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FINAL REPORT  
BETA SYSTEMS ERROR ANALYSIS

January 26, 1984

Contract No. NAS8-35329



Prepared for

George C. Marshall Space Flight Center  
Marshall Space Flight Center, AL 35812

**Applied Research Inc.**



P.O. Box 11220 • Huntsville, AL 35805 • (205) 837-3600



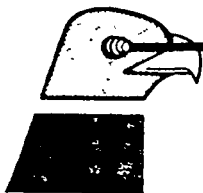
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## TABLE OF CONTENTS

1.0	Introduction.....	1
2.0	Review of the Algorithms for Determining the Backscatter Coefficient.....	2
2.1	Volume Mode Algorithm.....	2
2.2	Single Particle Mode Algorithm.....	7
2.3	Computer Implementation.....	12
2.4	Running the Data Prediction Algorithms.....	26
3.0	Measurement Errors.....	27
3.1	Volume Mode Errors.....	27
3.2	Single Particle Mode Errors.....	33
3.3	Anomalous Cases from Processed Data.....	49
4.0	Conclusions.....	50
	References.....	52
	Appendix.....	53

## LIST OF FIGURES

Figure	Page
1.	Geometry and Coordinates.....4
2.	Peak Signal versus Backscatter Cross-section Diagrams.....10
3.	Longitudinal Profile at 10 Meter Focus.....15
4.	Signal Processor Channel vs. Signal Level.....17
5a.	Flow Chart of Computer Implementation.....20
5b.	Flow Chart of Computer Implementation (con't)...21
6a.	Flow Chart of Computer Implementation of Single Particle Inversion Subprogram OPTIM.....22
6b.	Flow Chart of Computer Implementation of Single Particle Inversion Subprogram OPTIM (con't).....23
7.	Flow Chart of Computer Implementation of Single Particle Inversion Subprogram DATANAL....24
8.	Data Record.....25
9.	Statistical Error in Backscatter Coefficient as a Function of Number of Particles Pro- cessed for Flight 16 (Spike Removed).....44
10.	Statistical Error in Backscatter Coefficient as a Function of Number of Particles Pro- cessed for Flight 16 (with Spike).....45
11.	Statistical Error in Backscatter Coefficient as a Function of Number of Particles Pro- cessed for Flight 9.....46

12.	Backscatter Coefficient	for Flight 4.....	47
13.	Backscatter Coefficient	for Flight 13.....	48

## 1.0 Introduction

Since 1980, personnel of Applied Research, Inc. have supported NASA at Marshall Space Flight Center in the measurement of the atmospheric backscatter coefficient,  $\beta$ , with an airborne CO Laser Doppler Velocimeter (LDV) system operating in a continuous wave, focussed mode. A method, called the Single Particle Mode (SPM) algorithm, has been developed from concept through analysis of an extensive amount of data obtained with the system aboard a NASA aircraft. The SPM algorithm is intended to be employed in situations where one particle at a time appears in the sensitive volume of the LDV. In addition to giving the backscatter coefficient, the SPM algorithm also produces as intermediate results the aerosol density and the aerosol backscatter cross-section distribution.

A second method, which measures only the atmospheric backscatter coefficient, is called the Volume Mode (VM) and was simultaneously employed in obtaining the aforementioned data. The results of these two methods generally differed by slightly less than an order of magnitude. The purpose of this report is to examine the measurement uncertainties or other errors in the results of the two methods.

A review of the basis of each method is given in Section 2, including a discussion of the computer programming implementation of the SPM. A discussion of error inherent in each is given in Section 3, with conclusions summarized in Section 4.

## 2.0 Review of the Algorithms for Determining the Backscatter Coefficient

For convenience, the basis of the VM and SPM algorithms for obtaining the atmospheric backscatter coefficient  $\beta$  is presented here. It will be seen that the VM method works under more general conditions than the SPM method, but that the latter gives more information, namely the aerosol density and backscatter distribution. Each method has its own special calibration requirements.

### 2.1 Volume Mode Algorithm

The VM algorithm will now be derived from the response of the LDV to a single particle in its sensitive volume. This expression will be compared to the well known result for the signal-to-noise,  $S$ , of a focussed, cw LDV operating in the conventional "volume mode" with very many particles in its sensitive volume:

$$S = \beta G_V \text{ where}$$

$$\beta = \int \sigma n(\sigma) d\sigma$$

$$\sigma = \text{single particle backscatter cross-section (m}^2\text{)}$$

$$n(\sigma) = \text{backscatter cross-section distribution (m}^{-5}\text{)}$$

$$G_V = \text{volume mode gain factor determined by calibration (m).}$$

In this derivation, the system will be assumed to be aircraft borne with optical axis perpendicular to the aircraft velocity

vector. In this case each aerosol particle passes through the sensitive volume perpendicular to the optic axis with velocity  $v$ . See Figure 1. A particle at  $x, y, z$  with cross-section  $\sigma$  produces a signal-to-noise at time  $t$  given by

$$S(\sigma, t) = \sigma u(x, y, z)$$

where  $u(x, y, z)$  defines the LDV sensitive volume. That is, requiring  $S > 1$  defines a sensitive volume dependent on  $\sigma$ . Extending this expression to many particles with cross-section  $\sigma$  moving in the positive  $x$  direction, each with initial position  $x_{0i}$  such that

$$x_i = vt + x_{0i} \quad \text{gives}$$

$$S(\sigma, t) = \sigma \sum_i u(vt + x_{0i}, y_i, z_i)$$

Further extending to a time average over  $M$  time intervals  $\Delta t$  gives

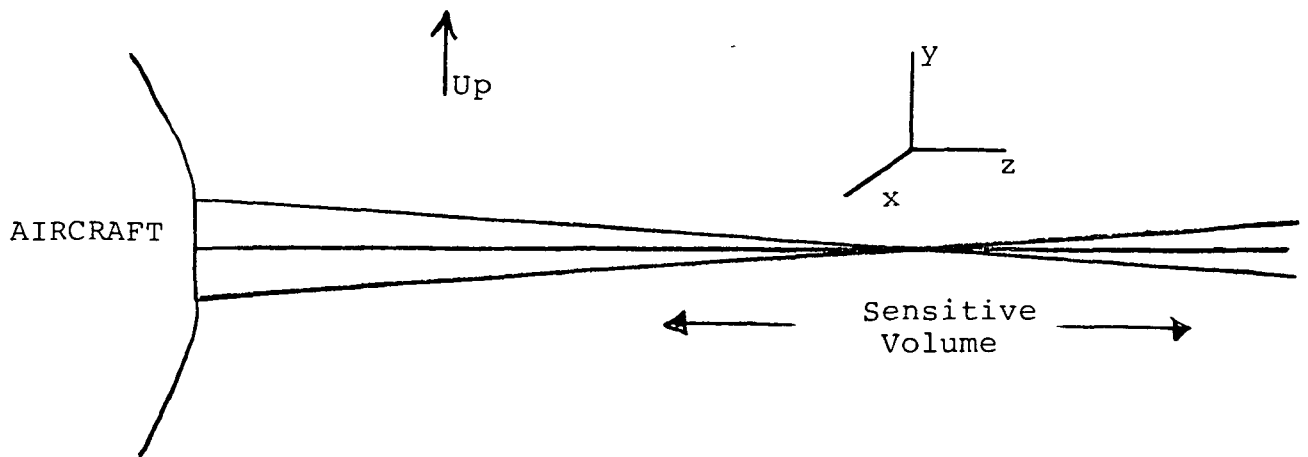
$$\begin{aligned} S(\sigma) &= \sum_{j=1}^M S(\sigma, t_j) / M \\ &= \sigma \sum_i u(y_i, z_i) m_i / M \end{aligned}$$

with

$$u(y_i, z_i) = \sum_j u(vt_j + x_{0i}, y_i, z_i) / m_i$$

and  $m_i$  is the number of integration points within the sensitive volume. This quantity depends on the trajectory of the particle





y is up

z is laser beam

x is along aircraft velocity vector

Particles penetrate perpendicular to the yz plane

Figure 1. Geometry and Coordinates

defined by the constants  $y_i$  and  $z_i$  through the sensitive volume and is independent of velocity. Actually

$$m_i = \Delta x(y_i, z_i) / v \Delta t$$

where  $x(y_i, z_i)$  is the width of the sensitive volume at  $y_i$  and  $z_i$ . Once again extending the expression by replacing the summation over particle number by integration over volume and the uniform density  $n(\sigma)$  gives

$$\begin{aligned} S(\sigma) &= n(\sigma) \sigma \int u(y, z) \Delta x(y, z) dy dz \\ &= n(\sigma) \sigma G(\sigma). \end{aligned}$$

A possible dependence of the gain factor  $G$  on  $\sigma$  is emphasized because of its importance in case this method is used when a single particle at a time is sensed. That is, if an effective threshold exists at  $S=1$ , the sensitive volume is defined by  $S>1$ , and the single particle sensitive volume is smaller than the many particle sensitive volume because many particles outside the single particle volume can build up a signal  $S>1$ . In order to include all particle sizes, the expression must be integrated over  $\sigma$ :

$$S = \int n(\sigma) \sigma G(\sigma) d\sigma.$$

Putting this in the form given at the beginning of this section

such that  $\beta$  can be isolated requires defining

$$G_{VM} = \frac{\int n(\sigma) \sigma G(\sigma) d\sigma}{\int n(\sigma) \sigma d\sigma}$$

so that

$$S = \beta G_{VM} .$$

Note that  $G_{VM} < G_V$ , the conventional many particle volume mode gain, if  $G(\sigma)$  is dependent on  $\sigma$ . This means that, if  $\beta$  is calculated from a measured signal  $S$  obtained from an average of single particle signals with  $\beta = S/G_V$ , too small a result would be obtained.

The basis of the VM method for measuring the backscatter cross-section has been developed. However it has been shown that the gain factor may depend on whether data is taken in a many particle or single particle situation.

## 2.2 Single Particle Mode Algorithm

The SPM algorithm functions by recording the peak signal from each particle which transits the sensitive volume. The geometry is the same as described previously. Single particle transits are assumed not to overlap in time. From the statistics of the peak signal distribution and knowledge of sensitivity contours within the sensitive volume, one may derive the particle density, backscatter cross-section distribution, and atmospheric backscatter coefficient. The algorithm will now be described using discrete mathematics with direct application to the computational programs.

Consider an interval of the single particle backscatter cross-section axis from  $\sigma_L$  to  $\sigma_H$  which covers all particles seen, and which itself is divided into  $M$  intervals. The backscatter coefficient will be taken as

$$\beta = \sum_{j=1}^M n_j \sigma_j$$

where

$n_j$  = number of particles per unit  
volume within the  $j$ th interval

$\sigma_j$  = cross-section at the center  
of the  $j$ th interval.

Suppose that the total number of particles seen per unit volume

is  $D$ ; then

$$w_j = n_j/D$$

is a probability distribution since

$$\sum_{j=1}^M w_j = \sum_{j=1}^M n_j/D = 1$$

Since each  $\sigma_j$  has a particular amount of the sensitive volume  $V_j$  in which the particle would give a signal above threshold  $S_L$ , the total number of particles seen,  $N$ , is

$$N = \sum_{j=1}^M n_j V_j = D \sum_{j=1}^M w_j V_j$$

and the density  $D$  is

$$D = N / \sum_{j=1}^M w_j V_j$$

which says that the relevant volume is an average volume weighted by the cross-sectional distribution  $w_j$ . Also

$$\begin{aligned} \beta &= \sum_{j=1}^M n_j \sigma_j / 4\pi = D \sum_{j=1}^M w_j \sigma_j / 4\pi \\ &= D \langle \sigma \rangle / 4\pi \end{aligned}$$

so that  $\beta$  is given by the particle density times the average cross-section. The SPM algorithm determines the probability distribution  $w_j$  through the relationship between the peak signal distribution and the sensitivity contours within the sensitive volume. This same information also determines the density.

In order to understand the SPM algorithm, the concept of the volume  $V_j$  sensitive to a particle of cross-section  $\sigma_j$  must be clear. For the geometry previously described with the laser axis perpendicular to the aircraft vector, this volume is a cylinder with axis in the direction of the aircraft velocity vector and length  $vt$ , where  $v$  is the aircraft speed and  $t$  is the time of observation. This cylinder intersects a vertical plane through the optic axis in an area  $A_j$ . The definition of the volume  $V_j$  is that particles  $\sigma_j$  passing through the area  $A_j$  will give a peak signal  $S$  (signal-to-noise) above threshold  $S_L$ . The gain factor  $g(y,z)$  in the equation  $S_L \leq g(y,z)$  determines the area  $A_j$ , where  $y,z$  are coordinates in the vertical plane of the sensitive volume. Furthermore, the notation  $g(A)$  is used to mean the gain on the contour surrounding the area  $A$ . These concepts and the relationship between the  $\sigma$  and  $S$  distributions are shown in Figure 2a. The line  $g(0)$  represents the maximum gain of the sensitive volume because the maximum gain occurs at a point. Three  $\sigma$  and  $S$  intervals are shown in this figure, with boundaries related by  $S = \sigma g(0)$ . Any other gain is represented by another line with slope  $g(a) < g(0)$ . Notice that a particle in interval  $\Delta\sigma_2$  may contribute to  $\Delta S_1$  and  $\Delta S_2$ , depending on the gain, but not



to  $\Delta S_3$  since this would require a gain larger than  $g(0)$ .

In order to relate the  $\sigma$  and  $S$  distributions, consider Figure 2b. Particles with a number per unit area density  $n(\sigma)$  at  $\sigma$  contribute signals  $\Delta N$  within  $\delta S$  according to  $\Delta N = \delta A n(\sigma)$ . To determine the contribution of a macroscopic interval  $\Delta\sigma$  to a macroscopic interval  $\Delta S$ , as shown in Figure 2c, the intergral

$$\Delta N = \int_{\Delta\sigma} n(\sigma) \Delta A(\sigma) \delta\sigma$$

is evaluated where  $n(\sigma)$  is the number of particles per unit volume per  $\sigma$  increment at  $\sigma$ ,  $\Delta A(\sigma) = A_2 - A_1$ , and  $\delta\sigma$  is a sub-interval in  $\sigma$ . Notice that the areas can be considered functions of the gain, and therefore  $A_2 = A(S_2/\sigma)$  and  $A_1 = A(S_1/\sigma)$ . This function has been determined by calibration and is included in the computational program (Section 2.3, 2.4 and Appendix in tabular form in subroutine DATANAL. The method of obtaining these data is described in Reference 1. In order to perform the above integral, the probabilities behind the  $n(\sigma)$  are assumed ( $w_j$  in previous discussion) and the probability of obtaining  $\Delta N$  particles is calculated in subroutine OPTIM. The actual numbers of particles are obtained by multiplying by the total number of particles observed. Contributions to each  $\Delta S$  interval from each possible  $\Delta\sigma$  interval are evaluated. The assumed distribution  $n(\sigma)$  is then varied until the best fit to the peak signal distribution is obtained in the least squares sense. With this "best fit" distribution the density, average cross-section  $\langle\sigma\rangle$ , and backscatter coefficient  $\beta$  are determined.



### 2.3 Computer Implementation

Implementation of the  $\beta$  prediction algorithms involved setting several parameters and making certain assumptions. These parameters/assumptions have little precedence, and therefore Applied Research will identify these variables/assumptions as clearly as possible.

1. The number of signal bins = 6. Six bins were processed and used for the inversion. A seventh bin was identified and used to store all large particle signals, but not considered in the inversion.
2. The number of processor bins which made up each of the six signal bins were:

Signal bin 1 = processor bins 5-8

Signal bin 2 = processor bins 9-16

Signal bin 3 = processor bins 17-32

Signal bin 4 = processor bins 33-64

Signal bin 5 = processor bins 65-128

Signal bin 6 = processor bins 129-255

Signal bin 7 = processor bin 256

Note that signal bins 1-6 contain progressively twice as many processor bins as the previous signal bin. This type of consolidation was done because the lower order processor bins get many more signals/bin than the higher order bins.

Note also that processor bins 1-4 are not used because the threshold was set at 4.

3. The signal processor threshold is equal to 4.
4. The volume channel bandwidth is 860 Khz.
5. The single particle processor bandwidth is 1.5 Mhz.
6. The LDV is always focussed at 10 meters.
7. The number of sigma bins = 6.

The above mentioned parameters/assumptions were employed throughout the data prediction results.

In addition to the pre-set parameters, several other pieces of information are very important to the data predictions. This information is all related to calibration of either the single particle mode or the volume mode. The volume mode calibration and method of prediction will be discussed first, followed by the single particle calibration and method of prediction.

For the VM calculations, two sets of calibration data were used. The first is identified as the "count" calibration and this data is read in at the beginning of the main program and stored in the array CAL (J,I). The first index J is over IF gain values from 45 to 70. The second index I is over DBSM values from -71 to -20. The proper calibration curve was picked depending upon the IF gain parameter. The volume "count" calibration data also had to be divided by 500 in order to scale the counts to one average count value.\* The volume "count" calibration data relates "counts" in the volume channel

---

\*Volume mode calibration data was performed by W.Jones of NASA. This information was relayed verbally to Applied Research, Inc.

to DBSM values. The second set of calibration data required is a measurement of the signal response of the LDV as a function of longitudinal distance while focussed at 10 meters. This data is shown in Figure 3. This data was used to calculate  $L_{eff}$  at 10 meters. (Reference 1) Longitudinal distance means along the optical axis of the LDV.

The volume  $\beta$  was calculated using the following equation:

$$\beta = (V_S/V_N)f_r/(S_d L_{eff} )$$

$V_S$  - integrated volume signal

$V_N$  - integrated volume noise

$S_d$  - signal-to-noise from a sandpaper disk  
at 10 meters focus with noise scaled from  
the calibration bandwidth of 100kHz to  
860kHz, the processor bandwidth, giving  
 $1.84 \times 10^6$ .

$f_r$  - bidirectional reflectance of a sandpaper  
disk equal to .016.

$L_{eff}$  - effective length of the LDV while focussed  
at 10 meters, found to be 64.1 cm.

$L_{eff}$ ,  $S_d$  and  $f_r$  were all determined prior to beginning the data predictions and remain fixed throughout. The volume signal and noise were calculated for each data point. The LDV data had alternating samples of noise data throughout each of the flights. This was accomplished by dithering a mirror in the optical train thereby effectively "losing" the signal. The raw output of the

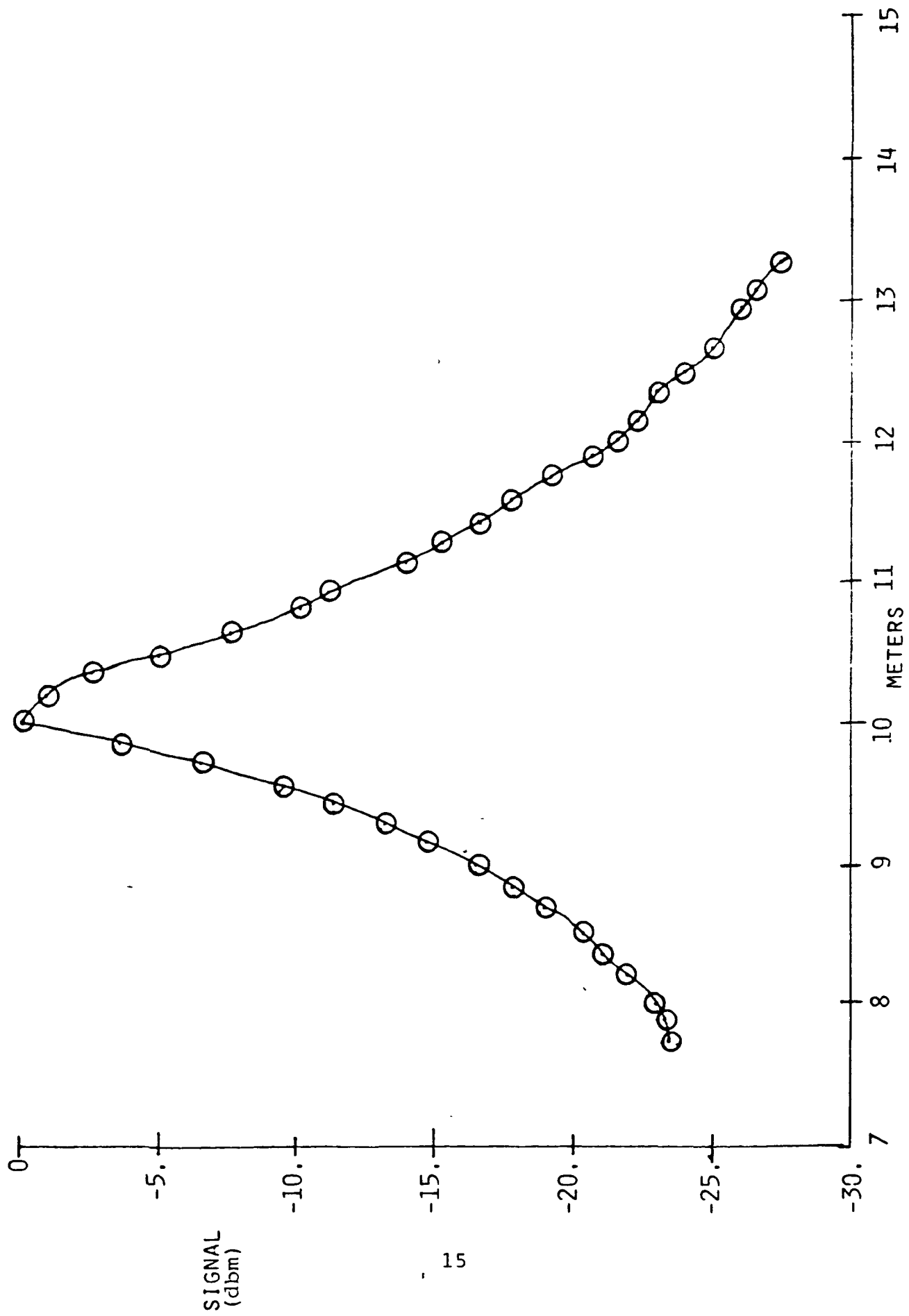


Figure 3. Longitudinal Profile at 10 Meter Focus

volume  $\beta$  channel on the LDV processor is called "counts". This count has to be divided by the number of times the channel was scanned in order to provide the average count for the time interval. The average count is then compared to the count calibration data (using the correct IF gain) to obtain a DBSM signal. The assumption was made that the volume channel count (data record) actually was signal plus noise while the noise particle count was noise only. Therefore to obtain the volume signal ( $V_S$ ) the noise signal ( $V_N$ ) was subtracted from the signal plus noise. This provided the  $V_S$  and  $V_N$  required to complete the volume  $\beta$  prediction.

Two pieces of calibration data are required to complete calibration for the single particle  $\beta$  calculation. These data are the correlation between signal value and channel number on the signal processor and the gain (equals signal/noise/cross-section) versus area curve.

The correlation between channel number and signal value is important to establishing what size particles are being seen by the processor. The "signals" here are tied to the calibration of the area curve discussed next. It is not known how this calibration data may depend upon the IF gain. All predictions were obtained using one calibration curve, Figure 4, which has an IF gain of 57.

The gain versus area curve is crucial to making the correct single particle  $\beta$  predictions. This data was taken by Applied

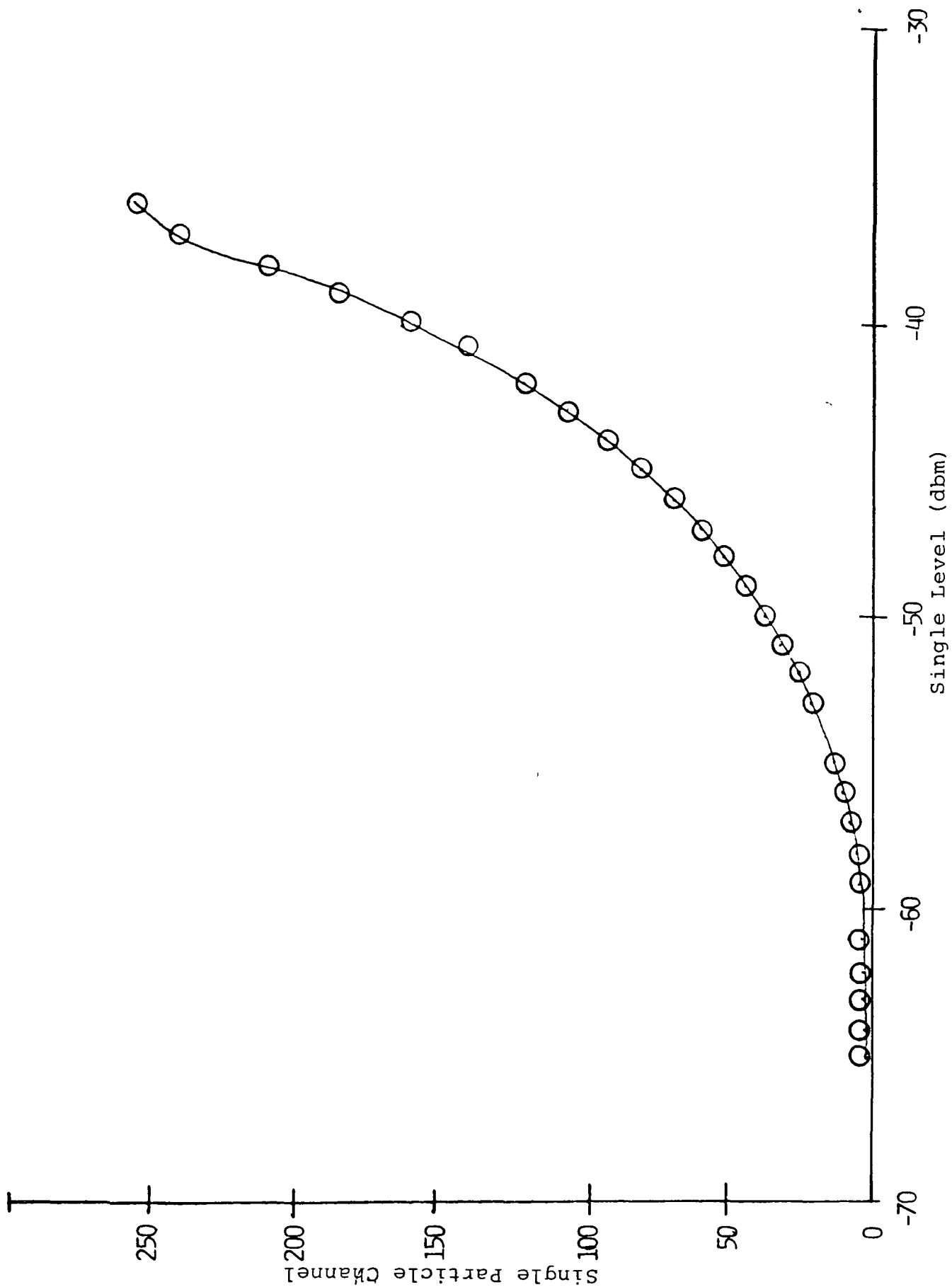


Figure 4. Signal Processor Channel vs. Signal Level

Research, Inc. and presented in Reference 1. This data resulted in a relative mapping of the sensitive focal volume of the LDV in a vertical plane containing the optical axis. "Relative" means that the scale of the map (signal/noise/sigma) was undefined. The remaining procedure then was to define the scale of the gain versus area map. This was done by using the following equation:

$$S_d/f_r = \int Cg'(A) dA$$

where  $S_d$  is the signal return from a sandpaper disk at 10 meters,  $f_r$  is the bidirectional reflectance of a sandpaper disk, and  $g'$  is the relatively scaled gain data. The values used were:

$$S_d = 1.053 \times 10^6$$

$$f_r = .016$$

$$\int g' dA = 1.44 \times 10^6$$

The  $S_d$  value is the calibration value of  $10^{7.2}$  scaled from 100kHz to 1.5MHz. The value of C determined was :  $C = 45.99$ . This value is used in subroutine DATANAL in a data statement as variable TRANS to scale the area curve to the proper values. Also as a result of this determination of a scale factor C, the single particle gain at an area of 0 can be used from the equation  $S/\sigma_{A=0} = g(0)$ . to relate a S/N value S to a  $\sigma$  value; i.e.  $\sigma = S/g(0)$ . This relationship is used in the main program about lines 218-220 with a value of  $1.1037 \times 10^7/\text{cm}^2$  for  $g(0)$ .

The result of the inversion is to return an average sensitive volume cross-sectional area (WV) and average particle cross-section (WS). The equation

$$\beta = (ISUM/4\pi)(WS/FLTL/WV)$$

was used to compute the single particle  $\beta$ , where ISUM is the number of particles in the histogram. The flight length, FLTL, is computed by using the data recorded in each record (or records) for the elapsed time and flight speed.

The results of the computer implementation were presented in Reference 2. The results presented were all obtained using a power law solution for the  $\sigma$  distribution in the inversion subroutine OPTIM. This was done because early test runs indicated that the power law solution was nearly always the best fit. Since run time was becoming a problem for processing the many flights, the exponential and log-normal solutions were bypassed. This "bypass" can be eliminated by removing line 603.07 - IF(IP.EQ.2) RETURN in the subroutine OPTIM.

Figures 5 - 7 contain a flowchart of the main program and various subprograms which constitute the computer implementation of the  $\beta$  prediction algorithms. The Appendix has a short description of each program of the  $\beta$  prediction algorithms and also contains a listing of the main program and associated subprograms.



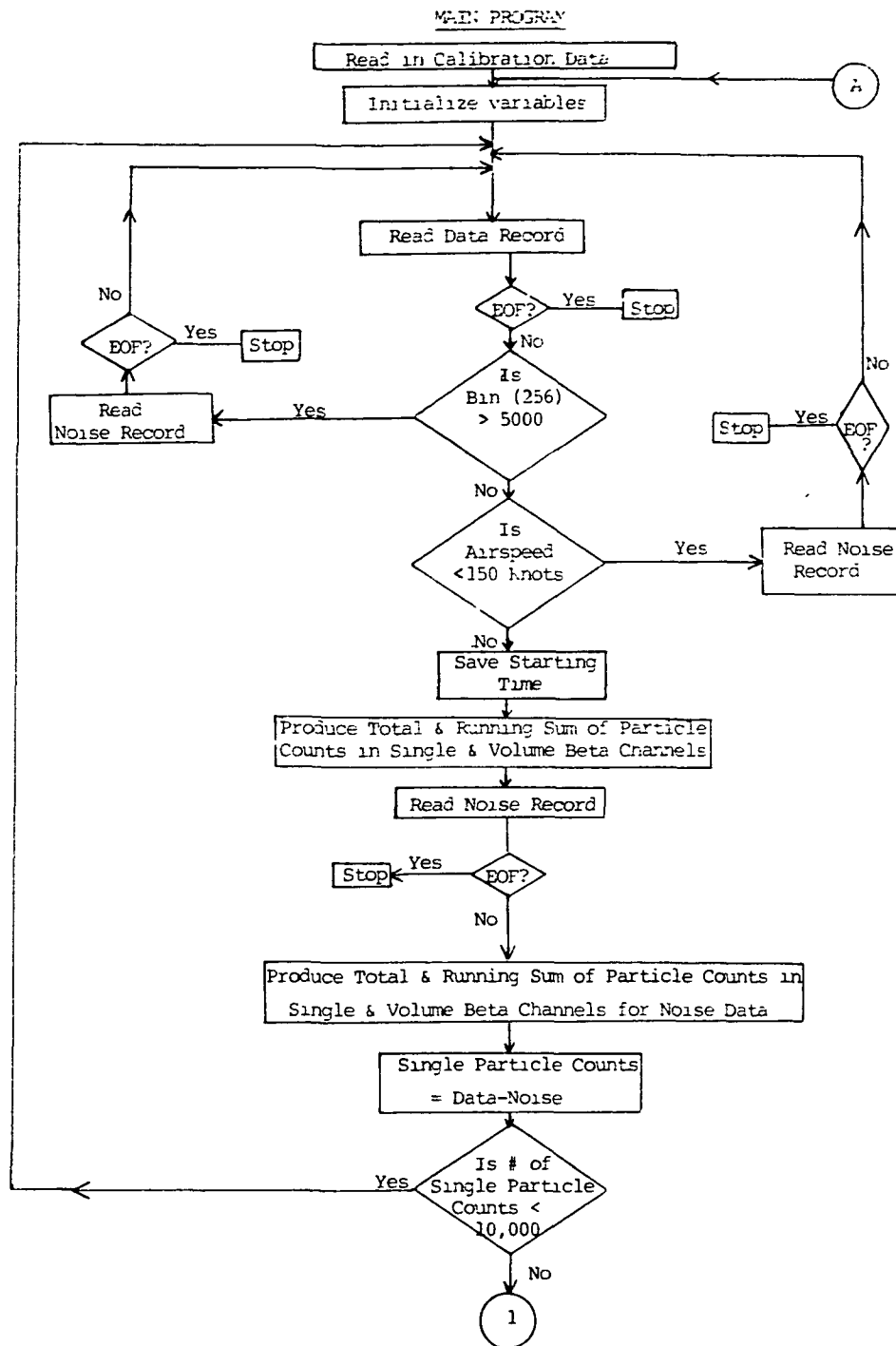


Figure 5a. Flow Chart of Computer Implementation

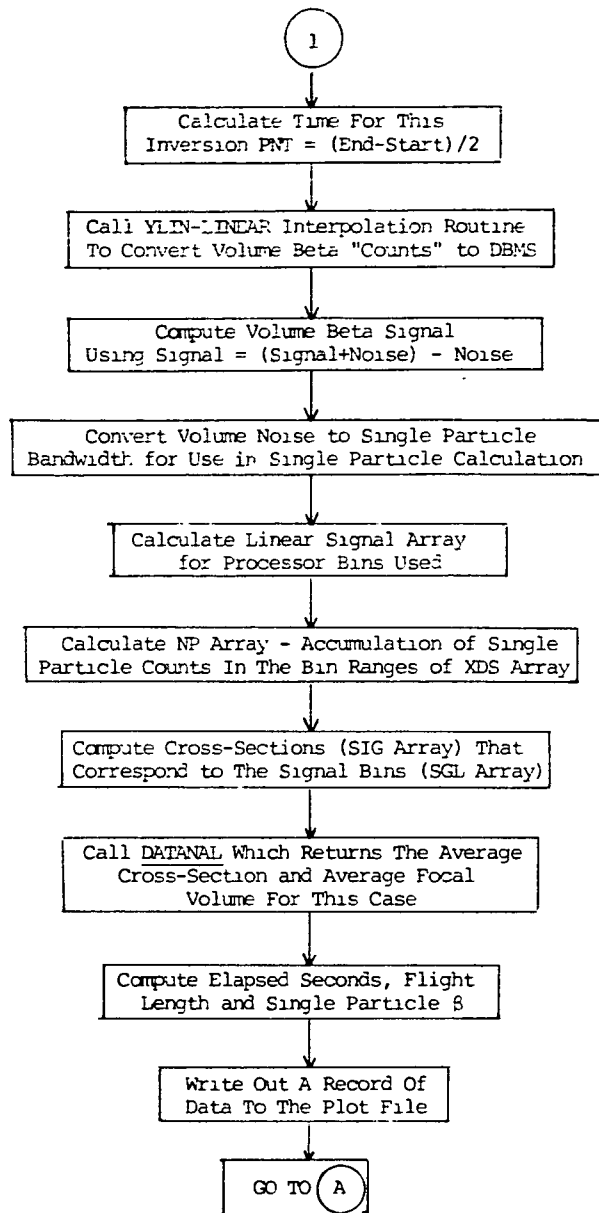


Figure 5b. Flow Chart of Computer Implementation (continued)

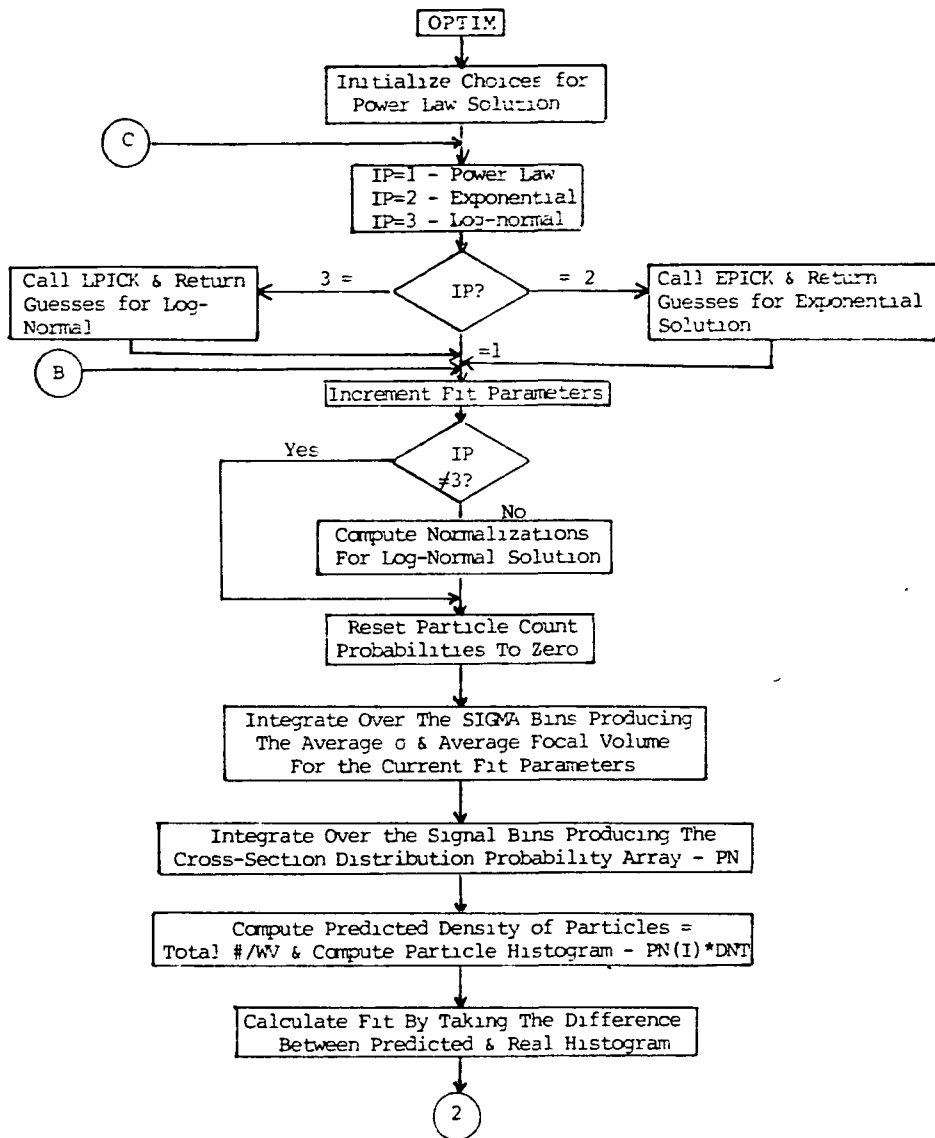


Figure 6a. Flow Chart of Computer Implementation of Single Particle Inversion Subprogram OPTIM

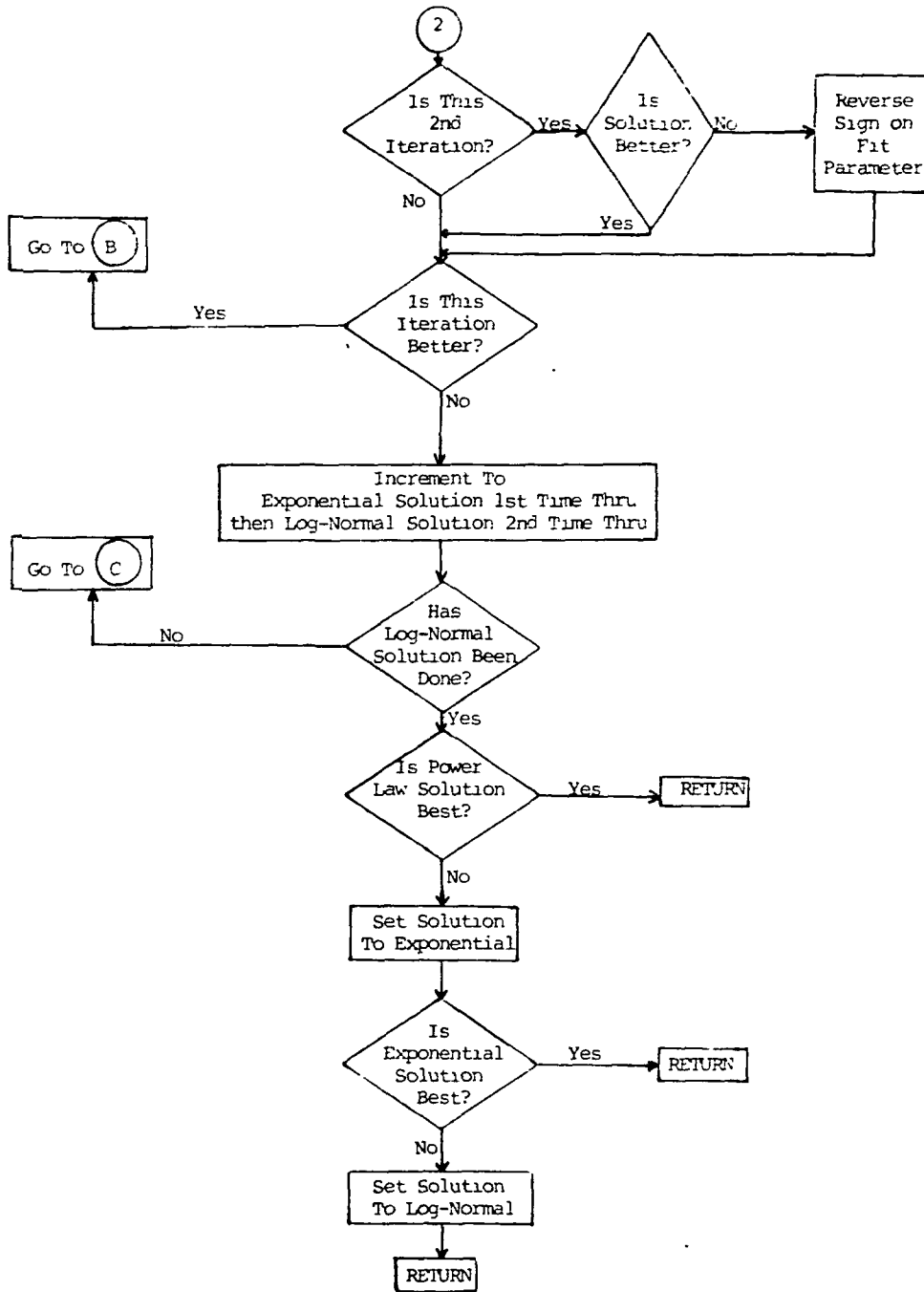


Figure 6b. Flow Chart of Computer Implementation of Single Particle Inversion Subprogram OPTIM (continued)

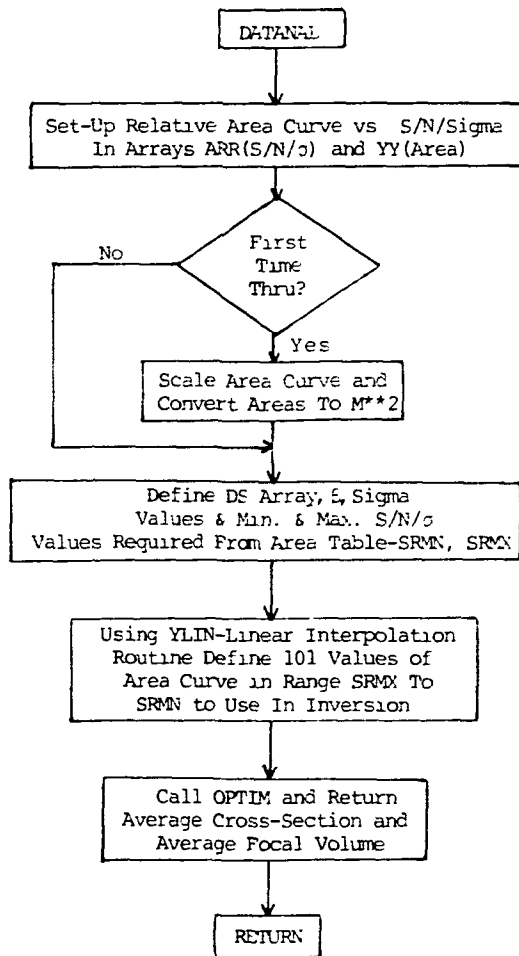


Figure 7. Flowchart of Computer Implementation of Single Particle Inversion Subprogram Datanal

Figure 8. DATA RECORD

0-	TIMH:	12	<u>CURRENT TIME</u>
	TIMM:	0	
	TIMS:	0	
	TIMF:	10°°	
4-	TIMH1:	12	<u>TIME AT START OF RECORD</u>
	TIMM1:	0	
	TIMS1:	0	
	TIMF1:	0	
8-	DATEM:	6	<u>CURRENT DATE</u>
	DATED:	1	
	DATEY:	32	
11-	STEPR1:	0	<u>STEPPER POSITIONS (NOT PRESENTLY USED)</u>
	STEPR2:	0	
	STEPR3:	0	
14-	VOLBH:	0	<u>VOLUME BETA INTEGRATORS</u>
	VOLBL:	0	
	VOLBN:	0	
19-	PARMS:	171356	<u>CONTROL REGISTER PARAMETERS</u>
	CLOCKP:	11.	<u>DIGITAL FILTER CLOCK PERIOD</u>
	FILTER:	2	<u>IF FILTER WIDTH</u>
20-	TIMEON:	3	<u>VIDEO TIME CONSTANT</u>
	VCOFRQ:	140.	<u>VCO FREQUENCY</u>
	DOFSET:	0 11.	<u>A/D FILTER BIAS</u>
23-	DISCRM:	0	<u>DISCRIMINATOR THRESHOLD</u>
	IFGAIN:	45.	<u>IF GAIN</u>
25-	FWDID:	0	<u>FORWARD/AFT IDENTIFIER</u>
	NDSETS:	1	<u># SCANS PER WRITE</u>
	INTSEC:	1000.	<u>MS PER INTEGRATION PERIOD</u>
	ADDASV:	0	<u>UP IF ADDAS LINK ON</u>
	ADDASI:	100.	<u># MS PER ADDAS OUTPUT</u>
30-	SCAN:	0	<u>UP IF SCANNER ENABLED</u>
	TASADD:	300	<u>TAS FROM ADDAS</u>
	TASKB:	300	<u>TAS FROM KEYBOARD</u>
	THETA:	500.	<u>ANGLE THETA IN .01-DEG UNITS</u>
34-	VCOOFS:	0	<u>VCO OFFSET IN 53-KHZ UNITS</u>

88 IDENT: BLHB 80. IDENTIFICATION STRING

## 2.4 Running The Data Prediction Algorithms

The  $\beta$  prediction algorithms are stored on disk on the Sigma V computer in account BILBRO, EB23175. The file name is DATANAL. A batch file which is used with the code is stored under BXD. Two input files are required, they are unit numbers 5 and 12. File unit number 5 must be LDV processor data in the format shown in Figure 8. This defines the data for which predictions are to be made. File unit number 12 is volume  $\beta$  calibration data and is stored under the file name CALFL4 in account BILBRO, EB23175. Units 6 and 10 are used as output unit numbers to obtain the printed results of the algorithm. Unit 13 is also an output unit but is used to store results for plotting and should therefore be given a file name by the user. Unit 13 produces one record for each  $\beta$  prediction during the flight in the following format:

```
Write(13) LH,LM,LS,LF,SINGLEB,VOLB,WS,FLTL,ELS,WV.
```

The definition of these variables is:

- LH - Hours for this prediction
- LM - Minutes for this prediction
- LS - Seconds for this prediction
- LF - Fractional seconds for this prediction
- SINGLEB - Single particle  $\beta$  prediction
- VOLB - Volume channel  $\beta$  prediction
- WS - Predicted average cross-section
- FLTL - Estimated flight length
- ELS - Number seconds for which data-recording occurred for this prediction
- WV - Predicted average focal "volume" cross-section

### 3.0 Measurement Errors

In the application of the previously discussed VM and SPM algorithms to the processing of the NASA flight data, two general classes of error are considered. The first class, systematic errors, involves errors of concept, principle, or application. The second class concerns statistical errors or uncertainties which result from lack of knowledge or from fluctuating random variables. Systematic error is the most difficult to handle since even its presence is not always obvious. In the case of the data under consideration, an average offset of the results from the two algorithms of about one order of magnitude indicates systematic error. However, more than one such error could be present. To uncover these errors, a reconsideration of concepts and procedures is necessary.

Statistical error is more easily treated. With estimates of the statistical uncertainty in independent variables, the uncertainty in the final result may be obtained. In the present case, also the number of particles processed per output  $\beta$  value is expected to govern statistical fluctuation in  $\beta$ . This result has been analyzed.

#### 3.1 Volume Mode Errors

The VM algorithm has been derived in Section 2.1. Possible systematic errors in the backscatter coefficient calculation may



reside in

- a) the processor output
- b) the interpretation of the processor output
- c) the concept for the volume mode gain when used with single particles (as discussed in Section 2.1)
- d) a systematic offset in the parameters used to calculate the backscatter coefficient value

Possible errors in the processor output or the curves supplied by NASA which translate output into signal level are not considered here, but must be investigated in the laboratory.

The interpretation of the processor output has been discussed in Section 2.3 and no error has been discovered.

As discussed in Section 2.1, if the gain factor  $G(\sigma)$  is dependent on  $\sigma$  as a result of a decreased sensitivity volume for smaller  $\sigma$ , calibration of the "single particle volume mode" should not be treated as the "conventional volume mode." As mentioned in Section 2.1,  $G_{VM} < G_V$  implies that  $\beta$  values calculated with the gain factor  $G_V$  for the conventional volume mode give too small a value by the ratio  $G_{VM}/G_V$ . Evaluation of  $G_{VM}$  requires laboratory determination of the sensitive volume for each value of  $\sigma$ , integration of the single particle gain over this volume, and then integration of this result over the backscatter cross-section distribution. Therefore, in measurement situations, this effect would require determination of the  $\sigma$  distribution. An

effect very similar to this occurs in the SPM where the aerosol density is calculated by dividing the number of particles seen by the average volume, calculated by averaging the sensitive volume elements for the SPM over the  $\sigma$  probability distribution. It is not clear whether the VM sensitive volume elements would be the same as those for the SPM since signal acquisition requirements are different for the two modes. One has the feeling that this effect would contribute errors of less than an order of magnitude. This question might be answered with computer modeling.

The backscatter coefficient is calculated from the expression

$$\beta = S/G_V$$

where  $S$  is the signal to noise found from the data as explained in Section 2.3, and  $G_V$  is found by calibration with

$$G_V = S_d L_{\text{eff}} / f_r$$

where

$S_d$  = signal to noise return from  
a calibration disk of bidirectional reflectivity  $f_r$

$$L_{\text{eff}} = \int g(x,y,z) dx dy dz / \int g(x,y,0) dx dy$$

(see Figure 1)

$L_{\text{eff}}$  = the effective length of the  
sensitive volume

Errors or uncertainties in  $\beta$  may be evaluated as

$$\delta\beta/\beta = \delta S/S + \delta S_d/S_d + \delta L_{\text{eff}}/L_{\text{eff}} + \delta f_r/f_r.$$

The change  $\Delta\beta$  in units of orders of magnitude is defined as

$$\begin{aligned}\Delta\beta &= \log(\beta + \delta\beta) - \log \beta \\ &= \log(1 + \delta\beta / \beta)\end{aligned}$$

Each of the above error sources is considered separately.

Error due to S:

The signal out of the processor and corrected by noise subtraction is assumed here as exact. A possible interpolation error of less than 1dBm occurs in obtaining the dBm level from the volume channel counts. This yields a  $\Delta\beta$  found as

$$\begin{aligned}\Delta\beta &= \log(1 + \delta S/S) = \log(S+\delta S) - \log S \\ &= [(S+\delta S)_{\text{dBm}} - S_{\text{dBm}}]/10 \\ &= .1\end{aligned}$$

Error due to  $S_d$  :

The calibration signal error from the rotating sandpaper disk at the sensitive volume waist would not be likely to have a reading error of more than 2 dBm, from inspection of the variation of the calibration data. Thus

$$\Delta\beta = .2$$

Error due to  $f_r$  :

The bidirectional reflectance of the aluminum oxide target for incidence and reflection at 45 degrees was taken to be .016/sr. An uncertainty of  $\pm 25\%$  has been quoted by workers in this field (Reference 3). This gives

$$\Delta\beta = .1$$

Error due to  $L_{eff}$  :

The error in the determination of  $L_{eff}$  is less than 10% from consideration of the methods used. This gives

$$\Delta\beta = .04 \quad .$$

In summary, the possible errors due to uncertainty in the quantities used to calculate the backscatter signal in the volume mode are given in the following table:

<u>Source</u>	$\Delta\beta$ (orders of magnitude)
S	.1
S <sub>d</sub>	.2
f <sub>r</sub>	.1
L <sub>eff</sub>	.04

These uncertainties may be positive or negative, and combine to less than half an order of magnitude at maximum. The error given for S considers only the uncertainty in interpolating the processor output. Systematic errors are not included in these numbers, but once identified, their effects would be calculated with the above formulae.

### 3.2 Single Particle Mode Errors

As discussed in Section 2.2, the backscatter coefficient for the SPM may be expressed as

$$\beta = D\langle\sigma\rangle/4\pi$$

where  $D$  is the particle density and  $\langle\sigma\rangle$  is the average single particle backscatter cross-section. These quantities are determined from the peak signal distribution and the gain contours versus enclosed area function resulting from mapping the sensitive focal volume area in the vertical plane of maximum gain - the  $yz$  plane of Figure 1.

Possible systematic errors for this mode concern

- a) the processor output
- b) the interpretation of the processor output
- c) the single particle per transit time condition on the applicability of the algorithm
- d) the gain versus area function determined by calibration
- e) operation of the SPM algorithm

Random errors and measurement uncertainties will be discussed following discussion of these topics.

The processor output will be assumed valid, subject to

laboratory tests, except possibly for point c). The interpretation of this output is described in Section 2.3 and questions are raised under point d). Some implications regarding conditions of validity for the SPM algorithms also follow from the discussion of point d) below. The SPM algorithm has been found valid for predicting  $\beta$ , subject to random errors, as previously documented.

In the course of the present work, considerable effort has been spent in an attempt to improve the application of calibration procedures which result in the single particle gain versus area function, with the result that a significant shift in the previously processed backscatter coefficient values is indicated. Originally, calibration plans for this program included a special calibration device which would emit single particles of known cross-section. Time constraints from the flight plans forced this effort to be interrupted and an alternate calibration procedure was sought involving the spinning disk. Under this contract this procedure has been reconsidered and improved.

Contours of constant single particle gain,  $g(x,y,z)$ , were mapped out in the  $x=0$  (vertical) laser beam plane within the sensitive volume, in a previous contract. Only relative values of these contours were determined by this mapping procedure, with overall normalization to be determined by another method. A more accurate way of obtaining this normalization follows.

The conventional volume mode gain  $G_V$  is defined as the integral over the single particle mode gain  $g(x,y,z)$  and

determined by calibration with a spinning disk at the waist as

$$G_V = \int g(x, y, z) dx dy dz$$
$$= S_d L_{\text{eff}} / f_r \quad .$$

The desired integral to be evaluated for normalization of the gain versus area function is

$$I = \int g(o, y, z) dy dz$$
$$= \int g(A) dA$$

where a change of variables transforming the integral from a two dimensional to a one dimensional integral is implied. The variable  $A$  is the total area within closed contours of  $g$ . With this integral evaluated,  $g$  is related to its unnormalized version  $g'$  by

$$g = ag'$$

where

$$a = I / \int g'(A) dA.$$

The value  $I$  can be determined from  $G_V$  if the sensitive volume is assumed cylindrically symmetric about the optical axis of the beam. Representing the integral for  $G_V$  by transforming to cylindrical coordinates gives



$$\begin{aligned}
G_V &= \int g(\rho, z) \rho d\rho d\theta dz \\
&= 2\pi \int g(\rho, z) \rho d\rho dz \\
&= 2\pi \rho_{av} \int g(\rho, z) d\rho dz.
\end{aligned}$$

This last integral is one-half of the desired integral I. Also

$$\rho_{av} = \int g(\rho, z) \rho d\rho dz / \int g(\rho, z) d\rho dz$$

is an average radius of the sensitive volume. Hence

$$G_V = \pi \rho_{av} I = S L_{eff} / f_r$$

and from

$$I = a \int g'(A) dA = a I'$$

one gets for the normalization factor

$$\begin{aligned}
a &= [S_d / (f_r I')] L_{eff} / (\pi \rho_{av}) \\
&= a_0 L_{eff} / (\pi \rho_{av})
\end{aligned}$$

where  $a_0$  was the normalization used in the processing of the flight data. The integrals for  $\rho_{av}$  were numerically evaluated to give  $\rho_{av} = .0265\text{cm}$ . (Compare this with Figure 9.21 of

Reference 1.) This gives

$$\begin{aligned} a &= [(64.1\text{cm})/ (.0265 \pi \text{ cm})] a_0 \\ &= 770 a_0 \end{aligned}$$

Any adjustment in the normalization of the gain versus area function affects the sizes of the particle distribution which can be detected and associated with a particular peak signal distribution. For the power law backscatter cross-section distribution function, which best fits the processed flight data, an adjustment "a" divides the average cross-section, but does not change the density. (See subroutine OPTIM). Thus

$$\begin{aligned} \beta &= \langle \sigma \rangle D/4\pi \\ &= \beta_0/770 \end{aligned}$$

and indicates that all calculated single particle  $\beta$  values should be decreased by about 2.9 orders of magnitude. A calibration factor of the same order of magnitude is indicated by using the incoherent beam profiles of Figures 8.3 and 8.4 of Reference 1. This implies that the system is sensitive to cross-sections as small as .00166 square microns since threshold peak signal levels required cross-sections of 1.28 square microns at the original calibration.

The signal-to-noise for a given cross-section is unchanged by this rescaling since its effect on  $g$  and  $\sigma$  cancel for a power law  $\sigma$  distribution. For example, around record 6 of flight number 9, processing of 10,000 particles gives a signal-to-noise of about .14 for the threshold in this case. To obtain this number one must use the calibration curve supplied by NASA for IF gain of 57. Flight 9 had an IF gain of 63. It is clearly these low signal-to-noise numbers combined with the higher single particle gain values which are responsible for such low  $\beta$  values.

This adjustment in the normalization of the gain means that the system is sensitive to smaller particles than previously indicated, without undergoing an adjustment in the required signal-to-noise threshold. The backscatter coefficient is consequently smaller because no corresponding adjustment in density occurs. This gives a result which is about two orders of magnitude lower than the VM measurement. Nominal densities calculated with the SMP algorithm give about 1 particle per 100 cubic centimeters, which seems rather low for distributions with an average cross-section of .007 square microns, as in the flight 9 case above. This density would be more appropriate for particles of greater than 1 micron diameter. Therefore, since the gain profile of the sensitive volume is fairly well established (coherent and incoherent methods give the same order of magnitude for the scaling), there is reason to question the signal-to-noise values assigned to the signal bins of the processor output. The method of calculating these has been rechecked with no mistake found.

The actual calibration curve provided by NASA which assigns signal level to a bin should be rechecked. Also the variation of these assignments with IF Gain should be considered. An increase in signal values through recalibration of the processor gain could bring SPM and VM results into agreement.

The following consideration suggests another possibility. With the same particle distribution, the VM result predicts densities of about two orders of magnitude higher. For this case of one particle per cubic centimeter, the system may see more than one particle per transit time since the sensitive cross-sectional area is 42 square centimeters. A coincidence rejection mechanism could give erroneous results since no compensation is made for rejected cases; or a coincidence rejection mechanism which is not properly responding could interpret clusters of particles as single particles, thereby decreasing the density. Hence it may be possible that the SPM was used outside the conditions of validity without proper compensation being made.

Random errors, or errors of uncertainty of measurement, in the single particle prediction can result from the gain versus area function determination, the interpretation of the peak signal bins, the operation of the algorithm, and the number of particles seen. As before, the uncertainty in  $\beta$  in units of orders of magnitude due to a component uncertainty  $\Delta\beta$  is

$$\Delta\beta = \log (1 + \delta\beta/\beta) \quad .$$

As documented in an informal memo, the algorithms produce an uncertainty of less than 5%.

Error due to algorithm:

$$\Delta\beta = .02$$

Random error due to interpolation of signal bin calibration is 1 dBm. (This does not include possible systematic error due to this calibration data discussed earlier). For small errors this has an approximately linear affect on the  $\sigma$  interval, and therefore on  $\langle\sigma\rangle$ . Hence

$$\delta\beta = 26\%$$

Error due to interpolation of peak signal calibration:

$$\Delta\beta = .1$$

The gain versus area function was previously discussed in terms of systematic error. Any alteration of this function by a factor "a" goes directly through to  $\langle\sigma\rangle$  and then to  $\delta\beta$ . It is helpful to derive an estimate for the uncertainty in "a" due to measurement errors by referring to the previous expression

$$a = a_0 L_{\text{eff}} / \rho_{\text{av}} \Pi$$

where

$$a_0 = S_d / f_r I'$$

and  $I'$  is the integration over the unnormalized contours. The uncertainty in  $I'$  is difficult to estimate precisely but is within 10%. Using the previous values for  $S_d$  and  $f_r$ , and taking  $\rho_{av}$  to have the same uncertainty as  $I'$  and  $L_{eff}$  gives the following results for random errors due to uncertainties in measurements used to calculate the backscatter coefficient in the single particle mode.

<u>Source</u>	$\Delta\beta$ (orders of magnitude)
Algorithm	.02
Peak signal interpolation	.1
$S_d$	.2
$f_r$	.1
$L_{eff}$	.04
$\rho_{av}$	.04
$I'$	.04

Errors due to particle number fluctuations are not treated in this format but considered in the following paragraph.

Errors resulting from fluctuations due to small particle samples have been examined by comparing with the results from the case when a 10,000 particle minimum was used. For processing runs utilizing various sample sizes less than 10,000, a running

time-weighted average of the results sufficient to include 10,000 particles was developed, and considered a "local average". This result was used in two ways. The difference of this local average from the 10,000 particle case was considered the error in the local average. (The local average value nearest in time to the 10,000 particle value was used). Also, the fluctuation from the local average was calculated from the differences of the small particle number data from the local average. This method was found to be reasonable if too sharp variations in the data do not occur. Figure 9 shows these results for a region of flight 16 with the sharp  $\beta$  spike at time 878 removed. These results show rms deviations in units of orders of magnitude. They indicate that the local error can be maintained with .1 orders of magnitude with particle samples of 1000 minimum. Fluctuations of the "instantaneous" data from the local average do not approach this value until around 5000 particles minimum are processed. In this case the SPM has lower deviations and fluctuations than the VM data. (The VM data was also compared with itself in the manner described above). Figure 10 shows the same flight with the  $\beta$  spike included, with results which do not settle down as well. Figure 9 shows the deviations of the local average to be smaller than the fluctuations of the data from the local average. Figure 10 shows some of the SPM versus VM behavior.

Figure 11 shows the same data from a region of flight 9. Here the fluctuations are lower than the deviation of the local mean, and the results do not settle down as well as the 10,000

particle case is approached. For the SPM the .1 order of magnitude error is approached at 1000 particles, while 3,000 particles seem to be required for the VM result.



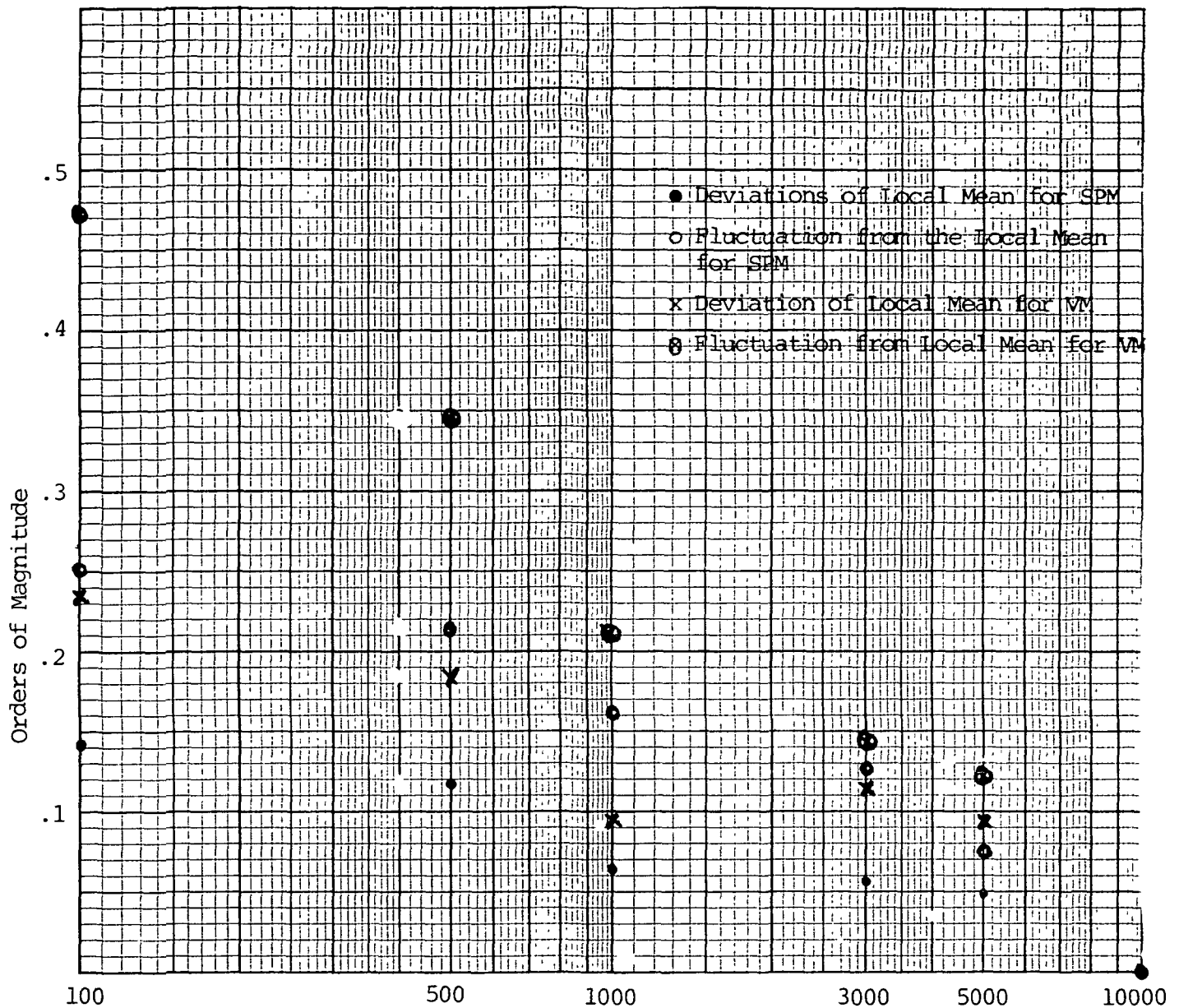


Figure 9. Statistical Error in Backscatter Coefficient as a Function of Number of Particles Processed for Flight 16 (Spike Removed)

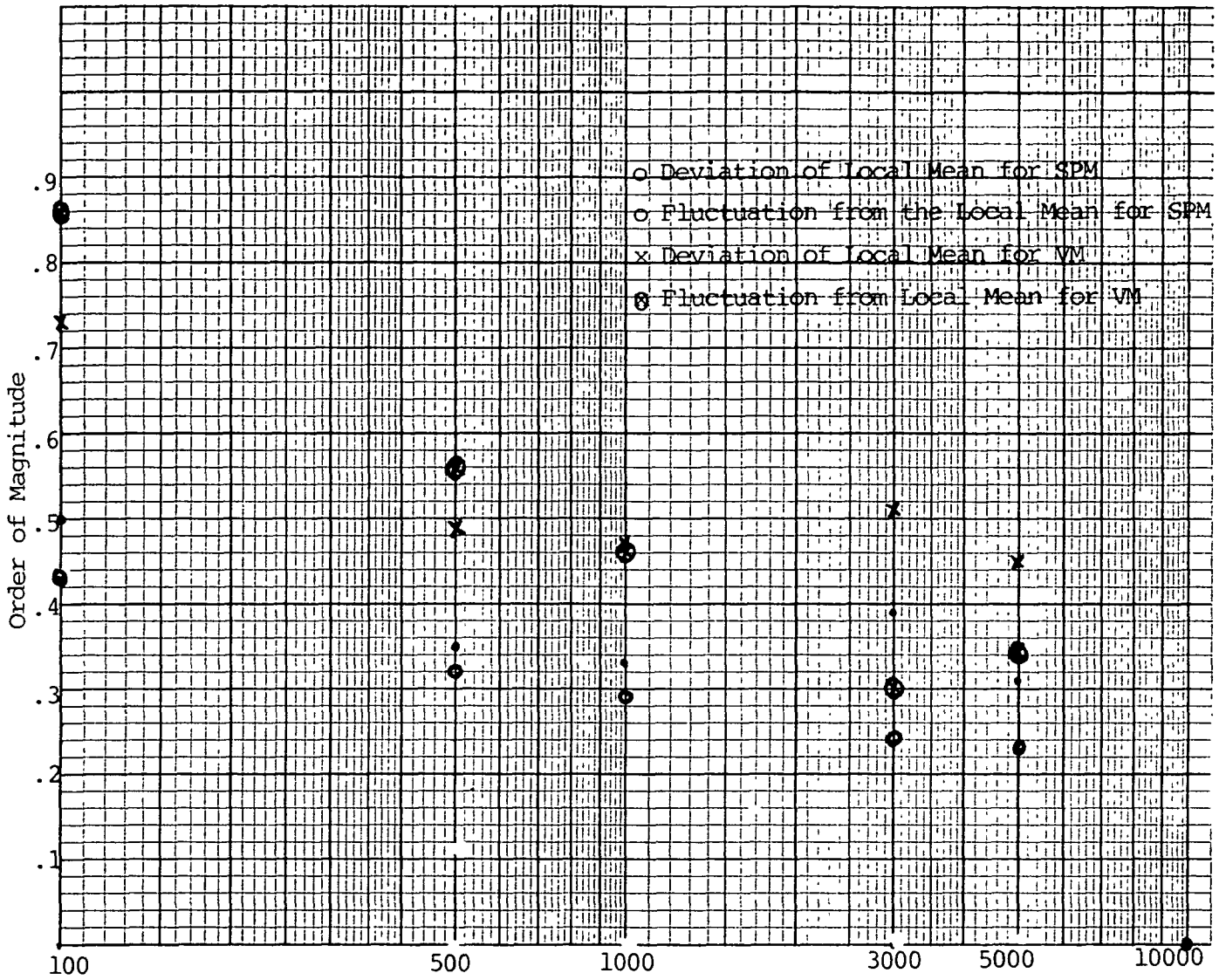


Figure 10. Statistical Error in Backscatter Coefficient as a Function of Number of Particles Processed for Flight 16 (with Spike)

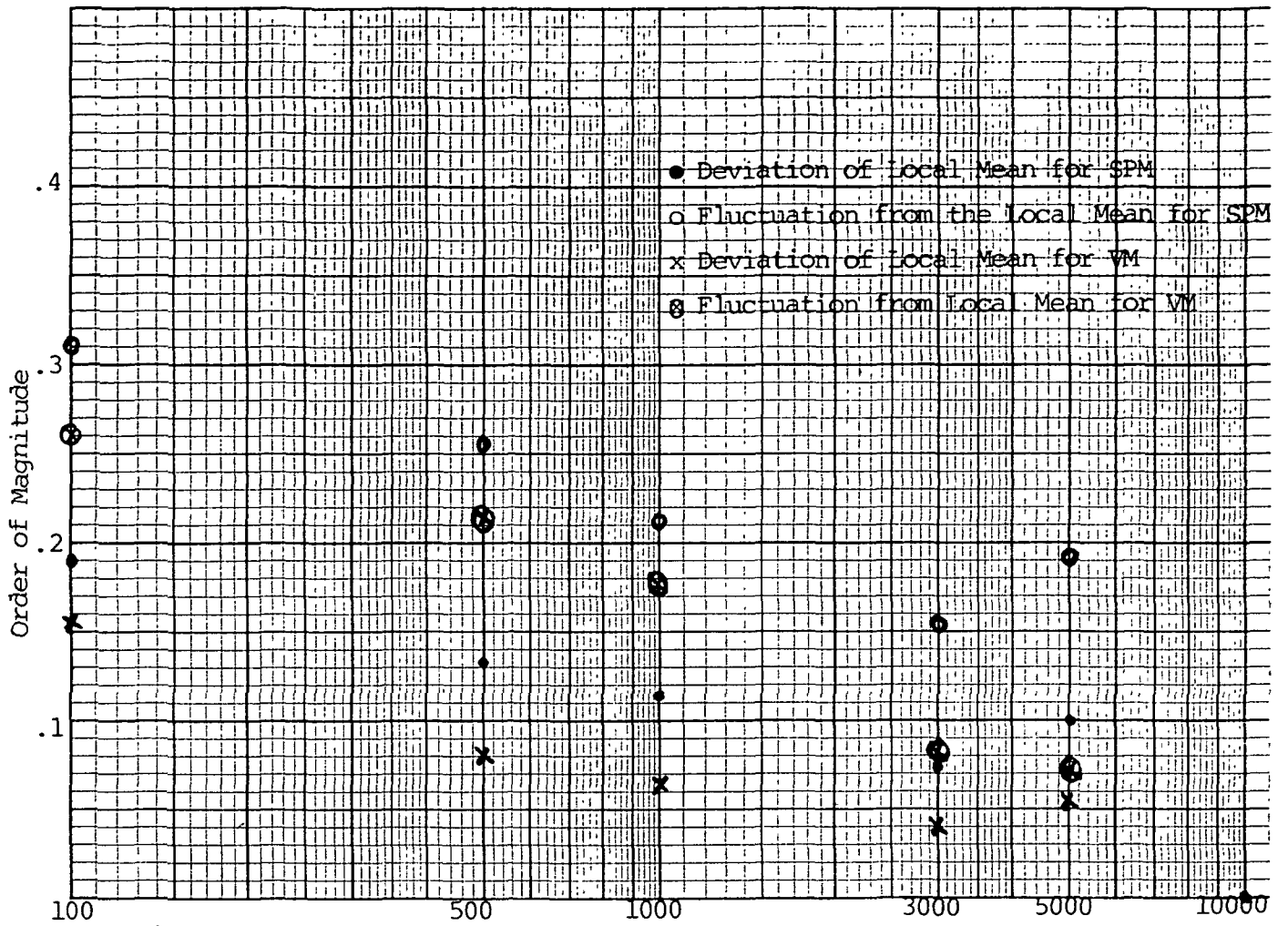


Figure 11. Statistical Error in Backscatter Coefficient as a Function of Number of Particles Processed for Flight 9

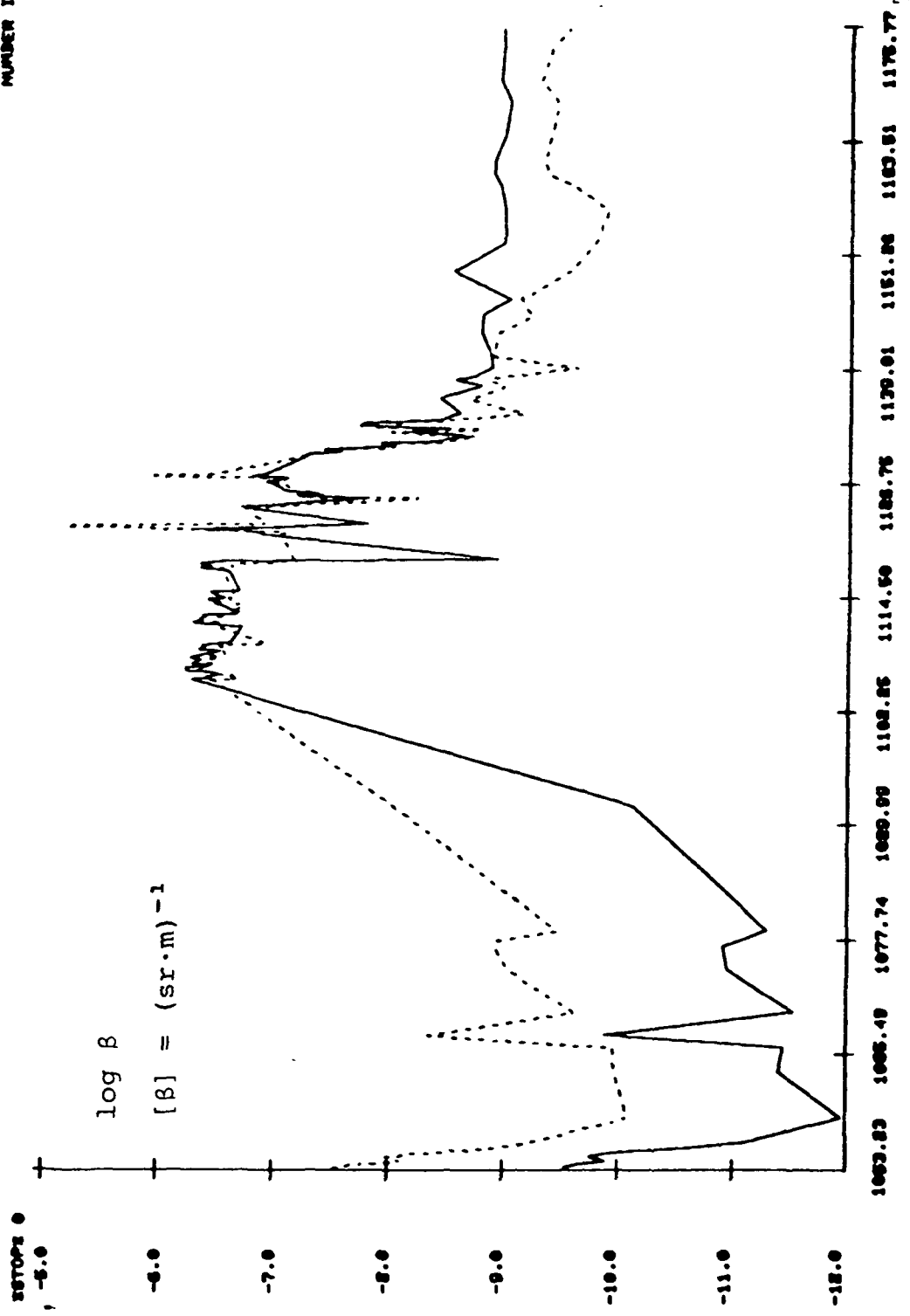


Figure 12. Backscatter Coefficient  $\beta$  for Flight 4

NUMBER IS 13

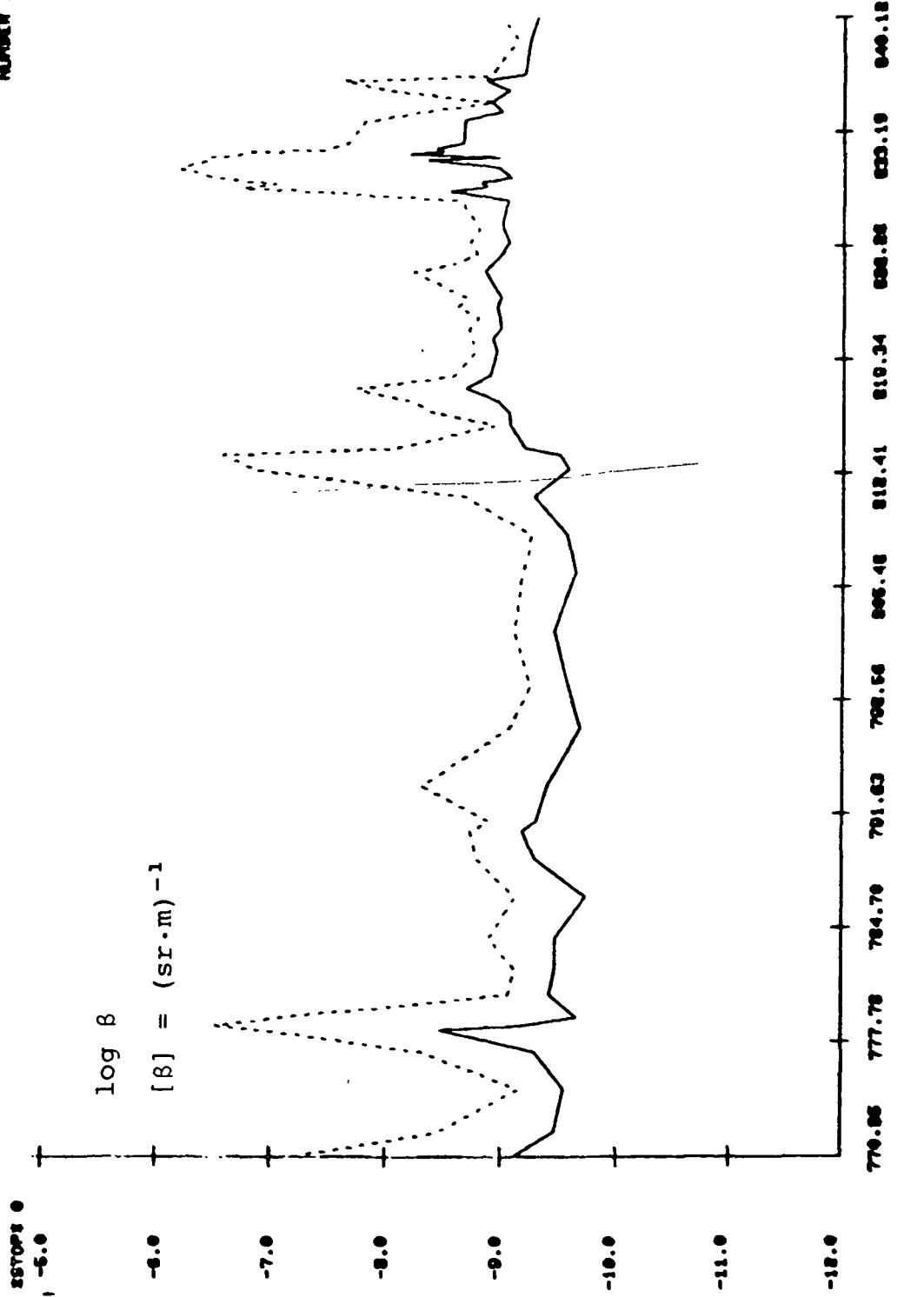


Figure 13. Backscatter Coefficient  $\beta$  for Flight 13

### 3.3 Anomalous Cases From Processed Data

Two pathological data prediction cases can be identified in Reference 2 and are shown in Figures 12 and 13. These cases are Flights 4 and 13. Flight 4 is unusual in that initially the single  $\beta$  predictions were much lower than the volume  $\beta$  and then about halfway through the flight the situation reversed. It was found that this was the case because the airspeed value was incorrect. Since airspeed is used to calculate flight length and then single particle  $\beta$ , the predicted results were much too low. Later on in the flight the problem was corrected and the predictions reversed the earlier trend.

Flight 13 also showed the trend of single  $\beta$  predictions less than the volume  $\beta$  predictions. A closer look at the computer run showed that the single  $\beta$  inversion program could not fit the histograms that were coming from the signal processor. The algorithm could not produce a fit because the lower signal bins were empty. The assumption made for all flights was that the threshold was set at 4 and therefore there would be counts in bin 5 and above. For flight 13 the counts did not pick up until around bin 30. This left a hole in the particle cross-section distribution which the inversion algorithm could not fit with a power law, and spurious predictions resulted.

## 4.0 Conclusions

The basis of the volume mode and single particle mode algorithms has been discussed. Programming and data handling techniques have been described. Some sources of systematic error in the previously processed flight data have been examined. Statistical uncertainty in the processed flight data has been evaluated.

A rescaling of the single particle gain function as a result of a more exact handling of the calibration has resulted in a decrease by 2.9 orders of magnitude of the backscatter coefficient in the single particle mode. This leaves a differential of about two orders of magnitude with the prediction of the volume mode method. Two possible explanations were offered for this difference: a) The single particle mode signal versus bin calibration for the processor is not correct. b) The particle density conditions during data collection did not conform to one particle per transit time. A further possibility is that the volume channel signal is either incorrect, or incorrectly interpreted.

The statistical errors for the two methods produced a maximum of  $\pm .44$  orders of magnitude uncertainty for the volume mode and  $\pm .54$  orders of magnitude uncertainty for the single particle mode. The processed results do not agree within these errors.

Studies of the effects of particle number fluctuations in

the processing of both modes show that, in order to reduce deviations of the local mean from a mean calculated with 10000 particles, and to reduce fluctuations of the data from the local mean, care must be exercised regarding the number of particles processed. To keep these errors near .1 orders of magnitude, this number of particles must be 1000 for the single particle mode, and 3000 for the volume mode. This requires a very short flight length (<1km) for particles with densities as low as one particle per 1000 cubic centimeters.

In order to better understand the behavior of LDV systems operating in these two modes, it is suggested that laboratory measurements on aerosol standards be accomplished with the inflight processor. The calibration techniques which were interrupted by the flight schedule could be continued, or perhaps the input or exhaust from a Knollenberg counter could be used. A comparison of the two methods needs to be accomplished and their limits of applicability determined in the laboratory. The methods are independent assessments of aerosol distribution characteristics and, operating together, offer a unique means of converging on more precise measurements.



## REFERENCES

1. Final Report on Contract No. NAS8-34337, Beta Experiment, June 1982, Applied Research, Inc.
2. Final Report on "Added Scope" to Contract NAS8-34337, Beta Experiment, April 30, 1983, Applied Research, Inc.
3. M.J. Post, et. al., "Calibration of Coherent Lidar Targets", Applied Optics, 19, 15 August 1983, p.2828.

## APPENDIX

### Program Descriptions

Main Program - Sets up calibration data (except for gain versus area table); controls reading of data and number of particles/inversion; contains volume  $\beta$  computations and writes the output data file; computes flight length and single  $\beta$  after calling DATANAL.

Subroutine GETDAT - Reads the flight data from disk as 192 words (4 bytes long) and converts to 384 words (unpacks the data).

- Inputs - None

- Outputs- BUF= 384 word array containing all data.

DATA= 256 word array containing the counts in the signal processor for the single particle.

Subroutine DATANAL - Sets up the gain versus area table and then calls OPTIM to do the actual inversion.

- Inputs - NT= Total # of particle counts

M = # of signal bin segments

MS= # of cross-section segments

- Outputs- WS= average cross-section

WV= average focal volume cross-section area

Subroutine OPTIM - does the inversion using three different fits

for the cross-section distribution: (1) power law (2) exponential (3) and log-normal. This routine iterates using each distribution type in turn to find the best match between the real single particle count histogram and the predicted count histogram.

- Inputs -
  - B= first power law exponent trial
  - N= total # of particle counts
  - M= # of signal bin segments
  - MS= # of sigma (cross-section) segments
  - NI= # of integration steps
  - YY= array that contains scaled gain values for the "area" table
  - ARR= array that contains areas for corresponding array YY
- Outputs-
  - WSS= predicted average cross-section
  - WVS= predicted average focal volume cross-sectional area

Subroutine COEF2 - calculates the difference between two area values in an integration step.

- Inputs -
  - I= index in SGL array (signal bin)
  - J= index in SIG array (cross-section)
  - K= integration step
  - DJ=  $\Delta$  sigma for index J
  - M= # of cross-section segments
- Outputs -
  - C= area difference

Subroutine LPICK - generate a good starting point for the log-normal solution.

- Inputs - SIG= cross-section array  
          MS= # of cross-section segments
- Outputs - BP= selected mean value of log  
          DB= mean value of log increment selected  
          ALP= selected standard deviation of log  
          DALP= standard deviation of log increment selected

Subroutine EPICK - generate a good starting point for the exponential solution.

- Inputs - SIG= cross-section array  
          BPl= selected power law fit from power law solution  
          MS= # of cross-section segments
- Outputs - BP= selected exponential power  
          DP= exponential power increment

Subroutine PROW - computes normalized probabilities for the power law, exponential and log-normal distribution depending upon the value of IP.

- Inputs - BP= fit parameter for solution:
  - power law - exponent
  - exponential - exponential coefficient
  - log-normal - mean value of log

IP= 1=power law

2=exponential

3=log-normal

SIP= selected cross-section for which probability  
will be calculated

SO= (required only for log-normal) selected  
standard deviation of log value

A3= (required only for log-normal) normalization  
factor for the selected log-normal  
parameters

Function YLIN - linear interpolation function.

- Inputs - N= # of data parts in array

XX= dependent variable that results is derived  
to be interpolated for

X= array of dependent variable values

Y= array of independent variable values for  
which interpolations are performed

- Outputs -YLIN= interpolated value

```

1 - 10,000 C *****
2 - 20,000 C
3 - 30,000 C THESE FILES MUST ALL BE ASSIGNED PRIOR TO STARTING DATANAL.
4 - 40,000 C
5 - 50,000 C 1. SET F:5/MM#;IN ( M## = DISK FILE CONTAINING FLIGHT DATA )
6 - 60,000 C 2. SET F:12/CALFIL4;IN ( CALIBRATION DATA DISK FILE )
7 - 70,000 C 3. SET F:10=ME;OUT ( CRT TERMINAL OUTPUT )
8 - 80,000 C 4. SET F:12=ME;OUT ( CRT TERMINAL OUTPUT )
9 - 90,000 C 5. SET F:13/P#;OUT ( P## = DISK FILE CONTAINING PLOT DATA )
10 - 100,000 C
11 - 110,000 C *****
12 - 120,000 C
13 - 130,000 C COMMON/OPT/DS(22),NP(22),FST,FN
14 - 140,000 C COMMON/COE2/SIG(22),SGL(22),WI
15 - 150,000 C INTEGER BUF, DATA
16 - 160,000 C DIMENSION DATA(256),ISBIN(256),BUF(384),CAL(26,51)
17 - 170,000 C DIMENSION IXBUF(26),XNOISE(51),YRUF(51),XSGL(22)
18 - 180,000 C DIMENSION ISN(256), XDS(22)
19 - 190,000 C DATA XSGL/=57.75,-56.0,-54.0,-50.25,-46.125,-41.5,-35.75/
20 - 200,000 C DATA XDS/4,6,16,32,64,127,1/,ITHRESH/4/,M/6/,MS/6/
21 - 210,000 C
22 - 220,000 C XSGL IS THE SIGNAL ARRAY AND CONTAINS THE DBSM VALUES
23 - 230,000 C FOR THE SELECTED SIGNAL BINS ON THE PROCESSOR.
24 - 240,000 C
25 - 250,000 C XDS IS THE SIGNAL BIN ARRAY AND CONTAINS THE SIGNAL BIN_RANGES
26 - 260,000 C ( 1-4 , 5-12 , 13-28 , ETC. ).
27 - 270,000 C
28 - 280,000 C IREC IS THE DATA RECORD COUNTER
29 - 290,000 C
30 - 300,000 C INPUT PROCESSING PARAMETERS / ASSUMPTIONS :
31 - 310,000 C
32 - 320,000 C M IS THE NUMBER OF SIGNAL BINS. ( M = 6 )
33 - 330,000 C
34 - 340,000 C MS IS THE NUMBER OF SIGMA BINS. ( MS = 6 )
35 - 350,000 C
36 - 360,000 C ITHRESH IS THE THRESHOLD SETTING ON THE PROCESSOR. ( ITHRESH = 4 )
37 - 370,000 C
38 - 380,000 C XDS = SIGNAL BIN_RANGES.
39 - 390,000 C
40 - 400,000 C # 1 = 4 BINS
41 - 410,000 C # 2 = 8 BINS
42 - 420,000 C # 3 = 16 BINS
43 - 430,000 C # 4 = 32 BINS
44 - 440,000 C # 5 = 64 BINS
45 - 450,000 C # 6 = 127 BINS
46 - 460,000 C # 7 = 1 BINS
47 - 470,000 C LAST SIGNAL BIN CONTAINS ALL PARTICLES WITH VALUES .GE.
48 - 480,000 C CORRESPONDING SIGNAL.
49 - 490,000 C
50 - 500,000 C XSGL = SIGNAL BIN VALUES THAT CORRESPOND TO SIGNAL BINS.

```

```

51 - 510.000 C
52 - 520.000 C
53 - 530.000 C
54 - 540.000 C
55 - 550.000 C
56 - 560.000 C
57 - 570.000 C
58 - 580.000 C
59 - 590.000 C
60 - 600.000 C
61 - 610.000 C
62 - 620.000 C
63 - 630.000 C
64 - 640.000 C
65 - 650.000 C
66 - 660.000 C
67 - 670.000 C
68 - 680.000 C
69 - 690.000 C
70 - 700.000 C
71 - 710.000 C
72 - 720.000 C
73 - 730.000 C
74 - 740.000 C
75 - 750.000 C
76 - 760.000 C
77 - 770.000 C
78 - 780.000 C
79 - 790.000 C
80 - 800.000 C
81 - 810.000 C
82 - 820.000 C
83 - 830.000 C
84 - 840.000 C
85 - 850.000 C
86 - 860.000 C
87 - 870.000 C
88 - 880.000 C
89 - 890.000 C
90 - 900.000 C
91 - 910.000 C
92 - 920.000 C
93 - 930.000 C
94 - 940.000 C
95 - 950.000 C
96 - 960.000 C
97 - 970.000 C
98 - 980.000 C
99 - 990.000 C
100 - 1000.000 C
101 - 1010.000 C
102 - 1020.000 C

```

OTHER ASSUMPTIONS :

- L<sub>EFF</sub> AT 10 METERS = 0.6407 METERS.
- WAIST RETURN FOR A SANDPAPER DISK AT 10 METERS = 1.053 E 6.
- SINGLE PARTICLE GAIN FOR A ZERO ARFA IS 1.10376 E 7 METERS \*\* -2.

```

IREC=0
DO 100 I=1,51
CALL BUFFERIN(12,1,IXBUF,26,ISTST,NMRO,IAB)
WRITE(9,137) (IXBUF(I),I=1,26)
FORMAT(1H '-',CAL DATA ',3(1X,9I8.7))
DO 110 J=1,26
CAL IS THE CALIBRATION DATA ARRAY.
IT IS USED TO CONVERT COUNTS TO DBMS FOR THE VOLUME
BETA CHANNEL AND TO OBTAIN NOISE FIGURES FOR THE
SINGLE BETA.
1ST INDEX IS OVER IF GAIN = 26 VALUES
2ND INDEX IS OVER DBSM VALUES RANGING FROM -71 TO -20
CAL(J,I) = IXBUF(J)
CONTINUE
DO 122 J=1,51
XNOISE(J)=71+J
CONTINUE
KH = 0
KS = 0
KF = 0
KKK = 0
NNSUM = 0
SSVOL = 0
NSUM = 0
SVOL = 0
ISUM = 0
DO 40 I=1,256
ISN(I) = 0
ISBIN(I)=0
GEIDAT READS THE DATA AND UNPACKS THE DATA
ARRAY TO CONFORM TO ORIGINAL DATA-TAKING
DROP OUT DATA IF AIRSPEED IS LESS THAN 150,
BECAUSE LDV USES THIS VALUE TO TUNE TO
THEREFORE DATA MAY BE BAD
DROP OUT DATA IF THE COUNT IN THE
LAST BIN IS GREATER THAN 5000
THIS MEANS THE INVERSION ALGORITHM

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103 - 1030.000 C      CANNOT HANDLE THESE CASES
104 - 1040.000 C
105 - 1050.000 S      CALL GETDAT(BUF, DATA)
106 - 1060.000      IF (DATA(256).GT.5000) GO TO 6
107 - 1070.000      IF (DATA(1).EQ.1E6) STOP
108 - 1080.000      IREC = IREC + 1
109 - 1090.000      IF (BUF(32).GT.150) GO TO 175
110 - 1100.000 6      CONTINUE
111 - 1110.000      CALL GETDAT(BUF, DATA)
112 - 1120.000      IF (DATA(1).EQ.1E6) STOP
113 - 1130.000      IREC=IREC+1
114 - 1140.000      GO TO 5
115 - 1150.000 175    CONTINUE
116 - 1160.000      IF (KKK.GT.0) GO TO 173
117 - 1170.000      KSH = BUF(5)
118 - 1180.000      KSM = BUF(6)
119 - 1190.000      KSS = BUF(7)
120 - 1200.000      KSF = BUF(8)
121 - 1210.000 173    CONTINUE
122 - 1220.000      IF (BUF(8).LE.BUF(4)) GO TO 69
123 - 1230.000      BUF(3) = BUF(3) - 1
124 - 1240.000      BUF(4) = BUF(4) + 1000
125 - 1250.000 69     NF = BUF(4) - BUF(8)
126 - 1260.000      IF (BUF(7).LE. BUF(3)) GO TO 71
127 - 1270.000      BUF(2) = BUF(2) - 1
128 - 1280.000      BUF(3) = BUF(3) + 60
129 - 1290.000 71     NS = BUF(3) - BUF(7)
130 - 1300.000      IF (BUF(6).LE. BUF(2) ) GO TO 73
131 - 1310.000      BUF(1) = BUF(1) - 1
132 - 1320.000      BUF(2) = BUF(2) + 60
133 - 1330.000 73     NM = BUF(2) - BUF(6)
134 - 1340.000      NH = BUF(1) - BUF(5)
135 - 1350.000      KS = KS + (3600 * NH) + (60 * NM) + NS
136 - 1360.000      KF = KF + NF
137 - 1370.000      IF (KF.LT.1000) GO TO 74
138 - 1380.000      KF = KF - 1000
139 - 1390.000      KS = KS + 1
140 - 1400.000 74     CONTINUE
141 - 1410.000      KBUF = KBUF + BUF(32)
142 - 1420.000      KKK = KKK + 1
143 - 1430.000 C
144 - 1440.000 C      ISUM IS THE TOTAL NUMBER OF PARTICLES FOR ALL BINS.
145 - 1450.000 C      LATER, THE NOISE IS SUBTRACTED FROM ISUM.
146 - 1460.000 C
147 - 1470.000 C      DATA IS AN INTEGER ARRAY CONTAINING A RUNNING TOTAL OF PARTICLE
148 - 1480.000 C      COUNTS FOR EACH BIN.
149 - 1490.000 C
150 - 1500.000 C      VB IS THE VOLUME BETA COUNT FOR THIS RECORD.
151 - 1510.000 C
152 - 1520.000 C      IFG IS THE IF GAIN FOR THIS RECORD.
153 - 1530.000 C
154 - 1540.000 C      SVOL IS THE RUNNING SUM OF THE VOLUME BETA COUNT.

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155 - 1550.000 C
156 - 1560.000 C
157 - 1570.000 C
158 - 1580.000 C
159 - 1590.000 C
160 - 1600.000 C
161 - 1610.000 C
162 - 1620.000 C
163 - 1630.000
164 - 1640.000
165 - 1650.000 50
166 - 1660.000
167 - 1670.000
168 - 1680.000
169 - 1690.000
170 - 1700.000
171 - 1710.000 C
172 - 1720.000 C
173 - 1730.000 C
174 - 1740.000
175 - 1750.000
176 - 1760.000
177 - 1770.000
178 - 1780.000
179 - 1790.000
180 - 1800.000 60
181 - 1810.000
182 - 1820.000
183 - 1830.000
184 - 1840.000
185 - 1850.000
186 - 1860.000
187 - 1870.000 C
188 - 1880.000 C
189 - 1890.000
190 - 1900.000 C
191 - 1910.000 C
192 - 1920.000 C
193 - 1930.000 C
194 - 1940.000 C
195 - 1950.000
196 - 1960.000
197 - 1970.000
198 - 1980.000
199 - 1990.000
200 - 2000.000
201 - 2010.000
202 - 2020.000 269
203 - 2030.000
204 - 2040.000
205 - 2050.000
206 - 2060.000

      ISN IS AN INTEGER ARRAY CONTAINING THE RUNNING TOTAL OF PARTICLE
      COUNTS FOR THE NOISE DATA IN EACH BIN.

      INOISE IS THE TOTAL NUMBER OF PARTICLE COUNTS FOR THE NOISE DATA.
      LATER, INOISE IS SUBTRACTED FROM ISUM.

      DO 50 I=1,256
      ISUM=ISUM + DATA(I)
      ISBIN(I) = ISBIN(I) + DATA(I)
      ITR = ISL(RUF(15),16)
      VB = IOR(ITR,BUF(16))
      IFG = RUF(25)
      NSUM = NSUM + BUF(17)
      SVOL = SVOL + VB

      CALL SUBROUTINE GETDAT TO READ THE NOISE DATA RECORD.

      INOISE = 0
      CALL GETDAT(BUF,DATA)
      IF (DATA(1).EQ.1E6) STOP
      IREC=IREC+1
      DO 60 L=1,256
      ISN(L) = ISN(L) + DATA(L)
      INOISE = INOISE + DATA(L)
      ISUM=ISUM-INOISE
      ITR = ISL (BUF(15),16)
      VB = IOR (ITR,BUF(16))
      IFG = BUF(25)
      NSUM = NSUM + BUF(17)
      SVOL = SVOL + VB
      OUTPUT ISUM, INOISE, ISBIN(256)
      IF (ISUM .LE. 1000) GO TO 5

      1000 PARTICLE COUNTS OR ABOVE MUST
      BE OBTAINED BEFORE DATA IS SENT TO
      INVERSION ALGORITHM

      KCH = BUF(1)
      KCM = BUF(2)
      KCS = BUF(3)
      KCF = BUF(4)
      IF (KSF .LE. KCF) GO TO 269
      KCS = KCS + 1
      KCF = KCF + 1000
      IFRAC = (KCF-KSF)/2
      IF (KSS .LE. KCS) GO TO 270
      KCM = KCM + 1
      KCS = KCS + .60

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207 = 2070.000 270 NSECS = (KCS - KSS)/2
208 = 2080.000 IF (KSM .LE. KCM) GO TO 271
209 = 2090.000 KCH = KCM - 1
210 = 2100.000 KCM = KCM + 60
211 = 2110.000 271 MNM = (KCM - KSM)/2
212 = 2120.000 NMR = KCH - KSH
213 = 2130.000 LF = KSF + IFRAC
214 = 2140.000 IF (LF .LT. 1000) GO TO 331
215 = 2150.000 LF = LF - 1000
216 = 2160.000 KSS = KSS + 1
217 = 2170.000 331 LS = KSS + NSECS
218 = 2180.000 IF (LS .LT. 60) GO TO 332
219 = 2190.000 LS = LS - 60
220 = 2200.000 KSM = KSM + 1
221 = 2210.000 332 LM = KSM + NMN
222 = 2220.000 IF (LM .LT. 60) GO TO 334
223 = 2230.000 LM = LM - 60
224 = 2240.000 KSH = KSH + 1
225 = 2250.000 334 LH = KSH + NMR
226 = 2260.000 OUTPUT IREC
227 = 2270.000 WRITE(6,138) VB,IFG,BUF(17)
228 = 2280.000 138 FORMAT(IX,'VR,IFG,BUF(17)=',F10.1,2I10)
229 = 2290.000 DO 200 I=1,51
230 = 2300.000 C
231 = 2310.000 C A SCALE FACTOR OF 500 CAME FROM A CONVERSATION WITH WILLIAM JONES.
232 = 2320.000 C YBUF(I) = CAL(71-IFG,I)/500
233 = 2330.000 C CONTINUE
234 = 2340.000 200
235 = 2350.000 C
236 = 2360.000 C VB IS THE ACCUMULATED VOLUME BETA COUNT FOR THE
237 = 2370.000 C NOISE DATA.
238 = 2380.000 C VSIGL IS THE VOLUME BETA LINEAR SIGNAL
239 = 2390.000 C VSIGL = DATA - NOISE.
240 = 2400.000 C
241 = 2410.000 C
242 = 2420.000 C RVB IS THE AVERAGE VOLUME BETA COUNT FOR THE DATA.
243 = 2430.000 C VNS IS THE VOLUME BETA LINEAR NOISE SIGNAL.
244 = 2440.000 C
245 = 2450.000 C FINALB IS THE FINAL VOLUME BETA FOR THIS DATA SET.
246 = 2460.000 C
247 = 2470.000 C
248 = 2480.000 C THE INTEGRATED VOLUME RETARVB) IS MULTIPLIED BY A
249 = 2490.000 C BIDIRECTIONAL REFLECTANCE PARAMETER ( = .016)
250 = 2500.000 C THEN DIVIDED BY THE SIGNAL RETURN FOR A
251 = 2510.000 C SANDPAPER DISK AT 10 METERS AT THE WAIST
252 = 2520.000 C ( = 1.642824E6) AND THEN DIVIDED BY THE L-EFF
253 = 2530.000 C AT 10 METERS ( = 0.6407). SEE APPLIED
254 = 2540.000 C RESEARCH REPORTS FOR COMPLETE DOCUMENTATION.
255 = 2550.000 C
256 = 2560.000 C
257 = 2570.000 C VR = SSVOL/MNSUM
258 = 2580.000 C

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259 - 2590.000 C CONVERT_VB_ID,DBMS ( NOISE DATA )
260 - 2600.000 C
261 - 2610.000 DBMNS = YLIN(S1,VB,YBUF,XNOISE)
262 - 2620.000 PVB=SVOL/NSUM
263 - 2630.000 C
264 - 2640.000 C CONVERT_PVB_TO_DBMS ( DATA )
265 - 2650.000 C
266 - 2660.000 SDBMNS=YLIN(S1,RVB,YBUF,XNOISE)
267 - 2670.000 VSIGL=10**((SDBMNS/10.)-10**((DBMNS/10.)
268 - 2680.000 VNS=10**((DBMNS/10.)
269 - 2690.000 FINALB=VSIGL/VNS*.016/1.842R924E6/.6407
270 - 2700.000 C OUTPUT DBMNS
271 - 2710.000 C OUTPUT_FINALB,VSIGL,VNS,SVOL,NSUM
272 - 2720.000 C
273 - 2730.000 C VB IS USED TO EXTRACT A NOISE VALUE FOR
274 - 2740.000 C THIS SET OF SINGLE PARTICLE DATA
275 - 2750.000 C BY INTERPOLATING
276 - 2760.000 C THE CALIBRATION DATA (CAL(I,J))
277 - 2770.000 C
278 - 2780.000 C DBMNS = THE NOISE IN DBMS
279 - 2790.000 C ITHRESH = THE BIN WHERE THE SIGNALS ARE
280 - 2800.000 C THRESHOLDED - ABOVE ITHRESH CONTAINS
281 - 2810.000 C DATA
282 - 2820.000 C NP = THE NUMBER OF PARTICLES ARRAY =
283 - 2830.000 C CONTAINS NUMBER OF PARTICLE HITS IN THE
284 - 2840.000 C SELECTED BINS
285 - 2850.000 C
286 - 2860.000 C THE FACTOR 1.5/.86 APPEARS IN THE NOISE
287 - 2870.000 C CALCULATION(DBMNS) BECAUSE THIS IS THE
288 - 2880.000 C DIFFERENCE IN BANDWIDTH BETWEEN THE SINGLE
289 - 2890.000 C PARTICLE DATA AND THE VOLUME CHANNEL DATA
290 - 2900.000 C
291 - 2910.000 C DBMNS IS THE SINGLE BETA NOISE FACTOR ( DBMS ).
292 - 2920.000 C
293 - 2930.000 C SGL (I) IS THE LINEAR SIGNAL VALUE THAT EACH PROCESSOR_BIN
294 - 2940.000 C USED CORRESPONDS TO.
295 - 2950.000 C
296 - 2960.000 C NP (J) IS THE ACCUMULATION OF SINGLE PARTICLE
297 - 2970.000 C COUNTS IN THE BIN RANGES SELECTED FROM
298 - 2980.000 C ARRAY XDS.
299 - 2990.000 C
300 - 3000.000 C CNV=10**((DBMNS/10)
301 - 3010.000 C DBMNS=10*LOG10(CNV*1.5/.86)
302 - 3020.000 C DO 210 I = 1,M+1
303 - 3030.000 C SGL(I) = 10**((XVSGL(I)-DBMNS)/10)
304 - 3040.000 C CONTINUE
305 - 3050.000 C OUTPUT SGL
306 - 3060.000 C K = ITHRESH + 1
307 - 3070.000 C DO 66 JJ=1,22
308 - 3080.000 C NP(JJ) = 0
309 - 3090.000 C CONTINUE
310 - 3100.000 C DO 55 J=1,M+1

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311 - 3110.000 KK=K+XDS(J)-1
312 - 3120.000 DO 10 I = K,KK
313 - 3130.000 NP(J) = NP(J) + ISAIN(I)-ISN(I)
314 - 3140.000 10 CONTINUE
315 - 3150.000 K=KK+1
316 - 3160.000 55 CONTINUE
317 - 3170.000 C OUTPUT NP,ISBIN,ISN
318 - 3180.000 C
319 - 3190.000 C
320 - 3200.000 C DETERMINE SIGMAS THAT CORRESPOND TO SIGNAL BINS
321 - 3210.000 C 1.E8- CONVERTS FROM CM**2 TO MICRON**2
322 - 3220.000 C 1.10376E7 IS THE SINGLE PARTICL GAIN AT AN AREA OF ZERO
323 - 3230.000 DO 300 J = 1,M + 1
324 - 3240.000 SIG(I) = SGL(I)*1.E8/1.10376E7
325 - 3250.000 300 CONTINUE
326 - 3260.000 C
327 - 3270.000 C SIG IS THE CROSS SECTION ARRAY.
328 - 3280.000 C
329 - 3290.000 C SIL IS THE SMALLEST CROSS SECTION.
330 - 3300.000 C
331 - 3310.000 C SIH IS THE LARGEST CROSS SECTION.
332 - 3320.000 C
333 - 3330.000 SIL = SIG(I)
334 - 3340.000 SIH = SIG(M + 1)
335 - 3350.000 C OUTPUT SIG
336 - 3360.000 C OUTPUT SIL,SIH
337 - 3370.000 C OUTPUT ISUM
338 - 3380.000 C
339 - 3390.000 C CALL SUBROUTINE DATANAL TO DO ACTUAL INVERSION.
340 - 3400.000 C
341 - 3410.000 C
342 - 3420.000 C ELS - THE ELAPSED TIME IN SECS FOR WHICH DATA
343 - 3430.000 C WAS TAKEN
344 - 3440.000 C FLTL - THE FLIGHT LENGTH IN METERS
345 - 3450.000 C SINGLEB - THE SINGLE PARTICLE BETA
346 - 3460.000 C WS - THE AVERAGE CROSS-SECTION OF PARTICLE
347 - 3470.000 C SQUARE MICRONS
348 - 3480.000 C MW - THE AVERAGE SIZE OF THE TRANSVERSE
349 - 3490.000 C CROSS-SECTION OF FOCAL VOLUME
350 - 3500.000 C PREDICTED FROM INVERSION ALGORITHM
351 - 3510.000 C
352 - 3520.000 C CALL DATANAL(ISUM,M,MS,WS,MV)
353 - 3530.000 C
354 - 3540.000 ELS = KS + KF/1000.
355 - 3550.000 FLTL = KBUF/KKK*.5144*ELS
356 - 3560.000 IF(MV.EQ.0) MW=1.E-30
357 - 3570.000 SINGLEB = ISUM/4/3.14159265359/FLTL/MV*MS
358 - 3580.000 OUTPUT SINGLEB,FLTL,ELS
359 - 3590.000 WRITE(6,702) BUF(9),BUF(10), BUF(11)
360 - 3600.000 702 FORMAT(1X,DATE,12,12,12,12,12,12,12,12,12,12,12,12)
361 - 3610.000 WRITE (6,703) LH,LW,LS,LF
362 - 3620.000 703 FORPAT(1X,TIME,12,12,12,12,12,12,12,12,12,12,12,12)

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363 - 3630.000 WRITE(6,704)
364 - 3640.000 704 FORMAT(////)
365 - 3650.000 WRITE(13) LM,LM,LS,LF,SINGLEB,FINALB,MS,FLTL,ELS,WV
366 - 3660.000 ISUM = 0
367 - 3670.000 INoise=0
368 - 3680.000 GO TO 122
369 - 3690.000 678 STOP
370 - 3700.000 END
371 - 3710.000 C
372 - 3720.000 C
373 - 3730.000 C
374 - 3740.000 SUBROUTINE GETDAT(BUF,DATA)
375 - 3750.000 C
376 - 3760.000 C THIS SUBROUTINE READS THE DATA FROM DISK AS 192 WORDS,
377 - 3770.000 C EACH WORD READ IN CONTAINS 4 BYTES.
378 - 3780.000 C THE DATA IS THEN CONVERTED SO THAT THERE ARE 384 WORDS.
379 - 3800.000 C
380 - 3810.000 DIMENSION DUM(7),DUMM(31),ID(20),DATA(256),BUFF(192),BUF(384)
381 - 3820.000 IMPLICIT INTEGER(C,S,D,F,V,B)
382 - 3830.000 III=0
383 - 3840.000 10. CONTINUE
384 - 3850.000 III=III+1
385 - 3860.000 III=0
386 - 3870.000 301 FORMAT(IX,6Hbuff=,48(IX,RIA,/)
387 - 3880.000 CALL BUFFER_IN(S,L,BUFF,192,ISTAT,NWRD,IAB)
388 - 3890.000 C OUTPUT ISTAT,NWRD,IAB
389 - 3900.000 C WRITE(6,301) (BUFF(I),I=1,384)
390 - 3910.000 C IF(ISTAT.EQ.3) DATA(I)=IE6
391 - 3920.000 C IF(ISTAT.EQ.3) RETURN
392 - 3930.000 DO 300 I=1,384,2
393 - 3940.000 II=II+1
394 - 3950.000 II=IAND(BUFF(II),8FF000000)
395 - 3960.000 I2=IAND(BUFF(II),8200FF0000)
396 - 3970.000 I3=IAND(BUFF(II),820000FF00)
397 - 3980.000 I4=IAND(BUFF(II),82000000FF)
398 - 3990.000 I1=ISL(I1,-24)
399 - 4000.000 I2=ISL(I2,-8)
400 - 4010.000 I3=ISL(I3,-8)
401 - 4020.000 I4=ISL(I4,8)
402 - 4030.000 BUF(I)=IOR(I2,I1)
403 - 4040.000 BUF(I+1)=IOR(I4,I3)
404 - 4050.000 300 CONTINUE
405 - 4060.000 DO 100 K=1,20
406 - 4070.000 ID(K)=BUF(K+48)
407 - 4080.000 100 CONTINUE
408 - 4090.000 DO 200 L=1,256
409 - 4100.000 DATA(L)=BUF(L+128)
410 - 4110.000 200 CONTINUE
411 - 4120.000 C *****
412 - 4130.000 C CH = CURRENT TIME HOURS *****
413 - 4140.000 C CM = CURRENT TIME MINUTES *****
414 - 4150.000 C CS = CURRENT TIME SECONDS *****

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415 = 4160.000 C CF = CURRENT TIME FRACTIONS
416 = 4170.000 C SH = START OF RECORD HOUR
417 = 4180.000 C SM = START OF RECORD MINUTE
418 = 4190.000 C SS = START OF RECORD SECOND
419 = 4200.000 C SF = START OF RECORD FRACTION
420 = 4210.000 C DRT = NUMBER BEFORE DIS. THRESHOLD
421 = 4220.000 C DT = DISCRIMINATOR THRESHOLD
422 = 4230.000 C FBI = NUMBER BEFORE FORWARD/AFT IDENTIFIER
423 = 4240.000 C FI = FORWARD/AFT IDENTIFIER
424 = 4250.000 C DATA = DATA
425 = 4260.000 C ID = IDENTIFICATION STRING
426 = 4270.000 C *****
427 = 4280.000 C CM=BUF(1)
428 = 4290.000 C CM=BUF(2)
429 = 4300.000 C CM=BUF(3)
430 = 4310.000 C CF=BUF(4)
431 = 4320.000 C SM=BUF(5)
432 = 4330.000 C SM=BUF(6)
433 = 4340.000 C SM=BUF(7)
434 = 4350.000 C SF=BUF(8)
435 = 4360.000 C DBT=BUF(23)
436 = 4370.000 C DT=BUF(24)
437 = 4380.000 C FBI=BUF(25)
438 = 4390.000 C FI=BUF(26)
439 = 4400.000 C
440 = 4410.000 401 WRITE(6,401) SM,SM,SS,SF
FORMAT(IX,START TIME: ',4I10)
441 = 4420.000 C WRITE(6,402) CH,CM,CS,CF
442 = 4430.000 C WRITE(6,405) BUF(15),BUF(16),BUF(17)
443 = 4440.000 405 FORMAT(IX,VOLUME BETA INT',3I10)
444 = 4450.000 402 FORMAT(IX,END TIME: ',4I10)
445 = 4460.000 C WRITE(6,403) DT
446 = 4470.000 403 FORMAT(IX,DISCRIMINATOR THRESHOLD ',I10)
447 = 4480.000 C WRITE(6,406) BUF(25)
448 = 4490.000 406 FORMAT(IX,IF GAIN',I10)
449 = 4500.000 C WRITE(6,404) FI
450 = 4510.000 404 FORMAT(IX,FORWARD/AFT ID ',I10)
451 = 4520.000 C WRITE(10) (ID(I),I=1,20)
452 = 4530.000 C WRITE(6,120) (DATA(I),I=1,128)
453 = 4540.000 120 FORMAT(IX,16(IX,8I8,/)
454 = 4550.000 IF (III.GT.500) RETURN
455 = 4560.000 RETURN
456 = 4570.000 END
457 = 4580.000 C
458 = 4590.000 C
459 = 4600.000 C
460 = 4610.000 C
461 = 4620.000 C
462 = 4630.000 C
463 = 4640.000 C
464 = 4650.000 C
465 = 4660.000 C
466 = 4670.000 C

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SUBROUTINE DATANAL(NT,M,MS,WS,WV)

THE PRIMARY FUNCTION OF THIS SUBROUTINE IS TO DEFINE  
THE AREA CURVE PROPERLY FOR THE CALL TO SUBROUTINE  
OPTIM. SOME OF THE CALCULATIONS DONE HERE ARE NOW  
UNNECESSARY.

467 - 4680.000 C ARR IS AN ARRAY CONTAINING THE UNSCALED LINEAR SIGNAL / NOISE / SIGMA  
 468 - 4690.000 C VALUES THAT CORRESPOND TO THE AREAS UNDER THE AREA CURVE.  
 469 - 4700.000 C  
 470 - 4710.000 C ARR VS. SIGMA / Y IS THE UNSCALED AREA CURVE.  
 471 - 4720.000 C  
 472 - 4730.000 C DS IS AN ARRAY CONTAINING THE RANGE OF SIGMA VALUES IN THE SIG ARRAY.  
 473 - 4740.000 C  
 474 - 4750.000 C AR IS THE FINAL ARRAY OF AREA VALUES THAT CORRESPOND TO  
 475 - 4760.000 C AX, THE SIGNAL / NOISE / SIGMA VALUES.  
 476 - 4770.000 C  
 477 - 4780.000 C SRMN IS THE MINIMUM SIGNAL / NOISE / SIGMA VALUE REQUIRED FROM  
 478 - 4790.000 C THE AREA TABLE.  
 479 - 4800.000 C  
 480 - 4810.000 C SRMX IS THE MAXIMUM SIGNAL / NOISE / SIGMA VALUE REQUIRED FROM  
 481 - 4820.000 C THE AREA TABLE.  
 482 - 4830.000 C  
 483 - 4840.000 C TRANS IS THE MULTIPLICATIVE FACTOR THAT CORRECTS  
 484 - 4850.000 C THE AREA CURVE  
 485 - 4860.000 C SO THAT THE AREAS CORRESPOND TO THE PROPER S/N/SIGMA  
 486 - 4870.000 C  
 487 - 4880.000 C  
 488 - 4890.000 C DIMENSION DAND(101,2)  
 489 - 4900.000 C DIMENSION YY(125),ARR(125)  
 490 - 4910.000 C COMMON/OPT/DS(22),NP(22),FSl,FN  
 491 - 4920.000 C COMMON/ARE/F(2),AL,RO,MI,A  
 492 - 4930.000 C COMMON/ARC1/ARC(101),DSR,SRMX,AXX(101)  
 493 - 4940.000 C COMMON/SS/X(2),Y(2),Z(2)  
 494 - 4950.000 C DATA PH,ETA,BW,RO,F,AL,AM,NI,FSl/5.,.05,  
 495 - 4960.000 C 1 1.E+6,.046,10.,10.,1.,.3.1622777,30,1.973/  
 496 - 4970.000 C DATA PI,HP,CL,FLDA  
 497 - 4980.000 C 1/.3.14159,6.62502E-34,3.E+8,10.6E-6/  
 498 - 4990.000 C DATA B,IP/1.5,1/  
 499 - 5000.000 C DATA ARR/31,2,4E5,2.30E5,2.30E5,2.30E5,2.30E5,2.30E5,  
 500 - 5010.000 C 1 2.35E5,2.34E5,2.32E5,2.31E5,2.30E5,2.30E5,2.29E5,  
 501 - 5020.000 C 1 2.28E5,2.27E5,2.25E5,2.22E5,2.20E5,2.19E5,2.16E5,  
 502 - 5030.000 C 1 2.12E5,2.11E5,2.10E5,2.1E5,2.05E5,2.01E5,1.98E5,  
 503 - 5040.000 C 1 1.89E5,1.85E5,1.80E5,1.76E5,1.72E5,1.69E5,1.65E5,  
 504 - 5050.000 C 1 1.60E5,1.57E5,1.53E5,1.50E5,1.46E5,1.43E5,1.38E5,1.35E5,  
 505 - 5060.000 C 1 1.32E5,1.25E5,1.19E5,1.13E5,1.07E5,1.03E5,9.7E4,  
 506 - 5070.000 C 1 9.3E4,8.9E4,8.6E4,8.3E4,7.7E4,7.5E4,7.3E4,6.9E4,  
 507 - 5080.000 C 1 6.6E4,6.2E4,5.9E4,5.2E4,4.8E4,4.5E4,4.2E4,3.9E4,3.7E4,  
 508 - 5090.000 C 1 3.3E4,2.9E4,2.6E4,2.3E4,2.1E4,1.95E4,1.8E4,1.75E4,  
 509 - 5100.000 C 1 1.52E4,1.40E4,1.3E4,1.2E4,1.11E4,1.03E4,9.7E3,9.2E3,  
 510 - 5110.000 C 1 8.6E3,8.1E3,7.5E3,7.2E3,6.3E3,5.6E3,4.5E3,  
 511 - 5120.000 C 1 4.0E3,3.5E3/  
 512 - 5130.000 C DATA YY/0.0,0.01,0.02,0.03,0.04,0.05,0.06,0.07,0.08,0.09,  
 513 - 5140.000 C A .10,.11,.12,.13,.14,.15,.16,.17,.18,.19,.20,  
 514 - 5150.000 C A .21,.22,.23,.24,.25,.26,.27,.28,.29,.30,  
 515 - 5160.000 C A .32,.33,.36,.38,.40,.42,.44,.46,.48,.50,.52,.54,.56,  
 516 - 5170.000 C A .58,.60,.65,.70,.75,.80,.85,.90,.95,1.0,1.1,1.2,1.3,  
 517 - 5180.000 C A 1.4,1.5,1.6,1.7,1.8,1.9,2.0,2.1,2.2,2.3,2.4,2.5,  
 518 - 5190.000 C A 2.6,2.7,2.8,2.9,3.0,3.2,3.4,3.6,3.8,4.0,4.2,4.4,4.6,

```

519 - 5200.000 A 4,8,5,0,5,2,5,4,5,6,5,8,6,0,6,5,7,0,7,5,8,0,8,5,9,0,
520 - 5210.000 A 9,5,10,0,11,12,13,14,15,16,17,18,19,20,21,
521 - 5220.000 A 22,23,24,25,26,27,28,29,30,32,34,36,38,
522 - 5230.000 A 40,42,
523 - 5240.000 DATA TRANS/45,99/
524 - 5250.000 DATA N/3E6/
525 - 5260.000 DATA ITEST/1/
526 - 5270.000 IF (ITEST.EQ. 0) GO TO 740
527 - 5280.000 DO 999 I=1,123
528 - 5290.000 ARR(I) = (ARR(I) * TRANS) * 1E-8
529 - 5300.000 999 CONTINUE
530 - 5310.000 C
531 - 5320.000 C 1,E-4 IS USED TO CONVERT THE AREAS FROM CM**2 TO M**2
532 - 5330.000 C
533 - 5340.000 DO 998 I = 1,123
534 - 5350.000 YY(I) = YY(I) * 1E-4
535 - 5360.000 998 CONTINUE
536 - 5370.000 DO 77 I = 1,123
537 - 5380.000 J = 124 - I
538 - 5390.000 IF(I.GT.J) GO TO 78
539 - 5400.000 ATEMP = ARR(I)
540 - 5410.000 APR(I) = ARR(J)
541 - 5420.000 ARR(J) = ATEMP
542 - 5430.000 YTEMP = YY(I)
543 - 5440.000 YY(J) = YY(J)
544 - 5450.000 YY(J) = YTEMP
545 - 5460.000 77 CONTINUE
546 - 5470.000 78 CONTINUE
547 - 5480.000 ITEST = 0
548 - 5490.000 740 A1 = AX*FLDA*FLDA*ETA/RW
549 - 5500.000 AWA1/(16.*PI*PI*PI)*1.E-12
550 - 5510.000 RD=PI*RO*RO/FLDA
551 - 5520.000 ALP=RD/F(1)
552 - 5530.000 R1=RO/2./RD
553 - 5540.000 REO1=F(1)*R1
554 - 5550.000 REO2=F(2)*R1
555 - 5560.000 G1=AZ/(REO1*REO1*REO1)
556 - 5570.000 G2=AZ/(REO2*REO2*REO2)
557 - 5580.000 DO 4 I = 1,M
558 - 5590.000 DS(I) = SIG(I+1) - SIG(I)
559 - 5600.000 4 CONTINUE
560 - 5610.000 X(1)=0.
561 - 5620.000 Y(1)=0.
562 - 5630.000 Z(1)=0.
563 - 5640.000 SIL = SIG(1)
564 - 5650.000 SIH=SIG(M+1)
565 - 5660.000 SRM=SGL(1)/SIL
566 - 5670.000 SRMX=SGL(1)/SIL
567 - 5680.000 ALP=1.+ALP*ALP
568 - 5690.000 G=SORT(SRMX/SRMN)
569 - 5700.000 SQ=SORT((G-1.)*ALS+1.)
570 - 5710.000 DSR=(SRMX-SRMN)/100.

```



```

571 - 5720.000      NPTS = 101
572 - 5730.000      OUTPUT ARR,YY
573 - 5740.000      DO 2 I=1,NPTS
574 - 5750.000      J = NPTS - I + 1
575 - 5760.000      SR = SRMX - DSR * (I-1)
576 - 5770.000      AXX(J) = SR
577 - 5780.000      AR(J) = YLIN(123,SR,ARR,YY)
578 - 5790.000      CONTINUE
579 - 5800.000      OUTPUT AXX,AR
580 - 5810.000      WRITE(103)(DAND(I,1),I=1,101),(DAND(I,2),I=1,101)
581 - 5820.000      GOTO 65
582 - 5830.000      CALL AREA(AT,SRMN)
583 - 5840.000      CALL AREA(AII,SRMN)
584 - 5850.000      OUTPUT AT,AII
585 - 5860.000      OUTPUT RD,ALP,ALS,G,SQ,F(1)
586 - 5870.000      OUTPUT SRMN,SRMX,(SIG(I),I=1,M+1),(SGL(I),I=1,M+1),XL,YL,ZL
587 - 5880.000      B = 2.5
588 - 5890.000      CALL OPTIM(B,NT,M,WS,NI, WS,WV,YY,ARR)
589 - 5900.000      JSIARN*WS
590 - 5910.000      OUTPUT WV,WS
591 - 5920.000      OUTPUT TSIA
592 - 5930.000      IF(WV.EQ.0.) WV=1.E-30
593 - 5940.000      BS =NI*WS/WV
594 - 5950.000      BM =4.*SMP*FLDA/AI
595 - 5960.000      479 FORMAT(6I12)
596 - 5970.000      489 FORMAT (12F8.3)
597 - 5980.000      RETURN
598 - 5990.000      65  END
599 - 6000.000      C
600 - 6010.000      C
601 - 6020.000      SUBROUTINE COEF2(C,I,J,K,DJ,M)
602 - 6030.000      C
603 - 6040.000      C THIS SUBROUTINE CALCULATES THE DIFFERENCE BETWEEN TWO
604 - 6050.000      C AREA VALUES IN AN INTEGRATION STEP.
605 - 6060.000      C
606 - 6070.000      C INPUTS :
607 - 6080.000      C
608 - 6090.000      C I IS THE INDEX IN ARRAY SGL.
609 - 6100.000      C
610 - 6110.000      C J IS THE INDEX IN ARRAY SIG.
611 - 6120.000      C
612 - 6130.000      C K IS THE INTEGRATION STA/EP.
613 - 6140.000      C
614 - 6150.000      C DJ IS THE VALUE OF SIGMA FOR A SINGLE INTEGRATION STEP.
615 - 6160.000      C
616 - 6170.000      C M IS THE NUMBER OF SIGMAS = SIG.
617 - 6180.000      C
618 - 6190.000      C OUTPUTS :
619 - 6200.000      C
620 - 6210.000      C C IS THE AREA DIFFERENCE.
621 - 6220.000      C
622 - 6230.000      COMMON/COE2/SIG(22),SGL(22),MI

```

COMMON/ARE1/AR(101),DSR,SRMX,AXX(101)

A2=0.  
SI=SIG(J)+(K-1)\*DJ  
SR=SGL(I)/SI  
AI = YLIN(101,SR,AXX,AR)  
IF(I.GT.M+1) GO TO 1  
IF(I.EQ.J) GO TO 1  
SR=SGL(I+1)/SI  
A2 = YLIN(101,SR,AXX,AR)  
1 C #A1=A2  
RETURN  
END

SUBROUTINE LPICK(SIG,MS, BP,DB,ALP,DALP)

THIS IS THE LOG NORMAL PICK SUBROUTINE, IT'S PURPOSE  
IS TO GENERATE A GOOD STARTING POINT FOR THE LOG-NORMAL  
SOLUTION.

INPUTS :

SIG IS THE CROSS SECTION ARRAY.

MS IS THE NUMBER OF SIGMAS IN THE ARRAY.

OUTPUTS :

ALP IS THE FITTING PARAMETER FOR THE LOG-NORMAL SOLUTION.

DALP IS THE FITTING PARAMETER INCREMENT FOR THE L-N SOL'N.

DIMENSION SIG(22)

DB=(SIG(MS+1)-SIG(1))/20.

BP=(SIG(1)+SIG(MS+1))/2.

AI=SQRT((LOG(SIG(MS+1))/2.)/SIG(1)+LOG(SIG(1))/SIG(1)))\*2/2.7/SIG(1)

1 /LOG(SIG(MS+1))-LOG(SIG(1))/SIG(1)

DALP=AI/20.

ALP=AI/2.

RETURN

END

SUBROUTINE EPICK(SIG,BPI,BP,MS,DP)

THIS IS THE EXPONENTIAL PICK SUBROUTINE, IT'S PURPOSE  
IS TO GENERATE A GOOD STARTING POINT FOR THE EXPONENTIAL  
SOLUTION.

INPUTS :

SIG IS THE CROSS SECTION ARRAY.

623 = 6240.000  
624 = 6250.000  
625 = 6260.000  
626 = 6270.000  
627 = 6280.000  
628 = 6290.000  
629 = 6300.000  
630 = 6310.000  
631 = 6320.000  
632 = 6330.000  
633 = 6340.000  
634 = 6350.000  
635 = 6360.000 C  
636 = 6370.000 C  
637 = 6380.000 C  
638 = 6390.000 C  
639 = 6400.000 C  
640 = 6410.000 C  
641 = 6420.000 C  
642 = 6430.000 C  
643 = 6440.000 C  
644 = 6450.000 C  
645 = 6460.000 C  
646 = 6470.000 C  
647 = 6480.000 C  
648 = 6490.000 C  
649 = 6500.000 C  
650 = 6510.000 C  
651 = 6520.000 C  
652 = 6530.000 C  
653 = 6540.000 C  
654 = 6550.000 C  
655 = 6560.000 C  
656 = 6570.000 C  
657 = 6580.000 C  
658 = 6590.000 C  
659 = 6600.000 C  
660 = 6610.000 C  
661 = 6620.000 C  
662 = 6630.000 C  
663 = 6640.000 C  
664 = 6650.000 C  
665 = 6660.000 C  
666 = 6670.000 C  
667 = 6680.000 C  
668 = 6690.000 C  
669 = 6700.000 C  
670 = 6710.000 C  
671 = 6720.000 C  
672 = 6730.000 C  
673 = 6740.000 C  
674 = 6750.000 C

675 = 6760.000 C  
 676 = 6770.000 C  
 677 = 6780.000 C  
 678 = 6790.000 C  
 679 = 6800.000 C  
 680 = 6810.000 C  
 681 = 6820.000 C  
 682 = 6830.000 C  
 683 = 6840.000 C  
 684 = 6850.000 C  
 685 = 6860.000 C  
 686 = 6870.000 C  
 687 = 6880.000 C  
 688 = 6890.000 C  
 689 = 6900.000 C  
 690 = 6910.000 C  
 691 = 6920.000 C  
 692 = 6930.000 C  
 693 = 6940.000 C  
 694 = 6950.000 C  
 695 = 6960.000 C  
 696 = 6970.000 C  
 697 = 6980.000 C  
 698 = 6990.000 C  
 699 = 7000.000 C  
 700 = 7010.000 C  
 701 = 7020.000 C  
 702 = 7030.000 C  
 703 = 7040.000 C  
 704 = 7050.000 C  
 705 = 7060.000 C  
 706 = 7070.000 C  
 707 = 7080.000 C  
 708 = 7090.000 C  
 709 = 7100.000 C  
 710 = 7110.000 C  
 711 = 7120.000 C  
 712 = 7130.000 C  
 713 = 7140.000 C  
 714 = 7150.000 C  
 715 = 7160.000 C  
 716 = 7170.000 C  
 717 = 7180.000 C  
 718 = 7190.000 C  
 719 = 7200.000 C  
 720 = 7210.000 C  
 721 = 7220.000 C  
 722 = 7230.000 C  
 723 = 7240.000 C  
 724 = 7250.000 C  
 725 = 7260.000 C  
 726 = 7270.000 C

MS IS THE NUMBER OF SIGMAS IN THE ARRAY.

BPI IS THE POWER LAW SOLUTION PARAMETER.

OUTPUT :

BP IS THE EXPONENTIAL POWER PICK.

DP IS THE EXPONENTIAL POWER INCREMENT.

DIMENSION SIG(22)

S1=BP1\*LOG(SIG(1))/SIG(1)

S2=BP1\*LOG(SIG(MS+1))/SIG(MS+1)

BP=92

DP= (S1-S2)/25.

RETURN

END

SUBROUTINE PROW(BP,IP,SIP,M)

THIS SUBROUTINE COMPUTES NORMALIZED PROBABILITIES FOR THE POWER LAW, EXPONENTIAL, AND LOG-NORMAL DISTRIBUTIONS FOR THE INPUT VALUES OF BP AND SIP USING THE SIG ARRAY.

INPUTS :

BP IS THE FITTING PARAMETER.

IP DETERMINES WHICH SOLUTION TO USE.

IP = 1 => POWER LAW

IP = 2 => EXPONENTIAL

IP = 3 => LOG-NORMAL

SIP IS THE CROSS SECTION VALUE.

S0 AND A3 ARE NORMALIZATION FACTORS REQUIRED ONLY FOR THE LOG-NORMAL SOLUTION.

OUTPUTS :

M IS THE NORMALIZED PROBABILITY.

COMMON/COE2/SIG(22),SGL(22),M

COMMON/ALR/S0,A3

OUTPUT IP,BP,SIP

IF(SIP.LE.0.) OUTPUT SIP

IF(SIP.LE.0) M=0

IF(SIP.LE.0) RETURN

GOTO (1,2,3)IP

1 X=1.-HP

```

727 - 7280.000      A1=(SIG(I1)**X-SIG(M+1)**X)/X
728 - 7290.000      IF(BP.GT.999.AND.BP.LT.1.001)A1=LOG(SIG(M+1)/SIG(I1))
729 - 7300.000      W=(SIP**(-BP))/A1
730 - 7310.000      RETURN
731 - 7320.000      2  A2=(EXP(-BP*SIG(I1))-EXP(-BP*SIG(M+1)))/BP
732 - 7330.000      W=EXP(-BP*SIP)/A2
733 - 7340.000      RETURN
734 - 7350.000      3  W=(EXP(-(LOG(SIP)-LOG(BP))**2/2./S0**2))/A3
735 - 7360.000      RETURN
736 - 7370.000      END
737 - 7380.000      C
738 - 7390.000      C
739 - 7400.000      C
740 - 7410.000      C
741 - 7420.000      C
742 - 7430.000      C
743 - 7440.000      C
744 - 7450.000      C
745 - 7460.000      C
746 - 7470.000      C
747 - 7480.000      C
748 - 7490.000      C
749 - 7500.000      C
750 - 7510.000      C
751 - 7520.000      C
752 - 7530.000      C
753 - 7540.000      C
754 - 7550.000      C
755 - 7560.000      C
756 - 7570.000      C
757 - 7580.000      C
758 - 7590.000      C
759 - 7600.000      10 CONTINUE
760 - 7610.000      I1=0
761 - 7620.000      RME1.E+60
762 - 7630.000      IF(NC.GT.1)IC=1
763 - 7640.000      IF(IC.EQ.1)NC=0
764 - 7650.000      IP=2
765 - 7660.000      IF(IC.EQ.0)IP=1
766 - 7670.000      IF(IT.GE.2)IP=3
767 - 7680.000      IC=0
768 - 7690.000      C
769 - 7700.000      C
770 - 7710.000      C
771 - 7720.000      C
772 - 7730.000      C
773 - 7740.000      C
774 - 7750.000      C
775 - 7760.000      C
776 - 7770.000      C
777 - 7780.000      C
778 - 7790.000      C

```

SUBROUTINE OPTIM(B,N,M,MS,NI ,WSS,WVS,YY,ARR)

THIS SUBROUTINE OPTIMIZES THE BETA INVERSION AND SELECTS THE CORRECT DISTRIBUTION OF CROSS SECTIONS TO PROVIDE THE BEST FIT.

DIMENSION PN(22)

DIMENSION ARR(125),YY(125)

COMMON/OPT/DS(22),NP(22),FSI,FN

COMMON/COE2/SIG(22),SGL(22),WJ

COMMON/ALN/S0,A1

COMMON/ARE1/AR(101),DSR,SRMX,AXX(101)

OUTPUT IP,R

NC=0

IP=1

IC=0

BP=8

IT=0

BP=8

DB=1

CONTINUE

I1=0

RME1.E+60

IF(NC.GT.1)IC=1

IF(IC.EQ.1)NC=0

IP=2

IF(IC.EQ.0)IP=1

IF(IT.GE.2)IP=3

IC=0

THIS CHECK NOW DEFEATS THE EXP AND LOG-NORMAL SOLNS TO USE THE EXP. AND LOG-NORM. SOLUTIONS AGAIN JUST REMOVE THE STMT. BELOW ( IF (IP.EQ.2) RETURN ).

IF(IP.EQ.2) RETURN

IF(IP.FO.2) CALL EPICK(SIG,BP1,BP,MS,DB)

IF(IT.EQ.2) CALL LPICK(SIG,MS , AM,DB,S0,DALP)

A CONTINUE

```

779 = 7800.000      II=II+1
780 = 7810.000      IF(IT.GT.100) RETURN
781 = 7820.000      IF(BP.LT.0. AND.IP.EQ.1) RETURN
782 = 7830.000      IF(IP.LE.2)GOTO 102
783 = 7840.000      AM=AM+DB
784 = 7850.000      IF(AM.LT.1.) DB=0.
785 = 7860.000      IF(AM.LT.1.) AM=ABS(AM/10)
786 = 7870.000      IF(IT.EQ.3)S0=90+DALP
787 = 7880.000      IF(IT.EQ.3)AM=BP1
788 = 7890.000      C
789 = 7900.000      C
790 = 7910.000      C
791 = 7920.000      A1=0.
792 = 7930.000      DO 101 J=1,MS
793 = 7940.000      DJ=DS(J)/NI
794 = 7950.000      DO 100 K=1,NI+1
795 = 7960.000      SIP=SIG(J)+(K-1)*DJ
796 = 7970.000      W=EXP(-(LOG(SIP)-LOG(AM))**2/2./S0**2)
797 = 7980.000      A1=A1+W*DJ
798 = 7990.000      S11=SIG(J)
799 = 8000.000      S12=SIG(J+1)
800 = 8010.000      W1=EXP(-(LOG(S11)-LOG(AM))**2/2./S0**2)
801 = 8020.000      W2=EXP(-(LOG(S12)-LOG(AM))**2/2./S0**2)
802 = 8030.000      A1=A1-.5*(W1+W2)*DJ
803 = 8040.000      BP=AM-DB
804 = 8050.000      C
805 = 8060.000      102 CONTINUE
806 = 8070.000      C
807 = 8080.000      C
808 = 8090.000      C
809 = 8100.000      6 DO 5 I=1,MS
810 = 8110.000      5 PN(I)=0.
811 = 8120.000      BP=BP+DB
812 = 8130.000      IF(IT.EQ.3)RP=BP1
813 = 8140.000      OUTPUT RP
814 = 8150.000      W9=0.
815 = 8160.000      W9=0.
816 = 8170.000      C
817 = 8180.000      C
818 = 8190.000      C
819 = 8200.000      C
820 = 8210.000      DO500 J=1,MS
821 = 8220.000      DJ=DS(J)/NI
822 = 8230.000      DO 501 K=1,NI +1
823 = 8240.000      SIP=SIG(J)+(K-1)*DJ
824 = 8250.000      SR=SGL(1)/SIP
825 = 8260.000      ASK=YLIN(101,SR,AXX,AR)
826 = 8270.000      CALL PPOW(RP,IP,SIP,MS)
827 = 8280.000      W9=MS+NI-SIP*DJ
828 = 8290.000      W9=W9+W1+ASK*DJ
829 = 8300.000      S11=SIG(J)
830 = 8310.000      S12=SIG(J+1)

```

THESE LOOPS PRODUCE THE AVERAGE CROSS SECTION AND FOCAL VOLUME ( WS AND WV ).

RESET PARTICLE PROBABILITIES TO ZERO.

```

831 - 8320.000 SR=SGL(I)/SIG(J)
832 - 8330.000 AS1=YLIN(101,SR,AXX,AR)
833 - 8340.000 SR=SGL(I)/S12
834 - 8350.000 AS2=YLIN(101,SR,AXX,AR)
835 - 8360.000 CALL PROM(BP,IP,S11,MS)
836 - 8370.000 W1=WI
837 - 8380.000 CALL PROM(BP,IP,S12,MS)
838 - 8390.000 W2=WI
839 - 8400.000 C
840 - 8410.000 C
841 - 8420.000 C
842 - 8430.000 W3=W3-.5*(W1+S11+W2+S12)*DJ
843 - 8440.000 500 W4=W4+.5*(W1+AS1+W2+AS2)*DJ
844 - 8450.000 W5=W5+1.E-12
845 - 8460.000 W59=WS1
846 - 8470.000 WVS=WV1
847 - 8480.000 WS1=MS
848 - 8490.000 WV1=WV
849 - 8500.000 C
850 - 8510.000 C N IS THE NUMBER OF SINGLE PARTICLE COUNTS THAT THIS
851 - 8520.000 C INVERSION IS DOING.
852 - 8530.000 C
853 - 8540.000 C PREDICTED DENSITY = NO. PARTICLES / AVG. FOCAL VOL.
854 - 8550.000 C
855 - 8560.000 C THESE LOOPS PRODUCE THE CROSS SECTION DISTRIBUTION
856 - 8570.000 C PROBABILITY ARRAY ( PN ).
857 - 8580.000 C
858 - 8590.000 FN=Z
859 - 8600.000 DNT=FN/WV
860 - 8610.000 BTE=NT*WS
861 - 8620.000 DO 1 I=1,M+1
862 - 8630.000 DO 1 J=1,MS
863 - 8640.000 DJ=DS(J)/NI
864 - 8650.000 DO 4 K=1,NI+1
865 - 8660.000 SIP=SIG(J)+(K-1)*DJ
866 - 8670.000 CALL PROM(BP,IP,SIP,MS)
867 - 8680.000 CALL COEF2(C,I,J,K,DJ,M)
868 - 8690.000 4 PN(I)=PN(I)+C*KI*DJ
869 - 8700.000 SIP=SIG(J)
870 - 8710.000 CALL PROM(BP,IP,SIP,MS)
871 - 8720.000 W1=WI
872 - 8730.000 SIP=SIG(J)+NI*DJ
873 - 8740.000 CALL PROM(BP,IP,SIP,MS)
874 - 8750.000 W2=WI
875 - 8760.000 CALL COEF2(C1,I,J,1,DJ,M)
876 - 8770.000 CALL COEF2(C2,I,J,NI+1,DJ,M)
877 - 8780.000 1 PN(I)=PN(I)+.5*(C1*W1+C2*W2)*DJ
878 - 8790.000 P=0
879 - 8800.000 DO 2 I=1,MS
880 - 8810.000 C
881 - 8820.000 C FN IS THE ACTUAL DATA
882 - 8830.000 C

```

```

883 - 8840.000 C      EP IS THE PREDICIED VALUES
884 - 8850.000 C
885 - 8860.000 C
886 - 8870.000 C      R IS THE DIFFERENCE BETWEEN THE PREDICTED AND
887 - 8880.000 C      ACTUAL DATA SQUARED.
888 - 8890.000 C
889 - 8900.000 C      FN=NP(I)
890 - 8910.000 C      FP=PN(I)*DNT
891 - 8920.000 C      OUTPUT R, FN, FP, I
892 - 8930.000 C      IF(I.LE.M) R=(FN-FP)**2+R
893 - 8940.000 C      CONTINUE
894 - 8950.000 C      NC=NC+1
895 - 8960.000 C      OUTPUT NC,DNT
896 - 8970.000 C      IF(NC.NE.2)GOTO 11
897 - 8980.000 C      IF(R.LT.RM)GOTO 11
898 - 8990.000 C      OUTPUT R,RM
899 - 9000.000 C      SAVE OLD VALUE
900 - 9010.000 C
901 - 9020.000 C      RM=R
902 - 9030.000 C      DR=DB
903 - 9040.000 C      IF(IT.EQ.3) DALP=DALP
904 - 9050.000 C
905 - 9060.000 C      JUST IN CASE SOLUTION IS WORSE ON 2ND PASS.
906 - 9070.000 C
907 - 9080.000 C      GOTO 8
908 - 9090.000 C      11. CONTINUE
909 - 9100.000 C
910 - 9110.000 C
911 - 9120.000 C      IF NEW SOLUTION BETER THAN PREVIOUS ONE
912 - 9130.000 C      THEN CONTINUE TO ITERATE.
913 - 9140.000 C
914 - 9150.000 C      IF(R.LT.RM) RM=R;GO TO 8
915 - 9160.000 C      19 FORMAT(5F10.0)
916 - 9170.000 C      29 FORMAT(F10.3,4E12.3)
917 - 9180.000 C      39 FORMAT(5F12.4)
918 - 9190.000 C      49 FORMAT(5F10.0)
919 - 9200.000 C      IT=IT+1
920 - 9210.000 C
921 - 9220.000 C      WSS IS THE AVERAGE SIGMA BAR.
922 - 9230.000 C
923 - 9240.000 C      WVS IS THE AVERAGE FOCAL VOLUME.
924 - 9250.000 C
925 - 9260.000 C      J. POWER LAW SOL'NS.
926 - 9270.000 C
927 - 9280.000 C      IF(IT.EQ.1)RPRM;WSPENSS;WVPEWVS
928 - 9290.000 C
929 - 9300.000 C      2. EXPONENTIAL SOL'NS.
930 - 9310.000 C
931 - 9320.000 C      IF(IT.EQ.2)REERM;MSE=WSS;MVE=WVS
932 - 9330.000 C
933 - 9340.000 C      3. LOG-NORMAL SOL'NS.
934 - 9350.000 C

```

```

935 = 9360.000
936 = 9370.000 C
937 = 9380.000
938 = 9390.000
939 = 9400.000
940 = 9410.000
941 = 9420.000
942 = 9430.000
943 = 9440.000
944 = 9450.000
945 = 9460.000 C
946 = 9470.000 C
947 = 9480.000 C
948 = 9490.000 C
949 = 9500.000 C
950 = 9510.000 C
951 = 9520.000
952 = 9530.000
953 = 9540.000 C
954 = 9550.000 C
955 = 9560.000 C
956 = 9570.000 C
957 = 9580.000 C
958 = 9590.000 C
959 = 9600.000
960 = 9610.000
961 = 9620.000 C
962 = 9630.000 C
963 = 9640.000 C
964 = 9650.000 C
965 = 9660.000
966 = 9670.000 C
967 = 9680.000
968 = 9690.000 C
969 = 9700.000 C
970 = 9710.000 C
971 = 9720.000 C
972 = 9730.000 C
973 = 9740.000 C
974 = 9750.000 C
975 = 9760.000 C
976 = 9770.000 C
977 = 9780.000 C
978 = 9790.000 C
979 = 9800.000
980 = 9810.000
981 = 9820.000
982 = 9830.000
983 = 9840.000 10
984 = 9850.000
985 = 9860.000 11
986 = 9870.000

```

```

IF (I1.GT.2) RLNRM,MSLN,WSS,WVLN,WVS
  RP1=BP-DB;OUTPUT BP1
  IF (BP.LT.0.) BP=0.
  7 BP=BP-DB
  IF (I1.LT.4) GOTO 10
  OUTPUT RP,RE,RLN
  WSS=WSP
  WVS=WVP
  IF THE POWER LAW SOL'N IS BEST
  THEN RETURN FROM HERE.
  IF (RP.LT.RE.AND.RP.LT.RLN)RETURN
  WSS=WSE
  WVS=WVE
  IF EXPONENTIAL SOL'N IS REST
  THEN RETURN FROM HERE.
  IF (RE.LT.RLN)RETURN
  WSS=MSLN
  WVS=WVLN
  IF LOG-NORMAL SOL'N IS BEST
  THEN RETURN FROM HERE.
  RETURN
END
FUNCTION YLIN(N,XX,X,Y)
THIS FUNCTION SUBPROGRAM PERFORMS A LINEAR INTERPOLATION.
N = NUMBER OF DATA POINTS
XX = X VALUE FOR WHICH Y VALUE MUST BE INTERPOLATED
X = DEPENDENT VARIABLE ARRAY
Y = INDEPENDENT VARIABLE ARRAY FOR WHICH
  INTERPOLATIONS ARE PERFORMED
DIMENSION X(I),Y(I)
  J=1
  DO 10 I=J,N
  IF (XX.LT. X(I)) GO TO 11
  CONTINUE
  I=N
  IF (I.EQ. 1) I=2
  J=I-1

```



```
987 = 9880.000  
988 = 9890.000  
989 = 9900.000  
990 = 9910.000  
991 = 9920.000  
P=(XX-X(JJ))/(X(I)-X(J))  
IF (P .LT. 0. .OR. P .GT. 1.) P = 0.0  
YLN=Y(J) +P*(Y(I)-Y(J))  
RETURN  
END
```