Mass Transfer from a Circular Cylinder - Effects of Flow Unsteadiness and "Slight Nonuniformities"
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September 1984

Prepared for
NATIONAL AERONAUTICS ANO SPACE ADMINISTRATION Lewis Research Center Under Grant NSG-3262

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## LIST OF SYMBOLS

| C |  | mass concentration |
| :---: | :---: | :---: |
| D | - | diameter of test cylinder |
| 2 | - | diffusion coefficient |
| e | - | AC voltage component |
| E | - | DC voltage component |
| f | - | frequency of oscillation in cycles per second |
| $\mathrm{h}_{\text {m }}$ | - | mass transfer coefficient |
| $\dot{\text { m }}^{\prime \prime}$ | - | mass transfer rate per unit area per unit time |
| M | - | mesh size of a turbulence generating screen, measured from the center of one wire to the center of an adjacent wire |
| n | - | frequency of turbulence in cycles per second |
| Nu | - | Nusselt number |
| P | - | pressure |
| Pr | - | Prandtl number |
| $\mathrm{Pr}_{t}$ | - | turbulent Prandtl number $=\varepsilon / \varepsilon_{\mathrm{H}}$ |
| R | - | radius of the test cylinder |
| Re | - | Reynolds number |
| Sc | - | Schmidt number |
| $\mathrm{Sc}_{\mathrm{t}}$ | - | turbulent Schmidt number $=\varepsilon / \varepsilon_{\mathrm{M}}$ |
| Sh | - | Sherwood number |
| St | - | Strouhal number |
| t | - | time |
| T | - | temperature |
| Tu | - | turbulence level $=\sqrt{\overline{u^{\prime}{ }^{2}} / \mathrm{U}}$ |


| $u^{\prime}$ | streamwise turbulent velocity |
| :---: | :---: |
| U | local mean velocity |
| $\mathrm{U}_{\infty}$ | - mean velocity far upstream of test cylinder |
| $\Delta \mathrm{U}$ | perturbation velocity |
| v | cross-stream, cross-span mean velocity component |
| $\mathrm{w}^{\prime}$ | spanwise turbulent velocity |
| W | spanwise mean velocity |
| x | streamwise coordinate measured from the cylinder's axis in the upstream direction |
| X | streamwise coordinate measured from the screen position in the downstream direction. 1 |
| 2 | spanwise coordinate measured from the center of the naphthalene strip |
| $\triangle$ | naphthalene sublimation depth |
| $\varepsilon$ | eddy diffusivity of momentum |
| $\varepsilon_{h}$ | eddy diffusivity of heat |
| $\varepsilon_{\text {m }}$ | eddy diffusivity of mass |
| 0 | - density |
| $\rho_{\text {NS }}$ | - density of solid naphthalene |
| $\rho_{\mathrm{N}, \mathrm{V}}$ | density of naphthalene vapor at the surface |
| $v$ | - kinematic viscosity |
| $\nu_{T}$ | eddy viscosity |
| $\phi$ | - angular coordinate measured along the surface of the cylinder from the stagnation line |
| $\phi_{0}$ | - maximum angular displacement of oscillation |

## PART 1

## INTRODUCTION

The design practices utilized by the modern gas turbine industry are at a critical stage of development. Currently designs are based upon steady two-dimensional modeling of the gas flow around blades or vanes. Quasi-steady and quasi-two-dimensional design systems are also in use to account for "slow" transients and certain three-dimensional effects. The recent advances in finite-difference, steady flow boundary layer programs allow the designer to account for such important effects as strong favorable pressure gradients, free stream turbulence, low Reynolds number, and surface curvature. These highly sophisticated treatments have led the designer quite far in predicting the aerodynamic losses and heat loads in a turbine and, accordingly, any design system advances of a steady, twodimensional nature will be of only secondary importance. (The single exception to this is the problem of predicting boundary layer transition from laminar to turbulent flow.)

Significant advances in turbine technology will require exact knowledge of the manner in which the flow proceeds through a turbine. In reality, this flow is three dimensional in nature and contains, in addition to the random fluctuations of turbulence, a regular periodic unsteadiness. The necessity of including three-dimensional effects in a next generation design system has been recognized and research in this regard has already begun; however, only a few in the turbine field recognize. the equal importance of unsteady flows. Practically no relevant information on unsteady flows is currently available to the designer.

Of particular importance is the effect of these unsteady flows upon the local heat transfer rate in the leading edge region of turbine blades. Since the effectiveness of cooling schemes in this region is limited by geometrical considerations and since the maximum heat load per unit area is on the leading edge of a blade, blade life critically depends upon leading edge design. Currently the uncertainty on leading edge design schemes is on the order of $70 \%$, and the degree of inaccuracy in leading edge heat transfer predictions due to the effects of unsteady flows remains, as of yet, unknown. The initial intent of the reported research effort was to partly fill this void.

Examining the flow through a turbine, it is obvious that, in order for work to be extracted, the streamlines of the flow must be unsteady. Present design systems account for this unsteadiness by assuming that the flow leaves a blade row in a steady uniform manner and at a constant exit angle; therefore, relative to the following blade row, which is moving with respect to the preceding row, the inlet velocity is steady. The analysis on the following blade row is then performed by examining the flow relative to the individual blades. The flow leaving a blade row is in reality, however, nonuniform and highly unsteady. A number of factors contribute to the unsteadiness of the exiting flow. These include the effects of wakes formed by the passage vortex and leakage flows, the secondary flows caused by the inlet velocity and temperature profiles, and the flow fluctuations originating in the burner; however, probably the most significant type of unsteadiness in the flow through a turbine is that created by the wakes behind the individual airfoils. Due to the variations of velocity and temperature
in these wakes, the flow relative to the following row fluctuates in a regular periodic manner.

To illustrate this point, the wake behind a row of airfoils is depicted two dimensionally in Fig. 1. Using a turbulent wake calculation for a typical turbine situation, the maximum deficits of velocity and total temperature at the leading edge position of the following row will be approximately

$$
\frac{U_{\infty}-U}{U_{\infty}}=.17 \quad \frac{T_{\infty}-T}{T_{\infty}-T_{c}}=.13
$$

respectively, where $U$ and $T$ are the wake centerline values and $T_{c}$ is the coolant inlet temperature. (For highly loaded and cooled blades these values are even higher.) The wake width, 2 b , at this position may also be estimated and is found to be on the order of the gap width, $\tau$. There is hence a slight interference between adjacent wakes, although they are not fully mixed.

In relation to a position fixed with respect to the rext blade row, the individual wakes of the airfoils in the preceding row pass at a period equal to the pitch, $P$, of the preceding row divided by the wheel speed, wr. Since the fluid in the wakes is moving slower than the mainstream fluid, it drifts upstream. The magnitude of this velocity deficit varies as the wake passes, and hence the flow incident to the second blade row varies both in direction and magnitude with time; that is, the incident flow is unsteady. To illustrate this effect, the velocity triangles at an inter row position are depicted in Fig. 2. Here velocities relative to the rotating row are depicted by the subscript $R$ and the wake vectors by dashed lines. All vectors are assumed to be parallel at the first row


Figure 1. Airfoil wakes


Figure 2. Velocity triangles at an interrow position
exit. In addition to the velocity deficit there is also a temperature deficit in the wake fluid as a result of both the decreased velocities and the injection of coolant along the surface of the upstream blade. This deficit is also a function of time when examined from a reference frame fixed with respect to the next blade row. Consequently, the flow incident on this second blade row is unsteady with fluctuations in: 1) its angle of attack, 2) its magnitude, and 3) the freestream temperature. Incidently, since the turbulence characteristic of the wake is different than that of the mainstream, it also varies.

As a part of an ongoing investigation into these unsteady effects, the current research effort examined the effect of a periodic variation in the angle of attack upon the local heat transfer rate in the leading edge region of a turbine blade. To model this effect, a simple and rather basic experiment was used. The flow arrangements of the experiment performed are schematically shown in Fig. 3. Since the leading edge region in most blade designs is formed by a cylindrical surface, a circular cylinder was used as a large scale model of the leading edge region. In all of the experiments a nominally uniform steady flow with a superimposed level of turbulence was used. To establish a basis of comparison for later tests, the initial series of experiments, illustrated in Fig. 3a, were performed on a stationary cylinder. The results of these tests can also be compared with the large volume of currently available measurements of the transfer rate from a circular cylinder in a uniform flow. For the unsteady phase of the investigation, the cylinder was oscillated rotationally about its axis. This flow configuration, illustrated in Fig. 3 b , simulates the fluctuation in the angle of attack


3a. Stationary cylinder


3b. Oscillating cylinder

Figure 3. Experimental configurations
of the flow incident to the turbine blade, since the incident flow angle fluctuates relative to the test cylinder. The parameters relevant to the experiment were chosen to model the actual turbine situation.

The oscillation of the test cylinder made the use of a heat transfer measurement technique unrealistic, since a heat transfer test body requires hundreds of electrical heating and thermocouple connections. These would fare poorly through the literally half-million cycles necessary to complete a single test. For this reason, a mass transfer measurement technique was utilized in the experiments. As will be discussed later, heat transfer information can be inferred from the mass transfer. results using the well-known heat-mass transfer analogy.

During the investigation, a remarkable three-dimensional effect was observed. Although the flow field incident to the test cylinder was "nominally" uniform with a mean velocity constant to with $\pm .2 \%$, large variations in the local transfer rate along the stagnation line were observed. A separate investigation into the nature and causes of this phenomena became a significant portion of the final research effort. To the author's knowledge, the reported measurements of spanwise variations in the local transfer rate and their connection to the incident flow field are the first of their kind. The results suggest that the well studied stagnation flow situation is, as of yet, not fully understood. As will be discussed later, this flow is, in a respect, unstable with significantly large deviations from the typical two-dimensional models. The results of the current research suggest that the full characterization of realistic stagnation flow fields, such as those found in a turbine, should consider this type of effect.

## PART 2

## HISTORICAL REVIEW

Numerous investigations, both theoretical and experimental, have been conducted to determine the heat transfer rate from a cylinder in a high Reynolds number crossflow. For the most part, these studies have assumed the incident flow field to be nominally steady and uniform, and that the effects of turbulence are also two dimensional in the average sense. For the case without turbulence, the usual theoretical treatment, first utilized by Frossling [1] and later by Merk [2] is to use a laminar boundary layer analysis together with an experimentally determined freestream velocity distribution to yield the local transfer rate over the forward portion of the cylinder up to separation. An analysis valid for the turbulent wake found after separation has yet to be presented. The laminar analyses demonstrate that the local nondimensional heat transfer coefficient, Nu , is dependent only on the incident Reynolds number, Re, and the Prandtl number, $\operatorname{Pr}$, a ratio of the diffusivity of vorticity, $v$, to the diffusivity of heat, $\alpha$. In the leading edge region, the dependence of the local heat transfer coefficient on these parameters is well represented by the relation

$$
\mathrm{Nu} \propto \operatorname{Re}^{1 / 2} \mathrm{Pr}^{\mathrm{n}}
$$

where the selected value for the coefficient $n$ depends upon the Prandtl number range of interest.

Early experiments to determine the rate of heat and mass transfer from cylinders in crossflow, such as those of Drew and Ryan [3], Small [4], and Schmidt and Wenner [5], were for the most part incompatible with each
other and with the developed laminar theory. This discord was somewhat clarified by subsequent investigations which quantitatively demonstrated the substantial effect of incident turbulence on the local transfer rate. The first results of this type were reported by Comings, Clap and Taylor [6]. The additional intensive investigations of Bollen [7] and Zapp [8] indicated that heat transfer distributions characteristic of Reynolds numbers higher than the incident Reynolds number were obtained when the incident turbulence level was elevated and increases in the local heat transfer as large as $40 \%$ were observed. More recent studies [.9-17] provide additional proof of the significant increase in the local transfer rate with an increase in turbulence level. Additionally a number of recent investigations, notably those of Yardi and Sukhatme [18] and Traci and Wilcox [19], suggest that not only is the turbulence level important but also its scale. In particular, it appears that the maximum effect of incident turbulence occurs when its integral length scale is on the order of ten times the boundary layer thickness. Unfortunately, the data from measurements of the transfer rate in turbulent fields is too widely scattered to provide a precise empirical relation and the comparison of the data from different investigators is limited by the rather widespread variation in the methods utilized to measure and report turbulence. Generally, the data suggests that, when the turbulent length scale is kept constant, the dependence of the local heat transfer coefficient on the turbulent intensity, Tu , is of the form

$$
\mathrm{Nu} / \sqrt{\operatorname{Re}}=\mathrm{fnc}(\mathrm{Tu} \sqrt{\operatorname{Re}})
$$

In addition to the nominally two-dimensional work, theoretical and experimental investigations have been conducted for spanwise periodic
incident flows. Treating only the region near stagnation, Sutera, Maeder and Kestin [20] and Sutera [21] obtained solutions to the laminar boundary layer equations which exhibit a regular spanwise pattern of streamwise vortices lying within the boundary layer. The theoretical work of Sadeh, Sutera and Maeder [22] suggests that spanwise periodic disturbances in the incident flow can be unstable insofar as they are greatly amplified as the flow approaches stagnation. This conclusion, although derived in a questionable manner, is confirmed by a number of flow visualization studies performed in the wakes of cylinders and turbulence grids. A quasisteady vortical behavior is remarkably evident in the results of Colak-Antic [23] obtained using a hydrogen bubble technique and in the smoke injection visualization work of Nagib and Hodson [24]. The hot-wire studies performed by Hassler [25] quantitatively demonstrate the development of the wake field behind a row of cylinders into a quasiregular unsteady flow on the stagnation zone. As pointed out in the extensive repiew of the subject presented by Morkovin [26], the experimental work to date strongly suggests the existence of an inherent instability in stagnation flows which give rise to a quasisteady vortex cell structure. As discussed by Morkovin, a full physical understanding of the phenomena has yet to be presented, and it is not yet known whether the observed three dimensionality can exist without being driven by slight irregularities in the incident flow field. The current research effort shows that the magnitude of the effect of the phenomena on the local transfer rate, even when driven by very small irregularities in the oncoming flow, necessitates a substantial alteration in the current physical conception and modeling of realistic stagnation flows.

A number of theoretical investigations have also been performed in an attempt to evaluate the effects of periodic unsteadiness in the flow incident to the stagnation zone. Lighthill [27] has presented a general theory to model the response of a laminar boundary layer to periodic fluctuations in the magnitude of the external flow field, and has applied the theory to stagnation flows. Rott [28] and Glauert [29] have derived exact solutions for the case of a flow stagnation on a plate which oscillates in its own plane. In this case the flow fluctuates not only in magnitude but also in direction. Recently, Childs [30] theoretically considered the problem of a circular cylinder oscillating rotationally in a steady incident stream, bringing into consideration the additional effects of curvature. In this case, the flow relative to the cylinder fluctuates in direction only. Expressions for the unsteady laminar skin friction and the local heat transfer coefficient were derived by extension of the methods of Lighthill, Rott and Glauert. The results suggest that the timeaveraged, local transfer rate is slightly decreased but differs by less than $4 \%$ from the steady case. To date, the importance of incident turbulence to the effects of periodic unsteadiness in the flow field has not been theoretically or experimentally investigated. The reported research includes a study of this aspect of the problem.

## PART 3

## THEORETICAL CONSIDERATIONS

### 3.1 Constituent Equations and Significant Parameters

Consider a cylinder oscillating rotationally in an incompressible laminar flow as depicted in Fig. 4a. The flow is assumed to be steady, unifarm and two dimensional. A fluid (Fluid 2), different than that of the mainstream flow (Fluid 1), is transported from the cylinder into the flow by a mass transfer process. At the surface of the cylinder the mass concentration of Fluid 2 is kept constant at a value $C_{w}$. The concentration of Fluid 2 in the undisturbed $f$ low is $C_{\infty}$. By virtue of the heatmass analogy, discussed in Sec. 3.2, this problem is analogous to that depicted in Fig. 4b, where heat is transported from cylinder whose surface is kept at a constant temperature, $T_{w}$ into a fluid whose temperature far upstream of the cylinder is $\mathrm{T}_{\infty}$.

For this discussion, a boundary layer coordinate system, depicted in Fig. 4a, will be used. This reference frame is fixed in space. The coordinate $x$ indicates the distance along the surface of the rotating cylinder from a line which passes through the cylinder's axis. The coordinate $y$ is measured from the surface of the cylinder. The corresponding velocities are denoted by $u$ and $v$, and the pressure by $p$. The local mass concentration of Fluid 2 is denoted by $C$. The position of a point $P$ on the surface of the cylinder is described, with respect to this coordinate system, by

$$
x(P)=x_{0}(P)+A g(2 \pi f t)
$$

where $x_{0}(P)$ denotes its time-averaged position, A is the maximum displacement,


4a. Mass transfer - constant surface concentration


4b. Heat transfer - constant surface temperature

Figure 4. Illustration of transfer processes from an oscillating cylinder
$g$ is a periodic function, $f$ is the frequency of oscillation and $t$ denotes time. The surface velocity is then given by $A \frac{d g}{d t}$.

The appropriate boundary layer equations are

$$
\begin{array}{ll}
\frac{\partial u}{\partial x}+\frac{\partial v}{\partial y}=0 & \text { (Continuity) } \\
\frac{\partial u}{\partial t}+u \frac{\partial u}{\partial x}+v \frac{\partial u}{\partial y}=U \frac{\partial U}{\partial x}+v \frac{\partial^{2} u}{\partial y^{2}} & \text { (Conservation of momentum) } \\
\frac{\partial C}{\partial t}+u \frac{\partial C}{\partial x}+v \frac{\partial C}{\partial y}=\theta \frac{\partial^{2} C}{\partial y^{2}} & \text { (Mass diffusion equation) }
\end{array}
$$

where $U(x)$ is the free stream velocity external to the boundary layer, and $v$ denotes the kinematic viscosity and is assumed to be constant. The diffusion coefficient for the diffusion of Fluid 2 into Fluid 1 is 9 . The boundary conditions are

$$
\begin{aligned}
& C=C_{w}, u=A \frac{d g}{d t}, \quad v=0^{\dagger} \text { at } y=0 \\
& C \rightarrow C_{\infty}, u \rightarrow U(x) \text { as } y \rightarrow \infty
\end{aligned}
$$

It is appropriate to put the governing equations into a dimensionless form. For this purpose, the dimensionless quantities

$$
\begin{array}{cl}
u^{*}=u / U_{\infty} & x^{*}=x / R \\
v^{*}=v / U_{\infty} & y^{*}=y / R \\
U^{*}=U / U_{\infty} & t^{*}=f t \\
C^{*}=\frac{C-C_{w}}{C_{\infty}-C_{w}}
\end{array}
$$

[^0]are defined, where $R$ denotes the cylinder's radius and $U_{\infty}$ the magnitude of the flow velocity far upstream of the cylinder. Using these quantities, the governing equations can be written in a nondimensional form as
\[

$$
\begin{aligned}
& \frac{\partial u^{*}}{\partial x^{*}}+\frac{\partial v^{*}}{\partial y^{*}}=0^{\prime} \\
& \left(\frac{f D}{U_{\infty}}\right) \frac{\partial u^{*}}{\partial t^{*}}+u^{\star} \frac{\partial u^{*}}{\partial x^{*}}+v^{*} \frac{\partial u^{*}}{\partial y^{*}}=U^{*} \frac{\partial U^{\star}}{\partial x^{*}}+\left(\frac{U}{U_{\infty} D}\right) \frac{\partial^{2} u^{*}}{\partial y^{*}} \\
& \left(\frac{£ D}{U_{\infty}}\right) \frac{\partial C^{\star}}{\partial t^{*}}+u^{*} \frac{\partial C^{\star}}{\partial x^{*}}+v^{*} \frac{\partial C^{*}}{\partial y^{*}}=\left(\frac{A}{v}\right) \frac{\partial^{2} C^{\star}}{\partial y^{2}}
\end{aligned}
$$
\]

and the boundary conditions can be written as

$$
\begin{array}{ll}
C^{*}=0, u^{*}=\left(\frac{A}{D}\right)\left(\frac{f D}{U_{\infty}}\right) \frac{d g\left(t^{*}\right)}{d t^{*}} & \text { at } y^{*}=0 \\
C^{*}=1, \quad u^{*}=U^{*}\left(x^{*}\right) & \text { as } y^{*} \rightarrow \infty
\end{array}
$$

By inspection of these dimensionless equations, it is obvious that the laminar problem is governed by four nondimensional groupings: $\left(\frac{U_{\infty} D}{V}\right),(V / \xi),\left(\frac{f D}{U_{\infty}}\right)$ and $(A / D)$. The first three are the Reynolds number, Re, a ratio of inertial to viscous forces; the Schmidt number, Sc, a ratio of the diffusivity of vorticity to the diffusivity of mass; and the Strouhal number, a nondimensional oscillation frequency. The remaining parameter, (A/D) is the characteristic amplitude of oscillation which will be denoted by $\phi_{0}$. To model the actual turbine situation, the Reynolds number in the reported investigation was varied between 75,000 and 125,000 , and Strouhal numbers from 0.0071 to 0.1406 were used.

An oscillation amplitude of $\phi_{0}=0.105$, which is also characteristic of that in a turbine, was used for the majority of the experiments. The effect of a larger amplitude, $\phi_{0}=0.210$, was also investigated. In the experiments, naphthalene vapor was utilized as the mass transfer substance. The Schmidt number for the diffusion of naphthalene in air is approximately 2.5 .

Since the flow in a turbine contains a degree of superimposed turbulence, the experiments were performed for a number of incident turbulent conditions. Experimentally, turbulence in an incident flow field is typically characterized by a turbulence level, Tu, a ratio of the root mean square turbulent velocity fluctuation to the free stream velocity, and. an integral length scale parameter, $L$, an average eddy size, which is typically nondimensionalized by the diameter of the cylinder, D. Turbulence levels up to $4.9 \%$ were used and L/D varied between 0.012 and 0.188 .

### 3.2 The Analogy Between Heat and Mass Transfer

The existence of a direct analogy between the heat transfer rate from an isothermal surface and the rate of mass transfer from a surface of constant mass concentration is readily demonstrated by an examination of the governing physical equations.

The flow of a constant property fluid is governed by the continuity and Navier-Stokes equations and their appropriate boundary conditions. These equations, and hence the character of the flow, are unaltered by the presence of heat or mass transfer, provided that the properties of the fluid, i.e. its density and viscosity can be assumed to remain constant. In the reported experiments the maximum local mass concentration, that is the ratio of the local density of naphthalene to the density of the air flow, was on the order of $2.9 \%$ hence, this constant property assumption is valid. Additionally, in order for an analogy to exist, the boundary conditions on the equations of motion for the heat and mass transfer situations must be identical. For the heat transfer case, the velocities both normal and perpendicular to the surface are zero; however, for the mass. transfer case there is a finite velocity, $\mathrm{V}_{\mathrm{w}}$, at the boundary due to the transport of vapor from the surface. This velocity is equal to the mass flow rate, $\dot{m}^{\prime \prime}$, of the diffusing vapor divided by its density. For the present case the velocity is on the order of $2\left(10^{-5}\right) \mathrm{ft} / \mathrm{sec}$. Since the velocity of the mainstream is on the order of $30 \mathrm{ft} / \mathrm{sec}$, only very small errors are incurred by assuming $\mathrm{V}_{\mathrm{w}}=0$.

Having shown that the flow fields in the mass and heat transfer situations are essentially identical, the analogy between the two processes can be demonstrated by an examination of the relevant transfer equations
and boundary conditions. To maintain generality, the turbulent form of the equations will be used.

Mass transfer in á two-component, nonreactive system is characterized by the equation

$$
\frac{D C^{*}}{D t^{*}}=\frac{1}{\operatorname{ReSc}^{S c}} \frac{\partial}{\partial \mathrm{x}_{i}{ }^{*}}\left[\left(1+\frac{\varepsilon}{v} \frac{S c}{S c_{t}}\right) \frac{\partial C^{\star}}{\partial \mathrm{x}_{i}{ }^{\star}}\right]
$$

where $\frac{D}{D t}$ denotes the material derivative and an indicial notation has been employed for convenience. The quantity $C *$ denotes a ratio of mass concentrations:

$$
C^{*}=\frac{C-C_{w}}{C_{\infty}-C_{w}}
$$

where $C_{w}$ is the concentration of the diffusing substance at the wall and $\mathrm{C}_{\infty}$ is the concentration of the unaffected flow. $\mathrm{Sc}_{t}$ is the turbulent Schmidt number, defined as the ratio of the turbulent diffusivity of momentum to the turbulent diffusivity of mass; and is in general a function of position, Reynolds number and Schmidt number. The relevant boundary conditions are

$$
\begin{aligned}
& C^{*}=0 \text { at the surface } \\
& C^{*} \rightarrow 1 \text { at a distance far from the surface }
\end{aligned}
$$

The heat transfer process is described by the dimensionless turbulent energy equation:

$$
\frac{D T^{*}}{D t^{*}}=\frac{1}{\operatorname{Re} \cdot \operatorname{Pr}} \frac{\partial}{\partial \mathrm{x}_{i}^{*}}\left[\left(1+\frac{\varepsilon}{\nu} \frac{\operatorname{Pr}}{\mathrm{Pr}_{t}}\right) \frac{\partial T^{\star}}{\partial \mathrm{x}_{i}{ }^{*}}\right]
$$

where the coordinates and velocities are nondimensionalized by characteristic parameters $T^{*}$ is the ratio

$$
T^{*}=\frac{T-T_{W}}{T_{\infty}-T_{W}}
$$

where $T_{w}$ is the temperature of the isothermal surface, $T_{\infty}$ is the temperature of the fluid far from the wall, and $T$ is the local fluid temperature. $\operatorname{Pr}_{t}$ denotes the turbulent Prandtl number defined as the ratio of the turbulent diffusivity of momentum, $\varepsilon$, to the turbulent diffusivity of heat. In general, $\mathrm{Pr}_{t}$ varies with position, Reynolds number, and Prandtl number. The appropriate boundary conditions for the energy equation are

```
T* = 0 on the surface
T* + 1 at a distance far from the surface
```

The two descriptive transfer equations are seen to be of identical form provided that $\operatorname{Pr}_{t}=S c_{t}$, an assumption which is well supported by experimental evidence. Therefore, since the imposed boundary conditions are identical, the two equations have the same solution when $T$ * and $\operatorname{Pr}$ are replaced by C* and Sc, respectively.

A solution to the equations would provide the local transfer rates on the surface. Typically, these are given in nondimensional form by the Sherwood number, Sh, and the Nusselt number, Nu, which are defined as

$$
\begin{aligned}
& S h=(\partial C * / \partial n *)_{W} \\
& N u=\left(\partial T * / \partial n^{*}\right)_{W}
\end{aligned}
$$

where $n$ is a nondimensional coordinate normal to the surface and the subscript w indicates that the values at the surface are used. Since the definitions of these quantities are also similar, it is obevious that for a specific point on the surface

$$
\begin{aligned}
& \mathrm{Sh}=\mathrm{fnc}(\mathrm{Re}, \mathrm{Sc}) \\
& \mathrm{Nu}=\mathrm{fnc}(\mathrm{Re}, \mathrm{Pr})
\end{aligned}
$$

where the functions in the two equations are identical. It is then obvious that distributions of the local heat transfer rate can be inferred from the measured mass transfer distributions by simply replacing Sh and Sc by Nu and Pr , respectively. The mass transfer results may be considered as heat transfer results at a Prandtl number equal to the appropriate Schmidt number.

For the case at hand, flow over a circular cylinder, the dependence of the Nusselt number on the Prandtl number may be detemined from a laminar boundary layer series solution of the type used by Frossling [1]. This dependence is well represented by
$\mathrm{Nu} \propto \mathrm{Pr}^{\mathrm{n}}$
where the value of $n$ depends upon the Prandtl number range of interest. Naphthalene, which was used in the experiments as the mass transfer substance, has a Schmidt number of approximately 2.5. Utilizing an experimentally determined velocity distribution and the calculation procedures of Childs \{30], the results of laminar analyses for Prandtl numbers of 2.5 and .7 were compared, and a value of $n=.38$ was determined. Hence, the heat transfer coefficients on a circular cyiinder in a cross stream may be calculated from the experimental mass transfer results by the equation

$$
\begin{array}{r}
\mathrm{Nu}=\operatorname{Sh}\left(\frac{\mathrm{Sc}}{\mathrm{Pr}}\right) \cdot 38 \\
\mathrm{Sc} \approx 2.5 \quad \operatorname{Pr} \approx .7
\end{array}
$$

## PART 4

## EXPERIMENTAL APPARATUS AND PROCEDURE

### 4.1 Wind Tunnel Apparatus

The experiments were performed in a low speed, open circuit wind tunnel built specifically for the study of turbine blade leading edge problems. This facility is schematically illustrated in Fig. 5. The air supply is provided by a centrifugal blower with variable angle inlet control vanes for adjusting the tunnel flowrate. The blower rotates at 1820 rpm producing a maximum flowrate of 13500 cfm . From the blower the air passes through a plenum, which is schematically illustrated in Fig. 6a, containing a geries of screens and baffles and a honeycomb flow straightener and is then accelerated through a two-to-one contraction nozzle into a turbulence generating section. The flow passes from the turbulence section into the working section of the tunnel in which the test cylinder is located. The flow then exits the tunnel and circulates back into the room. As will be explained later, it became necessary to reduce the operating temperature of the tunnel during the mass transfer tests. For this purpose, a large central air-conditioning unit was installed in the tunnel room. Air from this unit mixes with that exiting the tunnel and, in this manner, the operating temperature for experiments can be held constant to within $2^{\circ} \mathrm{F}$. Temperatures on the order of $65^{\circ}$ to $70^{\circ} \mathrm{F}$ were typically chosen. Through the course of each test, the temperature of the incident flow was monitored using a thermocouple placed in the flow. The velocity of the incident flow was monitored with a pitot static tube. The thermocouple and pitot static tube


Figure 5. Schematic of wind tunnel facility

पот7exnsityuos teumon •eg

Figure 6. Plenum chamber configurations
were installed in the working section of the tunnel ahead of and to either side of the test cylinder as shown in Fig. 5. The positions were chosen to be external to the flow region affected by the presence of the cylinder.

The special requirements of the experiments necessitated the construction of a working section specifically designed for the program. The section measures $18^{\prime \prime}$ high by $30^{\prime \prime}$ wide and is $70^{\prime \prime}$ long. The available flow velocities through the section are such that the Reynolds number of the flow incident to the $6^{\prime \prime}$ diameter test cylinder can be varied between 50,000 and 130,000 ; modeling those typical of incidents flows on the leading edges of turbine blades. For rigidity, the working section was constructed mainly from aluminum channels and plate. A $25^{\prime \prime}$ plexiglass panel on the side of the working section provided access to the test cylinder.

The turbulence generating section was also constructed specifically for this series of experiments. For the generation of turbulence, two types of screens were used; hand manufactured round-bar biplane-grids and commercially produced woven wire meshes. The dimensions of the screens used are given in Table 1. To provide greater variability of turbulence level and length scale, three positions are available in the generating section for installation of the screens, allowing the screens to be positioned $15^{\prime \prime}, 30.5^{\prime \prime}, 53.0^{\prime \prime}$ upstream of the cylinder's leading edge. The highest intensity available from the section was $2.7 \%$. In an attempt to attain higher incident turbulence levels, a large grid was also constructed for installation in the plenum chamber. The utilized plenum chamber configuration is illustrated in Fig. 6b. This screen provided an intensity of $4.9 \%$. The practical lower limit on the turbulence intensity is the
residual intensity of the tunnel which was determined to be approximately $0.6 \%$.

The configuration of the test cylinder in the tunnel is shown in Fig. 7. The cylinder is composed of three sections held together by an axial tension rod. With the rod in place, the upper and lower cans fit into and hold the central test section, which contains a cast insert of naphthalene - a substance that sublimates at room temperatures. With the tension rod removed, the upper can is free to lift vertically through its bearing allowing the test section to be removed for measurement. The naphthalene surface was measured before and after each test, as described in section 4.3 , to determine the amount of local sublimation during the test. The test cylinder was constructed in the manner described to facilitate fast insertion and removal of the test section. As the naphthalene sublimes continually, this was of primary importance to the measurement accuracy. For practical considerations, naphthalene surfaces were cast and measured at a location separate from the wind tunnel laboratory. The measurement and casting procedures will be discussed later.

For the unsteady experiments, the test cylinder with its cast naphthalene surface was oscillated rotationally using a simple direct link driving mechanism mounted to the bottom of the test section. This mechanism is schematically illustraṭed in Fig. 8. It can be shown analytically that for a sufficiently large value of $\mathrm{L} / \mathrm{R} 2$ the oscillation is approximately sinusoidal. This was desirable for easy comparison with theoretical models. A value of $L / R 2 \approx 5$ was used, and the actual oscillation was within $2 \%$ of a true sinusoid. The mechanism is powered by a $1 / 2 \mathrm{hp}$ rotor which drives the smaller disk in the system through a timing


Figure 7. Configuration of test cylinder

Figure 8. Oscillation mechanism
belt and pulley system. Oscillation amplitudes of $\pm 6^{\circ}$ were utilized for the majority of the unsteady experiments, and the frequency was varied up to 5.5 Hz . At higher frequencies, vibrations of the test section generated by the oscillatory motion became significant.

### 4.2 Casting of Naphthalene Surfaces

For the mass transfer tests, naphthalene was cast into the insertable steel test section. The apparatus used for forming the insert is shown in Fig. 9 and a drawing of the test section is shown in Fig. 10 . To cast a naphthalene insert into the test section, the cylindrical stainless steel sleeve shown in the figure is slip fit over the rims of the test section to form a mold cavity. This sleeve was machined with a $1 / 2^{\prime \prime}$ thick wall both to avoid distortion of its shape and to provide a substantial heat sink for the molten naphthalene. In use, this heat sink allowed the freeze front formed by the radial solidification of the naphthalene from both the inner and outer walls of the cavity to be a substantial distance away from the outer surface, providing greater strength and uniformity of the cast surface. To obtain very smooth surfaces, the inner surface of the steel sleeve was honed to a mirror finish when manufactured. To maintain this finish, the sleeve surface was periodically polished with 600 grit wet sandpaper, removing scratches and mars resulting from use.

Before the naphthalene was cast, both the sleeve and the test section were cleaned and degreased by immersion in a bath of clean acetone. After cleaning the mold was assembled with care taken to avoid hand contact with the inner surfaces. Before casting the surface, sufficient time was allowed for the room and casting apparatus to reach a steady temperature

Figure 9. Casting apparatus


Figure 10. Schematic of test section
of approximately $75^{\circ} \mathrm{F}$. Certified grade naphthalene crystals (residue after ignition of $.002 \%$ ) supplied by Fischer Chemical were then melted down in a clean glass flask. The liquid naphthalene was heated to $160^{\circ} \mathrm{C}$. Before pouring, local boiling in the flask was allowed to settle. The liquid naphthalene was poured into the mold through the inner ring of holes visible in Fig. 1.1. The naphithalene traveled down these sprues and entered the mold cavity from the bottom. The outer ring of holes served as vents for the cavity, allowing entrapped air to escape. While the naphthalene in the cavity solidified, it was necessary to periodicaliy unclog the vent holes by pouring hot naphthalene over the top of the mold. This also served to provide additional naphthalene to fill shrink cavities which formed on the surface near the vent holes. This process was continued until molten naphthalene was no longer visible through either the vent holes or the sprues.

The pouring having been completed, the ambient room temperature was lowered to the experimental operating temperature of approximately $65^{\circ} \mathrm{F}$, and sufficient time was allowed for the mold to reach steady state (typically 8 hours). This decrease in temperature from the ambient pouring temperature was found to be vital in order to obtain high quality surfaces. Surfaces cast without this decrease were regionally covered with loose naphthalene dust. Attempts to remove this dust resulted in local dips in the naphthalene surface, which were found to cause significant experimental errors. Efforts to further improve surface quality by using larger temperature changes and quenching of the mold, resulted in cracking of the cast. When the mold had sufficiently cooled, the outer steel ring was removed. To simplify its removal, the entire mold was placed on the


Figure 11. Assembled mold
aluminum pin shown in Fig. 9. (Aluminum was used to avoid damage to the mold,) The specially made drift block also shown in the figure was then positioned onto the steel sleeve, its four pins fitting corresponding holes on the top surface of the sleeve. At this point the sleeve was driven downward with a single, sharp hammer blow to the top of the drift, thus separating the sleeve from the naphthalene case with a shearing motion. To aid in this separation the sleeve was machined with a very slight taper on the order of a tenth of a degree. The substantial blow required to open the mold, necessitated the use of steel for the mold components to avoid impact damage: (A prototype aluminum mold was damaged beyond use after only a few castings.) When removed from the sleeve, the surface of the test section was visually inspected for flaws. A successfully cast surface had a uniform glass-like finish. Significantly flawed surfaces were discarded. (Surfaces with very slight single flaws were occasionally used. In these instances the orientation of the test section in the tunnel was chosen to place the flaw in a region near the rear stagnation point.)

As a final step in the preparation of the test section, the steel rims were dusted with clean towel paper to remove any loose naphthalene particles which could interfere with the profile measurements. Care was taken to minimize contact with the naphthalene surface. Mounting holes and keyways on the top and bottom of the section were also cleaned up at this time to insure a smooth fit onto the measuring table and into the wind tunnel. The prepared test section was then ready to be measured.

It should be pointed out at this time that the procedure
described above was arrived at through a detailed trial-and-error process,
and is somewhat different than that used by other authors. Evacuating the mold cavity as described by Sogin and Subramanian [31] was found to be unnecessary. Other authors utilized a parting dust on the inside of the mold cavity to ease in opening of the mold. This technique was avoided as it would cause contamination of the naphthalene surface and probably give rise to substantial experimental errors. Also to guarantee the utmost surface quality, an insert was cast for each test using new naphthalene. Old surfaces were removed in an acetone bath.

Experience with the mass transfer technique has demonstrated a direct connection between the local smoothness and repeatability of the resultant data. Surface casting procedures should be executed with the utmost care and attention to detail: Flawed surfaces should be discarded. The mass transfer technique can yield very repeatable data, but only if carefully performed.

### 4.3 Naphthalene Surface Measurements

The distribution of the local mass transfer rate on the surface of the test cylinder was determined by differencing profile measurements taken before and after each test. These profile measurements were made using the apparatus shown in Figs. 12 thru 15. When the test cylinder was mounted to the rotary table, four electronic displacement gauges (Federal products type EHE 1048) contacted its surface; one on each steel rim to establish a reference line, and two measuring gauges on the naphthalene surface. The surface could be rotated with respect to the four gauges by means of the rotary table and the two measuring gauges could traverse the naphthalene surface in the spanwise (vertical) direction using the cross slide.

Figure 12. Measuring table


Figure 13. Surface of measuring table


Figure 14. Measuring table with cylinder installed


Figure 15. Contact line of measuring gauges

The test section with its naphthalene surface was positioned on the table by the alignment fixture plate visible in Fig. 12, and shown in greater detail in Fig. 16. This fixture was designed to provide the minimum amount of support necessary to constrain the section against movement, thus optimizing mounting accuracy. It consists of a steel plate holding three support pins which fit into corresponding locations on the base of the test section, as illustrated in Fig. 15. The conically tipped pin fits the small diameter hole in the section, one spherical pin fits the vee-groove and the other simply rests against the flat face of the section's base. The three support pins combined with the rather substantial weight of the test section provide full support. The height of the pins was adjustable to insure that the naphthalene surface was approximately parallel to the axis of rotation of the table.

The alignment fixture was positioned on the rotary table by two adjustable clamp heads bolted to the surface of the table. A third spring loaded head, mounted $135^{\circ}$ from each of the other two, held the plate firmly against the adjustable screws. This apparatus, illustrated in Fig. 13, allowed the test section to be accurately centered on the table and, in addition, eased removal and placement of the section onto the alignment fixture. To remove the section, the table was rotated to place one of the adjustable pins $180^{\circ}$ from the contact line of the measuring gauges, and the reading of the bottom reference gauge contacting the lower steel rim was recorded. The section was then carefully backed away from the gauges using the adjustable head. To install the section the procedure was reversed, the section being slowly moved inward until the previously recorded position was reached. This technique successfully avoided movement

Figure 16. Alignment plate and bottom face
of the gauges relative to one another, which is inherent to the accuracy of the measurements, while sacrificing to a small degree the repeatability of the actual mounting position of the cylinder. However, as will be pointed out below, neither the position of the cylinder on the table nor its repeatability had an effect on the measurement accuracy. The rather small 20 mil measuring range of the gauges did necessitate fairly accurate centering and leveling of the section on the table to avoid overranging the gauges during the measurement traverses. Typically the positioning adjustments were realigned every 5 or 6 tests to avoid exceeding the range limitations during experimental measurements. (The procedure is discussed in Appendix A.)

Errors due to inaccuracies in the cylinder's position were avoided by using the steel rims on either side of the naphthalene insert to establish a reference surface. As this surface remained fixed with respect to the insert, the actual position of the cylinder during the measurement intervals was unimportant. The position of the reference surface was determined by the readings of the two gauges contacting the steel. rims. The two gauges contacting the naphthalene insert provided simultaneous measurement of two points on its surface.

Profile measurements were made before and after each experiment and, by differencing these tare and final profiles, a profile of the local sublimation depth was determined. The procedure used is illustrated in Fig. 17 where the off-horizontal tilt of the section, the gauging range and the sublimation depth have been greatly exaggerated for illucidation. Also, for simplicity, only one measuring gauge is shown on the naphthalene surface. The reading from each transducer is the distance from its zero.


Figure 17. Schematic of measurement procedure
position to its contact point. These are the distances $R U_{T},{ }^{R M} M_{T}$ and $\mathrm{RL}_{\mathrm{T}}$ for the tare measurement; and $\mathrm{RJ}_{\mathrm{F}}, \mathrm{RM} \mathrm{F}_{\mathrm{F}}$ and $\mathrm{RE}_{\mathrm{F}}$ for the final measurement. The distances from the zero position of the measuring and lower gauges to an arbitrary vertical line, which for convenience is chosen to pass through the zero position of the upper gauge, are OM and OL , respectively. (It should be noted that the zeyo positions of the gauges need not lie along a common line and no effort was made in this regard.) The vertical distances from the line of action of the measuring gauge to the lines of action of the upper and lower gages are HU and HL respectively. Using simple geometry

$$
\begin{gathered}
\Delta M_{T}=R M_{T}-\frac{H U}{H T} R L_{T}-\frac{H L}{H T} R U_{T}+\left(O M+O L \frac{H U}{H T}\right) \\
\Delta M_{F}=R M_{F}-\frac{H U}{H T} R L_{F}-\frac{H L}{H T} R U_{F}+\left(O M+O L \frac{H U}{H T}\right) \\
\Delta_{T}=\Delta M_{T} \cos \phi_{T} \\
\Delta_{F}=\Delta M_{F} \cos \phi_{F} \\
\Delta=\Delta_{F}-\Delta_{T}
\end{gathered}
$$

where $\Delta$ is the sublimation depth to be determined. The angles $\phi_{T}$ and $\phi_{F}$ are limited by the gauging range; that is

$$
\phi_{I}, \phi_{F}<\sin ^{-1} \text { (gauging range/section height) }=.020^{\prime \prime} / 3^{\prime \prime}=0.38^{\circ}
$$

hence

$$
\left(\cos \phi_{\mathrm{T}}, \cos \phi_{\mathrm{F}}\right)>0.9999 .
$$

Thus, only very small errors are incurred by assuming

$$
\Delta_{T}=\Delta M_{T}, \quad \Delta \Delta_{F}=\Delta M_{F}
$$

and the full equation for the sublimation depth is

$$
\Delta=\left(R M_{F}-R M_{T}\right)+\frac{H U}{H T}\left(R L_{T}-R L_{F}\right)+\frac{H L}{H T}\left(R U_{T}-R U_{F}\right)
$$

It should be noted that the described measurement calculation assumes that the line of action of each transducer is along a true horizontal, and that the contact points of the transducers on the section lie along a common vertical line. Careful set-up of the transducers was required to avoid substantial deviations from these assumptions. The procedure used is described in Appendix A.

As the output of the gauges is in the form of a voltage, $\Delta M_{T}$ and $\Delta M_{F}$ could be obtained directly by electronic combination of the outputs. An op-amp system was constructed for this purpose; however, due to calibration shifts in the circuit, it was found to be faster and more accurate to read the gauges directly.

Tare or Final profiles of the naphthalene surface consisted of a series of measurements of the type described. The surface can be traversed circumferentially in increments as small as 15 seconds, and vertically in increments as small as 1 mil using the rotary table and the cross slide, respectively. Generally, two types of profiles were utilized in the experiments. . In one type, a purely circumferential traverse in increments of $4^{\circ}$ was used, providing a circumferential distribution of the local mass loss at the spanwise positions of the two measuring gauges. In tests where spanwise distributions were of interest,
the test section was profiled with spanwise traverses, typically in . 05inch increments at a number of degree positions. Typical measuring intervals for either type of profile were on the order of 40 minutes. Due to the rather large $t$ ime required to perform the measurements, it was necessary to perform the experiments in a manner which insured that the naphthalene loss due to free sublimation during the measurement intervals was an insignificant percentage of the total sublimation depth. As the total depth was limited to that measurable with the transducers, this was achieved by performing the experiments at relatively low operating temperatures. Temperatures on the order of $65^{\circ} \mathrm{F}$ were used. The tunnel room temperature is controlled with a central air conditioning unit, and can be kept constant to within $2^{\circ} \mathrm{F}$. The ambient temperature of the measuring room was matched to the operating temperature of the tunnel using a room air conditioner. In this manner the vapor pressure of the naphthalene was kept low, limiting free sublimation losses to approximately . 1 mils for each test. The duration of a test in the wind tunnel was typically on the order of 9 hrs giving maximum sublimation depths on the order of 10 mils. The use of these rather large run times combined with the low operating temperatures greatly enhanced the experimental repeatability by reducing the importance of free sublimation. Typically, the experimental results obtained were repeatable to within about $2 \%$.

Although the free sublimation rate was substantially reduced by this procedure, the measured sublimation depth was compensated for losses during the measurement intervals. To determine the proper compensation, points measured at the beginning of each profile were repeated after its completion. Combining the two sets of readings in the same manner
described above yielded a direct measure of the naphthalene lost during the interval. Tare and final traverses were made in the same order, such that the elapsed time between the two measurements at specific points on the surface was uniform; hence the free sublimation losses around the cylinder were also approximately uniform and equal to those measured. The direct measurement provided fairly accurate determination of the proper compensation for losses during the measurement intervals and, indeed, was found to be far more reliable than calculation attempts. To account for the additional losses during installation of the cylinder, the measured loss depth was increased by a percentage determined from the ratio of the installation time to the measurement time. Typically, the elapsed time from complete installation of the section in the tunnel to complete installation on the measuring table was on the order of 8 minutes, requiring the measured loss to be increased by about $20 \%$.

The techniques that were utilized in the mass transfer measurements were developed in large part: by experience and, in general, the quality of the data obtained improved with time. The initial design conceptions and aspects of the techniques were extensions of procedures used by a number of other authors, such as Sogin and Subramanian [31], Kestin and Wood [14], and, most notably, Taylor [32]; however, the evolved procedure has been found to give a much higher degree of repeatability than those previously reported.

### 4.4 Mass Transfer Data Reduction

Distributions of the local Sherwood number, Sh , a nondimensional mass transfer coefficient, were calculated from the previously discussed profile measurements. Using the measured local depth of naphthalene sublimation, $\Delta$, the time averaged mass transfer rate is

$$
\dot{m}^{\prime \prime}=\frac{\rho_{N S}(\Delta-\delta)}{\tau}
$$

where $\rho_{N S}$ is the density of solid naphthalene and $\tau$ is the time duration of the test and $\delta$ is the loss correction. The mass transfer coefficient, $h_{m}$, is defined as

$$
h_{m}=\dot{m}^{\prime \prime} / \overline{\rho_{N, V}}
$$

where $\overline{\rho_{N, V}}$ is the average density of naphthalene vapor at the surface of the cylinder during the test interval. This was determined by numerical integration of the instantaneous vapor density relation, i.e.

$$
\overline{\rho_{\mathrm{N}, \mathrm{~V}}}=\frac{1}{\tau} \int_{\mathrm{o}}^{\tau} \rho_{\mathrm{N}, \mathrm{~V}} \mathrm{dt}
$$

where the values of $\rho_{\mathrm{NV}}$ were calculated from temperature measurements taken at 1 minute intervals throughout the test. To evaluate the instantaneous density from the measured temperature, the vapor pressure relationship

$$
\log _{10} P \cdot\left[\frac{\nmid \mathrm{bf}}{\mathrm{Ft}}\right]=11.884-\frac{6713}{\mathrm{~T}\left[{ }^{\circ} \mathrm{R}\right]}
$$

given by Sogin [33] was utilized along with the ideal gas law. The Sherwood number is defined as

$$
S h=h_{m} D / \mathcal{S}
$$

Although the reported Sherwood number distributions were repeatable to within $\mathbf{~} 2 \%$, exact knowledge of their accuracy is limited by the unknown accuracy in the utilized Schmidt number and vapor density relations. The values given by Sogin were used both to provide conformity with the measurements of previous investigators and also because they are, to the knowledge of the author, the only reliably determined values. Techniques for estimating the diffusion coefficient theoretically, as reported in [34], suggest values of the Schmidt number between 2.35 and 2.75 Other suggested vapor density relations such as those of [35] and [36] are within $1.5 \%$ of that used in the temperature range of interest.

### 4.5 Turbulence Measurements

Turbulence quantities were measured using the two-channel hot wire anemometer system schematically depicted in Fig. 18. The system consists of two TSI 1051 anemometers, two TSI 1047 signal conditioners which provide AC frequency filtering, a TSI 1015C correlator which provides various combinations of the output signals, and two TSI 1076 mean square voltmeters for the measurement of $A C$ signals. The $D C$ components of the outputs were measured with a TSI 1047 signal averaging circuit and an HP3466A voltmeter. An HP3580A spectrum analyzer was used to determine spectral distributions of the AC signals.

For the measurements, the anemometers were operated in a constant temperature mode; that is the resistance and hence the temperature of the corresponding sensing elements were kept constant via a Wheatstone bridge feedback loop. The output of each anemometer is a voltage which varies with the instantaneous cooling rate of the sensor. When the sensor is


Figure 18. Schematic of hot wire anemometer system
positioned normal to an incident flow field of constant temperature, its cooling rate varies solely as a function of the incident flow rate and hence the output voltage of each anemometer can be directly correlated to the local velocity. As discussed by Bradshaw [37], the commonly utilized correlation function is

$$
U^{.45}=A F(T) E^{2}+B
$$

where $U$ is the mean velocity of the incident flow, $E$ is the $D C$ output voltage of the anemometer and $A$ and $B$ are constants which are adjusted to fit the curve to the response of a particular sensor. The function $F(T)$ accounts for long-term shifts in the flow temperature and is given by Bradshaw [37] as

$$
F(T)=\frac{T_{W}-T_{o}}{T_{W}-T}\left[\frac{T_{0}}{T} \frac{T_{W}+T}{T_{W}+T_{o}}\right]^{.17}
$$

where $T_{0}$ is a reference temperature, $T_{w}$ is the operating temperature of the wire, and $T$ is the fluid temperature. In the reported measurements the wire temperature was $250^{\circ} \mathrm{C}$. The reference temperature used was $21^{\circ} \mathrm{C}$, a typically operating temperature of the tunnel.

Turbulent variations in the flow field generate an $A C$ voltage signal, $e_{T}$. If the magnitude of the turbulent velocity fluctuations is small, the relationship can be considered to be linear, i.e.

$$
\begin{array}{r}
e_{T}=\left.\frac{\partial E}{\partial U}\right|^{\prime}{ }^{\prime} \\
U=U_{0}
\end{array}
$$

where $u^{\prime}$ is the streamwise turbulent velocity component and $U_{0}$ is the measured mean velocity. In addition to the turbulence components of
interest, the AC signal of a real system contains a level of spurious noise generated by a number of sources. In the current research, the ambient noise was found to be a rather predominant portion of the output signals and methods were instituted for its elimination. In particular, pressure variations generated by the intermittent passage of blades in the wind tunnel blower and AC noise generated in the electronics of the measurement system were found to be significant.

The reported turbulence levels and length scales were measured with the test cylinder removed from the tunnel. Two hot wire sensors, TSI type 1218 were used for the removal of noise from the turbulence signals. These sensors were positioned along a line corresponding to the leading edge position of the test cylinder with their wires oriented normal to the flow and normal to their common line. To minimize interference from the probe supports, the probes were held in specially constructed $45^{\circ}$ adapters. This measurement configuration is illustrated in Fig. 19a.

The wires were calibrated in the wind tunnel through the fully connected measurement system to avoid errors due to changes in the sensor configurations and slight miscalibration of the electronics. The DC portions of the output voltages, denoted by $E_{1}$ and $E_{2}$, were recorded along with the flow temperature at a number of incident flow rates, which were measured with a pitot static tube positioned near the wires. The correlation function was curve fit to the data by selection of the constants A and B.

The calibration equation having been determined for each wire, the tunnel flow rate was adjusted to the range of interest. At this


19a. Measurement of turbulence levels and length scales


19b. Measurement of spanwise distributions of flow quantities

Figure 19. Hot wire probe configurations
operating speed, the response of the two sensors to fluctuations in the mean velocity, $\frac{\partial E_{1}}{\partial U}$ and $\frac{\partial E_{2}}{\partial U}$, were calculated from their respective calibration equations. To match the turbulent response of the two wires, the correlator gain pot* in the channel two system was adjusted to provide a DC readout of

$$
K E_{2}=E_{2} \frac{\partial E_{1} / \partial U}{\partial E_{2} / \partial U}
$$

where $K$ is the actual gain setting.
With the response of the two wires thus matched, the AC signals, $e_{1}$ and $K e_{2}$ could be combined to eliminate ambient noise from the true turbulence signal. Each AC signal contains three primary components: that due to turbulence, $e_{T}$; that due to pressure fluctuations, $e_{p}$; and that due to the circuit noise, $e_{c}$.

$$
\begin{aligned}
& e_{1}=e_{T_{1}}+e_{P_{1}}+e_{c_{1}} \\
& K e_{2}=e_{T_{2}}+e_{P_{2}}+e_{c_{2}}
\end{aligned}
$$

The pressure noise of the two signals should be identical in time, that is

$$
e_{P_{1}}(t)=e_{P_{2}}(t)=e_{p}(t)
$$

Since separate electronic systems were used to monitor the wire outputs, $e_{c_{1}}$ and $e_{c_{2}}$ should be uncorrelated in time and if the wires are placed a sufficient distance apart there should also be no correlation between the turbulence signals, $e_{T_{1}}$ and $e_{T_{2}}$. Hence, taking the mean square of the sum and difference of the outputs

[^1]\[

$$
\begin{aligned}
& \overline{\left(e_{1}+K e_{2}\right)^{2}}=\overline{e_{T_{1}}^{2}}+\overline{e_{T_{2}}^{2}}+\overline{4 e_{P}^{2}}+\overline{e_{c_{1}}^{2}}+\overline{e_{c_{2}}^{2}} \\
& \overline{\left(e_{1}-K e_{2}\right)^{2}}=\overline{e_{T_{1}}^{2}}+\overline{e_{T_{2}}^{2}}+\overline{e_{c_{1}}^{2}}+\overline{e_{c_{2}}^{2}}
\end{aligned}
$$
\]

If the turbulent field is uniform, the mean square turbulence quantities should be equal, i.e.

$$
\overline{e_{T_{1}}^{2}}=\overline{e_{T_{2}}^{2}}=\overline{e_{T}^{2}}
$$

Then, the signals of interest are

$$
\overline{e_{T}^{2}}=\frac{\overline{\left(e_{1}-K e_{2}\right)^{2}}}{2}-\frac{\left(\overline{e_{c_{1}}^{2}}+\overline{e_{c_{2}^{2}}^{2}}\right)}{2}
$$

and

$$
\overline{e_{p}^{2}}=\frac{\overline{\left(e_{1}+K e_{2}\right)^{2}}}{4}-\frac{\left(\overline{e_{c_{1}}^{2}}+\overline{e_{c_{2}^{2}}^{2}}\right)}{4}-\overline{e_{T}^{2}}
$$

The electrical noise levels were determined by turning off the tunnel and measuring the two $A C$ outputs. The true turbulence level and the apparent turbulence due to pressure noise can then be calculated using the predetermined sensitivity, $\frac{\partial U}{\partial E_{1}}$,

$$
\begin{gathered}
T u=\sqrt{\overline{e_{T}^{2}}} \frac{\partial U}{\partial E_{1}} \\
T_{p}=\sqrt{\overline{e_{p}^{2}}} \frac{\partial U}{\partial E_{1}}
\end{gathered}
$$

The reported integral length scales were determined by fitting an experimentally measured spectral distribution to the theoretical spectral distribution given by Taylor [38],

$$
\frac{U E(n)}{u^{\prime 2} L}=\frac{4}{1+4 \pi^{2}\left(\frac{n L}{U}\right)^{2}}
$$

where $L$ is the integral length scale, $n$ is the turbulence frequency in Hz and the function $E(n)$ represents the frequency distribution of the turbulent velocity $u$. The relationship is typically plotted on $\log -\log$ axes in the form shown in Fig. 20. The measured spectra were also plotted on log-log axes in the form

$$
\frac{U E(n)}{u^{\prime 2} D}=\operatorname{fnc}\left(\frac{n D}{U}\right)
$$

The integral scale could then be determined by overlaying the theoretical curve onto the data plot and shifting the curve to a best fit position. The value of $L / D$ was obtained from the amount of relative shift in the horizontal direction.

To obtain the frequency spectra, it was necessary to compensate the directly measured spectral distributions for the frequency response characteristics of the hot wire used. As discussed by Bradshaw [37], a hot-wire sensor behaves like a low pass filter and has a frequency response of the form

$$
\frac{1}{1+n^{2} \tau^{2}}
$$

where $\tau$ is a time constant which depends on the physical charactersitics of the sensor. The time constant for the tungsten sensors used in the experiments was determined by a comparison of the slope of the approxmately linear high frequency ranges of the directly measured spectra with the slope of the high frequency range of the theoretical curve. The values for $M$ determined in this manner varied by only $8 \%$, and were averaged to provide a value for 1 of $5.6\left(10^{-4}\right)$ sec. This compares well with the value of $6\left(10^{-4}\right)$ sec suggested by Bradshaw for a typical tungsten wire in air flow. In addition to the measurements of turbulence levels and scales,


Figure 20. Theoretical energy spectrum of turbulence (due to Taylor)
the investigation into the observed spanwise variations in mass transfer required the determination of the spanwise distribution of various flow quantities. A boundary layer cross wire probe, TSI 1243, was used with its sensors positioned in the stagnation plane and oriented at $\pm 45^{\circ}$ to the flow. The configuration is depicted in Fig. 19b. Distributions of the mean velocity, $U$, the mean square of the mainstream turbulence component, $u^{\prime \cdot}$, the mean square of the spanwise turbulence component, $\overline{w^{\prime 2}}$, and the mean shear stress $\overline{u^{\prime} w^{\top}}$ were measured. As suggested by Nagib [39], the spanwise distributions of the quantities were obtained by slowly traversing the flow and recording the appropriate outputs on a strip chart recorder. Using an automatic traverse device mounted to the top wall of the tunnel, the portion of the span ahead of the naphthalene insert was traversed at a speed of approximately $\frac{1}{2} \mathrm{~mm} / \mathrm{sec}$. Distributions were measured at a number of streamwise positions on the stagnation plane of the test cylinder both with and without the cylinder installed. The high frequency oscillations on the strip chart output were visually averaged to provide the reported distributions.

Since both sensors and hence both anemometer channels were required to determine the turbulence quantities of interest, the direct elimination of spurious noise was not possible. To eliminate low frequency noise from the measurements, the signals were passed through a 50 Hz high-pass filter provided in the signal conditioner units.

Methods for the determination of the turbulence quantities of interest can be obtained from an examination of the response of a sensor. skewed at an angle, $\phi_{o}$, to the flow. If an idealized noise-free system is considered, the AC output of the sensor is

$$
\begin{aligned}
e & =\left.\frac{\partial E}{\partial U}\right|_{U_{0}, \phi_{0}} u^{\prime}+\left.\frac{\partial E}{\partial \phi}\right|_{U_{0}, \phi_{0}} d \phi \\
& =\left.\frac{\partial E}{\partial U}\right|_{U_{0}, \phi_{0}} u^{\prime}+\left.\frac{1}{U_{0}} \frac{\partial E}{\partial \phi}\right|_{U_{0}, \phi_{0}} w^{\prime} \\
& =s_{1} u^{\prime}+s_{2} w^{\prime}
\end{aligned}
$$

where $s_{1}$ and $s_{2}$ denote the sensitivity of the output to the components $u$ and $w$, respectively.

Consider now the case of two sensors with identical response characteristics positioned at $\phi= \pm 45^{\circ}$. The AC signals from the corresponding anemometers will be

$$
\begin{aligned}
& e_{+45}=s_{1} u^{\prime}+s_{2} w^{\prime} \\
& e_{-45}=s_{1} u^{\prime}-s_{2} w^{\prime}
\end{aligned}
$$

The mainstream turbulence component, $u^{\prime}$, can be determined by addition of the signals

$$
u^{\prime}=\frac{e_{45}+e_{-45}}{2 s_{1}}
$$

and the cross stream component by subtraction of the signals

$$
w^{\prime}=\frac{e_{45}-e_{-45}}{2 s_{2}}
$$

The time averaged shear stress component is obtained from the difference of the mean squares of the outputs

$$
\overline{u^{\prime} w^{\prime}}=\frac{\overline{e^{2}}-\overline{e_{-45}^{2}}}{4 s_{1} s_{2}}
$$

The two sensitivities, $s_{1}$ and $s_{2}$, of a particular element can be determined by a calibration procedure. For a wire normal to the flow the response curve may be correlated in the manner described above. As the wire is turned away from a perpendicular position, the rate of cooling and hence the output voltage decreases. This may be considered in the correlation equation as a change in the effective velocity, i.e.

$$
E^{2}=\frac{U_{e f f}^{.45}-B}{A F(T)}
$$

where

$$
U_{\mathrm{eff}}=\mathrm{Uf}(\phi)
$$

Then the sensitivity to a cross stream turbulence component is

$$
s_{2}=\frac{1}{U} \frac{\partial E}{\partial U} \frac{\partial f}{\partial \phi}
$$

or by rearrangement

$$
s_{2}=\frac{\partial E}{\partial U} \frac{1}{f(\phi)} \frac{\partial f}{\partial \phi}
$$

The sensitivity to a mainstream turbulence component is

$$
s_{1}=\frac{\partial E}{\partial U}
$$

As discussed in Hinze [40], the functional dependence of the output on angle in a range near $45^{\circ}$ is well represented by

$$
f(\phi)=\sin \phi
$$

Using the relationship the sensitivites for $\phi=45^{\circ}$ are

$$
s_{1}=s_{2}=\frac{\partial E}{\partial U}
$$

Returning to the correlation equation, the effect of angle may be included in the constants $A$ and $B$, i.e.

$$
E^{2}=\frac{U^{.45}-B_{1}}{A_{1} F(T)}
$$

to provide an equation for the output voltage of the skewed wire which depends only upon the incident velocity. The correlation constants $A_{1}$ and $B_{1}$ for each of the cross wire sensors were determined directly from a calibration of the probe in its measurement configuration, i.e. with the sensors at $\phi= \pm 45^{\circ}$. In the manner previously described, the sensitivities of the individual wires were matched using the gain pot in the channel two system.

Since the variations in the local mean velocity were small, on the order of $\pm 0.2 \%$, a special technique was also instituted for their measurement. Using the signal conditioners, the DC output from one of the two anemometers and its corresponding cross wire element was biased to eliminate the bulk signal and then amplified. The output was then plotted on the strip chart recorder. The variations in the mean velocity were then discernible along with high frequency turbulent fluctuations.

## PART 5

RESULTS

### 5.1 Flow Measurements

A free-stream velocity distribution about the cylinder was obtained from the surface static pressure measurements using Bernoulli's equation. This distribution is shown in Fig. 21 where the local freestream velocity divided by the mean incident velocity is plotted against the angle around the cylinder in radians measured from stagnation. The results are shown only for one side since the static pressure measurements were symmetric about stagnation. The velocity distribution for an unbounded potential flow around an infinitely long circular cylinder is also shown in the figure. A comparison indicates that the acceleration of fluid around the cylinder's surface is slightly less than that for potential flow. This is caused by the blockage effect of the wake. Using a fifth-order polynomial, the best fit to the actual velocity distribution is given by

$$
\frac{U_{\phi}}{U_{\infty}}=1.915 \phi-0.320 \phi^{3}-0.526 \phi^{5} \quad(\phi<1.2)
$$

where $\phi$ is the angular position measured in radians.
The velocity distribution along the stagnation plane is shown in Fig. 22, where the local velocity is nondimensionalized by that far upstream and $x / R$ denotes the upstream distance measured from the axis of the test cylinder. This velocity distribution is, to within the limits of experimental error, identical to that predicted by potential flow theory. Hot-wire anemometer measurements taken in the spanwise direction indicate


Figure 21. Velocity distribution around test cylinder

Figure 22. Velocity distribution along the stagnation plane
that the incoming flow without turbulence generating screens is uniform to within $\pm 0.2 \%$.

The turbulence level and pressure noise of the tunnel flow in the absence of a turbulence generating screen are plotted in Fig. 23 as a function of the flow velocity. Although the cylinder was removed from the tunnel for the measurements, the flow velocity is given in the form of a Reynolds number based on the cylinder's diameter to establish a fraine of reference. The turbulence level varies slightly with the flowrate, reaching a maximum at a Reynolds number of about 88,000 . The pressure noise is seen to change drastically with flowrate and reaches magnitudes larger than the true turbulence level. The variations of both quantities is felt to be caused by the flowrate control of the tunnel, which consists of a set of variable angle inlet control vanes.

The physical characteristics of the turbulence generating screens used in the mass transfer tests are presented in Table 1. The turbulence levels behind the generating screens were measured at a Reynolds number (again based on the cylinder's diameter) of 110,000 , a midrange value of the Re's used in the mass transfer tests. Turbulence levels and scales were measured for all available positions of each screen. The results are presented in Table 2.

In Fig. 24, the growth in the integral scale of turbulence behind each of the three turbulence section screens is plotted as a function of the downstream distance based on the mesh size M. A linear relationship of the form

$$
\frac{L}{M}=a+b \frac{X}{M}
$$



Figure 23. Ambient turbulence and noise levels without generating screens

Table 1. Physical characteristics of turbulence generating screens

Screens used in generating section

|  | M | D | $M / D$ | type |
| :---: | :---: | :---: | :---: | :---: |
| 1 | .875" | .188" | 4.65 | hand manufactured round bar biplane mesh |
| 2 | .621" | .127" | 4.89 | hand manufactured round bar biplane mesh |
| 3 | .125" | .028" | 4.46 | woven wire screen |
| 4 | $\begin{aligned} & .063^{\prime \prime}(z \operatorname{dir} .) \\ & .056^{\prime \prime}(y \operatorname{dir} .) \end{aligned}$ | $\begin{aligned} & .012 " \prime \prime \\ & .012 " \end{aligned}$ | $\begin{aligned} & 5.25 \\ & 4.67 \end{aligned}$ | woven wire screen |
|  |  |  |  |  |
| Plenum chamber screen - installation configuration illustrated in Fig. 6b |  |  |  |  |
| 5 | 10.0" | 2.0 " | 5.00 | biplane mesh constructed with flat boards |

Table 2. Turbulence levels and length scales
M =.125"

## Position

(X/M)

L/D
L/M
$T u(\%)$

$\mathrm{M}=.621^{\prime \prime}$

| 29.0 | .018 | .177 | 1.869 |
| :--- | :--- | :--- | :--- |
| 53.9 | .022 | .209 | 1.361 |
| 90.2 | .033 | .338 | 1.086 |

$\mathrm{I} / \mathrm{M}=.0857+.00270(\mathrm{X} / \mathrm{M})$
$\left(\bar{U}^{2} / \overline{u^{2}}\right)=91.26[(\mathrm{X} / \mathrm{M})+3.44]$
M =.875"

| 20.6 | .030 | .206 | 2.651 |
| :--- | :--- | :--- | :--- |
| 38.3 | .038 | .263 | 1.801 |
| 64.0 | .050 | .343 | 1.182 |

$\mathrm{L} / \mathrm{M}=.1415+.00315(\mathrm{X} / \mathrm{M})$

$$
\left(\bar{U}^{2} / \overline{u^{\prime 2}}\right)=134.0[(X / M)-11.96]
$$

Plenum chamber screen

$$
\mathrm{M}=10^{\prime \prime}, \mathrm{L} / \mathrm{D}=.188, \mathrm{Tu}=4.9 \%
$$

Ambient conditions without screens
$\mathrm{L} / \mathrm{D}=.087$, $\mathrm{Tu}=.39 \%$ - . $68 \%$ as shown in Fig. 23
M =.0625" - results discussed in Section 5.4


Figure 24. Growth of length scale behind generating screens


Figure 25. Decay of turbulence behind generating screens
was fit to each set of data. The determined values of the constants $a, b$ for each screen are presented in Table 2. The values are comparable with those obtained by Dryden et al. [41] in an extensive investigation of the turbulence field behind screens.

The decay in turbulence level behind each of three turbulence section screens is presented in Fig. 25. The data for each screen was curve fit to the relationship

$$
\frac{U^{2}}{u^{2}}=A\left(\frac{X}{M}+\frac{X_{0}}{M}\right)
$$

by adjustment of the constants $A$ and $X_{o}$. The determined values of constants are also given in Table 2.

### 5.2 Mass Transfer Measurements - Stationary Cylinder <br> To establish a base of comparison for the investigation into

 the effect of oscillation of the test cylinder on the local mass transfer rate, a set of mass transfer experiments were performed on a stationary cylinder using a variety of incident Reynolds numbers and turbulence conditions. In this phase of the investigation, a number of the turbulence conditions available in the wind tunnel were found to produce strong spanwise varlations in the mass transfer rate. These results are presented and discussed later. The nominally two-dimensional mass transfer results reported in this section are compared to the measurements of other Investigators to demonstrate the accuracy of the developed measurement techniques.The first series of steady-state tests were performed in the absence of a turbulence generating screen. Circumferential distributions


Figure 27. Mass transfer distribution ( $\operatorname{Re}=82,500$ )





Figure 31. Comparison of leading edge results with previous measurements


Figure 32. Comparison of leading edge results ( $\operatorname{Re}=110,000$ ) with theory
of the local mass transfer rate at two spanwise positions were measured for incident Reynolds numbers of $75,000,82,500,110,000$ and 125,000 . The results are presented in Figs. 26 through 29. The distributions are compared in Fig. 30, where only a best curve fit to each sef of data is shown for clarity. In the leading edge region up to separation, the results scaled by $\sqrt{\operatorname{Re}}$ are idenifical to within the $\div 2 \%$ measurement repeatability. After separation the values of $\mathrm{Sh} / \sqrt{\operatorname{Re}}$ increase slightly with Reynolds number.

In Fig. 31 the results in the leading edge region for $\mathrm{Re}=110 \mathrm{~K}$ are compared with the mass transfer results obtained by. Sogin and Subramanian [31] and Kestin and Wood [14] for similar incident flow conditions. Near the stagnation point, a good agreement is seen. In the separation region, the current data deviates slightly from the other results and indicates that flow separation occurs further downstream. This is an effect of the high blockage ratio (cylinder diameter / tunnel width) of .2 used in the present investigation, Kestin and Wood used a blockage ratio of . 12 and Sogin and Subramanian used a ratio of . 13 .

The low turbulence level data can also be compared with a theoretical laminar result obtained by a series solution to the boundary layer equations similar to Froessling's [1] but using a Schmidt number of 2.5 The calculation procedure developed by Childs [30] was used in combination with the experimentally determined distribution of the free stream velocity around the test, cylinder, $U_{\phi}$. The theory predicts a distribution of the local mass transfer rate given by

$$
\frac{S h}{\sqrt{\operatorname{Re}}}=1: 612-0.253 \phi^{2}-.00216 \phi^{4}
$$

where $\phi$ is measured in radians. This theoretical result is plotted along with the experimental results for $\operatorname{Re}=110,000$ in Fig. 32. The slight discrepancy between the theory and the data is presently attributed to inaccuracies in the Schmidt number and vapor density relation. If the error is assumed to be caused only by the uncertainty in the Schmidt number, a value of 2.55 is required to make the theory and experiment correspond. This is within the error of experimentally and theoretically determined values.

Since the mass transfer surface occupies only $3^{\prime \prime}$ of the 18 " span of the test cylinder, it would be expected that some spanwise transport of mass occurs. To ascertain the degree to which the results were affected by the experimental configuration, an additional low turbulence level experiment was performed in which the entire test cylinder was coated with naphthalene. A Reynolds number of 110,000 was used. The transfer rate on the insert was measured in the spanwise direction on the front and rear stagnation lines and near separation. The results are shown in Fig. 33 along with results obtained without full body naphthalene coating. The results on the front stagnation line and near separation are seen to be unchanged. The results along the rear stagnation line are about $8 \%$ lower than the previous measurements. This would be expected due to the large scale transport by the turbulent eddies found in the wake. This effect is of little importance to the current research which is primarily concerned with transfer rates in the leading edge region. Also, the data measured along the rear portions of the cylinder is probably of little use for comparison with other investigations since one would expect the transfer rate there to be a strong function of the blockage ratio.


The results of the steady-state experiments performed behind turbulence generating grids are presented in Figs. 34 through 38. To demonstrate the effect of turbulence on the distribution of the local mass transfer rate, the results of the tests performed at $\mathbf{R e}=110,000$ are compared in Fig, 39. For clarity, a best curve fit to each data set is shown, From this figure the well-known effects of turbulence are readily evident. In the stagnation region, the mass transfer rate increases substantially as the incident turbulence level is increased, with augmentations as high as $30 \%$ being demonstrated by the current results. Further, the incident turbulence significantly alters the character of the flow near and after separation. For low turbulence levels, the transfer rate distributions along one side of the cylinder have a single minimum which occurs near the separation of the laminar boundary layer. At higher incident turbulence levels, the transfer rate distributions exhibit two minimum points, indicating that transition from a laminar to a turbulent boundary layer occurs before separation. After transition there is a rapid increase in the local transfer rate. In the present results, values for $\mathrm{Sh} / \sqrt{\mathrm{Re}}$ as high as 3.5 were observed in the region between transition and separation. It, should also be noted that the results observed at large turbulence levels are characteristic of low turbulence results measured at higher incident Reynolds numbers, and hence in simplistic terms, increases in the incident turbulence level can be viewed as a change in the effective Reynolds number of the flow.

In Fig. 40, the steady-state results at stagnation are plotted as a function of $\mathrm{Tu} \sqrt{\mathrm{Re}}$. For comparison with the heat transfer measurements



Figure 35. Mass transfer distribution ( $\operatorname{Re}=110000, \mathrm{Tu}=1.18 \%, \mathrm{~L} / \mathrm{D}=.050$ )


Figure 36. Mass transfer distribution
( $\mathrm{Re}=110000, \mathrm{Tu}=1.80 \%, \mathrm{~L} / \mathrm{D}=.038$ )

$\begin{array}{ll}\text { Figure 37. } & \text { Mass transfer distribution } \\ & (\operatorname{Re}=75000, \mathrm{Tu}=2.65 \%, I / D=.030)\end{array}$


Figure 38. Mass transfer distribution

$$
\left(\operatorname{Re}^{\prime}=710000, \mathrm{Tu}=2.65 \%, \mathrm{~L} / D=.030\right)
$$



Figure 39. Comparison of elevated turbulence level results ( $\mathrm{Re}=110000$ )

Figure 40. Comparison of stagnation point results with the
of other investigators, equivalent Nusselt numbers have been calculated from the mass transfer results through the use of the heat-mass transfer analogy. Due to the wide discrepancies in the methods used to report and measure turbulence levels, this figure should be viewed only as an indication of general trends, and not as a basis for the establisfment of precise empirical correlations. The figure does, however, demonstrate that the current results are well within the band of scatter of the data from other investigations, although they appear to be somewhat low at low turbulence levels. This may be due to inaccuracies in the Schmidt number and vapor density relation, or it may be due to the difficulties presented by the rather high levels of ambient noise in the tunnel, which made the measurement of low turbulence levels more prone to error.

### 5.3 Mass Transfer Measurements - Oscillating Cylinder

In the oscillation study, each of the flow situations which produced nominaily two-dimensional mass transfer results were repeated. Circumferential distributions of the time averaged local mass transfer rate were measured. For each case, the effects of oscillation on the transfer rate are evaluated by comparing the unsteady results to a "quasisteady" curve calculated from the steady-state results obtained with an identical flow. Physically, the quasisteady distributions represent the results which would be obtained from a cylinder oscillating at an infinitely small frequency. In this situation the surface velocity of the cylinder is negligible and the effect of oscillation is a simple averaging of the transfer rates seen by a particular point at particular times, i.e.

$$
\operatorname{Sh}_{\text {quasisteady }}(\phi)=\frac{1}{2 \pi} \int_{-\pi}^{\pi} \operatorname{Sh}_{\text {steady }}\left(\phi+\phi_{0} \sin \omega\right) \mathrm{d} \omega
$$

The quasisteady curves thus establish the "no effect" level for the oscillation tests. It should be noted that since the oscillation amplitudes used in the experiments are small, the quasisteady curve is essentially identical to the steady-state distribution in the stagnation zone and that it varies substantially only for the region around separation.

A summary of the oscillation tests performed is given in Table 3. Only two oi the incident turbulence condfions used provided results which demonstrated a measurable effect of oscillation. The results for the other cases lie essentially, to within the limits of experimental error, on the quasisteady curves. The only substantial deviations from these curves are in the regions around separation. This effect was observed in all of the oscillation tests performed. The results which did demonstrate an effect of oscillation are presented and discussed below. To insure that the results of the investigation were reproducible, most of the tests described were repeated; in some cases many times. For brevity, only one representative set of data is presented for each case discussed. The full set of experimental data is aṿailable in Appendix A.

All of the results which show an effect of oscillation were obtained from tests performed downstream of the $7 / 8^{\prime \prime}$ mesh turbulence generating grid. Tests were performed for all three available positions of the $g r i d, x / R=6.0,11.2$, and 18.7 where $x$ is the distance upstream from the cylinder's axis, at a Reynolds number of 110,000 , an oscillation amplitude of $6^{\circ}$, and a Strouhal number of 0.0639 . The latter corresponds to the maximum available operating frequency. The results obtained with the grid installed at $x / R=18.7$, which corresponds to $T u=1.182$ and $\frac{L}{D}=.050$ showed no effect of oscillation. The results for $x / R=11.2$,
$\mathrm{Re}=110000$
$\mathrm{St}=.0071$
$S t=.0213$

Fig. 48 Fig. $5^{2}$ $\operatorname{Re}=\frac{S t=.1041}{50000}$
which corresponds to $T u=1.801 \%$ and $\frac{L}{D}=.038$, are shown in Fig. 41. In this case a small effect of oscillation is discernible. The mass transfer rate at leading edge is about $3 \%$ higher than that suggested by the quasisteady curve. It is important to note, however, that this increase is barely above the $2 \%$ limit of experimental repeatability. The mass transfer measurements for the closest installation position of the grid, $x / R=6.0$, are given in Fig. 42. In this case the measured incident turbulence level and integral length scale were $2.65 \%$ and .03 D , respectively. The mass transfer rate at stagnation is, for this position of the grid, about $10 \%$ above the quasisteady transfer rate. Since this was the largest observed effect of oscillation, the turbulence field generated by this position of the $7 / 8^{\prime \prime}$ mesh grid was used for the remainder of the investigation.

In the next series of mass transfer experiments, the effect of Strouhal number was examined. Maintaining an oscillation amplitude of $\phi_{0}=6^{\circ}$ and a Reynolds number of 110,000 ; tests were performed for Strouhal' numbers ranging from 0.007 to 0.0781 . The results are presented in Figs. 43 through 48. Each case exhibited a small effect of oscillation, with łncreases in the mass transfer, rate ranging from $3 \%$ to $10 \%$, however, perhaps the most remarkable aspect of the results is the fact that an effect was observed even in the lowest frequency case, St $=0.0071$.

The effects of oscillations at Strouhal numbers higher than 0.0781 were also examined. Since the actual maximum oscillation frequency was constrained by the physical limitations of the oscillation mechanism, the Strouhal number, $\frac{f D}{U}$, was increased by lowering the flow velocity. It should be noted that this has the unfortunate consequence of lowering the


Figure 41. Mass transfer distribution with oscillation ( $\mathrm{Re}=110000, \mathrm{Tu}=1.80 \%, \mathrm{~L} / \mathrm{D}=.038, \mathrm{St}=.0639$ )


Figure 42. Mass transfer distribution with oscillation ( $\operatorname{Re}=110000, \mathrm{Tu}=2.65 \%, \mathrm{~L} / \mathrm{D}=.030, \mathrm{St}=.0639$ )


Figure 43. Mass transfer distribution with oscillation ( $\operatorname{Re}=110000, T u=2.65 \%, I / D=.030, S t=.0071$ )


Figure 44. Mass transfer distribution with oscillation
(Re $=110000, T u=2.65 \%, I / D=.030, \mathrm{St}=.0213$ )


Figure 45. Mass transfer distribution with oscillation ( $\mathrm{Re}=110000, \mathrm{Tu}=2.65 \%, \mathrm{~L} / \mathrm{D}=.030, \mathrm{St}=.0355$ )


Figure 46. Mass transfer distribution with oscillation ( $\operatorname{Re}=110000, T u=2.65 \%, L / D=.030, S t=.0497)$


Figure 47. Mass transfer distribution with oscillation (Re $=110000, \mathrm{Tu}=2.65 \%, \mathrm{~L} / \mathrm{D}=.030, \mathrm{St}=.0639$ )


Figure 48. Mass transfer distribution with oscillation ( $\mathrm{Re}=110000, \mathrm{Tu}=2.65 \%, \mathrm{~L} / \mathrm{D}=.030, \mathrm{St}=.0781$ )
effects of the incident turbulence level since the transfer rate depends in some manner on Tu $\sqrt{\text { Re. }}$. The results of these tests performed at Reynolds numbers of 75,000 and 50,000 are given in Figs. 49, 50 and 51 . In the $\operatorname{Re}=50,000$ case the results of the measurements at the two spanwise positions differed by approximately $7 \%$. This difference was observed in both the steady and the oscillation tests; however, when the oscillation data at each position is scaled to the quasisteady curve obtained for that position, the effect measured by the two gauges is essentially identical. The spanwise discrepancy in these tests was generated by skew in the incident velocity caused by operation of the tunnel in an off-design mode.

As a final oscillation test, the effect of changing the oscillation amplitude was investigated. Unfortunately, the vibration forces generated by the oscillation increase drastically with amplitude, severely limiting the maximum available frequency. A mass transfer test was performed for the intensively studied case of $T u=2.65 \%, \frac{L}{D}=.03$, at a Reynolds number of 110,000 . An oscillation amplitude of $\phi=12^{\circ}$ and a Strouhal number $=.0213$ were used. The results are presented in Fig. 52. The observed augmentation at stagnation is about $5 \%$ and is approximately equal to that measured at the previous oscillation amplitude.

The results of the unsteady tests performed for an incident turbulence level of $2.65 \%$ and an integral length scale of . O3D are correlated in Fig. 53. The augmentation ratio, that is the unsteady mass transfer rate divided by the quasisteady mass transfer rate for similar flow conditions, is plotted as a function of Strouhal number at the stagnation point. The augmentation is seen to initially increase with Strouhal number reaching a maximum value of 1.1 at $\mathrm{St} \approx .06$.


Figure 49. Mass transfer distribution with oscillation ( $\mathrm{Re}=75000, \mathrm{Tu}=2.65 \%, \mathrm{I} / \mathrm{D}=.030, \mathrm{St}=.0417$ )


Figure 50. Mass transfer distribution with oscillation ( $\operatorname{Re}=75000, T u=2.65 \%, L / D=.030, S t=.1041$ )



Figure 52. Results obtained with increased amplitude of oscillation ( $\mathrm{Re}=110000$, $\mathrm{Tu}=2.65 \%$, $L / D=.030, S t=.0639, \varnothing_{0}=12$ )


Figure 53. Correlation of oscillation results ( $\mathrm{Re}=110000, \mathrm{Tu}=2.65 \%, \mathrm{~L} / \mathrm{D}=.030$ )

For larger Strouhal numbers, the data suggests that the augmentation ratio decreases asymptotically back to 1.0 , the no-effect level. It must, however, be noted that the data in this range was obtained at lower Reynolds numbers and that the effects of turbulence are hence decreased. Also of interest is the fact that the result obtained with the increased oscillation amplitude falls along the curve suggested by the other data.

### 5.4 Investigation into Spanwise Variations in Mass Transfer

As a portion of the unsteady investigation, a series of steadystate mass transfer experiments were performed under a variety of turbulence conditions. To establish the degree of two dimensionality of the results, measurements were taken in the spanwise direction at a number of circumferential positions on the test cylinder. The results of these experiments have been condensed in Figs. 54 through 60 , where particular traverses have been selected from the full data set given in Appendix D. The results indicate that for certain turbulence conditions, which are associated with various combinations of generating screens and positions, the local mass transfer rate varied substantially across the span, while for other cases the mass transfer rate was nominally constant in the spanwise direction. In particular, the results presented in Figs. 57, 58, 59 and 60 are definitely three dimensional in nature. The measurements taken behind the 16 -mesh screen are the most remarkable of these cases, exhibiting a regular wavelike behavior with a wavelength of about . 15R. China clay flow visualizations performed across the full span of the test body indicated that the spanwise variations in the other cases were also somewhat periodic; however, the wavelengths for these cases were too large





to be visible on the $3^{\prime \prime}$-mass transfer surface.

For further comparison of these mass transfer results, the spanwise averaged transfer rates at the stagnation line are plotted as a function of $\mathrm{Tu} \sqrt{\operatorname{Re}}$ in Fig. 61. As seen by this figure, the results for the cases which exhibited substantial spaņise variations are on the order of $20 \%$ higher than the general trend indicated by the other results. This dramatic increase and the rather remarkable threedimensional behavior of the results obtained with a "nominally" uniform incident flow necessitated further investigation. Since the results measured behind the 16 -mesh screen exhibited the most regular behavior, this screen was used in the study.

To begin the investigation, the effect of altering the position of the 16 -mesh screen was examined. First, the streamwise position of the screen was changed from $\frac{x}{R}=6.0$, to $\frac{x}{R}=11.2$; where $x$ is the distance upstream of the cylinder's axis, with care taken to preserve the orientation and vertical position of the screen with respect to the test cylinder. The spanwise distributions of the mass transfer rate at the leading edge are compared for the two screen positions in Fig. 62. The general curve shapes obtained from the tests are seen to be similar in nature, with the peaks of the distributions occurring at about the same spanwise positions. From this result it is evident that the vertical position of the waves is either fixed with respect to the tunnel or fixed with respect to the screen.

To ascertain the importance of the generating screen, an additional experiment was performed with the screen at $x / R=6.0$, but shifted vertically upward $\frac{1}{4}$ ", approximately half of the observed wavelength. The spanwise variation in the mass transfer rate was observed to in turn


Figure 61. Comparison of average results obtained at stagnation point with and without spanwise variations
$\frac{5 h^{2}}{}{ }^{2.0}{ }^{2}$
Figure 62. Spanwise mass transfer distributions at two positions
shift upward the same distance, remaining in all other respects identical to the previous measurements. A comparison of the results at the leading edge for the two tests performed with the screen in a position $x / R=2.5$ is given in Fig. 63, where the data is plotted as a function of position with respect to the screen

Since the phenomena being observed in the mass transfer tests exhibited a wavelength on the order of $15 \%$ of the span of the naphthalene test surface, it was also necessary to ascertain the degree to which the results were affected by the spanwise transport of mass. For this purpose, an experiment was performed with the test body fully coated with naphthalene. The results are shown in Fig. 64, where spanwise traverses taken along front stagnation line and near separation are presented. For comparison similar measurements obtained from a test without full body coating are also presented. (It should be noted that the shapes of the curves in these results differ from those previously presented. This was probably caused by physical abuse of the screen in the interval between the tests.). It is evident from the figure that only the two waves at the edges of the naphthalene strip are affected by the experimental configuration and that even in these regions the effect is small.

The mass transfer tests performed with various positions of the generating screen demonstrated that the spanwise variations in the local transfer rate were in some manner caused by the screen. Since it was known that the flow through the tunnel without generating screens was rather uniform and contained, no wavelike disturbances, a full study of the flow field behind the 16 -mesh turbulence generating screen was undertaken. Spanwise distributions of $\overline{u^{\prime 2}}, \overline{w^{\prime 2}}, \overline{u^{\prime} w^{\prime}}$ and $U$ were measured at


various locations upstream of the test cylinder in the stagnation plane, The profiles were measured both with and without the cylinder installed in the tunnel. For the purpose of comparison, the spanwise range corresponding to the location of the mass transfer surface was covered.

The results of the flow traverses with the cylinder removed from the tunnel are presented in Figs. 65 through 70. In Fig. 65, the spanwise distributions of the mean velocity at various distances downstream of the screen are presented. The velocity is shown as a percent variation about the spanwise averaged velocity, $\bar{U}$. The spanwise distance, $z$, is measured from a horizontal line which corresponds to the center of the mass transfer surface when the test cylinder is installed. The streamwise distance downstream of the screen, $X$, is given in mesh lengths. For later comparison, the spanwise distance is given in terms of the cylinder's radius, $R$; as is the distance upstream of the cylinder's axis position, $x$. Also shown in this figure is the spanwise variation of the screen's mesh size, M, the vertical distance between individual wires. This was measured with a set of machinist's wire gauges of various diameters. From these measurements a periodic pattern can be identified. As shown in Fig. 65, this pattern induces a small magnitude wavelike disturbance in the mean velocity which persists for large distances downstream of the screen.

The decay in the amplitude of the mean velocity variations is shown in Fig. 66, where the average spanwise value of the half peak-topeak amplitude is plotted as a function of distance downstream of the screen. According to Townsend [42], the amplitude of a periodic disturbance in mean velocity should decay as

Figure 65. Spanwise distributions of mean velocity without test cylinder

Figure 66. Streamwise distribution of the average perturbation

$$
\frac{\Delta U}{U} \alpha \exp \left[\frac{-V T}{\nu}\left(\frac{2 \pi M}{\lambda}\right)^{2}\left(\frac{\nu}{U M}\right) \frac{X}{M}\right]
$$

where $\lambda$ is the wavelength of the disturbance and $v_{T}$ is the eddy viscosity. For the present experiments $\frac{U M}{V}=1146$ and $\lambda / M=7.3$. This decay law 15 also shown in Fig. 66, where the constant of proportionality and a value of $U_{T} / v$ have been chosen to provide a best $f$ it to the data. The latter value was $V_{T} / V=2.94$, a surprisingly small ratio when compared to the values of about 150 quoted by Townsend for flow behind parallel rods. Kellog and Corsin [43], however, found a value of $\nu_{T} / V=3.5$ for a situation similar to that in the present experiments. Estimates of the eddy viscosity, $V_{T}$, made from the measured mean velocity and turbulent shear stress ( $\overline{u W)}$ also provided a ratio of $\nu_{T} / \nu$ between 2 and 3.

The spanwise variations of the turbulence quantities without the cylinder are shown in Figs. 67 through 69. The periodic behavior is obvious in all, particularly the $\overline{u^{\prime} w^{\top}}$ distribution, and all have the same wavelength. A careful comparison between Figs. 65 and 69 will show a $90^{\circ}$ phase shift between the $\overline{u^{\prime} w^{\prime}}$ and mean velocity distributions as one might expect. The streamwise decay of the turbulence quantities is provided in Fig. 70. Spanwise averaged values or the relative intensities, $\overline{u^{\prime 2}}$ and $\overline{w^{\prime 2}}$, are presented along with.the average peak amplitude of $\overline{u^{\prime} w^{\prime}}$, the spanwise average of which is virtually zero. The decay in the streamwise component of turbulence behind the screen could be fitted by the decay law

$$
\frac{\mathrm{U}^{2}}{\mathrm{u}^{\prime 2}} \alpha\left(\mathrm{X}+\mathrm{X}_{0}\right) / \mathrm{M}
$$

where a value of $X_{0}=113 M$ gave the best $f i t$. When the cylinder was

Figure 67. Spanwise distributions of $\overline{u^{\prime}}$ without test cylinder


Figure 68. $\begin{aligned} & \text { Spanwise distribution of } w^{2} \text { without test } \\ & \text { cylinder }\end{aligned}$


Figure 69. Spanwise distributions of $\overline{u^{\prime} w^{\prime}}$ without test cylinder
installed for measurements its leading edge position was $x / M=488$. Although this is a large distance in terms of mesh size, it is almost an order of magnitude smaller in terms of the wavelength of the screen's pattern, viz. $x / \lambda=69$. Interestingly, a comparison of the amplitude of the spanwise variation in the mean velocity to the turbulence level at this position, 0.2 and $0.5 \%$, respectively, shows that the mean velocity disturbance is "buried" in turbulence. In fact, in the initial profile measurements obtained without traversing continuously, the mean velocity was found to be "nominally" uniform. This has important implications with respect to stagnating flows as will be seen shortly.

The results of the incident flow traverses with the cylinder in place are shown in Figs. 71 through 76. The spanwise distributions of mean velocity are presented in Fig. 71. In this figure, the velocity is shown as a percent variation about the local mean velocity, which was found to vary in the manner predicted by potential flow. Comparing the distributions to those taken without the cylinder in place, Fig. 65, make the effect of the cylinder quite evident. At the position nearest the cylinder, a threefold increase in the relative amplitude is found, with correspondingly smaller increases further from the cylinder. The closest position, $x / R=1.28$, is about 35 boundary layer thicknesses away.

The result is more graphic in Fig. 72 where the amplitudes of the mean velocity variation with the cylinder in place are plotted. Here the coordinate system associated with the cylinder is used. According to Sadeh et al. [22] the amplitude of a periodic disturbance in the velocity incident to a circular cylinder should vary as

Figure 71. Spanwise distributions of mean velocity ahead of

Figure 72. Streamwise distribytion of the average perturbstion in mean velocity ahead of test cylinder

$$
\frac{U}{\bar{U}} \propto\left[\frac{x^{2}}{x^{2}-R^{2}}\right]^{2}\left(\frac{x-R}{x+R}\right)^{\frac{1}{2}\left(\frac{2 \pi}{\lambda}\right)^{2} \frac{V_{T} R}{U_{\infty}}} \exp \left[\left(\frac{2 \pi}{\lambda}\right)^{2} \frac{V_{T} x}{U_{\infty}}\right]
$$

This expression was evaluated using the values for $\nu_{T} / v$ and the constant of proportionality determined from the previous fit to the Townsend decay law, since for large $x / R$ the relationship decays into the Townsend curve, and is plotted in the figure. Neither changing the kinematic viscosity nor the constant of proportionality provided a good fit over the entire range, indicating that as the cylinder is approached the structure of turbulence changes and cannot be modeled using the concept of an eddy viscosity. If only the behavior near the cylinder is of interest, the expression can fit to the data - but so can the expression one obtains from Bernoulli's equation, viz. $\Delta \mathrm{U} \alpha 1 / \mathrm{U}$.

The spanwise distributions of the turbulence quantities ahead of the cylinder are presented in Figs. 73 through 75. The wavelike disturbances in these quantities are also seen to be amplified as the cylinder is approached. The streamwise variations are given in Fig. 76 where spanwise averaged values of $\overline{u^{\prime 2}}, \overline{w^{\prime 2}}$ and the average peak amplitude of $\overline{u^{\prime} w^{\prime}}$ are plotted. The increase in the relative turbulent intensities as the cylinder is approached is apparent. This behavior was also obtained by Sadeh, Sutera and Maeder [22] who showed that the intensities continue to increase up to the boundary layer substantially modifying the "free stream" flow conditions there.

To establish an accurate comparison between the mass transfer variations and the disturbances in the flow quantities, an additional mass transfer test was performed. The results of this test are shown in

[^2]
Figure 74. Spanwise distributions of $w^{12}$ ahead of test

Figure 75. Spanwise distributions of $\overline{u^{\prime} w^{\prime}}$ ahead of test cylinder


[^3]Fig. 77, where the spanwise distribution of the local mass transfer rate is given at a number of degree positions. It should be noted that the wave shapes of this test are substantially different than those measured behind the 16 -mesh screen in the initial phases of the investigation. This was felt to be due to disturbance of the screen's mesh pattern by various attempts to measure the mesh size distribution. As in the previous measurements a regular wavelike pattern was obtained. This periodic nature of the results is unmistakable even up to separation, which occurs at $\phi=79^{\circ}$. Perhaps the most surprising result of this investigation is, however, the disproportionately large magnitude of the mass transfer variations, which are on the order of $15 \%$ generated by a $0.2-0.4 \%$ variation in the incident mean velocity.

Correlation of the results is made in Fig. 78 where the spanwise distributions of the Sherwood number at the leading edge, the mean velocity variation at $x / R=1.28$, and the distribution of the mesh size have been assembled. Not only is it seen that the patterns are similar, but one finds that the position of a high mass transfer rate corresponds to that of a high mean velocity - while that for a low rate corresponds to that for a low velocity. This observation is in qualitative agreement with the vorticity amplification models presented by Sutera et al. [20, 21] where the spanwise variation in the total pressure of the incident flow causes a periodic vortical motion around the cylinder. Under these circumstances, fluid moves toward the surface of the cylinder in regions of high velocity, increasing the transfer rate there, and away from the surface in low velocity regions decreasing the transfer rate there.


Figure 78. Correlation of results

## 

Figure 79. Effect of 16 M screen on spanwise average mass transfer

The overall effect of the screen on the mass transfer rate is shown in Fig. 79, where the circumferential distributions in the Sherwood number with and without the screen are presented. That with the screen corresponds to spanwise averaged results, while that without is a best fit curve to the no-screen data presented elsewhere in this report. The effects of the screen are seen to increase the mass transfer rate over the whole leading edge surface. At stagnation the mass transfer rate is augmented by $17 \%$. At this time it is difficult to ascertain how much of this increase is due to the variations in mean velocity and how much is attributable to the effects of turbulence. By comparing the present results through the heat-mass transfer analogy to those obtained from heat transfer experiments, it appears that the division is about equal.

## PART 6

## CONCLUSIONS

### 6.1 Steady-State Experiments

a) The mass transfer technique developed as a part of the reported research effort was found to yield results which were repeatable to within $+2 \%$. Although precise values for the diffusion coefficient and vapor pressure relation are not currently available, those given by Sogin [33] were found to provide results which compared well with the heat and mass transfer measurements of previous investigators and with a theoretical calculation.
b) Before an accurate empirical correlation between the turbulence characteristics of the incident $f$ low and the stagnation region transfer rate can be established, a drastic improvement must be made in the methods used to measure and report turbulence. Current techniques for the measurement of turbulence levels and scales involve inherent uncertainties on the order of $\pm \mathbf{2 0 \%}$. Reported measurements typically lack information concerning the decay length of the turbulence and the signal conditioning used in the measurements. Also, there seems to be no-existing convention for reporting turbulence quantities, with definitions of the "incident" characteristics varying widely among experimental investigators. In some cases, the measurements are taken without the cylinder in place, using positions which correspond to either its leading edge or its axis, while in others the measurements are made ahead of the installed cylinder. A comparison of measured transfer rates is difficult under such circumstances. Future transfer rate measurements should be accompanied by
a complete description of the incident turbulent field. Values of the turbulence level and integral length scale at the leading edge position of the test body should be reported along with their respective rate of decay or growth.

### 6.2 Oscillation Experiments

a) For the range of significant parameters considered in the experiments, the effect of rotational oscillation of the test cylinder on the distribution of the local transfer rate over the leading edge region is small. The largest observed effect was a $10 \%$ augmentation of the transfer rate at stagnation. Since the range of parameters used was chosen to model an actual turbine situation, the results suggest that the heat load in the leading edge region of a turbine blade is not significantly affected by the variation in the angle of attack of the incident flow generated by airfoil wakes. The implication of the measurements is that, for the Strouhal number range of interest, the residence time during which a fluid particle passes over the surface is small with respect to the period of the unsteadiness in the incident flow. This would further suggest that not only are the effects of variation of the incident angle of the flow small, but also the effects of variation of the flow magnitude since the Strouhal number is identical. Hence, the uncertainty in leading edge heat load predictions due to the unsteady effects of airfoil is only on the order of $10 \%$. Increases as large as $40 \%$ can be atributed to turbulence in the incident flow. The remainder of the $70 \%$ uncertainty in the predictions may be atcributable to three-dimensional effects generated by small nonuniformities in the incident flow of the type observed in the current research.
b) The magnitude of the oscillation effects is intimately connected to the level and scale of the incident turbulence. For the range of St and $\operatorname{Re}$ used in the investigation and for turbulence scales on the order of $L / D \approx .02$, the effect seems to increase with turbulence level. For turbulence levels below $1.5 \%$ no effect was observed while increasing the turbulence level to $1.8 \%$ and $2.6 \%$ gave increases at stagnation of $3 \%$ and $7 \%$, respectively. However, a larger length scale of $L / D=.18$, gave no effect even though the turbulence level was higher, $T u=4.9 \%$, indicating the importance of the scale to the observed results. Interestingly, the length scale at which significant effects are evident is about eight boundary layer thicknesses and of the order of the value of $\mathrm{L} / \delta \approx 10$ which produces the maximum transfer rate for a steady flow according to Yardi and Sukhatme.
c) At the incident turbulence conditions which demonstrate a significant effect of oscillation, $T u=2.65 \%, L / D=.03$, the magnitude of the augmentation initially increases with Strouhal number reaching a maximurn at $S t \approx 0.056$ after which the effect decreases. This would suggest that some type of interaction between the turbulent eddies and the oscillation velocities occurs for a narrow range of the ratio of the characteristic incident turnover frequency of a turbulent eddy to the frequency of oscillation, i.e.

$$
\left(\frac{\mathrm{Tu} U_{\infty}}{\mathrm{L}_{\mathrm{T}}}\right) /\left(\frac{\mathrm{St} \mathrm{U}_{\infty}}{\mathrm{D}}\right)=\mathrm{R}_{\mathrm{T}}^{\prime}
$$

The maximum effect occurs at $R_{T} \approx 16$. This parameter is, however, significant only when the scale of turbulence is of the proper magnitude, $L / D=.03$.

Since the scale of a turbulent eddy changes as the stagnation point is approached, this may be the incident eddy size which generates eddies at stagnation of a scale on the order of the boundary layer thickness.

### 6.3 Investigation into the Observed Spanwise Variation of Mass Transfer

a) Small irregularities in a screen produced long-lived spanwise perturbations in the mean velocity which were "buried" in the turbulence generated by the screen itself. Although the amplitude of these perturbations could be correlated using Townsend's decay law, it implied that the apparent kinematic eddy viscosity was of the order of the molecular viscosity.
b) With the cylinder in place, the mean-velocity perturbations amplified as one approached stagnation. Within this region, about one diameter from the cylinder, the turbulence quantities were also amplified similar to that previously shown by Sadeh et al. [22], although to a much lesser extent than the perturbations in the mean velocity. Apparently, this is a result of a change in the turbulent structure and the added importance of the dissipation of turbulent energy.
c) The most surprising result perhaps is the disproportionately larger spanwise variation in the mass transfer caused by the mean-velocity perturbations. Here an initial 0.2 to $0.4 \%$ perturbation was responsible. for a 15\% variation.
d) Finally, the screen produced a spanwise averaged mass transfer rate which was $17 \%$ greater than that obtained at the base turbulence level of the tunnel.

In the present case it appears that the increase in mass transfer found with the screen is caused by two mechanisms. The first is amplification
of the spanwise mean-velocity perturbations (incident flow vorticity) in the stagnation region by the divergent flow there. This produced a large scale, spanwise periodic vortical motion around the cylinder's leading edge having the same wavelength as that in the incident flow. Where the fluid moved toward the surface the mass transfer increased, and where it moved away the mass transfer decreased, producing a spanwise regular pattern of mass transfer around the leading edge. As a note, no such pattern was found after separation. Interestingly, the wavelength imposed by the screen just happened to be about twenty boundary layer thicknesses, i.e., $\lambda / \delta \approx 20$, which gives a single vortex cell size equal to the turbulence length scale that produces the greatest heat transfer rate according to Yardi and Sukhatme. Also, since the vortex scale is large compared to the boundary layer thickness, this mechanism is mainly an inviscid one.

The second mechanism involved in the increase of mass transfer is the amplification of the incident turbulence in the stagnation region, again by the divergent flow. However, in this case it appears that the scale is smaller than that associated with the vortex motion and that it is random in nature. As such, it can be considered to be convected by the vortex motion, further increasing the mass transfer from the surface, in addition to being produced, diffused and dissipated.

Presently, it is difficult to say how much of the increase is caused by each mechanism and, indeed, it now appears difficult to say exactly how much of the previously published data was affected in the same way.

PART 7

## LITERATURE CITED

[1] Frössling, N., "Verdunstung, Wärmeiibertragung und Geschwindigkeitsvertilung bei Zweidimensionaler und Rotationssymmetrisher Grenzchichtströmung," Acta Univ. Jund 2(4), 36(1940) (see also NACA TM1432).
[2] Merk, H. J., "Rapid Calculation of Boundary Layer Transfer Using Wedge Solutions and Asymptotic Expansion," Journal Fluid Mech., 5, pp. 460-480 (1959.
[3] Drew, T. and Ryan, W., "The Mechanism of Heat Transmission: Distribution of Heat Flow About the Circumference of a Pipe in a Stream of Fluid," Trans. Am. Inst. Chem. Engr., 26, pp. 118-147 (1931).
[4] Small, J., "The Average and local Rates of Heat Transfer from the Surface of a Hot Cylinder in a Transverse Stream of Fluid," Phil. Mag. 19, pp. 251-260 (1935).
[5] Schmidt, E. and Wenner, K., "Heat Transfer over the Circumference of a Heated Cylinder in Transverse Flow," Forsch. Geb. Ing. Wes. 12, pp. 65-73 (1941).
[6] Comings, E., Clap, J. and Taylor, J., "Air Turbulence and Transfer Processes," Ind. Engrg. Chem., 40(6), pp. 1076-1082 (1948).
[7] Bollen, W., "Effect of Turbulence on Local Heat Transfer Coefficient Distributions Around a Cylinder Normal to Air Flow," Master's Thesis, Oregon State College (1949).
[8] Zapp, G., Jr., "The Effect of Turbulence on Local Heat Transfer Coefficients Around a Cylinder Normal to an Air Stream," Master's Thesis Oregon State College (1950).
[9] Schnautz, J., "Effect of Turbulence Intensity on Mass Transfer from Plates, Cylinders and Spheres in Air Streams," Doctoral Dissertation, Oregon State Univ. (1958).
[10] Seban, R., "The Influence of Turbulence on Laminar Skin Friction and Heat Transfer," Physics Fluids, 9, pp. 2337-2344 (1966).
[11] Kestin, J., Maeder, P. F. and Sogin, H., 'The Influence of Turbulence on the Heat Transfer from Cylinders Near the Stagnation Point," 2. Agnew. Math. Phys. 12, pp. 115-132 (1969).
[12] Appelgvist, B., "The Influence of Turbulence on the Local Heat Transfer from a Cylinder Normal to an Air Stream, Including Further Development of a Method for Local Heat Transfer Measurements," Doctoral Dissertation, Institute of Applied Thermo and Fluid Dynamics, Chalmers University of Technology, Gothenburg (1965).
[13] Smith, M. and Kuethe, A., "Effects of Turbulence on Laminar Skin Friction and Heat Transfer," Physics Fluids, 9, pp. 2337-2344 (1966).
[14] Kestin, J. and Wood, R., "The Influence of Turbulence on the Mass Transfer from Cylinders," Journal Heat Transfer, 93C, pp. 321-327 (1971).
[15] Kayalar, L., "Experimentelle and Theoretische Untersuchungen über den Einfluss des Turbulenzgrades auf den Wärmeübergang in der Ungebung des Staupunktes eines Kreiszlinders," Eorsh. Geb. IngWes., 35, pp. 157-167 (1969).
[16] Dyban, E. and Epick, E., "Some Heat Transfer Features in the Air Flow of Intensified Turbulence," in Proc. of the Fourth Int. Heat Transfer Conf:, Paris (1970).
[17] Lowery, G. W. and Vachon, R. I., "The Effect of Turbulence on Heat Transfer from Heated Cylinders," Int. J. Heat Mass Transfer, 18, pp. 1229-1242 (1975).
[18] Yardi, N. R. and Sukhatme, S. P., "Effects of Turbulence Intensity and Integral Length Scale of a Turbulent Free Stream on Forced Convection Heat Transfer from a Circular Cylinder in Cross Flow," Proc. Sixth Int. Heat Transfer Conf., Toronto, Canada, Vol. 5, FC(b)-29, pp. 347352 (1978).
[19] Traci, R. M. and Willcox, D. C., "Freestream Turbulence Effects on Stagnation Point Heat Transfer," AIAA Journal, 13, pp. 890-896 (1965).
[20] Sutera, S. P., Maeder, P. F. and Kestin, J., "On the Sensitivity of Heat Transfer on the Stagnation Point Boundary Layer to Free Stream Vorticity," Journal Fluid Hechonics, 16/4, pp. 497-520 (1963).
[21] Sutera, S. P., 'Vorticity Amplification in Stagnation Point Flow and Its Effect on Heat Transfer," Journal Fluid Mechanics, 21/3, pp. 513534 (1965).
[22] Sadeh, W. Z., Sutera, S. P. and Maeder, P. F., "Analysis of Vorticity Amplification in the Flow Approaching a Two-Dimensional Stagnation Point," Z. Angew Math. Phys., 21, pp. 691-742 (1970).
[23] Colak-Antic, P., "Visuelle Untersuchungen von Langswirbeln im Staupunktgebiet eines Kreiszylinders bei Turbulenter Anströmung," DLR Mitteilung 71-13, Bericht Uber die DGLR-Fachausschuss-Sitzung, "Laminare and Turbulente Grenzschichtung," Gottingen, Pp. 194-220 (1971).
[24] Nagib, H. M. and Hodson, P. R., "Vortices Induced in Stagnation Region by Wakes; Aerodynamic Heating and Thermal Protection Systems," L. S. Fletcher, ed., 59, pp. 66-90, Progress in Aeronautics and Astronautics, AIAA (1977).
[25] Hassler, H., "Hitzdrahtmessungen von Langswirbelartigen Instabilitatserscheingen in Staupunktgebiet Eines Kreiszylindrrs in Turbulenter Anstromung," DLR Mitteilung 71-13, Bericht Über Die DGLR-Fachausschussitzung, Laminare and Turbulente Grenzschichtung," Gottingen, pp. 221239 (1971).
[26] Morkovin, M., "On the Question of Instabilities Upstream of Cylindrical Bodies," NASA CR3231 (1979).
[27] Lighthill, M. J., "The Response of Laminar Skin Friction and Heat Transfer to Fluctuations in the Stream Velocity," Proc. Roy. Soc. A224, pp. 1-23 (1954).
[28] Rott, M., 'Unsteady Viscous Flow in the Vicinity of a Stagnation Point," quart. Appl. Math., 13, pp. 444-451 (1956).
[29] Glauert, M. B., "The Laminar Boundary Layer on Oscillating PBates and Cylinders," Journal Fluid Mechanics, 1, pp. 9.7-110 (1956).
[30] Childs, E. P., Jr., "Analysis of the Response of Laminar Skin Friction and Heat Transfer to the Rotational Oscillation of a Circular Cylinder in a Steady Stream," Master's Thesis, Rensselaer Polytechnic Institute (1980).
[31] Sogin, H. H. and Subramanian, V. S., "Local Mass Transfer from Circular Cylinders in Cross Flow," Trans. ASME, Journal Heat Transfer, pp. 483493 (1961).
[32] Taylor, J., Master's Thesis, Univ. of Minn. (1975),
[33] Sogin, H. H., "Sublimation from Disks to Air Streams Flowing Normal to Their Surface," Trans. ASME, 80, p. 61 (1958).
[34] Skelland, A.H.P., Diffusional Mass Transfer, Wiley \& Sons, New York, pp. 49-54 (1974).
[35] Washburn, E. W., ed., International Critical Tables, Voi. IIf, McGrawHill, New York, p. 208 (1928).
[36] Bedingfield, C. H., Jr., and Drew, T. B., "Analogy between Heat and Mass Transfer: A Psychrometric Study," Ind. and Engrg. Chem., 42, Pt. 1, pp. 1165-1173 (1950).
[37] Bradshaw, P., An Introduction to Turbulence and Its Measurement, Pergamon Press, New York.
[38] Taylor, G. I., "The Spectrum of Turbulence," Proc. Roy. Soc., 164A, p. 476 (1938).
[39] Nagib, H. M., private communication.
[40] Hinze, J. O., Turbulence, McGraw-Hill, New York.
[41] Dryden, H. L., Schubauer, W. C., Mock, W. C., Jr. and Skramstad, H. K., "Measurements of Intensity and Scale of Wind Tunnel Turbulence and Their Relation to the Critical Reynolds Numbers of Spheres," NACA TR581 (1937).
[42] Townsend, A. A., The Structure of Turbulent Shear Flow, Cambridge Univ. Press, Cambridge, England, pp. 56-63 (1956).
[43] Kellog, R. M. and Corşin, S., "Evolution of a Spectrally Local Disturbance in Grid Generated, Nearly Isotropic Turbulence," Journal of Fluid Mechanics, 96/4, pp. 641-669 (1980).
[44] Abramowitz and Stegun, Hondbook of Mathematical Functions, Dover Publications, New York (1972).

## APPENDIX A <br> Procedure for the Setup of the Measuring Table

As pointed out in the discussion of the measurement procedure, accurate determination of the local mass loss of the naphthalene surface is to some degree dependent upon the precise configuration of the measurement apparatus. To avoid unnecessary measurement errors a detailed procedure was developed for the setup and positioning of the various components of the table. This procedure is outlined below.

To avoid overranging of the displacement transducers during a measurement traverse, it is necessary that the test section be accurately leveled and centered on the rotary table. Leveling adjustments are provided by the holding pins on the alignment fixture plate and the section can be centered by adjustment of the clamp heads which hold the fixture plate onto the rotary table. To calibrate these adjustments the test section and one of the displacement transducers are used. The section is installed onto the fixture plate and, through the use of the clamp head screws, roughly centered by eye. To level the section, the transducer is positioned on the upper face of the test section near the edge. The table is rotated and the reading of the gauge when above each of the three holding pins is recorded. The reading above one of the pins is arbitrarily chosen as the reference reading. The table is again rotated to place each of the other two pins in turn underneath the gauge needle. The height of each pin is adjusted until the reference reading is obtained. The entire leveling procedure is then repeated until the section is as level as possible. In this manner, the section can be leveled to within $5 \times\left(10^{-4}\right)$ inches.

Centering of the section is accomplished in a similar manner. The displacement transducer is positioned against the vertical face of the upper steel rim of the test section and used to indicate off-center runout. The table is rotated and the reading is recorded at four $90^{\circ}$ intervals which correspond to positions directly across from or over the brass positioning screws. The four readings are averaged to provide the reference reading which approximately corresponds to a centered section. The table is again rotated to position each of the clamp heads in turn across from the gauge and the clamp head screws are adjusted until the reference reading is obtained. Repetition of this procedure can center the section to within $1\left(10^{-4}\right)$ inches.

When the test section is accurately centered and leveled, the four displacement transducers can be positioned in the desired measurement configuration. For accurate results, the points at which the gauges contact the surface must lie approximately along a common vertical line and the line of action of each gauge needle must be approximately perpendicular to the surface of the test section. To accurately position the gauge heads, the test section with a cast naphthalene surface is used. With a machinist's square, a true vertical is marked across the cylindrical face of the test section, using a fine point scribe along the naphthalene insert and a sharp pencil on the steel rims. The desired contact points for the four gages are indicated by cross hatches. The table is rotated to place this spanwise line at the desired contact position and the gauges are approximately configured by visual inspection. Their clamps are tightened just enough to avoid slippage and yet allow for slight positional adjustments. A perpendicular line of action of the
gauge needles can be roughly approximated at this point by rotating the gauge heads until their bodies are square with respect to the cylindrical face of the test section. When the gauges are in place, the test section is removed from the table, noting the reading of the lowest gauge, which is used as a reference to later reinstall the section in a centered position. The line of action of the upper three gauges can now be accurately adjusted to a position perpendicular with respect to the cylindrical surface. (The lower gauge is adjusted later.) For this purpose a Starrett height transfer gauge is used. This gauge consists of two similar triangles which are stacked together to provide two parallel surfaces whose separation distance is adjustable. The gauge is used as a reference to position the lines of action of the displacement transducers parallel to the surface of the rotary table, which is perpendicular to the face of a leveled and centered test section. The height transfer gauge is positioned just in front of and below each needle in turn and the gap between the needle and the gauge is observed as the needle is moved in and out. (Although the range of the transducers is only 20 mils , a clutch mechanism allows the needles to be moved a substantial distance.) The gauge heads are adjusted with light twisting actions until there is no visible variation of the gap. The test section is then reinstalled on the table with the gauges contacting the marked spanwise line. The position of the upper gauge is checked by visual inspection and if necessary adjusted with light hand pressure. The correct position of the two napthalene gauges is obtained by "feeling out" the scribed lines with the respective gauge reading and continuous hand pressure. With care the angular orientation of the transducer heads will be unaltered by this
procedure. When the upper three gauges are accurately positioned, they are tightly clamped in place. A similar procedure is then followed to adjust the angular orientation and position of the remaining gauge, using the reading of the uppermost gauge as a reference for the removal and insertion of the test section.

When this procedure is complete, one final set of adjustments is made to move the operating range of each gauge inward or outward into an optimum position. This is done through the use of the fine adjustment screws on the gauge mounts. The two outer reference gauges are positioned such that their readings on a centered test section are approximately zero, the center of the operating range. The two measuring gauges are positioned farther inward, since their range must reach the depths of a sublimated surface. The gauges are positioned to give readings of approximately -5.0 mils on the centered test section (where the largest position reading corresponds to the most inward position). The measuring apparatus is then ready for use.

## APPENDIX B

## Measurements of Length Scales Using the Correlation Function

The reported values of the integral length scales of turbulence, L, were determined by fitting a measured spectral distribution to a theoretical distribution. Attempts were also made to determine the integral length scales from measurements of the lateral correlation function in the manner discussed by Hinze [40], however, the values determined using this technique were found to be drastically different from those obtained using the spectral distributions, which compare well with the previous measurements of Dryden et al. [41]. Also, due to the high levels of ambient noise in the wind tunnel and the electronic operations necessary to determine the correlation function, the former method was found to be highly prone to error. A discussion of the techniques used to determine the correlation function is given below, along with the results obtained. The lateral correlation function is defined as

$$
g\left(z_{1}\right)=\frac{\overline{u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right)}}{\sqrt{u^{\prime 2}\left(z_{0}\right)} \sqrt{u^{\prime 2}\left(z_{0}+z_{1}\right)}}
$$

where $z$ is the lateral (spanwise) coordinate. The integral length scale is given in terims of this function by

$$
L=\int_{0}^{\infty} g\left(z_{1}\right) d z_{l}
$$

The correlation function can be measured experimentally using two hot wires whose separation distance is variable. The configuration is illustrated in Fig. 19a. The length scale is determined by numerical integration of a curve fit to the correlation measured at a number of separation distances, $\mathbf{z}_{1}$.

The correlation function is determined from combinations of the $A C$ outputs of the two wires. Assuming that the turbulence field is uniform in the average sense, the terms in the denominator are constant across the span and equal to the measured turbulence level, T , i.e.

$$
(T u)^{2}=\sqrt{u^{\prime 2}\left(z_{0}\right)} \sqrt{u^{\prime 2}\left(z_{0}+z_{1}\right)}
$$

If the system is noise-free and the wires are of matched response characteristics, the turbulent velocities are given by

$$
\begin{gathered}
u^{\prime}\left(z_{0}\right)=\frac{\partial U}{\partial E} e_{1} \\
u^{\prime}\left(z_{0}+z_{1}\right)=\frac{\partial U}{\partial E} e_{2}
\end{gathered}
$$

and the correlation term $\overline{u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right)}$ can be determined by differencing the mean square sum and mean square difference of the signals, i.e.

$$
\overline{u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right)}=\frac{1}{4}\left(\frac{\partial U}{\partial E}\right)^{2}\left[\overline{\left(e_{1}+e_{2}\right)^{2}-\left(e_{1}-e_{2}\right)^{2}}\right] .
$$

In the actual flow there were, however, significant levels of pressure and electrical noise present. Since both wires and hence both available anemometer channels were required for the determination of the correlation function, this noise could not be directiy eliminated. Further, frequency filtering of the noise is improper since this would significantly alter the correlation distribution. The ambient noise was hence read along with the true turbulence outputs and later eliminated mathematically. The actual wire outputs are

$$
\begin{aligned}
& e_{1}=e_{T_{1}}+e_{C_{1}}+e_{p} \\
& e_{2}=e_{T_{2}}+e_{C_{2}}+e_{p}
\end{aligned}
$$

where the subscript $T$ denotes $A C$ components due to true turbulence, the subscript C denotes $A C$ components due to electrical noise, and the subscript $P$ denotes those due to pressure noise. The apparent value for $\overline{u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right)}$ is then given by

$$
\begin{aligned}
u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right)_{a p p}= & u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right) \text { actual } \\
& +\frac{1}{4}\left(\frac{\partial U}{\partial E}\right)^{2}\left[\overline{e_{C_{1}}}+\overline{e_{C_{2}}{ }^{2}}+4 \overline{e_{p}^{2}}\right]
\end{aligned}
$$

The last term due to noise should be approximately constant across the flow, and hence its value can be determined by measuring the apparent level of $\overline{u^{\prime}\left(z_{0}\right) u^{\prime}\left(z_{0}+z_{1}\right)}$ at a large value of $z$, for which the actual correlation term is zero. The equation for the correlation function is then

$$
\left.g\left(z_{1}\right) \geq \frac{1}{4}\left(\frac{U}{E}\right)^{2}\left(\frac{1}{T u}\right)^{2}\left[\overline{\left(e_{1}+e_{2}\right)^{2}}-\overline{\left(e_{1}-e_{2}\right)^{2}}-\overline{\left(e_{C_{1}}^{2}\right.}+\overline{e_{C_{2}}^{2}}+4 \overline{e_{P}^{2}}\right)\right]
$$

Determination of the correlation function in this manner requires extensive use of electronic mean square operations. With the equipment used in the reported measurements, the repeatability of such operations was found to be about $+15 \%$. This large level of uncertainty significantly affects the determination of the correlation function allowing for possible errors on the order of $\pm 30 \%$.

The length scales determined from measured correlation functions are given in Table Al along with the previously reported values obtained with the spectral technique. In general, the values obtained from the two methods compare poorly. In some cases, the discrepancy is larger than that allowed by the estimated uncertainties of each method. At present, further explanation of the discrepancy is unavailable. Since the values obtained from the spectral technique compared well with those suggested by the results of Dryden et al. [41], they were accepted as the most representative results.

Table A1. Comparison of length scales measured with correlation function to those determined from spectral distributions

| Screen | Pos-X/M | $(I / D)_{\text {corr }}$ | $(I / D)_{\text {spec }}$ |
| :---: | :---: | :---: | :---: |
| $M=.125^{\prime \prime}$ | 144 | .005 | .012 |
|  | 268 | .013 | .017 |
|  | 448 | .015 | .028 |
| $M=.621^{\prime \prime}$ | 29.0 | .027 | .018 |
|  | 53.9 | .035 | .022 |
|  | 90.2 | .043 | .030 |
| $M=.875^{\prime \prime}$ | 20.6 | .048 | .030 |
|  | 38.3 | .063 | .038 |
|  | 64.0 | .098 | .050 |

APPENDIX C<br>Theoretical Considerations of the Amplification<br>of Flow Nonuniformities in a Stagnation Zone

A number of theoretical investigations have been conducted to examine the amplification of a periodic variation superimposed on aniform mean flow as a stagnation zone is approached. Sutera et al. [20] and Sutera [21] have presented a model for the amplification within the region of the boundary layer normally associated with a two-dimensional stagnation point. In their analyses the relevant equations are not explicitly solved but rather used in an analog computer to obtain approximate distributions for the variables of interest. Sadeh, Sutera and Maeder [22] have attempted to extend the treatment beyond the boundary layer region. An equation for the distribution of vorticity along the stagnation plane is presented; however, the variation of the streamwise velocity component is not obtained. In an attempt to examine the nature of the assumptions made in these treatments and the validity of the results, the problem is developed below in a somewhat more rigorous manner than the previous investigations. Although a valid solution is not obtained, the analysis demonstrates some of the basic aspects of the mathematical structure of the problem and identifies some inherent invalidities on the previously presented solutions.

Consider an infinitely long cylinder immersed in a cross stream. whose velocity profile contains a uniform component and a component which varies periodically in the spanwise direction as shown in Fig. Al. For mathematical simplicity the variation is assumed to be sinusoidal. Tó model the situation investigated by the current experiments, the wavelength

is assumed to be large with respect to the boundary layer thickness normally associated with two-dimensional stagnation on a cylinder. Then, if only the external flow region is considered, the effects of viscosity can be neglected and the appropriate equations of motion are

$$
\begin{aligned}
& \bar{U} \frac{\partial \bar{U}}{\partial \bar{x}}+\bar{V} \frac{\partial \bar{U}}{\partial \bar{y}}+\bar{W} \frac{\partial \bar{U}}{\partial \bar{z}}=\frac{-1}{\rho} \frac{\partial \bar{P}}{\partial \bar{x}} \\
& \bar{U} \frac{\partial \bar{V}}{\partial \bar{x}}+\bar{V} \frac{\partial \bar{V}}{\partial \bar{y}}+\bar{W} \frac{\partial \bar{V}}{\partial \bar{z}}=\frac{-1}{\rho} \frac{\partial \bar{P}}{\partial \bar{y}} \\
& \bar{U} \frac{\partial \bar{W}}{\partial \bar{x}}+\bar{V} \frac{\partial \bar{W}}{\partial \bar{y}}+\bar{W} \frac{\partial \bar{V}}{\partial \bar{z}}=\frac{-1}{\rho} \frac{\partial \bar{P}}{\partial \bar{z}} \\
& \frac{\partial \bar{U}}{\partial \bar{x}}+\frac{\partial \bar{V}}{\partial \bar{y}}+\frac{\partial \bar{W}}{\partial \bar{z}}=0
\end{aligned}
$$

where the bars denote dimensional variables and the coordinate system shown in Fig. Al is used. With the assumed form of the incident velocity the boundary conditions far away from the cylinder are

$$
\left.\begin{array}{l}
\bar{U}(\bar{x}, \bar{y}, \bar{z}) \rightarrow U_{\infty}+K \cos \bar{z} / \lambda \\
\overline{\mathrm{V}}(\bar{x}, \bar{y}, \bar{z}) \rightarrow 0 \\
\overline{\mathrm{~W}}(\overline{\mathrm{x}}, \overline{\mathrm{y}}, \bar{z}) \rightarrow 0
\end{array}\right\} \begin{gathered}
\text { as } \overline{\mathrm{x}} \rightarrow \pm \infty \\
\text { or } \\
\text { as } \overline{\mathrm{y}}+ \pm \infty
\end{gathered}
$$

It will also be assumed for the moment that the interaction of the inviscid region with the internal viscid region will be of the type normally used in two-dimensional boundary layer analysis; the components of velocity normal to the surface are zero, i.e.

$$
\bar{U} \frac{\bar{x}}{R}+\bar{V} \frac{\bar{Y}}{R}=0 \quad \text { on } \quad \overline{x^{2}}+\overline{y^{2}}=R^{2}
$$

In addition to these conditions the equations necessitate conditions in the spanwise $(\bar{z})$ direction. Since we are considering a cylinder of infinite length, the relevant condition will be periodicity in $\bar{z}$. Further, a physical consideration of the flow field will demonstrate that there is no existing mechanism for a change in wavelength. (Such a change would have to occur in a continuous manner, the wavelength stretching about some point; however, the choice for this point would be arbitrary. Physically, there is no justification for the existence of such a point - hence, stretching of the wavelength cannot occur. This does not imply, however, that the velocity profile remains sinusoidal.) The conditions in the $z$ direction are then

$$
\left.\begin{array}{l}
\bar{U}\left(\bar{x}_{0}, \bar{y}_{0}, \bar{z}_{0}=u\left(\bar{x}_{0}, \bar{y}_{0}, \bar{z}_{0}+2 \pi n \lambda\right)\right. \\
\overline{\mathrm{V}}\left(\bar{x}_{0}, \bar{y}_{0}, \bar{z}_{0}\right)=\bar{v}\left(\bar{x}_{0}, \bar{y}_{0}, \bar{z}_{0}+2 \pi n \lambda\right) \\
\bar{W}\left(\bar{x}_{0}, \bar{y}_{0}, \bar{z}_{0}\right)=\bar{W}\left(x_{0}, \bar{y}_{0}, \bar{z}_{0}+2 \pi n \lambda\right)
\end{array}\right\} \begin{aligned}
& \text { for any } x_{0}, y_{0}, z_{0} \\
& \text { and integer values } \\
& \text { of } n .
\end{aligned}
$$

It is proper to nondimensionalize the equations and boundary conditions and for this purpose the following nondimensional variables are defined:

$$
\begin{aligned}
& \mathbf{x}=\bar{x} / R \quad U=\bar{U} / U_{\infty} \\
& y=\bar{y} / R \quad: \quad V=\bar{V} / U_{\infty} \\
& P=\frac{\bar{P}}{\rho U_{\infty}^{2}} \\
& z=\bar{z} / \lambda \quad W=\bar{W} / U_{\infty} \\
& a=R / \lambda \quad \delta=K / U_{\infty} .
\end{aligned}
$$

Using these variables the equations of motion and the boundary conditions are

$$
\begin{aligned}
& U \frac{\partial U}{\partial x}+V \frac{\partial U}{\partial y}+a W \frac{\partial U}{\partial z}=\frac{-\partial P}{\partial x} \\
& U \frac{\partial V}{\partial x}+V \frac{\partial V}{\partial y}+a W \frac{\partial V}{\partial z}=\frac{-\partial P}{\partial y} \\
& U \frac{\partial W}{\partial x}+V \frac{\partial W}{\partial y}+a W \frac{\partial W}{\partial z}=-a \frac{\partial P}{\partial z} \\
& \left.\begin{array}{l}
U \rightarrow 1+\delta \cos z \\
V \rightarrow 0 \\
W \rightarrow 0
\end{array}\right\} \quad \text { as } x+ \pm \infty \\
& U_{x}+V_{y}=0 \text { on } x^{2}+y^{2}=1 \\
& \left.\begin{array}{l}
U\left(x_{0}, y_{0}, z_{0}\right)=U\left(x_{0}, y_{0}, z_{0}+2 \pi n\right) \\
V\left(x_{0}, y_{0}, z_{0}\right)=V\left(x_{0}, y_{0}, z_{0}+2 \pi n\right) \\
W\left(x_{0}, y_{0}, z_{0}\right)=W\left(x_{0}, y_{0}, z_{0}+2 \pi n\right)
\end{array}\right\} \begin{array}{l}
\text { for any } x_{0}, y_{0}, z_{0} \\
\text { and integer values } \\
\text { of } n
\end{array}
\end{aligned}
$$

Since the incident flow field in the experiments is nominally uniform with a variation in magnitude of less than $\pm .2 \%$, the problem can be considered in the form of a perturbation about $\delta$ which is assumed to be much less than 1. (It should be noted that Sadeh et al. [22] use a similar technique. Sutera et al. [20] and Sutera [21] do not explicitly state their equations in a perturbation form; however, they do assume that the velocity field is that for two-dimensional flow with a superimposed three-dimensional variation. Since the superimposed flow is not allowed to alter the mean flow structure, their assumption is equivalent to the use of a perturbation analysis.) The solution for the velocities is then assumed to be in the form of a perturbation series, i.e.

$$
\begin{aligned}
& U=U_{0}(x, y, z)+\delta U_{1}(x, y, z)+\delta^{2} U_{2}(x, y, z)+\ldots \\
& V=V_{0}(x, y, z)+\delta V_{1}(x, y, z)+\delta^{2} V_{2}(x, y, z)+\ldots \\
& W=W_{0}(x, y, z)+\delta W_{1}(x, y, z)+\delta^{2} W_{2}(x, y, z)+\ldots
\end{aligned}
$$

Substituting these expressions into the equations of motion and examining the first-order terms, it is obvious that the first term in each series is simply the appropriate velocity for two-dimensional potential flow around a cylinder, i.e.

$$
U_{0}=1-\frac{x^{2}-y^{2}}{\left(x^{2}+y^{2}\right)^{2}}, \quad V_{0}=\frac{-2 x y}{\left(x^{2}+y^{2}\right)^{2}}, \quad W_{0}=0
$$

The equations for the terms of order $\delta$ are then

$$
\begin{aligned}
& U_{1} \frac{\partial U_{0}}{\partial x}+U_{0} \frac{\partial U_{1}}{\partial x}+V_{1} \frac{\partial U_{0}}{\partial y}+V_{0} \frac{\partial U_{1}}{\partial y}=\frac{-\partial P_{1}}{\partial x} \\
& U_{1} \frac{\partial V_{0}}{\partial x}+U_{0} \frac{\partial V_{1}}{\partial x}+V_{1} \frac{\partial V_{0}}{\partial y}+V_{0} \frac{\partial V_{1}}{\partial y}=\frac{-\partial P_{1}}{\partial y} \\
& U_{0} \frac{\partial W_{1}}{\partial x}+V_{0} \frac{\partial W_{1}}{\partial y}=-a \frac{\partial P_{1}}{\partial z} \\
& \frac{\partial U_{1}}{\partial x}+\frac{\partial V_{1}}{\partial y}+\frac{\partial W_{1}}{\partial z}=0
\end{aligned}
$$

and the appropriate boundary conditions are

$$
\begin{aligned}
& \left.\begin{array}{l}
U_{1} \rightarrow \cos z \\
V_{1} \rightarrow 0 \\
W_{1} \rightarrow 0
\end{array}\right\} \begin{array}{l}
\text { as } x \rightarrow \pm \infty \\
\text { or } y \rightarrow \pm \infty \\
U_{1} x+V_{1} y=0
\end{array} \quad \text { on } x^{2}+y^{2}=1
\end{aligned}
$$

$$
\left.\begin{array}{l}
u_{1}\left(x_{0}, y_{0}, z_{0}\right)=U_{1}\left(x_{0}, y_{0}, z_{0}+2 \pi n\right) \\
v_{1}\left(x_{0}, y_{0}, z_{0}\right)=v_{1}\left(x_{0}, y_{0}, z_{0}+2 \pi n\right) \\
W_{1}\left(x_{0}, y_{0}, z_{0}\right)=W_{1}\left(x_{0}, y_{0}, z_{0}+2 \pi n\right)
\end{array}\right\} \begin{aligned}
& \text { for any } x_{0}, y_{0}, z_{0} \\
& \text { and integer } \\
& \text { values of } n
\end{aligned}
$$

In an effort to simplify the problem, these equations can be considered for a small region near the stagnation plane, that is for $y \approx 0$. (Sadeh et al. [22], Sutera [21] and Sutera et al. [20] considered similar regions in their analyses.) If the functions are assumed to be analytic at $y=0$, the velocities can be expanded in Taylor series in $y$. It should be noted that since the flow field is symmetric about the stagnation plane,

$$
V(x, 0, z)=0 \quad \text { and } \quad \frac{\partial U}{\partial y}(x, 0, z)=0
$$

Expanding the velocities using these conditions

$$
\begin{aligned}
& U_{1}(x, y, z)=U_{1}(x, 0, z)+y \frac{\partial U_{1}}{y}(x, 0, z)+\ldots \\
& V_{1}(x, y, z)=y \frac{\partial V_{1}}{\partial y}(x, 0, z)+\frac{y^{2}}{2} \frac{\partial^{2} v_{1}}{\partial y^{2}}(x, 0, z)+\ldots \\
& W_{1}(x, y, z)=W_{1}(x, o, z)+y \frac{\partial W_{1}}{\partial y}(x, 0, z)+\ldots \\
& P_{1}(x, y, z)=P_{1}(x, o, z)+y \frac{\partial P_{1}}{\partial y}(x, o, z)+\ldots
\end{aligned}
$$

1
For' clarity, the following set of functions is defined:

$$
\begin{array}{ll}
F_{U}(x, z)=U_{1}(x, 0, z) & F_{P}(x, z)=P_{1}(x, 0, z) \\
F_{V},(x, z)=\frac{\partial V_{1}}{\partial y}(x, o, z) & F_{P^{\prime}}(x, z)=\frac{\partial P_{1}}{\partial y}(x, o, z) \\
F_{W}(x, z)=W_{1}(x, 0, z) &
\end{array}
$$

Substituting the Taylor expansions into the equations of motions and keeping only first-order terms yields

$$
\begin{aligned}
F_{U} \frac{\partial U_{O}}{\partial x}+U_{0} \frac{\partial F_{U}}{\partial x} & =\frac{-\partial F_{P}}{\partial x} \\
0 & =\frac{-\partial F_{P^{\prime}}}{\partial y} \\
U_{0} \frac{\partial F_{W}}{\partial x} & =-a \frac{\partial F_{P}}{\partial z} \\
\frac{\partial F_{U}}{\partial x}+a \frac{\partial F_{U}}{\partial z} & =-F_{V^{\prime}}
\end{aligned}
$$

The second equation of this set provides no useful information and is dropped. The first and third equations can be combined to eliminate $F_{p}$ giving the equation

$$
\frac{\partial U_{o}}{\partial x}\left(\frac{\partial F_{U}}{\partial z}-\frac{1}{a} \frac{\partial F_{W}}{\partial x}\right)=-U_{0} \frac{\partial}{\partial x}\left(\frac{\partial F_{U}}{\partial z}-\frac{1}{a} \frac{\partial F_{W}}{\partial x}\right) .
$$

This can be integrated with respect to $x$ to yield

$$
\frac{\partial F_{U}}{\partial z}-\frac{1}{a} \frac{\partial F_{W}}{\partial x}=\frac{K(z)}{U_{o}(x)}
$$

where $K(z)$ is a function of integration. Hence the problem statement becomes

$$
\begin{aligned}
& \frac{\partial F_{U}}{\partial z}-\frac{1}{a} \frac{\partial F_{W}}{\partial x}=\frac{K(z)}{U_{0}(x)} \\
& \left.\begin{array}{l}
\frac{\partial F_{U}}{\partial x_{i}}+a \frac{\partial F_{W}}{\partial z}=-F_{V}, \\
F_{U}(x, z) \rightarrow \cos z \\
F_{W}(x, z) \rightarrow 0
\end{array}\right\} \quad \text { as } x \rightarrow \infty \\
& F_{U}(k, z)=0 \\
& \left.F_{U}\left(x_{0}, z_{0}\right)=F_{U}\left(x_{0}, z_{0}+2 \pi n\right) \quad \begin{array}{l}
\text { for any } x_{0}, z_{o} \\
F_{W}\left(x_{0}, z_{0}\right)=F_{W}\left(x_{0}, z_{0}+2 \pi n\right)
\end{array}\right\} \begin{array}{l}
\text { and integer } \\
\text { values of } n .
\end{array}
\end{aligned}
$$

An examination of these equations immediately demonstrates that the problem is now underspecified: there are three unknowns, $F_{U}, F_{W}$ and $F_{V}$, and only two equations. In order to solve for the $U$ and $W$ velocity components, $F_{V}$, the gradient in the cross stream velocity $V$ at the stagnation plane, must be specified. In past investigations the assumption used was

$$
F_{V^{\prime}}=y F_{V}(x)
$$

Sadeh's solution shows that $F_{V}(x)$ decreases rapidly to zero as the cylinder is approached. Since the cross stream velocity must also go to zero at distances far from the cylinder, it will be assumed here that

$$
F_{V^{\prime}} \approx 0
$$

With this assumption, an explicit solution to the stated equations can be obtained in the form of a Fourier series

$$
\begin{aligned}
& F_{U}=\sum_{n=0}^{\infty}\left\{-A_{n}+\frac{1}{4} \text { an } A_{n}^{-} E_{1}[a n(x+1)] e^{a n(x+1)}\right. \\
& +\frac{1}{4} \text { an } A_{n} E_{i}[\operatorname{an}(x+1)] e^{-a n(x+1)} \\
& -\frac{1}{4} \text { an } A_{n} E_{1}[a n(x+1)] e^{a n(x-1)} \\
& -\frac{1}{4} \text { an } A_{n} E_{i}[\operatorname{an}(x-1)] e^{-a n(x-1)} \\
& \left.+c_{1 n} e^{a n x}+c_{2 n} e^{-a n x}\right\} \cos n z \\
& F_{W}=\frac{1}{a} \sum_{n=0}^{\infty}\left\{-\frac{1}{4} a^{2} n A_{n} E_{1}[a n(x+1)] e^{a n(x+1)}\right. \\
& -\frac{1}{4} a^{2} n A_{n} E_{i}[a n(x+1)] e^{-a n(x+1)} \\
& +\frac{1}{4} a^{2} n A_{n} E_{1}[a n(x-1)] e^{a n(x-1)} \\
& +\frac{1}{4} a^{2} n A_{n} E_{i}[a n(x-1)] e^{-a n(x-1)} \\
& \left.+c_{1 n} a e^{a n x}-c_{2 n} a e^{-a n x}\right\} \operatorname{sinn} z
\end{aligned}
$$

where $A_{n}, C_{1 n}$ and $C_{2 n}$ are constants of integration. $E_{i}$ and $E_{1}$ denote exponential integral functions as defined by Abramowitz and Stegun [44], i.e.

$$
\begin{aligned}
& E_{i}(r)=f_{-\infty}^{r} \frac{e^{t}}{t} d t \quad(r>0) \\
& E_{1}(r)=\int_{r}^{\infty} \frac{e^{-t}}{t} d t \quad(\arg r<\pi)
\end{aligned}
$$

Imposing the boundary conditions at infinity gives

$$
\begin{array}{ll}
C_{1 n}=0 & \text { for all } n \\
A_{1}=1 \\
A_{n}=0 & \text { for } n \neq 1
\end{array}
$$

## Further imposition of the boundary conditions at $x=1$ gives

$$
C_{2 n}=0 \quad \text { for all } n
$$

The streamwise component of velocity is then

$$
\begin{aligned}
F_{U}= & -1+\frac{1}{4} a E_{1}[a(x+1)] e^{a(x+1)}-\frac{1}{4} E_{1}[a(x-1)] e^{a(x-1)} \\
& \left.+\frac{1}{4} a E_{i}[a(x+1)] e^{-a(x+1)}-\frac{1}{4} a E_{i}[a(x-1)] e^{-a(x-1)}\right\} \cos z \\
= & u_{1}(x ; y, z) \text { for small } y .
\end{aligned}
$$

An examination of this solution will demonstrate that the assumptions made in the formulation of the problem are violated. Specifically, the assumed perturbation structure is invalid near the surface, since

$$
\lim _{x \rightarrow 0}\left(\frac{U_{1}}{U_{0}}\right) \rightarrow \infty
$$

This result is somewhat expected since the equation for $F_{U}$ obtained by cross differentiation

$$
\frac{\partial^{2} F_{U}}{\partial x^{2}}+a^{2} \frac{\partial^{2} F_{U}}{\partial z^{2}}=\frac{a^{2}}{U_{0}} \frac{d K}{d z}
$$

is singular at $x=1$ where $U_{0}=0$. This result would suggest that some type of inner-outer matching procedure is required to solve the stated perturbation problem. This is, however, somewhat of an anomaly since the equations do not exhibit the reduction of order for large $x$ characteristic of typical inner-outer perturbation problems, and hence an attempted solution would result in an unspecified set of constants. It should also be noted that the flow structure observed in the experiments of Nagib and Hodson [25] demonstrate that regions of flow
reversal exist near the surface of the cylinder. Mathematically this requires that $\delta U_{1}>U_{0}$ for some region near the surface, and hence the assumed form for the external (outer) flow region must be invalid for some inner region. This violation of assumptions also occurs in the previously presented models of Sadeh et al. [22], Sutera et al. [20] and Sutera [21].

## APPENDIX D

## Tabular Listing of Mass Transfer Data

In the following pages a full tabular listing of the reported mass transfer measurements is given. For brevity only the calculated transfer rates are reported. The actual experimental loss depths in mils can be calculated using the "multiplier" and "loss correction" included with each data set, i.e.

$$
\text { Depth }(\text { mils })=\frac{\mathrm{Sh}}{\sqrt{\mathrm{Re}}} \div \text { multiplier }+ \text { loss correction. }
$$

For convenience, the figure in which each data set is plotted is also given in the listings. An index to the data table is given below.

## Data Index

## Circumferential data

```
No screen, Re = 75000, St = 0.0
    Re = 82500, St = 0.0
    Re=110000, St = 0.0
    (3 runs)
    Re = 110000, St = 0.0639 (2 runs)
    Re = 125000, St = 0.0
Tu = 0.34%, Re=110000, St = 0.0
    St = 0.0639
Tu = 1.182%, Re = 110000, St = 0.0.
        St = 0.0639
Tu = 1.801%, Re = 110000, St = 0.0.
                St = 0.0639
Tu = 2.651%, Re= 50000, St = 0.0
    St = 0.1406
    Re = 75000,
    St = 0.0 (2 runs)
    St = 0.0417
    St = 0.1041
    Re = 110000,
        St = 0.0
        st = 0.0213 (2 runs)
        St = 0.0213 ( }\mp@subsup{0}{0}{}=1\mp@subsup{2}{}{\circ}
        St = 0.0355 (2 runs)
        St = 0.0497 (4 runs)
        St = 0.0539 (3 runs)
        St = 0.0781
Tu = 4.9%, Re = 110000, St = 0.0
        St = 0.0071
        St = 0.0213
        St = 0.0355
        St = 0.0497
        St = 0.0639
```

Spanwise Data $(\operatorname{Re}=110000)$



NO SCREEN $\quad R E=82500, S T=0.0$
(EIG 27)
MULTIPLIER=0.19925 /MIL LOSS CORRECTION=0.110 MILS

| DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=-.5^{\prime \prime} \end{gathered}$ | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=+.5^{\prime \prime} \end{gathered}$ | DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=-.5^{\prime \prime} \end{gathered}$ | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=+.5 " \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -176 | 2.368 | 2.355 | 4 | 1.539 | 1.588 |
| -172 | 2.369 | 2.354 | 8 | 1.546 | 1.591 |
| -168 | 2.232 | 2.287 | 12 | 1.553 | 1.576 |
| -164 | 2.192 | 2.222 | 16 | 1.525 | 1.557 |
| -160 | 2.117 | 2.096 | 20 | 1.509 | 1.544 |
| -156 | 2.083 | 2.067 | 24 | 1.479 | 1.525 |
| -152 | 2.032 | 1.980 | 28 | 1.469 | 1.518 |
| -148 | 1.961 | 1.891 | 32 | 1.434 | 1.500 |
| -144 | 1.890 | 1.834 | 36 | 1.431 | 1.493 |
| -140 | 1.831 | 1.748 | 40 | 1.399 | 1.459 |
| -136 | 1.748 | 1.717 | 44 | 1.326 | 1.410 |
| -132 | 1.660 | 1.679 | 48 | 1.337 | 1.358 |
| -128 | 1.648 | 1.623 | 52 | 1.326 | 1.333 |
| -124 | 1.641 | 1.625 | 56 | 1.257 | 1.260 |
| -120 | 1.558 | 1.548 | 60 | 1.215 | 1.163 |
| -116 | 1.477 | 1.428 | 64 | 1.107 | 1.069 |
| -112 | 1.354 | 1.290 | 68 | 0.999 | 0.950 |
| -108 | 1.239 | 1.159 | 72 | 0.863 | 0.755 |
| -104 | 1.122 | 1.075 | 76 | 0.585 | 0.515 |
| -100 | 1.087 | 1.031 | 80 | 0.446 | 0.473 |
| -96 | 1.048 | 0.992 | 84 | 0.585 | 0.613 |
| -92 | 0.961 | 0.881 | 88 | 0.779 | 0.794 |
| -88 | 0.780 | 0.710 | 92 | 0.894 | 0.946 |
| -84 | 0.592 | 0:553 | 96 | 1.049 | 1.063 |
| -80 | 0.449 | 0.404 | 100 | 1.064 | 1.048 |
| -76 | 0.526 | 0.571 | 104 | 1.107 | 1.162 |
| -72 | 0.780 | 0,818 | 108 | 1.200 | 1.234 |
| -68 | 0.950 | 0.985 | 112 | 1.315 | 1.355 |
| -64 | 1.062 | 1.083 | 116 | 1.427 | 1.498 |
| -60 | 5.000 | 5.000 | 120 | 1.518 | 1.591 |
| -56 | 1.236 | 1.232 | 124 | 1.613 | 1.656 |
| -52 | 1.305 | 1.316 | 128 | 1.610 | 1.659 |
| -48 | 1.330 | 1.354 | 132 | 1.626 | 1.682 |
| -44 | 1.347 | 1.392 | 136 | 1.687 | 1.714 |
| -40 | 1.399 | 1.427 | 140 | 1.727 | 1.794 |
| -36 | 1.438 | 1.472 | 144 | 1.831 | 1.873 |
| -32 | 1.431 | 1.493 | 148 | 1.932 | 1.967 |
| -28 | 1.497 | 1.518 | 152 | 2.010 | 1.953 |
| -24 | 1.506 | 1.518 | 156 | 2.027 | 2.077 |
| -20 | 1.528 | 1.560 | 160 | 2.113 | 2.144 |
| -16 | 1.544 | 1.566 | 164 | 2.157 | 2.207 |
| -12 | 1.548 | 1.574 | 168 | 2.226 | 2.328 |
| -8 | 1.554 | 1.574 | 172 | 2.336 | 2.371 |
| -4 | 1.548 | 1.572 | 176 | 2.348 | 2.373 |
| 0 | 1.556 | 1.580 | -180 | 2.383 | 2.385 |


| DEG | SH//RE |
| :---: | :---: |
|  | $2=0$ |
| -179 | 2.551 |
| -175 | 2.533 |
| -171 | 2.487 |
| -167 | 2.385 |
| -163 | 2.319 |
| -159 | 2.225 |
| -155 | 2.201 |
| -151 | 2.144 |
| -147 | 2.041 |
| -143 | 1.975 |
| -139 | 1.887 |
| -135 | 1.809 |
| -131 | 1.767 |
| -127 | 1.743 |
| -123 | 1.704 |
| -119 | 1.676 |
| -115 | 1.592 |
| -111 | 1.474 |
| -107 | 1.342 |
| -103 | 1.236 |
| -99 | 1.173 |
| -95 | 1.134 |
| -91 | 1.040 |
| -87 | 0.856 |
| -83 | 0.669 |
| -79 | 0.549 |
| -75 | 0.639 |
| -71 | 0.880 |
| -67 | 1.019 |
| -63 | 1.167 |
| -59 | 1.206 |
| -55 | 1.254 |
| -51 | 1.330 |
| -47 | 1.330 |
| -43 | 1.393 |
| -39 | 1.432 |
| -35 | 1.456 |
| -31 | 1.495 |
| -27 | 1.526 |
| -23 | 1.502 |
| -19 | 1.526 |
| -15 | 1.532 |
| -11 | 1.571 |
| -7 | 1.595 |
| -3 | 1.559 |
|  |  |


| DEG | SH/ $/$ RE |
| ---: | :---: |
|  | $2=0$ |
| 1 | 1.553 |
| 5 | 1.562 |
| 9 | 1.556 |
| 13 | 1.562 |
| 17 | 1.541 |
| 21 | 1.492 |
| 25 | 1.483 |
| 29 | 1.453 |
| 33 | 1.450 |
| 37 | 1.432 |
| 41 | 1.417 |
| 45 | 1.366 |
| 49 | 1.342 |
| 53 | 1.281 |
| 57 | 1.245 |
| 61 | 1.146 |
| 65 | 1.076 |
| 69 | 0.959 |
| 73 | 0.775 |
| 77 | 0.558 |
| 81 | 0.603 |
| 85 | 0.757 |
| 89 | 1.019 |
| 93 | 1.107 |
| 97 | 1.158 |
| 101 | 1.245 |
| 105 | 1.348 |
| 109 | 1.450 |
| 113 | 1.571 |
| 117 | 1.658 |
| 121 | 1.719 |
| 125 | 1.737 |
| 129 | 1.785 |
| 133 | 1.791 |
| 139 | 1.860 |
| 143 | 1.927 |
| 147 | 2.020 |
| 151 | 2.117 |
| 155 | 2.159 |
| 157 | 2.219 |
| 161 | 2.276 |
| 165 | 2.373 |
| 169 | 2.406 |
| 173 | 2.460 |
| 177 | 2.472 |
|  |  |
|  |  |

NO SCREEN $\quad$ RE $=110000, S T=0.0$ (RUN 2, EIG 28) MULTIPLIER=0.30095 /MIL LOSS CORRECTION=0.053 MILS

| DEG | $\begin{gathered} S H / \sqrt{R E} \\ Z=0 \end{gathered}$ | DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ Z=0 \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| -179 | 2.537 | 1 | 1.552 |
| -175 | 2.387 | 5 | 1.576 |
| -171 | 2.363 | 9 | 1.558 |
| -167 | 2.307 | 13 | 1.555 |
| -163 | 2.252 | 17 | 1.540 |
| -159 | 2.146 | 21 | 1.525 |
| -155 | 2.123 | 25 | 1.521 |
| -151 | 2.044 | 29 | 1.514 |
| -147 | 1.992 | 33 | 1.534 |
| -143 | 1.925 | 37 | 1.472 |
| -139 | 1.848 | 41 | 1.438 |
| -135 | 1.821 | 45 | 1.426 |
| -131 | 1.763 | 49 | 1.408 |
| -127 | 1.723 | 53 | 1.326 |
| -123 | 1.727 | 57 | 1.264 |
| -119 | 1.698 | 61 | 1.221 |
| -115 | 1.655 | 65 | 1.130 |
| -111 | 1.549 | 69 | 0.998 |
| -107 | 1.417 | 73 | 0.808 |
| -103 | 1.270 | 77 | 0.582 |
| -99 | 1.191 | 81 | 0.576 |
| -95 | 1.166 | 85 | 0.777 |
| -91 | 1.107 | 89 | 0.992 |
| -87 | 0.922 | 93 | 1.110 |
| -83 | 0.710 | 97 | 1.200 |
| -79 | 0.563 | 101 | 1.258 |
| -75 | 0.630 | 105 | 1.377 |
| -71 | 0.854 | 109 | 1.481 |
| -67 | 1.077 | 113 | 1.610 |
| -63 | 1.114 | 117 | 1.649 |
| -59 | 1.200 | 121 | 1.704 |
| -55 | 1.251 | 125 | 1.769 |
| -51 | 1.312 | 129 | 1.716 |
| -47 | 1.347 | 133 | 1.736 |
| -41 | 1.371 | 137 | 1.778 |
| -37 | 1.399 | 141 | 1.848 |
| -33 | 1.429 | 145 | 1.912 |
| -29 | 1.463 | 149 | 2.017 |
| -25 | 1.490 | 153 | 2.093 |
| -23 | 1.525 | 157 | 2.204 |
| -19 | 1.511 | 161 | 2.182 |
| -15 | 1.549 | 165 | 2.246 |
| -11 | 1.564 | 169 | 2.332 |
| -7 | 1.561 | 173 | 2.473 |
| -3 | 1.555 | 177 | 2.375 |



NO SCREEN $\quad R E=110000, S T=0.0639$ (RUN 1)
MULTIPLIER=0.23235 /MIL LOSS CORRECTION=0.034 MILS

| DEG | SH/ $/ \overline{\mathrm{RE}}$ | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ | DEG | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ | SH/ $\sqrt{\text { RE }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2=-.5" | $2=+.{ }^{\prime \prime}$ |  | $Z=-.{ }^{\prime \prime}$ | $\mathrm{z}=+.5^{\prime \prime}$ |
| -178 | 2.476 | 2.496 | 2 | 1.558 | 1.592 |
| -174 | 2.472 | 2.451 | 6 | 1.560 | 1.569 |
| -170 | 2.465 | 2.460 | 10 | 1.558 | 1.565 |
| -166 | 2.390 | 2.391 | 14 | 1.537 | 1.566 |
| -162 | 2.305 | 2.323 | 18 | 1.522 | 1.563 |
| -158 | 2.243 | 2.278 | 22 | 1.516 | 1.539 |
| -154 | 2.202 | 2.191 | 26 | 1.484 | 1.770 |
| -150 | 2.107 | 2.096 | 30 | 1.505 | 1.481 |
| -146 | 2.040 | 2.024 | 34. | 1.444 | 1.455 |
| -142 | 1.952 | 1.974 | 40 | 1.421 | 1.446 |
| -138 | 1.891 | 1.980 | 44 | 1.378 | 1.391 |
| -134 | 1.818 | 1.857 | 48 | 1.363 | 1.346 |
| -130 | 1.810 | 1.801 | 52 | 1.302 | 1.298 |
| -126 | 1.716 | 1.739 | 56 | 1.247 | 1.239 |
| -122 | 1.667 | 1.660 | 58 | 1.178 | 1.152 |
| -118 | 1.649 | 1.580 | 62 | 1.077 | 1.028 |
| -114 | 1.514 | 1.490 | 66 | 0.949 | 0.928 |
| -110 | 1.434 | 1.433 | 70 | 0.876 | 0.866 |
| -106 | 1.342 | 1.346 | 74 | 0.832 | 0.833 |
| -102 | 1.255 | 1.182 | 78 | 0.828 | 0.845 |
| -98 | 1.102 | 1.097 | 82 | 0.831 | 0.843 |
| -94 | 0.989 | 0.969 | 86 | 0.832 | 0.856 |
| -90 | 0.872 | 0.859 | 90 | 0.892 | 0.955 |
| -86 | 0.837 | 0.831 | 94 | 0.995 | 1.052 |
| -82 | 0.821 | 0.823 | 98 | 1.145 | 1.220 |
| -78 | 0.801 | 0.820 | 102 | 1.257 | 1.310 |
| -74 | 0.823 | 0.829 | 106 | 1.347 | 1.397 |
| -70 | 0.867 | 0.884 | 110 | 1.429 | 1.470 |
| -66 | 0.961 | 1.000 | 114 | 1.531 | 1.559 |
| -62 | 1.076 | 1.112 | 118 | 1.608 | 1.642 |
| -58 | 1.176 | 1.216 | 122 | 1.668 | 1.722 |
| -54 | 1.240 | 1.273 | 126 | 1.745 | 1.800 |
| -50 | 1.280 | 1.315 | 130 | 1.792 | 1.850 |
| -46 | 1.339 | 1.379 | 134 | 1.844 | 1.892 |
| -42 | 1.391 | 1.432 | 138 | 1.911 | 1.950 |
| -38 | 1.398 | 1.436 | 142 | 1.975 | 2.009 |
| -34 | 1.454 | 1.501 | 146 | 2.009 | 2.045 |
| -30 | 1.453 | 1.509. | 150 | 2.092 | 2.153 |
| -26 | 1.509 | 1.530 | 154 | 2.191 | 2.225 |
| -22 | 1.530 | 1.538 | 158 | 2.218 | 2.328 |
| -18 | 1.535 | 1.538 | -162 | 2.315 | 2.355 |
| -14 | 1.556 | 1.592 | 166 | 2.350 | 2.413 |
| -10 | 1.607 | 1.554 | 170 | 2.400 | 2.462 |
| -6 | 1.541 | 1.592 | 174 | 2.441 | 2.517 |
| -2 | 1.566 | $1.591^{\prime}$ | 178 | 2.491 | 2.522 |



| DEG | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ |
| ---: | :---: | :---: |
|  | $2=-.5 "$ | $2=+.5{ }^{\prime \prime}$ |
| -176 | 2.472 | 2.468 |
| -172 | 2.438 | 2.434 |
| -168 | 2.416 | 2.412 |
| -164 | 2.358 | 2.354 |
| -160 | 2.332 | 2.328 |
| -156 | 2.271 | 2.267 |
| -152 | 2.178 | 2.174 |
| -148 | 2.097 | 2.093 |
| -144 | 2.008 | 2.004 |
| -140 | 1.936 | 1.932 |
| -136 | 1.938 | 1.934 |
| -132 | 1.848 | 1.844 |
| -128 | 1.790 | 1.786 |
| -124 | 1.725 | 1.721 |
| -120 | 1.683 | 1.679 |
| -116 | 1.619 | 1.615 |
| -112 | 1.554 | 1.550 |
| -108 | 1.442 | 1.438 |
| -104 | 1.345 | 1.341 |
| -100 | 1.273 | 1.269 |
| -96 | 1.130 | 1.126 |
| -92 | 1.017 | 1.013 |
| -88 | 0.908 | 0.904 |
| -84 | 0.847 | 0.843 |
| -80 | 0.857 | 0.853 |
| -76 | 0.852 | 0.848 |
| -72 | 0.867 | 0.863 |
| -68 | 0.891 | 0.887 |
| -64 | 0.947 | 0.943 |
| -60 | 1.081 | 1.077 |
| -56 | 1.172 | 1.168 |
| -52 | 1.271 | 1.267 |
| -48 | 1.305 | 1.301 |
| -44 | 1.336 | 1.332 |
| -40 | 1.384 | 1.380 |
| -36 | 1.397 | 1.393 |
| -32 | 1.424 | 1.420 |
| -28 | 1.468 | 1.464 |
| -24 | 1.480 | 1.476 |
| -20 | 1.523 | 1.519 |
| -16 | 1.532 | $1 . .528$ |
| -12 | 1.522 | 1.518 |
| -8 | 1.550 | 1.546 |
| -4 | 1.585 | 1.581 |
| 0 | 1.555 | 1.551 |
|  |  |  |


| DEG | SH $/ \sqrt{R E}$ | SH/ $\sqrt{R E}$ |
| ---: | :---: | :---: |
|  | $Z=-.5 \prime$ | $Z=+.5 "$ |
| 4 | 1.572 | 1.568 |
| 8 | 1.544 | 1.540 |
| 12 | 1.528 | 1.524 |
| 16 | 1.520 | 1.516 |
| 20 | 1.525 | 1.521 |
| 24 | 1.515 | 1.511 |
| 28 | 1.505 | 1.501 |
| 32 | 1.471 | 1.467 |
| 36 | 1.423 | 1.419 |
| 42 | 1.390 | 1.386 |
| 46 | 1.372 | 1.368 |
| 50 | 1.334 | 1.330 |
| 54 | 1.286 | 1.282 |
| 58 | 1.211 | 1.207 |
| 60 | 1.137 | 1.133 |
| 64 | 1.038 | 1.034 |
| 68 | 0.907 | 0.903 |
| 72 | 0.826 | 0.822 |
| 76 | 0.773 | 0.769 |
| 80 | 0.760 | 0.756 |
| 84 | 0.784 | 0.780 |
| 88 | 0.814 | 0.810 |
| 92 | 0.831 | 0.827 |
| 96 | 0.951 | 0.947 |
| 100 | 1.080 | 1.076 |
| 104 | 1.202 | 1.198 |
| 108 | 1.319 | 1.315 |
| 112 | 1.396 | 1.392 |
| 116 | 1.495 | 1.491 |
| 120 | 1.551 | 1.547 |
| 124 | 1.616 | 1.612 |
| 128 | 1.698 | 1.694 |
| 132 | $1 . .764$ | 1.760 |
| 136 | 1.810 | 1.806 |
| 140 | 1.836 | 1.832 |
| 144 | 1.916 | 1.912 |
| 148 | 1.989 | 1.985 |
| 152 | 2.062 | 2.058 |
| 156 | 2.138 | 2.134 |
| 160 | 2.213 | 2.209 |
| 164 | 2.268 | 2.264 |
| 168 | 2.310 | 2.306 |
| 172 | 2.378 | 2.374 |
| 176 | 2.448 | 2.444 |
| 180 | 2.445 | 2.441 |
|  |  |  |

NO SCREEN $\quad$ RE=125000, $S T=0.0$
(FIG 29)
MULTIPLIER=0.25859 /MIL LOSS CORRECTION=0.049 MILS

| DEG | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ | $\mathrm{SH} / \sqrt{ } \overline{\mathrm{RE}}$ | DEG | $\mathrm{SH} / / \overline{\mathrm{RE}}$ | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $z=-.51$ | $\mathrm{Z}=+.5^{\prime \prime}$ |  | $z=-.5^{\prime \prime}$ | $2=+.5^{\prime \prime}$ |
| -176 | 2.526 | 2.646 | 4 | 1.565 | 1.617 |
| -172 | 2.488 | 2.615 | 8 | 1.573 | 1.583 |
| -168 | 2.486 | 2.550 | 12 | 1.577 | 1.554 |
| -164 | 2.415 | 2.475 | 16 | 1.566 | 1.590 |
| -160 | 2.335 | 2.427 | 20 | 1.545 | 1.569 |
| -156 | 2.217 | 2.366 | 24 | 1.545 | 1.574 |
| -152 | 2.217 | 2.278 | 28 | 1.505 | 1.552 |
| -148 | 2.156 | 2.184 | 32 | 1.524 | 1.538 |
| -144 | 2.028 | 2.100 | 36 | 1.469 | 1.503 |
| -140 | 1.978 | 2.010 | 40 | 1.403 | 1.471 |
| -136 | 1.921 | 1.956 | 44 | 1.393 | 1.441 |
| -132 | 1.862 | 1.891 | 48 | 1.354 | 1.375 |
| -128 | 1.806 | 1.861 | 52 | 1.310 | 1.324 |
| -124 | 1.779 | 1.852 | 56 | 1.252 | 1.275 |
| -120 | 1.759 | 1.810 | 60 | 1.186 | 1.189 |
| -116 | 1.690 | 1.765 | 64 | 1.103 | 1.119 |
| -112. | 1.645 | 1.676 | 68 | 1.004 | 1.011 |
| -108 | 1.522 | 1.548 | 72 | 0.822 | 0.825 |
| -104 | 1.394 | 1.435 | 76 | 0.601 | 0.596 |
| -100 | 1.295 | 1.304 | 80 | 0.589 | 0.631 |
| -96 | 1.237 | 1.275 | 84. | 0.775 | 0.852 |
| -92 | 1.161 | 1.242 | 88 | 1.017 | 1.109 |
| -88 | 1.003 | 1.069 | 92 | 1.171 | 1.307 |
| -84 | 0.764 | 0.801 | 96 | 1.258 | 1.362 |
| -80 | 0.600 | 0.624 | 100 | 1.302 | 1.395 |
| -76 | 0.569 | 0.641 | 104 | 1.417 | 1.503 |
| -72 | 0.818 | 0.843 | 108 | 1.492 | 1.565 |
| -68 | 0.987 | 1.018 | 112 | 1.587 | 1.721 |
| -64 | 1.108 | 1.113 | 116 | 1.684 | 1.748 |
| -60 | 1.192 | 1.245 | 120 | 1.792 | 1.814 |
| -56 | 1.270 | 1.305 | 124 | 1.821 | 1.874 |
| -52 | 1.323 | 1.344 | 128 | 1.787 | 1.888 |
| -48 | 1.370 | 1.396 | 132 | 1.835 | 1.923 |
| -44 | 1.402 | 1.445 | 136 | 1.848 | 1.972 |
| -40 | 1.445 | 1.472 | 140 | 1.945 | 2.038 |
| -36 | 1.453 | 1.506 | 144 | 2.036 | 2.109 |
| -32 | 1.499 | 1.531 | 148 | 2.150 | 2.218 |
| -28 | 1.483 | 1.548 | 152 | 2.224 | 2.323 |
| -24 | 1.508 | 1.568 | 156 | 2.294 | 2.385 |
| -20 | 1.535 | 1.596 | 160 | 2.390 | 2.441 |
| -16 | 1.521 | 1.614 | 164 | 2.383 | 2.495 |
| -12 | 1.567 | 1.620 | 168 : | 2.456 | 2.555 |
| -8 | 1.583 | 1.598 | 172 | 2.497 | 2.602 |
| -4 | 1.595 | 1.616 | 176 | 2.560 | 2.643 |
| 0 | 1.570 | 1.616 | -180 | 2.561 | 2.645 |

$T U=0.339 \%$, $\mathrm{L} / \mathrm{D}=0.028, \mathrm{RE}=110000, \mathrm{ST}=0.0$
(FIG 34) MULTIPLIER=0.19724 /MIL

LOSS CORRECTION=0.180 MILS

| DEG | $\begin{gathered} S H / \sqrt{R E} \\ 2=-.5^{\prime \prime} \end{gathered}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ | DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=-.5^{\prime \prime} \end{gathered}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -176 | 2.429 | 2.465 | 4 | 1.572 | 1.563 |
| -172 | 2.314 | 2.411 | 8 | 1.568 | 1.560 |
| -168 | 2.276 | 2.355 | 12 | 1.550 | 1.557 |
| -164 | 2.226 | 2.306 | 16 | 1.532 | 1.544 |
| -160 | 2.184 | 2.250 | 20 | 1.536 | 1.529 |
| -156 | 2.098 | 2.165 | 24 | 1.452 | 1.499 |
| -152 | 2.066 | 2.088 | 28 | 1.469 | 1.471 |
| -148 | 1.974 | 1.973 | 32 | 1.443 | 1.445 |
| -144 | 1.876 | 1.909 | 36 | 1.433 | 1.419 |
| -140 | 1.799 | 1.810 | 40 | 1.424 | 1.393 |
| -136 | 1.736 | 1.726 | 44 | 1.348 | 1.364 |
| -132 | 1.651 | 1.688 | 48 | 1.351 | 1.326 |
| -128 | 1.602 | 1. 646 | 52 | 1.299 | 1.334 |
| -124 | 1.598 | 1.654 | 56 | 1.227 | 1.254 |
| -120 | 1.588 | 1.631 | 60 | 1.183 | 1.178 |
| -116 | 1.548 | 1.563 | 64 | 1.088 | 1.082 |
| -112 | 1.464 | 1.435 | 68 | 1.014 | 0.968 |
| -108 | 1.314 | 1.383 | 72 | 0.838 | 0.803 |
| -104 | 1.162 | 1.180 | 76 | 0.581 | 0.559 |
| -100 | 1.086 | 1.097 | 80 | 0.496 | 0.524 |
| -96 | 1.034 | 1.075 | 84 | 0.628 | 0.684 |
| -92 | 1.026 | 1.057 | 88 | 0.854 | 0.903 |
| -88 | 0.897 | 0.896 | 92 | 1.034 | 1.057 |
| -84 | 0.669 | 0.666 | 96 | 1.019 | 0.987 |
| -80 | 0.481 | 0.473 | 100 | 1.058 | 1.000 |
| -76 | 0.485 | 0.452 | 104 | 1.220 | 1.216 |
| -72 | 0.726 | 0.692 | 108 | 1.348 | 1.370 |
| -68 | 0.938 | 0.898 | 112 | 1.484 | 1.526 |
| -64 | 1.046 | 1.025 | 116 | 1.560 | 1.602 |
| -60 | 1.106 | 1.079 | 120 | 1.615 | 1.641 |
| -56 | 1.178 | 1.154 | 124 | 1.614 | 1.701 |
| -52 | 1.241 | 1.217 | 128 | 1.646 | 1.754 |
| -48 | 1.305 | 1.278 | 132 | 1.672 | 1.750 |
| -44 | 1.326 | 1.311 | 136 | 1.719 | 1.821 |
| -40 | 1.355 | 1.333 | 140 | 1.783 | 1.854 |
| -36 | 1.400 | 1.383 | 144 | 1.851 | 1.954 |
| -32 | 1.455 | 1.401 | 148 | 1.913 | 2.049 |
| -28 | 1.478 | 1.417 | 152 | 2.041 | 2.109 |
| -24 | 1.511 | 1.491 | 156 | 2.133 | 2.139 |
| -20 | 1.526 | 1.533 | 160 | 2.191 | 2.199 |
| -16 | 1.517 | 1.527 | 164 | 2.220 | 2.291 |
| -12 | 1.550 | 1.534 | 168 | 2.282 | 2.369 |
| -8 | 1.560 | 1.532 | 172 | 2.352 | 2.441 |
| -4 | 1.559 | 1.546 | 176 | 2.402 | 2.462 |
| 0 | 1.563 | 1.550 | 180 | 2.417 | 2.485 |

$T U=0.339 \%, L / D=0.028, \mathrm{RE}=110000, \mathrm{ST}=0.0639$ MULTIPLIER=0.19396 /MIL

LOSS CORRECTION=0.168 MILS

| DEG | $\begin{aligned} & S H / \sqrt{R E} \\ & 7=-5 \end{aligned}$ | $\begin{gathered} \mathrm{SH} / \sqrt{R E} \\ 7=+5 \end{gathered}$ | DEG | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ $Z=-51$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & 7=+5 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -176 | 2.319 | 2.387 | 4 | 1.557 | 1.536 |
| -172 | 2.263 | 2.313 | 8 | 1.548 | 1.482 |
| -168 | 2.295 | 2.311 | 12 | 1.544 | 1.508 |
| -164 | 2.216 | 2.256 | 16 | 1.515 | 1.490 |
| -160 | 2.172 | 2.196 | 20 | 1.512 | 1.486 |
| -156 | 2.102 | 2.193 | 24 | 1.476 | 1.473 |
| -152 | 2.022 | 2.079 | 28 | 1.416 | 1.432 |
| -148 | 1.928 | 2.004 | 32 | 1.405 | 1.422 |
| -144 | 1.899 | 1.921 | 36 | 1.380 | 1.375 |
| -140 | 1.804 | 1.855 | 40 | 1.362 | 1.341 |
| -136 | 1.720 | 1.821 | 44 | 1.318 | 1.309 |
| -132 | 1.724 | 1.765 | 48 | 1.269 | 1.282 |
| -128 | 1.656 | 1.702 | 52 | 1.243. | 1.227 |
| -124 | 1.622 | 1.651 | 56 | 1.174 | 1.162 |
| -120 | 1.534 | 1.562 | 60 | 1.074 | 1.084 |
| -116 | 1.454 | 1.476 | 64 | 0.983 | 0.975 |
| -112 | 1.380 | 1.397 | 68 | 0.858 | 0.855 |
| -108 | 1.334 | 1.330 | 72 | 0.792 | 0.819 |
| -104 | 1.250 | 1.259 | 76 | 0.770 | 0.779 |
| -100 | 1.172 | 1.162 | 80 | 0.728 | 0.794 |
| -96 | 1.029 | 1.033 | 84 | 0.733 | 0.793 |
| -92 | 0.898 | 0.910 | 88 | 0.741 | 0.796 |
| -88 | 0.804 | 0.813 | 92. | 0.806 | 0.863 |
| -84 | 0.799 | 0.785 | 96 | 0.923 | 0.994 |
| -80 | 0.818 | 0.797 | 100 | 0.951 | 0.999 |
| -76 | 0.815 | 0.794 | 104 | 1.113 | 1.198 |
| -72 | 0.814 | 0.779 | 108 | 1.236 | 1.265 |
| -68 | 0.869 | 0.850 | 112 | 1.300 | 1.349 |
| -64 | 0.967 | 0.927 | 116 | 1.394 | 1.447 |
| -60 | 1.078 | 1.064 | 120 | 1.461 | 1.565 |
| -56 | 1.171 | 1.136 | 124 | 1.476 | 1.612 |
| -52 | 1.216 | 1.201 | 128 | 1.594 | 1.679 |
| -48 | 1.294 | 1.263 | 132 | 1.657 | 1.730 |
| -44 | 1.400 | 1.296 | 136 | 1.704 | 1.751 |
| -40 | 1.367 | 1.300 | 140 | 1.871 | 1.846 |
| -36 | 1.410 | 1.368 | 144 | 1.832 | 1.905 |
| -32 | 1.444 | 1.398 | 148 | 1.903 | 1.971 |
| -28 | 1.422 | 1.446 | 152 | 1.962 | 2.032 |
| -24 | 1.501 | 1.442 | 156 | 2.043 | 2.153 |
| -20 | 1.492 | 1.466 | 160 | 2.125 | 2.203 |
| -16 | 1.483 | 1.475 | 164 | 2.198 | 2.260 |
| -12 | 1.502 | 1.478 | 168 | 2.248 | 2.289 |
| -8 | 1.544 | 1.525 | 172 | 2.301 | 2.332 |
| -4 | 1.557 | 1.539 | 176 | 2.311 | 2.376 |
| 0 | 1.563 | 1.545 | 180 | 2.350 | 2.378 |

$T U=1.182 \%, L / D=0.050, \quad R E=110000, \quad S T=0.0$
(EIG 35) MULTIPLIER=0. $19834 / \mathrm{MIL}$

| DEG | $\mathrm{SH} / / \overline{\mathrm{RE}}$ | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ |
| ---: | :---: | :---: |
|  | $Z=-.5 \prime$ | $Z=+.5^{\prime \prime}$ |
| -176 | 2.267 | 2.378 |
| -172 | 2.224 | 2.280 |
| -168 | 2.166 | 2.279 |
| -164 | 2.137 | 2.238 |
| -160 | 2.081 | 2.126 |
| -156 | 2.039 | 2.083 |
| -152 | 1.980 | 2.005 |
| -148 | 1.895 | 1.929 |
| -144 | 1.824 | 1.778 |
| -140 | 1.823 | 1.805 |
| -136 | 1.721 | 1.731 |
| -132 | 1.669 | 1.716 |
| -128 | 1.695 | 1.695 |
| -124 | 1.647 | 1.714 |
| -120 | 1.450 | 1.391 |
| -116 | 1.633 | 1.674 |
| -112 | 1.617 | 1.638 |
| -108 | 1.582 | 1.584 |
| -104 | 1.466 | 1.513 |
| -100 | 1.449 | 1.556 |
| -96 | 1.289 | 1.319 |
| -92 | 1.123 | 1.170 |
| -88 | 0.888 | 0.903 |
| -84 | 0.623 | 0.614 |
| -80 | 0.518 | 0.493 |
| -76 | 0.706 | 0.657 |
| -72 | 0.936 | 0.906 |
| -68 | 1.078 | 1.044 |
| -64 | 1.213 | 1.171 |
| -60 | 1.290 | 1.261 |
| -56 | 1.373 | 1.321 |
| -52 | 1.414 | 1.399 |
| -48 | 1.474 | 1.426 |
| -44 | 1.513 | 1.517 |
| -40 | 1.557 | 1.579 |
| -36 | 1.591 | 1.607 |
| -32 | 1.661 | 1.663 |
| -28 | 1.702 | 1.671 |
| -24 | 1.705 | 1.701 |
| -20 | 1.700 | 1.735 |
| -16 | 1.767 | 1.787 |
| -12 | 1.753 | 1.773 |
| -8 | 1.792 | 1.788 |
| -4 | 1.820 | 1.796 |
| 0 | 1.806 | 1.813 |
| 0 |  |  |


| DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ Z=-.5^{\prime \prime} \end{gathered}$ | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=+.5^{\prime \prime} \end{gathered}$ |
| :---: | :---: | :---: |
| 4 | 1.794 | 1.792 |
| 8 | 1.770 | 1.747 |
| 12 | 1.724 | 1.765 |
| 16 | 1.735 | 1.726 |
| 20 | 1.713 | 1.710 |
| 24 | 1.686 | 1.698 |
| 28 | 1.623 | 1.654 |
| 32 | 1.627 | 1.630 |
| 36 | 1.589 | 1.570 |
| 40 | 1.537 | 1.522 |
| 44 | 1.522 | 1.471 |
| 48 | 1.437 | 1.417 |
| 52 | 1.456 | 1.476 |
| 56 | 1.316 | 1.274 |
| 60 | 1.231 | 1.195 |
| 64 | 1.158 | 1.089 |
| 68 | 0.984 | 0.946 |
| 72 | 0.791 | 0.710 |
| 76 | 0.561 | 0.510 |
| 80 | 0.580 | 0.598 |
| 84 | 0.870 | 0.895 |
| 88 | 1.341 | 1.559 |
| 92 | 1.326 | 1.373 |
| 96 | 1.438 | 1. 488 |
| 100 | 1.537 | 1.567 |
| 104 | 1.588 | 1.588 |
| 108 | 1.658 | 1.666 |
| 112 | 1.669 | 1.681 |
| 116 | 1.636 | 1.702 |
| 120 | 1.660 | 1.886 |
| 124 | 1.666 | 1.704 |
| 128 | 1.673 | 1.713 |
| 132 | 1.693 | 1.792 |
| 136 | 1.726 | 1.777 |
| 140 | 1.793 | 1.855 |
| 144 | 1.864 | 1.886 |
| 148 | 1.947 | 1.988 |
| 152 | 1.977 | 2.075 |
| 156 | 2.060 | 2.137 |
| 160 | 2.071 | 2.189 |
| 164 | 2.164 | 2.287 |
| 168 | 2.122 | 2.166 |
| 172 | 2.205 | 2.361 |
| 176 | 2.305 | 2.414 |
| -180 | 2.297 | 2.344 |

TU=1.182\%, L/D=0.050, $\mathrm{RE}=110000, \mathrm{ST}=0.0639$
MULTIPLIER=0.21396 /MIL
LOSS CORRECTION=0.020 MILS

| DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ 7 \end{gathered}$ | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ | DEG | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ | $\mathrm{SH} / \sqrt{\mathrm{RE}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| -176 | 2.190 | 2.359 | 4 | 1.765 | 1.832 |
| -172 | 2.133 | 2.450 | 8 | 1.772 | 1.818 |
| -168 | 2.097 | 2.364 | 12 | 1.739 | 1.797 |
| -164 | 2.016 | 2.233 | 16 | 1.712 | 1.765 |
| -160 | 1.999 | 2.150 | 20 | 1.692 | 1.766 |
| -156 | 1.950 | 2.051 | 24 | 1.677 | 1.753 |
| -152 | 1.912 | 2.027 | 28 | 1.653 | 1.693 |
| -148 | 1.861 | 1.999 | 32 | 1.626 | 1.666 |
| -144 | 1.822 | 1.903 | 36 | 1.559 | 1.631 |
| -140 | 1.772 | 1.848 | 40 | 1.517 | 1.577 |
| -136 | 1.730 | 1.809 | 44 | 1.431 | 1.519 |
| -132 | 1.718 | 1.808 | 48 | 1.416 | 1.453 |
| -128 | 1.715 | 1.769 | 52 | 1.329 | 1.371 |
| -124 | 1.690 | 1.729 | 56 | 1.257 | 1.319 |
| -120 | 1.621 | 1.681 | 60 | 1.133 | 1.174 |
| -116 | 1.617 | 1.659 | 64 | 1.017 | 1.044 |
| -112 | 1.588 | 1.664 | 68 | 0.897 | 0.904 |
| -108 | 1.497 | 1.584 | 72 | 0.825 | 0.846 |
| -104 | 1.472 | 1.478 | 76 | 0.758 | 0.830 |
| -100 | 1.349 | 1.418 | 80 | 0.799 | 0.872 |
| -96 | 2.194 | 1.262 | 84 | 0.800 | 0.905 |
| -92 | 1.060 | 1.080 | 88 | 0.867 | 0.969 |
| -88 | 0.898 | 0.950 | 92 | 0.988 | 1.088 |
| -84 | 0.823 | 0.889 | 96 | 1.172 | 1.265 |
| -80 | 0.805 | 0.843 | 100 | 1.332 | 1.430 |
| -76 | 0.782 | 0.838 | 104 | 1.422 | 1.535 |
| -72 | 0.797 | 0.855 | 108 | 1.510 | 1.627 |
| -68 | 0.865 | 0.924 | 112 | 1.581 | 1.659 |
| -64 | 0.984 | 1.053 | 116 | 1.604 | 1.704 |
| -60 | 1.110 | 1.173 | 120 | 1.653 | 1.717 |
| -56 | 1.212 | 1.280 | 124 | 1.650 | 1.763 |
| -52 | 1.287 | 1.369 | 128 | 1.693 | 1.777 |
| -48 | 1.383 | 1.409 | 132 | 1.714 | 1.816 |
| -44 | 1.439 | 1.496 | 136 | 1.752 | 1.864 |
| -40 | 1.508 | 1.578 | 140 | 1.825 | 1.898 |
| -36 | 1.574 | 1.586 | 144 | 1.847 | 1.961 |
| -32 | 1.549 | 1.646 | 148 | 1.900 | 2.033 |
| -28 | 1.625 | 1.666 | 152 | 1. 985 | 2.085 |
| -24 | 1.666 | 1.732 | 156 | 2.002 | 2.152 |
| -20 | 1.694 | 1.774 | 160 | 2.072 | 2.240 |
| -16 | 1.693 | 1.756 | 164 | 2.154 | 2.335 |
| -12 | 1.730 | 1.790 | 168 | 2.206 | 2.329 |
| -8 | 1.763 | 1.806 | 172 | 2.201 | 2.365 |
| -4 | 1.782 | 1.811 | 176 | 2.207 | 2.368 |
| 0 | 1.764 | 1.831 | 180 | 2.192 | 2.339 |

$T U=1.801 \%, L / D=0.038, \quad \mathrm{RE}=110000, \quad \mathrm{ST}=0.0$
(FIG 36) MULTIPLIER=0. 18572 MIL

LOSS CORRECTION=0.095 MILS

| DEG | $\begin{gathered} \mathrm{SH} / \sqrt{R E} \\ Z=-.5^{\prime \prime} \end{gathered}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ | DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=-. \mathrm{S}^{\prime \prime} \end{gathered}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -177 | 1.942 | 1.971 | 3 | 1.915 | 1.898 |
| -173 | 1.892 | 2.022 | 7 | 1.886 | 1.888 |
| -169 | 1.851 | 1.888 | 11 | 1.862 | 1.885 |
| -165 | 1.748 | 1.789 | 15 | 1.868 | 1.870 |
| -161 | 1.679 | 1.722 | 19 | 1.852 | 1.842 |
| -157 | 1.614 | 1.649 | 23 | 1.831 | 1.836 |
| -153 | 1.541 | 1.562 | 27 | 1.792 | 1.787 |
| -149 | 1.479 | 1.494 | 31 | 1.745 | 1.745 |
| -145 | 1.467 | 1.450 | 35 | 1.734 | 1.705 |
| -141 | 1.511 | 1.483 | 39 | 1.639 | 1.663 |
| -137 | 1.574 | 1.585 | 43 | 1.589 | 1.600 |
| -133 | 1.687 | 1.699 | 47 | 1.530 | 1.554 |
| -129 | 1.868 | 1.863 | 51 | 1.481 | 1.474 |
| -125 | 2.086 | 2.069 | 55 | 1.422 | 1.408 |
| -121 | 2.322 | 2.326 | 59 | 1.342 | 1.339 |
| -117 | 2.635 | 2.571 | 63 | 1.258 | 1.269 |
| -113 | 2.876 | 3.022 | 67 | 1.172 | 1.189 |
| -109 | 3.132 | 3.202 | 71 | 1.056 | 1.164 |
| -105 | 2.919 | 2.925 | 75 | 0.955 | 0.934 |
| -101 | 2.445 | 2.466 | 79 | 0.848 | 0.818 |
| -97 | 2.018 | 1.995 | 83 | 0.732 | 0.655 |
| -93 | 1.354 | 1.373 | 87 | 0.835 | 0.714 |
| -89 | 0.899 | 0.788 | 91 | 1.117 | 1.041 |
| -85 | 0.687 | 0.576 | 95 | 1.686 | 1.659 |
| -81 | 0.683 | 0.697 | 99 | 2.156 | 2.443 |
| -77 | 0.874 | 0.914 | 103 | 2.532 | 2.999 |
| -73 | 1.034 | 1.132 | 107 | 3.049 | 3.259 |
| -69 | 1.081 | 1.060 | 111 | 3.016 | 3.178 |
| -65 | 1.283 | 1.260 | 115 | 2.634 | 2.876 |
| -61 | 1.368 | 1.342 | 119 | 2.471 | 2.577 |
| -57 | 1.462 | 1.408 | 123 | 2.205 | 2. 290 |
| -53 | 1.491 | 1.456 | 127 | 1.970 | 2.005 |
| -49 | 1.545 | 1.522 | 131 | 1.824 | 1.879 |
| -45 | 1.600 | 1.577 | 135 | 1.680 | 1.687 |
| -41 | 1.649 | 1.595 | 139 | 1.573 | 1.561 |
| -37 | 1.744 | 1.661 | 143 | 1.533 | 1.509 |
| -33 | 1.790 | 1.728 | 147 | 1.567 | 1.520 |
| -29 | 1.773 | 1.754 | 151 | 1.608 | 1.526 |
| -25 | 1.802 | 1.795 | 155 | 1.655 | 1.600 |
| -21 | 1.833 | 1.796 | 159 | 1. 709 | 1.680 |
| -17 | 1.862 | 1.850 | 163 | 1.667 | 1.776 |
| -13 | 1.879 | 1.849 | 167 | 1.826 | 1.840 |
| -9 | 1.896 | 1.884 | 171 | 1.886 | 1.911 |
| -5 | 1.884 | 1.890 | 175 | 1.933 | 1.950 |
| -1 | 1.902 | 1.893 | 179 | 1.946 | 1.968 |

$\mathrm{TU}=1.801 \%, \mathrm{~L} / \mathrm{D}=0.038, \mathrm{RE}=110000, \mathrm{ST}=0.0639 \quad$ (EIG 41) MULTIPLIER=0.18564 /MIL

LOSS CORRECTION=0.092 MILS

| DEG | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=-.5^{\prime \prime} \end{aligned}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ | DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=-.5^{\prime \prime} \end{gathered}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -177 | 1.853 | 1.887 | 3 | 1.943 | 1.957 |
| -173 | 1.830 | 1.866 | 7 | 1.944 | 1.924 |
| -169 | 1.800 | 1.864 | 11 | 1.913 | 1.921 |
| -165 | 1.720 | 1.784 | 15 | 1.943 | 1.920 |
| -161 | 1.670 | 1.715 | 19 | 1.881 | 1.900 |
| -157 | 1.614 | 1.650 | 23 | 1.886 | 1.873 |
| -153 | 1.597 | 1.610 | 27 | 1.844 | 1.845 |
| -149 | 1.538 | 1.662 | 31 | 1.816 | 1.802 |
| -145 | 1.521 | 1.628 | 35 | 1.751 | 1.768 |
| -141 | 1.508 | 1.568 | 39 | 2.730 | 1.702 |
| -137 | 1.518 | 1.608 | 43 | 1.686 | 1.658 |
| -133 | 1.593 | 1.662 | 47 | 1.640 | 1.601 |
| -129 | 1.648 | 1.707 | 51 | 1.584 | 1.528 |
| -125 | 1.735 | 1.779 | 55 | 1.521 | 1.439 |
| -121 | 1.856 | 1.893 | 59 | 1.440 | 1.310 |
| -117 | 2.053 | 2.093 | 63 | 1.308 | 1.224 |
| -113 | 2.264 | 2. 321 | 67 | 1.163 | 1. 108 |
| -109 | 2.389 | 2.355 | 71 | 1.078 | 1.002 |
| -105 | 2.248 | 2.210 | 75 | 0.978 | 0.970 |
| -101 | 2.092 | 2.073 | 79 | 0.934 | 1.021 |
| -97 | 1.910 | 1.891 | 83 | 0.975 | 1.208 |
| -93 | 1.667 | 1.707 | 87 | 1.043 | 1.341 |
| -89 | 1.320 | 1.043 | 91 | 1.203 | 1.518 |
| -85 | 1.246 | 1.345 | 95 | 1.600 | 1.644 |
| -81 | 1.018 | 1.135 | 99 | 1.795 | 1.897 |
| -77 | 0.954 | 0.976 | 103 | 1.989 | 2.149 |
| -73 | 0.948 | 0.919 | 107 | 2.170 | 2.333 |
| -69 | 1.048 | 0.997 | 111 | 2.296 | 2.365 |
| -65 | 1.174 | 1.095 | 115 | 2.395 | 2.312 |
| -61 | 1.277 | 1.234 | 119 | 2.198 | 2.154 |
| -57 | 1.392 | 1.363 | 123 | 2.023 | 2.005 |
| -53 | 1.477 | 1.458 | 127 | 1.886 | 1.870 |
| -49 | 1.558 | 1.523 | 131 | 1.742 | 1.783 |
| -45 | 1.624 | 1.643 | 135 | 1.698 | 1.660 |
| -41 | 1.668 | 1.639 | 139 | 1.625 | 1.578 |
| -37 | 1.757 | 1.719 | 143 | 1.584 | 1.556 |
| -33 | 1.766 | 1.760 | 147 | 1.588 | 1.545 |
| -29 | 1.775 | 1.815 | 151 | 1.568 | 1.574 |
| -25 | 1.831 | 1.814 | 155 | 1.561 | 1.587 |
| -21 | 1.864 | 1.871 | 159 | 1.592 | 1.656 |
| -17 | 1.887 | 1.899 | 163 | 1.618 | 1.728 |
| -13 | 1.913 | 1.897 | 167 | 1.688 | 1.783 |
| -9 | 1.927 | 1.934 | 171 | 1.783 | 1.818 |
| -5 | 1.915 | 1.936 | 175 | 1.815 | 1.863 |
| -1 | 1.939 | 1.924 | 179. | 1.818 | 1.903 |

$T U=2.651 \%, L / D=0.030, \mathrm{RE}=50000, \mathrm{ST}=0.0$
MULTIPLIER=0.29838 /MIL
LOSS CORRECTION=0.060 MILS

| DEG | $\begin{gathered} \mathrm{SH} / \sqrt{\mathrm{RE}} \\ \mathrm{Z}=-.5^{n} \end{gathered}$ | $\begin{aligned} & \mathrm{SH} / \sqrt{\mathrm{RE}} \\ & \mathrm{Z}=+.5^{\prime \prime} \end{aligned}$ | DEG | $\begin{gathered} \mathrm{SH} / \sqrt{R E} \\ \mathrm{Z}=-.5^{\prime \prime} \end{gathered}$ | $\begin{gathered} \mathrm{SH} / \sqrt{R E} \\ \mathrm{Z}=+.5^{\prime \prime} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -176 | 2.036 | 2.004 | 4 | 1.908 | 1.801 |
| -172 | 1.983 | 1.944 | 8 | 1.917 | 1.756 |
| -168 | 1.925 | 1.885 | 12 | 1.901 | 1.751 |
| -164 | 1.790 | 1.809 | 16 | 1.876 | 1.734 |
| -160 | 1.709 | 1.731 | 20 | 1.880 | 1.703 |
| -156 | 1.652 | 1.690 | 24 | 1.828 | 1.696 |
| -152 | 1.595 | 1.645 | 28 | 1.840 | 1.672 |
| -148 | 1.530 | 1.582 | 32 | 1.839 | 1.682 |
| -144 | 1.513 | 1.501 | 36 | 1.735 | 1.630 |
| -140 | 1.425 | 1.467 | 40 | 1.693 | 1.580 |
| -136 | 1.408 | 1.447 | 44 | 1.657 | 1.509 |
| -132 | 1.441 | 1.447 | 48 | 1.565 | 1.437 |
| -128 | 1.439 | 1.458 | 52 | 1.537 | 1.417 |
| -124 | 1.438 | 1.444 | 56 | 1.492 | 1.352 |
| -120 | 1.440 | 1.439 | 60 | 1.397 | 1.267 |
| -116 | 1.427 | 1.447 | 64 | 1.324 | 1.165 |
| -112 | 1.404 | 1.458 | 68 | 1.225 | 1.040 |
| -108 | 1.406 | 1.474 | 72 | 1.094 | 0.911 |
| -104 | 1.382 | 1.471 | 76 | 0.890 | 0.694 |
| -100 | 1.298 | 1.384 | 80 | 0.612 | 0.468 |
| -96 | 1.161 | 1.223 | 84 | 0.488 | 0.473 |
| -92 | 0.943 | 0.972 | 88 | 0.646 | 0.702 |
| -88 | 0.708 | 0.692 | ' 92 | 0.918 | 1.001 |
| -84 | 0.516 | 0.492 | 96 | 1.142 | 1. 266 |
| -80 | 0.584 | 0.506 | 100 | 1.302 | 1.425 |
| -76 | 0.852 | 0.717 | 104 | 1.381 | 1.484 |
| -72 | 1.090 | 0.910 | 108 | 1.419 | 1.472 |
| -68 | 1.242 | 1.061 | 112 | 1.419 | 1.467 |
| -64 | 1.324 | 1.176 | 116 | 1.427 | 1.431 |
| - 60 | 1.405 | 1.242 | 120 | 1.426 | 1.456 |
| -56 | 1.492 | 1.318 | 124 | 1.428 | 1.469 |
| -52 | 1.528 | 1.384 | 128 | 1.453 | 1.459 |
| -48 | 1.592 | 1.463 | 132 | 1.437 | 1.439 |
| -44 | 1.636 | 1.497 | 136 | 1.404 | 1.428 |
| -40 | 1.672 | 1.556 | 140 | 1.408 | 1.459 |
| -36 | 1.697 | 1.594 | 144 | 1.456 | 1.507 |
| -32 | 1.759 | 1.613 | 148 | 1.539 | 1.558 |
| -28 | 1.780 | 1.628 | 152 | 1.585 | 1.625 |
| -24 | 1.845 | 1.738 | 156 | 1.664 | 1.687 |
| -20 | 1.907 | 1.713 | 160 | 1.714 | 1.753 |
| -16 | 1.889 | 1.793 | 164 | 1.764 | 1.820 |
| -12 | 1.895 | 1.802 | 168 | 1.883 | 1.906 |
| -8 | 1.895 | 1.778 | 172 | 1.939 | 1.994 |
| -4 | 1.880 | 1.775 | 176 | 2.028 | 2.048 |
| 0 | 1.928 | 1.825 | -180 | 2.029 | 2.005 |

```
TU=2.651%, L/D=0.030, RE= 50000, ST=0.1406 (FIG 51)
MULTIPLIER=0.27880 /MIL
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\mathrm{SH} / \sqrt{\mathrm{RE}}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
7=+51
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\)
\(\mathrm{Z}=+.5^{\prime \prime}\) \\
\hline & & & & \(2=-5^{\prime \prime}\) & \(2=+.5^{\prime \prime}\) \\
\hline -177 & 2.096 & 2.008 & 3 & 1.932 & 1.782 \\
\hline -173 & 2.056 & 1.933 & 7 & 1.949 & 1.785 \\
\hline -169 & 2.047 & 1.929 & 11 & 1.910 & 1.789 \\
\hline -165 & 1.927 & 1.873 & 15 & 1.922 & 1.736 \\
\hline -161 & 1.943 & 1.804 & 19 & 1.865 & 1.725 \\
\hline -157 & 1.837 & 1.771 & 23 & 1.859 & 1.759 \\
\hline -153 & 1.789 & 1.660 & 27 & 1.829 & 1.706 \\
\hline -149 & 1.689 & 1.599 & 31 & 1.787 & 1.780 \\
\hline -145 & 1.684 & 1.550 & 35 & 1.753 & 1.679 \\
\hline -141 & 1.606 & 1.572 & 39 & 1.709 & 1.609 \\
\hline -137 & 1.552 & 1.481 & 43 & 1.659 & 1.546 \\
\hline -133 & 1.530 & 1.470 & 47 & 1.604 & 1.485 \\
\hline -129 & 1.585 & 1.446 & 51 & 1.602 & 1.410 \\
\hline -125 & 1.528 & 1.466 & 55 & 1.503 & 1.377 \\
\hline -121 & 1.559 & 1.464 & 59 & 1.430 & 1.273 \\
\hline -117 & 1.481 & 1.496 & 63 & 1.378 & 1.215 \\
\hline -113 & 1.561 & 1.481 & 67 & 1.233 & 1.036 \\
\hline -109 & 1.443 & 1.456 & 71 & 1.103 & 0.960 \\
\hline -105 & 1.533 & 1.395 & 75 & 1.003 & 0.778 \\
\hline -101 & 1.374 & 1.302 & 79 & 0.954 & 0.872 \\
\hline -97 & 1.268 & 1.194 & 83 & 0.940 & 0.889 \\
\hline -93 & 1.121 & 1.037 & 87 & 0.924 & 0.947 \\
\hline -89 & 1.020 & 0.943 & 91 & 0.962 & 1.006 \\
\hline -85 & 0.939 & 0.860 & 95 & 1.050 & 1.121 \\
\hline -81 & 0.961 & 0.848 & 99 & 1.199 & 1.243 \\
\hline -77 & 0.943 & 0.797 & 103 & 1.290 & 1.434 \\
\hline -73 & 1.013 & 0.808 & 107 & 1.384 & 1.476 \\
\hline -69 & 1.117 & 0.946 & 111 & 1.427 & 1.473 \\
\hline -65 & 1.314 & 1.097 & 115 & 1.446 & 1.537 \\
\hline -61 & 1.332 & 1.221 & 119 & 1.487 & 1.546 \\
\hline -57 & 1.428 & 1.329 & 123 & 1.581 & 1.503 \\
\hline -53 & 1.486 & 1.393 & 127 & 1.462 & 1.546 \\
\hline -49 & 1.545 & 1.453 & 131 & 1.465 & 1.512 \\
\hline -45 & 1.548 & 1.499 & 135 & 1.580 & 1.498 \\
\hline -41 & 1.651 & 1.539 & 139 & 1.518 & 1.596 \\
\hline -37 & 1.680 & 1.649 & 143 & 1.535 & 1.638 \\
\hline -33 & 1.726 & 1.575 & 147 & 1.630 & 1.571 \\
\hline -29 & 1.748 & 1.695 & 151 & 1.640 & 1.625 \\
\hline -25 & 1.803 & 1.681 & 155 & 1.726 & 1.689. \\
\hline -21 & 1.789 & 1.750 & 159 & 1.867 & 1.844 \\
\hline -17 & 1.857 & 1.735 & 163 & 1.912 & 1.817 \\
\hline -13 & 1.849 & 1.830 & 167 & 1.982 & 1.857 \\
\hline -9 & 1.888 & 1.779 & 171 & 2.064 & 1.928 \\
\hline -5 & 1.933 & 1.783 & 175 & 2.173 & 2.015 \\
\hline -1 & 1.917 & 1.775 & 179 & 2.089 & 2.004 \\
\hline
\end{tabular}
\(\mathrm{TU}=2.651 \%, \mathrm{~L} / \mathrm{D}=0.030, \mathrm{RE}=75000, \mathrm{ST}=0.0\) (RUN 1, FIG 37) MULTIPLIER=0.19694 /MIL LOSS CORRECTION=0.295 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& \mathrm{Z}=+.5^{\prime \prime}
\end{aligned}
\] \\
\hline -176 & 1.847 & 1.993 & 4 & 1.958 & 2.028 \\
\hline -172 & 1.819 & 1.958 & 8 & 1.944 & 1.930 \\
\hline -168 & 1.745 & 1.875 & 12 & 1.918 & 1.952 \\
\hline -164 & 1.682 & 1.786 & 16 & 1.941 & 1.940 \\
\hline -160 & 1.605 & 1.690 & 20 & 1.923 & 1.962 \\
\hline -156 & 1.497 & 1.601 & 24 & 1.906 & 1.925 \\
\hline -152 & 1.434 & 1.512 & 28 & 1.883 & 1.902 \\
\hline -148 & 1.398 & 1.490 & 32 & 1.834 & 1.839 \\
\hline -144 & 1.358 & 1.438 & 36 & 1.784 & 1.809 \\
\hline -140 & 1.324 & 1.398 & 40 & 1.759 & 1.776 \\
\hline -136 & 1.322 & 1.374 & 44 & 1.707 & 1.724 \\
\hline -132 & 1.348 & 1.427 & 48 & 1.664 & 1.643 \\
\hline -128 & 1.396 & 1.420 & 52 & 1.582 & 1.567 \\
\hline -124 & 1.486 & 1.540 & 56 & 1.515 & 1.475 \\
\hline -120 & 1.583 & 1.607 & 60 & 1.448 & 1.428 \\
\hline -116 & 1.673 & 1.792 & 64 & 1.333 & 1.320 \\
\hline -112 & 1.875 & 1.899 & 68 & 1.282 & 1.216 \\
\hline -108 & 2.041 & 2.107 & 72 & 1.233 & 1.079 \\
\hline -104 & 2.219 & 2.230 & 76 & 0.947 & 0.871 \\
\hline -100 & 2.176 & 2.239 & 80 & 0.667 & 0.592 \\
\hline -96 & 1.871 & 1.964 & 84 & 0.436 & 0.421 \\
\hline -92 & 1.307 & 1.427 & 88 & 0.631 & 0.663 \\
\hline -88 & 0.792 & 0.855 & 92 & 1.145 & 1.207 \\
\hline -84 & 0.482 & 0.476 & 96 & 1.725 & 1.791 \\
\hline -80 & 0.615 & 0.504 & 100 & 2.114 & 2.209 \\
\hline -76 & 0.902 & 0.788 & 104 & 2.176 & 2.269 \\
\hline -72 & 1.108 & 1.132 & 108 & 2.093 & 2.130 \\
\hline -68 & 1.261 & 1.118 & 112 & 1.934 & 1.962 \\
\hline -64 & 1.390 & 1.236 & 116 & 1.720 & 1.786 \\
\hline -60 & 1.489 & 1.333 & 120 & 1.602 & 1.681 \\
\hline -56 & 1.527 & 1.411 & 124 & 1.478 & 1.557 \\
\hline -52 & 1.623 & 1.445 & 128 & 1.413 & 1.466 \\
\hline -48 & 1.697 & 1.536 & 132 & 1.344 & 1.412 \\
\hline -44 & 1.756 & 1.591 & 136 & 1.300 & 1.369 \\
\hline -40 & 1.807 & 1.648 & 140 & 1.326 & 1.361 \\
\hline -36 & 1.841 & 1.692 & 144 & 1.369 & 1.387 \\
\hline -32 & 1.878 & 1.722 & 148 & 1.399 & 1.445 \\
\hline -28 & 1.903 & 1.783 & 152 & 1.468 & 1.513 \\
\hline -24 & 1.927 & 1.823 & 156 & 1.524 & 1.584 \\
\hline -20 & 1.941 & 1.830 & 160 & 1.616 & 1.675 \\
\hline -16 & 1.951 & 1.880 & 164 & 1.657 & 1.737 \\
\hline -12 & 1.962 & 1.903 & 168 & 1.750 & 1.852 \\
\hline -8 & 1.942 & 1.916 & 172 & 1.841 & 1.952 \\
\hline -4 & 1.995 & 1.916 & 176 & 1.850 & 1.992 \\
\hline 0 & 1.964 & 1.939 & 180 & 1.864 & 1.973 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=75000, \mathrm{ST}=0.0 \quad\) (RUN 2) MULTIPLIER=0. 19726 /MIL

LOSS CORRECTION=0.030 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
2=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
z=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& Z=+.5^{\prime \prime}
\end{aligned}
\] \\
\hline -176 & 1.743 & 1.977 & 4 & 1.980 & 1.955 \\
\hline -172 & 1.699 & 1.912 & 8 & 1.963 & 1.960 \\
\hline -168 & 1.634 & 1.834 & 12 & 1.940 & 1.957 \\
\hline -164 & 1.586 & 1.737 & 16 & 1.924 & 1.941 \\
\hline -160 & 1.482 & 1.652 & 20 & 1.899 & 1.926 \\
\hline -156 & 1.407 & 1.525 & 24 & 1.906 & 1.908 \\
\hline -152 & 1.337 & 1.495 & 28 & 1.825 & 1.871 \\
\hline -148 & 1.265 & 1.375 & 32 & 1.781 & 1.831 \\
\hline -144 & 1.235 & 1.308 & 36 & 1.744 & 1.778 \\
\hline -140 & 1.213 & 1.282 & 40 & 1.681 & 1.766 \\
\hline -136 & 1.186 & 1.260 & 44 & 1.695 & 1.692 \\
\hline -132 & 1.235 & 1.291 & 48 & 1.560 & 1.651 \\
\hline -128 & 1.304 & 1.341 & 52 & 1.481 & 1.593 \\
\hline -124 & 1.379 & 1.431 & 56 & 1.390 & 1.485 \\
\hline -120 & 1.445 & 1.536 & 60 & 1.303 & 1.415 \\
\hline -116 & 1.613 & 1.616 & 64 & 1.240 & 1.321 \\
\hline -112 & 1.776 & 1.812 & 68 & 1.180 & 1.209 \\
\hline -108 & 1.984 & 1.984 & 72 & 1.078 & 1.076 \\
\hline -104 & 2.145 & 2.150 & 76 & 0.898 & 0.880 \\
\hline -100 & 2.112 & 2.177 & 80 & 0.605 & 0.621 \\
\hline -96 & 1.859 & 1.923 & 84 & 0.370 & 0.457 \\
\hline -92 & 1.318 & 1.411 & 88 & 0.530 & 0.694 \\
\hline -88 & 0.792 & 0.825 & 92 & 0.999 & 1.243 \\
\hline -84 & 0.499 & 0.448 & 96 & 1.521 & 1.796 \\
\hline -80 & 0.613 & 0.446 & 100 & 1.966 & 2.191 \\
\hline -76 & 0.936 & 0.702 & 104 & 2.106 & 2.267 \\
\hline -72 & 1.140 & 0.939 & 108 & 1.971 & 2.128 \\
\hline -68 & 1.297 & 1.073 & 112 & 1.778 & 1.953 \\
\hline -64 & 1.392 & 1.203 & 116 & 1.612 & 1.798 \\
\hline -60 & 1.451 & 1.292 & 120 & 1.478 & 1.658 \\
\hline -56 & 1.517 & 1.384 & 124 & 1.370 & 1.574 \\
\hline -52 & 1.576 & 1.437 & 128 & 1.299 & 1.466 \\
\hline -48 & 1.622 & 1.516 & 132 & 1.228 & 1.416 \\
\hline -44 & 1.664 & 1.565 & 136 & 1.178 & 1.373 \\
\hline -40 & 1.712 & 1.614 & 140 & 1.186 & 1.379 \\
\hline -36 & 1.759 & 1.661 & 144 & 1.200 & 1.378 \\
\hline -32 & 1.789 & 1.672 & 148 & 1.242 & 1.445 \\
\hline -28 & 1.836 & 1.758 & 152 & 1.311 & 1.502 \\
\hline -24 & 1.868 & 1.787 & 156 & 1.364 & 1.578 \\
\hline -20 & 1.904 & 1.838 & 160 & 1.464 & 1.656 \\
\hline -16 & 1.923 & 1.857 & 164 & 1.548 & 1.757 \\
\hline -12 & 1.952 & 1.903 & 168 & 1.592 & 1.789 \\
\hline -8 & 1.966 & 1.918 & 172 & 1.678 & 1.832 \\
\hline -4 & 1.970 & 1.947 & 176 & 1.721 & 1.919 \\
\hline 0 & 1.975 & 1.946 & -180 & 1.745 & 1.986 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=75000, \mathrm{ST}=0.0417\)
(EIG 49)
MULTIPLIER=0.20291 /MIL
LOSS CORRECTION=0.030 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/ RE & SH/ \(\sqrt{R E}\) & DEG & \(S H / \sqrt{R E}\) & \(\mathrm{SH} / \sqrt{\text { RE }}\) \\
\hline & \(\mathrm{Z}=-.5^{\prime \prime}\) & \(Z=+.5^{\prime \prime}\) & & Z \(=-.5^{\prime \prime}\) & \(2=+.51\) \\
\hline -176 & 1.957 & 1.914 & 4 & 2.108 & 2.131 \\
\hline -172 & 1.918 & 1.914 & 8 & 2.105 & 2.093 \\
\hline -168 & 1.880 & 1.838 & 1:2 & 2.086 & 2.083 \\
\hline -164 & 1.805 & 1.774 & 16 & 2.071 & 1.987 \\
\hline -160 & 1.710 & 1.704 & 20 & 2.053 & 2.034 \\
\hline -156 & 1.607 & 1.623 & 24 & 2.006 & 2.011 \\
\hline -152 & 1.551 & 1.569 & 28 & 1.981 & 1.988 \\
\hline -148 & 1.504 & 1.485 & 32 & 1.937 & 2.004 \\
\hline -144 & 1.449 & 1.449 & 36 & 1.912 & 1.932 \\
\hline -140 & 1.434 & 1.444 & 40 & 1.848 & 1.870 \\
\hline -136 & 1.442 & 1.441 & 44 & 1.797 & 1.809 \\
\hline -132 & 1.485 & 1.460 & 48 & 1.752 & 1.734 \\
\hline -128 & 1.551 & 1.538 & 52 & 1.662 & 1.690 \\
\hline -124 & 1.659 & 1.625 & 56 & 1.576 & 1.608 \\
\hline -120 & 1.782 & 1.746 & 60 & 1.417 & 1.495 \\
\hline -116 & 1.887 & 1.887 & 64 & 1.241 & 1.387 \\
\hline -112 & 1.900 & 1.965 & 68 & 1.130 & 1.232 \\
\hline -108 & 1.921 & 1.987 & 72 & 1.012 & 1.094 \\
\hline -104 & 1.907 & 1.871 & 76 & 0.962 & 0:994 \\
\hline -100 & 1.705 & 1.665 & 80 & 0.936 & 0.915 \\
\hline -96 & 1.465 & 1.505 & 84 & 1.016 & 1.050 \\
\hline -92 & 1.194 & 1.309 & 88 & 1.185 & 1.231 \\
\hline -88 & 0.990 & 1.145 & 92 & 1.259 & 1.359 \\
\hline -84 & 0.889 & 0.952 & 96 & 1.564 & 1.540 \\
\hline -80 & 0.861 & 0.910 & 100 & 1.734 & 1.715 \\
\hline -76 & 1.085 & 0.863 & 104 & 1.859 & 1.860 \\
\hline -72 & 1.135 & 1.019 & 108 & 0.0 & 0.0 \\
\hline -68 & 1.244 & 1.201 & 112 & 1.904 & 1.948 \\
\hline -64 & 1.408 & 1.365 & 116. & 1.885 & 1.851 \\
\hline -60 & 1.506 & 1.470 & 120 & 1.798 & 1.755 \\
\hline -56 & 1.562 & 1.549 & 124 & 1.682 & 1.645 \\
\hline -52 & 1.649 & 1.721 & 128 & 1.603 & 1.534 \\
\hline -48 & 1.701 & 1.650 & 132 & 1.583 & 1.465 \\
\hline -44 & 1.722 & 1.732 & 136 & 1.493 & 1.442 \\
\hline -40 & 1.759 & 1.811 & 140 & 1.464 & 1.457 \\
\hline -36 & 1.790 & 1.861 & 144 & 1.457 & 1.451 \\
\hline -32 & 1.856 & 1.894 & 148 & 1.510 & 1.469 \\
\hline -28 & 1.904 & 1.949 & 152 & 1.571 & 1.567 \\
\hline -24 & 1.956 & 2.016 & 156 & 1.645 & 1.624 \\
\hline -20 & 2.009 & 2.030 & 160 & 1.709 & 1.706 \\
\hline -16 & 2.045 & 2.052 & 164 & 1.781 & 1.798 \\
\hline -12 & 2.082 & 2.057 & 168 & 1.881 & 1.853 \\
\hline -8 & 2.103 & 2.059 & 172 & 1.837 & 1.920 \\
\hline -4 & 2.086 & 2.106 & 176 & 1.979 & 1.946 \\
\hline 0 & 2.112 & 2.106 & -180 & 1.983 & 1.933 \\
\hline
\end{tabular}
\(\mathrm{TU}=2.651 \%, \mathrm{~L} / \mathrm{D}=0.030, \mathrm{RE}=75000, \mathrm{ST}=0.1041 \quad\) (EIG 50)
MULTIPLIER \(=0.20290 / \mathrm{MIL} \quad\) LOSS CORRECTION=0.030 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/ \(/ \sqrt{R E}\) & SH/ \(\sqrt{\text { RE }}\) & DEG & SH/ \(/ \sqrt{\text { RE }}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) \\
\hline & \(2=-5^{\prime \prime}\) & \(2=+.5^{\prime \prime}\) & & \(2=-.5^{\prime \prime}\) & \(2=+.5^{\prime \prime}\) \\
\hline -178 & 1.926 & 1.940 & 2 & 1.970 & 1.959 \\
\hline -174 & 1.918 & 1.917 & 6 & 1.961 & 1.977 \\
\hline -170 & 1.896 & 1.885 & 10 & 1.949 & 1.974 \\
\hline -166 & 1.813 & 1.852 & 14 & 1.958 & 1.963 \\
\hline -162 & 1.745 & 1.761 & 18 & 1.950 & 1.957 \\
\hline -158 & 1.666 & 1.684 & 22 & 1.928 & 1.938 \\
\hline -154 & 1.612 & 1.622 & 26 & 1.911 & 1.909 \\
\hline -150 & 1.532 & 1.574 & 30 & 1.893 & 1.888 \\
\hline -156 & 1.479 & 1.497 & 34 & 1.841 & 1.828 \\
\hline -152 & 1.446 & 1.458 & 38 & 1.799 & 1.807 \\
\hline -138 & 1. 440 & 1.454 & 42 & 1.724 & 1.771 \\
\hline -134 & 1.481 & 1.452 & 46 & 1.681 & 1.700 \\
\hline -130 & 1.572 & 1.518 & 50 & 1.607 & 1.631 \\
\hline -126 & 1.645 & 1.537 & 54 & 1.608 & 1.539 \\
\hline -122 & 1.735 & 1.628 & 58 & 1.443 & 1.526 \\
\hline -118 & 1.866 & 1.732 & 62 & 1.294 & 1.401 \\
\hline -114 & 1.931 & 1.881 & 66 & 1.184 & 1.297 \\
\hline -110 & 1.927 & 1.935 & 70 & 1.067 & 1.152 \\
\hline -106 & 1.880 & 1.928 & 74 & 0.962 & 0.988 \\
\hline -102 & 1.746 & 1.763 & 78 & 0.940 & 0.922 \\
\hline -98 & 1.700 & 1.653 & 82 & 1.086 & 0.993 \\
\hline -94 & 1.451 & 1.491 & 86 & 1.189 & 1.114 \\
\hline -90 & 1.243 & 1.352 & 90 & 1.376 & 1.279 \\
\hline -86 & 1.080 & 1.220 & 94 & 1.517 & 1.386 \\
\hline -82 & 0.947 & 1.050 & 98 & 1.646 & 1.513 \\
\hline -78 & 0.924 & 0.880 & 102 & 1.762 & 1.710 \\
\hline -74 & 0.979 & 0.883 & 106 & 1.870 & 1.878 \\
\hline -70 & 1.062 & 0.946 & 110 & 1.927 & 1.954 \\
\hline -66 & 1.176 & 1.145 & 114 & 1.925 & 1.951 \\
\hline -62 & 1.306 & 1.279 & 118 & 1.824 & 1.893 \\
\hline -58 & 1.388 & 1.376 & 122 & 1.673 & 1.788 \\
\hline -54 & 1.464 & 1.449 & 126 & 1.616 & 1.653 \\
\hline -50 & 1.544 & 1.532 & 130 & 1.572 & 1.567. \\
\hline -46 & 1.614 & 1.616 & 134 & 1.506 & 1.514 \\
\hline -42 & 1.673 & 1.672 & 138 & 1.500 & 1.493 \\
\hline -38 & 1.754 & 1.848 & 142 & 1.509 & 1.483 \\
\hline -34 & 1.800 & 1.743 & 146 & 1.533 & 1.475 \\
\hline -30 & 1.853 & 1.810 & 150 & 1.568 & 1.533 \\
\hline -26 & 1.873 & 1.839 & 154 & 1.626 & 1.593 \\
\hline -22 & 1.905 & 1.881 & 158 & 1.683 & 1.651 \\
\hline -18 & 1.911 & 1.917 & 162 & 1.715 & 1.721 \\
\hline -14 & 1.923 & 1.935 & 166 & 1.761 & 1.784 \\
\hline -10 & 1.951 & 1.965 & 170 & 1.818 & 1.832 \\
\hline -6 & 1.962 & 1.960 & 174 & 1.898 & 1.903 \\
\hline -2 & 1.971 & 1.964 & 178 & 1.916 & 1.937 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0 \quad\) (RUN 1, EIG 38) MULTIPLIER=0.19374 /MIL

LOSS CORRECTION=0.056 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
S H / \sqrt{R E} \\
Z=+.5^{\prime \prime}
\end{gathered}
\] & 'DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& \mathrm{Z}=+.51
\end{aligned}
\] \\
\hline -178 & 1.960 & 1.957 & 2 & 2.062 & 2.091 \\
\hline -174 & 1.929 & 1.906 & 6 & 2.071 & 2.106 \\
\hline -170 & 1.868 & 1.853 & 10 & 2.077 & 2.079 \\
\hline -166 & 1.771 & 1.745 & 14 & 2.065 & 2.099 \\
\hline -162 & 1.674 & 1.602 & 18 & 2.039 & 2.074 \\
\hline -158 & 1.555 & 1.492 & 22 & 2.026 & 2.038 \\
\hline -154 & 1.424 & 1.368 & 28 & 1.994 & 1.970 \\
\hline -150 & 1.318 & 1.293 & 32 & 1.962 & 1.926 \\
\hline -146 & 1.259 & 1.221 & 36 & 1.914 & 1.898 \\
\hline -142 & 1.220 & 1.252 & 40 & 1.903 & 1.904 \\
\hline -138 & 1.314 & 1.339 & 44 & 1.846 & 1.803 \\
\hline -134 & 1.418 & 1.500 & 46 & 1.789 & 1.765 \\
\hline -130 & 1.676 & 1.689 & 50 & 1.734 & 1.691 \\
\hline -126 & 1.918 & 1.979 & 54 & 1.710 & 1.611 \\
\hline -122 & 2.213 & 2.273 & 58. & 1.635 & 1.548 \\
\hline -118 & 2.595 & 2.706 & 62 & 1.541 & 1.456 \\
\hline -114 & 3.056 & 3.134 & 66 & 1.488 & 1.379 \\
\hline -110 & 3.526 & 3.584 & 70 & 1.351 & 1.268 \\
\hline -106 & 3.880 & 3.739 & 74 & 1.278 & 1.163 \\
\hline -102 & 3.328 & 2.963 & 78 & 1.157 & 0.999 \\
\hline -98 & 2.117 & 1.671 & 82 & 0.942 & 0.794 \\
\hline -94 & 0.966 & 0.671 & 86 & 0.652 & 0.515 \\
\hline -90 & 0.471 & 0.436 & 90 & 0.471 & 0.521 \\
\hline -86 & 0.630 & 0.670 & 94 & 0.891 & 1.298 \\
\hline -82 & 0.925 & 0.950 & 98 & 1.954 & 2.572 \\
\hline -78 & 1.122 & 1.121 & 102 & 3.244 & 3.201 \\
\hline -74 & 1.283 & 1.256 & 106 & 0.0 & 0.0 \\
\hline -70 & 1.359 & 1.363 & 110 & 0.0 & 0.0 \\
\hline -66 & 1.466 & 1.461 & 114 & 3.148 & 2.876 \\
\hline -62 & 1.542 & 1.548 & 118 & 2.679 & 2.468 \\
\hline -58 & 1.610 & 1.576 & 122 & 2.306 & 2.099 \\
\hline -54 & 1.694 & 1.672 & 126 & 1.978 & 1.817 \\
\hline -50 & 1.736 & 1.732 & 130 & 1.725 & 1.576 \\
\hline -46 & 1.775 & 1.784 & 134 & 1.512 & 1.423 \\
\hline -42 & 1.832 & 1.835 & 138 & 1.353 & 1.299 \\
\hline -38 & 1.878 & 1.900 & 142 & 1.282 & 1.250 \\
\hline -34 & 1.913 & 1.932 & 146 & 1.274 & 1.254 \\
\hline -30 & 1.960 & 1.957 & 150 & 1.296 & 1.341 \\
\hline -26 & 1.954 & 2.013 & 154 & 1.376 & 1.473 \\
\hline -22 & 2.040 & 2.011 & 158 & 1.498 & 1.575 \\
\hline -18 & 2.035 & 2.085 & 162 & 1.638 & 1.685 \\
\hline -14 & 2.068 & 2.115 & 166 & 1.747 & 1.792 \\
\hline -10 & 2.073 & 2.094 & 170 & 1.849 & 1.859 \\
\hline -6 & 2.082 & 2.106 & 174 & 1.926 & 1.925 \\
\hline -2 & 2.079 & 2.123 & 178 & 1.938 & 1.948 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, ~ R E=110000, S T=0.0 \quad\) (RUN 2) MULTIPLIER \(=0.20601 / \mathrm{MIL}\) LOSS CORRECTION=0.076 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/ \(\sqrt{\text { RE }}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & DEG & SH/ \(\sqrt{\text { RE }}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) \\
\hline & \(Z=-.5 \prime\) & \(Z=+.5^{\prime \prime}\) & & \(Z=-.51\) & Z=+.5" \\
\hline -178 & 2.026 & 2.087 & 2 & 2.127 & 2.114 \\
\hline -174 & 2.011 & 2.017 & 6 & 2.082 & 2.099 \\
\hline -170 & 1.925 & 1.913 & 10 & 2.099 & 2.091 \\
\hline -166 & 1.821 & 1.811 & 14 & 2.055 & 2.079 \\
\hline -162 & 1.704 & 1.681 & 18 & 2.052 & 2.057 \\
\hline -158 & 1.588 & 1.570 & 22 & 2.045 & 2.022 \\
\hline -154 & 1.487 & 1.479 & 26 & 2.007 & 1.998 \\
\hline -150 & 1.363 & 1.405 & 30 & 1.964 & 1.981 \\
\hline -146 & 1.344 & 1.377 & 34 & 1.979 & 1.935 \\
\hline -142 & 1.384 & 1.404 & 38 & 1.914 & 1.893 \\
\hline -138 & 1.479 & 1.473 & 42 & 1.855 & 1.842 \\
\hline -134 & 1.647 & 1.649 & 46 & 1.827 & 1.779 \\
\hline -130 & 1.840 & 1.840 & 50 & 1.791 & 1.715 \\
\hline -126 & 2.111 & 2.103 & 54 & 1.720 & 1.650 \\
\hline -122 & 2.436 & 2.391 & 58 & 1.644 & 1.473 \\
\hline -118 & 2.811 & 2.790 & 62 & 1.587 & 1.498 \\
\hline -114. & 3.266 & 3.242 & 66 & 1.506 & 1.405 \\
\hline -110 & 3.455 & 3.483 & 70 & 1.390 & 1.314 \\
\hline -106 & 3.445 & 3.481 & 74 & 1.261 & 1.203 \\
\hline -102 & 2.751 & 3.119 & 78 & 1.073 & 1.036 \\
\hline -98 & 1.511 & 1.953 & 82 & 0.818 & 0.762 \\
\hline -94 & 0.631 & 0.921 & 86 & 0.550 & 0.492 \\
\hline -90 & 0.400 & 0.492 & 90 & 0.885 & 0.760 \\
\hline -86 & 0.709 & 0.742 & 94 & 1.887 & 1.731 \\
\hline -82 & 0.987 & 1.076 & 98 & 3.201 & 3.015 \\
\hline -78 & 1.166 & 1.237 & 102 & 3.752 & 3.634 \\
\hline -74 & 1.254 & 1.378 & 106 & 3.762 & 3.655 \\
\hline -70 & 1.362 & 1.480 & 110 & 3.384 & 3.336 \\
\hline -66 & 1.454 & 1.520 & 114 & 2.961 & 2.899 \\
\hline -62 & 1.526 & 1.573 & 118 & 2.579 & 2.517 \\
\hline -58 & 1.609 & 1.632 & 122 & 2.210 & 2.166 \\
\hline -54 & 1.646 & 1.681 & 126 & 1.932 & 1.877 \\
\hline -50 & 1.715 & 1.764 & 130 & 1.753 & 1.634 \\
\hline -46 & 1.764 & 1.801 & 134 & 1.584 & 1.460 \\
\hline -42 & 1.812 & 1.888 & 138 & 1.475 & 1.383 \\
\hline -38 & 1.845 & 1.925 & 142 & 1.450 & 1.348 \\
\hline -34 & 1.914 & 1.966 & 146 & 1.467 & 1.373 \\
\hline -30 & 1.954 & 1.986 & 150 & 1.534 & 1.419 \\
\hline -26 & 1.990 & 2.008 & 154 & 1.646 & 1.549 \\
\hline -22 & 2.021 & 2.030 & 158 & 1.742 & 1.677 \\
\hline -18 & 2.045 & 2.068 & 162 & 1.867 & 1.830 \\
\hline -14 & 2.075 & 2.087 & 166 & 1.932 & 1.934 \\
\hline -10 & 2.110 & 2.097 & 170 & 2.012 & 2.028 \\
\hline -6 & 2.091 & 2.098 & 174 & 2.049 & 2.015 \\
\hline -2 & 2.103 & 2.113 & 178 & 2.064 & 2.011 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \operatorname{RE}=110000, S T=0.0071\) (RUN 1, FIG 43) MULTIPLIER=0.20525 /MIL

LOSS CORRECTION=0.004 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH//RE & SH/ \(/\) RE & DEG & \(\mathrm{SH} / \widetilde{\mathrm{RE}}\) & SH/ \(/\) RE \\
\hline & Z=-.5" & Z=+.5" & & Z=-.5" & \(\mathrm{Z}=+.5^{\prime \prime}\) \\
\hline -176 & 1.930 & 1.880 & 4 & 2.131 & 2.154 \\
\hline -172 & 1.882 & 1.786 & 8 & 2.134 & 2.132 \\
\hline -168 & 1.790 & 1.789 & 12 & 2.123 & 2.082 \\
\hline -164 & 1.729 & 1.777 & 16 & 2.114 & 2.081 \\
\hline -160 & 1.621 & 1.714 & 20 & 2.099 & 2.067 \\
\hline -156 & 1.568 & 1.559 & 24 & 2.066 & 2.057 \\
\hline -152 & 1.463 & 1.490 & 28 & 1.957 & 1.989 \\
\hline -148 & 1.417 & 1.402 & 32 & 1.999 & 1.993 \\
\hline -144 & 1.398 & 1.420 & 36 & 1.949 & 1.952 \\
\hline -140 & 1.453 & 1.432 & 40 & 1.908 & 1.897 \\
\hline -136 & 1.582 & 1.511 & 44 & 1.875 & 1.849 \\
\hline -132 & 1.726 & 1.708 & 48 & 1.795 & 1.794 \\
\hline -128 & 1.954 & 1.952 & 52 & 1.763 & 1.719 \\
\hline -124 & 2.342 & 2.208 & 56 & 1.732 & 1.667 \\
\hline -120 & 2.712 & 2.620 & 60 & 1.661 & 1.589 \\
\hline -116 & 3.052 & 2.943 & 64 & 1.587 & 1.517 \\
\hline -112 & 3.023 & 3.080 & 68 & 1.490 & 1.408 \\
\hline -108 & 2.7 .40 & 2.882 & 72 & 1.404 & 1.291 \\
\hline -104 & 2.459 & 2.612 & 76 & 1.237 & 1.141 \\
\hline -100 & 2.225 & 2.344 & 80 & 1.089 & 0.998 \\
\hline -96 & 2.056 & 2.120 & 84 & 1.149 & 1.028 \\
\hline -92 & 1.736 & 1.887 & 88 & 1.382 & 1.240 \\
\hline -88 & 1.301 & 1.464 & 92 & 1.817 & 1.668 \\
\hline -84 & 1.031 & 1.130 & 96 & 2.188 & 2.031 \\
\hline -80 & 0.937 & 0.971 & 100 & 2.332 & 2.240 \\
\hline -76 & 1.151 & 1.086 & 104 & 2.589 & 2.439 \\
\hline -72 & 1.255 & 1.257 & 108 & 2.862 & 2.731 \\
\hline -68 & 1.365 & 1.397 & 112 & 3.138 & 3.012 \\
\hline -64 & 1.446 & 1.511 & 116 & 3.137 & 3.107 \\
\hline -60 & 1.533 & 1.580 & 120 & 2.938 & 2.849 \\
\hline -56 & 1.570 & 1.650 & 124 & 2.556 & 2.441 \\
\hline -52 & 1.653 & 1.729 & 128 & 2.215 & 2.063 \\
\hline -48 & 1. 7.49 & 1.792 & 132 & 1.938 & 1.796 \\
\hline -44 & 1.767 & 1.856 & 136 & 1.716 & 1.589 \\
\hline -40 & 1.889 & 1.902 & 140 & 1.590 & 1.462 \\
\hline -36 & 1.930 & 1.943 & 144 & 1.505 & 1.421 \\
\hline -32 & 1.973 & 1.982 & 148 & 1.486 & 1.419 \\
\hline -28 & 2.019 & 2.053 & 152 & 1.507 & 1.450 \\
\hline -24 & 2.043 & 2.062 & 156 & 1.600 & 1.494 \\
\hline -20 & 2.073 & 2.087 & 160 & 1.696 & 1.624 \\
\hline -16 & 2.091 & 2.107 & 164 & 1.748 & 1.690 \\
\hline -12 & 2.127 & 2.104 & 168 & 1.868 & 1.806 \\
\hline -8 & 2.144 & 2.121 & 172 & 1.932 & 1.849 \\
\hline -4 & 2.146 & 2.153 & 176 & 1.938 & 1.862 \\
\hline 0 & 2.154 & 2.150 & 180 & 1.938 & 1.906 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, ~ R E=110000, ~ S T=0.0071\) (RUN 2) MULTIPLIER=0.22151 /MIL

LOSS CORRECTION \(=0.068\) MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \(\mathrm{SH} / \sqrt{R E}\) & \(\mathrm{SH} / \sqrt{R E}\) & DEG & SH/ \({ }^{\text {RE }}\) & SH/ \(/ \sqrt{R E}\) \\
\hline & Z=-.5" & Z=+.5" & & \(\mathrm{Z}=-.5^{\prime \prime}\) & \(2=+.5^{\prime \prime}\) \\
\hline -178 & 1.898 & 1.928 & 2 & 2.210 & 2.275 \\
\hline -174 & 1.866 & 1.878 & 6 & 2.211 & 2.263 \\
\hline -170 & 1.832 & 1.839 & 10 & 2.204 & 2.263 \\
\hline -166 & 1.729 & 1.770 & 14 & 2.199 & 2.242 \\
\hline -162 & 1.634 & 1.675 & 18 & 2.097 & 2.228 \\
\hline -158 & 1.543 & 1.562 & 22 & 2.165 & 2.206 \\
\hline -154 & 1.465 & 1.458 & 26 & 2.116 & 2.152 \\
\hline -150 & 1.390 & 1.400 & 30 & 2.106 & 2.131 \\
\hline -146 & 1.394 & 1.381 & 34 & 2.060 & 2.090 \\
\hline -142 & 1.445 & 1.425 & 38 & 2.037 & 2.007 \\
\hline -138 & 1.550 & 1.530 & 42 & 1.993 & 1.953 \\
\hline -134 & 1.736 & 1.685 & 46 & 1.948 & 1.947 \\
\hline -130 & 2.005 & 1.928 & 50 & 1.866 & 1.898 \\
\hline -126 & 2.311 & 2.249 & 54 & 1.797 & 1.799 \\
\hline -122 & 2.702 & 2.596 & 58 & 1.735 & 1.775 \\
\hline -118 & 3.020 & 2.978 & 62 & 1.687 & 1.684 \\
\hline -114 & 3.015 & . 3.035 & 66 & 1.590 & 1.570 \\
\hline -110 & 2.746 & 2.828 & 70 & 1.436 & 1.451 \\
\hline -106 & 2.475 & 2.541 & 74 & 1.268 & 1.276 \\
\hline -102 & 2.278 & 2.342 & 78 & 1.107 & 1.094 \\
\hline -98 & 2.107 & 2.143 & 82 & 1.052 & 1.053 \\
\hline -94 & 1.747 & 1.849 & 86 & 1.268 & 1.240 \\
\hline -90 & 1.336 & 1.425 & 90 & 1.710 & 1.660 \\
\hline -86. & 1.067 & 1.101 & 94 & 2.052 & 2.078 \\
\hline -82 & 1.050 & 1.047 & 98 & 2.304 & 2.287 \\
\hline -78 & 1.225 & 1.169 & 102 & 2.489 & 2.490 \\
\hline -74 & 1.409 & 1.346 & 106 & 2.786 & 2.773 \\
\hline -70 & 1.516 & 1.484 & 110 & 3.084 & 3.082 \\
\hline -66 & 1.627 & 1.595 & 114 & 3.107 & 3.163 \\
\hline -62 & 1.697 & 1.667 & 118 & 2.872 & 2.873 \\
\hline -58 & 1.762 & 1.737 & 122 & 2.449 & 2.501 \\
\hline -54 & 1.869 & 1.822 & 126 & 2.069 & 2.112 \\
\hline -50 & 1.903 & 1.853 & 130 & 1.770 & 1.826 \\
\hline -46 & 1.935 & 1.953 & 134 & 1.589 & 1.624 \\
\hline -42 & 1.984 & 1.969 & 138 & 1.474 & 1.480 \\
\hline -38 & 2.046 & 2.032 & 142. & 1.407 & 1.414 \\
\hline -34 & 2.082 & 2.090 & 146 & 1.388 & 1.400 \\
\hline -30 & 2.122 & 2.105 & 150 & 1.413 & 1.435 \\
\hline -26 & 2.148 & 2.158 & 154 & 1.502 & 1.503 \\
\hline -22 & 2.165 & 2.180 & 158 & 1.600 & 1.604 \\
\hline -18 & 2.169 & 2.240 & 162 & 1.744 & 1.715 \\
\hline -14 & 2.207 & 2.269 & 166 & 1.817 & 1.774 \\
\hline -10 & 2.207 & 2.268 & 170 & 1.854 & 1.880 \\
\hline -6 & 2.199 & 2.270 & 174 & 1.900 & 1.933 \\
\hline -2 & 2.214 & 2.270 & 178 & 1.922 & 1.929 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0213\) (RUN 1, FIG 44) MULTIPLIER=0.20256 /MIL LOSS CORRECTION=0. 102 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
Z=+5^{\prime \prime}
\end{gathered}
\] \\
\hline -176 & \(2=-93\)
1.904 & 20+.5 & 4 & 2.194 & 2.183 \\
\hline -172 & 1.884 & 1.895 & 8 & 2.218 & 2.193 \\
\hline -168 & 1.825 & 1.842 & 12 & 2.206 & 2.177 \\
\hline -164 & 1.734 & 1.745 & 16 & 2.178 & 2.142 \\
\hline -160 & 1.652 & 1.659 & 20 & 2.122 & 2.133 \\
\hline -156 & 1.527 & 1.563 & 24 & 2.085 & 2.118 \\
\hline -152 & 1.447 & 1.487 & 28 & 2.087 & 2.020 \\
\hline -148 & 1.409 & 1.414 & 32 & 2.042 & 2.041 \\
\hline -144 & 1.411 & 1.402 & 36 & 1.982 & 2.001 \\
\hline -140 & 1.446 & 1.439 & 40 & 1.952 & 1.949 \\
\hline -136 & 1.563 & 1.549 & 44 & 1.917 & 1.881 \\
\hline -132 & 1.733 & 1.676 & 48 & 1.866 & 1.823 \\
\hline -128 & 1.976 & 1.888 & 52 & 1.777 & 1.766 \\
\hline -124 & 2.307 & 2.207 & 56 & 1.747 & 1.691 \\
\hline -120 & 2.686 & 2.537 & 60 & 1.671 & 1.633 \\
\hline -116 & 3.010 & 2.904 & 64 & 1.568 & 1.568 \\
\hline -112 & 3.018 & 2.998 & 68 & 1.464 & 1.459 \\
\hline -108 & 2.767 & 2.792 & 72 & 1.466 & 1.342 \\
\hline -104 & 2.457 & 2.497 & 76 & 1.195 & 1.183 \\
\hline -100 & 2.265 & 2.255 & 80 & 1.049 & 1.040 \\
\hline -96 & 2.095 & 2.056 & 84 & 1.080 & 1.051 \\
\hline -92 & 1.808 & 1.831 & 88 & 1.259 & 1.240 \\
\hline -88 & 1.413 & 1.464 & 92 & 1.659 & 1.646 \\
\hline -84 & 1.130 & 1.137 & 96 & 2.014 & 1.951 \\
\hline -80 & 1.073 & 0.996 & 100 & 2.145 & 2.114 \\
\hline -76 & 1.187 & 1.078 & 104 & 2.339 & 2.301 \\
\hline -72 & 1.356 & 1.253 & 108 & 2.575 & 2.551 \\
\hline -68 & 1.500 & 1.386 & 112 & 2.871 & 2.831 \\
\hline -64 & 1.606 & 1.501 & 116 & 2.945 & 3.912 \\
\hline -60 & 1.655 & 1.586 & 120 & 2.708 & 2.720 \\
\hline -56 & 1.719 & 1.658 & 124 & 2.346 & 2.434 \\
\hline -52 & 1.785 & 1.730 & 128 & 2.031 & 2.042 \\
\hline -48 & 1.864 & 1.796 & 132 & 1.778 & 1.790 \\
\hline -44 & 1.882 & 1.831 & 136 & 1.598 & 1.602 \\
\hline -40 & 1.963 & 1.897 & 140 & 1.478 & 1.482 \\
\hline -36 & 1.981 & 1.942 & 144 & 1.409 & 1.416 \\
\hline -32 & 2.055 & 2.035 & 148 & 1.379 & 1.383 \\
\hline -28 & 2.081 & 2.027 & 152 & 1.406 & 1.419 \\
\hline -24 & 2.135 & 2.052 & 156 & 1.492 & 1.495 \\
\hline -20 & 2.163 & 2.091 & 160 & 1.591 & 1.580 \\
\hline -16 & 2.159 & 2.111 & 164 & 1.622 & 1.618 \\
\hline -12 & 2.189 & 2.151 & 168 & 1.744 & 1.774 \\
\hline -8 & 2.186 & 2.188 & 172 & 1.810 & 1.856 \\
\hline -4 & 2.238 & 2.194 & 176 & 1.899 & 1.904 \\
\hline 0 & 2.188 & 2.189 & 180 & 1.911 & 1.909 \\
\hline
\end{tabular}
```

TU=2.651%, L/D=0.030, RE=110000, ST=0.0213 (RUN 2)
MULTIPLIER=0.20509 /MIL LOSS CORRECTION=0.065 MILS

```
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
S H / \sqrt{R E} \\
7=-5
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
S H / \sqrt{R E} \\
Z=-5
\end{gathered}
\] & \[
\mathrm{SH} / \sqrt{\mathrm{RE}}
\] \\
\hline -178 & \(Z=-.51\)
1.875 & \(2=+.5\)
1.935 & 2 & \(\mathrm{Z}=-.5^{\prime \prime}\)
2.154 & \(2=+.51\)
2.121 \\
\hline -174 & 1.818 & 1.855 & 6 & 2.151 & 2.122 \\
\hline -170 & 1.759 & 1.809 & 10 & 2.135 & 2.119 \\
\hline -166 & 1.689 & 1.756 & 14 & 2.112 & 2.082 \\
\hline -162 & 1.597 & 1.674 & 18 & 2.077 & 2.099 \\
\hline -158 & 1.526 & 1.587 & 22 & 2.065 & 2.063 \\
\hline -154 & 1.442 & 1.469 & 26 & 2.012 & 1.999 \\
\hline -150 & 1.368 & 1.401 & 30 & 1.976 & 1.981 \\
\hline -146 & 1.397 & 1.384 & 34 & 1.950 & 1.937 \\
\hline -142 & 1.468 & 1.416 & 38 & 1.873 & 1.886 \\
\hline -138 & 1.574 & 1.529 & 42 & 1.795 & 1.850 \\
\hline -134 & 1.728 & 1.676 & 46 & 1.810 & 1.776 \\
\hline -130 & 1.972 & 1.908 & 50 & 1.723 & 1.662 \\
\hline -126 & 2.287 & 2.180 & 54 & 1.646 & 1.630 \\
\hline -122 & 2.619 & 2.537 & 58 & 1.600 & 1.562 \\
\hline -118 & 2.963 & 2.896 & 62 & 1.509 & 1.502 \\
\hline -114 & 2.922 & 3.018 & 66 & 1.451 & 1.368 \\
\hline -110 & 2.617 & 2.834 & 70 & 1.312 & 1.255 \\
\hline -106 & 2.448 & 2.546 & 74 & 1.172 & 1.117 \\
\hline -102 & 2.251 & 2.242 & 78 & 1.045 & 0.977 \\
\hline -98 & 2.050 & 2.111 & 82 & 0.956 & 0.964 \\
\hline -94 & 1.794 & 1.844 & 86 & 1.355 & 1.292 \\
\hline -90 & 1.428 & 1.478 & 90 & 1.752 & 1.667 \\
\hline -86 & 1.128 & 1.148 & 94 & 2.092 & 1.995 \\
\hline -82 & 1.039 & 0.966 & 98 & 2.241 & 2.203 \\
\hline -78 & 1.162 & 1.056 & 102 & 2.470 & 2.413 \\
\hline -74 & 1.321 & 1.214 & 106 & 2.729 & 2.699 \\
\hline -70 & 1.437 & 1.369 & 110 & 2.965 & 3.084 \\
\hline -66 & 1.534 & 1.453 & 114 & 3.029 & 2.997 \\
\hline -62 & 1.614 & 1.534 & 118 & 2.807 & 2.712 : \\
\hline -58 & 1.688 & 1.602 & 122 & 2.439 & 2.387 \\
\hline -54 & 1.733 & 1.704 & 126 & 2.083 & 2.055 \\
\hline -50 & 1.847 & 1.707 & 130 & \(1.827^{\circ}\) & 1.766 \\
\hline -46 & 1.851 & 1.820 & 134 & 1.624 & 1.586 \\
\hline -42 & 1.889 & 1.855 & 138 & 1.445 & 1.468 \\
\hline -38 & 1.941 & 1.860 & 142 & 1.434 & 1.410 \\
\hline -34 & 1.974 & 1.904 & 146 & 1.432 & 1.390 \\
\hline -30 & 1.983 & 1.958 & 150 & 1.432 & 1.462 \\
\hline -26 & 2.048 & 2.020 & 154 & 1.524 & 1.515 \\
\hline -22 & 2.080 & 2.059 & 158 & 1.595 & 1.635 \\
\hline -18 & 2.093 & 2.078 & 162 & 1.689 & 1.669 \\
\hline -14 & 2.114 & 2.099 & 166 & 1.769 & 1.747 \\
\hline -10 & 2.110 & 2.105 & 170 & 1.840 & 1.831 \\
\hline -6 & 2.142 & 2.115 & 174 & 1.863 & 1.941 \\
\hline -2 & 2.162 & 2.119 & 178 & 1.895 & 1.926 \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|}
\hline \(\mathrm{TU}=2.6\) & \% L/D=0 & , RE=110000, & ST=0. & & IG 52) \\
\hline MULTIP & \(\mathrm{R}=0.239\) & MIL & LOSS CO & ECTION=0. & 68 MILS \\
\hline OSCILL & ON AMPL & JDE INCREASED & TO 12 & REES & \\
\hline DEG & \(\mathrm{SH} / \sqrt{\text { RE }}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & DEG & SH/ \(/\) RE & SH/ \(/\) RE \\
\hline & \(2=-.5^{\prime \prime}\) & \(2=+.51\) & & \(z=-.5^{\prime \prime}\) & \(\mathrm{z}=+.5^{\prime \prime}\) \\
\hline -177 & 1.608 & 1.603 & 3 & 2.177 & 2.180 \\
\hline -173 & 1.592 & 1.591 & 7 & 2.189 & 2.178 \\
\hline -169 & 1.519 & 1.562 & 11 & 2.162 & 2.146 \\
\hline -165 & 1.484 & 1.500 & 15 & 2.132 & 2.123 \\
\hline -161 & 1.442 & 1.427 & 19 & 2.101 & 2.104 \\
\hline -157 & 1.440 & 1.363 & 23 & 2.084 & 2.078 \\
\hline -153 & 1.429 & 1.278 & 27 & 2.046 & 2.047 \\
\hline -149 & 1.415 & 1.249 & 31 & 2.012 & 2.035 \\
\hline -145 & 1.409 & 1.317 & 35 & 1.971 & 1.983 \\
\hline -141 & 1.462 & 1.437 & 39 & 1.930 & 1.952 \\
\hline -137 & 1.580 & 1.524 & 43 & 1.892 & 1.879 \\
\hline -133 & 1.785 & 1.697 & 47 & 1.837 & 1.815 \\
\hline -129 & 2.159 & 1.925 & 51 & 1.783 & 1.752 \\
\hline -125 & 2.343 & 2.287 & 55 & 1.701 & 1.627 \\
\hline -121 & 2.385 & 2.344 & 59 & 1.605 & 1.531 \\
\hline -117 & 2.259 & 2.186 & 63 & 1.474 & 1.482 \\
\hline -113 & 2.081 & 2.036 & 67 & 1.333 & 1.359 \\
\hline -109 & 1.950 & 1.912 & 71 & 1.161 & 1.180 \\
\hline -105 & 1.928 & 1.923 & 75 & 1.033 & 1.034 \\
\hline -101 & 1.963 & 1.929 & 79 & 1.043 & 0.866 \\
\hline -97 & 1.898 & 1.888 & 83 & 1.287 & 1.324 \\
\hline -93 & 1.923 & 1.824 & 87 & 1.668 & 1.682 \\
\hline -89 & 1.787 & 1.703 & 91 & 1.879 & 1.909 \\
\hline -85 & 1.505 & 1.385 & 95 & 1.962 & 1.990 \\
\hline -81 & 1.228 & 1.072 & 99 & 1.930 & 1.978 \\
\hline -77 & 0.973 & 1.017 & 103 & 1.924 & 2.011 \\
\hline -73 & 1.092 & 1.079 & 107 & 1.963 & 2.005 \\
\hline -69 & 1.307 & 1.293 & 111 & 2.078 & 2.086 \\
\hline -65 & 1.458 & 1.441 & 115 & 2.197 & 2.216 \\
\hline -61 & 1.532 & 1.544 & 119 & 2.338 & 2.321 \\
\hline -57 & 1.634 & 1.628 & 123 & 2.377 & 2.442 \\
\hline -53 & 1.717 & 1.718 & 127 & 2.325 & 2.284 \\
\hline -49 & 1.789 & 1.803 & 131 & 2.030 & 2.010 \\
\hline -45 & 1.886 & 1.905 & 135 & 1.595 & 1.601 \\
\hline -41 & 1.943 & 1.927 & 139 & 1.510 & 1.476 \\
\hline -37 & 1.982 & 1.973 & 143 & 1.453 & 1.338 \\
\hline -33 & 2.026 & 2.012 & 147 & 1.398 & 1.325 \\
\hline -29 & 2.057 & 2.043 & 151 & 1.384 & 1.314 \\
\hline -25 & 2.121 & 2.083 & 155 & 1.399 & 1.344 \\
\hline -21 & 2.125 & 2.146 & 159 & 1.428 & 1.407 \\
\hline -17 & 2.143 & 2.137 & 163 & 1.464 & 1.459 \\
\hline -13 & 2.182 & 2.136 & 167 & 1.507 & 1.502 \\
\hline -9 & 2.169 & 2.143 & 171 & 1.546 & 1.543 \\
\hline -5 & 2.184 & 2.184 & 175 & 1.587 & 1.583 \\
\hline -1 & 2.183 & 2.194 & 179 & 1.611 & 1.617 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0355\) (RUN 1, EIG 45) MULTIPLIER=0.21920 /MIL LOSS CORRECTION=0.070 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
Z=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
Z=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] \\
\hline -176 & 1.942 & 1.921 & 4 & 2.271 & 2.268 \\
\hline -172 & 1.895 & 1.876 & 8 & 2.204 & 2.241 \\
\hline -168 & 1.854 & 1.794 & 12 & 2.232 & 2.256 \\
\hline -164 & 1.751 & 1.732 & 16 & 2.197 & 2.245 \\
\hline -160 & 1.637 & 1.635 & 20 & 2.187 & 2.187 \\
\hline -156 & 1.544 & 1.542 & 24 & 2.163 & 2.171 \\
\hline -152 & 1.459 & 1.449 & 28 & 2.122 & 2.060 \\
\hline -148 & 1.407 & 1.399 & 32 & 2.094 & 2.057 \\
\hline -144 & 1.399 & 1.396 & 36 & 2.078 & 2.021 \\
\hline -140 & 1.467 & 1.456 & 40 & 2.008 & 1.969 \\
\hline -136 & 1.599 & 1.568 & 44 & 1.954 & 1.940 \\
\hline -132 & 1.796 & 1.751 & 48 & 1.907 & 1.862 \\
\hline -128 & 2.051 & 1.988 & 52 & 1.815 & 1.815 \\
\hline -124 & 2.416 & 2.317 & 56 & 1.773 & 1.749 \\
\hline -120 & 2.816 & 2.704 & 60 & 1.715 & 1.670 \\
\hline -116 & 3.120 & 3.039 & 64 & 1.601 & 1.574 \\
\hline -112 & 3.100 & 2.980 & 68 & 1.489 & 1.477 \\
\hline -108 & 2.826 & 2.745 & 72 & 1.386 & 1.355 \\
\hline -104 & 2.550 & 2.432 & 76 & 1.224 & 1.159 \\
\hline -100 & 2.316 & 2.204 & 80 & 1.091 & 1.053 \\
\hline -96 & 2.120 & 2.044 & 84 & 1.049 & 1.036 \\
\hline -92 & 1.814 & 1.784 & 88 & 1.320 & 1.320 \\
\hline -88 & 1.390 & 1.378 & 92 & 1.700 & 1.719 \\
\hline -84 & 1.088 & 1.054 & 96 & 2.036 & 1.960 \\
\hline -80 & 1.054 & 0.989 & 100 & 2.200 & 2.199 \\
\hline -76 & 1.211 & 1.107 & 104 & 2.393 & 2.431 \\
\hline -72 & 1.369 & 1. 280 & 108 & 2.691 & 2.687 \\
\hline -68 & 1.504 & 1.425 & 112 & 2.960 & 2.952 \\
\hline -64 & 1.603 & 1.533 & 116 & 3.080 & 3.083 \\
\hline -60 & 1.699 & 1.612 & 120 & 2.838 & 2.791 \\
\hline -56 & 1.761 & 1.708 & 124 & 2.467 & 2.463 \\
\hline -52 & 1.844 & 1.784 & 128 & 2.149 & 2.053 \\
\hline -48 & 1.891 & 1.854 & 132 & 1.837 & 1.776 \\
\hline -44 & 1.944 & 1.913 & 136 & 1.628 & 1.575 \\
\hline -40 & 1.985 & 1.973 & 140 & 1.450 & 1.487 \\
\hline -36 & 2.024 & 1.991 & 144 & 1.395 & 1.379 \\
\hline -32 & 2.102 & 2.073 & 148 & 1.417 & 1.404 \\
\hline -28 & 2.119 & 2.135 & 152 & 1.454 & 1.436 \\
\hline -24 & 2.172 & 2.166 & 156 & 1.527 & 1.513 \\
\hline -20 & 2.165 & 2.183 & 160 & 1.620 & 1.620 \\
\hline -16 & 2.228 & 2.235 & 164 & 1.744 & 1.696 \\
\hline -12 & 2.262 & 2:241 & 168 & 1.893 & 1.794 \\
\hline -8 & 2.273 & 2.263 & 172 & 1.879 & 1.865 \\
\hline -4 & 2.280 & 2.281 & 176 & 1.942 & 1.933 \\
\hline 0 & 2.256 & 2.288 & -180 & 1.959 & 1.943 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \quad R E=110000, S T=0.0355\) (RUN 2)
MULTIPLIER=0.23509 MIL LOSS CORRECTION=0.062 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
z=-.5 \prime
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& \mathrm{Z}=+: 5^{\prime \prime}
\end{aligned}
\] \\
\hline -176 & 1.930 & 1.920 & 4 & 2.308 & 2.249 \\
\hline -172 & 1.871 & 1.878 & 8 & 2.300 & 2.262 \\
\hline -168 & 1.778 & 1.787 & 12 & 2.293 & 2.280 \\
\hline -164 & 1.707 & 1.698 & 16 & 2.281 & 2.217 \\
\hline -160 & 1.555 & 1.598 & 20 & 2.240 & 2.219 \\
\hline -156 & 1.481 & 1.507 & 24 & 2.210 & 2.173 \\
\hline -152 & 1.455 & 1.453 & 28 & 2.246 & 2.144 \\
\hline -148 & 1.421 & 1.425 & 32 & 2.104 & 2.098 \\
\hline -144 & 1.455 & 1.434 & 36 & 2.026 & 2.003 \\
\hline -140 & 1.558 & 1.520 & 40 & 1.979 & 1.938 \\
\hline -136 & 1.659 & 1.631 & 44 & 1.941 & 1.890 \\
\hline -132 & 1.932 & 1.860 & 48 & 1.885 & 1.827 \\
\hline -128 & 2.228 & 2.123 & 52 & 1.818 & 1.617 \\
\hline -124 & 2.575 & 2.490 & 56 & 1.719 & 1.716 \\
\hline -120 & 2.935 & 2.811 & 60 & 1:693 & 1.608 \\
\hline -116 & 3.063 & 3.020 & 64 & 1.605 & 1.524 \\
\hline -112 & 2.883 & 2.919 & 68 & 1.476 & 1.425 \\
\hline -108 & 2.571 & 2.673 & 72 & 1.339 & 1.250 \\
\hline -104 & 2.338 & 2.353 & 76 & 1.153 & 1.079 \\
\hline -100 & 2.181 & 2.177 & 80 & 1.010 & 1.013 \\
\hline -96 & 1.948 & 1.952 & 84 & 1.179 & 1.171 \\
\hline -92 & 1.552 & 1.606 & 88 & 1.509 & 1.549 \\
\hline -88 & 1.187 & 1.233 & 92 & 1.949 & 1.901 \\
\hline -84 & 1.034 & 1.011 & 96 & 2. 189 & 2.110 \\
\hline -80 & 1.238 & 1.070 & 100 & 2.358 & 2.330 \\
\hline -76 & 1.310 & 1.220 & 104 & 2.631 & 2.604 \\
\hline -72 & 1. 469 & 1.401 & 108 & 2.941 & 2.903 \\
\hline -68 & 1.587 & 1.515 & 112 & 3.116 & 3.062 \\
\hline -64 & 1.674 & 1.617 & 116 & 3.018 & 2.925 \\
\hline -60 & 1.740 & 1.696 & 120 & 2.675 & 2.546 \\
\hline -56 & 1.808 & 1.777 & 124 & 2.264 & 2.192 \\
\hline -52 & 1.865 & 1.884 & 128 & 1.948 & 1.902 \\
\hline -48 & 1.905 & 1.915 & 132 & 1.703 & 1.688 \\
\hline -44 & 2.017 & 1.950 & 136 & 1.552 & 1.525 \\
\hline -40 & 2.037 & 2.031 & 140 & 1.422 & 1.452 \\
\hline -36. & 2.079 & 2.075 & 144 & 1.436 & 1.429 \\
\hline -32 & 2.141 & 2.091 & 148 & 1.433 & 1.472 \\
\hline -28 & 2.136 & 2.182 & 152 & 1.494 & 1.527 \\
\hline -24 & 2.193 & 2.216 & 156 & 1.591 & 1.617 \\
\hline -20 & 2.218 & 2.213 & 160 & 1.679 & 1.697 \\
\hline -16 & 2.245 & 2.268 & 164 & 1.776 & 1.799 \\
\hline -12 & 2.260 & 2.267 & 168 & 1.882 & 1.868 \\
\hline -8 & 2.285 & 2.285 & 172 & 1.895 & 1.954 \\
\hline -4 & 2.297 & 2.301 & 176 & 1. 957 & 1.966 \\
\hline 0 & 2.304 & 2.283 & 180 & 1.956 & 1.966 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0497\) (RUN 1, EIG 46) MULTIPLIER=0.20514. MIL LOSS CORRECTION=0.107 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/ \(/\) RE & \(\mathrm{SH} / \sqrt{R E}\) & DEG & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & \(\mathrm{SH} / \sqrt{R E}\) \\
\hline & Z=-.5" & \(\mathrm{Z}=+.5^{\prime \prime}\) & & \(\mathrm{z}=-.5^{\prime \prime}\) & \(\mathrm{z}=+.5^{\prime \prime}\) \\
\hline -176 & 1.899 & 1.871 & 4 & 2.296 & 2.290 \\
\hline -172 & 1.846 & 1.891 & 8 & 2.271 & 2.255 \\
\hline -168 & 1.801 & 1.838 & 12 & 2.257 & 2.266 \\
\hline -164 & 1.735 & 1.773 & 16 & 2.251 & 2.224 \\
\hline -160 & 1.621 & 1.683 & 20 & 2.228 & 2.243 \\
\hline -156 & 1.518 & 1.573 & 24 & 2.211 & 2.201 \\
\hline -152 & 1.465 & 1.467 & 28 & 2.143 & 2.177 \\
\hline -148 & 1.396 & 1.419 & 32 & 2.103 & 2.135 \\
\hline -144 & 1.410 & 1.413 & 36 & 2.071 & 2.128 \\
\hline -140 & 1.486 & 1.462 & 40 & 2.023 & 2.066 \\
\hline -136 & 1.627 & 1.599 & 44 & 1.990 & 2.017 \\
\hline -132 & 1.845 & 1.792 & 48 & 1.983 & 1.955 \\
\hline -128 & 2.125 & 2.052 & 52 & 1.864 & 1.890 \\
\hline -124 & 2.479 & 2.411 & 56 & 1.775 & 1.774 \\
\hline -120 & 2.901 & 2.770 & 60 & 1.768 & 1.771 \\
\hline -116 & 3.151 & 3.098 & 64 & 1.736 & 1.701 \\
\hline -112 & 3.070 & 3.074 & 68 & 1.598 & 1.597 \\
\hline -108 & 2.701 & 2.807 & 72 & 1.481 & 1.479 \\
\hline -104 & 2.430 & 2.498 & 76 & 1.314 & 1.323 \\
\hline -100 & 2.314 & 2.327 & 80 & 1.187 & 1.144 \\
\hline -96 & 2.116 & 2.130 & 84 & 1.090 & 1.087 \\
\hline -92 & 1.809 & 1.809 & 88 & 1.287 & 1.258 \\
\hline -88 & 1.345 & 1.435 & 92 & 1.678 & 1.657 \\
\hline -84 & 1.126 & 1.130 & 96 & 2.088 & 2.052 \\
\hline -80 & 1.147 & 1.079 & 100 & 2.266 & 2.279 \\
\hline -76 & 1.306 & 1.233 & 104 & 2.411 & 2.398 \\
\hline -72 & 1.480 & 1.399 & 108 & 2.693 & 2.625 \\
\hline -68 & 1.590 & 1.546 & 112 & 2.963 & 2.878 \\
\hline -64 & 1.588 & 1.497 & 116 & 3.185 & 3.102 \\
\hline -60 & 1.744 & 1.705 & 120 & 3.184 & 3.017 \\
\hline -56 & 1.841 & 1.783 & 124 & 2.630 & 2.618 \\
\hline -52 & 1.919 & 1.894 & 128 & 2.178 & 2.206 \\
\hline -48 & 1.975 & 1.952 & 132 & 1.858 & 1.900 \\
\hline -44 & 2.028 & 2.025 & 136 & 1.658 & 1.656 \\
\hline -40 & 2.049 & 2.075 & 140 & 1.508 & 1.497 \\
\hline -36 & 2.101 & 2.106 & 144 & 1.418 & 1.422 \\
\hline -32 & 2.154 & 2.160 & 148 & 1.382 & 1.413 \\
\hline -28 & 2.182 & 2.206 & 152 & 1.440 & 1.465 \\
\hline -24 & 2.189 & 2.245 & 156 & 1.489 & 1.529 \\
\hline -20 & 2.236 & 2.239 & 160 & 1.594 & 1.603 \\
\hline -16 & 2.258 & 2.251 & 164 & 1.646 & 1.682 \\
\hline -12 & 2.281 & 2.295 & 168 & 1.756 & 1.766 \\
\hline -8 & 2.289 & 2.317 & 172 & 1.831 & 1.855 \\
\hline -4 & 2.305 & 2.320 & 176 & 1.895 & 1.857 \\
\hline 0 & 2.290 & 2.294 & 180 & 1.885 & 1.853 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0497\) (RUN 2)
MULTIPLIER=0.22538 MIL LOSS CORRECTION=0.108 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{R E} \\
& \mathrm{Z}=+.5^{\prime \prime}
\end{aligned}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] \\
\hline -176 & 1.905 & 1.930 & 4 & 2.318 & 2.335 \\
\hline -172 & 1.833 & 1.918 & 8 & 2.234 & 2.322 \\
\hline -168 & 1.785 & 1.777 & 12 & 2.307 & 2.321 \\
\hline -164 & 1.690 & 1.628 & 16 & 2.246 & 2.281 \\
\hline -160 & 1.593 & 1.568 & 20 & 2.238 & 2.240 \\
\hline -156 & 1.522 & 1.495 & 24 & 2.219 & 2.204 \\
\hline -152 & 1.452 & 1.409 & 28 & 2.168 & 2.131 \\
\hline -148 & 1.361 & 1.340 & 32 & 2.127 & 2.070 \\
\hline -144 & 1.443 & 1.436 & 38 & 2.022 & 2.029 \\
\hline -140 & 1.519 & 1.552 & 42 & 1.951 & 1.920 \\
\hline -136 & 1.686 & 1.736 & 46 & 1.963 & 1.872 \\
\hline -132 & 1.939 & 2.037 & 50 & 1.874 & 1.816 \\
\hline -128 & 2.240 & 2.340 & 54 & 1.810 & 1.770 \\
\hline -124 & 2.682 & 2.771 & 56 & 1.743 & 1.663 \\
\hline -120 & 3.051 & 3.078 & 60 & 1.744 & 1.624 \\
\hline -116 & 3.200 & 3.103 & 64 & 1.604 & 1.498 \\
\hline -112 & 2.891 & 2.916 & 68 & 1.467 & 1.383 \\
\hline -108 & 2.621 & 2.557 & 72 & 1.328 & 1.192 \\
\hline -104 & 2.198 & 2.182 & 76 & 1.215 & 1.019 \\
\hline -100 & 2.136 & 2.059 & 80 & 1.032 & 0.991 \\
\hline -96 & 1.916 & 1.725 & 84 & 1.090 & 1.197 \\
\hline -92 & 1.503 & 1.367 & 88 & 1.378 & 1.634 \\
\hline -88 & 1.114 & 1.034 & 92 & 1.838 & 2.037 \\
\hline -84 & 0.978 & 0.946 & 96 & 2.168 & 2.234 \\
\hline -80 & 1.056 & 1.039 & 100 & 2.355 & 2.469 \\
\hline -76 & 1.214 & 1.242 & 104 & 2.587 & 2.677 \\
\hline -72 & 1.385 & 1.343 & 108 & 2.835 & 2.990 \\
\hline -68 & 1.454 & 1.470 & 112 & 3.189 & 3.130 \\
\hline -64 & 1.600 & 1.622 & 116. & 3.234 & 2.987 \\
\hline -60 & 1.671 & 1.694 & 120 & 2.876 & 2.586 \\
\hline -56 & 1.751 & 1.769 & 124 & 2.516 & 2.180 \\
\hline -52. & 1.808 & 1.855 & 128 & 2.029 & 1.838 \\
\hline -48 & 1.923 & 1.943 & 132 & 1.780 & 1.598 \\
\hline -44 & 1.898 & 1.991 & 136 & 1.528 & 1.430 \\
\hline -40 & 1.992 & 2.070 & 140 & 1.443 & 1.411 \\
\hline -36 & 2.029 & 2.123 & 144 & 1.381 & 1.419 \\
\hline -32 & 2.074 & 2.112 & 148 & 1.357 & 1.410 \\
\hline -28 & 2.162 & 2.230 & 152 & 1.420 & 1.499 \\
\hline -24 & 2.223 & 2.257 & 156 & 1.510 & 1.549 \\
\hline -20 & 2.245 & 2.232 & 160 & 1.660 & 1.722 \\
\hline -16 & 2.297 & 2.249 & 164 & 1.755 & 1.800 \\
\hline -12 & 2.303 & 2.330 & 168 & 1.837 & 1.833 \\
\hline -8 & 2.285 & 2.318 & 172 & 1.854 & 1.904 \\
\hline -4 & 2.285 & 2.354 & 176 & 1.904 & 1.958 \\
\hline 0 & 2.330 & 2.346 & 180 & 1.940 & 1.931 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \quad \mathrm{RE}=110000, \mathrm{ST}=0.0497\) (RUN 3)
MULTIPLIER=0.23505 /MIL LOSS CORRECTION=0. 100 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& \mathrm{Z}=+.5^{\prime \prime}
\end{aligned}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{array}{r}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5
\end{array}
\] \\
\hline -176 & 1.875 & 2.006 & 4 & 2.311 & 2.298 \\
\hline -172 & 1.860 & 1.885 & 8 & 2.303 & 2.289 \\
\hline -168 & 1.760 & 1.820 & 12 & 2.277 & 2.259 \\
\hline -164 & 1.700 & 1.758 & 16 & 2.259 & 2.264 \\
\hline -160 & 1.618 & 1.654 & 20 & 2.250 & 2.251 \\
\hline -156 & 1.487 & 1.566 & 24 & 2.154 & 2.199 \\
\hline -152 & 1.430 & 1.466 & 28 & 2.124 & 2.140 \\
\hline -148 & 1.413 & 1.401 & 32 & 2.081 & 2.119 \\
\hline -144 & 1.384 & 1.397 & 36 & 2.057 & 2.070 \\
\hline -140 & 1.443 & 1.446 & 40 & 1.997 & 2.041 \\
\hline -136 & 1.378 & 1.347 & 44 & 1.981 & 1.977 \\
\hline -132 & 1.786 & 1.750 & 48 & 1.879 & 1.900 \\
\hline -128 & 2.058 & 2.041 & 52 & 1.865 & 1.860 \\
\hline -124 & 2.407 & 2.388 & 56 & 1.767 & 1.778 \\
\hline -120 & 2.837 & 2.785 & 60 & 1.692 & 1.719 \\
\hline -116 & 3.139 & 3.093 & 64 & 1.623 & 1.621 \\
\hline -112 & 3.045 & 3.113 & 68 & 1.550 & 1.532 \\
\hline -108 & 2.767 & 2.820 & 72 & 1.481 & 1.415 \\
\hline -104 & 2.515 & 2.520 & 76 & 1.305 & 1.250 \\
\hline -100 & 2.280 & 2.322 & 80 & 1.136 & 1.090 \\
\hline -96 & 2.124 & 2.128 & 84 & 1.025 & 0.992 \\
\hline -92 & 1.801 & 1.829 & 88 & 1.162 & 1.130 \\
\hline -88 & 1.347 & 1.410 & 92 & 1.567 & 1.529 \\
\hline -84 & 1.107 & 1.095 & 96 & 1.986 & 1.935 \\
\hline -80 & 1.112 & 1.020 & 100 & 2.207 & 2.165 \\
\hline -76 & 1.288 & 1.185 & 104 & 2.326 & 2.349 \\
\hline -72 & 1.444 & 1.342 & 108 & 2.594 & 2.597 \\
\hline -68 & 1. 565 & 1.474 & 112 & 2.875 & 2.823 \\
\hline -64 & 1.668 & 1.576 & 116 & 3.030 & 3.078 \\
\hline -60 & 1.749 & 1.655 & 120 & 2.930 & 2.965 \\
\hline -56 & 1.841 & 1.764 & 124 & 2.595 & 2.600 \\
\hline -52 & 1.883 & 1.819 & 128 & 2.213 & 2.234 \\
\hline -48 & 1.924 & 1.888 & 132 & 1.865 & 1.870 \\
\hline -44 & 1.981 & 1.951 & 136 & 1.611 & 1.626 \\
\hline -40 & 2.043 & 2.002 & 140 & 1.457 & 1.457 \\
\hline -36 & 2.099 & 2.052 & 144 & 1.386 & 1.360 \\
\hline -32 & 2.176 & 2.107 & 148 & 1.353 & 1.329 \\
\hline -28 & 2.187 & 2.135 & 152 & 1.378 & 1.347 \\
\hline -24 & 2.265 & 2.192 & 156 & 1.439 & 1.434 \\
\hline -20 & 2.292 & 2.195 & 160 & 1.490 & 1.533 \\
\hline -16 & 2.302 & 2.234 & 164 & 1.621 & 1.635 \\
\hline -12 & 2.299 & 2.242 & 168 & 1.742 & 1.770 \\
\hline -8 & 2.321 & 2.290 & 172 & 1.801 & 1.821 \\
\hline -4 & 2.335 & 2.296 & 176 & 1.882 & 1.883 \\
\hline 0 & 2.320 & 2.300 & 180 & 1.886 & 1.917 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0497\) (RUN 4) MULTIPLIER=0.23679 MIL LOSS CORRECTION=0!082 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
Z=-5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& Z=+.5^{\prime \prime}
\end{aligned}
\] \\
\hline -176 & 1.873 & 1.887 & 4 & 2.311 & 2.301 \\
\hline -172 & 1.819 & 1.869 & 8 & 2.303 & 2.307 \\
\hline -168 & 1.786 & 1.828 & 12 & 2.294 & 2.323 \\
\hline -164 & 1.699 & 1.777 & 16 & 2.251 & 2.304 \\
\hline -160 & 1.626 & 1.736 & 20 & 2.226 & 2.274 \\
\hline -156 & 1.550 & 1.610 & 24 & 2.222 & 2.245 \\
\hline -152 & 1.442 & 1.526 & 28 & 2.172 & 2.189 \\
\hline -148 & 1.399 & 1.503 & 32 & 2.119 & 2.135 \\
\hline -144 & 1.436 & 1.473 & 36 & 2.094 & 2.108 \\
\hline -140 & 1.518 & 1.514 & 40 & 2.030 & 2.057 \\
\hline -136 & 1.637 & 1.664 & 44 & 2.011 & 2.026 \\
\hline -132 & 1.840 & 1.729 & 48 & 1.949 & 1.947 \\
\hline -128 & 2.095 & 1.988 & 52 & 1.898 & 1.876 \\
\hline -124 & 2.436 & 2.325 & 56 & 1.863 & 1.785 \\
\hline -120 & 2.851 & 2.787 & 60 & 1.745 & 1.726 \\
\hline -116 & 3.144 & 3.088 & 64 & 1.674 & 1.629 \\
\hline -112 & 3.037 & 3.088 & 68 & 1.556 & 1.533 \\
\hline -108 & 2.658 & 2.823 & 72 & 1.427 & 1.378 \\
\hline -104 & 2.408 & 2.549 & 76 & 1.261 & 1.196 \\
\hline -100 & 2.214 & 2.330 & 80 & 1.107 & 1.078 \\
\hline -96 & 2.057 & 2.112 & 84 & 1.146 & 1.148 \\
\hline -92 & 1.732 & 1.817 & 88 & 1.426 & 1.450 \\
\hline -88 & 1.333 & 1.429 & 92 & 1.850 & 1.841 \\
\hline -84 & 1.098 & 1.101 & 96 & 2.137 & 2.202 \\
\hline -80 & 1.098 & 1.039 & 100 & 2.376 & 2.414 \\
\hline -76 & 1.253 & 1.186 & 104 & 2.556 & 2.560 \\
\hline -72 & 1.423 & 1.375 & 108 & 2.753 & 2.762 \\
\hline -68 & 1.526 & 1.506 & 112 & 3.014 & 3.033 \\
\hline -64 & 1.639 & 1.608 & 116 & 3.175 & 3.101 \\
\hline -60 & 1.747 & 1.699 & 120 & 2.917 & 2.872 \\
\hline -56 & 1.808 & 1.784 & 124 & 2.508 & 2.454 \\
\hline -52 & 1.881 & 1.877 & 128 & 2.202 & 2.092 \\
\hline -48 & 1.947 & 1.957 & 132 & 1.913 & 1.835 \\
\hline -44 & 2.008 & 2.004 & 136 & 1.618 & 1.578 \\
\hline -40 & 2.042 & 2.066 & 140 & 1.510 & 1.466 \\
\hline -36 & 2.080 & 2.108 & 144 & 1.431 & 1.387 \\
\hline -32 & 2.143 & 2.171 & 148 & 1.435 & 1.489 \\
\hline -28 & 2.190 & 2.211 & 152 & 1.498 & 1.544 \\
\hline -24 & 2.209 & 2.258 & 156 & 1.542 & 1.599 \\
\hline -20 & 2.230 & 2.247 & 160 & 1.647 & 1.663 \\
\hline -16 & 2.270 & 2.278 & 164 & 1.689 & 1.733 \\
\hline -12 & 2.268 & 2.306 & 168 & 1.781 & 1.832 \\
\hline -8 & 2.293 & 2.305 & 172 & 1.905 & 1.952 \\
\hline -4 & 2.314 & 2.328 & 176 & 1.929 & 1.970 \\
\hline 0 & 2.321 & 2.332 & 180 & 1.942 & 1.988 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0639\) (RUN 1, EIG 47) MULTIPLIER=0.30104 /MIL

LOSS CORRECTION=0.077 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] \\
\hline -176 & 1.918 & 1.898 & 4 & 2.283 & 2.300 \\
\hline -172 & 1.867 & 1.892 & 8 & 2.262 & 2.266 \\
\hline -168 & 1.787 & 1.824 & 12 & 2.231 & 2.246 \\
\hline -164 & 1.724 & 1.750 & 16 & 2.225 & 2.233 \\
\hline -160 & 1.635 & 1.645 & 20 & 2.193 & 2.201 \\
\hline -156 & 1.526 & 1.550 & 24 & 2.154 & 2.176 \\
\hline -152 & 1.429 & 1.450 & 28 & 2.109 & 2.139 \\
\hline -148 & 1.414 & 1.406 & 32 & 2.076 & 2.104 \\
\hline -144 & 1.410 & 1.403 & 36 & 2.036 & 2.054 \\
\hline -140 & 1.488 & 1.455 & 40 & 2.003 & 2.017 \\
\hline -136 & 1.578 & 1.582 & 44 & 1.948 & 1.961 \\
\hline -132 & 1.772 & 1.797 & 48 & 1.884 & 1.908 \\
\hline -128 & 2.065 & 2.012 & 52 & 1.836 & 1.806 \\
\hline -124 & 2.422 & 2.311 & 56 & 1.761 & 1.781 \\
\hline -120 & 2.857 & 2.675 & 60 & 1.689 & 1.697 \\
\hline -116 & 3.082 & 2.940 & 64 & 1.608 & 1.582 \\
\hline -112 & 3.029 & 2.897 & 68 & 1.516 & 1.496 \\
\hline -108 & 2.669 & 2.664 & 72 & 1.389 & 1.346 \\
\hline -104 & 2.444 & 2.357 & 76 & 1.219 & 1.170 \\
\hline -100 & 2.201 & 2.212 & 80 & 1.057 & 1.034 \\
\hline -96 & 2.013 & 2.020 & 84 & 1.037 & 1.048 \\
\hline -92 & 1.744 & 1.750 & 88 & 1.323 & 1.371 \\
\hline -88 & 1.344 & 1.407 & 92 & 1.754 & 1.765 \\
\hline -84 & 1.062 & 1.095 & 96 & 2.070 & 2.085 \\
\hline -80 & 1.023 & 0.981 & 100 & 2.291 & 2.287 \\
\hline -76 & 1.198 & 1.078 & 104 & 2.488 & 2.472 \\
\hline -72 & 1.319 & 1.269 & 108 & 2.733 & 2.719 \\
\hline -68 & 1.472 & 1.422 & 112 & 2.972 & 2.994 \\
\hline -64 & 1.579 & 1.502 & 116 & 3.040 & 2.980 \\
\hline -60 & 1.664 & 1.673 & 120 & 2.800 & 2.770 \\
\hline -56 & 1.749 & 1.769 & 124 & 2.421 & 2.387 \\
\hline -52 & 1.839 & 1.846 & 128 & 2.078 & 2.091 \\
\hline -48 & 1.876 & 1.907 & 132 & 1.806 & 1.863 \\
\hline -44 & 1.955 & 1.951 & 136 & 1.660 & 1.635 \\
\hline -40 & 2.016 & 2.009 & 140 & 1.427 & 1.447 \\
\hline -36 & 2.054 & 2.054 & 144 & 1.402 & 1.391 \\
\hline -32 & 2.100 & 2.098 & 148 & 1.367 & 1.392 \\
\hline -28 & 2.160 & 2.155 & 152 & 1.410 & 1.482 \\
\hline -24 & 2.216 & 2.163 & 156 & 1.494 & 1.552 \\
\hline -20 & 2.249 & 2.235 & 160 & 1.561 & 1.638 \\
\hline -16 & 2.267 & 2.264 & 164 & 1.692 & 1.705 \\
\hline -12 & 2.269 & 2.274 & 168 & 1.768 & 1:823 \\
\hline -8 & 2.260 & 2.292 & 172 & 1.853 & 1.884 \\
\hline -4 & 2.290 & 2.303 & 176 & 1.902 & 1.935 \\
\hline 0 & 2.290 & 2.281 & 180 & 1.939 & 1.941 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, R E=110000, S T=0.0639\) (RUN 2) MULTIPLIER=0.19963 /MIL

LOSS CORRECTION=0.070 MILS
\begin{tabular}{ccc} 
DEG & \(\mathrm{SH} / \sqrt{R E}\) & \(\mathrm{SH} / \sqrt{R E}\) \\
& \(Z=-.5^{\prime \prime}\) & \(Z=+.5^{\prime \prime}\) \\
-178 & 1.872 & 1.847 \\
-174 & 1.836 & 1.829 \\
-170 & 1.773 & 1.747 \\
-166 & 1.712 & 1.648 \\
-162 & 1.631 & 1.563 \\
-158 & 1.543 & 1.485 \\
-154 & 1.456 & 1.417 \\
-150 & 1.364 & 1.351 \\
-146 & 1.332 & 1.329 \\
-142 & 1.368 & 1.370 \\
-138 & 1.498 & 1.525 \\
-134 & 1.656 & 1.692 \\
-130 & 1.881 & 1.948 \\
-126 & 2.193 & 2.261 \\
-122 & 2.570 & 2.267 \\
-118 & 2.911 & 2.936 \\
-114 & 2.981 & 2.872 \\
-110 & 2.728 & 2.646 \\
-106 & 2.486 & 2.409 \\
-102 & 2.318 & 2.208 \\
-98 & 2.124 & 2.032 \\
-94 & 1.865 & 1.760 \\
-90 & 1.494 & 1.372 \\
-86 & 1.153 & 1.041 \\
-82 & 1.058 & 1.016 \\
-78 & 1.137 & 1.140 \\
-74 & 1.314 & 1.315 \\
-70 & 1.458 & 1.449 \\
-66 & 1.561 & 1.555 \\
-62 & 1.626 & 1.642 \\
-58 & 1.714 & 1.625 \\
-54 & 1.793 & 1.766 \\
-50 & 1.871 & 1.833 \\
-46 & 1.906 & 1.901 \\
-42 & 1.946 & 1.992 \\
-38 & 2.030 & 2.019 \\
-34 & 2.062 & 2.046 \\
-30 & 2.121 & 2.082 \\
-26 & 2.162 & 2.178 \\
-22 & 2.193 & 2.181 \\
-18 & 2.207 & 2.200 \\
-14 & 2.228 & 2.230 \\
-10 & 2.232 & 2.308 \\
-6 & 2.277 & 2.310 \\
-2 & 2.294 & 2.304 \\
& &
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& \mathrm{Z}=+.5^{\prime \prime}
\end{aligned}
\] \\
\hline 2 & 2.270 & 2.251 \\
\hline 6 & 2.263 & 2.258 \\
\hline 10 & 2.248 & 2.242 \\
\hline 14 & 2.359 & 2.239 \\
\hline 18 & 2.227 & 2.242 \\
\hline 22 & 2.198 & 2.181 \\
\hline 26 & 2.157 & 2.122 \\
\hline 30 & 2.083 & 2.069 \\
\hline 34 & 2.066 & 2.075 \\
\hline 38 & 2.054 & 2.017 \\
\hline 42 & 2.001 & 1.952 \\
\hline 46 & 1.916 & 1.853 \\
\hline 50 & 1.858 & 1.774 \\
\hline 54 & 1.794 & 1.729 \\
\hline 58 & 1.686 & 1.690 \\
\hline 62 & 1.684 & 1.599 \\
\hline 66 & 1.568 & 1.486 \\
\hline 70 & 1.475 & 1.370 \\
\hline 74 & 1.307 & 1.219 \\
\hline 78 & 1.160 & 1.073 \\
\hline 82 & 1.051 & 1.021 \\
\hline 86 & 1.068 & 1.150 \\
\hline 90 & 1.356 & 1.542 \\
\hline 94 & 1.728 & 1.853 \\
\hline 98 & 1.985 & 2.060 \\
\hline 102 & 1.157 & 2.239 \\
\hline 106 & 2.338 & 2.437 \\
\hline 110 & 2.556 & 2.697 \\
\hline 114 & 2.818 & 2.961 \\
\hline 118 & 2.959 & 2.828 \\
\hline 122 & 2.669 & 2.401 \\
\hline 126. & 2.335 & 2.138 \\
\hline 130 & 1.995 & 1.850 \\
\hline 134 & 1.717 & 1.613 \\
\hline 138 & 1.525 & 1.458 \\
\hline 142 & 1.374 & 1.323 \\
\hline 146 & 1.337 & 1. 344 \\
\hline 150 & 1.348 & 1.359 \\
\hline 154 & 1.379 & 1.452 \\
\hline 158 & 1.468 & 1.549 \\
\hline 162 & 1. 560 & 1.614 \\
\hline 166 & 1.643 & 1.736 \\
\hline 170 & 1.710 & 1.782 \\
\hline 174 & 1.794 & 1.830 \\
\hline 178 & 1.853 & 1.866 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0639\) (RUN 3)
MULTIPLIER=0.21404 MIL LOSS CORRECTION=0.030 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/ \(/\) RE & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & DEG & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & \(\mathrm{SH} / \sqrt{\text { RE }}\) \\
\hline & \(\mathrm{Z}=-.5^{\prime \prime}\) & Z=+.5" & & \(\mathrm{Z}=-.5^{\prime \prime}\) & \(2=+.5^{\prime \prime}\) \\
\hline -178 & 1.904 & 1.895 & 2 & 2.315 & 2.365 \\
\hline -174 & 1.866 & 1.873 & 6 & 2.324 & 2.393 \\
\hline -170 & 1.830 & 1.809 & 10 & 2.299 & 2.360 \\
\hline -166 & 1.737 & 1.745 & 14 & 2.281 & 2.389 \\
\hline -162 & 1.625 & 1.647 & 18 & 2.267 & 2.324 \\
\hline -158 & 1.581 & 1.518 & 22 & 2.233 & 2.298 \\
\hline -154 & 1.449 & 1.449 & 26 & 2.218 & 2.251 \\
\hline -150 & 1.398 & 1.411 & 30 & 2.164 & 2.225 \\
\hline -146 & 1.367 & 1.366 & 34 & 2.151 & 2.190 \\
\hline -142 & 1.401 & 1.426 & 40 & 2.092 & 2.128 \\
\hline -138 & 1.496 & 1.543 & 44 & 2.050 & 2.060 \\
\hline -134 & 1.662 & 1.730 & 48 & 2.018 & 1.981 \\
\hline -130 & 1.844 & 1.954 & 52 & 1.959 & 1.896 \\
\hline -126 & 2.227 & 2.323 & 56 & 1.869 & 1.872 \\
\hline -122 & 2.627 & 2.769 & 58 & 1.792 & 1.800 \\
\hline -118 & 2.971 & 3.025 & 62 & 1.742 & 1.706 \\
\hline -114 & 3.007 & 2.973 & 66 & 1.680 & 1.619 \\
\hline -110 & 2.755 & 2.733 & 70 & 1.168 & 1.248 \\
\hline -106 & 2.484 & 2.458 & 74 & 1.418 & 1.321 \\
\hline -102 & 2.303 & 2.245 & 78 & 1.231 & 1.162 \\
\hline -98 & 2.115 & 2.093 & 82 & 1.091 & 1.105 \\
\hline -94 & 1.873 & 1.829 & 86 & 1.083 & 1.240 \\
\hline -90 & 1.507 & 1.379 & 90 & 1.433 & 1.660 \\
\hline -86 & 1.130 & 1.064 & 94 & 1.863 & 2.024 \\
\hline -82 & 1.077 & 1.047 & 98 & 2.172 & 2.239 \\
\hline -78 & 1.152 & 1. 184 & 102 & 2.291 & 2.380 \\
\hline -74 & 1.390 & 1.357 & 106 & 2.503 & 2.580 \\
\hline -70 & 1.541 & 1.503 & 110 & 2.726 & 2.888 \\
\hline -66 & 1.607 & 1.613 & 114 & 2.958 & 2.965 \\
\hline -62 & 1.716 & 1.660 & 118 & 2.984 & 2.939 \\
\hline -58 & 1.832 & 1.756 & 122 & 2.754 & 2.554 \\
\hline -54 & 1.907 & 1.870 & 126 & 2.372 & 2.110 \\
\hline -50 & 1.995 & 1.955 & 130 & 1.987 & 1.802 \\
\hline -46 & 1.996 & 2.012 & 134 & 1.719 & 1.573 \\
\hline -42 & 2.077 & 2.069 & 138 & 1.513 & 1.409 \\
\hline -38 & 2.130 & 2.096 & 142 & 1.386 & 1.366 \\
\hline -34 & 2.118 & 2.199 & 146 & 1.348 & 1.349 \\
\hline -30 & 2.175 & 2.236 & 150 & 1.354 & 1.420 \\
\hline -26 & 2.228 & 2.295 & 154 & 1.415 & 1.481 \\
\hline -22 & 2.236 & 2.314 & 158 & 1.487 & 1.556 \\
\hline -18 & 2.255 & 2.291 & 162 & 1.596 & 1.662 \\
\hline -14 & 2.290 & 2.362 & 166 & 1.670 & 1.740 \\
\hline -10 & 2.317 & 2.378 & 170 & 1.773 & 1.838 \\
\hline -6 & 2.333 & 2.402 & 174 & 1.864 & 1.901 \\
\hline -2 & 2.310 & 2.392 & 178 & 1.854 & 1.919 \\
\hline
\end{tabular}
\(T U=2.651 \%, L / D=0.030, \mathrm{RE}=110000, \mathrm{ST}=0.0781\)
(FIG 49)
MULTIPLIER=0. 20449 MIL
LOSS CORRECTION=0.083 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \(\mathrm{SH} / \mathrm{VRE}^{\prime \prime}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & DEG & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) & \(\mathrm{SH} / \sqrt{R E}\) \\
\hline & \(2=-.5^{\prime \prime}\) & \(2=+.51\) & & \(z=-.5^{\prime \prime}\) & \(z=+.5^{\prime \prime}\) \\
\hline -176 & 1.903 & 1.966 & 4 & 2.206 & 2.262 \\
\hline -172 & 1.875 & 1.942 & 8 & 2.196 & 2.261 \\
\hline -168 & 1.830 & 1.851 & 12 & 2.192 & 2.249 \\
\hline -164 & 1.740 & 1.740 & 16 & 2.196 & 2.244 \\
\hline -160 & 1.616 & 1.680 & 20 & 2.176 & 2.194 \\
\hline -156 & 1.529 & 1.587 & 24 & 2.157 & 2.181 \\
\hline -152 & 1.439 & 1.496 & 28 & 2.106 & 2.135 \\
\hline -148 & 1.413 & 1.458 & 32 & 2.050 & 2.103 \\
\hline -144 & 1.415 & 1.437 & 36 & 2.051 & 2.056 \\
\hline -140 & 1.522 & 1.559 & 40 & 1.988 & 1.997 \\
\hline -136 & 1.640 & 1.630 & 44 & 1.939 & 1.931 \\
\hline -132 & 1.835 & 1.802 & 48 & 1.880 & 1.892 \\
\hline -128 & 2.094 & 2.089 & 52 & 1.780 & 1.818 \\
\hline -124 & 2.484 & 2.381 & 56 & 1.755 & 1.697 \\
\hline -120 & 2.827 & 2.781 & 60 & 1.681 & 1.669 \\
\hline -116 & 3.008 & 3.003 & 64 & 1.570 & 1.566 \\
\hline -112 & 2.872 & 2.951 & 68 & 1.471 & 1.457 \\
\hline -108 & 2.636 & 2.750 & 72 & 1.315 & 1.307 \\
\hline -104 & 2.417 & 2.475 & 76 & 1.152 & 1.120 \\
\hline -100 & 2.190 & 2.247 & 80 & 1.027 & 1.034 \\
\hline -96 & 2.038 & 2.071 & 84 & 1.082 & 1.166 \\
\hline -92 & 1.739 & 1.786 & 88 & 1.409 & 1.502 \\
\hline -88 & 1.351 & 1.439 & 92 & 1.788 & 1.869 \\
\hline -84 & 1.081 & 1.135 & 96 & 2.047 & 2.076 \\
\hline -80 & 1.038 & 1.030 & 100 & 2.225 & 2.305 \\
\hline -76 & 1.173 & 1.117 & 104 & 2.421 & 2.498 \\
\hline -72 & 1.342 & 1.306 & 108 & 2.644 & 2.770 \\
\hline -68 & 1.484 & 1.447 & 112 & 2.932 & 3.048 \\
\hline -64 & 1.607 & 1.571 & 116 & 3.053 & 2.994 \\
\hline -60 & 1.645 & 1.639 & 120 & 2.796 & 2.707 \\
\hline -56 & 1.744 & 1.719 & 124 & 2.415 & 2.393 \\
\hline -52 & 1.819 & 1.798 & 128 & 2.041 & 2.059 \\
\hline -48 & 1.896 & 1.868 & 132 & 1.800 & 1.823 \\
\hline -44 & 1.944 & 1.942 & 136 & 1.603 & 1.635 \\
\hline -40 & 1.989 & 1. 992 & 140 & 1.476 & 1.504 \\
\hline -36 & 2.056 & 2.040 & 144 & 1.410 & 1.437 \\
\hline -32 & 2.087 & 2.108 & 148 & 1.425 & 1.417 \\
\hline -28 & 2.091 & 2.138 & 152 & 1.476 & 1.477 \\
\hline -24 & 2.147 & 2.152 & 156 & 1.520 & 1.549 \\
\hline -20 & 2.183 & 2.214 & 160 & 1.649 & 0.0 \\
\hline -16 & 2.211 & 2.225 & 164 & 1.678 & 0.0 \\
\hline -12 & 2.218 & 2.248 & 168 & 1.752 & 1.758 \\
\hline -8 & 2.221 & 2.228 & 172 & 1.864 & 1.981 \\
\hline -4 & 2.249 & 2.252 & 176 & 1.906 & 1.990 \\
\hline 0 & 2.208 & 2.248 & 180 & 1.934 & 2.029 \\
\hline
\end{tabular}
\(\mathrm{TU}=4.9 \%, \mathrm{~L} / \mathrm{D}=0.188, \mathrm{RE}=110000, \mathrm{ST}=0.0\)
MULTIPLIER=0.23086 /MIL
LOSS CORRECTION \(=0.035\) MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/ \(\sqrt{\text { RE }}\) & \(\mathrm{SH} / \sqrt{\text { RE }}\) & DEG & \(\mathrm{SH} / \sqrt{R E}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) \\
\hline & \(\mathrm{z}=-.5^{\prime \prime}\) & \(Z=+.51\) & & \(\mathrm{Z}=-.5^{\prime \prime}\) & \(2=+.5^{\prime \prime}\) \\
\hline -176 & 1.839 & 1.987 & 4 & 1.987 & 2.000 \\
\hline -172 & 1.737 & 1.927 & 8 & 1.977 & 1.999 \\
\hline -168 & 1.673 & 1.835 & 12 & 1.973 & 1.987 \\
\hline -164 & 1.515 & 1.696 & 16 & 1.963 & 1.981 \\
\hline -160 & 1.419 & 1.551 & 20 & 1.928 & 1.960 \\
\hline -156 & 1.290 & 1.341 & 24 & 1.922 & 1.932 \\
\hline -152 & 1.213 & 1.333 & 28 & 1.885 & 1.900 \\
\hline -148 & 1.194 & 1.281 & 32 & 1.846 & 1.890 \\
\hline -144 & 1.263 & 1.312 & 36 & 1.829 & 1.832 \\
\hline -140 & 1.418 & 1.425 & 40 & 1.772 & 1.745 \\
\hline -136 & 1.626 & 1.632 & 44 & 1.723 & 1.747 \\
\hline -132 & 1.887 & 1.898 & 48 & 1.680 & 1.647 \\
\hline -128 & 2.212 & 2.207 & 52 & 1.612 & 1.613 \\
\hline -124 & 2.550 & 2.583 & 56 & 1.548 & 1.567 \\
\hline -120 & 2.977 & 3.058 & 60 & 1.475 & 1.478 \\
\hline -116 & 3.575 & 3.453 & 64 & 1.407 & 1.425 \\
\hline -112 & 3.429 & 3.880 & 68 & 1.340 & 1.348 \\
\hline -108 & 3.523 & 3.444 & 72 & 1.263 & 1.284 \\
\hline -104 & 2.335 & 2. 696 & 76 & 1.162 & 1.188 \\
\hline -100 & 1.089 & 1.350 & 80 & 1.001 & 1.058 \\
\hline -96 & 0.519 & 0.586 & 84 & 0.875 & 0.883 \\
\hline -92 & 0.543 & 0.484 & 88 & 0.707 & 0.659 \\
\hline -88 & 0.785 & 0.713 & 92 & 0.553 & 0.469 \\
\hline -84 & 0.931 & 0.917 & 96 & 0.725 & 0.740 \\
\hline -80 & 1.055 & 1.078 & 100. & 1.752 & 1.697 \\
\hline -76 & 1.262 & 1.204 & 104 & 3.080 & 3.091 \\
\hline -72 & 1.309 & 1.290 & 108 & 3.743 & 3.959 \\
\hline -68 & 1.366 & 1.347 & 112 & 3.536 & 3.831 \\
\hline -64 & 1.434 & 1.428 & 116 & 3.078 & 3.372 \\
\hline -60 & 1.504 & 1.506 & 120 & 2.670 & 2.924 \\
\hline -56 & 1. 565 & 1.573 & 124 & 2.219 & 2.476 \\
\hline -52 & 1.617 & 1.616 & 128 & 1.887 & 2.124 \\
\hline -48 & 1.681 & 1.669 & 132 & 1.574 & 1.797 \\
\hline -44 & 1.728 & 1.719 & 136 & 1.370 & 1.564 \\
\hline -40 & 1.781 & 1.767 & 140 & 1.218 & 1.389 \\
\hline -36 & 1.827 & 1.771 & 144 & 1.124 & 1.265 \\
\hline -32 & 1.900 & 1.804 & 148 & 1.097 & 1.247 \\
\hline -28 & 1.908 & 1.875 & 152 & 1.129 & 1.273 \\
\hline -24 & 1.931 & 1.915 & 156 & 1.243 & 1.396 \\
\hline -20 & 1.958 & 1.902 & 160 & 1. 401 & 1.539 \\
\hline -16 & 1.972 & 1.960 & 164 & 1.531 & 1.678 \\
\hline -12 & 1.973 & 1.956 & 168 & 1.666 & 1.813 \\
\hline -8 & 1.974 & 1.995 & 172 & 1.768 & 1.907 \\
\hline -4 & 1.984 & 1.987 & 176 & 1.840 & 1.958 \\
\hline 0 & 1.988 & 2.015 & -180 & 1.860 & 2.010 \\
\hline
\end{tabular}
\(T U=4.9 \%\), \(\mathrm{L} / \mathrm{D}=0.188, \mathrm{RE}=110000, \mathrm{ST}=0.0071\) MULTIPLIER=0.23546 /MIL

LOSS CORRECTION=0.024 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{n}
\end{gathered}
\] & \[
\begin{aligned}
& S H / \sqrt{R E} \\
& Z=+.5^{\prime \prime}
\end{aligned}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
Z=+.5^{\prime \prime}
\end{gathered}
\] \\
\hline -178 & 1.724 & 1.780 & 2 & 1.983 & 1.991 \\
\hline -174 & 1.714 & 1.786 & 6 & 1.965 & 1.990 \\
\hline -170 & 1.673 & 1.758 & 10 & 1.966 & 1.983 \\
\hline -166 & 1.617 & 1.745 & 14 & 1.948 & 1.971 \\
\hline -162 & 1.554 & 1.583 & 18 & 1.933 & 1.951 \\
\hline -158 & 1.446 & 1.500 & 22 & 1.907 & 1.930 \\
\hline -154 & 1.369 & 1.410 & 26 & 1.877 & 1.890 \\
\hline -150 & 1.312 & 1.347 & 30 & 1.838 & 1.870 \\
\hline -146 & 1.274 & 1.328 & 34 & 1.800 & 1.824 \\
\hline -142 & 1.299 & 1.364 & 38 & 1.771 & 1.808 \\
\hline -138 & 1.375 & 1.418 & 42 & 1.727 & 1.777 \\
\hline -134 & 1.610 & 1.567 & 46 & 1.683 & 1.730 \\
\hline -130 & 1.757 & 1.832 & 50 & 1.637 & 1.658 \\
\hline -126 & 2.052 & 2.105 & 54 & 1.583 & 1.624 \\
\hline -122 & 2.385 & 2.457 & 58 & 1.523 & 1.557 \\
\hline -118 & 2.703 & 2.817 & 62 & 1.450 & 1.512 \\
\hline -114 & 2.786 & 2.988 & 66 & 1.409 & 1.449 \\
\hline -110 & 2.549 & 2.766 & 70 & 1.324 & 1.349 \\
\hline -106 & 2.330 & 2.524 & 74 & 1.234 & 1.263 \\
\hline -102 & 2.093 & 2.256 & 78 & 1.132 & 1.143 \\
\hline -98 & 1.864 & 2.057 & 82 & 0.974 & 1.021 \\
\hline -94 & 1.543 & 1.728 & 86 & 0.871 & 0.881 \\
\hline -90 & 1.108 & 1.256 & 90 & 0.877 & 0.851 \\
\hline -86 & 0.838 & 0.900 & 94 & 1.111 & 1.053 \\
\hline -82 & 0.862 & 0.844 & 98 & 1.493 & 1.434 \\
\hline -78 & 0.941 & 0.953 & 102 & 1.877 & 1.851 \\
\hline -74 & 1.109 & 1.103 & 106 & 2.088 & 2.151 \\
\hline -70 & 1.215 & 1.226 & 110 & 2.330 & 2.378 \\
\hline -66 & 1.329 & 1.321 & 114 & 2.576 & 2.619 \\
\hline -62 & 1.435 & 1.410 & 118 & 2.832 & 2.864 \\
\hline -58 & 1.491 & 1.454 & 122 & 2.898 & 2.916 \\
\hline -54 & 1.558 & 1.529 & 126 & 2.636 & 2.724 \\
\hline -50 & 1.621 & 1.564 & 130 & 2.226 & 2.389 \\
\hline -46 & 1.667 & 1.646 & 134 & 1.984 & 2.102 \\
\hline -42 & 1.739 & 1.682 & 138 & 1.684 & 1.726 \\
\hline -38 & 1.779 & 1.743 & 142 & 1.489 & 1.500 \\
\hline -34 & 1.818 & 1.781 & 146 & 1.346 & 1.341 \\
\hline -30 & 1.859 & 1.824 & 150 & 1.294 & 1.336 \\
\hline -26 & 1.893 & 1.860 & 154 & 1.263 & 1.283 \\
\hline -22 & 1.929 & 1.890 & 158 & 1.321 & 1.310 \\
\hline -18 & 1.944 & 1.929 & 162 & 1.374 & 1.395 \\
\hline . -14 & 1.959 & 1.960 & 166 & 1.462 & 1.512 \\
\hline -10 & 1.969 & 1.974 & 170 & 1.565 & 1.586 \\
\hline -6 & 1.975 & 1.978 & 174 & 1.679 & 1.696 \\
\hline -2 & 1.982 & 1.997 & 178 & 1.707 & 1.745 \\
\hline
\end{tabular}
\(T U=4.9 \%, L / D=0.188, ~ R E=110000, ~ S T=0.0213\)
MULTIPLIER=0.20143 /MIL
LOSS CORRECTION=0.030 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
\mathrm{ZF}+. \mathrm{S}^{n}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime}
\end{gathered}
\] \\
\hline -176 & 1.761 & 1.873 & 4 & 1.983 & 2.011 \\
\hline -172 & 1.765 & 1.824 & 8 & 1.965 & 2.014 \\
\hline -168 & 1.696 & 1.781 & 12 & 1.971 & 2.004 \\
\hline -164 & 1.606 & 1.714 & 16 & 1.969 & 1.977 \\
\hline -160 & 1.512 & 1.602 & 20 & 1.946 & 1.976 \\
\hline -156 & 1.454 & 1.483 & 24 & 1.903 & 1.928 \\
\hline -152 & 1.353 & 1.427 & 28 & 1.896 & 1.895 \\
\hline -148 & 1.361 & 1.376 & 32 & 1.850 & 1.887 \\
\hline -144 & 1.362 & 1.348 & 36 & 1.836 & 1.846 \\
\hline -140 & 1.407 & 1.403 & 40 & 1.759 & 1.786 \\
\hline -136 & 1.524 & 1.528 & 44 & 1.722 & 1.733 \\
\hline -132 & 1.693 & 1.725 & 48 & 1.649 & 1.699 \\
\hline -128 & 1.979 & 1.995 & 52 & 1.605 & 1.662 \\
\hline -124 & 2.285 & 2.322 & 56 & 1.552 & 1.604 \\
\hline -120 & 2.642 & 2.670 & 60 & 1.594 & 1.540 \\
\hline -116 & 2.875 & 2.932 & 64 & 1.457 & 1.484 \\
\hline -112 & 2.723 & 2.831 & 68 & 1.377 & 1.407 \\
\hline -108 & 2.540 & 2.554 & 72 & 1.283 & 1.320 \\
\hline -104 & 2.183 & 2.309 & 76 & 1.213 & 1.231 \\
\hline -100 & 2.027 & 2.112 & 80 & 1.070 & 1.116 \\
\hline -96 & 1.772 & 1.835 & 84 & 0.951 & 0.971 \\
\hline -92 & 1.365 & 1.469 & 88 & 0.870 & 0.889 \\
\hline -88 & 1.023 & 1.068 & 92 & 1.002 & 1.012 \\
\hline -84 & 0.825 & 0.879 & 96 & 1.385 & 1.377 \\
\hline -80 & 0.896 & 0.893 & 100 & 1.796 & 1.824 \\
\hline -76 & 1.025 & 1.032 & 104 & 2.104 & 2.116 \\
\hline -72 & 1.084 & 1.126 & 108 & 2.221 & 2.321 \\
\hline -68 & 1.217 & 1.226 & 112 & 2.516 & 2.548 \\
\hline -64 & 1.314 & 1.318 & 116 & 2.790 & 2.790 \\
\hline -60 & 1.405 & 1.397 & 120 & 2.926 & 3.009 \\
\hline -56 & 1.464 & 1.447 & 124 & 2.792 & 2.842 \\
\hline -52 & 1.530 & 1.512 & 128 & 2.422 & 2.610 \\
\hline -48 & 1.567 & 1.660 & 132 & 2.074 & 2.236 \\
\hline -44 & 1.629 & 1.620 & 136 & 1.831 & 1.877 \\
\hline -40 & 1.681 & 1.675 & 140 & 1.613 & 1.650 \\
\hline -36 & 1.728 & 1.771 & 144 & 1.464 & 1.467 \\
\hline -32 & 1.795 & 1.782 & 148 & 1.350 & 1.367 \\
\hline -28 & 1.846 & 1.838 & 152 & 1.323 & 1.330 \\
\hline -24 & 1.911 & 1.872 & 156 & 1.363 & 1.349 \\
\hline -20 & 1.876 & 1.923 & 160 & 1.406 & 1.418 \\
\hline -16 & 1.921 & 1.952 & 164 & 1.489 & 1.523 \\
\hline -12 & 1.928 & 1.965 & 168 & 1.558 & 1:603 \\
\hline -8 & 1.960 & 1.926 & 172 & 1.631 & 1.708 \\
\hline -4 & 1.915 & 2.007 & 176 & 1.695 & 1.811 \\
\hline 0 & 1.999 & 2.022 & 180 & 1.750 & 1.848 \\
\hline
\end{tabular}
\(T U=4.9 \%\), \(L / D=0.188, ~ R E=110000, ~ S T=0.0355\)
MULTIPLIER=0.21068 /MIL
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
S H / \sqrt{R E} \\
Z=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{aligned}
& \mathrm{SH} / \sqrt{\mathrm{RE}} \\
& \mathrm{Z}=+.5^{\prime \prime}
\end{aligned}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=+.5^{\prime \prime}
\end{gathered}
\] \\
\hline -176 & 1.622 & 1.736 & 4 & 1.960 & 1.991 \\
\hline -172 & 1.605 & 1.759 & 8 & 1.931 & 1.986 \\
\hline -168 & 1.571 & 1.697 & 12 & 1.933 & 1.981 \\
\hline -164 & 1.504 & 1.616 & 16 & 1.933 & 1.974 \\
\hline -160 & 1.424 & 1.536 & 20 & 1.918 & 1.960 \\
\hline -156 & 1.358 & 1.440 & 24 & 1.896 & 1.941 \\
\hline -152 & 1.289 & 1.362 & 28 & 1.852 & 1.914 \\
\hline -148 & 1.229 & 1.318 & 32 & 1.833 & 1.889 \\
\hline -144 & 1.213 & 1.369 & 36 & 1.771 & 1.848 \\
\hline -140 & 1.227 & 1.333 & 40 & 1.752 & 1.811 \\
\hline -136 & 1.412 & 1.498 & 44 & 1.716 & 1.762 \\
\hline -132 & 1.656 & 1.657 & 48 & 1.685 & 1.720 \\
\hline -128 & 1.887 & 1.942 & 52 & 1.647 & 1.638 \\
\hline -124 & 2.225 & 2.277 & 56 & 1.587 & 1.585 \\
\hline -120 & 2.547 & 2.688 & 60 & 1.528 & 1.530 \\
\hline -116 & 2.762 & 2.891 & 64 & 1.448 & 1.441 \\
\hline -112 & 2.692 & 2.768 & 68 & 1.369 & 1.344 \\
\hline -108 & 2.516 & 2.529 & 72 & 1.286 & 1.255 \\
\hline -104 & 2.333 & 2.354 & 76 & 1.178 & 1.159 \\
\hline -100 & 2.068 & 2.157 & 80 & 1.077 & 1.135 \\
\hline -96 & 1.704 & 1.924 & 84 & 0.962 & 0.960 \\
\hline -92 & 1.212 & 1.532 & 88 & 0.931 & 0.858 \\
\hline -88 & 0.960 & 1.152 & 92 & 1.002 & 0.902 \\
\hline -84 & 0.906 & 0.877 & 96. & 1.235 & 1.172 \\
\hline -80 & 0.922 & 0.882 & 100 & 1.561 & 1.596 \\
\hline -76 & 1.058 & 1.042 & 104 & 1.984 & 1.950 \\
\hline -72 & 1.204 & 1.161 & 108 & 2.177 & 2.172 \\
\hline -68 & 1.304 & 1.281 & 112 & 2.411 & 2.312 \\
\hline -64 & 1.400 & 1.373 & 116 & 2.611 & 2.534 \\
\hline -60 & 1.484 & 1.426 & 120 & 2.769 & 2.772 \\
\hline -56 & 1.5 .48 & 1.504 & 124 & 2.737 & 2.786 \\
\hline -52 & 1.649 & 1.596 & 128 & 2.601 & 2.479 \\
\hline -48 & 1.674 & 1.679 & 132 & 2.130 & 2.107 \\
\hline -44 & 1.733 & 1.728 & 136 & 1.806 & 1.888 \\
\hline -40 & 1.766 & 1.789 & 140 & 1.591 & 1.563 \\
\hline -36 & 1.803 & 1.827 & 144 & 1.394 & 1.372 \\
\hline -32 & 1.862 & 1.873 & 148 & 1.248 & 1.297 \\
\hline -28 & 1.861 & 1.900 & 152 & 1.229 & 1.201 \\
\hline -24 & 1.885 & 1.919 & 156 & 1.232 & 1.269 \\
\hline -20 & 1.906 & 1.939 & 160 & 1.264 & 1.333 \\
\hline -16 & 1.961 & 1.958 & 164 & 1.310 & 1.406 \\
\hline -12 & 1.958 & 1.972 & 168 & 1.361 & 1.506 \\
\hline -8 & 1.963 & 1.981 & 172 & 1.411 & 1.601 \\
\hline -4 & 1.947 & 1.977 & 176 & 1.538 & 1.672 \\
\hline 0 & 1.952 & 1.999 & 180 & 1.579 & 1.730 \\
\hline
\end{tabular}
\(T U=4.9 \%, L / D=0.188, ~ R E=110000, ~ S T=0.0497\) MULTIPLIER=0. 20682 /MIL

LOSS CORRECTION=0.015 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & SH/VRE & \(\mathrm{SH} / \sqrt{\text { RE }}\) & DEG & \(\mathrm{SH} / \sqrt{\text { RE }}\) & \(\mathrm{SH} / \sqrt{\mathrm{RE}}\) \\
\hline & \(\mathrm{Z}=-.5^{\prime \prime}\) & \(\mathrm{Z}=+.5^{\prime \prime}\) & & \(Z=-.5^{\prime \prime}\) & \(Z=+.5^{\prime \prime}\) \\
\hline -176 & 1.749 & 1.816 & 4 & 2.030 & 2.031 \\
\hline -172 & 1.717 & 1.884 & 8 & 2.034 & 2.026 \\
\hline -168 & 1.671 & 1.786 & 12 & 2.025 & 2.014 \\
\hline -164 & 1.610 & 1.721 & 16 & 2.003 & 2.011 \\
\hline -160 & 1.538 & 1.647 & 20 & 1.991 & 1.991 \\
\hline -156 & 1.471 & 1.545 & 24 & 1.965 & 1.957 \\
\hline -152 & 1.411 & 1.470 & 28 & 1.943 & 1.915 \\
\hline -148 & 1.432 & 1.435 & 32 & 1.927 & 1.868 \\
\hline -144 & 1.460 & 1.419 & 36 & 1.884 & 1.861 \\
\hline -140 & 1.411 & 1.463 & 40 & 1.851 & 1.836 \\
\hline -136 & 1.532 & 1.593 & 44 & 1.791 & 1.768 \\
\hline -132 & 1.828 & 1.794 & 48 & 1.716 & 1.713 \\
\hline -128 & 2.084 & 2.042 & 52 & 1.656 & 1.668 \\
\hline -124 & 2.458 & 2.542 & 56 & 1.581 & 1.642 \\
\hline -120 & 2.722 & 2.704 & 60 & 1.490 & 1.545 \\
\hline -116 & 2.846 & 2.966 & 64 & 1.387 & 1.478 \\
\hline -112 & 2.841 & 2.851 & 68 & 1.303 & 1.410 \\
\hline -108 & 2.685 & 2.667 & 72 & 1.232 & 1.330 \\
\hline -104 & 2.432 & 2.418 & 76 & 1.127 & 1.196 \\
\hline -100 & 2.111 & 2.182 & 80 & 1.033 & 1.092 \\
\hline -96 & 1.821 & 1. 967 & 84 & 0.938 & 0.939 \\
\hline -92 & 1.605 & 1.618 & 88 & 0.897 & 0.881 \\
\hline -88 & 1.079 & 1.176 & 92 & 0.972 & 1.028 \\
\hline -84 & 0.921 & 0.934 & 96 & 1.204 & 1.382 \\
\hline -80 & 0.963 & 0.902 & 100 & 1.674 & 1.822 \\
\hline -76 & 1.070 & 1.030 & 104 & 1.957 & 2.011 \\
\hline -72 & 1.185 & 1.179 & 108 & 2.381 & 2.221 \\
\hline -68 & 1.287 & 1.306 & 112 & 2.565 & 2.482 \\
\hline -64 & 1.405 & 1.385 & 116 & 2.693 & 2.721 \\
\hline -60 & 1.492 & 1.474 & 120 & 2.697 & 2.914 \\
\hline -56 & 1.561 & 1.520 & 124 & 2.596 & 2.866 \\
\hline -52 & 1.634 & 1.595 & 128 & 2.253 & 2.481 \\
\hline -48 & 1.694 & 1.679 & 132 & 1.972 & 2.144 \\
\hline -44 & 1.741 & 1.708 & 136 & 1.727 & 1.859 \\
\hline -40 & 1.793 & 1.752 & 140 & 1.588 & 1.607 \\
\hline -36 & 1.830 & 1.819 & 144 & 1.445 & 1.485 \\
\hline -32 & 1.886 & 1.837 & 148 & 1.354 & 1.361 \\
\hline -28 & 1.910 & 1.887 & 152 & 1.330 & 1.321 \\
\hline -24 & 1.953 & 1.918 & 156 & 1.378 & 1.356 \\
\hline -20 & 2.000 & 1.963 & 160 & 1.475 & 1.415 \\
\hline -16 & 2.016 & 1.967 & 164 & 1. 541 & 1.504 \\
\hline -12 & 2.021 & 2.022 & 168 & 0.0 & 1.656 \\
\hline -8 & 2.030 & 2.002 & 172 & 0.0 & 1.718 \\
\hline -4 & 2.032 & 2.033 & 176 & 1.736 & 1.799 \\
\hline 0 & 2.041 & 2.028 & 180 & 1.764 & 1.815 \\
\hline
\end{tabular}
\(\mathrm{TU}=4.9 \%\), \(\mathrm{L} / \mathrm{D}=0.188, \mathrm{RE}=110000, \mathrm{ST}=0.0639\)
MULTIPLIER=0.22453 /MIL
LOSS CORRECTION=0.020 MILS
\begin{tabular}{|c|c|c|c|c|c|}
\hline DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
\mathrm{Z}=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
Z=+.5^{\prime \prime}
\end{gathered}
\] & DEG & \[
\begin{gathered}
\mathrm{SH} / \sqrt{R E} \\
Z=-.5^{\prime \prime}
\end{gathered}
\] & \[
\begin{gathered}
\mathrm{SH} / \sqrt{\mathrm{RE}} \\
Z=+.5^{\prime \prime}
\end{gathered}
\] \\
\hline -176 & 1.764 & 1.766 & 4 & 1.984 & 1.983 \\
\hline -172 & 1.749 & 1.755 & 8 & 1.986 & 1.966 \\
\hline -168 & 1.690 & 1.703 & 12 & 1.984 & 1.947 \\
\hline -164 & 1.634 & 1.659 & 16 & 1.975 & 1.942 \\
\hline -160 & 1.542 & 1.574 & 20 & 1.946 & 1.921 \\
\hline -156 & 1.453 & 1.441 & 24 & 1.913 & 1.967 \\
\hline -152 & 1.382 & 1.378 & 28 & 1.858 & 1.854 \\
\hline -148 & 1.324 & 1.288 & 32 & 1.833 & 1.840 \\
\hline -144 & 1.354 & 1.343 & 36 & 1.797 & 1.815 \\
\hline -140 & 1.403 & 1.392 & 40 & 1.760 & 1.759 \\
\hline -136 & 1.524 & 1.556 & 44 & 1.711 & 1.723 \\
\hline -132 & 1.722 & 1.732 & 48 & 1.655 & 1.672 \\
\hline -128 & 1.996 & 2.078 & 52 & 1.603 & 1.627 \\
\hline -124 & 2.323 & 2.311 & 56 & 1.557 & 1.528 \\
\hline -120 & 2.669 & 2.748 & 60 & 1.491 & 1.447 \\
\hline -116 & 2.919 & 2.973 & 64 & 1.409 & 1.415 \\
\hline -112 & 2.708 & 2.871 & 68 & 1.348 & 1.345 \\
\hline -108 & 2.544 & 2.608 & 72 & 1.287 & 1.282 \\
\hline -104 & 2.207 & 2.360 & 76 & 1.167 & 1.171 \\
\hline -100 & 2.045 & 2.097 & 80 & 1.086 & 1.072 \\
\hline -96 & 1.889 & 1.930 & 84 & 0.941 & 0.918 \\
\hline -92 & 1.415 & 1.567 & 88 & 0.795 & 0.859 \\
\hline -88 & 1.034 & 1.139 & 92 & 0.902 & 0.966 \\
\hline -84 & 0.858 & 0.909 & 96 & 1.254 & 1.295 \\
\hline -80 & 1.008 & 0.896 & 100 & 1.625 & 1.736 \\
\hline -76 & 1.131 & 1.003 & 104 & 1.996 & 2.026 \\
\hline -72 & 1.248 & 1.161 & 108 & 2.192 & 2.224 \\
\hline -68 & 1.331 & 1.264 & 112 & 2.393 & 2.428 \\
\hline -64 & 1.412 & 1.356 & 116 & 2.582 & 2.684 \\
\hline -60 & 1.471 & 1.434 & 120 & 2.801 & 2.903 \\
\hline -56 & 1.536 & 1.495 & 124 & 2.695 & 2.863 \\
\hline -52 & 1.603 & 1.563 & 128 & 2.399 & 2.590 \\
\hline -48 & 1.654 & 1.628 & 132 & 2.075 & 2.223 \\
\hline -44 & 1.670 & 1.679 & 136 & 1.759 & 1.892 \\
\hline -40 & 1.763 & 1.714 & 140 & .1.535 & 1.646 \\
\hline -36 & 1.791 & 1.750 & 144 & 1.395 & 1.468 \\
\hline -32 & 1.831 & 1.814 & 148 & 1.229 & 1.573 \\
\hline -28 & 1.865 & 1.802 & 152 & 1.287 & 1.329 \\
\hline -24 & 1.899 & 1.850 & 156 & 1.304 & 1.368 \\
\hline -20 & 1.917 & 1.892 & 160 & 1.345 & 1.395 \\
\hline -16 & 1.921 & 1.921 & 164 & 1.440 & 1.466 \\
\hline -12 & 1.953 & 1.940 & 168 & 1.541 & 1.548 \\
\hline -8 & 1.990 & 1.957 & 172 & 1.626 & 1.633 \\
\hline -4 & 1.993 & 1.965 & 176 & 1.703 & 1.717 \\
\hline 0 & 1.998 & 1.981 & -180 & 1.760 & 1.767 \\
\hline
\end{tabular}

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#### Abstract

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[^0]:    As will be discussed in the analogy section, the boundary condition $v=0$ is an approximation.

[^1]:    ${ }^{*}$ For this purpose it was necessary to replace the original single turn pot with a 10 turn pot.

[^2]:    cylinder
    ahead of test
    
    Figure 73.

[^3]:    Streamwise distribution of averaged turbulence
    
    $\stackrel{0}{2}$
    Figure

