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## COMPARISON OF MODERN ICING CLOUD INSTRUMENTS

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## CONTENTS

Page

1. INTRODUCTION ..... 1
2. IRT INSTRUMENTATION AND DESCRIPTIONS ..... 3
Axially Scattering Spectrometer Probe (AASSO-100) and Forward Scattering Spectrometer Probe (FSSP-100) ..... 6
Optical Array Cloud Particle Spectrometer Probe (OAP-200X) ..... 11
Leigh Ice Detector Set ..... 14
Johnson-Williams (J-W) Liquid Water Content Indicator ..... 16
Rosemount Model 102 Total Temperature Sensor ..... 17
Dew Point Hygrometers (E.G. \& G. Model 137-C3 and General Eastern Model 1011) ..... 18
3. DATA SET DESCRIPTION ..... 20
Data Recovery Percentages ..... 20
Tunnel Settings ..... 24
Data Selection ..... 25
Data Reduction Procedures ..... 28
Data Volume Description ..... 32
4. RESULTS AND DISCUSSION ..... 37
IRT Cloud Repeatability ..... 37
IRT Cloud Uniformity ..... 43
Effect of Steam Tube Wraps ..... 49
Effects of Temperature and Velocity on Probe Performance ..... 53
Instrument Intercomparisons ..... 55
Drop Size Distribution Form ..... 80
5. CONCLUSIONS ..... 104
6. RECOMMENDATIONS ..... 106
7. REFERENCES ..... 107
APPENDIX A TEST POINT SUMMARY ..... 108

## INTRODUCTION

During January 1981 the U.S. Air Force (USAF) Flight Test. Center (AFFTC) at Edwards Air Force Base, California, conducted a test program at the NASA Lewis Research Center (LeRC) Icing Research Tunnel (IRT) aimed at documenting and improving the performance of the USAF A-10 inlet Icing Protection System. While inlet testing was the primary objective, the testing period and schedule provided a unique opportunity for additional icing instrumentation studies. These additional studies were focused on comparisons between modern state-ofthe-art droplet/icing measurement systems and those systems and techniques aiready in use for some years. In addition, documentation and investigation of the characteristics of the IRT itself could be accomplished with both types of systems.

These studies were beyond the scope of interest to the USAF A-10 group. However, they were of vital interest to NASA, FAA, the U.S. Army and Air Force and indeed to the entire icing and cloud physics community. In August 1981, MRI was awarded a contract (NAS3-22760) from NASA LeRC to perform the analyses of the data obtained during USAF test program in January. The primary objectives of the contract were to provide the following:

- Descriptions of the "modern" icing instrumentation
installed in the IRT.
- Data listings for each tunnel test condition.
- Analyses of the data including information investi-
gations into:

1. $\quad$| The repeatability of the tunnel and tunnel |
| :--- |
| uniformity, |
2. | Instrument comparisons with other instruments |
| :--- |
| and comparison of tunnel droplet spectra |
| with natural cloud conditions, and |
3. | Velocity effects on spectrometers and temper- |
| :--- |
| ature effects on accretion instruments. |

This final report serves to accommodate these objectives in fulfillment of the report requirements of the contract. Section 2 presents descriptions of the instruments in addition to the instrumentation setup in the IRT. Documentation of the data reduction procedures for the data listings which are presented in a separate data volume is given in Section 3. Data recovery information and problems encountered during testing are also discussed. The results of the analyses are presented in Section 4 with conclusions and recommendations following in Section 5.

Figure 2-1 presents a schematic of the instrumented IRT. In addition to the instruments for recording of tunnel air speed, air temperature, and dew point temperature, the test section was equipped with a specially fabri" cated test stand for mounting of the cloud droplet instrumentation. The test stand was equipped with a Johnson and Williams hot wire device and a Leigh ice detection meter and was capable of mounting two of the Particle Measurement Systems, Inc. (PMS) cloud particle spectrometers as shown in Figure 2-2. The PMS probes tested incleded four Axially Scattering Spectrometer Probes (ASSP), two Forward Scattering Spectrometer Probes (FSSP), and two Cloud Particle Spectrometers (CPS). Probes belong to the following organizations were used in the IRT:

$$
\begin{aligned}
& \text { U.S. Air Force Geophysical Laboratory (AFGL). } \\
& \text { Meteorology Research, Inc. (MRI). } \\
& \text { Particle Measurement Systems, Inc. (PMS) (leased by MRI). } \\
& \text { Leigh Instruments, Limited. }
\end{aligned}
$$

The FSSP's and CPS's were interchanged at the location shown for the CPS in Figure 2\&2. The ASSP's were always mounted as shown in the figure. Data were recorded unto digital tape at a rate of once per second.

Since the heaters provided with the PMS probes were not able to de-ice the probes adequately at the cold temperatures, the PMS probes were wrapped with steam tubes. Special tests revealed that the steam tubes did not alter the air flow through the probes' sample tubes. Also, for given test conditions, near identical estimates of the cloud properties were detemined from the measurements with and without the steam rube wrappings as will be discussed in a later section.

The following subsections present descriptions of the probes installed on the test stand.
Figure 2-1. TOP VIEW OF IRT SHOWING INSTRUMENT LOCATIONS

fRONT VIEW

78-515s

78.5150

Figure 2-2. INSTRUMENTED TEST STAND ASSEMBLY

### 2.1 Axially Scattering Spectrometer Probe (ASSP-100) and Forward Scattering Spectrometer Probe (FSSP-100)

The Particle Measurement Systems, Inc. (PMS) ASSP-100 is a droplet sizing device devel oped in the early 1970's. Droplet sizes are estimated on a particle-by-particle basis from measurements of the amount of forward scattered light as droplets pass through a focused laser beain. Figure 2-3 presents a block diagram of the optical system. Particles intercepting the laser beam scatter light through the optics. The scattered light is received at a beamsplitting prism where one half of the beam is deflected $90^{\circ}$ and focused onto a detector (annular) which is masked at the center while the other half is focused onto an unmasked (or signal) detector.

Since the intensity of light scattered from a given size droplet is a function of its position within the focused beam, it is necessary to establish if the particle is contained within the desired depth-of-field and if the particle passes through the central part of the beam where the intensity is uniform. The depth-of.afield is defined as that region along the beam axis where the signal received by the unmasked detector exceeds that of the masked detector by a factor of 2.5. A droplet is rejected if the pulse pair comparisons indicate a smaller value. The transient time (or pulse width) of the particle as it passes through the laser beam is analyzed to determine its chordal transect through the beam. Particle transit times are measured and compared with a stored running mean of approximately 1,000 accepted pulse widths. Pulses exhibiting transient times greater than the average are accepted. This edge effect discrimination is performed to eliminate undersizing of particles as they pass through the outer and weaker intensity regions of the beam and is based upon the decrease in chordal transit distances from the center through the edge of the beam.

For a particle accepted as being within the depth-of-field and in the central region of the beam, the peak intensity is measured by a pulse height analyzer to determine particle size. Since Mie theory for spherical particles indicates that scattering intensity is near proportional to the square of particle size, the signal from the pulse height analyzer is gated to provide a count in one of 15 equally spaced size channels by a series of voltage comparators having square weighted voltage thresholds.

 ASSP

Each particie sized and counted by the ASSP causes a latch to be set and inhibits the measurement of other particles for a period of $4 \mu s$. This finite time period insures sufficient time for quantification and transfer of information without interference from subsequent particles entering the sampling aperature.

The FSSP was designed and built as an improved successor to the ISSP. The modifications included refinements to its optical and electronic subsystems rather than in basic operating principles. As compared to the ASSP, the FSSP analyzes light scattered at wider angles of $4-18^{\circ}$ as opposed to the $7-16^{\circ}$ in the ASSP. The FSSP also generally has a shallower deptif of field which results in sharper size discrimination and a smaller sampling area. The physical construction of the FSSP is also different as shown in the block diagram of the optical system in Figure 2-4.

Both probes are capable of sizing particles from 0.5 to 47 microns diameter in four size ranges ( $2=47 \mu \mathrm{~m}, 2-32 \mu \mathrm{~m}, 1-16 \mu \mathrm{~m}$, and $0.5-8 \mu \mathrm{~m}$ ) and resolves them into 15 equally spaced size intervals. They are also normally designed for airborne sampling velocities of 20 to $125 \mathrm{~m} / \mathrm{sec}$ ( $\sim 250 \mathrm{kts}$ ) and can be modified for use at lower or higher velocities. For measurements conducted at higher speeds, pulse height distortion leads to under estimation of particle size. The characteristics of the ASSP and FSSP are summarized in Tables 2.* and 2-2. As an option, the total number of pulses or strobes sensed through the beam width and within the depth-of-field can be recorded. Hence, an acceptance ratio (or efficiency) based on the total particle counts in the 15 size channels and total strobes provides a more accurate value for the effective beam diameter. Eariy versinns of the ASSP did not have this velocity reject feature and, therefore, assumed an effective diameter of approximately one half the beam width.

Another option on probe activity serves to provide information on possible errors in the counting efficiency of the probes. Since particles which are sensed as entering the beam (outside as well as within the depth of field) require finite time perfods in the acceptance/rejection logic, they are also counted and processed to provide outputs on probe activity from which the "busyness" of the probe is inferred. High (as opposed to low) activity indicates that a large (small) portion of the particles entering within the effective sampling area (effective beam width $x$ depth of fleld)
ORIENAL PBEE: :
OF POOR QUALTY


Table 2-1

## AXIALLY SCATTERING SPECTROMETER PROEE CHARACTERISTICS

Number of size channels ..... 15
Size range
3 to 45 microns
Size resolution
3 microns
Maximum particle rate
100 k Hz
Coincidence errors
Less than $10 \%$ with concentrations of $10^{3} \mathrm{~cm}^{-3}$
Maximum particle velocity
$125 \mathrm{~m} / \mathrm{sec}$
Power
$115 \mathrm{v}, 60 \mathrm{~Hz}, 1.0 \mathrm{amp}$ plus required de-icepower ( 300 W using 28 v heaters)
EnvironmentalTemperature: $-40^{\circ} \mathrm{C}$ to $+40^{\circ} \mathrm{C}$Altitude: 0 to $40,000 \mathrm{ft} \mathrm{msl}$
Mechanical
Probe: 24-inch long airfoil
Weight
Probe: approximately 6 ..... 6 lb
Table 2-2
FORWARD SCATTERING SPECTROMETER PROBE CHARACTERISTICS
Number of size channels ..... 15
Size range
Size resolution
3 to 45 microns
Maximum particle rate
3 microns
100 k Hz
Coincidence errors
Less than $10 \%$ with concentrations of $10^{3} \mathrm{~cm}^{-3}$
Maximum particle velocity
Power
Environmental
Mechanical
$125 \mathrm{~m} \mathrm{sec}^{-1}$
$115 \mathrm{v}, 60 \mathrm{~Hz}, 1.0$ a plus required de-ice power( 300 W using 28 v heaters)
Temperature: $-40^{\circ} \mathrm{C}$ to $+40^{\circ} \mathrm{C}$
Altitude: 0 to $40,000 \mathrm{ft} \mathrm{msl}$
Weight
Probe: 34-inch long, 7 -inch diameter cylinder
Probe: approximately 45 lb
would not be processed since a large (small) fraction of a given time period is lost in rejecting particles. Laboratory experiments at PMS show that the counting efficiency (probe count/true count) decreases exponenthaly from a value of 1 starting at an activity of about 40 percent to approximately 0.6 as activity increases to 80 percent. Hence bulk parameters such as liquid water content (LWC) and total number concentrations are usually underestimated at the higher activities. This type of coincidence error is thought not to affect the resulting size distribution shape or form from which medium volume diameter (MVD) is estimated since it applies equally to all particles. Although PMS provides empirical correction factors from their laboratory tests, it is felt that since scattering intensity is dependent upon particle size, the corrections would not necessarily apply to clouds having different particle size distributions. This contention is partially verifier in Section 4 where LWC estimates from probes having this option are compared.

### 2.2 Optical Array Cloud Particle Spectrometer Probe (OAP-200X)

The Cloud Particle Spectrometer counts and sizes particles from 20 to $300 \mu \mathrm{~m}$ by imaging the shadow of each particle on a linear array of photodiodes as shown in Figure 2-5. A helium-neon laser (6238 ) is used with condensing and imaging optics to focus the shadow of a particle ly ng within the sample volume. The beam is vertical between sampling arms, and the focal plane is centered between the two sampling arms. The particle may shadow one or more of the photodiode elements. Each active element of the photodiode array contains its own amplifying and logic circuit (PC). If the shadowing of an element causes at least a 50 percent reduction in iight level to PC (this is an electronic truncation of depth of field and minimum size), a flip-fiop circuit is triggered. Two end photodiode elements are used in logic to reject particle shadows extending over the end of the active part of the photodiode array.

Information from each PC of the array is acquired by an accumulator. The particle is sized in the BMS by accumulating flip-flop information from the $P C$, and converting this inio a particle size. The unit particle size results from a determination of the number of elements set, the size of each array element, and the magnification of the optical system. Each second of particle information collected by the BMS is dumped in proper form for recording.
ORIGINAL PAGE IS OF POOR QUALITY.

Figure 2-5. CLOUD PARTICLE SPECTROMETER PROBE OPTICAL SYSTEM DIAGRAM

These probes are equipped to size into 15 equal size channels. There are two basic size ranges rurrently in use. The cloud probe range is 20 to $300 \mu \mathrm{~m}$, and the precipitation size range generally over 200 to $4500 \mu \mathrm{~m}$. In the precipitation size range, some models size 200 to $3000 \mu \mathrm{~m}$, and others 300 to $4500 \mu \mathrm{~m}$, each divided into 15 equal size channels. Detailed specifications of these probes taken from PMS handbooks appear in Table 2-3.

Table 2-3

## CLOUD PARTICLE SPECTROMETER CHARACTERISTICS

| Number of array elements | 24 |
| :--- | :--- |
| Number of size channels | 15 |
| Size range (basis system) | 20 to 300 microns |
| Maximum particle velocity | 250 knots |
| Maximum aperture | 6.5 cm |
| Power | $115 \mathrm{v}, 50$ to 400 or $60 \mathrm{~Hz}, 60 \mathrm{~W}$ |
|  | De-ice: 28 vDC 70 W |
| Dimensions | Cylinder: 18 in (length); $6-1 / 2$ in (diameter); |
|  | Optical Extensions (two): 20 in (length); |
|  | 1 in (diameter) |
| Weight | 45 lt |
| Environmental | Temperature: $-60^{\circ} \mathrm{C} \mathrm{to}+50^{\circ} \mathrm{C}$ |
|  | Humidity: $10 \%$ to $100 \%$ |
|  | Altitude: 0 to $40,000 \mathrm{ft} \mathrm{ms}$ |

Of importance to users of these probes is their sampling volumes. Knollenberg (1970) used glass beads and opaque discs of various diameters placed on glass slides to determine their shadow size and light intensity distribution in a parallel plane as a function of distance. Using coherent illumination, he found that at close distances, the particle was in sharp focus and all of the decrease in light intensity was measured to be in a distance equal to the particle diameter. One would expect this from basic optics (Stone, 1963) and for non-spherical solid articles one would expect that at close distances all of the decrease in light intensity would be in an area equivalent to the cross sectional area of the particle. At distances far from the particle diameter, the decrease in intensity was found to be
distributed over a much wider distance than the particle diameter. The depth of fleld DF for the measured shadow size to be within $\pm 10$ percent of the actual particle size, which corresponded to a 40 percent reduction in light intensity, was found in non-dimensional units to be $D F= \pm 3$. The detection threshold of a 50 percent reduction in light level before the cir* cuits are triggered was derived from this criteria. The depth of field in dimensional units as a function of particle radius $R$ and illumination wave. length $\lambda$ is therefore, $D F= \pm 3 R^{2} / \lambda$. For a He-Ne laser where $\lambda=0.6328 \mu \mathrm{~m}$, for a $200 \mu \mathrm{~m}$ diameter particle $\mathrm{DF}=9.4 \mathrm{~cm}$, and for a $1000 \lambda \mathrm{~m}$ diameter particle, $D F=948 \mathrm{~cm}$.

The sampling volume is the product of the depth of field, the effective array width (which is related to the width of the array minus the diameter of the particle) and the true air speed. If the depth of field for a given particle diameter is wider than the separation between sampling arms, then the deptin of field is equal to the arm width of 6.1 cm . This is true for the drops having diameters larger than $160 \mu \mathrm{~m}$.

### 2.3 Leigh Ice Detector Set

The Leigh Ice Detector Set (IDS) aspirator features an annular ejector nozzle which when powered by compressed air is used to entrain ambient air and thereby induce high-velocity air flow over the ice-collecting probe (Figure 2-6). The air flow is maintained relatively constant despite variations in the freestream velocity vector. Thus, the IDS is designed to continuously sample the air for supercooled liquid water.

The ice-collecting probe which is located crosswise in the ejector duct takes the form of a small-diameter thin-wall tube (Figure 2-7). It has an ice-collecting efficiency close to unity as calibrated in the Canadian National Research Council's icing tunnel. The thin-wall tube has sufficient resistance to serve as its own heater with no internal filament required. The thermal inertia of the probe is therefore very low. In response to heat generated by probe de-icing, the ice interface at the probe is melted and the ice is shed out the tallpipe of the duct. The photodetector senses restoration of the beam to full strength at shedding and furns the probe de-ice power off. Continued cyclic icing and de-icing occurs

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Figure 2-6. ASPIRATOR OF THE LEIGH ICE DETECTOR SET


Figure 2-7. LEIGH ICE COLLECTING PROBE AND OPTICAL ICE THICKNESS SENSOR
until no further ice is encountered. It is notable that the presence of supercooled droplets is determined from icing of the supercooled water and not just the atmospheric conditions under which ice can but might not form.

Crosswise in the duct and at a $45^{\circ}$ angle to the probe axis is located a solid-state soft infra-red emitter and a photo transistor (Figure 2-7). The oblique light path ensures that a large ice catchment area on the sensor probe face is monitored for ice growth thereby accommodating minor variations in probe ice formations. Once a given thickness of ice is accreted on the probe, the IR beam is occluded and logic circuits within the unit turn on electric current to de-ice the probe.

The sawtooth output signal from the photo transistor resulting from the cyclic buildup of ice on the probe is then electronically processed to provide an initial ice warning signal and a computation of rate of formation of ice in terms of ambient liquid water content (LWC).

The ice detector unit provides a voltage signal that is proportional to the liquid water content being measured. This signal is used to drive a standard aircraft type instrument scaled in liquid water content (LWC). The signal can also be recorded for data gathering purposes.

### 2.4 Johnson-Williams (J-W) Liquid Water Content Indicator <br> The Johnson-Williams ( $J-W$ ) liquid water content indicator is a hot-

 wire aircraft instrument designed to measure the liquid water content (LWC) of droplets having diameters of less than about $40 \mu \mathrm{~m}$ and is an adaptation of the hot-wire anemometer. The device uses a nickel-iron wire of a known temperature coefficient of resistance and is heated at a constant current above the boiling point of water. In dry air, the sensing wire is balanced in a bridge circuit at a steady-state temperature between the electrical heat supplied and the heat removed by dry airflow. Droplets impinging the sensing wire evaporate, cool the wire, and thereby cause changes in wire resistance. The resulting imbalance in the bridge circuit is proportional to the liquid water content. Since larger drops tend to be sliced by the wire and not totally evaporated, LWC is underestimated when significant concentratiors of large drops exist in the clouds.The external probe houses two calibrated resistance wires which are mounted in a 1.1 inch diameter tube. The sensing wire is exposed perpendicular to the airstream and bisects the tube while the second wire is mounted with its axis parallel to the airstream direction and at the hase of the tube where it is not subject to water drop impingement. The base mounted wire serves to compensate for variations in air speed, altitude, and air temperature and is connected as part of the bridge circuit. At times, water or ice collected at the compensating wire causes changes and variations in the zero offset of the device and reselts in unreliable estimates of LWC. Characteristics of the J-W device are presented in Table 2-4.

Table 2-4
SPECIFICATIONS OF THE JOHNSON-WILLIAMS LIQUID WATER CONTENT INDICATOR MODEL LWH

Liquid water content range
Droplet diameter
response range
Time response
Accuracy
Precision
Power
Environmental

Mechanical

Weight
$0-3 \mathrm{~g} / \mathrm{m}^{3}$ or $0-1 \mathrm{~g} / \mathrm{m}^{3}$
$<40 \mu \mathrm{~m}$
1 second at 100 mph ;
$0.25 \mathrm{gm}^{-3}$
$0.1 \mathrm{gm}^{-3}$
27 VDC; 15 amperes
Temperature: totally compensated Altitude: 0-30,000 ft Speed: $100-400 \mathrm{mph}$
Cylindrical probe: 1.1 in diameter 2.1 in long

Probe with electronics: approximately 12 lbs

### 2.5 Rosemount Model 102 Total Temperature Sensor

The Rosemount temperature sensor makes use of a recessed platinum resistance element and a flow duct which is designed to achieve a consistently high ram recovery and to reduce the effect of droplet impinjement by inertial separation. Flow within the duct is controlled by bouldary layer bleed ports to improve time response and a right-angle baffle for separation of water
droplets from the sensing element. The housing is equipped with de-icing heaters without appreciable increase in sensing error. The sensing element is connected to a bridge circuit where a high gain operational amplifier converts changes in resistance to a voltage analog of temperature. The sensor specifications are listed in Table 2-5.

Table 2-5
ROSEMOUNT MODEL 102 TOTAL TEMPERATURE SENSOR SPECIFICATIONS

| Type | Platinum resistance thermometer: $50 \Omega$ at $0^{\circ} \mathrm{C}$ |
| :--- | :--- |
| Recovery factor | 0.99 |
| Range | $-50^{\circ} \mathrm{C}$ to $+50^{\circ} \mathrm{C}$ |
| Output | 0 to $5 \vee \mathrm{DC}$ |
| Resolution | $0.02^{\circ} \mathrm{C}$ |
| Linearity | $0.02^{\circ} \mathrm{C}$ |
| Time constant | 2 seconds |
| Power (heater) | 260 watts nominal |
|  |  |
| Qualified to MIL-P-277230 (ASG) |  |

### 2.6 Dew Point Hygrometers (E.G. \& G. Model 137-C3 and General Eastern Model 1011)

Both devices when used in conjunction with a water separator is capable of measuring dew point from an aircraft at speeds up to 300 knots and at altitudes up to $25,000 \mathrm{Kft}$. The instruments utilize the themoelectric or Peltier cooling effect to cool a mirror to the saturation temperature or dew point. A focused light on the mirror is reflected onto a photodetector which in turn drives the thermelectric cooler when changes in the reflected light are sensed. The mirror is cooled when a decrease of condensate occurs. The system stabilizes on and controls about a particular dew layer thickness. The measurement of the mirror temperature under stabilized conditions is thus taken as the dew frost point temperature. Table $2-6$ presents specifications of the two sensors.

Table 2-6
SPECIFICATIONS OF DEW POINT HYDROMETER

## E. G.\& G. 137-C3

|  | Control Unit | Sensor |
| :--- | :--- | :--- |
| Range | $+50^{\circ} \mathrm{C}$ to $-50^{\circ} \mathrm{C}$ | $+70^{\circ} \mathrm{C} \mathrm{to}-55^{\circ} \mathrm{C}$ |
| Accuracy | $\pm 0.5^{\circ} \mathrm{C}$ above $0^{\circ} \mathrm{C}$ | $\pm 0.5^{\circ} \mathrm{C}$ |
|  | $\pm 1.0^{\circ} \mathrm{C}$ below $0^{\circ} \mathrm{C}$ |  |
| Response | $2^{\circ} \mathrm{C} / \mathrm{sec}$ | $2^{\circ} \mathrm{C} / \mathrm{sec}$ |
| Power | $115 \mathrm{VAC} 50 / 1000 \mathrm{cps}$ |  |
|  | 20 watts |  |

## General Eastern Model 1011

|  | Sensor |
| :--- | :--- |
| Range | $-75^{\circ} \mathrm{C}$ to $+50^{\circ} \mathrm{C}$ |
| Accuracy | $\pm 0.2^{\circ} \mathrm{C}$ above $0^{\circ} \mathrm{C}$ |
|  | $\pm 0.4^{\circ} \mathrm{C}$ between $0^{\circ} \mathrm{C}$ to $-40^{\circ} \mathrm{C}$ |
|  | $\pm 1.0^{\circ} \mathrm{C}$ between $-40^{\circ} \mathrm{C}$ to $-75^{\circ} \mathrm{C}$ |
| Response | $2^{\circ} \mathrm{C} / \mathrm{sec}$ |
| Power | 115 VAC $50 / 500 \mathrm{~Hz}$ |
|  | 50 watts |

## 3. DATA SET DESCRIPTION

A total of 209 tests were conducted during the January 1981 testing program at the NASA LeRC IRT. For each test point, cloud measurements were taken in the IRT test section from a J-W device, a Leigh IDS, and two of the PMS probes. Eight additional test points obtained on June 8, 1981, supplement the data set. The testing in June was conducted to evaluate possible effects of the steam tube wrappings on the PMS probe measurements. The Leigh IDS was not available for these tests. Measurements were taken under a variety of turnel conditions and included variations in tunnel airspeed, temperature, cloud LWC and cloud median volume diameter (MVD). Airspeeds ranged from 50 to 285 mph while temperatures varied from about $-20^{\circ} \mathrm{F}\left(-29^{\circ} \mathrm{C}\right)$ to $68^{\circ} \mathrm{F}\left(20^{\circ} \mathrm{C}\right)$. Based on early tunnel calibrations with rotating cylinders, the ciouds produced in the IRT were characterized by LWC and MVD ranging from about 0.5 to $5 \mathrm{~g} / \mathrm{m}^{3}$ and 10 to $30 \mu \mathrm{~m}$, respectively. Due to the large matrix of testing conditions and to time constraints of the program, each test condition was not measured by all of the available PMS probes.

### 3.1 Data Recovery Percentages

Table 3-1 presents a summary of the various PMS probe configurations in the IRT and daia recovery information for each of the indicated cloud measurement devices. The test points are identified in chronological order for convenience. The eight test points (210-217) are listed separately since the two PMS probes and J-W device used in June were not identical to the probes used in January. The PMS probes are identified by type and a number from 1 to 4 for reference purpose. In this report the PMS probes will not be identified by organization since it is not pertinent to the analyses.

As shown, a large portion (~66 percent) of the J-W measurements from January were judged unacceptable and resulted from a loose wire connection in its control box which rendered the device as being either inoperative or intermittent. Measurements from the Leigh IDS were judged unacceptable if the device was not operating, operating intermittently, or operating beyond its full scale range. It is noted that seven of the tests were conducted at temperatures warmer than freezing on 21 January. Hence, since the Leigh device does not provide LWC estimates at these warm temperatures, these test points are not counted in the totals.
Table 3－1

| Data Tape | $\begin{gathered} \text { Date } \\ (1981) \end{gathered}$ | Numberof TestPoints | TestPointID | Acceptable Data From Indicated Probes |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID |  |  |  | J－W | Leigh | FSSP 1 | FSSP 2 | ASSP 1 | ASSP 2 | ASSP 3 | ASSP 4 | OAP 1 | OAP 2 |
| 3 | 1／8 | 13 | 1－13 | 3／13 | 7／13 |  | 0／13 |  | 13／13 |  |  |  |  |
| 4 | 1／9 | 22 | 14－45 | 5／22 | 14／22 |  |  |  | 19／22 |  |  |  | 21／22 |
| 5 | 1／12 | 18 | 46－53 | 0／18 | 18／18 | 18／18 |  |  |  | 17／18 |  |  |  |
| 6 | 1／14 | 32 | 54－85 | 5／32 | 22／32 | 32／32 |  |  |  | 31／32 |  |  |  |
| 7 | 1／15 | 34 | 86－119 | 0／34 | 26／34 | 33／34 |  | 33／34 |  |  |  |  | 윢윢 |
| 8 | 1／16 | 10 | 120－129 | 0／10 | 4／10 |  |  | 10／10 |  |  |  | 10／10 | $0 \frac{0}{2}$ |
| 9 | 1／16 | 11 | 130－140 | 5／11 | 6／11 |  | 0／11 | 11／11 |  |  |  |  | 鱿 |
| 10 | 1／19 | 6 | 141－146 | 5／6 | 6／6 | 0；6 |  |  |  |  | 6／6 |  | $\bigcirc$ |
| 11 | 1／19 | 28 | 147－174 | 27／28 | 24／28 | 0／28 |  |  |  |  | 26／28 |  | 足㗐 |
| 12 | 1／20 | 2 | 175－176 | 1／2 | $2 / 2$ | $0 / 2$ |  |  |  |  | 2／2 |  | 人 |
| 13 | 1／20 | 9 | 177－185 | 0／9 | 9／9 | 0／9 |  |  |  |  | 8／9 |  |  |
| 14 | 1／21 | 24 | 186－209 | 21／24 | 16／17 | 0／24 |  |  |  |  | 0／24 |  |  |
|  | Totals | 209 |  | 72／209 | 154／202 | 83／153 | 0／24 | 54／55 | 32／35 | 48／50 | 42／69 | 10／10 | 21／22 |
|  | \％Recove |  |  | 34 | 76 | 55 | 0 | 98 | 91 | 98 | 65 | 100 | 95 |
| 15 | 6／8 | 8 | 210－217＊ | 8／8 | NA | 7／8 |  |  | 7／8 |  |  |  |  |
|  | \％Recove |  |  | 100 |  | 88 |  |  | 88 |  |  |  |  |

＊The FSSP and ASSP used in June 1981 are identified as FSSP 1＇and ASSP 2＇，respectively．These probes were not the same probes used in January 1981.

Except for FSSP 2, sufficient numbers of test points were recovered from the remaining PMS probes. Glass bead calibrations performed prior to each test day and review of the measurements revealed that FSSP 2 was not calibrated to the manufacturer's specifications. Calibrations performed with four diffrent batches of bead sizes revealed that instead of peak counts being found at four different and widely spaced channel numbers, counts from two of the intermediate sized batches peacked at an identical channel number. Hence although three of the sized batches ( $10-15 \mu \mathrm{~m}, 25-35 \mu \mathrm{~m}$, and $35-45 \mu \mathrm{~m}$ ) had peak counts in their appropriate channel numbers ( 3,8 and 13 ), the counts from the intermediate sized batch ( $15-25 \mu \mathrm{~m}$ ) peaked in channel 8 instead of the nominal chanriel 5. The consequence of this problem resulted in bimodal mass distributions with a mode always found in channel 3 and with the second mode ranging between channels 6 to 8 . Measurements from the remaining PMS probes under identical tunnel conditions displayed single mode distributions.

An example of a typical bimodal distribution from FSSP 2 is presented in Figure 3-1. For comparison purposes, an acceptable measurement from ASSP 2 for the same test point and a rejected measurement from FSSF 1 are also included. The example of the rejected data point is presented since the exponential form of the distribution is characteristic of practically all of the rejected measurements from the remaining ASSP and FSSP probes. For all of the rejected data from ASSP 4 on Janaury 19 (test points 141-209), the pretest calibrations revealed significant changes in their measurement capability from the earlier tests. Whereas the counts from the bead lots of given size ranges peaked in their nominal probe channels early in the test program, they later fell in corresponding smaller numbered channels; thus indicating a broadening of channel band width and decrease in probe sensitivity. Calibrations performed on both of these probes with sized glass beads between $35-45 \mu \mathrm{~m}$ revealed peak counts falling from probe channels $12-13$ down to channels $8-9$ during the later tests. The apparent broadening of channel band width of from 3 to about $4.5 \mu \mathrm{~m}$ resulted in distributions of exponential froin which were characterized by number or mass density decrease with channel number (or particle size) increase. Although not verified, experience strongly suggests that probe deterioration in both these instances resulted from water being lodged in the optical lenses of both probes.

(\%) SS甘W

The remaining rejected PMS probe measurements resulted from probe deterioration due to problems associated witin their optical system. Rapid heating from about -4 to $29^{\circ} \mathrm{F}$ for the last test point (217) after the probes were "cold socked" in the IRT for several hours caused lense "fogging" in both FSSP $1^{\prime}$ and ASSP $2^{\prime}$. As for the remaining rejected samples, ice build up within the sampling tubes was observed to have obstructed the laser beam and thereby affected the measurements. These problems were readily detected by the operator in real time from noting the characteristic exponential distributions on the display console.

Subsequent review of the reduced data lead to rejecting an additional 4 test points and was based upon noting that both the estimated LWC and MVD for a given tunnel test condition (given air speed and tunnel pressure settings) differed significantly from the other measurements taken with the same probe. For these rejected samples, the LWC estimates were lower by a factor of 2 to 3 while the MVD was also lower by about 4 to $6 \mu \mathrm{~m}$.

### 3.2 Tunnel Settings

Cloud conditions (LWC and MVD) within the test section were controlled by separate air and water pressure settings of the spray system and by the air velocity through the enclosed and refrigerated IRT. The following empirical equations which were based on early work with rotating cylinders show these relationships.

$$
\begin{gathered}
\operatorname{LWC}\left(\mathrm{g} / \mathrm{m}^{3}\right)=\frac{6.545 \sqrt{38.7\left(P_{w}-P_{a}\right)}}{V} \\
\operatorname{MVD}(\mu \mathrm{~m})=\frac{1.09(43.9-\sqrt{3.48 V}) \sqrt{38.7\left(P_{w}-P_{a}\right)}}{\left(\frac{P_{a}}{1.13}+10\right)}+0.0052 V+4
\end{gathered}
$$

where

$$
\begin{aligned}
& P_{a}=\text { air pressure setting, psig } \\
& P_{W}=\text { water pressure setting, psig } \\
& V=\text { tunnel air speed, mph } \\
& 20<P_{a}<75 \\
& P_{W}<110 \\
& 5<\left(P_{W}-P_{a}\right)<65
\end{aligned}
$$

Table 3-2 presents a summary of the IRT cloud conditions which shows the number of test points as functions of given air and water pressure settings and tunnel air speeds. As shown, the greatest majority (212 test points) of the tests were conducted at 24 primary pressure (fixed air and water) settings where a minimum of at least 2 test points were obtained. Five of the remaining tests were conducted at five different pressure settings (ID 25). In four of the fixed pressure settings (ID 15, 18, 19, and 20), tunnel air velocity vas also varied systematically. Hence it is indicated that probe testing was subject to 54 different cloud conditions for which each is listed information on the control parameters, $P_{a}, P_{W}$, and $V$.

Temperatures are also tabulated and serve merely to present ranges over which each of the cloud conditions were run. Further information on the number of test points as function of temperature range is summarized in Table 3-3. Here it is shown that the majority of tests were conducted at temperatures between -20 to $19^{\circ} \mathrm{F}$ and that the largest number (89) of test points were obtained at temperatures between 10 to $19^{\circ} \mathrm{F}$. Had all of the measurements been judged acceptable, it becomes quite apparent that it was not possible to obtain measurements from each of the PMS probes for all test conditions (fixed cloud and temperature).

### 3.3 Data Selection

Measurements taken ove- periods ranging from about 20 to 300 seconds were processed to obtain representative estimates of each test condition which was maintained in the IRT test section for durations ranging from about 2 to 15 minutes. The sampling periods were chosen to represent the early steady state cloud conditions as revealed by time plots of key cloud parameters (LWC and MVD). Possible measurement deterioration with time increase due to ice buildup on the probes was the primary reason for selecting data early (as oppod to late) in the total spray period. Steady state conditions were usually measured at the test section some 40 to 60 seconds after the nozzles were turned on and properly adjusted. The nozzles were turned on after cooling (or heating) the IRT to a desired temperature and after ificreasing the tunnel air speeds from idfe velocity to a designated velocity.

| Pressure Setting ID | Air <br> Pressure (PSI) | Water Pressure (PSI) | IRT TAS mph $)$ | $\begin{gathered} \mathrm{IRT} \\ \mathrm{LWC} \\ \mathrm{~g} / \mathrm{m}^{3} \end{gathered}$ | IRT <br> MVD <br> ( $\mu \mathrm{m}$ ) |  | Temperature | Pressure Setting ID | Air Pressure (PSI) | Water Pressure (PSI) | $\begin{gathered} \text { IRT } \\ \text { TAS } \\ \text { (mph }) \end{gathered}$ | $\begin{aligned} & \text { IRT } \\ & \mathrm{LWC} \\ & \mathrm{~g} / \mathrm{m}^{3} \end{aligned}$ | $\begin{aligned} & \text { IRT } \\ & \text { MVD } \\ & (\mu \mathrm{m}) \end{aligned}$ | Number of test points | Temperature |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20.5 | 30.5 | 230 | 0.56 | 17.1 | 4 | -11 to 16 | 192 | 50.0 | 75.0 | 220 | 0.93 | 15.3 | 1 | - : 1 |
| 2 | 24.0 | 75.0 | 235 | 1.24 | 28.9 | 3 | 16 | 197 | 50.0 | 75.0 | 230 | 0.89 | 15.0 | 1 | -10 |
| 3 | 25.0 | 32.5 | 200 | 0.56 | 15.2 | 2 | 14 | 19 g | 50.0 | 75.0 | 240 | 0.85 | 14.6 | 1 | -10 |
| 4 | 26.0 | 42.0 | 100 | 1.63 | 25.3 | 5 | 5 to 15 | 19h | 50.0 | 75.0 | 250 | 0.81 | 14.3 | 1 | -11 |
| 5 | 30.0 | 55.0 | 200 | 1.02 | 21.3 | 2 | 16 | 191 | 50.0 | 75.0 | 260 | 0.78 | 14.0 | 2 | -10 |
| 6 | 30.0 | 63.0 | 194 | 1.19 | 23.9 | 7 | 13 to 14 | 19j | 50.0 | 75.0 | 270 | 0.75 | 13.7 | 1 | -10 |
| 7 | 31.0 | 41.0 | 200 | 0.64 | 15.1 | 4 | 13 亡o 14 | 19k | 50.0 | 75.0 | 283 | 0.72 | 13.3 | 1 | -10 |
| 8 | 32.0 | 39.0 | 100 | 1.08 | 16.3 | 12 | 13 to 54 | 20a | 50.0 | 90.0 | 50 | 5.15 | 28.5 | 3 | -20 to -11 |
| 9 | 35.0 | 57.0 | 235 | 0.81 | 17.1 | 3 | 16 | 20 b | 50.0 | 90.0 | 100 | 1.58 | 24.5 | 5 | -20 to -11 |
| 10 | 36.0 | 62.0 | 220 | 0.94 | 18.5 | 11 | 4 to 58 | 20 c | 50.0 | 90.0 | 150 | 1.78 | 21.4 | 5 | -20 to -11 |
| 11 | 36.0 | 70.0 | 260 | 0.91 | 18.4 | 10 | 4 to 62 | 20 d | 50.0 | 90.0 | 200 | 1.29 | 18.9 | 5 | -15 to -9 |
| 12 | 36.0 | 73.0 | 270 | 0.92 | 18.5 | 6 | 4 to 16 | 20 e | 50.0 | 90.0 | 220 | 1.17 | 18.0 | 2 | -11 |
| 13 | 36.0 | 76.0 | 285 | 0.90 | 18.2 | 10 | 5 to 68 | $20 f$ | 50.0 | 90.0 | 230 | 1.12 | 17.5 | 2 | -11 to -10 |
| 14 | 41.0 | 58.0 | 100 | 1.67 | 19.7 | 5 | 4 to 15 | 20 g | 50.0 | 90.0 | 240 | 1.07 | 17.1 | 2 | -11 |
| 15a | 42.5 | 56.0 | 150 | 1.00 | 15.7 | 20* | -9 to 53 | 20h | 50.0 | 90.0 | 250 | 1.03 | 16.7 | 2 | -11 to -9 |
| 15b | 42.5 | 56.0 | 200 | 0.79 | 14.8 | 6 | 13 to 14 | 201 | 50.0 | 90.0 | 260 | 0.99 | 16.3 | 2 | -9 |
| 16 | 44.0 | 75.0 | 240 | 0.94 | 16.8 | 6 | 4 to 16 | 20j | 50.0 | 90.0 | 270 | 0.95 | 15.9 | 2 | -12 to -8 |
| 17 | 46.0 | 78.0 | 228 | 1.01 | 17.1 | 2 | -11 | 20k | 50.0 | 90.0 | 285 | 0.90 | 15.3 | 2 | -11 to -8 |
| 18a | 50.0 | 60.0 | 50 | 2.58 | 16.4 | 2 | -14 to -13 | 21 | 53.0 | 76.0 | 173 | 1.13 | 16.0 | 3 | $5$ |
| 18b | 50.0 | 60.0 | 100 | 1.29 | 14.5 | 2 | -14 to -13 | 22 | 53.0 | 91.0 | 250 | 1.00 | 15.9 | 8 | 4 to 60 |
| 18c | 50.0 | 60.0 | 150 | 0.86 | 13.1 | 2 | -14 to -11 | 23 | 64.0 | 69.0 | 100 | 0.91 | 10.3 | 5 | 4 to 15 |
| 18d | 50.0 | 60.0 | 200 | 0.64 | 12.0 | 3 | -14 to 16 | 24 | 65.0 | 100.0 | 100 | 2.41 | 19.5 | 5 | 4 to 16 |
| 18 e | 50.0 | 60.0 | 220 | 0.59 | 11.6 | 2 | -9 | 25a | 13.5 | 42.5 | 150 | 1.46 | 39.8 | 1 | -11 |
| 19a | 50.0 | 75.0 | 50 | 4.07 | 23.5 | 2 | -18 to -11 | 25b | 30.0 | 46.0 | 228 | 0.76 | 16.9 | 1 | -11 |
| 19b | 50.0 | 75.0 | 100 | 2.04 | 20.3 | 2 | -18 to -11 | 25c | 23.0 | 69.0 | 228 | 1.21 | 29.0 | 1 | -11 |
| 19c | 50.0 | 75.0 | 150 | 1.36 | 17.9 | 2. | -18 to -11 | 25d | 36.0 | 67.0 | 220 | 1.03 | 19.8 | 1 | 9 |
| 19d | 50.0 | 75.0 | 200 | 1.02 | 16.0 | 17 | -12 to 56 | 25 e | 50.0 | 57.0 | 235 | 0.46 | 10.3 | 1 | 16 |

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Table 3-3

## NUMBER OF TEST POINTS AS FUNCTION <br> OF TEMPERATURE RANGE

| Temperature <br> Index | Temperature <br> Range | Number of <br> Test Points |
| :---: | :---: | :---: |
| 1 | -20 to -11 | 51 |
| 2 | -10 to -1 | 23 |
| 3 | 0 to 10 | 44 |
| 4 | 11 to 20 | 89 |
| 5 | 20 to 32 | $3 *$ |
| 6 | $>32$ | -7 |
|  | Totãl |  |

*Points taken from June 8 only.

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Figure 3-2 presents a tim: plot of measurements taken at the test stand during the conduct of a typical test (211). After initiating the spray nozzles ( 0 sec ), the spray cloud is shown to arrive at about 20 seconds and to reach near steady state at about 50 to 55 seconds. After approximately 90 seconds and for times to approximately 320 seconds into the run, the PMS probe estimates are shown to decrease while the $J-W$ trace remains at a nearly constant value. Although the largest decrease appears in the LWC trace of the ASSP, estimates of the FSSP on other occasions decreased at faster rates. The spray cloud was turned off after a five minute (at 300 sec ) testing period and was sensed approximately 25 seconds later ( 325 sec ) at the test stand as evidenced by the rapid decline of the indicated probe traces.

### 3.4 Data Reduction Procedures

Procedures employed in the reduction of the PMS probe measurements consisted of initially converting the raw counts in each of the 15 size channels to a number density $N_{i}$ by the following equation:

$$
N_{i}=\frac{C_{i}}{A_{i} \times V \times E F F \times \Delta t}
$$

where

$$
\begin{aligned}
& C_{i}=\text { raw counts recorded in each channel number, } i \text {, in a time } \\
& \text { interval, } \Delta t . \\
& A_{i}=\text { sample area for each channel number. } \\
& v=\text { true air speed. } \\
& \text { EFF }=\text { efficiency factor }
\end{aligned}
$$

For the ASSP and FSSP devices, $A_{i}$ remains constant for all 15 size channels, while the constant EFF is determined from the ratio of the sum of the raw counts in 15 size channels and the separately recorded total strobe counts (ST) during the time interval $\Delta t$.



For probes without the velocity reject feature, EFF is assumed to be equal to one.

The constant EFF also maintains a value of 1 for data from the OAP. However, in these optical array devices, the sample area varies with channel number as:

$$
A_{i}=\Delta D \times(K-i) \times L
$$

where

$$
\begin{aligned}
& \Delta D=\text { channel width. } \\
& K=N-1 . \\
& N=\text { number of sensitive elements in the photodiode array. } \\
& L=\text { depth of field. }
\end{aligned}
$$

For the larger channels ( $8-15$ ), L is larger than the probe aperture distance of 6.1 cm and hence remains fixed to it. Depth of field compensation for the smaller channels (1-7) is thus computed from the following equation:

$$
A_{i}=A_{i} \times\left(\frac{i}{8}\right)^{2}, i=1,7
$$

where $A_{i}$ to the right of the equal sign is computed from the previous equation.

Once determined, the number density values provide means for computation of the following bulk parameters from integration of the data.

1. Total number density, $N_{T}$

$$
N_{T}=\sum_{i=1}^{\Sigma=15} N_{i}
$$

2. Liquid water content, LWC

$$
L W C=\frac{\pi}{6} \rho_{W} \sum_{i=1}^{15} N_{i} D_{i}^{3}
$$

## ORIGINAL PACE IS <br> OF POOR QUALITY

where
$D_{i}=$ midpoint size of each channel, $D_{i}=\mathbf{i} \times \Delta D$
$\rho_{W}=$ density of water.
3. Median volume diameter, MVD

$$
M V D=\begin{aligned}
& D=M V D \\
& D=D_{i}
\end{aligned} N_{i} D_{i}^{3}=\frac{1}{2} \quad \sum_{i=1}^{15} N_{i} D_{i}^{3}
$$

Table 3-4 presents a summary of the sampling characteristics of the PMS probes tested in the IRT. The band widths listed were determined from the glass bead calibrations performed prior to each test.

Table 3-4
PMS PROBE SAMPLING CHARACTERISTICS

| Probe | $\Delta D$ <br> $(\mu \mathrm{~m})$ | $A_{i}$ <br> $\left(\mathrm{~mm}^{2}\right)$ | N | Velocity <br> Reject |
| :--- | :---: | :---: | :---: | :---: |
| FSSP 1 | 3.0 | 0.243 | - | No |
| FSSP 2 | 3.0 | 0.254 | - | No |
| ASSP 1 | 3.5 | 0.672 | - | Yes |
| ASSP 2 | 3.0 | 0.811 | - | Yes |
| ASSP 3 | 3.5 | 0.459 | - | No |
| ASSP 4 | 3.0 | 0.614 | - | No |
| FSSP 1 | 3.9 | 0.547 | - | Yes |
| ASSP 21 | 3.3 | 0.653 | Yes |  |
| OAP 1 | 2.0 | eq | - | - |
| OAP 2 | 2.0 | eq | 22 | - |

All cloud data were corrected for local velocity differences from bockage effects from the probe supports and traverse hardware in tunnel test section without the probes in place Although no significant velocity differences were measured at the sampling points of the PMS probes, pitot-static pressure measurements disclosed overspeeding at the Leigh IDS and J-W hot wire by factors of 1.18 and 1.13, respectively, and have been appropriately handled in the data reduction software.

### 3.5 Data Volume Description

Data listings in the form of a drop size distribution report for each test condition and PMS probe measurements are presented in a separate data volume as part of the contract requirements. An example is presented in Figure 3-3. Table 3-5 presents a summary of the information listed and identifying keys for the computer generated listings. It is noted that the IRT cloud expectations were computed from the equitions given in Section 3.2 for which the independent variables are also listed. Air and water pressur? settings, temperature, and air speed for each test point were obtained from the tunnel operator's log sheet. In addition to the written comments, negative values are also listed for some of the data judged unacceptable. For measurements from the $\mathrm{J}-\mathrm{W}$ and Leigh devices, a default value of $-0.88 \mathrm{~g} / \mathrm{m}^{3}$ is listed if they were inoperative while a negative sign is assigned to the estimate if they functioned intermittently. Missing relative humidity information for the test period is indicated by a default value of $\mathbf{- 9 9}$ percent.

To complement the distribution reports, the data volume also includes a computer generated test point summary for each of the data tapes listed in Table 3-1. The summaries precede the distribution reports. Figure 3-4 presents an example of a summary for Tape 3. Identifying keys for information summarized appear in Table 3-6. The test point summaries are also presented in Appendix A.

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$\begin{array}{llll}\text { nalt } 1 / 14 / 81 & \text { HUN } 10 \text { SB6I } \\ \text { STAKT TIME(LST) } 2016: 5 \text { DURATIMN(SEC) } 30\end{array}$ IKT TEST CINDITIGNS: TAS(MPH)= $230 \quad$ TEM(F) = $10 \quad H H(X)=-99$ SPRAY PRESSURE SETTIHGS
IFT CI UUD EXPECTATIORS:



$$
\begin{aligned}
& \text { AVERAGE SPECTHA INF GRMATION } \\
& \text { PRUBE AESP } 3
\end{aligned}
$$

$$
\begin{aligned}
& 110 \\
& (/ 6 M 4) \\
& .1436 F+n 5 \\
& .1055 E+00 \\
& .2027 E+00 \\
& .2092 t+100 \\
& .1453 F+00 \\
& .9614 E+05 \\
& .5691 E+05 \\
& .33 H 2 E+05 \\
& .1988 F+05 \\
& .9262 t+04 \\
& .1348 E+04 \\
& .3303 F+04 \\
& .1888 E+04 \\
& .1328 E+04 \\
& .8151 E+03
\end{aligned}
$$

$$
\begin{aligned}
& \text { CIHMERITS } \\
& \text { HELATIVE HUMIDITY HEASUREMENTS BUT TAKEN }
\end{aligned}
$$

Figure 3-3. EXAMPLE OF DROPLET SIZE DISTRIBUTION REPORT

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Table 3-5

## KEY FOR TEST POINT LISTING

| Information | Key | Units |
| :---: | :---: | :---: |
| Test point number | TEST POINT | - |
| Date | DATE | MO/DA/YR |
| Run number | RUN ID | - |
| Start time | Start time | LST |
| Sample duration | DURATION | sec |
| IRT Settings |  |  |
| Air speed | TAS | mph |
| Temperature | TEM | F |
| Relative humidity | RH | - |
| Air pressure | AIR | psig |
| Water pressure | H2O | psig |
| MVD | MVD | microns |
| LWC | LWC | $\mathrm{g} / \mathrm{m}^{3}$ |
| LWC from J-W device Coefficient of variation* | $\begin{aligned} & \mathrm{JW} \\ & \mathrm{CV} \end{aligned}$ | $\begin{aligned} & \mathrm{g} / \mathrm{m}^{3} \\ & \% \end{aligned}$ |
| LWC from Leigh device Coefficient of variation | $\begin{aligned} & \text { LEIGH } \\ & \text { CV } \end{aligned}$ | $\underset{\%}{g / m^{3}}$ |
| Probe identifier | PROBE | name |
| Size distribution/per channel |  |  |
| Mid-point diameter, Di | DI | microns |
| Normalized size, Di/MVD | DI/MVD |  |
| Number density, Ni | NI | $/ \mathrm{cm}_{4}^{3}$ |
| Number density per band width, $N_{D}$ | ND | $1 \mathrm{~cm}^{4}$ |
| Mass density, Mi <br> Mass density per band width, M | MI <br> MD | $\mathrm{g} / \mathrm{cm}^{3}$ |
| Mass density Percent mass, Mi/LWC | MI/LWC |  |
| Cumulative percent, mass, $\sum_{i}^{i} M i / L W C$ | SMI /LWC | \% |
| Probe LWC, $\Sigma M i$ Coefficient of variation | PROBE LWC CV | $\underset{\%}{\mathrm{~g} / \mathrm{m}^{3}}$ |
| Probe MVD Coefficient of variation | PROBE MVD CV | microns <br> \% |
| Probe total number density, $N_{T}$ Coefficient of variation | $\begin{aligned} & \text { NT } \\ & \text { CV } \end{aligned}$ | ${ }_{\alpha}^{/ \mathrm{cm}^{3}}$ |
| Data quality comments | COMMENTS | - |
| *The coefficient of variation is defined as the ratio of the standard devia tion to the mean of the parameters computed from the one-second data recordings; CV $=\sigma /$ mean. |  |  |

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- $\quad$ OF POOR QUALMTY
IRT TEST POINT SUMMARY JANUARY 1981
TAPE
APE

PT
m*
120

****
150





 PROHE
ID 2 OAP 1
ASSP
 $\begin{array}{rlr}44 & \text { OAP } & 1 \\ 2 & & 1 \\ & \text { ASSP } & 1 \\ 40 & \text { OAP } & 1 \\ 3 & & \\ & \text { ASSP } & 1\end{array}$
 $\begin{aligned} & 02 \text { OAP } \\ & 0 \\ & \text { ASSP } 1\end{aligned}$

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0 0
$88^{\circ}$
$7 * * *$ $0=\Gamma$ ***************
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$\underbrace{\infty}_{\infty} 0$ 0
88
8 0
-88

[^0]
## Table 3-6

KEY FOR IRT TEST POINT SUMMARIES

| Information | Key | Units |
| :---: | :---: | :---: |
| Data tape | TAPE | - |
| Run number | RUN ID | - |
| Day | DA | - |
| Start time | TIME | Local |
| Sample duration | DT | sec |
| Tunnel air speed | TAS | mph |
| Tunnel temperature | TEM | F |
| Tunnel relative humidity | RH | \% |
| Pa | PAIR | psig |
| $P_{W}$ | PH20 | psig |
| Tunnel LWC expectation | T-Q | $\mathrm{g} / \mathrm{m}^{3}$ |
| Tunnel MVD expectation | DV | microns |
| J-W LWC* | J-Q | $\mathrm{g} / \mathrm{m}^{3}$ |
| Leigh LWC | L-Q | $\mathrm{g} / \mathrm{m}^{3}$ |
| PMS probe |  |  |
| Probe name | PROBE | - |
| LWC | Q | $\mathrm{g} / \mathrm{m}^{3}$ |
| MVD | DV | miçons |
| $\mathrm{N}_{T}$ | NT | $/ \mathrm{cm}^{3}$ |
| Total raw counts/sec | RCT | $\times 10-2$ |
| Gamma distribution coefficient, $\alpha$ | ALP |  |
| Gamma distribution coefficient, $\lambda$ | LAM | $\times 10^{-3} / \mathrm{micron}$ |
| Average probe activity | ACT |  |
| Average probe efficiency | EFF | \% |
| Data quality comments | REMARKS | - |

## 4. RESULTS AND DISCUSSION

Test point measurements judged acceptable serve as the basic data set for the analyses. The following subsections present the results of the following analyses tasks.

- IRT cloud repeatability.
- IRT cloud uniformity.
- Effect of steam tube wraps on spectrometer measurements.
- Temperature and velocity effects on spectrometer measurements.
- Instrument intercomparisons.
4.1 IRT Cloud Repeatability

For obvious reasons, demonstration of cloud repeatability is essential to the remaining analyses tasks. For the purpose of obtaining quantitative estimates of cloud repeatability, the analyses evaluates the sample to sample variations with respect to the mean by the following standard statistical equations.

$$
\begin{gathered}
\bar{x}=\sum_{j \stackrel{n}{\Sigma}}^{n} x_{j} \\
s^{2}=\sum_{j \stackrel{n}{=}}\left(x_{j}-\bar{x}\right)^{2} /(n-1) \\
C V=\frac{s}{\bar{x}} \times 100 \%
\end{gathered}
$$

where

$$
\begin{aligned}
\frac{x_{j}}{} & =\text { a sample variable } \\
x & =\text { sample average or mean } \\
n & =\text { number of samples } \\
s & =\text { estimate of the standard deviation } \\
\mathrm{CV} & =\text { coefficient of variation }
\end{aligned}
$$

Hence low values computed for the coefficient of variation indicate high repeatability and vice versa.

Table 4-1 presents information on averages and on the temporal variation (CV) of the various measurements for given tests from data collected (1) during the time when the spray cloud passed through the test section (spray) and (2) during the intial time period of the spray (sample). Both of these corresponding data sets had identical starting times. The statistics were based upon samples computed for each second of recorded data and for the indi.. cated durations ( $n=$ number of seconds). For a given instrument and a given test, the following observations are made.

Based on the statistics given for the accretion (Leigh and J-W) devices, temporal variations in cloud LWC during a given spray remains small; typically between $4-8$ percent.

- Although the statistics from the accretion devices indicate higher absolute variations with increase in average cloud LHC amounts, their percentages are relatively constant and hence considered not affected by different airspeed or temperature settings in the IRT.

The sampling durations chosen are sufficient to provide precise estimates of the average spray conditions as evidenced by the near identical values listed for the spray and sample averages of the accretion devices. Of the five test conditions presented, four of the sample estimates are within about 1 percent while the fifth (test point 61) is within 7 percent of their corresponding spray average values. Based upon sampling considerations and the relatively small CV shown, it is quite apparent that the 20 to 50 second periods are more than sufficient to provide precise estimates of the average spray conditions.

The PMS probe estimates of the average spray LWC show significantly wider percent variations than those from the accretion devices and thus indicate that they are less reliable rather than that the cloud conditions varied widely during the course of the spray. Aside from the steady conditions indicated from the two accretion devices, support is provided from the sample values which generally show higher estimated averages having significantly smaller CV values. These differences between the spray and sample statistics reflect decreases in measurement precision during the course of the spray which resulted from ice buildup within the sampling tubes as indeed were confirmed by inspection after test conclusion.

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|  | $\begin{gathered} \text { TEM } \\ (\mathrm{F}) \\ \hline \end{gathered}$ | $\begin{gathered} v \\ (\mathrm{mph}) \end{gathered}$ | Duration (sec) | $\begin{gathered} \text { Leigh twc } \\ \left(\mathrm{g} / \mathrm{m}^{3}\right) \end{gathered}$ |  | $\begin{gathered} \text { JWLWC } \\ \left(\mathrm{g} / \mathrm{m}^{3}\right) \\ \hline \end{gathered}$ |  | $\begin{gathered} \text { FSSP LWC } \\ \left(\mathrm{g} / \mathrm{m}^{3}\right) \\ \hline \end{gathered}$ |  | $\begin{gathered} \text { ASSP LWC } \\ \left(\mathrm{g} / \mathrm{m}^{3}\right) \end{gathered}$ |  | $\begin{aligned} & \text { FSSP MVD } \\ & (s) \end{aligned}$ |  | $\begin{gathered} \text { ASSP MVD } \\ (\mu) \\ \hline \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Point |  |  |  | AVE | $\mathrm{CV}(\%)$ | AVE | CV(\%) | AVE | CV(\%) | AVE | CV(\%) | AVE | CV(\%) | AVE | CV(x) |
| SPRAY |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 | 14 | 200 | 575 | 0.99 | 4 | - | - | - | - | 0.06 | 64 | - | - | 15.8 | 1 |
| 61 | 7 | 100 | 265 | 1.78 | 4 | - | - | 0.34 | 28 | 2.30 | 10 | 22.7 | 7 | 20.8 | 3 |
| 183 | -11 | 220 | 260 | 0.63 | 6 | - | - | 0.05 | 23 | 0.04 | 84 | 14.5 | 5 | 18.2 | 17 |
| 210 | 29 | 150 | 300 | - | - | 0.72 | 8 | 0.55 | 27 | 2.53 | 5 | 20.1 | 5 | 20.3 | 1 |
| 213 | -4 | 150 | 720 | - | 二 | 0.79 | $\underline{6}$ | 0.65 | $\underline{25}$ | 1.18 | 74 | 22.3 | 8 | $17 . \mathrm{C}$ | $\underline{20}$ |
| Average |  |  |  | 1.13 | 5 | 0.76 | 7 | 0.40 | 23 | 1.22 | 47 | 19.9 | 6 | 18.5 | 8 |
| SAMPLE |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 | 14 | 200 | 30 | 1.00 | 4 | - | - | - | - | 0.14 | 8 | - | - | 16.5 | 2 |
| 61 | 7 | 100 | 30 | 1.91 | 4 | - | - | 0.50 | 14 | 2.83 | 5 | 25.3 | 4 | 22.5 | 2 |
| 183 | -11 | 220 | 40 | 0.63 | 4 | - | - | 0.07 | 9 | 0.09 | 5 | 15.5 | 3 | 18.6 | 1 |
| 210 | 29 | 150 | 55 | - | - | 0.71 | 8 | 0.71 | 3 | 2.61 | 3 | 21.8 | 1 | 20.5 | 1 |
| 213 | -4 | 150 | 30 | - | $=$ | 0.80 | 5 | 0.77 | 3 | 2.26 | 4 | 22.1 | 1 | $\underline{20.8}$ | 1 |
| Average |  |  |  | 1.18 | 4 | 0.76 | 7 | 0.51 | 7 | 1.98 | 5 | 21.2 | 2 | 19.8 | 1 |

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- Based on the near identical CV values listed for the PMS sample estimates of cloud I.WC and those from the accretion devices, it is indicated that the PMS probe measurements taken early during given tests are valid. Hence it is inferred from the sample estimates that the temporal variations in cloud MVD were also small and for these test points in the range of from 1 to 4 percent.
- Measurement deterioration due to ice buildup in the PMS probes results in a larger percentage decrease in estimating LWC than in estimating MVD as is inferred by the corresponding sample and spray averages and is as expected since LWC is proportional to the cube of particle size.

Table 4-2 presents additional information on the repeatability of the IRT spray clouds. Summarized information on both cloud LWC and MVD from measurements from each of the cloud instruments listed include:

Table 4-2
IRT REPEATABILITY SUMMARY FOR A GIVEN SPRAY CLOUD

| Instrument | Variation (\%) in LWC |  |  |  | Variation (\%) in MVD |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { Siven } \\ & \text { Spray } \\ & \hline \end{aligned}$ | $\begin{gathered} \text { Given } \\ \text { Day } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { Test } \\ & \text { Period } \\ & \hline \end{aligned}$ | Yearly | $\begin{aligned} & \text { Given } \\ & \text { Spray } \end{aligned}$ | $\begin{gathered} \text { Given } \\ \text { Day } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { Test } \\ & \text { Period } \end{aligned}$ |
| Leigh | 4 | 10 | 12 | - | - | - | - |
| J-W | 6 | 21 | 15 | 12* | - | - | - |
| FSSP 1 | 15 | 36 | 19 | - | 3 | 4 | 4 |
| ASSP 1 | 6 | 20 | 24 | - | 2 | 3 | 3 |
| ASSP 2 | 10 | 15 | - | - | 3 | 3 | - |
| ASSP 3 | 6 | 20 | 33 | - | 2 | 7 | 7 |
| ASS ${ }^{-1} 4$ | 9 | 37 | - | - | 3 | 7 | - |

*one tunnel setting.

1. Variation during a given spray is determined from the average of the CV values of all accepted test points.
2. Variation during a given day which represents an evaluation of test point averages taken under identical tunnel conditions (fixed air and water pressure and airspeed settings) at different times on a given day.

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3. Variation over the test period which represents an evaluation of test point averages taken under identical tunnel conditions on different days.
4. Yearly variasions which represent an evaluation of the year to year variations in the IRT spray clouds of a given set of tunnel settings.

Information presented for items 2-4 above represents a normalized form of the coefficient of variation (NCV) which is based upon (1) normalizing the sample to sample variations of the estimates ( $x_{i}=$ LWC or MVD) taken at a given tunnel condition, $s$, to their average, $\bar{x}_{5}$, and 2) pooling the normalized squared deviations of all possible given tunnel conditions, $k$, as follows:

$$
\begin{gathered}
N C V=\left[\begin{array}{cc}
\stackrel{k}{k} & \stackrel{n}{s}_{\sum_{s}}^{=}\left(\frac{x_{i}-\bar{x}_{s}}{\bar{x}_{s}}\right)^{2} \\
\sum_{i=1}^{k} n_{s}-1
\end{array}\right]^{1 / 2} \times 100 \% \\
\bar{x}_{s}=\frac{\sum_{i=1}^{n} x_{i}}{n_{s}} \\
n_{s}>1
\end{gathered}
$$

For evaluating item 2 above:
$x_{i}=$ sample estimate taken at a given tunnel condition on a given day.
$n_{S}=$ number of samples taken at a given tunne condition on a given day.

For evaluating the test period on daily variation:
$x_{i}=$ average of all sample estimates taken at a given tunnel condition on a given day.
$n_{S}=$ number of different days when samples were taken at a given tunnel condition.

For evaluating the yearly variation:

$$
\begin{aligned}
x_{\mathbf{i}}= & \text { average of all sample estimates taken at a given tunnel } \\
& \text { condition during a season. } \\
n_{\mathbf{s}}= & \text { number of different test periods (e.g., January and June } \\
& 1981 \text { ) when samples were taken at a given tunnel condition. }
\end{aligned}
$$

Based on this procedure, the samples were normalized to account for absolute cloud differences at the various tunnel settings and pooled to lend confidence to the variation estimates since in most cases with the PMS probes, only 1 to 3 tests were conducted at a given tunnel condition over a two day period. Hence 211 of the accepted samples from a given instrument were not necessarily used in evaluating the effects listed under each column of the table.

Prominent features of the summary table include the following observations:

- Larger LWC variations exist between sprays taken at fixed tunnel settings than during given sprays. Measurements from the accretion devices show average temporal deviations of 4 to 6 percent and normalized test point to test point variations of 10 to 20 percent.
- Generally larger LWC variations are indicated from the PMS probe measurements and infers that their estimates of LWC are less reliable than those of the accretion devices. Larger variations are also found between sprays of fixed tunnel conditions than during given sprays.
- Although slightly larger MVD variations are also shown to exist between sprays, the variations of between $3-7$ percent are small and not significantly different than the averages of 2 to 3 percent shown for given sprays. For a MVD of $25 \mu \mathrm{~m}$, these percentages translate to absolute variations of less than about $1 \mu \mathrm{~m}$.
- Cloud variations among tests conducted at given tunnel settings were similar irregardless of whether the tests were conducted on a given day or on different days as indicated by similar values listed beneath the given day and test period headings.
- Although a 12 percent yearly variation is listed, it is noted that the estimate is based only on one tunnel setting ( $k=1$ ) and on measurements taken with the $J-W$ device in January and June $1981\left(n_{S}=2\right)$ and therefore does not present a representative estimate of the yearly variation.

Based on these observations it is concluded that the IRT clouds are quite homogeneous ( $\pm 5$ percent in LWC and $\pm 2-3$ percent in MVD) during given tests and are highly reproducible ( $\pm 10-15$ percent in LWC and $\pm 3-7$ percent in MVD). These estimates are considered not to be inconsistent with estimates provided by NASA which are based upon errors due to pressure and velocity settings of the IRT operating equations given in a previous section.

NASA curves on drop size (MVD) error as functions of maximum errors of air and water pressure settings ( $\pm 2$ PSI) and of tunnel velocity ( $\pm 2 \mathrm{mph}$ ) are presented in Figures 4-1 to 4-3, respectively. Percentage error curves in LWC are presented in Figure 4-4 for maximum air and water pressure setting errors of $\pm 2$ PSI. Distingutshing features of the NASA error curves include the following:

- The drop size error due to an error in air pressure setting increases with decrease in air pressure and in tunnel velocity, and with increase in the absolute difference between the water and air pressure and amounts to less than $\pm 2 \mu \mathrm{~m}$ for $\mathrm{a} \pm 2$ PSI setting error.
- The drop size error due to an error in the water pressure setting increases with decrease in atr pressure setting and in tunnel velocity but with decrease in the absolute difference between the water and air pressures and amounts to less than $\pm 2 \mu \mathrm{~m}$ for $\mathrm{a} \pm 2$ PSI setting error.
- The drop size error due to an error in the velocity setting increases with decrease in air pressure setting and in tunnel velocity, and with increase in the absolute difference between the water and air pressure settings and amounts to less than $\pm 0.3 \mu \mathrm{~m}$ for $\mathrm{a} \pm 2 \mathrm{mph}$ setting error.
- For $a \pm 2$ PSI error in either the air or water pressure setting, the percentage error in LWC increases exponentially with decrease in the absolute difference between water and air pressure settings. For this seting error, a LWC error of $\pm 5$ percent is indicated for a 20 PSI pressure difference (PD) and increases exponentially to $\pm 20$ percent at a PD of 5 PSI. The effect of a $\pm 2 \mathrm{mph}$ velocity setting error has a negligible influence on cloud LWC and MVD.


### 4.2 IRT Cloud Uniformity

Cloud uniformity is concerned in this analysis task with cloud variations along a direction perpendicular to the air flow in the IRT test section

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\longrightarrow 100 \text { m.p.h. }
$$

-     -         -             - 250 m.p.h.


Figure 4-1. DROP SIZE ERROR IN IRT DUE TO PRESSURE SETTING ERROR ERROR IN PAIR of $\pm 2$ PSI (MAX ERROR)

100 m.p.h.


Figure 4-2. DROP SIZE ERROR IN IRT DUE TO PRESSURE SETTING ERROR ERROR IN PWATER of $\pm 2$ PSI

|  |  |
| :---: | :---: |



Figure 4-3. DROP SIZE ERROR IN IRT DUE TO VELOCITY SETTING ERROR ERROR IN VELOCITY of $\pm 2$ M.P.H. (MAX ERROR)


Figure 4-4. LWC ERROR IN IRT DUE TO PRESSURE SETTING ERROR
and serves to determine whether or not cloud (LWC and MVD) differences existed between the sampling locations of the two PMS probes. The probes were separated by approximately 8 inches. To attain this objective, measurements were taken at fixed and known distances from the center of the test section by moving the test stand along the cross-wind direction. For the evaluation, measurements made at fixed tunnel conditions on 8 January 1981 and on 30 0ctober 1979 (Boeing-Vertol tests) serve as the data base. Unfortunately, both the Leigh and J-W devices were inoperative during this segment of testing in January and were not installed during the Boeing-Vertol tests.

Table 4-3 presents comparisons of the cloud measurements for these tests which were conducted at two different but fixed tunnel conditions. From the 95 percent confidence interval (CI) given for the five centered measurements and from the approximate 10 percent CV determined for the two off-centered estimates, it can be concluded statistically that the given cloud was not significantly different at $\pm 12^{\prime \prime}$ from tunnel center on 8 January. Since only one test point measurement for a given tunnel condition was obtained at each of the test stand positions in the Boeing-Vertol tests, no statistical

Table 4-3
TUNNEL UNIFORMITY COMPARISONS OF
CLOUD LWC AND MVD AT GIVEN DISTANCES FROM TUNNEL CENTER FOR FIXED TUNNEL CONDITIONS

| Date | Test Stand Position | No. of test points | $\begin{gathered} \overline{L W C} \\ \left(\mathrm{~g} / \mathrm{m}^{3}\right) \end{gathered}$ | $\begin{aligned} & 95 \% \mathrm{CI} \\ & \left(\mathrm{~g} / \mathrm{m}^{3}\right) \end{aligned}$ | $\begin{aligned} & \overline{M V D} \\ & (\mu \mathrm{~m}) \end{aligned}$ | $\begin{gathered} 95 \% \mathrm{CI} \\ (\mu \mathrm{~m}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ASSP 2 ESTIMATES |  |  |  |  |  |  |
| 1/8/81 | $12^{\prime \prime}$ North | 1 | 0.09 | - | 21 | - |
|  | Center | 5 | 0.17 | 0.10-0.25 | 23 | 19-27 |
|  | $12^{\prime \prime}$ South | 1 | 0.11 | - | 19 | - |
|  | BOEING VERTOL - ASSP ESTIMATES |  |  |  |  |  |
| 10/30/79 | 24" North | 1 | 0.60 | - | 17 | - |
|  | Center | 1 | 0.88 | - | 19 | - |
|  | 24" South | 1 | 0.87 | - | 19 | - |

conclusions can be given. However, based on the statistics given for the PMS probe measurements on cloud repeatability, it is strongly inferred that the LWC and MVD estimates at the given test stand positions were also not significantly different. These inferences are strongly substantiated by a large number of tests conducted by NASA IRT engineers during February 1981. In these independent tests, vertical bars (2 inch cylinders, 6 ft long) were placed at nine locations across the 9 ft width of the tunnel. Ice accretion was measured on these bars at a number of heights for several cloud and air speed settings. Since tunnel velocity remains essentially constant in the test section except for distances within 6 inches of the walls, cloud uniformity can be determined from contour plots of ice accretion. Based on these test results, NASA engineers concluded that the clouds remain uniform $( \pm 10 \%)$ in an approximate 2 ft high by 3 ft wide center section of the tunnel.

### 4.3 Effect of Steam Tube Wraps

The series of tests (210-217) conducted on 8 June 1981 were specifically designed to determine whether or not the steam tube wraps (STW) had any significant effects on the measurement precision of the PMS scattering probes. A total of eight tests were conducted at a given cloud condition and included five test points with the wraps on and three without them. The tests were conducted at two tunnel temperatures; warm ( 23 to $29^{\circ} \mathrm{F}$ ) and cold $\left(-4^{\circ} \mathrm{F}\right)$. Test point 217 which was made without the wraps at the warm condition was rejected from the analysis. Subsequent rapid heating of the tunnel after an approximately two hours operation at the cold temperatures resulted in severe underestimating of particle sizes by both PMS probes due to fogging of the optics.

Table 4-4 presents a summary of the measurements. For a given probe, the LWC estimates from measurements made without the STW are shown to be within the range of those made with the STW and therefore the small differences ( $\pm 5$ percent) in the averages shown are considered insignificant. In comparing the estimates of MVD, no difference is indicated in the FSSP measurements while only a one micron or 5 percent difference is indicates in the

ASSP measurements. Since this 5 percent difference in MVD is similar in magnitude to the test point to test point variations given in Table 4-2, it is also considered insignificant. It is therefore concluded that the STW did not affect the measurement accuracy of these scattering probes as expected.

Table 4-4
SUMMARY OF PMS PROBE MEASUREMENTS WITH AND WITHOUT STEAM TUBE WRAPS

|  | $\begin{aligned} & \text { Temper- } \\ & \text { ature } \\ & \text { ( } \left.{ }^{\circ} \mathrm{F}\right) \\ & \hline \end{aligned}$ | Steam Tube Wrap |  |  |  | $\begin{gathered} \hline \text { FSSPI }{ }^{\top} \\ \text { MVD } \\ (\mu \mathrm{m}) \\ \hline \end{gathered}$ | $\begin{gathered} \text { ASSP2' }^{\top} \\ \text { MVD } \\ (\mu \mathrm{m}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 210 | 29 | ON | 0.71 | 0.71 | 2.61 | 22 | 21 |
| 211 | 23 | ON | 0.77 | 0.82 | 2.39 | 22 | 20 |
| 212 | -4 | ON | 0.77 | 0.78 | 2.19 | 22 | 21 |
| 213 | -4 | ON | 0.80 | 0.77 | 2.26 | 22 | 21 |
| 214 | -4 | ON | 0.83 | 0.76 | 2.17 | $\underline{22}$ | 21 |
| Average |  |  | 0.78 | 0.77 | 2.32 | 22 | 21 |
| 215 | -4 | OFF | 0.77 | 0.73 | 2.48 | 22 | 22 |
| 216 | -4 | OFF | 0.75 | 0.72 | 2.41 | $\underline{22}$ | $\underline{22}$ |
| Average |  |  | 0.76 | 0.73 | 2.45 | 22 | 22 |
| \% Diff $=$ | $\left(\frac{O N-O T F}{O N}-1\right.$ | $\times 100$ | 4 | 5 | -5 | 0 | -5 |

Time plots of probe estimates of LWC and MVD for tests conducted at $-4^{\circ} \mathrm{F}$ with and without the STW are presented in Figures $4-5$ and $4-6$, respectively. Although degradation is shown in the ASSP measurements in both tests, the adverse effect of not having the STW is shown (Figure 4-6) at approximately 240 seconds into the run when ice buildup practically disabled the probe. For the FSSP probe, no apparent change (compared to the J-W trace)
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(n) $\square \triangle \mathcal{W}$
is indicated with time in the test without the STW. However, some deterioration is shown in the measurements with the STW. The far greater deterioration in the ASSP was caused by interference to the laser beam from icing over of the water deflector protrusion which was located near the tip of the laser and withim its sampling tube. The FSSP devices do not have these obstructions in the sampling tube. To relieve this problem in some of the ASSP devices, the deflector pieces have since been removed and replaced functionally by wam air flow through a purge iine terminating at the base of the sampling tube. As expected, since mass is proportional to the cube of particle size, probe icing is shown to result in greater underestimations of LWC than of MVD. In the extreme case shown of the ASSP measurements in Figure 4-6, a decrease of more than one order of magnitude is indicated ( 270 sec ) in the LWC estimate for a factor of two underestimation in MVD. For the FSSP estimates shown in Figure 4-5, the $2 \mu \mathrm{~m}$ or 10 percent change in MVD corresponds to a reduction in LWC of about 30 percent. Hence, duriñ̄ nommal use and especially during moderate to severe natural icing conditions, it is indicated that the probe estimates of particle sizes or MVD would tend to be more precise than of the higher moment related parameters such as LWC.

### 4.4 Effects of Temperature and Velocity on Probe Performance

Of concern to users is knowledge of the measurement accuracy of the various cloud instruments under various operating and environmental conditions. The IRT provided opportunities to investigate two possible problem areas; namely the effects of temperature and velocity on instrument performance. Studies by NASA LeRC personnel suggest that all ice accretion instruments including the Leigh IDS systematically underestimated LWC at temperatures near the freezing point of water. This decrease in accuracy has been attributed to the Ludlam Limit which is associated with a condition where less than i00 percent of the supercooled deposits freeze upon impact as a result of heating caused by the release of the latent heat of fusion. Primary factors which determine the Ludlam Limit on the device are the ambient temperature, collection rate and perhaps droplet sizes. Since higher numbers of observations were taken during the January program, it seemed appropriate to further examine this effect. Unfortunately, the tests were conducted at temperatures
which were either much warmer than the operating limit ( $\left\langle 32^{\circ} \mathrm{F}\right)$ of the device or much colder ( $\left\langle 17^{\circ} \mathrm{F}\right.$ ) than the temperature range of 20 to $32^{\circ} \mathrm{F}$ where instrument accuracy was suspect.

For wiers with turbojet aircraft, information on the accuracy of the spectrometer measurements at airspeeds close to and beyond the upper limit set for by the manufacturer of about $250 \mathrm{Kts}(\sim 285 \mathrm{mph}$ ) is also desired. of particular interest is to what degree are the particles undersized at or beyond the upper velocity limit. Unfortunately, tunnel blockage by the test stand and associated hardware limited top airspeeds to approximately 285 mph . Nevertheless it was still felt worthy of investigation.

In order to evaluate both of these effects on measurement precision, absolute standards must first be known. In both of these investigations, the cloud LWC and MVD set forth by the tunnel operating equations (Section 3.0) were chosen as references. Since the operating equations indicate that the cloud LWC and MVD are also dependent on tunnel velocity, and since ony a few runs were made at a fixed cioud condition but with varying temperature, the ratios of the estimates to those given by the operating equations were stratified into given velocity and temperature ranges for evaluation. Table 4-5 presents the stratification intervals used in the evaluation with accompanying index values.

Table 4-5
DATA STRATIFICATIONS

| Index | TEM (F) | TAS (MPH) |
| :---: | :---: | :---: |
| 1 | $s-16$ | 50 |
| 2 | -15 to -6 | 100 |
| 3 | -6 to 0 | 150 |
| 4 | 0 to 10 | 200 |
| 5 | 10 to 20 | 225 to 275 |
| 6 | 20 to 30 | $>275$ |
| 7 | $>30$ | - |

The results of this evaluation procedure are presented in Figure 4-7 for measurements taken with the leigh and J-W devices, The means and standard deviations (error bars) are plottid against the corresonding index values. For the Leigh measurements, no systematic change with temperature increase is shown in the mean ratio values as expected. Except for the observations made at a tunnel velocity of 50 mph , the remaining average ratio values display no apparent dependency on velocity. At the lowest tunnel velocity, the Leigh device consistently underestimated the tunnel values. The random fluctuations of the means also indicate that the J-W estimates were not affected by the tunnel temperatures. Although a general increase in the values of the means is shown with speed increase, the wide error bars indicate that the effects of tunnel velocity were insignificant. These observations are consistent with the few runs made at fixes temperature and pressure settings but at varying tunnel velocities. Plots of these test point estimates for both these devices appear in Figure 4-8.

In the MVD evaluations (Figure 4-9) of the PMS probe measurements, the means also remain fairly constant indicating that temperature changes did not bias these estimates. However, the means are shown to increase systematically with increases in tuesel velocity. This dependency is further exemplified in Figure 4-1.0 from the test series conducted at fixed temperature and pressure settings and show that while the tunnel values based on the operating equations gradually decrease with speed increase, the probe estimates remain fairly constant for speeds exceeding about 100 to 150 mph . Although these comparisons may perhaps suggest possible bias in the probe estimates, they may likewise infer possible errors in the operating equations. Discussions on these comparisons are presented in the following section.

[^1]

Figure 4-7. AIR SPEED AND TEMPERATURE EFFECTS ON PROBE ESTIMTES OF LWC


Figure 4-8. VELOCITY EFFECTS ON PROBE ESTIMATES OF LWC FOR GIVEN SPRAY SETTINGS

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Figure 4-9. AIR SPEED AND TEMPERATURE EFFECTS ON PROBE ESTIMATES OF MVD


Figure 4-10. VELOCITY EFFECTS ON PROBE ESTIMATES OF MVD FOR GIVEN SPRAY SETTINGS

Table 4-6
INSTRUMENT COMPARISONS
LINEAR REGRESSION ANALYSIS SUMMARY

$$
y=a+b x
$$

| Instruments | $n$ | $a$ | $b$ | $r$ | $e$ | Compar- <br> $i s o n s ~$ |
| :--- | ---: | :---: | :---: | :---: | :---: | :---: |
| J-W vs Tunnel* | 80 | 0.75 | 0.24 | 0.28 | 0.26 | LWC |
| Leigh vs Tunnel | 154 | 0.39 | 0.60 | 0.79 | 0.21 | LWC |
| Leigh vs J-W | 57 | 0.45 | 0.61 | 0.51 | 0.25 | LWC |
| PMS vs Tunnel | 121 | 0.17 | 0.55 | 0.58 | 0.72 | LWC |
| FSSP 1 vs Tunne1 | 37 | 0.21 | 0.09 | 0.65 | 0.09 | LWC |
| ASSP 1 vs Tunne1 | 22 | 0.02 | 1.28 | 0.87 | 0.37 | LWC |
| ASSP 2 vs Tunnel | 10 | -0.01 | 0.57 | 0.95 | 0.27 | LWC |
| ASSP 3 vs Tunne1 | 29 | 0.34 | 0.81 | 0.87 | 0.51 | LWC |
| ASSP 4 vs Tunnel | 23 | -0.51 | 0.81 | 0.89 | 0.21 | LWC |
| PMS vs PMS | 121 | 0.0 | 1.00 | 0.65 | 0.66 | LWC |
| PMS vs Tunnel | 121 | 13.1 | 0.50 | 0.57 | 2.6 | MVD |
| FSSP 1 vs Tunne1 | 37 | 15.6 | 0.47 | 0.69 | 1.8 | MVD |
| ASSP 1 vs Tunne1 | 22 | 12.8 | 0.39 | 0.62 | 1.8 | MVD |
| ASSP 2 vs Tunne1 | 10 | 10.2 | 0.60 | 0.96 | 0.9 | MVD |
| ASSP 3 vs Tunne1 | 29 | 13.4 | 0.50 | 0.50 | 3.3 | MVD |
| ASSP 4 vs Tunne1 | 23 | 8.7 | 0.70 | 0.78 | 1.8 | MVD |
| PMS vs PMS | 121 | 0.0 | 1.00 | 0.79 | 1.9 | MVD |

*The tunnel estimates are based on the IRT operating equations.

1. $\quad n=$ number of data pairs.
2. $a=$ intercept of the linear equation of the form $y=a+b x$.
3. $b=$ slope of linear equations.
4. $r=$ correlation coefficient.
5. $\quad e=$ standard deviation of regression.

It is noted that for a given comparison, the estimates from the instrument listed first represent the dependent variables, while the estimates of the instrument listed second represent the independent variables. Hence, for the listed instruments, Leigh versus J-W, $y$ and $x$ are represented, respectively by the measurements from the Leigh and J-W devices. For these comparisons, the tunnel values were determined from the IRT operating equations.

Comparisons with the Leigh and J-W devices included all of the accepted test point estimates. The PMS scattering probe comparisons, however, included only those measurements from given tunnel conditions (fixed airspeed and pressure settings) where the measurements from at least two different probes were deemed acceptable. This compromised data selection was used since comparisons between probes should be made of clouds having common microphysics properties and since only a few (four) sets of acceptable measurements from all five of the PMS probes were obtained under the same tunnel or cloud conditions. Based on this data selection criteria, measurements from 37 different tunnel conditions were compared. In addition, for each tunnel condition, the data from each probe is represented by the average of the corresponding test point estimates.

Scatter diagrams comparing the LWC measurements from the Leigh and J-W devices against the tunnel estimates (IRT LWC) and against each other are presented in Figures $4-11$ to $4-13$ and show that the measurements are generally in agreement with the calibrations performed with the rotating cylinders. As compared to the tunnel values, the measurements from both instruments are shown to fall on either side of the one-to-one line for IRT LWC of less than about $2 \mathrm{~g} / \mathrm{m}^{3}$. Larger scatter is also evident of the $\mathrm{J}-\mathrm{W}$ measurements in this range as is also indicated from the larger values $n f$ e listed in Table 4-6. For IRT LWC exceeding $2 \mathrm{~g} / \mathrm{m}^{3}$, the measurements from both instruments fall below


[^2]$\left(\varepsilon{ }^{\omega / \sigma}\right)$ วMา Mг

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 figure 4-13. scac $\left(\mathrm{g} / \mathrm{m}^{3}\right.$ )

the one-to-one line. For the Leigh measurements plotted at the IRT LWC of $2.58 \mathrm{~g} / \mathrm{m}^{3}$, the two lowest estimates were taken at a tunnel velocity of 50 mph where the device consistently underestimated the tunnel values. At the IRT LWC setting of $2.41 \mathrm{~g} / \mathrm{m}^{3}$, the underestimations from the Leigh device is considered to have been caused by incomplete droplet freezing. Although not consistent with the total data set, the decrease with temperature increase (from 4 to $16^{\circ}$ F) at this relatively high LWC condition suggests that the Ludlam Limit was reached at temperatures much colder than observed in the earlier program. This inference is not inconsistent with the observations made at the higher IRT LWC setting of $2.58 \mathrm{~g} / \mathrm{m}^{3}$ and the identical tunnel velocity of 100 mph since the tunnel temperatures were much colder ( $-12^{\circ} \mathrm{F}$ ). Studies are currently being actively pursued by NASA LeRC personnel on the heat balance of the Leigh device and should provide more definite answers on the various causal relationships associated with the Ludlam Limit. For the J-W measurements taken at these two higher LWC settings, it is found that the ciouds were characterized by relatively large particles (MVD $\sim 25 \mu \mathrm{~m}$ ) and, therefore, the device would be expected to underestimate the true LWC. It is also noted that the instrument performed rather intermittently (CV ~20\%) at the $2.41 \mathrm{~g} / \mathrm{m}^{3}$ tunnel setting and hence the test point estimate (or mean) would also be low.

As compared to the tunnel estimates, the reduced scatter of the $\mathrm{J}-\mathrm{W}$ points from the line of equality in the comparison diagram with the Leigh device suggests that part of the scatter results from the uncertainty of the operating equations. This observation is reflected in the higher correlation coefficient listed for the comparisons between the two instruments. It is further noted that the J-W measurements were generally lower than those of the Leigh device.

The comparisons of the LWC estimates between the scattering probes and the tunnel are less encouraging as indicated by the wide range of values listed for the intercept and slope of the regression equation and by the corresponding scatter diagrams presented in Figures 4-14 to 4-18. The estimates from the individual probes either systematically overestimated or underestimated the the tunnel values and strongly suggests that in all but the estimates from FSSP 1, the discrepancies resulted primarily from uncertainties in their effective sampling areas. It is noted that at the two highest tunnel settings

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Figure 4-17. SCATTER diAgram of assp 3 LWC yersus irt lhc

(LWC $>4 \mathrm{~g} / \mathrm{m}^{3}$ ), significant amounts of water existed in particles having sizes much larger than the upper size limit of these probes and therefore the probe estimates should be considered invalid. The weak dependency exhibited between the estimates of FSSP 1 and the tunnel may have perhaps resulted from a malfunction in its velocity reject circuit which was discovered during the program. When viewed (Figure 4-19) collectively, it is found that the individual probe estimates vary by large amounts. Although part of the scatter may be due to uncertainties in the absolute calibrations of the spray clouds, the variations between the individual probe estimates at given tunnel settings still remains large as shown in Figure 4-20. In this plot, the probe values are plotted against the means of the individual probe estimates for given tunnel settings.

Although the data can be shown to be compatible to the tunnel values by applying appropriate correction factors, these results which were based upon use of the manufacturer's specifications, clearly indicate that if the sizedistribution measurements are used to estimate their bulk parameters (e.g., LWC), the probes should be calibrated against known standards. Also, due primarily to possible deterioration in measurement precision due to probe icing, it is further indicated that instruments such as the Leigh IDS or J-W device which make direct measurements of the integrated spectrum be used to complement the measurements. The relatively higher measurement precision offered by these accretion devices is indicated in Figures 4-21 and 4-22 which show that the average test point values for the given tunnel settings fall on the one-to-one line with a minimal amount of scatter. Of these two comparisons, the average measurements from the Leigh IDS shows greater precision and reliability.

The average MVD estimates for the given tunnel settings for each of the probes are plotted against the corresponding tunnel estimates in Figure 4-23. Wide deviations appear in the tunnel size range of from about 10 to $20 \mu \mathrm{~m}$ where the measured estimates are shown to be significantly larger. A closer correspondence is exhibited at the larger tunnel sizes. These observations are reflected in the best fit values given for the coefficients of the individual probe comparison equations in Table 4-6 which shows large intercept values ( $8-15$ ) and relatively small slope estimates of between 0.4 to 0.7 . When the

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probe estimates are collectively compared against the tunnel estimates (PMS vs Tunnel), it is shown that not only does the correlation decrease but that the scatter (e) also increases significantly.

Figure 4-24 presents comparisons of the probe estimates against their averages for given tunnel settings (PMS vs $\overline{P M S}$ ) and shows that the estimates were in most cases (112 of 121 or 93 percent) within $\pm 3 \mu \mathrm{~m}$ of each other. This error is consistent with the accuracy claimed by the manufacturer of the glass bead calibrations of $\pm$ one channel band width, which for these probes were between 3 to $3.5 \mu \mathrm{~m}$. It is noted that part of LWC variations between the probe estimates can be attributed to these differences although not to the large extent shown in the LWC comparison plot against the tunnel values. Thus, although the measurement accuracy of the probes may be questioned from the comparisons presented in Figure 4-23, the good agreement found between the individual probes suggests that the MVD calibrations performed by the rotaing cylinders may perhaps have been in error for some of the tunnel settings. Part of the disagreement between the probe and rotating cylinder estimates results from the fact that the probe MVD estimates did not decrease with tunnel velocity increase as indicated by the operating equations. Unfortunately, the documentation of the procedures used in determining the MVD from the rotating cylinders was not available for this study and, therefore, further evaluations of the disagreement cannot be pursued.

Figure 4-25 presents exampies of measurements taken at a given tunnel setting by all five of the scattering probes. The volume or mass distributions have been modified to account for measurement differences in LWC and in MVD by plotting the percentage mass in each of the channels against the scaled particle diameter, D/MVD. Although the individual probe measurements have been normalized for these differences, it is shown that significant measurement differences can stiil exist. Whereas the distributions from probes ASSP 1, ASSP 2, and ASSP 3 can be considered as being comparable to each other, those from FSSP 1 and ASSP 4 are not. Hence it is strongly suggested that calibration procedures be upgraded to also include means to evaluate the shape or form of the size distribution measurements.

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Figure 4-25. NORMALIZED MASS DENSITY VERSUS SCALED PARTICLE dIAMETER DISTRIBUTIONS TAKEN AT A GIVEN TUNNEL SETTING BY INDICATED PROBES

Of general interest to this study was the determination of a distribution function which best described the droplet size distribution measurements. For this purpose, the applicability of the gamma, log-normal, and Langmuir distribution functions were investigated. The approach consisted of evaluating the goodness of fit of the PMS probe measurements with the assumption that the given distribution functions were valid. The following presents brief descriptions of these functions and procedures used in their evaluation.

### 4.6.1

Gamma Distribution Function (GD)
The gamma distribution function is described by three parameters and is given as:

$$
\begin{align*}
N_{D} & =N_{0}\left(\frac{D}{D_{*}}\right)^{\alpha} \exp (-\lambda D) & & \text { for } D>0  \tag{1}\\
& =0 & & \text { for } 0 \leq 0
\end{align*}
$$

where
$N_{D} \Delta D=$ number density between $D$ and $D+\Delta D$
$D \quad=$ droplet diameter
$N_{0}=$ displacement parameter, $N_{0}>0$
$\alpha \quad=$ curvature parameter, $\alpha>-1$
$\lambda \quad=$ scale parameter, $\lambda>0$
$D_{\star} \quad=$ unit constant

A desirabie feature of the GD is the ease at which moment related bulk parameters of the distributions can through simple integration be resolved. Some of these parameters include:
a. Total number density, $\mathrm{N}_{\mathrm{T}}$

$$
\begin{aligned}
N_{T} & =\int_{0}^{\infty} N_{D} d D=N \int_{0}^{\infty} D^{\alpha} \exp (-\lambda D) d D \\
& =\frac{N \Gamma(\alpha+1)}{\lambda^{\alpha+1}}
\end{aligned}
$$

where I represents the gamma function and $N$ for mathematical convenience represents $N_{0} / D_{\star}^{\alpha}$.
b. Total volume density, M

$$
\begin{aligned}
M & =\int_{0}^{\infty} N_{D} D^{3} d D=N \int_{0}^{\infty} D^{\alpha+3} \exp (-\lambda D) d D \\
& =N \frac{\Gamma(\alpha+)}{\lambda^{\alpha+4}}
\end{aligned}
$$

c. Liquid water content, LWC

$$
L W C=\frac{\pi}{6} \rho_{W} M
$$

d. Reflectivity factor, $Z$

$$
\begin{aligned}
Z & =\int_{0}^{\infty} N_{D} D^{6} d D \\
& =N \frac{\Gamma(\alpha+7)}{\lambda^{\alpha+7}}
\end{aligned}
$$

Another feature of the GD is that the MVD (or $D_{0}$ ) of a given droplet size distribution is uniquely defined by the curvature and scale cosfficients as follows:

$$
\begin{equation*}
M V D=D_{0} \equiv(\alpha+3.67) / \lambda \tag{2}
\end{equation*}
$$

Since the GD is described by three parameters any three moment related bulk parameters of a given DSD may be used to estimate their values (Takeuci?: 1978). However, this method commonly referred to as the moment technique may also be inefficient and therefore iteration techniques which minimize the variance of the data points about their estimates can also be used.

The GD can also be normalized to account for sample to sample variations in the values of the descriptive coefficients by the following algebraic manipulations to Eq. 1 and use of the indentity given by Eq. 2.

$$
\begin{gather*}
\frac{N_{D}}{D^{\alpha}}=N \exp (-\lambda D)  \tag{3}\\
\frac{N_{D}}{D^{\alpha_{N}}}=\exp (-(\alpha+3.67) D / D 0) \\
\ln \left(\frac{N_{D}}{D^{\alpha} N}\right) /(\alpha+3.67)=-D / D_{0} \tag{4}
\end{gather*}
$$

or

$$
\begin{equation*}
Y=-D / D_{0} \tag{4}
\end{equation*}
$$

It is indicated by Eq. 4 that if the DSD measurements ( $N_{D}$ ) adhere to the $G D$, then plots on a linear graph between the unitless expressions given to the left of the equal sign and the scaled particle diameter $D / D_{0}$ will result in data points falling along a straight line having intercept and slope values of 0 and -1 , respectively.

For each DSD measurement, the descriptive coefficients of the GD were determined by the two different techniques mentioned earlier. Hence: two separate evaluations on the applicability of the GD were performed. To improve upon the efficiency of the moment technique (Gamma I), four moment related parameters were employed and cansisted of the following computational procedures.

$$
\begin{equation*}
\alpha=\frac{-b-\sqrt{b^{2}-4 a c}}{2^{a}} \tag{5}
\end{equation*}
$$

where

$$
\begin{aligned}
& \mathrm{a}=1-\mathrm{Q} \\
& \mathrm{~b}=11-5 \mathrm{Q} \\
& \mathrm{c}=30-6 \mathrm{Q} \\
& \mathrm{Q}=\frac{\mathrm{LZ}}{M F} \\
& \mathrm{~L}=\sum_{\mathrm{i}}^{\mathrm{\Sigma}}=1 \mathrm{~N} \mathrm{~N}_{\mathrm{i}} \mathrm{D}_{\mathrm{i}}
\end{aligned}
$$

$$
\begin{align*}
& M=\sum_{i=1}^{15} N_{i} D_{i}^{3} \\
& F=\sum_{i=1}^{\Sigma} N_{i} D_{i}^{4} \\
& Z=\sum_{i=1}^{=} N_{i} D_{i}^{6} \\
& \lambda=[(\alpha+6)(\alpha+5)(\alpha+4)(\alpha+3)(\alpha+2) L / Z]^{1 / 5}  \tag{6}\\
& N_{0}=\frac{M \lambda^{\alpha+4}}{\Gamma(\alpha+4)} \tag{7}
\end{align*}
$$

The second method (Gamma II) consisted of performing iterations on the linearized form of the GD given by Eq. 3.

$$
\begin{equation*}
\frac{N_{D}}{D^{\alpha}}=N \exp (-\lambda D) \tag{3}
\end{equation*}
$$

or

$$
\begin{equation*}
y=N^{\prime}-\lambda D \tag{3a}
\end{equation*}
$$

where

$$
\begin{aligned}
& y=\ln N_{D}-\alpha \ln D \\
& N^{\prime}=\ln N_{0}
\end{aligned}
$$

Equation 3a serves as the basis from which simple linear regression analyses (method of least squares) resolves unbiased estimates of the descriptive coefficients. The iterative technique (see Takeuchi and Chein, 1079 for further details) basically seeks a value of $\alpha$ for which the standard deviation of regression is minimized. Once minimized, values for $N_{0}$ and $\lambda$ are determined from the "best fit" estimates of the intercept ( $N_{0}=\exp \left(N^{\prime}\right)$ and slope, respectively. In this study, $\alpha$ computed from Eq. 5 served as the initial value in the iteration process. The MVD is defined by Eq. 2 in both techniques.

### 4.6.2 Log-normal Distribution, LN

If the volume (or mass) distributions are assumed to be log-normal, then the probability density function $p(D)$ is given as:

$$
\begin{equation*}
p(D)=\frac{1}{\sigma \sqrt{2 \pi}} \exp \left[-\left(\frac{\ln D-\ln D_{g}}{\sqrt{2} \sigma}\right)^{2}\right] \tag{8}
\end{equation*}
$$

where

$$
\begin{aligned}
p(D) \cdot \ln \left(\frac{D+\Delta D}{D}\right) & =\text { normalized volume density between } D \text { and } D+\Delta D, \\
& =\text { geometric mean diameter or antilog of average } \ln D \\
& =\text { standard deviation of } \ln D
\end{aligned}
$$

In order to objectively compare the goodness of fit of the measurements against that of the GD it is mandatory that Eq. 8 be linearized as follows:

$$
\begin{aligned}
& \ln (\sigma \sqrt{2 \pi} p(D))=-\left(\frac{\ln D-\ln D_{g}}{\sqrt{2} \sigma}\right)^{2} \\
& -2 \sigma^{2} \ln (\sigma \sqrt{2 \pi} p(D))=\left(\ln \frac{D}{D_{g}}\right)^{2} \\
& \pm\left[-2 \sigma^{2} \ln (\sigma \sqrt{2 \pi} p(D))\right]^{1 / 2}=\ln \frac{D}{D_{g}}
\end{aligned}
$$

or

$$
\begin{gathered}
\pm Y^{\prime}=\ln \frac{D}{D_{g}} \\
\exp \left(-Y^{\prime}\right)=D / D_{g} \text { for } D / D_{g} \leq 1
\end{gathered}
$$

and

$$
\begin{align*}
\exp \left(Y^{\prime}\right) & =D / D_{g} \text { for } D / D_{g}>1 \\
Y & =D / D_{g}=D / D_{0} \tag{9}
\end{align*}
$$

It is so indicated by Eq. 9 that if the volume distributions are in fact log-normal, the plots on a linear graph between the unitless expression given to the left of the equal sign and the scaled particle diameter $D / D_{g}$ will result in data points falling along a straight line having intercept and slope values of 0 and 1 , respectively. Also, since the volume frequency distribution is symmetrical about its geometric mean, the MVD is also identified by $\mathrm{D}_{\mathrm{g}}$.

It is further indicated that except for the difference in the sign of the slope, the values for both the intercept and slope and the expression, $D / D_{0}$, given to the right of the equal sign in both linearized forms of the GD and LN equations are identical. Hence, the goodness of fit of given measurements can be evaluated and objectively compared bętween the two assumed distribution functions by evaluating the root mean square (RMS) error of the data points from the straight lines.

The coefficients of the LN and normalized volume density ( $V_{i}$ ) were determined from each of the probe measurements by the following equations:

$$
\begin{gather*}
V_{i}=\frac{N_{i} D_{i}^{3}}{\sum_{i=1}^{\Sigma} N_{i} D_{i}^{3}}  \tag{10}\\
\ln D_{g}=\sum_{i=1}^{=15} V_{i} \ln D_{i}  \tag{11}\\
\sigma=\left[\sum_{i \stackrel{1}{=} 1}^{\sum}\left(V_{i} \ln D_{i}-\ln D_{g}\right)^{2}\right]^{1 / \tau} \tag{12}
\end{gather*}
$$

4.6 .3

Langmuir Distributions
The Langmuir distributions are assumed normalized volume densi'y distributions about the scaied particle diameters $D / D_{0}$ as given (Langmuir and 8lodgett, 1945) below:

## Table 4-7

FOUR ASSUMED DSD

| LWC <br> $(\%)$ | $B$ <br> $D / D_{0}$ | $C$ <br> $\left(D / D_{0}\right)^{1.5}$ | $D$ <br> $\left(D / D_{0}\right)^{2.0}$ | $\left(D / D_{0}\right)^{2.5}$ |
| ---: | :---: | :---: | :---: | :---: |
| 5 | 0.56 | 0.42 | 0.31 | 0.23 |
| 10 | 0.72 | 0.62 | 0.52 | 0.44 |
| 20 | 0.84 | 0.77 | 0.71 | 0.65 |
| 30 | 1.00 | 1.00 | 1.00 | 1.00 |
| 20 | 1.17 | 1.26 | 1.37 | 1.48 |
| 10 | 1.32 | 1.51 | 1.74 | 2.00 |
| 5 | 1.49 |  | 2.22 | 2.71 |

Common to these distributions is the given normalized volume density versus scaled midpoint diameter relationship of the $B$ distribution. The remaining distributions are defined by different power values to which $D / D_{0}$ of the $B$ distribution is raised. Hence the Langmuir distributions are defined as a single parameter distribution function.

Based on these considerations, the evaluation of the goodness of fit consisted of first determining the power values along given points of the normalized cumulative mass distribution of a given DSD measurement and second, computing the normalized RMS error of these values. The points along the normalized cumulative mass distribution were chosen to be at the midpoints as well as the intermediate points of the normalized volume distributions given in Table $0-7$ and are listed in Table $4-8$ along with the corresponding scaled diameters (DB) of the $B$ distribution. Given $D_{0}$, the determination of the power vaiues at each of base 12 points ( $K$ ) consisted of the following procedures:
a. Determine through linear interpolation, the diameter, $D_{K}$, at which the given percentage was found.
b. Establish a scaled diameter, $D S_{K}=D_{K} / D_{0}$ "

| Cumulative <br> LWC <br> $(\%)$ | $D B$ <br> $\left(D / D_{0}\right)$ | Cumulative <br> LWC <br> $(\%)$ | $D B$ <br> $\left(D / D_{0}\right)$ |
| :--- | :---: | :---: | :--- |
| 2.5 | 0.56 | 65 | 1.085 |
| 5 | 0.64 | 75 | 1.17 |
| 10 | 0.72 | 85 | 1.245 |
| 15 | 0.78 | 90 | 1.32 |
| 25 | 0.84 | 95 | 1.405 |
| 35 | 0.92 | 97.5 | 1.49 |

c. From the corresponding scaled diameter ( $D \mathrm{~B}_{\mathrm{K}}$ ) of the B distribution given in Table 4-8 determine the power value ( $E_{K}$ ) by the following equation:

$$
\begin{equation*}
E_{k}=\frac{\log _{10}\left(D S_{k}\right)}{\log _{10}\left(D B_{k}\right)} \tag{13}
\end{equation*}
$$

Given a number of DSD measurements, the normalized RMS error as defined by the following equation:

$$
\text { RMS }=\left[\begin{array}{cc}
n & \sum^{12}  \tag{14}\\
1 & k=1
\end{array}\left(\frac{E_{K}-\bar{E}}{\bar{E}}\right)^{2} / 12 n\right]^{1 / 2}
$$

Since the Langmuir distributions are characterized by a single parameter, the deviations of the power values from their mean value at the given frequencies essentially provide a measure of the goodness of fit. In Eq. 14, the deviations are also normalized to their paramter estimates (or mean power values) as done in the RMS error determinations of the linearized froms of the gamms and lognorial distribution functions. Hence, the applicability of the three distribution functions can be abjectively evaluated by comparing their RMS error estimates from a given set of DSD measurements.

### 4.6.4 Normalized DSD

Figures 4-26 to 4-32 present plots of the DSD measurements normalized to the three distribution functions. For the mere purpose of having the normalized measurements be inversely related to the scaled particle diameters as in the linearized GD plots, negative values of the normalized measurements $(Y)$ of the LN are plotted against the scaled diameters. The normalized deviations of the power values of the Langmuir distributions are also plotted with respect to the normalized line of the GD and at the corresponding scaled diameters found for the given cumulative volume frequencies.

Based on the least amount of scatter shown of the points about its straight line, it is indicated that the gamma distribution function best describes the measurements. These observations are reflected in the RMS errors listed in Table 4-9 for each of the assumed distribution functions. For the evaluations based on the entire spectra, it is shown that the RMS errors associated with the GD are lower than those of the LN by a factor of about 2. Ailso, of the two techniques used in estimating values for the descriptive coefficients of the GD, the estimates based on the iterative method resulted in slightly smaller errors as would be expected. In comparing the resulting errors between the three distribution functions for the mid-channel measurements, the average error resulting from the GD (Gamma I) approximation is shown to be lower than those associated with the Langmuir and LN assumptions by factors of 2 and 3 , respectively. Although a slightly larger average RMS error is indicated from use of the Gamma II estimations of the descriptive coefficients, the difference is considered to be negligible.

### 4.6.5 Comparisons with DSD from Natural Clouds

Based on the close adherence shown of the measurements to the GD, it can be stated that the GD adequately describes the probe measurements taken in the IRT. Hence given DSD may be compared through their coefficient values provided that they all confirm to the GD. Figure $4-33$ presents plots of measurements iaken in natural clouds which have been normalized to the three assumed distributions and shows that these measurements are also best described by the GD. Characteristics of the ten DSD are summarized in Table 4 m 10 which also includes evaluations of the goodness of fit. Since it has been


Figure 4-26. NORMALIZED DSD FROM FSSP I


Figure 4-27. NORMALIZED DSD FROM ASSP 1


Figure 4-28. NORMALIZED DSD FROM ASSP 2


Figure 4-29. NORMALIZED DSD FROM ASSP 3


Figure 4.30. NORMALIZED DSD FRDM ASSP 4


Figure 4-31. NORiAALIZED DSD FROM FSSP $1^{\prime}$


Figure 4-32. NORMALIZED DSD FROM ASSP $2^{\prime \prime}$

Table 4-9<br>IR CLOUD BSD FORM EVALUATION

RMS Error ( $100 \%$ LWC) for Given DSD Form




Figure 4-33. NORMALIZED DSD OF NATURAL CLOUDS
Table 4-10


shown that the estimates of LWC and MVD from the individual probe measurements differ under given cloud conditions, it is indeed difficult to compare the tunnel measurements against those made through the natural clouds. Nevertheless, since absolute differences in the absolute mass distributions can be appropriately normalued and since the displacement coefficient, $N_{0}$, is essentially removed in the volume frequency versus scaled particle diameter distri. butions, it may be appropriate to compare the values found for the curvature $(\alpha)$ and scale $(\lambda)$ parameters between these measurements.

Table 4-11 presents a computer generated summary of the curvature ( $\alpha$ ) and scale ( $\lambda$ ) values of the GD for measurements taken at the various tunnel settings. It is shown that these DSD were characterized by $\alpha$ values ranging from about 1 to 5 and by $\lambda$ values between 0.2 to $0.5 / \mu \mathrm{m}$. Also, for a given tunnel setting, variations in $\alpha$ and $\lambda$ between probes are indicated to be within about $\pm 1$ and $\pm 0.07 / \mu \mathrm{m}$, respectively. In contrast, most of the DSD from the natural clouds shown in Table $4-10$ had curvature values (Gamma II) of between 5 to 10 and $\lambda$ values $\left(\lambda=\frac{\alpha+3.6}{M V D}\right)$ between 0.5 to $1.0 / \mu \mathrm{m}$. These differences are further exemplified in Table 4-12 wnich presents the mean and standard deviations of the data sets. Where the IRT clouds show average $\alpha$ values of aboaut 2.3 to 3.5 , the natural clouds were, characterized by an of 6.8. It is noted that the range of $\alpha$ values from the natural cloud DSD are also consistent with the mean value of 8 found from approximately 500 samples taken with oil slides from natural clouds in Russia (Khrgian, 1963). Figures 4-34 and 4-35 present examples of the measurements used in the comparisons and basically show that except for Test Point 42, the normalized mass of the IRT clouds is distributed over a broader scaled size range. This observation is consistent with the firct that the IRT clouds where generally characterized by smaller curvature and scale values. In any event, the somewhat broader irt drop size spectrum will not have a measurable effect upon the ice accretion, relative to the accretion in natural clouds.

Table 4-11
AVERAGE SPECTRA SHARACTERISTICS
FOR INDICATED IRT SETTINGS AND PROBES




Table 4-12
SUMMARY STATISTICS OF MEAN
AND STANDARD DEVIATIONS ( $\sigma$ )
OF CURVATURE AND SHAPE PARAMETERS

| Probe | $\alpha$ |  | $\lambda(/ \mu \mathrm{m})$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Mean | $\sigma$ | Mean | $\sigma$ |
| FSSP1 | 3.4 | 1.0 | 0.33 | 0.07 |
| ASSP1 | 2.5 | 0.9 | 0.30 | 0.06 |
| ASSP2 | 2.3 | 0.3 | 0.25 | 0.03 |
| ASSP3 | 3.2 | 0.8 | 0.30 | 0.06 |
| ASSP4 | 2.4 | 0.5 | 0.27 | 0.06 |
| Natural Clouds | 6.8 | 1.7 | 0.67 | 0.21 |



Figure 4-34. EXAMPLES OF NORMALIZED MASS DENSITY VERSUS SCALED PARTICLE DIAMETER DISTRIBUTIONS OF IRT CLOUDS


Figure 4-35. EXAMPLES OF NORMALIZED MASS DENSITY VERSUS SCALED PARTICLE DIAMETER DISTRIBUTIONS OF NATURAL CLOUDS
5. CONCLUSIONS

Tests conducted in the NASA LeRC IRT at different air speeds, pressure settings, and temperatures lead to the following conclusions:
A. Instrument Comparisons:

1. There was no apparent velocity effect to the PMS probe measurements at air speeds ranging from 50 to 285 mph .
2. The measurements from the LWC instruments ( $\mathrm{J}-\mathrm{W}$ and Leigh) agreed (little scatter) with each othe and with the IRT calibrations.
3. The five PMS probes gave an excessively wide scatter in estimates of LWC ( 0.2 to 2.0 compared to the IRT setting of $1 \mathrm{~g} / \mathrm{m}^{3}$ ).
4. For given cloud conditions, the estimates of cloud MVD or drop size between the five PMS probes were within $\pm 3 \mu \mathrm{~m}$ of each other in 93 percent of the cases.
5. Significant failure rates were observed of these instruments especially when one considers that the instruments were required to be in proper operating condition for testing. Failure rates of 66 percent and 24 percent were observed in the J-W and Leigh devices, respectively. Failure rates ranging from 100 percent to 2 percent were observed at the six scattering probes installed in the tunnel. Some of the failures can be attributed to hardvare problems (e.g. J-W and all of the measurements from the FSSP 2), while others were related to measurement determination due to probe icing and perhaps to wetting of the optics.
B. Tunnel Concerns:
6. The cloud conditions produced in the IRT are highly repeatable as indicated tiy the values of the coefficient of variation determined for the following evaluations.

Source of Variation

| CV LNC (\%) | CV MVD ( $\%$ ) |  |
| :---: | :---: | :---: |
|  | $\pm 5$ |  |
| $\pm 10$ |  | $\pm 3-3$ |
| $\pm 12$ |  | $\pm 3-7$ |
| $\pm 12$ |  |  |

2. The PMS probe estimates of MVD exceeded those of the tunnel values which were based on rotating cylinder calibarations. The "best fit" regression equation determined between the five PMS probe estimates (PMVD) and the tunnel values (TMVD) is given as:

PMVD $=13.1+0.5$ TMVD
3. As compared to the log normal and Langmuir distribution functions, the gamma distribuation function best describes the drop size distribution measurements from the IRT and natural clouds. The drop size distributions from the IRT were slightly broader than those of the natural clouds as was also indicated by smaller values for both the curvature and scale parameters of the gamma distribution function.

RECOMMENDATIONS
The discrepancies shown between the measurements of the indiviciual probes of given cloud conditions in the IRT strongly set forth the need to establish a test facility(or facilities) where instruments can be calibrated against known cloud standards. Aside from providing means te better define the sample area and band widtn of individual probes, the resulting calibrations would add credibility to the measurements. An icing tunnel such as the IRT used in this study should be considered as a possible test facility in addition to those operated by the National Research Council (NRC) of Canada and by the Arnold Engineering Development Center (AEDC), Arnold AFS in Tennes see.

Due to possible measurement deterioration from probe icing it is recommended that direct LWC measurement devices (e.g., J-W and Leigh) such as used in this study complement the probe measurements during icing certification flights.

Based on the large differences found between the probe and tunnel estimates of cloud MVD, it is suggested that procedures used in estimating the MVD from the rotating cylinder measurements be reevaluated. Specific emphasis should be placed upon evaluating errors resulting from incorrect assumptions on DSD form. Also, the effects of air speed utilized in the present operating equations of the IRT should be reviewed in view of the discrepancies found in this study.

## 7. REFERENCES

Khrgian, A. Kh., Borovikov, A. M., I. I. Gaivoronskii, E. G. Zak, V. V. Kostarev, I. P. Mazin, V. E. Minervin, S. M. Schmeter, 1963: Cloud physics. Published in Israel Program for Scientific Translations. A. Kh. Khrgian, editor.

Knollenberg, R. G., 1970: The optical array: an alternative to scattering or extinction for airborne particle size determination. U. Appl. Met., pp. 501-508.

Langmuir, I. and K. B. Blodgett, 1949: Mathematical investigations of water droplet trajectories. General Electric Res. Lab., Rept. No. RI.-225s Schenectadys N.Y., 47 pp.

Stone, J. M., 1963: Radiation and optics. McGraw-Hill Book Co., 544 pp.
Takeuchi, D. M., 1978: Characterization of raindrop size distributions. From preprints "Conference on Cloud Physics and Atmospheric Electricity," July 31-August 4, 1978. Issaquah, Washington. American Meteorological Society, Boston, Mass.

Takeuchi, D. M., and P. C. Chen, 1979: A technique for determining parameter estimates of the gamma distribution. From preprints "Sixth Conference on Probability and Statistics in Atmospheric Sciences," October 9-12, 1979. Banff, Alta., Canada. American Meteorological Society, Boston, Mass.

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[^0]:    Figure 3-4. EXAMPLE OF TEST POINT SUMMARY

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    Instrument Intercomparisons
    Of primary interest to the total alalyses effort is perhaps the comparability of the measurements from the various instruments. Aside from establishing the compatability of the measurements from given clouds, the measurements also lend means to reevaluate the calibrations performed with the rotating cylinders. Table 4-6 presents regression analysis results (by the method of test squares) for the various instruments listed and includes the following information:

[^2]:    IRT LWC( $\mathrm{g} / \mathrm{m}^{3}$ )
    Figure 4-11. SCATTER DIAGRAM OF J-W LWC VERSUS IRT LWC

