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Reliability Analysis of an Ultra-Reliable Fault Tolerant Control System
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Reliability Analysis of an Ultra-Reliable Fault Tolerant Control System

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## SUMMARY

High system reliability in computer and control systems is necessary to meet the requirements of mission success. Using fault tolerant computers, rather than extremely reliable components, can be a more effective method of acheiving the desired system rellability. The architecture of NASA's Ultra-reliable Fault Tulerant Control System (UFTCS) is based on a larger number of redundant components and static redundancy management. This approach, as applied to vehicle control, consists of parallel and redundant paths of sensor modules, computation modules, and voter modules to acheive the fault tolerant operation.

This report analyzes the reliability of the NASA UFTCS architecture as it is currently envisioned for helicopter control. The analysis is exterded to air transport and spacecraft control usjing the sam somputational and voter modules applied within the UFTCS architevure. The system reliability is calculated for several points in the helicopter, air transport, and space flight missions when there are initially 4,5 , and 6 operating channels. Sensitivity analyses are used to explore the effects of sensor failure rates and different system configurations at the 10 hour point of the helicopter mission. These analyses show that the primary limitation to system reliability is the number of flux windings on ach flux summer ( 4 are assumed for the baseline case). Tables of system reliability at the 10 hour point are provided to allow designers to choose a configuration to meet specifisd reliability goals.

## INTRODUCTION

High system reliability in computer and control systems is necessary to meet the requirements of mission success. Even with the most reliable components envisioned to be available in the near future, a fault tolerant system architecture is required to meet system reliability goals.

There are many approaches to implementing fault tolerant computing. Several of these which are newly available in the commercial market place are described in [1]. Two approaches for aircraft control are described in [2] and [3]. These two methods, which were developed before the dramatic reductions in size, power requirements, and weight of microelectronics, depend on complex logic and system reconfiguration to minimize the amount of hardware.

The architecture of NASA's Ultra-reliable Fault Tolerant Control System (UFTCS) [4] relies on a larger number of redundant components and static redundancy management. This approach, as applied to vehicle control, consists of parallel and redundant paths of sensor modules, computation modules, and voter modules to achieve the fault tolerant operation. This architecture encourages spatial distribution of the modules and different hardware and/or software in the parallel paths to reduce the risk of common mode failures and common mode design errors.

The purpose of this report is to perform a reliability analysis for the NASA UFTCS architecture as it is currently envisioned for helicopter control. The analysis is extended to air transport and spacecraft control using the same computational and voter modules applied within the UFTCS architecture.

## SYSTEM DESCRIPTIONS

Functional Description

The NASA Ultra-reliable Fault Tolerant Control System (UFTCS) is based on the concept of interconnected modules for sensing, computation, actuation, and voting, and these modules contain parallel and redundant processes running asynchronously. The outputs of each sensor module and each computation module are cross-strapped to voting elements; that is, the output of each sensor module and the output of each computation module is directed to all following voting elements.

A typical block diagram for the control of a helicopter is shown in Figure 1 which displays $N_{m}$ sensor modules and their voters, $N_{c}$ computation modules and their voters, and the voting flux summers for each of the $N_{a}$ actuators. Each solid line in the diagram is a fiber optic communications path on which data are transmitted serially, and each dashed line is an analog signal path.

Each sensor module contains one sensor for each required measurement and thus the sensor module is capable of producing a complete measurement set. The sensor module sends the readings of all its sensors to all voters over the fiber optic link. It is possible to obtain a complete measurement as long as there is at least one valid sensor (and its corresponding transmitter) for each required measurement located somewhere within the $N_{m}$ sensor modules. In other words, sensors may fail within all sensor modules and a complete measurement set can still be realized.

Each voter following the sensor modules passes a valid measur"ment set to a single computation module. The output of each computation module is cross-strapped to four voter modules

Figure 1. uFtcS Diagram with $N_{\text {M }}$ Sensor Modules, $N_{C}$ Computatation Modules, and $\mathrm{N}_{\mathrm{a}}$ Actuators
which drive the actuaiors. These voters have one digital to analog converter (DAC) connected to every voting flux summer. Only four voters follow the computation modules because, in the system shown here, each voting flux summer requires four analog inputs each having limited authority. (The more general system configuration may have other than four voters, but there must be one for each analog input to the voting flux summers.)

Power Supplies

The ship's four redundant power supplies provide +28 volt DC unregulated power. These four supplies are cross-strapped to each circuit card and sensor (see the appendix for the circuit diagram).

Sensor Module

It is assumed for the analysis that each sensor module contains one sensor for each required measurement, and that all sensors are digitally encoded and feed into a computational element for transmission to the voter stage. (A computational element contains one 8026/8087 circuit card as shown on Drawing A14-82-235-101 supplied by NASA). The following assumptions have been made for the capabilities of the UFTCS:

Helicopter and Air Transport: The mission requires stability augmentation, altitude hold, and heading select. To meet these roquirements, the following sensors are included in each sensor module:

1 Altimeter

1 Flux gate compass (long term heading reference)

2 Accelerometers (J.ong tern gravity reference)

3 Rate gyros

Space Flight: The mission requires maintaining inertial attitude; thus the assumed sensors are

3 Angular position sensors (optical)

3 Rate gyros

Input Voter Module

The computations within the input voter module are performed by an 8086/8087 design (adapted from NASA Drawing A14-82-235-102). The voter module receives an input from each sensor module via the optical fiber communications link (one link for each sensor module). This requires one optical receiver and one 8751 input/output processor for each link so that, in general, the failure rate of each voter depends on the number of parallel, redundant paths.

The logic of the voter modules has not been specified at this point, yet certain characteristics are likely to be inccrporated. A voter logic which contains time history information will be useful in detecting hardover failures even with only two operating channels, allowing operation to one valid channel. With two channels operating, however, it would not be possible to unambiguously detect a drifting failure. See the Analysis Section for a further discussion of this point.

## Computation Module

The computation modules are made up of three 8086/8087 computation elements (adapted from NASA Drawing A14-82-235-101) sharing the computational load. Thus the failure of any component in any one of the three computational elements constitutes a failure of the module.

Output Voter Module

Like the input voter module, the computations within the output voter module are performed by an $8086 / 8087$ design (adapted from NASA Drawing A14-82-235-102). The voter module receives an input from each computational module via the optical fiber communications link (one link for each computational module). As with the input voter module, the failure rate of each output voter depends on the number of parallel, redundant paths.

The number of output voter modules is limited to four because of the quarter authority characteristics of the flux summer.

Voting Flux Summer Module

Each actuator is driven by four analog signals from output voter DACs, and each of these four signals has one quarter authority (flux summing). In addition, the voting flux summers can disconnect any of these drive signals if the error between the drive signal and the actuator feedback signal exceeds a specified threshold for a specified time. The UFTCS actuators will be considered operational if there are at least two of the four drive signals connected.

The following assumptions have been made for the actuator assignments in the three environments:

Helicopter: pitch, woll, yaw, collective
Air Transport: pitch, roll, yaw, ganged throttle quadrant
Space Flight: pitch, roll, yaw

ANALYSIS

Introduction

The reliability characteristics of the UFTCS are analyzed in this section leading to a computable expression for its predicted reliability over a given mission interval. The assumptions and approximations used in the analysis are stated. The formulation is general as to the number of power supplies, sensor modules, etc. employed in the system and it allows for different numbers of different modules. Thus, if the least reliable module should prove to be the sensor module, for example, the final reliability expression is applicable to a configuration that has more sensor modules than computation modules. This will permit the tailoring of a system to meet a reliability specification with a minimum number of components.

Assumptions

The assumptions used in this analysis are summarized in this section. These assumptions are common to most reliability anal.yses.

1) The failures we are analyzinfs, as reflected in the failure rates assigned, are permanent failures, not transient failures. This assumption seems especially well justified for the UFTCS because of its ability to return a component to active status after it had been declared failed for a transient reason.
2) The failure rate is assumed constant for all components. This nearly universal assumption is appropriate for high reliability systems in which a burn-in period is used to eliminate early failures due to manufacturing defects which have escaped inspection, and components which are subject to wearout effects are replaced on a scheduled basis.
3) Failures of individual components are considered independent. In a highly redundant system, it is important that the design of the components be such as to essentially guarantee this condition. This requires electrical isolation, spatial diversity and other measures to reduce the likelihood of one failure inducing others or single events causing several failures.

The combination of assumptions (2) and (3) means that the reliability of modules which have no redundancy within the module is given by the exponential form:

$$
\begin{aligned}
R\left(t_{m}\right) & \left.=P \text { (Module works at least as long as } t_{m}\right) \\
& =\exp \left(-\lambda t_{m}\right)
\end{aligned}
$$

with

$$
\lambda=\text { Sum of the } \lambda_{1} \text { for all the components which }
$$ are essential to the function of the module.

4) We assume all system components to be operational at the beginning of the mission. It may be useful, in future studies, to relieve this assumption, but in a combinatorial analysis such as is pursued here, it is very difficult to account for all combinations of system status at the beginning of the mission. The operational procedure for the system will surely be designed to approach this condition as closely as possible - and with the capacity for self-checking which is inherent in the structure of the system, it should be possible to do very well.

## Approximation

One approximation is employed to facilitate this analysis. That is to associate failures of the fiberoptic communication links and optical receivers and input/output processors in the voters with the module that drives them - the sensor module in the case of the input voters and the computation module in the case of the output voters. The driving module is considered to function only if it and all the communication links, optical receivers and input/output processors it drives also function. This is a conservative assumption in that it underestimates the reliability of the system. Without this assumption, one has to consider all combinations of sensor modules, optical receivers, and voter processors which permit the system to function. This is a very difficult combinatoric task. With the assumption, the sensor modules and associated sptical recelvers and input/output processors can be treated separately from the voter processors, because under the assumption, if the required number of sensor modules are working, the sensor data is available to the voter processors. It is then an independent quastion whether the required number of voter processors are working.

With this approximate treatment of both the input voters and
output voters, the components are associated for the purpose of the following analysis as shown in Figure 2.

## Power Supply System

There are $N_{p}$ unregulated power supplies tied to the power buss. Any one is capable, of supplying the load of powering the flight control system. Failures of these supplies are considered independent stich implies isolation such that failure of one cannot induce failures in other supplies or in other system components.

$$
\begin{aligned}
R_{\text {pss }} & =P(\text { At least one power supply works }) \\
& =P(\text { Not all power supplies have falled }) \\
& =1-\left(1-R_{p s}\right) N_{p}
\end{aligned}
$$

Whate $R_{p s}$ is the rellability of each unregulated power supply.

## Sensor System

Even with the approximation stated above, which isolates consideration of the sensor modules from the input voters, the sensor system is somewhat complex to analyze because of the interaction of sensor failures and sensor module common component failures. It is assumed that the input voters vote on the data from the different sensors separately, so it may be possible for the system to function on good gyro data from module 1, good accalerometer data from module 2, etc. Thus the failure of any one sensor does not rule out use of the data from the other

Figure 2. WFIES sysien conpowemis as associaied fon meliability amalysis.
sensors in that module. However, failure of the sensor module common components denies all of the sensor data from that module.

For economy of terminology, we will use the term "sensor module" in this section to refer to the sensor module common components and, under the stated assumption, all the communication links, optical receivers and input/output processors the module drives. As shown in Figure 2 , the reliability of that combination of components is called $R_{s m}$. The reliability of the sensor system will be evaluated by decomposing on the mutually exclusive set of events that $k$ sensor modules work - for $k=0,1, \cdots N_{m}$.

$$
\begin{aligned}
& R_{S S}=\sum_{k=1}^{N_{m}} P(k \text { sensor modules work }) P(\text { Correct sensor system } \\
&\text { data } \mid k \text { sensor modules work })
\end{aligned}
$$

$$
P(h \text { sensor modules work })=\binom{N_{m}}{k} R_{s m}^{k}\left(I-R_{s m}\right)^{N_{m}-k}
$$

where $\binom{N_{m}}{k}$ is the binomial coefficient.

$$
\binom{N_{m}}{k}=\frac{N_{m}!}{k!\left(N_{m}-k\right)!}
$$

If only 1 sensor module is working, we can derive good sensor data only if all the sensors in that particular module work and the input voters can decide which module is the working one.

$$
\begin{aligned}
& P \text { (Correct sensor systom data } \mid \text { I sensor module works) }= \\
& =\left[\prod_{i=1}^{N_{S}} R_{S i}\right] P(\text { Last sensor module fallure is covered) }
\end{aligned}
$$

The probability that the last sensor module failure is covered is at least 0.5 , which would result from a random choice of the two modules when the failure occurs, and could well be greater than that due to the fact that all the ensor data from the failed module go bad at once when the module fails.

For $k$ greater than 1 , the issue of covering module failures does not occur because the midpoint select logic reliably discriminates the failed module from among 3 or more.

```
\(P(\) Correct sensor system data \(\mid k\) sensor modules work) \(=\)
    \(=P\) (Correct gyro data and correct accelerometer data
        and \(\cdots\). \(k\) sensor modules work)
        \(=\prod_{-1=1}^{N_{S}} P(\) Correct sensor 1 data \(\mid k\) sensor modules
```

$$
\begin{aligned}
& P(\text { Correct sensor } i \text { data } \mid k \text { sensor modules work) }= \\
&= P(\text { Exactiy } 1 \text { good sensor } 1 \text { in } k \text { modules and the } \\
& \text { last failure was covered, or exactly } 2 \text { good } \\
& \text { sensors } i \text { in } k \text { modules, or } \cdots \text { or exactly } k \\
& \text { good sensors } i \text { in } k \text { modules) }
\end{aligned}
$$

Again, the question of failure coverage only arises when we fail from 2 good sensors to 1. Because these events are mutually exclusive,

$$
\begin{aligned}
P(C o r i r e c t ~ s e n s o r ~ & 1 \text { data } \mid k \text { sensor modules work })= \\
= & P(\text { Exactly } 1 \text { good sensor in } k \text { modules) } P(\text { Last } \\
& \text { fallure was covered })+P(\text { Exactly } 2 \text { good } \\
& \text { sensors in } k \text { modules })+\cdots+P(\text { Exactly } \\
& k \text { good sensors in } k \text { modules) }
\end{aligned}
$$

$P($ Exactly $j$ good sensors $i$ in $k$ modules $)=\binom{k}{j} I \sum_{s i}^{j}\left(I-R_{s i}\right)^{k-j}$
$P($ Last failure was covered $)=P$ (Last failure was drifting type) $x P$ (Failure was covered | Driftinks failure)
$+P$ (Last failure was hardover type)P(Failure was covered Hardover failure)
$=f_{d f} P$ (Failure was covered $\mid$ Drifting failure) $+\left(I-f_{d f}\right) P($ Failure was covered |, Hardover failure)

The expression for last failure coverage decomposes all sensor failures into drifting type and hardover type. In this context, "hardover" should be interpreted to mean "all failures other than drifting failures". The probability of covering these two modes of sensor failure could be different; the probability of covering a hardover failure should be close to 1 and the probability of covering a drifting failure may be only 0.5 which would result from a random choice from the two sensors.

The following identity can be used to simply the expression for the probability of having correct sensor i data given $k$ good sensor modules.
$\sum_{j=0}^{k} P($ Exactly $j$ good sensors in $k$ modules $)=1$
Therefore
$\sum_{j=2}^{k} P($ Exactly $j$ good sensors in $k$ modules $)=1-P(0$
good sensors in $k$ modules $)-P(1$ good sensor in k modules)
$P$ (Correct sensor $i$ data $\mid k$ sensor modules work) $=$ $=P(1$ good sensor in $k$ riodules) $P($ Last failure was
.- covered)

+ I-P(0 good sensors in $k$ modules)
- $P(1$ good sensor in $k$ modules)
$=1-\left(1-R_{\text {Si }}\right)^{k}-P(1$ good sensor in $k$ modules $)[1-$ $P($ Last failure was covered)]
$=1-\left(1-R_{S i}\right)^{k}-k R_{S i}\left(1-R_{S i}\right)^{k-l_{P}(\text { Last }}$ sensor failure not covered)

Both the fraction of drifting failures, $f_{d f}$, and the probabilty of last failure coverage can be different for each type of sensor. This last expression for the probability of correct sensor $i$ data with $k$ good sensor modules applies only for $k$ greater than or equal to 2 . The expression for $k$ equal to 1 was given earlier.

Input Voters and Computation Modules

We can fail to 2 of these channels without question because midpoint select in the output voters will distinguish 1 failea channel out of 3. Whether 1 failed channel out of 2 can be identified is unclear, but even if a random choice is made of the remaining two channels when one fails, there is probability 0.5 that the working channel will be selected and thus permit operation of the system with just one computational channel.

$$
\begin{aligned}
R_{c s}= & P(\text { Exactly } 1 \text { channel works) } P(\text { Last channel failure } \\
& \text { is covered) } \\
& +\sum_{k=2}^{N} P(\text { Exactiy } k \text { channels work })
\end{aligned}
$$

With the same approach used to simplify the expression for the probability of correct sensor i data given $k$ good sensor modules, this ca: be restated as

$$
\begin{array}{r}
R_{C S}=1-\left(1-R_{V C}\right) N_{C}-N_{C} R_{V C}\left(1-R_{V C}\right) N_{C}-1 P(\text { Last channel failure } \\
\text { was not covered })
\end{array}
$$

As indicated in Figure 2, R Rcis the reliability of each channel of voter processor, computation module, and associated communication links, optical receivers and input/output processors. $N_{C}$ is the number of those channels in the system which need not be the same as the number of sensor modules or output voters. The probability that the last channel failure was not covered should be no greater than 0.5 .

Output Voters and Actuators

Because of the flux summing operation on the actuators, the output voters, actuator drivers, and actuators must be treated together. The term "actuator driver" is used here to designate the circuitry that connects the output voter processor to the current coil on the actuator servo valve. The principal components of the actuator driver are indicated in Figure 2 to be the D/A converter and the current amplifier. There are Nooutput voters and the requirement for system operation will be taken to be the correc: application of current to $N_{f}$ of the $N_{O}$ coils on each actuator. Whe number $N_{f}$ of correct fluxes required on each actuator for proper operation depends on how well the effects of failed channels can be limited.

The reliability of the Voter-Actuator system will be decomposed on the number of working voter processors.
$R_{\mathrm{va}}=\sum_{k=N_{f}}^{N \rho} P($ Exactly $k$ voter processors work)P(Actuator $I$ system works and actuator 2 system works and ${ }^{\cdots}$ and actuator $N_{a}$ system works $\mid k$ voter processors work)

$$
\begin{gathered}
=\sum_{k=N_{f}}^{N o}\left[P \left(\text { Exactly } k \text { voter processors work) } \prod_{i=1}^{N_{2}} P \text { (Actuator } i\right.\right. \\
\text { system works } \mid k \text { voter processors work) }]
\end{gathered}
$$

$P($ Exactly $k$ voter processors work $)=\binom{N_{0}}{k} R_{v p}^{k}\left(1-R_{v p}\right)^{N_{0}}-k$
$P$ (Actuator i system works | k voter processors work) = $=P($ Actuator $i$ works $) P\left(A t\right.$ least $N_{f}$ fluxes on actuator $i$ are correct ! $k$ voter processors work)
$P($ Actuator $i$ works $)=R_{a i}$
P(At least $N_{f}$ fluxes on actuator $i$ are correct $\mid k$ voter

$$
\begin{aligned}
&\text { processors work })=\sum_{j=N_{f}}^{k} P(\text { Exactly } j \text { actuato } \\
& \text { from } k \text { voters wor } \\
&=\sum_{j=N_{f^{\prime}}}^{k}\binom{k}{j} R_{a d_{i}}^{j}\left(1-R_{a d_{i}}\right)^{k-j}
\end{aligned}
$$

Summary

The predicted reliability of the Ultra-reliable Fault Tolerant Control System with an arbitrary number of components is computed by the following series of calculations:

Component or module reliability:

OF POOR QUALM:

For the given mission time, compute al. 1 component or module reliabilities as

$$
R_{i}=\exp \left(-\lambda_{i} t_{m}\right)
$$

Power supply system reliability:

$$
R_{p s s}=1-\left(1-R_{p s}\right) N_{p}
$$

Sensor system reliability:
$P($ Last sensor failure was not covered) $=$

$$
\begin{aligned}
=1 & -f_{d f} P(\text { Failure was covered | Drifting failure }) \\
& -\left(1-f_{d f}\right) P(\text { Failure was covered | Hardover failure })
\end{aligned}
$$

$P($ Correct sensor $i$ data $\mid k$ sensor modules work) $=$

$$
=1-\left(1-R_{S i}\right)^{k}-k R_{S i}\left(1-R_{S i}\right)^{k-I_{P}(\text { Last sensor failure }}
$$ was not covered) $(k \geq 2)$

$R_{s s}=N_{m} R_{s m}\left(1-R_{s m}\right) N_{m}-1\left[\prod_{i=1}^{N_{s}} R_{s i}\right] \quad P($ Last sensor module failure
is covered) $+\sum_{k=2}^{N_{m}}\left[\binom{N_{m}}{k} R_{s m}^{k}\left(1-R_{s m}\right)^{N_{m}-k} \prod_{i=1}^{N_{s}} P\right.$ (Correct sensor $i$ data $\mid k$ sensor modules work)

Ometsen 2
of poon craniv
Input voter and computation system reliability:

$$
\begin{array}{r}
R_{c s}=1-\left(1-R_{v c}\right)^{N_{c}-N_{c} R_{v c}\left(1-R_{v c}\right)_{c}^{N_{c}-I_{P}(\text { Last channel failure }}} \text { was not covered) }
\end{array}
$$

Output voter and actuator system reliability:

$$
R_{v a}=\sum_{k=N_{f}}^{N_{0}}\left\{\binom{N_{0}}{k} R_{v p}^{k}\left(1-R_{v p}\right)^{N_{0}}{ }^{m k}\left[\prod_{1=1}^{N_{2}} R_{a 1}\left(\sum_{j=N_{f}}^{k}\binom{k}{j} R_{a d_{i}}^{j}\left(1-R_{a d_{i}}\right)^{k-j}\right)\right]\right\}
$$

UFTCS reliability:

$$
R_{\text {systern }}=R_{p s s} R_{s s} R_{c s} R_{v a}
$$

The probabilities of detecting the last failure can be manipulated to determine the system reliabilities for the "failing to two" and "failing to one" cases. For the "failing to one" case, the probability of covering the last sensor module failure and the probability of covering the last input voter and computation system failures should be set to one. Likewise, the probebility of covering the sensor failures should be set to some -easonable value (e.g. 0.5 for drifting failures and 1.0 for hard failures). For the "iailing to twol case, the probability of covering the last failure should be set to 0.0 for all modules and sensors.

## COMPONENT FAILURE RATES

## Sensor Failure Rates

Obtaining failure rates for the sensors was one of the more difficult tasks of the analysis for several reasons. First, the
sensor manufacturers were somewhat reluctant to provide information for the purposes of any analysis; they have been "blamed" for poor system performance in the past, and are therefore reluctant to participate in this manner. Second, several airframe manufacturers were contacted, but they buy combination sensor-computer subsystems (e.g., air data computers, and inertial reference systems), and they were not able to provide reliability figures for the specific sensors us ad in this analysis.

To sircumvent these difficulties, we have evaluated the UFTCS with a "best guess" reliability estimate for each generic sensor and have supplemented these calculations with a sensitivity analysis for the sensors in the helicopter mission. These sensitivity analyses can be used to determine the sensor reliability requirements to achieve desired overall system reliability.

This analysis assumes that re:iability is bore important than cost and that mass-produced sensors are not used. Therefore, the reliability iata used in this analysis is taken from the most reliable components found in the survey.

Converting Reliabilities Between Environments. In some instances the reliability estimates were obtajned for the same sensor, but in different environments. These reliabilities were multiplied by scale factors, not only to convert the reliabilities to one environment for choosing the "best guess" reliability, but also to convert the reliabilities to the three environments of the analysis (helicopter, air transport, and space flight). The scale factors are based on the environmental parameters found in MIL-HDBK-217D [6], and are shown in Table 1.

Table 1

Scale Factors for Converting Failure Rates Between Environments

To convert
from this
environment

Multiply the fallure rate by the indicated scale factor

## Helicopter Air Transport Space Flight

| Helicopter | 1.0 | 0.2 | 0.04 |
| :--- | ---: | :--- | :--- |
| Air Trnspt | 5.0 | 1.0 | 0.2 |
| Space Flight | 25.0 | 5.0 | 1.0 |

Accelerometer Reliablifties. Four Mean Time Between Failures (MTBF) were obtained for accelerometers. When converted to the air transport environment they were $50,000,30,000$, 20,000 , and 6,000 hours. Based on these estimates, a failure rate of 20 failures per million hours (air transport environment) was chosen P or the generic accelerometer.

Gyro Reliabilities. Three MTBFs for gyros were obtained, and when converted to the air transport environment, they were $70,000,60,000$, and 11,000 hours. A failure rate of 15 failures per million hours (air transport environment) was chosen for the generic gyro.

Long Term Heading Reference. Only one MTBF for a flux gate compass, 50,000 hours for the air transport environment, was obtained. A failure rato of 20 failures per million hours (air transport environwent) was chosen for the generic flux gate
compass.

Barometric Altimeter Reliability. Four MTBFs for a barometric altimeter, 25,000, 10,000, and two at 7,000 hours for the air tramsport environment, were obtained. A failure rate of 40 failures per million hours (air transport environment) was chosen for the generic altimeter.

Optical Position Sensors. Attempts to obtain reliability estimates for optical position sensors were unsuccessful. Thus a generic sensor was conceived and consists of 10 photo transistors in a linear array. Based on this assumption and the failure rates of phototransistors in [6], the failure rate of the optical. sensor is found to be 20 failures per million hours.

Table 2 summarizes the sensor failure rates used in the UFTCS reliability analyses.

Table 2

## Sensor Failure Rates Used in UFTCS Analyses (failures per million hours)

| Sensor |  | Environment |  |
| :--- | :---: | :---: | :---: |
|  | Helicopter | Air Transport | Space Flight |
| Accel. | 100 | 20 | -- |
| Gyro | 75 | 15 | 3 |
| Long Term |  |  |  |
| Hag Ref | 100 | 20 | -- |
| Baro Alt | 200 | 40 | -- |
| Opt. Pos. | $-\infty$ | -- | 20 |

## Other Failure Rates

Failure rates for the computational elements and voter elements were computed from the circuit design of these elements as adapted from drawings supplied by NASA. These calcualations were performed according to the procedures outlined in MIL-HDBK-217D [6], and are detailed in the Appendix.

The shipls power supplies and the actuators are not considered as part of this analysis, and so it is assumed that they have zero failure rates. The analysis has been formulated so that their reliabilities can be incorporated at a later date.

## RESULTS

## Assumptions and Constants

Certain assumptions have been made, and certain parameters are held constant for all of the calculations unless explicitly s'sated otherwise.

- The baseline sensor filure rates are those shown in Table 2.
- There are four output voters and actuator drivers (fiux windings) for each actuator. Valid signals are required on at least two windings for proper operation.
- The probabillty of "failing to two" means that there are at least two operating computation modules and there are at least two operating sensors for each measurement; each of these sensors feeds into an operating sensor module. The probability of "failing to one" means that there is at least one of' each of
these items in operation.
- When "failing to one", the probabilities of covering the last sensor module failure and the last voter/computation module failure is 1.0. The probability of covering the last sensor failure is 0.9 for all sensors. This result from assuming that 20\% of the sensor failures are drifting failures; the probability of covering the last drifting failure is 0.5 ; and the probability of covering a hardover sensor failure is 1.0 .


## Mission Reliability Estimates

The primary objective of this report is to supply reliability estimates of UFTCS operation at various times in the helicopter, air transport, and space flight missions. Initial system configurations are 4, 5, and 6 redundant paths (with four output voters and flux windings), and failures are allowed to 1 or 2 operating paths.

The reliability estimates are shown in Table 3 assuming perfect sensors (all sensor failure rates equal zero), and Table 4 assuming the baseline sensors. The results with the perfect
 itself, whereas the other table shows the reliability of the combination of sensors and controi system. Note that there is a "floor" to the probabilities of failure which, as will be shown later, are due to the assumption of 4 flux windings on each actuator.

## Sensitivity Analyses

This section describes the results of sensitivity analyses

Table 3
Predicted probabilities of failure for UFTCS

Helicopter environment (35C)

Fail to/ start with

| $1 / 4$ | $0.71 \mathrm{E}-13$ |
| :--- | :--- |
| $2 / 4$ | $0.10 \mathrm{E}-10$ |
| $1 / 5$ | $0.70 \mathrm{E}-13$ |
| $2 / 5$ | $0.72 \mathrm{E}-13$ |
| $1 / 6$ | $0.70 \mathrm{E}-13$ |
| $2 / 6$ | $0.70 \mathrm{E}-13$ |

Air transport environment (25C)
Operating time (hours, no maintenance) $1 \quad 10 \quad 20$
$0.71 \mathrm{E}-13$
$0.73 \mathrm{E}-10$
-.10E-10
$0.72 \mathrm{E}-13$
$0.70 \mathrm{E}-13$
$0.10 \mathrm{E}-07$
$2 / 4$
$1 / 5$
$1 / 6$
2/6
$0.70 \mathrm{E}-13$
$0.61 \mathrm{E}-09$
$0.80 \mathrm{E}-07$

Fail to/ start with

| $1 / 4$ | $0.20 \mathrm{E}-13$ | $0.22 \mathrm{E}-10$ | $0.19 \mathrm{E}-09$ |
| :--- | :--- | :--- | :--- |
| $2 / 4$ | $0.70 \mathrm{E}-11$ | $0.69 \mathrm{E}-08$ | $0.55 \mathrm{E}-07$ |
| $1 / 5$ | $0.20 \mathrm{E}-13$ | $0.20 \mathrm{E}-10$ | $0.16 \mathrm{E}-09$ |
| $2 / 5$ | $0.21 \mathrm{E}-13$ | $0.29 \mathrm{E}-10$ | $0.31 \mathrm{E}-09$ |
| $1 / 6$ | $0.20 \mathrm{E}-13$ | $0.20 \mathrm{E}-10$ | $0.16 \mathrm{E}-09$ |
| $2 / 6$ | $0.20 \mathrm{E}-13$ | $0.20 \mathrm{E}-10$ | $0.16 \mathrm{E}-09$ |

Space craft environment (250)
Fail tol
start with
$1 / 4$
$2 / 4$
$1 / 5$
$2 / 5$
$1 / 6$
$2 / 6$

2/6
0.64 E .07
$0.13 \mathrm{E}-04$
$0.21 \mathrm{E}-07$
$0.24 \mathrm{E}-06$
$0.20 \mathrm{E}-07$
$0.24 \mathrm{E}-07$
$0.73 \mathrm{E}-04$
$0.30 \mathrm{E}-02$
$0.94 E-03$
Operating time (hours, no maintenance)

- .

336
2190 4380
$0.20 \mathrm{E}-01$
$0.11 \mathrm{E}-04$
$0.20 \mathrm{E}-03$
$0.33 E-03$
$0.4^{1} \mathrm{E}-02$
$0.61 \mathrm{E}-05$
$0.69 \mathrm{E}-04$
$0.40 \mathrm{E}-04$

Table 4
Predicted probabilities of fatZure for UFTCS with baseline sensors

Helicopter environment (350)

Faiz tol start with
$1 / 4$
$2 / 4$
$1 / 5$
$2 / 5$
$1 / 6$
$2 / 6$

## 6

$0.70 \mathrm{E}-1$
$0.70 \mathrm{E}-13$
$0.1 \angle E-10$
$0.15 \mathrm{E}-09$
$0.75 \mathrm{E}-13$
$0.12 \mathrm{E}-12$
$0.70 \mathrm{E}-13$
$0.70 \mathrm{E}-13$
Operating time (hours, no maintenance)
1
$\angle E-10$
$5 E-09$
$5 E-13$
$2 E-12$
$0 E-13$
$0 E-13$
10
$0.14 \mathrm{E}-07$
$0.15 \mathrm{E}-06$
$0.11 \mathrm{E}-09$
$0.52 \mathrm{E}-09$
$0.70 \mathrm{E}-10$
$0.72 \mathrm{E}-10$
$0.12 \mathrm{E}-06$
$0.12 \mathrm{E}-05$
$0.13 \mathrm{E}-08$
$0.77 \mathrm{E}-08$
$0.57 \mathrm{E}-09$
$0.61 \mathrm{E}-09$

Air transport environment (250)

start with
$1 / 4$
2/4
1/5
$2 / 5$
1/6
$2 / 6$
$1_{1}^{\text {Operating time (hours, no maintenance) }} \underline{10}$
$0.77 \mathrm{E}-12$
$0.14 \mathrm{E}-10$
$0.20 \mathrm{E}-13$
$0.22 \mathrm{E}-13$
$0.20 \mathrm{E}-13$
$0.20 \mathrm{E}-13$
$0.77 \mathrm{E}-09$
$0.14 \mathrm{E}-07$
$0.21 \mathrm{E}-10$
$0.41 \mathrm{E}-10$
$0.20 \mathrm{E}-10$
0.62E-08
$0.12 \mathrm{E}-06$
$0.18 \mathrm{E}-09$
$0.49 \mathrm{E}-09$
$0.16 \mathrm{E}-09$
$0.16 \mathrm{E}-09$

Space craft environment (250)

| Fail to/ start with | Operating time <br> 336 | (hours, 2190 | ce) $4380$ |
| :---: | :---: | :---: | :---: |
| 1/4 | 0.28E-05 | 0.82E-03 | 0.67E-02 |
| 2/4 | 0.39E-04 | $0.88 \mathrm{E}-02$ | $0.55 \mathrm{E}-01$ |
| 1/5 | 0.83E-07 | $0.11 \mathrm{E}-03$ | 0.162-02 |
| 2/5 | $0.84 \mathrm{E}-06$ | $0.12 \mathrm{E}-02$ | $0.14 \mathrm{E}-01$ |
| 1/6 | 0.22E-07 | 0.20E-04 | $0.44 \mathrm{E}-03$ |
| 2/6 | $0.38 \mathrm{E}-07$ | $0.16 \mathrm{E}-03$ | 0.35E-02 |

to explore some of the parameters of interest in the UFTCS. The 10 hour point in the helicopter mission was chosen for examination because of the Ereater liklihood that UFTCS will be applied to helicopters in the immediate future.

Coverage of Sensor Failures. When failing from two to one sensors, there is a chance that the failure will not properly be Asolated, especially if it is a drifting failure. The parameter affecting system reliability is the probability of detecting this last sensor failure which is in the range of [0.5, 1.0]. Figure 3 shows the sensitivity of system reliability to this parameter when the initial configuration has 4 and 6 channels. Also shown for comparison purposes are the (constant) curves for failing to two for 4 and 6 channels. It can be seen that 4 channels failing to 1 is sensitive to this sensor coverage, and that the probability of system failure increases by a factor of 10 as the probability of sensor coverage drops from 1.0 to 0.9 , the nominal value. However, the sensitivity to this coverage is less for the other configurations because of the floor effect of the number of flux windings.

Barometric Altimeter Reliability. The reliability of the barometric altimeter is of interest because it is the least reliable of all sensors. Figure 4 shows the effect of this failure rate on overall system reliability. It can be seen that there are two floor effects here. For the 6 channel case, the floor is . $7 \mathrm{E}-10$ which is determined by the number of flux windings. The two floors for the 4 channel case are determined by the reliability of the other sensors in each sensor module. These floors are reached when the barometric altimeter failure rate is near those of the other sensors at approximately 100 failures per million hours (FPM).

Gyro Reliability. The effect of the reliability of the

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gyros is examined because three of the 6 sensors in each module are gyros, thus possibly magnifying the effect of increases in gyro failure rates. Figure 5 shows the effect of gyro failure rate with the same general pattern as for the barometric altimeter.

Number of Flux Windings. It is not necessary within the UFTCS architecture to have 4 flux windings driven by 4 output voters. However, it should be assumed that at least half of the flux windings must operate properly to have an operational system because of the flux summing operation. Figures 6 and 7 show the effects on system reliability of 2 to 10 flux windings for each actuator. Figure 6 is for the special case of perfect sensors to see the effects of the UFTCS hardware alone; Figure 7 shows the effects of the number of flux windings on the reliability of the sensor control system combined. The most striking results are the removal of the "floor" at . $7 \mathrm{E}-10$ when the number of windings is 6 or more, verifying the limitation on system failure rate seen in previous results. (Figure 6 also shows that a large number of windings can penalize system reliability, although the penalty is slight.) It can be seen in Figure 6 that the floor can become very low for perfect sensors, but Figure 7 indicates that with the nominal sensors there is little value in increasing the number of windings beyond 6 when there are 6 sensor and computational modules.

Sensor Modules vs. Computational Modules. Although it is convenient to think of the UFTCS as having $N$ channels, there is no requirement that the number of sensor modules must equal the number of computational modules or number of flux windings. The cross-strapping of information to the input voters and output voters removes the need for this constraint. In fact, it seems logical that there should be a large number of unreliable parts of the system and a small number of the reliable parts of the


Figure 5. Probability of system failure versus rate gyro
failure rate (baseline sensors). failure rate (baseline sensors).

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O 1/4 Sensor, input voter and computation modules

- 2/4 Sensor, input voter and computation modules
$\square 1 / 6$ Sensor, input voter and computation modules
- 2/6 Sensor, input voter and computation modules


Figure 7. Probability of system fallure versus number of flux sumuer windings requiring half of the windings for proper operation (baseline sensors).
system. Tables 5 and 6 show the system reliability as a function of the number of sensor modules, computation modules, and flux windings, failing to two and one. Table 5 assumes perfect sensors, in order to examine the effects of differing amounts of UFTCS hardware, and Table 6 assumes the baseline sensors, in order to examine the tradeoffs to obtain a reliable sensor/control system combination.

Tables 5 and 6 may be used to choose a system configuration to meet a desired system reliability goal at the 10 hour point of the helicopter mission. For example, Table 7 shows the system configurations that will meet a goal of system failure less than $1 \mathrm{E}-10$ assuming both perfect and baseline sensors.

Even though a configuration with baseline sensors and "failing to one" requires six sensor modules, we feel that a configuration with only five sensor modules would be adequate because of the conservative nature of the approximation made in the analysis. The approximation requires that all input processors driven by a sensor module be operational for that sensor module to work properly, and the input processor is among the most unreliable components in the system (see component C8751 in Table $A 4$ in the Appendix). A configuation consisting of four flux windings, four computation modules, and five sensor modules with baseline sensors results in a failure rate only slightly higher than $1 \mathrm{E}-10$.

Table 5
Probability of system failure versus configuration (perfect sensors)
[Upper entry is failing to one; lower entry is failing to two

| Number of sensor modules | Numbe 2 | of input 4 | $\begin{gathered} \text { ter/comp } \\ 5 \end{gathered}$ | $\begin{gathered} \text { tion modi } \\ 6 \end{gathered}$ | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Four output voters and flux windings |  |  |  |  |  |
| 2 | $\begin{aligned} & 0.19 \mathrm{E}-05 \\ & 0.35 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.36 \mathrm{E}-06 \\ & 0.12 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.46 \mathrm{E}-06 \\ & 0.14 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.57 \mathrm{E}-06 \\ & 0.15 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.83 \mathrm{E}-06 \\ & 0.18 \mathrm{E}-02 \end{aligned}$ |
| 4 | $\begin{aligned} & 0.17 \mathrm{E}-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.73 \mathrm{E}-10 \\ & 0.10 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.13 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.71 \mathrm{E}-10 \\ & 0.18 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.71 \mathrm{E}-10 \\ & 0.31 \mathrm{E}-08 \end{aligned}$ |
| 5 | $\begin{aligned} & 0.17 E-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.73 \mathrm{E}-10 \\ & 0.91 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.86 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.72 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.74 \mathrm{E}-10 \end{aligned}$ |
| 6 | $\begin{aligned} & 0.17 \mathrm{E}-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.73 \mathrm{E}-10 \\ & 0.91 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.85 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.70 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.70 \mathrm{E}-10 \end{aligned}$ |
| 8 | $\begin{aligned} & 0.17 E-05 \\ & 0.26 E-02 \end{aligned}$ | $\begin{aligned} & 0.73 \mathrm{E}-10 \\ & 0.91 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.85 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.70 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.70 \mathrm{E}-10 \end{aligned}$ |
| Six output voters and flux windings |  |  |  |  |  |
| 2 | $\begin{aligned} & 0.24 \mathrm{E}-05 \\ & 0.38 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.36 \mathrm{E}-06 \\ & 0.12 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.46 \mathrm{E}-06 \\ & 0.14 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.5^{\prime} 7 \mathrm{E}-06 \\ & 0.15 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.83 \mathrm{E}-06 \\ & 0.18 \mathrm{E}-02 \end{aligned}$ |
| 4 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.48 \mathrm{E}-11 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.28 \mathrm{E}-12 \\ & 0.13 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.38 \mathrm{E}-12 \\ & 0.17 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.74 \mathrm{E}-12 \\ & 0.30 \mathrm{E}-08 \end{aligned}$ |
| 5 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.47 \mathrm{E}-11 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.61 \mathrm{E}-13 \\ & 0.24 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.17 \mathrm{E}-11 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.35 \mathrm{E}-11 \end{aligned}$ |
| 6 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.47 \mathrm{E}-11 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.61 \mathrm{E}-13 \\ & 0.23 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.96 \mathrm{E}-13 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.58 \mathrm{E}-13 \end{aligned}$ |
| $\delta$ | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.47 \mathrm{E}-11 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.61 \mathrm{E}-13 \\ & 0.23 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.95 \mathrm{E}-13 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.54 \mathrm{E}-13 \end{aligned}$ |

Table 6
Probability (f system failure versus coringuration (baseline sensors)
[Upper entry is failing to one; lower entry is failing to two

| Number of sensor modules | Number of input voter/computation modules $2 \quad 4 \quad 5 \quad 6$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Four output voters and flux windings |  |  |  |  |  |
| 2 | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.18 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 E-02 \\ & 0.16 E-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ |
| 4 | $\begin{aligned} & 0.17 \mathrm{E}-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.14 \mathrm{E}-07 \\ & 0.15 \mathrm{E}-06 \end{aligned}$ | $\begin{aligned} & 0.16 \mathrm{E}-07 \\ & 0.16 \mathrm{E}-06 \end{aligned}$ | $\begin{aligned} & 0.18 \mathrm{E}-07 \\ & 0.18 \mathrm{E}-06 \end{aligned}$ | $\begin{aligned} & 0.22 \mathrm{E}-07 \\ & 0.22 \mathrm{E}-06 \end{aligned}$ |
| 5 | $\begin{aligned} & 0.17 \mathrm{E}-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.11 \mathrm{E}-09 \\ & 0.95 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.11 \mathrm{E}-09 \\ & 0.52 \mathrm{E}-09 \end{aligned}$ | $\begin{aligned} & 0.12 \mathrm{E}-09 \\ & 0.57 \mathrm{E}-09 \end{aligned}$ | $\begin{aligned} & 0.13 \mathrm{E}-09 \\ & 0.72 \mathrm{E}-09 \end{aligned}$ |
| 6 | $\begin{aligned} & 0.17 \mathrm{E}-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.73 \mathrm{E}-10 \\ & 0.91 \mathrm{E}-08 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.86 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.72 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.72 \mathrm{E}-10 \end{aligned}$ |
| 8 | $\begin{aligned} & 0.17 \mathrm{E}-05 \\ & 0.26 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.73 E-10 \\ & 0.91 E-08 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.85 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.70 \mathrm{E}-10 \end{aligned}$ | $\begin{aligned} & 0.70 \mathrm{E}-10 \\ & 0.70 \mathrm{E}-10 \end{aligned}$ |
| Six output voters and flux windings |  |  |  |  |  |
| 2 | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.18 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ | $\begin{aligned} & 0.15 \mathrm{E}-02 \\ & 0.16 \mathrm{E}-01 \end{aligned}$ |
| 4 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.14 \mathrm{E}-07 \\ & 0.16 \mathrm{E}-06 \end{aligned}$ | $\begin{aligned} & 0.16 \mathrm{E}-07 \\ & 0.16 \mathrm{E}-06 \end{aligned}$ | $\begin{aligned} & 0.18 \mathrm{E}-07 \\ & 0.18 \mathrm{E}-06 \end{aligned}$ | $\begin{aligned} & 0.22 \mathrm{E}-07 \\ & 0.22 \mathrm{E}-06 \end{aligned}$ |
| 5 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.42 \mathrm{E}-10 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.43 \mathrm{E}-10 \\ & 0.46 \mathrm{E}-09 \end{aligned}$ | $\begin{aligned} & 0.50 \mathrm{E}-10 \\ & 0.50 \mathrm{E}-09 \end{aligned}$ | $\begin{aligned} & 0.65 \mathrm{E}-10 \\ & 0.65 \mathrm{E}-09 \end{aligned}$ |
| 6 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.48 \mathrm{E}-11 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.18 E-12 \\ & 0.24 E-10 \end{aligned}$ | $\begin{aligned} & 0.19 \mathrm{E}-12 \\ & 0.15 \mathrm{E}-11 \end{aligned}$ | $\begin{aligned} & 0.24 \mathrm{E}-12 \\ & 0.20 \mathrm{E}-11 \end{aligned}$ |
| 8 | $\begin{aligned} & 0.22 \mathrm{E}-05 \\ & 0.29 \mathrm{E}-02 \end{aligned}$ | $\begin{aligned} & 0.47 \mathrm{E}-11 \\ & 0.13 \mathrm{E}-07 \end{aligned}$ | $\begin{aligned} & 0.61 E-13 \\ & 0.23 E-10 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.95 \mathrm{E}-13 \end{aligned}$ | $\begin{aligned} & 0.54 \mathrm{E}-13 \\ & 0.54 \mathrm{E}-13 \end{aligned}$ |


| Failing to | 4 flux windings <br> 4 | 4 computation modules <br> 4 sensor modules |
| :---: | :--- | :--- |
|  |  | 4 computation modules |
| Failing to | 6 sensor modules |  |
| 2 |  |  |$\quad$| 4 flux windings |
| :--- |

Table 7. System Configurations with probability of failure less than 1E-10

CONCLUSIONS

The reliability calculations for the baseline system clearly indicate that the 4 flux windings limit overall probability of system failure to no less than $\cdot 7 \mathrm{E}-10$ at the 10 hour point in the helicopter mission. The sensitivity analyses were also influenced by this limit. Tables for probabisity of failure at the 10 hour point in the helicopter mission are provided as a function of the number of computation modules, sensor modules, and flux windings; these tables allow the designer to choose a configuration which will meet a specified probability of failure at this point of the helicopter mission.

## APPENDIX

Component and Module Reliability Calculations

The component reliability values were determined using references 5 and 6. Tables A1 through A3 list the component-spesific data and assumptions used in the calculation. In addition, the following characteristics were assumed for all microelectronics:

1. Hermetically sealed,
2. Dual in-line packaging,
3. Eutectic die attach,
4. Glass seal,
5. MIL-M-38510, Class B, and
6. Learning factor $=1$.

Ambient temperatures for the calculations were $25^{\circ} \mathrm{C}$ for the space craft and air transport environments and $35^{\circ} \mathrm{C}$ for the helicopter environment. Case temperatures were taken from reference 6, table 5.1.2.5-4, note 2 (space flight, $40^{\circ} \mathrm{C}$; helicopter and air transport, $60^{\circ} \mathrm{C}$ ).
IV e[q8i
DATA USED TU DETERMINE COMPONENT FAILURE
.RATES - COMPONENTS NOT LISTED IN MIL -M-38510
Description
 230 gates (1) 296 gates (Ref. 6)
Number
of Ping
Circuit
Complexity

1
3
9

## 

- 

 On $10^{\circ} 0$ SOWS
E $700778 x$
Technology

2.0
2.5
3.0
$0.5(2)$
1.0
1.0
1.0
1.0
1.5 Approximated from 100 mA active current at 5 V (Ref. 5)

Part No.
C8751H-11
D8086
C8087-3
D2764
HM6116P-3
MD8282/B
MD8284/A!B
MD8286/B
MD8288/B
HD1-6/02A-9
Notes:

Table A2
CROSS REFERENGE OF COMPONENTS LISTED IN MIL-M-38510

| Part No. | M38510/ | Description |
| :---: | :---: | :---: |
| SNJ54LS02J | 30301 C | Quad 2 input positive NOR gates |
| SNJ54LSO4J | $30003 C$ | Hex inverters |
| SNJ54IS10J | 300050 | Triple 3 input positive NAND gates |
| SNJ54LS74AJ | 30102C | Dual D-type filp flops |
| SNJ54LS125AJ | 323010 | Quad bus buffer gates |
| SNJ54LS138J | 30701E | 3 to 8 line decoder |
| SNJ54LS139J | 30702E | Dual 2 to 4 Iine decoders |
| SNJ54LS367AJ | 32203E | Hex bus drivers |
| SNJ54LS368AJ | 32204E | Her bus drivers |
| SNJ55113J | 10405E | Line driver |
| SNJ55115J | 10404E | Line receiver |
| MC7805 | 10706Y | 5V Voltage Regulator |
| MC7824 | 10709Y | 24V Voltage Regulator |
| DAC08A | 11302E | 8 bit Digital to Analog Convertor |
| LM118 | 101070 | Operational Amplifier |

Table A3
ASSUMPTIONS FOR DISCRETE COMPONENT RELIABILITY CALCULATIONS

| Component | $\begin{aligned} & \text { MII-EDBK } \\ & =217 D \end{aligned}$ | Assumptions |
| :---: | :---: | :---: |
| Reststors | 5.1.6.1 | Composition resistors <br> MIL-R-39008 Level M <br> Less than 100 K ohms <br> Ratio of operating to rated wattage $=0.5$ |
| $\begin{aligned} & \text { Trimmer } \\ & \text { Resistors } \end{aligned}$ | 5.1 .6 .7 | Non wire wound resistors MIL-R-39035 Level M 10 to 50K ohms Ratio of operating to rated wattage $=0.5$ <br> Ratio of applied to rated voltage $=0.8$ to 0.1 |
| Capacitors | 5.1 .7 .4 | ```Ceramic capacitors MIL-C-39014 Level M Rated at 125* C Ratio of operating to rated voltage = 0.5``` |
| Zener Diodes | 5.1 .3 .5 | MIL-STD-19500 <br> JAN Quality Level <br> Max permissible junction <br> Temperature $=175^{\circ}$ to $200^{\circ} \mathrm{C}$ <br> Max case temperature ( $100 \%$ rated load and max junction <br> temperature not <br> exceeded) $=25^{\circ} \mathrm{C}$ <br> Ratio of (Power dissipated to $\max$ rated power) or (operating zener current to max rated zener current) $=0.5$ |
| Diodes | 5.1 .3 .4 | MIL-S-19500 <br> JAN Quality Level <br> Metallurgically bonded <br> Current rating $\leq 1$ amp <br> Ratio of applied to rated reverse voltage $\leq 0.6$ <br> Max permissible junction <br> temperature $=175^{\circ}$ to $200^{\circ} \mathrm{C}$ |


|  | Table A3 | (concluded) |
| :---: | :---: | :---: |
| Diodes (continued) |  | Ratio of operating forward current to maximum rated forward current $=0.5$ <br> Max case temperature ( $100 \%$ rated load and max junction temperature not exceeded $=25^{\circ} \mathrm{C}$ <br> Power recifier application |
| Photodiodes | 5.1.3.10 | JAN Quality Level |
| Photodiode Detectors | 5.1.3.10 | JAN Quality Level |
| Quartz Crystals | 5.1.15 | MII-C-3098 |
| Relays | 5.1 .10 | MIL SPEC Quality Level M Temperature rating $=125^{\circ} \mathrm{C}$ Ratio of operating load current to rated resistive load current $=0.5$ Cycles per hour < 1 High speed application Dry reed construction SPST action |
| Fiber Optic Cables | 5.1 .15 | Length $\leq 1 \mathrm{Km}$ <br>  |
| Fiber Optic Connectors | 5.1 .15 |  |
| Electrical Connectors | 5.1 .12 | MIL SPEC Quality <br> Type $B$ insert material <br> Number of active contacts $=3$ <br> 5 to 50 mating/unmating cycles per 1000 hours |
| Printed Wiring Boards | 5.1 .13 | MIL-P-55110 <br> One two-sided board per module 500 plated through holes per module |
| Solder Connections | 5.1 .14 | Kuflow lap solder <br> 500 solder connections per module |

To implement the optical link between modules, the line driver/receiver indicated on NASA drawings A14-82-235-101 and -102 (part number 75118) was replaced. Each line driver was replaced by a SNJ55113 lins driver and a photo diode, and each line receiver was replaced by a $S N J 55115$ line receiver, and $a$ photo diode detector. The basis for this subsiitution was that reference 6 contained failure rate data for thest devices, and no data related to currently available optical urivers/receivers could be obtained. However, these devices contain the basic hardware to implement the optical drivers/receivers, and the data should be reasonably accurate.

The design of the sensor voter module as described in NASA drawing A14-82-235-102 was modified slightly for the output voter module. To provide an analog output, the output driver for each actuator was replaced by an 8 bit digital-to-analog converter (DAC-08A), control logic (SNJ54LSO2 quad NOR gates), and a differential driver as shown in figure A1.

The failure rate for the flux summer module was calculated based on the design as shown in figure A2. The module failure rates do not include the electrical/mechanical interface (in figure A2, the LVDT).

The analog circuits on both the actuator voter and flux summer modules require other than a +5 V power supply. The design assumed for the power supplies is shown in figure A3.

The 8 bit microprocessor chip on all modules (C8751H-11) consists of a microprocessor and on-chip RAM (128 X 8) and ROM ( 4 K X 8). The composite failure rate for the chip was calculated by determining the failure rates for each sub-component (processor, RAM, and ROM) and summing the three results.
$\stackrel{\text { B. }}{\substack{\text { s. }}}$
 Dac-08A .
Figure A1. Actuator Voter Differential Output Stage.




Figure A3. DC Power Supply

A summary of the failure rates for each of the components in each of the three environments under study is included in table A4. The component parts count for each module is shown in table A5.

Table A4 COMPONENT FAILURE RATES(FAILORES/10**6 HOURS)

| COMPONENT | SPACE CRAFT | HELICOPTER | AIR TRANSPORT |
| :---: | :---: | :---: | :---: |
| C8751 | 2.059834 | 5.569568 | 5.410203 |
| D8086 | 0.586990 | 1.595600 | 1.465600 |
| C8087 | 1.430970 | 3.441400 | 3.309000 |
| D2764 | 0.504830 | 1.659030 | 1.561530 |
| HM6116P | 0.389820 | 1.451700 | 1.352700 |
| MD8282 | 0.016609 | 0.096705 | 0.050205 |
| MD8284A | 0.015914 | 0.087330 | 0.046830 |
| MD8286 | 0.011860 | 0.083900 | 0.039400 |
| MD8288 | 0.032147 | 0.132056 | 0.083231 |
| HD1-6402 | 0.281900 | 0.235450 | 0.110950 |
| 54 LSO | 0.005231 | 0.045853 | 0.019853 |
| 54 LSO 4 | 0.005400 | 0.046360 | 0.020360 |
| 54 LS 10 | 0.005128 | 0.045544 | 0.019544 |
| 54 IS 74 | 0.005986 | 0.048660 | 0.022160 |
| 54 LS125 | 0.005497 | 0.046480 | 0.020480 |
| 54 LS 138 | 0.007414 | 0.059850 | 0.027350 |
| 54LS139 | 0.007550 | 0.060250 | 0.027750 |
| 54LS 367 | 0.007123 | 0.058286 | 0.026286 |
| 54LS368 | 0.007051 | 0.058054 | 0.026054 |
| MC7805 | 0.017420 | 0.085500 | 0.066500 |
| MC7824 | 0.017420 | 0.085500 | 0.066500 |
| DAC08A | 0.055840 | 0.282 .300 | 0.212300 |
| LM118 | 0.018710 | 0.157350 | 0.119850 |
| OPT TRAN | 0.063460 | 0.455150 | 0.219910 |
| OPT RECV | 0.178930 | 0.892950 | 0.662050 |
| OPT CONN | 0.100000 | 0.100000 | 0.100000 |
| RESISTOR | 0.000380 | 0.010450 | 0.001064 |
| TRIM RES | 0.016200 | 0.655200 | 0.081000 |
| CAP 33 | 0.003744 | 0.244200 | 0.084150 |
| CAP .036 | 0.003744 | 0.115440 | 0.039780 |
| ZENER | 0.002550 | 0.076140 | 0.030600 |
| PWRDIODE | 0.000929 | 0.030193 | 0.011151 |
| CRYSTAL | 0.200000 | 0.200000 | 0.200000 |
| RELAY | 0.016886 | 0.816242 | 0.067543 |
| PC BOARD | 0.003000 | 0.060000 | 0.012600 |
| PC SOLDR | 0.040000 | 0.640000 | 0.120000 |
| ELEC CON | 0.002325 | 0.058311 | 0.011625 |
| OPT LINE | 0.100000 | 0.100000 | 0.100000 |

Table A5
COMPONENT PARTS COUNT

| Sensor | Input | Uutput | Actuator |
| :--- | :--- | :--- | :---: |
| Module | Voter/ Voter | Driver |  |
|  | Comp. | Module | Module |
|  | Module |  |  |


| 08751 | NC+1 | NO+3 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: |
| D8086 | 1 | 4 | 1 | 0 |
| C8087 | 1 | 4 | 1 | 0 |
| D2764 | 2 | 8 | 2 | 0 |
| HM6116P | 8 | 26 | 2 | 0 |
| MD8282 | 2 | 8 | 2 | 0 |
| MD8284A | 1 | 4 | 1 | 0 |
| MD8286 | 3 | 11 | 2 | 0 |
| MD8288 | 1 | 4 | 1 | 0 |
| HD1-6402 | 1 | 2 | 0 | 0 |
| 54LSO2 | 0 | 1 | 1 | 1 |
| 54LSO4 | 0 | 1 | 1 | 0 |
| 54LS10 | 1 | 3 | 0 | 0 |
| 54IS74 | 3 | 12 | 3 | 0 |
| 54LS125 | NC/4 | ( $\mathrm{NO} / 4$ ) +1 | 1 | 0 |
| 54LS138 | 2 | 6 | 0 | 0 |
| 54LS139 | 0 | 1 | 1 | 0 |
| 54LS367 | 1 | 4 | 1 | 0 |
| 54LS368 | 2 | 6 | 0 | 0 |
| MC7805 | 1 | 4 | 1 | 1 |
| MC7824 | 0 | 0 | 0 | 1 |
| DAC08A | 0 | 0 | 0 | 1 |
| LM118 | 0 | 0 | 0 | 7 |
| OPT TRAN | NC | $\mathrm{NO}+1$ | 0 | 0 |
| OPT EECV | NC | NO+1 | 0 | 0 |
| OPT CONN | 2*NC | ( $2 * \mathrm{NO}$ ) +2 | 0 | 0 |
| RESISTOR | NC+9 | $\mathrm{NO}+2 \mathrm{O}$ | 5 | 23 |
| TRIM RES | 0 | 0 | 0 | 1 |
| CAP 33 | NC+1 | NO+1 | 0 | 1 |
| CAP . 036 | NC+1 | $\mathrm{NO}+1$ | 0 | 0 |
| ZENER .- | 1 | 4 | 1 | 2 |
| PWRDIODE | 4 | 16 | 4 | 8 |
| CFISTAL | $(\mathrm{NC/2})+2$ | ( $\mathrm{NO} / 2$ ) +7 | 1 | 0 |
| RELAY | 0 | 0 | 0 | 1 |
| PC BOARD | 2 | 4 | 1 | $\dagger$ |
| PC SOLDR | 2 | 4 | 1 | 1 |
| ELEC CON | 1 | 4 | 1 | 4 |
| OPT LINE | NC | NO+1 | 0 | 0 |

NC = Number of input voter/computation modules NO = Number of output voter modules

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