are currently under development at various research centers. In order to verify the accuracy of such methods and also to aid the development of new methods, it is essential to have a comprehensive data base on three-dimensional flows in general and three dimensional wake flows with particular reference to the problem cited above. Such data should include information on velocities, pressure and the details of the turbulence properties. Measurement of turbulence properties in three dimensional flows is still a challenging task since the required measurement techniques are only in their early stages of development. Consequently, there is not much data available on the turbulence properties in three dimensional flows. The present research has been aimed at obtaining a set of detailed measurements, in a

relatively simple three-dimensional wake, namely the developing wake behind an infinite swept airfoil. Also as a part of this research program, significant effort has been directed towards the development and validation of a suitable technique for turbulence measurements in three-dimensional flows.

Previous work done in the wake of streamlined bodies have been largely restricted to two-dimensional flows. These include the work of Chevray and Kovasznay (1969), Pot (1979), Andreopoulos and Bradshaw (1980) as well as that of Sastry (1981) in the symmetric and asymmetric wakes of flat plates and airfoils. In these studies, the relevant components of the Reynolds stress tensor have been measured. Computational models have also been developed and used to describe these experimental findings. Of the above, Sastry's studies included the twodimensional wake of a Korn-Garabedian airfoil at incidence. The development of various wake parameters were studied and compared with those in the case of the flat plate wake. It should be noted that most of the data reported by the previous investigators have been restricted to the near or intermediate wake regions.

It is only very recently that experimental studies of wakes 'exhibiting three-dimensionality have been performed. One study, that of Cousteix and Pailhaus (1980) explored the wake behind a swept 'ONERA D' airfoil at incidence. This study contains hot-wire measurement of all the components of the Reynolds stress tensor in addition to data on mean velocities and flow inclination. Similar hot-wire data in the threedimensional wakes of turbomachinery blade have been obtained at Penn State University. These data, however, were obtained under very

difficult experimental conditions, with many uncertainties introduced by such factors as small physical size, probe orientation, probe dimensions, data reduction, etc. The data of Cousteix and Pailhaus (1980) were obtained under more favorable conditions. Yet, even in these experiments, (the airfoil studied had a chord of 200 mm and a span of 300 mm) tunnel wall interference on the wake development could have been significant.

In the present study some of the limitations of the above experiments have been removed. Present experiments were performed in the wake behind an "infinite" NACA 0012 airfoil swept at 30 degrees, and at zero incidence. Such a flow, being significantly three dimensional, yet relatively simple, is expected to provide useful information on growth rates, viscosity models and other properties of three-dimensional wakes. Also, these flows can be studied with regard to the manner in which they approach two-dimensionality at a large distance from the trailing edge.

A complete set of measurements are obtained both in the boundarylayer in the trailing edge region and in the developing wake behind the airfoil. These measurements include pressure distribution, mean velocity components, in the boundary layer and wake. Additionally, the six components of the Reynolds shear stress were also measured in the wake. The measurements extend up to two chord lengths downstream from the trailing edge. The turbulence measurements have been made using triplesensor hot-wire anemometry. A significant contribution of this study is the development and validation of a suitable technique for the measurement of turbulence properties using the triple-sensor probe and

a comparative study of alternative techniques. In fact, development of the present technique forms a part of a larger program of study on general three-dimensional boundary layer flows, currently in progress at the Institute of Hydraulic Research.

Chapter II will be devoted to the development of the triple-sensor anemometry. A complete description of the method is presented. Particulars concerning the airfoil experiments such as calibration procedures for hot-wire instrumentation, details of the airfoil fabrication, instrumentation, and mounting are discussed in Chapter III. The results and discussion are presented and discussed in Chapter IV. The effects of three-dimensionality are compared with previous two dimensional experiments and theory. Further, Chapter IV also contains the concluding remarks as well as suggestions toward further work.

CHAPTER II

DEVELOPMENT OF THREE-DIMENSIONAL HOT-WIRE INSTRUMENTATION

1. Problem Description and Quantities Requiring Measurement

In studies of three-dimensional turbulent flows, it is necessary to measure the instantaneous values of three mutually orthogonal velocities at a given point in space. The instantaneous values will contain three mean velocities as well as three time-dependent or fluctuating velocities. It is these three instantaneous fluctuating velocity components, in addition to the mean components that require retrieval in this study. This retrieval must be general enough, such that it allows one to study flow fields of arbitrary geometry.

2. Available Techniques and Relative Assessment

Hot-wire anemometry has been the most commonly used instrumentation for velocity measurements especially in three-dimensional flows. Laser velocimetry, which is currently gaining popularity, is complex and not well tested in three-dimensional flows. Two techniques, using hot-wire anemometry have been tried in three-dimensional flows. One of these uses a triple-sensor probe in which there are three independent sensing elements oriented in certain specific relative directions, and the other uses a single sensor or x-wire probe oriented sequentially at different angles to the flow. The first method, used by Gorton and Lakshminarayana (1976) and others, requires that the predominant direction of flow is known and that the probe axis coincides with it. The three instantaneous outputs u,v,w, from the sensors are then processed by an analog computer which solves for the mean values $\overline{U}, \overline{V}$, and \overline{W} as well as for the six Reynolds stresses u^2 , v'^2 , w'^2 , \overline{uv} , \overline{vw} and \overline{uw} via the solution of a set of linearized simultaneous equations. One of the drawbacks of this method is that, often, there may not be a predominant direction in the flow. Also, nonlinear effects may affect the accuracy of this method.

The second method, used by Elsenaar and Boelsma (1974), consists of a single inclined wire probe rotating about it's roll axis. The probe outputs at successive orientations of the probe are used to obtain solutions for the mean velocities and turbulent stresses. Here again, the major difficulties are the need for actual physical rotation of the probe itself and the interference of the probe support system with the flow. Elsenaar and Boelsma have noted this and the associated uncertainties.

Apart from the shortcomings mentioned above, information is lost in these methods during the analog processing for time-averaged results. Thus instantaneous velocities, their triple correlations, and higher order moments cannot be determined.

The method selected for the present study use a triple sensor probe oriented in an arbitrary direction to the flow. The instantaneous outputs from the three sensors are used to obtain not only the three mean velocity components and the six Reynolds stresses but also the instantaneous fluctuating velocity components. This is done through

digital data acquisition software. Two alternate schemes were developed for comparison purposes. Each of these is described below in detail.

2.1 Method A

Figure 1 shows the probe and flow coordinate system. Consider hot wire sensor 1 with respect to the X,Y,Z (flow) coordinate system. This sensor has an orthogonal coordinate system $(\zeta_1, \zeta_2, \zeta_3)$ associated with its orientation. We, then, have

$$(Q_1) = a_1 U + b_1 V + c_1 W$$
 (1)

$$(Q_2) = a_2 U + b_2 V + c_2 W$$
 (2)

$$(Q_3) = a_3 U + b_3 V + c_3 W$$
 (3)

where Q_1 , Q_2 and Q_3 are the instantaneous velocities in the $\zeta_1, \zeta_2, \zeta_3$ coordinate system, and U,V, and W are the instantaneous velocities in the X,Y, and Z coordinate system. The coefficients a_1 , b_1 , c_1 ,..., are the appropriate direction cosines of the X,Y, and Z axis with respect to the $(\zeta_1, \zeta_2, \zeta_3)$ coordinate system as shown in figure 1.

The effective velocity sensed by hot wire sensor 1 is given by [see for example Friehe and Schwarz (1968)]

$$Q_1 = [(Q_2)^2 + (Q_3)^2 + k_1^2 (Q_1)^2]^{1/2}$$
 (4)

with k_1 being the cross-sensitivity factor associated with deviation from the cosine law. Q_1 is obtained from the voltage output E_1 of the sensor 1, via its calibration curve. Now, if we substitute Eq. (1,2,3) into Eq. (4), the resulting expression becomes

$$Q_{1} = \left[a_{4}U^{2} + b_{4}V^{2} + c_{4}W^{2} + d_{4}UV + e_{4}UW + f_{4}VW\right]^{1/2}$$
(5)

The coefficients in the above equations are:

$$a_4 = a_2^2 + a_3^2 + k_1^2 a_1^2$$
 (6)

$$b_4 = b_2^2 + b_3^2 + k_1^2 b_1^2$$
(7)

$$c_4 = c_2^2 + b_3^2 + k_1^2 c_1^2$$
(8)

$$d_4 = 2(a_2b_2 + a_3b_3 + k_1^2 a_1b_1)$$
(9)

$$e_4 = 2(a_2c_2 + a_2c_3 + k_1^2a_1c_1)$$
(10)

$$f_4 = 2(b_2c_2 + b_3c_3 + k_1^2b_1c_1)$$
(11)

Similar expressions can be derived for sensors 2 and 3. One, then gets a set of three nonlinear algebraic equations for the three unknowns U,V, and W. These require solution by an iterative scheme. The method used is a Newton-Raphson scheme, which requires an initial guess to start the algorithm. In practice, the instantaneous outputs E_1, E_2 and E_3 of the three sensors are sampled, digitized and stored. These data are later recalled, calibrated and the velocity components U,V,W are computed on an instant to instant basis using the above procedure. After the entire set of instantaneous velocity components are evaluated, they are time averaged to obtain \overline{U} , \overline{V} , and \overline{W} . The turbulent fluctuations, u, v, and w are then recovered and stored for subsequent processing. Since this method involves the solution of nonlinear equations, for each set of instantaneously sampled data, it is computationally very time-consuming and expensive. However, it does not involve any linearization and can therefore be used even for very large fluctuations.

2.2 Method B

In this method the effective velocities and resultant velocities are both decomposed into their mean and fluctuating components. Eqs. (1-3), then, become:

$$(\overline{Q} + q)_{1} = a_{1}(\overline{U}+u) + b_{1}(\overline{V}+v) + c_{1}(\overline{W}+w)$$
(12)

$$(\overline{Q} + q)_2 = a_2(\overline{U} + u) + b_2(\overline{V} + v) + c_2(\overline{W} + w)$$
(13)

$$(\overline{Q} + q)_3 + a_3(\overline{U} + u) + b_3(\overline{V} + v) + c_3(\overline{W} + w)$$
(14)

Now, if they are substituted into Eq. (4), we get

$$[(a_{4}\overline{U}^{2} + b_{4}\overline{V}^{2} + c_{4}\overline{W}^{2} + d_{4}\overline{U}\overline{V} + e_{4}\overline{U}\overline{W} + f_{4}\overline{V}\overline{W}) + (2a_{4}\overline{U}u + 2b_{4}\overline{V}v + 2c_{4}\overline{W}w + d_{4}(\overline{U}v + \overline{V}u) \div e_{4}(\overline{U}w + \overline{W}u) + f_{4}(\overline{V}w + \overline{W}v) + (a_{4}u^{2} + b_{4}v^{2} + c_{4}w^{2} + d_{4}uv + c_{4}uw + d_{4}uv + c_{4}uw + f_{4}vw)]^{1/2}$$
$$= (\overline{Q} + q)_{1}$$
(15)

which can be written (collecting terms from Eq. 15 such that A_1 contains \overline{VW} terms, B_1 contains terms as \overline{Vu} , and C_1 contains uv terms):

$$\overline{Q}_{1} + q_{1} = \{R_{1} + B_{1} + C_{1}\}^{1/2}$$
 (16)

If we assume that $B_1 + C_1 \leq A_1$, we can linearize Eq. (16) as

$$\overline{Q}_{1} + q_{1} = A_{1}^{1/2} \left[1 + \frac{B_{1} + C_{1}}{2A_{1}} - \frac{1}{8} \frac{(B_{1} + C_{1})^{2}}{A_{1}} + \dots \right]$$
(17)

Squaring Eq. (16), time-averaging and neglecting terms of higher order, the resulting expressions for hot-wire sensor 1 in terms of the mean and fluctuating velocity components are

$$\overline{Q}_{1}^{2} = a_{4}\overline{U}^{2} + b_{4}\overline{V}^{2} + c_{4}\overline{W}^{2} + d_{4}\overline{U}\overline{V} + e_{4}\overline{U}\overline{W} + f_{4}\overline{V}\overline{W}$$
(18)
$$q_{1} = \frac{1}{2A_{1}^{1/2}} \left[u(2a_{4}\overline{U} + d_{4}\overline{V} + e_{4}\overline{W}) + v(2b_{4}\overline{V} + d_{4}\overline{U} + f_{4}\overline{W}) + u(2c_{4}\overline{W} + e_{4}\overline{U} + f_{4}\overline{V}) \right].$$
(19)

$$= \frac{1}{2A_1^{1/2}} (uP_1 + vS_1 + wR_1)$$
(20)

where P_1 , R_1 and S_1 denote the terms in parentheses in Eq. (19). Simultaneous solution of the three nonlinear algebraic equation like Eq. (18) will directly yield the mean velocity components $\overline{U}, \overline{V}$, and \overline{W} . Now, looking at (20) we find that it contains, as constants, the predetermined mean velocities and those of geometry. The variables remaining are the instantaneous fluctuations about the mean. Eq. (20) and the corresponding equations for the other two sensors will again yield three linear equations for the instantaneous turbulence velocities. Thus, the instantaneous details can be recovered in this method also, as was done in Method A. Since the equations for u,v,w are linear in nature, this procedure requires much less computer time (less by an order of 10) than method A, and also ensures absolute convergence. However, it should be reminded that this method involves the process of linearization and is therefore acceptable only for flow situations where the linearization assumption is valid.

2.3 Method C

If we consider Eq. (20) again, square it and time-average, we get

$$\overline{q}_{1}^{2} = \frac{1}{4A_{1}} \left[\overline{u}^{2} P_{1}^{2} + \overline{v}^{2} S_{1}^{2} + \overline{w}^{2} R_{1}^{2} + 2 \overline{u} \overline{v} P_{1} S_{1} + 2 \overline{u} \overline{w} P_{1} R_{1} + 2 \overline{v} \overline{v} S_{1} R_{1} \right]$$

$$(21)$$

Also for the effective shear stresses, the resulting expression is

$$\overline{q_{1}q_{2}} = \frac{1}{4A_{1}^{1/2}A_{2}^{1/2}} [\overline{u}^{2}P_{1}P_{2} + \overline{v}^{2}S_{1}S_{2} + \overline{w}^{2}R_{1}R_{2} + \overline{u}\overline{v}(P_{1}S_{2} + P_{2}S_{1}) + \overline{u}\overline{v}(P_{1}S_{2} + P_{2}S_{1}) + \overline{v}\overline{v}(S_{1}R_{2} + S_{2}R_{1})]$$
(22)

Similarly, one can obtain two such equations for each of the other two sensors. There would be a set of six linear algebraic equations with known coefficients, which can be solved once for all, for the six Reynold's stress components $\overline{u^2}$, $\overline{v^2}$, $\overline{w^2}$, \overline{uv} , \overline{vw} , and \overline{uw} in terms of the corresponding effective components as sensed by the three sensors. This method does not allow the instantaneous u,v, and w values to be recovered. It is, however, very economical computationally. This procedure is very similar to that used by Gorton and Lakshminarayana (1976), and has been used in the present studies chiefly to provide a comparison with methods A and B. In fact, the linearization assumption implied in this is less restrictive than in the method of Gorton and Lakshminayama.

2.4 Description of the Probe

Two probes were used for the test of the methodology and software. One of these (Probe 1) was developed in house and the other (Probe 2) was a commercial probe, Disa triaxial hot-wire probe. Probe 1 has dimensions and sensor orientation, as shown in Fig. 2a. It can be seen that the ratio of probe diameter to sensor support length is such that significant probe interference may be present. This probe was a first attempt at constructing a 3-wire probe at the Institute. The Disa probe, Fig. 2b, has a much longer sensor support as well as a small head diameter. Sensing elements in the Disa probe sense over the central 1.25 mm, whereas the in-house probe senses over its entire length (approximately 2.1 mm). This is due to the fact that the Disa sensor is a gold plated tungsten wire of 5 micron diameter, with the central portion etched to give a 1.25 mm sensing length. The in-house sensor is a bare platinum-rhodium wire of the same diameter. It is obvious that the spatial resolution of the Disa probe is much better. However, for flow measurement where spatial resolution was not crucial, the inhouse probe proved to be quite adequate.

2.5 Signal Processing: Hardware and Software

Each hot-wire sensor of the triaxial probe was operated by a Disa model 55M10 constant temperature anemometer. These instantaneous output voltages from the three anemometers were filtered using a high pass filter of 36 db/octave roll_off, set at 0.1 Hz. The voltage signals were then amplified by 3 Preston SW 8300 amplifiers and sampled at a rate of 50 samples per second for 50 seconds by a Preston GMAD-3 analog to digital converter (with a 3-channel'sample and hold front end). The data were stored on disk file on an HP-1000 minicomputer. At the end of the experiment the data were recalled from the disk file and Processed to obtain the velocities. A block diagram of the instrumentation is shown in Fig. 3.

The computer program used for data acquisition records 'he time and date when the samples were taken. This information is used to apply corrections for small drifts in probe calibration caused by temperature changes in the tunnel and probe contamination. This is done by calibrating the probe at the beginning and end of the experiment and applying a simple linear correction to the calibration coefficients with respect to time. The corrected calibration constants are then used to convert the voltages to effective velocities in each case. Time-associated changes in the calibration for the hot-wire anemometry are therefore eliminated.

Double precision arithmetic was used in calculating accumulated sums while computing average values where the numerics were suspected to exceed the single precision register size. This way, round-off and truncation errors were held to a minimum. Any errors still remaining have to be associated with the uncertainties in the overall process (i.e., probe orientation, tunnel speed, ... etc).

2.6 Accuracy of the Software

The stability of the Newton-Raphson algorithm used in Method A depends on the "closeness" of the initial velocity guesses as well as the convergence criteria specified. Tests on the program itself were performed to provide values of accuracy and reliability. In these tests, dummy values for the effective velocities, computed (independently) for a set of known velocities, were input to the program. The resultant velocities output by the program were compared with the correct values. It was found, that, in each case, the algorithm converged to the correct value in approximately 5 iterations with a convergence criterion of one

part in one thousand. The initial guess needed to be only of the same order of magnitude as the final converged correct value. In order to make the scheme converge quicker, the equations were analyzed and certain characteristics were noted. The predominant term in the three equations (Eqs. 5), were those that involved the U^2 terms and if the effective velocities were averaged and divided by the sum of the coefficients the resultant velocity was found to be within 2% of the final value. For the other two velocities the relative magnitudes of the effective velocities were noted and the appropriate sign for one of the two could be recovered. The remaining velocity was guessed as the mean of all the velocities in that direction by averaging first the effective velocities and then using that solution as the starting point for the discrete solution in question. Furthermore, a relaxation factor was applied to U such that instabilities were damped. These techniques helped in arriving at the final result for the particular sample set. However, if convergence was not achieved, the set would be discarded and calculation would proceed to the next sample set. This dropout rate would be recorded and later examined to decide whether or not the results should be accepted. Typical dropout rates were .05 per cent.

2.7 Triaxial Hot Wire Probe Calibration

Each sensor of the probe was calibrated at the beginning and end of an experiment. The probe was traversed to the freestream in the wind tunnel with the probe axis aligned with the flow direction. This condition represents a limiting case for the three simultaneous equations, namely the equivalent velocities sensed by each sensor must be equal.

This is true, of course, if the sensors are all symmetrically oriented with respect to the probe axis. A computer program was developed exclusively for probe calibration.

For the hot-wire anemometer, the output voltage across the sensor varies as a function of velocity, this variation being given by the well-known King's law. This law most commonly takes the form

$$E^2 = A + BV^n \tag{23}$$

where n is generally between .45 and .55.

The computer program developed would sample the sensor output at 50 samples per second for 50 seconds. These values were time averaged to obtain E. The calibration was carried out at several wind tunnel velocities. The computer program would fit Eq. (23) to these data by a least square procedure. This method of calibration required a minimum amount of time due to the fact that the three sensors were calibrated simultaneously.

2.8 Validation Tests of Hot Wire Anemometry

Two of the well known two-dimensional flow fields, namely, a flat plate boundary layer and a wake were used to validate the performance of the triple-sensor probe and the related software and hardware. The results obtained by the methods A, B, and C, in each case were compared with those obtained earlier in the <u>same</u> flow with a conventional x-wire probe by Sastry (1981). In the case of the flat plate boundary layer

measurements, the triaxial probe results were also compared with the data of Klebannof (1955). In this situation, however, only the in-house probe was tested.

The flat plate used by Sastry (1981) was mounted as in the earlier experiments. Velocity traverses were made in the boundary layer (at -76.3 mm from the leading edge), and in the wake (at 177.8 mm from the trailing edge). Various tests were then performed on the probe and the software to determine uncertainties, accuracies, as well as the sensitivity to errors in orientation of the probes with respect to the flow field. Effect of sample sizes and rates on drop out rates (in Method A) and accuracy was also studied.

Sensor orientation angles were measured to be within $\pm 1^{\circ}$ in the θ plane and $\pm 3^{\circ}$ in the ψ plane (see Fig. 1). Effects of uncertainties in probe orientation were estimated by sirulating these uncertainties in probe yaw, pitch and roll in the processing algorithm. Values determined from the adjusted geometric inputs deviated from the best known inputs substantially enough (approximately 5 to 10%) to verify the uncertainty ranges and their centers. Sample size and rates were varied also to find an efficient rate and size. The values used by Sastry (1981) were rechecked to see if such rates and si es were adequate for the three dimensional probe, and were, in fact, found to be so. The convergence criterion specified for the Newton-Raphson scheme was 0.1% of the freestream velocity, and further constraining (reducing the value) resulted in negligible changes (less than 2%) in the shear stresses (the most sensitive of the results).

2.9 Test Results

It is seen from Fig. 4 that at $y/\delta = .2$ in the boundary layer, the predominant turbulent shear stress \overline{uv} (obtained by Method A) is 25% below the data of Klebanoff (1955), whereas the results obtained by Method C, developed by the authors and very similar to that of Gorton and Lakshimaryana (1976) appear to agree very well with the data of Klebanoff. Intensities u' and v' determined by Method A or C show smaller departures from the data of Klebanoff than in the case of the Shear stress \overline{uv} (see Fig. 5). However, the most disturbing observation was that the nonprincipal shear stresses \overline{uw} and \overline{vw} (which should be zero) were found to be as large as the principal component \overline{uv} at some y locations. Results in the wake (shown in Table Al) for the in-house probe were found to be even worse in this regard, even though values for the principal stress \overline{uv} , were found to be of proper magnitude and to deviate by less than 20% from those of Sastry (1981).

The Disa triaxial probe 55P91 was traversed only in the wake because of probe support and mounting problems encountered in the boundary layer traverse. Principal shear stress component \overline{uv} , shown in Fig. 6 is in good agreement with the previous measurements. However, it was found that even though the nonprincipal stresses had decreased substantially in comparison with the inhouse probe, they are still as high as 30% of \overline{uv}_{max} in the worst case. Also shown for this case is a comparison of the three methods of data reduction presented earlier. It is seen that methods A and B agree well with each other and also with the data of Sastry (1981), especially in the evaluation of \overline{uv} . On the other hand, the time-averaged method C, while still giving good results for u', v', and w', estimates the shear stresses very poorly (see Figs. 6, 7, 8, 9). Since method B takes about 1/10 the computer time of method A and shows comparable accuracy, it is concluded that this is the most useful procedure for data reduction.

Looking at the spatial resolution of the two probes, Disa 55P91 and the in-house probe, and the corresponding values of the \overline{vw} and \overline{uw} obtained using them provides some insight into the requirements for threedimensional flow measurement. The in-house probe with a spatial resolution of approximately 5 mm has failed to determine turbulent quantities in the moderately high shear regions. On the other hand, the DISA 55P91 probe with a resolution of 3.2 mm has given better results. It is therefore recommended that a probe of even smaller size (such as the custom made Disa subminiature triaxial probe with a resolution of 1.2 mm) be used in future measurements. It is felt that such a probe is needed to measure \overline{uw} and \overline{vw} to a better level of accuracy.

2.10 Accuracies

An uncertainty of \pm .007 meters per second, due to micromanometer error, is inherent in the calibration procedure. Other uncertainties are associated with the software as well as with probe size and orientation. The convergence criteria for velocities in the software is less than .0010. This is the maximum uncertainty associated with software, hence, remaining inaccuracies are best described as being well within the uncertainty associated with geometry. However, in high shear regions, the errors extend beyond this and are due to size and displacement effects. Those errors due to misalignment and sensor angle error are approximately .5%

in the mean velocity components and 5% and 15% for the intensitites and shear stresses respectively. However, because of the finite size, the accuracies are reduced even further. While the probe size effect is not significant on the intensities u', v', w', the estimated values of \overline{vw} and \overline{uw} may be in error by as much as $\pm 35\%$ of \overline{uv}_{max} .

CHAPTER III

DESCRIPTION OF AIRFOIL EXPERIMENTS

In selecting a suitable airfoil for the study, several design requirements had to be satisfied before construction could begin. The test section of the wind tunnel used is octogonal throughout, with a distance of 1.67 m between the flats. This dimension provided the constraint for the span of the airfoil. The requirement of 'infinite' span conditions restricted the maximum chord. By combining these two constraints with the range of velocities possible in the wind tunnel used, the sweep angle, span and chord could be specified.

The profile selected is the NACA 0012 symmetric airfoil - a well studied profile. For the purpose of fabrication the coordinates describing the profile geometry were taker, from Abott and Van Doenhoff (1959).

A sweep angle of 30° was chosen, so that a sizeable crossflow component would be present at the trailing edge. The construction of the airfoil is shown in Fig. 10. Blocks of aluminum, milled to size, were secured to a central frame 12.5 mm thick aluminum plate, to form spanwise ribs. A wooden nose cone was attached to the central frame with pressure taps on both sides. Two aluminum sheets (0.75 mm) used as skins, were wrapped around the aluminum blocks on each side of the frame and were feathered to give a nominal trailing edge thickness of 1 mm. Pressure taps of 1.2 mm diameter (totaling 92) were provided on both sides

of the airfoil along midspan, and along two cff-mid span planes 15 cm away on either side of the midspan plane.

The airfoil was mounted in the wind tunnel with its spanwise direction located 30° from vertical. A false floor and boundary layer fence were used to remove end-wall boundary effects. This provided conditions close to the desired infinite airfoil configuration (see Fig. 11). Tubing and other mounting fixtures were concealed so as not to affect the flow under measurement. Flow visualization studies made, using wool tufts did not indicate any areas of separation or tunrel-wall effects. These tests also showed that the fence had no appreciable effect on the flow and hence was not used during the main experiments.

1. Coordinate System

The coordinate system used is a right handed orthogonal system, the freestream velocity direction corresponding to the x-direction. The ydirection is normal to the airfoil surface and towards the near wall of the tunnel. The z-direction is perpendicular to the tunnel ceiling. This system is shown in Fig. 10 and it should be noted that the sensor's direction cosines are referenced to this system.

Traversing the boundary layer and wake in the y-direction was accomplished by a servo-controlled stepping motor with a range of 20 cm and an accuracy of .025 mm. The traverse is moveble in the x-direction for the longitudinal repositioning. A list of traverse stations and their locations are shown in Table 1.

2. Pressure Measurements on the Airfoil

Measurements of static pressure were used to insure that the airfoil was mounted at zero incidence, and more importantly to provide the actual pressure distribution on the airfoil. A total of 92 pressure taps were used for this purpose. In the midplane of measurement, 22 taps were located on each side of the airfoil with additional 11 taps \pm 15 cm from the midplane. These were also located on both sides of the airfoil.

To perform the measurements a 48-port-selecting scani-valve was used in conjunction with an alcohol micromanometer. The micromanometer had an accuracy of .025 mm and was used for monitoring tunnel speed as well as measuring the static pressure.

Static pressure taps on the two sides of the airfoil and directly opposite to each other were used for initial alignment of the airfoil. For a further and more accurate check on alignment complete scans of all the pressure taps were made at a tunnel speed of 21.84 meters per second. The coefficients of pressure, C_p , defined as

$$C_{p} = \frac{P - P_{\infty}}{\frac{1}{2} \rho U_{\infty}^{2}}$$
(24)

are shown in Figs. 12 and 13. It is seen that the static pressure distributions at the three spanwise locations coincide reasonably well. This is an indication that the airfoil can be considered to be nearly 'infinite' in span. However, it should be noted that this test will be

pressure, which, according to Bussman and Ulrich (see Schlichting (1974)) is the region where natural transition occurs on an NACA 0012 airfoil. Past experience at the Institute has shown that sand paper strips perform better than trip wires often used for this purpose. With this tripping, the boundary layer on the airfoil was found to be fully turbulent and the Reynolds number based on the momentum thickness at 2.5 cm upstream of the trailing edge was 7280.

5. Experimental Procedure

The wind tunnel was started and allowed to warm up before starting the experiment. Typically, the temperature rise over the duration of an experiment was of the order of 1°C. First, yaw probe traverses were made in the boundary layer and wake. These included profiles on either side of the airfoil to check for symmetry and profiles at spanwise locations 15 cm above and below the midspan plane to check for infinite conditions. These locations are indicated in Table 1, referred to earlier. The yaw probe traverses were followed by traverses of the Disa 55P9; triaxial hot-wire probe in the wake. Location of the wake centerline was inferred from the minimum in the velocity distribution across the wake.

Uncertainty in the velocity measurements is estimated to be 2%. Static pressure is considered to be accurate within 15 - 20% and the flow angle within 0.5°. Hot wire uncertainties are primarily due to errors in probe alignment and resolution. Preset yaw is expected to be less than +0.5° and a preset error in pitch is likely to be less than +2°. Inaccuracies in probe manufacturing were of the order of 2° as determined by direct measurement through a steroscope with a graduated reticle. Roll inaccuracies were eliminated through the Disa type mounting that fixed the roll axis to the traversing mechanism. The overall uncertainties in the turbulence measurement were u', v', w': 5%, \overline{uv} : 15%, \overline{vw} : 30%. The uncertainties in the \overline{uw} were too large to be acceptable. Hence, these data are not discussed in this report. Further miniaturization of the probe is necessary in order to improve these results. Also not used in the discussion are the data on the various triple correlations such as $\overline{u^3}$, $\overline{u^2v}$, etc., since their accuracy has not been established so far. All the data are, however, reported in the Appendix, for the purpose of documentation. followed by boundary layer traverses in "the midplane" and "off-planes" for this aspect to be further verified.

3. Flow Angle Measurement and Calibration

Magnitude and cirection of the velocity vector were determined by a directionally sensitive three-hole yaw probe. This probe of similar type and size to that used by Ramaprian, Patel, and Choi (1978) and was calibrated in a similar manner. However, several changes were made to make the calibration more accurate. The probe was also calibrated to yield the local static pressure, in addition to the magnitude and direction of the velocity. Details of this calibration, including probe dimensions are shown in Fig. 14. The yaw probe outputs were read via a set of three STATHAM pressure transducers, amplified, scanned, digitized and recorded by the HP/1000 computer. The results were averaged over 20 seconds to obtain the mean pressure for each tube. The transducer calibration was repeated several times each day to see if the instrumentation and methodology used ensured repeatability.

4. Experimental Conditions

The experiments were performed at a tunnel velocity of about 22 meters per second corresponding to a trailing edge Reynolds number of approximately 1.36×10^6 . To fix transition to turbulence, a boundary layer 'trip' consisting of a strip of 20-grid sand aper, 15 cm wide and extending over the entire span, was glued to the surface on both sides of the airfoil at a distance of 20 cm from the leading edge. The location of the sand paper corresponds roughly to the region of lowest

CHAPTER IV

RESULTS AND DISCUSSION

1. General

The results of the experiments are presented and discussed in this chapter. A complete set of tabulated experimental data is provided in Appendix A.

2. Mean Flow Measurements

The variation of static pressure across the training edge boundary layer and wake is shown in Fig. 15. It is interesting to see that the static pressure varies across the wake and reaches a maximum value at the wake centerline. This trend persists mildly even at the last measuring station in the wake. This observation confirms similar observations made by Sastry (1981) in the developing two-dimensional wake of an airfoil. The static pressure variation across the wake can be viewed as the result of the interaction among the boundary layer, wake and the external inviscid flow. These data should, therefore, provide a good test case for interactive calculation methods.

Figure 16 shows the distributions of the longitudinal velocity component U across the boundary layer in the trailing edge region. Specifically, the velocity profiles at x/L = -0.220 and x/L = -0.014 are shown. It is seen that these profiles, especially the latter, resemble a typical distribution in a moderate adverse pressure gradient. The profile does not show any evidence of flow separation. The variation of the crossflow angle γ in the boundary layer at the same locations are also shown in Fig. 16. It is seen that the crossflow increases towards the trailing edge. Also, at the trailing edge, the crossflow is strong ($\gamma = 15^{\circ}$) enough to introduce significant three-dimensional effects into the wake flow. Furthermore, at x/L = - .124, spanwise variations in the boundary layer are seen to be small (see Fig. 17).

Figures 18 and 19 show the distributions across the wake of the chordwise velocity component. A close study of these profiles shows that there is slight asymmetry in the flow. The reason for this is not known. Also, the profile at the last station has been shown only for half of the wake since the traverse could not be extended to cover the other half of the wake at this station. The crossflow angle, (γ) profiles across the wake shown in Fig. 20 exhibit similar properties as the chordwise velocity profiles, namely decay of the crossflow angle and the increase in spread with distance downstream. It is also seen that at the last measuring station, the crossflow is verv small, indicating that the mean flow is virtually two-dimensional beyond this point.

3. Integral Parameters

We now define the following integral parameters for the wake:

displacement thickness
$$\delta_1 = \int_{-\infty}^{\infty} (1 - \frac{U}{U_{\infty}}) dy$$
 (25)

momentum thickness $\theta_{11} = \int_{-\infty}^{\infty} \frac{U}{U_{\infty}} (1 - \frac{U}{U_{\infty}}) dy$ (26)

momentum thickness
$$\theta_{21} = \int_{-\infty}^{\infty} \frac{W}{U_{\infty}} (1 - \frac{U}{U_{\infty}}) dy$$
 (27)

shape factor
$$H = \frac{\delta_1}{\theta_{11}}$$
 (28)

The distributions of these parameters with dcwnstream distance are shown in Figs 19-22. First, Fig. 21 shows the variation of θ_{11} . In this figure the reference length scale used is the momentum thickness θ_{f} at the far wake, defined as

$$\theta_{f} = \theta_{11}$$
 at the last measurement location

From Fig. 21 certain aspects concerning the flow may be noted. Clearly, the momentum thickness increases in the boundary layer due to the adverse pressure gradient. There is a small increase in θ_{11} again in the very near wake due to the finite thickness of the trailing edge of the airfoil. Continuing into the wake we see a gradual decrease of θ_{11} brought about by the combined contributions from the favorable longitudinal pressure gradient and the rotation of the velocity vector towards the streamwise direction. The effect of the gradual weakening of three-dimensionality in the flow is also seen from Fig. 22 which shows that the momentum deficit thickness θ_{21} decreases nearly to zero at the last station. Unfortunately, measurements could not continue beyond x/L = 1.928. It is assumed that the flow will be two-dimensional beyond this distance and hence θ_{11} will remain constant at its value θ_f at the last station. This value is, therefore, used as the reference length scale in the rest of the figures.

Figure 23 shows the variation of the displacement thickness along the streamwise direction. The initial increase in the boundary layer is caused again by the adverse pressure gradient in the trailing edge region. Subsequent reduction in δ_1 is primarily due to the evolution of the wakelike profile from the original boundary-layer-like profile. This trend is, of course, also influenced by factors such as the prevailing favorable pressure gradient and gradual decay of three-dimensionality. The changes in profile shape are more clearly seen from Fig. 24, which shows the variation of the shape factor H with θ_f . It is seen that the shape factor, at the trailing edge, has a value of about 1.5, indicating that the boundary layer is only under a moderate adverse pressure gradient. The shape factor is seen to drop quick¹ and at $x/\theta_f = 326$, is only slightly greater than 1, its asymptotic value at very large distances.

4. Growth and Decay of the Velocity Defect and Wake Width

The decay of the maximum longitudinal velocity defect w_{xo} is shown in Fig. 25 in the usual coordinates used for two-dimensional wakes. The distance downstream is normalized with θ_f . Also shown in the figure is the asymptotic decay law [See Sastry (1981)].

$$\left(\frac{U_{\infty}}{W_{x0}}\right)^{2} = .4\left(\frac{x}{\theta_{f}}\right)$$
(29)

for two-dimensional far-wake. The data seem to indicate that the decay rate approaches this law near the farthest downstream station $(x/\theta_f = 326)$. Likewise, Fig. 26 shows the half-width of the wake again plotted in the usual two-dimensional coordinates. The theoretical two-dimensional far-wake behavior given by [Sastry (1981)].

$$\left(\frac{b_{x}}{\theta_{f}}\right)^{2} = .355 (x/\theta_{f})$$
 (30)

is also shown in the figure. The wake width does not show any clear signs of approach to two-dimensional far-wake state, though changes in slope qualitatively resemble two-dimensional flow results. In Figure 25, if the dotted line can be assumed to represent the decay process at large distances, it intersects the x-axis, at a virtual origin corresponding to $x/\theta_f = 70$. If, this point is joined to the last data point in Fig. 26 the line is approximately parallel to the asymptotic growth line. This is a very rough indication that the wake has perhaps reached very nearly the two-dimensional far-wake state at $x/\theta_f = 326$. This observation is in conformity with the findings of Sastry (1981), who inferred that the two-dimensional wake behind a flat plate reaches an asymptotic state around $x/\theta_f = 350$. The present data, are inadequate to confirm this definitively. More closely spaced data as well as data extending further downstream are needed to substantiate the present observations.

Figures 27 and 28 show the corresponding decay and growth rates of parameters w_{zo} and b_z , the maximum defect velocity in the z-direction and half-width of this profile. The velocity defect in this case is normalized by $U_{\infty} \sin \phi$ (where ϕ is the sweep angle), since this is the maximum value that w_z can attain. It is seen that the crossflow defect velocity decays very rapidly compared to the longitudinal velocity. The wake half-width behaves qualitatively like b_x but is seen to be much larger.

5. Self Similar Velocity Profiles

The velocity data plotted in the conventional self-similar coordinates are shown in Figs. 29 and 30. In Fig. 29 showing the streamwise velocities, it is seen that beyond $x/L = 0.138 (x/\theta_f = 23.4)$ the profiles become very nearly self-similar and that the profiles follow closely the profile for asymptotic two-dimensional far-wakes. The spanwise velocity profiles shown in Fig. 30 also appear to approach selfsimilarity. Compared to the w_{x0} profile, however, the half-width of this self-similar profile is approximately 25% larger.

6. Turbulent Stress Measurement

The turbulence quantities measured using the three-dimensional hot wire probe can be analyzed in different ways. First of all, the three intensities u', v', w' and the three shear stresses uv, uw and vw are normalized with respect to the freestream velocity so that general trends may be observed. These results are shown in Figs. 31 thru 36. In general, the intensities are of similar magnitude and behave in a similar way. This indicates that the turbulence is not too far from isotropy. Furthermore, in Figs. 31, 32, and 33 it is seen that the profiles exhibit a minimum in the center and are fairly symmetric about the wake center-The shear stresses \overline{uv} , \overline{vw} and \overline{uw} are shown in Figs. 34, 35 and 36. line. It is seen that uv and vw are nearly anti-symmetric about the wake centerline changing sign as expected. In contrast, however uw measurements are considerably in error. This stress has almost the same magnitude as \overline{vw} . This trend is similar to that observed during the validation tests in the flat plate wake mentioned earlier. The ratio of \overline{vw} to \overline{uv} is shown in

Fig. 37. This ratio is a good measure of the three-dimensionality of the shear flow field. It is seen that at the last station $(x/\theta_f = 326)$, \overline{vw} is of the order of 15% of \overline{uw} , indicating the near two-dimensionality of the flow field. Next, the decay rates for u'_{max} \overline{uv}_{max} and \overline{vw}_{max} are shown in Fig. 38. The centerline turbulent intensity is seen to increase continuously with distance downstream. The normalized Reynolds shear stress $\frac{\overline{uv}_{max}}{2}$ is also increasing, but at the last measuring station its value is only slightly higher than the value of 0.48 for the asymptotic two-dimensional far-wake (Sastry 1981). The shear stress $\frac{vw_{max}}{2}$ on the other hand is found to be slowly decreasing at large values of x/θ_{f} . It is difficult to predict from the present measurements whether it would continue to decrease or reach an asymptotic value farther down-The development of \overline{uv}_{max} is faster than in the case of the flat stream. plate wake of Sastry or Pot (1979), but otherwise qualitatively similar in that it approaches the asymptotic value from "below". This is in contrast with the behavior of either the wake behind a cylinder or that behind a two-dimensional airfoil at incidence [Sastry (1981)]. In both these cases, \overline{uv}_{max} decreases to the asymptotic value from 'above". The trends in all these cases are consistent with the relative influence of the wall on the velocity profile just before the flow detaches from the wake generator.

7. Self Preservation of the Turbulence Profiles

Figures 39-41 show the profiles of u', \overline{uv} and \overline{vw} in self preserving coordinates. It is seen that the profiles are evolving continuously.

It <u>appears</u> that the turbulence properties have not attained self-similarity even at the last location. However, since \overline{uv}_{max} at $x/\theta_f = 326$ is nearly equal to the asymptotic value, further data in the far wake are needed to determine whether the turbulence profiles indeed have attained the asymptotic self-preserving form.

8. Eddy Viscosity Results

The present data can be used to calculate the eddy viscosity in both x and z directions defined by

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$$\varepsilon_{x} = \frac{\overline{uv}}{\partial U/\partial y}$$
(31)

and

$$\epsilon_z = \frac{\overline{vw}}{\partial \overline{w}/\partial y}$$
(32)

Plots in self-preserving coordinates of both ε_{χ} and ε_{z} are shown in Figs. 42 and 43. From this it is seen that both viscosities are evolving continuously. The eddy viscosity in the z direction exhibits considerable scatter, but is still of similar magnitude as ε_{χ} . As to whether or not the flow has reached asymptotic behavior it is difficult to confirm because of the lack of adequate data points between $x/\theta_{f} =$ 180 and 326. However, the value of ε_{χ} obtained from the present experiments can be compared with the asymptotic values given by Schlichting (173) and Sastry (1981). At $x/\theta_{f} =$ 326 the present value for $\varepsilon_{\chi}/U_{ef}^{0}$ is .039. This compares with .032 quoted by Sastry and a value of .044 by Schlichting. Therefore, it seems reasonable to say that at $x/\theta_f = 326$ the streamwise flow is sufficiently close to the two-dimensional far-wake.

If we now assume an average eddy viscosity from Figs. 42 and 43 for each x/L location, we should in turn be able to recalculate the stresses. Typical results for \overline{uv} and \overline{vw} are shown in Figs. 44-47. These figures allow us to compare the extent to which it is realistic to use a constant eddy viscosity model to describe the shear stress in the wake. For the shear stress \overline{uv} it is seen that the agreement with experiment is gcod. The plots for \overline{vw} show the difference in result obtained by using ε_z or ε_χ (scalar eddy viscosity assumption). Average values of the viscosity for the given x-iocation were used in each case. The comparison (considering experimental scatter) shows little difference and hence we conclude, that for calculation purposes, ε_χ can be used as a scalar eddy viscosity at least for mild crossflows.

9. The Structure Parameter

Nash proposed for three-dimensional turbulent shear flow, the following relations (see Nash and Patel 1972):

$$|\overline{uv}| = a \overline{q}^2 \frac{\Im^{1/\Im y}}{\left[\left(\frac{\partial U}{\partial y}\right)^2 + \left(\frac{\partial W}{\partial y}\right)^2\right]^{1/2}}$$
(33)

$$|\overline{vw}| = a \overline{q}^2 \left(\frac{\overline{\partial W}}{\partial y}\right) / \left[\left(\frac{\overline{\partial U}}{\partial y}\right)^2 + \left(\frac{\overline{\partial W}}{\partial y}\right)^2\right]^{1/2}$$
(34)

where $q^2 = (u'^2 + v'^2 + w'^2)/2$ and

"a" is often called the structure parameter. For two-dimensional flows, the proposal takes the form

$$|\overline{uv}| = a \overline{q^2}$$
(35)

Results of calculating 'a' from Eq. (34) are shown in Fig. 48. It is seen that except near the centerline and in the outer intermittent region, 'a' has a nearly constant value. Typical comparisons of the value of 'a' obtained using the alternate definitions Eq. (34) and Eq. (35) (three-dimensional and two-dimensional definitions) are shown in Fig. 49. It is seen that two-dimensional definition is adequate to evaluate 'a' in this mildly three-dimensional flow. Again, to assess the validity of the model for practical use in three-dimensional flows an average value for a (= .15) was used in Eq. (34) to calculate \overline{vw} for a few nearwake locations. These results are compared with measurements in Fig. 50. The agreement is seen to be moderate considering the uncertainties in measurement. Therefore, it can be concluded that the structure parameter model in the for of Eqs. (33) and (34) is reasonably satisfactory for describing dimensional wakes.

10. Conclusions

The following conclusions can be arrived at from the study reported in this thesis.

1. A triaxial hot-wire probe can be used, with one of the techniques developed in the present study, for turbulence measurements in three-dimensional shear flows. The accuracy of such measurements, critically depends on probe orientation, probe size and correct knowledge of sensor angles.

2. The present techniques A and B are superior to that used by Gorton and Lakshminarayana (1976) both in accuracy and versatility.

3. At present, the measurement of \overline{uw} is unsatisfactory. Further miniaturization of probe is necessary to get better results.

4. The study of the developing three-dimensional wake behind an infinite swept airfoil shows that the static pressure varies across the near-wake with the maximum occurring at the wake centerline.

5. The longitudinal and crossflow wake defect components reach near self-similar distributions within about 10 momentum thicknesses downstream of the trailing edge.

6. Three-dimensionality of the flow becomes negligible within about 325 momentum thicknesses. Also, at this distance, the wake begins to exhibit many of the mean and turbulent flow properties of two-dimensional far-wakes.

7. A scalar eddy viscosity, constant across the wake, can be used to describe both the shear stress components \overline{uv} and \overline{vw} reasonably well.

8. The turbulence in the wake exhibits structural similarity in the manner proposed by Nash.

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Schlichting, H., 1979 "Boundary Layer Theory," McGraw-Hill Book Co., New York, N.Y., USA.

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Station #	x/L	x/0 _f
1	220	-36.7
2	124	-21.0
3	014	- 2.37
4	+.014	2.37
5	.027	4.57
5	.041	6.94
,	.055	9.32
3	.138	23.4
)	.275	46.6
0	. 399	67.6
1	.661	112.0
2	.992	168.1
3	1.928	326.7

Table 1

Boundary Layer and Wake Traverse Stations

-

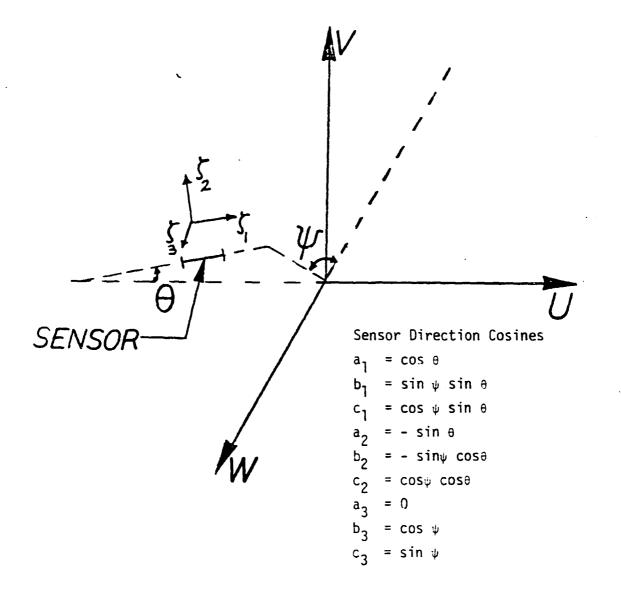
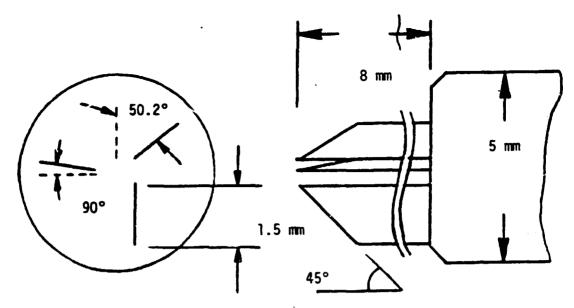
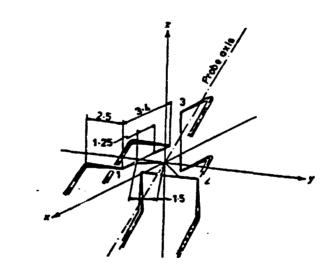


Figure 1. Sensor coordinate system and sensor direction cosines

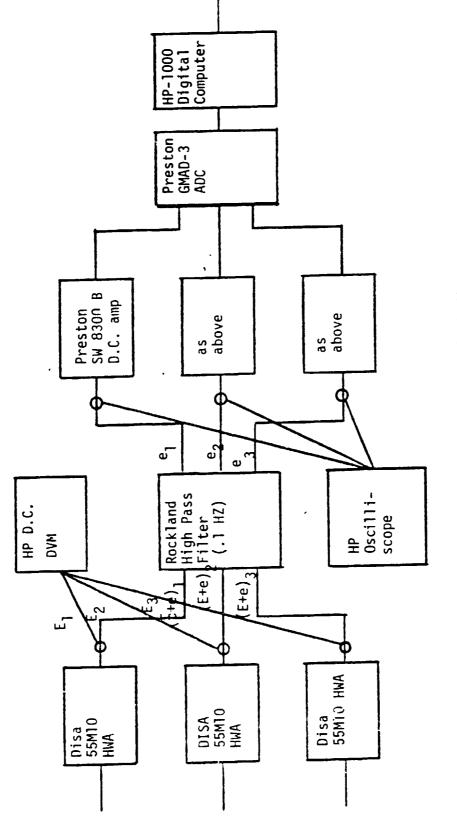


a. IIHR constructed three-dimensional hot-wire probe



b. Disa 55P91 three-dimensional hot-wire probe

Figure 2. Hot-Wire Probes



1. J. 100 - 100-



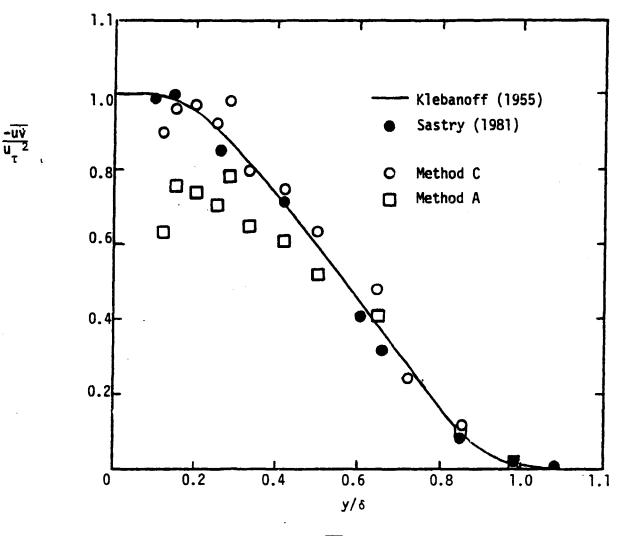


Figure 4. Distribution of \overline{uv} in the flat plate boundary layer at -76.3 mm

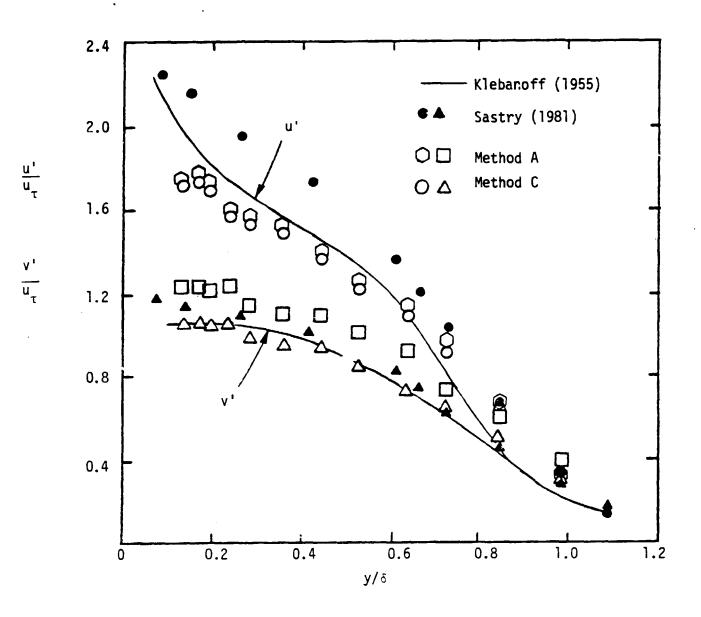


Figure 5. Distribution of u' and v' in flat plate boundary layer at -76.3 mm

-

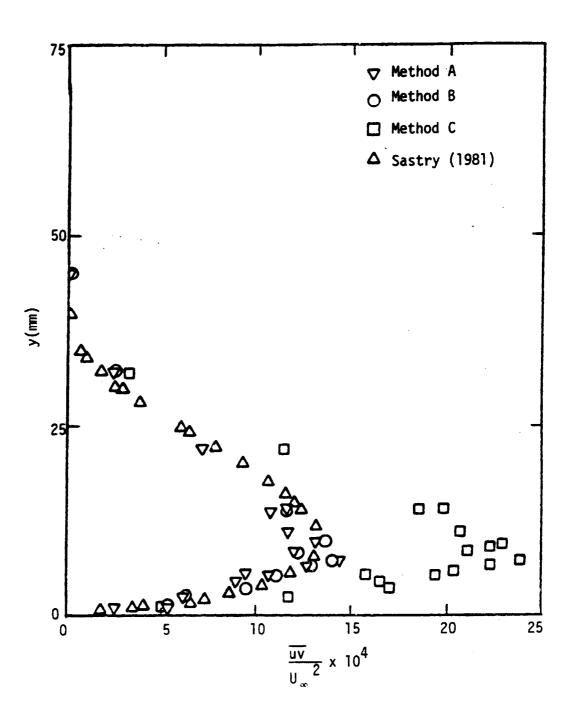


Figure 6. Distribution of \overline{uv} in the flat plate wake at 177.8 mm

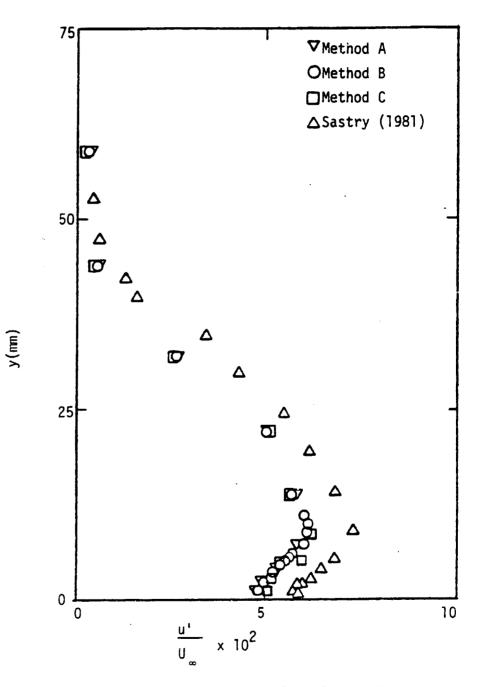


Figure 7. Distribution of u' in the flat plate wake at 177.8 mm

.

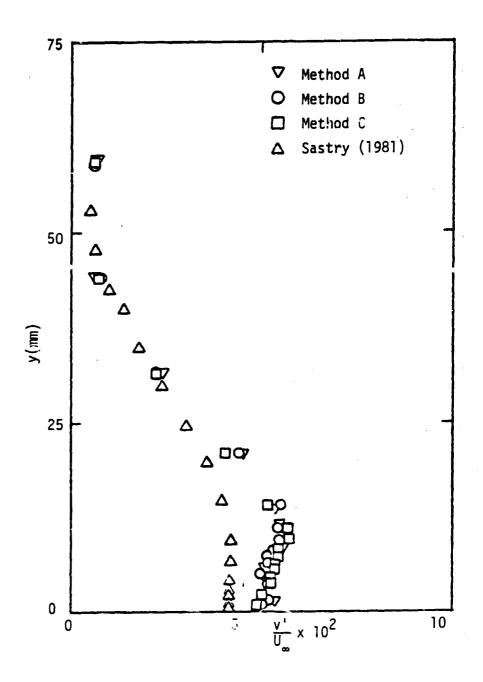


Figure 8. Distribution of v' in the flat plate wake at 177.8 $\ensuremath{\mathsf{mm}}$

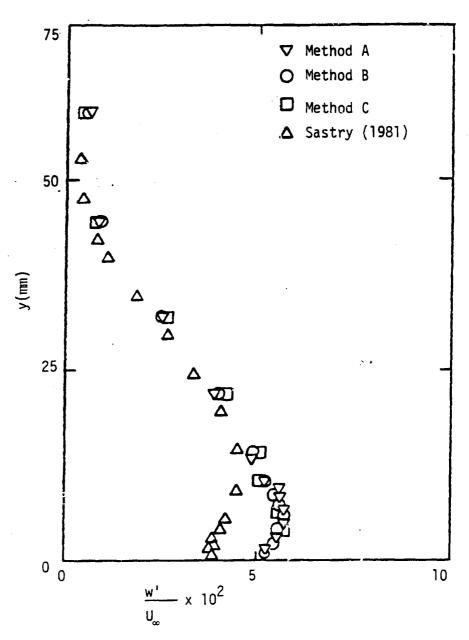
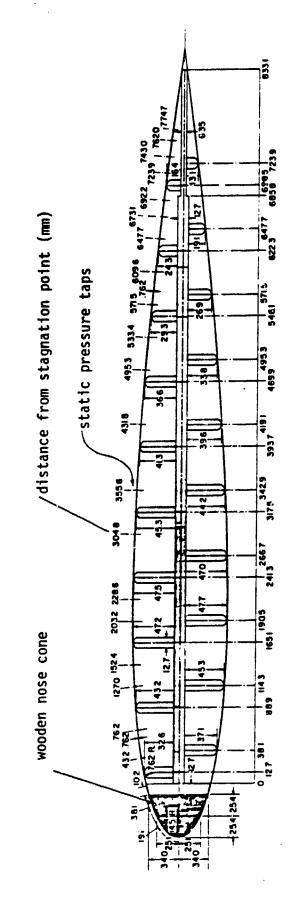


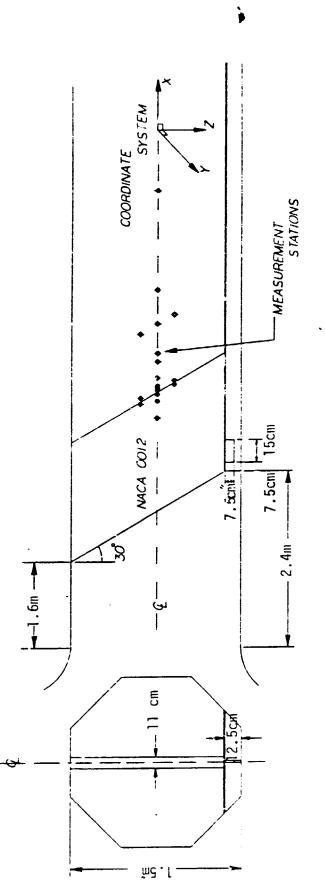
Figure 9. Distribution of w' in the flat plate wake at 177.8 mm



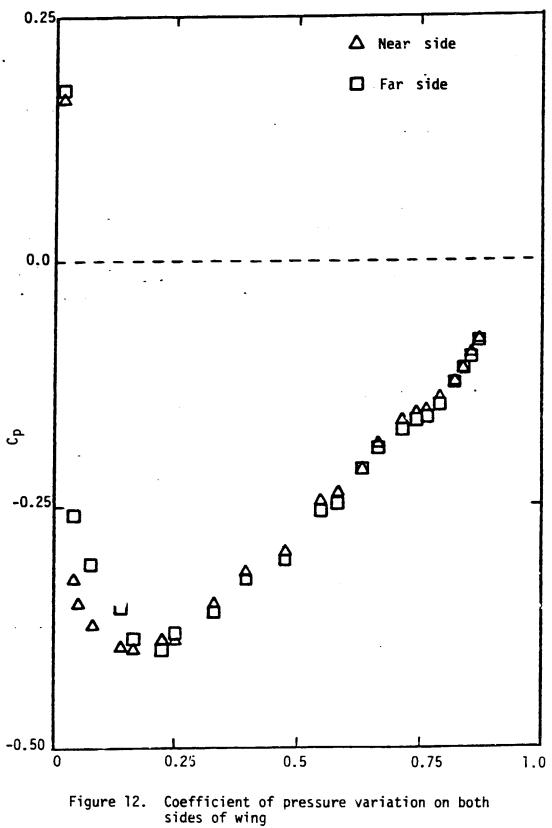
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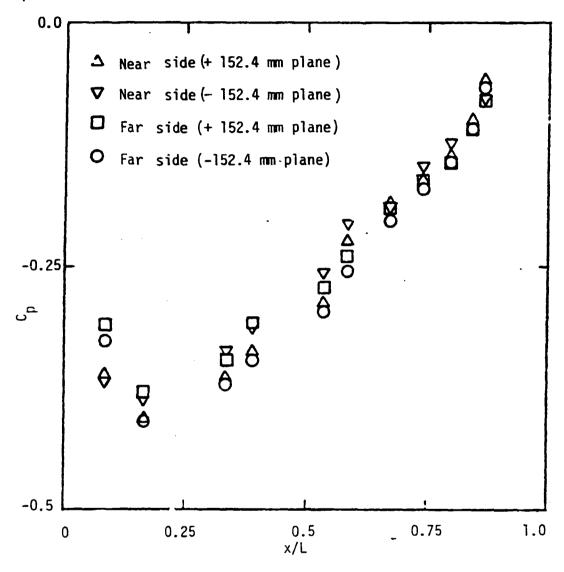
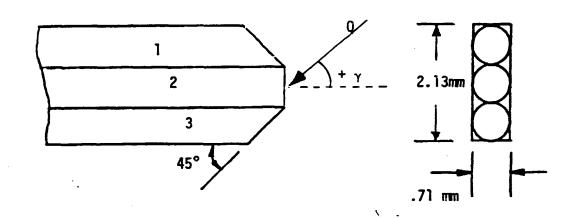


Figure 13. Coefficient of pressure variation on both sides of wing on a sinwise basis



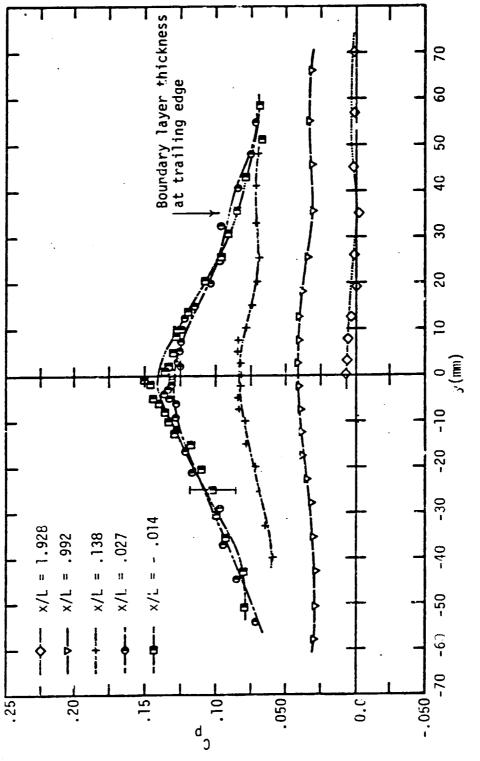
$$AKP = \frac{1 - \frac{1}{3}}{\frac{1 + \frac{1}{3}}{\frac{1}{2} - \frac{1}{2}}}$$

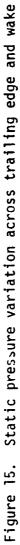
 $AK23 = P_2 - P_3$

$$\frac{1}{2} \circ 0^{2} = \frac{4}{2} \frac{51885 + .023779 *_{Y} - .0000142 *_{Y}^{2} - .0000035 *_{Y}^{3} - .0000001 *_{Y}^{4}]}{\gamma = -1.4345 + 10.28219 * AKP + .04959500 * AKP^{2} - .0246590 * AKP^{3} - .0148545 * AKP^{4}}$$

 $P_{\text{static}} = P_2 - [1.0088296 - .0011767 * \gamma - .0002621 \gamma^2] * 1/2 \rho Q^2$

Figure 14. Yaw probe description and calibration





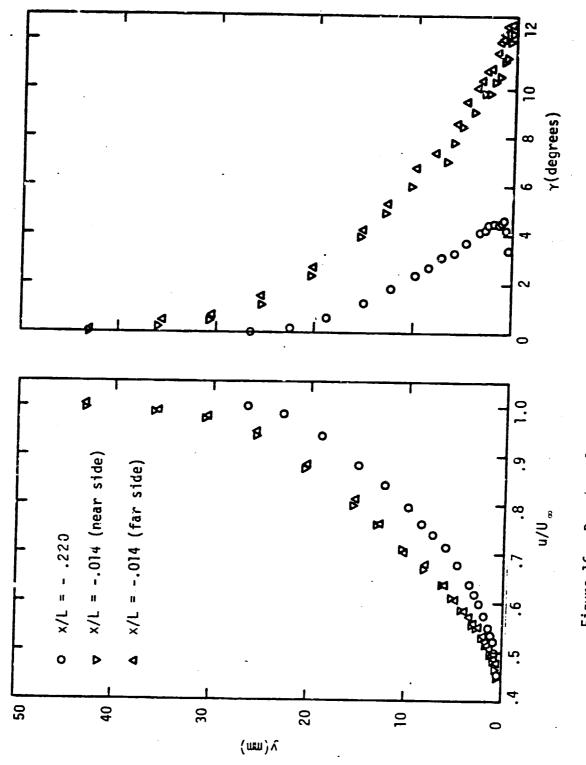
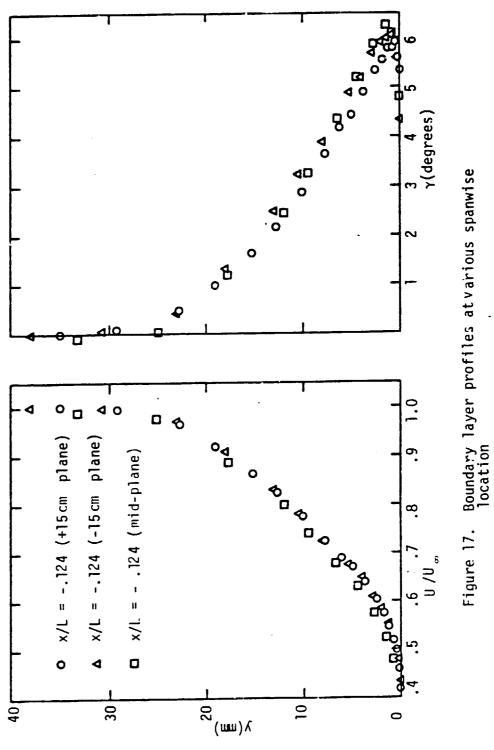


Figure 16. Boundary layer profiles at x/L =-.014 and -.220



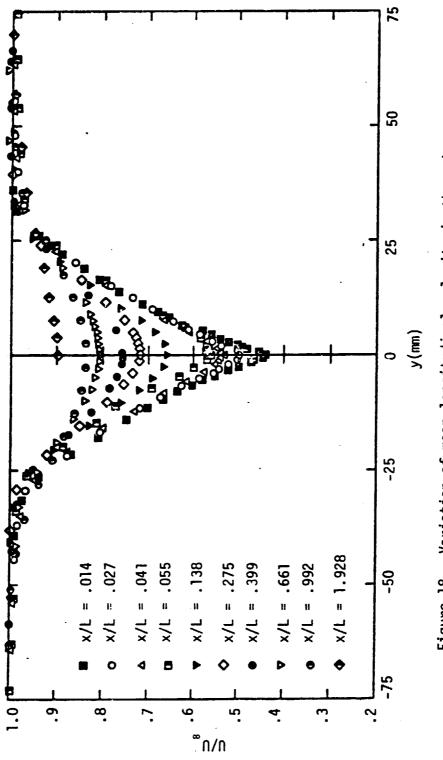
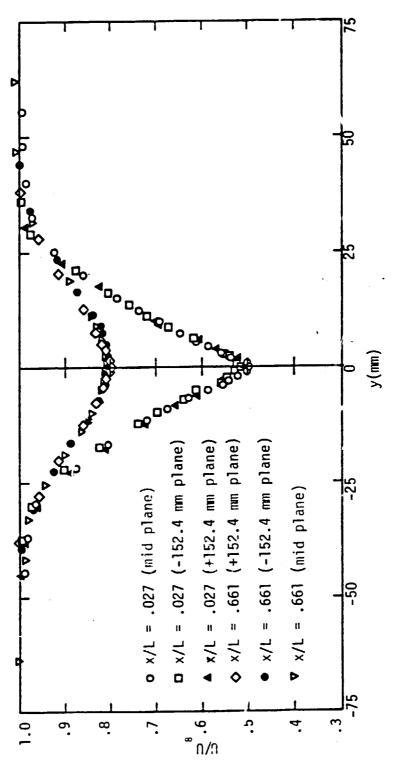
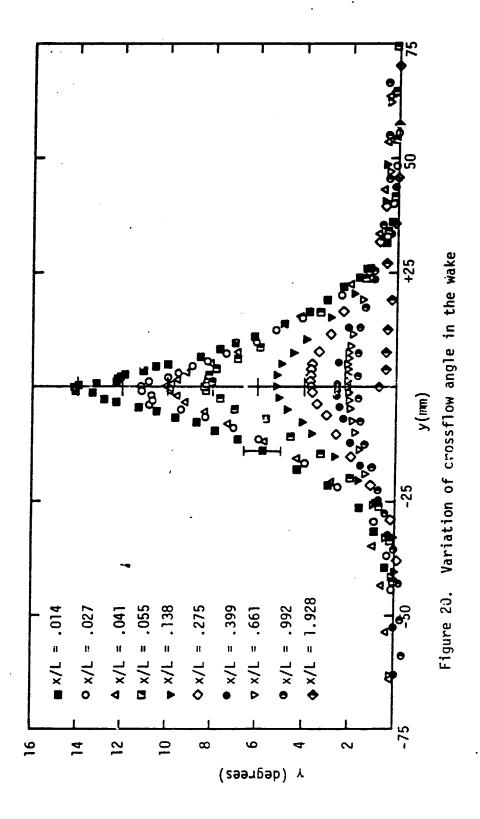
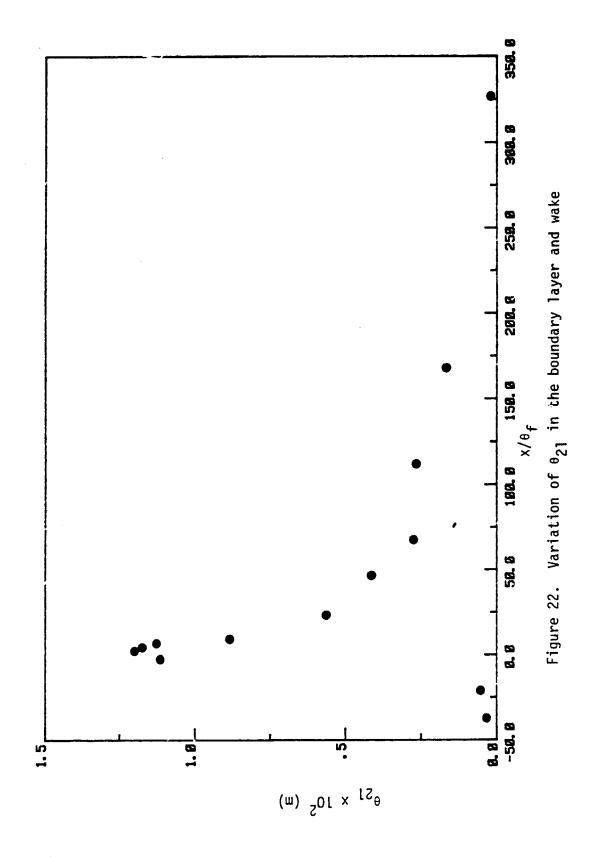


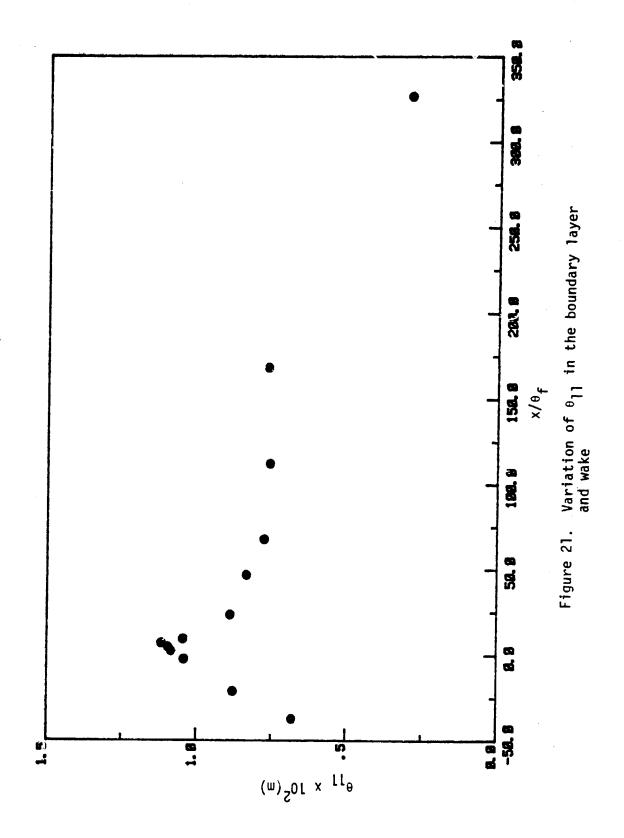
Figure 18. Variation of mean longitudinal velocity in the wake

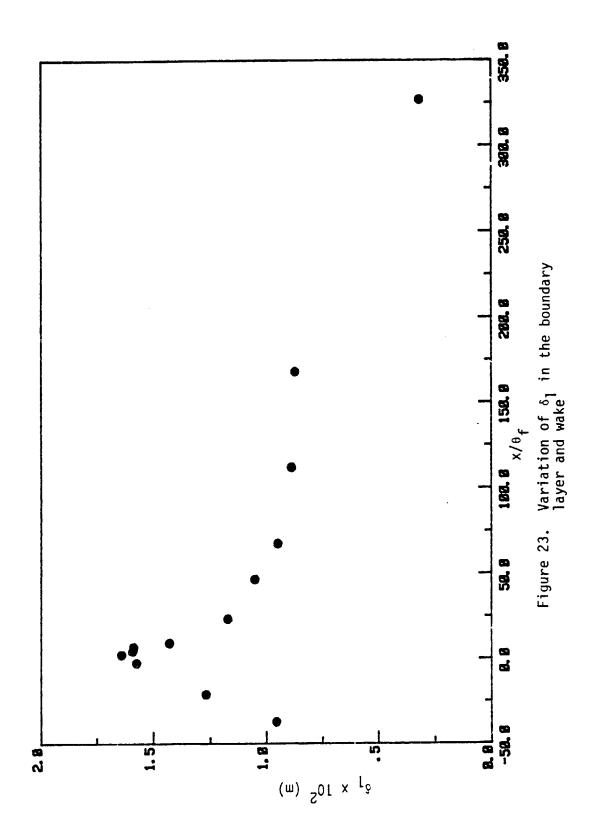


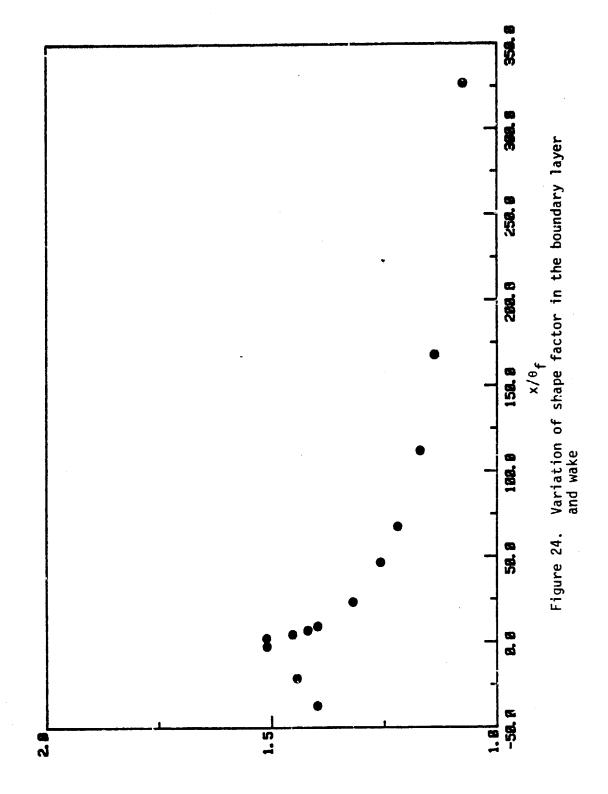




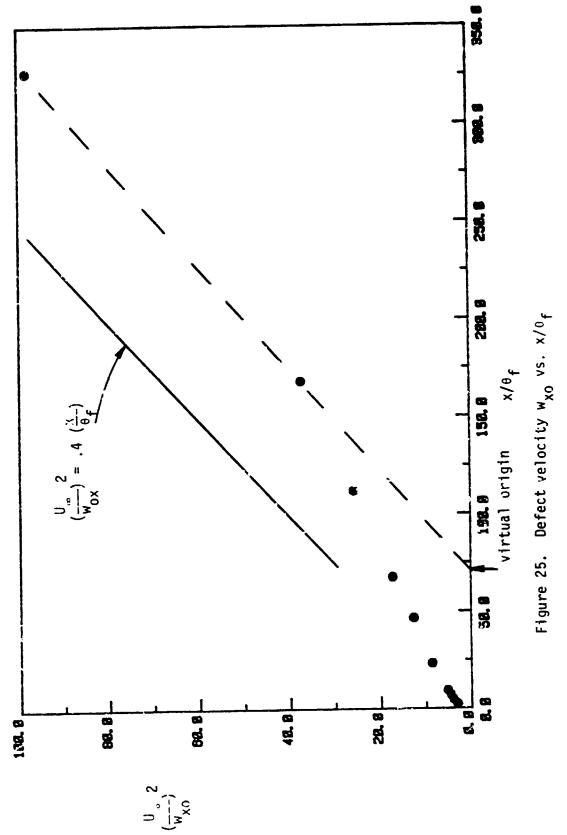


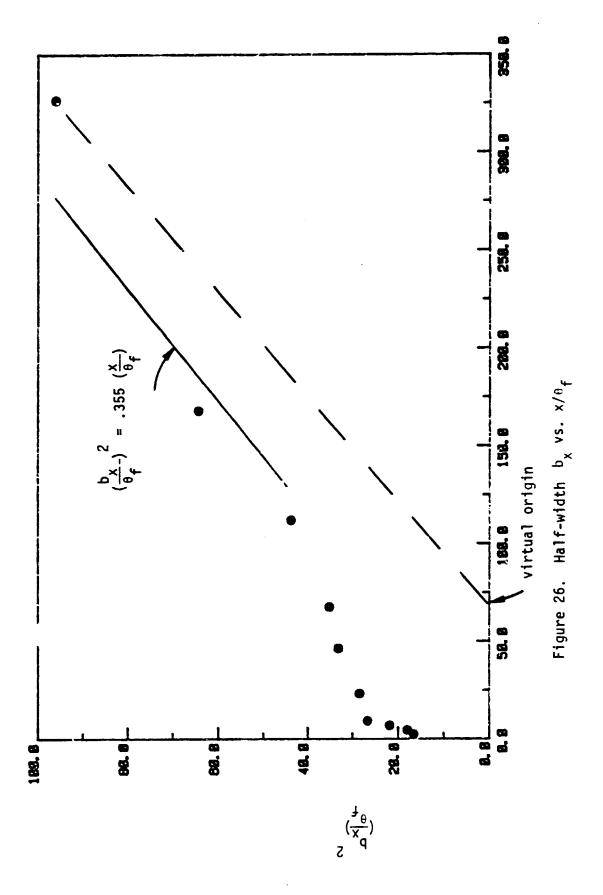


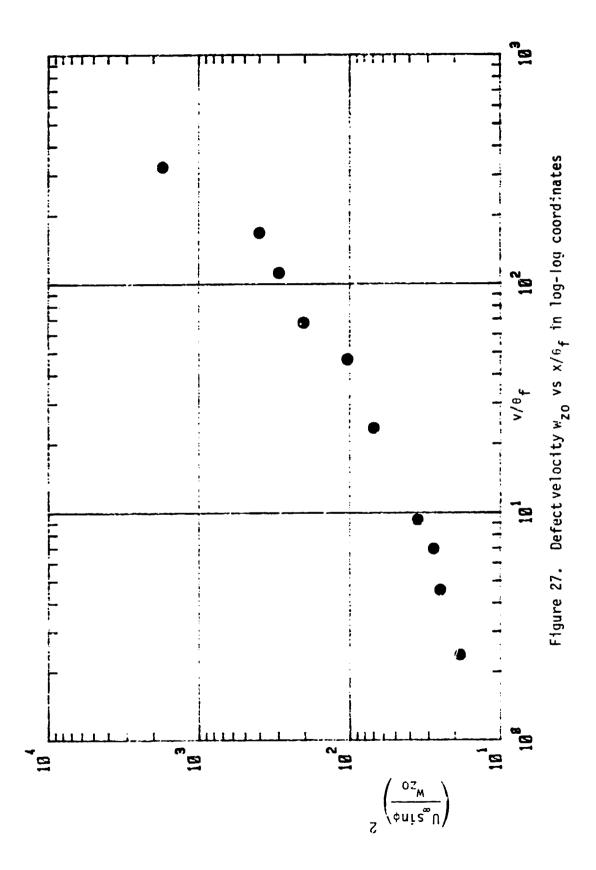


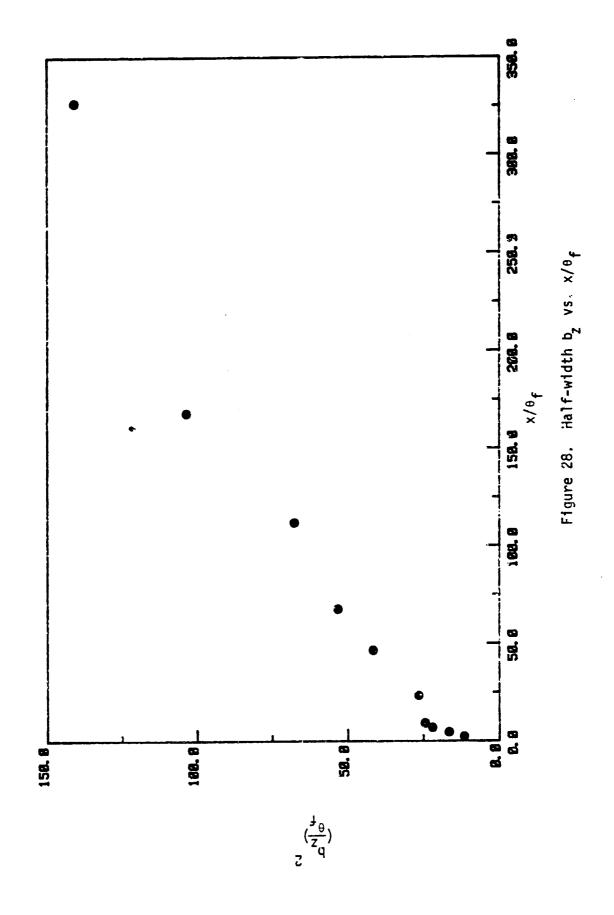


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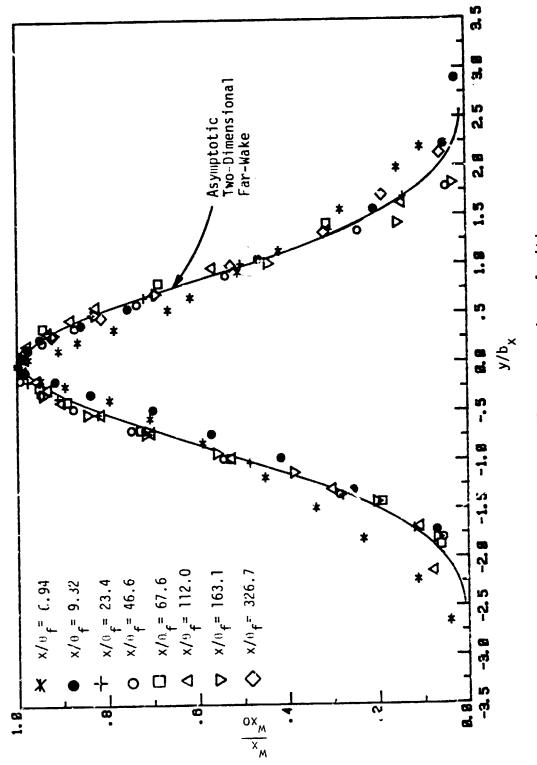
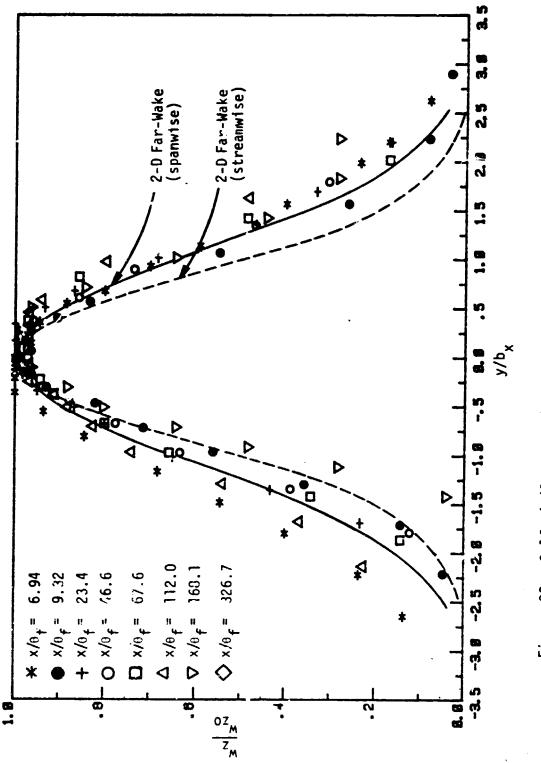
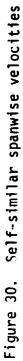
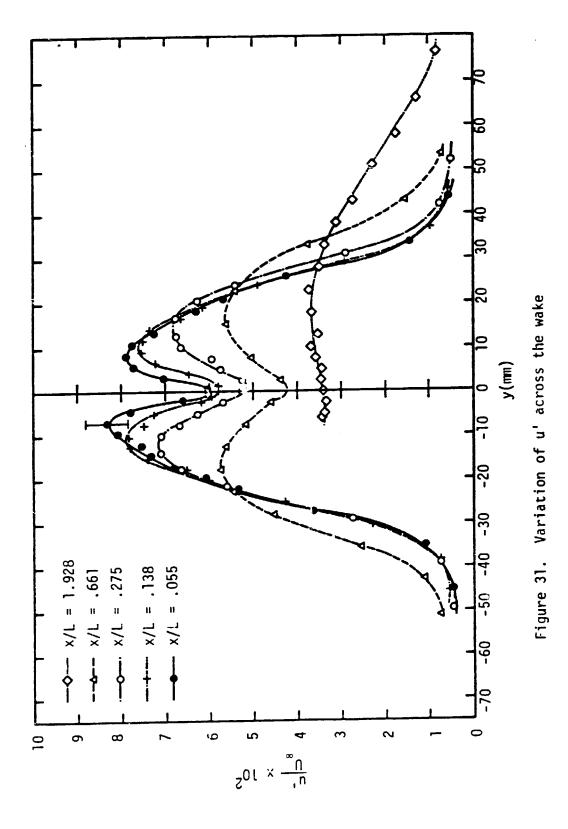
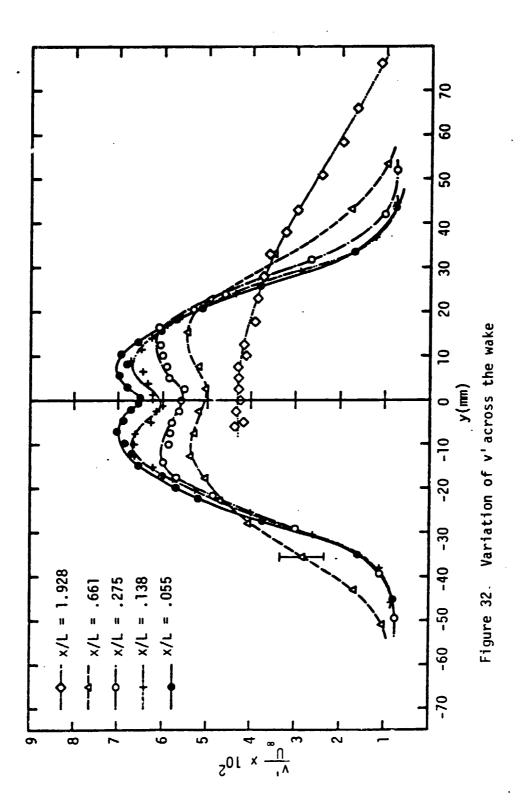


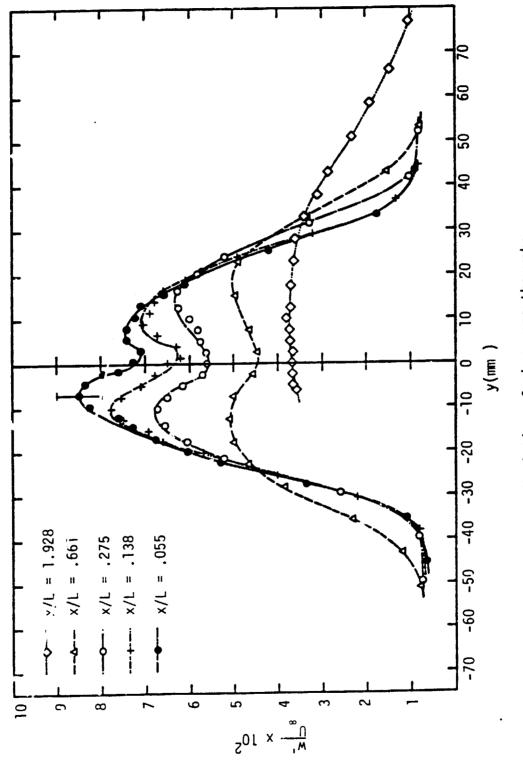
Figure 29. Self-similar streamwise velocities



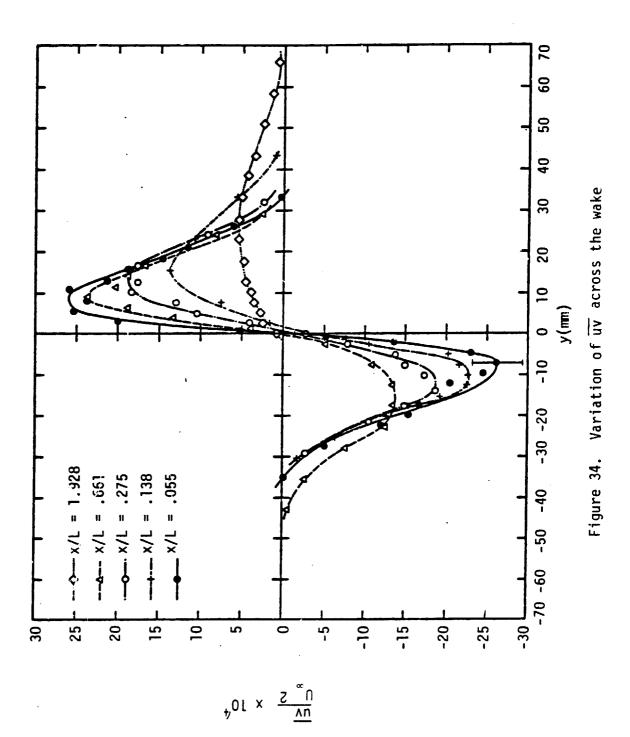


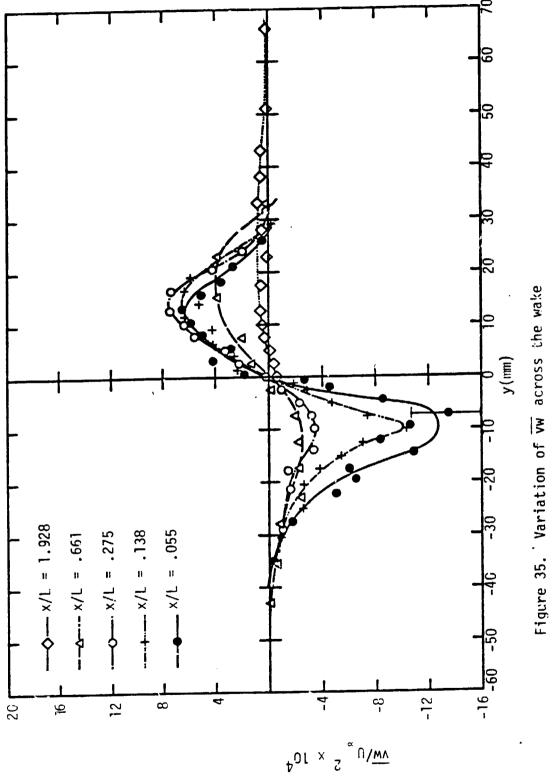


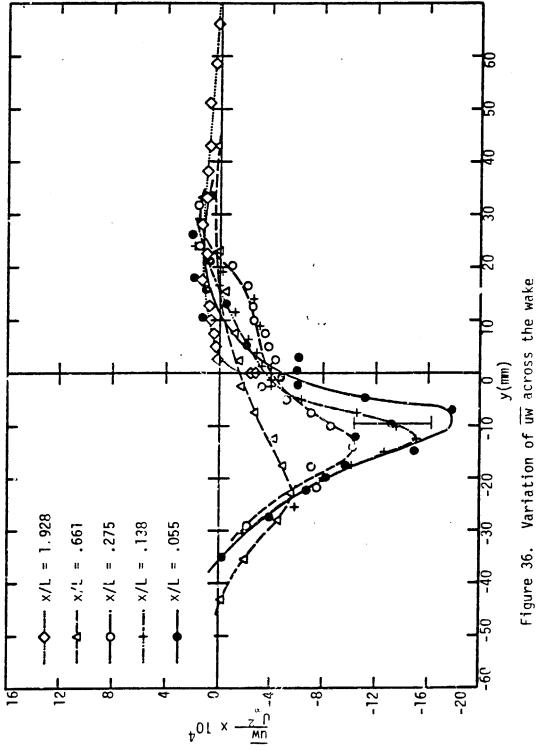


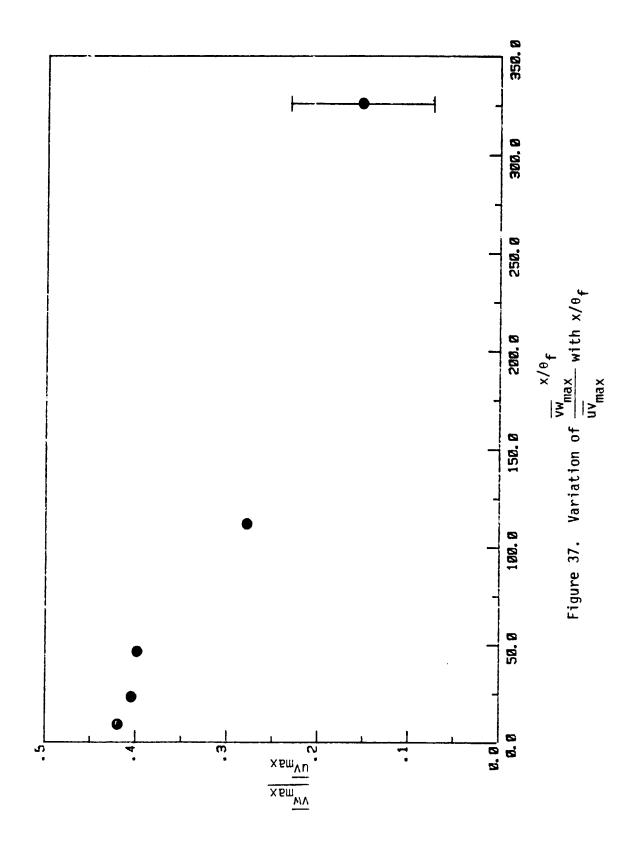


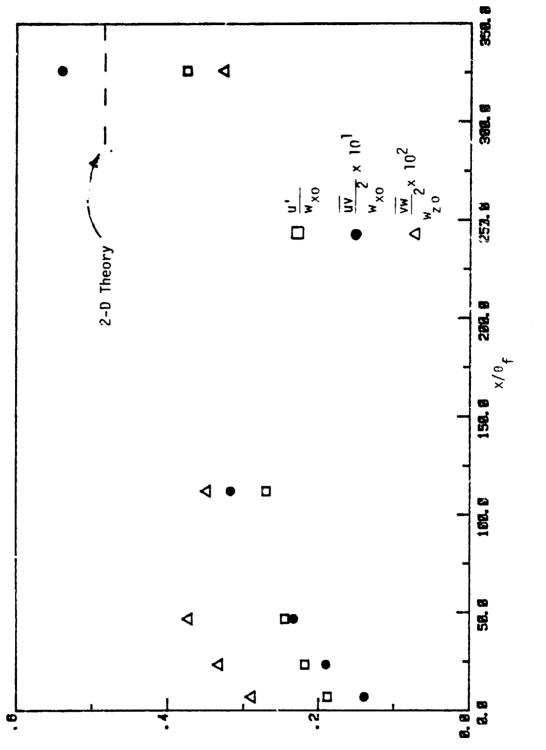


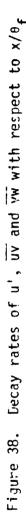




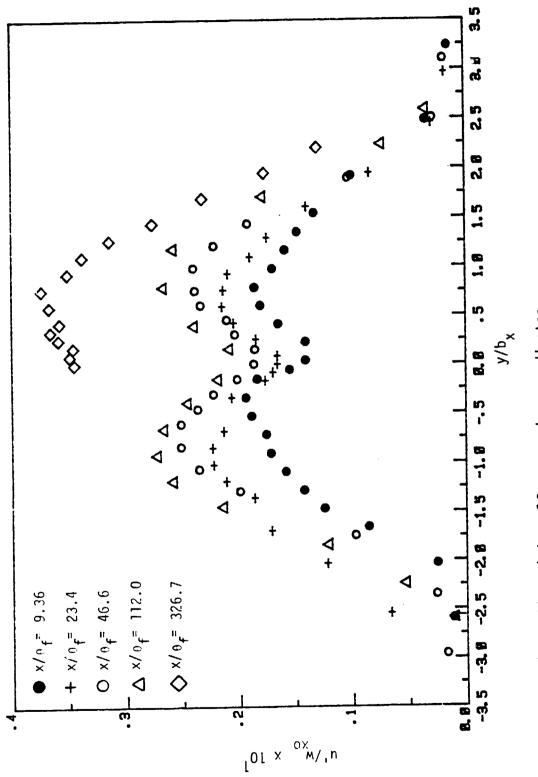




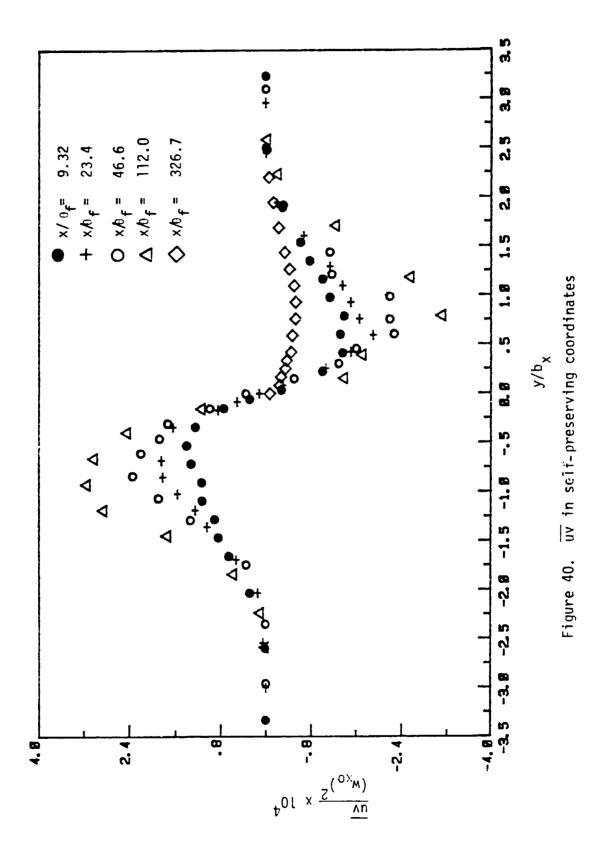


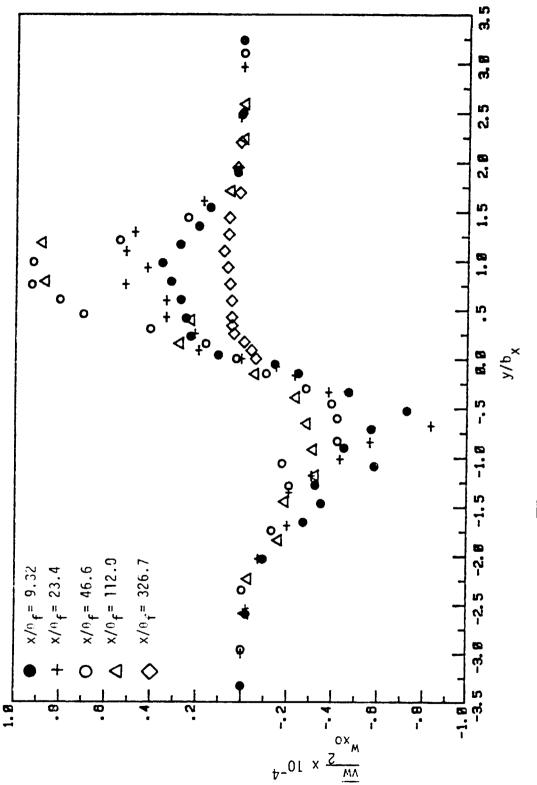


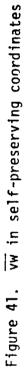
Non-Dimensional Growth Rates

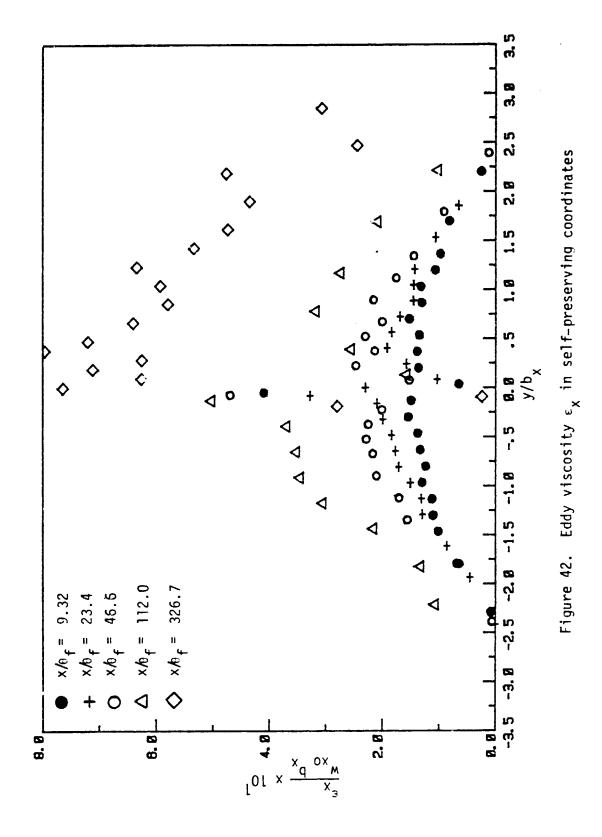


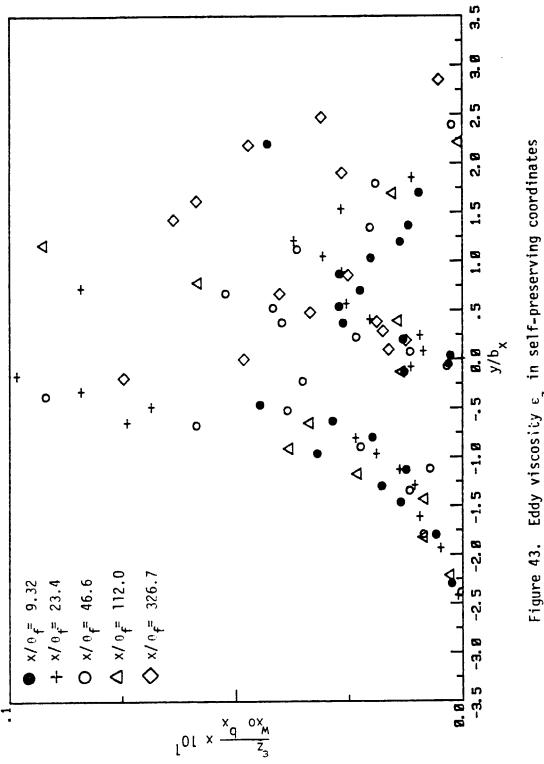


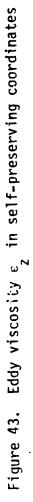


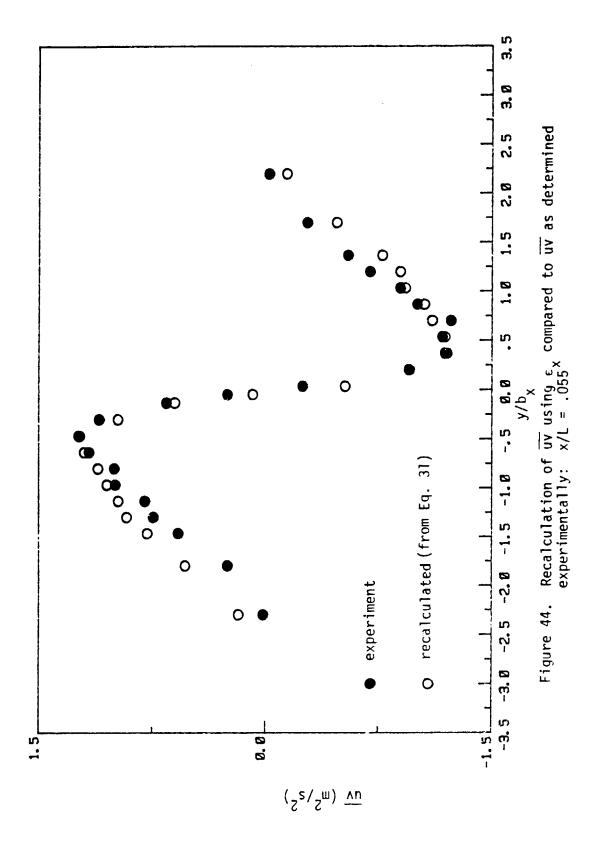


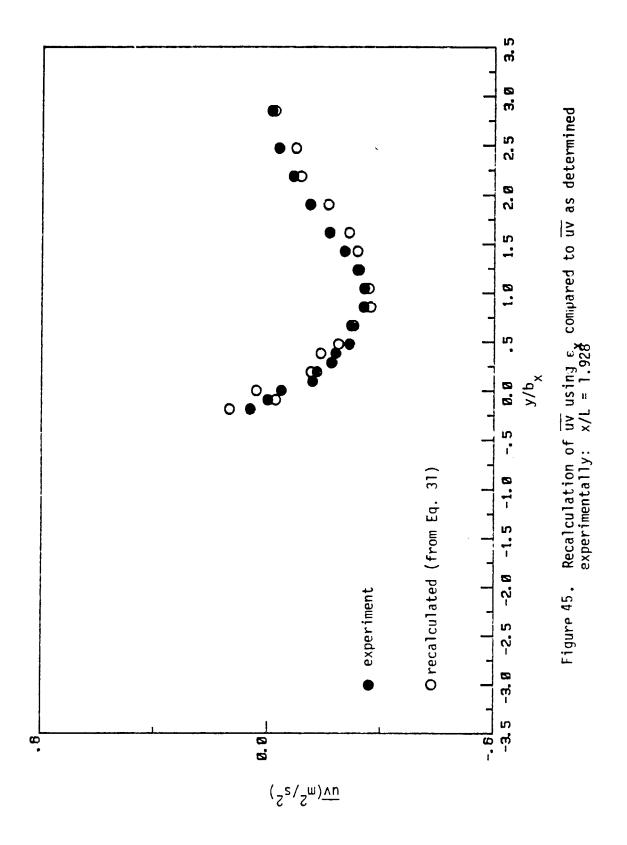




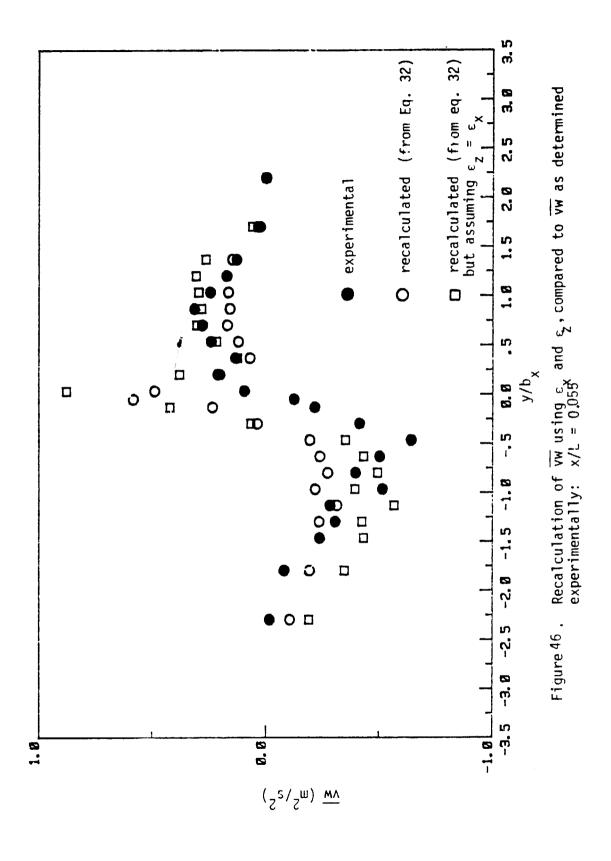


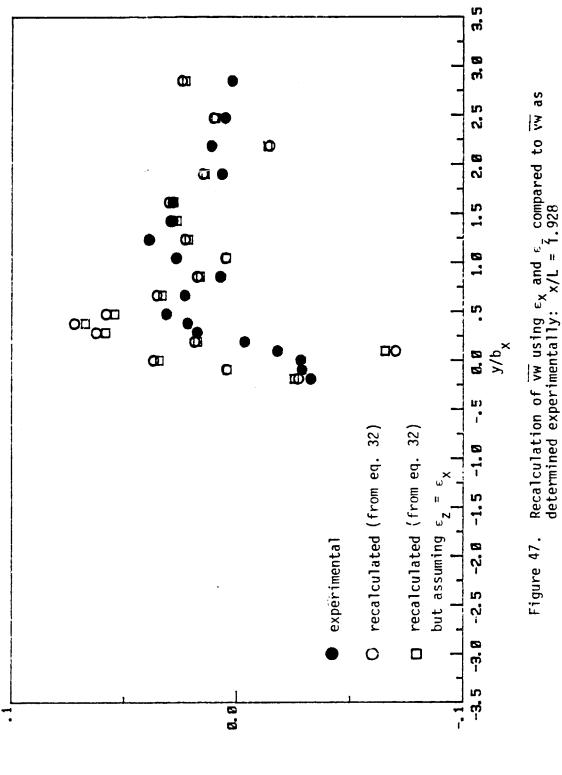






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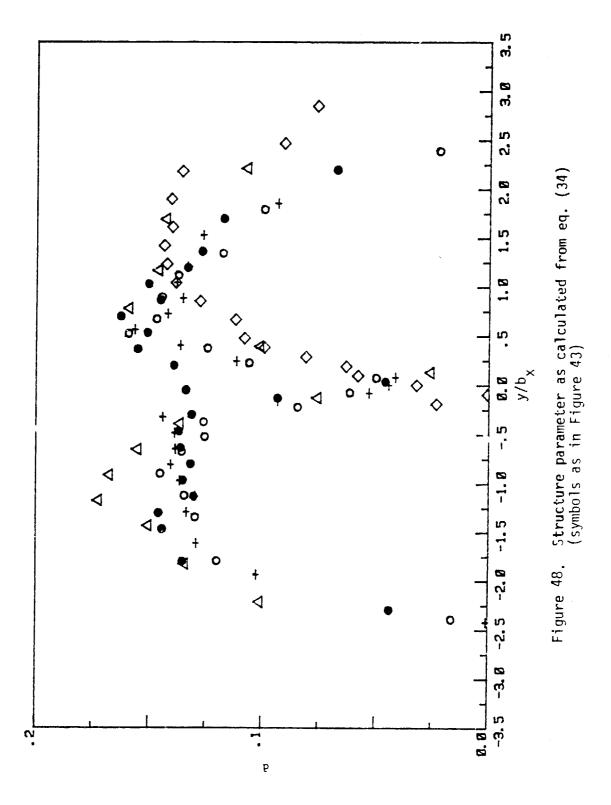


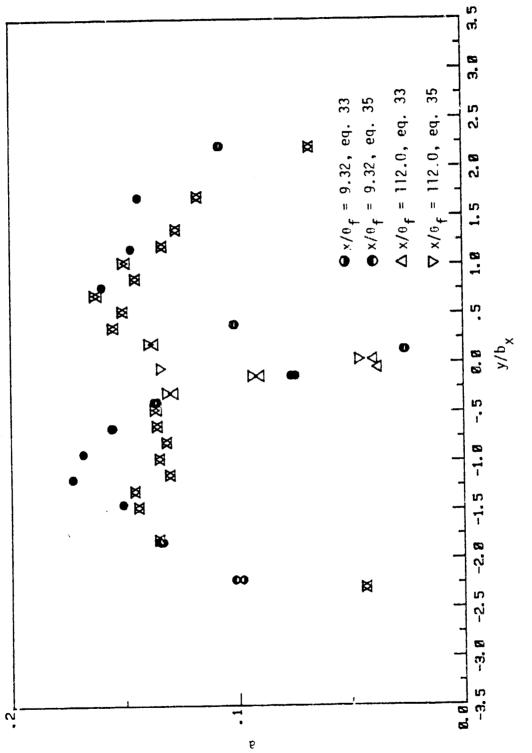


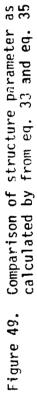
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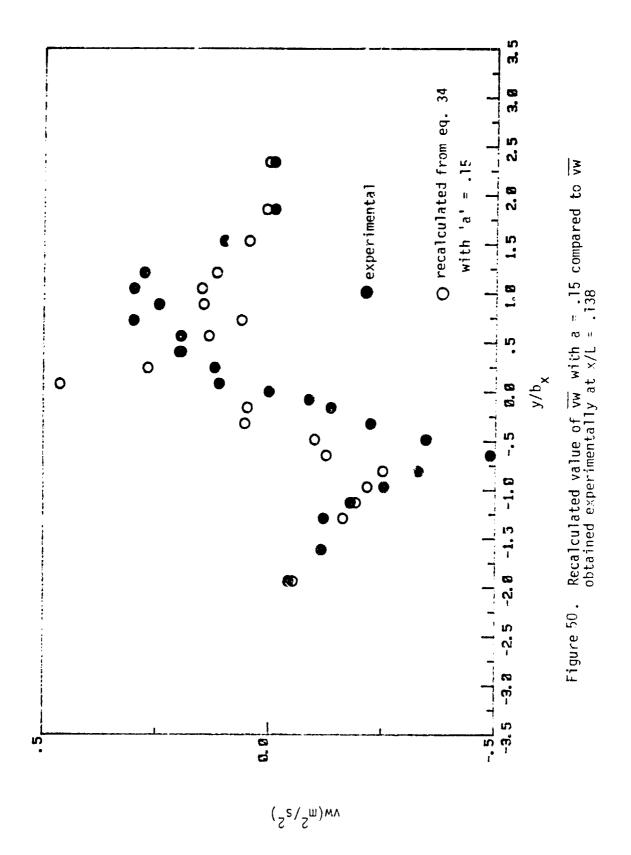
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(²s/²m) <u>wv</u>









APPENDIX

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TABLES OF EXPERIMENTAL DATA

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Beta	angle between mean flow vectors and the chordline
Gama	angle between mean flow vectors and the free streamline
Delta*sub x	δ _l meters
Delta*sub z	δ ₂ meters
Theta sub x	δ _{]]} meters
Theta sub z	δ ₂₂ meters
Theta sub xz	δ ₁₂ meters
Theta sub zx	δ ₂₁ meters
Pstatic	static pressure in inches of alcohol
u/Uinf	local chordwise velocity/reference velocity
w/Jinf	local spanwise velocity/reference velocity
U bar 1	u/U_{x} from 3-D hot wire probe
V bar	normal velocity component/U from 3-D hot wire probe
W bar	W/U_{∞} from 3-D hot wire probe
uu bar	√u ² /U _∞ x 100
vıv bar	$\sqrt{v^2}/U_{\infty} \times 100$
ww bar	√₩ ² /U_ x 100
uv bar	$\frac{\mathrm{uv}}{\mathrm{U_m^2}} \times 10^4$
Y(mm)	distance from wake centerline or wall in millimeters
uw bar	$\frac{\overline{uw}}{U_{\infty}^2} \times 10^4$

 $\frac{\overline{vw}}{U_{a}^{2}} \times 10^{4}$ vw bar $\frac{\bar{u}^3}{U_2^3} \times 10^5$ uuu bar $\frac{\bar{v}^3}{U_a^3}$ x 10⁵ vvv bar $\frac{\bar{w}^3}{U_{x}^{2}} \times 10^5$ www.bar $\frac{\overline{u^2 v}}{U_{\pi^3}} \times 10^5$ uuv bar $\frac{\overline{u^2 w}}{U_a^2} \times 10^5$ uuw bar • $\frac{uv^2}{U_x^2} \times 10^5$ vvu bar $\frac{\overline{v^2_w}}{\overline{U_m^3}} \times 10^5$ vvw bar $\frac{\overline{uw^2}}{U_x^3} \times 10^5$ www bar $\frac{vw^2}{U_x^2} \times 10^5$ www.bar $\frac{\overline{uvw}}{U_{x}^{2}}$ x 10⁵ uvw bar

Symmetric Flat Plate Wake Data (x = 177.8) using IIHR probe

Y	u/U _{inf}	uu _{bar}	vv _{bar}	wwbar	uvbar	vw _{bar} i	Wbar
9.62	.81	6.273	6.460	3.476	+10.879	-14.358	-7.370
5.81	.76	6.219	6.764	3.755	10.091	-13.694	-9.821
2.00	.72	5.381	6.709	.317	5.551	-6.361 -	15.538
.73	.709	5.098	6.422	4.713	4.056	-1.497 -	17.972
54	.710	4.933	6.009	5.075	-2.966	+4.693 -	17.587
-1.30	.711	5.131	5.758	5.349	-4.775	6.742 -	17.594
2.06	.714	5.292	5.645	5.613	-7.217	9.636 -	17.105
2.32	.717	5.530	5.572	5.724	-12.607	10.014 -	15.674
4.09	.729	5.799	5.084	5.873	-12.315	12.802 -	14.390
5.36	.742	5.086	4.965	5.926	-15.098	14.263 -	13.412
7.90	.769	6.409	4.931	5.829	-15.113	14.137 -	11.317
12.98	.839	6.259	4.819	5.279	-13.286	12.468	-9.424
18.06	.882	5.397	4.504	4.570	-9.857	8.262	-6.942
23.84	.930	4.648	3.660	3.646	-6.184	5.515	-4.753
33.0	.982	2.199	2.063	1.837	-1.058	1.273	-2.113
48.24	1.00	.477	.792	.603	002	.099	339

TAB	LE	A2
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Airfoil Boundary Layer Data at x/L = -.220 (central plane)

RUN # 4 DATE OF RUN 1981 Urefernce (m/s) = 21.84 X loca.= -.220 Unfinity (m/s) = 23.19 Integral Parameters Pelta*sub x = .4776659E-02 Delta*sub z = .3158540E-01 Theta sub x = .3417375E-02 Theta sub x = .3417375E-02 Theta sub z = .6247743E-03 Theta sub z = .1681640E-03 Shape Factor H = 1.398

Boundary Layer Profile

Y MM.	u/Uinf	Gama	w/Uinf	Beta	Pstatic
1111225346789498642 1111225346789498642 1111225346789498642	4025046898672505045400 4502357943898672594324400 55555559438986725948484800 555555946898000 1100	7871375000068781795650 31554432162063715100 0	7722335556419622689310 234444444449353221000000 00000000000000000000000000000	78713750096731795650 3444444433382115100 344444443338201100 35333333820110000	$\begin{array}{c} - & 0.016\\ 0.00423\\ 0.00421\\ 0.00022\\ 0.00019922\\ - & 0.02301455\\ - & 0.023014552\\ - & 0.0230145\\ - & 0.02301455\\ - & 0.02301455\\ - & 0.02301455\\ - & 0.02301455\\ - & 0.02301455\\ - & 0.02301455\\ - & 0.023014\\ - & 0.023014\\ - & 0.02301$

TABLE	A3
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Airfoil Boundary Layer Data at x/L = -.124 (central plane) RUN 4 1 DATE OF RUN 29381 . Urefernce (m/s) X loca.= -.124 21.71 = 22.61 Uinfinity (m/s) = Inteoral Parameters Delta*sub x = .6346047E-02 Delta*sub z = .7913063E-01 Theta sub x = .4398430E-02 Theta sub z = .7212564E-03 Theta sub xz = .7305337E-01 Theta sub zx = .2687818E-03 - ------ -Shape Factor H = 1.443Foundary Laver Profile u/Uinf w/Uinf Y MM. Gama Reta Pstatic 5273081455913993 12357023533884 112357023533884 1123533884 4.80 .035 0428 .416 48266 5566748 78876 6778876 890 0612 0635 66554324 10282324204385 0601 0520 0467 0407 0235 0173 034 - 002 - 005 - 003 991 997 0287 0214 998 1.000 0.00 0.000 .0145

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Airfoil Boundary Layer Data at x/L = - .124 (-6" plane) RUN # 2 DATE OF RUN 29881 Urefernce (m/s) X loca.= −.124 = 21.84 Uinfinity (M/s) = 22.66Integral Parameters Delta*sub x = .5580028E-02 Delta*sub z = .4887007E-01 Theta sub x = .3946812E-02 Theta sub z = .9489292E-03 Theta sub xz = .4355173E-01 Theta sub zx = .2616808E-03 Shape Factor H = 1.414Boundary Layer Profile Beta Petatic w/Uinf Gama Y MM. v/Uinf .033 .047 .055 34.35 35.61 36.06 .0369 4.35 5.61 6.06 1123458138314582 112345813831458318 112335358314558318 112333583138318 112333 435 .0425 0459 0465 058 .061 0412 061 .609 .646 .057 673 732 779 0355 .050 0294 044 036 831 908 0093 971 30 06 29 98 30 00 - 0006 - 0002 - 0019 001 998 1.001 0.000 46.48

Airfoil Boundary Layer Data at x/L = -.124 (+6" plane) RUN # 3 DATE OF RUN 2988i Urefernce (m/s) X loca.= -.124 21.84 = X loca.= Uinfinitv (m/s) = 22.65 Integral Parameters Delta*sub x = .5613346E-02 Delta*sub z = .4455488E-01 Theta sub x = .3972160E-02 Theta sub z = .8642757E-03Theta sub xz = .3918079E-01Thata sub zx = .2392422E-03Shape Factor H = 1.413 Boundary Layer Profile Y mm. w/Uinf Beta Pstatic v/Uinf Gama 35.36 35.58 35.91 039 1560 1111234568071567272 111123456803595962 111123456803595962 418 045 460 .1640 1000 520 . 053 . 548 .056 1560 1250 -671 -671 -775 -776 4.46 1450 197 4.197 3.6889 1.6889 1.600 1.600 051 . 1560 1450 1380 1280 825 1260 1260 1200 1160 025 854 49 263 997 008 002 . <u>i 0</u>01 000 1130 02 03 _ ; <u>1</u>.000 ---

Airfoil Roundary Layer Data at x/L = -.014 (far side)

RUN #5DATE OF RUN1981Urefernce (M/s)=X loca.=-.014Uinfinity (M/s)=22.23Integral ParametersDelta*sub x =.7026738E-02Delta*sub z =.5247342E-01Theta sub x =.4873316E-02Theta sub x =.4601236E-01Theta sub z =.4601236E-01Theta sub z =.5658745E-03Shape Factor H =1.442

Roundary Layer Profile

Y MM.	u∕Uinf	Gama	w/Uinf	Beta	Pstatic
16272834566803604208680 11111223545680250011117233445180 1111122353456802500530 11112235456802505500530	999577341034778221588899990 1.03555555555555555555555555555555555555	235531342233656267039710 65520948233656267039710 02220948233656267039710 02220948233656267039710 0	107 109 110 110 110 110 105 106 106 106 106 106 106 106 106 106 106	23631342233656267039710 655221100009076542100000 222221100009076542100000 444444443333333333333333333	58980094368104892547946 2222202202020202101920960211 22222022020202021019209602011 22222022020202021019209600011 222220202020202021111111111111111



Airfoil Boundary Layer Data at x/L = -.014 (near side) RUN # 6 DATE OF RUN 1981 Urefernce (m/s) X loca.= -.014 21.84 = Uinfinity (m/s) 22.07 Ξ Integral Parameters Delta*sub x = .7871451E-02Delta*sub z = .4484870E-01Theta sub x = .5212710E-02Theta sub z = .5540243E-02Theta sub xz = .4255312E-01Theta sub zx = .5575653E-02Shape Factor H = 1.510Boundary Laver Profile Y mm. u/Uinf Gama w/Uinf Beta Pstatic 010030405000 560945950045 44445555550045 1411003456000500 1111003456005000 111100355600 1110055000 38500584202767 28041508804767 2111110000008765 .098 42.23 41.88 41.25 .098 096 .097 096 .095 .093 . ŏ9ŏ . 087 . 636 . 538 . 568 . 758 . 758 . 797 . 8728 . 9778 . 97788 . 977888 . 97788 . 97788 . 977888 . 97788 082 1951 4.86 3.90 2.25 1.02 1832 . 064 054 .1.000 1649 034 30 41 1394 41 988 .0(14 43 43 51 05 58 67 02 30.07 30.02 30.00 997 .001 **9**00 000

0.000

0.00

1.000

100

.1065

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Airfoil Wake Data at x/L = .014 (central plane)

RUN # 7 DATE OF RUN 2981 Urefernce (M/s) = 21.84 X loca.= .140 Uinfinity (M/s) = 22.17 Integral Parameters Delta*sub x = .1640730E-01 Delta*sub z = .1054121E+00 Theta sub x = .1085906E-01 Theta sub z = .4158555E-02 Theta sub zx = .1375550E-02 Shape Factor H = 1.511

Wake Profile

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Ύ ΜΜ.	u/Uinf	Gama	w/Uinf	Beta	Pstatic
46000004060000000000000000000000000000	11 0002041040548570002501030 000204104054175228644109858 000208888775528644109858 888775528644444444444444444444444444444444444	011508562256291010107540 1105463008406551491102340 111144141	02499040405740404097.5469 0000123455740404097.5469 000000000000000011000009 111000009	11008582854801710107810 01051488808481081710107810 02001108894474444444444 05855555555555555555555555555	565546309732592006218 11024562335331778894825 111111111111111111111111111111111111

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Wake Profile

Y MM.	u/Uinf	Gama	w/Uinf	Heta	Petatic
- 25	439	14.16	.111	44.16	.2154
76	445	14.15	112	44.15	2140
-1.27	. 465	13.32	110 116	43.34 43.86	2221
-i. <u>78</u>	469	13.86 12.82	114	42.82	.2180
-2,54 -3,30	. 5 23	12.25	114	42.22	.2200
-4.32	.554	11.29	111	41.22	2154 2157
-5.33	. 580	10.47	.107 .103	40,47 39,69	2161
-6.60	604	$\frac{9}{8}$, $\frac{69}{70}$	1097	38.70	2046
-7.87 -9.65	. 669	7.87	093	37.87	2025
-11 43	.703	6.82	082	36.82	.2071
-13.97	.747	5.24	075	$\frac{35}{34}$, $\frac{76}{23}$	2024
-17.78	. 810	4,23 2,91	.060	32.51	1856
-21.59 -26.67	.869 1936	1.57	026	31.57	.1673
-31.75	976	.89	015	30.87	.1545
-39.37	.991	. 41	.007	30.41	1408
-46.99	1.000	0.00	002	30.12 30.00	1205
-54.61	1.000	0.00	0.000	and the second	·

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Airfoil Wake Data at x/L = .027 (central plane)

TABLE A10

Airfoil Wake Data at x/L = .027 (-6" plane)

RUN $\ddagger 9$ DATE OF RUN 3981 Urefernce (m/s) = 21.84 X loca.= .027 Uinfinity (m/s) = 21.94 Integral Parameters Delta%sub x = .1524869E-01 Delta%sub z = .1011579E+00 Theta sub x = .1042631E-01 Theta sub x = .1042631E-01 Theta sub xz = .8805762E-02 Theta sub xz = .1130750E-02 Shape Factor H = 1.463 Wake Profile

Y MM.	u∕Uinf	Gama	w/Uinf	Beta	Pstatic
2086462840259268620-63159791 543221111864321 01125079270975 114681631864321 01125079270975	1 00997700517389296060649934258663470 009977005177175530240246149320790 0099770051774755302402461493200790 1 00997700517389209606499954258663470	0464709874380899761965321 012627666689958246831584452165 01345676889900000008765321	002515220858702479201289025918 00001356778888999990012899025918 0008999999001109877531918 000899999001109877531918 0008000001109877531918 00000000110989025918	04647098743808997649657393124 00990234567889699764968745824 331 5888858899760000087455824 5888588899760000087455824 588585858555555555555555555555555	1333744480 1119993931103975222439900 11199993002229485501266664375 119999300000011266664375 11999002222000011266664375 119990022222222222222222222222222222222

TABLE A	1	1	
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Airfoil Wake Data at x/L = .027 (+6" plane)

RUN # 10 DATE OF RUN 3981 Urefernce (m/s) = 21.84 X loca.= .027 Uinfinity (m/s) = 22.15 Integral Parameters Delta*sub x = .1577514E-01 Delta*sub z = .1282676E+00 Theta sub x = .1068428E-01 Theta sub x = .1068428E-01Theta sub x = .1068428E-01Shape Factor H = 1.476

_ Wake Profile

Y MM.	u/Uinf	Gama	w/Uinf	Beta	Pstatic
64208680624653221068520453135791 93714877168000505077031645628407 05588027207545211 011346827207530 111111111111111111111111111111111111	10840476321093703903394448499411500 111098602405464221011224715208596900 111098602405464221011224715208596900 1109860047632000 1109860047632000 1109860047632000 1109860047632000 1109860047632000 1109860047632000 1109860047632000 1109860047632000 110986004763200 1109860047632000 110986004763200 110986004763200 110986004763200 100000 1000000 1000000 1000000	1 1 <td></td> <td>29776984782111947321429909358450 999900104597889999900098000000 999900104597888999900098000000 9999001045978889999900000000000000000000000000000</td> <td>11075135175470817580182860564909 112246912510455478786482860564909 111146920012222222222222222222222222222222222</td>		29776984782111947321429909358450 999900104597889999900098000000 999900104597888999900098000000 9999001045978889999900000000000000000000000000000	11075135175470817580182860564909 112246912510455478786482860564909 111146920012222222222222222222222222222222222

Airfoil Wake Data at x/L = .041 (central plane)

RUN \ddagger 11 DATE OF RUN 3981 Urefernce (m/s) = 21.84 X loca.= .041 Uinfinity (m/s) = 22.23 Integral Parameters Delta \ddagger sub x = .1587362E-01 Delta \ddagger sub z = .1556493E+00 Theta sub x = .1118588E-01 Theta sub z = .4402381E-02 Theta sub zz = .1409030E+00 Theta sub zx = .1127246E-02 Shape Factor H = 1.419

Wake Profile

Y mm.	v∕Uinf	Gama	w/Uinf	Beta	Pstatic
765348264285210123693453809517 111235815074334564 111235815074334564	99548232697782899999999999999999999999999999999	- 01480 446841468063158064710039766680 1915818952337384956680 099999999999999995421	$\begin{array}{c} - & 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0$	23333333333435297668 94444148806315809999987542100397668 11581580647100339766680 1000000000000000000000000000000000	$\begin{array}{c} 112586358530\\ 112586455850\\ 112586455850\\ 112586455850\\ 112586455850\\ 11258645555\\ 11258555555\\ 11258555555\\ 112585555555\\ 11258555555\\ 11258555555\\ 11258555555\\ 11258555555\\ 1125855555\\ 1125855555\\ 1125855555\\ 1125855555\\ 1125855555\\ 1125855555\\ 112585555\\ 112585555\\ 112585555\\ 112585555\\ 112585555\\ 112585555\\ 1125855\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 11258555\\ 1125555\\ 1125555\\ 112555\\ 1125555\\ 1125555\\ 1125555\\ 11255$

Airfoil Wake Data at x/L = .055 (central plane)

RUN #12
DATE OF RUN3981Urefernce (m/s)
X loca.==21.84Unfinity (m/s)=21.84Unfinity (m/s)=22.14Integral ParametersDelta*sub x =.1459999E-01Delta*sub z =.1879447E+00Theta sub x =Theta sub z =.1045328E-01Theta sub xz =Theta sub z =.2475021E-02Theta sub xz =Theta sub z =.1742300E+00Theta sub zx =Shape Factor H =1.397

Wake Profile

Ymm.	u/Uinf	Gama	w/Uinf	8eta	Pstatic
3159378615217420122460468406280 376543294074210 11246863444446 1234569 1234569 1234569	1.002 1.000 9992 9996899 9996815266279555555555555555555555555555555555	48800010565589265311438310296797 43210279256558926531143839310296797		622001066558926211439310296793 9999900134567888888807653100000 9999900134567888888807653100000 999990001345678888888807653100000 999990001345678888888807653100000 9999900013456788888888076531000000 9999900013456788888888076531000000000000000000000000000000000000	0961 12787380 122787380 12278735550 12278735550 12278735550 12278735550 12278735550 12278735550 12278735550 12278772664 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 1227875550 12278772664 12278772664 12278772664 12278772664 12278772664 12278772664 12278772664 1227875550 12278772664 12278772664 1227976655530 12278772664 1227976655530 122772664 1227976655530 122772664 1227976655530 122772664 1227976655530 122772664 12279766555530 122772664 12279766555530 122772664 12279766555530 122772664 122797766455530 122772664 1227977655550 12277267765555550 12277267765555550 1227726776555555555555555555555555555555

Turbulence Data

X/L Location = .055 Reference Velocity = 21.8 m/s

Wake Profile

Y 433.591 433.591 10853 -247.9247.9247.9247.9247.9247.9247.9247.9	Ubar 1.000 994 9952 8859 8859 740 6944 6944 6740 5779 6462 5779 6462 7793 8797 8707 8	Vbar00100224615833002182457787 0001-0002246158330021824577887 001158330021824577887 0066666666666666666666666666666666	Wb00312962856261622573447	14267 5444 5444 5444 5444 5444 5444 5444 5444 5444 5444 5444 5444 5444 5444 5444 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 546 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577 577	7737 7737 7737 7737 7737 7737 7737 773	870 1772 772 1772 1772 1772 1772 1772 1772 1772 1772 1657 1777 1777 1657 1777 16577 1657 1657 1657 1657 1657 1657 1657 1657 1
	909 962 992 995		. 024	5.335	5.190	5.314

Profile continued at X/L = .055

Y mm.	uvbar	uwbar	vwbar	uuubar_	vvvbar	wwwbar
43359 43359 115 115 115 115 115 115 115 1		i.053	34879145549347028745389487384 1 235545524129485745589487389 1 - 2111256555245524553894867389 1 - 1112555511 - 1 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	$\begin{array}{c} - & 002\\ 630\\ 9.611\\ 10.649\\ 11.487\\ 9.6253\\ -12596\\ -2531\\ -12596\\ -2537\\ -12596\\ -2537\\ -12596\\ -2536\\ -255\\ -2566\\ -25$.400 1.883 1.743 5.278 708 6.456 7.680	-4.075 -4.027 -4.627 -4.5240 -4.5240 -4.5240 -5.1420 -5.1420 -5.127 -14.527 -11.227 -12.1357 -12.13597 -12

.

Profile	continued	at X/L =	. 055	
Y mm.	uuvbar	uuwbar	vvubar	vvwbar
432211111 432211111 4332211111 4332211111 4332211111 4332211111 4332211111 4332211111 4332211111 4332211111 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 43322115 433251 433251 433251 433251 433251 433251 433251 433251 433251 433251 433251 433251 433251 433251 433251 433551 433551 433551 433551 433551 4355551 435551 435551 4355511 4355511 435551		0010439980 0218439980 -3233088880 -3211 -3211 -12384 -32110 -32110 -32110 -32110 -32110 -1100 -1110 -1110 -1110 -1100 -100 -1000 -1000 -10	$\begin{array}{c} - & 0.01\\ 0.0632\\ 1.32277534\\ 1.322775347169352\\ 1.651882332320\\ 1.651882332420\\ 1.633381755\\ 1.00\\ 1.4 \\ 2.4566654\\ 1.00\\ 1.$	004451 -132212121 -13222121 -13222121 -13222121 -1

Profile continued at X/L = .055

Y mm.	www.bar	wwvbar	uvwbar
432211111 33508530853 432211111 1111 1111 1111 11111 11111 11111 1111	-33320 = -33666571755732035531431 =	002 -1.834 -1.8874 -1.8879 -1.2887 -1.225869 -1.225869 -1.225869 -1.225869 -1.225869 -1.225869 -1.225869 -1.222234 -1.22234 -1.22234 -1.22234 -1.22234 -1.22234 -1.22234 -1.22234 -1.22234 -1.22244 -1.22244 -1.22244 -1.22244 -1.22244 -1.22244 -1.22	$\begin{array}{c} - & 0 \\ 0 \\ 0 \\ 1 \\ 5 \\ 8 \\ 5 \\ 8 \\ 5 \\ 8 \\ 5 \\ 8 \\ 5 \\ 5$

RUN # 13 DATE OF RUN 8931 Urefernce (m/s) X loca.= .138 = 21.84 Uinfinity (m/s) 22.10 = Integral Parameters x = .1171234E-01 z =.9371559E-01 x = .8880582E-02 Delta*sub x = Delta*sub z = Theta sub .2588599E-02 .8256759E-01 .5643530E-03 Theta sub z = Theta sub xz =Theta sub zx = Shape Factor H = 1.319Wake Profile Y MM. u/Uinf Gama w/Uinf Beta 4400024502640482642024 260472168505050612034024 4400205075528205050612034024 111122050 111122050 111122054 999 3307231388071914056 556188994912070666680 1120344515070666680 009 997 ĴŎŎŹ 663 252 010 020 028 896 829 82 041 756 716 685 056

566

650

668

996 1 000

0.00

Airfoil Wake Data at x/L = .138 (central plane)

.060

060

060 059

026

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0.000

Pstatic

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1044

Turbulence Data

X/L Location = _138 Reference Velocity = 21.8 m/s

Wake Profile

Y 4322111111863100748260482080 Y 432210594838202506172273441	Ubar 007 1 997625 977325328556888154877644680 9999 8805568815487764680 9999 9999 9999 9999	V	H H H H H H H H	ubar 24667777765556777776642 24667777765556777776642 24667777765556777776642 237	v72777796674885926289315549 12455666748859266289315549 124743220126562789811	9068964683093433692044008 1346666764683097157495044008
-38.10	1.000	.035	- 092 - 011	.728 .521	1,119 .789	.828 .700

Profile continued at X/L = .138

Y mm.	uvbar	uwbar	vwbar	uuubar	vvvbar	wwwbar
43221351739517074824820802 46949631863101257025344172 111112057025085 1111112057025085	$\begin{array}{c} 69.263113619711378649903452120\\ -2.814680383 \\ -2.814680383 \\ -2.814680383 \\ -2.814680383 \\ -2.814680383 \\ -2.84100422952486847001\\ -2.814680383 \\ -2.8410042295526 \\ -2.8410004229229 \\ -2.8410004229229 \\ -2.8410004229229 \\ -2.8410004229229 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.841000422929 \\ -2.84100042929 \\ -2.84100042929 \\ -2.84100042929 \\ -2.84100042929 \\ -2.84100042929 \\ -2.8410004299 \\ -2.841000429 \\ -2.8410000429 \\ -2.8410000429 \\ -2.8410000429 \\ -2.841000000000000000 \\ -2.841000000000000000000000000000000000000$	$\begin{array}{c} \textbf{4544641545599405361557442290}\\ \textbf{1168216214621408300003}\\ \textbf{1168216214621408300003}\\ \textbf{1168216214621408300003}\\ \textbf{116821661463722}\\ \textbf{11685161463722}\\ \textbf{11685161463722}\\ \textbf{1168516161663551000}\\ \textbf{116851661663551000}\\ 11685166663551000000000000000000000000000000$		$\begin{array}{c} - & 003748848464724435994144897731\\ - & 1299225114 \\ - & 95643345994144887731\\ - & - & - & - & - & - & - & - & - & - $	9393935820324268547671034872 2 335981213 133341566611-	007011158124828397652283280046 - 25555512 21 - 2322121215642 - 1 - 1 - 1 - 2 - 2 - 1 - 232221215642 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1

1101220				
Y mm.	uuvbar	uuwbar	vvubar	vvwbar
452211111 452211111 452211111 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		146803323734438920819611 02081825201681830766419700 1222111 112253058187900 1222111 1122550766419700	- 257442 - 257442 - 257442 - 257442 - 1369988433699850810 - 1111 - 111 - 1111 - 11111 - 1111	3855610 0299197813523220095955440 1113111122 1113664440700 111136644407000 111136644407000 111136644407000 111136644407000 1111366444070000 11113711 1111366444070000 11113711 1111366444070000 11113711 11113711 11113711 11113711 11113711 11113711 1111370000000000

Profile continued at X/L = .138

Profile continued at X/L =.138Y mm.wwwbarwwwbaruvwbar44.45-.002-.002-.00736.83.093-.176-.11529.212.186-.807-.30224.134.013-1.9475.07019.055.461-1.3168.47316.512.466-1.1566.85613.972.021.3016.35614.43.581.1888.1238.89-4.4501.3963.5246.355-4.4112.8694.6823.81-5.0932.704-.4261.27-5.440.310-3.2920.00-3.704.2433.171-1.254-4.778-1.8372.8486-5.08-6.139-2.0596.842-10.16-1.2031.012-1.012-12.703.1474.042-8.345-15.244.1693.455-8.901-17.785.5464.172-3.819-20.327.0902.998-6.711-25.404.5892.750-5.718-30.481.3975955-1.4322-38.10-.010.026-.032-45.72-.003.001-.0055

TABLE	A15
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 Ai	rfoil Wake Da	ta at x/L	= .225 (cen	tral plane)	
RUN # 1 DATE OF R	9 Un 8981				
Urefernce X loca.≕	(m/s) = .275	21.84			
Uinfinity	(m/s) =	22.31			
Integral	Parameters				
Delta*sub Delta*sub Theta sub	x = .10500 z =.817213 x = .83465	85E-01 1E-01 99E-02			
Theta sub Theta sub Theta sub	z = .22191 xz = .7163 zx = .4141	80E-02 467E-01 984E-03			
Shape Fac	tor $H = 1.2$	58			
Wake Prof:	ile		·		
Ymm.	v∕Uinf	Gama	w∕Uinf	Beta	Pstatic
380250748231687 3802504520748231687 1063210748231687 10125716209 11114239	1 000 982 9349 7555 77522 7755 7755 7755 7755 7755 77	7916660269810580960 68440588888864071190 12353333555559241 0	01133627 0234479 002344799 0044999 0044493319 0000 0000 0000 0000	7916669269810390960 33333333333333333333333333333333	0884974 0984974 09951207776 100307776 1005530583 1005530583 09972127 098879 08879

Turbulence Data

X/L Location = .275 Reference Velocity = 21.8 m/s

Wake Profile

7157210628404826789177 54714062075202570871975235 1114062075202570871995 11140289177 11142289	Ubar 1 0002 9225559 9225559 774397728855997690 774397728855997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 7754655997690 77546559997690 77546559997690 77546559997690 775559997690 775559997690 775559997690 7755559997690 7755559997690 7755559997690 7755559997690 7755559997690 7755559997690 775555990 7755559997690 7755559997690 7755559997690 775555990 775555990 775555990 775555990 77555500 7755500 775500 7755000 7555000 7555000 7555000 7555000 75550000000000	Vb 0003652721169349870765	W000011027271548487876836	ar 09556911132823432534688420 0979056403334787800332547 0970033478780032547 0972246261166774	v6246813925154456688514 12456655556888969690 1245665555688899690 1245666555568889968914	160350778040947458828 1228175925189559254282 13556655925189559254282 1355665559254282 1355665559254282 1355665559254282 135566555555555555555555555555555555555
-49.53	. 998	.016	008	. 479	.756 -	. 756

Frofile continued at X/L = ...275

Y MM.	uvbar	uwbar	vwbar	uuubar	vvvbar	wwwbar
54113210628404826789173 211122999 1111212999 1111212999 1111212999 1111212999 1111111212999 1111111111111111111111111111111111	$\begin{array}{c} 0.0051327\\ -0.005527\\ -0.005727\\ -0.0$			$\begin{array}{c} 0.057\\ - 4.333426732509892534883760\\ - 4.3399187988925245889755071257889252458897755\\ - 7.655800 \\ - 7.655800 \\ - 7.6557000 \\ - 7.6555 \\ - 0.000 \\ - 0.000 $	- 122345 53124 - 64443 - 005299586476615 - 0029916002188316975856476615 - 00000000000000000000000000000000000	$\begin{array}{c} 003\\ -1.9248\\ -9248\\ -5.14661\\ -2.5119\\ -2.887262\\ -2.887262\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.887266\\ -2.88726\\ -2.887$

Profile continued at X/L =.275 uuwbar Y MM. uuvbar vvubar vvwbar - 009 - $\begin{array}{c} 0 & 000 \\ - & 0025 \\ - & 3055 \\ -1 & 1697 \\ -1 & 6964 \\ - & 20569 \\ 1 & 3099 \\ 1 & 2499 \\ 1 & 648 \\ 1 & 479 \end{array}$.004 .005 .318 1.843 -2.335 -1.317 -1.222 2īō . 11 Q 743 998 -5.349 705 1 479 2 413 -6.622 -4.165 -2.225 .028 7 . 65 -1.487 4.173 2.225 .186 4.052 8.201 5.813 2.214 .030 . 077 1.773 -1.496 3.869 6.736 5.501 2.270 .025 871 -3.246 -1 662 -2 744 -4.458 -3.393 -1.582 - 958 0.000 -.002 -.003

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Profile	continued	at X/L =	. 275
Ymm.	wwubar	wwvbar	uvwbar
541140620715205050826789173 971532106206404826789173 	446951114439720500000000000000000000000000000000000	$\begin{array}{c} 001\\ -& 017\\ -&$	- 0041 0007882704 47774 27272953884355555519 47774 27272953884355555519 473135555519 4131315719 4121171131 000

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Airfoil Wake Data at x/L = .399 (central plane)

RUN # 14 DATE OF RUN 3981 Urefernce (M/s) = 21.84 X loca.: .399 Uinfinity (M/s) = 22.26 Integr. Parameters Deita*sub x = .9478079E-02 Delta*sub z = .1359371E+00 Theta sub x = .7767224E-02 Anta sub z = .1267331E+00 Theta sub zx = .2740450E-03 Shape Factor H = 1.220

Wake Profile

.....

Ymm.	v∕Uinf	Gama	w/Uinf	Beta	Pstatic
64.77 544.237 544.237 544.2237 544.2237 6.207 136.207 136.257 1164.1797 1164.17917 1164.17917 1164.17917 152.252 152	1.006 1.004 9925 8775 759 761 77825 88754 9998 9998 1.000	21943372961727440810 12222961727440810 0	000267 0001333200320 00133333200100 0013333200100 00000 00000 0000000000	300 1337 2194 300 1337 200 1337 200 200 200 200 200 200 200 20	$\begin{array}{c} - & 0736 \\ - & 0748 \\ - & 0824 \\ - & 0824 \\ - & 00043 \\ - & 00043 \\ 00043 \\ - & 000425 \\ - & 000127 \\ - & 00250 \\ - & 00548 \\ - & 0548 \\ - & 06649 \\ - & 06$

Airfoil Wake Data at x/L = .66i (central plane) RUN # 15 DATE OF RUN 3981 Urefernce (m/s) X loca.= .661 = 21.84 Unifinity (m/s) = 22.31Integral Parameters Delta*sub x = .8675665E-02Delta*sub z = .1211335E+00Theta sub x = .7585780E-02Theta sub z = .2496901E-02Theta sub xz = .1125227E+00Theta sub zx = .2651202E-03Shape Factor H = 1.170

Wake Profile

Y mm.	u/Uinf	Gama	w/Uinf	Beta	Pstatic
3975539258147075371205762 261918765321013470385205762 111876532101347038521205762	$\begin{array}{c} 1 & 008\\ 1 & 008\\ 971\\ 9837\\ 8837\\ 8826\\ 8816\\ 8807\\ 8807\\ 8807\\ 8807\\ 8807\\ 8805\\ 8801\\ 8801\\ 881229\\ 8805$	202107029289710753156460 7708234444444444321921746	327834445456544421969384 000000000000000000000000000000000000	202197029289710753156460 5353333335553353333555355156460 53533333555535535555156460	

Turbulence Data

X/L Location = .661 Reference Velocity = 21.8 m/s

Wake Profile

Y m 53.34 433.19 33.086 15.22 22.54 -27.56 -17.78 -27.56 -17.78 -27.56 -17.78 -27.56 -35.18 -43.80	Ubar 1.000 9965 903 847 8090 793 847 875 847 875 908 972 981 972 981 972 982	Vbar 003 001 -000 -001 -007 007 007 007 015 015 015 015 015 015 015 009 009	Wbar - 001 000 0008 014 0227 0229 0229 0229 0220 0220 0220 0220 0220 0220 0220 0220 0220 0220 023 000 - 000 002 0220 000 000 000 000 000	upai 1.5760 1.5760 1.5760 1.5760 1.5760 1.5760 1.6022 1.6022 1.55577 1.555777 1.555777 1.555777 1.555777 1.555777 1.555777 1.555777 1.555777 1.5557777 1.5557777 1.5557777777777	r vvba 974 1 783 3 460 466 466 466 466 466 466 466 466 466	wwbar 795 1.550 3.385 4.909 4.656 4.461 4.561 4.561 4.561 4.561 5.013 5.013 5.013 5.013 5.013 5.013 5.013 5.013 5.013 5.008 4.659 3.808 1.203 5.08
Pr01110	CONTINU	ed at X∕	L00	T		
Ymm.	uvbar	uwbar	vwbar	uuubar	vvvbar	wwwbar
31826424420 310826555677864680 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -11227555568 -1122755568 -11227555568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -11227555568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -112275568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -1122755568 -11227568 -11257568 -1125568 -11257568 -1125568 -1125568 -1125568 -11256	$\begin{array}{c} - & 0.027\\ - & 5.0848334429\\ - & 5.0848334429\\ - & 5.08482840\\ - & 7.1334441056440\\ 10511324988748460\\ 1051132498874860\\ 105113249887886\\ 105113249887886\\ 10511324988660\\ 10511324988660\\ 10511324988660\\ 10511324988660\\ 10511324988660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 1051132498660\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 10511266666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 10511266666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 105112666666\\ 105112666666\\ 105112666666\\ 10511266666\\ 10511266666\\ 10511266666\\ 105112666666\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 10511266666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 1051126666\\ 1051126666\\ 10511266666\\ 10511266666\\ 10511266666\\ 10511266666\\ 105112666666666\\ 105112666666666666\\ 105112666666666666\\ 105112666666666666666\\ 1051006666666666666$	$\begin{array}{c} 012\\ 133\\ 1 & 370\\ - & 453\\ -1 & 279\\ -1 & 5716\\ -278\\ -1 & 279\\ -1 & 5716\\ -24 & 0271\\ -4 & 0271\\ -4 & 028\\ -2 & 028\\ -2 & 028\\ - & 028\end{array}$	- 05177363552223601 2986355223601 11122023486605	$\begin{array}{c} - & 008\\ & 005531\\ & 005531\\ & 005584530\\ & -43584530\\ & -4357515\\ & -435751\\ & -24\\ & -357510\\ & -3575$	$\begin{array}{c} 011\\ 277\\ 1 & 358\\ 3458\\ 1 & 646\\ 8033\\ - & 2097\\ - & 3369\\ - & 2097\\ - & 3369\\ - & 29988\\ - & 29988\\ - & 014\\ \end{array}$	$\begin{array}{c} - & 070 \\ -1 & 054 \\ -4 & 095 \\ -6 & 974 \\ -1 & 893 \\ - & 0006 \\ -1 & 2621 \\ 1 & 257 \\ 2 & 347 \\ 4 & 557 \\ 3 & 573 \\ 3 & 573 \\ 3 & 836 \\ 204 \end{array}$

Profile continued at X/L = .661

Ymm.	vuvbar	uuwbar	vvubar	vvwbar
310826424420864680 31082655677885518 3333257227272785518 -+11223450	$\begin{array}{c} - 012 \\ - 0586 \\ - 22 \\ - 22 \\ - 3508 \\ 1 \\ - 22 \\ - 3508 \\ 1 \\ - 22 \\ - 2 \\ $	$\begin{array}{c} - & 0.03 \\ - & 0.037 \\ - & 6886 \\ - & 518 \\ & 114 \\ & 341 \\ & 5177 \\ & 6874 \\ - & 7025 \\ -1 & 0.018 \\ - & 0.18 \end{array}$	010 575 3 647 4 3461 -2 1666 -4 330 -2 1662 -4 330 -2 1662 4 782 7824 4 784 4 22 397 141	$\begin{array}{r} - 013\\ - 1492\\ -1 5209\\ -1 5209\\ - 257\\ - 257\\ - 257\\ - 28254\\ -12254\\ -12256\\ - 12256\\ - 12256\\ - 12256\\ - 1256\\ - 1256\\ - 1019\\ - 1009\\ - 100$

Profile continued at X/L = .661

Y mm.	wwwbar	wwvbar	uvwbar
555225722725530 - 112235530 - 11223530 - 11223530	$\begin{array}{c} - & 0.01\\ 0.0856\\ 2.00281\\ -150468\\ -11.5549\\ -11.554982\\ -11.554982\\ -11.554982\\ -11.554982\\ -12.55482\\ -12.55682\\ -$	- 01324334580 01324534580 01324552280 01324552280 01324552280 01324552280 01324552280 013245280 014555280 0145550 014550 014550000000000	02156 02156 02156 02156 02156 02156 02156 0255 0256 0255 0256 0255 0256 0255 0256 0255 0255

Airfoil Wake Data at x/L = .661 (+6" plane)

RUN # 16 DATE OF RUN 4981 Urefernce (m/s) X loca.= .661 21.84 = 661 22.50 Uinfinity (m/s) = Integral Parameters Delta*sub x = .8693721E-02 Delta*sub z =.9094906E-01 Theta sub x = .7425145E-02Theta sub z = .2110851E-02Theta sub xz = .8250125E-01Theta sub zx = .2459053E-03Shape Factor H = 1.171Wake Profile Y mm. v/Uinf Gama w/Uinf Beta 1.007 1.000 .252 4387022814770747153809 438702217532102551467075 101247941807 101247941807 101247941807 101247941807 42504747467909014679 9259-0202733313101014679 .015 016 024 915 .861 .833 <u>.</u>818 032 032 812 033 033 033 031 033 800 .814 . 81.0 -816 -822 -829 031 032 030 854 ŎŽĒ . 888 024

. 44

016 172

941

1.000

126

Pstatic

.0425

0409

0334

.0359

.0376

. 0399

. 0396

0445

0184 0229

.0037

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Airfoil Wake Data at x/L = .661 (-6" plane)

RUN #17
DATE OF RUN4981Urefernce (m/s)=21.84X loca.=.661Uinfinity (m/s)=23.04Integral ParametersDelta*sub x=.8813884E-02Delta*sub z=1470653E+00Theta sub z=.7528187E-02Theta sub z=.1384450E+00Theta sub zx=.1384450E+00Theta sub zx=.1375721E-03Shape Factor H=1.171

Wake Profile

Y mm.	v∕Uinf	Gama	w/Uinf	Beta	Pstatic
33715931392581470712316873 69764215486308520286458435 7444446187653210137162099 876543211 11123399 111123399 111123399 111123399 111123399 111123399 111123399 111123399 111123399 111123316873	$\begin{array}{c} 1 & 003 \\ 1 & 002 \\ 1 & 002 \\ 1 & 001 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 9776 \\ 98321 \\ 8812 \\ 8810 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 8805 \\ 9775 \\ 975 \\ 1 \\ 00 \\ 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0$	20142009579933514660318420 111111112211111111111111111111111111	457669847898997888663069200 00001122222222222222222222 00000100000000	201425095799335166660318480 254385110899999835166660318480 353355355555999335166660318480 3533553555559993353555555559923	02994 023374 023374 0223374 0223374 02224966 0024966 0024966 0033008994 0033008994 0033302007770 0033302007770 001221 0012319 0022199879



<u> Airfoil Wake Data at x/L = .992 (central plane)</u> RUN # 21 DATE OF RUN 10981 Urefernce (m/s) X loca.= .992 = 21.84 22.73 Uinfinitv (M/E) = Integral Parameters Delta*sub x = .8715063E-02 Delta*sub z = .1334729E+00 Theta sub x = .7656711E-02 Theta sub z = .1486612E-02 Theta sub zz = .1249248E+00 Theta sub zx = .1669065E-03 Shape Factor H = 1.138Wake Profile u/Uinf w/Uinf Y MM. Gama Beta Petatic 1.003 1.001 .995 .975 4739 48240802442086468 654557272272789518 655557272227272789518 11122341 008 007 007 .0496 .0510 .0478 . 0474 0525 0594 0623 011 1.01 1.37 1.57 1.69 016 021 024 928 .887 .865 86 0521 850 025 837 0646 836 024 . 0630 022 846 . 0614 86 . 0595 016 883 .0585 900 . 0529 937 0487 967 0467 **9**89 0443 0447 0447 . 002 - 005 - 172 998 - 29 -50.80 . 1.000 -58.42 .43

'AT	9LE	A21
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Airfoil Wake Data at x/L = 1.928 (central plane) RUN # 18 DATE OF RUN 4981 Urefernce (m/s) X loca.= 1.928 21.84 = Uinfinity (m/s) = 23.34 Integral Parameters Delta*sub x = .3185820E-02Delta*sub z = .1070817E+00Theta sub x = .2963738E-02Theta sub z = .3562933E-03 Theta sub xz = .1039173E+00 Theta sub zx = .2139227E-04 Shape Factor H = 1.075Wake Profile Y mm. u/Uinf Gama w/Uinf Beta Pstatic .899 .901 .907 .918 .930 .947 .947 .981 .981 75077509353 .012 0116 0.00 0372965557939 11234557939 008 0050 008 0029 . 0037 .0035 .001 1.001 0041 . 003 ŌŌ 1.000 .001

Turbulence Data

X/L Location = 1.928 Reference Velocity = 21.8 m/s

Half Wake Profile

Y 111223334556666	Ubar 9002 9002 90034 90034 9003 9003 9003 9003 9003 90	Vbar 00034 00034 00022 00022 00022 00022 00022 00022 00022 0001 0001 0001 0001 0001 0001 0001	Wb1567 001746554 001146554 00110987465550 00007465550 00007465550	00775386524440795499686032 0775334445565672531737286 077533555556795499686032	4444444433333221111	a 3566474651405346369340 35666677877654085209340 35666677877654085209340 40839920940
86.36			000	. 622	.930	. 840

Profile continued at X/L = 1.928

Y MM.	uvbar	uwbar	vwbar	uuubar	vvvbar	wwwbar
58404826086420802408 6505050647789011184023 117278788308664208 11727878830866640 1172787883086666408	89018203267293191928884 	4967792908873942177992 194213470226884088555521 1942134788493207855521 1111	P0209876505622044143		952261859271064217766176 95226182977036824852201 11 1	99559927360972997753 313493042848606599525 313493075741844609220 1 1 1 1 1 1 1 2 3220 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1

Profile continued at X/L = 1.928

Y MM.	uuvbar	ouwbar	vvubar	vvwbar
584048260864208001406 		643645075083296524494 004163550006626585959000 1	-11.5424 85424 854324 6632684 854336884 11.11.11 11.11	2311101257878585888888 434122235788585858888888

Profile continued at X/L = 1.928

Y mm.	wwwbar	wwvbar	uvwban
	$\begin{array}{c} - 036\\ 062\\ - 228\\ 061\\ 147\\ - 235\\ 114\\ 135\\ 2429\\ 650\\ 1 008\\ 828\\ 1 020\\ 896\\ 693\\ 403\\ 071\\ - 019\\ - 002\end{array}$	$\begin{array}{c} - 104 \\ - 089 \\ 103 \\ 1328 \\ - 2253 \\ - 2253 \\ - 2253 \\ - 2253 \\ - 511 \\ - 689 \\ - 557 \\ - 557 \\ - 354 \\ - 089 \\ - 354 \\ - 015 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$