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THE DISCOVERY CIRCUMSTANCES OF
: ARTH-APPROACHING ASTEROIDS
(NASA-CR-174327) SHE DISCOVERY N85-17920
CIRCUMSTANCES OF EARTH-APPEOACHING ASTEROIDS (Lincoln Lab.) $34 \mathrm{p} \mathrm{HC} \mathrm{AOB/HF} \mathrm{AO1} \mathrm{CSCL} \mathrm{03B}$

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* $\quad$.

Running Head: Asteroid discoveries

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#### Abstract

We have analyzed the discovery circumstances of all Earthapproaching asteroids detected in the last twenty-four years. In particular, we have calculated topocentric angular velocities, opposition distance, geocentric and heliocentric distances, phase argle, and lunar phase at discovery in an effort to separate any selection effects between chance and purposeful (i.e., as the result of a systematic search) discoveries. Another motivation was the possibility of discerning useful clues how to search more efficiently for such objects. There are 60 minor planets in our sample. Our principal result is that the discovery of Earthapproaching asteroids is dominated by serendipity. Therefore, searching for them at the current relatively bright limits at less than a very high rate seems pointless.


## I. FORMULATION

In this paper any asteroid whose perihelion distance is less than that of Mars's is termed an Eartl-approaching object. This includes the Aten, Apollo, and Amor classes and a few Marscrossing minor planets too. We have investigated the discovery circumstances of such objects with the intent of correcting the existing searches for systematic effects or exploiting such effects (if they exist) in order to enhance future search efforts. Because of the random first appearance on the celestial sphere of this usually fast-moving subset of the minor planets, any systematic advantage would be of great assistance. We looked for correlations amongst the discovery geocentric distance, heliocentric distance, phase angle, topocentric angular velocity, angular distance from opposition, lunar phase at the time of discovery, and seasonality variations of discovery rates.

In order to compute much of this information one needs an orbital element set. Orbital element sets for this subset of asteroids vary widely in quality. Factors influencing the accuracy of the element set include the total observational arc (days, months, or years herein), the distribution of astrometric data over this time span, the recovery of "pre-discovery" observations (again days to years for some members of this group), and the quality of the individual observations themselves. For some objects several element sets are now available and
represent various stages in the differential correction process. It was impossible to choose element sets of uniform auality. Given our desire to perform the essential research of this paper, some compromise had to be reached. The detailed references to the particular element sets we employed are given in Table I.

The longest running Earth-approaching asteroid search is that of Helin and Shoemaker, 1979. It dates from 1973. (Our own search is only four years old; Taff, 1981.) We have used the last eleven years and the preceding eleven too as the base for our sample. This includes 60 minor planets. Our aim in this case was to try and balance, as much as possible, the pre-search era with the post-search era. In this way we hoped to minimize long term effects having to do with the weather, observatory existence, distribution, and equipment, the essential observing techniques, and even astronomical fashion. Bringing the study up to date, (e.g. 1983VA, and so on) would only increase the number of objects without good element sets. Backdating further, say to include the Palomar-Leiden survey would add 1960VA $=2061$, 1959EH $=1980 \mathrm{RB}=2629$, 1959 LM , and three P-L objects (4789, 6344, 6743) for which the discovery circumstances were not published. Again we have made a debatable choice.

The original pair of discovery observations and orbital element sets have been taken directlv from the appropriate Minor Planet Circulars or International Astronomical Union Circulars.

The catalogues of Marsden and Bardwell, 1982a, b, proved very helpful in this regard as did a complete list of Atens, Apollos, and Amors kindly supplied to us by Dr. E. F. Helin.

In the next section we discuss the calculation of ous derived quantities and in the following one we analyze it in several wavs. Our conclusions are in the last section.
a) Angulat Velocities

Ideally the minor planet left a long trail, on a well timed plate, so that both ends of the trail could be independently measured and reduced. Slightly less ideal are two different photographs from the same night. In a few cases days intervened between the initial pair of observations. In even fewer instances there was only a single data point. Except in the last instance or when the textual remarks in an IAU Circular provided detailed information, we calculated $\Delta \alpha, \Delta \delta$, and $\Delta t$ in the obvious way. The topocentric angular speed'w and position angle $p$ were then computed from

$$
\begin{aligned}
(\Delta \alpha / \Delta t) \cos \delta & =\omega \sin P \\
\Delta \delta / \Delta t & =\omega \cos P
\end{aligned}
$$

$\omega$ is given in degrees/day (to the nearest hundredth) and $P$ is given in degrees (to the nearest one) in Table I [columns 4 and 5; column 2 gives the original source of the data (MPC or IAUC) and column 1 gives the provisional designationl. Those values computed from the longer time spans or other less reliable means are indicated by a colon in Table I.
b) Opposition Distance and Phase Angle

We used the geocentric (solar system barycentric post-1980)
equatorial rectangular coordinates of the Sun (Earth) to compute the solar right ascension and declination at the discovery time. Then we coupled this lineasly interpolated information from The American Ephemeris and Astronomical Almanac (The Astronomical Almanac) with the discovery location to compute the angular distance from the opposition at the instant of discovery. This is listed in the tenth column of Table I. The discovery location came from the element sets whose MPC source is given in the third column of Table $I$. We assumed that there were no perturbing influences acting over the time spans involved and that the element sets were representative of an osculating heliocentric location and velocity.

Phase angles were calculated from the above information according to their definition. They are listed in the ninth column of Table I. The heliocentric (r) and geocentric (R) discovery distances occupy columns seven and eight of the Table.
c) Lunar Phase and Seasonality

We anticipated that most discoveries would occur near New Moon rather than near full Moon. We assigned Full Moon a phase of 0, first Quarter a phase of 0.25 , New Moon a phase of 0.5 , and Third Quarter a phase of 0.75 . From the discovery date, the lunar synodic period, and old issues of The American Ephemeris and Nautical Almanac (or The Astronomical Almanac post-1980) the
phases in the si:ith column of Table I were deduced. Another: thing we examined was the seasonality variation -- both monthly and in seasons. As almost all of this information is present in the provisional designation, we have not listed the actual discovery dates.
Table I. Data on Earth-approaching Asteroids

| Designation | Discovery Reference ${ }^{\text {a }}$ | Element Set Reference ${ }^{\text {a }}$ | Angular Speed ( $\%$ d) | Position <br> Angle ( ${ }^{\circ}$ ) | Lunar <br> Phase | Heliocentic Distance (A.U.) | Geocentric Distance (A.U.) | Phase Angle( ${ }^{\circ}$ ) | Opposition Distancei* |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1963UA | 2308 | 3016 | 0.89: ${ }^{\text {b }}$ | 136: ${ }^{\text {b }}$ | 0.44 | 1.25 | 0.25 | 2.5 | 3.1 |
| 1968AA | 2845 | 3017 | 0.39: | 324: | 0.51 | 1.48 | 0.71 | 34.6 | 58.7 |
| 1971FA | 3895 | 3754 | 0.64 | 274 | 0.48 | 1.86 | 0.86 | 0.7 | 1.4 |
| 1971SC | 3299 | 5032 | 0.51 | 165 | 0.75 | 1.37 | 0.37 | 7.7 | 10.5 |
| 1971UA | 3896 | 3755 | 1.08 | 223 | 0.76 | 1.36 | 0.37 | 1.9 | 2.5 |
| 1972RA | 3381 | 4659 | 0.77: | 130: | 0.46 | 1.23 | 0.22 | 4.6 | 5.6 |
| 1972RB | 3381 | 4659 | 1.23 | 108 | 0.76 | 1.14 | 0.13 | 4.7 | 5.3 |
| 1972XA | 3619 | 3756 | 1.44 | 324 | 0.50 | 1.18 | 0.23 | 29.8 | 36.5 |
| 1973EA | 3525 | 4010 | 1.20 | 282 | 0.57 | 1.29 | 0.41 | 36.1 | 50.1 |
| 1973 EC | 3525 | 3899 | $0.80=$ | 150: | 0.80 | 1.14 | 0.23 | 47.2 | 57.0 |
| 1973NA | 3601 | 4659 | 11.90 | 206 | 0.62 | 1.11 | 0.09 | 14.6 | 16.0 |
| 1974MA | 3712 | 4659 | 0.91 | 31 | 0.73 | 1.40 | 0.68 | 43.4 | 70.5 |
| 1974UB | 3813 | 3910 | 0.88: | 309: | 0.67 | 1.68 | 0.69 | 5.7 | 9.5 |
| 1975TB | 5393 | 4541 | 2.43 | 210 | 0.40 | 1.13 | 0.16 | 32.9 | 37.9 |

Table I. Data on Earth-approaching Asteroids (Cont'd.)

| Designation | Discovery Referencea | Element Set Reference ${ }^{\text {a }}$ | Angular Speed ( $\% / \mathrm{d}$ ) | Position Angle ( ${ }^{\circ}$ ) | Lunar <br> Phase | Heliocentic Distance (A.U.) | Geocentric Distance (A.U.) | Phase Angle( ${ }^{\circ}$ ) | Opposition Distance( ${ }^{\circ}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1975YA | 3918 | 3919 | 20.32 | 337 | 0.29 | 1.02 | 0.05 | 40.2 | 42.0 |
| 1976AA | 3918 | 3919 | 2.51 | 328 | 0.67 | 1.11 | 0.13 | 7.1 | 8.0 |
| 1976UA | 4395 | 4659 | 15.17 | 151 | 0.48 | 1.01 | 0.01 | 39.7 | 40.2 |
| 1976WA | 4147 | 4660 | 0.58 | 14 | 0.41 | 1.36 | 0.61 | 41.8 | 66.3 |
| 1977HA | 4193 | 4660 | 0.62 | 103 | 0.45 | 1.13 | 0.17 | 40.1 | 46.4 |
| 1977HB | 4193 | 4406 | 1.24 | 256 | 0.68 | 1.19 | 0.18 | 1.5 | 1.8 |
| 1977RA | 4392 | 4660 | 0.23: | 39: | 0.24 | 1.24 | 0.25 | 17.8 | $2 \Sigma .2$ |
| 1977VA | 4396 | 4660 | 0.83: | 100: | 0.42 | 1.13 | 0.14 | 5.0 | 5.7 |
| 1978CA | 4392 | 4660 | 6.60: | 352: | 0.51 | 1.20 | 0.28 | 36.2 | 45.9 |
| 1978DA | 4392 | 6827 | 0.77: | 79: | 0.81 | 1.20 | 0.24 | 25.3 | 31.2 |
| 1978RA | 4496 | 4541 | 1.96 | 218 | 0.78 | 1.19 | 0. 19 | 5.2 | 6.2 |
| 1978SB | 4569 | 4661 | 1.25= | 289: | 0.38 | 1.32 | 0.33 | 15.3 | 20.3 |
| 1978VB2 | 4724 | -- | - | -- | 0.53 | -- | -- | -- | -- |
| 19790A | 4904 | -- | 1.59 : | 280: | 0.48 | -- | -- | -- | -- |

Table 1. Data on Earth-approaching Asteroids (Cont'd.)

| Designation | Discovery Reference ${ }^{\text {a }}$ | Eleaent Set Referencea | $\begin{gathered} \text { Angular } \\ \text { Speed }(\% / d) \end{gathered}$ | Position <br> Angle ( ${ }^{\circ}$ ) | Lunar <br> Phase | Heliocentic Distance (A.G.) | Geocentric Distance (A.U.) | Phase Angle(*) | Opposition Distance( ${ }^{\circ}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 19790B | 4904 | 5515 | 0.17 | 354 | 0.48 | 1.34 | 0.33 | 4.2 | 5.6 |
| 1979VA | 5120 | 5319 | 1.76 | 93 | 0.37 | 1.12 | 0.15 | 22.4 | 25.7 |
| 1979XA | 5121 | 5176 | 1.32 | 257 | 0.32 | 1.24 | 0.31 | 29.6 | 38.5 |
| 1979xB | 5120 | 5131 | 3.87 | 235 | 0.26 | 1.03 | 0.09 | 49.8 | 53.7 |
| 1980AA | 5138 | 5279 | 2.58: | 120: | 0.39 | 1.05 | 0.07 | 12.2 | 13.1 |
| 1980PA | 5514 | 5899 | 0.83 | 53 | 0.32 | 1.27 | 0.31 | 32.1 | 41.6 |
| 1980RB1 | 5594 | St4\% | 0.60 | 292 | 0.63 | 1.64 | 0.54 | 6.4 | 10.4 |
| 1980wF | 5669 | 5841 | 1.07 | 136 | 0.24 | 1.13 | 0.14 | 7.7 | 8.8 |
| 1980YS | 5827 | 5899 | 0.11 | 1 | 0.29 | 1.23 | 0.26 | 7.7 | 9.7 |
| 1981CW | 5886 | 5977 | 0.67 | 64 | 0.57 | 1.19 | 0.30 | 42.2 | 53.9 |
| 1981ET3 | 7093 | 7234 | 0.34 | 267 | 0.39 | 2.50 | 1.56 | 9.4 | 24.4 |
| 1981JD | 6036 | --- | 3.14 | 240 | 0.68 | - | -- | -- | - |
| 19810A | 5237 | 6702 | 0.91 | 127 | 0.21 | 1.19 | 0.20 | 26.3 | 31.4 |
| 19810B | 6254 | 6702 | 1.48 | 192 | 0.43 | 1.40 | 0.40 | 8.4 | 11.8 |

Table I. Data on Earth-approaching Asteroids (Cont'd.)

| Designation | Discovery Reference ${ }^{\text {a }}$ | Element Set Referencea | Angular speed ( $\% / d$ ) | Position Angle ( ${ }^{\circ}$ ) | Lunar <br> Phase | ```Heliocentic Distance (A.U.)``` | Geocentric Distance (A.U.) | Phase Angle(*) | Opposition Distance(") |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981VA | 6481 | 6702 | 2.19 | 196 | 0.74 | 1.22 | 0.29 | 32.5 | 41.5 |
| 1982BB | 6674 | 6703 | 0.75 | 342 | 0.35 | 1.40 | 0.50 | 27.5 | 41.1 |
| 1982CA | 6769 | -- | 1.88: | 248 | 0.17 | $\cdots$ | - | - | - |
| 1982 DB | 6675 | 6831 | 0.74 | 282 | 0.68 | 1.06 | 0.11 | 47.7 | 52.3 |
| 1982DV | 6690 | 6831 | 0.73 | 128 | 0.67 | 1.20 | 0.26 | 31.6 | 39.5 |
| 1982EA | 6770 | -- | 0.65 | 265 | 0.78 | - | - | - | $\square$ |
| 1982 FT | 6877 | 8538 | 1.07 | 211 | 0.66 | 1.31 | 0.36 | 26.3 | 35.5 |
| 1982HR | $3692{ }^{\text {a }}$ | 7840 | 2.49: | 264: | 0.54 | 1.05 | 0.06 | 38.4 | 40.4 |
| 1982RA | 7202 | 7602 | 1.70 | 334 | 0.33 | 1.24 | 0.32 | 37.4 | 48.5 |
| 1982RB | $3725^{\text {a }}$ | 7602 | 1.05 | 168 | 0.36 | 1.33 | 0.34 | 15.6 | 20.8 |
| 1982TA | 7342 | 8539 | 0.93 | 263 | 0. 27 | 1.48 | 0.50 | 13.3 | 20.5 |
| $1982 \times 8$ | 7563 | 7841 | 3.01 | 31 | 0.45 | 1.02 | 0.05 | 33.7 | 35.2 |
| 1982YA | $3758{ }^{\text {a }}$ | 8534 | 2.61: | $190=$ | 0.71 | 1.22 | 0.24 | 2.6 | 3.2 |
| 1983LB | 8014 | 8056 | 1.48 | 205 | 0.59 | 1. 31 | 0. 30 | 10.4 | 13.5 |

$a^{\text {a }}$ References marked by this symbol refer to an I.A.U. Circular. All others are MPC numbers.


## a) Angulat Velocities

We examined the angular velocity in three fashions. First we created the (binned) frequency of angular speeds, see Fig. 1. A bin size of $0 \% 25 / \mathrm{d}$ was used (e.g., $0 \% / \mathrm{d} \leq \omega 0 \% 25 / \mathrm{d}$ and so forth) up to $3: 25 / \mathrm{d}$. There were 4 minor planets with higher angulat speeds. The average value of $\omega$ ovar the sample is 2:05/d with a standard deviation about the mean (including Sheppard's corrections) of $3: 38 / \mathrm{d}$. The lack of low speed Earthapproaching minor planets needs no explanation because topocentric angular speed is the principal method of discrimination for these objects. We have no deep insight into the form of the curve. Next we looked at the distribution of the position angles (Fig. 2). As you can see it is almost uniform except for a slight northeast quadrant deficiency. The mean position angle is $196^{\circ}$ and the standard deviation about the mean (including Sheppard's corrections for the $45^{\circ}$ size bins) is $95^{\circ}$. The northeast quadrant deficiency is especially evident when quadrant binning is used. The frequency distribution is now 8, 17, 18, 16 around the compass. Furthermore, there is no correlation iswween $P$ and discovery date. Lastly we plotted, on polar coordinate graph paper, an angular velocity scatter diagram. The most striking feature about it is that there are no striking features.
b) Opposition Distance and Phase Angle

Let $\mathscr{E}_{A}$ be the heliocentric location of the asteroid, Ee the heliocentric location of the Earth, and $R_{A}$ be the geocentric ( $=$ topocentric) location of the asteroid. Then the phase angle $\phi$ and the opposition distance $\phi$ given by

$$
\cos \phi=\frac{\underline{R}_{A} \cdot \underline{\varepsilon}_{A}}{R_{A} r_{A}}, \quad \cos \phi=\frac{\underline{R}_{A} \cdot \underline{\underline{r}}_{E}}{R_{A} \underline{r}_{E}}
$$

Since $\underline{E}_{A}=\underline{R}_{A}+\underline{E}$ and $R_{A}$ is usually much smaller than re or $r_{A}$, it follows that

$$
\cos \phi=\cos \phi+\left(R_{A} / r_{E}\right) \cdot \sin \phi
$$

Hence, for most discoveries near opposition $\phi<\Phi$. Although there is a strong opposition effect ( $\approx 0.44$ ) in minor planet phase functions and an additional linear decrease of the phase function in magnitudes with increasing phase angle (beyond $\approx 8^{\circ}$ ), the histogram in Fig. 3 does not support the hypothesis that Earth-approaching asteroids are preferentially discovered near opposition. An equal area plot on the celestial sphere centered at opposition reinforces this conclusion. The phase angle at discovery frequency distribution is shown as the dotted histogram in Fi.g. 3. Apparently once an Earth-approaching minor planet becomes bright enough, and most are found with $\mathrm{V}<15 \mathrm{~m}$, it is detected by whomever photographed it and knew what to look for.

The geocentric and heliocentric distances in Table I show that Earth-approaching asteroids tend to be found when they approach the Earth. We assume that this is a consequence of their increased brightness and angular speed. There are unusual cases though (e.g., 1981ET3). The distributions are shown in Figs. 4 and 5.
c) Lunar Phase and Seasonality

We'll discuss seasonality first; the counts are given in Table II. There is a noticeable lack of non-uniformity due to a pronounced deficiency of discoveries during April, May, June, and July. We feel that the obvious Northern hemisphere bias of observatory distribution coupled with some elementary solar system geometry accounts for this (e.g., opposition is low in the sky at the summer solstice and the galactic plane high). Not surprisingly Spring is the lowest return season too: Winter 17, Spring 8, Summer 16 , and Fall 19. The big jump in the number of September discoveries (which props up the Summer discovery counts) is probably a result of the geometrical factors mentioned above as well as observer bias due to the Spring drought, the short Summer nights, a few months rest, renewed enthusiasm, good Fall weather, and so on.

The distribution of lunar phases is shown in Fig. 6. As we anticipated there is a dearth of discoveries near Full Moon and a maximum near New Moon. There is no bias towards the waning
Table II. Monthly Discovery Variation

|  | Jan. | Feb. | Mar. | Apr. | May | Jun. | Jul. | Aug. | Sep. | Oct. | Nov. | Dec. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number | 4 | 6 | 6 | 3 | 1 | 3 | 1 | 5 | 11 | 7 | 6 | 7 |

Third Quarter Moon relative to the waxing First Quarter Moon which is significant. Such an effect might have been predicted on the grounds that a well planned search would commence during the waning Third Quarter phase. For then, should an interesting asteroid be found, the maximum amount of dark time would be available for further observations. Alternatively, one's enthusiasm might be higher at the beginning of a search period then at the end, it is easier to work in the evenings than it is in the mornings, and one's eagerness and alertness would be expected to drop immediately after a discovery because experience has taught us of the rareness of any find.
d) Discovery Circumstances

What scientific research were the majority of the discoverers conducting when they exposed the photographic plate on which the minor planet's trail appeared? Most of them were not searching for Earth-approaching asteroids but were engaged in some other type of astronomy. In addition, some of the asteroids of interest credited to the Helin and Shoemaker, 1979 search were found while they were pursuing other studies. As an example l98lVA was found during a search for high inclination asteroids (Helin, et al., 1982). As a second illustration 1982DB was found while they were engaged in cometary studies. (JPL press relese \#990 4/7/82 MBM; see also Aviation Week \& Space Technology for May $10,1982, \mathrm{pg} .51$ or Sky and Telescope

63, 455, 1982.) These can clearly not be credited to their systematic Earth-approaching asteroid search efforts. As a thied example we have 198leT3, a "UCAS" discovery of R. Bus. In an effort to ascertain what fraction of the Earth-approaching asteroids discovered by and credited to the Helin and Shoemaker systematic search but should not be so attributed, we have critically examined their less well publicized discoveries.

## IV. SEARCH STRATEGY AND PAYOFF

What do we know about the probability of occurrence, based on the 55 element sets referenced in Table $I$, of an asteroid of this type? The means and standard deviations about the means are shown in Table III. Clearly these object can come from most fuarters of the celestial sphere but retrograde motion is ruled out (so far). Their speeds of approach (or recession!) are highly variable, no season or lunar phase is preferred, and so forth. The only certainty we have apart from this randomness is that they will be especially bright near opposition. The optimal search strategy for this situation is intuitivelv obvicus and rigorous calculations (Taff, 1984) verify that it can be improved upon by less than $10 \%$. Part and parcel of an efficient use of telescope time, photographic plates, human enthusiasm and fortitude, and so on is to search when the other constraints on the problem do not interfere. Thus, one should search near each New Moon and not in the Summer. June 23 and September 23 are equally unfavorable times of year except for a weather differential. Certainly Full Moons, July 15, and September 1 are to be avoided.

When are these minor planets actually found? Sixteen were found during the summer (effectivel.y one-quarter of the total of 60). Twenty-five were found outside of the optimum lunar phase range of $(0.33,0.67)$. While this is a lot closer to $1 / 3$ of the

Table III. Orbital Element Statistics

|  | Mean |  |
| :--- | :--- | :--- |
| Element | $1.90 \mathrm{A.U}$ | $0.55 \mathrm{~A} . \mathrm{U}$. |
| Semi-major axis | 0.489 | 0.163 |
| Eccentricity | $168^{\circ}$ | $101^{\circ}$ |
| Argument of perihelion | $17: 7$ | $14: 88$ |
| Inclination | $184^{\circ}$ | $96^{\circ}$ |

total thal it is to $2 / 3$ of it, seven of these were Summer events! Thus, thirty-four of sixty asteroids were found at most improbable times. Because we already know of the accidental discovery of at least three others (e.g., 1981ET3, l981VA, and 1982DB), it becomes increasingly clear that careful planning and the husbanding of resources have little to do with the discovery of these objects. Serendipity rules the skies.

We conclude that purposeful organized searches with current techniques (e.g., specifically with respect to search rates and limiting magnitude) have not had and will not have a high payoff in terms of discoveries. Sky coverage, awareness of the quarry, and very hard work will continue to yield unpredictably large numbers of discoveries if additional objects remain to be found.

Acknowledgements
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## Figure Captions

Eig. 1. Histogram of the number of Earth-approaching asteroidis as a function of topocentric angular speed at time of discovery.

Fig. 2. Same format as Fig. 1 for position angle of topocentric angular velocity.

Fig. 3. Same format as Fig. l for opposition distance.
Fig. 4. Same format as Eig. 1 for geocentric distance at time of discovery.

Fig. 5. Same format as Fig. 1 for heliocentric distance at time of discovery.

Fig. 6. Same format as Fig. 1 for lunar phase (New Monn $=0.5$ ) at time of discovery.

NO. OF EARTH-APPROACHING ASTEROIDS


NO. OF $\oplus$-APPROACHING ASTEROIDS


NUMBER OF EARTH-APTROACHING ASTEROIDS


Table 1. Data on Earth-approaching Asteroids

| Designation | Discovery Reference ${ }^{\text {a }}$ | Element Set Reference ${ }^{\text {a }}$ | Angular Speed ( $\% / d$ ) | Position <br> Angle ( ${ }^{\circ}$ ) | Lunar Phase | Heliocentic Distance (A.U.) | Geocentric Distance (A.U.) | Phase Angle( ${ }^{\circ}$ ) | Opposition Distance( ${ }^{\circ}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1963UA | 2308 | 3016 | 0.89: ${ }^{\text {b }}$ | 136: ${ }^{\text {b }}$ | 0.44 | 1.25 | 0.25 | 2.5 | 3.1 |
| 1968AA | 2845 | 3017 | 0.39: | 324: | 0.51 | 1.48 | 0.71 | 34.6 | 58.7 |
| 1971FA | 3895 | 3754 | 0.64 | 274 | 0.48 | 1.86 | 0.86 | 0.7 | 1.4 |
| 1971sc | 3299 | 5032 | 0.51 | 165 | 0.75 | 1.37 | 0.37 | 7.7 | 10.5 |
| 19710A | 3896 | 3755 | 1.08 | 223 | 0.76 | 1.36 | 0.37 | 1.9 | 2.5 |
| 1972RA | 3381 | 4659 | 0.77: | 130: | 0.46 | 1.23 | 0.22 | 4.6 | 5.6 |
| 1972RB | 3381 | 4659 | 1.23 | 108 | 0.76 | 1.14 | 0.13 | 4.7 | 5.3 |
| 1972XA | 3618 | 3756 | 1.44 | 324 | 0.50 | 1.18 | 0.23 | 29.8 | 36.5 |
| 1973EA | 3525 | 4010 | 1.20 | 282 | 0.57 | 1.29 | 0.41 | 35.1 | 50.1 |
| 1973EC | 3525 | 3899 | 0.80: | 150: | 0.80 | 1.14 | 0.23 | 47.2 | 57.0 |
| 1973NA | 3601 | 4659 | 11.90 | 206 | 0.62 | 1.11 | 0.09 | 14.6 | 16.0 |
| 1974 MA | 3712 | 4659 | 0.91 | 31 | 0.73. | 1.40 | 0.68 | 43.4 | 70.5 |
| 1974UB | 3813 | 3910 | 0.88: | 304: | 0.67 | 1.68 | 0.69 | 5.7 | 9.5 |
| 1975 TB | 5393 | 4541 | 2.43 | 210 | 0.40 | 1.13 | 0.16 | 32.9 | 37.9 |

Table I．Data on Earth－approaching Asこことoids（Cont＇d．）

| Desig－ nation | Discovery Reference ${ }^{\text {a }}$ | Element Set Referencea | Angular Speed（ ${ }^{\circ} / \mathrm{d}^{\prime}$ ） | Position Angle（ ${ }^{\circ}$ ） | Lunar Phase | ```Heliocentic Distance (A.U.)``` | Geocentric Distance （A．U．） | Phase Angle（ ${ }^{\circ}$ ） | Opposition Distance（ ${ }^{\circ}$ ） |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1975YA | 3918 | 3919 | 20.32 | 337 | 0． 29 | 1.02 | 0.05 | 40.2 | 42.0 |
| 1976AA | 3918 | 3919 | 2.51 | 328 | 0.67 | 1.11 | 0.13 | 7.1 | 8.0 |
| 1976 UA | 4395 | 4659 | 15.17 | 151 | 0.48 | 1.01 | 0.01 | 39.7 | 40.2 |
| 1976 WA | 4147 | 4660 | 0.58 | 14 | 0.41 | 1.36 | 0.61 | 41.8 | 66.3 |
| 1977HA | 4193 | 4660 | 0.62 | 103 | 0.45 | 1.13 | 0.17 | 40.1 | 46.4 |
| 1977 HB | 4193 | 4406 | 1.24 | 256 | 0.68 | 1.19 | 0.18 | 1.5 | 1.8 |
| 1977RA | 4392 | 4660 | 0．23： | 39： | 0.24 | 1.24 | 0.25 | 17.8 | 22.2 |
| 1977 VA | 4396 | 4660 | 0．83： | 100： | 0.42 | 1.13 | 0.14 | 5.0 | 5.7 |
| 1978CA | 4392 | 4660 | $0.60=$ | 352： | 0.51 | 1.20 | 0.28 | 36.2 | 45.9 |
| 1978DA | 4392 | 6827 | 0．77： | 79： | 0.81 | 1． 20 | 0.24 | 25.3 | 31.2 |
| 1978RA | 4496 | 4541 | 1.96 | 218 | 0.78 | 1.19 | 0.19 | 5.2 | 6.2 |
| 1978SB | 4569 | 4661 | 1．29： | 289： | 0.38 | 1． 32 | 0.33 | 15.3 | 20.3 |
| 1978VB2 | 4724 | －－ | －－ | －－ | 0.53 | －－ | －－ | －－ | －－ |
| 1979QA | 4904 | －－ | 1．59： | 280 ： | 0.48 | $\rightarrow$ | $\cdots$ | －－ | －－ |

Table I. Data on Earth-approaching Asteroids (Cont'd.)

| Designation | Discovery Reference ${ }^{\text {a }}$ | Element Set Reference ${ }^{\text {a }}$ | $\begin{gathered} \text { Angular } \\ \text { Speed }(\% / d) \end{gathered}$ | Position <br> Angle ( ${ }^{\circ}$ ) | Lunar <br> Phase | Heliocentic Distance (A.U.) | Geocentric Distance (A.U.) | Phase Angle( ${ }^{\circ}$ ) | Opposition Distance ${ }^{(0)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 19790B | 4904 | 5515 | 0.17 | 354 | 0.48 | 1.34 | 0.33 | 4.2 | 5.6 |
| 1979VA | 5120 | 5319 | 1.76 | 93 | 0.37 | 1.12 | 0.15 | 22.4 | 25.7 |
| 1979XA | 5121 | 5176 | 1.32 | 257 | 0.32 | 1.24 | 0.31 | 29.6 | 38.6 |
| 1979хв | 5120 | 5131 | 3.87 | 235 | 0.26 | 1.03 | 0.09 | 49.8 | 53.7 |
| 1980AA | 5138 | 5279 | 2.58: | 120: | 0.39 | 1.05 | 0.07 | 12.2 | 13.1 |
| 1980PA | 5514 | 5899 | 0.83 | 53 | 0.32 | 1.27 | 0.31 | 32.1 | 41.6 |
| 1980RB1 | 5594 | 5847 | 0.60 | 292 | 0.63 | 1.64 | 0.64 | 6.4 | 10.4 |
| 1980wF | 5669 | 5841 | 1.07 | 136 | 0.24 | 1.13 | 0.14 | 7.7 | 8.8 |
| 1930ys | 5827 | 5899 | 0.11 | 1 | 0.29 | 1.23 | 0.26 | 7.7 | 9.7 |
| 1981cw | 5886 | 5977 | 0.67 | 64 | 0.57 | 1.19 | 0.30 | 42.2 | 53.9 |
| 1981ET3 | 7093 | 7234 | 0.34 | 267 | 0.39 | 2.50 | 1.56 | 9.4 | 24.4 |
| 1981JD | 6036 | --- | 3.14 | 240 | 0.68 | -- | - | -- | - |
| 19810A | 6237 | 6702 | 0.91 | 127 | 0.21 | 1.19 | 0.20 | 26.3 | 31.4 |
| 19810B | 6254 | 6702 | 1.48 | 192 | 0.43 | 1.40 | 0.40 | 8.4 | 11.8 |

Table I. Data on Earth-approaching Asteroids (Cont'd.)

| Designation | Discovery Reference ${ }^{\text {a }}$ | Element Set Reference ${ }^{\text {a }}$ | Angular <br> Speed ( $\% / \mathrm{d}$ ) | Position Angle ( ${ }^{\circ}$ ) | Lunar <br> Phase | Heliocentic Distance (A.U.) | Geocentric Distance (A.U.) | Phase Angle( ${ }^{\circ}$ ) | Opposition Distance( ${ }^{\circ}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1981VA | 6481 | 6702 | 2.19 | 196 | 0.74 | 1.22 | 0.29 | 32.5 | 41.5 |
| 1982BB | 6674 | 6703 | 0.75 | 342 | 0.35 | 1.40 | 0.50 | 27.5 | 41.1 |
| 1982CA | 6769 | -- | 1.88: | 248: | 0.17 | -- | -- | - | -- |
| 1982DB | 6675 | 6831 | 0.74 | 282 | 0.68 | 1.06 | 0.11 | 47.7 | 52.3 |
| 1982dV | 6690 | 6831 | 0.73 | 128 | 0.67 | 1.20 | 0.26 | 31.6 | 39.5 |
| 1982EA | 6770 | -- | 0.65 | 266 | 0.78 | -- | - | -- | -- |
| 1982 FF | 6877 | 8538 | 1.07 | 211 | 0.66 | 1.31 | 0.36 | 26.3 | 35.5 |
| 1982HR | $3692{ }^{\text {a }}$ | 7840 | 2.49: | 264: | 0.54 | 1.05 | 0.06 | 38.4 | 40.4 |
| 1982RA | 7202 | 7602 | 1.70 | 334 | 0.33 | 1.24 | 0.32 | 37.4 | 48.5 |
| 1982RB | $3725^{\text {a }}$ | 7602 | 1.05 | 168 | 0.36 | 1.33 | 0.34 | 15.6 | 20.8 |
| 1982TA | 7342 | 8539 | 0.93 | 263 | 0.27 | 1.48 | 0.50 | 13.8 | 20.6 |
| 1982XB | 7563 | 7841 | 3.01 | 31 | 0.45 | 1.02 | 0.05 | 33.7 | 35.2 |
| 1982YA | $3758{ }^{\text {a }}$ | 8534 | 2.61: | 190: | 0.71 | 1.22 | 0.24 | 2.6 | 3.2 |
| 1983LB | 8014 | 2956 | 1.48 | 205 | 0.59 | 1.31 | 0.30 | 10.4 | 13.5 |

a References marked by this symbol refer to an I.A.U. Circulat. All others are MPC numbers.
b Colons indicate less certain values.

