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CONTRIBUTION TO THE PERFORMANCE DETERMINATION
OF MICROJETS

Dieter Hayn

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16. Abstract Theoretical investigations are made on the performance of microjets, and a description is given of experiments with micropropulsion units to correlate the results obtained in the first part of the report. Execution of performance measurements is discussed, and error calculations are presented.			
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CONTRIBUTION TO THE PERFORMANCE
DETERMINATION OF MICROJETS

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P R E F A C E

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Dieter Hayn

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SYMBOLS AND ABBREVIATIONS USED

A	= Surface area
a	= velocity of sound
b	= characteristic width
bl	= boundary layer
C_F	= thrust coefficient
c	= velocity
c^*	= characteristic velocity
c_{eff}	= effective discharge velocity
c_f	= thrust stress coefficient
F	= thrust; force
GEO	= geostationary orbit (24 hour orbit)
g_0	= acceleration due to gravity
Hz	= vibrations per second
h	= enthalpy
i	= inclination
I	= impulse
LEO	= <u>low Earth orbit</u>
M	= Mach number
m	= instantaneous mass of the gas storage container
m_{mol}	= molecular weight
\dot{m}	= Mass throughput
N_2	= molecular nitrogen (here purified)
Nu	= Nusselt number
n	= Direction of the normal (perpendicular) to a surface
ODE	= one-dimensional shifting equilibrium
ODF	= one-dimensional frozen equilibrium
ODK	= one-dimensional kinetic flow
Pr	= Prantl number
p	= pressure
R	= Special gas constant
\mathcal{R}	= general gas constant
Re	= Reynolds numerator
St	= Stanton number

s = coordinate tangential to the wall; entropy
T = temperature
TD = two-dimensional
TW = propulsive plant
t = time
v = velocity
x = nozzle axis coordinate
y = velocity distribution coordinate
z = altitude coordinate

Subscripts

acc = acceleration
ax = axial
c = combustion chamber
 c_D = constriction coefficient; throat throughput coefficient
ch = characteristic
D = drag
1-d = one-dimensional
2-d = two-dimensional
del = delivered
e = end cross-section; end condition
F = thrust
i = initial condition
inj = injector
lam = laminar
n/v = inviscid
r = radial
sp = specific
t = throat
tan = tangential
th = theoretical
turb = turbulent
ver = vertical
vis = viscous

W = balance
∞ = environment condition (vacuum chamber or laboratory)

Greek letters

α = heat transfer coefficient
 α_e = exit cone angle (divergent portion)
 α_i = exit cone angle (convergent portion)
 γ = isentropy exponent (c_p/c_v)
 δ = boundary layer thickness
 δ^* = displacement density
 δ_H = energy density
 ϵ = surface ratio; eccentricity
 η = viscosity
 θ = impulse loss density
 λ = thermal conductivity
 λ = geographical longitude
 μ = micro (10^{-6})
 ν = cinematic viscosity
 ρ = density
 τ = thrust stress
 χ = compressibility
 ψ = discharge coefficient
 Ω = rising node
 ω = rotation rate
 ∂ = differential operator

At the present time, the areas of application of communications satellites include national and international telephone connections, long-distance data transmission, radio and television signals, navigation for ships and aircraft, meteorological monitoring, satellite tracking and uses in development tasks.

The optimum orbit is determined by the task posed. Synchronous satellites occupy an exceptional position, since they travel in their orbit at the same angular velocity as Earth (geostationary orbits). If such an orbit occupies the equatorial plane, then the subsatellite point remains always over the same location on the Earth's surface: synchronous satellite.

But conditions along a satellite orbit are not as ideal as one could hope. Reality is far removed from the assumption of a dynamic two-body system that can in addition be represented by point masses. Hence a satellite suffers a series of distortions such as those caused by

- atmospheric resistance
- anisotropies in Earth's gravitational potential
- gravitational effects of other masses, especially the sun and the moon
- radiation pressure due to direct solar irradiation, Earth radiation and albedo, as well as the satellite's own radiation
- errors in the application of the control impulses
- discharge of refuse, degassing, uncontrolled fuel releases
- feedback coupling with attitude control systems
- interactions with the environment (cosmic radiation, the Earth's magnetic field, etc.)
- relativistic effects.

* Numbers in the right margin indicate foreign pagination

Under the effect of these disturbances the satellite is not going to maintain its anticipated orbit. In the case of geostationary satellites this means that the subsatellite point no longer remains stable in one location, but wanders in an uncontrolled manner.

Among the disturbing effects listed above, three have proven to be predominant, for geostationary satellites:

- 1) Anisotropy of the Earth's potential
- 2) Solar radiation pressure
- 3) Gravitational effects of the sun and the moon

Starting from the orbit distortions caused by these three influences, the velocity adjustment can be calculated that is necessary to return to the initial position, once the satellite has achieved a known deviation from that position [13,34,39,42-44,66,79,81,82, 85-87,93,98,110,129,131,152,164,166,173-175).

The Tables below provide a rough overview on the order of magnitude of the gravitational distortion due to other bodies, on the geostationary orbit, and of that due to solar radiation pressure:

**TABLE 1 GROSS ACCELERATIONS DUE TO GRAVITATIONAL FORCES,
OF BODIES IN THE PLANETARY SYSTEM, ON A SYNCHRONOUS
SATELLITE**

	<u>Acceleration (m/s²)</u>
Sun	5.931 x 10 ⁻³
Mercury	2.546 x 10 ⁻⁹
Venus	1.898 x 10 ⁻⁷
Earth	2.244 x 10 ⁻¹
Earth's moon	3.320 x 10 ⁻⁵
Mars	6.951 x 10 ⁻⁹
Jupiter	3.201 x 10 ⁻⁷
Saturn	2.324 x 10 ⁻⁸
Uranus	7.816 x 10 ⁻¹⁰
Neptune	3.708 x 10 ⁻¹⁰
Pluto	9.626 x 10 ⁻¹²

**TABLE 2 COMPARISON OF THE PERTURBING ACCELERATIONS DUE
TO SOLAR RADIATION PRESSURE AND DUE TO THE
GRAVITATION OF THE SUN AND MOON**

<u>Disturbance</u>	<u>Acceleration (m/s²)</u>
Solar gravitation	6.40 x 10 ⁻⁷
Grav. due to moon	2.44 x 10 ⁻⁶
Solar wind	
A/m = 2.05 m ² /kg	6.25 x 10 ⁻⁶
4.10	1.25 x 10 ⁻⁵
6.40	1.95 x 10 ⁻⁵
20.50	6.25 x 10 ⁻⁵

The distortions mentioned are calculated with the aid of the variation in orbit elements, even though at point 1 the validity of the numerically determined results is limited, since the higher terms describing the Earth's potential field are affected by large uncertainties. The Earth's potential anisotropy and the sun's radiation pressure essentially cause distortions only in the orbital plane, while the influence on changes in inclination in relation to point 3, above, can be neglected. /4

The consequence of equatorial ellipticity is a periodic motion around one of two stable points of the orbit, which are found on an extension of the equatorial ellipse's smaller semi-axis in both directions, at approximately 57° E and 123° W of geographical longitude. The largest distortions occur at a satellite position 45° away from such a stable point, attaining a radial deviation of ±41.7km and an overall E-W deviation of 90°. The distortion's period is approximately 580 days. Due to the Earth's flattening, the radius of a synchronous orbit is increased marginally, by approximately 0.5 km. However, this is not relevant to orbit control.

Orbit control becomes necessary when the satellite has reached a certain angular distance from its desired position. The return is accomplished by means of a classical Hohmann transition. The necessary velocity demand is independent of the number of control maneuvers but depends on the satellite's initial position with respect to the closest stable point. If this distance is 45°, then the velocity demand attains a maximum of

$$\Delta v_{\text{pot}} = 5.17 \text{ m/sec/yr.}$$

How large the distortion due to solar wind results for the satellite depends on the ratio of its cross-sectional area A and its mass m .

For $A/m = 10^{-3} \text{ m}^2/\text{kg}$, the maximum angular deviation from an arbitrary initial point is $\Delta\lambda = 0.25^\circ$ and a maximum radial deviation /5

is $r = 17.7$ km. If an angular deviation of 0.1° is allowed, as is customary with current communications satellites, then a yearly velocity demand of

$$\Delta v_{\text{sol}} = 3.75 \text{ m/sec/yr}$$

must be satisfied.

The gravitational forces of the sun and the moon (point 3) cause a distortion normal to the orbit's direction that becomes manifest as a change in inclination. This distortion has a period of $p = 53.6$ yr and a maximum deviation of 14.7 degrees. The initial change of inclination occurs at $\Delta i = 0.865^\circ/\text{yr}$. Applying a simple impulse, after a certain time and angular change the satellite is returned to its old position. During a five-year mission, with a permissible inclination change of 0.25° , the velocity demand is

$$\Delta v_{\text{grav}} = 48.55 \text{ m/sec/yr.}$$

By applying the "phase angle technique" this value can be reduced to

$$\Delta v_{\text{grav}} = 45.85 \text{ m/sec/yr.}$$

Normally orbital control is accomplished by means of chemical propulsion systems. This does not apply to the attitude control of geostationary satellites, which generally are equipped with a combined system of mechanical devices (gyroscopes) and reaction equipment. For this reason it is not possible to provide a precise value for the velocity demand for attitude control. At /6 a permissible deviation of 0.1° a realistic value of

$$\Delta v_{\text{att}} = 1 \text{ m/sec/yr}$$

may be assumed.

Thus, if a satellite is on a weakly elliptical orbit of inclination $i = 0$, on a synchronous Earth orbit, with an allowed longitudinal deviation of 0.1° and a 0.25° allowed lateral deflection, then a yearly velocity demand of at least

$$\Delta v_{\text{tot}} = 55.77 \text{ m/sec/yr}$$

must be provided for, assuming the orbital distortions are additive, in regard to the Δv due the sun, moon and Earth.

The requirement for high precision in maintaining a satellite's orbital position leads to the installation of orbit and attitude control systems.

Orbit control compensates for center-of-mass distortions, while the function of attitude control is to insure that the satellite retains its alignment with a certain target point. A system that satisfies both functions is highly desirable, but this goal has not been achieved, as yet.

In recent years a number of chemical and electrical [21,92,151] propulsion systems have been developed (as well as gyroscope systems for attitude control) and successfully installed in operational satellites. Many others are still in the planning stage. Consideration was also given to using the solar wind or the light pressure for orbit and attitude control. The extensive activities precisely in the field of control are not surprising, /7 since due to the high cost of space travels any possibility for savings must be taken advantage of.

One look at the basic equation of rocketry, $\Delta v = c_{\text{eff}} \cdot \ln (m_0/m_e)$ makes it very clear that for a given velocity demand and minimization of the fuel mass ($m_0 - m_e$), the highest possible exhaust velocity must be adopted. However, the consequent demand for the use of stable two-component systems of intermediate energy meets a series of technological restrictions: the required control

precision of the satellite with regard to orbit and attitude leads to the application of a large number of correction maneuvers with individual burning durations (typically 10,000 per year). Simultaneously, in order not to reduce the operating time per propulsion impulse to unrealistically brief periods of time, the propulsion unit's thrust must be correspondingly low. While for N/S corrections two-component systems can still be used (for instance, MBB propulsion unit at 10 Newton; $I_{sp} = 290$ sec), there are limits on miniaturization in the range of 0.5 to 2 N. Today, N_2H_4 single-component fuel systems are used here (without heating, $I_{sp} = 230$ sec; with electric heating: $I_{sp} = 295$ sec). Even smaller thrusts (50 mN), as required by precision attitude control, are accomplished by means of cold gas propulsion units (for instance, He of GN_2 [gaseous N_2]), since even the catalytic hydrazine devices can not be arbitrarily miniaturized. The low specific impulse of the engines (for nitrogen, typically 70 sec) forces an optimization of them with respect to combustion chamber pressure, expansion ratio, number of operating periods and overall consumption.

It is the purpose of this investigation to provide a contribution in this regard.

During the execution of the PAEHT study [56-63], the lack of computer programs adequate to precise performance prediction of chemical rocket propulsion units became very clear, in Europe [2,6,10,18,32,36,37,48,76,77,83,85,86,88,109,116,120,121,130,132,137,138,148,149,156,162]. The programs developed in the US /8 under the superordinate concept JANNAF Procedures (ODE, ODK, TDK, BLIMP) could be obtained but were only partially usable (not sufficiently) in Europe [16,22].

For these reasons the current study was initiated at the conclusion of the studies performed for the PAEHT Project by the Chair for Space Technology of the Technical University Munich.

The first main portion of the task consisted in the development of a simplified, explicit procedure for performance prediction, in the foreground, and the comparison with available theoretical results from the procedures mentioned above. On the basis of these results, the final objective was a collection of easily manipulated estimation formulas, such as those required in the design of rocket propulsion plants. Naturally, this also requires the corresponding comparisons with measured values. However, during the course of the studies already mentioned, considerable gaps were found also in the area of reliable, available performance measurement values for the case of small propulsion units as they are particularly in the foreground, here.

This gap is partially closed by means of the test program related to cold gas propulsion units, presented in Section 2.

2.1 Prediction by extrapolation of data from implemented propulsion units

There are two methods, in principle, for the prediction of performance parameters (not only of propulsion units) of future systems: extrapolation, starting from data of actually implemented equipment, or by determining the physical laws and interactions that govern the individual components.

The first of these requires extensive data collections for implemented systems, including parallel developments of different devices. Only thus can hasty judgements be prevented. The advantage of this way is that it is not necessary to delve very deeply into the individual systems and the physical laws that govern them, provided it is assured that the groups or companies participating have or had available the necessary experience. As applied to the chemical propulsion units (more especially, of low thrust) currently at the focus of our interest, however, the following serious problems occur, which we shall mention here only in terms of keywords:

- large numbers of different concepts
- few parallel developments
- To date, no large areas have been covered; rather, almost always special applications are placed in the foreground of a given development
- large differences in the technical implementation
- performance differences among participating groups
- insufficient documentation of the results.

For this reason we have preferred following the second way.

2.2 Performance prediction by determination of individual losses

/10

The starting point for the determination of individual losses in a rocket propulsion unit is the zero-loss, one-dimensional "shifting equilibrium" flow [ODE], whose performance values represent the upper theoretical limit. It is assumed that the gas composition corresponds in each case to the pressure and temperature conditions during expansion in the nozzle, and that the necessary reactions occur without delay time. The energy equation provides the isentropic exhaust velocity:

$$I_{sp,ODE,vac} g_0 = \sqrt{2(h_c - h_e)} \quad \text{with} \quad v_c = 0 \rightarrow \sqrt{2(c_{p,c} T_c - c_{p,e} T_e)} \quad (1)$$

However, in the real flow a series of performance-reducing factors occur, as a consequence of departure from the ideal conditions, $I_{sp,ODE,vac}$ (see also Figures 1, below and 2.1).

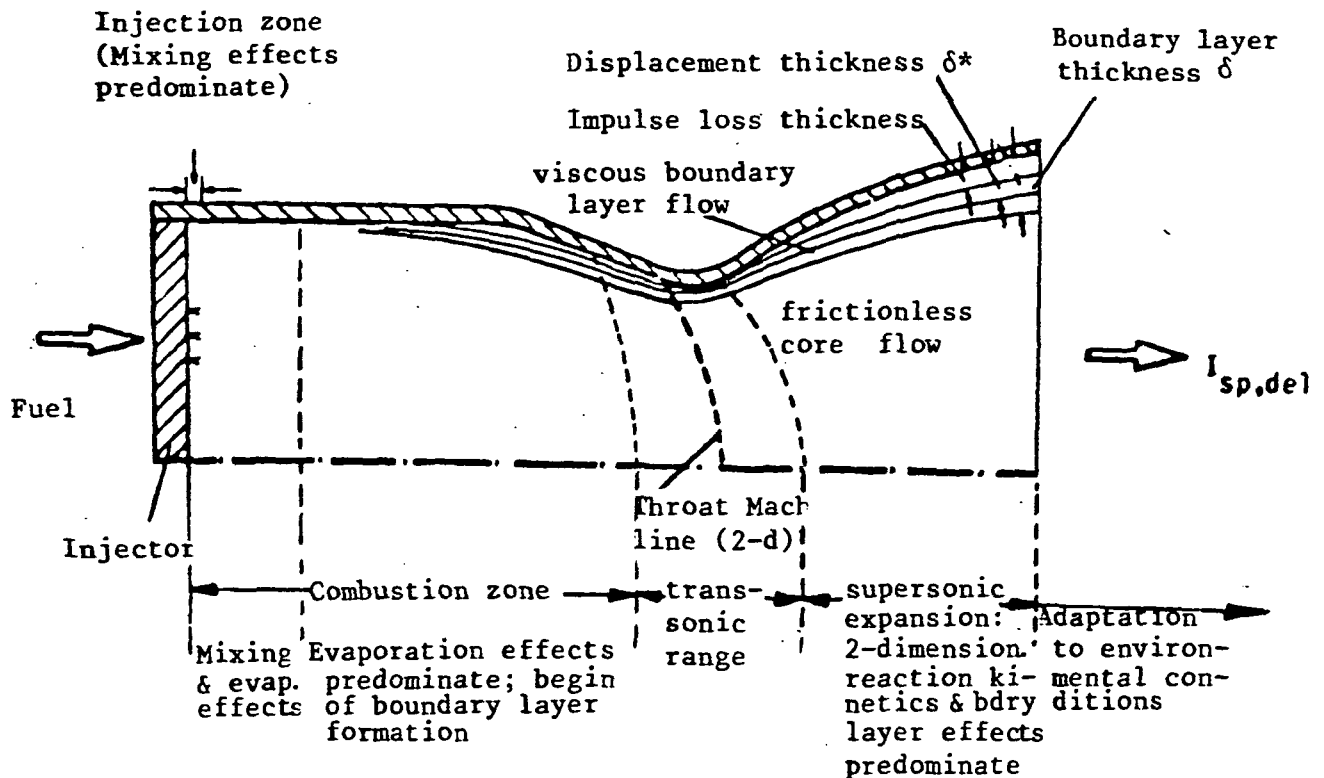


Figure 1 Processes in the combustion chamber and nozzle

$$I_{sp,del} = I_{sp,ODE,vac} \cdot \eta_{er} \cdot \eta_{kin} \cdot \eta_{part} \cdot \eta_{2-d,(3-d)} \cdot \eta_{bl} \cdot \eta_{adapt} \cdot \eta_h \quad (2)$$

2.2.1 Energy conversion in the combustion chamber

/11

The first efficiency term on the right side is called energy conversion efficiency (energy release) of the injector-combustion chamber system. In the general case of the chemical multi-component rocket propulsion unit it is not possible to obtain the total, theoretically possible energy yield, starting from the chemicals injected into the combustion chamber. Because of the finite dwell time in the combustion chamber ($v_c \neq 0$), incomplete mixing and fuel preparation, as well as due to technical implementation restrictions, η_{er} can not become equal to 1.0. However, implemented systems (SSME) today reach 0.997. Since here GN_2 occurs only as a single-component system and no reaction takes place, we can here set $\eta_{er} = 1.0$, however.

2.2.2 Kinetic efficiency

During the gas expansion process within the nozzle flow, the thermodynamically limiting parameters - such as T , p , ρ , λ , η - undergo significant changes and hence the combustion chamber conditions of the chemical condition ODE are no longer applicable. For instance, at high T_c dissociate molecules tend to recombine, as T decreases. Similarly, charged atoms and molecules (ions) are converted into neutral particles, by charge exchange. In addition, the state of excitation in the combustion chamber can initiate vibration processes in molecules, given a sufficiently high Δh . All of these phenomena have in common that if the pressure or the temperature of the working fluid decrease, given the availability of a sufficiently long period of time, recombination or respectively, a relaxation of the excited degrees of freedom would occur. However, if this time - which depends very critically

on the gas component's characteristics, in each case - is not made possible by assuming an infinitely large expansion velocity, then we refer to a one-dimensional frozen equilibrium [ODF]. It represents a lower theoretical chem-thermodynamic performance value, because the energy contained in the gas' dissociation, ionization and vibration is not available - in contrast to the ODE flow - for expansion work and hence, the required gas acceleration; rather, it is still contained in the gas stream beyond the nozzle, after leaving it, in the form of internal energy, without contributing positively to the thrust. In the "technical nozzle flow" the so-called ODK flow [one-dimensional kinetic equilibrium] always lies between ODE and ODF (see Figure 2.2). /12

Hence in general the dwell time is sufficient to include a part (but of course not all) of the difference $h(\text{ODE}-\text{ODF})$ in the expansion work. The lower kinetic performance value can be expressed as

$$I_{sp,ODF,vac} = \frac{c_{ODF}^* c_{F,ODF,vac}}{g_0} \quad (3)$$

Usually, to facilitate individual calculations, the total kinetic efficiency η_{kin} can be broken down into the product

$$\eta_{kin} = \eta_{k,dis} \cdot \eta_{k,ion} \cdot \eta_{k,vib} \quad (4)$$

At this point it must be recalled, in general, that in the area of chemical kinetics considerable gaps still exist in the sense of an applicable engineering approximation. For some very special cases (molecules or gases, respectively, at certain specific pressure and temperature conditions) there are indications, in the literature, on reaction and recombination constants, but the quantitative theoretical statements contradict each other [71] as well as the few available measurement results. As an example we shall consider only the simplest case of the biatomic gas N_2 in the excited state.

According to Landau and Teller [53] the energy exchange between /13 the vibrational and translational degrees of freedom can be described by means of the following linear differential equation (based on the model of the harmonic oscillator)

$$\frac{D e_v}{D t} = \frac{e_{v,Equi} - e_v}{\tau_v} \quad (5)$$

where e_v is the vibrational energy per unit mass of gas; $e_{v, equi}$ is the value of e_v when the molecule's vibration and translation are at equilibrium; and τ_v is the relaxation time for the exchange of vibrational and translational energy.

Assuming a Boltzmann distribution for the vibration energy steps, vibration temperatures T_v can be calculated for them and then e_v will be determined by

$$e_v = \frac{R h \nu}{k \mu_0 (e^{h\nu/kT_v} - 1)} \quad (6)$$

Hence τ_v can be derived using the local pressure p as parameter and compared to measured experimental data, for instance with the aid of Raman spectroscopy. The results of this comparison (the experiments were performed several times, by different authors) are a surprise until this day, and are still awaiting clarification. According to Landau-Teller the time τ_v would be higher by a factor of 70 than the measured relaxation time.

Sebacher hence foregoes a theoretically derived function and determined a compensating function adapted purely to empirical values:

$$\tau_v p = 3 \cdot 10^{-12} e^{(181 T^{-1/3})} \text{ (bar sec)} \quad (7) \quad /14$$

which here is typically 10 sec (T is the absolute gas temperature, here, NOT to be confused with T_v above).

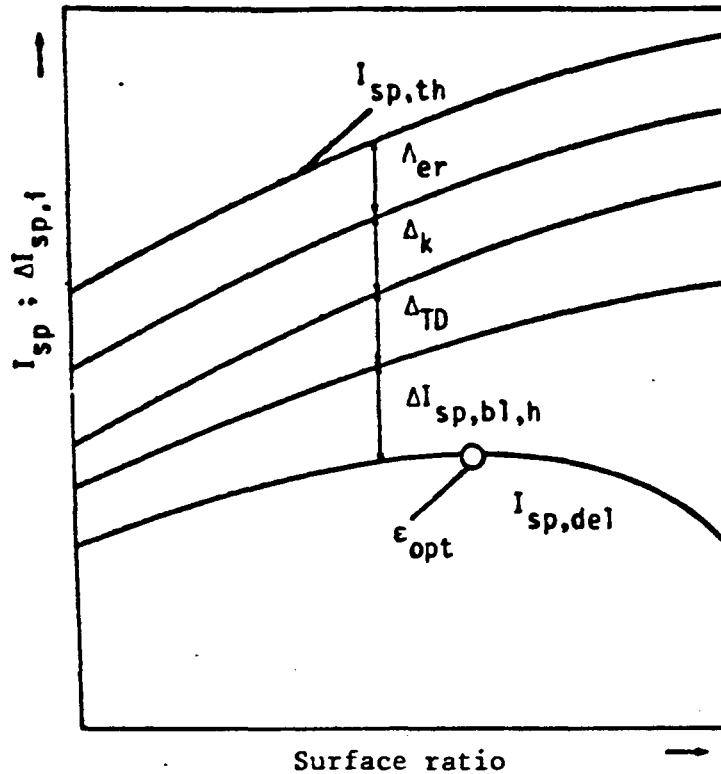


Figure 2.1 Qualitative course of the impulse, taking the various losses into consideration

Comparison with the residence time of the gas in the propulsion unit

$$t_{st} \approx \frac{1}{c^*} \left(\frac{\epsilon F}{p_c} \right)^{0,5} \rightarrow \text{typically } 10^{-5} \text{ sec} \quad (8)$$

shows that in practice the flow becomes "frozen" shortly behind the throat area, such that k_{reco} in the recombination equation

$$\eta_k = k_{reco} + \frac{I_{sp,ODF,vac}}{I_{sp,ODE,vac}} (1 - k_{reco}) \quad (9)$$

can be set equal to 0, and we thus finally arrive at $\eta_k = 1.0$ /15 for the case here under consideration.

This allows us to complete all remaining comparison calculations

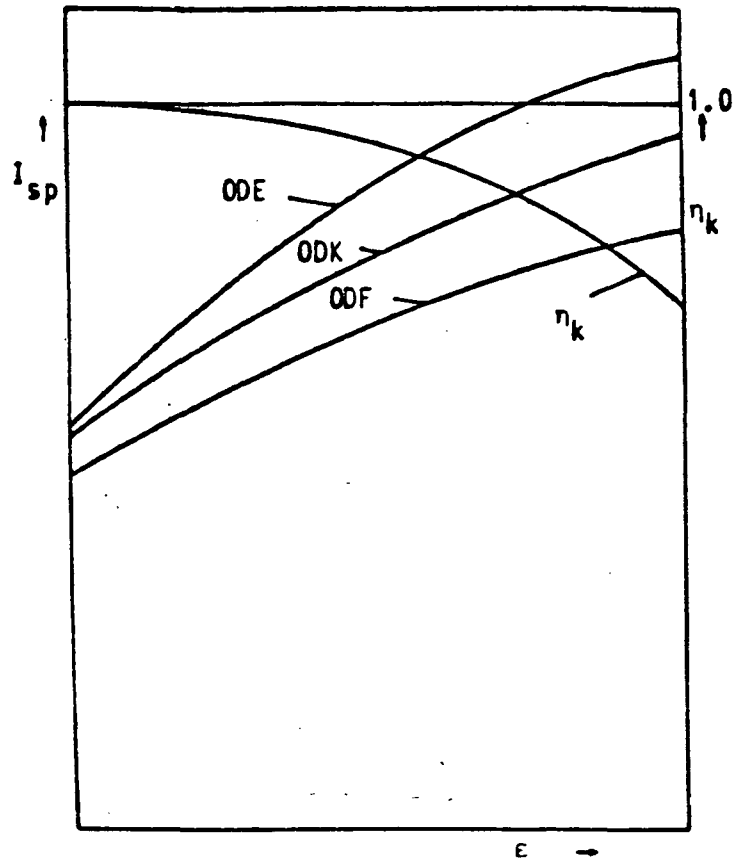


Figure 2.2 Qualitative courses of ODE, ODK and ODF impulses, as well as kinetic efficiency, as a function of the surface ratio [47]

with ODF parameters, which is very advantageous because then subsequent performance calculations can be separated from the kinetics problem. It is certain that also in the future chemical kinetics will considerably complicate total performance calculations for more complex gas combinations [33,91,112,125,138,157-160]

2.2.3 Particle flow

/16

In the case of the monopropulsion unit, gas particle flow as it occurs in modern solid fuel propulsion units (high A1 proportion), as well as condensed droplets, such as they occur in liquid fuel engines, do not take place. Nor was it possible to observe any wear in the galvanized nozzle wall (not even in the especially endangered throat region). Hence, $\eta_{part}=1.0$ shall be used.

2.2.4 Multidimensional flow losses

2.2.4.1 Divergence losses

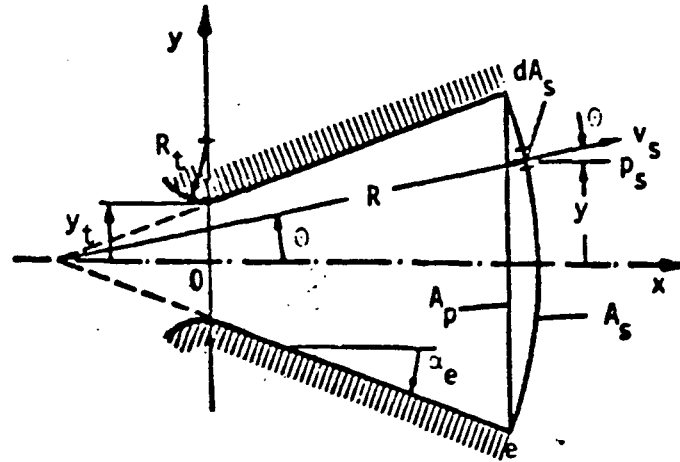


Figure 3 Geometry model to determine divergence losses

Due to radial divergence of the flowlines in the nozzle cross-section as well as the distribution of the velocity and pressure across the end cross-section surface area, there is an impulse loss (in relation to 1-d flow). (3-d effects, such as vortex formations due to asymmetry of the propulsion unit geometry, in general can be disregarded as very small). In the case of the bell nozzle, these multidimensional flow processes are usually numerically simulated by means of characteristics procedures [144]. In order to estimate TD losses in conical nozzles, however, the really rather voluminous computer programs are not necessary. Starting from a source flow (such as, for instance, the potential theory, [161]), the thrust fraction of the annular spherical surface element dA_s in Figure 3, above, [119,179] is

$$dF = \dot{m} v_s \cos \theta + (p_s - p_\infty) dA_s \cos \theta \quad (10) \quad /17$$

With $\dot{m} = \rho_s v_s dA_s$ and $dA_s = 2 \pi R^2 \sin \theta d\theta$ and integrating once,

$$F_{TD} = 2 \pi R^2 \int_0^{\alpha_e} \left[\rho_s v_s^2 + (p_s - p_\infty) \right] \cos \theta \sin \theta d\theta \quad (11)$$

Assuming that ρ_s , v_s and p_s are constant over the spherical surface A_s , and with

$$A_s = -2 \pi R^2 \cos \theta \Big|_0^{\alpha_e} = 2 \pi R^2 (1 - \cos \alpha_e) \quad (12)$$

$$(A_p = \pi R^2 \sin^2 \alpha_e)$$

equation (11) is rewritten as

$$F_{TD} = \left(\frac{1 + \cos \alpha_e}{2} \right) A_s [\rho_s v_s^2 + (p_s - p_\infty)] \quad (13)$$

With $\dot{m} = \rho_s A_s v_s$ the expression between brackets becomes

$$F_s = \dot{m} v_s + (p_s - p_\infty) A_s \quad (14)$$

F_s is the 1-dimensional thrust derived from the source flow model. The divergence factor η_{TD} corrects the 1-dimensional thrust taking into account the divergence losses and depends only on the opening angle α_e of the divergent portion of the nozzle: /18

$$\eta_{TD} = 0,5 (1 + \cos \alpha_e) \quad (15)$$

and hence

$$F_{TD} = \eta_{TD} F_s \quad (16)$$

With the aid of a Fortran program [144] available at the Chair for Space Technology it could be shown that the simplifying assumptions that led to the η_{TD} determined above for conical nozzles, are justified. The differences between the η_{TD} factor determined explicitly by means of the characteristics procedure and the simplified theory is less than 0.3% for a 15° conical nozzle [14,51,54,72,73,89,95,112,122-124,135,138,144,147,154,157].

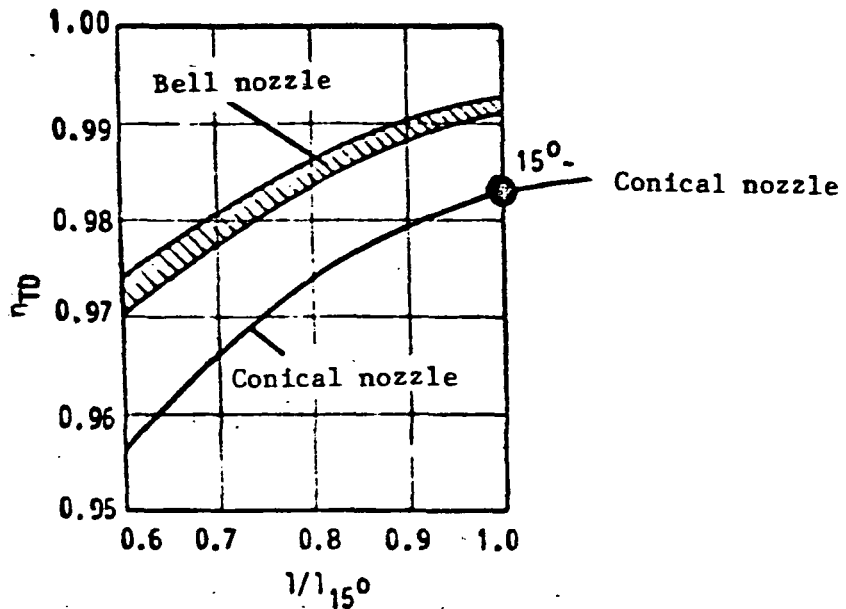


Figure 4 Two-dimensional flow losses for bell and conical nozzles as a function of normalized nozzle length

Figure 4, above, shows typical comparative results of the η_{TD} calculation for conical and bell nozzles.

2.2.4.2 Mass throughput reduction

/19

Because of constriction and boundary layer effects the actual mass throughput is reduced, with respect to \dot{m}_{ODE} .

In the LRT characteristics program already mentioned, a TD throat isobar is determined, starting from a Sauer-Nicholson procedure, which actually serves as a starting point for the entire procedure. It is not only possible to optimize the TD flow, thereby (including wall pressure distribution), but a TD- \dot{m} -efficiency can also be calculated, which usually lies between 0.993 and 0.996 (it does not include friction or boundary layer influences, yet). Based on the work of Back et al. [3-5], for instance, in addition the dependence of η_m^* on the throat's radius of curvature can be determined. The result is shown in Figure 5 (page 27), normalized with respect to r_t . It can be seen that the lowest \dot{m} loss occurs when the throat's transition radius r_r is equal to

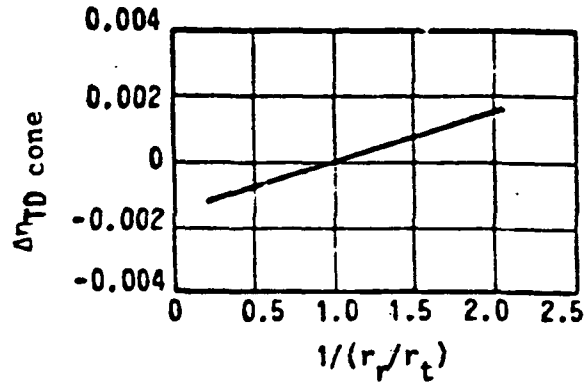


Figure 5. Effect of the throat transition radius r_r on the TD losses [27,69]

r_t . The most substantial decrease in the ODE mass flow can be attributed to viscous distortion effects, which "clog" the nozzle throat area.

Hall et al [53] proposed the following equations for discussion:

$$c_D = \frac{\dot{m}_v}{\dot{m}_{ODE}} = 1 - (\gamma + 1) \left(\frac{r_t}{r_r}\right)^2 \left[96 - \frac{8\gamma + 21}{4608} \left(\frac{r_t}{r_r}\right) + \frac{754\gamma^2 + 1971\gamma + 2007}{552960} \cdot \left(\frac{r_t}{r_r}\right)^2 - \dots \right] \quad (17)$$

Sauer, Oswatitsch and Rothstein[114,133,134] had already tried a similar equation, which does not require the second and third terms in the square bracket. Kuluva and Hosack [89] propose a somewhat different representation,

$$c_D = \left(\frac{r_r + 0,05 r_t}{r_r + 0,75 r_t}\right)^{0,019} \cdot \left[1 - \left(\frac{r_r + 0,1 r_t}{r_t}\right)^{0,21} \cdot \left(\frac{1}{Re}\right)^{0,5} \cdot f(\gamma) \right], \quad (18)$$

which in a second range, of $30 < Re < 10^5$ agrees well with the

experimental data. Figure 6, below, provides an overview; it

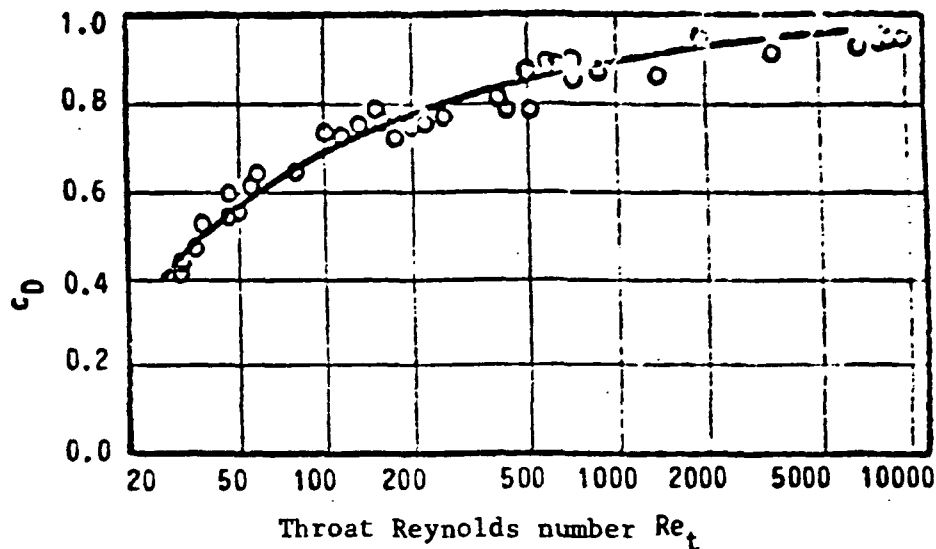


Figure 6 Mass throughput coefficient c_D as a function of Reynolds number in the throat. Experimental data: $r_T/r_t = 4.42$; $\gamma = 1.4$. Solid curve using equation (18)

can be seen that even at $Re = 2,300$, $c_D \approx 0.90$, which differs from other results reported. All of the statements found in the literature have in common that they were obtained with substantially larger nozzles (throat diameters) and a stronger influence of local heat flows. In the case of the small diameter here investigated, with a throat of 0.2 mm, and adiabatic conditions in the flow range along the walls, the characteristic throughput values depart from the equation above (see section 4.2). As was the case in the correction procedure mentioned in section 2.2.5.3 for the determination of u_v , in the determination of c_D we can resort directly to the available boundary layer quantity δ^* and θ . Since here - in contrast to nearly all procedures reported in the literature - in the area of the throat $\delta^* \neq 0$ and $\theta \neq 0$ (see also section 2.2.8), the contraction (or throat throughput) coefficient $c_D = \frac{A_{t,v}^*}{A_{t,n/v,ODE}}$ can be calculated with sufficient accuracy by numerical methods. In anticipation of sections 4.2 and 5, this way proves to be fully justified. /21

2.2.5 Boundary layer loss calculation

Because of gas viscosity and surface roughness on the propulsion unit's inner walls, boundary layers are formed, with the effect of reducing performance. (In large propulsion units these losses are merely a few (1-2) %, while they are substantially higher for smaller engines.) The first decision in the calculation of boundary layer problems requires an answer to the question of whether the flow is laminar or turbulent (see also [11,24,26,29, 30,38,41,65,94,95,99,100,103,104,107,108,112-114,117,118,122-124, 126,135,157,170,172,177,179]).

2.2.5.1 Flow condition

/22

Normally, laminar flow can be assumed for nozzles of small dimensions. Because of the high flow velocities, the large Reynolds numbers would permit turbulent flow and it hence must be shown whether the large acceleration causes a laminarization of the boundary layer, within the nozzle. According to Boldman et al. [15], the following criterion can be used:

$$K_{acc} = \left(\frac{v_{\infty}}{u_{\infty}^2} \frac{du_{\infty}}{dx} + 0,352 \frac{v_{\infty}}{u_{\infty}} \frac{dr}{r} \frac{dx}{} \right) > 2,88 \cdot 10^{-6} \quad (19)$$

It can be readily shown that in the case of small nozzles the acceleration parameter K_{acc} is several-fold above the critical value. Hence, all boundary layer calculations presented will be based on a laminar velocity profile.

2.2.5.2 Impulse equation

The starting point for boundary layer calculations is the impulse equation for axisymmetrical nozzle flow [1,7-9,96,97,136,146,167]

$$\frac{dD}{dz} = \frac{c_f}{2} \left[1 + \left(\frac{dr}{dz} \right)^2 \right]^{1/2} - 0 \left[\frac{2 - M^2 + \epsilon^*/0}{(1 - \frac{1}{2} \gamma M^2) M} \cdot \frac{dM}{dz} + \frac{1}{r} \frac{dr}{dz} \right] \quad (20)$$

where

$$\delta^* = \delta_r - \delta_p = \int_0^{\delta_r} \left(1 - \frac{\rho u}{\rho_\infty u_\infty}\right) dy$$

is the displacement thickness of the boundary layer (Figure 7):

/23

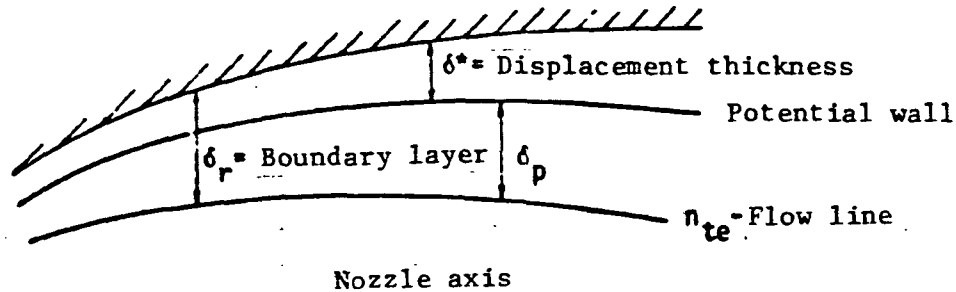


Figure 7 Designation of main flow lines

$$0 = \int_0^{\delta_r} \frac{\rho u}{\rho_\infty u_\infty} \left(1 - \frac{u}{u_\infty}\right) dy \quad (22)$$

is the impulse loss thickness, and

$$c_f = \frac{\tau_w}{\frac{\rho_\infty u_\infty^2}{2}} \quad (23)$$

the dimensionless friction coefficient with respect to wall shearing stress, M the Mach number of the core flow, r the local nozzle radius and d/dz the differential with respect to the nozzle axis coordinate.

In order to calculate the Mach number, we shall resort to an equation that can be solved only by iteration, for a given surface ratio ϵ :

$$\epsilon = \frac{1}{M} \left[\frac{2}{\gamma+1} \left(1 + \frac{\gamma-1}{2} M^2 \right) \right]^{\frac{\gamma+1}{2(\gamma-1)}} \quad (24)$$

/24

$$M = f(\epsilon, \gamma) \quad (25)$$

2.2.5.2.1 Geometry determination

For the boundary layer calculation to be sufficiently precise, it is necessary to simulate the exact nozzle contour, without edges or obstructions. In the EGVP program here developed, the task ($R = f(z)$) is solved by a subroutine in six sections, with the aid of the main geometry points shown in Figure 8, below.

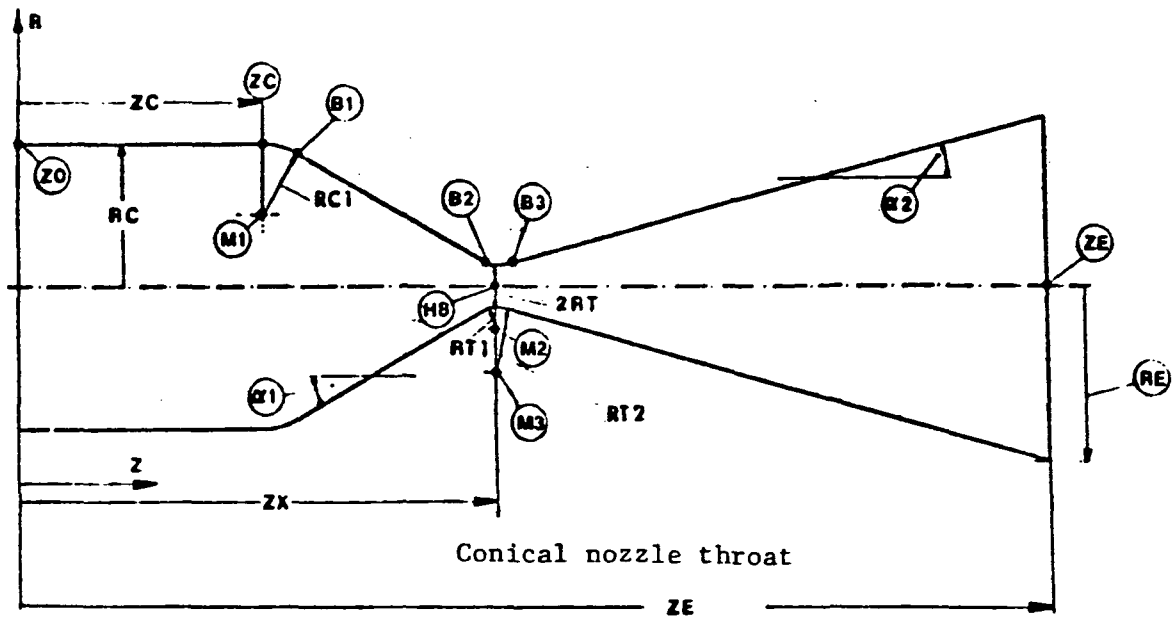


Figure 8 Nozzle geometry

- 1st section: Z0 to ZC
- 2nd section: ZC to B1
- 3rd section: B1 to B2

4th section: B2 to H8

5th section: H8 to B3

6th section: B3 to ZE

In contrast to most authors, who start the boundary layer calculations at the nozzle's narrowest cross-section - which seems justified in the case of large propulsion units, because the severe contraction of the flow at the throat reduces the boundary layer thickness to practically 0, at the narrowest cross-section - here we begin at the combustion chamber head. It is shown that even for small throat diameters (< 1 mm) the boundary layer thickness appears to be negligible in the throat region (see Figure 9, below). Nevertheless, including the subsonic

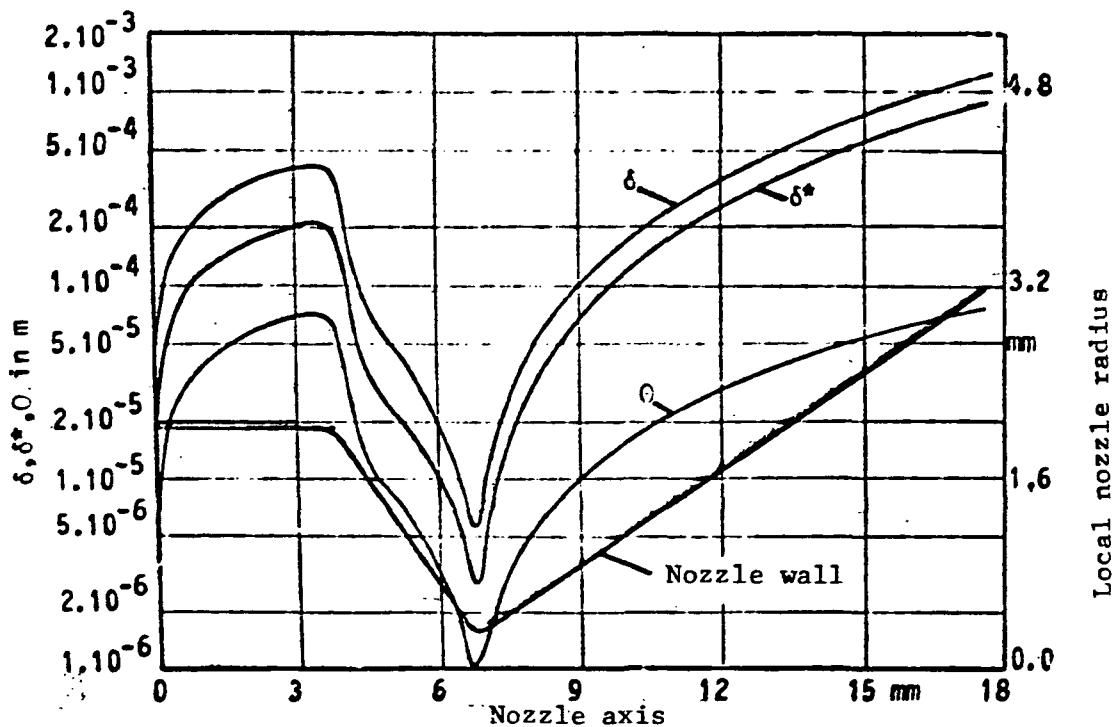


Figure 9 Boundary layer parameter development along the nozzle wall

range in the boundary layer calculation of nozzles represents a physical expansion and numerical completion.

2.2.5.2.2 Shearing stress coefficient c_f

In general, for locally constant viscosity the shearing stress at the wall is

$$\tau_w = \eta_w \left(\frac{\partial u}{\partial y} \right)_w \quad (26)$$

where η_w is the gas viscosity at the wall, which is a function of the temperature:

$$\eta_w = f(T_w) = f(M, u_\infty, T_c, \gamma, \epsilon) \quad (27)$$

The shearing stress coefficient is defined as

$$c_f = \frac{\tau_w}{\frac{\rho_w}{2} u_\infty^2} = 2 \frac{\eta_w}{\rho_w} \frac{1}{u_\infty^2} \frac{\partial u}{\partial y} \quad (28)$$

Figures 10 and 11, below, show the nomenclature, in further

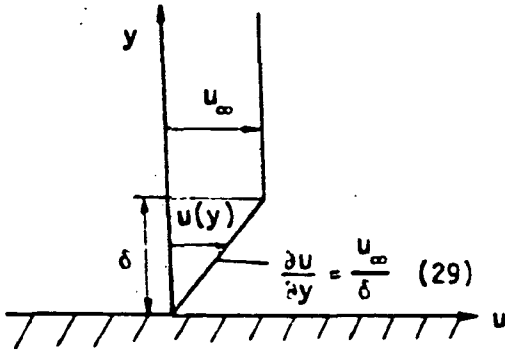


Figure 10 Linear velocity profile

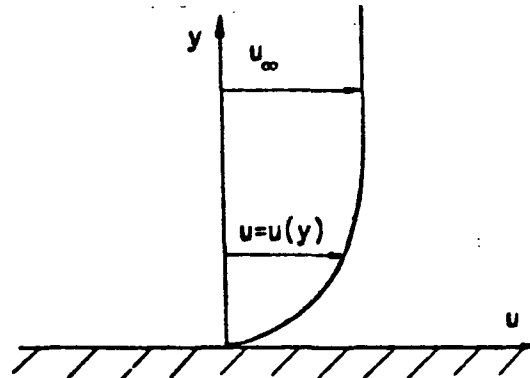


Figure 11 Parabolic velocity profile

considerations, for a general and a linear velocity profile within the boundary layer.

The gas density at the wall is derived from

$$\frac{\rho}{\rho_g} = \frac{T_g}{T} = \frac{1}{1 + \frac{\gamma-1}{2} M_g^2 \left\{ 1 - \left(\frac{u}{u_g}\right)^2 \right\}} \quad \text{with} \quad (30)$$

$$\frac{T_c}{T_g} = 1 + \frac{\gamma-1}{2} M_g^2 \quad \text{and} \quad (31)$$

$u = u_w = 0$ we can determine ρ_w , the density at the wall.

$$\rho_w = \rho_c \left(\frac{T_g}{T_c}\right)^{\frac{\gamma}{\gamma-1}} \quad (32)$$

where the subindices refer to:

- c = chamber conditions,
- g = edge of the boundary layer (to the core flow),
- w = wall.

We must now take into account the temperature dependence of the viscosity, $\eta = \eta(T)$. Anticipating experimental results, we shall assume that no heat is removed through the wall. With

$$\frac{T}{T_g} = 1 + \frac{\gamma-1}{2} \left[M_g^2 \left(1 - \left(\frac{u}{u_g}\right)^2 \right) \right] \quad \text{and} \quad (33)$$

$u = u_w = 0; \quad M_w = 0$ we obtain

$$T_w = T_c \quad \text{and hence also} \quad \eta_w = \eta_c \quad (34)$$

With equations (29) and (32), the shearing stress coefficient c_f /28 becomes:

$$c_f = \frac{2,0}{\delta u_\infty} \cdot \frac{\eta_c}{\rho_c \left(\frac{T}{T_c}\right)^{\frac{\gamma}{\gamma-1}}} \quad (35)$$

The temperature dependence of the GN_2 viscosity is approximated by means of

$$\eta = \eta_c \left(\frac{T}{T_c}\right)^x \quad (36)$$

where

$$T_c = 300 \text{ K}$$

$$\eta_c = 1,769 \cdot 10^{-5} \text{ kg/msec}$$

$$x = 0,71976$$

A variety of expressions is used in the literature:

$$c_f = \frac{0,5533}{Re_\theta} \quad (\text{Ziebland (177)}) \quad (37)$$

$$c_f = \frac{0,571}{Re_\theta} \quad (\text{Bartz (9)}) \quad (38)$$

/29

(general; see Figure 12; [61])

Here Re_θ represents the Reynolds number related to the impulse loss thickness.

$$c_f = \frac{K_1}{Re_\theta} \quad (39)$$

$$c_f = \frac{0,664}{\sqrt{Re_z}} = \frac{0,664}{\sqrt{\frac{u_\infty z}{\nu}}} \quad (\text{Schlichting (136)})$$

$$c_f = \frac{0,664}{\sqrt{Re_z}} - \frac{0,01085}{\sqrt{Re_z}} M_\infty^{3/2} \quad (\text{Shapiro (150)})$$

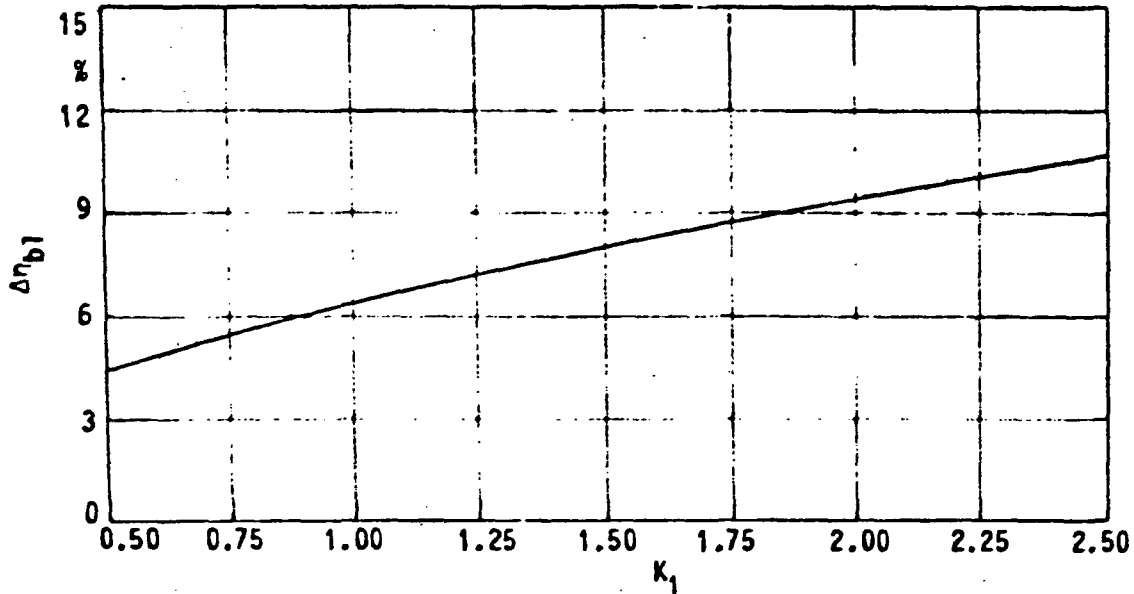


Figure 12 Effect of the shearing stress coefficient K_1 on the boundary layer losses

2.2.5.2.3 Derivation of the boundary layer shape factor, δ^*/θ /30

Using the usual integral equations of the boundary layer theory for the displacement and impulse loss thicknesses,

$$\delta^*/\delta = \int_0^1 \left(1 - \frac{\rho}{\rho_g} \frac{u}{u_g}\right) d\left(\frac{y}{\delta}\right) \quad (42)$$

$$\theta/\delta = \int_0^1 \frac{\rho}{\rho_g} \frac{u}{u_g} \left(1 - \frac{u}{u_g}\right) d\left(\frac{y}{\delta}\right) = \int_0^1 \frac{\rho}{\rho_g} \frac{u}{u_g} d\left(\frac{y}{\delta}\right) - \int_0^1 \frac{\rho}{\rho_g} \frac{u^2}{u_g^2} d\left(\frac{y}{\delta}\right) \quad (43)$$

where ρ and u are the density within the boundary layer, ρ_g and u_g the corresponding values at its edge, and y is the

coordinate perpendicular to the wall, the ratio δ^*/θ is sought, which is necessary for the integration of the impulse equation.

By introducing the ideal gas equation and using equation (38), it is possible to rewrite equation (29) thus

$$\frac{\rho}{\rho_g} = \frac{T_g}{T_c - T_g} \frac{1}{\frac{T_c}{T_c - T_g} - \left(\frac{u}{u_g}\right)^2} \quad (44)$$

Using the linear velocity distribution on which equation (36) is based (a comparison with the exact distribution is shown in Figure 13, below), the integral equation can be rewritten:

/31

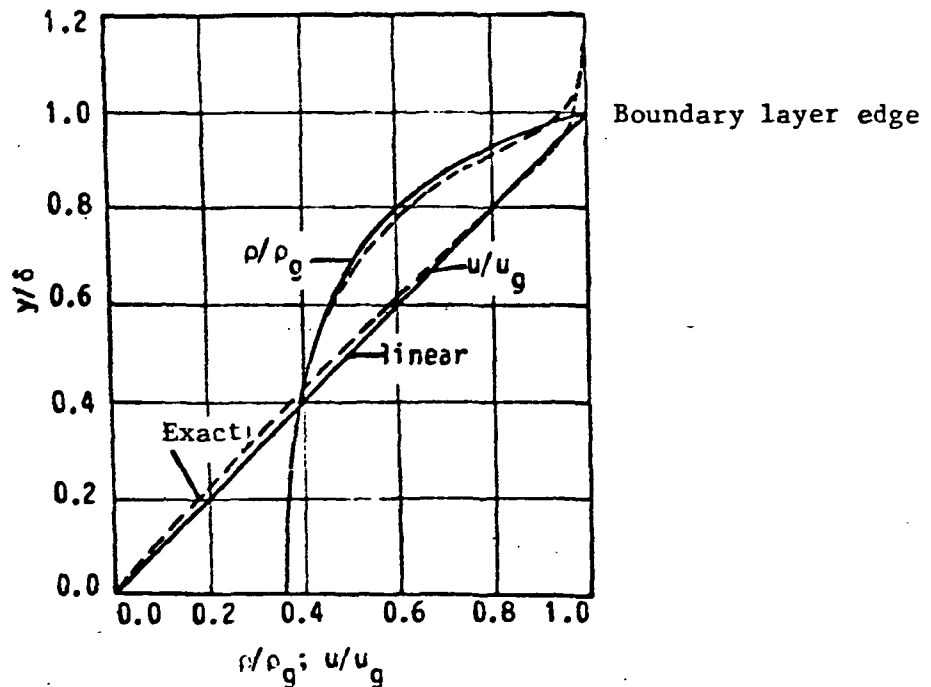


Figure 13 Comparison between the simplified linear and actual velocity distribution with respect to the course of density and velocity within the boundary layer

$$\int_0^1 \frac{\rho}{\rho_g} \frac{u}{u_g} d\left(\frac{y}{\delta}\right) = \frac{T_g}{\Delta T} \int_0^1 \frac{(y/\delta)}{\frac{T_c}{\Delta T} - (y/\delta)^2} d\left(\frac{y}{\delta}\right) \quad \text{and} \quad (45)$$

$$\int_0^1 \frac{\rho}{\rho_g} \frac{u^2}{u_g^2} d\left(\frac{y}{\delta}\right) = \frac{T_g}{\Delta T} \int_0^1 \frac{(y/\delta)^2}{\frac{T_c}{\Delta T} - (y/\delta)^2} d\left(\frac{y}{\delta}\right) \quad , \text{ where} \quad (46)$$

$$\Delta T = T_c - T_g \quad (47)$$

For equation (45), integration yields

/32

$$(48) \quad -\frac{T_g}{2\Delta T} \ln\left(1 - \frac{\Delta T}{T_c}\right) \quad \text{and for equation (46)}$$

$$\frac{T_g}{2\Delta T} \left[\left(\frac{T_c}{\Delta T}\right)^{0,5} \cdot \ln \frac{\left(\frac{T_c}{\Delta T}\right)^{0,5} + 1}{\left(\frac{T_c}{\Delta T}\right)^{0,5} - 1} - 2 \right] \quad (49)$$

With these intermediate results, the shape parameter δ^*/θ can be given in a form that now only depends on the corresponding temperatures, T_c and T_g .

$$\frac{\delta^*}{\theta} = \frac{-\frac{2(T_c - T_g)}{T_g} - \ln \frac{T_g}{T_c}}{\ln \frac{T_g}{T_c} - 2 + \left(\frac{T_c}{T_c - T_g}\right)^{0,5} \cdot \ln \frac{\left(\frac{T_c}{T_c - T_g}\right)^{0,5} + 1}{\left(\frac{T_c}{T_c - T_g}\right)^{0,5} - 1}} \quad (50)$$

Figure 14 (page 39) shows a plot of this parameter for increasing Mach numbers (or ϵ , respectively), with γ as the parameter.

For a non-adiabatic wall, the wall temperature will be lower than the stagnation temperature, and the gas density near the wall will be higher than in the adiabatic cases. Therefore δ^* will be smaller and also δ^*/θ , because

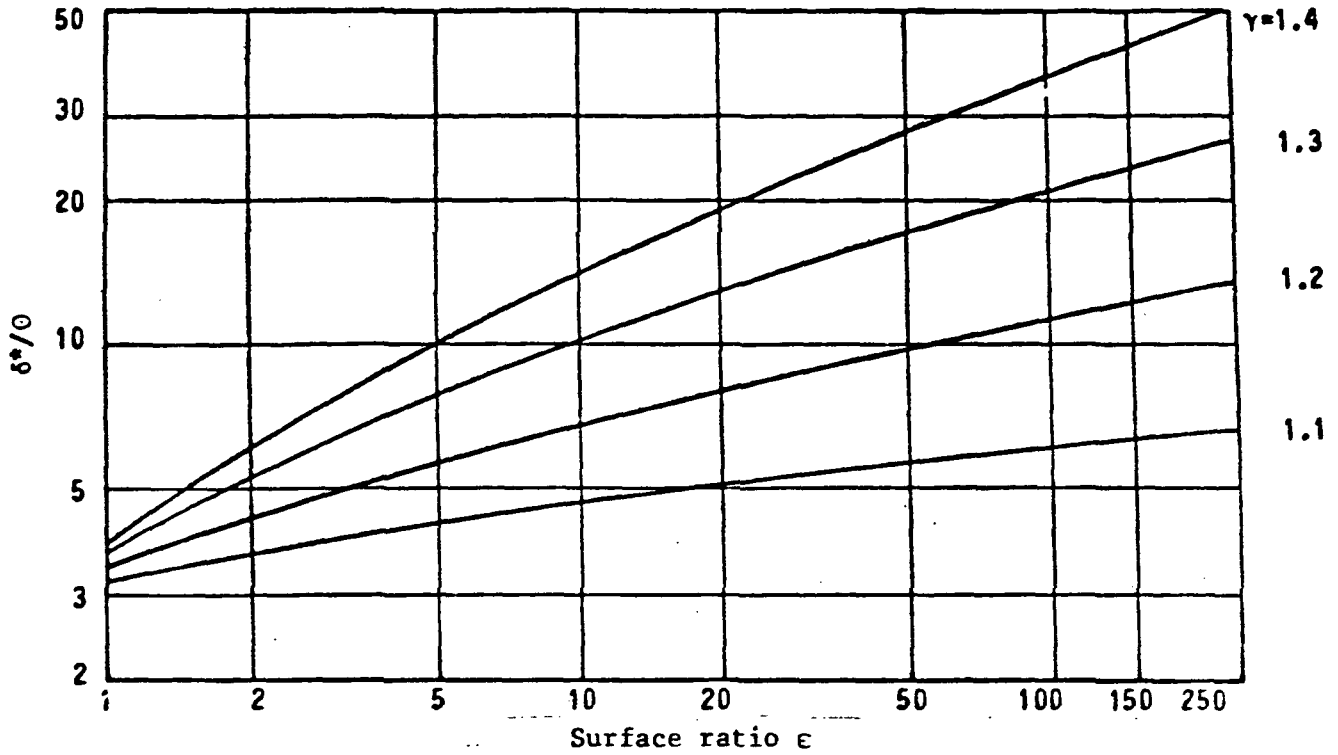


Figure 14 Increase in boundary layer shape parameter δ^*/θ as a function of ϵ with γ as parameter

$$\int_0^1 \frac{\rho}{\rho_g} \frac{u}{u_g} d\left(\frac{y}{\delta}\right) \Big|_{\text{adiabatic wall}} < \int_0^1 \frac{\rho}{\rho_g} \frac{u}{u_g} d\left(\frac{y}{\delta}\right) \Big|_{\text{Non-adiabatic wall}} \quad (51)$$

The gradient δ^*/θ is not much affected, however, precisely for the case of large surface ratios, in which the stationary wall temperature is considerably below either the combustion chamber or the stagnation temperature.

2.2.5.3 Nozzle shape correction

Due to the formation of the boundary layer, the inviscid geometrical cross-sectional area of the nozzle is reduced by the

impulse loss thickness. To determine the resulting thrust loss it is necessary to determine the fully viscous velocity distribution, which can be derived assuming that the mass throughput through the narrowest cross-section also flows through the nozzle end cross-section (contiguity equation) /34

$$\dot{m}_v = \dot{m}_{n/v} = \dot{m} \quad (52)$$

Including the usual boundary layer quantities, we obtain: for the mass throughput

$$\dot{m} = \pi \cdot u_{g,v} \cdot \rho_{g,v} (r_e - \delta)^2 + 2\pi (r_e - \frac{\delta}{2}) \cdot \rho_{g,v} \cdot u_{g,v} \cdot \delta \cdot \int_0^1 \frac{u \cdot \rho}{u_{g,v} \cdot \rho_{g,v}} d(\frac{y}{\delta}) \quad (53)$$

and for the thrust,

$$F = \pi \cdot u_g^2 \cdot \rho_g (r_e - \delta)^2 + 2\pi (r_e - \frac{\delta}{2}) \cdot \rho_g \cdot u_g^2 \cdot \delta \cdot \int_0^1 \bar{\rho} \bar{U}^2 d\bar{y} \quad (54)$$

with the abbreviations

$$\begin{aligned} u_{g,v} &= u_v \\ \rho_{g,v} &= \rho_v \\ \rho/\rho_{g,v} &= \bar{\rho} \\ u/u_{g,v} &= \bar{U} \end{aligned}$$

We can now rewrite equations (53) and (54), as

$$\pi u_v \rho_v (r - \delta)^2 + 2\pi (r - \frac{\delta}{2}) \rho_v u_v \delta (1 - \frac{\delta^*}{\delta}) = \pi r^2 \rho_{n/v} \cdot u_{n/v} \quad (55)$$

$$F_v = \pi u_v^2 \cdot \rho_v (r_e - \delta)^2 + 2\pi (r_e - \frac{\delta}{2}) \rho_v u_v^2 \cdot \delta \cdot (1 - \frac{\delta^*}{\delta} - \frac{\theta}{\delta}). \quad (56)$$

The viscous thrust (includes: boundary layer behavior due to gas viscosity and wall friction) will be, expressed in abbreviations:

$$F_v = \underbrace{\pi \cdot r_e^2 \cdot u_{n/v}^2 \cdot \rho_{n/v}}_{F_{n/v}} - \Delta F_{bl} \quad (57)$$

Using the customary definition for specific impulse: $I_{sp} = \dot{F}/\dot{m} g_0$ we obtain from equation (57), taking into consideration equations (55) and (56), the following loss of impulse

$$\Delta I_{sp,bl} \cdot g_0 = u_{n/v} - \frac{u_v^2 \cdot \rho_v}{u_{n/v} \cdot \rho_{n/v}} (1 - \frac{\delta}{r})^2 - 2 \frac{u_v^2 \cdot \rho_v}{u_{n/v} \cdot \rho_{n/v}} \cdot \frac{\delta}{r} (1 - \frac{\delta}{2r}) \cdot (1 - \frac{\delta^*}{\delta} - \frac{\theta}{\delta}) \quad (58)$$

/36

$$\Delta I_{sp} \cdot g_0 = u_{n/v} - \frac{u_v^2 \cdot \rho_v}{u_{n/v} \cdot \rho_{n/v}} \underbrace{\left[(1 - \frac{\delta}{r})^2 + \frac{2\delta}{r} (1 - \frac{\delta}{2r}) (1 - \frac{\delta^*}{\delta} - \frac{\theta}{\delta}) \right]}_{K_\theta} \quad (59)$$

The denominator of the factor in the square bracket (K_θ) can also be transformed, with the aid of equation (55), in a form that depends only on the boundary layer parameters

$$\rho_{n/v} \cdot u_{n/v} = \frac{\pi \cdot u_v^2 \cdot \rho_v (r - \delta)^2 + 2\pi (r - \frac{\delta}{2}) \rho_v u_v^2 \delta (1 - \frac{\delta^*}{\delta})}{\pi r^2} \quad (60)$$

or respectively,

$$\rho_{n/v} u_{n/v} = \rho_v u_v K_m \quad (61)$$

Equation (59) for the loss of impulse now becomes

$$\Delta I_{sp} \cdot g_0 = u_{n/v} - u_v \cdot \frac{K_0}{K_m} \quad (62)$$

The determination of the velocity ratio

$$\frac{u_v}{u_{n/v}} = \frac{\rho_{n/v}}{\rho_v} \frac{1}{K_m} \quad (63)$$

occurs by means of the relationship already presented in equation (30), and with the known definition of the Mach number

$$M_g^2 = \frac{u_g^2}{\gamma R T_g} \quad (64)$$

To begin with, we shall divide our considerations into two cases

$$T_g = T_{n/v} \quad \hat{=} \text{Case 1}$$

$$T_g = T_v \quad \hat{=} \text{Case 2}$$

Case 1):

$$\frac{T_c}{T_{n/v}} = 1 + \frac{\gamma-1}{2} M_{n/v}^2 = 1 + \frac{\gamma-1}{2} \frac{u_{n/v}^2}{\gamma R T_{n/v}} \quad \text{with} \quad (65)$$

$$K_{T_c} = \left(\frac{\gamma-1}{2 \gamma R T_c} \right)^{-0,5} \quad \text{therefore} \quad (66)$$

$$u_{n/v} = K_{T_c} \left(1 - \frac{T_{n/v}}{T_c} \right)^{0,5} \quad (67)$$

The abbreviation K_{T_c} is a constant for local nozzle points.

A similar treatment follows for Case 2):

/38

$$u_v = K_{T_c} \left(1 - \frac{T_v}{T_c}\right)^{0,5} \quad (68)$$

Now the velocity ratio in equation (63) can be expressed in a form that depends only on T

$$\left(\frac{u_v}{u_{n/v}}\right)^2 = (T_c - T_v)/(T_c - T_{n/v}) \quad (69)$$

With equation (61) and the general gas law, as well as a rewritten equation (69)

$$(70) \quad \frac{T_v}{T_{n/v}} = \frac{T_c}{T_{n/v}} \left[1 - \left(\frac{u_v}{u_{n/v}}\right)^2\right] + \left(\frac{u_v}{u_{n/v}}\right)^2 \quad \text{therefore}$$

$$\frac{u_v}{u_{n/v}} = \frac{1}{K_m} \frac{p_{n/v}}{p_v} \frac{T_v}{T_{n/v}} \quad (71)$$

Since the pressure can be determined from a temperature function

$$p \frac{\gamma-1}{\gamma} = T \quad \text{or} \quad p = T \frac{\gamma}{\gamma-1} \quad (72)$$

we conclude

/39

$$\frac{u_v}{u_{n/v}} = \frac{1}{K_m} \left(\frac{T_{n/v}}{T_v}\right)^{\frac{1}{\gamma-1}} \quad (73)$$

But since the viscous temperature T_v is not known explicitly, it is replaced by equation (70) and equation (73) now becomes

$$\frac{u_v}{u_{n/v}} = \frac{1}{K_m} \left[\frac{\frac{K_{T_c}^2 - u_{n/v}^2}{K_{T_c}^2}}{1 - \frac{u_v^2}{K_{T_c}^2}} \right]^{\frac{1}{\gamma-1}} \quad \text{or respectively,} \quad (74)$$

$$(u_v K_m)^{\gamma-1} (K_{Tc}^2 - u_v^2) = (K_{Tc}^2 - u_{n/v}^2) u_{n/v}^{\gamma-1} = A \quad (75)$$

The right hand side of this equation is already known, through the quantities that can be determined by the potential theory and hence the fully viscous velocity u_v sought must be determined by iteration from the final equation, which can not be solved explicitly,

$$u_v^{\gamma-1} K_{Tc}^2 - u_v^{\gamma+1} = \frac{A}{K_m^{\gamma-1}} \quad (76)$$

By means of the very important quantity u_v here determined, it is now possible to incorporate the influence of boundary layer development on the core flow within the nozzle, directly into the computer program. /40

2.2.5.4 Correction of the compressive thrust term

In analogy to the influence by the viscous velocity development, the compressive thrust portion must be corrected to include the boundary layer conditions.

The entire loss of thrust due to boundary layer effects is expressed by

$$\Delta F_{bl} = \Delta F_{bl, I_{sp}} + A_{e, 2-d} (p_{e, n/v} - p_{e, v}) \quad (77)$$

Taking into account the results of the $u_v = f(u_{n/v})$ determination, the following relationship exists between the pressure equation and the velocity distribution

$$\left(\frac{u_{n/v}}{u_v}\right)^2 = \frac{1 - \left(\frac{p_{e, n/v}}{p_c}\right)^{\frac{\gamma-1}{\gamma}}}{1 - \left(\frac{p_{e, v}}{p_c}\right)^{\frac{\gamma-1}{\gamma}}} \quad (78)$$

Rearranging and solving by viscous and inviscid terms yields

$$1 - \frac{1}{\left(\frac{u_{n/v}}{u_v}\right)^2} + \frac{\left(\frac{p_{e,n/v}}{p_c}\right)^{\frac{\gamma-1}{\gamma}}}{\left(\frac{u_{n/v}}{u_v}\right)^2} = \left(\frac{p_{e,v}}{p_c}\right)^{\frac{\gamma-1}{\gamma}} = K_p \quad (79)$$

The right-hand side includes only magnitudes already determined /41 and hence the fully viscous end pressure $p_{e/v}$ now depends only on p_c , γ and the already determined value K_p .

$$p_{e,v} = p_c K_p^{\frac{\gamma}{\gamma-1}} \quad (80)$$

2.2.5.5 Connection between nozzle end values and boundary layer losses

Based on the preceding considerations and the Fortran IV computer programs built on them, all required fully viscous nozzle end values can be numerically obtained with sufficient precision. On this basis, the total integrated boundary layer loss for supersonic flow can be obtained

$$\Delta I_{sp} \cdot g_0 = u_{n/v,e} \cdot \frac{u_{v,e}^2 \cdot \rho_{v,e}}{u_{n/v,e} \cdot \rho_{n/v,e}} \left[\left(1 - \frac{\delta_e}{r_e}\right)^2 + \frac{2\delta_e}{r_e} \cdot \left(1 - \frac{\delta_e}{2r_e}\right) \left(1 - \frac{\delta_e^*}{\delta_e} - \frac{0_e}{\delta_e}\right) + A_e \left(p_{e,n/v} - p_c \cdot K_p^{\frac{\gamma}{\gamma-1}}\right) \right] \quad (81)$$

or, related to a 1-dimensional loss free theoretical impulse

$$\eta_{bl} = \frac{I_{sp,n/v} - I_{sp,bl}}{I_{sp,n/v}} \quad (82)$$

A review of the numerical treatment of the functions and differential equations in the preceding portion is contained in the /42

form of a flow diagram, in the Appendix. The integration of the impulse differential equation (see section 2.2.5.2) is performed applying an explicit differences procedure, based on the Lax-Wendroff method [35,84,94,107,115].

2.2.5.6 Polynomial for the velocity profile

In order to prove that the simplified linear theory of the velocity profile described above does not represent an impermissible imprecision, a polynomial profile will be used in addition, derived from laminar flow (Pohlhausen) [136,165],

$$\frac{u}{u_g} = (2\eta - 2\eta^3 + \eta^4) + \frac{\Lambda}{6} (\eta - 3\eta^2 + 3\eta^3 - \eta^4) \quad (83)$$

$$\Lambda = \frac{\delta^2}{Y} \cdot \frac{du}{dz} \quad \text{and} \quad \eta = \frac{y}{\delta} \quad \text{for} \quad 0 < y < \delta \quad (84)$$

The $\Delta\eta_{bl}$ results thus obtained show no decisive departures from the results obtained with the linear profiles and hence all subsequent cases will be investigated using it.

2.2.5.7 Roughness equation

To include the effect of the roughness of the nozzle's inner wall on the formation of the boundary layer, at each computation stage in the core flow, $Re_{n/v}$ will be compared to the values known for pipe flow. As is known, at Reynolds numbers $>2,300$, Colebrook-White's equation [161] is valid for the transition range of the pipe friction number /43

$$\frac{1}{\sqrt{\lambda}} = -2 \log \frac{2,51}{Re_{n/v} \sqrt{\lambda}} + 0,27 \frac{Rau}{2R} \quad (85)$$

In contrast, by calculation of the laminarization parameter it is now known that laminar flow predominates. Hence, the calculated

Reynolds number ($> 2,300$) must be recalculated - with the aid of the pipe friction coefficients - to the Reynolds numbers of a laminar pipe flow Re_k , which is possible with

$$Re_k = \frac{64}{\lambda} \quad (86)$$

The effect of roughness is seen by correction of the viscosity parameter

$$\eta_{g,k} = \eta_g \frac{Re_{n/v}}{Re_k} \quad (87)$$

In the calculation processes, wall friction is taken into consideration by means of

$$c_f = \frac{k}{Re_z} \quad \text{with} \quad Re_z = \frac{p_c \delta^*}{c^* \eta_g \epsilon} \quad (88)$$

($k = 0.5$ in the smooth case).

In this model the factor $k = f(\text{rough})$ is connected with a Reynolds number that takes into account the displacement thickness δ^* and indirectly - through the corresponding surface ratio ϵ - also includes the geometry. If we set $k = f(\text{rough}/R)$, then the roughness is correlated directly with the geometry (Figures 15 and 16), as generally customary in pipe friction theory. /44

Other possibilities for a roughness equation are listed below. A roughness expression in terms of the wall shearing stress coefficient c_f seems most appropriate, since it is affected by the roughness of the surface layer. Thus, all possibilities that can expand c_f by means of an additive or multiplicative term, are open.

An additive term

$$c_f = \frac{0,5}{Re_{n/v}} + \frac{k_1}{Re_y} \quad (89)$$

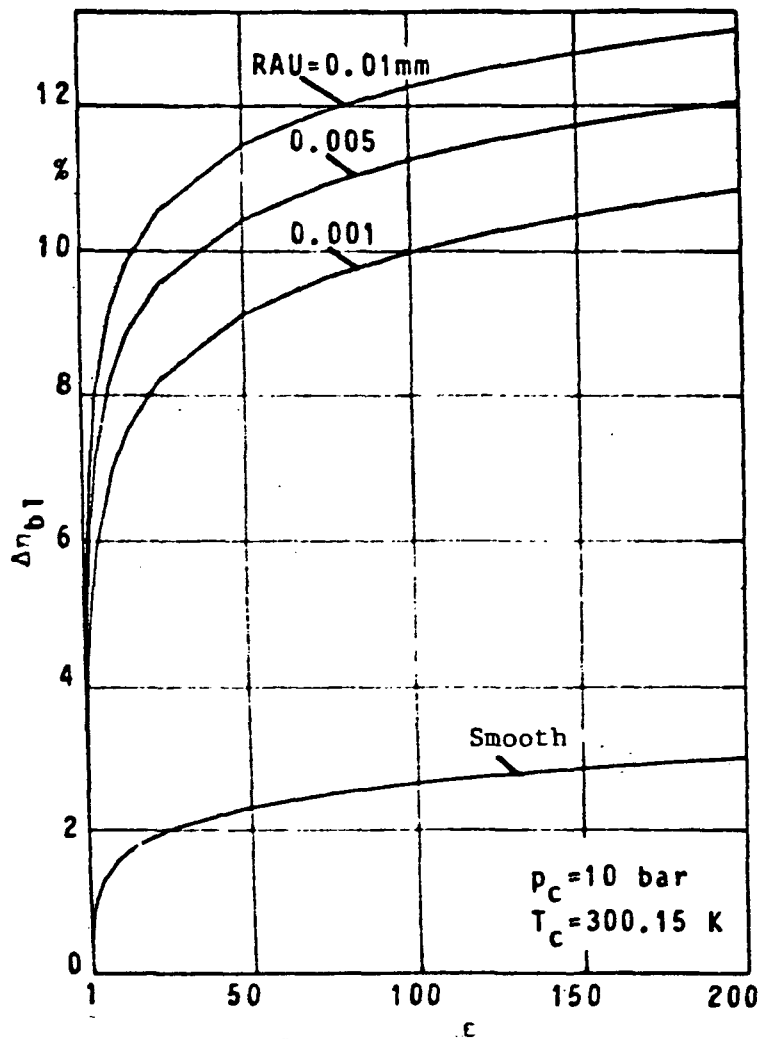


Figure 15 Effect of roughness calculated using REKOR. Nozzle 5

offers the possibility of introducing $k_1 = f(\text{rough})$ and to form the Reynolds number Re_y with the core flow velocity, or the velocity at the height of maximum roughness; Reynolds numbers formed on the basis of mean velocity values are also conceivable. A multiplicative term $c_f = \frac{0.5}{Re_{n/v}} k_2$ makes it possible to define a kind of loss efficiency of the wall roughness, in which the height of the roughness is related to length, to form k_2 . Suitable lengths are δ^* , r_t or a combination of both. The literature does not offer any suitable roughness expression that would be universally applicable to small nozzles with $Re > 2300$ (laminar).

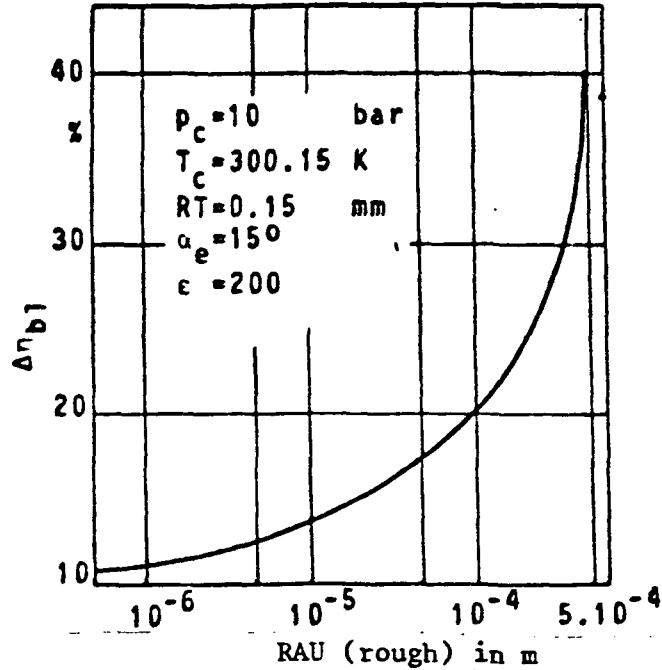


Figure 16 Effect of roughness calculated using pipe friction expression (REKOR)

Hence, the best suited must be found by measurements [15].

Anticipating the results of the tests here described, we find that roughness has no substantial effect on $\Delta\eta_{b1}$, which confirms /45 the approximate expression used earlier. The explanation for this could be that the relatively large boundary layer thicknesses in the case of small diameters extend far beyond the maximum roughness heights, such that the latter are unable to develop any large loss effects, i.e., the roughness effects come to rest within the viscous boundary layer. (Microscopic measurements of the manufactured propulsion units show an absolute roughness of $< 1/1000$ mm).

2.2.6 Adaptation losses due to environmental pressure effects /47

For a given pressure distribution within the propulsion unit, the thrust can be determined by means of

$$\vec{F} = \int_{(A)} (p_i - p_\infty) d\vec{A} \quad (90)$$

Integrating over the entire inner surface of the engine, we obtain, in a scalar description for 1-dimensional flow,

$$F = \dot{m}c + (p_e - p_\infty) A_e \quad (91)$$

The first term represents the so-called impulse thrust, while the second term, formed by the pressure difference between the nozzle end and the environmental pressure, determines the compressive thrust portion.

Since the expansion ratio of a nozzle is not infinite at any time, p_e always has a finite value greater than 0. Since in addition in the actual test case p_∞ is greater than 0, the propulsion unit's measured thrust must be corrected to attain the vacuum thrust necessary for performance specific comparisons. An additional precondition to this is that during experimental operation fully formed nozzle flow is maintained, without separation phenomena and compression shock within the nozzle, such as those occurring in the case of superexpanded propulsion units $p_e \ll p_\infty$.

(For large nozzles, the Summerfeld criterion can be applied to good approximation: $p_e > 0.4 p_\infty$; in the present case this ratio is shifted downwards - see also section 4.2). Since in reality the pressure distribution across the end cross-section A_e is not constant, a 2-dimensional pressure distribution is used to correct the measured F values, based on the calculation method and the theory described in connection with section 2.2.5. /48

2.2.7 Heat losses

In contrast to the large chemical propulsion units, which show a substantial decrease in wall temperature along the axial direction, here a homogeneous temperature distribution is assumed. The following boundary conditions must be mentioned, in this context:

- a) Large propulsion unit heat capacity
- b) Large heat capacity of suspension and supply lines
- c) Short test duration
- d) Good insulation of the entire assembly in the vacuum chamber
- e) Small temperature differences between thrust chamber and environment
- f) Radiation loss remains small, due to T_c

As a consequence of the last three points mentioned, heat losses can be neglected, in the comparative calculations for propulsion unit performance. Performance measurements already carried out, in conjunction with high-resolution temperature sensors for the control of adiabaticity, show this to be permissible.

2.2.8 Results of performance prediction calculations

For all the propulsion units examined in the course of the experiments, the most important thermodynamic and fluid dynamics parameters were determined using the EGVP procedure introduced. For better visibility (and also due to efficiency considerations), these parameters were plotted as a function of ϵ , using a specially developed boundary layer program (or alternatively, as a function of the nozzle axis coordinate).

Figure 17 (page 52) shows the pressure, temperature, viscosity (150) and density for nozzle No. 2, as an example. In addition, both in this and the two subsequent diagrams the nozzle shape was also drawn in.

Figure 18 (page 53) represents the changes in the core flow (151) velocity, Mach number and laminarization parameter, as a function of the nozzle length z [45,46].

The courses of the boundary layer parameters shown in Figure 19 (page 54) show that the boundary layer thickness in the throat

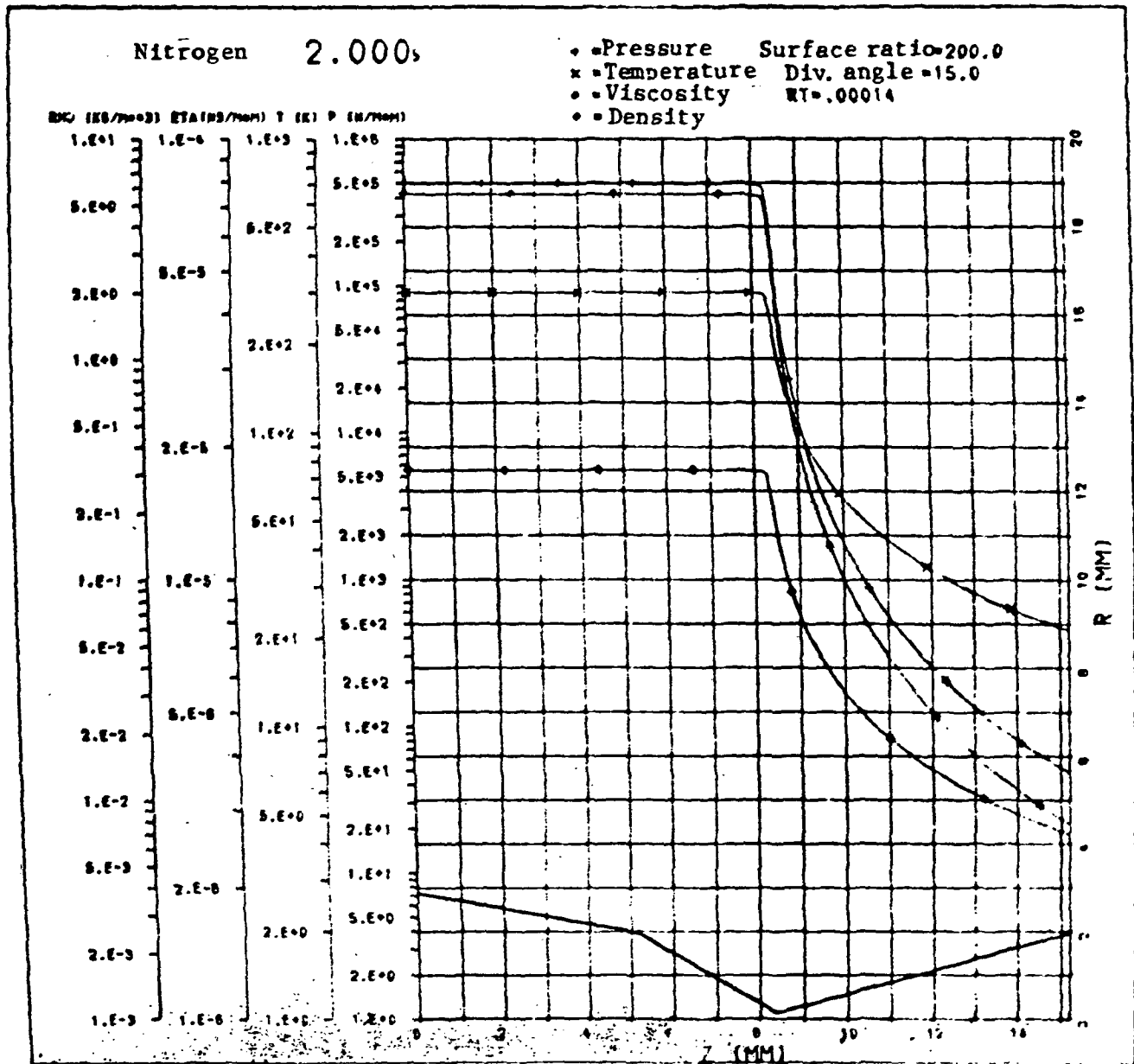


Figure 17 Course of the pressure, temperature, viscosity and density in nozzle No. 2

has been reduced to practically zero, in the convergent portion of the nozzle, by the predominating strong acceleration of the gases in the previous range (see also section 2.2.5.2.3).

With the two velocity profile expressions introduced in section (/52)

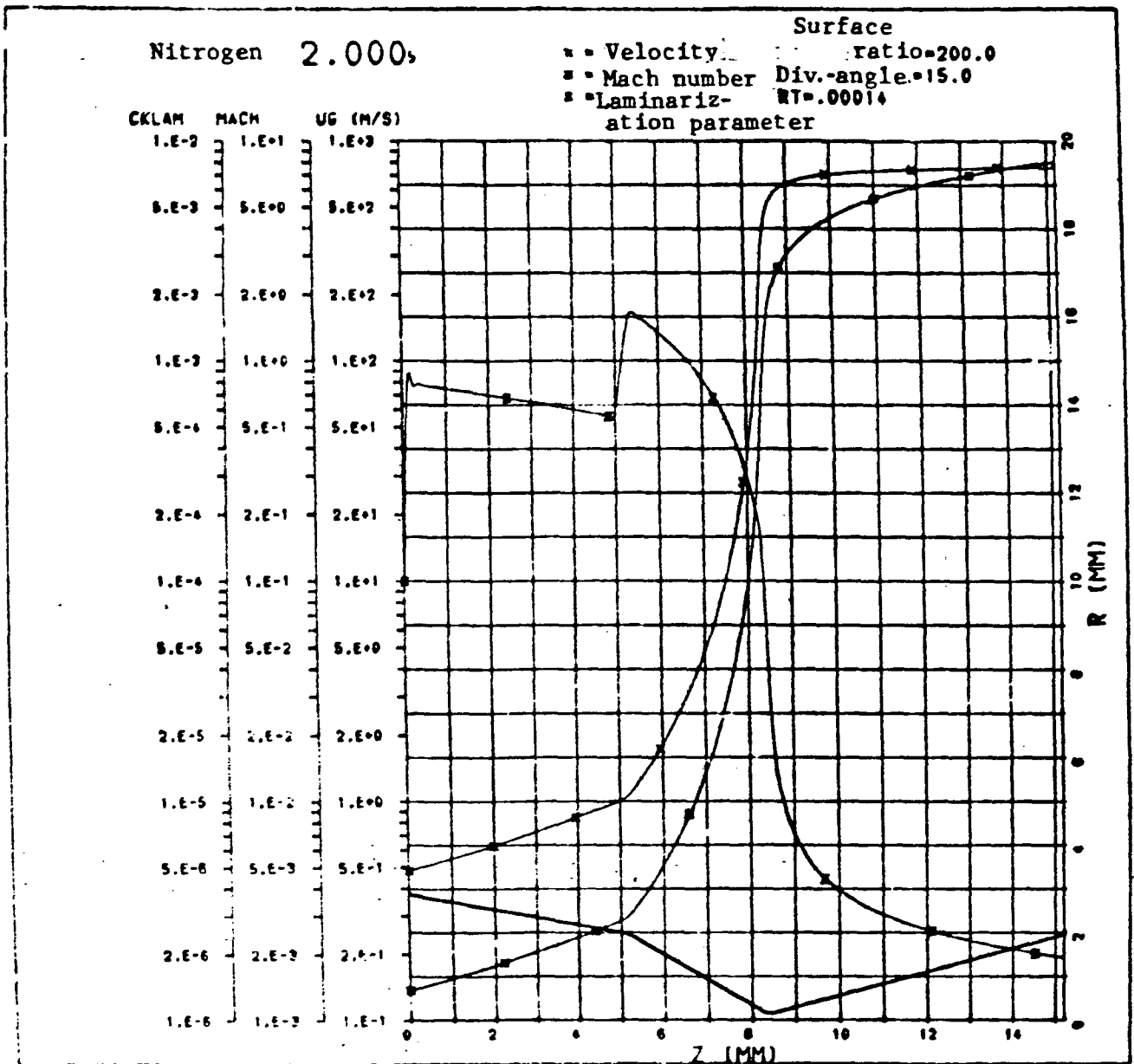


Figure 18 Course of the core flow velocity, Mach number and laminarization parameter K_{acc} along the nozzle axis (Nozzle No. 2)

2.2.5 and with p_c as parameter, Figure 20 (page 55) shows typical boundary layer losses, using nozzle No. 2 as an example. It can be seen that the linear and polynomial velocity expressions have no qualitative effect on the results. As p_c increase, there is a considerable decrease in $\Delta\eta_{b1}$ losses. The quantitative difference (a factor of approximately 2) is based only on the expression

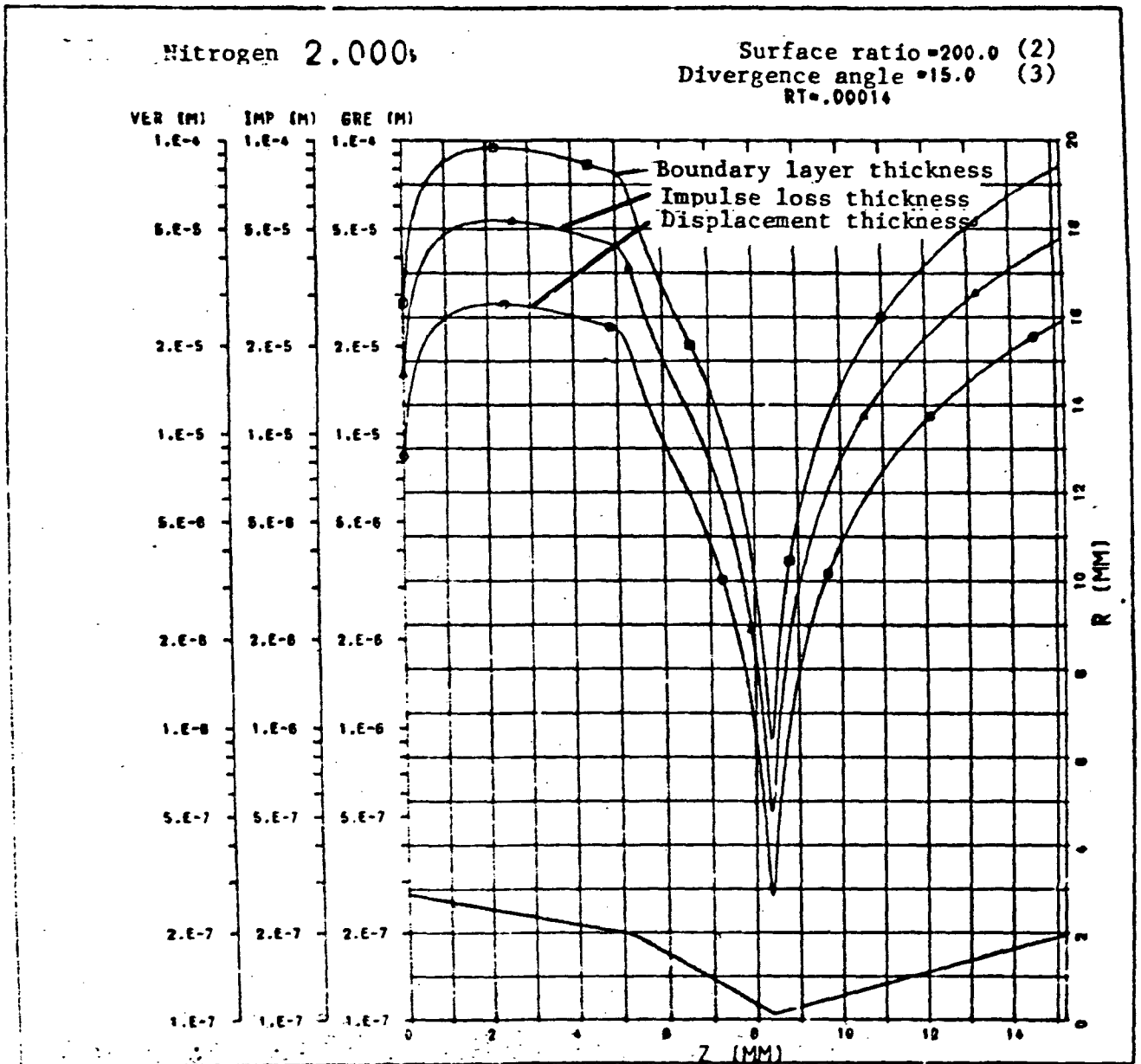


Figure 19 Boundary layer parameters δ , δ^* , θ as a function of z

of Λ and can be readily adapted (see also section 2.2.5.6).

Figure 21 (page 56) provides a comparative representation of the losses $\Delta\eta_{b1}$ in various media. Qualitatively, the boundary layer losses as a function of ϵ can be interpreted as reflecting

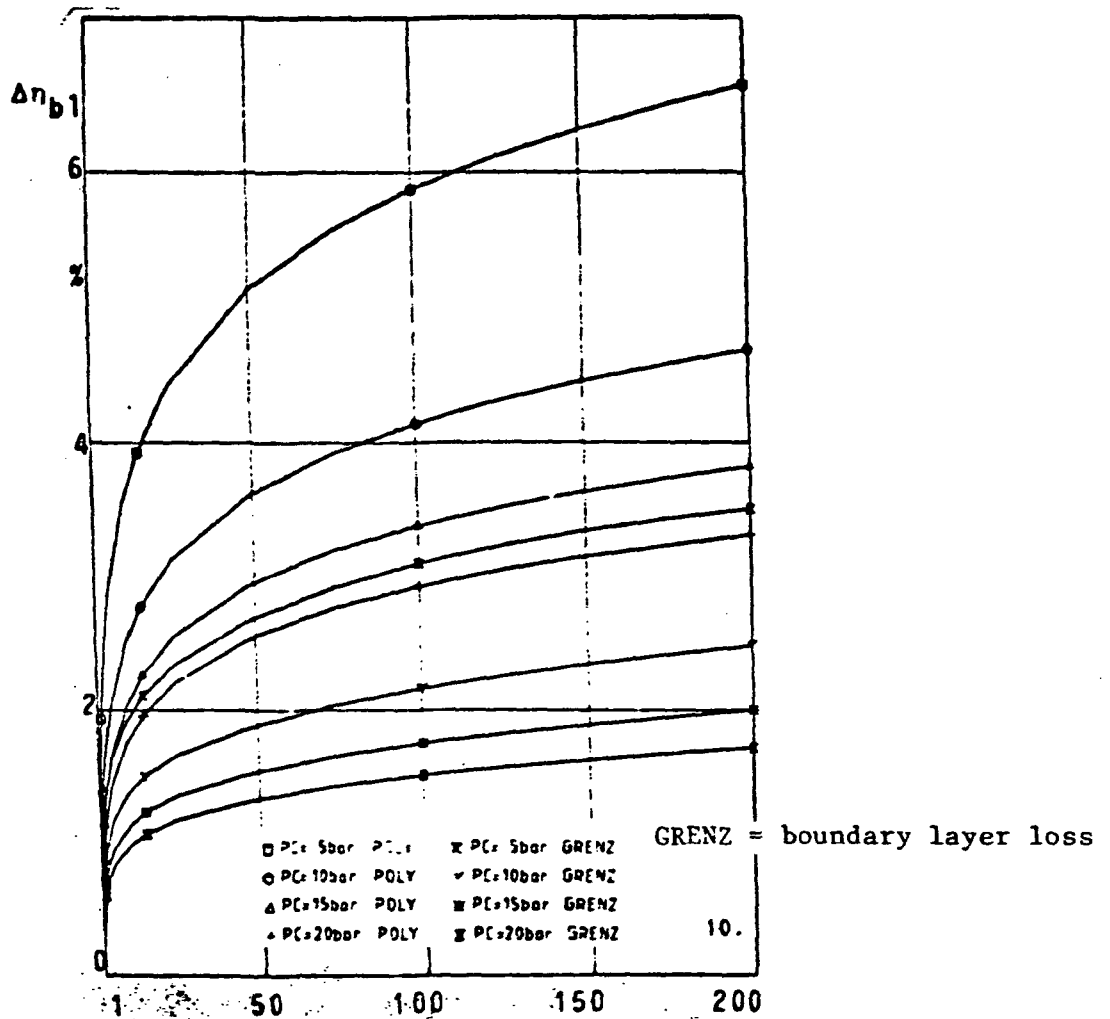


Figure 20 Boundary layer losses without roughness correction

the effect of the different viscosities (see also section 2.2.10). The only exception to the general trend (increase of $\Delta\eta_{b1}$ for increasing ϵ) is that of the curve for $(N_2H_4)_{x_{dis}} = 1.0$

Due to the strong cooling of the originally fully dissociated ammonia, a recombination to NH_3 is initiated, with the simultaneous release of energy, allowing the gas better expansion performance. Consequently the $\Delta\eta_{b1}$ losses decrease, percentually.

In contrast to large propulsion units (F-1, J-2, SSME), an additional design optimization is necessary with small propulsion /54

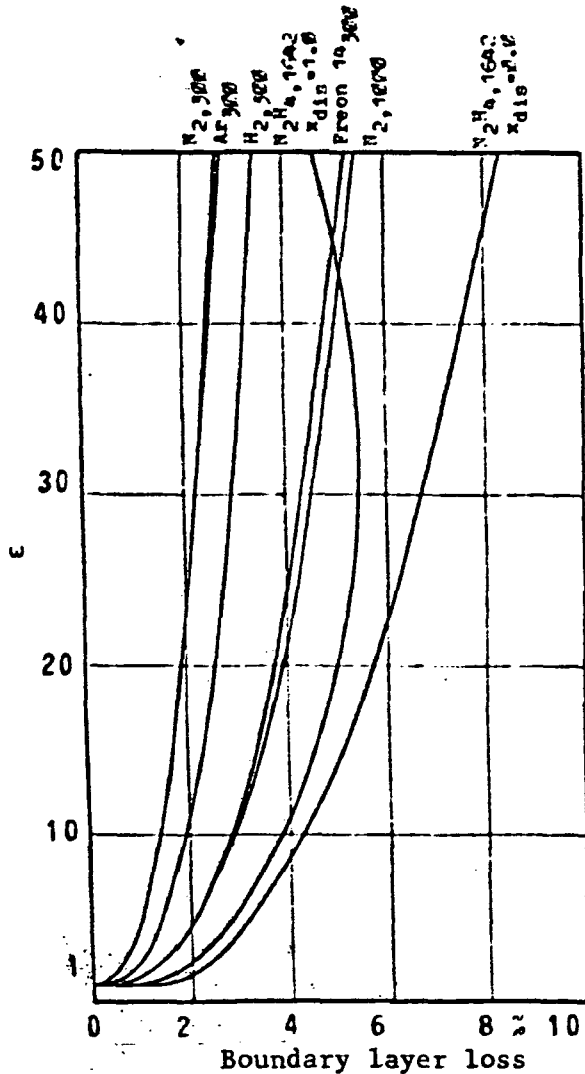


Figure 21 Surface ratio as a function of boundary layer loss for various types of gas. $\alpha_e = 15^\circ$

units, because of the greater influence of the boundary layer losses: the optimization of the surface ratio ϵ with respect to η_{TD} and η_{b1} (not to be confused with the ϵ -optimization of carrier rocket propulsion units with respect to $p_\infty = f(H)$ and $p_e = f(p_c, \epsilon, t, H)$). In general the $\Delta\eta_{TD}$ losses increase with increasing α_e . Since the specific impulse $I_{so,ODE,vac}$ steadily increases with increasing ϵ , an optimization calculation has to be performed to obtain the optimum ϵ . This must be followed by

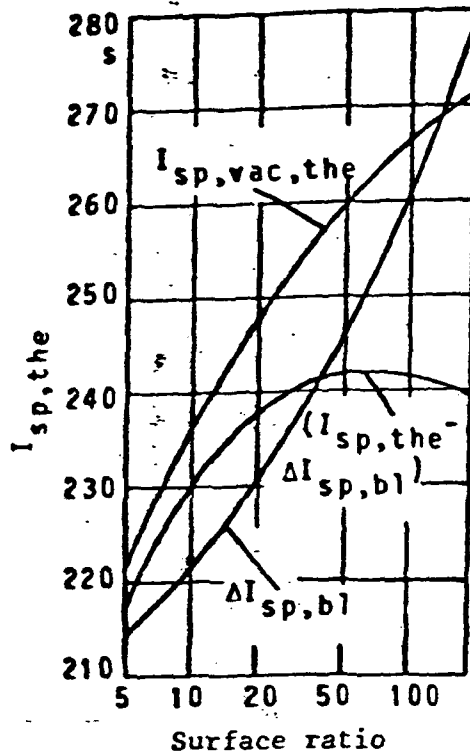


Figure 22 Boundary layer loss effect on the determination of the optimum surface ratio (N_2H_4 , $r_t = 0.3$ mm, $\alpha_e = 15^\circ$)

a second optimization, to take the influence of α_e into account: while at an assumed constant ϵ , for an increase in α_e , $\Delta\eta_{TD}$ becomes larger (conical nozzle), at the same time the absolute cone length decreases and hence the development of the boundary layer is fore-shortened. The mathematical formulation is

$$I_{sp,ODE,vac} \cdot \left[1 - \frac{\eta_{bl}}{100}\right] \cdot \left[1 - \frac{\eta_{TD}}{100}\right] = I_{sp,max,vac} \quad (92)$$

or

$$\frac{d}{d\epsilon} \left[I_{sp,ODE,vac} \cdot \left(1 - \frac{\eta_{bl}}{100}\right) \right] = 0 \quad (93)$$

Figure 23 (page 58) shows the result of the ϵ_{opt} study for the N_2H_4 nozzle, as an example (56 ÷ 63).

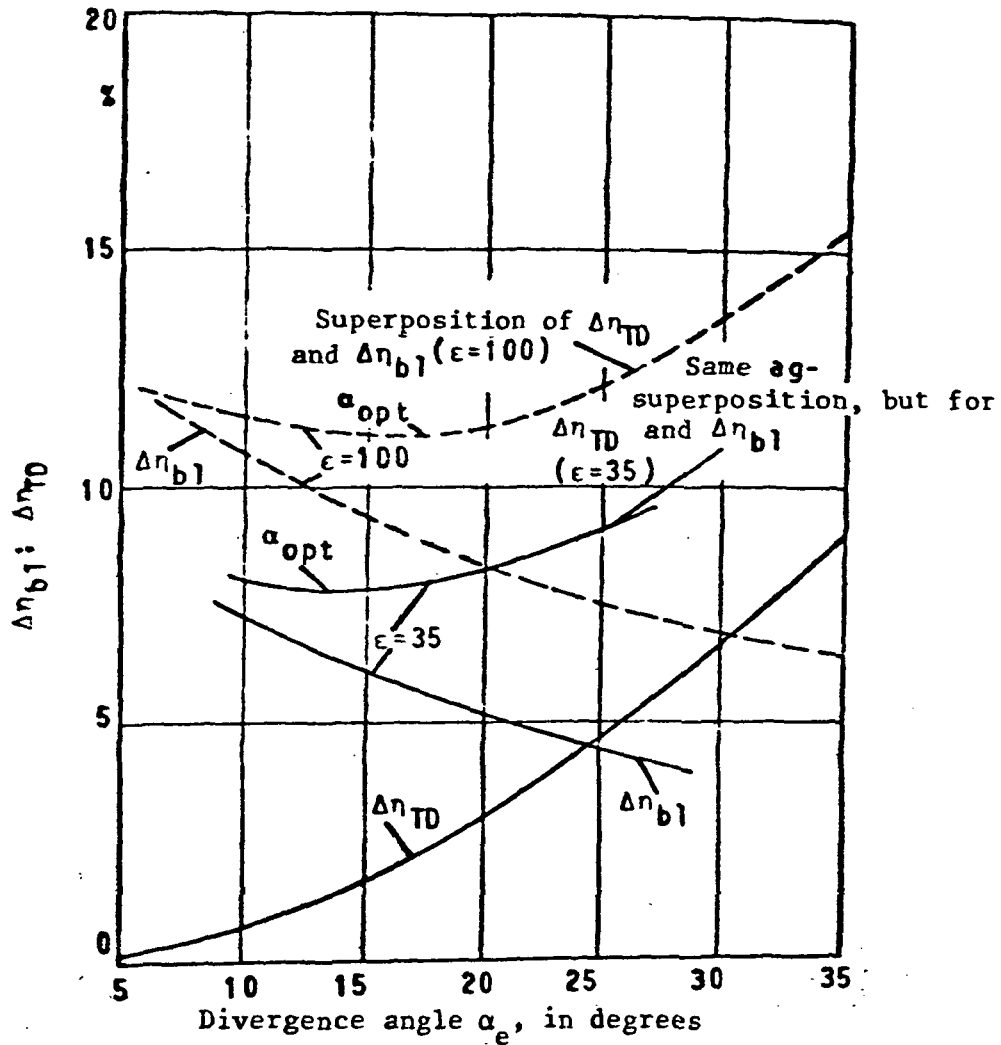


Figure 23 Optimum divergence angle taking the boundary layer and multi-dimensional losses into consideration, with ϵ as parameter (N_2H_4)

Since the optimized $I_{sp,del}$ curve shows a very flat maximum at $\epsilon = 80$ approximately, and in addition the effect of various errors is restrictive (for instance, the true degree of dissociation and the recombination behavior as a function of the expansion and the residence time in the TW [Triebwerk = propulsion unit], a fairly large bandwidth must be assumed here.

Figures 24 and 25 (pages 59 and 60) show the optimization

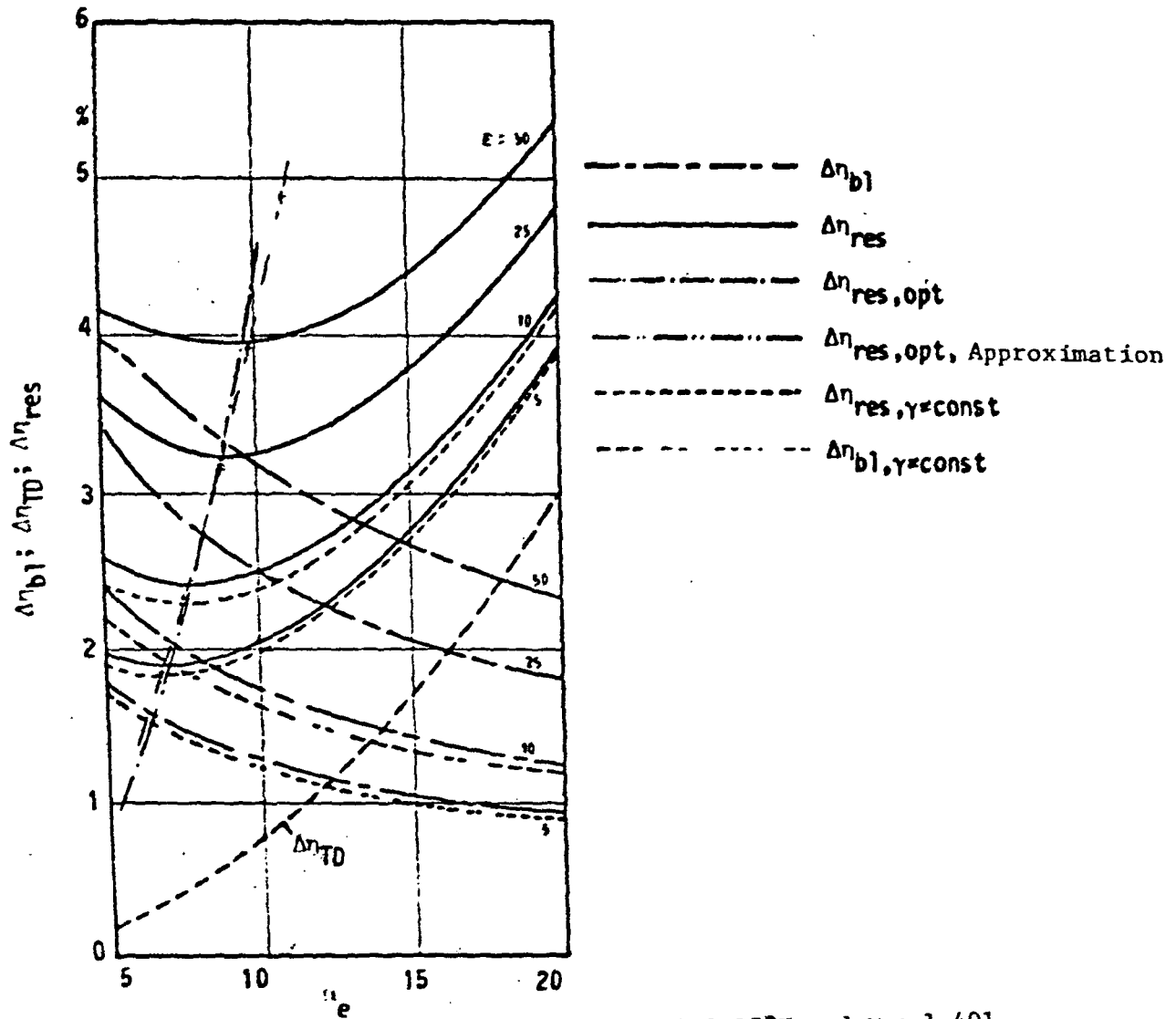


Figure 24 N_2 losses as a function of α_e , at $T_c = 300.15^\circ K$ and $\gamma = 1.401$ and $\gamma \neq \text{const}$

results for nitrogen. In addition to the line connecting the corresponding ϵ_{opt} points according to the explicit theory, Figure 24, above, also shows the line obtained connecting the points resulting according to the simple approximation equation (see section 2.2.10). The good agreement is apparent. The computation time decreases by three orders of magnitude, in the process. Figure 25 (page 60) shows the resulting ϵ_{opt} values, as a function of r_t , for a constant value of α_e . Due to the low

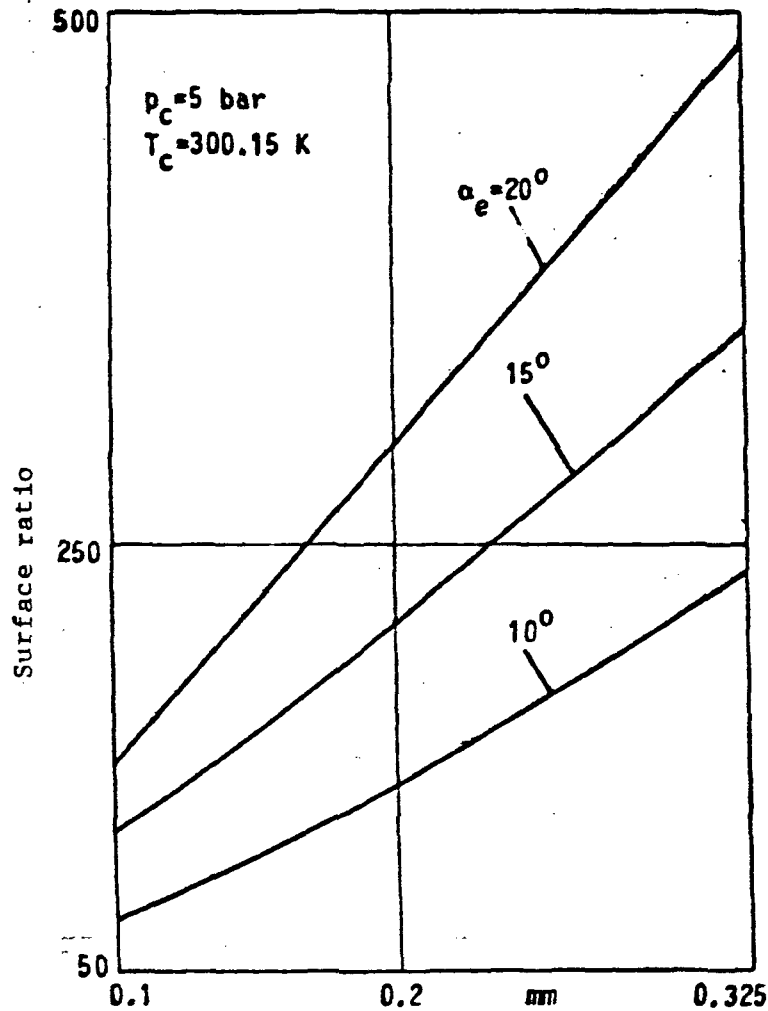


Figure 25 Optimum surface ratio

viscosity of N_2 in comparison to, for instance, H_2 or N_2H_4 -decomposition products, the optimized surface ratio becomes displaced towards larger values.

2.2.9 Comparison of the results presented in section 2.2.8 with those from other procedures (Cline, BLIMP [Boundary Layer Integral Matrix Procedure]) /58

The flow mechanics quantities calculated by the EGVP program - pressure p_g , temperature T_g , velocity u_g and Mach number M - are compared to those from the program VNAP (Cline [22,23,153]),

a program for 2-dimensional, compressible, time-dependent, fully viscous nozzle flow. Figures 26 to 29 (below and pages 62-64)

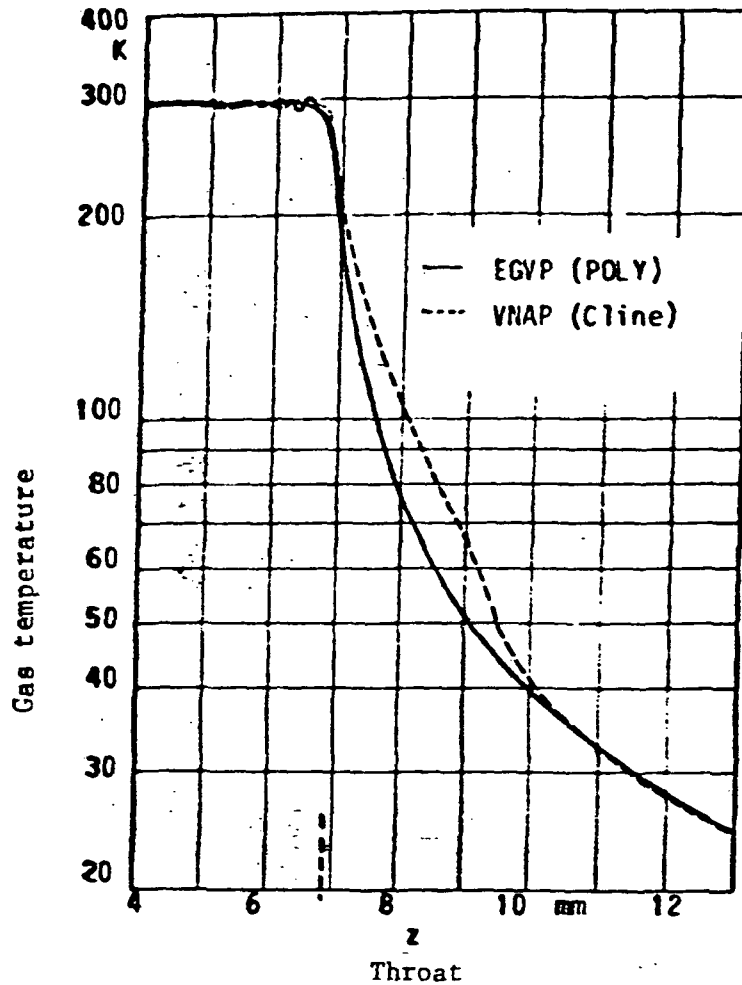


Figure 26 Comparison of programs EGVP and VNAP with respect to T_g , for N_2 nozzles

show the results. In the calculations with VNAP, the values of the core flow present discontinuities just before the nozzle throat; at high surface ratios they coincide with the values calculated by EGVP, which also shows good agreement in the throat region [50].

We have no explanation for the oscillations before the throat, in the values calculated by VNAP. The departures behind the throat could conceivably stem from the fact that VNAP uses only a throat

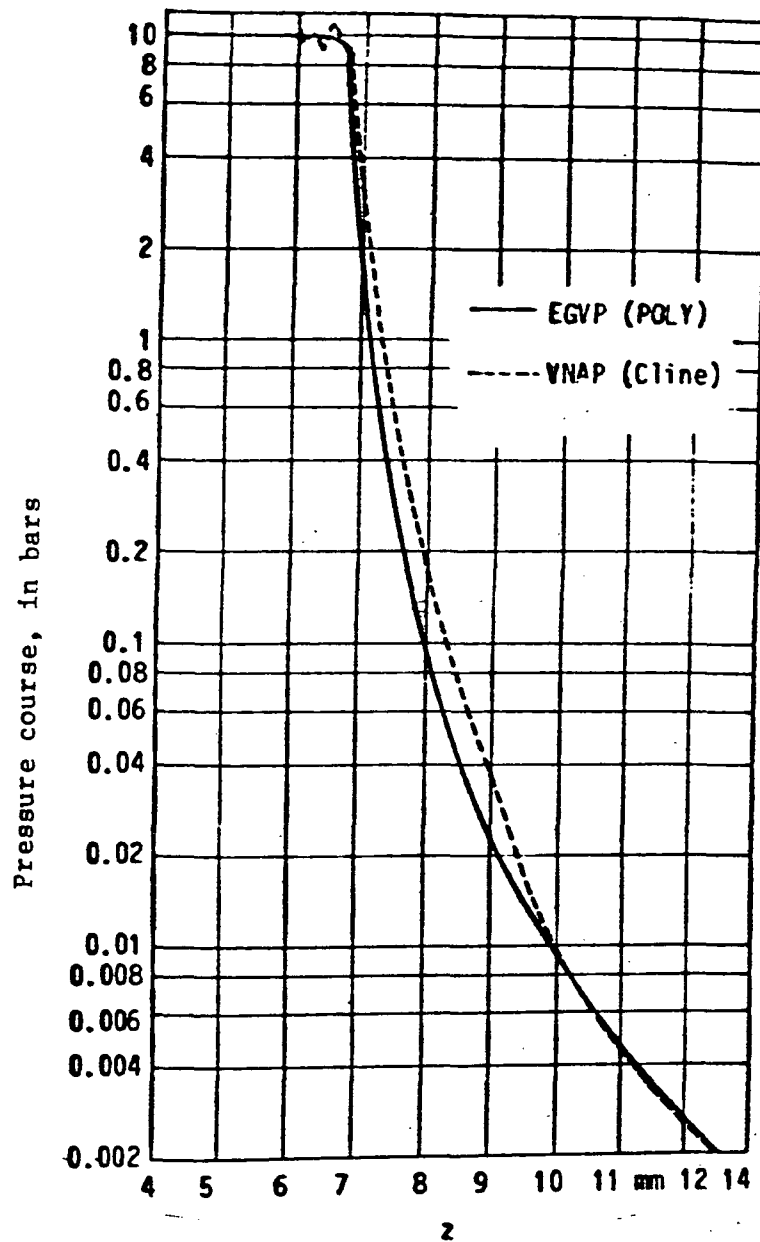


Figure 27 Comparison of the programs EGVP and VNAP with respect to the course followed by the pressure

transition radius and hence is unable to describe the optimum nozzle geometry with sufficient precision [70,102,105,106].

Since both the EGVP and the VNAP programs determine fully viscous flow mechanics data, and since $\Delta\eta_{b1}$ can be derived from them, we

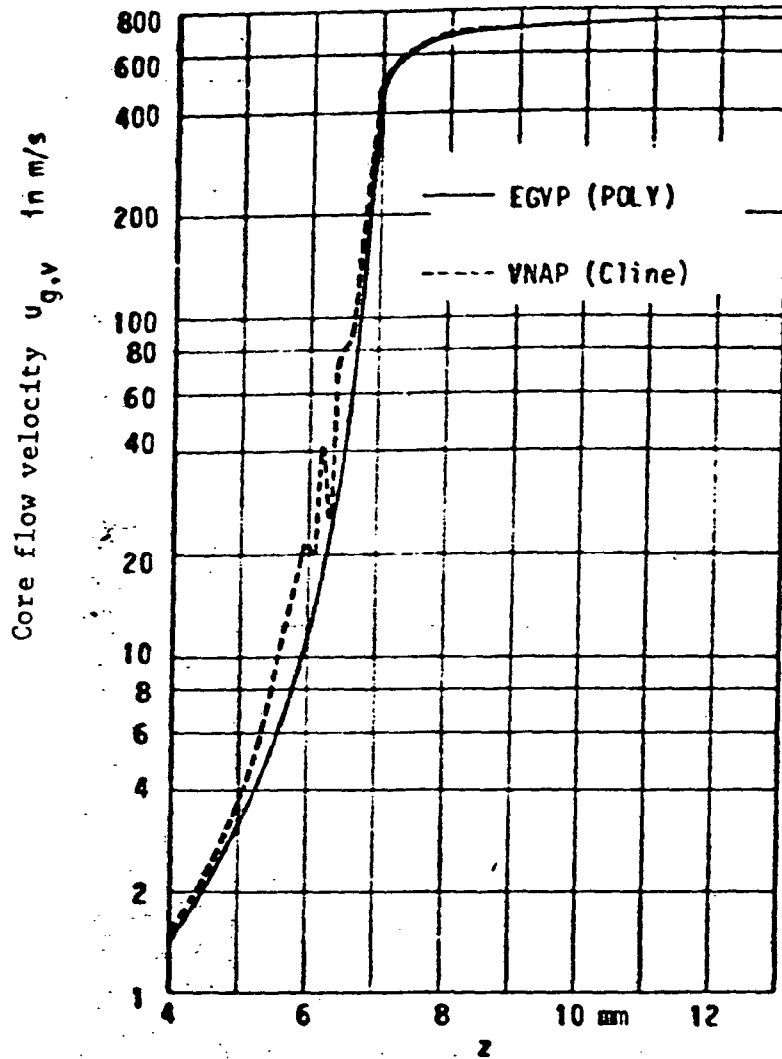


Figure 28 Comparison of the programs EGVP and VNAP with respect to the core flow velocity $u_{g,v}$

conclude from the agreement of u_g , M , p_g and T_g found above, that the boundary layer development is comprehended with a similar degree of agreement.

While work with the Cline procedure seemed relatively simple, due to correct program listings and a very precise description and good collaboration with the author, this can unfortunately not be extended to the second main comparison program, BLIMP [16,113].

Through at first fortunate circumstance, the Boundary Layer Integral Matric Procedure (BLIMP) reached the Chair for Space

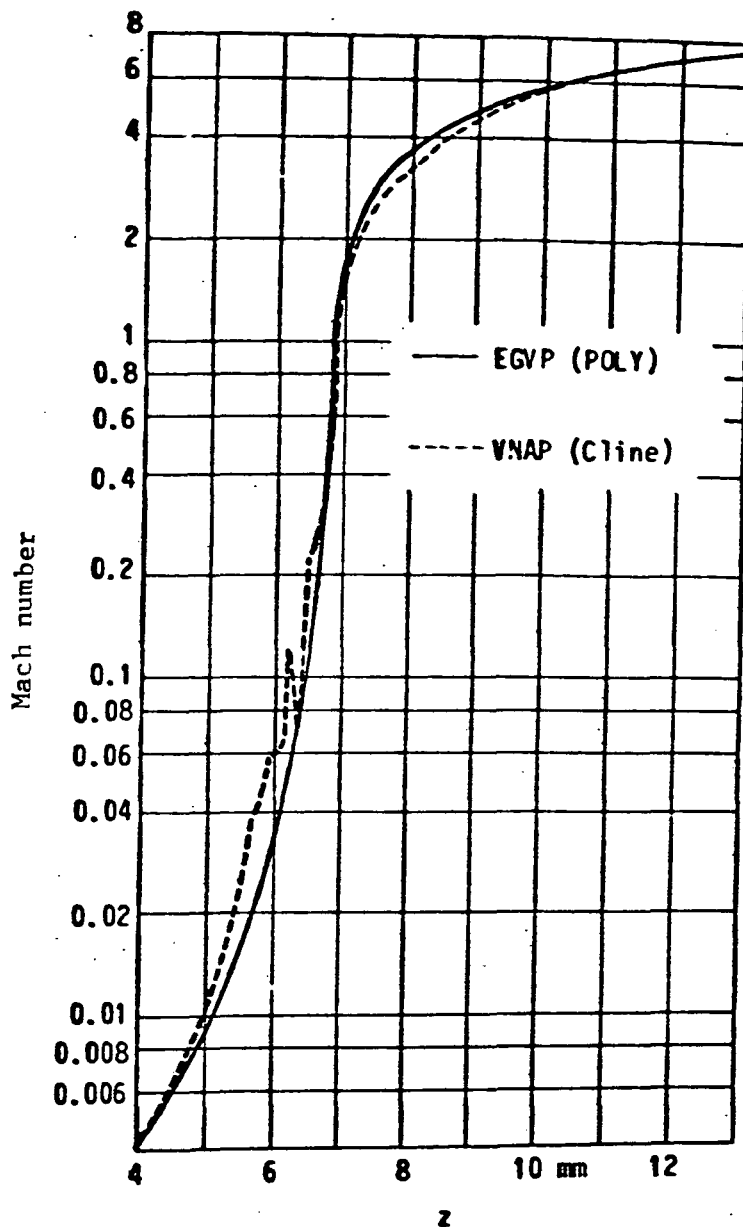


Figure 29 Program comparison EGVP-VNAP with respect to the Mach number

Technology. This program had been developed during the Seventies in the US, involving large expenditures in materials and leading /59 specialists, in the context of JANNAF, for application to many gas dynamics problems: from the flow over a flat surface under subsonic conditions, to 3-dimensional, non-stationary supersonic flow in rocket propulsion units. Since the documentation is

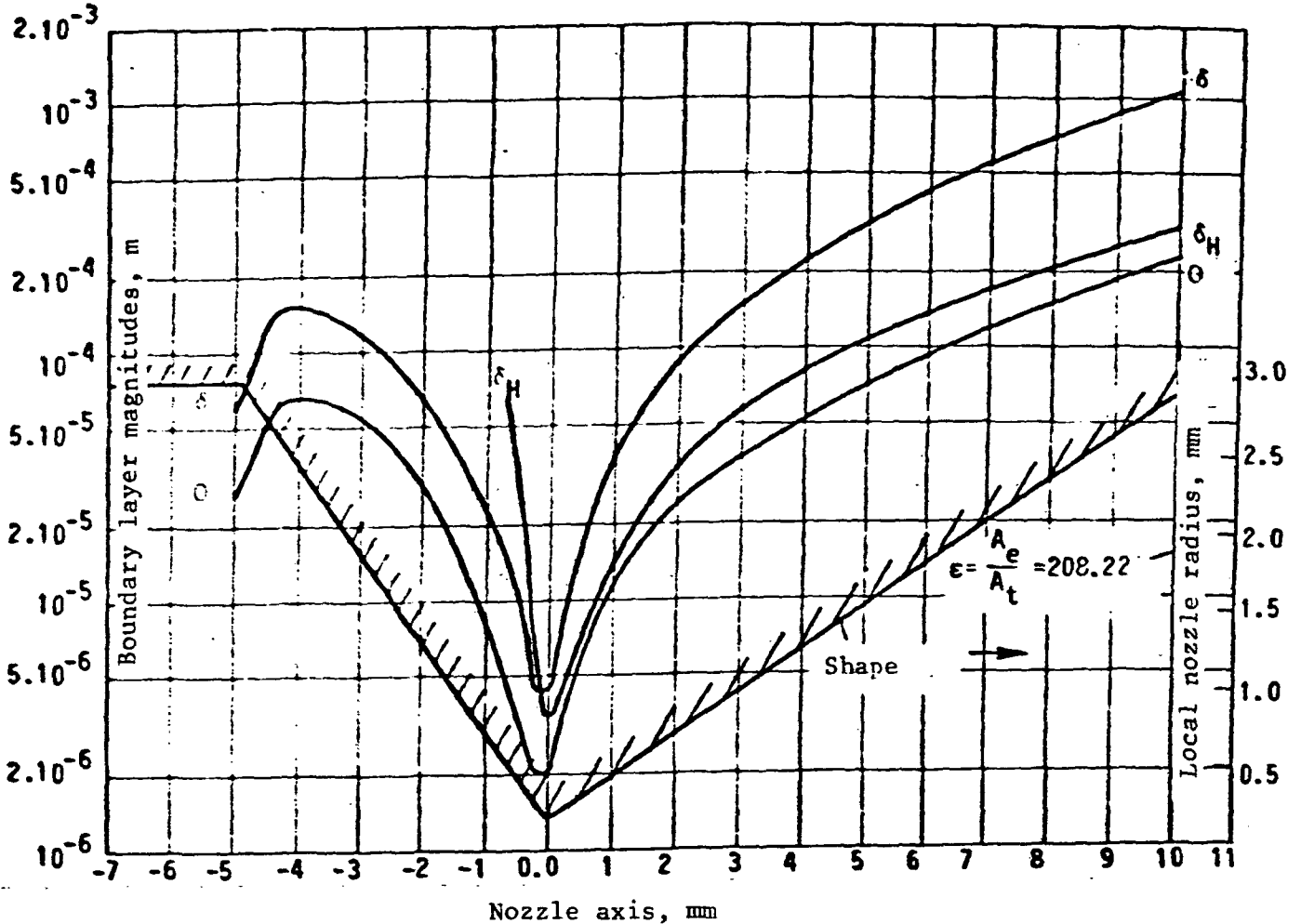


Figure 30 Course of boundary layer parameters obtained using BLIMP
 $p_c = 10$ bar; $T_c = 2300$ K; $r_t = 0.2$ mm; $\alpha_e = 15^\circ$; N_2H_4

insufficient and additional, machine-specific problems arose at the Leibnitz Computer Center of the Bavarian Academy of Sciences, we have to date been unsuccessful in our attempts to use the BLIMP program at the Technical University Munich. The example shown in Figure 30, above, was obtained directly in the US. It shows the boundary layer quantities δ , θ and δ_H (energy thickness) for a combustion chamber pressure of 10 bar, $T_c = 2,300$ K, $r_t = 0.2$ mm, $\alpha_e = 15^\circ$ and N_2H_4 (decomposed and heated). With the help of the energy thickness δ_H (see for instance Truckenbrodt [161]), it is possible to provide more comprehensive $\Delta\eta_{b1}$ loss

statements than with δ^* , otherwise (EGVP) used here. The mathematical formulation follows a similar principle and causes no additional problems. The comparison of BLIMP and EHVP data in regard to N_2H_4 propulsion units shows sufficient agreement; and hence additional justification for the simplified EGVP procedure and the system developed in section 2.2.10 is not necessary. It must still be remarked that a BLIMP calculation requires an initial data set provided with the aid of ODE, ODK (Gordon McBride) and TDK. After the first run of the BLIMP system the nozzle shape is corrected and the procedure is repeated. Customarily satisfactory convergence is established after two passes. Depending on the geometry and the reaction chemistry, the computer time required varies from 30 min to 2h CPU time. For comparison purposes, EGVP requires from 5 to 30 seconds.

2.2.10 Simplified performance prediction model

/63

While the computer program for predicting the performance of small rocket propulsion units, described in the preceding section, is considerably more modest, in regard to computer time and expense (by a factor of 100, compared to BLIMP), it still does not satisfy the criteria of simple engineering "rule of thumb" equations. This shall be attempted in the example of boundary layer losses, below.

2.2.10.1 Derivation of the approximation equation $\Delta\eta_{bl}$

The starting point is also the impulse equation, slightly modified for 1-dimensional flow,

$$\frac{dO}{dz} = \frac{c_f}{2 \cos \alpha} - \frac{O \tan \alpha}{r_t \epsilon^{0.5}} \cdot \frac{3 + 2 \epsilon^{*}/O - M^2}{M^2 - 1} \quad (94)$$

using the Reynolds number related to the impulse loss thickness

$$Re = \frac{p_c O}{c^* \epsilon \eta_g} \quad (95)$$

and with the viscosity function

$$\frac{\eta_{g,c}}{\eta_g} = k_{n,1} \epsilon^{k_{n,2}} \quad (96)$$

(The ϵ -dependence occurs because of the application of the ODE theory to T_g/T).

The shearing stress coefficient is determined as

/64

$$c_f = \frac{c^* \eta_{g,c} \epsilon^{1+k_{n,2}}}{\rho_c \theta} k_{c_f,2} \quad (97)$$

The impulse equation can now be rewritten

$$\frac{d\theta}{dz} = \frac{c^* \eta_{g,c}}{\rho_c} \epsilon^{1+k_{n,2}} \frac{1}{\theta} k_{\theta,1} \quad (98)$$

The surface ratio ϵ is replaced by $\epsilon = k_\epsilon \left(\frac{z}{r_t}\right)^2$. Using $\theta_0 = 0$ (start of integration at the narrowest cross-section), we obtain

$$(99) \quad \frac{\theta^2}{2} = \frac{c^* \eta_{g,c} r_t}{\rho_c} k_{\theta,2} \int_0^z \left(\frac{z}{r_t}\right)^{2(1+k_{n,2})} dz \quad \text{or}$$

$$\theta = \left(\frac{c^* \eta_{g,c} r_t}{\rho_c}\right)^{0,5} k_{\theta,4} \epsilon^{(0,75 + 0,5 k_{n,2})} \quad (100)$$

We can now determine $\Delta\eta_{bl}$ as

/65

$$\Delta\eta_{bl} = \left(\frac{c^* \eta_{g,c}}{\rho_c r_t}\right)^{0,5} \epsilon^{(0,25+0,5k_{n,2})} k_{n,bl,1} (1+\delta^*/\theta-\delta^2/2r_e\theta) \quad (101)$$

Introducing the throat Reynolds number

$$Re_t = \frac{\rho_c 2 r_t}{c^* \eta_{g,c}} \quad (102)$$

the expression for the boundary layer losses can be strongly /65
compressed:

$$\Delta\eta_{bl} = \frac{k_{\eta,bl}}{Re_t^{0.5}} \epsilon^k \quad (103)$$

2.2.10.2 Loss estimates for various working fluids

With increasing Reynolds numbers in the throat region - which can mean higher chamber pressure, larger propulsion unit dimensions and higher thrust - the boundary layer losses decrease, in terms of percentage. In contrast, an increase in the surface ratio also increases the losses. It is important to establish that the trend of equation (103) remains unchanged, even using other expressions for c_f . This has made it possible to formulate available experimental data and the theoretical results of extremely comprehensive computer programs with the help of a very simple equation. Hence the design of a future propulsion unit can be determined very efficiently with respect to the optimum surface ratio ϵ . The precision of the result of equation (103) is surely sufficient, if we take into consideration how difficult it is to determine the other parameters, such as c^* , p_c , T_c , ϵ , etc. To determine the two constants in equation (103), a series of available experimental data and voluminous calculations were /66 performed with the corresponding procedures, for different media.

The results of the determination of correlation coefficients for various working fluids are shown in Figure 31 (page 69). The Freon-14 curve lies above those for simple gases, even though the viscosity of H_2 , for instance, is higher than that of CF_4 . Apparently, the explanation for this departure must be sought in that during the expansion process (and the concomitant cooling of the gases) CF_4 recondenses to small droplets (boiling point at 1 bar approximately $-130^\circ C$), leading to higher loss measurements.

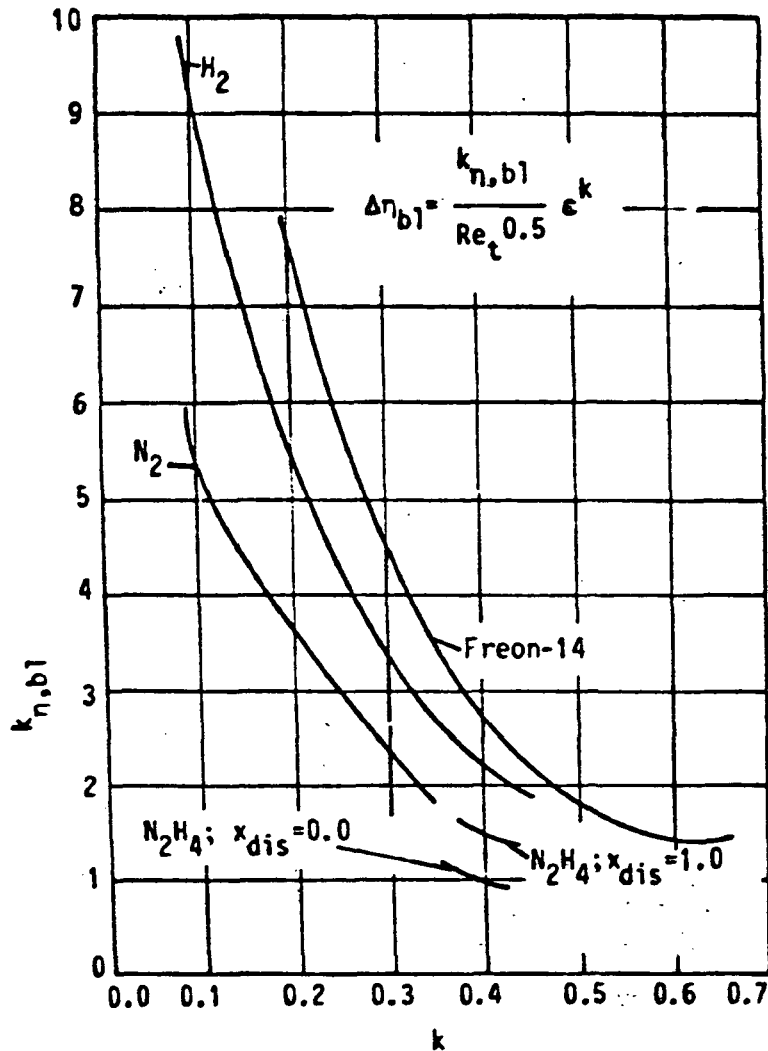


Figure 31 Course of the boundary layer loss coefficients for various types of gases, from available experimental data

In an ideal case, the curves shown in Figure 31 should come together at one point, for each type of gas. If this does not occur it is because the diagram was built using many sources, whose individual results show considerable departures [60]. Because of the hyperbolic nature of the curves and the mathematical quality of equation (103) it is possible to insert pairs of $k_{\eta,bl}/k$ values (by prescribing ϵ and Re_t), without the boundary layer loss $\Delta\eta_{bl}$ diverging substantially.

3 EXPERIMENTS WITH MICROPROPULSION UNITS TO BETTER CORRELATE /68 THE RESULTS OBTAINED IN SECTION 2

3.1 Requirements for the test and measurements facilities

A substantial experimental program is carried out to provide an underpinning for the results attained in the preceding section, to measure specific performance quantities in miniature propulsion units. As can be anticipated from the theoretical results, severe requirements must be placed on test design and measurement precision, in order to be able to identify the individual performance losses, for instance due to boundary layer effects.

The development of detailed test facilities must start, in each case, from the following boundary conditions and physical quantities:

TABLE 3 Precision requirements for the measurement installation

Thrust range:	10 - 2000 mN \pm 1%
Mass throughput:	10 - 2000 mg/sec \pm 1%
Combustion chamber pressure:	1 - 20 bar \pm 0.3%
Combustion chamber temperature:	290-300 K \pm 0.5 K
Nozzle throat diameter:	0.25 - 0.8 mm \pm 0.003 mm
Surface ratio:	1 - 200 \pm 0.5%
Gas type:	N ₂ repurified (99.99% N ₂)
Measurement durations:	1 - 100 sec \pm 0.1%
Safety	
Reproducibility	
Manufacture of individual components in the Chair's own shops	
Financial context	< 10,000 DM (outside financing)

3.2 Test facility description

Without the Chair for Thermodynamics (Prof. Dr. E. R. F. Winter)

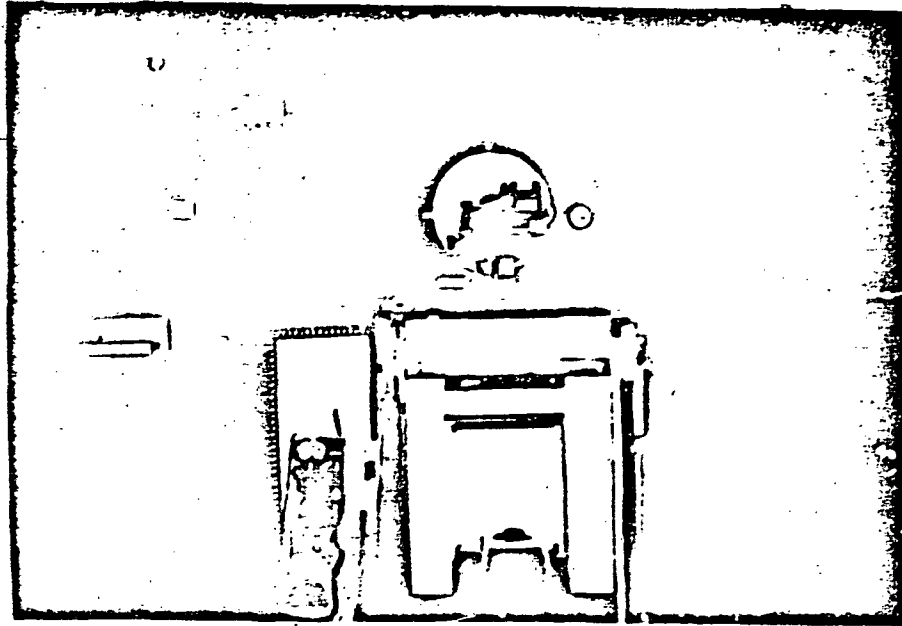
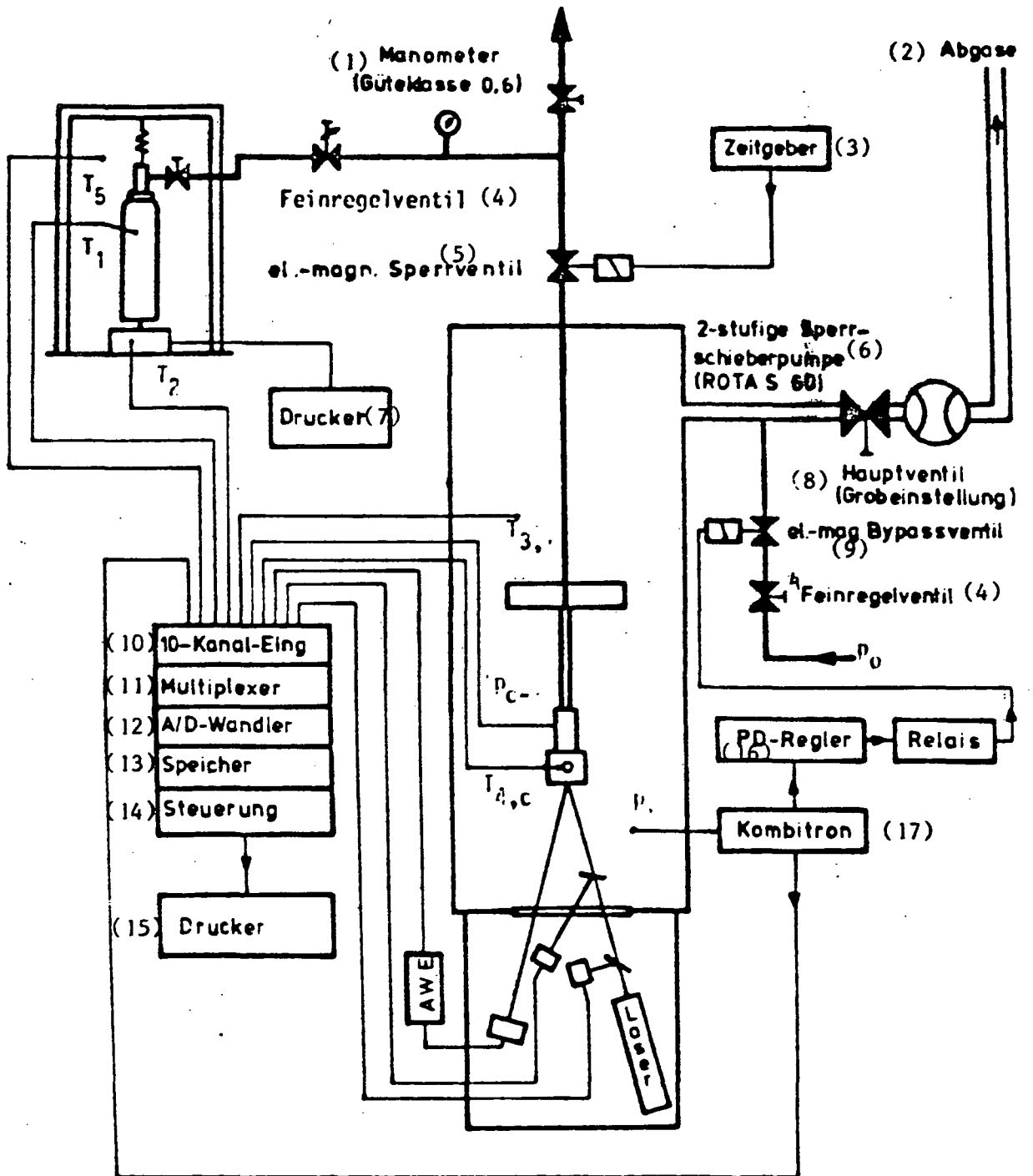


Figure 32 General view of the altitude test stand for cold gas propulsion units

at TUM [Technical University at Munich] generously providing a laboratory, due the extreme space scarcity at the Chair for Space Technology this experimental study in the area of rocket propulsion unit performance measurements would not have been possible [55,163]. A massive frame construction was installed in the already available (as a loan from the DFVLR [Deutsche Forschungs- und Versuchsanstalt fuer Luft und Raumfahrt = German Research and Test Facility for Air and Space Flight]) altitude simulation chamber. This frame holds the propulsion unit's suspension, F-calibration device, N_2 gas supply, p_c and p_∞ measurement pipes, temperature sensors and components of the optical thrust measurement arrangement. The Figures 32 (above) and 33 (page 72) show an overview. The N_2 supply storage (including the \dot{m} measurement system) is located outside the vacuum chamber, as are the main components of the thrust measurement system, various electrical supply devices and measurement value acquisition and processing [17,20,40,52,74,75,78,98,101,155,168,169,178].



(please see KEY page 73)

Figure 33 Test arrangement (schematic)

KEY to Figure 33 (page 72) 1 Manometer (quality rating 0.6) 2 Exhaust gases 3 Timer 4 Needle valve 5 Electromagnetic stop-valve 6 2-stage blocking piston valve pump 7 Printer 8 Main valve (gross adjustment) 9 Electromagnetic bypass-valve 10 10-channel input 11 Multiplexer 12 A/D converted 13 Memory 14 Control 15 Printer 16 PD regulator 17 Kombitron

3.2.1 Vacuum installation

/71

To compensate for the upthrust of the thrust equipment during calibration of the thrust measurement system, the environmental pressure in the vacuum chamber (useful volume approximately 150 liters) must be adjusted to the underpressure present during the calibration phase of the "nozzle test run" to be performed subsequently. To this end, the suction of the rotary vane pump (LH-S60) can be adjusted by means of a "bypass" needle valve. A specially developed analog PD regulator (see Figure 34, below)

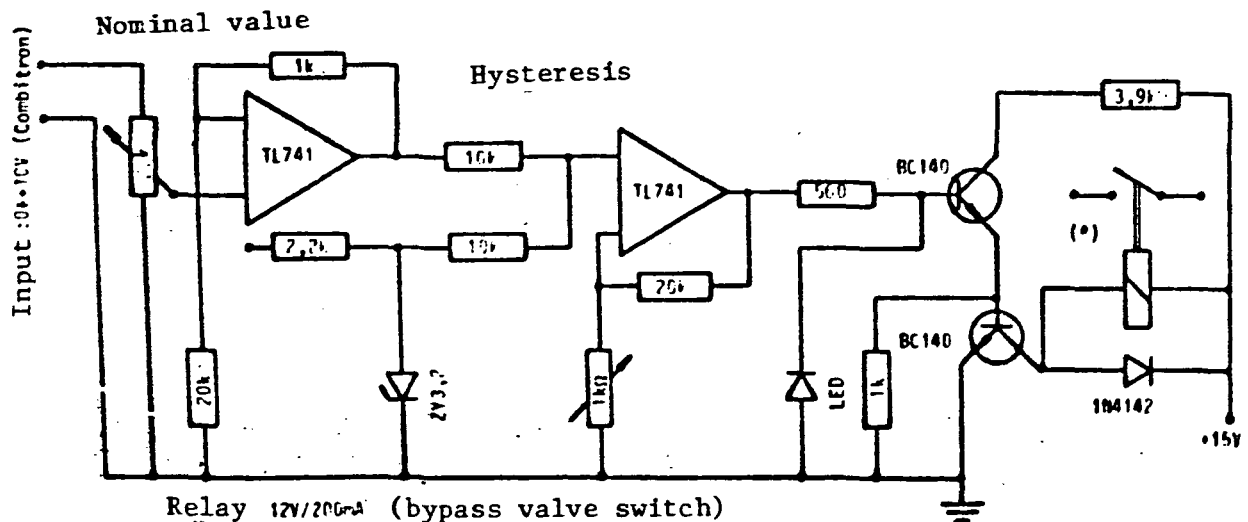


Figure 34 Circuit diagram of p_{∞} -adjustment (bypass valve control)

controls the "opening" and "closing", respectively, of the bypass admission of external air into the rotating vane pump's suction line. By using LH-Thermovac and LH-Penningvac pressure measurement pipes in connection with the LH Combifron supply and indicator system, the actual value of p_{∞} is supplied to the control circuit (Mr. Matthern of DFVLR Oberpfaffen was kind enough

to perform the calibration of the p_{∞} sensor system for us).

The p_{∞} adjustment makes it possible to achieve a reproducibility of better than 1% in the pressure range of 10^{-2} - 10 Torr here under consideration, which is sufficient with respect to thrust measurement errors due to upthrust effects (see also sections 3.2.2.2 and 4.3).

3.2.2 Thrust measurement system

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In general the thrust of a rocket propulsion system can be described as the product of the effective discharge velocity and the mass throughput:

$$F = \dot{m} c_{eff} \quad (104)$$

While in most test cases the propulsion unit's mass throughput can be determined with reasonable efforts, a direct, precise measurement of c_{eff} is not possible. This is due to the following reasons:

- 3-dimensional distribution of the discharge velocity
- 3-dimensional pressure distribution in the end cross-section
- Condensation shock, flow separation
- Assignment of local density and velocity distribution
- Sensor problems
- Reduced size of the nozzle geometry (in the case to be examined here)

Hence only an integral measurement of F can be used here. Because of the small forces involved, the methods used for large rocket propulsion units - using DMS sensor to measure the deformation of the thrust stand - can not be applied. While inductive displacement pick-ups could measure some of the "large" nozzles (2N) used here, their resolution is limited for the lower thrust

range (20 mN), and they can hence not be used. It was decided not to use torsion balances - as they are used for small N_2H_4 single-component fuel engines (ERNO) - since they allow the determination of only the thrust time integral, from the total torsion angle, rather than the temporal course of the thrust.

Because of the drift problems in the charge amplifiers that would be necessary for the nearly stationary operation case, piezoelectric sensors can not be used. In addition, to reduce the mechanical influence of supply lines and calibration devices on the thrust measurement method, contact-free methods should be included in a narrower selection. /73

- Due to the required resolution, it is not possible to use radar methods
- Optical interference methods are possible, but very demanding in their implementation and difficult in terms of measurements evaluation (linearity errors, counting problems)
- Optical "edge" and "slit" system were evaluated in preliminary testing but eliminated because of their strong dependence on the light source's intensity value.
- The situation is analogous for systems that translate the smallest deflection of thrust transverse beams into intensity changes, by means of the displacement of a polarization filter
- The F-measurement principle finally chosen is described in detail in Figure 35 and 36 (pages 76, and 77):

A simply polarized laser beam strikes a mirror installed on the propulsion unit's flange, parallel to the thrust direction (first surface mirror). The thrust frame consists of a cantilever beam that simultaneously represents the gas supply pipe. At its free end is the installation flange with the propulsion unit, which generates a thrust acting vertically downwards. This causes the pipe to be deformed along its deflection curve bending line,

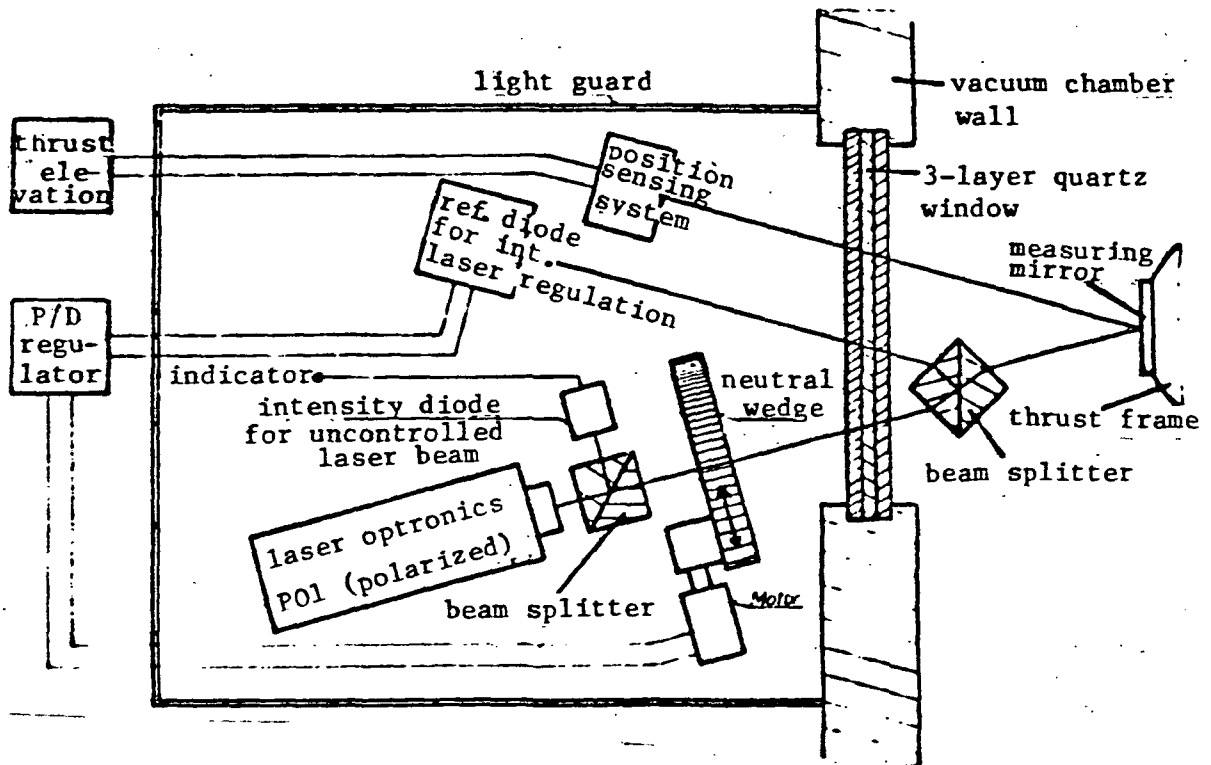


Figure 35 Laser thrust measuring system

such that the mirror alters the angle to the incident and the reflected beam. Outside of the vacuum chamber the reflected beam is sent to a homogeneous linear array (LSC-5D, United Technologies). This beam position measurement probe - which operates on the Schottky principle - permits a resolution of better than $0.1 \mu\text{m}$, using the appropriately adapted electronics (TS-Elektronik Munich, FRG).

In spite of the required resistance of the bending pipe against 175 internal pressure (to a maximum of 25 bar), the resolutions allows dimensioning that pipe in such a manner that in conjunction with the corresponding optical "lever arm" thrust forces in the range of 20 mN to 2 N can still be measured with sufficient precision.

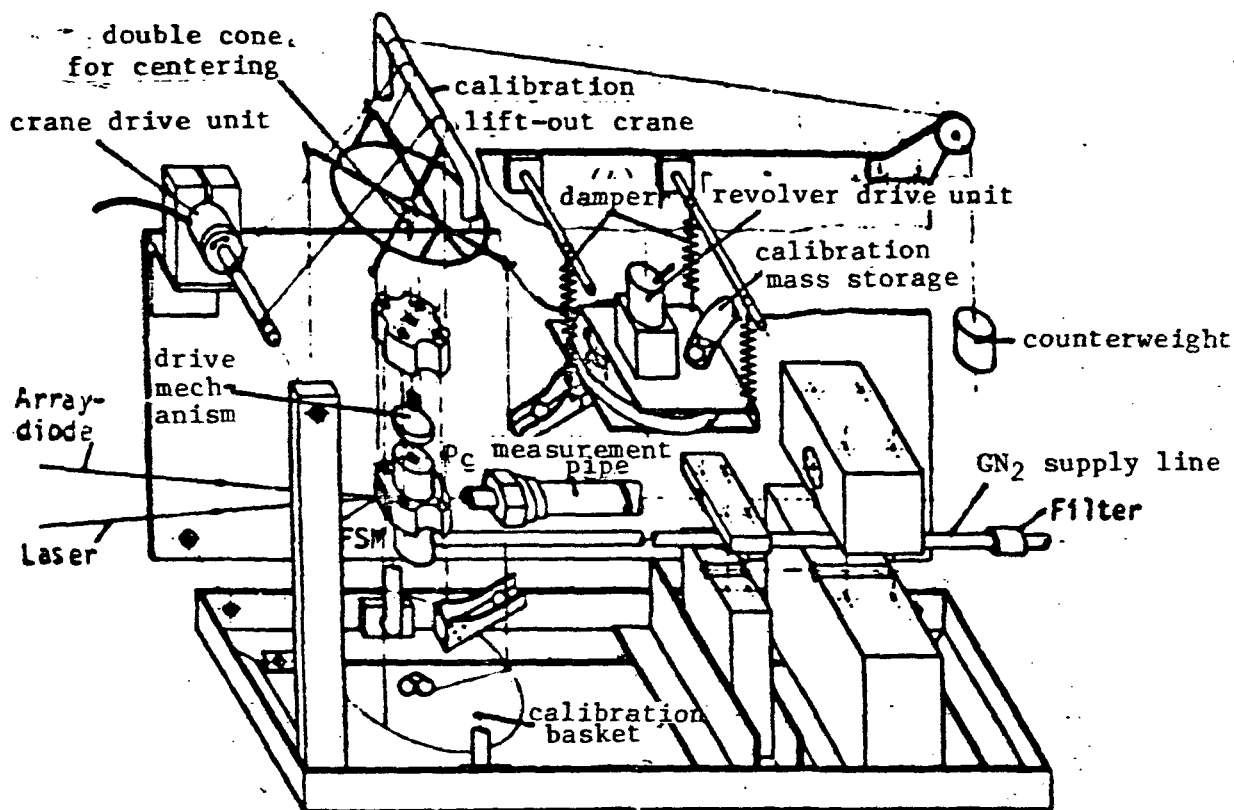


Figure 36 Mechanical test construction within the vacuum chamber (shown isometrically and partially disassembled for better understanding)

Interpretation involves purely elastic resistance expressions, which after numerous calibration measurements seems to be permissible (see also section 9.1).

Since both the LSC array sensors and the necessary evaluation electronics still require empirical values from use in day-to-day laboratory practice - in contrast to the segmented position sensors already used for longer periods of time - it may be assumed that the reproducible resolution of the position measurement procedure can still be improved upon. It does not seem necessary to point out in detail that the method here presented is also suitable for

larger propulsion units and other problems, in which the recording of very small position changes is necessary. Although in principle the optical thrust measurement procedure is of very simple design, during implementation the edge effects causes problems whose solution is quite laborious. Diffraction and refraction influences of the laser beam, caused by optical windows and beam refraction on gas molecules, can be corrected, or even avoided by the use of polarization filters, quartz windows and the required air density control in the vacuum chamber.

The main problem occurring in the intended experiments is keeping the laser beam intensity constant.

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Figure 37 Laser-optical thrust measurement system (beam path made visible using smoke. Exposure time: 4 minutes)

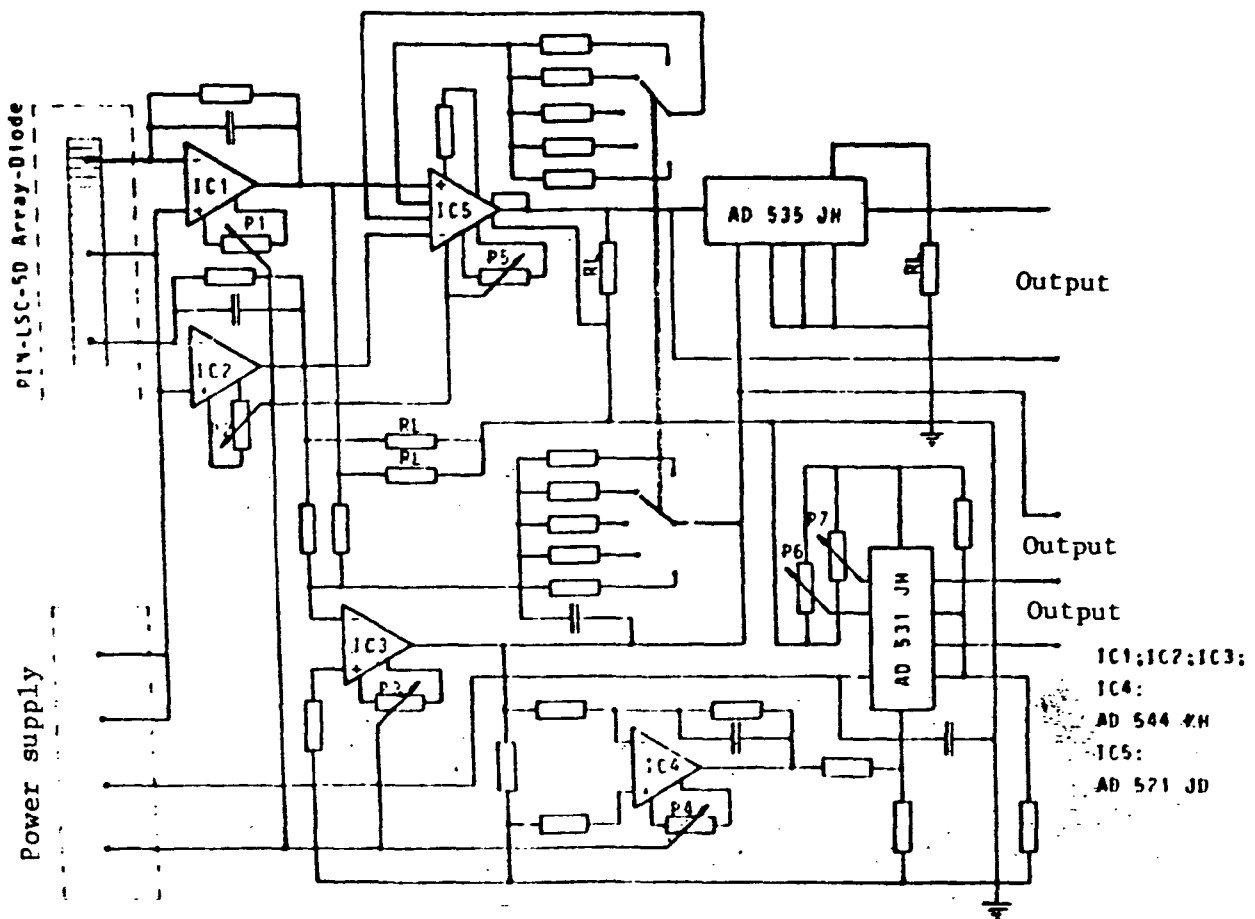


Figure 38 Laser-array diode evaluation electronics

3.2.2.1 Laser intensity control

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Long and short-period variations in the laser beam output intensity are due to line voltage variations (long-term and short-term), temperature influences and the plasma physics processes inside the laser tube. In the case of the He-Ne laser system used here, the amplitude can be up to 2% of the nominal initial output. In addition, there is the constant degradation of the beam output due to diffusion of foreign atoms in the gas laser's glass tube. The array diode deflection measurement procedure is capable of linearizing and compensating for the changes mentioned above, in a first approximation (including

the subsequent amplification and evaluation electronics). The remaining higher order interference terms, however, prove to be intolerable in their effect on the resolution and reproducibility of the thrust measurement procedure.

Hence it is necessary to develop a procedure for an active stabilization of the laser intensity. To this end, we first replaced the laser system CWR-LS-05 (with unregulated power supply), by means of the model Laser Optronics LO-101 P, whose power supply reduced the initially necessary ignition voltage of 10 kV, to a continued operating voltage of 1500 V, after the start of operation. In addition, it smoothes out intermediate-term tension variations of the supply line voltage.

We decided against the purchase of a very expensive (nearly DM 30,000) power supply, especially tailored for laser problems, since it can eliminate only certain line influences in the short and long-period fluctuation range, but does not eliminate the thermal variations of the laser intensity, or those due to plasma physics, ultimately. Among them are, for instance, the effects caused by "mistuning" of the laser mirror system at the two tube ends, caused by thermal shifts.

The intensity stabilization system finally used was shown in /78
Figure 35, in schematic form. Via a prismatic beam splitter, 50% of the beam output is deflected towards a photodiode operating in the He-Ne band, as an "actual value" indicator (in order to compensate for the influence of the different gas densities on the diffraction of the laser beam, the beam splitter is arranged within the altitude simulation chamber). In a specially developed PID regulator (circuit diagram below, page 81), the instantaneous actual value of the laser intensity is compared to an adjustable nominal value [40]. When the appropriate adjustment difference occurs ($\approx 50 \mu\text{V}$) it is amplified sufficiently so that a micro-metric control can be set in motion via a down-stream, direct current minimotor. On this mechanically prestressed control (to

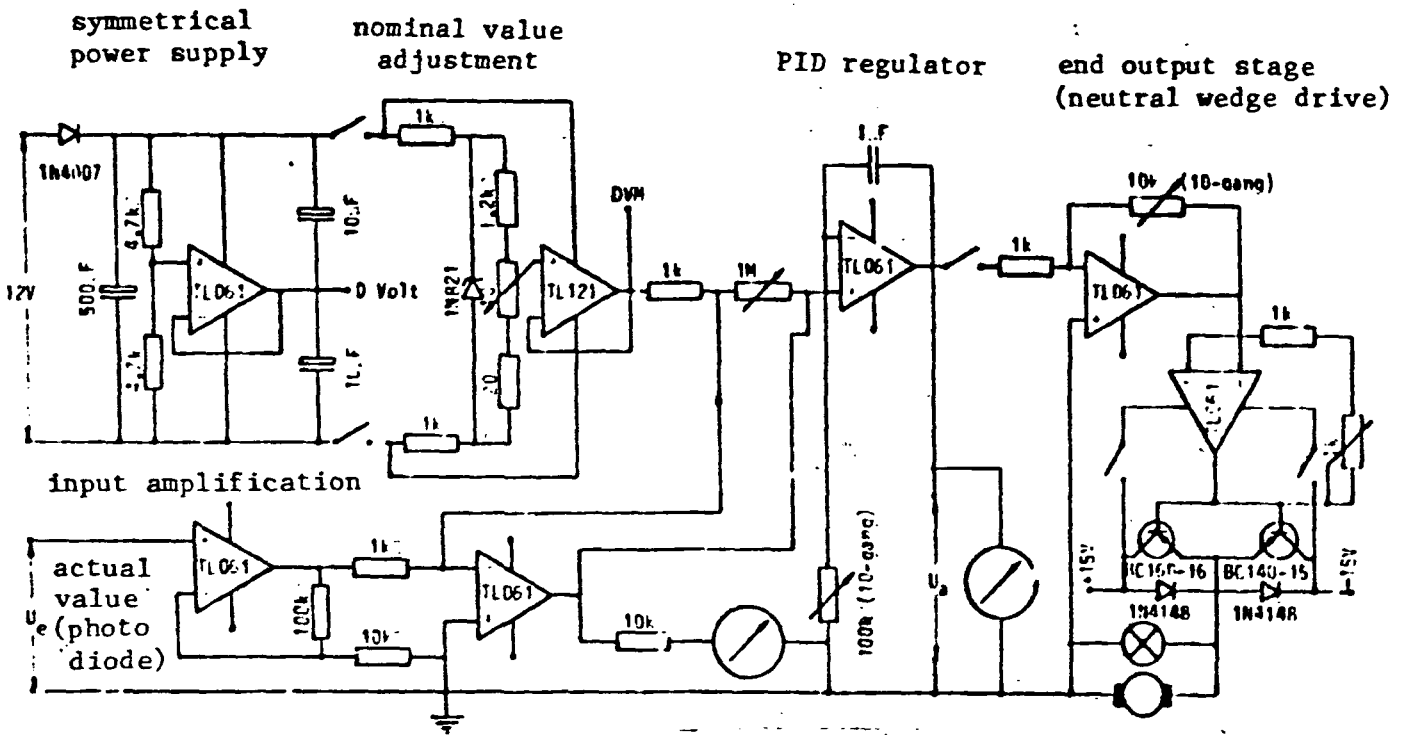


Figure 39 PID Laser intensity regulation

avoid slippage during pole reversal), there is located a continuous neutral wedge. This optical component - which acts as a linear filter - is placed in the beam path, between the laser exit and the prism mentioned above. It thereby becomes possible to correct for the smallest intensity variations and the continuous output decrease (life-time dependent). The integral portion of the regulator limits the long-term weakening to less than 3%. The differential portion of the control electronics makes it possible for the regulating circuit to react already at the beginning of a steep interference flank, before maximum amplitude is attained (leading effect). Large demands are placed on the proportional part, because of the necessary amplification factor of approximately 10^5 , since circuits of these characteristics, with amplification factors $>10^3$ tend to be dynamically unstable. Hence, a multi-stage amplification chain should be adopted. It is absolutely necessary, in addition, to use

"offset"-balanced operational amplifiers of a model with high temperature stability specifications. In spite of this very laborious detail work, in its technological implementation, we were at first not sully successful in compensating for the very strong short-term line fluctuations, determined by specific local conditions (caused by the discontinuous operation of machines of high power consumption). It thus became necessary to operate an independent supply line (see Figure 52). It consists /79 of a 24 V, 15 A battery charger, with a 400 Ah fork-lift accumulator and a 24 V DC/220 V, 50 Hz direct current/alternate current inverter (200 W output power). A test/loading cycle time of approximately 1:1 is thereby attained. The nominal block to block time is approximately 20 h: after at the most this period of time the laser power supply must be switched back to the public power network, to recharge the accumulator. Since the entire laser-optical thrust measurement system is kept under a light-tight cover to avoid outside light influences, active cooling must be provided to prevent heat accumulation near the laser, due to the laser's own heat losses. Open water circulation circuits are adequate for this purpose.

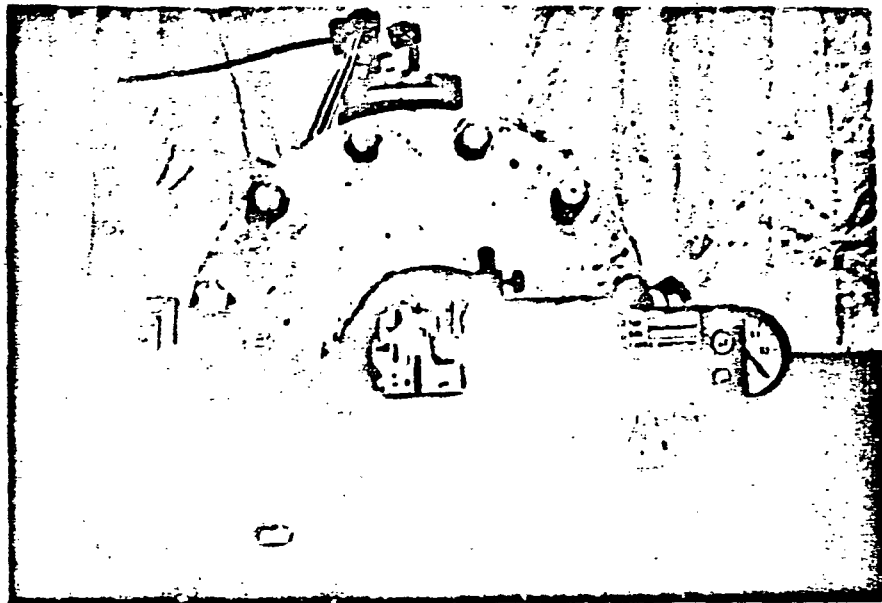


Figure 40 Portion of the thrust measurement system outside of the vacuum chamber

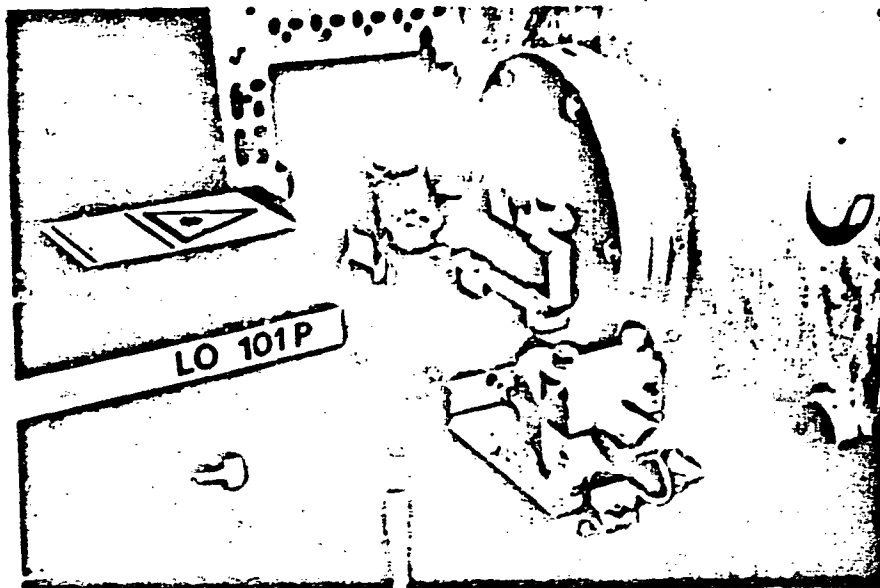


Figure 41 Neutral wedge control (active control member) for laser intensity stabilization

3.2.2.2 Calibration device for thrust measurements

81

In order to calibrate the thrust measurement system, first the environmental pressure p_{∞} occurring inside the vacuum chamber is established, in a preliminary tests, as it is under full pump suction power and nozzle flow (leak rate) at fixed p_c . Next the N_2 supply pipeline is interrupted and the p_{∞} regulating circuit is activated (see also 3.2.1). Thereby the environmental pressure is fixed at the value determined above and the upthrust influences due to residual gases in the chamber may be considered compensated. Now the calibration basket (see Figure 43, page 84) is introduced through the divergent nozzle portion. The basket's positioning is so designed (double cone, point contact) that calibration masses placed in the calibration basket can exert only vertical components in the thrust direction and position of the nozzle axis. By means of a revolver cassette system, arbitrary quantities of beads of precisely know mass can be admitted to the basket. These beads simulate the "calibration thrust" for the

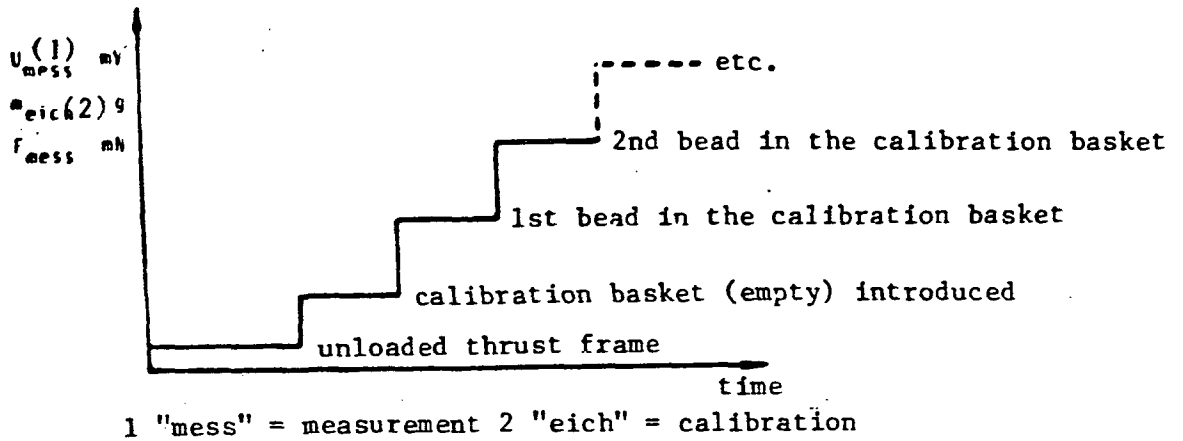


Figure 42 Qualitative course of the thrust calibration

(/82)

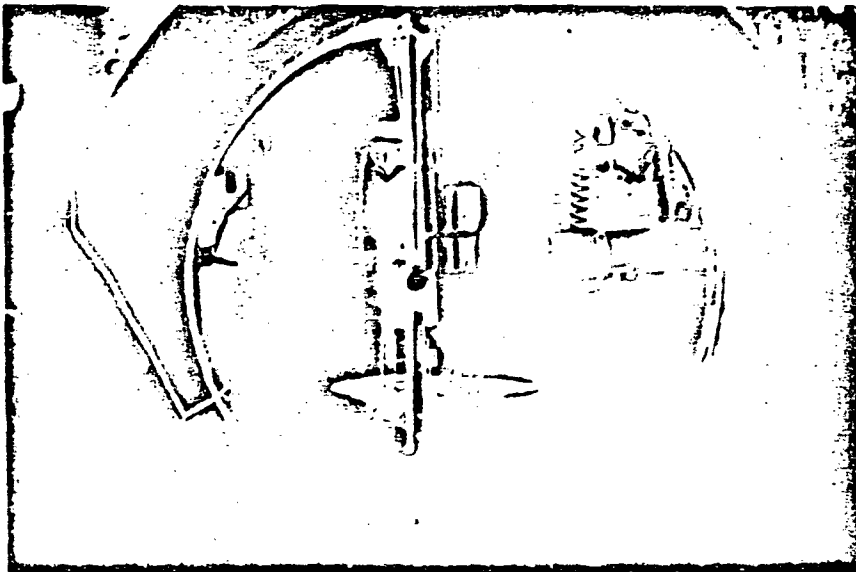


Figure 43 Propulsion unit suspension with flanged combustion chamber pressure determination and calibration device of the thrust measurement system

thrust measurement system. The response of the measurement system is shown in Figure 42, above, for the individual beads falling into the basket (Mass: typically 3 g).

From the step function obtained during the calibration phase /82
it is now possible to determine the gradient of the function
 $F = f(U_{\text{meas, thrust}})$. Once the calibration measurement is com-
pleted, the calibration basket including its position cone is
removed from the propulsion unit by means of automatic controls,
so that that the precision performance measurements can be
performed immediately following. Unavoidable zero-drift in the
instruments is thereby prevented from exerting undue influence
on the precision of the measurements. For additional control,
the calibration was repeated after each measurement series.

3.2.3 Mass throughput determination /83

The mass throughput \dot{m} is the most important limiting quantity
- next to the thrust - in the experimental determination of a
rocket propulsion unit's specific performance I_{sp} .

A large number of physical principles - which in turn can be
expressed technologically in an enormous multiplicity of forms -
could be used in its measurement. In the context of this study,
the most significant possibilities were examined either by
preliminary theoretical considerations, by borrowing existing
systems and by extensive preliminary testing. Therefore, the
listing following should be considered only as an overall review.

3.2.3.1 Comparison of the various alternatives [28,31]

a) Throughput measurements using turbine rotor systems:

A turbine rotor is fitted into a feed pipe, with its segmented
axle made alternately of conducting and non-conducting
material. The fluid's motion causes the turbine to start
rotating, and in a coil arranged around the axle, an alternating
current is induced, whose frequency can be assigned to the
rotation rate and hence, to \dot{m} . It can be shown that this equip-
ment - which functions satisfactorily for liquids (and large
throughput rates - does no longer operate with the required
precision in the case of small gas volumes, among other

reasons because of slippage and compressibility problems (see section 3.1). Furthermore, the calibration is possible only if an additional system is used (see point j), below).

b) Pressure difference determination:

The resolution of the Δp measurement range here demanded requires very small slit opening diameters (in the 0.1 mm range) and hence, is strongly dependent on the discharge coefficient ψ , which is a function of combustion chamber pressure (or respectively, of the injection pressure: $p_c + \Delta p_{inj}$).

Taking into account Mertel's work [101] and after some preliminary testing, this possibility was not further pursued.

/84

c) Perpendicular pipe with float element:

A vertical glass tube with calibration marks is installed in the N_2 pipeline (flow direction: vertical, upwards), inside which a spherule can move, of a material selected as a function of its specific gravity and the pipe flow's dynamic pressure. Independently of reading problems, this method - often used with liquids - is not satisfactory, due to slippage and environmental effects, for small gas quantities.

d) Filling status measurement using a secondary medium (liquid):

An alternative often used in technology is a liquid column connected to the gas storage container. The pressure remaining in the container can be estimated from the displacement of the liquid level, and hence, the quantity of gas used. Based on the required specification, the thermodynamic conditions (T-P problem) proved to be badly reproducible. An electronic indication of liquid level is additionally impeded by the lack of adequate liquids (conducting, or optically evaluated, etc.).

e) Measurement of the pressure increase upon discharge into a

large container:

The possibility of determining \dot{m} by recording the course of the pressure in a large chamber of known volume, as a function of the valve setting of the rate of flow, had to be discarded, after intensive preliminary testing. This was due to the fact that because of the necessary valve opening times Joule-Thomson effects and environmental temperature influences could no longer be neglected.

f) Direct optical measurement of the velocity of flow: /85

This alternative also had to be ruled out, because the density differences in the N_2 working medium were not sufficient to render clearly visible changes in the flow velocities within the pipe. The admixture of particles that would positively change this characteristic had to be excluded because of the gas purity requirements.

g) Direct inductive or capacitive measurement of the quantity discharged:

Preliminary work was performed also on this concept, in connection with variation d), above. This alternative also had to be abandoned because of purity requirements (see also f))

h) Heated wire probes:

After intensive collaboration with suppliers of such systems the integral measurements of the flow velocity and of the medium's density (repurified N_2) by heated wire anemometer procedures proved to be insufficiently precise for the small tube diameters here used (\emptyset typically 2 mm), as well as non-reproducible, because of capillary action and the influence of the probes on the flow itself.

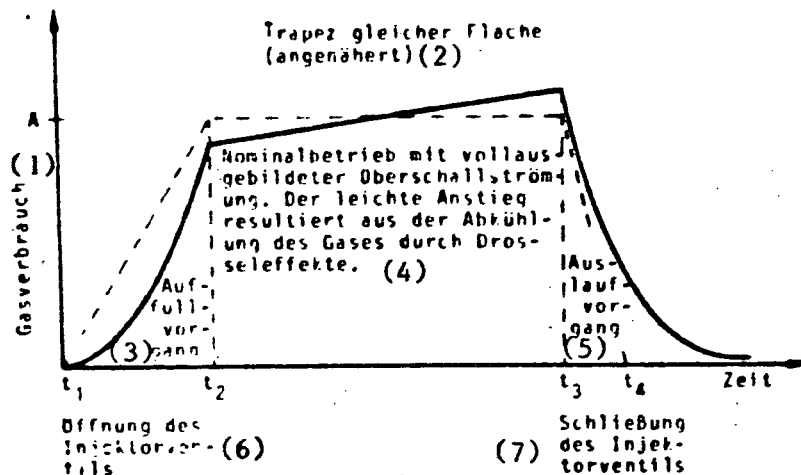
i) Laser Doppler velocity meter:

Eventually, this laser-optical method, given appropriate development efforts on the systems available today, will permit direct measurements of the flow profile in narrow tubes and of

the nozzle discharge velocity distribution. Since currently the obtainable precision is still insufficient, the application of this method had to be disallowed, in the context of this study.

j) Weighing system:

/86



KEY 1 Gas consumption 2 Trapeze of equal surface area (approximated)
 3 Filling process 4 Nominal operation at fully formed ultrasound flow. The slight increase is due to gas cooling by the throttling effect 5 Emptying process 6 Opening the injector valve 7 Closing the injector valve

Figure 44 Typical mass throughput course (time scale distorted)

All methods described would require additional calibration methods in the event of their application, ultimately based on gravimetric methods. Hence the idea arises of using such methods directly, without the intermediate steps described above. These gravimetric methods can be divided into two main groups:

- Continuous weighing $\rightarrow \dot{m} = f(t)$
- Integral weighing (before and after the flow process) \rightarrow

$$\int_{\text{vor}}^{\text{nach}} \dot{m} dt)$$

"nach" = after
 "vor" = before

The tendency shown in Figure 44 (page 88) is decisive for the latter of these versions.

The approximation of the N_2 throughput is usually performed /87 by application of the trapeze equation [68]

$$\int_{t_1}^{t_4} \dot{m} dt = A \cdot \left[\frac{(t_4 - t_1) + (t_3 - t_2)}{2} \right] = m_{\text{vor}} - m_{\text{nach}} \quad (105)$$

$$A \diamond \bar{m} = \frac{(m_{\text{vor}} - m_{\text{nach}}) \cdot 2}{(t_4 - t_1) + (t_3 - t_2)} \quad (106)$$

On the one hand, the trapeze method would be sufficiently precise (i.e., the filling and emptying processes could be neglected) if the increase in \dot{m} due to the throttle effect at very large differences $(t_3 - t_2)$ did not occur. On the other hand, however, it is precisely for large values of $(t_3 - t_2)$ that the throttle effect has an increasingly interfering effect, which forces keeping test times in the direction of smaller Δt values; because of the non-stationary gas consumption during switching on and off, this, in turn, worsens the precision.

In case of continuous weighings of the N_2 consumption, these effects are of subordinate importance, since one can wait for stationary conditions before taking several \dot{m} -values. This also makes it possible to evaluate drifts (caused by gas cooling) quantitatively.

3.2.3.2 Selected weighing system - PC 4400

The main problem of this measurement method is ultimately the required resolution per weighing (better than 0.01 g), with the simultaneous utilization of a relatively heavy storage container (approximately 7.5 kg). The balance eventually decided on (Mettler, Zurich; PC 4400), with a resolution of 0.001 g and a measurement range to 4.4 kg, is by far the best instrument on the market, for its range. Since no systems exists with a comparably high resolution beyond the measurement range of 4.4 kg, the measurement problem becomes therefore displaced to the precompensation of the remaining 3.1 kg of the storage container (including the reduction station and the gas supply), which can not be balanced by design changes. Safety regulations, the test times required and the mechanical design overall do not allow for a container with a total mass substantially below 7.5 kg. In the required prebalancing, a decisive advantage of the basic balancing principle of the PC 4400 chosen, finds its expression: the mass to be determined presses on a vertically freely moving cylinder, kept in its position by the action of a strong magnetic field. An optical edge establishes this position to better than 0.0001 mm and provide actual value information to a control circuit, such that it can change the coil current until the magnetic force fully compensates the force due to the weight, and the cylindrical rod again occupies its original (unloaded). This means that the PC 4400 balance weighs without displacement. Hence the coil current is a direct measure of the corresponding mass. /88

On this basis several prebalancing principles were examined theoretically and experimentally:

- Counterweights with roller or knife-edge bearings

In the end it was not possible to solve the mechanical bearing problems (close collaboration with the Chair for Precision Instruments, Prof. Unterberger [176]).

- Upthrust body

Immersion of hollow bodies into liquids or upthrust generation by means of gas-filled balloons had to be abandoned because of problems of reducibility due to environmental influences (mainly dependence of characteristic material values on T_{∞})

- Permanent magnet electromagnets

/89

These methods also had to be excluded because of their long-term behavior (decrease in field intensity) and dependence of the magnetic properties on T_{∞} , following very extensive preliminary testing (in addition, the balance system was affected by the strong compensation fields required.)

- Spring system

Since as we mentioned above, the PC 4400 weighs without displacement, spring compensation is appropriate

$$F_{Feder} = \Delta L \cdot c \quad ("Feder" = \text{spring}) \quad (107)$$

The first preliminary tests already showed that small changes in the environmental temperature, near the spring - caused, for instance, by convection currents - changed the spring constant so sensitively, that reasonable measurements became impossible. In order to solve this $c = f(T_{\infty})$ problem, first a pendulum construction (see also clock pendulum) was implemented using three compression and three tension springs, in this case, made of the same material; its main characteristic is that it solves the temperature stability problem with respect to the relief spring [176]. Unfortunately the manufacturing problems in relation to a symmetrical force introduction in the six equally long spring proved to be too difficult.

Hence we must forego a mechanical correction of the spring constant changes due to T_{∞} . The method chosen for use utilizes a cylindrical spring with extreme insulation thicknesses

surrounding the spring itself (without touching it!) and around the entire balance system (see also 3.2.2 and 3.4). In addition, this compensation spring does not act directly on the block but on a support thermally insulated from it. This prevents block shortenings (due to cooling effects of the gas in the reducing station) from affecting the spring length and hence, the force of compensation. The final design is shown in Figure 32 and 47. In addition, the balance's power supply (energy loss heat) was provided with water cooling to maintain temperature gradients (convection) as low as possible. /90

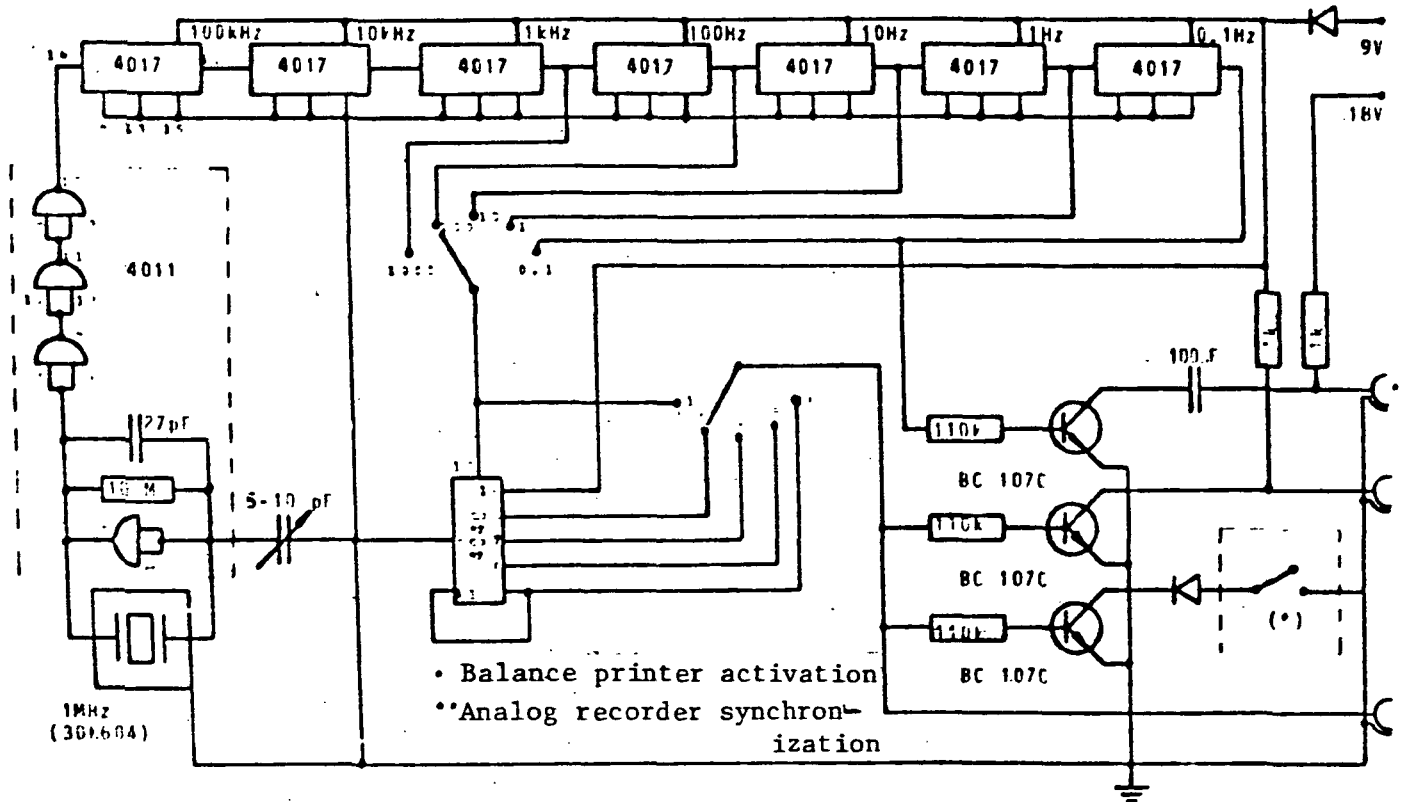


Figure 45 Balance printer control circuit diagram

For a simpler output of the balance's weight indications, these values are issued by a printer (Mettler GA 40). The printer system is activated by means of a quartz-stabilized control

designed by us. The circuit diagram for the printer control is shown in Figure 45, above.

3.2.3.3 Injector triggering

/91

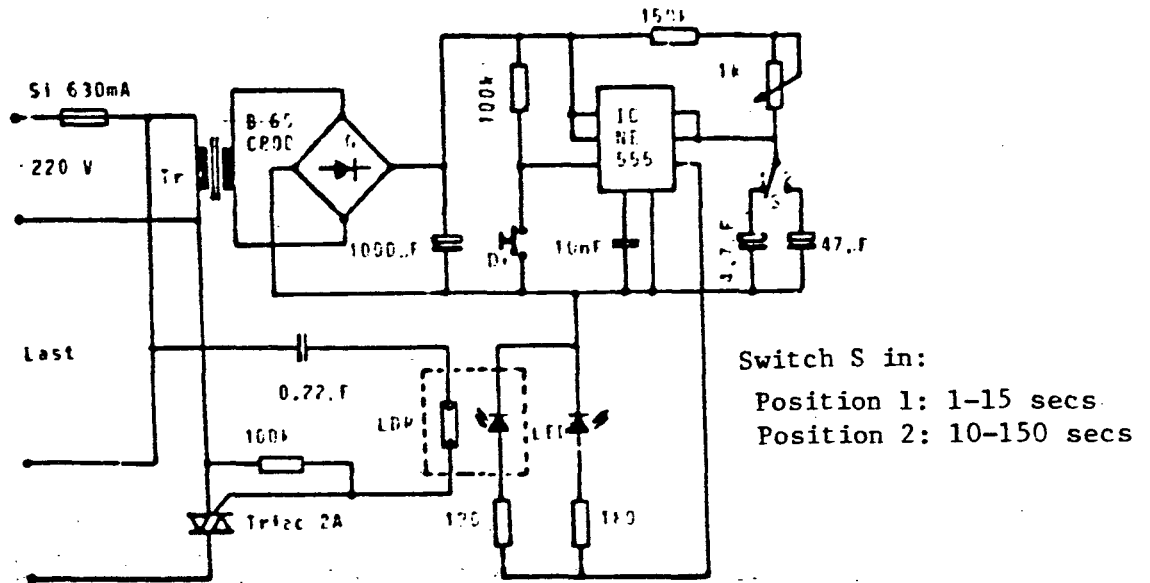


Figure 46 Circuit diagram for the injection time control

The control includes an adjustable time triggering (decadic subdivision, from 10^{-4} to 10 sec and powers from 2^1 to 2^5). This triggering controls not only the printing of the instantaneous balance weight value, but also serves as time synchronization for the remaining measurement value acquisition and processing units (see also section 3.3). In addition, a time switch was developed to allow preselection of the test time and subsequently control the injection valve. In order to avoid feedback between the electromagnetically actuated valve and the electronics, the latter is electrically isolated from the valve's actual control relays by an optic coupler.

When the injector valve is activated, the p_{∞} control of the

vacuum chamber is simultaneously switched off and full pumping power is released (see also section 3.2.2.2). Because of the very precise test duration control it is also possible to control the continuous \dot{m} -measurement here used by means of the integral method mentioned above.

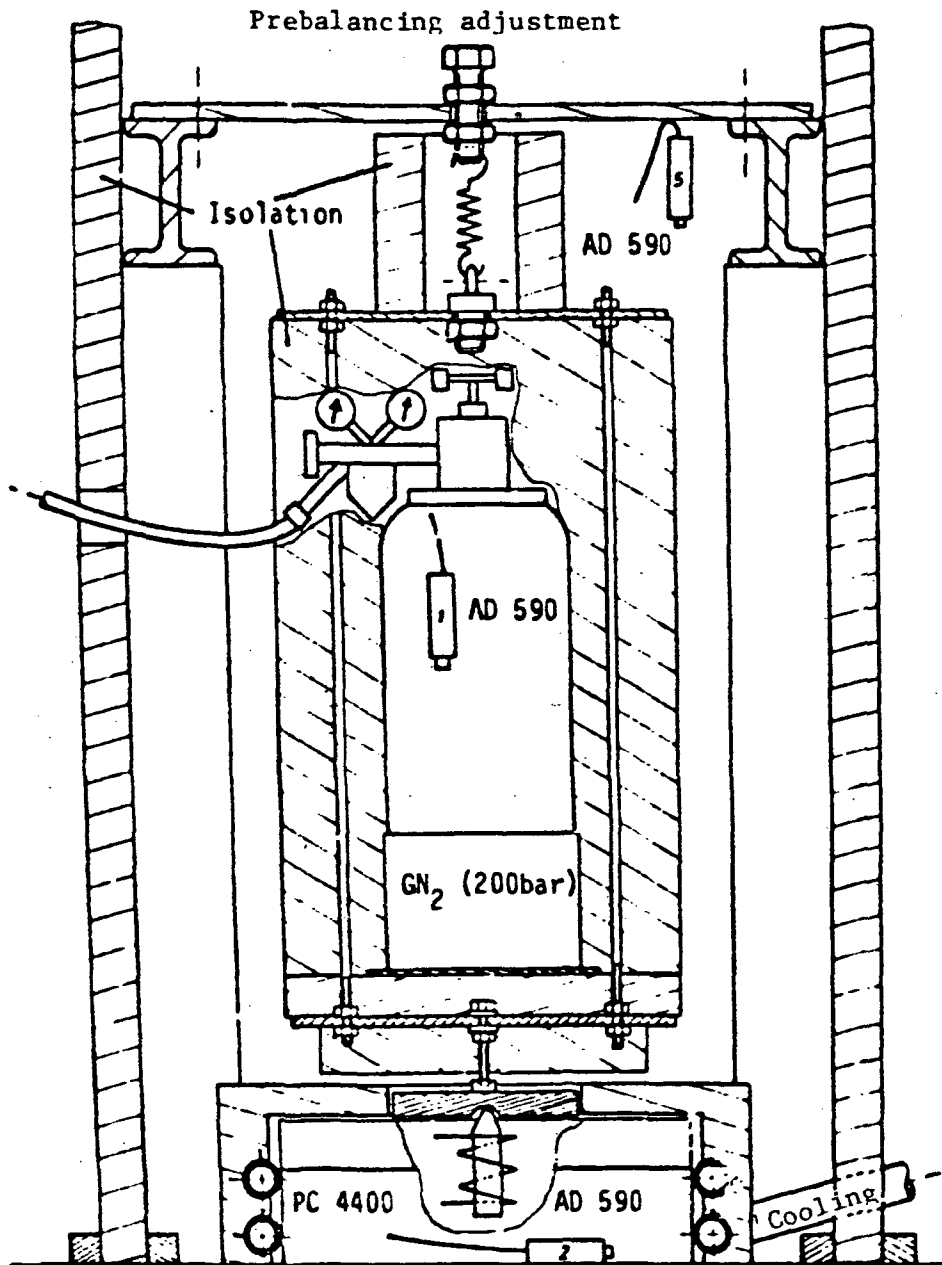


Figure 47 Mechanical assembly for throughput measurements (inside the balance's environmental chamber)

The standardization and calibration of the entire \dot{m} system was made possible using small steel beads (of known mass), which rolled into the receiving container, located in the isolated bottle block frame (see Figure 47, page 94), through a flexible tubing (i.e., the inverse of the procedure for N_2 discharge in the actual precision measurement test), at precisely known time intervals. Standardization tests show that after solving the main T_∞ problems (in relation to the spring constant c) the \dot{m} -measurement construction operates very satisfactorily.

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3.2.4 Combustion chamber pressure determination

/93

In order to determine the combustion chamber pressure, an HMB-11 (Hottinger-Baldwin Co.) pressure sensor designed following an inductive method is flange-mounted perpendicularly to the combustion chamber axis. It is connected to the chamber by a capillary (\emptyset 0.6 mm).

The pressure to be measured acts on a thin membrane, which in turn hermetically seals off a reference volume at a pressure of 1 bar. If this membrane is deformed due to a counterpressure, then it pushes a small piston attached to its center into an induction coil excited by a 100 kHz alternating current. Through a closed control circuit, the coil current is modified long enough (see section 3.2.3) - as a function of piston displacement - to return the membrane to its undeformed original position. After suitable electronic matching, the coil current allows a direct statement to be made regarding p_c . In contrast to many of the customary systems, the advantage of this sensor is the measuring probe's constant dead volume. The precision stabilization of the P11 measurement tube supply voltage, the 100 kHz carrier frequency generator, the membrane control circuit, the measurement value amplification and its matching are all housed in a fully integrated instrument, the HBM-MC-1A.

In order to minimize interfering pick-up and power influences, the MC-1A electronics, housed in a metal cylinder, is attached directly to the P11 pressure measurement tube. The arrangement can be seen in Figure 43. It is thereby also possible to reduce the number of external incoming leads to five cables: two for the coarsely stabilized 12 V supply, one cable for screening or grounding, respectively and two for the measurement value. Since the pressure measuring device is mechanically connected to the combustion chamber and hence also to the thrust frame, these incoming leads must be fashioned of very thin wire (that is permissible, since only very low electric power is needed) and flexibly suspended. Outside of the test chamber, the measurement value must be amplified further, for a better application to the measurement value acquisition system. An overview of the entire combustion chamber pressure detection system is shown in Figure 48, below, as a circuit diagram. We

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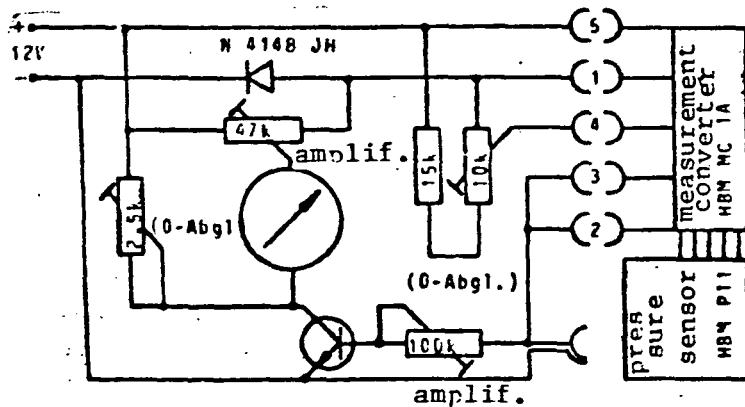


Figure 48 Measurement value amplification and adaptation of the combustion chamber pressure detection system

should remark that the utilization of sensors based on the piezo-electric effect must be avoided, since they are not well suited to stationary pressures (as they occur here, essentially), in comparison to strong, dynamic pressure variations (the problem of long-term drift in charge amplifiers.) Careful calibration

tests have shown suitable agreement with the required specifications: reproducibility better than 0.3% of the measurement range of 1 to 25 bar absolute pressure.

Due to the precise determination of the combustion chamber pressure it is possible to determine a 1-dimensional flow rate coefficient c_D , using a 1-dimensional mass throughput equation: $\dot{m} = p_c A_t / c^*$, with the aid of the direct \dot{m} -measurement method described in section 3.2.3

$$c_{D,1-d} = \frac{\dot{m}_{\text{Mess},W}}{\frac{p_c A_t}{c^*}} \quad (108)$$

Typical results are shown in Section 4.

3.2.4.1 Determination of the p_c -measurement tube installation error /95

Departing from the simplified theory, the gas velocity inside the combustion chamber is not identically 0, but has a finite value. Because of this and determined by the technical boundary conditions due to the connection of a pressure measurement probe to a propulsion unit, the measured pressure deviates minutely from the stagnation pressure [12]

$$\frac{p_{c,\text{Mess}}}{p_c} = 1 - \left(\frac{A_t}{A_M}\right)^2 \frac{\gamma}{2} \left(\frac{2}{\gamma+1}\right)^{\frac{\gamma+1}{\gamma-1}} \cdot f^2 \quad (109)$$

where A_t = throat cross-section,

A_M = installation cross-section

$f = \frac{1}{2} (1 + \cos \beta)$

β = angle between sensor axis and propulsion unit axis

(here $\beta = 0$)

With the boundary conditions applicable here, the pressure correction is merely

$$P_c = P_{c, \text{Mess}} \cdot 1,00000596$$

and can therefore be neglected.

In the course of the test execution it was confirmed that the initial assumption regarding the gas behaving adiabatically within the pipeline system and the combustion chamber, was correct. Because of the high heat capacity of the pipelines, made essentially of copper, the cooling phenomena in the working medium caused by throttle effects are compensated (provided care is taken not to extend the test duration to several minutes).

3.2.5 Temperature measurements

/96

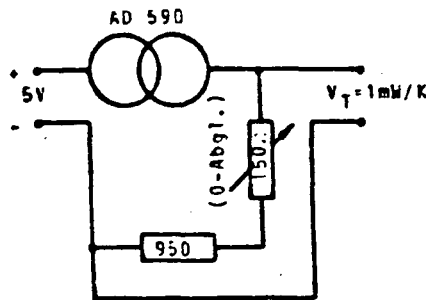


Figure 49 Power supply and measurement value adaptation of the AD 590 temperature sensors

In order to measure the N_2 gas temperature in the N_2 supply lines as well as in the combustion chamber of the cold gas propulsion unit, and at several location of the test installation to control environmental conditions, temperature sensors Model AD 590, of the Analog Devices company, are used. The decisive advantage of these models, in comparison to the customary thermoelements consists in that both measurement amplifiers and supply voltage stabilizers - as well as a 0°C reference temperature point - are integrated into the smallest volume ($2 \times 4 \times 0.5 \text{ mm}$). The calibration and spreading followed the very simple circuit shown above.

The sensor proves to have a high resolution (better than 0.01 °C) and an extraordinary long-term stability. The linearity error is less than 0.1% and dislocations due to contact problems, as they occur with thermoelements, have not been observed. Due to the low mass of the temperature-sensitive portion of the "sensor head", the response time (to 99% of the temperature value) is < 1 sec and hence certainly adequate to the application here contemplated.

3.3 Data acquisition and data processing

/97

All parameters essential to either measurement or test operation are recorded by high resolution analog recorders, for more rapid optical control (trouble shooting). Measurement variables that do not change during routine operation (such as $T_{\infty,lab}$, $P_{\infty,lab}$, p_{pump}) are rendered visible on meters. The variables necessary for performance determinations of the cold gas propulsion unit are in addition fed to the 10 channel ADC [analog to digital converter] developed at the Chair for Space Technology: it has an associated memory (capacity: 256 words 12 bits long = 4 decimal places). The circuit is shown in Figure 51 (page 101) (see also Roth, A. [127] and Neuwald, W. [111]). Following each measurement, the 10 data channels are printed out (including mean values) by means of a line printer. Through the use of modern microprocessors, the discretization errors of the ADC are at a level below 0.1%, which can be disregarded.

The block diagram below (page 100) provides an overview of data determination and output

KEY to Figure 50 (page 100) 1 combustion chamber pressure 2 Measurement tube 3 Carrier frequency amplifier 4 Amplifier 5 Tracing 6 Relay 7 laser beam control 8 Motor drive 9 internal stabilization 10 Intensity control 11 regulated laser 12 Thrust measurement 13 Measurement signal processing 14 Active band filter 15 Low pass, active/passive 16 Thrust 17 Vacuum chamber pressure measurement and control 18 PID regulator 19 Vacuum chamber pressure 20 Magnetic valve 21 Needle valve 22 Vacuum pump suction line

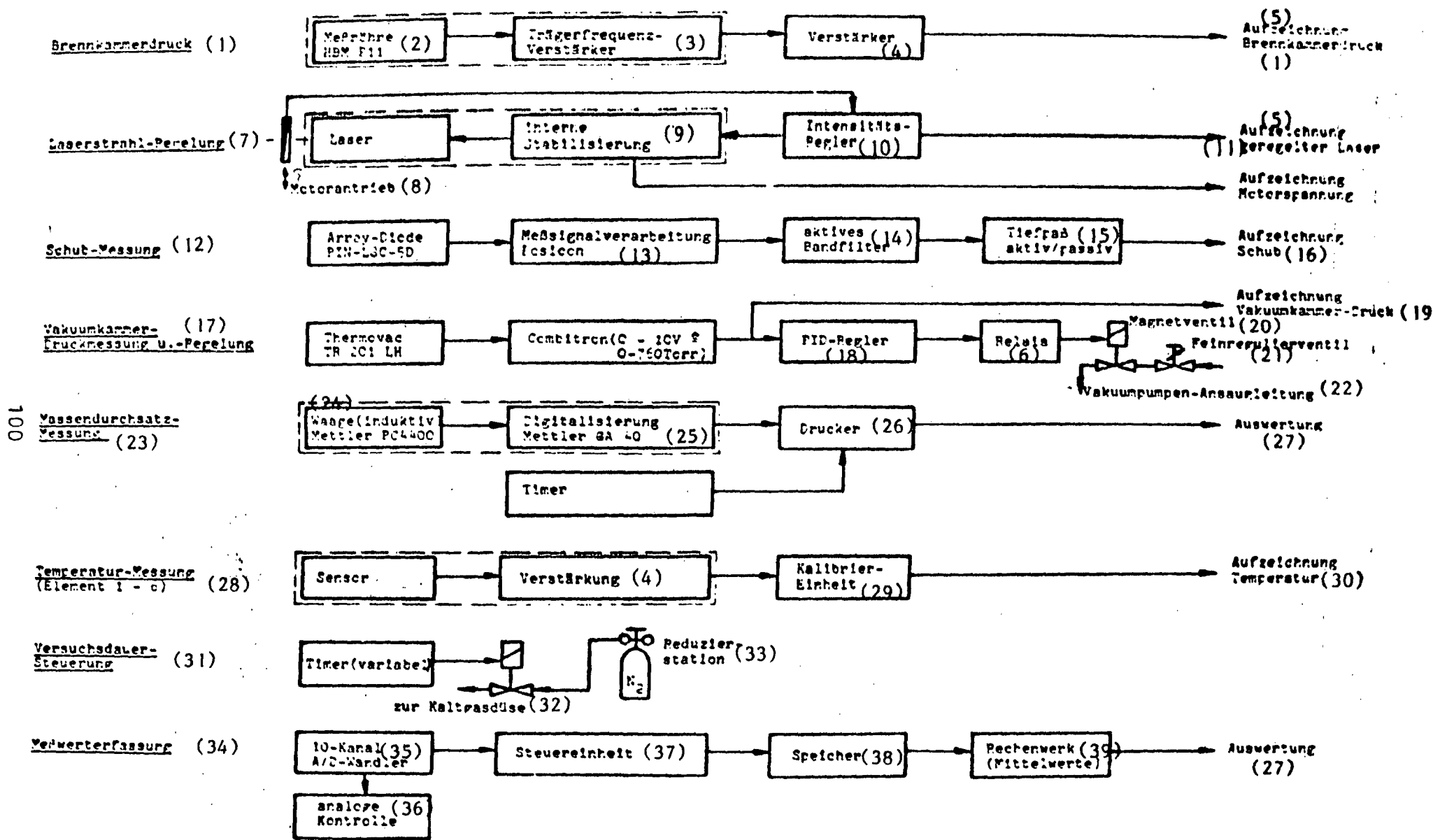


Figure 50 Block diagram of the data acquisition and processing method

(Key to Figure 50, continued)

23 Mass throughput measurement 24 Balance (inductive) 25 Digitalization
26 Printer 27 Evaluation 28 Temperature measurement 29 Calibration unit
30 Temperature 31 Test duration control 32 to cold gas nozzle 33 Reducing
station 34 Measurement value acquisition 35 10-channel ADC 36 Analog
control 37 Control unit 38 Memory 39 Computer (mean values)

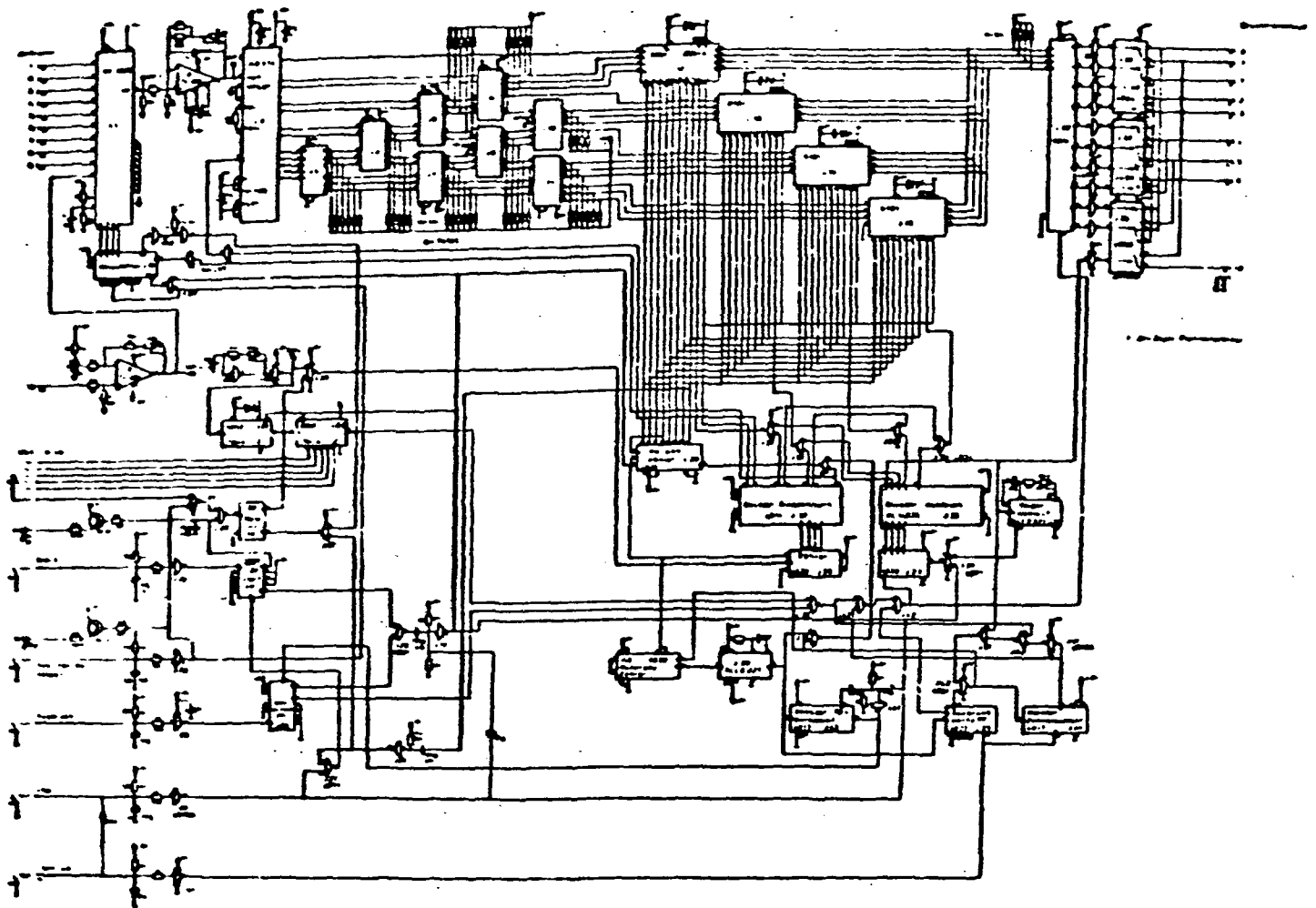


Figure 51 Block circuit diagram of the ADC and memory [27]

A problem always to be solved anew in vacuum technology is that of electrical lead-ins through a vacuum chamber's walls. For the task here posed, 10 measurement channels and 15 supply lines (two of which carry 220 V AC) must be introduced into the chamber and remain insulated from each other. Taking the cost problem into account, we opted for a newly developed 25-pole arrangement (manufacturing price: approximately DM 10.00). The savings per channel (in comparison to the customary 1-channel lead-ins such as those of the Leybold Heraeus company) is approximately DM 1,400.00

3.4 Additional devices to reduce negative local influences /100

The strong short-term variations in the laboratory line voltage (caused by the non-stationary power consumption of large external test facilities) force the utilization of the autonomous source of alternating power already described in section 3.2.2.1 (see Figure 52). In order to reduce the temperature effects, especially on the thrust and mass throughput measurements, the test arrangement is thermally isolated from the environment. To this end, a complete "house" made from 10 cm thick styrofoam blocks, was built around the vacuum chamber and the laser device. In addition, temperature variations within the laboratory were reduced by insulating the face of the windows and switching off the air conditioning unit, which operated much too irregularly.

During "test-free" periods the "house", including all working openings, is kept open, thus reducing to a minimum the temperature difference between the "house content" and the laboratory. Prior to the start of the test, the nozzle to be studied is built into the vacuum chamber and subsequently the thrust measurement chamber and the "house" are closed. The strongly insulating effect of the styrofoam insures that the effect of any small temperature differences between the vacuum chamber and the laboratory, during the test phase, can be ignored. In addition,

this covering performs the functions of a wind screen, something absolutely essential because of the resolution required of the thrust measuring device.

/101

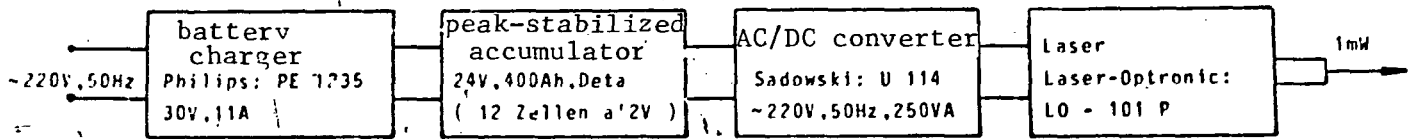


Figure 52 Independent 220 V AC power supply

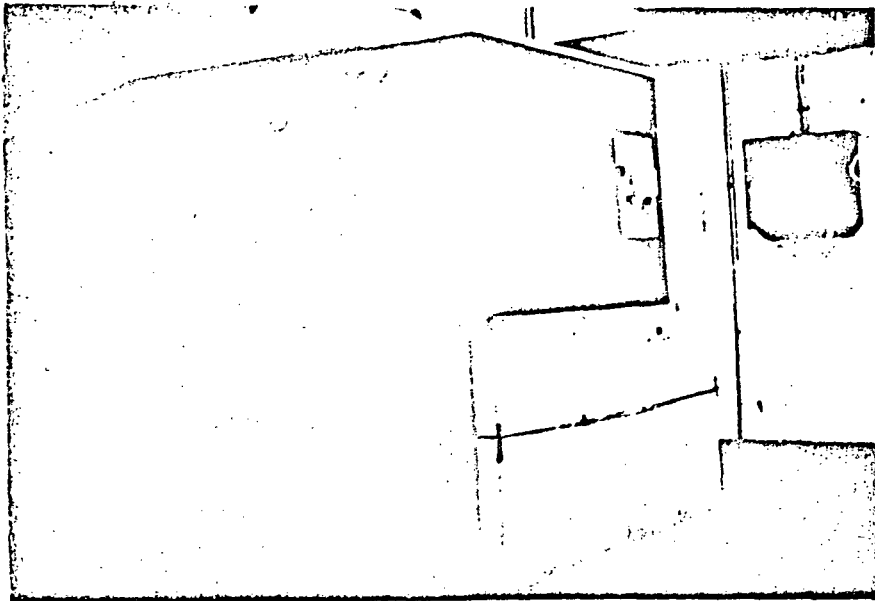


Figure 53 Environmental chamber

Influences due to stationary mechanical floor vibrations - such as those caused by a rotary sliding vane vacuum pump, for instance - can be canceled by using appropriately chosen mechanical dampers. Spontaneous strong disturbances such as those from traffic on the street, however, make it advantageous to perform any precision measurements during the night hours.

The measurements of the effect of ϵ on the development of the boundary layer losses require the divergent nozzle length to be changed, without affecting the remaining dimensions, especially in the throat area. The initially examined way of building the nozzle in slices, using thin foils of linearly increasing bore diameter, was impractical in its realization, since a multiplicity of very thin foils would have to be used, to avoid edge effects. In addition, accurate centering was not sufficiently possible. The alternative of boring the nozzle using precision drills or form cutters was closely examined and then discarded, following discussion with the appropriate companies. Neither the small bore dimensions nor the defined transition geometry in the nozzle throat area (backtaper) can be achieved in this manner. Arc erosive methods were also ruled out. While the craters produced thereby could subsequently be smoothed by grinding and polishing, satisfactory backtapering can not be obtained in this case, either.

The galvanoplastic manufacturing method finally chosen uses a common core, fashioned in one piece, for both the convergent and the divergent portions of the nozzle. This core is machined "flying" on a small, precision turning machine (by a method for which a patent is currently being sought). Figure 54 shows the main characteristics of this manufacturing step.

The forming blades here used were sharpened by scanning a strongly enlarged former plate, which in turn was fashioned using a profile projector. (The manufacture was kindly undertaken by the Wendel Co. of Eichenau, near Munich.)

Only the flying processing insures that the core does not break /104 at the narrowest cross-section (A_t) - the narrowest value attained was 0.23 mm - since backrest clamping and secondary drive methods were eliminated due to excessively large misalignment).

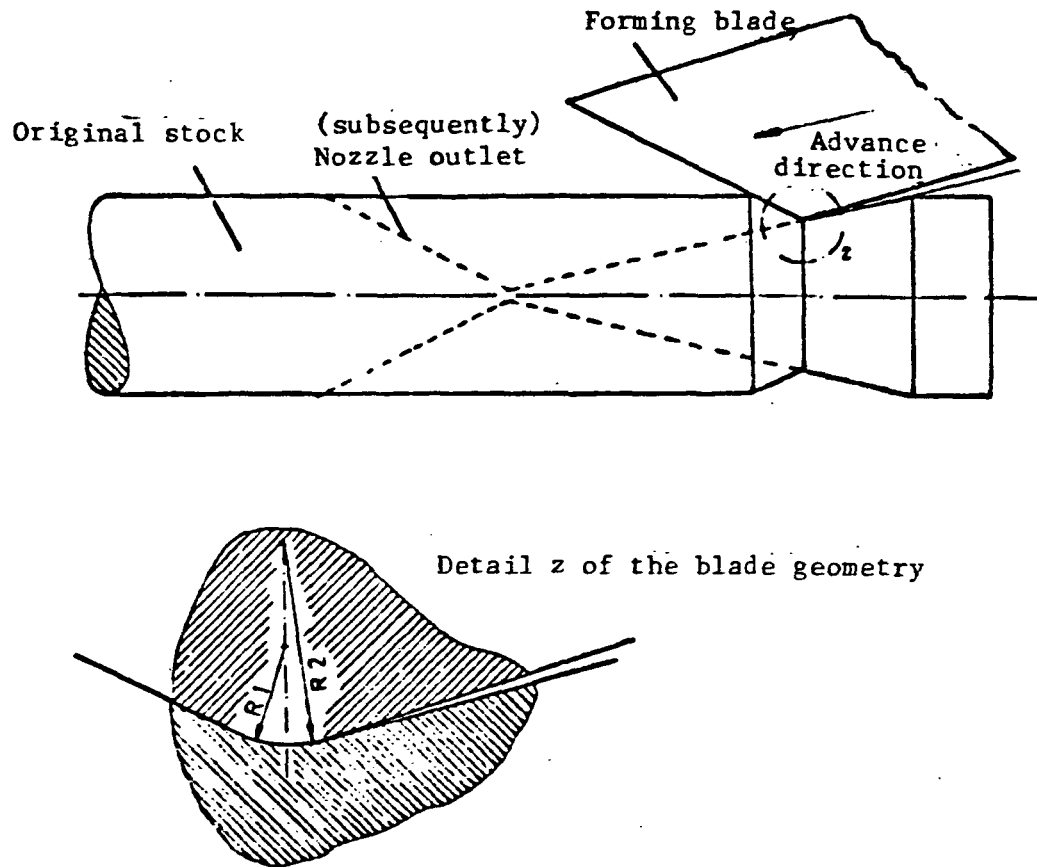


Figure 54 Schematic of the nozzle core's manufacture

Following manufacture of the core, a 3 mm wall thickness is electrodeposited from a copper electrolyte bath. After removal from the plating bath, the external contour of the propulsion unit is fashioned in copper and subsequently the core is removed by gently twisting and carefully pulling apart at both ends. In order to make possible the simple mounting and demounting of the propulsion unit, each copper nozzle is fitted into an installation flange and welded to it (for tightness). The individual steps in the nozzle manufacture are illustrated in Figure 55, page 106. Once a measurement series is completed, for a certain

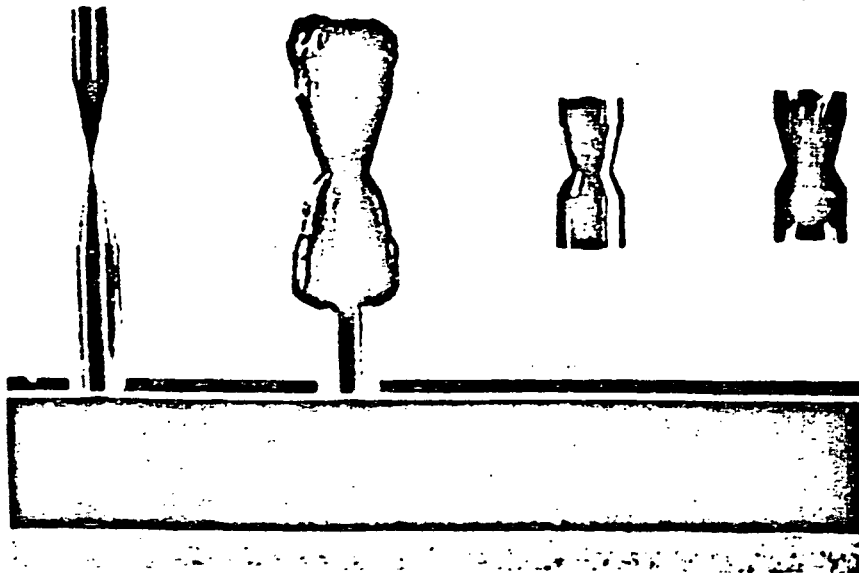


Figure 55 Nozzle manufacturing steps (model embedded in casting resin)

surface ratio ϵ , the propulsion unit is converted - with the aid of a specially made holding device - to the next length or ϵ step, by machining.

Table 4 (page 107) lists the main dimensions of the 12 propulsion units examined.

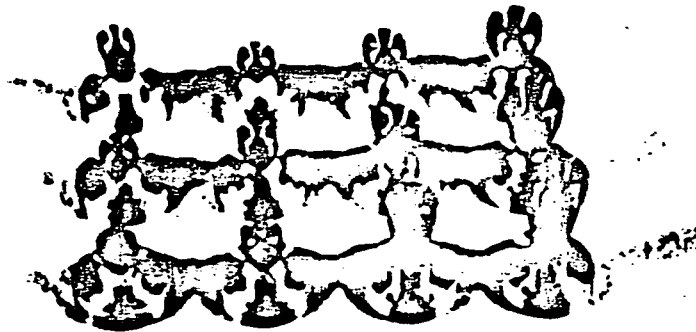


Figure 56 Original view of the 12 propulsion units examined (prior to first machining)

TABLE 4 MAIN GEOMETRIC DIMENSIONS OF THE 12 NOZZLES EXAMINED (NOZZLE NO. 1 WAS DAMAGED JUST PRIOR TO COMPLETING ITS MANUFACTURE)

Nozzle Nr.:	R _T (mm)	Bk _L (mm)	Bk _R (mm)	α _e (°)	D ₂₀₀ (mm)	l ₂₀₀ (mm)	ε ₂₀₀ (-)	D ₁₀₀ (mm)	l ₁₀₀ (mm)	ε ₁₀₀ (-)	D ₅₀ (mm)	l ₅₀ (mm)	ε ₅₀ (-)	D ₂₅ (mm)	l ₂₅ (mm)	ε ₂₅ (-)	D ₁₀ (mm)	l ₁₀ (mm)	ε ₁₀ (-)
2	0,142	5,0	2,0	15,0	3,89	15,19	187,89	2,84	13,22	99,65	1,93	11,47	46,31	1,41	10,48	24,59	0,85	9,48	8,96
3	0,138	5,0	2,0	20,0	3,87	13,67	196,96	2,80	12,14	102,73	1,96	10,96	50,34	1,37	10,15	24,81	0,97	9,44	12,54
4	0,153	3,663	2,0	10,0	4,28	20,78	195,66	3,09	17,31	101,64	2,17	14,68	50,54	1,51	12,84	24,53	0,93	11,20	9,30
5	0,176	5,0	2,0	15,0	4,92	17,08	194,06	3,55	14,48	100,71	2,54	12,54	51,88	1,78	11,09	25,49	1,11	9,84	9,95
6	0,166	5,0	2,0	15,0	4,68	16,59	198,07	3,33	14,05	100,00	2,39	12,22	51,68	1,66	10,84	25,03	1,03	9,71	9,68
7	0,165	5,0	2,0	20,0	4,59	14,62	192,39	3,31	12,85	99,85	2,40	11,51	52,89	1,68	10,49	25,72	1,00	9,61	9,18
8	0,206	3,443	2,0	10,0	5,79	25,41	196,58	4,13	20,70	99,88	2,93	17,26	50,58	2,07	14,78	25,21	1,29	12,62	9,82
9	0,215	5,0	2,0	15,0	5,87	18,70	186,36	4,31	15,77	100,47	3,07	13,38	51,11	2,16	11,61	25,30	1,34	10,12	9,73
10	0,223	5,0	2,0	20,0	6,18	16,45	191,75	4,47	14,11	100,00	3,21	12,30	51,73	2,25	10,96	25,36	1,38	9,79	9,56
11	0,306	3,092	2,0	10,0	8,42	30,94	188,51	6,09	24,43	98,54	4,41	19,45	51,72	3,08	15,64	25,22	1,72	11,85	7,93
12	0,322	5,0	2,0	15,0	9,12	24,40	200,15	6,51	14,92	101,87	4,59	15,77	50,66	3,22	13,23	24,95	2,02	11,03	9,86
13	0,324	5,0	2,0	20,0	9,03	20,24	194,28	6,53	16,72	101,47	4,59	14,03	50,29	3,25	12,17	25,13	2,00	10,51	9,57

Microscopic examinations of the nozzle throat area before and /106
after the test series showed that there was no substantial wear
and hence, change in geometrical dimensions. The evaluation was
based on images from the MPI* Heidelberg electron microscope,
provided by graduate engineer Peter Lell. Figure 57 shows the
throat area, while Figure 58 represents a strongly magnified
portion of the nozzle's external contour.

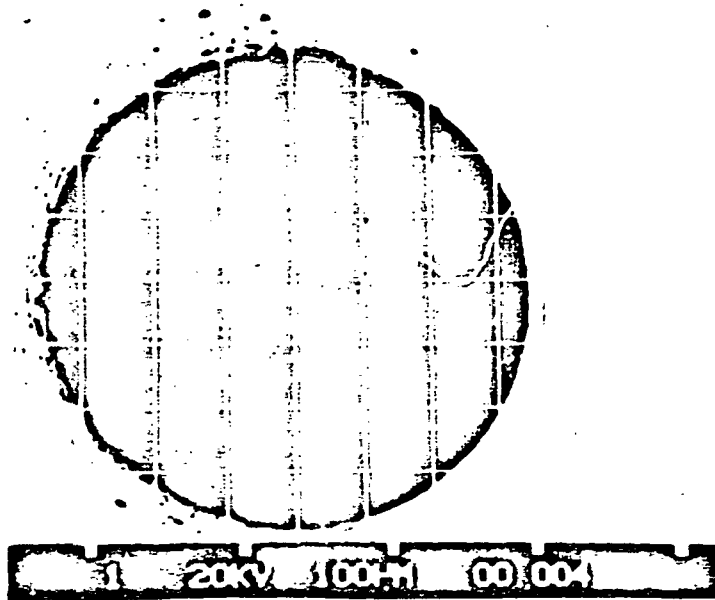


Figure 57 Scanning electron
microscope image of the throat
area (Magnification, X 200)

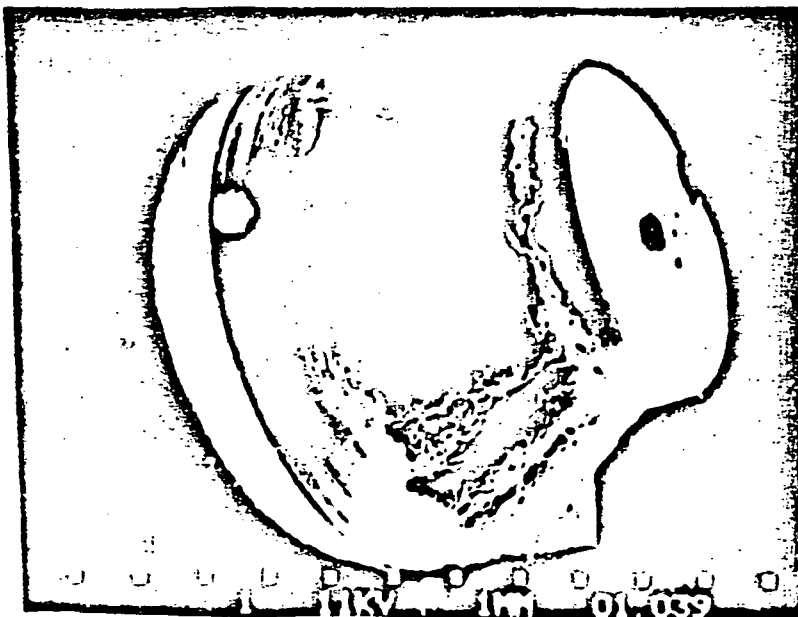


Figure 58 Partial
view of the external
contour

* No expansion provided in the foreign original

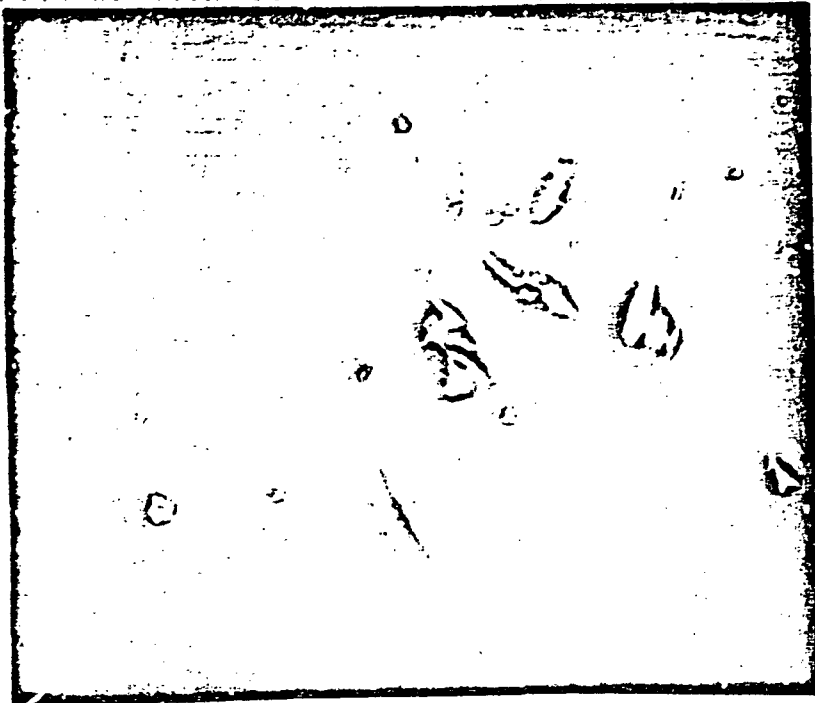


Figure 59 View of a complete propulsion unit

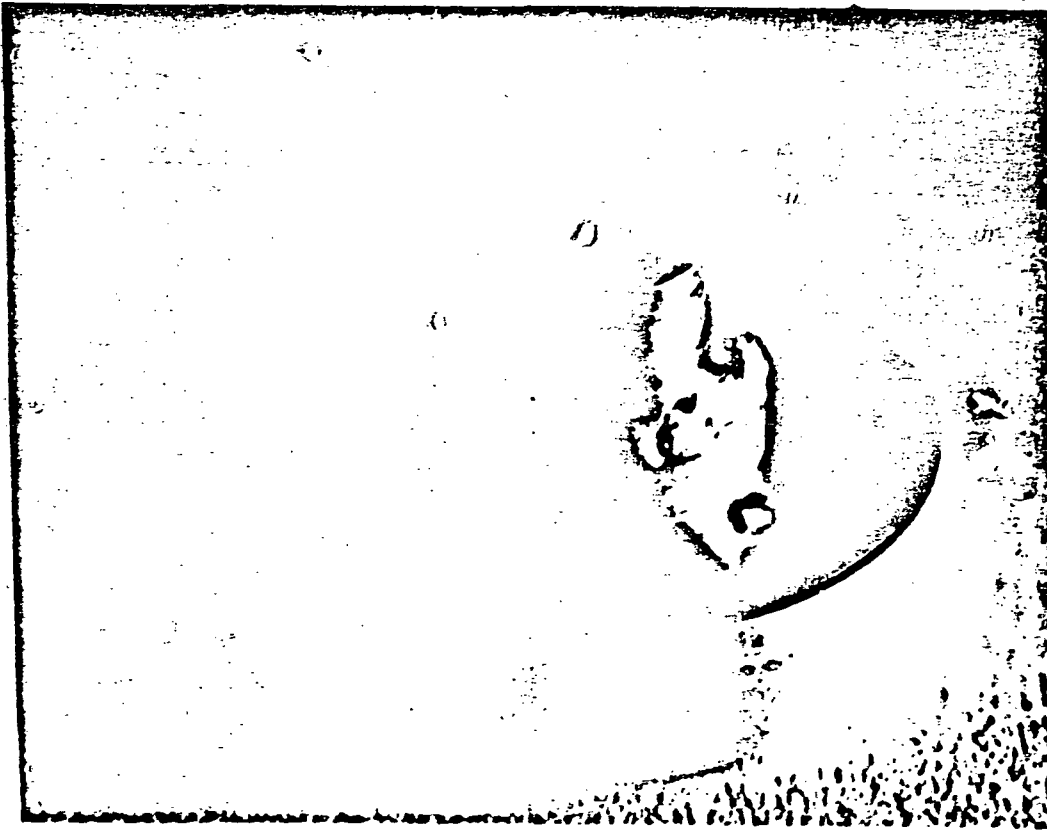


Figure 60 View of the complete propulsion unit

4.1 Review of the test extension

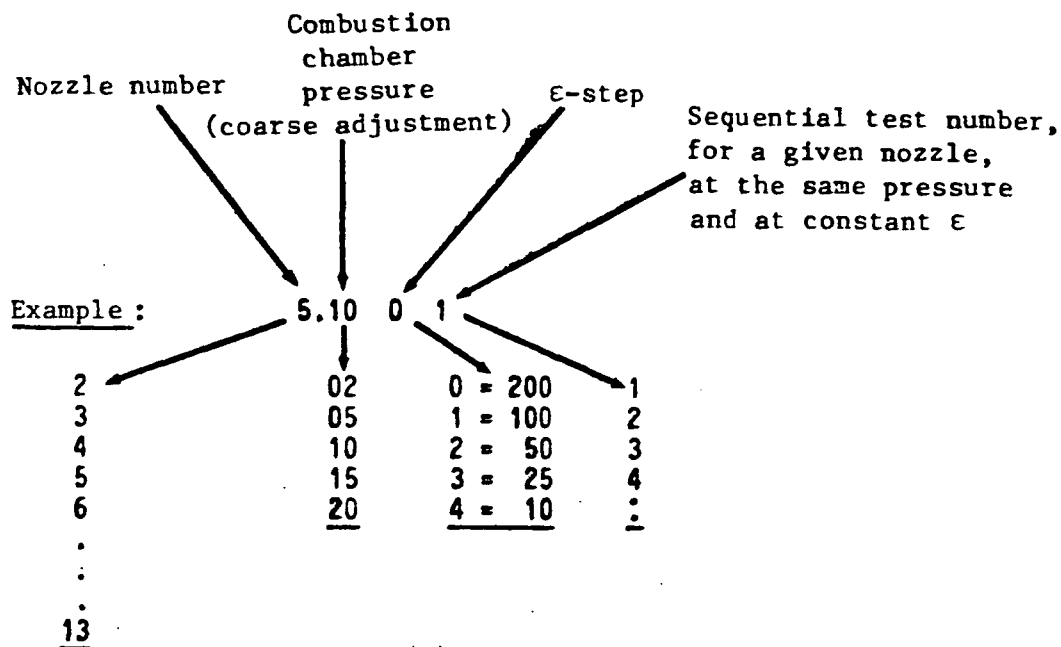
The twelve cold gas propulsion units were measured in five test series. After each of these series the nozzle's end cross-section was reduced by mechanical means (ϵ -steps: 200, 100, 50, 25, 10) and measured by microscopy. Within a given test series, five combustion chamber pressures were applied four times each,* for a total of 1200 individual tests. Few of the interferences with the measurement arrangement during a given test - caused mostly by eccentric loading of the m -balance of the N_2 -bottle frame - could be eliminated to complete the test. The installation of a sufficient number and size of readily accessible work openings proved to be extraordinarily positive (see section 3.4). Due credit must be given the T_{∞} stabilization, in this sense. Any subsequent experimental efforts should include the following improvements, to increase precision and facilitate test execution:

- fully airconditioned test space
- separate data acquisition room
- supply systems (mains operated power supply) outside of the test chamber
- more stable building construction
- low-traffic external environment

See also section 3.4, in this regard.

For a more ready control and handling of the large quantity of measurement values, in the subsequent calculations, we used the following nomenclature:

* 20, 15, 10, 5, and 2 bar



4.2 Evaluation of measurement results by means of typical examples

/110

The output from the measurement acquisition system arranges all experimental data according to the test number described above and makes them available to an evaluation program. Figure 78 (see section 9.2) shows an input listing for such a test run. Here all measurement variables are examined for their order of magnitude and units, and corrected (for instance, the thrust measurement value is corrected for the Bourdon effect; the p_c value for $p_{\infty, vac\ chmbr}$). Next, especially tailored to the corresponding test number, the theoretical performance prediction EGVP is started, such that in the end a data package arranged in parallel has been generated, with the theoretical and experimental performance parameters. In order to render the quantity of data thus created more tractable - by means of an interactive (i.e., terminal controlled) graphics program -

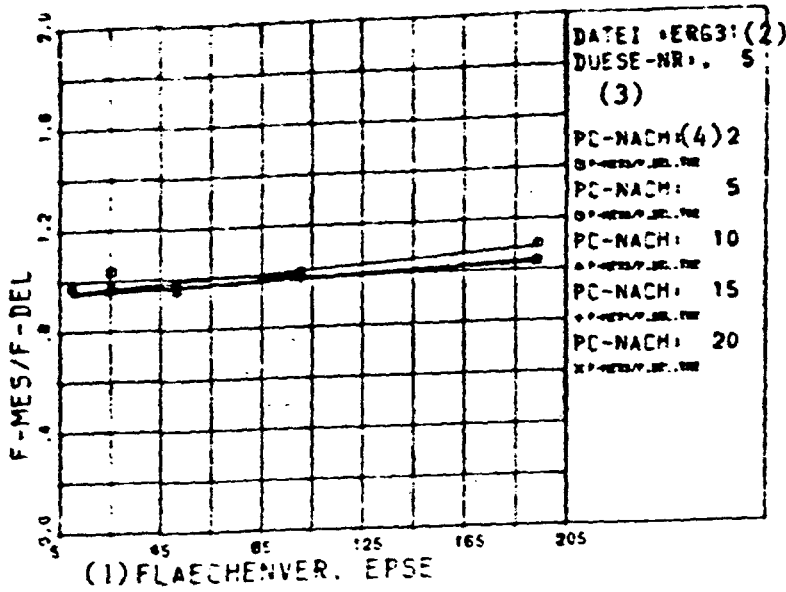


Figure 61 Ratio of measured to predicted thrust, plotted as a function of ϵ , with p_c as parameter

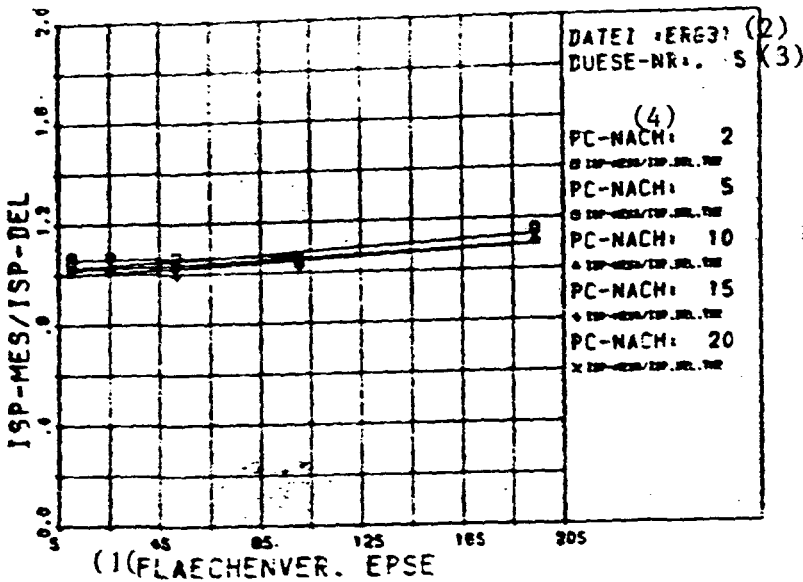


Figure 63 Ratio of measured to predicted impulse, plotted as a function of ϵ , with p_c as parameter

KEY 1 Surface ratio ϵ 2 Data package: result 31 3 Nozzle No. 4 from

the data are plotted. Not only can the scale of resolution be arbitrarily changed, but it is also possible to perform changes in the equalization curve, with respect to individual measurement points. Each of the 40 values per test run can be chosen to be x , y or a parameter point. Due to the interactive input

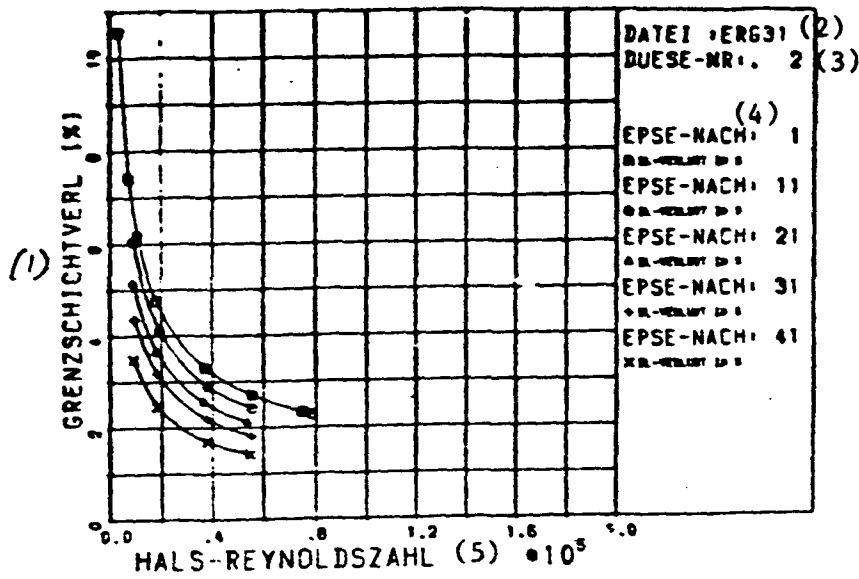


Figure 62 Boundary layer loss as a function of the throat-Reynolds number, with ϵ as parameter

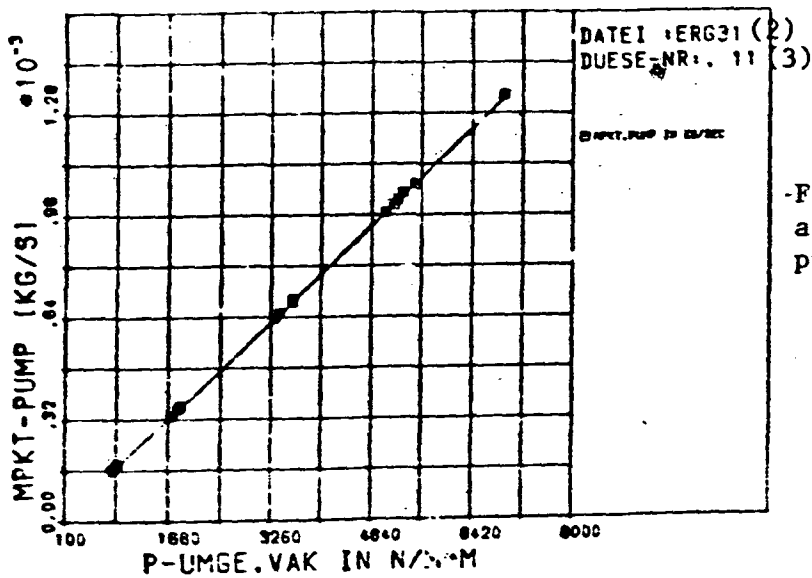


Figure 64 Pump throughput as a function of the environmental pressure in the vacuum chamber

KEY 1 Boundary layer loss 2 Data package: result 31 3 Nozzle No. 4 from 5 Throat Reynolds number

from the graphics terminal, previous verification of the results can help in decisively reducing paper waste due erroneous output.

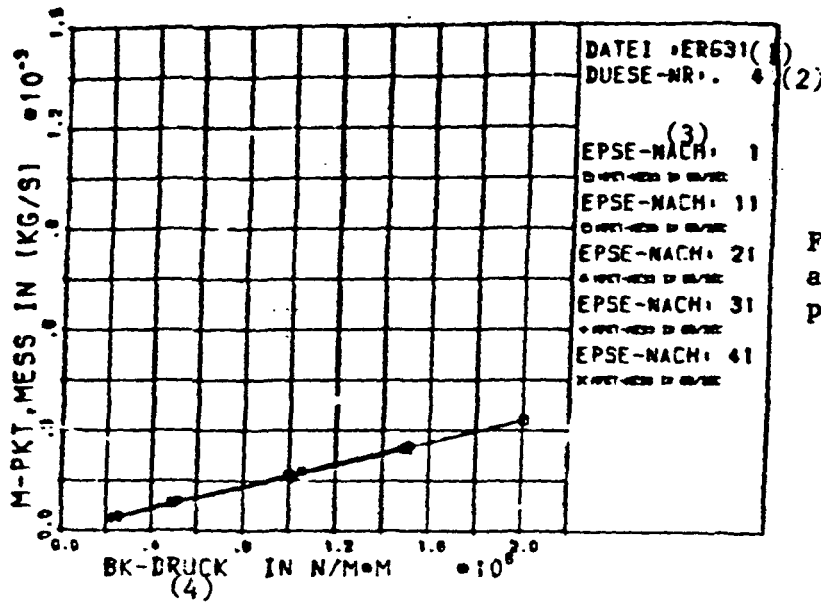


Figure 65 Mass throughput as a function of p_c with ϵ as parameter

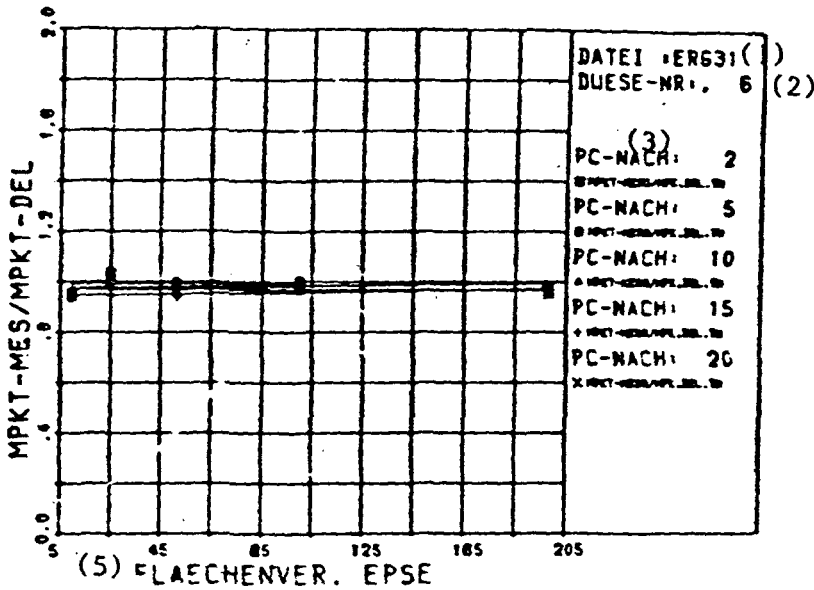


Figure 66 Measured over predicted mass throughput, with p_c as parameter

KEY 1 Data package: Result 31 2 Nozzle No. 3 from 4 Pressure 5 ϵ

Figures 61 to 73 show typical trends in the measurements after evaluation.

In contrast to the corresponding diagrams of the \dot{m} -ratio

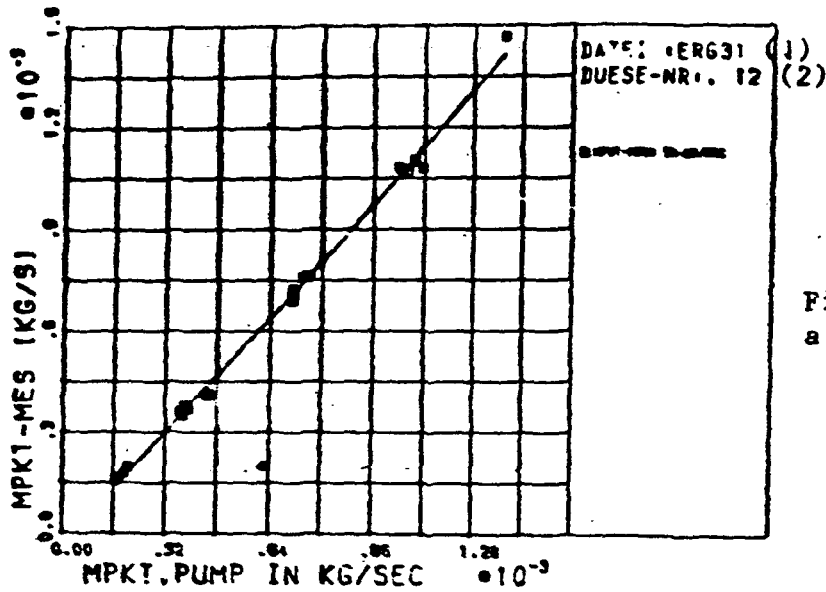


Figure 67 Mass throughput as a function of pump throughput

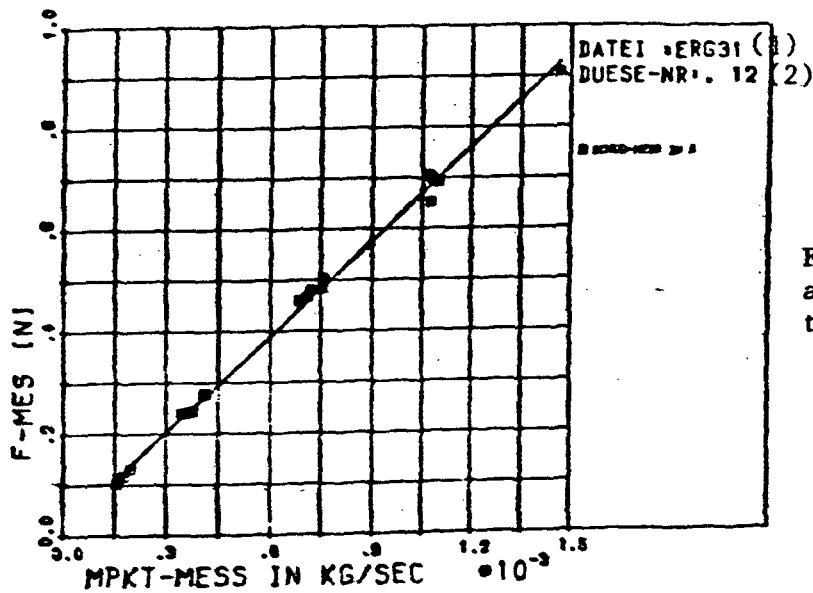


Figure 68 Measured thrust as a function of measured mass throughput

KEY 1 Data package: Result 31 2 Nozzle number

$(\dot{m}_{\text{mess}}/\dot{m}_{\text{del,the}})$, which shows good agreement between the measured and the predicted values of c_D over the entire range of ϵ , we can see from Figures 61 and 63 (page 112) - which describe the

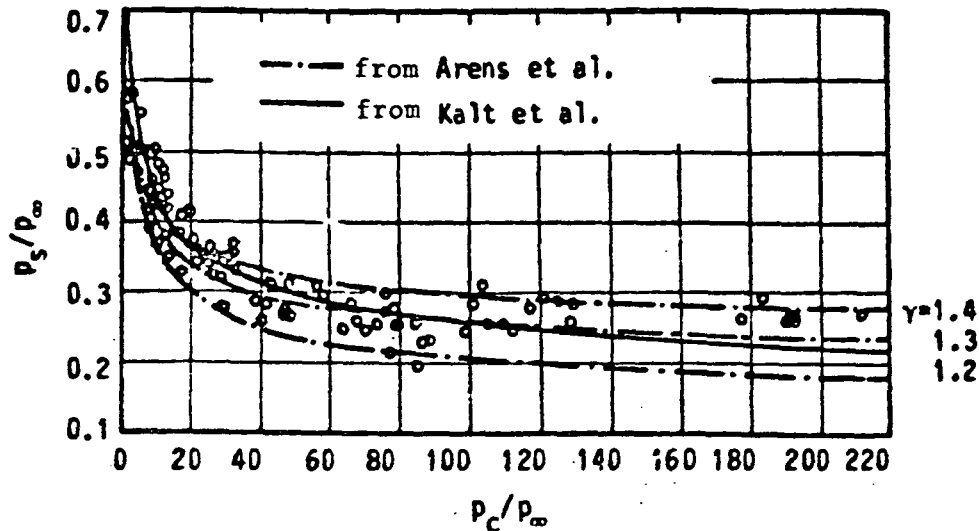


Figure 69 Flow separation ratio as a function of nozzle/environmental pressure

thrust and impulse behavior, respectively - that there is a certain displacement in direction > 1.0 for the higher ranges of ϵ . The explanation for this is as follows: the theory of performance prediction calculated here, at first, started from the premise (for lack of other information), that also for the /113 case of smaller nozzles the so-called "Summerfeld criterion" would be valid, with respect to flow separation during over-expansion. For the case $p_e < 0.4 p_\infty$, flow separation results and \rightarrow impulse losses. Since in all 12 of the micronozzles examined the measured thrust at $\epsilon > 100$ was greater than for Summerfeld 0.4 (including all losses), we may infer that for the small propulsion units under discussion here, this factor is smaller than 0.4. This means later separation of the flow from the wall and hence, a more widely usable ϵ -range. Due to the very flexible evaluation program mentioned earlier, it is possible to change the Summerfeld factor until good agreement can be obtained. The results of that particular investigation show a value of up to 0.15.

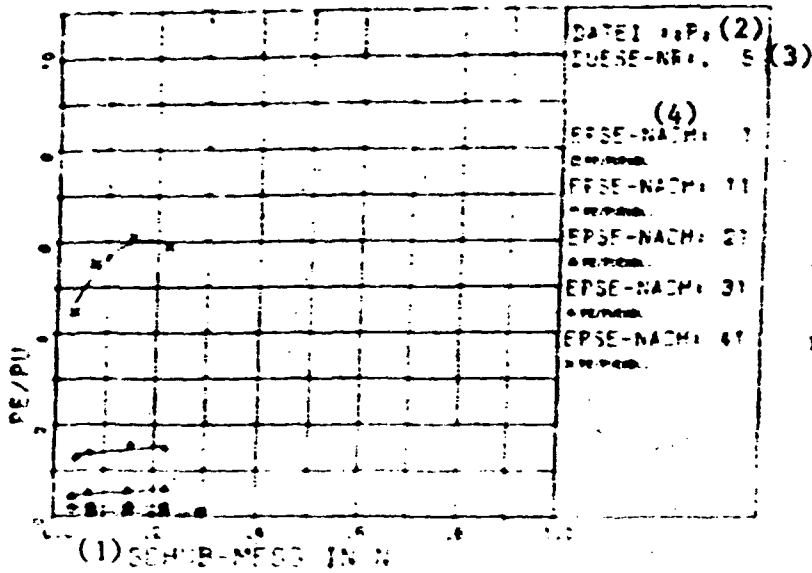


Figure 70 Ratio of end pressure to vacuum chamber environment pressure as a function of thrust, with ϵ as parameter

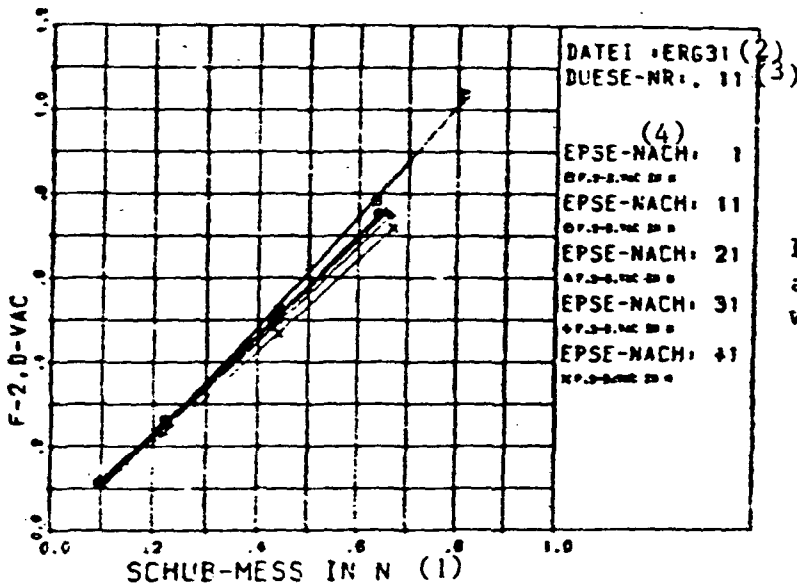


Figure 71 Measured thrust as a function of predicted thrust with ϵ as parameter

KEY 1 Thrust measurement 2 Data package: Result 31 3 Nozzle No. 4 from

The physical explanation of this discrepancy might be sought in that due to the greater influence of boundary layer formation in the case of extremely small propulsion unit dimensions (in contrast to full-scale propulsion units), the residual pressure

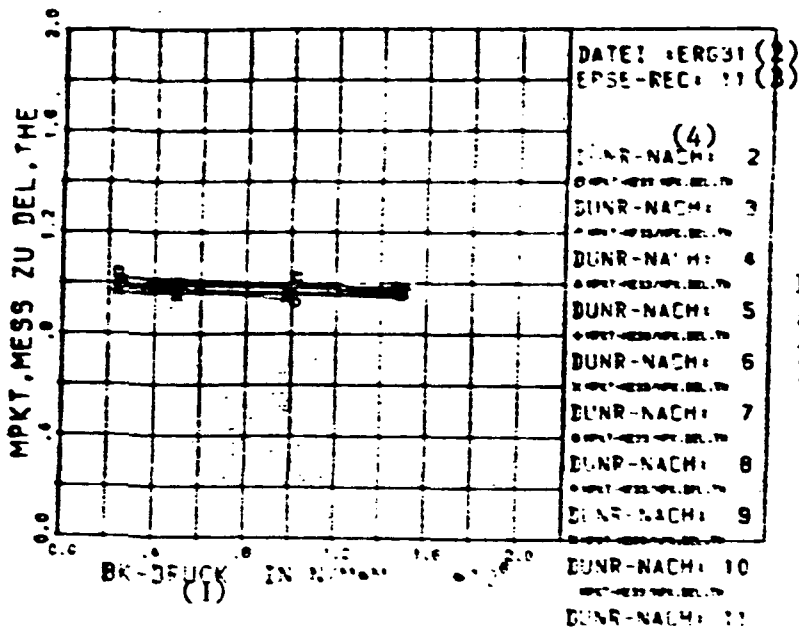


Figure 72 Throughput ratio as a function of combustion chamber pressure, with nozzle number as the parameter

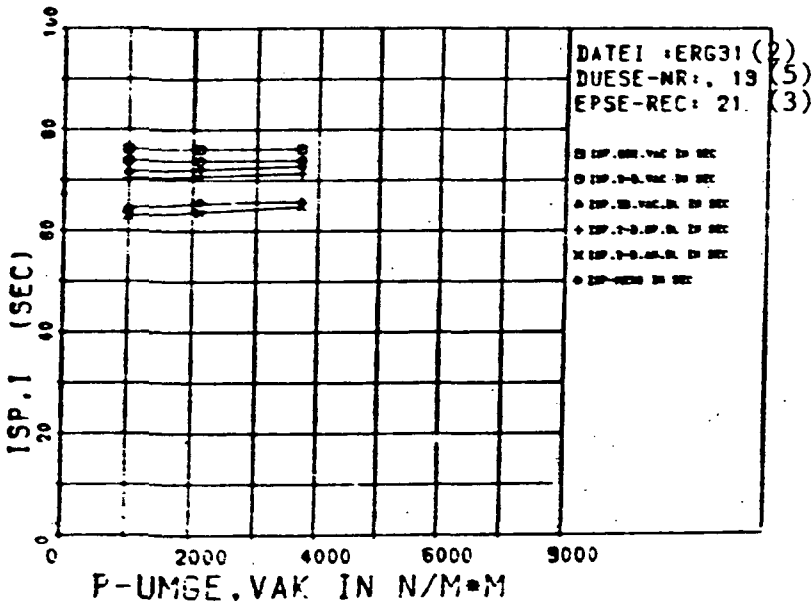


Figure 73 Specific impulse as a function of $p_{\infty, vac}$ chbr for the third estep

KEY 1 Pressure 2 Data package: Result 31 3 e 4 from 5 Nozzle No.

near the wall is higher than in purely potential flow. However, since separation occurs only when the wall pressure falls considerably below the environmental pressure (precisely for large

nozzles: factor 0.4) outside of the nozzle, here this point is displaced backwards, in the direction of a larger surface ratio (see also [19,25,49,90,95,108,118,122-124,139-143,145,154,157]).

We find indications of a tendency to deviate from a factor of 0.4 already in Kalt [80]. Figure 69 (page 116) shows a decrease in the separation factor to below 0.2 for increasing pressure ratio p_c/p_∞ and decreasing isentropy exponent γ . The expression

$$\frac{p_{sep}}{p_\infty} = \frac{2}{3} \left(\frac{p_c}{p_\infty} \right)^{-0.2} \quad (110) \quad \text{(corresponds to the solid line, in Figure 69)}$$

is a good approximation to the separation pressure ratios found. /114

(/116)

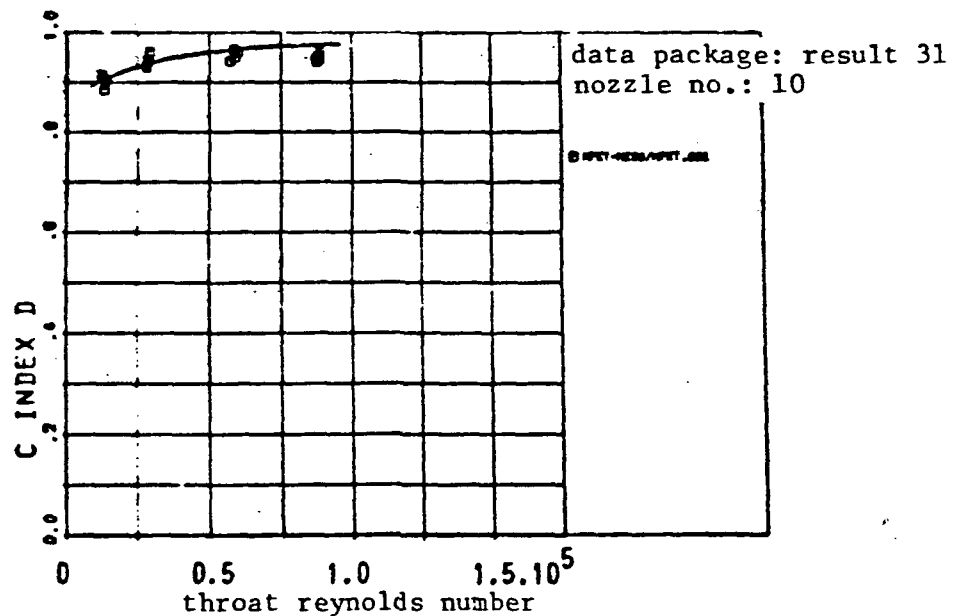


Figure 74 Throat throughput coefficient c_D as a function of the throat Reynolds number

The mass throughputs of the propulsion units and of the vacuum pumps, shown in these Figures, indicate a very precise agreement with the theory and provide a good control on the required pump constancy for different $p_{\infty, vac}$ chbr values. This is the only

way to verify a statement regarding stationary test conditions, as required here (and as we already assumed, at the start).

The courses of the boundary layer losses as a function of throat Reynolds number, shown in Figure 62 (page 112), are in good agreement with the theory described in section 2.5. They also make it clear that in the case of micronozzles the $\Delta\eta_{bl}$ losses have a substantially larger effect (by a factor of up to 10) than, for instance, in booster propulsion units.

Since in the determination of the theoretical/experimental characteristic magnitudes of a propulsion unit, necessary to a performance comparison, not all of them can be measured directly (for instance I_{sp} , c_{eff} , c^* , C_F), any statement about the limits of error must involve Gauss' law of error propagation.

Since the ODE functions are already quite complicated, it is obvious that their partial derivation - necessary for Gauss' method - will become rather cumbersome. Therefore, numerical results can no longer be obtained by quick estimates, but will require EDP [electronic data processing]. On the basis of reading errors and the standard deviations of individual measurement variables, we obtain the following table of input quantities for the program (see page 122).

The subsequent Figure 75 (page 123) shows a typical printout /118 for a complete test. In addition to the Gaussian error, in each case also the maximum error is shown that results from linear superposition. We should add that the computation time (CPU [central processing unit] time required) for the error program is of the same order of magnitude as that required for the entire boundary layer program.

TABLE 5 LISTING OF INDIVIDUAL ERRORS

$\Delta m_{\text{Balance}}$	$\leq 0.005 \cdot 10^{-3} \text{ kg}$
Δp_{∞}	$\leq 1 \%$
Δp_c	$\leq 0,4 \%$
ΔT_c	$\leq 0,2 \text{ k}$
ΔT_{∞}	$\leq 0,2 \text{ k}$
$\Delta \gamma$	$\leq 0,1 \text{ ‰}$
Δm_{mol}	$\leq 0,03 \text{ ‰}$
Δm_{calib}	$\leq 0,02 \text{ ‰}$
$\Delta \alpha_e$	$\leq 0,1^\circ$
Δc	$\leq 0,7 \%$
ΔL_{pipe}	$\leq 0,02 \%$
$\Delta F_{\text{upthrust}}$	$\leq 0,5 \%$ will be compensated
$\Delta m_{\text{Gas, in the thrust frame}}$	$\leq 0,17 \%$
$\Delta F_{\text{Bourdon}}$	$\leq 1,0 \%$ will be compensated (171)
$\Delta E_f(T)$	$\leq 0,4 \%$
$\Delta \text{Electronics}$	$\leq 0,3 \%$ for 30 sec test duration
ΔF_{Σ}	$\leq 0,9 \%$

*

(0) (1)
 9.2001

..... (2)

 (3) (4) (5) (6)

(0) (7)

 (8) (9) (10)

		(8)	(9)	(10)
.....	PER
..... (0)
.....
..... (12)
..... (13)
..... (14)
..... (15)
..... (16)	IS01
..... (16)	IS02
..... (16)	IS03
..... (16)	IS04

KEY 0 Illegible 1 Test number 2 Input data 3 Surface ratio 4 Environment pressure 5 Measured throughput 6 Measured thrust 7 Error 8 Function value 9 Maximum error 10 Gaussian error 11 Mass factor 12 Thrust coefficient 13 Effective velocity 14 Characteristic velocity 15 Thrust 16 Specific impulse

Figure 75 Error protocol printout for Test No. 9.2001

The agreement between the predicted mass throughput coefficient c_D and that determined experimentally, is very satisfactory (see Figures 72 and 74). The predicted specific propulsion unit impulse data (especially $I_{sp,del}$) have been clearly confirmed by measurements, in the range of $\epsilon = 10$ to 100 and $p_c = 2-10$ bar. Beyond $\epsilon = 100$ and $p_c = 10$ bar, some uncertainty should be assumed in the overall statement, because $p_e \ll p_\infty$ and due to the associated flow separation effects. We expect an improvement in future experiments, using vacuum pumps of higher suction capacity and developing a new method for the direct determination of the separation site on the nozzle wall, and of the separation pressure, p_{sep} . From the point of view of engineering manipulation, the model used for boundary layer calculations may be considered satisfactory, since it allow sufficient prediction precision over a wide range of propulsion unit sizes and operating conditions. Taking into consideration the simplified equation discussed in section 2.2.10, a fast answer in regard to $\Delta\eta_{bl}$ can be obtained in subsequent applications. Further improvements seem possible, in the future, in the measurement system; in connection with improved computer programs it should become possible to further improve the reliability of the statements obtained using 2.2.10. The results obtained in the present case, for stationary operation behavior, can also be extended to pulse operation (as is often the case in attitude control tasks). The digital acquisition of measurement values and their subsequent processing and comparison with theoretical predictions represents a considerable simplification of efforts and makes it possible to eliminate large sources of error often encountered in manula calculations.

It is possible, using the nozzle manufacturing method described, to produce not only conical nozzles with throat diameters in the 0.1 mm diameter range, but also optimized "bell nozzles", with specific impulses up to 2% higher. It can be shown that their application in future satellite systems (especially if the lifetime is > 5 years) can result in the saving of several kg of fuel (for a 1 ton satellite mass, for instance), which in turn increases the payload capacity. Since as of this date it is hardly possible to further reduce the structural factors, and a limit is going to be reached in the near future also for specific electronic masses, a decrease in the orbit and attitude adjustment fuel requirements is absolutely necessary.

The non-contact thrust measurement procedure here developed can be utilized also in other areas, in which the precise measurement of not directly accessible test objects is necessary.

The use of non-displacement weighing systems with simultaneous prebalancing of the storage container is an area usable in measurement technology (resolution: nearly six orders of magnitude of continuous mechanical processes), which is urgently needed to continue development of precise throughput measurement instruments and their calibration. By using the impulse-specific characteristic variables determined in the precision measurements, it is possible not only to more precisely adapt the extensive explicit computer programs, but also those more easily handled in the rapid design of propulsion units, providing "rule of thumb" but usable equations. In the continuation of these performance measurements using larger vacuum pumps (higher suction capacity), these results can be extended to large (>150) nozzle surface ratios.

The results of this effort can be used not only in space travel per se, but conceivably also in the development of gas dynamics laser systems or the U-235 enrichment by nozzle-separation methods.

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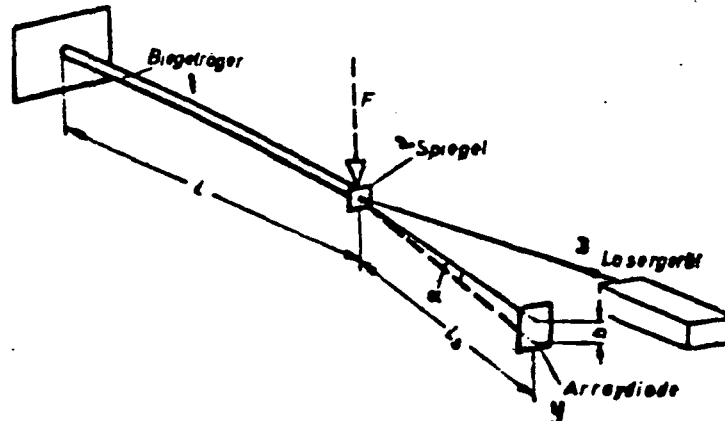
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9.1 Design of the cantilever beam



KEY 1 Bending carrier 2 Mirror 3 Laser instrument 4 Array diode

Figure 76 Arrangement of the bending carrier with mirror, laser instrument and array diode

Specified quantities:

$G = 15 \text{ N}$ (weight of nozzle and harness)

$L_{\max} = 250 \text{ mm}$

$L_s = 0.5 \text{ m}$

$S = 1 \text{ N}$ (thrust)

$a = 10 \text{ }\mu\text{m}$

$b_{\max} = 1.5 \text{ mm}$

$\Delta S = 10^{-2} \text{ N}$

For the bending line $w(x)$ we have, for small deformations with a line load q due to the carrier's own weight:

$$EI w^{IV} = -q$$

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Following quadruple integration

$$EI w = -\frac{1}{24} x^4 q - \frac{1}{6} x^3 F + \frac{1}{2} x^2 C_1 + C_2 x + C_3$$

With the boundary conditions

$$w(0) = w'(0) = w''(L) = 0$$

the integration constants become

$$C_3 = 0$$

$$C_2 = 0$$

$$C_1 = LF + \frac{1}{2} qL^2$$

We then have, for the bending line and its inclination

$$w(x) = \frac{1}{EI} \left[-\frac{1}{24} qx^4 - \frac{1}{6} x^3 F + \frac{1}{2} x^2 (LF + \frac{1}{2} qL^2) \right]$$

$$w'(x) = \frac{1}{EI} \left[-\frac{1}{6} qx^3 - \frac{1}{2} x^2 F + x (LF + \frac{L^2}{2} q) \right]$$

At the location of the mirror, $x = L$ and we have

$$w'(L) = \frac{FL^2}{2EI}$$

(here we assume $q = 0$ and $F = G + S$)

The angular change of the reflected laser beam will be twice the change of the slope in the bending line, due to the laws of reflection:

$$\alpha = 2 \left[w'(L)_{G+S} - w'(L)_G \right] \cong \frac{L^2}{Es} \cdot S$$

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The path b traversed by the laser beam's point of impact on the array diode is

$$b = L_s \tan \alpha$$

Since b is very small compared to L_s and therefore α is very small, $\tan \alpha = \alpha$ and hence,

$$b = \frac{L_s L^2}{E I} \cdot S$$

The carrier must satisfy the following conditions:

- 1) The deformation must be large enough to attain the desired precision

$$a < \frac{L_s L^2}{E I} \cdot \Delta S$$

- 2) The deformation must be smaller than the size of the array diode allows

$$b_{\max} > \frac{L_s L^2}{E I} S_{\max}$$

- 3) No plastic deformation of the tube under thrust or its own weight, respectively

$$\sigma < \sigma_{zul}$$

From 1) and 2):

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$$\frac{b_{\max}}{S_{\max} L_s} > \frac{L^2}{E I} > \frac{a}{\Delta S L_s}$$

with

$$\sigma_{\max} = \frac{M_{\max}}{W_b} = \frac{F L}{W_b}$$

and

$$I_{\text{Kreisrohr}} \approx \pi r_m^3$$

(Kreisrohr = circular tube)

or

$$w_b \approx \pi s r_m^2$$

as well as

$$\begin{aligned} L &= 200 \text{ mm} && \text{(Anticipating the result)} \\ \Delta S &= 10^{-2} \text{ N} && \text{("Stahl" = steel)} \\ L_s &= 0,5 \text{ m} \\ \sigma_s &= \frac{N}{\text{mm}^2} \end{aligned}$$

we obtain: $I \approx 100 \text{ mm}^4$; if a 1 mm wall thickness is chosen, then

$$r_m = \sqrt[3]{\frac{I}{\pi s}} \approx 3,2 \text{ mm}$$

$$\sigma_{\max} < \frac{F L}{\sqrt[3]{\pi s} s_{\max}^2 L^4 L_s^2 b_{\max}^{-2} E^{-2}} \sim L^{1/3}$$

or

$$\sigma_{\max} < C \cdot E^{2/3}$$

From this we realize that L must be chosen as large as possible /142 (within the vacuum chamber).

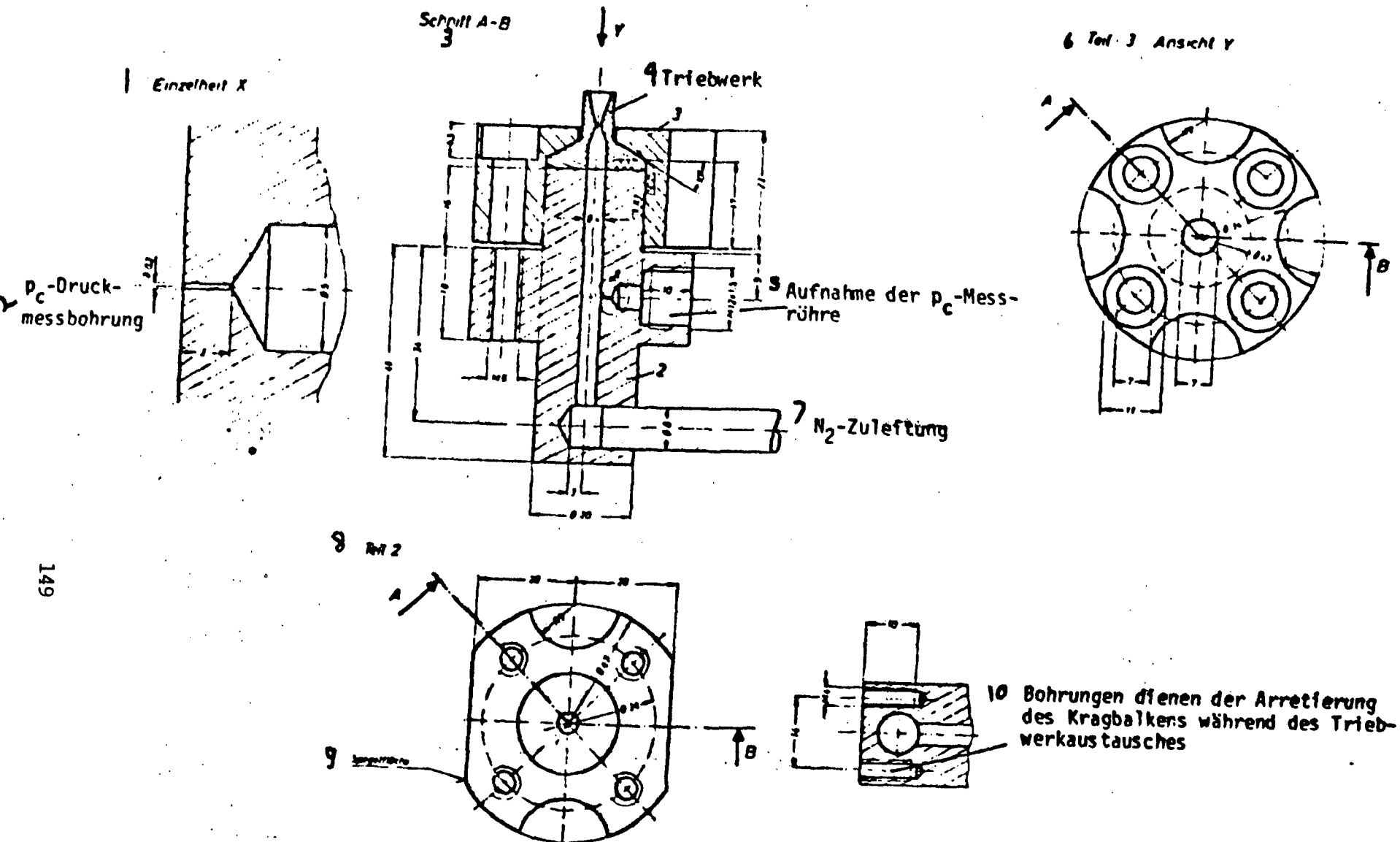
For the certainty against plastic deformation we have

$$S_{\text{plast}} > \frac{\sigma_s}{\sigma_{\max}}$$

With the design magnitudes listed above, S_{plast} becomes ≈ 2.7 , i.e., no weight compensation is necessary!

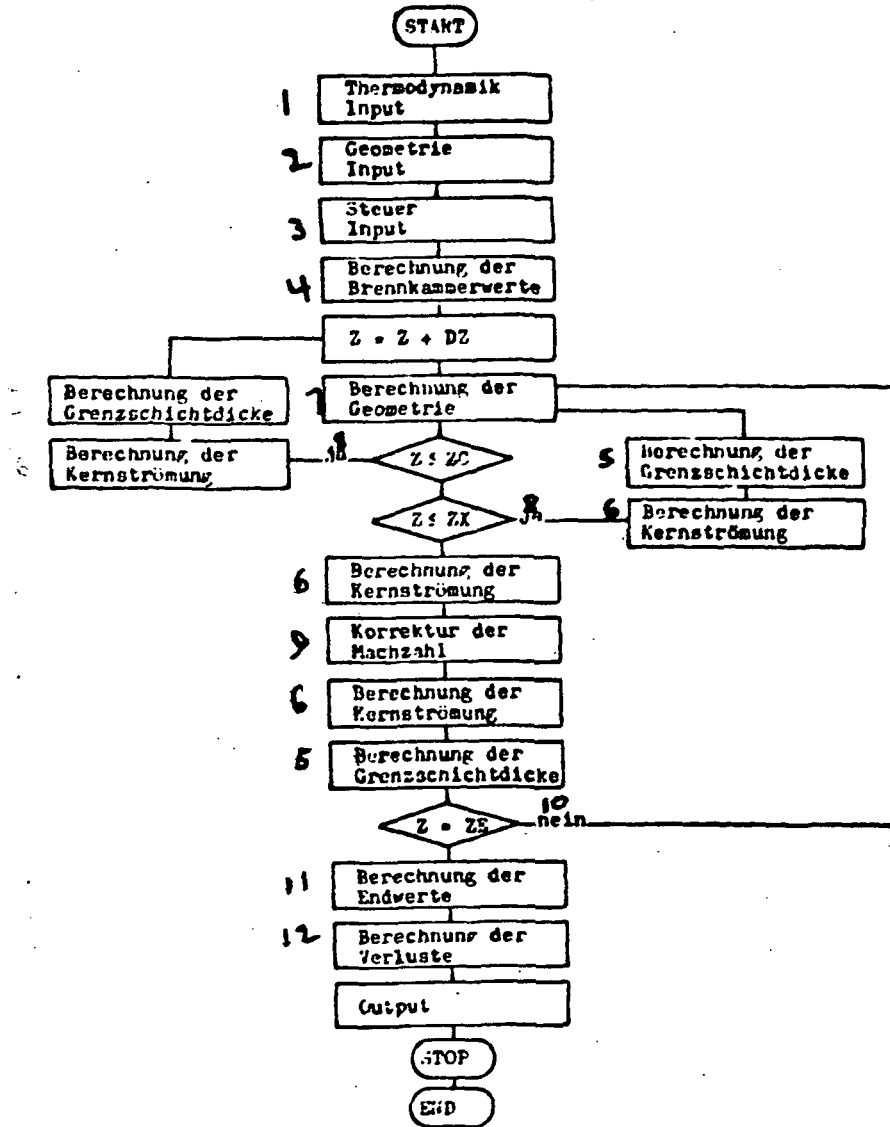
Of the materials examined, steel had the best qualities, in addition to its preference because of ready availability and simple processing (can be welded).

The nozzle holding flange welded to the free end of the cantilever beam (tube), including p_c tube (see Figure 77, page 150) remains clearly below 15 N, in weight, in the final design; hence the design calculations remain valid (with respect to S_{plast}). In addition the resolution of the array diode system could be considerably increased (see section 3.2.3).



KEY 1 Detail X 2 p_c pressure measurement boring 3 Section 4 Thruster 5 p_c meas. tube receptacle
 6 Part 3 View Y 7 N₂ inflow line 8 Part 2 9 [Illeg.] 10 Boreholes serve to arrest the cantilevered
 beam during the propulsion unit exchanges

Figure 77 Thruster receiving flange



KEY 1 Thermodynamic input 2 Geometry input 3 Control input 4 Calculation of combustion chamber values 5 Boundary layer thickness calculations 6 Core flow calculations 7 Geometry calculations 8 yes 9 Mach number correction 10 No 11 End value calculation 12 Loss calculations

Figure 78 Computer program flow diagram

9.3 Test protocol

Versuch: 5 / 10 / 01				Datum: 22.4.1981							
3 T _{Flasche}		4 T _c Brennkam.		5 T _∞ Vakuum		6 T ₀ Raum		7 T _{Waage}		8 T _{N2-Kammer}	
(mV)	[K]	(mV)	[K]	(mV)	[K]	(mV)	[K]	(mV)	[K]	(mV)	[K]
0.2894	291.2	0.2998	296.5	0.2921	294.6	0.2947	293.9	0.2918	300.3	0.2884	291.6
P ₀	P _c	P _∞ (+6 V !)		Δm _{vor}	Δm _{nach}	m _{vers.}	m _{korr.}	F _{o,v,DW}	F _{o,n,DW}	F _{DW}	F _{i/D}
[Torr]	[bar]	[V]	[Torr]	[g/s]	[g/s]	[g/s]	[g/s]	(mV)	(mV)	(mV)	(mV)
714.8	10.055	8.21	9.04	-0.0025	0.0015	0.2161	0.2156	+37.14	+37.19	+67.23	+67.22
ΔF	Schub	ε	r _t	Bk _l	Bk _φ	α _e	dF/d	Bemerkungen : P _{c,v} = 0.1002 P _{c,n} = 0.1001 P _{c,m} = 0.2007 P _{c,A/D} = 0.2009			
(mV)	[g]	[-]	[mm]	[mm]	[mm]	[°]	(g/mV)				
30.067	16.071	194.0656	0.176	5.0	4.0	15.0	0.5357				

KEY 1 Test No. 2 Date 3 Bottle 4 Combustion chamber 5 Vacuum 6 Room 7 Balance
8 N₂ chamber. 9 Thrust 10 Remarks

Figure 79 Example of test protocol (5.1001)

9.4 Cost analysis (180 + 188)

Balance and printer (Mettler)	DM 7,700
Laser 101P (Laser Optronic)	1,400
Components for measurement data acquisition	600 (approx)
P _c measurement tube and amplifier	450
PIN-LSC array diode system (incl. evaluation syst.)	1,800
Neutral wedge	190
Micrometer drive motor	80
Vacuum minimotor	140
Temperature measurement sensors (6)	180
Molding knife for nozzle manufacture	1,500
Nozzle manufacture (galvanoplastics)	280
N ₂ - 2 liter bottle (2)	300
1 transfer tube (special manufacture)	210
Small parts (approx.)	500
Working gas (approx.)	600
Documentation (approx.)	700
	<hr/>
Total (approx.)	DM 16,630*

* Of this, approximately DM 11,500 are outside financing

BIOGRAPHICAL DATA

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- [REDACTED] Born in [REDACTED] as son of civil engineer
 Erich Hayn and his wife Ruth, born Braun
- 06-03-70 Graduation from the mathematical-scientific high school
 Max von Laue, Koblenz
- 07-01-70/ Basic training for tank grenadier at Unna, Westphalia
 09-30-70
- 10-01-70/ Special Weapons Technical Batallion, Koblenz (service
 10-31-70 grade: Ppal. lance Corporal)
- 10-21-71 Matriculation at TU Munich, Technical Area Mechanical
 Engineering
- 07-01-72 Start of collaboration in the WARR [wissenschaftliche
Arbeitsgemeinschaft Raketentechnik und Raumfahrt =
 scientitif study group for rocket engineering and space
 flight]
- 04-23-74 Preliminary diploma in Mechanical Engineering
- 1974-1976 Technical spokesman for aeronautic and astronautical
 technologies
- 1974-1976 WARR director; development of a liquid rocket thruster
- 07-23-76 Married Ilsa Isabella Schgaguler
- 03-31-77 Concludes thesis at Chair C, Thermodynamics, on a laser
 interferometric measurement method
- 05-10-77 Receives degree in Aeronautical and Astronautical Engi-
 neering
- since Employed at the Chair for Astronautical Engineering of
 06-01-77 TU Munich
- 06-01-77/ Collaboration with the ERNO company, Bremen (FRG), in
 07-01-78 an ESA project for the PAEHT thruster
- 09-12-77 Decoration by the management of the DGLR [Deutsche
 Gesellschaft fuer Luft- und Raumfahrt = German Society
 for Aero and Astronautics] for the above activity, as
 Director of the WARR