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NSG 1185

KINEMATICS OF FOLDABLE DISCRETE SPACE CRANES

by

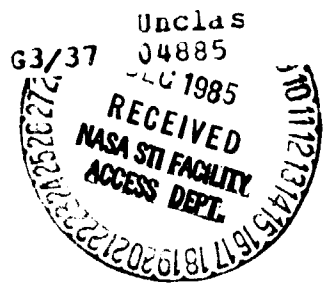
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ABSTRACT

Exact kinematic description of a NASA proposed prototype foldable-deployable discrete space crane are presented. A computer program is developed which maps the geometry of the crane once controlling parameters are specified. The program uses a building block type approach. In which it calculates the local coordinates of each repeating cell and then combines them with respect to a global coordinates system.

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## Introduction

The coming years will see an increasing utilization of space through the use of very large, lightweight structures constructed in orbit for such purposes as antennas, energy collection platforms and work stations. With the recent successful flights of the Space Shuttle, such projects are one step closer towards becoming reality. It will be most desirable that these structures be made of repeating sub-assemblies in order to aid in the ease of construction, minimize fabrication costs, and reduce complications in analysis.

Under our NASA Grant NSG 1185, we have been investigating various methods of designing and analyzing the geometry of discrete large space structures. Our previous extensive work has dealt with both the areas of design and analysis. Most recently, we completed and published results on establishing the dynamic behavior of large space structures in the forms of periodic trusses and frames.

For the purposes of in-space construction and subsequent repairs, large space tools are required. It is most desirable for these tools to be kept packed and to be deployed only whenever they are needed. An important example of such tools are the deployable crane (large arm) and telescopic supports as illustrated in Figure 1. This tool has the mobility of full or partial deployment and to move in any direction in order to reach desired points in the host structure.

The mechanism and control of the deployment of this tool is very essential. This specific NASA crane-prototype can be deployed and maneuvered in various directions by changing the lengths of members in its bays. To know how much change in these lengths is required to achieve the

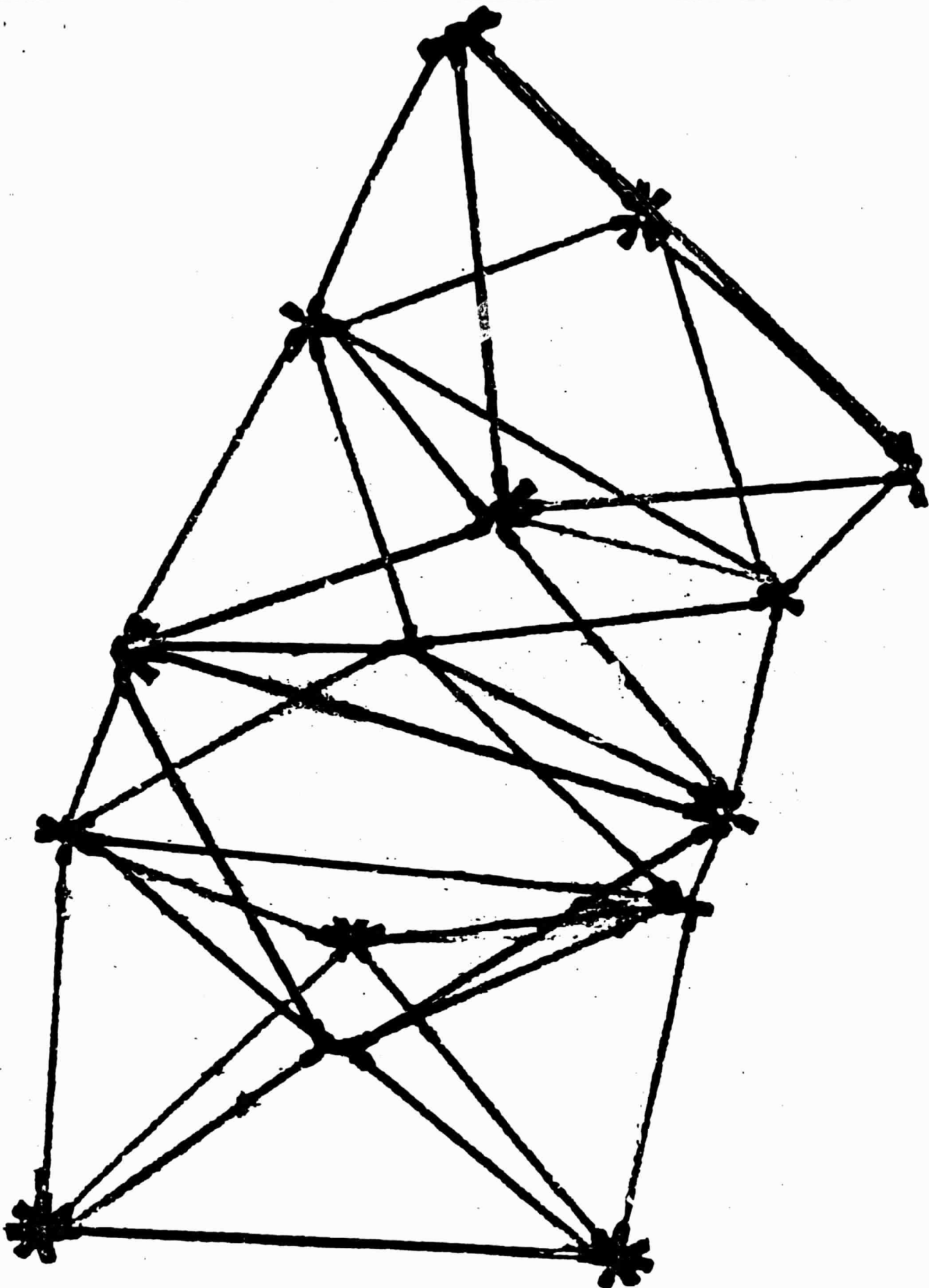


Figure 1 Crane Geometry

required configuration is essential. This is also important to know for the control of the vibrations of the crane.

In this report we analyze the kinematics of the crane configuration which result from the changes of the lengths of the bay members. Specifically, we developed a computer program capable of calculating the coordinates of each node of the crane resulting, from member length changes. This information is very essential in the utility of the crane. The new configuration kinematics can also be fed to a vibration program to calculate the dynamic characteristics of the new configuration, if found necessary.

### Structures Description

The specific crane structure under consideration consists of repeating unit cells as shown in Figure 2. Each unit cell constitutes a truss substructure with nine nodal points as illustrated in Figure 3. In this unit cell the lengths of the rods connecting the nodes 4, 5 and 6 are variables and hence control the overall shape of the cell and ultimately the total structure. On the other hand all remaining rod members have constant lengths. Specifically, members (1,2), (1,3), (2,3), (7,8), (7,9) and (8,9) have constant equal lengths denoted by  $G$ , and aside from the variable member lengths (4,5), (4,6) and (5,6), all remaining members have the constant equal lengths  $B$ .

### Summary of the Analysis Procedure

In order to give complete description of the kinematics of the crane with arbitrary number of unit cells, we use a building block type approach consisting of the following steps:

- (1) By choosing a local coordinate system (on the single unit cell level) we calculate the coordinates of its' nine nodes.

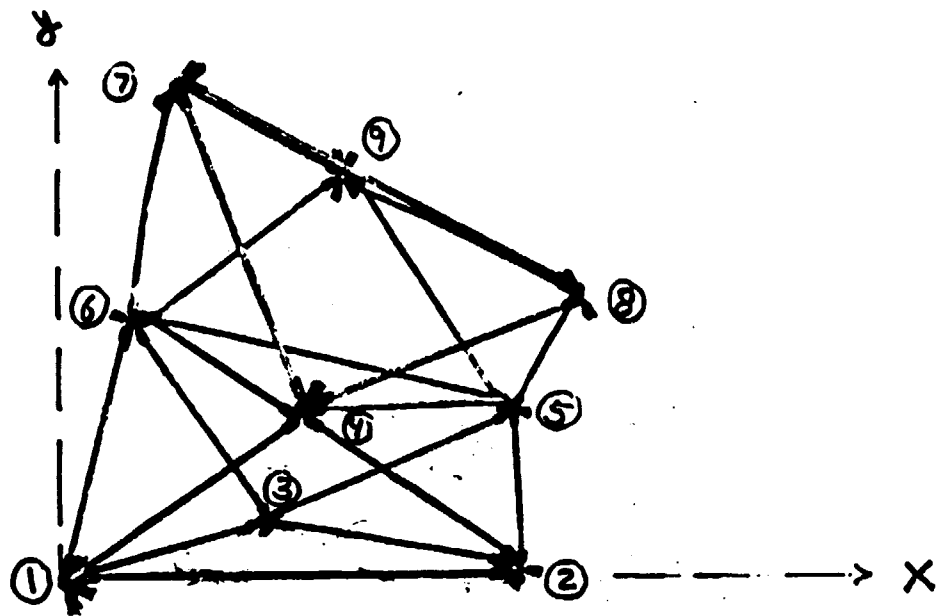


Figure 2 Repeating Unit Cell

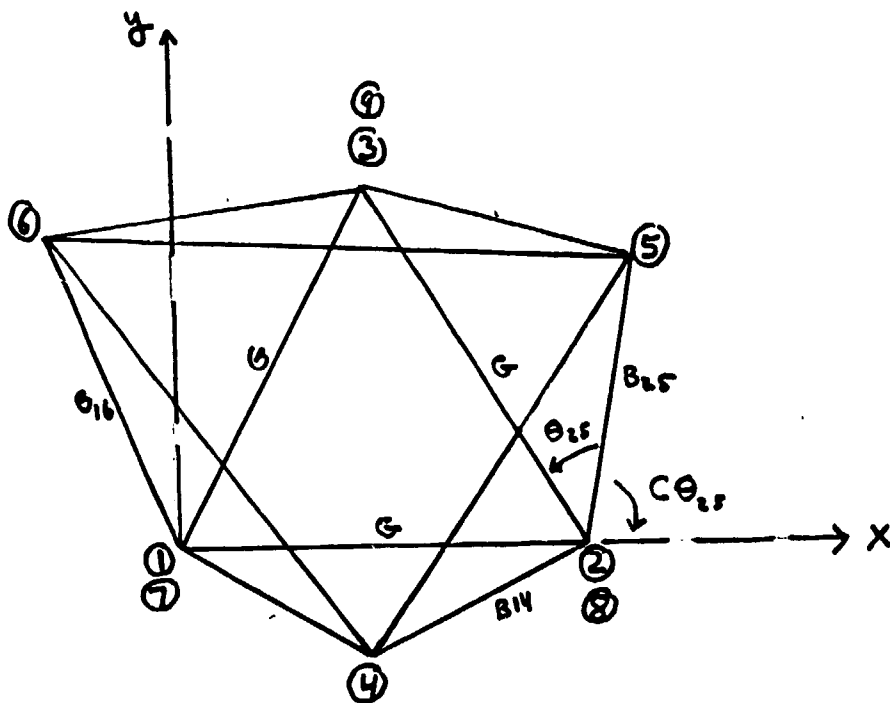


Figure 3 Projected Geometry

- (2) These coordinates are then referred to a pre-assigned global coordinate system (for the total structure).
- (3) If the nodal global coordinates of the (n-1)th cell are known, then the plane of its' top three nodes (7, 8 and 9) will define the base for the nth cell. This suggests the use of coordinate transformations to define such a base.
- (4) Orthogonal coordinate transformations are constructed for the top plane of each cell as a base for the next cell.

Note: A major fact in constructing the local coordinates of each unit cell is that the plane of its 7, 8 and 9 nodes is a mirror image of the plane of the nodes 1, 2 and 3; the mirror being the plane of the nodes 4, 5 and 6.

The floor of this unit cell is the equilateral triangle with side lengths G and having the nodal coordinates:

$$\text{Node 1: } (0,0,0) \quad (1)$$

$$\text{Node 2: } (G,0,0) \quad (2)$$

$$\text{Node 3: } (G/2, \frac{\sqrt{3}}{2} G, 0) \quad (3)$$

Now, let us arbitrarily assume that points 4, 5 and 6 have the vertical heights (coordinates)  $Z_4 = H_4$ ;  $Z_5 = H_5$  and  $Z_6 = H_6$ . If we now designate the projected lengths of the members 2-5, 1-6 and 1-4 by  $B_{25}$ ,  $B_{16}$  and  $B_{14}$ , respectively, then one concludes that

$$B_{25} = (B^2 - H_5^2)^{1/2} \quad (4)$$

$$B_{14} = (B^2 - H_4^2)^{1/2} \quad (5)$$

$$B_{16} = (B^2 - H_6^2)^{1/2} \quad (6)$$

where B is a constant.

Furthermore, by inspection one can immediately deduce the coordinates of the point 4 as

$$\text{Node 4: } \left( \frac{G}{2}, -[B_{14}^2 - (.5G)^2]^{1/2}, H_4 \right) \quad (7)$$

Let us now concentrate on finding the coordinates of point 5. From Figure 3 we see these to be

$$\text{Node 5: } (G + B_{25} \cos \theta_{25}, B_{25} \sin \theta_{25}, H_5) \quad (8)$$

using the trigonometric manipulations

$$\begin{aligned} \sin \theta_{25} &= \sin\left(\frac{2\pi}{3} - \theta_{25}\right) \\ &= \sin \frac{2\pi}{3} \cos \theta_{25} - \cos \frac{2\pi}{3} \sin \theta_{25} \\ &= \frac{\sqrt{3}}{2} \cos \theta_{25} + \frac{1}{2} \sin \theta_{25} \end{aligned}$$

yields

$$\sin \theta_{25} = \frac{\sqrt{3}}{2} \frac{G}{2B_{25}} + \frac{1}{2} \frac{[B_{25}^2 - (G/2)^2]^{1/2}}{B_{25}} \quad (9)$$

Hence,

$$\begin{aligned} Y_5 &= B_{25} \sin \theta_{25} \\ &= \frac{\sqrt{3}}{4} G + \frac{1}{2} (B_{25}^2 - (G/2)^2)^{1/2} \end{aligned} \quad (10)$$

and by similar arguments we see that

$$\begin{aligned} \cos \theta_{25} &= \cos\left(\frac{2\pi}{3} - \theta_{25}\right) \\ &= \cos \frac{2\pi}{3} \cos \theta_{25} + \sin \frac{2\pi}{3} \sin \theta_{25} \end{aligned}$$



$$\begin{aligned}
&= -\frac{1}{2}\cos\theta_{25} + \frac{\sqrt{3}}{2}\sin\theta_{25} \\
&= -\frac{1}{2}\frac{G}{2B_{25}} + \frac{\sqrt{3}}{2}\frac{[B_{25}^2 - (G/2)^2]^{\frac{1}{2}}}{B_{25}}
\end{aligned}
\tag{11}$$

Hence,

$$\begin{aligned}
X_5 &= G + B_{25} \cos\theta_{25} \\
&= \frac{3G}{4} + \frac{\sqrt{3}}{2}[B_{25}^2 - (G/2)^2]^{\frac{1}{2}}
\end{aligned}
\tag{12}$$

By symmetry and inspection of the coordinates of point 5 we can deduce the coordinates of point 6 as

Node 6:

$$x_6 = \frac{G}{4} - \frac{\sqrt{3}}{2}[B_{16}^2 - (G/2)^2]^{\frac{1}{2}}
\tag{13}$$

$$y_6 = \frac{\sqrt{3}}{4}G + \frac{1}{2}[B_{16}^2 - (G/2)^2]^{\frac{1}{2}}
\tag{14}$$

and

$$z_6 = H_6$$

#### Remarks

Notice that from (10) and (12) that

$$x_5 = \sqrt{3} y_5
\tag{15}$$

and from (13) and (14)

$$x_6 - 1 = -\sqrt{3} y_6
\tag{16}$$

Calculations of the Lengths  $D_{45}$ ,  $D_{46}$  and  $D_{56}$ :

In what follows we shall normalize our length  $G$  to be unity.

Accordingly, by inspection we have the further relations

$$x_4^2 + y_4^2 + z_4^2 = B^2 \quad (17a)$$

$$x_6^2 + y_6^2 + z_6^2 = B^2 \quad (17b)$$

$$(x_5 - 1)^2 + y_5^2 + z_5^2 = B^2 \quad (17c)$$

We also have

$$D_{45}^2 = (x_5 - x_4)^2 + (y_5 - y_4)^2 + (z_5 - z_4)^2 \quad (18a)$$

$$= x_5^2 + y_5^2 + z_5^2 + x_4^2 + y_4^2 + z_4^2$$

$$- 2(x_4x_5 + y_4y_5 + z_4z_5)$$

$$= (x_5 - 1)^2 + 2x_5 - 1 + y_5^2 + z_5^2 - 2(x_4x_5 + y_4y_5 + z_4z_5) + B \quad (18b)$$

$$= 2B^2 + 2x_5 - 1 - 2(x_4x_5 + y_4y_5 + z_4z_5)$$

where we used (17c), hence

$$D_{45}^2 = 2B^2 + 1 - 2[x_5 - x_4x_5 - y_4y_5 - z_4z_5] \quad (19a)$$

$$= 2[x_5(1-x_4) - y_4y_5 - z_4z_5] \quad (19b)$$

which from (7), where now  $x_4 = \frac{1}{2}$ ,

$$= 2\left[\frac{x_5}{2} - y_4y_5 - z_4z_5\right] \quad (19c)$$

Hence,

$$\frac{1}{2}[D_{45}^2 - 2B^2 + 1] = \frac{x_5}{2} - y_4y_5 - z_4z_5$$

which, by using the relation (15) can eliminate  $x_5$  to get

$$\frac{1}{2}[D_{45}^2 - 2B^2 + 1] = Y_5\left(\frac{\sqrt{3}}{2} - Y_4\right) - Z_4Z_5$$

which can be rewritten as

$$B^2 - \left(\frac{1+D_{45}^2}{2}\right) = Y_5\left(Y_4 - \frac{\sqrt{3}}{2}\right) + Z_4Z_5 \quad (20)$$

Let now

$$A_{45} = B^2 - \left(\frac{1+D_{45}^2}{2}\right) \quad (21)$$

Then we have

$$A_{45} = Y_5\left(Y_4 - \frac{\sqrt{3}}{2}\right) + Z_4Z_5 \quad (22)$$

Let further

$$Y_4^* = Y_4 - \frac{\sqrt{3}}{2} \quad (23)$$

Then

$$A_{45} = Y_5Y_4^* + Z_4Z_5 \quad (24)$$

By similar arguments one can replace subscript 5 by 6 and immediately obtain the relation

$$A_{46} = Y_6Y_4^* + Z_4Z_6 \quad (25)$$

where

$$A_{46} = B^2 - \frac{(1+D_{46}^2)}{2} \quad (26)$$

Finally from the relation

$$\begin{aligned} D_{56}^2 &= (X_5 - X_6)^2 + (Y_5 - Y_6)^2 + (Z_5 - Z_6)^2 \\ &= X_5^2 + Y_5^2 + Z_5^2 + B^2 - 2(X_5X_6 + Y_5Y_6 + Z_5Z_6) \end{aligned}$$

one gets,

$$D_{56}^2 = 2B^2 + 2X_5 - 1 - 2(X_5X_6 + Y_5Y_6 + Z_5Z_6)$$

thus, we define

$$A_{56} = B^2 - \frac{(1 + D_{56}^2)}{2} \quad (27a)$$

and get

$$A_{56} = X_5(X_6 - 1) + Y_5Y_6 + Z_5Z_6 \quad (27b)$$

which, if the relation (16) is used, finally yields

$$A_{56} = -\sqrt{3} X_5Y_6 + Y_6Y_5 + Z_5Z_6 \quad (27c)$$

Now, if the relation (15) is used to eliminate  $X_5$  we finally get

$$A_{56} = Z_5Z_6 - 2Y_5Y_6 \quad (28)$$

#### Method of Solution (The Inverse Problem)

We indicated earlier that if  $H_4$ ,  $H_5$  and  $H_6$  are known then all of the coordinates of the points 1, 2, 3, 4, 5 and 6 will be known. Unfortunately, what is known a priori are not the  $H_4$ ,  $H_5$  and  $H_6$ , but  $D_{45}$ ,  $D_{46}$  and  $D_{56}$ . In what follows we shall develop solution methods whereby if the lengths  $D_{45}$ ,  $D_{46}$  and  $D_{56}$  are given then we can solve the inverse problem and find  $H_4$ ,  $H_5$  and  $H_6$  and hence all the coordinates of the nodes. This will be done by simple iteration on the value of  $H_4$  as will be demonstrated below.

Let us assume that  $D_{45}$ ,  $D_{46}$ ,  $D_{56}$  and  $H_4$  are given. Then in the relations (24), (26) and (28), the parameters  $A_{45}$ ,  $A_{46}$ ,  $A_{56}$ ,  $Y_4$ ,  $Y_4^*$  and  $(Z_4 = H_4)$  will be known. Furthermore, since from (10),  $Y_5$  can be written in

terms of  $Z_5 = H_5$  and from (14)  $Y_6$  can be written in terms of  $Z_6 = H_6$ , we can easily see that we have only the two unknowns  $H_5$  and  $H_6$ .

Specifically, we now use the relations (24) and (10) and get

$$A_{45} = Y_4^* \left[ \frac{\sqrt{3}}{4} + \frac{1}{2}(B_{25}^2 - .25)^{\frac{1}{2}} \right] + Z_4 Z_5$$

or

$$A_{45} - \frac{\sqrt{3}}{4} Y_4^* = \frac{Y_4^*}{2}(B_{25}^2 - .25)^{\frac{1}{2}} + Z_4 Z_5$$

Now, from (4)

$$B_{25}^2 = B^2 - H_5^2 = B^2 - Z_5^2$$

we get

$$4(A_{45} - \frac{\sqrt{3}}{4} Y_4^* - Z_4 Z_5)^2 = Y_4^{*2} [B^2 - Z_5^2 - .25]$$

which can be further rearranged in the form of a quadratic equation for  $Z_5$

is

$$(4Z_4^2 + Y_4^{*2})Z_5^2 - 8F_{45}Z_4Z_5 + 4F_{45}^2 - Y_4^{*2}(B^2 - .25) = 0 \quad (29)$$

where

$$F_{45} = A_{45} - \frac{\sqrt{3}}{4} Y_4^* \quad (30)$$

Notice in (29) that if  $Z_4 = H_4$  is known and since  $B$  is known then  $Z_5$  is the only unknown. Hence, given  $H_4$  there is a unique value for  $Z_5$ .

By interchanging 5 and 6 similar relation to (29) can be constructed for point 6 as

$$(4Z_4^2 + Y_4^{*2})Z_6^2 - 8F_{46}Z_4Z_6 + 4F_{46}^2 - Y_4^{*2}(B^2 - .25) = 0 \quad (31)$$

where

$$F_{46} = A_{46} - \frac{\sqrt{3}}{4} Y_4^* \quad (32)$$

Thus, given  $Z_4 = H_4$  then there is a unique solution for  $Z_6$ .

Since, if  $Z_4$  is known, we can calculate  $Z_5$  and  $Z_6$  uniquely, the condition that fixes the exact value on  $Z_4$  is the relation (28). Specifically one has to iterate of  $Z_4$  until the calculated values  $Z_5$  and  $Z_6$  via (29) and (31) satisfy (28).

Now equations (29) and (31) admit the two solutions

$$Z_{5(1,2)} = [T_2 \pm (T_2^2 - T_1 T_3)^{\frac{1}{2}}] / T_1 \quad (33)$$

$$Z_{6(1,2)} = [W_2 \pm (W_2^2 - W_1 W_3)^{\frac{1}{2}}] / W_1 \quad (34)$$

where

$$T_1 = W_1 = 4Z_4^2 + Y_4^{*2}$$

$$T_2 = 4F_{45} Z_4$$

$$T_3 = 4F_{45}^2 - Y_4^{*2}(B^2 - .25)$$

$$W_2 = 4F_{46} Z_4$$

$$W_3 = 4F_{46}^2 - Y_4^{*2}(B^2 - .25) \quad (35)$$

Corresponding to the values (33) and (34) we can calculate new values for  $Y_5$  and  $Y_6$  which we shall refer to as  $K_5$  and  $K_6$ , respectively. Thus, we have (see (10) and (14) with  $G = 1$ )

$$K_5 = \frac{\sqrt{3}}{4} + \frac{1}{2}(V_{25}^2 - .25)^{\frac{1}{2}} \quad (36a)$$

$$K_6 = \frac{\sqrt{3}}{4} + \frac{1}{2}(V_{16}^2 - .25)^{\frac{1}{2}} \quad (36b)$$

where (see also (4) and (6))

$$V_{25} = (B^2 - Z_{5(1)}^2)^{\frac{1}{2}} \quad (37a)$$

$$V_{16} = (B^2 - Z_{6(1)}^2)^{\frac{1}{2}} \quad (37b)$$

From (33), (34), (36a) and (36b) we construct the function (see 28)

$$S_{56} = Z_{5(1)}Z_{6(1)} - 2K_5K_6 \quad (38)$$

where the idea here is to iterate on  $Z_4 = H_4$  until the value of  $S_{56}$  converges to the value of  $A_{56}$  as calculated via (27). Once this convergence takes place we will have the right values of  $Z_5$  and  $Z_6$  (i.e. namely  $H_5$  and  $H_6$ ) and we can then proceed to calculate the correct coordinates of points 4, 5 and 6.

#### Calculations of the Coordinates of Nodes 7, 8 and 9

By inspection one can easily find that the nodes 7, 8 and 9 are the mirror images of nodes 1, 2 and 3 respectively with respect to the plane of nodes 4, 5 and 6. To this end, using some algebraic manipulation we thus get:

$$\begin{aligned} X_{i+6} &= X_i - 2n_i P_i \\ Y_{i+6} &= Y_i - 2n_i P_i \\ Z_{i+6} &= Z_i - 2n_i P_i, \quad i = 1, 2, 3 \end{aligned} \quad (39)$$

where

$n_i$  are the components of the unit normal to the plane of the nodes 4, 5, 6 and  $P_i$  is the dot product between the normal  $\underline{n}$  and the vector

connecting the nodes 1 and 4. This completes the local coordinates of the repeating unit cell.

### Building Block Results

With the coordinates of nodes 7, 8 and 9 now known, their plane defines the base for the next unit cell. This is done by introducing a linear transformation of the original coordinates according to

$$X'_i = \beta_{ij} X_j \quad (40)$$

where  $X'_i$  are the new coordinates and  $\beta_{ij}$  are the direction cosines between  $X'_i$  and  $X_j$ . These values of the transformation tensor can be constructed from the normal to the plane of the vortices 7, 8 and 9. Once this is done then a building block approach yields the results for an arbitrary number of cells as is documented by the accompanying computer program. In the program a sample calculation of five unit cells is included and the coordinates of the vortices are listed in local and global coordinate systems.



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10 DIM XL(9), YL(9), ZL(9), X(200), Y(200), Z(200), B(3,3)
20 READ B, ERRO, NC
30 FOR I1=1 TO NC
40 G=1
50 READ R45, R46, R56
60 A45=B*B-(1+R45*R45)*.5
70 A46=B*B-(1+R46*R46)/2
80 A56=B*B-(1+R56*R56)/2
90 HM=SQR(B*B-.25)
100 FOR H4=HSTRT TO HM STEP .1: HSTRT=0
110 B14=SQR(B*B-H4*H4)
120 Y4=-SQR(B14*B14-(G/2)*(G/2))
130 Z4=H4
140 Y45=Y4-SQR(3)/2: F45=A45-(SQR(3)/4)*Y45
150 T1=4*Z4*Z4+Y45*Y45
160 T2=4*F45*Z4
170 T3=4*F45*F45-Y45*Y45*(B*B-.25)
180 NA=T2*T2-T1*T3: IF (NA=0) THEN 540
190 Z51=(T2+SQR(NA))/T1
200 F46=A46-(SQR(3)/4)*Y45
210 W1=T1
220 W2=4*F46*Z4
230 W3=4*F46*F46-Y45*Y45*(B*B-.25)
240 MA=W2*W2-W1*W3: IF (MA=0) THEN 540
250 Z61=(W2+SQR(MA))/W1
260 Z62=(W2-SQR(MA))/W1
270 V25=SQR(B*B-Z51*Z51)
280 V16=SQR(B*B-Z61*Z61)
290 K51=SQR(3)*G+2*SQR(V25*V25-G*G/4)/4
300 K61=SQR(3)*G+2*SQR(V16*V16-G*G/4)/4
310 S56=Z61*Z51-2*K5*K6: D=S56-A56
320 D=CDBL(D)
330 D1=D
340 IF (D) (ERRO THEN 590
350 IF D1*D=0 THEN 580
360 D1=D
370 GOTO 590
380 IF (NA=0) THEN 540
390 LPRINT TAB(1): "COMPLEX ROOTS": GOTO 550
400 NEXT H4
410 GOTO 590
420 G=1
430 H5=Z51
440 H6=Z61
450 HM=SQR(B*B-(G*G/3))
460 XL(1)=0
470 YL(1)=0
480 ZL(1)=0
490 XL(2)=0-G
500 YL(2)=0
510 ZL(2)=0
520 XL(3)=G/2
530 YL(3)=G*SQR(3)/2
540 ZL(3)=0
550 B14=SQR(B*B-H4*H4)
560 B25=SQR(B*B-H5*H5)
570 X4=G/2
580 Y4=-SQR(B14*B14-(G/2)*(G/2))
590 Z4=H4
600 X5=3*G/4+(SQR(3)/2)*SQR(B25*B25-(G/2)*(G/2))
610 Y5=5*G/4+(SQR(3)/2)*SQR(B25*B25-(G/2)*(G/2))
620 Z5=H4

```

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46

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630 Y5=Y5/4  
700 Z5=H5  
710 B16=SQR(B\*8-H6\*H6)  
720 REM X6=-B16\*COS(CTH16)  
730 X6=G/4-SQR(3)/2+SQR(B16\*B16-(G/2)\*G/2)  
740 Y6=SQR(3)\*G/2+SQR(B16\*B16-G/2\*G/2)  
750 Y6=Y6/4  
760 Z6=H6  
770 XL(4)=X4  
771 XL(5)=X5  
772 XL(6)=X6  
773 YL(5)=Y5  
774 YL(6)=Y6  
775 YL(4)=Y4  
776 ZL(4)=H4  
777 ZL(5)=H5  
778 ZL(6)=H6  
780 X1=XL(1)  
781 Y1=YL(1)  
782 Z1=ZL(1)  
783 X2=XL(2)  
784 Y2=YL(2)  
785 Z2=ZL(2)  
786 X3=XL(3)  
787 Y3=YL(3)  
788 Z3=ZL(3)  
790 R45=SQR((X5-X4)^2+(Y5-Y4)^2+(Z5-Z4)^2)  
800 R56=SQR((X5-X6)^2+(Y5-Y6)^2+(Z5-Z6)^2)  
810 R46=SQR((X4-X6)^2+(Y4-Y6)^2+(Z4-Z6)^2)  
820 P=((X5-X4)\*(X6-X4)+(Y5-Y4)\*(Y6-Y4)+(Z5-Z4)\*(Z6-Z4))/R45/R46  
830 F=SQR(1-F^2)  
840 N1=((Y5-Y4)\*(Z6-Z4)-(Y6-Y4)\*(Z5-Z4))/R45/R46  
850 N2=((X6-X4)\*(Z5-Z4)-(X5-X4)\*(Z6-Z4))/R45/R46  
860 N3=((X5-X4)\*(Y6-Y4)-(X6-X4)\*(Y5-Y4))/R45/R46  
870 N3=N3/P  
880 N2=N2/P  
890 N1=N1/P  
900 P1=(X1-X4)\*N1+(Y1-Y4)\*N2+(Z1-Z4)\*N3  
910 P2=(X2-X4)\*N1+(Y2-Y4)\*N2+(Z2-Z4)\*N3  
920 P3=(X3-X4)\*N1+(Y3-Y4)\*N2+(Z3-Z4)\*N3  
930 X7=X1-P1  
940 Y7=Y1-P2  
950 Z7=Z1-P3  
960 X8=X2-P1  
970 Y8=Y2-P2  
980 Z8=Z2-P3  
990 X9=X3-P1  
1000 Y9=Y3-P2  
1010 Z9=Z3-P3  
1020 R78=SQR((X7-X8)^2+(Y7-Y8)^2+(Z7-Z8)^2)  
1030 R79=SQR((X7-X9)^2+(Y7-Y9)^2+(Z7-Z9)^2)  
1040 XL(7)=X7:XL(8)=X8:XL(9)=X9:YL(7)=Y7:YL(8)=Y8:YL(9)=Y9:ZL(7)=Z7:ZL(8)=Z8:ZL(9)=Z9  
1050 X8=X16\*(II-2)+8:  
1060 Y7=Y(6\*(II-2)+7):  
1070 Y8=Y(6\*(II-2)+8):  
1080 Y9=Y(6\*(II-2)+9):  
1090 PCOS=((X8-X7)\*(X9-X7)+(Y8-Y7)\*(Y9-Y7)+(Z8-Z7)\*(Z9-Z7))/R78/R79  
1100 PSIN=SQR(1-PCOS\*PCOS)  
1110 N1=((Y8-Y7)\*(Z9-Z7)-(Y9-Y7)\*(Z8-Z7))/R78/R79  
1120 N1=N1/PSIN  
1130 N2=((X9-X7)\*(Z8-Z7)-(X8-X7)\*(Z9-Z7))/R78/R79  
1140 N2=N2/PSIN  
1150 N3=((X8-X7)\*(Y9-Y7)-(X9-X7)\*(Y8-Y7))/R78/R79  
1160 N3=N3/PSIN  
1170 B(1,1)=(X8-X7)/R78  
1180 B(1,2)=(Y8-Y7)/R78  
1190 B(1,3)=(Z8-Z7)/R78  
1200 B(2,1)=N1  
1210 B(2,2)=N2  
1220 B(2,3)=N3  
R89=SQR((X8-X9)^2+(Y8-Y9)^2+(Z8-Z9)^2)  
Z0=Z(6\*(II-2)+8):  
Y9=Y(6\*(II-2)+9):  
Z9=Z(6\*(II-2)+9):  
Y7=X(6\*(II-2)+7):  
Z9=Z(6\*(II-2)+9):

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1230 B(3,3)=N2
1240 B(3,3)=N3
1250 B(2,1)=P(3,2)*B(1,3)-B(1,2)*B(3,3)
1260 B(2,2)=B(1,1)*B(3,3)-B(3,1)*B(1,3)
1270 B(2,3)=B(1,2)*B(3,1)-B(1,1)*B(3,2)
1290 FOR IU=1 TO 9
1310 X(6*(II-1)+IU)=X(6*(II-1)+IU)+B(1,1)*YL(IU)+B(2,1)*YL(IU)+B(3,1)*ZL(IU):
      Y(6*(II-1)+IU)=Y(6*(II-1)+IU)+B(2,2)*YL(IU)+B(3,2)*ZL(IU)
      Z(6*(II-1)+IU)=Z(6*(II-1)+IU)+B(1,3)*XL(IU)+B(2,3)*YL(IU)+B(3,3)*ZL(IU)
1311 NEXT IU
1320 GOTO 1400
1330 REM THIS IS ONLY FOR THE FIRST CELL
1340 FOR FRT=1 TO 9:X(FRT)=XL(FRT):Y(FRT)=YL(FRT):Z(FRT)=ZL(FRT):NEXT FRT
1400 PRINT
1410 LPRINT :LPRINT TAB(50);"ANALYSIS COMPLETE";LPRINT TAB(50);"=====
1420 NEXT II
1430 END
5000 DATA -.6667,.01,2
5001 DATA 1,1,1
5002 DATA 1,1,1

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```

10 DIM XL(9),YL(9),ZL(9),X(200),Y(200),Z(200),B(3,3)
15 INPUT "PLEASE GIVE PROBLEMS NAME";P$;L1=LEN(P$);LPRINT :L=INT((120-L1)/2);LPRINT TAB(L);P$;LPRINT TAB(L);FOR I=1 TO L1:LPRINT
NT " ";NEXT I
20 D1=0
30 INPUT "PLEASE GIVE B " ;B
40 INPUT "PLEASE GIVE TOLERANCE " ;ERR0
50 INPUT "PLEASE GIVE THE NUMBER OF CELLS";NC
60 FOR I1=1 TO NC
70 PRINT CHR$(27);"Y";CHR$(27);"~k"
80 FOR I=1 TO 11:PRINT CHR$(27);"~R";FOR J=1 TO 80:PRINT " ";NEXT J;NEXT I :PRINT CHR$(27);"~r"
90 PRINT CHR$(27);"Y";CHR$(27);"~k"
100 G=1
110 PRINT TAB(5);"FOR CELL ";I1;PRINT TAB(5);"=====
115 LPRINT:LPRINT TAB(40);"++++++";LPRINT TAB(46);"U N I T N U M B E R " ;I1;LPRINT TA
B(46);"*****";LPRINT TAB(40);"++++++";LPRINT TAB(46);"U N I T N U M B E R " ;I1;LPRINT TA
120 INPUT "R45 ";R45:LPRINT TAB(20), "R45 = ";R45,
130 INPUT "R46 ";R46:LPRINT "R46 = ";R46,
140 INPUT "R56 ";R56:LPRINT "R56 = ";R56
LPRINT:LPRINT
150 A45=B*B-(1+R45*R45)*.5
160 A46=B*B-(1+R46*R46)/2
170 A56=B*B-(1+R56*R56)/2
180 REM FOR I=1 TO 130 :LPRINT "=";NEXT I
190 REM FOR I=1 TO 130:LPRINT "=";NEXT I
200 -HM=SQR (B*B-.25);STP=.1;HSTRT=0
210 PRINT CHR$(27);"Y";CHR$(27);"~k"
220 PRINT CHR$(27);"~B"CHR$(27);"~R";" H4"," H5"," H6"," DIFFERENCE " ;CHR$(27);"~b"CHR$(27);"~r"
230 FOR H4=HSTRT TO HM STEP STP
240 B14=SQR(B*B-H4*H4)
250 Y4=-SQR(B14*B14-(G/2)*(G/2))
260 Z4=H4
270 Y45=Y4-SQR(3)/2;F45=A45-(SQR(3)/4)*Y45
280 T1=4*Z4*Z4+Y45*Y45
290 T2=4*F45*Z4
300 T3=4*F45*F45-Y45*Y45*(B*B-.25)
310 NA=T2*T2-T1*T3;IF (NA<0) THEN S40
320 Z51=(T2+SQR(NA))/T1
330 Z52=(T2-SQR(NA))/T1
340 F46=A46-(SQR(3)/4)*Y45
350 W1=T1
360 W2=4*F46*Z4
370 W3=4*F46*F46-Y45*Y45*(B*B-.25)
380 MA=W2*W2-W1*W3;IF (MA<0) THEN S40
390 Z61=(W2+SQR(MA))/W1
400 Z62=(W2-SQR(MA))/W1
410 V25=SQR(B*B-Z51*Z51)
420 V16=SQR(B*B-Z61*Z61)
430 X5=(SQR(3)*G+2*SQR(V25*V25-V25*G*G/4))/4
440 X6=(SQR(3)*G+2*SQR(V16*V16-V16*G*G/4))/4
450 S56=Z61*Z51-Z51*W3*W3;D=S56-A56
460 D=CDBL(D);D1=CDBL(D1);IF ABS(D)<ERR0 THEN S70
470 IF D1<0 THEN S80
480 D1=0
490 REM LPRINT TAB(1);H4;TAB(19);Z51;TAB(39);Z52;TAB(59);Z61;TAB(79);Z62;TAB(99);S56;TAB(119):D
500 PRINT H4,Z51,Z61,D
510 REM FOR I=1 TO 130 :LPRINT "-" ;NEXT I
520 GOTO S50
530 IF (NA<0) THEN S40
540 LPRINT TAB(1);"COMPLEX ROOTS":GOTO S50
550 NEXT H4
560 GOTO S90
570 PRINT:PRINT CHR$(27);"~B";H4,Z51,Z61;CHR$(27);"~b";GOTO S90
580 PRINT CHR$(27);"~Y";CHR$(27);"~R";PRINT CHR$(27);"~r";PRINT TAB(40);"++++++";LPRINT TAB(46);"U N I T N U M B E R " ;I1;LPRINT TA

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500 0-1:HS=ZSI:H6=ZBI:PRINT " H5 = ";HS;PRINT " H6 = ";H6;PRINT " H4 = ";H4
600 HM=SQR(B*B-(G*G/3))
610 XL(1)=0:YL(1)=0:ZL(1)=0:XL(2)=0:YL(2)=0:ZL(2)=0:XL(3)=G/2:YL(3)=G*SQR(3)/2:ZL(3)=0
620 B14=SQR(B*B-H4*H4)
630 B25=SQR(B*B-H5*H5)
640 X4=G/2
650 Y4=-SQR(B14*B14-(G/2)*(G/2))
660 Z4=H4
670 X5=3*G/4+(SQR(3)/2)*SQR(B25*B25-(G/2)*(G/2))
680 Y5=SQR(3)*G/2+SQR(B25*B25-(G/2)*(G/2))
690 Y5=Y5/4
700 Z5=H5
710 B16=SQR(B*B-H6*H6)
720 REM X6=-B16*COS(CTH16)
730 X6=G/4-SQR(3)/2*SQR(B16*B16-(G/2)*G/2)
740 Y6=SQR(3)*G/2+SQR(B16*B16-G/2*G/2)
750 Y6=Y6/4
760 Z6=H6
770 XL(4)=X4:XL(5)=X5:XL(6)=X6:YL(5)=Y5:YL(6)=Y6:YL(4)=Y4:ZL(4)=H4:ZL(5)=H5:ZL(6)=H6
780 X1=XL(1):Y1=YL(1):Z1=ZL(1):X2=XL(2):Y2=YL(2):Z2=ZL(2):X3=XL(3):Y3=YL(3):Z3=ZL(3)
790 R45=SQR((X5-X4)^2+(Y5-Y4)^2+(H5-H4)^2)
800 R56=SQR((X5-X6)^2+(Y5-Y6)^2+(H5-H6)^2)
810 R46=SQR((X4-X6)^2+(Y4-Y6)^2+(H4-H6)^2)
820 PRINT R45,R56,R46
830 F=((X5-X4)*(X6-X4)+(Y5-Y4)*(Y6-Y4)+(H5-H4)*(H6-H4))/R45/R46
840 P=SQR(1-F^2)
850 N1=((Y5-Y4)*(Z6-Z4)-(Y6-Y4)*(Z5-Z4))/R45/R46
860 N1=N1/P
870 N2=((X6-X4)*(Z5-Z4)-(X5-X4)*(Z6-Z4))/R45/R46
880 N2=N2/P
890 N3=((X5-X4)*(Y6-Y4)-(X6-X4)*(Y5-Y4))/R45/R46
900 N3=N3/P
910 P1=(X1-X4)*N1+(Y1-Y4)*N2+(Z1-Z4)*N3
920 P2=(X2-X4)*N1+(Y2-Y4)*N2+(Z2-Z4)*N3
930 P3=(X3-X4)*N1+(Y3-Y4)*N2+(Z3-Z4)*N3
940 X7=X1-P1
950 Y7=Y1-P2
960 Z7=Z1-P3
970 X8=X2-P1
980 Y8=Y2-P2
990 Z8=Z2-P3
1000 X9=X3-P1
1010 Y9=Y3-P2
1020 Z9=Z3-P3
1030 R73=SQR((X7-X8)^2+(Y7-Y8)^2+(Z7-Z8)^2)
1040 R75=SQR((X7-X9)^2+(Y7-Y9)^2+(Z7-Z9)^2)
1050 XL(7)=X7:XL(8)=X8:XL(9)=X9:YL(7)=Y7:YL(8)=Y8:YL(9)=Y9:ZL(7)=Z7:ZL(8)=Z8:ZL(9)=Z9
1060 LPRINT TAB(48);"LOCAL CO-ORDINATE SYSTEM ";LPRINT TAB(48);"=====
";Z:LPRINT TAB(41);"=====";"=";"="="
1070 FOR Y6=1 TO 9:LPRINT TAB(41);Y5,XL(Y6),YL(Y6),ZL(Y6);NEXT Y6:LPRINT:LPRINT
1080 IF I=1 GO TO 1340
1090 X8=X(6*(I1-2)+8):Y8=Y(6*(I1-2)+8):Z8=Z(6*(I1-2)+8):X7=X(6*(I1-2)+7):Y7=Y(6*(I1-2)+7):Z7=Z(6*(I1-2)+7):X9=X(6*(I1-2)+9):Y9=Y(6*(I1-2)+9):Z9=Z(6*(I1-2)+9)
1100 R335=((X8-X7)*(X9-X7)+(Y8-Y7)*(Y9-Y7)+(Z8-Z7)*(Z9-Z7))/R78/R79
1110 P51=SQR(1-PCOS*PCOS)
1120 N1=((Y8-Y7)*(Z9-Z7)-(Y9-Y7)*(Z8-Z7))/R78/R79
1130 N1=N1/PSIN
1140 N2=((X8-X7)*(Z8-Z7)-(X8-X7)*(Z9-Z7))/R78/R79
1150 N2=N2/PSIN
1160 N3=((X8-X7)*(Y9-Y7)-(X9-X7)*(Y8-Y7))/R78/R79
1170 N3=N3/PSIN
1175 LPRINT TAB(13);",,,";"NORMAL VECTOR":LPRINT TAB(13);",,,";"=====
";LPRINT TAB(18);",,,";"N1 = ";N1,"N2 = ";N2,"N3 = ";N3
1180 R(1,1)=(X8-X7)/R78
1190 R(1,2)=(Y8-Y7)/R78
1200 R(1,3)=(Z8-Z7)/R78
1210 R(1,4)=(X8-Z7)/R78

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1220 B(3,1)=N1
1230 B(3,2)=N2
1240 B(3,3)=N3
1250 B(2,1)=B(3,2)*B(1,3)-B(1,2)*B(3,3)
1260 B(2,2)=B(1,1)*B(3,3)-B(3,1)*B(1,3)
1270 B(2,3)=B(1,2)*B(3,1)-B(1,1)*B(3,2)
1272 LPRINT
1275 LPRINT TAB(53); "TRANSFORMATION MATRIX"; LPRINT TAB(53); "=====
1280 LPRINT:FOR PLO=1 TO 3:LPRINT TAB(42); "I";:FOR LOP=1 TO 3:LPRINT ,B(PLO,LOP);:NEXT LOP:LPRINT TAB(97); "I";:LPRINT:NEXT PLO:LPR
INT :LPRINT
1290
1310 FOR IU=1 TO 9
1310 X(6*(II-1)+IU)=X(6*(II-1)+1)+B(1,1)*XL(IU)+B(2,1)*YL(IU)+B(3,1)*ZL(IU):Y(6*(II-1)+IU)=Y(6*(II-1)+1)+B(1,2)*X
L(IU)+B(2,2)*YL(IU)+B(3,2)*ZL(IU):Z(6*(II-1)+IU)=Z(6*(II-1)+1)+B(1,3)*XL(IU)+B(2,3)*YL(IU)+B(3,3)*ZL(IU):NEXT IU
1320 GOTO 1350
1330 REM THIS IS ONLY FOR THE FIRST CELL
1340 FOR FRT=1 TO 9:(FRT)=XL(FRT):Y(FRT)=YL(FRT):Z(FRT)=ZL(FRT):NEXT FRT
1350 LPRINT:LPRINT TAB(47); "GLOBAL CO-ORDINATE SYSTEM":LPRINT TAB(47); "=====
B(43); "GLOBAL NO. "; TAB(61); "X-COORD. "; TAB(73); "Y-COORD. "; TAB(88); "Z-COORD. "
1355 LPRINT TAB(33); "===== "; TAB(43); "===== "; TAB(61); "===== "; TAB(73); "===== "; TAB(88); "=====
LPRINT
1357 FOR TY=1 TO 9
1359 LPRINT TAB(33); TY; TAB(43); 6*(II-1)+TY; TAB(61); X(6*(II-1)+TY); TAB(73); Y(6*(II-1)+TY); TAB(88); Z(6*(II-1)+TY); NEXT TY:NEXT II:LPR
INT :LPRINT TAB(40); "+++++"; TAB(40); "=====
1370 LPRINT:LPRINT:LPRINT TAB(40); "GLOBAL CO-ORDINATES OF FINAL CONFIGURATION":LPRINT TAB(40);
=====
1380 LPRINT TAB(20); "LOCAL NO. "; TAB(35); "GLOBAL NO. "; TAB(55); "X-COORD. "; TAB(75); "Y-COORD. "; TAB(95); "Z-COORD. "
1390 LPRINT TAB(20); "===== "; TAB(35); "===== "; TAB(55); "===== "; TAB(75); "===== "; TAB(95); "=====
NC:FOR II=1 TO 9
1400 LPRINT TAB(20); II; TAB(35); 6*(I-1)+II; TAB(75); Y(6*(I-1)+II); TAB(95); Z(6*(I-1)+II);
=====
1420 END

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\*\*\*\*\*  
UNIT NUMBER 1  
\*\*\*\*\*

LOCAL CO-ORDINATE SYSTEM

NODE	X	Y	Z
1	0	0	0
2	1	0	0
3	.5	.866025	.3333
4	.5	-.288714	.333367
5	.999967	.577331	.333367
6	3.34829E-05	.577331	.666645
7	0	-5.15475E-05	.666645
8	1	-5.15475E-05	.666645
9	.5	.865974	.666779

GLOBAL CO-ORDINATE SYSTEM

LOCAL NO.	GLOBAL NO.	X-COORD.	Y-COORD.	Z-COORD.
1	0	0	0	0
2	1	0	0	0
3	.5	.866025		
4	.5	-.288714		.3333
5	.999967	.577331		.333367
6	3.34829E-05	.577331		.333367
7	0	-5.15475E-05		.666645
8	1	-5.15475E-05		.666645
9	.5	.865974		.666779

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UNIT NUMBER 2  
\*\*\*\*\*

LOCAL CO-ORDINATE SYSTEM

NODE	X	Y	Z
1	0	0	0
2	1	0	0
3	.5	.666025	.2472
4	.5	-.365153	.380875
5	.942442	.544119	.296735
6	-.0324797	.596103	.468538
7	-.0429944	-.0479607	.64866
8	.940477	-.0663983	.64866
9	.432774	.791034	.732607

NORMAL VECTOR  
 =====  
 N1 = 0      N2 = -1.54651E-04      N3 = 1  
 =====  
 TRANSFORMATION MATRIX  
 =====

I	1	0	0	I
I	0	1	1.54651E-04	I
I	0	-1.54651E-04	1	I

GLOBAL CO-ORDINATE SYSTEM  
 =====

LOCAL NO.	GLOBAL NO.	X-COORD.	Y-COORD.	Z-COORD.
1	7	0	-5.15475E-05	.666645
2	8	1	-5.15475E-05	.666645
3	9	.5	.865974	.666779
4	10	.5	-.365243	.913788
5	11	.942442	.544009	1.0475
6	12	-.0324797	.596005	.963472
7	13	-.0429944	-.0480847	1.13518
8	14	.940477	-.0655502	1.31529
9	15	.432774	.790869	1.39937

\*\*\*\*\*  
 UNIT NUMBER 3  
 \*\*\*\*\*

LOCAL CO-ORDINATE SYSTEM  
 =====

NODE	X	Y	Z
1	0	0	0
2	1	0	0
3	.5	.866025	.3476
4	.5	-.271328	.347558
5	.965023	.568703	.347558
6	.0149769	.568703	.695173
7	0	3.4479E-05	.695173
8	1	3.4479E-05	.695087
9	.5	.866025	.695087

NORMAL VECTOR  
 =====

N1 = -.180121      N2 = -.201076      N3 = .962873

TRANSFORMATION MATRIX  
 =====

I	.983472	-.0184655	.180119	I
I	-.0184376	.979402	.501079	I

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GLOBAL CO-ORDINATE SYSTEM

LOCAL NO.	GLOBAL NO.	X-COORD.	Y-COORD.	Z-COORD.
1	13	-.0429944	-.0480847	1.13518
2	14	.940477	-.0665502	1.31529
3	15	.432774	.790869	1.39937
4	16	.391134	-.392951	1.50537
5	17	.85266	.42083	1.76161
6	18	-.101353	.438742	1.58688
7	19	-.168211	-.187834	1.80455
8	20	.815261	-.206299	1.98466
9	21	.307573	.651137	2.06866

\*\*\*\*\*

UNIT NUMBER 4

\*\*\*\*\*

LOCAL CO-ORDINATE SYSTEM

NODE	X	Y	Z
1	0	0	0
2	1	0	0
3	.5	.866025	.2728
4	.5	-.346446	.27289
5	1.04997	.6062	.27289
6	-.0499691	.6062	.545666
7	0	-5.18601E-05	.545666
8	1	-5.18601E-05	.545666
9	.5	.865374	.54583

NORMAL VECTOR

N1 = -.180123 N2 = -.200979 N3 = .962893

TRANSFORMATION MATRIX

I	.983472	-.0184655	.180119
I	-.0184198	.979422	.200984
I	-.180123	-.200979	.962893

GLOBAL CO-ORDINATE SYSTEM

LOCAL NO.	GLOBAL NO.	X-COORD.	Y-COORD.	Z-COORD.
1	19	-.168211	-.187834	1.80455
2	20	.815261	-.206299	1.98466
3	21	.307573	.651137	2.06866

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23      .804084      .331658
24      -.277674      .351969
25      -.266497      -.297552
26      .716975      -.316017
27      .209258      .541386

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*****
UNIT NUMBER 5
*****

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LOCAL CO-ORDINATE SYSTEM

NODE	X	Y	Z
1	0	0	0
2	1	0	0
3	.5	.866025	0
4	.5	-.253369	.3609
5	1.019	.588321	.312989
6	9.67237E-03	.571766	.342687
7	.0209821	.028559	.723007
8	1.01933	.0263093	.671579
9	.518207	.890808	.632539

NORMAL VECTOR

N1 = -.18012 N2 = -.201165 N3 = .962855

TRANSFORMATION MATRIX

I	.983472	-.0184655	.180119	I
I	-.018454	.979383	.201166	I
I	-.18012	-.201165	.962855	I

GLOBAL CO-ORDINATE SYSTEM

LOCAL NO.	GLOBAL NO.	X-COORD.	Y-COORD.	Z-COORD.
1	25	.100497	-.297552	2.32995
2	26	.716975	-.316017	2.51007
3	27	.209258	.541386	2.59423
4	28	.16491	-.62753	2.71654
5	29	.66843	.196861	2.93321
6	30	-.32926	.193311	2.77627
7	31	-.377697	-.41662	3.04141
8	32	.614535	-.425706	3.16549
9	33	.112763	.438064	3.21159

GLOBAL CO-ORDINATES OF FINAL CONFIGURATION

\*\*\*\*\*

LOCAL NO.	COORD. NO.	X-COORD.	Y-COORD.	Z-COORD.
1	0	0	0	0
2	1	.866025	0	0
3	5	-.388714	0	0
4	5	.999967	-.388714	.3333
5	6	3.34829E-05	.577331	.333367
6	0	0	.577331	.333367
7	1	0	-5.15475E-05	.666645
8	1	0	-5.15475E-05	.666645
9	5	0	.865974	.666779
10	0	0	-5.15475E-05	.666645
11	1	0	-5.15475E-05	.666645
12	5	.942442	.865974	.666779
13	10	.942442	-.365243	.913788
14	12	-.0324797	.544009	1.0476
15	12	-.043944	.596005	.963472
16	13	.940477	-.0480847	1.13518
17	14	.432774	-.0665502	1.31529
18	15	.432774	.790869	1.39937
19	13	-.043944	-.0480847	1.13518
20	14	.940477	-.0665502	1.31529
21	15	.432774	.790869	1.39937
22	16	.391134	-.392951	1.50537
23	17	.85366	.42083	1.76161
24	18	-.101353	.438742	1.58688
25	19	-.168211	-.187834	1.80455
26	20	.815261	-.206299	1.98466
27	21	.307573	.651137	2.06866
28	19	-.168211	-.187834	1.80455
29	20	.815261	-.206299	1.98466
30	21	.307573	.651137	2.06866
31	22	.280769	-.59121	2.08765
32	23	.804084	.331658	2.37826
33	24	-.277674	.351969	2.18015
34	25	-.266497	-.297552	2.32995
35	26	.716975	-.316017	2.51007
36	27	.209258	.541386	2.59423
37	25	-.266497	-.297552	2.32995
38	26	.716975	-.316017	2.51007
39	27	.209258	.541386	2.59423
40	28	.16491	-.62753	2.71654
41	29	.66843	.136861	2.93321
42	30	-.32926	.193311	2.77667
43	7	-.377697	-.4.662	3.04141
44	8	.614535	-.42.706	3.16548
45	9	.112763	.438454	3.21159

ANALYSIS COMPLETE  
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