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Section 1

SUMMARY

The need for a computer program to perform kinematic and dynamic analyses of large truss structures while deploying from a packaged configuration in space led to the evaluation of several existing programs. ADAMS (Automatic Dynamic Analysis of Mechanical Systems), a generalized program for performing the dynamic simulation of mechanical systems undergoing large displacements, is applied to two concepts of deployable space antenna units. One concept is a one-cube folding unit of Martin Marietta's Box Truss Antenna and the other is a tetrahedral truss unit of a Tetrahedral Truss Antenna.

The purpose of this report is to describe the ADAMS program and discuss the problems and results of its application. In addition, a supplementary method for estimating surface member bending stresses at latch-up is described. Realistic surface member latch-up forces cannot be produced by the present version of ADAMS as it is limited to the assembly of rigid bodies. Future versions should solve this problem with a flexible body code. Results in this report include member displacement and velocity responses during extension and an example of member bending stress at latch-up.

INTRODUCTION

The concept of deploying antenna truss structures in space from packaged configurations as opposed to the erection of such structures by assembling the parts while in space requires the capability to perform kinematic and dynamic analyses of mechanical systems composed of many parts. A search for existing programs which might be evaluated for this purpose revealed several programs. of these, ADAMS (Automatic Dynamic Analysis of Mechanical Systems) (ref. 1) showed the most promise. Application of this program to the dynamic simulation of the deployment of two space antenna units is discussed in this report. A unit can be viewed as one of many bullding blocks which form an antenna. One concept is a one-cube folding unit of Martin Marietta's Box Truss Antenna (ref. 2) and the other is a tetrahedral folding unit of a Tetrahedral Truss Antenna (ref. 3). Simulation was accomplished on the VAX 11/780 computer through the time-sharing services of Mechanical Dynamics, Inc. (MDI), Ann Arbor, Michigan.

Other programs were considered for application. IMP (Integrated Mechanisms Program) was developed at the University of Wisconsin and is now available through General Electric CAE International, Inc. DADS (Dynamic Analysis and Design Systems) was developed at the University of Iowa. This program has only recently become commercially available. The rigid body code can now be purchased from Computer Aided Design Software, Inc., Dakdale, Iowa. Flexible body code should be available in the year 1986. DISCOS (Dynamic Interaction Simulation of Controls and Structures) developed by Martin Marietta Corporation under the auspices of NASA Goddard Space Flight Center, is a program designed for mechanical systems with flexible bodies. This program has the reputation for heing rather unwieldy to use, especially for systems with many parts. Available documentation was difficult to translate to application. SNAP (no acronym) is a proprietary program developed by General Dynamics, Corp., Convair Division, San Diego, California, for their Geo-Truss Antenna and is, therefore, not available.

The ADAMS program is described in Section 3. It was chosen for application primarily based on the strong position that the developer, MDI, has in the commerclal market and the avallability of user documentation, training classes, consultation services, and time-sharing facilities. The present version is limited to assembly of rıgid bodies which seriously limits member force analysis. There is a need to determine dynamic forces in the folding members when they latch-up to the extended position. This capability should become available when MDI completes the flexibility code in 1986. In the interim, however, estimates of surface member bending stresses at latch-up can be made by considering the surface member flexibility and kinetic enerqy in a separate analysis. A method such as this is descrihed in Section 4.

Results of the dynamic simulations during extension are limited to the displacement and velocity responses of the box truss unit and to the displacement response of the tetrahedral truss unit. A discussion of the input procedures, modeling problems, and output results for each antenna unit is given in Sections 5 and 6.

ADAMS, developed by Mechanical Dynamics Inc. (MDI), is a three-dimensional program which determines the time response of contiguous rigid bodies undergoing larqe displacements. Two bodies are contiquous if they are in actual contact by virtue of a force as with various forms of joints. The joint type specifies the number of constraints between the two bodies. A string of hodies may he connected so as to form closed loops, open loops or no loops.

There are five separate analysis modes in the ADAMS program (ref. 1):

1) Kineto-static
2) Static Equilibrium
3) Dynamic (Stıff Integration)
4) Dynamic (Non-Stiff Integration)
5) Quasistatic

The term kineto-static (ref. 4) is an expression used by MDI which is synonymous with the strict definition of the term, kinematic, as opposed to the often imprecise connotation referring to any system undergoing large qeometric changes. This mode of analysis is applicahle only to zero degree of freedom systems containing generators. In general, motion generators acting on a translational or revolute joint cause the system motion from which related displacements, velocities, accelerations, and forces are solved. It is an algebraic solution and no differential equations are solved. Therefore, this mode of analysis is not only faster but also more accurate than the dynamic mode.

The static equilibrium analysis is applicable to all mechanical systems having non-negative degrees of freedom. ADAMS will try to determine the configuration of the system where the system forces are in equilibrium at zero velocity and acceleration.

To perform a dynamic or transient analysis, the system must have degrees of freedom greater than zero. The analysis, descrihed in ref. 4 and 5 , involves the
simultaneous solution of differential equations with specified constraints. Fifteen first-order differential equations generated for each part are derived by combining the second order differential equations of motion and algebraic constraint equations with the addition of Lagrange multipliers. The Lagrange multipliers enable a solution of constraint (joint reaction) forces. The typical differential equations to be solved will be "stiff" and are therefore assumed by default. A stiff system is one with widely separated eigenvalues and the Gear algorithm is used for integration. The Adams-Moulton algorithm is used for a nonstiff integration. Both algorithms use a predictor-corrector procedure with variable order and variable step size.

For those problems where there is no interest in the temporal variation of variables such as displacement or velocity, the system should be simulated in the quasistatic mode. It is essentially a sequence of static equilibrium analyses performed on the system at different points in time. An example is the determination of the angle of a tilt tahle test stand at which it becomes unstable and tips over.

The Grubler mobility criterion (ref. 6) is an essential, but not necessarily sufficient method for determining the three-dimensional system degrees of freedom during assembly. The criterion as applied to the ADAMS program is written in the following form:

$$
\text { DOF }=6^{\star}(\text { PARTS }-1)-5^{\star}(\text { TRA }+R E V)-4^{\star}(C Y L+U N I)-3^{\star}(S P H+P L A)-1^{\star}(G E N+R A C K+S C R E W+U M C O N)
$$

where TRA, REV, etc. each equal an appropriate degree of freedom. The RACK and SCREW joints as well as the generator (GEN) and user written marker constraints (UMCON) are considered to each have a single constraint (ref. 1). When the DOF is less than zero, the system has no mobility and is a structure which causes ADAMS to halt execution. When DOF is zero, a kineto-static solution with system generators is assumed. When DOF is greater than zero, a force responsed dynamic simulation is assumed.

Input statements construct a model in ADAMS composed of parts, markers, joints, forces, generators, system parameters, and graphic elements. Output requests, necessary output control statements and other special features described in ref. 1 are also included in the input. The part statement must specify the part
center of mass, marker identification number, and mass moments of inertia. The parts are referenced by markers which specify initial locations and orientations. A marker is a point and an orthogonal triad of unit vectors forming a local coordinate system fixed with respect to the part. It is also used to define joints, forces and for graphic display. Standard forces are either constant or vary linearly but non-linear forces can be described by writing a function subprogram.

Eight types of joints are accepted by ADAMS. They are in order of degrees of freedom: revolute (1), translational (1), screw (1), rack-and-pinion (1), cylindrical (2), universal (2), spherical (3), and planar (3). As mentioned before, the screw and rack-and-pinion are considered single constraint joints. Initial displacements and velocities can be specified on the revolute and translational joints through the part statements.

Only the dynamic analysis mode (stiff integration) is illustrated in this report, although five static analyses were performed on the tetradehral truss unit to fold the unit into a position to begin the dynamic simulation of its deployment. The simulations are initiated by a "transient" command after which ADAMS displays the current value of time as TBEGIN and requests the final time (TEND) and the number of output steps (NSTEPS). Requested output is printer at intervals equal to (TEND-TBEGIN)/NSTEPS.

## Section 4

## MEMBER LATCH-UP RENDING STRESSES

The bending moments in the unfolding members as they latch-up into the extended position are the most significant dynamic member forces during the deployment condition. The lack of a flexible body code for computing these forces requires an alternate method. The following presents a method for estimating the member bending stresses at latch-up.

A free body of the member after latch-up is shown as follows:


The member is assumed a simple beam with constant cross-section, pinned at each end and vibrating after latch-up in the first bending mode. Rigid body kinetic energy at latch-up is assumed to transfer to bending strain energy at maximum deflection. Reference 7, in the chapter for energy methods, gives the following expression for energy in a vibrating simple beam:

$$
\begin{equation*}
K E=\frac{W}{2 g} \omega^{2} \int_{0}^{\ell} y^{2} d x \tag{1}
\end{equation*}
$$

where

```
KE = kinetic energy
w = weight/unit length
g = acceleration of gravity
\omega}=\mathrm{ fundamental frequency, radians/sec
y = mode shape function = a sin }\Pix/
\ell = beam length
```

Substituting the mode shape, a half sine wave, integrating and solving for the maximum deflection gives,

$$
\begin{equation*}
a=\frac{2}{\omega} \sqrt{\frac{(K E) g}{\omega \ell}} \tag{2}
\end{equation*}
$$

The fundamental frequency (ref. 7) for a simple beam is:

$$
\begin{equation*}
\omega=\pi^{2} \sqrt{\frac{E I g}{w \ell^{4}}} \tag{3}
\end{equation*}
$$

where

$$
\begin{aligned}
& E=\text { modulus of elasticity } \\
& I=\text { beam section area moment of inertia }
\end{aligned}
$$

Substituting Equation (3) in Equation (2) gives the beam deflection,

$$
\begin{equation*}
a=\frac{2}{\Pi^{2}} \sqrt{\frac{(K E) \ell^{3}}{E I}} \tag{4}
\end{equation*}
$$

With this deflection, the bending moment and stress can be obtained. Ideally, the inertial load distribution is in the form of a half sine wave, hut the assumption of a uniformly distributed load gives excellent results. The standard equations for deflection and bending moment (ref. 8), respectively, are:

$$
\begin{align*}
& a=\frac{5 w \ell^{4}}{384 E I}  \tag{5}\\
& M=\frac{W \ell^{2}}{8} \tag{6}
\end{align*}
$$

Substituting Equations (5) and (6) in Equation (4), and solving for $M$ gives,

$$
\begin{equation*}
M=1.95 \sqrt{\frac{(\mathrm{KE}) E I}{\ell}} \tag{7}
\end{equation*}
$$

For a thin circular section the heam moment of inertia (I) and section modulus(S), respectively, are $\Pi R^{3} t$ and $\pi R^{2} t$. Substituting these expressions and Equation (7) in the standard formula, $f b=M / S$, the bending stress is:

$$
\begin{equation*}
\mathrm{fb}=1.95 \sqrt{\frac{(\mathrm{KE}) \mathrm{E}}{\mathrm{H} \mathrm{\ell Rt}}} \tag{8}
\end{equation*}
$$

where

```
R = tube radius
t = tube thickness
```

Accuracy of this method depends on the accuracy of the kinetic energy. If there are significant energy losses before latch-up which cannot be neglected, the kinetic energy can be determined from the velocities of the significant masses at latch-up or the values of the losses must be at least estimated and subtracted from the potential energy. Assuming small losses, the energy can be based on the work done by the deployment forces. If significant, the deployment force would include, for example, the known frictional forces. It is assumed that the deployment forces are confined to each unit with little energy transfer to adjacent units. For example, the box truss and tetrahedral truss surface members are assumed to unfold by a lınear spring (see Section 5) over an angle of approximately 180 degrees. Without losses, a conservative assumption, the energy is then equal to 168 in $1 \mathrm{~b}-$ the area under the torque profile curve. In the case of the box truss unit, the latch-up bending stress from Equation (8) is $12,700 \mathrm{lb} / \mathrm{in}^{2}$. This is hased on a graphite/epoxy tubular member with $E=20 \times 10^{6} \mathrm{ib} / \mathrm{in}^{2}, \mathrm{R}=1.64 \mathrm{in}, \mathrm{t}=.026 \mathrm{in}$ and $\ell=590.56$ in and is a comfortably low stress for the material.

## BOX TRUSS UNIT

Figure $1(a)$ shows the stowed antenna after removal from the Orbiter. As indicated, the 15 meter box truss units are extended one row at a time progressing along the feed mast and then along the reflector until fully deployed as shown in figure 1(b).

The diagonals in each frame are cords composed of individual graphite/epoxy strands. Since the diagonals in a frame are not tensioned until the frame is fully extended, they are not included in the model shown in figure 2 and are assumed to have negligible influence on the deployment other than the fact that as the diagonals are tensioned near the full extension position, some kinetic energy will be absorbed.

Figure 2 shows the model of the box truss surface member. The numbers in squares are part numbers. On of the two superimposed reference frames is the global or ground reference frame and the other is the part reference frame and both are superimposed by default when the vector, $O G$, locating the part reference frame is omitted from the part statement.

Joint friction is assumed to be zero. All members are considered to be rigid bodies. Assuming all frames in a row will extend at the same rate, only one frame need be analyzed. By symmetry, the frame model can be reduced to one surface member (parts 3 and 4) and two dummy parts (parts 2 and 5) to constrain the motion of points 2 and 4 as they would be constrained with the full frame model. In addition, the dummy members represent the concentrated adjacent antenna masses.

The geometry for the model of the box truss unit in the folded position is given in table 1. Included are comments defining each type of joint. This is a two-dimensional problem being solved in a three-dimensional program, so a spherical joint was chosen for point 3 to provide sufficient degrees of freedom for a forced response simulation. A revolute joint would have caused the model to be overconstrained. Had the problem been solved with the two-dimensional program, DRAM (Dynamic Response of Articulated Machinery) discussed in ref. 5, a revolute joint
could have been used. The mass and mass moments of inertia for the components are given in table 2. Note that the model is slightly open in the folded position. Table 3 is the input file. In the first attempt to run the problem, the initial position of the model was such that points $?$ and 4 were coincident with point 6. Though this simplified input preparation and allowed an even 90 degrees of motion, ADAMS halted execution, and the output indicated a singular matrix. A slightly open position was tried and execution was successful as shown in tables 4 through 6.

Energy for deployment is assumed to be stored in a linear torsion spring in the joint at point 3 with a torque profile having a maximum torque of 80 in-lbs in the folded position to 27 in-lbs in the extended position acting over an angle of 180 degrees. This is input into the program with the force statement shown in the input file, table 3, after calculating by hand the parameters, KT and A. The keyword for this force is GTOROUE (GT) and is linearly dependent on the relative rotation and relative angular velocity (if damping is present) of the part markers. The torque equation is:

$$
T=-C T(d \alpha / d t)-K T(\alpha-A)+T^{\prime}
$$

where

```
T = torque exerted on part 3 marker by part 4 marker (in-1b) (positive in a
        counterclockwise sense).
CT = viscous damping coefficient (in-lb/rad/sec).
-KT = torsional spring constant (in-lb/degree).
A = angle of spring under zero load (degrees)
T' = torque of constant magnitude.
\alpha = relative angle between markers not to exceed 180 degrees.
```

The variables, $T, a$ and $d \alpha / d t$ are computed automatically by ADAMS.

The sensor statement in the input file causes the computations to halt when the parts are horizontal and the truss unit is fully extended. At this time, the relative angle between markers 0303 and 0403 is 178 degrees with an error of 1 degree. Note the output comments at the bottom of table 4 giving the time of 89.55 seconds at which this event occurred.

The output for request number 1 is in table 5. The request was for the relative displacement between marker 0303 and marker 0106 . Marker 0303 is located on part 3 at point 2 and marker 0106 is located on part 1 , the ground, at point 6 . This output shows the magnitude of the position vector varying from the initial value of 5 to the maximum value, the part length.

Request number 3 (REO/3) shown in table 3 asks for the relative velocity between the marker 0202 located on part 2 at point 2 and marker 0302 located on part 3 at point 2. The output shown in table 6 shows both the relative translational and angular velocities. Since the two marker origins are located in the same revolute joint, the small values of translational velocity are due to numerical error. The maximum angular velocity is shown to be . 65 radians $/ \mathrm{sec}$.

Figures 3, 4 and 5 show the position of the two surface member parts at times $0.0,85$ and 89.55 seconds, respectively. In figures 4 and 5, the display exceeds the graphic field on two views, but clearly show the symmetrical displacement of points 2 and 4 as it should be with equal masses at these points.

## TETRAHEDRAL TRUSS UNIT

Figure 1(a) shows the stowed antenna after removal from the Orbiter. As indicated, the 15 meter box truss units are extended one row at a time progressing along the feed mast and then along the reflector until fully deployed as shown in figure 1(b).

The diagonals in each frame are cords composed of individual graphite/epoxy strands. Since the diagonals in a frame are not tensioned until the frame is fully extended, they are not included in the model shown in figure 2 and are assumed to have negligible influence on the deployment other than the fact that as the diagonals are tensioned near the full extension position, some kinetic energy will be absorbed.

Figure 2 shows the model of the box truss surface member. The numbers in squares are part numbers. On of the two superimposed reference frames is the global or ground reference frame and the other is the part reference frame and both are superimposed by default when the vector, $0 G$, locating the part reference frame is omitted from the part statement.

Joint friction is assumed to be zero. All members are considered to be rigid bodies. Assuming all frames in a row will extend at the same rate, only one frame need be analyzed. By symmetry, the frame model can be reduced to one surface member (parts 3 and 4) and two dummy parts (parts 2 and 5) to constrain the motion of points 2 and 4 as they would be constrained with the full frame model. In addition, the dummy members represent the concentrated adjacent antenna masses.

The geometry for the model of the box truss unit in the folded position is given in table 1. Included are comments defining each type of joint. This is a two-dimensional problem being solved in a three-dimensional program, so a spherical joint was chosen for point 3 to provide sufficient degrees of freedom for a forced response simulation. A revolute joint would have caused the model to be overconstrained. Had the problem been solved with the two-dimensional program, DRAM (Dynamic Response of Articulated Machinery) discussed in ref. 5, a revolute joint
positions served the same purpose - to attach the model to ground. Components of the acceleration of gravity were set to zero in the system statement (table 11) as in a space environment, but the attachment to ground is still required during the static equilibrium solution.

Tables 9,10 , and 11 are the command file, the function subprogram, and the input file, respectively. Note that all statements in the input file which are indented five or more spaces to the right are in effect deleted as they are not interpreted as data cards. These statements could have been edited from the file but were left there for the record. The command file resets the three knee-joint torques, 90607, 90910, and 91213 so that the static equilibrium commands will fold the truss to the desired position. After this, the torque parameters are reset back to the values shown in the input file. Note that the parameters, $A$ and $T^{\prime}$ in the force statements are equal to zero and -27 , respectively. The torque profiles are the same as used for the box truss unit but with opposite sign. This is necessary, since the markers are oriented differently. Following this, the ground to upper fitting torques, 1427, 1497, and 1498 (ref. tables 9 and 11) are reset with zero spring rates which in effect disconnects the ground to fitting torque constraints. Translational separation from ground to fitting is automatic at time greater than zero by the function subprogram. The next six commands cause the calculated forces to be printed. The final command, TRAN, causes computation of the dynamic simulation for 3 seconds with 90 steps.

The function subprogram (table 10) computes the forces (FSUR) for the corresponding forces 1426,1428 , and 1429 acting between the upper fitting and ground (see figures 6 and 7 and table 11) during static equilibrium when the time is equal to zero. It also computes the damping torques (TSUR) for the corresponding forces, 80607 , 80913, and 81213 acting in the knee-joints during the dynamic simulation when the time is, of course, greater than zero and when PHI is less than or equal to 10 degrees. Referring to table 10 in $\operatorname{FSUR}, \operatorname{APAR}(1), \operatorname{APAR}(2)$, and $\operatorname{APAR}(3)$ are the $x, y$, and $z$ relative displacements, respectively, of marker $I$ and marker $J$ defined in each force statement. $\operatorname{PAR}(1)$ is a spring rate equal to $100 \mathrm{lbs} / \mathrm{in}$ (from table ll). For TSUB, PAR(l) is equal to 10 degrees and is also obtained from the corresponding force statement in tahle ll. ADAMS converts this angle to radians. PHI , in radians, is the angle between the x-axes of marker $I$ relative to marker J. DPHI, in radians/second, is the corresponding angular velocity. $\operatorname{PAR}(2)$ and $\operatorname{PAR}(3)$ are viscous damping coefficients equal to 1,000 in-lb/rad/sec.

The purpose of the additional torques from TSUB is to provide heavy damping in the knee-joints to brake the angular motion to a quick stop at the fully deployed position. This method was designed by the MDI consultant, who resolved the modeling problem discussed earlier. The advantage of this method over the use of a sensor (see box truss unit discussion) is that computations can continue past the latch-up time ( 1.7 sec ) up to the specified limit $(3.0 \mathrm{sec})$. The additional time frames were used in a video display of the deployment, a copy of which was provided to NASA/Langley. Had there been a reason for the latch-up to occur on some sort of spring (other than the members which must be rigid), the impact response, with appropriate input modifications, might have been simulated.

A limited reproduction of the output from request no. 9999 made in the input file is shown in table 17. It is the relative displacement response of marker 806 on part 8 to marker 906 on part 9 (see figure 6) expressed in the coordinate system of marker 806. It can be seen from the 806 marker statement in table 11 that the Euler angles rotate the marker triad 90 degrees about its $x$-axis such that the z-axis is in the plane of figure 6 pointing toward part 7. The z-axis for marker 906 is in the same position but its $x$-axis is almost perpendicular to the figure at time equal to zero seconds resulting in the relative angle between $x$-axes as -89.50 degrees. As the deployment progresses the angle approaches zero degrees, the theoretical latch-up angle at a time near 1.7 sec . A graphical sequence of this is shown at four points in time in figure 8 through 11.

## Section 7

## CONCLUDING REMARKS

ADAMS is considered the best available three-dimensional general-purpose program for performing large-displacement, kinematic, and dynamı analyses of a mechanical system, such as a deploying space antenna. According to reference 1 , ADAMS was designed to accommodate problems of virtually any size. However, solving a problem the size of a Tetrahedral Truss Antenna should be demonstrated. CPU time can be estimated by extrapolation. If not by extrapolation of actual data from a series of problems, a rough estimate of CPU time can be made by assuming the time to increase as the 1.5 to 2nd power of the number of equations (ref. 1) or the number of parts since the number of equations are related to the number of parts. Ultimately, though, the limitation must be determined by application.

ADAMS is excellent for solving static equilibrium problems and also kinematic problems involving, for example, the observation of certain moving parts for possible interferences or other functional considerations. Deployment position, velocity and acceleration time histories are accurately determined in the dynamic analysis mode. Excellent graphical and video displays can be created from the position time histories.

Since ADAMS is a rigid hody program, there is a limit in the scope of dynamic analysis. For example, deployment latch-up forces cannot be determined due to the absence of flexible members to absorb the kinetic energy. A new version of ADAMS, which should be available in the year 1986, will include a flexible body code and should be able to determine latch-up forces. A disadvantage of this code is the potential for huge increases in computer time. This problem is alleviated by limiting the number of flexible bodies in the model. As discussed in Section 4, a relatively simple alternate method of analysis is easily developed for estimating the maximum surface member bending stresses by considering the surface member flexibility and kinetic energy at latch-up in the first bending mode.

Large problems which make the flexible body code impractical to use may make it desirable to develop a special-purpose program for a particular antenna design.

General Dynamics' SNAP program is an example of a special-purpose program. Rather than develop a general-purpose program hased on rigorous large displacement dynamics for almost any mechanical system, the development was based on a deployable truss structure in mind and idealizing the members as lumped masses connected by springs and dampers. Satisfactory results are ohtained for the kinematics of deployment and the elastic response at latch-up. As the development of a large computer code is expensive, the limited use of a general-purpose program such as ADAMS might be employed before making the necessary commitment to a particular design.

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| Point | $X(I N)$. | $Y$ | $Z$ | Comment |
| :--- | ---: | :---: | :--- | :--- |
| 1 | 5.0 | 0. | 0. | Translational joint |
| 2 | 600.0 | 0. | 0. | Revolute joint |
| 3 | 605.0 | -295.28 | 0. | Spherical joint |
| 4 | 610.0 | 0. | 0. | Revolute joint |
| 5 | 605.0 | 0. | 0. | Cylindrical joint |
| 6 | 602.5 | -147.64 | 0. | Reference point |
| 0300 | 607.5 | -147.64 | 0. | CM of Part 3 |
| 0400 |  |  | CM of Part 4 |  |

Table 2. - Box Truss Component Data

Component Data
02 Lumped Mass

$$
\begin{aligned}
& \text { Mass }=3.6 \mathrm{ln} \mathrm{sec}^{2} / \mathrm{in} . \\
& I P=.01 .01 .01
\end{aligned}
$$

03 Surface Member
Mass $=.0122$

$$
I P=88.641 .088 .64
$$

04 Surface Member
Mass $=.0122$
$I P=88.641 .088 .64$
05 Lumped Mass
Mass $=3.6$
$I P=.01 .01 .01$

Note: $I P=I X$ IY IZ ( $1 \mathrm{~b} \sec ^{2}$ in)

## TABLE 3. - INPUT FILE FOR BOX TRUSS MEMBER.

```
BOXTRUSS FOLDING REMBER.FREE-FREE CONDITION
PART.01,GROUND
Th.0101.OP-5,0,0, EU-90,90,0
M4 0105,0P-1205,0,0,EU-90;90,0
MA.0106,00-605,6:0
PART, B2,MASS-3.6,CN-0202,IP=.01,.01,.01
MA/9201,OP-5,0,0,EU-90,90,0
Ma.0202,OP-600,0,0
PART/03,MASS.,0122,CN-0300,IP.88.64,1,88.64
NR.0300.0P-682.5,-147.64,0
MA.e382,0р-600,0,0
MA,8303,0P-605,-295.28,0
PART/04,NA5S=.0122,CN-0400,IP-88.64,1,88.64
RA/0400,0P=507.5,-147.64.0
MA-9403.OP-605,-285.2B,0
HM/0404,0P-610,0,0
PART/-05,MA55-3.6,CM-0504,1P-.01,.01,.01
MA,0584,0P-61B,6,0
MA-05e5,0P-1205,0,0,EU-90,90,0
    JOINTS,DOF - Z U/O GEN
J0/0102.TRA.100101.J-0281
j0ノeze3,REU,I &202,J-e302
J0/0304,5PH.I-9303,J-0403
J0/84e5,REU,1-0404,J-0504
Jo/e501,CYL,I-0505,J-0105
    FORCE
FO/1,GT,1-0303,J-0403,KT-.2944,A-271.74,T-0,CT-0
SENSOR/34,DISP,I-8303.J-8403,ANGI
.UALUE-17BD,PRINT,HALT,EO,ERROR-1.0D
    GRAPHICS
GRR1.OUT-8302,0303
GR/2,OUT-0403,0404
    OUTPUT
0EO/1,D15,1-0302,J-0106
PEO/2,DIS,I-0404,J-0106
RE0/3,UEL,I-8202,J-0302.RH-0202
        SYSTEM CARDS
SYS/GC-1., IGRAU-0.JGRAU-0,KGRAU-0
    OUTPUT CARDS
OUTPUT/SAUEREG,GRSAUE
END
```

TABLE 4. - INTERACTIVE TERMINAL DISPLAY AFTER LOADING AND EXECUTING.

```
abums
Enter HDANS anput-file neme for OUITis IOXPA.FRE;I4
Enter run-name for output filea ((CR)-sOXfM):
Enter subreutine binary-file namo ((CR)-none)t
Do you heve your own linked version of ADAMS (Y/N) ((CR)0N)s
Do you ment to run in batch mode? (V/N) ((CR)*N)t
Send output to Lorminal? (Y/H) (<CR)-N):
Begin execution of ADAMS....
    ENTERING INPUT PHASE
    IOXTRUSS FOLDING REMBER,FREE-FREE CONDITIOH
MUMEER OF EOUATIONS IN JACOSIAN - }9
CPU TIME E 1.770 SECONDS
ENTERIHG SIMULATION PHASE
ENTER SIMULATION CONMAND
ENTE
NEO- 46 HG: 298 MAXNUN- 8797
NEO. 98 NG. 516 MAXMUN- 13029
TBEGIN-0.00000E+00 ENTER TEND. HSTEPS
95 }19
TIMEN 2.50000D-02 H- 2.50000D-02 KFLAG & ORDER= 1 IFCT= & 1STP- 5
TIME- 9.50000D+00 H- 5.00000D-01 KFLAG• 1 ORDER- 2 IFCT- 47 ISTP- 31
TITE-1.90000D+01 H- S.00000D-01 KFLAG* & ORDER- 2 IFCT* 85 1STP* S0
TIME= 2.85000D+01 H- 5.00000D-01 KFLAG- & ORDER- 2 IFCT- 123 1STPa 69
TITE= 3.80000D+01 H- S.00000D-01 KFLAG= 1 ORDER= 2 IFCT- 161 15TP= 88
TIRE- 4.75000D+01 H- 5.00000D-01 KFLAG= 1 ORDER= 2 IFCT= 190 ISTP= 147
TITE-5.70000D+01 H- 5.00000D-0& KFLAG- I ORDER- 2 IFCT: 237 15TP- 126
TINE-6.65000D+01 H- 5.00000D-01 KFLAG- 1 ORDERe a IFCT- E75 15TPe 145
TINE= 7.6%e0eD+01 H- 5.00000D-01 KFLAG* & ORDER- a IFCT- 315 1STP- 164
TITE= 8.55000D+01 H- 5.00000D-91 KFLAG- 1 ORDER- 2 IFCT* 372 I5TP- 183
EEEZHOTE(EUNCHK) - SENSOR, 34 IS ACTIUE
EVENT UALUE - 3.10569E+00 SENSOR VALUE - 3.09078E+04 TINE - E.95545E401
ADAHS EXECUTION TERMINATED IY SUAROUTIME SEMACT
```

TABLE 5. - OUTPUT FOR BOX TRUSS MEMBER, REQUEST NO. 1.


TABLE 6. - OUTPUT FOR BOX TRUSS MEMBER, REQUEST NO. 3.


TABLE 7. - TETRAHEDRAL GEOMETRY DATA, OPEN POSITION.

| Point | X(IN.) | $Y$ | Z | Comment |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 0.0 | -1.25 | 243.179 | Bushing force |
| 2 | -1.083 | 0.625 | 243.179 | Bushing force |
| 3 | 1.083 | 0.625 | 243.179 | Bushing force |
| 4 | -148.375 | 83.788 | 0.00 | Revolute joint |
| 5 | -148.917 | 85.978 | 1.77 | Revolute joint |
| 6 | -146.750 | 86.603 | 0.00 | Revolute joint |
| 7 | 0.00 | 86.603 | 0.00 | Revolute joint |
| 8 | 146.750 | 85.603 | 0.00 | Revolute joint |
| 9 | 148.917 | 85.978 | 1.77 | Revolute joint |
| 10 | 148.375 | 83.788 | 0.00 | Revolute joint |
| 11 | 75.00 | -43.301 | 0.00 | Revolute joint |
| 12 | 1.625 | -170.390 | 0.00 | Revolute joint |
| 13 | 0.00 | -171.955 | 1.77 | Revolute joint |
| 14 | -1.625 | -170.390 | 0.00 | Bushing force |
| 15 | -75.00 | -43.301 | 0.00 | Revolute joint |
| 16 | 0.00 | 0.00 | 244.949 | Marker origin, upper fitting |
| 17 | 0.00 | 0.00 | 243.179 | Marker origin, upper fitting |
| 18 | -150.00 | 86.603 | 0.00 | Marker origin, lower fitting |
| 19 | 150.00 | 86.603 | 0.00 | Marker origin, lower fitting |
| 20 | 0.00 | -173.205 | 0.00 | Marker origin, lower fitting |
| 0100 | 0.00 | 0.00 | 244.199 | Upper fitting CM |
| 0200 | -75.00 | 43.302 | 124.975 | Diagonal CM |
| 0300 | 75.00 | 43.302 ? | 124.975 | Diagonal CM |
| 0400 | 0.00 | -86.603 | 124.975 | Diagonal CM |
| 0500 | 0.00 | -173.205 | 0.750 | Lower fitting CM |
| 0600 | -38.313 | -106.846 | 0.00 | Surface member CM |
| 0700 | -111.688 | 20.244 | 0.00 | Surface member CM |
| 0800 | -150.00 | 86.603 | 0.75 | Lower fitting CM |
| 0900 | -73.375 | 86.603 | 0.00 | Surface member CM |
| 1000 | 73.375 | 86.603 | 0.00 | Surface member CM |
| 1100 | 150.00 | 86.603 | 0.75 | Lower fitting CM |
| 1200 | 111.688 | 20.244 | 0.00 | Surface member CM |
| 1300 | 38.313 | -106.845 | 0.00 | Surface member C.M |
| 1426 | 0.0 | 0.0 | 254.949 | Marker orıgin, ground |
| 1428 | 10.0 | 0.0 | 244.949 | Marker origin, ground |
| 1429 | 0.0 | 10.0 | 244.949 | Marker origin, ground |
| 1491 | 0.0 | 0.0 | 244.949 | Marker origin, ground |
| 1492 | 0.0 | 0.0 | 244.949 | Marker origin, ground |
| 0191 | 0.0 | 0.0 | 244.199 | Marker origin, upper fitting |
| 0192 | 0.0 | 0.0 | 244.199 | Marker origin, upper fitting |

## TABLE 8. - TETRAHEDRAL COMPONENT DATA.

| Component | Data |
| :---: | :---: |
| Cluster Fittings | Mass $=.00259$ 1b $\sec ^{2} / 1 \mathrm{n}$. |
| 01, 05, 08, \& 11 | $I P=.01 .01 .005$ |
| Diagonal Members | Mass $=.004653$ |
| 02, 03, \& 04 | $I P=22.59622 .596 .10$ |
| Surface Members | Mass $=.002819$ |
| 06, 07, 09, 10, 12, \& 13 | $I P=5.07625 .0762 .10$ |
| e: $\quad I P=I X I Y I Z\left(1 b \sec ^{2} / n\right)$ |  |

TABLE 9. - COMMAND FILE FOR TETRAHEDRAL TRUSS.


# TABLE 10. - FUNCTION SUBPROGRAM FOR TETRAHEDRAL TRUSS. 

## TMPE JCATET.FOA,

C function FSUB(ID,TIME,APAR,PAR,DFLMA)
© Implicit realib (A-H, O-2)
DIMENSIOH APAR(6),PAR(5)
c LOGICAL DFLAG

C $\quad R A D=D S O R T(A P A R(1) \geq \pm 2+A P A R(2) \geq 22+A P A R(31 \geq z 2)$

RETURN
END
FUNCTION TSUB(ID,TIME, PHI, DPHI,PAR, DFLAG)
IMPLICIT REAL: 8 ( $A-H, 0-2$ )
DIMENSION PAR(5)
LOGICAL DFLAG

- TSUB-0.DO
c IF(TIME.EO.0.ө) RETURN
AHG-PAR(1)
IF (PHI. GT. ANG) RETURN
1F (PHI.LT. 0.6 ) $C 0$ TO 100
TSUB = (ANG-PHI ) $\mathrm{I}(27.8 /$ ANK
RETURN
c RETURN
100 C-PAR(2)
IF (DPHI.GT.0.01C-Cz0.1
TSUB-27.0-PAR(3) PRHI-CIDPHI
RETURT
END
$s$


## TABLE 11. - INPUT FILE FOR TETRAHEDRAL TRUSS.

## TETRAHEDRN TAUSS LUNIT

LIST

```
PART/81,MASS-88250,1P- 81, 81, E25 CM-81B0
MARKER/0102.OP-2 0.0 0,244 199
MM/0191,0P-0,0,244 199,2P-1,8,244 109
MK/E102,0P-0:0,244 109,2P-g,1 244 100
MURKER/DIO1,0P-8 0,-1 25,243 170,EU-90,00,0
MMRKER/Q1E2,OP--1 E93,0 625 243 170,EUNIS0,00,0
MARER/Q103,OP-1 Q83,0 625,243 179,EU-30,00,0
MARXER/Q110,0P-8 0,8 0,244 040
MARKER/0117,0P-8 व, © Q,243 170,EU-30,0,8
PART/02, MASS- 004853,IP-22 590,22 506, 1, CM-0200
```



```
MARAER/Q202,0P--1 R03,0 625,243 170,EU=150,00,8
MNRKER/Q2ES,OP--148 017, 85 O'78,1 77, हU-150,90,8
PART/03,MASS-604653 [P-22 596,22 596, 1,CM-0380
MMRKER/Q380,0P-75 80,43 302,124 075,EU-120,-35 28,8
```



```
MARKER/8389,0P-148 917,85 978,1 77,EU-30,98,8
PART/G4 MASS- 084B53,IP-22 500,22 500,1,CM-0400
MARXER/84R0,0P=6 日,-88 603,124075, {U-8,-35.20,0
MARKER/8421,OP-9 8,-1 25,243 179,EU-90,08,A
```



```
PART/PS MASS- 00259,IP= 01, 01, 805 CM-ESEa
MARXER/OSEO,OP-8 Q,-173 205,0.75
MARXER/QS13,0P-1] 0,-171 955,1 77, EU-00,98,0
MNRXER/RSI4,0P=-1 625,-170 390,8 80, EU-120,90,8
HARKER/O512,0P-1 625,-170 300,0 0 EU-60,90,0
MLRKER/OS20,0P-0 Q,-173.205 ת.0
```



MARKER/8614 DPP-1 $025,-178300,8$ Q, EV 120,00 , 1


PART/E7, MASS- 802929,1 P- $58782,58782,1, C T-0790$



```
TABLE 11. - (Cont.)
```

PART/08, MAS5- $28259,1 P-01,81 ; 805, C H-8880$


MARKER/2805, OP--148 $917.85078,177$, EU-150,00, 0

MARXER/8810, OP--150, 86803.010
PART/89, MASS- 882820,1 P. $50782,50782,1, \mathrm{CM}-2080$
MARKER/R980, OP=-73 $375,80683,860, E U-90,00,00$



PART/10 MASS- 002829 ,IP-5 $0782,50762,1, C M-1808$



PART/II MASS- 20259 ,IP- 01 . 01 , $205, \mathrm{CH}-1100$
RARXER/1120 DP-158 $80,88683,875$
MARKERノI188, © 0 - 148 750, 76 603, $080, E U-0,90,8$



PART/12 MASS- 802829 ,IP-5 0762.5 6762, I CM-1280
MARXER/1289, $0 \times-111688,28$ 244,0 $00, E U-150,90$,



PART/13 MASS- 002829, IP-5 0762,5 0782, $1, C M-1308$

MURKER/I311 , $\mathrm{P}=75 \mathrm{ED},-43 \quad 381,8 \mathrm{BR}, \mathrm{EU}=240,90,0$


## PART/14 GROUNO




MARKER/1418, OP- $15080,88603,08$


MKRER $1428,0 \mathrm{P}=10,0,2440 \mathrm{OH}$


```
TABLE 11. - (Cont.)
FOFEI1420,FINPUT,1-D182,J-1420, PAR-120
FCRCE/1428,FINPUT,1-2103,j-1420,PAR-108
FORCE/1429,FINPUT,J-81CO,J-1429,PAR-100
FORCE/1427, FTCPQLE I-8180, J-1420, XT-1800
FORCE/1497,CTCROLE,I-0101,J-1491 XT-1880
FORCE/1408,CTORQE,I-8192,JJ-1402 सT=1REQ 
        JOINTS
    J0/0184 ,REY,I-8101,J-042
FORCE/OIO1,RUSHINC,I-0101,J-8401, N-1 E4,1 E4 ,1 E4,KT-1 DE4,1 OE4
C- 2E4, ZE4, 2E4 LT-0 2E4,0 2E4,0
    j0/8102,REV,1-8182,J-0202
```



```
N- ZE4, 2E4, ZE4,CT-0 2E4,0 2E4,0
    J0/0103,REV ,1-0103,J-0303
FCRCE/0183, ,USHINE,I-DIO3,J-8503,N-1 E4,1 E4,I E4,NT-1 EE4,I EE4
N= ZE4, ZE4, ZE4,CT-0 2E4,0 2E4,8
J0/ES04,REV,I-0413,J-E513
    JOUESES,REV,I-RSI4 J-8814
```



```
L- ZE4, ZE4, ZE4,CT-D ZE4,』 ZE4,8
J0/OS13.REV,I-8512,J-1312
J0/8882,REV,I-2885,J-8205
J0/E807, REV,I-R884,J-0704
j0/8809,REV,1-8803,J-2628
j0/1103, REV,l-1109,J-8320
JO/1110,REV I-1108,J-1228
JO/1112,REY,I-1110,J-1210
JO/0687,NEV,I-2015,J-5715
```



```
JJN1213,REV,I-1211, J-1311
    CENERATORS
    CEN/BEB7,CON NOIMTGG837,PARO1 0.0 B
FORCE/Q3837, [TOROXE,I-015 N-715 גT-8.2044, T--27
FORCE/33037,TINPUT, 1-0815,N-715,PAR-100.1830,1000
REDNG880 FORCE,1-D015N-715,NH-715 < IOD
    CLNOPIO,CON NOINT-EO1Q PAR-1.0,O &
```



TABLE 11. - (Cont.)

```
                    10,Dog.
FORCE/E2O10,TINPUT,1-0037,J-1C37 PAR-180,1803, 1800
KEO/88B7,FORCE,I-8907,J-1007,RM-1807
    CEN:213, COY,JOINT-1213, PAR-1 0,80
```



```
FORCE/B1213,TINOUT,I-1201,J-1311,PAR-100,1000,1280
```



```
    SERSOR/811,01SP,I-0318,J-1119,x,VALUE ،300,PRINT
    MNLT EO,ERRCR-'10
        craphics
CR/1 OUT-8996,0987
CR/2 DUT-1037.1888
CR/3,0UT-1210,1211
CP/4:CDI-1311,1312
CR5,01JT-R514,0015
CR/6,0UT-8715,9704
CP17,04T-8285,0202
CP/8,0UT-0329,8303
CR/9 DUT-8481:6413
CRAIO CIR CM-9117RR-1 25,SEC-3
CR11 CIR,CM-9520 R-3 25,5EC-6
CR/12,0uT-8512,0520
CR/13,OUT-8514,0520
CR/15NIR,CM-CG18,R-3 25,5EC-6
CR/15 CIR ,CM-Ca18,R-3 25,5EC-6
CR/10,OUT-EEE8,8818
CR/17,0UT-8804,2818
CR/18 OuT-R218,&8aS
CR/10,CIR CM-1110,R-3 25,SEC-6
GR/20,0UT-11E9,1119
CR/21 OUT-1110,1118
CR/22 WUT=1110,1109
CUTPUT
```



```
REO/B102 F, 0102,8202, PRM-102
```





```
REOROS13,FOFCE, I-ES12, J-1312, RM-512
```





```
REO/1103,50RCE, \(1-1100, j-0300,84-1100\)
REDIIIO FORCE:I-11E9 N-1000, R4-1103
REQ 1110 FOACE I 11180 , J- 1888 , RM 1109
```






```
REO/8992 DISP A1E2,0202, AM-102
```



```
RED/G994. DiSp il-04i3 JJ-0513,RM-113
REOJOSOS DISP, \(1-0514\) J-3814,RM-514
REO/RSGO DISP, I-GSI2, J-1312,RM-512
REQ/O897 DISP, 1-0885, J-8205,RH-B2S
RED/9998 DISP , 1 -8824, J-8704, RM-804
```



```
REO/O981, DISP; \(1-1109\), J-8509,RH-1189
REQ/9982, DISP, I - \(1169, J-1208, R M-1129\)
REQ/8983, DISP , 1-1110, J-1210, RM-1110
REORO994 DISP, I-0315 N- 0715 RM-815
RED/O985, D15P , 1-0997 N-1E07, RM-097
REQ/9988, 015P, \(1-1211\), J-1311, RH-1211
grstem cafog
```



```
EPRRIHT. DOMP EPRINT, RECOURP, RHSOMKP
GMTPUT CAROS
QUTPUTISAVEEEO, CRSAVE ENO-10. ,PRA
ENO
```

TABLE 12. - OUTPUT FOR TETRAHEDRAL TRUSS, REQUEST NO. 9999.

| TETRAHEDRAL TRUSS UNIT REQEST NUMBER 9999 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| olshlacement of marker bog relative to marker 906 EXPRESSED IN THE COORDINATE SYSTEM OF MARMER 806 |  |  |  |  |  |
| $\begin{aligned} & \text { TIME } \\ & \text { PIICH } \end{aligned}$ | ROLL MAC | $x$ | $Y$ | 2 | YAN |
| $\begin{aligned} & 80000 \\ & 8020 \end{aligned}$ | $\text { - } 80800$ | 8000 | 0000 | 8 - 00 | -89 501 |
| ${ }_{0}^{0} 03333$ |  | 0800 | 0000 | 0080 | -89 518 |
| 08667 | - a bie | 0800 | 0800 | 0 -20 | -89 570 |
| $82000$ | - 800 ®00 | 0030 | 0008 | 0 ECO | -88 656 |
| $\begin{gathered} 0800 \\ 0 \quad 1333 \end{gathered}$ | $\begin{array}{rl} -0000 \\ 0 & 0.000 \end{array}$ | 0030 | 8000 | 0880 | -89 773 |
| $\begin{aligned} & 0800 \\ & 81667 \end{aligned}$ | $\begin{aligned} & 0.2020 \\ & 0.200 \end{aligned}$ | 8800 | 0800 | 8000 | -89 988 |
| $0 \text { eco }$ | $0 \text { อ } 20$ |  |  |  |  |
| 82000 | $0^{0} 880$ | 0.880 | a 8 80 | 0800 | -89990 |
| 8020 | - 0 ero | 0008 | 0220 | 0 Ees | -89 951 |
| ${ }^{0} \mathrm{E} 2888$ | - 283 | 0080 | 8880 | 8 20s | -89 677 |
| ${ }_{8}^{8} 820$ | - ถอ ${ }^{\text {E20 }}$ | 0003 | 0800 | 0088 | -89 122 |
|  | 082000 |  | 0238 | 08003 | -88 342 |
| $0008)$ | 0.0002 |  | 2 |  |  |
| 16333 | 0 0 $0^{\text {co }}$ | 0020 | 0 203 | 0 eco | -10 887 |
| - 026067 | $0022$ | 0000 | 0800 | 0 000 | -2 598 |
| 17020 | 2200 | 0000 | 0800 | 0 0c3 | 8541 |
| ${ }^{8}$ | - 4048 | 0808 | 0008 | 0200 | 0132 |
| $8 \mathrm{BPD}$ | 0800 | 0 |  | - |  |
| $17667$ | - 0 - 000 | 0800 | 0200 | 0000 | -8 747 |
| $0_{1}^{818000}$ | - 8 ¢20 | 0000 | 0800 | 0 ace | -8 655 |
| ${ }^{0}, 809$ | - 2200 | 8088 | 0000 | 00000 |  |
| 0 000 | - 0 อ |  | 0 | - | -805 |



Figure 2, - Box Truss Surface Member Model


Figure 3. - Box Truss Surface Member, Time $=0$. seconds


Figure 4. - Box Truss Surface Member, Time $=85$ seconds


Figure 5. - Box Truss Surface Member, Time $=89.55$ seconds


Figure 6. - Tetrahedral Truss Model


Figure 7. - Marker Locations for Retraction from Open to Closed Position.


Figure 8. - Tetrahedral Truss, Time $=0$. seconds


Figure 9. - Tetrahedral Truss, Time $=1.0$ seconds


Figure 10. - Tetrahedral Truss, Time $=1.5$ seconds


Figure 11. - Tetrahedral Truss, Time $=1.7$ seconds


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## End of Document


[^0]:    *For sale by the National Technical Information Service. Springield. Virginia 22161

