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WORKSHOP ON  
THE INTEGRATION OF FINITE ELEMENT MODELING  
WITH  
GEOMETRIC MODELING  
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**FINITE OCTREE MESHING  
THROUGH  
TOPOLOGICALLY DRIVEN  
GEOMETRIC OPERATORS**

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# **OCTREE TECHNIQUE**

## **HIERARCHIC STRUCTURE**

- PROVIDES POWERFUL DATA STRUCTURE

## **SPATIALLY ADDRESSABLE**

- REGULAR HEXAHEDRA (PARALLELEPIPED)

## **FINITE INFORMATION**

- DISCRETE PORTION OF THE MODEL

# **FINITE OCTREE**

# **FINITE OCTREE - OVERVIEW**

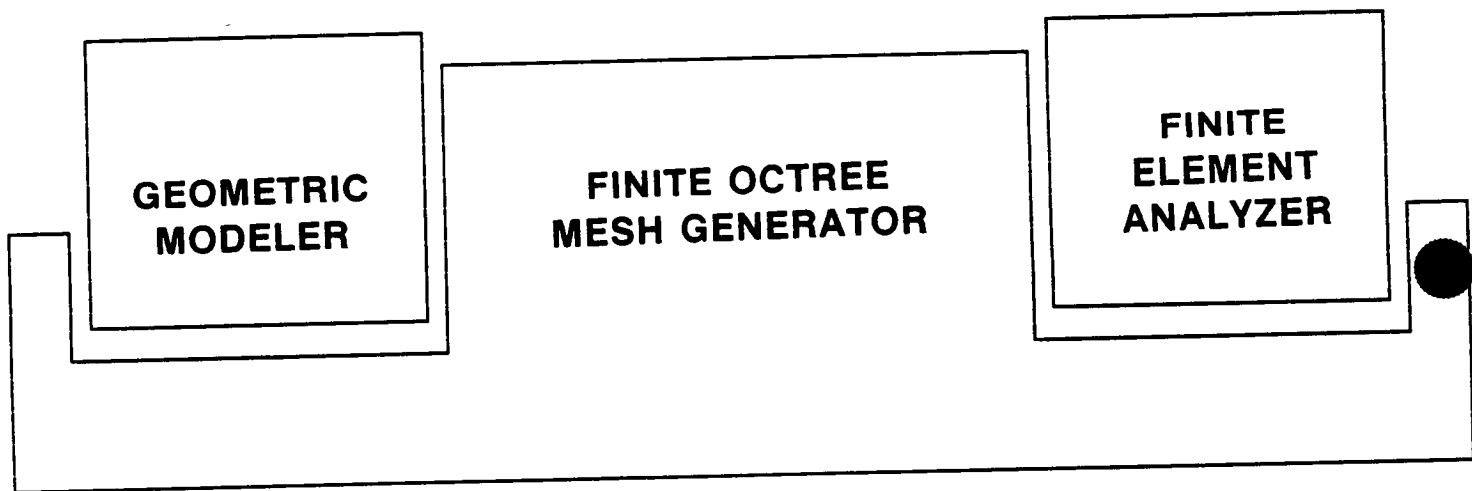
## **DISCRETIZATION OF SPACE**

- EACH TERMINAL CELL (OCTANT) CONTAINS SPECIFIC DISCRETE MODEL INFORMATION.
- THE DISCRETE INFORMATION IS TOPOLOGICALLY CORRECT, BUT GEOMETRICALLY INCOMPLETE.
- EACH DISCRETE ENTITY CONTAINS POINTERS BACK TO THE MODEL, SO ALL GEOMETRIC AMBIGUITIES CAN BE RESOLVED.

**THESE TERMINAL OCTANTS ARE FURTHER BROKEN UP INTO ELEMENTS.**

**THE ELEMENTS ARE THEN SUBMITTED TO AN ANALYSIS PACKAGE.**

**IF NEEDED, TERMINAL OCTANTS CAN BE EITHER RECOMBINED, OR FURTHER SUBDIVIDED IN AN ADAPTIVE TECHNIQUE.**



# **FINITE ELEMENT SYSTEM**

# **MODELER REQUIREMENTS**

## **BOUNDARY REPRESENTATION -**

- CONTAIN VERTEX, EDGE, FACE AND REGION ENTITIES ALONG WITH THE ADJACENCY INFORMATION.
- ALL COMPLETE AND UNIQUE GEOMETRIC REPRESENTATIONS CAN BE CONVERTED TO A B-REP.
- ANALYSIS ATTRIBUTES ARE DOMINATED BY INFORMATION ASSOCIATED WITH THE BOUNDARY.
- PROVIDES A GENERAL, ABSTRACT MEANS REPRESENTING NON-MANIFOLD STRUCTURE, ORIGINATING PERHAPS FROM AN IDEALIZATION OF THE MODEL

## **GEOMETRIC COMMUNICATION OPERATORS -**

- RESTRICTED SET OF QUERIES ON BOTH THE TOPOLOGICAL ADJACENCY AS WELL AS THE UNDERLYING GEOMETRIC DEFINITION.
- SIMILAR IN APPROACH TO THE CAM-I APPLICATION INTERFACE SPECIFICATION (AIS).
- PROVIDES MEANS OF INTERFACING TO VARIETY OF MODELERS.

# **MODELER REQUIREMENTS**

**EACH TOPOLOGIC ENTITY HAS A CORRESPONDING  
GEOMETRIC ENTITY ASSOCIATED WITH IT.**

- REGION TO VOLUME
- FACE TO SURFACE
- EDGE TO CURVE
- VERTEX TO POINT

**VOLUME, FACE AND EDGE ENTITIES CAN BE  
PARAMETERIZED**

**IDENTIFICATION OF EACH ENTITY IS UNIQUE**

# OCTREE DISCRETIZATION

ONE COULD VIEW THE COMPLETE DISCRETIZATION OF A MODEL AS POINT (OCTANT CORNERS) AND CELL (BOUNDARY INTERSECTIONS WITH OCTANTS) CLASSIFICATIONS.

THIS CLASSIFICATION AND THE ASSOCIATION WITH THE OCTANTS WILL PROVIDE THE DATA FOR GENERATING THE FINAL MESH.

POINT AND CELL CLASSIFICATION TECHNIQUES ARE EXTREMELY GEOMETRY INTENSIVE AND MAY REQUIRE EXTENSIVE QUERIES.

THESE CAPABILITIES MUST BE CAREFULLY IMPLEMENTED FOR USE IN A GENERAL MODELING ENVIRONMENT.

FROM A MODELING STAND POINT:

- IN NON-IMPLICIT REPRESENTATIONS, POINT CLASSIFICATION (IN/OUT/ON TESTING) IS NOT EFFICIENT.

FROM A FINITE OCTREE PERSPECTIVE:

- CLASSIFICATION OF AN 'ON' POINT IS MOST IMPORTANT (DETERMINATION OF A BOUNDARY).
- RESOLVE COMPLICATIONS OF THE MODEL AS EARLY AS POSSIBLE, INCLUDING CONTRIBUTIONS FROM ANALYSIS ATTRIBUTES.
- RESOLUTION OF NON-MANIFOLD REPRESENTATIONS COULD BE VERY COSTLY (ex: hanging faces).
- ONCE A DISCRETE REPRESENTATION OF THE BOUNDARY OF THE MODEL IS COMPLETE, IT IS A TRIVIAL MATTER TO IDENTIFY THE INTERIOR NODES.

# **OCTREE DISCRETIZATION**

## **GENERAL METHOD**

- INSERT TOPOLOGICAL ENTITIES OF THE MODEL FROM THE LOWEST ORDER UP
- VERTEX, EDGE, FACE, THEN INTERIOR (IF ANY)
- UTILIZE SPECIFIC GEOMETRIC COMMUNICATION OPERATORS, AVOID 'EXPENSIVE' OPERATIONS

## **ASSOCIATE THE DISCRETE ENTITIES BACK TO THE MODEL AND THE MODEL TO THE DISCRETE ENTITIES.**

- ALLOWS FOR RESOLUTION OF GEOMETRIC AMBIGUITIES
- ALLOWS FOR THE ASSIGNMENT OF GEOMETRICALLY ASSIGNED LOADS ON TO THE DISCRETE ENTITIES



# **GEOMETRIC COMMUNICATION OPERATORS**

**TWO TYPES CALLED BY THE FINITE OCTREE  
PROGRAM:**

- 8 EXPECT INFORMATION ON TOPOLOGICAL ADJACENCY OR ATTRIBUTES APPLIED TO THE TOPOLOGY.
- 10 EXPECT SPATIAL DATA AS A RESULT OF A COMPUTATION USING THE UNDERLYING GEOMETRY OF THE MODEL.
- ALL ARE TYPICALLY AVAILABLE IN GEOMETRIC MODELERS.

**GOES BEYOND THE STATIC FILE TRANSFER  
SCHEMES SUCH AS IGES, AND INTO A DYNAMIC  
INTERFACE WITH THE MODELER ITSELF.**

# **GEOMETRIC COMMUNICATION OPERATORS RETURNING TOPOLOGICAL ASSOCIATIVITY**

**GET A LIST OF MODEL ENTITIES, SUCH AS  
VERTICES, EDGES, OR FACES FOR INSERTION INTO  
THE TREE.**

**GET THE MESH CONTROL ATTRIBUTE ON THE  
MODEL ENTITIES.**

**GET LOWER ORDER ENTITIES ASSOCIATED WITH A  
SPECIFIED ENTITY. (ex: vertices of on edge)**

**GET HIGHER ORDER ENTITY ASSOCIATED WITH A  
SPECIFIED ENTITY. (ex: regions on either side of a  
face)**

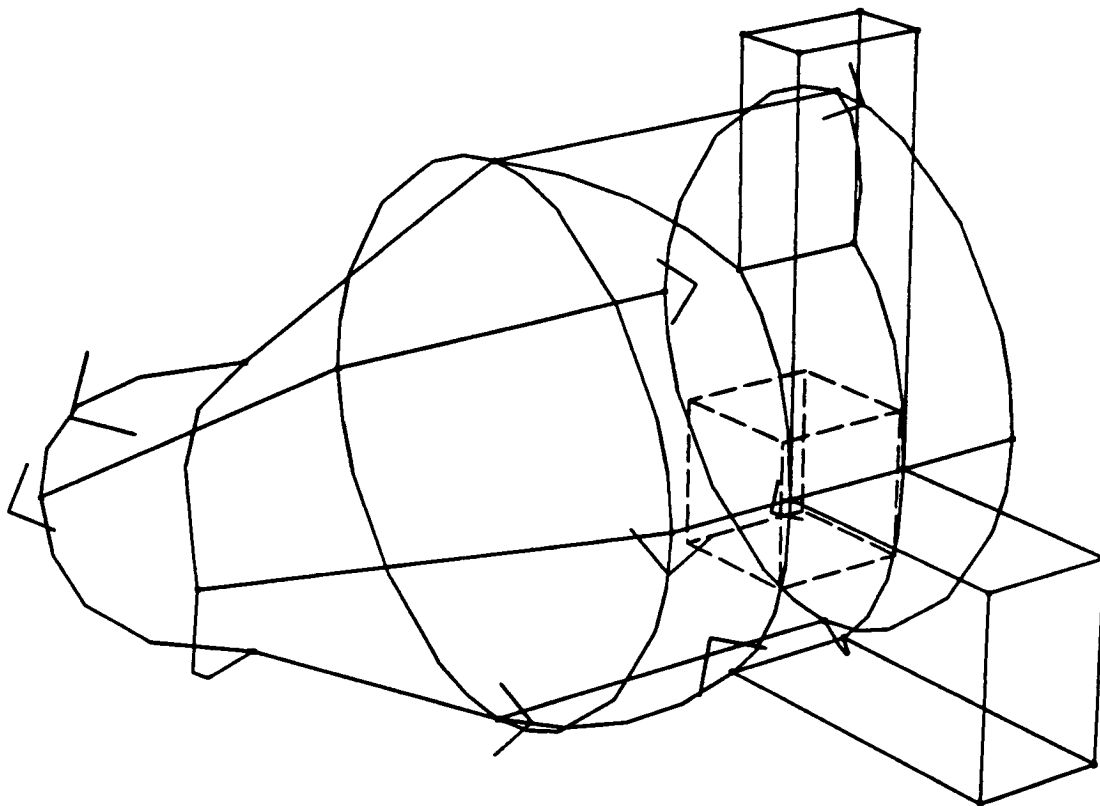
**VERIFY WHETHER AN ENTITY IS ASSOCIATED WITH  
ANOTHER. (ex: edge in face)**

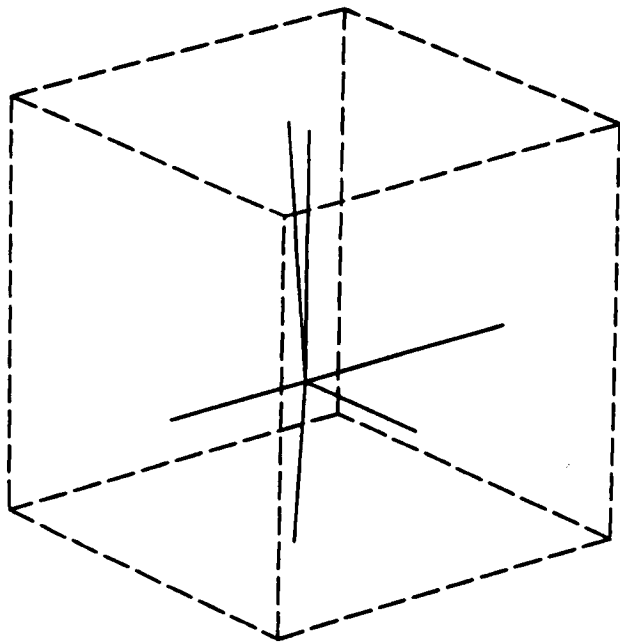
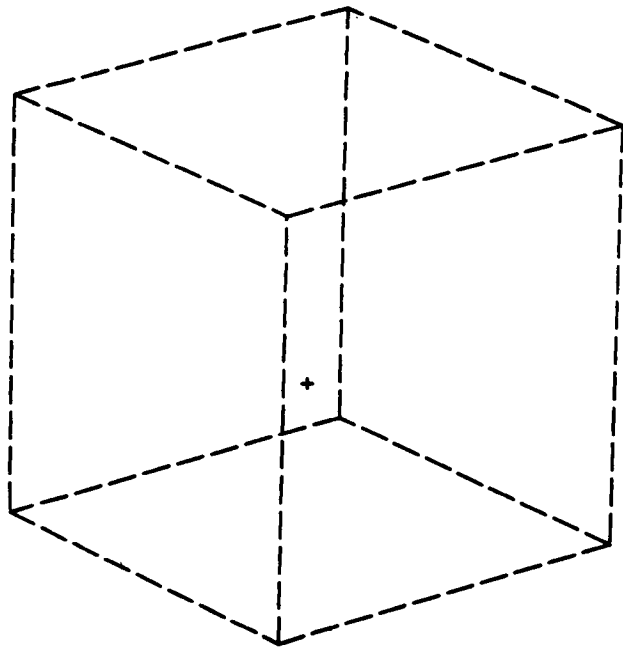
# **GEOMETRIC COMMUNICATION OPERATORS RETURNING SPATIAL DATA**

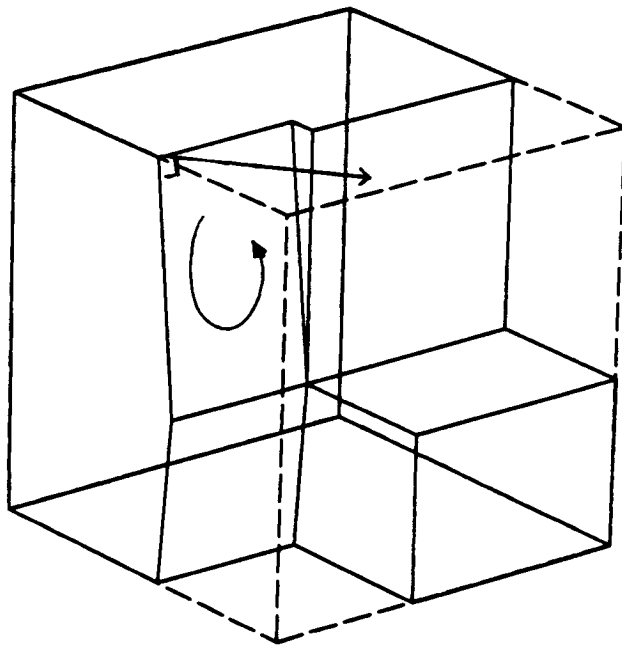
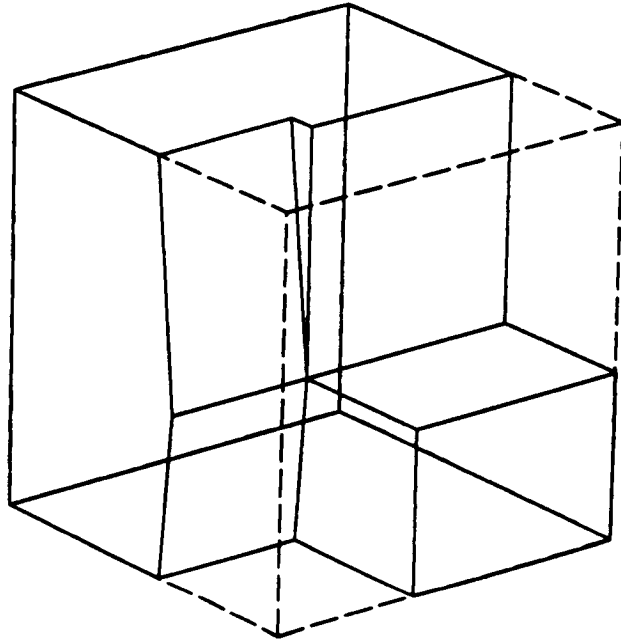
**RETURNED DATA IS ALWAYS BASED ON POINT  
INFORMATION: COORDINATES, PARAMETER  
VALUES, NORMALS, DISTANCES.**

## **EXAMPLES:**

- GET\_COORDINATE\_OF\_VERTEX
- INTERSECT\_PLANE\_WITH\_EDGE
- INTERSECT\_LINE\_WITH\_FACE
- GET\_NORMAL\_TO\_FACE





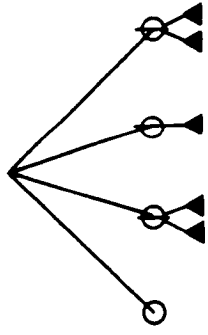
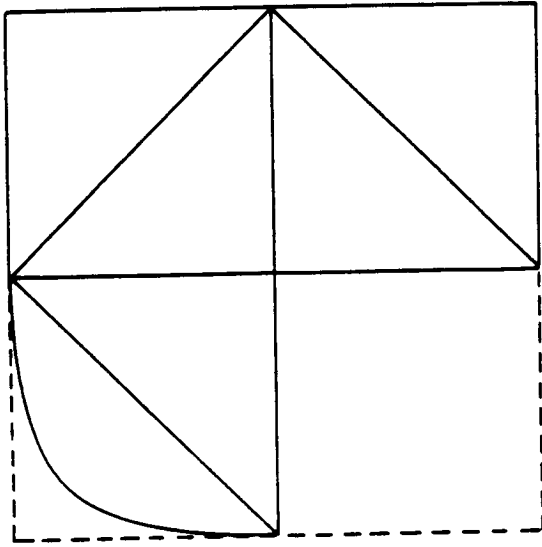


# **CAPABILITIES OF A FINITE OCTREE BASED MESHING PROCEDURE**

ADAPTIVE ANALYSIS TECHNIQUES WITH LOCAL  
REMESHING.

AUTOMATED METAL FORMING USING REMESHING  
CAPABILITIES.

# MODIFIED QUADTREE REFINEMENT

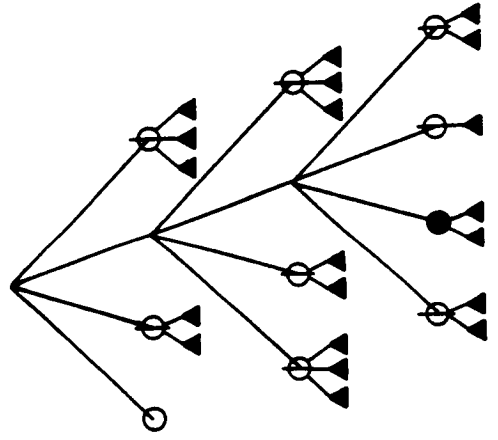
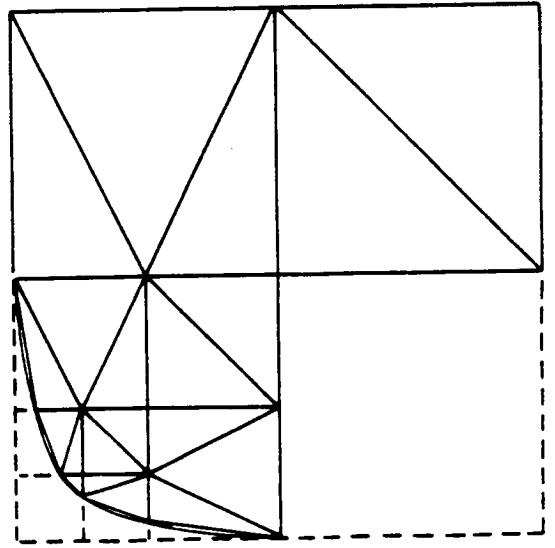


$\phi$  Boundary quadrant

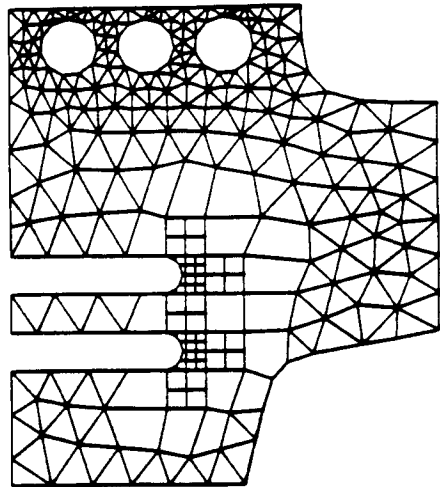
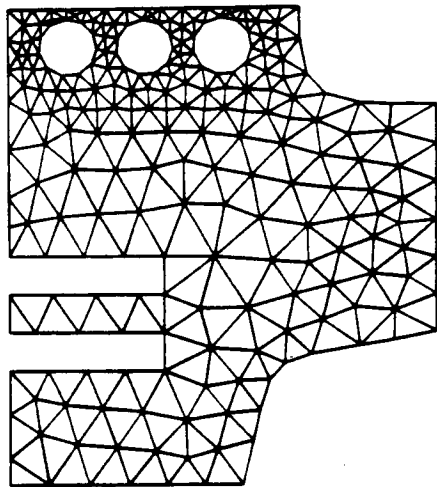
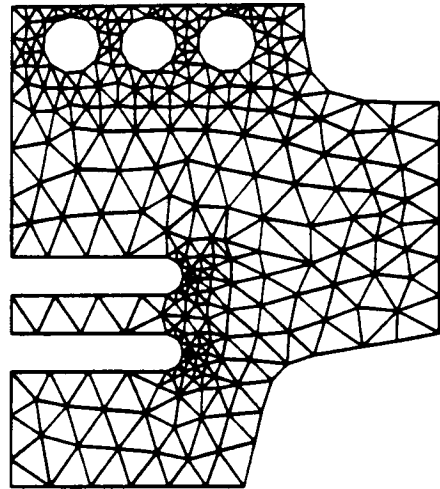
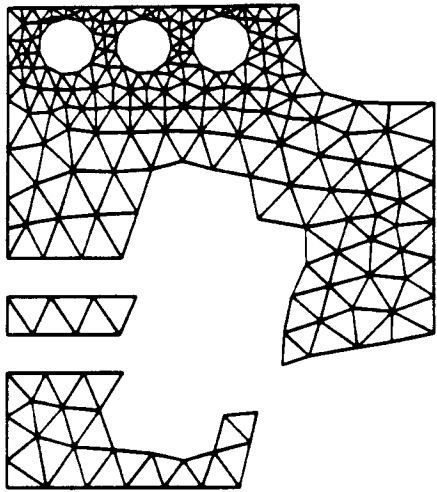
● Interior quadrant

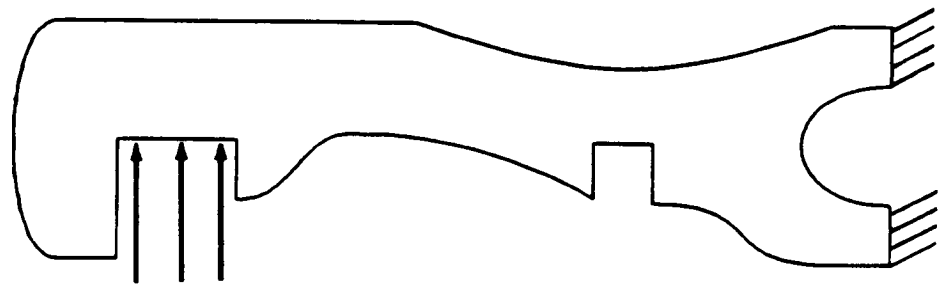
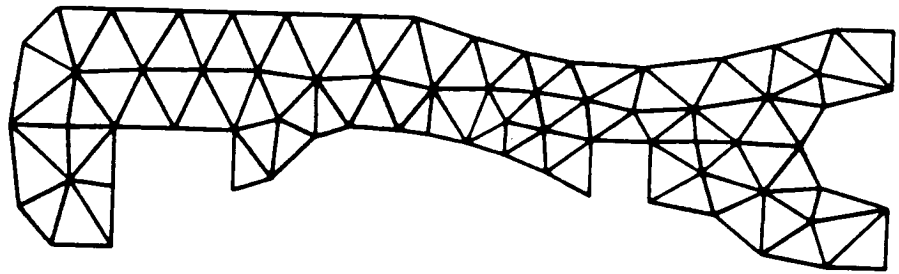
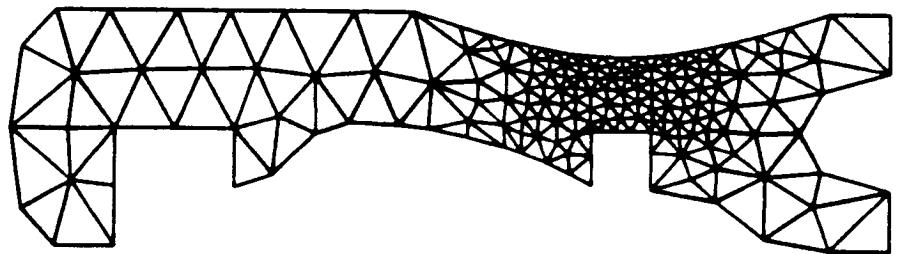
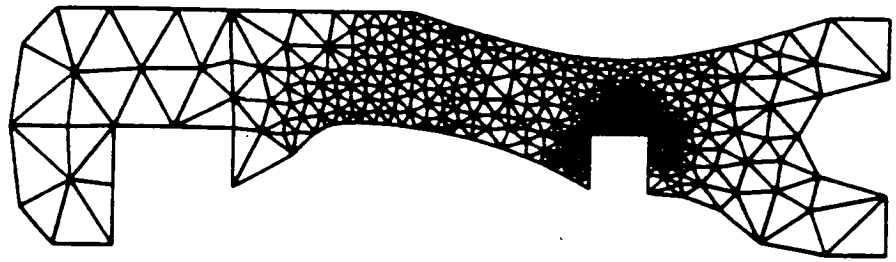
○ Exterior quadrant

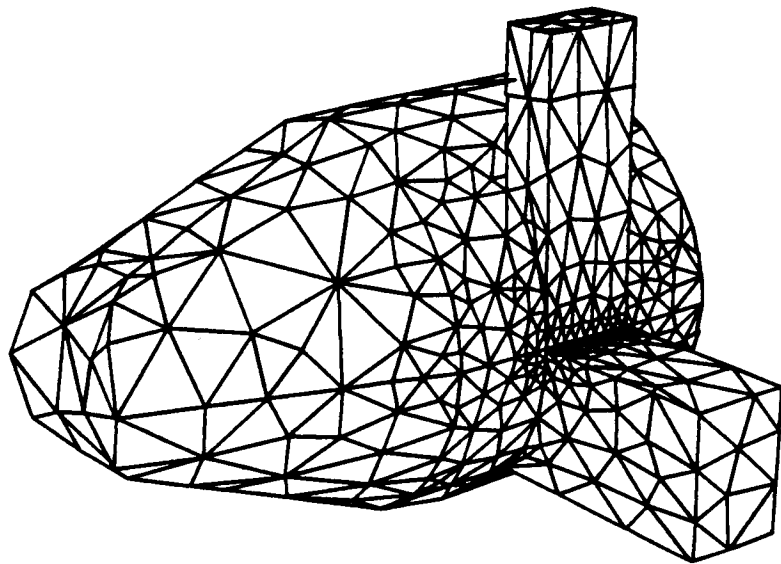
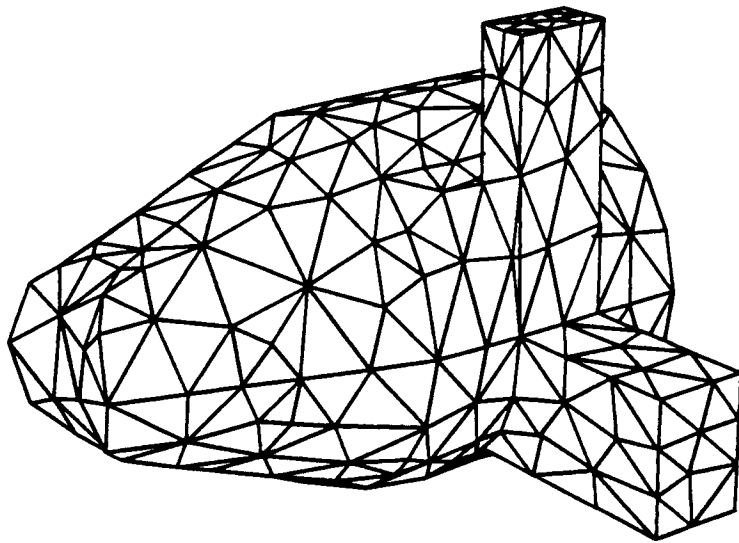
▲ Finite element

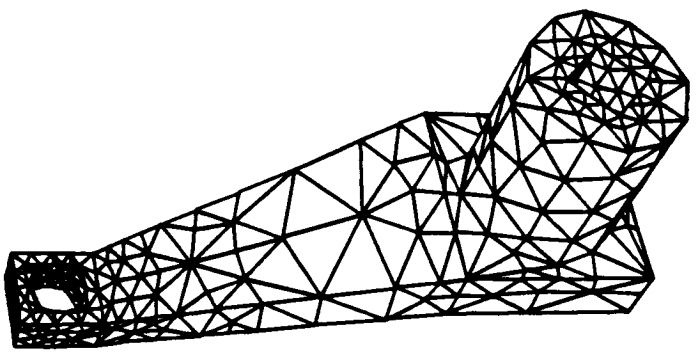
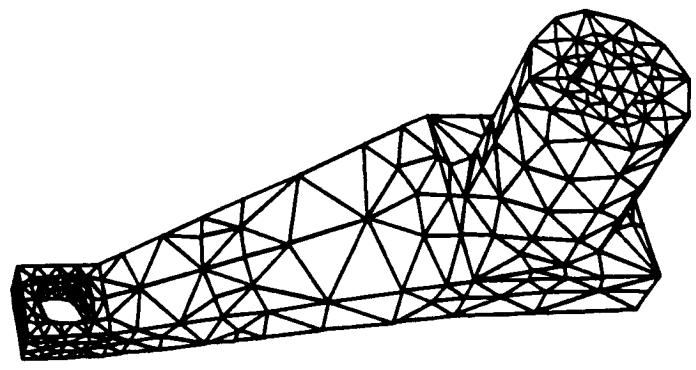












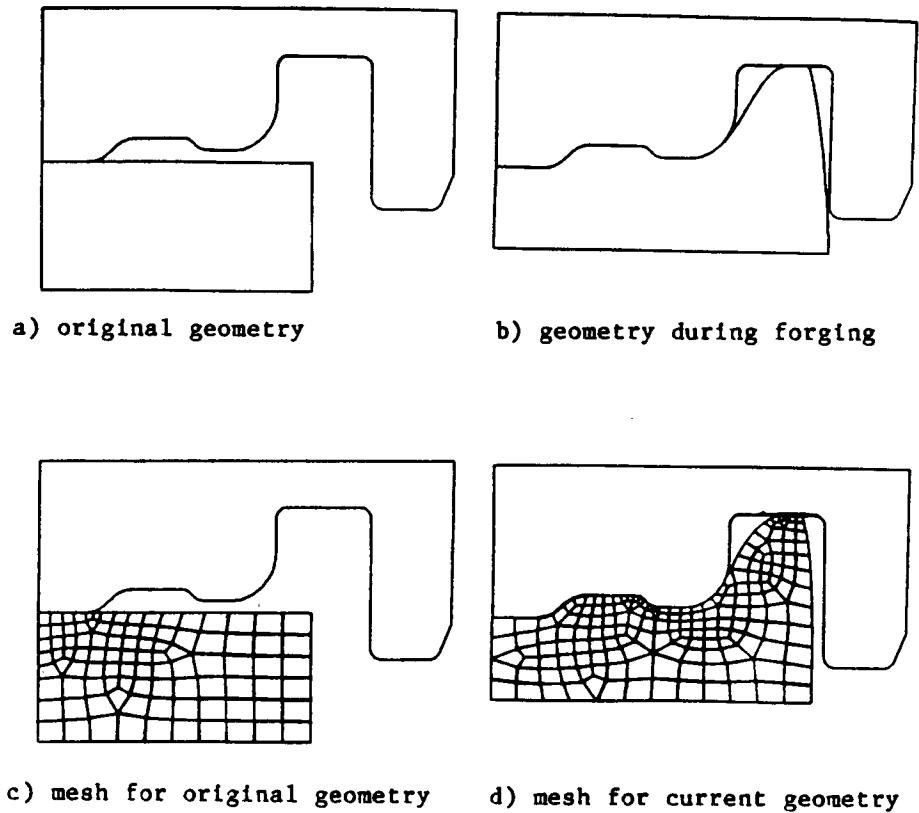


Figure 3. Modeling of forging process

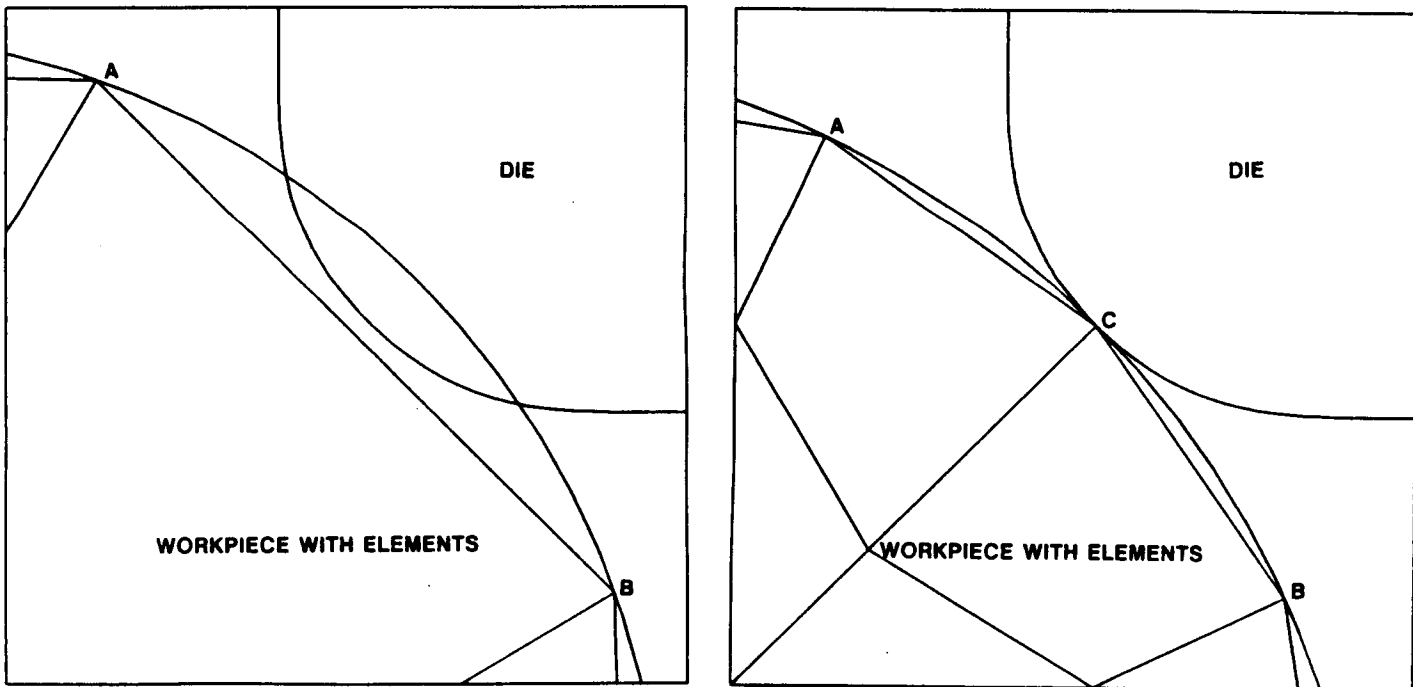


Figure 4. Volume control through geometric checks

# **SUMMARY**

**ADVANTAGES OF BOUNDARY REPRESENTATION**

**ADVANTAGES OF GEOMETRIC COMMUNICATION  
OPERATORS**

**IMPLEMENTATION PLAYS AN IMPORTANT ROLE IN  
THE INTEGRATION WITH A VARIETY OF GEOMETRIC  
MODELERS**

**CAPABILITIES OF CLOSED LOOP PROCESSES  
WITHIN A COMPLETE FINITE ELEMENT SYSTEM**

# **ELEMENT GENERATION**

## **PERFORMED ON AN OCTANT BY OCTANT BASIS**

- EACH OCTANT REPRESENTS ONE OR MORE DISCRETE REGIONS OF THE MODEL, EACH DISCRETE REGION BOUNDED BY DISCRETE FACES
- TOPOLOGICALLY CORRECT, BUT GEOMETRICALLY INCOMPLETE
- GEOMETRIC COMMUNICATION OPERATORS ARE STILL NECESSARY

**THE ELEMENTS ARE CREATED BY BREAKING THE DISCRETE REGION INTO A COLLECTION OF SIMPLEX ELEMENTS (TETRAHEDRONS)**

**CREATING THE ELEMENTS REQUIRES BOTH THE TRIANGULATION OF THE DISCRETE FACES AS WELL AS THE TETRAHEDRONIZATION OF THE DISCRETE REGIONS**

# **ELEMENT GENERATION**

## **FACE TRIANGULATION**

- SINGLE LOOP OF CONNECTED POINTS IN 3-SPACE IS BROKEN INTO A SET OF SIMPLEX ENTITIES (TRIANGLES)
- CRITERIA FOR TRIANGULATION BASED ON VALIDITY AND QUALITY
- NEITHER OF THESE CRITERIA CAN BE RESOLVED BASED ON THE TOPOLOGY OF THE LOOP, THE GEOMETRY OF THE MODEL MUST BE QUERIED

## **REGION TETRAHEDRONIZATION**

- BASED ON THE WORDENBER VOLUME TRIANGULATION TECHNIQUE
- OPERATIONS ARE EDGE REMOVAL AND VERTEX REMOVAL
- EACH REMOVAL MAY CREATE ADDITIONAL ENTITIES THAT MAY INTERFERE WITH THE GEOMETRIC MODEL, CAUSING INVALID ELEMENTS

**IN SHORT, THE TOPOLOGY SUPPLIED BY THE DISCRETE REPRESENTATION, IS SIMPLY NOT SUFFICIENT FOR TETRAHEDRONIZATION, GEOMETRIC QUERIES ASSURE A CORRECT AND APPROPRIATE MESH**



