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GAMMA-RAY BURSTER RECURRENCE TIMESCALES
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\section*{gAMMA-RAY BURSTER RECURRENCE TIMESCALES **}

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\section*{ABSTRACT}

Three optical transients have now been found (Schaefer 1981 and Schaefer et al. 1984) which are associated with gamma-ray bursters (GRBs). The deduced recurrence timescale for these optical transients ( \(\tau_{o p t}\) ) will depend on the minimum brightness for which a flash would be detected. We present a detailed analysis using all available data of \(\tau_{o p t}\) as a function of \(\varepsilon_{\gamma} / E_{o p t}\). For flashes similar to those found in the Harvard archives, the best estimate of \(T_{\text {opt }}\) is 0.74 years, with a \(99 \%\) confidence interval from 0.23 years to 4.7 years. It is currently unclear whether the optical transients from GRBs also give rise to gamma-ray events. One way to test this association is to measure the recurrence timescale of gamma-ray events ( \(\tau_{\gamma}\) ). We examine here a total of 210 gamma-ray error boxes and have found that the number of observed overlaps is not significantly different from the number expected from chance coincidence. This observation can be used to place limits on \(\tau_{\gamma}\) for an assumed luminosity function. We find that \(\tau_{\gamma} \geq 10 \mathrm{yr}\) if bursts are monoenergetic. However, if GRBs have a power law luminosity function with a wide dynamic range, then our limit is \(\tau_{\gamma} \geqslant 0.5 \mathrm{yr}\). Hence, the gamma-ray data do not require \(\tau_{\gamma}\) and \(\tau_{\text {opt }}\) to be different.
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\section*{I. INTRODUCTION}

In the decade since GRBs were discovered (Klebesadel, Strong, and 01 son 1973), many models have been proposed to explain the GRB phenomenon (Ruderman 1975). Part of the difficulty in distinguishing between the models is that they typically make few predictions which are either distinctive or verifiable. One of the few verifiable predictions of many models is the recurrence time scale, \(\tau_{\gamma}\). For example, some models (Woosley 1981) predict \(\tau^{\tau}{ }^{\sim} 1 \mathrm{yr}\), while some models (Colgate and Petschek 1981; Van Buren 1981; Michel 1984; and Hameury et al. 1982) predict \(\tau_{\gamma} \sim 10^{6} \mathrm{yr}\), and others (Zwicky 1974; Grindlay and Fazio 1974; Baan 1982; Teller and Johnson 1980; Brecher 1981) predict no recurrences a太 all.

Jennings and White (1981) have analyzed the \(\operatorname{LogN}(>S)\)-LogS curve and concluded that \(\tau_{\gamma}<10^{5} \mathrm{yr}\). Indeed, two GRBs have been observed (Mazets and Golenetskii 1982 and Golenetskii, Ilyinskii, and Mazets 1984) with \(\tau_{\gamma} \leqslant 1\) yr. One of these GRBS (GBSO520-66) is highly unusual for many reasons (Cline 1981), and may represent a separate class of GRBs. For this reason, the sixteen bursts from this source have been ignored in the analysis below.

One method to measure \(\tau_{\gamma}\) is to look for possible cases of recurrence as indicated by overlapping error boxes. Our analysis is composed of three procedures: (1) We have searched through known error regions for cases where the error regions overlap; (2) We have determined how many overlaps are expected by chance coincidence alone; and (3) We have calculated how many overlaps are expected due to recurrence for various assumed \(\tau_{\gamma}\) and luminosity functions.

\section*{II. GAMMA-RAY RECURRENCE TIMESCALE}

The 210 error regions which we used for procedure (1) were obtained from a variety of sources (Mazets et al. 1981; Klebesadel et al. 1982; Terrell et al. 1982; Nishimura et a1. 1978; Hueter 1983; Mazets 1983; Baity, Hueter, and Lingenfelter 1984; Ozel, Kiziloglu, and Tokdemir 1983; Ubertini et al. 1982; Strong, Klebesadel, and 01 son 1974; Sommer and Muller 1978; Katoh et al. 1984; Desai 1984; and Klebesadel et al. 1983). We found one case where ten error regions overlapped and several cases where nine error regions overlapped. We also found several cases where four thin (width \(<1^{\circ}\) ) annuli intersected. Roughly half of the 210 error regions are annuli on the sky derived from detections with only two spacecraft. Clearly, any two error regions with annulus shapes are quite likely to intersect. When all 210 error regions are considered, the number of annulus/annulus overlaps is much larger than the number of overlaps expected to be caused by recurrence for any \(\tau_{\gamma}>0.1\) yr . Therefore, we have searched a number of subsets of the 210 error regions for the subset which places the greatest restriction on \(\tau_{\gamma}\). We find the most restrictive subset is defined as consisting of those regions which subtend an area less than 200 square degrees and which entirely fit inside a circle of \(20^{\circ}\) radius. For bursts with two separated yet equally likely error regions, the later criterion was applied to each alternate area separately. For this subset of 89 error regions, the 37 overlaps which occur (fourteen double overlaps and three triple overlaps) are tabulated in Table 1.

A number of these overlaps, possibly all, are due to chance superposition of error regions from unrelated GRBs. Procedure (2) consists of calculating this number by means of a Monte Carlo analysis. In each of 100 Monte Carlo runs, the error regions are randomly scattered over the sky before the number of overlapping error regions is evaluated. For all subsets of error regions,

We find that the observed number of overlapping error regions is not significantly different from that expected from chance superposition alone. For example, the subset of 89 regions defined above has 37 overlaps whereas \(39.3 \pm 8.5\) are expected from coincidence. For the entire collection of 210 regions, several \(9 x\) overlaps and \(10 x\) overlaps are expected, as are a number of overlaps involving four or more thin annuli. These results indicate that the bulk of observed overlaps are not due to recurrence.

The number of expected overlaps caused by recurrence is model dependent. We have assumed that bursts from an individual GRB have a Poisson distribution in time with a mean of \(\tau_{\gamma}\). We assume (as has Jennings, 1982) that the number of bursts with a given gamma-ray energy \(n\left(E_{\gamma}\right)\), has a power law distribution;
\[
n\left(E_{\gamma}\right)=\frac{\alpha_{0} E_{\gamma}^{\alpha-1}}{E_{2}^{\alpha}\left(1-\zeta^{\alpha}\right)}, 0<E_{1} \leqslant E_{\gamma} \leqslant E_{2}, \zeta \equiv E_{1} / E_{2} .
\]

Note that as 5 approaches unity, the luminosity function becomes monoenergetic. Jennings \((1982,1984)\) finds that \(-1.5 \leqq \alpha \leqq 0\) and \(\zeta \leqq 0.04\) are consistent with the gamma-ray long \(N(>S)-l o g S\) observations. The sixteen bursts from GBS0520-66 (Golenetskii, Ilyinskii, and Mazets 1984) closely follow the power law luminosity function with \(\alpha \sim-0.4\) and \(\zeta \sim 10^{-3.5}\), although we remind the reader that these sixteen bursts are not used in the analysis in this paper. Belli (1984 and private commication) has demonstrated that \(\alpha \sim-2.5\) and \(\zeta \leqslant 10^{-3}\) for the population of bursts in the Konus catalogue (Mazets et al. 1981). We have evaluated our model for values of \(\alpha\) between 0.5 and -1.5 and for values of \(\zeta\) between 1 and \(10^{-7}\). Finally, we have assumed that the probability that a given burst will both be detected and be positioned is a function of the burst's fluence and date of occurrence. This probability was determined empirically by dividing the \(\log N(>S)-\log S\) curve for
the bursts included in the subset of error regions by the \(\operatorname{LogN}(>S)-\operatorname{LogS}\) curve for all bursts. A separate determination of the probability was made for each of five intervals of time since 1969 over which the probability is roughly constant (see Table 2).

With these assumptions, the expected number of observed recurrences can be calculated by means of a Monte Carlo analysis. For each trial run, a number of GRB distances, burst times, and burst luminosities are generated. Each burst is then determined to be "positioned" or "not positioned" based on the probability of positioning for a given date and fluence. The number of overlaps caused by recurrence can then be tallied by finding the number of multiple bursts from a given GRB which are positioned.

Allowance must be made for the possibility that error regions which are overlapping because of recurrence can also be overlapping with the error regions from other GRBs. To correct for this effect, the fraction of sky sovered by error regions must be known. Ninety-one percent of the sky is covered by our 210 total error regions, while only eight percent is covered by the subset of 89 regions.

The results of the Monte Carlo analysis are presented in Figure 1 and Table 3 for the subset of 89 error regions. The total number of expected overlaps (due to both recurrence and chance overlaps) is also presented. This number is to be compared to the 37 observed overlaps. It can be seen that a monoenergetic luminosity function ( \(\zeta=1\) ) is consistent with observation only if \(\tau_{\gamma} \geq 10 \mathrm{yr}\). However a luminosity function with a wide dynamic range \(\left(\zeta \ll 10^{-3}\right.\) ) is consistent with a recurrence timescale as short as 0.5 yr .
III. OPTICAL RECURRENCE IIMESCALE

Schaefer et al. (1984) have estimated that \(\tau_{\mathrm{opt}} \sim 1 \mathrm{yr}\). This estimate is based on the sum of exposure times of the archival plates examined. However, some of these plates are not sensitive enough to detect a flash which has a gamma-ray to optical energy ratio ( \(E_{\gamma} / E_{o p t}\) ) similar to those of the three detectea flashes (i.e., \(10^{3}\) ). The exposure times for these plates should not be used in calculating \(\tau_{\text {opt }}\) for bursts with \(E_{\gamma} / E_{o p t}=10^{3}\). Similarily, more sensitive plates can be used to limit \(\tau_{\text {opt }}\) for flashes with a larger maximum \(E_{\gamma} / E_{o p t}\). If estimates of \(\tau_{o p t}\) are stated as a function of \(E_{\gamma} / E_{o p t}\), then effects due to the differing GRB distances will be scaled out.

In Table 4, we have presented \(99 \%\) confidence limits on \(\tau_{\text {opt }}\) for flashes in a given range of \(E_{\gamma} / E_{\text {opt }}\). The data used in preparing Table 4 was compiled from a number of studies (Gehrels et a1. 1983; Schaefer, Seitzer, and Bradt 1983; Pedersen et al. 1983; and Schaefer et a1. 1984) in addition to the archival plate search (Schaefer 1984). In each of these studies, it is known how many hours of observations are capable of detecting a brief flash of any given optical fluence. With the measured \(E_{\gamma}\), the effective duration of observations can be stated as a function of \(E_{\gamma} / E_{o p t}\). In the second column of Table 4, the exposure for all bursters for the above mentioned studies were summed for each \(E_{\gamma} / E_{o p t}\) bin. Note that the limits on \(\tau_{o p t}\) are for the average of the \(\tau_{o p t}\) for each of the dozen or so GRB positions examined in these studies. For example, the best estimate for \(\tau_{o p t}\) for flashes with \(E_{\gamma} / E_{o p t} \sim 10^{3}\) is 0.74 yr (with a \(99 \%\) confidence interval of \(\left.0.23 \mathrm{yr}<\tau_{\mathrm{opt}}<4.7 \mathrm{yr}\right)\).

Table 4 was created with the assumption that the \(E_{\gamma}\) value of any burst from a given GRB would always be proportional to the fluence of one specific burst from that GRB reported by the instrument on board the Pioneer Venus spacecraft (Klebesadel et al. 1983). This assumption is valid only if GRBs
are monoenergetic. However, even if the assumption is false, the ratio of \(E_{\gamma}\) to \(E_{\text {opt }}\) still represents the best available means to construct a distance independent measure for comparing \(E_{\text {opt }}\).

\section*{IV. DISCUSSION}

We conclude that \(\tau_{\text {opt }}\) is consistent with the best current estimates of \(\tau_{Y}\) if \(\zeta \leqslant 10^{-3}\). Hence, we cannot yet answer such questions as: (1) Do the optical and gamma-ray events occur simultaneously on GRBs? (2) Is the archival \(E_{\gamma} / E_{\text {opt }}\) ratio a constant (cf. Schaefer et al. 1984)? (3) Is \(\tau_{\gamma}\) so small that many GRB models can be rejected?

GRB detectors onboard the recently launched Venera-13 and -14 satellites, as well as the continuously operating Solar Max, Pioneer Venus, and ICE instruments, āre expected to yield a number of new ganma-ray error regions. However, these new error regions are not likely to be greatly improved in either number or positional accuracy when compared to the earlier results that include Vemera-11 and -12 data (Mazets et al. 1981). In such a situation, the new observation may not greatly change our limit on \(\tau_{\gamma}\), because the models with \(5 \leqslant 10^{-3}\) will still predict that the number of recurrence caused overlaps will be comparable to or smaller than the uncertainty in the number of chance overlaps. The Gamma Ray Observatory (Fishman et al. 1984), however, is expected to produce several hundred error regions with an area of order 10 square degrees, and hence will yield a much stronger limitation on \({ }^{\tau_{\gamma}}\) than we present in this paper.

Acknowl edgements
We would like to thank Dr. U. D. Desai for supplying us with unpublished SMM data and other assistance. We also thank Dr. J. Norris for his help in initiating this project.

\section*{TABLE 1}

\section*{OBSERVED OVERLAPS OF GRB ERROR REGIONS}
\begin{tabular}{|c|c|c|c|c|}
\hline R.A. & \(\delta\) & \multicolumn{3}{|c|}{DATES OF OVERLAPPING BURSTS} \\
\hline \(117^{\circ}\) & -67 \({ }^{\circ}\) & 71/03/18 & 73/06/10 & 81/10/16 \\
\hline \(1.16^{\circ}\) & \(-63^{\circ}\) & 73/06/10 & 79/09/25 & \\
\hline \(99^{\circ}\) & \(-42^{\circ}\) & 78/03/30 & 79/08/26 & 79/10/14 \\
\hline \(294{ }^{\circ}\) & \(-40^{\circ}\) & 74/07/23 & 76/12/09 & \\
\hline \(338{ }^{\circ}\) & \(-32^{\circ}\) & 76/12/20 & 79/07/12 & \\
\hline \(33^{\circ}\) & \(-21^{\circ}\) & 78/10/25 & 79/07/28 & \\
\hline \(59^{\circ}\) & \(-13^{\circ}\) & 78/10/25 & 79/09/10 & \\
\hline \(94^{\circ}\) & \(-11^{\circ}\) & 76/08/16 & 79/04/12 & \\
\hline \(310^{\circ}\) & \(-8^{\circ}\) & 79/02/13 & 82/03/03 & \\
\hline \(164^{\circ}\) & \(0^{\circ}\) & 79/01/16 & 79/10/03 & \\
\hline \(287^{\circ}\) & \(5^{\circ}\) & 79/03/24 & 79/03/25 & 79/03/27 \\
\hline \(68^{\circ}\) & \(8^{\circ}\) & 71/03/18 & 73/06/10 & \\
\hline \(106^{\circ}\) & \(8^{\circ}\) & 76/01/28 & 77/07/08 & \\
\hline \(92^{\circ}\) & \(15^{\circ}\) & 77/07/08 & 79/10/06 & \\
\hline \(227^{\circ}\) & \(32^{\circ}\) & 78/09/18 & 78/10/19 & \\
\hline \(57^{\circ}\) & \(54^{\circ}\) & 73/03/02 & 79/11/15 & \\
\hline \(190^{\circ}\) & \(79^{\circ}\) & 72/05/14 & 79/10/16 & \\
\hline
\end{tabular}

\section*{TABLE 2}

PROBABILITY OF POSITIONING A GRB
\begin{tabular}{|c|c|c|c|c|c|}
\hline \(\operatorname{logS}\) & \[
\begin{aligned}
& 1969.6 \text { to } \\
& 1973.6
\end{aligned}
\] & \[
\begin{aligned}
& 1973.6 \text { to } \\
& 1976.0
\end{aligned}
\] & \[
\begin{aligned}
& 1976.0 \text { to } \\
& 1978.7
\end{aligned}
\] & \[
\begin{aligned}
& 1978.7 \text { to } \\
& 1980.1
\end{aligned}
\] & \[
\begin{aligned}
& 1980.1 \text { to } \\
& 1982.3
\end{aligned}
\] \\
\hline \(\underline{\underline{l o g}}\) & \(\underline{ }\) & \(\underline{1976.0}\) & \(\underline{ }\) & & \\
\hline >-3.5 & 0.50 & 0.40 & 0.50 & 1.0 & 0.50 \\
\hline -4.0 to -3.5 & 0.50 & 0.20 & 0.50 & 1.0 & 0.25 \\
\hline -4.5 to -4.0 & 0.11 & \(0.0^{\text {a }}\) & 0.10 & 1.0 & \(0.0^{\text {a }}\) \\
\hline -5.0 to -4.5 & \(0.0{ }^{\text {a }}\) & \(0.0{ }^{\text {a }}\) & 0.018 & 0.37 & 0.012 \\
\hline -5.5 to -5.0 & 0.0017 & 0.003 & 0.0025 & 0.067 & \(0.0^{\text {a }}\) \\
\hline -6.0 to -5.5 & \(0.0^{\text {a }}\) & \(0.0{ }^{\text {a }}\) & 0.0025 & 0.014 & \(0.0{ }^{\text {a }}\) \\
\hline <-6.0 & \(0.0{ }^{\text {a }}\) & \(0.0{ }^{\text {a }}\) & \(0.0{ }^{\text {a }}\) & 0.0020 & 0.0013 \\
\hline
\end{tabular}
a A zero probability merely means that no bursts with positional information were observed inside the indicated time and fluence bin.

TABLE 3

\section*{PREDICTED NUMBER OF OVERLAPS}
\begin{tabular}{|c|c|c|c|c|}
\hline \(\underline{\tau_{\gamma}(y r)}\) & \(\alpha\) & \(\zeta\) & Overlaps from Recurrence & Total Overlaps \({ }^{\text {a }}\) \\
\hline 1.0 & -- & 1 & \(44.3 \pm 13.9\) & \(83.6 \pm 16.3\) \\
\hline 5.0 & -- & 1 & \(23.7 \pm 7.7\) & \(63.0 \pm 11.5\) \\
\hline 10.0 & -- & 1 & \(13.3 \pm 4.7\) & \(52.6 \pm 9.7\) \\
\hline 15.0 & -- & 1 & \(7.5 \pm 3.7\) & \(46.8 \pm 9.3\) \\
\hline 20.0 & -- & 1 & \(6.1 \pm 2.6\) & \(45.4 \pm 8.9\) \\
\hline 1.0 & -0.5 & \(10^{-4}\) & \(5.5 \pm 1.2\) & \(44.8 \pm 8.6\) \\
\hline 0.5 & -0.5 & \(10^{-4}\) & \(9.9 \pm 2.2\) & \(49.2 \pm 8.8\) \\
\hline 10.0 & -0.5 & \(10^{-4}\) & \(3.1 \pm 2.2\) & \(42.4 \pm 8.8\) \\
\hline 1.0 & \(-1.0\) & \(10^{-4}\) & \(2.6 \pm 0.9\) & \(41.9 \pm 8.5\) \\
\hline 1.0 & 0.0 & \(10^{-4}\) & \(21.6 \pm 5.3\) & \(60.9 \pm 10.0\) \\
\hline 1.0 & -0.5 & \(10^{-3}\) & \(12.4 \pm 4.6\) & \(51.7 \pm 9.7\) \\
\hline 1.0 & -0.5 & \(10^{-5}\) & \(4.3 \pm 1.8\) & \(43.6 \pm 8.7\) \\
\hline
\end{tabular}
a The model predictions in this column are to be compared with the observed number of 37 overlaps.

TABLE 4

\section*{OPTICAL RECURRENCE TIME SCALE}
\begin{tabular}{|c|c|c|c|}
\hline \(\log \left(E_{\gamma} / E_{\text {opt }}\right)\) & \begin{tabular}{l}
Observing \\
Time (hr)
\end{tabular} & Number Flashes Observed & \begin{tabular}{l}
\(99 \%\) conf. \\
limit on \\
\(\tau_{\text {opt }}(y r)^{a}\)
\end{tabular} \\
\hline 1.75 to 2.25 & 28300 & 0 & > 0.70 \\
\hline 2.25 to 2.75 & 24400 & 0 & \(>0.61\) \\
\hline 2.75 to 3.25 & 19500 & 3 & > \(0.23,<4.7\) \\
\hline 3.25 to 3.75 & 12000 & 0 & \(>0.30\) \\
\hline 3.75 to 4.25 & 5680 & 0 & > 0.14 \\
\hline 4.25 to 4.75 & 2040 & 0 & \(>0.051\) \\
\hline 4.75 to 5.25 & 650 & 0 & \(>0.016\) \\
\hline 5.25 to 5.75 & 176 & 0 & > 0.0044 \\
\hline 5.75 to 6.25 & 46.0 & 0 & > 0.0011 \\
\hline 6.25 to 5.75 & 44.3 & 0 & \(>0.0011\) \\
\hline 6.75 to 7.25 & 38.4 & 0 & \(>0.00095\) \\
\hline 7.25 to 7.75 & 8.2 & 0 & \(>0.00020\) \\
\hline
\end{tabular}
a For Poisson statistics, if zero events are observed, then there is a \(99 \%\) probability that the average number of events observable for identical experiments is less than 4.6. Similarly, if tirree events are observed, then there is a \(99 \%\) prabability that the meari will be between 0.47 and 9.5 .

\section*{REFERENCES}

Baan, W. A. 1982, Ap. J. (Letters), 261, L67.
Baity, W. A., Hueter, G. J., and Lingenfelter, R. E. 1984, in "High Energy Transients in Astrophysics", ed. S. E. Woosley (New York: Am. Inst. Physics), p. 434.

Belli, B. M. 1984, in "High Energy Transients in Astrophysics", ed. S. E. Woosley (New York: Am. Inst. Physics), p. 42f.

Brecher, K. 1981, in "Gamna Ray Transients and Related Astrophysical
Phenomena", eds. R. E. Lingenfelter, H. S. Hudson, and D. M. Worrall (New York: Am. Inst. Physics), p. 293.

Cline, T. L. 1981, in "Gamma-Ray Transients and Related Astrophysical Phenomena", eds. R. E. Lingenfelter, H. S. Hudson, and D. M. Worrall (New York: Am. Inst. Physics), p. 17.

Colgate, S. A. and Petschek, A. G. 1981, Afy. Js, 248, 771.
Desai, U. D. 1094, private communication.
Fishman, G. J., Meegan, C. A., Parnell, T. A., Wilson, R. B., and Paciesas, W. 1984, in "High Energy Transients in Astrophysics", ed. S. E. Woosley (New York: Am. Inst. Physics), p. 651.

Gehrels, N., McMillan, R. S., Gehrels, T., Scotti, J. V., and Frecker, J. E. 1983, Bull. Am. Astr. Soc., 15, 939.

Golenetskii, S. V., Ilyinskii, V. N., and Mazets, E. P. 1984, Nature, 307, 41, Grindlay, J. E. and Fazio, G. G. 1974, Ap. J. (Letters), 187, L93.

Hameury, J. M., Bonazzola, S., Heyvaerts, J., and Ventura, J. 1982, Astr. Ap.; 111, 242.

Hueter, G. J. 1983, private communication.
Jennings, M. C. 1982, Ap. J., 258, 110.

Jennings, M. C. 1984, in "High Energy Transients in Astrophysics", ed. S. E. Woosley, (New York: Am. Inst. Physics), p. 412.

Jennings, M. C. and White, R. S. 1981, Ap. J., 238, 110.
Katoh, M., Murakami, T., Nishimura, J., Yamagami, T., Fujii, M., and Itoh, M. 1984, in "High Energy Transients in Astrophysics", ed. S. Woosley (New York: Am. Inst. Physics), p. 390.

Klebesadel, R. W., Strong, I. B. and 01 son, R. A. 1973, Ap. J. (Letters), 182, L85.

Klebesadel, R. W., et al. 1982, Ap. J., 254, 279.
Klebesadel, R. W., Evans, W. D., Fenimore, E. E., and Laros, J. G. 1983, Ap. J., submitted.

Mazets, E. P. et al. 1981, Ap. Space Sci., 80, 3.
Mazets, E. P. and Golenetskif, S. V. 1982, Ap. Space Sci., 88, 247.
Mazets, E. P. 1983, private communication.
Miche1, F. C. 1984, Ap. J., accepted.
Nishimura, J. et al. 1978, Nature, 272, 337.
Oze1, M. E., Kiziloglu, U., and Tokdemir, F. 1983, Astr. Ap., 118, 114.
Pedersen, H., et al. 1983, AD. J. (Letters), 270, L43.
Ruderman, M. 1975, Ann. N.Y. Acad. Sci., 262, 164.
Schaefer, B. E. 1981, Nature, 294, 722.
Schaefer, B. E. 1984, A. J., submitted.
Schaefer, B. F. et al. 1984, Ap. J. (Letters), accepted.
Schaefer, B. E., Seitzer, P., and Bradt, H. V., 1983, Ap. J. (Letters), 270, L49.

Schaefer, B. E., Vanderspek, R., Bradt, H. V., and Ricker, G. R. 1984, Ap. J., accepted.

Somner, M., and Muller, D. 1978, Ap. J. (Letters), 222, L17.

Strony, I. B., Klebesadel, R. W., and 01son, R. A. 1974, Ap. J. (Letters), 188, L1.

Teller, E. and Johnson, M. 1980, preprint.
Terrell, J., Fenimore, E. E., Klebesadel, R. W., and Desai, U. D., 1982, Ap. J., 254, 279.

Ubertini, P. et al., 1982, in "Accreting Neutron Stars", eds. W. Brinkmann and J. Trumper (Max-Planck-Institut, Garching), p. 223.

VanBuren, C. 1981, Ap. J., 249, 297.
Woosley, S. E. 1981, in "Gamma-Ray Transients and Related Astrophysical
Phenomena". eds. R. E. Lingenfelter, H. S. Hudson, and D. M. Worrall (New York: Am. Inst. Physics), p, 273.

Zwicky, F. 1974, Ap. Space Sci., 28, 111.

\section*{FIGURES}

Figure 1. Piedictions of Overlaps Due to Recurrence.
This figure shows a contour plot of the number of overlaps caused by recurrence which should be observed for the subset of 89 error regions. The model predictions are given as a function of the \(\alpha\) and \(\zeta\) parameters in the luminosity function. A monoenergetic luminosity function occurs when 5 equals unity. One of this paper's conclusions is that the majority of observed overlaps are due solely to chance coincidence. In this case, the number of recurrence overlaps must be small compared to the uncertainty in the number of chance overlaps. The diagram indicates that \(\tau_{\gamma}=1 \mathrm{yr}\) is acceptable if the luminosity function has \(\alpha<-0.3\) and \(\zeta<10^{-3}\).
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Figure 1```

