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# THE COMPUTATIONAL STRUCTURAL **MECHANICS TESTBED PROCEDURES** MANUAL

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## Preface

The purpose of this manual is to document standard procedures of the Computational Structural Mechanics (CSM) Testbed software system. A description of each procedure including its function, commands, data interface, and use is presented.

Periodically, updates to this manual will be released which describe new procedures or changes to existing procedures.

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### **CSM Testbed Procedures Manual**

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### CSM TESTBED DOCUMENTATION SET

- 1. Introduction to the Computational Structural Mechanics Testbed NASA TM 89096, 1987
- 2. Utilities for Master Source Code Distribution: MAX and Friends NASA CR 178383, 1988
- 3. The Computational Structural Mechanics Testbed Architecture: Volume I - The Language NASA CR 178384, 1988
- The Computational Structural Mechanics Testbed Architecture: Volume II - Directives NASA CR 178385, 1988
- The Computational Structural Mechanics Testbed Architecture: Volume III - The Interface NASA CR 178386, 1988
- The Computational Structural Mechanics Testbed Architecture: Volume IV - The Global-Database Manager GAL-DBM NASA CR 178387, 1988
- The Computational Structural Mechanics Testbed Architecture: Volume V - The Input-Output Manager DMGASP NASA CR 178388, 1989
- 8. The Computational Structural Mechanics Testbed User's Manual NASA TM 100644, 1989
- 9. The Computational Structural Mechanics Testbed Data Library Description NASA TM 100645, 1988
- 10. The Computational Structural Mechanics Testbed Generic Structural-Element Processor Manual NASA CR 181728, 1989
- 11. The Computational Structural Mechanics Testbed Procedures Manual NASA CR 100646, 1990
- 12. The Computational Structural Mechanics Testbed Utility Manual NASA CR XXXXX, 1990

# 1.0 Introduction to CSM Testbed Procedures Manual

This manual is designed to assist users in defining and using command procedures to perform structural analyses. It is expected that the user has read Chapters 1 and 2 of the CSM Testbed User's Manual (reference 1-1). It is assumed that the user is familiar with terms such as CLIP, macrosymbol, processor, and dataset.

Runstreams are the vehicle used to perform structural analyses with the CSM Testbed. The term "runstream" most commonly refers to the file (or files) used to perform a specific analysis, although it may also refer to input at an interactive session. A runstream will typically contain CLAMP directives and processor commands.

Directives, recognized and processed by CLIP, provide the user with, among other things, a means of defining command procedures. These command procedures, defined using the \*PROCEDURE directive, bear some resemblance to FORTRAN subroutines. They may contain branching and looping constructs (implemented using the \*DO, \*IF, and \*WHILE directives) as well as other directives and processor and macroprocessor commands. Command procedures may be given arguments which, unlike FORTRAN subroutine arguments, may be assigned default values. When a command procedure is called (using the \*CALL directive) execution control shifts to the command procedure until the last directive (an \*END directive) in the procedure is encountered. Once the \*END directive is encountered, control returns to the input line in the calling procedure or runstream immediately following the call.

Command procedures, while extremely useful, are not a requirement for performing many types of simple analyses. A command procedure is only <u>required</u> if using the looping or branching constructs (*i.e.*, the \*DO, \*IF, and \*WHILE directives). Procedures should not be used to carry out the computationally intensive activities that are better performed by processors.

This chapter begins with a discussion of CLAMP directives and continues with a discussion of the mechanics of processor execution. A template for linear, static analyses is provided in Section 1.3. Section 1.4 offers some suggestions for creating and using procedures and the CSM Testbed Procedures Manual is described in Section 1.5. Some examples of command procedures are given in Section 1.6.

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## 1.1 CLAMP Directives

Directives are special commands that are recognized and processed by CLIP and are not transported to the processor. A directive is to CLIP like ordinary input is to the processor. A directive is distinguished from ordinary input by beginning with a keyword prefixed by an asterisk. The keyword (directive verb) may be followed by a verb modifier, qualifiers, and parameters, as required by the syntax of the specific directive. See references 1-2 and 1-3 for a complete description of the command language. An interactive help facility, accessed by the \*HELP directive, is built in to explain directives. For a complete list with full descriptions, the user is directed to reference 1-3.

A summary of the most useful directives, grouped according to their function in the Testbed execution environment is provided here for easy reference. Detailed descriptions of all directives are provided in reference 1-3.

### Table 1.1-1 CLAMP Directive Summary

Global Data Manager Interface

*OPEN	Open data library
*CLOSE	Close data library
*TOC	Print table of contents of library
*PRINT	Print table of contents, dataset record contents, or record
	access table of dataset
*PACK	Pack a data library, deleting disabled datasets
*COPY	Copy datasets or dataset records
*DELETE	Delete (i.e., disable) dataset or record
*ENABLE	Enable previously deleted or disabled datasets or records
*FIND	Returns information on libraries, datasets, or records
*RENAME	Renames dataset or record
	Command Procedure Management
*SET PLIB	Set procedure library for residence of command procedures
*PROCEDURE	Initiates definition of command procedure
*CALL	Redirects input to a callable procedure ("calls" a procedure
	with optional argument replacement)
	Nonsequential Command Processing
*IF	Conditional branching construct
*ELSE	
*ELSEIF	
*ENDIF	
+D0	Looping construct
*D0	Poohing construct
*ENDDO	

*WHILE *ENDWHILE	While-looping construct
*JUMP	Transfer control to specified label
*RETURN	Force exit from command procedure
*END	Terminate definition of command procedure
	Macrosymbol Directives
*DEFINE	Define a macrosymbol or macrosymbol array
*UNDEFINE	Delete macrosymbol(s)
*SHOW MACRO	Show macrosymbols
*G2M	Define a macrosymbol from a database entity
*M2G	Create a database entity from the value of a macrosymbol
Built-in	Common constants, mathematical functions,
macrosymbols	generic functions, reserved variables, boolean
·	functions, logical functions, string catenator, string matchers,
	and status macros
	SuperClip Directives
*RUN	Start execution of another program
*STOP	Stops RUN-initiated execution and restarts the parent processor
	General Directives
*HELP	Lists information from NICE HELP file
*SET	Sets specified NICE control parameters
*SHOW	Shows specified NICE control parameters
*ADD	Redirects input to a text file
*REMARK	Print remark line
*UNLOAD	Unload contents of GAL library to an ASCII file
*LOAD	Load contents of GAL library from an ASCII file

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## **1.2 Executing Processors**

There are two types of analysis modules, or processors, associated with the Testbed: internal processors, which have been installed as part of the macroprocessor, and external processors. Either type of processor may be executed using the macroprocessor execute command, [XQT. The user merely appends the processor name to the [XQT and the named processor will begin execution. For example,

### [XQT INV

will start the execution of the processor INV. In order to use this method of execution for external processors, the executable version of the processor must reside in the default directory being used by the macroprocessor or in other pre-defined directories depending on computer system syntax. In addition, the name of an external processor cannot be the same as the name of any internal processor.

External processors may also be executed using the **\*RUN** directive. When this directive is used, a full pathname may be given so that external processors may be kept anywhere. For example, under the VMS operating system,

### \*RUN duaO: [testbed.extp] INVX

will begin execution of processor INVX, located in dua0: [testbed.extp].

Once a processor (internal or external) is running, it will begin to accept input according to the requirements of the individual processor as described in Chapters 4 through 14 of the CSM Testbed User's Manual (Ref. 1-1). The processor will continue accepting input until either another [XQT, a STOP, or a \*STOP is encountered. If a STOP occurs, execution will proceed to completion of the processor's assigned task after which the processor named on the next [XQT command begins execution. If an [XQT occurs, execution will proceed to completion of the processor's assigned task after which the processor named on that last [XQT begins execution. A \*STOP terminates processor execution immediately.

The following runstream provides an example of processor, macroprocessor, and CLIP interaction. The linear, static analysis, a very simple example, with one procedure definition, has been taken from the demonstration problem set library. The procedure is defined so that the \*DO directive may be used in defining joint locations (recall that the \*DO directive may only be used within a command procedure). Note also that the procedure is completely defined *before* it has been called. This is an absolute requirement – **procedures** must be defined before they are called.

. Directives \*procedure demo1 \*open 1 demo1.101 /new . Macroprocessor command to execute TAB [xqt TAB . Processor TAB input START 5 JOINT LOCATIONS . Directive to generate TAB input \*do \$i = 1,5. Comment node х Ż У . TAB Input <\$i>> 0. 0. <10.\*<\$i>> . Directive to end input loop \*enddo . Direct TAB input MATERIAL CONSTANTS 1 10.E+6 .3 .101 .1E-4 BEAM ORIENTATIONS 1 1 1 1 1. E21 SECTION PROPERTIES TUBE 1 2. 2.25 **CONSTRAINT DEFINITION 1** ZERO 1 2 3 4 5 6 1 . Macroprocessor command to execute ELD [xqt ELD . Direct ELD Input E21 1 2 2 3 3 4 4 5 . Macroprocessor command to execute TOPO [xqt TOPO . Macroprocessor command to execute E [xqt E . Macroprocessor command to execute EKS [xqt EKS . Macroprocessor command to execute K [xqt K . Macroprocessor command to execute INV [xqt INV . Direct AUS input ALPHA CASE TITLES **1'TRANSVERSE LOAD** 2'AXIAL LOAD SYSVEC APPLIED FORCES CASE 1 T=2 J=5 1000. CASE 2 I=3 J=5 10000. . Macroprocessor command to execute SSOL [xqt SSOL . Macroprocessor command to execute GSF [xqt GSF . Macroprocessor command to execute PSF [xqt PSF . Macroprocessor command to exit stop . Directive denoting procedure end \*end . Directive calling procedure demo1 \*call demo1 . Macroprocessor command to end execution [xqt exit

It is important to note that while directives may be used to generate input data, the directives themselves do not provide input to the processors. The \*DO directive, used in the JOINT LOCATIONS subprocessor of processor TAB, provides the user with a means of automatically generating TAB input; the line containing the \*do \$i = 1,5 provides no information to processor TAB but is meaningful to CLIP. The result of executing this \*DO directive is to produce five input lines for consumption by processor TAB.

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# **1.3** Runstream Organization

While the Testbed is highly modular, certain processors do depend on information generated by other processors, thus there is some degree of interdependence among the installed processors. In many cases, the order in which processors must be executed is the same as the order in which they appear in the CSM Testbed User's manual (ref. 1-1); this is not entirely true when using one or more of the independent element processors. The following section provides a template for performing a <u>linear static</u> analysis using one or more independent element processors (Section 1.3.1).

# **1.3.1 RUNSTREAM FOR INDEPENDENT ELEMENT PROCESSORS**

The generic element processor template was developed to provide greater flexibility to element developers. It does however, add a level of complexity to the analysis, even to a simple linear, static analysis. This complexity is kept hidden to the average user by the use of a "cover procedure." The procedure name is ES and details of its use may be found in reference 1-4. Essentially, procedure ES manages the execution of the independent element processors, ESi.

Listed below is the order of processor and procedure execution for a linear static analysis using one or more of the independent element processors. Following the list is an example (the same example used in the previous section) which calls procedure ES.

- 1. Procedure ES. Call procedure ES to define element parameters and several global macrosymbols which may be used to automate the definition of joint locations and element connectivity. This call must be made for <u>each different element type</u> in the model, regardless of the number of element processors used.
- 2. Processor TAB. Define joint locations, constraints, reference frames.
- 3. Processor AUS. Build tables of material and section properties.
- 4. Processor LAU. Form constitutive matrix.
- 5. Processor ELD. Define elements. Element definitions include element connectivity, element material reference frame number, element section type number.
- 6. Processor E. Initialize element datasets; create the dataset which will contain all important element information (e.g., intrinsic coordinates, element-to-global transformations, intrinsic stiffness matrices).
- 7. Procedure ES. Initialize element matrices.
- 8. Procedure ES. Calculate element intrinsic stiffness matrices.
- 9. Processor RSEQ or PFM. Resequence nodes for minimum total execution time.
- 10. Processor TOPO. Form maps which guide the assembly and factorization of system matrices.

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- 11. Processor K. Assemble system stiffness matrix.
- 12. Processor INV. Factor system stiffness matrix.
- 13. Processor AUS. Create applied nodal loading.
- 14. Processor SSOL. Solve for static displacements.
- 15. Procedure ES. Calculate element stress resultants.
- 16. Post-process using any of the following processors: VPRT, PRTE, PLOT, CONT, T2PT.

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### 1.3.2 EXAMPLE RUNSTREAM

The following runstream provides an example of a very simple linear static analysis. The problem is to calculate the stress in an isotropic flat plate subjected to a uniform end-shortening. One-fourth of the plate is modeled and symmetry boundary conditions are applied.

```
. Do not echo input
*set echo=off
                                        . ADD file containing procedure ES
*add [testbed.proclib]GENUTIL.PRC
                                        . Open data library
*open/new 1, flat_plate
*def/a es_name == 'EX91' . Element name
*def/a es_proc == 'ES1'
                         . Element processor name
*call ES ( function = 'DEFINE ELEMENTS'; es_proc = <es_proc/p>; --
           es_name = <es_name/p>)
[xqt TAB
                                         . Twenty five nodes total, dof 6 zero
     START 25 6
                                         . Enter joint locations
     JOINT LOCATIONS
                        0.0 2.5
                                         0.0 515
                                   0.0
            0.0
                  0.0
     1
                                         0.0
            0.0
                  2.5
                        0.0 2.5
                                   2.5
     5
                                         . Constraints:
     CONSTRAINT DEFINITION 1
                                         . Plane 2,3 plane of symmetry
       symm plane=1
                                         . Plane 1,3 plane of symmetry
       symm plane=2
                                         . Constrain center w
       zero 3: 1
                                         . Apply displacement at x=lx edge
       nonzero 1 : 5,25,5
                                         . Material and Section properties
[xqt AUS
*def/e g = 3.84615e+6
     TABLE(NI=16,NJ=3): OMB DATA 1 1 . Table of material properties
       I=1,2,3,4,5,6,7,8,9
       J=1: 10.0E+6 .30 10.0E+6 <g> <g> <g> 0.0 0.0 .1
```

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```
. Table of section properties
    TABLE (NI=3,NJ=1,itype=0): LAM OMB 1 1
      J=1 : 2 .1 0.00
                                         . Generate constitutive matrix
[xqt LAU
      NOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt
                  were all globally defined by procedure ES the first time
                   the procedure was called.
                                         . Define elements
[xqt ELD
       *def/i nst = <<es_nip>*<es_nstr>>
       EXPE <es_name> <es_nen> <es_opt> <es_nen> 6 <nst> 1 101 2
       NSECT = 1
       1 3 13 11 2 8 12 6 7 1 2 2
                                         . Initialize element datasets
[xqt E
     stop
     *open 1
                                         . Initialize element matrices
*call ES (function='INITIALIZE')
*call ES (function='FORM STIFFNESS/MATL') . Form intrinsic stiffness matrices
                                         . Resequence
[xqt RSEQ
                                         . Create maps
[xqt TOPO
                                         . Assemble global stiffness matrix
[xqt K
[xqt INV
     online=2
                                         . Form applied loading
[xqt AUS
     sysvec : appl moti
            J=5,25,5:
                         -0.001
     i=1:
                                         . Solve for static displacements
[xqt SSOL
     stop
     *open 1
*call ES (function = 'FORM STRESS'; -- . Calculate element stresses
          es_dis_ds = STAT.DISP.1.1 )
                                         . Print static displacements
[xqt VPRT
     format=4
     print STAT DISP
                                         . Print element stresses
[xqt PRTE
     reset seg1=7,seg2=7
[xqt exit
```

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# 1.4 Creating and Using Procedures

### 1.4.1 CREATING A PROCEDURE

Most directives are so simple that they may easily be entered from a keyboard terminal. One could try to define simple procedures in exactly that manner. There are two problems with this approach:

- 1. A keyed-in sequence of directives and commands is volatile and is not saved unless a log file has been opened, although a procedure definition is compiled and saved.
- 2. Post-facto editing is impossible; once the return key it pressed, the line is gone.

These disadvantages become increasingly serious in long or involved procedures. The most practical way to create most procedures is to use a text editor. Once the procedure source text is ready on a data file, it can be inserted into the command source stream with the **\*ADD** directive.

### **1.4.2 RESIDENCE OF CALLABLE PROCEDURE ELEMENTS**

When CLIP encounters a \*PROCEDURE directive, it enters directive mode and does not exit until the \*END directive is detected. The result of this process is an "object" version of the procedure, known as a *callable procedure element*. CLIP can store a callable procedure element in one of two residence media:

- 1. An ordinary direct-access formatted file created through a FORTRAN 77 OPEN statement. All records of such a file have the same length (namely 80 characters) and contain one data line. The file name is the same as the procedure name except on a VMS VAX where a .DAT is appended to the procedure name to create the file name. For example, a procedure named GEN\_PLATE will generate a file named GEN\_PLATE.DAT on a VMS VAX and a file named GEN\_PLATE on other machines. If the \*SET PLIB directive has <u>not</u> been used prior to the \*PROCEDURE directive, direct-access files will be created automatically.
- 2. A data library managed through the global data manager. A callable procedure is stored as a text group. In order to store procedures in a data library, the \*SET PLIB directive must be used.

The text of a callable procedure element is basically a copy of the source procedure body, prefaced by three linkage tables. These tables store argument names, argument default text, labels (explicit or generated) and their locations within the body of the procedure. **NEVER** tamper with a callable procedure element. If the procedure must be changed, change the source and reprocess the file.

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## 1.4.3 USING A PROCEDURE

Callable procedure elements are accessed through the \*CALL directive. Text substitution is controlled by the argument specification mechanism. In a command procedure reference, text is passed instead of addresses to data. The text supplied in the \*CALL directive is *replaced before the command is interpreted*. In addition, arguments not supplied in the \*CALL, assume the default values given in the \*PROCEDURE definition. A procedure body may include calls to other procedures, or may even call itself, with the ensuing call tree extending down several levels.

## 1.5 The CSM Testbed Procedures Manual

A GAL library which contains the callable procedure elements for all of the procedures described in the following sections (2-9) of this manual is read-accessible to all Testbed users. Separate subdirectories under the prc directory contain solution procedures (see Chapter 3), model generation procedures (see Chapter 2), utility procedures (see Chapter 6), and postprocessing procedures (see Chapter 7). This directory structure is the same across various computer systems with differences only in the description of the path name for each subdirectory. On a VMS VAX computer, this file is referred to by the name CSM\_PRC:PROCLIB.GAL; on UNIX-type computers, it is referred to by the name '\$CSM\_PRC/proclib.gal'. If the user does not need to define any new procedures for use in a particular Testbed runstream, this file can be used as the procedure library by including the following commands in the runstream:

*set plib = 28	
*open 28 CSM_PRC:PROCLIB.GAL /READ	(on VMS)
or	
*open 28 '\$CSM_PRC/proclib.gal' /READ	(on UNIX)

The source code for the procedures resides in subdirectories under the one which contains proclib.gal. These procedures are also read-accessible to all Testbed users. They can be included in the user's private procedure library by placing commands like the following in a Testbed runstream:

```
*set plib=28
      *open 28 proclib.gal /NEW
                                                                  (on VMS)
      *add GEN_UTIL:ES.CLP
         or
                                                                  (on UNIX)
      *add '$GEN_UTIL:es.clp'
or alternatively; on UNIX:
      cp $CSM_PRC/proclib.gal .
      chmod 755 proclib.gal
      testbed
      *set plib=28
      *open 28 proclib.gal
      *add local.prc
or on VMS:
      $COPY CSM_PRC:PROCLIB.GAL []
      $Testbed
      *set plib=28
      *open 28 proclib.gal
      *add local.prc
where local.prc is the CLAMP source file for personal procedure(s).
```

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## **1.6 Examples**

This section provides several examples of the use of procedures. For the sake of consistency, where files are discussed, VAX/VMS filenames have been used. The filename convention used is that a file with a \*.CLP extension contains a single procedure, while a file with a \*.PRC extension contains multiple procedures. The \*ADD and the driving \*CALL directives typically appear in files with the \*.COM extension.

### **1.6.1 A SIMPLE EXAMPLE**

As an introductory example, an annotated procedure is presented which may be used to run a variety of elements through the same flat plate problem. In most applications, this procedure would be kept in a file by itself and that file would be added (using the \*ADD directive) to a much shorter runstream located in an execution control file. The procedure and a VAX/VMS execution control file are listed in the following subsections.

### 1.6.1.1 The Procedure File

The following procedure is kept in a file named FLAT\_PLATE.CLP.

```
*procedure FLAT_PLATE ( es_proc ; es_name )
  ARGUMENTS:
       es_proc: Independent element processor name
      es_name: Element name
*if <ifeqs([es_name];E43)> /then
   *def/i es_nen = 4
*else
   *call ES ( function = 'DEFINE ELEMENTS'; es_proc = [es_proc]; --
             es_name = [es_name])
*endif
[xqt TAB
                                         . Twenty-five joints; dof 6 zero
     START 25 6
                                         . Define joint locations
     JOINT LOCATIONS
                  0.0 0.0 2.5
                                   0.0
                                        0.0 515
     1
            0.0
                  2.5 0.0 2.5
                                   2.5
                                        0.0
     5
            0.0
                                         . Constraints:
     CONSTRAINT DEFINITION 1
                                         . Plane 2,3 plane of symmetry
       symm plane=1
                                         . Plane 1,3 plane of symmetry
       symm plane=2
                                         . Constrain center w
       zero 3: 1
                                         . Apply displacement at x=lx edge
       nonzero 1 : 5,25,5
```

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#### Examples

```
[xqt AUS
*def/e g = 3.84615e+6
    TABLE(NI=16,NJ=3): OMB DATA 1 1
                                       . Define material properties
       I=1,2,3,4,5,6,7,8,9
       J=1: 10.0E+6 .30 10.0E+6 <g> <g> <g> 0.0 0.0 .1
                                        . Define Section properties
     TABLE (NI=3,NJ=1,itype=0): LAM OMB 1 1
          J=1 : 2 .1 0.00
                                         . Form constitutive matrix
[xqt LAU
     *if <ifeqs([es_name];E43)> /then
       reset SPAR=-1
     *endif
                                         . Define elements
[xqt ELD
     #if <ifeqs([es_name];E43)> /then
       E43
     +else
       NOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt
                   were globally defined by procedure ES the first time
                   the procedure was called.
       *def/i nst = <<es_nip>*<es_nstr>> . Number of stress resultants
       EXPE [es_name] <es_nen> <es_opt> <es_nen> 6 <nst> 1 101 2
     *endif
       NSECT = 1
     *if < <es_nen> /eq 4 > /then
                                         . Element connectivity for 4-node elts
       1 2 7 6 1 4 4
     *elseif < <es_nen> /eq 9 > /then
       1 3 13 11 2 8 12 6 7 1 2 2 . Element connectivity for 9-node elts
     *endif
                                         . Initialize all element datasets
 [xqt E
     stop
      *open 1
                                       . Form intrinsic stiffness matrices:
 *if <ifeqs([es_name];E43)> /then
                                               . for E43
     [xqt EKS
 *else
     *call ES (function='INITIALIZE')
                                                   for other elements
     *call ES (function='FORM STIFFNESS/MATL') .
 *endif
                                          . Resequence
 [xqt RSEQ
                                          . Create maps
 [xqt TOPO
                                          . Assemble system stiffness matrix
 [xqt K
                                          . Form applied loading
 [xqt AUS
      sysvec : appl moti
      i=1: J=5,25,5: -0.001
```

[xqt INV	. Factor stiffness matrix
online=2	
[xqt SSOL	. Solve for static displacements
stop	
*open 1	
-	. Calculate stresses
<pre>*if <ifeqs([es_name];e43)> /then</ifeqs([es_name];e43)></pre>	. for E43
[xqt GSF	
[xqt PSF	
reset display=2	
*else	. for other elements
<pre>+call ES ( function = 'FORM STRE:</pre>	SS'; es_dis_ds = STAT.DISP.1.1 )
*endif	
[xqt VPRT	. Print displacements
format=4	
print STAT DISP	
*end	

### 1.6.1.2 The Execution Control File

The file FLATPLATE.COM, listed below, contains no procedures, only the \*ADD and the \*CALL to the procedure defined in the previous section.

\$ testbed	! Execute Testbed macroprocessor		
<pre>*set echo off *open 1 flat_plate.l01</pre>	. Open data library		
*add flat_plate.clp	. Add procedure file BEFORE call		
*call FLAT_PLATE ( es_proc=ES1; es_name=Ex97 )			
[xqt EXIT	. Exit macroprocessor		

### **1.6.2 MACROSYMBOL USAGE EXAMPLE**

The runstream described in this section still contains only one procedure; that procedure is somewhat more complicated than the procedure of the first section although the problem to be solved is the same. The number of elements along x and y have been parameterized to allow for mesh convergence studies for the various elements. The logic of the procedure remains the same; there are simply more macrosymbol definitions. The procedure and the execution control file are listed in the following subsections.

### 1.6.2.1 The Procedure File

The following procedure is kept in a file named FLAT\_PLATE.CLP.

\*procedure FLAT\_PLATE ( es\_proc=ES1; es\_name=Ex97;-- )

```
NEL_x ; NEL_y )
  ARGUMENTS:
      es_proc: Independent element processor name
      es_name: Element name
      NEL_x: Number of elements in the x direction
                 Number of elements in the y direction
      NEL_y:
*if <ifeqs([es_name];E43)> /then
   *def/i es_nen = 4
*else
   *call ES ( function = 'DEFINE ELEMENTS'; es_proc = [es_proc]; --
             es_name = [es_name])
*endif
    Define necessary macrosymbols
     *def/i nn_x = <<[NEL_x]> + 1 > . Num. nodes in x-direction
*def/i nn_y = <<[NEL_y]> + 1 > . Num. nodes in v-direction
                                         . If 4-node elements are used:
*if << es_nen > /eq 4 > /then
     *def/i nn_total = <<nn_x>*<nn_y>> . Num. nodes total
*def/i nn_x = <2*<[NEL_x]> + 1 > . Num. nodes in x-direction

                                         . If 9-node elements are used:
                                         . Num. nodes in y-direction
     *def/i nn_y = <2*<[NEL_y]> + 1 >
     *def/i nn_total = <<nn_x>*<nn_y>> . Num. nodes total
*endif
[xqt TAB
                                         . Twenty-five joints; dof 6 zero
     START <nn_total> 6
                                         . Define joint locations
     JOINT LOCATIONS
                         0.0 2.5 0.0 0.0 <nn_x> 1 <nn_y>
             0.0
                   0.0
     1
                                   2.5 0.0
                 2.5
                        0.0 2.5
            0.0
   <nn_x>
     CONSTRAINT DEFINITION 1
                                          . Constraints
                                          . Plane 2,3 plane of symmetry
       symm plane=1
                                          . Plane 1,3 plane of symmetry
       symm plane=2
                                          . Constrain center w
       zero 3: 1
       nonzero 1 : <nn_x>,<nn_total>,<nn_x> . Apply displacement at x=lx edge
 [xqt AUS
 *def/e g = 3.84615e+6
                                          . Define material properties
      TABLE(NI=16,NJ=3): OMB DATA 1 1
       I=1,2,3,4,5,6,7,8,9
       J=1: 10.0E+6 .30 10.0E+6 <g> <g> <g> 0.0 0.0 .1
                                          . Define Section properties
      TABLE (NI=3,NJ=1,itype=0): LAM OMB 1 1
            J=1 : 2 .1 0.00
```

Examples

```
. Form constitutive matrix
[xqt LAU
    *if <ifeqs([es_name]; E43)>/ then
      reset SPAR=-1
    *endif
                                         . Define elements
[xqt ELD
    *if <ifeqs([es_name]; E43)>/ then
                                             E43 elements
      E43
    *else
      NOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt
                   were globally defined by procedure ES the first time
                   the procedure was called.
      *def/i nst = <<es_nip>*<es_nstr>> . Number of stress resultants
      EXPE [es_name] <es_nen> <es_opt> <es_nen> 6 <nst> 1 101 2
    *endif
      NSECT = 1
    *if < <es_nen> /eq 4 > /then
                                         . Use 4-node element mesh generator
      *def/i j1 = 1
       *def/i j2 = 2
       *def/i j3 = <<j2>+<nn_x>>
       *def/i j4 = <<j1>+<nn_x>>
                                         . Element connectivity for 4-node elts
      <j1> <j2> <j3> <j4> 1 <[NEL_x]> <[NEL_y]>
     *elseif < <es_nen> /eq 9 > /then
                                         . Use 9-node element mesh generator
      *def/i j1 = 1
      *def/i j5 = 2
       *def/i j2 = 3
       #def/i j8 = <<j1> + <nn_x>>
       *def/i j9 = <<j5> + <nn_x>>
       *def/i j6 = <<j2> + <nn_x>>
       *def/i j4 = <<j8> + <nn_x>>
       *def/i j7 = <<j9> + <nn_x>>
       *def/i j3 = <<j6> + <nn_x>>
                                         . Element connectivity for 9-node elts
       <j1> <j2> <j3> <j4> <j5> <j6> <j7> <j8> <j9> 1 <[NEL_x]> <[NEL_y]>
     *endif
                                         . Initialize all element datasets
[xqt E
    stop
    *open 1
                                       . Form intrinsic stiffness matrices
*if <ifeqs([es_name]; E43)>/ then
                                               . for E43
    [xqt EKS
*else
    *call ES (function='INITIALIZE')
```

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```
for other elements
   *call ES (function='FORM STIFFNESS/MATL') .
*endif
                                          . Resequence
[xqt RSEQ
                                          . Create maps
[xqt TOPO
                                          . Assemble system stiffness matrix
[xqt K
                                          . Form applied loading
[xqt AUS
     sysvec : appl moti
     i=1: J=<nn_x>,<nn_total>,<nn_x>:
                                       -0.001
                                          . Factor stiffness matrix
[xqt INV
     online=2
                                          . Solve for static displacements
[xqt SSOL
     stop
     *open 1
                                          . Calculate stresses
                                           for E43
*if <ifeqs([es_name]; E43)>/ then
   [xqt GSF
   [xqt PSF
        reset display=2
                                              for other elements
                                           .
*else
   *call ES ( function = 'FORM STRESS'; es_dis_ds = STAT.DISP.1.1 )
*endif
                                          . Print displacements
[xqt VPRT
     format=4
     print STAT DISP
*end
```

# 1.6.2.2 The Execution Control File

The file, FLATPLATE.COM, listed below contains no procedures, only the\*ADD and the \*CALL to the procedure defined in the previous section.

\$ testbed	! Execute Testbed macroprocessor		
<pre>*set echo off *open 1 flat_plate.101</pre>	. Open data library		
*add flat_plate.clp	. Add procedure file BEFORE call		
*call FLAT_PLATE ( es_proc=ES1; es_name=Ex97; Nel_x=4; Nel_y=4 )			
[xqt EXIT	. Exit macroprocessor		

One may notice that, except for the two extra arguments (NEL\_x and NEL\_y) in the \*CALL directive, this file is the same as the FLATPLATE.COM file of the last section.

## **1.6.3 A MULTIPLE PROCEDURE EXAMPLE**

In many cases, it may be to the user's advantage to build and maintain a procedure library which may be used for classes of problems. For example, in a solution library, one may keep procedures for providing linear static solutions, buckling eigenvalues, and nonlinear static solutions. In this section, the procedure of the previous section is split up into three procedures - PLATE\_MODEL, PLATE\_BC, and L\_STATIC - which generate the model, generate the boundary conditions, and perform the linear, static solution respectively. The three procedures are kept in two files: L\_STATIC.CLP (contains only procedure L\_STATIC) and FLATPLATE.PRC (contains PLATE\_MODEL and PLATE\_BC). Finally, the file FLATPLATE.COM uses the \*ADD directive to add the two files and the \*CALL directive to call the procedures.

## 1.6.3.1 The Model Generation Procedures

The following two procedures, PLATE\_MODEL and PLATE\_BC, are, for the sake of the example to be kept in a file named FLATPLATE.PRC. Note that the boundary conditions and applied loads are both in the procedure PLATE\_BC and that if other boundary conditions were desired, this procedure could be decoupled from the model generation procedure and stored in a separate file. In that case, the procedure name could be passed as an argument to PLATE\_MODEL which would then call the passed name instead of PLATE\_BC.

```
*procedure PLATE_MODEL ( es_proc ; es_name ; --
                          NEL_x ; NEL_y )
  ARGUMENTS:
      es_proc: Independent element processor name
                Element name
       es_name:
                 Number of elements in the x direction
       NEL_x:
                 Number of elements in the y direction
       NEL_y:
*if <ifeqs([es_name];E43)> /then
   *def/i es_nen = 4
*else
   *call ES ( function = 'DEFINE ELEMENTS'; es_proc = [es_proc]; --
              es_name = [es_name])
*endif
     Define necessary macrosymbols
                                         . If 4-node elements are used:
*if << es_nen > /eq 4 > /then
                                          . Num. nodes in x-direction
     #def/i nn_x = <<[NEL_x]> + 1 >
                                          . Num. nodes in y-direction
     *def/i nn_y = <<[NEL_y]> + 1 >
     #def/i nn_total = <<nn_x>#<nn_y>>
                                          . Num. nodes total
                                         . If 9-node elements are used:
*elseif << es_nen > /eq 9 > /then
                                          . Num. nodes in x-direction
     *def/i nn_x = <2*<[NEL_x]> + 1 >
                                          . Num. nodes in y-direction
     *def/i nn_y = <2*<[NEL_y]> + 1 >
                                          . Num. nodes total
     *def/i nn_total = <<nn_x>*<nn_y>>
*endif
```

[xqt TAB START <nn\_total> 6 . Twenty-five joints; dof 6 zero JOINT LOCATIONS . Define joint locations 0.0 2.5 0.0 0.0 <nn\_x> 1 <nn\_y> 0.0 0.0 1 0.0 2.5 2.5 2.5 0.0 <nn\_x> 0.0 . Call boundary condition procedure . to set up loads and b.c.'s \*call PLATE\_BC ( nn\_x = <nn\_x>; -nn\_total = <nn\_total> ) [xqt AUS \*def/e g = 3.84615e+6 TABLE(NI=16,NJ=3): OMB DATA 1 1 . Define material properties I=1,2,3,4,5,6,7,8,9 J=1: 10.0E+6 .30 10.0E+6 <g> <g> <g> 0.0 0.0 .1 . Define Section properties TABLE (NI=3,NJ=1,itype=0): LAM OMB 1 1 J=1 : 2 .1 0.00 . Form constitutive matrix [xqt LAU \*if <ifeqs([es\_name]; E43)> /then reset SPAR=-1 \*endif . Define elements [xqt ELD \*if <ifeqs([es\_name]; E43)> /then E43 elements E43 \*else NOTE -- The macrosymbols es\_nip, es\_nstr, es\_nen, and es\_opt were globally defined by procedure ES the first time the procedure was called. \*def/i nst = <<es\_nip>\*<es\_nstr>> . Number of stress resultants EXPE [es\_name] <es\_nen> <es\_opt> <es\_nen> 6 <nst> 1 101 2 \*endif NSECT = 1\*if < <es\_nen> /eq 4 > /then . Use 4-node element mesh generator \*def/i j1 = 1 +def/i j2 = 2\*def/i j3 = <<j2>+<nn\_x>> \*def/i j4 = <<j1>+<nn\_x>> . Element connectivity for 4-node elts <j1> <j2> <j3> <j4> 1 <[NEL\_x]> <[NEL\_y]> \*elseif < <es\_nen> /eq 9 > /then . Use 9-node element mesh generator

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```
*def/i j1 = 1
       *def/i j5 = 2
      *def/i j2 = 3
      *def/i j8 = << j1> + <nn_x>>
      *def/i j9 = << j5> + <nn_x>>
      *def/i j6 = << j2> + <nn_x>>
      *def/i j4 = <<j8> + <nn_x>>
      *def/i j7 = <<j9> + <nn_x>>
       *def/i j3 = << j6> + <nn_x>>
                                         . Element connectivity for 9-node elts
       <j1> <j2> <j3> <j4> <j5> <j6> <j7> <j8> <j9> 1 <[NEL_x]> <[NEL_y]>
     *endif
*end
*procedure PLATE_BC ( nn_x ; nn_total )
[xqt TAB
     CONSTRAINT DEFINITION 1
                                         . Constraints
                                         . Plane 2,3 plane of symmetry
       symm plane=1
                                         . Plane 1,3 plane of symmetry
       symm plane=2
                                         . Constrain center w
       zero 3: 1
      nonzero 1 : [nn_x],[nn_total],[nn_x] . Apply displacement at x=lx edge
                                         . Form applied loading
[xqt AUS
     sysvec : appl moti
     i=1: J=[nn_x],[nn_total],[nn_x]: -0.001
*end
```

### 1.6.3.2 The Linear Static Analysis Procedure

The following procedure performs the linear static analysis for models using either SPAR E43 elements or elements implemented using the generic element processors. The procedure will be kept in a file named  $L_STATIC.CLP$ .

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```
. Form intrinsic stiffness matrices
*if <ifeqs([es_name]; E43)> /then
                                                    for E43
                                                .
    [xqt EKS
*else
    *call ES (function='INITIALIZE')
    *call ES (function='FORM STIFFNESS/MATL') . for other elements
*endif
                                          . Resequence
[xqt RSEQ
                                          . Create maps
[xqt TOPO
                                          . Assemble system stiffness matrix
[xqt K
                                          . Factor stiffness matrix
[xqt INV
     online=2
                                          . Solve for static displacements
[xqt SSOL
     stop
     *open 1
                                          . Calculate stresses
*if <ifeqs([es_name]; E43)> /then
                                            for E43
   [xqt GSF
   [xqt PSF
        reset display=2
                                              for other elements
*else
   *call ES ( function = 'FORM STRESS'; es_dis_ds = STAT.DISP.1.1 )
*endif
                                          . Print displacements
[xqt VPRT
     format=4
     print STAT DISP
*end
```

## 1.6.3.3 The Execution Control File

The following file, FLATPLATE.COM, contains no procedures; it adds the two procedure files and calls the model generation and analysis procedures, PLATE\_MODEL and L\_STATIC.

```
$ testbed ! Execute Testbed macroprocessor
*set echo off
*open 1 flat_plate.101 . Open data library
.
*add flatplate.prc . Add procedure files BEFORE calls
*add l_static.clp
. Generate model
*call PLATE_MODEL ( es_proc=ES1; es_name=Ex97;--
nel_x=4; nel_y=4 )
. Solve for static solution
*call L_STATIC ( es_name=Ex97 )
.
[xqt EXIT . Exit macroprocessor
```

It should be emphasized that the procedure L\_STATIC may be used for any linear, static analysis using either the original SPAR elements or elements implemented using one or more of the Independent Element Processors. The procedure is not limited to SPAR E43

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elements as no element specific operations are being performed; element specific operations are performed in the model definition procedure(s).

By splitting the analysis into procedures, the model generation and solution have been decoupled allowing the solution procedure to be used for many different models. The advantages of this approach include the fact that a solution procedure need only be written once rather than once for each problem. It is highly recommended that the user organize procedures in this fashion. THIS PAGE LEFT BLANK INTENTIONALLY.

## 1.7 References

- 1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM 100644, October 1989.
- 1-2 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume I - The Language. NASA CR 178384, December 1988.
- 1-3 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.
- 1-4 Stanley, Gary and Nour-Omid, Shahram: The Computational Structural Mechanics Testbed Generic Structural-Element Processor Manual. NASA CR 181728, March 1990.

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# 2.0 Preprocessing Procedures

The five procedures documented in this chapter are general modeling procedures for specific structural geometries.

Procedure Name	Preprocessing Function	
GEN_BEAM	Generate 1-D models of straight beams using beam elements	
GEN_CANTILEVER	Generate 2-D models of a straight cantilever beam using plate/shell elements. Using the default values for the procedure arguments, the straight cantilever beam problem from the MacNeal-Harder test cases is generated.	
GEN_CURVED_BM	Generate 2-D models of a curved (circular) beam us- ing plate/shell elements. Using the default values for the procedure arguments, the curved beam problem from the MacNeal-Harder test cases is generated.	
GEN_PLATE	Generates 2-D models for general quadrilateral plates.	
GEN_SHELL	Generates 2-D models for general shells and curved surfaces.	

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# 2.1 Procedure GEN\_BEAM

# 2.1.1 GENERAL DESCRIPTION

This section describes a procedure which generates models of a straight beam using onedimensional beam elements.

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## 2.1.2 PROCEDURE USAGE

Procedure GEN\_BEAM may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

## \*call GEN\_BEAM ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN\_BEAM are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES6	Select element processor
ES_NAME	E210	Select element within ELT_PROC
NODES_X	3	Number of nodes in x-direction
LENGTH_X	10.	Length of beam
Е	120.	Young's elastic modulus
NU	0.	Poisson's ratio
AREA	1.0	Cross-sectional area
INERT_1	1.	Principal moment of inertia, $I_1$
INERT_2	10.	Principal moment of inertia, $I_2$
INERT_TORSIONAL	1.	Uniform torsion constant
BC_PROCEDURE	BEAM_BC	Procedure for boundary conditions

#### 2.1.3 ARGUMENT DESCRIPTIONS

#### 2.1.3.1 AREA

Cross-sectional area of beam (default: 1.0).

#### 2.1.3.2 BC\_PROCEDURE

Boundary condition procedure name (default: CC\_BC for specified forces; CCD\_BC for specified displacements). The term "boundary conditions" refers both to displacement constraints and applied loading. Procedures CC\_BC and CCD\_BC both have the same zero displacement constraints. The only difference is that the former procedure applies axial forces to the simply supported edge, while the latter procedure prescribes non-zero axial displacements on that edge. The argument BC\_PROCEDURE permits you to to supply your own boundary condition procedure, but keep in mind that this may drastically change the problem definition, and hence invalidate most of the discussion under Section 2.1.1.

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## 2.1.3.3 <u>E</u>

Young's elastic modulus (default: 120.0).

## 2.1.3.4 ES\_NAME

Element name (default: E210). This is the name of the specific beam-element type you wish to select, within the element processor defined by argument ES\_PROC. The default element type, E210, is a 2-noded beam element implemented in processor ES6, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.1-1).

## 2.1.3.5 ES\_PROC

Element Processor (default: ES6) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES6, is described in The Computational Structural Mechanics Testbed User's Manual.

## 2.1.3.6 <u>INERT\_1</u>

Principal moment of inertia (default: 1.0).

## 2.1.3.7 <u>INERT\_2</u>

Principal moment of inertia (default: 10.0).

## 2.1.3.8 INERT\_TORSION

Torsional constant (default: 1.0).

## 2.1.3.9 <u>LENGTH\_X</u>

Length of the beam in the x-direction (default: 10.0).

## 2.1.3.10 <u>NODES\_X</u>

Number of nodes along beam length (default: 3). Note that this number should be consistent with the number of nodes per element. For example, NODES\_X can be any number greater than 1 for 2-node beam elements, whereas it must be an odd number greater than 1 for 3-node beam elements.

## 2.1.3.11 <u>NNODES\_C</u>

Number of circumferential nodes (default: 7). This is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, *i.e.*, along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_C can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 2.1.3.12 <u>NU</u>

Poisson's ratio (default: 0.0).

## 2.1.4 USAGE GUIDELINES AND EXAMPLES

Procedure GEN\_BEAM may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call GEN\_BEAM

#### 2.1.5 LIMITATIONS

#### 2.1.6 ERROR MESSAGES AND WARNINGS

None.

#### 2.1.7 PROCEDURE FLOWCHART

#### 2.1.8 PROCEDURE LISTING

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```
START <nodes_tot>
JLOC
. DEFINE NODAL COORDINATES
*def/e dx = < [length_x] / ([nodes_x]-1) >
*def/i node = 0
  *def/e x = 0.
  *do $i = 1, [nodes_x]
     *def node = < <node> + 1 >
                                      . NODE DEFINITION
      <node> <x>, 0., 0.
     *def x = < <x> + <dx> >
  *enddo
. DEFINE FICTITIOUS ELASTIC MATERIAL PROPERTIES
MATC
1 [E] [PR]
. BEAM FACE ORIENTATION AND PROPERTIES
  MREF
  FORMAT=2
  1 1 0. 1.0 0.
  BA
  GIVN 1 [inert_1] 0. [inert_2] 0. [area] [inert_torsion]
. DEFINE LOADS AND BOUNDARY CONDITIONS
 *call [BC_PROCEDURE] ( nnx = [nodes_x] ; --
                       nen = <es_nen> )
 . GENERATE ELEMENTS
        [XQT ELD
   <es_expe_cmd>
   NSECT = 1
 .
     Define element nodal connectivity
     *call BM_ELT_CONN (nnx=[nodes_x]; nen=<es_nen>)
 *end
 . =DECK BM_ELT_CONN
 *procedure BM_ELT_CONN ( nnx; nen )
         . Define Element Connectivity Record for ELD Processor
```

```
*if < [nen] /eq 2 > /then
     *do $ix = 1, <[nnx]-1>
        *def/i n1 = < $ix >
        *def/i n2 = < <n1> +
                             1 >
         -----
         <n1> <n2>
         ********
     *enddo
*elseif < [nen] /eq 3 > /then
     *do $ix = 1, <[nnx]-2>, 2
        *def/i n1 = < $ix >
        *def/i n2 = < <n1> + 2 >
         *def/i n3 = < <n2> - 1 >
         ------
         <n1> <n2> <n3>
        ************
      *enddo
*endif
```

\*end

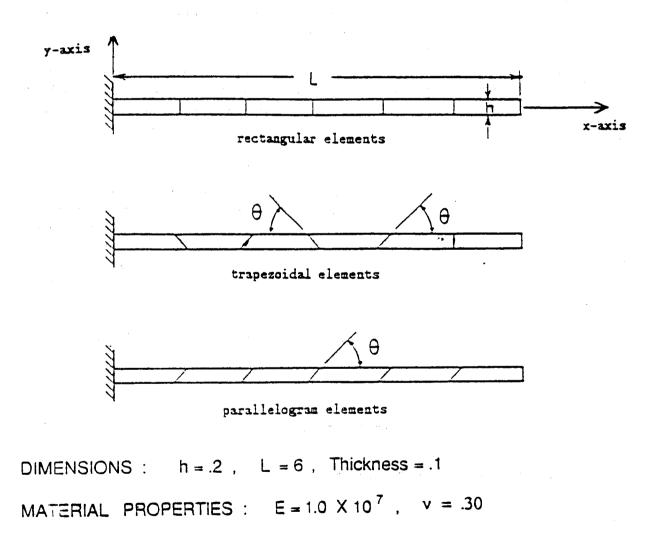
#### 2.1.9 REFERENCES

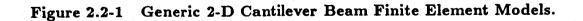
2.1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

## 2.2 Procedure GEN\_CANTILEVER

#### 2.2.1 GENERAL DESCRIPTION

This section describes a procedure which generates models of a straight cantilever beam using two-dimensional plate/shell elements. Using the default values for the procedure arguments, the straight cantilever beam problem from the MacNeal-Harder test cases (see ref. 2.2-1) is generated. The model used for the MacNeal-Harder cantilever beam test cases, is shown in figure 2.2-1.





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#### 2.2.2 PROCEDURE USAGE

Procedure GEN\_CANTILEVER may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

## \*call GEN\_CANTILEVER ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN\_CANTILEVER are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
ES_PROC	ES2	Select element processor
ES_NAME	EX41	Select element with ELT_PROC
ES_PARS	0.0	Set element-research parameters
AUTO_DOF_SUP	true	Automatic d.o.f. suppression
DRILLING_DOF	false	
NODES_X	7	Number of nodes in x-direction
NODES_Y	2	Number of nodes in y-direction
LENGTH_X	6.	Beam length (x-direction)
LENGTH_Y	.2	Beam width (y-direction)
E	1.E7	Young's elastic modulus
NU	.3	Poisson's ratio
THICKESS	.1	Thickness
DISTORT	.07071	
BC_PROCEDURE	CANTILEVER_BC	Procedure for boundary conditions

#### 2.2.3 ARGUMENT DESCRIPTIONS

#### 2.2.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

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#### 2.2.3.2 BC\_PROCEDURE

Boundary condition procedure name (default: CANTILEVER\_BC). The term "boundary conditions" refers both to displacement constraints and applied loading. The argument BC\_PROCEDURE permits the users to supply their own boundary condition procedure, but keep in mind that this may drastically change the problem definition.

#### 2.2.3.3 <u>DISTORT</u>

Distorted mesh parameter (default: 0.07071).

#### 2.2.3.4 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active -unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

#### 2.2.3.5 <u>E</u>

Young's elastic modulus (default:  $1.0 \times 10^7$ ).

#### 2.2.3.6 ES\_NAME

Element name (default: EX41). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX41, is a 4-noded quadrilateral element implemented in Processor ES2, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.2-1).

#### 2.2.3.7 ES\_PARS

Element research parameters (default: 0., ...). This argument allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 2.2.3.8 ES\_PROC

Element processor (default: ES2) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES2, is described in The Computational Structural Mechanics Testbed User's Manual.

## 2.2.3.9 NODES\_X

Number of nodes along x-direction (default: 7). This is the number of nodes you wish to have along the axial direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES\_X can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

#### 2.2.3.10 NODES\_Y

Number of nodes along y-direction (default: 2). This is the number of nodes you wish to have along the depth direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES\_Y can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 2.2.3.11 <u>NU</u>

Poisson's ratio (default: 0.3).

#### 2.2.3.12 THICKNESS

Beam thickness (default: 0.1).

## 2.2.4 USAGE GUIDELINES AND EXAMPLES

Procedure GEN\_CANTILEVER may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
= ES2 ; es_name = EX41 ; --
*call GEN_CANTILEVER ( es_proc
                       es_pars
                                     = 0.0 ; ---
                       auto_dof_sup = <true> ; --
                       drilling_dof
                                      = <false> ; --
                                      = 7
                                            ; nodes_y
                                                         = 2
                                                                :
                       nodes_x
                                            ; length_y = .2
                                                                ; --
                                      = 6.
                       length_x
                                             ; thickness = .1
                                                                 ; --
                       E=1.E7 ;
                                     NU=.3
                                      =.07071; --
                       distort
                       BC_PROCEDURE = CANTILEVERLEVER_BC )
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

\*call GEN\_CANTILEVER

#### 2.2.5 LIMITATIONS

## 2.2.6 ERROR MESSAGES AND WARNINGS

None.

#### 2.2.7 PROCEDURE FLOWCHART

#### 2.2.8 PROCEDURE LISTING

```
= ES2 ; es_name = EX41 ; --
*procedure GEN_CANTI ( es_proc
                           = 0.0 ; --
                   es_pars
                   auto_dof_sup = <true> ; --
                   drilling_dof = <false> ; --
                   nodes_x = 7 ; nodes_y = 2 ; --
length_x = 6. ; length_y = .2 ; --
                   E=1.E7 ; NU=.3 ; thickness = .1 ; --
                              =.07071; --
                   distort
                   BC PROCEDURE = CANTILEVER_BC )
      ______
   Register Element and Define Macros: ELT_NEN, ELT_NIP, ELT_NSTR, etc.
   *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
            es_name = [es_name] ; es_pars = [es_pars] )
[XQT TAB
*def nodes_tot = < [nodes_x] * [nodes_y] >
START <nodes_tot>
JLOC
. DEFINE NODAL COORDINATES
*def/e dx = < [length_x] / ([nodes_x]-1) >
*def/e dy = < [length_y] / ([nodes_y]-1) >
*def/i node = 0
\pm def/ey = 0.
*def/e skew = < -1. * [distort] >
*def/e dskew = < 2.0 * [distort] / ([nodes_y]-1) >
*do $j = 1,[nodes_y]
     def/e = 0.
```

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```
*do $i = 1, [nodes_x]
     *def node = < <node> + 1 >
                                          . NODE DEFINITION
      <node> <x>, <y>, 0.
     *def x = < <x> + <dx> >
        *if < <$i>/eq 1 > /then
           *def x = < <x> + <skew> >
        *endif
        *if < <$i> /eq <[nodes_x]-1> > /then
           *def x = < [length_x] >
        *endif
  *enddo
  *def y = < <y> + <dy> >
  *def skew = < <skew> + <dskew> >
*enddo
. DEFINE FICTITIOUS ELASTIC MATERIAL PROPERTIES
MATC
1 1.0 .3
. DEFINE LOADS AND BOUNDARY CONDITIONS
 *call [BC_PROCEDURE] ( nnx = [nodes_x] ; nny = [nodes_y] ; --
                        nen = <es_nen> ; drilling_dof = [drilling_dof] )
. DEFINE REAL MATERIAL/SECTION PROPERTIES
[XQT AUS
. Build Table of Material Data
TABLE(NI=16,NJ=1): OMB DATA 1 1
*def/e12.4 G = < [E] / (2.*(1.+[NU])) >
I=1,2,3,4,5,6
1=1
[E] [NU] [E] <G> <G> <G>
. Build Laminate Data Tables
TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
I=1,2,3 . (material_type, layer_thickness, angle(deg.)
                                                   0.0
                            [THICKNESS]
               1
J=1:
[XQT LAU
. GENERATE ELEMENTS
       [XQT ELD
       Define number of integration (stress) points based on element type
      *def/i nst = < <es_nip>*<es_nstr> >
```

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```
Define element attributes
   <ES_EXPE_CMD>
   NSECT = 1
    Define element nodal connectivity
   *call CANTI_ELT_CONN (nnx=[nodes_x]; nny=[nodes_y]; nen=<es_nen>)
    Suppress DOFs not supported by elements
    *if < [AUTO_DOF_SUP] > /then
      *call ES ( function = 'DEFINE FREEDOMS' )
    *endif
*end
*procedure CANTI_ELT_CONN ( nnx; nny; nen )
       . Define Element Connectivity Record for ELD Processor
       ------
  *if < [nen] /eq 4 > /then
    *do $iy = 1, <[nny]-1>
       *do $ix = 1, <[nnx]-1>
         *def/i n1 = < (<$iy>-1)*[nnx] + <$ix> >
         *def/i n2 = < <n1> + 1 >
         *def/i n3 = < <n2> + [nnx] >
         *def/i n4 = < <n3> - 1 >
          ________________
          <n1> <n2> <n3> <n4>
          *enddo
    #enddo
  *elseif < [nen] /eq 9 > /then
    *do $iy = 1, <[nny]-2>, 2
       *do $ix = 1, <[nnx]-2>, 2
         *def/i n1 = < (<$iy>-1)*[nnx] + <$ix> >
         *def/i n2 = < <n1> + 2 >
         *def/i n3 = < <n2> + (2*[nnx]) >
         *def/i n4 = < <n3> - 2 >
         *def/i n5 = < <n1> + 1 >
         *def/i n6 = < <n2> + [nnx] >
         *def/i n7 = < <n4> + 1 >
         *def/i n8 = < <n6> - 2 >
         *def/i n9 = < <n8> + 1 >
         <n1> <n2> <n3> <n4> <n5> <n6> <n7> <n8> <n9>
```

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```
*enddo
*enddo
*endif
*end
```

#### 2.2.9 REFERENCES

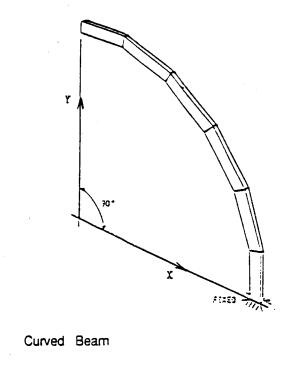
- 2.2-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
- 2.2-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

## 2.3 Procedure GEN\_CURVED\_BM

#### 2.3.1 GENERAL DESCRIPTION

PROBLEM :

This section describes a procedure which generates models of a curved (circular) beam using two-dimensional plate/shell elements. Using the default values for the procedure arguments, the curved beam problem from the MacNeal-Harder test cases (see ref. 2.3-1) is generated. The MacNeal-Harder curved beam test case is shown in figure 2.3-1.



DIMENSIONS : Inner radius = 4.12 Outer radius = 4.32 Thickness = .1

MATERIAL PROPERTIES :  $E = 1 \times 10^7$  v = .25

SOUNDARY CONDITIONS : Cantelever beam fixed at y = 0

LOADING : Unit forces applied at free end ; 1) in-plane (vertical) -- y-direction (case 1) 2) out-of-plane -- z-direction (case 2)

Figure 2.3-1 Generic 2-D Curved Beam Problem.

## 2.3.2 PROCEDURE USAGE

Procedure GEN\_CURVED\_BM may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call GEN_CURVED_BM ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN\_CURVED\_BM are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES2	Select element processor
ES_NAME	EX41	Select element within ELT_PROC
ES_PARS	0.0	Set element-research parameters
AUTO_DOF_SUP	<true></true>	Automatic d.o.f. suppression
DRILLING_DOF	<false></false>	
NODES_T	7	Number of nodes in tangential direction
NODES_R	2	Number of nodes in radial direction
RIN	4.12	Inner radius
ROUT	4.32	Outer radius
E	1.E7	Young's elastic modulus
NU	. 25	Poisson's ratio
THICKNESS	. 1	Thickness
BC_PROCEDURE	CURVED_BC	Procedure for boundary conditions

## 2.3.3 ARGUMENT DESCRIPTIONS

#### 2.3.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

### 2.3.3.2 BC\_PROCEDURE

Boundary condition procedure name (default: CURVED\_BC). The term "boundary conditions" refers both to displacement constraints and applied loading. The argument BC\_PROCEDURE permits you to to supply your own boundary condition procedure, but keep in mind that this may drastically change the problem definition.

## 2.3.3.3 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

#### 2.3.3.4 <u>E</u>

Young's elastic modulus (default:  $1.0 \times 10^7$ ).

#### 2.3.3.5 <u>ES\_NAME</u>

Element name (default: EX41). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX41, is a 4-noded quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.3-1).

#### 2.3.3.6 ES\_PARS

Element research parameters (default: 0., ...). This argument allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

#### 2.3.3.7 ES\_PROC

Element processor (default: ES2) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES2, is described in The Computational Structural Mechanics Testbed User's Manual.

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#### 2.3.3.8 <u>NODES\_R</u>

Number of radial nodes (default: 2). This is the number of nodes you wish to have along the radial direction of the curved beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES\_R can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 2.3.3.9 <u>NODES\_T</u>

Number of tangential nodes (default: 7). This is the number of nodes you wish to have along the tangential direction of the curved beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES\_T can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

#### 2.3.3.10 <u>NU</u>

Poisson's ratio (default: 0.25).

## 2.3.3.11 <u>RIN</u>

Inner radius of curved beam (default: 4.12).

#### 2.3.3.12 ROOT

Outer radius of curved beam (default: 4.32).

#### 2.3.3.13 THICKNESS

Beam thickness (default: 0.1).

## 2.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure GEN\_CURVED\_BM may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

= ES2 ; elt\_name = EX41 ; --\*procedure GEN\_CURVED\_BM (elt\_proc = 0.0 ; -elt\_pars auto\_dof\_sup = <true> ; -drilling\_dof = <false> ; ---; nodes\_r 2 = 7 nodes\_t 4.32 = 4.12; rout rin = .1 E=1.E7 ; ; thick PR=.25  $BC_PROCEDURE = CURVED_BC$ )

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

\*call GEN\_CURVED\_BM

#### 2.3.5 LIMITATIONS

2.3.6 ERROR MESSAGES AND WARNINGS

None.

#### 2.3.7 PROCEDURE FLOWCHART

#### 2.3.8 PROCEDURE LISTING

```
= ES2 ; es_name = EX41 ; --
*procedure GEN_CURVED (es_proc
                  es_pars = 0.0; --
                  auto_dof_sup = <true> ; --
                  drilling_dof = <false> ; --
                  nodes_t = 7 ; nodes_r = 2 ; --
                            = 4.12 ; rout = 4.32 ; --
                  rin
                  E=1.E7 ; NU=.25 ; thickness = .1 ; --
                  BC_PROCEDURE = CURVED_BC )
   Register Element and Define Macros: ELT_NEN, ELT_NIP, ELT_NSTR, etc.
   *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
            es_name = [es_name] ; es_pars = [es_pars] )
[XQT TAB
*def nodes_tot = < [nodes_t] * [nodes_r] >
START <nodes_tot>
JLOC
                           . use cylindrical coordinate system
     FORMAT = 2
. DEFINE NODAL COORDINATES
*def/e dx = < 90. / ([nodes_t]-1) >
*def/e dy = < < [rout] - [rin] > / ([nodes_r]-1) >
*def/i node = 0
*def/e r = [rin]
   $j = 1,[nodes_r]
*do
    *def/e theta = 90.
  *do  $i = 1,[nodes_t]
    *def node = < <node> + 1 >
```

```
. NODE DEFINITION
      <node> <r>>, <theta>, 0.
     *def theta = < <theta> - <dx> >
  *enddo
     *def r = < <r> + <dy> >
*enddo
. DEFINE FICTITIOUS ELASTIC MATERIAL PROPERTIES
MATC
1 1.0 .3
      Define DOF Directions
      ------
                                    Use local cylindrical basis vectors
         JREF
                                    for nodal DOFS:
                                    u,v,w = radial, circumfer., axial
         NREF = -1
                                   same convention for all nodes
         1 <nodes_tot>
                                 .
. DEFINE LOADS AND BOUNDARY CONDITIONS
 *call [BC_PROCEDURE] ( nnx = [nodes_t] ; nny = [nodes_r] ; --
                       nen = <es_nen> ; drilling_dof = [drilling_dof] )
. DEFINE REAL MATERIAL/SECTION PROPERTIES
[XQT AUS
. Build Table of Material Data
TABLE(NI=16,NJ=1): OMB DATA 1 1
*def/e12.4 G = < [E] / (2.*(1.+[NU])) >
I=1,2,3,4,5,6
J=1
[E] [NU] [E] <G> <G> <G>
. Build Laminate Data Tables
TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
I=1,2,3 . (material_type, layer_thickness, angle(deg.)
                           [THICKNESS]
                                                 0.0
J=1:
              1
[XQT LAU
. GENERATE ELEMENTS
       [XQT ELD
       Define number of integration (stress) points based on element type
 .
      *def/i nst = < <es_nip>*<_nstr> >
```

#### **Pre-Processing Procedures**

```
Define element attributes
   <ES_EXPE_CMD>
  NSECT = 1
    Define element nodal connectivity
    *call CURV_ELT_CONN (nnx=[nodes_t]; nny=[nodes_r]; nen=<es_nen>)
    Suppress DOFs not supported by elements
     _____
     *if < [AUTO_DOF_SUP] > /then
       *call ES ( function = 'DEFINE FREEDOMS' )
     *endif
*end
*procedure CURV_ELT_CONN ( nnx; nny; nen )
       . Define Element Connectivity Record for ELD Processor
       *if < [nen] /eq 4 > /then
     *do $iy = 1, <[nny]-1>
       *do $ix = 1, <[nnx]-1>
          *def/i n1 = < (<$iy>-1)*[nnx] + <$ix> >
          *def/i n2 = < <n1> + 1
                                >
          *def/i n3 = < <n2> + [nnx] >
          *def/i n4 = < <n3> ~ 1 >
          ************************
          <n1> <n2> <n3> <n4>
          *enddo
    *enddo
  *elseif < [nen] /eq 9 > /then
    *do $iy = 1, <[nny]-2>, 2
       *do $ix = 1, <[nnx]-2>, 2
         *def/i n1 = < (<$iy>-1)*[nnx] + <$ix> >
          #def/i n2 = < <n1> + 2 >
          *def/i n3 = < <n2> + (2*[nnx]) >
          *def/i n4 = < <n3> - 2 >
         *def/i n5 = < <n1> + 1 >
         *def/i n6 = < <n2> + [nnx] >
         *def/i n7 = < <n4> + 1 >
         *def/i n8 = < <n6> - 2 >
         *def/i n9 = < <n8> + 1 >
         <n1> <n2> <n3> <n4> <n5> <n6> <n7> <n8> <n9>
```

## 2.3.9 REFERENCES

- 2.3-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," *Finite Elements in Analysis and Design*, Vol. 1, 1985, pp. 3-20.
- 2.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

## 2.4 Procedure GEN\_PLATE

## 2.4.1 GENERAL DESCRIPTION

Procedure GEN\_PLATE is used to generate flat or warped 4-sided plate finite element models. The plate edges are defined to be straight with the surface defined as the bi-linearly interpolation of the edges. This type of interpolated surface is also known as a Coon's surface (see refs. 2.4-2 and 2.4-3).

## 2.4.2 PROCEDURE USAGE

Procedure GEN\_PLATE may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call GEN_PLATE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) preceded by a space may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN\_PLATE are summarized in the following table, along with their default values (if they exist). Exceptions to this rule are noted in the following section under detailed argument descriptions.

i

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Generic element processor
ES_NAME	EX97	Generic element name
ES_PARS	0.0	Element research parameters
XYZ1	1,0,0	Cartesian coordinates of point 1.
XYZ2	1,0,1	Cartesian coordinates of point 2.
XYZ3	1,90,1	Cartesian coordinates of point 3.
XYZ4	1,90,0	Cartesian coordinates of point 4.
NODES_1	7	Number of nodes along edge 1
NODES_2	7	Number of nodes along edge 2
		including duplicate nodes if plate closes
EDGE_WEIGHTS	1,1,1,1	Plate section property procedure
BC_PROCEDURE	> >	Boundary condition procedure
DRILLING_DOF	<true></true>	Drilling dof suppression flag
AUTO_DOF_SUP	<true></true>	Automatic dof suppression flag
SECTION_PRC	, ,	Plate section property procedure
NSECT	1	Plate section property number
The following va	lues not used if SE	CTION_PRC is specified.
Е	30.E6	Young's Modulus
NU	0.3	Poisson's ratio
WTDEN	0.1	Weight Density
THICKNESS	.1	Plate thickness

#### 2.4.3 ARGUMENT DESCRIPTIONS

#### 2.4.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffness (see argument DRILLING\_DOF).

#### 2.4.3.2 BC\_PROCEDURE

Name of user provided boundary condition procedure (default: ' '). The term "boundary conditions" refers both to displacement constraints and applied loading. If a boundary conditions procedure is provided, the following call will be performed. The macrosymbol <cs\_nen> equals the number of element nodes.

No action is taken if a boundary condition procedure name is not provided.

#### 2.4.3.3 DRILLING\_DOF

Drilling degree of freedom flag (default:  $\langle true \rangle$ ). Drilling freedoms are defined as rotations normal to the surface of the plate. Setting this flag set to  $\langle false \rangle$  forces all drilling freedoms in the model to be suppressed. Setting it to true forces all drilling freedoms to be active — unless they are automatically suppressed by use of the AUTO\_DOF\_SUP argument. Note that while many plate elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when plate elements are assembled as facets approximating an arbitrary plate surface, there is usually some misalignment between the element normal and the actual plate normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the plate normal is usually present in the model. (A clear exception to this is a flat plate, where element and plate normals are identical.) For a curved plate, the misalignment diminishes only as the number of elements is increased. Most plate elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

#### 2.4.3.4 <u>E</u>

Young's modulus (default: 30.E6). This argument is ignored if SECTION\_PRC parameter is specified. See the description for SECTION\_PRC for more detail.

#### 2.4.3.5 EDGE\_WEIGHTS

Node placement can be weighted along each surface edge according to the EDGE\_WEIGHTS parameter. The input format requires a list of four edge-node placement weightings representing the node weighting for edge1, edge2, edge3, and edge4 (default: 1.,1.,1.,1.).

The weighting value for a given edge represents the length of the last element divided by the length of the first element along that edge. The edge orientation arrows in figure 2.4-1 point from the first element to the last element along each edge. In the case of 9-node quad elements, the midside and center nodes are positioned at the appropriate locations based on the elements natural coordinate system.

The procedure interprets negative weight values to mean the positive reciprocal. For example, a value of -5.0 is identical to a value of 0.2.

#### 2.4.3.6 ES\_NAME

Element name (default: EX97). This argument is the name of the specific plate-element type you wish to select, within the element processor defined by argument ES\_PROC. The default plate-element type, EX97, is a 9-node quadrilateral element implemented in processor ES1, and described reference 2.4-1.

#### 2.4.3.7 ES\_PARS

Element research parameters (default: 0., ...). This argument is an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 2.4.3.8 ES\_PROC

Element processor (default: ES1) This argument is the name of the structural element (ES) processor that contains the plate element type you wish to employ in the model. The default plate-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

## 2.4.3.9 <u>NODES\_1</u>

Number of nodes on edge 1 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 3. This number should be consistent with the element type selected. For example, NODES\_1 can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 2.4.3.10 <u>NODES\_2</u>

Number of nodes on edge 2 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 4. This number should be consistent with the element type selected. For example, NODES\_2 can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 2.4.3.11 NSECT

Plate section property number (default: 1). The NSECT value is required when defining the element using the processor ELD. See the description of SECTION\_PRC for more detail.

## 2.4.3.12 NU

Poisson's ratio (default: 0.3). This argument is ignored if the SECTION\_PRC input parameter is specified. See the description of SECTION\_PRC for more detail.

## 2.4.3.13 XYZ1

The cartesian coordinates (x, y, z) which define corner number 1 of the model surface. The form of the input is three real values, each separated by a comma (default: 1.,0.,0.). The surface is defined by four edges which are defined as a linear interpolation in cartesian coordinates of four endpoints, or "corner" points.

## 2.4.3.14 XYZ2

The cartesian coordinates (x, y, z) defining the corner number 2 of the model surface (default: 1.,0.,1.).

## 2.4.3.15 XYZ3

The cartesian coordinates (x, y, z) defining the corner number 3 of the model surface (default: 1.,90.,1.).

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## 2.4.3.16 XYZ4

The cartesian coordinates (x, y, z) defining the corner number 4 of the model surface (default: 1.,90.,0.).

## 2.4.3.17 SECTION\_PRC

Name of a user supplied procedure to define the plate section properties (default = ' '). If a section properties procedure is provided, the following call will be performed.

\*call [section\_prc] ( nsect = [nsect] )

The effect of the default is to allow the procedure to generate an isotropic material section based on the input parameters E, NU, WTDEN, and THICKNESS. The section number is defined by the input parameter NSECT. If the call parameter SECTION\_PRC is defined by the user, then call parameters E, NU, WTDEN, and THICKNESS are ignored by procedure GEN\_PLATE.

#### 2.4.3.18 THICKNESS

Thickness of the plate wall (default = 1.0). This argument is ignored if SECTION\_PRC parameter is specified. See the description for SECTION\_PRC for more detail.

## 2.4.3.19 WTDEN

Weight density expressed in lb/in.<sup>3</sup> (default: 0.1 lb/in.<sup>3</sup>). This argument is ignored if the SECTION\_PRC input parameter is specified. Processor LAU will convert the weight density to mass density using the gravitational acceleration constant 386.4 in/sec<sup>2</sup>.

## 2.4.4 USAGE GUIDELINES AND EXAMPLES

Procedure GEN\_PLATE may be invoked using the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values in the procedure call. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*procedure GEN_PLATE ( ES_PROC = ES1 ; ES_NAME = EX97 ; ES_PARS = 0.0 ; --
                             = 0.,0.,0.; --
               XYZ1
                             = 1.,0.,0.; --
               XYZ2
                             = 1., 1., 0.;
               XYZ3
                             = 0., 1., 0.; --
               XYZ4
                             = 3 : --
               NODES_1
                             = 3 ; --
               NODES_2
               EDGE_WEIGHTS = 1.,1.,1.,1.; --
               BC_PROCEDURE = ' '; -- . Boundary condition procedure
               DRILLING_DOF = <true> ; --
               AUTO_DOF_SUP = <true> ; --
               SECTION_PRC = ' '; -- . Plate section property procedure
                                        . Plate section property ID
               NSECT = 1 ; --
               The following values not used if SECTION_PRC specified
```

```
E = 30.E6 ; -- . Young's Modulus
NU = .3 ; -- . Poissons ratio
THICKNESS = .1 -- . Plate thickness
```

## 2.4.4.1 Mesh Generation

)

The method of surface generation used by procedure GEN\_PLATE is described in the section. Terminology depicted on figure 2.4-1 provides a visual interpretation of the parameters used to generate a general plate surface. Node generation capability is provided by the Testbed processor MESH.

To define the plate surface, the user defines four coordinate positions in the cartesian reference frame. These coordinate positions represent the corners of a straight-sided quadrilateral region. The surface of the region is defined as the bi-linear interpolation of the four sides (see refs. 2.4-2 and 2.4-3).

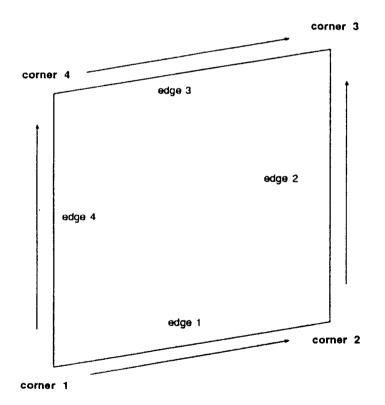


Figure 2.4-1 Generic Plate Surface Topology.

The connectivity of the surface is defined in figure 2.4-1. The user provides the coordinates for corners 1 to 4. Edge 1 of the region starts at corner 1 and ends at corner 2. The remaining edges are defined in a similar manner. The arrows indicate the orientation of the edges and the direction of increasing node numbers.

The topology of the resulting finite element grid is depicted in Figure 2.4-2. Nodes are created first along edge 1, then in successive lines terminating along edge 3. The user defines the number of nodes along edges 1 and 2, which also defines the number of nodes for edges 3 and 4. The relative position of the nodes along each edge may be controlled using the edge weighting parameter EDGE\_WEIGHTS.

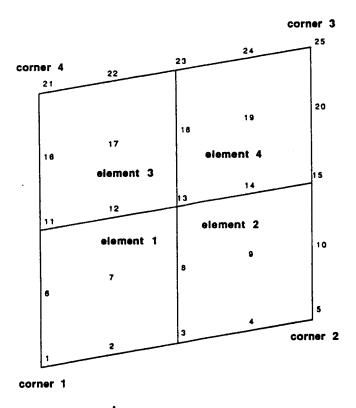


Figure 2.4-2 Node and Element Topology.

# 2.4.4.2 Flat Plates

In this section are presented examples of how procedure GEN\_PLATE may be used to create two-dimensional finite element plate models.

In the following example, procedure GEN\_PLATE is used to generate a flat rectangular plate with length of 10 inches and width of 5 inches using 4-noded quadrilateral elements (see figure 2.4-3).

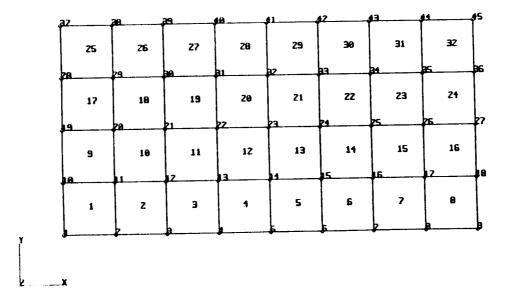
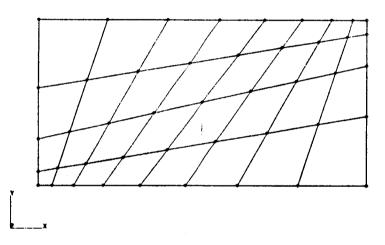


Figure 2.4-3 Rectangular Plate

This example demonstrates the use of the EDGE\_WEIGHTS parameter and how it affects both the 4-node and 9-node quadrilateral element mapping (see figure 2.4-4). The EDGE\_WEIGHTS specifies elements at the ends of edges 1 through 4 to be 5 times longer than elements at the beginning of the edges.

```
*call GEN_PLATE ( es_proc = 'ES1' ; es_name = 'EX97' ; --
    xyz1 = 0.,0.,0. ; --
    xyz2 = 10.,0.,0. ; --
    xyz3 = 10.,5.,0. ; --
    xyz4 = 0.,5.,0. ; --
    nodes_1 = 9 ; --
    nodes_2 = 5 ; --
    edge_weights = 5.,-5.,5. )
```



(a) 4-node elements

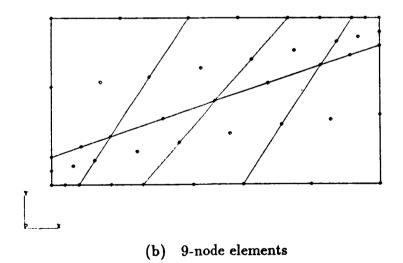


Figure 2.4-4 Rectangular Plate With Weighted Elements

The following example produced the skewed flat plate shown in figure 2.4-5.

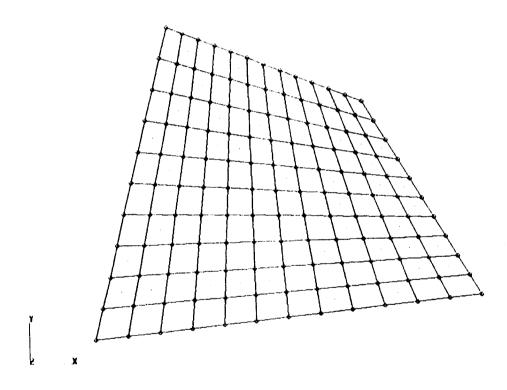


Figure 2.4-5 Skewed Flat Plate

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#### 2.4.4.3 Warped Plates

In the following example, procedure GEN\_PLATE is used to generate the highly warped surface shown in figure 2.4-6.

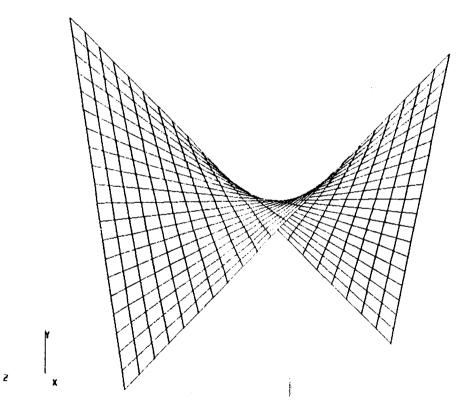


Figure 2.4-6 Warped Plate

# 2.4.5 LIMITATIONS

None.

# 2.4.6 ERROR MESSAGES AND WARNINGS

None.

# 2.4.7 PROCEDURE FLOWCHART

GEN_PLATE	(Plate generation procedure)
[BC_PROCEDURE]	(user supplied boundary conditions/loads procedure)
[SECTION_PRC]	(user supplied section property generation procedure)

# 2.4.8 PROCEDURE LISTING

```
*procedure GEN_PLATE ( es_proc = es1 ; es_name = ex97 ; es_pars = 0.0 ; --
                        = 0.,0.,0.; --
             xyz1
                        = 1.,0.,0. ; --
             xyz2
                        = 1.,1.,0. ; --
             xyz3
             xyz4
                        = 0.,1.,0. ; --
             nodes_1
                        = 3 ; --
                        = 3 ; --
             nodes_2
             edge_weights = 1.,1.,1.,1.; --
                        = 0 ; -- . suppress nodes and element output
             online
             bc_procedure = ' ' ; -- . Boundary condition procedure
             drilling_dof = <true> ; --
             auto_dof_sup = <true> ; --
             section_prc = ' '; -- . Shell section property procedure
             The following values used only if section_prc not specified
                                 . Shell section property ID
                 nsect = 1 ; --
                                   . Young's Modulus
                 E = 30.E6; --
                                   . Poisons ratio
                 NU = .3 ; --
                                   . Weight Density
                 WTDEN = .1 ; --
                                    . Shell thickness
                 thickness = .1 --
            )
   Model Definition Procedure for GENeric Plate in cartesian coordinates
    A general purpose clip procedure to create the finite element
          mesh for a plate with arbitraty straight sides using 4 or
          9 noded quadrilateral elements.
         If a procedure to generate shell section properties is not provided,
          the isotropic section described by E, NU, WTDEN, and THICKNESS will
```

```
be automatically generated. (see [section_prc] parameter)
       A boundary condition procedure should be provided but is
       optional. If not provided, no boundary conditions will be
       defined. (see [bc_procedure] parameter)
*remark GEN_PLATE MODEL GENERATION PROCEDURE
*def/i n1 = [nodes_1]
   *def/i n2 = [nodes_2]
   *def/e xyz1[1:3] = [xyz1]
   *def/e xyz2[1:3] = [xyz2]
   *def/e xyz3[1:3] = [xyz3]
   *def/e xyz4[1:3] = [xyz4]
   *def/e w[1:4] = [edge_weights]
   *def/e rc[1:4] = <xyz1[1]>,<xyz2[1]>,<xyz3[1]>,<xyz4[1]>
   *def/e tc[1:4] = <xyz1[2]>,<xyz2[2]>,<xyz3[2]>,<xyz4[2]>
   *def/e zc[1:4] = <xyz1[3]>,<xyz2[3]>,<xyz3[3]>,<xyz4[3]>
       ______
       Register Element and Define Macros: ES_NEN, ES_NIP, ES_NSTR, etc.
       *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
                                ; es_pars = [es_pars] )
            es_name = [es_name]
       _______________________
      Define nodal coordinates and element connectivities into
       separate formatted files. These files are gauranteed to have
       unique names that are not currently in use in the current
       directory.
       *def/i chk_closure = 0
    [xqt mesh
    *if <mesh_err> /then
      *remark Error occurred during MESH processor execution.
      *remark GEN_PLATE procedure terminated.
      *eof
    *endif
       _________
       Construct Model Data-base with TESTBED Processors
       [XQT TAB
   START <tot_nodes>
   ONLINE = [online]
   JLOC
    *show macros node_file
    *add <node_file>
```

```
Define Load/Boundary Conditions If Procedure Supplied
  *if <not(<ifelse([bc_procedure]; ;1;0)>)> /then
 *call [BC_PROCEDURE] ( nodes_1 = <n1> ; --
                 nodes_2 = \langle n2 \rangle; ---
                 es_nodes = <es_nen> ; --
                 drilling_dof = [drilling_dof] )
*else
  *remark BOUNDARY CONDITIONS NOT SPECIFIED
  *endif
  Define Shell Section Properties
  _____
*if <not(<ifelse([section_prc]; ;1;0)>)> /then
  *call [section_prc] ( nsect = [nsect] )
*else
  Define the default Material and Section Properties
  *def/e G = < [E]/(2.*(1+[NU])) >
  [XQT AUS
  Build Table of Material Data
  TABLE(ni=16,nj=1): OMB DATA 1 1
  i = 1,2,3,4,5,6,7,8,9
  j = 1
  E11 NU12 E22 G12 G13 G23 ALPHA1 ALPHA2 WTDEN
   [E] [NU] [E] <G> <G> <G> 0. 0. [WTDEN]
  Build Laminate Data Tables
  TABLE(ni=3,nj=1,itype=0): LAM OMB [nsect] 1
   i = 1,2,3
                  layer thickness matl angle
   j = 1 . matl #
                     [thickness]
                                    Ο.
              1
  EXOT LAU
  ONLINE = 2
*endif
   -----
   Generate Elements
```

#### **Pre-Processing Procedures**

\*end

#### 2.4.9 REFERENCES

- 2.4-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 2.4-2 Cook, William A.: "Body Oriented (Natural) Coordinates For Generating Three-Dimensional Meshes." International Journal For Numerical Methods in Engineering, 1974, Volume 8, pp. 27-43.
- 2.4-3 Forrest, A. R.: On Coons and Other Methods for the Representation of Curved Surfaces. Computer Graphics and Image Processing, 1972, Volume 1, pp. 341-359.

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# 2.5 Procedure GEN\_SHELL

# 2.5.1 GENERAL DESCRIPTION

Procedure GEN\_SHELL is used to generate a class of curved shell finite element models. All surfaces are modeled as bi-linearly interpolated surfaces (*i.e.*, Coon's surfaces) in cylindrical coordinate space (see refs. 2.5-2 and 2.5-3). Interpolation in cylindrical coordinates is especially well suited for generating shells of revolution, such as cylinders, cones, annular plates, and spiraling surfaces.

## 2.5.2 PROCEDURE USAGE

Procedure GEN\_SHELL may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

#### \*call GEN\_SHELL ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) preceded by a space may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN\_SHELL are summarized in the following table, along with their default values (if they exist). Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
ES_PROC	ES1	Generic element processor
ES_NAME	EX97	Generic element, name
ES_PARS	0.0	Element research parameters
RTZ1	1,0,0	Cylindrical coordinates of point 1.
RTZ2	1,0,1	Cylindrical coordinates of point 2.
RTZ3	1,90,1	Cylindrical coordinates of point 3.
RTZ4	1,90,0	Cylindrical coordinates of point 4.
NODES_1	7	Number of nodes along edge 1
NODES_2	7	Number of nodes along edge 2
		including duplicate nodes if shell closes
EDGE_WEIGHTS	1,1,1,1	Shell section property procedure
JREF	> >	Joint dof reference frame
BC_PROCEDURE	<b>)</b> )	Boundary condition procedure
DRILLING_DOF	<false></false>	Drilling dof suppression flag
AUTO_DOF_SUP	<false></false>	Automatic dof suppression flag
SECTION_PRC	, ,	Shell section property procedure
NSECT	1	Shell section property number
The following va	lues not used if SE	CTION_PRC is specified.
E	30.E6	Young's Modulus
NU	0.3	Poisson's ratio
WTDEN	0.1	Weight Density
THICKNESS	.1	Shell thickness

## 2.5.3 ARGUMENT DESCRIPTIONS

## 2.5.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <false>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffness (see argument DRILLING\_DOF).

## 2.5.3.2 BC\_PROCEDURE

Name of user provided boundary condition procedure (default: ' '). The term "boundary conditions" refers both to displacement constraints and applied loading. If a boundary condition procedure is provided, the following call will be performed. The macrosymbol  $\langle es\_nen \rangle$  equals the number of element nodes, while the macrosymbols  $\langle n1 \rangle$  and  $\langle n2 \rangle$  equal the number of nodes actually generated along edges one and two.

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**Pre-Processing Procedures** 

# drilling\_dof = [drilling\_dof] )

No action is taken if a boundary condition procedure name is not provided.

### 2.5.3.3 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag set to <false> forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active — unless they are automatically suppressed by use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

# 2.5.3.4 <u>E</u>

Young's modulus (default: 30.E6). This argument is ignored if SECTION\_PRC parameter is specified. See the description for SECTION\_PRC for more detail.

## 2.5.3.5 EDGE\_WEIGHTS

Node placement can be weighted along each surface edge according to the EDGE\_WEIGHTS parameter. The input format requires a list of four edge-node placement weightings representing the node weighting for edge1, edge2, edge3, and edge4 (default: 1.,1.,1.,1.).

The weighting value for a given edge represents the length of the last element divided by the length of the first element along that edge. The edge orientation arrows in figure 2.5-1 point from the first element to the last element along each edge. In the case of 9-node quad elements, the midside and center nodes are positioned at the appropriate locations based on the elements natural coordinate system.

The procedure interprets negative weight values to mean the positive reciprocal. For example, a value of -5.0 is identical to a value of 0.2.

## 2.5.3.6 ES\_NAME

Element name (default: EX97). This argument is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-node quadrilateral element implemented in processor ES1, and described reference 2.5-1.

# 2.5.3.7 ES\_PARS

Element research parameters (default: 0., ...). This argument is an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

# 2.5.3.8 ES\_PROC

Element processor (default: ES1) This argument is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

## 2.5.3.9 JREF

Joint degree of freedom (dof) reference frame (default: -1 for global cylindrical). The user may provide any alternate frame which has been created prior to calling this procedure. A negative value causes the frame to be interpreted as a cylindrical reference frame.

# 2.5.3.10 NODES\_1

Number of nodes on edge 1 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 3. This number should be consistent with the element type selected. For example, NODES\_1 can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

# 2.5.3.11 <u>NODES\_2</u>

Number of nodes on edge 2 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 4. This number should be consistent with the element type selected. For example, NODES\_2 can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 2.5.3.12 NSECT

Shell section property number (default: 1). The NSECT value is required when defining the element using the processor ELD. See the description of SECTION\_PRC for more detail.

# 2.5.3.13 <u>NU</u>

Poisson's ratio (default: 0.3). This argument is ignored if the SECTION\_PRC input parameter is specified. See the description of SECTION\_PRC for more detail.

# 2.5.3.14 RTZ1

The cylindrical coordinates  $(r, \theta, z)$  which define corner number 1 of the model surface ( $\theta$  in degrees). The form of the input is three real values, each separated by a comma (default: 1.,0.,0.). The surface is defined by four edges which are defined as a linear interpolation in cylindrical coordinates of four endpoints, or "corner" points.

#### 2.5.3.15 RTZ2

The cylindrical coordinates  $(r, \theta, z)$  defining the corner number 2 of the model surface (default: 1.,0.,1.).

#### 2.5.3.16 RTZ3

The cylindrical coordinates  $(r, \theta, z)$  defining the corner number 3 of the model surface (default: 1.,90.,1.).

#### 2.5.3.17 RTZ4

The cylindrical coordinates  $(r, \theta, z)$  defining the corner number 4 of the model surface (default: 1.,90.,0.).

#### 2.5.3.18 SECTION\_PRC

Name of a user supplied procedure to define the plate section properties (default = ' '). If a section properties procedure is provided, the following call will be performed.

\*call [section\_prc] ( nsect = [nsect] )

The effect of the default is to allow the procedure to generate an isotropic material section based on the input parameters E, NU, WTDEN, and THICKNESS. The section number is defined by the input parameter NSECT. If the call parameter SECTION\_PRC is defined by the user, then call parameters E, NU, WTDEN, and THICKNESS are ignored by procedure GEN\_SHELL.

#### 2.5.3.19 THICKNESS

Thickness of the shell wall (default = 1.0). This argument is ignored if SECTION\_PRC parameter is specified. See the description for SECTION\_PRC for more detail.

#### 2.5.3.20 WTDEN

Weight density expressed in lb/in.<sup>3</sup> (default: 0.1 lb/in.<sup>3</sup>). This argument is ignored if the SECTION\_PRC input parameter is specified. Processor LAU will convert the weight density to mass density using the gravitational acceleration constant 386.4 in/sec<sup>2</sup>.

## 2.5.4 USAGE GUIDELINES AND EXAMPLES

Procedure GEN\_SHELL may be invoked using the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values in the procedure call. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

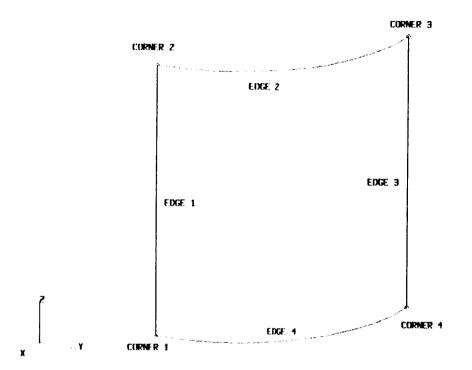
Revised 12/18/91

```
= 1.,90.,1.; --
RTZ3
                = 1.,90.,0.; --
RTZ4
                = 7 ; --
NODES 1
                = 7 ; --
NODES_2
                 = 1., 1., 1., 1.; --
EDGE_WEIGHTS
BC_PROCEDURE = ' '; -- . Boundary condition procedure
DRILLING_DOF = <true> ; --
AUTO_DOF_SUP = <true> ; --
SECTION_PRC = ' '; -- . Shell section property procedure
                            . Shell section property ID
NSECT = 1 ; --
   The following values not used if SECTION_PRC specified
      E = 30.E6; -- . Young's Modulus
NU = .3; -- . Poissons ratio
      NU = .3 ; -- . Poissons ratio
THICKNESS = .1 -- . Shell thickness
)
```

## 2.5.4.1 Mesh Generation

The method of surface generation used by procedure GEN\_SHELL is described in the section. Termology depicted on figure 2.5-1 provides a visual interpretation of the parameters used to generate a curved surface.

To the define the shell surface, the user definess four coordinate positions in a cylindrical reference frame. These four positions represent four corners of a four sided region. The sides of the region (which will also be referred to as edges) are defined by linearly interpolating between the coordinate values of the corner points. The surface of the region is defined as a bi-linear interpolation of the four sides, also known as a Coon's surface (see refs. 2.5-2 and 2.5-3). It must be remembered that since interpolations are performed in cylindrical coordinates, the surface and its edges will not generally be flat or straight, but rather curved.



# Figure 2.5-1 Generic Shell Surface Topology.

The connectivity of the surface is defined in figure 2.5-1. The user provides the coordinates for corners 1 to 4. Edge 1 of the region starts at corner 1 and ends at corner 2. The remaining edges are defined in a similar manner. The arrows indicate the orientation of the edges and the direction of increasing node numbers.

The topology of the resulting finite element grid is depicted in Figure 2.5-2. Nodes are created first along edge 1, then in successive lines terminating along edge 3. The user defines the number of nodes along edges 1 and 2, which also defines the number of nodes for edges 3 and 4. The relative position of the nodes along each edge may be controlled using the edge weighting parameter EDGE\_WEIGHTS.

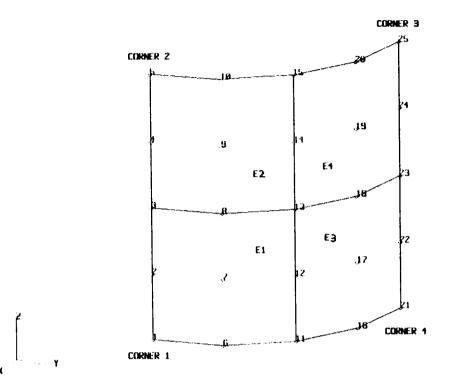


Figure 2.5-2 Node and Element Topology.

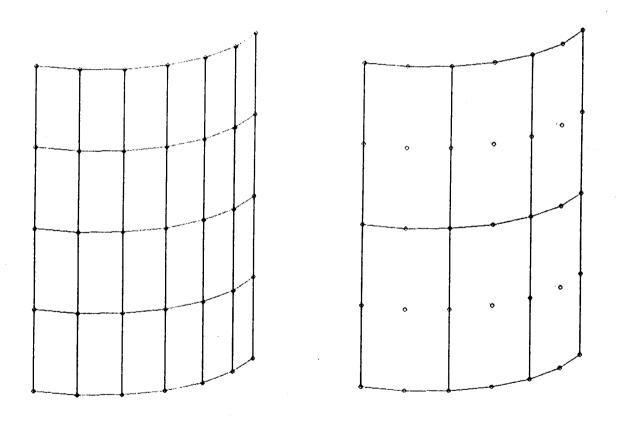
Recognizing that the surfaces generated by procedure GEN\_SHELL are four sided surfaces in cylindrical coordinates, it will be shown, by example, how to generate segments of cylinders, cones, annular plates, spirals, and more general surfaces. For applications which require a complete axisymmetric surface, such as a 360 degree cylinder, the procedure has the capability of joining the resulting finite element mesh where two sides of the region are coincident. Closure occurs automatically but is checked only along edges 1 and 3. Closure will not occur between edges 2 and 4. Note also that the user must request the number of nodes along edge 2 as though the surface were not closed. This requirement is to say that the user should not presume closure will occur.

# 2.5.4.2 Cylindrical Shell Sections

In this section there are presented examples of how procedure GEN\_SHELL may be used to create various shell segments on a right circular cylindrical surface.

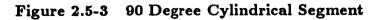
In the following example, procedure GEN\_SHELL is used to generate a cylindrical segment with radius of 5 inches and length of 10 inches. Only 90 degrees of the cylinder is generated (see figure 2.5-3).

```
*call GEN_SHELL ( es_proc = 'ES1'; es_name = 'EX47'; --
    rtz1 = 5.,0.,0.; --
    rtz2 = 5.,0.,10.; --
    rtz3 = 5.,90.,10.; --
    rtz4 = 5.,90.,0.; --
    nodes_1 = 5; --
    nodes_2 = 7 )
```



(a) 4-node elements

(b) 9-node elements



This example creates a complete 360 degree cylindrical shell using 9-node quadrilateral elements (see figure 2.5-4). Note that midside nodes are not shown. The input specifies elements at the end of edges 1 and 3 to be 5 times longer that elements at the beginning of the same edges. Closure of the cylinder is obtained by defining corner points 1 and 4, and corner points 2 and 3, to be coincident in the r and z directions, with a difference in  $\theta$  of 360 degrees.

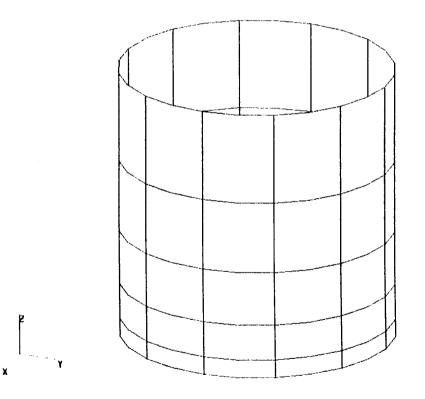


Figure 2.5-4 Right Circular Cylinder - 9-node Elements

By simply increasing the z coordinate values for corner points 3 and 4, the cylinder wall can be made to spiral about the z axis. The following example illustrates this technique. The resulting spiral is shown in figure 2.5-5. This configuration may be used to model a spring.

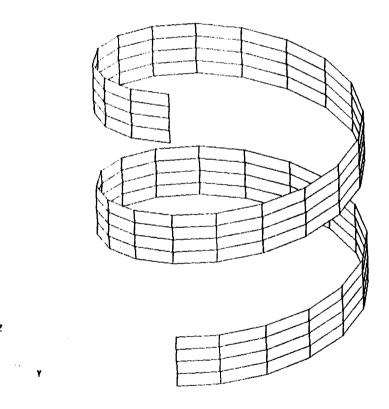


Figure 2.5-5 Spiraling Cylinder Wall

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The following example produced the cylinder of skewed elements shown in figure 2.5-6.

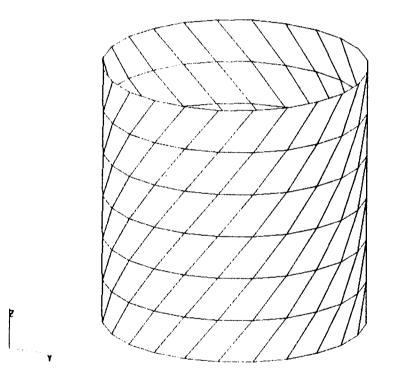


Figure 2.5-6 Cylinder With Skewed Elements

X

# 2.5.4.3 Conical Shell Sections

In this section, examples of how procedure GEN\_SHELL may be used to create shell segments on a conical surface are presented.

This example creates a complete 360 degree conical shell using 9-node quadrilateral elements (see figure 2.5-7). Elements are defined at the top of the cones to be 1/5 as long axially as those at the base. Closure of the cone is obtained by defining corner points 1 and 4, and corner points 2 and 3, to be coincident in r and z directions, with a difference in  $\theta$  of 360 degrees.

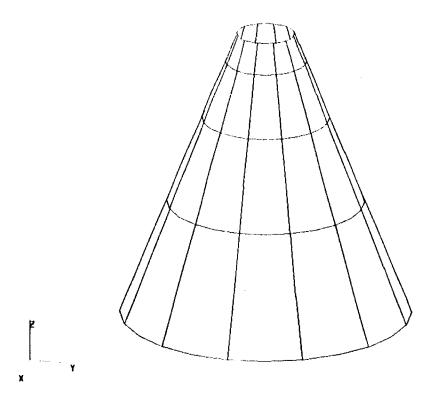


Figure 2.5-7 Conical Shell - 9-Node Elements

In the following example, procedure GEN\_SHELL is used to generate an unusual shell which lies on the conical surface of the previous example. The shell spans 360 degrees at the top but only spans 180 degrees at the base (see figure 2.5-8).

*call GEN_SHELL ( es_p	<pre>proc = 'ES1' ; es_name = 'EX47' ;</pre>
rtz1	= 5.,90.,0. ;
rtz2	= 1.,0.,10. ;
rtz3	= 1.,360.,10. ;
rtz4	= 5.,270.,0. ;
nodes_1	= 11 ;
nodes_2	= 21 ;
edge_weights	= -3.,1.,-3.,1. )

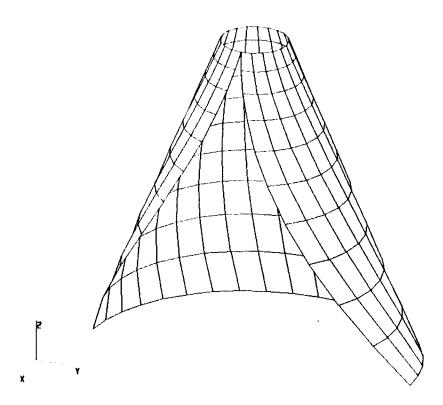


Figure 2.5-8 Unusual Conical Shell

# 2.5.4.4 Annular Plates

In this section examples of how procedure GEN\_SHELL may be used to create annular shell segments are presented.

This example creates a 90 degree annular shell segment using 9-node quadrilateral elements (see figure 2.5-9). Note that the midside nodes are not shown. The plate has an inner radius of 1 inch and the outer radius of 5 inches. Element size weighting is also demonstrated.

```
*call GEN_SHELL ( es_proc = 'ES1'; es_name = 'EX97'; --
    rtz1 = 1.,0.,0.; --
    rtz2 = 5.,0.,0.; --
    rtz3 = 5.,90.,0.; --
    rtz4 = 1.,90.,0.; --
    nodes_1 = 11; --
    nodes_2 = 11; --
    edge_weights = 6.,1.,6.,1. )
```

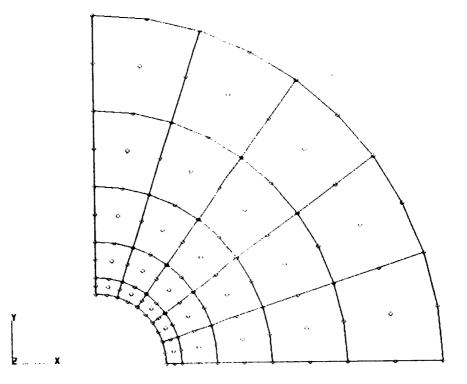


Figure 2.5-9 Flat Annular Shell

By simply increasing the z coordinate values for corner points 3 and 4, the annular surface can be made to spiral about the z axis. The following example illustrates this technique. The resulting spiral is shown in figure 2.5-10.

*call GEN_SHELL (	<pre>es_proc = 'ES1' ; es_name = 'EX47' ;</pre>
rtz1	= 3.,0.,0. ;
rtz2	= 5.,0.,0. ;
rtz3	= 5.,720.,10. ;
rtz4	= 3.,720.,10. ;
nodes_1	= 5 ;
nodes_2	= 33)

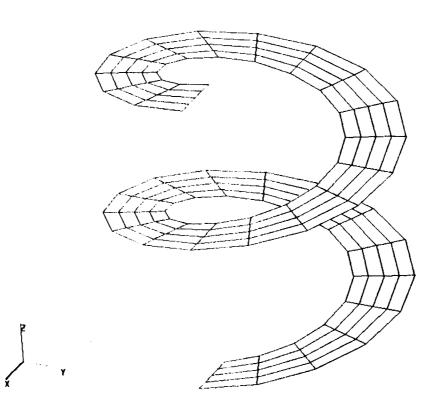


Figure 2.5-10 Spiraling Shell

# 2.5.4.5 Exotic Shell Sections

In this section examples of how procedure GEN\_SHELL may be used to create unusual shell segments are presented.

This example creates a spiraling surface which changes from a flat to a vertical shell while increasing in z direction and decreasing in radius (see figure 2.5-11).

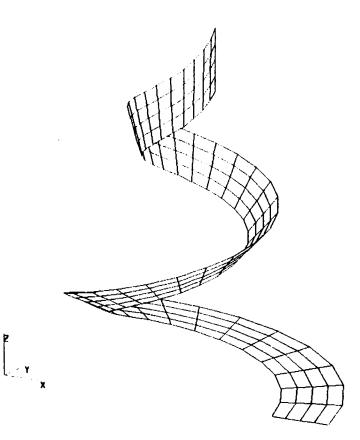


Figure 2.5-11 Exotic Spiral Shell

In the following example, procedure GEN\_SHELL is used to generate a vertical coiled shell (see figure 2.5-12).

```
*call GEN_SHELL ( es_proc = 'ES1'; es_name = 'EX47'; --
    rtz1 = 0.,0.,0.; --
    rtz2 = 0.,0.,1.; --
    rtz3 = 3.,1080.,1.; --
    rtz4 = 3.,1080.,0.; --
    nodes_1 = 5; --
    nodes_2 = 85 )
```

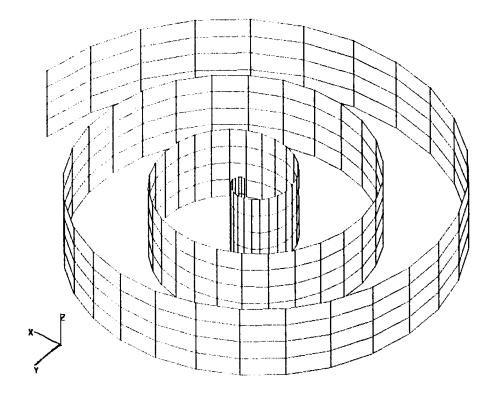


Figure 2.5-12 Vertical Coiled Shell

This example uses procedure GEN\_SHELL to generate a flat coiled shell (see figure 2.5-13).

```
*call GEN_SHELL ( es_proc = 'ES1'; es_name = 'EX47'; --
    rtz1 = 0.,0.,0.; --
    rtz2 = 1.,0.,0.; --
    rtz3 = 9.,720.,0.; --
    rtz4 = 5.5,720.,0.; --
    nodes_1 = 5; --
    nodes_2 = 51 )
```

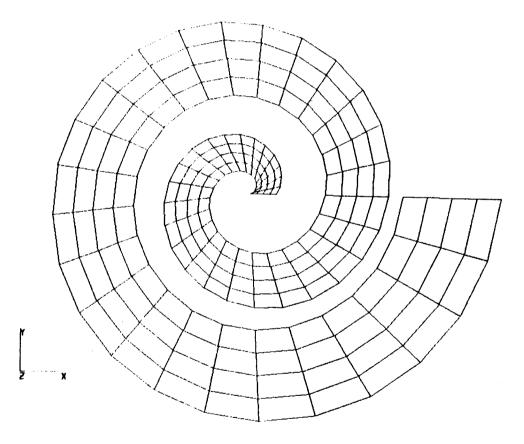


Figure 2.5-13 Flat Coiled Shell

Finally, an arbitrary shell is created to demonstrate the generality of the procedure GEN\_SHELL (see figure 2.5-14).

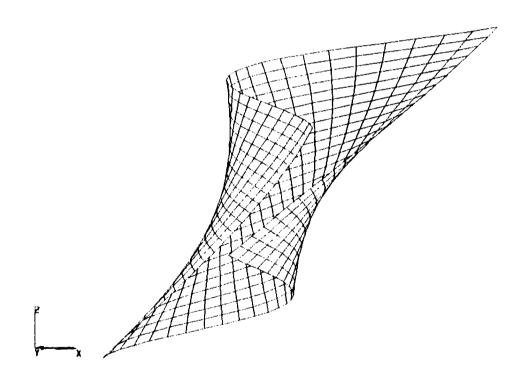


Figure 2.5-14 Arbitrary Shell

## 2.5.5 LIMITATIONS

As previously stated, to obtain closed axisymmetric surface models, the user must define edges 1 and 3 to be the coincident edges.

## 2.5.6 ERROR MESSAGES AND WARNINGS

None.

## 2.5.7 PROCEDURE FLOWCHART

GEN_SHELL	(Shell generation procedure)
[BC_PROCEDURE]	(user supplied boundary conditions/loads procedure)
[SECTION_PRC]	(user supplied section property generation procedure)
CYL_NODES	(surface node generation procedure)
CYL_ELT_CONN	(element connectivity definition procedure)

## 2.5.8 PROCEDURE LISTING

```
*procedure GEN_SHELL ( es_proc = es1 ; es_name = ex97 ; es_pars = 0. ; --
                 = 1.,0.,0. ; --
= 1.,0.,1. ; --
            rtzi
            rtz2
            rtz3
                       = 1.,90.,1. ; --
                       = 1.,90.,0.; --
            rtz4
            nodes_1
                      = 7 ; ---
            nodes_2
                       = 7 ; --
            edge_weights = 1.,1.,1.,1.; --
            jref
                       = -1 ; -- . Joint dof reference frame
            bc_procedure = ' '; -- . Boundary condition procedure
            online
                       = 0 ; -- . supress nodes/elts output
            drilling_dof = <true> ; --
            auto_dof_sup = <true> ; --
            section_prc = ' '; -- . Shell section property procedure
          The following values used only if section_prc not specified
                nsect = 1 ; -- . Shell section property ID
                E = 30.E6; --
                                . Young's Modulus
                NU = .3 ; --
                                . Poisons ratio
                                 . Weight Density
                WTDEN = .1 ; --
                                 . Shell thickness
                thickness = .1 --
            )
   Model Definition Procedure for GENeric Shell in cylindrical coordinates
   A general purpose clip procedure to create the finite element
```

```
mesh for a partial or complete cylindrical shell using 4 or
        9 noded quadrilateral elements.
       Note that when generating a 360 degree closed shell,
        the caller should specify the number of circumferential nodes as
        if the cylindrical shell were not closed, or in other words,
        the line of nodes where closure occurs should be counted twice.
        There will only be one set of nodes actually create where
        closure occurs.
       There is no verification performed to detect overlapping or
        otherwise improbable element generation. This should be done
        prior to calling this utility.
       If a procedure to generate shell section properties is not provided,
        the isotropic section described by E, NU, WTDEN, and THICKNESS will
        be automatically generated. (see [section_prc] parameter)
       A boundary condition procedure should be provided but is
        optional. If not provided, no boundary conditions will be
        defined. (see [bc_procedure] parameter)
*remark GEN_SHELL MODEL GENERATION PROCEDURE
*def/i n1 = [nodes_1]
    *def/i n2 = [nodes_2]
    *def/e rtz1[1:3] = [rtz1]
    *def/e rtz2[1:3] = [rtz2]
    *def/e rtz3[1:3] = [rtz3]
    *def/e rtz4[1:3] = [rtz4]
    *def/e w[1:4] = [edge_weights]
    *def/e rc[1:4] = <rtz1[1]>,<rtz2[1]>,<rtz3[1]>,<rtz4[1]>
    #def/e tc[1:4] = <rtz1[2]>,<rtz2[2]>,<rtz3[2]>,<rtz4[2]>
    *def/e zc[1:4] = <rtz1[3]>,<rtz2[3]>,<rtz3[3]>,<rtz4[3]>
       Register Element and Define Macros: ES_NEN, ES_NIP, ES_NSTR, etc.
       *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
                                   ; es_pars = [es_pars] )
             es_name = [es_name]
       Define nodal coordinates and element connectivities into
        separate formatted files. These files are gauranteed to have
        unique names that are not currently in use in the current
        directory.
       *def/i chk_closure = 1
    [xqt mesh
    *if <mesh_err> /then
```

```
*remark Error occurred during MESH processor execution.
     *remark GEN_SHELL procedure terminated.
     *eof
   *endif
      .
      Construct Model Data-base with TESTBED Processors
      [XQT TAB
   START <tot_nodes>
   ONLINE = [online]
   JLOC
                      . use cylindrical coordinate system
   FORMAT = 2
   *show macros node_file
   *add <node_file>
    _____
    Define DOF Directions
    Use local cylindrical basis vectors
      JREF
                       .
                         for nodal DOFS:
                         u,v,w = radial, circumfer., axial
      NREF = [jref]
                         same convention for all nodes
      1 <tot_nodes>
      Define Load/Boundary Conditions If Procedure Supplied
      *if <not(<ifelse([bc_procedure]; ;1;0)>)> /then
     *call [BC_PROCEDURE] ( nodes_1 = <n1> ; --
                    nodes_2 = \langle n2 \rangle; --
                    es_nodes = <es_nen> ; --
                    drilling_dof = [drilling_dof] )
    *else
      *remark BOUNDARY CONDITIONS NOT SPECIFIED
      *endif
      Define Shell Section Properties
      *if <not(<ifelse([section_prc]; ;1;0)>)> /then
      *call [section_prc] ( nsect = [nsect] )
    *else
      Define the default Material and Section Properties
```

```
*def/e G = < [E]/(2.*(1+[NU])) >
        EXQT AUS
       Build Table of Material Data
        TABLE(ni=16,nj=1): OMB DATA 1 1
        i = 1,2,3,4,5,6,7,8,9
        j = 1
        E11 NU12 E22 G12 G13 G23 ALPHA1 ALPHA2 WTDEN
                                 0.
                                       O. [WTDEN]
        [E] [NU] [E] <G> <G> <G>
        Build Laminate Data Tables
        TABLE(ni=3,nj=1,itype=0): LAM OMB [nsect] 1
        i = 1, 2, 3
        j = 1 . matl #
                           layer thickness matl angle
                                                 Ο.
                              [thickness]
                       1
       EXOT LAU
       ONLINE = 2
    *endif
        Generate Elements
        ___________
     [XQT ELD
     <ES_EXPE_CMD>
    NSECT = [nsect]
       Define element nodal connectivity
*show macros elem_file
     *add <elem_file>
       Suppress DOFs not supported by elements
       *if < [AUTO_DOF_SUP] > /then
       *call ES ( function = 'DEFINE FREEDOMS' )
     *endif
*end
```

#### 2.5.9 REFERENCES

- 2.5-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 2.5-2 Cook, William A.: "Body Oriented (Natural) Coordinates For Generating Three-Dimensional Meshes." International Journal For Numerical Methods in Engineering, 1974, Volume 8, pp. 27-43.
- 2.5-3 Forrest, A. R.: On Coons and Other Methods for the Representation of Curved Surfaces. Computer Graphics and Image Processing, 1972, Volume 1, pp. 341-359.

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# 3.0 Solution Procedures

The procedures documented in this chapter are for specific analysis tasks. These procedures provide examples of how to perform common structural analysis tasks (e.g., static solution, eigensolution) using the command language and processors available in the CSM Testbed Software System.

A summary of the procedures found in this chapter is provided in Table 3.0-1.

	Table 3.0-1         Solution Procedures	
Procedure Name	Analysis Description	
L_DYNAMIC_O	Linear transient dynamic analysis using modal anal- ysis	
L_DYNAMIC_1	Linear transient dynamic analysis using Newmark al- gorithm	
L_STABIL_1	Linear stability (buckling eigenvalue) analysis with prescribed prestress	
L_STABIL_2	Linear stability (buckling eigenvalue) analysis with linearly-computed prestress	
L_STATIC	Linear static analysis	
L_VIBRAT_0	Linear vibration (eigenvalue) analysis about un- stressed state	
L_VIBRAT_1	Linear vibration (eigenvalue) analysis about a pre- scribed prestressed state	
L_VIBRAT_2	Linear vibration (eigenvalue) analysis about a linearly- computed prestressed state	
NL_STATIC_1	Nonlinear static analysis; modified Newton iteration with arc-length control	
NL_STATIC_2	Advanced Riks method	
NL_DYNAMIC_1	Nonlinear Dynamic Analysis	

3.0 - 1

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# 3.1 Processor L\_DYNAMIC\_0

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# 3.2 Procedure L\_DYNAMIC\_1

### **3.2.1 GENERAL DESCRIPTION**

Procedure L\_DYNAMIC\_1 performs a linear transient dynamic analysis using either the Newmark- $\beta$  implicit direct time integration procedure outlined in reference 3.2-1. When Procedure L\_DYNAMIC\_1 is called, a transient response calculation by direct integration of the system equations with a fixed time step is performed. Procedure L\_DYNAMIC calls Procedure NEWMARK which implements the well-known Newmark integration method for second order, coupled systems. Parameters such as the names of the system stiffness and mass matrices, the time step, and the total number of time steps in the analysis are formal arguments to Procedure L\_DYNAMIC\_1. In Procedure NEWMARK, extensive use is made of the CLAMP macro expression capability for calculating integration constants and controlling the algorithm. The initial acceleration at time t = 0 is calculated from the given initial displacement and velocity vectors. This is done by using processor AUS to set up the equations of motion at t=0, and processors INV and SSOL to solve for the acceleration. At each subsequent time step, processor AUS is used to set up the recursion relations, and processor SSOL is used to solve for the displacement vector at the next time step. Then velocity and acceleration vectors are calculated and selectively printed.

#### 3.2.2 THEORY

#### 3.2.2.1 Introduction

The equations of motion for an undamped, linear elastic structure at time  $t + \Delta t$  are

$$\mathbf{M}\ddot{\mathbf{u}}_{t+\Delta t} + \mathbf{K}\mathbf{u}_{t+\Delta t} = \mathbf{P}_{t+\Delta t}$$
(3.2-1)

where

M is the mass matrix

K is the linear elastic stiffness matrix

 $\mathbf{P}_{t+\Delta t}$  is the load vector at time  $t + \Delta t$ 

 $\mathbf{u}_{t+\Delta t}$  is the displacement vector at time  $t + \Delta t$ 

 $\ddot{\mathbf{u}}_{t+\Delta t}$  is the acceleration vector at time  $t + \Delta t$ 

#### 3.2.2.2 Newmark-*β* Method

The Newmark- $\beta$  method is an implicit direct time integration procedure that is based on the following assumptions:

$$\dot{\mathbf{u}}_{t+\Delta t} = \dot{\mathbf{u}}_t + \left[ (1-\gamma) \ddot{\mathbf{u}}_t + \gamma \ddot{\mathbf{u}}_{t+\Delta t} \right] \Delta t \qquad (3.2-2)$$

$$\mathbf{u}_{t+\Delta t} = \mathbf{u}_t + \Delta t \dot{\mathbf{u}}_t + \left[ \left( \frac{1}{2} - \beta \right) \ddot{\mathbf{u}}_t + \beta \ddot{\mathbf{u}}_{t+\Delta t} \right] (\Delta t)^2 \qquad (3.2-3)$$

where

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 $\dot{\mathbf{u}}_{t+\Delta t}$  is the velocity vector at time  $t + \Delta t$  $\Delta t$  is time step size

The parameters  $\gamma$  and  $\beta$  determine integration accuracy and stability. When  $\gamma = \frac{1}{2}$  and  $\beta = \frac{1}{6}$ , the linear acceleration method is obtained (*i.e.*, the acceleration is assumed to vary linearly over a time step). When  $\gamma = \frac{1}{2}$  and  $\beta = \frac{1}{4}$ , Newmark's original, constant-average-acceleration method (also called the trapezoidal rule) is obtained.

#### 3.2.3 ALGORITHM

The Procedure L\_DYNAMIC\_1 closely follows the computational procedure presented in reference 3.2-1. Briefly, an outline of the procedure is as follows:

1. Select time step size,  $\Delta t$ , and parameters  $\gamma$  and  $\beta$ . Calculate integration constants:

$$\begin{split} \gamma \geq \frac{1}{2} ; \quad \beta \geq \frac{1}{4} \left(\frac{1}{2} + \gamma\right)^2 ; \\ a_o &= \frac{1}{\beta(\Delta t)^2}; \qquad a_1 = \frac{\gamma}{\beta \Delta t}; \qquad a_2 = \frac{1}{\beta(\Delta t)}; \\ a_3 &= \frac{1}{2\beta} - 1; \qquad a_4 = \frac{\gamma}{\beta} - 1; \qquad a_5 = \frac{\Delta t}{2} \left(\frac{\gamma}{\beta} - 2\right); \\ a_6 &= \Delta t (1 - \gamma); \qquad a_7 = \gamma \Delta t \end{split}$$

- 2. Initialize displacements  $u_o$ , velocities  $\dot{u}_o$ , and accelerations  $\ddot{u}_o$ .
- 3. Form effective stiffness matrix  $\hat{\mathbf{K}}$

$$\hat{\mathbf{K}} = \mathbf{K} + a_o \mathbf{M}$$

4. Decompose **K** 

$$\hat{\mathbf{K}} = \mathbf{L}\mathbf{D}\mathbf{L}^{T}$$

For each time step:

5. Calculate effective loads  $\mathbf{\hat{R}}_{t+\Delta t}$ 

$$\ddot{\mathbf{R}}_{t+\Delta t} = \mathbf{P}_{t+\Delta t} + \mathbf{M}(a_o \mathbf{u}_t + a_2 \dot{\mathbf{u}}_t + a_3 \ddot{\mathbf{u}}_t)$$

6. Solve for displacements at time  $t + \Delta t$ 

$$\mathbf{L}\mathbf{D}\mathbf{L}^T\mathbf{u}_{t+\Delta t} = \hat{\mathbf{R}}_{t+\Delta t}$$

7. Calculate accelerations and velocities at time  $t + \Delta t$ 

$$\ddot{\mathbf{u}}_{t+\Delta t} = a_o(\mathbf{u}_{t+\Delta t} - \mathbf{u}_t) - a_2\dot{\mathbf{u}}_t - a_3\ddot{\mathbf{u}}_t$$
$$\dot{\mathbf{u}}_{t+\Delta t} = \dot{\mathbf{u}}_t + a_6\ddot{\mathbf{u}}_t + a_7\ddot{\mathbf{u}}_{t+\Delta t}$$

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This procedure neglects damping and assumes that a single, constant time step size  $\Delta t$  is used throughout the analysis.

## **3.2.4 PROCEDURE USAGE**

Procedure L\_DYNAMIC\_1 is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call L_DYNAMIC_1 ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for Procedure L\_DYNAMIC\_1 are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For Procedure L\_DYNAMIC\_1, the following table lists each argument, its default value and meaning.

Argument	Default Value	Meaning
DELT	-	Time increment, $\Delta t$
NSTEP	-	Number of time steps
BETA	0.25	Time integrator parameter
GAMMA	0.50	Time integrator parameter

#### **3.2.5 ARGUMENT DESCRIPTION**

#### 3.2.5.1 BETA

in the Bas

Newmark- $\beta$  time integrator parameter,  $\beta$  (default: 1/4).

#### 3.2.5.2 DELT

Time step size. This argument specifies the size of the time step to be used in the analysis. A constant step size is assumed per procedure call.

#### 3.2.5.3 GAMMA

Newmark- $\beta$  time integrator parameter  $\gamma$  (default: 1/6).

#### 3.2.5.4 <u>NSTEP</u>

Number of time steps to march. This argument specifies the number of time steps to march in the transient response prediction using a constant time step size of DELT.

## 3.2.6 PROCEDURE FLOWCHART

L_DYNAMIC_1	(main procedure)
NEWMARK	(Newmark- $\beta$ time integration)

#### 3.2.7 LIMITATIONS

None.

#### 3.2.8 ERROR MESSAGES AND WARNINGS

None.

# 3.2.9 USAGE GUIDELINES AND EXAMPLES

Procedure L\_DYNAMIC\_1 is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

# 3.2.10 PROCEDURE LISTING

# 3.2.11 REFERENCES

3.2-1 Bathe, K. J., Finite Element Procedures in Engineering Analysis, Prentice-Hall, Inc., Englewood Cliffs, New Jersey, 1982, pp. 511-512.

# 3.3 Procedure L\_STABIL\_1

# **3.3.1 GENERAL DESCRIPTION**

Procedure L\_STABIL\_1 performs linear stability analysis using an eigensolver selected by the global macrosymbol eigensolver\_name (e.g., EIG2, LAN, LANZ) and structural element (ESi) processors based on the generic element processor template. The procedure assumes that the finite element model, loads, and boundary conditions have already been generated, that the prebuckling stress state has been specified, and that the buckling loads and mode shapes need to be calculated. The prebuckling stress state (*i.e.*, prestress state) is specified by prescribing values for procedure L\_STABIL\_1 arguments. A linear stability analysis is performed using this prescribed stress state.

#### 3.3.2 THEORY

Linear elastic stability analyses may be formulated using the concept of adjacent equilibrium. Membrane forces in beams, plates, and shells result in an equilibrium configuration in which the deformation pattern is tangent to the midsurface of the structure. However, another equilibrium configuration involving out-of-plane deflections and rotations may be adjacent to this membrane state. Buckling occurs when this membrane strain energy is converted to bending strain energy. The linear elastic stability analysis is an eigenvalue problem to calculate the critical load for the bifurcation in the solution (e.g., change from a membrane state to a bending state). This eigenvalue problem can be written as

$$\mathbf{K}\boldsymbol{\phi}_i + \lambda_i \mathbf{K}_g(\boldsymbol{\sigma})\boldsymbol{\phi}_i = \mathbf{0} \quad i = 1, 2, \dots \qquad (3.3-1)$$

where

 $\mathbf{K}$  = assembled linear elastic stiffness matrix  $\mathbf{K}_{g}(\sigma)$  = assembled geometric stiffness matrix  $\phi_{i}$  = *i*-th eigenvector or modeshape  $\lambda_{i}$  = *i*-th eigenvalue or buckling load factor

The matrix denoted by  $K_g$  has been called the initial stress stiffness matrix, the differential stiffness matrix, the geometric stiffness matrix, and the stability coefficient matrix (e.g., see ref. 3.3-1). It is independent of the elastic properties of the structure and dependent on the geometry, displacement field, and state of stress. Herein the matrix  $K_g$  will be referred to as the geometric stiffness matrix.

A general formulation for the geometric stiffness matrix is presented in reference 3.3-1. Strains can be written as

$$\boldsymbol{\epsilon} = \boldsymbol{\epsilon}_{\mathbf{L}} + \boldsymbol{\epsilon}_{\mathbf{NL}} \tag{3.3-2}$$

where  $\epsilon_{\mathbf{L}}$  contains the linear strain-displacement terms and  $\epsilon_{\mathbf{NL}}$  contains the higher-order or nonlinear strain-displacement terms. For a given stress state  $\sigma_0$ , elastic strain energy is stored and can be expressed as

where

$$U = U_L + U_{NL} (3.3-3)$$

$$U = \frac{1}{2} \int_{V} \boldsymbol{\epsilon}^{T} \boldsymbol{\sigma}_{0} dV \qquad (3.3 - 4a)$$

$$U_L = \frac{1}{2} \int_V \epsilon_L^T \sigma_0 dV \qquad (3.3-4b)$$

$$U_{NL} = \frac{1}{2} \int_{V} \epsilon_{NL}^{T} \sigma_0 dV \qquad (3.3 - 4c)$$

The geometric stiffness matrix is derived from the strain energy produced by stresses acting through displacements associated with the nonlinear strain-displacement relations. These relations couple the membrane and bending effects. Typically the strain-displacements relations are written using index notation as

$$\epsilon_{ij} = \frac{1}{2} \left[ \partial_i u_j + \partial_j u_i + \partial_i u_k \partial_j u_k \right]$$
(3.3-5)

where  $u_i = (u, v, w)$  for i = 1, 2, 3, respectively,  $\partial_i$  denotes differentiation with respect to *i*th coordinate direction and summation over repeated indices is implied. Let d denote the nodal degrees of freedom, then

$$\boldsymbol{\delta} = \mathbf{G}\mathbf{d} \tag{3.3-6}$$

where

 $\boldsymbol{\delta} = \{\partial_{\boldsymbol{x}}\boldsymbol{u}, \ \partial_{\boldsymbol{y}}\boldsymbol{u}, \ \partial_{\boldsymbol{z}}\boldsymbol{u}, \ \partial_{\boldsymbol{x}}\boldsymbol{v}, \ \partial_{\boldsymbol{y}}\boldsymbol{v}, \ \partial_{\boldsymbol{z}}\boldsymbol{v}, \ \partial_{\boldsymbol{x}}\boldsymbol{w}, \ \partial_{\boldsymbol{y}}\boldsymbol{w}, \ \partial_{\boldsymbol{z}}\boldsymbol{w}\}$ 

The coefficients of G are obtained by differentiating the element shape functions. Finally the matrix Q is defined as

$$\mathbf{Q} = \begin{bmatrix} \partial_x u & 0 & 0 & \partial_x v & 0 & 0 & \partial_x w & 0 & 0 \\ 0 & \partial_y u & 0 & 0 & \partial_y v & 0 & 0 & \partial_y w & 0 \\ 0 & 0 & \partial_z u & 0 & 0 & \partial_z v & 0 & 0 & \partial_z w \\ \partial_y u & \partial_x u & 0 & \partial_y v & \partial_x v & 0 & \partial_y w & \partial_z w & 0 \\ 0 & \partial_z u & \partial_y u & 0 & \partial_z v & \partial_y v & 0 & \partial_z w & \partial_y w \\ \partial_z u & 0 & \partial_x u & \partial_z v & 0 & \partial_x v & \partial_z w & 0 & \partial_z w \end{bmatrix}$$
(3.3-7)

With these definitions the nonlinear strains given by equation (3.3-2) can be written as

$$\boldsymbol{\epsilon}_{\mathbf{NL}} = \frac{1}{2} \mathbf{QGd} \tag{3.3-8}$$

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The vector of initial stresses is

$$\sigma_0 = \{ \sigma_{x0} \ \sigma_{y0} \ \sigma_{z0} \ \tau_{xy0} \ \tau_{yz0} \ \tau_{xz0} \}$$
(3.3-9)

Substituting equations (3.3-6) through (3.3-9) into equation (3.3-4c) gives

$$U_{NL} = \frac{1}{2} \mathbf{d}^T \left( \int_V \mathbf{G}^T \mathbf{Q}^T \boldsymbol{\sigma_0} \ dV \right)$$
(3.3 - 10)

However, the term  $\mathbf{Q}^T \sigma_0$  can be written as

$$\mathbf{Q}^{T}\boldsymbol{\sigma}_{\mathbf{0}} = \begin{bmatrix} \mathbf{s} & 0 & 0 \\ 0 & \mathbf{s} & 0 \\ 0 & 0 & \mathbf{s} \end{bmatrix} \boldsymbol{\delta} = \overline{\mathbf{S}}(\boldsymbol{\sigma}_{\mathbf{0}})\boldsymbol{\delta}$$
(3.3 - 11)

where

$$\mathbf{s} = \begin{bmatrix} \sigma_{x0} & \tau_{xy0} & \tau_{xz0} \\ \tau_{xy0} & \sigma_{y0} & \tau_{yz0} \\ \tau_{xz0} & \tau_{yz0} & \sigma_{z0} \end{bmatrix}$$
(3.3 - 12)

With these expressions, a general form of the geometric stiffness matrix can be written as

$$\mathbf{K}_{g}(\boldsymbol{\sigma}) = \int_{V} \mathbf{G}^{T} \overline{\mathbf{S}}(\boldsymbol{\sigma}_{0}) \mathbf{G} dV \qquad (3.3 - 13)$$

which is symmetric and explicitly dependent on the stress state.

The stress state used to form the geometric stiffness matrix may be obtained in two ways. The first way is first to perform a linear static stress analysis for the given load set and constraint set. This way is used in procedure L\_STABIL\_2. The second way is to specify, in advance, the values of the stress components given in equation (3.3-11) (*i.e.*, specify the prestress state). This way is used in procedure L\_STABIL\_1.

# 3.3.3 ALGORITHM

The algorithm used to solve equation (3.3-1) depends on the value of the global macrosymbol **eigensolver\_name**. Processor EIG2 is used if **eigensolver\_name** is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.3-2. Processor LAN is used if **eigensolver\_name** is defined to be LAN. Processor LANZ is used if **eigensolver\_name** is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.3-2 to 3.3-4.

# **3.3.4 PROCEDURE USAGE**

Procedure L\_STABIL\_1 may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call L\_STABIL\_1 ( arg1 = val1; arg2 = val2; ...)

where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L\_STABIL\_1; note that those arguments without default values are mandatory, while the others are optional.

Argument	<u>Default Value</u>	Meaning
PS_1		Prebuckling membrane stress resultant $N_x^o$
PS_2		Prebuckling membrane stress resultant $N_y^o$
PS_3		Prebuckling membrane stress resultant $N_{xy}^{o}$
BCON_SET	1	Constraint set for buckling analysis
ERROR_TOL	.0001	Convergence criterion for eigenvalues
FUNCTION	ALL	Select function to be performed by procedure
INIT_VECTOR	0	Number of initial vectors used to span the subspace
ISEQ	0	Resequencing method to be used
LDI	1	Local device index
LOAD_SET	1	Load set number
KNAME	K	First word of the name of the dataset containing the assembled stiffness matrix
MAX_ITERS	20	Maximum number of iterations allowed
N_GROUPS	1	
N_MODES	1	Number of eigenvalues to converge
PRINT	<false></false>	Flag to print displacement solution, internal forces, and element stresses, and eigenvectors
RENUMBER	<true></true>	Flag to resequence node numbers for equation solver
SHIFT	0.0	Eigenvalue shift

Tables 3.3-1, 3.3-2, and 3.3-3 list the datasets used or created by procedure L\_STABIL\_1, the procedures invoked by procedure L\_STABIL\_1, and the processors invoked by procedure L\_STABIL\_1, respectively.

Table 3.3-1 Datasets Input/Output by procedure L_STABIL_1			
Dataset	Description	Input	Output
AMAPic2.isize	Factorization Map for INV		$\checkmark$
BUCK.EVAL.i.j <sup>†</sup>	Buckling eigenvalues		$\checkmark$
BUCK.MODE. <i>i.j</i> †	Buckling eigenvalues		$\checkmark$
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	$\checkmark$	$\checkmark$
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$
DEF. <es_name>.0.nnod</es_name>	Element Definition (Connectivity)	$\checkmark$	
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	$\checkmark$	
INV.KSHF.j <sup>†</sup>	Factored Shifted System Matrix		$\checkmark$
INV. <kname>.j<sup>†</sup></kname>	Factored System Matrix		$\checkmark$
JDF1.BTAB.1.8	Model Summary	$\checkmark$	
KG.SPAR.jdf2	Assembled geometric stiffness matrix		$\checkmark$
KMAPic2.isize	Model Connectivity Map		$\checkmark$
<kname>.SPAR.jdf2</kname>	Assembled system matrix		$\checkmark$

 $\dagger$  i = <load\_set> and j = <cons\_set>

Table 3.3-2         Sub-Procedures Invoked by procedure L_STABIL_1		
Procedure	Туре	Function
ES	External	Element utility procedure
FACTOR	External	Factors assembled stiffness matrix
L_STABIL_1	Internal	Main procedure

Table 3.3-3 Processors Invoked by procedure L_STABIL_1		
Procedure	Туре	Function
AUS	Internal	Arithmetic Utilities
Е	Internal	Initializes EFIL datasets
EIG2	Internal	Solve eigenvalue problem using subspace iteration
ESi	External	Element processors based on GEP
к	Internal	Assemble system matrix
LAN	External	Solve eigenvalue problem using Lanczos method
LANZ	External	Solve eigenvalue problem using Lanczos method
RSEQ	Internal	Resequences nodes for equation solving
торо	Internal	Generates nodal topology maps
VPRT	Internal	Print SYSVEC system vectors

#### **3.3.5 ARGUMENT DESCRIPTION**

#### 3.3.5.1 BCON\_SET

Constraint set number for buckling analysis (default: 1). This argument selects which constraint set to use in solving the linear stability problem.

#### 3.3.5.2 <u>ERROR\_TOL</u>

Convergence criterion for eigenvalues (default: 0.0001). For the k-th iteration, the error measure for the *i*-th eigenvalue is

$$\epsilon_i^k = \frac{\|(\lambda_i^k - \lambda_i^{k-1})\|}{\|\lambda_i^k\|}$$

The *i*-th eigenvalue is converged if  $\epsilon_i^k$  is smaller than ERROR\_TOL.

#### 3.3.5.3 FUNCTION

Select function to be performed by procedure L\_STABIL\_1 (default: ALL). This procedure may be used to perform two functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh

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topology is analyzed, the system stiffness matrix is assembled and factored, and the eigenproblem is solved. For FUNCTION=EIGEN, procedure L\_STABIL\_1 uses a prescribed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

#### 3.3.5.4 INIT\_VECTOR

Number of initial vectors used to span the subspace (default: 0). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT\_VECTOR=0, the number of initial vectors will be calculated by the procedure as

INIT\_VECTOR=MINIMUM (2\*N\_MODES, N\_MODES + 8)

#### 3.3.5.5 ISEQ

Resequencing method to be used (default: 0). If the argument RENUMBER is  $\langle true \rangle$ , then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (*i.e.*, method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.3-2).

#### 3.3.5.6 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

# 3.3.5.7 LDI

Logical device index (default: 1).

#### 3.3.5.8 MAX\_ITERS

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

#### 3.3.5.9 <u>N\_GROUPS</u>

#### 3.3.5.10 <u>N\_MODES</u>

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR\_TOL.

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#### 3.3.5.11 PRINT

Flag to print modeshapes (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the buckling modeshapes.

# 3.3.5.12 PS\_1

Prescribed membrane stress resultant  $N_x^o$  for the prestressed state.

#### 3.3.5.13 PS\_2

Prescribed membrane stress resultant  $N_y^o$  for the prestressed state.

#### 3.3.5.14 PS\_3

Prescribed membrane stress resultant  $N_{xy}^{o}$  for the prestressed state.

#### 3.3.5.15 RENUMBER

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

#### 3.3.5.16 SHIFT

Eigenvalue shift (default: 0.0). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the shift in the buckling load factor.

#### **3.3.6 PROCEDURE FLOWCHART**

L_STABIL_1	(main procedure)
INITIALIZE	(initialize)
STIFFNESS	(form K)
STIFFNESS	(form $\mathbf{K}_g$ )
FACTOR	(factor using buckling boundary conditions)
EIGEN	(perform eigenvalue analysis)

# 3.3.7 LIMITATIONS

None.

# **3.3.8 ERROR MESSAGES AND WARNINGS**

None.

#### **3.3.9 USAGE GUIDELINES AND EXAMPLES**

Procedure L\_STABIL\_1 may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call L\_STABIL\_1 ( FUNCTION = ALL ; -- . Select function BCON\_SET = 1 ; -- . Select buckling constraint set ERROR\_TOL = .0001 ; -- . Eigenvalue convergence criterion INIT\_VECTOR = 0 ; -- . Number of initial vectors = -1 ; -- . Select resequencing method ISEO KNAME K ; -- . First word of stiffness matrix -- . dataset name  $MAX_ITERS = 20;$ -- Maximum number of iterations = 1; -- Number of eigenvalues N MODES  $N_GROUPS =$ 1; ----PS\_1 PS\_2 --PS\_3 -- . PRINT flag PRINT <true> ; = -- . RESEQUENCING flag RENUMBER <true> ; × 0.0 ; Eigenvalue shift SHIFT =

Before procedure L\_STABIL\_1 is called, the global macrosymbol eigensolver\_name should be defined as described in Section 3.3.3; otherwise, the default value of EIG2 will be used.

#### **3.3.10 PROCEDURE LISTING**

#### 3.3.11 REFERENCES

- 3.3-1 Cook, Robert D.: Concepts and Applications of Finite Element Analysis. (Second Edition). John Wiley and Sons, Inc., New York 1981.
- 3.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 3.3-3 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
- 3.3-4 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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# 3.4 Procedure L\_STABIL\_2

# **3.4.1 GENERAL DESCRIPTION**

Procedure L\_STABIL\_2 performs linear stability analysis using an eigensolver selected by the global macrosymbol eigensolver\_name (e.g., EIG2, LAN, LANZ) and structural element (ESi) processors based on the generic element processor template. The procedure assumes that the finite element model, loads, and boundary conditions have already been generated, and that the nodal displacements, reaction forces, element stresses, and buckling loads and mode shapes need to be calculated. The applied loads may be due to a combination of specified forces and displacements, and one constraint (*i.e.*, boundary condition) set is permitted per procedure call. A linear elastic stress analysis is performed first using procedure L\_STATIC (see Section 3.5) to calculate the prebuckling stress state (*i.e.*, prestress state). After the linear static solution, a linear stability analysis is performed.

#### 3.4.2 THEORY

Linear elastic stability analyses may be formulated using the concept of adjacent equilibrium. Membrane forces in beams, plates, and shells result in an equilibrium configuration in which the deformation pattern is tangent to the midsurface of the structure. However, another equilibrium configuration involving out-of-plane deflections and rotations may be adjacent to this membrane state. Buckling occurs when this membrane strain energy is converted to bending strain energy. The linear elastic stability analysis is an eigenvalue problem to calculate the critical load for the bifurcation in the solution (*e.g.*, change from a membrane state to a bending state). This eigenvalue problem can be written as

$$\mathbf{K}\boldsymbol{\phi}_i + \lambda_i \mathbf{K}_g(\boldsymbol{\sigma})\boldsymbol{\phi}_i = 0 \quad i = 1, 2, \dots \qquad (3.4-1)$$

where

The matrix denoted by  $K_g$  has been called the initial stress stiffness matrix, the differential stiffness matrix, the geometric stiffness matrix, and the stability coefficient matrix (e.g., see ref 3.4-1). It is independent of the elastic properties of the structure and dependent on the geometry, displacement field, and state of stress. Herein the matrix  $K_g$  will be referred to as the geometric stiffness matrix.

A general formulation for the geometric stiffness matrix is presented in reference 3.4-1. Strains can be written as

$$\boldsymbol{\epsilon} = \boldsymbol{\epsilon}_{\mathbf{L}} + \boldsymbol{\epsilon}_{\mathbf{NL}} \tag{3.4-2}$$

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where  $\epsilon_{L}$  contains the linear strain-displacement terms and  $\epsilon_{NL}$  contains the higher-order or nonlinear strain-displacement terms. For a given stress state  $\sigma_{0}$ , elastic strain energy is stored and can be expressed as

where

$$U = U_L + U_{NL} (3.4 - 3)$$

$$U = \frac{1}{2} \int_{V} \epsilon^{T} \sigma_{0} dV \qquad (3.4 - 4a)$$

$$U_L = \frac{1}{2} \int_V \boldsymbol{\epsilon}_{\mathbf{L}}^T \boldsymbol{\sigma}_0 dV \qquad (3.4 - 4b)$$

$$U_{NL} = \frac{1}{2} \int_{V} \epsilon_{NL}^{T} \sigma_0 dV \qquad (3.4 - 4c)$$

The geometric stiffness matrix is derived from the strain energy produced by stresses acting through displacements associated with the nonlinear strain-displacement relations. These relations couple the membrane and bending effects. Typically the strain-displacements relations are written using index notation as

$$\epsilon_{ij} = \frac{1}{2} \left[ \partial_i u_j + \partial_j u_i + \partial_i u_k \partial_j u_k \right]$$
(3.4-5)

where  $u_i = (u, v, w)$  for i = 1, 2, 3, respectively,  $\partial_i$  denotes differentiation with respect to *i*th coordinate direction and summation over repeated indices is implied. Let d denote the nodal degrees of freedom, then

$$\boldsymbol{\delta} = \mathbf{G}\mathbf{d} \tag{3.4-6}$$

where

$$\boldsymbol{\delta} = \{\partial_{\boldsymbol{x}} u, \ \partial_{\boldsymbol{y}} u, \ \partial_{\boldsymbol{z}} u, \ \partial_{\boldsymbol{x}} v, \ \partial_{\boldsymbol{y}} v, \ \partial_{\boldsymbol{z}} v, \ \partial_{\boldsymbol{x}} w, \ \partial_{\boldsymbol{y}} w, \ \partial_{\boldsymbol{z}} w\}$$

The coefficients of G are obtained by differentiating the element shape functions. Finally the matrix Q is defined as

$$\mathbf{Q} = \begin{bmatrix} \partial_x u & 0 & 0 & \partial_x v & 0 & 0 & \partial_x w & 0 & 0 \\ 0 & \partial_y u & 0 & 0 & \partial_y v & 0 & 0 & \partial_y w & 0 \\ 0 & 0 & \partial_z u & 0 & 0 & \partial_z v & 0 & 0 & \partial_z w \\ \partial_y u & \partial_x u & 0 & \partial_y v & \partial_z v & 0 & \partial_y w & \partial_x w & 0 \\ 0 & \partial_z u & \partial_y u & 0 & \partial_z v & \partial_y v & 0 & \partial_z w & \partial_y w \\ \partial_z u & 0 & \partial_x u & \partial_z v & 0 & \partial_x v & \partial_z w & 0 & \partial_z w \end{bmatrix}$$
(3.4-7)

With these definitions the nonlinear strains given by equation (3.4-2) can be written as

$$\boldsymbol{\epsilon}_{\mathbf{NL}} = \frac{1}{2} \mathbf{QGd} \tag{3.4-8}$$

#### Solution Procedures

The vector of initial stresses is

$$\sigma_0 = \{ \sigma_{x0} \sigma_{y0} \sigma_{z0} \tau_{xy0} \tau_{yz0} \tau_{xz0} \}$$
(3.4-9)

Substituting equations (3.4-6) through (3.4-9) into equation (3.4-4c) gives

$$U_{NL} = \frac{1}{2} \mathbf{d}^T \left( \int_V \mathbf{G}^T \mathbf{Q}^T \boldsymbol{\sigma}_0 \ dV \right)$$
 (3.4 - 10)

However, the term  $\mathbf{Q}^T \sigma_0$  can be written as

$$\mathbf{Q}^{T}\boldsymbol{\sigma}_{0} = \begin{bmatrix} \mathbf{s} & 0 & 0 \\ 0 & \mathbf{s} & 0 \\ 0 & 0 & \mathbf{s} \end{bmatrix} \boldsymbol{\delta} = \overline{\mathbf{S}}(\boldsymbol{\sigma}_{0})\boldsymbol{\delta}$$
(3.4 - 11)

where

$$\mathbf{s} = \begin{bmatrix} \sigma_{x0} & \tau_{xy0} & \tau_{xz0} \\ \tau_{xy0} & \sigma_{y0} & \tau_{yz0} \\ \tau_{xz0} & \tau_{yz0} & \sigma_{z0} \end{bmatrix}$$
(3.4 - 12)

With these expressions, a general form of the geometric stiffness matrix can be written as

$$\mathbf{K}_{g}(\boldsymbol{\sigma}) = \int_{V} \mathbf{G}^{T} \overline{\mathbf{S}}(\boldsymbol{\sigma}_{0}) \mathbf{G} dV \qquad (3.4 - 13)$$

which is symmetric and explicitly dependent on the stress state.

The stress state used to form the geometric stiffness matrix may be obtained in two ways. The first way is first to perform a linear static stress analysis for the given load set and constraint set. This way is used in procedure L\_STABIL\_2. The second way is to specify, in advance, the values of the stress components given in equation (3.4-11) (*i.e.*, specify the prestress state). This way is used in procedure L\_STABIL\_1.

#### **3.4.3 ALGORITHM**

The algorithm used to solve equation (3.4-1) depends on the value of the global macrosymbol **eigensolver\_name**. Processor EIG2 is used if **eigensolver\_name** is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.4-2. Processor LAN is used if **eigensolver\_name** is defined to be LAN. Processor LANZ is used if **eigensolver\_name** is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.4-2 to 3.4-4.

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# 3.4.4 PROCEDURE USAGE

Procedure L\_STABIL\_2 may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call L_STABIL_2 ( arg1 = val1; arg2 = val2; ...)
```

where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L\_STABIL\_2; note that those arguments without default values are mandatory, while the others are optional.

Argument	<u>Default Value</u>	Meaning
BCON_SET	1	Constraint set for buckling analysis
CONS_SET	1	Constaint set number for prestress analysis
DIRECTION	0	Direction for element stress output
ERROR_TOL	.0001	Convergence criterion for eigenvalues
FUNCTION	ALL	Select function to be performed by procedure
INIT_VECTOR	0	Number of initial vectors used to span the subspace
ISEQ	0	Resequencing method to be used
KNAME	K	First word of the name of the dataset containing the
		assembled stiffness matrix
LDI	1	Logical device index
LOAD_SET	1	Load set number
LOCATION	CENTROIDS	Location of the evaluation points for element stresses
MAX_ITERS	20	Maximum number of iterations allowed
N_MODES	1	Number of eigenvalues to converge
NVAL_METH	3	Method to be used for global smoothing
PRINT	<false></false>	Flag to print displacement solution, internal forces,
		element stresses, and eigenvectors
REACTION	<false></false>	Flag to compute internal forces or reactions
RENUMBER	<true></true>	Flag to resequence node numbers for equation solver
RHS	APPL.FORC	First two words of the dataset name for the
		right-hand side system vector
SHIFT	0.0	Eigenvalue shift
SMOOTH	<false></false>	Flag to compute smoothed global stresses
SOLN	STAT.DISP	First two words of the dataset name for the
		displacement solution
STRESS	<false></false>	Flag to compute element stresses (resultants)

Tables 3.4-1, 3.4-2, and 3.4-3 list the datasets used or created by procedure L\_STABIL\_2, the procedures invoked by procedure L\_STABIL\_2, and the processors invoked by procedure L\_STABIL\_2, respectively.

CSM Testbed	Procedures	Manual
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Table 3.4-1 Datasets Input/Output by procedure L_STABIL_2			
Dataset	Description	Input	Output
AMAPic2.isize	Factorization map for INV		$\checkmark$
APPL.FORC.i.1 <sup>†</sup>	Applied force vector	$\checkmark$	
APPL.MOTI. <i>i</i> .1 <sup>†</sup>	Specified displacement vector	$\checkmark$	
BUCK.EVAL. <i>i.j</i> †	Buckling eigenvalues		$\checkmark$
BUCK.MODE. <i>i.j</i> †	Buckling eigenvalues		$\checkmark$
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	$\checkmark$	$\checkmark$
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$
DEF. <es_name>.0.nnod</es_name>	Element Defn. (Connectivity)	$\checkmark$	
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	$\checkmark$	
INT.FORC. <i>i.j</i> †	System Internal Force Vector		$\checkmark$
INV.KSHF.j <sup>†</sup>	Factored Shifted System Matrix		$\checkmark$
INV. <kname>.j<sup>†</sup></kname>	Factored System Matrix		$\checkmark$
JDF1.BTAB.1.8	Model Summary	$\checkmark$	
KG.SPAR.jdf2	Assembled geometric stiffness matrix		$\checkmark$
KMAPic2.isize	Model connectivity map		$\checkmark$
<kname>.SPAR.jdf2</kname>	Assembled system matrix		$\checkmark$
STAT.DISP. <i>i.j</i> †	System Displacement Vector		$\checkmark$
STAT.REAC.i.j <sup>†</sup>	System Reaction Force Vector		$\checkmark$
STRS. <es_name>.i.j<sup>†</sup></es_name>	Element Stresses		$\checkmark$

 $\dagger i = \langle \text{load\_set} \rangle \text{ and } j = \langle \text{cons\_set} \rangle$ 

Table 3.4-2         Sub-Procedures Invoked by procedure L_STABIL_2		
Procedure	Туре	Function
ES	External	Element utility procedure
FACTOR	External	Factors assembled stiffness matrix
L_STABIL_2	Internal	Main procedure
L_STATIC	Internal	Linear static analysis

Table 3	Table 3.4-3 Processors Invoked by procedure L_STABIL_2		
Procedure	Туре	Function	
AUS	Internal	Arithmetic Utilities	
Е	Internal	Initializes EFIL datasets	
EIG2	Internal	Solve eigenvalue problem using subspace iteration	
ESi	External	Element processors based on GEP	
К	Internal	Assemble system matrix	
LAN	External	Solve eigenvalue problem using Lanczos method	
LANZ	External	Solve eigenvalue problem using Lanczos method	
RSEQ	Internal	Resequences nodes for equation solving	
торо	Internal	Generates nodal topology maps	
VPRT	Internal	Print system vectors	

# 3.4.5 ARGUMENT DESCRIPTION

#### 3.4.5.1 <u>BCON\_SET</u>

Constraint set number for buckling analysis (default: 1). This argument selects which constraint set to use in solving the linear stability problem.

#### 3.4.5.2 <u>CONS\_SET</u>

Constraint set number for prestress solution (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

# 3.4.5.3 DIRECTION

Direction for the element stress (stress resultant) output (default: 0). The element stress coordinate system will be used if direction=0. The material axes  $(x_m, y_m, z_m)$  will be used if direction=1; the material axes  $(y_m, z_m, x_m)$  will be used for direction=2; and the material axes  $(z_m, x_m, y_m)$  will be used for direction=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 3.4-2).

#### 3.4.5.4 ERROR\_TOL

Convergence criterion for eigenvalues (default: 0.0001). For the k-th iteration, the error measure for the k-th eigenvalue is

$$\epsilon^k_i = rac{\|(\lambda^k_i - \lambda^{k-1}_i)\|}{\|\lambda^k_i\|}$$

The *i*-th eigenvalue is converged if  $\epsilon_i^k$  is smaller than ERROR\_TOL.

#### 3.4.5.5 FUNCTION

Select function to be performed by procedure L\_STABIL\_2 (default: ALL). This procedure may be used to perform four functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, the displacement solution is obtained, optionally element stresses (stress resultants) and internal nodal forces (reactions) computed and the eigenproblem is solved. For FUNCTION=FACT\_SOLV, procedure L\_STABIL\_2 assumes that the system stiffness matrix has previously been assembled and that nodal resequencing has been performed. The procedure then proceeds to factor the system stiffness matrix, solves for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FUNCTION=SOLV, procedure L\_STABIL\_2 assumes that the system stiffness has previously been formed and factored. The procedure then proceeds to solve for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FUNCTION=EIGEN, procedure L\_STABIL\_2 uses a previously computed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

# 3.4.5.6 INIT\_VECTOR

Number of initial vectors used to span the subspace (default: 0). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT\_VECTOR=0, the number of initial vectors will be calculated by the procedure as

#### INIT\_VECTOR=MINIMUM (2\*N\_MODES, N\_MODES + 8)

# 3.4.5.7 ISEQ

Resequencing method to be used (default: 0). If the argument RENUMBER is  $\langle true \rangle$ , then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (*i.e.*, method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.4-2).

#### 3.4.5.8 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

#### 3.4.5.9 LDI

Logical device index (default: 1).

#### 3.4.5.10 LOAD\_SET

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

#### 3.4.5.11 LOCATION

Location of the evaluation points for the element stresses or stress resultants (default: CENTROIDS). The element stresses or stress resultants are optionally computed by calling procedure STRESS (see Section 6.4). This argument may have four values. For LOCATION=INTEG\_PTS, the element stresses are computed at the element integration points. For LOCATION=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries. For LOCATION=ALL, the element stresses are computed at the element integration points, element centroid, and element nodes.

# 3.4.5.12 MAX\_ITERS

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

# 3.4.5.13 <u>N\_MODES</u>

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR\_TOL.

#### 3.4.5.14 NVAL\_METH

Select method to be used for computing the smoothed global stresses (default: 3). Processor NVAL is used to compute the smoothed global stresses using the method defined by the argument NVAL\_METH (see Section 12.5 of reference 3.4-2). If NVAL\_METH=1, a topological interpolation of the element centroidal stresses is performed, and the element stresses must have been computed using LOCATION=CENTROIDS. If NVAL\_METH=2, a projected least-squares interpolation of the element centroidal stresses is performed, and the stresses must have been computed using LOCATION=CENTROIDS. If NVAL\_METH=3, the element nodal stresses (discontinuous across interelement boundaries) are averaged, and the element stresses must have been computed using LOCATION=NODES. Using LOCATION=ALL will generate element stresses at the element centroids, element nodes, and element gauss points. Acceptable values of LOCATION for specific values of NVAL\_METH are as follows:

NVAL_METH	LOCATION
1	CENTROIDS, ALL
2	CENTROIDS, ALL
3	NODES, ALL

#### 3.4.5.15 PRINT

Flag to print displacement solution, internal forces and element stresses (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the displacement solution and internal forces and processor PESR will be used to print the element stresses.

#### 3.4.5.16 REACTION

Flag to compute the internal nodal forces (default: <true>) If the argument REAC-TION=<true>, then the internal forces will be computed by calling procedure INT\_FORC (see Section 6.2).

#### 3.4.5.17 <u>RENUMBER</u>

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

#### 3.4.5.18 RHS

First two words of the dataset name for the right-hand side system vector (default: APPL.FORC).

#### 3.4.5.19 SHIFT

Eigenvalue shift (default: 0.0). Converged eigenvalues will only be obtained for values greater than SHIFT. The shift parameter refers to the shift in the buckling load factor.

#### 3.4.5.20 SMOOTH

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Flag to compute smoothed global stresses (default: <false>). If the argument SMOOTH=<true>, then smoothed global stresses will be computed by processor NVAL using the method defined by the argument NVAL\_METH.

#### 3.4.5.21 SOLN

First two words of the dataset name for the displacement solution (default: STAT.DISP).

#### 3.4.5.22 STRESS

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION, respectively, by calling procedure STRESS (see Section 6.4).

#### **3.4.6 PROCEDURE FLOWCHART**

L_STABIL_2	(main procedure)
L_STATIC	(linear static analysis procedure)
ES	(initialize, form K)
FACTOR	(factor assembled stiffness matrix)
SOLVE	(solve linear system of equations)
STRESS	(stress/strain recovery procedure)
ES	(calculate element and nodal stress/strain)
INT_FORCE	(internal force procedure)
ES	(internal force calculation)
ES	(form $\mathbf{K}_g$ )
FACTOR	(factor using buckling boundary conditions)

#### 3.4.7 LIMITATIONS

None.

#### 3.4.8 ERROR MESSAGES AND WARNINGS

None.

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#### **3.4.9 USAGE GUIDELINES AND EXAMPLES**

Procedure L\_STABIL\_2 may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call L\_STABIL\_2 ( FUNCTION = ALL ; -- . Select function CONS\_SET = 1 ; -- . Select constraint set BCON\_SET = 1 ; -- . Select buckling constraint set DIRECTION = 0 ; -- . Select direction for element stresses  $ERROR_TOL = .0001 ; - INIT_VECTOR = 0; -$ = 0 ; -- . Select resequencing method ISEO = K ; -- . First word of stiffness matrix KNAME 9 -- . dataset name LOAD\_SET = 1 ; -- . Select load set LOCATION = CENTROIDS ; -- Select location of element -- . stress evaluation points MAX\_ITERS = 20; -- Maximum number of iterations  $N_MODES = 1;$ -- Number of eigenvalues  $NVAL_METH = 3 ; --$ PRINT = <false> ; -- . PRINT flag REACTION = <false> ; -- . REACTIONS flag RENUMBER = <true> ; -- . RESEQUENCING flag = APPL. FORC ; -- . First two words of RHS RHS -- . vector dataset = 0.0 ; Eigenvalue shift SHIFT SMOOTH = <false> ; -- compute smoothed global stresses? STAT. DISP ; -- . First two words of SOLN SOLN = -- . dataset STRESS = <false> -- . STRESS flag

Before procedure L\_STABIL\_2 is called, the global macrosymbol eigensolver\_name should be defined as described in Section 3.4.3; otherwise, the default value of EIG2 will be used.

#### **3.4.10 PROCEDURE LISTING**

#### **3.4.11 REFERENCES**

- 3.4-1 Cook, Robert D.: Concepts and Applications of Finite Element Analysis. (Second Edition). John Wiley and Sons, Inc., New York 1981.
- 3.4-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 3.4-3 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.

3.4-4 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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# 3.5 Procedure L\_STATIC

#### **3.5.1 GENERAL DESCRIPTION**

Procedure L\_STATIC performs linear static analysis, using an equation solver selected by defining the global macrosymbol solver\_name (e.g., INV, BAND, ITER, SPK) and user specified structural element (ESi) processors based on the generic element processor template. The procedure assumes that the finite element model, loads, and boundary conditions, have already been generated, and that the nodal displacements, reaction forces, and element stresses need to be calculated. The applied loads may be due to a combination of specified forces and displacements, and one constraint (*i.e.*, boundary condition) set is permitted per procedure call.

#### 3.5.2 THEORY

Mathematically, procedure L\_STATIC solves the linear static problem:

$$\mathbf{K} \mathbf{d} = \mathbf{f} \tag{3.5-1}$$

where

 $\mathbf{K}$  = assembled linear stiffness matrix  $\mathbf{d}$  = generalized displacement vector

 $\mathbf{f} = \mathbf{external}$  force vector

Note that both the translational and rotational displacements in d are assumed to be infinitesimally small (linear strain-displacement relations are employed), and that the material (stress-strain relation) is assumed to be both linear and elastic. Once the displacement vector, d, is computed by solution of equation (3.5-1), the reaction forces are computed by multiplying those rows of the stiffness matrix K at which the displacements are prescribed (zero or non-zero) by the generalized displacement vector d. Finally, element stresses may be optionally computed.

#### 3.5.3 ALGORITHM

The algorithm used to solve equation 3.5-1 depends on the value of the global macrosymbol solver\_name. Processors INV and SSOL are used if solver\_name is defined to be INV. These processors use nodal-block sparse matrix approach as described in references 3.5-1, 3.5-2 and 3.5-3. Processor BAND (meth=28) is used if solver\_name is defined to be BAND. This algorithm is a LDL<sup>T</sup> direct method based on an Choleski variable bandwidth method with loop unrolling as described in references 3.5-1 and 3.5-4. Processor ITER (meth=0) is used if solver\_name is defined to be ITER. This algorithm is an iterative method based on a conjugate gradient method with diagonal scaling and sparse storage of the system matrix as described in references 3.5-1 and 3.5-4. Processor SPK is used if solver\_name is defined to be space of the system matrix as described in references 3.5-1 and 3.5-4. Processor SPK is used if solver\_name is defined to be space of the system matrix as described in references 3.5-1 and 3.5-4. Processor SPK is used if solver\_name is defined to be space of the system matrix as described in references 3.5-1 and 3.5-4. Processor SPK is used if solver\_name is defined to be SPK. This algorithm uses the vector-sum column Cholesky algorithms to

factor a general sparse matrix as described in references 3.5-1 and 3.5-5. Processor SPK contains a subset of the SPARSPAK-A package of FORTRAN programs designed to solve effectively large sparse systems of linear equations by direct methods (see reference 3.5-6).

#### **3.5.4 PROCEDURE USAGE**

Procedure L\_STATIC may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call L\_STATIC ( arg1 = val1; arg2 = val2; ...)

where **arg***i* are argument names and **val***i* are the corresponding values. The following are valid arguments for procedure L\_STATIC; note that those arguments without default values are mandatory, while the others are optional.

Argument	<u>Default Value</u>	Meaning
CONS_SET	1	Constraint set number
DIRECTION	1	Direction for element stress output
FUNCTION	ALL	Select function to be performed by procedure
ISEQ	-1	Resequencing method to be used
KNAME	K	First word of the name of the dataset containing the
		assembled stiffness matrix
LDI	1	Logical device index
LOAD_SET	1	Load set number
LOCATION	NODES	Location of the evaluation points for element stresses
NVAL_METH	3	Method to be used for global smoothing
PRINT	<false></false>	Flag to print computed results
REACTION	<false></false>	Flag to compute internal forces or reactions
RENUMBER	<true></true>	Flag to resequence node numbers for equation solver
RHS	APPL.FORC	First two words of the dataset name for the right-hand side system vector
SMOOTH	<false></false>	Flag to compute smoothed global stresses
SOLN	STAT.DISP	First two words of the dataset name for the displacement solution
STRESS	<false></false>	Flag to compute element stresses (resultants)

Tables 3.5-1, 3.5-2, and 3.5-3 list the datasets used or created by procedure L\_STATIC, the procedures invoked by procedure L\_STATIC, and the processors invoked by procedure L\_STATIC, respectively.

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Table 3.5-1 Datasets Input/Output by procedure L_STATIC			
Dataset	Description	Input	Output
AMAPic2.isize	Factorization Map for INV		$\checkmark$
APPL.FORC.i.1 <sup>†</sup>	Applied force vector	$\checkmark$	
APPL.MOTI.i.1 <sup>†</sup>	Specified displacement vector	· √	
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	$\checkmark$	$\checkmark$
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$
DEF. <es_name>.0.nnod</es_name>	Element Defn. (Connectivity)	$\checkmark$	
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	$\checkmark$	
INT.FORC. <i>i.j</i> <sup>†</sup>	System Internal Force Vector		$\checkmark$
INV. <kname>.i.j<sup>†</sup></kname>	Factored System Matrix		$\checkmark$
JDF1.BTAB.1.8	Model Summary	$\checkmark$	
JLOC.BTAB.2.5	Nodal Coordinates	$\checkmark$	
KMAPic2.isize	Model Connectivity Map		$\checkmark$
<kname>.SPAR.jdf2</kname>	Assembled System Matrix		$\checkmark$
PROP.BTAB.*	Material/Section Properties	$\checkmark$	
QJJT.BTAB.2.9	Nodal Transformations	$\checkmark$	
STAT.DISP.i.j <sup>†</sup>	System Displacement Vector		$\checkmark$
STAT.REAC.i.j <sup>†</sup>	System Reaction Force Vector		$\checkmark$
STRS. <es_name>.i.j<sup>†</sup></es_name>	Element Stresses		$\checkmark$

 $\dagger$  i = <load\_set> and j = <cons\_set>

Table 3.5-2 Sub-Procedures Invoked by procedure L_STATIC		
Procedure	Туре	Function
ES	External	Element utility procedure
FACTOR	External	Factors assembled stiffness matrix
INT_FORCE	External	Computes internal forces
L_STATIC	Internal	Main procedure
SOLVE	External	Solves for the displacement solution
STRESS	External	Computes element stresses

Table 3.5-3 Processors Invoked by procedure L_STATIC		
Procedure	Type Function	
Е	Internal	Initializes EFIL datasets
ESi	External	Element processors based on GEP
К	Internal	Assemble material stiffness matrix
RSEQ	Internal	Resequences nodes for equation solving
торо	Internal	Generates nodal topology maps
VPRT	Internal	Print SYSVEC-format vectors

# 3.5.5 ARGUMENT DESCRIPTION

#### 3.5.5.1 <u>CONS\_SET</u>

Constraint set number (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

#### 3.5.5.2 DIRECTION

Direction for the element stress (stress resultant) output (default: 1). The element stress coordinate system will be used if DIRECTION=0. The material axes  $(x_m, y_m, z_m)$  will be used if DIRECTION=1; the material axes  $(y_m, z_m, x_m)$  will be used for DIRECTION=2; and the material axes  $(z_m, x_m, y_m)$  will be used for DIRECTION=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 3.5-1).

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# 3.5.5.3 FUNCTION

Select function to be performed by procedure L\_STATIC (default: ALL). This procedure may be used to perform three functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, the displacement solution is obtained and optionally element stresses (stress resultants) and internal nodal forces (reactions) computed. For FUNCTION=FACT\_SOLV, procedure L\_STATIC assumes that the system stiffness matrix has previously been assembled and that nodal resequencing has been performed. The procedure then proceeds to factor the system stiffness matrix, solves for the displacement solution, and optionally computes the element stresses (stress resultants) and internal nodal forces (reactions). For FUNCTION=SOLV, procedure L\_STATIC assumes that the system stiffness has previously been formed and factored. The procedure then proceeds to solve for the displacement solution and optionally computes the element stresses (stress resultants) and internal nodal forces (reactions). Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

# 3.5.5.4 ISEQ

Resequencing method to be used (default: -1). If the argument RENUMBER is  $\langle true \rangle$ , then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (*i.e.*, method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.5-1). If the argument ISEQ has a value of -1, then a default method will be used depending on the value of the global macrosymbol  $\langle solver_name \rangle$ .

These default value are as follows:

<pre><solver_name></solver_name></pre>	ISEQ
INV	0
BAND	2
ITER	1
SPK	1

# 3.5.5.5 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

# 3.5.5.6 LDI

Logical device index (default: 1).

# 3.5.5.7 LOAD\_SET

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

# 3.5.5.8 LOCATION

Location of the evaluation points for the element stresses or stress resultants (default: NODES). The element stresses or stress resultants are optionally computed by calling procedure STRESS (see Section 6.4). This argument may have four values. For LOCATION=INTEG\_PTS, the element stresses are computed at the element integration points. For LOCATION=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries. For LOCATION=ALL, the element stresses are computed at the element integration points, element centroid, and element nodes.

#### 3.5.5.9 NVAL\_METH

Select method to be used for computing the smoothed global stresses (default: 3). Processor NVAL is used to compute the smoothed global stresses using the method defined by the argument NVAL\_METH (see Section 12.5 of reference 6.4-1). If NVAL\_METH=1, a topological interpolation of the element centroidal stresses is performed, and the element stresses must have been computed using LOCATION=CENTROIDS. If NVAL\_METH=2, a projected least-squares interpolation of the element centroidal stresses is performed, and the stresses must have been computed using LOCATION=CENTROIDS. If NVAL\_METH=3, the element nodal stresses (discontinuous across interelement boundaries) are averaged, and the element stresses must have been computed using LOCATION=NODES. Using LOCATION=ALL will generate element stresses at the element centroids, element nodes, and element gauss points. Acceptable values of LOCATION for specific values of NVAL\_METH are as follows:

NVAL_METH	LOCATION	
1	CENTROIDS, ALL	
2	CENTROIDS, ALL	
3	NODES, ALL	

#### 3.5.5.10 PRINT

Flag to print computed results such as the displacement solution, internal forces, and element and nodal stresses (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the displacement solution and internal forces, processor PESR will be used to print the element stresses and processor PNSR will be used to print nodal stresses.

# 3.5.5.11 REACTION

Flag to compute the internal nodal forces (default: <true>) If the argument REAC-TION=<true>, then the internal forces will be computed by calling procedure INT\_FORCE (see Section 6.2).

#### 3.5.5.12 RENUMBER

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations given by equation 3.5-1.

#### 3.5.5.13 RHS

First two words of the dataset name for the right-hand side system vector (default: APPL.FORC).

#### 3.5.5.14 SMOOTH

Flag to compute smoothed global stresses (default: <false>). If the argument SMOOTH=<true>, then smoothed global stresses will be computed by processor NVAL using the method defined by the argument NVAL\_METH.

#### 3.5.5.15 SOLN

First two words of the dataset name for the displacement solution (default: STAT.DISP).

#### 3.5.5.16 STRESS

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS is defined to be <true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION, respectively, by calling procedure STRESS (see Section 6.4).

#### 3.5.6 PROCEDURE FLOWCHART

L_STATIC	(main procedure)
ES	(initialize, form K)
FACTOR	(factor assembled stiffness matrix)
SOLVE	(solve linear system of equations)
STRESS	(stress/strain recovery procedure)
ES	(calculate element stresses and/or strains)
INT_FORCE	(internal force procedure)
ES	(internal force calculation)

# 3.5.7 LIMITATIONS

Procedure L\_STATIC assumes that all datasets either required or generated reside on library one (LDI=1).

#### 3.5.8 ERROR MESSAGES AND WARNINGS

None.

#### 3.5.9 USAGE GUIDELINES AND EXAMPLES

Procedure L\_STATIC may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis.

*call L_STATIC	( FUNCTION	= ALL ; Select function
		1 ; Select constraint set
D	IRECTION =	0 ; Select direction for element stresses
19	SEQ =	-1 ; Select resequencing method
KI	NAME =	K ; First word of stiffness matrix
		dataset name
L	OAD_SET =	1 ; Select load set
L	OCATION =	CENTROIDS ; Select location of element
		stress evaluation points
PI	RINT =	<true> ; PRINT flag</true>
RI	EACTION =	<false> ; REACTIONS flag</false>
RI	ENUMBER =	<true> ; RESEQUENCING flag</true>
RI	HS =	APPL. FORC ; First two words of RHS
		vector dataset
S	OLN =	STAT. DISP ; First two words of SOLN
		dataset
SI	TRESS =	<false> STRESS flag</false>
		)

Before procedure L\_STATIC is called, the global macrosymbol solver\_name should be defined as described in Section 3.5.3; otherwise, the default value of INV will be used.

# **3.5.10 PROCEDURE LISTING**

#### 3.5.11 REFERENCES

- 3.5-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 3.5-2 Whetstone, W. D.: "Computer Analysis of Large Linear Frames": Journal of the Structural Division, ASCE, Vol. 95, No. ST11, November 1969, pp. 2401-2417.
- 3.5-3 Regelbrugge, M. E. and Wright, M. A.: The Computational Structural Mechanics Testbed Matrix Processors Internal Logic and Dataflow Descriptions. NASA CR-181742, March 1989.
- 3.5-4 Poole, Eugene L. and Overman, Andrea L.: The Solution of Linear Systems of Equations with a Structural Analysis Code of the NAS Cray-2. NASA CR-4159, September 1988.
- 3.5-5 Chu, Eleanor and George, J. Alan: Sparse Matrix Methods Research Using the CSM Testbed Software System. NASA CR-4219, March 1989.
- 3.5-6 Chu, E.C.H.; George, J. A.; Liu, W-H.; and Ng, E. G-Y.: User's Guide for SPARSPAK-A: Waterloo Sparse Linear Equations Package. Technical Report CS-84-36, University of Waterloo, Waterloo Ontario, Canada, 1984.
- 3.5-7 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

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# **3.6 Procedure L\_VIBRAT\_0**

#### 3.6.1 GENERAL DESCRIPTION

Procedure L\_VIBRAT\_O performs a linear vibration analysis about an unstressed state. The eigensolver is selected by defining the global macrosymbol eigensolver\_name to be the name of the desired processor (e.g., EIG2, LAN, LANZ), and the structural element processors (ESi) form the elemental stiffness and mass matrices. The procedure assumes that the finite element model and boundary conditions have already been generated and that the vibration modeshapes and frequencies need to be calculated.

#### 3.6.2 THEORY

Linear vibration analyses are formulated using the equations of motion for an undamped structure. For the case of no external forces, the equations of motion are

$$\mathbf{M}\ddot{\mathbf{u}} + \mathbf{K}\mathbf{u} = \mathbf{0} \tag{3.6-1}$$

where

M = assembled mass matix (consistent or diagonal)
K = assembled linear stiffness matrix
ü = acceleration vector
u = displacement vector

If harmonic motion is assumed, then

$$\mathbf{u} = \boldsymbol{\phi}_i \, \sin \, \omega_i t \qquad i = 1, 2, \dots \tag{3.6-2}$$

where

 $\phi_i = i$ th eigen modeshape  $\omega_i = i$ th circular frequency (radians per second)

The *i*th cyclic frequency  $f_i$  (in hertz) is

$$f_i = \frac{\omega_i}{2\pi}$$

and the period  $T_i$  (in seconds) is

$$T_i = \frac{1}{f_i}$$

Substituting equation (3.6-2) in equation (3.6-1) gives

$$(\mathbf{K} - \lambda_i \mathbf{M}) \phi_i = 0$$
  $i = 1, 2, ...$  (3.6-3)

where

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3.6-1

$$\lambda_i = \omega_i^2.$$

If the user has specified the reset parameter GRAV in processor LAU to a value of unity then the matrix M has the meaning of a "weight" matrix instead of a "mass" matrix. This reset parameter is important for interpreting the eigenvalues calculated by the various eigensolvers.

## 3.6.3 ALGORITHM

The algorithm used to solve equation (3.6-1) depends on the value of the global macrosymbol eigensolver\_name. Processor EIG2 is used if eigensolver\_name is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.6-2. Processor LAN is used if eigensolver\_name is defined to be LAN. Processor LANZ is used if eigensolver\_name is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.6-2 and 3.6-3. If this global macrosymbol is not defined, procedure L\_VIBRAT\_O will set it to EIG2.

### **3.6.4 PROCEDURE USAGE**

Procedure  $L_VIBRAT_0$  may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call L_VIBRAT_0 ( arg1 = val1; arg2 = val2; ...)
```

where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L\_VIBRAT\_0; note that those arguments without default values are mandatory, while the others are optional.

Argument	<u>Default Value</u>	Meaning
ERROR_TOL	.0001	Convergence criterion for eigenvalues
FUNCTION	ALL	Select function to be performed by procedure
INIT_VECTORS	0	Number of initial vectors used to span the subspace
ISEQ	0	Resequencing method to be used
LDI	1	Logical device index
KNAME	K	First word of the name of the dataset containing the
		assembled stiffness matrix
MASS_TYPE	CONSISTENT	Type of mass matrix
MAX_ITERS	20	Maximum number of iterations
N_MODES	1	Number of eigenvalues to converge
PRINT	<false></false>	Flag to print eigenvectors
RENUMBER	<true></true>	Flag to resequence node numbers for equation solver
SHIFT	0.0	Eigenvalue shift
VCON_SET	1	Constraint set for vibration analysis

Tables 3.6-1, 3.6-2, and 3.6-3 list the datasets used or created by procedure L\_VIBRAT\_0, the procedures invoked by procedure L\_VIBRAT\_0, and the processors invoked by procedure L\_VIBRAT\_0, respectively.

Table 3.6-1 Datasets Input/Output by procedure L_VIBRAT_0				
Dataset	Description	Input	Output	
AMAPic2.isize	Factorization Map for INV		$\checkmark$	
CEM.SPAR	Consistent Mass Matrix		$\checkmark$	
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	$\checkmark$	$\checkmark$	
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$	
DEF. <es_name>.0.nnod</es_name>	Element Defn. (Connectivity)	$\checkmark$		
DEM.DIAG	Diagonal (Lumped) Mass Matrix		$\checkmark$	
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	$\checkmark$		
INV.KSHF.j <sup>†</sup>	Factored Shifted System Matrix		$\checkmark$	
INV. <kname>.j<sup>†</sup></kname>	Factored System Matrix		$\checkmark$	
JDF1.BTAB.1.8	Model Summary	$\checkmark$		
KG.SPAR.jdf2	Assembled geometric stiffness matrix		$\checkmark$	
KMAPic2.isize	Model Connectivity Map		$\checkmark$	
<kname>.SPAR.jdf2</kname>	Assembled system matrix		$\checkmark$	
VIBR.EVAL.1.j <sup>†</sup>	Vibration eigenvalues		$\checkmark$	
VIBR.MODE.1. <i>j</i> <sup>†</sup>	Vibration eigenvalues		$\checkmark$	

 $\dagger j = \langle cons\_set \rangle$ 

Table 3.6-3 Processors Invoked by Procedure L_VIBRAT_0			
Procedure	Туре	Function	
AUS	Internal	Arithmetic utilities	
Е	Internal	Initializes EFIL datasets	
EIG2	Internal	Solve eigenvalue problem using subspace iteration	
ESi	External	Element processors based on GEP	
К	Internal	Assemble system matrix	
LAN	External	Solve eigenvalue problem using Lanczos method	
LANZ	External	Solve eigenvalue problem using Lanczos method	
RSEQ	Internal	Resequences nodes for equation solving	
торо	Internal	Generates nodal topology maps	
VPRT	Internal	Print SYSVEC system vectors	

### 3.6.5 ARGUMENT DESCRIPTION

### 3.6.5.1 ERROR\_TOL

Convergence criterion for eigenvalues (default: 0.0001). For the k-th iteration, the error measure for the *i*-th eigenvalue is

$$\boldsymbol{\epsilon}_{i}^{k} = \frac{\|(\lambda_{i}^{k} - \lambda_{i}^{k-1})\|}{\|\lambda_{i}^{k}\|}$$

The *i*-th eigenvalue is converged if  $\epsilon_i^k$  is smaller than ERROR\_TOL.

### 3.6.5.2 FUNCTION

Select function to be performed by procedure L\_VIBRAT\_O (default: ALL). This procedure may be used to perform two functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, and the eigenproblem is solved. For FUNCTION=EIGEN, procedure L\_VIBRAT\_O uses a previously computed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model.

## 3.6.5.3 INIT\_VECTOR

Number of initial vectors used to span the subspace (default: 0). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT\_VECTOR=0, the number of initial vectors will be calculated by the procedure as

INIT\_VECTOR=MINIMUM (2\*N\_MODES, N\_modes + 8)

### 3.6.5.4 ISEQ

Resequencing method to be used (default: 0). If the argument RENUMBER is  $\langle true \rangle$ , then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (*i.e.*, method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.6-1).

### 3.6.5.5 LDI

Logical device index (default: 1).

### 3.6.5.6 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

### 3.6.5.7 <u>MASS\_TYPE</u>

Type of mass matrix (default: CONSISTENT). If MASS\_TYPE=CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS\_TYPE=DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

#### 3.6.5.8 MAX\_ITERS

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

### 3.6.5.9 <u>N\_MODES</u>

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR\_TOL.

### 3.6.5.10 PRINT

Flag to print displacement solution, internal forces and element stresses (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the vibration modeshapes.

### 3.6.5.11 RENUMBER

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

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#### 3.6.5.12 SHIFT

Eigenvalue shift (default: 0.0). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared (*i.e.*,  $\omega^2$ ) for vibration problems.

#### 3.6.5.13 <u>VCON\_SET</u>

Constraint set number for vibration analysis (default: 1). This argument selects which constraint set to use in solving the linear vibration problem.

### 3.6.6 PROCEDURE FLOWCHART

L_VIBRAT_O	(main procedure)
ES	(initialize, form $\mathbf{K}$ and $\mathbf{M}$ )
FACTOR	(factor using vibration boundary conditions)

### 3.6.7 LIMITATIONS

None.

### 3.6.8 ERROR MESSAGES AND WARNINGS

None.

### 3.6.9 USAGE GUIDELINES AND EXAMPLES

Procedure L\_VIBRAT\_0 may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. \*call L\_VIBRAT\_0 ( FUNCTION = ALL ; -- . Select function BCON\_SET = 1 ; -- . Select vibration constraint set ERROR\_TOL = .0001 ; -- . Eigenvalue convergence criterion INIT\_VECTOR = 0 ; -- . Number of initial vectors = -1 ; -- . Select resequencing method ISEO ; -- . First word of stiffness matrix KNAME × K -- . dataset name  $MAX_ITERS = 20;$ -- Maximum number of iterations = 1 ; -- Number of eigenvalues N MODES <true> ; -- . PRINT flag PRINT = -- . RESEQUENCING flag RENUMBER × <true> ; . Eigenvalue shift SHIFT = 0.0

Before procedure L\_VIBRAT\_0 is called, the global macrosymbol eigensolver\_name should be defined as described in Section 3.6-3; otherwise, the default value of EIG2 will be used.

#### **3.6.10 PROCEDURE LISTING**

#### **3.6.11 REFERENCES**

- 3.6-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 3.6-2 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
- 3.6-3 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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# 3.7 Procedure L\_VIBRAT\_1

#### 3.7.1 GENERAL DESCRIPTION

Procedure L\_VIBRAT\_1 performs a linear vibration analysis about a prescribed prestressed state. The eigensolver is selected by defining the global macrosymbol eigensolver\_name to be the name of the desired processor (e.g., EIG2, LAN), and the structural element processors (ESi) form the elemental stiffness and mass matrices. The procedure assumes that the finite element model and boundary conditions have already been generated, that the prestressed state has been prescribed, and that the vibration modeshapes and frequencies need to be calculated.

#### 3.7.2 THEORY

Linear vibration analyses are formulated using the equations of motion for an undamped structure. For the case of prestressed state, the equations of motion are

$$\mathbf{M}\ddot{\mathbf{u}} + \mathbf{K}\mathbf{u} + \mathbf{K}_g(\boldsymbol{\sigma})\mathbf{u} = 0 \tag{3.7-1}$$

where

M = assembled mass matix (consistent or diagonal)

 $\mathbf{K} = \mathbf{assembled}$  linear stiffness matrix

 $\mathbf{K}_{g}(\boldsymbol{\sigma})$  = assembled geometric stiffness matrix for given stress state

 $\ddot{\mathbf{u}} = \mathbf{acceleration} \ \mathbf{vector}$ 

 $\mathbf{u} = displacement \ vector$ 

$$\sigma = \text{prestress state}$$

The prestressed state may be defined in several ways. Procedure L\_VIBRAT\_1 assumes that a membrane prestressed state  $(N_x^o, N_y^o, N_{xy}^o)$  is explicitly prescribed.

If harmonic motion is assumed, then

$$\mathbf{u} = \boldsymbol{\phi}_i \, \sin \, \omega_i t \qquad i = 1, 2, \dots \qquad (3.7-2)$$

where

 $\phi_i = i$ th eigen modeshape  $\omega_i = i$ th circular frequency (radians per second)

The *i*th cyclic frequency  $f_i$  (in hertz) is

$$f_i = \frac{\omega_i}{2\pi}$$

and the period  $T_i$  (in seconds) is

$$T_i = \frac{1}{f_i}$$

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Substituting equation (3.7-2) in equation (3.7-1) gives

$$(\mathbf{K} + \mathbf{K}_{g}(\boldsymbol{\sigma}) - \lambda_{i}\mathbf{M})\boldsymbol{\phi}_{i} = 0 \qquad i = 1, 2, \dots \qquad (3.7 - 3)$$

where

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$$(\mathbf{K} + \mathbf{K}_g(\sigma) - \lambda_i \mathbf{W}) \varphi_i = 0 \qquad i = 1, 2, \dots \qquad (3.1 - 3)$$
$$\lambda_i = \omega_i^2.$$

If the user has specified the reset parameter GRAV in processor LAU to a value of unity then the matrix M has the meaning of a "weight" matrix instead of a "mass" matrix. This reset parameter is important for interpreting the eigenvalues calculated by the various eigensolvers.

# 3.7.3 ALGORITHM

The algorithm used to solve equation (3.7-1) depends on the value of the global macrosymbol **eigensolver\_name**. Processor EIG2 is used if **eigensolver\_name** is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.7-2. Processor LAN is used if **eigensolver\_name** is defined to be LANZ. Processor LANZ is used if **eigensolver\_name** is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.7-2 to 3.7-3. If this global macrosymbol is not defined, procedure L\_VIBRAT\_1 will set it to EIG2.

# **3.7.4 PROCEDURE USAGE**

Procedure L\_VIBRAT\_1 may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call L\_VIBRAT\_1 ( arg1 = val1; arg2 = val2; ...)

where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L\_VIBRAT\_1; note that those arguments without default values are mandatory, while the others are optional.

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Argument	<u>Default Value</u>	Meaning
PS_1		Prescribed membrane stres resultant $N_x^o$
PS_2		Prescribed membrane stres resultant $N_{y}^{o}$
PS_3		Prescribed membrane stres resultant $N_{xy}^{o}$
ERROR_TOL	.0001	Convergence criterion for eigenvalues
FUNCTION	ALL	Select function to be performed by procedure
INIT_VECTORS	0	Number of initial vectors used to span the subspace
ISEQ	0	Resequencing method to be used
LDI	1	Logical device index
KNAME	K	First word of the name of the dataset containing the assembled stiffness matrix
MASS_TYPE	CONSISTENT	Type of mass matrix
MAX_ITERS	20	Maximum number of iterations
N_GROUPS	1	
N_MODES	1	Number of eigenvalues to converge
PRINT	<false></false>	Flag to print eigenvectors
RENUMBER	<true></true>	Flag to resequence node numbers for equation solver
SHIFT	0.0	Eigenvalue shift
VCON_SET	1	Constraint set for vibration analysis

Tables 3.7-1, 3.7-2, and 3.7-3 list the datasets used or created by procedure L\_VIBRAT\_1, the procedures invoked by procedure L\_VIBRAT\_1, and the processors invoked by procedure L\_VIBRAT\_1, respectively.

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Table 3.7-1 Datasets Input/Output by procedure L_VIBRAT_1				
Dataset	Description	Input	Output	
AMAPic2.isize	Factorization Map for INV		$\checkmark$	
CEM.SPAR	Consistent Mass Matrix		$\checkmark$	
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	$\checkmark$	$\checkmark$	
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$	
DEF. <es_name>.0.nnod</es_name>	Element Defn. (Connectivity)	$\checkmark$		
DEM.DIAG	Diagonal (Lumped) Mass Matrix		$\checkmark$	
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	$\checkmark$		
INV.KSHF.j <sup>†</sup>	Factored Shifted System Matrix		$\checkmark$	
INV. <kname>.j<sup>†</sup></kname>	Factored System Matrix		$\checkmark$	
JDF1.BTAB.1.8	Model Summary	$\checkmark$		
KG.SPAR.jdf2	Assembled geometric stiffness matrix		$\checkmark$	
KMAPic2.isize	Model Connectivity Map		$\checkmark$	
<kname>.SPAR.jdf2</kname>	Assembled system matrix		$\checkmark$	
VIBR.EVAL.1.j <sup>†</sup>	Vibration eigenvalues		$\checkmark$	
VIBR.MODE.1. <i>j</i> <sup>†</sup>	Vibration eigenvalues		$\checkmark$	

 $\dagger j = \langle vcon_set \rangle$ 

Table 3.7-2 Sub-Procedures Invoked by procedure L_VIBRAT_1			
Procedure	Туре	Function	
ES	External	Element utility procedure	
FACTOR	External	Factors assembled stiffness matrix	
L_VIBRAT_1	Internal	Main procedure	

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Table 3.7-3 Processors Invoked by Procedure L_VIBRAT_1		
Procedure	Туре	Function
AUS	Internal	Arithmetic utilities
Е	Internal	Initializes EFIL datasets
EIG2	Internal	Solve eigenvalue problem using subspace iteration
ESi	External	Element processors based on GEP
K	Internal	Assemble system matrix
LAN	External	Solve eigenvalue problem using Lanczos method
LANZ	External	Solve eigenvalue problem using Lanczos method
RSEQ	Internal	Resequences nodes for equation solving
торо	Internal	Generates nodal topology maps
VPRT	Internal	Print SYSVEC system vectors

# **3.7.5 ARGUMENT DESCRIPTION**

# 3.7.5.1 <u>ERROR\_TOL</u>

Convergence criterion for eigenvalues (default: 0.0001). For the k-th iteration, the error measure for the *i*-th eigenvalue is

$$\boldsymbol{\epsilon}_{i}^{k} = \frac{\|(\lambda_{i}^{k} - \lambda_{i}^{k-1})\|}{\|\lambda_{i}^{k}\|}$$

The *i*-th eigenvalue is converged if  $\epsilon_i^k$  is smaller than ERROR\_TOL.

# 3.7.5.2 FUNCTION

Select function to be performed by procedure L\_VIBRAT\_1 (default: ALL). This procedure may be used to perform two functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, and the eigenproblem is solved. For FUNCTION=EIGEN, procedure L\_VIBRAT\_1 uses a prescribed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model.

# 3.7.5.3 INIT\_VECTOR

Number of initial vectors used to span the subspace (default: 0). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT\_VECTOR=0, the number of initial vectors will be calculated by the procedure as

INIT\_VECTOR=MINIMUM (2\*N\_MODES, N\_modes + 8)

### 3.7.5.4 ISEQ

Resequencing method to be used (default: 0). If the argument RENUMBER is  $\langle true \rangle$ , then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (*i.e.*, method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.7-1).

### 3.7.5.5 LDI

Logical device index (default: 1).

### 3.7.5.6 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

### 3.7.5.7 <u>MASS\_TYPE</u>

Type of mass matrix (default: CONSISTENT). If MASS\_TYPE=CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS\_TYPE=DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

#### 3.7.5.8 <u>N\_GROUPS</u>

Element group number (default: 1).

# 3.7.5.9 MAX\_ITERS

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

#### 3.7.5.10 <u>N\_MODES</u>

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR\_TOL.

# 3.7.5.11 PRINT

Flag to print modeshapes (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the vibration modeshapes.

# 3.7.5.12 PS\_1

Prescribed membrane stress resultant  $N_x^o$  for the prestressed state.

## 3.7.5.13 PS\_2

Prescribed membrane stress resultant  $N_y^o$  for the prestressed state.

# 3.7.5.14 PS\_3

Prescribed membrane stress resultant  $N_{xy}^o$  for the prestressed state.

## 3.7.5.15 RENUMBER

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

### 3.7.5.16 SHIFT

Eigenvalue shift (default: 0.0). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared (*i.e.*,  $\omega^2$ ) for vibration problems.

### 3.7.5.17 <u>VCON\_SET</u>

Constraint set number for vibration analysis (default: 1). This argument selects which constraint set to use in solving the linear vibration problem.

# 3.7.6 PROCEDURE FLOWCHART

L_VIBRAT_1	(main procedure)
ES	(initialize, form K and $M$ )
ES	(form Kg)
FACTOR	(factor using vibration boundary conditions)

# 3.7.7 LIMITATIONS

None.

# 3.7.8 ERROR MESSAGES AND WARNINGS

None.

### **3.7.9 USAGE GUIDELINES AND EXAMPLES**

Procedure L\_VIBRAT\_1 may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call L\_VIBRAT\_1 ( FUNCTION = ALL ; -- . Select function VCON\_SET = 1 ; -- . Select vibration constraint set ERROR\_TOL = .0001 ; -- . Eigenvalue convergence criterion INIT\_VECTOR = 0 ; -- . Number of initial vectors ; -- . Select resequencing method 0 ISEQ = KNAME K ; -- . First word of stiffness matrix -- . dataset name -- Maximum number of iterations  $MAX_ITERS = 20;$ = 1; -- Number of eigenvalues N\_MODES N\_GROUPS = 1; --PS\_1 ----PS\_2 PS\_3 ---; PRINT <true> : -- . PRINT flag = RENUMBER × <true> : -- . RESEQUENCING flag 0.0 ; Eigenvalue shift SHIFT =

Before procedure L\_VIBRAT\_1 is called, the global macrosymbol eigensolver\_name should be defined as described in Section 3.7-3; otherwise, the default value of EIG2 will be used.

#### **3.7.10 PROCEDURE LISTING**

#### **3.7.11 REFERENCES**

- 3.7-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 3.7-2 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
- 3.7-3 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

# 3.8 Procedure L\_VIBRAT\_2

### **3.8.1 GENERAL DESCRIPTION**

Procedure L\_VIBRAT\_2 performs a linear vibration analysis about a prescribed prestressed state. The eigensolver is selected by defining the global macrosymbol eigensolver\_name to be the name of the desired processor (e.g., EIG2, LAN), and the structural element processors (ESi) form the elemental stiffness and mass matrices. The procedure assumes that the finite element model and boundary conditions have already been generated, that the prestressed state has been prescribed, and that the vibration modeshapes and frequencies need to be calculated.

### 3.8.2 THEORY

Linear vibration analyses are formulated using the equations of motion for an undamped structure. For the case of prestressed state, the equations of motion are

$$\mathbf{M}\ddot{\mathbf{u}} + \mathbf{K}\mathbf{u} + \mathbf{K}_{g}(\boldsymbol{\sigma})\mathbf{u} = 0 \tag{3.8-1}$$

where

M = assembled mass matix (consistent or diagonal)

 $\mathbf{K} =$ assembled linear stiffness matrix

 $\mathbf{K}_{g}(\boldsymbol{\sigma})$  = assembled geometric stiffness matrix for given stress state

 $\ddot{\mathbf{u}} = \mathbf{acceleration} \ \mathbf{vector}$ 

 $\mathbf{u} = displacement vector$ 

 $\sigma = \text{prestress state}$ 

The prestressed state may be defined in several ways. Procedure L\_VIBRAT\_2 assumes that the prestressed state will be first calculated using procedure L\_STATIC.

If harmonic motion is assumed, then

$$\mathbf{u} = \boldsymbol{\phi}_i \sin \omega_i t \qquad i = 1, 2, \dots \qquad (3.8-2)$$

where

 $\phi_i = i$ th eigen modeshape

 $\omega_i = i$ th circular frequency (radians per second)

The *i*th cyclic frequency  $f_i$  (in hertz) is

$$f_i = \frac{\omega_i}{2\pi}$$

and the period  $T_i$  (in seconds) is

$$T_i=\frac{1}{f_i}$$

Substituting equation (3.8-2) in equation (3.8-1) gives

$$(\mathbf{K} + \mathbf{K}_g(\boldsymbol{\sigma}) - \lambda_i \mathbf{M})\boldsymbol{\phi}_i = 0 \qquad i = 1, 2, \dots \qquad (3.8 - 3)$$

where

$$\lambda_i = \omega_i^2$$
.

If the user has specified the reset parameter GRAV in processor LAU to a value of unity then the matrix M has the meaning of a "weight" matrix instead of a "mass" matrix. This reset parameter is important for interpreting the eigenvalues calculated by the various eigensolvers.

# 3.8.3 ALGORITHM

The algorithm used to solve equation (3.3-1) depends on the value of the global macrosymbol **eigensolver\_name**. Processor EIG2 is used if **eigensolver\_name** is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.3-2. Processor LAN is used if **eigensolver\_name** is defined to be LAN. Processor LANZ is used if **eigensolver\_name** is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.3-2 to 3.3-3. If this global macrosymbol is not defined, procedure L\_VIBRAT\_2 will set it to EIG2.

### **3.8.4 PROCEDURE USAGE**

Procedure L\_VIBRAT\_2 may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call L\_VIBRAT\_2 ( arg1 = val1; arg2 = val2; ...)

where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L\_VIBRAT\_2; note that those arguments without default values are mandatory, while the others are optional.

Argument	Default Value	Meaning
CONS_SET	1	Constaint set number for prestress analysis
DIRECTION	0	Direction for element stress output
ERROR_TOL	.0001	Convergence criterion for eigenvalues
FUNCTION	ALL	Select function to be performed by procedure
INIT_VECTORS	0	Number of initial vectors used to span the subspace
ISEQ	0	Resequencing method to be used
LDI	1	Logical device index
KNAME	K	First word of the name of the dataset containing the
		assembled stiffness matrix
LOAD_SET	1	Load set number
MASS_TYPE	CONSISTENT	Type of mass matrix
MAX_ITERS	20	Maximum number of iterations
N_GROUPS	1	
N_MODES	1	Number of eigenvalues to converge
PRINT	<false></false>	Flag to print computed solutions
REACTION	<false></false>	Flag to compute internal forces or reactions
RENUMBER	<true></true>	Flag to resequence node numbers for equation solver
SHIFT	0.0	Eigenvalue shift
STRESS	<false></false>	Flag to compute element stresses (resultants)
VCON_SET	1	Constraint set for vibration analysis

Tables 3.8-1, 3.8-2, and 3.8-3 list the datasets used or created by procedure L\_VIBRAT\_2, the procedures invoked by procedure L\_VIBRAT\_2, and the processors invoked by procedure L\_VIBRAT\_2, respectively.

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Table 3.8-1 Datasets Input/Output by procedure L_VIBRAT_2				
Dataset	Description	Input	Output	
AMAPic2.isize	Factorization Map for INV		$\checkmark$	
CEM.SPAR	Consistent Mass Matrix		$\checkmark$	
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	$\checkmark$	$\checkmark$	
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$	
DEF. <es_name>.0.nnod</es_name>	Element Defn. (Connectivity)	$\checkmark$		
DEM.DIAG	Diagonal (Lumped) Mass Matrix		$\checkmark$	
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	$\checkmark$		
INV.KSHF.j <sup>†</sup>	Factored Shifted System Matrix		$\checkmark$	
INV. <kname>.j<sup>†</sup></kname>	Factored System Matrix		$\checkmark$	
JDF1.BTAB.1.8	Model Summary	$\checkmark$		
KG.SPAR.jdf2	Assembled geometric stiffness matrix		$\checkmark$	
KMAPic2.isize	Model Connectivity Map		$\checkmark$	
<kname>.SPAR.jdf2</kname>	Assembled system matrix		$\checkmark$	
<b>VIBR.EVAL.1</b> . $j^{\dagger}$	Vibration eigenvalues		$\checkmark$	
VIBR.MODE.1. <i>j</i> <sup>†</sup>	Vibration eigenvalues		$\checkmark$	

 $\dagger j = \langle vcon_set \rangle$ 

Table 3.8-2         Sub-Procedures Invoked by procedure L_VIBRAT_2			
Procedure	Туре	Function	
ES	External	Element utility procedure	
FACTOR	External	Factors assembled stiffness matrix	
L_STATIC	Internal	Static solution procedure	
L_VIBRAT_2	Internal	Main procedure	

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Table 3.8-3 Processors Invoked by Procedure L_VIBRAT_2		
Procedure	Type	Function
AUS	Internal	Arithmetic utilities
E	Internal	Initializes EFIL datasets
EIG2	Internal	Solve eigenvalue problem using subspace iteration
ESi	External	Element processors based on GEP
К	Internal	Assemble system matrix
LAN	External	Solve eigenvalue problem using Lanczos method
LANZ	External	Solve eigenvalue problem using Lanczos method
RSEQ	Internal	Resequences nodes for equation solving
торо	Internal	Generates nodal topology maps
VPRT	Internal	Print SYSVEC system vectors

### **3.8.5 ARGUMENT DESCRIPTION**

### 3.8.5.1 <u>CONS\_SET</u>

Constraint set number for prestress solution (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

### 3.8.5.2 DIRECTION

Direction for the element stress (stress resultant) output (default: 0). The element stress coordinate system will be used if direction=0. The material axes  $(x_m, y_m, z_m)$  will be used if direction=1; the material axes  $(y_m, z_m, x_m)$  will be used for direction=2; and the material axes  $(z_m, x_m, y_m)$  will be used for direction=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 3.4-2).

### 3.8.5.3 ERROR\_TOL

Convergence criterion for eigenvalues (default: 0.0001). For the k-th iteration, the error measure for the *i*-th eigenvalue is

$$\boldsymbol{\epsilon}_{i}^{k} = \frac{\|(\lambda_{i}^{k} - \lambda_{i}^{k-1})\|}{\|\lambda_{i}^{k}\|}$$

The *i*-th eigenvalue is converged if  $\epsilon_i^k$  is smaller than ERROR\_TOL.

## 3.8.5.4 FUNCTION

Select function to be performed by procedure L\_VIBRAT\_2 (default: ALL). This procedure may be used to perform four functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, the displacement solution is obtained, optionally element stresses (stress resultants) and internal nodal forces (reactions) computed and the eigenproblem is solved. For FUNCTION=FACT\_SOLV, procedure L\_VIBRAT\_2 assumes that the system stiffness matrix has previously been assembled and that nodal resequencing has been performed. The procedure then proceeds to factor the system stiffness matrix, solves for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FUNCTION=SOLV, procedure L\_VIBRAT\_2 assumes that the system stiffness has previously been formed and factored. The procedure then proceeds to solve for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FUNCTION=EIGEN, procedure L\_VIBRAT\_2 uses a previously computed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

# 3.8.5.5 INIT\_VECTOR

Number of initial vectors used to span the subspace (default: 0). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT\_VECTOR=0, the number of initial vectors will be calculated by the procedure as

INIT\_VECTOR=MINIMUM (2\*N\_MODES, N\_modes + 8)

### 3.8.5.6 ISEQ

Resequencing method to be used (default: -1). If the argument RENUMBER is  $\langle true \rangle$ , then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (*i.e.*, method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.8-1).

# 3.8.5.7 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

### 3.8.5.8 LDI

Logical device index (default: 1).

# 3.8.5.9 LOAD\_SET

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

### 3.8.5.10 <u>MASS\_TYPE</u>

Type of mass matrix (default: CONSISTENT). If MASS\_TYPE=CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS\_TYPE=DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

#### 3.8.5.11 <u>MAX\_ITERS</u>

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

#### 3.8.5.12 <u>N\_MODES</u>

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR\_TOL.

#### 3.8.5.13 PRINT

Flag to print modeshapes (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the vibration modeshapes.

#### 3.8.5.14 REACTION

Flag to compute the internal nodal forces (default: <true>) If the argument REAC-TION=<true>, then the internal forces will be computed by calling procedure INT\_FORC (see Section 6.2).

#### 3.8.5.15 <u>RENUMBER</u>

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

### 3.8.5.16 SHIFT

Eigenvalue shift (default: 0.0). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared (*i.e.*,  $\omega^2$ ) for vibration problems.

#### 3.8.5.17 STRESS

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION, respectively, by calling procedure STRESS (see Section 6.4).

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#### 3.8.5.18 <u>VCON\_SET</u>

Constraint set number for vibration analysis (default: 1). This argument selects which constraint set to use in solving the linear vibration problem.

### 3.8.6 PROCEDURE FLOWCHART

L_VIBRAT_2	(main procedure)
L_STATIC	(linear static analysis procedure)
ES	(initialize, form K and M)
FACTOR	(factor assembled stiffness matrix)
SOLVE	(solve linear system of equations)
STRESS	(stress/strain recovery procedure)
ES	(calculate element and nodal stress/strain)
INT_FORCE	(internal force procedure)
ES	(internal force calculation)
ES	(form $\mathbf{K}_{g}$ )
FACTOR	(factor using vibration boundary conditions)

# 3.8.7 LIMITATIONS

None.

# **3.8.8 ERROR MESSAGES AND WARNINGS**

None.

### 3.8.9 USAGE GUIDELINES AND EXAMPLES

Procedure L\_VIBRAT\_2 may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call L_VIBRAT_2 ( FUNCTION = ALL ; -- . Select function
        VCON_SET = 1 ; -- . Select vibration constraint set
        ERROR_TOL = .0001 ; -- . Eigenvalue convergence criterion
        INIT_VECTOR = 0 ; -- . Number of initial vectors
        ISEQ = -1 ; -- . Select resequencing method
```

KNAME K ; -- . First word of stiffness matrix -- . dataset name  $MAX_ITERS = 20;$ -- Maximum number of iterations N\_MODES 1; -- Number of eigenvalues = CONS\_SET = 1 ; -- . Select constraint set DIRECTION = 0: -- . Select direction for element stresses ; -- . Select load set LOAD\_SET = 1 <false> ; -- . REACTIONS flag REACTION = STRESS Ŧ <false> -- . STRESS flag PRINT = <true> ; -- . PRINT flag RENUMBER \* <true> ; -- . RESEQUENCING flag SHIFT Ŧ 0.0 ; Eigenvalue shift

Before procedure L\_VIBRAT\_2 is called, the global macrosymbol eigensolver\_name should be defined as described in Section 3.8-3; otherwise, the default value of EIG2 will be used.

#### **3.8.10 PROCEDURE LISTING**

#### **3.8.11 REFERENCES**

- 3.8-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 3.8-2 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
- 3.8-3 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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# 3.9 Procedure NL\_STATIC\_1

#### 3.9.1 GENERAL DESCRIPTION

Procedure NL\_STATIC\_1, written by G. M. Stanley of Lockheed Palo Alto Research Laboratory, performs nonlinear static analysis based on a modified Newton/Raphson incremental strategy for automatic load-step control (e.g., ref. 3.1). Procedure NL\_STATIC\_1 relies on the Generic Element Processor (*i.e.*, structural element processors, ESi) and hence has a corotational option for geometric nonlinearity that enables arbitrarily large rotations.

Procedure NL\_STATIC\_1 solves a nonlinear algebraic equation system of the form:

$$\mathbf{f}^{int}(\mathbf{d}) = \mathbf{f}^{ext}(\lambda) \qquad (3.9-1)$$

where  $f^{int}$  is the nonlinear internal force vector for the discrete (*i.e.*, finite element) system,  $f^{ext}$  is the external force vector, d is the displacement vector, and  $\lambda$  is a load factor. The basic modified Newton/Raphson procedure solves this system of equations by linearizing it at each load level (*i.e.*, fixed  $\lambda$ ), leading to the solution of the following linear equations:

within an iteration loop where n+1 is the current (fixed) load-step number, i+1 is the iteration number at that load-step,  $\delta d$  is the iterative displacement change, and  $\mathbf{r} = \mathbf{f}^{ext} - \mathbf{f}^{int}$ is the nonlinear residual force vector. K is the effective tangent stiffness matrix, which is updated only at the first iteration of selected load steps (though typically at every step). Iteration is continued until the inner product of  $\delta d$  and  $\mathbf{r}$  become smaller than a user-specified error tolerance.

An arc-length constraint is added to the above equations so that i) the user doesn't have to select the load increment  $(\Delta \lambda = \lambda_{n+1} - \lambda_n)$ , and ii) the solution algorithm can automatically traverse limit points – maxima and minima in the load-displacement "curve". The user need only specify the initial load factor,  $\lambda_1$ ; the constraint equation converts this to an "arc-length" increment in load-displacement space, and adaptively adjusts this increment based on the iterative performance of the algorithm. Details of this algorithm are given in the theory and algorithm sections.

#### 3.9.2 THEORY

#### 3.9.2.1 Introduction

Procedure NL\_STATIC\_1 performs a quasi-static analysis of a system of nonlinear equilibrium equations using an adaptive arc-length-controlled Newton/Raphson incremental/iterative solution algorithm. The arc-length method adopted here is based on a variant

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of Crisfield's algorithm (ref. 3.1), where instead of using a nonlinear (quadratic) arclength constraint equation in conjunction with the linearized equilibrium equations, the constraint equation is consistently linearized as well. This eliminates the pitfalls associated with quadratic root selection in Crisfield's algorithm. By combining this modification with i) polynomial extrapolation of converged solutions to obtain step-predictor solutions, ii) an energy error norm that properly weights translational and rotational freedoms, and iii) generalization to large rotations, specified displacements and live loads; the present algorithm is both more general and more robust than the basic algorithm. Additional enhancements to overcome hard singularities at limit and bifurcation points are currently under development; and will be incorporated as procedures at a later date.

### NOTATION

d	Displacement vector.
δd	Iterative change in d.
$\Delta \mathbf{d}$	Incremental (load-step) change in d.
$\mathbf{d}_n^i$	Displacement vector at iteration $i$ of step $n$ .
$\Delta \mathbf{d}_n^i$	Incremental (step) change in d. $\Delta d_{n+1}^{(i+1)} = d_{n+1}^{(i)} - d_n$
δd	Tangential displacement = $\mathbf{K}^{-1} \mathbf{\hat{f}}^{ext}$
$\Delta \ell$	Incremental arc-length (step) parameter.
$\hat{\mathbf{f}}^{ext}$	External force vector – base load.
f <sup>int</sup>	Internal force vector.
r	Residual force vector.
К	Stiffness matrix.
$\delta \overline{\mathbf{d}}$	Basic (fixed-load) iterative change in d.
$\delta \mathbf{d}^*$	Linear combination of $\delta \overline{\mathbf{d}}$ and $\delta \widehat{\mathbf{d}}$ .
num_cuts	Number of times load step has been cut in half at current step.
num_div	Number of consecutive iterations at which divergence occurs.
Cn	Extrapolation coefficient corresponding to step $n$ .
ê	Relative error in energy norm.
ε	Absolute error in energy norm.
Eref	Reference value of $\epsilon$ ; initialized as zero.
€ <sub>tol</sub>	Relative error tolerance (default: $10^{-4}$ ).
λ	Load factor.
$\Delta\lambda$	Incremental (load-step) change in $\lambda$ .
K",	Stiffness submatrix coupling specified (s) displacement components with force components corresponding to unknown (u) displacements.
<b>d</b>	Base value of specified displacement vector.
ď	Current value of specified displacement vector. $\mathbf{d}^s = \lambda  \widehat{\mathbf{d}}^s$ .

### 3.9.2.2 Nonlinear Equations

The set of nonlinear equations solved by the present algorithm consist of: i) the system of equilibrium equations for the discrete (finite element) model, and ii) a single constraint equation governing the maximum "arc-length" to be traversed in a single solution increment along a curve in load-displacement space. These equations may be expressed as follows:

$$\mathbf{r}(\mathbf{d},\lambda) = 0$$
(Equilibrium) $c(\mathbf{d},\lambda) = 0$ (Arc-length Constraint)

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where d is the displacement vector representing all of the degrees-of-freedom (DOFs) for the discrete model, and  $\lambda$  is an external load parameter. In conventional load- or displacement-controlled solution algorithms,  $\lambda$  is usually specified by the user. In an arc-length controlled algorithm like the present one,  $\lambda$  is treated as an additional unknown. Thus, there are just as many independent equations in equation 3.9-3 as there are unknowns. The vector r represents the *residual* (or out-of-balance) force vector, which is identically zero at equilibrium.

For the special case of:

- Displacement-independent loading
- Proportional (one-parameter) force loading
- Load-independent arc-length constraint

 $\mathbf{r}$  and c take on the following form:

$$\mathbf{r}(\mathbf{d},\lambda) = \lambda \, \mathbf{\hat{f}}^{ext} - \mathbf{f}^{int}(\mathbf{d}) c(\mathbf{d},\lambda) = \|\Delta \mathbf{d}\|^2 - \Delta \ell^2$$
(3.9-4)

where  $\hat{\mathbf{f}}^{ext}$  is a normalized (base-value) external load vector,  $\mathbf{f}^{int}$  is the nonlinear internal force vector,  $\Delta \mathbf{d}$  is an incremental displacement vector, defined as

$$\Delta \mathbf{d} = \mathbf{d} - \mathbf{d}_n \qquad (3.9-5)$$

in which  $d_n$  is the known displacement vector at a nearby (previous) configuration, and  $\Delta \ell$  is a prescribed arc-length parameter defining the size of the increment.

The problem statement then is to solve equation 3.9-3 for a statically connected set of configurations,  $(\mathbf{d}, \lambda)$ , representing the load-displacement "history" of the structural model. Note that due to the nonlinear nature of the equations, this history is not always unique. For example, at pure bifurcation points, the present algorithm cannot determine the correct path, unless some sort of imperfection or "trigger" is introduced by the user – thus converting the bifurcation point into a limit point. Limit points (*i.e.*, local maximums and minimums in the load-displacement curve) cause no difficulty for the present algorithm – except when a load-step happens to lie "too close" to the actual limit point (see procedure NL\_STATIC-2 for a solution to this rare but frustrating problem).

### 3.9.2.3 Linearized Equations

To solve the above nonlinear equations, we use the modified Newton/Raphson algorithm, which requires their linearization -i.e., first-order Taylor series expansion of the simultaneous equations. The solution to the linearized equations is then used to update the nonlinear solution in an iterative process that continues until convergence has been obtained at a given configuration. Furthermore, the final configuration is typically obtained as a series of *steps*, or increments, with a new iteration cycle occuring within each step; and with information from preceding steps used to predict a starting solution at the new step. (This is

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commonly called an "incremental/iterative" algorithm.) Note that the *iterative* changes in displacement and load-factor, which we shall denote  $\delta d$  and  $\delta \lambda$ , respectively, are different than the *incremental* changes, denoted by  $\Delta d$  and  $\Delta \lambda$ . The incremental load/displacement changes are used to advance from one converged solution  $(d_n, \lambda_n)$  to another  $(d_{n+1}, \lambda_{n+1})$ , while the iterative changes all refer to successive approximations  $(d_{n+1}^{(i)}, \lambda_{n+1}^{(i)})$  of the same target configuration  $(d_{n+1}, \lambda_{n+1})$ . Thus,  $\delta d$  converges to zero at a given configuration, while  $\Delta d$  converges to a value dictated by the arc-length constraint equation 3.9-4b\*

Linearization of equations 3.9-4 about a reference configuration  $(\overline{\mathbf{d}}, \overline{\lambda})$  results in the following expressions:

$$\mathbf{r}(\mathbf{d},\lambda) \approx \mathbf{r}(\overline{\mathbf{d}},\overline{\lambda}) + \frac{\partial \mathbf{r}}{\partial \mathbf{d}}(\overline{\mathbf{d}},\overline{\lambda})\delta \mathbf{d} + \frac{\partial \mathbf{r}}{\partial \lambda}(\overline{\mathbf{d}},\overline{\lambda})\delta\lambda = 0$$
  

$$\mathbf{c}(\mathbf{d},\lambda) \approx \mathbf{c}(\overline{\mathbf{d}},\overline{\lambda}) + \frac{\partial \mathbf{c}}{\partial \mathbf{d}}(\overline{\mathbf{d}},\overline{\lambda})\delta \mathbf{d} + \frac{\partial \mathbf{c}}{\partial \lambda}(\overline{\mathbf{d}},\overline{\lambda})\delta\lambda = 0$$
(3.9-6)

where for the special assumptions listed in Section 3.9.9.1, the partial derivatives in equation 3.9-6 become:

$$\frac{\partial \mathbf{r}}{\partial \mathbf{d}}(\overline{\mathbf{d}},\overline{\lambda}) = -\mathbf{K}(\overline{\mathbf{d}}), \qquad \frac{\partial \mathbf{r}}{\partial \lambda}(\overline{\mathbf{d}},\overline{\lambda}) = \widehat{\mathbf{f}}^{ezt} 
\frac{\partial c}{\partial \mathbf{d}}(\overline{\mathbf{d}},\overline{\lambda}) = 2\Delta\overline{\mathbf{d}}, \qquad \frac{\partial c}{\partial \lambda}(\overline{\mathbf{d}},\overline{\lambda}) = 0$$
(3.9-7)

where  $\mathbf{K} = \partial \mathbf{f}^{int} / \partial \mathbf{d}$  is the tangent stiffness matrix. Substituting equation 3.9-7 into equation 3.9-6 leads to the simultaneous linear equations:

$$\overline{\mathbf{K}}\,\delta\mathbf{d} = \overline{\mathbf{r}} + \delta\lambda\,\widehat{\mathbf{f}}^{ext}$$

$$2\,\Delta\overline{\mathbf{d}}\cdot\delta\mathbf{d} = \overline{c}$$
(3.9-8)

where

$$\overline{\mathbf{r}} = \mathbf{r}(\overline{\mathbf{d}},\overline{\lambda}), \quad \overline{\mathbf{c}} = \mathbf{c}(\overline{\mathbf{d}},\overline{\lambda}), \quad \overline{\mathbf{K}} = \begin{cases} \mathbf{K}(\overline{\mathbf{d}}) \text{ for True Newton} \\ \mathbf{K}(\mathbf{d}_n) \text{ for Modified Newton} \end{cases}$$
 (3.9-9)

Solving the first of equations 3.9-8 for  $\delta d$  leads to

$$\delta \mathbf{d} = \overline{\mathbf{K}}^{-1} \left[ \overline{\mathbf{r}} + \widehat{\mathbf{f}}^{ezt} \delta \lambda \right] = \delta \overline{\mathbf{d}} + \delta \widehat{\mathbf{d}} \delta \lambda \qquad (3.9 - 10)$$

where

$$\begin{aligned}
\delta \overline{\mathbf{d}} &= \overline{\mathbf{K}}^{-1} \overline{\mathbf{r}} \\
\delta \widehat{\mathbf{d}} &= \overline{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{ext}
\end{aligned}$$
(3.9-11)

\* The reason for using a series of increments, instead of solving for the final solution in one single increment, is that the Newton/Raphson method converges only if the starting solution is sufficiently "close" to the final solution.

Similarly, we can solve for  $\delta\lambda$ , by substituting equation 3.9-10 into equation 3.9-8b, *i.e.*,

$$\overline{c} + 2\Delta \overline{d} \cdot \delta \overline{d} + 2(\Delta \overline{d} \cdot \delta \widehat{d})\delta \lambda = 0$$
 (3.9-12)

which yields

$$\delta\lambda = \frac{-\overline{c} - 2\Delta\overline{d} \cdot \delta\overline{d}}{2\Delta\overline{d} \cdot \delta\widehat{d}} = \frac{\Delta\ell^2 - \|\Delta\overline{d}\|^2 - 2\Delta\overline{d} \cdot \delta\overline{d}}{2\Delta\overline{d} \cdot \delta\widehat{d}}$$
(3.9-13)

#### 3.9.2.4 Update Procedure

The solution update procedure – from one iteration to the next at a fixed arc-length increment from a converged solution – consists of the following two (sequential) equations:

1) 
$$\delta \lambda = \frac{\Delta \ell^2 - 2\Delta \overline{d} - \|\Delta \overline{d}\|^2}{2\Delta \overline{d} \cdot \delta \widehat{d}}$$
  
2)  $\delta d = \delta \overline{d} + \delta \widehat{d} \delta \lambda$ 
(3.9-14)

where  $\delta \overline{\mathbf{d}}$  and  $\delta \widehat{\mathbf{d}}$  are first computed using equation 3.9-11, and  $\Delta \overline{\mathbf{d}}$  is the displacement increment from the previous converged solution to the previous iterate of the current solution, *i.e.*,  $\overline{\mathbf{d}} - \mathbf{d}_n$ .

Then we simply apply the update formulas:

$$\mathbf{d} = \mathbf{d} + \delta \mathbf{d}$$

$$\lambda = \overline{\lambda} + \delta \lambda$$

$$(3.9 - 15)$$

where special consideration must be given to equation 3.9-15a in the case of problems with large-rotational degrees-of-freedom (see Section 3.9.2.10).

#### 3.9.2.5 Predictor Solutions; arc-length-Constraint and Extrapolation Techniques

To obtain a prediction for  $d_{n+1}$  and  $\lambda_{n+1}$  at the beginning of step n+1 (so that the Newton iterations may occur within a sufficiently small neighborhood of the converged solution), we use one of the following two procedures:

1) The arc-length constraint equation 3.9-4b

or

2) Quadratic extrapolation of a series of converged solutions

The first approach (arc-length constraint) leads to the following predictor equations:

$$d_{n+1}^{(1)} = d_n + \underbrace{\Delta \lambda_{n+1}^{(1)} \delta \widehat{d}_{n+1}}_{\Delta d_{n+1}^{(1)}}$$

$$\lambda_{n+1}^{(1)} = \lambda_n \pm \underbrace{\frac{\Delta \ell_{n+1}}{\|\delta \widehat{d}_{n+1}\|}}_{\Delta \lambda_{n+1}^{(1)}}$$
(3.9-16)

where the sign in front of  $\Delta\lambda$  in equation 3.9-16b is taken as the sign of the determinant of  $\overline{\mathbf{K}}$ . Equation 3.9-16a was obtained by noting that

$$\Delta \mathbf{d}_{n+1}^{(1)} = \delta \mathbf{d}_{n+1}^{(1)} \qquad (3.9-17)$$

which from equation 3.9-10 can be written as

$$\delta \mathbf{d}_{n+1}^{(1)} = \delta \overline{\mathbf{d}}_{n+1}^{(1)} + \delta \lambda_{n+1}^{(1)} \, \delta \widehat{\mathbf{d}}_{n+1} = \Delta \lambda_{n+1}^{(1)} \, \delta \widehat{\mathbf{d}}_{n+1} \tag{3.9-18}$$

since

$$\delta \overline{\mathbf{d}}_{n+1}^{(1)} = \overline{\mathbf{K}}^{-1} \mathbf{r}_n = \overline{\mathbf{K}}^{-1} \mathbf{0} = \mathbf{0} \qquad (3.9 - 19)$$

and

$$\delta \lambda_{n+1}^{(1)} = \Delta \lambda_{n+1}^{(1)} \qquad (3.9-20)$$

Then, equation 3.9-16b follows by substituting equation 3.9-16a into the arc-length constraint equation

$$\|\Delta \mathbf{d}_{n+1}^{(1)}\| = \Delta \ell \qquad (3.9-21)$$

The second approach (quadratic extrapolation) leads to the following predictor equations:

$$\mathbf{d}_{n+1}^{(1)} = c_n \mathbf{d}_n + c_{n-1} \mathbf{d}_{n-1} + c_{n-2} \mathbf{d}_{n-2} \lambda_{n+1}^{(1)} = c_n \lambda_n + c_{n-1} \lambda_{n-1} + c_{n-2} \lambda_{n-2}$$

$$(3.9-22)$$

where  $(\mathbf{d}_n, \lambda_n)$ ,  $(\mathbf{d}_{n-1}, \lambda_{n-1})$ , and  $(\mathbf{d}_{n-2}, \lambda_{n-2})$  are the converged solutions at the three previous (consecutive) load steps, and the  $c_i$  are the quadratic Lagrange interpolation functions:

$$c_{n} = \frac{(\ell_{n+1} - \ell_{n-2})(\ell_{n+1} - \ell_{n-1})}{(\ell_{n} - \ell_{n-2})(\ell_{n} - \ell_{n-1})}$$

$$c_{n-1} = \frac{(\ell_{n+1} - \ell_{n-2})(\ell_{n+1} - \ell_{n})}{(\ell_{n-1} - \ell_{n-2})(\ell_{n-1} - \ell_{n})}$$

$$c_{n-2} = \frac{(\ell_{n+1} - \ell_{n-1})(\ell_{n+1} - \ell_{n})}{(\ell_{n-2} - \ell_{n-1})(\ell_{n-2} - \ell_{n})}$$
(3.9 - 23)

The arc-length parameter,  $\ell$ , is computed by arbitrarily setting  $\ell_{n-2} = 0$ , and accumulating the incremental parameters,  $\Delta \ell$ . Thus,

$$\ell_{n-2} = 0 
\ell_{n-1} = \Delta \ell_{n-1} 
\ell_n = \ell_{n-1} + \Delta \ell_n 
\ell_{n+1} = \ell_n + \Delta \ell_{n+1}$$
(3.9-24)

where the arc-length increments,  $\Delta \ell_{n-2}$ ,  $\Delta \ell_{n-1}$ ,  $\Delta \ell_n$ , and  $\Delta \ell_{n+1}$  are defined by the adaptive algorithm described in Section 3.9.2.6.

Note that unlike the arc-length-based predictor equations 3.9-16, the above extrapolation formulas do not require any additional information to determine the direction (*i.e.*, sign) of the load increment. This is because the curvature of the quadratic polynomial used for extrapolation automatically senses, and enables the traversal of, turning points in the solution path.

Quadratic extrapolation is usually much more efficient than the arc-length constraint approach for computing the predictor solutions. In some cases, extrapolation can reduce the number of load steps by up to an order of magnitude. However, in other cases – e.g., around very sharp turns in load-displacement space – quadratic extrapolation may be too *smooth* to capture the sudden changes. In such cases, small, arc-length-controlled predictor steps may be the most practical strategy for getting through the critical phases. (Adaptive algorithms for selectively switching between extrapolation and arc-length step predictors are recommended as a topic for future research.)

#### 3.9.2.6 Adaptive Load-Step (arc-length) Selection

To advance the solution from one load-step (n) to the next (n+1), it is also necessary to select a new arc-length increment,  $\Delta \ell_{n+1}$ . Note that this parameter, which represents a distance traversed along the load-displacement "curve", is (by definition) always positive,\* but may grow or shrink depending on solution difficulty. To automate the process, we use the following simple, but fairly robust, heuristic algorithm suggested by Crisfield (ref. 3.1):

$$\Delta \ell_{n+1} = \frac{\text{Desired number of iterations}}{\text{Actual number of iterations}} \times \Delta \ell_n \qquad (3.9-25)$$

where actual refers to the number of iterations required for convergence at the previous step (n), and the *desired* number of iterations is user-specified and typically around 4. This causes the step-size to grow or shrink in direct proportion to the convergence rate of the nonlinear solution, and generally leads to a nearly constant number of iterations (*i.e.*, computations) per step. In fact the number of load-steps will automatically adjust according to the curvature of the load-displacement curve, with more steps being required around turning points (high curvature) and less along smooth stretches (low curvature).

<sup>\*</sup> This is in contrast to conventional load-controlled algorithms, which require explicit selection of the load increment, – a parameter that may change sign at limit or bifurcation points.

#### Solution Procedures

Note that the initial value of the arc-length increment,  $\Delta \ell_1$ , must be specified – at least indirectly – by the user. However, since the user typically has no physical insight about the magnitude of  $\Delta \ell_1$ , we employ the arc-length constraint equation 3.9-10 to compute it in terms of the initial load-factor,  $\Delta \lambda_1$  – which the user can typically estimate based on some prior linear analysis. The expression used to compute the initial arc-length increment is thus

$$\Delta \ell_1 = \lambda_1 \|\delta \widehat{\mathbf{d}}_1\| \qquad (3.9-26)$$

which was derived by rewriting equation 3.9-16b as

$$\Delta \ell_{n+1} = \Delta \lambda_{n+1} \| \delta \mathbf{d}_{n+1} \| \qquad (3.9-27)$$

setting n = 0 and noting that

$$\Delta \lambda_1 = \lambda_1 - \lambda_0 = \lambda_1 \qquad (3.9 - 28)$$

The "tangential" displacement,  $\delta \hat{d}_1$ , in equation 3.9-26 is simply the linear solution obtained with the normalized external load vector as right-hand-side, *i.e.*,

$$\delta \widehat{\mathbf{d}}_1 = \mathbf{K}^{-1}(\mathbf{0}) \widehat{\mathbf{f}}^{e^{zt}} \qquad (3.9-29)$$

#### 3.9.2.7 Specified Displacements

The presence of specified-displacement loads (in addition to specified-force loads) affects the above algorithm in three subtle – but important – ways:

- i) It modifies the definition of the residual force vector, **r**, since the *internal* force vector,  $\mathbf{f}^{int}$ , becomes a function of the load-factor,  $\lambda$ .
- ii) Due to the above dependence, the derivative of **r** with respect to  $\lambda$  gains an additional term, which in turn modifies the definition of the tangential displacement vector,  $\delta \hat{\mathbf{d}}$ .
- iii) The specified displacement components must be included in all displacement norms and inner products appearing in the arc-length constraint equation, and in the computation of nonlinear error estimates.

The above modifications can be expressed mathematically as follows. First, define a specified displacement vector,  $d^s$ , which has zeros everywhere except in the components that are user-specified. Further assume that this specified displacement vector is scaled by the same load-factor,  $\lambda$ , as the external force vector, *i.e.*,

$$\mathbf{d}^{\mathbf{s}} = \lambda \, \widehat{\mathbf{d}}^{\mathbf{s}} \tag{3.9-30}$$

where  $\widehat{\mathbf{d}}^{\bullet}$  is a normalized vector containing the reference ( $\lambda = 1$ ) values of specified displacement. The expression for the residual force vector, equation 3.9-4, can then be re-written as

$$\mathbf{r}(\mathbf{d},\lambda) = \lambda \, \widehat{\mathbf{f}}^{ext} - \mathbf{f}^{int}(\mathbf{d},\mathbf{d}^s) \qquad (3.9-31)$$

and its derivative with respect to  $\lambda$  in equation 3.9-7 becomes

$$\frac{\partial \mathbf{r}}{\partial \lambda} = \hat{\mathbf{f}}^{ext} - \frac{\partial \mathbf{f}^{int}}{\partial \mathbf{d}^s} \frac{\partial \mathbf{d}^s}{\partial \lambda} = \hat{\mathbf{f}}^{ext} - \frac{\partial \mathbf{f}^{int}}{\partial \mathbf{d}^s} \hat{\mathbf{d}}^s \qquad (3.9 - 32)$$

But:

$$\frac{\partial \mathbf{f}^{int}}{\partial \mathbf{d}^s} = \mathbf{K}^{us} \tag{3.9-33}$$

where  $K^{us}$  is the partition of the tangent stiffness matrix that couples specified displacement increments to unknown force increments, *i.e.*, the *extended* stiffness matrix may be partitioned as

$$\mathbf{K}^* = \begin{bmatrix} \mathbf{K}^{uu} & \mathbf{K}^{us} \\ \mathbf{K}^{su} & \mathbf{K}^{ss} \end{bmatrix}$$
(3.9 - 34)

where  $K^{uu}$  is the active block of the stiffness matrix, *i.e.*, in the present terminology:

$$\mathbf{K} = \mathbf{K}^{uu} \qquad (3.9 - 35)$$

Thus, the new load-derivative of the residual force vector may be expressed as

$$\frac{\partial \mathbf{r}}{\partial \lambda} = \mathbf{\hat{f}}^{ext} - \mathbf{K}^{us} \mathbf{\hat{d}}^{s}$$
(3.9 - 36)

and the corresponding tangential displacement vector from equation 3.9-11b becomes:

$$\delta \widehat{\mathbf{d}} = \overline{\mathbf{K}}^{-1} \left( \widehat{\mathbf{f}}^{ext} - \overline{\mathbf{K}}^{us} \widehat{\mathbf{d}}^{s} \right)$$
(3.9 - 37)

where the superposed bar is defined in equation 3.9-9.

Note that the solution indicated in equation 3.9-37 is much like what is required for linear analysis with specified displacements: The right-hand-side is modified by multiplying a part of the extended stiffness matrix times the (normalized) specified displacements. This is in contrast to the solution for  $\delta \overline{d}$  in equation 3.9-11a, where specified displacements are accounted for exclusively through their nonlinear dependence in the residual force vector,  $\overline{r}$ .

#### 3.9.2.8 General Loading (e.g., "Live" Loads)

The last restriction we shall lift is the simple form of the external force vector given in equation 3.9-4a, *i.e.*, we shall replace:

$$\mathbf{f}^{ext} = \lambda \, \widehat{\mathbf{f}}^{ext} \tag{3.9-38}$$

by

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$$\mathbf{f}^{ext} = \lambda \, \widehat{\mathbf{f}}^{ext}(\mathbf{d}) \qquad (3.9-39)$$

This allows for the kind of displacement-dependent (or "live") loading that arises from hydrostatic, or follower, forces. The residual force vector then becomes

$$\mathbf{r}(\mathbf{d},\lambda) = \lambda \, \widehat{\mathbf{f}}^{ext}(\mathbf{d}) - \, \mathbf{f}^{int}(\mathbf{d},\lambda \, \widehat{\mathbf{d}}^{\prime}) \qquad (3.9-40)$$

and the only modifications to equations 3.9-7 are that i) the tangent stiffness matrix acquires a load-stiffness contribution, *i.e.*,

$$\frac{\partial \mathbf{r}}{\partial \mathbf{d}} = -\mathbf{K} = -(\mathbf{K}^{matl} + \mathbf{K}^{geom} + \mathbf{K}^{load}) \qquad (3.9-41)$$

where

$$\mathbf{K}^{load} = -\frac{\partial \mathbf{f}^{ext}}{\partial \mathbf{d}} \qquad (3.9-42)$$

and ii) the external-force contribution to the tangent load vector,  $\mathbf{r}_{,\lambda}$ , is no longer a constant, *i.e.*,

$$\frac{\partial \mathbf{r}}{\partial \lambda} = \mathbf{\hat{f}}^{ext}(\mathbf{d}) - \mathbf{K}^{us}(\mathbf{d}) \mathbf{\hat{d}}^{s}$$
(3.9-43)

Note that we have not allowed for a general external-load history, in which both the magnitude and direction of the external force vector may change from step to step, e.g.,

$$\mathbf{f}^{ext} = \mathbf{f}^{ext}(\mathbf{d}, \lambda) \tag{3.9-44}$$

Nor have we allowed for multiple load-factors,  $\lambda_a$ ,  $\lambda_b$ , ..., which can arise when several independent load systems are acting on a structure. Such complications require straightfoward generalization of the present arc-length algorithm, and will be considered as necessary for future applications.

#### 3.9.2.9 Convergence Criteria

As a measure of the error in the nonlinear equilibrium equations (not including discretization errors), we use an *energy norm*, which is the inner product of the residual force vector and the iterative displacement-change vector. This is effective for two reasons: i) it involves only a single error norm, in contrast to algorithms that check displacement and residual errors independently; and ii) the inner product of force and displacement introduces a natural scaling of different types of generalized freedoms (for example rotational freedoms versus translational freedoms) – by weighting each generalized displacement with its corresponding (conjugate) generalized force. Thus, sensitivity to physical units and choice of independent variables is minimized.

Convergence of the nonlinear solution process at a given load-step, n + 1, is checked by evaluating the following energy error norm at each iteration, *i*:

$$\|\operatorname{error}\|_{n+1}^{(i)} = \sqrt{\mathbf{r}_{n+1}^{(i)} \cdot \delta \mathbf{d}_{n+1}^{(i)}}$$
 (3.9-45)

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and comparing it with some user-specified fraction of a *reference* error norm. Thus, convergence is defined as satisfaction of the condition:

$$\|\operatorname{error}\|_{n+1}^{(i)} \leq \operatorname{tolerance} \times \|\operatorname{error}\|_{n+1}^{ref} \qquad (3.9-46)$$

where tolerance is the user-specified fraction, and the reference error is defined as:

$$\|\operatorname{error}\|_{n+1}^{ref} = \operatorname{MAX}(\|\operatorname{error}\|_{n+1}^{(1)}, \|\operatorname{error}\|_{n}^{ref})$$
 (3.9-47)

Note that at the first load-step,  $\|error\|_0^{ref}$  is assumed to be zero.

The above convergence criterion can be very sensitive to the user-specified error tolerance. Typically, a value of  $10^{-3}$  is adequate, but for some problems this may be an order of magnitude too large – or even too small (*i.e.*, causing more iterations than are actually needed). More adaptive and robust error tolerances are a recommended topic for future research.

### 3.9.2.10 Large Rotations

In problems involving rotational freedoms, e.g., with beam or shell elements, the following modification to equation 3.9-15a is used when the rotation angles become large (say greater than 10 degrees). First, note that the system displacement vector, and its iterative change, are typically partitioned by nodes, *i.e.*,

$$\mathbf{d} = \begin{cases} \mathbf{d}_1 \\ \mathbf{d}_2 \\ \vdots \\ \mathbf{d}_{\text{Nnodes}} \end{cases}, \quad \delta \mathbf{d} = \begin{cases} \delta \mathbf{d}_1 \\ \delta \mathbf{d}_2 \\ \vdots \\ \delta \mathbf{d}_{\text{Nnodes}} \end{cases}$$
(3.9-48)

where Nnodes is the total number of nodes in the problem. At nodes with both translational and rotational freedoms we can further partition:

$$\mathbf{d}_{A} = \left\{ \begin{array}{c} \mathbf{u}_{A} \\ \mathbf{T}_{A} \end{array} \right\}, \qquad \delta \mathbf{d}_{A} = \left\{ \begin{array}{c} \delta \mathbf{u}_{A} \\ \delta \boldsymbol{\theta}_{A} \end{array} \right\}$$
(3.9-49)

in which

 $\mathbf{u}_{\mathbf{A}} =$ translation at node A

 $\delta \mathbf{u}_A$  = iterative change in translation at node A

 $\mathbf{T}_A$  = rotation triad at node A

 $\delta \theta_A$  = iterative change in rotation pseudo-vector at node A

Thus the total displacement,  $d_A$ , is represented by the combination of a nodal translation, and a nodal triad that describes the orientation of a "rigid body" attached to the node. The iterative change in displacement,  $\delta d_A$ , is represented by an iterative change in translation, and an iterative change in a rotation pseudo-vector. The latter quantity uniquely describes iterative changes in the rotation triad.

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With the above definitions, the modified version of equation 3.9-15a at an individual node may be written as follows. For the translational freedoms we simply have:

$$\mathbf{u}_{\boldsymbol{A}} = \overline{\mathbf{u}}_{\boldsymbol{A}} + \delta \mathbf{u}_{\boldsymbol{A}} \qquad (3.9 - 50)$$

whereas for the rotational freedoms we use:

$$\mathbf{T}_{\boldsymbol{A}} = exp(\delta\boldsymbol{\theta}_{\boldsymbol{A}}) \overline{\mathbf{T}}_{\boldsymbol{A}}$$
(3.9 - 51)

where  $exp(\delta\theta_A)$  is the exponential of  $\delta\theta_A$ , which is an orthogonal (rotation) matrix whose rotation angle and direction correspond to the magnitude and direction of the pseudo-vector  $\delta\theta_A$ . The following explicit expression for this matrix is known as as "Rodriguez' formula" (see, e.g., ref. 3.2):

$$exp(\theta) = \mathbf{I} + \frac{\sin\theta}{\theta} \Theta + \frac{(1-\cos\theta)}{\theta^2} \Theta^2$$
 (3.9-52)

where  $\Theta$  is the skew-symmetric matrix corresponding to the pseudo-vector,  $\theta$ , i.e.,

$$\boldsymbol{\Theta} \mathbf{h} = \boldsymbol{\theta} \times \mathbf{h} \qquad (3.9 - 53)$$

for any vector h, so that

$$\Theta = \begin{bmatrix} 0 & -\theta_3 & \theta_2 \\ \theta_3 & 0 & -\theta_1 \\ -\theta_2 & \theta_1 & 0 \end{bmatrix}, \qquad \Theta = \begin{cases} \theta_1 \\ \theta_2 \\ \theta_3 \end{cases}$$
(3.9-54)

and  $\theta$  is the magnitude of  $\theta$ , *i.e.*,

$$\theta = \|\theta\| = \sqrt{\theta_1^2 + \theta_2^2 + \theta_3^2}$$
 (3.9-55)

where  $\theta_i$  (i = 1, 2, 3) are Cartesian components of  $\theta$ . Note that the pseudovector,  $\theta$ , behaves as a true vector in all ways except for vector addition – since the sum of two arbitrary large rotations is not a vectorial sum (see refs. 3.3or 3.4for the rules of rotation pseudovector addition).

The rotation update formula given by equation 3.9-19 need only be performed at nodes with rotational freedoms. It may also be used to perform *incremental* updates as well as iterative updates, *i.e.*,

$$\mathbf{T}_{A}^{n+1} = exp(\Delta \boldsymbol{\theta}_{A}) \mathbf{T}_{A}^{n} \qquad (3.9-56)$$

The above relation is employed in the computation of the *predictor* solutions described by equations 3.9-16 or 3.9-22. For the *extrapolated* predictor (equation 3.9-22), the extrapolated rotation triads are obtained by: i) extrapolating the rotational components of the displacement vector precisely as indicated by equation 3.9-22a; ii) computing the rotation increments between steps n and n + 1 by subtracting the rotational components of  $d_n$  from those of the extrapolated vector,  $d_{n+1}$ ; and iii) plugging the corresponding rotation-increments ( $\Delta \theta_A$ ) into equation 3.9-56. Note that while the rotation components of the "total" displacement vectors,  $d_A^n$  and  $d_A^{n+1}$  are meaningless for large rotations, the difference between these to vectors defines a valid incremental rotation pseudo-vector,  $\Delta \theta_A$ .

#### 3.9.3 ALGORITHM

#### **General Algorithm**

(1) STEP LOOP: for n = 2, 3, 4 ... (step = n+1)  
(1.1) Extrapolate Solution for Predictor  
call EXTRAP (
$$\Delta \ell_{n+1}, \Delta \ell_n, \Delta \ell_{n-1} \rightarrow c_n, c_{n-1}, c_{n-2}$$
)  
 $\lambda_{n+1}^{(1)} = c_n \lambda_n + c_{n-1} \lambda_{n-1} + c_{n-2} \lambda_{n-2}$   
 $d_{n+1}^{(1)} = c_n d_n + c_{n-1} d_{n-1} + c_{n-2} d_{n-2}$   
 $\Delta d_{n+1}^{(1)} = d_{n+1}^{(1)} - d_n$  ( $\mathbf{T}_{n+1}^{(1)} = \mathbf{R}(\Delta d_{n+1}^{(1)})\mathbf{T}_n$ )  
 $\Delta \lambda_{n+1}^{(1)} = \lambda_{n+1}^{(1)} - \lambda_n$ 

(1.2) Solve for Tangential Displacement based on Predictor

$$\delta \widehat{\mathbf{d}} = \mathbf{K}^{-1}(\mathbf{d}_{n+1}^{(1)}) \left[ \widehat{\mathbf{f}}^{ext} + \mathbf{K}^{us} \widehat{\mathbf{d}}^{s} \right]$$

(1.3) Form Residual based on Predictor

$$\mathbf{r}_{n+1}^{(1)} = \mathbf{r}(\mathbf{d}_{n+1}^{(1)}, \lambda_{n+1}^{(1)}) = \lambda_{n+1}^{(1)} \hat{\mathbf{f}}^{ext} - \mathbf{f}^{int}(\mathbf{d}_{n+1}^{(1)})$$
  
call CHK\_CONV (  $\mathbf{r}_{n+1}^{(1)}, \Delta \mathbf{d}_{n+1}^{(1)}, \epsilon_{ref} \rightarrow \hat{\epsilon}^{(1)}, \epsilon_{ref}$  )

(2) ITERATION LOOP: i = 1, 2, ... (iter = i+1 = 2, 3, ...)

(2.1) Solve for Basic Iterative Displacement Change

$$\delta \overline{\mathbf{d}} = \mathbf{K}^{-1}(\mathbf{d}_{n+1}^{(1)}) \mathbf{r}_{n+1}^{(i)}$$

(2.2) Solve Linearized arc-length Constraint Eqn for New Load Factor

$$\delta \lambda = \frac{\Delta \ell^2 - \Delta \mathbf{d}_{n+1}^{(i)} \cdot \Delta \mathbf{d}_{n+1}^{(i)} - 2(\Delta \mathbf{d}_{n+1}^{(i)} \cdot \delta \overline{\mathbf{d}})}{2(\Delta \mathbf{d}_{n+1}^{(i)} \cdot \delta \widehat{\mathbf{d}})}$$
$$\lambda_{n+1}^{(i+1)} = \lambda_{n+1}^{(i)} + \delta \lambda$$

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(2.3) Update Displacements  $\delta \mathbf{d} = \delta \mathbf{d} + \delta \lambda \, \delta \mathbf{d}$  $\mathbf{d}_{n+1}^{(i+1)} = \mathbf{d}_{n+1}^{(i)} + \delta \mathbf{d}$   $(\mathbf{T}_{n+1}^{(i+1)} = \mathbf{R}(\delta \mathbf{d}) \mathbf{T}_{n+1}^{(i)})$  $\Delta \mathbf{d}_{n+1}^{(i+1)} = \Delta \mathbf{d}_{n+1}^{(i)} + \delta \mathbf{d}$ (2.4) Compute New Residual  $\mathbf{r}_{n+1}^{(i+1)} = \mathbf{r}(\mathbf{d}_{n+1}^{(i+1)}, \lambda_{n+1}^{(i+1)}) = \lambda_{n+1}^{(i+1)} \mathbf{\hat{f}}^{ext} - \mathbf{f}^{int}(\mathbf{d}_{n+1}^{(i+1)})$ (2.5) Check Convergence call CHK\_CONV (  $\mathbf{r}_{n+1}^{(i+1)}, \delta \mathbf{d}, \hat{\epsilon}^{(i)}, \epsilon_{ref}, \hat{\epsilon}_{tol}, \text{num_div} \rightarrow$  $\hat{\epsilon}^{(i+1)}$ , <CONVERGED>, <DIVERGED> ) if ( <CONVERGED> ) then num\_iters\_required = iter  $\Delta \ell_{n+2} = \Delta \ell_{n+1} \left( \frac{\text{num_iters\_desired}}{\text{num\_iters\_required}} \right)$  $n \leftarrow n + 1$ go to (1) STEP LOOP elseif ( <DIVERGED> .or. (iter > max\_iters) ) then if ( num\_cuts < max\_cuts ) then  $\Delta \ell_{n+1} = \Delta \ell_{n+1}/2$  $num\_cuts = num\_cuts + 1$ go to (1.1)else STOP endif else  $i \leftarrow i + 1$ go to (2) ITER LOOP

endif

# Starting Procedure: Step 1 (n=0)

Replace Algorithm Steps (1.1)-(1.2) by:

$$d_{1}^{(0)} = 0$$
  

$$\delta \widehat{d} = \mathbf{K}^{-1}(\mathbf{d}_{1}^{(0)}) \left[ \widehat{\mathbf{f}}^{ext} + \mathbf{K}^{us} \widehat{\mathbf{d}}^{s} \right]$$
  

$$\lambda_{1}^{(1)} = \lambda_{start} \quad (\text{user specified})$$
  

$$\Delta \lambda_{1}^{(1)} = \lambda_{1}^{(1)}$$
  

$$\Delta \ell_{1} = \Delta \lambda_{1}^{(1)} \| \delta \widehat{\mathbf{d}} \|$$
  

$$\Delta \mathbf{d}_{1}^{(1)} = \Delta \lambda_{1}^{(1)} \delta \widehat{\mathbf{d}}$$
  

$$\mathbf{d}_{1}^{(1)} = \Delta \mathbf{d}_{1}^{(1)}$$

(Also, form  $\mathbf{K}(\mathbf{d}_1^{(1)})$  before next solve.)

# Starting Procedure: Step 2 (n=1)

Replace Algorithm Steps (1.1)-(1.2) by:

$$d_{2}^{(0)} = d_{1}$$

$$\delta \widehat{d} = K^{-1}(d_{2}^{(0)}) \left[ \widehat{f}^{ext} + K^{us} \widehat{d}^{s} \right]$$

$$\Delta \lambda_{2}^{(1)} = \Delta \ell_{2} / \| \delta \widehat{d} \|$$

$$\lambda_{2}^{(1)} = \lambda_{1} + \Delta \lambda_{2}^{(1)}$$

$$\Delta d_{2}^{(1)} = \Delta \lambda_{2}^{(1)} \delta \widehat{d}$$

$$d_{2}^{(1)} = d_{1} + \Delta d_{2}^{(1)} \quad (\mathbf{T}_{2}^{(1)} = \mathbf{R}(\Delta d_{2}^{(1)} \mathbf{T}_{1})$$
(But don't reform  $\mathbf{K}(d_{1}^{(1)})$  until step 3.)

)

# CHK\_CONV: Procedure to Check Convergence

Input: r,  $\delta d$ ,  $\hat{\epsilon}^{(i)}$ ,  $\epsilon_{ref}$ ,  $\hat{\epsilon}_{tol}$ , num\_div, iter Output:  $\hat{\epsilon}^{(i+1)}$ , num\_div, <CONVERGED>, <DIVERGED>

(1) Compute Energy Error Norm:  $\epsilon^{(i+1)} = |\mathbf{r} \cdot \delta \mathbf{d}|$ 

(2) Normalize: 
$$\hat{\epsilon}^{(i+1)} = \sqrt{\frac{\epsilon^{(i+1)}}{\epsilon_{ref}}}$$

(3) Check Convergence / Divergence:

```
if ( \hat{\epsilon}^{(i+1)} \leq \hat{\epsilon}_{tol} ) then

\langle \text{CONVERGED} \rangle = \text{TRUE}
```

else

if ( 
$$\hat{\epsilon}^{(i+1)} > \hat{\epsilon}^{(i)}$$
 ) then  
num\_div = num\_div + 1  
if ( num\_div > 1 ) then  
 $\langle \text{DIVERGED} \rangle = \text{TRUE}$   
endif

endif

endif

Modification for Iteration = 1 (i=0):

(1.5) if ( iter = 1 ) then if (  $\epsilon^{(1)} > \epsilon_{ref}$  ) then  $\epsilon_{ref} = \epsilon^{(1)}$ endif

сп

endif

# EXTRAP: Procedure to Compute Quadratic Extrapolation Coefficients

Input:  $\Delta \ell_{n+1}$ ,  $\Delta \ell_n$ ,  $\Delta \ell_{n-1}$ Output:  $c_n$ ,  $c_{n-1}$ ,  $c_{n-2}$ 

$$\ell_{n-1} = \Delta \ell_{n-1}$$

$$\ell_n = \ell_{n-1} + \Delta \ell_n$$

$$\ell_{n+1} = \ell_n + \Delta \ell_{n+1}$$

$$\Delta \ell_{tot} = \ell_{n+1} - \ell_{n-1}$$

$$c_n = \frac{(\ell_{n+1})(\Delta \ell_{tot})}{(\ell_n)(\Delta \ell_n)}$$

$$c_{n-1} = -\frac{(\ell_{n+1})(\Delta \ell_{n+1})}{(\ell_{n-1})(\Delta \ell_n)}$$

$$c_{n-2} = \frac{(\Delta \ell_{n+1})(\Delta \ell_{tot})}{(\ell_{n-1})(\ell_n)}$$

# **3.9.4 PROCEDURE USAGE**

Procedure NL\_STATIC\_1 may be invoked by the \*call directive:

\*call NL\_STATIC\_1 ( arg1 = val1; arg2 = val2; ...)

where argi are argument names and vali are the corresponding values you wish to give them. The following are valid arguments for procedure NL\_STATIC\_1; note that those without default values are mandatory, while the others are optional.

Argument	Default Value	Meaning
BEG_LOAD		Starting load factor (>0.)
BEG_STEP		Starting step number (>0)
MAX_LOAD		Upper_bound on load factor
MIN_LOAD		Lower_bound on load factor
MAX_STEPS		Maximum steps to compute
COROTATION	1	Corotational Update Option
DES_ITERS	4	Number of iterations per step desired
EXTRAPOLATE	<true>	Perform quadratic extrapolation of solution
FAC_STEPS	1	Steps_per_refactoring
MAX_ITERS	9	Maximum iterations per step
MAX_CUTS	3	Maximum number of successive step cuts
NL_GEOM	2	Geometric Nonlinearity Level (1 or 2)
NOMINAL_DB	NOMINAL.GAL	Results database file
NOMINAL_DS	<b>RESPONSE.HISTORY</b>	Results dataset
N_SELECT	0	Number of nodes for selected disp. output
PATH_SCALE	1.	arc-length scale factor for restarts
SEL_NODES	0	List of nodes for selected output
SEL_DOFS	0	Corresponding list of nodal freedoms (1-6)
TOL_E	1.E-3	Relative error tolerance in energy norm

In the above definitions, the term *step* refers to a load step. The total response is automatically subdivided into load steps, with the starting load factor prescribed by the user - using BEG\_LOAD. Subsequent load step sizes are automatically selected by the algorithm, using an arc-length constraint, as described in the theory section.

Table 3.9-1 Datasets Input/Output by procedure NL_STATIC_1					
Dataset	Description	Lib	Input	Output	
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	1	$\checkmark$	$\checkmark$	
ES.SUMMARY.O.nnod	ES Processor Status	1	$\checkmark$	$\checkmark$	
DEF. <es_name>.0.nnod</es_name>	Element Defn. (Connectivity)	1	$\checkmark$		
DIR. <es_name>0.nnod</es_name>	Element EFIL Directory	1	$\checkmark$		
INC.DISP	System Displacement Vector	1	$\checkmark$	$\checkmark$	
INT.FORC.step	Nodal Rotation Pseudovectors	1	$\checkmark$	$\checkmark$	
JDF1.BTAB.1.8	Model Summary	1	$\checkmark$		
JLOC.BTAB.2.5	Nodal Coordinates	1	$\checkmark$		
PROP.BTAB.*	Material/Section Properties	1	$\checkmark$		
QJJT.BTAB.2.9	Nodal Transformations	1	$\checkmark$		
TOT.DISP.step	System Displacement Vector	1	$\checkmark$	$\checkmark$	
TOT.ROTN.step	System Force Vector	1	$\checkmark$	$\checkmark$	

where step is the load-step number, and ranges consecutively from 1 to the total number of steps computed.

Table 3.9-2 Sub-Procedures Invoked by procedure NL_STATIC_1		
Procedure	Туре	Function
NL_STATIC_1	Internal	Main procedure
CHKCONV	Internal	Check convergence
DEFNS	Internal	Defines recursive macrosymbols
ES	External	Element utility procedure
EXTRAP	Internal	Quadratic extrapolation for next load step
INITIAL	Internal	Initialize displacements and rotations
POSTSTEP	Internal	Print load step summary
POSTRESS	Internal	Archive load step data
RESIDUAL	Internal	Forms residual-force vector
SOLVE	Internal	Solves linear equation systems
STIFFNESS	Internal	Forms and factors stiffness matrix
TANDIS	Internal	Solves for tangential displacements

### 3.9.5 ARGUMENT DESCRIPTION

### 3.9.5.1 BEG\_LOAD

Starting load factor  $(\lambda_1)$  for the nonlinear analysis. For applied *force* loading, this factor is multiplied by the reference applied force vector to obtain the starting load vector, *i.e.*,

$$\mathbf{f}_{1}^{ext} = \lambda_{1} \, \bar{\mathbf{f}}^{ext}$$

where  $\bar{\mathbf{f}}^{ext}$  is the reference applied force vector stored in dataset APPL.FORC.1. For applied *displacement* loading, the starting load factor is applied to the reference applied displacement vector, which is then used to compute the initial internal force vector, *i.e.*,

$$\mathbf{f}_{1}^{int(1)} = \mathbf{f}^{int}(\lambda_{1} \, \overline{\mathbf{d}}^{ezt})$$

where  $\overline{\mathbf{d}}^{ext}$  is the reference applied displacement vector stored in dataset APPL.MOTI.1. Note that this argument is *irrelevant* for re-start runs (*i.e.*, BEG\_STEP > 1).

# 3.9.5.2 <u>BEG\_STEP</u>

This argument defines the number of the first step to be computed in a given nonlinear analysis interval. It is important primarily for analysis re-starts. Initially, BEG\_STEP should be set to 1. To continue an analysis in a subsequent run, after having computed and saved "n" steps in the previous run, one would typically set BEG\_STEP equal to "n+1". For example, if the 10th step was successfully completed in the first run, then it could be continued in a second run by setting BEG\_STEP = 11. However, it is not necessary for BEG\_STEP to be larger than any previously computed step. That is, you may *re-compute* a sequence of steps by setting BEG\_STEP to the number of the first step to be re-computed. The procedure will automatically use those steps which immediately precede BEG\_STEP (*e.g.*, BEG\_STEP-1, BEG\_STEP-2 and BEG\_STEP-3) to smoothly effect the restart.

# 3.9.5.3 COROTATION

Corotational update switch for large-rotation problems (default:  $\langle true \rangle$ ). This switch should be set to  $\langle true \rangle$  when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element processor (ESi) section in the CSM Testbed User's Manual (see ref. 3.9-5) for specific guidelines.

# 3.9.5.4 DEBUG

Procedure debug switch (default: <false>). This switch should only be turned on to obtain additional diagnostic printout for procedure debugging.

# 3.9.5.5 DES\_ITERS

Desired number of iterations allowed for convergence at a given load step (default=4). This parameter is used to adaptively adjust the arc-length increment from one load step to the next, by comparing DES\_ITERS with the actual number of iterations required for convergence at the last step.

# 3.9.5.6 EXTRAPOLATE

Solution extrapolation switch (default:  $\langle true \rangle$ ). Extrapolation here refers to a technique for predicting the displacement vector and load factor at the beginning of a new load step, by fitting a quadratic curve through the converged solutions at the three previous load steps. It has been found to be a very effective strategy for accelerating traversal of the load-displacement "curve", *i.e.*, far fewer load steps are usually required with extrapolation turned on, than with it turned off. One exception is near very sharp turns in the loaddisplacement curve, where extrapolation may be too smooth to follow the curve, and may have to be temporarily suppressed. (Note: EXTRAPOLATE =  $\langle false \rangle$  option has not been fully tested.)

# 3.9.5.7 FAC\_STEPS

Number of load steps between updating (formation and re-factoring) of the stiffness matrix default = 1). FAC\_STEPS = n implies that re-factoring will be performed every n steps, starting with the first step of the analysis interval (BEG\_STEP). Best results are often obtained by allowing the procedure to re-factor at the beginning of each load step (FAC\_STEPS = 1).

### 3.9.5.8 <u>MAX\_CUTS</u>

Maximum number of step cuts permitted during the current nonlinear analysis interval (default=3). A step cut refers to a halving of the arc-length increment used to advance the solution from one step to the next. Step cuts are performed only if the maximum number of iterations are exceeded without converging at a given load step. Note that the relationship between the increment in "arc-length" and the increment in the load-factor,  $\lambda$ , is computed internally by the procedure.

### 3.9.5.9 MAX\_ITERS

Maximum number of iterations allowed for convergence at a given load step. This parameter is used to terminate the iteration process at a given load level. If convergence hasn't been obtained after MAX\_ITERS iterations, the load (*i.e.*, arc-length) increment is cut in half and the step is repeated – until either convergence has been obtained or MAX\_CUTS has been exceeded.

### 3.9.5.10 MAX\_LOAD

Maximum load factor. This sets an upper limit on the load level, and thus provides a convenient way of terminating the arc-length controlled solution algorithm. Since the load factor is actually an unknown in procedure NL\_STATIC\_1, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. The nonlinear analysis is terminated when either MAX\_LOAD, MIN\_LOAD, MAX\_STEPS or MAX\_CUTS is exceeded - whichever comes first.

### 3.9.5.11 MAX\_STEPS

Maximum number of load steps to compute in the current nonlinear analysis run. This provides an implicit limit on analysis run-time. Since the load factor is actually an unknown in procedure NL\_STATIC\_1 (controlled by the arc-length constraint), there is no way of knowing a-priori how many load steps will be required to attain a particular load level. The nonlinear analysis is thus terminated whenever MAX\_STEPS, MIN\_LOAD, MAX\_LOAD or MAX\_CUTS is exceeded – whichever comes first.

### 3.9.5.12 MIN\_LOAD

Minimum load factor. This sets a lower limit on the load level, and thus provides a convenient way of terminating the arc-length controlled solution algorithm. Since the load

factor is actually an unknown in procedure NL\_STATIC\_1, there is no way of knowing apriori how many load steps will be required to attain a particular load level. The nonlinear analysis is terminated when either MIN\_LOAD, MAX\_LOAD, MAX\_STEPS or MAX\_CUTS is exceeded - whichever comes first.

# 3.9.5.13 <u>NL\_GEOM</u>

Geometric nonlinearity level: 0, 1, or 2 (default =2). A value of zero means that the problem is geometrically linear; a value of one means that the geometric nonlinearity will be handled globally (*i.e.*, using corotational updates only); and a value of two means that the nonlinear element strain-displacement relations will be used in addition to any global treatment of geometric nonlinearity. If COROTATION =  $\langle true \rangle$ , options 1 and 2 refer to first-order and second-order corotation, respectively. The latter option can be significantly more accurate than the former for a given finite element model – depending on which element types are involved.

### 3.9.5.14 NOMINAL\_DB

Name of database (GAL file) where a step-wise history of important solution parameters and selected response variables is to be stored (default = NOMINAL.GAL).

# 3.9.5.15 NOMINAL\_DS

Name of dataset, within database defined by argument NOMINAL\_DB, where a step-wise history of important solution parameters and selected response variables is to be stored (default = RESPONSE.HISTORY). See the CSM Testbed Dataset Manual (ref. 3.9-6), under dataset RESPONSE.HISTORY, for a description of the individual data records stored in this dataset.

### 3.9.5.16 <u>N\_SELECT</u>

Number of user-selected displacement components to be saved in the dataset specified by argument NOMINAL\_DS (default =0). Values for these displacement components, the locations and directions of which are specified by arguments SEL\_NODES and SEL\_DOFS, respectively, are stored at every load-step.

### 3.9.5.17 PATH\_SCALE

This floating point number represents a scale factor to be applied to the incremental arclength (or pathlength) used for the first step of an analysis re-start run (default =1.0). If the default (1.0) is used, the arc-length increment from the previous step BEG\_STEP-1 will be used for the first step BEG\_STEP. Note that this may lead to a different load-step size than if the analysis had continued to step BEG\_STEP without a re-start. To eliminate this difference, the user can set:

```
[PATH_SCALE] = [DES_ITERS] / act_iters
```

where "act\_iters" is the actual number of iterations required for convergence at step [BEG\_STEP]-1.

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#### 3.9.5.18 SEL\_DOFS

List of nodal degrees-of-freedom at which displacement histories are to be saved in dataset NOMINAL\_DS (default =1.0). There should be N\_SELECT numbers in the list, in correspondence with the node numbers specified by argument SEL\_NODES. Values of each number in the list must range between 1 and 6, in correspondence to the nodal degree-of-freedom sequence  $(e.g., u, v, w, \theta_x, \theta_y, \theta_z)$  specified by the START command of processor TAB.

#### 3.9.5.19 <u>SEL\_NODES</u>

List of node numbers at which displacement histories are to be saved in dataset NOMINAL\_DS (default =0). There should be N\_SELECT numbers in the list, and node numbers can be repeated if more than one nodal degree-of-freedom is to be saved at a node. The corresponding nodal degree-of-freedom for each entry is specified by argument SEL\_DOFS.

#### 3.9.5.20 <u>TOL\_E</u>

Error tolerance used to establish convergence of the nonlinear equilibrium iteration procedure at each load step (default =1.e-3). The iteration loop at a given step is terminated whenever the following condition is met:

$$\epsilon \leq [TOL_E]$$

where

$$\epsilon = \sqrt{\frac{\mathbf{r}^{(i)} \cdot \delta \mathbf{d}^{(i)}}{\mathbf{r}^{(1)} \cdot \delta \mathbf{d}^{(1)}}}$$

is the relative energy error norm, r is the residual force vector,  $\delta d$  is the iterative displacement change, and *i* is the iteration counter.

# 3.9.6 PROCEDURE FLOWCHART

NL_STABIL_1	(main procedure)
DEFNS	(define recursive macrosymbols)
INITIAL	(initial displacements and rotations)
ES	(initialize element data)
EXTRAP	(quadratic extrapolation for next load step)
STIFFNESS	(form and form stiffness matrix)
TANDIS	(solve for tangential displacements)
SOLVE	(solve linear system of equations)
RESIDUAL	(form residual-force vector)
ES	(calculate residual)
CHKCONV	(check convergence)
POSTSTEP	(print load step summary)
POSTRESS	(archive load step data)

# 3.9.7 LIMITATIONS

# 3.9.7.1 Number of Database Libraries

All analysis (computational) data is assumed to be resident on a single database library (i.e., file), and that file is expected to be attached to logical device index 1 before calling procedure NL\_STATIC\_1. Additionally, important analysis statistics and re-start parameters, as well as selected post-processing data, will be deposited in a separate data library, which is automatically opened by procedure NL\_STATIC\_1 on logical device index 3. The name of this secondary library is user-specified using procedure argument NOMINAL\_DB, which has the default setting: NOMINAL\_DB = NOMINAL.GAL.

# 3.9.7.2 Element Types

Only shell elements have been tested thus far with procedure NL\_STATIC\_1. While the procedure is potentially compatible with beam and solid elements too, minor modifications to the generic element processor may be required to handle geometric nonlinearity for these elements.

# 3.9.7.3 <u>Number of Load/Constraint Systems</u>

Only one set of loads and constraints is accommodated by procedure NL\_STATIC\_1. Furthermore, they must be referred to as load set 1 and constraint set 1 in the database.

# 3.9.7.4 Specified Rotations

Specified (non-zero) rotational freedoms are currently not implemented in procedure **NL\_STATIC\_1** – unless rotation angles remain moderately small (*i.e.*, less than 10 degrees). For larger rotations, the specification of rotation components constitutes a nonlinear constraint, which must be translated into the motion of nodal rotation triads, and requires a modification to the linearized equilibrium equations. This capability is planned for a future version of procedure **NL\_STATIC\_1**.

# 3.9.7.5 Material Nonlinearity

Only geometric nonlinearity is accounted for by procedure NL\_STATIC\_1. However, this limitation is really due to current limitations within the generic element processor; the global nonlinear solution algorithm doesn't particularly care about the *source* of the nonlinearity, as long as it is properly represented by the tangent stiffness matrix and the residual force vector.

# 3.9.7.6 <u>Re-Starting from Step 1</u>

It is currently not permitted to re-start the analysis from step 1 (*i.e.*, re-run the problem from the beginning) unless you either: i) delete the database and recreate the model, or ii) **\*enable** the original APPL.MOTI and APPL.FORC datasets. The reason for this is that the original APPL.MOTI and APPL.FORC datasets are copied into new datasets – and marked for deletion – by procedure NL\_STATIC\_1 whenever BEG\_STEP = 1. This limitation will be removed in the next version of NL\_STATIC\_1.

# 3.9.7.7 EXTRAPOLATE Must be Turned On

Extrapolation is the only form of load/displacement step prediction that has been thoroughly tested. Without extrapolation, procedure NL\_STATIC\_1 is supposed to use the arclength constraint equation to generate a predictor solution (see theory section), and use information regarding the sign of the stiffness determinant to determine the load *direction* (increasing or decreasing) between one step and the next. However, the no-extrapolation option has not yet been quality assured. Note that the extrapolation option is the recommended approach anyway.

# 3.9.7.8 <u>True-Newton Iteration</u>

Only modified Newton/Raphson iteration is provided by the current version of procedure NL\_STATIC\_1. This means that the stiffness matrix is re-formed and re-factored only at the beginning (first iteration) of every FAC\_STEPS load steps (where FAC\_STEPS = 1 by default). In the next version, we plan to implement the option for *true* Newton/Raphson iteration, in which the stiffness matrix can be updated at each iteration of selected load steps. This option can be useful for problems with limit points that are nearly as sharp as bifurcation points.

# 3.9.7.9 Constant Load-Increments

Currently, all load increments (except the first one) are computed automatically by procedure NL\_STATIC\_1, using the arc-length constraint equation. Therefore, it is not possible for the user to fix the load increment, as is done in conventional load-controlled algorithms. Since this option may be useful for benchmarking (and research) purposes, we plan to include it in a future version of the procedure, wherein the arc-length constraint equation will be selectively bypassed.

# 3.9.7.10 Singularities due to Limit Points and Bifurcations

Procedure NL\_STATIC\_1 cannot handle singularities in the stiffness matrix that arise when the load-stepping algorithm lands too close to a limit point, or attempts to traverse a bifurcation point. (Note: Singularities due to limit points are overcome by procedure NL\_STATIC\_2.)

# 3.9.8 ERROR MESSAGES AND WARNINGS

### 3.9.8.1 "Non-Convergence at Step n. Revise Strategy."

This message means that the maximum number of nonlinear iterations (MAX\_ITERS) has been exhausted, as well as the maximum number of step cuts (MAX\_CUTS), and convergence still hasn't been obtained at step n. A possible cure is to re-start the analysis from several steps back, and decrease the arc-length increment at that point (using the PATH\_SCALE argument). However, just increasing MAX\_ITERS or MAX\_CUTS, or even TOL\_E, may also solve the problem. In other words, re-think the definition of all solution parameters based on the observed behavior of the solution algorithm just prior to the break-down.

# 3.9.8.2 "Divergence at Step n. Revise Strategy."

This message has similar implications to the previous message, but it occurs when the error grows instead of decreases during two successive nonlinear iterations. The difference between divergence and non-convergence is that divergence cannot be cured by increasing MAX\_ITERS; and probably should not be "cured" by increasing TOL\_E. It generally means that the step-size is too big - or that the error tolerance (TOL\_E) has been too big all along, so that changes are occurring suddenly that should have been detected by the solution algorithm at earlier load steps. Thus, you might try re-starting from an earlier step, reducing PATH\_INC, and possibly reducing TOL\_E as well.

### 3.9.8.3 "Specified Displacements are Identically Zero"

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed – in which case the message should be taken merely as a warning.

#### 3.9.8.4 "Specified Forces are Identically Zero"

This is not necessarily an abortive error. As long as either nonzero specified displacements *or* specified forces are defined, the solution can proceed – in which case the message should be taken merely as a warning.

### 3.9.9 USAGE GUIDELINES AND EXAMPLES

Procedure NL\_STATIC\_1 may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call NL\_STATIC\_1 ( --

<pre>beg_step =1 ; Starting step number (&gt;0)</pre>
max_steps=1 ; Maximum steps to compute
max_iters=9 ; Maximum iterations per step
des_iters=4 ; Number of iterations desired
<pre>fac_steps=1 ; Steps_per_refactoring</pre>
max_cuts=3 ; Maximum number of step cuts
tol_e=1.E-3 ; Energy error tolerance
beg_load ; Starting load factor (>0.)
mar_load ; Upper_bound on load factor
min_load ; Lower_bound on load factor
<pre>path_scale=1.; Path_inc scl_factor (restart)</pre>
extrapolate= <true> ;</true>
line_search=1.; Initial line-search parameter
debug= <false>; Debug_print switch</false>
$NL_GEOM = 2$ ; Geom. Nonlin. Level (1 2)
COROTATION=1 ; Corotational Flag (leave on !!)
Nominal_DB = NOMINAL.GAL ; Selected Output
Nominal_DS = RESPONSE.HISTORY ;
N_SELECT ; SEL_NODES; SEL_DOFS )

# 3.9.9.1 Starting an Analysis

To begin a nonlinear static analysis with procedure NL\_STATIC\_1, it is only necessary that the finite element model be defined. This does not require pre-formation of element stiffness matrices, node renumbering for optimal factorization time, or any form of linear analysis (unless initial geometric imperfections are based on linear displacement modes). Only nodal coordinates/transformations, material properties and element connectivity are prerequisite to nonlinear analysis. To invoke procedure NL\_STATIC\_1, only those arguments that don't have default values (see procedure usage section) need be specified.

For example, suppose you wanted to start an analysis with an initial load-factor of .1, a maximum load-factor of 1., a minimum load-factor of 0., and compute no more than 20 load-steps. You could then invoke the procedure as follows:

\*call NL\_STATIC\_1 ( BEG\_STEP = 1 ; MAX\_STEPS = 20 ; --BEG\_LOAD = .1 ; MAX\_LOAD = 1. ; MIN\_LOAD = 0. )

Keep in mind that the number of load-steps actually performed during the above run will depend on the number of adaptively-sized arc-length increments needed to attain the maximum load level. Since it may be difficult to estimate this in advance, you may want to start with only a few load-steps (e.g., set MAX\_STEPS = 3) to get some experience, and later re-start the analysis with more steps allowed.

# 3.9.9.2 <u>Re-Starting (or Continuing) an Analysis</u>

To re-start an analysis from a previously computed, converged solution, you need only specify the first step to compute as argument BEG\_STEP. If the EXTRAPOLATE argument is activated (which is the default), the three solution steps immediately preceding the one you wish to compute must be resident on the database. If the EXTRAPOLATE argument is turned off, only one preceeding solution step is required. Thus, to continue an analysis that has already produced ten load steps, you could issue the call:

```
*call NL_STATIC_1 ( BEG_STEP = 11; MAX_STEPS = 100 ; --
MAX_LOAD = 1. ; MIN_LOAD = 0. )
```

Note that the argument BEG\_LOAD is not necessary for a continuation (or re-start) run; the new load level is automatically computed using the preceeding value of the arc-length increment. However, you can modify the new increment, by using the PATH\_SCALE argument, which is a scale factor applied to the previous arc-length increment to generate the new increment. The default value of PATH\_SCALE is 1.0.

Furthermore, on analysis continuations/restarts, you are free to modify any of the other solution parameters (*i.e.*, procedure arguments). For example, you may want to increase **MAX\_ITERS**, reduce TOL\_E, or even change DES\_ITERS. The default values for these solution parameters are not suitable for all problems; they are useful primarily for gaining experience by trial and error.

#### **3.9.10 PROCEDURE LISTING**

```
. =DECK NL_STATIC_1
*procedure NL_STATIC_1 ( --
                       beg_step =1 ; -- . Starting step number (>0)
                      max_steps=1 ; -- . Maximum steps to compute
                      max_iters=9 ; -- . Maximum iterations per step
                      des_iters=4 ; -- . Number of iterations desired
                       fac_steps=1 ; -- . Steps_per_refactoring
                      max_cuts=3 ; -- . Maximum number of step cuts
tol_e=1.E-3 ; -- . Energy error tolerance
                      beg_load ; -- . Starting load factor (>0.)
max_load ; -- . Upper_bound on load factor
                      min_load ; -- . Lower_bound on load factor
                      path_scale=1.; -- . Path_inc scl_factor (restart)
                       extrapolate=<true> ; --
                       line_search=1.;-- . Initial line-search parameter
                       debug=<FALSE>; -- . Debug_print switch
                      NL_GEOM = 2; --. Geom. Nonlin. Level (1|2)
                       COROTATION=1 ; -- . Corotational Flag (leave on !!)
                       Nominal_DB = NOMINAL.GAL ; -- . Selected Output
                       Nominal_DS = RESPONSE.HISTORY ; --
                       N_SELECT ; SEL_NODES; SEL_DOFS
                     )
 *Remark
                              *Remark |
 *Remark
                            NL_STATIC_1
 *Remark
                   CSM Testbed Procedure for Nonlinear Statics:
 *Remark
 *Remark
                     o Corotational Newton/Raphson algorithm
*Remark
*Remark
                     o Linearized Crisfield/Riks arc-length control
*Remark
                      o Applied forces and/or displacements
*Remark
*Remark
                   Authors: G.M. Stanley and C.C. Rankin
                  Version: MAR-03-1988
*Remark
                                                                        I
*Remark |
*Remark
                         _____
```

#### 3.9.11 REFERENCES

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# 3.10 Procedure NL\_STATIC\_2

### **3.10.1 GENERAL DESCRIPTION**

NL\_STATIC\_2 is a modification to NL\_STATIC\_1 Riks arclength strategy that allows solution of a limit point problem in the immediate neighborhood of a critical point. Developed and written by C. C. Rankin in consultation with E. Riks, this modified algorithm avoids the singularity in the stiffness matrix at the critical point, thereby permitting a smooth continuation of the solution even when a solution point *coincides exactly* with the critical point. NL\_STATIC\_2 is preferred over NL\_STATIC\_1 whenever solution points are desired very near the critical area, or when the singularity of the stiffness is likely to persist over some distance along the solution path. In the absence of numerical difficulties, however, NL\_STATIC\_1 and NL\_STATIC\_2 produce *identical* results.

### **3.10.2 PROCEDURE USAGE**

Procedure NL\_STATIC\_2 may be invoked by the \*call directive:

\*call NL\_STATIC\_2 ( arg1 = val1; arg2 = val2; ...)

where argi are argument names and vali are the corresponding values you wish to give them. The following are valid arguments for NL\_STATIC\_1; note that those without default values are mandatory, while the others are optional.

Argument	<u>Default Value</u>	Meaning
BEG_LOAD	_	Starting load factor (>0.)
BEG_STEP	_	Starting step number (>0)
MAX_LOAD	_	Upper_bound on load factor
MIN_LOAD	_	Lower_bound on load factor
MAX_STEPS		Maximum steps to compute
COROTATION	1	Corotational Update Option
DES_ITERS	4	Number of iterations per step desired
EXTRAPOLATE	<true></true>	Perform quadratic extrapolation of solution
FAC_STEPS	1	Steps_per_refactoring
MAX_ITERS	9	Maximum iterations per step
MAX_CUTS	3	Maximum number of successive step cuts
NL_GEOM	2	Geometric Nonlinearity Level (1 or 2)
NOMINAL_DB	NOMINAL.GAL	Results database file
NOMINAL_DS	<b>RESPONSE.HISTORY</b>	Results dataset
N_SELECT	0	Number of nodes for selected disp. output
PATH_SCALE	1.	Arclength scale factor for restarts
SEL_NODES	0	List of nodes for selected output
SEL_DOFS	0	Corresponding list of nodal freedoms (1–6)
TOL_E	<b>1.E-3</b>	Relative error tolerance in energy norm
ADV_RIKS	<false></false>	If true, advanced Riks; else, do NL_STATIC_1

# **3.10.3 ARGUMENT GLOSSARY**

The only additional argument that NL\_STATIC\_2 has is ADV\_RIKS. All other arguments are identical in name and function as their counterparts in NL\_STATIC\_1.

# 3.10.3.1 ADV\_RIKS

This is a logical parameter, that, when set to <true>, invokes the advanced Riks option. Otherwise, NL\_STATIC\_2 reduces to NL\_STATIC\_1.

# **3.10.4 INPUT/OUTPUT DATASETS**

The input/output requirements of NL\_STATIC\_2 are identical to NL\_STATIC\_1.

# 3.10.5 SUB-PROCEDURES AND PROCESSORS

Table 3.10-2 Sub-Procedures Invoked by Procedure NL_STATIC_2		
Procedure	Туре	Function
NL_STATIC_2	Internal	Main Procedure
CHK_CONV	Internal	Check convergence
DEFNS	Internal	Defines recursive macrosymbols
ES	External	Element utility Procedure
FACT_STIFF	Internal	Factors Stiffness Matrix
FORM_STIFF	Internal	Forms Stiffness Matrix
RESIDUAL	Internal	Forms residual-force vector
SOLVE	Internal	Solves linear equation systems
STIF_COLMN	Internal	Fixes Freedom $I$ , Extracts Stiffness Col. $I$
TWO_BY_TWO	Internal	Computes Advanced Riks Reduced Coefficients

Table 3.10-3 Processors Invoked by Procedure NL_STATIC_2		
Procedure	Туре	Function
AUS	Internal	Extracts column I of Stiffness
E	Internal	Initializes EFIL datasets
ESi	External	Element Processors based on GEP
INV	Internal	Factors stiffness matrix
SSOL	Internal	Solves linear equation systems
VEC	Internal	Performs all vector/pseudo-vector algebra

# 3.10.6 LIMITATIONS

NL\_STATIC\_2 has the all the limitations that are listed in Section 4.1.6. However, whereas numerical difficulties can be expected with NL\_STATIC\_1 near a critical point, no difficulties whatsoever should be expected with NL\_STATIC\_2 near *limit* (as opposed to bifurcation points). There are two additional software limitations described in the next two subsections.

# 3.10.6.1 AUS Limitation

Due to hard wired data set naming conventions in processor AUS for system matrices (e.g. K.SPAR.36), the number of DOF's per node specified on the START command of processor TAB is presently restricted to be 6. AUS is currently essential to NL\_STATIC.2 for computing the product of the stiffness with an elementary vector to extract row I of the stiffness matrix. This restriction will be removed when we make the connection to the Generic Matrix Processor.

#### 3.10.6.2 First Two Steps

Because of the way the extrapolation is set up, NL\_STATIC\_2 operates as NL\_STATIC\_1 for the first two steps for a new (not restart) analysis. This limitation is not important, since it is highly unlikely that a critical point will be reached at the very beginning of a solution sequence.

#### **3.10.7 ERROR MESSAGES**

All error messages have the same meaning as in NL\_STATIC\_1 (section 4.1.7).

# **3.10.8 USAGE GUIDELINES AND EXAMPLES**

As they are identical to NL\_STATIC\_1, please consult section 4.1.8 for usage guidelines.

#### 3.10.9 THEORY

#### 3.10.9.1 Introduction

Procedure NL\_STATIC\_2, like NL\_STATIC\_1, performs a quasi-static analysis of a system of nonlinear equilibrium equations using an adaptive arclength-controlled Newton/Raphson incremental/iterative solution algorithm. The function of the arclength constraint, the stepsize selection, and convergence criteria are identical to NL\_STATIC\_1. Because almost all of the theory underlying NL\_STATIC\_2 is covered in Section 4.1.9, only the matrix partitioning and pivoting process that avoids the factoring of a singular or near singular stiffness matrix is covered here.

#### 3.10.9.2 The Block Pivot Strategy

The difficulties that occur in NL\_STATIC\_1 can be readily seen by examining Eq. (8).

$$\overline{\mathbf{K}}\,\delta\mathbf{d} = ???rbbold + \delta\lambda\,\widehat{\mathbf{f}}^{ext}$$

$$2\Delta\overline{\mathbf{d}}\cdot\delta\mathbf{d} = \overline{c} \qquad (3.10-1)$$

where  $\overline{\mathbf{r}}$  is the residual,  $\mathbf{\tilde{f}}^{ext}$  is the external load,  $\overline{c}$  is the arclength parameter, and  $\delta \overline{\mathbf{d}}$  is the desired displacement increment. Clearly, if  $\overline{\mathbf{K}}$  is singular, we will have a problem in solving this pair of equations. For *limit points*, however, the extended equation system containing the constraint (second of (57)) is non-singular. A simple and robust method of overcoming the singularity is to select out the equation for a particular freedom and treat it the same way as the constraint equation, solving *three* rather than *two* sets of equations, as illustrated by the following

$$\begin{bmatrix} \widehat{\mathbf{K}} & \widehat{\mathbf{f}}^{I} & -\widehat{\mathbf{f}}^{ext} \\ (\widehat{\mathbf{f}}^{I})^{T} & K_{II} & -f_{I}^{ext} \\ \widehat{\mathbf{c}} & c_{I} & 0 \end{bmatrix} \begin{bmatrix} \delta \widehat{\mathbf{d}} \\ \delta d_{I} \\ \delta \lambda \end{bmatrix} = \begin{bmatrix} \widehat{\mathbf{r}} \\ \mathbf{r}_{I} \\ \overline{\mathbf{c}} \end{bmatrix}$$
(3.10 - 2)

where  $\hat{\mathbf{K}}$  is the stiffness matrix with row and column *I* removed. The hats over vectors also indicate that row *I* has been deleted.  $\hat{\mathbf{f}}^{I}$  is column *I* of the stiffness, with  $K_{II}$  being the diagonal element for freedom *I*. The same partitioning also applies to the external force  $\mathbf{f}^{ext}$  and the constraint equation c.

If we formally solve the first of (58) for  $\delta d$  and substitute the result into the remaining two equations, we obtain the following two-by-two nonsymmetric system of equations for  $\delta d_I$  and  $\delta \lambda$ :

$$\begin{bmatrix} K_{II} - (\widehat{\mathbf{f}}^{I})^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{I} & (\widehat{\mathbf{f}}^{I})^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{ext} - f_{I}^{ext} \\ c_{I} - \widehat{\mathbf{c}}^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{I} & \widehat{\mathbf{c}}^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{ext} \end{bmatrix} \begin{bmatrix} \delta d_{I} \\ \delta \lambda \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{I} - (\widehat{\mathbf{f}}^{I})^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{r}} \\ \overline{\mathbf{c}} - \widehat{\mathbf{c}}^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{r}} \end{bmatrix}$$
(3.10 - 3)

One additional forward/backsolve is required with this algorithm. After each factoring of the stiffness matrix, one must solve the pair

$$\widehat{\mathbf{K}}\delta\widehat{\mathbf{v}} = \widehat{\mathbf{f}}^{I}$$

$$\widehat{\mathbf{K}}\delta\widehat{\mathbf{w}} = \widehat{\mathbf{f}}^{e^{zt}}$$

$$(3.10-4)$$

for vector  $\delta \hat{\mathbf{v}}$  and  $\delta \hat{\mathbf{w}}$ .  $\delta \hat{\mathbf{w}}$  corresponds to  $\delta \hat{\mathbf{d}}$  in the second of (11).  $\delta \hat{\mathbf{d}}$  is also used for  $\delta \hat{\mathbf{w}}$  in the description of the NL\_STATIC\_2 algorithm. The following vector must be solved every iteration:

$$\widehat{\mathbf{K}}\widehat{\mathbf{u}} = \widehat{\mathbf{r}} \tag{3.10-5}$$

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This equation corresponds to the first of (11). The two-by-two system (59) becomes

$$\begin{bmatrix} K_{II} - (\widehat{\mathbf{f}}^{I})^{T} \delta \widehat{\mathbf{v}} & (\widehat{\mathbf{f}}^{I})^{T} \delta \widehat{\mathbf{w}} - f_{I}^{ext} \\ c_{I} - \widehat{\mathbf{c}}^{T} \delta \widehat{\mathbf{v}} & \widehat{\mathbf{c}}^{T} \delta \widehat{\mathbf{w}} \end{bmatrix} \begin{bmatrix} \delta d_{I} \\ \delta \lambda \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{I} - (\widehat{\mathbf{f}}^{I})^{T} \widehat{\mathbf{u}} \\ \overline{\mathbf{c}} - \widehat{\mathbf{c}}^{T} \widehat{\mathbf{u}} \end{bmatrix}$$

$$(3.10 - 6)$$

$$\begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} \delta d_{I} \\ \delta \lambda \end{bmatrix} = \begin{bmatrix} R_{1} \\ R_{2} \end{bmatrix}$$

We have rewritten the first of (62) with the notation used in the description of the algorithm, where the coefficients  $A_{ij}$  and  $R_i$  are the reduced Riks coefficients and residuals, respectively; a comparison of the first of (62) with the second yields their values.

Once  $\delta d_I$  and  $\delta \lambda$  are known, the full solution becomes the sum

$$\widehat{\delta}\mathbf{d} = \widehat{\mathbf{u}} - \delta d_I \delta \widehat{\mathbf{v}} + \delta \lambda \delta \widehat{\mathbf{w}} \qquad (3.10 - 7)$$

 $\delta \hat{\mathbf{d}}$  is then expanded by one freedom and the explicit value  $\delta \mathbf{d}_I$  previously solved for is inserted. The advantage of (62) is that this system, in contrast to (8) is never singular at a limit point, provided that the component *I* does not correspond to a zero entry in the tangent displacement vector at the critical point.

# **3.10.9.3** Selecting Freedom I and the Vector $\hat{f}^I$

A simple method for ensuring a nonsingular reduced stiffness  $\hat{\mathbf{K}}$  is to look at the difference between the last converged solution and the predicted solution for the current step. We choose that particular component with the largest absolute value; its index becomes I, and the stiffness column belonging to that freedom becomes  $\hat{\mathbf{f}}^I$  with diagonal  $K_{II}$ . In practice, after we have selected the proper index, we generate an elementary vector that is zero except for unity in position I.  $\mathbf{f}^I$  is just the product of the stiffness matrix with the elementary vector.  $\hat{\mathbf{f}}^I$  is this same column with row I deleted.

### 3.10.9.4 Constructing the Solution

Immediately after the stiffness matrix has been factored, we solve (60) for  $\delta \hat{\mathbf{v}}$  and  $\delta \hat{\mathbf{w}}$ . Solution for  $\delta \hat{\mathbf{w}}$  is treated like the corresponding solution for  $\delta \mathbf{d}$  in (37), with specified displacements being handled exactly as in NL\_STATIC\_1. The only difference is that the new stiffness has one additional freedom held fixed. In practice, entry *I* is added to the specified displacement list (and if *I* has changed since the last step, the previous freedom is "released" or "unfixed"). The solutions  $\delta \hat{\mathbf{v}}, \delta \hat{\mathbf{w}}$  are full system vectors with a zero in the *I*th slot. At each iteration, a new basic displacement increment  $\hat{\mathbf{u}}$  is also solved for (62). After solution of the reduced two-by-two system (62), (63) is used to construct the full displacement increment. This is followed by direct insertion of the increment for component *I*.

# 3.10.9.5 Computing the Stiffness Determinant

The determinant of the stiffness  $\widehat{\mathbf{K}}$  is not equal to that of the original, unconstrained stiffness. However, since our algorithm is a special case of a block Gauss elimination, it is a simple matter to compute it. The full determinant of the stiffness matrix is the product

$$Det(\mathbf{K}) = Det(\widehat{\mathbf{K}})A_{11} \qquad (3.10-8)$$

Note that when  $A_{11}$  vanishes, the stiffness determinant also vanishes. However, the system (62) is still nonsingular whenever the off diagonal reduced coefficients are nonzero (the extended system).

#### **3.10.10 ALGORITHM FLOW CHART**

#### **General Algorithm**

(1) STEP LOOP: n = 2, 3, 4 ... (step = n+1) (1.1) Extrapolate Solution for Predictor call EXTRAP ( $\Delta \ell_{n+1}, \Delta \ell_n, \Delta \ell_{n-1} \rightarrow c_n, c_{n-1}, c_{n-2}$ )  $\lambda_{n+1}^{(1)} = c_n \lambda_n + c_{n-1} \lambda_{n-1} + c_{n-2} \lambda_{n-2}$   $d_{n+1}^{(1)} = c_n d_n + c_{n-1} d_{n-1} + c_{n-2} d_{n-2}$   $\Delta d_{n+1}^{(1)} = d_{n+1}^{(1)} - d_n$  ( $\mathbf{T}_{n+1}^{(1)} = \mathbf{R}(\Delta d_{n+1}^{(1)})\mathbf{T}_n$ )  $\Delta \lambda_{n+1}^{(1)} = \lambda_{n+1}^{(1)} - \lambda_n$ 

(1.2) Form and Assemble Stiffness

(1.3) Find Index of Largest Tangent Component Extract Column I from Stiffness (including diagonal)

$$I = \operatorname{Arg} \{ \max_{\forall k} |\Delta \mathbf{d}(k)_{n+1}^{(1)} | \}$$
$$\widehat{\mathbf{f}}^{I} = \mathbf{K} \mathbf{e}_{I}$$

(1.4) Fix freedom I to give constrained  $\mathbf{K}(\hat{\mathbf{K}})$ 

(1.5) Solve for Tangential Displacement based on Predictor

$$\delta \widehat{\mathbf{d}} = \widehat{\mathbf{K}}^{-1}(\mathbf{d}_{n+1}^{(1)}) \left[ \widehat{\mathbf{f}}^{ext} + \mathbf{K}^{us} \widehat{\mathbf{d}}^{s} \right]$$

(1.6) Solve for perturbation displacement  $\delta \hat{\mathbf{v}}$ 

$$\delta \widehat{\mathbf{v}} = \widehat{\mathbf{K}}^{-1}(\mathbf{d}_{n+1}^{(1)}) \widehat{\mathbf{f}}^{I}$$

(1.7) Solve for Riks reduced system coefficients

$$\begin{split} \delta \widehat{\boldsymbol{v}}_{I} &= \boldsymbol{0}.\\ \delta \widehat{\boldsymbol{d}}_{I} &= \boldsymbol{0}.\\ A_{11} &= \widehat{\boldsymbol{f}}_{I}^{I} - \widehat{\boldsymbol{f}}^{I} \cdot \delta \widehat{\boldsymbol{v}}\\ A_{12} &= -\widehat{\boldsymbol{f}}_{I}^{ezt} + \widehat{\boldsymbol{f}}^{I} \cdot (\delta \widehat{\boldsymbol{d}} - \widehat{\boldsymbol{d}}^{s})\\ A_{21} &= 2(\Delta \boldsymbol{d}(I)_{n+1}^{(1)} - \Delta \boldsymbol{d}_{n+1}^{(1)} \cdot \delta \widehat{\boldsymbol{v}})\\ A_{22} &= 2\Delta \boldsymbol{d}_{n+1}^{(1)} \cdot \delta \widehat{\boldsymbol{d}} \end{split}$$

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(1.7) Form Residual based on Predictor

$$\mathbf{r}_{n+1}^{(1)} = \mathbf{r}(\mathbf{d}_{n+1}^{(1)}, \lambda_{n+1}^{(1)}) = \lambda_{n+1}^{(1)} \hat{\mathbf{f}}^{ext} - \mathbf{f}^{int}(\mathbf{d}_{n+1}^{(1)})$$
  
call CHK\_CONV (  $\mathbf{r}_{n+1}^{(1)}, \Delta \mathbf{d}_{n+1}^{(1)}, \epsilon_{ref} \rightarrow \hat{\epsilon}^{(1)}, \epsilon_{ref}$  )

(2) ITERATION LOOP: i = 1, 2, ... (iter = i+1 = 2, 3, ...)

(2.1) Solve for Basic Iterative Displacement Change

$$\delta \overline{\mathbf{d}} = \widehat{\mathbf{K}}^{-1}(\mathbf{d}_{n+1}^{(1)}) \mathbf{r}_{n+1}^{(i)}$$

(2.2) Solve for Reduced r.h.s.

 $\delta \vec{d}_I = 0.$ 

$$R_{1} = \mathbf{r}(I)_{n+1}^{(i)} - \mathbf{\widehat{f}}^{I} \cdot \delta \mathbf{\overline{d}}$$
  

$$R_{2} = \Delta \ell^{2} - \Delta \mathbf{d}_{n+1}^{(i)} \cdot \Delta \mathbf{d}_{n+1}^{(i)} - 2\Delta \mathbf{d}_{n+1}^{(i)} \cdot \delta \mathbf{\overline{d}}$$

(2.3) Solve 2 x 2 Reduced system:

ļ	<b>A</b> <sub>11</sub>	$A_{12}$	$\delta d_I$		$\begin{bmatrix} R_1 \end{bmatrix}$	
	$A_{21}$	$\begin{bmatrix} A_{12} \\ A_{22} \end{bmatrix}$	δλ	=	$\begin{bmatrix} R_2 \end{bmatrix}$	

(2.4) Update Displacements and Load Factor

$$\delta \mathbf{d} = \delta \mathbf{\overline{d}} + \delta \lambda \, \delta \mathbf{\widehat{d}} - \delta d_I \delta \mathbf{\widehat{v}}$$
  

$$\mathbf{d}_{n+1}^{(i+1)} = \mathbf{d}_{n+1}^{(i)} + \delta \mathbf{d} \qquad (\mathbf{T}_{n+1}^{(i+1)} = \mathbf{R}(\delta \mathbf{d}) \, \mathbf{T}_{n+1}^{(i)})$$
  

$$\Delta \mathbf{d}_{n+1}^{(i+1)} = \Delta \mathbf{d}_{n+1}^{(i)} + \delta \mathbf{d}$$
  

$$\lambda_{n+1}^{(i+1)} = \lambda_{n+1}^{(i)} + \delta \lambda$$

(2.4) Compute New Residual

$$\mathbf{r}_{n+1}^{(i+1)} = \mathbf{r}(\mathbf{d}_{n+1}^{(i+1)}, \lambda_{n+1}^{(i+1)}) = \lambda_{n+1}^{(i+1)} \mathbf{\hat{f}}^{ext} - \mathbf{f}^{int}(\mathbf{d}_{n+1}^{(i+1)})$$

(2.5) Check Convergence

call CHK\_CONV (  $\mathbf{r}_{n+1}^{(i+1)}, \delta \mathbf{d}, \hat{\epsilon}^{(i)}, \epsilon_{ref}, \hat{\epsilon}_{tol}, \text{num_div} \rightarrow \hat{\epsilon}^{(i+1)}, \langle \text{CONVERGED} \rangle, \langle \text{DIVERGED} \rangle$ )

if (  $\langle CONVERGED \rangle$  ) then

num\_iters\_required = iter

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```
\begin{array}{l} \Delta \ell_{n+2} = \Delta \ell_{n+1} \Big( \frac{\text{num\_iters\_desired}}{\text{num\_iters\_required}} \Big) \\ n \leftarrow n+1 \\ \text{go to (1) STEP LOOP} \\ \text{elseif ( <DIVERGED> .or. (iter > max\_iters) ) then} \\ \text{if ( num\_cuts < max\_cuts ) then} \\ \Delta \ell_{n+1} = \Delta \ell_{n+1}/2 \\ \text{num\_cuts = num\_cuts + 1} \\ \text{go to (1.3)} \\ \text{else} \\ \text{STOP} \\ \text{endif} \\ \text{else} \\ i \leftarrow i+1 \\ \text{go to (2) ITER LOOP} \\ \text{endif} \end{array}
```

# Starting Procedure: Step 1 (n=0)

Replace Algorithm Steps (1.1)-(1.2) by:

 $d_{1}^{(0)} = 0$   $\delta \widehat{d} = \mathbf{K}^{-1}(d_{1}^{(0)}) \left[ \widehat{\mathbf{f}}^{ezt} + \mathbf{K}^{us} \widehat{\mathbf{d}}^{s} \right]$   $\lambda_{1}^{(1)} = \lambda_{start} \quad (\text{user specified})$   $\Delta \lambda_{1}^{(1)} = \lambda_{1}^{(1)}$   $\Delta \ell_{1} = \Delta \lambda_{1}^{(1)} \| \delta \widehat{\mathbf{d}} \|$   $\Delta d_{1}^{(1)} = \Delta \lambda_{1}^{(1)} \delta \widehat{\mathbf{d}}$  $d_{1}^{(1)} = \Delta d_{1}^{(1)}$ 

(Also, form  $\mathbf{K}(\mathbf{d}_1^{(1)})$  before next solve. )

# Starting Procedure: Step 2 (n=1)

Replace Algorithm Steps (1.1)-(1.2) by:

$$d_{2}^{(0)} = d_{1}$$

$$\delta \widehat{d} = K^{-1}(d_{2}^{(0)}) \left[ \widehat{f}^{ezt} + K^{us} \widehat{d}^{s} \right]$$

$$\Delta \lambda_{2}^{(1)} = \Delta \ell_{2} / \| \delta \widehat{d} \|$$

$$\lambda_{2}^{(1)} = \lambda_{1} + \Delta \lambda_{2}^{(1)}$$

$$\Delta d_{2}^{(1)} = \Delta \lambda_{2}^{(1)} \delta \widehat{d}$$

$$d_{2}^{(1)} = d_{1} + \Delta d_{2}^{(1)} \quad (\mathbf{T}_{2}^{(1)} = \mathbf{R}(\Delta d_{2}^{(1)} \mathbf{T}_{1}))$$

( But don't reform  $K(d_1^{(1)})$  until step 3. )

# NOTATION

d	Displacement vector.
δd	Iterative change in <b>d</b> .
$\Delta \mathbf{d}$	Incremental (load-step) change in d.
$\mathbf{d}_n^i$	Displacement vector at iteration $i$ of step $n$ .
$\Delta \mathbf{d}_n^i$	Incremental (step) change in d. $\Delta d_{n+1}^{(i+1)} = d_{n+1}^{(i)} - d_n$
δ <b>d</b>	Tangential displacement = $\mathbf{K}^{-1} \hat{\mathbf{f}}^{ext}$
$\Delta \ell$	Incremental arclength (step) parameter.
f <sup>ezt</sup>	External force vector — base load.
f <sup>int</sup>	Internal force vector.
$\hat{\mathbf{f}}^{I}$	I'th column of K
r	Residual force vector.
К	Stiffness matrix.
Ŕ	Stiffness matrix with I'th row and column deleted
Ŷ	Solution vector corresponding to $\widehat{\mathbf{K}}^{-1}\widehat{\mathbf{f}}^{I}$
$\delta \overline{\mathbf{d}}$	Basic (fixed-load) iterative change in d¿
$\delta d^*$	Linear combination of $\delta \overline{\mathbf{d}}$ and $\delta \widehat{\mathbf{d}}$ .
$A_{ij}$	Advanced-Riks reduced system coefficients
R <sub>i</sub>	Advanced-Riks reduced residuals
num_cuts	Number of times load step has been cut in half at current step.
num_div	Number of consecutive iterations at which divergence occurs.
Cn	Extrapolation coefficient corresponding to step $n$ .
ê	Relative error in energy norm.
ε	Absolute error in energy norm.
Eref	Reference value of $\epsilon$ ; initialized as zero.
Etol	Relative error tolerance (default: $10^{-4}$ ).
λ	Load factor.
$\Delta\lambda$	Incremental (load-step) change in $\lambda$ .
K"	Stiffness submatrix coupling specified (s) displacement components with force components corresponding to unknown (u) displacements.
<b>d</b> '	Base value of specified displacement vector.
ď	Current value of specified displacement vector. $\mathbf{d}^{*} = \lambda  \widehat{\mathbf{d}}^{*}$ .

#### 3.10.11 PROCEDURE LISTING

```
*procedure NL_STATIC_2 ( --
                     beg_step =1 ; -- . Starting step number (>0)
                     max_steps=1 ; -- . Maximum steps to compute
                     max_iters=9 ; -- . Maximum iterations per step
                     des_iters=4 ; -- . Number of iterations desired
                     fac_steps=1 ; -- . Steps_per_refactoring
                     max_cuts=3 ; -- . Maximum number of step cuts
                     tol_e=1.E-3 ; -- . Energy error tolerance
                     beg_load ; -- . Starting load factor (>0.)
                     max_load ; -- . Upper_bound on load factor
                     min_load
                                ; -- . Lower_bound on load factor
                     path_scale=1.; -- . Path_inc scl_factor (restart)
                     extrapolate=<true> ; --
                     line_search=1.;-- . Initial line-search parameter
                     debug=<FALSE>; -- . Debug_print switch
                     NL_GEON = 2 ; -- . Geom. Nonlin. Level (1|2)
                     COROTATION=1 ; -- . Corotational Flag (leave on !!)
                     adv_riks = <false> ; -- . Advanced RIKS flag.
                     Nominal_DB = NOMINAL.GAL ; -- . Selected Output
                     Nominal_DS = RESPONSE.HISTORY ; --
                     N_SELECT ; SEL_NODES; SEL_DOPS --
                   )
 *Remark
            -----
                            -------
 *Remark |
 *Remark
                           NL_STATIC_1
*if < [adv_riks] > /then
    *rezark
                             ADVANCED RIKS
*endif
 *Remark
 *Remark
                 CSM Testbed Procedure for Nonlinear Statics:
*Remark
*Romark
                    o Corotational Newton/Raphson algorithm
*Renark
                    o Linearized Crisfield/Riks arc-length control
 *Remark
                    o Applied forces and/or displacements
 Benark
 *Remark
                 Authors: G.M. Stanley and C.C. Rankin
 *Remark
                 Version: MAR-03-1988
*Remark |
                                                                    1
 *Remark
. INITIALIZATION
#def/i ns_overwrite == <true>
*def/i debug
                 == [debug]
*def/i max_step == <[beg_step]+[max_steps]-1>
                  == [des_iters]
*def/i num_iters
*def/d path_scale == [path_scale]
*def/i extrapolate == [extrapolate]
 +def/a NOM_DB
                  == [Nominal_DB]
 #def/a NOM_DS
                  == [Nominal_DS]
```

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```
*def/i N_SELECT
                   == [N_SELECT]
*def/i SEL_NODES[1:<N_SELECT>] == [SEL_NODES]
*def/i SEL_DOFS[1:<N_SELECT>] == [SEL_DOFS]
*def/i NL_GEOM
                  == [NL_GEOM]
*def/i COROTATION == [COROTATION]
*CALL DEFNS ( STEP = [BEG_STEP]; ITER = 0 )
*IF < [BEG_STEP] /EQ 1 > /THEN
   *Remark INITIALIZATION:
   *call INITIAL
+ENDIF
. BEGIN STEP_LOOP
*D0 :STEP_LOOP $n = 0, <[max_steps]-1>
    *def/i step == < [beg_step]+<$n> >
    *def/i pass == 1
    *def/i tot_iters == 1
    *if < <<step> /gt 2> /and <<extrapolate> /eq <true>> > /then
       #def/i extrap_this_step == <true>
    +else
       *def/i extrap_this_step == <false>
    *endif
    *Remark
    *remark _____
                                     _____
    *remark
    *Remark
                 BEGINNING STEP <STEP>
    *remark _____
    *remark
    *call DEFNS ( step = <step>; iter = 1 )
    :NEW_PASS
                       . Re-entry point for step-size reduction
    [XQT VEC
   *if < <<step> /gt 1> /and <<pre>yeq 1> > /then
     #def/d path_inc == < <path_scale>#<path_inc_n> >
     *Remark New PATH INCREMENT = <path_inc>
   *endif
. . . Generate Displacement PREDICTOR
    *if <extrap_this_step> /then
       *Remark Predicting displacements/load via EXTRAPOLATION
       *call EXTRAP ( dx_np1 = <path_inc> ; cx_n = cx_n
                                                           ; --
                      dr_n = <path_inc_n> ; cr_nm1 = cr_nm1; --
                      dr_nm1 = <path_inc_nm1>; cr_nm2 = cr_nm2 )
       *def/d lam_np1_i == < (<cr_n>*<lam_n>)
                                                  ---
                            + (<cr_nm1>*<lam_nm1>) --
                            + (<cr_nm2> + <lam_nm2>) >
        <d_np1_i> <- <cx_n> <d_n> + <cx_nai> <d_nai>
        <d_np1_i> <- <d_np1_i> + <cx_nm2> <d_nm2>
        <d_inc_i> <- <d_np1_i> - <d_n>
         ROTATE <T_n> * <d_inc_i> -> <T_np1_i>
    *else
       *Remark Using Previous Step as Displacement Predictor
       *remark
```

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```
*remark
                    Last displacement dataset : <d_n>
       *remark
       *def lam_np1_i == <lam_n>
        <d_np1_i> <- <d_n>
        <T_np1_i> <- <T_n>
        <d_inc_i> <- <d_n>
    *endif
    *if < <spec_disp_flag> > /then
       SPECIFY <lam_np1_i> <d_ext> -> <d_np1_i>
    *endif
 . . Form Stiffness based on Predictor
    #if < < <pre>yeq 1 > /or <extrap_this_step> > /then
       *call FORM_STIFF (displacement = <d_np1_i>; --
                         rotation
                                      = <T_np1_i>; --
                                      = \langle K_{asm} \rangle )
                          stiffness
                                                         . output
. . . Find largest tangent component I = <ndef> <fd>
. . . Extract corresponding column of system matrix
. . . Specify freedom NDEF, FD as constrained to zero
     *if <adv_riks> /then
         *if <<step> /le 1> /then
             *def/i ndef==0
          *else
             *call STIF_COLMN
         *endif
      *else
          *def/i ndef==0
      *endif
 . . Factor stiffness with the added constraint
       *call FACT_STIFF
. . . Solve for Tangential Displacement
        *call TANDIS ( step = <step> ; iter = 1 ; --
                      displacement = <d_np1_i> ; --
                       rotation
                                   = <T_np1_i> ; --
                       load_factor = <lam_np1_i>; --
                                   = [max_load] ; --
                       max_load
                       external_force = <F_ext> ; --
                       internal_force = <F_int> ; --
                       specified_disp = <d_ext> ; --
                       tangent_force = <F_T>
                                               ; --
                       tangent_disp = <delta_T> )
. . . Solve for incremental displacement based on stiffness column I
      #if <<ndef> /gt 0> /then
```

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```
*call SOLVE ( RHS = <K_I>; SOLN = <delta_I> )
     *endif
    *endif
. . . Compute Magnitude of Tangential Displacement
     NORM <delta_T> -> mag_delta_T . magnitude of tang. displacement
. . Predict Load Factor and Path Increment for Current Step
   *if < <step> /eq 1 > /then
      *if < <pass> /eq 1 > /then
         #def/d lam_np1_i == [beg_load]
         *def/d lam_inc == <lam_np1_i>
         *def/d path_inc ** < <lam_inc>*<mag_delta_T> >
         #def/i load_dir == <SIGN(1.;<lam_inc>)>
      *else
         *def/d lam_inc == < <pre>containc>/<mag_delta_T> >
         #def/d lam_np1_i == <lam_inc>
      *endif
   *elseif < <step> /gt 1 > /then
. . . Path_Increment based on Iterative Performance, Set Direction
      *if < <sign_det> /ne <sign_det_n> > /then
         *def/i load_dir == < -1.*<load_dir_n> >
      *else
         #def/i load_dir == <load_dir_n>
      *endif
. . . Compute Load_Increment
      *if <extrap_this_step> /then
         #def/d lam_inc == < <lam_np1_i> - <lam_n> >
      +else
          *Remark USING CONSTRAINT EQN TO PREDICT LOAD AT STEP <step>
          *def/d lam_inc == << <pre>cpath_inc>/<mag_delta_T> >*<load_dir>>
          #def/d lam_np1_i == <<lam_n>+<lam_inc>>
      *endif
   *endif
   *Remark LAMBDA_<step>^ 1 = <lam_np1_i> , LAMBDA_INC = <lam_inc>
   *if < <lam_np1_i> /gt [max_load] > /then
      *Remark MAXIMUM LOAD_LEVEL OBTAINED.
      *jump to :EXIT
   *elseif < <lam_np1_i> /le [min_load] > /then
      *Remark MINIMUM LOAD_LEVEL OBTAINED.
      *jump to :EXIT
   *endif
   *if <<extrap_this_step> /eq <false>> /then
      *Remark MODIFYING PREDICTOR VIA PATH-CONSTRAINT
       <d_inc_i> <- <lam_inc> <delta_T>
       <d_np1_i> <- <d_n> + <d_inc_i>
       ROTATE <T_n> * <d_inc_i> -> <T_np1_i>
```

```
*if < <spec_disp_flag> > /then
          SPECIFY <lam_np1_i> <d_ext> -> <d_np1_i>
       *endif
   *endif
. . . Compute 2 x 2 system coefficients
        *call TWO_BY_TWO (free = <ndef>)
 . . Form (Stress and) Residual_Force Vector
    *call RESIDUAL ( step
                              = <step>
                                          ; -- . input
                     iter
                              = 1
                                           ; --
                                                 ; ---
                     displacement = <d_np1_i>
                     rotation = <T_np1_i>
                                                 ; ---
                     load_factor
                                   = <lam_np1_i> ; --
                                                ; --
                     external_force = <F_ext>
                     internal_force = <F_int>
                                                    ; --
                     residual_force = <R_np1_i> ) . output
. . . Initialize Convergence Criteria
    *call CHKCONV ( STEP = 1 ; ITER = 1
                                                       ; --
                    Residual_force = <R_np1_i>
                                                     ; --
                    displacement_inc = <d_inc_i>
                                                      ; --
                    load_inc
                                   = <lam_inc>
                                                       ; --
                    relaxation
                                    = s)
    *if <CONVERGENCE> /then
       #def/d lam_np1_ip1 == <lam_np1_i>
       *jump to :CONVERGED
    *endif
. -- BEGIN ITERATION LOOP
   *D0 :ITER_LOOP $i = 1, [max_iters]
         *def/i iter == <<$i>+1>
         *def/i tot_iters == <<tot_iters>+1>
         *if < <<step> /eq 1> /and <<iter> /eq 2> > /then
           *call FORM_STIFF (displacement = <d_np1_i>; --
                             rotation = <T_np1_i>; --
                                       = <K_asu> )
                             stiffness
                                                           . output
. . . Find largest tangent component I = <ndef> <fd>
. . . Extract corresponding column of system matrix
. . . Specify freedom NDEF, FD as constrained to zero
           *if <adv_riks> /then
               *if <<step> /le 1> /then
                   *def/i ndef==0
                *else
                   *call STIF_COLMN
               *endif
           *else
```

```
*def/i ndef==0
           *endif
 . . Factor stiffness with the added constraint
           *call FACT_STIFF
      . . . Update Tangential Displacement if Specified Displs., etc.
            *if < <spec_disp_flag> /or <live_load_flag> > /then
               *Remark o Recomputing Tangential Displacement
               *call TANDIS ( step = <step> ; iter = <$i>; --
                              displacement = <d_np1_i> ; --
                              rotation
                                          = <T_np1_i> ; ---
                              load_factor = <lam_np1_i>; --
                                          = [max_load] ; --
                              max_load
                              external_force = <F_ext> ; --
                              internal_force = <F_int> ; --
                              specified_disp = <d_ext> ; --
                              tangent_force = <F_T>
                                                      ; --
                              tangent_disp = <delta_T> )
             *endif
. . . Solve for incremental displacement based on stiffness column I
            #if <<ndef> /gt 0> /then
               *call SOLVE ( RHS = <K_I>; SOLN = <delta_I> )
             *endif
. . . Compute 2 x 2 system coefficients
            *call TWO_BY_TWO (free = <ndef>)
           *endif
  .... Compute Basic Displacement Iteration (delta_B)
         *call SOLVE ( RHS = <R_np1_i>; SOLN = <DELTA_B> )
  . . . . Compute New Load-Factor and Displacement Component I
      . . Advanced Riks (2 x 2) system.
          DOT <delta_B> * <d_inc_i> -> db_DOT_Dd
          DOT <d_inc_i> * <d_inc_i> -> Dd_DOT_Dd
          *def/d B_2 == < <pre>containc>*>path_inc> >
          *def/d B_2 == < <B_2> - <Dd_DOT_Dd> - <2.0*<db_DOT_Dd>> >
          *if <<ndef> /gt 0> /then
              COMPONENT <ndef> <fd> <r_np1_i> -> r_I
             DOT <delta_B> * <K_I> -> db_DOT_K_I
             *def/d R_1 == <<r_I> - <db_DOT_K_I>>
        . Solve 2 x 2 RIKS system
```

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```
#def/d Bdet = <<<i_11> + <i_22>> - <<i_12> + <i_21>>>
            *def/d dd_I = <<<R_1> * <A_22>> - <<R_2> * <A_12>>>
            #def/d dlam = <<<4_11> # <R_2>> - <<4_21> # <R_1>>>
            *def/d dd_I = <<dd_I> / <Rdet>>
            #def/d dlam = <<dlam> / <Rdet>>
         **
 . . . . Solve simple 1-D RIKS system for load factor (Normal Riks)
            *def/d dlam = <<R_2>/<A_22>>
         *endif
. . . . . Update Load Factor
         #def/d lam_np1_ip1 = < <lam_np1_i> + <dlam> >
*remark
*remark *REMARK RANKIN'S ROOT SELECTION:
*remark Dd # Dd # <Dd_dot_Dd>
*remark dlam = <Dlam>
*remark lambda = <lam_np1_ip1>
*remark *remark
        :LOAD_LEVEL
. . . . Update Increments
                    <- <delta_B> + <dlam> <delta_T>
          <delta>
          #if <<ndef> /gt 0>/then
. . . . . . . (Advanced Riks Only)
            <delta>
                        <- <delta> - <dd_i> <delta_I>
. . . . . . . Set last component
            COMPONENT <ndef> <fd> <delta> <- <dd_I>
          *endif
. . . . Update Displacements, Rotations
          <d_np1_ip1> <- <d_np1_i> + <delta>
          ROTATE <T_np1_i> * <delta> ' -> <T_np1_ip1>
          <d_inc_ip1> <- <d_inc_i> + <delta>
         *if < <spec_disp_flag> > /then
          SPECIFY <lam_np1_ip1> <d_ext> -> <d_np1_ip1>
         *endif
         *if < <DEBUG> > /then
           *print 1, <d_np1_ip1>
            *print 1, <T_np1_ip1>
         *endif
. . . . FORM (STRESSES AND) RESIDUAL_FORCE
```

```
*call RESIDUAL ( step
                                = <step>
                                          : --
                                                   . input
                      iter
                               = <iter>
                                            : --
                       displacement = <d_np1_ip1>
                                                    ; ---
                      rotation = <T_np1_ip1>
                                                    ; ---
                      load_factor
                                      = <lam_np1_ip1> ; --
                      external_force = <f_ext> ; --
internal_force = <F int> : --
                       internal_force = <F_int>
                                                      ; ---
                      residual_force = <R_np1_ip1> ) . output
    . CHECK CONVERGENCE
      *call CHKCONV
                     ( step
                                 = <step>
                                                : -- . input
                                 = <iter>
                                               ; --
                       iter
                       Residual_force = <R_np1_ip1> ; --
                       displacement_inc = <delta>
                                                    ; --
                       load_inc = 0.0 ; -- . for error norm
                       tol_e
                                      = [tol_e] ; --
                       max_iters
                                      = [max_iters] ; --
                       convergence = CONVERGENCE; -- . output
                       divergence = DIVERGENCE ; --
                       relaxation = s )
   #if <<CONVERGENCE> /eq <TRUE>> /then
    *jump to :CONVERGED
   *elseif <<DIVERGENCE> /eq <TRUE>> /then
    *if < <pass> /le [max_cuts] > /then
       *jump to :REPEAT
     *else
       *Remark Maximum number of automatic step cuts exhausted.
        *jump to :DIVERGED
     *endif
   *endif
   #def/d lam_np1_i == <lam_np1_ip1>
:ITER_LOOP
:NEUTRAL
*if < <pass> /le [max_cuts] > /then
  *jump to :REPEAT
*else
  *Remark Maximum number of automatic step cuts exhausted.
*endif
                NON-CONVERGENCE AT STEP <stop>. REVISE STRATEGY.
*Remark
*jump to :EXIT
:REPEAT
*def/i pass
                == < <pass>+1 >
*def path_inc == < <path_inc>/2. >
*Remark
*Remark CONVERGENCE DIFFICULTIES; REPEATING STEP <stop>
 *Remark with reduced path_increment = <path_inc>
*Remark Pass: <pass>
*jump to :NEW_PASS
:DIVERGED
*Remark
                DIVERGENCE AT STEP <STEP>. REVISE STRATEGY.
*jump to :EXIT
```

```
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```

```
: CONVERGED
                    CONVERGENCE AT STEP <STEP>.
   *Remark
   :NEXTSTEP
   *def/i num_iters
                      == <iter>
   *def/d path_scale == <[des_iters]/<num_iters>>
   *def/d path_inc_nm1 == <path_inc_n>
   #def/d path_inc_n == <path_inc>
                    == <lam_nmi>
   *def/d lam_nm2
                    == <lam_n>
   *def/d lam_nm1
                    == <lam_np1_ip1>
   *def/d lam_n
   *def/i sign_det_n == <sign_det>
   *def/i load_dir_n == <load_dir>
   *call POSTSTEP ( step=<step>; iter=<iter> )
:STEP_LOOP
:EXIT
+end
. =DECK CHKCONV
                                       ; -- . input
*procedure CHKCONV
                    ( STEP
                      ITER
                                       ; --
                      DISPLACEMENT_INC ; --
                      RESIDUAL_FORCE ; --
                      LOAD_INC
                                       : --
                      TOL_E
                                       ; --
                      MAX_ITERS
                                       ; --
                      CONVERGENCE=CONVERGENCE ; -- . output
                      DIVERGENCE = DIVERGENCE ; --
                      relaxation = s )
[XOT VEC
 . Initialize
   *def/i [CONVERGENCE] == <FALSE>
   *def/i [DIVERGENCE] == <FALSE>
   *if < [ITER] /gt 1 > /then
      *def/d12.4 ERR_E_I == <ERR_E_IP1>
   *endif
. . Compute Current Incremental Energy Norm
   DOT [RESIDUAL_FORCE] * [DISPLACEMENT_INC] -> INC_E_IP1
   *if < [ITER] /le 1 > /then
      *if < <ABS(<INC_E_IP1>)> /gt <REF_E> > /then
         *def/d12.4 REF_E == <ABS(<INC_E_IP1>)>
      *endif
      *def/17.2 [RELAXATION] == 1.0
      *def/i num_diverges == 0
   *endif
. . Compute Error Norms
   *def/d12.4 ERR_E_RAW == < <INC_E_IP1>/<REF_E> >
   *def/d12.4 ERR_E_IP1 == < <ABS(<ERR_E_RAW>)>^ .5 >
```

```
. . Check for displacement convergence
  *if < <ERE_E_IPi> /le [TOL_E] > /then
. . . Step Converged
     *DEF/I [CONVERGENCE] == <TRUE>
     *jump to :BOTTOM_LINE
   *endif
   #if < [ITER] /le 1 > :BOTTOM_LINE
. . . Step Not Converged; Check for Divergence
     *IF < <ERR_E_IP1>/<ERR_E_I> /GT 1.0 > /THEN
        *def num_diverges == < <num_diverges>+1 >
        #if <<num_diverges> /gt 1 > /then
           *DEF/I [DIVERGENCE] == <TRUE>
        *ENDIF
     +ENDIF
. . Select Relaxation (i.e., line-search) Parameter: s
  *def/f7.2 ls = <[relaxation]>
  *if < <<err_e_ip1>/<err_e_i>> /gt .5 > /then
      COMP <max_nod> <max_dof> [DISPLACEMENT_INC] -> max_d_ip1
     #if < <max_d_ip1>*<max_d_i> /lt 0 > /then
        *def ls = < <ls>-.3 >
        +def ls = <MAX(<ls>;.4)>
     *elseif < <ABS(<max_d_ipi>)> /lt <ABS(<max_d_i>)> > /then
        #def ls = < <ls>+.4 >
        *def ls = <HIN(<ls>;2.)>
     *else
        *def ls = 1.0
     *endif
  *endif
  *def/f7.2 [relaxation] == <ls>
:BOTTON_LINE
NORM/MAX [DISPLACEMENT_INC] -> max_d_i max_mod max_dof
NORM/MAX [RESIDUAL_FORCE]
                           -> max_f_i max_nod_f max_dof_f
*if < [ITER] /LE 1 > /then
 *def/e12.4 load_factor = <lam_np1_i>
+else
  *def/e12.4 load_factor = <lam_np1_ip1>
*endif
*remark
*remark _____
                          *remark ITER=[ITER] LD=<load_factor> ERR=<err_e_ipi> REF=<ref_e>
           delta_d_max=<max_d_i> node=<max_nod> dof=<max_dof>
*remark
                resid_f_max=<max_f_i> node=<max_nod_f> dof=<max_dof_f>
*remark
*remark
*remark
   *if < <DEBUG> > /then
      *print 1, [DISPLACEMENT_INC]
```

```
*print 1, [RESIDUAL_FORCE]
   *andif
*END
. =DECK DEFNS
*procedure DEFNS ( step; iter )
. Purpose: Define basic macro_symbols for NLSTATIC3 procedure
*def/i np1 = [step]
*def/i n = < <np1>-1 >
*def/i nm1 = < <n>-1 >
*def/i nm2 = < <n>-2 >
*if < [iter] /eq 0 > /then
                                      . run initialization
  *def/i NS_ldi
                  == 1
  *def/i NOM_1di
                 == 3
  *def/i iset
                 == 1
  *def/i icon
                   ±= 1
   *def/a f_spec
                   == APPL.FORC.<iset>.<icon>
  *def/a d_spec
                   == APPL.MOTI.<iset>.<icon>
. Check for Prescribed Force/Displacement Loading
  *find dataset <NS_ldi> <f_spec> /seq=ids
  *if < <ids> /gt 0 > /then
     *Remark Note: Applied forces dataset <f_spec>, will be used
     *def/i spec_force_flag == <true>
  +else
     *def/i spec_force_flag == <false>
  *endif
  #find dataset <NS_ldi> <d_spec> /seq=ids
  if < <ids> /gt 0 > /then
     *Remark Note: Specified displacement dataset <d_spec> will be used
     *def/i spec_disp_flag == <true>
  *else
     *def/i spec_disp_flag == <false>
  *endif
  *if < <<spec_force_flag>/eq 0> /and <<spec_disp_flag>/eq 0>> /then
       *remark ; *remark Procedure stopped: no loads defined
   endif
  *def/i live_load_flag == <false>
  *def/a d_ext
                  == EXT.DISP
  *def/a f_ext
                  == EXT.FORC
  *def/a f_int
                  == INT.FORC
  *def/a f_T
                  == TAN.FORC
  *def/a R_np1_i == RES.FORC
  *def/a R_np1_ip1 == RES.FORC
  *def/a d_inc_i == INC.DISP
  *def/a d_inc_ip1 == INC.DISP
  *def/a delta_T == HAT.DISI
  *def/a delta_B == BAR.DISI
  *def/a delta_S == STR.DISI
                  == TOT.DISI
  +def/a delta
```

```
+def/a K_asa
                    == ASM.STIF
                    == FAC.STIF
    *def/a K_fac
    *def/a K_I
                     == COL.STIF.1.1
    *def/a Delta_I
                   == STF.DISI
    *def/i ndef
                    == 0
    #def/a d_active == ACT.DISI
    Retrieve Control Parameters from DATA_BASE
    *if < [step] /eq 1 > /then
     *def/i sign_det
                        == 1
     #def/i load_dir
                        == 1
    *def/d lam_n
                        == 0.0
     *def/d lam_nm1
                        == 0.0
    *def/d lam_nm2
                        == 0.0
    #def/d path_inc_n == 0.0
    *def/d path_inc_nm1 == 0.0
    #def/d ref_e
                        == 0.0
    *Remark
               STARTING PARAMETERS INITIALIZED.
   *alse
    *open <NOM_ldi> <NOM_DB>
    *find dataset <nom_ldi> <nom_ds> /seq=nom_ids
    *g2m /name==lam_n /type=d <nom_ldi> <nom_ids> LOAD.<n>
    *g2m /name==lam_nm1 /type=d <nom_ldi> <nom_ids> LOAD.<nm1>
    *g2m /name==lam_nm2 /type=d <nom_ldi> <nom_ids> LOAD.<nm2>
    *g2m /name==path_inc_n /type=d <nom_ldi> <nom_ids> PATH_INC.<n>
    *g2m /name==path_inc_nm1 /type=d <nom_ldi> <nom_ids> PATH_INC.<nm1>
    *g2m /name==sign_det_n /type=I <nom_ldi> <nom_ids> SIGN_DET.<n>
    *g2m /name==load_dir_n /type=I <nom_ldi> <nom_ids> LOAD_DIR.<n>
    *g2m /name==ref_e /type=d <nom_ldi> <nom_ids> REF_ERR.<n>
    *g2m /name==ndef /type=i <nom_ldi> <nom_ids> NDEF
    *g2m /name==fd /type=i <nom_ldi> <nom_ids> FD
    *close <NOM_ldi>
    *Remark
    *remark _
    tranark.
    *Remark
            RE-START PARAMETERS:
    *Remark
               LOAD_FACTORS (n,n-i,n-2) = <lam_n>, <lam_nmi>, <lam_nm2>
    *Renark
               PATH_INCREMS (n, nm1) = <path_inc_n>, <path_inc_nm1>
    *Remark
                SIGN_DET (n)
                                        = <sign_det_n>
    *Remark
                LOAD_DIR (n)
                                         = <load_dir_n>
    *remark
    *remark
   *endif
*endif
. Define Global Datasets for Upcoming Step
*def/a d_nm2
                == TOT.DISP.<n=2>
*def/a d_nm1
                == TOT.DISP.<nm1>
*def/a d_n
                == TOT.DISP.<n>
*def/a d_np1_i == TOT.DISP.<np1>
*def/a d_np1_ip1 == TOT.DISP.<np1>
```

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```
*def/a T_n
                == TOT.ROTN. <n>
*def/a T_np1_i == TOT.ROTN.<np1>
*def/a T_np1_ip1 == TOT.ROTN.<np1>
*end
. =DECK EXTRAP
*procedure EITRAP ( dx_np1; dx_n; dx_nm1; cx_n; cx_nm1; cx_nm2 )
   *def dx_np1 = [dx_np1]
   def dx_n = [dx_n]
   *def dx_nm1 = [dx_nm1]
   *def x_nm1 = <dx_nm1>
   *def x_n = < <x_nmi>+<dx_n> >
   *def x_np1 = < <x_n>+<dx_np1> >
   *def s_nm1 = < <x_np1>-<x_nm1> >
   *def s_n = < <x_np1>-<x_n> >
   *def [cx_n] ==  < <x_npi>*<s_nmi>/<<x_n>*<dx_n>> >
   *def [cx_nm1] == < -1.*<x_np1>*<s_n>/<<x_nm1>*<dx_n>> >
                      < <<u>s_nm1></u>*<<u>s_n>/</u><<<u>r_nm1></u>*<<u>x_n>></u> >
   *def [cx_nm2] ==
*end
. =DECK FACT_STIFF
*procedure FACT_STIFF
                                    . Factor stiffness
    [XQT INV
     RESET CON = 1
     RESET LRA = 7168
     RESET DZERO = 1.E-10
     RESET SPDP = <csm_precision>
    *remark
                        MATRIX BEING FACTORED (in Double Precision).
    *Remark
 . Define factored-matrix parameters as global macrosymbols
 [XOT VEC
                         Determinant = <coef_det> * 10 ^ <exp10_det>
 *remark
                         Neg. roots = <num_neg>
 *remark
 *def/i sign_det == <SIGN(1.;<coef_det>)>
 *remark
                         Sign of det = <sign_det>
 *remark
+END
 . =DECK FORM_STIFF
*procedure FORM_STIFF ( DISPLACEMENT ; --
                         ROTATION
                                      ; --
                         STIFFNESS )
                                            . output
                       FORMING NEW STIFFNESS MATRIX
   *Remark
     *call ES ( function = 'FORM STIFFNESS/TANG' ; --
                 es_nl_geom = <NL_GEOM>
                                                    ; --
                          = <COROTATION>
                                                    ; --
                 es_coro
                 es_dis_ds = [DISPLACEMENT]
                                                    ; --
                 es_rot_ds = [ROTATION] )
                                     . Transform/assemble stiffness
     EXQT K
 *END
 . =DECK INITIAL
 *procedure INITIAL
 . CLEAR INITIAL DISPLACEMENTS AND ROTATIONS (n = 0)
```

```
*g2m /name=parameters /type=i /maxn=18 <NS_LDI> JDF1.BTAB.1.8 DATA.1
   *def/i WNODES = <PARAMETERS[1]>
   *def/i NDOF = <PARAMETERS[2]>
   *Remark Problem Dimensions: N_nodes = <NNODES>, N_dofn = <NDOF>
[XQT VEC
   INIT_DOF CON.. <icon> -> DOF.TABL
              DOF TABLE initialized.
   *Remark
   INIT_VEC <d_inc_ip1>
                           <NDOF> BY <NNODES> . Zeroize translations
   INIT_VEC <K_I> <NDOF> BY <NNODES> . Zeroize translations
   INIT_VEC <Delta_I> <NDOF> BY <NNODES> . Zeroize translations
   INIT_VEC <d_active> <NDOF> BY <NNODES> . Zeroize translations
   INIT_VEC <d_n> <NDOF> BY <NNODES> . Zeroize translations
   INIT_VEC <T_n> 3 BY <NNODES> . Zeroize rotation pseudovectors
            Displacements initialized.
   *Remark
   *if < <spec_disp_flag> > /then
    <d_ext> <- <d_spec>
                                                            . for VEC
    NORM <d_ext> -> norm_d
    *if < <norm_d> /eq 0. > /then
       *Remark
       *Remark NOTE: Specified displacements are identically zero.
       *Remark
    *endif
    *copy <NS_ldi> = <NS_ldi>, <d_spec>
                                                            . for SSOL
    <d_spec> <- 0
               Specified displacements saved in <d_ext>.
    *Remark
   *endif
   *if <<spec_force_flag>> /then
      <F_ext> <- <F_spec>
                                                            . for VEC
      NORM <f_ext> -> norm_f
      *if < <norm_f> /eq 0. > /then
          *Remark
          *Remark NOTE: External forces are identically zero.
          *Remark
      *endif
               External force vector saved in <F_ext>.
      *Remark
                                                            . for SSOL
      *copy <NS_ldi> = <NS_ldi>, <F_spec>
   +else
      INIT_VEC <F_ext> <NDOF> BY <NNODES>
      INIT_VEC <F_spec> <NDOF> BY <NNODES> /single_precision . for SSOL
   *endif
   *Remark
              Right-hand-side vector zeroized (in <F_spec>).
   INIT_VEC <F_int> <NDOF> BY <NNODES>
   *Remark Internal force vector zeroized (in <F_int>).
INITIALIZE ELEMENT CONFIGURATION
[XQT E
[XQT RSEQ
        reset method=0,marcon=35
[XQT TOPO
        reset maxsub = 40000,lram=8196
*call ES ( function = 'INITIALIZE' )
```

```
Element configuration initialized.
 *Remark
*end
. =DECK POSTRES
*procedure POSTRES ( step )
[XQT VEC
 *find dataset <NOM_LDI> <NOM_DS> /seq=post_ids
 *if < <post_ids> /le 0 > /then
    *put dataset <NOM_LDI> <NOM_DS> /mrat=2000 /seq=post_ids
 *endif
. Save selected displacements on nominal data-base
  *def/a dof_names = U, V, W, RU, RV, RW
  *do $isel = 1, <N_SELECT>
   *def/i node = <SEL_NODES[<$isel>]>
   *def/i dof = <SEL_DOFS[<$isel>]>
   *def/a dof_name = <dof_names[<dof>]>
    COMPONENT <node> <dof> TOT.DISP.[step] -> DISP
   *def/a recd_name = DISP_<dof_name>_<node>.[step]
    *Remark <recd_name> = <DISP>
   *m2g /name=disp /type=d <nom_ldi> <post_ids> <recd_name>
    Save Reaction Forces for Current Step
    REAC.FORC.[stop] <- INT.FORC
   *if < [step] /eq 0 > /then
      REAC.FORC.0 <- 0.0
    +endif
    *if < <spec_disp_flag> > /then
       COMPONENT <node> <dof> REAC.FORC.[step] -> FORCE
      *def/a recd_name = FORCE_<dof_name>_<node>.[step]
      *Remark <recd_name> = <FORCE>
      *m2g /name=force /type=d <nom_ldi> <post_ids> <recd_name>
    *endif
   *enddo
*end
. =DECK POSTSTEP
*procedure POSTSTEP ( step; iter )
*Remark _____
*Remark STEP [step] SUMMARY :
*Remark
*Remark Load Factor _____ <lam_np1_ip1>
*Remark Load Direction _____ <load_dir>
*Remark Stiffness determinant _____ <coef_det> * 10 ^ <exp10_det>
*Remark Number of negative roots _____ <num_neg>
*Remark Path_length_increment _____ /path_inc>
*Remark Relative energy_error _____ <err_e_ip1>
*Remark Number of Iterations _____ <num_iters>
*Remark Number of Step Cuts _____ <<pre>cyass>-1>
*Remark Total Number of Iterations _____ <tot_iters>
*Remark _____
```

```
#open <NOM_ldi> <NOM_DB>
*if < [step] /eq 1 > /then
   *call POSTRES ( step = 0 )
   *def/d load_0=0.
   *m2g /name=load_0 /type=d <NOM_LDI> <NOM_DS> LOAD.0:0
*endif
*call POSTRES ( step=[step] )
#find dataset <NOM_LDI> <NOM_DS> /seq=nom_ids
*m2g /name=lam_np1_ip1 /type=d <nom_ldi> <nom_ids> LOAD.[STEP]
*m2g /name=path_inc /type=d <nom_ldi> <nom_ids> PATH_INC.[STEP]
*m2g /name=err_e_ip1 /type=d <nom_ldi> <nom_ids> ERROR.[STEP]
*m2g /name=ref_e /type=d <nom_ldi> <nom_ids> REF_ERR.[STEP]
*m2g /name=load_dir /type=i <nom_ldi> <nom_ids> LOAD_DIR.[STEP]
*m2g /name=sign_det /type=i <nom_ldi> <nom_ids> SIGN_DET.[STEP]
*m2g /name=coef_det /type=d <nom_ldi> <nom_ids> COEF_DET.[STEP]
*m2g /name=exp10_det /type=i <nom_ldi> <nom_ids> EXP10_DET.[STEP]
*m2g /name=num_neg /type=d <nom_ldi> <nom_ids> NEG_ROOTS.[STEP]
*m2g /name=num_iters /type=i <nom_ldi> <nom_ids> NUM_ITERS.[STEP]
*m2g /name=tot_iters /type=i <nom_ldi> <nom_ids> TOT_ITERS.[STEP]
*def/i passm1 = <<pass>-1>
*m2g /name=passm1 /type=i <nom_ldi> <nom_ids> NUM_CUTS.[STEP] . cgl, 7/26/88
*m2g /name=ndef /type=i <nom_ldi> <nom_ids> NDEF
if <<ndef> /eq 0> /then
   #def/i fd==0
*endif
*m2g /name=fd /type=i <nom_ldi> <nom_ids> FD
*close <NOM_ldi>
*end
. =DECK RESIDUAL
*procedure RESIDUAL ( STEP=1; ITER=1
                                       ; ---
                                            . input
                                       ; --
                      DISPLACEMENT
                      ROTATION
                                       ; --
                      LOAD_FACTOR
                                       ; --
                      SPECIFIED_DISP
                                       : --
                      INTERNAL_FORCE
                                       : --
                      EXTERNAL_FORCE
                                       : --
                      RESIDUAL_FORCE )
                                             output
 [XOT VEC
     [INTERNAL_FORCE] <- 0.
*call ES ( function = 'FORM FORCE/INT'; --
            es_nl_geom = <NL_GEOM>
                                         ; ---
            es_coro = <COROTATION>
                                         ; --
            os_dis_ds = [DISPLACEMENT]
                                         : --
            es_rot_ds = [ROTATION]
            es_frc_ds = [INTERNAL_FORCE] )
[XQT VEC
[BESIDUAL_FORCE] <- [load_factor] [EXTERNAL_FORCE] - [INTERNAL_FORCE]
+END
. =DECK SOLVE
*procedure SOLVE ( RHS ; SOLN )
. Copy Right-Hand-Side Vector to Expected SPAR (Single Precision) Dataset
```

```
[XQT VEC
    APPL.FORC.<iset>.<icon> <- [RHS]
                                                  /single_precision
. Solve
  [IQT SSOL
   RESET CON = <icon>
   RESET SET = (iset>
   RESET REAC = 0
. Copy SPAR Solution Vector to Double Precision Dataset
   [XOT VEC
    [SOLN] <- STATIC.DISP.<iset>.<icon>
*and
. =DECK STIP_COLMN
*procedure STIF_COLMN
[XQT VEC
  *if <<NDEF> /gt 0> /then
     FREE <NDEF> <FD>
   #endif
   *if <<spec_disp_flag> > /then
       <d_active> <- <d_inc_i>
       SPECIFY 0. <d_ext> -> <d_active>
       NORM/MAX <d_active> -> D_II NDEF FD
   +else
       NORM/MAX <d_inc_i> -> D_II NDEF FD
   *endif
[XQT AUS
    SYSVEC : UNIT I 1 1
        I=<FD> : J=<NDEF> : 1.0
    SYSVEC : COL STF 1 1
    DEFINE E = <NS_1di> UNIT I 1 1
    DEFINE K = <NS_1di> K SPAR 36
    COL STF 1 1 = PRODUCT (K,E)
[XOT VEC
   FIX <NDEF> <FD>
   <K_I> <- COL.STF.1.1
*END
. =DECK STIPPNESS
*procedure STIFFNESS ( DATA_BASE
                                         . input
                                    ; ---
                                    ; ---
                       STEP
                       ITER
                                    ; ---
                       LOAD_FACTOR ; --
                       DISPLACEMENT ; --
                       ROTATION
                                    ; --
                       STIFFNESS )
                                           . output
   *Remark
                       FORMING NEW STIFFNESS MATRIX
     *call ES ( function = 'FORM STIFFNESS/TANG' ; --
                es_nl_geom = <NL_GEOM>
                                                    ; --
```

```
es_coro = <COROTATION>
                                                   ; --
                es_dis_ds = [DISPLACEMENT]
                                                   ; --
                es_rot_ds * [ROTATION] )
    EXOT K
                                    . Transform/assemble stiffness
    [XQT INV
                                    . Factor stiffness
    RESET CON = 1
    RESET LRA = 7168
     RESET DZERO = 1.E-10
    RESET SPDP = <csm_precision>
    *remark
    *Remark
                        MATRIX BEING FACTORED (in Double Precision).
. Define factored-matrix parameters as global macrosymbols
 [XQT VEC
                         Determinant = <coef_det> * 10 ^ <erp10_det>
 *remark
 *remark
                         Neg. roots = <num_neg>
 *def/i sign_det == <SIGN(1.;<coef_det>)>
 *remark
                         Sign of det = <sign_det>
 *remark
+END
. =DECK TANDIS
*procedure TANDIS ( step;
                            iter; displacement ; rotation
                                                                ; --
                    load_factor ; max_load
                                                 ; external_force; --
                    specified_disp; internal_force; --
                    tangent_force ; tangent_disp )
*if < <spec_disp_flag> > /then
                                 . Load standard spec_disp dataset
   [XQT VEC
       SPECIFY 1.0 [specified_disp] -> <d_spec>
*endif
*call SOLVE ( RHS = [external_force]; SOLN = [tangent_disp] )
#if < <spec_disp_flag> > /then . Clear standard spec_disp dataset
   [IQT VEC
       <d_spec> <- 0.0
*endif
*end
. =DECK TWO_BY_TWO
*procedure TWO_BY_TWO ( FREE )
. . . Compute 2 x 2 system coefficients
    [XQT VEC
. . . A_22 is used for both ordinary and advanced RIKS
        DOT <d_inc_i> + <delta_T> -> A_22
        *def/d A_22 == < 2.0 * <A_22>>
. . . The remainder of Procedure is invoked only for Advanced Riks
         *if <[FREE] /gt 0> /then
           COMPONENT <ndef> <fd> <K_I> -> K_II
           COMPONENT <ndef> <fd> <f_ext> -> fe_I
           COMPONENT <ndef> <fd> <d_inc_i> -> D_II
           DOT <K_I> + <delta_I> -> K_DOT_d_I
```

```
DOT <K_I> * <delta_T> -> K_DOT_T

DOT <d_inc_i> * <delta_I> -> dd_DOT_d_I

*def/d A_11 == <<K_II> - <K_DOT_d_I>>

*def/d A_12 == <<K_DOT_T> - <fe_I>>

*if <<spec_disp_flag>>/then

DOT <K_I> * <d_ext> -> K_DOT_d_ext

*def/d A_12 == <2.0 *<<D_II> - <dd_DOT_d_I>>

*endif

*def/d A_21 == < 2.0 *<<D_II> - <dd_DOT_d_I>>

*endif
```

\*end

# 3.11 Procedure NL\_DYNAMIC\_1

#### 3.11.1 GENERAL DESCRIPTION

Procedure NL\_DYNAMIC\_1, written by C. C. Rankin and B. Nour-Omid of Lockheed Palo Alto Research Laboratory, performs nonlinear transient analysis using a one-step, self-starting, implicit integration algorithm containing adjustable parameters. The nonlinear system is solved using a modified Newton/Raphson incremental/iterative solution sequence. Like NL\_STATIC\_1, procedure NL\_DYNAMIC\_1 relies on the Generic Element Processor (*i.e.*, structural element processors, ES*i*) and hence has a corotational option for geometric nonlinearity that enables arbitrarily large rotations.

Procedure NL\_DYNAMIC\_1 solves the transient system

$$\mathbf{M}\ddot{\mathbf{u}} + \mathbf{f}^{int}(\mathbf{u}) = \mathbf{f}^{ext} \tag{3.11-1}$$

Here M is the mass matrix, u is the displacement, and dots over quantities refer to differentiation with respect to time. These equations are discretized over time using the following relations involving two parameters  $\theta$  and  $\alpha$ :

$$\mathbf{Ma}_{n+\theta} + (1+\alpha)\mathbf{f}^{int}(\mathbf{d}_{n+\theta}) - \alpha\mathbf{f}^{int}(\mathbf{d}_n) = \mathbf{f}_{n+\theta}^{ext}$$
(3.11-2)

where  $d_{n+\theta}$  and  $a_{n+\theta}$  are the approximations to the displacement and acceleration at time  $(n+\theta)\Delta t$ , and where Wilson's  $\theta$  interpolation parameter is used to obtain the desired acceleration according to

$$\mathbf{a}_{n+\theta} = (1-\theta)\mathbf{a}_n + \theta \mathbf{a}_{n+1} \tag{3.11-3}$$

Velocity v and acceleration a are related to the displacements at the point  $n + \theta$  by

$$\mathbf{v}_{n+\theta} = \mathbf{v}_n + \theta \Delta t [(1-\gamma)\mathbf{a}_n + \gamma \mathbf{a}_{n+\theta}]$$
  
$$\mathbf{d}_{n+\theta} = \mathbf{d}_n + \theta \Delta t \mathbf{v}_n + (\theta \Delta t)^2 [(\frac{1}{2} - \beta)\mathbf{a}_n + \beta \mathbf{a}_{n+\theta}]$$
(3.11-4)

where we have introduced the two standard Newmark parameters  $\beta$  and  $\gamma$  as the last two parameters in our system. The resulting system to be solved is

$$\mathbf{M}\mathbf{d}_{n+\theta} + (\theta\Delta t)^2 \beta (1+\alpha) \mathbf{f}^{int}(\mathbf{d}_{n+\theta}) - \tilde{\mathbf{f}}_{n+\theta} = 0$$
(8)

where the quantity  $\tilde{f}_{n+\theta}$  is known from the last converged time step (see Section 4.3.9.2. for a complete derivation of equations and definition of symbols).

NL\_DYNAMIC\_1 is designed to solve any well posed initial value transient analysis problem with non-negative mass. This includes problems with initial velocity and/or initial displacement, as well as a generalized imposed external forcing with either built-in or user-suppled time dependence. Currently, the procedure uses the same external loading as NL\_STATIC\_1, with a multiplier defined by a force-time procedure. The built-in procedures are described in Sections 4.3.3.7 and 4.3.3.8. Since (66) is a nonlinear system similar to (1), much of what is in NL\_STATIC\_1 applies to NL\_DYNAMIC\_1. In particular, we mention the solution of a banded system with similar structure to the stiffness matrix, identical handling of large rotations, similar procedures for archiving results of solutions and retrieving restart information, and very similar convergence and stepsize adjustment procedures. We shall henceforth concentrate on the differences between the static and dynamic algorithms, with particular emphasis on operations involving the mass, time step, and the four adjustable integration parameters. In some respects, NL\_DYNAMIC\_1 is simpler than its static analogues, since no arclength constraint is needed for a positive-definite mass/stiffness system.

#### 3.11.2 PROCEDURE USAGE

Procedure NL\_DYNAMIC\_1 may be invoked by the \*call directive:

```
*call NL_DYNAMIC_1 ( arg1 = val1; arg2 = val2; ...)
```

where **argi** are argument names and **vali** are the corresponding values you wish to give them. The following are valid arguments for NL\_DYNAMIC\_1; note that those without default values are mandatory, while the others are optional.

Argument	Default Value	Meaning
BEG_STEP	-	Starting step number (>0)
MAX_STEPS	-	Maximum steps to compute
BEG_TIME	-	Problem starting time
MAX_TIME	-	Upper_bound on problem time
DEL_TIME	-	Beginning time step
INT_PARS	1.,0.,.25,.5	Time integration parameters
LOAD_STIFF	<false></false>	Include load stiffness
FT_PROC	FT_ZERO	Forcing procedure
FT_ARGS	0.	Parameter array for FT_PROC
COROTATION	1	Corotational Update Option
DES_ITERS	4	Number of iterations per step desired
EXTRAPOLATE	<true></true>	Perform quadratic extrapolation of solution
FAC_STEPS	1	Steps_per_refactoring
MAX_ITERS	9	Maximum iterations per step
MAX_CUTS	3	Maximum number of successive step cuts
NL_GEOM	2	Geometric Nonlinearity Level (1 or 2)
NOMINAL_DB	NOMINAL.GAL	Results database file
NOMINAL_DS	<b>RESPONSE.HISTORY</b>	Results dataset
N_SELECT	0	Number of nodes for selected disp. output
SEL_NODES	0	List of nodes for selected output
SEL_DOFS	0	Corresponding list of nodal freedoms (1–6)
TOL_E	1.E-3	Relative error tolerance in energy norm

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In the above definitions, the term step refers to a time step. The total response is automatically subdivided into time steps, with the starting time prescribed by the User — using BEG\_TIME. The initial time step is set by DEL\_TIME, and held constant unless trouble occurs. If convergence is difficult, the time step will be cut, and a new initial value problem will be started at the last converged solution.

## 3.11.3 ARGUMENT GLOSSARY

## 3.11.3.1 <u>BEG\_STEP</u>

This argument defines the number of the first step to be computed in a given nonlinear analysis interval. It is important primarily for analysis re-starts. Initially, BEG\_STEP should be set to 1. To continue an analysis in a subsequent run, after having computed and saved "n" steps in the previous run, one would typically set BEG\_STEP equal to "n+1". For example, if the 10th step was successfully completed in the first run, then it could be continued in a second run by setting BEG\_STEP = 11. However, it is not necessary for BEG\_STEP to be larger than any previously computed step. That is, you may re-compute a sequence of steps by setting BEG\_STEP to the number of the first step to be re-computed. The procedure will automatically use the step that immediately precedes BEG\_STEP (e.g., BEG\_STEP-1) to obtain the necessary initial displacements, velocities, and accelerations.

# 3.11.3.2 <u>BEG\_TIME</u>

The starting problem time. For the initial run, the value of this parameter is usually set to zero.

# **3.11.3.3** <u>COROTATION</u> (default = $\langle true \rangle$ )

Corotational update switch for large-rotation problems. This switch should be set to  $\langle true \rangle$  when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element Processor (ESi) section in the Testbed User's Manual for specific guidelines.

# **3.11.3.4 DEBUG** (default = $\langle false \rangle$ )

Procedure debug switch. This switch should only be turned on to obtain additional diagnostic printout for procedure debugging.

# 3.11.3.5 <u>DEL\_TIME</u>

The initial time step. If all goes well with the integration, this will be the time increment throughout the analysis. For restart, it is possible to use the time increment that was in force for the previous run. For restart only, input zero to cause the procedure to read in and use the previous DEL\_TIME.

# 3.11.3.6 <u>DES\_ITERS</u> (default = 4)

Desired number of iterations allowed for convergence at a given load step. This parameter is used to adaptively adjust the arclength increment from one load step to the next, by comparing DES\_ITERS with the actual number of iterations required for convergence at the last step.

# 3.11.3.7 $\underline{FT}_{PROC}$ (default = $\underline{FT}_{ZERO}$ )

FT\_PROC is the name of a procedure that will obtain the load factor  $(\lambda)$  for the timedependent forcing function. For applied *force* loading, this factor is multiplied by the reference applied force vector to obtain the current load vector, *i.e.*,

$$\mathbf{f}_1^{ext} = \lambda(t) \, \bar{\mathbf{f}}^{ext}$$

where  $\overline{\mathbf{f}}^{ext}$  is the reference applied force vector stored in dataset APPL.FORC.1. For applied *displacement* loading, the starting load factor is applied to the reference applied displacement vector, which is then used to compute the initial internal force vector, *i.e.*,

$$\mathbf{f}_{1}^{int(1)} = \mathbf{f}^{int}[\lambda(t)\,\overline{\mathbf{d}}^{\,ext}]$$

where  $\overline{\mathbf{d}}^{ext}$  is the reference applied displacement vector stored in dataset APPL.MOTI.1.

The user can supply any procedure he desires for FT\_PROC. If this is the case, FT\_PROC is the *name* of that procedure. FT\_PROC has three arguments of its own. T is the current problem time, FT\_ARGS is an array of up to six scalars, and F\_MAC is the name of the macrosymbol (set by NL\_DYNAMIC\_1) to contain  $\lambda(t)$ .

If the user wishes to use the FT procedures supplied here, he has four choices, as illustrated in Fig. 4.3-1.

FT\_ZERO This is the default option, which means that there will be no external forcing.

FT\_LIN Piecewise linear forcing function.

FT\_SIN Sinusoidal forcing function.

FT\_EXP Exponential decay.

# 3.11.3.8 <u>FT\_ARGS</u>

These are the arguments to either the user-supplied forcing function, or required for FT\_LIN, FT\_SIN, or FT\_EXP. For these last three procedures (supplied here), we offer the same options that are supplied with the code Structural Analysis of General Shells (STAGS). We have reproduced the forcing function diagram from the STAGS manual, which here appears as Fig. 4.3-1. In this figure, PA is the function  $\lambda(t)$ , TIME is in units of problem time, and CA1 through CA6 are FT\_ARGS[1:6], respectively. A summary for each each case follows:

For FT\_LIN (piecewise linear time dependence), the array is as follows:

- FT\_ARGS[1] Maximum load factor (CA1 in figure).
- FT\_ARGS[2] Delay time before applied load ramps up (CA2). Can be zero.
- FT\_ARGS[3] Time at which load reaches maximum (CA3). Can be equal to FT\_ARGS[2].
- FT\_ARGS[4] Time at which load begins to drop (CA4). Can be equal to FT\_ARGS[3] if FT\_ARGS[3] is not equal to FT\_ARGS[2].
- FT\_ARGS[5] Time at which load drops (CA5).
- FT\_ARGS[3:5] can be safely set to larger than MAX\_TIME if that is what the user wants.
- For FT\_SIN (sinusoidal time dependence), the array is as follows:
- FT\_ARGS[1] Peak height of sine wave (see Fig. 4.3-1, CA1)
- FT\_ARGS[2] Load offset for the sine wave function (CA2). If zero, the sine wave will oscillate to plus/minus FT\_ARGS[1].
- FT\_ARGS[3] Half wavelength (CA3).
- FT\_ARGS[4] Problem time to first maximum load (CA4).
- FT\_ARGS[5] Delay time to imposition of load (CA5).
- FT\_ARGS[6] Time at which all loading will terminate (can be a large number), or CA6 in Fig. 4.3-1.
- For FT\_EXP (Exponential decay), the array is as follows:
- FT\_ARGS[1] Peak height of exponential (see Fig. 4.3-1, CA1)
- FT\_ARGS[2] Delay time before any load is imposed (CA2). Can be zero.
- FT\_ARGS[3] Half life time of exponential decay.
- FT\_ARGS[4] This argument is not used. In the Fig. 4.3-1, CA4 must be half CA1. If this is not the case, then FT\_ARGS[3] should be recomputed.

Figure 4.3-1 Load Factor Histories

## 3.11.3.9 INT\_PARS (default=1.,0.,.25,.5)

The values contained in this array set the characteristics of the time integrator. INT\_PARS[1] is Wilson's  $\theta$  interpolator (see Theory, Section 4.3.9), INT\_PARS[2] is  $\alpha$ , and INT\_PARS[3:4] are the Newmark  $\beta$  and  $\gamma$  parameters, respectively. A sophisticated user can reset these parameters for special integrator performance characteristics. Unless there is reason to tinker with their default values, it is better for the user to leave these parameters alone.

## 3.11.3.10 LOAD\_STIFF / (default=<false>)

If true, include load stiffness in the total stiffness matrix assembly.

# **3.11.3.11** <u>MAX\_CUTS (default=3)</u>

Maximum number of step cuts permitted during the current nonlinear analysis interval. A step cut refers to a halving of the arclength increment used to advance the solution from one step to the next. Step cuts are performed only if the maximum number of iterations are exceeded without converging at a given load step. Note that the relationship between the increment in "arclength" and the increment in the load-factor,  $\lambda$ , is computed internally by the procedure.

### 3.11.3.12 MAX\_TIME

Problem time for which the analysis is to be terminated.

# 3.11.3.13 **MAX\_ITERS**

Maximum number of iterations allowed for convergence at a given load step. This parameter is used to terminate the iteration process at a given load level. If convergence hasn't been obtained after MAX\_ITERS iterations, the load (*i.e.*, arclength) increment is cut in half and the step is repeated — until either convergence has been obtained or MAX\_CUTS has been exceeded.

# 3.11.3.14 <u>MAX\_STEPS</u>

Maximum number of load steps to compute in the current nonlinear analysis run. This provides an implicit limit on analysis run-time. The transient analysis is thus terminated whenever MAX\_STEPS or MAX\_TIME is exceeded — whichever comes first.

# 3.11.3.15 <u>NL\_GEOM (default = 2)</u>

Geometric nonlinearity level: 0, 1, or 2.  $0 \Rightarrow$  the problem is geometrically linear;  $1 \Rightarrow$  geometric nonlinearity will be handled globally, *e.g.*, using corotational updates only; and  $2 \Rightarrow$  nonlinear element strain-displacement relations should be used in addition to any global treatment of geometric nonlinearity. If COROTATION = <true>, options 1 and 2 refer to first-order and second-order corotation, respectively. The latter option can be significantly more accurate than the former for a given finite element model — depending on which element types are involved.

### 3.11.3.16 <u>NOMINAL\_DB</u> (default = NOMINAL.GAL)

Name of database (GAL file) where a step-wise history of important solution parameters and selected response variables is to be stored.

### 3.11.3.17 <u>NOMINAL\_DS</u> (default = **RESPONSE.HISTORY**)

Name of dataset, within database defined by argument NOMINAL\_DB, where a stepwise history of important solution parameters and selected response variables is to be stored. See the CSM Testbed Dataset Manual, under dataset RESPONSE.HISTORY, for a description of the individual data records stored in this dataset.

#### 3.11.3.18 <u>N\_SELECT</u> (default = 0)

Number of user-selected displacement components to be saved in the dataset specified by argument NOMINAL\_DS. Values for these displacement components, the locations and directions of which are specified by arguments SEL\_NODES and SEL\_DOFS, respectively, are stored at every time step.

#### **3.11.3.19** <u>SEL\_DOFS (default = 0)</u>

List of nodal DOF's at which displacement histories are to be saved in dataset [NOM-INAL\_DS]. There should be [N\_SELECT] numbers in the list, in correspondence with the node numbers specified by argument SEL\_NODES. Values of each number in the list must range between 1 and 6, in correspondence to the nodal DOF sequence (e.g.,  $u, v, w, \theta_x, \theta_y, \theta_z$ ) specified by the START command of Processor TAB.

#### **3.11.3.20** <u>SEL\_NODES (default = 0)</u>

List of node numbers at which displacement histories are to be saved in dataset [NOM-INAL\_DS]. There should be [N\_SELECT] numbers in the list, and node numbers can be repeated if more than one nodal DOF is to be saved at a node. The corresponding nodal DOF for each entry is specified by argument SEL\_DOFS.

#### 3.11.3.21 <u>TOL\_E (default = 1.e-3)</u>

Error tolerance used to establish convergence of the nonlinear equilibrium iteration procedure at each load step. The iteration loop at a given step is terminated whenever the following condition is met:

$$\epsilon \leq [\text{TOL}_E]$$

where

$$\epsilon = \sqrt{\frac{\mathbf{r}^{(i)} \cdot \delta \mathbf{d}^{(i)}}{\mathbf{r}^{(1)} \cdot \delta \mathbf{d}^{(1)}}}$$

is the relative energy error norm, r is the residual force vector,  $\delta d$  is the iterative displacement change, and *i* is the iteration counter.

# 3.11.4 INPUT/OUTPUT DATASETS

Table 3.11-1 Datasets Input/Output by Procedure NL_DYNAMIC_1				
Dataset	Description Lib L		Input	Output
<es_name>.EFIL.*</es_name>	Element Computational Data	1	$\checkmark$	$\checkmark$
ES.SUMMARY	ES Processor Status	1	$\checkmark$	$\checkmark$
DEF. <es_name>.*</es_name>	Element Defn. (Connectivity)	1	$\checkmark$	
DIR. <es_name>.*</es_name>	Element EFIL Directory	1	$\checkmark$	
JDF1.BTAB.*	Model Summary	1	$\checkmark$	
JLOC.BTAB.*	Nodal Coordinates	1	$\checkmark$	
PROP.BTAB.*	Material/Section Properties	1	$\checkmark$	
QJJT.BTAB.*	Nodal Transformations	1	$\checkmark$	
TOT.DISP.step	System Displacement Vector	1	$\checkmark$	$\checkmark$
TOT.ROTN.step	Nodal Rotation Pseudovectors	1	$\checkmark$	$\checkmark$
TOT.VEL.step	System Velocity Vector	1	$\checkmark$	$\checkmark$
TOT.ACC.step	System Acceleration Vector	1	$\checkmark$	$\checkmark$
<b>REAC.FORC</b> .step	System Internal Force Vector	1		$\checkmark$

where step is the time step number, and ranges consecutively from 1 to the total number of steps computed. We must emphasize here that if one wishes to solve an initial value problem with either nonzero initial velocities or displacements (and not a restart), the user must supply TOT.DISP.0 and/or TOT.VEL.0. If they are not supplied, the procedure will initialize these to zero.

# **3.11.5 SUB-PROCEDURES AND PROCESSORS**

Table 3.11-2 Sub-Procedures Invoked by Procedure NL_DYNAMIC_1			
Procedure	Туре	Function	
NL_DYNAMIC_1	Internal	Main Procedure	
CHK_CONVD	Internal	Check convergence	
CONSTRAIN	Internal	Impose constraints on freedoms	
DEFND	Internal	Defines recursive macrosymbols	
ES	External	Element utility Procedure	
FACTOR	Internal	Factor stiffness matrix	
FORCE	Internal	Forms INTERNAL/EXTERNAL force vector	
FT_ZERO	Internal	Zero force-time history	
FT_LIN	Internal	Piecewise linear force-time history	
FT_SIN	Internal	Sinusoidal force-time history	
FT_EXP	Internal	Exponential decay force-time history	
MASS	Internal	Compute mass	
MASS_STIFF	Internal	Combine mass and stiffness matrices	
NL_INITD	Internal	Initialize datasets and set restart	
POSTRES	Internal	Save selected data, internal forces	
POSTSTPD	Internal	Save data for restart	
SOLVE	Internal	Solves linear equation systems	
STIFFNESS	Internal	Forms and assembles stiffness matrix	

Table 3.11-3 Processors Invoked by Procedure NL_DYNAMIC_1			
Procedure	Туре	Function	
AUS	Internal	Combines mass and stiffness matrices	
Е	Internal	Initializes EFIL datasets	
ESi	External	Element Processors based on GEP	
INV	Internal	Factors stiffness matrix	
SSOL	Internal	Solves linear equation systems	
VEC	Internal	Performs all vector/pseudo-vector algebra	

# 3.11.6 LIMITATIONS

Limitations spelled out in Sections 4.1.6.1 through 4.1.6.8 apply also to NL\_DYNAMIC\_1. In addition, the following limitations also exist:

# 3.11.6.1 <u>No Damping Included</u>

No damping is included in this first version of NL\_DYNAMIC\_1. Damping that preserves the bandwidth of the problem will be included in a later version.

## 3.11.6.2 Initial Velocities and Displacements

These are currently the responsibility of the user. NL\_DYNAMIC\_1 will expect to see data sets TOT.DISP.0 and TOT.VEL.0 for these types of problems. Currently, there is no way to initialize rotational triads. This is a topic for future development.

## 3.11.6.3 Diagonal Mass

Currently, only diagonal mass can be used. This limitation will soon be removed.

## 3.11.6.4 AUS Limitation

Due to hard wired data set naming conventions in processor AUS for system matrices (e.g. K.SPAR.36), the number of DOF's per node specified on the START command of processor TAB is presently restricted to be 6. AUS is currently essential to NL\_DYNAMIC\_1 for computing the sum of the mass and stiffness matrices to obtain the dynamic operator. This restriction will be removed when we make the connection to the Generic Matrix Processor.

# **3.11.7 ERROR MESSAGES**

# 3.11.7.1 "Non-Convergence at Step n. Revise Strategy."

This message means that the maximum number of nonlinear iterations (MAX\_ITERS) has been exhausted, as well as the maximum number of step cuts (MAX\_CUTS), and convergence still hasn't been obtained at step n. A possible cure is to re-start the analysis from several steps back, and decrease the arclength increment at that point (using the PATH\_SCALE argument). However, just increasing MAX\_ITERS or MAX\_CUTS, or even TOL\_E, may also solve the problem. In other words, re-think the definition of all solution parameters based on the observed behavior of the solution algorithm just prior to the break-down.

# 3.11.7.2 "Divergence at Step n. Revise Strategy."

This message has similar implications to the previous message, but it occurs when the error grows instead of decreases during two successive nonlinear iterations. The difference between divergence and non-convergence is that divergence cannot be cured by increasing MAX\_ITERS; and probably should not be "cured" by increasing TOL\_E. It generally

means that the step-size is too big — or that the error tolerance (TOL\_E) has been too big all along, so that changes are occurring suddenly that should have been detected by the solution algorithm at earlier load steps. Thus, you might try re-starting from an earlier step, reducing PATH\_INC, and possibly reducing TOL\_E as well.

## 3.11.7.3 "Specified Displacements are Identically Zero"

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed — in which case the message should be taken merely as a warning.

## 3.11.7.4 "Specified Forces are Identically Zero"

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed — in which case the message should be taken merely as a warning.

#### 3.11.8 USAGE GUIDELINES AND EXAMPLES

### 3.11.8.1 Starting an Analysis

To begin a nonlinear transient analysis with procedure NL\_DYNAMIC\_1, it is only necessary that the finite element model be defined. This does not require pre-formation of element stiffness matrices, node renumbering for optimal factorization time, or any form of linear analysis (unless initial geometric imperfections are based on linear displacement modes). Only nodal coordinates/transformations, material properties and element connectivity are pre-requisite to nonlinear analysis. To invoke procedure NL\_DYNAMIC\_1, only those arguments that don't have default values (see PROCEDURE USAGE section) need be specified.

For example, if you wanted to start an analysis with an initial time of 0., maximum time of .01, a time step of .005, and compute no more than 20 time steps with an initial velocity profile defined in data set TOT.VEL.0, you could invoke the procedure as follows:

\*call NL\_DYNAMIC\_1 ( BEG\_STEP = 1 ; MAX\_STEPS = 20 ; -BEG\_TIME = .0 ; MAX\_TIME = .1 ; -DEL\_TIME = 0.005 )

Keep in mind that the number of time-steps actually performed during the above run will depend on whether convergence difficulties were encountered. If that happened, the step will be cut, and the number of steps to maximum time will be greater. Since it may be difficult to estimate this in advance, you may want to start with only a few time steps  $(e.g., \text{ set MAX}_STEPS = 3)$  to get some experience, and later re-start the analysis with more steps allowed.

### 3.11.8.2 <u>Re-Starting (or Continuing) an Analysis</u>

To re-start an analysis from a previously computed, converged solution, you need only specify the first step to compute, the maximum time, and any changes in the forcing function. The only requirement is that a previous complete set of solution data for a converged time step must be present on the database. If, for example, one wishes to restart from step 10 (compute beginning step 11), then the call could be

\*call NL\_DYNAMIC\_1 ( BEG\_STEP = 11; MAX\_STEPS = 100 ; -MAX\_TIME= .1 ; DEL\_TIME = 0. ; -FT\_PROC=FT\_LIN ; FT\_ARGS=100.,0.,0.,1. )

In this case, the user wants to restart the previous example at time .05 with the sudden imposition of a step forcing function with scaled magnitude of 100. By examining Fig. 4.3-1, one can see that the step load is to be continued well beyond the termination time. FT\_LIN is one of the procedures supplied here.

It is also possible to modify integration parameters and the time step, as well as any of the other applicable procedure arguments. Note that the parameter DEL\_TIME is always required. The value zero is used to tell the procedure to look into the database for the last value. A nonzero value for this parameter overrides the time step saved in the data base.

#### 3.11.9 THEORY

#### 3.11.9.1 Introduction

Procedure NL\_DYNAMIC\_1 performs a nonlinear transient analysis of a system using a time integration algorithm that has adjustable parameters which allow for the automatic selection of a family of related transient analyzers. All of them are self starting, require no "historical" vectors, and for a useful range of parameters, are unconditionally stable. All are based on discrete matrix equations of motion that may or may not include damping. The internal and external force vectors can be nonlinear functions of the displacements (unknowns).

#### 3.11.9.2 Development of the Algorithm

The discrete form of the equations of motion are

$$\mathbf{M}\ddot{\mathbf{u}} + \mathbf{f}^{int}(\mathbf{u}) = \mathbf{f}^{ext} \tag{3.11-5}$$

where for simplicity we have omitted damping, and where the dependence of the internal forces on displacement and the external forces has been emphasized. Here **M** is the mass matrix, **u** is the displacement, and dots over quantities refer to differentiation with respect to time. Our goal is to find a discrete solution to (69) at time  $t + \Delta t$  (step n + 1), given information at time t (step n). In order to do this, we need additional relations between the displacements, velocities, and accelerations being solved for.

We begin with a two parameter family of the equations of motion (69) discretized in time as follows:

$$\mathbf{Ma}_{n+\theta} + (1+\alpha)\mathbf{f}^{int}(\mathbf{d}_{n+\theta}) - \alpha \mathbf{f}^{int}(\mathbf{d}_n) = \mathbf{f}_{n+\theta}^{ext}$$
(3.11-6)

where  $d_{n+\theta}$  and  $a_{n+\theta}$  are the approximations to the displacement and acceleration at time  $(n+\theta)\Delta t$ , and where Wilson's  $\theta$  interpolation parameter is used to obtain the desired acceleration according to

$$\mathbf{a}_{n+\theta} = (1-\theta)\mathbf{a}_n + \theta \mathbf{a}_{n+1} \tag{3.11-7}$$

The parameter  $\alpha$  is a measure of the "degree of implicitness" of the integrator. If  $\alpha$  is 0, the equations of motion are to be satisfied at some point  $\theta$  greater than unity. If  $\alpha = -1$ , we have an explicit system, with the acceleration extrapolated from values at the previous step.

To relate the velocity and acceleration to the displacements at the point  $n + \theta$ , we introduce the two standard Newmark parameters  $\beta$  and  $\gamma$ :

$$\mathbf{v}_{n+\theta} = \mathbf{v}_n + \theta \Delta t [(1-\gamma)\mathbf{a}_n + \gamma \mathbf{a}_{n+\theta}]$$
(3.11-8)

$$\mathbf{d}_{n+\theta} = \mathbf{d}_n + \theta \Delta t \mathbf{v}_n + (\theta \Delta t)^2 [(\frac{1}{2} - \beta) \mathbf{a}_n + \beta \mathbf{a}_{n+\theta}]$$
(3.11 - 9)

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$$\widetilde{\mathbf{d}}_{n+\theta} = \mathbf{d}_n + \theta \Delta t \mathbf{v}_n + (\theta \Delta t)^2 (\frac{1}{2} - \beta) \mathbf{a}_n \qquad (3.11 - 10)$$

then, using (73), we have

$$\mathbf{d}_{n+\theta} = \tilde{\mathbf{d}}_{n+\theta} + (\theta \Delta t)^2 \beta \mathbf{a}_{n+\theta}$$
 (3.11-11)

If we multiply Eq. (70) by  $(\theta \Delta t)^2 \beta$  and eliminate  $\mathbf{a}_{n+\theta}$  using (74), we obtain

$$\mathbf{M}\mathbf{d}_{n+\theta} + (\theta \Delta t)^2 \beta (1+\alpha) \mathbf{f}^{int}(\mathbf{d}_{n+\theta}) - \tilde{\mathbf{f}}_{n+\theta} = 0 \qquad (3.11-12)$$

where the quantity  $\tilde{\mathbf{f}}_{n+\theta}$  is known from the last converged time step:

$$\widetilde{\mathbf{f}}_{n+\theta} = (\theta \Delta t)^2 \beta [\mathbf{f}_{n+\theta}^{ext} + \alpha \mathbf{f}^{int}(\mathbf{d}_n)] + \mathbf{M} \widetilde{\mathbf{d}}_{n+\theta}$$
(3.11-13)

Eq. (77) is a nonlinear system of equations which must be solved for  $d_{n+\theta}$ ; these displacements will be solved for using an extrapolated starting solution followed by modified Newton corrections. The solution of this system is very similar to what is in NL\_STATIC\_1, with the exception of the arclength constraint and load factor equation. Thus, solution of (77) proceeds like a fixed-step static algorithm with a modified "stiffness" matrix and residual vector. In the algorithm description, these are labeled the dynamic operator and dynamic residual, respectively.

#### 3.11.9.3 Derivation of the Dynamic Operator and Residual

The derivation of the dynamic operator and residual follows directly from the linearization of (77). Using a procedure similar to that for static analysis, we carry out a Taylor expansion of (77) and drop all terms of order higher than first. The result is the system

$$[\mathbf{M} + (\theta \Delta t)^2 \beta (1+\alpha) \mathbf{K} (\mathbf{d}_{n+\theta}^{(0)})] \delta \mathbf{d}_{n+\theta}^{(i)} = \vec{\mathbf{f}}_{n+\theta}^{(i)}$$
(3.11-14)

where

$$\widetilde{\mathbf{f}}^{(i)} = \widetilde{\mathbf{f}}_{n+\theta} - \mathbf{M}\mathbf{d}_{n+\theta}^{(i-1)} - (\theta\Delta t)^2\beta(1+\alpha)\mathbf{f}^{int}(\mathbf{d}_{n+\theta}^{(i-1)})$$
(3.11-15)

is the dynamic residual. Here

$$\widetilde{\mathbf{f}}_{n+\theta} = (\theta \Delta t)^2 \beta [\mathbf{f}^{ext}(t_{n+\theta}) + \alpha \mathbf{f}^{int}(\mathbf{d}_n)] + \mathbf{M} \widetilde{\mathbf{d}}_{n+\theta}$$
(3.11-16)

which is computed from information known at the previous step or computed from the known external forcing function.  $\delta d_{n+\theta}^{(i)}$  is the vector of unknown displacement increments at iteration *i*, time point  $t + \theta \Delta t$ . One can tell that this is a modified Newton sequence, because of the argument of the stiffness matrix in (78). For true Newton, one would have to reform and refactor the stiffness matrix using the latest displacement information.

#### **3.11.9.4** Recovery of Quantities at Step n+1

Once the displacements at point  $t+\theta\Delta t$  are known, we need to update the accelerations and compute the new velocities and displacements at the desired new step. Starting with  $d_{n+\theta}$ , we use the second of (73) to solve for  $a_{n+\theta}$ . Introducing (74), the equation for the acceleration becomes

$$\mathbf{a}_{n+\theta} = \frac{1}{(\theta \Delta t)^2 \beta} (\mathbf{d}_{n+\theta} - \widetilde{\mathbf{d}}_{n+\theta})$$
(3.11 - 17)

We now require the accelerations, velocities, and displacements at time step n + 1. Using (72), we have for  $a_{n+1}$ 

$$\mathbf{a}_{n+1} = \frac{1}{\theta} \mathbf{a}_{n+\theta} + (1 - \frac{1}{\theta}) \mathbf{a}_n \qquad (3.11 - 18)$$

Eqs. (72) and (73) can then be used with  $\theta = 1$  to interpolate velocities and displacements to step n + 1, given the new and old accelerations:

$$\mathbf{v}_{n+1} = \mathbf{v}_n + \Delta t [(1-\gamma)\mathbf{a}_n + \gamma \mathbf{a}_{n+1}]$$
  
$$\mathbf{d}_{n+1} = \mathbf{d}_n + \Delta t \mathbf{v}_n + \Delta t^2 [(\frac{1}{2} - \beta)\mathbf{a}_n + \beta \mathbf{a}_{n+1}]$$
(3.11-19)

#### 3.11.9.5 The Composition of New Displacements and Velocities

Whenever a new velocity vector is to be updated from a previous vector, the increment is simply added to the vector. For displacements, however, only the translations are handled this way. The rotational triads must be updated by the product rule, covered in Section 4.1.9.10. NL\_DYNAMIC\_1 is no different from NL\_STATIC\_1 in this respect. However, the reader will notice that the vector  $\hat{d}_{n+\theta}$  is treated like a velocity, with no accompanying rotational update. The reason is that  $\hat{d}_{n+\theta}$  eventually ends up as part of an incremental quantity used to account for inertial effects in the dynamic residual. The rotational freedoms in this vector are accumulated like their translational counterparts. To avoid confusion in the algorithm description, compositions that require special rotational treatment will be denoted by the symbol  $\oplus$ . Again, this is similar to the static case.

#### 3.11.9.6 The Integration Parameters

The integration parameters allow the user to taylor the integrator to the special needs of his problem. The following table defines what we mean by each parameter. For detailed information on the various integrator options, the reader should consult references at the end of this section.

Parameter	Name		
β, γ	Newmark Parameters		
θ	Wilson's Collocation Parameter		
α	Dissipation Parameter		

Table 3.11-4 Parameter names used in the NL\_DYNAMIC Procedure.

Special choices of these parameters select out well known integrators whose behavior has been studied extensively. These integrators, the parameter choices, and their regions of stability for stiff linear systems can be found in the following table.

Algorithm	α	β	γ	θ	Remarks
Newmark	0			1	Implicit and unconditionally stable when $2\beta \ge \gamma \ge \frac{1}{2}$
Trapezoidal	0	$\frac{1}{4}$	$\frac{1}{2}$	1	Implicit and unconditionally sta- ble
Linear Acceleration	0	$\frac{1}{6}$	$\frac{1}{2}$	1	Implicit and conditionally stable
Fox-Goodwin	0	$\frac{1}{12}$	$\frac{1}{2}$	1	Implicit and conditionally stable
Central Difference	0	0	$\frac{1}{2}$	1	Explicit and conditionally stable
Wilson- <b>0</b>	0	1 6	$\frac{1}{2}$		Implicit and unconditionally stable when $\theta \ge 1.366025$
Collocation	0		$\frac{1}{2}$		Implicit and unconditionally stable when $\theta \ge 1$ and $\frac{\theta}{2(\theta+1)} \ge \beta \ge \frac{2\theta^2 - 1}{4(2\theta^3 - 1)}$
α-Method				1	Implicit and unconditionally stable when $-\frac{1}{3} \leq \alpha \leq 0$ , $\gamma = \frac{1}{2}(1-2\alpha)$ and $\beta = \frac{1}{4}(1-\alpha)^2$

**Table 3.11-5.** Some properties of the algorithms that can be produced using NL\_DYNAMIC\_1 through the  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\theta$  parameters.

## 3.11.10 ALGORITHM

**General Algorithm** 

(1) INITIALIZATION

(1.1) Initialize  $\alpha, \beta, \gamma, \theta$ .

(1.2) Initialize  $d_0$ , v.

(1.3) Compute time at  $\theta$ 

$$t_{\theta} = t_0 + \theta \Delta t$$

(1.4) Compute weighted out-of-balance force

$$\mathbf{\bar{f}} = \beta \mathbf{f}^{ext}(t_{\theta}) + (\frac{1}{2} - \beta) \mathbf{f}^{ext}(t_0) + \mathbf{f}^{int}(\mathbf{d}_0)[\beta(1 + \alpha) - \frac{1}{2}]$$

(1.5) Add inertial terms

$$\mathbf{\tilde{f}}_{\theta} = \mathbf{M}(\mathbf{d}_0 + \theta \Delta t \mathbf{v}_0) + (\Delta t \theta)^2 \mathbf{\bar{f}}$$

(1.6) Compute initial estimate of displacements

$$\mathbf{d}_{\boldsymbol{\theta}}^{(0)} = \mathbf{d}_0 \oplus \boldsymbol{\theta} \Delta t \mathbf{v}_0$$

(1.7) Compute initial dynamic residual

$$\widetilde{\mathbf{f}}^{(i)} = \widetilde{\mathbf{f}}_{n+\theta} - \mathbf{M}\mathbf{d}_{n+\theta}^{(i-1)} - (\theta \Delta t)^2 \beta (1+\alpha) \mathbf{f}^{int}(\mathbf{d}_{n+\theta}^{(i-1)})$$

(1.8) Set  $n = 0, t = t_0 + \Delta t, n_{beg} = 1$ 

(2) STEP LOOP: for  $n = n_{beg}$ ,  $n_{beg} + 1$ , ...

(2.1) Form and Assemble Stiffness Matrix based on predicted displacements

(2.2) Compute the Dynamic Operator

$$\mathbf{E} = [\mathbf{M} + (\theta \Delta t)^2 \beta (1 + \alpha) \mathbf{K} (\mathbf{d}_{n+\theta}^{(0)})]$$

(3) ITERATION LOOP: i = 1, 2, ... (iter = i+1 = 2, 3, ...)

(3.1) Solve for incremental displacement change

$$\mathbf{E}\delta \mathbf{d}_{n+ heta}^{(i)} = \overline{\mathbf{f}}_{n+ heta}^{(i)}$$

(3.2) Update displacements

$$\mathbf{d}_{n+\theta}^{(i)} = \mathbf{d}_{n+\theta}^{(i-1)} \oplus \delta \mathbf{d}_{n+\theta}^{(i)}$$

(3.3) Set iteration counter

$$i \leftarrow i+1$$

(3.4) Compute new Dynamic Residual

$$\mathbf{\tilde{f}}^{(i)} = \mathbf{\tilde{f}}_{n+\theta} - \mathbf{M}\mathbf{d}_{n+\theta}^{(i-1)} - (\theta \Delta t)^2 \beta (1+\alpha) \mathbf{f}^{int}(\mathbf{d}_{n+\theta}^{(i-1)})$$

(3.5) Check Convergence

call CHK\_CONV ( 
$$\mathbf{r}_{n+1}^{(i+1)}, \delta \mathbf{d}, \hat{\epsilon}^{(i)}, \epsilon_{ref}, \hat{\epsilon}_{tol}, \text{num_div} \rightarrow \hat{\epsilon}^{(i+1)}, \langle \text{CONVERGED} \rangle, \langle \text{DIVERGED} \rangle$$
)

if ( <CONVERGED> ) then

num\_iters\_required = iter  $n \leftarrow n + 1$ go to (2.3) STEP LOOP

elseif ( <DIVERGED> .or. (iter > max\_iters) ) then

if ( num\_cuts < max\_cuts ) then

 $\Delta t_{n+1} = \Delta t_{n+1}/2$ num\_cuts = num\_cuts + 1  $n_{beg} = n$ GO TO (1.3)

else

STOP

endif

else

go to (3) ITER LOOP

endif

(2.3) Compute acceleration at  $n + \theta$ 

$$\mathbf{a}_{n+\theta} = \frac{1}{(\theta \Delta t)^2 \beta} (\mathbf{d}_{n+\theta} - \widetilde{\mathbf{d}}_{n+\theta})$$

(2.4) Compute acceleration at n+1

$$\mathbf{a}_{n+1} = \frac{1}{\theta}\mathbf{a}_{n+\theta} + (1-\frac{1}{\theta})\mathbf{a}_n$$

(2.5) Extract velocities

$$\mathbf{v}_{n+1} = \mathbf{v}_n + \Delta t[(1-\gamma)\mathbf{a}_n + \gamma \mathbf{a}_{n+1}]$$

(2.6) If  $\theta \neq 1$ , recompute displacements

$$\mathbf{d}_{n+1} = \mathbf{d}_n \oplus \{\Delta t \mathbf{v}_n + \Delta t^2 [(\frac{1}{2} - \beta) \mathbf{a}_n + \beta \mathbf{a}_{n+1}]\}$$

(2.7) Update counters, timestep

$$n \leftarrow n+1; \quad t \leftarrow t+1$$

(2.8) Check to see if  $t > t_{max}$  or  $n > n_{max}$ 

(2.9) If either statement in 2.8 is true, STOP; else GO TO 2.10 (2.10) Compute  $\tilde{d}_{n+\theta}$ 

$$\widetilde{\mathbf{d}}_{n+\theta} = \mathbf{d}_n + \theta \Delta t \mathbf{v}_n + (\theta \Delta t)^2 (\frac{1}{2} - \beta) \mathbf{a}_n$$

(2.11) Compute external loads  $f^{ext}(t)$  at current time t

(2.12) Compute  $\tilde{f}_{n+\theta}$ 

$$\mathbf{\widetilde{f}}_{n+\theta} = (\theta \Delta t)^2 \beta [\mathbf{f}^{ext}(t_{n+\theta}) + \alpha \mathbf{f}^{int}(\mathbf{d}_n)] + \mathbf{M} \mathbf{\widetilde{d}}_{n+\theta}$$

(2.13) Compute initial estimate of new solution

$$\Delta \mathbf{d}_{n+\theta} = \widetilde{\mathbf{d}}_{n+\theta} + (\theta \Delta t)^2 \beta \mathbf{a}_n - \mathbf{d}_n$$
$$\mathbf{d}_{n+\theta}^{(0)} = \mathbf{d}_n \oplus \Delta \mathbf{d}_{n+\theta}$$

(2.14) END STEP\_LOOP

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## NOTATION

d	Displacement vector.
v	Velocity vector.
a	Acceleration vector.
$\delta \mathbf{d}$	Iterative change in d.
ã	Extrapolated displacement from step n
$\hat{\mathbf{f}}^{ext}$	External force vector — base load.
f <sup>int</sup>	Internal force vector.
f <sup>ext</sup>	External force vector.
Ĩ	Extrapolated out-of-balance force.
Ī	The dynamic residual.
К	Stiffness matrix.
num_cuts	Number of times load step has been cut in half at current step.
num_div	Number of consecutive iterations at which divergence occurs.
ê	Relative error in energy norm.
ε	Absolute error in energy norm.
Eref	Reference value of $\epsilon$ ; initialized as zero.
€tol	Relative error tolerance (default: $10^{-4}$ ).
λ	Load factor.
<b>d</b> ′	Base value of specified displacement vector.
ď	Current value of specified displacement vector. $\mathbf{d}^{s} = \lambda  \widehat{\mathbf{d}}^{s}$ .
t	Problem time.
$\Delta t$	Time increment.
$n + \theta$	Time at step $n + \theta \Delta t$

#### **3.11.11 PROCEDURE LISTING**

```
*procedure NL_DYNAMIC_1 ( --
                     beg_step =1 ; -- . Starting step number (>0)
                     max_steps=1 ; -- . Maximum steps to compute
                     max_iters=9 ; -- . Naximum iterations per step
                     des_iters=4 ; -- . Number of iterations desired
                     fac_steps=1 ; -- . Steps_per_refactoring
                     max_cuts=3 ; -- . Maximum number of step cuts
                     tol_e=1.E-3 ; -- . Energy error tolerance
                     beg_time ; -- . Starting time
                     max_time ; -- . Upper_bound on time
                     del_time
                                 ; -- . Time increment
                     int_pars = 1.,0.,.25,.5 ; -- . Itegration parameters
                     load_stiff=<false> ; -- . Include load stiffness
                     FT_proc=FT_ZERO
                                       ; -- . Name of force-time procedure
                                       ; -- . Parameter array for above
                     PT_args
                     debug=<FALSE>; -- . Debug_print switch
                     NL_GEOM = 2 ; -- . Geom. Nonlin. Level (1|2)
                     COROTATION=1 ; -- . Corotational Flag (leave on !!)
                     Nominal_DB = NOMINAL.GAL ; -- . Selected Output
                     Nominal_DS = RESPONSE.HISTORY ; --
                     N_SELECT ; SEL_NODES; SEL_DOFS --
                   )
 *Remark
                             *Remark |
                                                                   1
 *Renark
                           NL_DYNAHIC_1
 *Remark
 *Renark
                CSM Testbed Procedure for Nonlinear Statics:
*Renark
*Remark
                    o Corotational Newton/Raphson algorithm
                    o Linearized Crisfield/Riks arc-length control
*Remark
*Remark
                    o Applied forces and/or displacements
 *Remark
*Renark
                Authors: G.M. Stanley and C.C. Rankin
*Remark
                 Version: MAR-03-1988
*Remark |
                                                                    L
 *Renark
. INITIALIZATION
*def/i ns_overwrite == <false>
*def/i debug == [debug]
*def/i max_step == <[beg_step]+[max_steps]-1>
#def/i num_iters == [des_iters]
                == [Nominal_DB]
*def/a NOM_DB
*def/a NOM_DS
                  == [Nominal_DS]
*def/i N_SELECT
                  == [N_SELECT]
*dof/i SEL_NODES[1:<N_SELECT>] == [SEL_NODES]
*def/i SEL_DOFS[1:<N_SELECT>] == [SEL_DOFS]
*def/i NL_GEOM
                 == [NL_GEOM]
+def/i COROTATION == [COROTATION]
```

```
#def/d beg_time
                     == [beg_time]
 *def/d max_time
                     == [max_time]
 *def/d int_pars[1:4] = [int_pars]
. . . . . Set time integration parameters
 *def/d theta == <int_pars[1]>
 #def/d alpha == <int_pars[2]>
 *def/d newm_bet == <int_pars[3]>
 #def/d news_gam == <int_pars[4]>
. . . . Initialize dataset names, constants
 *CALL DEFND ( STEP = [BEG_STEP]; ITER = 0 )
 *IF [BEG_STEP] /EQ 1 /THEN
    *Remark INITIALIZATION:
    *call NL_INITD
    *def/d t == [beg_time]
    *def/d dt == [del_time]
 *else
    *if < [del_time] /eq 0.0 > /then
       *def/d dt == <dt_n>
    *else
       *def/d dt == [del_time]
    *endif
    *def/d
              == <t_n>
 *endif
. . . . Set initial step, initial iteration parameters
 *def/i pass == 1
 *def/i tot_iters == 1
 *def/i istep == [beg_step]
. . . . Set initial time, basic time integration scalars
*def/d one_p_alp == <1. + <alpha>>
*def/d b_op_a
               == <<nevm_bet>*<one_p_alp>>
*def/d h_m_bet == <.5 - <newm_bet>>
#def/d o_d_th
                 == <1./<theta>>
#def/d o_m_odth == <1. - <o_d_th>>
*def/d o_m_gam == <1. - <nevm_gam>>
. . . . Reintery for problem restart on failure of convergence
. . . System is treated as a new initial value problem
:NEW_PASS
                     . Re-entry point for step-size reduction
. . . . Set iteration and step-independent integration scalars
*def/d th_dt
                     == <<theta>*<dt>>
*def/d t_wils
                     == <<t> + <th_dt>>
#def/d th_dt_sq
                     == <<th_dt>*<th_dt>>
```

```
*def/d th_b
                    == <<news_bet>*<th_dt_sq>>
 *def/d a_th_b == <<th_b> * <alpha>>
 *def/d o_d_thb == <1./<th_b>>
 #def/d f0_coef == <<b_op_a> - .5>
 #def/d k_coeff #= <<th_dt_sq>*<b_op_a>>
 #def/d v_n_coeff == <<dt>*<o_m_gam>>
 *def/d v_np1_coeff == <<dt>*<nevs_gam>>
 #def/d dtsq == <<dt>#def/d dtsq
 *def/d h_mb == <<dtsq>*<h_m_bet>>
 #def/d dt_b == <<dtsq>#<newm_bet>>
 #def/d h_mb_th ## <<th_dt_sq>#<h_m_bet>>
. . . . Set initial displacement estimate, first step
. . . . Set initial estimate of weighted out-of-balance forces
. . . . Compute external force weighting constant lambda_n(time)
    *call [FT_proc] ( T = <t>
                                           ; -- . Problem time
                      FT_ args = [ft_args] ; -- . Force-time paremeters
                      F_mac = lambda_n ). External forcing scale factor
    *call FORCE ( type
                              = EXTERNAL
                                                 ; --
                  nl_geom
                              = [nl_geom]
                                                 ; --
                  nl_load
                               = <true>
                                                 ; --
                  displacement = <d_n>
                                                 ; --
                  rotation = <T_n>
                                                 ; --
                  corotation = [corotation]
                                                 ; --
                  load_factor = <lambda_n>
                                                 ; --
                  input_force = <F_ref>
                                                ; --
                  output_force = <F_ext> )
  . . Set internal force
    *call FORCE ( type
                              = INTERNAL
                                                  : --
                  nl_geom = [nl_geom]
                                                  ; ---
                  displacement = <d_n>
                                                  ; ---
                  rotation
                             ≠ <T_n>
                                                 ; ---
                  corotation = [corotation]
                                                  ; --
                  output_force = <F_int> )
. stop_1
            *stop
. . . . Weighted difference between internal and external force
 [XQT VEC
 <a_th> <- <f_ext> - <f_int>
 <f_bar> <- <h_m_bet> <F_ext> + <f0_coef> <F_int>
. . . External force at time = T + <theta> * DT
    *call [FT_proc] ( T = <t_wils>
                                       ; -- . Problem time
                      FT_ args = [ft_args] ; -- . Force-time paremeters
                      F_mac = lambda_np1
                                            ) . External forcing scale factor
    *call FORCE ( type
                               = EXTERNAL
                                                  ; --
```

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```
nl_geom = [nl_geom]
nl_load = <true>
                                             ; --
                nl_load
                                             ; --
                displacement = <d_n>
                                            ; ---
                rotation = <T_n>
                                            : --
                corotation = [corotation]
                                            ; --
                load_factor = <lambda_npi>
                                           ; --
                input_force = <F_ref>
                                             ; --
                output_force = <F_ext> )
. . . . Add correction to external force
[XOT VEC
 <f_bar> <- <f_bar> + <news_bet> <F_ext>
 <f_bar> <- <th_dt_sq> <f_bar>
. . . . Initial estimate of displacements
 <delta> <- <th_dt> <v_n>
 <d_np1_i> <- <d_n> + <delta>
 ROTATE <T_n> * <delta> -> <T_np1_i>
 <d_tilde> <- <d_np1_i>
. . . . Scaling displacement increment for convergence check
. stop_2 *stop
 PROD <inv_mass> <a_th> -> <d_inc_i>
 <d_inc_i> <- <h_mb_th> <d_inc_i> + <delta>
. . . Mass * Displacements + scaled out-of-balance force
PROD <mass> <d_np1_i> -> <f_tilde>
<f_tilde> <- <f_tilde> + <f_bar>
. . . BEGIN STEP_LOOP ******** ********* ********
*D0 :STEP_LOOP $n = <istep>, <[max_steps]-1>
    *def/i step == <$n>
    *Remark
    *remark _____
    Fremark
                BEGINNING STEP <STEP>
    *Remark
    *renark _____
    *remark
    *call CONSTRAIN ( load_factor = <lambda_np1 > ; --
                    applied_motion = <d_spec> ; --
                                                   )
                    displacement = <d_np1_i>
. . . Form Stiffness based on Predictor
```

```
*call STIFFNESS ( type
                                   = TANGENT
                                                     ; ---
                        nl_geom = [nl_geom]
nl_load = [load_stiff]
                                                     ; ---
                                                      ; --
                        load_factor = <lambda_np1> ; --
                        displacement = <d_np1_i>
                                                    ; --
                        rotation = <T_np1_i>
                                                     ; ---
                        corotation = [corotation] ; --
                                                        ) . output
                        stiffness = <K_asm>
 . . Combine MASS and STIFFNESS into one matrix <M_p_K>
       *call MASS_STIFF ( mass
                                     = <mass>
                                                 ; -- . Mass vector
                                     = <K_asm> ; -- . Assembled Stiffness
                         stif
                         mult
                                     = <k_coeff> ; -- . Stiffness Multiplier
                         M_p_K
                                     = <M_p_K> ) . The dynamic operator
 . . Factor DYNAMIC OPERATOR
       *call FACTOR
                      ( input_matrix = <M_p_K> ; --
                        output_matrix= <M_p_K> )
 . . Obtain MASS RESIDUAL
    *call FORCE ( type
                             = INTERNAL
                                                 ; ---
                 nl_geom = [nl_geom]
                                                 ; ---
                 displacement = <d_np1_i>
                                                 ; --
                 rotation = <T_np1_i>
                                                ; --
                 corotation = [corotation]
                                                ; --
                 output_force = <F_int> )
. stop_3 *stop
[XQT VEC
    PROD <mass> <d_np1_i> -> <R_np1_i>
    <R_np1_i> <- <f_tilde> - <R_np1_i>
    <R_npi_i> <- <R_npi_i> - <k_coeff> <F_int>
. . . Initialize Convergence Criteria
    *call CHKCNVD ( STEP
                                    = 1
                                                       ; --
                   ITER
                                    = 1
                                                       ; ---
                   Residual_force = <R_np1_i>
                                                      ; --
                                                          )
                   displacement_inc = <d_inc_i>
. -- BEGIN ITERATION LOOP
                          ****** ******* ******* ********
. stop_4 *stop
*echo,on,ma,md
   *D0 :ITER_LOOP $i = 1, [max_iters]
```

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```
#def/i iter == <<$i>>+1>
         *def/i tot_iters == <<tot_iters>+1>
   . . . Compute Basic Displacement Iteration (delta_th)
         *call SOLVE ( rhs = <R_np1_i>; soln = <delta_th>; matrix = <N_p_K> )
   . . . Update Displacements, Rotations, Increments
EXOT VEC
          <d_np1_ip1> <- <d_np1_i> + <delta_th>
          ROTATE <T_np1_i> * <delta_th> -> <T_np1_ipi>
         *call CONSTRAIN ( load_factor = <lambda_npi>; --
                          applied_motion = <d_spec>
                                                    ; --
                           displacement = <d_np1_ip1> )
         *if < <DEBUG> > /then
            *print 1, <d_np1_ip1>
            *print 1, <T_np1_ip1>
         *endif
  . . . . Compute DYNAMIC RESIDUAL
    *call FORCE ( type
                              = INTERNAL
                                               ; --
                  nl_geom
                             = [nl_geom]
                                                ; ---
                  displacement = <d_np1_ip1>
                                                ; --
                  rotation = <T_np1_ip1>
                                                ; --
                  corotation = [corotation]
                                                ; ---
                  output_force = <F_int> )
[XOT VEC
PROD <mass> <d_np1_ip1> -> <R_np1_ip1>
<R_np1_ip1> <- <f_tilde> - <R_np1_ip1>
<R_np1_ip1> <- <R_np1_ip1> - <k_coeff> <F_int>
. . . . . CHECK CONVERGENCE
                                  = <step> ; -- . input
         *call CHKCNVD ( step
                          iter
                                   = <iter>
                                                 ; --
                          Residual_force = <R_np1_ip1> ; --
                          displacement_inc = <delta_th>
                                                          ; --
                                         = [tol_e]
                          tol_e
                                                       ; ---
                          max_iters
                                          = [max_iters] ; --
                          convergence = CONVERGENCE ; -- . output
                          divergence = DIVERGENCE
                                                           )
      *if <CONVERGENCE> /eq <TRUE> /then
        *jump to :CONVERGED
      *elseif <DIVERGENCE> /eq <TRUE> /then
        *if <pass> /le [max_cuts] /then
           *jump to :REPEAT
        *else
           *Remark Maximum number of automatic step cuts exhausted.
```

```
*jump to :DIVERGED
        *endif
      *endif
   :ITER_LOOP
   :NEUTRAL
   *if <pass> /le [max_cuts] /then
      *jump to :REPEAT
   +else
      *Remark Maximum number of automatic step cuts exhausted.
   *endif
                    NON-CONVERGENCE AT STEP <stop>. REVISE STRATEGY.
   *Remark
   +jump to :EXIT
   :REPEAT
    *def/i pass
                    == < <pass>+1 >
    *def/d dt == <<dt>*.5>
    *Remark
    *Remark CONVERGENCE DIFFICULTIES; REPEATING STEP <step>
    *Remark with half original time step
    *Remark New TIME increment is <dt>
    *Remark Pass: <pass>
    #jump to :NEW_PASS
   :DIVERGED
                    DIVERGENCE AT STEP <STEP>. REVISE STRATEGY.
   *Remark
   *jump to :EXIT
   : CONVERGED
                    CONVERGENCE AT STEP <STEP>.
   *Renark
   :NEXTSTEP
   *def/i num_iters == <iter>
   *def/d path_scale == <[des_iters]/<num_iters>>
   #def/d lam_n
                       == <lambda_np1>
   *def/i sign_det_n
                      == <sign_det>
   *def/i load_dir_n
                      == <load_dir>
. . . Compute current acceleration
 [XQT VEC
  #if <<theta> /ne 1.0> /then
    <a_th> <- <o_d_th> <d_np1_ip1> - <o_d_th> <d_tilde>
    <a_np1> <- <o_d_th> <a_th> + <o_odth> <a_n>
  *else
    <a_np1> <- <o_d_th> <d_np1_ip1> - <o_d_th> <d_tilde>
  *endif
. . . . Update velocity vector
 <a_th> <- <v_n_coeff> <a_n> + <v_npi_coeff> <a_npi>
  <v_np1> <- <v_n> + <a_th>
 . . . For strange (non-unity) values of Wilson's parameter, update
             displacements to step n+1
. . . .
 *if <<theta> /ne 1.0> /then
     <a_th> <- <h_mb> <a_n> + <dt_b> <a_np1>
```

```
<delta> <- <dt> <v_n> + <a_th>
    <d_np1_i> <- <d_n> + <delta>
   ROTATE <T_n> * <delta> -> <T_np1_i>
*endif
. . . . Postprocess and save results of computations st <<STEP> + 1>
  *call POSTSTPD ( step=<step>; iter=<iter> )
. . . . Reset iteration counters
*def/i pass == 1
*def/i tot_iters == 1
. . . . Update current time
*def/d t_wils == <<t> + <th_dt>>
*def/d t == <<t> + <dt>> . can be altered by path_scale
*stop
. . . . Check for max time and max steps
*if <<t> /gt <max_time> > /then
*remark *
*remark *
        Maximum problem time <max_time> reached or exceeded.
*remark *
                      Computation terminated
*remark *
                                                          *
*jump to :EXIT
*endif
*if <<step> /eq <<max_steps>- 1>>/then
*remark *
*remark * Maximum steps <max_steps> exceeded.
*remark *
                  Problem time is <t>
*remark *
*jump to :EXIT
*endif
. . . Reset step counter for datasets to step <<step> + 1>
*call DEFND ( STEP = <<STEP> + 1>; ITER=1)
. . . . Compute new "historical" displacement d_tilde
[XQT VEC
<a_th> <- <th_dt> <v_n> + <h_mb_th> <a_n>
<d_tilde> <- <d_n> + <a_th>
. . . . Compute new external force for step n+1
```

```
*call [FT_proc] ( T = <t_wils>
                                       ; -- . Problem time
                    FT_ args = [ft_args] ; -- . Force-time paremeters
                    F_mac = lambda_npi ). External forcing scale factor
                           = EXTERNAL
    *call FORCE ( type
                                             ; --
                 nl_geom
                           = [nl_geom]
                                             : --
                 nl_load = <true>
                                              ; --
                 displacement = <d_n>
                                              ; --
                 rotation = <T_n>
                                              ; --
                 corotation = [corotation]
                                             ; --
                 load_factor = <lambda_np1> ; --
                 input_force = <F_ref>
                                             ; --
                 output_force = <F_ext> )
. . . . Set internal force if Wilson's constant is not unity
    *if<<theta> /ne 1.> /then
       ; --
                                                 ; ---
                                                 ; --
                    displacement = <d_n>
                                                 ; --
                    rotation = <T_n>
                                                 : --
                                                 ; ---
                    corotation = [corotation]
                    load_factor = <lambda_np1>
                                                 ; --
                    input_force = <F_ref>
                                                 ; --
                    output_force = <F_int> )
     *endif
. . . . Weighted sum of internal and external force
[XQT VEC
 <f_bar> <- <th_b> <F_ext> + <a_th_b> <F_int>
PROD <mass> <d_n> -> <f_tilde>
<f_tilde> <- <f_tilde> + <f_bar>
. . . . Compute new initial estimate, displacements
[IQT VEC
 <delta> <- <d_tilde> - <d_n>
 <delta> <- <delta> + <th_b> <a_n>
 <d_np1_i> <- <d_n> + <delta>
 ROTATE <T_n> * <delta> -> <T_np1_i>
. . . End Step LOOP
:STEP_LOOP
:EXIT
*end
. =DECK CHKCNVD
*procedure CHKCNVD
                   ( STEP
                                           ; -- . input
                     ITER
                                           ; ---
                                           ; ---
                     DISPLACEMENT_INC
                     RESIDUAL_FORCE
                                           ; --
                     TOL_E
                                           ; ---
```

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```
MAX_ITERS
                                             ; --
                       CONVERGENCE=CONVERGENCE ; -- . output
                       DIVERGENCE =DIVERGENCE
[IQT VEC
. . Initialize
   +def/i [CONVERGENCE] == <FALSE>
   *def/i [DIVERGENCE] == <FALSE>
   #if [ITER] /gt 1 /then
      *def/d12.4 ERR_E_I == <ERR_E_IP1>
   *endif
. . Compute Current Incremental Energy Norm
   DOT [RESIDUAL_PORCE] * [DISPLACEMENT_INC] -> INC_E_IP1
   *if [ITER] /le 1 /then
      #if <ABS(<INC_E_IP1>)> /gt <REF_E> /then
         #def/d12.4 REF_E == <ABS(<INC_E_IP1>)>
      *endif
      *def/i
               num_diverges == 0
   *endif
. . Compute Error Norms
   *def/d12.4 ERR_E_RAW == < <INC_E_IP1>/<REF_E> >
   *def/d12.4 ERR_E_IP1 *= < <ABS(<ERR_E_RAW>)>^ .5 >
. . Check for displacement convergence
   *if < <ERR_E_IP1> /le [TOL_E] > /then
. . . Step Converged
     *DEF/I [CONVERGENCE] == <TRUE>
     *jump to :BOTTOM_LINE
   *endif
  #if < [ITER] /le 1 > :BOTTOM_LINE
. . . Step Not Converged; Check for Divergence
     *IF < <ERR_E_IP1>/<ERR_E_I> /GT 1.0 > /THEN
        *def num_diverges == < <num_diverges>+1 >
        *if <num_diverges> /gt 1 /then
           *DEF/I [DIVERGENCE] == <TRUE>
        *ENDIF
     *ENDIF
  :BOTTOM_LINE
  #def/e12.4 load_factor = <lambda_np1>
+remark
*remark _____
                                                  *remark
               ITER=[ITER] T=<t> LD=<load_factor>
               ERR=<err_e_ip1>
                                 REF=<ref_e>
*remark
```

```
+remark
*remark
+ END
. =DECK DEFND
*procedure DEFND ( step; iter )
. Purpose: Define basic macro_symbols for NL_DYNAMIC procedure
*def/i np1 = [step]
*def/i n = < <np1>-1 >
*if [iter] /eq 0 /then
                                  . run initialization
                  == 1
  *def/i NS_ldi
  *def/i NOM_ldi == 3
  *def/i iset
                  == 1
  *def/i icon
                  == 1
   *def/a f_spec
                  == APPL.FORC.<iset>.1
  *def/a d_spec
                  == APPL.MOTI.<iset>.1
. Check for Specified Displacement Loading
   #find dataset <NS_ldi> <d_spec> /seq=ids
  *if < <ids> /gt 0 > /then
     *Remark Note: Specified displacement dataset <d_spec> will be used
     *def/i spec_disp_flag == <true>
   *else
     *def/i spec_disp_flag == <false>
   *endif
  *def/a F_ref == REF.FORC
   *def/a f_ext == EXT.FORC
   *def/a f_int
                 == INT.FORC
                   == M.DIAG
   +def/a mass
  *def/a inv_mass == MINV.DIAG
  #def/a R_np1_i == RES.FORC
  *def/a R_np1_ip1 == RES.FORC
  *def/a d_inc_i == INC.DISP
   *def/a d_inc_ip1 == INC.DISP
  *def/a v_inc_i == INC.VEL
  *def/a v_inc_ip1 == INC.VEL
   #def/a delta_TH == THET.DISI
  *def/a a_TH == THET.ACC
  *def/a delta
                  == TOT.DISI
  *def/a d_tilde ## TILD.DISP
  *def/a f_tilde == TILD.FORC
  *def/a f_bar
                 == BAR.FORC
  *def/a K_asm
                  == K
   *def/a K_fac
                  == K
   *def/a M_p_K
                  == MpK
   Retrieve Control Parameters from DATA_BASE
   *if [step] /eq 1 /then
     *def/d t_n
                   == <beg_time>
```

```
#def/i sign_det == 1
      *def/d ref_e
                   == 0.0
      *def/d lambda_n == 0.0
      •Remark STARTING PARAMETERS INITIALIZED.
   *else
      +open <NOM_ldi> <NOM_DB>
      #find dataset <nom_ldi> <nom_ds> /seq=nom_ids
      *g2m /name==t_n
                            /type=D <nom_ldi> <nom_ids> TIME.<n>
      *g2m /name==sign_det_n /type=I <nom_ldi> <nom_ids> SIGN_DET.<n>
      *g2m /name==lambda_n /type=D <nom_ldi> <nom_ids> LOAD.<n>
                           /type=D <nom_ldi> <nom_ids> REF_ERR.<n>
      *g2m /name==ref_e
      *close <NOM_ldi>
      *Remark
      *remark _____
      *remark
      *Remark
              RE-START PARAMETERS:
      *Remark
                 TIME
                                        = <t_n>
      *Remark
                  SIGN_DET (n)
                                        = <sign_det_n>
                  LOAD
      *Remark
                                         = <lambda_n>
      *remark
      *remark _____
   *endif
*endif
. Define Global Datasets for Upcoming Step
*def/a d_n
                == TOT.DISP.<n>
*def/a d_np1_i == TOT.DISP.<np1>
*def/a d_np1_ip1 == TOT.DISP.<np1>
              == TOT.VEL.<n>
*def/a v_n
+def/a v_np1
               == TOT.VEL.<np1>
*def/a a_n
               == TOT.ACC.<n>
*def/a a_np1
               == TOT.ACC.<np1>
*def/a T_n
                == TOT.ROTN. <n>
*def/a T_np1_i == TOT.ROTN.<np1>
#def/a T_np1_ip1 == TOT.ROTN.<np1>
*end
. =DECK FT_ZERO
*procedure FT_ZERO ( t ; ft_args ; F_mac )
. . . . Provide for zero dependence of force on time (no external forces)
#def/d [F_mac] == 0.
*end
. =DECK FT_LIN
*procedure FT_LIN ( t ; ft_args ; F_mac )
. . . . Provide piecewise linear forcing function
*def/d ft_args[1:5] = [ft_args]
```

```
*if <[t] /le <ft_args[2]>> /then
     *def/d [F_mac] == 0.
*elseif <[t] /lt <ft_args[3]>> /then
     *def/d c_fact = <<ft_args[3]>-<ft_args[2]>>
     *if <<c_fact> /le 0.> /then
          #def/d [F_mac] == <ft_args[1]>
     *else
          *def/d [F_mac] == <<<[t]-<ft_args[2]>> * --
                      <ft_args[1]>>/<c_fact>>
     *endif
*elseif <[t] /le <ft_args[4]>> /then
     *def/d [F_mac] == <ft_args[i]>
*elseif <[t] /lt <ft_args[5]>> /then
     *def/d c_fact = <<ft_args[5]>-<ft_args[4]>>
     *if <<c_fact> /le 0.> /then
          *def/d [F_mac] == 0.
     *else
          *def/d [F_mac] == <<<<ft_args[5]> - [t]> + --
                     <ft_args[1]>>/<c_fact>>
     *endif
*else
      +def/d [F_mac] == 0.
 *endif
*end
. =DECK PT_SIN
*procedure FT_SIN ( t ; ft_args ; F_mac )
 *def/d ft_args[1:6] = [ft_args]
 . . . . Piecewise sinusoidal forcing function
 *if <[t] /ge <ft_args[6]>> /then
     +def/d [F_mac] = 0.
 *elseif <[t] /ge <ft_args[5]>> /then
     *if <<ft_args[3]> /le 0.> /then
         *def/d [F_mac] == 0.
     +else
         *def/d tc = <<<[t] - <ft_args[4]>>*<pi>>/<ft_args[3]>>
         *def/d [F_mac] == <<ft_args[2]> + <cos(<tc>)> * <ft_args[1]>>
     *endif
 +else
     +def/d [F_mac] == 0.
 *endif
*end
. =DECK FT_EXP
*procedure FT_EXP ( t ; ft_args ; F_mac )
  . . . Exponential docay
```

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```
*def/d ft_args[1:3] = [ft_args]
*if <[t] /lt <ft_args[2]>> /then
    +def/d [F_mac] == 0.
÷else
    #def/d apl = <.6931471806/<ft_args[3]>>
    #def/d axl = <<apl>*<[t] - <ft_args[2]>>>
    *def/d [F_mac] ** <<ft_args[1]>* <EXP(-<axl>)>>
*endif
*end
. =DECK NL_INITD
*procedure NL_INITD ( ldi=1 )
  ------
  PERFORM STANDARD INITIALIZATION
  *call INITIALIZE ( constraint_set = <icon> )
  . CLEAR INITIAL DISPLACEMENTS AND ROTATIONS (n = 0)
  *g2m /name=num_nodes /type=i [ldi] MODEL.SUMMARY NUM_NODES
  *g2m /name=num_dofs /type=i [ldi] MODEL.SUMMARY NUM_DOFS
          Problem Dimensions: N_nodes = <num_nodes>, N_dofn = <num_dofs>
  *Renark
  #find dataset <NS_ldi> <d_n> /seq=ids_disp
  #if < <ids_disp> /gt 0 > /then
     *Remark Note: Initial displacement dataset <d_n> will be used
  +else
     INIT_VEC <d_n> <num_dofs> BY <num_nodes> . Zeroize translations
     *Remark
              Displacements (<d_n>) initialized.
  *endif
  *find dataset <NS_ldi> <T_n> /seq=ids_rotn
  *if < <ids_rotn> /gt 0 > /then
     *Remark Note: Initial rotation dataset <T_n> will be used
  *else
     INIT_VEC <T_n> 3
                            BY <num_nodes> . Zeroize rotation pseudovectors
     *Remark
             Rotations (<T_n>) initialized.
  *endif
  *find dataset <NS_ldi> <v_n> /seq=ids_vel
  *if < <ids_vel> /gt 0 > /then
     *Remark Note: Initial velocity dataset <v_n> will be used
  *else
    INIT_VEC <v_n> <num_dofs> BY <num_nodes> . Zeroize velocity
    *Remark
             Velocities (<v_n>) initialized.
  *endif
  *find dataset <NS_ldi> <a_n> /seq=ids_acc
  #if < <ids_acc> /gt 0 > /then
     *Remark Note: Initial acceleration dataset <a_n> will be used
  **].**
     INIT_VEC <a_n> <num_dofs> BY <num_nodes> . Zeroize acceleration
     *Remark Accelerations (<a_n>) initialized.
  *endif
         ______
```

#### NL'DYNAMIC'1

```
. FORM INITIAL (BASE-LOAD) EXTERNAL-FORCE VECTOR
 *call FORCE ( type = EXTERNAL ; --
              input_force = <f_spec> ; --
                                       )
              output_force = <F_ref>
 . Form mass and inverse mass (diagonal form)
  *remark
*remark MASS bypassed for testing purposes defined in BASE.DBC
*remark
   *call MASS ( type = DIAGONAL ; --
               BASS = <BASS>
                                   )
  [XQT VEC
     DIAG_INV <mass> -> <inv_mass>
+and
. =DECK MASS_STIPP
*procedure MASS_STIFF ( mass
                            ; -- . diagonal mass vector
                            ; -- . assembled stiffness
                     stif
                             ; -- . the dynamic weighting factor
                     mult
                     M_p_K
                             ) . the dynamic operator
[XOT AUS
   DEFINE M = <NS_1di> M DIAG
   DEFINE K = <NS_1di> [STIF] SPAR 36
   [M_p_K] SPAR 36 = SUM(M, [MULT] K)
*end
. =DECK POSTRES
*procedure POSTRES ( step )
 [XQT VEC
 #find dataset <NOM_LDI> <NOM_DS> /seq=post_ids
 #if < <post_ids> /le 0 > /then
    *put dataset <NON_LDI> <NON_DS> /mrat=2000 /seq=post_ids
 endif
. Save selected displacements on nominal data-base
  *def/a dof_names = U, V, W, RU, RV, RW
  *do $isel = 1, <N_SELECT>
   *def/i node = <SEL_NODES[<$isel>]>
   #def/i dof = <SEL_DOFS[<$isel>]>
   *def/a dof_name = <dof_names[<dof>]>
    COMPONENT <node> <dof> TOT.DISP.[step] -> DISP
   *def/a recd_name = DISP_<dof_name>_<node>.[step]
   *Remark <recd_name> = <DISP>
   *m2g /name=disp /type=d <nom_ldi> <post_ids> <recd_name>
    Save Reaction Forces for Current Step
```

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```
REAC.FORC.[step] <- INT.FORC
    *if < [step] /eq 0 > /then
      REAC.FORC.0 <- 0.0
    *endif
    #if < <spec_disp_flag> > /then
       COMPONENT <node> <dof> REAC.FORC.[step] -> FORCE
      *def/a recd_name = FORCE_<dof_name>_<node>.[step]
      *Remark <recd_name> = <FORCE>
      *m2g /name=force /type=d <nom_ldi> <post_ids> <recd_name>
    *endif
   *enddo
*end
. =DECK POSTSTPD
*procedure POSTSTEP ( step; iter )
*Remark _____
*Remark STEP [step] SUMMARY :
*Remark
*Remark Load Factor _____ <lambda_npi>
*Remark Stiffness determinant _____ <coef_det> * 10 ^ <exp10_det>
*Remark Number of negative roots _____ <num_neg>
*Remark Relative energy_error _____ <err_e_ipi>
*Remark Number of Iterations _____ <num_iters>
*Remark Number of Step Cuts _____ <<pre>//pass>-1>
*Remark Total Number of Iterations _____ <tot_iters>
*Remark _____
                        *open <NOM_ldi> <NOM_DB>
*if < [step] /eq 1 > /then
   *call POSTRES ( step = 0 )
  #def/d load_0=0.
  *m2g /name=load_0 /type=d <NOM_LDI> <NOM_DS> LOAD.0:0
*endif
*call POSTRES ( step=[step] )
*find dataset <NOM_LDI> <NOM_DS> /seq=nom_ids
*m2g /name=lambda_np1 /type=d <nom_ldi> <nom_ids> LOAD.[STEP]
*m2g /name=err_e_ip1 /type=d <nom_ldi> <nom_ids> ERROR.[STEP]
*m2g /name=ref_e
                   /type=d <nom_ldi> <nom_ids> REF_ERR.[STEP]
*m2g /name=sign_det
                    /type=i <nom_ldi> <nom_ids> SIGN_DET.[STEP]
*m2g /name=coef_det
                    /type=d <nom_ldi> <nom_ids> COEF_DET.[STEP]
*m2g /name=exp10_det /type=i <nom_ldi> <nom_ids> EXP10_DET.[STEP]
                   /type=d <nom_ldi> <nom_ids> NEG_ROOTS.[STEP]
*m2g /name=num_neg
*m2g /name=num_iters /type=i <nom_ldi> <nom_ids> NUM_ITERS.[STEP]
*m2g /name=tot_iters /type=i <nom_ldi> <nom_ids> TOT_ITERS.[STEP]
*m2g /name=t
                    /type=i <nom_ldi> <nom_ids> TIME.[STEP]
*def/i passm1 = <<pre>pass>-1>
*m2g /name=passm1 /type=i <nom_ldi> <nom_ids> NUM_CUTS.[STEP] . cgl, 7/26/88
*close <NOM_ldi>
*end
```

#### 3.11.12 REFERENCES

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- 3.11-2 Hilber, H.M. and Hughes, T.J.R, "Colocation, Dissipation and Overshoot for Time Integration Schemes in Structural Dynamics," *Earthquake Engineering and Structural Dynamics*, Vol. 6, pp. 99-118, 1978.
- 3.11-3 Newmark, N.M., "A Method of Computation for Structural Dynamics," Journal of the Engineering Mechanics Division, ASCE, pp. 67-94, 1959.
- 3.11-4 Hilber, H.M., Hughes, T.J.R., and Taylor, R.L., "Improved Numerical Dissipation for Time Integration Algorithms in Structural Dynamics," *Earthquake Engineering* and Structural Dynamics, Vol. 5, pp. 283-292, 1977.
- 3.11-5 Bathe, K.J., and Wilson, E.L., "Stability and Accuracy Analysis of Direct Integration Methods," *Earthquake Engineering and Structural Dynamics*, pp. 283-291, 1973.
- 3.11-6 Wilson, E.L., "A Computer Program for Dynamic Stress Analysis of Underground Structures," SESM Report No. 68-1, Division of Structural Engineering and Structural Mechanics, University of California, Berkeley, 1968.

# 4.0 Application Procedures

The procedures documented in this chapter are representative of the types of procedures that may be written to solve specific application (structural analysis) problems. Many of these high-level procedures invoke other (lower-level) procedures to perform preprocessing, solution, and postprocessing functions; which are described elsewhere in this manual. The use of procedures to perform structural analysis applications can provide users flexibility for parameterizing geometric data (e.g., stiffener spacing) as well as spatial discretization parameters (e.g., number of elements). The problems represented here are also intended to serve as part of a standard series of test problems to assess new structural elements installed in the CSM Testbed.

A summary of the procedures found in this chapter is provided in Tables 4.0-1.

Procedure Name	Problem Description						
CLAMPED_BEAM	Transient response of a clamped beam modeled with 2-D shell elements.						
COMPRESSED_CYL	Classical buckling and postbuckling analysis of an axially compressed cylindrical shell; modeled with shell elements and initial imperfections.						
COOKS_MEM	Linear in-plane bending response of a wing-like trape- zoidal plate modeled with shell elements. (Referred to as Cook's membrane problem in the literature.)						
ELASTICA	Classical large rotation analysis of a cantilevered beam with an applied end moment. Final configuration is a complete circle — with 360 degrees rotation at the free edge. Modeled with shell elements.						
EULER_COLUMN	Inplane buckling of a column modeled with 2-D shell ele- ments. An overall Euler buckling modeshape is obtained.						
FOCUS_PANEL	Analysis of the composite blade-stiffened panel with a dis- continuous center stiffener.						
FREE_EDGE	Free-edge stress analysis of a 4-ply composite laminate.						
GEN_STF_PANEL	Linear buckling analysis of stiffened panel configurations subjected to combined in-plane compression and shear loading. Configurations considered include flat rectangu- lar panels with hat-stiffeners, z-stiffeners and blade stiff- eners, as well as a corrugated panel. Modeled with shell elements.						
HINGED_CYL	Postbuckling (nonlinear) analysis of a hinged cylindrical shell subjected to concentrated transverse load. Shell ex- hibits snap-through buckling behavior and requires a so- lution algorithm employing arc-length step control. Mod- eled with shell elements.						

Procedure Name	Problem Description
PEAR_CYL	Buckling analysis of a pear-shaped cylindrical shell sub- jected to axial compression. Modeled with shell elements.
PINCHED_CYL	Linear inextensional bending of a thin pinched cylindri- cal shell. Modeled with shell elements; two opposing radial forces applied at center; and both free and rigid- diaphragm edges considered. (MacNeal-Harder case)
PW_HOLE	Linear elastic stress analysis of a rectangular isotropic plate with a central circular hole.
RECT_PLATE	Eigenvalue (vibration and buckling) analyses of a rect- angular plate subjected to various inplane loading condi- tions.
RHOMBIC_PLATE	Linear bending of a simply supported rhombic plate under constant pressure. (MacNeal-Harder case)
TRUNCATED_CONE	Linear transient dynamic analysis of impulsively loaded truncated cone.
VIB_2D	Vibration analysis of a bar, beam, or ring modeled with 2-D shell elements.

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# 4.1 Processor CLAMPED\_BEAM

THIS SECTION UNDER PREPARATION

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## 4.2 Procedure COMPRESSED\_CYL

#### 4.2.1 GENERAL DESCRIPTION

#### 4.2.1.1 Problem Description

This application problem involves the static buckling and postbuckling analysis of a thin cylindrical shell  $(R/t \approx 300)$  simply supported along its edges, and subjected to uniform axial compression (see Figure 4.2-1). It is a particularly important classical problem for testing linear and nonlinear performance of shell elements, as well as solution algorithms capable of traversing non-monotonic load-displacement curves. A noteworthy feature of the problem is that the buckling eigenvalues of the cylindrical shell are very closely spaced, even though the mode shapes are radically different. This can pose a challenge for both eigensolvers and nonlinear solution algorithms — which are expected to find and maintain the physically dominant (lowest-energy) mode. (It is interesting that the buckling characteristics of this simple cylindrical shell problem have much in common with the more practical problem of an optimally-stiffened cylinder, which also has many diverse mode shapes occurring at the same critical load level.) Another noteworthy feature is that such problems are notoriously imperfection sensitive. Thus, a small initial geometric imperfection can cause a substantial reduction in the peak axial load capacity, compared with the classical critical buckling load corresponding to a perfect cylinder. This implies that the model must be refined enough to represent the initially imperfect configuration, as well as the finally deformed configuration.

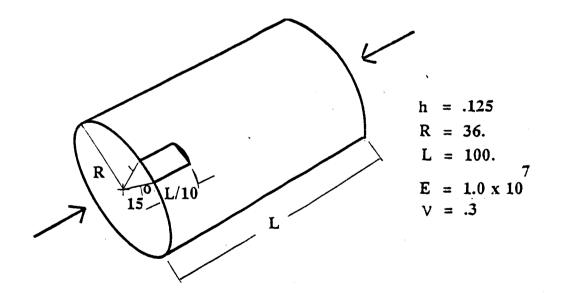


Figure 4.2-1 Compressed Cylinder Problem.

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# 4.2.1.2 Model Description

Procedure COMPRESSED\_CYL employs a partial  $(L/10 \times 15^{\circ})$  shell-element based model of the cylindrical shell to capture both linear and nonlinear response. A typical model is shown in Figure 4.2-2. The mesh is rectangular in topology, and restricted to quadrilateral shell elements of either 4- or 9-node variety. Symmetry conditions on all but the one edge that is simply supported enable the model to represent the lowest energy buckling mode with a relatively small number of elements. This particular ("diamond") mode shape consists of 5 axial half-waves and 12 circumferential whole waves over the entire cylinder (in classical terminology: m=5, n=12). Thus, the partial model will contain 1 axial quarter-wave and 1 axial half-wave, and less than 10 shell elements should be required in each direction to obtain engineering accuracy. The axial force is distributed evenly and consistently on the simply supported edge; and is scaled so that the magnitude corresponds to the classical buckling load.

## 4.2.1.3 Analysis Description

The analysis is conducted in stages, some of which are optional. First, a linear buckling (eigenvalue) analysis is performed (using procedure L\_STABIL\_1). Due to the selected magnitude of the applied load, the lowest eigenvalue should be close to 1 (for a sufficiently refined mesh). Next, the buckling mode corresponding to the lowest (critical) eigenvalue is scaled and used to perturb the geometry. This is achieved by adding the scaled radial displacements to the initial finite element nodal coordinates. The scale factor is selected so that the maximum radial perturbation is some percentage of the shell thickness (see procedure IMPERFECTION). This initial imperfection is necessary to trigger a realistic postbuckling response in the nonlinear analysis. Due to the extreme imperfection sensitivity of thin axially-compressed cylinders (e.g., see ref. 4.2-3) as little as a 1%-thickness imperfection is adequate to trigger such a response (although a 10%-thickness imperfection is recommended). The nonlinear (postbuckling) analysis is then begun (using procedure NL\_STATIC\_1). A reasonable description of the load-displacement history can usually be obtained with about 20-30 load steps, from a starting load of about one-tenth of the classical buckling load.

## 4.2.1.4 Available Solutions

Analytical solutions are available for the buckling (eigenvalue) analysis (e.g., see ref. 4.2-1). Several of the buckling modes corresponding to the classical stability solution are shown in Figure 4.2-2 (Figure 6.9 of ref. 4.2-2) using finite-element meshes. Note that the critical loads (or eigenvalues) for these diverse mode shapes – smooth, axisymmetric, and diamond-pattern – are within 5% of one another. While there are no closed-form solutions for the nonlinear postbuckling response of the axially-compressed cylindrical shell, there are approximate solutions for the "knock-down" factor corresponding to a given initial imperfection, and various numerical solutions are given in the CSM Testbed Applications Manual (see ref. 4.2-4). Figure 4.2-3 gives a sampling of these numerically obtained response curves, for different magnitudes of initial imperfection (50%, 10% and 1% of the shell thickness). Note that with only a 10%-thickness imperfection, the peak load is "knocked-down" to approximately 70% of the value for a perfect (unattainable) shell.

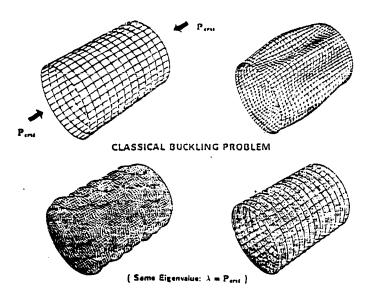


Figure 4.2-2 Buckling of Axially-Compressed Cylinder: Generic Problem Description

Figure 4.2-3 Postbuckling of Axially-Compressed Cylinder:

## 4.2.2 PROCEDURE USAGE

Procedure COMPRESSED\_CYL may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call COMPRESSED_CYL ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure COMPRESS\_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	<b>EX97</b>	Element name
ES_PARS	0.	Element research parameters
NNODES_A	5	Number of axial nodes
NNODES_C	5	Number of circumferential nodes
SPEC_DIS	<false></false>	Specified displacements
PRE_STRESS	<false></false>	Constant pre-stress
AUTO_DOF_SUP	<true></true>	Automatic d.o.f. suppression
DRILLING_DOF	<false></false>	Drilling (normal rotational) freedoms
BC_PROCEDURE	CC_BC	Boundary condition procedure
NSTEPS	30	Number of nonlinear load steps
BEG_STEP	1	Starting load step number
MAX_CUTS	3	Maximum number of step cuts (halvings)
BEG_LOAD	.1	Starting load factor
MAX_LOAD	1.0	Maximum load factor
DBC	CC.DBC	Computational database name
DBR	CC.DBR	Results database name
PREP	<true></true>	Perform pre-processing (model generation)
STABILITY	<true></true>	Perform linear stability (buckling) analysis
IMPERFECTION	<true></true>	Superpose imperfections from (buckling) analysis
		before performing nonlinear(postbuckling) analysis
NUM_IMP_MODES	1	Number of buckling modes used in creating
		imperfection
IMP_MODES	1	Mode numbers used in creating imperfection
IMP_AMPS	.1	Mode amplitudes
NONLINEAR	<true></true>	Perform nonlinear (postbuckling) analysis
POST	<false></false>	Perform post-processing (selected data archival)

## 4.2.3 ARGUMENT DESCRIPTIONS

## 4.2.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

## 4.2.3.2 BC\_PROCEDURE

Boundary condition procedure name (default: CC\_BC for specified forces; CCD\_BC for specified displacements). The term "boundary conditions" refers both to displacement constraints and applied loading. Procedures CC\_BC and CCD\_BC both have the same zero displacement constraints. The only difference is that the former procedure applies axial forces to the simply supported edge, while the latter procedure prescribes non-zero axial displacements on that edge. The argument BC\_PROCEDURE permits you to to supply your own boundary condition procedure, but keep in mind that this may drastically change the problem definition, and hence invalidate most of the discussion under Section 4.2.1.

## 4.2.3.3 BEG\_LOAD

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then  $BEG\_LOAD = .1$  means that the first load step to be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is *irrelevant* for re-start runs. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.2.3.4 <u>BEG\_STEP</u>

Number of starting load step in nonlinear analysis (default=1). This is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1. When re-starting (*i.e.*, continuing in a subsequent run) a nonlinear analysis, BEG\_STEP should be set to the number of the next step to be computed — not to the number of the last step computed. The solution procedure (NL\_STATIC\_1) will automatically use any previous step(s) required to continue the analysis — providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.2.3.5 DBC

Name of computational database file (default=CC.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

## 4.2.3.6 DBR

Name of results database file (default=CC.DBR). This file will contain one dataset called **RESPONSE.HISTORY** generated during nonlinear analysis. The dataset will contain record groups — indexed by load step number — for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

## 4.2.3.7 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

## 4.2.3.8 ES\_NAME

Element name (default: EX97). This argument is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-noded quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.2-1).

## 4.2.3.9 ES\_PARS

Element research parameters (default: 0., ...). This array is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 4.2.3.10 ES\_PROC

Element Processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

## 4.2.3.11 IMPERFECTION

Imperfection superposition flag (default <true>). This flag should be turned on if you want geometric imperfections, corresponding to buckling modes, to be superimposed on the initial geometry. Pre-requisites for this option are pre-processing and stability analysis. If you are just starting or re-starting a nonlinear analysis in the current run, and imperfections have already been superposed in a previous run, then you should turn this flag off.

## 4.2.3.12 <u>IMP\_AMPS</u>

List of buckling mode amplitudes to be used in generating the imperfection (default=.1, 10% of shell thickness). This option is relevant only if IMPERFECTION=<true>. The amplitudes in this list are interpreted as the maximum radial displacement to add to the initial nodal coordinates for a given buckling mode. Thus, the maximum coordinate perturbation due to a single buckling mode will occur wherever the mode shape has its maximum radial component.

## 4.2.3.13 <u>IMP\_MODES</u>

List of buckling mode numbers to be used in generating the imperfection (default=1). This option is relevant only if IMPERFECTION=<true>. The numbers in this list should be separated by commas, and there should be a total of NUM\_IMP\_MODES numbers.

## 4.2.3.14 <u>MAX\_CUTS</u>

Maximum number of load step cuts in nonlinear analysis (default=3). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.2.3.15 <u>MAX\_LOAD</u>

Maximum load factor in nonlinear analysis (default=1.0). This sets an upper limit for the load level, which can be a convenient way of terminating the arc-length controlled solution algorithm employed within procedure NL\_STATIC\_1. Since the load factor is actually an unknown in this solution procedure, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. Thus, the analysis will be terminated when either MAX\_LOAD is exceeded or NSTEPS is exceeded — whichever comes first. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.2.3.16 <u>NNODES\_A</u>

Number of axial nodes (default: 7). This is the number of nodes you wish to have along the axial direction of the cylindrical shell model, *i.e.*, along one-tenth of the full cylinder's length. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_A can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 4.2.3.17 <u>NNODES\_C</u>

Number of circumferential nodes (default: 7). This argument is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, *i.e.*, along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_C can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 4.2.3.18 NONLINEAR

Nonlinear (postbuckling) analysis flag (default=<true>). This flag should be turned on if you want to perform nonlinear analysis in the current run. The pre-requisites are preprocessing, stability analysis and imperfection superposition, all of which may be performed either in a previous run or in the current run — by setting the appropriate arguments (*i.e.*, **PREP**, **STABILITY** and **IMPERFECTION**).

## 4.2.3.19 <u>NSTEPS</u>

Maximum number of load steps to be computed in the current nonlinear analysis run (default=30). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.2.3.20 NUM\_IMP\_MODES

Number of buckling modes used to represent geometric imperfections for nonlinear analysis (default=1). This option is relevant only if IMPERFECTION=<true>.

## 4.2.3.21 POST

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the CC.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed if you wish to archive special displacement and/or internal force component response histories post-facto.

## 4.2.3.22 PREP

Preprocessing flag (default=<true>). This flag must be turned on the first time procedure COMPRESSED\_CYL is run, as it causes the model to be generated. If subsequent runs are used to perform other stages of the analysis (*e.g.*, nonlinear re-starts), then PREP must be set to <false> for those subsequent runs.

## 4.2.3.23 <u>PRE\_STRESS</u>

Constant pre-stress flag (default: <false>). By setting this flag to <true>, the procedure bypasses computing the linear solution to obtain the prebuckling stresses, and instead prescribes the prebuckling axial stress resultants to be uniform throughout the shell. This amounts to procedure COMPRESSED\_CYL invoking solution procedure L\_STABIL\_1 instead of procedure L\_STABIL\_2 to perform the buckling eigenvalue analysis. While the prescribed pre-stress used with this option is equal to the classical buckling value, the results can be somewhat different than those obtained using L\_STABIL\_2. The reason for this is that due to the simply supported boundary condition on the loaded edge, the prebuckling stress distribution (*i.e.*, both the exact one and that obtained using a linear prebuckling analysis) is not really uniform. Note that even when the uniform PRE\_STRESS option is selected, it is used only to obtain the buckling eigenvalues and mode shapes — which are in turn used as initial imperfections for the nonlinear analysis. The uniform pre-stress values are then ignored during the nonlinear analysis, which applies either forces or displacements to the simply-supported edge (depending on argument SPEC\_DIS).

#### 4.2.3.24 <u>SPEC\_DIS</u>

Specified displacement flag (default:  $\langle false \rangle$ ). By setting this flag to  $\langle true \rangle$ , uniform axial end-shortening is imposed instead of the uniform axial loading. This can make a significant difference in both the buckling and postbuckling response, and is not recommended for novice users of this procedure. This is because thin axially-compressed shells are not only imperfection sensitive, but also *boundary condition* sensitive, and uniform axial loading does not correspond (exactly) to uniform axial edge displacements. Note that the reference specified displacement (*i.e.*, end-shortening) magnitude equals .01 inches, and corresponds to an axial load of about .467 times the classical buckling load.

## 4.2.3.25 <u>STABILITY</u>

Stability (buckling) analysis flag (default: <true>). This flag should be turned on if you want the buckling eigenvalue analysis to be performed in the current run. Preprocessing is a pre-requisite for this option. If you are just performing a nonlinear analysis re-start run, then you should turn this flag off.

## 4.2.4 USAGE GUIDELINES AND EXAMPLES

Procedure COMPRESS\_CYL may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

*call (	COMPRESS_CYL	(										
								NNODES_C	z	1	;	
			SPEC_DIS									
			DRILLING	_DOF	' =	<false></false>	•	;				
			AUTO_DOF	_SUF	) =	<true></true>	ł	;				
			PREP	Ξ		<true></true>	1	;				
			STABILIT	Y =		<true></true>	į	;				
			IMPERFEC'	TION	[ =	<true></true>	;					
			NONLINEA	R =		<true></true>						
			POST	=		<true></true>	;					

BEG_STEP	= 1	;	
NSTEPS	= 10	;	
BEG_LOAD	= .1	;	
MAX_LOAD	= 3.0	;	
DBc	= CC.DBc	; DBr	= CC.DBr )

(E1) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING\_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

 Table 4.2-1
 Typical CPU Times for Various Computer Systems

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

(E2) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call COMPRESSED\_CYL

This will perform linear buckling eigenvalue analysis and 30 steps of nonlinear analysis with a  $7 \times 7$  grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.2-1.

### 4.2.5 LIMITATIONS

(L1) Only 4-node and 9-node shell elements can be employed in the model. (Note: This can be easily modified.)

(L2) Not all of the solution parameters provided by procedure NL\_STATIC\_1 are accessible using this procedure. The main reason for this is the CLIP limitation of 25 arguments per procedure. Procedure COMPRESSED\_CYL is exactly at this limit now.

#### 4.2.6 ERROR MESSAGES AND WARNINGS

If you have to repeat the preprocessing phase, you need to either delete the computational (.DBC) database, or delete the ES.SUMMARY dataset. Otherwise, the element processors will be run more than once for each element function (*e.g.*, FORM STIFFNESS), and the effect will be cumulative. This is due to a lack of explicit initialization in the registration of element processors using procedure ES.

#### 4.2.7 PROCEDURE FLOWCHART

COMPRESSED_CYL	(main procedure)
GEN_SHELL	(generate shell model)
CC_BC	(generate boundary conditions/loads)
L_STABIL_2	(perform stability analysis)
IMPERFECTION	(superpose buckling modes as imperfections)
NL_STATIC_1	(perform nonlinear static analysis)
HISTORY	(archive selected displacement/force histories)

### 4.2.8 PROCEDURE LISTING

### 4.2.9 REFERENCES

- 4.2-1 Timoshenko, S. P.; and Gere, J. M.: Theory of Elastic Stability, McGraw-Hill, New York, 1961.
- 4.2-2 Stanley, G. M.: "Continuum-Based Shell Elements," PhD Dissertation, Stanford University, 1985.
- 4.2-3 Donnel, L. H.: Beams, Plates, and Shells, McGraw-Hill, New York, 1976.
- 4.2-4 CSM Testbed Applications Manual.

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# 4.3 Procedure COOK\_MEM

### 4.3.1 GENERAL DESCRIPTION

This section describes a procedure that solves for the deflection of a trapezoidal panel subject to inplane shear and bending, also known as Cook's membrane (see ref. 4.3-1). The geometry of the membrane resembles a wing plan form (see figure 4.3-1) with an applied end shear load. The membrane has constant thickness, and the material is isotropic.

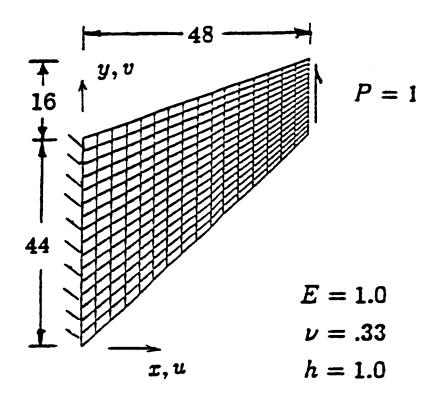


Figure 4.3-1 Cook's Membrane

## 4.3.1.1 Model Description

## 4.3.1.2 Analysis Description

## 4.3.1.3 Available Solutions

## 4.3.2 PROCEDURE USAGE

Procedure COOK\_MEM may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and all have default values thus making them optional. The formal syntax is as follows:

```
*call COOK_MEM ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure COOK\_MEM are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

<u>Argument</u>	<u>Default Value</u>	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	<b>EX97</b>	Element name
ES_PARS	0.	Element research parameters
NDATA	4	Number of grids to analyze
NNODES	3,5,7,9	Number of nodes on each edge
AUTO_DOF_SUP	<true></true>	Automatic d.o.f. suppression
DRILLING_DOF	<false></false>	Drilling (normal rotational) freedoms
CM_DB	CM.DB	Cook membrane database name

### 4.3.3 ARGUMENT DESCRIPTIONS

#### 4.3.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

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### 4.3.3.2 <u>CM\_DB</u>

Name of Cook membrane database file (default=CM.DB). This file will contain all model data and analysis results.

#### 4.3.3.3 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active --unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

#### 4.3.3.4 <u>ES\_NAME</u>

Element name (default: EX97). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-node quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.3-2).

#### 4.3.3.5 <u>ES\_PARS</u>

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

#### 4.3.3.6 ES\_PROC

Element processor (default: ES1) This is the name of the structural element (ES) Processor that contains the shell element type you wish to employ in the model. The default shellelement, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

### 4.3.3.7 <u>NDATA</u>

Specifies the number of model/mesh refinements to analyze (default: 4). The degree of mesh refinement for each analysis is defined by the NNODES parameter.

### 4.3.3.8 <u>NNODES</u>

A list of integers which represent the number of nodes on each edge of the surface for each analysis to be performed (default: 3,5,9,17). The length of the list is defined by the NDATA parameter. The numbers in the list must be consistent with the element type selected. For example, NNODES can be any list of numbers greater than 1 for 4-node quadrilateral elements, whereas it must be a list of odd numbers greater than 1 for 9-node quadrilateral elements.

### 4.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure Procedure COOK\_MEM may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call COOK\_MEM

This call will perform a linear static analysis for each of the element configurations specified by the default NNODES parameter. Also, a fine grid analysis is performed with approximately four times the nodes of the last analysis specified by parameter NNODES. The results of the fine grid analysis are used to normalize the results of each requested analysis. All analysis results are presented in table format by the procedure:

Cook's Membrane Analysis Data Element Name = EX97				
NODES	DISPLACEMENT	NORMALIZED		
3	0.22677967E+02	0.9440006730146		
5	0.23594924E+02	0.982170233148691		
9	0.23889961E+02	0.994451542428496		
17	0.23989798E+02	0.998607390930779		

#### \*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*

A plot showing the deformed shape of the membrane is provided in figure 4.3-2. The analysis model used 9-node quadrilateral elements with 17 nodes per edge.

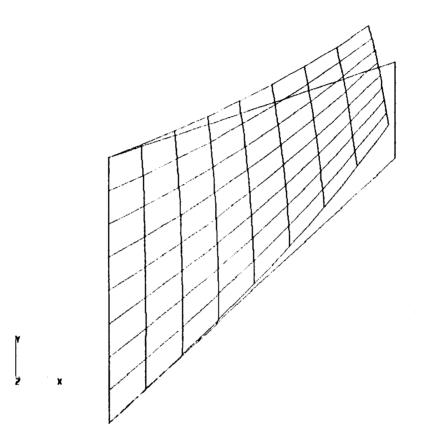


Figure 4.3-2 Cooks Membrane Deflection Plot

The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.3-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

Table 4.3-1CPU TIMES Table

## 4.3.5 LIMITATIONS

None.

### 4.3.6 ERROR MESSAGES AND WARNINGS

None.

### 4.3.7 PROCEDURE FLOWCHART

COOK_MEM	(main procedure)
GEN_PLATE	(generate model)
CM_BC	(generate boundary conditions/loads)
L_STATIC	(perform linear static analysis)

#### 4.3.8 PROCEDURE LISTING

#### 4.3.8.1 UNIX Script

cook\_mem.com

```
cd $SCR/$USER
cp $CSM_PRC/proclib.gal proclib.gal
chmod u+w proclib.gal
rm CMEX97.*
time testbed <<\endinput
*set echo, off
*set plib=28
*open 28 proclib.gal /old
+add '$CSM_APP/cook_mem/cook_mem.clp'
*call COOK_MEM ( ES_PROC = ES1 ; -- . Element Processor
                  ES_NAME = EX97 ; -- . Element name
                  ES_PARS = 0. ; -- . Element parameters
                               ; -- . Number of grids to analyze
                  NDATA = 4
                  NNODES = 3,5,9,17 ; -- . Number of nodes per side
                  AUTO_DOF_SUP=<true> ; --
                  DRILLING_DOF=<false> ; --
                  CM_DB = CMEX97.LO1 -- . Database
                )
*stop
*close 28 /delete
[xqt exit
\endinput
```

4.3.8.2 CLAMP Procedure

cook\_mem.clp

```
*procedure COCK_MEM ( es_proc = es1 ; -- . element processor
                  es_name = ex97 ; -- . element name
                  es_pars = 0. ; -- . element parameters
                  ndata = 4 ; -- . Number of grids to analyze
                  nnodes = 3,5,9,17 ; -- . Number of nodes per side
                  auto_dof_sup=<true> ; --
                  drilling_dof=<false> ; --
                  cm_db = cm.db -- . database
                 )
. procedure for analysis of in-plane bending of trapezoidal membrane
*def/i ndata = [ndata]
*def/i nnodes[1:<ndata>] = [nnodes]
*def/i nnodes[<<ndata>+1>] = < (<nnodes[<ndata>]>*2) + 1>
#def/i lib = 1
*do $j=1,<<ndata>+1>
  #if < <$j> /lt <<ndata>+1> > /then
    *open <lib>, [cm_db] /new
```

```
+else
     *open <lib>, zzzscr.lib /new
  *endif
  *def/i nnt = < <nnodes[<$j>]>*<nnodes[<$j>]> >
  *def/e • = 1.0
  *def/e nu = .33
  def/e h = 1.0
  *call GEN_PLATE ( es_proc
                                = [es_proc] ; --
                              = [es_name] ; ---
                   es_name
                   es_pars
                               = [es_pars] ; --
                               = <nnodes[<$j>]> ; --
                   nodes_1
                                = <nnodes[<$j>]> ; --
                   nodes_2
                                = 48.,44., 0. ; --
                   xyzi
                                = 48.,60., 0.; --
                   xyz2
                                = 0.,44., 0.; --
                   xyz3
                                = 0., 0., 0.; --
                   xyz4
                    • = <e> ; nu = <nu> ; thickness = <h> ; --
                    auto_dof_sup = [auto_dof_sup]; --
                   drilling_dof = [drilling_dof]; --
                   bc_procedure = TP_BC )
         perform static analysis
  *def/a solver_name == BAND
  *call L_STATIC
         store the results for this run
  [xqt AUS
     MACRO <1ib> STAT DISP 1 1 semilocal 2 <6+<nnodes[<$j>]>> 6 'disps
     STOP
  *def/e avgdisp = 0.
  *do $jj=1,<nnodes[<$j>]>
  *def/e avgdisp = <<avgdisp> + <disps[<$jj>]> >
  *enddo
  *def/e avgd[<$j>] = < <avgdisp> / <nnodes[<$j>]> >
  *show macros
*enddo
         delete the normalizing analysis
*close <lib> /delete
         done
*remark
*remark
*remark
tremark
Cook's Membrane Analysis Data
*rezark
                 Element Name = [es_name]
*remark
```

**Application Procedures** 

```
tresart sevenesessessessessessessessessessesses
*remark NODES DISPLACEMENT
                                   NORMALIZED
*remark
*do $j=1,<ndata>
                        <avgd[<$j>]>
                                      <<avgd[<$j>]>/<avgd[<<ndata>+1>]>>
*remark <nnodes[<$j>]>
*enddo
trenart sussaussessessessessessessessessesses
*remark
*repark
*remark
*remark
[xqt EXIT
+end
*procedure TP_BC ( nodes_1 ; nodes_2 ; es_nodes ; drilling_dof=<false> )
. boundary condition procedure for trapezoidal plate analysis
*def/i nn1 = [nodes_1]
 *def/i nn2 = [nodes_2]
 *def/i nen = [es_nodes]
 *def/i node_A = 1
 *def/i node_B = <nn1>
 *def/i node_D = < <nn1>*<nn2> >
 *def/i node_C = < <node_D> - <nn1> + 1 >
. boundary conditions
  edge c-d gets clamped
.
     constraint = 1
       zero 123456
                                 . clamp edge c-d
        <node_C> <node_D>
                                       of constant theta
       *if < [drilling_dof] /eq <false> > /then
       zero 4
                                 . remove drilling dof
        <node_A> <node_D>
                                      everywhere
       *endif
. loading conditions
   edge a-b receives uniform shear in positive global y direction
.
[xqt aus
 alpha
 case title
 1 'in-plane shear (i.e., bending) of trapezoidal membrane'
 sysvec : appl forc 1 1
\neq def/e p = 1.0
               . total axial force on model boundary
*if < <nen> /eq 4 > /then
  *def/i nelts = < <nn1> - 1 >
  *def/e12.4 Pelt = < <p> / <nelts> >
```

```
*def/e12.4 Pend = < <Pelt>/2. >
   *do $jn * <node_A>, <node_B>
     *if < <<$jn> /eq <node_A>> /or <<$jn> /eq <node_B>> > /then
       i=2 : j=<$jn> : <Pend>
      *else
      i=2 : j=<$jn> : <Pelt>
      *endif
   *enddo
*elseif < <nen> /eq 9 > /then
   *def/i nelts = < (<nn1> - 1)/2 >
   *def/e12.4 Pelt = < <p> / <nelts> >
   *def/e12.4 Pelt_1 = < 1.*<Pelt>/6. >
   *def/e12.4 Pelt_2 = < 2.*<Pelt>/6. >
   *def/e12.4 Pelt_4 = < 4.*<Pelt>/6. >
          midside nodes
   *do $j4 = <<node_A> + 1>, <<node_B>-1>, 2
       i=2 : j= <$j4> : <Pelt_4>
   *enddo
          shared nodes
   *if < <nelts> /gt 1 > /then
      *do $j2 = <<node_A>+2>, <<node_B>-2>, 2
       i=2 : j= <$j2> : <Pelt_2>
      *enddo
   *endif
          corner nodes
       i=2 : j= <node_&> : <Pelt_1>
       i=2 : j= <node_B> : <Pelt_1>
*endif
*end
```

### 4.3.9 REFERENCES

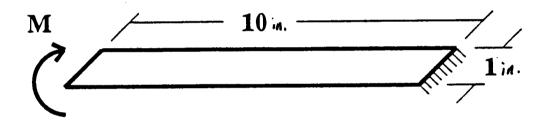
- 4.3-1 Stanley, G. M.: Continuum-Based Shell Elements. PhD Dissertation, Stanford University, Stanford, CA, 1985.
- 4.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.4 Procedure ELASTICA

#### 4.4.1 GENERAL DESCRIPTION

#### 4.4.1.1 Problem Description

This section describes a procedure that solves the classical large deflection, large rotation problem of a cantilevered beam with an applied end moment as shown in Figure 4.4-1. The nonlinear response of the cantilevered beam bent into a circle by an applied end moment is determined.



Thickness = 1. in:  $M = 2 \pi i n \cdot \frac{1}{3} / \frac{1}{3} .$   $E = 120. P^{si}$  V = 0.

# Figure 4.4-1 Elastica Problem.

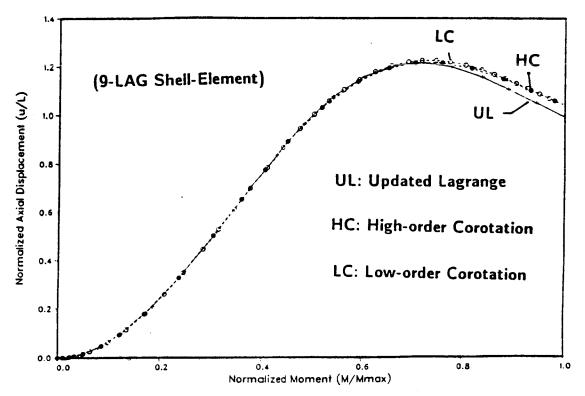
# 4.4.1.2 Model Description

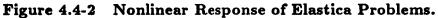
Procedure ELASTICA models the entire strip using 2-D quadrilateral elements. The mesh is generated using procedure GEN\_PLATE. Two sets of boundary conditions are available. The set in procedure ELASTICA\_BC imposes a clamped condition at one end of the strip and a moment at the other end. Procedure EL\_ECC\_BC also imposes a clamped condition at one end and an eccentric axial load at the other.

## 4.4.1.3 Analysis Description

Procedure ELASTICA performs either a linear static analysis using procedure L\_STATIC or a nonlinear static analysis using procedure NL\_STATIC\_1.

## 4.4.1.4 Available Solutions





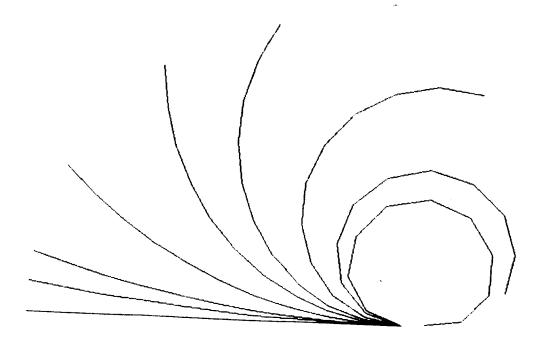


Figure 4.4-3 Sequence of Deformed Shapes.

# 4.4.2 PROCEDURE USAGE

Procedure ELASTICA may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call ELASTICA ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure ELASTICA are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For the procedure ELASTICA, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Select element processor
ES_NAME	EX97	Select element within ES_PROC
ES_PARS	0.	Set element-research parameters
NNODES_X	11	Number of nodes in x-direction
NNODES_Y	3	Number of nodes in y-direction
PREP	<true></true>	Preprocessing flag
POST	<true></true>	Postprocessing flag
LINEAR	<true></true>	Perform Linear Analysis
NONLINEAR	<true></true>	Perform Nonlinear Analysis
AUTO_DOF_SUP	<false></false>	Automatic degree of freedom suppression
DRILLING_DOF	<true></true>	
BEG_STEP	1	Beginning Load Step Number
BEG_LOAD	.01	Beginning Load Factor
NSTEPS	10	Number of Load Steps
DBC	ELASTICA.DBC	Computational Database
DBR	ELASTICA.DBR	Results Database

### 4.4.3 ARGUMENT DESCRIPTIONS

### 4.4.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness

associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

### 4.4.3.2 BC\_PROCEDURE

Boundary condition procedure name (default: ELASTICA\_BC). Two sets of boundary conditions are available. The set in procedure ELASTICA\_BC imposes a clamped condition at one end of the strip and a moment at the other end. Procedure EL\_ECC\_BC also imposes a clamped condition at one end and an eccentric axial load at the other.

### 4.4.3.3 <u>BEG\_LOAD</u>

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then  $BEG_LOAD = .1$  means that the first load step to be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is *irrelevant* for re-start runs. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.4.3.4 <u>BEG\_STEP</u>

Number of starting load step in nonlinear analysis (default=1). This argument is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1. When re-starting (*i.e.*, continuing in a subsequent run) a nonlinear analysis, BEG\_STEP should be set to the number of the next step to be computed — not to the number of the last step computed. The solution procedure (NL\_STATIC\_1) will automatically use any previous step(s) required to continue the analysis — providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.4.3.5 DBC

Name of computational database file (default=ELASTICA.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

### 4.4.3.6 DBR

Name of results database file (default=ELASTICA.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups — indexed by load step number — for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

### 4.4.3.7 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

### 4.4.3.8 ES\_NAME

Element name (default: EX97). This argument specifies the name of the specific shellelement type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-noded quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.4-1).

### 4.4.3.9 ES\_PARS

Element research parameters (default: 0., ...). This array allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

### 4.4.3.10 ES\_PROC

Element processor (default: ES1) This argument specifies the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.4-1).

### 4.4.3.11 <u>NNODES\_X</u>

Number of nodes along beam length (default: 11). This argument is the number of nodes along the x-direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_X can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

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### 4.4.3.12 <u>NNODES\_Y</u>

Number of nodes along beam depth (default: 3). This argument is the number of nodes along the y-direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_Y can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

### 4.4.3.13 NONLINEAR

Nonlinear (postbuckling) analysis flag (default=<true>). This flag should be turned on to perform nonlinear analysis in the current run.

#### 4.4.3.14 <u>NSTEPS</u>

Maximum number of load steps to be computed in the current nonlinear analysis run (default=30). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.4.3.15 POST

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the ELASTICA.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed to archive special displacement and/or internal force component response histories post-facto.

#### 4.4.3.16 PREP

Preprocessing flag (default=<true>). This flag must be turned on the first time procedure ELASTICA is run, as it causes the model to be generated. If subsequent runs are used to perform other stages of the analysis (*e.g.*, nonlinear restarts), then PREP must be set to <false> for those subsequent runs.

### 4.4.4 USAGE GUIDELINES AND EXAMPLES

Procedure ELASTICA may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

*call	ELASTICA	(	ES_PROC	= ES1 ;
			ES_NAME	= EX97 ;
			ES_PARS	= 0.0 ;
			NNODES_X	= 11 ;
			NNODES_Y	= 3 ;
			PREP	= <true>;</true>
			LINEAR	= <true>;</true>

```
POST =<false>; --
NONLINEAR =<false>; --
NSTEPS = 10 ; --
DBc = ELASTICA.DBc ; -- . Computational database
DBr = ELASTICA.DBr -- . Results database)
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call ELASTICA

This call will perform linear buckling eigenvalue analysis and 10 steps of nonlinear analysis with a  $11 \times 3$  grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.4-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

Table 4.4-1 CPU TIMES Table

(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING\_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

## 4.4.5 LIMITATIONS

(L1) Only 4-node and 9-node shell elements can be employed in the model. (Note: This can be easily modified.)

#### 4.4.6 ERROR MESSAGES AND WARNINGS

If you have to repeat the preprocessing phase, you need to either delete the computational (.DBC) database, or delete the ES.SUMMARY dataset. Otherwise, the element processors will be run more than once for each element function (*e.g.*, FORM STIFFNESS), and the effect will be cumulative. This is due to a lack of explicit initialization in the registration of element processors using procedure ES.

### 4.4.7 PROCEDURE FLOWCHART

ELASTICA	(main procedure)
GEN_PLATE	(generate model)
ELASTICA_BC	(generate boundary conditions and end moment)
EL_ECC_BC	(generate boundary conditions and eccentric axial load)
L_STATIC	(perform linear static analysis)
IMPERFECTION	(superpose buckling modes as imperfections)
NL_STATIC_1	(perform nonlinear static analysis)
HISTORY	(archive selected displacement/force histories)

#### 4.4.8 PROCEDURE LISTING

4.4.8.1 UNIX Script

#### elastica.com

```
cd $SCR/$USER
cp $CSM_PRC/proclib.gal proclib.gal
chmod u+w proclib.gal
rm ELASTICA.+
time testbed << \endinput
 *set echo,off
 *set plib=28
 *open/old 28 proclib.gal
 *add '$CSN_APP/elastica/elastica.clp'
 *def/a solver_name == INV
 *call ELASTICA ( ES_PROC
                               = ES1 ; ---
                               = EX97 ; ---
                  ES_NAME
                  ES_PARS
                               = 0.0 ; --
                  NNODES_X
                                = 11
                                       ; --
                  NNODES_Y
                                = 3 ; --
                  LINEAR=<false>; NONLINEAR
                                                =<true>; --
                                                            ; ---
                                = 36;drilling_dof=<false>
                  NSTEPS
                  DBc = ELASTICA.DBc ; -- . Computational database
                  DBr = ELASTICA.DBr
                                         -- . Results database
                )
 *stop
\endinput
```

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#### 4.4.8.2 CLAMP Procedure

```
elastica.clp
*procedure ELASTICA ( ES_PROC
                                = ES1 : -- .
                                = EX97 ; -- .
                    ES_NAME
                                = 0. ; --
                    ES_PARS
                                 = 11 ; -- .
                    NNODES_X
                    NNODES_Y
                                 = 3 ; -- .
                    PREP
                                 =<true>; -- .
                    POST
                                 =<true>; -- .
                    LINEAR
                                 =<true>; -- .
                                 =<true>; -- .
                    NONLINEAR
                    AUTO_DOF_SUP =<false>; -- .
                    DRILLING_DOF =<true>; -- .
                                 = 1 ; -- .
                    BEG_STEP
                    BEG_LOAD
                                 = .01; -- .
                    NSTEPS
                                 = 10 ; -- . Number of load steps
                    DBc = ELASTICA.DBc ; -- . Computational database
                    DBr = ELASTICA.DBr
                                        -- . Results database
                  )
           . CSM Testbed Procedure for Analysis of ELASTICA Problem
 *open 1, [DBc]
. Generate Plate Model of Cantilever Beam
*if < [PREP] > /then
   *call GEN_PLATE ( ES_PROC=[ES_PROC]
                                      ; ES_NAME=[ES_NAME] ;--
                           =[NNODES_X] ; NODES_2 =[NNODES_Y] ;--
                   NODES_1
                   E = 120.
                                 ; NU = 0. ; THICKNESS = 1.
                                                                  ; --
                   xyz1=0.,0.,0.; xyz2=10.,0.,0.; --
                   xyz3=10.,1.,0.; xyz4=0.,1.,0.; --
                   AUTO_DOF_SUP =[auto_dof_sup] ; --
                   DRILLING_DOF = [drilling_dof] ; --
                   BC_PROCEDURE = ELASTICA_BC )
   *toc
*endif
. Perform Solution
*if < [LINEAR] > /then
   *call L_STATIC
   *if < [POST] > /then
      *open 2, [DBr]
                 = [ES_PROC].[ES_NAME].[NNODES_X].[NNODES_Y]
      *def/a ds_r
      *call HISTORY ( input_ldi =1 ; input_ds =STAT.DISP.1.1; --
                    output_ldi=2 ; output_ds=<ds_r>
                                                       ; --
                    output_rn =LATERAL_DISP; nodes=1; component=3 )
      *call HISTORY ( input_ldi =1 ; input_ds =STAT.DISP.1.1; --
                    output_ldi=2 ; output_ds=<ds_r>
                                                       ; --
```

```
output_rn =END_ROTATION; nodes=1; component=5 )
      *call HISTORY ( input_ldi =1 ; input_ds =STAT.DISP.1.1; --
                    output_ldi=2 ; output_ds=<ds_r>
                                                  ; --
                    output_rn =AXIAL_DISP; nodes=1; component=1 )
      *resark
      *remark
      *remark _____
      *remark
      *remark ELASTICA Linear Results
      sressry.
      *remark Exact:
      *remark
                LATERAL_DISP (compare with W at node 1) = 31.41
      *remark
                 END_ROTATION (compare with RV at node 1) = 6.28
                 AXIAL_DISP (compare with U at node 1) = 0.0
      *remark
      *remark
      *remark Computed:
      *print rec 2, <ds_r> LATERAL_DISP /l=drx
      *print rec 2, <ds_r> END_ROTATION /l=drx
      *print rec 2, <ds_r> AXIAL_DISP
                                  /l=drx
      *remark
      *remark _____
      *remark
   *andif
*endif
*if < [NONLINEAR] > /then
   *def ns_overwrite = <true>
   *call NL_STATIC_1 ( beg_step = [BEG_STEP] ; --
                     max_stops = [NSTEPS] ; --
                     beg_load = [BEG_LOAD] ; --
                                           ; ---
                     max_load =1.00
                     NL_GEOM
                               = 2
                                           : --
                      COROTATION =
                                 1
                                           ; ---
                     Nominal_DB = [DBr]
                                           ; ---
       Nominal_DS = [ES_PROC].[ES_NAME].[NNODES_X].[NNODES_Y] ;--
                     N_SELECT = 2; --
                     SEL_NODES = 1, 1 ; SEL_DOFS = 1, 3 )
*toc [DBR]
endif
[xqt exit
+end
*procedure EL_ECC_BC ( nodes_1; nodes_2; es_nodes; drilling_dof=<false> )
. Define Loads and Boundary Conditions for ELASTICA Model
*def/i nn_tot = < [nodes_1]*[nodes_2] >
. DEFINE BOUNDARY CONDITIONS
[xqt TAB
CON 1
*if < [drilling_dof] /eq <false> > /then
```

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```
ZERO 6
                              . Suppress NORMAL ROTATIONS Everywhere
  *do $n=1,<nn_tot>
     <$n>
  *enddo
*endif
                              . Suppress LATERAL MOTION Everywhere
ZERO 2
*do $n=1,<nn_tot>
  <$n>
*enddo
                              . Suppress TORSIONAL ROTATION Everywhere
ZERO 4
*do $n=1,<nn_tot>
  <$n>
*enddo
                              . CANTILEVER Right End of Bean
ZERO 1,2,3,4,5,6
*do $n = [nodes_1], <nn_tot>, [nodes_1]
   <$n>
*enddo
. Define Loads
. ...........
[xqt AUS
. Apply Uniform Eccentric Load Consistently (over unit width)
    Pr results in Moment about Y of 2*PI since Eccentricity = .5
*def/e12.4 Px = < -4.*<PI> >
*def/e12.4 Pr_1 = < <Px>/2. >
  SYSVEC : APPL FORC 1
*if < [ES_NODES] /eq 4 > /then
   i=1 : j=1
                      : <Px_1>
   i=1 : j=<[nodes_1]+i> : <Px_1>
*elseif < [ES_NODES] /eq 9 > /then
  *def/e12.4 Px_1 = < <Px>/6. >
  *def/e12.4 Px_4 = < 4*<Px>/6. >
  i=1 : j=1
                       : <Px_1>
   i=1 : j=<[nodes_1]+1>
                          : <Px_4>
   i=1 : j=<(2*[nodes_1])+1> : <Px_1>
*endif
*end
*procedure ELASTICA_BC ( nodes_1; nodes_2; es_nodes; drilling_dof=<false> )
. Define Loads and Boundary Conditions for ELASTICA Model
*def/i nn_tot = < [nodes_1]*[nodes_2] >
. DEFINE BOUNDARY CONDITIONS
[xqt TAB
 CON 1
```

```
Elastica
```

```
*if < [drilling_dof] /eq <false> ) /then
   ZERO 6
                                . Suppress NORMAL ROTATIONS Everywhere
  *do $n=1,<nn_tot>
      <$n>
   *enddo
*endif
ZERO 2
                                . Suppress LATERAL MOTION Everywhere
*do $n=1,<nn_tot>
   <$n>
*enddo
ZERO 4
                                . Suppress TORSIONAL ROTATION Everywhere
*do $n=1,<nn_tot>
   <$n>
*enddo
                                . CANTILEVER Right End of Beam
ZERO 1,2,3,4,5,6
*do $n = [nodes_1], <nn_tot>, [nodes_1]
  <$n>
*enddo
. ..............
. Define Loads
-----
[xqt AUS
. Apply Uniform M_y Consistently (over unit width)
*def/e12.4 My = < 2.*<PI> >
*def/e12.4 Hy_1 = < <Hy>/2. >
  SYSVEC : APPL FORC 1
*if < [ES_NODES] /eq 4 > /then
  i=5 : j=1
                       : <My_1>
  i=5 : j=<[nodes_1]+1> : <My_1>
*elseif < [ES_NODES] /eq 9 > /then
  *def/e12.4 Hy_1 = < <My>/6. >
  *def/e12.4 Hy_4 = < 4*<Hy>/6. >
   i=5 : j=1
                         : <My_1>
   i=5 : j=<[nodes_1]+1> : <My_4>
   i=5 : j=<(2*[nodes_1])+i> : <My_1>
*endif
*end
```

#### 4.4.9 REFERENCES

- 4.4-1 Timoshenko, S. P.; and Gere, J. M.: Theory of Elastic Stability, McGraw-Hill, New York, 1961.
- 4.4-2 Stanley, G. M.: "Continuum-Based Shell Elements," PhD Dissertation, Stanford University, 1985.
- 4.4-3 Donnel, L. H.: Beams, Plates, and Shells, McGraw-Hill, New York, 1976.

4.4-4 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.5 Procedure EULER\_COLUMN

### 4.5.1 GENERAL DESCRIPTION

### 4.5.1.1 Problem Description

This application problem involves a linear bifurcation buckling analysis of a thin isotropic strip subjected to uniform compression (see Figure 4.5-1). This problem is important in that plate and shell elements are frequently used to model stiffeners of stiffened panels. When these panels buckle in an "overall" Euler modeshape the stiffeners must also buckle in their plane (see Figure 4.5-2).

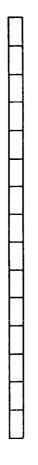


Figure 4.5-1 Euler Column Problem

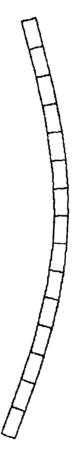


Figure 4.5-2 Euler Buckling Modeshape

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### 4.5.1.2 Model Description

Procedure EULER\_COLUMN models the entire strip using 2-D quadrilateral elements. The mesh is generated using procedure GEN\_PLATE and the boundary conditions are specified in procedure COLUMN\_BC.

#### 4.5.1.3 Analysis Description

Procedure EULER\_COLUMN performs a single linear buckling analysis with a specified prestress. The solution procedure L\_STABIL\_1 is used to perform the buckling analysis.

#### 4.5.1.4 Available Solutions

Analytical solution for the Euler buckling load is readily obtained from reference 4.5-1, page 22-28. The Euler buckling load is given by

$$P_{EULER} = \frac{\pi^2 EI}{L^2}$$

where

E = Young's Modulus I = Moment of Inertia =  $\frac{1}{12}th^3$  L = Column Length t = Column Thickness h = Column Width

ŝ

For a specified uniform membrane stress resultant  $N_x^o$  of -1000 lb/in., the corresponding buckling load factor is

$$(N_x)_{EULER} = P_{EULER}/h = \lambda_{EULER}N_x^o$$

For the geometry and material properties used as default values of the procedure arguments, the exact solution for simple-support boundary conditions corresponds to a value of 0.456926 for  $\lambda_{EULER}$  (*i.e.*, the smallest eigenvalue).

#### 4.5.2 PROCEDURE USAGE

Procedure EULER\_COLUMN may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call EULER\_COLUMN ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

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The allowable arguments for procedure EULER\_COLUMN are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
E	10.E6	Young's Modulus
ES_PROC	ES1	Element Processor
ES_NAME	<b>EX4</b> 7	Element name
LX	30.0	Length in x-direction
LY	1.0	Length in y-direction
NODES_1	31	Number of nodes along <b>x</b>
NODES_2	3	Number of nodes along y
NU	0.0	Poisson's ratio
PRINT	<false></false>	Print flag
PS_1	-1000.0	Uniform axial compression prestress
THICKNESS	0.05	Thickness

## 4.5.3 ARGUMENT DESCRIPTIONS

### 4.5.3.1 <u>E</u>

Young's elastic modulus (default:  $10.0 \times 10^6$  psi).

#### 4.5.3.2 <u>ES\_NAME</u>

Element name (default: EX47). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX47, is a 4-noded quadrilateral element implemented in processor ES1, and described in the Computational Structural Mechanics Testbed User's Manual (see ref. 4.5-2).

### 4.5.3.3 ES\_PROC

Element Processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES1, is described in the Computational Structural Mechanics Testbed User's Manual (see refs. 4.5-2).

### 4.5.3.4 LX

Length of the plate model in the x-direction (default: 31.0 inches).

### 4.5.3.5 <u>LY</u>

Length of the plate model in the y-direction (default: 1.0 inches).

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#### 4.5.3.6 NODES\_1

Number of nodes along x-direction (default: 31).

#### 4.5.3.7 <u>NODES\_2</u>

Number of nodes along y-direction (default: 3).

#### 4.5.3.8 <u>NU</u>

Poisson's ratio (default: 0.0).

#### 4.5.3.9 PRINT

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, modeshapes, stresses) will be printed.

#### 4.5.3.10 PS\_1

Uniform axial compression prestress (default: -1000 lb/in.).

#### 4.5.3.11 THICKNESS

Thickness of the plate (default: 0.05 inches).

#### 4.5.3.12 <u>WTDEN</u>

Weight density (default: 0.1 lb/in.<sup>3</sup>). Processor LAU converts the weight density to mass density.

#### 4.5.4 USAGE GUIDELINES AND EXAMPLES

Procedure EULER\_COLUMN may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call EULER_COLUMN ( ES_PROC = ES1 ; ES_NAME = EX47 ; --
    LX = 7.5 ; --
    LY = 10.0 ; --
    E = 30.E6 ; --
    NU = 0.3 ; --
    PRINT = <false> ; --
    THICKNESS = 0.1 ; --
    WTDEN = 0.1 )
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,

#### \*call EULER\_COLUMN

Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.5-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

### Table 4.5-1CPU TIMES Table

### 4.5.5 LIMITATIONS

None

### 4.5.6 ERROR MESSAGES AND WARNINGS

None.

### 4.5.7 PROCEDURE FLOWCHART

EULER_COLUMN	(main procedure)
GEN_PLATE	(define model)
COLUMN_BC	(define simple-support boundary conditions)

### 4.5.8 PROCEDURE LISTING

## 4.5.8.1 UNIX Script

euler\_column.com

```
cd $SCR/$USER
rm euler_column.101
cp $CSM_PRC/proclib.gal proclib.gal
chmod u+w proclib.gal
time testbed << \endinput</pre>
```

#### **Application Procedures**

```
*open 1 euler_column.101
*set echo off
*def/a eigensolver_name = EIG2
*def/a solver_name = INV
.
*set plib=28
*open 28 proclib.gal /old
*add '$CSM_APP/euler_column/euler_column.clp'
.
.
. Inplane Buckling of a Thin Strip
.
*call EULER_COLUMN ( es_name='ex97'; es_proc='es7')
.
[XQT EXIT
\endinput
```

#### 4.5.8.2 CLAMP Procedure

euler\_column.clp

```
*procedure EULER_COLUMN (
                            es_name = 'EX47' ; --
                             es_proc = 'ES1' ; --
                                    = 10.0e+6; --
                            •
                            nu
                                    = .3
                                             ; --
                            thickness= 0.05 ; --
                                     = -1000.0; --
                            ps_1
                            lx
                                     =30.0 ; --
                            ly
                                     =1.0 ; --
                            nodes_1 = 31 ; --
                            nodes_2 = 3 )
*call GEN_PLATE ( es_proc=[es_proc];es_name=[es_name]; --
                  xyz1=0.0,0.0,0.0 ; --
                  xyz2=[1x],0.0,0.0 ; --
                  xyz3=[lx],[ly],0.0 ; --
                  xyz4=0.0,[1y],0.0 ; --
                  nodes_1=[nodes_1]; nodes_2=[nodes_2]; --
                  nsect=1; e=[e];nu=[nu];thickness=[thickness]; --
                  bc_procedure= 'COLUMN_BC' )
*toc 1
[XQT TAB
TITLE'EULER COLUMN BUCKLING PROBLEM
*call L_STABIL_1 ( ps_1=[ps_1]; print=<true> )
*toc 1
*end
*procedure COLUMN_BC (nodes_1=31; nodes_2=3; --
      es_nodes=<es_nen>; drilling_dof=<true>)
*def/i n1 = 1
*def/i n2 = [nodes_1]
*def/i n3 = < [nodes_1]*[nodes_2] >
*def/i n4 = < [nodes_1]*([nodes_2]-1) + 1 >
CON CASE 1
```

```
ZER0 3 4 5 : <n1>,<n3>
ZER0 2 : <n1>,<n4>,[nodes_1]
ZER0 2 : <n2>,<n3>,[nodes_1]
*if < [drilling_dof] /eq 0 > /then
ZER0 6: <n1>,<n3>
*endif
*end
```

#### 4.5.9 REFERENCES

- 4.5-1 Brush, Don O. and Almroth, Bo O.: Buckling of Bars, Plates, and Shells, McGraw-Hill Book Company, New York, 1975.
- 4.5-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.6 Processor FOCUS\_PANEL

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# 4.7 Processor FREE\_EDGE

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THIS SECTION UNDER PREPARATION

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# 4.8 Processor GEN\_STF\_PANEL

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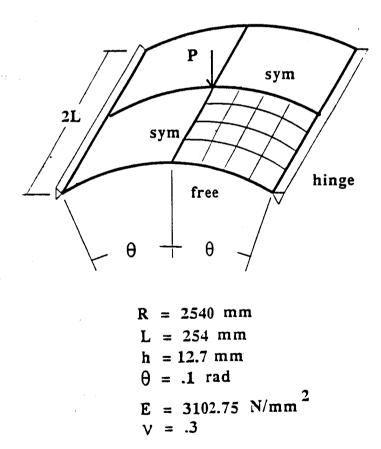
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# 4.9 Procedure HINGED\_CYL

### 4.9.1 GENERAL DESCRIPTION

To verify the nonlinear aspects of the shell-element formulation, implementation, and adaptive (Crisfield/Riks) quasi-static solution algorithm, the snap-through of a hinged cylinder under a point force is considered. This problem, which involves only moderate geometric nonlinearities, is nevertheless interesting due to the limit-point characteristics of the loaddisplacements curve. Furthermore, due to the popularity of the problem, an abundance of numerical results are available for comparison.

This section describes a preedure that solves the hinged cylinder problem (see figure 4.9-1) which exhibits snap-through behavior.



#### Figure 4.9-1 Hinged Cylinder Problem.

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## 4.9.1.1 Model Description

## 4.9.1.2 Analysis Description

## 4.9.1.3 Available Solutions

## 4.9.2 PROCEDURE USAGE

Procedure HINGED\_CYL may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call HINGED_CYL ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure HINGED\_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default_Value</u>	<u>Meaning</u>
ES_PROC	ES1	Element Processor
ES_NAME	EX97	Element name
ES_PARS	0.	Element research parameters
NNODES_A	5	Number of axial nodes
NNODES_C	5	Number of circumferential nodes
SPEC_DIS	<false></false>	Specified displacements
AUTO_DOF_SUP	<true></true>	Automatic d.o.f. suppression
DRILLING_DOF	<false></false>	Drilling (normal rotational) freedoms
NSTEPS	10	Number of nonlinear load steps
BEG_STEP	1	Starting load step number
MAX_CUTS	3	Maximum number of step cuts (halvings)
BEG_LOAD	.1	Starting load factor
MAX_LOAD	1.0	Maximum load factor
DBC	CC.DBC	Computational database name
DBR	CC.DBR	Results database name
PREP	<true></true>	Perform pre-processing (model generation)
LINEAR	<false></false>	Perform nonlinear (post-buckling) analysis
TH_SCALE	1.0	
TOL	.001	

## 4.9.3 ARGUMENT DESCRIPTIONS

### 4.9.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

### 4.9.3.2 <u>BEG\_LOAD</u>

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then  $BEG_LOAD = .1$  means that the first load step to be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is *irrelevant* for re-start runs. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.9.3.3 <u>BEG\_STEP</u>

Number of starting load step in nonlinear analysis (default=1). This is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1. When re-starting (*i.e.*, continuing in a subsequent run) a nonlinear analysis, BEG\_STEP should be set to the number of the next step to be computed — not to the number of the last step computed. The solution procedure (NL\_STATIC\_1) will automatically use any previous step(s) required to continue the analysis — providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.9.3.4 DBC

Name of computational database file (default=HC.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

### 4.9.3.5 DBR

Name of results database file (default=HC.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups — indexed by load step number — for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

## 4.9.3.6 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

## 4.9.3.7 ES\_NAME

Element name (default: EX97). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-noded quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.9-1).

## 4.9.3.8 ES\_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 4.9.3.9 <u>ES\_PROC</u>

Element processor (default: ES1) This is the name of the structural element (ES) Processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

## 4.9.3.10 <u>MAX\_CUTS</u>

Maximum number of load step cuts in nonlinear analysis (default=3). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.9.3.11 <u>MAX\_LOAD</u>

Maximum load factor in nonlinear analysis (default=1.0). This sets an upper limit for the load level, which can be a convenient way of terminating the arc-length controlled solution

algorithm employed within procedure NL\_STATIC\_1. Since the load factor is actually an unknown in this solution procedure, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. Thus, the analysis will be terminated when either MAX\_LOAD is exceeded or NSTEPS is exceeded — whichever comes first. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.9.3.12 <u>NNODES\_A</u>

Number of axial nodes (default: 7). This is the number of nodes you wish to have along the axial direction of the cylindrical shell model, *i.e.*, along one-tenth of the full cylinder's length. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_A can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

### 4.9.3.13 <u>NNODES\_C</u>

Number of circumferential nodes (default: 7). This is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, *i.e.*, along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_C can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

### 4.9.3.14 NONLINEAR

Nonlinear (post-buckling) analysis flag (default= $\langle true \rangle$ ). This flag should be turned on if you want to perform nonlinear analysis in the current run. The pre-requisites are preprocessing, stability analysis and imperfection superposition, all of which may be performed either in a previous run or in the current run — by setting the appropriate arguments (*i.e.*, **PREP**, **STABILITY** and **IMPERFECTION**).

### 4.9.3.15 <u>NSTEPS</u>

Maximum number of load steps to be computed in the current nonlinear analysis run (default=30). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.9.3.16 POST

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the HC.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed if you wish to archive special displacement and/or internal force component response histories post-facto.

## 4.9.3.17 PREP

Preprocessing flag (default=<true>). This flag must be turned on the first time procedure COMPRESSED\_CYL is run, as it causes the model to be generated. If subsequent runs are used to perform other stages of the analysis (*e.g.*, nonlinear re-starts), then PREP must be set to <false> for those subsequent runs.

## 4.9.3.18 <u>SPEC\_DIS</u>

Specified displacement flag (default:  $\langle false \rangle$ ). By setting this flag to  $\langle true \rangle$ , uniform axial end-shortening is imposed instead of the uniform axial loading. This can make a significant difference in both the buckling and post-buckling response, and is not recommended for novice users of this procedure. This is because thin axially-compressed shells are not only imperfection sensitive, but also *boundary condition* sensitive, and uniform axial loading does not correspond (exactly) to uniform axial edge displacements. Note that the reference specified displacement (*i.e.*, end-shortening) magnitude equals .01 inches, and corresponds to an axial load of about .467 times the classical buckling load.

# 4.9.4 USAGE GUIDELINES AND EXAMPLES

Procedure HINGED\_CYL may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call HINGED_CYL ( ES_PROC = ES1
                                         ; ES_NAME = EX97 ;
                     NNODES_A
                               = 5
                                            ; NNODES_C = 5
                     SPEC_DIS =
                                     <false> ;
                     DRILLING_DOF = <false>
                     AUTO_DOF_SUP = <true>
                     PREP
                               =
                                     <true>
                     NONLINEAR =
                                      <true>
                     POST
                               æ
                                     <true>
                               = 1
                     BEG_STEP
                     NSTEPS
                                = 10
                     BEG_LOAD
                               Ŧ
                                  . 1
                                            ;
                     MAX_LOAD
                               -
                                   3.0
                                              ---
                                            ;
                                            ; DBr
                     DBc
                                = HC.DBc
                                                     = HC.DBr )
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

### \*call HINGED\_CYL

This will perform linear buckling eigenvalue analysis and 30 steps of nonlinear analysis with a  $5 \times 5$  grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of systems is shown in Table 4.9-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

Table 4.9-1 CPU TIMES Table

(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING\_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

## 4.9.5 LIMITATIONS

## 4.9.6 ERROR MESSAGES AND WARNINGS

None.

## 4.9.7 PROCEDURE FLOWCHART

HINGED_CYL	(main procedure)
GEN_SHELL	(generate model)
HC_BC	(generate boundary conditions and applied loads)
HCD_BC	(generate boundary conditions and specified displacements)
L_STATIC_1	(perform linear static analysis)
NL_STATIC_1	(perform nonlinear static analysis)
HISTORY	(archive selected displacement/force histories)

## 4.9.8 PROCEDURE LISTING

### 4.9.9 REFERENCES

4.9-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.10 Procedure PEAR\_CYL

### 4.10.1 GENERAL DESCRIPTION

The nonlinear shell response of cylindrical shells with a noncircular cross-section became the subject of intense research in the early 1970's. Early Space Shuttle fuselage configurations were noncircular, and the "pear-shaped" cross-section was a leading candidate. The pear-shaped cylinder shown in Figure 4.10-1 has been adopted by many researchers and the behavior of this shell subject to a uniform end-shortening investigated (*e.g.*, refs. 4.10-1 and 4.10-2). The results in this section are compared with results reported by Hartung and Ball (ref. 4.10-1) and by Almroth and Brogan (ref. 4.10-2). In all cases, only one fourth of the cylinder is modeled. The shell is isotropic with a uniform thickness of 0.01 inches. The boundaries are simply supported.

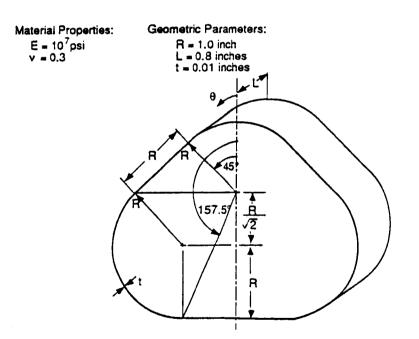


Figure 4.10-1 Pear-shaped cylinder – geometry, properties, and loading.

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## 4.10.1.1 Model Description

The finite element model of the pear-shaped cylinder is generated in segments as shown in figure 4.10-2. Joint locations and element connectivity are defined using the mesh generating capabilities of Testbed processors TAB and ELD. The user must specify only the number of elements along the  $45^{\circ}$  arc of segment 1 (NEL\_ARC), the number of elements along the flat edge of segment 2 (NEL\_FLAT), and the number of elements and through the depth of the cylinder in the z-direction (NEL\_DEPTH). The finite element mesh, loading, and constraints are then automatically generated. In order to facilitate both the model generation and the results interpretation, several alternate reference frames have been defined.

Reference frames 1, 2, and 3 are defined automatically in processor TAB as global reference frames, rotated  $-90^{\circ}$  about z axis, and rotated  $90^{\circ}$  about y axis, respectively. Reference frames 4, 5, and 6 are translations of the origin to points A, B, and C, respectively (see figure 4.10-2). Frames 7 and 8 involve rotations about the global z-axis and include no translations.

The results of interest in this analysis are the normal and tangential stresses and displacements. Each joint is therefore assigned a joint reference frame to which displacements, constraints, and loads are referred. The stress component directions are defined by the order of the element connectivity using the element network generators of processor ELD.

Segment 1 of the finite element model is generated using reference frame 4. The FORMAT=2 statement of the TAB/JLOC subprocessor allows for the generation of a regular mesh of nodes on the cylindrical surface of segment 1. The TAB/JLOC input is in cylindrical coordinates with point A as the origin of the cylindrical frame. The joints in this segment are each assigned joint reference frame -4 indicating a cylindrical frame with the joint 1-axis concident with the outward normal at each joint, the joint 3-axis coincident with the global z-axis, and the joint 2-axis coincident with the tangent to each joint.

Segment 2 is also generated using frame 4 although in this case, frame 4 is employed as a rectangular frame. The TAB/JLOC subprocessor generates a regular mesh of nodes connecting the four corners of the rectangular surface of the segment. The TAB/JLOC input is in cartesian coordinates with point A at the origin of the rectangular frame. Each joint in this segment is assigned joint reference frame 7 indicating that the 1- and 2-axes of each joint are coincident with x and y axes rotated 135° about global z. The joint 3-axis and global z-axis are coincident.

Segment 3, a 135° section of arc, is generated using reference frame 5, centered at point B. As with segment 1, the FORMAT=2 statement of the TAB/JLOC subprocessor is used to generate a regular mesh of nodes on the cylindrical segment. The number of elements around the circumference of this segment is assumed to be three times the number of elements around the circumference of Segment 1. The joints in this segment are each assigned joint reference frame -5 indicating a cylindrical frame with the joint 1-axis coincident with the outward normal at each joint, the joint 3-axis coincident with the global z-axis, and the joint 2-axis coincident with the tangent to each joint.

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Segment 4 is generated using reference frame 6, centered at point C. Frame 6 is used as a rectangular frame to generate a regular mesh of nodes connecting the four corners of the rectangular surface of the segment. The number of elements along this segment is half that used in segment 2. Each joint in this segment is assigned joint reference frame 8 indicating that the 1- and 2-axes of each joint are coincident with x- and y- axes rotated 270° about global z-axis. The joint 3-axis and global z-axis are coincident.

Three finite element models were considered in this study as shown in Figure 4.10-3. Mesh 1  $(3 \times 26)$  has three nodes through the cylinder depth and 26 nodes around the half-cylinder circumference (see Figure 4.10-3a). The mesh is composed of 50 4-node quadrilateral shell elements (ES1/EX47 or ES5/E410) and a total of 78 nodes. Mesh 2  $(5 \times 37)$  has five nodes through the cylinder depth and 37 nodes around the half-cylinder circumference (see Figure 4.10-3b). This mesh accommodates both 4- and 9-node elements and will contain either 144 4-node (ES1/EX47 or ES5/E410) or 36 9-node (ES1/ES97) quadrilateral shell elements and 185 nodes. Mesh 3  $(7 \times 51)$  has seven nodes through the cylinder depth and 51 nodes around the half-cylinder circumference (see Figure 4.10-3c). Mesh 3 accommodates both 4- and 9-node elements and 51 nodes around the half-cylinder circumference (see Figure 4.10-3c). Mesh 3 accommodates both 4- and 9-node (ES1/EX47 or ES5/E410) or 75 9-node (ES1/EX47 or ES5/E410) or 36 9-node (ES1/EX47 or ES5/E410) or 75 9-node (ES1/EX97) quadrilateral shell elements and 357 nodes.

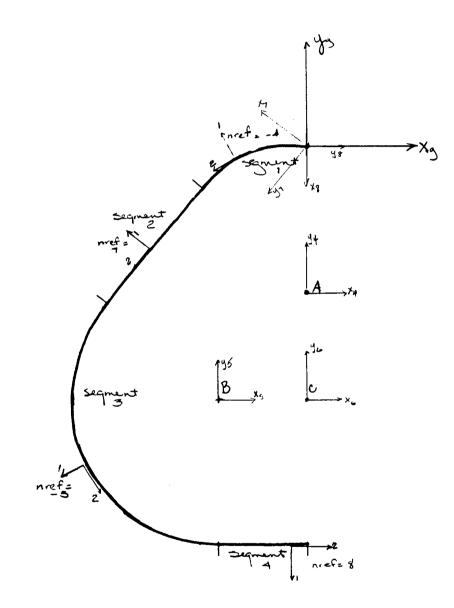


Figure 4.10-2 Model Generation Strategy and Reference Frames

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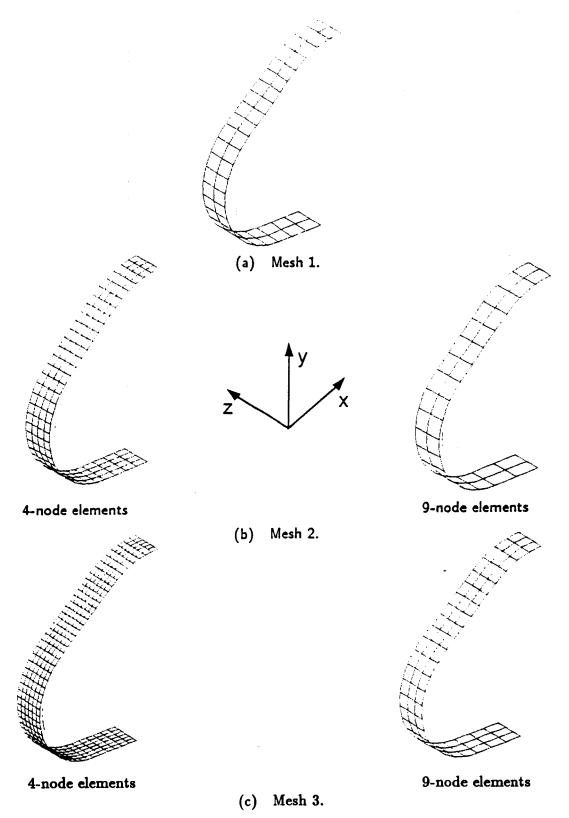


Figure 4.10-3 Finite element models of pear-shaped cylinder.

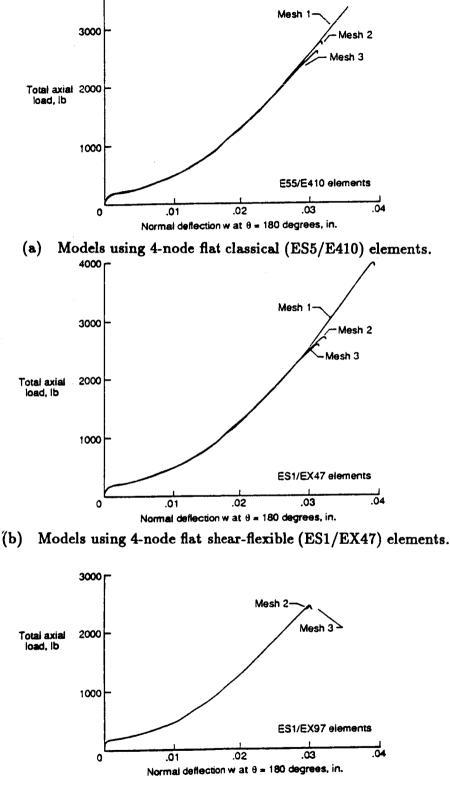
## 4.10.1.2 Analysis Description

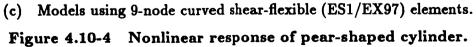
## 4.10.1.3 Available Solutions

The pear-shaped cylinder is representative of a shell-type structure with a complex nonlinear collapse behavior. The shell response becomes nonlinear at a very low value of applied end-shortening, and the normal deflections of the flat portions of the shell increase rapidly. The nonlinear analysis of the cylinder is performed using the procedure NL\_STATIC\_1. The distribution of the normal displacement (normal to the shell surface) is shown in Figure 4.10-4 as a function of the applied load for the point of maximum normal displacement (at x = 0,  $\theta = 180^{\circ}$ ) and for all meshes and element types considered. These results indicate that a converged solution is provided by the ES1/EX97 elements as the curves for Mesh 2 and Mesh 3 in Figure 4.10-4c are nearly identical. These three solutions correspond to a discretization with 185 nodes with either 144 4-node flat classical (ES5/E410) elements, 144 4-node flat shear-flexible (ES1/EX47) elements, or 36 9-node curved shear-flexible (ES1/EX97) elements.

A comparison of the three solutions obtained using Mesh 2 is provided in Figure 4.10-5. The effects of transverse shear flexibility, present in the ES1/EX97 and ES1/EX47 elements but not present in ES5/E410 elements, are apparent near collapse. The response curves begin to separate slightly at approximately half the elastic collapse load with the shear flexible elements exhibiting a consistent, yet slightly lower, stiffness than the response obtained using the ES5/E410 element. The elastic collapse loads obtained using the 4-node flat elements is nearly the same. However, results obtained using higher-order curved elements to model the shell and its response are approximately 10% lower than the collapse loads obtained using the flat elements.

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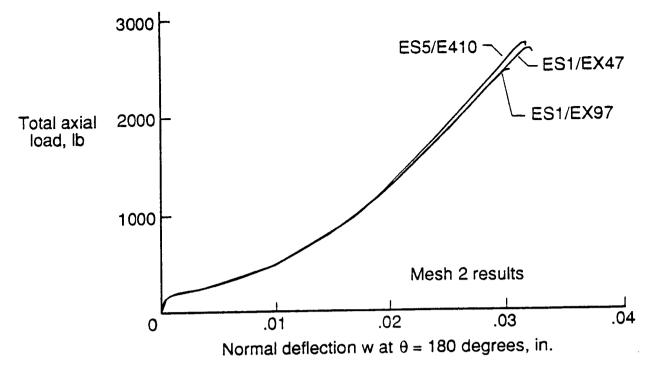


Figure 4.10-5 Nonlinear response of pear-shaped cylinder – Mesh 2.

Hartung and Ball (ref. 4.10-1) reported an elastic collapse load of 2372 pounds using a finite difference version of STAGS. Several years later, Almroth and Brogan (ref. 4.10-2) performed a convergence study using the finite element version of STAGS and estimated that the elastic collapse load was between 2300 and 2400 pounds. These results, along with the Testbed results, and results from independent elastic collapse analyses using the STAGSC-1 computer code, are summarized in Table 4.10-1.

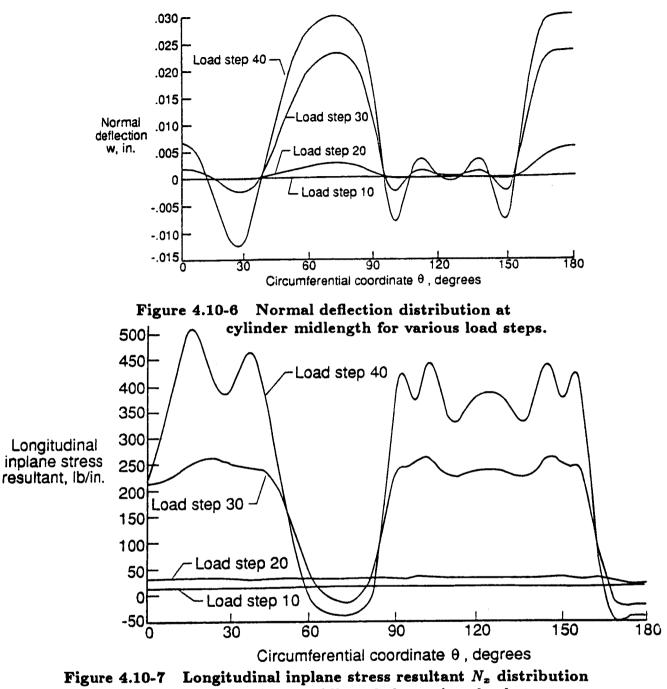
In Figure 4.10-6, the normal deflection at x = 0 is plotted as a function of the circumferential coordinate  $\theta$  for four different levels of applied load: 154, 300, 1689, and 2464 pounds (load steps 10, 20, 30 and 40 respectively). The final load step (step 40 at 2464 pounds) occurs just after collapse. The flat portions of the shell, from  $45^{\circ} \le \theta \le 90^{\circ}$  and  $157.5^{\circ} \le \theta \le 180^{\circ}$ , show a rapid growth in normal deflections. Associated with this growth is a redistribution of the longitudinal stress indicating that the curved portions begin to take up a larger percentage of the total axial load. This type of behavior can be seen in Figure 4.10-7 which plots the longitudinal stress resultant as a function of the circumferential coordinate for load steps 10, 20, 30 and 40.

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	Element		Elastic Collapse Load,
Source	Name	$Mesh^{(1)}$	pounds
Hartung and Ball	(2)	4 × 40	2372
Almroth and Brogan	411	$3 \times 27$	3586
		$5 \times 37$	2731
		7 × 47	2586
	440	5 × 37	2657
		7 × 47	2530
STAGSC-1	410	$3 \times 26$	3570
		5 × 37	2734
CSM Testbed	ES5/E410	<b>3</b> × 26	3343
		5 × 37	2753
		7 × 51	2577
	ES1/EX97	5 × 37	2475
		$7 \times 51$	2466
	ES1/EX47	3 × 26	3945
		5 × 37	2696
		$7 \times 51$	2568

Table 4.10-1	Elastic collapse loa	ds for pear-shaped cylinder.
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(1) Mesh description is  $n \times m$  meaning n rows by m columns of nodes. (2) Finite difference version of STAGS.



at cylinder midlength for various load steps.

## 4.10.2 PROCEDURE USAGE

Procedure PEAR\_CYL may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call PEAR_CYL ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PEAR\_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	EX97	Element name
ES_PARS	0.	Element research parameters
NEL_ARC		Number of elements along 45° arc segment
NEL_DEPTH		Number of elements along depth of shell
NEL_FLAT		Number of elements along largest flat segment
LD_DIR		Direction to total load
LINEAR		Perform linear analysis
NSTEPS	30	Number of nonlinear load steps
BEG_STEP	1	Starting load step number
MAX_CUTS	3	Maximum number of step cuts (halvings)
BEG_LOAD	.1	Starting load factor
MAX_LOAD	1.0	Maximum load factor
DBC	PEAR.DBC	Computational database name
DBR	PEAR.DBR	Results database name
STABILITY	<true></true>	Perform linear stability (buckling) analysis
NONLINEAR	<true></true>	Perform nonlinear analysis
POST	<false></false>	Perform postprocessing (selected data archival)

## 4.10.3 ARGUMENT DESCRIPTIONS

### 4.10.3.1 <u>BEG\_LOAD</u>

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then  $BEG\_LOAD = .1$  means that the first load step to

be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is *irrelevant* for re-start runs. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

## 4.10.3.2 <u>BEG\_STEP</u>

Number of starting load step in nonlinear analysis (default=1). This is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1. When re-starting (*i.e.*, continuing in a subsequent run) a nonlinear analysis, **BEG\_STEP** should be set to the number of the next step to be computed — not to the number of the last step computed. The solution procedure (**NL\_STATIC\_1**) will automatically use any previous step(s) required to continue the analysis — providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure **NL\_STATIC\_1**.

## 4.10.3.3 DBC

Name of computational database file (default=PEAR.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

### 4.10.3.4 DBR

Name of results database file (default=PEAR.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups — indexed by load step number — for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

### 4.10.3.5 ES\_NAME

Element name (default: EX97). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-node quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.10-3).

### 4.10.3.6 ES\_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 4.10.3.7 <u>ES\_PROC</u>

Element processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.10-3).

### 4.10.3.8 LD\_DIR

Direction in which to total the load (default: 3). This argument specifies the direction in which the reaction forces will be summed in order to determine the total load applied.

### 4.10.3.9 LINEAR

Linear analysis flag (default: **<false>**). This flag should be turned on to perform only a linear static analysis.

### 4.10.3.10 MAX\_CUTS

Maximum number of load step cuts in nonlinear analysis (default=3). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.10.3.11 <u>MAX\_LOAD</u>

ł

Maximum load factor in nonlinear analysis (default=1.0). This sets an upper limit for the load level, which can be a convenient way of terminating the arc-length controlled solution algorithm employed within procedure NL\_STATIC\_1. Since the load factor is actually an unknown in this solution procedure, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. Thus, the analysis will be terminated when either MAX\_LOAD is exceeded or NSTEPS is exceeded — whichever comes first. For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.10.3.12 <u>NEL\_ARC</u>

Number of elements along arc segment (default: 4). This argument specifies the number of elements along a 45° arc segment of the shell.

### 4.10.3.13 <u>NEL\_DEPTH</u>

Number of elements along depth of shell (default: 1). This argument specifies the number of elements along the length (or depth) of the shell.

## 4.10.3.14 <u>NEL\_FLAT</u>

Number of elements along flat segments (default: 4). This argument specifies the number of elements along the flat segments of the shell.

### 4.10.3.15 NONLINEAR

Nonlinear analysis flag (default=<true>). This flag should be turned on to perform nonlinear analysis in the current run.

## 4.10.3.16 <u>NSTEPS</u>

Maximum number of load steps to be computed in the current nonlinear analysis run (default=30). For more details, refer to the same argument name under solution procedure NL\_STATIC\_1.

### 4.10.3.17 POST

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the PEAR.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed if you wish to archive special displacement and/or internal force component response histories post-facto.

### 4.10.3.18 **STABILITY**

Stability (buckling) analysis flag (default <true>). This flag should be turned on if you want the buckling eigenvalue analysis to be performed in the current run. Preprocessing is a pre-requisite for this option. If you are just performing a nonlinear analysis re-start run, then you should turn this flag off.

## 4.10.4 USAGE GUIDELINES AND EXAMPLES

Procedure PEAR\_CYL may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

*call PEAR_CYL (	<pre>ES_PROC = ES1 ; Element Processor ES_NAME = EX97 ; Element name NEL_ARC = 4 ; Elements along 45 deg. arc NEL_FLAT = 4 ; Elements along flat segment NEL_DEPTH= 2 ; Elements through depth (z) LINEAR = <true> ; PREP = <true> ; STABILITY = <false> ; NONLINEAR = <false> ; DBC = PEAR.DBC ; DBR = PEAR.DBR ; NSTEPS = 30 ; BEG STEP = 1 ;</false></false></true></true></pre>
	DBR = PEAR.DBR ;
	•
	$BEG_STEP = 1 ;$
	$MAX_CUTS = 3 ;$
	$BEG_LOAD = .1 ;$
	$MAX_LOAD = 1 ;$
	LD_dir = 3 Direction of total load calculation )

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

### \*call PEAR\_CYL

This will perform linear buckling eigenvalue analysis and 30 steps of nonlinear analysis with a  $7 \times 7$  grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU times required for a stability analysis and a nonlinear analysis on various computer systems are shown in Table 4.10-2.

Computer System	Total CPU Time, sec.		
	Stability	Nonlinear	
VAX 11/785 VMS 4.7			
MicroVAX ULTRIX 2.2			
SUN SUNVIEW 4.0		****	
CONVEX C220 VERSION 7.0			
CRAY-2 UNICOS 4.0			

Table 4.10-2 CPU TIMES Table

(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING\_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

## 4.10.5 LIMITATIONS

None.

## 4.10.6 ERROR MESSAGES AND WARNINGS

None.

#### 4.10.7 PROCEDURE FLOWCHART

PEAR_CYL	(main procedure)
PEAR_MODEL	(define model)
ES	(define elements)
PEAR_CON	(define boundary conditions)
MATDAT	(define material properties)
DEF_ELTS4	(define 4-node models)
DEF_ELTS9	(define 9-node models)
PEAR_AD	(define applied displacements)
L_STATIC	(linear static analysis procedure)
TOTAL_LOAD	(sum reaction forces to get total load)
L_STABIL_2	(linear stability analysis procedure)
TOTAL_LOAD	(sum reaction forces to get total load)
NL_STATIC_1	(nonlinear static analysis procedure)
HISTORY	(archive historical data)
TOTAL_LOAD	(sum reaction forces to get total load)

#### 4.10.8 PROCEDURE LISTING

4.10.8.1 <u>UNIX Script</u>

```
pear_cyl.com
```

```
cd $SCR/$USER
cp $CSM_PRC/proclib.gal proclib.gal
chmod u+w proclib.gal
rm PEAR.*
time testbed << \endinput
  *set echo off
  *set plib 28
  *open 28 proclib.gal /old
  *add '$CSM_APP/pear_cyl/pear_cyl.clp'
*def/i es_proj = 1
*def/i es_coro = 1
#def/i nl_geom = 2
*def/a solver_name =BAND
*def/a nl_solver =BAND
*call PEAR_CYL ( ES_PROC = ES1 ; -- . Element Processor
                      ES_NAME = EX97 ; -- . Element name
```

NEL\_arc = 4 ; -- . Elements along 45 deg. arc  $NEL_flat = 4$ ; -- . Elements along flat segment NEL\_depth= 3 ; -- . Elements through depth (z) NSTEPS = 60 ; -- . DBC = PEAR.DBC ; --DBR = PEAR.DBR ; --PREP = <true> ; --LINEAR = <false> ; --STABILITY= <false> ; --NONLINEAR= <true> ; ---NEWTON = <false> ; --= <true> ; ---POST BEG\_LOAD = .2 ; -- . MAX\_LOAD = 120.0 )

[xqt EXIT \endinput

#### 4.10.8.2 CLAMP Procedure

pear\_cyl.clp

```
*procedure PEAR_CYL ( ES_PROC = ES1 ; -- . Element Processor
                         ES_NAME = EX97 ; -- . Element name
                         NEL_arc = 4 ; -- . Elements in 45 deg. arc
                         NEL_flat = 4 ; -- . Elements along flat segment
                                      ; -- . Elements through depth
                         NEL_depth= 1
                         LD_dir = 3
                                      ; -- . Direction of total load
                         NSTEPS = 30
                                         ; ---
                         BEG_STEP = 1
                                         ; --
                         BEG_LOAD = .01
                                         ; --
                         MAX_LOAD = 1.0 ; --
                         MAX_CUTS = 3
                                         ; --
                         DBC = PEAR.DBC; DBR = PEAR.DBR; --
                         PREP = <true>; --
                         LINEAR = <true>; --
                         STABILITY = <false>; --
                         NONLINEAR = <false>; --
                         NEWTON = <false>; --
                         POST = <false> ---
                       )
           CSM Testbed Procedure for Analysis of Pear-Shaped Cylinder
                 written by S. McCleary (PRC Kentron) -- 2/88
*def/i NOM_ldi = 3
*open/new 1 [DBc]
.
*if [PREP] /then
   *call PEAR_MODEL ( ES_proc = [ES_PROC]; --
                     ES_name = [ES_NAME]; --
```

nel\_a = [NEL\_arc] ; -nel\_f = [NEL\_flat]; -nel\_z = [NEL\_depth] ) \*endif \*if < [LINEAR] >/then \*call L\_STATIC \*call TOTAL\_LOAD ( EQUIL\_CK= 0 ; --; --NSTEPS = 0LOAD\_SET = 1 ; -- $CONS_SET = 1$ ; --NAME1 = 'STAT' ; --NAME2 = 'REAC' ; ---FAC = 1.0 ; --LD\_DIR = [Ld\_dir] --) \*elseif < [STABILITY] > /then \*call L\_STABIL\_2 (function='all';n\_modes=2;print=<true>;stress=<true> ; -cons\_set=1; bcon\_set=1 ) \*call TOTAL\_LOAD ( EQUIL\_CK= 0 ; --NSTEPS = 0; ---LOAD\_SET = 1 ; -- $CONS_SET = 1$ ; ---NAME1 = 'STAT' ; --NAME2 = 'REAC' ; --FAC = 1.0; ---LD\_DIR = [Ld\_dir] --) \*endif \*open/new 3, [DBr] \*if < [NONLINEAR] > /then \*def/i ns\_overwrite == <true> \*call NL\_STATIC\_1 ( NL\_GEON = <nl\_geom> ; --COROTATION=<es\_coro> ; --NEWTON = [NEWTON] ; --BEG\_STEP = [BEG\_STEP] ; --MAX\_STEPS = [NSTEPS] ; --- $BEG_LOAD = [BEG_LOAD]$ ; --MAX\_LOAD = [MAX\_LOAD] ; --MAX\_CUTS = [MAX\_CUTS] ; --NOMINAL\_DB = [DBr] ; --NOMINAL\_DS = [ES\_PROC].[ES\_NAME].1.1 ; -- $N_SELECT = 2$ ; --

```
SEL_NODES = 1, <<nntotal>-<nnod_z>+1> ; --
                     SEL_DOFS = 1,1
                                             ---
                   )
  *toc 1
*endif
*if < [POST] /gt 0 > /then
   *open 1, [DBc]
   *open 3, [DBr]
   *if < [POST] /eq 1 > /then
         *call HISTORY ( input_ds = TOT.DISP; output_ldi = 1
                                                            ; --
                       output_ds= [ES_PROC].[ES_NAME].1.1
                                                           ; --
                       output_rn= RADIAL_DISP ; LOCATION = NODES ; --
                       num_steps = [NSTEPS]
                                                           ; --
                       steps = [BEG_STEP]:<[BEG_STEP]+[NSTEPS]-1>; --
                       num_nodes= 1
                                                             ; ---
                       nodes = <<nntotal>-<nnod_z>+1>
                                                             ; --
                       component = 1
                                                               ---
                     )
         *call TOTAL_LOAD ( EQUIL_CK= 0
                                         ; --
                          NSTEPS = [NSTEPS] ; --
                          LOAD_SET = 0
                                        : --
                          CONS_SET = 0
                                         : --
                          NAME1 = 'REAC'
                                       ; --
                          NAME2 = 'FORC'
                                       ; --
                                         ; ---
                          FAC = 1.0
                          LD_DIR = [Ld_dir] --
                        )
          *print 3 1 TOTAL* /out=9
          *print 3 1 DISP_U_<<nntotal>-<nnod_z>+1>* /out=9
 *endif
*endif
*end
*procedure PEAR_MODEL ( ES_proc = ES1 ; --
                     ES_name = EI97 ; --
                     nel_a = 4 ; ---
                           = 4
                                   ; ---
                     nel_f
                           = 2
                                   )
                     nel_z
      Initialize element macros
      *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [ES_PROC]; --
                                     es_name = [ES_NAME] )
            _____
.
      Set dimensions and number-of-nodes macros:
```

```
. Depth (in z direction) of cylinder
*def/g dz == 0.40
                                     . Radius of curved portions of cylinder
*def/g r == 1.0
*def/g sq2 = (2.0^0.5)
*def/g rs2 = < <r> * <sq2> >
*def/g rd2 = < <r>/<sq2> >
*def/g rr2 = < <r> + <rd2> >
*def/g rm = < -<r> >
*def/g rr2m = < -<rr2> >
*def/g rd2m = < -<rd2> >
#def/g rs2m = < -<rs2> >
*def/i nel_b = <[nel_f]*if < <es_nen> /eq 4 > /then
                                                     . Through z
    *def/i nnod_z == < [nel_z] + i >
    #def/i nnod_a == < [nel_a] + 1 >
                                                     . Along arc
                                                     . Along flat segment
    *def/i nnod_f == < [nel_f] + 1 >
                                                     . Along bottom segment
    *def/i nnod_b == < <nel_b> + 1 >
                                                     . Circumferentially
    *def/i nnod_c == <4*[nel_a]+[nel_f]+<nel_b> + 1 >
*elseif < <es_nen> /eq 9 > /then
                                                     . Through z
    *def/i nnod_z == < 2*[nel_z] + 1 >
    *def/i nnod_a == < 2*[nel_a] + 1 >
                                                     . Along arc
                                                     . Along flat segment
    *def/i nnod_f == < 2*[nel_f] + 1 >
                                                      . Along bottom segment
    *def/i nnod_b == < 2*<nel_b> + 1 >
    *def/i nnod_c == < 2*<4*[nel_a]+[nel_f]+<nel_b>> + 1 > . Circumferentially
#endif
*def/i nnod_3a = < 3*< <nnod_a> - 1 > + 1 >
                                                     . Around 135 deg. arc
                                                     . Start segment 1
*def/i bseg1 = 1
*def/i bseg2 = < <bseg1> + <<nnod_a> -1>*<nnod_z> > . Start segment 2
*def/i bseg3 = < <bseg2> + <<nnod_f> -1>*<nnod_z> > . Start segment 3
*def/i bseg4 = < <bseg3> + <<nnod_3a>-1>*<nnod_z> > . Start segment 4
                                                     . Total number of nodes
*def/i nntotal == < <nnod_c>*<nnod_z> >
[xqt TAB
     START <nntotal>
     Define alternate reference frames to be used in setting up joint locations:
     ALTERNATE REPERENCE FRAMES
          1,0. 2,0. 3,0. 0.0
                                      <ra>
                                             0.0
       4
               2,0. 3,0. <rd2m> <rr2m> 0.0
       Б
           1,0.
                                      <rr2m> 0.0
                2,0. 3,0.
                              0.0
       6
          1,0.
          1,0. 2,0. 3,135.
       7
                2,0. 3,270.
       8
          1,0.
      Define joint locations:
     ------
     JOINT LOCATIONS
  \mathbf{NREF} = \mathbf{4}
                    . 90 to 135 degree arc
  FORMAT = 2
                                     135.0 0.0 <nnod_a> <nnod_z> <nnod_z>
  <bseg1> <r>
                   90.0 0.0
                               <r>
                                     135.0 0.4
           <r>
                   90.0 0.4
                               <r>>
     1
```

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```
FORMAT = 1
                  . Flat segment
 <bseg2> <rd2m> <rd2> 0.0 <rs2m> 0.0
                                       0.0 <nnod_f> <nnod_z> <nnod_z>
   1
         <rd2m> <rd2> 0.4 <rs2m> 0.0
                                       0.4
 \mathbf{NREF} = \mathbf{5}
                 . 135 degree arc
 FORMAT = 2
 <bseg3> <r> 135.0 0.0
                           <r>
                                 270.0 0.0 <nnod_3a> <nnod_z> <nnod_z>
                135.0 0.4 <r>
   1
        <r>
                                 270.0 0.4
NREF = 6
                 . Bottom flat segment
 FORMAT = 1
 <bseg4> <rd2m> <rm> 0.0 0.0 <rm> 0.0 <nnod_b> <nnod_z> <nnod_z>
   1
         <rd2m> <rm> 0.4 0.0
                               <rm> 0.4
    Assign Joint Reference Frames:
    *******
    JOINT REFERENCE FRAME ASSIGNMENTS
     NREF = -4: <br/> <br/> <br/> <br/> <br/> <br/> <br/> <br/> >bseg1>, <<br/> <br/> <br/> <br/> >bseg2> - 1>
     NREF = 7: <bseg2>, <<bseg3> - 1>
     NREF = -5: <bseg3>, <<bseg4> - 1>
     NREF = 8: <bseg4>, <nntotal>
    ______
    Constraint Definitions:
    ____
*call PEAR_CON ( nnod_z = <nnod_z> ; nntotal = <nntotal> )
    _____
    Material Properties:
    ------
*call MATDAT
    Element Definitions:
    *if < <es_nen> /eq 4 > /then
   *call DEF_ELTS4 ( ES_name = [ES_name] ; --
                  nel_a = [nel_a] ; --
                  nel_f = [nel_f]
                                    ; --
                  nel_z = [nel_z]
                                      ; --
                  nel_b
                        = <nel_b>
                                    )
*else
   *call DEF_ELTS9 ( ES_name = [ES_name] ; --
                  nel_a = [nel_a] ; --
                  nel_f = [nel_f]
                                   ; --
                  nel_z = [nel_z]
                                     ; --
                          = <nel_b> )
                  nel_b
*endif
    _____
```

```
Applied Loading:
     _____
*call PEAR_AD ( nnod_z = <nnod_z> ; nntotal = <nntotal> )
*end
*procedure PEAR_CON ( nnod_z ; nntotal )
                                       . Buckling; simply supported
    CONSTRAINT DEFINITION 1
                                       . Plane 2,3 plane of symmetry
      symm plane=1
                                        . Plane 1,2 plane of symmetry
      symm plane=3
      nonzero 3 : [nnod_z],[nntotal],[nnod_z] . Apply displacement at z=dz
      zero 1,2,6: [nnod_z],[nntotal],[nnod_z] . Edge z=dz simply supported
      *if <ifeqs(<es_name>;E410)> /then
          *Remark E410 drilling freedoms ON
      +else
                    1, [nntotal], 1 . Constrain in-plane rotations
          zero 4 :
      *endif
*end
*procedure DEF_ELTS4 ( ES_name ; --
                             ; --
                      nel_a
                      nel_f
                             ; --
                      nel_z
                               ; --
                      nel_b
                               )
*def/i nel_circum = <4*[nel_a] + [nel_f] + [nel_b]>
#def/i jinc = <[nel_x]+1>
*def/i j1 = 1
*def/i j2 = 2
*def/i j3 = <<j2> + <jinc>>
*def/i j4 = <<j1> + <jinc>>
[xqt ELD
    <es_expe_cmd>
    <j1> <j2> <j3> <j4> 1 [nel_z] <nel_circum>
    stop
*end
*procedure DEF_ELTS9 ( ES_name ; --
                      nel_a
                              ; ---
                               ; --
                      nel_f
                      nel_z
                                ; ---
                      nel_b
                                )
*def/i nel_circum = <4*[nel_a] + [nel_f] + [nel_b]>
*def/i jinc = <2*[nel_z]+1>
#def/i j1 = 1
*def/i j2 = <<j1>+2>
```

```
*def/i j3 = <<j2> + 2*<jinc>>
*def/i j4 = <<j1> + 2*<jinc>>
*def/i j5 = <<j1> + 1>
*def/i j6 = <<j2> + <jinc>>
*def/i j7 = <<j5> + 2*<jinc>>
#def/i j8 = <<j1> + <jinc>>
*def/i j9 = <<j5> + <jinc>>
[xat ELD
  <es_expe_cmd>
   <j1> <j2> <j3> <j4> <j5> <j6> <j7> <j8> <j9> 1 [nel_z] <nel_circum>
   stop
+end
*procedure MATDAT
[xqt AUS
*def g = 3.84615e+6
*def/g t == 0.01
. E11 NU12 E22 G12 G13 G23 ALPHA1 ALPHA2 WTDEN
    TABLE(NI=16,NJ=1): OMB DATA 1 1
    I=1,2,3,4,5,6,7,8,9
    J=1: 10.0E+6 .30 10.0E+6 <g> <g> <g> 0.0 0.0 .1
    TABLE (NI=3,NJ=1,itype=0): LAN OMB 1 1
           J=1 : 1 <t> 0.00
[xqt lau
*end
#procedure PEAR_AD ( nnod_z ; nntotal )
[xqt AUS
    sysvec : appl moti
    i=3 : j=[nnod_z],[nntotal],[nnod_z] : -2.E-5
*end
```

#### 4.10.9 REFERENCES

- 4.10-1 Hartung, R. F.; and Ball, R. E.: A Comparison of Several Computer Solutions to Three Structural Shell Analysis Problems. AFFDL TR-73-15, April 1973.
- 4.10-2 Almroth, B. O. and Brogan, F. A. (1981). "Computational Efficiency of Shell Elements," Nonlinear Finite Element Analysis of Plates and Shells, Hughes, T. J. R., Pifko, A., and Jay, A. (Editors), AMD Vol. 48, ASME, pp. 147-165.

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4.10-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.11 Procedure PINCHED\_CYL

## 4.11.1 GENERAL DESCRIPTION

The pinched cylinder – a circular cylindrical shell subjected to two equal and opposite radial forces at 0 and 180 degrees along its mid-span circumference – is a classical problem that has been used extensively to check the ability of shell elements to represent inextensional bending deformation. Two versions of the problem are considered here: (i) with open ends, and (ii) with a rigid membrane diaphragm on each end to prevent cross-sectional distortion. The open-ended version leads to pure inextensional deformation (i.e., zero membrane strains) in the limit as the shell thickness to shell radius ratio h/R approaches zero. An exact solution for this limiting case may be found in reference 4.11-1. The pinched cylinder with closed ends does not exhibit pure inextensional deformation, but rather a complex combination of bending and membrane effects with a bending boundary layer in the immediate vicinity of the concentrated loads. A series solution for this latter case may be found in reference 4.11-2.

This section describes a procedure that solves another classical problem which is one of the MacNeal-Harder test cases. Two versions of this circular cylindrical shell subjected to equal and opposite radial forces at its mid-span circumference are provided: (i) with open ends and (ii) with a rigid membrane diaphragm on each end. The L/2 by 90-degree model used in each case is shown in figure 4.11-1.

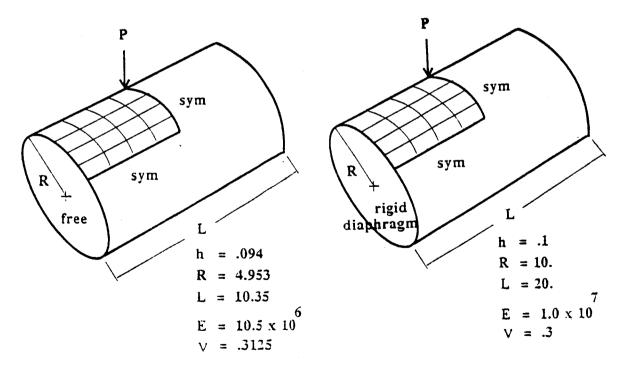


Figure 4.11-1 Pinched Cylinder Problem.

## 4.11.1.1 Model Description

## 4.11.1.2 Analysis Description

4.11.1.3 Available Solutions

## 4.11.2 PROCEDURE USAGE

Procedure PINCHED\_CYL may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call PINCHED\_CYL ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PINCHED\_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
ES_PROC	ES1	Element processor
ES_NAME	<b>EX97</b>	Element name
ES_PARS	0.	Element research parameters
NNODES_A	5	Number of axial nodes
NNODES_C	5	Number of circumferential nodes
AUTO_DOF_SUP	<true></true>	Automatic degrees of freedom suppression
DRILLING_DOF	<false></false>	Drilling (normal rotational) freedoms
DBC	PC.DBC	Computational database name
DBR	PC.DBR	Results database name
PREP	<true></true>	Perform preprocessing (model generation)
LINEAR	<true></true>	Perform linear static analysis
REACTION	<false></false>	Calculate internal forces or reactions
POST	<true></true>	Perform postprocessing (selected data archival)

## 4.11.3 ARGUMENT DESCRIPTIONS

### 4.11.3.1 AUTO\_DOF\_SUP

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them — for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING\_DOF).

#### 4.11.3.2 DBC

Name of computational database file (default=PC.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

#### 4.11.3.3 DBR

Name of results database file (default=PC.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups — indexed by load step number — for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

## 4.11.3.4 DRILLING\_DOF

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active ---unless they are automatically suppressed using use of the AUTO\_DOF\_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO\_DOF\_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING\_DOF argument should be set to <true> regardless of how AUTO\_DOF\_SUP is set.

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## 4.11.3.5 <u>ES\_NAME</u>

Element name (default: EX97). This argument is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-noded quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.1-1).

## 4.11.3.6 ES\_PARS

Element research parameters (default: 0., ...). This argument allows is an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 4.11.3.7 <u>ES\_PROC</u>

Element processor (default: ES1) This argument is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

## 4.11.3.8 LINEAR

Linear stress analysis flag (default: <true>).

## 4.11.3.9 <u>NNODES\_A</u>

Number of axial nodes (default: 7). This argument is the number of nodes you wish to have along the axial direction of the cylindrical shell model, *i.e.*, along one-tenth of the full cylinder's length. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_A can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 4.11.3.10 <u>NNODES\_C</u>

Number of circumferential nodes (default: 7). This argument is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, *i.e.*, along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, NNODES\_C can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9-node quadrilateral elements.

## 4.11.3.11 POST

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the CC.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed if you wish to archive special displacement and/or internal force component response histories post-facto.

#### 4.11.3.12 PREP

Pre-processing flag (default= $\langle true \rangle$ ). This flag must be turned on the first time procedure **PINCHED\_CYL** is run, as it causes the model to be generated. If subsequent runs are used to perform other stages of the analysis (*e.g.*, nonlinear restarts), then **PREP** must be set to  $\langle false \rangle$  for those subsequent runs.

#### 4.11.4 USAGE GUIDELINES AND EXAMPLES

Procedure PINCHED\_CYL may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis.

<pre>*call PINCHED_CYL ( ES_PROC = ES1 ; ES_NAME = EX97 ;</pre>
$NNODES_A = 7 ; NNODES_C = 7 ;$
SPEC_DIS = <false> ;</false>
DRILLING_DOF = <false> ;</false>
AUTO_DOF_SUP = <true> ;</true>
$PREP = \langle true \rangle ;$
STABILITY = <true> ;</true>
IMPERFECTION = <true> ;</true>
LINEAR = <true> ;</true>
POST = <true> ;</true>
$BEG_STEP = 1 ;$
NSTEPS = 10 ;
$BEG_LOAD = .1 ;$
$MAX_LOAD = 3.0 ;$
DBc = PC.DBc ; DBr = PC.DBr )

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call PINCHED\_CYL

This will perform linear buckling eigenvalue analysis and 10 steps of nonlinear analysis with a  $7 \times 7$  grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.11-1.

#### Table 4.11-1 CPU TIMES Table

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING\_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

## 4.11.5 LIMITATIONS

#### 4.11.6 ERROR MESSAGES AND WARNINGS

None.

## 4.11.7 PROCEDURE FLOWCHART

PINCHED_CYL	(main procedure)	
GEN_SHELL	(generate model)	
PC_BC	(generate boundary conditions/loads)	
PDC_BC		
L_STATIC_1	(perform linear static analysis)	
POST		

## 4.11.8 PROCEDURE LISTING

#### 4.11.9 REFERENCES

- 4.11-1 Timoshenko, S. and Woinowsky-Krieger, S., Theory of Plates and Shells, McGraw-Hill. New York, 1969.
- 4.11-2 Lindberg, G.M., Olson, M.D. and Cowper, G.R. "New Developments in the Finite Element Analysis of Shells", Q. Bull. Div. Mech. Eng. and the National Aeronautical Establishment, National Research Council of Canada, vol. 4, 1969, pp. xxx.
- 4.11-3 Ashwell, D.G.: "Strain Elements, with Applications to Arches, Rings, and Cylindrical Shells," *Finite Elements for Thin Shells and Curved Members*, D.G. Ashwell and R.H. Gallagher (editors), John Wiley and Sons, New York, 1974, pp. 91-111.
- 4.11-4 Forsberg, Kevin: "An Evaluation of Finite Difference and Finite Element Techniques for Analysis of General Shells," In Proceedings of the Symposium on High Speed Computing of Elastic Structures, B. Fraeijs de Veubeke (editor), I.U.T.A.M., Liège, 1970, pp. 837-859.
- 4.11-5 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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## 4.12 Procedure PWHOLE

#### 4.12.1 GENERAL DESCRIPTION

#### 4.12.1.1 Problem Description

This application problem involves a linear static stress analysis of a thin isotropic membrane with a central circular hole subjected to uniform compression (see Figure 4.12-1). This problem is important in that plate and shell elements are frequently used to model regions with a severe stress gradient.

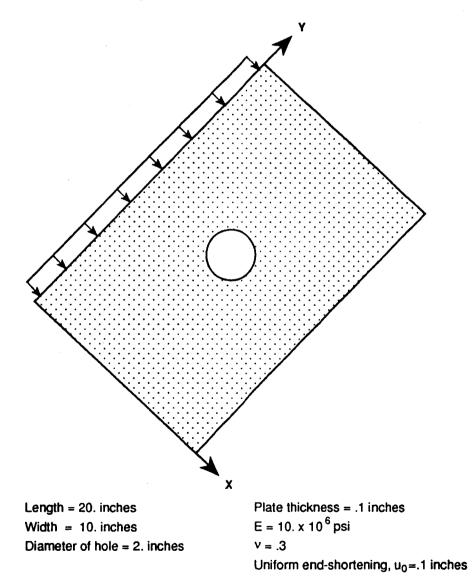


Figure 4.12-1 Plate with Circular Hole

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## 4.12.1.2 Model Description

Procedure PWHOLE models an entire rectangular membrane using 2-D quadrilateral elements. The mesh is generated using processor CSM1. This processor generates a file named PANEL.PRC which is added to the procedure library. This file contains various procedures associated with model generation (PANEL\_BC), and applied displacements (PANEL\_AD).

## 4.12.1.3 Analysis Description

Procedure PWHOLE performs a single linear static stress analysis. The solution procedure L\_STATIC described in Chapter 3 is used to perform the static stress.

## 4.12.1.4 Available Solutions

## 4.12.2 PROCEDURE USAGE

Procedure PWHOLE may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call PWHOLE ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PWHOLE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Element processor
ES_NAME	EX47	Element name
ES_PAR	0.0	Element research parameters
NRINGS	4	Number of rings of elements
NSPOKES	16	Number of radial spokes of nodes
NELX	6	Number of elements along $x$ -direction
NELE	2	Number of elements across edge
NELBS	2	Number of elements between interior stiffeners
PRINT	<false></false>	Print flag
DIRECTION	1	Direction of stress reference frame
LOCATION	'NODES'	Location for stress recovery

## 4.12.3 ARGUMENT DESCRIPTIONS

## 4.12.3.1 DIRECTION

Direction for the element stress (stress resultant) output (default: 1). The element stress coordinate system will be used if DIRECTION=0. The material axes  $(x_m, y_m, z_m)$  will be used if DIRECTION=1; the material axes  $(y_m, z_m, x_m)$  will be used for DIRECTION=2; and the material axes  $(z_m, x_m, y_m)$  will be used for DIRECTION=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 4.12-3).

## 4.12.3.2 ES\_NAME

Element name (default: EX47). This argument specifies the name of the specific shellelement type to select within the element processor defined by argument ES\_PROC. The default shell-element type, EX47, is a 4-node quadrilateral element implemented in processor ES1, and described in the Computational Structural Mechanics Testbed User's Manual (see ref. 4.12-2).

## 4.12.3.3 <u>ES\_PARS</u>

Element research parameters (default:  $0.0, \ldots$ ). This array allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 4.12.3.4 ES\_PROC

Element processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell-element type you wish to employ in the model. The default shell-element, processor ES1, is described in the Computational Structural Mechanics Testbed User's Manual (see refs. 4.12-2).

#### 4.12.3.5 LOCATION

Location of the evaluation points for the element stresses or stress resultants (default: NODES). The element stresses or stress resultants are optionally computed by calling procedure STRESS (see Section 6.4). This argument may have four values. For LOCATION=INTEG\_PTS, the element stresses are computed at the element integration points. For LOCATION=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries.

## 4.12.3.6 <u>NELBS</u>

Number of elements between interior stiffness (default: 2). Refer to processor CSM1 in reference 4.12-3 for a discussion of this argument.

## 4.12.3.7 <u>NELE</u>

Number of elements across edge (default: 2). Refer to processor CSM1 in reference 4.12-3 for a discussion of this argument.

## 4.12.3.8 <u>NELX</u>

Number of elements along x-direction (default: 6). Refer to processor CSM1 in reference 4.12-3 for a discussion of this argument.

## 4.12.3.9 <u>NRINGS</u>

Number of rings of elements (default: 4). This argument specifies the number of rings of elements, either 4-node or 9-node quadrilateral elements, around the hole.

## 4.12.3.10 <u>NSPOKES</u>

Number of radial spokes of nodes (default: 16). This argument specifies the number of radial spokes of nodes which must be a multiple of 8.

## 4.12.3.11 PRINT

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, stresses) will be printed.

## 4.12.4 USAGE GUIDELINES AND EXAMPLES

Procedure PWHOLE may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call PWHOLE ( ES_PROC = ES1 ; -- . ES_NAME = EX47 ; -- .
ES_PAR = 0.0 ; -- . Element research parameters
NRINGS = 4 ; -- . Number of rings of elements
NSPOKES = 16 ; -- . Number of radial spokes of nodes
NELX = 6 ; -- . Number of elements along x-direction
NELE = 2 ; -- . Number of elements across edge
NELBS = 2 ; -- . Number of elements between interior stiffeners
DIRECTION = 1 ; -- . Direction of stress reference frame
LOCATION = 'NODES' -- . Location for stress recovery
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,

#### \*call PWHOLE

Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.12-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

Table 4.12-1 CPU TIMES Table

#### 4.12.5 LIMITATIONS

None

#### 4.12.6 ERROR MESSAGES AND WARNINGS

None.

## 4.12.7 PROCEDURE FLOWCHART

(main procedure)	
(define elements)	
(define start card)	
(define joint locations)	
(define boundary conditions)	
(define material properties)	
(define element connectivity)	
(define freedoms)	
(define applied displacements)	
(linear static solution procedure)	

#### 4.12.8 PROCEDURE LISTING

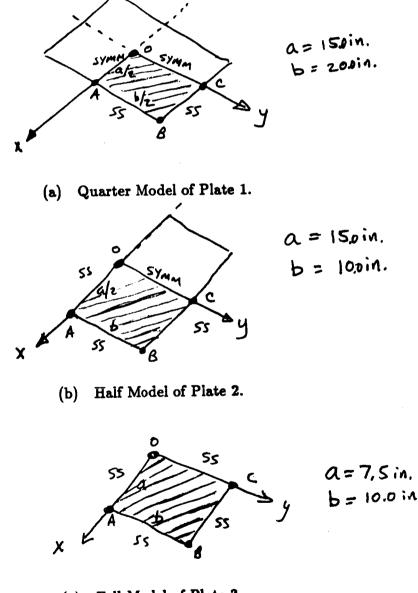
#### 4.12.9 REFERENCES

- 4.12-1 Timoshenko, S. P. and Goodier, J. N.: Theory of Elasticity (Third Edition). McGraw-Hill Book Company. New York, 1970, pp. 90-97.
- 4.12-2 Peterson, R. E.: Stress Concentration Design Factors. John Wiley and Sons-International, New York, 1953, pp. 77-88.
- 4.12-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.13 Procedure RECT\_PLATE

## 4.13.1 GENERAL DESCRIPTION

This application problem involves linear static stress analysis, linear buckling analysis and linear vibration analysis of three thin isotropic rectangular plates simply supported along their edges (see Figure 4.13-1). Various loading cases are considered including uniaxial and biaxial compression, uniform inplane shear, and inplane bending (see Figure 4.13-2).



(c) Full Model of Plate 3.

Figure 4.13-1 Rectangular Plate Problems.

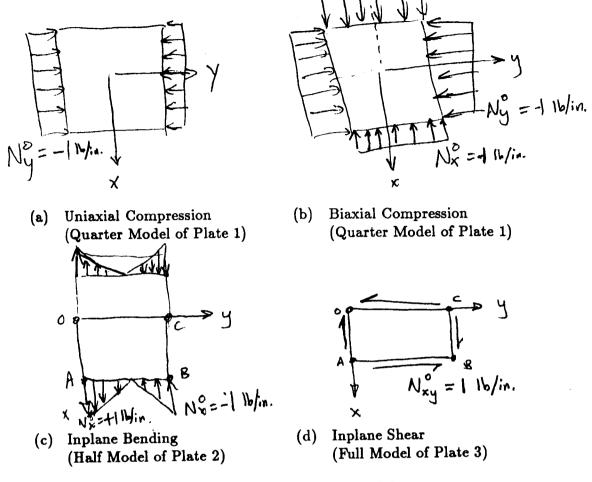


Figure 4.13-2 Loading Conditions.

## 4.13.1.1 Model Description

Procedure RECT\_PLATE uses a quarter model, a half model, and a full model of a plate depending on the loading case. The mesh topology is rectangular and restricted to quadrilateral shell elements with 4-nodes. For the quarter model shown in Figure 4.13-1a, two edges are simply supported and two edges have symmetry conditions imposed. For the half model shown in Figure 4.13-1b, three edges are simply supported and symmetry conditions are imposed on the remaining edge. For the full model shown in Figure 4.13-1c, all four edges are simply supported.

## 4.13.1.2 Analysis Description

Procedure RECT\_PLATE performs six different analyses through successive procedure calls using the various solution procedures described in Chapter 3. The analyses performed are:

- Linear free vibration analysis about an unstressed state;
- Linear buckling analysis using a linearly-computed prestress state for uniform uniaxial compression;

- Linear buckling analysis using a prescribed prestress state for uniform biaxial compression;
- Linear free vibration analysis about a prescribed prestressed state for uniform biaxial tension;
- Linear buckling analysis using a linearly-computed prestress state for uniform inplane bending;
- Linear buckling analysis using a linearly-computed prestress state for uniform inplane shear.

## 4.13.1.3 Available Solution

Analytical solutions for the vibration analyses are available in reference 4.13-1 and for the buckling analyses in reference 4.13-2.

#### Case 1: Free vibration

For this analysis, the quarter model of plate 1 is used. From pages 492-494 of reference 4.13-1, the frequencies for vibration are given as

$$\omega_{mn} = \frac{\pi^2}{a^2} \sqrt{\frac{D}{\rho h}} \left( m^2 + n^2 \frac{a^2}{b^2} \right)$$
(4.13-1)

where

 $\omega_{mn} = \text{circular frequency (radians/second)}$ 

$$ho = ext{mass density}$$
 $D = rac{Eh^3}{12(1-
u^2)}$ 
 $h = ext{plate thickness}$ 

E = Young's modulus

 $\nu =$ Poisson's ratio

m, n = number of half-waves in the x-, y- directions, respectively

and

$$f_{mn} = rac{\omega_{mn}}{2\pi}$$
 (hertz)

Using this formula, frequencies for this problem may be computed as follows:

m	n	$\omega_{mn}^2$	$f_{mn}$
1	1	$4.9867  imes 10^5$	112.4
1	3	$75.0712 imes10^{5}$	436.1
3	1	$186.7724 \times 10^{5}$	687.8

## Case 2: Uniform Uniaxial Compression

For this analysis, the quarter model of plate 1 is used and the loading corresponds to  $N_y = -1.0$  lb/in. From pages 351-356 of reference 4.13-2, the buckling load is given as

$$(N_y)_{cr} = \frac{\pi^2 D}{b^2} \left( n + \frac{1}{n} \frac{b^2}{a^2} \right)^2 \tag{4.13-2}$$

This expression implies that a plate buckles in such a way that there are n halfwaves in the direction of compression and only one halfwave in the perpendicular direction. The first term in equation (4.13-2) represents the Euler load for a strip of unit width and of length b. The second term represents the change in buckling load for a continuous plate from an isolated strip. For this plate,

n	$(N_y)_{cr}$ , lb/in.
1	523.04
3	874.89
5	1944.23

#### Case 3: Uniform Biaxial Compression

For this analysis, the quarter model of plate 1 is used and the loading corresponds to uniform biaxial compression

$$N_x^o = N_y^o = -1.0 \text{ lb/in.}$$

From pages 356-360 of reference 4.13-2, the buckling load may be derived from

$$N_{z}\frac{m^{2}\pi^{2}}{a^{2}} + N_{y}\frac{n^{2}\pi^{2}}{b^{2}} = D\left(\frac{m^{2}\pi^{2}}{a^{2}} + \frac{n^{2}\pi^{2}}{b^{2}}\right)^{2}$$
(4.13-3)

If  $N_x$  and  $N_y$  are proportional, then

$$N_y = RN_x$$

where R is constant. Substituting this relation into equation (4.13-3) and solving for critical values of  $N_x$  gives

$$(N_x)_{cr} = \frac{\pi^2 D}{a^2} \frac{\left(m^2 + n^2 \frac{a^2}{b^2}\right)^2}{\left(m^2 + Rn^2 \frac{a^2}{b^2}\right)}$$
(4.13-4)

The value of R is 1 for the loading case being considered. Thus

$$(N_x)_{cr} = \frac{\pi^2 D}{a^2} \left( m^2 + n^2 \frac{a^2}{b^2} \right)$$
(4.13-5)

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The critical values are therefore

m	n	$(N_x)_{cr}, \ lb/in.$
1	1	188.29
1	3	730.58
3	1	1152.36
1	5	1815.15
5	1	3080.48

#### Case 4: Vibration with Prestress State

For this analysis, the quarter model of plate 1 is used and the prestress state corresponds to uniform biaxial tension.

$$N_x^o = N_y^o = S = 1000 \text{ lb/in.}$$

From pages 481-483 and 492-494 of reference 4.13-1, the vibration frequencies for a prestressed rectangular plate may be derived as

$$\omega_{mn}^2 = \frac{\pi^4 D}{a^4 \rho h} \left( m^2 + n^2 \frac{a^2}{b^2} \right)^2 + \frac{\pi^2 S}{a^2 \rho h} \left( m^2 + n^2 \frac{a^2}{b^2} \right)$$
(4.13 - 6)

The first term of equation 4.13-6 represents the free vibration frequency. The second term represents the effect of uniform prestress on the vibration frequencies. Tensile prestress forces increases the vibration frequencies while compressive prestress forces decrease the vibration frequencies. For the plate considered herein, the vibration frequencies for a tensile prestress force S of 1000 lb/in. are as follows:

m	n	$\omega_{mn}^2$	f <sub>mn</sub>
1	1	$3.1470  imes 10^6$	292.34
1	3	$17.7827  imes 10^6$	671.15
3	1	$34.8851  imes 10^6$	940.03

#### Case 5: Inplane Bending

For this analysis, the half model of plate 2 is used and the loading across the edge AB varies linearly from  $N_x^o = 1.0$  lb/in. at point A to  $N_x^o = -1.0$  lb/in. at point B. From pages 373-379 of reference 4.13-2, the buckling load is given as

$$(N_x)_{cr} = k \frac{\pi^2 D}{b^2} \tag{4.13-7}$$

where the value of k depends on the ratio  $\frac{a}{b}$  and on the linear distribution of the loading. Specific values of k are given in Table 9-6 on page 337 of reference 4.13-2. For the plate considered herein, the value of k is 24.1 which then gives a critical load of 6534.54 lb/in.

#### Uniform Inplane Shear

For this analysis, the full model of plate 3 is used and the loading corresponds to

$$N_{xy}^{o} = 1.0 \text{ lb/in.}$$

From pages 379-385 of reference 4.13-2, the buckling load is given as

$$(N_{zy})_{cr} = k \frac{\pi^2 D}{a^2} \tag{4.13-8}$$

where the value of k depends on the ratio of  $\frac{b}{a}$  and is given in Table 9-10 on page 382 of reference 4.13-2. For the plate considered herein, the value of k is 7.53 which then gives a critical load of 3629.69 lb/in.

## 4.13.2 PROCEDURE USAGE

Procedure RECT\_PLATE may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure RECT\_PLATE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
CASE	0	Select analysis case
E	30.E6	Young's Modulus
ES_PROC	ES1	Element Processor
ES_NAME	EX47	Element name
LX	7.5	Length in x-direction
LY	10.0	Length in y-direction
NU	0.3	Poisson's ratio
PRINT	<false></false>	Print flag
THICKNESS	0.1	Thickness
WTDEN	0.1	Weight density

## 4.13.3 ARGUMENT DESCRIPTIONS

#### 4.13.3.1 CASE

Select analysis case (default: 0). This argument is used to select a specified analysis case number from one to six. The procedure will then perform only that specific analysis. If all six analysis cases are desired, then the argument CASE should be set to zero.

#### 4.13.3.2 <u>E</u>

Young's elastic modulus (default:  $30.0 \times 10^6$  psi).

#### 4.13.3.3 ES\_NAME

Element name (default: EX47). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX47, is a 4-noded quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.13-3).

#### 4.13.3.4 ES\_PROC

Element Processor (default: ES1) This is the name of the structural element (ES) Processor that contains the shell element type you wish to employ in the model. The default shell-element, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

#### 4.13.3.5 <u>LX</u>

Length of the plate model in the x-direction (default: 7.5 inches).

#### 4.13.3.6 <u>LY</u>

Length of the plate model in the y-direction (default: 10.0 inches).

#### 4.13.3.7 <u>NU</u>

Poisson's ratio (default: 0.3).

#### 4.13.3.8 PRINT

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, modeshapes, stresses) will be printed.

#### 4.13.3.9 THICKNESS

Thickness of the plate (default: 0.1 inches).

#### 4.13.3.10 WTDEN

Weight density (default: 0.1 lb/in.<sup>3</sup>). Processor LAU converts the weight density to mass density.

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# 4.13.4 USAGE GUIDELINES AND EXAMPLES

Procedure RECT\_PLATE may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,

#### \*call RECT\_PLATE

Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.13-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

Table 4.13-1 Typical CPU Times for Various Computer Systems

## 4.13.5 LIMITATIONS

The finite element model is restricted to models using 4-node quadrilateral elements. The model has a total of 54 nodes and 40 elements (5 elements in the x-direction and 8 elements in the y-direction).

## 4.13.6 ERROR MESSAGES AND WARNINGS

None.

#### 4.13.7 PROCEDURE FLOWCHART

RECT_PLATE	(main procedure)
ES	(define elements)
L_VIBRAT_O	(free vibration analysis; CASE=1)
L_STABIL_2	(buckling analysis with uniaxial compression; CASE=2)
L_STABIL_1	(buckling analysis with biaxial compression; CASE=3)
L_VIBRAT_1	(vibration with prestress; CASE=4)
L_STABIL_2	(buckling with inplane bending; CASE=5)
L_STABIL_1	(buckling with inplane shear; CASE=6)

#### 4.13.8 PROCEDURE LISTING

## 4.13.8.1 UNIX Script

#### rect\_plate.com

```
cd /scr/$USER
cp $CSM_PRC/proclib.gal proclib.gal
chmod u+w proclib.gal
rm rect_plate.l01
time testbed << \endinput
*set echo off
*set plib=28
*open 28 proclib.gal /old
*add '$CSM_APP/rect_plate/rect_plate.clp'
*open 1 rect_plate.l01 /new
*def/a solver_name = BAND
*def/a eigensolver_name = LANZ
.
.
.
Eigenvalue Problems (Buckling and Vibration)
. for an Isotropic Rectangular Plate
```

```
*call RECT_PLATE ( case=2; es_name=ex47;es_proc=es7;print=<true>)
*stop
*close 28 /delete
\endinput
```

#### 4.13.8.2 CLAMP Procedure

rect\_plate.clp

```
*PROCEDURE RECT_PLATE ( case=0; es_name='ex47';es_proc='es1'; --
                        lx=7.5;ly=10.0;e=30.0e+6;nu=0.3; --
                        thickness=0.1;wtden=0.1;print=<false> )
. Rectangular plate
              = < [•] / <2. * <1.+[nu]> > >
*def/e g
*def/e alpha = .1-4
EXOT TAB
 START 54,6
TITLE'RECTANGULAR PLATE PROBLEM
TEXT
'THE POLLOWING PLATE PROBLEMS ARE SOLVED IN THIS RUN:
' 1 FREE VIBRATION OF A RECTANGULAR PLATE.
' 2 BUCKLING OF A RECTANGULAR PLATE, COMPRESSED IN ONE DIRECTION.
* 3 BUCKLING OF A RECTANGULAR PLATE, UNIFORM COMPRESSION.
' 4 FREE VIBRATION OF A PRE-STRESSED RECTANGULAR PLATE.
> 5 BUCKLING OF A RECTANGULAR PLATE, BENDING LOAD.
' 6 BUCKLING OF A RECTANGULAR PLATE, SHEAR LOAD.
JOINT LOCATIONS
  1000 [lx] 00619
  6 0 [ly] 0 [lx] [ly] 0
          CONSTRAINT CASE 1:
CON CASE 1
SYMMETRY PLANE=1
SYMMETRY PLANE=2
ZERO 3 4: 6,48,6
ZERO 3 5: 49,53
ZERO 3: 54
          CONSTRAINT CASE 2:
CON CASE 2
SYMMETRY PLANE=1
ZERO 2: 25
ZERO 3: 1,6: 12,54,6: 49,53
'ZERO 4: 12,48,6
ZERO 5: 1,5: 49,53
          CONSTRAINT CASE 3:
```

**Application Procedures** 

```
CONSTRAINT CASE 3
ZERO 1: 1,6: 54
ZERO 2: 1.49,6
ZERO 3: 1,6: 12,54,6: 7,49,6: 50,53
ZERO 4: 12,48,6: 7,43,6
ZERO 5: 2,5: 50 53
[XQT AUS
     TABLE(NI=16,NJ=1): OMB DATA 1 1
        I=1,2,3,4,5,6,7,8,9
        J=1: [e] [nu] [e] <g> <g> <g> <alpha> <alpha> [wtden]
     TABLE (NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
        J=1 : 1 [thickness] 0.
[XOT LAU
stop
*call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc] ; --
                                ; es_pars = 0.0 )
           es_name = [es_name]
[IQT ELD
   <ES_EXPE_CMD>
     NSECT = 1
       1 2 8 7 1 5 8
          LOAD CASE 1:
[XQT AUS
ALPHA: CASE TITLE 1
1'compressive forces in y-direction applied at y=10.
SYSVEC: APPLIED FORCES 1
I=2
JOINTS=49: 54: -.75
JOINTS=50,53: -1.5
          LOAD CASE 2:
ALPHA: CASE TITLE 2
1'compressive forces in x- and y-directions applied at y=10., x=7.5
SYSVEC: APPLIED FORCES 2
I#2
JOINTS=49: 54: -.75
JOINTS=50,53: -1.50
I=1
JOINTS=6:54:-.625
JOINTS=12,48,6: -1.25
          LOAD CASE 3:
ALPHA: CASE TITLE 3
1'bending forces applied at x=7.5
SYSVEC: APPLIED FORCES 3
I=1
JOINTS=6: .57292
```

```
JOINTS=12,24,6: .9375 .6250 .3125
JOINTS=36,48,6: -.3125 -.6250 -.9375
JOINTS=54: -.57292
          LOAD CASE 4:
ALPHA: CASE TITLE 4
1'shear forces applied at x=7.5 and y=10.
SYSVEC: APPLIED FORCES 4
I=2
JOINTS=6: 54: .625
JOINTS=12,48,6: 1.250
I=1
JOINTS=49: 54: .750
JOINTS=50,53: 1.500
          LOAD CASE 5:
ALPHA: CASE TITLE 5
1'tensile forces in x-direction applied at x=7.5
SYSVEC: APPLIED FORCES 5
I=1
JOINTS=6: 54: 1250.
JOINTS=12,48,6: 2500.
stop
         PROCESS
*if < [case] /eq 0 >/then
*call L_VIBRAT_0 ( function='all';N_modes=6;print=[print];vcon_set=1 ; --
                    mass_type='consistent' )
*call L_STABIL_2 ( function='fact_solv';N_modes=2; --
                    cons_set=1; bcon_set=1; --
                    shift=0.0; stress=<true>; --
                      reaction=<true>;print=[print] )
*call L_STABIL_1 ( function='EIGEN'; bcon_set=1; --
                    N_modes=2; ps_1=-1.0;ps_2=-1.0;print=[print] )
 *call L_VIBRAT_1 ( function='all';vcon_set=1; --
                    ps_1=1000.0;ps_2=1000.0;N_modes=6;print=[print] ; --
                     mass_type='consistent' )
 *call L_STABIL_2 ( function='fact_solv';N_modes=2; --
                     cons_set=2;bcon_set=2;load_set=3; --
                     shift=0.0; stress=<true>; --
                       reaction=<true>;print=[print] )
 *call L_STIBIL_1 ( function='all';N_modes=2; --
                     ps_3=1.0;bcon_set=3; --
                     shift=0.0; --
```

۱

```
print=[print] )
*else
*if < [case] /eq 1 >/then
*call L_VIBRAT_0 ( function='all';N_modes=6;print=[print];vcon_set=1 ; --
                    mass_type='consistent' )
*elseif < [case] /eq 2 >/then
*call L_STABIL_2 ( function='all';N_modes=2; --
                   location='all';direction=1; --
                   cons_set=1; bcon_set=1; --
                   shift=0.0; stress=<true>; --
                      reaction=<true>;print=[print] )
*elseif < [case] /eq 3 >/then
*call L_STABIL_1 ( function='all'; bcon_set=1; --
                   N_modes=2; ps_1=-1.0;ps_2=-1.0;print=[print] )
*elseif < [case] /eq 4 >/then
*call L_VIBRAT_1 ( function='all';vcon_set=1; --
                   ps_1=1000.0;ps_2=1000.0;N_modes=6;print=[print] ; --
                    mass_type='consistent' )
*elseif < [case] /eq 5 >/then
*call L_STABIL_2 ( function='all';N_modes=2; --
                    cons_set=2;bcon_set=2;load_set=3; --
                    shift=0.0; stress=<true>; --
                      reaction=<true>;print=[print] )
=elseif < [case] /eq 6 >/then
*call L_STABIL_1 ( function='all';N_modes=2; --
                    ps_3=1.0;bcon_set=3; --
                    shift=0.0; --
                    print=[print] )
*endif
*endif
[xqt dcu
 toc 1
*end
```

### 4.13.9 REFERENCES

- 4.13-1 Timoshenko, S., Young, D. H. and Weaver, W., Jr.: Vibration Problems in Engineering, Fourth Edition, John Wiley and Sons, Inc., New York, 1974.
- 4.13-2 Timoshenko, S. P.; and Gere, J. M.: Theory of Elastic Stability, Second Edition, McGraw-Hill, New York, 1961.
- 4.13-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 4.14 Processor RHOMBIC\_PLATE

THIS SECTION UNDER PREPARATION

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# 4.15 Processor TRUNCATED\_CONE

# 5/24/90

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## 4.16 Procedure VIB\_2D

## 4.16.1 GENERAL DESCRIPTION

This application procedure involves linear free vibration analyses of a beam and a circular ring (see Figure 4.16-1). These one-dimensional structures are modeled using twodimensional shell elements. Various boundary conditions are imposed to obtain vibration modes about different coordinate axes.

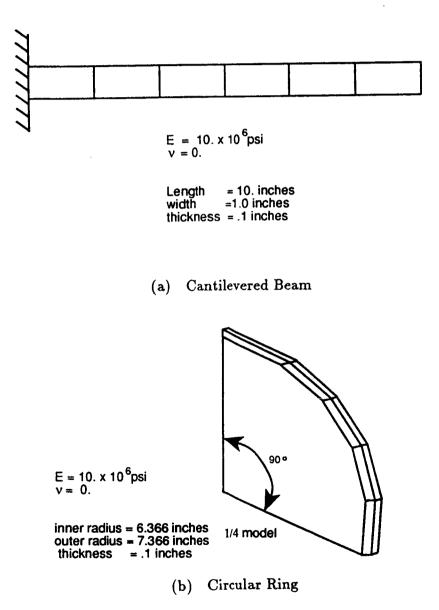


Figure 4.16-1 Free Vibration Problems

Revised 5/23/90

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## 4.16.1.1 Model Description

Procedure VIB\_2D uses a full model of the cantilevered beam and a quarter model of the circular ring. The mesh topology is rectangular and restricted to quadrilateral shell elements with 4- or 9-nodes. The mesh generation capability of processor ELD is used to generate the various meshes used in this application problem. The cantilevered beam shown in figure 4.16-1a is fixed at one end and free at the other. Only a quarter of the circular ring shown in figure 4.16-1b is modeled with symmetry conditions imposed at both ends.

## 4.16.1.2 Analysis Description

Procedure VIB\_2D performs three different linear free vibration analyses through successive procedure calls using the solution procedure L\_VIBRAT\_0 described in Chapter 3.

## 4.16.1.3 Available Solution

Analytical solutions for the vibration analyses are available in reference 4.16-1.

## Case 1: Free Inplane Vibration

For this analysis, all degrees of freedom in the z-direction have been constrained to zero so that only inplane vibration will occur. From page 369 of reference 4.16-1, the frequencies for longitudinal (axial) vibration are given as

$$\omega_m = \frac{m\pi}{2L} \sqrt{\frac{E}{\rho}} \tag{4.16-1}$$

and the frequencies for inplane flexural vibrations are given on page 426 of references 4.16-1 as

$$\omega_m = k_m^2 \sqrt{\frac{EI_{zz}}{\rho A}} \tag{4.16-2}$$

where

 $\omega_m = \text{circular frequency (radians/second)}$ 

 $\rho = mass density$ 

$$L = beam length$$

E = Young's modulus

$$I_{zz}$$
 = Moment of Inertia about z-axis,  $\frac{1}{12}b^3h$ 

 $\nu = \text{Poisson's ratio}$ 

m = number of half-waves in the x-directions, respectively

and

$$f_m = \frac{\omega_m}{2\pi}$$
 (hertz)

The constant  $k_m$  is obtained from the roots of the equation

$$\cos k_m L \cosh k_m L = -1 \tag{4.16-3}$$

The consecutive roots of this equation are

m	$k_m L$
1	1.875
2	4.694
3	7.855
4	10.996

Using these formula, frequencies for this problem may be computed as follows:

m	$\omega_m^2$	$f_m$	Туре
1	$4.776  imes 10^5$	109.990	Flexural
2	$187.590  imes 10^{5}$	689.326	Flexural
1	$1144.085 \times 10^{5}$	1702.351	Axial
3	$1471.031  imes 10^{5}$	1930.328	Flexural
2	$4576.338  imes 10^{5}$	3404.702	Axial
4	$5649.057 \times 10^{5}$	3782.754	Flexural
3	$10296.761  imes 10^5$	5107.054	Axial

#### Case 2: Free Lateral Vibration

For this analysis, only the degrees of freedom in the z-direction are unconstrained and hence lateral vibration mode shapes and frequencies will be obtained. From page 426 of reference 4.16-1, the frequencies are given as

$$\omega_m = k_m^2 \sqrt{\frac{EI_{yy}}{\rho A}} \tag{4.16-4}$$

where

 $k_m = \text{roots of equation 4.16-3}$ 

$$I_{yy} =$$
moment of inertia about y-axis,  $\frac{1}{12}bh^3$ 

Using this formula, the vibration frequencies for this problem may be computed as follows:

m	$\omega_m^2$	$f_m$
1	$4.776\times10^{3}$	10.999
2	$187.590 \times 10^{3}$	68.933
3	$1471.031 \times 10^{3}$	193.033
4	$5649.057\times10^{3}$	378.275

#### Case 3: Free Vibration of Ring

For this analysis, a quarter model of the circular ring is used. The extensional vibration modes resemble the longitudinal vibration modes of prismatic beams. The simplest extensional mode of vibration corresponds to uniform radial motion of the ring (circles of periodically varying radius). From pages 476-477 of reference 4.16-1, the frequencies for the extensional vibration modes are given as

$$\omega_m = \sqrt{\frac{E(1+m^2)}{\rho R^2}}$$
(4.16-5)

where R is the radius of centerline of ring.

Pure radial vibrations are obtained for the case of m = 0. Using this formula, the frequencies for extensional vibration may be computed as follows:

m	$\omega_m^2$	fm
0	$1.1441 \times 10^{8}$	1702.351
1	$2.2882  imes 10^8$	2407.488
2	$5.7204 imes10^8$	3806.573
3	$11.4408\times10^{8}$	5383.308

The inplane flexural vibration of a circular ring corresponds to vibration modes in the plane of the ring. From pages 479-481 of reference 4.16-1, these frequencies are given as:

$$\omega_m = \sqrt{\frac{EI_{zz}m^2(1-m^2)^2}{\rho A \ R^4(1+m^2)}}$$
(4.16-6)

For m = 1, the frequency is zero which implies that the ring moves as a rigid body. Using this formula, the frequencies for the inplane vibration modes may be computed as follows:

m	$\omega_m^2$	fm
1	0.0	0.0
2	169.3749	2.071
3	1354.9994	5.858
4	4981.6155	11.233
6	28038.4171	26.650
8	91931.4991	48.256
10	228278.8317	76.042

## 4.16.2 PROCEDURE USAGE

Procedure VIB\_2D may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

+ = = 11	VIB_2D	(	argi	=	val1	•	arg2	=	val2	:	)	ł
<b>∓ca</b> ⊥⊥	ATD-SD	· (	argi	-	AGTT		argz	-	Tarz	,		Ł

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure VIB\_2D are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
CASE	BAR	Select vibration case
E	10.E6	Young's Modulus
ES_PROC	ES1	Element Processor
ES_NAME	<b>EX9</b> 7	Element name
GRIDS	1	Grid identification numbers
NGRIDS	1	Number of grids
NNX	3	Number of nodes for each grid
L	10.0	Length in x-direction
PRINT	<false></false>	Print flag
THICKNESS	0.1	Thickness
WTDEN	5/6	Weight density
В	1.0	Beam or ring depth
DBC	VIB_2D.DBC	Computational database name
DBR	VIB_2D.DBR	Results database name
SHIFT	0.0	Eigenvalue shift
MASS_TYPE	CONSISTENT	Type of mass matrix
N_MODES	5	Number of eigenvalues desired

#### 4.16.3 ARGUMENT DESCRIPTIONS

#### 4.16.3.1 CASE

Select vibration case (default: BAR). This argument selects the vibration analysis to perform. The options include BAR, BEAM, and RING. The CASE=BAR, the analysis corresponds to the axial vibration of a rod. For CASE=BEAM, the analysis corresponds to the lateral vibration of a beam. For CASE=RING, the analysis corresponds to extensional and flexural vibration of a circular ring.

## 4.16.3.2 DBC

Name of computational database file (default=VIB\_2D.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

## 4.16.3.3 DBR

Name of results database file (default=VIB\_2D.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups — indexed by load step number — for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

## 4.16.3.4 <u>E</u>

Young's elastic modulus (default:  $10.0 \times 10^6$  psi).

## 4.16.3.5 <u>ES\_NAME</u>

Element name (default: EX97). This argument gives the name of the specific shell-element type to select, within the element processor defined by argument ES\_PROC. The default shell-element type, EX97, is a 9-node quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.16-2).

## 4.16.3.6 ES\_PROC

Element processor (default: ES1) This argument gives the name of the structural element (ES) processor that contains the shell element type to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

## 4.16.3.7 GRIDS

Grid identification numbers (default: 1). This array specifies the identification number for each discretization.

## 4.16.3.8 <u>L</u>

Length of the beam model in the x-direction (default: 10.0 inches). For the case of the circular ring, the radius is calculated as  $2L/\pi$ .

## 4.16.3.9 <u>MASS\_TYPE</u>

Type of mass matrix (default: CONSISTENT). If MASS\_TYPE = CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS\_TYPE = DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

### 4.16.3.10 NGRIDS

Number of grids (default: 1). This argument provides a mechanism to perform automatically a limited convergence study using several different discretizations.

## 4.16.3.11 <u>N\_MODES</u>

Number of converged eigenvalues desired (default: 5). This argument specifies the number of eigenvalues to calculate to a convergence criterion of .0001.

## 4.16.3.12 <u>NNX</u>

Array of number of nodes for NGRIDS models (default: 3). This array is of length NGRIDS and represents the number of nodes along the length of the beam or along the circumference of the ring.

## 4.16.3.13 PRINT

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, modeshapes, stresses) will be printed.

## 4.16.3.14 SHIFT

Eigenvalue shift (default: 0.0). Converged eigenvalues will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared  $(\omega^2)$  for vibration problems.

#### 4.16.3.15 THICKNESS

Thickness of the beam (default: 0.1 inches). The ring thickness has a default value of one-tenth the beam thickness.

#### 4.16.3.16 WTDEN

Weight density (default: 5/6 lb/in.<sup>3</sup>). Processor LAU converts the weight density to mass density.

## 4.16.4 USAGE GUIDELINES AND EXAMPLES

Procedure VIB\_2D may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

- DBR = VIB\_2D.DBR ; --MASS\_TYPE = CONSISTENT ; --GRIDS = 1,2,3 ; --NGRIDS = 3 ; --NNX = 5,9,17 ; --SHIFT = 0.0 ; --N\_MODES = 5 ; --PRINT = <false> ; --THICKNESS = 0.1 ; --WTDEN = 0.1 )
- (E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,

#### \*call VIB\_2D

Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.16-1.

Computer System	Total CPU Time, seconds.
VAX 11/785 VMS 4.7	
MicroVAX ULTRIX 2.2	
SUN SUNVIEW 4.0	
CONVEX C220 VERSION 7.0	
CRAY-2 UNICOS 4.0	

Table 4.16-1 Typical CPU Times for Various Computer Systems

## 4.16.5 LIMITATIONS

None.

## 4.16.6 ERROR MESSAGES AND WARNINGS

None.

#### 4.16.7 PROCEDURE FLOWCHART

VIB\_2D

(main procedure)
(control procedure)
(define 2-D models of beam/ring)
(define elements)
(define connectivities)
(define boundary conditions)
(define freedoms)
(linear free vibration solution procedure)

#### VIB\_2D

## 4.16.8 PROCEDURE LISTING

#### 4.16.8.1 UNIX Script

#### vib\_2d.com

```
cd /scr/$USER
cp $CSM_PRC/proclib.gal proclib.gal
chmod u+w proclib.gal
rm VIB*.*
time testbed << \endinput
*set echo off
*set plib=28
*open 28 proclib.gal /old
*add '$CSM_APP/vib_2d/vib_2d.clp'
*def/a solver_name = INV
*def/a eigensolver_name = EIG2
. Axial Vibration of a Bar
                   = BAR; mass_type = CONSISTENT; --
*call VIB_2D ( case
                  ES_PROC=ES7 ; ES_NAME=EX97; --
                          = 10.0 ; thickness = .1 ; b = 1.0 ; --
                  L
                          = 1.e7 ; wtden = <5./6.> ; ---
                   R
                                                   ; --
                                 ; print= <false>
                   N_modes = 5
                   shift=0.0 ; nnx=7,9,11; grids=1,2,3; ngrids=3; --
                   DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
  Lateral Vibration of a Beam
                    = BEAM ; mass_type = CONSISTENT; --
*call VIB_2D ( case
                   ES_PROC=ES7 ; ES_NAME=EX97; --
                          = 10.0 ; thickness = .1 ; b = 1.0
                                                                ; --
                   L
                          = 1.e7 ; wtden = <5./6.> ; ---
                   E
                                 ; print= <false>
                                                     ; --
                   N_modes = 5
                   shift=0.0 ; nnx=5,9,17; grids=1,2,3; ngrids=3; --
                   DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
  Extensional and Flexural Vibrations of a Circular Ring
                    = RING ; mass_type = CONSISTENT; --
 *call VIB_2D ( case
                   ES_PROC=ES7 ; ES_NAME=EX97; --
                          = 10.0 ; thickness = .1 ; b = 1.0
                                                               ; --
                   L
                           = 1.e7 ; wtden = <5./6.> ; ---
                   E
                                                    ; --
                                  ; print= <false>
                   N_modes = 5
                   shift=0.0 ; nnx=5,9,17; grids=1,2,3; ngrids=3; --
                   DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
  *stop
  *close 28 /delete
 \endinput
```

#### 4.16.8.2 CLAMP Procedure

vib\_2d.clp

```
; -- . BAR | BEAM | RING
                            = BAR
*procedure VIB_2D_CTL ( case
                mass_type = CONSISTENT ; -- . CONSISTENT | DIAGONAL
                              ; ES_NAME=EX97; --
                 ES_PROC=ES1
                       = 10.0 ; thickness = .1 ; b = 1.0
                                                        : --
                T.
                       = 1.e7 ; wtden = <5./6.> ; ---
                 P.
                                                ; ---
                               ; print= <false>
                 N_modes = 5
                          ; nnx=5; grid=1; --
                 shift=0.0
                DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
      *open/new 1, [DBc]
      *call WIB_2D_MOD ( es_proc = [es_proc] ; es_name = [es_name]; --
                          = [nnx] ; L = [L]; h=[thickness] ; --
                      nnx
                      E=[E]; b=[b]; rho=[wtden]; case=[case] )
. *show macros
. *set echo.on
     *call L_VIBRAT_0 ( N_modes=[N_modes]; print = [print]; --
                      shift=[shift]; --
                      mass_type=[mass_type] )
*end
*procedure VIB_2D_MOD ( es_proc=ES1; es_name=EX97; es_pars=0.; --
                    nnx
                          = 11 ; ---
                    L
                           = 10.0; h = .1; --
                           = 1.e7; b = 1.0; --
                    E
                    rho
                           = \langle 5./6. \rangle; case = BAR )
     . Vibrations of a Cantilevered Beam via Plate Elements
 _____
. Define Model
  *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
            es_name = [es_name]
                                    ; es_pars = [es_pars] )
  *def/i nny = < <ES_NEN>^.5 >
  [XQT TAB
  *def/i nnt = < [nnx]*<nny> >
   START <nnt>
   JLOC
. DEFINE NODAL COORDINATES
  *if < <IFELSE([case];RING;1;0)> > /then
 . Define First Quadrant of a Cylinder of Unit Axial Length
*def/e theta = 90.
     *def/e radius = ([L]*2/<pi>)
     FORMAT = 2
             <radius>, 0., 0., <radius>, <theta>, 0., [nnx], 1, <nny>
     1,
     [nnx], <radius>, 0., 1., <radius>, <theta>, 1.
```

```
JREF
       NREF = -1
          1, <nnt>
  *else
                                               [nnx], 1, <nny>
             0., 0., 0., [L], 0., 0.,
     1.
     [nnx], 0., [b], 0., [L], [b], 0.
  *endif
. DEFINE MATERIAL/SECTION PROPERTIES
  [XOT AUS
. Build Table of Material Data
  TABLE(NI=16,NJ=1): OMB DATA 1 1
  *def/e12.4 NU = 0.0
  *def/g12.4 G = < [E] / (2.*(1.+<NU>)) >
  I=1,2,3,4,5,6,7,8,9
  J=1: [E] <NU> [E] <G> <G> <G> 0. 0. [rho]
. Build Laminate Data Tables
  TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
  I=1,2,3 . (material_type, layer_thickness, angle(deg.)
                                            0.0
                              [h]
  J=1:
               1
   [XQT LAU
   ONLINE=2
. GENERATE ELEMENTS
   [xqt ELD
    <ES_EXPE_CMD>
     NSECT = 1
    Define element nodal connectivity
     *call VIB_2D_CONN ( nnx=[nnx]; nny=<nny>; nen=<es_nen> )
. DEFINE BOUNDARY CONDITIONS
                                    ; nny = <nny> ; --
      *call VIB_2D_BCS ( nnx = [nnx]
                         nen = <es_nen> ; case = [case] )
      *call ES ( function = 'DEFINE FREEDOMS' )
*end
*procedure VIB_2D_CONN ( nnx; nny; nen )
        . Define Element Connectivity Record for ELD Processor
        *if < [nen] /eq 4 > /then
      *do $iy = 1, <[nny]-1>
         *do $ix = 1, <[nnx]-1>
```

```
#def/i n1 = < (<$iy>-1)*[nnx] + <$ix> >
         *def/i n2 = < <n1> + 1 >
         *def/i n3 = < <n2> + [nnx] >
         *def/i n4 = < <n3> - 1
         ************************
         <n1> <n2> <n3> <n4>
         ------
      *enddo
    *enddo
  *elseif < [nen] /eq 9 > /then
    *do $iy = 1, <[nny]-2>, 2
      *do $ix = 1, <[nnx]-2>, 2
         *def/i n1 = < (<$iy>-1)*[nnx] + <$ix> >
         *def/i n2 = < <n1> + 2 >
         *def/i n3 = < <n2> + (2*[nnx]) >
         *def/i n4 = < <n3> - 2 >
         *def/i n5 = < <n1> + 1 >
         #def/i n6 = < <n2> + [nnx] >
         *def/i n7 = < <n4> + 1 >
         *def/i n8 = < <n6> - 2 >
         *def/i n9 = < <n8> + 1 >
         <n1> <n2> <n3> <n4> <n5> <n6> <n7> <n8> <n9>
         *enddo
    *enddo
  *endif
*end
*procedure VIB_2D_BCS ( nnx=3; nny=3; nen=9; case = BAR )
. Define Boundary Conditions for Beam/Plate Vibrations
*def/i nnt = < [nnx]*[nny] >
[xqt TAB
CON 1
*if < <IFELSE([case];BAR;1;0)> > /then
. DEFINE CLAMPED BOUNDARY CONDITIONS for LONGITUDINAL VIBRATIONS
 . Suppress Out-of-Plane DOFS Everywhere
  ZERO 3, 4, 5 : 1, <nnt>
                       . Clamp left boundary
  ZERO 1,2,3,4,5,6
  *do $n=1,<<nnt>-[nnx]+1>, [nnx]
     <$n>
  *enddo
*elseif < <IFELSE([case];BEAM;1;0)> > /then
. DEFINE CLAMPED BOUNDARY CONDITIONS for INPLANE VIBRATIONS
 *******
```

```
. Suppress In-Plane DOFS Everywhere
   ZERO 1, 2, 6: 1, <nnt>
                          . Clamp left boundary
   ZERO 1,2,3,4,5,6
  *do $n=1,<<nnt>-[nnx]+1>, [nnx]
      <1n>
  *enddo
*elseif < <IFELSE([case];RING;1;0)> > /then
. DEFINE BOUNDARY CONDITIONS for EXTENSIONAL and PLEXURAL VIBRATIONS
 ZERO 3, 4, 5: 1, <nnt> . Suppress Out-of-Plane DOFS Everywhere
  SYMMETRY PLANE = 1 . Symmetry at theta = 90; 1/4 Model
                          . Symmetry at theta = 0
  SYMMETRY PLANE = 2
*endif
*end
*procedure VIB_2D ( case=BAR; mass_type=CONSISTENT;ngrids=1; grids=1; --
                      = 10.0 ; thickness = .1 ; b = 1.0
                                                            ; --
                 L
                        = 1.e7 ; wtden = <5./6.>
                                                     ; ---
                 E
                 N_modes = 5 ; print= <false> ; nnx=3 ; --
                 shift=0.0 ; es_proc=ES1; es_name=EX97; --
                 DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
  *if < <IFELSE([CASE];BAR;1;0)> > /then
     *def/d thickness = [thickness]
   *elseif < <IFELSE([CASE];BEAN;1;0)> > /then
     *def/d thickness = [thickness]
   *elseif < <IFELSE([CASE];BING;1;0)> > /then
      *def/d thickness = < [thickness] / 10.0 >
   *endif
   *def/i grids[1:[ngrids]] = [grids]
   *def/i nnx[1:[ngrids]] = [nnx]
   *do $g = 1, [ngrids]
      *def/i grid = <grids[<$g>]>
      *def/i nnxs = <nnx[<$g>]>
                             = [case]; mass_type = [mass_type] ; --
      *call VIB_2D_CTL ( case
                   es_proc = [es_proc]; es_name = [es_name] ; --
                   nnx = <nnxs> ; thickness = <thickness> ; --
                        = [L] ; b= [b] ; --
                  T.
                         = [E] ; wtden = [wtden]
                                                  ; ---
                  R.
                  N_modes = [N_modes]; print= [print]
                                                    ; --
                  shift=[shift]
                                : --
                  DBC=[DBC]; DBR=[DBR] ; --
                   grid=<grid> )
   *enddo
 *end
```

## 4.16.9 REFERENCES

- 4.16-1 Timoshenko, S., Young, D. H. and Weaver, W., Jr.: Vibration Problems in Engineering, Fourth Edition, John Wiley and Sons, Inc., New York, 1974.
- 4.16-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

## 5.0 Element Assessment Procedures

The procedures documented in this chapter are representative of the types of procedures that may be written to solve specific application (structural analysis) problems. Many of these high-level procedures invoke other (lower-level) procedures to perform preprocessing, solution, and postprocessing functions; which are described elsewhere in this manual. The use of procedures to perform structural analysis applications can provide users flexibility for parameterizing geometric data (e.g., stiffener spacing) as well as spatial discretization parameters (e.g., number of elements). The problems represented here are also intended to serve as part of a standard series of test problems to assess new structural elements installed in the CSM Testbed.

A summary of the procedures found in this chapter is provided by Table 5.0-1.

Procedure Name	Problem Description
DISTORTED_PC	Distorted-mesh version of the pinched_cyl problem; used to study mesh distortion sensitivity of shell elements.
MH_BEAM	MacNeal-Harder Beam problems.
MH_CYL	MacNeal-Harder Thick-Walled Cylinder Problem.
MH_PLATE	MacNeal-Harder Plate Problems.
MH_SPHERE	Linear inextensional bending of a hemispherical shell loaded by point forces. Model features "warped" quadri- lateral shell-element (facet) discretization.
PATCH_TEST	Patch Test Problems.
SKEWED_GRID	Plate Buckling Problem with Skewed Grid.

# 5.1 Processor DISTORTED\_PC

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# 5.2 Processor DISTORTED\_PC\_3D

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# 5.3 Procedure MH\_BEAMS

## 5.3.1 GENERAL DESCRIPTION

## 5.3.1.1 Problem Description

This application problem solves the three MacNeal/Harder cantilever beam problems – the twisted beam, the straight beam, and the curved beam. All three beams are solved with 4- and 9-node 2-D elements and 8-, 20-, and 32-node 3-D elements.

#### 5.3.1.2 Model Description

The straight cantilever beam problem is solved using three element shapes – rectangular, trapezoidal, and parallelogram. This problem tests an element's ability to handle distorted meshes under various types of loading. It is clamped on one end and free at the other end where unit loads are applied in four directions – extension, torque, in-plane, and out-of-plane. The dimensions, mesh, and material properties of the beam are given in Figure 5.3-1.

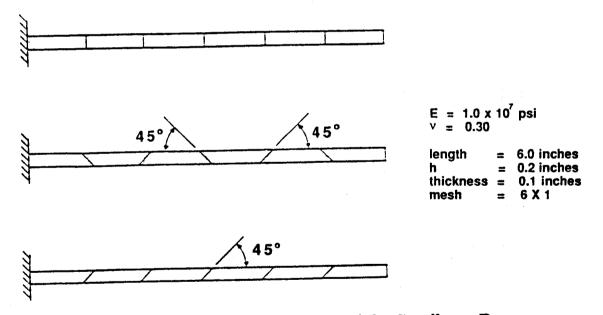
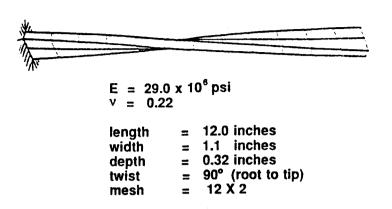


Figure 5.3-1 MacNeal/Harder Straight Cantilever Beam

The twisted cantilever beam is modeled with 24 elements. The beam is clamped on one end and free at the other. It is twisted through 90° root to tip. This problem tests an element's ability to handle warped elements (the four corners of the element do not lie in the same plane). Two different loading conditions are applied at the free end – in-plane unit load, and out-of-plane unit load. The dimensions, mesh, and material properties are shown in Figure 5.3-2.





The curved cantilever beam is modeled with six elements. It is clamped on one end and free at the other end, where unit loads are applied. The beam is curved, forming a 90° arc. Two loading conditions are used – in-plane (vertical) and out-of-plane. This problem tests an element's ability to model in-plane curvature. The dimensions, mesh, and material properties are shown in Figure 5.3-3.

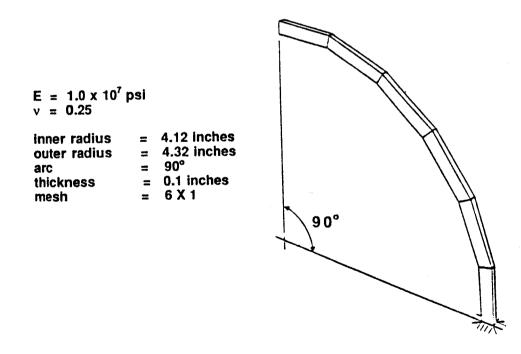


Figure 5.3-3 MacNeal/Harder Curved Cantilever Beam

0.5

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## 5.3.1.3 Analysis Description

A static, linear elastic analysis is performed, for any or all of the three problems. If the user chooses, displacements at the point of, and in the direction of the load are calculated and normalized with the theoretical results, for each loading condition.

## 5.3.1.4 Available Solutions

From reference 5.3-1, the theoretical solutions for the tip displacements for each problem and each loading condition are shown in Table 5.3-1.

	Tip displacement in direction of load (inches)					
Load Condition	Straight	Curved	Twisted			
Extension	$3.0 \times 10^{-5}$	_	_			
In-plane	.1081	.08734	.005424			
Out-of-plane	.4321	.5022	.001754			
Twist	.03208	-	-			

Table 5.3-1 Theoretical tip displacements for each beam.

#### 5.3.2 PROCEDURE USAGE

Procedure MH\_BEAMS may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

## \*call MH\_BEAMS ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH\_BEAMS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
ES_PARS	0.	Element research parameters
ES_PROC	ES1	Element Processor
ES_NAME	EX47	Element name
SPAR_DIM	none	2-D or 3-D SPAR element
DEL_LIB	<false></false>	Delete libraries
REPORT	<true></true>	Generate "report card" file
STRAIGHT	<true></true>	Solve straight beam
TWISTED	<true></true>	Solve twisted beam
CURVED	<true></true>	Solve curved beam

## 5.3.3 ARGUMENT DESCRIPTIONS

#### 5.3.3.1 ES\_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

#### 5.3.3.2 ES\_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES\_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

#### 5.3.3.3 <u>ES\_NAME</u>

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES\_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.3-2).

#### 5.3.3.4 SPAR\_DIM

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

#### 5.3.3.5 <u>DEL\_LIB</u>

Libraries are created for each model-stbm.101 for the straight beam, cvbm.101 for the curved beam, and twbm.101 for the twisted beam. As the analysis proceeds, these libraries will automatically be deleted if DEL\_LIB is <true>. This allows disk space to be conserved if the analyst does not need the libraries.

#### 5.3.3.6 <u>REPORT</u>

Print report file (default=<true>). If REPORT is <true> an external file named BEAM\_<es\_name>.<es\_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

#### 5.3.3.7 STRAIGHT

Solve straight beam problem (default: <true>. This parameter simply indicates whether the straight cantilever beam problem is to be solved or not.

#### 5.3.3.8 <u>TWISTED</u>

Solve twisted beam problem (default: <true>. This parameter simply indicates whether the twisted cantilever beam problem is to be solved or not.

#### 5.3.3.9 CURVED

Solve curved beam problem (default: <true>. This parameter simply indicates whether the curved cantilever beam problem is to be solved or not.

## 5.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH\_BEAMS may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

*procedure MH_BEAMS	( ES_NAME = EX47	;	
<b>P</b>	$ES_PROC = ES1$	;	
	$ES_PARS = O$	;	
	SPAR_DIM	;	
	DEL_LIB = <false></false>	;	
	STRAIGHT = <true></true>	;	
	TWISTED = <true></true>	ĵ	
	CURVED = <true></true>	;	
	REPORT = <true></true>	)	

(E1) To perform an analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call MH\_BEAMS

This will perform a static, linear elastic analysis of the MH\_BEAM problems. Since STRAIGHT, CURVED, and TWISTED are <true> and all three will be solved. Since REPORT is <true> and report card file named BEAM\_EX47.ES1 will be generated containing the normalized displacements of the corner nodes at the free end of the beams, Figure 5.3-4.

쁖

		ELE	MENT MENT		EX47	BEAM PROBLE ES1 .TS	MS 	
	*	1	*	2	*	3	*	<b>4</b>
********	***	******	***** *	*********	******	********	*	• <del>•</del> • • • • • • • • • • • • • • • • •
	*	extension		in-plane		out-of-pla	ne	torsion
*****	* *	*****	*****	********	*****	******	*****	*****
	*							
STRAIGHT	*					0.0004		0.9096
rect	*	0.9955		0.9036		0.9801		
rect	*	0.9955		0.9036		0.9801		0.9096
	*							0 0400
trap	*	0.7605		0.4693		0.7644		2.2199
trap	*	0.7610		0.4693		0.7624		-0.4299
	*							
parl	*	0.9660		0.3306		0.9379		-0.1234
parl	*	0.9656		0.3306		0.9393		1.8199
-	*							
	*							
TWISTED	*			0.9849		0.9941		
	*			0.9850		0.9941		
	*			0.9849		0.9941		
	*							
	*							
CURVED	*			0.9446		0.9221		
	*			0.9446		0.9484		
	*							

#### \*\*\*\*\*\*\*\*\*\*

Figure 5.3-3 Report file generated using default arguments.

(E2) The following call statement will solve only the twisted beam problem for the element EX08 in processor ES3.

\*call MH\_BEAMS ( ES\_NAME = EX08 ; --ES\_PROC = ES3 ; --DEL\_LIB = <true> ; --STRAIGHT = <false> ; --CURVED = <false> ; --REPORT = <true> )

The library twbm.101 will automatically be deleted. The report file BEAM\_EX08.ES3 is generated, Figure 5.3-5.

*******	****	*****	****	****	****	*******	****	*****
				3-D CANTIL		AM PRUBLI	<u>ems</u>	
				NAME =	EX08	_		
				PROCESSOR	= ES	3		
		EL		PARAMETERS		_		
			]	NORMALIZED	RESULT			-
	*	1	*	2	*	3	*	4
******	****	********	*****	******	*****	*****	*****	*****
	*		*		*		*	
	*	extension		in-plane	0	ut-of-pla	ane	torsion
	*							
*****	****	*******	*****	*****	******	******	*****	*****
	*							
	*							
TWISTED	*			0.9907		0.9880		
	*			0.9907		0.9880		
	*			0.9907		0.9881		
	*			0.9907		0.9881		
	*			0.9907		0.9880		
	*			0.9907		0.9880		

\*\*\*\*\*

Figure 5.3-5 BEAM\_EX08.ES3 resulting from the calling statement (E2).

(E3) The following call statement will solve the straight and twisted cantilever beam problems for the SPAR E43 element and generate the report file BEAM\_E43.SPAR.

*call MH_BEAMS	$( ES_NAME = E43$	;
	$ES_PROC = SPAR$	;
	$SPAR_DIM = 2$	;
	CURVED = <false></false>	;
	REPORT = <true></true>	)

#### 5.3.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8- and 20-node solid elements.

## 5.3.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR\_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR\_DIM must be defined as 2 or 3 when using SPAR elements. Please set this argument and rerun.

## 5.3.7 PROCEDURE FLOWCHART

## 5.3.8 PROCEDURE LISTING

#### 5.3.9 REFERENCES

- 5.3-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," *Finite Elements in Analysis and Design*, Vol. 1, 1985, pp. 3-20.
- 5.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

## 5.4 Procedure MH\_CYL

## 5.4.1 GENERAL DESCRIPTION

## 5.4.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The thick-walled cylinder problem is used to test an element's ability to handle a nearly incompressible material. As Poisson's ratio approaches 0.5, singularities may arise in the stiffness matrix as a result of dividing by  $(1-2\nu)$ . Rubber, perhaps the most common nearly incompressible material, is sometimes used in structural components.

## 5.4.1.2 Model Description

A 10° of the thick-walled cylinder, inner radius = 6 inches, outer radius = 9 inches, is modeled with only five elements as is shown in Figure 5.4-1. The thickness of this cross section is unity. Constraints are applied to all nodes so as to allow only radial displacements.

Either plate elements (2-D) or solid elements (3-D) may be used in this procedure. The 2-D elements may be either the 4- or 9-node variety and the 3-D elements may be either 8- or 20-node elements.

The cylinder is loaded with a unit pressure at the inner radius. This pressure is applied as a total force of .5236 lbs. distributed consistently on the nodes at the inner radius of the model, as is shown in Figure 5.4-2. Three sets of material properties are used in the analysis. Young's Modulus for all three is  $1000.0 \text{ lb/in}^2$ , but Poisson's ratio is allowed to approach 0.5 by assuming the three values .49, .499, and .4999.

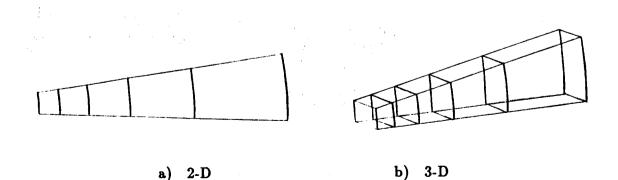
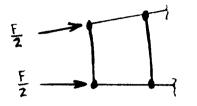
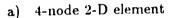
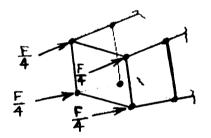


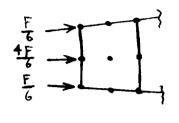
Figure 5.4-1 MacNeal/Harder Thick-Walled Cylinder



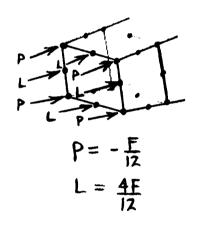




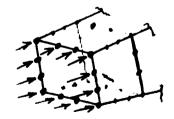
c) 8-node 3-D element



b) 9-node 2-D element



d) 20-node 3-D element



ON CORNER NODES = -F/8 ON MIDEDGE NODES = 3F/6

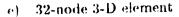


Figure 5.4-2 Consistent loading, 1.0 psi pressure at inner radius. F = .5236 lb.

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#### 5.4.1.3 Analysis Description

A static, linear elastic analysis is performed. The radial displacements of the nodes at the inner radius are compared to theoretical displacements, and normalized results are printed.

### 5.4.1.4 Available Solutions

From reference 5.4-1, the exact solution for the radial displacement is:

$$u(r) = \frac{(1+\nu)PR_1^2}{E(R_2^2 - R_1^2)} \left[ \frac{R_2^2}{r} + (1-2\nu)r \right]$$

where  $R_1$  is the inner radius,  $R_2$  is the outer radius, P is the applied pressure, and r is the variable radial position. Evaluating this expression at the inner radius (r = 3.0) for each value of  $\nu$  yields the theoretical results in Table 5.4-1.

Table 4.5-1		
Poisson's Ratio Radial displacement at inner radius (inche		
0.49	$5.0399 \times 10^{-3}$	
0.499 $5.0602 \times 10^{-3}$		
0.4999	$5.0623  imes 10^{-3}$	

#### 5.4.2 PROCEDURE USAGE

Procedure MH\_CYL may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call MH\_CYL ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH\_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	EX47	Element name
ES_PARS	0.	Element research parameters
SPAR_DIM	none	2-D or 3-D SPAR element
REPORT	<true></true>	Generate "report card" file

# 5.4.3 ARGUMENT DESCRIPTIONS

#### 5.4.3.1 ES\_NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES\_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.4-2).

#### 5.4.3.2 ES\_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES\_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

#### 5.4.3.3 ES\_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

#### 5.4.3.4 <u>SPAR\_DIM</u>

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

#### 5.4.3.5 <u>REPORT</u>

Print report file (default=<true>). If REPORT is <true> an external file named CYL\_<es\_name>.<es\_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

-----

# 5.4.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH\_CYL may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

*procedure	MH_CYL	(	$ES_NAME = EX47$	;
•				;
			$ES_PARS = 0$	;
			SPAR_DIM	;
			REPORT = <tru< td=""><td>18&gt;)</td></tru<>	18>)

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

\*call MH\_CYL

This will perform a static, linear elastic analysis of the MacNeal/Harder thickwalled cylinder problem using the EX47 element in processor ES1. Results will be given for all three values of Poisson's Ratio. The datasets will be written into a library called MH\_CYL.LO1, and the "report card" file named CYL\_EX47.ES1 will be generated, Figure 5.4-3.

		*****
	• •• •• •• •• •• ••	****
	NEAL-HARDER 2-D NAME = EX47	THICK-WALLED CYLINDER
ELEMENT	PROCESSOR =	ES1
	******	********
••••	*	
Poisson's	*	Normalized displacements
ratio	*	at inner radius
	*	
*******	*****	**************
	*	1.0054
.49	*	1.0054
	*	
. 499	*	1.0063
. 100	*	1.0063
	*	
. 4999	*	1.0063
	*	1.0063
	*	****
******	################### ##################	**************************************

Figure 5.4-3 "Report Card" using default arguments.

(E2) To perform an entire analysis using an ES element, invoke the procedure with the appropriate arguments, *i.e.* 

\*call MH\_CYL ( ES\_NAME = BR20 ; - ES\_PROC = ES10 ; - ES\_PARS = 3, 3 ; - REPORT = <true> )

This will perform a static linear elastic analysis using the BR20 element, a 20-node brick element located in processor ES10. A report file will be generated named CYL\_BR20.ES10.

(E3) To perform the analysis using a SPAR element, invoke the procedure using the appropriate arguments as follows:

\*call MH\_CYL ( ES\_NAME = E43 ; - ES\_PROC = SPAR ; - SPAR\_DIM = 2 ; - REPORT = <true> )

This will perform the analysis using the SPAR E43 element and generate the "report card" file named CYL\_E43.SPAR. Note that the argument SPAR\_DIM must be defined when using a SPAR element.

## 5.4.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8-, 20-, and 32-node solid elements.

## 5.4.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR\_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR\_DIM must be defined as 2 or 3 when using SPAR elements. Please set this argument and rerun.

## 5.4.7 PROCEDURE FLOWCHART

## 5.4.8 PROCEDURE LISTING

#### 5.4.9 REFERENCES

- 5.4-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
- 5.4-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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Revised 5/23/90

## 5.5 Procedure MH\_PATCH

## 5.5.1 GENERAL DESCRIPTION

## 5.5.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The patch test is used to test an element's ability to handle a state of constant strain with a distorted grid. This is a necessary condition to guarantee convergence of the solution.

#### 5.5.1.2 Model Description

The patch test is modeled for both 2-D and 3-D elements. The 2-D model consists of 5 distorted quadrilateral elements forming a .24 by .12 inch rectangular plate of thickness one inch, Figure 5.5-1. The 3-D model consists of seven distorted hexagonal elements forming a one inch cube, Figure 5.5-2. Element corner node locations for both the 2-D and 3-D model are shown in Table 5.5-1. For all higher order elements (2-D - 9-node and 3-D 20- and 32- node) the midedge nodes are placed equidistant from the corner nodes. However, for the 2-D 9-node model, a parameter called TWEEK has been added to allow the elements to have curved sides. See section 5.5.3 for details. The 2-D patch test is actually two separate tests, the membrane patch test, and the bending patch test. However, the bending patch test is not currently implemented.

In the membrane patch test, displacements are applied according to the following formulas:

$$u = 10^{-3}(x + y/2)$$
 in.  
 $v = 10^{-3}(y + x/2)$  in.

yielding a state of constant strain.

For the bending patch test:

$$w = 10^{-3}(x^2 + xy + y^2)/2 \text{ in.}$$
$$\theta_x = \frac{\partial w}{\partial y} = 10^{-3}(y + x/2)$$
$$\theta_y = -\frac{\partial w}{\partial x} = 10^{-3}(-x - y/2)$$

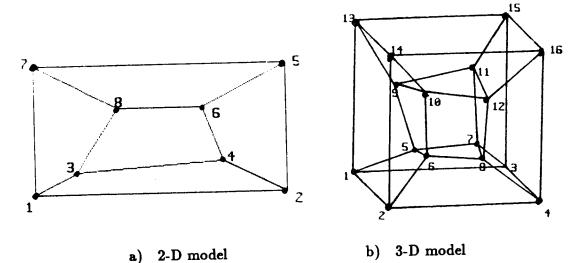
yielding a state of constant curvature.

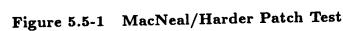
A state of constant strain is applied to the 3-D model according to the formulas:

$$u = 10^{-3}(2x + y + z)/2 \text{ in.}$$
  

$$v = 10^{-3}(x + 2y + z)/2 \text{ in.}$$
  

$$w = 10^{-3}(x + y + 2z)/2 \text{ in.}$$





	3-D Model		2-D Model		
NODE	Х	Y	Z	X	Y
1	0.000	0.000	0.000	0.00	0.00
2	1.000	0.000	0.000	0.24	0.00
3	0.000	1.000	0.000	0.04	0.02
4	1.000	1.000	0.000	0.18	0.03
5	0.249	0.342	0.192	0.24	0.12
6	0.826	0.288	0.288	0.16	0.08
° 7	0.273	0.750	0.230	0.00	0.12
8	0.850	0.649	0.263	0.08	0.08
9	0.320	0.186	0.643		
10	0.677	0.305	0.683		
11	0.165	0.745	0.702		
12	0.788	0.693	0.644		
13	0.000	0.000	1.000		
14	0.000	0.000	1.000		
15	0.000	1.000	1.000		
16	1.000	1.000	1.000		

Table 5.5-1	Element	Corner	Node	Locations
-------------	---------	--------	------	-----------

## 5.5.1.3 Analysis Description

A static, linear elastic analysis is performed. Stresses are calculated and printed, as is specified by the user, at the integration points, centroids, and/or nodes. See section 5.5.2 for details.

CSM	Testbed	Procedures	Manual
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#### 5.5.1.4 Available Solutions

From reference 5.5-1, the exact solutions are as follows:

2-D Membrane Patch Test

$$\varepsilon_x = \varepsilon_y = \gamma_{xy} = 10^{-3}$$
  
 $\sigma_x = \sigma_y = 1333 \ psi$   
 $\tau_{xy} = 400 \ psi$ 

2-D Bending Patch Test

$$M_x = M_y = 1.111 \times 10^{-7} \text{ in.lb.}$$
$$M_{xy} = 10^{-7} \text{ in.lb.}$$
$$\sigma_x = \sigma_y = \pm .667 \text{ psi}$$
$$\tau_{xy} = \pm .200 \text{ psi}$$

3-D Solid Patch Test

$$\varepsilon_{x} = \varepsilon_{y} = \varepsilon_{z} = \gamma_{xy} = \gamma_{yz} = \gamma_{xz} = 10^{-3}$$
  
$$\sigma_{z} = \sigma_{y} = \sigma_{z} = 2000 \ psi$$
  
$$\tau_{xy} = \tau_{yz} = \tau_{xz} = 400 \ psi$$

#### 5.5.2 PROCEDURE USAGE

Procedure MH\_PATCH may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call MH\_PATCH ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH\_PATCH are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	EX47	Element name
ES_PARS	ο.	Element research parameters
SPAR_DIM	none	2-D or 3-D SPAR element
REPORT	<true></true>	Generate "report card" file
STR_ALL	<true></true>	Compute stresses at nodes, integration points, and centroids
STR_NODES	<false></false>	Compute stress at nodes
STR_INTPTS	<false></false>	Compute stress at integration points
STR_CENTS	<false></false>	Compute stress at centroids
TWEEK	0,0,0,0	Move midside nodes print stresses
DISPLAY	1	Print stresses
NODES	1	Stresses at nodes and centroids
CROSS	1	Stresses at top, mid, and bottom surfaces

## 5.5.3 ARGUMENT DESCRIPTIONS

## 5.5.3.1 ES\_NAME

Element name (default=EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES\_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.5-2).

## 5.5.3.2 ES\_PROC

Element processor (default=ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES\_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

## 5.5.3.3 ES\_PARS

Element research parameters (default=0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 5.5.3.4 <u>SPAR\_DIM</u>

Number of dimensions of SPAR element (default=none). If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

## 5.5.3.5 <u>REPORT</u>

Print report file (default=<true>). If REPORT is <true> an external file named CYL\_<es\_name>.<es\_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

## 5.5.3.6 <u>STR\_ALL</u>

(default=<true>). If <true> stresses will be calculated at the element nodes, centroids, and integration points. If REPORT is <true>, stress values at all three locations will be printed in the report file.

## 5.5.3.7 <u>STR\_NODES</u>

(default=<false>). By setting this argument to <true>, STR\_ALL will be automatically reset to <false>, and stresses will be calculated only at the nodes. If REPORT is <true>, stress values at the nodes will be printed in the report file.

## 5.5.3.8 STR\_INTPTS

(default=<false>). By setting this argument to <true>, STR\_ALL will be automatically reset to <false>, and stresses will be calculated only at the integration points. If REPORT is <true>, stress values at the integration points will be printed in the report file.

## 5.5.3.9 <u>STR\_CENTS</u>

(default=<false>). By setting this argument to <true>, STR\_ALL will be automatically reset to <false>, and stresses will be calculated only at the centroids. If REPORT is <true>, stress values at the centroids will be printed in the report file.

## 5.5.3.10 TWEEK

(default=0., 0., 0., 0.). The TWEEK parameters are used to offset the midside nodes on 9-node 2-D elements. This allows the user to test an element's sensitivity to curved edges. There are four TWEEK parameters that one separated by commas, with the location and positive direction shown in Figure 5.5-3. =

## 5.5.3.11 <u>DISPLAY</u>

(default=1). For SPAR elements only. For the various values of DISPLAY, the following will be printed in the report file:

	For two-dimensional elements,
If DISPLAY	= 1, stresses
	= 2, membrane stress resultants
	= 3, bending stress resultants
	For three-dimensional solids (S41, S61, S81),
	= 1, x, y, z stress components
	relative to the element reference frame
	= 2, principal stresses
	= 3, octahedral normal stress (ONS),
	octahedral shear stress (OSS),
	stress intensity (SI),
	and yield stress ratio (YSR)
	= 4, display of $S_{xx}/Y_{xx}, S_{yy}/Y_{yy}, S_{zz}/Y_{zz}$

## 5.5.3.12 <u>NODES</u>

(default=1). For SPAR elements only. This parameter controls whether results will be printed for the element centroids or the nodes as follows:

If NODES	=	0, restrict printout to element center
	=	1, printout for each node and element center

## 5.5.3.13 CROSS

(default=1). For SPAR elements only. This parameter controls whether results are printed for the element mid-surface of top, mid and bottom surfaces as follows:

If CROSS = 0, restrict printout to mid-surface stresses = 1, printout for top, mid, and bottom surface stresses

Note: The parameters DISPLAY, NODES and CROSS are actually resets to processor PSF. See section 12.2 in reference 5.5-2 for details.

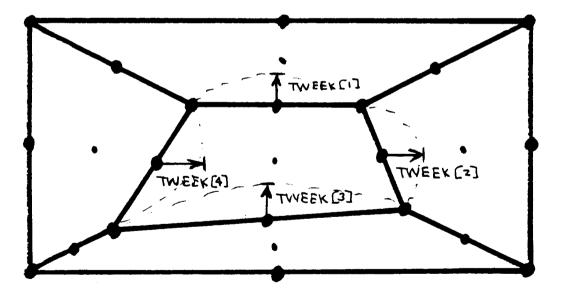


Figure 5.5-2 Location and positive direction of TWEEK parameters

## 5.5.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH\_PATCH may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

*procedure	MH_PATCH	$( ES_NAME = EX47$	;	
<b>L</b>	_	$ES_PROC = ES1$	;	
		$ES_PARS = 0$	;	
		SPAR_DIM	;	
		STR_ALL = <true></true>	;	
		STR_NODES = <false></false>	;	
		STR_INTPTS = <false></false>	;	
		STR_CENTS = <false></false>	;	
		DISPLAY = 1		;
		NODES = 1		;
		CROSS = 1		;
		TWEEK = 0., 0., 0., 0.	•	;
		REPORT = <true></true>		)

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call MH\_PATCH

This will perform a static, linear elastic analysis of the MacNeal/Harder patch test using the EX47 element in processor ES1. Stresses will be calculated at nodes, centroids, and integration points and the results will be printed to a file named PATCH\_EX47.ES1. The datasets will be written to a library named patch.101.

(E2) To perform an analysis using the BRO8 element in processor ES10 and generating stresses only at the integration points:

*call	MH_PATCH ( ES_NAME = EX43	;	
	$ES_PROC = ES4$	;	
	STR_NODES = <true></true>	;	
	REPORT = <true></true>	)	

The report file named PATCH\_BR08.ES10 will be generated containing the stresses at the element integration points only, Figure 5.5-3.

(E3) To perform an analysis using a SPAR element, invoke the procedure using the appropriate arguments as follows:

*call	MH_PATCH ( ES_NAME = E4	3 ;
	$ES_PROC = SPAR$	;
	$SPAR_DIM = 2$	;
	DISPLAY = 1	;
	NODES = O	;
	CROSS = 0	;
	REPORT = <true></true>	)

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The report file PATCH\_E43.SPAR will be generated containing stresses (display=1) at the element centroid midsurface (nodes=0, cross=0). See reference 5.5-2, section 12.2 for further information about the parameters display, nodes, and cross (they are actually resets to processor PSF). Note that SPAR\_DIM must be defined when using a SPAR element.

			*****	******	*****	**************************************
					2-D PATCH TEST	
		_		an acc	EX43	
		-		PROCESSOR		
		F	ELEMENT	PARAMATERS	= 0	
						******
**	BEGI	N PESR *	r* DA	FA SPACE=	2000000 WORDS	
<b>PT 1</b>	MENT	EX43/	TOAD	CASE 1/	GLOBAL REFER	ENCE FRAME
		LEM LOCA		NX I/	NY	NXY
	1	1	1N	1.333333E+	00 1.333333E+00	4.000000E-01
	-	-	2N	1.333333E+	00 1.333333E+00	4.000000E-01
			4N	1.333333E+	-00 1.333333E+00	4.00000E-01
			3N	1.333333E+	-00 1.333333E+00	4.000000E-01
	1	2	2N	1.333333E+	00 1.333333E+00	4.00000E-01
			5N	1.333333E+	00 1.333333E+00	4.000000E-01
			6N	1.333333E+	00 1.333333E+00	4.000000E-01
			4N	1.333333E4	00 1.333333E+00	4.00000E-01
	1	3	5 <b>N</b>	1.333333E	00 1.333333E+00	4.000000E-01
			7N	1.333333E4	+00 1.333333E+00	
			8N	1.333333E+	00 1.333333E+00	4.000000E-01
			6N	1.333333E	+00 1.333333E+00	4.00000E-01
	1	4	7 N	1.333333E	+00 1.333333E+00	4.000000E-01
			1N	1.333333E	+00 1.333333E+00	
			3N	1.333333E-	+00 1.333333E+00	4.000000E-01
			8N	1.333333E-	+00 1.333333E+00	4.000000E-01
	1	5	3 <b>N</b>	1.333333E-	+00 1.333333E+00	
			4N	1.333333E-	+00 1.333333E+00	
			6N	1.333333E-		
			8N	1.333333E		
EX	IT PR	ISR CPUT	IME=	0.6 I/O(D	IR,BUF)= 0	0
		*****	*****	***	*****	*****
		#######	#######	***	*****	*****

Figure 5.5-3 "Report Card" using EX43 in ES4.

## 5.5.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8-, 20-, and 32-node solid elements.

(L2) Currently only the 2-D membrane patch test and the 3-D test are operational.

## 5.5.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR\_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR\_DIM must be defined as 2 or 3 when using SPAR elements. Please set this argument and rerun.

#### 5.5.7 PROCEDURE FLOWCHART

## 5.5.8 PROCEDURE LISTING

#### 5.5.9 REFERENCES

- 5.5-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," *Finite Elements in Analysis and Design*, Vol. 1, 1985, pp. 3-20.
- 5.5-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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## 5.6 Procedure MH\_PLATE

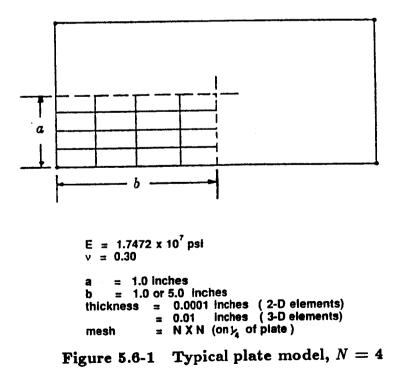
#### 5.6.1 GENERAL DESCRIPTION

#### 5.6.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The plate problem tests an element's ability to handle aspect ratio, thinness, and various types of loading and boundary conditions. The problem can be solved with 4- or 9-node 2-D elements or 8-node 3-D elements.

## 5.6.1.2 Model Description

Due to the symmetry of the physical problem a quarter model is used. Symmetry boundary conditions are applied at x=0 and y=0. At x=a and y=b two different boundary conditions are used – simply supported and clamped. Two different types of loading are applied – a central point load of  $P = 4.0 \times 10^{-4}$  lbs. and a uniform pressure of  $q = 10^{-4}$  psi. The value of a is 1.0 in., but, in order to test an element's sensitivity to aspect ratio, b has two values, 1.0 in. and 5.0 in. The quarter plate is modeled with  $N \times N$  elements. A mesh convergence study is done, with N taking the value in Table 5.6-1. The two values of b gives element aspect ratios of 1 and 5. A typical model with N = 4, material properties, and dimensions are shown in Figure 5.6-1.



	2-D Model		3-D Model		
	4-node	9-node	8-node	20-node	
N =	2	2	2	2	
	4	4	4	4	
	6	6	6	6	
	8		8		

Table 5.6-1 Values of N for different element types

# 5.6.1.3 Analysis Description

A static, linear elastic analysis is performed for each of the eight possible combinations of aspect ratio, loading, and boundary condition. Libraries named  $pl<aspect>_<grid>.101$  are created, where <aspect> is aspect ratio and <grid> is N, the mesh size. As the analysis proceeds, these libraries may be deleted by setting the argument DEL.LIB is <true>. If the argument REPORT is <true>, the normalized midplate displacements will be printed in an external "report file" named PLATE\_<es\_name>.<es\_proc>, where <es\_name> is the element name and <es\_proc> is the element processor.

## 5.6.1.4 Available Solutions

From reference 5.6-1, the exact solutions for the mid-plate displacement in the direction of the load for each boundary condition, load type, and aspect ratio are shown in Table 5.6-2.

Boundary	Aspect	Mid-plate displacer	nent (inches)
Condition	Ratio b/a	Uniform Pressure	Point Load
 	1.0	4.062	11.60
Simple	5.0	12.97	16.96
	1.0	1.26	5.60
Clamped	5.0	2.56	7.23

Table 5.6-2	Theoretical	tip displacements	for each beam.
-------------	-------------	-------------------	----------------

## 5.6.2 PROCEDURE USAGE

Procedure MH\_PLATE may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call MH\_PLATE ( arg1 = val1 ; arg2 = val2 ; ...)

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where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH\_PLATE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PARS	0.	Element research parameters
ES_PROC	ES1	Element Processor
ES_NAME	<b>EX4</b> 7	Element name
SPAR_DIM	none	2-D or 3-D SPAR element
DEL_LIB	<false></false>	Delete libraries
REPORT	<true></true>	Generate "report card" file

## **5.6.3 ARGUMENT DESCRIPTIONS**

## 5.6.3.1 ES\_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 5.6.3.2 ES\_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES\_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

## 5.6.3.3 ES\_NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES\_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.6-2).

## 5.6.3.4 <u>SPAR\_DIM</u>

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

## 5.6.3.5 <u>DEL\_LIB</u>

As the mesh convergence study proceeds, DEL\_LIB determines whether or not the individual libraries for each N will be deleted. This allows disk space to be conserved if the analyst does not need the libraries.

## 5.6.3.6 <u>REPORT</u>

Print report file (default=<true>). If REPORT is <true> an external file named PLATE\_<es\_name>.<es\_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

## 5.6.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH\_PLATE may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call MH\_PLATE

This will perform a static, linear elastic, analysis of the MH\_PLATE problem. The normalized mid-plate displacements for all combinations of loading, boundary conditions, and aspect ratio will be calculated and printed in the report file named PLATE\_EX47.ES1, Figure 5.6-2. Eight libraries named pl1\_2.101, pl1\_4.101, pl1\_6.101, pl1\_8.101, pl5\_2.101, pl5\_4.101, pl5\_6.101, and pl5\_8.101 will be generated. In a library named plA\_N.101, A is the aspect ratio and N is the mesh. These eight libraries will not be deleted as the analysis proceeds, because the default value of DEL\_LIB is <false>.

#### 

ELEMENT NAME = **EX47** ES1 **ELEMENT PROCESSOR** = ٥ ELEMENT PARAMATERS = --- NORMALIZED RESULTS ------\*\*\*\*\*\*\* \* ASPECT RATIO = 1\* \*\*\*\*\*\* DISTRIBUTED LOAD CENTRAL POINT LOAD \*\*\*\*\*\* \*\*\*\*\* simply simply \* clamped clamped \*

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	*		*	supported	*		*	supported	*
******	******	*****	*****	**********	*****	******	*****	*****	*
	*								*
MESH=2	*	0.8811		1.0042		0.9790		0.9866	*
	*								*
MESH=4	*	0.9706		0.9979		0.9969		0.9972	*
	*	0.0100							*
MESH=6	*	0.9876		0.9986		1.0009		0.9988	*
mbom-0	*	0.0010		0.0000					*
MESH=8	*	0.9936		0.9991		1.0024		0.9994	*
niijii-0	- -	0.5550		0.0001		1.0021			*
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******	* ******	<b>CENTRAL</b>	*****	LOAD	*	DIS' *********	******		*
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******	* * * * *	******	*	simply	* **** *	******	******* *	**************************************	* * *
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******** ******** MESH=2	* ****** * * *******	******	*	simply	* **** *	******	******* *	**************************************	* * *
	* * * * * * * * *	<pre>************************************</pre>	*	simply supported ************************************	* **** *	**************************************	******* *	**************************************	* * * * *
********* ********* MESH=2 MESH=4	* ****** * * *******	**************************************	*	simply supported	* **** *	************* clamped *********	******* *	**************************************	* * * * * *
MESH=4	* ************************************	<pre>************************************</pre>	*	simply supported ************************************	* **** *	**************************************	******* *	**************************************	* * * * *
	* ************************************	<pre>************************************</pre>	*	simply supported ************************************	* **** *	**************************************	******* *	**************************************	* * * * * *
MESH=4 MESH=6	* ************************************	<pre>************************************</pre>	*	simply supported ************************************	* **** *	**************************************	******* *	**************************************	* * * * * * * *
MESH=4	* ************************************	<pre>************************************</pre>	*	simply supported ************************************	* **** *	**************************************	******* *	**************************************	* * * * * *

\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*

Figure 5.6-2 Report file generated using default arguments.

(E2) To solve the MacNeal/Harder Plate problem with element E410 in processor ES5, deleting the libraries as the analysis proceeds, use the following call statement.

*call	MH_PLATE	(	ES_NAME	=	E410	;	
			ES_PROC	=	ES5	;	
			DEL_LIB	=	<true></true>	;	
			REPORT	Ξ	<true></true>	)	

(E3) To perform the analysis using a SPAR element, invoke the procedure with the appropriate element name and SPAR for the processor. The argument SPAR\_DIM must be defined when using a SPAR element. The libraries will be deleted as the analysis proceeds.

```
*call MH_PLATE ( ES_NAME = E43 ; --
    ES_PROC = SPAR ; --
    SPAR_DIM = 2 ; --
    DEL_LIB = <true> ; --
```

```
REPORT = <true> )
```

#### 5.6.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8-node solid elements.

## 5.6.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR\_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR\_DIM must be defined as 2 or 3 when using SPAR elements. Please set this argument and rerun.

## 5.6.7 PROCEDURE FLOWCHART

## 5.6.8 PROCEDURE LISTING

#### 5.6.9 REFERENCES

- 5.6-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," *Finite Elements in Analysis and Design*, Vol. 1, 1985, pp. 3-20.
- 5.6-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 5.7 Procedure MH\_SPHERE

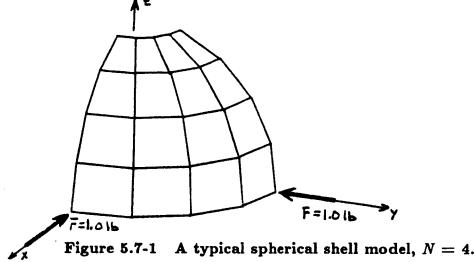
## 5.7.1 GENERAL DESCRIPTION

## 5.7.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The spherical shell problem tests an element's ability to handle double curvature.

## 5.7.1.2 Model Description

The spherical shell is modeled for both 2-D and 3-D elements. As is shown in figure 5.7-1, it is a one-eighth model of a spherical shell with a 12° hole in the top. The hole in the top of the sphere allows triangular (2-D) and wedge-shaped (3-D) elements to be avoided. The sphere is loaded by two point loads (1 lb. each) applied at centric points as is shown in figure 5.7-1. The sphere is modeled with  $N \times N$  elements. A mesh convergence study is done with N taking the values in table 5.7-1.



An example of a 2-D and a 3-D model are shown in figure 5.7-2.

## 5.7.1.3 Analysis Description

A static, linear elastic analysis is performed. Displacements at the point of, and in the direction of the loads are calculated, normalized with theoretical results, and printed for each value of N (table 5.7-1).

## 5.7.1.4 Available Solutions

From reference 5.7-1, the exact theoretical solution for the displacement at the point of, and in the direction of the load is .0940 inches.

## 5.7.2 PROCEDURE USAGE

Procedure MH\_SPHERE may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_SPHERE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH\_SPHERE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	EX47	Element name
ES_PARS	0.	Element research parameters
SPAR_DIM	none	2-D or 3-D SPAR element
REPORT	<true></true>	Generate "report card" file
DEL_LIB	<false></false>	Delete libraries

## 5.7.3 ARGUMENT DESCRIPTIONS

## 5.7.3.1 <u>ES\_NAME</u>

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES\_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in The Computational Structural Mechanics Testbed User's Manual (reference 5.7-2).

## 5.7.3.2 <u>ES\_PROC</u>

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES\_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

## 5.7.3.3 <u>ES\_PARS</u>

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 5.7.3.4 <u>SPAR\_DIM</u>

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

## 5.7.3.5 <u>REPORT</u>

Print report file (default=<true>). If REPORT is <true> an external file named CYL\_<es\_name>.<es\_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

## 5.7.3.6 <u>DEL\_LIB</u>

Delete libraries (default=< false>). As the mesh convergence study progresses, libraries named SPLN.L01 are generated, where N is the number of elements along each edge of model. If DEL\_LIB is set to < true>, these libraries will be deleted during the analysis. This allows disk space to be conserved if the analyst does not need the libraries.

	2-D Model		3-D Model	
	4-node	9-node	8-node	20-node
N =	2	1	4	2
	4	2	8	4
	6	3	12	6
	8	4		
	10	5		
	12	6		

# Table 5.7-1 N = number of elements for convergence study. Model is $N \times N$ .

## 5.7.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH\_SPHERE may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call MH\_SPHERE

This will perform a static, linear elastic analysis of the MacNeal/Harder spherical shell using the EX47 element in processor ES1. The one-eighth sphere, modeled by  $N \times N$  elements, will be analyzed with N = 2, 4, 6, 8, 10, and 12. Six libraries will be created, SPHN.L01, one for each value of N. If the argument DEL\_LIB is <true>, these libraries will be automatically deleted as the analysis proceeds. If the argument REPORT is <true>, the normalized displacements at the point of, and in the direction of, the load will be printed in a report file named CYL\_EX47.ES1 for each value of N, figure 5.7-3.

*****	*****
	****
MACNE	EAL-HARDER 2-D SPHERICAL SHELL PROBLEM
ELEMENT	NAME = $EX47$
ELEMENT	PROCESSOR = ES1
ELEMENT	PARAMATERS = 0
	NORMALIZED RESULTS
****	*******
GRID = 2	0.9676
	0.9676
GRID = 4	1.0176
	1.0176
GRID = 6	1.0012
	1.0012
GRID = 8	0.9950
	0.9950
GRID = 10	0.9923
	0.9923
GRID = 12	0.9919
	0.9919
*****	*******

Figure 5.7-3 Report file generated using default arguments.

(E2) The following call statement will solve the spherical shell problem for the solid element EX20 in processor ES3. The libraries for each value of N will be deleted.

\*call MH\_SPHERE ( ES\_NAME = EX20 ; --ES\_PROC = ES3 ; --DEL\_LIB = <true> ; --REPORT = <true> )

(E3) To perform the analysis using a SPAR element, invoke the procedure using the appropriate 4-node 2-D element or 8-node 3-D element and SPAR for ES\_PROC. Note that the argument SPAR\_DIM must be defined when using a SPAR element.

#### 5.7.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8- and 20-node solid elements.

#### 5.7.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR\_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR\_DIM must be defined as 2 or 3 when using SPAR elements. Please set this argument and rerun.

#### 5.7.7 PROCEDURE FLOWCHART

#### 5.7.8 PROCEDURE LISTING

#### 5.7.9 REFERENCES

- 5.7-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," *Finite Elements in Analysis and Design*, Vol. 1, 1985, pp. 3-20.
- 5.7-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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## 5.8 Procedure MH\_ROOF

## 5.8.1 GENERAL DESCRIPTION

#### 5.8.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The Scordelis-Lo Roof problem tests an element's ability to handle single curvature and distributed gravity loading.

#### 5.8.1.2 Model Description

The Scordelis-Lo Roof is modeled for both 2-D and 3-D elements. Due to symmetry, only one-fourth of the roof is modeled. Loading is applied to the roof in the form of a distributed gravity load equal to 90.0 pounds per square foot of surface area. For higher-order elements the load is applied using consistent loading concepts. The roof is modeled with  $N \times N$  elements on the quarter model. A mesh convergence study is done with N taking the values in Table 5.8-1. An example of a 2-D model, N=4, is shown in Figure 5.8-1. Material properties, boundary conditions, and dimensions are also shown in Figure 5.8-1.

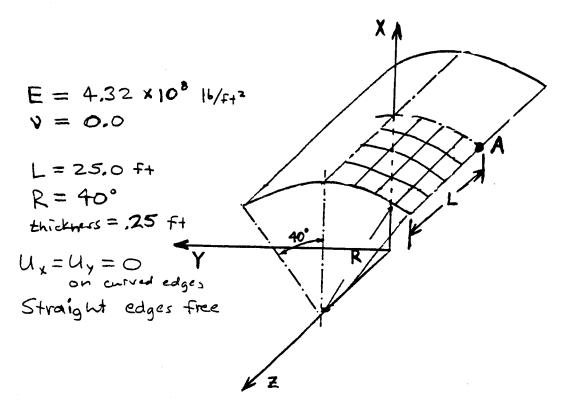


Figure 5.8-1 Example Scordelis-Lo Roof Model, N = 4.

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## 5.8.1.3 Analysis Description

A static, linear elastic analysis is performed. The x-direction displacement at the midside of free edge, point A in Figure 5.8-1, is calculated, normalized with the theoretical result, and printed for each value of N (Table 5.8-1).

## 5.8.1.4 Available Solutions

From reference 5.8-1, the theoretical solution for the displacement in the direction of the load at the midside of the free edge is .3024 inches.

## 5.8.2 PROCEDURE USAGE

Procedure MH\_ROOF may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_ROOF ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH\_ROOF are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	<u>Default Value</u>	Meaning
ES_PROC	ES1	Element Processor
ES_NAME	EX47	Element name
ES_PARS	0.	Element research parameters
SPAR_DIM	none	2-D or 3-D SPAR element
REPORT	<true></true>	Generate "report card" file
DEL_LIB	<false></false>	Delete libraries

## 5.8.3 ARGUMENT DESCRIPTIONS

## 5.8.3.1 <u>ES\_NAME</u>

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES\_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in The Computational Structural Mechanics Testbed User's Manual (reference 5.8-2).

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## 5.8.3.2 ES\_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES\_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

## 5.8.3.3 <u>ES\_PARS</u>

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

#### 5.8.3.4 <u>SPAR\_DIM</u>

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

## 5.8.3.5 <u>REPORT</u>

Print report file (default=<true>). If REPORT is <true> an external file named ROOF\_<es\_name>.<es\_proc> will be generated. This file contains the normalized vertical displacement of the node at the midside of the free edge, point A in Figure 5.8-1.

#### 5.8.3.6 <u>DEL\_LIB</u>

Delete libraries (default=< false>). As the mesh convergence study progresses, libraries named ROOFN.L01 are generated, where N is the number of elements along each edge of model. If DEL\_LIB is set to < true>, these libraries will be deleted during the analysis. This allows disk space to be conserved if the analyst does not need the libraries.

	2-D Model		<b>3-D</b>	Model
	4-node	9-node	8-node	20-node
N =	2	1	4	2
	4	2	8	4
	6	3	12	6
	8	4		
	10	5		
	12	6		

Table 5.8-1 N = number of elements for convergence study. Model is  $N \times N$ .

## 5.8.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH\_ROOF may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, *i.e.*,

#### \*call MH\_ROOF

This will perform a static, linear elastic analysis of the MacNeal/Harder Scordelis-Lo roof using the EX47 element in processor ES1. The one-fourth roof, modeled by  $N \times N$  elements, will be analyzed with N = 2, 4, 6, 8, 10, and 12. Six libraries will be created, ROOFN.L01, one for each value of N. If the argument DEL\_LIB is <true>, these libraries will be automatically deleted as the analysis proceeds. If the argument REPORT is <true>, the normalized displacements at the point of, and in the direction of, the load will be printed in a report file named ROOF\_EX47.ES1 for each value of N, Figure 5.8-3.

*********	******
*****	******
MACNEAL-HARDER 2-D SCO	DRDELIS-LO ROOF PROBLEM
ELEMENT NAME = EX47	7
ELEMENT PROCESSOR =	ES1
ELEMENT PARAMATERS =	0.
NORMALIZEI	) RESULTS
*************************************	*************
GRID = 2	1.1225
GRID = 4	0.9703
GRID = 6	0.9884
GRID = 8	0.9941
GRID = 10	0.9971
GRID = 12	1.0000
*****	*****

Figure 5.8-3 Report file generated using default arguments.

(E2) The following call statement will solve the Scordelis-Lo roof problem for the solid element EX08 in processor ES3. The libraries for each value of N will be deleted.

\*call MH\_ROOF ( ES\_NAME = EXO8 ; - ES\_PROC = ES3 ; - DEL\_LIB = <true> ; --

REPORT = <true> )

(E3) To perform the analysis using a SPAR element, invoke the procedure using the appropriate 4-node 2-D element or 8-node 3-D element and SPAR for ES\_PROC. Note that the argument SPAR\_DIM must be defined when using a SPAR element.

```
*call MH_ROOF ( ES_NAME = S81 ; --
        ES_PROC = SPAR ; --
        SPAR_DIM = 3 ; --
        REPORT = <true> )
```

## 5.8.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8- and 20-node solid elements.

## 5.8.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR\_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR\_DIM must be defined as 2 or 3 when using SPAR elements. Please set this argument and rerun.

## 5.8.7 PROCEDURE FLOWCHART

## 5.8.8 PROCEDURE LISTING

#### 5.8.9 REFERENCES

- 5.8-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
- 5.8-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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# 5.9 Processor SKEWED\_GRID

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# 6.0 Postprocessing Procedures

The procedures documented in this chapter are for postprocessing the results of a given computation. These procedures provide examples of stress recovery and internal force calculations as well as examples for extracting selected data from the computational database.

A summary of the procedures found in this chapter is provided in Table 6.0-1.

	Table 6.0-1Solution Procedures	
Procedure Name	Description	
HISTORY	Tabulate Response History in Database	
POST	Tabulate Selected Results in Database	
STRESS	Compute Stresses and/or Strains from Displacements	
TOTAL_LOAD	Compute Total Load for Applied Displacement Prob- lems	

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# 6.1 Procedure HISTORY

## 6.1.1 GENERAL DESCRIPTION

Procedure HISTORY is typically used to consolidate the response history of one or more nodes or elements into a database other than the database used for the analysis. The procedure allows for the extraction of a single nodal degree of freedom from one or more nodes. It also provides the means for extracting a single stress component from one or more elements.

## **6.1.2 PROCEDURE USAGE**

Procedure HISTORY may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call HISTORY ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure HISTORY are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure HISTORY, the following table lists each argument, its default value and meaning.

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	Argument	Default Value	Meaning
	COMPONENT		nodal dof or element stress component
	ELEMENT_DS		name of element-list dataset
	ELEMENT_RN		name of element-list record
	ELEMENTS		element numbers
	INPUT_DS		root name of input dataset
	OUTPUT_DS		full name of output dataset
	OUTPUT_RN		root name of output record
	NODE_DS		name of node-list dataset
	NODE_RN		name of node-list record
	NODES		node numbers
<u></u>	NUM_ELEMENTS		number of elements to process
	AVERAGE	<false></false>	average flag
	INPUT_LDI	1	logical device index of input database
	LOCATION	NODES	post nodal quantities
	NUM_NODES	1	number of nodes to process
	NUM_STEPS	1	number of steps
	OUTPUT_LDI	2	logical device index of output database
	STEPS	0:0	step numbers
	SUM	<false></false>	summation flag (over nodes)

## **6.1.3 ARGUMENT DESCRIPTIONS**

#### 6.1.3.1 AVERAGE

Average flag (default: <false>). If <true>, an average value for specified nodes or elements will be computed and saved in the database; otherwise individual nodal or elemental values are computed and saved.

## 6.1.3.2 INPUT\_LDI

Logical device index of input database (default: 1).

## 6.1.3.3 LOCATION

Identifies location of data to be processed; either NODES or ELEMENTS (default: NODES).

## 6.1.3.4 NUM\_NODES

Number of nodes to process (default: 1). This argument is a required argument only if LOCATION=NODES.

## 6.1.3.5 <u>NUM\_STEPS</u>

Number of steps for historical data recovery (default: 1).

#### 6.1.3.6 OUTPUT\_LDI

Logical device index of output database (default: 2).

## 6.1.3.7 STEPS

Step numbers for historical data recovery (default: 0). This argument is an array of length NUM\_STEPS. If the argument STEPS=0, the linear solution is used.

## 6.1.3.8 <u>SUM</u>

Flag to perform summation (default: <false>). If <true> the quantity of interest wil be summed over either the elements or nodes as specified by LOCATIONS. It is the summed (resultant) value is then saved in the database.

## 6.1.3.9 COMPONENT

Column of data to be extracted. When LOCATION=NODES (e.g., COMPONENT=1 corresponds to u-direction displacement). When LOCATION=ELEMENT, COMPONENT is typically a stress resultant (e.g., COMPONENT=1 corresponds to  $N_x$ ). This argument is always required.

## 6.1.3.10 ELEMENT\_DS

Name of dataset containing list of elements to be processed. This argument is an active argument only if LOCATION=ELEMENTS.

## 6.1.3.11 ELEMENT\_RN

Name of element-list record. This argument is an active argument only if LOCATION=ELEMENTS.

## 6.1.3.12 ELEMENTS

Element numbers to extract historical data. The argument ELEMENTS is an array of length NUM\_ELEMENTS that lists the element numbers for which historical data are extracted. This is an active argument only if LOCATION=ELEMENTS. Element numbers may be input either through the ELEMENTS argument or through a dataset containing the list (*i.e.*, using the ELEMENTS\_DS and ELEMENT\_RN arguments.

#### 6.1.3.13 <u>INPUT\_DS</u>

Root name (i.e., first two words) of source dataset. This argument is always required.

## 6.1.3.14 <u>OUTPUT\_DS</u>

Root name (*i.e.*, first two words) of destination dataset. This argument is always required. The dataset is written one record per step per element for LOCATION=ELEMENTS or one record per step per node for LOCATION=NODES.

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#### 6.1.3.15 OUTPUT\_RN

Root name (i.e., first word) of destination record. This argument is always required.

#### 6.1.3.16 NODE\_DS

Name of dataset containing list of nodes to be processed. This argument is an active argument only if LOCATION=NODES.

#### 6.1.3.17 <u>NODE\_RN</u>

Name of node-list record. This argument is an active argument only if LOCATION=NODES.

#### 6.1.3.18 NODES

Node numbers to extract historical data. The argument NODES is an array of length NUM\_NODES that lists the node numbers for which historical data are extracted. This is an active argument only if LOCATION=NODES. Node numbers may be input either through the NODES argument or through a dataset containing the list (*i.e.*, using the NODE\_DS and NODE\_RN arguments).

#### 6.1.3.19 <u>NUM\_ELEMENTS</u>

Number of elements to extract historical data. The argument NUM\_ELEMENTS specifies the number of elements from which historical data are extracted. This is a required argument only if LOCATION=ELEMENTS.

## 6.1.4 USAGE GUIDELINES AND EXAMPLES

Procedure HISTORY may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*procedure HISTORY ( input_ldi = 1 ; -- . ldi of input database
                    input_ds ; -- . root name of input dataset
                    output_ldi = 2 ; -- . ldi of output database
                                ; -- . full name of output dataset
; -- . root name of output record
                    output_ds
                    output_rn
                    location = NODES ; -- . post nodal quantities
                    num_steps = 1 ; -- . number of steps
                    steps = 0:0; -- . step numbers
                    num_nodes = 1 ; -- . number of nodes to process
                                    : -- . node numbers
                    nodes
                                   ; -- . nodal dof or element stress
                    component
                    sum = <false> ; -- . summation flag (over nodes)
                    average = <false> ; -- . average flag
                                    ; -- . name of node-list dataset
                    node_ds
```

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node\_rn ; -- . name of node-list record element\_ds ; -- . name of element-list dataset element\_rn ; -- . name of element-list record num\_elements ; -- . number of elements to process elements -- . element numbers)

#### 6.1.5 LIMITATIONS

Due to a restriction on the number of active macrosymbols, no more than 700 nodes or elements may be processed using NODE\_DS or ELEMENT\_DS.

Procedure HISTORY should be used only to process limited amounts of data due to the procedure's inherent inefficiency. Except for small problems, the SUM argument should not be used to perform summation over the nodes for multiple load steps. In most cases this operation should be performed using the TOTAL\_LOAD procedure (see Section 6.5).

#### 6.1.6 ERROR MESSAGES AND WARNINGS

None.

#### 6.1.7 PROCEDURE FLOWCHART

#### **6.1.8 PROCEDURE LISTING**

*procedure HISTORY (	<pre>input_ds output_ldi = 2 output_ds output_rn location = NODD num_steps = 1 steps = 0:0 num_nodes = 1 nodes component sum = <false> average = <fals node_ds node_rn element_ds element_rn</fals </false></pre>	; name of element-list dataset ; name of element-list record
	element_ds element_rn num_elements	; name of element-list dataset
)		

. Procedure to Postprocess Response History from/to Database

```
*def/i steps[1:[num_steps]] = [steps]
*if < <IFELSE([LOCATION];NODES;1;0)> > /then
   *if < <IFELSE([node_ds]; ;1;0)> > /then
      *def/i num_nodes = [num_nodes]
      $ def/i nodes[1:<num_nodes>] == [nodes]
   *else
      *find record [input_ldi], [node_ds], [node_rn] /nor=num_nodes
      *g2m /name==nodes /type=i /maxn=<num_nodes> [input_ldi] [node_ds] --
           [node_rn].1:<num_nodes>
   *endif
  [XOT VEC
   *find dataset [output_ldi] [output_ds] /seq=ids
   *if <<ids> /le 0 > /then
      *put dataset [output_ldi] [output_ds] /mrat=2000 /seq=ids
   *endif
   *do $is = 1, [num_steps]
      *def/i step_num = <steps[<$is>]>
      #find dataset [input_ldi] [input_ds].<step_num> /seq=hist_ids
      *if < <hist_ids> /le 0 > /then
         *remark
         *remark Dataset [input_ds].<step_num> not found by HISTORY
         *remark
         *return
      *endif
      *if < [sum] /or [average] > /then
         *def/e resultant = 0.0
      *endif
      *do $in = 1, <num_nodes>
         *def/i node_num = <nodes[<$in>]>
      COMPONENT <node_num> [component] [input_ds].<step_num> -> val
         *if < [sum] /or [average] > /then
            *def/e resultant = < <resultant> + <val> >
         *else
            *m2g /name=val /type=d [output_ldi] <ids> --
                 [output_rn].<step_num>
         *endif
       *enddo
       *if < [sum] /or [average] > /then
         *if < [average] > /then
            *def/e resultant = < <resultant> / <num_nodes> >
          *endif
          *m2g /name=resultant /type=d [output_ldi] <ids> --
               [output_rn].<step_num>
       * and if
    *enddo
 *elseif < <IFELSE([LOCATION];ELEMENTS;1;0)> > /then
    *if < <IFELSE([element_ds]; ;1;0)> > /then
       *def/i num_elements = [num_elements]
       *def/i elements[1:<num_elements>] == [elements]
    +else
       *find record [input_ldi], [element_ds], [element_rn] --
```

```
/nor=num elements
         *g2m /name=elements /type=i /maxn=<num_elements> [input_ldi] --
              [element_ds] [element_rn].1:<num_elements>
      *endif
     [XQT VEC
      *do $is = 1, [num_steps]
         *def/i step_num = <steps[<$is>]>
         *find dataset [input_ldi] [input_ds].<step_num> /seq=hist_ids
         *if < <hist_ids> /le 0 > /then
            *remark
            *remark Dataset [input_ds].<step_num> not found by HISTORY
            *remark
            *return
         *endif
         *if < [sum] /or [average] > /then
            *def/e resultant = 0.0
         *endif
         *do $in = 1, <num_elements>
            *def/i element_num = <elements[<$in>]>
         COMPONENT <element_num> [component] [input_ds].<step_num> -> val
            *if < [sum] /or [average] > /then
               *def/e resultant = < <resultant> + <val> >
            Velse
               *m2g /name=val /type=d [output_ldi] [output_ds] --
                    [output_rn].<step_num>
            *endif
         *enddo
         *if < [sum] /or [average] > /then
            *if < [average] > /then
               *def/e resultant = < <resultant> / <num_elements> >
            *endif
            *m2g /name=resultant /type=d [output_ldi] [output_ds] --
                 [output_rn].<step_num>
         *endif
      *enddo
   endif
+end
```

## **6.1.9 REFERENCES**

- 6.1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 6.1-2 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

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# 6.2 Procedure POST

## 6.2.1 GENERAL DESCRIPTION

Procedure POST is used to extract the response history of one or more nodes from one database and to consolidate it into another database. This procedure differs from procedure HISTORY in that POST cannot operate on element data (*e.g.*, element stress resultants).

## **6.2.2 PROCEDURE USAGE**

Procedure POST may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call POST ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure POST are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure POST, the following table lists each argument, its default value and meaning.

Parameter	<u>Default Value</u>	Meaning
DOF		Nodal degree of freedom index
INPUT_DS		Root name of input dataset
NODES		Node numbers
NODES_DS		Name of node-list input dataset
NODES_RN		Name of node-list input record
OUTPUT_DS		Full name of output dataset
OUTPUT_RN		Root name of output record
INPUT_LDI	1	Logical device index of input database
OUTPUT_LDI	1	Logical device index of output database
NSTEPS	1	Number of steps
STEPS	0:0	Step numbers
NNODES	1	Number of nodes to process
SUM	<false></false>	Summation flag (over node list)

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## **6.2.3 ARGUMENT DESCRIPTIONS**

## 6.2.3.1 <u>INPUT\_LDI</u>

Logical device index of input database (default: 1).

## 6.2.3.2 OUTPUT\_LDI

Logical device index of output database (default: 1).

## 6.2.3.3 <u>NSTEPS</u>

Number of steps for historical data recovery (default: 1).

## 6.2.3.4 STEPS

Step numbers for historical data recovery (default: 0). This argument is an array of length NUM\_STEPS. If the argument STEPS=0, the linear solution is used.

## 6.2.3.5 <u>NNODES</u>

Number of nodes to process (default: 1).

## 6.2.3.6 SUM

Flag to sum over nodes (default: <false>). If the argument SUM=<true>, the summation and not the nodal values will be saved in the database.

## 6.2.3.7 DOF

Nodal degree of freedom index (i.e., 1, 2, 3, 4, 5, or 6).

## 6.2.3.8 <u>INPUT\_DS</u>

Root name (first two words) of source dataset. This argument is mandatory.

## 6.2.3.9 NODES

Node numbers for which historical data are extracted. The argument NODES is an array of length NODES. Node numbers may be input either through the NODES argument or through a dataset containing the list (*i.e.*, using the NODES\_DS and NODES\_RN arguments).

## 6.2.3.10 <u>NODES\_DS</u>

Name of dataset containing list of nodes to be processed.

## 6.2.3.11 <u>NODES\_RN</u>

Name of node-list record.

#### 6.2.3.12 <u>OUTPUT\_DS</u>

Root name (*i.e.*, first two words) of destination dataset. This argument is mandatory. The dataset is written one record per step per node.

### 6.2.3.13 <u>OUTPUT\_RN</u>

Root name (i.e., first word) of destination record. This argument is mandatory.

## 6.2.4 USAGE GUIDELINES AND EXAMPLES

Procedure POST may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call POST ( input_ldi = 1 ; -- . ldi of input database
                                ; -- . root name of input dataset
                 input_ds
                 output_ldi = 1 ; -- . ldi of output database
                 output_ds
                                ; -- . full name of output dataset
                                ; -- . root name of output record
                 output_rn
                            = 1 ; -- . number of steps
                 nsteps
                            =0:0; -- . step numbers
                 steps
                 nnodes
                            = 1 ; -- . number of nodes to process
                 nodes
                                ; -- . node numbers
                 dof
                                ; -- . nodal degree of freedom index
                 sum = <false> ; -- . summation flag (over node list)
                                ; -- . [name of node-list input dataset]
                 nodes_ds
                 nodes_rn
                                  -- . [name of node-list input record])
```

## 6.2.5 LIMITATIONS

Due to a restriction on the number of active macrosymbols, no more than 700 nodes should be processed using NODE\_DS and NODE\_RN.

#### 6.2.6 ERROR MESSAGES AND WARNINGS

None.

#### 6.2.7 PROCEDURE FLOWCHART

Procedure POST is self-contained and has no subprocedures.

### **6.2.8 PROCEDURE LISTING**

```
*procedure POST ( input_ldi = 1 ; -- . ldi of input database
                             ; -- . root name of input dataset
                 input_ds
                 output_ldi = 1 ; -- . ldi of output database
                             ; -- . full name of output dataset
                 output_ds
                 output_rn
                               ; -- . root name of output record
                           = 1 ; -- . number of steps
                 nsteps
                           =0:0; -- . step numbers
                 steps
                           = 1 ; -- . number of nodes to process
                 nnodes
                               ; -- . node numbers
                 nodes
                               ; -- . nodal degree of freedom index
                 dof
                 sum = <false> ; -- . summation flag (over node list)
                             ; -- . [name of node-list input dataset]
                 nodes_ds
                                 -- . [name of node-list input record]
                 nodes_rn
               )
        ______
 CLAMP Procedure to Post Response History in a Database
  *def/i steps[1:[nsteps]] = [steps]
   *if < <IFELSE([nodes_ds]; ;1;0)> > /then
     *def/i nnodes = [nnodes]
      *def/i nodes[1:<nnodes>] = [nodes]
   *else
      #find record [input_ldi], [nodes_ds], [nodes_rn] /nor=nnodes
      *do $in = 1, <nnodes>
        *g2m /name=nodes[<$in>] /type=i [input_ldi] [nodes_ds] --
             [nodes_rn].<$in>
      *enddo
   *endif
  [XQT VEC
  *find dataset [output_ldi] [output_ds] /seq=ids
  *if < <ids> /le 0 > /then
     *put dataset [output_ldi] [output_ds] /mrat=2000 /seq=ids
  *endif
   *do $is = 1, [nsteps]
      *def/i step_num = <steps[<$is>]>
      *if < [sum] > /then
         *def/e resultant = 0.0
      *endif
      *do $in = 1, <nnodes>
        *def/i node_num = <nodes[<$in>]>
          COMPONENT <node_num> [dof] [input_ds].<step_num> -> value
         *if < [sum] > /then
           *def/e resultant = < <resultant> + <value> >
         *else
           *m2g /name=value /type=d [output_ldi] [output_ds] --
                [output_rn]_<node_num>.<step_num>
         *endif
      *enddo
      *if < [sum] > /then
```

```
*m2g /name=resultant /type=d [output_ldi] [output_ds] --
       [output_rn].<step_num>
       *endif
       *enddo
*end
```

#### 6.2.9 REFERENCES

- 6.2-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 6.2-2 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

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## 6.3 Procedure STRESS

#### 6.3.1 GENERAL DESCRIPTION

Procedure STRESS drives the calculation of stress resultant and strain component datasets for either linear or nonlinear analyses. The user may select recovery of stress resultants or strain components at element centroids, element nodes, element integration points or at all three locations.

### **6.3.2 PROCEDURE USAGE**

Procedure STRESS may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call STRESS ( arg1 = val1 ; arg2 = val2 ; ...)

For procedure STRESS, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
CONS_SET	1	Constraint set number
COROTATION	1	Corotational flag (0=OFF, 1=ON)
DIM	2	Intrinsic element spatial dimension (2=2D, 3=3D)
DIRECTION	1	Direction for element stress and strain recovery
DISP_DS	STAT.DISP	First two words of displacement dataset name
LOAD_SET	1	Load set number
LOCATION	NODES	Location of the evaluation points for element stresses
NL_GEOM	0	Geometric nonlinearity flag
NUM_STEPS	1	Total number of steps requiring stress calculations
NVAL_METH	3	Method to be used for global smoothing
PRINT	<false></false>	Flag to print computed results
ROTN_DS	STAT.ROTN	First two words of rotation-vector dataset name
SMOOTH	<false></false>	Flag to compute smoothed global stresses
STEPS	0	Step numbers
STRAIN	<false></false>	Flag to compute element strains
STRESS	<true></true>	Flag to compute element stresses

Tables 6.3-1, 6.3-2, and 6.3-3 list the datasets used or created by procedure STRESS, the procedures invoked by procedure STRESS, and the processors invoked by procedure STRESS, respectively.

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Table 6.3-1 Datase	Table 6.3-1 Datasets Input/Output by procedure STRESS			
Dataset	Description	Lib	Input	Output
ES.SUMMARY	ES Processor Status	1	$\checkmark$	$\checkmark$
PROP.BTAB.*	Material/Section Properties	1	$\checkmark$	
STAT.DISP.i.j <sup>†</sup>	System Displacement Vector	1		$\checkmark$
<b>STRS.</b> $\langle$ <b>ES_NAME</b> $\rangle$ . $i.j^{\dagger} =$	Element Stresses	1		$\checkmark$

 $\dagger$  i = <load\_set> and j = <cons\_set>

Table 6.3	-2 Sub-P	rocedures Invoked by procedure STRESS
Procedure	Туре	Function
ES	External	Element utility procedure
STRESS	Internal	Computes element stresses

Table 6.3	-3 Proce	ssors Invoked by procedure STRESS
Procedure Type Function		Function
ESi	External	Element processors based on GEP
NVAL	Internal	Perform global smoothing
PESR	Internal	Print element stresses
PNSR	Internal	Print nodal stresses

## **6.3.3 ARGUMENT DESCRIPTIONS**

## 6.3.3.1 <u>CONS\_SET</u>

Constraint set number (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

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------	---

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### 6.3.3.2 COROTATION

Corotational update switch for large-rotation problems (default:  $\langle true \rangle$ ). This switch should be set to  $\langle true \rangle$  when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element processor (ESi) section in the CSM Testbed User's Manual (see ref. 6.3-1) for specific guidelines.

## 6.3.3.3 <u>DIM</u>

Intrinsic element spatial dimension (default: 2). This argument selects the element spatial dimension: 2 for a two-dimensional element or 3 for a three-dimensional solid element.

## 6.3.3.4 DIRECTION

Direction for the element stress (stress resultant) output (default: 1). The element stress coordinate system will be used if DIRECTION=0. The material axes  $(x_m, y_m, z_m)$  will be used if DIRECTION=1; the material axes  $(y_m, z_m, x_m)$  will be used for DIRECTION=2; and the material axes  $(z_m, x_m, y_m)$  will be used for DIRECTION=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 6.3-1).

## 6.3.3.5 <u>DISP\_DS</u>

First two words of the dataset name for the displacement solution (default: STAT.DISP).

## 6.3.3.6 LOAD\_SET

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

## 6.3.3.7 LOCATION

Location of the evaluation points for the element stresses or stress resultants (default: NODES). The element stresses or stress resultants are optionally computed. This argument may have four values. For LOCATION=INTEG\_PTS, the element stresses are computed at the element integration points. For LOCATION=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries. For LOCATION=ALL, the element stresses are computed at the element integration points, element centroid, and element nodes.

## 6.3.3.8 <u>NL\_GEOM</u>

Geometric nonlinearity level: 0, 1, or 2 (default =2). A value of zero means that the problem is geometrically linear; a value of one means that the geometric nonlinearity will be handled globally (*i.e.*, using corotational updates only); and a value of two means that

the nonlinear element strain-displacement relations will be used in addition to any global treatment of geometric nonlinearity. If COROTATION =  $\langle true \rangle$ , options 1 and 2 refer to first-order and second-order corotation, respectively. The latter option can be significantly more accurate than the former for a given finite element model — depending on which element types are involved.

## 6.3.3.9 <u>NUM\_STEPS</u>

Number of steps for stress recovery (default: 1).

## 6.3.3.10 <u>NVAL\_METH</u>

Select method to be used for computing the smoothed global stresses (default: 3). Processor NVAL is used to compute the smoothed global stresses using the method defined by the argument NVAL\_METH (see Section 12.5 of reference 6.3-1). If NVAL\_METH=1, a topological interpolation of the element centroidal stresses is performed, and the element stresses must have been computed using LOCATION=CENTROIDS. If NVAL\_METH=2, a projected least-squares interpolation of the element centroidal stresses is performed, and the stresses must have been computed using LOCATION=CENTROIDS. If NVAL\_METH=3, the element nodal stresses (discontinuous across interelement boundaries) are averaged, and the element stresses must have been computed using LOCATION=NODES. Using LOCATION=ALL will generate element stresses at the element centroids, element nodes, and element gauss points. Acceptable values of location for specific values of NVAL\_METH are as follows:

NVAL_METH	Location
1	CENTROIDS, ALL
2	CENTROIDS, ALL
3	NODES, ALL

## 6.3.3.11 PRINT

Flag to print computed results (default: <false>). If the argument PRINT=<true>, then the element stresses and/or nodal stresses will be printed.

## 6.3.3.12 <u>ROTN\_DS</u>

First two words of the dataset name for the rotation solution (default: STAT.ROTN).

## 6.3.3.13 SMOOTH

Flag to compute smoothed global stresses (default: <false>). If the argument SMOOTH=<true>, then smoothed global stresses will be computed by processor NVAL using the method defined by the argument NVAL\_METH.

## 6.3.3.14 STEPS

Step numbers for stress recovery (default: 0). This argument is an array of length NUM\_STEPS. If the argument STEPS=0, the linear solution is used.

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### 6.3.3.15 STRAIN

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRAIN=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION.

### 6.3.3.16 STRESS

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION.

## 6.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure STRESS may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call STRESS ( STRESS
                           = <true>
                     STRAIN
                                = <false>
                     LOCATION
                                = CENTROIDS
                     DIRECTION = 0 ; --
                     NL_GEOM
                                = 0 : ---
                     CORO
                                = 1 :
                                      --
                     LOAD_SET
                                = 1 ;
                                      --
                     CONS_SET
                                = 1 :
                                      _ _ _
                     NUM_STEPS = 1 ; --
                     PRINT
                                = <false> ;
                     NVAL_METH = 3 ; --
                     SMOOTH
                                = <false> ;
                                = 2 : --
                     DIM
                     STEPS
                                = 0 ; ---
                     DISP_DS
                                = STAT.DISP
                                = STAT.ROTN )
                     ROTN_DS
```

## 6.3.5 LIMITATIONS

Applicable only to elements implemented using the generic element processor template. Procedure STRESS assumes that all datasets either required or generated reside on library one (LDI = 1).

#### STRESS

## 6.3.6 ERROR MESSAGES AND WARNINGS

An error message is printed and global stress smoothing will not be performed if the values of NVAL\_METH and LOCATION are inconsistent. Processing of element data will continue. See Section 12.5 of reference 6.3-1 for usage of processor NVAL.

### 6.3.7 PROCEDURE FLOWCHART

STRESS	(main procedure)
ES	(calculate element stresses and/or strains)

#### **6.3.8 PROCEDURE LISTING**

```
*procedure STRESS ( STRESS = <true>
                                 ; --
                STRAIN = <false>
                                  ; --
                LOCATION = CENTROIDS ; --
                DIRECTION = 0 ; --
                NL_GEOM = 0 ; --
                        = 1 ;print=<false>; --
                CORO
                LOAD_SET = 1 ; --
                CONS_SET = 1 ; --
                NUM_STEPS = 1 ; --
                        = <false>; NVAL_METH = 3; --
                SMOOTH
                        = 2 ; ---
                DIM
                        = 0 ; ---
                STEPS
                DISP_DS = STAT.DISP ; --
                ROTN_DS = STAT.ROTN --
               )
*remark ************
*remark STRESS RECOVERY
*remark *************
  Loop on Solution Steps
  *****
  *def/i steps[1:[num_steps]] = [steps]
  *do $is = 1, [num_steps]
     *def/i istep = <steps[<$is>]>
     *if <<istep> /ne 0> /then
      *def/a DS_SFI = <istep>
      *else
      *def/a DS_SFX = [load_set].[cons_set]
     *endif
 *if < <[STRAIN] /ne <false>> /or <[STRESS] /ne <false>> > /then
     Define Element Stress/Strain Option and Dataset Names
```

```
*if < <[STRAIN] /eq <true>> /and <[STRESS] /eq <false>> > /then
       *def/p function = 'FORM STRAIN'
       *def/a STRAIN_DS = <DS_SFX>
       *def/a STRESS_DS = ' '
    *elseif < <[STRAIN] /eq <true>> /and <[STRESS] /eq <true>> > /then
       *def/p function = 'FORM STRESS'
       *def/a STRAIN_DS = <DS_SFI>
       *def/a STRESS_DS = <DS_SFI>
    *elseif < <[STRAIN] /eq <false>> /and <[STRESS] /eq <true>> > /then
       *def/p function = 'FORM STRESS'
       *def/a STRAIN_DS = ' '
       *def/a STRESS_DS = <DS_SFX>
    *endif
     Invoke Element Processors to Form Stress/Strain
    _____
    *if < ifeqs( [location];ALL) > /then
     Calculate the stresses/strains at element nodes, centroids,
     and gauss points
*do $iloc = 1,3
   *if < ifeqs( <$iloc>;1) > /then
    *def/a location = CENTROIDS
    *elseif < ifeqs( <$iloc>;2) > /then
    *def/a location = NODES
    *elseif < ifeqs( <$iloc>;3) > /then
    *def/a location = INTEG_PTS
   *endif
         *call ES ( function = <function>
                                                ; --
                   es_nl_geom = [nl_geom]
                                                ; --
                    es_coro = [coro]
                                                ; --
                    es_dis_ds = [DISP_DS].<DS_SFX> ; --
                    es_rot_ds = [ROTN_DS].<DS_SFX> ; --
                                               ; --
                    es_str_dir = [DIRECTION]
                    es_str_loc = <location>
                                               ; --
                    es_strain_ds = <strain_ds>
                                               ; --
                   es_stress_ds = <stress_ds>
                                                    )
*enddo
     +else
    Calculate the stresses/strains only at [LOCATION]
    *call ES ( function = <function>
                                            : --
               es_nl_geom = [nl_geom]
                                            ; --
               es_coro = [coro]
                                           ; --
               es_dis_ds = [DISP_DS].<DS_SFX> ; --
               es_rot_ds = [ROTN_DS].<DS_SFX> ; --
               es_str_dir = [DIRECTION]
                                           ; --
               es_str_loc = [LOCATION]
                                           ; --
                                          ; --
               es_strain_ds = <strain_ds>
               es_stress_ds = <stress_ds>
                                                )
   *endif
```

```
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```

```
Print the Element Stresses
  *if < [print] > /then
    *if < ifeqs([location];ALL) > /then
     *def/i stress_loc = 0
    *elseif < ifeqs([location];CENTROIDS) > /then
     *def/i stress_loc = 1
    *elseif < ifeqs([location];NODES) > /then
     *def/i stress_loc = 2
    *elseif < ifeqs([location];INTEG_PTS) > /then
     *def/i stress_loc = 3
    *endif
    [xqt pesr
     SELECT /global=[direction] /LOCATION=<stress_loc>
     *if < <istep> /eq 0> /then
     PRINT /LOAD_SET=[load_set] /CONSTRAINT=[cons_set]
     +else
     PRINT /LOAD_SET=<istep> /CONSTRAINT=0
     *endif
     STOP
  *endif
*endif
     Calculate nodal stresses using processor NVAL
*if < [SMOOTH] > /then
     *if < ifeqs( [LOCATION];ALL) > /then
     *elseif /then < <[NVAL_METH] /eq 3> /and --
                  <ifeqs([LOCATION];NODES)> >
     *elseif /then < <[NVAL_METH] /ne 3> /and --
                  <ifeqs([LOCATION];CENTROIDS)> >
     *else
     *remark Stress evaluation point not consistent with
     *remark stress smoothing method selected.
     *jump :EXIT
      *endif
     *def/a STRS = STRS.<es_name>.<stress_ds>
      [xqt NVAL
      reset meth=[NVAL_METH], DIM=[DIM], DS=<STRS>
      reset first=1, last=<es_nstr>
      #if < [NVAL_METH] /eq 3 > /then
      *def/a REC = NODES_S[direction]
      +else
      *def/a REC = CENTROIDS_S[direction]
      *endif
      reset RECNAME=<REC>
      STOP
     Print the Nodal Stresses
```

÷

## Postprocessing Procedures

```
*if < [print] > /then
    [xqt pnsr
    *if < (istep> /eq 0 > /then
    PRINT /load=[load_set] /constraint=[cons_set] /method=[nval_meth]
    *else
    PRINT /load=<istep> /constraint=0 /method=[nval_meth]
    *endif
    STOP
    :EXIT
  *endif
*endif
*endif
*endif
```

### 6.3.9 REFERENCES

6.3-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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## 6.4 Procedure TOTAL\_LOAD

#### **6.4.1 GENERAL DESCRIPTION**

Procedure TOTAL\_LOAD sums the reaction forces to determine the total applied load for problems with applied displacements for either linear or nonlinear analyses. The computed total load may be divided by a constant and scaled by a second constant.

#### 6.4.2 PROCEDURE USAGE

Procedure TOTAL\_LOAD may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows (see example usage in Section 6.4.4):

\*call TOTAL\_LOAD ( arg1 = val1 ; arg2 = val2 ; ...)

For procedure TOTAL\_LOAD, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
INPUT_LDI	1	Input library number
OUTPUT_LDI	1	Output library number
NL_RES_LDI	3	Library containing nonlinear results dataset
LOAD_SET	1	Load set number
CONS_SET	1	Constraint set number
NSTEPS	0	Total number of load steps to be processed
BEGIN_STEP	1	First load step to be processed
END_STEP	-1	Last load step to be processed
LD_DIR	1	Load direction
EQUIL_CK	0	Flag enabling an equilibrium check
EA	1.0	Scaling constant
FAC	2.0	Scaling constant
NAME1	'STAT'	First word of input dataset name
NAME2	'REAC'	Second word of input dataset
INPUT_DS	, ,	Full name of input dataset
OUTPUT_DS	<b>&gt;</b> >	Full name of output dataset
NL_RES_DS	, ,	Full name of dataset containing nonlinear results
INPUT_REC	'DATA'	Input dataset record key
OUTPUT_REC	<b>&gt; &gt;</b>	Output record key
OUTPUT_FILE	, ,	Output file name

Table 6.4-1 lists the datasets used by procedure TOTAL\_LOAD.

```
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```

Table 6.4-1	Table 6.4-1 Datasets Input/Output by procedure TOTAL_LOAD			
Dataset	Description	Lib	Input	Output
STAT.REAC.i.j <sup>†</sup>	Reaction Force Vector	INPUT_LDI	$\checkmark$	
JDF1.BTAB.1.8	Number of nodes and active d.o.f.	INPUT_LDI	$\checkmark$	

<sup>†</sup>  $i = \langle \text{load\_set} \rangle$  and  $j = \langle \text{cons\_set} \rangle$  for linear analyses  $i = \langle \text{step} \rangle$  and j=0 for nonlinear analyses

## 6.4.3 ARGUMENT DESCRIPTIONS

#### 6.4.3.1 <u>INPUT\_LDI</u>

Input library number (default: 1).

#### 6.4.3.2 <u>OUTPUT\_LDI</u>

Output library number (default: 1). This argument sets the number of the output data library if an output dataset name (OUTPUT\_DS) has been set. If an output dataset name has not been specified, this argument is ignored.

#### 6.4.3.3 <u>NL\_RES\_LDI</u>

Library containing nonlinear results dataset (default: 3). This argument is used only if the number of nonlinear load steps is to be calculated automatically (*i.e.*, NSTEPS = ALL). In this case, the number of load steps is calculated based on the number of records found in the results dataset contained in the NL\_RES\_LDI library.

#### 6.4.3.4 LOAD\_SET

Load set number (default: 1). This argument selects the load set to be used as a right-hand side vector. LOAD\_SET is an active argument only if NSTEPS = 0 and END\_STEP = -1 (the default values).

#### 6.4.3.5 <u>CONS\_SET</u>

Load set number (default: 1). This argument selects the constraint set to be used in the solution of the linear system of equations. CONS\_SET is an active argument only if NSTEPS = 0 and END\_STEP = -1 (the default values).

#### 6.4.3.6 <u>NSTEPS</u>

Number of steps to be processed (default: 0). The number of load steps may be set to an integer or to the character string ALL. If NSTEPS = ALL, the number of load steps to be processed is calculated based on the information contained in the NL\_RES\_DS in library NL\_RES\_LDI. For use in linear static analyses, NSTEPS must be set to zero.

#### 6.4.3.7 BEGIN\_STEP

First load step to be processed (default: 1). This argument is active only if END\_STEP is greater than zero in which case, load steps BEGIN\_STEP through END\_STEP will be processed.

#### 6.4.3.8 END\_STEP

Last load step to be processed (default: -1). This argument is active only if it is greater than zero in which case, load steps BEGIN\_STEP through END\_STEP will be processed.

#### 6.4.3.9 <u>LD\_DIR</u>

Load direction (default: 1). This argument defines the direction in which to perform the summation. The value of LD\_DIR must be an active degree of freedom (*i.e.*, 1, 2, 3, 4, 5, or 6 and not specified as globally constrained in TAB/START).

#### 6.4.3.10 EQUIL\_CK

Flag enabling an equilibrium check (default: 0). The total load is calculated by summing the absolute value of the nodal contributions in the direction of LD\_DIR. When EQUIL\_CK is set to one (1), the absolute value is not used when performing the summation.

#### 6.4.3.11 EA

Scaling factor (default: 1.0). Frequently the total load may be normalized by the extensional stiffness or critical buckling load. The total will be divided by the scaling factor EA before being saved or written out.

#### 6.4.3.12 FAC

Scaling factor (default: 2.0). The default value of 2.0 will be used in most applications where the total load is being calculated. This is due to the use of the absolute value in the summation which essentially doubles the applied load. Frequently for finite element models with symmetry conditions imposed, the total load is only half the value of the summed reaction forces. The total load will be divided by the scaling factor FAC before being saved or written out.

#### 6.4.3.13 <u>NAME1</u>

First word of reaction force dataset name (default: STAT). This is an active argument only if INPUT\_DS = ' ' (the default value).

#### 6.4.3.14 NAME2

Second word of reaction force dataset name (default: REAC). This is an active argument only if INPUT\_DS = ' ' (the default value).

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```
*call TOTAL_LOAD ( --
    nsteps = ALL ; -- . process all load steps
    ld_dir = 3 ; -- . direction of load is 3
    name1 = 'REAC' ; -- . first word of input dataset
    name2 = 'FORC' ; -- . second word of input dataset
    output_file = 'sum_load.dat' ) . output file name
```

#### 6.4.5 LIMITATIONS

None.

#### **6.4.6 ERROR MESSAGES AND WARNINGS**

None.

#### **6.4.7 PROCEDURE FLOWCHART**

Procedure TOTAL\_LOAD is self-contained and calls no other procedures.

#### **6.4.8 PROCEDURE LISTING**

```
*procedure TOTAL_LOAD ( --
          input_ldi = 1
                              ; -- . Input library
                              ; -- . Output library
          output_ldi = 1
          nl_res_ldi = 3
                              ; -- . Library containing nonlinear results ds
                              ; -- . load set (linear only)
          load_set = 1
                              ; -- . constraint set (linear only)
          cons_set = 1
          nsteps
                      = 0
                              ; -- . number of load steps to process
          begin_step = 1
                              ; -- . first load step to process
          end_step = -1
                              ; -- . last load step to process
                              ; -- . direction of load
          ld_dir
                    = 1
                              ; -- . if = 0, total load; if = 1, check equil.
          equil_ck = 0
                              ; -- . EA (to get P/EA)
                     = 1.0
          EA
                              ; -- . divide final load
          fac
                     = 2.0
                     = 'STAT' ; -- . first word of input dataset
          name1
                     = 'REAC' ; -- . second word of input dataset
          name2
                     = ''' ''; -- . full name of input dataset
          input_ds
          output_ds = ''' ''; -- . output dataset
          nl_res_ds = 'ES*' ; -- . nonlinear results dataset name
          input_rec = 'DATA' ; -- . input dataset record key
          output_rec = 'TOTAL_LOAD'; -- . output record
          output_file = ''' ''') . output file name
 [xqt LOAD
                               outlib=[output_ldi], reslib=[nl_res_ldi]
     reset inlib=[input_ldi],
                               ncon=[cons_set]
     reset iset=[cons_set],
                                                     stop=[end_step]
     reset nsteps=[nsteps],
                                strt=[begin_step],
     reset idir=[ld_dir],
                                eqck=[equil_ck]
```

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```
reset ea=[EA], lfac=[fac]
reset n1=[name1], n2=[name2]
reset dsin=[input_ds], dsout=[output_ds], dsres=[n1_res_ds]
reset rnin=[input_rec], rnout=[output_rec]
reset outfil=[output_file]
stop
```

\*end

## 6.4.9 REFERENCES

None.

# 7.0 Utility Procedures

The procedures documented in this chapter are convenient utility procedures that are useful in many analysis tasks.

A summary of the procedures found in this chapter is provided in Table 7.0-1.

	Table 7.0-1         Utility Procedures	
Procedure Name	Utility Description	
CONSTRAIN	Impose Scaled Applied Displacements	
COPY_DS	Copy a Dataset and Rename	
EIGEN	Perform Eigenvalue Analysis	
ES	Generic Element Processor Control	
FACTOR	Factor (Decompose) System Stiffness Matrix	
FORCE	Form Force Vectors	
IMPERFECTION	Superpose Initial Geometric Imperfection	
INITIALIZE	Model initialization	
MASS	Form Mass Matrix	
MODEL_SUMMARY	Model Summary Information	
PRINT_EFIL	Print Selected Segments of EFIL Dataset	
RESEQUENCE	Resequence Nodal Equations	
SOLVE	Solve System of Equations	
STIFFNESS	Form Stiffness Matrix	
SWITCH_DS	Switch the Names of Two Datasets	

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# 7.1 Procedure CONSTRAIN

## 7.1.1 GENERAL DESCRIPTION

Procedure CONSTRAIN scales the applied motion vector. This procedure is generally used for nonlinear analyses with applied displacements.

### 7.1.2 PROCEDURE USAGE

Procedure CONSTRAIN is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call CONSTRAIN ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure CONSTRAIN are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

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For procedure CONSTRAIN, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
APPLIED_MOTION CONSTRAINT_SET	1	Name of applied motion dataset Constraint set number
DISPLACEMENT	*	Name of scaled applied motion dataset
LDI	1	Logical device index
LOAD_FACTOR	1.0	Load factor

## 7.1.3 ARGUMENT DESCRIPTIONS

## 7.1.3.1 APPLIED\_MOTION

Full dataset name of the basic applied displacements (e.g., APPL.MOTI.1.1).

## 7.1.3.2 CONSTRAINT\_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

## 7.1.3.3 DISPLACEMENT

Full dataset name of the scaled applied displacements (e.g., TOT.DISP.1).

## 7.1.3.4 LDI

Logical device index (default: 1).

## 7.1.3.5 LOAD\_FACTOR

Load factor (default: 1.0). This argument defines the load factor or scaling constant to be used to scale the basic applied motions.

## 7.1.4 USAGE GUIDELINES AND EXAMPLES

Procedure CONSTRAIN is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call CONSTRAIN ( LDI = 1 ; CONSTRAINT_SET = 1 ;
LOAD_FACTOR = 1.0 ;
APPLIED_MOTION = APPL.MOTI.1.1;
DISPLACEMENT = TOT.DISP.1 )
```

## 7.1.5 LIMITATIONS

Procedure CONSTRAIN assumes that processor VEC is executing.

## 7.1.6 ERROR MESSAGES AND WARNINGS

None.

## 7.1.7 PROCEDURE FLOWCHART

Procedure CONSTRAIN is self-contained with no subprocedures.

## 7.1.8 PROCEDURE LISTING

```
*procedure CONSTRAIN ( 1di
                             = 1
                                  ; --
                  constraint_set = 1
                                  ; --
                  load_factor
                            = 1.0 ; --
                  applied_motion
                                  ; ---
                  displacement
                                    )
  . Impose Specified Displacement Constraints (Single Point)
 *if < <spec_disp_flag> > /then
    SPECIFY [load_factor] [applied_motion] -> [displacement]
  *endif
*end
```

## 7.1.9 REFERENCES

7.1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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# 7.2 Procedure COPY\_DS

### 7.2.1 GENERAL DESCRIPTION

Procedure COPY\_DS copies a dataset in a given library to another dataset in possibly a different library. This procedure only uses directives from the command language (see reference 7.1-1).

### 7.2.2 PROCEDURE USAGE

Procedure COPY\_DS may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call COPY\_DS ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure COPY\_DS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure COPY\_DS, the following table lists each argument, its default value and meaning.

Parameter	<u>Default Value</u>	Meaning
FROM_DS		Source dataset name
TO_DS		Target dataset name
FROM_LDI	1	Source logical device index
TO_LDI	1	Target logical device index

#### 7.2.3 ARGUMENT DESCRIPTIONS

#### 7.2.3.1 FROM\_LDI

Source logical device index (default: 1).

#### 7.2.3.2 FROM\_DS

Source dataset to be copied.

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### 7.2.3.3 <u>TO\_LDI</u>

Target logical device index (default: 1).

### 7.2.3.4 TO\_DS

Target dataset for copying source dataset into.

## 7.2.4 USAGE GUIDELINES AND EXAMPLES

Procedure COPY\_DS may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

\*procedure COPY\_DS ( from\_ldi=1; from\_ds; to\_ldi=1; to\_ds )

## 7.2.5 LIMITATIONS

None.

### 7.2.6 ERROR MESSAGES AND WARNINGS

None.

## 7.2.7 PROCEDURE FLOWCHART

Procedure COPY\_DS is self contained with no subprocedures.

## 7.2.8 PROCEDURE LISTING

\*endif
\*end

## 7.2.9 REFERENCES

7.1-1 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989. THIS PAGE LEFT BLANK INTENTIONALLY.

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# 7.3 Procedure EIGEN

## 7.3.1 GENERAL DESCRIPTION

Procedure EIGEN solves a linear eigenvalue problem using an eigensolver defined by the global macrosymbol eigensolver\_name. If eigensolver\_name is EIG or EIG2, a matrix iteration procedure with subspace iteration is used as implemented in processors EIG and EIG2, respectively (see Section 9.1 of reference 7.3-1). If eigensolver\_name is defined to be LAN, a Lanczos algorithm implemented in processor LAN will be used (see Section 9.2 of reference 7.3-1). If eigensolver\_name is defined to be LANZ, the alternate Lanczos method implemented in processor LANZ will be used (see Section 9.3 of reference 7.3-1).

## 7.3.2 PROCEDURE USAGE

Procedure EIGEN is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call EIGEN ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure EIGEN are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
CONSTRAINT_SET	1	Constraint set number
LDI	1	Logical device index
LOAD_SET	1	Load set number
KNAME	K	First word of the name of the dataset containing the assembled stiffness matrix.
PROBLEM_TYPE	'BUCK'	Define problem type for either buckling or vibration.
MASS_TYPE	'CONSISTENT'	Form of mass matrix (consistent or diagonal)
ERROR_TOL	1.0E-4	Error tolerance for eigenvalue convergence
N_MODES	1	Number of converged eigenmodes desired
INIT_VECTORS	0	Number of iteration vectors
SHIFT	0.0	Eigenvalue shift
MAX_ITERS	20	Maximum number of iterations

For procedure EIGEN, the following table lists each argument, its default value and meaning.

Tables 7.3-1 and 7.3-2 list the datasets used or created by procedure EIGEN and the processors invoked by procedure EIGEN, respectively.

Table 7.3-1 Datasets Input/Output by procedure EIGEN				
Dataset	Description		Output	
AMAPic2.isize	Factorization Map for INV	$\checkmark$		
CONj	Constraints	$\checkmark$		
INV. <kname>.j</kname>	Factored Stiffness Matrix	$\checkmark$		
JDF1.BTAB.1.8	Model Summary	$\checkmark$		
JSEQ.BTAB.2.17	Nodal Elimination Sequence	$\checkmark$		
KMAPnsubs.ksize	Model Connectivity Map	$\checkmark$		
<kname>.SPAR.jdf2</kname>	Assembled Stiffness Matrix	$\checkmark$		
<kgname>.SPAR.jdf2</kgname>	Assembled Geometric Stiffness Matrix	$\checkmark$		
<mname>.SPAR.jdf2</mname>	Assembled Consistent Mass Matrix	$\checkmark$		
VIBR.MODE. <i>i.j</i> †	Vibration eigenmodes	·	$\checkmark$	
VIBR.EVAL. <i>i.j</i> <sup>†</sup>	Vibration eigenvalues		$\checkmark$	
BUCK.MODE.i.j <sup>†</sup>	Buckling eigenmodes		$\checkmark$	
BUCK.EVAL. <i>i.j</i> †	Buckling eigenvalues		$\checkmark$	

 $\dagger i = \langle \text{load\_set} \rangle \text{ and } j = \langle \text{cons\_set} \rangle$ 

Table 7.3-2         Processors Invoked by procedure EIGEN		
Procedure	Туре	Function
EIG/EIG2	Internal	Solves eigenproblem using subspace iteration
LAN	External	Solves eigenproblem uing Lanczos method
LANZ	External	Solves eigenproblem using Lanczos method
GETK	Internal	Converts nodal block matrix format to compact sparse for- mat

## 7.3.3 ARGUMENT DESCRIPTIONS

#### 7.3.3.1 PROBLEM\_TYPE

Defines problem type (default: 'BUCK'). This argument selects the type of eigenproblem to solve either buckling (BUCK) or vibration (VIBR).

#### 7.3.3.2 ECON\_SET

Constraint set number for eigenproblem (default: 1). This argument selects which constraint set to be used in solving the eigenproblem which may be different from that used for determining the prestress state.

#### 7.3.3.3 LDI

Logical device index (default: 1).

#### 7.3.3.4 LOAD\_SET

Load set number (default: 1). This argument selects which load set to be used as a right-hand side vector.

#### 7.3.3.5 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

#### 7.3.3.6 KGNAME

First word of the dataset name containing the assembled geometric stiffness matrix (de-fault: KG).

#### 7.3.3.7 MNAME

First word of the dataset name containing the assembled mass matrix (default: CEM).

#### 7.3.3.8 MASS\_TYPE

Form of mass matrix (default: 'CONSISTENT'. This argument defines the form of the mass matrix to be either consistent or diagonal.

#### 7.3.3.9 <u>ERROR\_TOL</u>

Error tolerance for convergence of eigenvalues (default: 1.0E-4).

### 7.3.3.10 <u>N\_MODES</u>

Number of converged eigenmodes desired (default: 1).

Number of initial iteration vectors (default: 0). If the default value is used, then the number of initial iteration vectors will be the minimum of <2\*  $<N_MODES>>$  and  $<<N_MODES>+8>$ .

### 7.3.3.12 SHIFT

Eigenvalue shift (default: 0.0).

### 7.3.3.13 <u>MAX\_ITER</u>

Maximum number of iterations in solving the eigenproblem (default: 20).

### 7.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure EIGEN is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis.

\*call EIGEN ( KNAME = K ; ECON\_SET = 1 ; LOAD\_SET = 1 ; KGNAME = KG )

Before procedure EIGEN is called the global macrosymbol eigensolver\_name should be defined as described in Section 7.3.1 and should be consistent with the value used when procedure FACTOR was called. If it is not specified, then the default value EIG2 will be used.

### 7.3.5 LIMITATIONS

None.

### 7.3.6 ERROR MESSAGES AND WARNINGS

None.

# 7.3.7 PROCEDURE FLOWCHART

Procedure EIGEN is self-contained with no subprocedures.

# 7.3.8 PROCEDURE LISTING

```
*procedure EIGEN ( PROBLEM_TYPE = 'BUCK' ; -- . Problem type: BUCK or VIBR
                 ldi = 1 ; -- . library number
                 kname = 'K' ; -- . First name of material stiffness matrix
                 kgname = 'KG' ; -- . First name of geometric stiffness matrix
                 mname = 'CEN' ; -- . First name of mass matrix
                 error_tol = 1.0e-4 ; -- . Error tolerance on eigenevalues
                 load_set = 1 ; -- . Load set number
                 mass_type = 'CONSISTENT' ; -- . Form of mass matrix
                 N_modes = 1; -- . Number of modes desired
                 INIT_vectors = 0 ; -- . Number of initial vectors
                 SHIFT =0.0 ; -- . Eigenvalue shift
                 max_iters = 20 ; -- . Maximum number of iterations
                 econ_set = 1 ) . Constraint set for eigenproblem
. Procedure to solve the eigenvalue problem using different
. eigensolvers. The eigensolver is selected using the
. global macrosymbol "eigensolver_name".
      _____
  Perform Eigenvalue Analysis (with [kname].SPAR and [kgname].SPAR)
   *if < [INIT_vectors] /eq 0 > /then
    *def/i N_vectors = < MIN( 2*[N_modes]; [N_modes]+8) >
    *else
    *def/i N_vectors = [INIT_vectors]
   *endif
   _____
  Select eigensolver
  -----
  Use processor EIG
*if < ifeqs(<eigensolver_name>;EIG) > /then
   *def NS_OVERWRITE = <false>
   [XOT EIG
   RESET PROB=[PROBLEM_TYPE]
   RESET INIT=<N_vectors>, SHIPT=[shift], NREQ=[N_modes]
   RESET CONV=[error_tol], NDYN=[max_iters], con=[econ_set],NEWSET=[load_set]
   RESET K=[kname]
   RESET KG=[kgname]
   RESET M=[mname]
   RESET KLIB=[LDI], KILIB=[LDI], KGLIB=[LDI], MLIB=[LDI], OUTLIB=[LDI]
   RESET INLIB=[LDI],OLDSET=[LDI]
   STOP
  Use processor EIG2
```

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```
*elseif < ifeqs(<eigensolver_name>;EIG2) > /then
   *def NS_OVERWRITE = <false>
   INT EIG2
  RESET PROB=[PROBLEM_TYPE]
  RESET INIT=<N_vectors>, SHIFT=[shift], NREQ=[N_modes]
  RESET CONV=[error_tol], NDYN=[max_iters], con=[econ_set],NEWSET=[load_set]
  RESET K=[kname]
  RESET KG=[kgname]
  RESET M=[mname]
  RESET KLIB=[LDI],KILIB=[LDI],KGLIB=[LDI],MLIB=[LDI],OUTLIB=[LDI]
  RESET INLIB=[LDI],OLDSET=[LDI]
  STOP
*elseif < ifeqs(<eigensolver_name>;LAN) > /then
  Use processor LAN
   *def NS_OVERWRITE = <false>
   [xat LAN
     RESET PROB=[PROBLEM_TYPE],LDI=[LDI]
     RESET KNAM=[kname],KGNA=[kgname],MNAM=[mname]
     RESET NK=[max_iters], shift=[shift], ncon=[econ_set]
     STOP
*elseif < ifeqs(<eigensolver_name>;LANZ) > /then
   *def NS_OVERWRITE = <false>
 #if < ifeqs([PROBLEM_TYPE];BUCK) > /then
   [xqt GETK
     reset sipr=0, form=2, save=1
     reset k=k, redo=0, kred=k, reac=0
   [xqt GETK
     reset sipr=0, form=2, save=1
     reset k=kg, redo=1, kred=k, reac=0
   [xqt LANZ
  RESET PROB=2, plvl=3, check=1, con=[econ_set]
  RESET nreq=[N_modes], conv=[error_tol]
   RESET kg=[kgname]
 *elseif < ifeqs([PROBLEM_TYPE];VIBR) > /then
   [xqt GETK
     reset sipr=0, form=2, save=1
     reset k=k, redo=0, kred=k, reac=0
   *if < ifeqs([mass_type];CONSISTENT) > /then
   *def/i mcase=1
   [xqt GETK
     reset sipr=0, form=2, save=1
     reset k=[mname], redo=1, kred=k, reac=0
   *01 50
   *def/i mcase=0
   *endif
   [xqt LANZ
   RESET mcase=<mcase>, plvl=3,check=1,con=[econ_set]
   RESET nreq=[N_modes], conv=[error_tol]
   RESET ==[mname]
 *endif
```

\*endif

\*end

# 7.3.9 REFERENCES

7.3-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.4 Procedure ES

# 7.4.1 GENERAL DESCRIPTION

Procedure ES is a high-level procedure that controls the structural element processors (ESi). The Generic Element Processor (GEP) provides a *template* with which many individual finite-element processors may be developed and coexist as independent modules in the CSM Testbed (see ref. 7.4-1). The GEP template for *structural* elements is referred to as ES, and all element processors built with this template have names that begin with ES (*e.g.*, ES1, ES2, ...). Each of these ESi processors performs all operations for all of the elements implemented within the processor — including element definition, stiffness, force, mass (etc.) generation, and various pre/post-processing functions.\*

Since ESi processors are typically built by different developers, you might expect a wide variety of User-interface characteristics. However, because of the generic template employed, all ESi processors share the same command language and global datasets. This means that once the user has learned to invoke one ESi processor, the user has learned them all.

The main difference between ESi processors will be in the specific elements implemented within them. Some ESi processors may have only one element type inside. Others may have a family of elements of a certain class (e.g., 4-, 9- and 16-node shell elements). Still others may embed an entire library of structural elements, containing various members of each class (e.g., beam, shell, solid). Each of these specific element types is given a corresponding name within each ESi processor; so that the combination of ESi processor name and element type is unique. Thus, to employ a particular ESi processor correctly, the user will have to consult specific documentation on the individual elements contained within that processor. Such documentation is provided in the CSM Testbed User's Manual (see ref. 7.4-2).

In the following sections, the generic features of ESi processors are described in detail.

<sup>\*</sup> Exception: Element connectivity for all element processors is currently performed by Testbed processor ELD.

The description includes ESi processor commands and macrosymbols, and the datasets required or produced by these commands (Section 2.2), the high-level procedure interface, which makes it possible to write analysis procedures that invoke a single, generic procedure (called ES) to generate element arrays automatically for all ESi processors required in a given problem; a glossary of ES macrosymbols, which gives more detailed definitions for the macrosymbols and procedure arguments; and some explicit examples of how to use ESi processors, interactively, or using the procedure ES interface.

# 7.4.2 PROCEDURE USAGE

Procedure ES may be invoked by the \*call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are orderindependent, and most have default values thus making them optional. The formal syntax is as follows:

\*call ES ( arg1 = val1; arg2 = val2; ...)

where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure ES; note that those arguments without default values are mandatory, while the others are optional.

Argument	Default_Value	Meaning
ES_NAME		Element-type name
ES_NL_GEOM		Geometric nonlinearity
ES_NL_MATL		Material nonlinearity
ES_NL_LOAD	·	Load nonlinearity
ES_PARS		Research parameters
ES_PROC		Processor name
FUNCTION		Processor command
 ES_CORO	1	Corotational option
ES_COUNT	0	Create or accumulate ES.SUMMARY
ES_DIS_DS	STAT.DISP.1.1	Displacement dataset
ES_DOF_DS	ES.DOFS	Active-freedom dataset
ES_ECC_DS	WALL.PROP	Eccentricity dataset
ES_FRC_DS	INT.FORC.1.1	Force vector dataset
ES_ROT_DS	STAT_ROTA.1.1	Rotation vector dataset
ES_STR_LOC	CENTROIDS	Stress locations
ES_STR_DIR	0	Stress directions
ES_STRAIN_DS	٢,	Element strain dataset
ES_STRESS_DS	( )	Element stress dataset
ES_SUM_DS	ES. SUMMARY	ES summary dataset
LDI	1	Logical device index
NUM_CON_DS	1	Number of constraint datasets

Table 7.4-1         Datasets Input/Output by Procedure ES				
Dataset	Description	Lib	Input	Output
ES.SUMMARY	ES Processor Status	1		$\checkmark$
ES.DOFS	1			$\checkmark$
<es_name>.EFIL.0.nnod</es_name>	Element Computational Data	1		$\checkmark$
DIR. <es_name>.0.nnod</es_name>	Element EFIL Directory	1	$\checkmark$	
DEF. <es_name>.0.nnod</es_name>	Element Definition (Connectivity)	1	$\checkmark$	
PROP.BTAB.2.*	Material/Section Properties	1	$\checkmark$	
STAT.DISP.i.j	System Displacement Vector	1	$\checkmark$	
STAT.ROTA.i.j	System Rotation Vector	1	$\checkmark$	
QJJT.BTAB.	Nodal Transformations	1	$\checkmark$	
INT.FORC.i.j	System Internal Force Vector	1		$\checkmark$
DEM.DIAG	Diagonal (Lumped) Mass Matrix	1		$\checkmark$
CEM.SPAR.jdf2	Assembled Consistent Mass Matrix	1		$\checkmark$
STRN. <es_name>.</es_name>	Element Strains	1		$\checkmark$
<es_strain_ds></es_strain_ds>				
STRS. <es_name>.</es_name>	Element Stresses	1		$\checkmark$
<es_stress_ds></es_stress_ds>				
K.SPAR.jdf2	Assembled material stiffness matrix	1		$\checkmark$
KG.SPAR.jdf2	Assembled geometric stiffness matrix	1		$\checkmark$

 $\dagger$  i = <load\_set> and j = <cons\_set>

Table 7.4-2 Sub-Procedures Invoked by Procedure ES					
Procedure	Type	Function			
ES	Internal	Main procedure			
ES_DOFS	Internal	Automatic DOF Suppression for ESi			

Table 7.4-3 Sub-Procedures Invoked by Procedure ES				
Processor	Туре	Function		
ESi	External	Various element processors		
7	-	Vector functions		

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Macrosymbol	Туре	Definition
<u>ES_C</u>	I	Continuity of interelement "displacement" field, e.g., $0 \Rightarrow C^0$ (displacement continuity only) $1 \Rightarrow C^1$ (displacement and slope continuity)
ES_CLAS	A	Element class. Currently valid classes: BEAM, SHELL, SOLID, WILD (See Section 3.4 for examples.)
ES_CNS	I	Constitutive interface option (see Chapter 5).
		$0 \Rightarrow$ elements use the standard constitutive interface for stress and tangent-modulus calculations; $1 \Rightarrow$ elements compute their own stresses, but use standar constitutive interface for tangent-modulus calculations; $\geq 2 \Rightarrow$ elements compute their own stresses and tangent moduli; standard constitutive interface is not used.
ES_CORO	I	Corotation switch; employed by ES processor for automatic treatment of geometric nonlinearity due to large rotations. Relevant only if problem is geometrically non- linear. (See Chapter 4 for an explanation of these options.) $0 \Rightarrow \text{Off: corotational operations will be skipped;}$ $1 \Rightarrow \text{Low-Order Option: basic corotational transformations will be employed to enable large rotations;}$ $2 \Rightarrow \text{High-Order Option: a more accurate (and expensive treatment of large rotations and consistent linearization than option 1 will be employed.}$
ES_COUNT	I	Element processor count. Relevant only for DEFINE EI EMENTS command. $0 \Rightarrow$ First element processor to be defined; creat ES.SUMMARY dataset. $> 0 \Rightarrow$ Not first element processor to be defined; use ex- isting ES.SUMMARY dataset and Increment element pro- cessor number by one.
ES_DIM	I	Number of intrinsic element spatial dimensions, e.g., 1 if ES_CLAS = BEAM 2 if ES_CLAS = SHELL 2 or 3 if ES_CLAS = SOLID

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Macrosymbol	Туре	Definition
ES_DIS_DS	A	Name of system displacement-vector dataset (SYSVE( format). Relevant for most FORM commands and som POST commands. (Default: STAT.DISP.1.1)
ES_DOF_DS	A	Name of element freedom-table dataset (SYSVEC for mat). Relevant only for DEFINE FREEDOMS com mand. When using procedure ES, this dataset will au tomatically be created, initialized, and updated cumu latively with contributions from all pertinent ES pro cessors. (Default: ES.DOFS)
ES_ECC_DS	A	First two words of dataset name that contains section property data including reference surface eccentricities (Default: WALL.PROP).
ES_EXPE_CMD	A	Complete EXPE command line appropriate for defin- ing elements with processor ELD. This macrosymbol is constructed only in response to a call to procedure ES with FUNCTION='DEFINE ELEMENTS'.
ES_FRC_DS	A	Name of system force-vector dataset (SYSVEC format) where element distributed forces (internal and/or ex- ternal) are to be assembled. Relevant only for FORM FORCE command, in which case this vector must be created and initialized before issuing the command (or calling procedure ES). Contributions from all pertinent ES processors will be assembled into this vector if proce- dure ES is called with argument FUNCTION = 'FORM FORCE'. (Default: INT.FORC.1.1)
ES_LOAD_FACTOR	F	Load factor. (Default: 1.0)
ES_LOAD_SET	I	Load set number. (Default: 1)

Macrosymbol	Type	Definition
ES_MASS_DIAG	A	First word of the dataset name for a diagonal mass matrix. (Default: DEM).
ES_MASS_DS	A	First two words of the dataset name for a diagonal mass matrix. (Default: <es_mass_diag>.DIAG).</es_mass_diag>
ES_NAME	A	Name of element type, within current ES processor, to be processed by subsequent commands. (For example EX97 would be a valid element-type name within pro- cessor ES1.)
<u>ES_NDOF</u>	I	Number of freedoms per element node.Currently valid options (2, 3 or 6), e.g., $2$ for 2-D solid elements $(u, v)$ $3$ for 3-D solid elements $(u, v, w)$
		6 for beam, plate or shell elements $(u, v, w, \theta_x, \theta_y, \theta_z)$
ES_NEE	I	Number of element equations; = $ES_NEN \times ES_NDOF$ .
ES_NEN	I	Number of element nodes.
<u>ES_NIP</u>	I	Number of element integration points; <i>i.e.</i> , points at which stresses (continuum or resultants, depending on element type) are stored.
ES_NL_GEOM	I	Geometric nonlinearity switch; $0 \Rightarrow \text{Off: problem is geometrically linear (small displacements/rotations);}$
		$1 \Rightarrow$ Low-Order Option: problem is geometrically non- linear, but elements should use linear strain-displacement relations. Meaningful only if ES_CORO > 0, so that large rotations can be handled automatically by the corota- tional algorithm;

Macrosymbol	Туре	Definition
		$2 \Rightarrow$ High-Order Option: problem is geometrically non- linear and elements should use nonlinear element strain- displacement relations. May be used in conjunction with ES_CORO > 0 to obtain higher-order accuracy for beam and shell elements that employ moderate-rotation strain- displacement relations;
		$3 \Rightarrow$ same as 2 plus finite strains are expected.
ES_NL_LOAD	I	Load nonlinearity switch; $1 \Rightarrow$ process displacement-dependent element loads only; $0 \Rightarrow$ process displacement-independent element loads only.
ES_NL_MATL	I	Material nonlinearity switch; $1 \Rightarrow$ element is materially nonlinear; $0 \Rightarrow$ element materially linear.
<u>ES_NORO</u>	I	Element normal-rotation parameter. Relevant only for au- tomatic freedom suppression of plate/shell elements. In- dicates minimum angle (in degrees) between shell element normal vector and any computational basis vector — at each element node — below which the corresponding rota- tional freedom should be suppressed if no other elements are attached;
	· .	$=0 \Rightarrow$ Element has normal-rotation ("drilling") stiffness; normal rotational freedoms will automatically be sup- pressed.
		$>0 \Rightarrow$ Element does not have normal-rotation ("drilling") stiffness; it is assumed that rotational stiffness exists about any computational axis that makes an angle of at least <es_noro> degrees with the element normal vec- tor at an element node.</es_noro>

Macrosymbol	Туре	Definition
ES_NPAR	I	Number of element research parameters in array ES_PARS
<u>ES_NSTR</u>	I	Number of stress components per integration point. Cur- rently valid options compatible with standard constitutive interface: 8 for ES_CLAS = SHELL and ES_C = 0; 6 for ES_CLAS = SOLID and ES_DIM = 3; 6 for ES_CLAS = SHELL and ES_C = 1; 6 for ES_CLAS = BEAM and ES_C = 0; 4 for ES_CLAS = BEAM and ES_C = 1; 3 for ES_CLAS = SOLID and ES_DIM = 2.
ES_OPT	I	Element-type option number. Meaningful only to the ele- ment developer; it is the developer's numerical equivalent of ES_NAME.
ES_PARS	D	Array of element research parameters. Meaning depends on specific element type. (Consult appropriate section in CSM Testbed User's Manual, ref. 4).
ES_PROC	A	Name of element (ES) processor to be executed (e.g., ES1, ES2,); currently relevant only as an argument for procedure ES, and only when argument FUNCTION = 'DE-FINE ELEMENTS'.

Macrosymbol	Type	Definition
ES_PROJ	I	Rigid-body projection option. Used to automatically re- move (most of) the spurious energy generated by some elements during infinitesimal rigid-body motion. This is performed by operating on the element stiffness and force arrays with a projection matrix (or projector). The pro- jector, and its derivative, can have a beneficial effect on element accuracy in both linear and geometrically nonlin- ear regimes. $0 \Rightarrow Off:$ projection will be omitted; $1 \Rightarrow Low-order Option:$ basic projection will be included; $2 \Rightarrow$ High-order Option: basic projection plus a differential
		correction to the geometric stiffness will be included.
ES_ROT_DS	<b>A</b> .	Name of system rotation pseudo-vector dataset (SYSVEC format). Relevant for most FORM commands dur- ing geometrically nonlinear analysis, but only if ele- ments with rotational freedoms are involved. (Default: STAT.ROTA.1.1)
ES_SHAP	A	Shape of element surface used to define coordinate triad; currently recognized options: LINE, TRIA or QUAD.
ES_STOR	I	Number of "private" variables to be stored/retrieved for the element developer in dataset EFIL. <es_name>.</es_name>
ES_STR_DIR	I	Element stress/strain direction option. Indicates in which coordinate system element stresses or strains in datasets defined by <es_stress_ds> or <es_strain_ds> (respectively) will be computed. Relevant only for com- mand = 'FORM STRAIN' or 'FORM STRESS'. Valid options: <math>0 \Rightarrow</math> element stress coordinate system <math>1 \Rightarrow</math> material axes <math>\{x_m, y_m, z_m\} = \{x_g, y_g, z_g\}</math> <math>2 \Rightarrow</math> material axes <math>\{y_m, z_m, x_m\} = \{y_g, z_g, x_g\}</math> <math>3 \Rightarrow</math> material axes <math>\{z_m, x_m, y_m\} = \{z_g, x_g, y_g\}</math> (Note: For isotropic materials, the first material axis is replaced by the corresponding global axis; see the SREF command under processor ELD in the Testbed User's</es_strain_ds></es_stress_ds>

Macrosymbol	Туре	Definition
ES_STR_LOC	A	Element stress/strain evaluation point option. Indicates where stresses or strains in datasets defined by <es_stress_ds> or <es_strain_ds> (respectively) will be computed. Relevant only for command = 'FORM STRAIN' or 'FORM STRESS'. Currently valid options: CENTROIDS ⇒ element centroids; creates record group: CENTROIDS ⇒ element centroids; creates record group: NODES ⇒ element nodes; creates record group: NODES_<es_str_dir>.1:nel INTEG_POINTS ⇒ element integration points; creates: INTEG_PTS_<es_str_dir>.1:nel where "nel" is the number of elements in the dataset and where macrosymbol ES_STR_DIR designates the di rections of the stress/strain components, and is defined elsewhere in this Glossary. (Default: 'CENTROIDS')</es_str_dir></es_str_dir></es_strain_ds></es_stress_ds>
ES_STRAIN_DS	A	Third part of element strain dataset name. The first name is always STRN; the second name is always the element-type name, <i>i.e.</i> , <es_name>; and the third name, <es_strain_ds> must be a string of integers separated by periods. For example, if <es_strain_ds> = <step>.<iter> where <step> = 20 and <iter> = 3, and if the element type name were EX97, then the full dataset name would be: STRN.EX97.20.3 Relevant only for command = 'FORM STRAIN'. (No default; absence means that strains will be stored (embedded) within dataset EFIL.<es_name> only - currently not implemented.)</es_name></iter></step></iter></step></es_strain_ds></es_strain_ds></es_name>

Macrosymbol	Туре	Definition
ES_STRESS_DS	A	Third part of element stress dataset name. The first name is always STRS; the second name is always the element-type name, <i>i.e.</i> , $\langle \text{ES_NAME} \rangle$ ; and the third name, $\langle \text{ES_STRESS_DS} \rangle$ must be a string of integers separated by periods. For example, if $\langle \text{ES_STRESS_DS} \rangle$ = $\langle \text{step} \rangle$ . $\langle \text{iter} \rangle$ , where $\langle \text{step} \rangle = 20$ and $\langle \text{iter} \rangle = 3$ , and if the element- type name were EX97, then the full dataset name would be: STRS.EX97.20.3 Relevant only for command = 'FORM STRESS'. (No default; absence means that stresses will be stored (embedded) within dataset EFIL. $\langle \text{ES_NAME} \rangle$ only.)
ES_SUM_DS	A	Name of ES summary dataset, which contains nominal records corresponding to most of the macrosymbol pa- rameters appearing in this Glossary — for each ES pro- cessor/element defined in the model. Relevant for all ES commands. (Default: ES.SUMMARY)
<u>ES_TWIS</u>	I	Sign of twisting curvature for shell elements.         +1 ⇒twist based on continuum definition of shear strain;         -1 ⇒twist based on negative of continuum definition.         (Note: The default convention for constitutive matrices output from processor LAU corresponds to the -1 option. Hence processor ES compensates for this reversal if ES_TWIS = +1.)
ES_TGC_DS	I	Name of nodal transformation dataset (QJJT.BTAB.*.*)
ES_XYZ_DS	I	Name of nodal coordinate dataset (JLOC.BTAB.*.*)
LDI	I	Logical device index or library number for archiving and retrieving data. (Default: 1)

# 7.4.3 ARGUMENT DESCRIPTION

### 7.4.3.1 ES\_CORO

Corotation switch; employed by ESi processors for automatic treatment of geometric nonlinearity due to large rotations. Relevant only if problem is geometrically nonlinear. (See Chapter 4 of reference 7.4-1 for an explanation of these options.) If ES\_CORO equals zero, then the corotational operations will be skipped. If ES\_CORO equals one (low-order option), then the basic corotational transformations will be employed to enable large rotations. If ES\_CORO equals two (high-order option), then a more accurate (and expensive) treatment of large rotations and consistent linearization than option 1 will be employed.

### 7.4.3.2 ES\_COUNT

Element processor count (default: 0). This argument is used to create and/or accumulate data in the ES.SUMMARY dataset for finite element models using multiple element processors.

# 7.4.3.3 <u>ES\_DIS\_DS</u>

Name of system displacement-vector dataset in SYSVEC format (default: STAT.DISP.1.1). Relevant for most FORM commands.

# 7.4.3.4 ES\_DOF\_DS

Name of element freedom-table dataset (SYSVEC format). Relevant only for DEFINE FREE-DOMS command. When using procedure ES, this dataset will automatically be created, initialized, and updated cumulatively with contributions from all pertinent ESi processors. (Default: ES.DOFS)

### 7.4.3.5 <u>ES\_ECC\_DS</u>

Name of element section property eccentricity dataset (default: WALL.PROP). Relevant for all FORM commands.

## 7.4.3.6 ES\_FRC\_DS

Name of system force-vector dataset in SYSVEC format, where element distributed forces (internal and/or external) are to be assembled (default: STAT.REAC.1.1). Relevant only for FORM FORCE command, in which case this vector must be created and initialized before issuing the command (or calling procedure ES). Contributions from all pertinent ESi processors will be assembled into this vector if procedure ES is called with argument FUNCTION = 'FORM FORCE.

# 7.4.3.7 ES\_NAME

Name of element type, within current ESi processor, to be processed by subsequent commands. (For example, EX97 would be a valid element-type name within processor ES1.)

# 7.4.3.8 ES\_NL\_GEOM

Geometric nonlinearity switch. If ES\_NL\_GEOM equals zero (no corotational frames), then the problem is geometrically linear (small displacements/rotations). If ES\_NL\_GEOM equals one (low-order option), then the problem is geometrically nonlinear, but elements should use linear strain-displacement relations. Meaningful only if ES\_CORO > 0, so that large rotations can be handled automatically by the corotational algorithm. If ES\_NL\_GEOM equals two (high-order option), then the problem is geometrically nonlinear and elements should use *nonlinear* element strain-displacement relations. May be used in conjunction with ES\_CORO > 0 to obtain higher-order accuracy for beam and shell elements that employ moderate-rotation strain-displacement relations.

# 7.4.3.9 <u>ES\_NL\_MATL</u>

Material nonlinearity switch. If ES\_NL\_MATL is greater than zero, then the element is materially nonlinear. If ES\_NL\_MATL is zero, then the element is materially linear.

# 7.4.3.10 ES\_NL\_LOAD

Load nonlinearity switch. If ES\_NL\_LOAD is greater than zero, then the element loads are displacement dependent. If ES\_NL\_LOAD equals zero, then the element loads are not displacement dependent.

# 7.4.3.11 ES\_PARS

Array of element research parameters. Meaning depends on specific element type. Consult appropriate section in CSM Testbed User's Manual, ref. 7.4-2.

7.4.3.12 ES\_PROC

Name of element (ES)*i* processor to be executed (*e.g.*, ES1, ES2, ...); currently relevant only as an argument for procedure ES, and only when argument FUNCTION = 'DEFINE ELEMENTS'.

# 7.4.3.13 <u>ES\_ROT\_DS</u>

Name of system rotation pseudo-vector dataset in SYSVEC format (default: STAT.ROTA.1.1). Relevant for most FORM commands during *geometrically nonlinear* analysis; but only if elements with rotational freedoms are involved.

# 7.4.3.14 ES\_STR\_LOC

Element stress/strain location option (default: 'CENTROIDS'). Indicates where stresses or strains in datasets defined by <ES\_STRESS\_DS> or <ES\_STRAIN\_DS> (respectively) will be computed. Relevant only for FUNCTION = 'FORM STRAIN' or 'FORM STRESS'. Currently valid options:

- CENTROIDS ⇒ element centroids; creates record group: CENTROIDS\_<ES\_STR\_DIR>.1:nel
- NODES ⇒ element nodes; creates record group:
   NODES\_<ES\_STR\_DIR>.1:nel
- INTEG\_POINTS ⇒ element integration points; creates: INTEG\_PTS\_<ES\_STR\_DIR>.1:nel

where "nol" is the number of elements in the dataset, and where macrosymbol ES\_STR\_DIR designates the directions of the stress/strain components, and is defined elsewhere in this glossary.

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### 7.4.3.15 <u>ES\_STR\_DIR</u>

Element stress/strain direction option (default: E). Indicates in which coordinate system element stresses or strains in datasets defined by  $\langle ES\_STRESS\_DS \rangle$  or  $\langle ES\_STRAIN\_DS \rangle$  (respectively) will be computed. Relevant only for FUNCTION = 'FORM STRAIN' or 'FORM STRESS'. Currently valid options include E for the element stress coordinate system, M for the material coordinate system, and Gi for the coordinate system whose x axis corresponds to global coordinate axis  $x_i$ .

### 7.4.3.16 ES\_STRAIN\_DS

Third part of element strain dataset name. The first name is always STRN; the second name is always the element-type name, *i.e.*, <ES\_NAME>; and the third name, <ES\_STRAIN\_DS> must be a string of integers separated by periods (see CSM Testbed Data Library Description, reference 7.4-3). For example, if <ES\_STRAIN\_DS> = <step>.<iter> where <step> = 20 and <iter> = 3, and if the element-type name were EX97, then the full dataset name would be: STRN.EX97.20.3. Relevant only for FUNCTION = 'FORM STRAIN'. No default; absence means that strains will be stored (embedded) within dataset EFIL.<ES\_NAME> only — currently not implemented.

# 7.4.3.17 ES\_STRESS\_DS

Third part of element stress dataset name. The first name is always STRS; the second name is always the element-type name, *i.e.*, <ES\_NAME>; and the third name, <ES\_STRESS\_DS> must be a string of integers separated by periods same as previously stated. For example, if <ES\_STRESS\_DS> = <step>.<iter>, where <step> = 20 and <iter> = 3, and if the element-type name were EX97, then the full dataset name would be: STRS.EX97.20.3. Relevant only for FUNCTION = 'FORM STRESS'. No default; absence means that stresses will be stored (embedded) within dataset EFIL.<ES\_NAME> only.

### 7.4.3.18 <u>ES\_SUM\_DS</u>

Name of ES summary dataset, which contains nominal records corresponding to most of the macrosymbol parameters appearing in this glossary — for each ESi processor/element defined in the model (default: ES.SUMMARY). Relevant for all ES commands.

# 7.4.3.19 FUNCTION

All structural element (ESi) processors based on the generic element processor template, share the same processor commands. This makes it easier for the User, and enables the construction of a generic command procedure to handle any combination of ESi processors. The commands recognized by ESi processors fall into three categories: INITIALIZE, DEFINE, and FORM, which roughly correspond to preprocessing and computation phases of analysis. The INITIALIZE command initializes the element data. The DEFINE commands are used to prepare or re-format model definition datasets, such as element connectivity, freedom activity, loads, etc.\* The FORM commands are used to form element computational data, such as stiffness matrices, force vectors, etc. Table 7.4-5 provides a summary of ES processor commands and their respective functions.

<sup>\*</sup> Again, element connectivity is currently performed using Testbed processor ELD.

Table 7.4-5         Summary of Generic ES Processor Commands					
	Command	Description			
INITIALI	ZE	Initialize element data			
DEFINE	ELEMENTS	Define element parameters			
	FREEDOMS	Perform automatic DOF			
		suppression			
FORM	STIFFNESS [/MATL/GEOM/LOAD/TANG]	Form element stiffness			
	FORCE [/INT/EXT/RES/DYN]	Form element force			
	MASS [/CONS/DIAG]	Form element mass			
	STRAIN	Form element strains			
	STRESS	Form element stress			

In addition to these commands, ESi processors can be controlled with a number of built-in *macrosymbols*, all of which begin with ES\_. The macrosymbols typically set logical switches and/or control parameters, and allow re-assignment of database names from their default values.

Table 7.4-6 ANALYSIS/COMMAND CORRESPONDENCE						
ES Processor Commands vs Analysis Type						
Analysis Type Processor Commands						
All Preprocessing	INITIALIZE					
	DEFINE ELEMENTS					
	DEFINE FREEDOMS					
Linear Statics	FORM STIFFNESS/MATL					
	FORM FORCE/EXT					
Linear Dynamics	FORM STIFFNESS/MATL					
	FORM MASS/CONS					
	FORM FORCE/EXT					
Buckling Eigenvalue	FORM STIFFNESS/MATL					
	FORM STIFFNESS/GEOM					
	FORM FORCE/EXT					
Vibration Eigenvalue	FORM STIFFNESS/MATL					
	FORM MASS/{CONS   DIAG}					
Nonlinear Statics	FORM STIFFNESS/TANG					
	FORM FORCE/INT					
	FORM FORCE/EXT					
	FORM FORCE/RES					
Nonlinear Dynamics	FORM STIFFNESS/TANG					
	FORM MASS/{CONS   DIAG}					
	FORM FORCE/INT					
	FORM FORCE/EXT					
	FORM FORCE/DYN					

### 7.4.4 PROCEDURE FLOWCHART

ËS	(main procedure)
ES_DOFS	(automatic DOF suppression for $ESi$ )

### 7.4.5 LIMITATIONS

Procedure ES assumes that all datasets either required or generated will reside on library one (LDI=1).

### 7.4.6 ERROR MESSAGES AND WARNINGS

None.

### 7.4.7 USAGE GUIDELINES AND EXAMPLES

Procedure ES may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis.

*call ES (	FUNCTION	#		;	 Processor command
	ES_PROC	=		;	 . Processor name
	ES_NAME	=		;	 . Element-type name
	ES_PARS	=	0.0	;	 . Research parameters
	ES_CORO	z	1	;	 . Corotational option
	ES_NL_GEOM	Ξ	<false></false>	;	 . Geom. nonlinearity
	ES_NL_MATL	=	<false></false>	;	 . Matl. nonlinearity
	ES_NL_LOAD	=	<false></false>	;	 . Load nonlinearity
	ES_DIS_DS	z	STAT.DISP	;	 . Displacement dataset

ES_DOF_DS =	ES.DOFS	; Active-freedom dataset
ES_ECC_DS =	ES.ECCEN	; Eccentricity dataset
ES_FRC_DS =	STAT.REAC	; Force-vector dataset
ES_ROT_DS =	STAT.ROTA	; Rotation-vector dataset
ES_SUM_DS =	ES.SUMMARY	; ES summary dataset
ES_STRAIN_DS	= <false></false>	; Element strain dataset
ES_STRESS_DS	= <false></false>	; Element stress dataset
ES_STR_LOC	✓ 'CENTROIDS'	; Stress locations
ES_STR_DIR	= 'E'	; Stress directions
NUM_CON_DS	= 1	; No. of constraint datasets
LDI	= 1	Logical device index
)		

The following examples illustrate how element processors based on the generic structuralelement (ES) processor template can be used to perform structural analysis with the CSM Testbed. For simplicity, we consider preprocessing (*i.e.*, model generation), linear analysis, nonlinear analysis, and postprocessing (*i.e.*, stress recovery, etc.) examples separately. The differences between employing individual ES*i* processors directly versus accessing them using the generic ES procedure interface will be stressed, with an intended bias towards the latter.

### 7.4.7.1 <u>Preprocessing Examples</u>

For clarity, a very simple problem will be considered, and the use of the generic structuralelement processor illustrated by showing all of the steps involved in generating a finite element (FE) model for this problem. Both the physical problem and the discrete model to be used is given in Figure 7.4-1. The problem is a rectangular plate (10 in. by 5 in.), cantilevered on one edge, and loaded on the other by a concentrated lateral force. For the model, a 3 by 3 grid is used which corresponds to a 2 by 2 mesh of 4-node plate/shell elements. The Testbed procedure for this model is given in Figure 7.4-2. The interpretation of each line of the procedure will now be described.

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The \*procedure statement in Figure 7.4-3 shows the arguments (parameters) for the procedure and sets default values for each of them (x-length, y-length, thickness, elastic modulus, Poisson's ratio, and precision). Thus the dimensions and properties of the plate model are parameterized, but the finite element discretization is fixed.<sup>†</sup> The next two lines ([xqt TAB and START 9) run the processor TAB and reserve space for a total of 9 nodes. Then, the JLOC command and subsequent data define the global coordinates for these 9 nodes in a rectangular 3 by 3 grid.

Material and section properties are then defined by first executing processor AUS to tabulate the raw data, and then executing processor LAU to generate an integrated constitutive matrix for shell elements (see the CSM Testbed User's Manual for details on processor LAU).

The key portion of the example begins with the \*call to procedure ES with FUNCTION = 'DEFINE ELEMENTS', in which element type EX42 of processor ES1 is registered for participation in the model. This call also causes a number of element type-oriented macrosymbols, all beginning with ES\_, to be defined — for example, ES\_NEN (number of element nodes), ES\_NIP (nuber of element integration points), etc. These macrosymbol values are automatically built into the character string macrosymbol ES\_EXPE\_CMD (by procedure ES), which serves as the EXPE command for processor ELD. Note that in the PLATE\_MODEL example, <ES\_EXPE\_CMD> appears immediately after [XQT ELD (execute processor ELD). This sequence causes the ES\_EXPE\_CMD macrosymbol to expand internally into the following commmand line:

EXPE	<es_name></es_name>	<es_nen></es_nen>	<es_opt></es_opt>	<es_nen></es_nen>		<es_ndof></es_ndof>	
			<es_s< td=""><td>TOR&gt;</td><td>1</td><td>10<es_dim></es_dim></td><td><csm_precision></csm_precision></td></es_s<>	TOR>	1	10 <es_dim></es_dim>	<csm_precision></csm_precision>

which would eventually decode into:

EXPE EX42 4 2 4 6 0 1 102 2

The execution of processor ELD with the above EXPE command is necessary for generation of various element datasets such as DEF.EX42.\* and DIR.EX42.\* (see the CSM Testbed

<sup>&</sup>lt;sup>†</sup> In practice, it is often the other way around: The model properties and dimensions are fixed, while the discretization is varied. We have fixed the discretization here merely to simplify the example.

User's and Dataset Manuals, references 7.4.2 and 7.4-3, respectively). Note that the ES\_ macrosymbols referenced in this example are all described in the Macrosymbol Glossary in Table 7.4-4.

Next, the NSECT command is used as a section property pointer. NSECT=1 means that the integrated constitutive matrix stored in the first column of dataset PROP.BTAB.2.101 will be employed by all elements whose nodal connectivity is defined on the following lines. The element nodal connectivity is then defined for four 4-node elements. Note that the numbering convention is counter-clockwise within each element (see Fig. 2.2-1). Boundary conditions and loads are then defined using the CON command of processor TAB, and the SYSVEC command of processor AUS, respectively (see Figure 7.4-2). The CON command suppresses all freedoms along x = 0 (the built-in edge), and the SYSVEC command distributes transverse nodal forces along the other edge, which add up to a unit load. Note that both boundary conditions and loads have been defined with respect to nodes rather than elements. Automatic consistent element nodal load generation will be available once the DEFINE LOADS command has been implemented within the ES processor shell.

Finally, procedure ES is called again to perform *automatic degree of freedom suppression*, using the DEFINE FREEDOMS command. In this case, the effect will be for processor ES1 to suppress drilling rotational freedoms (*i.e.*, the 6th degree of freedom) at all nodes, since element type EI42 has no stiffness associated with these freedoms. (Note: If the plate had blade stiffeners which were also modeled with EI42 elements, all 6 degrees of freedoms at nodes along the plate/stiffener intersection lines would be retained, since at least one of the intersecting elements at those nodes would possess the necessary stiffness.)

```
*Procedure PLATE_MODEL ( Lx=10.; Ly=5.; h=.1; E=1.e7; PR=.3; prec=2 )
    [xqt TAB
     START 9
. GENERATE NODES ( rectangular grid, 3 x 3 nodes )
     JLOC
            0., 0., 0.
       1
                         [Lx], 0., 0. 3, 1, 3
       3
            0., [Ly], 0. [Lx], [Ly], 0.
. TABULATE MATERIAL AND SECTION PROPERTIES
    [xqt AUS.
       TABLE(NI=16,NJ=1): OMB DATA 1 1...
        I=1,2,3,4,5,6 : J=1 : [E] [PR] [E] <G> <G> <G>
       TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
        I=1,2,3 . : J=1: 1 [h] 0.0.
. RUN CONSTITUTIVE PRE-PROCESSOR
    [xqt LAU
 GENERATE ELEMENTS
             *call ES ( function='DEFINE ELEMENTS'; ES_PROC=ES1; ES_NAME=EX42 )
      ____
    [xqt ELD
       <ES_EXPE_CMD>
        NSECT = 1
                    elt 2
                                 elt 3
          elt 1
                                                elt 4
        1 2 5 4 : 2 3 6 5 : 4 5 8 7 : 5 6 9 8
```

Figure 7.4-1 Sample Preprocessing Procedure.

\*end



# 7.4.8 Linear Analysis Examples

A sample linear static analysis procedure, which employs the procedure ES to invoke the appropriate ESi processors is shown in Figure 7.4-4. For purposes of illustration, the problem has been kept simple (notice that there are no procedure arguments), but keep in mind that many analysis procedures may involve more sophisticated features. The procedure in Figure 7.4-4 can be read as follows. The [xqt E directive causes processor E to construct \*.EFIL.\* datasets for all participating element types. Note that, while space for these datasets is reserved in the database, meaningful data has not yet been deposited there.

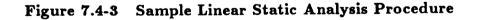
The first call to procedure ES then causes INITIALIZE to be stored in the EFIL datasets by all participating ESi processors — as prescribed by previous calls to procedure ES with function = 'DEFINE ELEMENTS'. For example, if the preprocessing example given in Figure 7.4-3 had preceded the call to L\_STATIC, then only processor ES1, element type EX42, would be invoked to INITIALIZE. More information on the effect of the INITIALIZE command may be found in Section 2.2. The second call to procedure ES is to form the element material (linear) stiffness matrices for all elements in the model using \*call ES (function='FORM STIFFNESS/MATL'). The element matrices are deposited in Segment 5 of the EFIL dataset. Since no other arguments are employed in this call to the procedure ES, the default values are implied. Thus, for example, the problem is assumed to be linear (ES\_NL\_GEOM = 0), and there is no need for a displacement dataset (whose name is given by argument ES\_DIS\_DS) to be input by the ES Processors.

Next, assembly of the element stiffness matrices into a system matrix is performed by processor K. Note that the element matrices have already been transformed to the computational (nodal degrees of freedom) bases, so that the function of processor K is merely to add appropriate submatrices.

Finally, processors INV and SSOL are executed in order to factor and solve the assembled system of equations, respectively. The displacement solution will be stored, as indicated by the RESET command for processor SSOL, in dataset STAT.DISP.1.1.

\*procedure L\_STATIC

```
_____
 Initialize Element Datasets
 _____
 [xqt E
     Initialize Element Computational Data
 ______
 *call ES ( function = 'INITIALIZE' )
   ------
 Form Element Material Stiffness Matrices
 _____
 *call ES ( function = 'FORM STIFFNESS/MATL' )
   Assemble Material Stiffness Matrix
   [xqt K
    _____
 Factor Stiffness Matrix
   _____
 [xqt INV
   ______
 Solve for Displacements
 _____
 [XOT SSOL
  RESET SET=1, CON=1
*end
```



# 7.4.9 Nonlinear Analysis Examples

A brief example of how to employ ESi processors in nonlinear analysis procedures, by including selected excerpts from an actual nonlinear static analysis procedure that will hopefully convey the essential aspects. Typically, engineering-oriented users will invoke an existing nonlinear analysis procedure rather than writing their own, so this example is intended more for researchers involved in algorithm development.

The "skeleton" of a nonlinear static analysis procedure is shown in Figure 7.4-5, with only those aspects involving ESi processors shown. There is very little difference in the use of the procedure ES to invoke ES processors from what was employed in the *linear* static analysis procedure compare with Figure 7.4-4, except that some additional arguments must be explicitly defined.

First, the usual call to INITIALIZE for all ESi processors is present. This call enables the participating element processors to generate, and store, any data that will be used repeatedly during the analysis — rather than having to recompute it at each iteration of every analysis load step.

Next, the nested load-step and iteration loops, typical of most incremental/iterative nonlinear solution algorithms for structural analysis are encountered. Within these loops, it is necessary to compute residual force vectors (right-hand sides) at each iteration and tangent stiffness matrices at selected load steps/iterations.

The assembled residual force vector is computed by first initializing a system internal force vector (using processor VEC), calling the procedure ES to form/assemble all element contributions to the internal force vector, and finally subtracting the assembled internal force vector from a load-step scaled external force vector, which is assumed to have been generated elsewhere.

Notice that in the FORM FORCE/INT call to procedure ES, arguments ES\_NL\_GEOM, ES\_CORO, ES\_DIS\_DS, ES\_ROT\_DS and ES\_FRC\_DS are each explicitly defined. The reader is urged to look up these arguments in the Macrosymbol/Argument Glossary, Table 7.4-4. These arguments let the ESi processors know that the problem is geometrically nonlinear (both globally and at the element level). The corotational algorithm is to be employed to make the rotational motion "appear" small at the element level, but allow it to be arbitrarily large globally. The current displacement dataset is called TOT.DISP.<\$step>, where <\$step> is the load-step number; the current rotation (pseudo-vector) dataset is called TOT.ROTA.<\$step>; and the current system internal force vector into which the element contributions are to be assembled is called INT.FORC.<\$step>.

Finally, the formation/factorization of the tangent stiffness matrix is shown in Figure 7.4-5 which involves first the formation/transformation of the element tangent stiffness matrices by ESi processors, which are deposited in the \*.EFIL.\* datasets; then the assembly of the element matrices into the system tangent stiffness matrix by processor K; and finally the factorization of the assembled (system) tangent stiffness matrix by processor INV. Note that both material and geometric stiffness contributions have been superimposed at the element level.

```
*procedure NL_STATIC ( NUM_STEPS = 1; NUM_ITERS = 10 )
  _____
. Initialize Element Computational Data
*call ES ( function = 'INITIALIZE' )
 *do $step = 1, [NUM_STEPS]
    *do $iter = 1, [NUM_ITERS]
        ______
      FORM RESIDUAL FORCE VECTOR
      _________________
      [xqt VEC
       INT.FORC <- 0.
. .
      *call ES ( function = 'FORM FORCE/INT'; --
                es_nl_geom = 2; es_coro = 1; --
                es_dis_ds = TOT.DISP.<$step>; --
                es_rot_ds = TOT.ROTA.<$step>; --
                es_frc_ds = INT.FORC.<$step> )
     [xqt VEC
      RES.FORC <- <load_factor> * EXT.FORC - INT.FORC.<$step>
   :
        _____
      FORM/FACTOR TANGENT STIFFNESS MATRIX
           _____
     *call ES ( function = 'FORM STIFFNESS/TANG' ; --
               es_nl_geom = 2; es_coro = 1; --
               es_dis_ds = TOT.DISP.<$step>; --
               es_rot_ds = TOT.ROTA.<$step>; --
               es_frc_ds = INT.FORC.<$step> )
     [xqt K
     [xqt INV
    *enddo
  *enddo
```

# Figure 7.4-4 Sample Nonlinear Static Analysis Procedure Excerpts

# 7.4.10 Postprocessing Examples

By postprocessing refers to functions which can be performed after the displacement solution has been obtained for a linear or nonlinear structural analysis. For example, in a nonlinear static (or transient) analysis, the user may choose not to archive the stresses and strains which were used as intermediate variables during the process of obtaining a displacement solution history. The user may then compute stresses and/or strains at selected load (or time) steps and save these in the database for perusal. The end-user phase of postprocessing is of course the actual printing or display of the results (displacements, stresses, strains, etc.); however, the main interest here is in the prerequisite functions that are performed by ESi processors.

An example of a postprocessing procedure that employs ESi processors to form, and archive in the database, both stresses and strains after the mainstream analysis has already been performed. Procedure STRESS\_STRAIN contains arguments to select the stress/strain locations (the default is at element centroids), component directions (the default is in the element local stress/strain coordinate system), existing displacement and rotation (for nonlinear analysis) datasets to be employed for strain computation.

Note that there is a step loop in the procedure, and that both stresses and strains for all participating elements are formed by just a single call to procedure ES per step. This is because the FORM STRESS command automatically causes strains to be formed as well as stresses, and when both ES\_STRAIN\_DS and ES\_STRESS\_DS are explicitly defined, then both of these quantities are also output to the database.

```
*procedure STRESS_STRAIN ( LOCATION = CENTROIDS ; DIRECTION = 0
                                                       ; ---
                      NL_GEOM = 0; CORO = 0
                                                       ; ---
                      NUM_STEPS = 1
                                       ; STEPS
                                                  = 1:1 ; --
                      DIS_DS = TOT.DISP ; ROT_DS = TOT.ROTA )
  ------
  Loop on Solution Steps
•
  _____
  *def/i steps[1:[num_steps]] = [steps]
  *do \$is = 1, [num_steps]
     *def/i step = <steps[<\$is>]>
           ______
    Invoke Element Processors to Form Stress/Strain
        _____
     *call ES ( function = 'FORM STRESS'
                                       ; --
              es_nl_geom = [nl_geom]
                                      ; --
              es_coro = [coro]
                                      ; --
              es_dis_ds = [DIS_DS].<step> ; --
              es_rot_ds = [ROT_DS].<step> ; --
              es_str_dir = [DIRECTION]
                                      ; ---
              es_str_loc = [LOCATION]
                                      ; --
              es_strain_ds = <step>
                                     ; --
              es_stress_ds = <step> )
```

\*enddo

\*end



#### 7.4.11 PROCEDURE LISTING

```
*procedure ES ( function ; --
es_proc ; --
es_name ; --
es_pars ; --
```

```
. beg_update 06_NAY_1989 [GHS] ES_COUNT
            es_count = 0 ; -- . 0/1=>create/accum ES.SUMMARY
. end_update
            es_coro = 1; ---
            es_nl_geom = 0 ; --
            es_nl_matl = 0 ; --
            es_nl_load = 0 ; --
            es_dis_ds = STAT.DISP.1.1
                                      ; --
            es_dof_ds = ES.DOFS
                                       : --
            es_ecc_ds = WALL.PROP
                                       ; --
            es_frc_ds = INT.FORC.1.1 ; --
            es_rot_ds = STAT.ROTA.1.1 ; --
            es_sum_ds = ES.SUMMARY
                                     ; --
            es_mass_diag = DEM
                                       ; --
             es_strain_ds = ' '
                                       ; --
             es_stress_ds = ' '
                                       ; --
             es_str_loc = CENTROIDS
                                      ; --
             es_str_dir = 0
                                       ; ---
            num_con_ds = 1
                                       ; --
. beg_update 26_APR_1989 [GMS] CONSISTENT LOADS
             es_load_factor = 1.0
                                      ; --
             es_load_set = 1
                                       ; --
. end_update 26_APR_1989 [GNS] CONSISTENT LOADS
             ldi
                = 1 )
  . Generic Procedure for Structural Element (ES) Processors
```

#### Utility Procedures

```
+if < <IFELSE([function];DEFINE ELEMENTS;1;0)> > /then
  *def/a es_proc
                  = [es_proc]
  *def/a es_name = [es_name]
  *def/d es_pars[1:10] = [es_pars]
  *def/a es_sum_ds
                    = [es_sum_ds]
     _____
     Initialize ES SUMMary Dataset
     _____
     #find dataset [ldi] <es_sum_ds> /seq=es_ids
. beg_update 06_MAY_1989 [GMS] ES_COUNT
     *if < < <es_ids> /le 0 > /or < [es_count] /eq 0 > > /then
        *put dataset [ldi] <es_sum_ds> /mrat=2000 /seq=es_ids
        *def/i es_num = 1
     +else
        *find record [1di], <es_sum_ds>, ES_PROC /nor=es_num
        *def/i es_num = < <es_num> + 1 >
     *endif
. end_update
     *m2g /name==es_proc /type=a [ldi] <es_ids> ES_PROC.<es_num>
     *m2g /name==es_name /type=a
                               [ldi] <es_ids> ES_NAME.<es_num>
     *m2g /name==es_pars /type=d /maxn=10 [ldi] <es_ids> ES_PARS.<es_num>
   ______
  Run ES Processor
   -----
   [IQT <es_proc>
      [function]
```

İ.

```
. Define macrosymbol for ELD/EXPE command
 *if < <es_stor> /gt 0 > /then
       *def/i es_nst = < ((<es_stor>-1)/<es_nen>) + 1 >
    *else
       *def/i es_nst = 1
    *endif
. BEG_UPDATE MAY_5_1989 [SNO] EXPE CHANGE
    *def/a ES_EXPE_CMD=='EXPE '[es_name]' '<es_nen>' '--
    *def/a ES_EIPE_CMD=='EXPE '[es_name]' '4' '--
. END_UPDATE
<es_opt>' '<es_nen>' '<es_ndof>' '<es_nst>' 1 10'<es_dim>' '<csm_precision>
*else
 *find dataset [ldi] [es_sum_ds] /seq=es_ids
 *def/a es_mass_diag == [es_mass_diag]
 *def/a es_mass_ds == [es_mass_diag].DIAG
  Find Number of Element Processors from Database
  *find record [ldi], <es_ids>, ES_PROC /nor=num_es_proc
  *if < <num_es_proc> /le 0 > /then
     *remark Cannot find any ES Processor names in dataset [es_sum_ds]
```

```
6
  +endif
  *if < <IFELSE([function];DEFINE FREEDOMS;1;0)> > /then
     *call ES_DOFS ( function=INITIALIZE; es_dof_ds=[es_dof_ds] )
  *endif
  _____
 Process all Element Processors Found
  ***********
  *do $ies = 1, <num_es_proc>
     *g2m /name==ES_PROC /type=a [ldi] <es_ids> ES_PROC.<$ies>
     *g2m /name==ES_NAME /type=a [ldi] <es_ids> ES_NAME.<$ies>
     *g2m /name==ES_PARS /type=d [ldi] <es_ids> ES_PARS.<$ies>
     *g2m /name==ES_NSTR /type=d [ldi] <es_ids> ES_NSTR.<$ies>
     *def/i ES_COR0 = [es_coro]
     *def/a ES_DIS_DS = [es_dis_ds]
     *def/a ES_DOF_DS = [es_dof_ds]
     *def/a ES_ECC_DS = [es_ecc_ds]
     $def/i ES_FIKI = [es_fikx]
     *def/a ES_FRC_DS = [es_frc_ds]
     *def/i ES_NL_GEOM = [es_nl_geom]
     *def/i ES_NL_LOAD = [es_nl_load]
     *def/i ES_NL_MATL = [es_nl_matl]
     *def/a ES_ROT_DS = [es_rot_ds]
. beg_update 26_APR_1989 [GMS] CONSISTENT LOADS
     #def/g ES_LOAD_FACTOR = [es_load_factor]
     #def/i ES_LOAD_SET = [es_load_set]
. end_update 26_APR_1989 [GMS] CONSISTENT LOADS
```

```
*def/a ES_STR_DIR = [es_str_dir]
     *def/a ES_STR_LOC = [es_str_loc]
     *if < <IFELSE([es_strain_ds]; ;0;1)> > /then . (if not blank)
        *def/a ES_STRAIN_DS = [es_strain_ds]
     *endif
     *if < <IFELSE([es_stress_ds]; ;0;1)> > /then . (if not blank)
        *def/a ES_STRESS_ds = [es_stress_ds]
     *endif
     [IQT <es_proc>
      [function] . DEFINE FREEDOMS | FORM FORCE | STIFFNESS | ...
  *enddo
  *if < <IFELSE([function];DEFINE FREEDOMS;1;0)> > /then
     *call ES_DOFS ( function=FINALIZE; es_dof_ds=[es_dof_ds]; --
                                       num_con_ds=[num_con_ds] )
  *endif
*endif
STOP
+end
. =DECK ES_DOFS
*procedure ES_DOFS ( function=INITIALIZE; es_dof_ds=ES.DOFS; --
                                       num_con_ds=1; ldi=1 )
  *if < <IFELSE([function];INITIALIZE;1;0)> > /then
     *remark
     *remark ES_DOFS: Performing Automatic DOF Suppression for ES Elts
     *def/i ns_overwrite == <true>
      Initialize Element DOF Dataset
```

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```
_____
  *g2m /name=parameters /type=i /maxn=18 [ldi] JDF1.BTAB.1.8 DATA.1
  #def/i num_nodes = <parameters[1]>
  *def/i num_dofs = <parameters[2]>
  [XQT VEC
   INIT_TAB [es_dof_ds] <num_dofs> BY <num_nodes>
*elseif < <IFELSE([function];FINALIZE;1;0)> > /then
  Merge Element DOF Dataset with Constraint Datasets
  _____
  *def/i num_cds = 0
  *do $cds = 1, [num_con_ds]
     *def/a con_ds = CON..<$cds>
     #find dataset [ldi], <con_ds> /seq=id_cds
     *if < <$cds> /eq 1 > /then
      [XQT VEC
     *endif
     #if < <id_cds> /gt 0 > /then
        *remark ES_DOFS Processing Constraint Dataset: <con_ds>
        MERGE_DOF [es_dof_ds] -> <con_ds>
        *def/i num_cds = < <num_cds> + 1 >
     *endif
  *enddo
  *remark
  *remark ES_DOFS Processed <num_cds> Constraint Datasets
  *remark
  *def/i ns_overwrite == <false>
```

\*endif

\*end

### 7.4.12 REFERENCES

- 7.4-1 Stanley, G. M.; and Nour-Omid, S.: The Computational Structural Mechanics Testbed Generic Structural-Element Processor Manual. NASA CR-181728, March 1990.
- 7.4-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Users Manual. NASA TM-100644, October 1989.
- 7.4-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

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# 7.5 Procedure FACTOR

## 7.5.1 GENERAL DESCRIPTION

Procedure FACTOR decomposes or factors a system matrix using a solver defined by the global macrosymbol solver\_name. If solver\_name is defined to be INV, the original nodalblock sparse solver implemented in processor INV will be used (see Section 6.7 of reference 7.5-1). If solver\_name is defined to be BAND, a variable-bandwidth direct solver implemented in processor BAND will be used (see Section 8.5 of reference 7.5-1).

### 7.5.2 PROCEDURE USAGE

Procedure FACTOR is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are orderindependent, and most have default values thus making them optional. The formal syntax is as follows:

\*call FACTOR ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure FACTOR are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure FACTOR, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
CONSTRAINT_SET	1	Constraint set number
INPUT_MATRIX	K	First word of the name of the dataset containing
		the assembled stiffness matrix
OUTPUT_MATRIX	K	Second word of the name of the dataset containing
		the factored system stiffness matrix
INPUT_LDI	1	Logical device index for input_matrix
OUTPUT_LDI	1	Logical device index for output_matrix

Tables 7.5-1 and 7.5-2 list the datasets used or created by procedure FACTOR and the processors invoked by procedure FACTOR, respectively.

Table 7.5-1 Datasets Input/Output by procedure FACTOR			
Dataset	Description	Input	Output
AMAPic2.isize	Factorization Map for INV	$\checkmark$	
CON <i>j</i> <sup>†</sup>	Constraints	$\checkmark$	
INV. <i>O_M.j</i> <sup>†</sup> *	Factored Stiffness Matrix		$\checkmark$
JDF1.BTAB.1.8	Model Summary	$\checkmark$	
JSEQ.BTAB.2.17	Nodal Elimination Sequence	$\checkmark$	
KMAPnsubs.ksize	Model Connectivity Map	$\checkmark$	
I_M.SPAR.jdf2**	Assembled Stiffness Matrix	$\checkmark$	

 $\dagger j = \langle \text{constraint\_set} \rangle * O_M = \langle \text{output\_matrix} \rangle * I_M = \langle \text{input\_matrix} \rangle$ 

Table 7.5-2 Processors Invoked by procedure FACTOR		
Procedure	Туре	Function
INV	Internal	Factor stiffness matrix in nodal-block-sparse format
BAND	External	Factor stiffness matrix in variable-bandwidth format

## 7.5.3 ARGUMENT DESCRIPTIONS

## 7.5.3.1 CONSTRAINT\_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

## 7.5.3.2 INPUT\_MATRIX

First word of the dataset name containing the assembled stiffness matrix (default: K).

## 7.5.3.3 OUTPUT\_MATRIX

Second word of the dataset name containing the factored system stiffness matrix (default: K). This notation is only valid if the macrosymbol solver\_name is set to INV.

#### 7.5.3.4 <u>INPUT\_LDI</u>

Input logical device index containing the input matrix (default: 1).

#### 7.5.3.5 OUTPUT\_LDI

Output logical device index containing the output matrix (default: 1).

#### 7.5.4 USAGE GUIDELINES AND EXAMPLES

Procedure FACTOR may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call FACTOR ( INPUT_MATRIX = K ; CONSTRAINT_SET = 1 )
```

Before procedure FACTOR is called, the global macrosymbol solver\_name should be defined as described in Section 7.5.1; otherwise, the default value of INV will be used.

#### 7.5.5 LIMITATIONS

None.

### 7.5.6 ERROR MESSAGES AND WARNINGS

None.

#### 7.5.7 PROCEDURE FLOWCHART

Procedure FACTOR is self-contained with no subprocedures.

#### 7.5.8 PROCEDURE LISTING

```
#if < ifeqs( <solver_name>;INV) > /then
. Use original nodal block sparse solver originally in SPAR
[XQT INV
     reset K
                 = [input_matrix]
     reset KLIB = [input_ldi]
     reset KILIB = [output_ldi]
     reset CON
               = [constraint_set]
                = 40000
     reset LRA
     reset DZERO = 1.E-20
     reset spdp = <csm_precision>
*elseif < ifeqs( <solver_name>;BAND) > /then
. Use Banded solver
[XQT BAND
    reset meth=28, 1dl=1, klib=[input_1di]
    reset ncon=[constraint_set], dzero=1.0e-20, k=[input_matrix]
    reset opt=1, res=-1
#endif
STOP
. Define factored-matrix parameters as global macrosymbols
*if < ifeqs( <solver_name>;ITER) > /then
   *def/e coef_det == 1.0E+01
   *def/i exp10_det == 1
   *def/i num_neg == 0
   *def/i sign_det == 1
*else
   *remark Determinant of [input_matrix] = <coef_det> * 10 ** <exp10_det>
   *remark Number of negative roots = <num_neg>
   *def/i sign_det == <SIGN(1.;<coef_det>)>
*endif
*end
```

## 7.5.9 REFERENCES

7.5-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.6 Procedure FORCE

## 7.6.1 GENERAL DESCRIPTION

Procedure FORCE drives the calculation of force vectors for either linear or nonlinear analyses.

## 7.6.2 PROCEDURE USAGE

Procedure FORCE may be used by preceding the procedure name by the \*call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call FORCE ( arg1 = val1 ; arg2 = val2 ; ...)

For procedure FORCE, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
COROTATION	1	Corotational flag $(0, 1, 2)$
DISPLACEMENT		First two words of displacement dataset name
LDI	1	Logical device index
LOAD_SET	1	Load set number
LOAD_FACTOR	1.0	Load factor
NL_GEOM	0	Geometric nonlinearity flag
NL_LOAD	0	Nonlinear load terms (live terms)
NL_MATL	0	Material nonlnearity flag
ROTATION		First two words of rotation-vector dataset name
TYPE	RESIDUAL	Type of force vector (residual, external, internal)
INPUT_FORCE		Input force vector dataset name
OUTPUT_FORCE	SYS.FORCE	Output force vector dataset name

Tables 7.6-1, 7.6-2, and 7.6-3 list the datasets used or created by procedure FORCE, the procedures invoked by procedure FORCE, and the processors invoked by procedure FORCE, respectively.

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Table 7.6-1 Datasets Input/Output by procedure FORCE			
Dataset	Description	Input	Output
ES.SUMMARY	ES Processor Status	$\checkmark$	$\checkmark$
INT.FORC. <i>i.j</i> <sup>†</sup>	System Internal Force Vector		$\checkmark$
STAT.DISP.i.j <sup>†</sup>	System Displacement Vector		$\checkmark$
STAT.REAC.i.j <sup>†</sup>	System Reaction Force Vector		$\checkmark$

 $\dagger$  i = <load\_set> and j = <cons\_set>

Table 7.6-2 Sub-procedures Invoked by procedure FORCE		
Procedure	Туре	Function
ES	External	Element utility procedure
FORCE		Main Procedure

Table 7.6-3 Processors Invoked by procedure FORCE		
Procedure	Туре	Function
ESi	External	Element processors based on GEP
VPRT	Internal	Print SYSVEC-format vectors

## 7.6.3 ARGUMENT DESCRIPTIONS

### 7.6.3.1 COROTATION

Corotational update switch for large-rotation problems (default: 1). This switch should be set to 1 when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element processor (ESi) section in the CSM Testbed User's Manual (see ref. 7.6-1) for specific guidelines.

## 7.6.3.2 DISPLACEMENT

First two words of the dataset name for the displacement solution.

### 7.6.3.3 INPUT\_FORCE

Full dataset name for the input or basic force vector.

### 7.6.3.4 OUTPUT\_FORCE

Full dataset name for the output force vector (default: SYS.FORCE).

7.6.3.5 LDI

Logical device index (default: 1).

### 7.6.3.6 LOAD\_FACTOR

Load factor used to scale the basic applied loads or displacements (default: 1.0).

#### 7.6.3.7 <u>NL\_GEOM</u>

Geometric nonlinearity level: 0, 1, or 2 (default: 2). A value of zero means that the problem is geometrically linear; a value of one means that the geometric nonlinearity will be handled globally (*i.e.*, using corotational updates only); and a value of two means that the nonlinear element strain-displacement relations will be used in addition to any global treatment of geometric nonlinearity.

### 7.6.3.8 ES\_NL\_MATL

Material nonlinearity switch. If ES\_NL\_MATL is greater than zero, then the element is materially nonlinear. If ES\_NL\_MATL is zero, then the element is materially linear.

#### 7.6.3.9 <u>NL\_LOAD</u>

Nonlinear loading index for live loads (default: 0).

#### 7.6.3.10 ROTATION

First two words of the dataset name for the rotation solution.

### 7.6.3.11 <u>TYPE</u>

Type of force vector to form (default: RESIDUAL. This argument selects the type of force vector to form (RESIDUAL, INTERNAL, or EXTERNAL).

### 7.6.4 USAGE GUIDELINES AND EXAMPLES

Procedure FORCE may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call FORCE ( LOAD_SET = 1 ; INPUT_FORCE = APPL.FORC.[load_set].1;
OUTPUT_FORCE = EXT.FORC; TYPE = EXTERNAL;
LOAD_FACTOR = 2.5; LDI = 1 )
```

### 7.6.5 LIMITATIONS

Applicable only to elements implemented using the generic element processor template.

### 7.6.6 ERROR MESSAGES AND WARNINGS

None.

### 7.6.7 PROCEDURE FLOWCHART

FORCE	(main procedure)
-------	------------------

ES (internal force calculation)

#### 7.6.8 PROCEDURE LISTING

```
*procedure FORCE ( type = RESIDUAL ; -- . RESIDUAL | EXTERNAL | INTERNAL
                                      ; --
                input_force
                output_force = SYS.FORCE ; --
                                      ; ---
                load_set = 1
                load_factor = 1.0
                                      ; ---
                nl_geom = 0
                                      ; ---
                                      ; ---
                nl_matl = 0
                                      ; --
                nl_load = 0
                                      ; --
                displacement
                                      ; --
                rotation
                corotation = 0
                                      ; ---
                ldi = 1 )
     [xqt VEC
      _____
      Initialize Output Force Vector
      _____
      *find [ldi] [output_force] /seq=ids_oforce
      *if < <ids_oforce> /le 0 > /then
```

```
+g2m /name=num_nodes /type=i [ldi] MODEL.SUMMARY NUM_NODES
        +g2m /name=num_dofs /type=i [ldi] MODEL.SUMMARY NUM_DOFS
        INIT_VEC [output_force] <num_dofs> BY <num_nodes>
      *else
         [output_force] <- 0.
      *endif
      Add Scaled Input Force Vector
•
      _____
      *if < <IFELSE([input_force]; ;0;1)> > /then
        *find [ldi] [input_force] /seq=ids_iforce
        *if < <ids_iforce> /gt 0 > /then
         [output_force] <- [load_factor] [input_force]
         *endif
      *endif
      ____
      Add Element Forces
.
      -----
      *call ES ( function = 'FORM FORCE/[type]'; --
                ldi
                          = [ldi]
                                           ; ---
                es_nl_geom = [nl_geom]
                                           ; ---
                es_nl_load = [nl_load]
                                           : --
                        = [corotation]
                                           ; ---
                es_coro
                es_dis_ds = [displacement]
                                          ; --
                                           ; --
                es_rot_ds = [rotation]
                es_load_factor = [load_factor]; --
                es_load_set = [load_set]
                                          ; --
                es_frc_ds = [output_force] )
```

\*end

#### 7.6.9 REFERENCES

7.6-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989. THIS PAGE LEFT BLANK INTENTIONALLY.

# 7.7 Procedure IMPERFECTION

## 7.7.1 GENERAL DESCRIPTION

Procedure IMPERFECTION to superpose a set of normalized buckling modes to form an initial geometric imperfection shape. This imperfection shape is then added to the nodal coordinates of the structure. The original nodal coordinates are first copied into another dataset and saved for subsequent use if desired.

## 7.7.2 PROCEDURE USAGE

Procedure IMPERFECTION is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call IMPERFECTION ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure IMPERFECTION are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure IMPERFECTION, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
AMPS	1.0	Amplitude of each buckling mode
MODE	1	Mode numbers
N_MODES	1	Number of buckling modes used
		in computing imperfection shape
LDI	1	Logical device index

Processor IMP is used to perform the modal superposition (see reference 7.7-1).

## 7.7.3 ARGUMENT DESCRIPTIONS

## 7.7.3.1 AMPS

Amplitudes of buckling mode shapes (default: 1.0). This argument gives an array of amplitudes for the buckling mode shapes. The array amps has N\_MODES entries.

## 7.7.3.2 LDI

Logical device index (default: 1).

## 7.7.3.3 MODE

Buckling mode shape numbers (default: 1). This argument gives an array of mode numbers to be used in generating the initial geometric imperfection shape. The array MODE has N\_MODES entries.

## 7.7.3.4 <u>N\_MODES</u>

Number of buckling mode shapes to use (default: 1). This argument gives the total number of buckling mode shapes to be superposed to form the initial geometric imperfection shape.

## 7.7.4 USAGE GUIDELINES AND EXAMPLES

Procedure IMPERFECTION may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

\*call IMPERFECTION ( n\_modes=1; modes=1; amps=1.0 )

## 7.7.5 LIMITATIONS

Procedure IMPERFECTION only considers normalized buckling modeshapes in forming the initial geometric imperfection shape.

## 7.7.6 ERROR MESSAGES AND WARNINGS

None.

## 7.7.7 PROCEDURE FLOWCHART

IMPERFECTION	(main procedure)
COPY_DS	(copy datasets)
SWITCH_DS	(switch datasets)

### 7.7.8 PROCEDURE LISTING

```
*procedure IMPERFECTION ( n_modes=1; modes=1; amps=1.0; ldi=1 )
 . CLAMP Procedure to Superpose Buckling Modes as Initial Imperfections
 *remark
 *remark Imposing Geometric Imperfections
 *remark
 *remark - - - Saving old nodal coordinates in JLOC.OLD.2.5
  *call COPY_DS ( from_ldi=[ldi]; from_ds = JLOC.BTAB.2.5 ; --
    to_ldi = [ldi]; to_ds = JLOC.OLD.2.5 )
  *call SWITCH_DS ( ldi=[ldi]; --
    ds_1 = JLOC.BTAB.2.5; ds_2 = JLOC.OLD.2.5)
 *remark
 *remark - - - Adding linear combination of buckling modes to coords
 *remark
  [XQT IMP
    *def/i
             modes[1:[n_modes]] = [modes]
    #def/e12.4 amps[1:[n_modes]] = [amps]
    #do $im = 1, [n_modes]
      SUPERPOSE <amps[<$im>]> BUCK.NODE.1.1 /mode=<modes[<$im>]> /NORN
    *remark
              --- Mode = <modes[<$im>]> , Amplitude = <amps[<$im>]>
    *enddo
*end
```

#### 7.7.9 REFERENCES

7.7-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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## 7.8 Procedure INITIALIZE

### 7.8.1 GENERAL DESCRIPTION

Procedure INITIALIZE performs standard initialization functions and resequencing of the joint.

#### 7.8.2 PROCEDURE USAGE

Procedure INITIALIZE is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call INITIALIZE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure INITIALIZE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions. For procedure INITIALIZE, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
CONSTRAINT_SET	1	Constraint set number
LDI	1	Logical device index
MAXCON	35	Maximum number of joints connected to any one joint
RENUMBER	<false></false>	Flag to resequence the joints internally
RSEQ_METHOD	-1	Resequencing method

## 7.8.3 ARGUMENT DESCRIPTIONS

### 7.8.3.1 CONSTRAINT\_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.8.3.2 MAXCON

Maximum number of joints connected to any one joint (default: 35).

### 7.8.3.3 RENUMBER

Flag to resequence the joints internally (default: <false>).

### 7.8.3.4 RSEQ\_METHOD

Resequence method (default: -1). This argument selects which resequencing method to use. The procedure RESEQUENCE is called for this task (see Section 7.12).

## 7.8.3.5 LDI

Logical device index (default: 1).

## 7.8.4 USAGE GUIDELINES AND EXAMPLES

Procedure INITIALIZE is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call INITIALIZE ( LDI = 1 ; CONSTRAINT\_SET = 1 ; RENUMBER = <true> )

### 7.8.5 LIMITATIONS

None.

## 7.8.6 ERROR MESSAGES AND WARNINGS

None.

## 7.8.7 PROCEDURE FLOWCHART

INITIALIZE	(main procedure)
ES	(initialize element processor)
RESEQUENCE	(resequence the joints)
MODEL_SUMMARY	(create MODEL_SUMMARY dataset)

### 7.8.8 PROCEDURE LISTING

```
*procedure INITIALIZE ( renumber=<false>; constraint_set = 1; ldi=1; --
                 rseq_method = -1; maxcon = 35 )
 Perform Standard Initialization Functions
  INITIALIZE ELEMENT CONFIGURATION
 [XQT E
 *call ES ( function = 'INITIALIZE'; ldi=[ldi] )
 *Remark
       Element configuration initialized.
 . RESEQUENCE NODES FOR SOLVER EFFICIENCY
 *****
 *if < [renumber] > /then
   *call RESEQUENCE ( rseq_method=[rseq_method]; --
                ldi=[ldi]; maxcon=[maxcon] )
 *endif
 ------
 CONSTRUCT MATRIX TOPOLOGY MAPS
 [XQT TOPO
      reset maxsub = 100000, lram=40000, lrkm=100000
 RESET BLIB=[1di]
 RESET HLIB=[1di]
 RESET ILIB=[1di]
 *if < ifeqs( <solver_name>;INV ) > /then
 *else
 reset AMAP=0
 *endif
 CONSTRUCT DOF TABLE
 [XOT VEC
   INIT_DOF CON..[constraint_set] -> DOF.TABL
```

#### 7.8.9 REFERENCES

7.8-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.9 Procedure MASS

## 7.9.1 GENERAL DESCRIPTION

Procedure MASS forms the assembled unconstrained mass matrix.

### 7.9.2 PROCEDURE USAGE

Procedure MASS is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MASS ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MASS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions. For procedure MASS, the following table lists each argument, its default value and meaning.

Argument	Default Value	Meaning
TYPE	CONSISTENT	Type of mass matrix
MASS	CEM	Output dataset name
LDI	1	Logical device index

Tables 7.9-1 and 7.9-2 list the datasets used or created by procedure MASS and the processors invoked by procedure MASS, respectively.

Table 7.9-1 Datasets Input/Output by procedure MASS			
Dataset	Description	Input	Output
JDF1.BTAB.1.8	Model Summary	$\checkmark$	
JSEQ.BTAB.2.17	Nodal Elimination Sequence	$\checkmark$	
KMAPnsubs.ksize	Model Connectivity Map	$\checkmark$	
<mass>.SPAR.jdf2</mass>	Assembled Mass Matrix		$\checkmark$
DEM.DIAG	Diagonal Mass Matrix		$\checkmark$

	Table 7.9-2 Processors Invoked by procedure MASS				
Procedure Type Function					
VEC	Internal	l Vector algebra utilities			
к	Internal Assembles unconstrained system matrices				
<b>ESu</b> External Various element processors based on the GEP		Various element processors based on the GEP			

## 7.9.3 ARGUMENT DESCRIPTIONS

## 7.9.3.1 LDI

Logical device index (default: 1).

## 7.9.3.2 MASS

Name of the mass matrix dataset (default: CEM). For a consistent mass matrix, the dataset name is [MASS].SPAR.*jdf2*. For a diagonal mass matrix, the dataset name will be <es\_mass\_diag> or DEM.DIAG.

#### 7.9.3.3 <u>TYPE</u>

Type of mass matrix (default: CONSISTENT). This argument defines the form of the mass matrix to be either consistent or diagonal.

### 7.9.4 USAGE GUIDELINES AND EXAMPLES

Procedure MASS is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis.

\*call MASS ( TYPE = DIAGONAL; MASS = <es\_mass\_diag>; ldi = 1)

### 7.9.5 LIMITATIONS

None.

## 7.9.6 ERROR MESSAGES AND WARNINGS

None.

### 7.9.7 PROCEDURE FLOWCHART

MASS (main procedure)

(form element mass matrices)

### 7.9.8 PROCEDURE LISTING

ES

*procedure MASS	( type = CONSISTENT ; CONSISTENT   DIAGONAL ldi=1; mass = CEM ) . Output dataset
*remark	
*Remark *remark	Forming [type] Mass Matrix
<pre>#1f &lt; <ifels< pre=""></ifels<></pre>	E([TYPE];DIAGONAL;1;0)> > /then
	e Diagonal (Lumped) Mass Matrix
+g2m /nam [XQT VEC	e=num_dofs /type=i [ldi] MODEL.SUMMARY NUM_DOFS e=num_nodes /type=i [ldi] MODEL.SUMMARY NUM_NODES <es_mass_ds> <num_dofs> BY <num_nodes></num_nodes></num_dofs></es_mass_ds>
. Form Element	Mass Matrices (in EFIL Dataset)

### 7.9.9 REFERENCES

7.9-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.10 Procedure MODEL\_SUMMARY

## 7.10.1 GENERAL DESCRIPTION

Procedure MODEL\_SUMMARY generates a summary dataset which contains parameters about the finite element model. These parameters include the number of element processors used (<num\_es\_types>), the total number of nodes (<num\_nodes>), the number of unconstrained degrees of freedom (<num\_dofs>), and the number of equations (<num\_eqns>). These parameters are written to the MODEL.SUMMARY dataset.

## 7.10.2 PROCEDURE USAGE

Procedure MODEL\_SUMMARY is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call MODEL\_SUMMARY ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MODEL\_SUMMARY are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure MODEL\_SUMMARY, the following table lists each argument, its default value and meaning.

Argument	Default Value	Meaning
CONSTRAINT_SET	1	Constraint set number
LDI	1	Logical device index

Table 7.10-1 lists the datasets used or created by procedure MODEL\_SUMMARY.

Table 7.10-1 Datasets Input/Output by procedure MODEL_SUMMARY				
Dataset	Description .		Input	Output
JDF1.BTAB.1.8	Model Summary	$\checkmark$		
MODEL.SUMMARY	Model Summary Parameters		$\checkmark$	

### 7.10.3 ARGUMENT DESCRIPTIONS

#### 7.10.3.1 CONSTRAINT\_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

#### 7.10.3.2 LDI

Logical device index (default: 1).

### 7.10.4 USAGE GUIDELINES AND EXAMPLES

Procedure MODEL\_SUMMARY is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call MODEL\_SUMMARY ( LDI = 1 ; CONSTRAINT\_SET = 1 )

### 7.10.5 LIMITATIONS

None.

## 7.10.6 ERROR MESSAGES AND WARNINGS

None.

### 7.10.7 PROCEDURE FLOWCHART

Procedure MODEL\_SUMMARY is self-contained with no subprocedures.

### 7.10.8 PROCEDURE LISTING

```
*procedure MODEL_SUMMARY ( ldi=1 ; constraint_set=1 )
. Get model parameters from various datasets
*find record [ldi] ES.SUMMARY, ES_PROC /nor=num_es_types
*g2m /name=parameters /type=i /maxn=18 [ldi] JDF1.BTAB.1.8 DATA.1
*def/i num_nodes = <parameters[1]>
*def/i num_dofs = <parameters[2]>
_ _____
. Install the MODEL.SUMMARY dataset, if necessary
 *find dataset [ldi] MODEL.SUMMARY /seq=ids_MS
*if < <ids_MS> /le 0 > /then
    *put dataset [ldi] NODEL.SUMMARY /mrat=64 /seq=ids_MS
*endif
_ _____
. Store parameters in the MODEL.SUMMARY dataset
*m2g /name=num_es_types /type=i [ldi] MODEL.SUMMARY NUM_ES_TYPES
*m2g /name=num_nodes /type=i [ldi] MODEL.SUMMARY NUM_NODES
*m2g /name=num_dofs /type=i [ldi] MODEL.SUMMARY NUM_DOFS
*m2g /name=num_eqns /type=i [ldi] MODEL.SUMMARY NUM_EQNS
*end
```

## 7.10.9 REFERENCES

7.10-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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# 7.11 Procedure PRINT\_EFIL

## 7.11.1 GENERAL DESCRIPTION

Procedure PRINT\_EFIL prints one or all segments of the es\_name.EFIL.itype.nnod dataset where es\_name is the element name (e.g., EX97). The procedure processes <u>all</u> elements of the specified element type.

## 7.11.2 PROCEDURE USAGE

Procedure PRINT\_EFIL is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call PRINT\_EFIL ( arg1 = val1 ; arg2 = val2 )

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PRINT\_EFIL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure PRINT\_EFIL, the following table lists each argument, its default value and meaning.

Argument	Default Value	Meaning
ELEMENT	EX97	Element name
SEGMENT	ALL	EFIL segment

The segments of the EFIL are printed using processor PRTE (see reference 7.11-1).

### 7.11.3 ARGUMENT DESCRIPTIONS

#### 7.11.3.1 <u>ELEMENT</u>

Element name (default: EX97). The argument specifies the element name for which the EFIL segments are to be printed.

## 7.11.3.2 SEGMENT

EFIL segment to be printed (default: ALL). The EFIL (see reference 7.11-2) contains nine segments. Any one or all of the segments may be selected for printing using the argument SEGMENT. The EFIL segments are as follows:

	Segment	Item	Length	Туре	Description
1	Definition			Integ	Same as dataset DEF. <es_name>.</es_name>
2	Material			Real	(currently unused)
3	Geometry			Real	Element geometric parameters.
		XE0	(3,nen)		Initial element nodal coordinates in element basis.
		TEG	(3,3)		Transf. from global to current element basis.
		TEC	(3,3,nen)		Transf. from computational to element basis at element nodes.
		XG0	(3, <i>nen</i> )		Initial elt. nodal coords in global basis.
		TEG0	(3,3)		Transf. from global to initial element basis.
		DE	(nee)		Deformational displacements $(\mathbf{d}_{e}^{def})$ .
4	Property			Real	(currently unused)
5	Matrix	КМ	nmt	Real*	Element matrix (stiffness/mass); only upper triangle of nodal blocks.
6	Aux. Storage			Real	Auxiliary storage for element developer.
7	Stress			Real	(currently unused)
8	Therm. Force			Real	(currently unused)
9	Therm. Stress			Real	(currently unused)

\*The element stiffness/mass matrix, item KM in Segment 5, may be stored in either single or double precision, as specified in dataset DIR.es\_name.itype.nnod (entry 15). However, all of the other REAL data in the es\_name.EFIL.itype.nnod dataset are stored exclusively in single precision.

## 7.11.4 USAGE GUIDELINES AND EXAMPLES

Procedure PRINT\_EFIL may be used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank <u>is required</u> between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

\*call PRINT\_EFIL ( element = EX97; segment = ALL )

## 7.11.5 LIMITATIONS

None.

#### 7.11.6 ERROR MESSAGES AND WARNINGS

None.

# 7.11.7 PROCEDURE FLOWCHART

Procedure PRINT\_EFIL is self-contained with no subprocessors.

#### 7.11.8 PROCEDURE LISTING

```
*procedure PRINT_EFIL ( element = EX97; segment = ALL )
. Print Segment(s) of EFIL Dataset
#if < <ifelse([segment];ALL;i;0)> > /then
  *def/i seg1 = 1
  *def/i seg2 = 9
*else
  *if < <ifelse([segment];DEFINITION;1;0)> > /then
     *def/i seg1 = 1
  *elseif < <ifelse([segment];MATERIAL;1;0)> > /then
     #def/i seg1 = 2
  *elseif < <ifelse([segment];GEOMETRY;1;0)> > /then
     *def/i seg1 = 3
  *elseif < <ifelse([segment];PROPERTY;1;0)> > /then
     *def/i seg1 = 4
  *elseif < <ifelse([segment];STIFFNESS;1;0)> > /then
     *def/i seg1 = 5
  *elseif < <ifelse([segment];STRESS_RECOVERY;1;0)> > /then
     *def/i seg1 = 6
  *elseif < <ifelse([segment];STORE;1;0)> > /then
     *def/i seg1 = 6
  *elseif < <ifelse([segment];STRESS;1;0)> > /then
     #def/i seg1 = 7
  *elseif < <ifelse([segment];THERMAL_FORCE;1;0)> > /then
     *def/i seg1 = 8
```

```
*elseif < <ifelse([segment];THERMAL_RECOVERY;1;0)> > /then
        *def/i seg1 = 9
     *endif
     *def/i seg2 = <seg1>
*endif
[XQT PRTE
RESET SEG1 = <seg1>
RESET SEG2 = <seg2>
[element]
STOP
*end
```

#### 7.11.9 REFERENCES

- 7.11-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
- 7.11-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

# 7.12 Procedure RESEQUENCE

#### 7.12.1 GENERAL DESCRIPTION

Procedure RESEQUENCE resequences the node numbers internally for a solver defined by the global macrosymbol solver\_name. If rseq\_method is -1, then a resequencing method implemented in processor RSEQ (see Section 6.1 of reference 7.12-1) is selected which is appropriate for the equation solver defined by the global macrosymbol solver\_name. That is,

solver_name	rseq_method
INV	1
BAND	2
ITER	1
SPK	none

If **rseq\_method** is 10, then the profile-front minimization resequencing method implemented in processor PFM (see Section 6.2 of reference 7.12-1). If the global macrosymbol **solver\_name** is SPK, no resequencing is performed since processor SPK performs its own resequencing (see Section 8.6 of reference 7.12-1). Other values of **rseq\_method** will select a specific resequencing method requested by a user.

## 7.12.2 PROCEDURE USAGE

Procedure **RESEQUENCE** is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call RESEQUENCE ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure RESEQUENCE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure RESEQUENCE, the following table lists each argument, its default value and meaning.

Argument	<u>Default Value</u>	Meaning
LDI	1	Logical device index
MAXCON	35	Maximum number of joints connected to any one joint
RSEQ_METHOD	-1	Resequencing method

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#### RESEQUENCE

Tables 7.12-1 and 7.12-2 list the datasets used or created by procedure RESEQUENCE and the processors invoked by procedure RESEQUENCE, respectively.

Table 7.12-1 Datas	ets Input/Output by proce	edure R	ESEQUENCE
Dataset	Description	Input	Output
JSEQ.BTAB.2.17	Nodal Elimination Sequence		$\checkmark$
KMAPnsubs.ksize	Model Connectivity Map	$\checkmark$	

Table 7.12-2         Processors Invoked by procedure RESEQUENCE		
Procedure	Туре	Function
RSEQ	Internal	Joint resequencing
PFM	Internal	Joint resequencing using profile-front minimization

# 7.12.3 ARGUMENT DESCRIPTIONS

#### 7.12.3.1 LDI

Logical device index (default: 1).

## 7.12.3.2 MAXCON

Maximum number of joints connected to any one joint (default: 35).

## 7.12.3.3 RSEQ\_METHOD

Resequencing method (default: -1). If rseq\_method is -1, then a resequencing method implemented in processor RSEQ (see Section 6.1 of reference 7.12-1) is selected which is appropriate for the equation solver defined by the global macrosymbol solver\_name.

solver_name	rseq_method
INV	1
BAND	2
ITER	1
SPK	none

If **rseq\_method** is 10, then the profile-front minimization resequencing method implemented in processor PFM (see Section 6.2 of reference 7.12-1). If the global macrosymbol solver\_name is SPK, no resequencing is performed since processor SPK performs its own resequencing (see Section 8.6 of reference 7.12-1). Other values of rseq\_method will select a specific resequencing method requested by a user.

## 7.12.4 USAGE GUIDELINES AND EXAMPLES

Procedure **RESEQUENCE** is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call RESEQUENCE ( RSEQ\_METHOD = 2 )

#### 7.12.5 LIMITATIONS

None.

## 7.12.6 ERROR MESSAGES AND WARNINGS

None.

## 7.12.7 PROCEDURE FLOWCHART

Procedure RESEQUENCE is self-contained with no subprocedures.

## 7.12.8 PROCEDURE LISTING

```
*procedure RESEQUENCE ( rseq_method=-1 ; maxcon=35; ldi=1 )
*if < ifeqs( <solver_name>;SPK) > /then
 *remark ****************************
 *remark * Processor SPK does its own resequencing *
 +else
   *if < [rseq_method] /eq 10 > /then
       [xqt PPM
           RESET BLIB=[1di]
           reset maxcon = [maxcon]
   *elseif < [rseq_method] /ne -1 > /then
       [IOT RSEO
           RESET BLIB=[1di]
           reset method=[rseq_method], maxcon=[maxcon]
   *else
      *if < ifeqs( <solver_name>;INV) > /then
         *def/i rseq_method = 1
```

```
*elseif < ifeqs( <solver_name>;BAND) > /then
    *def/i rseq_method = 2
    *else
        *def/i rseq_method = 1
    *endif
    [XQT RSEQ
        RESET BLIB=[ldi]
        reset method=<rseq_method>, maxcon=[maxcon]
    *endif
.
*endif
.
```

#### 7.12.9 REFERENCES

7.12-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.13 Procedure SOLVE

## 7.13.1 GENERAL DESCRIPTION

Procedure SOLVE solves a linear system of equations using a solver defined by the global macrosymbol solver\_name. If solver\_name is INV, the forward-reduction-back-substitution phase of the original nodal-block sparse solver implemented in processor SSOL will be used (see Section 8.3 of reference 7.13-1). If solver\_name is defined to be BAND, a variable-bandwidth direct solver implemented in processor BAND will be used (see Section 8.5 of reference 7.13-1). If solver\_name is defined to be ITER, an iterative method implemented in processor ITER will be used (see Section 8.4 of reference 7.13-1). If solver\_name is defined to be SPK, the SPARSPAK-A direct solver will be used to factor and solve the system of equations (see Section 8.6 of reference 7.13-1).

#### 7.13.2 PROCEDURE USAGE

Procedure SOLVE is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure SOLVE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

Argument	Default Value	Meaning
APPLIED_MOTION	1	Flag for applied displacements
CONSTRAINT_SET	1	Constraint set number
LDI	1	Logical device index
LOAD_SET	1	Load set number
MATRIX	K	First word of the name of the dataset containing the assembled stiffness matrix.
RHS	APPL.FORC	First two words of the dataset name for the right-hand side system vector.
SOLN	STAT.DISP	First two words of the dataset name for the displacement solution

For procedure SOLVE, the following table lists each argument, its default value and meaning.

Tables 7.13-1 and 7.13-2 list the datasets used or created by procedure SOLVE and the processors invoked by procedure SOLVE, respectively.

Table 7.13-1 Datasets Input/Output by procedure SOLVE				
Dataset	Description	Lib	Input	Output
AMAPic2.isize	Factorization Map for INV	1	$\checkmark$	
APPL.FORC.i.1 <sup>†</sup>	Applied force vector	1	$\checkmark$	
APPL.MOTI.i.1 <sup>†</sup>	Specified displacement vector	1	$\checkmark$	
CONj	Constraints	1	$\checkmark$	
EQNF.FORC.iset.1	Equivalent nodal forces	1	$\checkmark$	
INV. <kname>.j</kname>	Factored Stiffness Matrix	1	$\checkmark$	
JDF1.BTAB.1.8	Model Summary	1	$\checkmark$	
JSEQ.BTAB.2.17	Nodal Elimination Sequence	1	$\checkmark$	
KMAPnsubs.ksize	Model Connectivity Map	1	$\checkmark$	
<kname>.SPAR.jdf2</kname>	Assembled Stiffness Matrix	1	$\checkmark$	
STAT.DISP.i.j <sup>†</sup>	System Displacement Vector	1		$\checkmark$
STAT.REAC. <i>i.j</i> <sup>†</sup>	System Reaction Force Vector	1		$\checkmark$

 $\dagger$  i = <load\_set> and j = <cons\_set>

Table 7.13-2 Processors Invoked by procedure SOLVE		
Procedure	Турс	Function
BAND	External	Solves system of equations using stiffness matrix in variable- bandwidth solver
ITER	External	Solves system of equations using iterative method
SPK	External	Solves system of equations using SPARSPAK-A solve
SSOL	Internal	Solves system of equations using nodal-block-sparse solver
VEC	Internal	Vector algebra utilities

#### 7.13.3 ARGUMENT DESCRIPTIONS

#### 7.13.3.1 APPLIED\_MOTION

Flag indicating that applied displacements are involved in the loading (default: 0 or FALSE).

#### 7.13.3.2 CONSTRAINT\_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

## 7.13.3.3 LDI

Logical device index (default: 1).

## 7.13.3.4 LOAD\_SET

Load set number (default: 1). This argument selects which load set to be used as a right-hand side vector.

## 7.13.3.5 MATRIX

First word of the dataset name containing the assembled stiffness matrix (default: K).

#### 7.13.3.6 RHS

First two words of the dataset name for the right-hand side system vector (default: APPL.FORC).

## 7.13.3.7 <u>SOLN</u>

First two words of the dataset name for the displacement solution (default: STAT.DISP).

# 7.13.4 USAGE GUIDELINES AND EXAMPLES

Procedure SOLVE is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call SOLVE ( MATRIX = K ; CONSTRAINT\_SET = 1 ; LOAD\_SET = 'APPL.FORC' ; SOLN = 'STAT.DISP' )

Before procedure SOLVE is called the global macrosymbol solver\_name should be defined as described in Section 7.12.1 and should be consistent with the value used when procedure FACTOR was called. If it is not specified, then the default value INV will be used.

#### 7.13.5 LIMITATIONS

None.

#### 7.13.6 ERROR MESSAGES AND WARNINGS

None.

#### 7.13.7 PROCEDURE FLOWCHART

Procedure SOLVE is self-contained with no subprocedures.

#### 7.13.8 PROCEDURE LISTING

```
*procedure SOLVE ( rhs='appl.forc'; soln='stat.disp' ; matrix = K
                                                    : --
              load_set=1; constraint_set=1; applied_motion; --
              ldi=1 )
. Procedure to solve a linear system of equations using different solvers.
. The solver is selected using the global macrosymbol "solver_name".
+if < ifeqs( <solver_name>; ) > /then
*def/a solver_name == INV
*endif
                _____
  Define Unique Pseudo Load Set Number for SSOL Vector Datasets
  +def/i iunique = 9999
  Copy Right-Hand-Side Vector to SSOL Force Dataset
                                            *
     _____
  [xqt VEC
```

```
APPL.FORC.<iunique>.1 <- [rhs] /single_precision
  Copy Applied Motions to SSOL Applied Motion Dataset
  **********
 #find [ldi] APPL.MOTI.<iunique>.1 /seq=ids_AMU
 #if < <ids_AMU> /gt 0 > /then
    APPL.MOTI.<iunique>.1 <- 0.
 *else
    *g2m /name=num_nodes /type=i [ldi] MODEL.SUMMARY NUM_NODES
    *g2m /name=num_dofs /type=i [ldi] MODEL.SUMMARY NUM_DOFS
    INIT_VEC APPL.MOTI.<iunique>.1 <num_dofs> BY <num_nodes>
 *endif
 *if < <IFELSE([applied_motion]; ;0;1)> >/then
    *find [ldi] [applied_motion] /seq=ids_AM
    #if < <ids_AM> /gt 0 > /then
       APPL.MOTI.<iunique>.1 <- [applied_motion]
    *endif
 *endif
*if < ifeqs( <solver_name>;INV) > /then
. Use original nodal block sparse solver originally in SPAR
[IQT SSOL
    RESET K
               = [matrix]
    RESET KLIB = [1di]
    RESET KILIB = [ldi]
    RESET QLIB = [1di]
    RESET SET = <iunique>
    RESET CON = [constraint_set]
*elseif < ifeqs( <solver_name>;BAND) > /then
. Use Banded solver
[XQT BAND
   reset meth=28, 1d1=1
   reset ncon=[constraint_set], dzero=1.0e-20, k=[matrix]
   reset opt=2, res=1, iset=<iunique>
*elseif < ifeqs( <solver_name>;ITER) > /then
. Use Iterative solver
[XQT ITER
   reset ep=1, init=11, xnit=-.1, meth=1, time=1, itol=15
   reset ncon=[constraint_set], iset=<iunique>; k=[matrix]
   reset amax=0.5
*elseif < ifeqs( <solver_name>;SPK) > /then
. Use SPARSPAK solver
EXOT SPK
   select /const=[constraint_set] /kname=[matrix]
   select /msglva=2 /msglvl=2 /load=<iunique>
+endif
```

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```
[xqt VEC
```

## 7.13.9 REFERENCES

7.13-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.14 Procedure STIFFNESS

## 7.14.1 GENERAL DESCRIPTION

Procedure STIFFNESS forms the assembled unconstrained stiffness matrix.

## 7.14.2 PROCEDURE USAGE

Procedure STIFFNESS is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call STIFFNESS ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure STIFFNESS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions. For procedure STIFFNESS, the following table lists each argument, its default value and meaning.

Argument	Default Value	Meaning
түре	TANG	Type of stiffness matrix to form (default: TANG). This argument defines the type of stiffness to form linear material stiffness matrix (MATL), geometric stiffness matrix (GEOM), or the tangent stiffness matrix (TANG).
CONSTRAINT_SET	1	Constraint set number (default: tt 1). This argument selects which constraint set to be used in solving the linear system of equations.
COROTATION	1	Corotation flag
NL_GEOM	0	Geometric nonlinearity flag
NL_LOAD	0	Load nonlinearity flag
NL_MATL	0	Material nonlinearity flag
INPUT_LDI	1	Logical device index with the element stiffness matrices (default: 1).
OUTPUT_LDI	1	Logical device index for the assembled unconstrained stiffness matrix (default: 1).
LOAD_SET	1	Load set number (default: 1). This argument selects which load set to be used as a right-hand-side vector.
LOAD_FACTOR	1.0	Load factor for the basic load system (default: 1.0).
STIFFNESS	K	First word of the dataset containing the assembled unconstrained stiffness matrix (default: K).
DISPLACEMENT		Full dataset name for the displacement vector.
ROTATION		Full dataset name for the rotation vector.

Tables 7.14-1 and 7.14-2 list the datasets used or created by procedure STIFFNESS and the processors invoked by procedure STIFFNESS, respectively.

Table 7.14-1 Datasets Input/Output by procedure STIFFNESS			
Dataset	Description	Input	Output
JDF1.BTAB.1.8	Model Summary	$\checkmark$	
JSEQ.BTAB.2.17	Nodal Elimination Sequence	$\checkmark$	
KMAPnsubs.ksize	Model Connectivity Map	$\checkmark$	
<stiffness>.SPAR.jdf2</stiffness>	Assembled Stiffness Matrix		$\checkmark$

Table 7.14-2 Processors Invoked by procedure STIFFNESS		
Procedure	Туре	Function
VEC	Internal	Vector algebra utilities
ESi	External	Various element processors based on the GEP
к	Internal	Assembles unconstrained stiffness matrix

## 7.14.3 ARGUMENT DESCRIPTIONS

#### 7.14.3.1 <u>TYPE</u>

Type of stiffness matrix to form (default: TANG). This argument defines the type of stiffness to form linear material stiffness matrix (MATL), geometric stiffness matrix (GEOM), or the tangent stiffness matrix (TANG).

#### 7.14.3.2 CONSTRAINT\_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

#### 7.14.3.3 <u>INPUT\_LDI</u>

Logical device index with the element stiffness matrices (default: 1).

## 7.14.3.4 <u>OUTPUT\_LDI</u>

Logical device index for the assembled unconstrained stiffness matrix (default: 1).

## 7.14.3.5 LOAD\_SET

Load set number (default: 1). This argument selects which load set to be used as a right-hand side vector.

#### 7.14.3.6 LOAD\_FACTOR

Load factor for the basic load system (default: 1.0).

## 7.14.3.7 STIFFNESS

First word of the dataset name containing the assembled unconstrained stiffness matrix (default: K).

## 7.14.3.8 DISPLACEMENT

Full dataset name for the displacement vector.

#### 7.14.3.9 ROTATION

Full dataset name for the rotation vector.

## 7.14.3.10 COROTATION

Corotation switch; employed by ESi processors for automatic treatment of geometric nonlinearity due to large rotations (default: 1). Relevant only if problem is geometrically nonlinear. (See Chapter 4 of reference 7.2-1 for an explanation of these options.) If CORO-TATION equals zero, then the corotational operations will be skipped. If COROTATION equals one (low-order option), then the basic corotational transformations will be employed to enable large rotations. If COROTATION equals two (high-order option), then a more accurate (and expensive) treatment of large rotations and consistent linearization than option 1 will be employed.

## 7.14.3.11 <u>ES\_NL\_GEOM</u>

Geometric nonlinearity switch (default: 0). If ES\_NL\_GEOM equals zero (no corotational frames), then the problem is geometrically linear (small displacements/rotations). If NL\_GEOM equals one (low-order option), then the problem is geometrically nonlinear, but elements should use linear strain-displacement relations. Meaningful only if COROTATION > 0, so that large rotations can be handled automatically by the corotational algorithm. If NL\_GEOM equals two (high-order option), then the problem is geometrically nonlinear and elements should use nonlinear element strain-displacement relations. May be used in conjunction with COROTATION > 0 to obtain higher-order accuracy for beam and shell elements that employ moderate-rotation strain-displacement relations.

## 7.14.3.12 <u>NL\_MATL</u>

Material nonlinearity switch (default: 0). If NL\_MATL is greater than zero, then the element is materially nonlinear. If L\_MATL is zero, then the element is materially linear.

## 7.14.3.13 <u>NL\_LOAD</u>

Load nonlinearity switch (default: 0). If NL\_LOAD is greater than zero, then the element loads are displacement dependent. If NL\_LOAD equals zero, then the element loads are not displacement dependent.

## 7.14.4 USAGE GUIDELINES AND EXAMPLES

Procedure STIFFNESS is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

\*call STIFFNESS ( TYPE = MATL ; CONSTRAINT\_SET = 1 ; STIFFNESS = K )

## 7.14.5 LIMITATIONS

None.

## 7.14.6 ERROR MESSAGES AND WARNINGS

None.

#### 7.14.7 PROCEDURE FLOWCHART

STIFFNESS	(main procedure)
ES	(form element stiffness matrices)

## 7.14.8 PROCEDURE LISTING

*procedure STIFFNESS	<pre>( type = TANG nl_geom = 0 nl_matl = 0 nl_load = 0</pre>	;
	displacement rotation corotation = 1	; Input dataset ; Input dataset ;
	<pre>load_factor = 1.0 load_set = 1 stiffness = K input_ldi = 1 output_ldi = 1</pre>	; ; Output dataset ;
*ronark *Ronark *ronark	<pre>constraint_set = 1 Forming [type] Stiff</pre>	
	Element Stiffness Matrices (in EFIL Dataset)	
•call ES (function ldi	= 'FORM STIFFN = [input_ldi] oom = [nl_geom]	

```
es_nl_matl = [nl_matl]
                                              ; --
           es_nl_load = [nl_load]
es_dis_ds = [displacement]
                                              ; --
                                              ; --
           es_rot_ds
                       = [rotation]
                                              ; --
                    = [corotation]
           es_coro
                                              ; --
           es_load_factor = [load_factor]
                                              ; ---
           es_load_set = [load_set] )
  **************
  Assemble Element Stiffness Matrix into System Matrix
  [XQT K
   RESET NAME = [stiffness]
   RESET BLIB = [input_ldi]
   RESET ELIB = [input_ldi]
   RESET HLIB = [input_ldi]
   RESET OUTLIB = [output_1di]
   RESET SPDP = <csm_precision>
+end
```

#### 7.14.9 REFERENCES

7.14-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

# 7.15 Procedure SWITCH\_DS

# 7.15.1 GENERAL DESCRIPTION

Procedure SWITCH\_DS switches two datasets within the same data library. This procedure only uses directives from the command language (see reference 7.7-1).

# 7.15.2 PROCEDURE USAGE

Procedure SWITCH\_DS is used by preceding the procedure name by the \*call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

\*call SWITCH\_DS ( arg1 = val1 ; arg2 = val2 ; ...)

where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure SWITCH\_DS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally *mandatory*, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure SWITCH\_DS, the following table lists each argument, its default value and meaning.

Argument	Default Value	Meaning
DS_1		Source dataset name
DS_2		Target dataset name
LDI	1	Logical device index

# 7.15.3 ARGUMENT DESCRIPTIONS

# 7.15.3.1 LDI

Source logical device index (default: 1). Data library number containing the two datasets DS\_1 and DS\_2.

# 7.15.3.2 DS\_1

Source dataset to be copied from within the data library with a logical device index of LDI to the target dataset named DS\_2.

## 7.15.3.3 DS\_2

Target dataset for copying the source dataset named DS\_1 from within the data library with a logical device index of LD1.

#### 7.15.4 USAGE GUIDELINES AND EXAMPLES

Procedure SWITCH\_DS is used by preceding the procedure name by the \*call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call SWITCH_DS ( ldi=1; ds_1; ds_2 )
```

#### 7.15.5 LIMITATIONS

None.

#### 7.15.6 ERROR MESSAGES AND WARNINGS

None.

#### 7.15.7 PROCEDURE FLOWCHART

Procedure SWITCH\_DS is self contained with no subprocedures.

## 7.15.8 PROCEDURE LISTING

```
*procedure SWITCH_DS ( ldi=1; ds_1; ds_2 )
. CLAMP Procedure to switch two datasets within a data library
 *def/a tmp_ds = xxxx.xxxx.99999.99999
 *rename [ldi], [ds_1] = <tmp_ds>
 *rename [ldi], [ds_2] = [ds_1]
 *rename [ldi], <tmp_ds> = [ds_2]
*end
```

#### 7.15.9 REFERENCES

7.7-1 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

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