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Computation of Supersonic Jet Mixing Noise for an Axisymmetric CD Nozzle Using k- ϵ Turbulence Model

Abbas Khavaran Sverdrup Technology, Inc. Lewis Research Center Group Brook Park. Ohio and Eugene A. Krejsa and Chan M. Kim National Aeronautics and Space Administration Lewis Research Center Cleveland, Ohio Prepared for the 30th Aerospace Sciences Meeting and Exhibit sponsored by the American Institute of Aeronautics and Astronautics Reno, Nevada, January 6-9, 1992 N92-14795 COMPUTATION OF SUPERSONIC (NASA-TM-105338) JET MIXING NOISE FOR AN AXISYMMETRIC CD NOZZLE USING K-EPSILON TURBULENCE MODEL Unclas CSCL 20A (NASA) 16 p G3/71 0057142



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Computation of Supersonic Jet Mixing Noise for an Axisymmetric CD Nozzle Using $k - \epsilon$ Turbulence Model

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Abstract

The turbulent mixing noise of a supersonic jet is calculated for a round convergent-divergent nozzle at the design pressure ratio. Aerodynamic computations are performed using the PARC code with a k- ϵ turbulence model. Lighthill's acoustic analogy combined with Ribner's assumption is adopted. The acoustics solution is based upon the methodology followed by GE in the MGB code. The source correlation function is expressed as a linear combination of second-order tensors. Assuming separable second-order correlations and incorporating Batchelor's isotropic turbulence model, the source term was calculated from the kinetic energy of turbulence. A Gaussian distribution for the time-delay of correlation was introduced. The CFD solution was used to obtain the source strength as well as the characteristic time-delay of correlation. The effect of sound/flow interaction was incorporated using the high frequency asymptotic solution to Lilley's equation for axisymmetric geometries. Acoustic results include sound pressure level directivity and spectra at different polar angles. The aerodynamic and acoustic results demonstrate favorable agreement with experimental data.

Introduction

Recent advances in the area of computational fluid dynamics have provided researchers with new tools for approaching aeroacoustic problems. Though the direct computation of the sound field and its propagation mechanism is the ultimate goal in an area which has been labeled as computational aeroacoustics, the extraordinary difficult nature of these computations at the present time lead to a more practical approach, namely using the available computational resources. Such an approach is taken here to study the high speed jet noise because of the current interest in High Speed Civil Transport (HSCT).

Over a decade ago, a unified aerodynamic/acoustic prediction model was developed by GE for the Federal Aviation Administration [2]. The aerodynamic predictions within this code are carried out by applying an extension of Reichardt's model. The three components of turbulent shearing stress are computed based upon contour integrals around the nozzle exit geometry and utilized in deriving an expression for the source strength. Though the closed form nature of Reichardt's solution has led to a versatile and relatively fast numerical scheme, the assumptions inherent in the derivations render inaccurate aerodynamic prediction for complex geometries.

Reichardt's solution essentially assumes exhaust nozzle elements discharge axially. It neglects radial mean flow and swirl and does not take into account the effect of shock structure on mixing and turbulence. These assumptions, among others, could vitiate the aerodynamic predictions substantially. In the light of these assumptions the model proves insufficient for noise prediction of new lobed hypermix nozzles that are the present focus in HSCT research. To circumvent some of the pitfalls associated with Reichardt's model, a two-stage algorithm is considered in which the aerodynamic calculations are carried out independently and the resulting plume data are introduced for noise computation. The following computational advantages are associated with a two-stage algorithm:

- the aerodynamic calculations can start from within the nozzle, giving a more realistic model of the exit conditions;
- (2) grid selection can be done independently for aerodynamic and acoustic purposes. The plume is treated as an integration of axial slices in acoustic computations;
- (3) proper prediction of shock-cell structure and intensity for off-design conditions improves shock noise assessment.

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The geometry considered in this paper is a round convergent-divergent nozzle. This particular nozzle has previously been tested aerodynamically and acoustically for NASA-Lewis by General Electric [1]. Test data has been especially helpful in assessing the CFD results before proceeding with noise computations. The flowpath is designed to obtain an isentropic, uniform and parallel flow at the nozzle exit for the design Mach number of 1.4, thereby eliminating to a large degree, any shock induced noise. An axisymmetric version of PARC code with Chien's k- ϵ turbulence model [3] has been used. The complete Reynolds-averaged Navier Stokes equations are solved in conservative law form. The viscus coefficients are determined based on Sutherland's viscosity law, Stokes hypothesis and constant Prandtl number assumption. The jet plume flow field is compared with data as well as solution from Reichardt's model.

Method of Solution

The solution technique is essentially based upon the methodology followed by GE in developing the MGB code [2]. Reichardt's aerodynamic model is replaced with CFD and the technique is briefly outlined here with emphasis on the new changes and comparisons with the original model.

The solution technique is described in two sections, source spectrum model and sound/flow interaction. The first section describes the application of PARC with a k- ϵ turbulence model to computation of source strength and its spectrum and explains the empirical constants used in computation of supersonic convection factor. In the second section the effect of surrounding medium on radiated noise from convecting quadrupole sources is described. It is explained how the mean flow temperature and velocity, as obtained from CFD, are used in computation of sound/flow interaction of axisymmetric jets.

1. Source Spectrum Model

The mean-square sound pressure in the far field, in absence of convection and refraction is written using Lighthill's acoustic analogy approach [4,5].

$$\overline{p^2}(R,\theta,\phi) = \frac{R_i R_j R_k R_\ell}{16\pi^2 C_\infty^4 R^6} \int_{\vec{y}} \int_{\vec{\xi}} \frac{\partial^4}{\partial \tau^4} \overline{T_{ij} T_{k\ell}'} d\vec{\xi} d\vec{y} \quad (1)$$

The source strength is assumed to be dominated by unsteady momentum flux i.e. $T_{ij} \sim \rho V_i V_j$. Vector $\vec{\xi}$ in the above integration is the separation vector of the correlation between $\rho V_i V_j$ computed at \vec{y} and $\rho' V'_k V'_\ell$ at $\vec{y} + \vec{\xi}$ and τ is the time delay of correlation. The corresponding spectrum can be expressed in terms of the Fourier transform of the autocorrelation function

$$\overline{p_{\omega}^2} = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \overline{p^2} e^{i\omega\tau} d\tau \qquad (2)$$

As such, for a quasi-incompressible turbulence, the source strength is characterized by a two-point timedelayed fourth-order velocity correlation tensor. For a nearly parallel mean flow, the constituent velocities may be written as the sum of the local mean velocity and the turbulent velocity, $V_i = U\delta_{i1} + v_i$. Substituting V_i into equation (1), the contribution to the integral due to the self noise terms is shown to be independent of the mean flow. This contribution, as shown by Ribner [6], is primarily due to terms like $v_i v_j v'_k v'_l$. As explained by Mani [7], the distinction between shear noise and self noise becomes less important when the interpretation of the source terms is based upon Lilley's [8] formulation rather than Lighthill's equation. Assuming a normal joint probability for turbulent velocity components, as suggested by Ribner [6] and using the isotropic turbulence model of Batchelor [9], the fourth-order correlation can be written as a linear combination of second-order correlations.

$$\overline{v_i v_j v_k' v_\ell'} = (\overline{v_i v_k'})(\overline{v_j v_\ell'}) + (\overline{v_i v_\ell'})(\overline{v_j v_k'}) + (\overline{v_i v_j'})(\overline{v_k v_\ell'})$$
(3)

Further by assuming that the two-point velocity correlations, $v_i v'_j$, are separable in space/time factors, as postulated by Ribner,

$$\overline{v_i v_j'} = R_{ij}(\vec{\xi})g(\tau) \tag{4}$$

the integration on separation vector of correlation can be carried out in closed form. The space factor, according to Batchelor, is written as:

$$R_{ij}(\vec{\xi}) = T[(f + \frac{1}{2}\xi f')\delta_{ij} - \frac{1}{2}f'\xi_i\xi_j/\xi]$$
(5)

where $T = \frac{1}{3}\overline{v_i v_i}$ is the intensity of turbulence replacing the axial turbulence intensity in the Reichardt's model and $f' = \partial f/\partial \xi$. The three components of the separation vector of correlation are represented as ξ_i for i = 1, 2, 3. Function $f(\xi)$ can be expressed as $f(\xi) = exp(-\pi\xi^2/L^2)$. This expression makes $f(\xi)$ decrease to zero for large ξ with sufficient rapidity to make $\int_0^\infty \xi^m f(\xi) d\xi$ converge for $m \ge 0$. Length L is the longitudinal macroscale of turbulence, representing the linear extent of the region within which velocities are appreciably correlated. The time factor of correlation is expressed as $g(\tau) = exp(-\tau/\tau_o)$ where τ_o denotes the characteristic time-delay in a moving reference frame. For axisymmetric jets, Davies et al. [10] have shown that τ_o is proportional to the inverse of mean shear i.e. $1/\tau_o = (\partial U/\partial r)$ where U denotes the mean velocity and r the radial distance. In addition, turbulence intensity can be expressed in terms of L and τ_o according to $\tau_o \sim L/\sqrt{T}$. Since the eddy length scale L_ϵ is related to kinetic energy of turbulence $k = \overline{v_i v_i}/2$ and its dissipation rate ϵ as $L_\epsilon = k^{3/2}/\epsilon$, assuming that L_ϵ and L are proportional, it can be concluded that $1/\tau_o \sim \epsilon/k$. The above conclusion can also be derived from the algebraic turbulence model. Comparison of τ_o , as computed from k and ϵ , with the corresponding results obtained from the velocity gradient and Reichardt's aerodynamic solution are presented under the numerical discussions.

Ribner [6] evaluates the contribution to self noise for various source strength components. The corresponding spectrum is evaluated by using a Fourier transform on the time delay of the correlation [2]. In the final analysis the source intensity spectrum can be expressed as

$$I(\Omega) \sim \rho^2 k^{\frac{1}{2}} (\Omega \tau_o)^4 e^{\frac{-1}{\bullet(\Omega \tau_o)^2}} \tag{6}$$

To compute the noise field, this equation will later be used in conjunction with the refraction effect of the mean flow. The doppler effect relating the source frequency Ω and the observed frequency f is expressed through a convection factor, \overline{C} , as $\Omega = 2\pi f \overline{C}$. The singular behavior of the eddy convection factor $\overline{C} =$ $(1 - M_c \cos\theta)$ at supersonic convection speeds $(M_c > 1)$ has been discussed by Ffowcs Williams [11]. The autocorrelation function in this region, which corresponds to emission of eddy Mach wave, becomes zero and thus the integrand remains finite. In our analysis a modified convection factor described by

$$\overline{C} = \sqrt{\left(1 - M_c \cos\theta\right)^2 + \left(\alpha_c k^{-5} / C_{\infty}\right)^2}$$
(7)

has been selected for numerical computation. The empirical convection constant α_c was determined from comparison of prediction with data. A value of $\alpha_c = .5$ is generally a good approximation for most observation angles. The convection Mach number was expressed as a function of the weighted average of the nozzle exit Mach number and local Mach M

$$M_c = .5M + \beta_c M_j \tag{8}$$

Values in the range of .25 to .3 for the convection constant β_c appear to yield best results.

2. Sound/Flow Interaction

Lighthill's acoustic analogy approach, based on classical wave equation doesn't incorporate the effect of

surrounding mean flow on the sound radiation caused by convected multipole sources. It is clear that these pressure fluctuations should propagate through a region of nonuniform velocity and temperature before reaching the observer point. Thus the location of source within the jet plume has a strong effect on the amount of radiated sound. The mean flow results in not only the refraction of the radiated sound, but also an additional convection amplification due to fluid motion. A number of investigators have studied the radiation field of multipole sources immersed in parallel sheared flows. Mani [7,12,13] studied the mean flow interaction of round jets for slug flow profiles assuming quadrupole sources convecting along the centerline of the jet. Gliebe and Balsa [14] and Goldstein [15] extended the above analysis to arbitrary velocity profiles in high frequency and low frequency limits respectively. The generalization to arbitrarily located sources in continuously varying monotonic profiles were derived by Balsa [16] and Goldstein [17,18]. For supersonic jets, the high frequency solution provides an adequate approximation as suggested by Tester and Morfey [19] and Pao [20].

Lilley's equation is considered as the starting point by most recent investigators studying the sound/flow interactions. For a parallel flow, the Green's function solution to a convected monopole of frequency Ω is obtained by applying a sequence of Fourier transformations. The solution corresponding to multipole singularities are obtained by differentiating the monopole solution with respect to appropriate source coordinate; once in the case of a dipole source and twice for quadrupole sources. Balsa and Mani [2] provide a comprehensive analysis of the shielding effect of an axisymmetric mean flow, i.e. when the jet velocity and temperature profiles are arbitrary functions of the radial variable. To study the effect of asymmetry in the mean flow, Goldstein [21] solves Lilley's equation for high frequency multipole sources in a jet flow whose Mach number and temperature are functions of crossflow coordinates. This leads to an ordinary differential equation that traces the cross-stream projection of an acoustic ray starting from any given source location. The differential equation is solved repeatedly as one selects initial departure angle for rays leaving the source. Subsequent ray tracing through the shear layer and study of the spreading or focusing of the acoustic emission as it approaches far field, results in a circumferential directivity factor for each source volume element.

For our axisymmetric geometry, Mani and Balsa's formulation, as used in the MGB code, has been applied whereby the turbulent properties of the jet has been coupled with its acoustic radiation. Thus the mean square pressure in the far field is expressed as

$$\overline{p^2}(R,\theta,\Omega) = \int_{\vec{y}} \Lambda(a_{xx} + 4a_{xy} + 2a_{yy} + 2a_{yz})d\vec{y} \quad (9)$$

The contribution to noise field due to each of the quadrupoles contained within a turbulent eddy volume element is described by the directivity factors $a_{xx}, ..., a_{yz}$. The corresponding weighting factors were derived by Ribner [6]. A is a factor related to the source intensity and frequency

$$\Lambda \sim \frac{\left(\frac{\rho_{\infty}}{\rho}\right)^2 I(\Omega)}{\left(4\pi R C_{\infty} C\right)^2 \left(1 - M \cos\theta\right)^2 \left(1 - M_c \cos\theta\right)^2} \quad (10)$$

The directivity factors are functions of the shielding function g^2 which is expressed in terms of the polar observation angle θ , local sound velocity C and Mach numbers $M(r) = U(r)/C_{\infty}$ and $M_c = U_c/C_{\infty}$.

$$g^{2}(r) = \frac{(1-M)^{2} (\frac{C_{\infty}}{C})^{2} - \cos^{2}\theta}{(1-M_{c}\cos\theta)^{2}}$$
(11)

The mean flow variables, as obtained from CFD, are used in computation of $g^2(r)$ and hence the directivity factors $a_{xx}, ..., a_{yz}$. Location r where $g^2(r)$ changes in sign is called transition point or turning point. When $g^2(r)$ is negative between the source and observer, the possibility of fluid shielding exists. The position of the source with respect to the turning points of $g^2(r)$ contributes to the amount of fluid shielding through factor $exp(-2K \int_{r_1}^{r_2} \sqrt{|g^2(r)|} dr)$. The limits of the integration are determined by the location of the source relative to the turning points.

Wave number $K = \omega/C$ in the above exponential factor tends to increase the attenuation of the high frequencies. An extensive list of directivity factors corresponding to a case with two turning points have been listed in [2]. A maximum of four turning points have been considered in the present computations. A correction of one Doppler factor has been utilized for source volume effects according to Ffowcs Williams [11]. The correction for flight speed has been included using flight dynamic factor $(1 + M_{\infty} \cos \theta)^{-1}$ where M_{∞} is the flight Mach number.

Numerical Results and Discussion

To obtain the flow field solution a 141×60 grid (Figure 1), highly clustered around the jet lip-line was used. A run time of over four hours on CRAY-YMP was required to achieve the necessary convergence within PARC-k ϵ code. The aerodynamic results obtained from PARC code were input to a noise prediction code. Aerodynamic and acoustic calculations were compared with available data. Also turbulent intensity and characteristic time delay of correlation, as predicted by PARC code, were compared with Reichardt's solution. All laser velocimeter, shadowgraph and acoustic tests for this model were conducted in the General Electric anechoic free-jet facility [1]. The test point (corresponding to the design condition) is listed in table 1. The Mach contour plot (Figure 2) indicates the formation of a Mach disc inside the nozzle as well as a weak shock outside the exit plane, also seen in the shadowgraph photo [2].

Figures 3 and 4 demonstrate the close agreement with data in the velocity profiles on the lip-line, centerline, and also at four axial positions along the jet. The small oscillations in velocity near the centerline can better be predicted by increasing the grid resolution from exit to 10 diameters downstream. Figure 5 exhibits the contour plot for the intensity of turbulence, indicating the extension of noise sources to nearly 18 diameters downstream. The contour levels are nondimensionalized with respect to reference sound speed, a_r^2 , which is computed at the stagnation temperature. Further details of the turbulence intensity distribution are demonstrated in Figures 6 and 7. The axial distribution of the turbulence intensity near the lip-line (Figure 6a) shows a level of 13 percent near the exit plane with a growing decay rate after 12 diameters, generally in good agreement with data. Reichardt's model predicts a much faster decay after 5 diameters. The radial distribution (Figure 6b) was plotted only at X/D = 8.21where test data was available for comparison. Obviously PARC code does a better job in predicting the maximum turbulence level. Near the centerline, which is still within the potential core, the CFD computations clearly under-predict the data by 3 to 4 percent. This can be attributed to the boundary conditions used in a CFD solution and should not introduce any significant error in noise computation because of low level of source intensity and high shielding effect. Further comparison of the source term using the two aerodynamic prediction methods is illustrated in Figure 7. Reichardt's model predicts a faster spreading rate and also fails to properly predict the ending of the potential core where increased turbulence intensity near the centerline is expected. In addition, Reichardt's model does not accurately predict the axial decay of the turbulence intensity (see Figure 6a).

The characteristic time delay τ_o was obtained using two different definitions alluded to earlier. The corresponding Strouhal numbers defined as $(\epsilon/k)(D/U_j)$ and $(\partial U/\partial r)(D/U_j)$ are plotted in Figures 8 and 9. It is clear that outside the proportionality factor α_f needed for the computation of τ_o , these curves demonstrate remarkable resemblance, showing a peak value moving in toward the centerline with increasing X. A third curve was also included based on Reichardt's solution, showing the same general features but failing to properly predict the radial location of the maximum.

In our acoustic computations τ_o was calculated from $1/\tau_o = \alpha_f \epsilon/k$. Factor α_f can shape the sound spectrum in terms of the location of the maximum and should be determined empirically. A value of $\alpha_f = 2$ was selected in these calculations. For nonaxisymmetric geometries, additional modification in the definition of τ_o is necessary as the circumferential gradient of the mean velocity also contributes to this factor. The dissipation rate of turbulent kinetic energy is plotted in Figure 10. The contour levels are nondimensionalized with respect to a_r^3/L_r where L_r is the reference length used in the PARC code. The acoustic computations for a 40 foot radius are presented in Figures 11 and 12. The overall sound pressure (OASPL) directivity as obtained from PARC shows reasonable agreement with data at most observation angles. The empirical factors β_c and α_f were selected to obtain the best fit at angles where the jet mixing noise is maximum. Obviously for off-design conditions, the shock noise dominates at angles close to upstream axis and several dB's difference in our predictions would not significantly alter the directivity of the total noise. The over-prediction of up 5 dB's at $\theta = 80$ degrees can be improved by selecting an angle dependent convection constant α_c . Reichardt's solution also generates results in close agreement with data as the empirical constants used in this aerodynamic prediction model are calibrated for a conical flow field. The spectral components of noise, based on a one-third octave band are shown in figure 12. The overall agreement seems acceptable.

Concluding Remarks

The source strength has been successfully predicted using PARC code with a k- ϵ turbulence model. The resulting noise predictions compare reasonably with experimental data. This application has removed four empirical constants used in the Reichardt's model, which are calibrated for a conical flow field. The limitations on aerodynamic grid selection has been removed by adopting a two-stage aerodynamic and acoustic algorithm. Further, the time-delay of correlation has been computed using two different models. The acoustic computations, according to the present model, is based on two fundamental assumptions as suggested by Ribner and Batchelor. A proper prediction of the noise spectrum depends on an accurate assessment of the time-delay of correlation.

For non-axisymmetric geometries, a proper circumferential averaging of the flow variables can be used as a first step in the computation of the polar directivity of jet noise. Also contributions from other components of the mean velocity gradient should be included in the computation of τ_o . More elaborate analysis such as geometric ray theory is needed to predict the azimuthal spreading of jet noise. In addition, the empirical constants introduced in the determination of supersonic convection factor should further be investigated for other geometries.

Nomenclature

~ ~	1 . 1
C, C_{∞}	local and ambient speeds of sound
	convection factor
D, D_{eq}	exit and throat diameters
J V(A)	observed irequency
$I(\Omega)$	source intensity spectrum
k	turbulent kinetic energy $= v_i v_i/2$
K	wave number
L	longitudinal macroscale of turbulence
Le	eddy length scale
M, M_j	local and exit Mach numbers
M_c, M_∞	convection and flight Mach numbers
r	radial distance
R	source to observer distance
R _i	observer coordinate
T	intensity of turbulence $= \overline{v_i v_i}/3$
T_{ij}	unsteady momentum flux
$oldsymbol{U}$	mean velocity in direction of flow
Uj	exit jet velocity
vi	fluctuating velocity component in X_i
	direction
V_i	local velocity component in X_i
	direction
$\overline{v_i v_j'}$	two-points time-delayed second-order
	correlation = $\int_{-\infty}^{+\infty} v_i(\vec{y}, t) v_j(\vec{y} + \vec{\xi}, t + \tau) dt$
<i></i>	source coordinate
α_c, β_c	convection constants
αι	proportionality factor $(1/\tau_o = \alpha_f \epsilon/k)$
δ_{ij}	Kronecker's delta
é	dissipation rate of kinetic energy
	$= \nu \overline{(\partial v_i / \partial X_j)(\partial v_i / \partial X_j)}$
θ	polar angle with respect to
	downstream axis
Λ	source factor
Ē	vector separation of correlation
P. Pm	local and ambient densities
ν	molecular viscosity
au	time delay of correlation
$ au_{o}$	characteristic time delay of correlation
å	azimuthal angle
$\tilde{\omega, \Omega}$	observer and source radian frequencies
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Table 1. Design Parmaters for C-D Nozzle

Throat Diameter	5.1 in.
Exit Diameter	5.395 in.
Distance from Throat to Exit	5.525 in.
Exit Velocity	2409 fps
Ambient Velocity	400 fps
Pressure Ratio	3.121
Stagnation Temp	1716° R
Stagnation Temp.	1716°R



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Fig. 1: Nozzle geometry and grid.



Fig. 2: Mach number contour plot $(M_j = 1.4)$.



Fig. 3: Comparison of velocity profiles with experimental results [1] at four different axial locations.



Fig. 4: Comparison of the velocity profiles with experimental results [1] on the (a) centerline (b) lip-line.



Fig. 5: Turbulent intensity contour plot (PARC- $k\epsilon$).

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Fig. 7: Comparison of PARC-ke turbulent intensity profiles with Reichardt's solution at different axial locations, (a) PARC-k ϵ (b) Reichardt's model.



Fig. 3: Strouhal No., (a) St. defined as $(\epsilon/k)(D/U_j)$ obtained from PARC-k ϵ , (b) St. defined as $(\partial U/\partial r)(D/U_j)$ obtained from PARC-k ϵ , (c) same as (b) but obtained from Reichardt's model.

Fig. 9: Strouhal No., (a) and (b) obtained from PARC-k ϵ , (c) Reichardt.



Fig. 10: Contour plot for dissipation rate of turbulent kinetic energy (PARC- $k\epsilon$).







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Fig. 12: Comparison of the spectral components of noise with data [1] at different polar angles based on a 1/3 octave center frequency (band number 11 corresponds to 50 Hz.).



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13. ABSTRACT (Meximum 200 words) The turbulent mixing noise of a supersonic jet is calculated for a round convergent-divergent nozzle at the design pressure ratio. Aerodynamic computations are performed using the PARC code with a k-e turbulence model. Lighthill's acoustic analogy combined with Ribner's assumption is adopted. The acoustics solution is based upon the methodology followed by GE in the MGB code. The source correlation function is expressed as a linear combination of second-order tensors. Assuming separable second-order correlations and incorporating Batchelor's isotropic turbulence model, the source term was calculated from the kinetic energy of turbulence. A Gaussian distribution for the time-delay of correlation. The effect of sound/flow interaction was incorporated using the high frequency asymptotic solution to Lilley's equation for axisymmetric geometries. Acoustic results include sound pressure level directivity and spectra at different polar angles. The aerodynamic and acoustic results demonstrate favorable agreement with experimental data.					
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