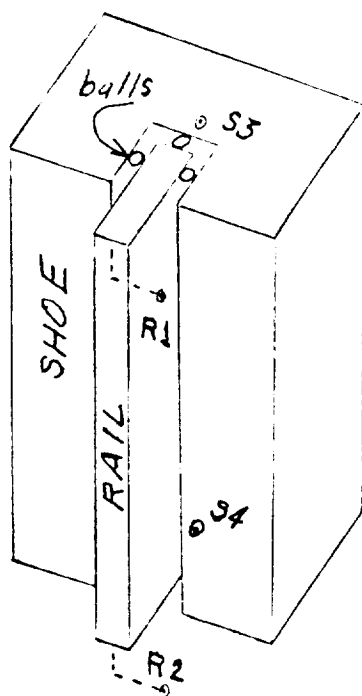


N91-20510

## MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

Thomas G. Butler  
BUTLER ANALYSES

The focus of this paper is on joints that are only partially connected such as slip joints in bridges and in ship superstructures or sliding of a grooved structure onto the rails of a mating structure as shown in the sketch.



In substructure analysis it is desirable to organize each substructure so as to be self contained for purposes of validity checking. If part of the check is to embrace a connection, then all of the elements of the interface that it sees in

## MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

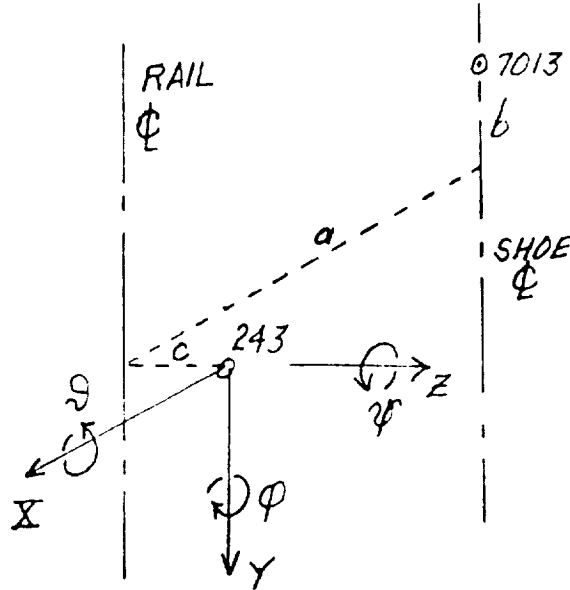
its mate should be included within its model. In the case of the groove/rail structure, shown above, it will enhance the checking if the rail points, to which the shoe points will connect, are duplicated in the substructure with the shoe. Thus a complete job of checking out the shoe substructure can be done in Phase 1 with statics and eigenvalues and not protract the checking procedure of basic substructures into Phase 2.

To implement such a scheme, referring to the sketch, points R1 & R2 are included in the shoe model. The connection from S3 to R1 and from S4 to R2 are made in Phase 1 and now become available for complete checkout of the shoe substructure, including its mating with the rail. To make this example general, postulate that the planes through the four points are not parallel to the coordinate planes. In effect there are offsets. Generally, one likes to plan to avoid having out-of-plane offsets, but exigencies do crop up which forces the analyst to face up to such realities. Often such interface connections involve MPC's or elastic ties. In any case a requirement of Substructure Analysis is that points that are to be connected in Phase 2 must be available in Phase 2; i.e. they cannot be condensed out or constrained out in Phase 1. Therefore, if an MPC is used, the connecting points must be the independent degrees of freedom in the MPC relationship.

The needs of this joint are that there will be no relative translation in either transverse direction and no relative rotation about the long axis of the rail. In terms of the indicated coordinate system, translations in x and z directions must be constrained together and rotations about y must be constrained together. Just a pair of connecting points will be used herein to carry on the discussion. A sketch will be used to

## MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

assist in the discussion of making the connection by means of multi-point constraints.



Include rail point 243 in the Shoe Model. When Phase 2 COMBINE operation is invoked, NASTRAN will recognize that rail 243 = shoe 243. As remarked above, since point 243 is going to be commanded to connect in Phase 2, it must therefore be an active available point for joining; and must therefore be an independent point in an MPC relationship. Now following the needs of this joint, constrain point 7013(X,Z,ϕ) to 243(X,Z,ϕ). The constraint equations for translations in X and Z are:

$$7013(X) = 243(X) - c \times 243(\phi) + b \times 243(\psi)$$

$$7013(Z) = 243(Z) + a \times 243(\phi) - b \times 243(\theta).$$

But 243(ψ) and 243(θ) are rail rotations which are not sensed by the shoe. If 243(4,6) are included in the shoe model they would be independent shoe rotations which will engage in the MPC relationship but would have no elastic path out to other parts of

## MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

the shoe. Thus, if nominal mass were added to these rail points to keep the eigenvalue matrix from being singular, an eigenvalue check for rigid body modes would show the shoe model to fail. One might argue, why not leave the rotations in until they are connected during COMBINE, then they are no longer disjoint. I cannot afford to leave the 243(4,6) rotations in the shoe model, because after connecting with the rail these rail rotations must not be transmitted back to the shoe. Moments in the shoe/rail configuration about the two transverse axes are produced only by couples of forces not by local rotational bending. This rules out the use of MPC's during Phase 1 in this case. There are other cases of connections between substructures in which MPC's in Phase 1 would work. The case in which there were no transverse offsets would work. A NASTRAN run of a simple model demonstrates these results in Appendix A.

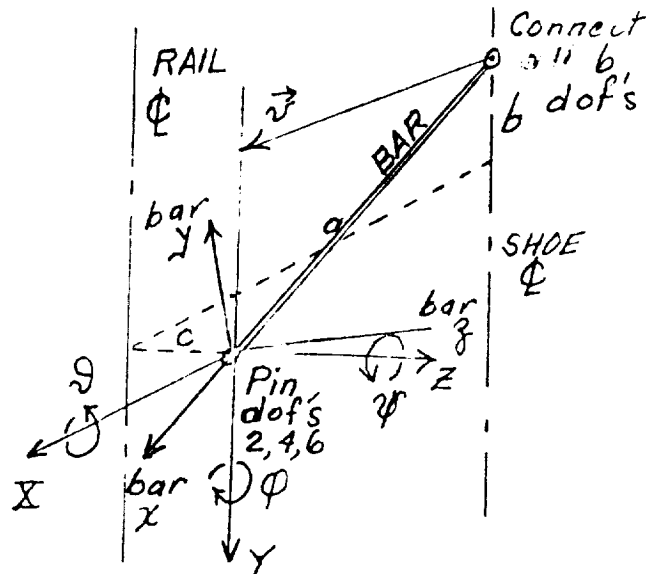
The alternative is to make a stiff elastic connection, but not so stiff as to cause matrix ill-conditioning. If a bar instead of elastic scalars is used, it will be modeled so as to be fully connected in all 6 degrees of freedom at the shoe end, but only partially connected at the rail end. At the rail end it must allow for sliding along the rail and not transmit rotations to the shoe about the rail transverse axes. This implies that pin flags must be used at the rail and to inhibit these freedoms.

This stiff bar connection can be implemented the wrong way or the right way. One gets trapped into modeling the wrong way by forgetting that pin flags are applied to bar coordinates not to the displacement coordinates. I fell into this trap and will show you what happens. Then I will follow it up with the correct way to model it.

# MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

## BAR CONNECTION

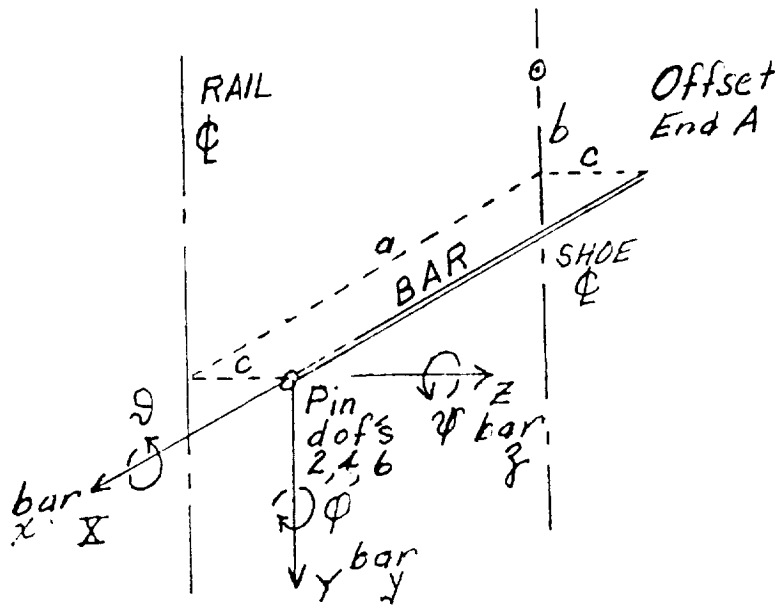
### WRONG WAY



Include the rail grid points in the shoe model and apply SPC's at the GRID level in d.o.f.'s 2,4,6. Connect the shoe point to the rail point with a stiff bar. Note that the connection from shoe GP to rail GP produces bar coordinates that are skewed with respect to the displacement coordinates. Thus when bar element coordinate 2 is pinned, a component of force still develops at the rail end of the bar in the Y displacement coordinate direction, and so the eigenvalue check for rigid body modes fails once again. The listing in Appendix B of a simple model, incorporating this wrong approach, shows the constraint forces in the rigid body modes in freedoms T1, R1, & R3 to be non-negligible. Then the elastic mode shows large constraint forces in these freedoms.

# MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

## BAR CONNECTION RIGHT WAY



Offset the bar at the shoe end so as to terminate the bar at the rail end so as to be perpendicular to all displacement coordinates at the rail end. This connection passes the eigenvalue check for rigid body modes. Appendix C is a listing of a simple demonstration problem of the joint modeled the right way. Note that the constraint forces in freedoms T2, R1, & R3 are negligible in rigid body modes as well as in elastic modes.

## MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

### CONCLUSIONS

This paper has demonstrated that complete checkout of a basic substructure can be done under the special circumstances of a sliding connection with offsets. Stiff bar connections make this possible so long as the bar coordinates are aligned with the displacement coordinates at the sliding surface.

MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

APPENDIX A  
RUN WITH MPC CONNECTION



ID OFFSET,CONNECT  
 APP DISP  
 SOL 3.0  
 DIAG 8,21,22  
 TIME 10  
 CEND

FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH MPC'S  
 ALIGNED WITH OFFSETS. RAIL END INDEPENDENT.

UAI/NASTRAN VERSION 11.1A

PAGE

2

C A S E C O N T R O L P A C K E T E C H O

TITLE = FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH MPC'S  
 SUBTITLE = ALIGNED WITH OFFSETS. RAIL END INDEPENDENT.  
 OUTPUT

DISP = ALL  
 ELFORCES = ALL  
 \$ SPCFORCES = ALL  
 SUBCASE 1

LABEL = ALL 6 DOF'S RETAINED ON BOTH ENDS.  
 MPC = 20  
 METHOD = 3  
 BEGIN BULK

SORTED COUNT		S O R T E D B U L K D A T A E C H O												
1-	1	.....1.....	.....2.....	.....3.....	.....4.....	.....5.....	.....6.....	.....7.....	.....8.....	.....9.....	.....10.....			
2-	2	CBAR 1	1	71	72	1.0	1.0	1.0	0.0				SHOE	
3-	3	CMASS2 132	0.1	13	2								31Y	
4-	4	CMASS2 142	0.1	14	2								14Y	
5-	5	CMASS2 715	0.1	71	5								71PHI	
6-	6	CMASS2 725	0.1	72	5								72PHI	
7-	7	EIGR 3	INV	0.0	10.0	8	8	6	1.0	1.0	1.0	1.0	+ALLMODE	
8-	8	+ALLMODE MAX												
9-	9	GRID 13	0	3.0	2.0	2.0	2.0	0					RAIL1PT	
10-	10	GRID 14	0	3.0	17.0	2.0	2.0	0					RAIL2PT	
11-	11	GRID 71	0	0.0	0.0	0.0	0.0	0					SHOE1PT	
12-	12	GRID 72	0	0.0	15.0	0.0	0.0	0					SHOE2PT	
13-	13	MAT1 1	3.+7		0.28	2.4-4								
14-	14	MPC 20	71	1	1.0	13	13	1					+UP1BAR	
15-	15	MPC 71	13	5	2.0	13	13	6					+UP3BAR	
16-	16	MPC 20	71	3	1.0	13	13	3					+UP5BAR	
17-	17	+UP3BAR	13	4	2.0	13	13	5					+LO1BAR	
18-	18	MPC 20	71	5	1.0	13	13	5					+LO3BAR	
19-	19	MPC 20	72	1	1.0	14	14	1					+LO5BAR	
20-	20	+LO1BAR	14	5	2.0	14	14	6						
21-	21	MPC 20	72	3	1.0	14	14	3						
22-	22	+LO3BAR	14	4	2.0	14	14	5						
23-	23	MPC 20	72	5	1.0	14	14	5						
24-	24	PARAM	COUPMASS 7											
25-	25	PBAR 1	1	1.0	1.0	1.0	1.0	1.0						
		PBAR 2	1	100.0	100.0	100.0	100.0	100.0						
		ENDDATA												

R E A L E I G E N V A L U E S

MODE NO.	EXTRACTION ORDER	EIGENVALUE	RADIAN FREQUENCY	CYCLIC FREQUENCY	GENERALIZED MASS	GENERALIZED STIFFNESS
1	3	0.000000E+00	0.000000E+00	0.000000E+00	1.521215E-03	0.000000E+00
2	4	0.000000E+00	0.000000E+00	0.000000E+00	4.247887E-03	0.000000E+00
3	5	0.000000E+00	0.000000E+00	0.000000E+00	1.607912E-03	0.000000E+00
4	6	0.000000E+00	0.000000E+00	0.000000E+00	2.451029E-03	0.000000E+00
5	7	0.000000E+00	0.000000E+00	0.000000E+00	1.061112E-03	0.000000E+00
6	9	0.000000E+00	0.000000E+00	0.000000E+00	1.012346E-01	0.000000E+00
7	1	9.563905E-12	3.092556E-06	4.921956E-07	4.928215E-02	4.713298E-13
8	2	1.161892E-08	1.077911E-04	1.715549E-05	3.912935E-03	4.546408E-11
9	8	1.562500E+07	3.952847E+03	6.291152E+02	2.222214E-02	3.472210E+05

EIGENVALUE = 0.000000E+00

FREQUENCY = 0.000000E+00 HZ.

R E A L E I G E N V E C T O R N O . 1

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	4.885226E-01	-3.069099E-02	1.000000E+00	0.0	2.000755E-02	0.0
14	GRID	-1.334166E-03	-3.41052E-03	-6.272650E-01	0.0	2.000755E-02	0.0
71	GRID	4.485075E-01	1.761184E-01	1.060023E+00	-1.084843E-01	2.000755E-02	3.265712E-02
72	GRID	-4.134927E-02	1.761184E-01	-5.672423E-01	-1.084843E-01	2.000755E-02	3.265712E-02

EIGENVALUE = 0.000000E+00

FREQUENCY = 0.000000E+00 HZ.

R E A L E I G E N V E C T O R N O . 2

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-6.913960E-02	3.166597E-02	1.000000E+00	0.0	-1.377827E-01	0.0
14	GRID	-3.550368E-01	3.518357E-03	9.440481E-02	0.0	-1.377827E-01	0.0
71	GRID	2.064258E-01	5.781769E-04	5.866519E-01	-6.037301E-02	-1.377827E-01	1.905981E-02
72	GRID	-7.947137E-02	5.781769E-04	-3.189434E-01	-6.037301E-02	-1.377827E-01	1.905981E-02

EIGENVALUE = 0.000000E+00

FREQUENCY = 0.000000E+00 HZ.

R E A L E I G E N V E C T O R N O . 3

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	8.612644E-01	-1.089826E-02	-3.312686E-01	0.0	-2.891179E-03	0.0
14	GRID	-5.001400E-01	-1.188542E-03	1.000000E+00	0.0	-2.891179E-03	0.0
71	GRID	8.670468E-01	4.258756E-03	-3.399421E-01	8.875124E-02	-2.891179E-03	9.076030E-02
72	GRID	-4.943576E-01	4.258756E-03	9.913265E-01	8.875124E-02	-2.891179E-03	9.076030E-02

SUBCASE 1

MODE NUMBER = 4      FREQUENCY = 0.000000E+00 HZ.      EIGENVALUE = 0.000000E+00

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	1.000000E+00	3.279515E-03	-5.439819E-01	0.0	-1.890255E-03	0.0
14	GRID	-6.589970E-02	3.642190E-04	-6.497411E-01	0.0	-1.890255E-03	0.0
71	GRID	1.003780E+00	-1.787680E-03	-5.496526E-01	-7.050612E-03	-1.890255E-03	7.105998E-02
72	GRID	-6.211919E-02	-1.787680E-03	-6.554118E-01	-7.050612E-03	-1.890255E-03	7.105998E-02

MODE NUMBER = 5      FREQUENCY = 0.000000E+00 HZ.      EIGENVALUE = 0.000000E+00

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-2.679756E-01	-4.753040E-03	-7.319843E-02	0.0	-3.266693E-03	0.0
14	GRID	1.000000E+00	-5.290496E-04	2.902177E-01	0.0	-3.266693E-03	0.0
71	GRID	-2.614422E-01	2.310795E-03	-8.299851E-02	2.422774E-02	-3.266693E-03	-8.453170E-02
72	GRID	1.006533E+00	2.310795E-03	2.804176E-01	2.422774E-02	-3.266693E-03	-8.453170E-02

MODE NUMBER = 6      FREQUENCY = 0.000000E+00 HZ.      EIGENVALUE = 0.000000E+00

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-1.127395E-05	-1.111122E-01	2.954264E-05	0.0	-8.683184E-07	0.0
14	GRID	9.360020E-05	1.000000E+00	-1.109201E-05	0.0	1.072533E-06	0.0
71	GRID	-9.537311E-06	-4.564906E-07	2.693768E-05	-2.320808E-06	-8.683184E-07	-6.732830E-06
72	GRID	9.145513E-05	-4.564906E-07	-7.874410E-06	-2.320804E-06	1.072533E-06	-6.732828E-06

MODE NUMBER = 7      FREQUENCY = 4.921956E-07 HZ.      EIGENVALUE = 9.563905E-12

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	1.000000E+00	6.632150E-01	7.963101E-01	0.0	1.036273E-01	0.0
14	GRID	2.864973E-01	7.369055E-02	-3.282914E-01	0.0	1.036273E-01	0.0
71	GRID	7.927454E-01	2.984467E-01	1.107192E+00	-7.497343E-02	1.036273E-01	4.756685E-02
72	GRID	7.924265E-02	2.984467E-01	-1.740939E-02	-7.497343E-02	1.036273E-01	4.756685E-02

ALIGNED WITH OFFSETS. RAIL END INDEPENDENT.  
 ALL 6 DOF'S RETAINED ON BOTH ENDS.

SUBCASE 1

EIGENVALUE = 1.161892E-08

FREQUENCY = 1.715549E-05 HZ.

MODE NUMBER = 8

REAL EIGENVECTOR NO. 8

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-2.487581E-01	-1.668238E-03	-4.699167E-01	0.0	-1.139360E-02	0.0
14	GRID	-9.521336E-03	-1.851357E-04	2.772007E-01	0.0	-1.139360E-02	0.0
71	GRID	-2.259709E-01	1.000000E+00	-5.040975E-01	4.980783E-02	-1.139360E-02	-1.594912E-02
72	GRID	1.326586E-02	1.000000E+00	2.430200E-01	4.980783E-02	-1.139360E-02	-1.594912E-02

EIGENVALUE = 1.562500E+07

FREQUENCY = 6.291152E+02 HZ.

MODE NUMBER = 9

REAL EIGENVECTOR NO. 9

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-6.666663E-01	7.100735E-08	1.000000E+00	0.0	-3.333327E-01	0.0
14	GRID	6.666647E-01	-6.390596E-07	-9.999965E-01	0.0	3.333327E-01	0.0
71	GRID	-7.944661E-07	-1.626112E-10	1.744123E-06	-7.029677E-07	-3.333327E-01	-3.188153E-07
72	GRID	-7.893768E-07	1.631945E-10	1.717579E-06	6.817177E-07	3.333327E-01	3.147009E-07

MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

APPENDIX B  
RUN WITH WRONG BAR CONNECTION

GRID POINT	POINT SINGULARITY ORDER	SINGULARITY LIST	SINGULARITY LIST	SINGULARITY LIST	SPC 0	MPC 0
71	G	1	5	4		
72	G	1	5	4		

6 ROOTS BELOW 1.973921E+01

EIGENVALUE ANALYSIS SUMMARY (INVERSE POWER METHOD)

NUMBER OF EIGENVALUES EXTRACTED	7
NUMBER OF STARTING POINTS USED	1
NUMBER OF STARTING POINT MOVES	0
NUMBER OF TRIANGULAR DECOMPOSITIONS	1
TOTAL NUMBER OF VECTOR ITERATIONS	34
REASON FOR TERMINATION	7*
LARGEST OFF-DIAGONAL MODAL MASS TERM	0.13E-06
MODE PAIR	6
NUMBER OF OFF-DIAGONAL MODAL MASS TERMS FAILING CRITERION	0
(* 1 OR MORE ROOT OUTSIDE FR.RANGE. SEE NASTRAN U.M. SECTION 2.3.3)	

REAL EIGENVALUES

MODE NO.	EIGENVALUE	CYCLIC FREQUENCY	GENERALIZED MASS	GENERALIZED STIFFNESS
*****				
* NASTRAN INFORMATION MESSAGE 3308, LOWEST EIGENVALUE FOUND *				
* AS INDICATED BY THE STURM'S SEQUENCE OF THE DYNAMIC MATRIX *				
* (THIS MESSAGE CAN BE SUPPRESSED BY DIAG 37) *				
*****				
1	-7.963921E-08	4.491420E-05	2.016630E-01	-1.606029E-08
2	2.852769E-08	2.688150E-05	1.250841E-01	3.568360E-09
3	9.751177E-08	4.969911E-05	1.946527E-01	1.898093E-08
4	1.989545E-07	7.098997E-05	1.088651E-01	2.165920E-08
5	2.305249E-07	7.641507E-05	2.362906E-01	5.447087E-08
6	3.321909E-07	9.173054E-05	1.223466E-01	4.064244E-08
7	7.002442E+06	4.211578E+02	1.515952E-01	1.061536E+06

ID OFFSET,CONNECT  
 APP DISP  
 SOL 3,0  
 DIAG 8,21,22  
 TIME 10  
 CEND

FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH BARS JAN 20,1991 PAGE 2  
 WRONG WAY WITH CONNECTOR BAR SKEWED TO RAIL.

C A S E C O N T R O L D E C K E C H O

TITLE = FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH BARS  
 SUBTITLE = WRONG WAY WITH CONNECTOR BAR SKEWED TO RAIL.WANT 3 RB MODES.

OUTPUT

DISP = ALL

MPCFORCES = ALL

ELFORCES = ALL

SPCFORCES = ALL

SUBCASE 1

LABEL = BARS PINNED AT RAIL END. NO OFFSETS AT SHOE END.

METHOD = 3

BEGIN BULK

S O R T E D B U L K D A T A E C H O

	---1---	+++2+++	---3---	+++4+++	---5---	+++6+++	---7---	+++8+++	---9---	+++10+++
CBAR	1	1	71	72	1.0	1.0	0.0			SHOE
CBAR	2	2	71	13	14					+TIE UP
+TIE UP			246							
CBAR	3	2	72	14	13					+TIE DWN
+TIE DWN			246							
CMASS2	131	0.1	13	4						31THETA
CMASS2	141	0.1	14	4						14THETA
CMASS2	711	0.1	71	4						71THETA
CMASS2	712	0.1	71	5						71PHI
CMASS2	721	0.1	72	4						72THETA
CMASS2	722	0.1	72	5						72PHI
EIGR	3	INV	0.0	1.0	6	6	3	1.-3		+ALLMODE
+ALLMODEMAX										
GRID	13	0	3.0	2.0	2.0	0	246			RAIL1PT
GRID	14	0	3.0	17.0	2.0	0	246			RAIL1PT
GRID	71	0	0.0	0.0	0.0	0				SHOE1PT
GRID	72	0	0.0	15.0	0.0	0				SHOE1PT
MAT1	1	3.+7		0.28	2.4-4					
PARAM	COUPMASS7									
PBAR	1	1	1.0	1.0	1.0	1.0				
PBAR	2	1	100.0	100.0	100.0	100.0				
ENDDATA										

SUBCASE 1 EIGENVALUE = -7.963921E-08  
 REAL EIGENVECTOR NO. 1

PT ID.	T1	T2	T3	R1	R2	R3
13	3.308091E-01	0.0	5.615981E-01	0.0	9.189782E-02	0.0
14	-6.346744E-01	0.0	-9.552183E-01	0.0	9.189782E-02	0.0
71	3.910763E-01	-5.288029E-01	1.000000E+00	-1.011211E-01	6.503133E-02	6.436E-2
72	-5.744071E-01	-5.288029E-01	-5.168163E-01	-1.011211E-01	6.503133E-02	6.436E-2

EIGENVALUE = 2.852769E-08 REAL EIGENVECTOR NO. 2

PT ID.	T1	T2	T3	R1	R2	R3
1	-1.806720E-01	0.0	3.554041E-01	0.0	-1.205854E-01	0.0
14	-7.829153E-01	0.0	1.000000E+00	0.0	-1.205854E-01	0.0
71	1.403818E-01	-1.730800E-01	4.690333E-02	4.297306E-02	-8.839797E-02	4.015E-2
72	-4.618614E-01	-1.730800E-01	6.914992E-01	4.297306E-02	-8.839797E-02	4.015E-2

EIGENVALUE = 9.751177E-08 REAL EIGENVECTOR NO. 3

PT ID.	T1	T2	T3	R1	R2	R3
13	-7.289532E-01	0.0	2.853720E-01	0.0	-1.817658E-01	0.0
14	3.520157E-01	0.0	2.345846E-01	0.0	-1.817658E-01	0.0
71	-8.096893E-02	-6.163144E-01	-7.029006E-02	-3.385834E-03	-2.055022E-01	-7.2E-1
72	1.000000E+00	-6.163144E-01	-1.210776E-01	-3.385834E-03	-2.055022E-01	-7.2E-1

EIGENVALUE = 1.989545E-07 REAL EIGENVECTOR NO. 4

PT ID.	T1	T2	T3	R1	R2	R3
13	3.177751E-01	0.0	1.764639E-02	0.0	-3.180602E-01	0.0
14	-4.354112E-01	0.0	3.301453E-01	0.0	-3.180602E-01	0.0
71	1.000000E+00	-9.989289E-02	-9.057981E-01	2.083326E-02	-2.929949E-01	5.02E-2
72	2.468137E-01	-9.989289E-02	-5.932992E-01	2.083326E-02	-2.929949E-01	5.02E-2

EIGENVALUE = 2.305249E-07 REAL EIGENVECTOR NO. 5

PT ID.	T1	T2	T3	R1	R2	R3
13	9.812109E-01	0.0	1.000000E+00	0.0	-1.272332E-02	0.0
14	8.707730E-01	0.0	5.573768E-01	0.0	-1.272332E-02	0.0
71	7.983168E-01	4.514050E-01	8.229362E-01	-2.950821E-02	-2.407710E-02	7.363E-3
72	6.878789E-01	4.514050E-01	3.803130E-01	-2.950821E-02	-2.407710E-02	7.363E-3

EIGENVALUE = 3.321909E-07 REAL EIGENVECTOR NO. 6

PT ID.	T1	T2	T3	R1	R2	R3
13	-7.600989E-01	0.0	1.000000E+00	0.0	-3.662173E-01	0.0
14	-3.776701E-01	0.0	3.752712E-01	0.0	-3.662173E-01	0.0
71	-1.461953E-01	2.568173E-01	-1.776728E-01	-4.164859E-02	-3.932845E-01	-2.6E-1
72	2.362335E-01	2.568173E-01	-8.024015E-01	-4.164859E-02	-3.932845E-01	-2.6E-1

EIGENVALUE = 7.002442E+06 REAL EIGENVECTOR NO. 7

PT ID.	T1	T2	T3	R1	R2	R3
13	-6.670417E-01	0.0	1.000000E+00	0.0	-6.548009E-01	0.0
14	5.839078E-01	0.0	-8.773038E-01	0.0	5.701413E-01	0.0
71	6.416196E-01	1.446323E-03	-9.644380E-01	2.011386E-01	-5.263158E-01	1.14E-1
72	-5.595077E-01	7.309780E-03	8.305104E-01	5.448166E-02	5.091975E-01	4.52E-2



EIGENVALUE = -7.963921E-08 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	2.806213E+01	0.0	-2.590351E+01	0.0	-1.726900E+01
14	0.0	-1.530662E+01	0.0	-4.709728E+00	0.0	-3.139819E+00

EIGENVALUE = 2.852769E-08 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	2.551103E+00	0.0	1.177432E+00	0.0	7.849547E-01
14	0.0	-2.551103E+00	0.0	-1.118560E+01	0.0	-7.457070E+00

EIGENVALUE = 9.751177E-08 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	-1.275551E+00	0.0	1.876532E+00	0.0	1.251022E+00
14	0.0	5.102206E+00	0.0	1.103843E-01	0.0	7.358950E-02

EIGENVALUE = 1.989545E-07 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	9.566635E-01	0.0	3.017170E+00	0.0	2.011446E+00
14	0.0	-5.102206E+00	0.0	4.121012E+00	0.0	2.747341E+00

EIGENVALUE = 2.305249E-07 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	1.020441E+01	0.0	1.964840E+01	0.0	1.309893E+01
14	0.0	2.793968E-09	0.0	-5.077676E+00	0.0	-3.385117E+00

EIGENVALUE = 3.321909E-07 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	-2.551103E+00	0.0	-3.532296E+01	0.0	-2.354864E+01
14	0.0	-2.551103E+00	0.0	-1.236304E+01	0.0	-8.242024E+00

EIGENVALUE = 7.002442E+06 FORCES OF SINGLE-POINT CONSTRAINT

PT ID.	T1	T2	T3	R1	R2	R3
13	0.0	-3.846585E+01	0.0	-2.479790E+04	0.0	-1.653193E+04
14	0.0	-1.149591E+02	0.0	2.221343E+04	0.0	1.480896E+04

MODELING OF CONNECTIONS BETWEEN SUBSTRUCTURES

APPENDIX C  
RUN WITH RIGHT BAR CONNECTION

ID OFFSET,CONNECT  
 APP DISP  
 SOL 3,0  
 DIAG 8,21,22  
 TIME 10  
 CEND

FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH BARS PAGE 2  
 RIGHT WAY WITH CONNECTOR BAR NORMAL TO RAIL.

C A S E C O N T R O L P A C K E T E C H O

TITLE = FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH BARS  
 SUBTITLE = RIGHT WAY WITH CONNECTOR BAR NORMAL TO RAIL.  
 OUTPUT

DISP = ALL  
 ELFORCES = ALL  
 SPCFORCES = ALL

SUBCASE 1

LABEL = BARS PINNED AT RAIL END. OFFSETS AT SHOE END.  
 METHOD = 3  
 BEGIN BULK

SORTED COUNT		S O R T E D B U L K D A T A E C H O									
1-	1	.....1....	.....2....	.....3....	.....4....	.....5....	.....6....	.....7....	.....8....	.....9....	.....10....
2-	2	CBAR 1	2	71	72	1.0	1.0	1.0	0.0		SHOE
3-	246	CBAR 2	71	13	1.0	1.0	1.0	0.0			+TIE UP
4-	2	+TIE UP	246	0.0	2.0	2.0	2.0	0.0			+TIE DWN
5-	2	CBAR 3	2	72	14	1.0	1.0	1.0	0.0		
6-	246	+TIE DWN	246	0.0	2.0	2.0	2.0				
7-	131	CMASS2	131	0.1	13	4					31THETA
8-	141	CMASS2	141	0.1	14	4					14THETA
9-	711	CMASS2	711	0.1	71	4					71THETA
10-	712	CMASS2	712	0.1	71	5					71PHI
11-	721	CMASS2	721	0.1	72	4					72THETA
12-	722	CMASS2	722	0.1	72	5					72PHI
13-	3	EIGR	3	INV	0.0	10.0	6	6	3	1.-3	+ALLMODE
14-		+ALLMODE MAX									
15-	13	GRID	13	0	3.0	2.0	2.0	0	246		RAILIPT
16-	14	GRID	14	0	3.0	17.0	2.0	0	246		RAILIPT
17-	71	GRID	71	0	0.0	0.0	0.0	0			SHOEIPT
18-	72	GRID	72	0	0.0	15.0	0.0	0			SHOEIPT
19-	1	MAT1	1	3.+7	0.28	2.4-4					
20-	7	PARAM	COUPMASS	7							
21-	1	PBAR	1	1	1.0	1.0	1.0	1.0	1.0	1.0	
21-	2	PBAR	2	1	100.0	100.0	100.0	100.0	100.0	100.0	
21-		ENDDATA									

R E A L E I G E N V A L U E S

MODE NO.	EXTRACTION ORDER	EIGENVALUE	RADIAN FREQUENCY	CYCLIC FREQUENCY	GENERALIZED MASS	GENERALIZED STIFFNESS
1	2	-8.597651E-07	9.272352E-04	1.475741E-04	8.360698E-02	-7.188236E-08
2	3	-3.708519E-07	6.089761E-04	9.692155E-05	7.466593E-02	-2.769000E-08
3	4	5.746691E-08	2.397236E-04	3.815303E-05	1.415073E-01	8.131985E-09
4	1	1.050890E-07	3.241743E-04	5.159394E-05	1.495338E-01	1.571424E-08
5	5	1.103310E-07	3.321611E-04	5.286507E-05	2.399001E-01	2.646841E-08
6	6	3.483668E-07	5.902261E-04	9.393740E-05	1.215011E-01	4.232696E-08

EIGENVALUE = -8.597651E-07

FREQUENCY = 1.475741E-04 HZ.

MODE NUMBER = 1

R E A L E I G E N V E C T O R N O . 1

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-2.433693E-04	0.0	9.871816E-01	0.0	-3.738998E-01	0.0
14	GRID	-4.052280E-01	0.0	1.000000E+00	0.0	-3.738998E-01	0.0
71	GRID	8.015541E-01	4.693623E-03	-1.362268E-01	8.545591E-04	-3.738998E-01	2.699898E-02
72	GRID	3.965695E-01	4.693623E-03	-1.234084E-01	8.545591E-04	-3.738998E-01	2.699898E-02

EIGENVALUE = -3.708519E-07

FREQUENCY = 9.692155E-05 HZ.

MODE NUMBER = 2

R E A L E I G E N V E C T O R N O . 2

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	7.450739E-02	0.0	9.888168E-02	0.0	2.797289E-01	0.0
14	GRID	-5.090036E-01	0.0	-3.656060E-01	0.0	2.797289E-01	0.0
71	GRID	-4.071489E-01	1.079729E-01	1.000000E+00	-3.096585E-02	2.797289E-01	3.890074E-02
72	GRID	-9.906599E-01	1.079729E-01	5.355123E-01	-3.096585E-02	2.797289E-01	3.890074E-02

EIGENVALUE = 5.746691E-08

FREQUENCY = 3.815303E-05 HZ.

MODE NUMBER = 3

R E A L E I G E N V E C T O R N O . 3

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	2.404255E-01	0.0	2.897290E-01	0.0	1.577857E-01	0.0
14	GRID	6.952828E-01	0.0	5.630910E-01	0.0	1.577857E-01	0.0
71	GRID	-1.357936E-01	-3.387907E-01	7.266380E-01	1.822414E-02	1.577857E-01	-3.032382E-02
72	GRID	3.190636E-01	-3.387907E-01	1.000000E+00	1.822414E-02	1.577857E-01	-3.032382E-02

EIGENVALUE = 1.050890E-07

FREQUENCY = 5.159394E-05 HZ.

MODE NUMBER = 4

R E A L E I G E N V E C T O R N O . 4

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	8.741319E-01	0.0	-1.770641E-01	0.0	-3.227559E-02	0.0
14	GRID	4.142550E-01	0.0	3.377019E-01	0.0	-3.227559E-02	0.0
71	GRID	1.000000E+00	7.083516E-01	-3.425264E-01	3.431774E-02	-3.227559E-02	3.065846E-02
72	GRID	5.401231E-01	7.083516E-01	1.722396E-01	3.431774E-02	-3.227559E-02	3.065846E-02

FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH BARS PAGE 27  
 RIGHT WAY WITH CONNECTOR BAR NORMAL TO RAIL.

BARS PINNED AT RAIL END. OFFSETS AT SHOE END. SUBCASE 1  
 MODE NUMBER = 5 FREQUENCY = 5.286507E-05 HZ. EIGENVALUE = 1.103310E-07

REAL EIGENVECTOR NO. 5

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	-9.356353E-01	0.0	1.000000E+00	0.0	-1.059662E-01	0.0
14	GRID	9.272855E-01	0.0	-2.696967E-01	0.0	-1.059662E-01	0.0
71	GRID	-9.720924E-01	5.534579E-01	8.513944E-01	-8.464644E-02	-1.059662E-01	-1.241947E-01
72	GRID	8.908284E-01	5.534579E-01	-4.183022E-01	-8.464644E-02	-1.059662E-01	-1.241947E-01

MODE NUMBER = 6 FREQUENCY = 9.393740E-05 HZ. EIGENVALUE = 3.483668E-07

REAL EIGENVECTOR NO. 6

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	7.174048E-01	0.0	6.860800E-01	0.0	-9.937754E-02	0.0
14	GRID	8.860417E-02	0.0	-6.589323E-01	0.0	-9.937754E-02	0.0
71	GRID	1.000000E+00	-4.786835E-01	5.672824E-01	-8.966749E-02	-9.937754E-02	4.192004E-02
72	GRID	3.711993E-01	-4.786835E-01	-7.777300E-01	-8.966749E-02	-9.937754E-02	4.192004E-02

MODE NUMBER = 1 FREQUENCY = 1.475741E-04 HZ. EIGENVALUE = -8.597651E-07

FORCES OF SINGLE-POINT CONSTRAINT

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	0.0	-4.023161E-10	0.0	0.0	0.0	2.413897E-09

MODE NUMBER = 2 FREQUENCY = 9.692155E-05 HZ. EIGENVALUE = -3.708519E-07

FORCES OF SINGLE-POINT CONSTRAINT

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	0.0	-5.796661E-10	0.0	0.0	0.0	3.477997E-09

MODE NUMBER = 3 FREQUENCY = 3.815303E-05 HZ. EIGENVALUE = 5.746691E-08

FORCES OF SINGLE-POINT CONSTRAINT

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	0.0	4.518601E-10	0.0	0.0	0.0	-2.711161E-09

FREE-BODY MODAL STUDY OF SHOE/RAIL CONNECTIONS WITH BARS  
 RIGHT WAY WITH CONNECTOR BAR NORMAL TO RAIL.

SUBCASE 1  
 EIGENVALUE = 1.050890E-07

BARS PINNED AT RAIL END. OFFSETS AT SHOE END.  
 MODE NUMBER = 4 FREQUENCY = 5.159394E-05 HZ.

F O R C E S O F S I N G L E - P O I N T C O N S T R A I N T

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	0.0	-4.568466E-10	0.0	0.0	0.0	2.741080E-09

MODE NUMBER = 5 FREQUENCY = 5.286507E-05 HZ. EIGENVALUE = 1.103310E-07

F O R C E S O F S I N G L E - P O I N T C O N S T R A I N T

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	0.0	1.850646E-09	0.0	0.0	0.0	-1.110387E-08

MODE NUMBER = 6 FREQUENCY = 9.393740E-05 HZ. EIGENVALUE = 3.483668E-07

F O R C E S O F S I N G L E - P O I N T C O N S T R A I N T

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
13	GRID	0.0	-6.246573E-10	0.0	0.0	0.0	3.747944E-09