

SINGLE PARTICLE MOMENTUM AND ANGULAR DISTRIBUTIONS
IN HADRON-HADRON COLLISIONS AT ULTRAHIGH ENERGIES

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1. Introduction. The forward-backward charged multiplicity distribution $P(n_F, n_B)$ of events in the 540 GeV $\bar{p}p$ collider has been extensively studied by the UA5 Collaboration. It was pointed out that the distribution with respect to $n = n_F + n_B$ satisfies approximate KNO scaling and that with respect to $Z = n_F - n_B$ is binomial [1]. The geometrical model of hadron-hadron collision interprets [2] the large multiplicity fluctuation as due to the widely different nature of collisions at different impact parameters b . For a single impact parameter b , the collision in the geometrical model should exhibit stochastic behavior. This separation of the stochastic and non-stochastic (KNO) aspects of multiparticle production processes gives conceptually a lucid and attractive picture of such collisions [3], leading to the concept of partition temperature T_P and the single particle momentum spectrum to be discussed in detail below.

2. Description of Model. Assuming the separation of stochastic from non-stochastic aspects of collision to remain valid as $n \rightarrow \infty$, we expect [1] that the distribution in the two-dimensional $(n_F/\bar{n}) - (n_B/\bar{n})$ plane would become more and more concentrated in a narrow region. For 540 GeV $\bar{p}p$ collisions this region is in the form of an ellipse as shown in Fig. 1(a). When \bar{n} becomes large, it becomes thinner and eventually collapses into a line segment (Fig. 1(b)). This line segment is a collection of points, at each of which $n_F \approx n_B$ and both n_F and n_B fluctuate only to the extent of $\sqrt{n_F}$ (i.e., like a stochastic distribution). For example; if $n = 2 \times 10^6$, then n_F could easily be as small as 0.5×10^6 or as large as 2×10^6 . But in either case, one can predict that $n_B \approx n_F$ with fractional

errors of the order $(\bar{n})^{-1/2} \sim 10^{-3}$.

Accepting this picture for very high energies, we see that for fixed n_F , the distribution of n_B is stochastic. How then is the energy partitioned in the backward hemisphere? We shall assume that the energy partition for each hemisphere for a fixed $z = (n_F + n_B)/\bar{n}$ is also stochastic but subject to a number of conditions: (a) that the total energy of all outgoing particles on each side is $E_0 h$, (b) Bloch-Nordsieck factor $d^3 p/E$ for each particle, and (c) transverse momentum (p_T) cutoff factor $g(p_T)$. In other words, the probability distribution for central particles on each side will be taken as

$$\delta(\sum_i E_i - E_0 h) \prod_i (d^3 p_i / E_i) g(p_{Ti}) \quad (1)$$

where $E_0 = \sqrt{s}/2$, $E_0(1-h)$ = total energy of all leading particles, and $i = 1, 2, \dots$ ranges over all the particles (positive, negative, and neutral) on one side minus the leading particles. h is a parameter that describes the fraction of E_0 that fragments into all particles in the central region.

Now the mathematical problem (1) is well-known in statistical mechanics as describing a microcanonical ensemble. By the well-known Darwin-Fowler method the single particle distribution of such an ensemble is given by the canonical ensemble:

$$dn = K (d^3 p/E) g(p_T) \exp(-E/T_p) \quad (2)$$

where T_p will be called the partition temperature and K is a normalization constant. Notice that all particles, positive, negative, and neutral, kaons, nucleons as well as pions, share the same T_p .

3. Comparison with Experimental Angular Distribution at 540 GeV. As Fig. 1(a) shows, at the 540 $\bar{p}p$ collider, the distribution is still an ellipse. We shall nevertheless test the validity of (2) at 540 GeV by evaluating the single particle angular distribution from it. We write

$$dn/d\eta = 2\pi K \sin^2 \theta \int_0^{E_0 h} p^2 (dp/E) g(p \sin \theta) \exp(-E/T_p) \quad (3)$$

where η = pseudo-rapidity, $\cosh \eta = \csc \theta$, and

$$g(p \sin \theta) = \exp(-\alpha p \sin \theta). \quad (4)$$

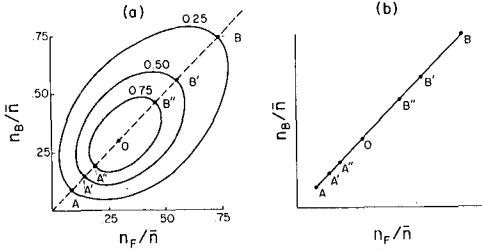


Fig. 1 Schematic diagram for forward-backward multiplicity distribution at very high energies. (a) The contour lines represent $P(n_F, n_B)$ at constant fractions of its maximum value at $\sqrt{s} = 540$ GeV where $\bar{n} \approx 29$. (b) The same contour lines degenerate to straight lines for extremely large \bar{n} .

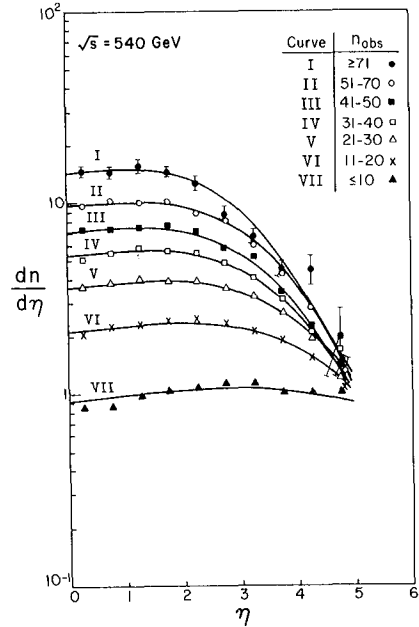


Fig. 2 Calculated and experimental $dn/d\eta$ vs. η at $\sqrt{s} = 540$ GeV.

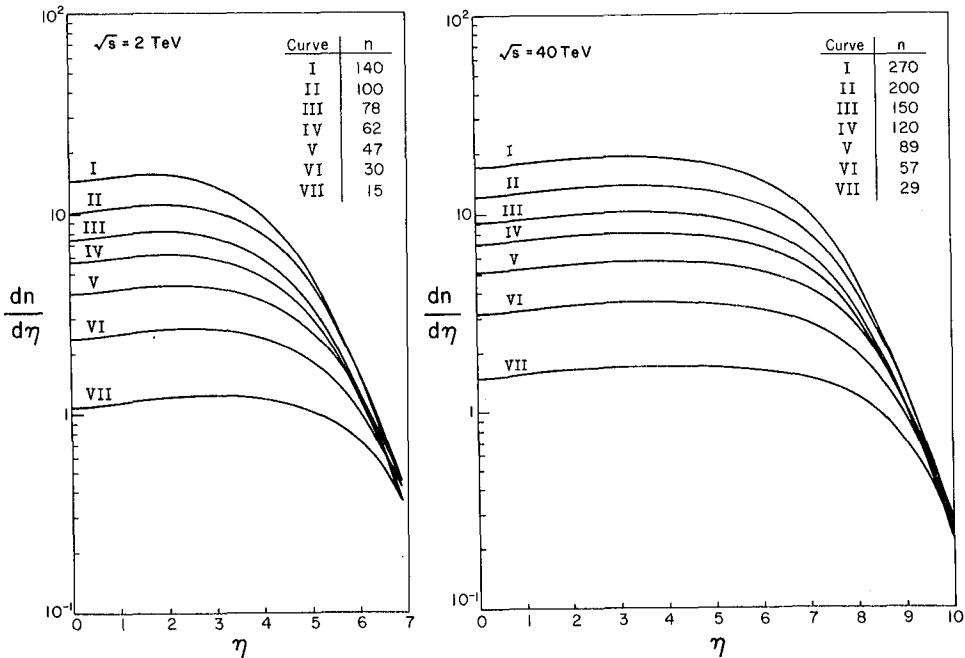


Fig. 3 Calculated $dn/d\eta$ versus η at $\sqrt{s} = 2$ TeV and 40 TeV.

We take α to be equal to $5.25(\text{GeV}/c)^{-1}$. Only pions are included in this calculation. The angular distribution is evaluated from (3) and compared with the results [4] of UA5 in Fig. 2. It is found that the UA5 curve for each multiplicity n is well fitted by (3) for one value of T_p . We emphasize that there are no adjustable parameters in this computation, the cutoff α having been taken from experiments [5] concerning p_T distributions. The parameter h and normalization constant K are both determined from the curves themselves.

We conclude that the angular distribution (3) that results from (2) is in excellent agreement with experiment. Furthermore, we believe (2) would give a complete description of the single particle momentum distribution for central particles.

4. Extrapolation to Higher Energies. We made extrapolations of the angular distribution to $\sqrt{s} = 2$ TeV (Tevatron) and 40 TeV (SSC). The assumptions made in these computations are as follows: (i) The values of α for these energies are taken to be 5.0 and 4.4 $(\text{GeV}/c)^{-1}$, respectively [5]. (ii) The parameter h is taken to be a function of the KNO variable $z = n/\bar{n}$ only. (iii) The values of \bar{n}_{ch} for these energies are taken to be 41 and 78, respectively, by extrapolation. The results are presented in Fig. 3.

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