Thermal-Stress Analysis For A Wood Composite Blade

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THERMAL-STRESS ANALYSIS FOR A WOOD COMPOSITE BLADE

Introduction

Since 1977, NASA Lewis Research Center has been pursuing the development of low cost rotor blade technology for large horizontal axis wind turbine. Laminated wood manufactured by bonding together 1/10" to 1/8" thick sheets, or plys, with epoxy is a particularly attractive candidate material for a rotor blade since the raw material has high specific strength, high specific stiffness and low cost. This led to the manufacturing of eight laminated wood blades in 1980. They were installed as Mod-OA wind turbine at three different locations; Kahuku Point, Hawaii, Culebra, Puerto Rico, and Block Island, Rhode Island. Mod-OA turbines have 125' diameter rotors and generate 200 Kilo-Watts each when in operation. Their performances were closely monitored. In 1981, a crack was found in Blade No. 1012 located in Block Island, which occurred in the leading edge extending along the entire blade. The cause of the crack was unknown, but thermal-stress induced by the sun was suspected to be one of the main reasons. Therefore, the investigation has been pursuaded along this line.

The analysis of thermal-stress of the blade induced by solar insolation consists of two phases. The first phase is to find the temperature distribution throughout the blade, a heat conduction problem. The second phase is to determine the thermal-stress distribution of the blade caused by the temperature distribution found in the first phase, a thermal-stress analysis problem. Since wood is an orthotropic material in the senses of heat conduction and stress-strain relationships, these characteristics must be included in the analyses of both phases.

Phase I: Heat Conduction Analysis

A. The Blade and the Assumed Environment

Blade No. 1012 is 700 inches long with maximum chord width of 62.4 inches, see Fig. 1 for its overall dimensions. Airfoil standard section NACA 230 [1], is used. The thickness to chord ratio of the blade is varied from 31.75 at station 150 to 7.5 at station 732.

In the determination of temperature distribution throughout the blade, it is reasonable to assume that a two-dimensional heat conduction analysis of a typical blade section is adequate, because the blade is basically a slender body. In addition, the thermal conductivity of wood in longitudinal direction of the blade, which is parallel to the grain, is two to three times higher than those in transversal directions. As a result, the temperature gradient in longitudinal direction is far smaller than those in transversal directions. This again indicates that a two-dimensional analysis is adequate.

The section at station 126 is arbitrarily selected as a typical section for analysis. The thickness to chord ratio at this station is 30.4, which is close to those of the sections in the neighborhood of station 300, the main body of the blade, see Fig. 2. In the nose portion, called D-spar, 3" thick laminated rotary veneers of Douglas Fir is used. In the tail portion, 3/4" thick honeycomb paper core is installed to provide stiffness and light-weight. Pieces of sawn Douglas Fir are used for stringers. On the surface, the blade is covered with a layer of 1/8" thick Birch Plywood.

Two parked positions of the blade are considered; one keeps the section in horizontal position, the other, vertical. Technically speaking, the difference between these two positions is that the heat flux input zones are different as shown in Fig. 3 and 4. The heat flux input zone is defined as the portion of boundary surface of the blade exposed to the sun. The solar insolation is estimated at 363 BTU/$_{\text{ft}^2\text{-hr}}$ [2]. The absorbtivity of the blade surface is estimated at 0.9, which is not only on the safe side for the purpose of stress analysis but also has a good reason: after a long period of exposure, the blade surface is usually dirty and full of bug remains, which often drastically increase the surface absorbtivity. Thus, the heat flux input, q_r, for the heat flux input zone is

$$q_r = 363 \times 0.9 = 326 \text{ BTU}/_{\text{ft}^2\text{-hr}} .$$

The ambient temperature, T_∞, is assumed to be 90°F, typical temperature for a hot summer morning in Block Island. Further, the air is assumed to be still, and the convective heat transfer coefficient, h, for the blade surface is assumed to be 5 BTU/$_{\text{ft}^2\text{-hr.}°\text{F}}$.

In description of wood properties, three mutually perpendicular axes, longitudinal, radial and tangential, need to be used. The longitudinal axis, L, is parallel to the grain; the radial axis, R, is normal to the growth rings; and the tangential axis, T, is perpendicular to the grain but tangent to the growth rings. The thermal conductivities of the wood in L, T and R directions [9] are listed in Table 1, note that a small difference of 10% is assumed between k_T and k_R to account for possible physical differential between these two directions. Since rotary veneer is used in blade construction, the axes L, T, and R correspond to principal material axes ξ, ζ and η respectively. The material axes will be used in next section.

The thermal conductivity of honeycomb paper core may be estimated by using the average value for paper and air, which is 0.013 BTU/$_{\text{hr.ft.}°\text{F}}$.

Table 1. Thermal Conductivity of Wood

Wood	k_L	k_T	k_R
Douglas Fir	0.172 BTU/hr.ft.°F	0.068 BTU/hr.ft.°F	0.075 BTU/hr.ft.°F
Birch	0.211	0.084	0.093

B. Governing Partial Differential Equation

Because of the configurational complexity of the blade section and the orthotropic property of heat conduction of the wood composite, finite element method with variational approach is chosen as the method of solution. This method may also be called as a numerical method in solving partial differential equations. For an element of an orthotropic material, the controlling partial differential equations may be derived in the following outlines.

Heat flux input - Heat flux output = Heat retention in body (1)

Referring to Figure 5, let 'f' be the heat flux and 'k', the thermal conductivity, their directions along axes y, z, ζ and η are indicated by subscripts. 'T' represents the temperature, 'C_p', specific heat and 'ρ', the density of wood. Thus, Equation (1) may be expressed as

$$f_y\big|_y dxdz + f_z\big|_z dxdy - [f_y\big|_{y+\Delta y} dxdz] - [f_z\big|_{z+\Delta z} dxdy]$$

$$= \rho\ dxdydz\ C_p \frac{\partial T}{\partial t} \qquad (2)$$

Applying Taylor's Series and simplifying, Equation (2) becomes,

$$\frac{\partial}{\partial y}(-f_y) + \frac{\partial}{\partial z}(-f_z) = \rho\, C_p \frac{\partial T}{\partial t} \tag{3}$$

Since the principal axes of the material, ζ, and η, are in general at an angle, β, with global axes y and z as shown in Fig. 5, the following transformation may be used,

$$\begin{bmatrix} f_y \\ f_z \end{bmatrix} = \begin{bmatrix} \cos\beta & -\sin\beta \\ \sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} f_\zeta \\ f_\eta \end{bmatrix} = \begin{bmatrix} \cos\beta & -\sin\beta \\ \sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} -k_\zeta \dfrac{\partial T}{\partial \zeta} \\ -k_\eta \dfrac{\partial T}{\partial \eta} \end{bmatrix}$$

Using chain rule;

$$\begin{bmatrix} \dfrac{\partial T}{\partial \zeta} \\ \dfrac{\partial T}{\partial \eta} \end{bmatrix} = \begin{bmatrix} \dfrac{\partial y}{\partial \zeta} & \dfrac{\partial z}{\partial \zeta} \\ \dfrac{\partial y}{\partial \eta} & \dfrac{\partial z}{\partial \eta} \end{bmatrix} \begin{bmatrix} \dfrac{\partial T}{\partial y} \\ \dfrac{\partial T}{\partial z} \end{bmatrix} = \begin{bmatrix} \cos\beta & \sin\beta \\ -\sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} \dfrac{\partial T}{\partial y} \\ \dfrac{\partial T}{\partial z} \end{bmatrix}$$

we have,

$$\begin{bmatrix} f_y \\ f_z \end{bmatrix} = \begin{bmatrix} \cos\beta & -\sin\beta \\ \sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} -k_\zeta & 0 \\ 0 & -k_\eta \end{bmatrix} \begin{bmatrix} \cos\beta & \sin\beta \\ -\sin\beta & \cos\beta \end{bmatrix} \begin{bmatrix} \dfrac{\partial T}{\partial y} \\ \dfrac{\partial T}{\partial z} \end{bmatrix} \tag{4}$$

Substitute (4) into (3), we obtain:

$$(k_\zeta \cos^2\beta + k_\eta \sin^2\beta) \frac{\partial^2 T}{\partial y^2} + (k_\zeta - k_\eta) \operatorname{Sin} 2\beta \frac{\partial^2 T}{\partial y \, \partial z}$$

$$+ \ (k_\zeta \sin^2\beta + k_\eta \cos^2\beta) \frac{\partial^2 T}{\partial z^2} = \rho \, C_p \frac{\partial T}{\partial t} \tag{5}$$

Equation (5) is the governing partial differential Equation for the heat conduction analysis of the blade.

The boundary conditions around the surface of the blade are:

(a) prescribed heat flux, q_r, in the heat flux input zone, namely,

$$q_r = 326 \text{ BTU}/_{ft^2} \text{ hr} \,. \tag{5a}$$

(b) convective heat transfer loss, q_c, for the entire boundary surface of the blade,

$$q_c = h(T_s - T_\infty) \tag{5b}$$

where T_s is the surface temperature of the blade, a variable.

C. Calculus of Variation

For a given problem with a governing differential equation and boundary conditions, the task of the variational formulation is to find the unknown function 'F' for the differential equation, which extremizes or makes stationary a functional 'I' subject to the same boundary conditions of the problem.

where,

$$I = \int_{0}^{L} F(x, \tilde{T}(x), \tilde{T}'(x))\, dx \qquad (6)$$

$\tilde{T}(x)$, is a weak variation of T(x), namely

$$\tilde{T}((x) = T(x) + \varepsilon\eta(x) \qquad (7)$$

ε is an error term of a small magnitude , $\eta(x)$ is an error function which vanishes at its boundaries.

From the calculus of variation [3], when 'I' is extremized respect to 'T' and the error term ε is made to approach zero, the Euler-Lagrange Equation is formed, namely

$$\frac{\partial F}{\partial T} - \frac{d}{dx}\frac{\partial F}{\partial T'} = 0 \qquad (8)$$

In other words, the functional 'I' is extremized or made stationary when the Euler-Langrange equation and its boundary conditions are satisfied. Therefore, the task of seeking solution, T(x), for the governing partial differential Equation (5) becomes a numerically simpler problem, that is, finding first the 'F' in such a way that its Euler-Lagrange equation is identical to the governing differential equation. Next, the Functional 'I' is formed. Then the finite element method is used to find an approximate temperature profile which extremizes the functional and satisfies the boundary conditions. The temperature profile so obtained is the solution to the heat conduction problem in question.

For the governing differential equation, (5), the function 'F' may be formed as follows:

$$F = \frac{1}{2} [(k_\zeta \cos^2\beta + k_\eta \sin^2\beta) (\frac{\partial T}{\partial y})^2 + (k_\zeta \sin^2\beta + k_\eta \cos^2\beta) (\frac{\partial T}{\partial z})^2$$

$$+ (k_\zeta - k_\eta) \sin2\beta (\frac{\partial T}{\partial y}) (\frac{\partial T}{\partial z}) + 2\rho C_p \frac{\partial T}{\partial t} T] \qquad (9)$$

Thus, the functional which contains the Function 'F' as described in Equation (9) and the corresponding function for boundary conditions (5a) and (5b), is

$$I = \int_V FdV + \int_S [q_r T + \frac{1}{2} h (T - T_\infty)^2] ds \qquad (10)$$

D. Finite Element Method - Variational Approach

The cross section of the blade at station 126 is selected as the typical section for temperature profile determination. Triangular elements are used. The blade consists of 3 different kind of materials, Douglas Fir, Birch plywood and honeycomb paper core. It was divided into 75 regions, see Fig. 6. Each region was further divided into proper numbers of columns and rows. See Table 2. Then the triangular finite element mesh is generated automatically [4]. The results of regions 12 and 54 are shown in Fig. 7 as a typical example.

Table 2.

Region	Row	Column	Region	Row	Column	Region	Row	Column
1	2	2	26	2	7	51	3	3
2	2	5	27	2	5	52	3	9
3	2	7	28	2	3	53	3	9
4	2	7	29	2	3	54	3	9
5	2	5	30	2	3	55	3	9
6	2	3	31	2	3	56	3	3
7	2	3	32	2	5	57	3	3
8	2	3	33	2	7	58	3	2
9	2	3	34	2	7	59	3	2
10	2	9	35	2	5	60	3	3
11	2	9	36	2	2	61	3	3
12	2	9	37	2	2	62	3	3
13	2	9	38	3	2	63	3	3
14	2	3	39	3	5	64	3	3
15	2	3	40	3	7	65	3	5
16	2	3	41	3	7	66	3	7
17	2	3	42	3	5	67	3	7
18	2	5	43	3	3	68	3	5
19	2	7	44	3	3	69	3	2
20	2	7	45	3	3	70	2	2
21	2	5	46	3	3	71	5	3
22	2	2	47	3	3	72	3	3
23	2	2	48	3	2	73	3	2
24	2	5	49	3	2	74	5	3
25	2	7	50	3	3	75	2	10

To describe the finite element method, a typical element as shown in Fig. 8 is chosen. An approximate temperature profile, T(y,z), can be constructed by using shape functions N_i, N_j and N_k to linearly interpolate among the nodal temperatures T_i, T_j and T_k, the values of which are to be determined. T(y,z) is described as:

$$T(y,z) = N_i T_i + N_j T_j + N_k T_k \tag{11}$$

where

$$Ni = \frac{1}{2A} [a_i + b_i y + c_i z]$$

$$N_j = \frac{1}{2A} [a_j + b_j y + c_j z] \tag{11a}$$

$$N_k = \frac{1}{2A} [a_k + b_k y + c_k z]$$

$$A = \frac{1}{2} \begin{vmatrix} 1 & Y_i & Z_i \\ 1 & Y_j & Z_j \\ 1 & Y_k & Z_k \end{vmatrix} \tag{11b}$$

and

$$\begin{aligned} a_i &= Y_j Z_k - Y_k Z_j, & a_j &= Y_k Z_i - Z_k Y_i, & a_k &= Y_i Z_j - Y_j Z_i \\ b_i &= Z_j - Z_k, & b_j &= Z_k - Z_i, & b_k &= Z_i - Z_j \\ c_i &= Y_k - Y_j, & c_j &= Y_i - Y_k, & c_k &= Y_j - Y_i \end{aligned} \tag{11c}$$

Substitute T(y,z) into Equation (10), and partial differentiate 'I' with respect to unknown nodal temperatures. Then, set them equal to zero. The result is a set of equations:

$$[C]\,\frac{\partial\{T\}}{\partial t} + [K]\,[T] = [P] \tag{12}$$

where

$$[C] = \sum_{e=1}^{n} [C_e], \qquad [K] = \sum_{e=1}^{n} [\,K_e], \qquad [P] = \sum_{e=1}^{n} [P_e]$$

and

$$[C_e] = \frac{\rho C_p A}{12} \begin{bmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 2 \end{bmatrix},$$

$$[P_e] = (-q_r + h\,T_\infty) * \left[\frac{L_{ij}}{2} \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} \text{ or } \frac{L_{jk}}{2} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \text{ or } \frac{L_{ki}}{2} \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} \right]$$

$$[K_e] = \frac{k_\zeta \cos^2\beta + k_\eta \sin^2\beta}{4A} \begin{bmatrix} b_ib_i & b_ib_j & b_ib_k \\ b_jb_i & b_jb_j & b_jb_k \\ b_kb_i & b_kb_j & b_kb_k \end{bmatrix} + \frac{k_\zeta \sin^2\beta + k_\eta \cos^2\beta}{4A}$$

$$\begin{bmatrix} c_ic_i & c_ic_j & c_ic_k \\ c_jc_i & c_jc_j & c_jc_k \\ c_kc_i & c_kc_j & c_kc_k \end{bmatrix} + \frac{(k_\zeta - k_\eta)\sin 2\beta}{4A} \begin{bmatrix} b_ic_i & b_ic_j & b_ic_k \\ b_jc_i & b_jc_j & b_jc_k \\ b_kc_i & b_kc_j & b_kc_k \end{bmatrix}$$

$$+ \frac{h\,L_{ij}}{6} \begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & 0 \\ 0 & 0 & 0 \end{bmatrix} \text{ or } + \frac{h\,L_{jk}}{6} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix} \text{ or } + \frac{h\,L_{ki}}{6} \begin{bmatrix} 2 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 2 \end{bmatrix}$$

Note that n is the total number of elements of the blade. [C] is the capacitance matrix, [P], the heat flux matrix and [K], the conductance matrix of the entire blade. $[P_e]$ and $[K_e]$ contain 'or' in their expressions. The purpose is to accommodate the elements with one edge or two edges on the boundary of the blade. For example, if edge j-k is on the boundary, the term which contains L_{jk} is maintained and the other two are deleted. For a non-boundary element, L_{ij}, L_{jk} and L_{ki} are assumed a value of zero. Thus, the last term of $[K_e]$ is deleted and $[P_e]$ is dropped off for that element.

Equation (12) describes the heat conduction problem in trancient state. When it reaches the steady state, the rate of change of temperature respect to time vanishes, i.e.,

$$\frac{\partial \{T\}}{\partial t} = 0$$

Equation (12) becomes,

$$[K]\,[T] = [P] \tag{13}$$

Equation (13) describes the heat conduction problem in steady state.

E. Heat Conduction in Steady State

Two steay-state Heat Conduction Analyses are made on the University NAS 6650 computer system. The first analysis is performed when the blade section is placed in horizontal position, the second, in vertical position. The sun is assumed to shine vertically on the top of the blade, which defines the heat flux input zone as shown in Fig. 3 or 4. So only the element with an edge on the top side has heat flux input 'q_r' entering the element thru that edge. The temperatures on all nodal points were obtained. Only the temperatures of the exterior nodes are plotted in Fig. 9 and 10. Temperatures of interior nodes are shown representively on typical sections in Fig. 11.

Observing Fig. 9 and 10, one finds that both of the sunny side surfaces reach a high temperature of 155°F and the opposite sides are on or slightly above 90°F. The identicalness of the results and that the low temperature is so close to the ambient temperature offer strong assurances that the analysis is correct. Further, Fig. 11 shows a smooth transition from high temperature side to low temperature side in all sections. They again indicate that the results are quite reasonable and hence reliable.

F. Heat Conduction in Transient State

It is important to determine the length of sunshine time required for the blade to reach the steady-state temperature. If the length of time required is not more than the sunshine hours of a day in the summer, the steady-state temperature may be used as the critical temperature distribution for anlaysis. Otherwise, temperature distribution at the end of sunshine hours of a day should be used.

In time domain, a linear interpolation model is used, see Fig. 12. The unknown temperature field $\{T\}$, spanning from one time to another separated by a time step Δt, may be expressed as

$$\{T\} = N_i \{T_i\} + N_j \{T_j\} \tag{14}$$

where N_i and N_j are shape functions, namely,

$$N_i = 1 - \frac{t}{\Delta t} \qquad \frac{\partial N_i}{\partial t} = \frac{-1}{\Delta t}$$

hence,

$$N_j = \frac{t}{\Delta t} \qquad \frac{\partial N_j}{\partial t} = \frac{1}{\Delta t}$$

substitute Equation (14) into Equation (12) and apply Galerkin's method [5], two integral matrix equations are produced, they are,

$$\int_0^{\Delta t} N_i \left([C] \frac{d\{T\}}{dt} + [K]\{T\} - \{P\}\right) dt = 0 \tag{15a}$$

$$\int_0^{\Delta t} N_j \left([C] \frac{d\{T\}}{dt} + [K]\{T\} - \{P\}\right) dt = 0 \tag{15b}$$

The time derivative of Equation (14) is,

$$\frac{d\{T\}}{dt} = \frac{dN_i}{dt} \{T_i\} + \frac{dN_j}{dt} \{T_j\} = - \frac{1}{\Delta t} \{T_i\} + \frac{1}{\Delta t} \{T_j\} \tag{16}$$

Substitute Equations (14) and (16) into Equation (15a), we have,

$$\int_0^{\Delta t} (1 - \frac{t}{\Delta t})(\frac{[C]}{\Delta t} \{T_j\} - \frac{[C]}{\Delta t} \{T_i\} + \frac{t[K]}{\Delta t} \{T_j\} + (1 - \frac{t}{\Delta t}) [K] \{T_j\} - \{P_i\}) dt = 0$$

After integration, it yields,

$$\left(\frac{[C]}{2} + \frac{\Delta t}{6} [K]\right) \{T_j\} = \left(\frac{[C]}{2} - \frac{\Delta t}{3} [K]\right) \{T_i\} + \frac{\Delta t}{2} [P_i] \tag{17}$$

The constants in parentheses are weighting factors, which may be modified to improve the stability of the numerical solution process. Based on Donea's suggestion [6], Equation (17) is modified to the following form.

$$\left(\frac{[C]}{2} + \frac{\Delta t}{3} [K]\right) \{T_j\} = \left(\frac{[C]}{2} - \frac{\Delta t}{6} [K]\right) \{T_i\} + \frac{\Delta t}{2} [P_i] \tag{18}$$

Equation (18) is the equation of solution in time domain.

The initial temperature of the blade is assumed to be uniform and same as the ambient temperature, 90°F, namely,

$$\{T_i\} = \{T_0\}_{t=0°} = \{90°\}$$

then, an iterative process is commenced to determine the temperature at the next time step $t + \Delta t$, namely $\{T_j\}$, by using Equation (18). This process is repeated until the maximum difference between $\{T_j\}$ and $\{T_i\}$ is smaller than a predetermined small quantity. In this analysis, 500 second is chosen as Δt and good results are obtained as shown in Figs. 13 and 14.

Observing Figs. 13 and 14 and the computer results, numerical instability is experienced in the first hour, but thereafter, stability is restored and steady-state condition is reached. They indicate that the length of sunshine time required for the blade to reach the steady-state temperature is in the neighborhood of 4 hours. Obviously, this is possible. Thus, steady-state temperature distribution of the blade is used as the input of Phase II, finite element thermal-stress analysis.

PHASE II. THERMAL-STRESS ANALYSIS

A. Plane-Strain Thermoelastic Problem

From the previous discussions, it has been stated that the blade is a slender body, its length is large compared with its maximum cross-sectional dimension. The thermal input along the blade axis is close to uniform, namely, the blade temperature is independent of the axial coordinate. Under these conditions, the use of the concept of plain strain not only provides a good solution [7], but also greatly reduces the computational effort, because it decreases a three-dimensional problem to a two-dimensional one.

If the orthogonal axes system ζ, η and ξ are used, the fundamental assumptions for a plane-strain thermoelastic problem are:

$$\mu_\xi = 0, \qquad \mu_\zeta = \mu_\zeta(\zeta,\eta), \qquad \mu_\eta = \mu_\eta(\zeta,\eta) \tag{19}$$

The corresponding strain components have the form:

$$\varepsilon_\xi = \varepsilon_{\xi\zeta} = \varepsilon_{\xi\eta} = 0$$

$$\varepsilon_{\zeta\zeta} = \varepsilon_{\zeta\zeta}(\zeta,\ \eta), \qquad \varepsilon_{\eta\eta} = \varepsilon_{\eta\eta}(\zeta,\ \eta), \qquad \varepsilon_{\zeta\eta} = \varepsilon_{\zeta\eta}(\zeta,\ \eta) \tag{20}$$

The stress field is related to the strain field by the elastic constants of modulus of elasticity and Poisson's ratios. As stated before, wood is an orthotropic material, the modulus of elasticity of wood in longitudinal direction (parallel to grain) have in general, a significant difference with those in radial or tangential direction, some twenty times as large [9]. To account for the possible difference in radial and tangential directions, a 10% difference is again maintained in this computation. For plywood, an average value is taken. They are listed in Table 3.

Table 3.

	Douglas Fir	Birch	Birch Plywood
E_L	$1.95\text{x}10^6$ psi	$2.10\text{x}10^6$ psi	$1.38\text{x}10^6$ psi
E_T	$0.098\text{X}10^6$ psi	$0.105\text{x}10^6$	$0.77\text{x}10^6$
E_R	$0.133\text{x}10^6$ psi	$0.164\text{x}10^6$	$0.164\text{x}10^6$
G_{TR}	$0.014\text{x}10^6$ psi	$0.036\text{x}10^6$	$0.076\text{x}10^6$

The Poisson's ratios 'ν' and the thermal expansion coefficients, α, of wood are also different significantly in the major axis directions. They [9] are listed in Table 4.

Table 4.

	Douglas Fir	Birch	Birch Plywood
α_L	$2.1\text{x}10^{-6}$/°F	$2.1\text{x}10^{6}$/°F	$14.57\text{x}10^{-6}$
α_T	$34.9\text{X}10^{-6}$/°F	$39.52\text{x}10^{-6}$/°F	$27.05\text{x}10^{-6}$
α_R	$25.9\text{x}10^{-6}$/°F	$30.38\text{x}10^{-6}$/°F	$30.38\text{x}10^{-6}$
ν_{LR}	0.292	0.426	0.433
ν_{LT}	0.449	0.451	0.308
ν_{RT}	0.390	0.697	0.476
ν_{TR}	0.287	0.447	0.440
ν_{RL}	0.020	0.033	0.255
ν_{TL}	0.022	0.023	0.166

B. Formulation of Potential Energy

In Phase I, the heat conduction portion of the problem, a governing partial differential equation needs to be established first, then, the finite element method in Variational approach is employed as a numerical procedure to obtain its solution. Now, for the problem of finding the thermal-stresses due to a temperature distribution, no controlling differential equation can be found. Thus, a conceptually different technique must be used to determine directly the displacement field, {f}, without going through the intermediate step of establishing the differential equation. Once {f} is found, the stress field $\{\sigma\}$ can be determined accordingly.

First, with an assumed displacement field and under the influence of temperature rises at various locations, the total potential energy, P.E., may be expressed as

$$P.E. = \int_V \left(\frac{1}{2}\,[\varepsilon]^T[E]\,[\varepsilon] - [\varepsilon]^T[E]\,[\alpha T]\right)dv \tag{21}$$

where V represents the total volume of the blade. In a two-dimensional case, it may be replaced by the multiplication of thickness and cross-sectional area, i.e., t * A.

Let v and w be the displacements of a point in ζ and η directions, we may express $[\varepsilon]$ in terms of the displacement field {f} as follows:

$$\{\varepsilon\} = [\partial]\,\{f\}$$

where
$$\{\varepsilon\} = \begin{bmatrix} \varepsilon_\zeta \\ \varepsilon_\eta \\ \gamma_{\zeta\eta} \end{bmatrix}, \quad [\partial] = \begin{bmatrix} \frac{\partial}{\partial\zeta} & 0 \\ 0 & \frac{\partial}{\partial\eta} \\ \frac{\partial}{\partial\eta} & \frac{\partial}{\partial\zeta} \end{bmatrix}, \quad \{f\} = \begin{bmatrix} v \\ w \end{bmatrix}$$

Further, the strain components of a point, $\{\varepsilon\}$, may be expressed in terms of nodal displacements $\{D\}$. For demonstration purpose, a triangular element as shown in Fig. 15 and the aforementioned shape functions, $[N]$, are again used, the strain field, $\{\varepsilon\}$, may be expressed as:

$$\{\varepsilon\} = [\partial]\,[N]\,\{D\},$$

or

$$\{\varepsilon\} = [B]\,\{D\} \tag{22}$$

where

$$[B] = [\partial]\,[N]$$

$$[N] = \begin{bmatrix} N_i & 0 & N_j & 0 & N_k & 0 \\ 0 & N_i & 0 & N_j & 0 & N_k \end{bmatrix}$$

$$[D] = \begin{bmatrix} v_i & w_i & v_j & w_j & v_k & w_k \end{bmatrix}^T$$

$$N_i = \frac{1}{2A}\,[a_i + b_i\,\zeta + c_i\,\eta]$$

$$N_j = \frac{1}{2A}\,[a_j + b_j\,\zeta + c_j\,\eta]$$

$$N_k = \frac{1}{2A}\,[a_k + b_k\,\zeta + c_k\,\eta]$$

Note that A, a_i, a_j and a_k have been described in (11b) and (11c).

Expanding $\{D\}$ to cover all the nodal displacements in the entire blade section and substituting Equation (22) into Equation (21), one obtains:

$$\text{P.E.} = \frac{1}{2}\,[D]^T\,\{\int[B]^T[E][B]dv\}\,[D] - [D]^T\int[B]^T[E][\alpha T]dv \tag{23}$$

Equation (23) expresses the total potential energy of the blade section in finite element formulation.

C. Finite Element Method--Minimum Potential Energy Approach

Recall that the total potential energy, P.E., is formed based on an assumed displacement field {f}, for each element. These fields are then expressed in terms of unknown nodal displacements by using shape functions. Although admissible fields are chosen, the compatibility conditions are therefore satisfied within the elements and at the nodes, yet the equilibrium conditions remain to be determined.

It is known that among all admissible configurations of a conservative system, those that satisfy the equations of equilibrium make the potential energy stationary with respect to small variations of displacement. If the stationary condition is a minimum, the equilibrium state is stable. Thus, the equilibrium conditions may be sought through the minimization of the total potential energy P.E., namely,

$$\frac{\partial\, P.E.}{\partial D} = 0 \tag{24}$$

or,

$$\left(\sum_{1}^{m} \int_{v} [B]^T[E][B]dv\right) \{D\} = \sum_{1}^{m} \int_{v} [B]^T[E][\alpha T]dv \tag{25}$$

where v is the volume of an element.

Equation (25) may be written in the following simplified form:

$$[K]\ [D] = [P] \tag{26}$$

where [K] is the total stiffness of the blade and [k] is the stiffness of each element, $[p_e]$ is the thermal load produced at nodal points in a

given temperature field and [E], Matrix of modulus of elasticity;

$$[K] = \sum_{1}^{m} [k]$$

$$[k] = \int [B]^T [E][B] dv \tag{27}$$

$$[P] = \sum_{1}^{m} [p_e]$$

$$[p_e] = \int_V [B]^T [E][\alpha t] dv$$

Equation (26) is the finite element formulation of the blade section if isotropic material is used. But the wood composite is an orthotropic material, the matrices of modulus of elasticity [E] in Equation (25), need to be modified accordingly as to be described in the following sections.

D. The Treatment of Orthotropic Property

For an orthotropic material such as wood [8] and in the case of plain strain, the normal strain-stress relationships apply:

$$\begin{aligned} \varepsilon_\zeta &= \frac{1}{E_\zeta} \sigma_\zeta - \frac{\nu_{\zeta\eta}}{E_\eta} \sigma_\eta - \frac{\nu_{\zeta\xi}}{E_\xi} \sigma_\xi \\ \varepsilon_\eta &= -\frac{\nu_{\eta\zeta}}{E_\zeta} \sigma_\zeta + \frac{1}{E_\eta} \sigma_\eta - \frac{\nu_{\eta\xi}}{E_\xi} \sigma_\xi \end{aligned} \tag{28}$$

also

$$\varepsilon_\xi = -\frac{\nu_{\xi\zeta}}{E_\zeta} \sigma_\zeta - \frac{\nu_{\xi\eta}}{E_\eta} \sigma_\eta + \frac{1}{E_\xi} \sigma_\xi = 0$$

Thus

$$\sigma_\xi = \frac{E_\xi}{E_\zeta} \nu_{\xi\zeta} \sigma_\zeta + \frac{E_\xi}{E_\eta} \nu_{\xi\eta} \sigma_\eta \tag{29}$$

Note that $\nu_{\zeta\eta}$ denotes the strain in the ζ direction due to strain in the η direction.

Substitution of Equation (29) into (28) produces:

$$\varepsilon_\zeta = \frac{1}{E_\zeta}(1 - \nu_{\zeta\xi}\,\nu_{\xi\zeta})\,\sigma_\zeta - \frac{1}{E_\eta}(\nu_{\zeta\eta} + \nu_{\zeta\xi}\,\nu_{\xi\eta})\,\sigma_\eta \tag{30}$$

$$\varepsilon_\eta = \frac{-1}{E_\zeta}(\nu_{\eta\zeta} + \nu_{\eta\xi}\,\nu_{\xi\zeta})\,\sigma_\zeta + \frac{1}{E_\eta}(1 - \nu_{\eta\xi}\,\nu_{\xi\eta})\,\sigma_\eta$$

Solving the above equations, one finds:

$$\sigma_\zeta = (aE_\zeta\varepsilon_\zeta + bE_\zeta\varepsilon_\eta)\;/\;(ad - bc)$$

$$\sigma_\eta = (cE_\eta\varepsilon_\zeta + dE_\eta\varepsilon_\eta)\;/\;(ad - bc) \tag{31}$$

$$\tau_{\zeta\eta} = G_{\zeta\eta}\,\gamma_{\zeta\eta}$$

where,

$a = 1 - \nu_{\eta\xi}\,\nu_{\xi\eta}$

$b = \nu_{\zeta\eta} + \nu_{\zeta\xi}\,\nu_{\xi\eta}$

$c = \nu_{\eta\zeta} + \nu_{\eta\xi}\,\nu_{\xi\zeta}$

$d = 1 - \nu_{\zeta\xi}\,\nu_{\xi\zeta}$

or, the stress-strain relationships may be described in a matrix form as

$$\{\sigma\} = [E_m]\,\{\varepsilon\} \tag{32}$$

where

$$[E_m] = \frac{1}{ad - bc}\begin{bmatrix} a\,E_\zeta & b\,E_\zeta & 0 \\ c\,E_\eta & d\,E_\eta & 0 \\ 0 & 0 & (ad - bc)G_{\zeta\eta} \end{bmatrix} \tag{33}$$

From the Maxwell-Betti's Reciprocal theorem,

$$cE_\eta = bE_\zeta\,,$$

or,

$$\frac{E_\eta}{E_\zeta} = \frac{b}{c}\,,$$

so the matrix of modulus of elasticity remains symmetrical for wood.

Equation (33) gives the matrix $[E_m]$ for plane strain in an orthotropic material, where ζ, η and ξ are principal directions of orthotropy.

The elasticity constants of wood, ν, E, α and G, have been described in Tables 3 and 4. In view of the blade construction, wood property axis T corresponds to axis ζ in this section, R to η and L to ξ.

E. Element Axes to Structural Axes

Because of the blade curvature, the principal axes of material at one point in the blade section have in general, a different orientation with respect to the structural axes than those at another point. A typical orientation of laminated wood has been shown in Fig. 5, where ζ, η and ξ are the principal axes of material and local axes of the element, while y, z and x are the structural axes and the axes of the blade section. The transformation from material axes to structural axes is necessary for all elements in order to unify them in the framework of structural axes. This transformation process may be described as follows:

T_{ms} = Transformation from structural axes to material axes

then,

$$\{\varepsilon_m\} = [T_{ms}]\,\{\varepsilon_s\} \tag{34}$$

where subscript m and s represent material axes and structures axes, and

$$[T_{ms}] = \begin{bmatrix} \cos^2\beta & \sin^2\beta & \sin\beta\cos\beta \\ \sin^2\beta & \cos^2\beta & -\sin\beta\cos\beta \\ -2\sin\beta\cos & 2\sin\beta\cos\beta & \cos^2\beta - \sin^2\beta \end{bmatrix}$$

In addition, the stress transformation from material axes to structural axes is

$$\{\sigma_s\} = [T_{ms}]^T \{\sigma_m\} \tag{35}$$

A proper stress-strain transformation may then be obtained by first stating the stress-strain relationships in material axes, namely,

$$\{\sigma_m\} = [E_m] \{\varepsilon_m\} \tag{36}$$

where $[E_m]$ has been described in Equation (33). Substitution of Equation (34) and (36) into (35) gives:

$$\{\sigma_s\} = [T_{ms}]^T [E_m] [T_{ms}] \{\varepsilon_s\}$$

or

$$\{\sigma_s\} = [E_s] \{\varepsilon_s\} \tag{37}$$

where

$$[E_s] = [T_{ms}]^T [E_m] [T_{ms}]$$

$[E_s]$ is the matrix of modulus of elasticity for orthotropic material, of which the material axes ζ and η are oriented at β angle with respect to principal axes y and z, and material axis ξ coinsides with structural axis x. This matrix is used in place of [E] in Equation (25) for the determination of the stiffness of each element, [k], and thermal load matrix of each element, $[P_e]$. Then, proper combinations of [k] and $[P_e]$ respectively for all elements render [K] and [P] as described in Equations (25) to (27). Finally, the equation (26) is solved and the displacements of all nodal points [D] are determined. When the displacement field is found, the stresses at each element can be computed accordingly. Thus, the determination of thermal-stress distribution on the wood blade is accomplished.

F. Thermal Stresses

Corresponding to the two steady-state Heat Conduction analyses made in Phase I, two thermal-stress analyses are run on the University computer. The stresses are all computed in material axes ξ and η as shown in Fig. 5. Only the stresses of elements in the surface layer are plotted. For example, Fig. 16 shows the stresses in ξ direction when the blade section is in horizontal position, and Fig. 17 shows the same type of stresses when the blade section is in vertical position.

Observing Fig. 16 and 17, one finds that the high temperature sides of the blades, stresses of same magnitude are induced. This offers an independent check on the correctness of the computations. The sense of the stresses on the high temperature side is tensile, this is largely due to the special characteristics of the blade construction. As described before, in D-spar a thin layer of 1/8" Birch plywood wraps around 3" of lamintated Douglas Fir. The thermal expansion coefficient in tangential direction of Douglas Fir is about 23% higher than that of Birch plywood. When the temperature rises, the thin layer of Birch plywood is 'stretched' by the expanding Douglas Fir. Thus, tensile stresses are produced on the exterior surface of the blade. This computational phenomenon agrees to the rationality of engineering. Furthermore, in view of the smooth transition from high stress area to low stress area; in Fig. 16 the stresses on the tail portion varies when the interior materials changed from Douglas Fir to honeycomb paper core; and the approximately symmetrical stress distribution on Fig. 17 for an approximately symmetrical blade geometry and thermal loadings; one can conclude, short of experimental verification, that the analysis offers a set of results with high believability.

Conclusion Remarks

A. Pre-run Program Testings

For the purpose of increasing the reliability of the finite element analyses, both the heat conduction analysis computer programs and the thermal-stress analysis computer programs have undergone several testings before using on the analysis of the blade. These testings consist of solving smaller but similar engineering problems with either theoretical solutions or solutions given by other authors. Nearly identical results have been obtained in all testings.

B. Finer-Mesh Testing

After the thermal-stress analysis has been performed on the blade, for a finite element model of 388 elements, the analysis is repeated on a finer-mesh model of 688 elements. For the finer-mesh model, the stresses in ζ direction of the surface layer elements are shown in Fig. 18. A comparison of Fig. 16 to Fig. 18 shows that the stresses of the former are converging to the corresponding stresses of the later. This is considered to be a good convergence test for finite element analysis.

C. Engineering Judgement

The final results of steady-state temperature distribution and the thermal-stress distribution as shown in Figs. 6, 7, 16 and 17 are agreeable to engineering rationality as stated in section E of Phase I and section F of Phase II.

D. The Cause of Cracking

The allowable stresses in principal directions of Birch plywood [9] are listed in Table 5. A comparison reveals that the maximum blade thermal-stress, which occurs in ζ direction, is far lower than the allowable stress in the corresponding direction, σ_T. Although the trancient thermal-stress analysis is not performed due to time limitation of the research project, yet it is believed that they should not exceed the allowable stress level for a prolonged period, since the sun is a mild heat source.

Table 5

Allowable Stresses for Birch Plywood		
	Compressive	Tensile
σ_L	5,770 psi	13,640 psi
σ_T	3,370	7,280
σ_R	970	920

E. Conclusion

In conclusion, the cause of cracking of the blade is not due to thermal stresses induced by the sun. Investigation of other causes, such as poor manufacturing, needs to be made. In addition to the elimination of thermal stress as a possible reason of blade cracking, the research brings forth a method and a practical example of thermal-stress analysis for an engineering body of orthotropic materials, which will find many applications in the Engineering Community.

Acknowledgement

The work was supported by NASA Grant NAG3-373. The encouragement received from Mr. Darrell H. Baldwin, Manager of Wind Energy Project Office and Dr. David A. Spera, Chief engineer of the same Office is highly appreciated by the senior author. Acknowledgement is due to Mr. Timothy Sullivan, Research engineer of the same office, for providing constant guidance throughout the project.

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[9] Forest Service, U.S. Department of Agriculture, "Wood Handbook: Wood as an Engineering Material," Revised August, 1974, U.S. Government Printing Office, Washington, D.C.

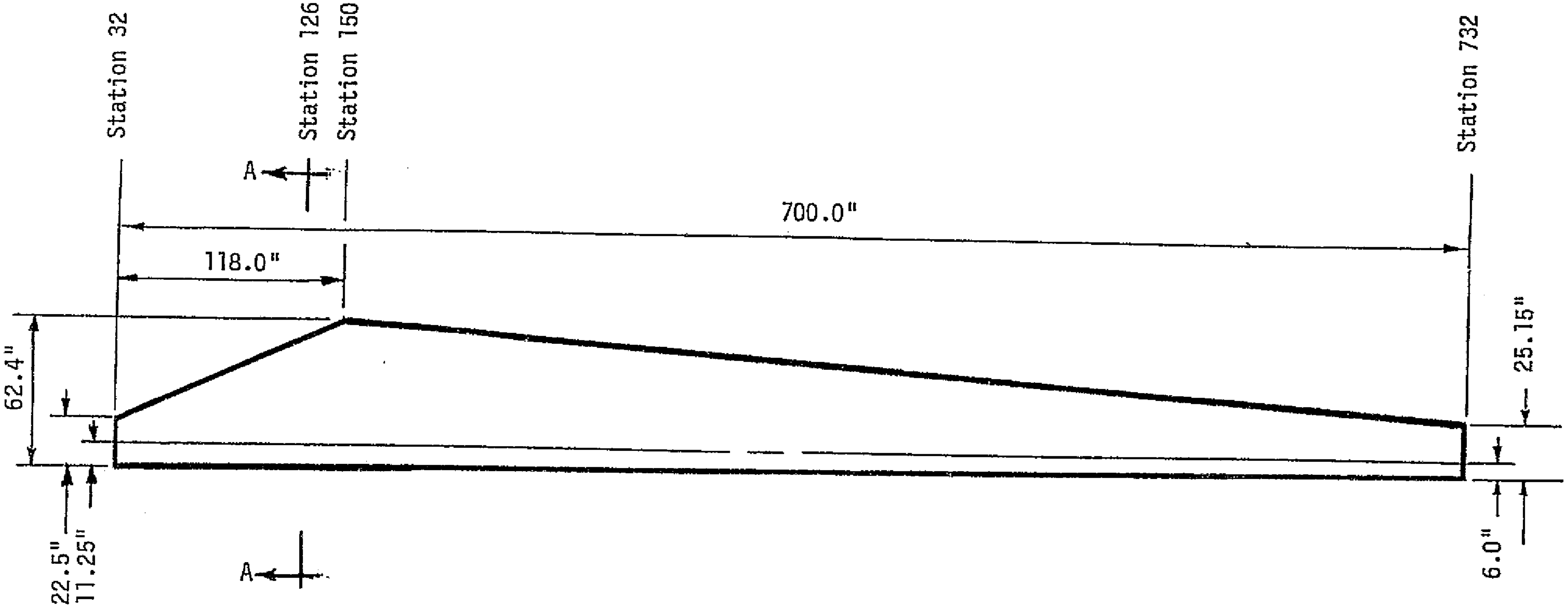


Figure 1

Scale: 1:80

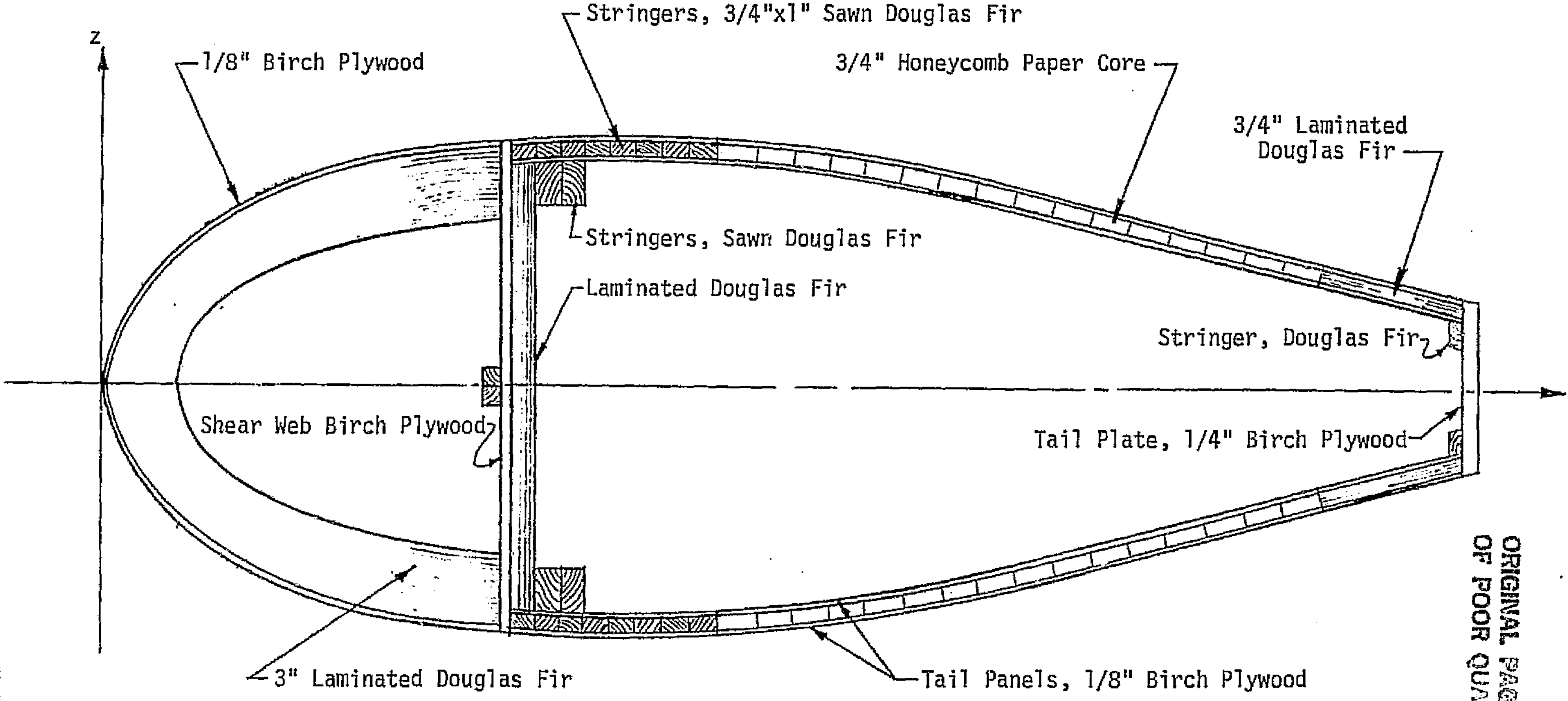


Figure 2. Section A-A at Station 126

Scale: 1:6

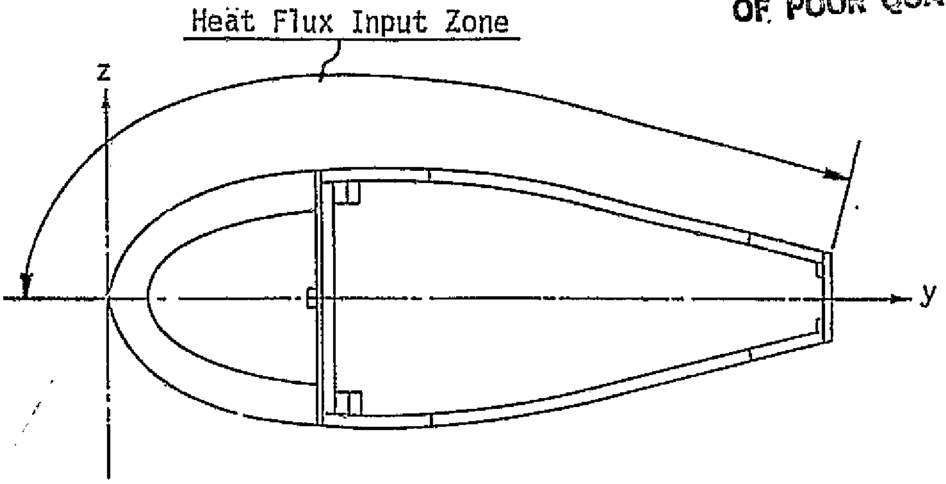


Figure 3

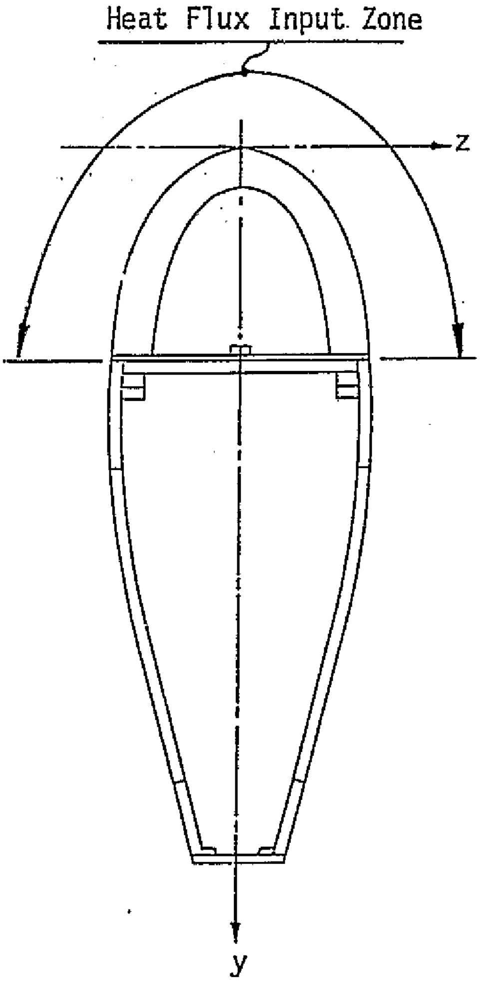


Figure 4

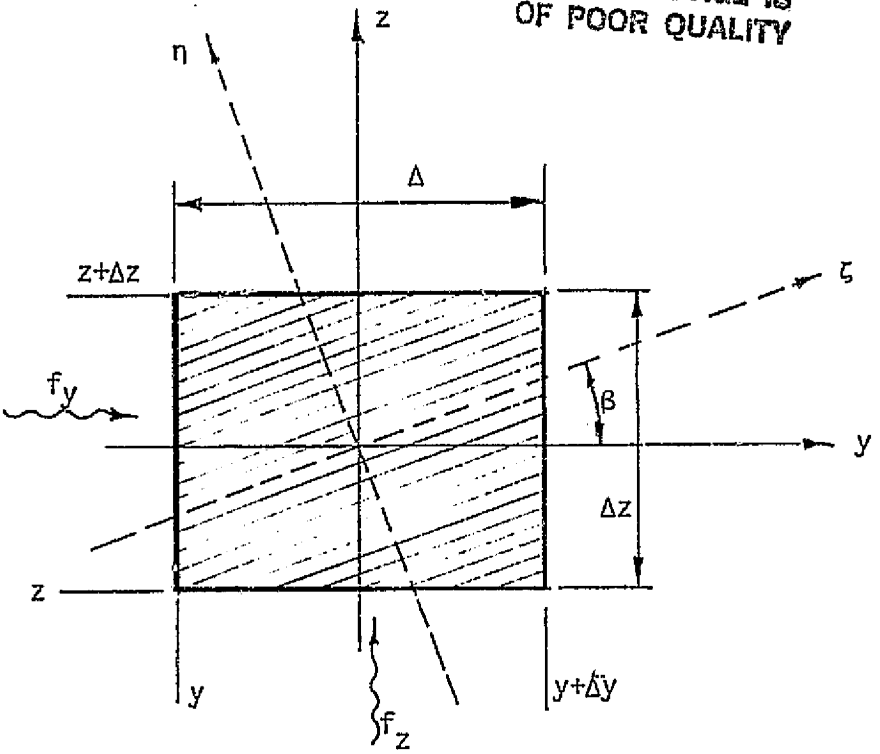


Figure 5

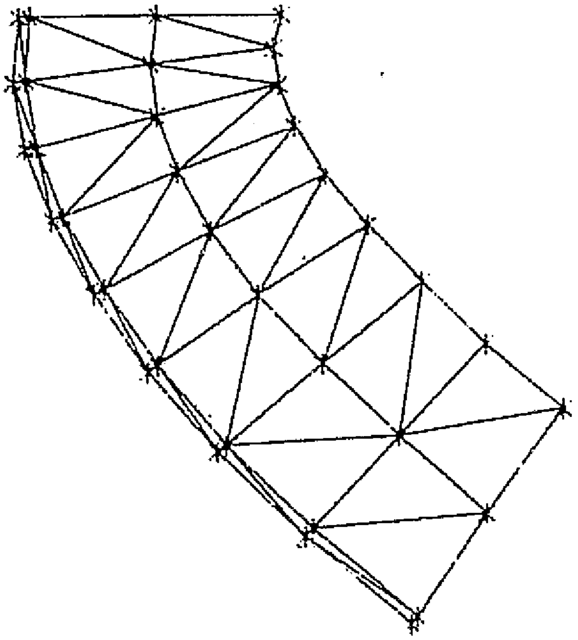


Figure 7

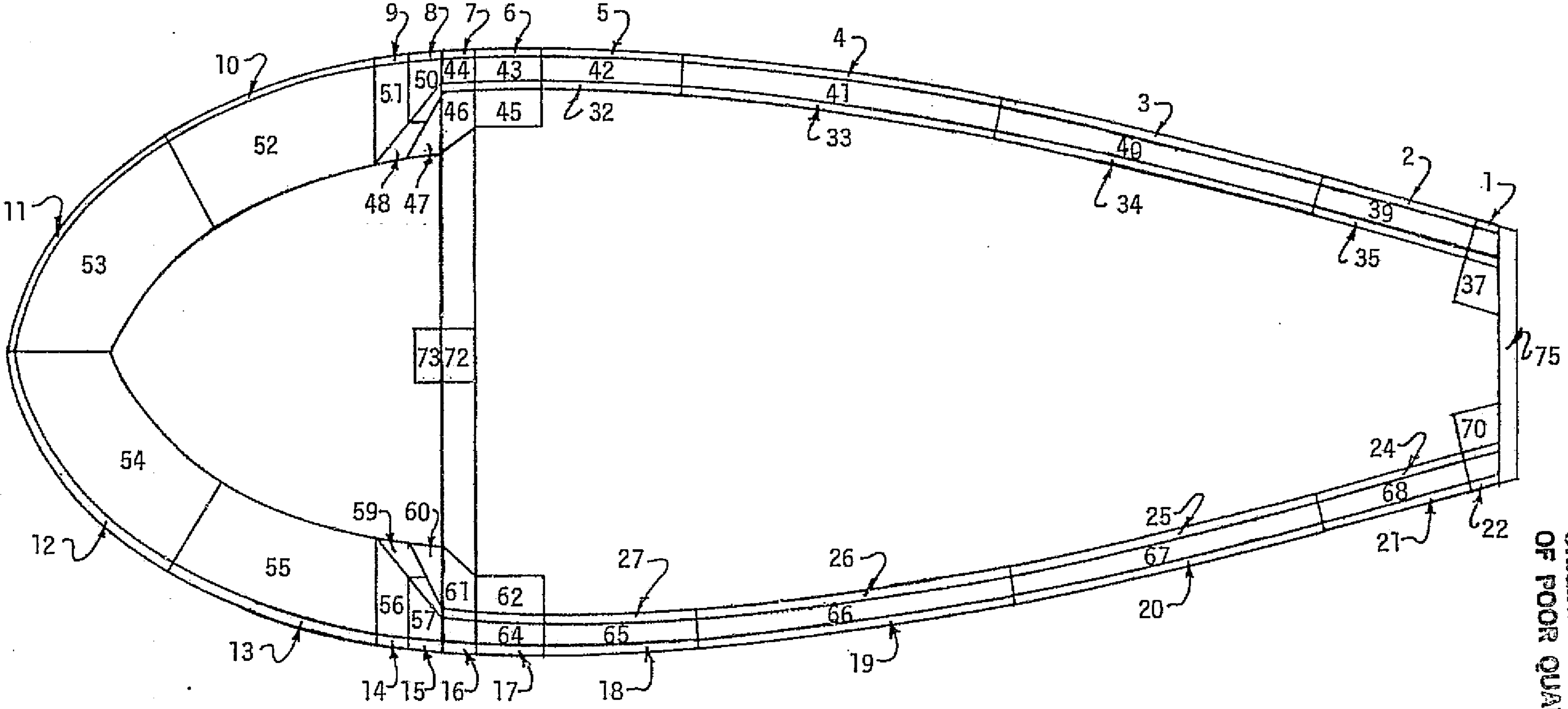


Figure 6. Regions for Mesh Generation

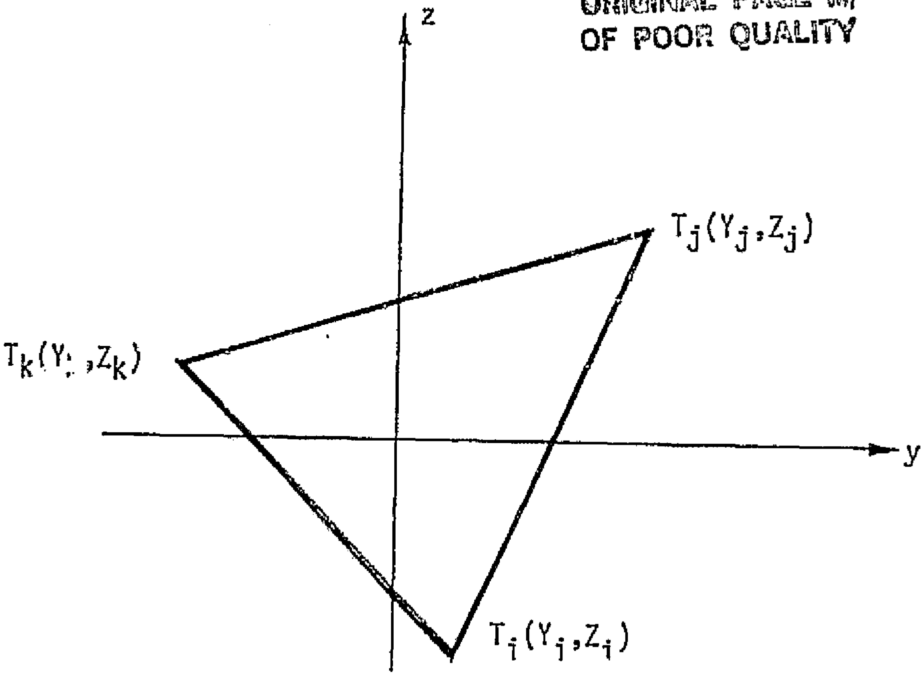


Figure 8

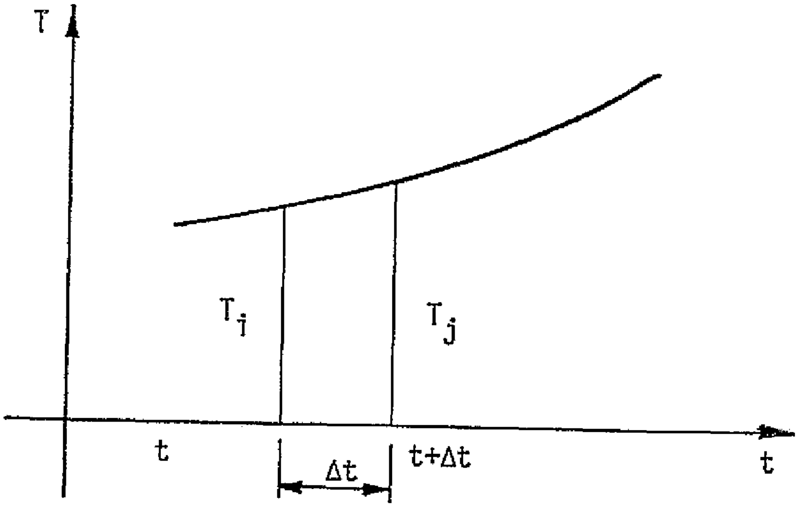


Figure 12

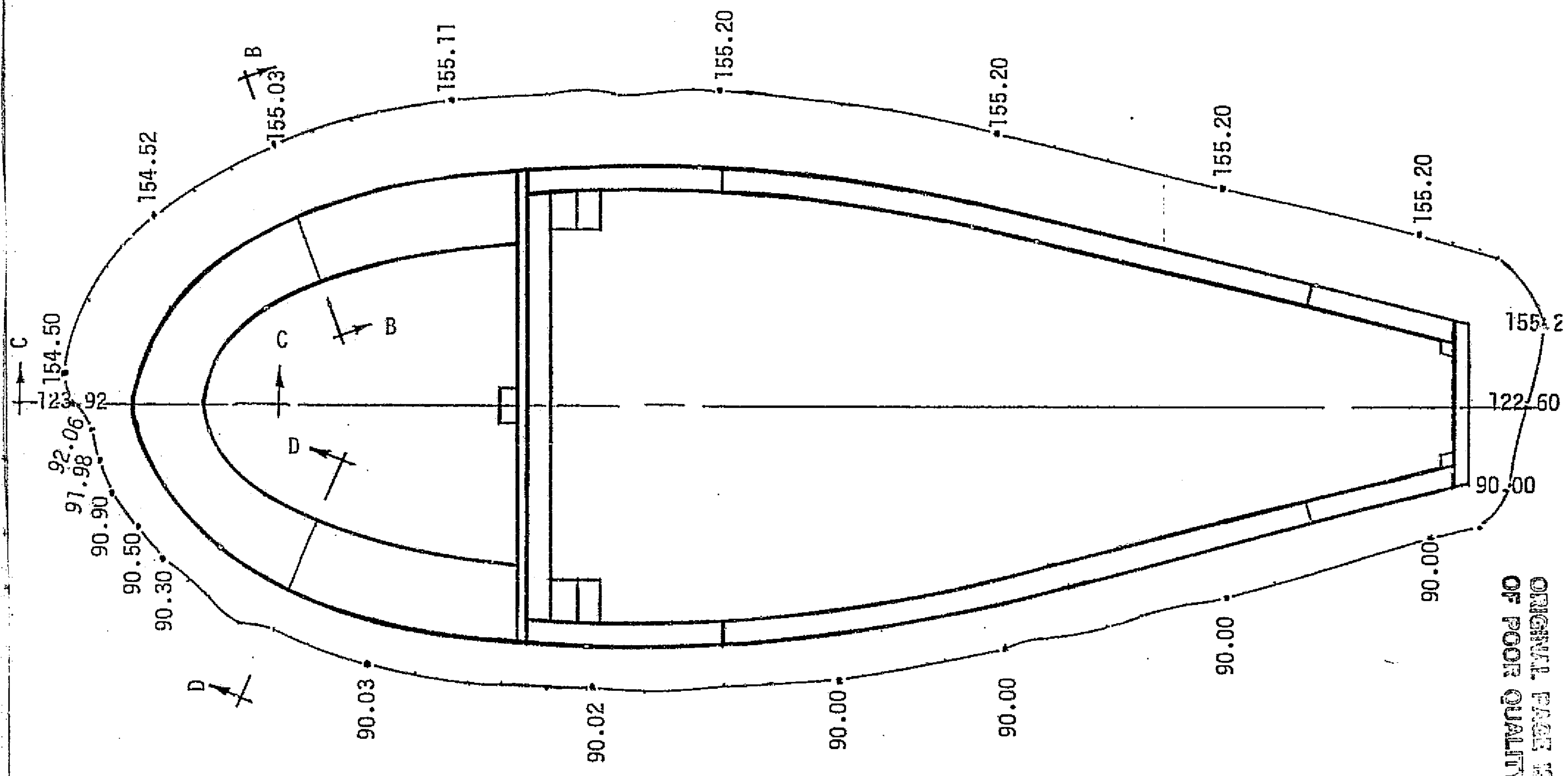


Figure 9. Temperature Distribution of Exterior Elements, Blade Section in Horizontal Position

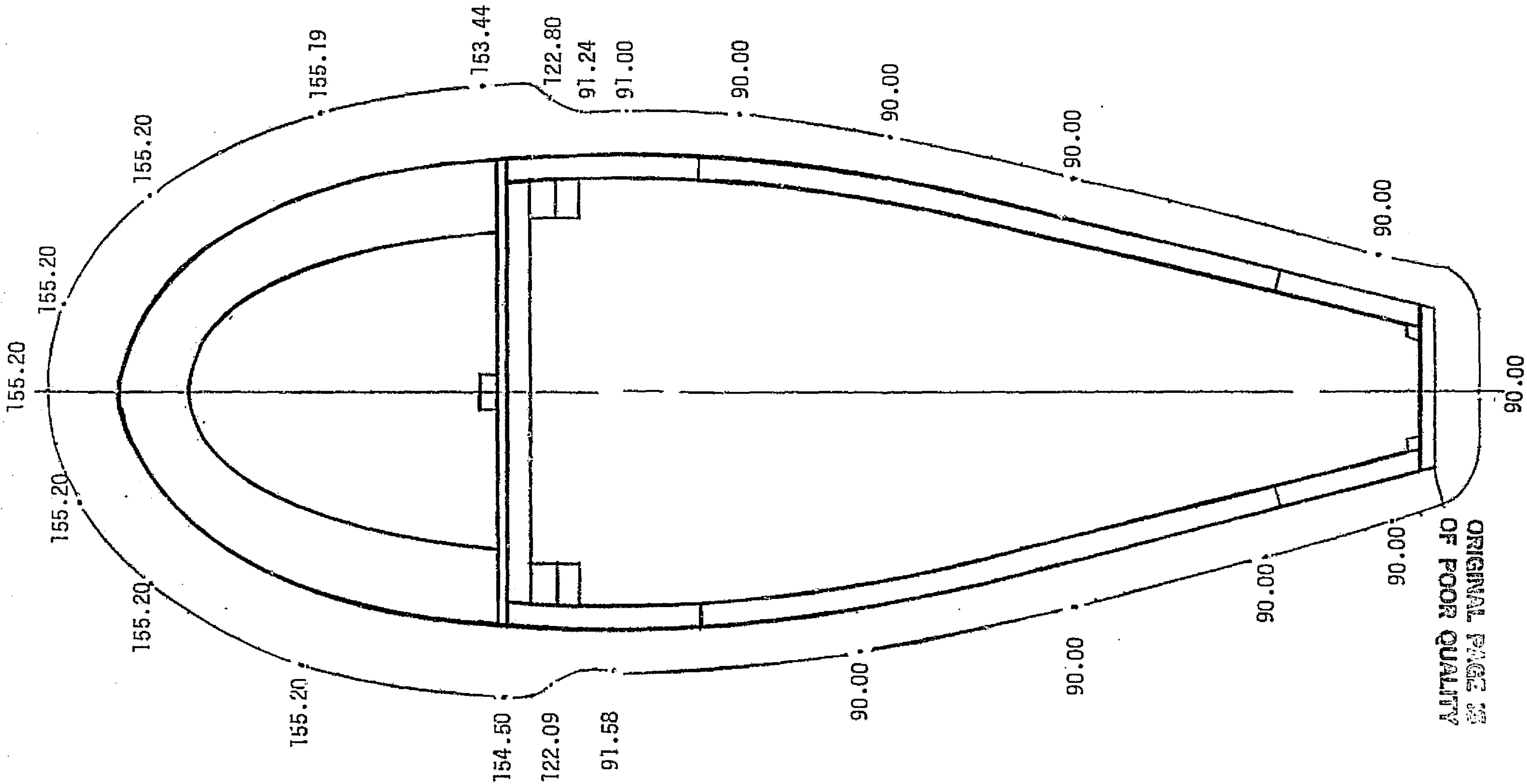
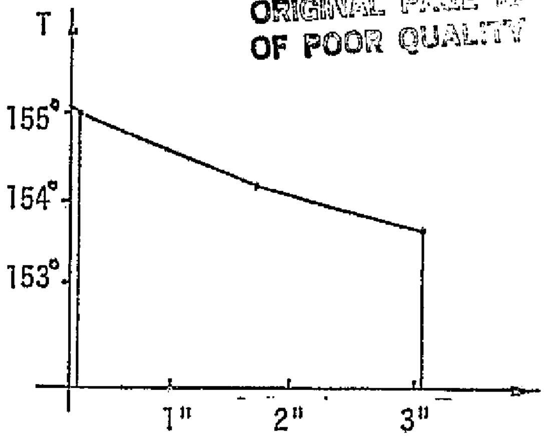
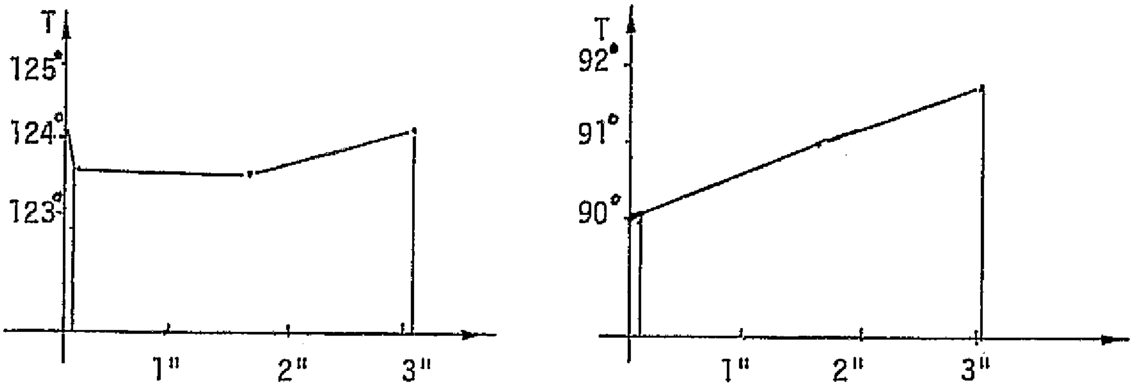


Figure 10. Temperature Distribution of Exterior Elements, Blade Section in Vertical Position



Section B-B



Section C-C

Section D-D

Figure 11. Temperature Profiles

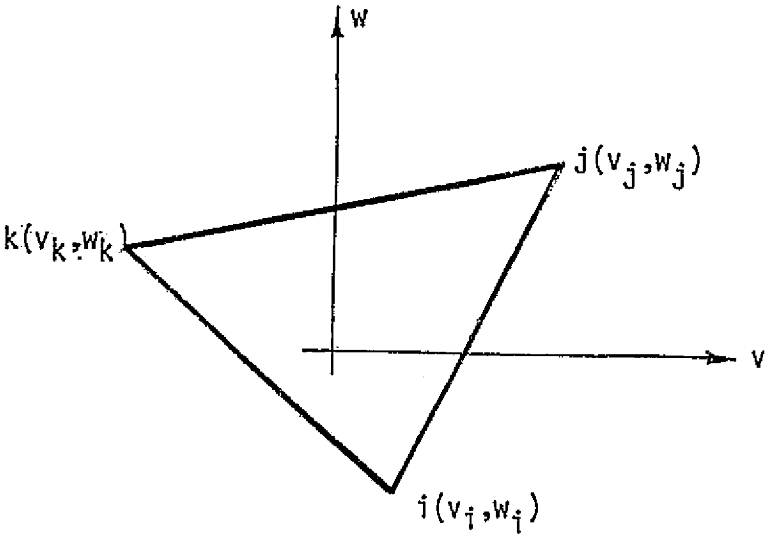


Figure 15

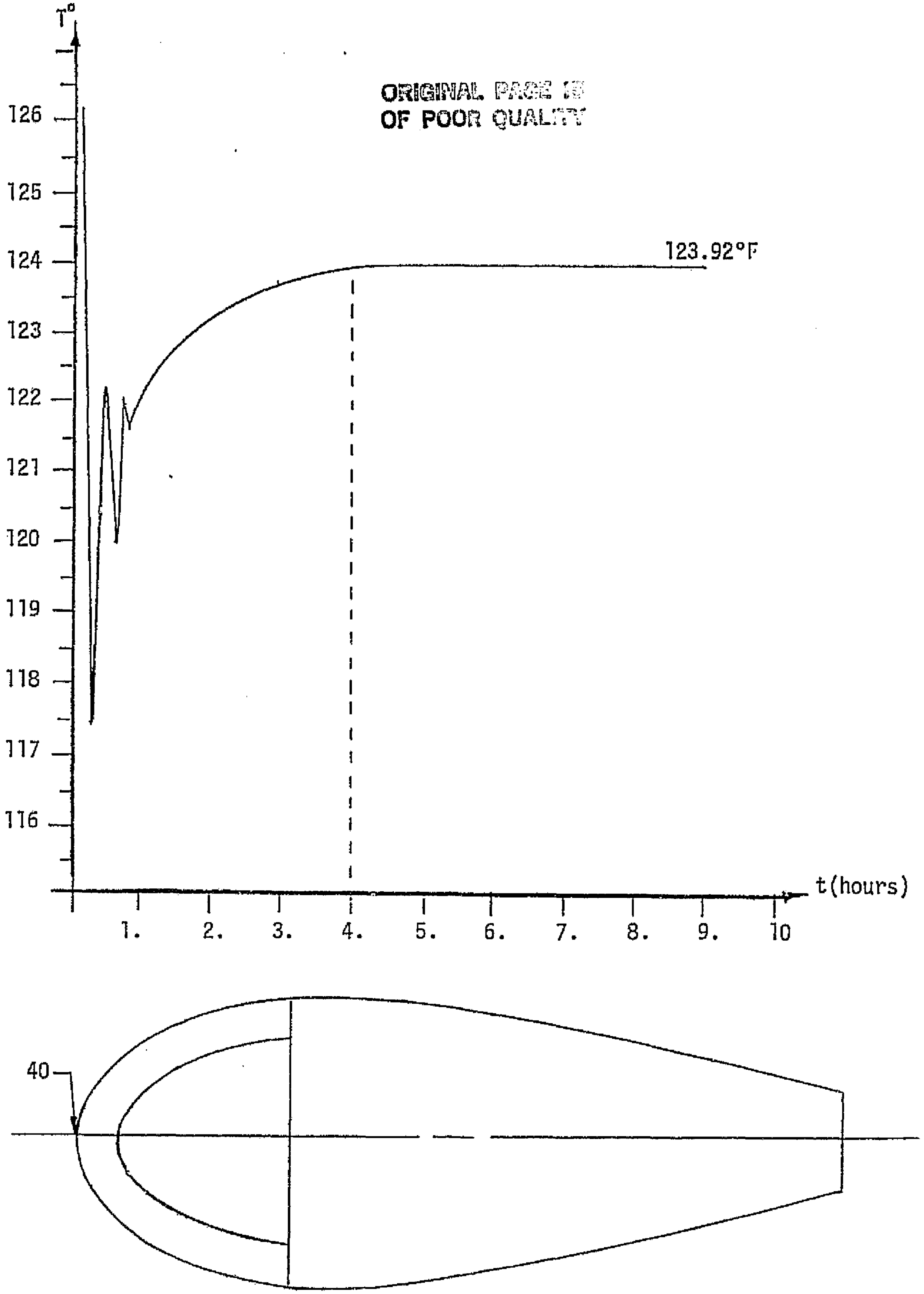


Figure 13. Temperature History at Node 40

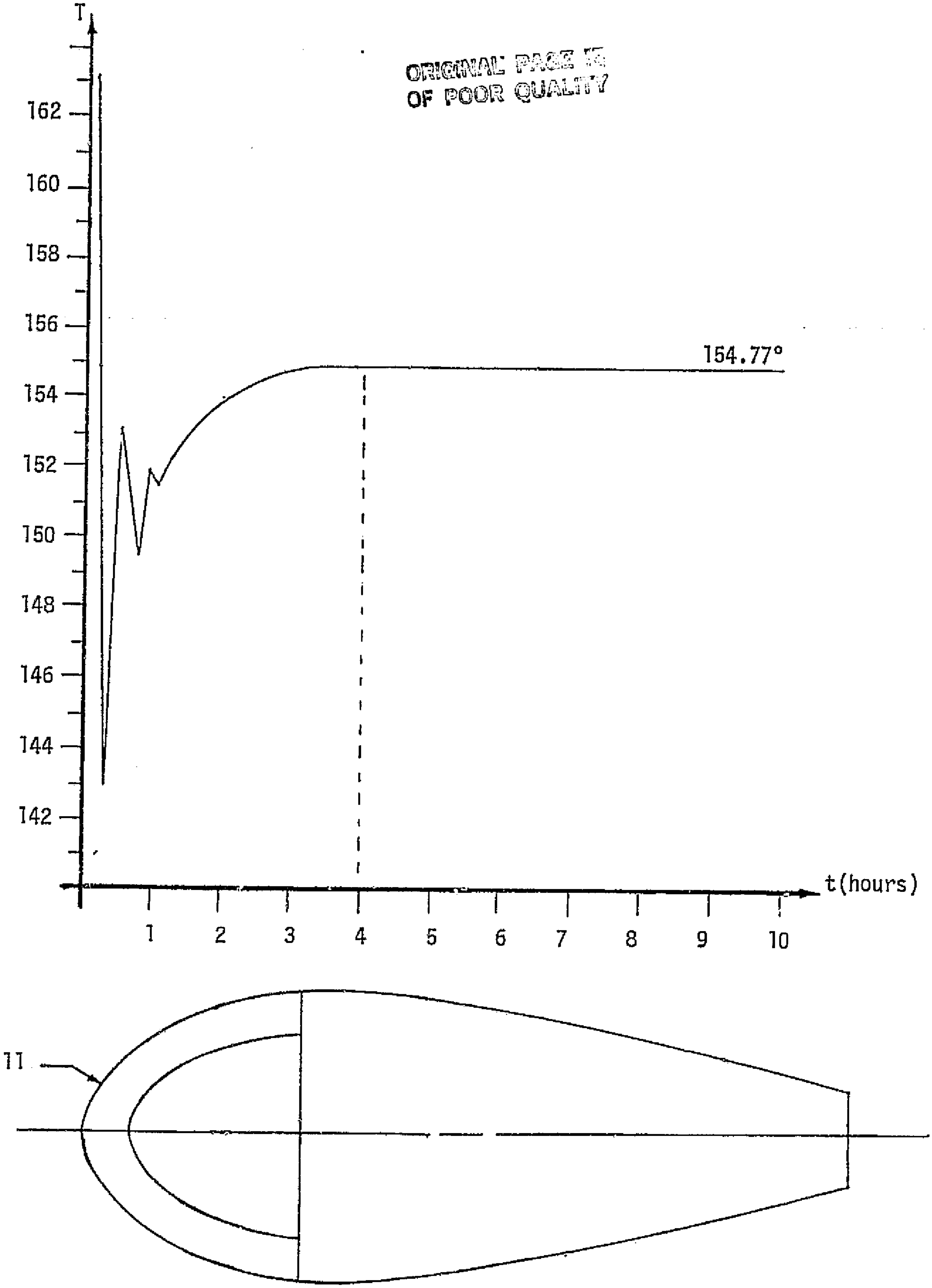


Figure 14. Temperature History at Node 11

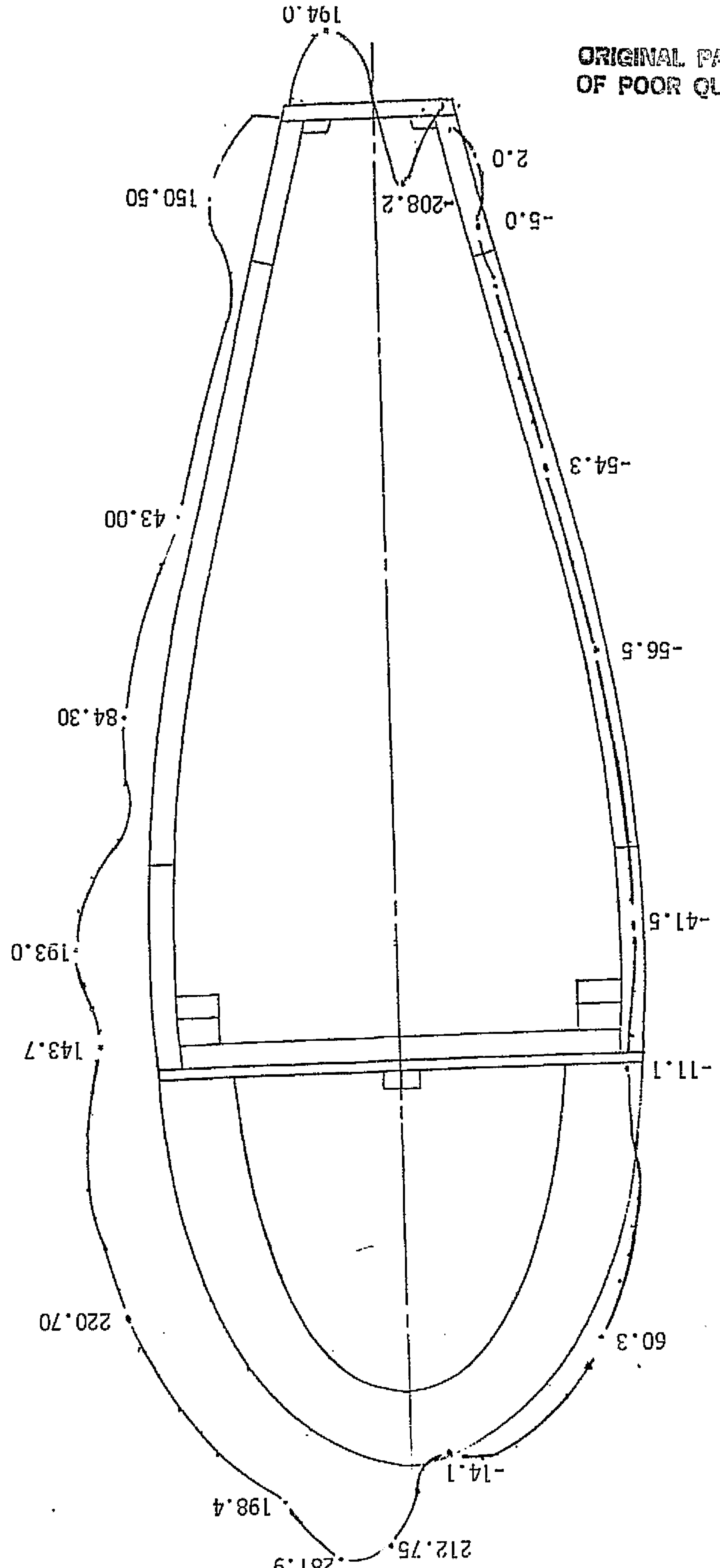


Figure 16. Thermal Stressess in ζ Direction Blade Section in Horizontal Position

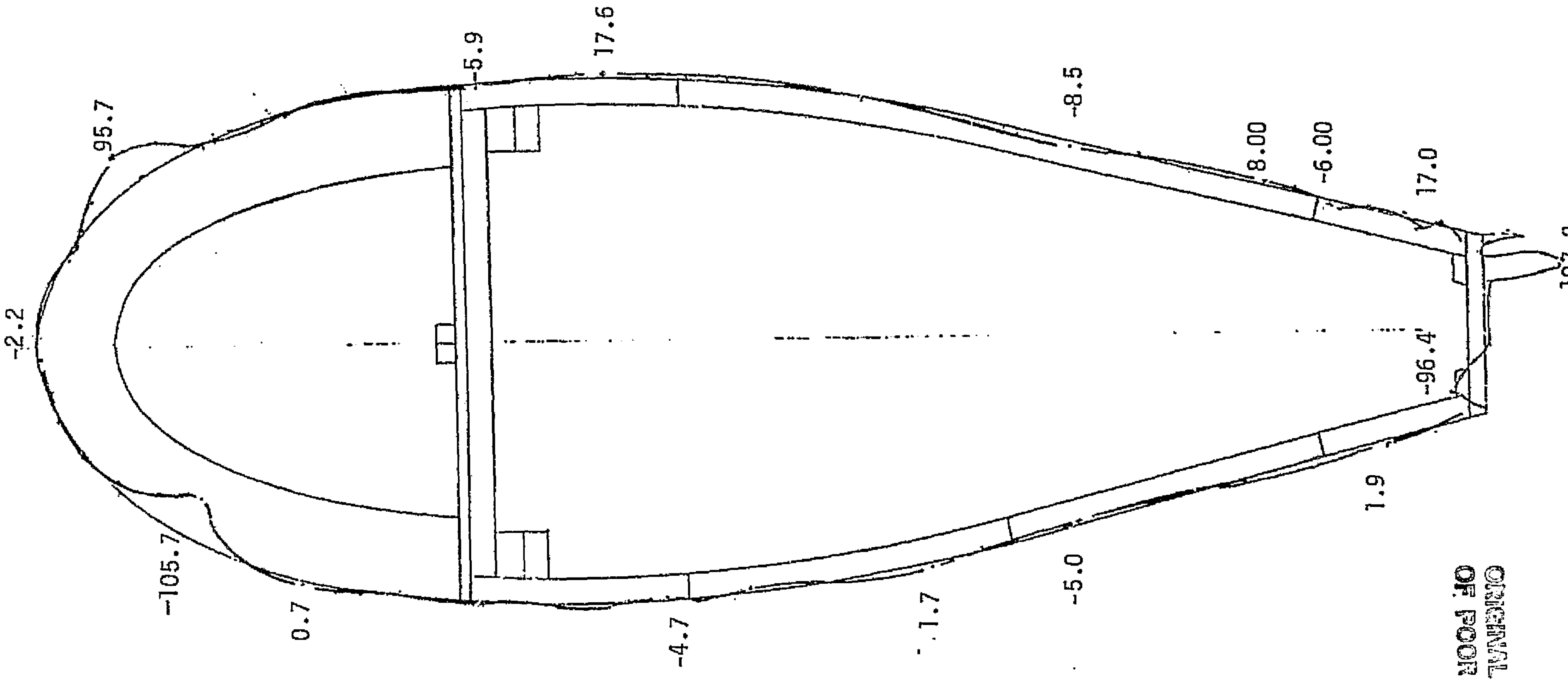


Figure 16a. Thermal Stresses in η Direction, Blade Section in Horizontal Position

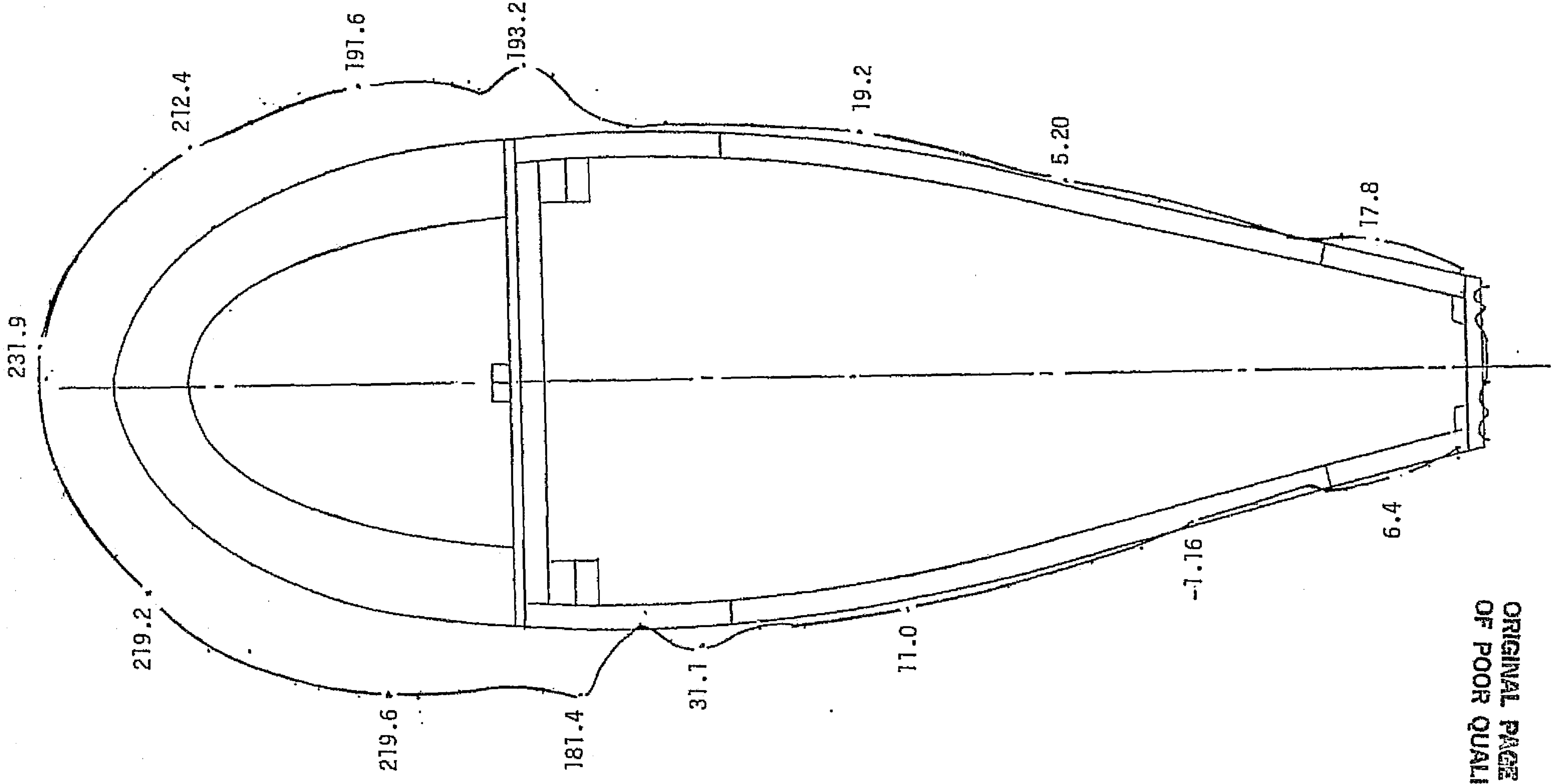


Figure 17. Thermal Stresses in ζ Direction, Blade Section in Vertical Position

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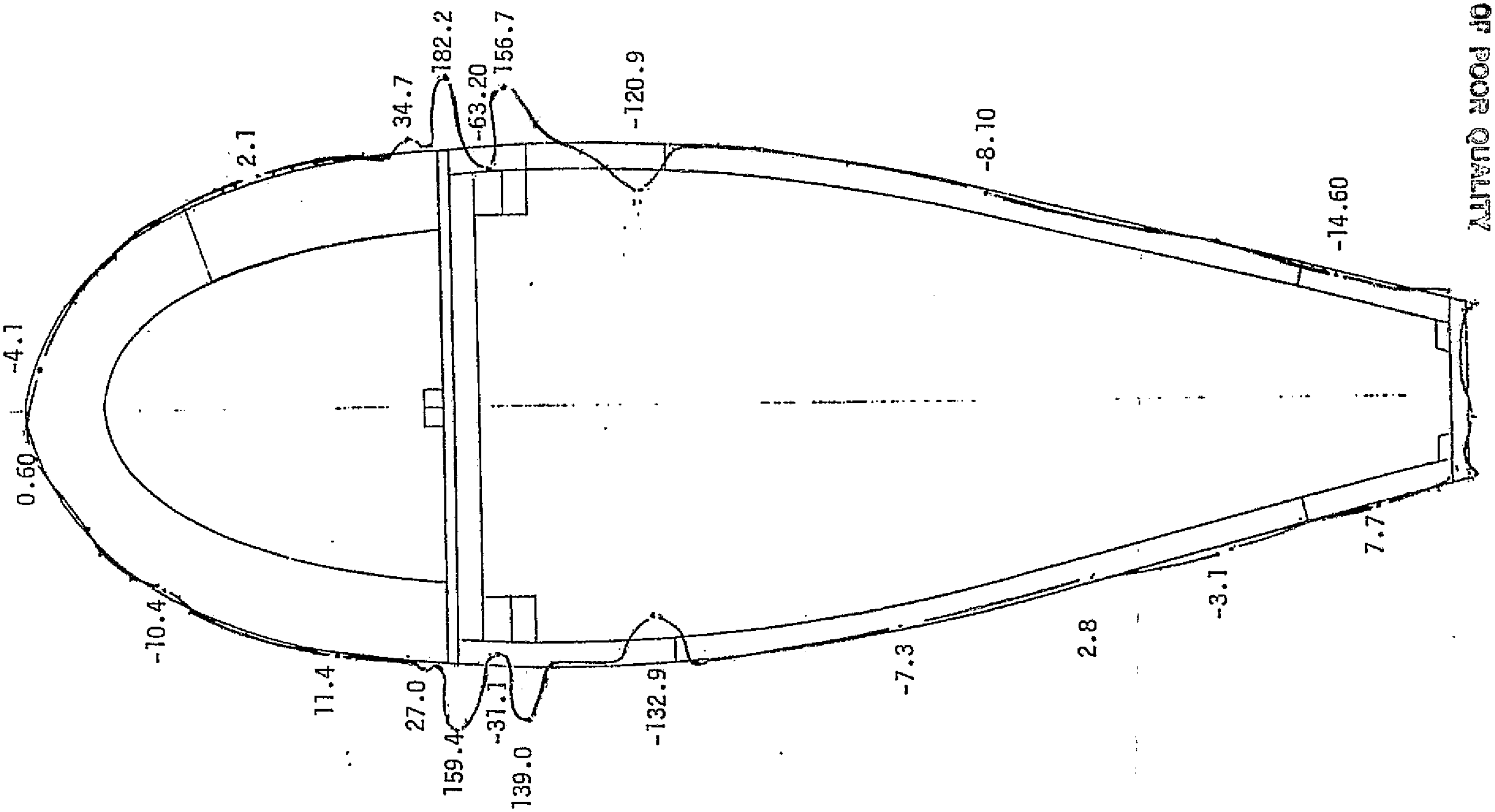

Figure 17a. Thermal Stresses in η Direction, Blade Section in Vertical Position

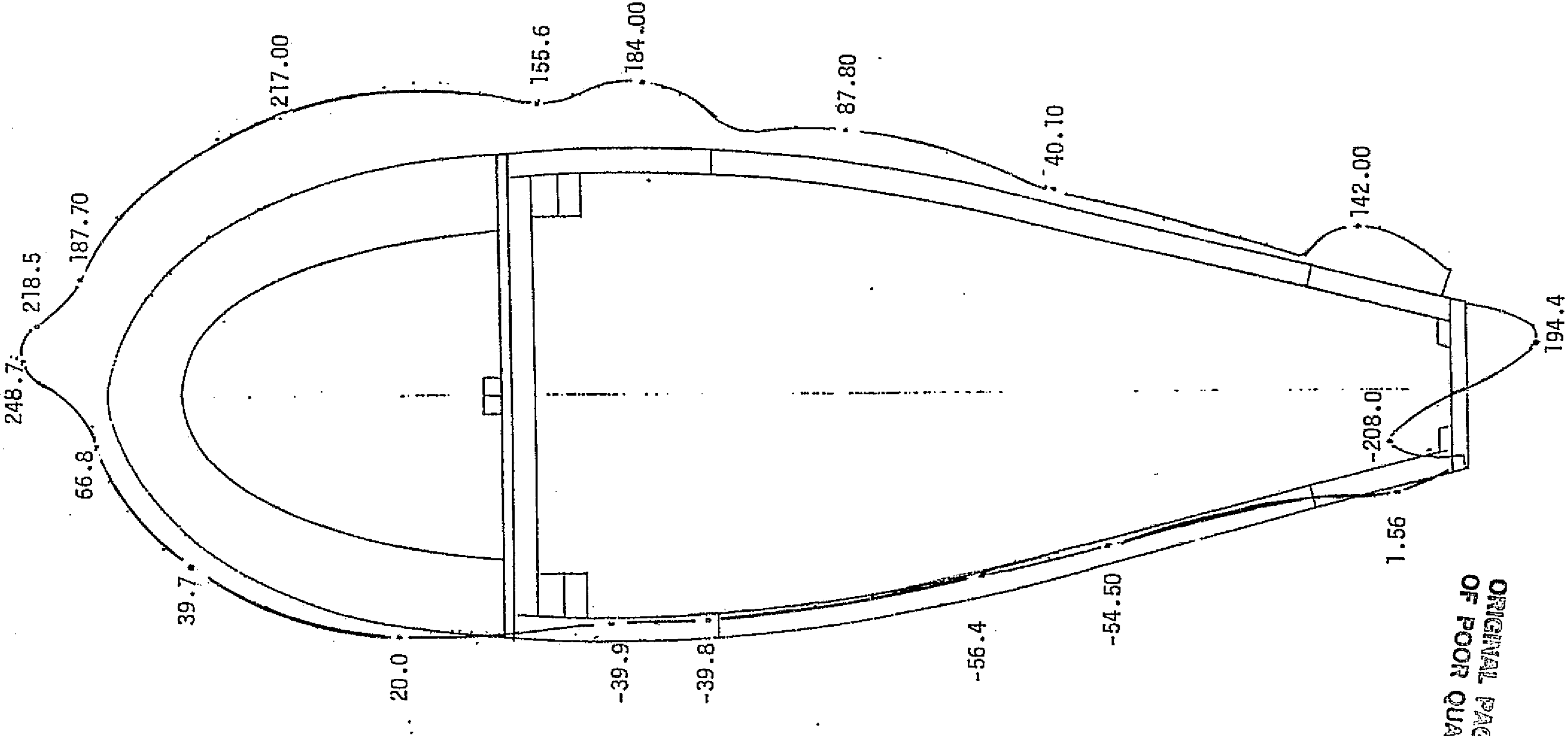

Figure 18. Finer-Mesh Analysis--Thermal Stresses in ζ Direction, Blade Section in Horizontal Position

Appendix

Computer Programs and Output Examples

```
C|<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C|                                                                <>
C|              THIS PROGRAM GENERATES THE GRIDS FOR ANY GIVEN    <>
C|              REGION                                            <>
C|              TRAINGULAR FINITE ELEMENT                         <>
C|                                                                <>
C|<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
C
      DIMENSION  NOO(2500,6),IRR(500)
      DIMENSION XP(500),YP(500),XRG(9),YRG(9),N(8),NDN(8),XC(21,21),
     1JT(74,4),ICOMP(4,4),NN(21,21),NNRB(74,4,21),XE(3000),YE(3000),
     1NE(3000),NR(4),LB(3),TITLE(10),IIRO(90),IICO(90),
     2NOU(3000),NOUK(3000),YC(21,21)
      REAL N
      DATA NBW/0/,NB/0/,NEL/0/
      DATA ICOMP/-1,1,1,-1,1,-1,-1,1,1,-1,-1,1,-1,1,1,-1/
      DATA IN/5/,IO/6/
      DATA  IP /11/
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
C                             FINITE ELEMENT GRID GENERATION PROGRAM
C
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
C     TITLE=AN IDENTIFICATION STATEMENT
C     INRG=THE NUMBER OF REGIONS ORIGINALLY DEFINED
C        (CAN SPECIFY A MAX OF 20 REGIONS)
C     INBP=THE NUMBER OF BOUNDARY POINTS OR GLOBAL POINTS ORIGINALLY DEF
C        (MUST HAVE 8 IN EACH REGION)
C     IPCH=0 IF ELEMENT DATA IS NOT TO BE PUNCHED
C     IPCH=1 IF ELEMENT DATA IS TO BE PUNCHED
C     XP(I)=THE X COORDINATE OF EACH OF THE ORIGINAL BOUNDARY POINTS
C     YP(I)=THE Y COORDINATE OF EACH OF THE ORIGINAL BOUNDARY POINTS
C     NRG=THE REGION NUMBER
C     JT(NRG,J)=THE REGION CONNECTIVITY DATA
C     NROWS=THE NUMBER OF ROWS OF NODES IN A REGION
C     NCOL=THE NUMBER OF COLUMNS OF NODES IN A REGION
C        (CAN SPECIFY A MAX OF 21 ROWS AND 21 COLUMNS IN A GIVEN REGION)
C     NDN(I)=THE GLOBAL NODE NUMBERS ORIGINALLY DEFINED IN A GIVEN REGIO
C
C
C
  100 FORMAT(10A4)
101   FORMAT(3I3)
  102 FORMAT(8F6.2)
103   FORMAT(5I3,2A4)
1113  FORMAT(1X,5I10)
  104 FORMAT(////1X,10A4//1X,18HGLOBAL COORDINATES //1X,
     130HNUMBER      X COORD      Y COORD   )
  105 FORMAT(2X,I3,7X,F7.4,5X,F7.4)
  106 FORMAT(//1X,17HCONNECTIVITY DATA/1X,41HREGION     SIDE    1      2
     1     3      4  )
  107 FORMAT(2X,I3,14X,4(I2,5X))
```

```
  108 FORMAT(11I3)
  109 FORMAT(///1X,12H***  REGION ,I3,6H   ***//10X,I2,5H ROWS,10X,I2
     1,8H COLUMNS//10X,21HBOUNDARY NODE NUMBERS,10X,8I5)
  110 FORMAT(//1X,19HREGION NODE NUMBERS/)
  111 FORMAT(1X,20I5)
  112 FORMAT(//5X,17HNEL  NODE NUMBERS,9X,4HX(1),8X,4HY(1),8X,4HX(2),8X,
     14HY(2),8X,4HX(3),8X,4HY(3)    )
  113 FORMAT(1X,5I5,3X,6F12.4)
  114 FORMAT(4I4,6F14.5)
  115 FORMAT(///1X,21HBANDWIDTH QUANTITY IS,I4,22H CALCULATED IN ELEMENT
     1,I4)
      READ(IN,100) TITLE
C     READ(IN,129)NRA,SEL,RMO,RA,RMI,SHR
129   FORMAT(I3,5F10.5)
      DO 400 IIM=1,1
      NEL=0
      NB=0
      READ(IN,101) INRG,INBP,IPCH
      WRITE(IO,116) INRG,INBP,IPCH
116   FORMAT(1X,3I3)
      READ(IN,102) (XP(I),I=1,INBP)
      WRITE(IO,102) (XP(I),I=1,INBP)
      READ(IN,102) (YP(I),I=1,INBP)
      WRITE(IO,102) (YP(I),I=1,INBP)
      DO 1 I=1,INRG
      READ(IN,103) NRG,(JT(NRG,J),J=1,4) ,IRR(I)
      WRITE(IO,117) NRG,(JT(NRG,J),J=1,4),IRR(I)
117   FORMAT(//,1X,5I3,2A4)
  1   CONTINUE
C     WRITE(IO,104) TITLE
      IF(IIM.EQ.2)GO TO 401
      WRITE(IP,100)TITLE
C     WRITE(IP,129)NRA,SEL,RMO,RA,RMI,SHR
401   WRITE(IO,105) (I,XP(I),YP(I),I=1,INBP)
C%%   WRITE(IO,106)
      DO 2 I=1,INRG
C%%   WRITE(IO,107) I,(JT(I,J),J=1,4)
 2    CONTINUE
C
C***********************************************************************
C
C     LOOP ON THE REGIONS IN ORDER TO GENERATE THE ELEMENTS
C
C***********************************************************************
C
      DO 22 KK=1,INRG
      READ(IN,108) NRG,IIRO(KK),IICO(KK),(NDN(I),I=1,8)
      WRITE(IO,109) NRG, IIRO(KK),IICO(KK),(NDN(I),I=1,8)
      NROWS=IIRO(KK)
      NCOL=IICO(KK)
C
C     GENERATION OF THE ELEMENT NODAL COORDINATES
C
      DO 3 I=1,8
```

```
      II=NDN(I)
      XRG(I)=XP(II)
    3 YRG(I)=YP(II)
      XRG(9)=XRG(1)
      YRG(9)=YRG(1)
      TR=NROWS-1
      DETA=2.0/TR
      TR=NCOL-1
      DSI=2.0/TR
      DO 4 I=1,NROWS
      TR=I-1
      ETA=1.0-TR*DETA
      DO 4 J=1,NCOL
      TR=J-1
      SI=-1.0+TR*DSI
      N(1)=-.25*(1.0-SI)*(1.0-ETA)*(SI+ETA+1.0)
      N(2)=.50*(1.0-SI**2)*(1.0-ETA)
      N(3)=.25*(1.0+SI)*(1.0-ETA)*(SI-ETA-1.0)
      N(4)=.50*(1.0+SI)*(1.0-ETA**2)
      N(5)=.25*(1.0+SI)*(1.0+ETA)*(SI+ETA-1.0)
      N(6)=.50*(1.0-SI**2)*(1.0+ETA)
      N(7)=.25*(1.0-SI)*(1.0+ETA)*(ETA-SI-1.0)
      N(8)=.50*(1.0-SI)*(1.0-ETA**2)
      XC(I,J)=0.0
      YC(I,J)=0.0
      DO 4 K=1,8
      XC(I,J)=XC(I,J)+XRG(K)*N(K)
      YC(I,J)=YC(I,J)+YRG(K)*N(K)
    4 CONTINUE
C
C     GENERATION OF THE REGION NODE NUMBERS
C
      KN1=1
      KS1=1
      KN2=NROWS
      KS2=NCOL
      DO 11 I=1,4
      NRT=JT(NRG,I)
      IF(NRT.EQ.0.OR.NRT.GT.NRG) GO TO 11
      DO 5 J=1,4
    5 IF(JT(NRT,J).EQ.NRG) NRTS=J
      K=NCOL
      IF(I.EQ.2.OR.I.EQ.4) K=NROWS
      JL=1
      JK=ICOMP(I,NRTS)
      IF(JK.EQ.-1) JL=K
      DO 10 J=1,K
      GO TO (6,7,8,9),I
    6 NN(NROWS,J)=NNRB(NRT,NRTS,JL)
C       WRITE(6,7000)NN(NROWS,J)
      KN2=NROWS-1
      GO TO 10
    7 NN(J,NCOL)=NNRB(NRT,NRTS,JL)
C       WRITE(6,7001)NN(J,NCOL)
```

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```
 7000   FORMAT(//' STATION  2 ' , I9/)
 7001   FORMAT(//' STATION  1 ' , I9/)
 7002   FORMAT(//' STATION  3 ' , I9/)
 7003   FORMAT(//' STATION  4 ' , I9/)
      KS2=NCOL-1
      GO TO 10
    8 NN(1,J)=NNRB(NRT,NRTS,JL)
C     WRITE(6,7004)NRT,NRTS,JL
7004   FORMAT(//' NRT=',I9/'  NRTS =',I9/'  JL =',I9)
C     WRITE(6,7002)NN(1,J)
      KN1=2
      GO TO 10
    9 NN(J,1)=NNRB(NRT,NRTS,JL)
C     WRITE(6,7003)NN(J,1)
      KS1=2
   10 JL=JL+JK
   11 CONTINUE
      IF(KN1.GT.KN2) GO TO 16
      IF(KS1.GT.KS2) GO TO 16
      DO 12 I=KN1,KN2
      DO 12 J=KS1,KS2
      NB=NB+1
C     WRITE(IO,777)NB
   12 NN(I,J)=NB
777   FORMAT(////'    NB =   ',I6)
C
C     STORAGE OF THE BOUNDARY NODE NUMBERS
C
      DO 13 I=1,NCOL
      NNRB(NRG,1,I)=NN(NROWS,I)
   13 NNRB(NRG,3,I)=NN(1,I)
      DO 14 I=1,NROWS
      NNRB(NRG,2,I)=NN(I,NCOL)
   14 NNRB(NRG,4,I)=NN(I,1)
C
C     OUTPUT OF THE REGION NODE NUMBERS
C
      WRITE(IO,110)
      DO 15 I=1,NROWS
      WRITE(IO,111) (NN(I,J),J=1,NCOL)
 15    CONTINUE
C
C     DIVISION INTO TRIANGULAR ELEMENTS
C
 16   CONTINUE
      WRITE(IO,112)
      K=1
      DO 17 I=1,NROWS
      DO 17 J=1,NCOL
      XE(K)=XC(I,J)
      YE(K)=YC(I,J)
      NE(K)=NN(I,J)
   17 K=K+1
      L=NROWS-1
```

```
      DO 21 I=1,L
      DO 21 J=2,NCOL
      DIAG1=SQRT((XC(I,J)-XC(I+1,J-1))**2+(YC(I,J)-YC(I+1,J-1))**2)
      DIAG2=SQRT((XC(I+1,J)-XC(I,J-1))**2+(YC(I+1,J)-YC(I,J-1))**2)
      NR(1)=NCOL*I+J-1
      NR(2)=NCOL*I+J
      NR(3)=NCOL*(I-1)+J
      NR(4)=NCOL*(I-1)+J-1
      DO 21 IJ=1,2
      NEL=NEL+1
      IF((DIAG1/DIAG2).GT.1.02) GO TO 18
      J1=NR(1)
      J2=NR(IJ+1)
      J3=NR(IJ+2)
      GO TO 19
   18 J1=NR(IJ)
      J2=NR(IJ+1)
      J3=NR(4)
   19 LB(1)=IABS(NE(J1)-NE(J2))+1
      LB(2)=IABS(NE(J2)-NE(J3))+1
      LB(3)=IABS(NE(J1)-NE(J3))+1
      DO 20 IK=1,3
      IF(LB(IK).LE.NBW) GO TO 20
      NBW=LB(IK)
      NELBW=NEL
   20 CONTINUE
       IF( KK . NE . 46 ) GO TO 888
C       WRITE(6,666) J3 , NE(J3)
 666   FORMAT(///// '  J3 = ',I9,' NE(J3) = ' , I9 )
 888   CONTINUE
       WRITE(IO,113) KK,NEL,NE(J1),NE(J2),NE(J3),XE(J1),YE(J1),XE(J2),
     1 YE(J2),XE(J3),YE(J3)
      IF(IPCH.EQ.0) GO TO 21
      WRITE(IP,114) NEL,NE(J1),NE(J2),NE(J3),XE(J1),YE(J1),XE(J2),YE(J2)
     1,XE(J3),YE(J3)
      NOO(NEL,1)=KK
      NOO(NEL,2)=NEL
      NOO(NEL,3)=NE(J1)
      NOO(NEL,4)=NE(J2)
      NOO(NEL,5)=NE(J3)
      NOO(NEL,6)=IRR(KK)
   21 CONTINUE
   22 CONTINUE
      WRITE(IO,115) NBW,NELBW
      DO 95 IB=1,1000
95    NOU(IB)=0
C%%   WRITE(IO,35)
35    FORMAT(///,10X,'**** BOUNDARY NODE NUMBERS ****')
40    FORMAT(22I3)
      DO 30 I=1,INRG
C%%   WRITE(IO,34)I,IIRO(I),IICO(I)
34    FORMAT(/3X,'REGION',I2,3X,I2,1X,'ROWS',3X,I2,1X,'COLUMNS')
      DO 30 II=1,4
        NRT=JT(I,II)
```

```
        IF(NRT.GT.0)GO TO 30
        K=IICO(I)
        IF(II.EQ.2.OR.II.EQ.4)K=IIRO(I)
C%%     WRITE(IO,33)II,(NNRB(I,II,III),III=1,K)
33      FORMAT(1X,'SIDE',I2,/,3X,15I4)
      DO 90 III=1,K
      NII=NNRB(I,II,III)
90    NOU(NII)=1
30     CONTINUE
      IKK=1
      DO 91 IB=1,700
      IF(NOU(IB).EQ.0)GO TO 91
      NOUK(IKK)=IB
      IKK=IKK+1
91    CONTINUE
      IKK=IKK-1
      WRITE(IP,94)IKK
94    FORMAT(/50X,I4,46X)
      WRITE(IP,92)(NOUK(I),I=1,IKK)
C%%   WRITE(IO,93)(NOUK(I),I=1,IKK)
92    FORMAT(20I5)
93    FORMAT(15I4)
      DO 333 I=1,NEL
      WRITE(IP,575)( NOO(I,J),J=1,6)
      WRITE(15,575)( NOO(I,J),J=1,6)
C%%   WRITE(IO,575)( NOO(I,J),J=1,6)
 333  CONTINUE
 575  FORMAT(5I5,A4)
 576  FORMAT(10X,5I10,10X,A10)
400   CONTINUE
       STOP
       END
//*
//*==================================================================¢!
//*                                                                  ¢!
//*   B A N D W I D T H   R E D U C T I O N   P R O G R A M          ¢!
//*                                                                  ¢!
//*==================================================================¢!
//*                                                                  ¢!
C
      COMMON/AAA/ NOO(2500,6),NTT(80)
      COMMON/BBB/ X(3,2000),Y(3,2000),NBO(1000),TITLE(10)
      COMMON/CCC/ NODES,LMENTS,JT(12000),MEMJT(24000),JMEM(3000),
     $JNT(3000),IDIFF,MINMAX
      DATA IN/11/,IO/6/,IP/12/
C
      READ (IN,100)TITLE
      WRITE(IP,100)TITLE
100   FORMAT(10A4)
122   FORMAT(I3,5F10.5)
      J =1
      JJ=0
150   READ(IN,17)(JT(3000*(I-1)+J),I=1,3),(X(I,J),Y(I,J),I=1,3)
      JT(9000+J)=0
```

```
      NODES=MAX0(JT(J),JT(3000+J),JT(6000+J),JJ)
      JJ=NODES
      IF(JT(3000+J).EQ.0)GO TO 152
      J=J+1
      GO TO 150
152   LMENTS=J-1
      NODES=JJ
  12    FORMAT(//,5X,15HNUMBER OF NODES,I4,15X,
     1'NUMBER OF ELEMENTS   ',I4,//)
      WRITE(IO,105)TITLE
105   FORMAT(//,1X,20A4,//)
      WRITE(IO,12)NODES,LMENTS
      WRITE(IO,13)
13    FORMAT(//,3X,18HNEL  JT1  JT2  JT3,10X,4HX(1),8X,
     $4HY(1),8X,4HX(2),8X,4HY(2),8X,4HX(3),8X,4HY(3))
17    FORMAT(4X,3I4,6F14.5)
      DO 10 J=1,LMENTS
C     WRITE(IO,11)J,(JT(3000*(I-1)+J),I=1,3),(X(I,J),Y(I,J),I=1,3)
11    FORMAT(1X,4I5,3X,6F12.4)
10    CONTINUE
      READ(IN,300)IBO
300   FORMAT(50X,I4,46X)
      READ(IN,301)(NBO(I),I=1,IBO)
      WRITE(IO,302)
      DO 333  I=1,LMENTS
      READ (IN,444)(NOO(I,J),J=1,6)
 333  CONTINUE
C     WRITE(IO,303)(NBO(I),I=1,IBO)
302   FORMAT(//,'  *** BOUNDARY NUMBERS ***')
      CALL SETUP
      NTBAN=IDIFF+1
      WRITE(IO,202)NTBAN
202   FORMAT(//,2X,25HTHE ORIGINAL BANDWIDTH IS,I4,//)
      CALL OPTNUM
      IF(IDIFF.LE.MINMAX)GO TO 115
      MIBAN=MINMAX+1
      WRITE(IO,198)
198   FORMAT(1H1///,1X,5(3HOLD,3X,3HNEW,7X),/,1X,
     $5(4HNODE,2X,4HNODE,6X))
      WRITE(IO,200)(J,JNT(J),J=1,NODES)
      WRITE(7,200)(J,JNT(J),J=1,NODES)
200   FORMAT(5(I5,1X,I5,5X))
      WRITE(IO,13)
      DO 180 J=1,LMENTS
      DO 555 II=1,3
      III=II+2
 555  NOO(J,III)=JNT(JT(3000*(II-1)+J))
C
180   CONTINUE
C     WRITE(IO,11)J,(JNT(JT(3000*(I-1)+J)),I=1,3),
C    $(X(I,J),Y(I,J),I=1,3)
      WRITE(IO,201)MIBAN
201   FORMAT(//,2X,'THE NEW BANDWIDTH IS',I3,/)
      WRITE(IP,310)NODES,LMENTS,MIBAN
```

```
      DO 181 J=1,LMENTS
181   WRITE(IP,18)J,(JNT(JT(3000*(I-1)+J)),I=1,3),(X(I,J),
     $Y(I,J),I=1,3)
18    FORMAT(4I5,6F10.4)
      WRITE(IO,302)
      WRITE(IP,300)IBO
      WRITE(IP,301)(JNT(NBO(I)),I=1,IBO)
C     WRITE(IO,303)(JNT(NBO(I)),I=1,IBO)
303   FORMAT(15I4)
      GO TO 117
115   CONTINUE
      WRITE(IO,101)
117   CONTINUE
101   FORMAT(///,2X,'THE ORIGINAL BANDWIDTH IS MININMUM')
      WRITE(IP,310)NODES,LMENTS,NTBAN
310   FORMAT(3I5)
      DO 190 J=1,LMENTS
 190  WRITE(IP,18)J,(JT(3000*(I-1)+J),I=1,3),
     1(X(I,J),Y(I,J),I=1,3)
      WRITE(IP,300)IBO
      WRITE(IP,301)(NBO(I),I=1,IBO)
301   FORMAT(20I5)
C--------------------------C!
 444  FORMAT(5I5,A4)
      LLL = NOO(1,6)
C
      LOL=0
      MMM=0
      NNN=1
      DO 666 II=1,LMENTS
      IF ( LLL.EQ.NOO(II,6) )GO TO 1888
      NNN=NNN-1
      LOL=LOL+NNN
      MMM=MMM+1
      NTT(MMM)=LOL
C     WRITE(IO,888) NNN,NTT(MMM)
      LLL=NOO(II,6)
      NNN=1
 1888 CONTINUE
C     WRITE(IO,777)NNN,(NOO(II,J),J=1,6),(X(I,II),Y(I,II),I=1,3)
      IF (II. NE . LMENTS) GO TO 1889
      LOL=LOL+NNN
      MMM=MMM+1
      NTT(MMM)=LOL
C     WRITE(IO,888) NNN,NTT(MMM)
 1889 NNN=NNN+1
 666  CONTINUE
C
 777  FORMAT(4X,6I6,4X,A8,6F12.5)
 888  FORMAT(//'  NUMBER OF ELEMENTS IN THIS REGION =',2I10/)
400   CONTINUE
C
C-------------------------------------------------
C-------------------------------------------------
```

```
      STOP
      END
       SUBROUTINE OPTNUM
C
      DIMENSION NEWJT(3000),JOINT(3000)
      COMMON/AAA/ NOO(1500,6),NTT(80)
      COMMON/BBB/ X(3,2000),Y(3,2000),NBO(1000),TITLE(10)
      COMMON/CCC/ NODES,LMENTS,JT(12000),MEMJT(24000),JMEM(3000),
     $JNT(3000),IDIFF,MINMAX
      MINMAX=IDIFF
      DO 60 IK=1,NODES
      DO 20 J =1,NODES
      JOINT(J)=0
20    NEWJT(J)=0
      MAX=0
      I=1
      NEWJT(1)=IK
      JOINT(IK)=1
      K=1
30    K4=JMEM(NEWJT(I))
      IF(K4.EQ.0)GO TO 45
      JSUB=(NEWJT(I)-1)*8
      DO 40 JJ=1,K4
      K5=MEMJT(JSUB+JJ)
      IF(JOINT(K5).GT.0)GO TO 40
      K=K+1
      NEWJT(K)=K5
      JOINT(K5)=K
      NDIFF=IABS(I-K)
      IF(NDIFF.GE.MINMAX) GO TO 60
      IF(NDIFF.GT.MAX)MAX=NDIFF
40    CONTINUE
      IF(K.EQ.NODES) GO TO 50
45    I=I+1
      GO TO 30
50    MINMAX=MAX
      DO 55 J=1,NODES
55    JNT(J)=JOINT(J)
60    CONTINUE
      RETURN
       END
      SUBROUTINE SETUP
      COMMON/AAA/ NOO(1500,6),NTT(80)
      COMMON/BBB/ X(3,2000),Y(3,2000),NBO(1000),TITLE(10)
      COMMON/CCC/ NODES,LMENTS,JT(12000),MEMJT(24000),JMEM(3000),
     $JNT(3000),IDIFF,MINMAX
      IDIFF=0
      DO 15 J=1,NODES
15    JMEM(J)=0
      DO 60 J=1,LMENTS
      DO 50 I=1,4
      JNTI=JT(3000*(I-1)+J)
      IF(JNTI.EQ.0) GO TO 60
      JSUB=(JNTI-1)*8
```

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```
      DO 40 II=1,4
      IF(II.EQ.I) GO TO 40
      JJT=JT(3000*(II-1)+J)
      IF(JJT.EQ.0) GO TO 50
      MEM1=JMEM(JNTI)
      IF(MEM1.EQ.0) GO TO 30
      DO 20 III=1,MEM1
      IF(MEMJT(JSUB+III).EQ.JJT) GO TO 40
20    CONTINUE
30    JMEM(JNTI)=JMEM(JNTI)+1
      MEMJT(JSUB+JMEM(JNTI))=JJT
      IF(IABS(JNTI-JJT).GT.IDIFF)IDIFF=IABS(JNTI-JJT)
40    CONTINUE
50    CONTINUE
60    CONTINUE
      RETURN
      END
C
C
C
C
C*******************************************************************
C                                                                  <>
C&1B                                   H E A T ... 1        ......<>
C
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C                                                                  <>
      REAL KXX,KXXX
      DIMENSION    TITLE(10) ,NT1(11),NT2(80)
      DIMENSION NS(3),T(3)
      DIMENSION ISIDE(2),ICON(2),PHI(3)
      DIMENSION  CFV(6),NODNUM(6)
C
      INTEGER NP,IER,N
      REAL*8 Z(482),R(482),AREAE(752),X(3),Y(3),DDT,TIME,TDT
     2 ,X1,X2,X3,Y1,Y2,Y3,COF,THSTF(482,35),THCAP(482,35)
      COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3)
      REAL*8   ZZ(482,35),WK(8694),F,EF
      COMMON / SOLVEQ / F(482,1),EF(752)
      REAL *8 KZETA,KETA,RHOCP,BETA
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
C
      DATA     IN/12/,IO/6/
C     DATA NT1/343,347,351,355,359,363,367,371,375,379,383/
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
C  DEFINITION OF THE CONTROL PARAMETERS
C        AREAE( NE ) : ARRAY CONTAINS AREA OF EACH ELEMENTS
C        R     ( NE*3): ARRAY CONTAINS THE X-COORDINATES OF EACH ELEMENT
C        Z     ( NE*3): ARRAY CONTAINS THE Y-COORDINATES OF EACH ELEMENT
C        T     ( 3 )  : ARRAY CONTAINS THE TEMP. OF THE ELEMENT'S THREE
```

```
C                      NODES.
C        TOLD ( NE*3): ARRAY  COPIES THE T(3) ARRAY FOR EACH ELEMENT
C     NE   = NUMBER OF ELEMENTS
C     NP   = NUMBER OF GLOBAL TEMPERATURES
C     NBW  = BAND WIDTH
C     H    = CONVECTION COEFFICIENT
C     TINF = AMBIENT AIR TEMP.
C
C
C
C
C  INPUT OF THE TITLE CARD AND THE CONTROL PARAMETERS
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
      TINF =10.00
      REWIND 12
C.........................................................
      READ(IN,3)    TITLE
C     WRITE (IO,4 ) TITLE
      READ(IN,2)     NP,NE,NBW
      NBW=NBW+17
      WRITE(IO,1102) NP,NE,NBW
C.........................................................
    1 FORMAT(4I5,6F10.4)
    2 FORMAT(3I5)
    3 FORMAT(10A4)
    4 FORMAT(1H1,///1X,10A4)
1102  FORMAT(1X,3I6)
C
C........................................
C
C  OUTPUT OF TITLE AND DATA HEADINGS
C----------------------------------------
   44 FORMAT(1H1,////1X,20A4//1X,5HKXX =,F7.1,10X,5HKYY = ,F7.1/1X,
     121HCONVECTION COEFF(1) =,F7.1,3X,21HCONVECTION COEFF(2) =,F7.1/,
     21X,15HFLUID TEMP(1) =,F7.1,3X,15HFLUID TEMP(2) =,F7.1//,1X,
     317HNEL   NODE NUMBER,6X,4HX(1),6X,4HY(1),6X,4HX(2),6X,4HY(2),
     46X,4HX(3),6X,4HY(3)  )
C**********
C  ASSEMBLYING OF THE GLOBAL STIFFNESS MATRIX AND GLOBAL FORCE MATRIX
C**********
C
C  INPUT AND ECHO PRINT OF ELEMENT DATA
C
C.........................................................
C        WRITE(6,604)
 604    FORMAT(1H1,/////)
C        WRITE(6,304)
 304  FORMAT('  T(1)     T(2)       T(3)
     1  ISIDE(1)  ISIDE(2)    '/)
 1061  FORMAT(6F10.3,2I10)
  11   FORMAT(' ',3F10.3,2I10)
C      WRITE(6,1107)
C      WRITE(6,1108)
```

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C
C      NE :  TOTAL  NUMBER OF ELEMENTS
C
C..IN:12 ........................MAIN  LOOP ...................
       T(1)=10.
       T(2)=10.
       T(3)=10.
       DO 180 I=1,NE
       H(I)=0.001D0
       ISIDEH(I,1)=0
       ISIDEH(I,2)=0
180    CONTINUE
      DO 178 JJ=1,90
      N=2*JJ
      ISIDEH(N,1)=2
      ISIDEH(N,2)=0
      H(N)=5.D0
178   CONTINUE
C
C     BIRCH LOOP.................
C
      DO 1001 J=1,280
      KZETA(J)=.0924
      KETA(J)=.0836
1001  CONTINUE
C
C     DOUGLAS FIR LOOP ...........
C
      DO 1002 J=281, 302
      KZETA(J)=.0754
      KETA(J)=.06820
1002  CONTINUE
      DO 1010 J=351,638
      KZETA(J)=.0754
      KETA(J)=.0682
1010  CONTINUE
      DO 1015 J=687,752
      KZETA(J)=.0754
      KETA(J)=.0682
1015  CONTINUE
C
C    PAPER LOOP.............
C
      DO 1020 J=303,350
      KZETA(J)=.011161
      KETA(J)=.011161
1020  CONTINUE
      DO 1111 J =639,686
      KZETA(J)=.011161
      KETA(J)=.011161
1111  CONTINUE
C
C    LOOP ON THE REGIONS............
C
```

```
      DO 7 KK=1,NE
      IF(KK.GE.1.AND.KK.LE.22) BETA(KK)=-.2618
      IF(KK.GE.23.AND.KK.LE.34) BETA(KK)=-.15707
      IF(KK.GE.35.AND.KK.LE.58) BETA(KK)=0.0
      IF(KK.GE.59.AND.KK.LE.66) BETA(KK)=.38394
      IF(KK.GE.67.AND.KK.LE.74) BETA(KK)=.17452
      IF(KK.GE.75.AND.KK.LE.82) BETA(KK)=1.22164
      IF(KK.GE.83.AND.KK.LE.90) BETA(KK)=.69808
      IF(KK.GE.91.AND.KK.LE.98) BETA(KK)=2.4433
      IF(KK.GE.99.AND.KK.LE.106) BETA(KK)=1.91972
      IF(KK.GE.107.AND.KK.LE.114) BETA(KK)=2.9668
      IF(KK.GE.115.AND.KK.LE.122) BETA(KK)=2.7574
      IF(KK.GE.123.AND.KK.LE.146) BETA(KK)=3.14136
      IF(KK.GE.147.AND.KK.LE.158) BETA(KK)=3.29843
      IF(KK.GE.159.AND.KK.LE.202) BETA(KK)=3.40314
      IF(KK.GE.203.AND.KK.LE.214) BETA(KK)=3.29843
      IF(KK.GE.215.AND.KK.LE.230) BETA(KK)=3.14136
      IF(KK.GE.231.AND.KK.LE.246) BETA(KK)=0.0
      IF(KK.GE.247.AND.KK.LE.258) BETA(KK)=-.15707
      IF(KK.GE.259.AND.KK.LE.326) BETA(KK)=-.2618
      IF(KK.GE.327.AND.KK.LE.350) BETA(KK)=-.15707
      IF(KK.GE.351.AND.KK.LE.430) BETA(KK)=0.0
      IF(KK.GE.431.AND.KK.LE.438) BETA(KK)=.38394
      IF(KK.GE.439.AND.KK.LE.446) BETA(KK)=.17452
      IF(KK.GE.447.AND.KK.LE.454) BETA(KK)=.38394
      IF(KK.GE.455.AND.KK.LE.462) BETA(KK)=.17452
      IF(KK.GE.463.AND.KK.LE.470) BETA(KK)=1.2216
      IF(KK.GE.471.AND.KK.LE.478) BETA(KK)=.69808
      IF(KK.GE.479.AND.KK.LE.486) BETA(KK)=1.2216
      IF(KK.GE.487.AND.KK.LE.494) BETA(KK)=.69808
      IF(KK.GE.495.AND.KK.LE.502) BETA(KK)=2.4433
      IF(KK.GE.503.AND.KK.LE.510) BETA(KK)=1.91972
      IF(KK.GE.511.AND.KK.LE.518) BETA(KK)=2.4433
      IF(KK.GE.519.AND.KK.LE.526) BETA(KK)=1.91972
      IF(KK.GE.527.AND.KK.LE.534) BETA(KK)=2.9668
      IF(KK.GE.535.AND.KK.LE.542) BETA(KK)=2.7574
      IF(KK.GE.543.AND.KK.LE.550) BETA(KK)=2.9668
      IF(KK.GE.551.AND.KK.LE.558) BETA(KK)=2.7574
      IF(KK.GE.559.AND.KK.LE.638) BETA(KK)=3.14136
      IF(KK.GE.639.AND.KK.LE.662) BETA(KK)=3.29843
      IF(KK.GE.663.AND.KK.LE.708) BETA(KK)=3.40314
      IF(KK.GE.709.AND.KK.LE.752) BETA(KK)=0.0

      READ(IN,1) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3)
      WRITE(6,121) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3),BETA(KK)
C     WRITE(7,122) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3),BETA(KK)
 121  FORMAT(4I5,7F10.4)
 122  FORMAT(4I4,7F8.4)
C
C  DIMENSION IN FEET...
        X1=X(1)
        X2=X(2)
        X3=X(3)
        Y1=Y(1)
```

```
       Y2=Y(2)
       Y3=Y(3)
C
      X ( 1 )= X(1) /12.0D0
      X ( 2 )= X(2) /12.0D0
      X ( 3 )= X(3) /12.0D0
      Y ( 1 )= Y(1) /12.0D0
      Y ( 2 )= Y(2) /12.0D0
      Y ( 3 )= Y(3) /12.0D0
C
       T1=T(1)
       T2=T(2)
       T3=T(3)
 1107  FORMAT(1H1,///20X
     *  ,'    T(1)      T(2)      T(3)    '
     *  ,' ISIDE(1)  ISIDE(2)    ')
 1108  FORMAT(' ',20X
     *  ,' -------  --------  --------  -------   -------    ------- '
     *  ,'---------')
C      WRITE(IO,11)T,ISIDEH(KK,1),ISIDEH(KK,2)
C
C
C
C      TOLD(NS(1))=T(1)
C      TOLD(NS(2))=T(2)
C      TOLD(NS(3))=T(3)
C      H : CONVECTION COEFFICIENT
C      WRITE(6,5152)KK,NS(1),NS(2),NS(3),TOLD(NS(1)),TOLD(NS(2)),
C     1  TOLD(NS(3)), H(KK),(ISIDE(JJ),JJ=1,2),
C     1  X1,Y1,X2,Y2,X3,Y3,NOT(KK,1),NOT(KK,6)
 5152 FORMAT(' ',4I5,3F10.3,F5.0,2I2,6F8.4,I5,A8)
C
       T(1)=T1
       T(2)=T2
       T(3)=T3
C
C  ECHO THE INPUT........
C     WRITE(IO,23) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3)
C    * , HH,RHO,CP,ISIDE,T
   23 FORMAT(1H0,I5,1X,3I5,2X,6(1X,F8.4),2X,2F5.0,F6.3,2X,2I3,
     *  2X,3F6.0)
C  CALCULATION OF THE CONDUCTION MATRIX
C
C    NPT (NE,3) : ARRAY STORES THE NODE NUMBERS FOR EACH ELEMENT
      NPT(KK,1) = NS(1)
      NPT(KK,2) = NS(2)
      NPT(KK,3) = NS(3)
      R(NS(1)) =  X(1)
      R(NS(2)) =  X(2)
      R(NS(3)) =  X(3)
      Z(NS(1)) =Y(1)
      Z(NS(2)) =Y(2)
      Z(NS(3)) =Y(3)
     AREAE(KK)=(X(2)*Y(3)-X(2)*Y(1)+X(3)*Y(1)-X(3)*Y(2)
```

```
     1  + X(1)*Y(2)-X(1)*Y(3))/2.0
C-----------------------------------------------------------¢!-------------¢!
C---------------------------------------------------------------------------¢!
C        WRITE(6,266)KK,X(1),Y(1),X(2),Y(2),X(3),Y(3),AREAE(KK)
 266    FORMAT(1H0,I5,6(1X,F8.4 ),2X,D14.7)
C       WRITE(6,319)KK,(T(I),I=1,3)
 319    FORMAT('  ELEMENT  NO.   ',I8,3F12.4)
   7    CONTINUE
C..................................END OF THE DO LOOP ........¢!
C       WRITE(6,264)(I,TOLD(I),I=1,NP)
 264    FORMAT(1H0,I5,E14.5,2X,I5,E14.5,2X,I5,E14.5,2X,I5,E14.5
     * ,2X,I5,E14.5,2X,I5,E14.5)
C
C ADD EXTERNALLY APPL. CONC. NODAL FORCES VECTOR TO EF VECTOR
         ID1=0
         INK=0
 202     READ(IN,203) NODNUM,CFV
 203     FORMAT(6I3,2X,6F10.5)
         ID=0
         DO 204 L=1,6
         IF( NODNUM(L).LE.0) GOTO 205
         ID=ID+1
         INODNU=NODNUM(L)
 204     EF(INODNU)=CFV(L)+EF(INODNU)
         GOTO 206
 205     INK=1
         IF(ID.EQ.0) GOTO 216
 206     IF(ID1.EQ.1)GOTO 222
         WRITE(IO,208)
 208     FORMAT(1H1,' NODE NUMBER ',10X,' GENERALIZED  NODAL FORCES ')
 222     WRITE(IO,207)(NODNUM(L),CFV(L),L=1,ID)
 207     FORMAT(1H0,6(I3,E14.5,2X))
         IF(INK.EQ.1)GOTO 216
         ID1=1
         GOTO 202
 216     CONTINUE
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
        JJJKNT=0
C
          CALL FORMTK (NE,NP,NBW)
          CALL FORMTF (NE,NP,NBW)
          CALL ASSMBL (NP,NBW,ZZ)
C         WRITE(6,9999)((ZZ(I,J),J=1,NBW),I=1,NP)
9999      FORMAT(2X,7G11.5)
C         WRITE(6,9988)(F(I,1),I=1,NP)
9988      FORMAT(2X,G11.5)
          CALL LEQT1B(ZZ,NP,17,17,NP,F,1,NP,0,WK,IER)
          JJJKNT=JJJKNT+1
          IF(JJJKNT.GE.1)GOTO 979
          GOTO 980
979       CONTINUE
980       CONTINUE
          WRITE(IO,666)
```

```
666       FORMAT(' NODE NO.',7X,'TEMPERATURE IN DEGREE  F',/)
          WRITE(6,787)(I,F(I,1),I=1,NP)
787       FORMAT( 2X,I5,10X,F15.8)
          WRITE(7,777)(F(I,1),I=1,NP)
777       FORMAT(9F8.4)
C
C
          STOP
          END
          SUBROUTINE FORMTK (NE,NP,NBW)
C***********************************************************************
C.......... FORM BANDED THERMAL CONDUCTANCE MATRIX
C
      IMPLICIT REAL*4(A-H,O-Z)
      REAL*8 KZETA,KETA,RHOCP,BETA
      REAL*8 BI,BJ,BK,CI,CJ,CK,COF,CON1,CON2,CON3
      REAL*8 RBAR,CON,LG,RCTL,ELKT(3,3),THSTF(482,35)
      REAL*8 A00,A11,A22,B00,B11,B22,C00,THCAP(482,35)
      REAL*8 Z(482),R(482),AREAE(752),X(3),Y(3),DDT,TIME,ATIM,P
      COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3)
       REAL*8    ZZ(482,35),F,B,FF,EF
      COMMON / SOLVEQ / F(482,1),EF(752)
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
C
C
C
C.......... INITIALIZE GLOBAL THERMAL STIFFNESS MATRIX
       IN=5
       IO=6
      DO 120 J=1,NBW
      DO 110 I=1,NP
      THSTF(I,J) = 0.D0
  110 CONTINUE
  120 CONTINUE
C
C
  130 NBAND = 0
      DO 899 J=1,NE
C      WRITE(6,788)KZETA(J),KETA(J),BETA(J)
788   FORMAT(3X,3F20.9)
899   CONTINUE
C
C         WRITE(6,7776)
 7776   FORMAT(' CONDUCTION MATRIX ELEMENTS ARE ',/)
      DO 230 N=1,NE
C<><><><><><>---------------------------------<><><><><><><><><><><><>
C
      II = NPT(N,1)
      JJ = NPT(N,2)
      KK = NPT(N,3)
      BI = Z(JJ)-Z(KK)
```

```
      BJ = Z(KK)-Z(II)
      BK = Z(II)-Z(JJ)
      CI = R(KK)-R(JJ)
      CJ = R(II)-R(KK)
      CK = R(JJ)-R(II)
      X(1) =R(II)
      X(2) =R(JJ)
      X(3) =R(KK)
      Y(1) =Z(II)
      Y(2) =Z(JJ)
      Y(3) =Z(KK)
C     WRITE(6,555)X(1),X(2),X(3),Y(1),Y(2),Y(3)
555   FORMAT(2X,6F12.6)
      ALPHA=BETA(N)
C     CON1=(KZETA(N)*(COS(BETA(N)))**2+KETA(N)*(SIN(BETA(N)))**2)
C    1/(4.*AREAE(N))
C     CON2=(KZETA(N)-KETA(N))*SIN(2.*BETA(N))/(4.*AREAE(N))
C     CON3=(KZETA(N)*(SIN(BETA(N)))**2+KETA(N)*(COS(BETA(N)))**2)
C    1/(4.*AREAE(N))
      CON1=(KZETA(N)*(COS(ALPHA))**2+KETA(N)*(SIN(ALPHA))**2)
     1/(4.*AREAE(N))
      CON2=(KZETA(N)-KETA(N))*SIN(2.*ALPHA)/(4.*AREAE(N))
      CON3=(KZETA(N)*(SIN(ALPHA))**2+KETA(N)*(COS(ALPHA))**2)
     1/(4.*AREAE(N))
C
C     WRITE(6,7999)CON1,CON2,CON3,AREAE(N)
7999  FORMAT(2X,3F10.3,2X,F10.7)
      ELKT(1,1) = (BI**2)*CON1+(CI**2)*CON3+(BI*CI)*CON2
      ELKT(1,2) = (BI*BJ)*CON1+(CI*CJ)*CON3+(BI*CJ)*CON2
      ELKT(1,3) = (BI*BK)*CON1+(CI*CK)*CON3+(BI*CK)*CON2
      ELKT(2,1) = (BI*BJ)*CON1+(CJ*CI)*CON3+(BJ*CI)*CON2
      ELKT(2,2) = (BJ**2)*CON1+(CJ**2)*CON3+(BJ*CJ)*CON2
      ELKT(2,3) = (BJ*BK)*CON1+(CJ*CK)*CON3+(BJ*CK)*CON2
      ELKT(3,1) = (BK*BI)*CON1+(CK*CI)*CON3+(BK*CI)*CON2
      ELKT(3,2) = (BK*BJ)*CON1+(CK*CJ)*CON3+(BK*CJ)*CON2
      ELKT(3,3) = (BK**2)*CON1+(CK**2)*CON3+(BK*CK)*CON2
        WRITE(6,*)N,H(N),( ISIDEH(N,J1),J1=1,2)
        DO 10 IQ=1,2
C       WRITE(6,7805)N,( ISIDEH(N,J1),J1=1,2)
 7805    FORMAT(' SIDE EXPOSED ',3I10)
        IF ( ISIDEH(N,IQ) . LE . 0 ) GO TO 240
        JQ = ISIDEH (N,IQ)
C        WRITE(IO,12) JQ,N
 12     FORMAT(1H0,' INSIDE',I3,3X,' OF ELEMENT',I5)
        KQ = JQ +1
        IF ( JQ.EQ . 3) KQ=1
        LG = DSQRT((X(KQ)-X(JQ))**2+(Y(KQ)-Y(JQ))**2)
        HL =H(N)*LG/6.
        WRITE(6,*) N,H(N),LG,HL
        IF(JQ.EQ.1) GO TO 20
        IF(JQ.EQ.2) GO TO 30
        IF(JQ.EQ.3) GO TO 40
        GO TO 10
 20     ELKT(1,1)= ELKT(1,1)+HL * 2.
```

```
        ELKT(2,2)= ELKT(2,2)+HL * 2.
        ELKT(1,2)= ELKT(1,2)+HL
        ELKT(2,1)=ELKT(2,1)+HL
        GO TO 10
C
 30     ELKT(2,2)= ELKT(2,2)+HL*2.
        ELKT(3,3)= ELKT(3,3)+HL*2.
        ELKT(2,3)= ELKT(2,3)+HL
        ELKT(3,2)=ELKT(3,2)+HL
        GO TO 10
C
 40     ELKT(1,1)= ELKT(1,1)+HL * 2.
        ELKT(3,3)= ELKT(3,3)+HL * 2.
        ELKT(1,3)= ELKT(1,3)+HL
        ELKT(3,1)=ELKT(3,1)+HL
 10     CONTINUE
C
C     WRITE(IO,2000)N,II,JJ,KK,X(1),Y(1),X(2),Y(2),X(3),Y(3),CONDTY(N),
C    1AREAE(N),RBAR,CON,ELKT(1,1),ELKT(1,2),ELKT(1,3),ELKT(2,2),
C    2ELKT(2,3),ELKT(3,3)
 2000 FORMAT(1H0,4I5,8G11.4,/21X,8G11.4)
C--------------------------------------------------------C!
C      S T O R E    I N   G L O B A L   M A T R I X      C!
C--------------------------------------------------------C!
 240   CONTINUE
C     WRITE( IO,266)N,X(1),Y(1),X(2),Y(2),X(3),Y(3),AREAE(N),NBAND
 266  FORMAT(1H0,I5,6(1X,F8.4),2X,D14.7,2X,I5)
C       WRITE(6,277)N,(( ELKT(I,J),J=1,3),I=1,3)
 277  FORMAT(' ',I5/ 3(3F25.6/))
      DO 220 LL=1,3
      I=NPT(N,LL)
      DO 210 MM=1,3
      J=NPT(N,MM)-I+18
      THSTF(I,J) =THSTF(I,J)+ELKT(LL,MM)
C      WRITE(6,7543)I,J,II,JH,NPT(N,J),NPT(N,I)
 7543 FORMAT(' ',6I8,    '******')
       IF (J.GT.NBAND) NBAND=J
 210  CONTINUE
 220  CONTINUE
  230 CONTINUE
C     WRITE(6,5050)((THSTF(I,J),J=1,NBW),I=15,20)
 5050 FORMAT(7G11.5)
C
C      WRITE (6,200) NBAND
 200  FORMAT(1H0,'  NBAND= ',I5)
C
C.......... END OF PROGRAM
C
C
      RETURN
      END
      SUBROUTINE FORMTF(NE,NP,NBW)
C
C      FORM THERMAL FORCE VECTOR
```

```
C
C
C
      REAL*8 ELF(3),LG,RCTL,COF,THCAP(482,35),THSTF(482,35)
      REAL*8 Z(482),R(482),AREAE(752),X(3),Y(3),DDT
      COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3)
      REAL*8   ZZ(482,35),F,EF,B,ELF1,ELF2,ELF3,FF,HLL
      COMMON / SOLVEQ / F(482,1),EF(752)
      REAL *8 KZETA,KETA,RHOCP,BETA
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
      REAL *8 QR(752),HL(752)
C     DATA PI/3.14159265D0/
          IO=6
         TINF = 0.D0
C
C
C      FOR EACH ELEMENT ,FORM THERMAL FORCE VECTOR
C
C          WRITE(6,9999)
 9999      FORMAT(' FORCE VECTORS ARE ',/)
          DO 110 I=1,NE
          EF(I)   = 0.D0
          QR(I)=0.0
 110      CONTINUE
          DO 1070 J=1,45
          N=2*J
          QR(N)=326.0
1070      CONTINUE
          DO 230 N=1,NE
          ELF(1)=0.D0
          ELF(2)=0.D0
          ELF(3)=0.D0
          II=NPT(N,1)
          JJ=NPT(N,2)
          KK=NPT(N,3)
          CI = R(KK)-R(JJ)
          CJ = R(II)-R(KK)
          CK = R(JJ)-R(II)
          X(1)=R(II)
          X(2)=R(JJ)
          X(3)=R(KK)
          Y(1)=Z(II)
          Y(2)=Z(JJ)
          Y(3)=Z(KK)
          DO 10 IQ=1,2
          IF(ISIDEH(N,IQ).LE.0)GO TO 240
          JQ=ISIDEH (N,IQ)
          KQ=JQ+1
          IF(JQ.EQ.3) KQ=1
          LG=DSQRT((X(KQ)-X(JQ))**2+ (Y(KQ)-Y(JQ))**2)
C         WRITE(6,999)LG
```

```
999        FORMAT(2X,F10.5)
          HL(N)=QR(N)+H(N)*TINF
          IF ( JQ.EQ.1)GO TO 20
          IF ( JQ.EQ.2)GO TO 30
          IF (JQ .EQ.3)GO TO 40
          GO TO 240
 20       ELF(1) =HL(N)*LG*.5+ELF(1)
          ELF(2) =HL(N)*LG*.5+ELF(2)
          GO TO 10
 30       ELF(2) =HL(N)*LG*.5+ELF(2)
          ELF(3) =HL(N)*LG*.5+ELF(3)
          GO TO 10
 40       ELF(1) =HL(N)*LG*.5+ELF(1)
          ELF(3) =HL(N)*LG*.5+ELF(3)
 10       CONTINUE
C
 240      EF(II)= EF(II)+ELF(1)
          EF(JJ)=EF(JJ) +ELF(2)
          EF(KK)=EF(KK) +ELF(3)
 707      FORMAT(' ',2I8,5F15.5)
C         IF(EF(II).EQ.0) GO TO 50
C         IF(EF(JJ).EQ.0) GO TO 50
C         IF(EF(KK).EQ.0) GO TO 50
C         GOTO 230
C50       WRITE(6,1999)N,II,JJ,KK,EF(II),EF(JJ),EF(KK)
1999      FORMAT(1H0,4I6,2X,3F10.4)
 230       CONTINUE
C          WRITE(IO,2000)(EF(I),I=1,NP)
 2000      FORMAT(2X,F10.4)
C           WRITE(IO,1000)
 1000      FORMAT(1H0,' LEAVING  FORMTF      IN TDHEAT ...1B')
           RETURN
           END
      SUBROUTINE ASSMBL (NP,NBW,ZZ)
C.......... ASSEMBLE MATRICES FOR RECURRENCE FORMULAS
       REAL *8 Z(482),R(482),AREAE(752)
      REAL*8 DDT,DT,THSTF(482,35),THCAP(482,35)
       COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1   ,THCAP,NPT(752,3)
       REAL*8   ZZ(482,35),F,EF,B,FF(15,1)
      COMMON / SOLVEQ / F(482,1),EF(752)
      REAL *8 KZETA,KETA,RHOCP,BETA
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)

       DO 150 I=1,NP
C
C.......... COEFFICIENT MATRIX
C
      DO 110 J=1,NBW
      ZZ(I,J) = THSTF(I,J)
  110 CONTINUE
C      WRITE(6,2000) (ZZ(I,J),J=12,26)
```

```
 2000  FORMAT(' ',6E9.5)
C
C.......... THERMAL LOAD VECTOR
C
      F(I,1) = EF(I)
C
  150 CONTINUE
C     WRITE(6,1313)(F(I,1),I=1,NP)
1313  FORMAT(' ',G11.5)
 1001 FORMAT (1H ,I3,11G11.5)
C
C.......... END OF PROGRAM
C
       RETURN
       END
```

```
C*********************************************************************
C                                                                    <>
C&1B                                  H E A T  ... 2      .......<>
C
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C                                                                    <>
      REAL KXX,KXXX
      DIMENSION    TITLE(10) ,NT1(11),NT2(80)
      DIMENSION NS(3),T(3)
      DIMENSION ISIDE(2),ICON(2),PHI(3)
      DIMENSION  CFV(6),NODNUM(6),FIJ(483,100),TIME(100)
C
      INTEGER NP,IER,N
      REAL*8 Z(483),R(483),AREAE(752),X(3),Y(3),DDT,TIME,TDT
     2 ,X1,X2,X3,Y1,Y2,Y3,COF,THSTF(483,18),THCAP(483,18),TOLD(483)
      COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3),TOLD
      REAL*8   ZZ(483,18),WK(10000),F,EF,MAX(500)
      COMMON / SOLVEQ / F(483),EF(752),ZZ
      REAL *8 KZETA,KETA,RHOCP,BETA
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
C
      DATA     IN/12/,IO/6/
C     DATA NT1/343,347,351,355,359,363,367,371,375,379,383/
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
C  DEFINITION OF THE CONTROL PARAMETERS
C         AREAE( NE ) : ARRAY CONTAINS AREA OF EACH ELEMENTS
C         R    ( NE*3): ARRAY CONTAINS THE X-COORDINATES OF EACH ELEMENT
C         Z    ( NE*3): ARRAY CONTAINS THE Y-COORDINATES OF EACH ELEMENT
C         T    ( 3 )  : ARRAY CONTAINS THE TEMP. OF THE ELEMENT'S THREE
C                       NODES.
C         TOLD ( NE*3): ARRAY  COPIES THE T(3) ARRAY FOR EACH ELEMENT
C      NE   = NUMBER OF ELEMENTS
C      NP   = NUMBER OF GLOBAL TEMPERATURES
C      NBW  = BAND WIDTH
C      H    = CONVECTION COEFFICIENT
C      TINF = AMBIENT AIR TEMP.
C
C
C
C
C  INPUT OF THE TITLE CARD AND THE CONTROL PARAMETERS
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C DELTA T: TIME INTERVAL FOR EACH ITERATION
      TDT=500.0
      DDT=TDT/3600.
      REWIND 12
C........................................................
      READ(IN,3)    TITLE
C     WRITE (IO,4 ) TITLE
      READ(IN,2)     NP,NE,NBW
```

```
      WRITE(IO,1102) NP,NE,NBW
C.........................................................
    1 FORMAT(4I5,6F10.4) .
    2 FORMAT(3I5)
    3 FORMAT(10A4)
    4 FORMAT(1H1,///1X,10A4)
1102  FORMAT(1X,3I6)
C
C....................................
C
C  OUTPUT OF TITLE AND DATA HEADINGS
C-----------------------------------------
   44 FORMAT(1H1,////1X,20A4//1X,5HKXX =,F7.1,10X,5HKYY = ,F7.1/1X,
     121HCONVECTION COEFF(1) =,F7.1,3X,21HCONVECTION COEFF(2) =,F7.1/,
     21X,15HFLUID TEMP(1) =,F7.1,3X,15HFLUID TEMP(2) =,F7.1//,1X,
     317HNEL   NODE NUMBER,6X,4HX(1),6X,4HY(1),6X,4HX(2),6X,4HY(2),
     46X,4HX(3),6X,4HY(3)  )
C*********
C  ASSEMBLYING OF THE GLOBAL STIFFNESS MATRIX AND GLOBAL FORCE MATRIX
C*********
C
C  INPUT AND ECHO PRINT OF ELEMENT DATA
C
C.........................................................
C        WRITE(6,604)
 604    FORMAT(1H1,/////)
C        WRITE(6,304)
 304  FORMAT('  T(1)     T(2)      T(3)
     1  ISIDE(1)  ISIDE(2)   '/)
 1061  FORMAT(6F10.3,2I10)
  11   FORMAT(' ',3F10.3,2I10)
C      WRITE(6,1107)
C      WRITE(6,1108)
C
C      NE :  TOTAL  NUMBER OF ELEMENTS
C
C..IN:12 .......................MAIN  LOOP ..................
       T(1)=10.
       T(2)=10.
       T(3)=10.
       DO 180 I=1,NE
       H(I)=0.0D0
       ISIDEH(I,1)=0
       ISIDEH(I,2)=0
180    CONTINUE
      DO 178 JJ=1,90
      N=2*JJ
      ISIDEH(N,1)=2
      ISIDEH(N,2)=0
      H(N)=5.D0
178   CONTINUE
C
C     BIRCH LOOP................
C
```

```
      DO 1001 J=1,280
      KZETA(J)=.0924
      KETA(J)=.0836
      RHOCP(J)=10.94246
1001  CONTINUE
C
C     DOUGLAS FIR LOOP ..........
C
      DO 1002 J=281, 302
      KZETA(J)=.0754
      KETA(J)=.0682
      RHOCP(J)=8.5488
1002  CONTINUE
      DO 1010 J=351,638
      KZETA(J)=.0754
      KETA(J)=.0682
      RHOCP(J)=8.5488
1010  CONTINUE
      DO 1015 J=687,752
      KZETA(J)=.0754
      KETA(J)=.0682
      RHOCP(J)=8.5488
1015  CONTINUE
C
C    PAPER LOOP............
C
      DO 1020 J=303,350
      KZETA(J)=.011161
      KETA(J)=.011161
      RHOCP(J)=8.1357
1020  CONTINUE
      DO 1111 J =639,686
      KZETA(J)=.011161
      KETA(J)=.011161
      RHOCP(J)=8.1357
1111  CONTINUE
C
C    LOOP ON THE REGIONS............
C
      DO 7 KK=1,NE
      IF(KK.GE.1.AND.KK.LE.22) BETA(KK)=-.2618
      IF(KK.GE.23.AND.KK.LE.34) BETA(KK)=-.15707
      IF(KK.GE.35.AND.KK.LE.58) BETA(KK)=0.0
      IF(KK.GE.59.AND.KK.LE.66) BETA(KK)=.38394
      IF(KK.GE.67.AND.KK.LE.74) BETA(KK)=.17452
      IF(KK.GE.75.AND.KK.LE.82) BETA(KK)=1.22164
      IF(KK.GE.83.AND.KK.LE.90) BETA(KK)=.69808
      IF(KK.GE.91.AND.KK.LE.98) BETA(KK)=2.4433
      IF(KK.GE.99.AND.KK.LE.106) BETA(KK)=1.91972
      IF(KK.GE.107.AND.KK.LE.114) BETA(KK)=2.9668
      IF(KK.GE.115.AND.KK.LE.122) BETA(KK)=2.7574
      IF(KK.GE.123.AND.KK.LE.146) BETA(KK)=3.14136
      IF(KK.GE.147.AND.KK.LE.158) BETA(KK)=3.29843
      IF(KK.GE.159.AND.KK.LE.202) BETA(KK)=3.40314
```

```
      IF(KK.GE.203.AND.KK.LE.214) BETA(KK)=3.29843
      IF(KK.GE.215.AND.KK.LE.230) BETA(KK)=3.14136
      IF(KK.GE.231.AND.KK.LE.246) BETA(KK)=0.0
      IF(KK.GE.247.AND.KK.LE.258) BETA(KK)=-.15707
      IF(KK.GE.259.AND.KK.LE.326) BETA(KK)=-.2618
      IF(KK.GE.327.AND.KK.LE.350) BETA(KK)=-.15707
      IF(KK.GE.351.AND.KK.LE.430) BETA(KK)=0.0
      IF(KK.GE.431.AND.KK.LE.438) BETA(KK)=.38394
      IF(KK.GE.439.AND.KK.LE.446) BETA(KK)=.17452
      IF(KK.GE.447.AND.KK.LE.454) BETA(KK)=.38394
      IF(KK.GE.455.AND.KK.LE.462) BETA(KK)=.17452
      IF(KK.GE.463.AND.KK.LE.470) BETA(KK)=1.2216
      IF(KK.GE.471.AND.KK.LE.478) BETA(KK)=.69808
      IF(KK.GE.479.AND.KK.LE.486) BETA(KK)=1.2216
      IF(KK.GE.487.AND.KK.LE.494) BETA(KK)=.69808
      IF(KK.GE.495.AND.KK.LE.502) BETA(KK)=2.4433
      IF(KK.GE.503.AND.KK.LE.510) BETA(KK)=1.91972
      IF(KK.GE.511.AND.KK.LE.518) BETA(KK)=2.4433
      IF(KK.GE.519.AND.KK.LE.526) BETA(KK)=1.91972
      IF(KK.GE.527.AND.KK.LE.534) BETA(KK)=2.9668
      IF(KK.GE.535.AND.KK.LE.542) BETA(KK)=2.7574
      IF(KK.GE.543.AND.KK.LE.550) BETA(KK)=2.9668
      IF(KK.GE.551.AND.KK.LE.558) BETA(KK)=2.7574
      IF(KK.GE.559.AND.KK.LE.638) BETA(KK)=3.14136
      IF(KK.GE.639.AND.KK.LE.662) BETA(KK)=3.29843
      IF(KK.GE.663.AND.KK.LE.708) BETA(KK)=3.40314
      IF(KK.GE.709.AND.KK.LE.752) BETA(KK)=0.0

      READ(IN,1) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3)
C     WRITE(6,121) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3),BETA(KK)
 121  FORMAT(4I5,7F10.4)
C
C  DIMENSION IN FEET...
        X1=X(1)
        X2=X(2)
        X3=X(3)
        Y1=Y(1)
        Y2=Y(2)
        Y3=Y(3)
C
       X ( 1 )= X(1) /12.0D0
       X ( 2 )= X(2) /12.0D0
       X ( 3 )= X(3) /12.0D0
       Y ( 1 )= Y(1) /12.0D0
       Y ( 2 )= Y(2) /12.0D0
       Y ( 3 )= Y(3) /12.0D0
C
        T1=T(1)
        T2=T(2)
        T3=T(3)
 1107   FORMAT(1H1,///20X
     *  ,'     T(1)       T(2)       T(3)     '
     *  ,' ISIDE(1)  ISIDE(2)    ')
 1108   FORMAT(' ',20X
```

```
     *  ,' -------  --------  --------  -------   -------    ------- '
     *  ,'---------')
C       WRITE(IO,11)T,ISIDEH(KK,1),ISIDEH(KK,2)
C
C
C
        TOLD(NS(1))=T(1)
        TOLD(NS(2))=T(2)
        TOLD(NS(3))=T(3)
C       H : CONVECTION COEFFICIENT
C       WRITE(6,5152)KK,NS(1),NS(2),NS(3),TOLD(NS(1)),TOLD(NS(2)),
C     1  TOLD(NS(3)), H(KK),(ISIDE(JJ),JJ=1,2),
C     1  X1,Y1,X2,Y2,X3,Y3,NOT(KK,1),NOT(KK,6)
 5152  FORMAT(' ',4I5,3F10.3,F5.0,2I2,6F8.4,I5,A8)
C
        T(1)=T1
        T(2)=T2
        T(3)=T3
C
C  ECHO THE INPUT........
C     WRITE(IO,23) NEL,NS,X(1),Y(1),X(2),Y(2),X(3),Y(3)
C    * , HH,RHO,CP,ISIDE,T
   23 FORMAT(1H0,I5,1X,3I5,2X,6(1X,F8.4),2X,2F5.0,F6.3,2X,2I3,
     *  2X,3F6.0)
C  CALCULATION OF THE CONDUCTION MATRIX
C
C    NPT (NE,3) : ARRAY STORES THE NODE NUMBERS FOR EACH ELEMENT
       NPT(KK,1) = NS(1)
       NPT(KK,2) = NS(2)
       NPT(KK,3) = NS(3)
       R(NS(1)) =  X(1)
       R(NS(2)) =  X(2)
       R(NS(3)) =  X(3)
       Z(NS(1)) =Y(1)
       Z(NS(2)) =Y(2)
       Z(NS(3)) =Y(3)
      AREAE(KK)=(X(2)*Y(3)-X(2)*Y(1)+X(3)*Y(1)-X(3)*Y(2)
     1  + X(1)*Y(2)-X(1)*Y(3))/2.0
C-----------------------------------------------------C!-------------C!
C---------------------------------------------------------------------C!
C        WRITE(6,266)KK,X(1),Y(1),X(2),Y(2),X(3),Y(3),AREAE(KK)
 266    FORMAT(1H0,I5,6(1X,F8.4,),2X,D14.7)
C       WRITE(6,319)KK,(T(I),I=1,3)
 319    FORMAT('  ELEMENT  NO.  ',I8,3F12.4)
   7    CONTINUE
C.....................................END OF THE DO LOOP ........C!
C       WRITE(6,264)(I,TOLD(I),I=1,NP)
 264    FORMAT(1H0,I5,E14.5,2X,I5,E14.5,2X,I5,E14.5,2X,I5,E14.5
     * ,2X,I5,E14.5,2X,I5,E14.5)
C
C ADD EXTERNALLY APPL. CONC. NODAL FORCES VECTOR TO EF VECTOR
         ID1=0
         INK=0
 202     READ(IN,203) NODNUM,CFV
```

```
 203     FORMAT(6I3,2X,6F10.5)
         ID=0
         DO 204 L=1,6
         IF( NODNUM(L).LE.0) GOTO 205
         ID=ID+1
         INODNU=NODNUM(L)
 204     EF(INODNU)=CFV(L)+EF(INODNU)
         GOTO 206
 205     INK=1
         IF(ID.EQ.0) GOTO 216
 206     IF(ID1.EQ.1)GOTO 222
         WRITE(IO,208)
 208     FORMAT(1H1,' NODE NUMBER ',10X,' GENERALIZED  NODAL FORCES ')
 222     WRITE(IO,207)(NODNUM(L),CFV(L),L=1,ID)
 207     FORMAT(1H0,6(I3,E14.5,2X))
         IF(INK.EQ.1)GOTO 216
         ID1=1
         GOTO 202
 216     CONTINUE
C<><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><><>
C
        JJJKNT=0
C
          DO 3000 ITER=1,100
          CALL FORMTK (NE,NP,NBW,TIME,ITER)
          CALL FORMTC (NE,NP,NBW)
          CALL FORMTF (NE,NP,NBW)
          CALL ASSMBL (NP,NBW,DDT,ITER)
C         WRITE(6,9999)((ZZ(I,J),J=1,NBW),I=1,NP)
9999      FORMAT(2X,7G11.5)
C         WRITE(6,9988)(F(I,1),I=1,NP)
9988      FORMAT(2X,G11.5)
          CALL SOLVE(NP,NBW)
          JJJKNT=JJJKNT+1
          IF(JJJKNT.GE.1)GOTO 979
          GOTO 980
979       CONTINUE
          TIME(ITER)=DDT*ITER
          DO 2001 I = 1,483
          FIJ(I,ITER) = F(I)
2001      CONTINUE
C         WRITE(IO,666)TIME,ITER,TDT
C66       FORMAT(//,1H1,' TEMPERATURE DISTRIBUTION AT THE TIME =',
C    * E15.6, ' HOUR ' ,/'  ITERATION NO. =',I10, '#',
C    * '       *&*    TDHEAT.2            DDT=',F10.6,/)
C       IF(ITER.EQ.22)
C    1    WRITE(7,777)(I,F(I),I=1,NP)
C77       FORMAT( 1H0,I5,F14.5,2X,I5,F14.5,2X,I5,F14.5,2X,I5,F14.5,
C    *2X,I5,F14.5,2X,I5,F14.5)
C77       FORMAT(I4,F10.4)
980       CONTINUE
          MAX(1)=0.0
          STT=0.0
          DO 1515 I=1,NP
```

```
          MAX(I+1)=DABS(F(I)-TOLD(I))
CF        WRITE(6,1211)MAX(I+1)
1211      FORMAT(2X,F15.6)
          IF(MAX(I+1).LT.MAX(I))GOTO 1515
          IF(MAX(I+1).GT.MAX(I))FAXM=MAX(I+1)
          IF(FAXM.GT.STT)GTST=FAXM
          STT=GTST
1515      CONTINUE
C         WRITE(6,1222)GTST
CF    GTST IS THE STOPPING CRITERION. ITERATION STOPS WHEN DIFF. BETW
CF    T(NEW) AND T(OLD) IS LESS THAN 0.3 DEGREE
1222      FORMAT(/,2X,F10.5)
          IF(GTST.LT.0.3)GOTO 1200
          DO 2000 I=1,NP
          TOLD(I)=F(I)
2000      CONTINUE
3000      CONTINUE
1200      DO 3011  IJP = 1,483
          WRITE(7,666)IJP
666      FORMAT(//,' TEMPRATUE DISTRIBUTION AT POINT  ',I5,/)
C         WRITE(7,777)(I,TIME(I),FIJ(IJP,I), I =1,65)
777       FORMAT(I5,2F10.4)
3011     CONTINUE
C
C
C200      STOP
          END
          SUBROUTINE FORMTK (NE,NP,NBW,TIME,ITER)
C***********************************************************************
C.......... FORM BANDED THERMAL CONDUCTANCE MATRIX
C
      IMPLICIT REAL*4(A-H,O-Z)
      REAL*8 KZETA,KETA,RHOCP,BETA
      REAL*8 BI,BJ,BK,CI,CJ,CK,COF,CON1,CON2,CON3
      REAL*8 RBAR,CON,LG,RCTL,ELKT(3,3),THSTF(483,18)
      REAL*8 A00,A11,A22,B00,B11,B22,C00,THCAP(483,18),TOLD(483)
      REAL*8 Z(483),R(483),AREAE(752),X(3),Y(3),DDT,TIME,ATIM,P
      COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3),TOLD
       REAL*8   ZZ(483,18),F,B,FF,EF
      COMMON / SOLVEQ / F(483),EF(752),ZZ
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
C
C
C
C.......... INITIALIZE GLOBAL THERMAL STIFFNESS MATRIX
       IN=5
       IO=6
      DO 120 J=1,NBW
      DO 110 I=1,NP
      THSTF(I,J) = 0.D0
  110 CONTINUE
```

```
  120 CONTINUE
C
C
  130 NBAND = 0
      DO 899 J=1,NE
C      WRITE(6,788)KZETA(J),KETA(J),BETA(J)
788   FORMAT(3X,3F20.9)
899   CONTINUE
C
C        WRITE(6,7776)
 7776   FORMAT(' CONDUCTION MATRIX ELEMENTS ARE ',/)
      DO 230 N=1,NE
C<><><><><><>---------------------------------<><><><><><><><><><><><>
C
      II = NPT(N,1)
      JJ = NPT(N,2)
      KK = NPT(N,3)
      BI = Z(JJ)-Z(KK)
      BJ = Z(KK)-Z(II)
      BK = Z(II)-Z(JJ)
      CI = R(KK)-R(JJ)
      CJ = R(II)-R(KK)
      CK = R(JJ)-R(II)
      X(1) =R(II)
      X(2) =R(JJ)
      X(3) =R(KK)
      Y(1) =Z(II)
      Y(2) =Z(JJ)
      Y(3) =Z(KK)
C     WRITE(6,555)X(1),X(2),X(3),Y(1),Y(2),Y(3)
555   FORMAT(2X,6F12.6)
      ALPHA=BETA(N)
      CON1=(KZETA(N)*(COS(ALPHA))**2+KETA(N)*(SIN(ALPHA))**2)
     1/(4.*AREAE(N))
      CON2=(KZETA(N)-KETA(N))*SIN(2.*ALPHA)/(4.*AREAE(N))
      CON3=(KZETA(N)*(SIN(ALPHA))**2+KETA(N)*(COS(ALPHA))**2)
     1/(4.*AREAE(N))
C
C     WRITE(6,7999)CON1,CON2,CON3,AREAE(N)
7999  FORMAT(2X,3F10.3,2X,F10.7)
      ELKT(1,1) = (BI**2)*CON1+(CI**2)*CON3
      ELKT(1,2) = (BI*BJ)*CON1+(CI*CJ)*CON3
      ELKT(1,3) = (BI*BK)*CON1+(CI*CK)*CON3
      ELKT(2,2) = (BJ**2)*CON1+(CJ**2)*CON3
      ELKT(2,3) = (BJ*BK)*CON1+(CJ*CK)*CON3
      ELKT(3,3) = (BK**2)*CON1+(CK**2)*CON3
        DO 10 IQ=1,2
C       WRITE(6,7805)N,( ISIDEH(N,J1),J1=1,2)
 7805    FORMAT(' SIDE EXPOSED ',3I10)
        IF ( ISIDEH(N,IQ) . LE . 0 ) GO TO 240
        JQ = ISIDEH (N,IQ)
C        WRITE(IO,12) JQ,N
 12     FORMAT(1HO,' INSIDE',I3,3X,' OF ELEMENT',I5)
        KQ = JQ +1
```

```
        IF ( JQ.EQ . 3) KQ=1
        LG = DSQRT((X(KQ)-X(JQ))**2+(Y(KQ)-Y(JQ))**2)
        HL =H(N)*LG/6.
        IF(JQ.EQ.1) GO TO 20
        IF(JQ.EQ.2) GO TO 30
        IF(JQ.EQ.3) GO TO 40
        GO TO 10
 20     ELKT(1,1)= ELKT(1,1)+HL * 2.
        ELKT(2,2)= ELKT(2,2)+HL * 2.
        ELKT(1,2)= ELKT(1,2)+HL
        GO TO 10
C
 30     ELKT(2,2)= ELKT(2,2)+HL*2.
        ELKT(3,3)= ELKT(3,3)+HL*2.
        ELKT(2,3)= ELKT(2,3)+HL
        GO TO 10
C
 40     ELKT(1,1)= ELKT(1,1)+HL * 2.
        ELKT(3,3)= ELKT(3,3)+HL * 2.
        ELKT(1,3)= ELKT(1,3)+HL
 10     CONTINUE
C
C     WRITE(IO,2000)N,II,JJ,KK,X(1),Y(1),X(2),Y(2),X(3),Y(3),CONDTY(N),
C    1AREAE(N),RBAR,CON,ELKT(1,1),ELKT(1,2),ELKT(1,3),ELKT(2,2),
C    2ELKT(2,3),ELKT(3,3)
 2000 FORMAT(1H0,4I5,8G11.4,/21X,8G11.4)
C--------------------------------------------------------C!
C      S T O R E   I N   G L O B A L   M A T R I X     C!
C--------------------------------------------------------C!
 240   CONTINUE
C     WRITE( IO,266)N,X(1),Y(1),X(2),Y(2),X(3),Y(3),AREAE(N),NBAND
 266  FORMAT(1H0,I5,6(1X,F8.4),2X,D14.7,2X,I5)
C       WRITE(6,277)N,(( ELKT(I,J),J=1,3),I=1,3)
 277  FORMAT(' ',I5/ 3(3F25.6/))
      DO 220 LL=1,3
      DO 210 MM=1,3
      IF(MM.LT.LL) GOTO 210
      I=NPT(N,LL)
      J=IABS(NPT(N,MM)-I)+1
      IF(NPT(N,MM).LT.NPT(N,LL)) I=NPT(N,MM)
      THSTF(I,J) =THSTF(I,J)+ELKT(LL,MM)
C      WRITE(6,7543)I,J,II,JH,NPT(N,J),NPT(N,I)
 7543 FORMAT(' ',6I8,   '******')
       IF (J.GT.NBAND) NBAND=J
 210  CONTINUE
 220  CONTINUE
  230 CONTINUE
C     WRITE(6,5050)((THSTF(I,J),J=1,NBW),I=15,20)
 5050 FORMAT(7G11.5)
C
C      WRITE (6,200) NBAND
 200  FORMAT(1H0,'  NBAND= ',I5)
C
C.......... END OF PROGRAM
```

```
C
C
      RETURN
      END
C
C.......... FORM BANDED CAPACITANCE MATRIX FOR A DEFORMING F.E. MESH
C
        SUBROUTINE FORMTC (NE,NP,NBW)
C
      REAL*8 Z(483),R(483),AREAE(752),X(3),Y(3),DDT
      REAL * 8 CON ,ELCAP(3,3),THCAP(483,18),TOLD(483),THSTF(483,18)
     1 ,THSTF1(747,17)
      COMMON/CONVEN/H(752),SIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3),TOLD
       REAL*8   ZZ(483,18),F,EF,B,COF,FF,KZETA,KETA
      COMMON / SOLVEQ / F(483),EF(752),ZZ
      DIMENSION FF(15,1)
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
C
C
      REAL * 8 R1,R2,R3,R4,R5,R6
C
C.......... INITIALIZE GLOBAL THERMAL CAPACITANCE MATRIX
C
        IO=6
        J9=0
       DO 120 J=1,NBW
       DO 110 I=1,NP
       THCAP(I,J) = 0.D0
  110  CONTINUE
  120  CONTINUE
C
C
C     WRITE(6,8880)
8880  FORMAT(' CAPACITANCE MATRIX ELEMENTS ARE ',/)
  200  DO 230 N=1,NE
C
C......... FOR EACH ELEMENT, FOR THERMAL CAPACITCANCE MATRIX
C
      II = NPT(N,1)
      JJ = NPT(N,2)
      KK = NPT(N,3)
      CON=RHOCP(N)*AREAE(N)/12.
      ELCAP(1,1)=2.*CON
      ELCAP(1,2)=1.*CON
      ELCAP(1,3)=1.*CON
      ELCAP(2,2)=2.*CON
      ELCAP(2,3)=1.*CON
      ELCAP(3,3)=2.*CON
C
C
C       WRITE(IO,2000)N,II,JJ,KK,R(II),Z(II),R(JJ),Z(JJ),R(KK),Z(KK),
```

```
C     1 RHOCP(N),AREAE(N),CON,ELCAP(1,1),ELCAP(1,2),ELCAP(1,3),
C     2       ELCAP(2,2),ELCAP(2,3),ELCAP(3,3)
 2000  FORMAT(1H0,4I5,9G11.4/21X,6G11.4)
C
C......... STORE IN GLOBAL MATRIX
      DO 220 I=1,3
      DO 210 J=1,3
      IF(J.LT.I) GOTO 210
      II=NPT(N,I)
      JJ=IABS(NPT(N,J)-II)+1
      IF (NPT(N,J).LT.NPT(N,I)) II=NPT(N,J)
      THCAP(II,JJ) = THCAP(II,JJ)+ELCAP(I,J)
 210    CONTINUE
 220    CONTINUE
C
C      WRITE(6,277)N,(( ELCAP(I,J),J=1,3),I=1,3)
 277  FORMAT(' ',I5/ 3(3F25.6/))
 230  CONTINUE
C
C      WRITE(IO,4000)(THCAP(I,J),J=1,NBW)
 4000  FORMAT(1H0,'THCAP',10G11.4/6X,10G11.4/6X,10G11.4/6X,10G11.4)
C       WRITE(IO,1000)
 1000  FORMAT(1H0,'LEAVING FORMTC       IN  TDHEAT ..1B ')
 264    FORMAT(1H0,I5,E14.5,2X,I5,E14.5,2X,I5,E14.5,2X,I5,E14.5
     * ,2X,I5,E14.5,2X,I5,E14.5)
C
C.......... END OF PROGRAM
C
        RETURN
        END
      SUBROUTINE FORMTF(NE,NP,NBW)
C
C      FORM THERMAL FORCE VECTOR
C
C
C
      REAL*8 ELF(3),LG,RCTL,COF,THCAP(483,18),THSTF(483,18)
      REAL*8 Z(483),R(483),AREAE(752),X(3),Y(3),DDT,TOLD(483)
      COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1 ,THCAP,NPT(752,3),TOLD
      REAL*8   ZZ(483,18),F,EF,B,ELF1,ELF2,ELF3,FF,HLL
      COMMON / SOLVEQ / F(483),EF(752),ZZ
      REAL *8 KZETA,KETA,RHOCP,BETA
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)
      REAL *8 QR(752),HL(752)
      DATA W/ .6666666666D0/
          IO=6
         TINF =10.D0
C
C
C      FOR EACH ELEMENT ,FORM THERMAL FORCE VECTOR
C
```

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```
C         WRITE(6,9999)
 9999     FORMAT(' FORCE VECTORS ARE ',/)
          DO 110 I=1,NE
          EF(I)   = 0.D0
          QR(I)=0.0
 110      CONTINUE
          DO 1070 J=1,45
          N=2*J
          QR(N)=326.0
1070      CONTINUE
          DO 230 N=1,NE
          ELF(1)=0.D0
          ELF(2)=0.D0
          ELF(3)=0.D0
          II=NPT(N,1)
          JJ=NPT(N,2)
          KK=NPT(N,3)
          CI = R(KK)-R(JJ)
          CJ = R(II)-R(KK)
          CK = R(JJ)-R(II)
          BI=Z(JJ)-Z(KK)
          BJ=Z(KK)-Z(II)
          BK=Z(II)-Z(JJ)
          X(1)=R(II)
          X(2)=R(JJ)
          X(3)=R(KK)
          Y(1)=Z(II)
          Y(2)=Z(JJ)
          Y(3)=Z(KK)
          ALPHA=BETA(N)
          CON2=(KZETA(N)-KETA(N))*SIN(2.*ALPHA)/(4.*AREAE(N))
          ELF1=CON2*(BI*CI*TOLD(II)+BI*CJ*TOLD(JJ)+BI*CK*TOLD(KK))
          ELF2=CON2*(BJ*CI*TOLD(II)+BJ*CJ*TOLD(JJ)+BJ*CK*TOLD(KK))
          ELF3=CON2*(BK*CI*TOLD(II)+BK*CJ*TOLD(JJ)+BK*CK*TOLD(KK))
          ELF(1)=-W*ELF1
          ELF(2)=-W*ELF2
          ELF(3)=-W*ELF3
          DO 10 IQ=1,2
          IF(ISIDEH(N,IQ).LE.0)GO TO 240
          JQ=ISIDEH (N,IQ)
          KQ=JQ+1
          IF(JQ.EQ.3) KQ=1
          LG=DSQRT((X(KQ)-X(JQ))**2+ (Y(KQ)-Y(JQ))**2)
C         WRITE(6,999)LG
999        FORMAT(2X,F10.5)
          HL(N)=QR(N)+H(N)*TINF
          IF ( JQ.EQ.1)GO TO 20
          IF ( JQ.EQ.2)GO TO 30
          IF (JQ .EQ.3)GO TO 40
          GO TO 240
 20       ELF(1) =HL(N)*LG*.5+ELF(1)
          ELF(2) =HL(N)*LG*.5+ELF(2)
          GO TO 10
 30       ELF(2) =HL(N)*LG*.5+ELF(2)
```

```
          ELF(3) =HL(N)*LG*.5+ELF(3)
          GO TO 10
 40       ELF(1) =HL(N)*LG*.5+ELF(1)
          ELF(3) =HL(N)*LG*.5+ELF(3)
 10       CONTINUE
C
 240      EF(II)= EF(II)+ELF(1)
          EF(JJ)=EF(JJ) +ELF(2)
          EF(KK)=EF(KK) +ELF(3)
 707      FORMAT(' ',2I8,5F15.5)
C         IF(EF(II).EQ.0) GO TO 50
C         IF(EF(JJ).EQ.0) GO TO 50
C         IF(EF(KK).EQ.0) GO TO 50
C         GOTO 230
C50       WRITE(6,1999)N,II,JJ,KK,EF(II),EF(JJ),EF(KK)
1999      FORMAT(1H0,4I6,2X,3F10.4)
 230       CONTINUE
C          WRITE(IO,2000)(EF(I),I=1,NP)
 2000      FORMAT(2X,F10.4)
C           WRITE(IO,1000)
 1000      FORMAT(1H0,' LEAVING  FORMTF      IN TDHEAT ...1B')
           RETURN
           END
      SUBROUTINE ASSMBL (NP,NBW,DDT,ITER)
C.......... ASSEMBLE MATRICES FOR RECURRENCE FORMULAS
           REAL*8 Z(483),R(483),AREAE(752),THSTF(483,18),THCAP(483,18)
     1 ,THSTF1(747,17)
       REAL*8   ZZ(483,18),F,EF,B,ZO(747,17),FF(15,1),TOLD(483)
       COMMON/CONVEN/H(752),ISIDEH(752,2)
C
      COMMON / SOLID / Z,R,AREAE,THSTF
     1   ,THCAP,NPT(752,3),TOLD
      COMMON / SOLVEQ / F(483),EF(752),ZZ
      COMMON /CONT/ KZETA(752),KETA(752),RHOCP(752),BETA(752)

C      WEIGHTING FACTORS FOR GALERKIN ANALYSIS........
C
       DATA W1,W2,W3,W4/ 0.3333333333333333D0 ,
     1                      0.5000000000000000D0 ,
     2                     -0.1666666666666667D0 ,
     3                     0.5000000000000000D0 /
C
      IO=6
      DT = DDT
C      WRITE (IO,1000) W1,W2,W3,W4,DT
 1000 FORMAT (1H0,'ASSEMBLE    IN TDHEAT ....1'//,5E15.8/'   ZZ
     1  COL  1  TO 6 '/)
C
 6567      FORMAT(' ',I5,6F12.6)
 3000 FORMAT(1H0,'THSTF',10G11.4/6X,10G11.4/6X,10G11.4/6X,10G11.4/)
 4000 FORMAT(1H0,'THCAP',10G11.4/6X,10G11.4/6X,10G11.4/6X,10G11.4/)
C
       DO 150 I=1,NP
C
```

```
C.......... COEFFICIENT MATRIX
C
      DO 110 J=1,NBW
      ZZ(I,J) = W1*(THSTF(I,J))+W2*(THCAP(I,J))/DT
  110 CONTINUE
C      WRITE(IO,2000) (ZZ(I,J),J=1,NBW)
 2000  FORMAT(' ',8E15.6)
C
C.......... THERMAL LOAD VECTOR
C
      F(I) = EF(I)/2.D0
C
      IF (I.EQ.1)   GO TO 130
      JST = I+1-NBW
      IF (JST.LT.1)   JST=1
      JEND = I-1
C     WRITE (6,1000) I,JST,JEND
C
      DO 120 J=JST,JEND
      II = I+1-J
C-----------------------------------------------¢!----------------
C
      F(I) =F(I)+(W3*(THSTF(J,II))+W4*(THCAP(J,II))
     1 /DT)* (TOLD(J))
C     WRITE (6,1000) I,J,II,THSTF(J,II),THCAP(J,II),TOLD(J),F(I)
  120 CONTINUE
C
  130 JST = I
      JEND = I-1+NBW
      IF (JEND.GT.NP)   JEND=NP
C     WRITE (6,1000) JST,JEND
      DO 140 J=JST,JEND
      JJ = J-I+1
      F(I) =F(I)+(W3*(THSTF(I,JJ))+W4*(THCAP(I,JJ))
     1 /DT)* (TOLD(J))
C     WRITE (6,1000) I,J,JJ,THSTF(I,JJ),THCAP(I,JJ),TOLD(J),F(I)
  140 CONTINUE
C     WRITE (6,1000) I,JST,JEND,F(I)
C     WRITE (6,1001) I,(ZZ(I,J),J=1,NBW),F(I),TOLD(I)
  150 CONTINUE
 1001 FORMAT (1H ,I3,6G11.5)
C
C.......... END OF PROGRAM
C
       RETURN
       END
         SUBROUTINE SOLVE(NP,NBW)
C
C        SOLUTION OF EQUATIONS BY GAUSS ELIMINATION
C        NP=NO. OF NODAL POINTS    NBW=BANDWIDTH
C          =NO. OF UNKNOWNS
C          =NO. OF EQUATIONS
C
         REAL*8   ZZ(483,18),F,EF,B,P,EXTRA
```

```
      COMMON/SOLVEQ/F(483),EF(752),ZZ
      IO=6
C      WRITE(6,1002)
 1002 FORMAT('   IN SOLVE    ZZ(I,J)  COL 1 TO 4  '/)
 100  DO 130 I=1,NP
C      WRITE(IO,1001)I,(ZZ(I,J),J=1,4),F(I)
 1001 FORMAT(' ',I5,5E15.5)
C     REDUCE THE STIFFNESS MATRIX............
C
      DO 120 J=2,NBW
      II=I+J-1
      IF(ZZ(I,J).EQ.0.0) GO TO 120
      P= ZZ(I,J)/ZZ(I,1)
      JJ=0
      DO 110 K=J,NBW
      JJ=JJ+1
      IF(ZZ(I,K).NE.0.0D0) ZZ(II,JJ)=ZZ(II,JJ)-P*ZZ(I,K)
C
      IF(DABS(ZZ(II,JJ)).LT. 1.E-20)ZZ(II,JJ)=0.0D0
 110   CONTINUE
       ZZ(I,J) =P
C
C      REDUCE LOAD VECTOR
C
       F(II) = F(II)-P*F(I)
C
 120   CONTINUE
       F(I) = F(I)/ZZ(I,1)
C
C      WRITE(IO,1000)I,ZZ(I,J),J=1,NBW),F(I)
 1000  FORMAT(1H0,'SOLVE',I3/4(5E15.8/))
 130   CONTINUE
C
C.......BACK SUBSTITUTION
C
 200   N=NP
 210   N=N-1
       IF(N.EQ.0) GO TO 300
       II=N
       DO 220 J=2,NBW
       II=II+1
       IF ( ZZ(N,J).NE.0.0) F(N)=F(N)-ZZ(N,J)*F(II)
 220   CONTINUE
       GO TO 210
C
C .........SOLUTION VECTOR STORED IN    F   ARRAY
C
 300   RETURN
       END
```

```
C
C     THE GRID PROGRAM IS MODIFIED TO GENERATE  RECTANGULAR ELEMENTS.
C     THE CHANGES  ARE AS FOLLOW:
C
CH    THE DIMENSION OF NOO(2500,6) IS CHANGED  TO NOO(2500,7)
CH    THE DIMENSION OF NR(3) IS CHANGED TO NR(4)
CH    THE DIMENSION OF IS CHANGED TO LB(3) TO LB(6)
C
C     DIVISION INTO RECTANGULAR ELEMENTS
C
      K=1
      DO 17 I=1,NROWS
      DO 17 J=1,NCOL
      XE(K)=XC(I,J)
      YE(K)=YC(I,J)
      NE(K)=NN(I,J)
   17 K=K+1
      L=NROWS-1
      DO 21 I=1,L
      DO 21 J=2,NCOL
CH    DIAG1=SQRT((XC(I,J)-XC(I+1,J-1))**2+(YC(I,J)-YC(I+1,J-1))**2)
CH    DIAG2=SQRT((XC(I+1,J)-XC(I,J-1))**2+(YC(I+1,J)-YC(I,J-1))**2)
      NR(1)=NCOL*I+J-1
      NR(2)=NCOL*I+J
      NR(3)=NCOL*(I-1)+J
      NR(4)=NCOL*(I-1)+J-1
CH    DO 21 IJ=1,2
      NEL=NEL+1
CH    IF((DIAG1/DIAG2).GT.1.02) GO TO 18
      J1=NR(1)
      J2=NR(2)
      J3=NR(3)
      J4 = NR(4)
CH    GO TO 19
CH 18 J1=NR(IJ)
CH    J2=NR(IJ+1)
CH    J3=NR(4)
CH   LB(3),LB(5) AND LB(6) ARE ADDED
      LB(1)=IABS(NE(J1)-NE(J2))+1
      LB(2)=IABS(NE(J1)-NE(J3))+1
      LB(3)=IABS(NE(J1)-NE(J4))+1
      LB(4)=IABS(NE(J2)-NE(J3))+1
      LB(5)=IABS(NE(J2)-NE(J4))+1
      LB(6)=IABS(NE(J3)-NE(J4))+1
      DO 20 IK=1,6
      IF(LB(IK).LE.NBW) GO TO 20
      NBW=LB(IK)
      NELBW=NEL
   20 CONTINUE
       IF( KK . NE . 46 ) GO TO 888
C       WRITE(6,666) J3 , NE(J3)
 666   FORMAT(///// '  J3 = ',I9,' NE(J3) = ' , I9 )
 888   CONTINUE
       WRITE(IO,113) KK,NEL,NE(J1),NE(J2),NE(J3),NE(J4),XE(J1),YE(J1),
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```
     1 XE(J2),YE(J2),XE(J3),YE(J3),XE(J4),YE(J4)
      IF(IPCH.EQ.0) GO TO 21
      WRITE(IP,114) NEL,NE(J1),NE(J2),NE(J3),NE(J4),XE(J1),YE(J1),XE(J2)
     1,YE(J2),XE(J3),YE(J3),XE(J4),YE(J4)
CH   NOO(NEL,6) IS ADDED
      NOO(NEL,1)=KK
      NOO(NEL,2)=NEL
      NOO(NEL,3)=NE(J1)
      NOO(NEL,4)=NE(J2)
      NOO(NEL,5)=NE(J3)
      NOO(NEL,6)=NE(J4)
      NOO(NEL,7)=IRR(KK)
   21 CONTINUE
   22 CONTINUE
```

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```
CH  THE DIMENSION OF NOO, X, I, OR Y IS INCREASED BY 1
C
       COMMON/AAA/ NOO(2500,7),NTT(80)
       COMMON/BBB/ X(4,2000),Y(4,2000),NBO(1000),TITLE(10)
       COMMON/CCC/ NODES,LMENTS,JT(12000),MEMJT(24000),JMEM(3000),
      $JNT(3000),IDIFF,MINMAX
       DATA IN/11/,IO/6/,IP/12/
C
       READ (IN,100)TITLE
       WRITE(IP,100)TITLE
100    FORMAT(10A4)
122    FORMAT(I3,5F10.5)
       J =1
       JJ=0
CH     I IS CHANGED FROM 3 TO 4
150    READ(IN,17)(JT(3000*(I-1)+J),I=1,4),(X(I,J),Y(I,J),I=1,4)
CH     JT(9000+J)=0
C      WRITE(IO,17)(JT(3000*(I-1)+J),I=1,4),(X(I,J),Y(I,J),I=1,4)
       NODES=MAX0(JT(J),JT(3000+J),JT(6000+J),JT(9000+J),JJ)
       JJ=NODES
       IF(JT(3000+J).EQ.0)GO TO 152
       J=J+1
       GO TO 150
152    LMENTS=J-1
       NODES=JJ
  12     FORMAT(//,5X,15HNUMBER OF NODES,I4,15X,
      1'NUMBER OF ELEMENTS    ',I4,//)
       WRITE(IO,105)TITLE
105    FORMAT(//,1X,20A4,//)
C      WRITE(IO,12)NODES,LMENTS
C      WRITE(IO,13)
C3     FORMAT(//,3X,18HNEL  JT1  JT2  JT3,10X,4HX(1),8X,
C     $4HY(1),8X,4HX(2),8X,4HY(2),8X,4HX(3),8X,4HY(3))
17     FORMAT(4X,4I4,8F10.5)
       DO 10 J=1,LMENTS
       WRITE(IO,11)J,(JT(3000*(I-1)+J),I=1,4),(X(I,J),Y(I,J),I=1,4)
11     FORMAT(1X,5I5,3X,8F12.4)
10     CONTINUE
       READ(IN,300)IBO
300    FORMAT(50X,I4,46X)
       READ(IN,301)(NBO(I),I=1,IBO)
C      WRITE(IO,302)
       DO 333  I=1,LMENTS
       READ (IN,444)(NOO(I,J),J=1,7)
 333   CONTINUE
C      WRITE(IO,303)(NBO(I),I=1,IBO)
302    FORMAT(//,'  *** BOUNDARY NUMBERS ***')
       CALL SETUP
       NTBAN=IDIFF+1
       WRITE(IO,202)NTBAN
202    FORMAT(//,2X,25HTHE ORIGINAL BANDWIDTH IS,I4,//)
       CALL OPTNUM
       IF(IDIFF.LE.MINMAX)GO TO 115
       MIBAN=MINMAX+1
```

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```
      WRITE(IO,198)
198   FORMAT(1H1///,1X,5(3HOLD,3X,3HNEW,7X),/,1X,
     $5(4HNODE,2X,4HNODE,6X))
      WRITE(7,200)(J,JNT(J),J=1,NODES)
200   FORMAT(5(I5,1X,I5,5X))
C     WRITE(IO,13)
      DO 180 J=1,LMENTS
      DO 555 II=1,4
      III=II+2
 555  NOO(J,III)=JNT(JT(3000*(II-1)+J))
C
180   CONTINUE
C     WRITE(IO,11)J,(JNT(JT(3000*(I-1)+J)),I=1,4),
C    $(X(I,J),Y(I,J),I=1,4)
      WRITE(IO,201)MIBAN
201   FORMAT(//,2X,'THE NEW BANDWIDTH IS',I3,/)
C     WRITE(IP,310)NODES,LMENTS,MIBAN
C     DO 181 J=1,LMENTS
C81   WRITE(IP,18)J,(JNT(JT(3000*(I-1)+J)),I=1,4),(X(I,J),
C    $Y(I,J),I=1,4)
C8    FORMAT(5I5,8F10.4)
C     WRITE(IO,302)
C     WRITE(IP,300)IBO
C     WRITE(IP,301)(JNT(NBO(I)),I=1,IBO)
C     WRITE(IO,303)(JNT(NBO(I)),I=1,IBO)
303   FORMAT(15I4)
      GO TO 117
115   CONTINUE
      WRITE(IO,101)
117   CONTINUE
101   FORMAT(///,2X,'THE ORIGINAL BANDWIDTH IS MININMUM')
      WRITE(IP,310)NODES,LMENTS,NTBAN
310   FORMAT(3I5)
C     DO 190 J=1,LMENTS
C190  WRITE(IP,18)J,(JT(3000*(I-1)+J),I=1,4),
C    1(X(I,J),Y(I,J),I=1,4)
C     WRITE(IP,300)IBO
C     WRITE(IP,301)(NBO(I),I=1,IBO)
301   FORMAT(20I5)
C--------------------------C!
 444  FORMAT(6I5,A4)
      LLL = NOO(1,7)
C
      LOL=0
      MMM=0
      NNN=1
      DO 666 II=1,LMENTS
      IF ( LLL.EQ.NOO(II,7) )GO TO 1888
      NNN=NNN-1
      LOL=LOL+NNN
      MMM=MMM+1
      NTT(MMM)=LOL
C     WRITE(IO,888) NNN,NTT(MMM)
      LLL=NOO(II,7)
```

```
      NNN=1
 1888 CONTINUE
      WRITE(IO,777)NNN,(NOO(II,J),J=1,7),(X(I,II),Y(I,II),I=1,4)
C     WRITE(7,1012)NOO(II,2),NOO(II,6)
      WRITE(7,199) (NOO(II,J),J=2,6),(X(I,II),Y(I,II),I=1,4)
      IF (II. NE . LMENTS) GO TO 1889
      LOL=LOL+NNN
      MMM=MMM+1
      NTT(MMM)=LOL
C     WRITE(IO,888) NNN,NTT(MMM)
 1889 NNN=NNN+1
 666  CONTINUE
C
C1012  FORMAT(I5,A5,I5,A5,I5,A5,I5,A5,I5,A5,I5,A5,I5,A5)
 777  FORMAT(2X,7I5,1X,A8,8F10.5)
 199  FORMAT(5I4,8F7.4)
 888  FORMAT(//'  NUMBER OF ELEMENTS IN THIS REGION =',2I10/)
400   CONTINUE
C
C--------------------------------------------------
C--------------------------------------------------
      STOP
      END
```

```
C
C    T R A S F E R     P R O G R A M
C
         DIMENSION X(482),Y(482),T(482),BETA(376),PROB(3,7),ALFA(3,3),
     1             BI(150),TA(482),TG(482)
         INTEGER NN,I,J,K, II,IE(376,5),III,IT,MID(376),IG(482),IS(482)
         CHARACTER*3  TIPE(376),PT(150)
C         DOUBLE PRECISION  PROB,ALFA,BETA
         DATA PROB /770000.0,97500.0,1000.0,
     1              164000.0,132600.0,1500.0,
     1             1380000.0,1950000.0,3000.0,
     1              0.440,0.287,0.40,
     1              0.166,0.022,0.02,
     1              0.255,0.02,0.02,
     1               76000.0,14000.0,500.0/
        DATA ALFA      /0.00002705,0.00003490,0.0000005,
     1                  0.00003038,0.0000259,0.0000005,
     1                  0.00001457,0.0000021,0.0000005/
C        DATA BIRT/'BIRT'/,BIRL/'BIRL'/, FI/' FI'/,PAP /'PAP'/
        DO 3 I = 1,3
C      WRITE(7,55) (PROB(I,J), J = 1,7)
C      WRITE(7,44) (ALFA(I,J), J =1,3)
3        CONTINUE
55      FORMAT(3F10.1,3F10.8,F10.1)
44      FORMAT(3F10.8)
         PI = 3.1415927
         TI = 70.0
C
         DO 5 I = 1,389
         IF(I.LE.140)TIPE(I) ='BIR'
         IF((I.GE.141).AND.(I.LE.151)) TIPE(I) ='FIR'
         IF((I.GE.152).AND.(I.LE.175)) TIPE(I) ='PAP'
         IF((I.GE.176).AND.(I.LE.319)) TIPE(I) ='FIR'
         IF((I.GE.320).AND.(I.LE.343)) TIPE(I) ='PAP'
         IF((I.GE.344).AND.(I.LE.376)) TIPE(I) ='FIR'
C        IF((I.GE.377).AND.(I.LE.389)) TIPE(I) ='BIR'
5        CONTINUE
      DO 51 KK = 1,389
      IF(KK.GE.1.AND.KK.LE.11) BETA(KK)=-.2618
      IF(KK.GE.12.AND.KK.LE.17) BETA(KK)=-.15707
      IF(KK.GE.18.AND.KK.LE.29) BETA(KK)=0.0
      IF(KK.GE.30.AND.KK.LE.33) BETA(KK)=.38394
      IF(KK.GE.34.AND.KK.LE.37) BETA(KK)=.17452
      IF(KK.GE.38.AND.KK.LE.41) BETA(KK)=1.22164
      IF(KK.GE.42.AND.KK.LE.45) BETA(KK)=.69808
      IF(KK.GE.46.AND.KK.LE.49) BETA(KK)=2.4433
      IF(KK.GE.50.AND.KK.LE.53)  BETA(KK)=1.91972
      IF(KK.GE. 54.AND.KK.LE.57)  BETA(KK)=2.9668
      IF(KK.GE. 58.AND.KK.LE.61)  BETA(KK)=2.7574
      IF(KK.GE. 62.AND.KK.LE.73)  BETA(KK)=3.14136
      IF(KK.GE. 74.AND.KK.LE.79)  BETA(KK)=3.29843
      IF(KK.GE. 80.AND.KK.LE.101) BETA(KK)=3.40314
      IF(KK.GE.102.AND.KK.LE.107) BETA(KK)=3.29843
      IF(KK.GE.108.AND.KK.LE.115) BETA(KK)=3.14136
```

ORIGINAL PAGE IS
OF POOR QUALITY

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      IF(KK.GE.116.AND.KK.LE.123) BETA(KK)=0.0
      IF(KK.GE.124.AND.KK.LE.129) BETA(KK)=-.15707
      IF(KK.GE.130.AND.KK.LE.163) BETA(KK)=-.2618
      IF(KK.GE.164.AND.KK.LE.175) BETA(KK)=-.15707
      IF(KK.GE.176.AND.KK.LE.215) BETA(KK)=0.0
      IF(KK.GE.216.AND.KK.LE.219) BETA(KK)=.38394
      IF(KK.GE.220.AND.KK.LE.223) BETA(KK)=.17452
      IF(KK.GE.224.AND.KK.LE.227) BETA(KK)=.38394
      IF(KK.GE.228.AND.KK.LE.231) BETA(KK)=.17452
      IF(KK.GE.232.AND.KK.LE.235) BETA(KK)=1.2216
      IF(KK.GE.236.AND.KK.LE.239) BETA(KK)=.69808
      IF(KK.GE.240.AND.KK.LE.243) BETA(KK)=1.2216
      IF(KK.GE.244.AND.KK.LE.247) BETA(KK)=.69808
      IF(KK.GE.248.AND.KK.LE.251) BETA(KK)=2.4433
      IF(KK.GE.252.AND.KK.LE.255) BETA(KK)=1.91972
      IF(KK.GE.256.AND.KK.LE.259) BETA(KK)=2.4433
      IF(KK.GE.260.AND.KK.LE.263) BETA(KK)=1.91972
      IF(KK.GE.264.AND.KK.LE.267) BETA(KK)=2.9668
      IF(KK.GE.268.AND.KK.LE.271) BETA(KK)=2.7574
      IF(KK.GE.272.AND.KK.LE.275) BETA(KK)=2.9668
      IF(KK.GE.276.AND.KK.LE.279) BETA(KK)=2.7574
      IF(KK.GE.280.AND.KK.LE.319) BETA(KK)=3.14136
      IF(KK.GE.320.AND.KK.LE.331) BETA(KK)=3.29843
      IF(KK.GE.332.AND.KK.LE.354) BETA(KK)=3.40314
      IF(KK.GE.355.AND.KK.LE.376) BETA(KK)=0.0
C     IF(KK.GE.377.AND.KK.LE.389) BETA(KK)=1.57079
 51   CONTINUE
        READ(5,200)(IG(I),I=1,482)
C       WRITE(6,200)(IG(I),I=1,482)
        READ(5,200)(IS(I),I=1,482)
C       WRITE(6,200)(IS(I),I=1,482)
200     FORMAT(5(6X,I5,5X))
         DO 10 L = 1,376
         READ(5,777) NM,I,J,K,N,X(I),Y(I),X(J),Y(J),X(K),Y(K),X(N),Y(N)
C       WRITE(6,777) NM,I,J,K,N,X(I),Y(I),X(J),Y(J),X(K),Y(K),X(N),Y(N)
          IE(L,1) = NM
          IE(L,2)  = I
          IE(L,3) =  J
          IE(L,4) =  K
          IE(L,5) =  N
10     CONTINUE
777    FORMAT(5I4,8F7.4)
       READ(5,666) (T(I), I = 1,482)
C     WRITE(6,666) (T(I), I = 1,482)
       DO 12 I = 1,482
12     TG(IG(I))=T(IS(I))
666    FORMAT(9F8.4)
      MID(1) =1
       DO 50 I = 2,376
        IF((TIPE(I).NE.TIPE(I-1)).OR.(BETA(I).NE.BETA(I-1)))GO TO 25
         MID(I) = MID(I-1)
         GO TO 50
25       MID(I) = MID(I-1) + 1
50     CONTINUE
```

```
          IT = 0
       DO 70 I = 1,376
       IF(MID(I).GE.IT)  GO TO 15
15         IT = MID(I)
         BI(IT) = BETA(I)
         PT(IT) = TIPE(I)
         WRITE(6,16)I,  TIPE(I), BETA(I), IT
C       WRITE(6,66) IT,PT(IT)
70     CONTINUE
16     FORMAT(I5,5X,A4,F10.4, I5)
       DO  30 I = 1,482
        TA(I) = 90.0 + TG(I)
      WRITE(7,555) I,X(I),Y(I),TA(I)
30     CONTINUE
555    FORMAT(I5,40X,2F10.4,5X,F10.4)
       DO 80 I=1,IT
C       WRITE(6,66) I, PT(I)
       BII = BI(I)*180.0/PI
      WRITE(7,11) I,BII
       IF(PT(I).EQ.'BIR') GO TO  7
       IF(PT(I).EQ.'FIR') GO TO 17
       IF(PT(I).EQ.'PAP') GO TO 27
 7    WRITE(7,22) TI,(PROB(1,J), J=1,7)
      WRITE(7,33) (ALFA(1,J), J =1,3)
       GO TO 80
 17   WRITE(7,22) TI,(PROB(2,J), J=1,7)
      WRITE(7,33) (ALFA(2,J), J =1,3)
       GO TO 80
 27   WRITE(7,22) TI,(PROB(3,J), J=1,7)
      WRITE(7,33) (ALFA(3,J), J =1,3)
 80    CONTINUE
66     FORMAT(I5,5X,A4)
 11    FORMAT(I5,25X,F10.4)
 22    FORMAT(4F10.1,3F10.8,F10.1)
 33    FORMAT(3F10.8)
       TH=1.000
        N= 4
        TR = 70.00
C        M =1
       DO 40 I =1,376
       WRITE(7,444) (IE(I,J),J=1,5),MID(I),TR, N, TH
40     CONTINUE
444    FORMAT(6I5,F10.4,10X,I5,5X,F10.4)
       STOP
       END
```

```
//UOFT1230 JOB (UT,
// 06250065,2,,,V)
//STEP1 EXEC SAPIV
//FT06F001 DD  SYSOUT=V,OUTLIM=1000000
//GO.SYSIN DD *
 THERMAL STRESSES IN THE BLADE  USING PLANE STRAIN APPROACH
  496    1    1
    1   -1              -1   -1   -1          4.3519   13.0728        147.8842
    2                                         3.8200   12.5000        144.3767
    3                                         3.2448   14.0923        150.2360
    4                                         2.6075   13.3675        147.7226
    5                                         5.0275   13.6888        150.4952
    6                                         4.0394   14.8344        152.0367
    7                                         3.4319   11.9703        139.9296
    8                                         2.1273   12.6598        144.3721
    9                                         2.1441   15.1056        154.4340
   10                                         1.4000   14.2300        154.0150
   11                                         3.0588   15.9725        154.7096
   12                                         0.8266   13.3456        153.5614
   13                                         5.8469   14.3478        152.3099
   14                                         4.9911   15.5936        153.2852
   15                                         4.1441   16.8306        154.9098
   16                                         3.1875   11.4838        134.7187
   17                                         1.8044   11.9694        139.7209
   18                                         0.4237   12.4525        152.5827
   19                                         2.0344   15.2103        154.7712
   20                                         1.2800   14.3200        154.5201
   21                                         2.9625   16.0887        154.9232
   22                                         0.6994   13.4178        154.2866
   23                                         4.0644   16.9553        155.0355
   24                                         0.2925   12.5037        153.5707
   25                                         6.8100   15.0500        153.5261
   26                                         6.1000   16.3700        154.1107
   27                                         5.4000   17.6800        155.0395
   28                                         5.3400   17.8100        155.1139
   29                                         3.0869   11.0403        129.1960
   30                                         1.6386   11.2961        133.0223
   31                                         0.1916   11.5506        150.4510
   32                                         0.0594   11.5778        154.5046
   33                                         7.2091   15.3441        153.9100
   34                                         6.5538   16.6739        154.3554
   35                                         5.9059   18.0200        155.0804
   36                                         5.8544   18.1544        155.1307
   37                                         3.1300   10.6400        124.1252
   38                                         1.6300   10.6400        123.5315
   39                                         0.1300   10.6400        123.5111
   40                                         0.0000   10.6400        123.9204
   41                                         7.8038   15.6287        154.2687
   42                                         7.2100   16.9706        154.5677
   43                                         6.6213   18.3550        155.1068
   44                                         6.5775   18.4925        155.1460
   45                                         3.0397   10.2559        119.1247
   46                                         1.5559   10.0748        115.2346
   47                                         0.0772    9.8925         97.1668
```

48	-0.0594	9.8781	92.0556
49	8.5941	15.9040	154.5623
50	8.0688	17.2601	154.7453
51	7.5459	18.6850	155.1289
52	7.5094	18.8243	155.1588
53	3.0913	9.8112	113.2342
54	1.6412	9.4569	108.1028
55	0.2013	9.1000	93.2964
56	0.0625	9.0725	91.9792
57	9.5800	16.1700	154.7605
58	9.1300	17.5425	154.8743
59	8.6800	19.0100	155.1474
60	8.6500	19.1500	155.1694
61	3.2847	9.3059	107.4809
62	1.8859	8.7861	102.8803
63	0.5022	8.2625	91.9885
64	0.3656	8.2231	91.1432
65	10.7616	16.4266	154.8534
66	10.3938	17.8177	154.9407
67	10.0234	19.3300	155.1605
68	9.9994	19.4693	155.1775
69	3.6200	8.7400	102.4331
70	2.2900	8.0625	98.9507
71	0.9800	7.3800	91.4340
72	0.8500	7.3300	90.8650
73	12.1388	16.6737	154.8177
74	11.8600	18.0856	154.9131
75	11.5763	19.6450	155.1579
76	11.5575	19.7825	155.1759
77	4.0972	8.1134	98.3440
78	2.8534	7.2861	95.8928
79	1.6347	6.4525	90.9115
80	1.5156	6.3931	90.5528
81	13.7116	16.9116	154.5817
82	13.5288	18.3464	154.7357
83	13.3384	19.9550	155.1338
84	13.3244	20.0894	155.1635
85	4.7163	7.4263	95.3039
86	3.5763	6.4569	93.6887
87	2.4663	5.4800	90.5535
88	2.3625	5.4125	90.3444
89	15.4800	17.1400	153.8904
90	15.4000	18.6000	154.2581
91	15.3100	20.2600	155.0557
92	15.3000	20.3900	155.1067
93	5.4772	6.6784	93.2149
94	4.4584	5.5748	92.1772
95	3.4747	4.4625	90.3037
96	3.3906	4.3881	90.1936
97	16.3600	17.2000	153.0317
98	16.6300	17.7400	152.9341
99	15.8000	17.8000	153.7650
100	15.8025	18.9350	154.2794
101	15.8000	20.2600	155.0328

102	15.8000	20.3900	155.0989
103	6.3800	5.8700	91.8505
104	5.5000	4.6400	91.1968
105	4.6600	3.4000	90.1492
106	4.6000	3.3200	90.0924
107	16.8200	17.2300	152.0987
108	16.9700	18.0400	152.8914
109	17.0800	18.8300	153.7508
110	16.8200	18.2800	153.2712
111	16.3800	18.3600	153.6377
112	16.3400	19.2200	154.3084
113	16.3000	20.2600	155.0112
114	16.3000	20.3900	155.0851
115	6.7350	5.5134	91.4067
116	5.9581	4.2261	90.8833
117	5.2137	2.9275	90.1065
118	5.1578	2.8425	90.0704
119	17.2200	17.2200	150.9112
120	17.2200	18.3000	153.1369
121	17.2200	19.3400	154.2458
122	16.7600	19.0000	154.0092
123	17.2200	19.4600	154.3388
124	16.7600	19.5750	154.4896
125	16.7600	20.2600	154.9978
126	16.7600	20.3900	155.0772
127	7.2900	5.1663	90.9979
128	6.6150	3.8294	90.6383
129	5.9650	2.4800	90.0829
130	5.9137	2.3900	90.0547
131	17.8400	17.5400	151.4541
132	17.9050	18.4900	153.2845
133	17.2200	15.6538	144.1907
134	17.8725	15.7737	144.6731
135	17.9700	19.3600	154.2331
136	17.9700	19.5000	154.3391
137	17.2200	19.8400	154.6544
138	17.9700	19.8750	154.6646
139	17.2200	20.2600	154.9879
140	17.2200	20.3900	155.0715
141	8.0450	4.8284	90.6712
142	7.4706	3.4498	90.4450
143	6.9137	2.0575	90.0612
144	6.8678	1.9625	90.0401
145	18.4700	17.8600	152.5973
146	18.4700	18.6700	153.6167
147	18.4700	15.8938	145.1270
148	18.4700	19.3600	154.2830
149	17.2200	14.1600	138.0302
150	17.9050	14.1600	138.0316
151	18.4700	14.1600	138.0318
152	18.4700	19.5400	154.4113
153	18.4700	19.9100	154.7148
154	17.9700	20.2600	154.9807
155	18.4700	20.2600	154.9871

156	17.9700	20.3900	155.0665
157	9.0000	4.5000	90.4415
158	8.5250	3.0875	90.3062
159	8.0600	1.6600	90.0439
160	8.0200	1.5600	90.0285
161	19.4700	17.8700	153.7898
162	19.4700	18.6550	154.0946
163	19.4700	19.3700	154.5283
164	19.4700	19.5200	154.6021
165	17.2200	12.7388	132.1555
166	17.9375	12.6987	132.0249
167	18.4700	12.6587	131.8744
168	19.4700	19.8925	154.8245
169	19.4700	20.2600	155.0414
170	18.4700	20.3900	155.0680
171	19.4700	20.3900	155.1040
172	10.1550	4.1809	90.3129
173	9.7781	2.7423	90.2227
174	9.4038	1.2875	90.0314
175	9.3703	1.1825	90.0198
176	20.4700	17.8800	154.1075
177	20.4700	18.6400	154.3112
178	20.4700	19.3800	154.7841
179	20.4700	19.5100	154.8236
180	20.4700	19.8800	154.9594
181	17.2200	11.3900	126.2683
182	17.9700	11.3900	126.7595
183	18.4700	11.3900	126.8414
184	20.4700	20.2600	155.0976
185	20.4700	20.3900	155.1358
186	11.5100	3.8713	90.2962
187	11.2300	2.4144	90.2166
188	10.9450	0.9400	90.0313
189	10.9187	0.8300	90.0196
190	21.7062	19.3500	155.1174
191	21.7012	19.4887	155.1178
192	21.7181	19.8631	155.1418
193	21.7325	20.2350	155.1785
194	17.2200	10.6400	124.3878
195	17.9700	10.6400	124.4096
196	16.4700	10.6400	124.3720
197	16.4700	11.3900	125.3677
198	18.4700	10.6400	124.4140
199	21.7387	20.3550	155.1893
200	13.0650	3.5709	90.4361
201	12.8806	2.1036	90.3264
202	12.6838	0.6175	90.0457
203	12.6653	0.5025	90.0261
204	22.9400	19.3000	155.1814
205	22.9400	19.4400	155.1815
206	22.9675	19.8175	155.1866
207	22.9900	20.1800	155.1946
208	23.0000	20.3000	155.1970
209	17.2200	9.8500	122.3997

210	17.9700	9.8500	121.9564
211	16.4700	9.8500	123.2855
212	18.4700	9.8500	121.8808
213	14.8200	3.2800	90.9077
214	14.7300	1.8100	90.6688
215	14.6200	0.3200	90.1157
216	14.6100	0.2000	90.0768
217	24.1712	19.2300	155.1958
218	24.1862	19.3637	155.1959
219	24.2181	19.7431	155.1970
220	24.2425	20.0950	155.1988
221	24.2537	20.2250	155.1994
222	17.2200	8.1750	115.1947
223	17.9400	8.2131	115.3302
224	18.4700	8.2537	115.4882
225	15.2600	2.7000	91.1052
226	15.2650	1.4925	90.7231
227	16.0200	3.2000	91.7380
228	16.3000	2.6500	91.8801
229	15.2600	0.2800	90.1457
230	15.2400	0.1500	90.0878
231	25.4000	19.1400	155.1987
232	25.4400	19.2600	155.1988
233	25.4700	19.6400	155.1991
234	25.4900	19.9800	155.1997
235	25.5000	20.1300	155.1999
236	17.2200	6.5000	108.2843
237	17.9100	6.4975	108.2734
238	18.4700	6.5000	108.2838
239	15.9800	2.1000	91.3425
240	15.9400	1.1600	90.7478
241	16.6000	2.1200	91.7607
242	15.9000	0.2300	90.1710
243	16.6000	3.1600	92.6067
244	16.7350	2.3650	92.1014
245	16.8800	1.5800	91.3814
246	15.8800	0.1000	90.1029
247	27.4722	18.9144	155.1998
248	27.5022	19.0455	155.1998
249	27.5397	19.4275	155.1999
250	27.5722	19.7844	155.2000
251	27.5855	19.8969	155.2000
252	17.2200	4.8250	101.3809
253	17.8800	4.7031	100.8879
254	18.4700	4.5887	100.4528
255	16.6000	1.5100	91.2262
256	16.5800	0.8375	90.6678
257	16.5600	0.2000	90.1982
258	16.5500	0.0700	90.1203
259	17.2200	3.1500	94.2286
260	17.2200	2.1000	92.0724
261	17.2200	1.0500	90.9383
262	17.2200	0.9300	90.8391
263	29.5188	18.6544	155.2000

264	29.5422	18.7922	155.2000
265	29.5856	19.1733	155.2000
266	29.6289	19.5444	155.2000
267	29.6455	19.6355	155.2000
268	17.8500	2.8300	93.6769
269	18.4700	2.5200	92.5586
270	17.2200	0.5200	90.4926
271	17.2200	0.1700	90.2098
272	17.2200	0.0500	90.1317
273	17.9100	1.9350	91.9496
274	17.9700	1.0300	90.9540
275	17.9700	0.9100	90.8619
276	17.9700	0.5200	90.5194
277	31.5400	18.3600	155.2000
278	31.5600	18.5000	155.2000
279	31.6075	18.8775	155.2000
280	31.6600	19.2600	155.2000
281	31.6800	19.3400	155.2000
282	18.4700	1.7800	91.6346
283	19.4700	2.5400	91.3945
284	19.4700	1.7900	91.1279
285	17.9700	0.1600	90.2209
286	17.9700	0.0300	90.1343
287	18.4700	1.0200	90.8996
288	18.4700	0.9000	90.8143
289	18.4700	0.5200	90.5006
290	18.4700	0.1400	90.2044
291	33.5355	18.0311	155.2000
292	33.5555	18.1689	155.2000
293	33.6055	18.5400	155.2000
294	33.6655	18.9311	155.2000
295	33.6888	19.0122	155.2000
296	19.4700	1.0300	90.6696
297	20.4700	2.5600	91.1005
298	20.4700	1.8000	90.9125
299	20.4700	1.0400	90.4442
300	18.4700	0.0200	90.1300
301	19.4700	0.9000	90.6054
302	19.4350	0.5150	90.3788
303	19.4100	0.1400	90.1577
304	19.4100	0.0200	90.0994
305	35.5055	17.6678	155.2000
306	35.5289	17.7989	155.2000
307	35.5797	18.1608	155.2000
308	35.6455	18.5578	155.2000
309	35.6722	18.6522	155.2000
310	20.4700	0.9100	90.3968
311	21.2187	1.0387	90.1452
312	21.2175	0.9162	90.1430
313	20.4700	0.5200	90.2397
314	20.4900	0.1500	90.0937
315	20.4700	0.0400	90.0601
316	37.4500	17.2700	155.2000
317	37.4800	17.3900	155.2000

318	37.5299	17.7400	155.2000
319	37.6000	18.1400	155.2000
320	37.6300	18.2600	155.2000
321	21.2100	0.5300	90.1030
322	22.2900	1.0800	90.0357
323	22.2900	0.9600	90.0355
324	22.2850	0.5800	90.0275
325	21.2175	0.1538	90.0439
326	21.2100	0.0375	90.0284
327	37.8422	17.2166	155.2000
328	37.8555	17.3455	155.2000
329	37.8680	17.7036	155.2000
330	37.8988	18.1066	155.2000
331	37.9122	18.2377	155.2000
332	22.2900	0.2000	90.0110
333	23.6837	1.1637	90.0063
334	23.6875	1.0413	90.0062
335	23.6950	0.6700	90.0048
336	23.7075	0.2887	90.0019
337	22.2900	0.0800	90.0062
338	38.8589	16.9933	155.2000
339	38.8622	17.1289	155.2000
340	38.8555	17.4911	155.2000
341	38.8655	17.8933	155.2000
342	38.8689	18.0311	155.2000
343	23.7100	0.1675	90.0010
344	25.4000	1.2900	90.0013
345	25.4100	1.1600	90.0013
346	25.4400	0.8000	90.0009
347	25.4700	0.4200	90.0002
348	25.4700	0.3000	90.0001
349	40.5000	16.6000	155.2000
350	40.5000	16.7400	155.2000
351	40.4925	17.1025	155.2000
352	40.5000	17.5000	155.2000
353	40.5000	17.6400	155.2000
354	27.3933	1.5367	90.0002
355	27.4111	1.4111	90.0002
356	27.4577	1.0478	90.0001
357	27.5011	0.6711	90.0000
358	27.5155	0.5456	90.0000
359	42.7655	16.0367	155.2000
360	42.7689	16.1789	155.2000
361	42.7788	16.5378	155.2000
362	42.8022	16.9267	155.2000
363	42.8055	17.0644	155.2000
364	29.3733	1.8133	90.0000
365	29.3978	1.6911	90.0000
366	29.4577	1.3244	90.0000
367	29.5111	0.9511	90.0000
368	29.5355	0.8222	90.0000
369	45.6555	15.3033	155.2000
370	45.6689	15.4456	155.2000
371	45.7147	15.7970	155.2000

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372	45.7722	16.1733	155.2000
373	45.7855	16.3044	155.2000
374	31.3400	2.1200	90.0000
375	31.3700	2.0000	90.0000
376	31.4400	1.6300	90.0000
377	31.5000	1.2600	90.0000
378	31.5300	1.1300	90.0000
379	49.1700	14.4000	155.2000
380	49.2000	14.5400	155.2000
381	49.2999	14.8800	155.2000
382	49.4100	15.2400	155.2000
383	49.4400	15.3600	155.2000
384	33.2933	2.4567	90.0000
385	33.3277	2.3378	90.0000
386	33.4044	1.9644	90.0000
387	33.4677	1.5978	90.0000
388	33.4989	1.4689	90.0000
389	50.4525	14.0200	155.2000
390	50.5025	14.1600	155.2000
391	50.6056	14.5037	155.2000
392	50.7162	14.8625	155.2000
393	50.7450	14.9675	155.2000
394	35.2333	2.8233	90.0000
395	35.2711	2.7044	90.0000
396	35.3511	2.3278	90.0000
397	35.4144	1.9644	90.0000
398	35.4422	1.8389	90.0000
399	51.7400	13.6400	155.2000
400	51.8000	13.7800	155.2000
401	51.9075	14.1250	155.2000
402	52.0200	14.4800	155.2000
403	52.0500	14.5800	155.2000
404	37.1600	3.2200	90.0000
405	37.2000	3.1000	90.0000
406	37.2800	2.7200	90.0000
407	37.3400	2.3600	90.0000
408	37.3600	2.2400	90.0000
409	53.0325	13.2600	155.2000
410	53.0925	13.4000	155.2000
411	53.2056	13.7437	155.2000
412	53.3212	14.0925	155.2000
413	53.3550	14.1975	155.2000
414	39.1844	3.6967	90.0000
415	39.2222	3.5822	90.0000
416	39.3083	3.1958	90.0000
417	39.3811	2.8344	90.0000
418	39.4156	2.7244	90.0000
419	54.3300	12.8800	155.2000
420	54.3800	13.0200	155.2000
421	54.5000	13.3600	155.2000
422	54.6200	13.7000	155.2000
423	54.6600	13.8200	155.2000
424	41.2044	4.1933	90.0000
425	41.2422	4.0822	90.0000

426	41.3333	3.6933	90.0000
427	41.4178	3.3344	90.0000
428	41.4622	3.2278	90.0000
429	55.0600	12.6600	155.2000
430	55.0600	12.8300	155.2000
431	54.1000	12.1600	155.2000
432	55.0600	11.8600	155.2000
433	55.0600	13.2100	155.2000
434	55.0600	13.5800	155.2000
435	55.0600	13.7000	155.2000
436	43.2200	4.7100	90.0000
437	43.2600	4.6000	90.0000
438	43.3549	4.2125	90.0000
439	43.4500	3.8600	90.0000
440	43.5000	3.7500	90.0000
441	45.2311	5.2467	90.0000
442	45.2755	5.1355	90.0000
443	45.3733	4.7533	90.0000
444	45.4777	4.4111	90.0000
445	45.5289	4.2911	90.0000
446	47.2377	5.8033	90.0000
447	47.2888	5.6889	90.0000
448	47.3883	5.3158	90.0000
449	47.5011	4.9878	90.0000
450	47.5488	4.8511	90.0000
451	49.2400	6.3800	90.0000
452	49.3000	6.2600	90.0000
453	49.4000	5.9000	90.0000
454	49.5200	5.5900	90.0000
455	49.5600	5.4300	90.0000
456	50.5250	6.7750	90.0000
457	50.5550	6.6475	90.0000
458	50.6637	6.2981	90.0000
459	50.7825	5.9812	90.0000
460	50.8250	5.6675	90.0000
461	51.8000	7.1800	90.0000
462	51.8200	7.0500	90.0000
463	51.9350	6.7075	90.0000
464	52.0500	6.3800	90.0000
465	52.1000	6.0200	90.0000
466	53.0650	7.5950	90.0000
467	53.0950	7.4675	90.0000
468	53.2137	7.1281	90.0000
469	53.3225	6.7863	90.0000
470	53.3850	6.4875	90.0000
471	54.3200	8.0200	90.0000
472	54.3800	7.9000	90.0000
473	54.5000	7.5600	90.0000
474	54.6000	7.2000	90.0000
475	54.6800	7.0700	90.0000
476	55.0600	8.2600	90.0000
477	55.0600	8.1400	90.0000
478	55.0600	9.0500	90.0000
479	54.0800	8.7400	90.0000

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  480                                           55.0600    7.7300         90.0000
  481                                           55.0600    7.3400         90.0000
  482                                           55.0600    7.2000         90.0000
  483                                           55.0600    10.455        122.6000
  484                                           55.3100    13.700        155.2000
  485                                           55.3100    13.640        155.2000
  486                                           55.3100    13.210        155.2000
  487                                           55.3100    12.830        155.2000
  488                                           55.3100    12.660        155.2000
  489                                           55.3100    11.860        155.2000
  490                                           55.3100    10.455        122.6000
  491                                           55.3100    9.0500         90.0000
  492                                           55.3100    8.2600         90.0000
  493                                           55.3100    8.1400         90.0000
  494                                           55.3100    7.7300         90.0000
  495                                           55.3100    7.3400         90.0000
  496                                           55.3100    7.2000         90.0000
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    7                           39.9970
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    8                          139.9907
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    9                          109.9917
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   10                          169.9851
      70.0  770000.0  164000.0 1380000.00.440000000.166000010.25500000    76000.0
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   11                          157.9873
      70.0  770000.0  164000.0 1380000.00.440000000.166000010.25500000    76000.0
0.000027050.000030380.00001457
   12                          179.9866
      70.0  770000.0  164000.0 1380000.00.440000000.166000010.25500000    76000.0
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   14                           194.9855
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   15                           188.9861
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0.000027050.000030380.00001457
   16                           179.9866
      70.0  770000.0  164000.0 1380000.00.440000000.166000010.25500000   76000.0
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   17                             0.0000
      70.0  770000.0  164000.0 1380000.00.440000000.166000010.25500000   76000.0
0.000027050.000030380.00001457
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   19                           -15.0000
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   23                             0.0000
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   25                             9.9993
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   26                            21.9981
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   27                             9.9993
      70.0   97500.0  132600.0 1950000.00.287000000.022000000.02000000   14000.0
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   28                            69.9925
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   29                            39.9970
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    32                               139.9907
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    33                               109.9917
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    34                               139.9907
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    35                               109.9917
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    36                               169.9851
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0.000034900.000025900.00000210
    37                               157.9873
       70.0    97500.0   132600.0 1950000.00.287000000.022000000.02000000    14000.0
0.000034900.000025900.00000210
    38                               169.9851
       70.0    97500.0   132600.0 1950000.00.287000000.022000000.02000000    14000.0
0.000034900.000025900.00000210
    39                               157.9873
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    40                               179.9866
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    44                                 0.0000
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    1  422  434  435  423     1     70.0000              4          1.0000
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 18  184  193  199  185    3   70.0000              4          1.0000
 19  193  207  208  199    3   70.0000              4          1.0000
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 22  155  169  171  170    3   70.0000              4          1.0000
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 26  113  125  126  114    3   70.0000              4          1.0000
 27  125  139  140  126    3   70.0000              4          1.0000
 28   91  101  102   92    3   70.0000              4          1.0000
 29  101  113  114  102    3   70.0000              4          1.0000
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 36   75   83   84   76    5   70.0000              4          1.0000
 37   83   91   92   84    5   70.0000              4          1.0000
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 39   31   18   24   32    6   70.0000              4          1.0000
 40   18   12   22   24    6   70.0000              4          1.0000
 41   12   10   20   22    6   70.0000              4          1.0000
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 44   11   15   23   21    7   70.0000              4          1.0000
 45   15   27   28   23    7   70.0000              4          1.0000
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 48   87   79   80   88    8   70.0000              4          1.0000
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 52   55   47   48   56    9   70.0000              4          1.0000
 53   47   39   40   48    9   70.0000              4          1.0000
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 55  202  188  189  203   10   70.0000              4          1.0000
 56  188  174  175  189   10   70.0000              4          1.0000
 57  174  159  160  175   10   70.0000              4          1.0000
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 59  143  129  130  144   11   70.0000              4          1.0000
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62	242	229	230	246	12	70.0000	4	1.0000
63	229	215	216	230	12	70.0000	4	1.0000
64	271	257	258	272	12	70.0000	4	1.0000
65	257	242	246	258	12	70.0000	4	1.0000
66	290	285	286	300	12	70.0000	4	1.0000
67	285	271	272	286	12	70.0000	4	1.0000
68	314	303	304	315	12	70.0000	4	1.0000
69	303	290	300	304	12	70.0000	4	1.0000
70	347	336	343	348	12	70.0000	4	1.0000
71	336	332	337	343	12	70.0000	4	1.0000
72	332	325	326	337	12	70.0000	4	1.0000
73	325	314	315	326	12	70.0000	4	1.0000
74	407	397	398	408	13	70.0000	4	1.0000
75	397	387	388	398	13	70.0000	4	1.0000
76	387	377	378	388	13	70.0000	4	1.0000
77	377	367	368	378	13	70.0000	4	1.0000
78	367	357	358	368	13	70.0000	4	1.0000
79	357	347	348	358	13	70.0000	4	1.0000
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81	449	444	445	450	14	70.0000	4	1.0000
82	444	439	440	445	14	70.0000	4	1.0000
83	439	427	428	440	14	70.0000	4	1.0000
84	427	417	418	428	14	70.0000	4	1.0000
85	417	407	408	418	14	70.0000	4	1.0000
86	474	469	470	475	14	70.0000	4	1.0000
87	469	464	465	470	14	70.0000	4	1.0000
88	464	459	460	465	14	70.0000	4	1.0000
89	459	454	455	460	14	70.0000	4	1.0000
90	481	474	475	482	14	70.0000	4	1.0000
91	476	471	472	477	14	70.0000	4	1.0000
92	471	466	467	472	14	70.0000	4	1.0000
93	466	461	462	467	14	70.0000	4	1.0000
94	461	456	457	462	14	70.0000	4	1.0000
95	456	451	452	457	14	70.0000	4	1.0000
96	451	446	447	452	14	70.0000	4	1.0000
97	446	441	442	447	14	70.0000	4	1.0000
98	441	436	437	442	14	70.0000	4	1.0000
99	436	424	425	437	14	70.0000	4	1.0000
100	424	414	415	425	14	70.0000	4	1.0000
101	414	404	405	415	14	70.0000	4	1.0000
102	404	394	395	405	15	70.0000	4	1.0000
103	394	384	385	395	15	70.0000	4	1.0000
104	384	374	375	385	15	70.0000	4	1.0000
105	374	364	365	375	15	70.0000	4	1.0000
106	364	354	355	365	15	70.0000	4	1.0000
107	354	344	345	355	15	70.0000	4	1.0000
108	344	333	334	345	16	70.0000	4	1.0000
109	333	322	323	334	16	70.0000	4	1.0000
110	322	311	312	323	16	70.0000	4	1.0000
111	311	299	310	312	16	70.0000	4	1.0000
112	299	296	301	310	16	70.0000	4	1.0000
113	296	287	288	301	16	70.0000	4	1.0000

114	287	274	275	288	16	70.0000	4	1.0000
115	274	261	262	275	16	70.0000	4	1.0000
116	121	135	136	123	17	70.0000	4	1.0000
117	135	148	152	136	17	70.0000	4	1.0000
118	148	163	164	152	17	70.0000	4	1.0000
119	163	178	179	164	17	70.0000	4	1.0000
120	178	190	191	179	17	70.0000	4	1.0000
121	190	204	205	191	17	70.0000	4	1.0000
122	204	217	218	205	17	70.0000	4	1.0000
123	217	231	232	218	17	70.0000	4	1.0000
124	231	247	248	232	18	70.0000	4	1.0000
125	247	263	264	248	18	70.0000	4	1.0000
126	263	277	278	264	18	70.0000	4	1.0000
127	277	291	292	278	18	70.0000	4	1.0000
128	291	305	306	292	18	70.0000	4	1.0000
129	305	316	317	306	18	70.0000	4	1.0000
130	316	327	328	317	19	70.0000	4	1.0000
131	327	338	339	328	19	70.0000	4	1.0000
132	338	349	350	339	19	70.0000	4	1.0000
133	349	359	360	350	19	70.0000	4	1.0000
134	359	369	370	360	19	70.0000	4	1.0000
135	369	379	380	370	19	70.0000	4	1.0000
136	379	389	390	380	19	70.0000	4	1.0000
137	389	399	400	390	19	70.0000	4	1.0000
138	399	409	410	400	19	70.0000	4	1.0000
139	409	419	420	410	19	70.0000	4	1.0000
140	419	429	430	420	19	70.0000	4	1.0000
141	431	432	429	419	20	70.0000	4	1.0000
142	421	433	434	422	20	70.0000	4	1.0000
143	420	430	433	421	20	70.0000	4	1.0000
144	381	391	392	382	20	70.0000	4	1.0000
145	391	401	402	392	20	70.0000	4	1.0000
146	401	411	412	402	20	70.0000	4	1.0000
147	411	421	422	412	20	70.0000	4	1.0000
148	380	390	391	381	20	70.0000	4	1.0000
149	390	400	401	391	20	70.0000	4	1.0000
150	400	410	411	401	20	70.0000	4	1.0000
151	410	420	421	411	20	70.0000	4	1.0000
152	318	329	330	319	21	70.0000	4	1.0000
153	329	340	341	330	21	70.0000	4	1.0000
154	340	351	352	341	21	70.0000	4	1.0000
155	351	361	362	352	21	70.0000	4	1.0000
156	361	371	372	362	21	70.0000	4	1.0000
157	371	381	382	372	21	70.0000	4	1.0000
158	317	328	329	318	21	70.0000	4	1.0000
159	328	339	340	329	21	70.0000	4	1.0000
160	339	350	351	340	21	70.0000	4	1.0000
161	350	360	361	351	21	70.0000	4	1.0000
162	360	370	371	361	21	70.0000	4	1.0000
163	370	380	381	371	21	70.0000	4	1.0000
164	233	249	250	234	22	70.0000	4	1.0000
165	249	265	266	250	22	70.0000	4	1.0000
166	265	279	280	266	22	70.0000	4	1.0000
167	279	293	294	280	22	70.0000	4	1.0000

168	293	307	308	294	22	70.0000	4	1.0000
169	307	318	319	308	22	70.0000	4	1.0000
170	232	248	249	233	22	70.0000	4	1.0000
171	248	264	265	249	22	70.0000	4	1.0000
172	264	278	279	265	22	70.0000	4	1.0000
173	278	292	293	279	22	70.0000	4	1.0000
174	292	306	307	293	22	70.0000	4	1.0000
175	306	317	318	307	22	70.0000	4	1.0000
176	180	192	193	184	23	70.0000	4	1.0000
177	192	206	207	193	23	70.0000	4	1.0000
178	206	219	220	207	23	70.0000	4	1.0000
179	219	233	234	220	23	70.0000	4	1.0000
180	179	191	192	180	23	70.0000	4	1.0000
181	191	205	206	192	23	70.0000	4	1.0000
182	205	218	219	206	23	70.0000	4	1.0000
183	218	232	233	219	23	70.0000	4	1.0000
184	153	168	169	155	23	70.0000	4	1.0000
185	168	180	184	169	23	70.0000	4	1.0000
186	152	164	168	153	23	70.0000	4	1.0000
187	164	179	180	168	23	70.0000	4	1.0000
188	137	138	154	139	23	70.0000	4	1.0000
189	138	153	155	154	23	70.0000	4	1.0000
190	123	136	138	137	23	70.0000	4	1.0000
191	136	152	153	138	23	70.0000	4	1.0000
192	146	162	163	148	23	70.0000	4	1.0000
193	162	177	178	163	23	70.0000	4	1.0000
194	145	161	162	146	23	70.0000	4	1.0000
195	161	176	177	162	23	70.0000	4	1.0000
196	120	132	135	121	23	70.0000	4	1.0000
197	132	146	148	135	23	70.0000	4	1.0000
198	119	131	132	120	23	70.0000	4	1.0000
199	131	145	146	132	23	70.0000	4	1.0000
200	98	108	109	110	23	70.0000	4	1.0000
201	108	120	121	109	23	70.0000	4	1.0000
202	97	107	108	98	23	70.0000	4	1.0000
203	107	119	120	108	23	70.0000	4	1.0000
204	99	98	110	111	23	70.0000	4	1.0000
205	89	97	98	99	23	70.0000	4	1.0000
206	122	109	121	123	23	70.0000	4	1.0000
207	111	110	109	122	23	70.0000	4	1.0000
208	112	124	125	113	23	70.0000	4	1.0000
209	124	137	139	125	23	70.0000	4	1.0000
210	111	122	124	112	23	70.0000	4	1.0000
211	122	123	137	124	23	70.0000	4	1.0000
212	90	100	101	91	23	70.0000	4	1.0000
213	100	112	113	101	23	70.0000	4	1.0000
214	89	99	100	90	23	70.0000	4	1.0000
215	99	111	112	100	23	70.0000	4	1.0000
216	26	34	35	27	24	70.0000	4	1.0000
217	34	42	43	35	24	70.0000	4	1.0000
218	42	50	51	43	24	70.0000	4	1.0000
219	50	58	59	51	24	70.0000	4	1.0000
220	58	66	67	59	25	70.0000	4	1.0000
221	66	74	75	67	25	70.0000	4	1.0000

222	74	82	83	75	25	70.0000	4	1.0000
223	82	90	91	83	25	70.0000	4	1.0000
224	25	33	34	26	26	70.0000	4	1.0000
225	33	41	42	34	26	70.0000	4	1.0000
226	41	49	50	42	26	70.0000	4	1.0000
227	49	57	58	50	26	70.0000	4	1.0000
228	57	65	66	58	27	70.0000	4	1.0000
229	65	73	74	66	27	70.0000	4	1.0000
230	73	81	82	74	27	70.0000	4	1.0000
231	81	89	90	82	27	70.0000	4	1.0000
232	38	30	31	39	28	70.0000	4	1.0000
233	30	17	18	31	28	70.0000	4	1.0000
234	17	8	12	18	28	70.0000	4	1.0000
235	8	4	10	12	28	70.0000	4	1.0000
236	4	3	9	10	29	70.0000	4	1.0000
237	3	6	11	9	29	70.0000	4	1.0000
238	6	14	15	11	29	70.0000	4	1.0000
239	14	26	27	15	29	70.0000	4	1.0000
240	37	29	30	38	30	70.0000	4	1.0000
241	29	16	17	30	30	70.0000	4	1.0000
242	16	7	8	17	30	70.0000	4	1.0000
243	7	2	4	8	30	70.0000	4	1.0000
244	2	1	3	4	31	70.0000	4	1.0000
245	1	5	6	3	31	70.0000	4	1.0000
246	5	13	14	6	31	70.0000	4	1.0000
247	13	25	26	14	31	70.0000	4	1.0000
248	104	94	95	105	32	70.0000	4	1.0000
249	94	86	87	95	32	70.0000	4	1.0000
250	86	78	79	87	32	70.0000	4	1.0000
251	78	70	71	79	32	70.0000	4	1.0000
252	70	62	63	71	33	70.0000	4	1.0000
253	62	54	55	63	33	70.0000	4	1.0000
254	54	46	47	55	33	70.0000	4	1.0000
255	46	38	39	47	33	70.0000	4	1.0000
256	103	93	94	104	34	70.0000	4	1.0000
257	93	85	86	94	34	70.0000	4	1.0000
258	85	77	78	86	34	70.0000	4	1.0000
259	77	69	70	78	34	70.0000	4	1.0000
260	69	61	62	70	35	70.0000	4	1.0000
261	61	53	54	62	35	70.0000	4	1.0000
262	53	45	46	54	35	70.0000	4	1.0000
263	45	37	38	46	35	70.0000	4	1.0000
264	214	201	202	215	36	70.0000	4	1.0000
265	201	187	188	202	36	70.0000	4	1.0000
266	187	173	174	188	36	70.0000	4	1.0000
267	173	158	159	174	36	70.0000	4	1.0000
268	158	142	143	159	37	70.0000	4	1.0000
269	142	128	129	143	37	70.0000	4	1.0000
270	128	116	117	129	37	70.0000	4	1.0000
271	116	104	105	117	37	70.0000	4	1.0000
272	213	200	201	214	38	70.0000	4	1.0000
273	200	186	187	201	38	70.0000	4	1.0000
274	186	172	173	187	38	70.0000	4	1.0000
275	172	157	158	173	38	70.0000	4	1.0000

276	157	141	142	158	39	70.0000	4	1.0000
277	141	127	128	142	39	70.0000	4	1.0000
278	127	115	116	128	39	70.0000	4	1.0000
279	115	103	104	116	39	70.0000	4	1.0000
280	240	226	229	242	40	70.0000	4	1.0000
281	226	214	215	229	40	70.0000	4	1.0000
282	239	225	226	240	40	70.0000	4	1.0000
283	225	213	214	226	40	70.0000	4	1.0000
284	228	225	239	241	40	70.0000	4	1.0000
285	227	213	225	228	40	70.0000	4	1.0000
286	245	255	262	261	40	70.0000	4	1.0000
287	241	239	255	245	40	70.0000	4	1.0000
288	270	256	257	271	40	70.0000	4	1.0000
289	256	240	242	257	40	70.0000	4	1.0000
290	262	255	256	270	40	70.0000	4	1.0000
291	255	239	240	256	40	70.0000	4	1.0000
292	260	244	245	261	40	70.0000	4	1.0000
293	244	228	241	245	40	70.0000	4	1.0000
294	259	243	244	260	40	70.0000	4	1.0000
295	243	227	228	244	40	70.0000	4	1.0000
296	282	273	274	287	40	70.0000	4	1.0000
297	273	260	261	274	40	70.0000	4	1.0000
298	269	268	273	282	40	70.0000	4	1.0000
299	268	259	260	273	40	70.0000	4	1.0000
300	298	284	296	299	40	70.0000	4	1.0000
301	284	282	287	296	40	70.0000	4	1.0000
302	297	283	284	298	40	70.0000	4	1.0000
303	283	269	282	284	40	70.0000	4	1.0000
304	289	276	285	290	40	70.0000	4	1.0000
305	276	270	271	285	40	70.0000	4	1.0000
306	288	275	276	289	40	70.0000	4	1.0000
307	275	262	270	276	40	70.0000	4	1.0000
308	313	302	303	314	40	70.0000	4	1.0000
309	302	289	290	303	40	70.0000	4	1.0000
310	310	301	302	313	40	70.0000	4	1.0000
311	301	288	289	302	40	70.0000	4	1.0000
312	346	335	336	347	40	70.0000	4	1.0000
313	335	324	332	336	40	70.0000	4	1.0000
314	324	321	325	332	40	70.0000	4	1.0000
315	321	313	314	325	40	70.0000	4	1.0000
316	345	334	335	346	40	70.0000	4	1.0000
317	334	323	324	335	40	70.0000	4	1.0000
318	323	312	321	324	40	70.0000	4	1.0000
319	312	310	313	321	40	70.0000	4	1.0000
320	406	396	397	407	41	70.0000	4	1.0000
321	396	386	387	397	41	70.0000	4	1.0000
322	386	376	377	387	41	70.0000	4	1.0000
323	376	366	367	377	41	70.0000	4	1.0000
324	366	356	357	367	41	70.0000	4	1.0000
325	356	346	347	357	41	70.0000	4	1.0000
326	405	395	396	406	41	70.0000	4	1.0000
327	395	385	386	396	41	70.0000	4	1.0000
328	385	375	376	386	41	70.0000	4	1.0000
329	375	365	366	376	41	70.0000	4	1.0000

330	365	355	356	366	41	70.0000	4	1.0000
331	355	345	346	356	41	70.0000	4	1.0000
332	453	448	449	454	42	70.0000	4	1.0000
333	448	443	444	449	42	70.0000	4	1.0000
334	443	438	439	444	42	70.0000	4	1.0000
335	438	426	427	439	42	70.0000	4	1.0000
336	426	416	417	427	42	70.0000	4	1.0000
337	416	406	407	417	42	70.0000	4	1.0000
338	452	447	448	453	42	70.0000	4	1.0000
339	447	442	443	448	42	70.0000	4	1.0000
340	442	437	438	443	42	70.0000	4	1.0000
341	437	425	426	438	42	70.0000	4	1.0000
342	425	415	416	426	42	70.0000	4	1.0000
343	415	405	406	416	42	70.0000	4	1.0000
344	473	468	469	474	43	70.0000	4	1.0000
345	468	463	464	469	43	70.0000	4	1.0000
346	463	458	459	464	43	70.0000	4	1.0000
347	458	453	454	459	43	70.0000	4	1.0000
348	472	467	468	473	43	70.0000	4	1.0000
349	467	462	463	468	43	70.0000	4	1.0000
350	462	457	458	463	43	70.0000	4	1.0000
351	457	452	453	458	43	70.0000	4	1.0000
352	480	473	474	481	43	70.0000	4	1.0000
353	477	472	473	480	43	70.0000	4	1.0000
354	478	479	471	476	43	70.0000	4	1.0000
355	222	223	210	209	44	70.0000	4	1.0000
356	223	224	212	210	44	70.0000	4	1.0000
357	236	237	223	222	44	70.0000	4	1.0000
358	237	238	224	223	44	70.0000	4	1.0000
359	252	253	237	236	44	70.0000	4	1.0000
360	253	254	238	237	44	70.0000	4	1.0000
361	259	268	253	252	44	70.0000	4	1.0000
362	268	269	254	253	44	70.0000	4	1.0000
363	194	195	182	181	44	70.0000	4	1.0000
364	195	198	183	182	44	70.0000	4	1.0000
365	209	210	195	194	44	70.0000	4	1.0000
366	210	212	198	195	44	70.0000	4	1.0000
367	196	194	181	197	44	70.0000	4	1.0000
368	211	209	194	196	44	70.0000	4	1.0000
369	133	134	131	119	44	70.0000	4	1.0000
370	134	147	145	131	44	70.0000	4	1.0000
371	149	150	134	133	44	70.0000	4	1.0000
372	150	151	147	134	44	70.0000	4	1.0000
373	165	166	150	149	44	70.0000	4	1.0000
374	166	167	151	150	44	70.0000	4	1.0000
375	181	182	166	165	44	70.0000	4	1.0000
376	182	183	167	166	44	70.0000	4	1.0000
377	434	485	484	435	45	70.0000	4	1.0000
378	433	486	485	434	45	70.0000	4	1.0000
379	430	487	486	433	45	70.0000	4	1.0000
380	429	488	487	430	45	70.0000	4	1.0000
381	432	489	488	429	45	70.0000	4	1.0000
382	483	490	489	432	45	70.0000	4	1.0000
383	478	491	490	483	45	70.0000	4	1.0000

```
 384  476  492  491  478   45   70.0000             4          1.0000
 385  477  493  492  476   45   70.0000             4          1.0000
 386  480  494  493  477   45   70.0000             4          1.0000
 387  481  495  494  480   45   70.0000             4          1.0000
 388  482  496  495  481   45   70.0000             4          1.0000

      1.0


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//
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```
C
C   RADIAL-TANGENTIAL STRESS PRGRAM
C
       DIMENSION SZETA(90),SEATA(90),SZT(90),BETA(90)
      REAL S11, S22, S12, AA, BB
       INTEGER NN, NEL
      DO 20  KK = 1,90
      IF(KK.GE.1.AND.KK.LE.11) BETA(KK)=-.2618
      IF(KK.GE.12.AND.KK.LE.17) BETA(KK)=-.15707
      IF(KK.GE.18.AND.KK.LE.29) BETA(KK)=0.0
      IF(KK.GE.30.AND.KK.LE.33) BETA(KK)=.38394
      IF(KK.GE.34.AND.KK.LE.37) BETA(KK)=.17452
      IF(KK.GE.38.AND.KK.LE.41) BETA(KK)=1.22164
      IF(KK.GE.42.AND.KK.LE.45) BETA(KK)=.69808
      IF(KK.GE.46.AND.KK.LE.49) BETA(KK)=2.4433
      IF(KK.GE.50.AND.KK.LE.53)  BETA(KK)=1.91972
      IF(KK.GE. 54.AND.KK.LE.57)  BETA(KK)=2.9668
      IF(KK.GE. 58.AND.KK.LE.61)  BETA(KK)=2.7574
      IF(KK.GE. 62.AND.KK.LE.73)  BETA(KK)=3.14136
      IF(KK.GE. 74.AND.KK.LE.79)  BETA(KK)=3.29843
       IF(KK.GE. 80.AND.KK.LE.90) BETA(KK)=3.40314
 20    CONTINUE
         READ(5,11)NN
 11     FORMAT(I5)
         WRITE(6,15)
 15    FORMAT(//,10X,3HNEL,9X,6HS-ZETA,9X,6HS-EATA,9X,10HTUE-ZET-ET,//)
         DO 10 I=1,NN
          READ(5,22)  NEL,S11, S22, S12
          AA=(S11+S22)/2
          BB= (S11-S22)/2
           SZETA(NEL)=AA+BB*COS(2*BETA(NEL))+S12*SIN(2*BETA(NEL))
           SEATA(NEL)=AA-BB*COS(2*BETA(NEL))-S12*SIN(2*BETA(NEL))
           SZT(NEL) =-BB*SIN(2*BETA(NEL))+S12*COS(2*BETA(NEL))
           WRITE(6,33)NEL,SZETA(NEL),SEATA(NEL),SZT(NEL)
 10       CONTINUE
 22      FORMAT(I5,3E15.5)
 33      FORMAT(5X,I5,5X,3F15.3,/)
       STOP
       END
```

```
                    TEMPERATURE IN DEGREE  F

NODE NO.     TEMP.    NODE NO.    TEMP.    NODE NO.    TEMP.    NODE NO.     TEMP.

     1      64.771      2        64.015       3       64.434      4          64.520
     5      64.923      6        63.561       7       54.372      8          57.723
     9      64.710     10        60.236      11       64.287     12          65.035
    13      62.583     14        49.721      15       44.719     16          49.930
    17      54.377     18        64.910      19       62.037     20          57.884
    21      63.571     22        65.114      23       60.451     24          43.022
    25      39.196     26        65.039      27       63.285     28          64.111
    29      60.495     30        64.505      31       65.080     32          65.131
    33      33.511     34        33.532      35       34.125     36          64.355
    37      62.310     38        63.526      39       63.910     40          33.920
    41      65.107     42        65.146      43        7.167     44          25.235
    45      29.125     46        64.568      47       64.269     48           2.056
    49      65.129     50        65.159      51        3.296     52          18.103
    53      23.234     54        64.745      55       64.562     56           1.979
    57      65.147     58        65.169      59        1.989     60           1.143
    61      12.880     62        17.481      63       64.874     64          64.760
    65      65.161     66        65.177      67        1.434     68           0.865
    69       8.951     70        12.433      71       64.941     72          64.853
    73      65.158     74        65.176      75        0.911     76           0.553
    77       5.893     78         8.344      79       64.913     80          64.818
    81      65.134     82        65.163      83        0.554     84           0.344
    85       3.689     86         5.304      87       64.736     88          64.582
    89      65.056     90        65.107      91       64.258     92           0.304
    93       0.194     94         2.177      95        3.215     96          63.890
    97      65.033     98        65.099      99       64.279    100          63.765
   101       0.149    102         1.197     103        0.092    104           1.851
   105      63.032    106        65.011     107       65.085    108          64.308
   109      63.638    110        62.934     111        0.107    112           0.883
   113       1.407    114         0.070     115       62.099    116          64.998
   117      65.077    118        64.490     119       64.009    120          63.271
   121      62.891    122         0.083     123        0.638    124           0.998
   125       0.055    126        60.911     127       64.988    128          65.071
   129      64.654    130        64.339     131       63.751    132          64.246
   133      63.137    134         0.061     135        0.445    136           0.671
   137       0.040    138        61.454     139       54.191    140          54.673
   141      64.981    142        65.067     143       64.665    144          64.339
   145      64.233    146        63.285     147        0.044    148           0.306
   149       0.441    150         0.029     151       62.597    152          55.127
   153      48.030    154        48.032     155       48.032    156          64.987
   157      65.068    158        64.715     159       64.411    160          64.283
   161      63.617    162         0.031     163        0.223    164           0.313
   165       0.020    166        63.790     167       64.095    168          42.156
   169      42.025    170        41.874     171       65.041    172          65.104
   173      64.824    174        64.602     175       64.528    176           0.031
   177       0.217    178         0.296     179        0.020    180          64.107
   181      64.311    182        64.784     183       36.268    184          36.760
   185      36.841    186        65.098     187       65.136    188          64.959
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189        64.824  190        0.046  191        0.326  192        0.436
193         0.026  194       65.117  195       65.118  196       34.388
197        34.372  198       35.368  199       34.410  200       34.414
201        65.179  202       65.189  203       65.142  204        0.116
205         0.669  206        0.908  207        0.077  208       65.181
209        65.182  210       65.187  211       32.400  212       33.285
213        31.956  214       31.881  215       65.195  216       65.197
217         0.146  218        0.723  219        1.105  220        1.738
221         0.088  222       65.196  223       65.196  224       65.197
225        65.199  226       25.195  227       25.330  228       25.488
229        65.199  230        0.171  231        0.103  232        0.748
233         1.343  234        1.880  235        2.607  236       65.199
237        65.199  238       65.199  239       65.200  240       65.200
241        18.284  242       18.273  243       18.284  244        0.198
245         0.120  246        0.668  247        1.226  248        1.761
249         2.101  250        4.229  251       65.200  252       65.200
253        65.200  254       65.200  255       65.200  256       11.381
257        10.888  258       10.453  259        0.210  260        0.493
261         0.132  262        0.839  263        1.381  264        2.072
265         3.677  266       65.200  267       65.200  268       65.200
269        65.200  270       65.200  271        2.559  272        0.221
273         0.519  274        0.862  275        0.134  276        0.954
277         0.938  278        1.950  279       65.200  280       65.200
281        65.200  282       65.200  283       65.200  284        1.635
285         1.394  286        0.204  287        0.501  288        0.814
289         0.900  290        0.130  291       65.200  292       65.200
293        65.200  294       65.200  295       65.200  296        1.128
297         1.100  298        0.158  299        0.379  300        0.670
301         0.605  302        0.099  303       65.200  304       65.200
305        65.200  306       65.200  307       65.200  308        0.913
309         0.094  310        0.060  311        0.240  312        0.444
313         0.397  314       65.200  315       65.200  316       65.200
317        65.200  318       65.200  319        0.044  320        0.028
321         0.103  322        0.143  323        0.145  324       65.200
325        65.200  326       65.200  327       65.200  328       65.200
329         0.011  330        0.028  331        0.006  332        0.036
333         0.035  334       65.200  335       65.200  336       65.200
337        65.200  338       65.200  339        0.002  340        0.005
341         0.001  342        0.006  343        0.006  344       65.200
345        65.200  346       65.200  347       65.200  348       65.200
349         0.000  350        0.001  351        0.001  352        0.000
353         0.001  354       65.200  355       65.200  356       65.200
357        65.200  358       65.200  359        0.000  360        0.000
361         0.000  362        0.000  363       -0.000  364       65.200
365        65.200  366       65.200  367       65.200  368       65.200
369         0.000  370        0.000  371        0.000  372        0.000
373         0.000  374       65.200  375       65.200  376       65.200
377        65.200  378       65.200  379       -0.000  380        0.000
381         0.000  382        0.000  383       -0.000  384       65.200
385        65.200  386       65.200  387       65.200  388       65.200
389         0.000  390        0.000  391        0.000  392        0.000
393         0.000  394       65.200  395       65.200  396       65.200
397        65.200  398       65.200  399       -0.000  400        0.000
401         0.000  402        0.000  403       -0.000  404       65.200
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405      65.200  406      65.200  407      65.200  408      65.200
409       0.000  410       0.000  411       0.000  412       0.000
413       0.000  414      65.200  415      65.200  416      65.200
417      65.200  418      65.200  419      -0.000  420       0.000
421       0.000  422       0.000  423      -0.000  424      65.200
425      65.200  426      65.200  427      65.200  428      65.200
429      65.200  430       0.000  431       0.000  432       0.000
433       0.000  434       0.000  435      65.200  436      -0.000
437       0.000  438       0.000  439       0.000  440      -0.000
441       0.000  442       0.000  443       0.000  444       0.000
445       0.000  446      -0.000  447      -0.000  448       0.000
449       0.000  450      -0.000  451       0.000  452       0.000
453       0.000  454       0.000  455       0.000  456       0.000
457      -0.000  458       0.000  459       0.000  460       0.000
461       0.000  462       0.000  463       0.000  464       0.000
465       0.000  466       0.000  467      -0.000  468       0.000
469       0.000  470       0.000  471       0.000  472       0.000
473       0.000  474       0.000  475       0.000  476       0.000
477       0.000  478       0.000  479       0.000  480       0.000
481       0.000  482       0.000
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	σ_ζ	σ_η	$\tau_{\zeta\eta}$
NEL	S-ZETA	S-EATA	TUE-ZET-ET
1	72.753	-25.031	0.097
2	128.730	21.610	-10.909
3	150.471	17.487	-3.885
4	134.717	7.048	-3.030
5	103.118	-6.019	-6.335
6	42.985	1.648	1.088
7	43.985	8.558	0.592
8	40.778	4.444	0.450
9	36.630	-2.692	0.738
10	34.134	-8.519	-4.441
11	30.389	-9.585	6.986
12	58.134	-24.751	-12.546
13	71.830	-7.608	4.800
14	84.303	-0.846	1.810
15	85.364	4.561	-1.291
16	74.380	5.382	-0.979
17	57.161	0.881	-0.938
18	182.210	6.823	-4.466
19	193.090	13.623	-6.950
20	184.950	17.615	-4.893
21	138.810	5.602	2.921
22	141.180	-6.364	3.446
23	159.040	-0.724	8.298
24	159.540	-1.576	-4.006
25	143.690	-5.850	-3.097
26	181.040	-1.726	-2.301
27	175.540	1.292	-2.021
28	206.120	-2.201	-0.493
29	196.080	-0.605	-2.915
30	219.495	2.378	8.540
31	220.655	3.084	3.971
32	219.076	0.208	-4.697
33	218.126	-1.217	-8.853
34	220.024	-0.417	2.685
35	219.586	1.129	3.916
36	219.361	0.641	0.488
37	216.837	-0.101	-3.518
38	212.754	62.153	24.500
39	281.875	95.675	-25.342
40	228.291	42.228	-19.808
41	198.368	4.434	-18.915
42	196.845	-7.460	11.578
43	205.437	1.011	6.168
44	211.376	0.407	-3.798
45	218.019	-1.705	-8.118
46	54.648	-2.145	-4.063
47	60.289	-0.573	-6.099

48	64.369	0.498	-9.703
49	70.544	2.808	-12.586
50	71.693	-12.204	-2.760
51	44.375	-42.569	-23.700
52	-14.116	-79.770	-49.946
53	21.449	-105.675	-27.785
54	-0.499	-1.587	-1.159
55	-9.181	-0.671	-2.958
56	18.219	0.743	-0.578
57	25.410	0.581	0.050
58	34.978	1.825	-0.734
59	40.194	1.519	-1.884
60	39.774	1.679	-5.518
61	32.715	-3.919	-8.640
62	-9.067	-1.591	1.703
63	-6.920	-3.156	1.557
64	-13.227	-0.119	0.270
65	-11.307	-0.518	1.700
66	-9.902	2.126	-1.099
67	-11.378	0.579	-2.753
68	-33.096	-5.307	3.648
69	-15.536	1.261	2.706
70	-36.337	6.309	-2.919
71	-40.329	0.062	-1.569
72	-44.515	-2.928	-0.573
73	-47.240	-4.734	-0.251
74	-55.141	0.136	-3.032
75	-55.361	-1.528	-1.849
76	-56.541	-0.846	-0.927
77	-58.733	0.498	-0.432
78	-62.359	1.659	0.193
79	-67.046	-0.531	5.309
80	-32.720	-6.246	-3.719
81	-38.555	-5.031	0.494
82	-44.718	-3.183	0.305
83	-50.290	-0.961	0.029
84	-54.344	2.025	0.268
85	-56.160	4.501	1.446
86	1.913	2.701	-3.104
87	1.889	1.905	-0.896
88	1.010	1.776	0.904
89	-5.577	0.805	3.054
90	1.411	-4.648	-8.905