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# Sensor Performance Analysis

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National Aeronautics and Space Administration Office of Management Scientific and Technical Information Division

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# **CONTENTS**

Liet	of Symbols
1.	INTRODUCTION
2.	POWER AND SIGNAL
3.	SPECTRAL RADIANCE
٥.	3.1 Visible and Shortwave (SWIR) Spectral Radiance
	3.2 Infrared Spectral Radiance
4.	DWELL TIME
т.	4.1 Spinning Mirror
	4.2 Rocking Mirror
	4.3 Linear Array
5.	NOISE
٥.	5.1 Visible and SWIR Noise
	5.1.1 Visible and SWIR Detector Noise Sources
	5.1.2 Visible and SWIR System Noise
	5.2 Infrared Noise
	5.2.1 Infrared Detector Noise
	5.2.2 Infrared System Noise
6.	FIGURES OF MERIT
0.	6.1 Noise Equivalent Delta Reflectance
	6.2 Noise Equivalent Delta Temperature
7.	MODULATION TRANSEER FUNCTION (MTF)
7.	7.1 Total MTF
	7.2 Component MTFs
	7.2.1 Optical Aperture MTF
	7.2.2 Detector Aperture MTF
	7.2.3 Satellite Motion MTF
	The state of the s
	7.2.5 Charge Transfer MTF
	REFERENCES
8.	PENDIX A-DETECTOR IRRADIANCE
API	PENDIX B-COMPUTED EARTH/ATMOSPHERE RADIANCES
API	PENDIX C-SENSOR FIELD OF VIEW (FOV)
API	PENDIX C—SENSOR FIELD OF VIEW (FOV) VIEWING A CIRCUI AR
API	PENDIX D-VIEW FACTOR FOR A SINGLE DETECTOR VIEWING A CIRCULAR
	BACKGROUND
API	PENDIX E-VIEW FACTOR FOR A DETECTOR IN AN N BY M ARRAY
	VIEWING A RECTANGULAR BACKGROUND
API	PENDIX F-COMPUTATION OF GAMMA
ADI	DENIDIV C. MOICE FOHIVALENT DELLA TEMPEKATUKE

# LIST OF SYMBOLS

A = Overlap factor across track, given by Equation (C-9) in Appendix C.

 $A_0$  = Sensor entrance aperture area (cm<sup>2</sup>).

 $A_D$  = Detector area (m<sup>2</sup>).

 $A_I$  = The area of the ground resolution element (km<sup>2</sup>), used in Equation (A-2).

 $A_{m}$  = A function used in the MTF<sub>OA</sub> computation, Equation (7-2).

B = Overlap factor along track, given by Equation (4-9).

 $B(\lambda)$  = Planck's spectral distribution of radiation (W/cm<sup>2</sup>-sr- $\mu$ m) from a blackbody, given by Equation (3-5).

 $B'(\lambda)$  = Planck's spectral distribution of radiation (p/sec-cm<sup>2</sup>-sr- $\mu$ m) from a blackbody, given by Equation (3-7).

 $B_{\rm m}$  = A function used in the MTF<sub>OA</sub> computation, Equation (7-2).

c = Speed of light =  $2.998 \times 10^{10}$  (cm/sec).

C = A constant used in Equation (2-8).

 $C_1$  =  $2\pi hc^2$  = A constant used in the computation of B( $\lambda$ ).

 $C_0$  = Output capacitance.

 $C_{\rm m}$  = A function used in the MTF<sub>OA</sub> computation, Equation (7-2).

 $C'_1$  =  $2\pi c = A$  constant used in the computation  $B'(\lambda)$ .

 $C_2$  =  $hc/k_B$  = A constant used in the computation of  $B(\lambda)$  and  $B'(\lambda)$ .

 $d_C$  = Distance covered cross track during the time required to map the Earth  $t_M$ , given by Equation (C-6).

D = Aperture diameter of the sensor, used in Equation (A-7).

D\* = Specific detectivity (laboratory or handbook value), defined in Equation (5-20).

 $D_{BLIP}^*$  = Background-limited value of  $D_{SLIP}^*$ , given by Equation (5-33).

d = Photodetector depletion region depth, used in Equation (7-19).

d<sub>m</sub> = Distance moved by the satellite along the ground track during one scan period, given by Equation (4-7).

d<sub>C</sub> = The extent imaged along the ground track at nadir during one scan mirror period,

- given by Equation (4-6).
- $d_S$  = Width of square detector ( $\mu$ m).
- $d\lambda$  = Differential of wavelength  $\lambda$ .
- E(λ) = Scene spectral irradiance (W/cm<sup>2</sup>-μm) into the detector, given by Equation (2-10).
- E'(λ) = Scene spectral irradiance (p/sec-m<sup>2</sup>-μm) into the detector, given by Equation (2-6).
- $E'_{BG}$  = The irradiance at the infrared detector from the scene and the background, given by Equation (5-25).
- $E_G$  = Silicon band gap (e-v) used in Equation (5-6a).
- F<sub>M</sub> = A factor used in Equation (4-5) to distinguish between a 45-degree scan mirror and a paddle scan mirror.
- $E_{\lambda 0}$  = Spectral irradiance (mw/cm<sup>2</sup>- $\mu$ m) of the direct sunlight above the atmosphere, used in Equation (B-2).
- $E_{\lambda s}$  = The solar irradiance (mw/cm<sup>2</sup>) of the direct sunlight at sea level, used in Equation (B-2).
- f = Focal length (cm), used in Equation (A-6).
- F<sub>A</sub> = View factor for a detector in an n by m array viewing a rectangular background, given by Equation (E-1), in Appendix E.
- $F_L$  = View factor of the detector in the laboratory where D\* was measured, given by Equation (5-19).
- $F_C$  = View factor for a cold shielded detector viewing the scene through a circular aperture, given by Equation (5-29).
- $f_N$  = The f-number (nd) of the optical system, given by Equation (A-9).
- g<sub>m</sub> = Transconductance.
- $J_0$  = Zeroth-order Bessel function, used in Equation (7-26).
- J<sub>DC</sub> = Dark current density (a/cm<sup>2</sup>), given by Equation (5-6a).
- H = Satellite height (km).
- h = Planck's constant =  $6.626 \times 10^{-34} \text{ (W-sec}^2\text{)}$ .
- k = Spatial frequency (cycles/mm).
- $k_0 = 1/2\lambda f_N$ , used in the MTF<sub>OA</sub> computations and given by Equation (7-12).

 $k_B$  = Boltzmann's constant = 1.380 × 10<sup>-23</sup> (W-sec/K).

 $k_C$  =  $2k_o$  = Cutoff frequency, used to compute MTF<sub>OA</sub> in Equation (7-13).

L = A function used in the  $MTF_{CT}$  and given by Equation (7-22).

 $L_0$  = Diffusion length, used in Equation (7-22).

 $L(\lambda)$  = Scene spectral radiance (W/cm<sup>2</sup>-sr- $\mu$ m), given by Appendix B for the visible bands and by Equation (3-2) for the infrared bands.

 $L'(\lambda)$  = Scene spectral radiance (p/sec-cm<sup>2</sup>-sr- $\mu$ m), given by Equation (2-12).

 $L_A^N$  = Spectral radiance (W/cm<sup>2</sup>-sr- $\mu$ m) from the atmosphere observed by the sensor when viewing along the nadir direction, used in Equation (B-4).

 $L^{N}$  = Total spectral radiance (W/cm<sup>2</sup>-sr- $\mu$ m) observed by the sensor when viewing along the nadir direction, given by Equation (B-4).

 $L_S$  = Spectral radiance (W/cm<sup>2</sup>-sr- $\mu$ m) observed by the sensor which comes from the surface of the Earth, used in Equation (B-4).

M = Mass of the Earth (kg).

 $M_{CT}$  = Total number of charge transfers, used in Equation (7-23).

 $M_g$  = Number of gate transfers.

MTF = Modulation transfer function, given by Equation (7-1).

 $MTF_{CT}$  = Charge transfer MTF, given by Equation (7-23).

 $MTF_{DA}$  = Detector aperture MTF, given by Equation (7-16).

 $MTF_{OA}$  = Optical aperture MTF, given by Equation (7-2).

MTF<sub>SI</sub> = Satellite jitter MTF, given by Equation (7-26).

 $MTF_{SM}$  = Satellite motion MTF, given by Equation (7-17).

m = Mass of the electron =  $9.1 \times 10^{-31}$  (kg).

 $m_p$  = Number of clock phases for readout, used in Equation (7-24).

 $m_S$  = Number of stages, detectors or picture elements, used in Equation (7-24).

 $N_{BT}$  = Bulk trap noise (e), given by Equation (5-3).

 $N_{CT}$  = Charge transfer noise (e), given by Equation (5-11).

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N_{DC} = Dark current noise (e), given by Equation (5-5).
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N<sub>DCS</sub> = Dark current noise (e) for a Schottky barrier detector, given by Equation (5-9).

 $N_{DET}$  = Detector noise (e), used in Equations (5-1) and (5-16).

NEE = Noise equivalent electrons (e), given by Equation (5-21).

NEP = Noise equivalent power (W), given by Equation (5-20).

NE $\Delta T$  = Noise equivalent delta temperature (K), given by Equation (6-5).

 $NE\Delta\rho$  = Noise equivalent delta reflectance (nd), given by Equation (6-1).

 $N_{M}$  = Multiplexer noise (e).

 $N_{OA}$  = Output amplifier noise (e), given by Equation (5-4).

 $N_{OD}$  = Other detector noise (e), given by Equation (5-17).

 $N_{OS}$  = Other system noise (e).

 $N_p$  = Photon noise (e), given by Equation (5-2) for the visible domain and by Equation (5-23) for the infrared domain.

 $N_{PL}$  = Photon noise (e) under laboratory conditions, given by Equation (5-18).

 $N_Q$  = Quantization noise (e), given by Equation (5-12) for the visible domain and by Equation (5-34) for the infrared domain.

 $N_T$  = Thermal (Johnson) noise (e), given by Equation (5-8).

 $N_{TOT}$  = Total noise from all sources (e), given by Equation (5-1).

 $N_{SYS}$  = System noise (e), used in Equation (5-1).

n = Size distribution function for aerosol particles, used in Equation (B-3).

 $n_D$  = Number of detectors per spectral band.

n'<sub>D</sub> = Number of detectors along an array, used to compute the charge transfer noise in Equation (5-11).

 $n_E$  = Number of resolution elements along a scan line, given by Equation (4-1).

 $n_f$  = Number of facets in a 45-degree scan mirror.

n<sub>p</sub> = The number of phases used to transfer charge along a detector array, used in Equation (5-11).

n<sub>S</sub> = A factor used in Equation (4-14) to distinguish between imaging in one scan mirror direction and imaging in both scan mirror directions.

 $n_{SS}$  = Density of surface states, used in Equation (5-3).

 $P_D$  = Detector pitch ( $\mu$ m).

Q = Number of bits used in the analog-to-digital converter.

q = Charge of an electron =  $1.602 \times 10^{-19}$  (Coul).

R = Resistance (ohms).

 $R(\lambda)$  = Detector current responsivity (A/W), given by Equation (2-3).

 $R_C$  =  $4\pi q \text{mk}^2/\text{h}^3$  = Richardson constant (a/cm<sup>2</sup>-K<sup>2</sup>), used in Equation (5-9a).

 $R_e$  = 6378.165 (km) = Radius of the Earth.

 $R_S$  = Distance (km) from the center of the Earth to the satellite, given by Equation (B-2).

r = Radius of aerosol particle, used in Equation (B-3).

S = Signal (A) from the detector, given by Equation (2-2).

 $S_F$  = Saturation factor, defined by Equation (5-14).

S' = Signal (e) from the detector, given by Equation (2-7).

 $S'_{SAT}$  = The saturation signal (e), given by Equation (5-13).

S<sub>d</sub> = Distance (km) from the satellite to the point on the Earth that corresponds to the maximum scan angle, given by Equation (C-3).

 $S_W$  = Swath width (km) on the Earth, given by Equation (C-5).

 $S_0$  = Percentage overlap along track, used in Equation (4-10).

 $S'_{O}$  = Percentage overlap across track, used in Equation (C-9).

T = Blackbody temperature (K).

 $T_{BG}$  = Background temperature for the sensor (K).

 $T_{BGL}$  = Background temperature (K) when D\* is measured in the laboratory.

 $T_S$  = Earth's surface temperature (K).

 $T_A$  = Earth's atmospheric temperature (K).

 $t_A$  = Active scan time, which is that part of the scan mirror period when data are being acquired, given by Equation (4-4).

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t<sub>I</sub> = Detector integration time (sec), given by Equation (2-8).
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- t<sub>D</sub> = Detector dwell time (sec), given by Equations (4-3) and (4-12) for a spinning scan mirror; Equations (4-14) and (4-17) for a rocking scan mirror; and by Equation (4-18) for a linear array.
- $t_{\rm M}$  = Period of the scan mirror (sec), given by Equation (4-11) for a spinning mirror and by Equation (4-16) for a rocking scan mirror.

 $t_{MAP}$  = Time to map the Earth (days).

t<sub>S</sub> = Satellite orbital period (sec), given by Equation (C-8).

 $V_{SUB}$  = The velocity (km/sec) of the subsatellite point, given by Equation (4-8).

 $V_I$  = Image velocity (km/sec), given by Equation (7-18).

z = A curve-fitted function used to compute the silicon absorption coefficient, given by Equation (7-21).

 $\alpha$  = Instantaneous angular field of view (r), given by Equation (4-2).

 $\alpha_a$  = Silicon absorption coefficient (nd), used in Equation (7-19).

 $\alpha_{M}$  = A material-dependent factor used in Equation (5-6a).

 $\beta$  =  $D_0/D$ , used in the MTF<sub>OA</sub> computations, given by Equation (7-15).

 $\gamma$  = (S/N) · NE $\Delta \rho$  and is given by Equation (6-2).

 $\gamma_{\rm o}$  = (S/N) · NE $\Delta \rho$  along nadir and is given by Equation (6-3).

 $\Delta f$  = Electrical bandwidth (Hz), given by Equation (5-22).

 $\Delta \lambda$  =  $\lambda_2 - \lambda_1$  = Spectral bandpass ( $\mu$ m).

 $\delta_A$  = Optical thickness (nd) of the aerosols, used in Equation (B-1).

 $\delta_G$  = Optical thickness (nd) of the absorbing gases, used in Equation (B-1).

 $\delta_R$  = Optical thickness (nd) due to Rayleigh scattering, used in Equation (B-1).

 $\delta_{\rm T}$  = Optical thickness (nd).

 $\delta_{TN}$  = Optical thickness (nd) in the nadir direction, used in Equations (6-4) and (B-1).

 $\eta$  = Detector quantum efficiency (nd).

 $\eta_{\rm M}$  = A material-dependent carrier recombination factor, used in Equation (5-6a).

 $\epsilon$  = Charge transfer inefficiency (nd), used to compute MTF<sub>CT</sub>.

 $\epsilon_{A}$  = Emissivity of the atmosphere (nd).

Field-of-view (FOV) angle (deg) subtended by the swath width at the satellite. It is given by Equation (4-8) for a linear array and by Appendix C [Equation (C-1)] for whiskbroom (scanning) systems.

 $\Theta_{M}$  = Maximum satellite angular movement (rad) used to compute jitter MTF in Equation (7-26).

 $\theta$  = Optics half-cone angle (deg), given by Equation (A-10).

 $\theta_{BG}$  = The full-cone angle (deg) of the background used in Equation (5-29).

 $\theta_{\rm z}$  = Solar zenith angle (deg), angle between Earth normal and Sun direction, used in Table B-2.

 $\kappa$  = Scan efficiency (nd), given by Equation (4-5) for spinning mirrors.

 $\pi$  = The well-known ratio between the circumference and the diameter of a circle, 3.14159 (nd).

 $\lambda$  = Center wavelength of a spectral band ( $\mu$ m).

 $\Lambda$  = k/k<sub>o</sub>, used in the MTF<sub>OA</sub> computations.

 $\lambda_1$  = Lower wavelength of a spectral band ( $\mu$ m).

 $\lambda_2$  = Upper wavelength of a spectral band ( $\mu$ m).

 $\mu$  = GM, the product of the gravitational constant G and the mass of the Earth M = 3.98603  $\times$  10<sup>5</sup> (km<sup>3</sup>-sec<sup>-2</sup>).

 $\rho$  = Reflectance of the Earth's surface (nd).

Transmittance (nd) of the atmosphere in the visible spectral region, given by Equation (B-2).

 $\tau'$  = Total number of electrons produced by an infrared detector from the scene and the background, given by Equation (5-24).

 $\tau_{\rm A}$  = Transmittance (nd) of the atmosphere, used for the infrared spectral region.

 $\tau_{\rm AN}$  = Optical transmittance (nd) along the nadir direction, given by Equation (6-4).

 $\tau_{\rm O}$  = Optical transmittance (nd) from the sensor entrance aperture to the detector, used in Equation (5-26).

- $\Phi$  = Power (W) incident on the detector, given by Equation (2-1).
- $\Phi'$  = Photon flux incident on the detector (p/sec).
- $\Phi_{S}$  = Angle (deg) subtended at the satellite by ground swath, given by Equation (C-4).
- $\phi_{\rm C}$  = Cone angle (deg) for detector view, used in Equation (5-19).
- $\phi_f$  = The angle between the normal to the differential area  $dA_B$  and the line between the center of the detector and the center of the area  $dA_B$ , used in Appendix F.
- $\phi_{\rm m}$  = A function that when multiplied by the charge of an electron q, gives the work function of the metal in the semiconductor. It is used in Equation (5-9a).
- $\phi'$  = The angle (deg) between the line of sight and the surface normal, used in Equation (6-2).
- $\psi$  = A function used in the MTF<sub>OA</sub> computation, given by Equation (7-10).
- $\Omega$  = The effective solid angle (sr) through which the detector receives energy from the resolution element, given by Equation (5-27).
- $\Omega_{\rm o}$  = Effective solid angle (sr) subtended by the entrance aperture at the subsatellite point, used in Equation (A-7).
- $\Omega_{BG}$  = Effective solid angle (sr) of the background, given by Equation (5-28).

# 1. INTRODUCTION

The purpose of this paper is to present an analytic model of an imaging sensor system so that: (1) sensor performance predictions can be made; (2) design tradeoffs and sensitivity analyses can be rapidly performed; and (3) insight into various aspects of imaging sensor performance can be obtained. The model is applicable to image sensors which operate from the visible through the thermal infrared spectral regions.

The design of sensors for remote observation of the Earth from polar orbiting satellites takes about a decade and occurs in five different stages. These stages are:

- Definition of Scientific Requirements. During this stage, scientific working groups formulate the scientific requirements (e.g., spatial, temporal, and spectral resolution; measurement accuracy, etc.)
- Preliminary Design. During this stage a "paper design" is developed. (Determination is made of such parameters as f-number, detector size, and number of detectors) that permit the sensor to meet the scientific requirements (e.g., signal-to-noise ratio, noise-equivalent delta temperature, or noise-equivalent delta reflectance).
- Feasibility Studies (Phase B). During this stage, engineering feasibility is established without regard to optimization of the design.
- Design Studies (Phase B). During this phase, the design is optimized, and an in-depth analysis is performed on each subsystem (e.g., optics, focal plane, cooler, electronics, mechanical systems) and a credible cost estimate is produced.
- Flight Hardware Design, Development, Test and Integration into the Space Platform

  (Phase C/D). During this stage, flight hardware is designed, developed, and tested to prove that it meets the specification, and is integrated into the space platform.

Only Preliminary Design (the second stage) is addressed in this document. Derivations or references are given for all the equations to make it easy to change the theory as required in future applications.

The spectral range is limited to 0.4 to 15.0  $\mu m$  which is generally appropriate for studies of the Earth

and its environment. The types of scanners include the "pushbroom" and two different kinds of "whiskbrooms." A substantial portion of the analysis presented herein has been incorporated into a self-documented Lotus 1-2-3 spreadsheet.

Analytic (as opposed to statistical) methods are used in the model. Analyses are carried out at very low spatial (and therefore temporal) frequencies in order to simplify the computations. High spatial frequencies are used only to determine the MTF of the sensor. Carrying out the analyses at low spatial frequencies also avoids the necessity of working in the frequency domain which generally involves fourier transformations or convolutions in the time domain, and would therefore make the sensor model very complex. To further simplify the analyses, it is also assumed that the sensors have narrow spectral bandwidths so that those parameters that are spectrally dependent (e.g., detector responsivity) can be reduced to a constant.

The model assumes that the sensor is a linear system from the optical input through the electronic signal processing. This assumption is satisfied if (1) the optical system is not dominated by diffraction effects; (2) incoherent detection methods are employed; (3) the various noise sources are additive in an rss sense; (4) the imaging process is spatially invariant; and (5) the electronic signal processing constitute linear operations. These assumptions are all valid for the types of imaging sensors that the model is presently being applied to.

Appropriate scene radiance levels must be assigned in order to assess sensor system performance. In the model described in this document, tables are included which allow a user to determine radiances at the top of the Earth-atmosphere system as a function of wavelength. These tables apply to the visible and near ir spectral regions. The origin of the tables is discussed in Appendix B. For the thermal infrared region, radiances are directly computed.

Section 2 addresses the power incident on the detector during an observation interval and the signal coming out the detector. These are written as functions of the irradiance at the detector and as a function of the scene radiance.

Section 3 provides a description of the model used for the scene radiance.

Section 4 derives the equations for detector dwell time for four different scanning configurations which include: a spinning 45-degree scan mirror, a spinning paddle mirror, a rocking scan mirror, and a linear array-pushbroom.

Section 5 is devoted to the major noise sources associated with visible and infrared detectors.

Section 6 presents definitions and derivations of various "figures of merit" including Noise Equivalent Delta Reflectance (NE $\Delta\rho$ ) and Noise Equivalent Delta Temperature (NE $\Delta T$ ).

Section 7 develops the Modulation Transfer Function (MTF) for the optical aperture, the detector aperture, satellite motion, charge diffusion, charge transfer, and satellite jitter.

The Appendixes treat many of the equations in a tutorial manner.

#### 2. **POWER AND SIGNAL**

When viewing the scene, the power (flux) into the detector is given by

$$\Phi = A_{\rm D} \begin{cases} \lambda_2 \\ E(\lambda) \ d\lambda \end{cases} [W], \tag{2-1}$$

where  $A_D$  = the area of the detector (cm<sup>2</sup>);  $E(\lambda)$  = scene spectral irradiance at the detector (W/cm<sup>2</sup>- $\mu$ m);

 $\lambda$  = center wavelength of spectral band ( $\mu$ m); and

 $\Delta \lambda = \lambda_2 - \lambda_1 = \text{spectral bandpass } (\mu \text{m}).$ 

The signal out of the detector is given by

$$S = A_{D} \begin{cases} \lambda_{2} \\ E(\lambda)R(\lambda) d\lambda \end{cases}$$
 [A], (2-2)

where  $R(\lambda)$  is the detector current responsivity and is given by

$$R(\lambda) = \frac{q\eta}{hc} \lambda \qquad [A/W], \qquad (2-3)$$

the charge of an electron =  $1.60 \times 10^{-19}$  [coul]; where q

the detector quantum efficiency [nd] (assumed to be constant over the spectral η bandpass  $\Delta \lambda$ );

Planck's constant =  $6.63 \times 10^{-34} \text{ [Wsec}^2\text{]}$ ; and

the speed of light =  $3.00 \times 10^{10}$  [cm/sec]. c

Substituting Equation (2-3) into Equation (2-2) gives

$$S = \frac{A_D q \eta}{hc} \begin{cases} \lambda_2 \\ E(\lambda) \lambda \ d\lambda \end{cases} \qquad [A]. \tag{2-4}$$

Equation (2-4) may be written in terms of the spectral photon irradiance as

$$S = A_D q \eta \begin{cases} \lambda_2 \\ E'(\lambda) d\lambda \end{cases} [A], \qquad (2-5)$$

where the scene spectral photon irradiance  $E'(\lambda)$  at the detector is given by

$$E'(\lambda) = \frac{\lambda}{hc} \quad E(\lambda) \qquad [p/sec-cm^2 - \mu m] . \qquad (2-6)$$

The signal out of the detector is given by

$$S' = \frac{t_I}{q} \quad S \qquad [e], \tag{2-7}$$

where the integration time t<sub>I</sub> is given by

$$t_{I} = Ct_{D} \qquad [sec], \tag{2-8}$$

where C is an input constant and  $t_D$  is the sensor dwell time, which is described in detail in Section 4.

Substituting Equation (2-5) into Equation (2-7) gives

$$S' = t_{I} A_{D} \eta \begin{cases} \lambda_{2} \\ E'(\lambda) d\lambda \quad [e] . \end{cases}$$
 (2-9)

The scene spectral irradiance at the detector is related to the scene spectral radiance by the following two equations given in terms of watts and photons, respectively. (See Appendix A.) The first equation is

$$E(\lambda) = \frac{\tau_0 \pi}{4f^2_N} L(\lambda) \qquad [W/cm^2 - \mu m], \qquad (2-10)$$

where  $\tau_{\rm o}$  = the optical transmittance [nd] from the sensor aperture to the detector, and

 $f_N = f$ -number of the optics [nd].

The second equation is

E' 
$$(\lambda) = \frac{\tau_0 \pi}{4f^2_N} L'(\lambda)$$
 [p/sec-cm<sup>2</sup>-\mu m]. (2-11)

Also, for completeness, note that

$$L'(\lambda) = \frac{\lambda}{hc} L(\lambda) \qquad [p/cm^2 - sec - sr - \mu m] . \qquad (2-12)$$

For the visible and shortwave infrared (SWIR) wavelengths, it is assumed that the spectral bandpass  $\Delta\lambda$  is small and that the scene spectral photon irradiance  $E'(\lambda)$  varies slowly over  $\Delta\lambda$ . In this case, the integration in Equations (2-1) and (2-4) can then be approximated by  $E'\Delta\lambda$ , where E' is the average value of  $E(\lambda)$  over the spectral bandpass  $\Delta\lambda$ .

# 3. SPECTRAL RADIANCE

In this section, we will show how to obtain the spectral radiance for the visible and SWIR spectral wavelengths (0.4 to 2.2  $\mu$ m) and the infrared spectral wavelengths (2.2 to 15  $\mu$ m).

# 3.1 Visible and Shortwave Infrared (SWIR) Spectral Radiance

A table of values of the scene spectral radiance at the sensor aperture is given in Appendix B as a function of  $\rho$ ,  $\theta_z$ , and  $\lambda$ 

where  $\rho$  = Earth's surface reflectance (nd), and

 $\theta_z$  = solar zenith angle (deg).

The scene spectral radiance  $L(\lambda)$  is obtained from the tables by trilinear interpolation at the desired values of  $\rho$ ,  $\theta_z$ , and  $\lambda$ . Although the values of scene spectral radiance in the tables were computed for a nadir viewing sensor, we assume that the values are independent of viewing angle. (See Equation C-4).

# 3.2 Infrared Spectral Radiance

The total scene spectral radiance in the infrared is given by

$$L(\lambda) = \tau_{A} B(\lambda, T_{S}) + \epsilon_{A} B(\lambda, T_{A}) [W/cm^{2}-sr-\mu m]$$
(3-2)

where  $\tau_A$  is the atmospheric transmittance for an optical depth  $\delta$ , given by

$$\tau_{\mathbf{A}} = \mathrm{e}^{-\delta} \tag{3-3}$$

and where  $\epsilon_{A}$  is the atmospheric emissivity given by

$$\epsilon_{\mathbf{A}} = 1 - \tau_{\mathbf{A}} \tag{3-4}$$

The quantities  $B(\lambda, T_S)$  and  $B(\lambda, T_A)$  are the spectral radiances of the Earth's surface at temperature  $T_S$  and the atmosphere at temperature  $T_A$ , respectively, and are given by Planck's equation (Hudson, 1969, p. 35) for a blackbody at temperature  $T_S$ 

$$B(\lambda,T) = \frac{C_1}{\pi \lambda^5} \frac{1}{\exp\left(\frac{C_2}{\lambda T}\right) - 1} [w/cm^2 - sr - \mu m]$$
 (3-5)

where Hudson's equation (2-8) has been divided by  $\pi$  to convert to radiance, and where

$$C_1 = 2\pi hc^2 = 3.74 \times 10^4 [W-\mu m^4/cm^2];$$

h = Planck's constant = 
$$6.63 \times 10^{-34} \text{ [W-sec}^2\text{]};$$

c = speed of light = 
$$2.998 \times 10^{10}$$
 [cm/sec];

$$C_2 = hc/k_B = 1.44 \times 10^4 [\mu m-K];$$

$$k_B$$
 = Boltzmann's constant = 1.38 × 10<sup>-23</sup> [W-sec/K]; and

T = Blackbody temperature [K].

The total scene spectral photon radiance is given by

$$L'(\lambda) = \tau_A B'(\lambda, T_S) + \epsilon_A B'(\lambda, T_A) \qquad [p/sec-cm^2-sr-\mu m], \qquad (3-6)$$

where the surface spectral photon radiance  $B'(\lambda, T_S)$  and the atmospheric spectral photon radiance  $B'(\lambda, T_A)$  are found by evaluating the following equation (Hudson, 1969, p. 38) at  $T_S$  and  $T_A$ , respectively:

$$B'(\lambda,T) = \frac{C'_1}{\pi \lambda^4} \frac{1}{\left(\exp\left(\frac{C_2}{\lambda T}\right) - 1\right)} [p/\sec-cm^2-sr-\mu m]$$
 (3-7)

where

$$C'_1 = 2\pi c = 1.88 \times 10^{23} \text{ [p-sec}^{-1}\text{-cm}^{-2}\text{-}\mu\text{m}^3\text{]}$$

# 4. DWELL TIME

As the satellite moves in orbit, it images along scan lines perpendicular to the ground track. Let the extreme ends of the scan lines on the Earth subtend an angle  $\Theta$  at the satellite. This angle is called the field-of-view (FOV). See Figure 1 for an illustration of the geometry involved and refer to Appendix C for a discussion of the relations between the parameters shown in the figure. The number of angular resolution elements  $n_E$  is given by

$$n_{\rm E} = \frac{\Theta}{\alpha} \text{ [nd]}$$

and (as can be seen from Figure 1) the instantaneous angular field of view  $\alpha$  (geometric only) is given by

$$\alpha = \frac{d_S}{f} \quad [rad] \tag{4-2}$$

where  $d_S$  = detector width (mm), and

f = focal length of the optical system (mm).

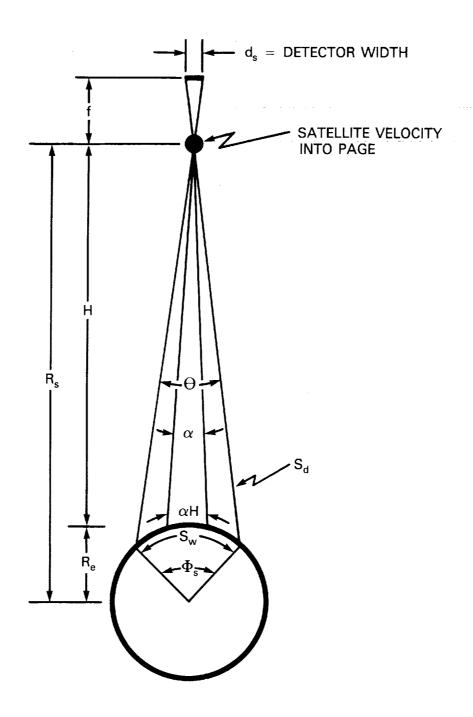
A scan line can be formed by a spinning mirror, a rocking mirror, or a linear array. Each of these are discussed in the following sections.

# 4.1 Spinning Mirror

Two types of spinning mirrors are discussed in this section: the 45-degree scan (faceted) mirror and the paddle scan mirror (Figures 2a and 2b). The axis of rotation for a 45-degree scan mirror is parallel to the sensor's optical axis, and a change in the angle of rotation of  $\theta$  will produce an equal change in the line-of-sight angle. The axis of rotation for a paddle scan mirror is perpendicular to the sensor's optical axis, and therefore, a change in the angle of rotation of  $\theta$  will result in a  $2\theta$  change in the line-of-sight angle.

The dwell time for a spinning mirror is given by

$$t_{D} = \frac{t_{A}}{n_{E}n_{f}} [sec], \qquad (4-3)$$



 $d_s$  = Width of square detector ( $\mu$ m)

f = Focal length (cm)

H = Satellite height (km)

 $R_e = Radius of Earth (km)$   $R_s = Earth-to-satellite distance (km)$ 

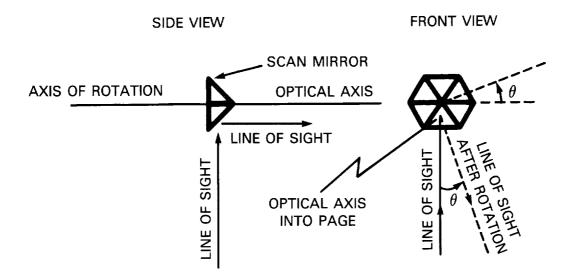
 $S_d$  = Maximum scan angle distance (km)  $\alpha$  = Instantaneous angular FOV (deg)

 $\Theta$  = Swath width FOV (deg)

 $\Phi_{\text{s}} = \text{ Ground swath angle (deg)}$ 

 $S_w = Swath width (km)$ 

Figure 1. FOV and IFOV Geometry



\*NOTE: AS MIRROR ROTATES THROUGH AN ANGLE  $\theta$  THE LINE OF SIGHT ALSO ROTATES THROUGH AN ANGLE  $\theta$ 

Figure 2a. Scan Mirror Geometry for 45-Degree Faceted Scan Mirror

PADDLE SCAN FLAT MIRROR

# AXIS OF ROTATION INTO THE PAGE LHS OF ROTATION OPTICAL AXIS 2 0

\*NOTE: AS THE MIRROR ROTATES THROUGH AN ANGLE  $\theta$  THE LINE OF SIGHT ROTATES THROUGH AN ANGLE  $2\theta$ 

Figure 2b. Scan Mirror Geometry for Paddle Scan Flat Mirror

where  $n_f =$  the number of facets,

$$n_f \geqslant 1$$
 for a 45-degree scan mirror, and  $n_f \geqslant 1$  for a paddle scan mirror.

The active scan time t<sub>A</sub>, which is that part of the scan mirror period during which data are acquired, is given by

$$t_{A} = \kappa t_{M} \quad [sec], \tag{4-4}$$

where the scan mirror period  $t_M$  is the time for the spinning scan mirror to make a complete revolution, and the scan efficiency  $\kappa$  is given by

$$\kappa = \frac{n_f \Theta}{2\pi F_M} \quad [nd], \tag{4-5}$$

where  $F_M = 1$  for a 45-degree scan mirror,  $F_M = 2$  for a paddle scan mirror.

During each scan, an area on the ground is imaged. The extent imaged along the ground track at nadir (Figures 3 and 4) is

$$d_{C} = n_{f} n_{D} \alpha H \quad [km], \qquad (4-6)$$

where H =the satellite height [km], and

 $n_D^{-1}$  = the number of detectors per spectral band.

Also, during each scan, the satellite moves a distance d<sub>m</sub> measured along the ground track, which is given by

$$d_{m} = t_{M}V_{SUB} \quad [km], \qquad (4-7)$$

where V<sub>SUB</sub> is the speed of the subsatellite point along the ground track and is given by

$$V_{SUB} = R_e \frac{(\mu)^{1/2}}{(R_e + H)^{3/2}}$$
, (4-8)

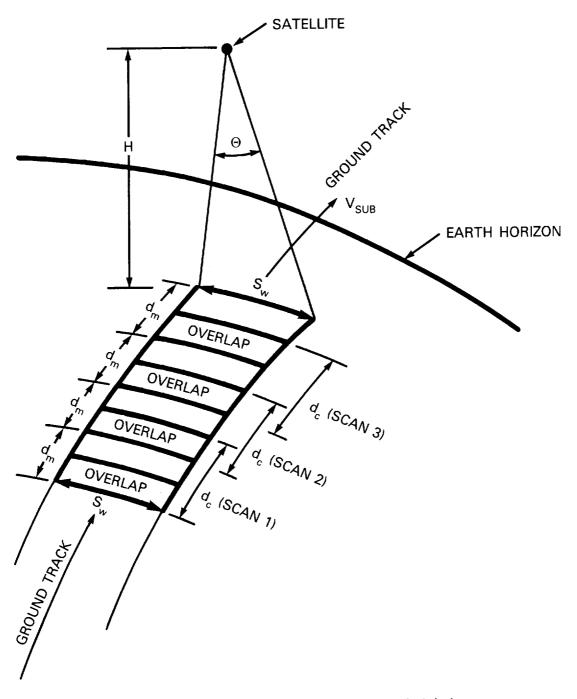
where

$$\mu = GM = 3.98603 \times 10^5 \text{ (km}^3\text{-sec}^{-2}\text{)}$$

where G is the universal gravitational constant, and M is the mass of the Earth.

The overlap factor B is given by

$$B = \frac{d_C}{d_m} \quad [nd], \tag{4-9}$$



= Ground distance moved per scan period (m)

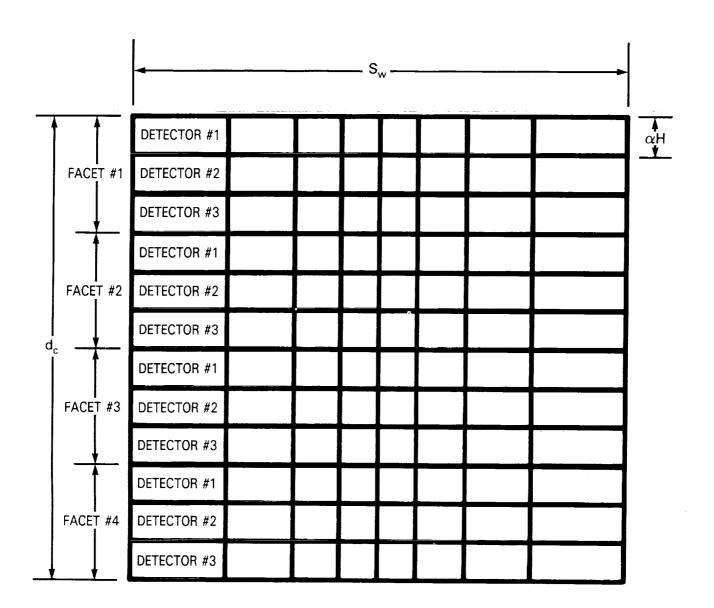
= Extent imaged along ground track per scan period (m)

 $\begin{matrix}\mathsf{d_m}\\\mathsf{d_c}\\\Theta\end{matrix}$ = Swath width FOV (deg) = Satellite height (km) Н

= Swath width

= Subsatellite velocity (km/sec)

Figure 3. Ground Track and Scanning Geometry



 $n_f = 4$  = Number of facets on scan mirror

 $n_D = 3$  = Number of detectors per spectral band

H = Satellite height (km)

 $S_w = Swath width (km)$ 

 $\alpha$  = Instantaneous angular FOV (as in Fig. 1) (deg)

 $d_c$  = Extent imaged along ground track per scan (m)

Figure 4. Example of Scanning Geometry for a 45-Degree Faceted Scan Mirror

where B = 1 for contiguous coverage, B > 1 for overlap, and B < 1 for incomplete coverage (underlap). In terms of the percentage of overlap  $S_0$  we may write

$$B = 1 + \frac{S_0}{100} \quad [nd] \quad . \tag{4-10}$$

Using Equations (4-7), (4-9), and (4-6), one obtains

$$t_{\rm M} = \frac{n_{\rm f} n_{\rm D} \alpha H}{B V_{\rm SUB}} \quad [\rm sec] \quad . \tag{4-11}$$

However, from Equations (4-1), (4-3), (4-4), and (4-5),  $t_D$  may be written as

$$t_{D} = \frac{\alpha}{2\pi F_{M}} t_{M} \quad [sec] . \tag{4-12}$$

From Equation (4-12) it can be seen that  $t_D$  is independent of the field of view  $\Theta$ , and therefore, changing the swath width does not change the dwell time. Substituting Equation (4-11) into (4-12) yields

$$t_{\rm D} = \frac{\alpha}{2\pi} \frac{n_{\rm f} n_{\rm D} \alpha H}{B V_{\rm SUB} F_{\rm M}} [\text{sec}] . \tag{4-13}$$

# 4.2 Rocking Mirror

During a complete cycle, the rocking mirror rotates back and forth through an angle that covers the  $FOV \Theta$  twice—once in each direction. For this case, the dwell time is

$$t_{\rm D} = \frac{t_{\rm A}}{n_{\rm S} n_{\rm E}} \quad [\text{sec}] \tag{4-14}$$

where  $n_S = 1$ , for imaging in the forward scan direction only, and

 $n_S$  = 2, for imaging in both directions.

The active scan time  $t_A$  is given by Equation (4-4). However, in this case, the scan efficiency  $\kappa$  depends on the sensor design parameters; e.g., mirror turnaround time, value of  $n_S$ , and mirror inertia. The scan period  $T_M$  in this case is the time for the rocking mirror to do a forward scan and retrace to its initial position.

During each scan period an area on the ground is imaged. The extent imaged along the ground track at nadir (Figure 3) is

$$d_{C} = n_{S} n_{D} \alpha H [km] . \qquad (4-15)$$

Use of Equations (4-7), (4-9), and (4-15) results in

$$t_{\rm M} = \frac{n_{\rm S} n_{\rm D} \alpha H}{B V_{\rm SUB}} \quad [\text{sec}] \quad . \tag{4-16}$$

Using Equations (4-4), (4-14), and (4-16) gives

$$t_{\rm D} = \frac{\kappa n_{\rm D} \alpha H}{n_{\rm E} B V_{\rm SUB}} \quad [\text{sec}] . \tag{4-17}$$

# 4.3 Linear Array

In this case, no scan mirror is used, and the number of angular resolution elements  $n_E$  is equal to the number of detectors in the cross-track direction. The dwell time for a linear array is, therefore,

$$t_{D} = \frac{\alpha H}{V_{SUB}} \quad [sec], \tag{4-18}$$

and the field of view  $\Theta$  is given by

$$\Theta = n_{E} \alpha \quad [rad] \quad . \tag{4-19}$$

# 5. NOISE

The total sensor noise is composed of detector noise and system noise. The detector noise is composed of a number of different noises that depend on the material composition of the detector and whether it is a single detector or is used in an array.

The total sensor noise is given by

$$N_{TOT} = \left(N^2_{DET} + N^2_{SYS}\right)^{1/2}$$
, (5-1)

where  $N_{DET}$  = root-mean-square detector noise, and

 $N_{SYS}$  = root-mean-square system noise.

The following sections present a discussion of these various noise sources.

# 5.1 Visible and SWIR Detector Noise

Here we will describe the various types of noise encountered in visible and SWIR detectors.

# 5.1.1 Visible and SWIR Detector Noise Sources

## 5.1.1.1 Photon Noise

Photon noise or shot noise is due to the random arrival of photons at the detector. Because the incident photon flux follows a Poisson distribution, the photon noise is given by (Levi, 1968, p. 153)

$$N_{\rm P} = (S')^{1/2} [e] ,$$
 (5-2)

where the signal S' is the mean number of electrons produced by the photons arriving at the detector and is given by Equation (2-9).

# 5.1.1.2 Bulk Trap Noise

Bulk trap noise occurs in CCD focal plane arrays and arises from the random trapping and emission from interface or bulk states (Dereniak, 1984, p. 243) and is given by

$$N_{BT} = \left(M_g k_B T A_D n_{SS} \ln 2\right)^{1/2} [e],$$
 (5-3)

where  $M_g$  = the number of gate transfers;

n<sub>SS</sub> = the density of surface states;

 $A_D$  = the detector area;

 $k_{\mathbf{R}}$  = Boltzmann's constant; and

T = Temperature [K].

Typical values of N<sub>BT</sub> are:

- Surface Channel CCD-1000 electrons
- Buried Channel CCD-100 electrons.

# 5.1.1.3 Output Amplifier Noise

The output amplifier noise is associated with the amplifier that buffers the signal from the focal plane and is generally a metal oxide semiconductor field effect transistor (MOSFET) of a given transconductance. An expression that can be used to compute this noise is (Dereniak, 1984, p. 244)

$$N_{OA} = \left(\frac{8C_o^2 k_B T \Delta f}{3q^2 g_m}\right)^{1/2} [e],$$
 (5-4)

where  $C_0$  = the output capacitance [ $\mu$ farad];

 $\Delta f$  = the electrical bandwidth [Hz];

 $g_{m}$  = the transconductance of the MOSFET [mhos];

q = the charge of an electron [coul]; and

k<sub>B</sub> = Boltzmann's constant.

# 5.1.1.4 Dark Current Noise

Dark current or thermal generation noise is associated with charge carriers that are thermally generated to bring the CCD potential well into thermal equilibrium. Dark current root-mean-square (rms) noise is given by (Honeywell, 1986, p. 5-26)

$$N_{DC} = \left(\frac{2J_{DC}A_{D}t_{I}}{q}\right)^{1/2} \quad [e], \tag{5-5}$$

where  $J_{DC} = dark$  current density at temperature T [a/cm<sup>2</sup>];

 $A_D = detector area [cm<sup>2</sup>];$ 

 $t_I$  = integration time [sec]; and

q = electron charge [coul].

The dark current density  $J_{DC}$  is given by

$$J_{DC} = \alpha_{M} T^{3} \exp \left(-\frac{qE_{g}}{\eta_{M} k_{B} T}\right)$$
 (5-6a)

where  $E_g$  = silicon band gap = 1.12 eV;

 $k_{\rm B}$  = Boltzmann's constant = 8.62 × 10<sup>-5</sup> [eV/K];

T = temperature [K];

 $\eta_{\rm M}$  = a material-dependent carrier recombination factor; for silicon  $\eta_{\rm M}$  = 2; and

 $\alpha_{\rm M}$  = a material-dependent factor, typically  $\alpha_{\rm M}$  = 1.1 × 10<sup>-6</sup> [A/cm<sup>3</sup>-K<sup>3</sup>]

# 5.1.1.5 Johnson (Thermal) Noise

The thermal motion of electrons in a resistor gives rise to voltage fluctuations across the resistor leads. These fluctuations are known as Johnson or thermal noise. The noise current is given by (Dereniak, 1984, p. 39)

$$i_{rms} = \left(\frac{4k_B T \Delta f}{R}\right)^{1/2} \quad [A], \tag{5-7}$$

where  $\Delta f$  = the effective bandwidth of the circuit [Hz] and

 $R = the resistance [\Omega].$ 

It follows that the noise in electrons is given by

$$N_{\rm T} = \frac{t_{\rm I}}{R} \left( \frac{4k_{\rm B}T \Delta f}{q} \right)^{1/2} \quad [e] \quad . \tag{5-8}$$

# 5.1.1.6 Schottky Noise

Electrons in the semiconductor of an M-S (metal-semiconductor) junction may overcome the potential barrier to reach the metal and produce a noise current. The noise current is called Schottky barrier noise and is given by (Yang, 1978, p. 130)

$$I_o = A_D R_C T^2 \exp\left(-\frac{q\phi_m}{k_B T}\right) [A], \qquad (5-9a)$$

where  $R_C = 4\pi qmk^2/h^3 = Richardson's constant = 120 [A/cm^2-k^2];$ 

 $A_D$  = detector area [cm];

 $q\phi_m$  = work function = 0.0354 [eV], for PdSi:Si diodes;

 $k_B$  = Boltzmann's constant = 8.62 × 10<sup>-5</sup> [eV/K];

T = temperature [K]; and

q = electron charge [coul].

The Schottky noise current can be converted to electrons and is given by

$$N_{DCS} = \left(\frac{I_0 t_I}{q}\right)^{1/2} \quad [e]. \tag{5-9b}$$

# 5.1.1.7 Charge Transfer Noise

Charge transfer or transfer inefficiency noise is associated with CCD structures and occurs because of the random amount of charge lost by a signal upon transfer and the amount of charge introduced to a signal upon entering a well. The noise N<sub>CT</sub> associated with a single well (Dereniak, 1984, p. 242) is given by

$$N_{CT} = \left(2\epsilon S'\right)^{1/2} \quad [e], \tag{5-10}$$

where  $\epsilon$  = the transfer efficiency [nd].

If the number of detectors is  $n'_D$ , and the number of phases to transfer the charge is  $n_p$ , then the total number of wells is  $n_p n'_D$ . Hence the total charge transfer noise is given by

$$N_{CT} = \left(2\epsilon n_D' n_P S'\right)^{1/2} \quad [e] \quad . \tag{5-11}$$

# 5.1.2 Visible and SWIR System Noise

# 5.1.2.1 Quantization Noise

The quantization noise  $N_Q$  is given by (Montgomery, 1978, p. B-1)

$$N_{Q} = \frac{S'_{SAT}}{12^{1/2} 2^{Q}} \quad [e], \tag{5-12}$$

where Q is the number of bits used in the analog-to-digital (A/D) converter. From Equation (2-9) one obtains for the visible and SWIR

$$S'_{SAT} = t_I A_D \eta \overline{E}'_{SAT} \Delta \lambda \quad [e], \qquad (5-13)$$

where  $S'_{SAT}$  is the signal that would result if the detector were receiving the saturation irradiance. This is the flux that produces a signal level that just causes the A/D converter to saturate.

The saturation irradiance  $\overline{E}'_{SAT}$  is given by

$$\overline{E}'_{SAT} = E'_{M}S_{F} \quad [p/sec-cm^{2}-\mu m], \qquad (5-14)$$

where, from Equation (2-11),  $E'_{M}$  is given by

$$E'_{M} = \frac{\tau_{o}\pi}{4f^{2}_{N}} L'_{M} \quad [p/sec-cm^{2}-\mu m] .$$
 (5-15)

When the saturation factor  $S_F$  is multiplied by the maximum expected scene irradiance  $E'_M$  at the detector, an irradiance  $\bar{E}'_{SAT}$  will be produced that will just saturate the A/D converter.

# 5.1.2.2 Other System Noise

When system noises are from unknown sources, they are designated as other system noise.

## 5.2 Infrared Detector Noise

### 5.2.1 Infrared Detector Noise Sources

The detector noise is composed of two parts, photon noise and other noise. It is given by

$$N_{DET} = \left(N_{P}^{2} + N_{OD}^{2}\right)^{1/2}$$
 [e] (5-16)

We will calculate the photon noise  $N_P$  on the basis of a cold shielded and cold filtered detector. The other detector noise  $N_{OD}$ , will be estimated from laboratory values of  $D^*$ . We will estimate the other detector noise from  $D^*$  first.

# 5.2.1.1 Other Detector Noise

Consider the detector that will be used in the sensor (same area and electrical bandwidth), but with background temperature and viewing angles identical to those used in the laboratory measurement of D\*.

The other detector noise N<sub>OD</sub> is given by

$$N_{OD} = \left(NEE^2 - N_{PL}^2\right)^{1/2} \quad [e] . \tag{5-17}$$

The other detector noise  $N_{OD}$  is assumed to be independent of the level of cold shielding and cold filtering. The photon noise under laboratory conditions is

$$N_{PL} = \left(t_{I}F_{L} \pi \eta A_{D} \int_{0}^{\lambda_{C}} B'(T_{BGL}, \lambda) d\lambda\right)^{1/2} \quad [e], \qquad (5-18)$$

where  $\lambda_C$  is the detector cutoff wavelength,  $T_{BGL}$  is the background temperature in the laboratory,  $B'(T_{BGL}, \lambda)$  is defined by Equation (3-7), and  $F_L$  is the view factor in the laboratory ( $F_L = 1$  when viewing 180°, or  $2\pi$  steradians). In general

$$F_{L} = \sin^{2}\left(\frac{\phi_{C}}{2}\right) \quad [nd] \tag{5-19}$$

where  $\phi_{C}$  is the full-cone view angle.

The detector noise equivalent power is given by

NEP = 
$$\frac{(A_D \ \Delta f)^{1/2}}{D^*}$$
 [W], (5-20)

where  $A_D = \text{detector are [cm}^2$ ]; and

 $D^*$  = the laboratory value of specific detectivity [cm-Hz<sup>1/2</sup>/W].

The number of noise equivalent electrons NEE is given by

$$NEE = \frac{Rt_I}{q} NEP \quad [e]$$
 (5-21)

and the effective noise bandwidth is given by

$$\Delta f = \frac{\beta}{2t_{\rm I}} \quad [kHz], \tag{5-22}$$

where  $\beta$  is the ratio of noise bandwidth to information bandwidth, and  $t_I$  is the integration time given by Equation (2-8).

#### 5.2.1.2 Photon Noise (Infrared)

The photon noise is given by (Levi, 1968, p. 153)

$$N_{\rm p} = (\tau')^{1/2}$$
 [e], (5-23)

where the total number of electrons produced by the scene and background is given by

$$\tau' = t_{I} A_{D} \eta \left[ \int_{\lambda_{1}}^{\lambda_{2}} E'(\lambda) d\lambda + \int_{\lambda'_{1}}^{\lambda'_{2}} E'_{BG}(\lambda) d\lambda \right]$$
 [e], (5-24)

where  $\lambda_1$  to  $\lambda_2$  is the spectral bandpass of the scene photon spectral irradiance  $E'(\lambda)$ , which is given by Equation (2-11), and  $\lambda'_1$  to  $\lambda'_2$  is the spectral bandpass of the background photon spectral irradiance  $E'_{BG}(\lambda)$ , which is governed by the cold filter.

The background spectral irradiance  $E'_{BG}(\lambda)$  is given by

$$E'_{BG}(\lambda) = \left[\Omega \epsilon_{o} + (\Omega_{BG} - \Omega) \tau_{CF}\right] B'(\lambda, T_{BG}) \quad [p/\text{sec-cm}^{2} - \mu m]$$
 (5-25)

and the emissivity of the optics is given by

$$\epsilon_0 = 1 - \tau_0 \quad [nd], \tag{5-26}$$

where  $B'(\lambda, T_{BG})$  = the background spectral photon radiance, [p/sec-cm<sup>2</sup>-sr- $\mu$ m] obtained from Equation (3-7);

 $T_{BG}$  = the background temperature [K] of any radiant energy source other than the ground resolution element; and

 $\tau_{\rm CF}$  = optical transmission [nd] of the cold filter.

The effective solid angle  $\Omega$  (Figure 5) through which the detector receives energy from the ground resolution element is given by

$$\Omega = \frac{\pi}{4f^2_N} \quad [sr] \quad . \tag{5-27}$$

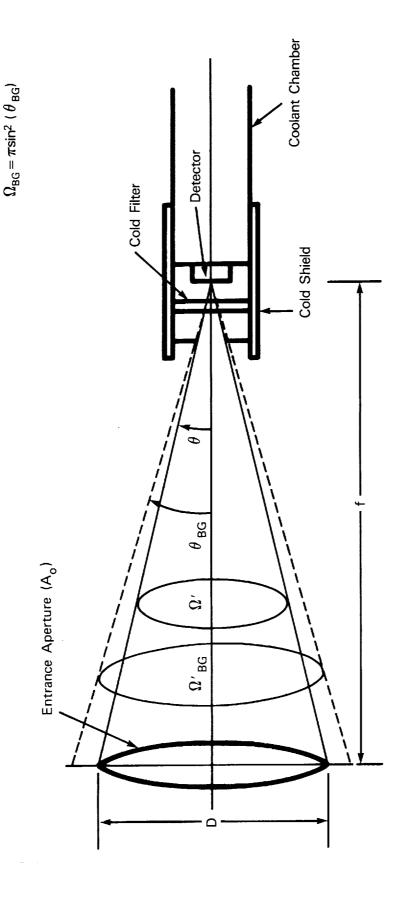
The background effective solid angle  $\Omega_{BG}$  includes the effective solid angle  $\Omega$  plus a little more for tolerance purposes. Ideally, they would be identical.

Solid Angles  $\Omega' = 2\pi(1-\cos\theta)$   $\Omega'_{\rm BG} = 2\pi(1-\cos\theta_{\rm BG})$ 

4f<sup>2</sup><sub>N</sub>

Effective Solid Angles

 $\Omega = \pi \sin^2(\theta) =$ 



Background effective solid angle (sr) = Optics effective solid angle (sr) Background solid angle (sr) Optics solid angle (sr) 11 || ກ ກ<sup>86</sup> ກ'<sub>86</sub> Diameter of sensor entrance aperture (cm) Area of sensor entrance aperture (cm²) Background half-cone angle (deg) = Optics half-cone angle (deg) = Background L. Y. Focal length (cm) II П

A<sub>o</sub> D 6  $\theta$  Figure 5. Background Viewing Geometry

The effective solid angle of the background  $\Omega_{\mbox{BG}}$  is given by

$$\Omega_{BG} = \pi F_{S} \quad [sr], \tag{5-28}$$

where the view factor F<sub>S</sub> is defined as

 $F_S$  =  $F_C$  for a cold shielded detector viewing the scene through a circular aperture (Appendix D), and

 $F_S = F_A$  for a detector array surrounded by a cold fence (Appendix E).

It follows that:

$$F_{C} = \sin^{2} \left[ \frac{\theta_{BG}}{2} \right] \quad [sr], \tag{5-29}$$

where  $\theta_{BG}$  is the full-cone angle [deg] of the background.

From Equation (5-20) one can write

$$D*_{S} = \frac{[A_{D} \ \Delta f]^{1/2}}{NEP} \qquad [cm-Hz^{1/2}/W]$$
 (5-30)

and

NEP = 
$$\frac{q}{R(\lambda) t_{I}} \left[ N_{P}^{2} + N_{OD}^{2} \right]^{1/2} [W]$$
 (5-31)

Substituting Equation (5-31) into Equation (5-30) and setting  $N_{OD} = 0$  yields

$$D_{BLIP}^*(\lambda) = \frac{R(\lambda)t_I \left(A_D \Delta f\right)^{1/2}}{qN_D} \qquad [cm-Hz^{1/2}/W]$$
 (5-32)

where  $D^*_{BLIP}$  is the background-limited photon (BLIP) value of  $D^*$ .

Substituting Equations (2-3), (5-21), (5-23), and (5-24) into Equation (5-32) gives

$$D*_{BLIP}(\lambda) = \frac{\lambda}{h \ c} \left(\frac{\eta}{2}\right)^{1/2} \left(\int_{\lambda_1}^{\lambda_2} E'(\lambda) \ d\lambda + \int_{\lambda'_1}^{\lambda'_2} d\lambda\right)^{-1/2} [cm-Hz^{1/2}/W] \ . (5-33)$$

Equation (5-33) includes only the photon noise and is for a photovoltaic detector. For a photoconductive detector there is an additional term due to generation-recombination noise, and it reduces  $D_{BLIP}^*$  by a factor of  $(2)^{1/2}$ .

# 5.2.2 <u>Infrared System Noise</u>

### 5.2.2.1 Quantization Noise

The quantization noise is given by (Montgomery, 1978, p. B-1)

$$N_Q = \frac{S'_{SAT}}{(12)^{1/2} 2^Q}$$
 [e], (5-34)

where Q is the number of bits used in the A/D converter.

The infrared saturation signal is given by

$$S'_{SAT} = t_i A_D \eta \int_{\lambda_1}^{\lambda_2} E'_{SAT}(\lambda) d\lambda \qquad [e], \qquad (5-35)$$

where the infrared saturation spectral photon irradiance  $E'_{SAT}(\lambda)$  is given by (see Appendix A)

$$E'_{SAT}(\lambda) = \frac{\tau_0 \pi}{4f_N^2} L'_{SAT}(\lambda) \qquad [p/sec-cm^2 - \mu m]$$
 (5-36)

and where the infrared saturation radiance  $L'_{SAT}(\lambda)$  is the appropriate value to just saturate the A/D converter.

## 5.2.2.2 Other Infrared System Noise

When the system noises are from unknown sources, they are designated as other system noise.

### 6. FIGURES OF MERIT

One important figure of merit that we will discuss here is the signal-to-noise ratio SNR, which is easily obtained by using the results of Section 2 for the signal S' and Section 5 for the noise  $N_{TOT}$ . We will also discuss a figure of merit used in the visible and SWIR bands, the Noise Equivalent Delta Reflectance (NE $\Delta\rho$ ), and for the infrared we shall discuss the Noise Equivalent Delta Temperature (NE $\Delta T$ ).

### 6.1 Noise Equivalent Delta Reflectance

When visible sensors are assessed with respect to surface observations such as reflectance, the SNR is not always a convenient figure of merit. Users of space or airborne remote sensor data are frequently concerned with the characterization of ground targets through the measurement of variations in target reflectance. Because the variations of interest are often small in magnitude and are difficult to measure precisely, there is considerable interest in the definition and measurement of the capability of the sensor to respond to small reflectance changes. This capability, related to sensitivity, is often described in terms of Noise Equivalent Delta Reflectance (NE $\Delta\rho$ ), which is the minimum detectable variation in reflectance, and is sometimes preferred by the science user community over the spatial resolution of the system.

For the visible and SWIR bands, NE $\Delta\rho$  is the amount by which  $\rho$  would need to change to cause the signal to change by an amount equal to the noise, or it is the smallest change in reflectance between two adjacent surface elements that can be resolved by the sensor. In this section we compute NE $\Delta\rho$  from the SNR.

The figure of merit NE $\Delta \rho$  is given by

$$NE\Delta\rho = \frac{L}{\left(\frac{S}{N}\right)\left(\frac{dL}{d\rho}\right)} = \frac{\gamma}{\frac{S}{N}} \quad [nd], \tag{6-1}$$

where  $\gamma$  (see Appendix F) is

$$\gamma = \frac{\gamma_0}{\tau_{AN}^{(\sec \phi' - 1)}} \quad [nd]$$
 (6-2)

and where

$$\gamma_{o} = \frac{\rho}{1 - \frac{L_{A}^{N}}{L^{N}}} \quad [nd] \quad . \tag{6-3}$$

Also,  $\phi'$  is the angle between the line of sight and the surface normal (see Figure 6) and  $L_A^N$  and  $L^N$  are the atmospheric and scene radiances respectively, from the tables in Appendix B.

The atmospheric optical transmission in the nadir direction  $\tau_{AN}$  is given by

$$\tau_{AN} = e^{-\delta_{TN}} \quad [nd], \tag{6-4}$$

where the total nadir optical thickness  $\delta_{TN}$  is obtained from the tables in Appendix B.

### 6.2 Noise Equivalent Delta Temperature

For the infrared bands NEAT is given by

NE
$$\Delta T = \frac{L'}{\tau_A \left(\frac{S}{N}\right) \left(\frac{dL'_S}{dT_S}\right)}$$
 [K]

where L' = the scene photon radiance  $[p/sec-cm^2-sr]$ ,

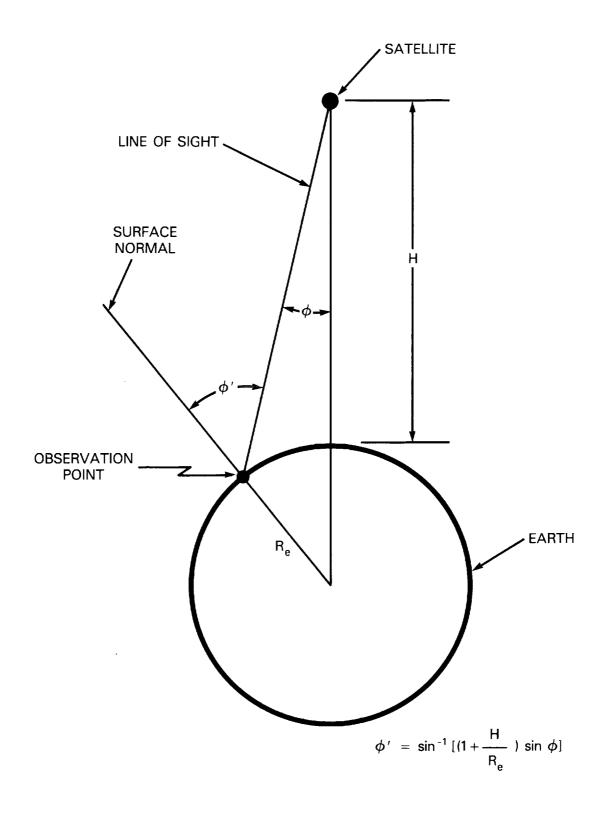
 $\tau_{A}$  = atmospheric transmission [nd],

S = signal [e],

N = noise [e], and

 $dL'_S/dT_S$  = the differential change in surface radiance with respect to surface temperature [p/sec-cm<sup>2</sup>-sr-K].

(See Appendix G for a detailed derivation.)



 $\phi$  = Sensor view angle (deg)

 $\phi'$  = Angle between line of sight and the surface normal (deg)

H = Height

 $R_e = Radius of Earth$ 

Figure 6. Satellite/Scene Viewing Geometry

## 7. MODULATION TRANSFER FUNCTION (MTF)

If the sensor were to scan a very low spatial frequency (sinusoidal variation in radiance) an amplitude variation  $\Delta S(0)$  in signal would result. At spatial frequency k [cycles/mm] an amplitude variation of  $\Delta S(k)$  would be obtained. The ratio of  $\Delta S(k)$  to  $\Delta S(0)$  is the Modulation Transfer Function (MTF) of the sensor; i.e.,

$$MTF = \frac{\Delta S(k)}{\Delta S(0)} \quad [nd] \tag{7-1}$$

### 7.1 Total MTF

For a linear system, the total modulation transfer function is the product of the modulation transfer functions of the individual elements of the system. There are many different MTFs associated with a sensor system, which typically might include:

- $MTF_{OA}$  = Optical Aperture MTF
- $MTF_{DA}$  = Detector Aperture MTF
- $MTF_{SM}$  = Satellite Motion MTF
- MTF<sub>CD</sub> = Charge Diffusion MTF
- MTF<sub>CT</sub> = Charge Transfer MTF
- MTF<sub>SI</sub> = Satellite Jitter MTF.

The total or system MTF is the product of the component MTFs; i.e.,

$$\mathsf{MTF} = \mathsf{MTF}_{\mathsf{OA}} \cdot \mathsf{MTF}_{\mathsf{DA}} \cdot \mathsf{MTF}_{\mathsf{SM}} \cdot \mathsf{MTF}_{\mathsf{CD}} \cdot \mathsf{MTF}_{\mathsf{CT}}$$

#### 7.2 Component MTFs

In this section we list the MTF equations and their reference sources.

# 7.2.1 Optical Aperture MTF

The diffraction MTF is given by (O'Neill, 1955 and 1956)

$$MTF_{OA} = \frac{A_{m} + B_{m} + C_{m}}{(1 - \beta^{2})} , \qquad (7-2)$$

where

$$A_{\rm m} = \frac{2}{\pi} \left\{ \cos^{-1} \left( \frac{\Lambda}{2} \right) - \left( \frac{\Lambda}{2} \right) \left[ 1 - \left( \frac{\Lambda}{2} \right)^2 \right]^{1/2} \right\} \quad \text{for } 0 \le \frac{\Lambda}{2} \le 1 \quad (7-3)$$

and

$$A_{\rm m} = 0$$
 for  $\frac{\Lambda}{2} > 1$ , (7-4)

where

$$B_{\rm m} = \frac{2\beta^2}{\pi} \left\{ \cos^{-1} \left( \frac{\Lambda}{2\beta} \right) - \left( \frac{\Lambda}{2\beta} \right) \left[ 1 - \left( \frac{\Lambda}{2\beta} \right)^2 \right]^{1/2} \right\} \text{ for } 0 \leqslant \frac{\Lambda}{2\beta} \leqslant 1 \qquad (7-5)$$

and

$$B_{\rm m} = 0 for \frac{\Lambda}{2\beta} > 1 (7-6)$$

and where

$$C_{\rm m} = -2\beta^2$$
 for  $0 < \frac{\Lambda}{2} \le \frac{(1-\beta)}{2}$  (7-7)

$$C_{\rm m} = -2\beta^2 + \frac{2\beta}{\pi} \sin\psi + \left(\frac{1+\beta^2}{\pi}\right)\psi$$

$$-2\left(\frac{1-\beta^2}{\pi}\right) \operatorname{Tan}^{-1} \left[\left(\frac{1+\beta}{1-\beta}\right) \operatorname{Tan} \frac{\psi}{2}\right]$$

$$\operatorname{for} \frac{1-\beta}{2} \leqslant \frac{\Lambda}{2} \leqslant \frac{1+\beta}{2} \quad (7-8)$$

and

$$C_{\rm m} = 0 \qquad \qquad \text{for } \frac{\Lambda}{2} > \frac{1+\beta}{2} , \quad (7-9)$$

and  $\psi$  is given by

$$\psi = \cos^{-1}\left(\frac{1+\beta^2 - \Lambda^2}{2\beta}\right) \tag{7-10}$$

with

$$\Lambda = \frac{k}{k_0} \tag{7-11}$$

where k is the spatial frequency [cycles/mm] measured in the image plane and

$$k_0 = \frac{1}{2\lambda f_N} \quad [cycles/mm] . \tag{7-12}$$

The modulation transfer function  $MTF_{OA} = 0$  for  $\Lambda = 2$  at the cutoff frequency when  $k = k_C$ , where

$$k_C = 2 k_0 \quad [cycles/mm], \tag{7-13}$$

and where

$$f_{N} = \frac{f}{D} \quad [nd] \quad . \tag{7-14}$$

where  $\lambda$  is the wavelength, f is the focal length of the optics, and D is the diameter of the optics; and

$$\beta = \frac{D_o}{D} \quad [nd] \tag{7-15}$$

where  $\boldsymbol{D}_{o}$  is the diameter of any obscuration.

Note that the quantity  $k_0$  given in Equation (7-12) is not defined in O'Neill's paper but must be defined this way to be consistent with his Figure 3 in which the MTF goes to zero at  $\Lambda = 2.0$ .

## 7.2.2 Detector Aperture MTF

The detector aperture MTF is given by (Jensen, 1968, p. 27)

$$MTF_{DA} = \left| \frac{\sin(\pi k d_S)}{\pi k d_S} \right|$$
 (7-16)

where  $d_S$  = the detector width [mm], and

k = spatial frequency in the image plane [cycles/mm].

#### 7.2.3 Satellite Motion MTF

The MTF due to linear image motion is given by (Jensen, 1968, p. 117)

$$MTF_{SM} = \left| \frac{\sin(\pi k V_I t_I)}{\pi k V_I t_I} \right|$$
 (7-17)

where the image velocity  $\boldsymbol{V}_{\boldsymbol{I}}$  is given by

$$V_{I} = \frac{fV_{SUB}}{H} \quad [km/sec], \tag{7-18}$$

where  $V_{SUB}$  = the subsatellite point velocity [km/sec];

k = spatial frequency in the image plane [cycles/mm]; and

 $t_{I}$  = integration time [sec].

## 7.2.4 Charge Diffusion MTF

The charge diffusion MTF is given by (Jespers, 1975, p. 519)

$$MTF_{CD} = \frac{1 - \frac{\exp - \alpha_a d}{1 + \alpha_a L}}{\frac{\exp - \alpha_a d}{1 + \alpha_a L_o}}$$
(7-19)

where  $d = photodetector depletion region depth (typical value = 5 <math>\mu$ m).

The silicon absorption coefficient  $\alpha_a$  is a function of wavelength and temperature and is given by

$$\alpha_a = 10^z \text{ [cm}^{-1}\text{]}$$
 (7-20)

where, after curve fitting to Jespers' Figure 25 for silicon, we have

$$z = 2.897652 - 4.044143 (\lambda - 0.82) - 5.219219 (\lambda - 0.82)^{2}$$
$$- 3.828495 (\lambda - 0.82)^{3} + 22.16724 (\lambda - 0.82)^{4} , \qquad (7-21)$$

where  $\lambda = \text{wavelength } [\mu m]$ ,

 $L_0 =$  diffusion length (typical value = 50  $\mu$ m),

and where

$$L = \left[ \frac{L_0^2}{1 + (2\pi k L_0)^2} \right]^{1/2} . \tag{7-22}$$

## 7.2.5 Charge Transfer MTF

The MTF due to inefficiency in charge transfer in a CCD detector is given by (Jespers, 1976, p. 520)

$$MTF_{CT} = e^{-M_{CT} \epsilon} \left[ 1 - \cos \left( \frac{\pi k}{k_{max}} \right) \right]$$
 (7-23)

where  $\epsilon$  is the charge transfer inefficiency and where the number of charge transfers  $M_{CT}$  is given by

$$M_{CT} = m_S m_P , \qquad (7-24)$$

where m<sub>S</sub> = the number of stages, detectors, or picture elements, and

 $m_p$  = the number of clock phases for readout.

The Nyquist spatial frequency  $k_{\text{max}}$  is given by

$$k_{\text{max}} = \frac{1}{2P_{\text{D}}} , \qquad (7-25)$$

where  $\boldsymbol{P}_{\boldsymbol{D}}$  is the detector pitch.

# 7.2.6 Satellite Jitter MTF

The satellite jitter MTF is given by (Jensen, 1968, p. 124)

$$MTF_{SJ} = J_0(2\pi kf\Theta_M)$$
 (7-26)

where  $\Theta_{M}$  = maximum satellite angular movement [rad],

 $J_0$  = zeroth order Bessel function, and

f = focal length (mm).

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#### APPENDIX A

### **DETECTOR IRRADIANCE**

The objective of this appendix is to show the relationship between the scene spectral radiance and the irradiance on the detector.

When a sensor images an area on the surface of the Earth called the instantaneous field of view (IFOV), it also receives energy from the intervening atmosphere. The scene spectral radiance  $L(\lambda)$  [W/cm<sup>2</sup>-sr- $\mu$ m] is defined as the combined spectral radiance from the atmosphere and the IFOV area  $A_I$  as viewed from the sensor. The power that the area  $A_I$  and the intervening atmosphere radiate through the solid angle  $\Omega_o$  into the sensor entrance aperture and into the detector is then

$$\Phi = \begin{cases} \lambda_2 \\ d\phi(\lambda) & [W] \end{cases}$$
 (A-1)

where

$$d\phi(\lambda) = \tau_0 \Omega_0 A_1 L(\lambda) d\lambda \quad [W]$$
 (A-2)

and where  $\tau_0$  = the sensor optical transmission. However, by definition, for a detector of area  $A_D$ , Equation (A-2) may also be written in terms of the detector spectral irradiance  $E(\lambda)$  [W/cm<sup>2</sup>- $\mu$ m] as

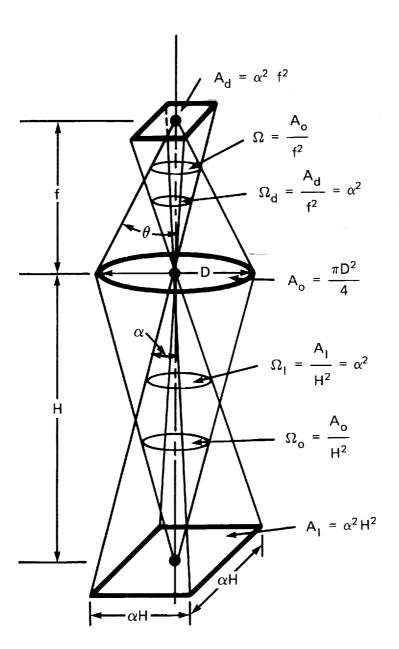
$$d\phi(\lambda) = A_D E(\lambda) d\lambda \quad [W]$$
 (A-3)

By comparing Equations (A-2) and (A-3), one can express the scene spectral irradiance  $E(\lambda)$  in terms of the scene spectral radiance  $L(\lambda)$  and sensor design-related parameters  $A_D$ ,  $A_I$ , and  $\Omega_o$  as

$$E(\lambda) = \frac{\tau_0 \Omega_0 A_I}{A_D} L(\lambda) \quad [W/cm^2 - \mu m) . \tag{A-4}$$

Now, from Figure A-1,

$$A_1 = \alpha^2 H^2, \tag{A-5}$$



 $A_d = Detector area (\mu m^2)$ 

 $A_0^{\sim}$  = Area of sensor entrance aperture (cm<sup>2</sup>)

 $A_1^{\circ}$  = Area of ground resolution element (cm<sup>2</sup>)

D = Diameter of sensor entrance aperture (cm)

f = Effective focal length (cm)

H = Satellite height (km)

 $\alpha$  = Instantaneous angular FOV (as in previous figs) (rad)

 $\theta$  = Half-cone angle of optics (deg)

 $\Omega$  = The effective solid angle through which the detector receives energy (sr)

 $\Omega_{\rm o}$  = Solid angle subtended by the sensor entrance aperture at the ground resolution element (sr)

 $\Omega_1$  = Solid angle subtended by the ground resolution element at the sensor entrance aperture (sr)

 $\Omega_{d}^{'}$  = Solid angle subtended by the detector at the entrance aperture (sr)

Figure A-1. Radiometric Geometry

where  $\alpha$  = the sensor instantaneous field of view (IFOV), and

H = the distance from the satellite to the area  $A_I$ .

Also, for a square detector

$$A_D = \alpha^2 f^2, \tag{A-6}$$

where f is the sensor optics effective focal length, which represents the optical path length and is approximately equal to the geometric focal length for small optical convergence angles ( $<10^{\circ}$ ), and

$$\Omega_{0} = \frac{A_{0}}{H^{2}} = \frac{\pi D^{2}}{4H^{2}} , \qquad (A-7)$$

where D = aperture diameter of the sensor.

Using Equations (A-5), (A-6) and (A-7), one can write

$$\frac{A_{\rm I}\Omega_{\rm o}}{A_{\rm D}} = \frac{\pi}{4f_{\rm N}^2} \tag{A-8}$$

where the sensor optics f-number  $f_N$  is given by

$$f_{N} = \frac{f}{D} . ag{A-9}$$

The half-cone angle  $\theta$  of the optics is given by

$$\sin \theta = \frac{D}{2f} . \tag{A-10}$$

It is also given by

$$\tan \theta = \frac{D}{2f'}.$$
 (A-11)

The f-number  $f_N$  is related to the approximate f-number  $\left(\frac{f'}{D}\right)$  by the expression

$$f_{N} = \left(\frac{f'}{D}\right) \left[1 + \left(\frac{1}{2 \cdot \frac{f'}{D}}\right)^{2}\right]^{1/2}$$
(A-12)

Substituting Equation (A-8) into Equation (A-4) (See Figure A-2) gives

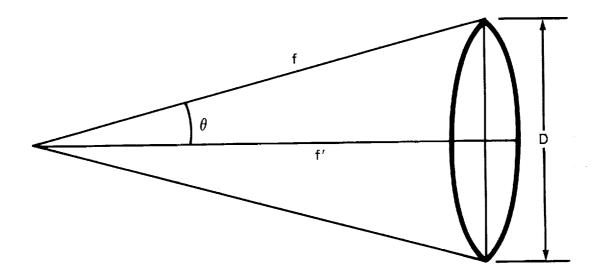


Figure A-2. Comparison of  $f_{\mbox{\scriptsize $N$}}$  and f'/D

$$E(\lambda) = \frac{\pi \tau_0}{4f_N^2} L(\lambda) \qquad [W/cm^2 - \mu m] . \qquad (A-13)$$

# REFERENCES

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#### APPENDIX B

### COMPUTED EARTH ATMOSPHERE RADIANCES

With the permission of the authors, the following discussion has been taken from a NASA unpublished report (Mattoo, 1984) and a memorandum (Fraser, 1981).

The computations are made for plane-parallel models of the Earth-atmosphere system; that is, the optical properties of the models do not vary in a horizontal plane. However, the vertical profiles of the concentrations of the atmospheric constituents are arbitrary, but realistic. The ground reflects light according to Lambert's law, which implies that the radiance of the reflected light is constant, independent of direction.

Only one atmospheric model is used, and it contains the standard dry gas and the gases that absorb in the spectral bands of interest. The variable trace gases are 316 Dobson units of  $O_3$  and 2.5 cm of  $O_3$ . The model also contains particulates, but not liquid or ice clouds.

The average normal optical thickness of each constituent is given for each spectral band in Table B-1. The total nadir optical thickness ( $\delta_{TN}$ ) at a wavelength equals the sum of the optical thicknesses of the constituents:

$$\delta_{\text{TN}} = \delta_{\text{R}} + \delta_{\text{G}} + \delta_{\text{A}} , \qquad (B-1)$$

where  $\delta_R$  = the scattering optical thickness (Rayleigh) of the dry atmosphere,

 $\delta_A$  = the optical thickness of the aerosols (particulates), and

 $\delta_C$  = the optical thickness of the absorbing gases.

The total optical transmission  $\tau$  for the direct sunlight is given by

$$\tau = \frac{E_{\lambda s}}{E_{\lambda o}} = \exp(-\delta_{TN} \sec \theta_z)$$
 (B-2)

where  $E_{\lambda s}$  and  $E_{\lambda o}$  are the spectral irradiance of the direct sunlight at sea level and above the atmos-

Table B-1. Optical Thicknesses for Scattering by Molecules ( $\delta_R$ ), Absorption by Gases ( $\delta_G$ ), and Scattering from Aerosols ( $\delta_A$ )

λ	0.4	0.44	0.48	0.52	0.56
$\delta_{ m R}$	0.3637	0.2451	0.1713	0.1234	0.0912
$\delta_{\mathbf{G}}$	0.0000	0.0007	0.0048	0.0151	0.0296
$\delta_{A}$	0.3600	0.3273	0.3000	0.2796	0.2571
$\delta_{ ext{TN}}$	0.7237	0.5731	0.4761	0.4181	0.3779
λ	0.62	0.66	0.70	0.74	0.82
$\delta_{\mathbf{R}}$	0.0603	0.0468	0.0368	0.0294	0.0195
$\delta_{ m G}$	0.0325	0.0169	0.0135	0.0145	0.0560
${\color{blue}\delta_{G} \atop \delta_{A}}$	0.2370	0.2228	0.2087	0.1988	0.1794
δ <sub>TN</sub>	0.3298	0.2865	0.2590	0.2427	0.2549
λ	0.88	1.05	1.25	1.60	2.20
$\delta_{ m R}$	0.0147	0.0072	0.0036	0.0013	0.0004
$\delta_{G}^{R}$	0.0039	0.0000	0.0092	0.0066	0.0608
$\delta_{\mathbf{A}}^{\mathbf{G}}$	0.1694	0.1420	0.1193	0.0932	0.0682
$\delta_{ ext{TN}}$	0.1880	0.1492	0.1321	0.1011	0.1294

phere, respectively, and  $\theta_z$  is the solar zenith angle. The values of  $E_{\lambda o}$  are given in Table B-2. The quantity  $E_{\lambda o}$  is the solar irradiance on a square centimeter of surface perpendicular to the solar rays.

The aerosols (particulates) are assigned properties of those occurring in continential regions. The size distribution function (n) of the particle radius (r), which is the number of particles per cubic centimeter of air per micrometer of radius, decreases very rapidly with increasing radius:

$$n \sim r^{-4} . ag{B-3}$$

The index of refraction of the particulates is m = 1.4300 - 0.0035i. The nadir radiances of the model are not sensitive to the vertical profile of the particulate concentration. Here, a realistic profile with a high concentration near the ground is assumed.

The computations are made with a computer code developed by Dr. J. V. Dave of IBM as modified by R. S. Fraser of NASA. The equation of radiative transfer is solved numerically by a procedure that iteratively accounts for successive scatterings of light from the atmosphere and the ground. The polarization characteristics are not accounted for, and as a result, the computed radiances are in error by a few percent.

The input parameters for the computations include the model parameters: the vertical profiles of the concentrations of the gases and aerosols (particulates), the scattering and absorption optical thickness, the gaseous absorption coefficients, and 10 values of the surface reflectance  $\rho$ . The volume extinction, scattering and absorption coefficients and scattering phase function of the particulates are computed according to the Mie theory by a separate code, and are part of the input.

The nadir spectral radiance at the top of the atmosphere L<sup>N</sup> can be expressed as follows:

$$L^{N} = L_{S} e^{-\delta_{TN}} + L_{A}^{N}$$
, (B-4)

where the first term on the right-hand side of the equation gives the radiance at the surface (ground)  $L_S$  (assumed to be Lambertian) attenuated by the atmosphere; the second term gives the radiance of just the atmosphere  $L_A^N$ , or path radiance. The radiances  $L^N$  and  $L_A^N$  are given in Table B-2, where

 $\lambda$  = the center wavelength [mm],

 $\theta_z$  = the solar zenith angle [rad],

 $\rho$  = the surface reflectance [nd],

 $\delta_{TN}$  = the total optical thickness [nd],

 $E_{\lambda o}$  = the solar spectral irradiance [mW/cm<sup>2</sup>- $\mu$ m],

 $L^{N}$  = the total nadir spectral radiance [mW/cm<sup>2</sup>-sr- $\mu$ m] and

 $L_A^N$  = the atmospheric path spectral radiance [mW/cm<sup>2</sup>-sr- $\mu$ m].

Table B-2. Reflected Solar Spectral Radiance

= 0.72	20	LA	10.885 10.785 10.347 9.634 8.683 7.604 6.369 4.893	1.00	LA	33.437 33.418 31.478 28.985 25.195 20.732 15.670 10.414 4.918
δ <sub>TN</sub>	0.20	$\Gamma_{N}$	14.987 14.806 14.140 13.058 11.611 9.931 8.024 5.865 3.211	1.0	LN	53.944 53.522 50.445 46.106 39.835 32.365 23.945 15.273 6.830
	01	LA	9.291 9.173 8.847 8.254 7.507 6.669 5.707 4.499	0.75	LA	24.104 24.073 22.744 20.999 18.379 15.313 11.830 8.136
•	0.10	$\Gamma_{ m N}$	11.341 11.183 10.743 9.966 8.970 7.832 6.535 4.985	0.	LN	39.484 39.152 36.970 33.840 29.359 24.038 18.036 11.781
165.400 mW/cm <sup>2</sup> -µm,	0.05	LA	8.569 8.441 8.167 7.627 6.973 6.244 5.407 4.320 2.615	0.50	LNA	17.045 16.989 16.130 14.942 13.211 11.204 8.918 6.409
= 165.400	0.0	LN	9.594 9.447 9.115 8.484 7.705 6.826 5.821 4.563	0.5	$\Gamma_{N}$	27.298 27.041 25.614 23.502 20.531 17.021 13.056 8.838 4.355
$E_{\lambda_{\mathrm{o}}}$	10	LA	8.025 7.890 7.655 7.156 6.570 5.924 5.181 4.185 2.565	01	LA	14.741 14.672 13.969 12.960 11.520 9.860 7.967 5.843
	0.01	Γ <sub>N</sub>	8.230 8.091 7.844 7.327 6.717 6.041 5.263 4.233	0.40	ΓN	22.944 22.714 21.556 19.809 17.376 14.514 11.276 7.787
,m,	00	LA	7.894 7.757 7.531 7.042 6.473 5.847 5.126 4.152 2.552	30	$L_{ m A}^{ m N}$	12.695 12.612 12.048 11.197 10.017 8.665 7.120 5.340
$\lambda = 0.400 \ \mu \text{m},$	0.00	$\Gamma_{\rm N}$	7.894 7.757 7.531 7.042 6.473 5.847 5.126 4.152 2.552	0:30	$\Gamma_{N}$	18.848 18.643 17.739 16.333 14.409 12.155 9.602 6.797
	ď	$\theta_{\rm z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0	ď	$\theta_{\rm z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

$\delta_{TN} = 0.57$	50	LN	9.263 9.083 8.750 8.071	6.381 5.389 4.167 2.536
$^{\delta}_{ m TN}$	0.20	$\Gamma_{N}$	14.677 14.395 13.772 12.624	9.523 7.653 5.515 3.062
	01	${ m L}_{ m A}^{ m N}$	7.598 7.450 7.205 6.676	5.409 4.683 3.779 2.393
,	0.10	$\Gamma^{ m N}$	10.305 10.106 9.717 8.953 8.027	6.980 6.980 5.815 4.452 2.656
$= 177.300 \text{ mW/cm}^2 - \mu \text{m}$	)5	LA	6.838 6.705 6.501 6.040	4.965 4.360 3.602 2.329
= 177.300 1	0.05	ZJ	8.191 8.033 7.756 7.178	5.750 5.750 4.926 3.939 2.460
$\mathrm{E}_{\lambda_0}$ =	)1	LA	6.263 6.142 5.968 5.559	2.078 4.629 4.116 3.469 2.280
	0.01	LN	6.534 6.408 6.219 5.786	5.294 4.786 4.230 3.536 2.307
ım,	00	LA	6.124 6.006 5.839 5.442	4.947 4.057 3.437 2.269
$\lambda = 0.440 \ \mu \text{m},$	00'0	LN	6.006 5.839 5.442	4.397 4.548 4.057 3.437 2.269
-	σ	$\theta_z$	0.0 10.0 20.0 30.0	40.0 50.0 60.0 70.0 80.0

00	LA	31.420 30.813 29.302 26.652 23.364 19.303 14.756 9.424 4.497
1.00	LN	58.490 57.371 54.416 49.416 42.952 35.012 26.073 16.160 7.129
75	LA	22.520 22.084 21.047 19.187 16.905 14.115 10.998 7.301
0.75	$\Gamma_{ m N}$	42.823 42.003 39.882 36.260 31.597 25.898 19.486 12.353 5.675
50	LN	15.549 15.248 14.581 13.341 11.844 10.050 8.051 5.647 3.084
0.50	$\Gamma_{\rm N}$	29.084 28.527 27.138 24.723 21.639 17.905 13.710 9.015 4.400
01	LA	13.223 12.967 12.423 11.390 10.155 8.693 7.067 5.098 2.880
0.40	N <sub>J</sub>	24.051 23.590 22.469 20.496 17.990 14.977 11.594 7.792 3.932
30	LA	11.133 10.917 10.484 9.638 8.637 7.473 6.182 4.606 2.698
0:30	LN	19.254 18.884 18.018 16.468 14.513 12.186 9.577 6.627
ď	$^{\mathrm{z}}_{\theta}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

= 0.48	0	LA	8.669	8.487	8.179	7.522	6.737	5.890	4.977	3.931	2.481		00	LA	31.480
II NL γ	0.20	$\Gamma_N$	15.840	15.526	14.845	13.581	11.971	10.114	8.046	5.776	3.195		1.00	$\Gamma_{ m N}$	67.336
	0	LA	6.881	6.732	6.517	6.012	5.432	4.838	4.212	3.471	2.303		7.5	$L_{\mathbf{A}}^{\mathbf{N}}$	22.506
,	0.10	$\Gamma_{ m N}$	10.467	10.252	9.850	9.041	8.049	6.950	5.746	4.394	2.660		0.75	LN	49.398
206.000 mW/cm²-μm,	)5	${ m L}_{ m A}^{ m N}$	6.061	5.927	5.755	5.318	4.833	4.355	3.861	3.260	2.221		20	LA	15.309
= 206.000 r	0.05	LN	7.854	7.686	7.422	6.833	6.142	5.411	4.628	3.721	2.400		0.50	LN	33.237
$\mathrm{E}_{\lambda_0}$	10	LA	5.438	5.316	5.177	4.792	4.379	3.988	3.594	3.100	2.159		10	LA	12.870
	0.01	LN	5.797	5.668	5.510	5.095	4.641	4.200	3.748	3.192	2.195		0.40	L'N	27 213
ım,	01	LA	5.287	5.168	5.036	4.665	4.269	3.900	3.530	3.061	2.144		30	LA	10 661
$\lambda = 0.480 \ \mu \text{m},$	0.00	LN	5.287	5.168	5.036	4.665	4.269	3.900	3.530	3.061	2.144		0.30	NJ	21.418
	ď	$\theta_z$	0.0	10.0	20.0	30.0	40.0	50.0	0.09	70.0	80.0		ď	$\theta_{z}$	0

01	LA	31.480 30.880 29.379 26.799 23.387 19.321 14.738 9.801 4.754
1.00	LN	67.336 66.075 62.709 57.090 49.561 40.441 30.084 19.025 8.327
7.5	$L_{\mathbf{A}}^{\mathbf{N}}$	22.506 22.070 21.039 19.216 16.837 14.037 10.898 7.492 3.860
0.75	$\Gamma_{ m N}$	49.398 48.466 46.036 41.934 36.467 26.877 22.407 14.410 6.539
20	LA	15.309 15.006 14.350 13.134 11.584 9.800 7.818 5.640 3.143
0.50	2	33.237 32.603 31.015 28.280 24.670 20.359 15.491 10.252 4.929
01	LN	12.870 12.611 12.083 11.073 9.803 8.364 6.775 5.012 2.899
0.40	L'N	27.213 26.689 25.415 23.189 20.273 16.811 12.913 8.702 4.329
30	LA	10.661 10.443 10.030 9.206 8.191 7.063 5.829 4.444
0.30	LN	21.418 21.001 20.029 18.293 16.043 13.399 10.433 7.211
ď	$\theta_{z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

= 0.42	20	LA	6.329	6.184	5.962	5.454	4.862	4.230	3.559	2.804	1.775		00.1	LA
~ ~	0.20	LN	13.202	12.931	12.356	11.272	668.6	8.306	6.532	4.594	2.454		1:0	LN
	0.10	LA	4.873	4.755	4.608	4.223	3.795	3.368	2.930	2.425	1.632		7.5	LA
r	0	LN	8.310	8.129	7.805	7.132	6.314	5.405	4.416	3.321	1.971		0.75	LZ
$= 183.400 \text{ mW/cm}^2 - \mu\text{m},$	0.05	LA	4.201	4.096	3.983	3.655	3.302	2.969	2.639	2.251	1.566		0.50	LA
= 183.400	0.0	ΓN	5.919	5.783	5.581	5.110	4.562	3.988	3.383	2.698	1.735		0.	Γ <sub>N</sub>
$\mathrm{E}_{\lambda \mathrm{o}}$	01	LN	3.690	3.594	3.507	3.223	2.927	2.666	2.418	2.118	1.515		0†	Ϋ́Τ
	0.01	ΓN	4.033	3.931	3.827	3.514	3.179	2.870	2.567	2.207	1.549		0.40	$\Gamma_{\mathrm{N}}$
тш,	00	$\Gamma_{\mathbf{A}}^{\mathrm{N}}$	3.565	3.472	3.391	3.118	2.836	2.593	2.365	2.086	1.503		30	$L_A^N$
$\lambda = 0.520 \ \mu \text{m},$	0.00	$L^{N}$	3.565	3.472	3.391	3.118	2.836	2.593	2.365	2.086	1.503		0:30	L <sup>N</sup>
	φ	$\theta_{\mathrm{z}}$	0.0	10.0	20.0	30.0	40.0	50.0	0.09	70.0	80.0		θ	$\theta_{\rm z}$

		5	55	 97	<u>4</u>	33	15	4	51	 요
1.00	LA	24.24	23.76	22.62	20.60	17.99	14.84	11.30	7.461	3.54
1	ΓN	58.606	57.502	54.597	49.696	43.178	35.224	26.166	16.415	6.935
75	LA	17.317	16.966	16.182	14.745	12.915	10.739	8.309	5.660	2.857
0.75	LN	43.087	42.269	40.160	36.564	31.804	26.024	19.455	12.375	5.403
0.50	LA	11.657	11.411	10.917	9.958	8.767	7.386	5.862	4.188	2.299
0.5	Z <sub>1</sub>	28.837	28.280	26.902	24.504	21.359	17.575	13.293	8.665	3.997
01	LA	9.713	9.504	9.110	8.315	7.342	6.235	5.022	6.683	2.108
0.40	ΓN	23.458	22.999	21.898	19.952	17.416	14.386	10.967	7.265	3.466
0;	LA	7.940	7.765	7.460	6.816	6.043	5.184	4.256	3.222	1.934
0:30	$\Gamma_{ m N}$	18.348	17.886	17.051	15.543	13.598	11.298	8.714	5.908	2.952
σ	$\theta_{\mathrm{z}}$	0.0	10.0	20.0	30.0	40.0	50.0	0.09	70.0	80.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

_			
$\delta_{\mathrm{TN}} = 0.38$	0)	LA	5.227 5.101 4.918 4.479 3.939 3.435 2.247 1.410
δTN	0.20	$\Gamma_{ m N}$	12.392 12.136 11.586 10.549 9.226 7.691 5.973 4.111
	0	$L_A^N$	3.927 3.823 3.707 3.378 3.015 2.663 2.307 1.907
_	0.10	LN	7.509 7.341 7.041 6.412 5.643 4.791 3.859 2.839 1.622
$E_{\lambda_0} = 183.000 \text{ mW/cm}^2 - \mu\text{m},$	5	LA	3.324 3.232 3.146 2.867 2.572 2.305 1.749 1.219
= 183.000 r	0.05	$\Gamma_{ m N}$	5.115 4.990 4.813 4.385 3.887 3.369 2.822 2.215 1.390
$\mathrm{E}_{\lambda^{\mathrm{o}}}$	01	LA	2.865 2.780 2.718 2.478 2.235 2.032 1.847 1.629 1.173
	0.01	LN	3.223 3.132 3.052 2.781 2.498 2.244 2.002 1.722 1.207
ım,	00	LA	2.753 2.670 2.614 2.383 2.153 1.965 1.798 1.599 1.161
$\lambda = 0.560 \ \mu \text{m},$	0.00	Z.1	2.753 2.670 2.614 2.383 2.153 1.965 1.798 1.599 1.161
	d	zθ	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

	T	
00	LN	20.832 20.426 19.442 17.698 14.420 12.706 9.924 6.323
1.00	$\Gamma_{ m N}$	56.654 55.601 52.782 48.047 41.705 33.984 25.142 15.643 6.383
5	LA	14.870 14.571 13.893 12.648 11.045 9.164 7.043 4.766 2.368
0.75	$\Gamma_{ m N}$	41.736 40.952 38.898 35.409 30.759 25.123 18.682 11.756 4.938
0	LA	9.936 9.725 9.300 8.468 7.424 6.233 4.907 3.477
0.50	LN	27.847 27.312 25.970 23.642 20.567 16.872 12.666 8.137 3.592
0.	LAZ	8.226 8.046 7.709 7.020 6.170 5.217 4.167 3.031
0.40	Z <sub>J</sub>	22.555 22.116 21.045 19.159 16.684 13.729 10.375 6.759 3.080
0	LA	6.659 6.506 6.250 5.692 5.019 4.286 3.489 2.621 1.553
0:30	ΓN	17.405 17.059 16.252 14.796 12.905 10.669 8.144 5.417 2.581
ď	$\theta_{\rm Z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

$\delta_{\rm TN} = 0.33$	0.20	LA	4.087 3.978 3.839 3.074 2.655 2.212 1.739 1.086
$\delta_{TN}$	0.2	LN	11.266 11.030 10.527 9.581 8.365 6.953 5.364 3.647 1.790
	01	LA	2.979 2.892 2.809 2.545 2.260 1.992 1.727 1.439 0.977
•	0.10	$\Gamma_{ m N}$	6.569 6.417 6.153 5.593 4.141 3.302 2.393 1.329
$= 172.400 \text{ mW/cm}^2 - \mu\text{m},$	)5	$\mathbf{L}_{\mathbf{A}}^{\mathbf{N}}$	2.464 2.386 2.329 2.108 1.881 1.683 1.500 1.299 0.926
= 172.400	0.05	$L^{N}$	4.258 4.149 4.001 3.632 3.203 2.757 2.288 1.776 1.102
$E_{\lambda o}$	)1	$L_{\mathbf{A}}^{\mathbf{N}}$	2.069 1.999 1.962 1.773 1.591 1.446 1.327 1.192 0.887
	0.01	ΓN	2.428 2.351 2.297 2.078 1.855 1.661 1.485 0.922
μm,	00	LAA	1.973 1.905 1.873 1.692 1.520 1.389 1.285 1.166 0.877
$\lambda = 0.620 \ \mu \text{m},$	00.00	LN	1.973 1.905 1.873 1.692 1.520 1.389 1.285 1.166 0.877
	ď	$\theta_z$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

	r	
1.00	LN	17.036 16.687 15.889 14.474 12.601 10.414 7.895 5.231 2.360
1.0	LN	52.932 51.945 49.332 44.954 39.057 31.903 23.650 14.771 5.881
75	LA	12.149 11.890 11.341 10.326 9.005 7.486 5.750 3.916 1.879
0.75	r <sub>Z</sub> 7	39.070 38.334 36.423 33.186 28.846 23.603 17.567 11.070 4.520
20	LA	8.052 7.869 7.528 6.850 5.991 5.031 3.952 2.811 1.476
0.50	Ги	25.999 25.498 24.249 22.090 19.218 15.776 11.830 7.581
40	$\mathbf{L}_{\mathbf{A}}^{\mathbf{N}}$	6.619 6.463 6.195 5.634 4.937 4.173 3.324 2.424 1.335
0.40	LN	20.977 20.567 19.572 17.826 15.519 12.769 9.626 6.240 2.744
0:30	$L_A^N$	5.299 5.168 4.966 4.513 3.965 3.382 2.744 2.067 1.205
0.	L <sup>N</sup>	16.067 15.745 14.999 13.657 11.902 9.828 7.471 4.929
ď	$\theta_{\rm z}$	0.0 10.0 20.0 330.0 40.0 50.0 60.0 80.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

$\delta_{TN} = 0.29$	20	LA	3.413 3.323 3.211 2.912 2.568 2.222 1.860 1.473 0.969
νL	0.20	$\Gamma_N$	10.382 10.171 9.715 8.854 7.745 6.453 4.996 3.413 1.723
	0	LA	2.438 2.364 2.301 2.080 1.844 1.629 1.421 1.201 0.864
	0.10	$\Gamma_{N}$	5.922 5.788 5.553 5.051 4.432 3.745 2.889 2.171
nW/cm² –µm,	5	LA	1.983 1.916 1.876 1.692 1.506 1.352 1.216 1.074 0.815
$= 156.400 \text{ mW/cm}^2 - \mu \text{m}$	0.05	ΓN	3.725 3.628 3.628 3.502 3.177 2.800 2.410 2.000 1.559 1.003
$E_{\lambda_0}$	11	LA	1.634 1.573 1.550 1.394 1.247 1.140 1.059 0.977
	0.01	LN	1.053 1.916 1.876 1.691 1.506 1.352 1.212 1.074 0.815
ım,	01	LA	1.549 1.489 1.471 1.321 1.184 1.088 1.021 0.953
$\lambda = 0.660 \ \mu \text{m},$	0.00	LN	1.549 1.489 1.471 1.321 1.184 1.088 1.021 0.953
. •	ď	$\theta_{\rm z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

	<del></del>	
00	LA	14.655 14.377 13.701 12.503 10.915 9.953 6.917 4.607 2.181
1.00	$L^{N}$	49.499 48.617 46.219 42.210 36.798 30.211 22.600 14.308 5.954
5	LA	10.441 10.234 9.768 8.908 7.786 6.493 5.021 3.433 1.726
0.75	LN	36.574 35.914 34.157 31.188 27.198 22.361 16.784 10.708 4.556
0	LA	6.883 6.736 6.449 5.873 5.144 4.331 3.421 2.441 1.343
0.50	$\Gamma_{ m N}$	24.305 23.856 22.708 20.727 18.086 14.910 11.263 7.291
0	LA	5.633 5.507 5.282 4.807 4.216 3.571 2.858 2.092 1.208
0.40	LN	19.571 19.203 18.290 16.689 14.570 12.034 9.132 5.973
0	LA	4.478 4.370 4.204 3.820 3.358 2.869 2.339 1.770 1.083
0:30	T <sub>N</sub>	14.931 14.642 13.960 12.733 11.123 9.216 7.044 4.680 2.215
d	$\theta_{\rm z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

				_			
= 0.26		${ m L}_{ m A}^{ m N}$	2.789 2.713 2.625 2.376 2.093 1.805 1.513 1.185 0.807		00	$L_{ m A}^{ m N}$	12.242 12.007 11.459 10.458 9.146 7.577 5.817 3.803 1.894
$\delta_{TN}$	0.20	$\Gamma_{ m N}$	9.313 9.125 8.718 7.949 6.957 5.793 4.484 3.040 1.543		1.00	$L^{ m N}$	44.864 44.071 41.927 38.322 33.467 27.515 20.670 13.077
	0	LA	1.959 1.897 1.849 1.666 1.473 1.299 1.136 0.957		0.75	LA	8.718 8.542 8.166 7.445 6.517 5.425 4.213 2.824 1.490
,	0.10	$\Gamma_{ m N}$	5.221 5.103 4.896 4.453 3.905 3.293 2.621 1.885 1.079			Γ <sub>N</sub>	33.184 32.590 31.017 28.343 24.757 20.379 15.352 9.779
140.900 mW/cm <sup>2</sup> -μm,	)5	LA	1.571 1.515 1.486 1.334 1.184 1.062 0.959 0.851		0.50	LA	5.726 5.601 5.370 4.285 5.598 2.850 1.995
= 140.900	0.05	$\Gamma_{ m N}$	3.202 3.118 3.010 2.728 2.400 2.059 1.702 1.314 0.850			ГМ	22.037 21.633 20.604 18.820 16.445 13.568 10.277 6.632 2.986
$E_{\lambda o}$	)1	${ m L}_{ m A}^{ m N}$	1.273 1.222 1.208 1.080 0.962 0.880 0.823 0.769		0.40	LA	4.671 4.563 4.383 3.985 3.497 2.370 1.704
	0.01	N <sup>7</sup>	1.599 1.543 1.513 1.358 1.205 1.080 0.972 0.862			$\Gamma_{ m N}$	17.719 17.388 16.571 15.130 13.225 10.929 8.311 5.413
ιm,	00	$\mathbf{L}_{\mathbf{A}}^{\mathrm{N}}$	1.201 1.151 1.140 1.018 0.907 0.836 0.790 0.749 0.623		30	$\Gamma_{\mathbf{A}}^{\mathbf{N}}$	3.692 3.601 3.469 3.148 2.767 2.357 1.924 1.434 0.912
$\lambda = 0.700 \ \mu \text{m},$	0.00	$L^{N}$	1.201 1.151 1.140 1.018 0.907 0.836 0.790 0.749 0.623		0.30	$\Gamma^{ m N}$	13.479 13.220 12.609 11.508 10.063 8.338 6.380 4.216
	б	$\theta^{z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0		σ	$\theta^z$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

	$\lambda = 0.740 \ \mu \text{m},$	,mr		Ε <sub>λο</sub> =	11	128.300 mW/cm <sup>2</sup> -µm	,		$^{ m Q}_{ m LN}$	$\delta_{TN} = 0.24$
ď	0.0	0.00	0.01	)1	0.05	)5	0.10	0	0.20	0
$z_{\theta}$	LN	LA	LN	LA	$\Gamma_{ m N}$	LA	$\Gamma_{ m N}$	LA	$\Gamma_{ m N}$	LA
0.0	0.956	0.956	1.322	1.019	2.793	1.277	4.645	1.613	8.395	2.331
10.0	0.913	0.913	1.273	0.975	2.719	1.229	4.540	1.560	8.226	2.266
20.0	0.907	0.907	1.249	996.0	2.623	1.207	4.354	1.521	7.857	2.191
30.0	0.804	0.804	1.118	0.858	2.375	1.079	3.958	1.366	7.162	1.979
40.0	0.714	0.714	0.987	0.761	2.086	0.954	3.468	1.205	6.268	1.740
50.0	0.658	0.658	0.882	0.697	1.784	0.855	2.919	1.061	5.217	1.500
0.09	0.625	0.625	0.793	0.654	1.466	0.772	2.314	0.927	4.030	1.255
20.07	0.599	0.599	0.704	0.617	1.126	0.691	1.657	0.788	2.732	0.993
80.0	0.508	0.508	0.550	0.515	0.718	0.545	0.930	0.583	1.358	0.665

	—	
00	LA	10.420 10.221 9.745 8.887 7.778 6.454 4.960 3.312 1.587
1.00	LN	40.738 40.023 38.072 34.804 30.416 25.037 18.832 12.006 5.053
.5	LA	7.419 7.270 6.942 6.324 5.538 4.616 3.585 2.452 1.245
0.75	LN	30.158 29.621 28.188 25.762 22.516 18.553 13.990 8.972
0.	LA	4.859 4.752 4.552 4.137 3.627 3.048 2.413 1.718 0.953
0.50	$\Gamma_{ m N}$	20.018 19.653 18.715 17.096 14.946 12.339 9.349 6.065
01	LA	3.952 3.860 3.705 3.363 2.950 2.493 1.998 1.458
0.40	$\Gamma_{\rm N}$	16.079 15.781 15.036 13.730 12.005 9.926 7.547 4.936
08	$L_{ m A}^{ m N}$	3.110 3.032 2.919 2.644 2.322 1.977 1.612 1.217 0.753
0.30	L <sup>N</sup>	12.206 11.973 11.417 10.419 9.113 7.552 5.774 3.825 1.793
d	$\theta_{\mathrm{z}}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

													•		_
$\delta_{\text{TN}} = 0.25$ $0.20$	07	$\Gamma_{\mathbf{A}}^{\mathrm{N}}$	1.548	1.500	1.450	1.302	1.134	0.965	0.790	0.601	0.363			1.00	,
$\delta_{TN}$	0.20	$\Gamma_{ m N}$	6.396	6.263	5.971	5.426	4.718	3.884	2.938	1.907	0.834			1.0	,
	0	LA	1.050	1.011	986.0	0.879	992.0	0.665	0.570	0.467	0.315			.5	,
	0.10	$\Gamma_{\rm N}$	3.474	3.393	3.247	2.940	2.558	2.125	1.644	1.120	0.550			0.75	ļ
$= 107.500 \text{ mW/cm}^2 - \mu\text{m},$	5	${ m L}_{ m A}^{ m N}$	0.816	0.782	692.0	0.680	0.593	0.525	0.466	0.405	0.292			0	
= 107.500 n	0.05	$\Gamma_{ m N}$	2.028	1.973	1.899	1.711	1.489	1.254	1.003	0.731	0.410	:		0.50	,
$\mathrm{E}_{\lambda_0}$ :	1	LA	0.635	0.605	0.601	0.527	0.460	0.416	0.386	0.357	0.275			01	
	0.01	$\Gamma_{ m N}$	0.878	0.843	0.827	0.733	0.639	0.562	0.494	0.422	0.299			0.40	,
m,	0	$L_{\mathbf{A}}^{\mathbf{N}}$	0,591	0.562	0.560	0.489	0.428	0.390	0.367	0.345	0.271			0	
$\lambda = 0.820 \ \mu \text{m},$	0.00	$\Gamma_{ m N}$	0.591	0.562	0.560	0.489	0.428	0.390	0.367	0.345	0.271			0:30	
,	ď	$\theta_{\mathrm{z}}$	0.0	10.0	20.0	30.0	40.0	50.0	0.09	70.0	80.0			ď	

1.00	Z LA	7.075 736 6.919 97 6.595 817 5.998 7.238 5.215 886 4.291 976 3.235 813 2.082 849 0.895
	LN LN	5.040 31.314 4.923 30.736 4.701 29.197 4.269 26.617 3.712 23.138 3.067 18.886 2.335 13.976 1.537 8.613 0.699 3.249
0.75	LN	23.219 22.786 21.652 19.733 17.155 14.013 10.390 6.434
20	LA	3.291 3.208 3.072 2.782 2.420 2.014 1.561 1.068 0.531
0.50	$\Gamma_{ m N}$	15.410 15.116 14.373 13.092 11.382 9.311 6.931 4.333
0.40	LA	2.668 2.597 2.492 2.253 1.960 1.639 1.285 0.901 0.471
0.	$\Gamma_{ m N}$	12.363 12.124 11.533 10.500 9.130 7.477 5.582 3.513 1.412
0:30	LA	2.087 2.028 1.952 1.760 1.532 1.290 1.028 0.745
0	$\Gamma_{N}$	9.359 9.173 8.732 7.945 6.909 5.668 4.251 2.704
d	z <sub>\theta</sub>	0.0 10.0 20.0 30.0 40.0 50.0 60.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

				_			
= 0.19	0	$L_A^N$	1.416 1.375 1.334 1.200 1.053 0.908 0.759 0.605 0.423		1.00	LN	6.565 6.441 6.160 5.616 4.927 4.110 3.171 2.149
$\delta_{ m TN}$	0.20	$\Gamma_{ m N}$	6.319 6.196 5.922 5.407 4.742 3.954 3.058 2.078 1.042		1.	$\Gamma_{N}$	31.078 30.549 29.102 26.652 23.371 19.344 14.669 9.514
	0	LA	0.951 0.917 0.898 0.801 0.703 0.618 0.541 0.364		.5	LA	4.671 4.577 4.385 3.991 3.502 2.932 2.283 1.581 0.835
	0.10	$\Gamma_{N}$	3.403 3.328 3.192 2.905 2.548 2.142 1.691 1.203 0.674		0.75	LN	23.056 22.658 21.591 19.768 17.334 14.357 10.907 7.105
V/cm <sup>2</sup> –μm,	S	LA	0.733 0.703 0.693 0.614 0.539 0.483 0.439 0.439		0	LN	3.041 2.973 2.857 2.593 2.275 1.918 1.520 1.092 0.628
$= 96.300 \text{ mW/cm}^2 - \mu\text{m},$	0.05	LN	1.959 1.908 1.841 1.666 1.461 1.244 1.014 0.769 0.492		0.50	LN	15.298 15.027 14.328 13.111 11.497 9.535 7.269 4.775
$\rm E_{\lambda_0}$ =	1	LA	0.565 0.537 0.536 0.470 0.318 0.350 0.350 0.315			LA	2.460 2.402 2.313 2.095 1.838 1.557 1.247 0.918
	0.01	Z	0.810 0.778 0.765 0.680 0.597 0.530 0.475 0.424 0.346		0.40	z T	12.265 12.045 11.489 10.510 9.216 7.650 5.847 3.864 1.794
B,	0	LA	0.524 0.497 0.495 0.382 0.382 0.352 0.352 0.341 0.338		0	LA	1.919 1.869 1.805 1.631 1.431 1.220 0.994 0.756 0.487
$\lambda = 0.880 \ \mu \text{m},$	0.00	ZJ.	0.524 0.497 0.495 0.435 0.382 0.382 0.341 0.338		0.30	r z	9.273 9.102 8.688 7.942 6.964 5.790 4.444 2.966 1.416
^	ď	$\theta_{z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0		ď	zθ	0.0 10.0 20.0 30.0 40.0 50.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

= 0.15		LN	0.786 0.762 0.740 0.664 0.581 0.417 0.333 0.237	00		$\mathbf{L}_{\mathbf{A}}^{\mathbf{N}}$	3.759 3.686 3.528 3.222 2.827 2.361 1.835 0.641	
$\delta_{ m TN}$	0.20	LN	4.336 4.254 4.066 3.718 3.264 2.724 2.109 1.432 0.716	ı	1.00	$\Gamma^{ m N}$	21.507 21.146 20.155 18.489 16.244 13.486 10.291 6.749 3.034	
	0	LA	0.514 0.494 0.485 0.430 0.375 0.329 0.288 0.249 0.200		75	${ m L}_{ m A}^{ m N}$	2.673 2.617 2.509 2.287 2.006 1.681 1.317 0.918 0.494	
	0.10	$\Gamma_{N}$	2.289 2.240 2.148 1.957 1.717 1.441 1.133 0.799 0.440	0.75	LN	15.984 15.712 14.980 13.738 12.069 10.025 7.659 5.039 2.288		
63.300 mW/cm <sup>2</sup> -μm,	15	LN	0.386 0.368 0.365 0.320 0.279 0.227 0.209 0.183	0.50	0	$L_{ m A}^{ m N}$	1.732 1.692 1.627 1.478 1.295 1.091 0.868 0.626 0.366	
= 63.300 m	0.05	$\Gamma_{N}$	1.273 1.241 1.196 1.083 0.949 0.805 0.649 0.484 0.303		5.0	$\Gamma_{ m N}$	10.606 10.422 9.940 9.111 8.004 6.654 5.097 3.374 1.562	
$ extstyle{E}_{\lambda o}$		$L_{A}^{N}$	0.287 0.271 0.272 0.235 0.204 0.187 0.180 0.179	07.0		10	$L_{ m A}^{ m N}$	1.395 1.360 1.311 1.188 1.041 0.880 0.708 0.522 0.320
	0.01	$\Gamma_{N}$	0.465 0.446 0.438 0.388 0.298 0.264 0.234 0.194		0.40	$\Gamma_{N}$	8.494 8.344 7.962 7.295 6.407 5.330 4.090 2.720	
ım,	00	LA	0.263 0.247 0.249 0.214 0.186 0.172 0.168 0.171			10	${ m L}_{ m A}^{ m N}$	1.080 1.050 1.015 0.917 0.803 0.683 0.557 0.424
$\lambda = 1.050 \ \mu \text{m},$	0.00	$\Gamma_{ m N}$	0.263 0.247 0.249 0.214 0.186 0.172 0.168 0.171		0.30	$\Gamma_{ m N}$	6.404 6.288 6.003 5.497 4.020 3.094 2.073 0.995	
	θ	$\theta_{z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 80.0		σ	$\theta_{\mathrm{z}}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 80.0	

Table B-2. Reflected Solar Spectral Radiance (Continued)

 $E_{\lambda_0} = 46.400 \text{ mW/cm}^2 - \mu\text{m},$ 

 $\lambda = 1.250 \ \mu \text{m},$ 

 $\delta_{\rm TN}=0.13$ 

				-	<del></del>	
0	LA	0.614 0.430 0.417 0.374 0.325 0.278 0.231 0.183		00	LA	2.157 2.118 2.022 1.849 1.618 1.315 1.046 0.713 0.356
0.20	$\Gamma_{\rm N}$	2.961 2.907 2.776 2.539 2.228 1.856 1.430 0.961 0.465		1.00	LN	14.746 14.503 13.816 12.676 11.131 9.238 7.041 4.607 2.043
0.05 0.10	LA	0.285 0.274 0.269 0.237 0.206 0.179 0.156 0.134		0.50	LA	1.534 1.504 1.438 1.312 1.148 0.961 0.750 0.520 0.273
	ΓN	1.544 1.512 1.448 1.320 1.157 0.968 0.755 0.523			$\Gamma_{ m N}$	10.975 10.793 10.284 9.433 8.283 6.876 5.245 3.440 1.538
	LAN	0.211 0.200 0.199 0.173 0.149 0.132 0.120 0.120			LA	0.991 0.969 0.930 0.845 0.738 0.621 0.491 0.352 0.200
	LN	0.840 0.820 0.788 0.715 0.625 0.527 0.420 0.305			LN	7.286 7.162 6.827 6.259 5.495 4.565 3.489 2.299 1.044
	LA	0.153 0.144 0.145 0.124 0.096 0.096 0.093 0.093		0.40	Z'Z A	0.796 0.777 0.747 0.677 0.591 0.399 0.292 0.174
0.01	LN	0.279 0.267 0.263 0.232 0.201 0.175 0.175 0.153 0.132			LN	5.832 5.731 5.008 4.396 3.654 2.796 1.849 0.849
ου.0 σ	LA	0.139 0.130 0.132 0.112 0.095 0.087 0.088 0.088		0.30	LN	0.614 0.597 0.576 0.520 0.453 0.385 0.312 0.236 0.150
	LN	0.139 0.130 0.132 0.112 0.095 0.087 0.086 0.088			LN	4.390 4.313 4.115 3.769 3.307 2.751 2.110 1.404 0.656
	$\theta_{\rm z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0		d	$\theta_{z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 80.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

				_
$\delta_{TN} = 0.10$	0.20	${ m L}_{ m A}^{ m N}$	0.184 0.178 0.173 0.155 0.134 0.015 0.095 0.075	
		$\Gamma_{N}$	1.591 1.563 1.492 1.367 1.201 1.002 0.773 0.521 0.253	
$= 24.900 \text{ mW/cm}^2 - \mu \text{m},$	0.10	$L_{ m A}^{ m N}$	0.116 0.111 0.110 0.096 0.083 0.072 0.063 0.054	
		$\Gamma_{ m N}$	0.820 0.804 0.769 0.702 0.617 0.516 0.402 0.277	
	0.05	LA	0.084 0.080 0.080 0.069 0.059 0.052 0.047 0.044	
		ηT	0.436 0.426 0.409 0.372 0.374 0.217 0.155 0.089	
. Ε <sub>λο</sub>	0.01	$\mathbb{L}_{A}^{N}$	0.060 0.056 0.056 0.048 0.040 0.036 0.035 0.036	
		$_{ m N}$ T	0.130 0.125 0.122 0.108 0.094 0.081 0.069 0.058	
.m,	0	$L_{A}^N$	0.054 0.050 0.051 0.042 0.036 0.033 0.032 0.033	وسندر بروسوس ورده والاراد والوارد والمار
$\lambda = 1.600 \ \mu \text{m}$	0.00	$\Gamma_{ m N}$	0.054 0.050 0.051 0.042 0.036 0.033 0.032 0.035	
-	σ	$\theta^{z}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0	

00	$L_{\mathbf{A}}^{\mathbf{N}}$	0.913 0.895 0.857 0.783 0.687 0.575 0.447 0.306
1.00	$\Gamma_{N}$	7.948 7.818 7.452 6.844 6.021 5.011 3.837 2.534 1.156
5	$L_{ m A}^{ m N}$	0.649 0.635 0.609 0.555 0.487 0.408 0.320 0.223 0.120
0.75	$\Gamma_{ m N}$	5.925 5.827 5.555 5.101 4.487 3.735 2.862 1.894 0.869
0	${ m L}_{ m A}^{ m N}$	0.418 0.408 0.392 0.356 0.312 0.262 0.208 0.149
0.50	$\Gamma_{ m N}$	3.936 3.870 3.890 3.387 2.979 2.480 1.903 1.263 0.586
0:	LA	0.335 0.326 0.314 0.285 0.249 0.210 0.168 0.123 0.075
0.40	$\Gamma_{N}$	3.149 3.095 2.953 2.709 2.382 1.984 1.524 1.014 0.474
0	$\mathbf{L}_{\mathbf{A}}^{\mathbf{N}}$	0.257 0.250 0.241 0.217 0.190 0.161 0.130 0.098 0.098
0.30	$\Gamma_{N}$	2.367 2.327 2.220 2.036 1.790 1.148 0.767 0.363
ď	$\theta_{\mathrm{z}}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

Table B-2. Reflected Solar Spectral Radiance (Continued)

$E_{\lambda_0} = 8.300 \text{ mW/cm}^2 - \mu \text{m},$ $\delta_{TN} = 0.13$	0.10 0.20	LA	0.040 0.039 0.038 0.033 0.029 0.019 0.015		0.75	LA	0.200 0.196 0.188 0.170 0.149 0.023 0.061
		LN	0.471 0.462 0.440 0.402 0.351 0.289 0.218 0.140 0.058	] ]		$\Gamma_{ m N}$	2.355 2.315 2.202 2.013 1.759 1.447 1.084 0.686 0.273
		LA	0.025 0.024 0.024 0.021 0.018 0.015 0.013 0.010			LA	0.142 0.139 0.133 0.120 0.105 0.087 0.066 0.044
		$\Gamma_{ m N}$	0.241 0.236 0.225 0.205 0.179 0.112 0.073			$\Gamma_{ m N}$	1.758 1.728 1.644 1.503 1.313 1.080 0.810 0.513 0.205
	0.05	LA	0.018 0.017 0.017 0.015 0.013 0.009 0.009		0.50	$L_{\mathbf{A}}^{\mathrm{N}}$	0.092 0.089 0.086 0.077 0.067 0.043 0.029 0.015
		$\Gamma_{N}$	0.126 0.123 0.118 0.107 0.093 0.077 0.059 0.040			$\Gamma^{N}$	1.169 1.149 1.093 0.999 0.873 0.718 0.539 0.342
	0.01	LA	0.013 0.012 0.012 0.010 0.008 0.007 0.007 0.007		0.40	$\mathbb{L}_{\mathbf{A}}^{\mathrm{N}}$	0.073 0.071 0.069 0.062 0.054 0.045 0.035 0.035
		$\Gamma_{N}$	0.034 0.033 0.032 0.028 0.024 0.021 0.017 0.013			Γ <sub>N</sub>	0.935 0.919 0.874 0.799 0.698 0.574 0.431 0.274
$\lambda = 2.200 \ \mu \text{m},$	0.00	${ m L}_{ m A}^{ m N}$	0.011 0.010 0.010 0.001 0.007 0.007 0.006 0.006		0	LA	0.056 0.054 0.053 0.047 0.034 0.037 0.019 0.019
		$\Gamma^{ m N}$	0.011 0.010 0.011 0.009 0.007 0.006 0.006	0:30	LN	0.702 0.690 0.657 0.600 0.524 0.431 0.324 0.207	
	ď	$\theta_z$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0		ď	$\theta^{\mathrm{z}}$	0.0 10.0 20.0 30.0 40.0 50.0 60.0 70.0

### APPENDIX C

### SENSOR FIELD OF VIEW

Each time the satellite completes an orbit around the Earth, it maps out a swath on the Earth's surface of width  $S_w$ . The angle subtended at the satellite by  $S_W$  is the sensor field of view  $\Theta$ . Referring to Figure 1 and using the law of cosines, one can write

$$\Theta = 2 \text{ Cos}^{-1} \left( \frac{R^2_S + S^2_d - R^2_e}{2S_d R_S} \right) \text{ [rad] }, \tag{C-1}$$

where

$$R_S = H + R_e \quad [km] \tag{C-2}$$

and

$$S_{d} = \left[ R_{S}^{2} + R_{e}^{2} - 2R_{S}R_{e} \cos\left(\frac{\Phi_{S}}{2}\right) \right]^{1/2}$$
 [km] (C-3)

From Figure 1, it can also be seen that

$$\Phi_{S} = \frac{S_{W}}{R_{e}} \quad [rad] . \tag{C-4}$$

The swath width S<sub>W</sub> is given by

$$S_{W} = \frac{Ad_{C}}{N_{S}} \quad [km] \tag{C-5}$$

where  $d_C$  is the cross-track distance covered by the sensor and, for total coverage at the equator, is given by

$$d_{C} = 2\pi R_{e} \quad [km] . \tag{C-6}$$

Now, if the total time required to map the Earth  $t_{MAP}$  is known, then the total number of swaths  $N_S$  required to map the Earth is

$$N_{S} = \frac{t_{MAP}}{t_{S}} \quad [nd] , \qquad (C-7)$$

where t<sub>S</sub> is the satellite's orbital period or the time required to map one swath and is given by

$$t_{S} = \frac{2\pi R_{e}}{V_{SUB}} \quad [sec] \quad . \tag{C-8}$$

Finally, the cross-track overlap factor A is given by,

$$A = \left(1 + \frac{S'_0}{100}\right) \quad [nd] , \qquad (C-9)$$

where S  $_{\rm O}^{\prime}$  is the percentage overlap across the ground track.

### APPENDIX D

# VIEW FACTOR FOR A SINGLE DETECTOR VIEWING A CIRCULAR BACKGROUND

The view factor  $F_C$  for a detector that is receiving radiation from a circular background can be defined as

$$F_{C} = \frac{\Phi'}{\pi A_{D} L'_{\Lambda \lambda}} \quad [nd] , \qquad (D-1)$$

where  $\Phi'$  = the photon flux into the detector [p/sec],

 $A_D$  = the area of the detector [cm<sup>2</sup>],

and

$$L'_{\Delta\lambda} = \int_{0}^{\lambda_c} B'(\lambda, T_{BG}) d\lambda \qquad [p/\text{sec-cm}^2 - \text{sr}] , \qquad (D-2)$$

where  $B'(\lambda, T_{BG})$  = Planck's function evaluated at the background temperature  $T_{BG}$ , and  $\lambda_c$  = the detector cutoff wavelength.

If a detector of area  $A_D$  views a source of radiance  $L'_{\Delta\lambda}$  with area dA' through a solid angle  $\Omega$ , the flux into the detector is

$$d\Phi' = L'_{\Delta\lambda}\Omega \operatorname{Cos}(\phi'_{c}) dA' \qquad [p/\text{sec}] . \tag{D-3}$$

The angle  $\phi'_c$  is shown in Figure D-1.

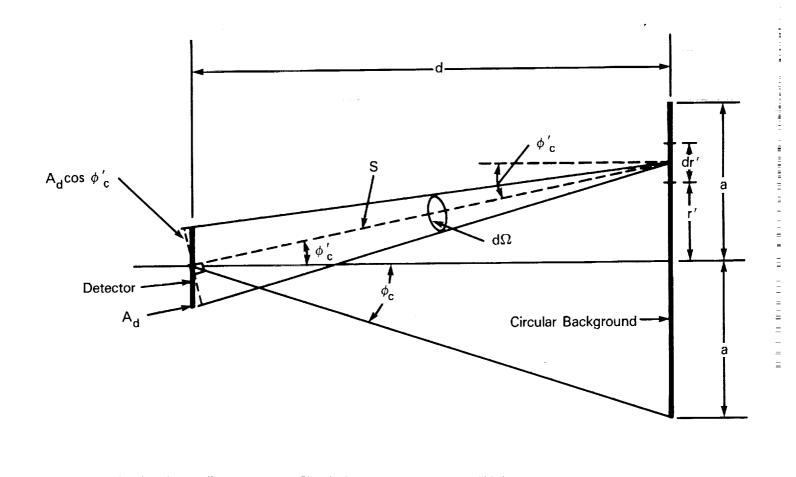
However,

$$dA' = 2\pi r' dr' \qquad [cm^2] \tag{D-4}$$

and

$$\Omega = \frac{A_D \cos(\phi'_c)}{s^2} \quad [sr] \quad (D-5)$$

Substituting Equations (D-4) and (D-5) into Equation (D-3) gives



= Circular background radius (cm)

= Area of detector  $(\mu m)$ 

= Distance between the detector and the circular background (cm)

 $dA' = 2\pi r' dr' = Area of elemental annular ring of radius r' (cm<sup>2</sup>)$ 

= Distance from center of detector to elemental area on circular background (cm)

= Half angle subtended by the circular background at the center of the detector (deg)

= Half angle subtended by the elemental circular area dA' at the center of the detector (deg)

 $\phi_c'$  = Half angle subtended by the detector at a point on the elemental area dA' (sr)

Figure D-1. View Factor Geometry for a Single Detector Viewing a Circular Background

$$d\Phi' = \frac{2\pi r A_D L'_{\Delta\lambda} \cos^2(\phi'_c) dr'}{S^2} \qquad [p/sec] . \tag{D-6}$$

However, from Figure D-1 we see that

$$\cos \phi_{\rm c}' = \frac{\rm d}{\rm S} = \frac{\rm d}{\left({\rm d}^2 + {\rm r}'^2\right)^{1/2}}$$
 [rad], (D-7)

and substituting Equation (D-7) into Equation (D-6) gives

$$d\Phi' = 2\pi d^2 A_D L'_{\Delta\lambda} \frac{r' dr'}{(d^2 + r'^2)^2}$$
 [p/sec] . (D-8)

It follows that

$$\Phi' = 2\pi d^2 A_D L'_{\Delta\lambda} \int_0^a \frac{r' dr'}{(d^2 + r'^2)^2} \qquad [p/sec] .$$
 (D-9)

However,

$$\int_{0}^{a} \frac{r' dr'}{(d^{2} + r'^{2})^{2}} = \frac{1}{2 d^{2}} - \frac{1}{2(d^{2} + a^{2})}.$$
 (D-10)

Therefore, substituting Equation (D-10) into Equation (D-9) gives

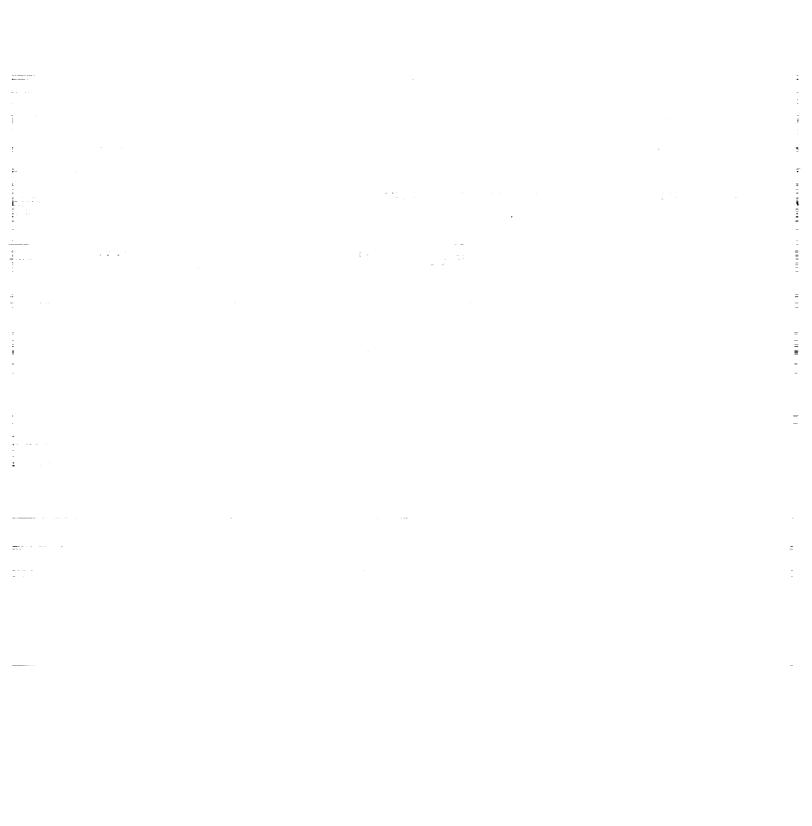
$$\Phi' = \pi A_D L'_{\Delta \lambda} \left( 1 - \frac{d^2}{d^2 + a^2} \right) [p/sec] . \qquad (D-11)$$

However,

$$\frac{d}{\left(d^2 + a^2\right)^{1/2}} = \frac{d}{S_a} = \cos \phi_c \quad [nd] . \tag{D-12}$$

Therefore, by substituting Equation (D-12) into Equation (D-11) we obtain

$$\Phi' = \pi A_D L'_{\Delta \lambda} \sin^2 \phi_c \quad [p/\text{sec}] . \tag{D-13}$$



### APPENDIX E

# VIEW FACTOR FOR A DETECTOR IN AN n X m ARRAY VIEWING A RECTANGULAR BACKGROUND

The view factor  $F_A$  for a detector in an n by m array viewing a rectangular background (Figure E-1) is given by

$$F_{A} = \frac{\Phi'}{\pi A_{D} L'_{\Delta \lambda}} \tag{E-1}$$

where  $\Phi'$  is the total number of photons per second entering the detector from the background through a rectangular aperture, given by

$$\Phi' = L'_{\Delta\lambda} \int_{0}^{A_b} \Omega_d \cos \phi_f \, dA_B \qquad [p/sec]$$
 (E-2)

and, as in Appendix D,  $L'_{\Delta\lambda}$  is

$$L'_{\Delta\lambda} = \int_{0}^{\lambda_{c}} B'(\lambda, T_{BG}) d\lambda \qquad [p/sec-cm^{2}-sr]$$

where the photon radiance  $L'_{\Delta\lambda}$  is given by Equation (E-2) and

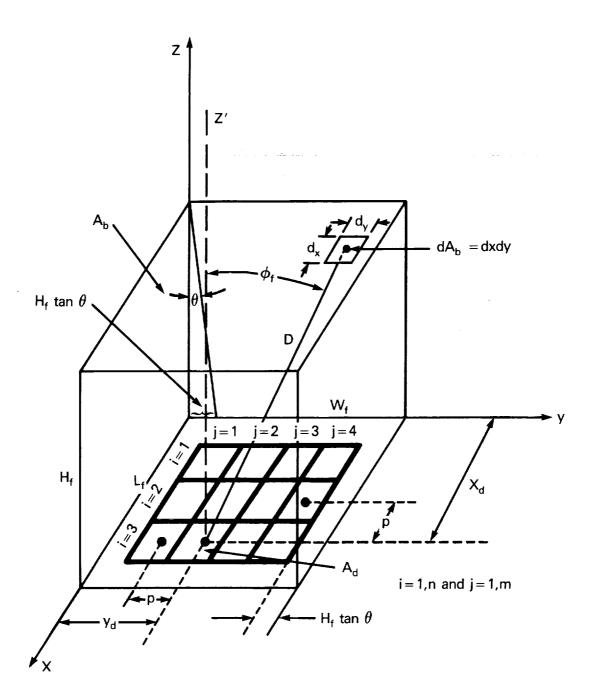
where  $B'(\lambda, T_{BG})$  = the Planck function evaluated at the background temperature  $T_{BG}$  [p/sec-cm<sup>2</sup>-sr- $\mu$ m];

 $\Omega_{\mathrm{D}}$  = the solid angle subtended by the detector at an arbitrary point on the rectangular aperture through which the background is viewed;

 $dA_R$  = the differential area on the background; and

 $\phi_{\rm f}$  = the angle between the normal to the differential area dA<sub>B</sub> and the line between the center of the detector and the center of the differential area dA<sub>B</sub>.

If D is the distance between the center of the detector and the differential area dAB then



 $A_b$  = Background area (cm<sup>2</sup>)

 $A_d$  = Detector area ( $\mu$ m<sup>2</sup>)

D = Distance from center of detector to  $dA_b$  (cm)

 $dA_b$  = Differental background area (cm<sup>2</sup>)

H<sub>f</sub> = Fence height (cm)
L<sub>f</sub> = Fence length (cm)
p = Detector pitch (cm)
W<sub>f</sub> = Fence width (cm)

heta = Optics half-cone angle (deg)  $\phi_{\rm f}$  = Differential area normal angle

Figure E-1. Geometry for a Detector in n X m Array Viewing a Rectangular Background

$$\Omega_{\rm d} = \frac{A_{\rm d} \cos(\phi_{\rm f})}{D^2} \quad [sr] , \qquad (E-3)$$

where

$$Cos(\phi_f) = \frac{z}{D} \qquad [nd] . \tag{E-4}$$

To evaluate the quantities D,  $\phi_f$ , and z in Equations E-3 and E-4, it is convenient to define two sets of coordinates. The two systems (x,y,z) and (x',y',z') are shown in Figure E-1. The n X m detector array lies in the x-y plane and the plane of the rectangular aperture, through which the background is viewed, is a distance  $H_f$  from the x-y plane.

Consider an n  $\times$  m array of detectors, and let p be the pitch (distance between detector centers) in both directions (Figure E-1). Let the detector array be symmetrically surrounded by very cold sides (fence) of length  $L_f$ , width  $W_f$ , and height  $H_f$ . The length and width are adjusted for a given height so that the edge detectors in the array can just accommodate the optical bundle which is defined by half the bundle cone angle  $\theta$ . The relationships for the length  $L_f$  and width  $W_f$  of the fenced area that surrounds the detector array are

$$L_f = np + 2H_f Tan(\theta) \quad [m] , \qquad (E-5)$$

and

$$W_f = mp + 2H_f Tan(\theta) \quad [m] , \qquad (E-6)$$

where n = the number of detectors along the length of the detector array, and

m = the number of detectors along the width of the detector array.

Equations (E-5) and (E-6) follow because

$$Sin(\theta) = \frac{1}{2f_n} . ag{E-7}$$

The coordinates of detector i, j with respect to the edges of the fenced area are given by

$$x_{d} = H_f \operatorname{Tan}(\theta) - \frac{p}{2} + ip$$
 (E-8)

and

$$y_d = H_f \operatorname{Tan}(\theta) - \frac{p}{2} + jp , \qquad (E-9)$$

where i = the number of detectors along the fence length, (i = 1, ..., n) and

j = the number of detectors along the fence width, (j = 1, ..., m).

The coordinates of the arbitrarily placed differential area  $dA_B$  on the surface formed by the top edges of the fence are (x,y,z). The coordinates with respect to the center of the detector i, j are given by

$$\mathbf{x}' = \mathbf{x} - \mathbf{x}_d , \qquad (E-10)$$

$$y' = y - y_d , \qquad (E-11)$$

and

$$z' = z , (E-12)$$

where

$$z = H_f ag{E-13}$$

and

$$D = (x'^2 + y'^2 + z'^2)^{1/2} . (E-14)$$

By substituting Equations (E-10) through (E-13) into Equation (E-14), one gets

$$D = \left[ \left( x - x_d \right)^2 + \left( y - y_d \right)^2 + z^2 \right]^{1/2} . \tag{E-15}$$

Letting

$$dA_{h} = dx dy ag{E-16}$$

and substituting Equations (E-3), (E-4), (E-13), and (E-16) into Equation (E-2) results in

$$\Phi' = A_D H_f^2 B' \Delta \lambda$$

$$\begin{cases} W_f \\ \frac{dx \ dy}{D^4} \end{cases}$$
[p/sec] . (E-17)

Substituting Equation (E-17) into Equation (E-1) yields

$$F_{A} = \frac{H_{f}^{2}}{\pi} \int_{0}^{W_{f}} g(y) dy , \qquad (E-18)$$

where

$$g(y) = \int_0^{L_f} \frac{dx}{D^4} . \tag{E-19}$$

Equation (E-19) may also be written as

$$g(y) = \int_0^{L_f} \frac{dx}{x^2} , \qquad (E-20)$$

where

$$X = ax^2 + bx + c ag{E-21}$$

$$a = 1 (E-22)$$

$$b = -2x_d (E-23)$$

and

$$c = x_d^2 + (y - y_d)^2 + z^2$$
 (E-24)

It follows from Equations (E-22) through (E-24) that

$$4ac - b^2 = 4(y - y_d)^2 + 4z^2$$
 (E-25)

Now, Equation (E-25) reveals that

$$4ac > b^2$$
 . (E-26)

Therefore, Equation (E-20) may be written (Dwight, 1947, p. 33, Equations 160.01 and 160.02) as

$$\int \frac{dx}{X^2} = \frac{2ax + b}{rX} + \frac{4a}{R_2} - Tan^{-1} \left( \frac{2ax + b}{R_1} \right) , \qquad (E-27)$$

where

$$r = 4ac - b^2 ag{E-28}$$

and

$$R_1 = r^{1/2} = \left(4ac - b^2\right)^{-1/2}$$
 (E-29)

and

$$R_2 = rR_1 = r^{3/2}$$
 (E-30)

Applying Equation (E-27) to Equation (E-28), one gets

$$g(y) = \frac{2aL_f + b}{r\left(aL_f^2 + bL_f + c\right)} + \frac{4a}{R_2} Tan^{-1} \left(\frac{2aL_f + b}{R_1}\right)$$
$$-\frac{b}{rc} - \frac{4a}{R_2} Tan^{-1} \left(\frac{b}{R_1}\right)$$
(E-31)

Use of Equation (E-31) in Equation (E-18) and numerical integration enable the form factor F<sub>A</sub> to be computed.

# APPENDIX F

# COMPUTATION OF $\gamma$

Substituting Equations (2-11) and (2-12) into Equation (2-9) yields

$$S' = t_I \tau_o A_D \eta \left(\frac{\lambda}{hc}\right) \left(\frac{\pi}{4f^2_N}\right) \int_{\lambda_1}^{\lambda_2} L(\lambda) d\lambda \quad [e] . \tag{F-1}$$

Therefore, the signal equation for the visible and SWIR bands is given by

$$S' = t_I \tau_o A_D \eta \left(\frac{\lambda}{hc}\right) \left(\frac{\pi}{4f^2 N}\right) L \Delta \lambda \quad [e]$$
 (F-2)

where we have replaced the integral in Equation (F-1) by  $L\Delta\lambda$  because  $L(\lambda)$  varies slowly over the spectral bandpass  $\Delta\lambda$ . Taking the differential of Equation (F-2) with respect to the scene radiance, one obtains

$$dS' = t_I \tau_o A_D \eta \left(\frac{\lambda}{hc}\right) \left(\frac{\pi}{4f^2_N}\right) dL \Delta \lambda \quad [e] . \qquad (F-3)$$

Dividing Equation (F-2) by (F-3) gives

$$\frac{S}{N} = \frac{S'}{dS'} = \frac{L}{dL} \quad [nd]$$
 (F-4)

where the signal S = S', and the noise N = dS'.

However,

$$dL = \left(\frac{dL}{d\rho}\right) d\rho \qquad [W/cm^2 - sr - \mu m] . \tag{F-5}$$

Substituting Equation (F-5) into Equation (F-4) gives

$$\frac{S}{N} = \frac{L}{\left(\frac{dL}{d\rho}\right) d\rho} \quad [nd] . \tag{F-6}$$

Letting

$$\gamma \equiv \frac{L}{\left(\frac{dL}{d\rho}\right)} \quad [nd] , \qquad (F-7)$$

$$d\rho \equiv NE\Delta\rho \tag{F-8}$$

and substituting Equations (F-7) and (F-8) into Equation (F-5), one obtains

$$\frac{S}{N} = \frac{\gamma}{NE\Delta\rho} \ . \tag{F-9}$$

However,

$$L = L_S^S + L_A^S \quad [W/cm^2 - sr - \mu m]$$
 (F-10)

where the surface spectral radiance  $\boldsymbol{L}_{S}^{S}$  has the functional form

$$L_S^S = \rho K_1 \qquad [W/cm^2 - sr - \mu m] \tag{F-11}$$

and the atmospheric spectral radiance is a constant with respect to  $\rho$  and is given by

$$L_{A}^{S} = K_{2} \quad [W/cm^{2}-sr-\mu m]$$
 (F-12)

The superscript S denotes that the sensor observes these spectral radiances along a slanted path. (See Figure 6.) Since the scene spectral radiances are assumed to be equal in the normal and slant directions, no superscript is used.

Substituting Equations (F-11) and (F-12) into Equation (F-10) gives

$$L = K_1 \rho + K_2 \quad [W/cm^2 - sr - \mu m]$$
 (F-13)

Differentiating Equation (F-13) with respect to  $\rho$  results in

$$\frac{dL}{d\rho} = K_1 \quad [W/cm^2 - sr - \mu m] \tag{F-14}$$

Solving for  $K_1$  in Equation (F-11) and substituting it into Equation (F-14) results in

$$\frac{dL}{d\rho} = \frac{L_S^S}{\rho} \quad [W/cm^2 - sr - \mu m] . \tag{F-15}$$

Substituting Equation (F-15) into Equation (F-7) gives

$$\gamma = \left(\frac{L}{L_S^S}\right) \rho \quad [nd] \quad . \tag{F-16}$$

The spectral radiances L and L<sub>S</sub><sup>S</sup> are observed along the line-of-sight direction with angle of  $\phi$  and a line-of-sight surface-normal angle  $\phi'$  (Figure 6). These angles are related by

$$\phi' = \sin^{-1} \left[ \left( 1 + \frac{H}{R_e} \right) \sin \phi \right] \quad [rad] \quad . \tag{F-17}$$

The surface spectral radiance LS is given by

$$L_{S}^{S} = \frac{E_{S}}{\pi} \rho \tau_{AN}^{Sec}(\phi') \qquad [W/cm^{2}-sr-\mu m]$$
 (F-18)

where  $E_S$  = the irradiance at the surface of the Earth [W/cm<sup>2</sup>- $\mu$ m]

The atmospheric transmission along the nadir direction is given by

$$\tau_{AN} = e^{-\delta_0} \quad [nd] , \qquad (F-19)$$

where  $\delta_0$  is the optical depth along the nadir direction. (See Appendix B)

The surface spectral radiance  $L_S$  observed along the nadir direction (for which  $\phi' = 0$ ) is given by

$$L_{\rm S}^{\rm N} = \frac{E_{\rm S}}{\pi} \rho \tau_{\rm AN} \qquad [W/cm^2 - sr - \mu m] . \qquad (F-20)$$

Dividing Equation (F-18) by Equation (F-19) gives

$$L_S^S = L_S^N \tau_{AN}^{(Sec \phi' - 1)} \qquad [W/cm^2 - sr - \mu m] .$$
 (F-21)

Substituting Equation (F-21) into Equation (F-16) we obtain

$$\gamma = \frac{\gamma_0}{\tau_{AN}^{(Sec \ \phi' - 1)}} \quad [nd]$$

where

$$\gamma_{\rm o} = \frac{L\rho}{L_{\rm S}^{\rm N}} \qquad [\rm nd] . \tag{F-23}$$

We assume the total spectral radiance L is the same along the nadir and slant directions; hence

$$L = L_S^N + L_A^N \qquad [W/cm^2 - sr - \mu m]$$
 (F-24)

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$$L_S^N = L - L_A^N \quad [W/cm^2 - sr - \mu m] .$$
 (F-25)

Substituting Equation (F-25) into Equation (F-23) gives

$$\gamma_{0} = \left[\frac{L}{L - L_{A}^{N}}\right] \rho \quad [nd]$$
 (F-26)

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$$\gamma_{\rm o} = \frac{\rho}{\left[1 - \frac{L_{\rm A}^{\rm N}}{L}\right]} \quad [nd] . \tag{F-27}$$

### APPENDIX G

# NOISE EQUIVALENT DELTA TEMPERATURE

Equation (2-9) enables the signal to be written as

$$S' = t_I A_D \eta E'_{\Delta \lambda} \quad [e] , \qquad (G-1)$$

where

$$E'_{\Delta\lambda} = \int_{\lambda_1}^{\lambda_2} E'(\lambda) d\lambda \qquad [p/\text{sec-cm}^2] . \tag{G-2}$$

However,

$$E'(\lambda) = \frac{\pi \tau_0}{4f^2_N} L'(\lambda) \qquad [p/sec-cm^2 - \mu m]$$
 (G-3)

and

$$L'(\lambda) = \tau_{A}B'(\lambda, T_{S}) + \epsilon_{A}B'(\lambda, T_{A}) \qquad [p/\text{sec-cm}^{2} - \text{sr-}\mu\text{m}] . \tag{G-4}$$

Therefore,

$$E'_{\Delta\lambda} = \frac{\pi \tau_o}{4f^2_N} \quad L'_{\Delta\lambda} \qquad [p/sec-cm^2]$$
 (G-5)

where

$$L'_{\Delta\lambda} = \int_{\lambda_1}^{\lambda_2} L'(\lambda) d\lambda \qquad [p/\text{sec-cm}^2 - \text{sr}] . \tag{G-6}$$

Equation (G-4) can be written as

$$L'_{\Delta\lambda} = \tau_A L'_{S\Delta\lambda} + \epsilon_A L'_{A\Delta\lambda} \qquad [p/\text{sec-cm}^2 - \text{sr}] , \qquad (G-7)$$

where

$$L'_{S\Delta\lambda} = \int_{\lambda_1}^{\lambda_2} B'(\lambda, T_S) d\lambda \qquad [p/\text{sec-cm}^2 - \text{sr}]$$
 (G-8)

and

$$L'_{A\Delta\lambda} = \int_{\lambda_1}^{\lambda_2} B'(\lambda, T_A) d\lambda \qquad [p/sec-cm^2-sr] . \tag{G-9}$$

Taking the differential of Equation (G-1), one obtains

$$dS' = (t_1 A_D \eta) dE'_{\Delta \lambda} \quad [e] . \tag{G-10}$$

Replacing dS' by N, and dE' $_{\Delta\lambda}$  by NEI results in

$$N = (t_I A_D \eta) \text{ NEI} \qquad [e] , \qquad (G-11)$$

where N =the total noise [e], and

NEI = the noise equivalent photon irradiance into the detector [p/sec-cm<sup>2</sup>].

Taking the differential of Equation (G-5) gives

$$dE'_{\Delta\lambda} = \frac{\pi \tau_0}{4f^2_N} dL'_{\Delta\lambda} \qquad [p/sec-cm^2] . \qquad (G-12)$$

Replacing  $dE'_{\Delta\lambda}$  by NEI, and  $dL'_{\Delta\lambda}$  by the noise equivalent photon radiance (NEPR) gives

$$NEI = \frac{\pi \tau_0}{4f^2_N} \quad NEPR \qquad [p/sec-cm^2] . \tag{G-13}$$

Taking the differential of Equation (G-7) gives

$$dL'_{\Delta\lambda} = \tau_A dL'_{S\Delta\lambda} + \epsilon_A dL'_{A\Delta\lambda} \qquad [p/sec-cm^2-sr] . \tag{G-14}$$

However, since we are not interested in perturbations due to changes in the atmosphere, we assume  $L'_{A\Delta\lambda}$  is to be constant. Equation (G-14) then becomes

$$dL'_{\Delta\lambda} = \tau_A dL'_{S\Delta\lambda}$$
 [p/sec-cm<sup>2</sup>-sr] . (G-15)

Replacing  $dL'_{\Delta\lambda}$  with NEPR, and  $dL'_{S\Delta\lambda}$  with the surface NEPR, NEPR<sub>S</sub> in Equation (G-15), gives

$$NEPR = \tau_A NEPR_S \qquad [p/sec-cm^2-sr] . \qquad (G-16)$$

However, by definition,

$$dL'_{S\Delta\lambda} \equiv \frac{dL'_{S\Delta\lambda}}{dT_{S}} dT_{S} \qquad [p/\text{sec-cm}^{2}-\text{sr}]$$
 (G-17)

or

$$dT_{S} = \frac{dL'_{S\Delta\lambda}}{\left(\frac{dL'_{S\Delta\lambda}}{dT_{S}}\right)} \quad [K] . \tag{G-18}$$

Replacing dT  $_S$  with NEDT and dL'  $_{S\Delta\lambda}$  with NEPR  $_S$  in Equation (G-18) yields

$$NE\Delta T = \frac{NEPR_S}{\left(\frac{dL'_S\Delta\lambda}{dT_S}\right)} \quad [K]$$
 (G-19)

and

$$\frac{dL'_{S}\Delta\lambda}{dT_{S}} = \int_{\lambda_{1}}^{\lambda_{2}} \frac{dB(\lambda, T_{S}) d\lambda}{dT_{S}} \qquad [p/sec-cm^{2}-K] , \qquad (G-20)$$

where the Planck function is given by

$$B'(\lambda, T_S) = \frac{C_1'}{\lambda^4} \frac{1}{\left[\exp\left(\frac{C_2}{\lambda T_S}\right) - 1\right]} \quad [p/\sec-cm^2-sr-\mu m] . \tag{G-21}$$

Differentiating Equation (G-21) with respect to T<sub>S</sub> yields

$$\frac{dB'(\lambda, T_S)}{dT_S} = \frac{C_2 \lambda^3 \left(B'(\lambda, T_S)\right)^2 \exp\left(\frac{C_2}{\lambda T_S}\right)}{C'_1 T_S^2} \qquad [p/sec-cm^2-sr-\mu m-K] . \tag{G-22}$$

Equation (G-19) may be written in terms of signal-to-noise ratio (S/N) as follows. Dividing Equation (G-1) by Equation (G-11) gives

$$\frac{S}{N} = \frac{E'\Delta\lambda}{NEI} \quad [nd] . \tag{G-23}$$

Substituting Equations (G-5) and (G-13) into Equation (G-23) and replacing  $dL'_{\Delta\lambda}$  with NEPR gives

$$\frac{S}{N} = \frac{L'_{\Delta\lambda}}{NEPR} \quad [nd] . \tag{G-24}$$

Substituting Equation (G-16) into Equation (G-24) gives

$$\frac{S}{N} = \frac{L'_{\Delta\lambda}}{\tau_{\Delta} NEPR_{S}} \quad [nd]$$
 (G-25)

or

NEPR<sub>S</sub> = 
$$\frac{L'_{\Delta\lambda}}{\tau_A \left(\frac{S}{N}\right)}$$
 [p/sec-cm<sup>2</sup>-sr] (G-26)

and, finally, by substituting Equation (G-26) into Equation (G-19), one obtains

$$NE\Delta T = \frac{L'_{\Delta\lambda}}{\tau_A \left(\frac{S}{N}\right) \left(\frac{dL'_S}{dT_S}\right)} \quad [K] . \tag{G-27}$$

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