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Computing Induced Velocity
Perturbations Due to a
Helicopter Fuselage
in a Free Stream

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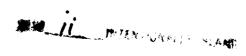
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Contents

Introduction
Symbols
Mathematical Formulation
Experiment
Results and Discussion
Concluding Remarks
Appendix A—Source-Panel Formulation
Symbols
Potential Formulation
Near-Field
Mid-Field
Far-Field
Appendix B—Fuselage Geometry Description
Symbols
General Equation
Tables
Appendix C—Analysis of Measurement Accuracy
Symbols
Tunnel Velocity Accuracy
Laser Velocimeter Accuracy
Effect of Tunnel Velocity Accuracy
Uncertainty in Presented Perturbation Velocities
References
Tables
Figures
References
Tables
Figures 56

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Introduction

To understand and predict the complex flow associated with rotorcraft, particularly in forward flight, the elements contributing to the flow must be identified and properly modeled. The rotor and its wake are the major contributors to the flow field, and significant work has been performed to identify the effect of the lifting rotary wing on the flow field. A historical perspective of this work is presented in reference 1.

Rotor inflow has a significant effect on the performance of the rotor. Inflow is the effective flow seen at the rotor disk and is affected by several factors: the free-stream velocity, the rotor/wake induced velocities, and fuselage induced velocities. Rotor performance codes use inflow models that range from the assumption of uniform inflow to complex, timevarying, vortex filament, "free-wake" models and, generally, ignore the effects of the fuselage on the velocities seen by elements of the lifting rotor.

The fuselage affects the rotor inflow in two ways: the velocity perturbation due to the presence of the fuselage, and the velocity perturbations due to changes in the rotor wake. The effect of the velocity perturbation due to the fuselage can be modeled using potential-flow theory, whereas the effect of the fuselage on the rotor wake is a highly complex problem from which no simple models have been developed. To date, the effect of the fuselage on the flow field has been studied with a relatively limited effort. Several researchers have considered the effects of the fuselage both experimentally (refs. 2–9) and with analysis (refs. 10–17).

The effects of the fuselage have been modeled by previous researchers in various ways. The work of Crimi and Trenka (ref. 10) modeled both the rotor wake and the fuselage in predicting the downwash field of the helicopter. The source-panel method is used by Keys (ref. 5) for the fuselage effect on angle of attack at the rotor. An assessment of the fuselage effects on rotor performance and loads using a simple axisymmetric fuselage was made by Johnson and Yamauchi (ref. 15). The work of Ryan et al. (ref. 17) demonstrates the effect of modeling a region of separated flow from the fuselage on velocities at the rotor plane. The effect of the fidelity of fuselage modeling on the rotor-inflow velocities has not been demonstrated by any of the researchers.

An experimental rotorcraft program has been undertaken to provide detailed measurements of rotor inflow (refs. 18–25). These data have been used to evaluate the rotor-inflow models used by rotor performance codes (refs. 18 and 24). These flow field measurements were made with a two-component laser

Doppler velocimeter over a helicopter model with a realistic, although simplified, fuselage. Data were also collected over the fuselage without a lifting rotor to assess the magnitude of the isolated fuselage perturbations.

The purpose of this study is to assess the effect of the fuselage used in the experimental rotorcraft program on the inflow velocity field. A potentialflow, source-panel method is used to predict the inflow velocity perturbations due to the fuselage for a fuselage with three levels of complexity, and these perturbations are compared with the experimental flow field measurements. Predictions of the velocity perturbations for the rotor conditions investigated in the experimental rotorcraft program are presented. The data and analyses presented in this report show the velocity perturbation due only to the presence of the fuselage since the data were collected and computed in the absence of the rotor. The use of these data presumes that superposition of fuselage and rotor/wake effects can be used to model the combined flow field.

Symbols

 $ec{V}_{\infty}$

The symbols used in the basic report are given as follows:

A	influence coefficient matrix
a	aerodynamic influence coefficient (see eq. (2))
В	scalar array of boundary condition
$ec{n}$	surface normal vector
0	occurrences
O_u, O_w	occurrences in u and w velocities, respectively (see table 1)
\boldsymbol{p}	point on body of potential evaluation
\boldsymbol{q}	source location on body
R	reference radius, Fuselage length/2, 3.33 ft
r	radial distance from hub center
r_m	rotor radius of specific rotor blade set
S	scalar array of source strength
U, W	velocity components (laser velocimeter), fps
u	tangential velocity perturbation (downstream tangent to rotor plane), fps
V_{∞}	free-stream speed, fps

free-stream velocity vector, fps

v	lateral velocity perturbation (lateral tangent to rotor plane), fps
w	normal velocity perturbation (normal to rotor plane), fps
x, y, z	Cartesian coordinates
α	rotor-disk angle of attack, deg
σ	source strength; also standard deviation where indicated
ψ	rotor azimuth angle (counterclockwise from downstream), deg

Mathematical Formulation

The mathematical basis for the analysis code is classical potential flow. Green's theorem is used to describe the potential field as integrals of singularity functions over the boundaries of the flow. A source-panel method, based on the work of Hess and Smith (refs. 26 and 27), has been implemented for body configurations that can be modeled with quadrilateral panels. Appendix A contains the basic formulation of the relations between the strength of a distributed source over a quadrilateral panel and the velocity produced at any point in space. The relations shown in appendix A are implemented as a subroutine that computes a velocity vector for a panel geometry, strength, and field point.

The source-panel method has been in use for over 20 years and has an established record for analysis of incompressible potential flow. The implementation here uses existing mathematical relations with current computer-solution techniques not possible when the original formulation was implemented.

A computer program was developed to solve for the source strengths over arbitrary paneled shapes in the presence of uniform flow. The solution was developed by satisfying the no-penetration condition at each panel centroid. The form of this equation is

$$\sum_{q} d\vec{V}_{q} \cdot \vec{n}_{p} = -\vec{V}_{\infty} \cdot \vec{n}_{p} \tag{1}$$

where $d\vec{V}_q$ is the portion of the velocity vector at p due to the source panel at q.

A system of linear equations can be formed for the unknown source strengths:

$$\begin{bmatrix} a_{11} & a_{12} & \dots & a_{1N} \\ a_{21} & a_{22} & \dots & a_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ a_{N1} & a_{N2} & \dots & a_{NN} \end{bmatrix} \begin{bmatrix} \sigma_1 \\ \sigma_2 \\ \vdots \\ \sigma_N \end{bmatrix} = \begin{bmatrix} -\vec{V}_{\infty} & \cdot \vec{n}_1 \\ -\vec{V}_{\infty} & \cdot \vec{n}_2 \\ \vdots \\ -\vec{V}_{\infty} & \cdot \vec{n}_N \end{bmatrix}$$
(2)

In matrix notation, this system can be written as a coefficient matrix **A** that is multiplied by the unknown scalar array of the source strength **S** and set equal to the scalar array of the boundary condition **B**.

The elements of the coefficient matrix **A** are computed using the velocity-computing subroutine described above and detailed in appendix **A**, but substituting the value of unity for the source strength of the panel. The unknown scalar array of source strength **S** can be solved by the normal methods for linear systems.

In the specific program used for the analysis presented, the linear system is solved by lower-upper decomposition by Crout's algorithm with implicit partial pivoting and back substitution using the implementation of reference 28. Once the source strengths are known, the field point velocities are computed by the same subroutine used to compute the coefficient matrix elements. The program saves the decomposed coefficient matrix so that new strengths can be computed by changing the right-hand-side vector and returning to the back-substitution step for the unknown source strengths.

Experiment

Experimental measurements of the perturbation velocity due to a representative helicopter fuselage were made during a helicopter inflow-measurement program. The rotor-inflow data are reported in references 19–23. The isolated fuselage velocities are reported here. The experiment was conducted in the Langley 14- by 22-Foot Subsonic Tunnel. This facility is an atmospheric, closed-circuit tunnel designed specifically for high-lift and powered-model testing at low to moderate speeds. The facility is described in detail in references 29 and 30. The perturbation velocity measurements were made using a two-component laser velocimeter (refs. 31 and 32).

The fuselage shape used in this study is an analytic shape that can be parameterized using easily defined coordinates. The specific geometry is described in references 4 and 33, and the equations, their coefficients, and tabulated coordinates are given in appendix B. This geometry consists of a slender main body with a slender nacelle portion about the rotor shaft. The model is shown mounted for testing in figure 1; however, the measurements presented here were taken without the rotor blades.

The velocity measurements were made along the fuselage centerline 3 in. above the plane that would have been the rotor tip path plane if a rotor had been operating on the model. This includes an assumption of no oscillatory flapping about the rotor shaft axis, a steady coning of the rotor blades of 1.5°, and a

shaft angle tilt of 3° nose down. Figure 2 shows the locations used in the inflow investigation relative to the fuselage. The free-stream velocity was held at approximately 94 fps to simulate an advance ratio of 0.15 with an assumed tip speed of 624 fps. The fuselage attitude with respect to the rotor shaft was 2.5° nose up, giving the fuselage an effective angle of attack with respect to the free-stream velocity of 0.5° nose down. The assumed radius of the rotor blades r_m was 33.88 in.

The measured velocities are presented in table 1 as perturbation velocities normalized by the tunnel free-stream velocity and in the tip-path-plane reference system. The normal (u) and tangential (w) components of perturbation velocity are computed from the laser velocimeter components, U and W, by

$$u = (U - V_{\infty})\cos\alpha + W\sin\alpha \tag{3}$$

and

$$w = W \cos \alpha - (U - V_{\infty}) \sin \alpha \tag{4}$$

The nondimensional mean velocities for the u- and w-components are listed, as well as the standard deviation σ and the number of samples or occurrences O that determine each average. The average tunnel free-stream velocity V_{∞} for each data point is also listed.

It should be noted that the tunnel free-stream velocity was not determined using the laser velocimeter, but it was measured using wind-tunnel instrumentation. An error analysis of both laser velocimeter and tunnel velocity systems has been conducted, and the results are detailed in appendix C. The laser velocimeter measurements had a velocity accuracy from 1.19 to 1.80 percent for the test conditions of this experiment. The accuracy of the tunnel velocity measurements was approximately 8 percent of the free-stream velocity in this experiment. tunnel-indicated free-stream velocity has been corrected based on the laser velocimeter measurement farthest from the body disturbance. This correction, detailed in appendix C, amounts to approximately 4 percent of the experimental free stream. The correction reduces the error associated with the freestream velocities reported here to that of the laser velocimetry system. The large inaccuracy of the indicated tunnel velocity was found to be due to operator oversight and is applicable only for these reported data.

Results and Discussion

Three panel models of the experimental fuselage were constructed to predict the flow perturbations.

These predictions were made to compare with experimental results. The first model represents only the smooth portions of the experimental model, that is, the main fuselage shape and the faired nacelle shape. The resulting panel configuration for the first model is shown in figure 3 and is referred to as the ROBIN fuselage, which was derived from the rotor body interaction studies conducted at the Langley Research Center. (See refs. 2 and 4 for examples.) The code used to generate this basic fuselage shape is given in appendix B. The second and third models were constructed to assess the effect of more or less detail in the modeling of the fuselage and, in particular, the shaft and hub. The second model includes a simplified panel representation of the rotor shaft and hub. Because of the relative complexity of the hub and pitch change links, a radius was chosen for the shaft and hub body to represent the frontal area relative to the oncoming flow. The resulting panel configuration for the second model is shown in figure 4. The third model is a representation of the fuselage as an ellipsoid of equivalent fineness ratio relative to the fuselage width, in this case 1:8. The resulting panel configuration for the third model is shown in figure 5.

A comparison of the measured and computed velocity perturbations due to the fuselage along the measurement plane centerline is shown in figure 6. The figure also compares the predicted perturbation due to the three models for the fuselage. Two components of perturbation velocity will be presented, the normal component (relative to the plane of the rotor disk) and the tangential component (tangent to the rotor disk and directed downstream). The velocity ratios shown in this figure have the free-stream velocity removed from the local velocity and the result divided by the free-stream velocity. In figure 6(a) the normal component of the velocity perturbation is shown. In figure 6(b) the tangential component of the velocity perturbation is shown. The figures show a velocity ratio derived from the free-stream velocity and corrected as described in appendix C.

The velocity perturbation ahead of the hub shows good agreement with the measured experimental values, although all three fuselage models underestimate the normal component. The ellipsoid model underpredicts the flow by a wide margin, whereas the two ROBIN models have similar predictions at the most forward locations. As the hub is approached, the ROBIN fuselage and nacelle model does not predict the measured velocities as well as the model with the crude hub representation. However, close to the hub region, the crude model apparently overestimates the magnitude of the perturbations. Behind the hub the

models predict the normal component well, but they do not agree as well with the downstream component.

The disagreement between measured velocity perturbations and the predictions based on source-panel models behind the hub may be attributed to the large amount of unmodeled separated flow in this region of the flow. The existence of this separated region has been confirmed and is routinely accounted for in rotorcraft drag-estimation techniques such as that described by Keys (ref. 5). The flow over the aft portion of the fuselage is likely to be affected by both hub separation and perhaps some amount of fuselage separation. It is interesting to note that the simple ellipsoid fuselage shape comes closest to adequately predicting the downstream component of perturbation behind the hub. It is likely that the larger cross section of the ellipsoid in this region models the existence of separated flow in the aft section of the fuselage. With the exception of the two measurement locations closest to the hub, the ROBIN fuselage models, both without and with hub, predict the correct perturbation trend in the normal component. At the measurement location just ahead of the hub, the use of a hub model predicts the downstream component of perturbation well and shows the correct trend for the normal component prediction, although it overestimates the magnitude.

It is necessary to comment on the applicability of these computations. The computation and experiment are made in the absence of the rotor and its wake. The use of an isolated rotor/wake model with linear (i.e., superposition) inclusion of these fuselage effects ignores the possibility of wake deformation due to the fuselage and the effect of the rotor and wake on the source strength distribution on the fuselage surface. These nonlinear effects will be expected to change the magnitude and perhaps the local sign of the isolated fuselage interactions. This nonlinear effect must be properly modeled for complete rotor-fuselage interaction studies.

In a first-order sense, however, the assumption of linear superposition between the rotor wake and the fuselage may be a reasonable hypothesis. The reasoning for this assumption lies in the fact that the fuselage presents two disturbance types to the flow. The first disturbance is a volume disturbance that is modeled here as a source distribution on the surface. The second is a rotational disturbance that is formed by viscous action at the fuselage surface and is not modeled in this study. The volume disturbance of the fuselage has a direct effect on the wake trajectory but cannot change the strength of the wake elements. The rotational disturbance, however, has only a minor effect on the wake trajectory, but in close proximity, it can merge with the wake and thus

change its strength. If the rotational disturbance is weak, as is assumed here in the nonlifting fuselage assumption, the only effect on the wake is due to the trajectory perturbation. If the overall trajectory perturbations are small, the additional nonlinear effect of the fuselage on the rotor inflow is small. The actual magnitudes of these interacting disturbances must be assessed by either analysis or experiment to confirm this hypothesis.

For each of the experimental test conditions from references 19-23, which are summarized in table 2, the velocity perturbations are predicted using the source-panel method and the basic fuselagepanel configuration. The perturbations are predicted where the inflow velocity measurements occurred. The reference coordinates for locating the center of the radius/azimuth measurement plane are given relative to the fuselage coordinates. The basic fuselage, shown in figure 2, is 2R long with the x-coordinate of the nose station reference equal to zero. The fuselage midsection, from x = 0.40R to x = 0.80R, is constant with the x-coordinate and symmetrical in the y- and z-coordinates, thus giving the center of this uniform section to be the reference y=0 and z=0. In this coordinate system, the center of the inflow measurement plane is located at x = 0.685R, y = 0.0R, and z = 0.4074R. The inclination of the fuselage to the measurement plane is the experimental 2.5° from the reference fuselage waterline.

To help correlate the computed perturbations to the experimental rotor-inflow data found in references 19-23, the significant differences in rotor radius and angle of attack are summarized in table 2. The tests were conducted in these references at slight variations in angle of attack to account for the propulsive force required from the rotor to trim at each forward speed. The results of the calculation for velocity perturbation for these rotor conditions for the basic fuselage-nacelle model are given in table 3 which contains four subtables—two for each of the significant angles of attack and two for each of the rotor reference lengths. (The shorter rotor was not tested, however, at the higher angle of attack.) Results similar to those found in table 3(a) for the fuselage-nacelle-hub model are given in table 4. Results for the ellipsoid model are given in table 5.

To assess the effect of the minor differences in test condition, figure 7 presents maps of the w-component of velocity perturbation for three test conditions: (1) $r_m/R = 0.8470$ and $\alpha = -3.0^{\circ}$ (referred to as the reference test condition); (2) $r_m/R = 0.8470$ and $\alpha = -4.0^{\circ}$; and (3) $r_m/R = 0.8125$ and $\alpha = -3.0^{\circ}$. The change in rotor radius is simply a scaling of the radial dimension of the figure, since the rotor is not present. The variation in w-distribution between

conditions (1) and (2) is small and diminishes away from the hub.

Maps of the distribution of predicted velocity perturbations in the u-, v-, and w-components for the reference condition are presented in figures 8, 9, and 10, respectively. In each of these figures, the predictions from the three modeling configurations are given in parts (a), (b), and (c). Part (a) is the map from a panel configuration for the fuselagenacelle combination only, part (b) is a map from the fuselage-nacelle-hub panel configuration, and part (c) is a map from the ellipsoid fuselage configuration.

The effect of modeling the regions near the top of the fuselage on the tangential flow can be seen in figure 8. For a reasonable model of the fuselage and nacelle, the accelerated region is centered over the rotor shaft, thus coinciding with the closest region of the fuselage and amounting to 3 percent of freestream velocity. For the rough approximation to the rotor hub and fuselage, perturbation velocities approaching 10 percent of free stream are predicted at the sides of the hub model, but they reduce quickly away from the hub to levels comparable with the fuselage-nacelle model. For the ellipsoid, only a moderate (1 percent of free stream) velocity increase is predicted over the thickest portion of the fuselage. The ellipsoid model, however, showed better correlation with the measured velocities aft of the hub (fig. 6).

The effect of fuselage modeling on the lateral flow can be seen in figure 9. For the fuselage-nacelle model, the regions of maximum perturbation velocity are antisymmetrically distributed about the rotor shaft and amount to less than 2 percent of freestream velocity. The regions of largest perturbation are found at approximately 1/4 radius on either side of the fuselage centerline at approximately 1/4 radius ahead of the hub. For the approximation to the rotor hub and fuselage, velocities approaching 5 percent of free stream are predicted at the diagonal quadrants of the hub model, but they reduce quickly away from the hub to levels comparable with the fuselage-nacelle model. The computed values of the magnitudes of lateral velocity perturbation are less than the predicted values for either the normal component or tangential component. For the ellipsoid, only a small (half of a percent of free stream) velocity perturbation is predicted over either side of the front portion of the fuselage.

The effect of modeling the fuselage on the normal velocity perturbations can be seen in figure 10. For the fuselage and nacelle model, upflow occurs over the forward half of the measurement disk with the highest perturbation, about 4 percent of free stream, along the centerline about 1/3 radius ahead of the

hub. With the same model, a 3-percent downflow is found about 1/3 radius behind the hub. For the approximation to the rotor hub and fuselage, upflow perturbations approaching 15 percent of free stream are predicted ahead of the hub model and downflow of 13 percent behind the hub, but they reduce quickly away from the hub to levels comparable with the fuselage-nacelle model. For the ellipsoid, only a moderate (2 percent of free stream) perturbation is predicted over the fuselage nose, with the zero normal component line behind the hub at the location of maximum fuselage thickness.

The high normal velocity perturbation predicted close to the hub can be attributed to the panels placed vertically around the hub. There are no vertical faces on the experimental hub. In figure 6(a), the difference between the hub and fuselage prediction and the experimental value at $\psi = 180^{\circ}$ and $r/r_m = 0.20$ verifies that the hub model produces too much normal component in the close proximity of the hub. The normal-component prediction shows agreement at the next experimental station, $r/r_m = 0.50$. The model without the hub and with the model with the hub, respectively, predict approximately 3 percent and 15 percent of free-stream normal perturbation. The experimental value of normal perturbation at $r/r_m = 0.20$ is approximately 8 percent of the free stream, thus indicating that the model used for the hub induces twice the appropriate perturbation in its local vicinity.

Concluding Remarks

The velocity field of a representative helicopter fuselage in a free stream is computed. Perturbation velocities due to the fuselage are computed in a plane above the location of the helicopter rotor (rotor removed) corresponding to experimental rotor-inflow velocities measured. Velocity measurements made with a laser velocimeter over an isolated helicopter fuselage with hub are presented and compared with the velocities computed using three fuselage panel models. The models used in this study were a representative helicopter fuselage both with and without a hub model and a body-of-revolution fuselage.

The velocity perturbations computed using the source-panel method on the two helicopter fuselage shapes agree well with the measured velocity field except in the close vicinity of the rotor hub. In the hub region, modeling of the effective fuselage is difficult without knowing the extent of separation and the effective source shape of the rotating hub. The effects of the fuselage perturbations are not well-predicted with a body-of-revolution fuselage.

The effects of slight changes in fuselage attitude (needed for rotor trim) are shown to be insignificant in the fuselage induced velocity perturbations.

The normal velocity perturbations due to the fuselage at the plane of the inflow measurements have magnitudes of less than 8 percent of free-stream velocity. The tangential velocity perturbations due to the fuselage in the same plane have magnitudes of less than 6 percent of free-stream velocity. The lateral velocity perturbations due to the fuselage in

the same plane have an antisymmetric pattern with magnitudes less than either the normal or tangential components of velocity perturbation. Computed data are tabulated for conditions corresponding to reported experimental inflow data.

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Appendix A

Source-Panel Formulation

Symbols

The symbols used in this appendix are given as follows:

\boldsymbol{A}	area of a panel
d	length of panel edge
$e,h,\mathcal{P},\mathcal{Q}$	simplifying expressions (see subsequent text) $$
I	panel inertia (see subsequent text)
\boldsymbol{k}	subscript used as panel corner identifier
M	panel moment (see subsequent text)
m	panel edge slope
$ec{n}$	surface normal vector
P	point in space of potential evaluation
\boldsymbol{p}	point on body of potential evaluation
q	source location on body
r	distance from source to evaluation point
S	surface of body
$ec{V}$	velocity with components $V_x, V_y,$ and V_z
$ec{V}_{\infty}$	free-stream velocity vector
w	simplifying expression in mid-field calculations (see eq. (A13)), $1/r$
x, y, z	Cartesian coordinates
ξ,η	coordinates in plane of panel
σ	source strength
φ	velocity potential

Potential Formulation

This appendix describes the background and specific relations between distributed source panels and their velocity field. The basis for the source-panel method is the solution for the potential field by the method of Green's theorem. The specific solution for Laplace's equation is that of a potential source.

For irrotational incompressible flow, the governing equation, expressed in terms of velocity potential φ , is:

$$\nabla^2 \varphi = 0 \tag{A1}$$

where ∇ denotes the common del operator and the velocity potential φ is related to the velocity by

$$\vec{V} = -\vec{\nabla}\varphi \tag{A2}$$

The potential at any point P in space due to a closed surface S of potential source $\sigma(q)$, where q is a location on S, can be written as

$$\varphi(x, y, z) = \iint_{S} \frac{\sigma(q)}{r(P, q)} dS$$
 (A3)

as shown in reference 26. As the point of integration approaches the surface, the integrand becomes singular. At the surface point p, the singular value is determined to be

$$\frac{\partial \varphi}{\partial n} = -2\pi \ \sigma(p) + \iint_{S} \frac{\partial}{\partial n} \left[\frac{1}{r(p,q)} \right] \sigma(q) \ dS \quad (A4)$$

where $\partial/\partial n$ is the partial derivative normal to the surface. The resulting integral equation for the source values is

$$2\pi \ \sigma(p) - \iint_{S} \frac{\partial}{\partial n} \left[\frac{1}{r(p,q)} \right] \sigma(q) \ dS = -\vec{n}(p) \cdot \vec{V}_{\infty}$$
(A5)

The panel method of discretizing the surface reduces the surface integration to a small panel region that can be assumed to be planar, thus making direct integration possible. The method used here is that developed by Hess and Smith (refs. 26 and 27). A planar panel is projected from the four corners of the panel quadrilateral.

The panel geometry is defined by its four corner points, numbered clockwise as 1, 2, 3, 4. The coordinate system ξ, η will be used for locations on the panel and is mapped from the x, y space. The point at which the induced velocity is to be found is given by its coordinates in panel local notation x, y, z.

The potential at x, y, z is given by

$$\varphi = \iint_{A} \frac{1}{r} dA$$

$$= \iint_{A} \frac{d\xi \ d\eta}{\sqrt{(x-\xi)^2 + (y-\eta)^2 + z^2}}$$
 (A6)

Here, the value of r is the distance from P to the point on the panel with coordinates $(\xi, \eta, 0)$. The area of integration A is the surface of the panel. The components of induced velocity can now be computed:

$$V_{x} = -\frac{\partial \varphi}{\partial x}$$

$$= \iint_{A} \frac{x - \xi}{r^{3}} d\xi \ d\eta \tag{A7}$$

$$V_{y} = -\frac{\partial \varphi}{\partial y}$$

$$= \iint_{A} \frac{y - \eta}{r^{3}} d\xi \ d\eta \tag{A8}$$

$$V_z = -\frac{\partial \varphi}{\partial z}$$

$$= \iint\limits_A \frac{z}{r^3} d\xi \ d\eta \tag{A9}$$

The relationship between induced velocity and panel geometry is given by Hess and Smith and is in three forms which reduce the amount of computation needed based on the distance from the panel. In the "near-field," the form takes an exact representation of the velocity induced by a planar-distributed source panel. The near-field is defined as the region where the square of the distance from the panel centroid is less than six times the square of the larger panel diagonal. In the "mid-field," the form taken consists of the lower-order terms of an expansion of the exact solution about the panel centroid. The mid-field is defined as the region where the square of the distance from the panel centroid is between 6 and 16 times the square of the larger panel diagonal. In the "farfield," the form used is the velocity due to a point source at the panel centroid. The far-field is defined as the region where the square of the distance from the panel centroid exceeds 16 times the square of the larger panel diagonal.

Near-Field

The quadrilateral source panel is divided into two triangular regions of integration. After considerable manipulation, the resulting formulas for the three induced components of velocity at x, y, z are written as

$$V_{x} = \frac{\eta_{2} - \eta_{1}}{d_{12}} \log \left(\frac{r_{1} + r_{2} - d_{12}}{r_{1} + r_{2} + d_{12}} \right)$$

$$+ \frac{\eta_{3} - \eta_{2}}{d_{23}} \log \left(\frac{r_{2} + r_{3} - d_{23}}{r_{2} + r_{3} + d_{23}} \right)$$

$$+ \frac{\eta_{4} - \eta_{3}}{d_{34}} \log \left(\frac{r_{3} + r_{4} - d_{34}}{r_{3} + r_{4} + d_{34}} \right)$$

$$+ \frac{\eta_{1} - \eta_{4}}{d_{41}} \log \left(\frac{r_{4} + r_{1} - d_{41}}{r_{4} + r_{1} + d_{41}} \right) \qquad (A10)$$

$$V_{y} = \frac{\xi_{1} - \xi_{2}}{d_{12}} \log \left(\frac{r_{1} + r_{2} - d_{12}}{r_{1} + r_{2} + d_{12}} \right)$$

$$+ \frac{\xi_{2} - \xi_{3}}{d_{23}} \log \left(\frac{r_{2} + r_{3} - d_{23}}{r_{2} + r_{3} + d_{23}} \right)$$

$$+ \frac{\xi_{3} - \xi_{4}}{d_{34}} \log \left(\frac{r_{3} + r_{4} - d_{34}}{r_{3} + r_{4} + d_{34}} \right)$$

$$+ \frac{\xi_{4} - \xi_{1}}{d_{41}} \log \left(\frac{r_{4} + r_{1} - d_{41}}{r_{4} + r_{1} + d_{41}} \right) \qquad (A11)$$

$$V_{z} = \tan^{-1} \left(\frac{m_{12}e_{1} - h_{1}}{zr_{1}} \right) - \tan^{-1} \left(\frac{m_{12}e_{2} - h_{2}}{zr_{2}} \right)$$

$$+ \tan^{-1} \left(\frac{m_{23}e_{2} - h_{2}}{zr_{2}} \right) - \tan^{-1} \left(\frac{m_{34}e_{3} - h_{3}}{zr_{3}} \right)$$

$$+ \tan^{-1} \left(\frac{m_{34}e_{3} - h_{3}}{zr_{3}} \right) - \tan^{-1} \left(\frac{m_{41}e_{4} - h_{4}}{zr_{4}} \right)$$

$$+ \tan^{-1} \left(\frac{m_{41}e_{4} - h_{4}}{zr_{4}} \right) - \tan^{-1} \left(\frac{m_{41}e_{1} - h_{1}}{zr_{1}} \right)$$

$$(A12)$$

where the panel edge lengths are given by

$$d_{12} = \sqrt{(\xi_2 - \xi_1)^2 + (\eta_2 - \eta_1)^2}$$

$$d_{23} = \sqrt{(\xi_3 - \xi_2)^2 + (\eta_3 - \eta_2)^2}$$

$$d_{34} = \sqrt{(\xi_4 - \xi_3)^2 + (\eta_4 - \eta_3)^2}$$

$$d_{41} = \sqrt{(\xi_1 - \xi_4)^2 + (\eta_1 - \eta_4)^2}$$

the edge slopes are given by

$$m_{12} = \frac{\eta_2 - \eta_1}{\xi_2 - \xi_1} \qquad m_{23} = \frac{\eta_3 - \eta_2}{\xi_3 - \xi_2}$$

$$m_{34} = \frac{\eta_4 - \eta_3}{\xi_4 - \xi_3} \qquad m_{41} = \frac{\eta_1 - \eta_4}{\xi_1 - \xi_4}$$

and the simplifying terms relative to the four corners (with k = 1, 2, 3, 4) are given as

$$r_k = \sqrt{(x - \xi_k)^2 + (y - \eta_k)^2 + z^2}$$

$$e_k = z^2 + (x - \xi_k)^2$$

$$h_k = (y - \eta_k)(x - \xi_k)$$

Mid-Field

The cost of computing the exact contribution of the distributed source can be reduced by simplifying the equation outside the field where exact solution is important. The near-field solution can be simplified by using a multipole expansion for the integrand of equation (A6). By expanding at the panel centroid, i.e., $\xi = \eta = 0$, the geometry of the panel is eliminated from the calculation. The integrand being expanded is

$$w = \frac{1}{r} = \frac{1}{\sqrt{x^2 + y^2 + z^2}}$$
 (A13)

This expansion, to terms of second order, is given as

$$\varphi = Aw - (M_x w_x + M_y w_y) + \frac{1}{2} (I_{xx} w_{xx} + 2I_{xy} w_{xy} + I_{yy} w_{yy}) + \cdots$$
 (A14)

where

$$A = \iint\limits_A d\xi \ d\eta$$
 $M_x = \iint\limits_A \xi \ d\xi \ d\eta$ $M_y = \iint\limits_A \eta \ d\xi \ d\eta$ $I_{xx} = \iint\limits_A \xi^2 \ d\xi \ d\eta$ $I_{xy} = \iint\limits_A \xi \eta \ d\xi \ d\eta$ $I_{yy} = \iint\limits_A \eta^2 \ d\xi \ d\eta$

Using this expansion and forming the velocities from the directional derivatives of the potential, the velocities can be computed from

$$V_x = -\frac{\partial \varphi}{\partial x}$$

$$= -\left(Aw_x + \frac{1}{2}I_{xx}w_{xxx} + I_{xy}w_{xxy} + \frac{1}{2}I_{yy}w_{xyy}\right)$$
(A15)

$$V_{y} = -\frac{\partial \varphi}{\partial y}$$

$$= -\left(Aw_{y} + \frac{1}{2}I_{xx}w_{xxy} + I_{xy}w_{xyy} + \frac{1}{2}I_{yy}w_{yyy}\right)$$

$$(A16)$$

$$V_{z} = -\frac{\partial \varphi}{\partial z}$$

$$= -\left[Aw_{z} + \frac{1}{2}I_{xx}w_{xxz} + I_{xy}w_{xyz} + \frac{1}{2}I_{yy}w_{yyz}\right]$$

$$(A17)$$

where the quantities A, I_{xx} , I_{xy} , and I_{yy} are given by the geometry and defined above. The derivatives of w are found to be

$$w_x = -x/r^3$$

$$w_y = -y/r^3$$

$$w_z = -z/r^3$$

$$w_{xxx} = 3x(3\mathcal{P} + 10x^2)/r^7$$

$$w_{xxy} = 3y\mathcal{P}/r^7$$

$$w_{xyy} = 3x\mathcal{Q}/r^7$$

$$w_{yyy} = 3y(3\mathcal{Q} + 10y^2)/r^7$$

$$w_{xxz} = 3z\mathcal{P}/r^7$$

$$w_{xyz} = -15xyz/r^7$$

$$w_{yyz} = 3z\mathcal{Q}/r^7$$

where

$$\mathcal{P} = y^2 + z^2 - 4x^2$$

$$\mathcal{Q} = x^2 + z^2 - 4y^2$$

Far-Field

In the far-field, the distribution of the source is of no significance; only the lumped effect, i.e., point source, is necessary. The point-source model for the effect of panel with unit source strength in the farfield can be expressed as

$$V_x = A(x - x_0)/r^3 (A18)$$

$$V_y = A(y - y_0)/r^3 (A19)$$

$$V_z = A(z - z_0)/r^3$$
 (A20)

Here, the subscript 0 indicates the panel centroid.

Appendix B

Fuselage Geometry Description

The fuselage described for the experimental program is referred to as the ROBIN fuselage, derived from an earlier rotor body interaction program. The purpose in creating this fuselage shape was to have an analytically derived shape that could be recreated mathematically with little effort.

Symbols

The symbols used in this appendix are given as follows:

scale factor in x
scale factor in y
dimensional constant
equation coefficient array
fuselage height
power constant in y
cross-section (elliptic) power constant
power constant in x
reference radius
radius in yz -plane
fuselage width
Cartesian coordinates
initial offset in x
initial offset in y
offset in z (camber line)
angle in yz -plane

General Equation

The fuselage shape is derived from the superellipse equation of the form

$$\left(\frac{x+x_0}{A}\right)^n + \left(\frac{y+y_0}{B}\right)^m = C$$
 (B1)

where n and m are not of necessity equal to 2, an integer, or to each other. Also, A, B, C, x_0 , and y_0 are constants. The fuselage is parameterized by the longitudinal station coordinate x where the cross-section y- and z-coordinates are defined by functions

of height H, width W, camber line Z_0 , and elliptic power N. These defining values are found by solving the superellipse equation for y in terms of x:

$$y = F(x) = B \left[C - \left(\frac{x + x_0}{A} \right)^n \right]^{1/m} - y_0$$
 (B2)

To compute fuselage geometry, an array of geometry coefficients is used for each of the separate fuselage elements. This array, C_1 to C_8 , is related to the defining equation parameters by

$$C_1 = C$$
 $C_2 = *$ $C_3 = x_0$ $C_4 = A$
 $C_5 = n$ $C_6 = -y_0$ $C_7 = B$ $C_8 = m$

Note that the constant C_2 is arbitrary (*).

The cross-section parameters H, W, Z_0 , and N are all treated as functions F(x) with an independent set of C_1 to C_8 coefficients. The actual cross-section coordinates (y,z) are defined in polar coordinates (r,ϕ) from the superellipse equation with

$$y + y_0 = r\cos\phi \tag{B3}$$

$$x + x_0 = r\sin\phi \tag{B4}$$

and with C = 1 and n = m = N. Solving for r, this relation becomes

$$r = \left[\frac{(AB)^N}{(A\sin\phi)^N + (B\cos\phi)^N}\right]^{1/N}$$
 (B5)

The coordinates of the fuselage can now be derived in terms of longitudinal station x and cylindrical coordinate ϕ .

The ROBIN fuselage is made of four body and two nacelle elements with the coefficients given in table B1. A listing for a FORTRAN program that generates the ROBIN fuselage is also given in table B1. The output of this program must be edited to match the nacelle edge to the fuselage seam so that aligning control points will be coincident between the nacelle and fuselage. A table of the fuselage-nacelle control points used in this study is given in table B2.

For the portion of the study involving the effects of a hub model, a simplified hub geometry was patched into the paneled ROBIN geometry described above. The fuselage-nacelle-hub control points used are given in table B3.

Table B1. Coefficients for Fuselage Generation and Computer Listing

Function	x/R	C_1	C_2	C_3	C_4	C_5	C_6	C ₇	C_8
•				Main fuselage p	parameters				
Н	0 → 0.4	1.000	-1.000	-0.400	0.400	1.800	0	0.250	1.800
W	1	1.000	-1.000	400	.400	2.000	0	.250	2.000
z_0	Ì	1.000	-1.000	400	.400	1.800	080	.080	1.800
N	1	2.000	3.000	0	.400	1.000	0	1.000	1.000
Н	0.4 → 0.8	0.250	0	0	0	0	0	0	0
W		.250	0	0	0	0	0	0	0
z_0		0	0	0	0	0	0	0	0
N	\downarrow	5.000	0	0	0	0	0	0	0
Н	$0.8 \rightarrow 1.9$	1.000	-1.000	-0.800	1.100	1.500	0.050	0.200	0.600
W		1.000	-1.000	800	1.100	1.500	.050	.200	.600
z_0		1.000	-1.000	800	1.100	1.500	.040	040	.600
N	\downarrow	5.000	-3.000	800	1.100	1.000	0	0	0
Н	1.9 → 2.0	1.000	-1.000	-1.900	0.100	2.000	0	0.050	2.000
W		1.000	-1.000	-1.900	.100	2.000	0	.050	2.000
Z_0		.040	0	0	0	0	0	0	0
N	\downarrow	2.000	0	0	0	0	0	0	0
-				Pylon para	meters		-		
H	$0.4 \to 0.8$	1.000	-1.000	-0.800	0.400	3.000	0	0.200	3.000
W		1.000	-1.000	800	.400	3.000	0	.172	3.000
z_0		.125	0	0	0	0	0	0	0
N	1	5.000	0	0	0	0	0	0	0
Н	$0.8 \to 1.018$	1.000	-1.000	-0.800	0.218	2.000	0	0.200	2.000
W		1.000	-1.000	800	.218	2.000	0	.172	2.000
Z_0		1.000	-1.000	800	1.100	1.500	.065	.060	.600
N	\downarrow	5.000	0	0	0	0	0	0	0

```
ROBIN
      program ROBIN
       correction from the coefficients in TM 80051 (JDB-88)
C
      real xor(50), ch(6,8), cw(6,8), cz0(6,8), cn(6,8)
      character*8 labxor(6)
       data labxor/'0.0->0.4','0.4->0.8','0.8->1.9'.
                      '1.9->2.0','0.4->0.8','-> 1.018'/
       data xor/0.00, 0.04, 0.08, 0.12, 0.16, 0.24, 0.28, 0.32,
                 0.40, 0.45, 0.56, 0.80, 0.96, 1.018, 1.28, 1.48,
     +
                  1.72, 1.90, 1.96, 2.00,30*0.0/
                                                                                                                   10
      data ch/ 1.0, .25, 1.0, 1.0, 1.0, 1.0,
                 -1.0, 0.0, -1.0, -1.0, -1.0, -1.0,
                 -0.4, 0.0, -0.8, -1.9, -0.8, -0.8,
                 0.4, 0.0, 1.1, 0.1, 0.4, 218,
                 1.8, 0.0, 1.5, 2.0, 3.0, 2.0,
                 0.0, 0.0, .05, 0.0, 0.0, 0.0,
                 0.25, 0.0, 0.2, .05, 0.2, 0.2,
                 1.8, 0.0, 0.6, 2.0, 3.0, 2.0/
      data cw/ 1.0, .25, 1.0, 1.0, 1.0, 1.0,
     +
                 -1.0, 0.0, -1.0, -1.0, -1.0, -1.0,
                                                                                                                   20
                -0.4, 0.0, -0.8, -1.9, -0.8, -0.8,
                 0.4, 0.0, 1.1, 0.1, 0.4, 218,
                 2.0, 0.0, 1.5, 2.0, 3.0, 2.0,
                 0.0, 0.0,0.05, 0.0, 0.0, 0.0,
                 .25, 0.0, 0.2, .05, .172, .172,
                 2.0, 0.0, 0.6, 2.0, 3.0, 2.0/
      data cz0/1.0, 0.0, 1.0, .04,.125, 1.0,
                -1.0, 0.0, -1.0, 0.0, 0.0, -1.0,
                -0.4, 0.0, -0.8, 0.0, 0.0, -0.8,
                 0.4, 0.0, 1.1, 0.0, 0.0, 1.1,
                                                                                                                   30
                 1.8, 0.0, 1.5, 0.0, 0.0, 1.5,
                -.08, 0.0, .04, 0.0, 0.0, .065,
                 .08, 0.0, -.04, 0.0, 0.0, .06,
                 1.8, 0.0, 0.6, 0.0, 0.0, 0.6/
      data cn/ 2.0, 5.0, 5.0, 2.0, 5.0, 5.0,
                 3.0, 0.0, -3.0, 0.0, 0.0, 0.0
                 0.0, 0.0, -0.8, 0.0, 0.0, 0.0,
                 0.4, 0.0, 1.1, 0.0, 0.0, 0.0,
                 1.0, 0.0, 1.0, 0.0, 0.0, 0.0,
                 0.0, 0.0, 0.0, 0.0, 0.0, 0.0,
                                                                                                                   40
                 1.0, 0.0, 0.0, 0.0, 0.0, 0.0,
                 1.0, 0.0, 0.0, 0.0, 0.0, 0.0
 -- print the coefficient table (per tm80051)
     open(100,file='robin.tab',status='unknown')
      write(100,'(///,30x,''fuselage parameters'',//)')
      write(100,1005)
      write(100,'(5x,
             ''function x/r
                                                                       c5'',
                                      c1
                                              c2
                                                       c3
                                                               c4
             , ,
                                      c8'')'}
                     c6
                             с7
                                                                                                                   50
     write(100,1005)
     do j = 1.4
        write(100,1001)labxor(j),(ch(j,i),i=1,8)
        write(100,1002)(cw(j,i),i=1,8)
```

```
write(100,1003)(cz0(j,i),i=1,8)
         write(100,1004)(cn(j,i),i=1,8)
       end do
       write(100,'(///,32x,''pylon parameters'',/)')
       write(100,1005)
       do j=5.6
                                                                                                                 60
         write(100,1001)labxor(j),(ch(j,i),i=1,8)
         write(100,1002)(cw(j,i),i=1,8)
         write(100,1003)(cz0(j,i),i=1,8)
         write(100,1004)(cn(j,i),i=1,8)
       end do
       close(100)
 1001 format(8x,'h',2x,a8,1x,8f7.3)
 1002 format(8x,'w',11x,8f7.3)
 1003 format(8x,'z0',10x,8f7.3)
 1004 format(8x,'n',11x,8f7.3/)
                                                                                                                70
 1005 format(5x,71('-'))
\mathbf{c}
       call interact(ch,cw,cz0,cn)
       if (1.eq.1) stop 'temporary stop'
c
      twopi = 8*atan(1.0)
               6.28318
      open(101,file='robin.tmp',status='unknown')
      do i=2,20
           if (xor(i) .lt. 0.4) ix = 1
           if (xor(i) .ge. 0.4 .and. xor(i) .lt. 0.8) ix = 2
                                                                                                                80
           if (xor(i) .ge. 0.8 .and. xor(i) .lt. 1.9) ix = 3
           if (xor(i) .ge. 1.9) ix = 4
           xn = geom(cn, ix, xor(i))
           xz0=geom(cz0,ix,xor(i))
           xw = geom(cw, ix, xor(i))
           xh=geom(ch,ix,xor(i))
  -- first strip of zeros
           if (i.eq.2) then
               do j=1,17
                                                                                                                90
                    \mathbf{k} = \mathbf{0}
                    if (j \cdot eq. 1) k = 2
                    write(101,100)xor(1),0.,geom(cz0,1,xor(1)),k,0
               end do
           end if
           do j=1,17
               th = twopi*(j-1)/16.
               k = 0
               if (j .eq. 1) k = 1
               sth = sin(th)
                                                                                                               100
               cth = cos(th)
               denom = (abs(xh*sth)**xn + abs(xw*cth)**xn)**(1./xn)
               rval = .5*xh*xw/denom
               xval = xor(i)
               yval = rval*sth
               zval = xz0 + rval*cth
```

```
write(101,100)xval,yval,zval,k,0
                                                                                                                110
            end do
           if (i.eq.20) then
                do j = 1.17
                    k = 0
                    if (j .eq. 1) k = 1
                     write(101,100)xor(20),0.,geom(cz0,4,xor(20)),k,0
                end do
           end if
       end do
                                                                                                                120
c -- now for the 'dog-house'
       do i=1,6
           indx = i+8
           ix=5
           if (i.gt.4) ix=6
           xn = geom(cn,ix,xor(indx))
           xz0=geom(cz0,ix,xor(indx))
           xw = geom(cw,ix,xor(indx))
           xh = geom(ch,ix,xor(indx))
c
                                                                                                                130
c -- first strip of zeros
           if (i.eq.1) then
                do j = 1,9
                    \mathbf{k} = \mathbf{0}
                    if (j .eq. 1) k = 2
                    write(101,100)xor(indx),0.,geom(cz0,ix,xor(indx)),k,0
                end do
           else if (i .eq. 6) then
                do j=1,9
                    k = 0
                                                                                                                140
                    if (j \cdot eq. 1) k = 1
                    write(101,100)xor(indx),0.,geom(cz0,ix,xor(indx)),k,0
                end do
           else
                do j=1,9
                    th = .5*twopi*(9-j)/8.
                    \mathbf{k} = 0
                    if (j .eq. 1) k = 1
                    sth = sin(th)
                    cth = cos(th)
                                                                                                                150
C
                    denom = (abs(xh*sth)**xn + abs(xw*cth)**xn)**(1./xn)
                    rval = .5*xh*xw/denom
c
                    xval = xor(indx)
                    yval = rval*cth
                    zval = xz0 + rval*stli
c
                    write(101,100)xval,yval,zval,k,0
                end do
                                                                                                                160
           end if
      end do
```

```
c
      close(101)
      stop 'done'
      format(3f10.3,2i1)
100
      end
c
                                                                                                     VALU
      real function VALU(coef,ix,xval)
      real coef(6,8)
      valu= coef(ix,6)
      if (coef(ix,8) .ne. 0.) then
           x1=(xval-coef(ix,3))/coef(ix,4)
           x2 = coef(ix,1) - coef(ix,2) * x1 * * coef(ix,5)
           valu = valu + coef(ix,7)*x2**(1./coef(ix,8))
      end if
      return
      end
                                                                                                    GEOM
      real function GEOM(coef,ix,xval)
      real coef(6,8)
                                                                                                           181
      if (coef(ix,4) .eq. 0.) then
           geom = coef(ix,1)
      else
           x1 = coef(ix,1) + coef(ix,2)*(abs((xval+coef(ix,3))
                 /coef(ix,4))**coef(ix,5)
          if (coef(ix,8) .eq. 0. .or. coef(ix,8) .eq. 1.0) return
           geom = coef(ix,7)*(abs(x1))**(1.0/coef(ix,8))+coef(ix,6)
      end if
                                                                                                           190
      return
      end
c
                                                                                             INTERACT
      subroutine INTERACT(co1,co2,co3,co4)
      real co1(6,8), co2(6,8), co3(6,8), co4(6,8)
      write(6,*) ' interactive mode: '
  10 write(6,*), enter segment (1-6) and x station:
      read(5,*,end=99)iseg,x
                                                                                                           200
c
      write(6,*) 'dimensions are:'
      write(6,*) '
                         height: ',geom(co1,iseg,x)
      write(6,*) '
                          width: ',geom(co2,iseg,x)
      write(6,*) '
                       z offset: ',geom(co3,iseg,x)
      write(6,*) '
                          power: ',geom(co4,iseg,x)
      go to 10
      continue
      return
                                                                                                           210
      end
```

Table B2. ROBIN Fuselage-Nacelle Geometry

(a) Element 1

\blacksquare	_																	<u> </u>																
2	0.075	.073	.058	.021	020	090'-	098	113	114	113	098	090'-	020	.021	.058	.073	.075	0.102	101.	.085	.038	009	056	103	119	120	119	103	056	009	.038	.085	.101	.102
y	0	038	078	860	100	860	078	038	0	.038	820.	860:	.100	860:	.078	.038	0	0	046	094	113	115	113	094	046	0	.046	.094	.113	.115	.113	.094	.046	0
\boldsymbol{x}	0.160																→	0.240																\rightarrow
Strip	4												-					5	-															
Ŋ	0.031	.029	.018	007	037	990'-	091	102	104	102	091	990	037	007	.018	.029	.031	0.055	.054	.040	600.	027	063	095	108	110	108	095	063	027	600	.040	.054	.055
y	0	027	054	071	075	071	054	027	0	.027	.054	.071	.075	170.	.054	.027	0	0	033	067	086	089	086	067	033	0	.033	290.	980.	680.	980.	.067	.033	0
x	0.080																→	0.120																→
Strip	2													•				3																
2	-0.080																→	-0.003	005	013	029	050	071	087	095	097	095	087	071	050	029	013	005	003
y	0							_							-		- →	0	019	037	051	054	051	037	019	0	.019	.037	.051	.054	.051	.037	.019	0
x	0								-								→	0.040														-		→
Strip	0																	-																

2	0.112	.111	.094	.044	005	054	105	121	122	121	105	054	005	.044	.094	.111	.112	0.119	.118	.102	.048	002	053	107	123	124	123	107	053	002	.048	.102	.118	.119
y	0	048	100	118	119	118	100	048	0	.048	.100	.118	.119	.118	.100	.048	0	0	050	104	122	122	122	104	050	0	.050	.104	.122	.122	.122	.104	.050	0
\boldsymbol{x}	0.280																→	0.320												•				\rightarrow
Strip	9																	2																
22	0.075	.073	.058	.021	020	090'-	860'-	113	114	113	860	090'-	020	.021	.058	.073	.075	0.102	101.	.085	.038	009	056	103	119	120	119	103	056	009	.038	.085	.101	.102
y	0	038	078	098	100	098	820	038	0	.038	.078	860:	.100	860.	.078	.038	0	0	046	094	113	115	113	094	046	0	.046	.094	.113	.115	.113	.094	.046	0
\boldsymbol{x}	0.160																\rightarrow	0.240																\rightarrow
Strip	4																	5																
z	0.031	.029	.018	007	037	990	091	102	104	102	091	990	037	007	.018	.029	.031	0.055	.054	.040	600.	027	063	095	108	110	108	095	063	027	600:	.040	.054	.055
y	0	027	054	071	075	071	054	027	0	.027	.054	120.	.075	.071	.054	.027	0	0	033	067	980	089	980'-	067	033	0	.033	290.	980:	680.	980.	.067	.033	0
\boldsymbol{x}	0.080																\rightarrow	0.120																\rightarrow
Strip	2																	3																
z	-0.080						<u>-</u>										→	-0.003	005	013	029	050	071	087	095	097	095	087	071	050	029	013	005	003
y	0																→	0	019	037	051	054	051	037	019	0	.019	.037	.051	.054	.051	.037	.019	0

(a) Continued

z	0.099	860.	.085	.051	.017	016	050	064	064	064	050	016	.017	.051	.085	860.	660.	0.085	.084	.073	.050	.027	.003	020	030	031	030	020	.003	.027	.050	.073	.084	.085
y	0	034	068	081	082	081	068	034	0	.034	890:	.081	.082	.081	890	.034	0	0	024	047	057	058	057	047	024	0	.024	.047	.057	.058	.057	.047	.024	0
x	1.280																→	1.480																→
Strip	14																-	15			-					<u>-</u>					-		-	
*	0.120	.111	.103	.051	.004	044	960'-	112	112	112	960	044	.004	.051	.103	.111	.120	0.116	.116	.100	.051	900:	040	089	105	105	105	089	040	900.	.051	.100	.116	.116
y	-0.068	084	100	115	116	115	100	048	0	.048	.100	.115	.116	.115	.100	.084	890.	0	046	095	110	111	110	095	046	0	.046	.095	.110	.111	.110	.095	.046	0
x	096.0	_															→	1.018						_										→
Strip	12															_		13																
×	0.119	.109	760.	.052	0	052	109	125	125	125	109	052	0	.052	260.	.109	.119	0.115	.109	760.	.052	0	052	109	125	125	125	109	052	0	.052	760.	.109	.115
y	-0.092	109	117	125	125	125	109	052	0	.052	.109	.125	.125	.125	.117	.109	.092	-0.100	109	117	125	125	125	109	052	0	.052	.109	.125	.125	.125	.117	.109	.100
x	0.560	-									-							0.800											-				-	• →
Strip	12	ì																11																
×	0.125	.125	.109	.052	0	052	109	125	125	125	109	052	0	.052	.109	.125	.125	0.124	.120	.109	.052	0	052	109	125	125	125	109	052	0	.052	.109	.120	.124
'n	C	052	109	125	125	125	109	052	0	.052	.109	.125	.125	.125	.109	.052	0	-0.069	089	109	125	125	125	109	052	0	.052	.109	.125	.125	.125	.109	680	690.
H	0.400	-															- →	0.450																\rightarrow
Strip	α	·																6																

Table B2. Concluded

(b) Element 2

(a) Concluded

N	0.115	.166	.205	.211	.211	.211	.205	.166	.115	0.124	.148	.174	.178	.178	.178	.174	.148	.124	0.116					-		_	→
'n	0.100	660.	080	.036	0	036	080	099	100	0.068	890.	.054	.024	0	024	054	890	068	0								→
\boldsymbol{x}	0.800								→	096.0					-,			→	1.018								→
Strip	3									4	-								2								-
Z	0.125								→	0.124	.153	.180	.184	.184	.184	.180	.153	.124	0.119	.163	.198	.204	.204	.204	.198	.163	.119
y.	0	_							→	0.069	690:	.055	.025	0	025	055	690	690'-	0.092	.092	.073	.033	0	033	073	092	092
я	0.400								→	0.450					<u>-</u>			→	0.560								→
Strip	0									1									2								
																		T									

×	090.0	.058	.054	.048	.040	.032	.026	.022	.020	.022	.026	.032	.040	.048	.054	.058	090.	0.040																→
y	0	008	014	018	020	018	014	008	0	800.	.014	.018	.020	.018	.014	800.	0	0							·									\rightarrow
x	1.960																→	2.000														-		→
Strip	18																	19																
N	0.070	690.	.062	.050	.036	.023	.011	.004	.002	.004	.011	.023	.036	.050	.062	690.	.070	0.065	.063	.058	.050	.040	.030	.022	.017	.015	.017	.022	.030	.040	.050	.058	.063	.065
y	0	013	026	033	034	033	026	013	0	.013	.026	.033	.034	.033	.026	.013	0	0	010	018	023	025	023	018	010	0	.010	.018	.023	.025	.023	.018	.010	0
x	1.720															_	-	1.900																→
Strip	16																	17																

Table B3. ROBIN Fuselage-Nacelle-Hub Geometry

(a) Element 1

2	0.112	.111	.094	.044	005	054	105	121	122	121	105	054	005	.044	.094	.111	.112	0.119	.118	.102	.048	002	053	107	123	124	123	107	053	002	.048	.102	.118	.119
y	0	048	100	118	119	118	100	048	0	.048	.100	.118	911.	.118	.100	.048	0	0	050	104	122	122	122	104	050	0	.050	.104	.122	.122	.122	.104	.050	0
x	0.280																→	0.320																\rightarrow
Strip	9																	2											-					
N	0.075	.073	.058	.021	020	090	860	113	114	113	098	060	020	.021	.058	.073	.075	0.102	.101	.085	.038	009	056	103	119	120	119	103	056	009	.038	.085	.101	.102
y	0	038	078	098	100	098	078	038	0	.038	820.	860.	.100	860.	.078	.038	0	0	046	094	113	115	113	094	046	0	.046	.094	.113	.115	.113	.094	.046	0
x	0.160					·											\rightarrow	0.240																\rightarrow
Strip	4																	2															_	
2	0.031	.029	.018	007	037	990	091	102	104	102	091	990	037	007	.018	.029	.031	0.055	.054	.040	600.	027	063	095	108	110	108	095	063	027	600.	.040	.054	.055
y	0	027	054	071	075	071	054	027	0	.027	.054	.071	.075	120.	.054	.027	0	0	033	067	980	089	980'-	790'-	033	0	.033	290.	980.	.089	980.	290.	.033	0
x	0.080																→	0.120																→
Strip	2																	3																
2	-0.080																→	-0.003	005	013	029	050	071		095	097	095	087	071	050	029	013	005	003
y	0																→	0	019	037	051	054	051	037	019	0	.019	.037	.051	.054	.051	.037	.019	0
x	0																\rightarrow	0.040																→
Strip	0																	-																

Table B3. Continued

(a) Continued

y	-0.068	084	100	115	116	115	100	048	0	.048	.100	.115	.116	.115	.100	.084	890:	0	046	095	110	111	110	095	046	0	.046	.095	.110	.111	.110	.095	.046	0
x	0.960																→	1.018							-									\rightarrow
Strip	14																	15																
×	0.115	.109	.097	.052	0	052	109	125	125	125	109	052	0	.052	760.	.109	.115	0.115	.109	760.	.052	0	052	109	125	125	125	109	052	0	.052	260.	.109	.115
'n	-0.100	109	117	125	125	125	109	052	0	.052	.109	.125	.125	.125	.117	.109	.100	-0.100	109	117	125	125	125	109	052	0	.052	.109	.125	.125	.125	.117	.109	.100
a	0.739																→	0.800																→
Strip	12																	13																
															•											_								
*	0.119	.109	760.	.052	0	052	109	125	125	125	109	052	0	.052	760.	.109	.119	0.116	.109	760.	.052	0	052	109	125	125	125	109	052	0	.052	.097	.109	.116
y	-0.092	109	117	125	125	125	109	052	0	.052	.109	.125	.125	.125	.117	.109	.092	-0.098	109	117	125	125	125	109	052	0	.052	.109	.125	.125	.125	.117	.109	860.
x	0.560																→	0.639																\rightarrow
Strip	10																	11																
2	0.125	.125	.109	.052	0	052	109	125	125	125	109	052	0	.052	.109	.125	.125	0.124	.120	.109	.052	0	052	109	125	125	125	109	052	0	.052	.109	.120	.124
'n	0	052	109	125	125	125	109	052	0	.052	.109	.125	.125	.125	.109	.052	0	-0.069	089	109	125	125	125	109	052	0	.052	.109	.125	.125	.125	.109	.089	690.
x	0.400																→	0.450																→
Strip	∞																	6																

0.120

(a) Concluded

Strip	20																																	
																										_								
22	0.070	690.	.062	.050	.036	.023	.011	.004	.002	.004	.011	.023	.036	.050	.062	690:	.070	0.065	.063	.058	.050	.040	.030	.022	.017	.015	.017	.022	.030	.040	.050	.058	.063	.065
y	0	013	026	033	034	033	026	013	0	.013	.026	.033	.034	.033	.026	.013	0	0	010	018	023	025	023	018	010	0	.010	.018	.023	.025	.023	.018	.010	0
æ	1.720																\rightarrow	1.900																\rightarrow
Strip	18																	19				-												
2	0.099	860.	.085	.051	.017	016	050	064	064	064	050	016	.017	.051	.085	860.	.099	0.085	.084	.073	.050	.027	.003	020	030	031	030	020	.003	.027	.050	.073	.084	.085
y	0	034	068	081	082	081	068	034	0	.034	890:	.081	.082	.081	890:	.034	0	0	024	047	057	058	057	047	024	0	.024	.047	.057	.058	.057	.047	.024	0
x	1.280																\rightarrow	1.480																→
Strip	16																	17																

2	0.040									-							→
y	0	_														_	→
x	2.000																→
Strip	21																
22	090.0	.058	.054	.048	.040	.032	920.	.022	.020	.022	.026	.032	.040	.048	.054	.058	090
ĥ	0	008	014	018	020	018	014	008	0	800.	.014	.018	.020	.018	.014	800.	0
\boldsymbol{x}	1.960					-											→
Strip	07																

Table B3. Continued

(c) Element 3

(b) Element 2

0.210 .210 .205 .166 .115 .0.211 .201 .205 .166 .178 .178 .178 .178 .178 .178 -.036 -.080 -.099 -.100 0 --.036 --.080 --.099 0 -.024 -.054 -.068 -.068 1.0180.739 0.960 0.800 \boldsymbol{x} Strip 9 2 œ 0.184 1.184 1.184 1.153 1.153 1.154 1.024 1.198 1. 0.12513 -.033 -.073 -.092 -.092 0 -.025 -.055 -.069 -.035 -.078 -.097 -.098 -0.050 -.065 -.079 -.099 -.099 0.450 $\frac{x}{0.400}$ 0.560 0.639 0.689 Strip 0 7 က 4 0.115 .166 .205 .211 .211 .211 .148 .174 .178 .178 0.115 .166 .205 .210 .210 0.100 .099 .080 .036 .036 .068 .068 .054 y 00.100 .099 .080 1.018 $\frac{x}{0.739}$ 0.960 0.800 Strip 5 œ 9 0.124 .153 .180 .184 .184 0.119 .163 .198 .204 .204 .204 .203 .203 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .208 .209 $\frac{z}{0.125}$ 0.098 .097 .078 .035 0.099 .099 .079 .065 0.069 .069 .055 .025 .025 .092 .092 .073 0.689 0.639 $\frac{x}{0.400}$ 0.4500.560Strip 0 က 4 ~

Table B3. Concluded

(d) Element 4

2 0.356

\boldsymbol{x}	0.683							-								•																		
Strip	9																																	
N	0.275	.276	.277	.278	.280	.282	.283	.284	.285	.284	.283	.282	.280	278	277	276	275	0.325	326	327	328	330	.332	333	334	.335	334	333	333	330	300	327	326	325
h	0	051	094	123	133	123	094	051	0	.051	.094	.123	.133	.123	.094	150	0	6	- 051	- 094	123	133	123	094	051	0	.051	100.	123	133	123	760	.051	0
\boldsymbol{x}	0.553	.563	.592	.635	989.	.737	.780	808	.819	808	.780	.737	989.	.635	.592	.563	.553	0.551	.561	.590	.633	.684	.735	.778	807	.817	807	778	735	284	633	290	.561	.551
Strip	4																	5)															
z	0.232	.232	.232	.233	.233	.233	.234	.234	.234	.234	.234	.233	.233	.233	.232	.232	.232	0.265	.265	.265	.266	.266	.266	.267	.267	.267	.267	.267	.266	.266	.266	.265	.265	.265
y	0	010	018	023	025	023	018	010	0	.010	.018	.023	.025	.023	.018	.010	0	0	010	018	023	025	023	018	010	0	.010	.018	.023	.025	.023	.018	.010	0
x	0.663	.664	029.	.678	889.	269.	.705	.711	.713	.711	.705	.697	.688	.678	029.	.664	.663	0.661	.663	699.	229	989.	969.	.704	.710	.711	.710	.704	969.	989.	.677	699:	.663	.661
Strip	2																	က																
z	0.208	.208	.209	.209	.210	.210	.210	.210	.210	.210	.210	.210	.210	.209	.209	.208	.208	.214	.214	.214	.215	.215	.215	.216	.216	.216	.216	.216	.215	.215	.215	.214	.214	.214
y	0	013	025	038	050	038	025	013	0	.013	.025	.038	.050	.038	.025	.013	0	0	010	018	023	025	023	018	010	0	.010	810.	.023	.025	.023	.018	.010	0
x	0.639	.651	.664	.677	689	.701	.714	.726	.739	.726	.714	.701	689	.677	.664	.651	.639	0.663	.665	129.	629.	.688	869.	.706	.711	.713	.711	902:	869.	889.	629	.671	.665	.663
Strip	0																	-																

Appendix C

Analysis of Measurement Accuracy

Measurement accuracy in both free-stream velocity and laser velocimeter velocities will be estimated for the particular case of velocity measurements over a helicopter fuselage model in the Langley 14- by 22-Foot Subsonic Tunnel. The perturbation velocity measurements shown here have an estimated error of less than 2.5 percent in the u-component and less than 1.8 percent in the w-component.

Symbols

The symbols used in this appendix are given as follows:

C	tunnel flow correction constant
P_I	indicated pressure, psf
P_T	total or stagnation pressure, psf
P_V	vapor pressure, psf
Q	dynamic pressure, psf
Q_I	indicated dynamic pressure, psf
r	radial distance from hub center
r_m	rotor radius of specific rotor blade set
$T_{ m dew}$	dew point, °F
T_R	ambient temperature, °R
U	downstream component of laser- measured velocity, fps
U_P	laser-measured downstream velocity, fps
\boldsymbol{u}	tangential velocity perturbation, fps
u_P	downstream velocity perturbation, fps
V_{∞}	tunnel free-stream velocity, fps
V_I	tunnel indicated velocity, fps
ΔV	difference velocity (see subsequent text), fps
W	vertical component of laser-measured velocity, fps
w	normal velocity perturbation, fps
α	tip path plane angle of attack
γ	gas constant, 1.4
ρ	fluid density, slugs/ft ³
σ_U	error in U velocity, fps
U	÷ · -

σ_u	error in u velocity, fps
σ_{V_∞}	error in V_{∞} velocity, fps
σ_W	error in W velocity, fps
σ_w	error in w velocity, fps
ψ	rotor azimuth angle, deg

Tunnel Velocity Accuracy

There are several component measurements that affect the calculation of tunnel velocity. The relation used in determining velocity V is

$$V = \sqrt{\frac{2Q}{\rho}} \tag{C1}$$

where

$$Q = CQ_I \tag{C2}$$

Here, Q_I is the indicated dynamic pressure and C is an empirical constant, ranging from 1.1266 to 1.1952 and calibrated for each specific wall-floor-suction configuration of the tunnel. The indicated dynamic pressure is measured by a digital pressure gauge with a stated instrument accuracy of ± 0.04 percent of full scale. The instrument used during this test had a full-scale pressure of 200 kPa.

The density ρ is determined from measurement of the temperature, dew point, and total pressure:

$$\rho = \frac{P_T - 0.3789 P_V}{1718.0 T_R} \left(\frac{P_I}{P_T}\right)^{1/\gamma} \tag{C3}$$

Vapor pressure P_V is found from a simple quadratic in dew point:

$$P_V = 2.80288 + 0.0954685 T_{\rm dew} + 0.0070509 T_{\rm dew}^2$$
 (C4)

Ambient temperature T_R (in degrees Rankine) and dew point are read by an electronic dew point hygrometer with a stated accuracy of $\pm 0.54^{\circ}$ F. The total pressure is measured by a digital pressure gauge similar to the dynamic pressure sensor, but with a full-scale range of 0 to 110 kPa.

An estimate of the velocity measurement accuracy can be conducted using several methods. At any given condition, the errors producing the most positive change in velocity can be used to obtain a high estimate, and the errors producing the most negative change in velocity can be used to obtain a low estimate. This type of analysis is a "worst case" method and is not a good estimate of the likely error in the tunnel velocity. A better estimate can be obtained by perturbing each of the error sources separately, finding the high and low velocity perturbations due to each of the error sources, and using the square

root of the sum of the squares of the high perturbations for the high estimate, and likewise for the low estimate.

At the test condition for the helicopter fuselage the values recorded on the static data system will be used for this error estimate. Four separate instrument errors contribute to the errors in dynamic pressure and velocity. A contributing factor to the velocity error is the computation of density. In table C1, the nominal instrument reading and its maximum error are tabulated against the estimates of high- and low-error values resulting from the instrument error using the data reduction procedure in the static data system.

Table C1 shows that the accuracy of the indicated tunnel velocity is principally due to the accuracy of the dynamic-pressure indicating instrument.

Laser Velocimeter Accuracy

The errors in the laser velocimeter measurements are summarized in table C2. These error calculations are based on the development of system measurement precision in references C1 and C2. The main sources of error in these measurements are due to the crossbeam-angle measurement and the clock synchronization and quantization in the signal processor.

The crossbeam-angle error reflects the ability to accurately measure the angle between the two crossed laser beams, since the measured velocity is proportional to the frequency divided by the sine of the angle. The clock synchronization and quantization errors occur in the signal processor as a result of the clock speed and integer nature of the counter.

Other errors, such as time jitter, velocity bias, Bragg bias, and velocity gradient are negligible because of the improvements in the signal processing equipment and the method of data processing over that used in reference C1. The expansion of the laser beams was not measured during the experimental program, so the error induced by diverging fringes in the sample volume is not known. The error introduced by the ability of the seed particle to faithfully follow the flow is dependent upon the size of the particle and the accelerations in the flow. It was found that for this study, the particle lag error is negligible.

The bias errors are summed to give the total bias error, and the total random error is found by taking the square root of the sum of the squares of the individual random errors. The total system error is determined by squaring both the bias and the random error, and then taking the square root of the sum of those squares. The resulting total system error is between 1.19- and 1.80-percent velocity.

Effect of Tunnel Velocity Accuracy

The measured velocity data found in table 1 of the basic report have been corrected for suspected inaccuracies in the measured tunnel velocity. The procedure and rationale for this correction follow.

The large discrepancy between the laser-measured velocity and tunnel free-stream velocity at the forward-most portion of the measurement plane did not correlate well with the expected velocity perturbation due to the presence of the fuselage. After estimating the possible error in tunnel velocity (above), it was determined that the discrepancy between laser measurement and tunnel measurement should be corrected in the presented data.

The least velocity perturbation in the field of laser measurements should occur (from potential theory) at the forward-most position in the measurement plane. At this location the two analytical fuselage models predicted similar perturbations approaching the limiting zero-perturbation case. The velocity correction procedure assumed that a correction velocity ΔV existed that could be defined as the difference between the actual tunnel velocity V_{∞} and the indicated tunnel velocity V_I :

$$V_{\infty} = V_I + \Delta V \tag{C5}$$

At the forward-most laser measurement, the value measured is assumed to be the sum of the free-stream velocity V_{∞} and a perturbation velocity u_P because of the presence of the fuselage:

$$U_P = V_{\infty} + u_P \tag{C6}$$

Dividing by the free-stream velocity V_{∞} and assuming that the perturbation due to the fuselage is given accurately by the source-panel model, the correction velocity can now be found as

$$\Delta V = \frac{U_P}{1 + (u_P/V_\infty)} - V_I \tag{C7}$$

The correction velocity was found to be -3.89 fps.

This correction was applied to the tunnel indicated velocity at each measurement location. Table C3 shows the uncorrected or indicated (I) and corrected (C) free-stream velocities and the percent of change in velocity ΔV_{∞} . The change is about one-half the accuracy computed above.

To demonstrate the effect of this correction, figure C1 shows the differences between the corrected and original velocity perturbations. Figure C1(a) displays the data with the tunnel indicated velocity used as the free-stream velocity, whereas figure C1(b)

displays the data with the free-stream velocity corrected based on the laser velocimeter measurement.

Uncertainty in Presented Perturbation Velocities

To determine the resulting uncertainty in the presented perturbation velocities u and w, the method of Taylor expansion from reference C3 is used. The velocities are computed as

$$u = (U - V_{\infty}) \cos \alpha + W \sin \alpha \tag{C8}$$

$$w = W \cos \alpha - (U - V_{\infty}) \sin \alpha \tag{C9}$$

The u perturbation velocity can be represented as

$$u = f(U, V_{\infty}, W) \tag{C10}$$

This function f can be expanded in a Taylor series:

$$u + \sigma_u = u + \frac{\partial u}{\partial U} \sigma_U + \frac{\partial u}{\partial V_{\infty}} \sigma_{V_{\infty}} + \frac{\partial u}{\partial W} \sigma_W \quad (C11)$$

Assuming independence of the variables U, V_{∞} , and W, the square of the error σ_u is

$$\sigma_u^2 = \cos^2 \alpha \, \sigma_U^2 + \cos^2 \alpha \, \sigma_{V_\infty}^2 + \sin^2 \alpha \, \sigma_W^2 \qquad (C12)$$

If $\alpha = -3.0^{\circ}$, then σ_U , $\sigma_{V_{\infty}}$, and σ_W are equal to 1.8 percent; the resulting σ_u is 2.5 percent. Similarly, the w perturbation-velocity component error σ_w is computed to be 1.8 percent.

References

- C1. Young, Warren H., Jr.; Meyers, James F.; and Hepner, Timothy E.: Laser Velocimeter Systems Analysis Applied to a Flow Survey Above a Stalled Wing. NASA TN D-8408, 1977.
- C2. Dring, R. P.: Sizing Criteria for Laser Anemometry Particles. Trans. ASME, J. Fluids Eng., vol. 104, Mar. 1982, pp. 15-17.
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Table C1. Potential Errors in Tunnel Flow Parameters

	· · · · · · · · · · · · · · · · · · ·			Velocity,	Density,
Instrument	Nominal	Error	Q, percent	percent	percent
Q_I	10.0 psf	1.670 psf	±16.7	+8.06 to -8.76	±0.064
P_T	2137 psf	0.919 psf		± 0.022	± 0.043
$T_{ m dew}$	57.31°F	0.540°F		± 0.004	±0.009
T_R	540.0°R	0.540°R		± 0.050	±0.100
Cumulativ	e errors		±16.7	+8.06 to -8.76	±0.127

Table C2. Potential Errors in Laser Velocimeter Measurements^a

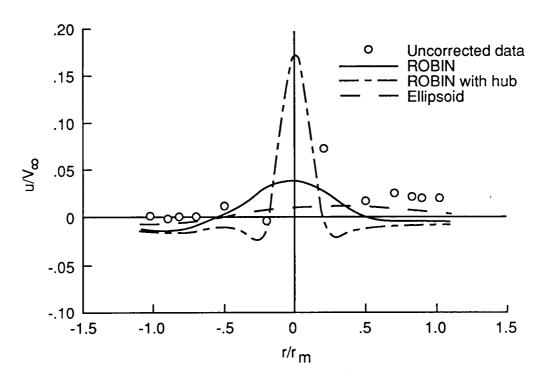
Error source	Bias error, percent	Random error, percent
Crossbeam angle measurement	±0.81	N/A
Diverging fringes	N/M	N/M
Time jitter 	N/A	N/A
Clock synchronization	0.56	±0.56
Quantization	N/M	±1.02
Velocity bias	Negligible	Negligible
Bragg bias	Negligible	Negligible
Velocity gradient	Negligible	Negligible
Particle lag	Negligible	Negligible
Total errors	-0.25 to 1.37	±1.164

^aN/A: not applicable; N/M: not measured; Negligible: less than 0.001 percent.

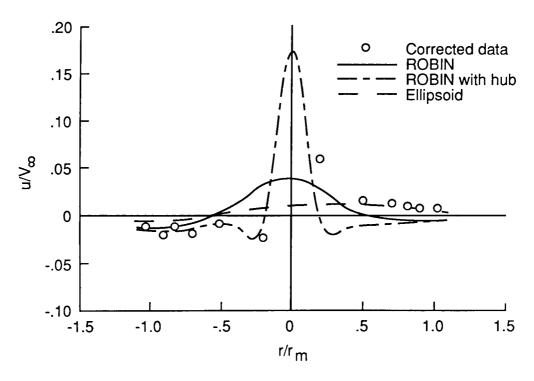
Table C3. Effect of Tunnel Velocity Correction^a

ψ , deg	r/r_m	$V_{\infty,I}$, fps	$V_{\infty,C}$, fps	ΔV_{∞} , percent
0	0.20	93.765	89.875	4.15
	.50	94.300	90.410	4.13
	.70	93.778	89.888	4.15
	.82	93.768	89.878	4.15
	.90	93.771	89.881	4.15
	1.02	93.770	89.880	4.15
180	0.20	94.479	90.589	4.12
	.50	94.452	90.562	4.12
	.70	94.426	90.536	4.12
	.82	93.794	89.904	4.15
	.90	94.336	90.476	4.12
	1.02	93.817	89.927	4.15

^aSubscript I: indicated; subscript C: corrected.



(a) Tunnel indicated velocity.



(b) Corrected free-stream velocity.

Figure C1. Velocity perturbations over fuselage centerline.

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Table 1. Measured Induced Velocities of Fuselage [Corrected values from table C3]

ψ , deg	r/r_m	u/V_{∞}	σ_u , fps	O_u	w/V_{∞}	σ_w , fps	O_w	V_{∞} , fps
0	0.20	0.0594	0.0359	1518	0.0053	0.0093	1190	89.875
	.50	.0158	.0344	1434	0199	.0291	1175	90.410
	.70	.0127	.0333	1539	0153	.0306	1108	89.888
	.82	.0096	.0326	1469	0119	.0313	1065	89.878
1	.90	.0075	.0339	1467	0114	.0293	981	89.881
	1.02	.0079	.0333	1415	0102	.0299	1031	89.880
180	0.20	-0.0239	0.0376	1345	0.0807	0.0324	515	90.589
	.50	0086	.0403	611	.0556	.0297	195	90.562
	.70	0191	.0430	139				90.536
	.82	0124	.0353	1505	.0391	.0293	794	89.904
	.90	0211	.0350	1531	.0346	.0284	596	90.476
	1.02	0121	.0366	1559	.0270	.0299	695	89.927

Table 2. Test Conditions Described in References 19-23

Reference	r_m/R	$lpha,\deg$	V_{∞} , fps
19	0.8470	-3.00	93.0
20	.8470	-3.04	143.2
21	.8470	-4.04	187.1
22	.8125	-3.04	94.1
23	.8125	-3.05	144.0

Table 3. Induced Velocity Perturbations of Basic Fuselage Computed at Inflow Measurement Plane

(a) $r_m/R = 0.8470$; $\alpha = -3.0^{\circ}$

	Τ-,	1	/**	17.7	11 / 1	Ι,	177		17.7
ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
0	0.20	0.027622	-0.000150	-0.027460	180	0.20	0.031654	-0.000208	0.034158
	.40	.006401	000129	033328		.40	.011556	000209	.046595
1	.50	.000416	000095	029066		.50	.003801	000172	.045412
	.60	002422	000058	024602		.60	002628	000128	.042575
	.70	003833	000044	021063		.70	008236	000097	.037851
	.74	004176	000036	019825		.74	010052	000087	.035394
	.78	004463	000030	018691		.78	011544	000078	.032736
	.82	004712	000024	017639		.82	012680	000070	.029938
	.86	004929	000020	016648		.86	013454	000063	.027094
1	.90	005117	000016	015705		.90	013903	000057	.024293
	.94	005273	000013	014794		.94	014019	000051	.021606
	.98	005386	000007	013937		.98	013879	000045	.019095
	1.02	005493	000004	013107		1.02	013538	000040	.016793
	1.04	005540	000002	012712		1.04	013309	000038	.015725
	1.10	005625	0	011542	<u> </u>	1.10	012456	000032	.012864
30	0.20	0.028703	-0.005137	-0.021882	210	0.20	0.031864	-0.008950	0.026492
,	.40	.011359	011401	023959		.40	.015995	018060	.029609
	.50	.006164	011676	020305		.50	.009949	019169	.026436
	.60	.003100	011059	016651		.60	.005230	018872	.022699
	.70	.001272	010136	013556		.70	.001559	017598	.018801
	.74	.000752	009742	012481		.74	.000378	016891	.017259
	.78	.000316	009350	011494		.78	000623	016098	.015750
	.82	000048	008961	010586		.82	001457	015243	.014294
	.86	000355	008580	009753		.86	002131	014353	.012912
	.90	000615	008203	008980		.90	002659	013448	.011616
	.94	000839	007826	008258		.94	003055	012548	.010416
	.98	001024	007463	007601		.98	003336	011667	.009316
	1.02	001182	007103	006986		1.02	003521	010819	.008316
	1.04	001250	006930	006701		1.04	003582	010409	.007853
	1.10	001411	006417	005902		1.10	003664	009247	.006604

Table 3. Continued

(a) Continued

	1 ,	1 /**	17.7	1	II , , ,	T -, -	1 /**	177	,,,,
ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
60	0.20	0.030362	-0.003487	-0.010684	240	0.20	0.031798	-0.008302	0.012668
	.40	.017344	007670	010557		.40	.019523	012185	.010122
!	.50	.012860	007759	008696		.50	.014845	011731	.008079
	.60	.009654	007263	006942		.60	.011230	010716	.006351
	.70	.007329	006544	005491		.70	.008468	009519	.004965
	.74	.006591	006242	004998		.74	.007564	009024	.004491
	.78	.005937	005940	004550		.78	.006757	008538	.004062
	.82	.005360	005643	004144		.82	.006037	008059	.003671
	.86	.004848	005353	003775		.86	.005397	007595	.003316
	.90	.004393	005072	003443		.90	.004827	007149	.002996
	.94	.003985	004807	003144		.94	.004322	006722	.002706
	.98	.003623	004548	002872		.98	.003873	006313	.002444
	1.02	.003301	004302	002626		1.02	.003476	005927	.002208
	1.04	.003152	004184	002512		1.04	.003294	005741	.002099
	1.10	.002749	003847	002202		1.10	.002810	005217	.001805
90	0.20	0.031299	0.002389	0.000704	270	0.20	0.031269	-0.002499	0.000506
	.40	.019696	.001763	000661		.40	.019667	001718	000806
	.50	.015395	.001359	000740		.50	.015370	001298	000849
	.60	.012103	.001041	000696		.60	.012083	000978	000771
	.70	.009597	.000815	000604		.70	.009580	000758	000657
	.74	.008770	.000744	000565		.74	.008755	000690	000611
[.78	.008027	.000681	000527		.78	.008013	000631	000566
	.82	.007363	.000625	000491		.82	.007350	000579	000525
	.86	.006759	.000576	000456		.86	.006747	000532	000486
	.90	.006215	.000531	000424		.90	.006204	000491	000450
	.94	.005726	.000490	000394		.94	.005715	000453	000417
	.98	.005282	.000454	000367		.98	.005273	000419	000387
	1.02	.004880	.000421	000341		1.02	.004871	000389	000359
	1.04	.004693	.000406	000329		1.04	.004684	000375	000346
	1.10	.004183	.000364	000296		1.10	.004175	000336	000310

Table 3. Continued

(a) Concluded

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ,\deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
120	0.20	0.031860	0.008169	0.012908	300	0.20	0.030354	0.003342	-0.010873
	.40	.019553	.012232	.010347		.40	.017321	.007707	010721
	.50	.014851	.011809	.008245		.50	.012823	.007828	008819
	.60	.011222	.010795	.006468		.60	.009610	.007322	007028
	.70	.008455	.009590	.005047		.70	.007287	.006594	005544
	.74	.007549	.009090	.004563		.74	.006551	.006286	005041
	.78	.006742	.008599	.004124		.78	.005898	.005979	004586
	.82	.006022	.008115	.003724		.82	.005323	.005678	004174
	.86	.005382	.007647	.003363		.86	.004813	.005384	003801
	.90	.004813	.007198	.003038		.90	.004361	.005099	003464
	.94	.004307	.006767	.002743		.94	.003956	.004831	003162
	.98	.003860	.006355	.002477		.98	.003596	.004570	002887
	1.02	.003462	.005965	.002237		1.02	.003275	.004321	002639
	1.04	.003281	.005778	.002126		1.04	.003127	.004202	002524
_	1.10	.002797	.005250	.001828		1.10	.002728	.003862	002211
150	0.20	0.031921	0.008669	0.026720	330	0.20	0.028709	0.004903	-0.022038
	.40	.015957	.017969	.029969		.40	.011303	.011321	024182
	.50	.009862	.019136	.026724		.50	.006067	.011653	020466
	.60	.005140	.018867	.022902		.60	.003003	.011057	016757
	.70	.001479	.017604	.018945		.70	.001188	.010134	013617
	.74	.000304	.016899	.017386		.74	.000675	.009741	012528
	.78	000693	.016107	.015861		.78	.000246	.009346	011526
	.82	001522	.015254	.014392		.82	000111	.008959	010609
	.86	002192	.014365	.012999		.86	000409	.008576	009764
	.90	002716	.013460	.011693]	.90	000664	.008201	008987
	.94	003108	.012560	.010484		.94	000882	.007822	008260
	.98	003386	.011679	.009375		.98	001062	.007459	007599
	1.02	003568	.010830	.008368		1.02	001215	.007098	006983
j	1.04	003628	.010419	.007901		1.04	001279	.006923	006696
	1.10	003706	.009257	.006644		1.10	001436	.006409	005896

Table 3. Continued

(b) $r_m/R = 0.8470$; $\alpha = -4.0^{\circ}$

	T		Ţ		11			1	1
ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
0	0.20	0.028314	-0.000142	-0.024951	180	0.20	0.031126	-0.000211	0.036910
	.40	.007224	000119	031642		.40	.010669	000215	.048646
	.50	.001199	000086	027701		.50	.002816	000178	.047073
	.60	001691	000050	023493	1	.60	003649	000133	.043812
	.70	003153	000037	020180		.70	009205	000100	.038671
	.74	003518	000029	019024		.74	010978	000090	.036062
	.78	003828	000023	017969		.78	012416	000081	.033269
	.82	004100	000018	016991		.82	013490	000073	.030351
ļ	.86	004342	000014	016070		.86	014199	000065	.027404
	.90	004556	000010	015192		.90	014581	000059	.024516
	.94	004739	000008	014343		.94	014630	000053	.021758
	.98	004877	000002	013545		.98	014425	000047	.019189
	1.02	005013	.000001	012770		1.02	014025	000042	.016844
	1.04	005075	.000003	012402		1.04	013767	000040	.015757
	1.10	005201	.000005	011297	:	1.10	012836	000033	.012853
30	0.20	0.029263	-0.004164	-0.019674	210	0.20	0.031458	-0.009995	0.028872
	.40	.011935	010341	022864		.40	.015422	019269	.030887
	.50	.006678	010725	019588		.50	.009367	020257	.027277
	.60	.003548	010242	016206		.60	.004676	019777	.023193
	.70	.001657	009460	013304		.70	.001064	018304	.019047
	.74	.001113	009121	012288		.74	000086	017522	.017431
	.78	.000654	008781	011350		.78	001054	016657	.015862
	.82	.000267	008443	010486		.82	001855	015737	.014357
	.86	000061	008109	009688		.86	002496	014787	.012935
	.90	000341	007778	008946		.90	002992	013828	.011610
	.94	000585	007442	008248		.94	003357	012880	.010386
	.98	000790	007117	007611		.98	003610	011957	.009269
	1.02	000967	006792	007012		1.02	003768	011072	.008257
	1.04	001043	006635	006733		1.04	003816	010645	.007789
	1.10	001230	006166	005948		1.10	003864	009441	.006531

Table 3. Continued

(b) Continued

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
		· ·	1	-0.008949	240	0.20	0.031628	-0.009782	0.014470
60	0.20	0.030665	-0.002059		240	.40	.019320	-0.009782 013432	.010641
	.40	.017587	006489	010071		1	1 ' '	i .	.010041
	.50	.013057	006829	008502		.50	.014655	012715	.006388
	.60	.009812	006551	006908		.60	.011060	011462	I i
	.70	.007457	006008	005538		.70	.008323	010074	.004915
	.74	.006708	005764	005064		.74	.007429	009515	.004420
	.78	.006044	005514	004629		.78	.006632	008972	.003978
	.82	.005458	005264	004232		.82	.005922	008443	.003578
	.86	.004937	005014	003870		.86	.005290	007934	.003217
	.90	.004474	004770	003540		.90	.004729	007450	.002894
	.94	.004059	004537	003242		.94	.004232	006988	.002603
	.98	.003691	004306	002970		.98	.003791	006550	.002342
	1.02	.003363	004086	002722		1.02	.003400	006137	.002108
	1.04	.003211	003978	002607		1.04	.003221	005940	.002001
	1.10	.002801	003672	002293		1.10	.002746	005384	.001711
90	0.20	0.031366	0.003932	0.002265	270	0.20	0.031325	-0.004038	0,002068
	.40	.019721	.002913	000339		.40	.019682	002867	000481
	.50	.015407	.002229	000666		.50	.015374	002168	000771
	.60	.012107	.001686	000739		.60	.012081	001624	000812
	.70	.009597	.001291	000698		.70	.009575	001236	000748
	.74	.008768	.001166	000668		.74	.008748	001114	000712
	.78	.008025	.001056	000635		.78	.008006	001007	000673
	.82	.007360	.000958	000602		.82	.007343	000913	000635
	.86	.006756	.000872	000567	Ì	.86	.006740	000830	000596
	.90	.006211	.000795	000534		.90	.006197	000756	000559
	.94	.005722	.000725	000502		.94	.005709	000689	000524
	.98	.005279	.000664	000471		.98	.005267	000630	000490
	1.02	.004877	.000609	000442		1.02	.004865	000578	000459
	1.04	.004689	.000584	000428		1.04	.004679	000554	000444
i	1.10	.004179	.000515	000389		1.10	.004170	000489	000402
	1.10	1003110	.000010	.00000	II	L	1 .0011.0		

Table 3. Continued

(b) Concluded

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ,\deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
120	0.20	0.031699	0.009650	0.014715	300	0.20	0.030648	0.001919	-0.009132
	.40	.019358	.013484	.010871	1	.40	.017557	.006526	010224
	.50	.014666	.012798	.008457		.50	.013014	.006894	008613
	.60	.011057	.011545	.006507		.60	.009765	.006606	006984
ļ	.70	.008313	.010147	.004998		.70	.007411	.006053	005583
	.74	.007417	.009583	.004493		.74	.006665	.005804	005100
	.78	.006620	.009036	.004041		.78	.006002	.005549	004658
	.82	.005909	.008502	.003631		.82	.005418	.005294	004256
	.86	.005277	.007989	.003265		.86	.004900	.005040	003889
	.90	.004716	.007500	.002936		.90	.004440	.004792	003556
	.94	.004219	.007035	.002641		.94	.004028	.004556	003255
	.98	.003779	.006593	.002375	1	.98	.003663	.004323	002980
	1.02	.003389	.006177	.002137		1.02	.003336	.004100	002731
	1.04	.003210	.005978	.002028		1.04	.003185	.003992	002615
	1.10	.002735	.005418	.001734		1.10	.002779	.003683	002299
150	0.20	0.031521	0.009710	0.029108	330	0.20	0.029264	0.003940	-0.019821
	.40	.015385	.019180	.031260		.40	.011877	.010268	023071
	.50	.009278	.020226	.027575		.50	.006579	.010707	019734
	.60	.004585	.019773	.023404		.60	.003452	.010242	016297
	.70	.000984	.018312	.019197		.70	.001574	.009459	013352
	.74	000161	.017532	.017564		.74	.001037	.009119	012322
	.78	001125	.016668	.015978		.78	.000585	.008776	011371
	.82	001921	.015750	.014459		.82	.000206	.008440	010498
	.86	002559	.014800	.013026		.86	000113	.008104	009689
	.90	003050	.013842	.011689		.90	000388	.007773	008942
	.94	003412	.012893	.010456		.94	000626	.007435	008241
	.98	003661	.011970	.009331		.98	000825	.007110	007599
	1.02	003816	.011084	.008311		1.02	000997	.006784	006999
	1.04	003863	.010657	.007840		1.04	001070	.006625	006718
	1.10	003906	.009451	.006572		1.10	001251	.006155	005934

Table 3. Continued

(c) $r_m/R = 0.8125$; $\alpha = -3.0^{\circ}$

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ,deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
0	0.20	0.028476	-0.000149	-0.026583	180	0.20	0.032332	-0.000201	0.033065
	.40	.007763	000134	033793		.40	.013056	000214	.046535
	.50	.001325	000102	030033		.50	.005217	000182	.045818
	.60	001926	000065	025631	:	.60	001117	000138	.043412
	.70	003532	000051	022014		.70	006771	000104	.039418
	.74	003923	000042	020747		.74	008711	000094	.037276
	.78	004239	000035	019585		.78	010386	000085	.034863
	.82	004507	000029	018513		.82	011756	000077	.032281
	.86	004740	000024	017513		.86	012795	000069	.029585
	.90	004946	000019	016568		.90	013503	000063	.026857
	.94	005124	000016	015665		.94	013914	000056	.024175
	.98	005273	000013	014793	l	.98	014019	000051	.021601
	1.02	005381	000008	013970		1.02	013888	000046	.019188
	1.04	005434	000007	013560	ŀ	1.04	013750	000043	.018052
	1.10	005565	000001	012413		1.10	013113	000037	.014952
30	0.20	0.029435	-0.004765	-0.021272	210	0.20	0.032461	-0.008421	0.025863
	.40	.012470	011205	024446		.40	.017144	017684	.029981
	.50	.007013	011724	021085		.50	.011050	019082	.027154
	.60	.003706	011240	017482		.60	.006279	019042	.023629
	.70	.001708	010415	014380		.70	.002500	018045	.019918
	.74	.001135	010039	013282		.74	.001250	017434	.018419
	.78	.000656	009661	012271		.78	.000158	016734	.016944
	.82	.000251	009285	011338		.82	000772	015960	.015505
	.86	000088	008914	010479		.86	001549	015134	.014118
	.90	000379	008548	009685		.90	002181	014278	.012800
	.94	000625	008187	008948		.94	002678	013409	.011563
	.98	000839	007826	008256		.98	003055	012546	.010414
	1.02	001018	007477	007625		1.02	003327	011701	.009357
	1.04	001099	007302	007323		1.04	003428	011288	.008863
	1.10	001295	006797	006488		1.10	003616	010105	.007517

Table 3. Continued

(c) Continued

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
60		0.030930	-0.003208	-0.010424	240	0.20	0.032301	-0.007959	0.012593
00	0.20		-0.003208 007554		240	1	.020397	-0.007939 012167	.010479
	.40	.018218		010832 009079		.40	.020397	012107 011888	.010479
	.50	1	007808		[]		1	l .	1
	.60	.010350	007414	007343		.60	.012026	010989	.006741
	.70	.007917	006758	005873		.70	.009180	009868	.005330
}	.74	.007137	006471	005366		.74	.008235	009397	.004844
	.78	.006450	006181	004902		.78	.007391	008925	.004400
	.82	.005837	005890	004480		.82	.006633	008458	.003994
	.86	.005293	005607	004096		.86	.005954	008001	.003625
	.90	.004809	005328	003745		.90	.005346	007557	.003288
	.94	.004375	005060	003429		.94	.004804	007130	.002983
i	.98	.003984	004806	003143		.98	.004321	006721	.002705
	1.02	.003637	004558	002882		1.02	.003890	006329	.002454
	1.04	.003477	004438	002760		1.04	.003692	006140	.002337
	1.10	.003043	004096	002429		1.10	.003163	005604	.002020
90	0.20	0.031800	0.002375	0.000810	270	0.20	0.031759	-0.002486	0.000605
	.40	.020498	.001831	000637		.40	.020475	001783	000793
	.50	.016185	.001433	000740		.50	.016160	001373	000856
	.60	.012827	.001109	000713		.60	.012806	001046	000796
	.70	.010242	.000873	000631		.70	.010224	000814	000689
	.74	.009385	.000797	000594		.74	.009368	000741	000645
	.78	.008611	.000730	000557	ļ	.78	.008596	000678	000601
]	.82	.007912	.000672	000520		.82	.007898	000622	000559
l	.86	.007284	.000619	000486		.86	.007272	000573	000520
	.90	.006712	.000572	000453		.90	.006700	000529	000483
	.94	.006193	.000530	000422		.94	.006182	000490	000449
1	.98	.005725	.000490	000394	ll .	.98	.005714	000453	000417
1	1.02	.005298	.000455	000368		1.02	.005289	000420	000388
	1.04	.005099	.000439	000355		1.04	.005090	000405	000374
	1.10	.004556	.000395	000320		1.10	.004548	000365	000336
		100200			U				

Table 3. Continued

(c) Concluded

120 0	r/r_m 0.20 $.40$ $.50$ $.60$ $.70$	u/V_{∞} 0.032363 $.020432$ $.015715$ $.012020$	v/V_{∞} 0.007815 0.12198 0.11963	$w/V_{\infty} = 0.012827 \\ 0.010702$	$\psi, \deg 300$	r/r_m 0.20	u/V_{∞}	v/V_{∞}	w/V_{∞}
	.40 .50 .60 .70	.020432 $.015715$.012198		აսս			0.0000000	0.010600
	.50 .60 .70	.015715		1 .010702	H	1	0.030922	0.003053	-0.010609
	.60 .70		.011903	000050		.40	.018195	.007585	011008
	.70	012020	!	.008652		.50	.013625	.007873	009212
			.011069	.006869		.60	.010306	.007475	007439
i i		.009167	.009941	.005421	}	.70	.007874	.006811	005933
	.74	.008221	.009466	.004923		.74	.007095	.006519	005416
i I	.78	.007376	.008989	.004470		.78	.006409	.006224	004944
	.82	.006618	.008518	.004055		.82	.005798	.005929	004516
	.86	.005939	.008057	.003678		.86	.005256	.005641	004125
1	.90	.005332	.007609	.003335		.90	.004775	.005358	003771
1 1	.94	.004790	.007179	.003025		.94	.004343	.005087	003451
	.98	.004306	.006766	.002742		.98	.003955	.004830	003162
1	102	.003876	.006371	.002486		1.02	.003609	.004580	002897
1.	1.04	.003678	.006180	.002368		1.04	.003450	.004459	002775
1.	1.10	.003150	.005640	.002046		1.10	.003020	.004113	002440
150 0.	0.20	0.032520	0.08140	0.026075	330	0.20	0.029442	0.004526	-0.021421
.	.40	.017111	.017584	.030359		.40	.012419	.011111	024670
1 .	.50	.010969	.019039	.027460		.50	.006925	.011697	021266
.	.60	.006190	.019034	.023851	ļ	.60	.003600	.011243	017605
.	.70	.002417	.018049	.020077		.70	.001619	.010413	014454
1.	.74	.001172	.017440	.018558		.74	.001053	.010037	013340
]],	.78	.000085	.016742	.017068		.78	.000581	.009659	012315
.	.82	000841	.015970	.015615		.82	.000183	.009283	011371
]] .	.86	001614	.015145	.014215		.86	000151	.008911	010500
1	.90	002241	.014289	.012886		.90	000432	.008546	009698
.	.94	002735	.013421	.011639		.94	000674	.008185	008954
1	.98	003109	.012558	.010481		.98	000883	.007821	008259
	1.02	003378	.011712	.009416		1.02	001055	.007473	007623
1	1.04	003477	.011300	.008919		1.04	001135	.007297	007320
1	1.10	003661	.010115	.007563		1.10	001323	.006790	006482

Table 3. Continued

(d) $r_m/R = 0.8125$; $\alpha = -4.0^{\circ}$

	Г	1	1	1	п		1	1	
ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	$\mid w/V_{\infty} \mid$
0	0.20	0.029151	-0.000142	-0.024042	180	0.20	0.031823	-0.000205	0.035843
	.40	.008591	000124	032048		.40	.012188	000220	.048647
	.50	.002117	000093	028608		.50	.004249	000188	.047563
	.60	001182	000057	024462		.60	002136	000142	.044753
	.70	002837	000043	021071		.70	007763	000108	.040352
	.74	003249	000035	019885		.74	009670	000098	.038058
	.78	003586	000028	018800		.78	011302	000088	.035502
	.82	003876	000022	017803		.82	012618	000080	.032793
	.86	004132	000017	016874		.86	013597	000072	.029985
	.90	004361	000013	015995		.90	014242	000065	.027159
	.94	004565	000010	015155		.94	014589	000058	.024395
	.98	004739	000008	014341		.98	014629	000053	.021753
	1.02	004871	000002	013576		1.02	014437	000047	.019284
	1.04	004938	000001	013192		1.04	014269	000045	.018125
	1.10	005111	.000004	012121		1.10	013551	000038	.014972
30	0.20	0.029986	-0.003811	-0.019014	210	0.20	0.032068	-0.009442	0.028291
	.40	.013055	010131	023277		.40	.016576	018904	.031340
	.50	.007540	010748	020301		.50	.010467	020202	.028077
	.60	.004169	010389	016978		.60	.005714	019995	.024199
	.70	.002111	009699	014079		.70	.001985	018808	.020227
	.74	.001515	009377	013046		.74	.000763	018121	.018646
	.78	.001012	009051	012089		.78	000299	017349	.017103
	.82	.000585	008725	011202		.82	001198	016508	.015608
	.86	.000225	008403	010384		.86	001943	015620	.014175
	.90	000086	008081	009623		.90	002543	014707	.012821
	.94	000352	007763	008915		.94	003010	013787	.011555
	.98	000586	007441	008247		.98	003358	012878	.010384
	1.02	000783	007130	007635		1.02	003602	011992	.009310
	1.04	000874	006973	007341		1.04	003690	011562	.008810
	1.10	001094	006513	006524		1.10	003841	010330	.007450

Table 3. Continued

(d) Continued

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
60	0.20	0.031231	-0.001795	-0.008619	240	0.20	0.032137	-0.009422	0.014465
	.40	.018469	006334	010282		.40	.020193	013456	.011066
	.50	.013867	006828	008838		.50	.015512	012925	.008733
	.60	.010517	006653	007278		.60	.011850	011789	.006810
	.70	.008054	006177	005902		.70	.009027	010472	.005298
	.74	.007262	005949	005418		.74	.008093	009935	.004788
	.78	.006565	005714	004971		.78	.007258	009403	.004326
	.82	.005942	005473	004561		.82	.006509	008883	.003908
	.86	.005389	005233	004185		.86	.005839	008379	.003531
	.90	.004897	004993	003840		.90	.005241	007893	.003188
	.94	.004456	004760	003526		.94	.004707	007430	.002881
	.98	.004058	004536	003241		.98	.004231	006987	.002603
	1.02	.003705	004315	002980		1.02	.003807	006566	.002352
	1.04	.003542	004208	002857		1.04	.003613	006365	.002236
	1.10	.003100	003899	002523		1.10	.003093	005794	.001923
90	0.20	0.031868	0.003909	0.002447	270	0.20	0.031817	-0.004016	0.002242
	.40	.020525	.003031	000257		.40	.020491	002981	000409
	.50	.016200	.002357	000628		.50	.016166	002297	000740
	.60	.012833	.001804	000736		.60	.012805	001742	000815
	.70	.010243	.001392	000716		.70	.010220	001334	000771
	.74	.009384	.001259	000691		.74	.009363	001204	000739
	.78	.008609	.001142	000662		.78	.008589	001091	000704
	.82	.007909	.001039	000630		.82	.007891	000991	000667
	.86	.007281	.000947	000598		.86	.007265	000902	000630
	.90	.006708	.000865	000565		.90	.006693	000823	000593
	.94	.006189	.000792	000533		.94	.006175	000753	000557
	.98	.005721	.000725	000502		.98	.005708	000689	000524
	1.02	.005295	.000666	000473		1.02	.005283	000633	000492
ļ	1.04	.005096	.000639	000458		1.04	.005084	000607	000476
	1.10	.004553	.000565	000418		1.10	.004542	000537	000433

Table 3. Concluded

(d) Concluded

	т :		T	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	II			1 /	
ψ,\deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ,\deg	$ r/r_m $	u/V_{∞}	v/V_{∞}	w/V_{∞}
120	0.20	0.032207	0.009280	0.014704	300	0.20	0.031214	0.001645	-0.008799
	.40	.020237	.013492	.011294		.40	.018438	.006364	010448
	.50	.015528	.013005	.008914		.50	.013824	.006891	008961
	.60	.011850	.011873	.006940		.60	.010468	.006710	007364
	.70	.009018	.010548	.005390	ŀ	.70	.008006	.006225	005954
	.74	.008082	.010007	.004868		.74	.007216	.005993	005461
	.78	.007246	.009471	.004397		.78	.006521	.005753	005006
	.82	.006497	.008946	.003970		.82	.005901	.005507	004590
	.86	.005827	.008438	.003585		.86	.005350	.005262	004208
	.90	.005228	.007947	.003236		.90	.004861	.005018	003859
	.94	.004694	.007480	.002923		.94	.004422	.004782	003542
	.98	.004218	.007034	.002640		.98	.004027	.004555	003255
	1.02	.003795	.006610	.002385		1.02	.003676	.004332	002991
	1.04	.003601	.006406	.002267		1.04	.003514	.004224	002867
	1.10	.003082	.005831	.001949		1.10	.003075	.003912	002531
150	0.20	0.032132	0.009157	0.028510	330	0.20	0.029987	0.003583	-0.019155
	.40	.016544	.018805	.031731		.40	.013001	.010046	023486
	.50	.010385	.020161	.028394		.50	.007451	.010726	020467
	.60	.005624	.019988	.024429		.60	.004064	.010394	017086
	.70	.001901	.018814	.020392		.70	.002023	.009697	014140
	.74	.000684	.018129	.018791		.74	.001433	.009375	013090
	.78	000374	.017359	.017232		.78	.000938	.009049	012120
	.82	001268	.016520	.015722		.82	.000518	.008722	011223
	.86	002009	.015633	.014276		.86	.000163	.008398	010393
	.90	002605	.014720	.012910		.90	000137	.008077	009625
	.94	003068	.013801	.011634		.94	000399	.007758	008911
	.98	003413	.012891	.010454		.98	000627	.007434	008239
	1.02	003653	.012005	.009372		1.02	000818	.007123	007623
	1.04	003740	.011575	.008868		1.04	000906	.006965	007328
	1.10	003887	.010341	.007498		1.10	001120	.006504	006510

Table 4. Induced Velocity Perturbations of Fuselage and Hub Computed at Inflow Measurement Plane $[r_m/R=0.8470;\,\alpha=-3.0^\circ]$

ψ, \deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
0	0.20	-0.003858	0.000231	-0.125306	180	0.20	-0.010468	0.000233	0.147124
	.40	013455	000116	047204		.40	012023	000239	.060708
	.50	011484	000101	035480		.50	009735	000174	.051497
	.60	009927	000066	027879	l.	.60	011014	000131	.045533
	.70	008813	000051	022889		.70	013723	000099	.039392
	.74	008453	000043	021292		.74	014732	000089	.036587
	.78	008160	000035	019879		.78	015568	000080	.033674
	.82	007924	000029	018607		.82	016158	000072	.030680
	.86	007734	000024	017442		.86	016478	000064	.027684
ĺ	.90	007579	000020	016360		.90	016545	000058	.024766
ļ	.94	007444	000016	015339		.94	016338	000052	.021987
	.98	007307	000010	014391		.98	015924	000046	.019404
	1.02	007199	000007	013485		1.02	015349	000041	.017044
	1.04	007150	000005	013058		1.04	015016	000039	.015953
	1.10	006984	000002	011810	<u> </u>	1.10	013896	000033	.013035
30	0.20	0.019383	-0.043685	-0.107474	210	0.20	0.016630	-0.057727	0.122390
	.40	000418	025524	035721		.40	.002066	034533	.041106
	.50	000979	019871	025632		.50	.001889	028347	.031255
	.60	001417	016114	019323		.60	.000206	024438	.024996
	.70	001729	013443	015030	1	.70	001744	021180	.019984
	.74	001826	012568	013663		.74	002444	019931	.018179
,	.78	001913	011780	012449		.78	003054	018701	.016475
	.82	001987	011064	011365		.82	003564	017487	.014870
	.86	002050	010410	010393		.86	003968	016298	.013373
	.90	002103	009804	009510		.90	004268	015144	.011989
	.94	002153	009232	008699		.94	004471	014035	.010719
	.98	002189	008705	007971		.98	004589	012977	.009563
	1.02	002218	008205	007299		1.02	004633	011978	.008519
	1.04	002228	007969	006988		1.04	004632	011502	.008038
	1.10	002240	007293	006129		1.10	004553	010170	.006744

Table 4. Continued

				1	11 -			1	,
ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
60	0.20	0.067178	-0.041777	-0.062326	240	0.20	0.068858	-0.057459	0.065002
	.40	.021649	021614	017492		.40	.023747	028066	.015930
	.50	.014958	015785	011817		.50	.016932	020498	.010416
	.60	.010835	012182	008509	ľ	.60	.012386	016025	.007439
	.70	.008057	009743	006358		.70	.009168	012948	.005517
	.74	.007203	008972	005695		.74	.008149	011941	.004919
	.78	.006456	008287	005118		.78	.007251	011040	.004397
	.82	.005803	007676	004610		.82	.006457	010221	.003937
	.86	.005230	007123	004162		.86	.005756	009475	.003528
	.90	.004725	006621	003766		.90	.005138	008793	.003166
	.94	.004275	006170	003415		.94	.004592	008168	.002844
	.98	.003879	005754	003102		.98	.004109	007592	.002557
	1.02	.003527	005373	002822		1.02	.003683	007061	.002300
	1.04	.003364	005194	002694		1.04	.003489	006812	.002183
	1.10	.002928	004701	002347		1.10	.002973	006123	.001868
90	0.20	0.093008	0.006021	-0.001777	270	0.20	0.093084	-0.007733	-0.000741
	.40	.032285	.002224	001405		.40	.032297	002339	001601
	.50	.022191	.001502	001174	·	.50	.022173	001494	001326
	.60	.016140	.001124	000944		.60	.016124	001083	001045
	.70	.012175	.000872	000761		.70	.012162	000826	000829
	.74	.010961	.000792	000698		.74	.010948	000745	000758
	.78	.009903	.000724	000640		.78	.009891	000678	000691
	.82	.008980	.000663	000588		.82	.008969	000620	000632
	.86	.008163	.000610	000540		.86	.008153	000569	000578
	.90	.007441	.000563	000497		.90	.007432	000523	000530
	.94	.006803	.000519	000458		.94	.006794	000482	000487
	.98	.006234	.000480	000423		.98	.006225	000445	000448
	1.02	.005724	.000444	000391		1.02	.005717	000412	000413
	1.04	.005489	.000428	000376		1.04	.005482	000397	000397
	1.10	.004856	.000384	000335		1.10	.004849	000356	000353

Table 4. Concluded

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ,\deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
120	0.20	0.069952	0.056236	0.064087	300	0.20	0.068251	0.040711	-0.061515
	.40	.023794	.027974	.016199		.40	.021740	.021562	017706
	.50	.016970	.020540	.010623		.50	.014959	.015821	011986
	.60	.012391	.016092	.007580		.60	.010806	.012234	008625
	.70	.009159	.013012	.005614		.70	.008022	.009792	006430
	.74	.008138	.012003	.005002		.74	.007168	.009018	005755
	.78	.007238	.011098	.004469		.78	.006421	.008329	005167
	.82	.006443	.010276	.003998		.82	.005769	.007713	004652
1	.86	.005742	.009527	.003583		.86	.005197	.007156	004197
	.90	.005124	.008841	.003214		.90	.004694	.006651	003796
İ	.94	.004577	.008212	.002886		.94	.004247	.006197	003441
	.98	.004095	.007633	.002593		.98	.003852	.005778	003124
	1.02	.003670	.007100	.002333		1.02	.003501	.005395	002841
	1.04	.003476	.006849	.002213		1.04	.003340	.005215	002711
	1.10	.002961	.006156	.001893		1.10	.002906	.004719	002361
150	0.20	0.017812	0.057633	0.121920	330	0.20	0.020389	0.043674	-0.107096
	.40	.002091	.034398	.041512		.40	000371	.025474	035990
	.50	.001824	.028312	.031578		.50	001049	.019842	025836
	.60	.000123	.024433	.025219		.60	001514	.016123	019475
	.70	001823	.021184	.020139		.70	001817	.013443	015113
	.74	002518	.019939	.018315		.74	001908	.012568	013727
	.78	003124	.018710	.016595		.78	001988	.011778	012496
	.82	003630	.017497	.014975		.82	002054	.011063	011400
	.86	004030	.016310	.013465		.86	002109	.010408	010415
	.90	004326	.015156	.012070		.90	002156	.009803	009526
1	.94	004526	.014046	.010790		.94	002201	.009229	008709
	.98	004640	.012989	.009626		.98	002230	.008701	007975
	1.02	004681	.011989	.008574		1.02	002255	.008200	007301
	1.04	004679	.011513	.008089		1.04	002261	.007963	006989
	1.10	004595	.010179	.006786		1.10	002267	.007286	006127

Table 5. Induced Velocity Perturbations of Ellipsoid Fuselage Computed at Inflow Measurement Plane $[r_m/R=0.8470;\,\alpha=-3.0^\circ]$

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
0	0.20	0.011207	0.000000	0.004913	180	0.20	0.007893	0.000000	0.015063
	.40	.011188	.000000	000409		.40	.004059	.000001	.018593
	.50	.010824	.000001	002970		.50	.001541	.000002	.019375
	.60	.010220	.000001	005421		.60	001206	.000001	.019159
	.70	.009379	.000001	007713		.70	003846	000001	.017770
	.74	.008973	.000001	008582		.74	004768	000001	.016887
	.78	.008530	.000001	009411		.78	005563	000001	.015839
	.82	.008044	.000002	010200		.82	006206	000001	.014671
	.86	.007518	.000002	010940		.86	006681	000001	.013429
	.90	.006949	.000002	011626		.90	006986	000001	.012160
	.94	.006341	.000002	012256		.94	007132	000001	.010899
	.98	.005693	.000002	012820		.98	007132	000001	.009693
	1.02	.005007	.000002	013314		1.02	007020	000001	.008571
	1.04	.004652	.000002	013533		1.04	006925	000001	.008046
	1.10	.003541	.000002	014062		1.10	006542	.000000	.006627
30	0.20	0.010864	0.001302	0.005293	210	0.20	0.008049	-0.003063	0.013638
	.40	.010314	.000651	.000642		.40	.004682	006331	.014164
	.50	.009688	000153	001201		.50	.002793	007432	.013306
	.60	.008889	001093	002642		.60	.000996	007959	.011868
	.70	.007954	002050	003684		.70	000514	007894	.010080
	.74	.007553	002415	003995		.74	001006	007725	.009327
	.78	.007139	002762	004250		.78	001428	007486	.008572
	.82	.006718	003086	004450		.82	001777	007195	.007832
	.86	.006290	003384	004600		.86	002054	006864	.007121
	.90	.005859	003655	004704		.90	002264	006508	.006447
	.94	.005427	003895	004765		.94	002414	006138	.005818
	.98	.004997	004103	004787		.98	002510	005760	.005234
	1.02	.004570	004279	004774		1.02	002562	005390	.004702
	1.04	.004359	004355	004755		1.04	002572	005207	.004453
	1.10	.003741	004529	004653		1.10	002553	004684	.003783

Table 5. Continued

ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
60	0.20	0.010068	0.002625	0.006380	240	0.20	0.008508	-0.004221	0.010754
	.40	.008680	.002372	.002585		.40	.005892	006513	.008298
	.50	.007800	.001743	.001321		.50	.004640	006695	.006812
	.60	.006907	.001070	.000458		.60	.003557	006445	.005451
	.70	.006049	.000465	000092		.70	.002675	005941	.004295
	.74	.005722	.000252	000246		.74	.002376	005701	.003893
	.78	.005406	.000058	000370		.78	.002107	005449	.003525
	.82	.005101	000118	000468		.82	.001867	005192	.003190
	.86	.004809	000275	000543		.86	.001653	004934	.002886
	.90	.004528	000412	000600		.90	.001463	004680	.002612
	.94	.004260	000533	000641		.94	.001295	004430	.002363
	.98	.004005	000637	000668		.98	.001147	004188	.002139
	1.02	.003762	000726	000685		1.02	.001018	003954	.001937
	1.04	.003645	000765	000690		1.04	.000959	003841	.001844
	1.10	.003313	000863	000694		1.10	.000804	003518	.001592
90	0.20	0.009211	0.003773	0.008177	270	0.20	0.009210	-0.003773	0.008176
	.40	.007192	.004541	.004823		.40	.007191	004540	.004822
	.50	.006189	.004216	.003532		.50	.006188	004215	.003531
	.60	.005282	.003728	.002560		.60	.005281	003727	.002559
	.70	.004496	.003207	.001852		.70	.004496	003206	.001852
	.74	.004216	.003004	.001628		.74	.004215	003004	.001627
	.78	.003952	.002809	.001431		.78	.003951	002809	.001431
	.82	.003705	.002622	.001259	}	.82	.003705	002622	.001259
	.86	.003475	.002445	.001109		.86	.003475	002445	.001108
	.90	.003262	.002278	.000977		.90	.003261	002278	.000977
	.94	.003063	.002122	.000862		.94	.003062	002122	.000862
	.98	.002877	.001975	.000761		.98	.002876	001974	.000760
	1.02	.002704	.001837	.000672		1.02	.002703	001837	.000672
	1.04	.002622	.001771	.000632		1.04	.002622	001771	.000631
	1.10	.002393	.001589	.000525		1.10	.002393	001588	.000525

Table 5. Concluded

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ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}	ψ , deg	r/r_m	u/V_{∞}	v/V_{∞}	w/V_{∞}
120	0.20	0.008508	0.004222	0.010754	300	0.20	0.010067	-0.002624	0.006380
	.40	.005892	.006515	.008300		.40	.008679	002372	.002585
İ	.50	.004641	.006696	.006813		.50	.007798	001743	.001321
	.60	.003557	.006445	.005452		.60	.006906	001070	.000458
	.70	.002675	.005942	.004296		.70	.006048	000465	000092
	.74	.002376	.005701	.003894		.74	.005721	000252	000246
	.78	.002107	.005450	.003526		.78	.005405	000058	000370
	.82	.001867	.005193	.003191		.82	.005101	.000118	000468
	.86	.001653	.004935	.002887		.86	.004808	.000275	000543
	.90	.001463	.004681	.002613		.90	.004527	.000412	000600
ĺ	.94	.001295	.004431	.002364		.94	.004259	.000533	000640
	.98	.001147	.004188	.002140		.98	.004004	.000637	000668
	1.02	.001018	.003955	.001937		1.02	.003761	.000726	000685
	1.04	.000959	.003841	.001844		1.04	.003645	.000765	000690
	1.10	.000804	.003518	.001592		1.10	.003313	.000863	000694
150	0.20	0.008049	0.003063	0.013638	330	0.20	0.010864	-0.001302	0.005293
	.40	.004682	.006331	.014165		.40	.010314	000651	.000642
	.50	.002792	.007433	.013308		.50	.009687	.000153	001201
	.60	.000997	.007959	.011871		.60	.008888	.001093	002641
	.70	000515	.007894	.010082		.70	.007953	.002050	003683
	.74	001007	.007725	.009329		.74	.007552	.002415	003994
	.78	001429	.007486	.008574		.78	.007138	.002762	004249
	.82	001778	.007195	.007834		.82	.006717	.003086	004449
	.86	002056	.006865	.007122		.86	.006289	.003384	004599
	.90	002265	.006508	.006449		.90	.005859	.003655	004703
	.94	002415	.006138	.005819		.94	.005427	.003895	004764
	.98	002511	.005761	.005235		.98	.004996	.004103	004786
	1.02	002562	.005390	.004703		1.02	.004570	.004278	004772
	1.04	002573	.005207	.004454		1.04	.004359	.004354	004754
	1.10	002553	.004684	.003784	L	1.10	.003741	.004529	004651

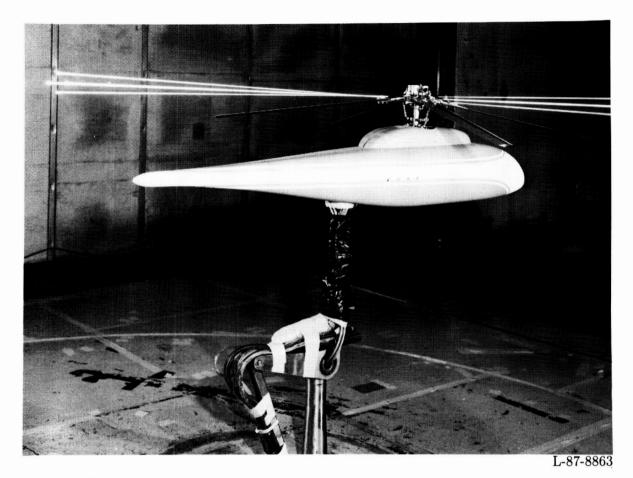


Figure 1. ROBIN fuselage in the Langley 14- by 22-Foot Subsonic Tunnel.

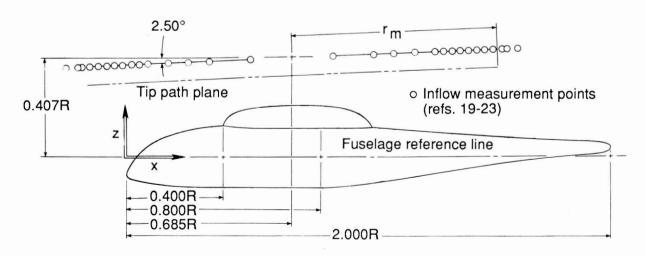


Figure 2. Fuselage coordinate system.

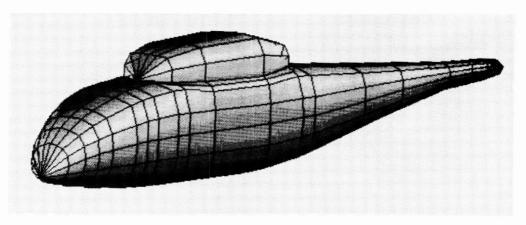


Figure 3. ROBIN fuselage with nacelle panel configuration.

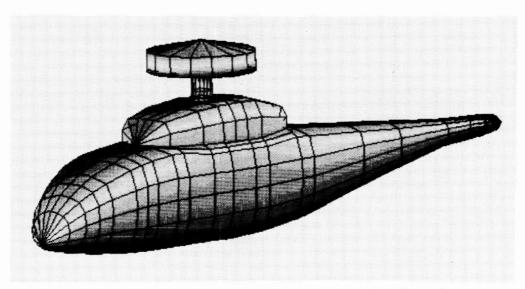


Figure 4. ROBIN fuselage with nacelle and hub panel configuration.

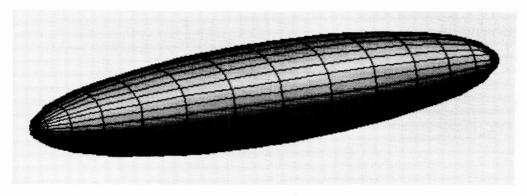
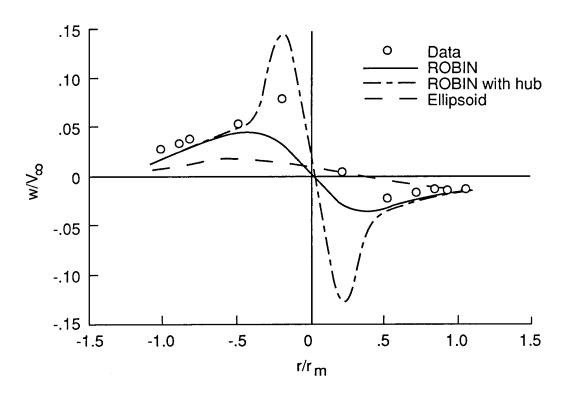
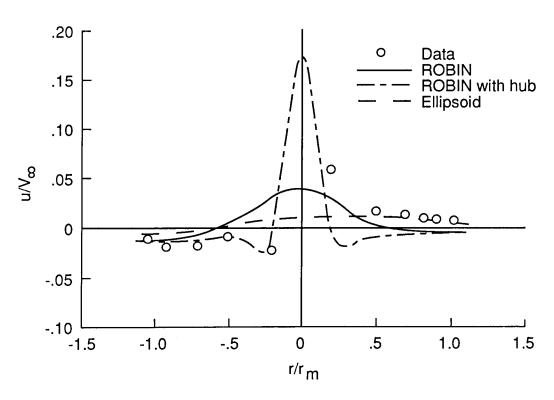


Figure 5. Ellipsoid fuselage panel configuration.

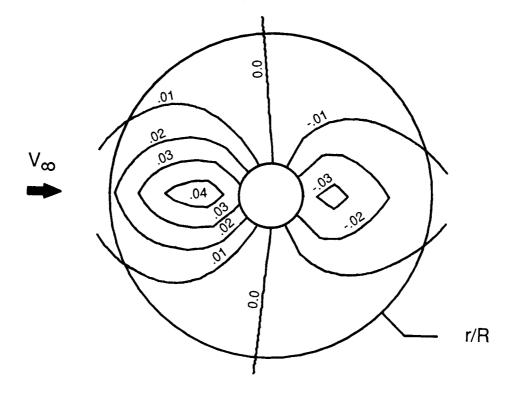


(a) Normal component.

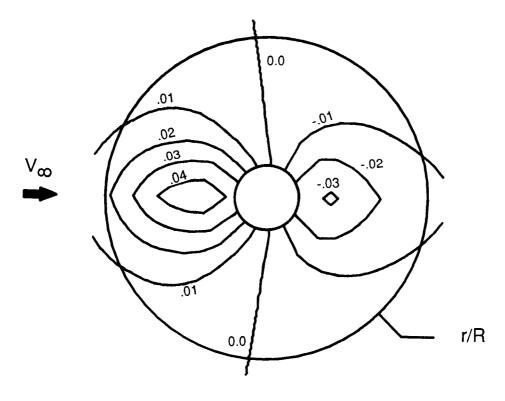


(b) Tangential component.

Figure 6. Velocity perturbations over fuselage centerline.

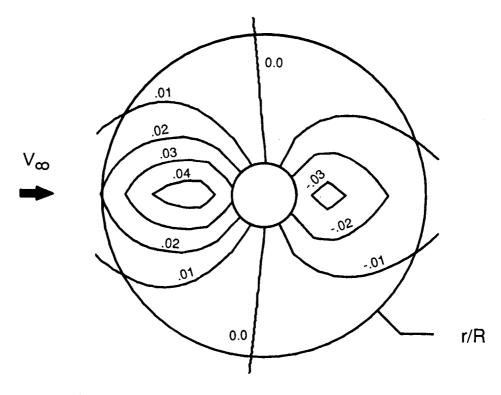


(a) $\alpha = -3.0^{\circ}$; $r_m/R = 0.8470$.



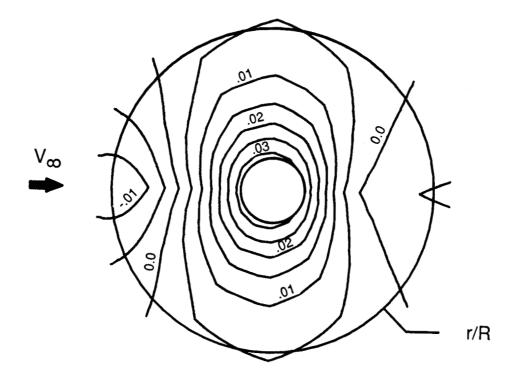
(b) $\alpha = -4.0^{\circ}$; $r_m/R = 0.8470$.

Figure 7. Normal velocity perturbations computed at inflow measurement plane.

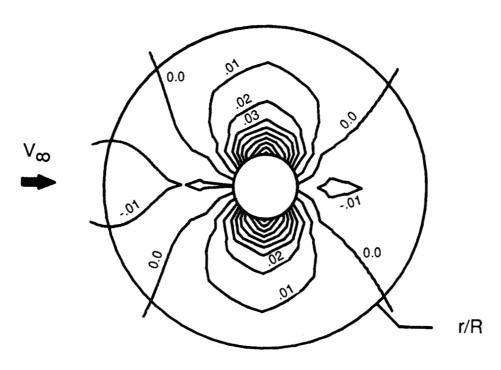


(c) $\alpha = -3.0^{\circ}$; $r_m/R = 0.8125$.

Figure 7. Concluded.



(a) u-component due to ROBIN fuselage-nacelle configuration.

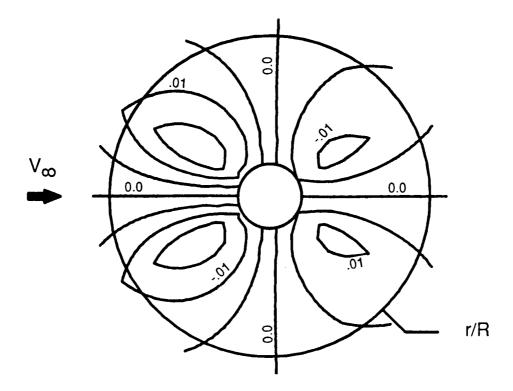


(b) u-component due to ROBIN and hub.

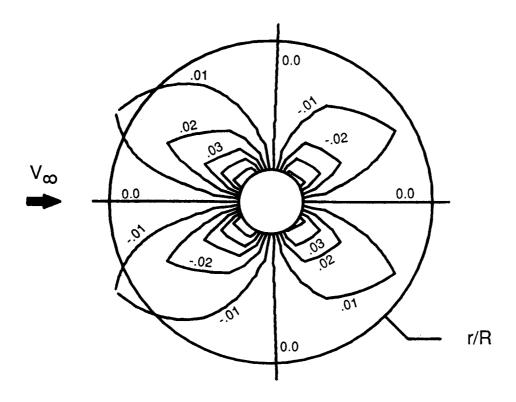
Figure 8. Downstream tangential perturbation velocities computed at inflow measurement plane for $\alpha=-3.0^{\circ}$ and $r_m/R=0.8470$.

V₈ 00⁸
(c) u-component due to ellipsoid.

Figure 8. Concluded.

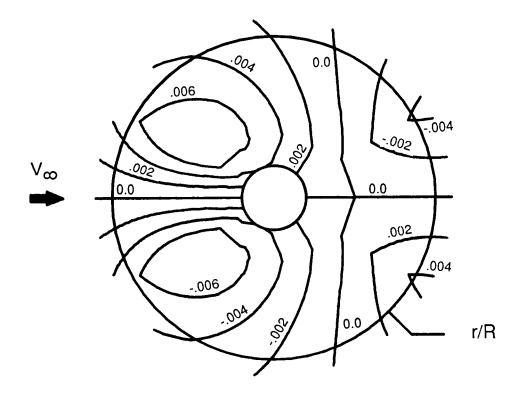


(a) v-component due to ROBIN fuselage-nacelle configuration.



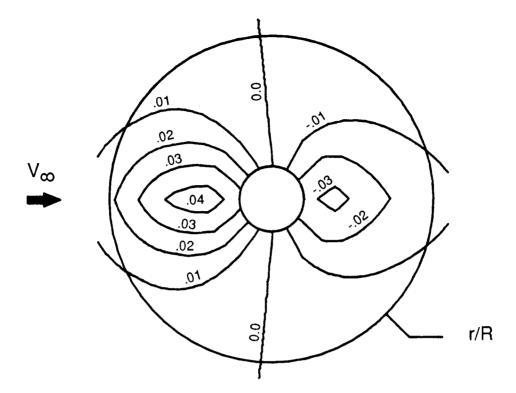
(b) v-component due to ROBIN and hub.

Figure 9. Lateral tangential perturbation velocities computed at inflow measurement plane for $\alpha=-3.0^{\circ}$ and $r_m/R=0.8470$.

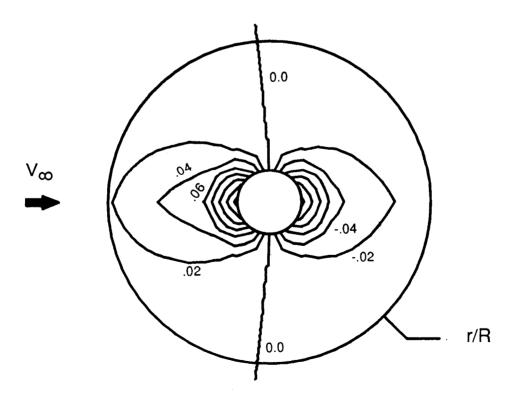


(c) v-component due to ellipsoid.

Figure 9. Concluded.

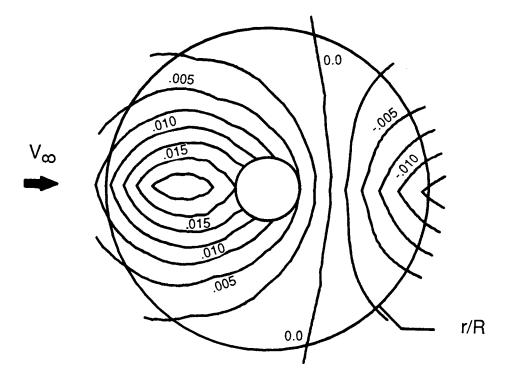


(a) w-component due to ROBIN fuselage-nacelle configuration. Map same as that of figure 7(a).



(b) w-component due to ROBIN and hub.

Figure 10. Normal perturbation velocities computed at inflow measurement plane for $\alpha=-3.0^\circ$ and $r_m/R=0.8470$.



(c) w-component due to ellipsoid.

Figure 10. Concluded.

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The velocity field of a representative helicopter fuselage in a free stream is computed. Perturbation velocities due to the fuselage are computed in a plane above the location of the helicopter rotor (rotor removed). The velocity perturbations computed by a source-panel model of the fuselage are compared with experimental measurements taken with a laser velocimeter. Three paneled fuselage models are studied: fuselage shape, fuselage shape with hub shape, and a body of revolution. The velocity perturbations computed for both fuselage shape models agree well with the measured velocity field except in the close vicinity of the rotor hub. In the hub region, without knowing the extent of separation, modeling of the effective source shape is difficult. The effects of the fuselage perturbations are not well-predicted with a simplified ellipsoid fuselage. The velocity perturbations due to the fuselage at the plane of the measurements have magnitudes of less than 8 percent of free-stream velocity. The velocity perturbations computed by the panel method are tabulated for the same locations at which previously reported rotor-inflow velocity measurements were made.						
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