# Feasibility of a Nuclear <br> Gauge for Fuel Quantity <br> Measurement Aboard Aircraft 

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## N/SA

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## Summary

Capacitance fuel gauges have served as the basis for fuel quantity indicating systems in aircraft for several decades. However, there have been persistent reports by the airlines that these gauges often give faulty indications due to microbial growth and other contaminants in the fuel tanks. This report describes the results of a feasibility study of using gamma ray attenuation as the basis for measuring fuel quantity in the tanks. Studies with a weak $\mathrm{Am}^{241} 59.5-\mathrm{keV}$ radiation source indicate that it is possible to continuously monitor the fuel quantity in the tanks to an accuracy of better than 1 percent. These measurements also indicate that there are easily measurable differences in the physical properties and resultant attenuation characteristics of JP-4, JP-5, and Jet A fuels. The experimental results, along with a suggested source-detector geometrical configuration, are described.

## Introduction

Capacitance fuel gauges have served as the basis for fuel quantity indicating systems in aircraft for several decades. These gauges, in the form of concentric cylinders, are mounted vertically at several locations inside the fuel tanks (ref. 1). The summations of their indications give the total tank fuel content at any time. However, there have been persistent reports (ref. 2) by the airlines that the capacitance gauges often give faulty indications of tank fuel contents. The problem has been attributed to microbial growth and/or contaminants in the fuel tanks. The microbes can occur in storage tanks, delivery lines, pump trucks, and consequently, in the aircraft fuel tanks. The microbes attack the capacitance cylinder coatings and thus expose the cylinder surfaces (electrodes) for subsequent corrosion and electrical noise in the capacitance bridge circuit. They also corrode the output signal leads. It is thus highly desirable that a fuel quantity indicating system insensitive to fuel contamination be developed. Such a system should be highly accurate (better than 1 percent), safe to use and operate, and inexpensive.

An investigation of the feasibility of using gamma ray attenuation as the basis for measuring the fuel quantity in aircraft tanks has been conducted. The results of these studies are described in the following sections.

## Principle of Operation of a Nuclear Gauge

The operation of a nuclear gauge is based on the attenuation of gamma rays passing through matter. As a result of interaction of gamma rays with the atoms in the test medium, the number of unaffected
primary photons arriving at the detector is a function of the path length in the test medium. For a uniform medium, it is given by the following expression (ref. 3):

$$
\begin{equation*}
I_{x}=I_{o} e^{-\mu x} \tag{1}
\end{equation*}
$$

where

| $I_{x}$ | number of unaffected primary <br> photons transmitted through test <br> medium |
| :--- | :--- |
| $I_{o}$ | number of photons incident on test <br> medium |
| $\mu$ | linear attenuation coefficient for <br> incident photons in test medium |
| $x$ | path length in test medium |

Clearly, such a gauge will be more sensitive if the attenuation coefficient ( $\mu$ ) is large for the incident photons. This dictates the choice of low-energy (less than 100 keV ) photon sources. Two plausible candidate sources that meet the necessary criteria of low photon energy, long source half-life, and a wellresolved photon spectrum are $\mathrm{Am}^{241}$ ( 458 years) and $\mathrm{Cd}^{109}$ (453 days).

The decay schemes (ref. 4) for these two sources are shown in figures 1 and 2 , respectively. It is noted that the $59.5-\mathrm{keV}$ radiation from the $\mathrm{Am}^{241}$ source results from a super-allowed electric dipole (E1) transition in $\mathrm{Np}^{237}$, whereas the 87.7 -keV radiation from the $\mathrm{Cd}^{109}$ source arises from a weakly allowed electric octopole (E3) transition in $\mathrm{Ag}^{109}$. The latter transition is strongly internally converted and produces a large, lower energy Ag K X-ray flux. For example, a $10-\mathrm{mCi} \mathrm{Am}^{241}$ disc source emits $7.4 \times 10^{6}$ photons ( 59.5 keV ) per second per steradian, whereas a $10-\mathrm{mCi} \mathrm{Cd}^{109}$ source emits $2.6 \times 10^{7}$ photons ( 22.6 keV ) per second per steradian (ref. 5). The relative intensities of gamma rays and characteristic X-Rays emitted from these sources are summarized in table I (ref. 4). Thus, even though the choice of a $\mathrm{Cd}^{109}$ source will necessitate changing the source every 3 years or so, $\mathrm{Cd}^{109}$ still appears to be a viable candidate source by virtue of its large lower energy photon yield.

## Experimental Procedures for Measuring Attenuation Coefficients

Since the exact compositions of aviation fuels are seldom known (refs. 6 and 7), it was not possible to calculate their attenuation coefficients for Am ${ }^{241}$ and $\mathrm{Cd}^{109}$ gamma rays. It was therefore decided to determine the attenuation coefficients of selected types of fuels experimentally.

Attenuation coefficients of several samples of commercial aviation fuels were measured in the narrow beam geometry illustrated in figure 3 . The fuel cells were made of glass and were fabricated in the form of 3 -in. ( $7.62-\mathrm{cm}$ ) diameter flat-ended cylinders of three different lengths for easy data reduction. The gamma rays were detected with a $2-\mathrm{in}$. $(5.08-\mathrm{cm}$ ) diameter $\times$ $2-\mathrm{in}$. ( $5.08-\mathrm{cm}$ ) thick NaI ( Tl ) crystal coupled to a high-gain photomultiplier. Figure 4 shows the geometrical details of the source, collimators, fuel cells, and detector assembly.

Measurements were made with empty fuel cells and cells filled with the test fluids. To further test the sensitivity of the system, measurements were also made with distilled water in the fuel cells. Typical $\mathrm{Am}^{241}$ and $\mathrm{Cd}^{109}$ spectra are shown in figures 5 and 6.

For the $\mathrm{Am}^{241}$ source, the single-channel analyzer (SCA) limits were adjusted to accept the strong 59.5keV peak. For the $\mathrm{Cd}^{109}$ source, the SCA limits were set to accept the weaker $87.7-\mathrm{keV}$ total capture peak rather than the stronger, but unresolved, lower energy $\mathrm{Ag} \mathrm{K}_{\alpha}(22.1 \mathrm{keV})$ and $\mathrm{Ag} \mathrm{K}_{\beta}(25.0 \mathrm{keV})$ peaks.

The nominal radioactive source strengths readily available for this test were of the order of $10 \mu \mathrm{Ci}$ $\left(\mathrm{Am}^{241}\right)$ and $100 \mu \mathrm{Ci}\left(\mathrm{Cd}^{109}\right)$. They provided good counting statistics for all test fluids over a period of 10 minutes. Measurements were made with and without the source in each case to subtract the counts due to cosmic rays and other background sources of radiation.

The attenuation coefficients were measured for water, JP-4 fuel, JP-5 fuel, Jet A fuel, regular leaded automobile gasoline, and unleaded automobile gasoline.

## Data Reduction and Results

Counts were recorded for 10 minutes for each source for the three fuel cells filled with the test fluids. The geometrical details of the configurations incorporating test cells G-2, G-3, and G-4 are shown in figure 4. Typical results are summarized in table II.

As illustrated in figure 4, the photons have to pass through air, glass fuel cell ends, test fluid, and a $0.079-\mathrm{cm}$-thick aluminum housing for the $\mathrm{NaI}(\mathrm{Tl})$ crystal before arriving at the detector surface, that is,

$$
\begin{align*}
I_{\mathrm{x}}= & I_{\mathrm{o}}\left(e^{-\mu_{\text {air }} x_{\text {air }}} e^{-\mu_{\mathrm{glass}} x_{\mathrm{glass}}}\right. \\
& \left.\times e^{-\mu_{\text {fluid }} x_{\text {fluid }}} e^{-\mu_{A 1} x_{A l}}\right) \tag{2}
\end{align*}
$$

The values of $\mu_{\text {air }}$ and $\mu_{\mathrm{Al}}$ at 59.5 keV and 87.7 keV have been reported by a number of authors (refs. 8
to 10 ). With these values, $\mathrm{I}_{0}$ can be easily calculated from equation (2) if the entire path length is made up of air and aluminum. If an empty glass fuel cell is introduced in the path of the beam, the drop in the counting rate provides a direct measure of $\mu_{\text {glass }}$ for the incident photons. If the fuel cells are filled with the test fluids, the changes in the counting rates will reflect the effects of attenuation characteristics of the test fluids. The experimental values of linear attenuation coefficients of the various test fluids are summarized in table III. These values are based on several independent sets of data of the type summarized in table II.

Since the mass attenuation coefficients ${ }^{1}$ of the media are of more fundamental value than the linear attenuation coefficients (ref. 3), it was necessary to determine the densities of the test fluids. The densities of all the fluids were measured with a standard $50-\mathrm{ml}$ pycnometer, and these values were used to calculate the mass attenuation coefficients of the test fluids. These results are also included in table III. It is interesting to note that there are easily measurable differences in the attenuation coefficients of various test fluids.

Subsequent to the measurements of the respective attenuation coefficients of all the test fluids for the $\mathrm{Am}^{241}$ and $\mathrm{Cd}^{109}$ gamma rays, it was finally decided to test the sensitivity of attenuation of low-energy photons as the basis for a fuel gauging system aboard aircraft. The wing tank geometry for a Boeing 737 airplane was selected for the computer model as representative of all aircraft with positive wing tip inclination with respect to the horizontal while on the ground. The computational procedures and the program developed for calculations for an $\mathrm{Am}^{241}$ gamma ray source and Jet A fuel test medium are described below.

## Computational Procedure

The computer program WNGTNK is written in FORTRAN Version 5 language for the Control Data CYBER 170 series digital computer system with network operating system (NOS) 2.3. The program requires approximately 40000 octal locations of core storage. A typical case requires less than 4 central processing unit (CPU) seconds on the CYBER 173.

The wing tank (Boeing 737) modeled by the program is illustrated in figure 7. For purposes of modeling, each of the 14 compartments in this figure is approximated by a rectangular box. Any similar wing

[^0]tank can be modeled by this technique by simply adjusting the number of compartments and the dimensions of each rectangular box. Figure 8 illustrates the tank model as viewed from the front of the aircraft with the fuselage (not shown) to the left. The program provides the user with the capability of specifying the height of the bottom of each compartment, $B_{i}$, to simulate the bending of the wing associated with flight conditions. The solid dot (.) in each compartment depicts the source location, SL, and the detectors are assumed to be fixed to the bottom of each compartment. Table IV summarizes the specific data used in the modeling of the Boeing 737, where $W_{i}, H_{i}$, and $D_{i}$ are the compartment widths, heights, and depths, respectively.

Once the tank geometry has been defined, the program steps through fixed percentages of tank fuel capacity. For each amount of fuel, the fuel level is computed with the assumption of a level fuel surface. With the fuel level known, the path length between each source-detector pair occupied by fuel or air is determined. From these path lengths, the number of counts is determined. The baffles between compartments contained in the wing structure are assumed to absorb radiation, so there is no interference between adjacent compartments.

Program input consists of 14 numbers, separated by commas, representing the height, $B_{i}$, of each compartment bottom in inches. Program output includes both tabular and graphic results.

Typical results corresponding to the configuration of figure 8 are included as table V and are illustrated in figure 9. These data were acquired with a source strength of about $30 \mu \mathrm{Ci}$ at each station in a counting interval of 1 second. Obviously, this system has a fast response time (approximately 1 second) and high resolution (approximately 1 percent). In this figure, each line depicts the relationship between counts and fuel expended for a specific compartment, with the lines toward the right nearer the wing tip and the lines toward the left nearer the fuselage. In particular, note that when the tank is full, the counting rates are the same in each compartment, since the path lengths through fuel are all equal. As fuel is expended, the counting rates change first in those compartments near the wing tip. After approximately 35 percent of the fuel has been expended, the compartment nearest the tip is empty and shows no further change in counting rate. Also note that the source in compartment 1 is completely immersed in the fuel until approximately 85 percent of the fuel is expended and begins to show a change in counting rate as the fuel is reduced below this level. Figure 9 also shows that significant changes in counts can be
observed in one or more compartments as the fuel level varies, regardless of the tank contents.

A listing of the computer program used in this analysis is included as an appendix.

## Discussion

For the sake of specificity, we will confine our discussions to the results for an $\mathrm{Am}^{241}(59.5-\mathrm{keV})$ gamma source. Similar results are expected for a $\mathrm{Cd}^{109}(87.7-\mathrm{keV})$ gamma source.

As seen from the data in table $V$, the counting rate is constant at all stations when the tank is full. A 1-percent reduction in the fuel content in the tank causes a large increase (about 56.9 percent) in the counting rate at the wing tip detector (station 14). A further reduction of 1 percent in the fuel causes an additional increase (about 26.6 percent) in the counting rate at the wing tip detector. It also results in a counting rate increase of about 16.2 percent at station 13. These counting rate changes are easily measurable. The same trend continues as more fuel is consumed. For example, when 10 percent of the fuel has been consumed, the total cumulative counting rate increases at stations 14, 13, and 12 are 238.6, 114.6, and 35.9 percent, respectively. At the other end of the spectrum when the tank is nearly empty, the counting rates in the outer station detectors have stabilized, but the counting rates at the stations near the fuselage are changing fast. For example, when the tank is only 5 percent full, the counting rates at stations 1, 2, and 3 are 330.1, 521.0, and 822.6 percent higher than the counting rate for the full tank. A further reduction of 1 percent in the fuel causes the counting rates to increase to 392.3, 619.1 , and 977.1 percent of the values for the full tank, respectively.

From these data it is apparent that the fuel quantity gauging system detailed in this report is capable of detecting changes as low as 1 percent in the fuel contents at the two extreme limits, that is, when the tank is almost full and when it is almost empty. A careful examination of table V illustrates that a similar degree of sensitivisty exists for all levels of tank fuel contents.

From the foregoing discussion, it is apparent that a continuous monitoring of counting rates at all the detector stations should enable continuous tracking of airplane fuel tank contents with a high degree of sensitivity.

## Concluding Remarks

It has been demonstrated that a suitably designed nuclear gauge should enable a continuous monitoring of the tank fuel contents to an accuracy of better
than 1 percent. Such accurate information-both at the point of flight origination when the tanks are presumably full and at the final destination when the tanks are almost empty-should prove very useful to the airlines. It should provide reliable information about the payload capacity at the beginning of the flight and safety margin near the end of the flight. The nuclear gauge is not expected to be susceptible to the fouling and corrosion problems experienced by the conventional capacitance gauges, since both the source and the radiation detector are sealed. Any algae or microbial growth on the source and detector windows can be easily removed during scheduled periodic maintenance checks of the gauging system.

An added advantage of the nuclear gauge is its inherent capability to detect water buildup in the tank. Since water is expected to gravitate toward the fuselage, any reduction in the counting rates at stations 1 through 5 when the tank is at least half full can be used to infer the quantity of water in the tank. It is also a self-calibrating system with a high degree of cross-checking capability. This capability renders the nuclear gauging system independent of any background count rate changes with altitude. (In any case, changes in background count rate at altitudes less than 10 miles are expected to be minimal in the SCA window centered at 59.5 keV .)

It should perhaps be noted that despite the large low-energy photon flux obtainable with a $\mathrm{Cd}^{109}$ source, an $\mathrm{Am}^{241}$ source would be more economical, since it would require no source replacement because of its long half-life. It would also be comparatively safer to handle and/or shield because of its lower energy. As a matter of fact, $\mathrm{Am}^{241}$-based densitometers are currently in use aboard some aircraft. The licensing requirements for an $\mathrm{Am}^{241}$-based fuel quantity measurement system would be no different from what they are for those aircraft. By an appropriate choice of the $\mathrm{Am}^{241}$ source strength, the response time of the nuclear gauge can be safely arranged to be less than 1 second.

The effects of temperature on the fuel volume can be easily taken care of by simultaneousbut independent-measurements of temperature and density. These measurements will also enable realtime computation of fuel mass (as opposed to fuel volume) at any time in flight or on the ground.

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## TABLE I. RELATIVE INTENSITIES OF CHARACTERISTIC X-RAYS AND GAMMA RAYS EMITTED FROM Am ${ }^{241}$ AND Cd ${ }^{109}$ RADIOACTIVE SOURCES

| $\mathrm{Am}^{241}$ source |  | $\mathrm{Cd}^{109}$ source |  |
| :---: | :---: | :---: | :---: |
| Photon <br> energy <br> $(\mathrm{keV})$ | Relative <br> intensity | Photon <br> energy <br> $(\mathrm{keV})$ | Relative <br> intensity |
| $11.89\left(\mathrm{~Np} L_{l}\right)$ | 2.2 | $22.1\left(\mathrm{Ag} K_{\alpha}\right)$ | 25.5 |
| $13.90\left(\mathrm{~Np} L_{\alpha}\right)$ | 37.5 | $25.0\left(\mathrm{Ag} \mathrm{K} K_{\beta}\right)$ | 5.0 |
| $17.80\left(\mathrm{~Np} L_{\beta}\right)$ | 51.2 | 87.7 | 1.0 |
| $20.80\left(\mathrm{~Np} L_{\gamma}\right)$ | 13.8 |  |  |
| 26.35 | 7.0 |  |  |
| 59.50 | 100.0 |  |  |

TABLE II. COUNTS PER 10-MINUTE INTERVAL FOR VARIOUS TEST MEDIA WITH $\mathrm{Am}^{241}$ AND Cd ${ }^{109}$ SOURCES ${ }^{\text {a }}$

| Test medium | $\mathrm{Am}^{241}$ source |  |  | $\mathrm{Cd}^{109}$ source |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { Cell G-2 } \\ L_{2}=4.982 \mathrm{~cm} \\ \hline \end{gathered}$ | $\begin{gathered} \text { Cell G-3 } \\ L_{2}=7.522 \mathrm{~cm} \\ \hline \end{gathered}$ | $\begin{gathered} \text { Cell G-4 } \\ L_{2}=10.062 \mathrm{~cm} \end{gathered}$ | $\begin{gathered} \text { Cell G-2 } \\ L_{2}=4.982 \mathrm{~cm} \end{gathered}$ | $\begin{gathered} \text { Cell G-3 } \\ L_{2}=7.522 \mathrm{~cm} \end{gathered}$ | $\begin{gathered} \text { Cell G-4 } \\ L_{2}=10.062 \mathrm{~cm} \end{gathered}$ |
| Air (no cell) | 75446 | 49988 | 35710 | 43650 | 30476 | 23184 |
| Air (empty cell) | 54489 | 36705 | 25491 | 35404 | 24897 | 18906 |
| JP-4 fuel | 27880 | 13899 | 7480 | 21080 | 12950 | 9192 |
| JP-5 fuel | 26859 | 13204 | 7018 | 20765 | 12569 | 9018 |
| Jet A fuel | 26816 | 12918 | 7229 | 20322 | 12431 | 8802 |
| Leaded gasoline | 28732 | 14462 | 7981 | 21110 | 13105 | 9233 |
| Unleaded gasoline | 28966 | 14353 | 8094 | 20948 | 13107 | 9202 |
| Water | 22095 | 9832 | 5267 | 18455 | 10937 | 8001 |
| Background | 1817 | 1850 | 1876 | 5319 | 5391 | 5270 |

${ }^{\text {a }}$ See figure 4 for geometrical details of fuel cell and associated shields/collimators.

TABLE III. SUMMARY OF ATTENUATION COEFFICIENTS FOR VARIOUS TEST FLUIDS

| Test fluid | Test fluid density, $\rho$, $\mathrm{g} / \mathrm{cm}^{3}$ | $\mathrm{Am}^{241}(59.5 \mathrm{keV})$ source |  | $\mathrm{Cd}^{109}(87.7 \mathrm{keV})$ source |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mu, \mathrm{cm}^{-1}$ | $\mu_{\mathrm{m}} \mathrm{cm}^{2} / \mathrm{g}$ | $\mu, \mathrm{cm}^{-1}$ | $\mu_{\mathrm{m}, \mathrm{cm}^{2} / \mathrm{g}}$ |
| JP-4 fuel | 0.7546 | $0.143 \pm 0.003$ | $0.190 \pm 0.004$ | $0.127 \pm 0.002$ | $0.169 \pm 0.003$ |
| JP-5 fuel | 0.8097 | $0.150 \pm 0.002$ | $0.185 \pm 0.003$ | $0.134 \pm 0.004$ | $0.165 \pm 0.005$ |
| Jet A fuel | 0.8107 | $0.150 \pm 0.002$ | $0.185 \pm 0.003$ | $0.137 \pm 0.002$ | $0.168 \pm 0.003$ |
| Leaded gasoline | 0.7300 | $0.135 \pm 0.001$ | $0.185 \pm 0.002$ | $0.126 \pm 0.003$ | $0.172 \pm 0.004$ |
| Unleaded gasoline | 0.7443 | $0.135 \pm 0.002$ | $0.182 \pm 0.003$ | $0.125 \pm 0.002$ | $0.167 \pm 0.003$ |
| Water | 0.9974 | $0.194 \pm 0.002$ | $0.194 \pm 0.002$ | $0.165 \pm 0.002$ | $0.166 \pm 0.002$ |

TABLE IV. DATA USED FOR BOEING 737 WING TANK MODEL
$\left[\begin{array}{c}\text { Source type- }-\mathrm{Am}^{241}(59.5 \mathrm{keV}) \text {; source strength }-10^{6} \text { counts per second; } \\ \text { source enclosure }-0.01 \text {-in.-thick aluminum }\end{array}\right]$

| Compartment | W, <br> in. | H, <br> in. | D, <br> in. | B, <br> in. | SL, <br> in. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 24.0 | 26.8 | 82.0 | 0.0 | 8.2 |
| 2 | 24.0 | 24.6 | 78.0 | 1.5 | 8.2 |
| 3 | 24.0 | 22.6 | 73.0 | 3.0 | 8.2 |
| 4 | 24.0 | 20.6 | 68.0 | 4.5 | 8.2 |
| 5 | 24.0 | 18.6 | 63.0 | 6.0 | 8.2 |
| 6 | 24.0 | 16.6 | 58.0 | 7.5 | 8.2 |
| 7 | 24.0 | 14.6 | 53.0 | 9.0 | 8.2 |
| 8 | 24.0 | 13.6 | 49.8 | 10.5 | 8.2 |
| 9 | 24.0 | 12.7 | 46.5 | 12.0 | 8.2 |
| 10 | 24.0 | 11.8 | 43.2 | 13.5 | 8.2 |
| 11 | 24.0 | 10.9 | 39.9 | 15.0 | 8.2 |
| 12 | 24.0 | 10.0 | 36.6 | 16.5 | 8.2 |
| 13 | 24.0 | 9.1 | 33.3 | 18.0 | 8.2 |
| 14 | 24.0 | 8.2 | 30.0 | 19.5 | 8.2 |


| TABLE V. SUMMARY OF THE COUNTING RATES AT VARIOUS STATIONS AS A FUNCTION OF THE FUEL IN THE WING TANK |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Counts per second in compartment- |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Fuel content, percent | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| . 00 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 1.00 | 2939 | 4481 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 2.00 | 2209 | 3486 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | . 4558 | 4558 | 4558 | 4558 |
| 3.00 | 1753 | 2766 | 4366 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 4.00 | 1475 | 2328 | 3674 | 4558 | 455P | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 5.00 | 1241 | 1959 | 3093 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 6.00 | 1070 | 1688 | 2665 | 4206 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 7.00 | 036 | 1477 | 2332 | 3680 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 8.00 | 819 | 1293 | 2041 | 3221 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 9.00 | 720 | 1136 | 1793 | 2830 | 4467 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 10.00 | 644 | 1017 | 1606 | 2535 | 4000 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 11.00 | 577 | 911 | 1438 | 2270 | 3582 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 12.00 | 517 | 816 | . 1288 | 2033 | 3208 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 13.00 | 463 | 731 | 1154 | 1822 | 2875 | 4537 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 14.00 | 421 | 665 | 1049 | 1656 | 2614 | 4126 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 15.00 | 383 | 604 | 954 | 1506 | 2377 | 3751 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 16.00 | 376 | 549 | 867 | 1360 | 2161 | 3410 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 17.00 | 376 | 499 | 789 | 1245 | 1965 | 3101 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 18.00 | 376 | 455 | 719 | 1135 | 1791 | 2827 | 4462 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |
| 19.00 | 376 | 418 | 660 | 1043 | 1646 | 2598 | 4100 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 | 4558 |

Fuel content,

| TABLE V. Continued |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Counts per second in compartment- |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Fuel content, percent | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 42.00 | 376 | 376 | 376 | 376 | 376 | 483 | 763 | 1204 | 1900 | 2999 | 4558 | 4558 | 4558 | 4558 |
| 43.00 | 376 | 376 | 376 | 376 | 376 | 453 | 716 | 1130 | 1783 | 2814 | 4442 | 4558 | 4558 | 4558 |
| 44.00 | 376 | 376 | 376 | 376 | 376 | 426 | 673 | 1062 | 1677 | 2647 | 4177 | 4558 | 4558 | 4558 |
| 45.00 | 376 | 376 | 376 | 376 | 376 | 401 | 633 | 999 | 1577 | 2489 | 3928 | 4558 | 4558 | 4558 |
| 46.00 | 376 | 376 | 376 | 376 | 376 | 377 | 595 | 940 | 1483 | 2341 | 3695 | 4558 | 4558 | 4558 |
| 47.00 | 376 | 376 | 376 | 376 | 376 | 376 | 560 | 884 | 1395 | 2202 | 3475 | 4558 | 4558 | 4558 |
| 48.00 | 376 | 376 | 376 | 376 | 376 | 376 | 526 | 831 | 1312 | 2070 | 3268 | 4558 | 4558 | 4558 |
| 49.00 | 376 | 376 | 376 | 376 | 376 | 376 | 495 | 782 | 1234 | 1947 | 3073 | 4558 | 4558 | 4558 |
| 50.00 | 376 | 376 | 376 | 376 | 376 | 376 | 466 | 735 | 1160 | 1831 | 2890 | 4558 | 4558 | 4558 |
| 51.00 | 376 | 376 | 376 | 376 | 376 | 376 | 439 | 693 | 1095 | 1728 | 2727 | 4304 | 4558 | 4558 |
| 52.00 | 378 | 376 | 376 | 376 | 376 | 376 | 414 | 654 | 1033 | 1630 | 2573 | 4061 | 4558 | 4558 |
| 53.00 | 376 | 376 | 376 | 376 | 376 | 376 | 391 | 617 | 974 | 1538 | 2428 | 3832 | 4558 | 4558 |
| 54.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 582 | 919 | 1451 | 2291 | 3615 | 4558 | 4558 |
| 55.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 549 | 867 | 1369 | 2161 | 3411 | 4558 | 4558 |
| 56.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 516 | 818 | 1292 | 2039 | 3218 | 4558 | 4558 |
| 57.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 489 | 772 | 1219 | 1924 | 3037 | 4558 | 4558 |
| 58.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 462 | 729 | 1150 | 1816 | 2866 | 4524 | 4558 |
| .59 .00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 437 | 689 | 1088 | 1718 | 2712 | 4280 | 4558 |
| 60.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 413 | 652 | 1030 | 1625 | 2565 | 4049 | 4558 |
| 61.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 391 | 617 | 974 | 1538 | 2427 | 3830 | 4558 |
| 62.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 584 | 922 | 1455 | 2296 | 3624 | 4558 |
| 63.00 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 376 | 552 | 872 | 1376 | 2172 | 3428 | 4558 |


| せ | $\underset{\substack{\infty \\ \\ \\ \hline}}{ }$ | $\stackrel{\infty}{\stackrel{\infty}{n}}$ | $\begin{gathered} \infty \\ \underset{\sim}{\infty} \\ \underset{\sim}{n} \end{gathered}$ | $\begin{gathered} \mathbf{m} \\ \stackrel{4}{4} \\ \hline \end{gathered}$ | $\begin{aligned} & \infty \\ & \underset{\sim}{-1} \end{aligned}$ | $\begin{aligned} & \stackrel{6}{8} \\ & \stackrel{0}{6} \end{aligned}$ | $\begin{aligned} & \text { N } \\ & \text { ion } \end{aligned}$ | $\begin{aligned} & 0 \\ & \underset{m}{n} \end{aligned}$ | $\begin{aligned} & \infty \\ & \mathbf{N} \\ & \mathbf{m} \end{aligned}$ | $\underset{\substack{\mathbb{N} \\ \sim \\ \sim}}{ }$ | $\begin{aligned} & N \\ & \underset{\sim}{\alpha} \\ & \underset{N}{2} \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\mathbf{m}} \\ & \mathbf{\infty} \end{aligned}$ | $\begin{aligned} & \boldsymbol{o} \\ & \infty \\ & 0 \\ & \boldsymbol{N} \end{aligned}$ | $\begin{aligned} & \text { in } \\ & \stackrel{N}{N} \end{aligned}$ | $\begin{gathered} \infty \\ \stackrel{\rightharpoonup}{4} \\ \underset{\sim}{n} \end{gathered}$ | $\begin{aligned} & \mathbf{N} \\ & \underset{N}{N} \end{aligned}$ | $\underset{\sim}{N}$ | $\begin{aligned} & \text { Ha } \\ & 0 \\ & 0 \end{aligned}$ | $\stackrel{\leftrightarrow}{\sim}$ | $\begin{gathered} m \\ \substack{m \\ \\ \hline} \end{gathered}$ | $\stackrel{\circ}{i n}$ | $\begin{aligned} & n \\ & \stackrel{n}{0} \\ & 0 \\ & \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{9}{9}$ | $\begin{gathered} \underset{\sim}{m} \\ \underset{\sim}{N} \end{gathered}$ | $\begin{aligned} & \infty \\ & \stackrel{8}{8} \\ & \hline \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\circ} \\ & \underset{\sim}{\alpha} \end{aligned}$ | $\stackrel{N}{N} \underset{\sim}{N}$ | $\begin{aligned} & 0 \\ & \mathbf{8} \\ & \mathbf{N} \end{aligned}$ | $\stackrel{ \pm}{N}$ | $\begin{aligned} & 0 \\ & \stackrel{\rightharpoonup}{w} \\ & \underset{\sim}{*} \end{aligned}$ | $\begin{aligned} & N \\ & \mathbb{N} \\ & \mathbf{N} \end{aligned}$ | $\begin{gathered} \mathbf{0} \\ \underset{\sim}{0} \end{gathered}$ | $\begin{aligned} & \alpha \\ & \stackrel{\alpha}{\alpha} \\ & -1 \end{aligned}$ | $\begin{aligned} & \text { № } \\ & \stackrel{\circ}{\infty} \\ & \underset{\sim}{\boldsymbol{n}} \end{aligned}$ | $\underset{\sim}{\underset{\sim}{\sigma}}$ | $\underset{\substack{t \\ \underset{\sim}{0} \\ \hline}}{ }$ | $\begin{gathered} 0 \\ \underset{-1}{0} \\ r-1 \end{gathered}$ | $\stackrel{N}{N} \underset{\sim}{N}$ | $\begin{gathered} N \\ \mathbf{N} \\ \underset{\sim}{*} \end{gathered}$ | $\underset{\underset{\sim}{N}}{\underset{\sim}{n}}$ | $\begin{aligned} & \circ \\ & \stackrel{\circ}{9} \\ & \underset{\sim}{2} \end{aligned}$ | $\stackrel{\otimes}{N}$ | $\underset{\sim}{\underset{\sim}{2}}$ | $\underset{\sim}{\underset{\sim}{7}}$ | $$ |
| $\stackrel{\sim}{\sim}$ | $\begin{aligned} & \text { in } \\ & \stackrel{n}{0} \\ & \sim \end{aligned}$ | $\begin{gathered} \stackrel{\rightharpoonup}{t} \\ 0 \\ -1 \end{gathered}$ | $\begin{aligned} & \underset{\sim}{\infty} \\ & \underset{\sim}{\infty} \end{aligned}$ | $\underset{\sim}{\underset{\sim}{+}}$ | $\begin{gathered} n \\ \\ \end{gathered}$ | $\begin{aligned} & \text { N } \\ & \stackrel{\circ}{n} \end{aligned}$ | $$ | $\begin{aligned} & \text { o } \\ & \text { ¢ } \\ & \hline \end{aligned}$ | $\begin{aligned} & \infty \\ & m \\ & m \\ & \hline \end{aligned}$ | $\begin{aligned} & \hat{N} \\ & N \\ & N \end{aligned}$ | $\underset{\sim}{\underset{\sim}{N}}$ | $\stackrel{\underset{\sim}{\underset{\sim}{m}} \underset{\sim}{m}}{ }$ | $\begin{aligned} & 0 \\ & \mathbf{\infty} \\ & 0 \\ & 0 \end{aligned}$ | $\underset{\sim}{\underset{\sim}{N}} \underset{\substack{0}}{ }$ | $\stackrel{\circ}{\circ}$ | N | $\underset{\infty}{N}$ | $\underset{\mathbf{N}}{\boldsymbol{N}}$ | $\underset{\sim}{\infty}$ | $\stackrel{m}{\underset{\sim}{f}}$ | $\stackrel{i n}{\circ}$ | $\begin{aligned} & \infty \\ & \hline 0 \\ & \hline 0 \end{aligned}$ |
| $=$ | $\begin{aligned} & \text { N } \\ & \text { O } \\ & \text { Hen } \end{aligned}$ | $\begin{gathered} N \\ N \\ N \end{gathered}$ | $\begin{aligned} & n \\ & \stackrel{n}{0} \\ & -1 \end{aligned}$ | $\begin{aligned} & \text { in } \\ & \text {-1 } \end{aligned}$ | $\begin{aligned} & \text { N} \\ & \underset{\sim}{+} \end{aligned}$ | $\stackrel{m}{\alpha}$ | $\stackrel{-1}{6}$ | $\stackrel{m}{\infty}$ | $\begin{aligned} & 0 \\ & \mathbf{\infty} \end{aligned}$ | $\begin{aligned} & \text { N } \\ & \text { O } \end{aligned}$ | - | $\underset{N}{N}$ | $\begin{aligned} & \boldsymbol{\sim} \\ & \infty \\ & 0 \end{aligned}$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{0} \end{aligned}$ | $\begin{aligned} & n \\ & \underset{0}{n} \end{aligned}$ | $\begin{aligned} & \infty \\ & \infty \\ & \hline \end{aligned}$ | $\stackrel{n}{n}$ | $\begin{aligned} & N \\ & \text { N } \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\alpha} \\ & \underset{\sim}{2} \end{aligned}$ | $\underset{\underset{\sim}{t}}{\underset{\sim}{2}}$ | $\begin{aligned} & 0 \\ & + \\ & \hline \end{aligned}$ | $\stackrel{m}{\sim}$ |
| $\bigcirc$ | $\underset{\infty}{\underset{\infty}{\sim}}$ | $\begin{aligned} & \text { O } \\ & \underset{\sim}{\circ} \end{aligned}$ | $\stackrel{\infty}{\underset{\sim}{n}}$ | 을 | $\begin{aligned} & n \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \text { a } \\ & \text { N } \end{aligned}$ | $\stackrel{\circ}{2}$ | $\cdots$ | $\stackrel{\infty}{i}$ | $\begin{aligned} & \infty \\ & 0 \\ & \hline \end{aligned}$ | $$ | $\underset{\sim}{n}$ | $\underset{\substack{m \\ \hline}}{ }$ | $\underset{-7}{-7}$ | $\begin{aligned} & \boldsymbol{\alpha} \\ & \infty \\ & \infty \end{aligned}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\infty}{\infty}$ | $\stackrel{0}{\infty}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{\infty}{\stackrel{0}{m}}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\stackrel{\infty}{m}$ |
| 羞 | $\begin{aligned} & N \\ & \text { in } \end{aligned}$ | $\begin{gathered} \text { t } \\ \text { oun } \end{gathered}$ | $\begin{aligned} & \infty \\ & 0 \\ & 0 \end{aligned}$ | $\stackrel{m}{\stackrel{m}{+}}$ | $$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{\infty} \\ & \hline \end{aligned}$ | $\stackrel{\infty}{\infty}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\perp}{\infty}$ | $\begin{aligned} & 0 \\ & \mathrm{~m} \end{aligned}$ | $\underset{\sim}{\sim}$ | $\stackrel{0}{n}$ | $\stackrel{0}{\sim}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{\infty}$ | $\underset{m}{N}$ | $\stackrel{\infty}{m}$ | 品 | $\stackrel{0}{n}$ | $\frac{0}{\mathrm{~m}}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\stackrel{\infty}{m}$ |
| $\text { 合 } \quad \infty$ | $\underset{m}{\sim}$ | $\stackrel{D}{m}$ | $\stackrel{\circ}{\sim}$ | $\stackrel{0}{\infty}$ | $\stackrel{0}{\infty}$ | $\stackrel{c}{\infty}$ | $\underset{\sim}{n}$ | $\underset{\sim}{n}$ | $\stackrel{0}{\sim}$ | $\stackrel{\infty}{n}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{\sim}{N}$ | $\stackrel{O}{\mathrm{~m}}$ | $\stackrel{0}{m}$ | $\stackrel{0}{\sim}$ | $\underset{\sim}{\infty}$ | $\underset{m}{\circ}$ | $\stackrel{0}{\mathrm{n}}$ | $\stackrel{0}{m}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{m}{\infty}$ |
| $\begin{aligned} & 8 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\frac{0}{m}$ | $\stackrel{0}{m}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{\infty}$ | $\underset{m}{\circ}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\underset{m}{n}$ | $\underset{\sim}{\circ}$ | $\underset{m}{n}$ | $\stackrel{\circ}{m}$ | $\stackrel{0}{n}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\circ}{\infty}$ | $\underset{\sim}{n}$ | $\stackrel{0}{m}$ | $\stackrel{\circ}{m}$ | $\stackrel{0}{\infty}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{m}$ | $\stackrel{n}{n}$ | $\stackrel{\bullet}{\mathrm{m}}$ |
| $\stackrel{n}{F} \quad 0$ | on | $\stackrel{0}{\mathrm{n}}$ | $\stackrel{0}{m}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{\infty}$ | $\underset{m}{\infty}$ | $\stackrel{0}{n}$ | $\stackrel{0}{\infty}$ | $\frac{n}{m}$ | $\stackrel{0}{n}$ | $\stackrel{0}{\infty}$ | $\underset{m}{\infty}$ | $\underset{m}{n}$ | $\stackrel{N}{\mathrm{~m}}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\circ}{\mathrm{o}}$ | $\underset{m}{n}$ | $\stackrel{\circ}{\infty}$ | on | $\stackrel{0}{\mathrm{~m}}$ | $\cdots$ |
| 15 | $\stackrel{0}{\mathrm{~m}}$ | $\underset{m}{\sim}$ | $\stackrel{\infty}{\sim}$ | $\stackrel{N}{\mathrm{~m}}$ | $\stackrel{\infty}{m}$ | $\underset{m}{N}$ | $\underset{m}{c}$ | $\stackrel{0}{n}$ | $\underset{m}{\infty}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\underset{m}{N}$ | $\stackrel{N}{\mathrm{~m}}$ | $\underset{m}{\infty}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{\infty}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\underset{m}{n}$ | $\stackrel{0}{n}$ | $\stackrel{o}{\sim}$ | $\stackrel{0}{m}$ | $\underset{m}{\infty}$ | $\stackrel{0}{\sim}$ |
| \＃ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\underset{m}{\infty}$ | $\stackrel{0}{\sim}$ | $\stackrel{\circ}{m}$ | $\stackrel{\infty}{\sim}$ | $\stackrel{\circ}{\infty}$ | $\stackrel{\circ}{m}$ | $\stackrel{0}{m}$ | $\stackrel{o}{\mathrm{~m}}$ | $\underset{\sim}{\infty}$ | $\underset{m}{n}$ | $\frac{e^{\prime}}{m}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{m}{n}$ | $\stackrel{0}{m}$ | $\stackrel{N}{\sim}$ | $\stackrel{\infty}{\infty}$ | $\stackrel{\circ}{\infty}$ | $\stackrel{n}{m}$ | $\stackrel{0}{n}$ | $\stackrel{\circ}{\mathrm{m}}$ |
| $\infty$ | $\stackrel{\infty}{m}$ | $\stackrel{0}{n}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{n}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\infty}{\infty}$ | $\stackrel{\infty}{\mathrm{m}}$ | $\underset{m}{\sim}$ | $\underset{m}{\infty}$ | $\underset{\sim}{c}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{\sim}{\underset{\sim}{c}}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\stackrel{e}{m}$ | $\frac{0}{n}$ | $\stackrel{c}{c}$ | $\underset{m}{p}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{\circ}{\circ}$ | $\stackrel{n}{\mathrm{~m}}$ | $\stackrel{N}{\mathrm{~m}}$ | $\stackrel{0}{\sim}$ |
| N | $\stackrel{o}{m}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{\sim}{\infty}$ | $\stackrel{\circ}{\sim}$ | $\underset{\sim}{n}$ | $\underset{\sim}{\infty}$ | $\underset{\sim}{\infty}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{m}{\infty}$ | $\underset{\sim}{N}$ | $\underset{m}{\stackrel{c}{\mathrm{~m}}}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{\sim}{n}$ | $\underset{m}{\infty}$ | $\stackrel{0}{\mathrm{~m}}$ | $\frac{o}{m}$ | $\stackrel{\infty}{\infty}$ | $\underset{m}{\infty}$ | $\stackrel{0}{m}$ | $\stackrel{0}{\mathrm{~m}}$ | $\stackrel{0}{\infty}$ | $\stackrel{0}{n}$ |
| $-1$ | $\stackrel{c}{\sim}$ | $\stackrel{c}{\sim}$ | $\stackrel{0}{\circ}$ | $\stackrel{0}{m}$ | $\underset{\sim}{\infty}$ | $\underset{m}{\circ}$ | $\stackrel{\circ}{m}$ | $\underset{m}{\infty}$ | $\underset{m}{\infty}$ | $\stackrel{\infty}{m}$ | $\underset{m}{n}$ | $\underset{m}{N}$ | $\stackrel{0}{\mathrm{~m}}$ | $\underset{m}{\sim}$ | $\stackrel{0}{\sim}$ | $\stackrel{\circ}{\sim}$ | $\stackrel{n}{\infty}$ | $\stackrel{0}{\sim}$ | $\stackrel{c}{c}$ | $\stackrel{\circ}{\mathrm{m}}$ | $\underset{m}{\infty}$ | $\cdots$ |
|  | $\begin{aligned} & 8 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & \text { in } \\ & 0 \end{aligned}$ | $\begin{aligned} & \therefore \\ & 0 \\ & \vdots \\ & \therefore \end{aligned}$ | $\begin{aligned} & \text { ㅇ } \\ & \text { i } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & 8 \\ & 8 \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & \text { O } \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & \dot{8} \end{aligned}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{2} \end{aligned}$ | $\begin{aligned} & 8 \\ & \text { N } \end{aligned}$ | $\begin{aligned} & 0 \\ & \text { O } \\ & \text { R } \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & + \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { C } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & \stackrel{\circ}{\circ} \end{aligned}$ | $\begin{aligned} & 8 \\ & \dot{8} \\ & i \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & \infty \\ & \sim \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & \text { i } \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \\ & 0 \\ & \infty \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \\ & \text { M } \\ & \infty \end{aligned}$ | $\begin{aligned} & 8 \\ & 0 \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & 8 \\ & \text { E } \\ & \text { d } \end{aligned}$ | 8 8 $\infty$ $\infty$ |


















## Appendix

## Listing of Computer Programs

## Program WNGTNK

```
    PROGRAM WNGTNK(DUTPUT,INPUT,TAPEG=OUTPUT,TAPE5=INPUT)
```

    PROGRAM WNGTNK(DUTPUT,INPUT,TAPEG=OUTPUT,TAPE5=INPUT)
    CNMMON/GE\capMTY/W(14),H(14),D(14),B(14),SL(14),VTOT,NC
    CNMMON/GE\capMTY/W(14),H(14),D(14),B(14),SL(14),VTOT,NC
    CDMMON/ANS/CDUNTS(14.101)
    CDMMON/ANS/CDUNTS(14.101)
    DIMENSIGN FRAC(101)
    DIMENSIGN FRAC(101)
        INTEGER COUNTS
        INTEGER COUNTS
        DATA ERROR/1.E-5/
        DATA ERROR/1.E-5/
    1 FIRMAT(1H1,45X,SUMMARY OF COUNTS*////
1 FIRMAT(1H1,45X,SUMMARY OF COUNTS*////
1 5X, %% LIQUID*,45X, 'COMPARTMENT' f

```
    1 5X, %% LIQUID*,45X, 'COMPARTMENT' f
```




```
    3:rrrrrin
```

    3:rrrrrin
    2 FORMAT(1HO,5X,F7.2,2X,14I7)
2 FORMAT(1HO,5X,F7.2,2X,14I7)
CALL PSEUDO
CALL PSEUDO
CALL CALPLT(1,0,1,,-3)
CALL CALPLT(1,0,1,,-3)
CALL INIT
CALL INIT
NCM=NC-1
NCM=NC-1
NFILL=101
NFILL=101
READ(5,*,END=10) B
READ(5,*,END=10) B
10 1F(EOF(5).NF.O) GD TO 120
10 1F(EOF(5).NF.O) GD TO 120
ISGN = -1
ISGN = -1
V = -0.01*VTTT
V = -0.01*VTTT
DO 100 K=1,NFILL
DO 100 K=1,NFILL
ISGN = ISGN
ISGN = ISGN
DVOL = 0.01*VTOT
DVOL = 0.01*VTOT
V = V + OVOL
V = V + OVOL
FRAC(K)=100.*V/VTOT
FRAC(K)=100.*V/VTOT
7=0.
7=0.
DO 20 I=1,NCM
DO 20 I=1,NCM
7 B(I+1)
7 B(I+1)
V1 = 0.
V1 = 0.
DO 20 J=1,I
DO 20 J=1,I
TOP=Z
TOP=Z
BOTTOM = B(N)
BOTTOM = B(N)
IF(TOP.GT.(B(J) + H(J))) TOP = B(J) + H(J)
IF(TOP.GT.(B(J) + H(J))) TOP = B(J) + H(J)
V1 = V1 + D(J)*W(J)*(TDP - BDTTOM)
V1 = V1 + D(J)*W(J)*(TDP - BDTTOM)
IFIVI.GT.VI GO TO 30
IFIVI.GT.VI GO TO 30
20 CONTINUF
20 CONTINUF
I=NC
I=NC
30 CONTINUE
30 CONTINUE
J=I-1
J=I-1
VPOT =0.
VPOT =0.
IF(J.EQ.O) GO TO }5
IF(J.EQ.O) GO TO }5
nO 40 I=1,J
nO 40 I=1,J
Z=B(J+1)
Z=B(J+1)
TOP=Z
TOP=Z
BOTTOM B(I)
BOTTOM B(I)
IF(TGP.GT.{B(I) + H(I))} TOP B(I) \& H(I)
IF(TGP.GT.{B(I) + H(I))} TOP B(I) \& H(I)
VBOT * VBOT + D(I)*W(I)*(TOP - BOTTOM)
VBOT * VBOT + D(I)*W(I)*(TOP - BOTTOM)
40 CONTINUE
40 CONTINUE
50 CONTINUE
50 CONTINUE
J=J + 1
J=J + 1
ZOLD=B(J)
ZOLD=B(J)
D7 = B(J) + 0.75*H(J)
D7 = B(J) + 0.75*H(J)
6O CONTINUE
6O CONTINUE
VI = O.
VI = O.
ZMAX = 0.
ZMAX = 0.
DO 70 I=1,J
DO 70 I=1,J
IF(IB(I) \& H(I)).GT.ZMAX) ZMAX m B\I) \& H(I)

```
    IF(IB(I) & H(I)).GT.ZMAX) ZMAX m B\I) & H(I)
```

            TOO = ZOLD
            BOTTOM \(=B(J)\)
            IF(TПP.GT.(B(I) + H(I))) TDP = B(I) + H(I)
            IF(BOTTOM.GT.(B(I) \(+H(I)))\) BOTTOM \(=B(I)+H(I)\)
            V1 = V1 + D(I)*W(I)*(TOP - BOTTOM)
    70 CONTINUE
VOLUME VBOT + VI
TSTV = V
IF(V.EQ.O.) TSTV $=1$.
IF(ABS(VOLUME - V)/TSTV.LT.ERROR) GO TO 90
IF(VOLUME.LT.V) GO TO 80
TOLD = ZOLD - D?
$D Z=0.5 * D Z$
GOTO 60
802 OLD $=20 L D+D 2$
60 TO 60
Qo CONTINUE
IF(ZOLD.GT.ZMAX) ZOLD $=$ ZMAX
CALL TABL (ZOLD,K)
IF(K.EQ.I) CALL PICT(ZOLD)
100 CDNTINUE
WRITE 6,1$)$
DO $110 \mathrm{I}=1$,NFILL
WRITE( 6,2 ) FRAC(I), (COUNTS $(K, I), K=1, N C)$
110 CONTINUE
CALL PLTCNT
120 CONTINUE
CALL CALPLT $0.0,0.999$ )
STOP
END

Subroutine INIT

```
SUBRDUTINE INIT
    COMMIN/GEПMTY/W(14),H(14),D(14),B(14),SL(14),VTOT,NC
    NC = 14
    D(1) = 82.
    D(2)=78.
    n(3)=73.
    D(4)=58.
    D(5)=63.
    D(6) = 53.
    D(7) = 53.
    D(8)=49.8
    D(9)=46.5
    O(10)=43.2
    D(11)=39.9
    D(12)=36.6
    D(13)=33.3
    D(14)=30.
    H(1) = 26.8
    H(2)=24.5
    H(3)=22.6
    H(4)=20.6
    H(5) = 19.6
    H(6)=16.6
    H(7)=14.6
    H(8)=13.6
    H(9)=12.7
    H(10)=11.8
    H(11)=10.9
    H(12)=10.
    H(13)=9.1
    H(14)=8.2
    VTOT = 0.
```


## Subroutine PICT

```
    DN 10 I=1,NC
    H(I)=24.
    VTOT = VTOT + W(I)*H(I)*D(I)
10 CONTINUE
    NCO2 = NC/2
    CR 20 I=1,NC
    SL(I) = 8.2
20 CDNTINUE
    RETURN
    END
```

```
    SURRDUTINF PICT(Z)
    COMMON/GEOMTY/W(14),H(14),D(14),B(14),SL(14),VTOT,NC
    DIMENSION XA(35),YA(35),XB(35),YB(35)
    DATA EPS/1.E-41
    IND = 1
    X=0.
    Y =0.
    XI =0.
    YI = 1.O*(B(NC) + H(NC))/34.
    CALL CALPLT(XI,YI,3)
    XA(IND)=XI
    YA(IND) = YI
    IF(1.*Z/34..LT.YI) YA(IND)=1.*Z/34*
    IF(YA(INO).LT.1.*B(NC)/34.) YA(IND)= 10*B(NC)/34.
    IND = IND + I
    DO 10 I=1,NC
    X=X+W(NC+1-I)/34.
    Y=1.0*(B(NC+1-I) + H(NC+1-I))/34.
    CALL CALPLT(X,Y,Z)
    XA(INDI = - EPS
    YA(IND) = Y
    IF(1.*Z/34*.LT.Y) YA(IND)=10*7/34.
    IF(YA(IND).LT.1.*B(NC+1-1)/34*) YA(IND)=10*B(NC+1-I)/34*
    IND = IND + I
    IF(I,NE.NC)
    IY = 1.0*(B(NC-I) + H(NC-I))/34.
    IF(I.EQ.NC) Y m 0.
    CALL CALDLT(X,Y,Z)
    XA(IMD) =X+EPS
    YA(IND) Y
    IF(1.*Z/34..LT,Y) YA(IND) 1.*Z/34.
    IF(YA(IND).LT.1**B(NC-I)/34.) YA(IND) = 1.*B(NC-I)/34.
    IND = IND + 1
10 CONTINUE
    CALL CALPLT(XI,YI;3)
    X= XI
    Y=1.0*B(NC)/34.
    CALL CALPLT(X,Y,2)
    IND=1
    XB(IND) = X
    YB(IND) * Y
    IND = IND + 1
    DO 20 I=1,NC
    X X +W(NC+1-1)/34.
    Y=1.0*8(NC+1-1)/34.
    CALL CALPLT(X,Y,2)
    XB(IND)=X-EPS
    YB(IND) Y
    IND = IND + 1
    IF(I,EO.NC) GO TO 20
```

Subroutine TABL

```
    Y=1.0*B(NC-I)/34.
```

    Y=1.0*B(NC-I)/34.
        CALL CALPLT(X,Y,2)
        CALL CALPLT(X,Y,2)
        XB(IND) =X + EPS
        XB(IND) =X + EPS
        YR(IND)=Y
        YR(IND)=Y
        IND = IND + I
        IND = IND + I
        20 CONTINUE
        20 CONTINUE
    XA(29)=0.
    XA(29)=0.
    XP(20)}=0
    XP(20)}=0
    XA(30)=1.
    XA(30)=1.
    XB(30)=1.
    XB(30)=1.
    YA(29)=0.
    YA(29)=0.
    YB(29)=0.
    YB(29)=0.
    YA(30)=1.
    YA(30)=1.
    YB(30)=1.
    YB(30)=1.
    NP=2B
    NP=2B
    C CALL HAFTONE(XA,YA,NP,XB,YB,ND,9)
C CALL HAFTONE(XA,YA,NP,XB,YB,ND,9)
CALL LINPLT(XA,YA,NP,1,0,0,0,0)
CALL LINPLT(XA,YA,NP,1,0,0,0,0)
XI = -0.5*W(14)/34.
XI = -0.5*W(14)/34.
DO 30 I=1,NC
DO 30 I=1,NC
XI = XI +W(NC-I+I)/34.
XI = XI +W(NC-I+I)/34.
YI=10*(B(NC-I+1)+SL(NC-I+1))/34.
YI=10*(B(NC-I+1)+SL(NC-I+1))/34.
CALL PNTPLT(XI,YI,22,1)
CALL PNTPLT(XI,YI,22,1)
30 CONTINUE
30 CONTINUE
CALL NFRAME
CALL NFRAME
CALL CALPLT(1.,1.,-3)
CALL CALPLT(1.,1.,-3)
RFTURN
RFTURN
END

```
    END
```

```
    SUBROUTINE TABL(Z;K)
    COMMON/GEOMTY/W(14),H(14),D(14),B(14),SL(14),VTOT,NC
    CCMMON/ANS/CDUNTS(14,101)
    PEAL LIOSIGPLIQDEN
    INTEGER COUNTS
    DATA AIPSIG,AIRDEN,LIQSIG,LIODEN,ALSIG,ALDEN/
    1 0.178,0.001293,0.150,.7999,0.248,2.71
    DATA STRNGT/1,E+6/
    DI = ACOS(-1.)
    DC 10 I=1,NC
    HEIGHT = H(I)
    TOP = Z
    IF(TOP.GT.(H(I)+B(I)| TOP m H(I) & B(I)
    IF(TOP.LT.B(I)) TOP m B(I)
    SLDANG 10.*2.54/(4.*PI*(2.54*SL(I))**2)
    DLIQ = TOP - B(I)
    DAIR = SL(I) - DLIQ
    IF(DLIQ.GT.SL(I|) DLIQ = SLII)
    IFIDLIQ.EQ.SL(I|) DAIR = O.
    XC = SLDANG*STRNGT
    XC = XC*EXP(-2.54*0.01*ALSIG*ALDEN)
    XC = XC*EXP(-2.54*DLIO*LIOSIG*LIODEN)
    XC = XC*EXP(-2.54*DAIR*AIRSIG*AIRDEN)
    COUNTS(I,K) = XC
10 CONTINUE
    RETURN
    END
```


## Subroutine PLTCNT

```
    SUBRDUTINE PLTCNT
    COMMON/GEDMTY/W(14),H(14),D(14),B(14),SL(14),VTBT,NC
    COMMON/ANS/COUNTS(14,101)
    DIMENSIDN FRAC(101)
    INTEGER COUNTS
    DIMENSION X(105),Y(105)
    DO 30 J=1,NC
    x(102)=0.
    x(103)=10.
    Y(102)=0.
    Y(103)=600.
        IF(J.NE.1) GO TO 10
        CALL AXES(0.,0.,0.,10., X(102),X(103),1.,0.,
    1 8H% LIQUID,0.2,-8)
    CALL AXES (0.,0.,90.,8.,Y(102),Y(103),1.,0.,
    1 GHCDUNTS,0.2,6)
10 CONTINUE
    DO 20 I=1,101
    X(I) = FLDAT(I-1)
    Y(I) = CIUNTS(J,I)
20 CONTINUE
    CALL LINPLT (X,Y,101,1,0,0,0,0)
30 CDNTINUE
    RETURN
    END
```



Figure 1. Decay scheme for $\mathrm{Am}^{241} \xrightarrow{\alpha} \mathrm{~Np}^{237}$.


Figure 2. Decay scheme for $\mathrm{Cd}^{109} \xrightarrow{E C} \mathrm{Ag}^{109}$.


Figure 3. Schematic diagram of experimental system used for measuring attenuation coefficients of $\mathrm{Am}^{241}$ and $\mathrm{Cd}^{109}$ gamma rays.


Figure 4. Geometrical details of fuel cell and associated shields/collimators.


Figure 5. Typical spectra of $\mathrm{Am}^{241}$ ( 59.5 keV ) radiation source through measurement cell.


Figure 6. Typical spectra of $\mathrm{Cd}^{109}(87.7 \mathrm{keV})$ radiation source through measurement cell.


Figure 7. Wing compartment diagram for Boeing 737 airplane.


Figure 8. Vertical cross section of wing tank in flight.


Figure 9. Counting rate versus fuel content in wing tank at various source-detector stations.

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[^0]:    1 The mass attenuation coefficients are independent of the actual density and physical state (gas, liquid, or solid) of the absorber.

