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PERFORMANCE IMPROVEMENT OF ROBOTS USING  
A LEARNING CONTROL SCHEME

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ABSTRACT

Many applications of robots require that the same task be repeated a number of times. In such applications, the errors associated with one cycle are also repeated every cycle of the operation. An off-line learning control scheme is used here to modify the command function which would result in smaller errors in the next operation. The learning scheme is based on a knowledge of the errors and error rates associated with each cycle. Necessary conditions for the iterative scheme to converge to zero errors are derived analytically considering a second order servosystem model. Computer simulations show that the errors are reduced at a faster rate if the error rate is included in the iteration scheme. The results also indicate that the scheme may increase the magnitude of errors if the rate information is not included in the iteration scheme. Modification of the command input using a phase and gain adjustment is also proposed to reduce the errors with one attempt. The scheme is then applied to a computer model of a robot system similar to PUMA 560. Improved performance of the robot is shown by considering various cases of trajectory tracing. The scheme is also applied to a real robot PUMA 560. The results show that the proposed scheme can be successfully used to improve the performance of actual robots within the limitations of the repeatability and noise characteristics of the robot.

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## 1.0 INTRODUCTION

Several methods of performance improvement of robots have been attempted previously by many researchers. Some of these employ on-line adaptive control schemes<sup>1,2</sup> considering factors such as flexibility of the arms and variation of loads. Such control schemes are required for trajectories which are not defined a priori or require accurate trajectory control in the first attempt. For repetitive type of operations, as most commonly required in industrial applications, such as welding, cutting or sealing, a control scheme which can learn based on its previous performance appears to be more attractive because of the simplicity of the technique. A method to obtain a modified command input signal called Computed Repetitive Adjustment Technique (CREATE)<sup>3</sup> is embodied in an algorithm for correcting a robot's motion in successive testing of the same job. This repetitive testing is continued until the trajectory errors are within the acceptable bound before performing the actual work. The technique was later applied<sup>4,5</sup> to improve the performance of a mathematical model of a three-link robot arm.

A scheme very similar to CREATE was studied by Craig<sup>6</sup> for application by considering a linearized model of the robot. Conditions for the convergence of the scheme to yield minimum errors were obtained with the assumption that several critical parameters of the system are known. Arimoto<sup>7</sup> proposed a learning scheme based on measuring error rate only. He later extended<sup>8,9</sup> the control scheme to include the error and error rate information. However, the conditions<sup>8</sup> he arrived at are found to be unsatisfactory. Several other researchers<sup>10,11,12</sup> have attempted to obtain convergence conditions for the iteration scheme, but the analysis are generally inadequate. Togai<sup>13,14</sup> obtained interesting algorithms by using discrete analysis and by applying optimal control techniques. An algorithm based on optimal control technique is also given by Harokopos<sup>15</sup> for continuous systems. Bedewi<sup>16</sup> used CREATE technique to refine the performance of the robot starting with a dynamic inverse of the model of the system. In this paper, the learning control scheme proposed by Arimoto<sup>8</sup> will be considered. Analysis of the scheme will be attempted with a servosystem model. The scheme will then be applied to a mathematical model of a three-link robot to show the improvement in performance.

## 2.0 SECOND ORDER SERVOSYSTEM MODEL

### 2.1 Description of the Servosystem Model

A servo control design is given in this section which will be applied to design independent control of each joint of the robot. The second order servosystem model is also used in this section to test the proposed learning control scheme. The scheme is then applied to improve the performance of the robot model in section 3.

The dynamics of the servosystem can be represented, by ignoring the damping factor for the sake of simplicity, as

$$I\ddot{\theta} = T_C \quad (1)$$

where  $\theta$  is the angular position (a function of time, t)

$T_C$  is the control torque

$I$  is the moment of inertia of the servo, and  
 $\ddot{\theta}$  is the second derivative of  $\theta$  with respect to time

It is necessary to feedback the angular position,  $\theta$ , and its rate,  $\dot{\theta}$ , to obtain a stable position control system. An integral feedback of the position may also be used to obtain a higher speed of response. However, an integral feedback increases the order of the system and introduces oscillations in the system response. These characteristics are not desirable for the present application and hence only a proportional plus derivative controller is considered for stabilizing the servosystem as shown in Fig. 1. The characteristic equation of the closedloop system can be written as,

$$s^2 + (K_2/I)s + (K_1/I) = 0 \quad (2)$$

This equation may be compared with the damped oscillatory system

$$s^2 + 2\zeta\omega_n s + \omega_n^2 = 0 \quad (3)$$

where  $\zeta$  is the damping ratio and  $\omega_n$  is the natural frequency of the system. It is desirable to have a high value of  $\omega_n$  to get a large bandwidth of the system. The stability of the second order system is guaranteed as long as  $K_1$  and  $K_2$  remain positive. However, the feedback gain value  $K_1$  can not be increased beyond a certain limit (due to the practical limitations of the actuator) in an effort to increase the bandwidth of the system. Within these limits, the feedback gain values are obtained using the relations (obtained from Eqs. (2) and (3)) as,

$$K_1 = \omega_n^2 I \quad \text{and} \quad K_2 = 2\zeta\omega_n I \quad (4)$$

The rate feedback gain,  $K_2$ , is assumed to achieve critical damping in the closedloop system. For such a case, the system will have the highest speed of response corresponding to the lowest settling time and for a given bandwidth of the system. Fig. 2 shows the transient response of the second order system for a step input and for the selected feedback gain values.

Case (a)	$K_1 = 100$	$K_2 = 20$	$\omega_n = 10$ rad/sec
(b)	$K_1 = 144$	$K_2 = 24$	$\omega_n = 12$ rad/sec
(c)	$K_1 = 625$	$K_2 = 50$	$\omega_n = 25$ rad/sec

Case (c) shows the lowest rise time of approximately 0.2 sec. The same feedback gain values will be considered later to control the robot arm joints.

## 2.2 A Learning Control Scheme

The second order system considered may be represented as (from Fig. 2),

$$(Is^2 + K_2s + K_1)\theta = \theta_c \quad (5)$$

1, the command function,  $\theta_C$ , is the same as the desired trajectory,  $\theta_d$ , is

$$\dot{\theta}_d - \dot{\theta}_a + b(\theta_d - \theta_a) \quad (6)$$

re constants proportional to the error rate and the error, respectively. For  
the command signal,  $\theta_C$ , is modified as,

$$\theta_C + \theta_e \quad (7)$$

the system to this modified command signal is determined. The new error  
obtained using Eq. (6) The command signal is again modified according to  
w command signal is used in Eq. (2.5) and the response of the system is  
: process is repeated until the errors,  $\theta_e$ , fall within an acceptable value.

ndy is possible for the second order system considered here. Eq. (5)  
second order system is written in a slightly different form for the kth

$$\theta_k = \theta_{ck} \quad (8)$$

eration the equation as

$$1 + K_1 \theta_{k+1} = \theta_{ck} + \theta_{ek} \quad (9)$$

$$k) + b(\theta_d - \theta_k) \quad (10)$$

(8) from Eq. (9), we get

$$= \theta_{ek} \quad (11)$$

$k$

$$ad_k + bd_k \quad (12)$$

$$(\tau) d\tau \quad (13)$$

Then

$$\begin{aligned}
 J_{k+1} &= \int_0^t \theta_{ek+1}^2(\tau) d\tau \\
 &= \int_0^t \left[ \theta_{ek} - (a\dot{d}_k + bd_k) \right]^2 d\tau
 \end{aligned}$$

Expanding and using equations (13) and (10), we get

$$\begin{aligned}
 J_k - J_{k+1} &= \int_0^t \{ (2aq - a^2 - 2b) \dot{d}_k^2 + (2bp - b^2) d_k^2 \} d\tau + a\dot{d}_k^2(t) \\
 &\quad + (ap + bq - ab) d_k^2 + 2bd_k\dot{d}_k \\
 &\geq 0, \text{ for } a^2 > 2b \\
 &\quad \quad \quad a < 3q/2 \\
 &\quad b < 2p \text{ and for small error rates}
 \end{aligned} \tag{14}$$

Eq.(14) gives sufficient conditions for the guaranteed convergence of the error to zero value with each step of the proposed iteration scheme.

Since only the command signals are being modified, the torque requirements on the actuators will not drastically change provided the initial errors are small. The feedback values selected for the application in this section are  $K_1 = 100$  and  $K_2 = 20$  and corresponds to a closedloop frequency of 10 rad/sec. The response of the servosystem to a command input,

$$\theta_C = \sin(\omega t)$$

is shown in Fig. 3 for  $\omega = \pi$  rad/sec. The actual trajectory shows a phase lag and an amplitude modification. Application of the learning control scheme shows reduced errors with the first iteration (Fig. 4) and the third iteration (Fig. 5) and for the parameters  $a = 0.1$  and  $b = 0.9$ . The figures compare average errors associated with each iteration. The average

as

$$AE = \frac{\sum_{i=1}^{NP} |\theta_{ei}|}{NP} \quad (15)$$

number of points on the trajectory. Higher values of  $\omega$  were considered next and the convergence of the iteration scheme was studied. Fig. 6 shows the average error for each iteration for various values of "a" and "b" and for  $\omega = 2\pi$  rad/sec. The results clearly show that for the case in which  $a = 0$ , the errors tend to increase after a certain number of iterations in accordance with the derived conditions (Eq. (14)). Similar results are observed for  $\omega = 4\pi$  rad/sec. In general, the results show that the rate of convergence increases with increasing values of "a" up to a certain value. For the present study, the best results are obtained with  $a = 0.2$  and  $b = 0.8$  at all values of  $\omega$ . The increasing error rate in the modification procedure is obvious from Figs. 6 and 7. It is observed that the conditions given by Eq. (14) are rather conservative.

### 1 Phase Adjustment Technique

From the previous results that there is a unique command function,  $\theta_C$ , for a given desired trajectory,  $\theta_D$ , will be the same as the desired trajectory, at least for single-output systems. In the previous examples, inclusion of the error feedback helped a great deal in arriving at the unique command function with only a few iterations. The next obvious question is whether it is possible to obtain the ideal command function with a single iteration so that the resulting trajectory would follow the desired trajectory. An attempt has been made in this section to answer the question.

The response of the second order system shows that the output of the system follows the desired trajectory, provided the frequencies associated with the function are well within the system bandwidth. As the input frequency approaches the system bandwidth, the output of the system shows marked deviation from the input signal. The input-output relationship is studied and the gain plots in which the phase difference and the ratio of the output to the input are plotted as a function of the input frequency.

In the previous example,  $\theta_D = \sin(\omega t)$ , with  $\omega = \pi$  rad/sec. The time response of the system is as shown in Fig. 3., for the first trial. A modification scheme was employed with  $a=0.1$  and  $b=0.9$ . The actual trajectories obtained in the first and third iteration are shown in Figs. 4 and 5, respectively. From Fig. 3 values of phase (-0.5969 rad) and gain (0.91) were obtained. The command function was modified as

$$\theta_D = \sin(\omega t + 0.5969)$$

The trajectory obtained for this modified command signal is shown in Fig. 8. The actual trajectory and the desired trajectory overlap within the accuracy of the plotter. Thus, for a linear system, it was possible to obtain a modified command signal to follow the desired trajectory without an iteration scheme. This method will be applied to the control of a three-link robot system in section 3, which is an example of a nonlinear system.

### 3.0 APPLICATION TO A THREE-LINK ROBOT

#### 3.1 Dynamics of a Three-Link Robot Arm

Fig. 9 shows the selected coordinate reference frame for the three-link robot arm. X, Y, Z, is the inertial system with the origin at joint 1. The fourth coordinate frame has the origin fixed at the tip of the robot arm. The first link can rotate only about the vertical axis Z, carrying the second and the third links. The second link can rotate about an axis fixed in link 2 and is normal to both the first and the second link. The third link moves about an axis parallel to the axis of rotation of the second link.

The three transformations are represented by the following matrices

$$\begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \begin{bmatrix} C_1 & -S_1 & 0 & 0 \\ S_1 & C_1 & 0 & 0 \\ 0 & 0 & 1 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_1 \\ Y_1 \\ Z_1 \\ 1 \end{bmatrix}$$

or  $r = [A_1] r_1$  (16)

$$\begin{bmatrix} X_1 \\ Y_1 \\ Z_1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & C_2 & -S_2 & C_2 d_2 \\ 0 & S_2 & C_2 & S_2 d_2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_2 \\ Y_2 \\ Z_2 \\ 1 \end{bmatrix}$$

or  $r_1 = [A_2] r_2$  (17)

$$\begin{bmatrix} X_2 \\ Y_2 \\ Z_2 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & C_3 & -S_3 & C_3 d_3 \\ 0 & S_3 & C_3 & S_3 d_3 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_3 \\ Y_3 \\ Z_3 \\ 1 \end{bmatrix}$$

or  $r_2 = [A_3] r_3$  (18)

where  $C_j = \cos \theta_j$ , and  $S_j = \sin \theta_j$ ,  $j=1,2,3$

A point  $r_i$  described with respect to link  $i$  can be related to the base coordinate by

$$r = [T_i] r_i \quad (19)$$

where,  $T_1 = [A_1]$ ,  $T_2 = [A_1][A_2]$ , and  $T_3 = [T_2][A_3]$

The dynamic equation for the robot arm is obtained as, <sup>17</sup>

$$F_i = \sum_{j=1}^3 D_{ij} \ddot{q}_j + I_{a_i} \ddot{q}_i + \sum_{j=1}^3 \sum_{k=1}^3 D_{ijk} \dot{q}_j \dot{q}_k + D_i \quad (20)$$

where:

$$D_{ij} = \sum_{p=\max(i,j)}^3 \text{Trace} \left( \frac{\partial T_p}{\partial q_j} J_p \frac{\partial T_p^T}{\partial q_i} \right)$$

$$D_{ijk} = \sum_{p=\max(i,j)}^3 \text{Trace} \left( \frac{\partial^2 T_p}{\partial q_j \partial q_k} J_p \frac{\partial T_p^T}{\partial q_i} \right)$$

$$D_i = \sum_{p=1}^3 -m_p g^T \frac{\partial T_p^T}{\partial q_i} r_p$$

$I_{a_i}$  is the  $i^{\text{th}}$  actuator inertia,  $m_p$  is the mass of the  $p^{\text{th}}$  link

$g$  is a vector in the direction of the gravity force

$J_p$  is a pseudo inertia matrix for the  $p^{\text{th}}$  link

Eq. (20) are used to compute the joint torques required. For the purpose of simulation of the first, second and the third links are assumed to have lengths equal to 0.5m, 0.4m, and masses 4kg, and 2 kg, and 1kg, respectively. The inertias of the links 1,2, and, 3 are assumed to be  $5 \times 10^{-4}$ , and  $2.5 \times 10^{-4}$ , and  $1.25 \times 10^{-4} \text{ kgm}^2$ , respectively. Actuator inertias corresponding to joints 1,2, and, 3 are taken to be  $1 \times 10^{-3}$ ,  $5 \times 10^{-3}$ , and  $2.5 \times 10^{-4}$ ,  $\text{kgm}^2$  respectively.

### 3.2 Inverse Kinematics

The trajectory to be traced by the robot arm is given by a set of points which are usually defined in the base (inertial) coordinate system. Therefore, it is necessary to find the joint angles corresponding to each point on the trajectory using the geometry of the robot. Let us assume that the tip of the robot arm follows the given trajectory, so that a transformation of the tip point into the base coordinates can be made as follows:

$$(P) = [T_3] (r_3) \quad (21)$$

where  $r_3$  is actually the origin of the fourth coordinate system. Substituting for  $T_3$  and expanding we get,

$$P_x = -S_1(C_2D_2 + C_23D_3) \quad (22)$$

$$P_y = C_1(C_2D_2 + C_23D_3) \quad (23)$$

$$P_z = D_1 + D_2S_2 + D_3C_23 \quad (24)$$

Algebraic manipulations of the above equations give the expressions for the joint angles as

$$\theta_1 = -\tan^{-1} (x_1/y_1) \quad (25)$$



$$\frac{-d_1}{d} - \cos^{-1} \left\{ \frac{d^2 + d_2^2 - d_3^2}{2dd_2} \right\} \quad (26)$$

$$\frac{1/c_1)^2 + (z_1 - d_1)^2 - d_2^2 - d_3^2}{2d_2d_3} \quad (27)$$

compute the joint angles only once in order to find the command signals. This can be done off-line using the robot central computer in the iterative technique is then applied to modify the joint angle commands to eliminate errors to zero.

### Control system

employed here is to control the motion of the joints so that the tip of the trajectory. Independent control of each of the joints based on only the position and rate feedbacks is considered here for the sake of simplicity. defined in the base coordinate system is converted into joint command angles kinematics. The dynamic equations (20) are rearranged for the control techniques as follows.

$$\sum_{k=1}^3 D_{ijk} \dot{\theta}_j \dot{\theta}_k - \sum_{j=1}^3 D_{ij} \ddot{\theta}_j - D_i \} / (D_{ii} + I a_i) \quad (28)$$

in angular coordinates,  $T_{ci}$  is the torque about the joint  $i$ . Control is defined from the block diagram shown in Fig.1 as

$$T_c(\theta_i - \theta_c) \quad (29)$$

is a sixth order nonlinear differential equation with coupled coefficients. It is numerically solved here using a fourth order Runge-Kutta integration

### of Learning Control Scheme

is the case in which the desired trajectory for the tip of the arm is a circle. defined in the inertial coordinate system as follows.

$$s(\omega t) \quad (30)$$

$$0.5 \sin(\omega t)$$

is modified so that the joint command angles are obtained from the inertial system through a kinematic transformation. The computer time required is approximately 20 minutes and hence only four iterations are considered. The results obtained are shown in Fig. 11. There are two curves in Fig. 11 relating to the errors associated with X and Z coordinates. The errors in

the Y direction is not so important and is not shown here. It may be seen that the errors tend to become smaller at a faster rate when the error rate information is included in the command input modification procedure. Fig. 12 shows the torque characteristics of the joints 1 and 2 before and after the application of the learning control scheme. Figs. 13 to 15 show the actual response of the robot corresponding to  $a=0$  and  $b=1$ . A trajectory very close to the desired circular trajectory could be obtained with  $a=0.1$  and  $b=1$  after 6 iterations (figure not shown).

### 3.5 Application of Gain and Phase Adjustment Technique

It was shown in section 2.3 that a modified command input could be obtained so that the resulting actual trajectory is very close to the desired trajectory for linear dynamic systems. However, the robots are in general are characterized by nonlinearities and varying moments of inertia parameters. Coupling between the joint coordinates are also very significant. Two examples of trajectory tracing, one a circle and the other a straight line, is considered for the application of the gain and phase modification technique.

The trajectory defined by Eq.(30) describes a circle in the X-Z plane. The actual trajectory traced by the robot is given in Fig. 13. The responses of the robot after first and fourth iterations using the learning scheme are as shown in Figs. 14 and 15, respectively. It may be seen that even after four iterations the trajectory traced is still not a complete circle. The gain and phase modification technique was then attempted as follows.

The response of the system to the command trajectory which is the same as the desired trajectory was plotted in the X and Z coordinate system as a function of time (not shown). Ideally, X coordinate should be a cosine function and Z a sine function as given by Eq. (30). However, depending on the value of  $w$ , there will be a phase and gain change. The actual response was found to fit the following functions.

$$\begin{aligned} X &= \cos(\omega t - 0.17) \\ Z &= \sin(\omega t - 0.19) \end{aligned} \quad (31)$$

Modified command signals were then obtained as

$$\begin{aligned} X &= \cos(\omega t + 0.17) \\ Z &= \sin(\omega t + 0.19) \end{aligned} \quad (32)$$

The response of the robot to the modified command signal is as shown in Fig. 16. The actual trajectory obtained is seen to be very close to the desired trajectory. It is very interesting to see that the nonlinearity, the coupling between the joint coordinates, gravity and the varying moments of inertias did not have much effect as far as the phase shift and gain values are considered. The present example, however, is very simple because the desired trajectory could be represented by simple sine and cosine functions.

The second example considered is the one in which the tip of the robot traces a straight line. The joint angles will have to go through a nonlinear motion so that the tip of the robot could result in a straight line. Hence, this example is more complicated than the first case. The command function in the inertial coordinate system for the example of a straight line is taken to be

$$X = 0.5 - 0.5 w t$$

Y  
Z

The response system with  $w = 1$  is as shown in Fig. 17. For the sake of simplicity, only the  $X$  coordinate is considered for modification. Learning control scheme is then used to obtain a trajectory after 6 iterations as shown. For the application of gain and phase mod, the command signal for the  $X$  coordinate is obtained as follows.

$$X = 0.5 w t + X_e(t + t_p) X_g$$

where  $X_e$  is obtained as

$$X_e = X_a$$

and  $t_p$  is the shift obtained from the first trial. The response obtained with this modified command is shown in Fig. 17. The phase  $t_p$  is taken to be 0.18 secs and the gain,  $X_g$ , 1.1 (trial and error). The actual trajectory obtained for this command is almost as good as the trajectory obtained through 6 iterations.

The phase,  $t_p$ , gain,  $X_g$ , were also obtained by a Fourier analysis of the error function associated with the trajectory. Fig. 18 shows the response of the corresponding modified command ( $w = 0.2$  secs and  $X_g = 1.117$ ). The response appears to be at least as good as the response shown in Fig. 17. Hence, it may be concluded that the Fourier analysis can be used to compute the phase and gain value to obtain a modified command and to reduce errors considerably in the second trial. Further minimization of errors may be done by the iterative technique, if necessary.

### 3.6 Application to a Real Robot

The performance improvement technique is attempted on a real robot PUMA 560. Fig. 19 shows a schematic diagram of the robot. Instructions to the robot arm is given by using the operating system software, VAL-II<sup>18</sup>. Different values of the coefficient of the error are considered (with the parameter 'a'=0) to study the rate of convergence of the scheme to yield minimum errors. Fig. 20 shows the performance of the robot after 11 iterations for a desired trajectory of the robot to move along the  $Y$  axis at approximately 1.5ft/sec. The figure shows the error in the  $X$  direction with the first attempt and after 11 iterations with  $b=0.2$ . The error associated with the first trial is 0.4145mm and, after 11 iterations, 0.07mm.

The same case was then repeated with various values of the error coefficient,  $b$ , and the average errors obtained as a function of the trial number are shown in Fig. 21. The results clearly show that the rate at which the average error decreases is proportional to the value of  $b$ . However, larger values of  $b$  tends to increase the average error after a few iterations. This trend was also observed and discussed in section 2.

The iterative technique was also applied to improve the performance of the robot under a variety of other operating conditions. The results show, in general, that the lower limit of the average error after reached (which is 0.1mm) is restricted by the repeatability and the noise associated with the joint sensors. Further work is continuing at this time to include the rate information in the application of the learning scheme to the real robot.

## 4.0 CONCLUSIONS

An off-line learning control scheme is analyzed here which can be used to improve the performance of robots. Necessary conditions for the iterative scheme to reduce errors with each iteration are derived considering a second order servo system model. The scheme is also applied to a mathematical model of a three-link robot similar to PUMA 560. In general, the results show that the learning control scheme reduces errors more efficiently if the error rate information is included in the scheme. The results also show that the scheme may increase the magnitude of the errors, if the rate information is not included in the iteration scheme. Preliminary results of the application of the technique to a real robot has shown that the scheme can be successfully used to improve the performance of actual robots within the limitations of the repeatability and noise characteristics of the robots.

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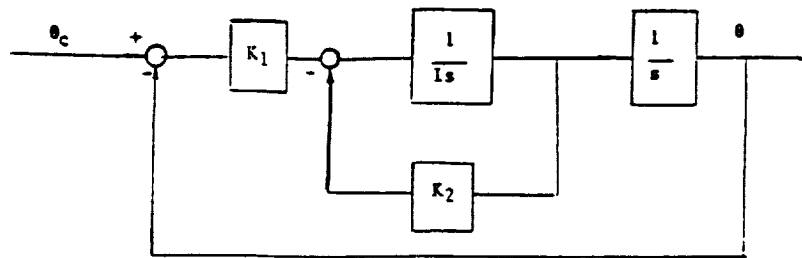
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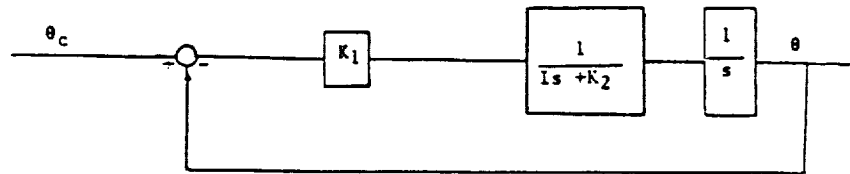
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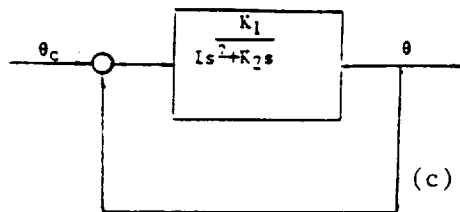
"User's Guide to VAL" Unimation, Inc., Danbury, Connecticut.



(a)



(b)

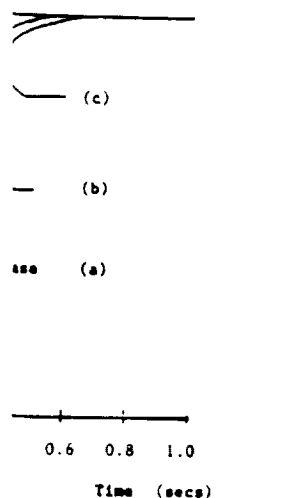


(c)

Closed-Loop Transfer Function:

$$\frac{\theta}{\theta_c} = \frac{K_1}{Is^2 + K_2s + K_1}$$

Block-Diagram Representation of the Servo Control System and (c) Block-Diagram Reduction Steps



Input Response for different sets of Gain

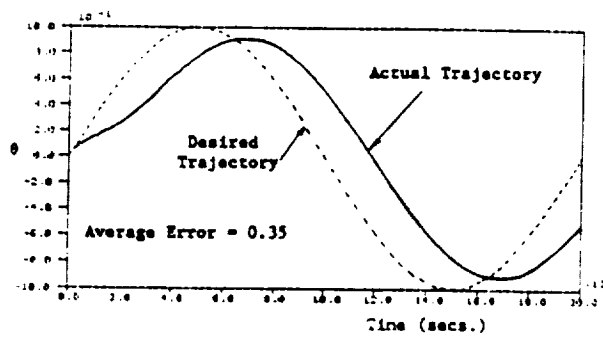


Fig. 3. Transient Response of the Servosystem

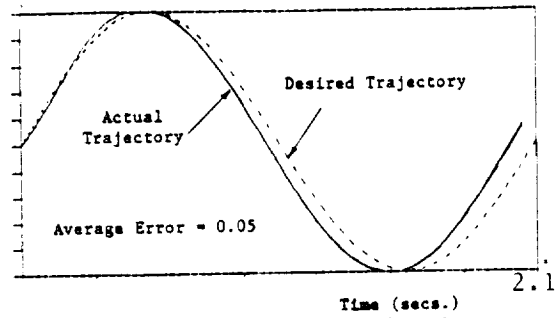
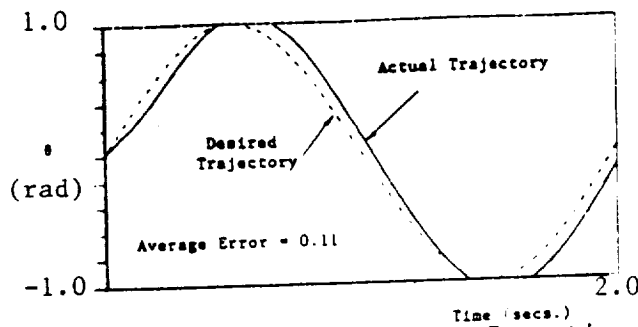
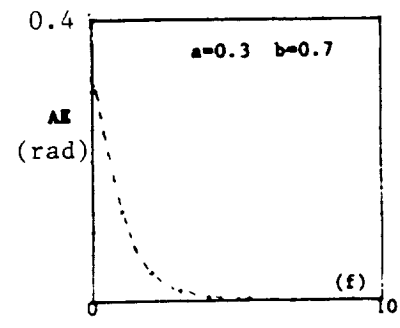
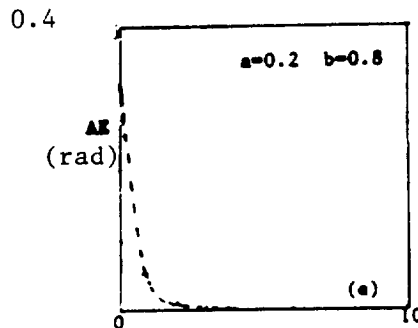
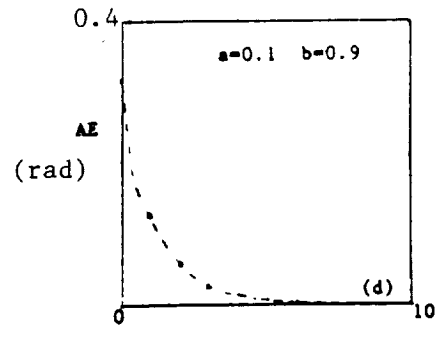
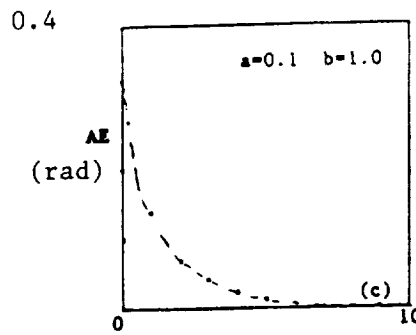
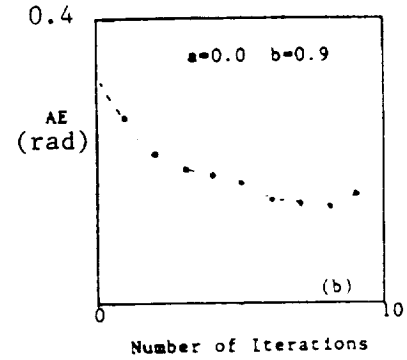
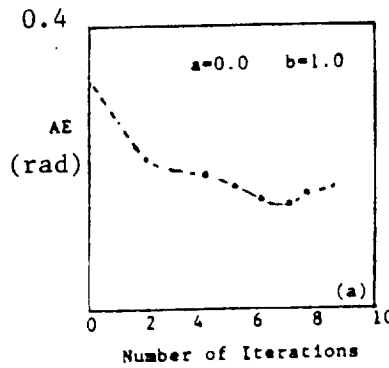


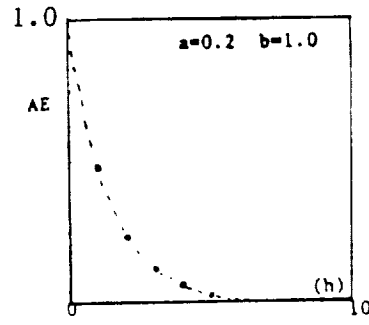
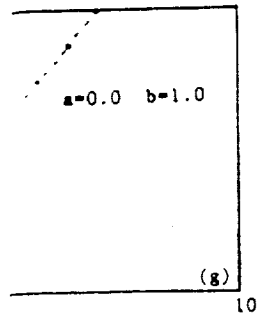
Fig. 4 Response After First Iteration Fig. 5. Response After Third Iteration



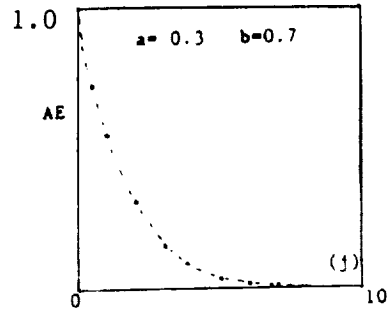
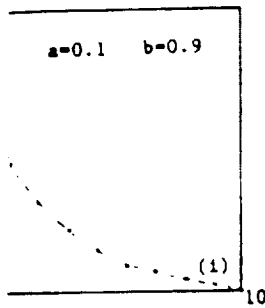
$$X_c = \sin \omega t$$

$$\omega = 2 \pi \text{ rad/sec}$$

Fig. 6. Error Convergence of the Servosystem with the Learning Control Scheme

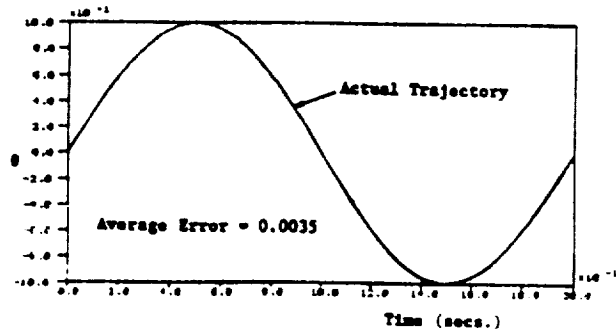


Number of Iterations



$$c = \sin(\omega t) \quad \omega = 4 \pi \text{ rad/sec}$$

Convergence of the Servosystem with the Learning Control Scheme



Use of the System for the Modified Command Input



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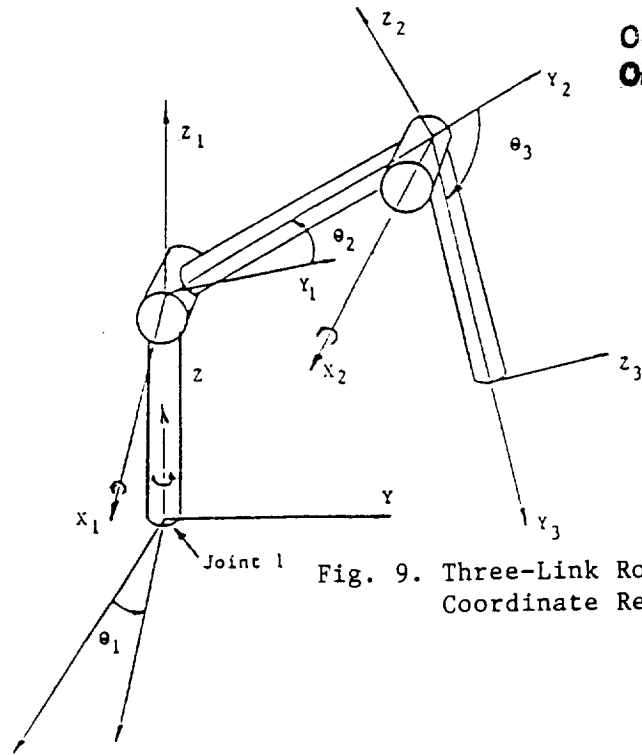
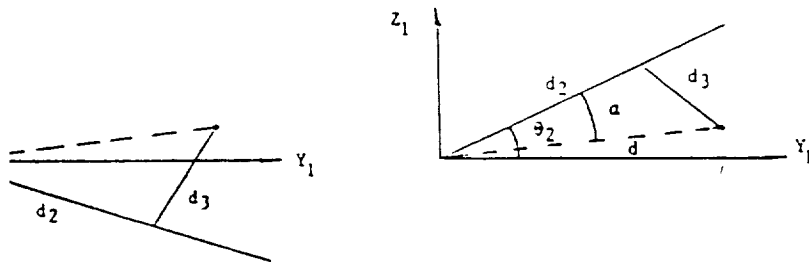
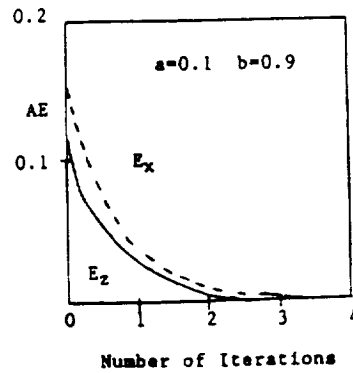
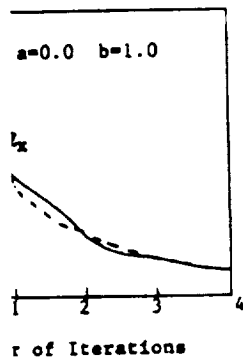


Fig. 9. Three-Link Robot Arm and the Coordinate Reference Frames



ible Configurations of Links 2 and 3 to reach a  
int



Convergence for a Three-Link Robot Computer Model

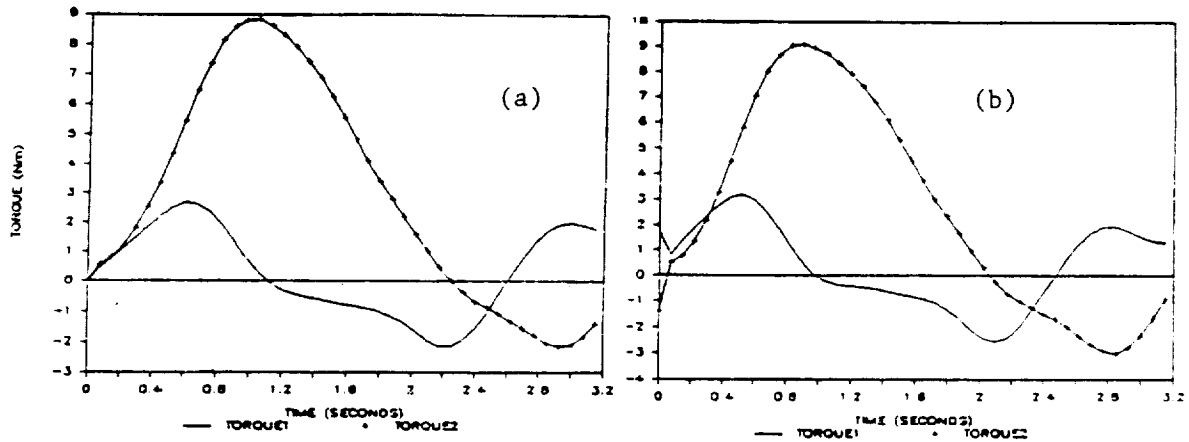


Fig. 12. Torque Characteristics (a) First Trial  
(b) After Four Iterations

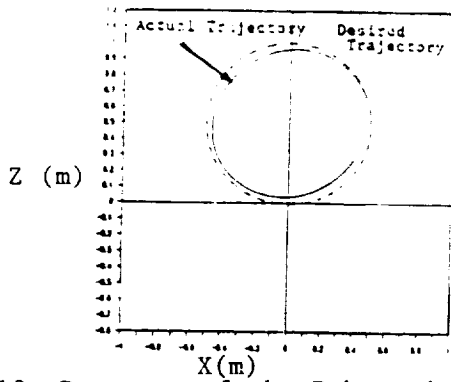


Fig. 13. Response of the Robot with Command Input Same as Desired Trajectory

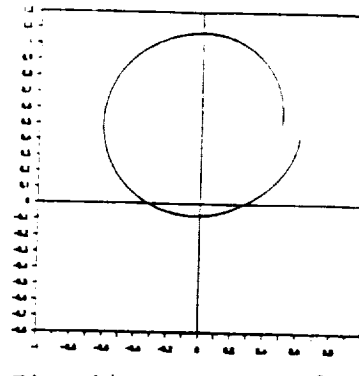


Fig. 14. Response of the Robot After 1 Iteration

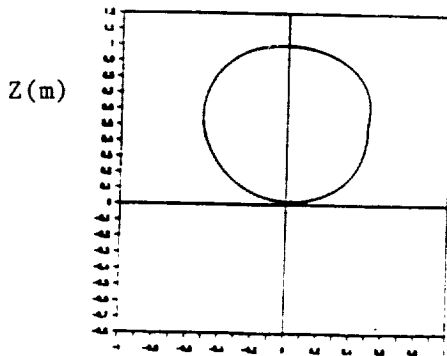


Fig. 15. Response of the Robot After Four Iterations

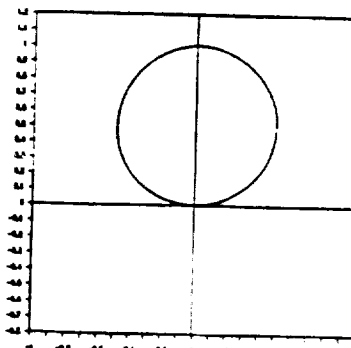


Fig. 16. Response of the Robot for a Modified Command Input

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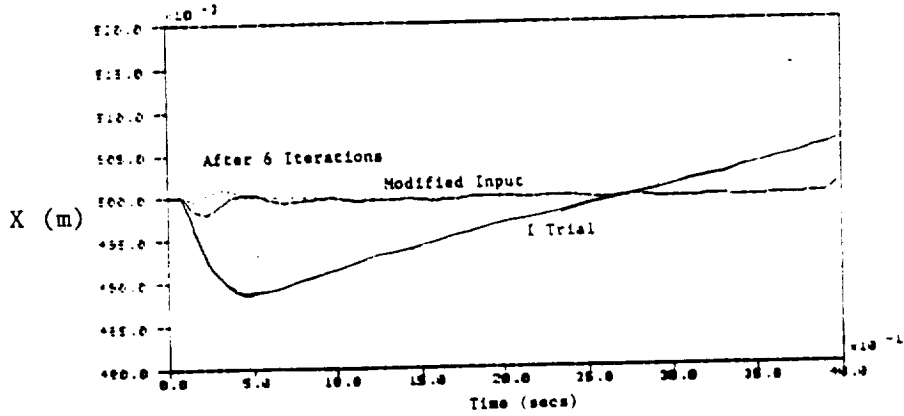


Fig. 17. Response of the Robot After 6 Iterations and A Modified Command Input

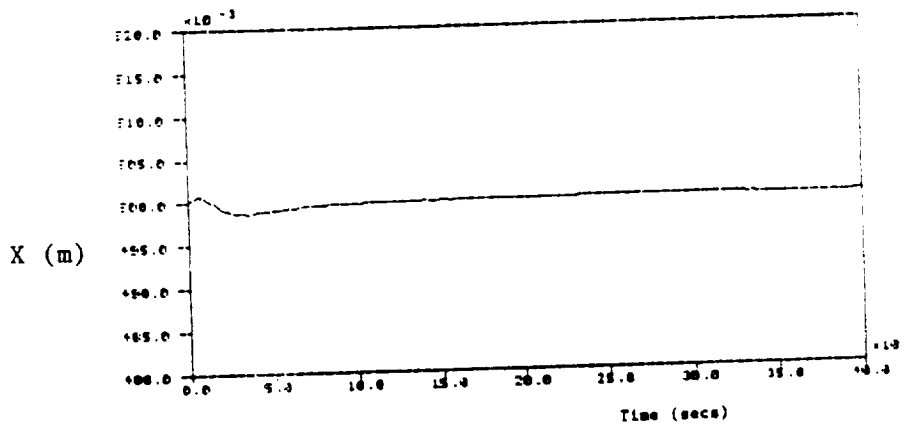


Fig. 18. Response of the Robot for a Modified Command Input  
( $t_p = 0.2$  secs.)

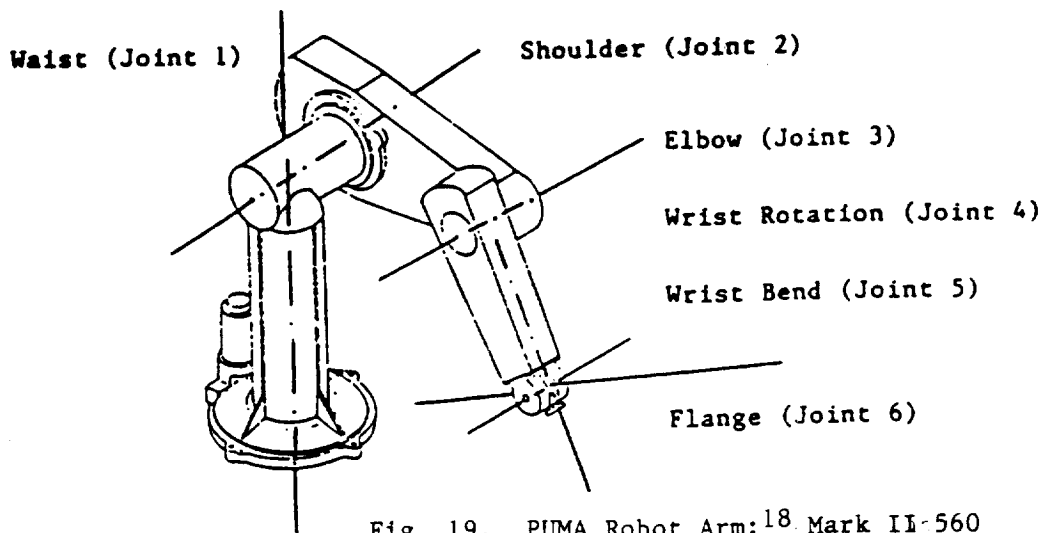


Fig. 19. PUMA Robot Arm: 18 Mark II-560

Fig. 20

STRAIGHT LINE ALONG Y AXIS,  
ATTACHED PAYLOAD NONE, SPEED 150

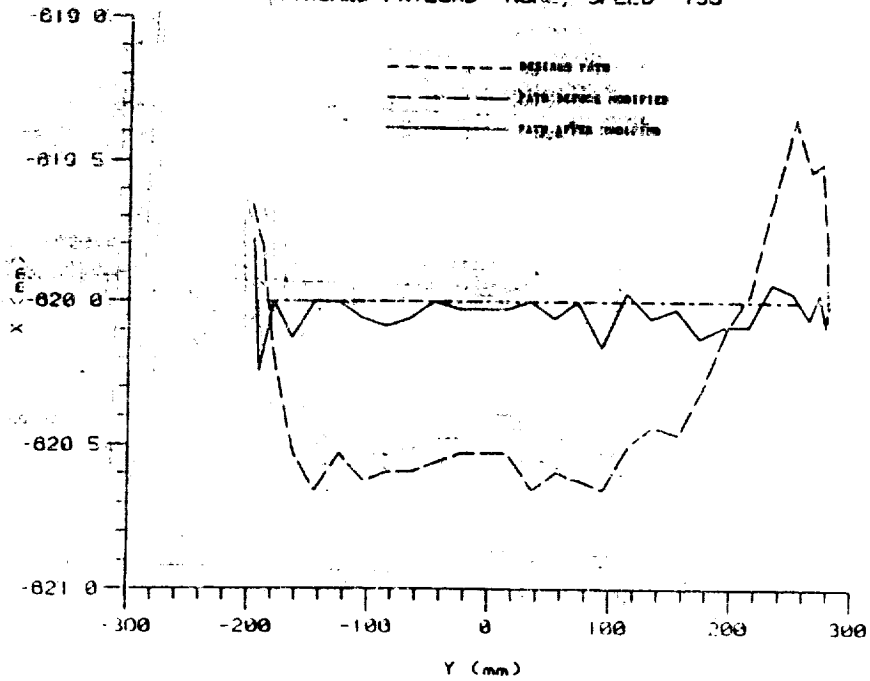
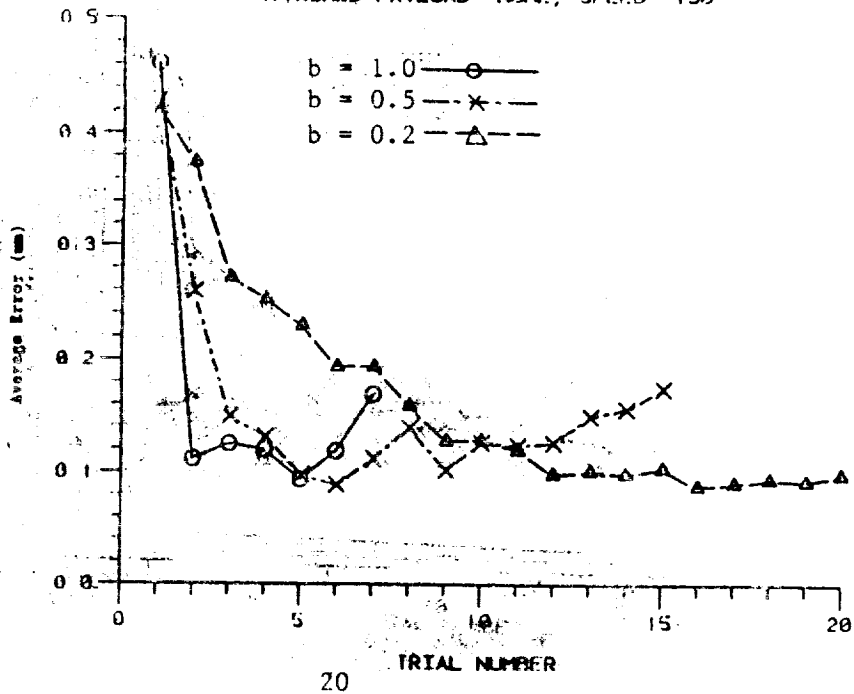


Fig. 21

STRAIGHT LINE ALONG Y AXIS,  
ATTACHED PAYLOAD NONE, SPEED 150



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