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# THE COMPUTATIONAL STRUCTURAL MECHANICS TESTBED PROCEDURES MANUAL 

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## Preface

The purpose of this manual is to document standard procedures of the Computational Structural Mechanics (CSM) Testbed software system. A description of each procedure including its function, commands, data interface, and use is presented.

Periodically, updates to this manual will be released which describe new procedures or changes to existing procedures.

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## CSM Testbed Procedures Manual

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## CSM TESTBED DOCUMENTATION SET

1. Introduction to the Computational Structural Mechanics Testbed NASA TM 89096, 1987
2. Utilities for Master Source Code Distribution: MAX and Friends NASA CR 178383, 1988
3. The Computational Structural Mechanics 'Testbed Architecture:

Volume I - The Language
NASA CR 178384, 1988
4. The Computational Structural Mechanics Testbed Architecture:

Volume II - Directives
NASA CR 178385, 1988
5. The Computational Structural Mechanics Testbed Architecture:

Volume III - The Interface
NASA CR 178386, 1988
6. The Computational Structural Mechanics Testbed Architecture:

Volume IV - The Global-Database Manager GAL-DBM
NASA CR 178387, 1988
7. The Computational Structural Mechanics Testbed Architecture:

Volume V - The Input-Output Manager DMGASP
NASA CR 178388, 1989
8. The Computational Structural Mechanics Testbed User's Manual

NASA TM 100644, 1989
9. The Computational Structural Mechanics Testbed Data Library Description NASA TM 100645, 1988
10. The Computational Structural Mechanics Testbed Generic

Structural-Element Processor Manual
NASA CR 181728, 1989
11. The Computational Structural Mechanics Testbed Procedures Manual NASA CR 100646, 1990
12. The Computational Structural Mechanics Testbed Utility Manual

NASA CR XXXXXX, 1990

### 1.0 Introduction to CSM Testbed Procedures Manual

This manual is designed to assist users in defining and using command procedures to perform structural analyses. It is expected that the user has read Chapters 1 and 2 of the CSM Tcstbed User's Manual (reference 1-1). It is assumed that the user is familiar with terms such as CLIP, macrosymbol, processor, and dataset.

Runstreams are the vehicle used to perform structural analyses with the CSM Testbed. The term "runstream" most commonly refers to the file (or files) used to perform a specific analysis, although it may also refer to input at an interactive session. A runstream will typically contain CLAMP directives and processor commands.

Directives, recognized and processed by CLIP, provide the user with, among other things, a means of defining command procedures. These command procedures, defined using the *PROCEDURE directive, bear some resemblance to FORTRAN subroutines. They may contain branching and looping constructs (implemented using the *DO, *IF, and *WHILE directives) as well as other directives and processor and macroprocessor commands. Command procedures may be given arguments which, unlike FORTRAN subroutine arguments, may be assigned default values. When a command procedure is called (using the *CALL directive) execution control shifts to the command procedure until the last directive (an *END directive) in the procedure is encountered. Once the *END directive is encountered, control returns to the input line in the calling procedure or runstream immediately following the call.

Command procedures, while extremely useful, are not a requirement for performing many types of simple analyses. A command procedure is only required if using the looping or branching constructs (i.e., the *DO, *IF, and *WHILE directives). Procedures should not be used to carry out the computationally intensive activities that are better performed by processors.

This chapter begins with a discussion of CLAMP directives and continues with a discussion of the mechanics of processor execution. A template for linear, static analyses is provided in Section 1.3. Section 1.4 offers some suggestions for creating and using procedures and the CSM Testbed Procedures Manual is described in Section 1.5. Some examples of command procedures are given in Section 1.6.

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### 1.1 CLAMP Directives

Directives are special commands that are recognized and processed by CLIP and are not transported to the processor. A directive is to CLIP like ordinary input is to the processor. A directive is distinguished from ordinary input by beginning with a keyword prefixed by an asterisk. The keyword (directive verb) may be followed by a verb modifier, qualifiers, and parameters, as required by the syntax of the specific directive. See references 1-2 and 1-3 for a complete description of the command language. An interactive help facility, accessed by the *HELP directive, is built in to explain directives. For a complete list with full descriptions, the user is directed to reference 1-3.

A summary of the most useful directives, grouped according to their function in the Testbed execution environment is provided here for easy reference. Detailed descriptions of all directives are provided in reference 1-3.

Table 1.1-1 CLAMP Directive Summary

## Global Data Manager Interface

```
*OPEN Open data library
*CLOSE Close data library
*TOC Print table of contents of library
*PRINT Print table of contents, dataset record contents, or record
    access table of dataset
    Pack a data library, deleting disabled datasets
    Copy datasets or dataset records
    Delete (i.e., disable) dataset or record
    Enable previously deleted or disabled datasets or records
    Returns information on libraries, datasets, or records
    Renames dataset or record
Open data library
Close data library
Print table of contents of library
Print table of contents, dataset record contents, or record access table of dataset
*PACK
*COPY
*DELETE
*ENABLE
*FIND
*RENAME
Renames dataset or record
Pack a data library, deleting disabled datasets
Copy datasets or dataset records
Delete (i.e., disable) dataset or record
Enable previously deleted or disabled datasets or records
Returns information on libraries, datasets, or records
```


## Command Procedure Management

*SET PLIB

Set procedure library for residence of command procedures
Redirects input to a callable procedure ("calls" a procedure
*CALL Initiates definition of command procedure with optional argument replacement)

## Nonsequential Command Processing

## *PROCEDURE <br> *PROCEDURE

*CALL

```
*IF Conditional branching constructConditional branching construct
Conditional branching construct
```

```
*ELSE
*ELSEIF
*ENDIF
*DO
    Looping construct
*ENDDO
```

Looping construct

```
*ELSEIF
*ENDIF
*DO Looping construct
*ENDDO
```

| *WHILE <br> *ENDWHILE | While-looping construct |
| :---: | :---: |
| * JUMP | Transfer control to specified label |
| *RETURN | Force exit from command procedure |
| *END | Terminate definition of command procedure |
|  | Macrosymbol Directives |
| *DEFINE | Define a macrosymbol or macrosymbol array |
| * UNDEFINE | Delete macrosymbol(s) |
| *SHOW MACRO | Show macrosymbols |
| *G2M | Define a macrosymbol from a database entity |
| *M2G | Create a database entity from the value of a macrosymbol |
| Built-in macrosymbols | Common constants, mathematical functions, generic functions, reserved variables, boolean functions, logical functions, string catenator, string matchers, and status macros |

*RUN
*STOP
Start execution of another program
Stops RUN-initiated execution and restarts the parent processor

## General Directives

Lists information from NICE HELP file
Sets specified NICE control parameters
Shows specified NICE control parameters
Redirects input to a text file
Print remark line
Unload contents of GAL library to an ASCII file
Load contents of GAL library from an ASCII file

### 1.2 Executing Processors

There are two types of analysis modules, or processors, associated with the Testbed: internal processors, which have been installed as part of the macroprocessor, and external processors. Either type of processor may be executed using the macroprocessor execute command, [XQT. The user merely appends the processor name to the [XQT and the named processor will begin execution. For example,

## [XQT INV

will start the execution of the processor INV. In order to use this method of execution for external processors, the executable version of the processor must reside in the default directory being used by the macroprocessor or in other pre-defined directories depending on computer system syntax. In addition, the name of an external processor cannot be the same as the name of any internal processor.

External processors may also be executed using the *RON directive. When this directive is used, a full pathname may be given so that external processors may be kept anywhere. For example, under the VMS operating system,

> *RUN duaO: [testbed.extp]INVX
will begin execution of processor INVX, located in dua0: [testbed.extp].
Once a processor (internal or external) is running, it will begin to accept input according to the requirements of the individual processor as described in Chapters 4 through 14 of the CSM Testbed User's Manual (Ref. 1-1). The processor will continue accepting input until either another [XQT, a STOP, or a $*$ STOP is encountered. If a STOP occurs, execution will proceed to completion of the processor's assigned task after which the processor named on the next [XQT command begins execution. If an [XQT occurs, execution will proceed to completion of the processor's assigned task after which the processor named on that last [XQT begins execution. A *STOP terminates processor execution immediately.

The following runstream provides an example of processor, macroprocessor, and CLIP interaction. The linear, static analysis, a very simple example, with one procedure definition, has been taken from the demonstration problem set library. The procedure is defined so that the *DO directive may be used in defining joint locations (recall that the *DO directive may only be used within a command procedure). Note also that the procedure is completely defined before it has been called. This is an absolute requirement - procedures must be defined before they are called.

```
*procedure demol
*open 1 demo1.l01/new
[xqt TAB
    START 5
    JOINT LOCATIONS
    *do $i = 1,5
            node x y z . Comment
            <$i> 0. 0. <10.*<$i>> . TAB Input
        *enddo
        Directive to end input loop
    MATERIAL CONSTANTS
    . Direct TAB input
    1 10.E+6 . 3 . 101 .1E-4
    BEAM ORIENTATIONS
    11111.
    E21 SECTION PROPERTIES
    TUBE 1 2. 2.25
    CONSTRAINT DEFINITION 1
    ZERO 12 3456
            1
[xqt ELD . Macroprocessor command to execute ELD
    E21 . Direct ELD Input
    12
    2 3
    34
    45
[xqt TOPO . Macroprocessor command to execute TOPO
[xqt E . Macroprocessor command to execute E
[xqt EKS . Macroprocessor command to execute EKS
[xqt K . Macroprocessor command to execute K
[xqt INV . Macroprocessor command to execute INV
    ALPHA
        CASE TITlES
        1'TRANSVERSE LOAD
        2'AXIAL LOAD
        SYSVEC
        APPLIED FORCES
            CASE 1
        I=2
        J=5
        1000.
            CASE 2
        I=3
        J=5
        10000.
    [xqt SSOL . Macroprocessor command to execute SSOL
    [xqt GSF
[xqt PSF
            stop
*end
*call demo1 . Directive calling procedure demo1
[xqt exit . Macroprocessor command to end execution
```

It is important to note that while directives may be used to generate input data, the directives themselves do not provide input to the processors. The $* D 0$ directive, used in the JOINT LOCATIONS subprocessor of processor TAB, provides the user with a means of automatically generating TAB input; the line containing the $* \mathrm{do} \$ \mathrm{i}=1,5$ provides no information to processor TAB but is meaningful to CLIP. The result of executing this *DO directive is to produce five input lines for consumption by processor TAB.

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### 1.3 Runstream Organization

While the Testbed is highly modular, certain processors do depend on information generated by other processors, thus there is some degree of interdependence among the installed processors. In many cases, the order in which processors must be executed is the same as the order in which they appear in the CSM Testbed User's manual (ref. 1-1); this is not entirely true when using one or more of the independent element processors. The following section provides a template for performing a linear static analysis using one or more independent element processors (Section 1.3.1).

### 1.3.1 RUNSTREAM FOR INDEPENDENT ELEMENT PROCESSORS

The generic element processor template was developed to provide greater flexibility to element developers. It does however, add a level of complexity to the analysis, even to a simple linear, static analysis. This complexity is kept hidden to the average user by the use of a "cover procedure." The procedure name is ES and details of its use may be found in reference 1-4. Essentially, procedure ES manages the execution of the independent element processors, ESi.

Listed below is the order of processor and procedure execution for a linear static analysis using one or more of the independent element processors. Following the list is an example (the same example used in the previous section) which calls procedure ES.

1. Procedure ES. Call procedure ES to define element parameters and several global macrosymbols which may be used to automate the definition of joint locations and element connectivity. This call must be made for each different element type in the model, regardless of the number of element processors used.
2. Processor TAB. Define joint locations, constraints, reference frames.
3. Processor AUS. Build tables of material and section properties.
4. Processor LAU. Form constitutive matrix.
5. Processor ELD. Define elements. Element definitions include element connectivity, element material reference frame number, element section type number.
6. Processor E. Initialize element datasets; create the dataset which will contain all important element information (e.g., intrinsic coordinates, element-to-global transformations, intrinsic stiffness matrices).
7. Procedure ES. Initialize element matrices.
8. Procedure ES. Calculate element intrinsic stiffness matrices.
9. Processor RSEQ or PFM. Resequence nodes for minimum total execution time.
10. Processor TOPO. Form maps which guide the assembly and factorization of system matrices.
11. Processor K. Assemble system stiffness matrix.
12. Processor INV. Factor system stiffness matrix.
13. Processor AUS. Create applied nodal loading.
14. Processor SSOL. Solve for static displacements.
15. Procedure ES. Calculate element stress resultants.
16. Post-process using any of the following processors: VPRT, PRTE, PLOT, CONT, T2PT.

### 1.3.2 EXAMPLE RUNSTREAM

The following runstream provides an example of a very simple linear static analysis. The problem is to calculate the stress in an isotropic flat plate subjected to a uniform endshortening. One-fourth of the plate is modeled and symmetry boundary conditions are applied.

```
#set echo=off . Do not echo input
*add [testbed.proclib]GENUTIL.PRC . ADD file containing procedure ES
*open/new 1, flat_plate . Open data library
*def/a es_name == 'EX91' . Element name
*def/a es_proc == 'ES1', . Element processor name
*call ES ( function = 'DEFINE ELEMEHTS'; es_proc = <es_proc/p>; --
    es_name = <es_name/p\rangle
Exqt TAB
    START 256 . Twenty live nodes total, dof 6 zero
    JOINT LOCATIONS . Enter joint locations
\begin{tabular}{llllllllll}
1 & 0.0 & 0.0 & 0.0 & 2.5 & 0.0 & 0.0 & 5 & 1 & 5 \\
5 & 0.0 & 2.5 & 0.0 & 2.5 & 2.5 & 0.0 & &
\end{tabular}
    CONSTRAIMT DEFINITION 1 Constraints:
        symm plane=1 . Plane 2,3 plane of symmetry
        symm plane=2 . Plane 1,3 plane of symmetry
        zero 3:1 . Constrain center W
        nonzero 1 : 5,25,5 . Apply displacement at x=1x edge
    [xqt AUS . Material and Section properties
    *def/e g = 3.84615e+6
    TABLE(NI=16,NJ=3): OMB DATA 1 1 Table of material properties
        I=1,2,3,4,5,6,7,8,9
        J=1: 10.0E+6 . 30 10.0E+6 <g> <g\rangle\langleg\rangle 0.0 0.0 .1
```

TABLE ( $\bar{N} \overline{1}=\overline{3}, \mathrm{NJ}=1, \mathrm{itype}=0$ ) : LaM OMB 11
$\mathrm{J}=1$ : 2.10 .00
[xqt LAU . Generate constitutive matrix
. NOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt
. were all globally defined by procedure ES the first time the procedure was called.
[xqt ELD
. Define elements

```
    *def/i nst = <<es_nip>*<es_nstr>>
    EXPE <es_name> <es_nen> <es_opt> <es_nen> 6 <nst> 1 101 2
    NSECT = 1
    1
```

[xqt E
. Initialize element datasets
stop
*open 1
*call ES (function='INITIALIZE') . Initialize element matrices
*call ES (function='FORM STIFFNESS/MATL') . Form intrinsic stiffness matrices
[xqt RSEQ . Resequence
[xqt TOPD . Create maps
[xqt K . Assemble global stiffness matrix
[xqt INV
online=2
[xqt AUS . Form applied loading
sysvec : appl moti
i=1: $J=5,25,5: \quad-0.001$
[xqt SSOL . Solve for static displacements
stop
*open 1
*call ES (function = 'FORM STRESS'; -- . Calculate element stresses
es_dis_ds = STAT.DISP.1.1)
[xqt VPRT . Print static displacements
format=4
print STAT DISP
[xqt PRTE . Print element stresses
reset $\operatorname{seg} 1=7, \operatorname{seg} 2=7$
[xqt exit

### 1.4 Creating and Using Procedures

### 1.4.1 CREATING A PROCEDURE

Most directives are so simple that they may easily be entered from a keyboard terminal. One could try to define simple procedures in exactly that manner. There are two problems with this approach:

1. A keyed-in sequence of directives and commands is volatile and is not saved unless a $\log$ file has been opened, although a procedure definition is compiled and saved.
2. Post-facto editing is impossible; once the return key it pressed, the line is gone.

These disadvantages become increasingly serious in long or involved procedures. The most practical way to create most procedures is to use a text editor. Once the procedure source text is ready on a data file, it can be inserted into the command source stream with the *ADD directive.

### 1.4.2 RESIDENCE OF CALLABLE PROCEDURE ELEMENTS

When CLIP encounters a *PROCEDURE directive, it enters directive mode and does not exit until the *END directive is detected. The result of this process is an "object" version of the procedure, known as a callable procedure element. CLIP can store a callable procedure element in one of two residence media:

1. An ordinary direct-access formatted file created through a FORTRAN 77 OPEN statement. All records of such a file have the same length (namely 80 characters) and contain one data line. The file name is the same as the procedure name except on a VMS VAX where a .DAT is appended to the procedure name to create the file name. For example, a procedure named GEN_PLATE will generate a file named GEN_PLATE.DAT on a VMS VAX and a file named GEN_PLATE on other machines. If the *SET PLIB directive has not been used prior to the *PROCEDURE directive, direct-access files will be created automatically.
2. A data library managed through the global data manager. A callable procedure is stored as a text group. In order to store procedures in a data library, the *SET PLIB directive must be used.
The text of a callable procedure element is basically a copy of the source procedure body, prefaced by three linkage tables. These tables store argument names, argument default text, labels (explicit or generated) and their locations within the body of the procedure. NEVER tamper with a callable procedure element. If the procedure must be changed, change the source and reprocess the file.

### 1.4.3 USING A PROCEDURE

Callable procedure elements are accessed through the *CALL directive. Text substitution is controlled by the argument specification mechanism. In a command procedure reference, text is passed instead of addresses to data. The text supplied in the *CALL directive is replaced before the command is interpreted. In addition, arguments not supplied in the *CALL, assume the default values given in the *PROCEDURE definition. A procedure body may include calls to other procedures, or may even call itself, with the ensuing call tree extending down several levels.

### 1.5 The CSM Testbed Procedures Manual

A GAL library which contains the callable procedure elements for all of the procedures described in the following sections (2-9) of this manual is read-accessible to all Testbed users. Separate subdirectories under the pre directory contain solution procedures (see Chapter 3), model generation procedures (see Chapter 2), utility procedures (see Chapter 6), and postprocessing procedures (see Chapter 7). This directory structure is the same across various computer systems with differences only in the description of the path name for each subdirectory. On a VMS VAX computer, this file is referred to by the name CSM_PRC:PROCLIB.GAL; on UNIX-type computers, it is referred to by the name , \$CSM_PRC/proclib.gal'. If the user does not need to define any new procedures for use in a particular Testbed runstream, this file can be used as the procedure library by including the following commands in the runstream:

```
*set plib = 28
*open 28 CSM_PRC:PROCLIB.GAL /READ (on VMS)
    or
*open 28 '$CSM_PRC/proclib.gal' /READ
```


## (on VMS)

(on UNIX)

The source code for the procedures resides in subdirectories under the one which contains proclib.gal. These procedures are also read-accessible to all Testbed users. They can be included in the user's private procedure library by placing commands like the following in a Testbed runstream:

```
*set plib=28
*open 28 proclib.gal /NEW
*add GEN_UTIL:ES.CLP (on VMS)
    or
*add '$GEN_UTIL:es.clp' (on UNIX)
```

or alternatively; on UNIX:

```
cp $CSM_PRC/proclib.gal.
chmod 755 proclib.gal
testbed
*set plib=28
*open 28 proclib.gal
*add local.prc
•
•
```

or on VMS:
\$COPY CSM_PRC:PROCLIB.GAL []
\$Testbed
*set plib=28
*oper 28 proclib.gal
*add local.prc
-
-
where local.pre is the CLAMP source file for personal procedure(s).

### 1.6 Examples

This section provides several examples of the use of procedures. For the sake of consistency, where files are discussed, VAX/VMS filenames have been used. The filename convention used is that $\bar{a}$ file with $a *$. CLP extension contains a single procedure, while a file with a *.PRC extension contains multiple procedures. The *ADD and the driving *CALL directives typically appear in files with the *.COM extension.

### 1.6.1 A SIMPLE EXAMPLE

As an introductory example, an annotated procedure is presented which may be used to run a variety of elements through the same flat plate problem. In most applications, this procedure would be kept in a file by itself and that file would be added (using the *ADD directive) to a much shorter runstream located in an execution control file. The procedure and a VAX/VMS execution control file are listed in the following subsections.

### 1.6.1.1 The Procedure File

The following procedure is kept in a file named flat_PLATE.CLP.

```
*procedure FLAT_PLATE ( es_proc ; es_name )
. ARGUMENTS :
- es_proc: Independent element processor name
. es_name: Element name
*if <ifeqs ([es_name];E43)>/then
    *def/i es_nen \(=4\)
*else
    *call ES (function = 'DEFINE ELENENTS'; es_proc = [es_proc]; --
        es_name = [es_name])
*endif
-
[xqt TAB
    START 256 . Twenty-five joints; dof 6 zero
    JOINT LOCATIONS . Define joint locations
    \(10.0 \quad 0.0 \quad 0.0 \quad 2.5 \quad 0.0 \quad 0.0 \quad 5 \quad 15\)
    \(\begin{array}{lllllll}5 & 0.0 & 2.5 & 0.0 & 2.5 & 2.5 & 0.0\end{array}\)
        CONSTRAINT DEFINITION 1 . Constraints:
    symm plane=1 . Plane 2,3 plane of symmetry
    symm plane=2 . Plane 1,3 plane of symmetry
    zero 3:1 . Constrain center w
    nonzero 1 : 5,25,5 Apply displacement at \(x=1 x\) edge
```

[xqt AUS
-
*def/e g = 3.84615e+6
TABLE ( $\mathrm{NI}=16, \mathrm{NJ}=3$ ): OMB DATA 11 . Define material properties
$\mathrm{I}=1,2,3,4,5,6,7,8,9$
$\mathrm{J}=1: 10.0 \mathrm{E}+6.3010 .0 \mathrm{E}+6\langle\mathrm{~g}\rangle\langle\mathrm{g}\rangle\langle\mathrm{g}\rangle 0.0$ 0.0 . 1
. Define Section properties
TABLE ( $\mathrm{NI}=3, \mathrm{NJ}=1$, itype $=0$ ) : LAM OMB 11
$\mathrm{J}=1$ : 2.10 .00
[xqt LAU
. Form constitutive matrix
*if <ifeqs ([es_name];E43)>/then reset $\mathrm{SPAR}=-1$
*endif
[xqt ELD . Define elements
*if <ifeqs ([es_name];E43)>/then E43
*else
. NOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt were globally defined by procedure ES the first time the procedure was called.
*def/inst $=$ <<es_nip>*<es_nstr>> . Number of stress resultants
EXPE [es_name] <es_nen> <es_opt> <es_nen> 6 <nst> 11012
*endif
NSECT = 1
*if \lles_nen>/eq $4>/$ then
12761444 . Element connectivity for 4-node olts
*elseif \lles_nen>/eq 9 >/then
$\begin{array}{llllllllll}1 & 3 & 13 & 11 & 2 & 8 & 12 & 6 & 7 & 2\end{array}$. Element connectivity for 9-node elts
*endif
[xqt E . Initialize all element datasets
stop
*open 1
*if <ifeqs ([es_name];E43)> /then . Form intrinsic stiffness matrices:
[xqt EKS . for E43
*else
*call ES (function='IMITIALIZE')
*call ES (function='FORM STIFFMESS/MATL') . for other elements
*endif
[xqt RSEQ . Resequence
[xqt TOPO . Create maps
[xqt K . Assemble system stiffness matrix
[xqt AUS . Form applied loading
sysvec : appl moti
$i=1: J=5,25,5: \quad-0.001$

```
[xqt INV . Factor stiffness matrix
    online=2
[xqt SSOL . Solve for static displacements
    stop
    *open 1
*if <ifeqs([es_name];E43)>/then . for E43
    [xqt GSF
    [xqt PSF
        reset display=2
*else . for other elements
    *call ES ( function = 'FORM STRESS'; es_dis_ds = STAT.DISP.1.1)
*endif
[xqt VPRT . Print displacements
    format=4
    print STAT DISP
*end
```


### 1.6.1.2 The Execution Control File

The file FLATPLATE. COM, listed below, contains no procedures, only the *ADD and the *CALL to the procedure defined in the previous section.

```
$ testbed ! Execute Testbed macroprocessor
*get echo off
*open 1 flat_plate. }101\mathrm{ . Open data library
*add flat_plate.clp . Add procedure file BEFORE call
*call FLAT_PLATE ( es_proc=ES1; es_name=Ex97)
-
[xqt EXIT . Exit macroprocessor
```


### 1.6.2 MACROSYMBOL USAGE EXAMPLE

The runstream described in this section still contains only one procedure; that procedure is somewhat more complicated than the procedure of the first section although the problem to be solved is the same. The number of elements along $x$ and $y$ have been parameterized to allow for mesh convergence studies for the various elements. The logic of the procedure remains the same; there are simply more macrosymbol definitions. The procedure and the execution control file are listed in the following subsections.

### 1.6.2.1 The Procedure File

The following procedure is kept in a file named FLAT_PLATE.CLP.
*procedure FLAT_PLATE (es_proc=ES1; es_name=Ex97;-- )

NEL_X ; NEL_y )

ARGUMENTS:

```
es_proc: Independent element processor name
es_name: Element name
NEL_x: Number of elements in the x direction
NEL_y: Number of elements in the y direction
*if <ifeqs([es_name];E43)> /then
    *def/i es_nen = 4
*else
    *call ES ( function = 'DEFINE ELEMENTS'; es_proc = [es_proc]; --
            es_name = [es_name])
*endif
- Define necessary macrosymbols
#if << es_nen >/eq 4 >/then . If 4-node elements are used:
    *def/i nn_x = <<[NEL_x]> + 1 > . Num. nodes in x-direction
    *def/i nn_y = <<[NEL_y]> + 1 > . Num. nodes in y-direction
    #def/i nn_total = <<nn_x>*\langlenn_y>> . Num. nodes total
*elseif << es_nen >/eq 9 >/then
If 9-node elements are used:
    #def/1 nn_x = <2&\langle[NEL_x]> + 1 > . Num. nodes in x-direction
    *def/i nn_y = <2*<[NEL_y]> + 1 > . Num. nodes in y-direction
    #def/i nn_total = <<nn_x>*\langlenn_y>> . Num. nodes total
*endif
.
[xqt TAB
```

        START <nn_total>6 6 Twenty-five joints; dof 6 zero
        JOINT LOCATIONS . Define joint locations
    | 1 | 0.0 | 0.0 | 0.0 | 2.5 | 0.0 | 0.0 | $\left\langle n n_{-} x\right\rangle$ | <nn_y> |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left\langle n n_{-} x\right\rangle$ | 0.0 | 2.5 | 0.0 | 2.5 | 2.5 | 0.0 |  |  |

        CONSTRAINT DEFINITION 1 . Constraints
        symm plane=1 . Plane 2,3 plane of symmetry
        symm plane=2 . Plane 1,3 plane of symmetry
        zero 3: 1 . Constrain center \(\mathbb{W}\)
        nonzero 1 : <nn_x>,<nn_total>,<nn_x> . Apply displacement at \(x=1 x\) edge
    [xqt AUS
*def/e g = 3.84615e+6
TABLE(NI=16, $\mathrm{NJ}=3$ ): OMB DATA 11 . Define material properties
$I=1,2,3,4,5,6,7,8,9$
$\mathrm{J}=1: 10.0 \mathrm{E}+6.3010 .0 \mathrm{E}+6\langle\mathrm{~g}\rangle\langle\mathrm{g}\rangle\langle\mathrm{g}\rangle 0.0 \quad 0.0 .1$
- Define Section properties
TABLE ( $\mathrm{NI}=3$, $\mathrm{NJ}=1$, itype=0): LAM OMB 11
$\mathrm{J}=1: 2.10 .00$

```
[xqt LAU . Form constitutive matrix
    *if <ifeqs([es_name]; E43)>/ then
        reset SPAR=-1
    *endif
[xqt ELD . Define alements
    *if <ifeqg([es_name]; E43)>/ then
        E43
    *else
. NOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt
                    were globally defined by procedure ES the first time
                    the procedure was called.
        *def/i nst = <<es_nip>*<es_nstr>> . Number of stress resultants
        EXPE [es_name] <es_nen> <es_opt> <es_nen> 6 <nst> 1 101 2
    *endif
        NSECT = 1
    *if <<es_nen>/eq 4 >/then
```

            *def/i j1 = 1
            *def/i j2 = 2
            *def/i j3 \(=\left\langle\langle j 2\rangle+\left\langle n n \_x\right\rangle\right\rangle\)
            *der/i j4 \(=\left\langle\langle j 1\rangle+\left\langle n n_{-} x\right\rangle\right\rangle\)
                                    . Element connectivity for 4-node elts
            <j1> <j2> <j3> <j4> 1 < [NEL_x]> <[NEL_y]>
        *elseif \lles_nen>/eq 9 >/then
                                    . Use 9-node element mesh generator
            *def/i j1 = 1
            *def/i j5 = 2
            *def/i j2 = 3
            *def/i \(\mathrm{j} 8=\left\langle\langle j 1\rangle+\left\langle n n_{-x}>\right\rangle\right.\)
            *def/i j9 = <<j 5\(\rangle+\left\langle n n_{-x}>\right\rangle\)
            *def/i j6 = <<j2> + <nn_x>>
            *def/i j4 \(=\left\langle\langle j 8\rangle+\left\langle n n_{-x}\right\rangle\right\rangle\)
            *def/i j7 \(=\left\langle\langle j 9\rangle+\left\langle n n_{-x}\right\rangle\right\rangle\)
            *def/i j3 = <<j6> + 〈nn_x>>
            <j1> <j2> <j3> <j4> <j5> <j6> <j7> <j8> <j9> 1 <[NEL_x]> <[NEL_y]>
    *endif
    [xqt E
. Initialize all element datasets
stop
*open 1
*if <ifeqs([es_name]; E43)>/ then . Form intrinsic stiffness matrices
[xqt EKS
Element connectivity for 9-node elts
for E43
*else
*call ES (function='INITIALIZE')

```
    *call ES (function='FORM STIFFNESS/MATL') . for other elements
*endif
[xqt RSEQ
                                    .Resequence
                                    - Create maps
xqt TOPO
    . Assemble system stiffness matrix
[xqt K
[xqt AUS
    sysvec : appl moti
    i=1: J=\langlenn_x\rangle,\langlenn_total>,\langlenn_x\rangle: -0.001
[xqt INV
    . Factor stiffness matrix
online=2
[xqt SSOL
. Solve for static displacements
    stop
    *open 1
    Calculate stresses
*if <ifeqs([es_name]; E43)>/ then . for E43
    [xqt GSF
    [xqt PSF
        reset display=2
    *else . for other elements
    *call ES ( function = 'FORM STRESS'; es_dis_ds = STAT.DISP.1.1)
    *endif
    [xqt VPRT
        format=4
        print STAT DISP
    *end
```


### 1.6.2.2 The Execution Control File

The file, FLATPLATE.COM, listed below contains no procedures, only the*ADD and the *CALL to the procedure defined in the previous section.

```
$ testbed ! Execute Testbed macroprocessor
*set echo off
*open 1 flat_plate. }10
. Open data library
*add flat_plate.clp . Add procedure file BEFORE call
*call FLAT_PLATE ( es_proc=ES1; es_name=Ex97; --
    Nel_x=4; Nel_y=4 )
[xqt EXIT . Exit macroprocessor
```

One may notice that, except for the two extra arguments (NEL_x and NEL_y) in the *CALL directive, this file is the same as the FLATPLATE. COM file of the last section.

### 1.6.3 A MULTIPLE PROCEDURE EXAMPLE

In many cases, it may be to the user's advantage to build and maintain a procedure library which may be used for classes of problems. For example, in a solution library, one may keep procedures for providing linear static solutions, buckling eigenvalues, and nonlinear static solutions. In this section, the procedure of the previous section is split up into three procedures - PLATE MODEL, PLATE_BC, and L STATIC - which generate the model, generate the boundary conditions, and perform the linear, static solution respectively. The three procedures are kept in two files: L_STATIC.CLP (contains only procedure L_STATIC) and flatplate. pRC (contains Plate_model and Plate_bc). Finally, the file flatplate.com uses the *ADD directive to add the two files and the *CALL directive to call the procedures.

### 1.6.3.1 The Model Generation Procedures

The following two procedures, PLATE_MODEL and PLATE_BC, are, for the sake of the example to be kept in a file named FLATPLATE. PRC. Note that the boundary conditions and applied loads are both in the procedure PLATE BC and that if other boundary conditions were desired, this procedure could be decoupled from the model generation procedure and stored in a separate file. In that case, the procedure name could be passed as an argument to PLATE MODEL which would then call the passed name instead of PLATE_BC.

```
*procedure PLATE_MODEL ( es_proc ; es_name ; --
                                    NEL_x ; NEL_y )
ARGUMENTS:
- es_proc: Independent element processor name
. es_name: Element name
. NEL_x: Number of elements in the x direction
. NEL_y: Number of elements in the y direction
•
*if <ifeqs([es_name];E43)>/then
    *def/i es_nen = 4
*else
    *call ES ( function = 'DEFINE ELEMENTS'; es_proc = [es_proc]; --
                es_name = [es_name])
*endif
. Define necessary macrosymbols
*if << es_nen > /eq 4 >/then . If 4-node elements are used:
    *def/i nn_x = <<[NEL_x]> + 1> > . Num. nodes in x-direction
    *def/i nn_y = <<[NEL_y]> + 1> . Num. nodes in y-direction
    *def/i nn_total = <<nn_x>*<nn_y>> . Num. nodes total
*elseif << es_nen > /eq 9 > /then . If 9-node elements are used:
    *def/i nn_x = <2*<[HEL_x]> + 1 > . Num. nodes in x-direction
    *def/i nn_y = <2*<[NEL_y]> + 1 > . Num. nodes in y-direction
    *def/i nn_total = <<nn_x>*<nn_y>> . Num. nodes total
*endif
```

[xqt TAB

```
        START <nn_total> 6 . Twenty-five joints; dof 6 zero
        JOINT LOCATIONS . Define joint locations
        1 0.0 0.0 0.0
```

        Call boundary condition procedure
    *call PLATE_BC ( nn_x = <nn_x>; -- . to set up loads and b.c.'s
nn_total $=$ <nn_total>)
[xqt AUS
*def/eg = 3.84615e+6
TABLE ( $\mathrm{NI}=16, \mathrm{NJ}=3$ ) : OMB DATA 11 . Define material properties
$\mathrm{I}=1,2,3,4,5,6,7,8,9$
$\mathrm{J}=1: 10.0 \mathrm{E}+6.3010 .0 \mathrm{E}+6\langle\mathrm{~g}\rangle\langle\mathrm{g}\rangle\langle\mathrm{g}\rangle 0.00 .0 .1$
. Define Section properties
TABLE ( $\mathrm{NI}=3, \mathrm{NJ}=1$, itype=0): LAM OMB 11
$\mathrm{J}=1$ : 2 . 10.00
[xqt LaU
. Form constitutive matrix
*if <ifeqs([es_name]; E43)>/then
reset SPAR=-1
*endif
[xqt ELD
. Define elements
*if <ifeqs ([es_name]; E43)>/then
E43
E43 elements
*else
. HOTE -- The macrosymbols es_nip, es_nstr, es_nen, and es_opt
were globally defined by procedure ES the first time
the procedure was called.
*def/inst $=\left\langle\left\langle e s \_n i p\right\rangle *\left\langle e s \_n s t r\right\rangle\right\rangle$. Number of stress resultants
EXPE [es_name] <es_nen> <es_opt> <es_nen> 6 <nst> 11012
*endif
NSECT $=1$
*if \lles_nen>/eq 4 >/then
. Use 4-node element mesh generator
*der/i j1 = 1
*def/i j2 = 2
*def/i j3 $=\left\langle\langle j 2\rangle+\left\langle n n_{-} x\right\rangle\right\rangle$
*def/i $j 4=\left\langle\langle j 1\rangle+\left\langle\pi n_{-} x\right\rangle\right\rangle$
Element connectivity for 4-node elts
<j1><j2><j3><j4> 1 <[HEL_x]> <[NEL_y]>
*elseif \lles_nen>/eq 9 >/then
. Use 9-node element mesh generator

```
        *def/i j1 = 1
        *def/i j5 = 2
        *def/i j2 = 3
        *def/i j8 = <<jl>> + <nn_x>>
        *def/i j9 = <<j5> + <nn_x>>
```



```
        *def/i j4 = <<j8> + <nn_x>>
        *def/i j7 = <<j9> + \langlenn_x>>
        *def/i j3 = <<j6> + <nn_x>>
        . Element connectivity for 9-node elts
        <j1> <j2> <j3> <j4> <j5> <j6> <j7> <j8> <j9> 1 <[NEL_x]> <[NEL_y]>
        *endif
*end
*procedure PLATE_BC ( nn_x ; nn_total )
[xqt TAB
    CONSTRAINT DEFINITION 1 . Constraints
        symm plane=1 . Plane 2,3 plane of symmetry
        symm plane=2 . Plane 1,3 plane of symmetry
        zero 3: 1 . Constrain center w
        nonzero 1 : [nn_x],[nn_total],[nn_x] . Apply displacement at x=lx edge
[xqt AUS . Form applied loading
    sysvec : appl moti
    i=1: J=[nn_x],[nn_total],[nn_x]: -0.001
*end
```


### 1.6.3.2 The Linear Static Analysis Procedure

The following procedure performs the linear static analysis for models using either SPAR E43 elements or elements implemented using the generic element processors. The procedure will be kept in a file named L_STATIC.CLP.

```
*procedure L_STATIC (es_name)
[xqt E \(\quad\). Initialize all element datasets
```

```
*if <ifeqs([es_name]; E43)> /then . Form intrinsic stiffness matrices
    [xqt EKS . for E43
*else
    *call ES (function='INITIALIZE')
    *call ES (function='FORM STIFFNESS/MATL') . for other elements
*endif
[xqt RSEQ . Resequence
[xqt TOPO . Create maps
[xqt K
[xqt INV
. Assemble system stiffness matrix
. Factor stiffness matrix
        online=2
[xqt SSOL . Solve for static displacements
        stop
        *open 1
*if <ifeqs([es_name]; E43)> /then . for E43
        [xqt GSF
        [xqt PSF
            reset display=2
*else . for other elements
    *call ES ( function = 'FORM STRESS'; es_dis_ds = STAT.DISP.1.1 )
*endif
[xqt VPRT . Print displacements
    format=4
    print STAT DISP
*end
```


### 1.6.3.3 The Execution Control File

The following file, FLATPLATE.COM, contains no procedures; it adds the two procedure files and calls the model generation and analysis procedures, PLATE_MODEL and L_STATIC.

```
$ testbed ! Execute Testbed macroprocessor
*set echo off
*open 1 flat_plate. 101 . Open data library
#add flatplate.prc . Add procedure files BEFORE calls
*add l_static.clp
                            - Generate model
#call PLATE_MODEL ( es_proc=ES1; es_name=Ex97;--
    nel_x=4; nel_y=4 )
                            . Solve for static solution
*Call L_STATIC ( es_name=Ex97 )
[xqt EXIT . Exit macroprocessor
```

It should be emphasized that the procedure L_STATIC may be used for any linear, static analysis using either the original SPAR elements or elements implemented using one or more of the Independent Element Processors. The procedure is not limited to SPAR E43
elements as no element specific operations are being performed; element specific operations are performed in the model definition procedure(s).

By splitting the analysis into procedures, the model generation and solution have been decoupled allowing the solution procedure to be used for many different models. The advantages of this approach include the fact that a solution procedure need only be written once rather than once for each problem. It is highly recommended that the user organize procedures in this fashion.

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### 1.7 References

1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM 100644, October 1989.

1-2 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume I-The Language. NASA CR 178384, December 1988.

1-3 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

1-4 Stanley, Gary and Nour-Omid, Shahram: The Computational Structural Mechanics Testbed Generic Structural-Element Processor Manual. NASA CR 181728, March 1990.

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### 2.0 Preprocessing Procedures

The five procedures documented in this chapter are general modeling procedures for specific structural geometries.

Table 2.0-1 Summary of Preprocessing Procedures

| Procedure Name | Preprocessing Function |
| :--- | :--- |
| GEN_BEAM | Generate 1-D models of straight beams using beam <br> elements |
| GEN_CANTILEVER | Generate 2-D models of a straight cantilever beam <br> using plate/shell elements. Using the default values <br> for the procedure arguments, the straight cantilever <br> beam problem from the MacNeal-Harder test cases is <br> generated. |
| GEN_CURVED_BM | Generate 2-D models of a curved (circular) beam us- <br> ing plate/shell elements. Using the default values for <br> the procedure arguments, the curved beam problem <br> from the MacNeal-Harder test cases is generated. |
| GEN_PLATE | Generates 2-D models for general quadrilateral <br> plates. |
| GEN_SHELL | Generates 2-D models for general shells and curved <br> surfaces. |

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### 2.1 Procedure GEN_BEAM

### 2.1.1 GENERAL DESCRIPTION

This section describes a procedure which generates models of a straight beam using onedimensional beam elements.

### 2.1.2 PROCEDURE USAGE

Procedure GEN_BEAM may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
*call GEN BEAM ( arg1 = val1 ; arg2 = val2 ; ...)
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (-) may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN_BEAM are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument | Default Value |
| :--- | :---: |
|  | ES6 |
| ES_PROC | E210 |
| ES_NAME | 3 |
| NODES_X | 10. |
| LENGTH_X | 120. |
| E | 0. |
| NU | 1.0 |
| AREA | 1. |
| INERT_1 | 10. |
| INERT_2 | 1. |
| INERT_TORSIONAL | BEAM_BC |

Meaning<br>Select element processor<br>Select element within ELT_PROC<br>Number of nodes in $x$-direction<br>Length of beam<br>Young's elastic modulus<br>Poisson's ratio<br>Cross-sectional area<br>Principal moment of inertia, $\mathrm{I}_{1}$<br>Principal moment of inertia, $\mathrm{I}_{2}$<br>Uniform torsion constant<br>Procedure for boundary conditions

### 2.1.3 ARGUMENT DESCRIPTIONS

### 2.1.3.1 AREA

Cross-sectional area of beam (default: 1.0).

### 2.1.3.2 BC_PROCEDURE

Boundary condition procedure name (default: CC_BC for specified forces; CCD_BC for specified displacements). The term "boundary conditions" refers both to displacement constraints and applied loading. Procedures CC_BC and CCD_BC both have the same zero displacement constraints. The only difference is that the former procedure applies axial forces to the simply supported edge, while the latter procedure prescribes non-zero axial displacements on that edge. The argument BC_PROCEDURE permits you to to supply your own boundary condition procedure, but keep in mind that this may drastically change the problem definition, and hence invalidate most of the discussion under Section 2.1.1.

### 2.1.3.3 E

Young's elastic modulus (default: 120.0).

### 2.1.3.4 ES_NAME

Element name (default: E210). This is the name of the specific beam-element type you wish to select, within the element processor defined by argument ES_PROC. The default element type, E210, is a 2 -noded beam element implemented in processor ES6, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.1-1).

### 2.1.3.5 ES_PROC

Element Processor (default: ES6) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES6, is described in The Computational Structural Mechanics Testbed User's Manual.

### 2.1.3.6 INERT_1

Principal moment of inertia (default: 1.0).

### 2.1.3.7 INERT_2

Principal moment of inertia (default: 10.0).

### 2.1.3.8 INERT_TORSION

Torsional constant (default: 1.0).

### 2.1.3.9 LENGTH_X

Length of the beam in the $x$-direction (default: 10.0).

### 2.1.3.10 NODES_X

Number of nodes along beam length (default: 3). Note that this number should be consistent with the number of nodes per element. For example, NODES_X can be any number greater than 1 for 2 -node beam elements, whereas it must be an odd number greater than 1 for 3 -node beam elements.

### 2.1.3.11 NNODES_C

Number of circumferential nodes (default: 7). This is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, i.e., along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, NNODES_C can be any number greater than 1 for 4node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

### 2.1.3.12 NU

Poisson's ratio (default: 0.0).

### 2.1.4 USAGE GUIDELINES AND EXAMPLES

Procedure GEN BEAM may be used by preceding the procedure name by the $*$ call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*procedure GEN_BEAM (es_proc = ES6 ; es_name = E210 ; --
    nodes_x = 3 ;--
    length_x =10. ;--
    E=120.; PR=0. ; area =1.0 ; --
    inert_1=1. ; inert_2=10. ; inert_torsion=1. ;--
    BC_PROCEDURE = BEAM_BC )
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call GEN_BEAM

### 2.1.5 LIMITATIONS

### 2.1.6 ERROR MESSAGES AND WARNINGS

None.

### 2.1.7 PROCEDURE FLOWCHART

### 2.1.8 PROCEDURE LISTING

```
*procedure GEN_BEAM ( es_proc = ES6 ; es_name = E210 ; --
    nodes_x = 3 ;--
    length_x =10. ;--
    E=120.; PR=0. ; area = 1.0 ; --
    inert_1=1. ; inert_2=10. ; inert_torsion=1. ;--
    BC_PROCEDURE = BEAM_BC )
*call ES_DEFN ( es_proc=[es_proc]; es_name=[es_name]
[XQT TAB
*def nodes_tot = < [nodes_x]>
```

```
START <nodes_tot>
JLOC
. dEFINE NODAL CDORDINATES
*def/e dx = < [length_x] ( ([nỡढ̄̄_x] 1) >
*def/i node = 0
    *def/e x = 0.
    *do $i = 1,[nodes_x]
        *def node = < <node> + 1 >
            <node\rangle \langlex\rangle, 0., 0. . NODE DEFINITION
            *def x = < <x\rangle + \langledx\rangle >
    *enddo
. define fictitious elastic material propertiES
MATC
1 [E] [PR]
beam face orientation ind properties
    mREF
    FORMAT=2
    1 1 0. 1.0 0.
    BA
    GIVN 1 [inert_1] 0. [inert_2] 0. [area] [inert_torsion]
    . DEFINE LOADS aND bOUNDARY CONDITIONS
    *call [BC_PROCEDURE] ( nnx = [nodes_x] ; --
                                nen = \langlees_nen> )
. generate elehents
. [XQT ELD
    <es_expe_cmd>
        NSECT = 1
. Define element nodal connectivity
* *call BM_ELT_CONN (nnx=[nodes_x]; nen=<es_nen>)
*end
. =DECK BM_ELT_CONN
*procedure BM_ELT_CONN (nnx; nen )
. ===========================
. Define Element Connectivity Record for ELD Processor
. ============================
.
    Revised 12/18/91
```

    *if < [nen] /eq 2 >/then
    #do $ix = 1, <[nnx]-1>
            *def/i n1 = < $ix >
            *def/i n2 = < <n1> + 1 >
    . ==========
<n1> <n2>

```

```

    *enddo
    *elseif < [nen]/eq 3>/then
    *do $ix = 1, <[nnx]-2>, 2
        *def/i n1 = < &ix >
            *def/i n2 = < <n1> + 2 >
            *def/i n3 = < <n2\rangle-1\rangle
    . ===============
<n1> <n2> <n3>
z=============
*enddo
*endif
*end

```

\subsection*{2.1.9 REFERENCES}
2.1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{2.2 Procedure GEN_CANTILEVER}

\subsection*{2.2.1 GENERAL DESCRIPTION}

This section describes a procedure which generates models of a straight cantilever beam using two-dimensional plate/shell elements. Using the default values for the procedure arguments, the straight cantilever beam problem from the MacNeal-Harder test cases (see ref. 2.2-1) is generated. The model used for the MacNeal-Harder cantilever beam test cases, is shown in figure 2.2-1.


DIMENSIONS : \(h=.2, L=6\), Thickness \(=.1\)
MATERIAL PROPERTIES: \(E=1.0 \times 10^{7}, \quad v=.30\)

Figure 2.2-1 Generic 2-D Cantilever Beam Finite Element Models.

\subsection*{2.2.2 PROCEDURE USAGE}

Procedure GEN_CANTILEVER may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call GEN_CANTILEVER ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN_CANTILEVER are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES.PROC & ES2 & Select element processor \\
\hline ES_NAME & EX41 & Select element with ELT_PROC \\
\hline ES_PARS & 0.0 & Set element-research parameters \\
\hline AUTO_DOF_SUP & true & Automatic d.o.f. suppression \\
\hline DRILLING_DOF & false & \\
\hline NODES \(X\) & 7 & Number of nodes in \(\mathbf{x}\)-direction \\
\hline NODES_Y & 2 & Number of nodes in y-direction \\
\hline LENGTH_X & 6. & Beam length (x-direction) \\
\hline LENGTH_Y & . 2 & Beam width (y-direction) \\
\hline E & \(1 . \mathrm{E7}\) & Young's elastic modulus \\
\hline NU & . 3 & Poisson's ratio \\
\hline THICKESS & . 1 & Thickness \\
\hline DISTORT & . 07071 & \\
\hline BC.PROCEDURE & CANTILEVER_BC & Procedure for boundary conditions \\
\hline
\end{tabular}

\subsection*{2.2.3 ARGUMENT DESCRIPTIONS}

\subsection*{2.2.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{2.2.3.2 BC_PROCEDURE}

Boundary condition procedure name (default: CANTILEVER_BC). The term "boundary conditions" refers both to displacement constraints and applied loading. The argument BC.PROCEDURE permits the users to supply their own boundary condition procedure, but keep in mind that this may drastically change the problem definition.

\subsection*{2.2.3.3 DISTORT}

Distorted mesh parameter (default: 0.07071).

\subsection*{2.2.3.4 DRILLING_DOF}

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{2.2.3.5 E}

Young's elastic modulus (default: \(1.0 \times 10^{7}\) ).

\subsection*{2.2.3.6 ES_NAME}

Element name (default: EX41). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, Ex41, is a 4-noded quadrilateral element implemented in Processor es2, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.2-1).

\subsection*{2.2.3.7 ES_PARS}

Element research parameters (default: \(0 ., \ldots\) ). This argument allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{2.2.3.8 ES_PROC}

Element processor (default: ES2) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES2, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{2.2.3.9 NODES_X}

Number of nodes along \(x\)-direction (default: 7). This is the number of nodes you wish to have along the axial direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES_X can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.2.3.10 NODES_Y}

Number of nodes along \(y\)-direction (default: 2). This is the number of nodes you wish to have along the depth direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES_Y can be any number greater than 1 for 4-node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.2.3.11 NU}

Poisson's ratio (default: 0.3).

\subsection*{2.2.3.12 THICKNESS}

Beam thickness (default: 0.1).

\subsection*{2.2.4 USAGE GUIDELINES AND EXAMPLES}

Procedure GEN_CANTILEVER may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.
```

*call GEN_CANTILEVER ( es_proc $=$ ES2 ; es_name = EX41 ; --
es_pars $\quad=0.0$; --
auto_dof_sup $=\langle$ true〉; --
drilling_dof $=\langle f a l s e\rangle ;--$
nodes_x $=7$; nodes_y $=2$; -
length_x $=6 . \quad ; l_{\text {ength_y }}=.2$;-
$\mathrm{E}=1 . \mathrm{E} 7$; $\mathrm{NU}=.3$; thickness $=.1$; -
distort $=.07071$; --
BC_PROCEDURE = CANTILEVERLEVER_BC )

```
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call GEN_CANTILEVER

\subsection*{2.2.5 LIMITATIONS}

\subsection*{2.2.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{2.2.7 PROCEDURE FLOWCHART}

\subsection*{2.2.8 PROCEDURE LISTING}
```

*procedure GEN_CANTI ( es_proc = ES2 ; es_name = EX41 ; --
es_pars = 0.0 ; --
auto_dof_sup = <true> ; --
drilling_dof = <false\rangle; --
nodes_x = 7 ; nodes_y = 2 ; --
length_x = 6. ; length_y = .2 ; --
E=1.E7 ; NO=.3 ; thickness =.1 ; --
distort =.07071; --
BC_PROCEDORE = CANTILEVER_BC )
Register Element and Define Macros: ELT_NEN, ELT_NIP, ELT_NSTR, etc.
*call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
es_name = [es_name] ; es_pars = [es_pars])
[xqT TAB
*def nodes_tot = < [nodes_x] * [nodes_y] >
START <nodes_tot>
JLOC
. dEFINE NODAL COORDINATES
*def/e dx = < [length_x] / ([nodes_x]-1) >
*def/e dy = < [length_y] / ([nodes_y]-1) >
*def/i node = 0
*def/e y = 0.
*def/e skev = < -1. * [distort] >
*def/e dskew = < 2.0 * [distort] / ([nodes_y]-1) >
*do \$j = 1,[nodes_y]
*def/e x = 0.

```
```

    *do $i = 1,[nodes_x]
    Cdef node = < <node> + 1 >
        <node\rangle \langlex\rangle,\langley\rangle, 0. . NODE DEFINITION
    *def x = < <x\rangle + \langledx\rangle >
            *if <<$i>/eq 1 > /then
                *def x = < <x\rangle + \langleskew\rangle >
            *endif
            *if <<$i\rangle/eq <[nodes_x]-1\rangle>/then
                *def x = < [length_x] >
            *endif
    *enddo
    *def y = < <y\rangle + \langledy\rangle\rangle
    *def skew = < <skew\rangle + \langledskew\rangle >
    *enddo
D DEFINE FICTITIOUS ELASTIC MATERIAL PROPERTIES
matc
1 1.0.3
DEFINE LOADS AND BOUNDARY CONDITIONS
*call [BC_PROCEDURE] ( nnx = [nodes_x] ; nny = [nodes_y] ; --
nen = <es_nen> ; drilling_dof = [drilling_dof])
D dEFINE REAL MATERIAL/SECTION PROPERTIES
[xqT AOS

- Build Table of Material Data
TABLE(NI=16,NJ=1): OMB DATA 1 1
*def/e12.4 G = < [E] / (2.*(1.+[NU])) >
I=1,2,3,4,5,6
J=1
[E] [NO] [E] <G\rangle <G\rangle <G\rangle
. Build Laminate Data Tables
TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
I=1,2,3 . (material_type, layer_thickness, angle(deg.)
J=1: 1 [THICKNESS] 0.0
[XQT LAU
GENERATE ELEMENTS
[XQT ELD
Define number of integration (stress) points based on element type
*def/i nst = <<es_nip>*<es_nstr>>

```
```

        Define element attributes
    <ES_EXPE_CMD>
    NSECT = 1
    - Define element nodal connectivity
*call CANTI_ELT_CONN (nnx=[nodes_x]; nny=[nodes_y]; nen=<es_nen>)
Suppress DOFs not supported by elements
*if < [AUTO_DOF_SUP] > /then
*call ES ( function = 'DEFINE FREEDOHS' )
*endif
*end
*procedure CANTI_ELT_CONN ( nnx; nny; nen )

```

```

- Define Element Connectivity Record for ELD Processor
==========\#================
*if < [nen] /eq 4 >/then
*do $iy = 1, <[nny]-1>
          #do &ix = 1, <[nnx]-1>
          #def/i n1 = < (\langle&iy>-1)*[nnx] + \langle$ix\rangle>
*def/i n2 = < <n1> + 1 >
*def/i n3 = < <n2> + [nnx]>
Hdet/i n4 = < <n3> - 1 >

```

```

                    <n1> <n2> <n3> <n4>
                    ======================
            *enddo
        *enddo
    *olseif < [nen]/eq 9>/then
        *do $iy = 1, <[nny]-2>, 2
        *do $ix = 1, <[nnx]-2>, 2
            *def/i n1 = < (<$iy>-1)*[nnx] + \langle$ix\rangle>
            *def/i n2 = < <n1\rangle + 2\rangle
            *def/i n3 = < <n2> + (2*[nnx]) >
            mdef/i n4 = < <n3> - 2\rangle
            *def/i n5 = < <n1\rangle + 1\rangle
            *def/i n6 = < <n2\rangle + [nnx]>
            *del/i n7 = < <n4\rangle + 1\rangle
            #def/i n8 = < <n6\rangle - 2\rangle
            *def/i n9 = < <n8\rangle + 1\rangle
    ```




\section*{* enddo}
*enddo
*endif
* \(\boldsymbol{*}\) nd

\subsection*{2.2.9 REFERENCES}
2.2-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
2.2-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{2.3 Procedure GEN_CURVED_BM}

\subsection*{2.3.1 GENERAL DESCRIPTION}

This section describes a procedure which generates models of a curved (circular) beam using two-dimensional plate/shell elements. Using the default values for the procedure arguments, the curved beam problem from the MacNeal-Harder test cases (see ref. 2.3-1) is generated. The MacNeal-Harder curved beam test case is shown in figure 2.3-1.


PROBLEM : Curved Beam
OIMENSIONS: Inner radius \(=4.12 \quad\) Outer radius \(=4.32\)
Thickness \(=.1\)
MATERIAL PROPERTIES: \(E=1 \times 10^{\circ} \quad v=.25\)
BOUNDARY CONDITIONS: Cantelever beam fixed at \(y=0\)
LOADING: Unit forces applied at free end;
1) in-olane (verical) -- y-direction (case 1)
2) out-of-plane -- E-cirection (case 2)

Figure 2.3-1 Generic 2-D Curved Beam Problem.

\subsection*{2.3.2 PROCEDURE USAGE}

Procedure GEN_CURVED_BM may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call GEN_CURVED_BM ( arg1 = val1 ; arg2 = val2 ; ...)

```
where \(\arg 1\) and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN_CURVED_BM are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{lccl} 
Argument & Default Value & & Meaning \\
\cline { 1 - 1 } ES_PROC & ES2 & & Select element processor \\
ES_NAME & EX41 & & Select element within ELT_PROC \\
ES_PARS & 0.0 & & Set element-research parameters \\
AUTO_DOF_SUP & <true> & & Automatic d.o.f. suppression \\
DRILLING_DOF & <false> & & \\
NODES_T & 7 & & Number of nodes in tangential direction \\
NODES_R & 2 & & Number of nodes in radial direction \\
RIN & 4.12 & & Inner radius \\
ROUT & 4.32 & & Outer radius \\
E & \(1 . E 7\) & & Young's elastic modulus \\
NU & .25 & & Poisson's ratio \\
THICKNESS & .1 & & Thickness \\
BC_PROCEDURE & CURVED_BC & & Procedure for boundary conditions
\end{tabular}

\subsection*{2.3.3 ARGUMENT DESCRIPTIONS}

\subsection*{2.3.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{2.3.3.2 BC_PROCEDURE}

Boundary condition procedure name (default: CURVED_BC). The term "boundary conditions" refers both to displacement constraints and applied loading. The argument BC.PROCEDURE permits you to to supply your own boundary condition procedure, but keep in mind that this may drastically change the problem definition.

\subsection*{2.3.3.3 DRTLLING_DOF}

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{2.3.3.4 E}

Young's elastic modulus (default: \(1.0 \times 10^{7}\) ).

\subsection*{2.3.3.5 ES_NAME}

Element name (default: EX41). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX41, is a 4-noded quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.3-1).

\subsection*{2.3.3.6 ES_PARS}

Element research parameters (default: \(0 ., \ldots\) ). This argument allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{2.3.3.7 ES_PROC}

Element processor (default: ES2) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES2, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{2.3.3.8 NODES_R}

Number of radial nodes (default: 2). This is the number of nodes you wish to have along the radial direction of the curved beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES_ \(\mathbb{R}\) can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.3.3.9 NODES_T}

Number of tangential nodes (default: 7). This is the number of nodes you wish to have along the tangential direction of the curved beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NODES_T can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.3.3.10 NU}

Poisson's ratio (default: 0.25).

\subsection*{2.3.3.11 RIN}

Inner radius of curved beam (default: 4.12).

\subsection*{2.3.3.12 ROOT}

Outer radius of curved beam (default: 4.32).

\subsection*{2.3.3.13 THICKNESS}

Beam thickness (default: 0.1).

\subsection*{2.3.4 USAGE GUIDELINES AND EXAMPLES}

Procedure GEN_CURVED_BM may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.
```

*procedure GEN_CURVED_BM (elt_proc $\quad=$ ES2 ; elt_name = EX41 ; --
elt_pars $\quad=0.0$;
auto_dof_sup $=\langle$ true〉; --
drilling_dof $=\langle f a l s e\rangle ;--$
nodes_t $=7$; nodes_r $=2$;
rin $=4.12$; rout $=4.32 ;--$
$\mathrm{E}=1 . \mathrm{E} 7$; $\mathrm{PR}=.25$; thick $=.1$; --
BC_PROCEDURE = CURVED_BC )

```
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call GEN_CURVED_BM

\subsection*{2.3.5 LIMITATIONS}

\subsection*{2.3.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{2.3.7 PROCEDURE FLOWCHART}

\subsection*{2.3.8 PROCEDURE LISTING}
```

*procedure GEN_CURVED (es_proc = ES2 ; es_name = EX41 ; --
es_pars = 0.0 ; --
auto_dot_sup = <true\rangle; --
drilling_dof = \langleialse\rangle; --
nodes_t = 7 ; nodes_r = 2 ; --
rin = 4.12 ; rout = 4.32 ; --
E=1.E7 ; NU=.25 ; thickness =.1 ; --
BC_PRDCEDURE = CURVED_BC )
. Register Element and Define Macros: ELT_NEN, ELT_NIP, ELT_NSTR, etc.
*call ES ( function = 'DEFINE ELEMENTS' ; 0s_proc = [es_proc]; --
es_name = [es_name] ; es_pars = [es_pars])
[XQT TAB
*de1 nodes_tot = < [nodes_t] * [nodes_r]>
START <nodes_tot>
JLOC
FORMAT = 2 . use cylindrical coordinate system
. DEFINE NODAL COORDINATES
*def/e dx = < 90. / ([nodes_t]-1) >
*def/e dy = < < [rout] - [rin] > / ([nodes_r]-1) >
*def/i node = 0
*def/er r [rin]
*do \$j = 1,[nodes_r]
*def/e theta = 90.
\#do \$i = 1,[nodes_t]
*del node = < <node\rangle + 1 >

```
```

        <node> <r>, <theta>, 0. . NODE DEFINITION
        *def theta = < <theta> - <dx\rangle>
    *enddo
        *def r = < \langler\rangle + \langledy\rangle \rangle
    *enddo
. define fictitious elastic material properties
Matc
1 1.0.3
. =======ミ========ミ====
Define DOF Directions
======================
JREF . Use local cylindrical basis vectors
for nodal DOFS:
. u,v,w = radial, circumfer., axial
NREF = -1
1 <nodes_tot> . same convention for all nodes
. define loads and boundary conditions
*call [BC_PROCEDURE] ( nnx = [nodes_t] ; nny = [nodes_r] ; --
nen = \langlees_nen> ; drilling_dof = [drilling_dof] )
. DEFINE REAL MATERIAL/SECTION PROPERTIES
[XQT AUS
. Build Table of Material Data
TABLE(NI=16,NJ=1): OMB DATA 1 1
*def/e12.4 G = < [E] / (2.*(1.+[NU])) >
I=1,2,3,4,5,6
J=1
[E] [NU] [E] <G> <G> <G>
. Build Laminate Data Tables
TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
I=1,2,3 . (material_type, layer_thickness, angle(deg.)
J=1: 1 [THICKNESS] 0.0
[xgT laU
. generate Elements
[XQT ELD
. Define number of integration (stress) points based on element type
*def/i nst = < <es_nip>*<_nstr\rangle>

```
    2.3-6
```

. Define element attributes
<ES_EXPE_CMD>
NSECT = 1
. Define element nodal connectivity
*call CURV_ELT_CONN (nnx=[nodes_t]; nny=[nodes_r]; nen=<es_nen>)
. Suppress DoFs not supported by elements
. ----------------------------------------
*if < [AUTO_DOF_SUP] > /then
*call ES ( function = 'DEFINE FREEDOMS' )
*endif
*end
*procedure CURV_ELT_CONN ( nnx; nny; nen )
. ==コ==ェ=====================

- Define Element Connectivity Record for ELD Processor
. ===========================
*if < [nen] /eq 4 >/then
*do \$iy = 1, <[nny]-1>
*do $ix = 1, <[nnx]-1>
              *dof/i n1 = < (<$iy>-1)*[nnx] + <\$ix>>
*def/i n2 = < <n1\rangle + 1 >
*def/i n3 = < <n2\rangle + [nnx] >
*def/i n4 = < <n3> - 1 >

```

```

                        <n1> <n2> <n3> <n4>
                        ======================
        *enddo
        *enddo
    *elseif < [nen] /eq 0 > /then
        *do $iy = 1, <[nny]-2>, 2
        *do $ix = 1, <[nnx]-2>, 2
            *def/i n1 = < (<$iy>-1)*[nnx] +\langle$ix\rangle>
            *de1/i n2 = < <n1\rangle + 2 >
            *def/i n3 = < <n2\rangle + (2*[nnx]) >
            *def/i n4 = < <n3> - 2 >
            *def/i n6 = < <n1\rangle + 1 \rangle
            *def/i n6 = < <n2> + [nnx] >
            *def/i n7 = <\langlen4\rangle + 1\rangle
            *de1/i n8 = < <n6> - 2 \rangle
            *de1/i n9 = \langle <n8\rangle + 1\rangle
    ```

```

            <n1> <n2> <n3> <n4> <n5> <n6> <n7> <n8> <n9>
    ```

```

            *enddo
        *enddo
    *endif
    *end

```

\subsection*{2.3.9 REFERENCES}
2.3-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
2.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{2.4 Procedure GEN_PLATE}

\subsection*{2.4.1 GENERAL DESCRIPTION}

Procedure GEN_PLATE is used to generate flat or warped 4 -sided plate finite element models. The plate edges are defined to be straight with the surface defined as the bi-linearly interpolation of the edges. This type of interpolated surface is also known as a Coon's surface (see refs. 2.4-2 and 2.4-3).

\subsection*{2.4.2 PROCEDURE USAGE}

Procedure GEN_PLATE may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call GEN_PLATE ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg 1 and arg 2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) preceded by a space may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN_PLATE are summarized in the following table, along with their default values (if they exist). Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES.PROC & ES1 & Generic element processor \\
\hline ES_NAME & Ex97 & Generic element name \\
\hline ES.PARS & 0.0 & Element research parameters \\
\hline XYZ1 & 1,0,0 & Cartesian coordinates of point 1. \\
\hline XYZ2 & 1,0,1 & Cartesian coordinates of point 2. \\
\hline XYZ3 & 1,90,1 & Cartesian coordinates of point 3. \\
\hline XYZ4 & 1,90,0 & Cartesian coordinates of point 4. \\
\hline NODES_1 & 7 & Number of nodes along edge 1 \\
\hline NODES_2 & 7 & Number of nodes along edge 2 including duplicate nodes if plate closes \\
\hline EDGE_WEIGHTS & 1,1,1,1 & Plate section property procedure \\
\hline BC.PROCEDURE & , , & Boundary condition procedure \\
\hline DRILLING_DOF & <true> & Drilling dof suppression flag \\
\hline AUTO_DOF_SUP & <true> & Automatic dof suppression flag \\
\hline SECTION_PRC & , , & Plate section property procedure \\
\hline NSECT & 1 & Plate section property number \\
\hline \multicolumn{3}{|l|}{The following values not used if SECTION_PRC is specified.} \\
\hline E & 30.E6 & Young's Modulus \\
\hline N0 & 0.3 & Poisson's ratio \\
\hline WTDEN & 0.1 & Weight Density \\
\hline THICKNESS & . 1 & Plate thickness \\
\hline
\end{tabular}

\subsection*{2.4.3 ARGUMENT DESCRIPTIONS}

\subsection*{2.4.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffness (see argument DRILLING_DOF).

\subsection*{2.4.3.2 BC.PROCEDURE}

Name of user provided boundary condition procedure (default: ''). The term "boundary conditions" refers both to displacement constraints and applied loading. If a boundary conditions procedure is provided, the following call will be performed. The macrosymbol <es_nen> equals the number of element nodes.
```

*call [BC_PROCEDURE] ( nodes_1 = [nodes_1] ; --
nodes_2 $=$ [nodes_2] ; --
es_nodes $=\left\langle e s_{-}\right.$nen> ; --
drilling_dof = [drilling_dof] )

```

No action is taken if a boundary condition procedure name is not provided.

\subsection*{2.4.3.3 DRILLING_DOF}

Drilling degree of freedom flag (default: <true>). Drilling freedoms are defined as rotations normal to the surface of the plate. Setting this flag set to <false> forces all drilling freedoms in the model to be suppressed. Setting it to true forces all drilling freedoms to be active - unless they are automatically suppressed by use of the AUTO_DOF_SUP argument. Note that while many plate elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when plate elements are assembled as facets approximating an arbitrary plate surface, there is usually some misalignment between the element normal and the actual plate normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the plate normal is usually present in the model. (A clear exception to this is a flat plate, where element and plate normals are identical.) For a curved plate, the misalignment diminishes only as the number of elements is increased. Most plate elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{2.4.3.4 E}

Young's modulus (default: 30.E6). This argument is ignored if SECTION_PRC parameter is specified. See the description for SECTION_PRC for more detail.

\subsection*{2.4.3.5 EDGE_WEIGHTS}

Node placement can be weighted along each surface edge according to the EDGE_WEIGHTS parameter. The input format requires a list of four edge-node placement weightings representing the node weighting for edge1, edge2, edge3, and edge4 (default: 1.,1.,1.,1.).
The weighting value for a given edge represents the length of the last element divided by the length of the first element along that edge. The edge orientation arrows in figure 2.4-1 point from the first element to the last element along each edge. In the case of 9 -node quad elements, the midside and center nodes are positioned at the appropriate locations based on the elements natural coordinate system.
The procedure interprets negative weight values to mean the positive reciprocal. For example, a value of -5.0 is identical to a value of 0.2 .

\subsection*{2.4.3.6 ES_NAME}

Element name (default: EX97). This argument is the name of the specific plate-element type you wish to select, within the element processor defined by argument ES_PROC. The default plate-element type, EX97, is a 9 -node quadrilateral element implemented in processor ES1, and described reference 2.4-1.

\subsection*{2.4.3.7 ES_PARS}

Element research parameters (default: 0., ...). This argument is an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{2.4.3.8 ES_PROC}

Element processor (default: ES1) This argument is the name of the structural element (ES) processor that contains the plate element type you wish to employ in the model. The default plate-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{2.4.3.9 NODES_1}

Number of nodes on edge 1 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 3 . This number should be consistent with the element type selected. For example, NODES_1 can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.4.3.10 NODES_2}

Number of nodes on edge 2 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 4 . This number should be consistent with the element type selected. For example, NODES_2 can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.4.3.11 NSECT}

Plate section property number (default: 1). The NSECT value is required when defining the element using the processor ELD. See the description of SECTION_PRC for more detail.

\subsection*{2.4.3.12 NU}

Poisson's ratio (default: 0.3). This argument is ignored if the SECTION_PRC input parameter is specified. See the description of SECTION_PRC for more detail.

\subsection*{2.4.3.13 XYZ1}

The cartesian coordinates \((x, y, z)\) which define corner number 1 of the model surface. The form of the input is three real values, each separated by a comma (default: \(1,0 ., 0\).). The surface is defined by four edges which are defined as a linear interpolation in cartesian coordinates of four endpoints, or "corner" points.

\subsection*{2.4.3.14 XYZ2}

The cartesian coordinates ( \(x, y, z\) ) defining the corner number 2 of the model surface (default: 1.,0.,1.).

\subsection*{2.4.3.15 XYZ3}

The cartesian coordinates ( \(x, y, z\) ) defining the corner number 3 of the model surface (default: 1.,90.,1.).

\subsection*{2.4.3.16 XYZ4}

The cartesian coordinates ( \(x, y, z\) ) defining the corner number 4 of the model surface (default: 1.,90.,0.).

\subsection*{2.4.3.17 SECTIONPRC}

Name of a user supplied procedure to define the plate section properties (default \(=\) ' '). If a section properties procedure is provided, the following call will be performed.
```

*call [section_prc] ( nsect = [nsect] )

```

The effect of the default is to allow the procedure to generate an isotropic material section based on the input parameters E, NO, WTDEN, and THICKNESS. The section number is defined by the input parameter NSECT. If the call parameter SECTION_PRC is defined by the user, then call parameters E, NU, WTDEN, and THICKNESS are ignored by procedure GEN PLATE.

\subsection*{2.4.3.18 THICKNESS}

Thickness of the plate wall (default \(=1.0\) ). This argument is ignored if SECTION_PRC parameter is specified. See the description for SECTION_PRC for more detail.

\subsection*{2.4.3.10 WTDEN}

Weight density expressed in \(\mathrm{lb} / \mathrm{in} .^{3}\) (default: \(0.1 \mathrm{lb} / \mathrm{in} .^{3}\) ). This argument is ignored if the SECTION_PRC input parameter is specified. Processor LAU will convert the weight density to mass density using the gravitational acceleration constant \(386.4 \mathrm{in} / \mathrm{sec}^{2}\).

\subsection*{2.4.4 USAGE GUIDELINES AND EXAMPLES}

Procedure GEN_PLATE may be invoked using the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values in the procedure call. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.
```

*procedure GEN_PLATE ( ES_PROC = ES1 ; ES_NAME = EX97 ; ES_PARS = 0.0 ; --
XYZ1 = 0.,0.,0. ; --
XYZ2 = 1.,0.,0. ; --
XYZ3 = 1.,1.,0. ; --
XYZ4 = 0.,1.,0. ; --
NODES_1 = 3; --
NODES_2 = 3 ; --
EDGE_WEIGHTS = 1.,1.,1.,1.; --
BC_PROCEDURE = , , ; -- . Boundary condition procedure
DRILLING_DOF = <true> ; --
AUTO_DOF_SUP = <true> ; --
SECTION_PRC = , ; -- . Plate section property procedure
NSECT = 1 ; -- . Plate section property ID
The following values not used if SECTION_PRC specified

```
```

        E = 30.E6 ; -- . Young's Modulus
        NU = . 3 ; -- . Poissons ratio
        THICKNESS = . 1 -- . Plate thickness
    )

```

\subsection*{2.4.4.1 Mesh Generation}

The method of surface generation used by procedure GEN_PLATE is described in the section. Terminology depicted on figure 2.4-1 provides a visual interpretation of the parameters used to generate a general plate surface. Node generation capability is provided by the Testbed processor MESH.
To define the plate surface, the user defines four coordinate positions in the cartesian reference frame. These coordinate positions represent the corners of a straight-sided quadrilateral region. The surface of the region is defined as the bi-linear interpolation of the four sides (see refs. 2.4-2 and 2.4-3).


Figure 2.4-1 Generic Plate Surface Topology.

The connectivity of the surface is defined in figure 2.4-1. The user provides the coordinates for corners 1 to 4. Edge 1 of the region starts at corner 1 and ends at corner 2. The remaining edges are defined in a similar manner. The arrows indicate the orientation of the edges and the direction of increasing node numbers.
The topology of the resulting finite element grid is depicted in Figure 2.4-2. Nodes are created first along edge 1 , then in successive lines terminating along edge 3. The user defines the number of nodes along edges 1 and 2 , which also defines the number of nodes for edges 3 and 4. The relative position of the nodes along each edge may be controlled using the edge weighting parameter EDGE_WEIGHTS.


Figure 2.4-2 Node and Element Topology.

\subsection*{2.4.4.2 Flat Plates}

In this section are presented examples of how procedure GEN_PLATE may be used to create two-dimensional finite element plate models.
In the following example, procedure GEN_PLATE is used to generate a flat rectangular plate with length of 10 inches and width of 5 inches using 4-noded quadrilateral elements (see figure 2.4-3).
```

*call GEN_PLATE ( es_proc = 'ES1' ; es_name = 'EX47' ; --
xyz1
xyz2 = 10.,0.,0. ; --
xyz3 = 10.,5.,0.; --
xyz4 = 0.,5.,0. ; --
nodes_1 = 9 ; --
nodes_2 = 5 )

```

\(\left.\right|_{2} ^{x}\)

Figure 2.4-3 Rectangular Plate

This example demonstrates the use of the EDGE_WEIGHTS parameter and how it affects both the 4 -node and 9 -node quadrilateral element mapping (see figure 2.4-4). The EDGE_WEIGHTS specifies elements at the ends of edges 1 through 4 to be 5 times longer than elements at the beginning of the edges.
*cell GEN_PLATE (es_proc = 'ES1' ; es_name = 'EX97' ; --
\[
\begin{array}{ll}
\text { xyz1 } & =0 ., 0 ., 0 . ;-- \\
\text { xyz2 } & =10,0,0 . ;- \\
\text { xyz3 } & =10,, 5 ., 0 . ;- \\
\text { xyz4 } & =0 ., 5 ., 0 . ;- \\
\text { nodes_1 } & =9 ;- \\
\text { nodes_2 } & =5 ;-- \\
\text { edge_veights } & =5,,-5 .,-5,5 .)
\end{array}
\]

(a) 4-node elements

(b) 9-node elements

Figure 2.4-4 Rectangular Plate With Weighted Elements

The following example produced the skewed flat plate shown in figure 2.4-5.
*call GEN_PLATE ( es_ proc = 'ES1' ; es_name = 'EX47' ; --
xyz1 xyz2 xyz3 xyz4 nodes _1 nodes_2
\(=0 ., 0 ., 0\). ; --
\(=10 ., 1 ., 0\). ;-
\(=7 ., 6 ., 0 . ;-\)
\(=13\);
\(=11\) )


Figure 2.4-5 Skewed Flat Plate

\subsection*{2.4.4.s Warped Plates}

In the following example, procedure GEN_PLATE is used to generate the highly warped surface shown in figure 2.4-6.
```

*call GEN_PLATE ( es_proc = 'ES1' ; es_name = 'EX47' ; --
xyz1
xyz2
xyz3
= 5.,5.,0. .--
= 5.,0.,5. ; --
xyz4
=0.,5.,5. ; --
nodes_1
nodes_2
=21;-
=23 )

```


Figure 2.4-6 Warped Plate

\subsection*{2.4.5 LIMITATIONS}

None.

\subsection*{2.4.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{2.4.7 PROCEDURE FLOWCHART}
\begin{tabular}{ll} 
GEN_PLATE & (Plate generation procedure) \\
[BC_PROCEDURE] & (user supplied boundary conditions/loads procedure) \\
[SECTION_PRC] & (user supplied section property generation procedure)
\end{tabular}

\subsection*{2.4.8 PROCEDURE LISTING}
```

*procedure GEN_PLATE (es_proc = es1 ; es_name = ex97 ; es_pars = 0.0 ; --
xyz1 =0.,0.,0. ; --
xyz2 = 1.,0.,0.; --
xyz3 = 1.,1.,0.; --
xyz4 = 0.,1.,0. : --
nodes_1 = 3 ; --
nodes_2 = 3 ; --
odge_weights = 1.,1.,1.,1. ; --
online = 0 ; -- . suppress nodes and element output
bc_procedure = , ; -- . Boundary condition procedure
drilling_dot = <true> ; --
auto_dof_sup = <true\rangle ; --
section_prc = , ; -- . Shell section property procedure
The following values used only if section_prc not specified
nsect = 1 ;- . Shell section property ID
E = 30.E6 ; -- . Young's Modulus
NU = . 3 -- . Poisons ratio
WTDEN = .1 ; - . Weight Density
thickness = . 1 -- . Shell thickness
)

```

```

- Model Definition Procedure Ior GENeric Plate in cartesian coordinates

```

```

| \& general purpose clip procedure to create the finite element
. mesh for a plate with arbitraty straight sides using 4 or

- 9 noded quadrilateral elements.
. If a procedure to generate shell section properties is not provided,
the isotropic section described by E, ND, UTDEN, and THICKNESS will

```
```

be automatically generated. (see [section_prc] parameter)
A boundary condition procedure should be provided but is
optional. If not provided, no boundary conditions will be
defined. (see [bc_procedure] parameter)

```

```

*remark GEN_PLATE MODEL GENERATION PROCEDORE

```

```

    *def/i n1 = [nodes_1]
    *def/i n2 = [nodes_2]
    *def/e xyz1[1:3] = [xyz1]
    *def/e xyz2[1:3] = [xyz2]
    *def/e xyz3[1:3] = [xyz3]
    *def/e xyz4[1:3] = [xyz4]
    *def/e v[1:4] = [edge_weights]
    *def/e rc[1:4] = <xyz1[1]>,\langlexyz2[1]\rangle,\langlexyz3[1]>,\langlexyz4[1]\rangle
    *def/e tc[1:4] = <xyz1[2]>,\langlexyz2[2]>,\langlexyz3[2]\rangle,\langlexyz4[2]>
    *def/e zc[1:4] = <xyz1[3]>,\langlexyz2[3]>,\langlexyz3[3]>,\langlexyz4[3]>
    ```

```

        Hegister Element and Define Macros: ES_NEN, ES_NIP, ES_NSTR, etc.
    ```

```

    *call ES (function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
        es_name = [es_name] ; es_pars = [es_pars])
    ```

```

        Detine nodal coordinates and element connectivities into
        separate formatted files. These files are gauranteed to have
        unique names that are not currently in use in the current
        directory
    ```

```

        mdef/1 chk_closure = 0
        [xqt mesh
        *if <mesh_err>/then
            *remark Error occurred during HESH processor execution.
            *remark GEN_PLATE procedure terminated.
            *e01
        #endif
    ```

```

C Construct Model Data-bese with TESTBED Processors

```

```

    [YQT TAB
    START <tot_nodes>
    ONLINE = [online]
    JLOC
    *show macros node_file
    madd <node_file>
    ```

```

    Define Load/Boundary Conditions If Procedure Supplied
    ```

```

    *if <not(<ifelse([bc_procedure]; ;1;0)>)>/then
    *call [BC_PROCEDURE] ( nodes_1 = <n1\rangle ; --
                nodes_2 = <n2\rangle ; --
                es_nodes = <es_nen> ; --
                drilling_dof = [drilling_dof] )
    *else
    ```

```

        *remark BOUNDARY CONDITIONS NOT SPECIFIED
    ```

```

    *endif
    ```

```

        Define Shell Section Properties
    ```

```

    #if <not(<ifelse([section_prc]; ;1;0)>)>/then
    *call [section_prc] ( nsect = [nsect] )
    *else
    ```

```

        Define the default Material and Section Properties
    ```

```

    *def/e G = < [E]/(2.*(1+[NO])) >
        [XQT AOS
        Build Table of Material Data
        TABLE(ni=16,nj=1): OMB DATA 1 1
        i = 1,2,3,4,5,6,7,8,9
        j = 1
        E11 NU12 E22 G12 G13 G23 ALPHA1 ALPHA2 UTDEN
        [E] [NU] [E] \langleG\rangle \langleG\rangle \langleG\rangle 0. 0. [WTDEN]
        Build Laminate Data Tables
        TABLE(ni=3,nj=1,itype=0): LAM OMB [nsect] 1
        i = 1,2,3
        j = 1 . matl % layer thickness matl angle
            1 [thickness] 0.
        CXQT LAU
        ONLINE = 2
    *endif
    ```

```

*=================

```
```

    [XGT ELD
    <ES_EXPE_CMD>
    NSECT = [nsect]
        Define element nodal connectivity
    *show macros elem_file
*add <elem_file>

```

```

        Suppress DOFs not supported by elements
    ```

```

    *if < [AOTO_DOP_SUP] > /then
        *call ES ( function = 'DEFINE FREEDOMS' )
    *ondif
    *end

```

\subsection*{2.4.9 REFERENCES}
2.4-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
2.4-2 Cook, William A.: "Body Oriented (Natural) Coordinates For Generating ThreeDimensional Meshes." International Journal For Numerical Methods in Engineering, 1974, Volume 8, pp. 27-43.
2.4-3 Forrest, A. R.: On Coons and Other Methods for the Representation of Curved Surfaces. Computer Graphics and Image Processing, 1972, Volume 1, pp. 341-359.

\subsection*{2.5 Procedure GEN_SHELL}

\subsection*{2.5.1 GENERAL DESCRIPTION}

Procedure GEN_SHELL is used to generate a class of curved shell finite element models. All surfaces are modeled as bi-linearly interpolated surfaces (i.e., Coon's surfaces) in cylindrical coordinate space (see refs. 2.5-2 and 2.5-3). Interpolation in cylindrical coordinates is especially well suited for generating shells of revolution, such as cylinders, cones, annular plates, and spiraling surfaces.

\subsection*{2.5.2 PROCEDURE USAGE}

Procedure GEN_SHELL may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
*call GEN_SHELL ( arg1 = val1 ; arg2 = val2 ; ...)
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) preceeded by a space may be used to continue the argument list on the next line.

The allowable arguments for procedure GEN_SHELL are summarized in the following table, along with their default values (if they exist). Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES_PROC & ES1 & Generic element processor \\
\hline ES_NAME & EX97 & Generic element name \\
\hline ES_PARS & 0.0 & Element research parameters \\
\hline RTZ1 & 1,0,0 & Cylindrical coordinates of point 1. \\
\hline RTZ2 & 1,0,1 & Cylindrical coordinates of point 2. \\
\hline RTZ3 & 1,90,1 & Cylindrical coordinates of point 3. \\
\hline RTZ4 & 1,90,0 & Cylindrical coordinates of point 4. \\
\hline NODES_1 & 7 & Number of nodes along edge 1 \\
\hline NODES_2 & 7 & Number of nodes along edge 2 including duplicate nodes if shell closes \\
\hline EDGE_WEIGHTS & 1,1,1,1 & Shell section property procedure \\
\hline JREF & , , & Joint dof reference frame \\
\hline BC_PROCEDURE & , & Boundary condition procedure \\
\hline DRILLING_DOF & <false> & Drilling dof suppression flag \\
\hline AUTO_DOF_SUP & <false> & Automatic dof suppression flag \\
\hline SECTION_PRC & , , & Shell section property procedure \\
\hline NSECT & 1 & Shell section property number \\
\hline \multicolumn{3}{|l|}{The following values not used if SECTION_PRC is specified.} \\
\hline E & 30.E6 & Young's Modulus \\
\hline NU & 0.3 & Poisson's ratio \\
\hline WTDEN & 0.1 & Weight Density \\
\hline THICKNESS & . 1 & Shell thickness \\
\hline
\end{tabular}

\subsection*{2.5.3 ARGUMENT DESCRIPTIONS}

\subsection*{2.5.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <false>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffness (see argument DRILLING_DOF).

\subsection*{2.5.3.2 BC_PROCEDURE}

Name of user provided boundary condition procedure (default: ' '). The term "boundary conditions" refers both to displacement constraints and applied loading. If a boundary condition procedure is provided, the following call will be performed. The macrosymbol <es_nen> equals the number of element nodes, while the macrosymbols <n1> and <n2> equal the number of nodes actually generated along edges one and two.
```

*cal1 [BC_PROCEDURE] ( nodes_1 = <n1\rangle ; --
nodes_2 = <n2\rangle ; --
es_modes = <es_nen> ; --

```
```

drilling_dof = [drilling_dof] )

```

No action is taken if a boundary condition procedure name is not provided.

\subsection*{2.5.3.3 DRILLTNG_DOF}

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag set to <false> forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active - unless they are automatically suppressed by use of the AUTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{2.5.3.4 E}

Young's modulus (default: 30.E6). This argument is ignored if SECTION_PRC parameter is specified. See the description for SECTION_PRC for more detail.

\subsection*{2.5.3.5 EDGE_WEIGHTS}

Node placement can be weighted along each surface edge according to the EDGE_WEIGHTS parameter. The input format requires a list of four edge-node placement weightings representing the node weighting for edge1, edge2, edge3, and edge4 (default: 1.,1.,1.,1.).
The weighting value for a given edge represents the length of the last element divided by the length of the first element along that edge. The edge orientation arrows in figure 2.5-1 point from the first element to the last element along each edge. In the case of 9 -node quad elements, the midside and center nodes are positioned at the appropriate locations based on the elements natural coordinate system.

The procedure interprets negative weight values to mean the positive reciprocal. For example, a value of -5.0 is identical to a value of 0.2 .

\subsection*{2.5.3.6 ES_NAME}

Element name (default: EX97). This argument is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX97, is a 9 -node quadrilateral element implemented in processor ES1, and described reference 2.5-1.

\subsection*{2.5.3.7 ES_PARS}

Element research parameters (default: 0., ...). This argument is an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{2.5.3.8 ES_PROC}

Element processor (default: ES1) This argument is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{2.5.3.9 JREF}

Joint degree of freedom (dof) reference frame (default: -1 for global cylindrical). The user may provide any alternate frame which has been created prior to calling this procedure. A negative value causes the frame to be interpreted as a cylindrical reference frame.

\subsection*{2.5.3.10 NODES_1}

Number of nodes on edge 1 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 3. This number should be consistent with the element type selected. For example, NODES_1 can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.5.3.11 NODES_2}

Number of nodes on edge 2 including the nodes at the surface corners (default: 7). This argument is also the number of nodes on edge 4 . This number should be consistent with the element type selected. For example, NODES_2 can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{2.5.3.12 NSECT}

Shell section property number (default: 1). The NSECT value is required when defining the element using the processor ELD. See the description of SECTION_PRC for more detail.

\subsection*{2.5.3.13 NU}

Poisson's ratio (default: 0.3). This argument is ignored if the SECTION_PRC input parameter is specified. See the description of SECTION_PRC for more detail.

\subsection*{2.5.3.14 RTZ1}

The cylindrical coordinates ( \(r, \theta, z\) ) which define corner number 1 of the model surface ( \(\theta\) in degrees). The form of the input is three real values, each separated by a comma (default: \(1 ., 0 ., 0\). .) The surface is defined by four edges which are defined as a linear interpolation in cylindrical coordinates of four endpoints, or "corner" points.

\subsection*{2.5.3.15 RTZ2}

The cylindrical coordinates \((r, \theta, z)\) defining the corner number 2 of the model surface (default: 1.,0.,1.).

\subsection*{2.5.3.16 RTZ3}

The cylindrical coordinates \((r, \theta, z)\) defining the corner number 3 of the model surface (default: 1.,90.,1.).

\subsection*{2.5.3.17 RTZ4}

The cylindrical coordinates ( \(r, \theta, z\) ) defining the corner number 4 of the model surface (default: 1.,90.,0.).

\subsection*{2.5.3.18 SECTION_PRC}

Name of a user supplied procedure to define the plate section properties (default \(=\) ' '). If a section properties procedure is provided, the following call will be performed.
```

*call [section_prc] ( nsect = [nsect] )

```

The effect of the default is to allow the procedure to generate an isotropic material section based on the input parameters E, NU, WTDEN, and THICKNESS. The section number is defined by the input parameter NSECT. If the call parameter SECTION_PRC is defined by the user, then call parameters E, NU, WTDEN, and THICKNESS are ignored by procedure GEN_SHELL.

\subsection*{2.5.3.19 THICKNESS}

Thickness of the shell wall (default \(=1.0\) ). This argument is ignored if SECTION_PRC parameter is specified. See the description for SECTION_PRC for more detail.

\subsection*{2.5.3.20 WTDEN}

Weight density expressed in lb/in. \({ }^{3}\) (default: \(0.1 \mathrm{lb} / \mathrm{in} .^{3}\) ). This argument is ignored if the SECTION_PRC input parameter is specified. Processor LAU will convert the weight density to mass density using the gravitational acceleration constant \(386.4 \mathrm{in} / \mathrm{sec}^{2}\).

\subsection*{2.5.4 USAGE GUIDELINES AND EXAMPLES}

Procedure GEN_SHELL may be invoked using the \(*\) call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values in the procedure call. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.
```

*procedure $G E N_{-}$SHELL ( ES_PROC = ES1 ; ES_NAME = EX97 ; ES_PARS $=0.0$; --
RTZ1 $=1 ., 0 ., 0$. ; --
RTZ2 $=1 ., 0 ., 1$. ;--

```
```

RTZ3 = 1.,90.,1. ; --
RTZ4 = 1.,90.,0. ; --
NODES_1 = 7 ; --
NODES_2 = 7 ; --
EDGE_WEIGHTS = 1.,1.,1.,1. ; --
BC_PROCEDURE = , ; -- . Boundary condition procedure
DRILLING_DOF = \langletrue> ; --
AUTO_DOF_SUP = <true> ; --
SECTION_PRC = , ; -- . Shell section property procedure
NSECT = 1 ;- . Shell section property ID
The following values not used if SECTION_PRC specified
E = 30.E6 ; -- . Young's Modulus
NU = . 3 -- . Poissons ratio
THICKNESS = .1 -- . Shell thickness
)

```

\subsection*{2.5.4.1 Mesh Generation}

The method of surface generation used by procedure GEN_SHELL is described in the section. Termology depicted on figure 2.5-1 provides a visual interpretation of the parameters used to generate a curved surface.
To the define the shell surface, the user definess four coordinate positions in a cylindrical reference frame. These four positions represent four corners of a four sided region. The sides of the region (which will also be referred to as edges) are defined by linearly interpolating between the coordinate values of the corner points. The surface of the region is defined as a bi-linear interpolation of the four sides, also known as a Coon's surface (see refs. 2.5-2 and 2.5-3). It must be remembered that since interpolations are performed in cylindrical coordinates, the surface and its edges will not generally be flat or straight, but rather curved.


Figure 2.5-1 Generic Shell Surface Topology.

The connectivity of the surface is defined in figure 2.5-1. The user provides the coordinates for corners 1 to 4. Edge 1 of the region starts at corner 1 and ends at corner 2. The remaining edges are defined in a similar manner. The arrows indicate the orientation of the edges and the direction of increasing node numbers.

The topology of the resulting finite element grid is depicted in Figure 2.5-2. Nodes are created first along edge 1 , then in successive lines terminating along edge 3 . The user defines the number of nodes along edges 1 and 2, which also defines the number of nodes for edges 3 and 4. The relative position of the nodes along each edge may be controlled using the edge weighting parameter EDGE_WEIGHTS.


Figure 2.5-2 Node and Element Topology.
Recognizing that the surfaces generated by procedure GEN_SHELL are four sided surfaces in cylindrical coordinates, it will be shown, by example, how to generate segments of cylinders, cones, annular plates, spirals, and more general surfaces. For applications which require a complete axisymmetric surface, such as a 360 degree cylinder, the procedure has the capability of joining the resulting finite element mesh where two sides of the region are coincident. Closure occurs automatically but is checked only along edges 1 and 3 . Closure will not occur between edges 2 and 4 . Note also that the user must request the number of nodes along edge 2 as though the surface were not closed. This requirement is to say that the user should not presume closure will occur.

\subsection*{2.5.4.2 Cylindrical Shell Sections}

In this section there are presented examples of how procedure GEN SHELL may be used to create various shell segments on a right circular cylindrical surface.

In the following example, procedure GEN_SHELL is used to generate a cylindrical segment with radius of 5 inches and length of 10 inches. Only 90 degrees of the cylinder is generated (see figure 2.5-3).
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1 = 5.,0.,0.; --
rtz2 = 5.,0.,10. ; --
rtz3 = 5.,90.,10. ; --
rtz4 = 5.,90.,0. ; --
nodes_1 = 5 ; --
nodes_2 = 7 )

```

(a) 4-node elements

(b) 9-node elements

Figure 2.5-3 90 Degree Cylindrical Segment

This example creates a complete 360 degree cylindrical shell using 9 -node quadrilateral elements (see figure 2.5-4). Note that midside nodes are not shown. The input specifies elements at the end of edges 1 and 3 to be 5 times longer that elements at the beginning of the same edges. Closure of the cylinder is obtained by defining corner points 1 and 4, and corner points 2 and 3 , to be coincident in the \(r\) and \(z\) directions, with a difference in \(\theta\) of 360 degrees.
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX97' ; --
rtz1 = 5.,0.,0.; --
rtz2 = 5.,0.,10. ; --
rtz3 = 5.,360.,10. ; --
rtz4 = 5.,360.,0. ; --
nodes_1 = 11 ; --
nodes_2 = 25 ; --
edge_weights = 5.,1.,5.,1.)

```


Figure 2.5-4 Right Circular Cylinder - 9-node Elements

By simply increasing the \(z\) coordinate values for corner points 3 and 4 , the cylinder wall can be made to spiral about the \(z\) axis. The following example illustrates this technique. The resulting spiral is shown in figure 2.5-5. This configuration may be used to model a spring.
*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1 \(=5 ., 0 ., 0\). ; --
rtz2 = 5.,0.,2. ; --
rtz3 \(=5 ., 720 ., 12\). ; --
rtz4
nodes_1
\(=5 ., 720 ., 10\). : --
nodes_2
\(=5\); --
\(=37\) )


Figure 2.5-5 Spiraling Cylinder Wall

The following example produced the cylinder of skewed elements shown in figure 2.5-6.
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1 = 5.,0.,0.; --
rtz2 = 5.,90.,10. ; --
rtz3 = 5.,450.,10. ; --
rtz4 = 5.,360.,0. ; --
nodes_1
= 7 ; --
nodes_2 = 25 )

```


Figure 2.5-6 Cylinder With Skewed Elements

\subsection*{2.5.4.3 Conical Shell Sections}

In this section, examples of how procedure GEN_SHELL may be used to create shell segments on a conical surface are presented.

This example creates a complete 360 degree conical shell using 9 -node quadrilateral elements (see figure 2.5-7). Elements are defined at the top of the cones to be \(1 / 5\) as long axially as those at the base. Closure of the cone is obtained by defining corner points 1 and 4 , and corner points 2 and 3 , to be coincident in \(r\) and \(z\) directions, with a difference in \(\theta\) of 360 degrees.
```

*call GEN_SHELL ( es_proc = 'ES1' ; 0s_name = 'EX97' ; --
rtz1 = 5.,0.,0. ; --
rtz2 = 1.,0.,10. ; --
rtz3 = 1.,360.,10. ; --
rtz4 = 5.,360.,0. ; --
nodes_1 = 9 ; --
nodes_2 = 25 ; --
edge_\nablaeights = -4.,1.,-4.,1.)

```


Figure 2.5-7 Conical Shell - 9-Node Elements

In the following example, procedure GEN_SHELL is used to generate an unusual shell which lies on the conical surface of the previous example. The shell spans 360 degrees at the top but only spans 180 degrees at the base (see figure 2.5-8).
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1
rtz2
= 1.,0.,10. ; --
rtz3 = 1.,360.,10. ; --
rtz4 = 5.,270.,0. ; --
nodes_1 = 11; --
nodes_2 = 21; --
edge_meights = -3.,1.,-3.,1.)

```


Figure 2.5-8 Unusual Conical Shell

\subsection*{2.5.4.4 Annular Plates}

In this section examples of how procedure GEN_SHELL may be used to create annular shell segments are presented.
This example creates a 90 degree annular shell segment using 9-node quadrilateral elements (see figure 2.5-9). Note that the midside nodes are not shown. The plate has an inner radius of 1 inch and the outer radius of 5 inches. Element size weighting is also demonstrated.
*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX97' ; --
rtz1 \(=1 ., 0 ., 0\); -rtz2 \(=\) 5.,0.,0. ; --
rtz3 \(=5 ., 90 ., 0\). ; --
rtz4 \(=1 ., 90 ., 0\). ;-
nodes_1 \(=11\); -
nodes_2 \(=11\); --
edge_weights \(=6 ., 1 ., 6 ., 1\).


Figure 2.5-9 Flat Annular Shell

By simply increasing the \(z\) coordinate values for corner points 3 and 4, the annular surface can be made to spiral about the \(z\) axis. The following example illustrates this technique. The resulting spiral is shown in figure 2.5-10.
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name m 'EX47' ; --
rtz1 = 3.,0.,0.; --
rtz2 = 5.,0.,0. ; --
rtz3 = 5.,720.,10. ; --
rtz4 = 3.,720.,10. ; --
nodes_1 = 5 ; --
modes_2 = 33)

```


Figure 2.5-10 Spiraling Shell

\subsection*{2.5.4.5 Exotic Shell Sections}

In this section examples of how procedure GEM_SHELL may be used to create unusual shell segments are presented.

This example creates a spiraling surface which changes from a flat to a vertical shell while increasing in \(z\) direction and decreasing in radius (see figure 2.5-11).
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX97' ; --
rtz1 = 3.,0.,0. ; --
rtz2 = 5.,0.,0. ; --
rtz3 = 1.,720.,12.; --
rtz4 = 1.,720.,10.; --
modes_1 = 5; --
nodes_2 = 45)

```


Figure 2.5-11 Exotic Spiral Shell

In the following example, procedure GEN_SHELL is used to generate a vertical coiled shell (see figure 2.5-12).
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1 =0.,0.,0.;--
rtz2 = 0.,0.,1. ; --
rtz3 = 3.,1080.,1. ; --
rtz4 = 3.,1080.,0. ; --
nodes_1 = 5 ; --
nodes_2 = 85)

```


Figure 2.5-12 Vertical Coiled Shell

This example uses procedure GEN_SHELL to generate a fiat coiled shell (see figure 2.5-13).
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1 = 0.,0.,0.; -
rtz2
= 1.,0.,0. ; --
rtz3 = 9.,720.,0. ; --
rtz4 = 5.5,720.,0. ; --
nodes_1 = 5 ; --
nodes_2 = 51)

```


Figure 2.5-13 Flat Coiled Shell

Finally, an arbitrary shell is created to demonstrate the generality of the procedure GEN_SHELL (see figure 2.5-14).
```

*call GEN_SHELL ( es_proc = 'ES1' ; es_name = 'EX47' ; --
rtz1 = -2.,-25.,0. ; --
rtz2 = 7.,190.,-3. ; --
rtz3 = -2.,230.,7. ; --
rtz4 = 6.,0.,10. ; --
nodes_1 = 25 ; --
nodes_2 = 25)

```


Figure 2.5-14 Arbitrary Shell

\subsection*{2.5.5 LIMITATIONS}

As previously stated, to obtain closed axisymmetric surface models, the user must define edges 1 and 3 to be the coincident edges.

\subsection*{2.5.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{2.5.7 PROCEDURE FLOWCHART}
\begin{tabular}{ll} 
GEN_SHELL & (Shell generation procedure) \\
[BC_PROCEDURE] & (user supplied boundary conditions/loads procedure) \\
[SECTION_PRC] & (user supplied section property generation procedure) \\
CYL_NODES & (surface node generation procedure) \\
CYL_ELT_CONN & (element connectivity definition procedure)
\end{tabular}

\subsection*{2.5.8 PROCEDURE LISTING}
```

*procedure GEN_SHELL ( es_proc = es1 ; es_name = ex97 ; es_pars = 0. ; --
rtz1 = 1.,0.,0. ; --
rtz2 = 1.,0.,1. ; --
rtz3 = 1.,90.,1. ; --
rtz4 = 1.,90.,0. ; --
nodes_1 = 7 ; --
nodes_2 = 7 ; --
edge_weights = 1.,1.,1.,1. ; --
jref = -1 ; -- . Joint dof reference frame
bc_procedure = , ; -- . Boundary condition procedure
online = 0 ; -- . supress nodes/elts output
drilling_dof = <true> ; --
auto_dof_sup = <true> ; --
section_prc = , ; -- . Shell section property procedure
The follouing values used only if section_prc not specified
nsect = 1 ; -- . Shell section property ID
E = 30.E6 ; -- . Young's Modulus
NU = . 3 ; -- . Poisons ratio
WTDEN = .1 ; -- . Weight Density
thickness = .1 -- . Shell thickness
)

```

```

. Model Definition Procedure for GENeric Shell in cylindrical coordinates
. A general purpose clip procedure to create the finite element

```
```

        mesh for partial or complete cylindrical shell using 4 or
        9 noded quadrilateral elements.
    Note that when generating a 360 degree closed shell,
the caller should specify the number of circumferential nodes as
if the cylindrical shell were not closed, or in other words,
the line of nodes where closure occurs should be counted twice.
There will only be one set of nodes actually create where
closure occurs.
There is no verification performed to detect overlapping or
otherwise improbable element generation. This should be done
prior to calling this utility.
If a procedure to generate shell section properties is not provided,
the isotropic section described by E, NU, WTDEN, and THICKNESS will
be automatically generated. (see [section_prc] parameter)
A boundary condition procedure should be provided but is
optional. If not provided, no boundary conditions will be
defined. (see [bc_procedure] parameter)
\#remark ****************************************
*remark GEN_SHELL MODEL GENERATION PROCEDORE

```

```

*def/i n1 = [nodes_1]
*def/i n2 = [nodes_2]
*def/e rtz1[1:3] = [rtz1]
*def/e rtz2[1:3] = [rtz2]
*def/e rtz3[1:3] = [rtz3]
*def/e rtz4[1:3] = [rtz4]
*def/e w[1:4] = [edge_weights]
*def/e rc[1:4] = <rtz1[1]>,\langlertz2[1]>,\langlertz3[1]\rangle,\langlertz4[1]>
*def/e tc[1:4] = <rtz1[2]>,\langlertz2[2]>,\langlertz3[2]\rangle,\langlertz4[2]\rangle
*def/0 zc[1:4] = <rtz1[3]>,\langlertz2[3]>,\langlertz3[3]>,\langlertz4[3]\rangle

```

```

    Register Element and Define Macros: ES_NEN, ES_NIP, ES_NSTR, etc.
    ```

```

    *call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
            es_name = [es_name] ; es_pars = [es_pars])
    ```

```

        Define nodal coordinates and element connectivities into
        separate formatted liles. These files are gauranteed to have
        unique names that are not currently in use in the current
        directory.
    ```

```

    #def/i chk_closure = 1
    [xqt mesh
    *if <mesh_err>/then
    ```
```

    *remark Error occurred during MESH processor execution.
    *remark GEN_SHELL procedure terminated.
    *eof
    *endif

```

```

    Construct Model Data-base with TESTBED Processors
    =================================================
    [XQT TAB
START <tot_nodes>
ONLINE = [online]
JLOC
FORMAT = 2 . use cylindrical coordinate system
*show macros node_file
*add <node_file>

```

```

    Define DOF Directions
    ======ェ======ェ=======
        JREF . Use local cylindrical basis vectors
        . for nodal DOFS:
                                . u,v,w = radial, circumfer., axial
        NGEF = [jref]
        1 <tot_nodes> . same convention for all nodes
    ```

```

.D.D.Dine Load/Boundary Conditions If Procedure Supplied
*if <not(<ifelse([bc_procedure]; ;1;0)>)> /then
*call [BC_PROCEDORE] ( nodes_1 = <n1> ; --
nodes_2 = <n2> ; --
es_nodes = <es_nen> ; --
drilling_dof = [drilling_dof] )
**lse
*remark **********************************
*romark BOUNDARY CDNDITIONS NOT SPECIFIED

```

```

*endif

```

```

. Define Shell Section Properties
. =========================\=====
*if <not(<ifelse([section_prc]; ;1;0)>)>/then
*call [section_prc] ( nsect = [nsect] )
*olse

```

```

. Define the default Material and Section Properties

```

-
.
```

*def/e G = < [E]/(2.*(1+[NO])) >

```
[XQT AOS
\begin{tabular}{|c|}
\hline \multirow[t]{5}{*}{```
TABLE(ni=16,nj=1): OMB DATA 1 1
i = 1, 2,3,4,5,6,7,8,9
j = 1
E11 NU12 E22 G12 G13 G23 ALPHA1 ALPHA2 WTDEN
[E] [NO] [E] <G> <G> <G\rangle 0. 0. [WTDEN]
Build Laminate Data Tables
TABLE(ni=3,nj=1,itype=0): LAM OMB [nsect] 1
i = 1,2,3
j = 1 matl * layer thickness matl angle
1 [thickness]
0.
```} \\
\hline \\
\hline \\
\hline \\
\hline \\
\hline
\end{tabular}
        [XQT LAU
        ONLINE \(=2\)
    *endif

        Generate Elements

    [XQT ELD
    <ES_EXPE_CMD>
    NSECT \(=\) [nsect]
        Define element nodal connectivity
*show macros elem_file
        *add 〈olem_file>

            Suppress DOFs not supported by elements

        *if < [AUTO_DOF_SUP] >/then
        *call ES ( function = 'DEFINE FREEDOMS' )
    *endif
*end

\subsection*{2.5.9 REFERENCES}
2.5-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
2.5-2 Cook, William A.: "Body Oriented (Natural) Coordinates For Generating ThreeDimensional Meshes." International Journal For Numerical Methods in Engineering, 1974, Volume 8, pp. 27-43.
2.5-3 Forrest, A. R.: On Coons and Other Methods for the Representation of Curved Surfaces. Computer Graphics and Image Processing, 1972, Volume 1, pp. 341-359.

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\subsection*{3.0 Solution Procedures}

The procedures documented in this chapter are for specific analysis tasks. These procedures provide examples of how to perform common structural analysis tasks (e.g., static solution, eigensolution) using the command language and processors available in the CSM Testbed Software System.
A summary of the procedures found in this chapter is provided in Table 3.0-1.

Table 3.0-1 Solution Procedures
\begin{tabular}{ll}
\hline Procedure Name & \multicolumn{1}{c}{ Analysis Description } \\
\hline L_DYNAMIC_0 & \begin{tabular}{l} 
Linear transient dynamic analysis using modal anal- \\
ysis
\end{tabular} \\
\hline L_DYNAMIC_1 & \begin{tabular}{l} 
Linear transient dynamic analysis using Newmark al- \\
gorithm
\end{tabular} \\
\hline L_STABIL_1 & \begin{tabular}{l} 
Linear stability (buckling eigenvalue) analysis with \\
prescribed prestress
\end{tabular} \\
\hline L_STABIL_2 & \begin{tabular}{l} 
Linear stability (buckling eigenvalue) analysis with \\
linearly-computed prestress
\end{tabular} \\
\hline L_STATIC & \begin{tabular}{l} 
Linear static analysis
\end{tabular} \\
\hline L_VIBRAT_0 & \begin{tabular}{l} 
Linear vibration (eigenvalue) analysis about un- \\
stressed state
\end{tabular} \\
\hline L_VIBRAT_1 & \begin{tabular}{l} 
Linear vibration (eigenvalue) analysis about a pre- \\
scribed prestressed state
\end{tabular} \\
\hline L_VIBRAT_2 & \begin{tabular}{l} 
Linear vibration (eigenvalue) analysis about a linearly- \\
computed prestressed state
\end{tabular} \\
\hline NL_STATIC_1 & \begin{tabular}{l} 
Nonlinear static analysis; modified Newton iteration \\
with arc-length control
\end{tabular} \\
\hline NL_STATIC_2 & \begin{tabular}{l} 
Advanced Riks method
\end{tabular} \\
\hline NL_DYNAMIC_1 & \begin{tabular}{l} 
Nonlinear Dynamic Analysis
\end{tabular} \\
\hline
\end{tabular}

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\subsection*{3.1 Processor L_DYNAMIC_0}

THIS SECTION UNDER PREPARATION

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\subsection*{3.2 Procedure L_DYNAMIC_1}

\subsection*{3.2.1 GENERAL DESCRIPTION}

Procedure L_DYNAMIC_1 performs a linear transient dynamic analysis using either the Newmark- \(\beta\) implicit direct time integration procedure outlined in reference 3.2-1. When Procedure L_DYNAMIC_1 is called, a transient response calculation by direct integration of the system equations with a fixed time step is performed. Procedure L_DYNamIC calls Procedure NEWMARK which implements the well-known Newmark integration method for second order, coupled systems. Parameters such as the names of the system stiffness and mass matrices, the time step, and the total number of time steps in the analysis are formal arguments to Procedure L_DYHAMIC_1. In Procedure NEMMARK, extensive use is made of the CLAMP macro expression capability for calculating integration constants and controlling the algorithm. The initial acceleration at time \(t=0\) is calculated from the given initial displacement and velocity vectors. This is done by using processor AUS to set up the equations of motion at \(t=0\), and processors INV and SSOL to solve for the acceleration. At each subsequent time step, processor AUS is used to set up the recursion relations, and processor SSOL is used to solve for the displacement vector at the next time step. Then velocity and acceleration vectors are calculated and selectively printed.

\subsection*{3.2.2 THEORY}

\subsection*{3.2.2.1 Introduction}

The equations of motion for an undamped, linear elastic structure at time \(t+\Delta t\) are
\[
\begin{equation*}
\mathbf{M} \ddot{\mathbf{u}}_{t+\Delta t}+\mathbf{K} \mathbf{u}_{t+\Delta t}=\mathbf{P}_{t+\Delta t} \tag{3.2-1}
\end{equation*}
\]
where
M is the mass matrix
\(K\) is the linear elastic stiffness matrix
\(\mathbf{P}_{t+\Delta t}\) is the load vector at time \(t+\Delta t\)
\(\mathbf{u}_{t+\Delta t}\) is the displacement vector at time \(t+\Delta t\)
\(\ddot{\mathbf{u}}_{t+\Delta t}\) is the acceleration vector at time \(t+\Delta t\)

\subsection*{3.2.2.2 Newmark- \(\boldsymbol{\beta}\) Method}

The Newmark- \(\beta\) method is an implicit direct time integration procedure that is based on the following assumptions:
\[
\begin{align*}
\dot{\mathbf{u}}_{t+\Delta t} & =\dot{\mathbf{u}}_{t}+\left[(1-\gamma) \ddot{\mathrm{u}}_{t}+\gamma \ddot{\mathrm{u}}_{t+\Delta t}\right] \Delta t  \tag{3.2-2}\\
\mathbf{u}_{t+\Delta t} & =\mathbf{u}_{t}+\Delta t \dot{\mathbf{u}}_{t}+\left[\left(\frac{1}{2}-\beta\right) \ddot{\mathrm{u}}_{t}+\beta \ddot{\mathrm{u}}_{t+\Delta t}\right](\Delta t)^{2} \tag{3.2-3}
\end{align*}
\]
where
\(\dot{\mathbf{u}}_{t+\Delta t}\) is the velocity vector at time \(t+\Delta t\)
\(\Delta t\) is time step size
The parameters \(\gamma\) and \(\beta\) determine integration accuracy and stability. When \(\gamma=\frac{1}{2}\) and \(\beta=\frac{1}{6}\), the linear acceleration method is obtained (i.e., the acceleration is assumed to vary linearly over a time step). When \(\gamma=\frac{1}{2}\) and \(\beta=\frac{1}{4}\), Newmark's original, constant-averageacceleration method (also called the trapezoidal rule) is obtained.

\subsection*{3.2.3 ALGORITHM}

The Procedure L_DYNAMIC_1 closely follows the computational procedure presented in reference 3.2-1. Briefly, an outline of the procedure is as follows:
1. Select time step size, \(\triangle t\), and parameters \(\gamma\) and \(\beta\). Calculate integration constants:
\[
\begin{array}{rlrl}
\gamma \geq \frac{1}{2} ; \quad \beta \geq \frac{1}{4}\left(\frac{1}{2}+\gamma\right)^{2} ; \\
a_{o} & =\frac{1}{\beta(\Delta t)^{2}} ; & a_{1} & =\frac{\gamma}{\beta \Delta t} ; \quad a_{2}=\frac{1}{\beta(\Delta t)} ; \\
a_{3} & =\frac{1}{2 \beta}-1 ; & a_{4} & =\frac{\gamma}{\beta}-1 ; \quad a_{5}=\frac{\Delta t}{2}\left(\frac{\gamma}{\beta}-2\right) ; \\
a_{6} & =\triangle t(1-\gamma) ; & a_{7} & =\gamma \Delta t
\end{array}
\]
2. Initialize displacements \(\mathbf{u}_{\mathbf{o}}\), velocities \(\dot{\mathbf{u}}_{\mathbf{o}}\), and accelerations \(\ddot{\mathbf{u}}_{\mathbf{o}}\).
3. Form effective stiffness matrix \(\hat{\mathbf{K}}\)
\[
\hat{\mathbf{K}}=\mathbf{K}+a_{0} \mathbf{M}
\]
4. Decompose \(\hat{\mathbf{K}}\)
\[
\hat{\mathbf{K}}=\mathbf{L D L}^{\boldsymbol{T}}
\]

For each time step:
5. Calculate effective loads \(\hat{\mathbf{R}}_{t+\Delta t}\)
\[
\hat{\mathbf{R}}_{t+\Delta t}=\mathbf{P}_{t+\Delta t}+\mathbf{M}\left(a_{o} u_{t}+a_{2} \dot{\mathbf{u}}_{t}+a_{3} \ddot{\mathbf{u}}_{t}\right)
\]
6. Solve for displacements at time \(t+\Delta t\)
\[
\mathbf{L D L}^{T} \mathbf{u}_{t+\Delta t}=\hat{\mathbf{R}}_{t+\Delta t}
\]
7. Calculate accelerations and velocities at time \(t+\Delta t\)
\[
\begin{aligned}
& \ddot{\mathbf{u}}_{t+\Delta t}=a_{o}\left(\mathbf{u}_{t+\Delta t}-\mathbf{u}_{t}\right)-a_{2} \dot{\mathbf{u}}_{t}-a_{3} \ddot{\mathbf{u}}_{t} \\
& \dot{\mathbf{u}}_{t+\Delta t}=\dot{\mathbf{u}}_{t}+a_{6} \ddot{\mathbf{u}}_{t}+a_{7} \ddot{\mathbf{u}}_{t+\Delta t}
\end{aligned}
\]

This procedure neglects damping and assumes that a single, constant time step size \(\Delta t\) is used throughout the analysis.

\subsection*{3.2.4 PROCEDURE USAGE}

Procedure L_DYNAMIC_1 is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.
```

*call L_DYNAMIC_1 ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for Procedure L_DYNAMIC_1 are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For Procedure L_DYNAMIC_1, the following table lists each argument, its default value and meaning.
\begin{tabular}{lcl} 
Argument & Default Value & Meaning \\
\cline { 2 - 4 } DELT & - & Time increment, \(\Delta t\) \\
NSTEP & - & Number of time steps \\
\hline BETA & 0.25 & Time integrator parameter \\
GAMAA & 0.50 & Time integrator parameter
\end{tabular}

\subsection*{3.2.5 ARGUMENT DESCRIPTION}

\subsection*{3.2.5.1 BETA}

Newmark- \(\beta\) time integrator parameter, \(\beta\) (default: 1/4).

\subsection*{3.2.5.2 DELT}

Time step size. This argument specifies the size of the time step to be used in the analysis. A constant step size is assumed per procedure call.

\subsection*{3.2.5.3 GAMMA}

Newmark- \(\beta\) time integrator parameter \(\gamma\) (default: 1/6).

\subsection*{3.2.5.4 NSTEP}

Number of time steps to march. This argument specifies the number of time steps to march in the transient response prediction using a constant time step size of DELT.

\subsection*{3.2.6 PROCEDURE FLOWCHART}
\begin{tabular}{rl} 
L_DYNAMIC_1 & (main procedure) \\
NEWMARK & (Newmark- \(\beta\) time integration)
\end{tabular}

\subsection*{3.2.7 LIMITATIONS}

None.

\subsection*{3.2.8 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{3.2.9 USAGE GUIDELINES AND EXAMPLES}

Procedure L_DYNAMIC_1 is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_DYNAMIC_1 ( delt = 0.02 ; --
nstep = 100 ; --
beta = 0.25 ; --
gamma = 0.50)

```

\subsection*{3.2.10 PROCEDURE LISTING}

\subsection*{3.2.11 REFERENCES}
3.2-1 Bathe, K. J., Finite Element Procedures in Engineering Analysis, Prentice-Hall, Inc., Englewood Cliffs, New Jersey, 1982, pp. 511-512.

\subsection*{3.3 Procedure L_STABIL_1}

\subsection*{3.3.1 GENERAL DESCRIPTION}

Procedure L_STABIL_1 performs linear stability analysis using an eigensolver selected by the global macrosymbol eigensolver_name (e.g., EIG2, LAN, LANZ) and structural element (ESi) processors based on the generic element processor template. The procedure assumes that the finite element model, loads, and boundary conditions have already been generated, that the prebuckling stress state has been specified, and that the buckling loads and mode shapes need to be calculated. The prebuckling stress state (i.e., prestress state) is specified by prescribing values for procedure L_STABIL_1 arguments. A linear stability analysis is performed using this prescribed stress state.

\subsection*{3.3.2 THEORY}

Linear elastic stability analyses may be formulated using the concept of adjacent equilibrium. Membrane forces in beams, plates, and shells result in an equilibrium configuration in which the deformation pattern is tangent to the midsurface of the structure. However, another equilibrium configuration involving out-of-plane deflections and rotations may be adjacent to this membrane state. Buckling occurs when this membrane strain energy is converted to bending strain energy. The linear elastic stability analysis is an eigenvalue problem to calculate the critical load for the bifurcation in the solution (e.g., change from a membrane state to a bending state). This eigenvalue problem can be written as
\[
\begin{equation*}
\mathbf{K} \phi_{i}+\lambda_{i} \mathbf{K}_{g}(\sigma) \phi_{i}=\mathbf{0} \quad i=1,2, \ldots \tag{3.3-1}
\end{equation*}
\]
where
\[
\begin{aligned}
\mathbf{K} & =\text { assembled linear elastic stiffness matrix } \\
\mathbf{K}_{g}(\sigma) & =\text { assembled geometric stiffness matrix } \\
\boldsymbol{\phi}_{\boldsymbol{i}} & =i \text {-th eigenvector or modeshape } \\
\lambda_{i} & =i \text {-th eigenvalue or buckling load factor }
\end{aligned}
\]

The matrix denoted by \(\mathbf{K}_{g}\) has been called the initial stress stiffness matrix, the differential stiffness matrix, the geometric stiffness matrix, and the stability coefficient matrix (e.g., see ref. 3.3-1). It is independent of the elastic properties of the structure and dependent on the geometry, displacement field, and state of stress. Herein the matrix \(\mathbf{K}_{\boldsymbol{g}}\) will be referred to as the geometric stiffness matrix.

A general formulation for the geometric stiffness matrix is presented in reference 3.3-1. Strains can be written as
\[
\begin{equation*}
\boldsymbol{\epsilon}=\epsilon_{\mathbf{L}}+\epsilon_{\mathbf{N L}} \tag{3.3-2}
\end{equation*}
\]
where \(\epsilon_{L}\) contains the linear strain-displacement terms and \(\epsilon_{\mathrm{NL}}\) contains the higher-order or nonlinear strain-displacement terms. For a given stress state \(\sigma_{0}\), elastic strain energy
is stored and can be expressed as
\[
\begin{equation*}
U=U_{L}+U_{N L} \tag{3.3-3}
\end{equation*}
\]
where
\[
\begin{align*}
U & =\frac{1}{2} \int_{V} \epsilon^{T} \sigma_{0} d V  \tag{3.3-4a}\\
U_{L} & =\frac{1}{2} \int_{V} \epsilon_{\mathrm{L}}^{T} \sigma_{0} d V  \tag{3.3-4b}\\
U_{N L} & =\frac{1}{2} \int_{V} \epsilon_{\mathrm{NL}}^{T} \sigma_{0} d V \tag{3.3-4c}
\end{align*}
\]

The geometric stiffness matrix is derived from the strain energy produced by stresses acting through displacements associated with the nonlinear strain-displacement relations. These relations couple the membrane and bending effects. Typically the strain-displacements relations are written using index notation as
\[
\begin{equation*}
\epsilon_{i j}=\frac{1}{2}\left[\partial_{i} u_{j}+\partial_{j} u_{i}+\partial_{i} u_{k} \partial_{j} u_{k}\right] \tag{3.3-5}
\end{equation*}
\]
where \(u_{i}=(u, v, w)\) for \(i=1,2,3\), respectively, \(\partial_{i}\) denotes differentiation with respect to \(i\) th coordinate direction and summation over repeated indices is implied. Let d denote the nodal degrees of freedom, then
\[
\begin{equation*}
\delta=\mathbf{G d} \tag{3.3-6}
\end{equation*}
\]
where
\[
\delta=\left\{\partial_{x} u, \partial_{y} u, \partial_{z} u, \partial_{x} v, \partial_{y} v, \partial_{z} v, \partial_{x} w, \partial_{y} w, \partial_{z} w\right\}
\]

The coefficients of \(\mathbf{G}\) are obtained by differentiating the element shape functions. Finally the matrix \(\mathbf{Q}\) is defined as
\[
\mathbf{Q}=\left[\begin{array}{ccccccccc}
\partial_{x} u & 0 & 0 & \partial_{x} v & 0 & 0 & \partial_{x} w & 0 & 0  \tag{3.3-7}\\
0 & \partial_{y} u & 0 & 0 & \partial_{y} v & 0 & 0 & \partial_{y} w & 0 \\
0 & 0 & \partial_{z} u & 0 & 0 & \partial_{z} v & 0 & 0 & \partial_{z} w \\
\partial_{y} u & \partial_{x} u & 0 & \partial_{y} v & \partial_{x} v & 0 & \partial_{y} w & \partial_{x} w & 0 \\
0 & \partial_{z} u & \partial_{y} u & 0 & \partial_{z} v & \partial_{y} v & 0 & \partial_{z} w & \partial_{y} w \\
\partial_{z} u & 0 & \partial_{x} u & \partial_{z} v & 0 & \partial_{x} v & \partial_{z} w & 0 & \partial_{x} w
\end{array}\right]
\]

With these definitions the nonlinear strains given by equation (3.3-2) can be written as
\[
\begin{equation*}
\boldsymbol{\epsilon}_{\mathbf{N L}}=\frac{1}{2} \mathbf{Q} \mathbf{G d} \tag{3.3-8}
\end{equation*}
\]

The vector of initial stresses is
\[
\sigma_{0}=\left\{\begin{array}{lllll}
\sigma_{x 0} & \sigma_{y 0} & \sigma_{z 0} & \tau_{x y 0} & \tau_{y z 0}  \tag{3.3-9}\\
\tau_{x x 0}
\end{array}\right\}
\]

Substituting equations (3.3-6) through (3.3-9) into equation (3.3-4c) gives
\[
\begin{equation*}
U_{N L}=\frac{1}{2} \mathrm{~d}^{T}\left(\int_{V} \mathbf{G}^{T} \mathbf{Q}^{T} \sigma_{0} d V\right) \tag{3.3-10}
\end{equation*}
\]

However, the term \(\mathbf{Q}^{\boldsymbol{T}} \sigma_{0}\) can be written as
\[
Q^{T} \sigma_{0}=\left[\begin{array}{lll}
\mathbf{s} & 0 & 0  \tag{3.3-11}\\
0 & \mathrm{~s} & 0 \\
0 & 0 & \mathrm{~s}
\end{array}\right] \delta=\overline{\mathbf{S}}\left(\sigma_{0}\right) \boldsymbol{\delta}
\]
where
\[
\mathrm{s}=\left[\begin{array}{ccc}
\sigma_{x 0} & \tau_{x y 0} & \tau_{x z 0}  \tag{3.3-12}\\
\tau_{x y 0} & \sigma_{y 0} & \tau_{y z 0} \\
\tau_{x x 0} & \tau_{y z 0} & \sigma_{z 0}
\end{array}\right]
\]

With these expressions, a general form of the geometric stiffness matrix can be written as
\[
\begin{equation*}
\mathbf{K}_{g}(\sigma)=\int_{V} \mathbf{G}^{T} \overline{\mathbf{S}}\left(\sigma_{0}\right) \mathbf{G} d V \tag{3.3-13}
\end{equation*}
\]
which is symmetric and explicitly dependent on the stress state.
The stress state used to form the geometric stiffness matrix may be obtained in two ways. The first way is first to perform a linear static stress analysis for the given load set and constraint set. This way is used in procedure L_STABIL_2. The second way is to specify, in advance, the values of the stress components given in equation (3.3-11) (i.e., specify the prestress state). This way is used in procedure L_STABIL_1.

\subsection*{3.3.3 ALGORITHM}

The algorithm used to solve equation (3.3-1) depends on the value of the global macrosymbol eigensolver_name. Processor EIG2 is used if eigensolver_name is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.3-2. Processor LAN is used if eigensolver_name is defined to be LAN. Processor LANZ is used if eigensolver_name is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.3-2 to 3.3-4.

\subsection*{3.3.4 PROCEDURE USAGE}

Procedure L_STABIL_1 may be invoked by the *call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
*call L_STABIL_1 ( arg1 = val1; arg2 = val2; ...)
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L_STABIL_1; note that those arguments without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline PS_1 & -- & Prebuckling membrane stress resultant \(N_{x}^{o}\) \\
\hline PS_2 & -- & Prebuckling membrane stress resultant \(N_{y}^{\circ}\) \\
\hline PS_3 & -- & Prebuckling membrane stress resultant \(N_{x y}^{o}\) \\
\hline BCON_SET & 1 & Constraint set for buckling analysis \\
\hline ERROR_TOL & . 0001 & Convergence criterion for eigenvalues \\
\hline FUNCTION & ALL & Select function to be performed by procedure \\
\hline INIT_VECTOR & 0 & Number of initial vectors used to span the subspace \\
\hline ISEQ & 0 & Resequencing method to be used \\
\hline LDI & 1 & Local device index \\
\hline LOAD_SET & 1 & Load set number \\
\hline KNAME & K & First word of the name of the dataset containing the assembled stiffness matrix \\
\hline max_ITERS & 20 & Maximum number of iterations allowed \\
\hline H_GROUPS & 1 & \\
\hline H.MODES & 1 & Number of eigenvalues to converge \\
\hline PRINT & <false> & Flag to print displacement solution, internal forces, and element stresses, and eigenvectors \\
\hline RENUMBER & <true> & Flag to resequence node numbers for equation solver \\
\hline SHIFT & 0.0 & Eigenvalue shift \\
\hline
\end{tabular}

Tables 3.3-1, 3.3-2, and 3.3-3 list the datasets used or created by procedure L_STABIL_1, the procedures invoked by procedure L_STABIL_1, and the processors invoked by procedure L_STABIL_1, respectively.
\begin{tabular}{|l|l|c|c|}
\hline \multicolumn{4}{|c|}{ Table 3.3-1 Datasets Input/Output by procedure L_STABIL_1 } \\
\hline Dataset & Description & Input & Output \\
\hline AMAP..ic2.isize & Factorization Map for INV & & \(\checkmark\) \\
\hline BUCK.EVAL.i. \(j^{\dagger}\) & Buckling eigenvalues & & \(\checkmark\) \\
\hline BUCK.MODE.i. \(\dagger\) & Buckling eigenvalues & & \(\checkmark\) \\
\hline <ES_NAME>.EFIL.0.nnod & Element Computational Data & \(\checkmark\) & \(\checkmark\) \\
\hline ES.SUMMARY & ES Processor Status & \(\checkmark\) & \(\checkmark\) \\
\hline DEF.<ES_NAME>.0.nnod & Element Definition (Connectivity) & \(\checkmark\) & \\
\hline DIR.<ES_NAME>.0.nnod & Element EFIL Directory & \(\checkmark\) & \\
\hline INV.KSHF.j \(\dagger\) & Factored Shifted System Matrix & & \(\checkmark\) \\
\hline INV.<KNAME>. \(\dagger\) & Factored System Matrix & & \(\checkmark\) \\
\hline JDF1.BTAB.1.8 & Model Summary & \(\checkmark\) & \\
\hline KG.SPAR.jdf2 & Assembled geometric stiffness matrix & & \(\checkmark\) \\
\hline KMAP..ic2.isize & Model Connectivity Map & & \(\checkmark\) \\
\hline <KNAME>.SPAR.jdf2 & Assembled system matrix & & \(\checkmark\) \\
\hline \(\boldsymbol{i}=\) <load_set> and \(j=\) <cons_set> & & \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Table 3.3-2 & \multicolumn{3}{|l|}{ Sub-Procedures Invoked by procedure L_STABIL_1 } \\
\hline Procedure & Type & Function \\
\hline ES & External & Element utility procedure \\
\hline FACTOR & External & Factors assembled stiffness matrix \\
\hline L_STABIL_1 & Internal & Main procedure \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \multicolumn{2}{|c|}{ Table 3.3-3 Processors Invoked by procedure L_STABIL_1 } \\
\hline Procedure & Type & Function \\
\hline AUS & Internal & Arithmetic Utilities \\
\hline E & Internal & Initializes EFIL datasets \\
\hline EIG2 & Internal & Solve eigenvalue problem using subspace iteration \\
\hline ESi & External & Element processors based on GEP \\
\hline K & Internal & Assemble system matrix \\
\hline LAN & External & Solve eigenvalue problem using Lanczos method \\
\hline LANZ & External & Solve eigenvalue problem using Lanczos method \\
\hline RSEQ & Internal & Resequences nodes for equation solving \\
\hline TOPO & Internal & Generates nodal topology maps \\
\hline VPRT & Internal & Print SYSVEC system vectors \\
\hline
\end{tabular}

\subsection*{3.3.5 ARGUMENT DESCRIPTION}

\subsection*{3.3.5.1 BCON_SET}

Constraint set number for buckling analysis (default: 1). This argument selects which constraint set to use in solving the linear stability problem.

\subsection*{3.3.5.2 ERROR_TOL}

Convergence criterion for eigenvalues (default: 0.0001). For the \(k\)-th iteration, the error measure for the \(i\)-th eigenvalue is
\[
\epsilon_{i}^{k}=\frac{\left\|\left(\lambda_{i}^{k}-\lambda_{i}^{k-1}\right)\right\|}{\left\|\lambda_{i}^{k}\right\|}
\]

The \(i\)-th eigenvalue is converged if \(\epsilon_{i}^{k}\) is smaller than ERROR_TOL.

\subsection*{3.3.5.3 FUNCTION}

Select function to be performed by procedure L_STABIL_1 (default: ALL). This procedure may be used to perform two functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh
topology is analyzed, the system stiffness matrix is assembled and factored, and the eigenproblem is solved. For FUNCTION=EIGEN, procedure L_STABIL_1 uses a prescribed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

\subsection*{3.3.5.4 INIT_VECTOR}

Number of initial vectors used to span the subspace (default: 0 ). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT_VECTOR=0, the number of initial vectors will be calculated by the procedure as
```

INIT_VECTOR=MINIMOM (2*N_MODES, H_MODES + 8)

```

\subsection*{3.3.5.5 ISEQ}

Resequencing method to be used (default: 0). If the argument RENUMBER is <true>, then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (i.e., method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.3-2).

\subsection*{3.3.5.6 XNAME}

First word of the dataset name containing the assembled stiffness matrix (default: \(\mathbb{K}\) ).

\subsection*{3.3.5.7 LDI}

Logical device index (default: 1).

\subsection*{3.3.5.8 MAX_ITERS}

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

\subsection*{3.3.5.9 N_GROUPS}

\subsection*{3.3.5.10 N_MODES}

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR_TOL.

\subsection*{3.3.5.11 PRINT}

Flag to print modeshapes (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the buckling modeshapes.

\subsection*{3.3.5.12 PS_1}

Prescribed membrane stress resultant \(N_{x}^{o}\) for the prestressed state.

\subsection*{3.3.5.13 PS_2}

Prescribed membrane stress resultant \(N_{y}^{o}\) for the prestressed state.

\subsection*{3.3.5.14 PS_3}

Prescribed membrane stress resultant \(N_{x y}^{o}\) for the prestressed state.

\subsection*{3.3.5.15 RENUMBER}

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENOMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

\subsection*{3.3.5.16 SHIFT}

Eigenvalue shift (default: 0.0 ). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the shift in the buckling load factor.

\subsection*{3.3.6 PROCEDURE FLOWCHART}
\begin{tabular}{ll} 
L_STABIL_1 & (main procedure) \\
INITIALIZE & (initialize) \\
STIFFNESS & (form K) \\
STIFFNESS & (form \(\mathbf{K}_{g}\) ) \\
FACTOR & (factor using buckling boundary conditions) \\
EIGEN & (perform eigenvalue analysis)
\end{tabular}

\subsection*{3.3.7 LIMITATIONS}

None.

\subsection*{3.3.8 ERROR MESSAGES AND WARNINGS}

None.
3.3-8

\subsection*{3.3.8 USAGE GUIDELINES AND EXAMPLES}

Procedure L_STABIL_1 may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_STABIL_1 ( FUNCTION = ALL ; -- . Select function
BCON_SET = 1 ; -- . Select buckling constraint set
ERROR_TOL = . 0001; -- . Eigenvalue convergence criterion
INIT_VECTOR = 0 ; -- . Number of initial vectors
ISEQ =-1 ; -- . Select resequencing method
KNAME = K ; -- . First word of stiffness matrix
-- . dataset name
MAX_ITERS = 20; -- Maximum number of iterations
N_MODES = 1 ; -- Number of eigenvalues
N_GROUPS = 1 ; --
PS_1 ; --
PS_2 ; --
PS_3 ; --
PRINT = <true> ; -- . PRINT flag
RENOMBER = <true> ; -- . RESEQUENCING flag
SHIFT =0.0; Eigenvalue shift
)

```

Before procedure L_STABIL_1 is called, the global macrosymbol eigensolver_name should be defined as described in Section 3.3.3; otherwise, the default value of EIG2 will be used.

\subsection*{3.3.10 PROCEDURE LISTING}

\subsection*{3.3.11 REFERENCES}
3.3-1 Cook, Robert D.: Concepts and Applications of Finite Element Analysis. (Second Edition). John Wiley and Sons, Inc., New York 1981.
3.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.3-3 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
3.3-4 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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\subsection*{3.4 Procedure L_STABIL_2}

\subsection*{3.4.1 GENERAL DESCRIPTION}

Procedure L_STABIL_2 performs linear stability analysis using an eigensolver selected by the global macrosymbol eigensolver_name (e.g., EIG2, LAN, LANZ) and structural element ( \(\mathrm{ES} \boldsymbol{i}\) ) processors based on the generic element processor template. The procedure assumes that the finite element model, loads, and boundary conditions have already been generated, and that the nodal displacements, reaction forces, element stresses, and buckling loads and mode shapes need to be calculated. The applied loads may be due to a combination of specified forces and displacements, and one constraint (i.e., boundary condition) set is permitted per procedure call. A linear elastic stress analysis is performed first using procedure L_STATIC (see Section 3.5) to calculate the prebuckling stress state (i.e., prestress state). After the linear static solution, a linear stability analysis is performed.

\subsection*{3.4.2 THEORY}

Linear elastic stability analyses may be formulated using the concept of adjacent equilibrium. Membrane forces in beams, plates, and shells result in an equilibrium configuration in which the deformation pattern is tangent to the midsurface of the structure. However, another equilibrium configuration involving out-of-plane deflections and rotations may be adjacent to this membrane state. Buckling occurs when this membrane strain energy is converted to bending strain energy. The linear elastic stability analysis is an eigenvalue problem to calculate the critical load for the bifurcation in the solution (e.g., change from a membrane state to a bending state). This eigenvalue problem can be written as
\[
\begin{equation*}
\mathbf{K} \phi_{i}+\lambda_{i} \mathbf{K}_{g}(\sigma) \phi_{i}=0 \quad i=1,2, \ldots \tag{3.4-1}
\end{equation*}
\]
where
\[
\begin{aligned}
\mathbf{K} & =\text { assembled linear elastic stiffness matrix } \\
\mathbf{K}_{g}(\boldsymbol{\sigma}) & =\text { assembled geometric stiffness matrix } \\
\phi_{i} & =i \text {-th eigenvector or modeshape } \\
\lambda_{i} & =i \text {-th eigenvalue or buckling load factor }
\end{aligned}
\]

The matrix denoted by \(\mathbf{K}_{g}\) has been called the initial stress stiffness matrix, the differential stiffness matrix, the geometric stiffness matrix, and the stability coefficient matrix (e.g., see ref 3.4-1). It is independent of the elastic properties of the structure and dependent on the geometry, displacement field, and state of stress. Herein the matrix \(\mathbf{K}_{\boldsymbol{g}}\) will be referred to as the geometric stiffness matrix.

A general formulation for the geometric stiffness matrix is presented in reference 3.4-1. Strains can be written as
\[
\begin{equation*}
\boldsymbol{\epsilon}=\epsilon_{\mathbf{L}}+\epsilon_{\mathbf{N L}} \tag{3.4-2}
\end{equation*}
\]
where \(\epsilon_{L}\) contains the linear strain-displacement terms and \(\epsilon_{N L}\) contains the higher-order or nonlinear strain-displacement terms. For a given stress state \(\sigma_{0}\), elastic strain energy is stored and can be expressed as
\[
\begin{equation*}
U=U_{L}+U_{N L} \tag{3.4-3}
\end{equation*}
\]
where
\[
\begin{align*}
U & =\frac{1}{2} \int_{V} \epsilon^{T} \sigma_{0} d V  \tag{3.4-4a}\\
U_{L} & =\frac{1}{2} \int_{V} \epsilon_{\mathbf{L}}^{T} \sigma_{0} d V  \tag{3.4-4b}\\
U_{N L} & =\frac{1}{2} \int_{V} \epsilon_{\mathbf{N L}}^{T} \sigma_{0} d V \tag{3.4-4c}
\end{align*}
\]

The geometric stiffness matrix is derived from the strain energy produced by stresses acting through displacements associated with the nonlinear strain-displacement relations. These relations couple the membrane and bending effects. Typically the strain-displacements relations are written using index notation as
\[
\begin{equation*}
\epsilon_{i j}=\frac{1}{2}\left[\partial_{i} u_{j}+\partial_{j} u_{i}+\partial_{i} u_{k} \partial_{j} u_{k}\right] \tag{3.4-5}
\end{equation*}
\]
where \(u_{i}=(u, v, w)\) for \(i=1,2,3\), respectively, \(\partial_{i}\) denotes differentiation with respect to \(i\) th coordinate direction and summation over repeated indices is implied. Let \(\mathbf{d}\) denote the nodal degrees of freedom, then
\[
\begin{equation*}
\boldsymbol{\delta}=\mathbf{G d} \tag{3.4-6}
\end{equation*}
\]
where
\[
\delta=\left\{\partial_{x} u, \partial_{y} u, \partial_{z} u, \partial_{x} v, \partial_{y} v, \partial_{z} v, \partial_{x} w, \partial_{y} w, \partial_{z} w\right\}
\]

The coefficients of \(\mathbf{G}\) are obtained by differentiating the element shape functions. Finally the matrix \(\mathbf{Q}\) is defined as
\[
\mathbf{Q}=\left[\begin{array}{ccccccccc}
\partial_{x} u & 0 & 0 & \partial_{x} v & 0 & 0 & \partial_{x} w & 0 & 0  \tag{3.4-7}\\
0 & \partial_{y} u & 0 & 0 & \partial_{y} v & 0 & 0 & \partial_{y} w & 0 \\
0 & 0 & \partial_{z} u & 0 & 0 & \partial_{z} v & 0 & 0 & \partial_{z} w \\
\partial_{y} u & \partial_{x} u & 0 & \partial_{y} v & \partial_{x} v & 0 & \partial_{y} w & \partial_{x} w & 0 \\
0 & \partial_{z} u & \partial_{y} u & 0 & \partial_{z} v & \partial_{y} v & 0 & \partial_{z} w & \partial_{y} w \\
\partial_{z} u & 0 & \partial_{x} u & \partial_{z} v & 0 & \partial_{x} v & \partial_{z} w & 0 & \partial_{x} w
\end{array}\right]
\]

With these definitions the nonlinear strains given by equation (3.4-2) can be written as
\[
\begin{equation*}
\boldsymbol{\epsilon}_{\mathbf{N L}}=\frac{1}{2} \mathbf{Q} \mathbf{G d} \tag{3.4-8}
\end{equation*}
\]

The vector of initial stresses is
\[
\sigma_{0}=\left\{\begin{array}{lllll}
\sigma_{x 0} & \sigma_{y 0} & \sigma_{z 0} & \tau_{x y 0} & \tau_{y z 0}  \tag{3.4-9}\\
\tau_{x z 0}
\end{array}\right\}
\]

Substituting equations (3.4-6) through (3.4-9) into equation (3.4-4c) gives
\[
\begin{equation*}
U_{N L}=\frac{1}{2} \mathbf{d}^{T}\left(\int_{V} \mathbf{G}^{T} \mathbf{Q}^{T} \sigma_{0} d V\right) \tag{3.4-10}
\end{equation*}
\]

However, the term \(Q^{\boldsymbol{T}} \sigma_{0}\) can be written as
\[
\mathbf{Q}^{T} \sigma_{0}=\left[\begin{array}{lll}
\mathbf{s} & 0 & 0  \tag{3.4-11}\\
0 & \mathbf{s} & 0 \\
0 & 0 & \mathbf{s}
\end{array}\right] \boldsymbol{\delta}=\overline{\mathbf{S}}\left(\sigma_{0}\right) \boldsymbol{\delta}
\]
where
\[
\mathbf{s}=\left[\begin{array}{ccc}
\sigma_{x 0} & \tau_{x y 0} & \tau_{x z 0}  \tag{3.4-12}\\
\tau_{x y 0} & \sigma_{y 0} & \tau_{y z 0} \\
\tau_{x z 0} & \tau_{y z 0} & \sigma_{z 0}
\end{array}\right]
\]

With these expressions, a general form of the geometric stiffness matrix can be written as
\[
\begin{equation*}
\mathbf{K}_{g}(\sigma)=\int_{V} \mathbf{G}^{T} \overline{\mathbf{S}}\left(\sigma_{0}\right) \mathbf{G} d V \tag{3.4-13}
\end{equation*}
\]
which is symmetric and explicitly dependent on the stress state.
The stress state used to form the geometric stiffness matrix may be obtained in two ways. The first way is first to perform a linear static stress analysis for the given load set and constraint set. This way is used in procedure L_STABIL_2. The second way is to specify, in advance, the values of the stress components given in equation (3.4-11) (i.e., specify the prestress state). This way is used in procedure L_STABIL_1.

\subsection*{3.4.3 ALGORITHM}

The algorithm used to solve equation (3.4-1) depends on the value of the global macrosymbol eigensolver_name. Processor EIG2 is used if eigensolver_name is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.4-2. Processor LAN is used if eigensolver_name is defined to be LaN. Processor LANZ is used if eigensolver_name is defined to be LaNZ. These processors are based on the Lanczos algorithm as described in references 3.4-2 to 3.4-4.

\subsection*{3.4.4 PROCEDURE USAGE}

Procedure L_STABIL_2 may be invoked by the *call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call L_STABIL_2 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L_STABIL_2; note that those arguments without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline BCON_SET & 1 & Constraint set for buckling analysis \\
\hline CONS_SET & 1 & Constaint set number for prestress analysis \\
\hline DIRECTION & 0 & Direction for element stress output \\
\hline ERROR_TOL & . 0001 & Convergence criterion for eigenvalues \\
\hline FUNCTION & ALL & Select function to be performed by procedure \\
\hline INIT_VECTOR & 0 & Number of initial vectors used to span the subspace \\
\hline ISEQ & 0 & Resequencing method to be used \\
\hline RNAME & K & First word of the name of the dataset containing the assembled stiffness matrix \\
\hline LDI & 1 & Logical device index \\
\hline LOAD_SET & 1 & Load set number \\
\hline LOCATION & CENTROIDS & Location of the evaluation points for element stresses \\
\hline MAX_ITERS & 20 & Maximum number of iterations allowed \\
\hline H.MODES & 1 & Number of eigenvalues to converge \\
\hline nVAL_METH & 3 & Method to be used for global smoothing \\
\hline PRINT & <false> & Flag to print displacement solution, internal forces, element stresses, and eigenvectors \\
\hline REACTION & <false> & Flag to compute internal forces or reactions \\
\hline RENOMBER & <true> & Flag to resequence node numbers for equation solver \\
\hline RHS & APPL. FORC & First two words of the dataset name for the right-hand side system vector \\
\hline SHIFT & 0.0 & Eigenvalue shift \\
\hline SMOOTH & <false> & Flag to compute smoothed global stresses \\
\hline SOLN & STAT.DISP & First two words of the dataset name for the displacement solution \\
\hline STRESS & <false> & Flag to compute element stresses (resultants) \\
\hline
\end{tabular}

Tables 3.4-1, 3.4-2, and 3.4-3 list the datasets used or created by procedure L_STABIL_2, the procedures invoked by procedure L_STABIL_2, and the processors invoked by procedure L_STABIL_2, respectively.
\begin{tabular}{|c|c|c|c|}
\hline Dataset & Description & Input & Output \\
\hline AMAP..ic2.isize & Factorization map for INV & & \(\checkmark\) \\
\hline APPL.FORC. i. \({ }^{\dagger}\) & Applied force vector & \(\checkmark\) & \\
\hline APPPL.MOTI. \({ }^{\text {a }}\). \({ }^{\dagger}\) & Specified displacement vector & \(\checkmark\) & \\
\hline BUCK.EVAL. \(\mathrm{i} . \mathrm{j} \dagger\) & Buckling eigenvalues & & \(\checkmark\) \\
\hline BUCK.MODE.i.j \(\dagger\) & Buckling eigenvalues & & \(\sqrt{ }\) \\
\hline <ES_NAME>.EFIL.0.nnod & Element Computational Data & \(\checkmark\) & \(\checkmark\) \\
\hline ES.SUMMARY & ES Processor Status & \(\checkmark\) & \(\checkmark\) \\
\hline DEF.<ES_NAME \(>\).0.nnod & Element Defn. (Connectivity) & \(\checkmark\) & \\
\hline DIR.<ES_NAME>.0.nnod & Element EFIL Directory & \(\checkmark\) & \\
\hline INT.FORC.i.j \({ }^{\dagger}\) & System Internal Force Vector & & \(\checkmark\) \\
\hline INV.KSHF. \({ }^{\dagger}\) & Factored Shifted System Matrix & & \(\checkmark\) \\
\hline INV. \(<\) KNAME \(>.{ }^{\dagger} \dagger\) & Factored System Matrix & & \(\checkmark\) \\
\hline JDF1.BTAB.1.8 & Model Summary & \(\checkmark\) & \\
\hline KG.SPAR.jdf2 & Assembled geometric stiffness matrix & & \(\checkmark\) \\
\hline KMAP..ic2.isize & Model connectivity map & & \(\checkmark\) \\
\hline <KNAME>.SPAR.jdf2 & Assembled system matrix & & \(\checkmark\) \\
\hline STAT.DISP.i.j \(\dagger\) & System Displacement Vector & & \(\checkmark\) \\
\hline STAT.REAC.i.j \({ }^{\dagger}\) & System Reaction Force Vector & & \(\checkmark\) \\
\hline STRS. \(<\) ES_NAME \(>\). i. \({ }^{\dagger}{ }^{\dagger}\) & Element Stresses & & \(\checkmark\) \\
\hline
\end{tabular}

Table 3.4-2 Sub-Procedures Invoked by procedure L_STABIL_2
\begin{tabular}{|l|l|l|}
\hline Procedure & Type & Function \\
\hline ES & External & Element utility procedure \\
\hline FACTOR & External & Factors assembled stiffness matrix \\
\hline L_STABIL_2 & Internal & Main procedure \\
\hline L_STATIC & Internal & Linear static analysis \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \multicolumn{2}{|c|}{ Table 3.4-3 Processors Invoked by procedure L_STABIL_2 } \\
\hline Procedure & Type & Function \\
\hline AUS & Internal & Arithmetic Utilities \\
\hline E & Internal & Initializes EFIL datasets \\
\hline EIG2 & Internal & Solve eigenvalue problem using subspace iteration \\
\hline ES \(i\) & External & Element processors based on GEP \\
\hline K & Internal & Assemble system matrix \\
\hline LAN & External & Solve eigenvalue problem using Lanczos method \\
\hline LANZ & External & Solve eigenvalue problem using Lanczos method \\
\hline RSEQ & Internal & Resequences nodes for equation solving \\
\hline TOPO & Internal & Generates nodal topology maps \\
\hline VPRT & Internal & Print system vectors \\
\hline
\end{tabular}

\subsection*{3.4.5 ARGUMENT DESCRIPTION}

\subsection*{3.4.5.1 BCON_SET}

Constraint set number for buckling analysis (default: 1). This argument selects which constraint set to use in solving the linear stability problem.

\subsection*{3.4.5.2 CONS_SET}

Constraint set number for prestress solution (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

\subsection*{3.4.5.3 DIRECTIOH}

Direction for the element stress (stress resultant) output (default: 0). The element stress coordinate system will be used if direction=0. The material axes ( \(x_{m}, y_{m}, z_{m}\) ) will be used if direction=1; the material axes ( \(y_{m}, z_{m}, x_{m}\) ) will be used for direction= \(\overline{2}\); and the material axes ( \(z_{m}, x_{m}, y_{m}\) ) will be used for direction=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 3.4-2).

\subsection*{3.4.5.4 ERROR.TOL}

Convergence criterion for eigenvalues (default: 0.0001 ). For the \(k\)-th iteration, the error measure for the \(k\)-th eigenvalue is
\[
\epsilon_{i}^{k}=\frac{\left\|\left(\lambda_{i}^{k}-\lambda_{i}^{k-1}\right)\right\|}{\left\|\lambda_{i}^{k}\right\|}
\]

The \(i\)-th eigenvalue is converged if \(\epsilon_{i}^{k}\) is smaller than ERROR_TOL.

\subsection*{3.4.5.5 FUNCTION}

Select function to be performed by procedure L_STABIL_2 (default: ALL). This procedure may be used to perform four functions. For \(\operatorname{FONCTION=ALL,~the~element~data~are~initialized~}\) and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, the displacement solution is obtained, optionally element stresses (stress resultants) and internal nodal forces (reactions) computed and the eigenproblem is solved. For FUNCTION=FACT_SOLV, procedure L_STABIL_2 assumes that the system stiffness matrix has previously been assembled and that nodal resequencing has been performed. The procedure then proceeds to factor the system stiffness matrix, solves for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For \(\operatorname{FONCTION}=\) SOLV, procedure L_STABIL_2 assumes that the system stiffness has previously been formed and factored. The procedure then proceeds to solve for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FONCTION=EIGEN, procedure L_STABIL_2 uses a previously computed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

\subsection*{3.4.5.6 INIT.VECTOR}

Number of initial vectors used to span the subspace (default: 0 ). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT_VECTOR \(=0\), the number of initial vectors will be calculated by the procedure as
\[
\text { INIT_VECTOR=MINIMUM ( } 2 * \text { N_MODES, N_MODES }+8 \text { ) }
\]

\subsection*{3.4.5.7 ISEQ}

Resequencing method to be used (default: 0). If the argument RENOMBER is <true>, then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (i.e., method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.4-2).

\subsection*{3.4.5.8 KNAME}

First word of the dataset name containing the assembled stiffness matrix (default: \(\mathbb{K}\) ).

\subsection*{3.4.5.9 LDI}

Logical device index (default: 1).

\subsection*{3.4.5.10 LOAD_SET}

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

\subsection*{3.4.5.11 LOCATION}

Location of the evaluation points for the element stresses or stress resultants (default: CENTROIDS). The element stresses or stress resultants are optionally computed by calling procedure STRESS (see Section 6.4). This argument may have four values. For LOCATION=IMTEG_PTS, the element stresses are computed at the element integration points. For LOCATIOH=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries. For LOCATION=ALL, the element stresses are computed at the element integration points, element centroid, and element nodes.

\subsection*{3.4.5.12 MAX_ITERS}

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

\subsection*{3.4.5.13 NMODES}

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR_TOL.

\subsection*{3.4.5.14 HVAL_NETH}

Select method to be used for computing the smoothed global stresses (default: 3). Processor NVAL is used to compute the smoothed global stresses using the method defined by the argument wVAL_METH (see Section 12.5 of reference 3.4-2). If YYAL_METH=1, a topological interpolation of the element centroidal stresses is performed, and the element stresses must have been computed using LOCATION=CENTROIDS. If NVAL_METH=2, a projected least-squares interpolation of the element centroidal stresses is performed, and the stresses must have been computed using LOCATION=CENTROIDS. If NVAL_METH=3, the element nodal stresses (discontinuous across interelement boundaries) are averaged, and the element stresses must have been computed using LOCATION=NODES. Using LOCATION=ALL will generate element stresses at the element centroids, element nodes, and element gauss points. Acceptable values of LOCATION for specific values of NVAL_METH are as follows:
\begin{tabular}{|c|c|}
\hline NVAL_METH & LOCATION \\
\hline 1 & CENTROIDS, ALL \\
2 & CENTROIDS, ALL \\
3 & NODES, ALL \\
\hline
\end{tabular}

\subsection*{3.4.5.15 PRINT}

Flag to print displacement solution, internal forces and element stresses (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the displacement solution and internal forces and processor PESR will be used to print the element stresses.

\subsection*{3.4.5.16 REACTION}

Flag to compute the internal nodal forces (default: <true>) If the argument reacTION=〈true〉, then the internal forces will be computed by calling procedure INT_FORC (see Section 6.2).

\subsection*{3.4.5.17 RENOMBER}

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENOMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

\subsection*{3.4.5.18 RHS}

First two words of the dataset name for the right-hand side system vector (default: APPL. FORC).

\subsection*{3.4.5.19 SHIFT}

Eigenvalue shift (default: 0.0 ). Converged eigenvalues will only be obtained for values greater than SHIFT. The shift parameter refers to the shift in the buckling load factor.

\subsection*{3.4.5.20 SMOOTH}

Flag to compute smoothed global stresses (default: <false>). If the argument SMOOTH=<true>, then smoothed global stresses will be computed by processor NVAL using the method defined by the argument NVAL_METH.

\subsection*{3.4.5.21 SOLN}

First two words of the dataset name for the displacement solution (default: STAT.DISP).

\subsection*{3.4.5.22 STRESS}

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION, respectively, by calling procedure STRESS (see Section 6.4).

\subsection*{3.4.6 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
L_STABIL_2 & (main procedure) \\
L_STATIC & (linear static analysis procedure) \\
ES & (initialize, form K) \\
FACTOR & (factor assembled stiffness matrix) \\
SOLVE & (solve linear system of equations) \\
STRESS & (stress/strain recovery procedure) \\
ES & (calculate element and nodal stress/strain) \\
INT_FORCE & (internal force procedure) \\
\multicolumn{1}{c}{ ES } & (internal force calculation) \\
& (form \(\mathbf{K}_{g}\) ) \\
ES & (factor using buckling boundary conditions)
\end{tabular}

\subsection*{3.4.7 LIMITATIONS}

None.

\subsection*{3.4.8 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{3.4.8 USAGE GUIDELINES AND EXAMPLES}

Procedure L_STABIL_2 may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_STABIL_2 ( FUNCTION = ALL ; -- . Select function
CONS_SET = 1 ; -- . Select constraint set
BCON_SET = 1 ; -- . Select buckling constraint set
DIRECTION = 0 ; -- . Select direction for element stresses
ERROR_TOL = .0001 ; --
INIT_VECTOR = 0 ; --
ISEQ = 0 ; -- . Select resequencing method
KNAME = K ; -- . First word of stiffness matrix
9 -- . dataset name
LOAD_SET = 1 ; -- . Select load set
LOCATION = CENTROIDS ; -- Select location of element
-- . stress evaluation points
MAX_ITERS = 20; -- Maximum number of iterations
N_MODES = 1 ; -- Number of eigenvalues
NVAL_METH = 3 ; --
PRINT = <false> ; -- . PRINT flag
REACTION = <false\rangle; -- . REACTIONS flag
RENUMBER = <true> ; -- . RESEQUENCING flag
RHS = APPL. FORC ; -- . First tro words of RHS
-- . vector dataset
SHIFT = 0.0 ; Eigenvalue shift
SMOOTH = <false> ; -- compute smoothed global stresses?
SOLN = STAT. DISP ; -- . First two words of SOLN
STRESS = <false> -- . STRESS flag

```

Before procedure L_STABIL_2 is called, the global macrosymbol eigensolver_name should be defined as described in Section 3.4.3; otherwise, the default value of EIG2 will be used.

\subsection*{3.4.10 PROCEDURE LISTING}

\subsection*{3.4.11 REFERENCES}
3.4-1 Cook, Robert D.: Concepts and Applications of Finite Element Analysis. (Second Edition). John Wiley and Sons, Inc., New York 1981.
3.4-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.4-3 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
3.4-4 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

\subsection*{3.5 Procedure L_STATIC}

\subsection*{3.5.1 GENERAL DESCRIPTION}

Procedure L_STATIC performs linear static analysis, using an equation solver selected by defining the global macrosymbol solver_name (e.g., INV, BAND, ITER, SPK) and user specified structural element ( \(\mathrm{ES} i\) ) processors based on the generic element processor template. The procedure assumes that the finite element model, loads, and boundary conditions, have already been generated, and that the nodal displacements, reaction forces, and element stresses need to be calculated. The applied loads may be due to a combination of specified forces and displacements, and one constraint (i.e., boundary condition) set is permitted per procedure call.

\subsection*{3.5.2 THEORY}

Mathematically, procedure L_STATIC solves the linear static problem:
\[
\begin{equation*}
\mathbf{K} \mathbf{d}=\mathbf{f} \tag{3.5-1}
\end{equation*}
\]
where
\[
\begin{aligned}
\mathbf{K} & =\text { assembled linear stiffness matrix } \\
\mathbf{d} & =\text { generalized displacement vector } \\
\mathbf{f} & =\text { external force vector }
\end{aligned}
\]

Note that both the translational and rotational displacements in d are assumed to be infinitesimally small (linear strain-displacement relations are employed), and that the material (stress-strain relation) is assumed to be both linear and elastic. Once the displacement vector, \(d\), is computed by solution of equation (3.5-1), the reaction forces are computed by multiplying those rows of the stiffness matrix \(K\) at which the displacements are prescribed (zero or non-zero) by the generalized displacement vector d. Finally, element stresses may be optionally computed.

\subsection*{3.5.3 ALGORITHM}

The algorithm used to solve equation 3.5-1 depends on the value of the global macrosymbol solver_name. Processors INV and SSOL are used if solver_name is defined to be INV. These processors use nodal-block sparse matrix approach as described in references 3.5-1, 3.5-2 and 3.5-3. Processor BAND (meth=28) is used if solver_name is defined to be BAND. This algorithm is a LDL \({ }^{T}\) direct method based on an Choleski variable bandwidth method with loop unrolling as described in references 3.5-1 and 3.5-4. Processor ITER (meth=0) is used if solver_name is defined to be ITER. This algorithm is an iterative method based on a conjugate gradient method with diagonal scaling and sparse storage of the system matrix as described in references \(3.5-1\) and 3.5-4. Processor SPK is used if solver_name is defined to be SPK. This algorithm uses the vector-sum column Cholesky algorithms to
factor a general sparse matrix as described in references 3.5-1 and 3.5-5. Processor SPK contains a subset of the SPARSPAK-A package of FORTRAN programs designed to solve effectively large sparse systems of linear equations by direct methods (see reference 3.5-6).

\subsection*{3.5.4 PROCEDURE USAGE}

Procedure L_STATIC may be invoked by the *call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call L_STATIC ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L_STATIC; note that those arguments without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline CONS_SET & 1 & Constraint set number \\
\hline DIRECTION & 1 & Direction for element stress output \\
\hline FUNCTION & ALL & Select function to be performed by procedure \\
\hline ISEQ & -1 & Resequencing method to be used \\
\hline KNAME & K & First word of the name of the dataset containing the assembled stiffness matrix \\
\hline LDI & 1 & Logical device index \\
\hline LOAD_SET & 1 & Load set number \\
\hline LOCATION & NODES & Location of the evaluation points for element stresses \\
\hline NVAL_METH & 3 & Method to be used for global smoothing \\
\hline PRINT & <false> & Flag to print computed results \\
\hline REACTION & <false> & Flag to compute internal forces or reactions \\
\hline RENUMBER & <true> & Flag to resequence node numbers for equation solver \\
\hline RHS & APPL. FORC & First two words of the dataset name for the right-hand side system vector \\
\hline SMOOTH & <false> & Flag to compute smoothed global stresses \\
\hline SOLN & STAT.DISP & First two words of the dataset name for the displacement solution \\
\hline STRESS & <false> & Flag to compute element stresses (resultants) \\
\hline
\end{tabular}

Tables 3.5-1, 3.5-2, and 3.5-3 list the datasets used or created by procedure L_STATIC, the procedures invoked by procedure L_STATIC, and the processors invoked by procedure L_STATIC, respectively.
\begin{tabular}{|c|c|c|c|}
\hline Dataset & Description & Input & Output \\
\hline AMAP..ic2.isize & Factorization Map for INV & & \(\checkmark\) \\
\hline APPL.FORC. i. \({ }^{\dagger}\) & Applied force vector & \(\checkmark\) & \\
\hline APPL.MOTI. \(\mathbf{i s}^{1}{ }^{\dagger}\) & Specified displacement vector & \(\checkmark\) & \\
\hline <ES_NAME>.EFIL.0.nnod & Element Computational Data & \(\checkmark\) & \(\checkmark\) \\
\hline ES.SUMMARY & ES Processor Status & \(\checkmark\) & \(\checkmark\) \\
\hline DEF.<ES_NAME \(>\). \(0 . n \mathrm{nod}\) & Element Defn. (Connectivity) & \(\checkmark\) & \\
\hline DIR.<ES_NAME \(>\). \(0 . n\) nod & Element EFIL Directory & \(\checkmark\) & \\
\hline INT.FORC.i.j \({ }^{\dagger}\) & System Internal Force Vector & & \(\checkmark\) \\
\hline INV.<KNAME>.i.j \(\dagger\) & Factored System Matrix & & \(\checkmark\) \\
\hline JDF1.BTAB.1.8 & Model Summary & \(\checkmark\) & \\
\hline JLOC.BTAB.2.5 & Nodal Coordinates & \(\checkmark\) & \\
\hline KMAP..ic2.isize & Model Connectivity Map & & \(\checkmark\) \\
\hline <KNAME>.SPAR.jdf2 & Assembled System Matrix & & \(\checkmark\) \\
\hline PROP.BTAB.* & Material/Section Properties & \(\checkmark\) & \\
\hline QJJT.BTAB.2.9 & Nodal Transformations & \(\checkmark\) & \\
\hline STAT.DISP.i.j \(\dagger\) & System Displacement Vector & & \(\checkmark\) \\
\hline STAT.REAC.i. \(\dagger\) ¢ & System Reaction Force Vector & & \(\checkmark\) \\
\hline STRS.<ES_NAME \(>\).i.j \(\dagger\) & Element Stresses & & \(\checkmark\) \\
\hline \multicolumn{4}{|l|}{\(\dagger i=<\) load_set> and \(\boldsymbol{j}=\) <cons_set>} \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Table 3.5-2 & Sub-Procedures Invoked by procedure L_STATIC \\
\hline Procedure & Type & Function \\
\hline ES & External & Element utility procedure \\
\hline FACTOR & External & Factors assembled stiffness matrix \\
\hline INT_FORCE & External & Computes internal forces \\
\hline L_STATIC & Internal & Main procedure \\
\hline SOLVE & External & Solves for the displacement solution \\
\hline STRESS & External & Computes element stresses \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \multicolumn{2}{|l|}{ Table 3.5-3 Processors Invoked by procedure L_STATIC } \\
\hline Procedure & Type & Function \\
\hline E & Internal & Initializes EFIL datasets \\
\hline ESi & External & Element processors based on GEP \\
\hline K & Internal & Assemble material stiffness matrix \\
\hline RSEQ & Internal & Resequences nodes for equation solving \\
\hline TOPO & Internal & Generates nodal topology maps \\
\hline VPRT & Internal & Print SYSVEC-format vectors \\
\hline
\end{tabular}

\subsection*{3.5.5 ARGUMENT DESCRIPTION}

\subsection*{3.5.5.1 CONS_SET}

Constraint set number (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

\subsection*{3.5.5.2 DIRECTION}

Direction for the element stress (stress resultant) output (default: 1). The element stress coordinate system will be used if DIRECTION \(=0\). The material axes ( \(x_{m}, y_{m}, z_{m}\) ) will be used if DIRECTION \(=1\); the material axes \(\left(y_{m}, z_{m}, x_{m}\right)\) will be used for DIRECTION=2; and the material axes \(\left(z_{m}, x_{m}, y_{m}\right)\) will be used for DIRECTION \(=3\). For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 3.5-1).

\subsection*{3.5.5.3 FUNCTION}

Select function to be performed by procedure L_STATIC (default: ALL). This procedure may be used to perform three functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices fömed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, the displacement solution is obtained and optionally element stresses (stress resultants) and internal nodal forces (reactions) computed. For FUNCTION=FACT_SOLV, procedure L_STATIC assumes that the system stiffness matrix has previously been assembled and that nodal resequencing has been performed. The procedure then proceeds to factor the system stiffness matrix, solves for the displacement solution, and optionally computes the element stresses (stress resultants) and internal nodal forces (reactions). For FUNCTION=SOLV, procedure L_STATIC assumes that the system stiffness has previously been formed and factored. The procedure then proceeds to solve for the displacement solution and optionally computes the element stresses (stress resultants) and internal nodal forces (reactions). Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

\subsection*{3.5.5.4 ISEQ}

Resequencing method to be used (default: -1). If the argument RENUMBER is <true>, then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (i.e., method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.5-1). If the argument ISEQ has a value of -1 , then a default method will be used depending on the value of the global macrosymbol <solver_name>.

These default value are as follows:
\begin{tabular}{|c|c|}
\hline <solver_name> & ISEQ \\
\hline INV & 0 \\
BAND & 2 \\
ITER & 1 \\
SPK & 1 \\
\hline
\end{tabular}

\subsection*{3.5.5.5 KNAME}

First word of the dataset name containing the assembled stiffness matrix (default: \(\mathbb{K}\) ).

\subsection*{3.5.5.6 LDI}

Logical device index (default: 1).

\subsection*{3.5.5.7 LOAD_SET}

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

\subsection*{3.5.5.8 LOCATION}

Location of the evaluation points for the element stresses or stress resultants (default: NODES). The element stresses or stress resultants are optionally computed by calling procedure STRESS (see Section 6.4). This argument may have four values. For LOCATION=INTEG_PTS, the element stresses are computed at the element integration points. For LOCATION=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries. For LOCATION=ALL, the element stresses are computed at the element integration points, element centroid, and element nodes.

\subsection*{3.5.5.9 NVAL_METH}

Select method to be used for computing the smoothed global stresses (default: 3). Processor NVAL is used to compute the smoothed global stresses using the method defined by the argument NVAL_METH (see Section 12.5 of reference 6.4-1). If NVAL_METH=1, a topological interpolation of the element centroidal stresses is performed, and the element stresses must have been computed using LOCATION=CENTROIDS. If NVAL_METH=2, a projected least-squares interpolation of the element centroidal stresses is performed, and the stresses must have been computed using LOCATION=CENTROIDS. If NVAL METH=3, the element nodal stresses (discontinuous across interelement boundaries) are averaged, and the element stresses must have been computed using LOCATION=NODES. Using LOCATION=ALL will generate element stresses at the element centroids, element nodes, and element gauss points. Acceptable values of LOCATION for specific values of NVAL_METH are as follows:
\begin{tabular}{|c|c|}
\hline NVAL_METH & LOCATION \\
\hline 1 & CENTROIDS, ALL \\
2 & CENTROIDS, ALL \\
3 & NODES, ALL \\
\hline
\end{tabular}

\subsection*{3.5.5.10 PRINT}

Flag to print computed results such as the displacement solution, internal forces, and element and nodal stresses (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the displacement solution and internal forces, processor PESR will be used to print the element stresses and processor PNSR will be used to print nodal stresses.

\subsection*{3.5.5.11 REACTION}

Flag to compute the internal nodal forces (default: <true>) If the argument REACTION=<true>, then the internal forces will be computed by calling procedure INT_FORCE (see Section 6.2).

\subsection*{3.5.5.12 RENUMBER}

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations given by equation 3.5-1.

\subsection*{3.5.5.13 RHS}

First two words of the dataset name for the right-hand side system vector (default: APPL.FORC).

\subsection*{3.5.5.14 SMOOTH}

Flag to compute smoothed global stresses (default: 〈false〉). If the argument SMOOTH=<true>, then smoothed global stresses will be computed by processor NVAL using the method defined by the argument NVAL METH.

\subsection*{3.5.5.15 SOLN}

First two words of the dataset name for the displacement solution (default: STAT.DISP).

\subsection*{3.5.5.16 STRESS}

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS is defined to be <true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION, respectively, by calling procedure STRESS (see Section 6.4).

\subsection*{3.5.6 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
L_STATIC & (main procedure) \\
ES & (initialize, form K) \\
FACTOR & (factor assembled stiffness matrix) \\
SOLVE & (solve linear system of equations) \\
STRESS & (stress/strain recovery procedure) \\
ES & (calculate element stresses and/or strains) \\
INT_FORCE & (internal force procedure) \\
ES & (internal force calculation)
\end{tabular}

\subsection*{3.5.7 LIMITATIONS}

Procedure L_STATIC assumes that all datasets either required or generated reside on library one ( \(\mathrm{LDI}=1\) ).

\subsection*{3.5.8 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{3.5.9 USAGE GUIDELINES AND EXAMPLES}

Procedure L_STATIC may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_STATIC ( FUNCTION = ALL ; -- . Select function
CONS_SET = 1 ; -- . Select constraint set
DIRECTION = 0 ; -- . Select direction for element stresses
ISEQ = -1 ; -- . Select resequencing method
KMAME = K ; -- . First word of stiffness matrix
-- . dataset name
LOAD_SET = 1 ; -- . Select load set
LOCATION = CENTROIDS ; -- Select location of element
-- . stress evaluation points
PRINT = <true> ; -- . PRINT flag
REACTION = <false\rangle; -- . REACTIONS flag
RENUMBER = <true> ; -- . RESEQUENCING flag
RHS = APPL. FORC ; -- . First two words of RHS
-- . vector dataset
SOLN = STAT. DISP ; -- . First two words of SOLM
-- . dataset
STRESS = <false> -- . STRESS flag
)

```

Before procedure L_STATIC is called, the global macrosymbol solver_name should be defined as described in Section 3.5.3; otherwise, the default value of INV will be used.

\subsection*{3.5.10 PROCEDURE LISTING}

\subsection*{3.5.11 REFERENCES}
3.5-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.5-2 Whetstone, W. D.: "Computer Analysis of Large Linear Frames": Journal of the Structural Division, ASCE, Vol. 95, No. ST11, November 1969, pp. 2401-2417.
3.5-3 Regelbrugge, M. E. and Wright, M. A.: The Computational Structural Mechanics Testbed Matrix Processors Internal Logic and Dataflow Descriptions. NASA CR181742, March 1989.
3.5-4 Poole, Eugene L. and Overman, Andrea L.: The Solution of Linear Systems of Equations with a Structural Analysis Code of the NAS Cray-2. NASA CR-4159, September 1988.
3.5-5 Chu, Eleanor and George, J. Alan: Sparse Matrix Methods Research Using the CSM Testbed Software System. NASA CR-4219, March 1989.
3.5-6 Chu, E.C.H.; George, J. A.; Liu, W-H.; and Ng, E. G-Y.: User's Guide for SPARSPAK-A: Waterloo Sparse Linear Equations Package. Technical Report CS-84-36, University of Waterloo, Waterloo Ontario, Canada, 1984.
3.5-7 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

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\subsection*{3.6 Procedure L_VIBRAT_0}

\subsection*{3.6.1 GENERAL DESCRIPTION}

Procedure L_VIBRAT_O performs a linear vibration analysis about an unstressed state. The eigensolver is selected by defining the global macrosymbol eigensolver_name to be the name of the desired processor (e.g., EIG2, LAN, LANZ), and the structural element processors (ESi) form the elemental stiffness and mass matrices. The procedure assumes that the finite element model and boundary conditions have already been generated and that the vibration modeshapes and frequencies need to be calculated.

\subsection*{3.6.2 THEORY}

Linear vibration analyses are formulated using the equations of motion for an undamped structure. For the case of no external forces, the equations of motion are
\[
\begin{equation*}
\mathbf{M} \ddot{\mathbf{u}}+\mathbf{K} \mathbf{u}=\mathbf{0} \tag{3.6-1}
\end{equation*}
\]
where
\[
\begin{aligned}
& \mathbf{M}=\text { assembled mass matix (consistent or diagonal) } \\
& \mathbf{K}=\text { assembled linear stiffness matrix } \\
& \ddot{\mathbf{u}}=\text { acceleration vector } \\
& \mathbf{u}=\text { displacement vector }
\end{aligned}
\]

If harmonic motion is assumed, then
\[
\begin{equation*}
\mathbf{u}=\phi_{i} \sin \omega_{i} t \quad i=1,2, \ldots \tag{3.6-2}
\end{equation*}
\]
where
\[
\begin{aligned}
& \phi_{i}=i \text { th eigen modeshape } \\
& \omega_{i}=i \text { th circular frequency (radians per second) }
\end{aligned}
\]

The \(i\) th cyclic frequency \(f_{i}\) (in hertz) is
\[
f_{i}=\frac{\omega_{i}}{2 \pi}
\]
and the period \(T_{i}\) (in seconds) is
\[
T_{i}=\frac{1}{f_{i}}
\]

Substituting equation (3.6-2) in equation (3.6-1) gives
\[
\begin{equation*}
\left(\mathbf{K}-\lambda_{i} \mathbf{M}\right) \phi_{i}=0 \quad i=1,2, \ldots \tag{3.6-3}
\end{equation*}
\]
where
\[
\lambda_{i}=\omega_{i}^{2}
\]

If the user has specified the reset parameter GRAV in processor LAU to a value of unity then the matrix \(M\) has the meaning of a "weight" matrix instead of a "mass" matrix. This reset parameter is important for interpreting the eigenvalues calculated by the various eigensolvers.

\subsection*{3.6.3 ALGORITHM}

The algorithm used to solve equation (3.6-1) depends on the value of the global macrosymbol eigensolver_name. Processor EIG2 is used if eigensolver_name is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.6-2. Processor LAN is used if eigensolver_name is defined to be LAH. Processor LANZ is used if eigensolver_name is defined to be LaNZ. These processors are based on the Lanczos algorithm as described in references \(3.6-2\) and \(3.6-3\). If this global macrosymbol is not defined, procedure L_VIbRat_0 will set it to EIG2.

\subsection*{3.6.4 PROCEDURE USAGE}

Procedure L_VIBRAT_O may be invoked by the *call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call L_VIBRAT_0 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L_VIBRAT_0; note that those arguments without default values are mandatory, while the others are optional.
\begin{tabular}{lccl} 
Argument & Default Value & & Meaning \\
ERROR_TOL & .0001 & & Convergence criterion for eigenvalues \\
FUNCTION & aLL & & Select function to be performed by procedure \\
INIT_VECTORS & 0 & & Number of initial vectors used to span the subspace \\
ISEQ & 0 & & Resequencing method to be used \\
LDI & 1 & & Logical device index
\end{tabular}

Tables 3.0-1, 3.6-2, and 3.6-3 list the datasets used or created by procedure L_vibrat_0, the procedures invoked by procedure L_VIBRAT_0, and the processors invoked by procedure L_VIBRAT_0, respectively.
\begin{tabular}{|l|l|l|l|}
\hline \multicolumn{2}{|c|}{ Table 3.6-1 Datasets Input/Output by procedure L_VIBRAT_0 } \\
\hline Dataset & Description & Input & Output \\
\hline AMAP..ic2.isize & Factorization Map for INV & & \(\sqrt{ }\) \\
\hline CEM.SPAR & Consistent Mass Matrix & & \(\sqrt{ }\) \\
\hline <ES_NAME>.EFIL.0.nnod & Element Computational Data & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline ES.SUMMARY & ES Processor Status & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline DEF.<ES_NAME>.0.nnod & Element Defn. (Connectivity) & \(\sqrt{ }\) & \\
\hline DEM.DIAG & Diagonal (Lumped) Mass Matrix & & \(\sqrt{ }\) \\
\hline DIR.<ES_NAME>.0.nnod & Element EFIL Directory & \(\sqrt{ }\) & \\
\hline INV.KSHF.j \(\dagger\) & Factored Shifted System Matrix & & \(\sqrt{ }\) \\
\hline INV.<KNAME>.j \(\dagger\) & Factored System Matrix & & \(\sqrt{ }\) \\
\hline JDF1.BTAB.1.8 & Model Summary & \(\sqrt{ }\) & \\
\hline KG.SPAR.jdf2 & Assembled geometric stiffness matrix & & \(\sqrt{ }\) \\
\hline KMAP..ic2.isize & Model Connectivity Map & & \(\sqrt{ }\) \\
\hline <KNAME>.SPAR.jdf2 & Assembled system matrix & & \(\sqrt{ }\) \\
\hline VIBR.EVAL.1. \(\dagger\) & Vibration eigenvalues & & \(\sqrt{ }\) \\
\hline VIBR.MODE.1. \(\dagger\) & Vibration eigenvalues & & \(\sqrt{ }\) \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \multicolumn{2}{|c|}{ Table 3.6-3 Processors Invoked by Procedure L_VIBRAT_0 } \\
\hline Procedure & Type & Function \\
\hline AUS & Internal & Arithmetic utilities \\
\hline E & Internal & Initializes EFIL datasets \\
\hline EIG2 & Internal & Solve eigenvalue problem using subspace iteration \\
\hline ESi & External & Element processors based on GEP \\
\hline K & Internal & Assemble system matrix \\
\hline LAN & External & Solve eigenvalue problem using Lanczos method \\
\hline LANZ & External & Solve eigenvalue problem using Lanczos method \\
\hline RSEQ & Internal & Resequences nodes for equation solving \\
\hline TOPO & Internal & Generates nodal topology maps \\
\hline VPRT & Internal & Print SYSVEC system vectors \\
\hline
\end{tabular}

\subsection*{3.6.5 ARGUMENT DESCRIPTION}

\subsection*{3.6.5.1 ERROR_TOL}

Convergence criterion for eigenvalues (default: 0.0001). For the \(k\)-th iteration, the error measure for the \(i\)-th eigenvalue is
\[
\epsilon_{i}^{k}=\frac{\left\|\left(\lambda_{i}^{k}-\lambda_{i}^{k-1}\right)\right\|}{\left\|\lambda_{i}^{k}\right\|}
\]

The \(i\)-th eigenvalue is converged if \(\epsilon_{i}^{k}\) is smaller than ERROR_TOL.

\subsection*{3.6.5.2 FUNCTION}

Select function to be performed by procedure L_VIBRAT_0 (default: ALL). This procedure may be used to perform two functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, and the eigenproblem is solved. For FUNCTION=EIGEN, procedure L_VIBRAT_O uses a previously computed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model.

\subsection*{3.6.5.3 INIT_VEGTOR}

Number of initial vectors used to span the subspace (default: 0 ). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT_VECTOR=0, the number of initial vectors will be calculated by the procedure as
```

INIT_VECTOR=MINIMUM (2*N_MODES, N_modes + 8)

```

\subsection*{3.6.5.4 ISEQ}

Resequencing method to be used (default: 0). If the argument RENUMBER is <true>, then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (i.e., method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.6-1).

\subsection*{3.6.5.5 LDI}

Logical device index (default: 1).

\subsection*{3.6.5.6 KNAME}

First word of the dataset name containing the assembled stiffness matrix (default: \(\mathbb{K}\) ).

\subsection*{3.6.5.7 MASS_TYPE}

Type of mass matrix (default: CONSISTENT). If MASS_TYPE=CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor \(K\) to form the system mass matrix. If MASS_TYPE=DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

\subsection*{3.6.5.8 MAX_ITERS}

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

\subsection*{3.6.5.9 M_MODES}

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR_TOL.

\subsection*{3.6.5.10 PRINT}

Flag to print displacement solution, internal forces and element stresses (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the vibration modeshapes.

\subsection*{3.6.5.11 RENUMBER}

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENOMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

\subsection*{3.6.5.12 SHIFT}

Eigenvalue shift (default: 0.0 ). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared (i.e., \(\omega^{\mathbf{2}}\) ) for vibration problems.

\subsection*{3.6.5.13 VCON_SET}

Constraint set number for vibration analysis (default: 1). This argument selects which constraint set to use in solving the linear vibration problem.

\subsection*{3.6.6 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
L_VIBRAT_O & (main procedure) \\
ES & (initialize, form \(\mathbf{K}\) and \(\mathbf{M}\) ) \\
FACTOR & (factor using vibration boundary conditions)
\end{tabular}

\subsection*{3.6.7 LIMITATIONS}

None.

\subsection*{3.6.8 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{3.6.9 USAGE GUIDELINES AND EXAMPLES}

Procedure L_VIBRAT_0 may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_VIBRAT_O ( FUNCTIOY = ALL ; -- . Select function
BCON_SET = 1 ; -- . Select vibration constraint set
ERROR_TOL = . 0001 ; -- . Eigenvalue convergence criterion
INIT_VECTOR = 0 ; -- . Number of initial vectors
ISEQ = -1 ; -- . Sslect resequencing method
KNAME = K ; -- . First mord of stiffness matrix
MAX_ITERS = 20; -- Maximum number of iterations
N_MODES = 1 ; -- Number of eigenvalues
PRINT = <true> ; -- . PRINT flag
RENUMBER = <true> ; -- . RESEQUENCING flag
SHIFT =0.0 -- ; Eigenvalue shift

```

Before procedure L_vibrat_o is called, the global macrosymbol eigensolver_name should be defined as described in Section 3.6-3; otherwise, the default value of EIG2 will be used.

\subsection*{3.6.10 PROCEDURE LISTING}

\subsection*{3.6.11 REFERENCES}
3.6-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.6-2 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
3.6-3 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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\subsection*{3.7 Procedure L_VIBRAT_1}

\subsection*{3.7.1 GENERAL DESCRIPTION}

Procedure L_VIBRAT_1 performs a linear vibration analysis about a prescribed prestressec. state. The eigensolver is selected by defining the global macrosymbol eigensolver_name to be the name of the desired processor (e.g., EIG2, LAN), and the structural element processors ( ESi ) form the elemental stiffness and mass matrices. The procedure assumes that the finite element model and boundary conditions have already been generated, that the prestressed state has been prescribed, and that the vibration modeshapes and frequencies need to be calculated.

\subsection*{3.7.2 THEORY}

Linear vibration analyses are formulated using the equations of motion for an undamped structure. For the case of prestressed state, the equations of motion are
\[
\begin{equation*}
\mathbf{M} \ddot{\mathbf{u}}+\mathbf{K} \mathbf{u}+\mathbf{K}_{g}(\boldsymbol{\sigma}) \mathbf{u}=\mathbf{0} \tag{3.7-1}
\end{equation*}
\]
where
\[
\begin{aligned}
\mathbf{M} & =\text { assembled mass matix (consistent or diagonal) } \\
\mathbf{K} & =\text { assembled linear stiffness matrix } \\
\mathbf{K}_{\boldsymbol{g}}(\boldsymbol{\sigma}) & =\text { assembled geometric stiffness matrix for given stress state } \\
\ddot{\mathbf{u}} & =\text { acceleration vector } \\
\mathbf{u} & =\text { displacement vector } \\
\boldsymbol{\sigma} & =\text { prestress state }
\end{aligned}
\]

The prestressed state may be defined in several ways. Procedure L_VIBRaT_1 assumes that a membrane prestressed state ( \(N_{x}^{o}, N_{y}^{o}, N_{x y}^{o}\) ) is explicitly prescribed.
If harmonic motion is assumed, then
\[
\begin{equation*}
\mathbf{u}=\phi_{i} \sin \omega_{i} t \quad i=1,2, \ldots \tag{3.7-2}
\end{equation*}
\]
where
\[
\begin{aligned}
& \phi_{i}=i \text { th eigen modeshape } \\
& \omega_{i}=i \text { th circular frequency (radians per second) }
\end{aligned}
\]

The \(i\) th cyclic frequency \(f_{i}\) (in hertz) is
\[
f_{i}=\frac{\omega_{i}}{2 \pi}
\]
and the period \(T_{i}\) (in seconds) is
\[
T_{i}=\frac{1}{f_{i}}
\]

Substituting equation (3.7-2) in equation (3.7-1) gives
\[
\begin{equation*}
\left(\mathbf{K}+\mathbf{K}_{g}(\sigma)-\lambda_{i} \mathbf{M}\right) \phi_{i}=0 \quad i=1,2, \ldots \tag{3.7-3}
\end{equation*}
\]
where
\[
\lambda_{i}=\omega_{i}^{2}
\]

If the user has specified the reset parameter GRAV in processor LAU to a value of unity then the matrix M has the meaning of a "weight" matrix instead of a "mass" matrix. This reset parameter is important for interpreting the eigenvalues calculated by the various eigensolvers.

\subsection*{3.7.3 ALGORITHM}

The algorithm used to solve equation (3.7-1) depends on the value of the global macrosymbol eigensolver_name. Processor EIG2 is used if eigensolver_name is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.7-2. Processor LAN is used if eigensolver_name is defined to be LAN. Processor LANZ is used if eigensolver_name is defined to be LANZ. These processors are based on the Lanczos algorithm as described in references 3.7-2 to 3.7-3. If this global macrosymbol is not defined, procedure L_VIBRAT_1 will set it to EIG2.

\subsection*{3.7.4 PROCEDURE USAGE}

Procedure L_VIbrat_1 may be invoked by the *call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call L_VIBRAT_1 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L_VIBRAT_1; note that those arguments without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline PS_1 & -- & Prescribed membrane stres resultant \(N_{x}^{o}\) \\
\hline PS_2 & -- & Prescribed membrane stres resultant \(N_{y}^{\circ}\) \\
\hline PS_3 & -- & Prescribed membrane stres resultant \(N_{x y}^{o}\) \\
\hline ERROR_TOL & . 0001 & Convergence criterion for eigenvalues \\
\hline FUNCTION & ALL & Select function to be performed by procedure \\
\hline INIT_VECTORS & 0 & Number of initial vectors used to span the subspace \\
\hline ISEQ & 0 & Resequencing method to be used \\
\hline LDI & 1 & Logical device index \\
\hline kname & K & First word of the name of the dataset containing the assembled stiffness matrix \\
\hline MASS_TYPE & CONSISTENT & Type of mass matrix \\
\hline Max_Iters & 20 & Maximum number of iterations \\
\hline N_GROUPS & 1 & \\
\hline WMODES & 1 & Number of eigenvalues to converge \\
\hline PRINT & <false> & Flag to print eigenvectors \\
\hline RENUYYER & <true> & Flag to resequence node numbers for equation solver \\
\hline SHIFT & 0.0 & Eigenvalue shift \\
\hline VCON_SET & 1 & Constraint set for vibration analysis \\
\hline
\end{tabular}

Tables 3.7-1, 3.7-2, and 3.7-3 list the datasets used or created by procedure L_VIBRAT-1, the procedures invoked by procedure L_VIBRAT_1, and the processors invoked by procedure L_VIBRAT_1, respectively.
\begin{tabular}{|l|l|c|c|}
\hline \multicolumn{2}{|c|}{ Table 3.7-1 Datasets Input/Output by procedure L_VIBRAT_1 } \\
\hline Dataset & Description & Input & Output \\
\hline AMAP..ic2.isize & Factorization Map for INV & & \(\sqrt{ }\) \\
\hline CEM.SPAR & Consistent Mass Matrix & & \(\sqrt{ }\) \\
\hline <ES_NAME>.EFIL.0.nnod & Element Computational Data & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline ES.SUMMARY & ES Processor Status & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline DEF.<ES_NAME>.0.nnod & Element Defn. (Connectivity) & \(\sqrt{ }\) & \\
\hline DEM.DIAG & Diagonal (Lumped) Mass Matrix & & \(\sqrt{ }\) \\
\hline DIR.<ES_NAME>.0.nnod & Element EFIL Directory & \(\sqrt{ }\) & \\
\hline INV.KSHF.j \(\dagger\) & Factored Shifted System Matrix & & \(\sqrt{ }\) \\
\hline INV.<KNAME>. \(\dagger\) & Factored System Matrix & & \(\sqrt{ }\) \\
\hline JDF1.BTAB.1.8 & Model Summary & \(\sqrt{ }\) & \\
\hline KG.SPAR.jdf2 & Assembled geometric stiffness matrix & & \(\sqrt{ }\) \\
\hline KMAP..ic2.isize & Model Connectivity Map & & \(\sqrt{ }\) \\
\hline <KNAME>.SPAR.jdf2 & Assembled system matrix & & \(\sqrt{ }\) \\
\hline VIBR.EVAL.1.j \(\dagger\) & Vibration eigenvalues & & \(\sqrt{ }\) \\
\hline VIBR.MODE.1.j \(\dagger\) & Vibration eigenvalues & \(\sqrt{ }\) \\
\hline
\end{tabular}
\(\dagger j=\) <vcon_set>
\begin{tabular}{|l|l|l|}
\hline Table 3.7-2 & Sub-Procedures Invoked by procedure L_VIBRAT_1 \\
\hline Procedure & Type & Function \\
\hline ES & External & Element utility procedure \\
\hline FACTOR & External & Factors assembled stiffness matrix \\
\hline L_VIBRAT_1 & Internal & Main procedure \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \multicolumn{2}{|c|}{ Table 3.7-3 Processors Invoked by Procedure L_VIBRAT_1 } \\
\hline Procedure & Type & Function \\
\hline AUS & Internal & Arithmetic utilities \\
\hline E & Internal & Initializes EFIL datasets \\
\hline EIG2 & Internal & Solve eigenvalue problem using subspace iteration \\
\hline ESi & External & Element processors based on GEP \\
\hline K & Internal & Assemble system matrix \\
\hline LAN & External & Solve eigenvalue problem using Lanczos method \\
\hline LANZ & External & Solve eigenvalue problem using Lanczos method \\
\hline RSEQ & Internal & Resequences nodes for equation solving \\
\hline TOPO & Internal & Generates nodal topology maps \\
\hline VPRT & Internal & Print SYSVEC system vectors \\
\hline
\end{tabular}

\subsection*{3.7.5 ARGUMENT DESCRIPTION}

\subsection*{3.7.5.1 ERROR_TOL}

Convergence criterion for eigenvalues (default: 0.0001 ). For the \(k\)-th iteration, the error measure for the \(i\)-th eigenvalue is
\[
\epsilon_{i}^{k}=\frac{\left\|\left(\lambda_{i}^{k}-\lambda_{i}^{k-1}\right)\right\|}{\left\|\lambda_{i}^{k}\right\|}
\]

The \(\boldsymbol{i}\)-th eigenvalue is converged if \(\epsilon_{i}^{k}\) is smaller than ERROR_TOL.

\subsection*{3.7.5.2 FUNCTION}

Select function to be performed by procedure L_VIBRAT_1 (default: all). This procedure may be used to perform two functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, and the eigenproblem is solved. For FUNCTION=EIGEN, procedure L_VIBRAT_1 uses a prescribed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model.

\subsection*{3.7.5.3 INIT_VECTOR}

Number of initial vectors used to span the subspace (default: 0). This argument defines the number of trial vectors used to initiate the subspace iteration. If IAIT_VECTOR \(=0\), the number of initial vectors will be calculated by the procedure as
```

INIT_VECTOR=MINIMUM (2*N_MODES, N_modes + 8)

```

\subsection*{3.7.5.4 ISEQ}

Resequencing method to be used (default: 0). If the argument RENUMBER is <true>, then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (i.e., method=0,1,2,3; see Section 6.1 of the CSM Testbed User's Manual, ref. 3.7-1).

\subsection*{3.7.5.5 LDI}

Logical device index (default: 1 ).

\subsection*{3.7.5.6 KNAME}

First word of the dataset name containing the assembled stiffness matrix (default: K).

\subsection*{3.7.5.7 MASS_TYPE}

Type of mass matrix (default: CONSISTENT). If MASS_TYPE=CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS_TYPE=DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

\subsection*{3.7.5.8 M_GROUPS}

Element group number (default: 1).

\subsection*{3.7.5.9 MAX_ITERS}

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

\subsection*{3.7.5.10 NMODES}

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR_TOL.

\subsection*{3.7.5.11 PRINT}

Flag to print modeshapes (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the vibration modeshapes.

\subsection*{3.7.5.12 PS_1}

Prescribed membrane stress resultant \(N_{x}^{o}\) for the prestressed state.

\subsection*{9.7.5.13 PS_2}

Prescribed membrane stress resultant \(N_{y}^{o}\) for the prestressed state.

\subsection*{3.7.5.14 PS_3}

Prescribed membrane stress resultant \(N_{x y}^{o}\) for the prestressed state.

\subsection*{3.7.5.15 RENOMBER}

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENUKBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

\subsection*{3.7.5.16 SHIFT}

Eigenvalue shift (default: 0.0 ). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared (i.e., \(\boldsymbol{\omega}^{\mathbf{2}}\) ) for vibration problems.

\subsection*{3.7.5.17 VCON_SET}

Constraint set number for vibration analysis (default: 1). This argument selects which constraint set to use in solving the linear vibration problem.

\subsection*{3.7.6 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
L_VIBRAT_1 & (main procedure) \\
ES & (initialize, form \(\mathbf{K}\) and \(\mathbf{M}\) ) \\
ES & (form \(\mathbf{K g}\) ) \\
FACTOR & (factor using vibration boundary conditions)
\end{tabular}

\subsection*{3.7.7 LIMITATIONS}

None.

\subsection*{3.7.8 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{3.7.9 USAGE GUIDELINES AND EXAMPLES}

Procedure L_VIBRAT_1 may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_VIBRAT_1 ( FUNCTION = ALL ; -- . Select function
VCON_SET $=1$; -- . Select vibration constraint set
ERROR_TOL =. 0001 ; -- . Eigenvalue convergence criterion
INIT_VECTOR = 0 ; -- . Number of initial vectors
ISEQ $=0$; -- . Select resequencing method
KNAME $=K$; -- . First word of stiffness matrix
-- . dataset name
MAX_ITERS $=20$; -- Maximum number of iterations
N_MODES $=1$; -- Number of eigenvalues
H_GROUPS = 1 ; --
PS_1 ; --
PS_2 ; --
PS_3 ; --
PRINT $=$ 〈true> ; -- . PRINT flag
RENUMBER = <true>; -- . RESEQUENCING flag
SHIFT $=0.0$; Eigenvalue shift

```

Before procedure L_VIBRAT_1 is called, the global macrosymbol eigensolver_name should be defined as described in Section 3.7-3; otherwise, the default value of EIG2 will be used.

\subsection*{3.7.10 PROCEDURE LISTING}

\subsection*{3.7.11 REFERENCES}
3.7-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.7-2 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
3.7-3 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

\subsection*{3.8 Procedure L_VIBRAT_2}

\subsection*{3.8.1 GENERAL DESCRIPTION}

Procedure L_VIBRAT_2 performs a linear vibration analysis about a prescribed prestressed state. The eigensolver is selected by defining the global macrosymbol eigensolver_name to be the name of the desired processor (e.g., EIG2, LAN), and the structural element processors ( \(\mathrm{ES} i\) ) form the elemental stiffness and mass matrices. The procedure assumes that the finite element model and boundary conditions have already been generated, that the prestressed state has been prescribed, and that the vibration modeshapes and frequencies need to be calculated.

\subsection*{3.8.2 THEORY}

Linear vibration analyses are formulated using the equations of motion for an undamped structure. For the case of prestressed state, the equations of motion are
\[
\begin{equation*}
\mathbf{M} \ddot{\mathbf{u}}+\mathbf{K} \mathbf{u}+\mathbf{K}_{g}(\boldsymbol{\sigma}) \mathbf{u}=\mathbf{0} \tag{3.8-1}
\end{equation*}
\]
where
\[
\begin{aligned}
\mathbf{M} & =\text { assembled mass matix (consistent or diagonal) } \\
\mathbf{K} & =\text { assembled linear stiffness matrix } \\
\mathbf{K}_{\boldsymbol{g}}(\boldsymbol{\sigma}) & =\text { assembled geometric stiffness matrix for given stress state } \\
\ddot{\mathbf{u}} & =\text { acceleration vector } \\
\mathbf{u} & =\text { displacement vector } \\
\boldsymbol{\sigma} & =\text { prestress state }
\end{aligned}
\]

The prestressed state may be defined in several ways. Procedure L_VIBrat_2 assumes that the prestressed state will be first calculated using procedure L_STATIC.

If harmonic motion is assumed, then
\[
\begin{equation*}
\mathbf{u}=\phi_{i} \sin \omega_{i} t \quad i=1,2, \ldots \tag{3.8-2}
\end{equation*}
\]
where
\[
\begin{aligned}
& \phi_{i}=i \text { th eigen modeshape } \\
& \omega_{i}=i \text { th circular frequency (radians per second) }
\end{aligned}
\]

The \(i\) th cyclic frequency \(f_{i}\) (in hertz) is
\[
f_{i}=\frac{\omega_{i}}{2 \pi}
\]
and the period \(T_{i}\) (in seconds) is
\[
T_{i}=\frac{1}{f_{i}}
\]

Substituting equation (3.8-2) in equation (3.8-1) gives
\[
\begin{equation*}
\left(\mathbf{K}+\mathbf{K}_{g}(\sigma)-\lambda_{i} \mathbf{M}\right) \phi_{i}=0 \quad i=1,2, \ldots \tag{3.8-3}
\end{equation*}
\]
where
\[
\lambda_{i}=\omega_{i}^{2}
\]

If the user has specified the reset parameter GRAV in processor LAU to a value of unity then the matrix \(M\) has the meaning of a "weight" matrix instead of a "mass" matrix. This reset parameter is important for interpreting the eigenvalues calculated by the various eigensolvers.

\subsection*{3.8.3 ALGORITHM}

The algorithm used to solve equation (3.3-1) depends on the value of the global macrosymbol eigensolver_name. Processor EIG2 is used if eigensolver_name is defined to be EIG2. This processor uses a nodal-block sparse matrix approach as described in reference 3.3-2. Processor LAN is used if eigensolver_name is defined to be LAN. Processor LANZ is used if eigensolver_name is defined to be LaNZ. These processors are based on the Lanczos algorithm as described in references 3.3-2 to 3.3-3. If this global macrosymbol is not defined, procedure L_VIBRAT_2 will set it to EIG2.

\subsection*{3.8.4 PROCEDURE USAGE}

Procedure L_vibrat_2 may be invoked by the *call directive, and following it by a list of arguments separated by semicolons(;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call L_VIBRAT_2 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure L_VIBRAT_2; note that those arguments without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline CONS_SET & 1 & Constaint set number for prestress analysis \\
\hline DIRECTION & 0 & Direction for element stress output \\
\hline EPROR_TOL & . 0001 & Convergence criterion for eigenvalues \\
\hline FUNCTION & ALL & Select function to be performed by procedure \\
\hline INIT_VECTORS & 0 & Number of initial vectors used to span the subspace \\
\hline ISEQ & 0 & Resequencing method to be used \\
\hline LDI & 1 & Logical device index \\
\hline RNAME & K & First word of the name of the dataset containing the assembled stiffness matrix \\
\hline LOAD_SET & 1 & Load set number \\
\hline MASS_TYPE & CONSISTENT & Type of mass matrix \\
\hline MaX_ITERS & 20 & Maximum number of iterations \\
\hline H_GROUPS & 1 & \\
\hline H.MODES & 1 & Number of eigenvalues to converge \\
\hline PRINT & <false> & Flag to print computed solutions \\
\hline REACTION & <false> & Flag to compute internal forces or reactions \\
\hline RENOMBER & <true> & Flag to resequence node numbers for equation solver \\
\hline SHIFT & 0.0 & Eigenvalue shift \\
\hline STRESS & <false> & Flag to compute element stresses (resultants) \\
\hline VCON_SET & 1 & Constraint set for vibration analysis \\
\hline
\end{tabular}

Tables 3.8-1, 3.8-2, and 3.8-3 list the datasets used or created by procedure L_VIBRAT_2, the procedures invoked by procedure L_VIBRAT_2, and the processors invoked by procedure L_VIBRAT_2, respectively.
\begin{tabular}{|l|l|c|c|}
\hline \multicolumn{4}{|c|}{ Table 3.8-1 Datasets Input/Output by procedure L_VIBRAT_2 } \\
\hline Dataset & Description & Input & Output \\
\hline AMAP..ic2.isize & Factorization Map for INV & & \(\checkmark\) \\
\hline CEM.SPAR & Consistent Mass Matrix & & \(\checkmark\) \\
\hline <ES_NAME>.EFIL.0.nnod & Element Computational Data & \(\checkmark\) & \(\checkmark\) \\
\hline ES.SUMMARY & ES Processor Status & \(\checkmark\) & \(\checkmark\) \\
\hline DEF.<ES_NAME>.0.nnod & Element Defn. (Connectivity) & \(\checkmark\) & \\
\hline DEM.DIAG & Diagonal (Lumped) Mass Matrix & & \(\checkmark\) \\
\hline DIR.<ES_NAME>.0.nnod & Element EFIL Directory & \(\checkmark\) & \\
\hline INV.KSHF.j \(\dagger\) & Factored Shifted System Matrix & & \(\checkmark\) \\
\hline INV.<KNAME>.j \(\dagger\) & Factored System Matrix & & \(\checkmark\) \\
\hline JDF1.BTAB.1.8 & Model Summary & \(\checkmark\) & \\
\hline KG.SPAR.jdf2 & Assembled geometric stiffness matrix & & \(\checkmark\) \\
\hline KMAP..ic2.isize & Model Connectivity Map & & \(\checkmark\) \\
\hline <KNAME>.SPAR.jdf2 & Assembled system matrix & & \(\checkmark\) \\
\hline VIBR.EVAL.1.j \(\dagger\) & Vibration eigenvalues & & \(\checkmark\) \\
\hline VIBR.MODE.1.j \(\dagger\) & Vibration eigenvalues & & \(\checkmark\) \\
\hline
\end{tabular}
\(\dagger j=<\) vcon_set>
\begin{tabular}{|l|l|l|}
\hline \multicolumn{3}{|c|}{ Table 3.8-2 } \\
\hline \multicolumn{2}{|l|}{ Sub-Procedures Invoked by procedure L_VIBRAT_2 } \\
\hline Procedure & Type & Function \\
\hline ES & External & Element utility procedure \\
\hline FACTOR & External & Factors assembled stiffness matrix \\
\hline L_STATIC & Internal & Static solution procedure \\
\hline L_VIBRAT_2 & Internal & Main procedure \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline \multicolumn{2}{|c|}{ Table 3.8-3 Processors Invoked by Procedure L_VIBRAT_2 } \\
\hline Procedure & Type & Function \\
\hline AUS & Internal & Arithmetic utilities \\
\hline E & Internal & Initializes EFIL datasets \\
\hline EIG2 & Internal & Solve eigenvalue problem using subspace iteration \\
\hline ESi & External & Element processors based on GEP \\
\hline K & Internal & Assemble system matrix \\
\hline LAN & External & Solve eigenvalue problem using Lanczos method \\
\hline LANZ & External & Solve eigenvalue problem using Lanczos method \\
\hline RSEQ & Internal & Resequences nodes for equation solving \\
\hline TOPO & Internal & Generates nodal topology maps \\
\hline VPRT & Internal & Print SYSVEC system vectors \\
\hline
\end{tabular}

\subsection*{3.8.5 ARGUMENT DESCRIPTION}

\subsection*{3.8.5.1 CONS_SET}

Constraint set number for prestress solution (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

\subsection*{3.8.5.2 DIRECTION}

Direction for the element stress (stress resultant) output (default: 0 ). The element stress coordinate system will be used if direction=0. The material axes ( \(x_{m}, y_{m}, z_{m}\) ) will be used if direction \(=1\); the material axes ( \(y_{m}, z_{m}, x_{m}\) ) will be used for direction=2; and the material axes ( \(z_{m}, x_{m}, y_{m}\) ) will be used for direction=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 3.4-2).

\subsection*{3.8.5.3 ERROR_TOL}

Convergence criterion for eigenvalues (default: 0.0001 ). For the \(k\)-th iteration, the error measure for the \(i\)-th eigenvalue is
\[
\epsilon_{i}^{k}=\frac{\left\|\left(\lambda_{i}^{k}-\lambda_{i}^{k-1}\right)\right\|}{\left\|\lambda_{i}^{k}\right\|}
\]

The \(i\)-th eigenvalue is converged if \(\epsilon_{i}^{k}\) is smaller than ERROR_TOL.

\subsection*{3.8.5.4 FUNCTION}

Select function to be performed by procedure L_VIbrat_2 (default: ALL). This procedure may be used to perform four functions. For FUNCTION=ALL, the element data are initialized and elemental stiffness matrices formed; nodal resequencing may be performed, the mesh topology is analyzed, the system stiffness matrix is assembled and factored, the displacement solution is obtained, optionally element stresses (stress resultants) and internal nodal forces (reactions) computed and the eigenproblem is solved. For FUZCTIOH=FACT_SOLV, procedure L_VIbrat_2 assumes that the system stiffness matrix has previously been assembled and that nodal resequencing has been performed. The procedure then proceeds to factor the system stiffness matrix, solves for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FUNCTION=SOLV, procedure L_VIBRAT_2 assumes that the system stiffness has previously been formed and factored. The procedure then proceeds to solve for the displacement solution, optionally computes the element stresses (stress resultants) and internal nodal forces (reactions) and solves the eigenproblem. For FUNCTION=EIGEN, procedure L_VIBRAT_2 uses a previously computed prestress state in solving the eigenvalue problem. Using the FUNCTION argument, the user may solve for a variety of constraint (boundary conditions) sets on a given model subjected to a variety of loading conditions.

\subsection*{3.8.5.5 INIT_VECTOR}

Number of initial vectors used to span the subspace (default: 0 ). This argument defines the number of trial vectors used to initiate the subspace iteration. If INIT_VECTOR \(=0\), the number of initial vectors will be calculated by the procedure as
\[
\text { INIT_VECTOR=MINIMUM ( } 2 * \text { N_MODES, N_modes }+8 \text { ) }
\]

\subsection*{3.8.5.6 ISEQ}

Resequencing method to be used (default: -1). If the argument RENOMBER is <true>, then nodal resequencing will be performed using processor RSEQ. The method used by processor RSEQ to resequence the nodes depends on the value of ISEQ. If the argument ISEQ is greater than or equal to zero, then that method will be used (i.e., method \(=0,1,2,3\); see Section 6.1 of the CSM Testbed User's Manual, ref. 3.8-1).

\subsection*{3.8.5.7 KNAME}

First word of the dataset name containing the assembled stiffness matrix (default: \(\mathbb{K}\) ).

\subsection*{3.8.5.8 LDI}

Logical device index (default: 1).

\subsection*{3.8.5.9 LOAD_SET}

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

\subsection*{3.8.5.10 MASS_TYPE}

Type of mass matrix (default: CONSISTENT). If MASS_TYPE=CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS_TYPE=DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

\subsection*{3.8.5.11 MAX_ITERS}

Maximum number of iterations (default: 20). This argument specifies the maximum number of iterations that can be used per call to eigensolver.

\subsection*{3.8.5.12 MMODES}

Number of converged eigenvalues desired (default: 1). This argument specifies the number of eigenvalues to calculate to a convergence criterion of ERROR_TOL.

\subsection*{3.8.5.13 PRINT}

Flag to print modeshapes (default: <false>). If printing of these computed results is requested, processor VPRT will be used to print the vibration modeshapes.

\subsection*{3.8.5.14 REACTION}

Flag to compute the internal nodal forces (default: <true>) If the argument REACTION=<true>, then the internal forces will be computed by calling procedure INT_FORC (see Section 6.2).

\subsection*{3.8.5.15 RENOMBER}

Flag to resequence node numbers prior to equation solving (default: <true>). If the argument RENOMBER=<true>, then processor RSEQ will be used to perform nodal resequencing, otherwise no resequencing will be performed. Note that the nodal resequencing may greatly reduce the time required to factor and solve the linear system of equations.

\subsection*{3.8.5.16 SHIFT}

Eigenvalue shift (default: 0.0). Converged eigenvalue will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared (i.e., \(\boldsymbol{\omega}^{\mathbf{2}}\) ) for vibration problems.

\subsection*{3.8.5.17 STRESS}

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION, respectively, by calling procedure STRESS (see Section 6.4).

\subsection*{3.8.5.18 VCON_SET}

Constraint set number for vibration analysis (default: 1). This argument selects which constraint set to use in solving the linear vibration problem.

\subsection*{3.8.6 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
L_VIBRAT_2 & (main procedure) \\
L_STATIC & (linear static analysis procedure) \\
ES & (initialize, form K and \(\mathbf{M}\) ) \\
FACTOR & (factor assembled stiffness matrix) \\
SOLVE & (solve linear system of equations) \\
STRESS & (stress/strain recovery procedure) \\
ES & (calculate element and nodal stress/strain) \\
INT_FORCE & (internal force procedure) \\
& ES \\
(internal force calculation) \\
ES & (form \(\mathbf{K}_{g}\) ) \\
FACTOR & (factor using vibration boundary conditions)
\end{tabular}

\subsection*{3.8.7 LIMITATIONS}

None.

\subsection*{3.8.8 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{3.8.9 USAGE GUIDELINES AND EXAMPLES}

Procedure L_VIBRaT_2 may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call L_VIBRAT_2 ( FUNCTION = ALL ; -- . Select function
VCON_SET = 1 ; -- . Select vibration constraint set
ERROR_TOL = . 0001 ; -- . Eigenvalue convergence criterion
INIT_VECTOR = 0 ; -- . Number of initial vectors
ISEQ =-1 ; - . Select resequencing method

```
```

KNAME = K ; -- . First word of stiffness matrix
MAX_ITERS = 20; -- Maximum number of iterations
H_MODES = 1 ; -- Number of eigenvalnes
CONS_SET = i ; -- . Select coūstriaiñt sêt
DIRECTION = 0 ; -- . Select direction for element stresses
LOAD_SET = 1 ; -- . Select load set
REACTION = <false> ; -- . REACTIONS flag
STRESS = <false\rangle -- . STRESS flag
PRINT = <true> ; -- . PRINT flag
RENUNBER = <true> ; -- . RESEQUENCING flag
SHIFT =0.0 ; Eigenvalve shift

```

Before procedure L_VIBRAT_2 is called, the global macrosymbol eigensolver_name should be defined as described in Section 3.8-3; otherwise, the default value of EIG2 will be used.

\subsection*{3.8.10 PROCEDURE LISTING}

\subsection*{3.8.11 REFERENCES}
3.8-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.8-2 Bostic, S. W. and Fulton R. E.: A Lanczos Eigenvalue Method on a Parallel Computer. AIAA Paper No. 87-0725-CP.
3.8-3 Jones, Mark T. and Patrick, Merrell L.: The Use of Lanczos's Method to Solve the Large Generalized Symmetric Definite Eigenvalue Problem. NASA CR-181914, September 1989. (Also available as ICASE Report No. 89-69).

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\subsection*{3.9 Procedure NL_STATIC_1}

\subsection*{3.9.1 GENERAL DESCRIPTION}

Procedure NL_STATIC_1, written by G. M. Stanley of Lockheed Palo Alto Research Laboratory, performs nonlinear static analysis based on a modified Newton/Raphson incremental strategy for automatic load-step control (e.g., ref. 3.1). Procedure NL_STATIC_1 relies on the Generic Element Processor (i.e., structural element processors, ESi) and hence has a corotational option for geometric nonlinearity that enables arbitrarily large rotations.

Procedure WL_STATIC_1 solves a nonlinear algebraic equation system of the form:
\[
\begin{equation*}
\mathbf{f}^{i n t}(\mathbf{d})=\mathbf{f}^{e x t}(\lambda) \tag{3.9-1}
\end{equation*}
\]
where \(f^{\text {int }}\) is the nonlinear internal force vector for the discrete (i.e., finite element) system, \(\mathbf{f}^{e x t}\) is the external force vector, \(\mathbf{d}\) is the displacement vector, and \(\lambda\) is a load factor. The basic modified Newton/Raphson procedure solves this system of equations by linearizing it at each load level (i.e., fixed \(\lambda\) ), leading to the solution of the following linear equations:
\[
\begin{align*}
\mathbf{K} \delta \mathbf{d}_{n+1}^{(i+1)} & =\mathbf{r}\left(\mathbf{d}_{n+1}^{(i)}, \lambda_{n+1}\right)  \tag{3.9-2}\\
\mathbf{d}_{n+1}^{(i+1)} & =\mathbf{d}_{n+1}^{(i)}+\delta \mathbf{d}_{n+1}^{(i+1)}
\end{align*}
\]
within an iteration loop where \(n+1\) is the current (fixed) load-step number, \(i+1\) is the iteration number at that load-step, \(\delta \mathbf{d}\) is the iterative displacement change, and \(\mathbf{r}=\mathbf{f}^{e x t}-\mathbf{f}^{\text {int }}\) is the nonlinear residual force vector. \(K\) is the effective tangent stiffness matrix, which is updated only at the first iteration of selected load steps (though typically at every step). Iteration is continued until the inner product of \(\delta \mathbf{d}\) and \(\mathbf{r}\) become smaller than a user-specified error tolerance.

An arc-length constraint is added to the above equations so that i) the user doesn't have to select the load increment ( \(\Delta \lambda=\lambda_{n+1}-\lambda_{n}\) ), and ii) the solution algorithm can automatically traverse limit points - maxima and minima in the load-displacement "curve". The user need only specify the initial load factor, \(\lambda_{1}\); the constraint equation converts this to an "arc-length" increment in load-displacement space, and adaptively adjusts this increment based on the iterative performance of the algorithm. Details of this algorithm are given in the theory and algorithm sections.

\subsection*{3.9.2 THEORY}

\subsection*{3.9.2.1 Introduction}

Procedure NL_STATIC_1 performs a quasi-static analysis of a system of nonlinear equilibrium equations using an adaptive arc-length-controlled Newton/Raphson incremental/iterative solution algorithm. The arc-length method adopted here is based on a variant
of Crisfield's algorithm (ref. 3.1), where instead of using a nonlinear (quadratic) arclength constraint equation in conjunction with the linearized equilibrium equations, the constraint equation is consistently linearized as well. This eliminates the pitfalls associated with quadratic root selection in Crisfield's algorithm. By combining this modification with i) polynomial extrapolation of converged solutions to obtain step-predictor solutions, ii) an energy error norm that properly weights translational and rotational freedoms, and iii) generalization to large rotations, specified displacements and live loads; the present algorithm is both more general and more robust than the basic algorithm. Additional enhancements to overcome hard singularities at limit and bifurcation points are currently under development; and will be incorporated as procedures at a later date.

\section*{NOTATION}
d Displacement vector.
\(\delta d \quad\) Iterative change in \(d\).
\(\Delta d \quad\) Incremental (load-step) change in \(d\).
\(\mathrm{d}_{n}^{i} \quad\) Displacement vector at iteration \(i\) of step \(n\).
\(\Delta d_{n}^{i} \quad\) Incremental (step) change in \(d . \Delta d_{n+1}^{(i+1)}=d_{n+1}^{(i)}-d_{n}\)
\(\delta \hat{\mathbf{d}} \quad\) Tangential displacement \(=\mathbf{K}^{-1} \mathbf{f}^{e x t}\)
\(\Delta \ell \quad\) Incremental arc-length (step) parameter.
\(\hat{\mathbf{f}}^{\text {ext }} \quad\) External force vector - base load.
\(f^{\text {int }} \quad\) Internal force vector.
\(\mathbf{r}\) Residual force vector.
\(\mathbf{K} \quad\) Stiffness matrix.
\(\delta \overline{\mathbf{d}} \quad\) Basic (fixed-load) iterative change in \(\mathbf{d}\).
\(\delta \mathbf{d}^{*} \quad\) Linear combination of \(\delta \overline{\mathbf{d}}\) and \(\delta \hat{\mathbf{d}}\).
num_cuts Number of times load step has been cut in half at current step.
num_div Number of consecutive iterations at which divergence occurs.
\(c_{n} \quad\) Extrapolation coefficient corresponding to step \(n\).
\(\widehat{\epsilon} \quad\) Relative error in energy norm.
\(\epsilon \quad\) Absolute error in energy norm.
\(\epsilon_{\text {ref }} \quad\) Reference value of \(\epsilon\); initialized as zero.
\(\epsilon_{\text {tol }} \quad\) Relative error tolerance (default: \(10^{-4}\) ).
\(\lambda \quad\) Load factor.
\(\Delta \lambda \quad\) Incremental (load-step) change in \(\lambda\).
\(K^{u \bullet} \quad\) Stiffness submatrix coupling specified (s) displacement components with force components corresponding to unknown ( \(u\) ) displacements.
\(\hat{d}^{*} \quad\) Base value of specified displacement vector.
\(\mathbf{d}^{d} \quad\) Current value of specified displacement vector. \(\mathbf{d}^{s}=\lambda \widehat{\mathbf{d}}^{d}\).

\subsection*{3.9.2.2 Nonlinear Equations}

The set of nonlinear equations solved by the present algorithm consist of: i) the system of equilibrium equations for the discrete (finite element) model, and ii) a single constraint equation governing the maximum "arc-length" to be traversed in a single solution increment along a curve in load-displacement space. These equations may be expressed as follows:
\[
\begin{array}{ll}
\mathbf{r}(\mathbf{d}, \lambda)=0 & \text { (Equilibrium) }  \tag{3.9-3}\\
\mathbf{c}(\mathbf{d}, \lambda)=0 & \text { (Arc-length Constraint) }
\end{array}
\]
where \(d\) is the displacement vector representing all of the degrees-of-freedom (DOFs) for the discrete model, and \(\lambda\) is an external load parameter. In conventional load- or displacementcontrolled solution algorithms, \(\lambda\) is usually specified by the user. In an arc-length controlled algorithm like the present one, \(\lambda\) is treated as an additional unknown. Thus, there are just as many independent equations in equation 3.9-3 as there are unknowns. The vector r represents the residual (or out-of-balance) force vector, which is identically zero at equilibrium.
For the special case of:
- Displacement-independent loading
- Proportional (one-parameter) force loading
- Load-independent arc-length constraint
\(r\) and \(c\) take on the following form:
\[
\begin{align*}
& \mathbf{r}(\mathbf{d}, \lambda)=\lambda \widehat{\mathbf{f}}^{e x t}-\mathbf{f}^{i n t}(\mathbf{d})  \tag{3.9-4}\\
& c(\mathbf{d}, \lambda)=\|\Delta \mathbf{d}\|^{2}-\Delta \ell^{2}
\end{align*}
\]
where \(\widehat{f}^{e x t}\) is a normalized (base-value) external load vector, \(f^{i n t}\) is the nonlinear internal force vector, \(\Delta \mathbf{d}\) is an incremental displacement vector, defined as
\[
\begin{equation*}
\Delta \mathbf{d}=\mathbf{d}-\mathbf{d}_{n} \tag{3.9-5}
\end{equation*}
\]
in which \(d_{n}\) is the known displacement vector at a nearby (previous) configuration, and \(\Delta \ell\) is a prescribed arc-length parameter defining the size of the increment.

The problem statement then is to solve equation 3.9-3 for a statically connected set of configurations, ( \(\mathrm{d}, \lambda\) ), representing the load-displacement "history" of the structural model. Note that due to the nonlinear nature of the equations, this history is not always unique. For example, at pure bifurcation points, the present algorithm cannot determine the correct path, unless some sort of imperfection or "trigger" is introduced by the user - thus converting the bifurcation point into a limit point. Limit points (i.e., local maximums and minimums in the load-displacement curve) cause no difficulty for the present algorithm except when a load-step happens to lie "too close" to the actual limit point (see procedure NL_STATIC_2 for a solution to this rare but frustrating problem).

\subsection*{3.9.2.3 Linearized Equations}

To solve the above nonlinear equations, we use the modified Newton/Raphson algorithm, which requires their linearization - i.e., first-order Taylor series expansion of the simultaneous equations. The solution to the linearized equations is then used to update the nonlinear solution in an iterative process that continues until convergence has been obtained at a given configuration. Furthermore, the final configuration is typically obtained as a series of steps, or increments, with a new iteration cycle occuring within each step; and with information from preceding steps used to predict a starting solution at the new step. (This is
commonly called an "incremental/iterative" algorithm.) Note that the iterative changes in displacement and load-factor, which we shall denote \(\delta \mathbf{d}\) and \(\delta \lambda\), respectively, are different than the incremental changes, denoted by \(\Delta d\) and \(\Delta \lambda\). The incremental load/displacement changes are used to advance from one converged solution ( \(\mathrm{d}_{n}, \lambda_{n}\) ) to another ( \(\mathrm{d}_{n+1}, \lambda_{n+1}\); while the iterative changes all refer to successive approximations \(\left(d_{n+1}^{(i)}, \lambda_{n+1}^{(i)}\right)\) of the same target configuration ( \(\mathrm{d}_{n+1}, \lambda_{n+1}\) ). Thus, \(\delta \mathrm{d}_{\text {converges to zero at a given configuration, }}\) while \(\Delta \mathrm{d}\) converges to a value dictated by the arc-length constraint equation 3.9-4b*
Linearization of equations 3.9-4 about a reference configuration ( \(\overline{\mathrm{d}}, \bar{\lambda}\) ) results in the following expressions:
\[
\begin{align*}
\mathbf{r}(\mathbf{d}, \lambda) & \approx \mathbf{r}(\overline{\mathbf{d}}, \bar{\lambda})+\frac{\partial \mathbf{r}}{\partial \mathbf{d}}(\overline{\mathbf{d}}, \bar{\lambda}) \delta \mathbf{d}+\frac{\partial \mathbf{r}}{\partial \lambda}(\overline{\mathbf{d}}, \bar{\lambda}) \delta \lambda=0  \tag{3.9-6}\\
c(\mathbf{d}, \lambda) & \approx c(\overline{\mathbf{d}}, \bar{\lambda})+\frac{\partial c}{\partial \mathbf{d}}(\overline{\mathbf{d}}, \bar{\lambda}) \delta \mathbf{d}+\frac{\partial c}{\partial \lambda}(\overline{\mathbf{d}}, \bar{\lambda}) \delta \lambda=0
\end{align*}
\]
where for the special assumptions listed in Section 3.9.9.1, the partial derivatives in equation 3.9-6 become:
\[
\begin{array}{rlrl}
\frac{\partial \mathbf{r}}{\partial \mathbf{d}}(\overline{\mathbf{d}}, \bar{\lambda})=-\mathbf{K}(\overline{\mathbf{d}}), & \frac{\partial \mathbf{r}}{\partial \lambda}(\overline{\mathbf{d}}, \bar{\lambda}) & =\widehat{\mathbf{f}}^{e x t} \\
\frac{\partial c}{\partial \mathbf{d}}(\overline{\mathbf{d}}, \bar{\lambda})=2 \Delta \overline{\mathbf{d}}, & \frac{\partial c}{\partial \lambda}(\overline{\mathbf{d}}, \bar{\lambda})=0 \tag{3.9-7}
\end{array}
\]
where \(K=\partial \mathrm{f}^{\text {int }} / \partial \mathrm{d}\) is the tangent stiffness matrix. Substituting equation 3.9-7 into equation 3.9-6 leads to the simultaneous linear equations:
\[
\begin{align*}
\overline{\mathbf{K}} \delta \mathbf{d} & =\overline{\mathbf{r}}+\delta \lambda \widehat{\mathbf{f}}^{\mathbf{e x t}}  \tag{3.9-8}\\
2 \Delta \overline{\mathbf{d}} \cdot \delta \mathbf{d} & =\overline{\mathbf{c}}
\end{align*}
\]
where
\[
\overline{\mathbf{r}}=\mathbf{r}(\overline{\mathbf{d}}, \bar{\lambda}), \quad \overline{\boldsymbol{c}}=\boldsymbol{c}(\overline{\mathbf{d}}, \bar{\lambda}), \quad \overline{\mathbf{K}}=\left\{\begin{array}{l}
\mathbf{K}(\overline{\mathbf{d}}) \text { for True Newton }  \tag{3.9-9}\\
\mathbf{K}\left(\mathbf{d}_{\boldsymbol{n}}\right) \text { for Modified Newton }
\end{array}\right.
\]

Solving the first of equations \(3.9-8\) for \(\delta d\) leads to
\[
\begin{equation*}
\delta \mathbf{d}=\overline{\mathbf{K}}^{-1}\left[\overline{\mathbf{r}}+\widehat{\mathbf{f}}^{e x t} \delta \lambda\right]=\delta \overline{\mathbf{d}}+\delta \hat{\mathbf{d}} \delta \lambda \tag{3.9-10}
\end{equation*}
\]
where
\[
\begin{align*}
& \delta \overline{\mathbf{d}}=\overline{\mathbf{K}}^{-1} \overline{\mathbf{r}}  \tag{3.9-11}\\
& \delta \hat{\mathbf{d}}=\overline{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{\text {ext }}
\end{align*}
\]

\footnotetext{
* The reason for using a series of increments, instead of solving for the final solution in one single increment, is that the Newton/Raphson method converges only if the starting solution is sufficiently "close" to the final solution.
}

Similarly, we can solve for \(\delta \lambda\), by substituting equation \(3.9-10\) into equation \(3.9-8 \mathrm{~b}\), i.e.,
\[
\begin{equation*}
\overline{\mathbf{c}}+2 \Delta \overline{\mathbf{d}} \cdot \dot{\delta} \overline{\mathbf{d}}+2(\Delta \overline{\mathbf{d}} \cdot \delta \widehat{\mathbf{d}}) \delta \lambda=0 \tag{3.9-12}
\end{equation*}
\]
which yields
\[
\begin{equation*}
\delta \lambda=\frac{-\bar{c}-2 \Delta \overline{\mathbf{d}} \cdot \delta \overline{\mathbf{d}}}{2 \Delta \overline{\mathbf{d}} \cdot \delta \hat{\mathbf{d}}}=\frac{\Delta \ell^{2}-\|\Delta \overline{\mathbf{d}}\|^{2}-2 \Delta \overline{\mathbf{d}} \cdot \delta \overline{\mathbf{d}}}{2 \Delta \overline{\mathbf{d}} \cdot \delta \hat{\mathbf{d}}} \tag{3.9-13}
\end{equation*}
\]

\subsection*{3.9.2.4 Update Procedure}

The solution update procedure - from one iteration to the next at a fixed arc-length increment from a converged solution - consists of the following two (sequential) equations:
1) \(\delta \lambda=\frac{\Delta \ell^{2}-2 \Delta \bar{d}-\|\Delta \overline{\mathbf{d}}\|^{2}}{2 \Delta \overline{\mathbf{d}} \cdot \delta \hat{\mathbf{d}}}\)
2) \(\delta \mathbf{d}=\delta \overline{\mathbf{d}}+\delta \widehat{\mathbf{d}} \delta \lambda\)
where \(\delta \overline{\mathrm{d}}\) and \(\delta \widehat{\mathrm{d}}\) are first computed using equation 3.9-11, and \(\Delta \overline{\mathrm{d}}\) is the displacement increment from the previous converged solution to the previous iterate of the current solution, i.e., \(\overline{\mathbf{d}}-\mathbf{d}_{n}\).

Then we simply apply the update formulas:
\[
\begin{align*}
& \mathbf{d}=\overline{\mathbf{d}}+\delta \mathbf{d} \\
& \lambda=\bar{\lambda}+\delta \lambda \tag{3.9-15}
\end{align*}
\]
where special consideration must be given to equation 3.9-15a in the case of problems with large-rotational degrees-of-freedom (see Section 3.9.2.10).

\subsection*{3.9.2.5 Predictor Solutions; arc-length-Constraint and Extrapolation Techniques}

To obtain a prediction for \(\mathrm{d}_{n+1}\) and \(\lambda_{n+1}\) at the beginning of step \(n+1\) (so that the Newton iterations may occur within a sufficiently small neighborhood of the converged solution), we use one of the following two procedures:
1) The arc-length constraint equation \(3.9-4 \mathrm{~b}\)
or
2) Quadratic extrapolation of a series of converged solutions

The first approach (arc-length constraint) leads to the following predictor equations:
\[
\begin{align*}
& \mathbf{d}_{n+1}^{(1)}=\mathbf{d}_{n}+\underbrace{\Delta \lambda_{n+1}^{(1)} \delta \hat{\mathbf{d}}_{n+1}}_{\Delta \mathbf{d}_{n+1}^{(1)}}  \tag{3.9-16}\\
& \lambda_{n+1}^{(1)}=\lambda_{n} \pm \underbrace{\frac{\Delta \ell_{n+1}}{\left\|\delta \hat{\mathbf{d}}_{n+1}\right\|}}_{\Delta \lambda_{n+1}^{(1)}}
\end{align*}
\]
where the sign in front of \(\Delta \lambda\) in equation \(3.9-16 \mathrm{~b}\) is taken as the sign of the determinant of \(\bar{K}\). Equation 3.9-16a was obtained by noting that
\[
\begin{equation*}
\Delta \mathrm{d}_{n+1}^{(1)}=\delta \mathrm{d}_{n+1}^{(1)} \tag{3.9-17}
\end{equation*}
\]
which from equation 3.9-10 can be written as
\[
\begin{equation*}
\delta \mathbf{d}_{n+1}^{(1)}=\delta \overline{\mathbf{d}}_{n+1}^{(1)}+\delta \lambda_{n+1}^{(1)} \delta \hat{\mathrm{d}}_{n+1}=\Delta \lambda_{n+1}^{(1)} \delta \hat{\mathrm{d}}_{n+1} \tag{3.9-18}
\end{equation*}
\]
since
\[
\begin{equation*}
\delta \overline{\mathbf{d}}_{n+1}^{(1)}=\overline{\mathbf{K}}^{-1} \mathbf{r}_{n}=\overline{\mathbf{K}}^{-1} \mathbf{0}=\mathbf{0} \tag{3.9-19}
\end{equation*}
\]
and
\[
\begin{equation*}
\delta \lambda_{n+1}^{(1)}=\Delta \lambda_{n+1}^{(1)} \tag{3.9-20}
\end{equation*}
\]

Then, equation 3.9-16b follows by substituting equation 3.9-16a into the arc-length constraint equation
\[
\begin{equation*}
\left\|\Delta \mathrm{d}_{n+1}^{(1)}\right\|=\Delta \ell \tag{3.9-21}
\end{equation*}
\]

The second approach (quadratic extrapolation) leads to the following predictor equations:
\[
\begin{align*}
& \mathbf{d}_{n+1}^{(1)}=c_{n} \mathbf{d}_{n}+c_{n-1} d_{n-1}+c_{n-2} d_{n-2}  \tag{3.9-22}\\
& \lambda_{n+1}^{(1)}=c_{n} \lambda_{n}+c_{n-1} \lambda_{n-1}+c_{n-2} \lambda_{n-2}
\end{align*}
\]
where \(\left(d_{n}, \lambda_{n}\right),\left(d_{n-1}, \lambda_{n-1}\right)\), and \(\left(d_{n-2}, \lambda_{n-2}\right)\) are the converged solutions at the three previous (consecutive) load steps, and the \(c_{i}\) are the quadratic Lagrange interpolation functions:
\[
\begin{align*}
c_{n} & =\frac{\left(\ell_{n+1}-\ell_{n-2}\right)\left(\ell_{n+1}-\ell_{n-1}\right)}{\left(\ell_{n}-\ell_{n-2}\right)\left(\ell_{n}-\ell_{n-1}\right)} \\
c_{n-1} & =\frac{\left(\ell_{n+1}-\ell_{n-2}\right)\left(\ell_{n+1}-\ell_{n}\right)}{\left(\ell_{n-1}-\ell_{n-2}\right)\left(\ell_{n-1}-\ell_{n}\right)}  \tag{3.9-23}\\
c_{n-2} & =\frac{\left(\ell_{n+1}-\ell_{n-1}\right)\left(\ell_{n+1}-\ell_{n}\right)}{\left(\ell_{n-2}-\ell_{n-1}\right)\left(\ell_{n-2}-\ell_{n}\right)}
\end{align*}
\]

The arc-length parameter, \(\ell\), is computed by arbitrarily setting \(\ell_{\boldsymbol{n}-2}=0\), and accumulating the incremental parameters, \(\Delta \ell\). Thus,
\[
\begin{align*}
\ell_{n-2} & =0 \\
\ell_{n-1} & =\Delta \ell_{n-1} \\
\ell_{n} & =\ell_{n-1}+\Delta \ell_{n}  \tag{3.9-24}\\
\ell_{n+1} & =\ell_{n}+\Delta \ell_{n+1}
\end{align*}
\]
where the arc-length increments, \(\Delta \ell_{n-2}, \Delta \ell_{n-1}, \Delta \ell_{n}\), and \(\Delta \ell_{n+1}\) are defined by the adaptive algorithm described in Section 3.9.2.6.
Note that unlike the arc-length-based predictor equations 3.9-16, the above extrapolation formulas do not require any additional information to determine the direction (i.e., sign) of the load increment. This is because the curvature of the quadratic polynomial used for extrapolation automatically senses, and enables the traversal of, turning points in the solution path.
Quadratic extrapolation is usually much more efficient than the arc-length constraint approach for computing the predictor solutions. In some cases, extrapolation can reduce the number of load steps by up to an order of magnitude. However, in other cases - e.g., around very sharp turns in load-displacement space - quadratic extrapolation may be too smooth to capture the sudden changes. In such cases, small, arc-length-controlled predictor steps may be the most practical strategy for getting through the critical phases. (Adaptive algorithms for selectively switching between extrapolation and arc-length step predictors are recommended as a topic for future research.)

\subsection*{3.9.2.6 Adaptive Load-Step (arc-length) Selection}

To advance the solution from one load-step ( n ) to the next ( \(\mathrm{n}+1\) ), it is also necessary to select a new arc-length increment, \(\Delta \ell_{n+1}\). Note that this parameter, which represents a distance traversed along the load-displacement "curve", is (by definition) always positive,* but may grow or shrink depending on solution difficulty. To automate the process, we use the following simple, but fairly robust, heuristic algorithm suggested by Crisfield (ref. 3.1):
\[
\begin{equation*}
\Delta \ell_{n+1}=\frac{\text { Desired number of iterations }}{\text { Actual number of iterations }} \times \Delta \ell_{n} \tag{3.9-25}
\end{equation*}
\]
where actual refers to the number of iterations required for convergence at the previous step ( n ), and the desired number of iterations is user-specified and typically around 4. This causes the step-size to grow or shrink in direct proportion to the convergence rate of the nonlinear solution, and generally leads to a nearly constant number of iterations (i.e., computations) per step. In fact the number of load-steps will automatically adjust according to the curvature of the load-displacement curve, with more steps being required around turning points (high curvature) and less along smooth stretches (low curvature).

\footnotetext{
* This is in contrast to conventional load-controlled algorithms, which require explicit selection of the load increment, - a parameter that may change sign at limit or bifurcation points.
}

Note that the initial value of the arc-lengit increment, \(\Delta \hat{\ell}_{1}\), must be specified - at least indirectly - by the user. However, since the user typically has no physical insight about the magnitude of \(\Delta \ell_{1}\), we employ the arc-length constraint equation 3.9-10 to compute it in terms of the initial load-factor, \(\Delta \lambda_{1}\) - which the user can typically estimate based on some prior linear analysis. The expression used to compute the initial arc-length increment is thus
\[
\begin{equation*}
\Delta \ell_{1}=\lambda_{1}\left\|\delta \hat{\mathrm{~d}}_{1}\right\| \tag{3.9-26}
\end{equation*}
\]
which was derived by rewriting equation 3.9-16b as
\[
\begin{equation*}
\Delta \ell_{n+1}=\Delta \lambda_{n+1}\left\|\delta \widehat{\mathbf{d}}_{n+1}\right\| \tag{3.9-27}
\end{equation*}
\]
setting \(n=0\) and noting that
\[
\begin{equation*}
\Delta \lambda_{1}=\lambda_{1}-\lambda_{0}=\lambda_{1} \tag{3.9-28}
\end{equation*}
\]

The "tangential" displacement, \(\delta \widehat{\mathbf{d}}_{1}\), in equation 3.9-26 is simply the linear solution obtained with the normalized external load vector as right-hand-side, i.e.,
\[
\begin{equation*}
\delta \widehat{\mathbf{d}}_{1}=\mathbf{K}^{-1}(0) \widehat{\mathbf{f}}^{e x t} \tag{3.9-29}
\end{equation*}
\]

\subsection*{3.9.2 .7 Specified Displacements}

The presence of specified-displacement loads (in addition to specified-force loads) affects the above algorithm in three subtle - but important - ways:
i) It modifies the definition of the residual force vector, \(r\), since the internal force vector, \(f^{\text {int }}\), becomes a function of the load-factor, \(\lambda\).
ii) Due to the above dependence, the derivative of \(\mathbf{r}\) with respect to \(\lambda\) gains an additional term, which in turn modifies the definition of the tangential displacement vector, \(\delta \widehat{\mathbf{d}}\).
iii) The specified displacement components must be included in all displacement norms and inner products appearing in the arc-length constraint equation, and in the computation of nonlinear error estimates.

The above modifications can be expressed mathematically as follows. First, define a specified displacement vector, \(\mathrm{d}^{\mathbf{}}\), which has zeros everywhere except in the components that are user-specified. Further assume that this specified displacement vector is scaled by the same load-factor, \(\lambda\), as the external force vector, i.e.,
\[
\begin{equation*}
\mathbf{d}^{t}=\lambda \hat{\mathbf{d}}^{\prime} \tag{3.9-30}
\end{equation*}
\]
where \(\hat{\mathbf{d}}^{s}\) is a normalized vector containing the reference \((\lambda=1)\) values of specified displacement. The expression for the residual force vector, equation 3.9-4, can then be re-written as
\[
\begin{equation*}
\mathbf{r}(\mathbf{d}, \lambda)=\lambda \widehat{\mathbf{f}}^{e x t}-\mathbf{f}^{i n t}\left(\mathbf{d}, \mathrm{~d}^{d}\right) \tag{3.9-31}
\end{equation*}
\]
and its derivative with respect to \(\lambda\) in equation 3.9-7 becomes
\[
\begin{equation*}
\frac{\partial \mathbf{r}}{\partial \lambda}=\widehat{\mathbf{f}}^{e x t}-\frac{\partial \mathbf{f}^{i n t}}{\partial \mathbf{d}^{s}} \frac{\partial \mathbf{d}^{e}}{\partial \lambda}=\widehat{\mathbf{f}}^{e x t}-\frac{\partial \mathbf{f}^{i n t}}{\partial \mathbf{d}^{s}} \widehat{\mathbf{d}}^{s} \tag{3.9-32}
\end{equation*}
\]

But:
\[
\begin{equation*}
\frac{\partial \mathbf{f}^{i n t}}{\partial \mathrm{~d}^{t}}=\mathbf{K}^{u s} \tag{3.9-33}
\end{equation*}
\]
where \(K^{u s}\) is the partition of the tangent stiffness matrix that couples specified displacement increments to unknown force increments, i.e., the extended stiffness matrix may be partitioned as
\[
\mathbf{K}^{*}=\left[\begin{array}{ll}
\mathbf{K}^{u u} & \mathbf{K}^{u s}  \tag{3.9-34}\\
\mathbf{K}^{s u} & \mathbf{K}^{s e}
\end{array}\right]
\]
where \(K^{u u}\) is the active block of the stiffness matrix, i.e., in the present terminology:
\[
\begin{equation*}
\mathbf{K}=\mathbf{K}^{u \mathbf{u}} \tag{3.9-35}
\end{equation*}
\]

Thus, the new load-derivative of the residual force vector may be expressed as
\[
\begin{equation*}
\frac{\partial \mathbf{r}}{\partial \lambda}=\widehat{\mathbf{f}}^{e x t}-\mathbf{K}^{u s} \hat{\mathbf{d}}^{s} \tag{3.9-36}
\end{equation*}
\]
and the corresponding tangential displacement vector from equation 3.9-11b becomes:
\[
\begin{equation*}
\delta \widehat{\mathbf{d}}=\overline{\mathbf{K}}^{-1}\left(\mathbf{f}^{e x t}-\overline{\mathbf{K}}^{u \bullet} \hat{\mathbf{d}}^{\boldsymbol{t}}\right) \tag{3.9-37}
\end{equation*}
\]
where the superposed bar is defined in equation 3.9-9.
Note that the solution indicated in equation 3.9-37 is much like what is required for linear analysis with specified displacements: The right-hand-side is modified by multiplying a part of the extended stiffness matrix times the (normalized) specified displacements. This is in contrast to the solution for \(\delta \overline{\mathrm{d}}\) in equation \(3.9-11 \mathrm{a}\), where specified displacements are accounted for exclusively through their nonlinear dependence in the residual force vector, \(\overline{\mathbf{r}}\).

\subsection*{3.9.2.8 General Loading (e.g., "Live" Loads)}

The last restriction we shall lift is the simple form of the external force vector given in equation 3.9-4a, i.e., we shall replace:
\[
\begin{equation*}
\mathbf{f}^{e x t}=\lambda \widehat{\mathbf{f}}^{e x t} \tag{3.9-38}
\end{equation*}
\]
by
\[
\begin{equation*}
\mathbf{f}^{e x t}=\lambda \widehat{\mathbf{f}}^{e x t}(\mathbf{d}) \tag{3.9-39}
\end{equation*}
\]

This allows for the kind of displacement-dependent (or "live") loading that arises from hydrostatic, or follower, forces. The residual force vector then becomes
\[
\begin{equation*}
r(d, \lambda)=\lambda \hat{\mathbf{f}}^{e x t}(\mathbf{d})-\mathbf{f}^{i n t}\left(\mathbf{d}, \lambda \hat{\mathbf{d}}^{\prime}\right) \tag{3.9-40}
\end{equation*}
\]
and the only modifications to equations 3.9-7 are that i) the tangent stiffness matrix acquires a load-stiffness contribution, i.e.,
\[
\begin{equation*}
\frac{\partial \mathbf{r}}{\partial \mathbf{d}}=-\mathbf{K}=-\left(\mathbf{K}^{m a t l}+\mathbf{K}^{g e o m}+\mathbf{K}^{\text {load }}\right) \tag{3.9-41}
\end{equation*}
\]
where
\[
\begin{equation*}
\mathbf{K}^{\text {load }}=-\frac{\partial \mathbf{f}^{e x t}}{\partial \mathbf{d}} \tag{3.9-42}
\end{equation*}
\]
and ii) the external-force contribution to the tangent load vector, \(r_{, \lambda}\), is no longer a constant, i.e.,
\[
\begin{equation*}
\frac{\partial \mathbf{r}}{\partial \lambda}=\widehat{\mathbf{f}}^{e x t}(\mathbf{d})-\mathbf{K}^{u s}(\mathbf{d}) \hat{\mathbf{d}}^{t} \tag{3.9-43}
\end{equation*}
\]

Note that we have not allowed for a general external-load history, in which both the magnitude and direction of the external force vector may change from step to step, e.g.,
\[
\begin{equation*}
\mathbf{f}^{e x t}=\mathbf{f}^{e x t}(\mathbf{d}, \lambda) \tag{3.9-44}
\end{equation*}
\]

Nor have we allowed for multiple load-factors, \(\lambda_{a}, \lambda_{b}, \ldots\), which can arise when several independent load systems are acting on a structure. Such complications require straightfoward generalization of the present arc-length algorithm, and will be considered as necessary for future applications.

\subsection*{3.9.2.9 Convergence Criteria}

As a measure of the error in the nonlinear equilibrium equations (not including discretization errors), we use an energy norm, which is the inner product of the residual force vector and the iterative displacement-change vector. This is effective for two reasons: i) it involves only a single error norm, in contrast to algorithms that check displacement and residual errors independently; and ii) the inner product of force and displacement introduces a natural scaling of different types of generalized freedoms (for example rotational freedoms versus translational freedoms) - by weighting each generalized displacement with its corresponding (conjugate) generalized force. Thus, sensitivity to physical units and choice of independent variables is minimized.
Convergence of the nonlinear solution process at a given load-step, \(n+1\), is checked by evaluating the following energy error norm at each iteration, \(i\) :
\[
\begin{equation*}
\| \text { error } \|_{n+1}^{(i)}=\sqrt{\mathbf{r}_{n+1}^{(i)} \cdot \delta d_{n+1}^{(i)}} \tag{3.9-45}
\end{equation*}
\]
and comparing it with some user-specified fraction of a reference error norm. Thus, convergence is defined as satisfaction of the condition:
\[
\begin{equation*}
\| \text { error } \|_{n+1}^{(i)} \leq \text { tolerance } \times \| \text { error } \|_{n+1}^{r e f} \tag{3.9-46}
\end{equation*}
\]
where tolerance is the user-specified fraction, and the reference error is defined as:
\[
\begin{equation*}
\|\operatorname{error}\|_{n+1}^{\text {ref }}=\operatorname{MAX}\left(\| \text { error }\left\|_{n+1}^{(1)},\right\| \text { error } \|_{n}^{\text {ref }}\right) \tag{3.9-47}
\end{equation*}
\]

Note that at the first load-step, \(\|\) error \(\|_{0}^{\text {ref }}\) ) is assumed to be zero.
The above convergence criterion can be very sensitive to the user-specified error tolerance. Typically, a value of \(10^{-3}\) is adequate, but for some problems this may be an order of magnitude too large - or even too small (i.e., causing more iterations than are actually needed). More adaptive and robust error tolerances are a recommended topic for future research.

\subsection*{3.9.2.10 Large Rotations}

In problems involving rotational freedoms, e.g., with beam or shell elements, the following modification to equation 3.9-15a is used when the rotation angles become large (say greater than 10 degrees). First, note that the system displacement vector, and its iterative change, are typically partitioned by nodes, i.e.,
\[
\mathbf{d}=\left\{\begin{array}{l}
\mathbf{d}_{\mathbf{1}}  \tag{3.9-48}\\
\mathbf{d}_{\mathbf{2}} \\
\vdots \\
\mathbf{d}_{\text {Nnodes }}
\end{array}\right\}, \quad \delta \mathbf{d}=\left\{\begin{array}{l}
\delta \mathbf{d}_{\mathbf{1}} \\
\delta \mathbf{d}_{\mathbf{2}} \\
\vdots \\
\delta \mathbf{d}_{\text {Nnodes }}
\end{array}\right\}
\]
where Nnodes is the total number of nodes in the problem. At nodes with both translational and rotational freedoms we can further partition:
\[
\mathbf{d}_{A}=\left\{\begin{array}{c}
\mathbf{u}_{A}  \tag{3.9-49}\\
\mathbf{T}_{A}
\end{array}\right\}, \quad \delta \mathbf{d}_{A}=\left\{\begin{array}{c}
\delta \mathbf{u}_{A} \\
\delta \boldsymbol{\theta}_{A}
\end{array}\right\}
\]
in which
\[
\begin{aligned}
\mathbf{u}_{A} & =\text { translation at node } \mathrm{A} \\
\delta \mathbf{u}_{A} & =\text { iterative change in translation at node } \mathrm{A} \\
\mathbf{T}_{\boldsymbol{A}} & =\text { rotation triad at node } \mathrm{A} \\
\delta \boldsymbol{\theta}_{\boldsymbol{A}} & =\text { iterative change in rotation pseudo-vector at node } \mathrm{A}
\end{aligned}
\]

Thus the total displacement, \(\mathbf{d}_{A}\), is represented by the combination of a nodal translation, and a nodal triad that describes the orientation of a "rigid body" attached to the node. The iterative change in displacement, \(\delta \mathbf{d}_{A}\), is represented by an iterative change in translation, and an iterative change in a rotation pseudo-vector. The latter quantity uniquely describes iterative changes in the rotation triad.

With the above definitions, the modified version of equation 3.9-15a at an individual node may be written as follows. For the translational freedoms we simply have:
\[
\begin{equation*}
\mathbf{u}_{A}=\overline{\mathbf{u}}_{\boldsymbol{A}}+\delta \mathbf{u}_{\boldsymbol{A}} \tag{3.9-50}
\end{equation*}
\]
whereas for the rotational freedoms we use:
\[
\begin{equation*}
\mathbf{T}_{\boldsymbol{A}}=\exp \left(\delta \boldsymbol{\theta}_{\boldsymbol{A}}\right) \overline{\mathbf{T}}_{\boldsymbol{A}} \tag{3.9-51}
\end{equation*}
\]
where \(\exp \left(\delta \theta_{A}\right)\) is the exponential of \(\delta \theta_{A}\), which is an orthogonal (rotation) matrix whose rotation angle and direction correspond to the magnitude and direction of the pseudovector \(\delta \theta_{A}\). The following explicit expression for this matrix is known as as "Rodriguez' formula" (see, e.g., ref. 3.2):
\[
\begin{equation*}
\exp (\theta)=\mathbf{I}+\frac{\sin \theta}{\theta} \Theta+\frac{(1-\cos \theta)}{\theta^{2}} \Theta^{2} \tag{3.9-52}
\end{equation*}
\]
where \(\Theta\) is the skew-symmetric matrix corresponding to the pseudo-vector, \(\theta\), i.e.,
\[
\begin{equation*}
\boldsymbol{\Theta} \mathbf{h}=\boldsymbol{\theta} \times \mathbf{h} \tag{3.9-53}
\end{equation*}
\]
for any vector \(h\), so that
\[
\Theta=\left[\begin{array}{ccc}
0 & -\theta_{3} & \theta_{2}  \tag{3.9-54}\\
\theta_{3} & 0 & -\theta_{1} \\
-\theta_{2} & \theta_{1} & 0
\end{array}\right], \quad \theta=\left\{\begin{array}{l}
\theta_{1} \\
\theta_{2} \\
\theta_{3}
\end{array}\right\}
\]
and \(\theta\) is the magnitude of \(\theta\), i.e.,
\[
\begin{equation*}
\theta=\|\theta\|=\sqrt{\theta_{1}^{2}+\theta_{2}^{2}+\theta_{3}^{2}} \tag{3.9-55}
\end{equation*}
\]
where \(\theta_{i}(i=1,2,3)\) are Cartesian components of \(\theta\). Note that the pseudovector, \(\boldsymbol{\theta}\), behaves as a true vector in all ways except for vector addition - since the sum of two arbitrary large rotations is not a vectorial sum (see refs. 3.3or 3.4for the rules of rotation pseudovector addition).

The rotation update formula given by equation 3.9-19 need only be performed at nodes with rotational freedoms. It may also be used to perform incremental updates as well as iterative updates, i.e.,
\[
\begin{equation*}
\mathbf{T}_{\boldsymbol{A}}^{n+1}=\exp \left(\Delta \boldsymbol{\theta}_{\boldsymbol{A}}\right) \mathbf{T}_{\boldsymbol{A}}^{n} \tag{3.9-56}
\end{equation*}
\]

The above relation is employed in the computation of the predictor solutions described by equations 3.9-16 or 3.9-22. For the extrapolated predictor (equation 3.9-22), the extrapolated rotation triads are obtained by: i) extrapolating the rotational components of the displacement vector precisely as indicated by equation 3.9-22a; ii) computing the rotation increments between steps \(n\) and \(n+1\) by subtracting the rotational components of \(d_{n}\) from those of the extrapolated vector, \(\mathrm{d}_{n+1}\); and iii) plugging the corresponding rotationincrements \(\left(\Delta \boldsymbol{\theta}_{A}\right)\) into equation 3.9-56. Note that while the rotation components of the "total" displacement vectors, \(\mathbf{d}_{A}^{n}\) and \(\mathbf{d}_{A}^{n+1}\) are meaningless for large rotations, the difference between these to vectors defines a valid incremental rotation pseudo-vector, \(\Delta \theta_{A}\).

\subsection*{3.9.3 ALGORITHM}

\section*{General Algorithm}
(1) STEP LOOP: for \(\mathrm{n}=2,3,4 \ldots(\) step \(=n+1)\)
(1.1) Extrapolate Solution for Predictor
\[
\text { call EXTRAP }\left(\Delta \ell_{n+1}, \Delta \ell_{n}, \Delta \ell_{n-1} \rightarrow c_{n}, c_{n-1}, c_{n-2}\right)
\]
\(\lambda_{n+1}^{(1)}=c_{n} \lambda_{n}+c_{n-1} \lambda_{n-1}+c_{n-2} \lambda_{n-2}\)
\(\mathbf{d}_{n+1}^{(1)}=c_{n} d_{n}+c_{n-1} d_{n-1}+c_{n-2} d_{n-2}\)
\[
\begin{aligned}
& \Delta \mathrm{d}_{n+1}^{(1)}=\mathbf{d}_{n+1}^{(1)}-\mathbf{d}_{n} \quad\left(\mathbf{T}_{n+1}^{(1)}=\mathbf{R}\left(\Delta \mathbf{d}_{n+1}^{(1)}\right) \mathbf{T}_{n}\right) \\
& \Delta \lambda_{n+1}^{(1)}=\lambda_{n+1}^{(1)}-\lambda_{n}
\end{aligned}
\]
(1.2) Solve for Tangential Displacement based on Predictor
\[
\delta \hat{\mathbf{d}}=\mathbf{K}^{-1}\left(\mathbf{d}_{n+1}^{(1)}\right)\left[\widehat{\mathbf{f}}^{e x t}+\mathbf{K}^{u s} \hat{\mathbf{d}}^{s}\right]
\]
(1.3) Form Residual based on Predictor
\[
\mathbf{r}_{n+1}^{(1)}=\mathbf{r}\left(\mathbf{d}_{n+1}^{(1)}, \lambda_{n+1}^{(1)}\right)=\lambda_{n+1}^{(1)} \widehat{\mathbf{f}}^{e x t}-\mathbf{f}^{i n t}\left(\mathbf{d}_{n+1}^{(1)}\right)
\]
\[
\text { call CHK_CONV }\left(\mathbf{r}_{n+1}^{(1)}, \Delta \mathbf{d}_{n+1}^{(1)}, \epsilon_{r e f} \rightarrow \widehat{\epsilon}^{(1)}, \epsilon_{r e f}\right)
\]
(2) ITERATION LOOP: \(\mathrm{i}=1,2, \ldots\) (iter \(=\mathrm{i}+1=2,3, \ldots\) )
(2.1) Solve for Basic Iterative Displacement Change
\[
\delta \overline{\mathbf{d}}=\mathbf{K}^{-1}\left(\mathbf{d}_{n+1}^{(1)}\right) \mathbf{r}_{n+1}^{(i)}
\]
(2.2) Solve Linearized arc-length Constraint Eqn for New Load Factor
\[
\begin{gathered}
\delta \lambda=\frac{\Delta \ell^{2}-\Delta \mathrm{d}_{n+1}^{(i)} \cdot \Delta \mathrm{d}_{n+1}^{(i)}-2\left(\Delta \mathrm{~d}_{n+1}^{(i)} \cdot \delta \overline{\mathrm{d}}\right)}{2\left(\Delta \mathrm{~d}_{n+1}^{(i)} \cdot \delta \widehat{\mathrm{d}}\right)} \\
\lambda_{n+1}^{(i+1)}=\lambda_{n+1}^{(i)}+\delta \lambda
\end{gathered}
\]
(2.3) Update Displacements
\[
\begin{aligned}
\delta \mathbf{d} & =\delta \overline{\mathbf{d}}+\delta \lambda \delta \hat{\mathbf{d}} \\
\mathbf{d}_{n+1}^{(i+1)} & =\mathbf{d}_{n+1}^{(i)}+\delta \mathbf{d} \quad\left(\mathbf{T}_{n+1}^{(i+1)}=\mathbf{R}(\delta \mathbf{d}) \mathbf{T}_{n+1}^{(i)}\right) \\
\Delta \mathbf{d}_{n+1}^{(i+1)} & =\Delta \mathbf{d}_{n+1}^{(i)}+\delta \mathbf{d}
\end{aligned}
\]
(2.4) Compute New Residual
\[
\mathbf{r}_{n+1}^{(i+1)}=\mathbf{r}\left(\mathbf{d}_{n+1}^{(i+1)}, \lambda_{n+1}^{(i+1)}\right)=\lambda_{n+1}^{(i+1)} \mathbf{f}^{e x t}-\mathbf{f}^{i n t}\left(\mathbf{d}_{n+1}^{(i+1)}\right)
\]
(2.5) Check Convergence
call CHK_CONV ( \(\mathbf{r}_{n+1}^{(i+1)}, \delta \mathbf{d}, \widehat{\epsilon}^{(i)}, \epsilon_{r e f}, \widehat{\epsilon}_{\text {tol }}\), num_div \(\rightarrow\)
\[
\left.\widehat{\epsilon}^{(i+1)},<\text { CONVERGED }>,<\text { DIVERGED }>\right)
\]
if (<CONVERGED>) then
numiters_required \(=\) iter
\(\Delta \ell_{n+2}=\Delta \ell_{n+1}\left(\frac{\text { numiters_desired }}{\text { num_iters_required }}\right)\)
\(n \leftarrow n+1\)
go to (1) STEP LOOP
elseif (<DIVERGED> .or. (iter > maxiters) ) then
if ( num_cuts \(<\) max_cuts) then
\(\Delta \ell_{n+1}=\Delta \ell_{n+1} / 2\) num_cuts \(=\) num_cuts +1 go to (1.1)
else
STOP
endif
else
\(i \leftarrow i+1\)
go to (2) ITER LOOP
endif

\section*{Starting Procedure: Step 1 ( \(\mathbf{n}=\mathbf{0}\) )}

Replace Algorithm Steps (1.1)-(1.2) by:
\[
\begin{aligned}
\mathbf{d}_{1}^{(0)} & =\mathbf{0} \\
\delta \widehat{\mathbf{d}} & =\mathbf{K}^{-1}\left(\mathbf{d}_{1}^{(0)}\right)\left[\widehat{\mathbf{f}}^{e x t}+\mathbf{K}^{u s} \widehat{\mathbf{d}}^{0}\right] \\
\lambda_{1}^{(1)} & \left.=\lambda_{s t a r t} \quad \text { (user specified }\right) \\
\Delta \lambda_{1}^{(1)} & =\lambda_{1}^{(1)} \\
\Delta \ell_{1} & =\Delta \lambda_{1}^{(1)}\|\delta \widehat{\mathbf{d}}\| \\
\Delta \mathbf{d}_{1}^{(1)} & =\Delta \lambda_{1}^{(1)} \delta \widehat{\mathbf{d}} \\
\mathbf{d}_{1}^{(1)} & =\Delta \mathbf{d}_{1}^{(1)}
\end{aligned}
\]
(Also, form \(\mathbf{K}\left(\mathbf{d}_{1}^{(1)}\right)\) before next solve. )

Starting Procedure: Step \(2(n=1)\)
Replace Algorithm Steps (1.1)-(1.2) by:
\[
\begin{aligned}
\mathbf{d}_{2}^{(0)} & =\mathbf{d}_{\mathbf{1}} \\
\delta \widehat{\mathbf{d}} & =\mathbf{K}^{-1}\left(\mathbf{d}_{2}^{(\mathbf{0})}\right)\left[\widehat{\mathbf{f}}^{e x t}+\mathbf{K}^{u \mathbf{s}^{\mathbf{d}}}\right]
\end{aligned}
\]
\[
\begin{aligned}
\Delta \lambda_{2}^{(1)} & =\Delta \ell_{2} /\|\delta \hat{\mathbf{d}}\| \\
\lambda_{2}^{(1)} & =\lambda_{1}+\Delta \lambda_{2}^{(1)} \\
\Delta \mathbf{d}_{2}^{(1)} & =\Delta \lambda_{2}^{(1)} \delta \widehat{\mathbf{d}} \\
\mathbf{d}_{2}^{(1)} & =\mathbf{d}_{1}+\Delta \mathbf{d}_{2}^{(1)} \quad\left(\mathbf{T}_{2}^{(1)}=\mathbf{R}\left(\Delta \mathbf{d}_{2}^{(1)} \mathbf{T}_{1}\right)\right.
\end{aligned}
\]
(But don't reform \(\mathbf{K}\left(\mathbf{d}_{1}^{(1)}\right)\) until step 3.)

CHK_CONV: Procedure to Check Convergence
Input: \(\mathbf{r}, \delta \mathbf{d}, \widehat{\epsilon}^{(i)}, \epsilon_{r e f}, \widehat{\epsilon}_{\text {tol }}\), num_div, iter
Output: \(\widehat{\epsilon}^{(i+1)}\), num_div, <CONVERGED>, <DIVERGED>
(1) Compute Energy Error Norm: \(\boldsymbol{\epsilon}^{(\boldsymbol{i + 1})}=|\mathbf{r} \cdot \delta \mathbf{d}|\)
(2) Normalize: \(\widehat{\epsilon}^{(i+1)}=\sqrt{\frac{\epsilon^{(i+1)}}{\epsilon_{\text {ref }}}}\)
(3) Check Convergence / Divergence:
\[
\begin{aligned}
& \text { if }\left(\hat{\epsilon}^{(i+1)} \leq \hat{\epsilon}_{\text {tol }}\right) \text { then } \\
& \text { <CONVERGED> = TRUE } \\
& \text { else } \\
& \text { if }\left(\widehat{\epsilon}^{(i+1)}>\widehat{\epsilon}^{(i)}\right) \text { then } \\
& \text { num_div }=\text { num_div }+1 \\
& \text { if ( num_div }>1 \text { ) then } \\
& \text { <DIVERGED> = TRUE } \\
& \text { endif } \\
& \text { endif } \\
& \text { endif }
\end{aligned}
\]

Modification for Iteration \(=1(\mathrm{i}=0):\)
(1.5) if (iter \(=1\) ) then
\[
\begin{aligned}
& \text { if }\left(\epsilon^{(1)}>\epsilon_{\text {ref }}\right) \text { then } \\
& \qquad \epsilon_{\text {ref }}=\epsilon^{(1)} \\
& \text { endif }
\end{aligned}
\]
endif

\section*{EXTRAP: Procedure to Compute Quadratic Extrapolation Coefficients}

Input: \(\Delta \ell_{n+1}, \Delta \ell_{n}, \Delta \ell_{n-1}\)
Output: \(c_{n}, c_{n-1}, c_{n-2}\)
\[
\begin{aligned}
\ell_{n-1} & =\Delta \ell_{n-1} \\
\ell_{n} & =\ell_{n-1}+\Delta \ell_{n} \\
\ell_{n+1} & =\ell_{n}+\Delta \ell_{n+1} \\
\Delta \ell_{t o t} & =\ell_{n+1} \cdots \ell_{n-1} \\
c_{n} & =\frac{\left(\ell_{n+1}\right)\left(\Delta \ell_{t o t}\right)}{\left(\ell_{n}\right)\left(\Delta \ell_{n}\right)} \\
c_{n-1} & =-\frac{\left(\ell_{n+1}\right)\left(\Delta \ell_{n+1}\right)}{\left(\ell_{n-1}\right)\left(\Delta \ell_{n}\right)} \\
c_{n-2} & =\frac{\left(\Delta \ell_{n+1}\right)\left(\Delta \ell_{t o t}\right)}{\left(\ell_{n-1}\right)\left(\ell_{n}\right)}
\end{aligned}
\]

\subsection*{3.9.4 PROCEDURE USAGE}

Procedure NL_STATIC_1 may be invoked by the *call directive:
```

*call NL_STATIC_1 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values you wish to give them. The following are valid arguments for procedure NL_STATIC_1; note that those without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline BEGLOAD & -- & Starting load factor ( \(>0\). ) \\
\hline BEG_STEP & -- & Starting step number ( \(>0\) ) \\
\hline MAX_LOAD & -- & Upper bound on load factor \\
\hline MIN_LOAD & -- & Lower_bound on load factor \\
\hline MAX_STEPS & -- & Maximum steps to compute \\
\hline COROTATION & 1 & Corotational Update Option \\
\hline DES_ITERS & 4 & Number of iterations per step desired \\
\hline EXTRAPOLATE & <true> & Perform quadratic extrapolation of solution \\
\hline FAC_STEPS & 1 & Steps_per_refactoring \\
\hline MAX_ITERS & 9 & Maximum iterations per step \\
\hline MAX_CUTS & 3 & Maximum number of successive step cuts \\
\hline NL_GEOM & 2 & Geometric Nonlinearity Level (1 or 2) \\
\hline NOMINAL_DB & NOMINAL. GAL & Results database file \\
\hline NOMINAL_DS & RESPONSE.HISTORY & Results dataset \\
\hline N_SELECT & 0 & Number of nodes for selected disp. output \\
\hline PATH_SCALE & 1. & arc-length scale factor for restarts \\
\hline SEL_NODES & 0 & List of nodes for selected output \\
\hline SEL_DOFS & 0 & Corresponding list of nodal freedoms (1-6) \\
\hline TOL_E & 1. E-3 & Relative error tolerance in energy norm \\
\hline
\end{tabular}

In the above definitions, the term step refers to a load step. The total response is automatically subdivided into load steps, with the starting load factor prescribed by the user - using BEG_LOAD. Subsequent load step sizes are automatically selected by the algorithm, using an arc-length constraint, as described in the theory section.
\begin{tabular}{|l|l|l|l|c|}
\hline \multicolumn{3}{|c|}{ Table 3.9-1 Datasets Input/Output by procedure NL_STATIC_1 } \\
\hline Dataset & Description & Lib & Input & Output \\
\hline <ES_NAME>.EFIL.O.nnod & Element Computational Data & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline ES.SUMMARY.O.nnod & ES Processor Status & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline DEF.<ES_NAME>.0.nnod & Element Defn. (Connectivity) & 1 & \(\sqrt{ }\) & \\
\hline DIR.<ES_NAME>..0.nnod & Element EFIL Directory & 1 & \(\sqrt{ }\) & \\
\hline INC.DISP & System Displacement Vector & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline INT.FORC.step & Nodal Rotation Pseudovectors & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline JDF1.BTAB.1.8 & Model Summary & 1 & \(\sqrt{ }\) & \\
\hline JLOC.BTAB.2.5 & Nodal Coordinates & 1 & \(\sqrt{ }\) & \\
\hline PROP.BTAB.* & Material/Section Properties & 1 & \(\sqrt{ }\) & \\
\hline QJJT.BTAB.2.9 & Nodal Transformations & 1 & \(\sqrt{ }\) & \\
\hline TOT.DISP.step & System Displacement Vector & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline TOT.ROTN.step & System Force Vector & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline
\end{tabular}
where step is the load-step number, and ranges consecutively from 1 to the total number of steps computed.
\begin{tabular}{|l|l|l|}
\hline Table 3.9-2 & Sub-Procedures Invoked by procedure NL_STATIC_1 \\
\hline Procedure & Type & Function \\
\hline NL_STATIC_1 & Internal & Main procedure \\
\hline CHKCONV & Internal & Check convergence \\
\hline DEFNS & Internal & Defines recursive macrosymbols \\
\hline ES & External & Element utility procedure \\
\hline EXTRAP & Internal & Quadratic extrapolation for next load step \\
\hline INITIAL & Internal & Initialize displacements and rotations \\
\hline POSTSTEP & Internal & Print load step summary \\
\hline POSTRESS & Internal & Archive load step data \\
\hline RESIDUAL & Internal & Forms residual-force vector \\
\hline SOLVE & Internal & Solves linear equation systems \\
\hline STIFFNESS & Internal & Forms and factors stiffness matrix \\
\hline TANDIS & Internal & Solves for tangential displacements \\
\hline
\end{tabular}

\subsection*{3.9.5 ARGUMENT DESCRIPTION}

\subsection*{3.9.5.1 BEG_LOAD}

Starting load factor ( \(\lambda_{1}\) ) for the nonlinear analysis. For applied force loading, this factor is multiplied by the reference applied force vector to obtain the starting load vector, i.e.,
\[
\mathbf{f}_{1}^{e x t}=\lambda_{1} \overline{\mathbf{f}}^{e x t}
\]
where \(\overline{\mathbf{f}}^{\text {ext }}\) is the reference applied force vector stored in dataset APPL.FORC.1. For applied displacement loading, the starting load factor is applied to the reference applied displacement vector, which is then used to compute the initial internal force vector, i.e.,
\[
\mathbf{f}_{1}^{i n t(1)}=\mathbf{f}^{i n t}\left(\lambda_{1} \overline{\mathbf{d}}^{e x t}\right)
\]
where \(\overline{\mathbf{d}}^{e x t}\) is the reference applied displacement vector stored in dataset APPL.MOTI.1; Note that this argument is irrelevant for re-start runs (i.e., BEG_STEP \(>1\) ).

\subsection*{3.9.5.2 BEG_STEP}

This argument defines the number of the first step to be computed in a given nonlinear analysis interval. It is important primarily for analysis re-starts. Initially, BEG_STEP should be set to 1 . To continue an analysis in a subsequent run, after having computed and saved " \(n\) " steps in the previous run, one would typically set BEG_STEP equal to " \(n+1\) ". For example, if the 10 th step was successfully completed in the first run, then it could be continued in a second run by setting BEG_STEP \(=11\). However, it is not necessary for BEG_STEP to be larger than any previously computed step. That is, you may re-compute a sequence of steps by setting BEG_STEP to the number of the first step to be re-computed. The procedure will automatically use those steps which immediately precede BEG_STEP (e.g., BEG_STEP-1, BEG_STEP-2 and BEG_STEP-3) to smoothly effect the restart.

\subsection*{3.9.5.3 COROTATION}

Corotational update switch for large-rotation problems (default: <true>). This switch should be set to <true> when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element processor (ESi) section in the CSM Testbed User's Manual (see ref. 3.9-5) for specific guidelines.

\subsection*{3.9.5.4 DEBUG}

Procedure debug switch (default: 〈false>). This switch should only be turned on to obtain additional diagnostic printout for procedure debugging.

\subsection*{3.9.5.5 DES_ITERS}

Desired number of iterations allowed for convergence at a given load step (default=4). This parameter is used to adaptively adjust the arc-length increment from one load step to the next, by comparing DES_ITERS with the actual number of iterations required for convergence at the last step.

\subsection*{3.9.5.6 EXTRAPOLATE}

Solution extrapolation switch (default: <true>). Extrapolation here refers to a technique for predicting the displacement vector and load factor at the beginning of a new load step, by fitting a quadratic curve through the converged solutions at the three previous load steps. It has been found to be a very effective strategy for accelerating traversal of the load-displacement "curve", i.e., far fewer load steps are usually required with extrapolation turned on, than with it turned off. One exception is near very sharp turns in the loaddisplacement curve, where extrapolation may be too smooth to follow the curve, and may have to be temporarily suppressed. (Note: EXTRAPOLATE \(=\langle f a l s e\rangle\) option has not been fully tested.)

\subsection*{3.9.5.7 FAC_STEPS}

Number of load steps between updating (formation and re-factoring) of the stiffness matrix default \(=1\) ). FAC_STEPS \(=n\) implies that re-factoring will be performed every \(n\) steps, starting with the first step of the analysis interval (BEG_STEP). Best results are often obtained by allowing the procedure to re-factor at the beginning of each load step (FAC_STEPS \(=1\) ).

\subsection*{3.9.5.8 MAX_CUTS}

Maximum number of step cuts permitted during the current nonlinear analysis interval (default=3). A step cut refers to a halving of the arc-length increment used to advance the solution from one step to the next. Step cuts are performed only if the maximum number of iterations are exceeded without converging at a given load step. Note that the relationship between the increment in "arc-length" and the increment in the load-factor, \(\lambda\), is computed internally by the procedure.

\subsection*{3.9.5.9 MAX_ITERS}

Maximum number of iterations allowed for convergence at a given load step. This parameter is used to terminate the iteration process at a given load level. If convergence hasn't been obtained after MAX_ITERS iterations, the load (i.e., arc-length) increment is cut in half and the step is repeated - until either convergence has been obtained or Max_CUTS has been exceeded.

\subsection*{3.9.5.10 MAX_LOAD}

Maximum load factor. This sets an upper limit on the load level, and thus provides a convenient way of terminating the arc-length controlled solution algorithm. Since the load factor is actually an unknown in procedure NL_STATIC_1, there is no way of knowing apriori how many load steps will be required to attain a particular load level. The nonlinear analysis is terminated when either MAX_LOAD, MIN_LOAD, MAX_STEPS or MAX_CUTS is exceeded - whichever comes first.

\subsection*{3.9.5.11 MAX_STEPS}

Maximum number of load steps to compute in the current nonlinear analysis run. This provides an implicit limit on analysis run-time. Since the load factor is actually an unknown in procedure HL_STATIC_1 (controlled by the arc-length constraint), there is no way of knowing a-priori how many load steps will be required to attain a particular load level. The nonlinear analysis is thus terminated whenever MAX_STEPS, MIN_LOAD, MAX_LOAD or max_CUTS is exceeded - whichever comes first.

\subsection*{3.9.5.12 MINLOAD}

Minimum load factor. This sets a lower limit on the load level, and thus provides a convenient way of terminating the arc-length controlled solution algorithm. Since the load
factor is actually an unknown in procedure NL_STATIC_1, there is no way of knowing apriori how many load steps will be required to attain a particular load level. The nonlinear analysis is terminated when either MIN_LOAD, MAX_LOAD, MAX_STEPS or MAX_CUTS is exceeded - whichever comes first.

\subsection*{3.9.5.13 NL_GEOM}

Geometric nonlinearity level: 0,1 , or 2 (default \(=2\) ). A value of zero means that the problem is geometrically linear; a value of one means that the geometric nonlinearity will be handled globally (i.e., using corotational updates only); and a value of two means that the nonlinear element strain-displacement relations will be used in addition to any global treatment of geometric nonlinearity. If COROTATION = <true>, options 1 and 2 refer to first-order and second-order corotation, respectively. The latter option can be significantly more accurate than the former for a given finite element model - depending on which element types are involved.

\subsection*{3.9.5.14 NOMINAL_DB}

Name of database (GAL file) where a step-wise history of important solution parameters and selected response variables is to be stored (default = NOMINAL.GAL).

\subsection*{3.9.5.15 NOMINAL_DS}

Name of dataset, within database defined by argument NOMINAL_DB, where a step-wise history of important solution parameters and selected response variables is to be stored (default = RESPONSE. HISTORY). See the CSM Testbed Dataset Manual (ref. 3.9-6), under dataset RESPONSE. HISTORY, for a description of the individual data records stored in this dataset.

\subsection*{3.9.5.16 N_SELECT}

Number of user-selected displacement components to be saved in the dataset specified by argument NOMINAL_DS (default =0). Values for these displacement components, the locations and directions of which are specified by arguments SEL_NODES and SEL_DOFS, respectively, are stored at every load-step.

\subsection*{3.9.5.17 PATH_SCALE}

This floating point number represents a scale factor to be applied to the incremental arclength (or pathlength) used for the first step of an analysis re-start run (default =1.0). If the default (1.0) is used, the arc-length increment from the previous step BEG_STEP-1 will be used for the first step BEG_STEP. Note that this may lead to a different load-step size than if the analysis had continued to step BEG_STEP without a re-start. To eliminate this difference, the user can set:
```

[PATH_SCALE] = [DES_ITERS] / act_iters

```
where "actiters" is the actual number of iterations required for convergence at step [BEG_STEP]-1.

\subsection*{3.9.5.18 SEL_DOFS}

List of nodal degrees-of-freedom at which displacement histories are to be saved in dataset NOMINAL_DS (default \(=1.0\) ). There should be N_SELECT numbers in the list, in correspondence with the node numbers specified by argument SEL_NODES. Values of each number in the list must range between 1 and 6 , in correspondence to the nodal degree-of-freedom sequence (e.g., \(u, v, w, \theta_{x}, \theta_{y}, \theta_{z}\) ) specified by the START command of processor TAB.

\subsection*{3.9.5.19 SEL_HODES}

List of node numbers at which displacement histories are to be saved in dataset NOMINAL_DS (default \(=0\) ). There should be \(\mathbb{N}_{\text {sELECT }}\) numbers in the list, and node numbers can be repeated if more than one nodal degree-of-freedom is to be saved at a node. The corresponding nodal degree-of-freedom for each entry is specified by argument SEL_DOFS.

\subsection*{3.9.5.20 TOL_}

Error tolerance used to establish convergence of the nonlinear equilibrium iteration procedure at each load step (default =1.e-3). The iteration loop at a given step is terminated whenever the following condition is met:
\[
\epsilon \leq[\text { TOL_E }]
\]
where
\[
\epsilon=\sqrt{\frac{\mathbf{r}^{(i)} \cdot \delta \mathbf{d}^{(i)}}{\mathbf{r}^{(1)} \cdot \delta \mathbf{d}^{(1)}}}
\]
is the relative energy error norm, \(r\) is the residual force vector, \(\delta \mathrm{d}\) is the iterative displacement change, and \(i\) is the iteration counter.

\subsection*{3.9.6 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
NL_STABIL_1 & (main procedure) \\
DEFNS & (define recursive macrosymbols) \\
INITIAL & (initial displacements and rotations) \\
ES & (initialize element data) \\
EXTRAP & (quadratic extrapolation for next load step) \\
STIPFNESS & (form and form stiffness matrix) \\
TANDIS & (solve for tangential displacements) \\
SOLVE & (solve linear system of equations) \\
RESIDUAL & (form residual-force vector) \\
ES & (calculate residual) \\
CHKCONV & (check convergence) \\
POSTSTEP & (print load step summary) \\
POSTRESS & (archive load step data)
\end{tabular}

\subsection*{3.6.7 LIMITATIONS}

\subsection*{3.9.7.1 Number of Database Libraries}

All analysis (computational) data is assumed to be resident on a single database library (i.e., file), and that file is expected to be attached to logical device index 1 before calling procedure NL_STATIC_1. Additionally, important analysis statistics and re-start parameters, as well as selected post-processing data, will be deposited in a separate data library, which is automatically opened by procedure NL_STATIC_1 on logical device index 3. The name of this secondary library is user-specified using procedure argument NOMINAL_DB, which has the default setting: NOMINAL_DB = NOMINAL.GAL.

\subsection*{3.9.7.2 Element Types}

Only shell elements have been tested thus far with procedure NL_STATIC_1. While the procedure is potentially compatible with beam and solid elements too, minor modifications to the generic element processor may be required to handle geometric nonlinearity for these elements.

\subsection*{3.9.7.3 Number of Load/Constraint Systems}

Only one set of loads and constraints is accommodated by procedure NL_STATIC_1. Furthermore, they must be referred to as load set 1 and constraint set 1 in the database.

\subsection*{3.9.7.4 Specified Rotations}

Specified (non-zero) rotational freedoms are currently not implemented in procedure NL_STATIC_1 - unless rotation angles remain moderately small (i.e., less than 10 degrees). For larger rotations, the specification of rotation components constitutes a nonlinear constraint, which must be translated into the motion of nodal rotation triads, and requires a modification to the linearized equilibrium equations. This capability is planned for a future version of procedure NL_STATIC_1.

\subsection*{3.9.7.5 Material Nonlinearity}

Only geometric nonlinearity is accounted for by procedure NL_STATIC_1. However, this limitation is really due to current limitations within the generic element processor; the global nonlinear solution algorithm doesn't particularly care about the source of the nonlinearity, as long as it is properly represented by the tangent stiffness matrix and the residual force vector.

\subsection*{3.9.7.6 Re-Starting from Step 1}

It is currently not permitted to re-start the analysis from step 1 (i.e., re-run the problem from the beginning) unless you either: i) delete the database and recreate the model, or ii) *enable the original APPL.MOTI and APPL.FORC datasets. The reason for this is that the original APPL.MOTI and APPL.FORC datasets are copied into new datasets - and marked for deletion - by procedure NL_STATIC_1 whenever BEG_STEP \(=1\). This limitation will be removed in the next version of NL_STATIC_1.

\subsection*{3.9.7.7 EXTRAPOLATE Must be Turned On}

Extrapolation is the only form of load/displacement step prediction that has been thoroughly tested. Without extrapolation, procedure NL_STATIC_1 is supposed to use the arclength constraint equation to generate a predictor solution (see theory section), and use information regarding the sign of the stiffness determinant to determine the load direction (increasing or decreasing) between one step and the next. However, the no-extrapolation option has not yet been quality assured. Note that the extrapolation option is the recommended approach anyway.

\subsection*{3.9.7.8 True-Newton Iteration}

Only modified Newton/Raphson iteration is provided by the current version of procedure NL_STATIC_1. This means that the stiffness matrix is re-formed and re-factored only at the beginning (first iteration) of every FAC_STEPS load steps (where FAC_STEPS \(=1\) by default). In the next version, we plan to implement the option for true Newton/Raphson iteration, in which the stiffness matrix can be updated at each iteration of selected load steps. This option can be useful for problems with limit points that are nearly as sharp as bifurcation points.

\subsection*{3.9.7.9 Constant Load-Increments}

Currently, all load increments (except the first one) are computed automatically by procedure NL_STATIC_1, using the arc-length constraint equation. Therefore, it is not possible for the user to fix the load increment, as is done in conventional load-controlled algorithms. Since this option may be useful for benchmarking (and research) purposes, we plan to include it in a future version of the procedure, wherein the arc-length constraint equation will be selectively bypassed.

\subsection*{3.9.7.10 Singularities due to Limit Points and Bifurcations}

Procedure NL_STATIC_1 cannot handle singularities in the stiffness matrix that arise when the load-stepping algorithm lands too close to a limit point, or attempts to traverse a bifurcation point. (Note: Singularities due to limit points are overcome by procedure NL_STATIC_2.)

\subsection*{3.9.8 ERROR MESSAGES AND WARNINGS}

\subsection*{3.9.8.1 "Non-Convergence at Step n. Revise Strategy."}

This message means that the maximum number of nonlinear iterations (MAX_ITERS) has been exhausted, as well as the maximum number of step cuts (MAX_CUTS), and convergence still hasn't been obtained at step \(n\). A possible cure is to re-start the analysis from several steps back, and decrease the arc-length increment at that point (using the PATH_SCALE argument). However, just increasing MAX_ITERS or MAX_COTS, or even TOL_E, may also solve the problem. In other words, re-think the definition of all solution parameters based on the observed behavior of the solution algorithm just prior to the break-down.

\subsection*{3.9.8.2 "Divergence at Step n. Revise Strategy."}

This message has similar implications to the previous message, but it occurs when the error grows instead of decreases during two successive nonlinear iterations. The difference between divergence and non-convergence is that divergence cannot be cured by increasing MAX_ITERS; and probably should not be "cured" by increasing TOL_E. It generally means that the step-size is too big - or that the error tolerance (TOL_E) has been too big all along, so that changes are occurring suddenly that should have been detected by the solution algorithm at earlier load steps. Thus, you might try re-starting from an earlier step, reducing PATH_INC, and possibly reducing TOL_E as well.

\subsection*{3.9.8.3 "Specified Displacements are Identically Zero"}

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed - in which case the message should be taken merely as a warning.

\subsection*{3.9.8.4 "Specified Forces are Identically Zero"}

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed - in which case the message should be taken merely as a warning.

\subsection*{3.9.9 USAGE GUIDELINES AND EXAMPLES}

Procedure NL_STATIC_1 may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*cal1 ML_STATIC_1 ( --
beg_step =1 ; -- . Starting step number (>0)
max_steps=1 ; -- . Maximum steps to compute
max_iters=9 ; -- . Maximum iterations per step
des_iters=4 ; -- . Number of iterations desired
fac_steps=1 ; -- . Steps_per_refactoring
max_cuts=3 ; -- . Maximum number of step cuts
tol_e=1.E-3 ; -- . Energy error tolerance
beg_load ; -- . Starting load factor (>0.)
max_load ; -- . Upper_bound on load factor
min_load ; -- . Lower_bound on load factor
path_scale=1.; -- . Path_inc scl_factor (restart)
extrapolate=<true> ; --
line_search=1.;-- . Initial line-search parameter
debug=<FALSE>; -- . Debug_print smitch
NL_GEOM = 2 ; -- . Geom. Nonlin. Level (1|2)
COROTATION=1 ; -- . Corotational Flag (leave on!!)
Nominal_DB = NOMINAL.GAL ; -- . Selected Output
Nominal_DS = RESPONSE.HISTORY ; --
N_SELECT ; SEL_NODES; SEL_DOFS )

```

\subsection*{3.9.9.1 Starting an Analysis}

To begin a nonlinear static analysis with procedure NL_STATIC_1, it is only necessary that the finite element model be defined. This does not require pre-formation of element stiffness matrices, node renumbering for optimal factorization time, or any form of linear analysis (unless initial geometric imperfections are based on linear displacement modes). Only nodal coordinates/transformations, material properties and element connectivity are prerequisite to nonlinear analysis. To invoke procedure NL_STATIC_1, only those arguments that don't have default values (see procedure usage section) need be specified.

For example, suppose you wanted to start an analysis with an initial load-factor of .1 , a maximum load-factor of 1 ., a minimum load-factor of 0 ., and compute no more than 20 load-steps. You could then invoke the procedure as follows:
```

*call NL_STATIC_1 ( BEG_STEP = 1 ; MAX_STEPS = 20 ; --
BEG_LOAD = .1 ; MAX_LOAD = 1. ; MIN_LOAD = 0. )

```

Keep in mind that the number of load-steps actually performed during the above run will depend on the number of adaptively-sized arc-length increments needed to attain the maximum load level. Since it may be difficult to estimate this in advance, you may want to start with only a few load-steps (e.g., set MAX_STEPS \(=3\) ) to get some experience, and later re-start the analysis with more steps allowed.

\subsection*{3.9.9.2 Re-Starting (or Continuing) an Analysis}

To re-start an analysis from a previously computed, converged solution, you need only specify the first step to compute as argument BEG_STEP. If the EXTRAPOLATE argument is activated (which is the default), the three solution steps immediately preceding the one you wish to compute must be resident on the database. If the EXTRAPOLATE argument is turned off, only one preceeding solution step is required. Thus, to continue an analysis that has already produced ten load steps, you could issue the call:
```

*call NL_STATIC_1 ( BEG_STEP = 11; MAX_STEPS = 100 ; --
MAX_LOAD = 1. ; MIN_LOAD = 0. )

```

Note that the argument BEG_LOAD is not necessary for a continuation (or re-start) run; the new load level is automatically computed using the preceeding value of the arc-length increment. However, you can modify the new increment, by using the PATH_SCALE argument, which is a scale factor applied to the previous arc-length increment to generate the new increment. The default value of Path_SCALE is 1.0.

Furthermore, on analysis continuations/restarts, you are free to modify any of the other solution parameters (i.e., procedure arguments). For example, you may want to increase MAX_ITERS, reduce TOL_E, or even change DES_ITERS. The default values for these solution parameters are not suitable for all problems; they are useful primarily for gaining experience by trial and error.

\subsection*{3.9.10 PROCEDURE LISTING}
```

. =DECK NL_STATIC_1
*procedure NL_STATIC_1 ( --
beg_step =1 ; -- . Starting step number (>0)
max_steps=1 ; -- . Maximum steps to compute
max_iters=9 ; -- . Maximum iterations per step
des_iters=4 ; -- . Number of iterations desired
fac_steps=1 ; -- . Steps_per_refactoring
max_cuts=3 ; -- . Maximum number of step cuts
tol_e=1.E-3 ; -- . Energy error tolerance
beg_load ; -- . Starting load factor (>0.)
max_load. ; -- . Upper_bound on load factor
min_load ; -- . Lover_bound on load factor
path_scale=1.; -- . Path_inc scl_factor (restart)
extrapolate=<true> ; --
line_search=1.;-- . Initial line-search parameter
debug=<FALSE>; -- . Debug_print sषitch
HL_GEOM = 2 ; -- . Geom. Nonlin. Level (1|2)
COROTATION=1 ; -- . Corotational Flag (leave on!!)
Nominal_DB = NOMINAL.GAL ; -- . Selected Dutput
Nominal_DS = RESPONSE.HISTORY ; --
N_SELECT ; SEL_NODES; SEL_DOFS --
)
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
*Remark
|-----------------------------------------------------------------
NL_STATIC_1
CSM Testbed Procedure for Monlinear Statics:

- Corotational Nerton/Raphson algorithm
- Linearized Crisfield/Riks arc-length control
- Applied forces and/or displacements
Authors: G.M. Stanley and C.C. Rankin
Version: MAR-03-1988
*Remark

```

\subsection*{3.9.11 REFERENCES}
3.9-1. Crisfield, M. A.: "A Fast Incremental/Iterative Solution Procedure that Handles Snap-Through." Computers and Structures, Vol. 13, 1983, pp. 55-62.
3.9-2. Kane, T. R.; Likins, P. W.; and Levinson, D. A.: Spacecraft Dynamics, McGrawHill Book Co., New York, 1983.
3.9-3. Argyris, J. H.: "An Excursion into Large Rotations." International Journal for Numerical Methods in Engineering, Vol. 32, 1982, pp. 85-155.
3.9-4. Rankin, C. C. and Brogan, F. A.: "An Element-Independent Corotational Procedure for the Treatment of Large Rotations." In Collapse Analysis of Structures, edited by Sobel, L.H. and Thomas, K., ASME, New York, 1984, pp. 85-100.
3.9-5. Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
3.9-6. Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

\subsection*{3.10 Procedure NL_STATIC_2}

\subsection*{3.10.1 GENERAL DESCRIPTION}

NL_STATIC_2 is a modification to NL_STATIC_1 Riks arclength strategy that allows solution of a limit point problem in the immediate neighborhood of a critical point. Developed and written by C. C. Rankin in consultation with E. Riks, this modified algorithm avoids the singularity in the stiffness matrix at the critical point, thereby permitting a smooth continuation of the solution even when a solution point coincides exactly with the critical point. NL_STATIC_2 is preferred over NL_STATIC_1 whenever solution points are desired very near the critical area, or when the singularity of the stiffness is likely to persist over some distance along the solution path. In the absence of numerical difficulties, however, NL_STATIC_1 and NL_STATIC_2 produce identical results.

\subsection*{3.10.2 PROCEDURE USAGE}

Procedure NL_STATIC_2 may be invoked by the *call directive:
```

*call NL_STATIC_2 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values you wish to give them. The following are valid arguments for NL_STATIC_1; note that those without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline BEG_LOAD & - & Starting load factor ( \(>0\). \\
\hline BEG_STEP & - & Starting step number ( \(>0\) ) \\
\hline MAX_LOAD & - & Upper_bound on load factor \\
\hline MIN_LOAD & - & Lower_bound on load factor \\
\hline MAX_STEPS & - & Maximum steps to compute \\
\hline COROTATION & 1 & Corotational Update Option \\
\hline DES_ITERS & 4 & Number of iterations per step desired \\
\hline EXTRAPOLATE & <true> & Perform quadratic extrapolation of solution \\
\hline FAC_STEPS & 1 & Steps_per_refactoring \\
\hline MAX_ITERS & 9 & Maximum iterations per step \\
\hline MAX_CUTS & 3 & Maximum number of successive step cuts \\
\hline NL_GEOM & 2 & Geometric Nonlinearity Level (1 or 2) \\
\hline NOMINAL_DB & NOMINAL.GAL & Results database file \\
\hline NOMINAL_DS & RESPONSE.HISTORY & Results dataset \\
\hline N.SELECT & 0 & Number of nodes for selected disp. output \\
\hline PATH_SCALE & 1. & Arclength scale factor for restarts \\
\hline SEL_NODES & 0 & List of nodes for selected output \\
\hline SEL_DOFS & 0 & Corresponding list of nodal freedoms (1-6) \\
\hline TOL_E & 1.E-3 & Relative error tolerance in energy norm \\
\hline ADV_RIKS & <false> & If true, advanced Riks; else, do NL_STATIC_ \\
\hline
\end{tabular}

\subsection*{3.10.3 ARGUMENT GLOSSARY}

The only additional argument that NL_STATIC_2 has is ADV_RIKS. All other arguments are identical in name and function as their counterparts in NL_STATIC_1.

\subsection*{3.10.3.1 ADV_RIKS}

This is a logical parameter, that, when set to <true>, invokes the advanced Riks option. Otherwise, NL_STATIC_2 reduces to NL_STATIC_1.

\subsection*{3.10.4 INPUT/OUTPUT DATASETS}

The input/output requirements of NL_STATIC_2 are identical to NL_STATIC_1.

\subsection*{3.10.5 SUB-PROCEDURES AND PROCESSORS}

Table 3.10-2 Sub-Procedures Invoked by Procedure NL_STATIC_2
\begin{tabular}{|l|l|l|}
\hline Procedure & Type & Function \\
\hline NL_STATIC_2 & Internal & Main Procedure \\
\hline CHK_CONV & Internal & Check convergence \\
\hline DEFNS & Internal & Defines recursive macrosymbols \\
\hline ES & External & Element utility Procedure \\
\hline FACT_STIFF & Internal & Factors Stiffness Matrix \\
\hline FORM_STIFF & Internal & Forms Stiffness Matrix \\
\hline RESIDUAL & Internal & Forms residual-force vector \\
\hline SOLVE & Internal & Solves linear equation systems \\
\hline STIF_COLMN & Internal & Fixes Freedom \(I\), Extracts Stiffness Col. \(I\) \\
\hline TWO_BY_TWO & Internal & Computes Advanced Riks Reduced Coefficients \\
\hline
\end{tabular}
\begin{tabular}{|l|l|l|}
\hline Table 3.10-3 Processors Invoked by Procedure NL_STATIC_2 \\
\hline Procedure & Type & Function \\
\hline AUS & Internal & Extracts column I of Stiffness \\
\hline E & Internal & Initializes EFIL datasets \\
\hline ESi & External & Element Processors based on GEP \\
\hline INV & Internal & Factors stiffness matrix \\
\hline SSOL & Internal & Solves linear equation systems \\
\hline VEC & Internal & Performs all vector/pseudo-vector algebra \\
\hline
\end{tabular}

\subsection*{3.10.6 LIMITATIONS}

NL_STATIC_2 has the all the limitations that are listed in Section 4.1.6. However, whereas numerical difficulties can be expected with NL_STATIC_1 near a critical point, no difficulties whatsoever should be expected with NL_STATIC_2 near limit (as opposed to bifurcation points). There are two additional software limitations described in the next two subsections.

\subsection*{3.10.6.1 AUS Limitation}

Due to hard wired data set naming conventions in processor AUS for system matrices (e.g. K.SPAR.36), the number of DOF's per node specified on the START command of processor TAB is presently restricted to be 6. AUS is currently essential to NL_STATIC_ 2 for computing the product of the stiffness with an elementary vector to extract row \(I\) of the stiffness matrix. This restriction will be removed when we make the connection to the Generic Matrix Processor.

\subsection*{3.10.6.2 First Two Steps}

Because of the way the extrapolation is set up, NL_STATIC_2 operates as NL_STATIC_1 for the first two steps for a new (not restart) analysis. This limitation is not important, since it is highly unlikely that a critical point will be reached at the very beginning of a solution sequence.

\subsection*{3.10.7 ERROR MESSAGES}

All error messages have the same meaning as in NL_STATIC_1 (section 4.1.7).

\subsection*{3.10.8 USAGE GUIDELINES AND EXAMPLES}

As they are identical to NL_STATIC_1, please consult section 4.1.8 for usage guidelines.

\subsection*{3.10.9 THEORY}

\subsection*{3.10.9.1 Introduction}

Procedure NL_STATIC_2, like NL_STATIC_1, performs a quasi-static analysis of a system of nonlinear equilibrium equations using an adaptive arclength-controlled Newton/Raphson incremental/iterative solution algorithm. The function of the arclength constraint, the stepsize selection, and convergence criteria are identical to NL_STATIC_1. Because almost all of the theory underlying NL_STATIC_2 is covered in Section 4.1.9, only the matrix partitioning and pivoting process that avoids the factoring of a singular or near singular stiffness matrix is covered here.

\subsection*{3.10.9.2 The Block Pivot Strategy}

The difficulties that occur in NL_STATIC_1 can be readily seen by examining Eq. (8).
\[
\begin{align*}
\overline{\mathbf{K}} \delta \mathbf{d} & =? ? ? r b b o l d+\delta \lambda \widehat{\mathbf{f}}^{e x t}  \tag{3.10-1}\\
2 \Delta \overline{\mathbf{d}} \cdot \delta \mathbf{d} & =\overline{\mathbf{c}}
\end{align*}
\]
where \(\overline{\mathbf{r}}\) is the residual, \(\widehat{\mathbf{f}}^{e x t}\) is the external load, \(\overline{\mathbf{c}}\) is the arclength parameter, and \(\delta \overline{\mathbf{d}}\) is the desired displacement increment. Clearly, if \(\bar{K}\) is singular, we will have a problem in solving this pair of equations. For limit points, however, the extended equation system containing the constraint (second of (57)) is non-singular. A simple and robust method of overcoming the singularity is to select out the equation for a particular freedom and treat it the same way as the constraint equation, solving three rather than two sets of equations, as illustrated by the following
\[
\left[\begin{array}{ccc}
\widehat{\mathbf{K}} & \widehat{\mathbf{f}}^{I} & -\mathbf{f}^{e x t}  \tag{3.10-2}\\
(\widehat{\mathbf{f}})^{T} & K_{I I} & -f_{I}^{e x t} \\
\widehat{\mathbf{c}} & \boldsymbol{c}_{I} & 0
\end{array}\right]\left[\begin{array}{c}
\delta \widehat{\mathrm{d}} \\
\delta d_{I} \\
\delta \lambda
\end{array}\right]=\left[\begin{array}{c}
\widehat{\mathbf{r}} \\
r_{I} \\
\bar{c}
\end{array}\right]
\]
where \(\widehat{\mathbf{K}}\) is the stiffness matrix with row and column \(I\) removed. The hats over vectors also indicate that row \(I\) has been deleted. \(\widehat{f}\) is column \(I\) of the stiffness, with \(K_{I I}\) being the diagonal element for freedom \(I\). The same partitioning also applies to the external force \(f^{e x t}\) and the constraint equation \(c\).
If we formally solve the first of (58) for \(\delta \hat{d}\) and substitute the result into the remaining two equations, we obtain the following two-by-two nonsymmetric system of equations for \(\delta d_{I}\) and \(\delta \lambda\) :
\[
\left[\begin{array}{cc}
K_{I I}-\left(\mathbf{f}^{I}\right)^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{I} & (\mathbf{f})^{T} \widehat{\mathbf{K}}^{-1} \mathbf{f}^{e x t}-f_{I}^{e x t}  \tag{3.10-3}\\
c_{I}-\widehat{\mathbf{c}}^{T} \widehat{\mathbf{K}}^{-1} \mathbf{f}^{I} & \widehat{\mathbf{c}}^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{f}}^{e x t}
\end{array}\right]\left[\begin{array}{l}
\delta d_{I} \\
\delta \lambda
\end{array}\right]=\left[\begin{array}{c}
r_{I}-\left(\widehat{\mathbf{f}}^{I}\right)^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{r}} \\
\overline{\mathbf{c}}-\widehat{\mathbf{c}}^{T} \widehat{\mathbf{K}}^{-1} \widehat{\mathbf{r}}
\end{array}\right]
\]

One additional forward/backsolve is required with this algorithm. After each factoring of the stiffness matrix, one must solve the pair
\[
\begin{align*}
\widehat{\mathbf{K}} \delta \hat{\mathbf{v}} & =\widehat{\mathbf{f}}^{\prime} \\
\widehat{\mathbf{K}} \delta \hat{\mathbf{w}} & =\widehat{\mathbf{f}}^{e x t} \tag{3.10-4}
\end{align*}
\]
for vector \(\delta \hat{\mathbf{v}}\) and \(\delta \widehat{w} . \delta \widehat{w}\) corresponds to \(\delta \hat{\mathbf{d}}\) in the second of (11). \(\delta \hat{\mathbf{d}}\) is also used for \(\delta \widehat{\mathbf{w}}\) in the description of the NL_STATIC_ 2 algorithm. The following vector must be solved every iteration:
\[
\begin{equation*}
\widehat{\mathbf{K}} \widehat{\mathbf{u}}=\widehat{\mathbf{r}} \tag{3.10-5}
\end{equation*}
\]

This equation corresponds to the first of (11). The two-by-two system (59) becomes
\[
\begin{align*}
{\left[\begin{array}{cc}
K_{I I}-(\widehat{\mathbf{f}})^{T} \delta \widehat{\mathbf{v}} & \left(\mathbf{f}^{I}\right)^{T} \delta \widehat{\mathrm{w}}-f_{I}^{e x t} \\
c_{I}-\widehat{\mathbf{c}}^{T} \delta \widehat{\mathrm{v}} & \widehat{\mathbf{c}}^{T} \delta \widehat{\mathrm{w}}
\end{array}\right]\left[\begin{array}{l}
\delta d_{I} \\
\delta \lambda
\end{array}\right]=} & {\left[\begin{array}{c}
r_{I}-\left(\mathbf{f}^{I}\right)^{T} \widehat{\mathbf{u}} \\
\overline{\mathrm{c}}-\widehat{\mathbf{c}}^{T} \widehat{\mathbf{u}}
\end{array}\right] }  \tag{3.10-6}\\
& {\left[\begin{array}{ll}
A_{11} & A_{12} \\
A_{21} & A_{22}
\end{array}\right]\left[\begin{array}{l}
\delta d_{I} \\
\delta \lambda
\end{array}\right]=\left[\begin{array}{l}
R_{1} \\
R_{2}
\end{array}\right] }
\end{align*}
\]

We have rewritten the first of (62) with the notation used in the description of the algorithm, where the coefficients \(A_{i j}\) and \(R_{i}\) are the reduced Riks coefficients and residuals, respectively; a comparison of the first of (62) with the second yields their values.

Once \(\delta d_{I}\) and \(\delta \lambda\) are known, the full solution becomes the sum
\[
\begin{equation*}
\widehat{\delta} \mathbf{d}=\widehat{\mathbf{u}}-\delta d_{I} \delta \widehat{\mathbf{v}}+\delta \lambda \delta \widehat{\mathbf{w}} \tag{3.10-7}
\end{equation*}
\]
\(\delta \hat{\mathbf{d}}\) is then expanded by one freedom and the explicit value \(\delta \mathrm{d}_{I}\) previously solved for is inserted. The advantage of (62) is that this system, in contrast to (8) is never singular at a limit point, provided that the component \(I\) does not correspond to a zero entry in the tangent displacement vector at the critical point.

\subsection*{3.10.9.3 Selecting Freedom \(I\) and the Vector \(\widehat{f}^{I}\)}

A simple method for ensuring a nonsingular reduced stiffness \(\widehat{\mathbf{K}}\) is to look at the difference between the last converged solution and the predicted solution for the current step. We choose that particular component with the largest absolute value; its index becomes \(I\), and the stiffness column belonging to that freedom becomes \(\vec{f}^{I}\) with diagonal \(K_{I I}\). In practice, after we have selected the proper index, we generate an elementary vector that is zero except for unity in position \(I . \mathbf{f}^{I}\) is just the product of the stiffness matrix with the elementary vector. \(\mathbf{f}^{I}\) is this same column with row \(I\) deleted.

\subsection*{3.10.9.4 Constructing the Solution}

Immediately after the stiffness matrix has been factored, we solve ( 60 ) for \(\delta \hat{\mathbf{v}}\) and \(\delta \widehat{w}\). Solution for \(\delta \hat{\mathbf{w}}\) is treated like the corresponding solution for \(\delta \mathbf{d}\) in (37), with specified displacements being handled exactly as in NL_STATIC_1. The only difference is that the new stiffness has one additional freedom held fixed. In practice, entry \(I\) is added to the specified displacement list (and if \(I\) has changed since the last step, the previous freedom is "released" or "unfixed"). The solutions \(\delta \widehat{v}, \delta \widehat{w}\) are full system vectors with a zero in the Ith slot. At each iteration, a new basic displacement increment \(\widehat{\mathbf{u}}\) is also solved for (62). After solution of the reduced two-by-two system (62), (63) is used to construct the full displacement increment. This is followed by direct insertion of the increment for component \(I\).

\subsection*{3.10.9.5 Computing the Stiffness Determinant}

The determinant of the stiffness \(\widehat{\mathbf{K}}\) is not equal to that of the original, unconstrained stiffness. However, since our algorithm is a special case of a block Gauss elimination, it is a simple matter to compute it. The full determinant of the stiffness matrix is the product
\[
\begin{equation*}
\operatorname{Det}(\mathbf{K})=\operatorname{Det}(\widehat{\mathbf{K}}) A_{\mathbf{1 1}} \tag{3.10-8}
\end{equation*}
\]

Note that when \(A_{11}\) vanishes, the stiffness determinant also vanishes. However, the system (62) is still nonsingular whenever the off diagonal reduced coefficients are nonzero (the extended system).

\subsection*{3.10.10 ALGORITHM ̄ FLOW CHART}

\section*{General Algorithm}
(1) STEP LOOP: \(\mathrm{n}=2,3,4 \ldots\) (step \(=\mathrm{n}+1\) )
(1.1) Extrapolate Solution for Predictor
\[
\text { call EXTRAP }\left(\Delta \ell_{n+1}, \Delta \ell_{n}, \Delta \ell_{n-1} \rightarrow c_{n}, c_{n-1}, c_{n-2}\right)
\]
\[
\lambda_{n+1}^{(1)}=c_{n} \lambda_{n}+c_{n-1} \lambda_{n-1}+c_{n-2} \lambda_{n-2}
\]
\[
\mathbf{d}_{n+1}^{(1)}=c_{n} \mathbf{d}_{n}+c_{n-1} \mathbf{d}_{n-1}+c_{n-2} \mathbf{d}_{n-2}
\]
\(\Delta \mathrm{d}_{n+1}^{(1)}=\mathbf{d}_{n+1}^{(1)}-\mathbf{d}_{n} \quad\left(\mathbf{T}_{n+1}^{(1)}=\mathbf{R}\left(\Delta \mathbf{d}_{n+1}^{(1)}\right) \mathbf{T}_{n}\right)\)
\(\Delta \lambda_{n+1}^{(1)}=\lambda_{n+1}^{(1)}-\lambda_{n}\)
(1.2) Form and Assemble Stiffness
(1.3) Find Index of Largest Tangent Component

Extract Column \(I\) from Stiffness (including diagonal)
\[
\begin{aligned}
I & =\operatorname{Arg}\left\{\max _{\forall k}\left|\Delta \mathrm{~d}(k)_{n+1}^{(1)}\right|\right\} \\
\widehat{\mathbf{f}}^{I} & =\mathbf{K e}_{I}
\end{aligned}
\]
(1.4) Fix freedom \(I\) to give constrained \(\mathbf{K}\) ( \(\widehat{\mathbf{K}}\) )
(1.5) Solve for Tangential Displacement based on Predictor
\[
\delta \hat{\mathbf{d}}=\widehat{\mathbf{K}}^{-1}\left(\mathbf{d}_{n+1}^{(1)}\right)\left[\widehat{\mathbf{f}}^{\mathrm{ext}}+\mathbf{K}^{u s} \hat{\mathbf{d}}^{2}\right]
\]
(1.6) Solve for perturbation displacement \(\delta \hat{\mathbf{v}}\)
\[
\delta \widehat{\mathbf{v}}=\widehat{\mathbf{K}}^{-1}\left(\mathbf{d}_{n+1}^{(1)}\right) \widehat{\mathbf{f}}^{I}
\]
(1.7) Solve for Risks reduced system coefficients
\[
\begin{aligned}
& \delta \widehat{v}_{I}=0 . \\
& \delta \widehat{\mathbf{d}}_{I}=0 . \\
& A_{11}=\widehat{\mathbf{f}}_{I}^{I}-\widehat{\mathbf{f}}^{I} \cdot \delta \widehat{\mathrm{v}} \\
& A_{12}=-\widehat{\mathbf{f}}_{I}^{\text {ext }}+\widehat{\mathbf{f}}^{I} \cdot\left(\delta \widehat{\mathbf{d}}-\widehat{\mathbf{d}}^{\mathbf{a}}\right) \\
& A_{21}=2\left(\Delta \mathrm{~d}(I)_{n+1}^{(1)}-\Delta \mathbf{d}_{n+1}^{(1)} \cdot \delta \widehat{\mathrm{v}}\right) \\
& A_{22}=2 \Delta \mathbf{d}_{n+1}^{(1)} \cdot \delta \widehat{\mathrm{d}}
\end{aligned}
\]
(1.7) Form Residual based on Predictor
\(\mathbf{r}_{n+1}^{(1)}=\mathbf{r}\left(\mathbf{d}_{n+1}^{(1)}, \lambda_{n+1}^{(1)}\right)=\lambda_{n+1}^{(1)} \widehat{\mathbf{f}}^{\mathbf{e x t}}-\mathbf{f}^{\mathrm{int}}\left(\mathbf{d}_{n+1}^{(1)}\right)\)
call CHK_CONV ( \(\left.\mathbf{r}_{n+1}^{(1)}, \Delta \mathbf{d}_{n+1}^{(1)}, \epsilon_{\text {ref }} \rightarrow \widehat{\epsilon}^{(1)}, \epsilon_{\text {ref }}\right)\)
(2) ITERATION LOOP: \(\mathrm{i}=1,2, \ldots\) (iter \(=\mathrm{i}+1=2,3, \ldots\) )
(2.1) Solve for Basic Iterative Displacement Change
\[
\delta \overline{\mathbf{d}}=\widehat{\mathbf{K}}^{-1}\left(\mathbf{d}_{n+1}^{(1)}\right) \mathbf{r}_{n+1}^{(i)}
\]
(2.2) Solve for Reduced r.h.s.
\[
\begin{aligned}
\delta \bar{d}_{I} & =0 \\
R_{1} & =\mathbf{r}(I)_{n+1}^{(i)}-\widehat{\mathbf{f}}^{I} \cdot \delta \overline{\mathbf{d}} \\
R_{2} & =\Delta \ell^{2}-\Delta \mathbf{d}_{n+1}^{(i)} \cdot \Delta \mathbf{d}_{n+1}^{(i)}-2 \Delta \mathbf{d}_{n+1}^{(i)} \cdot \delta \overline{\mathbf{d}}
\end{aligned}
\]
(2.3) Solve \(2 \times 2\) Reduced system:
\[
\left[\begin{array}{ll}
A_{11} & A_{12} \\
A_{21} & A_{22}
\end{array}\right]\left[\begin{array}{c}
\delta d_{I} \\
\delta \lambda
\end{array}\right]=\left[\begin{array}{l}
R_{1} \\
R_{2}
\end{array}\right]
\]
(2.4) Update Displacements and Load Factor
\[
\begin{aligned}
\delta \mathbf{d} & =\delta \overline{\mathbf{d}}+\delta \lambda \delta \hat{\mathbf{d}}-\delta d_{I} \delta \hat{\mathbf{v}} \\
\mathbf{d}_{n+1}^{(i+1)} & =\mathbf{d}_{n+1}^{(i)}+\delta \mathbf{d} \quad\left(\mathbf{T}_{n+1}^{(i+1)}=\mathbf{R}(\delta \mathbf{d}) \mathbf{T}_{n+1}^{(i)}\right) \\
\Delta \mathbf{d}_{n+1}^{(i+1)} & =\Delta \mathbf{d}_{n+1}^{(i)}+\delta \mathbf{d} \\
\lambda_{n+1}^{(i+1)} & =\lambda_{n+1}^{(i)}+\delta \lambda
\end{aligned}
\]
(2.4) Compute New Residual
\[
\mathbf{r}_{n+1}^{(i+1)}=\mathbf{r}\left(\mathbf{d}_{n+1}^{(i+1)}, \lambda_{n+1}^{(i+1)}\right)=\lambda_{n+1}^{(i+1) \mathbf{f}^{e x t}}-\mathbf{f}^{i n t}\left(\mathbf{d}_{n+1}^{(i+1)}\right)
\]
(2.5) Check Convergence
call CHK_CONV ( \(\mathbf{r}_{n+1}^{(i+1)}, \delta \mathbf{d}, \widehat{\epsilon}^{(i)}, \epsilon_{\text {ref }}, \widehat{\epsilon}_{t o l}\), num_div \(\rightarrow\)
\(\widehat{\epsilon}^{(i+1)},<\) CONVERGED>, <DIVERGED> )
if (<CONVERGED> ) then
\[
\text { num_iters_required }=\text { iter }
\]
```

    \Delta\mp@subsup{\ell}{n+2}{}=\Delta\mp@subsup{\ell}{n+1}{}(\frac{\mathrm{ numiters_desired }}{\mathrm{ num_iters_required }})
    n\leftarrown+1
    go to (1) STEP LOOP
    elseif(<DIVERGED> .or. (iter > maxiters)) then
if (num_cuts < max_cuts) then
\Delta\mp@subsup{\ell}{n+1}{}=\Delta\mp@subsup{\ell}{n+1}{\prime}/2
num_cuts = num_cuts + 1
go to (1.3)
else
STOP
endif
else
i\leftarrowi+1
go to (2) ITER LOOP
endif

```

\section*{Starting Procedure: Step \(1(\mathbf{n}=\mathbf{0})\)}

Replace Algorithm Steps (1.1)-(1.2) by:
\[
\begin{aligned}
\mathbf{d}_{1}^{(0)} & =0 \\
\delta \widehat{\mathbf{d}} & =\mathbf{K}^{-1}\left(\mathbf{d}_{1}^{(0)}\right)\left[\widehat{\mathbf{f}}^{e x t}+\mathbf{K}^{u \&} \widehat{\mathbf{d}}^{\ell}\right] \\
\lambda_{1}^{(1)} & =\lambda_{\text {start }} \quad \text { (user specified) } \\
\Delta \lambda_{1}^{(1)} & =\lambda_{1}^{(1)} \\
\Delta \ell_{1} & =\Delta \lambda_{1}^{(1)}\|\delta \hat{\mathbf{d}}\| \\
\Delta \mathbf{d}_{1}^{(1)} & =\Delta \lambda_{1}^{(1)} \delta \hat{\mathbf{d}} \\
\mathbf{d}_{1}^{(1)} & =\Delta \mathbf{d}_{1}^{(1)}
\end{aligned}
\]
(Also, form \(K\left(d_{1}^{(1)}\right)\) before next solve. )

\section*{Starting Procedure: Step \(2(n=1)\)}

Replace Algorithm Steps (1.1)-(1.2) by:
\[
\begin{aligned}
\mathbf{d}_{2}^{(0)} & =\mathbf{d}_{1} \\
\delta \widehat{\mathbf{d}} & =\mathbf{K}^{-1}\left(\mathbf{d}_{2}^{(0)}\right)\left[\widehat{\mathbf{f}}^{e x t}+\mathbf{K}^{u s} \widehat{\mathbf{d}}^{d}\right]
\end{aligned}
\]
\[
\begin{aligned}
& \Delta \lambda_{2}^{(1)}=\Delta \ell_{2} /\|\delta \widehat{\mathbf{d}}\| \\
& \lambda_{2}^{(1)}=\lambda_{1}+\Delta \lambda_{2}^{(1)} \\
& \Delta \mathbf{d}_{2}^{(1)}=\Delta \lambda_{2}^{(1)} \delta \hat{\mathbf{d}} \\
& \mathbf{d}_{2}^{(1)}=\mathbf{d}_{1}+\Delta \mathbf{d}_{2}^{(1)} \quad\left(\mathbf{T}_{2}^{(1)}=\mathbf{R}\left(\Delta \mathbf{d}_{2}^{(1)} \mathbf{T}_{1}\right)\right. \\
&\left(\text { But don't reform } \mathbf{K}\left(\mathbf{d}_{1}^{(1)}\right) \text { until step } 3 .\right)
\end{aligned}
\]

\section*{NOTATION}
d Displacement vector.
\(\delta \mathrm{d} \quad\) Iterative change in \(\mathbf{d}\).
\(\Delta \mathbf{d} \quad\) Incremental (load-step) change in \(\mathbf{d}\).
\(\mathrm{d}_{n}^{i} \quad\) Displacement vector at iteration \(i\) of step \(n\).
\(\Delta d_{n}^{i} \quad\) Incremental (step) change in \(d . \Delta d_{n+1}^{(i+1)}=d_{n+1}^{(i)}-d_{n}\)
\(\delta \hat{\mathbf{d}} \quad\) Tangential displacement \(=\mathbf{K}^{-1} \hat{\mathbf{f}}^{\text {ext }}\)
\(\Delta \ell \quad\) Incremental arclength (step) parameter.
\(\mathbf{f}^{e x t} \quad\) External force vector - base load.
\(\mathbf{f}^{\text {int }} \quad\) Internal force vector.
\(\mathbf{f}^{I} \quad I^{\prime}\) th column of \(\mathbf{K}\)
\(\mathbf{r}\) Residual force vector.
K Stiffness matrix.
\(\widehat{\mathbf{K}} \quad\) Stiffness matrix with I'th row and column deleted
\(\widehat{\mathbf{v}} \quad\) Solution vector corresponding to \(\widehat{\mathbf{K}}^{-1} \hat{\mathbf{f}}^{I}\)
\(\delta \overline{\mathbf{d}} \quad\) Basic (fixed-load) iterative change in \(\mathbf{d}_{i}\)
\(\delta \mathbf{d}^{*} \quad\) Linear combination of \(\delta \overline{\mathbf{d}}\) and \(\delta \hat{\mathbf{d}}\).
\(A_{i j} \quad\) Advanced-Riks reduced system coefficients
\(\boldsymbol{R}_{\boldsymbol{i}} \quad\) Advanced-Riks reduced residuals
num_cuts Number of times load step has been cut in half at current step.
num_div Number of consecutive iterations at which divergence occurs.
\(c_{n} \quad\) Extrapolation coefficient corresponding to step \(n\).
\(\widehat{\epsilon} \quad\) Relative error in energy norm.
\(\epsilon \quad\) Absolute error in energy norm.
\(\epsilon_{\text {ref }} \quad\) Reference value of \(\epsilon\); initialized as zero.
\(\epsilon_{\text {tol }} \quad\) Relative error tolerance (default: \(10^{-4}\) ).
\(\lambda \quad\) Load factor.
\(\Delta \lambda \quad\) Incremental (load-step) change in \(\lambda\).
\(\mathrm{K}^{\mathbf{u s}} \quad\) Stiffness submatrix coupling specified (s) displacement components with force components corresponding to unknown (u) displacements.
\(\widehat{\mathbf{d}}^{0} \quad\) Base value of specified displacement vector.
\(\mathbf{d}^{\mathbf{A}} \quad\) Current value of specified displacement vector. \(\mathbf{d}^{\mathbf{s}}=\lambda \hat{\mathbf{d}}^{\mathbf{A}}\).

\subsection*{3.10.11 PROCEDURE LISTING}
```

\#procedure ML_STATIC_2( --
beg_step =1 ; -- . Starting step number (>0)
max_stops=1 ; -- . Maxinur stops to compute
max_iters=9 ; -- . Maximum iterations per step
des_iters=4 ; -- . Number of iterations desired
fac_steps=1 ; -- . Steps_per_refactoring
max_cuts=3 ; -- . Maximun number of etep cuts
tol_e=1.E-3 ; -- . Energy error tolerance
beg_load ; -- . Starting load factor (>0.)
max_load ; -- . Uppor_bound on load factor
_in_load ; -- . Lover_bound on load factor
path_scale=1.; -- . Path_inc scl_factor (restart)
extrapolate=<true> ; --
line_search=1.;-- . Initial line-search paraneter
debug=<FALSE>; -- . Debug_print switch
NL_GEOM = 2 ; -- . Geom. Nonlin. Level (1|2)
COROTATION=1 ; -- . Corotational Flag (leave on!!)
adv_riks m <talse\rangle ; -- . Ldvanced RIKS flag.
Noninal_DB = NOMINAL.GAL ; -- . Selected Output
Nominal_DS = RESPONSE.HISTORY ; --
N_SELECT ; SEL_NODES; SEL_DOFS --
)
*Renark
*Ronark
Hemark NL_ST ATIC__1
\#if < [adv_riks] > /then
*remark ADVANCED EIKS
*endif
*Remark
\#Remark CSM Testbed Procedure for Nonlinear Statice:
*ReIark
*Remark O Corotational Mewton/Raphson algorithm
*Remark o Linearized Crisfield/Riks arc-length control
*Renark o Applied forces and/or displacements
-Renark
\#lenark Authors: G.M. Stanley and C.C. Rankin
*Renark Version: MAR-03-1988
*Remark | |
*Renark
. INITIALIZATION
*det/i ns_overwrite z= <true>
*det/i debug == [dobug]
*def/i max_step == <[beg_step]+[max_steps]-1>
*def/i num_iters z= [des_iters]
*def/d path_scale x= [path_scale]
*de1/i extrapolate == [extrapolate]
*de1/a NOM_DB == [Nominal_DB]
*def/a NOH_DS == [Nominal_DS]

```
```

*defi/i N_SELEECT == [TM_SEELECT]
*def/i SEL_NODES[1:<N_SELECT>] == [SEL_NODES]
*def/i SEL_DOFS[1:<N_SELECT>] == [SEL_DOFS]
*def/i NL_GEOM == [NL_GEOM]
*deí/i COROTATION z= [COROTATION]
*CALL DEFNS ( STEP = [BEG_STEP]; ITER = 0 )
*IF < [BEG_STEP] /EQ 1 >/THEN
*Ronark IMITIALIZATION:
*call INITIAL
*ENDIF
. BEGIN STEP_LOOP
\#DO :STEP_LOOP \&n = O, <[max_ateps]-1>
*def/i step x < < [beg_step]+\langle\$n>>
*def/i pass =x 1
*def/i tot_iters==1
*if < <<step> /gt 2> /and <<extrapolate> /eq <true>>> /then
*de1/i extrap_this_step =x <true>
*else
*dei/i extrap_this_step == <false>
*ondif
*Renark
*ronark
*renark
*Honark BEGIMMING STEP <STEP>
*ramark
*renark
*call DEFNS ( step = <step>; iter = 1)
:NEU_PASS . He-entry point for step-size reduction
[XqT VEC
*if <<<step>/gt 1> /and <<pass> /oq 1> > /thon
*def/d path_inc == << <path_scele>*<path_inc_n>>
\#lonark Nem PaTH INCREMENT = <path_inc>
*andif
. . . Gonerate Displacement PREDICTOR
*if <extrap_this_step>/then
*Ronark Predicting displacements/load via EXTRAPOLATION
*call EXTRAP (dx_np1 = <path_inc> ; cx_n = cx_n ; --
dx_n = <path_inc_n> ; cx_nal = cx_nm1; --
dx_na1 = <path_inc_nm1>; cx_nm2 = cx_nm2 )
*def/d lam_np1_i == < (\langlecx_n\rangle*<lam_n\rangle) --
+ (<cx_nm1\rangle*<lan_nm1\rangle) --
+ (<cx_nm2>*<lan_nm2>) >
<d_np1_i\rangle <- \langlecx_n\rangle \langled_n\rangle + \langlecx_nm1\rangle \langled_nm1\rangle
<d_np1_i\rangle <- <d_np1_i\rangle + \langlecx_nm2\rangle <d_nm2\rangle
<d_inc_i\rangle <- <d_np1_i\rangle - \langled_n\rangle
ROTATE <T_n\rangle * <d_inc_i\rangle -> <T_np1_i\rangle
*else
*Romark Using Previous Step as Displacement Predictor
*ronark

```
```

    *ronark Last displacenent dataset : <d_n>
    *renark
    *dof lan_np1_i mx <lam_n>
        <d_np1_i\rangle <- <d_n>
        <T_np1_i\rangle <- <T_n\rangle
        <d_inc_i> <- <d_n>
    *andif
    *if < <spec_disp_flag> > /thon
        SPECIFY <lam_np1_i> <d_ext> -> <d_np1_i>
    *ondif
    . . . Forn Stiffness based on Predictor
*if <<<pass>/oq 1 > /or <extrap_this_step> > /then
*call PORM_STIFF (displacoment = <d_np1_i\rangle; --
rotation = <T_np1_i\rangle; --
stiffness = <K_asm>) . output
. . . Find largest tangent component I = <ndef> <fd>
. . . Extract corresponding column of systen matrix
. . . Specify freedon NDEF, PD as constrained to zero
*if <adv_riks>/then
*if <<step>/le 1>/then
*def/i ndefx=0
*olse
*call STIF_COLMN
*endif
*else
*def/i ndef==0
*endif
. . . Pactor stiffness with the added constraint
*call PACT_STIPF
. . . Solve for Tangential Displacenent
*call TANDIS ( step = <step> ; iter = 1 ; --
displacement = <d_np1_i\rangle ; --
rotation = <T_np1_i\rangle ; --
load_factor = <lam_np1_i>; --
max_load = [max_load] ; --
external_force = <F_ext> ; --
internal_force = <F_int> ; --
specified_disp = <d_ext> ; --
tangent_force = <F_T\rangle ; --
tangent_disp = <delta_T> )
Solve for incremental displacement based on stiffness column I
*if <<ndef>/gt 0>/then

```
```

        *call SOLVE ( RHS = <K_I\rangle; SOLN = <delta_I\rangle )
        *endif
    *endif
    . . . Compute Magnitude of Tangential Displacenent
NORM <delta_T> -> mag_delta_T . magnitude of tang. displacement
. . Predict Load Factor and Path Increnont for Curront Stop
*if < <step>/eq 1>/then
*if < <pase> /eq 1 >/thon
*dof/d lan_np1_i == [bog_load]
*dof/d lam_inc == <la_np1_i>
*dof/d path_inc == <<la_inc>*<nag_delta_T>>
*de1/i load_dir == <SIGN(1.;<lan_inc>)>
*0lse
*dof/d lam_inc == < <path_inc>/<nag_delta_T\rangle >
*det/d lam_np1_i =m <lan_inc>
*endif
*elseit <<step>/gt 1>/then
. . . . Path_Increment based on Itorative Performance, Set Direction
*if < <sign_det> /ne <sign_det_n>> /thon
*dof/i load_dir == < -1.*<load_dir_n> >
**lse
*dof/i load_dir == <load_dir_n>
*endif
. . . . Compute Load_Increnent
*if <oxtrap_this_step>/then
*def/d lam_inc == < <lam_np1_i\rangle - <lam_n>>
*olse
\#Romark USING CONSTRAINT EQN TO PREDICT LOAD AT STEP <step>
*dof/d lam_inc m= << <path_inc>/<mag_delta_T> >*<load_dir>>
*def/d lam_np1_i == <<lan_n>+<iam_inc>>
*ondif
*ondif
*Romark LAMBDA_<step>` 1 = <lam_np1_i\rangle , LAMBDA_INC = <lam_inc>
*if < <lan_np1_i> /gt [nax_load] > /then
*Renark MAXIMOM LOAD_LEVEL OBTAINED.
* junp to :EXIT
*elsoif < <lam_np1_i> /le [nin_load] > /then
*Ronark MINIMOM LOAD_LEVEL OBTAINED.
*jump to :EXIT
*endif
*if <<oxtrap_this_step> /eq <false>> /then
*Ronark MODIFYING PREDICTOR VIA PATH-CONSTRAIMT
<d_inc_i\rangle <- <lam_inc> <delta_T>
<d_np1_i\rangle <- <d_n> + <d_inc_i\rangle
ROTATE <T_n> * <d_inc_i\rangle -> <T_np1_i\rangle

```
```

    *if < <spec_disp_flag> > /then
        SPECIPI <lam_np1_i> <d_ext> -> <d_np1_i>
        *endif
    #endif
    . . . Compute 2 x 2 systen coefficients
*call TMO_BY_TWO (free = \langlendef\rangle)
. . . Porm (Stress and) Residual_Force Vector
*call mESIDUAL (step m <step> ; -- . input
iter \# 1 ; --
displacement = <d_npi_i\rangle ; --
rotation : <T_npi_i\rangle ; --
load_factor = <lam_np1_i\rangle : --
external_force = <P_बxt> ; --
internal_force : <<_int> ; --
residual_force : <R_np1_i> ) . output
. . . Initialize Convergence Criteria
*Call CHKCONV ( STEP = 1 ; ITER = 1 ; --
Residunl_force : <R_np1_1\rangle ; --
displacenent_inc = <d_inc_i\rangle ; --
load_inc = <lan_inc> ; --
relaxation = % )
*if <CONVERGENCE> /thon
\#def/d lan_mp1_ip1 == <lam_np1_i>
* jump to :CONVERGED
*endif
. -- BEGIN ITERATION LOOP
\#DO :ITER_LOOP \$1 = 1, [max_iters]
*def/i iter == <<<i>+1>
*def/i tot_iters == <<tot_iters>+1\rangle
*if <<<step\rangle/eq 1\rangle/and <<iter> /eq 2\rangle >/then
由call FOM__STIPF (displacoment = <d_np1_i\rangle; --
rotation = <T_np1_i>; --
stiffness = <K_asm> ) . output
. . . Pind largest tangent component I = <ndef> <fd>
. . . Extract correaponding colunn of systen matrix

- . . Specify freedon NDEF, FD as constrained to zero
*if <adv_riks>/thon
|il <<|tep>/1e 1>/then
*def/i ndef==0
*else
*call STIF_COLMN
*endif
*0lse

```
```

    *derifi ndeí==0
    *ondif
    . . Pactor stiffnese with the added constraint
. . . . . . Update Tangential Displacoment if Specified Displs., etc.
*if < <spec_disp_flag> /or <live_load_flag> > /then
\#Remark o Lecomputing Tangential Displacement
*call TANDIS ( stop = <step> ; iter = <\$i>; --
displacoment = <d_np1_i\rangle ; --
rotation = <T_npi_i\rangle ; --
load_factor = <lan_np1_i>; --
max_load = [max_load] ; --
external_force = <F_ext> ; --
internal_force = <F_int> ; --
specified_disp = <d_ext> ; --
tangent_force = <F_T\rangle ; --
tangent_diEp = <delta_T>)
*ondif
. . . Solve for incremental displacenent based on stiffness colunn I
*if <<ndef>/gt 0>/then
*call SOLVE ( RHS = <K_I\rangle; SOLN = <delta_I\rangle )
*ondif
. . . Conpute 2 x 2 syston coefficionts
*call TWO_BY_TWO (free: <ndef>)
*ondir
. . . . . Conpute Basic Displacenont Iteration (delta_B)
*call SOLVE ( RHS = <R_np1_1\rangle; SOLN = <DELTA_B\rangle )
. . . . . Compute Hev Load-Factor and Displacenent Component I
. . . . . Advanced Rikz (2 x 2) syston.
DOT <delta_B\rangle \# <d_inc_i> -> db_DOT_Dd
DOT <d_inc_i\rangle * <d_inc_i> -> Dd_DOT_Dd
*def/d __2 == < <path_inc>*<path_inc>>
*def/d m_2 == < <R_2\rangle - <Dd_DOT_Dd\rangle - <2.0*<db_DOT_Dd>>>
*if <<ndef>/gt 0>/then
COMPONENT <ndef> <fd> <r_np1_i> -> r_I
DOT <delta_B\rangle \# <K_I\rangle -> db_DOT_K_I
*def/d R_1 == <<r_I> - <db_DOT_K_I>>
Solve 2x 2 RIKS systen

```
```

        Hdef/d Idet = <<<A_11> * <A_22>> - <<A_12> * <A_21>>>
        *def/d dd_I = <<<\mp@subsup{R}{_}{\prime}1\rangle * <A_22\rangle\rangle - <<R_2\rangle * <A_12>>\rangle
        *dof/d dlan = <<<\Lambda_11\rangle * <R_2>> - <<\Lambda_21\rangle * <R_1>>>
        *dof/d dd_I = <<dd_I\rangle / <Rdot>>
        *def/d dlan = <<dlan> / <Rdet>>
        *olse
        Solve simple 1-D RIKS systen for load factor (Normal Riks)
        *def/d dlam z <<<_2>/<A_22>>
        *endif
    . . . . . Opdate Lond Factor
*dof/d lam_np1_ip1 = < <lan_np1_i\rangle + \langledlan>>
*romark
*ronark *REMMR RANKIN'S hOOT SELECTION:
*romark Dd * Dd = <Dd_dot_Dd\rangle
*remark dlan = <Dlan>
*ronark lambda = <lam_np1_ip1\rangle
\#renark *renark
:LOAD_LEVEL
. . . . . Update Incroments
<delta> <- <delta_B\rangle + <dlam> <delta_T>
*if <<ndef> /gt 0>/then
. . . . . . . Add Solution Due to Porturbation in I'th Displacenent Component
(Advanced Riks Only)
<delta> <- <delta> - <dd_i> <delta_I>
. . . . . . Set last component
COMPONENT <ndef> <fd> <delta> <- <dd_I>
*ondif
. . . . . Update Displacements, Rotations
<d_np1_ip1\rangle <- <d_np1_i\rangle + \langledelta\rangle
ROTATE <T_np1_i\rangle * <delta> -> <T_np1_ip1>
<d_inc_ip1\rangle <- <d_inc_i\rangle + <delta>
*if < <spec_disp_flag> > /then
SPECIFY <lan_np1_ip1> <d_ext> -> <d_np1_ip1>
*endif
*if < <DEBUG> > /then
*print 1, <d_np1_ip1>
*print 1, <T_np1_ip1>
*endif
FORM (STRESSES AND) RESIDUAL_FORCE

```
```

*call RESIDOAL ( step = <step> ; -- . input
iter m <iter> ; --
displacenent = <d_np1_ip1> ; --
retation = <T_np1_ip1> ; --
load_factor =<lan_np1_ip1\rangle ; --
external_force = <f_ext> ; --
internal_force = <P_int> ; --
residual_force m<R_np1_ip1>) . output

```

\section*{check convergence}
＊call CHKCONV（ step \(=\langle s t e p\rangle\) ；－．input
                        iter \(=\langle\) iter \(\quad\); --
Residual_force \(=\langle\) _np1_ipi〉 ; --
                        displaconent_inc \(=\langle d e l t a\rangle \quad ;--\)
                        load_inc \(\quad 0.0\); -- . for ertor norm
                                tol_e \(\quad\) [tol_e] ; --
                                max_iters \(=[\) max_iters] ; --
                                convergence \(=\) CONVERGENCE; - . output
                        divargence = DIVERGENCE ; --
                        relaxation \(=s\) )
    *if <<CONVERGENCE>/eq <TROE>>/then
        * jump to :CONVERGED
    **lseif <<DIVRRGENCE>/eq <TROE>>/thon
            *if \llpass>/le [max_cuts] >/then
                * jump to : REPEAT
            *else
                    *Lenark Maximu number of autonatic stop cuts exhausted.
                - juap to :DIVERGED
            *endif
        *endif
        *def/d lan_np1_i \(==\left\langle l a n \_n p 1 \_i p 1\right\rangle\)
    : ITER_LOOP
    :NEUTRAL
*if \llpass>/le [nax_cuts] >/thon
    *jump to : Repeat
*else
    *Renark Maximum number of eutomatic stop cuts exhausted.
*endif
*Renark NOM-CONVERGENCE AT STEP <step>. REviSE STRATEGT.
*junp to : EXIT
: elepeat
    *def/i pass \(==\langle\) <pass>+1 >
    *dof path_inc \(x=\left\langle\left\langle p a t h \_i n c>/ 2\right.\right.\). >
    *Renark
    *Renark CONVERGENCE DIPFICULTIES; REPEATING STEP <stop>
    *Renark vith reduced path_increnent \(=\) 〈path_inc〉
    *Renark Pass: <pass>
    *jump to :NEH_PASS
    : DIVERGED
*Remark DIVERGENCE \(1 T\) STEP <STEP>. REVISE STRATEGY.
*jump to :EXIT
```

        :CONVERGED
        *Remark CONVERGENCE AT STEP <STEP>.
        :NEXTSTEP
    tdof/i num_iters == <iter>
    *def/d peth_scale zx <[des_iters]/<num_iters>>
    *def/d path_inc_na1 == <path_inc_n>
    *def/d path_inc_n == <path_inc>
    *def/d lam_n=2 == <lan_nm1>
    *dof/d len_nal == <lan_n>
    *def/d lam_n == <lam_np1_ipi>
    *def/i sign_det_n == <sign_det>
    *def/i load_dir_n == <load_dir>
    *call POSTSTEP ( step=<step>; iter=<iter> )
    :STEP_LOOP
:EXIT
*end
. =DECK CHKCONY
*procedure CHKCONY ( STEP ; -- . input
ITER ; -
DISPLACEMENT_INC ; -
RESIDUAL_FORCE ; --
LOAD_INC ; -
TOL_E ; --
MAX_ITERS ; -
CONVERGENCE=CONVERGENCE ; -- . output
DIVERGENCE =DIVERGENCE ; --
relaxation = \& )
XQT VEC
. . Initialize
*def/i [CONVERGENCE] == <PALSE>
*dof/i [DIVERGENCE] =m <PALSE>
*if < [ITER] /gt 1 >/then
*dof/d12.4 ERR_E_I == <ERR_E_IP1>
*endif
. . Compute Current Incremental Rnergy Norm
DOT [RESIDUAL_FORCE] * [DISPLACEHENT_INC] -> INC_E_IP1
*if < [ITRR] /le 1 > /then
*if < <ABS(<INC_E_IP1>)> /gt <REF_E> > /then
*def/d12.4 EEF_E x= <ABS(<INC_E_IP1>)>
*endif
*def/i7.2 [RELAXATION] == 1.0
*def/i nun_diverges == 0
*endif
. . Compute Error Morms
*def/d12.4 ERR_E_RAM == < <INC_E_IP1>/<REF_E> >
*def/d12.4 ERR_E_IP1 == <\langleABS(\langleERR_E_RAU\rangle)>* . . >

```
```

. . Check for displacement convergence
*if <<ERR_E_IP1> /1e [TOL_E] > /then
. . . Stiep Convergea
*DEF/I [CONVERGENCE] == <TROE>
*jump to :BOTTOM_LINE
*endif
*if < [ITER] /le 1> :BOTTOM_LINE
. . . Step Mot Converged; Check for Divergence
*IF <<ERR_E_IP1>/<ERR_E_I\rangle/GT 1.0 > /THEN
*def num_diverges = = < <num_diverges>+1 >
*if <<num_diverges>/gt 1 >/then
*DEP/I [DIVERGENCE] == <TRDE>
*RNDIF
*ENDIP
. . Select Relaxation (i.e., line-search) Parameter: :
*dof/f7.2 ls = <[relaxation]>
*if < <<err_e_ip1>/<err_\bullet_i>>/gt .5 >/then
COMP <nax_nod> <nax_dof> [DISPLACEMENT_INC] -> nax_d_ip1
*if <<<ax_d_ip1>*<nax_d_i\rangle /lt 0 > /then
* def ls = < <ls\rangle-. 3 \rangle
*def ls = <MAX(<ls>;.4)>
*elseif < <ABS(<max_d_ipi>)> /lt <ABS(<nax_d_i>)> >/then
*def 1: = < <ls\rangle+.4\rangle
*def 1s = <MIM(<ls>;2.)>
*else
*def ls = 1.0
*ondif
*ondif
*def/f7.2 [relaxation] == <ls>
:BOTTOM_LINE
YORM/HAX [DISPLACEMENT_INC] -> nax_d_i Iax_mod max_do1
NOMM/HAX [RESIDOAL_FORCE] -> max_f_i max_nod_1 max_dof_1
*if < [ITER]/LE 1 >/thon
*def/e12.4 load_factor = <lan_np1_i>
*olse
*dof/e12.4 load_factor = <lan_np1_ip1>
*ondif
*renark
*rolark ---------------------------------------------------------------------
*remark ITElx[[ITER] LD=<load_factor> ERR=\langleerr_e_ip1> REF=\langleref_e\rangle
*remark delta_d_max=<nax_d_i> node=<nax_nod> dof=\langlenax_dof>
*ronark resid_f_max=<nax_f_i> node=<nax_nod_1> dof=\langlenax_dof_1>
*romark
*renark
*if < <DEBUG> > /then
*print 1, [DISPLACEMENT_INC]

```
＊print 1，［RESIDUAL＿PORCE］
endif
＊END
．＝DECK DEFNS
＊procedure DEFNS（ step；iter ）
－Purpose：Dofine basic nacro＿symbols for NLSTATIC3 procedure
＊def／i np1＝［step］
＊def／i \(n=\langle\langle n p 1\rangle-1\rangle\)
＊def／i nm1 \(=\langle\langle n\rangle-1\rangle\)
＊def／i \(\mathrm{nm} 2=\langle\langle\mathrm{n}\rangle-2\rangle\)
＊if＜［iter］／eq 0 ＞／then ．run initialization
＊def／i NS＿1di \(==1\)
＊def／i NON＿1di＝＝ 3
＊def／i iset \(==1\)
＊def／i icon \(\quad=1\)
＊der／a f＿spec \(==\) APPL．PORC．〈iset＞．〈icon＞
＊def／a d＿spec \(==\) APPL．MOTI．〈iset＞．〈icon＞
Check for Prescribed Force／Displacement Loading
＊find dataset＜NS＿ldi＞＜f＿spec＞／seq＝ids
＊if \llids＞／gt 0 〉／then
＊Remark Note：Applied forces dataset 〈f＿spec＞，will be used ＊def／i spec＿force＿flag \(==\) 〈true〉
－else
＊def／i spec＿force＿flag \(==\langle f a l s \theta\rangle\)
＊endif
＊find dataset＜NS＿ldi＞＜d＿spec＞／seq＝ids
－if 〈＜ids＞／gt 0 〉／then
＊Remark Note：Specified displacement dataset 〈d＿spec＞will be used
＊def／i spec＿disp＿flag＝＝＜true＞
＊else
＊def／i spec＿disp＿flag＝＝〈false〉
＊endif
＊if \ll＜spec＿force＿flag＞／eq 0＞／and＜＜spec＿disp＿flag＞／eq 0＞＞／then
＊remark ；＊remark Procedure stopped：no loads defined
＊endif
＊def／i live＿load＿flag＝＝＜false＞
＊def／a d＿ext \(==\) EXT．DISP
＊def／a f＿ext＝＝EXT．FORC
＊def／a f＿int \(==\) INT．FORC
＊def／a f＿T \(==\) TAN．FORC
＊def／a R＿np1＿i \(==\) RES．FORC
＊def／a R＿np1＿ip1 \(==\) RES．FORC
＊def／a d＿inc＿i \(==\) INC．DISP
＊def／a d＿inc＿ip1 \(==\) INC．DISP
＊def／a delta＿T＝＝HAT．DISI
＊def／a delta＿B \(==\) BAR．DISI
＊def／a delta＿S \(==\) STR．DISI
＊def／a delta \(==\) TOT．DISI
```

    #def/a K_anem =% ASM.STIF
    *det/a K_fac == FAC.STIF
*def/a K_I == COL.STIF.1.1
*der/a Delta_I s= STP.DISI
*det/i ndef == 0
*def/a d_ective z= ACT.DISI
Retrieve Control Paraneters from DATA_BASE
*il < [step] /eq 1 >/then
*def/1 Eign_det =m 1
*def/i load_dir == 1
*det/d 1am_n E= 0.0
*def/d lam_nmi == 0.0
*def/d lan_n!2 == 0.0
*def/d path_inc_n == 0.0
*def/d path_inc_nm1 == 0.0
*del/d rel_e == 0.0
*Romark STARTING PARAMETERS INITIALIZED.
*else
*opon <NOM_ldi> <NOM_DB>
*find dataset <nom_ldi> <nom_ds>/seq=nom_ids
*g2n /names=lam_n /typexd <nom_Idi> <nom_ids> LOAD.<n>
*g2m /namezvlan_nm1 /typerd <nom_ldi> <nom_ids> LOAD.<nmi>
*g2m/namem=lam_nm2 /type=d <nom_ldi> <nom_ids> LOAD.<nm2>
*g2n /names=path_inc_n /type=d <nom_ldi> <nom_ids> PATH_INC.<n>
*g2m /namexmpath_inc_nm1 /type=d <nom_ldi> <nom_ids> PATH_INC.<nm1>
*g2n /namesmsign_det_n /type=I <nom_ldi> <now_ids> SIGN_DET.<n>
\#g2n /namea=load_dir_n /type=I <nom_ldi> <nom_ids> LOAD_DIR.<n>
\#g2m /namer=ref_e/type=d <nom_ldi> <nom_ids> REP_ERR.<n>
*g2m /name=mdef /type=i <nom_ldi> <nom_ids> NDEF
\#g2m /namesefd /type=i <nom_ldi> <nom_ids> FD
*close <NOM_ldi>
*Renark
*ronark
*renark
*Remark RE-START PARAMETERS:

```

```

    #Romark PATH_INCREMS (n, na1) = <path_inc_n>, <path_inc_mmi>
    HRemark SIGN_DET (n) = \langlesign_det_n\rangle
    *Romark LOAD_DIR (n) = <load_dir_n>
    #remark
    #renark
    *endif
    *ondif

- Define Global Datasets for Jpcosing Stop
*def/a d_me2 E= TOT.DISP.<nu2>
*de1/a d_nm1 == TOT.DISP.<nu1>
*def/a d_n == TOT.DISP.<n>
*def/a d_np1_i == TOT.DISP.<np1>
*def/a d_np1_ip1 == TOT.DISP.<np1>

```
```

*def/a T_n == TOT.ROTN.\langlen>
*def/a T_np1_i == TOT.ROTN.<np1>
*dof/a T_np1_ip1 == TOT.ROTN.<np1>
\#end

- =DECK EXTRAP
*procedure EXTRAP ( dx_np1; dx_n; dx_nm1; cx_n; cx_nm1; cx_nm2 )
*def dx_np1 = [dx_np1]
*def dx_n = [dx_n]
*def dx_nm1 = [dx_nm1]
tdef x_n=1 = <dx_nm1>
*def x_n = < <x_nm1\rangle+\langledx_n\rangle \rangle
*def x_np1 = < <x_n>+<dx_np1\rangle>
*def s_n=1 = < <x_np1>-\langlex_nm1\rangle \rangle
*def s_n = < <x_np1\rangle-\langlex_n\rangle \rangle
*def [cx_n] == < <x_np1\rangle*<s_nm1>/<<<x_n\rangle*<dx_n>>>>

```

```

    *def [cx_nm2] =m < <s_nm1>*<s_n>/<<<x_nm1>*<x_n>> >
    *end
. =DECK FACT_STIPF
*procedure FICT_STIFF
[XQT INV . Factor stiffness
RESET CON = 1
RESET LRA = 7108
RESET DRERO = 1.E-10
RESET SPDP = <csm_precision>
*remark
*Romark MATRIX BEING FACTORED (in Double Precision).
. Define factored-natrix parameters as global macrosymbols
[XQT VEC
*remark Determinant = <coef_det> * 10 - <exp10_det>
\#ronark Neg. roots = <num_neg>
*def/i sign_det == <SIGN(1.;<coof_det>)>
*remark Sign of det = <sign_det>
*renark
*END
. =DECK FORM_STIPF
*procedure PORM_STIFP ( DISPLACEMENT ; --
ROTATION ; --
STIPFNESS ) . output
*Remark FOMMING NEU STIFFNESS MATRIX
*call ES ( function = 'FORM STIPFNESS/TANG' ; --
en_nl_geon = <NL_GEOM> ; --
es_coro = <COROTATION> ; --
es_dis_ds = [DISPLACEMENT] ; --
es_rot_ds = [ROTATION] )
[XQT K . Transform/assemble stiffness
*END
. =DECK INITIAL
*procedure INITIAL

- clear initial displacements and rotations ( n = 0)

```
```

    #g2n framo=parameters /type=i /maxn=18 <HS_LDI> JDP1.BTAB.1.8 DATA.1
    *def/i MNODES = <PARAMETERS[1]>
    *dof/i HDOF = <PARAMETERS[2]>
    *Renark Problen DimensionE: N_moden = <NNODES>, M_doin = <NDOF>
    [XqT VEC
INIT_DOF CON..<icon> -> DOF.TABL
*Renark DOF TABLE initialized.
INIT_VEC <d_inc_ip1> <NDOF> BY <NNODES> . Zeroize translations
INIT_VEC <K_I> <NDOP> BY <NNODES> . Zeroize translations
INIT_VEC <Delta_I> <NDOF> BY <NNODES> . Zeroize translations
INIT_VEC <d_active> <NDOF> BY <NNODES> . Zoroize translations
IMIT_VEC <d_n> <NDOF> BY <NNODES> . Zeroize translations
INIT_VEC <T_n> 3 BY <NNODES> . Zeroize rotation pseudovectors
*Ronark Displacenents initialized.
*if < <spec_disp_flag> > /then
<d_ext> <- <d_spec> . for VEC
NORM <d_ext> -> norn_d
*if < <norm_d> /eq 0. > /then
*lonark
*Renerk NOTE: Specified displacements are identically zero.
*Ronark
*ondif
*copy <NS_ldi> = <NS_1di\rangle, <d_spec>
<d_spec> <- 0 . for SSOL
*Remark Specified displacenents saved in <d_ext>.
*endif
*if <<spec_force_flag>> /thon
<F_ext> <- <F_spec> . for VEC
NORM <f_ext> -> norn_f
*if <<norn_f>/eq 0. >/then
*Renark
\#lenark NOTE: External forces are identically zero.
*Ronark
*endif
*Ronark External force vector saved in <P_ext>.
*copy <HS_ldi> = <NS_ldi>, <P_spec> . for SSOL
*else
INIT_VEC <P_ext> <NDOP> BY <NNODES>
INIT_VEC <F_spec> <NDOF> BY <NNODES> /single_precision . for SSOL
*endif
*lemark Right-hand-side vector zeroized (in <F_spec>).
INIT_VEC <F_int> <NDOF> BY <NNODES>
*Remark Internal force vector zeroized (in <F_int>).
INITIALIZE ELEMENT CONFIGURATION
[xQT E
[XQT RSEQ
resot nethod=0,naxcon=35
[XQT TOPO
reset maxsub = 40000,1ram=8196
*call ES ( function = 'INITIALIZE' )

```
```

    *Ronark Elenent configuration initialized.
    *and
. =DECK POSTRES
*procedure POSTRES ( step )
[XQT VEC
*find dataset <NOM_LDI> <NOM_DS> /seq=post_ids
*if < <post_ids>/le 0 > /then
*put dateset <NOM_LDI> <NOM_DS> /arat=2000 /seq=post_ids
mondif
Save selected displacements on nominal data-base
*def/a dof_names = O, V, W, RO, RV, RU
*do \&isel = 1, <N_SELECT>
*def/i node = <SEL_NODES[<$isel>]>
        *def/i dof = <SEL_DOPS[<$ise1>]>
*dof/a dof_name = <dof_names[<dof>]>
COMPONENT <node> <dof> TOT.DISP.[step] -> DISP
*def/a recd_nane = DISP_<dof_name>_<node>.[step]
*Renark <recd_name> = <DISP>
*n2g /name=disp /type=d <nom_ldi> <post_ids> <recd_name>
Save Leaction Porces for Current Step
BEIC.FORC.[step] <- INT.PORC
*if < [step] /eq 0 >/then
EEAC.PORC.0 <- 0.0
*endif
*if < <spec_disp_flag> > /then
COMPONENT <node> <dof> REAC.POBC.[step] -> FORCE
*def/a recd_name = FORCE_<dof_name>_<node>. [step]
*Renark <recd_name> = <FORCE>
\#m2g /namexforce /type=d <non_ldi> <post_ids> <recd_name>
*ondif
*enddo
*end
. =DECK POSTSTEP
*procedure POSTSTEP ( step; iter )
*Renark
-_-------------------
*Henark STEP [stop] SUMMARY :
*Ronark -------------------------------------------------------------------
*lonark Load Pactor _---------------------- <lam_np1_ip1>
*Romark Load Direction _---------------------- <load_dir>
*Renark Stiffness determinant _------.------ <coef_det> * 10 ` <exp10_det>
*Remark Number of negative roots --------- <num_neg>
*Renark Path_length_increment _----------- <path_inc>
*Ronark Relative enorgy_error _-.-.-..-...- <err_e_ip1>
*Renark Number of Iterations ------------- <num_iters>
*Renark Number of Stop Cuts _-_--.--.-.-.-- <<pass>-1>
*Remark Total Number of Iterations _-.-.-.- <tot_iters>
*Renark

```
```

\#open <NOn_1dI> SNOM_DB>
*if < [step] /eq 1 >/then
*call POSTRES ( stop = 0 )
*dor/d load_0=0.
**2g/nawexlond_0 /type=d <NOM_LDI> <NON_DS> LOAD.0:O
*endif
*cell POSTRES ( stop=[stop])
*find dataset <NOM_LDI> <NOM_DS> /seq=non_ids
*n2g /name=1an_np1_ip1 /typead <nom_ldi> <non_ids> LOAD.[STEP]
*n2g /name=path_inc /type=d <nom_ldi> <nom_ids> PATH_INC.[STEP]
*n2g /namezerr_e_ip1 /typerd <nom_ldi> <nom_ids> ERROR.[STEP]
*n2g /namexref_e/type=d <nOm_ldi> <nOM_ids> REP_ERR.[STEP]
*n2g /name=load_dir /typeri <nom_ldi> <nom_ide> LOAD_DIR.[STEP]
*mgg/namexaign_det /typexi <nom_ldi> <nom_ids> SIGN_DET.[STEP]
*m2g /namercoef_dot /type=d <non_ldi> <non_ids> COEF_DET.[STEP]
*n2g/namezexp10_det /type=i <nom_ldi> <nom_ids> EXP10_DET.[STEP]
*n2g/namexnum_neg /typexd <nom_ldi> <nom_ids> NEG_ROOTS.[STEP]
*m2g /namemnum_iters /typexi <nom_ldi> <nom_ids> NUM_ITERS.[STEP]
*n2g/naneztot_iters /typexi <non_ldi> <nom_ids> TOT_ITERS.[STEP]
*dof/i passm1 = <<pass>-1>
*n2g /name=passa1 /typexi <non_ldi> <nom_ids> NOM_CUTS.[STEP] . cgl, 7/26/88
*m2g /name=ndef /type=i <nom_ldi> <nom_ids> NDEF
*if <<ndef>/oq 0>/thon
*def/i fd==0
*endif
*m2g/name:id /type=i <non_ldi> <nom_ids> FD
*close <NOM_ldi>
*ond
. =DECK residual
*Procedure RESIDOAL ( STEP=1; ITER=1 ; -- . input
dISPLACEMENT ; --
MOTATION ; --
LOAD_FACTOR ; --
SPECIPIED_DISP ; --
INTERNAL_FORCE ; --
EXTERNAL_FORCE ; --
RESIDOAL_FORCE ) .output
[xqT VEC
[INTERHAL_PORCE] <- 0.
*call ES ( function = 'FORM FORCE/INT'; --
e3_nl_geon = <NL_GEOM> ; --
es_coro = <COROTATIOM> ; --
0s_dis_ds = [DISPLACEMENT] ; --
es_rot_ds = [ROTATION] ; --
es_frc_ds = [INTERNAL_PORCE] )
[xqT vEC
[RESIDUAL_PORCE] <- [load_factor] [EXTERNAL_FORCE] - [INTERNAL_FORCE]
*END
. =DECK SOLVE
*Procedure SOLVE ( RHS ; SOLN )
. Copy Right-Hand-Side Vector to Expected SPAR (Single Precision) Dataset

```
```

        [IQT VEC
            APPL.FORC.<iset>.<icon> <- [RHS] /single_precision
    .Solve
[xQT SSOL
RESET CON = <icon>
RESET SET = <iset>
RESET REAC = 0
. Copy SPAR Solution Vector to Double Precision Dataset
[XqT VEC
[SOLN] <- STATIC.DISP.<iset>.<icon>
*end
. =DECK STIP_COLMM
*procedure STIP_COLMN
[XQT VEC
-if <<NDEP>/gt 0>/then
FREE <NDEF> <FD>
*endif
*if <<spec_disp_flag> > /then
<d_active> <- <d_inc_i>
SPECIPY 0. <d_ext> -> <d_active>
NORM/MAX <d_active> -> D_II NDEF FD
*slse
MOMM/MAX <d_inc_i> -> D_II NDEF FD
*ondif
[XQT AOS
SYSVEC : UNIT I 1 1
I=<PD> : J=<NDEF> : 1.0
SYSVEC : COL STF 1 }
DEFINE E = <MS_ldi> UNIT I 1 1
DEPINE K = <US_ldi> K SPAR 36
COL STF 1 1 = PRODUCT (K,E)
[xqT vEC
PIX <NDEP> <FD>
<K_I> <- COL.STF.1.1
*END
. =DECK STIPFNESS
*procedure STIPFNESS ( DATA_BASE ; -- . input
STEP ; --
ITER ; --
LOAD_FACTOR ; --
DISPLACEMENT ; --
MOTATION ; --
STIFFNESS ) . output
\#Remark FORMING NEU STIFPNESS MATRIX
*call LS ( function = 'FORM STIPFNESS/TANG' ; --
en_nl_geom = <NL_GEOM> ; --

```
```

                es_coro = <COROTATION> ; --
                    es_dis_ds = [DISPLACEMENT] ; --
    es_rot_ds = [ROTATION] )
[xQT K
- Transform/assenble stiffness
[xqT IMy

```

```

    RESET COM = 1
    RESET LRA = }716
    RESET DZERO = 1.E-10
    RESET SPDP = <csm_precision>
    *renark
    *Renark MITRIX BEING FACTORED (in Double Precision).
    . Define factored-matrix parameters as global nacrosymbols
[XqT vEC
*renark Determinant = <coof_det> * 10 " <exp10_det>
*ronark Heg. roots m <num_neg>
*def/i sign_det == <SIGN(1.;<coef_det>)>
\#renark Sign of det = <sign_det>
*ronark
*END
. =DECK TANDIS
*procedure TANDIS ( step; iter; displacement ; rotation ; --
load_factor ; max_load ; external_force; --
specified_disp; internal_force; -
tangent_force ; tangent_disp )
*if < <spec_disp_flag> > /then . Load standard spec_disp dataset
[XQT VEC
SPECIFY 1.0 [specified_disp] -> <d_spec>
*endif
*call SOLVE ( RHS = [external_force]; SOLN = [tengent_disp] )
*if < <spec_disp_flag> > /then . Clear standard spec_disp dataset
[xqT VEC
<d_spec> <- 0.0
*ondif
*ond
. =DECK THO_BY_TMO
*procedure TWO_BY_TMO ( FREE )

- . . Compute 2 a 2 sjotem cosificients
[xqt vec
. . . A_22 is used for both ordinary and advanced RIKS
DOT <d_inc_i> * <delta_T> -> A_22
*dof/d 1_22 == < 2.0 * <4_22>>
. . . The remainder of Procedure is invoked only for Advanced Riks
*if <[PREE]/gt 0>/then
COMPONENT <ndef> <ld> <K_I> -> K_II
COMPONENT <ndef> <fd> <f_ext> -> fe_I
COMPONENT <ndef> <fd> <d_inc_i> -> D_II
DOT <K_I\rangle \# <delta_I\rangle -> K_DOT_d_I

```
```

    DOT <K_I\rangle * <delta_T> -> K_DOT_T
    DOT <d_inc_i\rangle * <delta_I\rangle -> dd_DOT_d_I
    *dof/d 1_11 == <<K_II> - <K_DOT_d_I>>
    *def/d 1_12 == <<K_DOT_T> - <Ie_I>>
    *if <<spec_disp_flag>>/then
        DOT <K_I\rangle * <d_ext\rangle -> K_DOT_d_ext
        *def/d A_12 = < <<__12\rangle - <K_DOT_d_ext>>
    *endif
    *def/d A_21 =x < 2.0 *<<D_II> - <dd_DOT_d_I>> >
    *endif

```
*end

\subsection*{3.11 Procedure NL_DYNAMIC_1}

\subsection*{3.11.1 GENERAL DESCRIPTION}

Procedure NL_DYNAMIC_1, written by C. C. Rankin and B. Nour-Omid of Lockheed Palo Alto Research Laboratory, performs nonlinear transient analysis using a one-step, self-starting, implicit integration algorithm containing adjustable parameters. The nonlinear system is solved using a modified Newton/Raphson incremental/iterative solution sequence. Like NL_STATIC_1, procedure NL_DYNAMIC_1 relies on the Generic Element Processor (i.e., structural element processors, ESi) and hence has a corotational option for geometric nonlinearity that enables arbitrarily large rotations.

Procedure NL_DYNAMIC_1 solves the transient system
\[
\begin{equation*}
\mathbf{M} \ddot{\mathbf{u}}+\mathbf{f}^{i n t}(\mathbf{u})=\mathbf{f}^{e x t} \tag{3.11-1}
\end{equation*}
\]

Here \(M\) is the mass matrix, \(u\) is the displacement, and dots over quantities refer to differentiation with respect to time. These equations are discretized over time using the following relations involving two parameters \(\theta\) and \(\alpha\) :
\[
\begin{equation*}
\mathbf{M a} \mathbf{a}_{n+\theta}+(1+\alpha) \mathbf{f}^{i n t}\left(\mathrm{~d}_{n+\theta}\right)-\alpha \mathrm{f}^{i n t}\left(\mathrm{~d}_{n}\right)=\mathbf{f}_{n+\theta}^{e x t} \tag{3.11-2}
\end{equation*}
\]
where \(\mathbf{d}_{n+\theta}\) and \(\mathbf{a}_{n+\theta}\) are the approximations to the displacement and acceleration at time \((n+\theta) \Delta t\), and where Wilson's \(\theta\) interpolation parameter is used to obtain the desired acceleration according to
\[
\begin{equation*}
\mathbf{a}_{n+\theta}=(1-\theta) \mathbf{a}_{n}+\theta \mathbf{a}_{n+1} \tag{3.11-3}
\end{equation*}
\]

Velocity \(v\) and acceleration a are related to the displacements at the point \(n+\theta\) by
\[
\begin{align*}
& \mathbf{v}_{n+\theta}=\mathbf{v}_{n}+\theta \Delta t\left[(1-\gamma) \mathbf{a}_{n}+\gamma \mathbf{a}_{n+\theta}\right] \\
& \mathbf{d}_{n+\theta}=\mathbf{d}_{n}+\theta \Delta t \mathbf{v}_{n}+(\theta \Delta t)^{2}\left[\left(\frac{1}{2}-\beta\right) \mathbf{a}_{n}+\beta \mathbf{a}_{n+\theta}\right] \tag{3.11-4}
\end{align*}
\]
where we have introduced the two standard Newmark parameters \(\beta\) and \(\gamma\) as the last two parameters in our system. The resulting system to be solved is
\[
\begin{equation*}
\mathbf{M d}_{n+\theta}+(\theta \Delta t)^{2} \beta(1+\alpha) \mathbf{f}^{i n t}\left(\mathbf{d}_{n+\theta}\right)-\widetilde{\mathbf{f}}_{n+\theta}=0 \tag{8}
\end{equation*}
\]
where the quantity \(\tilde{\mathbf{f}}_{n+\theta}\) is known from the last converged time step (see Section 4.3.9.2. for a complete derivation of equations and definition of symbols).

NL_DYNAMIC_1 is designed to solve any well posed initial value transient analysis problem with non-negative mass. This includes problems with initial velocity and/or initial displacement, as well as a generalized imposed external forcing with either built-in or user-suppled time dependence. Currently, the procedure uses the same external loading as NL_STATIC_1, with a multiplier defined by a force-time procedure. The built-in procedures are described in Sections 4.3.3.7 and 4.3.3.8.

Since (66) is a nonlinear system similar to (1), much of what is in NL_STATIC_1 applies to NL_DYNAMIC_1. In particular, we mention the solution of a banded system with similar structure to the stiffness matrix, identical handling of large rotations, similar procedures for archiving results of solutions and retrieving restart information, and very similar convergence and stepsize adjustment procedures. We shall henceforth concentrate on the differences between the static and dynamic algorithms, with particular emphasis on operations involving the mass, time step, and the four adjustable integration parameters. In some respects, NL_DYNAMIC_1 is simpler than its static analogues, since no arclength constraint is needed for a positive-definite mass/stiffness system.

\subsection*{3.11.2 PROCEDURE USAGE}

Procedure NL_DYNAMIC_1 may be invoked by the *call directive:
```

*call NL_DYNAMIC_1 ( arg1 = val1; arg2 = val2; ...)

```
where argi are argument names and vali are the corresponding values you wish to give them. The following are valid arguments for NL_DYNAMIC_1; note that those without default values are mandatory, while the others are optional.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline BEG_STEP & - & Starting step number ( \(>0\) ) \\
\hline MAX_STEPS & - & Maximum steps to compute \\
\hline BEG_TIME & - & Problem starting time \\
\hline MAX_TIME & - & Upper_bound on problem time \\
\hline DEL_TIME & - & Beginning time step \\
\hline INT_PARS & 1.,0.,.25,.5 & Time integration parameters \\
\hline LOAD_STIFF & <false> & Include load stiffness \\
\hline FT_PROC & FT_ZERO & Forcing procedure \\
\hline FT_ARGS & 0. & Parameter array for FT_PROC \\
\hline COROTATION & 1 & Corotational Update Option \\
\hline DESITERS & 4 & Number of iterations per step desired \\
\hline EXTRAPOLATE & <true> & Perform quadratic extrapolation of solution \\
\hline FAC_STEPS & 1 & Steps_per_refactoring \\
\hline MAX_ITERS & 9 & Maximum iterations per step \\
\hline MAX_CUTS & 3 & Maximum number of successive step cuts \\
\hline NL_GEOM & 2 & Geometric Nonlinearity Level (1 or 2) \\
\hline NOMINAL_DB & NOMINAL.GAL & Results database file \\
\hline NOMINAL_DS & RESPONSE.HISTORY & Results dataset \\
\hline N_SELECT & 0 & Number of nodes for selected disp. output \\
\hline SEL_NODES & 0 & List of nodes for selected output \\
\hline SEL_DOFS & 0 & Corresponding list of nodal freedoms (1-6) \\
\hline TOL_E & 1.E-3 & Relative error tolerance in energy norm \\
\hline
\end{tabular}

In the above definitions, the term step refers to a time step. The total response is aütomatically subdivided into time steps, with the starting time prescribed by the User using BEG_TIME. The initial time step is set by DEL_TIME, and held constant unless trouble occurs. If convergence is difficult, the time step will be cut, and a new initial value problem will be started at the last converged solution.

\subsection*{3.11.3 ARGUMENT GLOSSARY}

\subsection*{3.11.3.1 BEG_STEP}

This argument defines the number of the first step to be computed in a given nonlinear analysis interval. It is important primarily for analysis re-starts. Initially, BEG_STEP should be set to 1 . To continue an analysis in a subsequent run, after having computed and saved " \(n\) " steps in the previous run, one would typically set BEG_STEP equal to " \(\mathrm{n}+1\) ". For example, if the 10 th step was successfully completed in the first run, then it could be continued in a second run by setting BEG_STEP \(=11\). However, it is not necessary for BEG_STEP to be larger than any previously computed step. That is, you may re-compute a sequence of steps by setting BEG_STEP to the number of the first step to be re-computed. The procedure will automatically use the step that immediately precedes BEG_STEP (e.g., BEG_STEP-1) to obtain the necessary initial displacements, velocities, and accelerations.

\subsection*{3.11.3.2 BEG_TIME}

The starting problem time. For the initial run, the value of this parameter is usually set to zero.

\subsection*{3.11.3.3 COROTATION (default \(=\langle\) true \(>\) )}

Corotational update switch for large-rotation problems. This switch should be set to <true> when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate eiement Processor ( \(\mathrm{ES} \mathrm{S}_{i}\) ) section in the Testbed User's Manual for specific guidelines.

\subsection*{3.11.3.4 DEBUG (default \(=<\) false \(>\) )}

Procedure debug switch. This switch should only be turned on to obtain additional diagnostic printout for procedure debugging.

\subsection*{3.11.3.5 DEL_TIME}

The initial time step. If all goes well with the integration, this will be the time increment throughout the analysis. For restart, it is possible to use the time increment that was in force for the previous run. For restart only, input zero to cause the procedure to read in and use the previous DEL_TIME.

\subsection*{3.11.3.6 DESITERS (default = 4)}

Desired number of iterations allowed for convergence at a given load step. This parameter is used to adaptively adjust the arclength increment from one load step to the next, by comparing DES_ITERS with the actual number of iterations required for convergence at the last step.

\subsection*{3.11.3.7 FT_PROC (default = FT_ZERO)}

FT-PROC is the name of a procedure that will obtain the load factor ( \(\lambda\) ) for the timedependent forcing function. For applied force loading, this factor is multiplied by the reference applied force vector to obtain the current load vector, i.e.,
\[
\mathbf{f}_{1}^{e x t}=\lambda(t) \overline{\mathbf{f}}^{-\boldsymbol{e x t}}
\]
where \(\overline{\mathbf{f}}^{e x t}\) is the reference applied force vector stored in dataset APPL.FORC.1. For applied displacement loading, the starting load factor is applied to the reference applied displacement vector, which is then used to compute the initial internal force vector, i.e.,
\[
\mathbf{f}_{1}^{i n t(1)}=\mathbf{f}^{i n t}\left[\lambda(t) \overline{\mathbf{d}}^{e x t}\right]
\]
where \(\overline{\mathbf{d}}^{e x t}\) is the reference applied displacement vector stored in dataset APPL.MOTI.1. The user can supply any procedure he desires for FT_PROC. If this is the case, FT_PROC is the name of that procedure. FT_PROC has three arguments of its own. T is the current problem time, FT_ARGS is an array of up to six scalars, and F_MAC is the name of the macrosymbol (set by NL_DYNAMIC_1) to contain \(\lambda(t)\).

If the user wishes to use the FT procedures supplied here, he has four choices, as illustrated in Fig. 4.3-1.

FT ZERO This is the default option, which means that there will be no external forcing. FT.LIN Piecewise linear forcing function. FT_SIN Sinusoidal forcing function. FTEXP Exponential decay.

\subsection*{3.11.3.8 FT_ARGS}

These are the arguments to either the user-supplied forcing function, or required for FTLIN, FT_SIN, or FTEXP. For these last three procedures (supplied here), we offer the same options that are supplied with the code Structural Analysis of General Shells (STAGS). We have reproduced the forcing function diagram from the STAGS manual, which here appears as Fig. 4.3-1. In this figure, PA is the function \(\lambda(t)\), TIME is in units of problem time, and CA1 through CA6 are FTARGS[1:6], respectively. A summary for each each case follows:
For FT_LIN (piecewise linear time dependence), the array is as follows:

FT_ARGS[1] Maximum load factor (CA1 in figure).
FT_ARGS[2] Delay time before applied load ramps up (CA2). Can be zero.
FT_ARGS[3] Time at which load reaches maximum (CA3). Can be equal to FT_ARGS[2].
FT_ARGS[4] Time at which load begins to drop (CA4). Can be equal to FT_ARGS[3] if FT_ARGS[3] is not equal to FT_ARGS[2].
FT_ARGS[5] Time at which load drops (CA5).
FT_ARGS[3:5] can be safely set to larger than MAX_TIME if that is what the user wants.

For FT_SIN (sinusoidal time dependence), the array is as follows:
FT_ARGS[1] Peak height of sine wave (see Fig. 4.3-1, CA1)
FT_ARGS[2] Load offset for the sine wave function (CA2). If zero, the sine wave will oscillate to plus/minus FT_ARGS[1].
FT_ARGS[3] Half wavelength (CA3).
FT_ARGS[4] Problem time to first maximum load (CA4).
FT_ARGS[5] Delay time to imposition of load (CA5).
FT_ARGS[6] Time at which all loading will terminate (can be a large number), or CA6 in Fig. 4.3-1.

For FT_EXP (Exponential decay), the array is as follows:
FT_ARGS[1] Peak height of exponential (see Fig. 4.3-1, CA1)
FT_ARGS[2] Delay time before any load is imposed (CA2). Can be zero.
FT_ARGS[3] Half life time of exponential decay.
FT_ARGS[4] This argument is not used. In the Fig. 4.3-1, CA4 must be half CA1. If this is not the case, then FT_ARGS[3] should be recomputed.

Figure 4.3-1 Load Factor Histories

\subsection*{3.11.3.8 INT PARS (default \(=1,0 ., 25, .5\) )}

The values contained in this array set the characteristics of the time integrator. INT_PARS[1] is Wilson's \(\theta\) interpolator (see Theory, Section 4.3.9), INT_PARS[2] is \(\alpha\), and INT_PARS[3:4] are the Newmark \(\beta\) and \(\gamma\) parameters, respectively. A sophisticated user can reset these parameters for special integrator performance characteristics. Unless there is reason to tinker with their default values, it is better for the user to leave these parameters alone.

\subsection*{3.11.3.10 LOAD_STIFF / (default \(=<\) false \(>\) )}

If true, include load stiffness in the total stiffness matrix assembly.

\subsection*{3.11.3.11 MAX_CUTS (default=3)}

Maximum number of step cuts permitted during the current nonlinear analysis interval. A step cut refers to a halving of the arclength increment used to advance the solution from one step to the next. Step cuts are performed only if the maximum number of iterations are exceeded without converging at a given load step. Note that the relationship between the increment in "arclength" and the increment in the load-factor, \(\lambda\), is computed internally by the procedure.

\subsection*{3.11.3.12 MAX_TIME}

Problem time for which the analysis is to be terminated.

\subsection*{3.11.3.13 MAX_ITERS}

Maximum number of iterations allowed for convergence at a given load step. This parameter is used to terminate the iteration process at a given load level. If convergence hasn't been obtained after MAX_ITERS iterations, the load (i.e., arclength) increment is cut in half and the step is repeated - until either convergence has been obtained or MAX_CUTS has been exceeded.

\subsection*{3.11.3.14 MAX_STEPS}

Maximum number of load steps to compute in the current nonlinear analysis run. This provides an implicit limit on analysis run-time. The transient analysis is thus terminated whenever MAX_STEPS or MAX_TIME is exceeded - whichever comes first.

\subsection*{3.11.3.15 NL_GEOM (default \(=2\) )}

Geometric nonlinearity level: 0,1 , or 2 . \(0 \Rightarrow\) the problem is geometrically linear; \(1 \Rightarrow\) geometric nonlinearity will be handled globally, e.g., using corotational updates only; and \(2 \Rightarrow\) nonlinear element strain-displacement relations should be used in addition to any global treatment of geometric nonlinearity. If COROTATION \(=<\) true>, options 1 and 2 refer to first-order and second-order corotation, respectively. The latter option can be significantly more accurate than the former for a given finite element model - depending on which element types are involved.

\subsection*{3.11.3.16 NOMINAL_DB (default = NOMINAL.GAL)}

Name of database (GAL file) where a step-wise history of important solution parameters and selected response variables is to be stored.

\subsection*{3.11.3.17 NOMINAL_DS (default = RESPONSE.HISTORY)}

Name of dataset, within database defined by argument NOMINAL_DB, where a stepwise history of important solution parameters and selected response variables is to be stored. See the CSM Testbed Dataset Manual, under dataset RESPONSE.HISTORY, for a description of the individual data records stored in this dataset.

\subsection*{3.11.3.18 N_SELECT (default \(=0\) )}

Number of user-selected displacement components to be saved in the dataset specified by argument NOMINAL_DS. Values for these displacement components, the locations and directions of which are specified by arguments SEL_NODES and SEL_DOFS, respectively, are stored at every time step.

\subsection*{3.11.3.19 SEL_DOFS (default \(=0\) )}

List of nodal DOF's at which displacement histories are to be saved in dataset [NOMINAL_DS]. There should be [N_SELECT] numbers in the list, in correspondence with the node numbers specified by argument SEL_NODES. Values of each number in the list must range between 1 and 6 , in correspondence to the nodal DOF sequence (e.g., \(\left.u, v, w, \theta_{x}, \theta_{y}, \theta_{z}\right)\) specified by the START command of Processor TAB.

\subsection*{3.11.3.20 SEL_NODES (default \(=0\) )}

List of node numbers at which displacement histories are to be saved in dataset [NOMINAL_DS]. There should be [N.SELECT] numbers in the list, and node numbers can be repeated if more than one nodal DOF is to be saved at a node. The corresponding nodal DOF for each entry is specified by argument SEL_DOFS.

\subsection*{3.11.3.21 TOL_E (default \(=1 . e-3\) )}

Error tolerance used to establish convergence of the nonlinear equilibrium iteration procedure at each load step. The iteration loop at a given step is terminated whenever the following condition is met:
\[
\epsilon \leq[\text { TOL_E }]
\]
where
\[
\epsilon=\sqrt{\frac{\mathbf{r}^{(i)} \cdot \delta \mathbf{d}^{(i)}}{\mathbf{r}^{(1)} \cdot \delta \mathbf{d}^{(1)}}}
\]
is the relative energy error norm, \(\mathbf{r}\) is the residual force vector, \(\delta \mathbf{d}\) is the iterative displacement change, and \(i\) is the iteration counter.

\subsection*{3.11.4 INPUT/OUTPUT DATASETS}
\begin{tabular}{|l|l|l|l|l|}
\hline Table 3.11-1 Datasets Input/Output by Procedure NL_DYNAMIC_1 \\
\hline Dataset & Description & Lib & Input & Output \\
\hline <ES_NAME>.EFIL.* & Element Computational Data & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline ES.SUMMARY & ES Processor Status & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline DEF.<ES_NAME>.* & Element Defn. (Connectivity) & 1 & \(\sqrt{ }\) & \\
\hline DIR.<ES_NAME>.* & Element EFIL Directory & 1 & \(\sqrt{ }\) & \\
\hline JDF1.BTAB.* & Model Summary & 1 & \(\sqrt{ }\) & \\
\hline JLOC.BTAB.* & Nodal Coordinates & 1 & \(\sqrt{ }\) & \\
\hline PROP.BTAB.* & Material/Section Properties & 1 & \(\sqrt{ }\) & \\
\hline QJJT.BTAB.* & Nodal Transformations & 1 & \(\sqrt{ }\) & \\
\hline TOT.DISP.step & System Displacement Vector & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline TOT.ROTN.step & Nodal Rotation Pseudovectors & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline TOT.VEL.step & System Velocity Vector & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline TOT.ACC.step & System Acceleration Vector & 1 & \(\sqrt{ }\) & \(\sqrt{ }\) \\
\hline REAC.FORC.step & System Internal Force Vector & 1 & & \(\sqrt{ }\) \\
\hline
\end{tabular}
where step is the time step number, and ranges consecutively from 1 to the total number of steps computed. We must emphasize here that if one wishes to solve an initial value problem with either nonzero initial velocities or displacements (and not a restart), the user must supply TOT.DISP. 0 and/or TOT.VEL.0. If they are not supplied, the procedure will initialize these to zero.

\subsection*{3.11.5 SUB-PROCEDURES AND PROCESSORS}
\begin{tabular}{|l|l|l|}
\hline Table 3.11-2 Sub-Procedures Invoked by Procedure NL_DYNAMIC_1 \\
\hline Procedure & Type & Function \\
\hline NL_DYNAMIC_1 & Internal & Main Procedure \\
\hline CHK_CONVD & Internal & Check convergence \\
\hline CONSTRAIN & Internal & Impose constraints on freedoms \\
\hline DEFND & Internal & Defines recursive macrosymbols \\
\hline ES & External & Element utility Procedure \\
\hline FACTOR & Internal & Factor stiffness matrix \\
\hline FORCE & Internal & Forms INTERNAL/EXTERNAL force vector \\
\hline FT_ZERO & Internal & Zero force-time history \\
\hline FT_IIN & Internal & Piecewise linear force-time history \\
\hline FT_SIN & Internal & Sinusoidal force-time history \\
\hline FT_EXP & Internal & Exponential decay force-time history \\
\hline MASS & Internal & Compute mass \\
\hline MASS_STIFF & Internal & Combine mass and stiffness matrices \\
\hline NL_INITD & Internal & Initialize datasets and set restart \\
\hline POSTRES & Internal & Save selected data, internal forces \\
\hline POSTSTPD & Internal & Save data for restart \\
\hline SOLVE & Internal & Solves linear equation systems \\
\hline STIFFNESS & Internal & Forms and assembles stiffness matrix \\
\hline
\end{tabular}

Table 3.11-3 Processors Invoked by Procedure NL_DYNAMIC_1
\begin{tabular}{|l|l|l|}
\hline Procedure & Type & Function \\
\hline AUS & Internal & Combines mass and stiffness matrices \\
\hline \(\mathbf{E}\) & Internal & Initializes EFIL datasets \\
\hline ESi & External & Element Processors based on GEP \\
\hline INV & Internal & Factors stiffness matrix \\
\hline SSOL & Internal & Solves linear equation systems \\
\hline VEC & Internal & Performs all vector/pseudo-vector algebra \\
\hline
\end{tabular}

\subsection*{3.11.6 LIMITATIONS}

Limitations spelled out in Sections 4.1.6.1 through 4.1.6.8 apply also to NL_DYNAMIC_1. In addition, the following limitations also exist:

\subsection*{3.11.6.1 No Damping Included}

No damping is included in this first version of NL_DYNAMIC_1. Damping that preserves the bandwidth of the problem will be included in a later version.

\subsection*{3.11.6.2 Initial Velocities and Displacements}

These are currently the responsibility of the user. NL_DYNAMIC_1 will expect to see data sets TOT.DISP. 0 and TOT.VEL. 0 for these types of problems. Currently, there is no way to initialize rotational triads. This is a topic for future development.

\subsection*{3.11.6.3 Diagonal Mass}

Currently, only diagonal mass can be used. This limitation will soon be removed.

\subsection*{3.11.6.4 AUS Limitation}

Due to hard wired data set naming conventions in processor AUS for system matrices (e.g. K.SPAR.36), the number of DOF's per node specified on the START command of processor TAB is presently restricted to be 6. AUS is currently essential to NL_DYNAMIC_1 for computing the sum of the mass and stiffness matrices to obtain the dynamic operator. This restriction will be removed when we make the connection to the Generic Matrix Processor.

\subsection*{3.11.7 ERROR MESSAGES}

\subsection*{3.11.7.1 "Non-Convergence at Step n. Revise Strategy."}

This message means that the maximum number of nonlinear iterations (MAX_ITERS) has been exhausted, as well as the maximum number of step cuts (MAX_CUTS), and convergence still hasn't been obtained at step \(n\). A possible cure is to re-start the analysis from several steps back, and decrease the arclength increment at that point (using the PATH_SCALE argument). However, just increasing MAX_ITERS or MAX_CUTS, or even TOL E, may also solve the problem. In other words, re-think the definition of all solution parameters based on the observed behavior of the solution algorithm just prior to the break-down.

\subsection*{3.11.7.2 "Divergence at Step n. Revise Strategy."}

This message has similar implications to the previous message, but it occurs when the error grows instead of decreases during two successive nonlinear iterations. The difference between divergence and non-convergence is that divergence cannot be cured by increasing MAX_ITERS; and probably should not be "cured" by increasing TOL_E. It generally
means that the step-size is too big - or that the error tolerance (TOL_E) has been too big all along, so that changes are occurring suddenly that should have been detected by the solution algorithm at earlier load steps. Thus, you might try re-starting from an earlier step, reducing PATH_INC, and possibly reducing TOL_E as well.

\subsection*{3.11.7.3 "Specified Displacements are Identically Zero"}

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed - in which case the message should be taken merely as a warning.

\subsection*{3.11.7.4 "Specified Forces are Identically Zero"}

This is not necessarily an abortive error. As long as either nonzero specified displacements or specified forces are defined, the solution can proceed - in which case the message should be taken merely as a warning.

\subsection*{3.11.8 USAGE GUIDELINES AND EXAMPLES}

\subsection*{3.11.8.1 Starting an Analysis}

To begin a nonlinear transient analysis with procedure NL_DYNAMIC_1, it is only necessary that the finite element model be defined. This does not require pre-formation of element stiffness matrices, node renumbering for optimal factorization time, or any form of linear analysis (unless initial geometric imperfections are based on linear displacement modes). Only nodal coordinates/transformations, material properties and element connectivity are pre-requisite to nonlinear analysis. To invoke procedure NL_DYNAMIC_1, only those arguments that don't have default values (see PROCEDURE USAGE section) need be specified.
For example, if you wanted to start an analysis with an initial time of 0 ., maximum time of .01 , a time step of .005 , and compute no more than 20 time steps with an initial velocity profile defined in data set TOT.VEL.0, you could invoke the procedure as follows:
\[
\begin{gathered}
\text { *call NL_DYNAMIC_1 ( BEG_STEP }=1 ; \text { MAX_STEPS }=20 ;- \\
\text { BEG_TIME }=.0 ; \text { MAX_TIME }=.1 ;- \\
\text { DEL_TIME }=0.005)
\end{gathered}
\]

Keep in mind that the number of time-steps actually performed during the above run will depend on whether convergence difficulties were encountered. If that happened, the step will be cut, and the number of steps to maximum time will be greater. Since it may be difficult to estimate this in advance, you may want to start with only a few time steps (e.g., set MAX_STEPS \(=3\) ) to get some experience, and later re-start the analysis with more steps allowed.

\subsection*{3.11.8.2 Re-Starting (or Continuing) an Analysis}

To re-start an analysis from a previously computed, converged solution, you need only specify the first step to compute, the maximum time, and any changes in the forcing function. The only requirement is that a previous complete set of solution data for a converged time step must be present on the database. If, for example, one wishes to restart from step 10 (compute beginning step 11), then the call could be
\[
\text { *call NL_DYNAMIC_1 } \begin{aligned}
& \text { BEG_STEP }=11 ; \text { MAX_STEPS }=100 ;- \\
& \text { MAX_TIME }=.1 ; \text { DEL_TIME }=0 . ;- \\
& \text { FT_PROC }=\text { FT_LIN } ; \text { FT_ARGS }=100 ., 0 ., 0 ., 1 .)
\end{aligned}
\]

In this case, the user wants to restart the previous example at time .05 with the sudden imposition of a step forcing function with scaled magnitude of 100 . By examining Fig. 4.3-1, one can see that the step load is to be continued well beyond the termination time. FTLIN is one of the procedures supplied here.
It is also possible to modify integration parameters and the time step, as well as any of the other applicable procedure arguments. Note that the parameter DEL_TIME is always required. The value zero is used to tell the procedure to look into the database for the last value. A nonzero value for this parameter overrides the time step saved in the data base.

\subsection*{3.11.も THEORY}

\subsection*{3.11.9.1 Introduction}

Procedure NL_DYNAMIC_1 performs a nonlinear transient analysis of a system using a time integration algorithm that has adjustable parameters which allow for the automatic selection of a family of related transient analyzers. All of them are self starting, require no "historical" vectors, and for a useful range of parameters, are unconditionally stable. All are based on discrete matrix equations of motion that may or may not include damping. The internal and external force vectors can be nonlinear functions of the displacements (unknowns).

\subsection*{3.11.9.2 Development of the Algorithm}

The discrete form of the equations of motion are
\[
\begin{equation*}
\mathbf{M} \ddot{\mathbf{u}}+\mathbf{f}^{\mathbf{i n t}}(\mathbf{u})=\mathbf{f}^{e x t} \tag{3.11-5}
\end{equation*}
\]
where for simplicity we have omitted damping, and where the dependence of the internal forces on displacement and the external forces has been emphasized. Here \(\mathbf{M}\) is the mass matrix, \(\mathbf{u}\) is the displacement, and dots over quantities refer to differentiation with respect to time. Our goal is to find a discrete solution to (69) at time \(t+\Delta t\) (step \(n+1\) ), given information at time \(\boldsymbol{t}\) (step \(\boldsymbol{n}\) ). In order to do this, we need additional relations between the displacements, velocities, and accelerations being solved for.

We begin with a two parameter family of the equations of motion (69) discretized in time as follows:
\[
\begin{equation*}
\mathbf{M a} a_{n+\theta}+(1+\alpha) \mathbf{f}^{i n t}\left(\mathrm{~d}_{n+\theta}\right)-\alpha \mathrm{f}^{i n t}\left(\mathrm{~d}_{n}\right)=\mathrm{f}_{n+\theta}^{e x t} \tag{3.11-6}
\end{equation*}
\]
where \(d_{n+\theta}\) and \(a_{n+\theta}\) are the approximations to the displacement and acceleration at time \((n+\theta) \Delta t\), and where Wilson's \(\theta\) interpolation parameter is used to obtain the desired acceleration according to
\[
\begin{equation*}
\mathbf{a}_{n+\theta}=(1-\theta) \mathbf{a}_{n}+\theta \mathbf{a}_{n+1} \tag{3.11-7}
\end{equation*}
\]

The parameter \(\alpha\) is a measure of the "degree of implicitness" of the integrator. If \(\alpha\) is 0 , the equations of motion are to be satisfied at some point \(\theta\) greater than unity. If \(\alpha=-1\), we have an explicit system, with the acceleration extrapolated from values at the previous step.

To relate the velocity and acceleration to the displacements at the point \(n+\theta\), we introduce the two standard Newmark parameters \(\beta\) and \(\gamma\) :
\[
\begin{gather*}
\mathbf{v}_{n+\theta}=\mathbf{v}_{n}+\theta \Delta t\left[(1-\gamma) \mathbf{a}_{n}+\gamma \mathbf{a}_{n+\theta}\right]  \tag{3.11-8}\\
\mathbf{d}_{n+\theta}=\mathbf{d}_{n}+\theta \Delta t \mathbf{v}_{n}+(\theta \Delta t)^{2}\left[\left(\frac{1}{2}-\beta\right) \mathbf{a}_{n}+\beta \mathbf{a}_{n+\theta}\right] \tag{3.11-9}
\end{gather*}
\]

Eq. (72) is required when damping is present. If we define the known quantity
\[
\begin{equation*}
\tilde{\mathbf{d}}_{n+\theta}=\mathbf{d}_{n}+\theta \Delta t \mathbf{v}_{n}+(\theta \Delta t)^{2}\left(\frac{1}{2}-\beta\right) \mathbf{a}_{n} \tag{3.11-10}
\end{equation*}
\]
then, using (73), we have
\[
\begin{equation*}
\mathbf{d}_{n+\theta}=\tilde{\mathbf{d}}_{n+\theta}+(\theta \Delta t)^{2} \beta \mathbf{a}_{n+\theta} \tag{3.11-11}
\end{equation*}
\]

If we multiply Eq. (70) by \((\theta \Delta t)^{2} \beta\) and eliminate \(a_{n+\theta}\) using (74), we obtain
\[
\begin{equation*}
\mathbf{M d}_{n+\theta}+(\theta \Delta t)^{2} \beta(1+\alpha) \mathbf{f}^{i n t}\left(\mathbf{d}_{n+\theta}\right)-\tilde{\mathbf{f}}_{n+\theta}=0 \tag{3.11-12}
\end{equation*}
\]
where the quantity \(\overline{\mathrm{f}}_{n+\theta}\) is known from the last converged time step:
\[
\begin{equation*}
\tilde{\mathbf{f}}_{n+\theta}=(\theta \Delta t)^{2} \beta\left[\mathbf{f}_{n+\theta}^{e x t}+\alpha \mathbf{f}^{i n t}\left(\mathbf{d}_{n}\right)\right]+\mathbf{M} \tilde{\mathbf{d}}_{n+\theta} \tag{3.11-13}
\end{equation*}
\]

Eq. (77) is a nonlinear system of equations which must be solved for \(\mathrm{d}_{n+\boldsymbol{\theta}}\); these displacements will be solved for using an extrapolated starting solution followed by modified Newton corrections. The solution of this system is very similar to what is in NL_STATIC_1, with the exception of the arclength constraint and load factor equation. Thus, solution of (77) proceeds like a fixed-step static algorithm with a modified "stiffness" matrix and residual vector. In the algorithm description, these are labeled the dynamic operator and dynamic residual, respectively.

\subsection*{3.11.9.3 Derivation of the Dynamic Operator and Residual}

The derivation of the dynamic operator and residual follows directly from the linearization of (77). Using a procedure similar to that for static analysis, we carry out a Taylor expansion of (77) and drop all terms of order higher than first. The result is the system
\[
\begin{equation*}
\left[\mathbf{M}+(\theta \Delta t)^{2} \beta(1+\alpha) \mathbf{K}\left(\mathbf{d}_{n+\theta}^{(0)}\right)\right] \delta \mathbf{d}_{n+\theta}^{(i)}=\bar{f}_{n+\theta}^{(i)} \tag{3.11-14}
\end{equation*}
\]
where
\[
\begin{equation*}
\overline{\mathbf{f}}^{(i)}=\tilde{\mathbf{f}}_{n+\theta}-\mathbf{M d}_{n+\theta}^{(i-1)}-(\theta \Delta t)^{2} \beta(1+\alpha) \mathbf{f}^{i n t}\left(\mathrm{~d}_{n+\theta}^{(i-1)}\right) \tag{3.11-15}
\end{equation*}
\]
is the dynamic residual. Here
\[
\begin{equation*}
\widetilde{\mathbf{f}}_{n+\theta}=(\theta \Delta t)^{2} \beta\left[\mathbf{f}^{e x t}\left(t_{n+\theta}\right)+\alpha \mathbf{f}^{i n t}\left(\mathbf{d}_{n}\right)\right]+\mathbf{M} \widetilde{\mathbf{d}}_{n+\theta} \tag{3.11-16}
\end{equation*}
\]
which is computed from information known at the previous step or computed from the known external forcing function. \(\delta \mathrm{d}_{n+\theta}^{(i)}\) is the vector of unknown displacement increments at iteration \(i\), time point \(t+\theta \Delta t\). One can tell that this is a modified Newton sequence, because of the argument of the stiffness matrix in (78). For true Newton, one would have to reform and refactor the stiffness matrix using the latest displacement information.

\subsection*{3.11.9.4 Recovery of Quantities at Step \(n+1\)}

Once the displacements at point \(t+\theta \Delta t\) are known, we need to update the accelerations and compute the new velocities and displacements at the desired new step. Starting with \(\mathbf{d}_{n+\theta}\), we use the second of (73) to solve for \(a_{n+\theta}\). Introducing (74), the equation for the acceleration becomes
\[
\begin{equation*}
a_{n+\theta}=\frac{1}{(\theta \Delta t)^{2} \beta}\left(d_{n+\theta}-\tilde{d}_{n+\theta}\right) \tag{3.11-17}
\end{equation*}
\]

We now require the accelerations, velocities, and displacements at time step \(n+1\). Using (72), we have for \(a_{n+1}\)
\[
\begin{equation*}
\mathbf{a}_{n+1}=\frac{1}{\theta} \mathbf{a}_{n+\theta}+\left(1-\frac{1}{\theta}\right) \mathbf{a}_{n} \tag{3.11-18}
\end{equation*}
\]

Eqs. (72) and (73) can then be used with \(\theta=1\) to interpolate velocities and displacements to step \(n+1\), given the new and old accelerations:
\[
\begin{align*}
& \mathbf{v}_{n+1}=\mathbf{v}_{n}+\Delta t\left[(1-\gamma) \mathbf{a}_{n}+\gamma \mathbf{a}_{n+1}\right. \\
& \mathbf{d}_{n+1}=\mathbf{d}_{n}+\Delta t \mathbf{v}_{n}+\Delta t^{2}\left[\left(\frac{1}{2}-\beta\right) \mathbf{a}_{n}+\beta \mathbf{a}_{n+1}\right] \tag{3.11-19}
\end{align*}
\]

\subsection*{3.11.9.5 The Composition of New Displacements and Velocities}

Whenever a new velocity vector is to be updated from a previous vector, the increment is simply added to the vector. For displacements, however, only the translations are handled this way. The rotational triads must be updated by the product rule, covered in Section 4.1.9.10. NL_DYNAMIC_1 is no different from NL_STATIC_1 in this respect. However, the reader will notice that the vector \(\widehat{\mathbf{d}}_{n+\theta}\) is treated like a velocity, with no accompanying rotational update. The reason is that \(\hat{\mathrm{d}}_{\boldsymbol{n}+\boldsymbol{\theta}}\) eventually ends up as part of an incremental quantity used to account for inertial effects in the dynamic residual. The rotational freedoms in this vector are accumulated like their translational counterparts. To avoid confusion in the algorithm description, compositions that require special rotational treatment will be denoted by the symbol \(\oplus\). Again, this is similar to the static case.

\subsection*{3.11.9.6 The Integration Parameters}

The integration parameters allow the user to taylor the integrator to the special needs of his problem. The following table defines what we mean by each parameter. For detailed information on the various integrator options, the reader should consult references at the end of this section.
\begin{tabular}{|l|c|}
\hline Parameter & Name \\
\hline\(\beta, \gamma\) & Newmark Parameters \\
\(\theta\) & Wilson's Collocation Parameter \\
\(\alpha\) & Dissipation Parameter \\
\hline
\end{tabular}

Table 3.11-4 Parameter names used in the NL_DYNAMIC Procedure.
Special choices of these parameters select out well known integrators whose behavior has been studied extensively. These integrators, the parameter choices, and their regions of stability for stiff linear systems can be found in the following table.
\begin{tabular}{|c|c|c|c|c|c|}
\hline Algorithm & \(\alpha\) & \(\boldsymbol{\beta}\) & \(\boldsymbol{\gamma}\) & \(\theta\) & Remarks \\
\hline Newmark & 0 & & & 1 & Implicit and unconditionally stable when \(2 \beta \geq \gamma \geq \frac{1}{2}\) \\
\hline Trapezoidal & 0 & \(\frac{1}{4}\) & \(\frac{1}{2}\) & 1 & Implicit and unconditionally stable \\
\hline Linear Acceleration & 0 & \(\frac{1}{6}\) & \(\frac{1}{2}\) & 1 & Implicit and conditionally stable \\
\hline Fox-Goodwin & 0 & \(\frac{1}{12}\) & \(\frac{1}{2}\) & 1 & Implicit and conditionally stable \\
\hline Central Difference & 0 & 0 & \(\frac{1}{2}\) & 1 & Explicit and conditionally stable \\
\hline Wilson- \(\theta\) & 0 & \(\frac{1}{6}\) & \(\frac{1}{2}\) & & Implicit and unconditionally stable when \(\theta \geq 1.366025\) \\
\hline Collocation & 0 & & \(\frac{1}{2}\) & & Implicit and unconditionally stable when \(\theta \geq 1\) and \(\frac{\theta}{2(\theta+1)} \geq \beta \geq\) \(\frac{2 \theta^{2}-1}{4\left(2 \theta^{3}-1\right)}\) \\
\hline \(\boldsymbol{\alpha}\)-Method & & & & 1 & Implicit and unconditionally stable when \(-\frac{1}{3} \leq \alpha \leq 0, \gamma=\) \(\frac{1}{2}(1-2 \alpha)\) and \(\beta=\frac{1}{4}(1-\alpha)^{2}\) \\
\hline
\end{tabular}

Table 3.11-5. Some properties of the algorithms that can be produced using NL.DYNAMIC_1 through the \(\alpha, \beta, \gamma\), and \(\theta\) parameters.

\subsection*{3.11.10 ALGORITHM}

\section*{General Algorithm}
(1) INITIALIZATION
(1.1) Initialize \(\alpha, \beta, \gamma, \theta\).
(1.2) Initialize \(d_{0}, v\).
(1.3) Compute time at \(\theta\)
\[
t_{\theta}=t_{0}+\theta \Delta t
\]
(1.4) Compute weighted out-of-balance force
\[
\overline{\mathbf{f}}=\beta \mathbf{f}^{e x t}\left(t_{\theta}\right)+\left(\frac{1}{2}-\beta\right) \mathbf{f}^{e x t}\left(t_{0}\right)+\mathbf{f}^{i n t}\left(\mathrm{~d}_{0}\right)\left[\beta(1+\alpha)-\frac{1}{2}\right]
\]
(1.5) Add inertial terms
\[
\tilde{\mathbf{f}}_{\theta}=\mathbf{M}\left(\mathbf{d}_{0}+\theta \Delta t \mathbf{v}_{0}\right)+(\Delta t \theta)^{2} \overline{\mathbf{f}}
\]
(1.6) Compute initial estimate of displacements
\[
\mathbf{d}_{\theta}^{(0)}=\mathbf{d}_{0} \oplus \theta \Delta t \mathbf{v}_{0}
\]
(1.7) Compute initial dynamic residual
\[
\mathbf{f}^{(i)}=\tilde{\mathbf{f}}_{n+\theta}-\mathbf{M d}_{n+\theta}^{(i-1)}-(\theta \Delta t)^{2} \beta(1+\alpha) \mathbf{f}^{i n t}\left(\mathbf{d}_{n+\theta}^{(i-1)}\right)
\]
(1.8) Set \(n=0, t=t_{0}+\Delta t, n_{b e g}=1\)
(2) STEP LOOP: for \(n=n_{b e g}, n_{b e g}+1, \ldots\)
(2.1) Form and Assemble Stiffness Matrix based on predicted displacements
(2.2) Compute the Dynamic Operator
\[
\mathbf{E}=\left[\mathbf{M}+(\theta \Delta t)^{2} \beta(1+\alpha) \mathbf{K}\left(\mathbf{d}_{n+\theta}^{(0)}\right)\right]
\]
(3) ITERATION LOOP: \(\mathrm{i}=1,2, \ldots\) (iter \(=\mathrm{i}+1=2,3, \ldots\) )
(3.1) Solve for incremental displacement change
\[
\mathbf{E} \delta \mathbf{d}_{n+\theta}^{(i)}=\overline{\mathrm{f}}_{n+\theta}^{(i)}
\]
(3.2) Update displacements
\[
\mathbf{d}_{n+\theta}^{(i)}=\mathbf{d}_{n+\theta}^{(i-1)} \oplus \delta \mathbf{d}_{n+\theta}^{(i)}
\]
(3.3) Set iteration counter
\[
i \leftarrow i+1
\]
(3.4) Compute new Dynamic Residual
\[
\bar{f}^{(i)}=\widetilde{\mathbf{f}}_{n+\theta}-\mathbf{M d}_{n+\theta}^{(i-1)}-(\theta \Delta t)^{2} \beta(1+\alpha) \mathrm{f}^{i n t}\left(\mathrm{~d}_{n+\theta}^{(i-1)}\right)
\]
(3.5) Check Convergence
call CHK_CONV ( \(\mathbf{r}_{n+1}^{(i+1)}, \delta \mathbf{d}, \widehat{\epsilon}^{(i)}, \epsilon_{\text {ref }}, \widehat{\epsilon}_{\text {tol }}\), num_div \(\rightarrow\)
\(\widehat{\epsilon}^{(i+1)},<\) CONVERGED \(>,<\) DIVERGED> )
if ( <CONVERGED> ) then
numiters_required \(=\) iter
\(\boldsymbol{n} \leftarrow \boldsymbol{n}+1\)
go to (2.3) STEP LOOP
elseif (<DIVERGED> .or. (iter > maxiters) ) then
if ( num_cuts < max_cuts) then
\(\Delta t_{n+1}=\Delta t_{n+1} / 2\)
num_cuts \(=\) num_cuts +1
\(n_{\text {beg }}=n\)
GO TO (1.3)
else
STOP
endif else
go to (3) ITER LOOP
endif
(2.3) Compute acceleration at \(n+\theta\)
\[
\mathbf{a}_{n+\theta}=\frac{1}{(\theta \Delta t)^{2} \beta}\left(\mathbf{d}_{n+\theta}-\tilde{\mathbf{d}}_{n+\theta}\right)
\]
(2.4) Compute acceleration at \(n+1\)
\[
\mathbf{a}_{n+1}=\frac{1}{\theta} \mathbf{a}_{n+\theta}+\left(1-\frac{1}{\theta}\right) \mathbf{a}_{n}
\]
(2.5) Extract velocities
\[
\mathbf{v}_{n+1}=\mathbf{v}_{n}+\Delta t\left[(1-\gamma) \mathbf{a}_{n}+\gamma \mathbf{a}_{n+1}\right]
\]
(2.6) If \(\theta \neq 1\), recompute displacements
\[
\mathbf{d}_{n+1}=\mathbf{d}_{n} \oplus\left\{\Delta t \mathbf{v}_{n}+\Delta t^{2}\left[\left(\frac{1}{2}-\beta\right) \mathbf{a}_{n}+\beta \mathbf{a}_{n+1}\right]\right\}
\]
(2.7) Update counters, timestep
\[
n \leftarrow n+1 ; \quad t \leftarrow t+1
\]
(2.8) Check to see if \(t>t_{\max }\) or \(n>n_{\max }\)
\[
\text { (2.9) If either statement in } 2.8 \text { is true, STOP; else GO TO } 2.10
\]
(2.10) Compute \(\tilde{\mathbf{d}}_{n+\theta}\)
\[
\tilde{\mathbf{d}}_{n+\theta}=\mathbf{d}_{n}+\theta \Delta t \mathbf{v}_{n}+(\theta \Delta t)^{2}\left(\frac{1}{2}-\beta\right) \mathbf{a}_{n}
\]
(2.11) Compute external loads \(\mathrm{f}^{e x t}(t)\) at current time \(t\)
(2.12) Compute \(\widetilde{f}_{n+\theta}\)
\[
\widetilde{\mathbf{f}}_{n+\theta}=(\theta \Delta t)^{2} \beta\left[\mathbf{f}^{e x t}\left(t_{n+\theta}\right)+\alpha \mathbf{f}^{i n t}\left(\mathbf{d}_{n}\right)\right]+\mathbf{M} \widetilde{\mathbf{d}}_{n+\theta}
\]
(2.13) Compute initial estimate of new solution
\[
\begin{aligned}
\Delta \mathbf{d}_{n+\theta} & =\tilde{\mathbf{d}}_{n+\theta}+(\theta \Delta t)^{2} \beta \mathbf{a}_{n}-\mathbf{d}_{n} \\
\mathbf{d}_{n+\theta}^{(0)} & =\mathbf{d}_{n} \oplus \Delta \mathbf{d}_{n+\theta}
\end{aligned}
\]
(2.14) END STEPLOOP

\section*{NOTATION}
\begin{tabular}{|c|c|}
\hline d & Displacement vector. \\
\hline \(v\) & Velocity vector. \\
\hline a & Àcceleration vector. \\
\hline \(\delta\) d & Iterative change in d. \\
\hline d & Extrapolated displacement from step n \\
\hline \(\widehat{f}^{\text {ext }}\) & External force vector - base load. \\
\hline \(\mathrm{f}^{\text {int }}\) & Internal force vector. \\
\hline \(\mathrm{f}^{\text {ext }}\) & External force vector. \\
\hline f & Extrapolated out-of-balance force. \\
\hline \(\overline{\mathbf{f}}\) & The dynamic residual. \\
\hline K & Stiffness matrix. \\
\hline num_cuts & Number of times load step has been cut in half at current step. \\
\hline num-div & Number of consecutive iterations at which divergence occurs. \\
\hline \(\widehat{\epsilon}\) & Relative error in energy norm. \\
\hline \(\boldsymbol{\epsilon}\) & Absolute error in energy norm. \\
\hline \(\epsilon_{\text {ref }}\) & Reference value of \(\epsilon\); initialized as zero. \\
\hline \(\epsilon_{\text {tol }}\) & Relative error tolerance (default: \(10^{\mathbf{- 4}}\) ). \\
\hline \(\lambda\) & Load factor. \\
\hline \(\hat{\mathbf{d}}^{\prime}\) & Base value of specified displacement vector. \\
\hline \(\mathrm{d}^{\prime}\) & Current value of specified displacement vector. \(\mathbf{d}^{\mathbf{z}}=\lambda \hat{\mathbf{d}}^{\mathbf{3}}\). \\
\hline \(t\) & Problem time. \\
\hline \(\Delta t\) & Time increment. \\
\hline \(n+\theta\) & Time at step \(n+\theta \Delta t\) \\
\hline
\end{tabular}

\subsection*{3.11.11 PROCEDURE LISTING}
```

*procedure NL_DYMAMIC_1 ( --
bog_step =1 ; -- . Starting step numbor (>0)
max_steps=1 ; -- . Maximus steps to compute
max_iters=9 ; -- . Maximum iterations por stop
des_iters=4 ; -- . Number of iterations desired
fac_stops=1 ; -- . Steps_per_refactoring
max_cuts=3 ; -- . Maxinue number of stop cuts
tol_ब=1.E-3 ; -- . Energy error tolerance
beg_tine ; -- . Starting tine
max_time ; -- . Upper_bound on tile
del_time ; -- . Time increment
int_pars = 1.,0.,.25,.5 ; -- . Itegration parametors
load_stiff=<false> ; -- . Include load stiffness
FT_proc=FT_ZERO ; -- . Name of force-tine procedure
FT_arg: ; -- . Parametor array for above
debug=<PALSE>; -- . Debug_print suitch
NL_GEOK = 2 ; -- . Geon. Nonlin. Level (1|2)
COROTATION=1 ; -- . Corotational Flag (leave on!!)
Nominal_DB = NOMINAL.GAL ; -- . Selected Output
Nominal_DS = RESPONSE.HISTORY ; --
N_SELECT ; SEL_NODES; SEL_DOFS --
)
*Renark
*Renark I I
*Renark NL_DYNAMIC_1
*Renark
Henerk CSM Testbed Procedure for Nonlinear Statics:
*Renark
*Ronark O Corotational Nevton/Raphson algorithm
*Rozark o Linearized Crisfield/Riks arc-length control
*Remerk O Applied forces and/or displacements
*Rozark
*Renark Authors: G.M. Stanley and C.C. Rankin
\#Remark Fersion: MAR-03-1988
*Renark I I
*lonark
initializition
*dof/i ns_overwrite == <false>
*def/i debug == [debug]
*def/i nax_stop == <[beg_step]+[nax_steps]-1>
*def/i num_iters a= [des_iters]
*def/a NOM_DB == [Nominal_DB]
*def/a NOM_DS == [Nominal_DS]
*dof/i N_SELECT }==\mathrm{ [N_SELECT]
*def/1 SEL_NODES[1:<N_SELECT>] == [SEL_NODES]
*def/i SEL_DOPS[1:<N_SELECT>] == [SEL_DOFS]
*def/i ML_GEOM == [NL_GEOM]
*def/i cOROTATION == [COROTATION]

```
```

\#äifa bag_time == [bog_time]
*def/d max_time == [max_time]
*def/d int_pars[1:4] = [int_pars]
. . . . . Set time integration parametarg
*def/d thota =x <int_pars[1]>
*def/d alpha == <int_pars[2]>
*def/d nemm_bet == <int_pars[3]>
*def/d nemm_gan =x <int_pars[4]>
. . . . . Initialize dataset names, constants
*CALL DEFND ( STEP = [BEG_STEP]; ITER = 0)
*IF [BEG_STEP] /EQ 1 /THEN
*Renark INITIALIZATION:
*call NL_INITD
*def/d t =x [beg_time]
*def/d dt =x [del_time]
*olse
*if < [del_time] /eq 0.0>/thon
*def/d dt = = <dt_n>
*olse
*def/d dt =r [del_tine]
*ondif
*def/d =w<t_n>
*endif
. . . Set initial step, initial iteration parameters
*dof/i pass == 1
*dof/i tot_iters == 1
*def/i istop == [bog_stop]
. . . . Set initial time, basic tine integration scalars
*dof/d one_p_alp == <1. + <alpha>>
*dei/d b_op_a == <<\piewn_bet\rangle*\langleone_p_alp\rangle\rangle
*def/d h_m_bet s= <.5 - <nemn_bet>>
*def/d o_d_th == <1./<thete>>
*def/d O_m_odth }==\langle1. - <0_d_th>>
*de1/d O_m_gan z= <1. - <nomn_gan>>
. . . . Rointery for problon restart on failure of convergence
. . . . Syster is treated as a nev initial value problem
:NEU_PISS . Le-entry point for step-size reduction
. . . . Set itoration and step-independent integration scalars
*def/d th_dt == <<theta>*<dt>>
*def/d t_wil: == <<t> + <th_dt>>
*det/d th_dt_sq = = <<th_dt>*<th_dt>>

```
```

*def/d th_b =m <<nemm_bet>*<th_dt_sq>>
*def/d a_th_b == <<th_b> * <alpha>>
*def/d O_d_thb == <1./<th_b>>
*def/d f0_coef = = <<b_Op_a> - .5>
*def/d k_coeff a= <<th_dt_sq>*<b_op_a>>
*def/d v_n_cooff == <<dt>*<o_m_gan>>
*def/d v_np1_cooff == <<dt>*<nevn_gan>>
*def/d dtsq == <<dt>*<dt>>
*def/d h_mb =m <<dtsq>*<h_m_bet>>
*dof/d dt_b mx <<dtsq>*<nemn_bot>>
*def/d h_mb_th z= <<th_dt_sq>*<h_m_bet>>
. . . . Set initial displacenent estinate, first step
. . . . Set initial estimate of weighted out-of-balance forces
. . . . Compute external force meighting constant lambda_n(tine)
*call [PT_proc] ( T = <t> ; -- . Problen tine
FT_ args = [ft_args] ; -- . Force-time pareneters
F_mac = lambda_n ) . External forcing scale factor
*call PORCE ( type = EXTERNAL ; --
nl_geom = [nl_geon] ; --
nl_load = <true> ; --
displacenent = <d_n>
rotation = <T_n>
corotation = [corotation] ; --
load_factor = <lambda_n> ; --
input_force = <P_ref> ; --
output_iorce = <P_ext> )
. . . . Set intornal force
*call FORCE ( type = INTERNAL ; -
nl_geon =[nl_ge0n] ; --
displacenent = <d_n\rangle ; --
rotation = <T_n\rangle ; --
corotation = [corotation] ; --
output_force = <F_int> )
|top_1
*stop
. . . Heighted difference between internal and external force
[XQT VEC
<a_th> <- <f_ext> - <f_int>
<f_bar> <- <h_n_b\bullett> <P_ext> + <fO_coef\rangle <P_int>
. . . . External force at tine = T + <theta> * DT
*call [FT_proc] ( T = <t_wils> ; -- . Problen time
FT_ args = [ft_args] ; -- . Force-tine pareneters
F_mac = lambda_np1 ). External forcing scale factor
*call FORCE ( type = ExTERNAL ; --

```
```

            nl_geon = [nl_geon] ; --
            nl_load = <true\rangle ; --
            displacement = <d_n> ; --
            rotation = <T_n\rangle ; --
            córotbetion a [coniotetioñ] ; --
            load_factor = <lambda_npi> ; --
                    input_force = <P_ret\rangle ; --
                    output_force = <P_ext\rangle )
    . . . . Add correction to external force
[xQT VEC
<f_bar> <- <f_bar> + <newn_bet> <F_ext>
<I_bar> <- <th_dt_sq> <I_bar>
. . . . Initial estimate of displaconents
<delta> <- <th_dt> <v_n>
<d_np1_i\rangle <- <d_n\rangle + \langledelta\rangle
HOTATE <T_n> * <delta> -> <T_np1_i>
<d_tilde> <- <d_npi_i>
. . . . Scaling displacement increment for convergence check
stop_2 *stop
PRDD <inv_mass> <n_th> -> <d_inc_i>
<d_inc_i\rangle <- <h_mb_th> <d_inc_i\rangle + <delta\rangle
. . . . Mass * Displacenents + scaled out-oi-balance force
PROD <ness> <d_mp1_i\rangle -> <t_tilde\rangle
<1_tilde> <- <i_tilde> + <1_bar>
-
*

```

```

* 

*DO :STEP_LOOP in = <istep>, <[max_steps]-1>
*def/i step == <<n>
*Romark
*romark
Hromark
*Remark BEGINNING STEP <STEP>
\#remark
\#renark
*call COMSTRAIN ( load_factor = <lanbda_np1 > ; --
applied_motion = <d_spec\rangle ; --
displacement = <d_np1_i\rangle
. . . Porm Stiffness based on Predictor

```
```

*call STIPFNESS ( type = TANGENT ; --
nl_geon = [nl_geon]
nl_load = [lond_stiff]
load_factor = <lambda_np1> ; --
displacenent = <d_np1_i\rangle ; --
rotation = <T_np1_i\rangle ; --
corotation = [corotation] ; --
stiffness = <K_asn> ) . output
. . . Conbine MASS and STIFFNESS into one matrix <M_P_K>
*call MASS_STIFF ( nass = <nass> ; -- . Mase vector
stif = <K_asc> ; -- . Lssembled Stiffness
mult = <k_cooff> ; -- . Stiffness Multiplior
M_P_K = <M_P_K> ) . The dynamic operator
. . . Factor DYNAMIC OPERATOR
*call PACTOR ( input_matrix = <M_P_K> ; --
output_matrix= <M_P_K> )
. . . Obtain mass residjal
*call PORCE ( type = INTERNAL ; -
nl_geom : [nl_geon] ; --
displacenent = <d_np1_i\rangle ; ; --
corotation = [corotation] ; --
output_force = <F_int>)
. stop_3 *stop
[XQT VEC
PROD <nass> <d_np1_i\rangle -> <R_np1_i\rangle
<R_np1_i\rangle <- <{_tilde\rangle - <R_np1_1\rangle
<R_np1_i\rangle <- <n_np1_i> - <k_coofi> <F_int>
. . . Initialize Convergence Criteria
*call CHKCNYD ( STEP = 1 ;
ITER = 1 ; --
Residual_force = <R_np1_i\rangle ; --
displacement_inc = <d_inc_i> )

```

```

.stop_4 *stop
*echo,on,ma,md
*DO :ITER_LDOP \$i = 1, [max_iters]

```
```

    #doi/i iter == <<$i>+i>
    *def/i tot_iters == <<tot_iters>+1>
    . . . . . Compute Basic Displacement Iteration (delta_th)
*call SOLVE ( rhs = <R_np1_i\rangle; soln = \langledelta_th\rangle; matrix = <M_p_K\rangle )
. . . . Opdate Displacenents, Rotations, Increments
[xgT VEC
<d_np1_ip1> <- <d_npi_i> + <delta_th>
MOTATE <T_np1_i> * <delta_th> -> <T_np1_ip1>
*call CONSTRAII}( load_factor = <lanbda_np1>; --
applied_motion = <d_spec\rangle ; --
displacenont = <d_np1_ip1>)
*if < <DEBUG> > /then
*print 1, <d_np1_ip1>
*print 1, <T_np1_ip1>
*endif
. . . . . Compute dTMAMIC RESIDUAL
*call FORCE ( type = INTERNAL ; --
nl_geon = [nl_geon] ; --
displacement = <d_np1_ip1> ; --
rotation = <T_np1_ip1> ; --
corotation = [corotation] ; --
output_force = <P_int>)
[xqT vEC
PROD <nass> <d_np1_ip1> -> <R_np1_ip1>
<R_np1_ip1> <- <1_tilde> - <R_np1_ip1>
<R_np1_ip1> <- <R_np1_ip1> - <k_cooff> <P_int>
. . . . . check comyergence
*call CHKCNYD ( step = <step> ; -- . input
iter = <iter> ; --
Residual_force = <R_np1_ip1> ; --
displacenent_inc = <delta_th> ; --
tol_e = [tol_e] ; --
max_itors = [max_itors] ; --
convergence = CONVERGEMCE ; -- . output
divergence = DIVERGENCE )
*if <COMVRRGENCE>/eq <TROE>/thon
*junp to :CONVERGED
*olseif <DIVERGENCE> /oq <TROE>/then
*if <pass> /le [nax_cuts] /then
*jump to :REPEAT
**lse
*Romark haximun number of automatic step cuts oxhausted.

```
```

            *Jump to :DIYERGED
            *ondif
        * endif
    :ITER_LOOP
    :NEOTRAL
    *if <pass>/1e [max_cuts]/then
        *jump to :PEPEAT
        *else
            *Remark Maximun number of autometic step cuts exhausted.
        *ondif
        *Rorark MON-CONYERGENCE AT STEP <step>. REVISE STRATEGY.
        -jump to :EXIT
        :REPEAT
        *dof/i pass =m < <pasg>+1 >
        *def/d dt =E <<dt>*.5>
        *Remark
        *Remark CONVERGENCE DIPFICULTIES; REPEATING STEP <step>
        Remark with hall original tine step
        &Remark Nev TIME increnent is <dt>
        *Romark Pass: <pase>
        *jump to :NEW_PASS
        -DIVERGED
    #Remark DIVERGENCE AT STEP <STEP>. REVISE STRATEGY.
    * jump to :EXIT
    :CONVERGED
    *Remark CONVERGENCE AT STEP <STEP>.
    :NEXTSTEP
    *def/i num_iters mx <iter>
    *def/d path_scele m= <[den_iters]/<num_iters>>
    #del/d lan_n =x <lanbda_np1>
    #del/i sign_det_n == <sign_det>
    #def/i load_dir_n =m <load_dir>
    . . . Compute current acceleration
[xQT VEC
Hif <<theta> /ne 1.0>/then
<a_th\rangle <- <0_d_th\rangle <d_np1_ip1\rangle - <0_d_th\rangle <d_tilde>
<a_np1\rangle <- <0_d_th\rangle \langlea_th\rangle + <0_odth\rangle \langlea_n\rangle
*el:*
<a_np1\rangle <- <0_d_th\rangle <d_np1_ip1\rangle - <0_d_th> <d_tilde\rangle
*ondif
. . . . Jpdate velocity vector
<a_th\rangle <- \langlev_n_coef1\rangle \langlea_n\rangle + <v_np1_coef1\rangle <a_np1\rangle
<v_mp1\rangle <- <v_n> + <n_th>
. . . For strange (non-unity) values of Ullson's parameter, update
.. . . displacementa to step n+1
*if <<theta>/ne 1.0>/then
<a_th\rangle\langle- \langleh_mb\rangle \langlea_n\rangle + \langledt_b\rangle <a_npi\rangle

```
```

    <delta\rangle <- <dt\rangle \langlev_n\rangle + <a_th\rangle
    <d_np1_i\rangle <- <d_n\rangle + \langledelta\rangle
    mOTATE <T_n> * <delta> -> <T_mp1_i>
    *endif
. . . . Postprocese and save results of computations st <<STEP> + 1>
*call POSTSTPD ( step=<step>; iter=<iter>)
. . . . Heset iteration counters
*def/i pass =m 1
*dof/i tot_iters =3 1
. . . . Jpdate current time
*dof/d t_vils == <<t\rangle + \langleth_dt>>
*def/d t == <<t\rangle + \langledt>> . can be altered by path_scale
*stop
. . . . Check for max time and max steps
*if <<t>/gt <nax_tine>>/then
*ramark ************************************************************************
*renat
\#renark * Maximum problon time <nax_tino> reached or exceeded. *
\#remark * Computation terminated *
*ronark * *

```

```

    *junp to :EXIT
    *ondif
*if <<step> /eq <<nax_stops>- 1>>/then

```

```

*ramark 事 *
\#remark * Maximus steps <nax_steps> exceeded. *
*ronark Problen time is <t> *
由ronark * *

```

```

    * junp to :EXIT
    \&endif
. . . . Reset step counter for dataset: to step <<step> + 1>
*call DEFND (STEP = <<STEP\rangle + 1\rangle; ITER=1)
. . . . Compute nev "historical" displacement d_tilde
[XqT VEC
<a_th\rangle <- <th_dt\rangle \langlev_n\rangle + <h_nb_th\rangle <a_n\rangle
<d_tilde\rangle <- \langled_n\rangle + \langlea_th\rangle
. . . . Compute nem external force lor step n+1

```
```

    *call [PT_proc] ( I = <t_wils> ; -- . Problen time
            PT_ args = [ft_args] ; -- . Porce-time paremeters
            F_mac = lanbda_npi ). Externel forcing scele factor
    *call FORCE ( type = EXTERNAL ; -
nl_geon = [nl_geom] ; --
nl_load = <true> ; --
displacenent = <d_n\rangle ; --
rotation = <I_n\rangle ; --
corotation = [corotation] ; --
load_factor = <lambda_np1> ; --
input_force = <P_rөf> ; --
output_force = <F_ext> )
. . . Set internal force if Wilson's constant is not unity
*if<<theta> /ne 1.>/then
*call FORCE ( type = INTERNAL ; --
nl_geom = [nl_ge0n] ; --
nl_load = <true> ; --
displaconent = <d_n\rangle ; --
rotation = <T_n> ; --
corotation = [corotation] ; --
load_factor = <lambda_np1> ; --
input_force = <F_ref> ; --
output_force = <F_int> )
*endif
. . . . Weighted sum of internal and external force
[xqT VEC
<1_bar> <- <th_b> <F_ext> + <a_th_b> <P_int>
PROD <ness> <d_n> -> <I_tilde>
<i_tilde> <- <f_tilde> + <f_bar>
. . . . Compute nov initial estimate, displacozents
[xgt vec
<delta\rangle <- <d_tilde\rangle - <d_n>
<delta\rangle <- <delta\rangle + \langleth_b\rangle <a_n\rangle
<d_np1_i\rangle <- <d_n> + <delta>
mOTATE <T_n> * <delta> -> <T_np1_i>
. . . . End Step LDOP
:STEP_LOOP
: EXIT
*end
. =DECK CHKCNVD
*procedure CHKCNVD ( STEP ; -- . input
ITER ; --
DISPLACEMENT_INC ; --
RESIDUAL_PORCE ; --
TOL_E ; --

```
```

MAX_ITERS ; --
CONYERGENCE=CONVERGENCE ; -- . output
DIVERGENCE =DIVERGENCE )

```
[xqT VEC
. . Initialize
    *dof/i [Convergence] =x <PILSE>
    *def/i [DIVERGENCE] \(=\) = <PALSE>
    *if [ITER] /gt 1 /thon
        *def/d12.4 ERR_E_I =x 〈ERR_E_IP1〉
    *endif
- Conpute Current Incremental Energy Morm
    dot [RESIDOAL_PORCE] * [DISPLACEMENT_INC] -> INC_E_IP1
    *if [ITER] /le 1 /thon
        *if <ABS(<INC_E_IP1>)>/gt <REF_E>/then
            *dof/d12.4 REP_E = = <ABS(〈INC_E_IP1>)>
        *ondif
        *def/i num_diverges \(=0\)
    *endif
. Compute Error Morzs
    *dof/d12.4 ERR_E_RAY = \(=\langle\) <INC_E_IP1>/<REF_E\gg
    *dof/d12.4 ERR_E_IP1 \(==\left\langle\left\langle A B S\left(\left\langle E R R_{-} E_{-} R 1 H\right\rangle\right)\right\rangle-.5\right\rangle\)
- Check for displacenent convergonce
    *if \llERR_E_IP1>/1• [TOL_E] >/then
. . . Step Converged
        *DEP/I [CONYERGENCE] \(==\) <TROE>
        * junp to :BOTTOM_LINE
    *ondit
    *if 〈[ITER] /le 1\(\rangle\) : BOTTOM_LINE
- . Step Mot Converged; Check for Divergence
        *IP 〈〈ERR_E_IP1>/<ERR_E_I>/GT 1.0\(\rangle / T H E N\)
        *def num_diverges \(=\) = \llnun_diverges>+1>
        *if <num_diverges>/gt \(1 /\) then
                *DEF/I [DIVERGENCE] \(==\) <TRUE>
            *ENDIF
        *EMDIP
    : BOTTOM_LIME
    *dof/e12.4 load_factor \(=\left\langle l a z b d a \_n p 1\right\rangle\)
*romark
*renark
*ronark ITER=[ITER] Tx<t> LD=〈load_factor>
*renark ERR=〈orr_e_ip1〉 LEP=〈ref_e〉
```

*renark
*ronark
|END
. =DECK DEFND
*procedure DEFND ( step; iter )
. Purpose: Define basic nacro_symbols for ML_DNNAMIC procedure
*def/i npi = [step]
*dof/i n = < <np1>-1\rangle
*if [itor] /eq 0 /thon . run initialization
*def/i HS_ldi == 1
*def/i MOM_ldi == 3
*dof/i isot = = 1
*def/i icon == 1
*def/e 1_spec =x APPL.PORC.<iset>.1
\#def/a d_spec == APPL.HOTI.<iset>.1
Check for Specified Displacenent Loading
*ind dataset <NS_ldi> <d_spec> /seq=ids
*if <<ids>/gt 0 >/then
*Renark Note: Specified displacenent dataset <d_spec> will be used
*def/i spec_disp_flag == <true>
*el:e
*def/i spec_disp_flag == <falso>
*endif
*def/a P_ref == REP.FORC
*def/a f_ext == EXT.PORC
*def/a 1_int == INT.FORC
*def/a ness =x M.DIAG
*def/a inv_mass Ex MINV.DIAG
*def/a R_np1_i == RES.FORC
*def/a l_np1_ip1 =a RES.FOLC
*def/a d_inc_i == INC.DISP
*def/a d_inc_ip1 m= INC.DISP
*dof/a v_inc_i == INC.VEL
*doi/a v_inc_ip1 =m INC.VEL
*def/a delta_TH ma THET.DISI
*def/a a_TH == THET.ACC
*def/a delta m= TOT.DISI
*def/a d_tilde m= TILD.DISP
*dof/a 1_tilde == TILD.FORC
*def/a f_bar == BAR.FORC
*def/a K_asm == K
*dof/a K_fac == K
*def/a M_P_K =m MpK
Retrieve Control Parameters from DATA_BASE
*if [step]/eq 1/then
*def/d t_n == <beg_time>

```
```

        #def/i sign_det == 1
        *dei/d rof_* == 0.0
        *def/d lambda_n =x 0.0
        *Romark STARTING PARAMETERS IMITIALIZED.
        *elme
        *open <NOM_ldi> <NOM_DB>
        *find dateset <nom_ldi> <nom_ds>/seq=nom_ids
    *g2m /nanex=t_n /type=D <nom_ldi> <nom_ids> TMME.<n>
    *g2a /namex=aign_det_n /type=I <nom_ldi> <nom_ids> SIGM_DET.<n>
    *g2n /namezalanbda_n /type=D <nom_ldi> <nom_ids> LOAD.<n>
    *g2m /name=mref_* /typexD <non_ldi> <nom_ids> REF_ERR.<n>
    *close <MOM_Idi>
    *Romark
    *remark
    #romark
    *Ronark me-Start parameters:
    *Renark TIME = <t_n>
    *Renark SIGN_DET (n) = <sign_det_n>
    *Renark LOAD = <lambda_n>
    *renark
    *remark
    *ondif
    *ondif

- Dofine Global Datasets for Opconing Step
- 

*dof/a d_n == TOT.DISP.<n>
*dof/a d_np1_i m= TOT.DISP.<np1>
*def/a d_np1_ip1 == TOT.DISP.<np1>
*def/a v_n == TOT.vEL.<n>
*def/a v_np1 == TOT.vEL.\langlenp1>
*def/a a_n == TOT.1CC.<n>
*def/a a_np1 == TOT.ACC.\langlenp1>
*def/a T_n m= TOT.ROTN.<n>
*dof/a T_np1_i == TOT.ROTN.<np1>
*dof/a T_np1_ip1 == TOT.ROTN.<np1:
*ond
=DECK FT_ZERO
*procedure FT_ZERO ( t ; ft_args ; F_mac )
. . . Provide for zero dependence of force on time (no external forces)
*dof/d [F_mac] x= 0.
*ond
. =DECK FT_LIN
*procedure PT_LIM ( t ; ft_args ; F_mac )
. . . . Provide piecenise linear forcing function
*dof/d ft_arga[1:5] = [ft_args]

```
```

*if <[t] /le <ft_args[2]>> /thon
*dof/d [P_mac] == 0.
*elsoif <[t] /1t <ft_args[3]>>/thon
*dof/d c_fact = <<ft_args[3]>-<ft_args[2]>>
*if <<c_fact>/le 0.>/then
*dof/d [F_mac] =x <ft_args[1]>
*0l:e
*dof/d [F_mac] =x <<<[t]-<ft_args[2]>> * --
<ft_args[1]>>/<c_fact>>
*endif
*elseif <[t] /1e <ft_args[4]>> /then
*dof/d [F_mac] == <ft_args[1]>
*elseif <[t]/lt <ft_orgs[5]>>/thon
*def/d c_fact = <<ft_args[6]>-<ft_args[4]>>
*if <<c_fact> /le 0.>/then
\#dof/d [P_mac] == 0.
*0lse
*dof/d [F_mac] == <<<<ft_args[5]> - [t]> * --
<ft_args[1]>>/<c_fact>>
*endif
**lse
*def/d [P_nac] == 0.
*endif
-
*ond
. =DECK PT_SIN
*procedure PT_SIN ( t ; ft_args ; F_mac )
*dof/d ft_args[1:0] = [ft_args]
. . . . . Piecovise sinusoidal forcing function
*if <[t]/ge <ft_args[6]>>/then
*def/d [P_mac] = 0.
*elseif <[t]/ge<ft_args[6]>>/then
*if <<ft_args[3]> /1\bullet 0.>/then
*dof/d [P_mac] == 0.
*olso
*def/d tc = <<<[t] - <ft_args[4]>>*<pi>>/<ft_args[3]>>

```

```

    *ondif
    *\&1s0
*dof/d [P_mac] == 0.
*endif
.
**nd
. =DECK FT_EXP
*Procedure FT_EXP ( t ; ft_args ; F_mac )
. . . . Exponential docay

```
```

*def/d ft_args[1:3] = [ft_args]
*if <[t] /1t <ft_args[2]>>/thon
*dof/d [P_mac] == 0.
*-is*
*def/d apl = <.6931471806/<ft_args[3]>>
*def/d axl = <<apl>*<[t] - <ft_args[2]>>>
*def/d [P_mac] == <<ft_args[1]>* <EXP(-<axl>)>>
*endif
•
*ond
. =DECK ML_IMITD
*procedure 盺_IMITD ( ldi=1 )
PERPORM STANDARD INITIALIZATION
*call IMITIALIZE ( constraint_set = <icon>)
CLEAR INITIAL DISPLACEMENTS AND motations ( n = 0)
*g2a /namesnum_nodes /type=i [ldi] MODEL.SUMMARY NOM_NODES
*g2n /nanexnum_dof: /type=i [ldi] MODEL.SUMMARY NOM_DOFS
*Renark Problen Dinensions: N_nodes = <num_nodes>, N_dofn = <num_dofs>
*find dataset <MS_ldi> <d_n> /seq=ids_disp
\#if < <ids_disp>/gt 0 > /then
*Renark Note: Initial displacenent dataset <d_n> will be used
*else
INIT_VRC <d_n> <nun_dofs> BY <num_nodes> . Zoroize translations
*Renark Diaplacenonts (<d_n\rangle) initialized.
*ondif
*ind dataset <MS_ldi> <T_n>/seq*ids_rotn
*it <<ids_rotn>/gt 0>/thon
*Remark Hote: Initial rotation dataset <T_n> vill be used
*0lse
IMIT_TEC <T_n> 3 BY <num_nodes> . Zeroize rotation pseudovectors
*Remark Lotetions (<T_n>) initialized.
*endif
*find dataset <NS_ldi> <v_n> /seq=ids_vel
*if < <ids_vel>/gt 0 >/then
*Renark Note: Initial velocity dataset <v_n> will be used
*else
INIT_VEC <v_n> <nun_dofs> BY <num_nodes> . Zoroize velocity
\#Romark Volocitien (\langlev_n\rangle) initialized.
*endif
*find dataset <NS_ldi> <a_n> /seqzids_acc
*if < <ids_acc> /gt 0 > /then
*Renark Note: Initial acceleration dataset <a_n> vill be used
*else
INIT_VEC <a_n> <num_dofs> BY <num_nodes> . Zeroize acceleration
*Renark Accelorations (<a_n>) initialized.
*endif

```
```

    FORA IMITIAL (BASE-LOAD) EXTERNAL-FORCE VECTOR
    *call FORCE ( type = EXTERNAL ; --
    input_force = <f_spec\rangle ; --
    output_force = <P_ref\rangle )
    •
Form mass and invorse mass (diagonal form)
. --------------------------------------------------
-
*ronark
*renark MASS bypassed for testing purposes defined in BASE.DBC
*ronark
. *call mass ( type = dIAGOMAL ; --
[XGT VEC
DIAG_INV <nase> -> <inv_mass>
*ond
. =DECK MASS_STIPF
*procedure MASS_SIIFF ( mass ; -- . diagonal mass vector
stif ; -- . assonbled stiffness
mult ; -- . the dynamic weighting factor
M_p_K ) . the dynamic operator
[xqT AOS
DEPINE M = <MS_ldi> M DIAG
DEPINE K = <NS_ldi> [STIP] SPAR 36
[M_P_K] SPAR 36 = SUM(H, [HOLT] K)
•
*end
. =DECK POSTRES
*procedure posTaES ( step )
[xqT VEC
*find dataset <MOM_LDI> <MOM_DS> /seq=post_ids
*if < <post_ids>/10 0 >/thon
*put dataset <MOM_LDI> <NOM_DS> /arat=2000 /seq=post_ids
*endif
. Save selected displacenents on nominal data-base
*def/a dof_names = U, V, W, RU, RV, RW
*do $isel = 1, <N_SELECT>
        *def/i node = <SEL_MODES[<$is01>]>
*dof/i dof = <SEL_DOFS[<\$isel>]>
*def/a dof_name = <dof_names[<dof>]>
COMPONENT <node> <dof> TOT.DISP.[step] -> DISP
*def/a recd_name = DISP_<dof_nane>_<node>.[step]
*Lenark <recd_nane> = <DISP>
*mgg /name=disp /typexd <nom_ldi> <post_ids> <recd_name>
Save Reaction Porces for Current Stop

```
```

        gEAC.FORC.[stop] <- INT.FORC
        *if < [step] /oq 0 > /then
        REAC.FORC.0 <- 0.0
    *ondif
    *ii < <spec_disp_ilag> > finon
        COMPONENT <node> <dof> REAC.FORC.[stop] -> FORCE
        *def/a recd_name = FORCE_<dof_nane>_<node>.[step]
        *Romark <recd_nane> = <PORCE>
        *n2g /namexforce /type=d <non_ldi> <post_ids> <recd_name>
        *endif
        *onddo
    *end
. =DECK POSTSTPD
*procedure POSTSTEP ( step; iter )
*Renark
_-------------------
*Renark STEP [step] SUMMARY :
\#Remark

```

```

*lenark Stiffness determinant _------------ <coef_det> * 10 - <exp10_det>
*Remark Number of negative roots _-------- <num_neg>
*Renark Relative energy_error _------------ <err_e_ipi>
*Renark Number of Iterations ------------- <num_iters>
*Renark Number of Stop Cuts _---------.----- <<pass>-1>
*Remark Total Number of Iterations _--.--. <tot_iters>
*Renark
*open <NOM_ldi> <NOM_DB>
*if < [step] /eq 1 >/then
*call POSTRES ( atep = 0)
*def/d load_0=0.
*E2g/nane=load_0 /type=d <NOM_LDI> <NOM_DS> LOAD.0:0
*endif
*call POSTRES ( step=[step])
*find dataset <NOM_LDI> <NOM_DS> /seq=nom_ids
*m2g/name=lambda_np1 /type=d <nom_ldi> <nom_ids> LOAD.[STEP]
\#n2g/name=orr_e_ip1 /typexd <non_ldi> <nom_ids> ERROR.[STEP]
*m2g /name=ref_e /type=d <non_ldi> <nom_ids> REF_ERR.[STEP]
*m2g /name=sign_det /type=i <non_ldi> <nom_ids> SIGN_DET.[STEP]
*n2g /namezcoef_det /type=d <nom_ldi> <nom_ids> CORF_DET.[STEP]
*m2g/name=exp10_det /type=i <nom_ldi> <nom_ids> EXP10_DET.[STEP]
*m2g/name=num_neg /type=d <nom_ldi> <nom_ids> NEG_BODTS.[STEP]
\#n2g/naze=num_iters /type=i <nom_ldi> <nom_ids> NUM_ITERS.[STEP]
*n2g/nare=tot_iters /typexi <nom_ldi> <nom_ids> TOT_ITERS.[STEP]
*m2g/nameat /type=i <nom_ldi> <nom_ids> TIME.[STEP]
*dof/i passa1 = <<pass>-1>
*m2g/namezpasem1 /type=i <nom_ldi> <nom_ids> NOH_CUTS.[STEP] . cgl, 7/26/88
*close <NOM_ldi>
*ond

```

\subsection*{3.11.12 REFERENCES}
3.11-1 Almroth, B.O., Brogan, F.A., and Stanley, G.M., "Structural Analysis of General Shells, Volume II, User's Instructions for STAGSC-1," Lockheed Palo Alto Research Laboratory, Palo Alto, CA, Rept. \#LMSC-D633873, December 1982.
3.11-2 Hilber, H.M. and Hughes, T.J.R, "Colocation, Dissipation and Overshoot for Time Integration Schemes in Structural Dynamics," Earthquake Engineering and Structural Dynamics, Vol. 6, pp. 99-118, 1978.
3.11-3 Newmark, N.M., "A Method of Computation for Structural Dynamics," Journal of the Engineering Mechanics Division, ASCE, pp. 67-94, 1959.
3.11-4 Hilber, H.M., Hughes, T.J.R., and Taylor, R.L., "Improved Numerical Dissipation for Time Integration Algorithms in Structural Dynamics," Earthquake Engineering and Structural Dynamics, Vol. 5, pp. 283-292, 1977.
3.11-5 Bathe, K.J., and Wilson, E.L., "Stability and Accuracy Analysis of Direct Integration Methods," Earthquake Engineering and Structural Dynamics, pp. 283-291, 1973.
3.11-6 Wilson, E.L., "A Computer Program for Dynamic Stress Analysis of Underground Structures," SESM Report No. 68-1, Division of Structural Engineering and Structural Mechanics, University of California, Berkeley, 1968.

\subsection*{4.0 Application Procedures}

The procedures documented in this chapter are representative of the types of procedures that may be written to solve specific application (structural analysis) problems. Many of these high-level procedures invoke other (lower-level) procedures to perform preprocessing, solution, and postprocessing functions; which are described elsewhere in this manual. The use of procedures to perform structural analysis applications can provide users flexibility for parameterizing geometric data (e.g., stiffener spacing) as well as spatial discretization parameters (e.g., number of elements). The problems represented here are also intended to serve as part of a standard series of test problems to assess new structural elements installed in the CSM Testbed.

A summary of the procedures found in this chapter is provided in Tables 4.0-1.

Table 4.0-1. Summary of Application Procedures

\section*{Procedure Name}

\section*{Problem Description}

CLAMPED_BEAM Transient response of a clamped beam modeled with 2-D shell elements.

COMPRESSED_CYL Classical buckling and postbuckling analysis of an axially compressed cylindrical shell; modeled with shell elements and initial imperfections.
COOKS MEM Linear in-plane bending response of a wing-like trapezoidal plate modeled with shell elements. (Referred to as Cook's membrane problem in the literature.)

ELASTICA Classical large rotation analysis of a cantilevered beam with an applied end moment. Final configuration is a complete circle - with 360 degrees rotation at the free edge. Modeled with shell elements.

EULER_COLUMN Inplane buckling of a column modeled with 2-D shell elements. An overall Euler buckling modeshape is obtained.

FOCUS_PANEL Analysis of the composite blade-stiffened panel with a discontinuous center stiffener.

FREE_EDGE Free-edge stress analysis of a 4-ply composite laminate.
GEN_STF_PANEL Linear buckling analysis of stiffened panel configurations subjected to combined in-plane compression and shear loading. Configurations considered include flat rectangular panels with hat-stiffeners, z-stiffeners and blade stiffeners, as well as a corrugated panel. Modeled with shell elements.

HINGED_CYL Postbuckling (nonlinear) analysis of a hinged cylindrical shell subjected to concentrated transverse load. Shell exhibits snap-through buckling behavior and requires a solution algorithm employing arc-length step control. Modeled with shell elements.

Table 4.0-1; concluded.
\begin{tabular}{ll}
\hline Procedure Name & \multicolumn{1}{c}{ Problem Description } \\
\hline PEAR_CYL & \begin{tabular}{l} 
Buckling analysis of a pear-shaped cylindrical shell sub- \\
jected to axial compression. Modeled with shell elements.
\end{tabular} \\
\hline PINCHED_CYL & \begin{tabular}{l} 
Linear inextensional bending of a thin pinched cylindri- \\
cal shell. Modeled with shell elements; two opposing \\
radial forces applied at center; and both free and rigid- \\
diaphragm edges considered. (MacNeal-Harder case)
\end{tabular} \\
\hline PU_HOLE & \begin{tabular}{l} 
Linear elastic stress analysis of a rectangular isotropic \\
plate with a central circular hole.
\end{tabular} \\
\hline RECT_PLATE & \begin{tabular}{l} 
Eigenvalue (vibration and buckling) analyses of a rect- \\
angular plate subjected to various inplane loading condi- \\
tions.
\end{tabular} \\
\hline RHOMBIC_PLATE & \begin{tabular}{l} 
Linear bending of a simply supported rhombic plate under \\
constant pressure. (MacNeal-Harder case)
\end{tabular} \\
\hline TRUNCATED_CONE & \begin{tabular}{l} 
Linear transient dynamic analysis of impulsively loaded \\
truncated cone.
\end{tabular} \\
\hline VIB_2D & \begin{tabular}{l} 
Vibration analysis of a bar, beam, or ring modeled with \\
2-D shell elements.
\end{tabular} \\
\hline
\end{tabular}

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\subsection*{4.1 Processor CLAMPED_BEAM}

THIS SECTION UNDER PREPARATION

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\subsection*{4.2 Procedure COMPRESSED_CYL}

\subsection*{4.2.1 GENERAL DESCRIPTION}

\subsection*{4.2.1.1 Problem Description}

This application problem involves the static buckling and postbuckling analysis of a thin cylindrical shell \((R / t \approx 300)\) simply supported along its edges, and subjected to uniform axial compression (see Figure 4.2-1). It is a particularly important classical problem for testing linear and nonlinear performance of shell elements, as well as solution algorithms capable of traversing non-monotonic load-displacement curves. A noteworthy feature of the problem is that the buckling eigenvalues of the cylindrical shell are very closely spaced, even though the mode shapes are radically different. This can pose a challenge for both eigensolvers and nonlinear solution algorithms - which are expected to find and maintain the physically dominant (lowest-energy) mode. (It is interesting that the buckling characteristics of this simple cylindrical shell problem have much in common with the more practical problem of an optimally-stiffened cylinder, which also has many diverse mode shapes occurring at the same critical load level.) Another noteworthy feature is that such problems are notoriously imperfection sensitive. Thus, a small initial geometric imperfection can cause a substantial reduction in the peak axial load capacity, compared with the classical critical buckling load corresponding to a perfect cylinder. This implies that the model must be refined enough to represent the initially imperfect configuration, as well as the finally deformed configuration.


Figure 4.2-1 Compressed Cylinder Problem.

\subsection*{4.2.1.2 Model Description}

Procedure COMPRESSED_CYL employs a partial ( \(L / 10 \times 15^{\circ}\) ) shell-element based model of the cylindrical shell to capture both linear and nonlinear response. A typical model is shown in Figure 4.2-2. The mesh is rectangular in topology, and restricted to quadrilateral shell elements of either 4 - or 9 -node variety. Symmetry conditions on all but the one edge that is simply supported enable the model to represent the lowest energy buckling mode with a relatively small number of elements. This particular ("diamond") mode shape consists of 5 axial half-waves and 12 circumferential whole waves over the entire cylinder (in classical terminology: \(\mathrm{m}=5, \mathrm{n}=12\) ). Thus, the partial model will contain 1 axial quarter-wave and 1 axial half-wave, and less than 10 shell elements should be required in each direction to obtain engineering accuracy. The axial force is distributed evenly and consistently on the simply supported edge; and is scaled so that the magnitude corresponds to the classical buckling load.

\subsection*{4.2.1.3 Analysis Description}

The analysis is conducted in stages, some of which are optional. First, a linear buckling (eigenvalue) analysis is performed (using procedure L_STABIL_1). Due to the selected magnitude of the applied load, the lowest eigenvalue should be close to 1 (for a sufficiently refined mesh). Next, the buckling mode corresponding to the lowest (critical) eigenvalue is scaled and used to perturb the geometry. This is achieved by adding the scaled radial displacements to the initial finite element nodal coordinates. The scale factor is selected so that the maximum radial perturbation is some percentage of the shell thickness (see procedure IMPERFECTION). This initial imperfection is necessary to trigger a realistic postbuckling response in the nonlinear analysis. Due to the extreme imperfection sensitivity of thin axially-compressed cylinders (e.g., see ref. 4.2-3) as little as a \(1 \%\)-thickness imperfection is adequate to trigger such a response (although a \(10 \%\)-thickness imperfection is recommended). The nonlinear (postbuckling) analysis is then begun (using procedure NL_STATIC_1). A reasonable description of the load-displacement history can usually be obtained with about 20-30 load steps, from a starting load of about one-tenth of the classical buckling load.

\subsection*{4.2.1.4 Available Solutions}

Analytical solutions are available for the buckling (eigenvalue) analysis (e.g., see ref. 4.21). Several of the buckling modes corresponding to the classical stability solution are shown in Figure 4.2-2 (Figure 6.9 of ref. 4.2-2) using finite-element meshes. Note that the critical loads (or eigenvalues) for these diverse mode shapes - smooth, axisymmetric, and diamond-pattern - are within \(5 \%\) of one another. While there are no closed-form solutions for the nonlinear postbuckling response of the axially-compressed cylindrical shell, there are approximate solutions for the "knock-down" factor corresponding to a given initial imperfection, and various numerical solutions are given in the CSM Testbed Applications Manual (see ref. 4.2-4). Figure 4.2-3 gives a sampling of these numerically obtained response curves, for different magnitudes of initial imperfection (50\%, 10\% and \(1 \%\) of the shell thickness). Note that with only a \(10 \%\)-thickness imperfection, the peak load is "knocked-down" to approximately \(70 \%\) of the value for a perfect (unattainable) shell.


Figure 4.2-2 Buckling of Axially-Compressed Cylinder: Generic Problem Description

Figure 4.2-3 Postbuckling of Axially-Compressed Cylinder:

\subsection*{4.2.2 PROCEDURE USAGE}

Procedure COMPRESSED_CYL may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call COMPRESSED_CYL ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (-) may be used to continue the argument list on the next line.

The allowable arguments for procedure COMPRESS_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES_PROC & ES1 & Element Processor \\
\hline ES_NAME & EX97 & Element name \\
\hline ES_PARS & 0. & Element research parameters \\
\hline NNODES_A & 5 & Number of axial nodes \\
\hline NNODES_C & 5 & Number of circumferential nodes \\
\hline SPEC_DIS & <false> & Specified displacements \\
\hline PRE_STRESS & <false> & Constant pre-stress \\
\hline AUTO_DOF_SUP & <true> & Automatic d.o.f. suppression \\
\hline DRILLIMG_DOF & <false> & Drilling (normal rotational) freedoms \\
\hline BC_PROCEDURE & CC_BC & Boundary condition procedure \\
\hline NSTEPS & 30 & Number of nonlinear load steps \\
\hline BEG_STEP & 1 & Starting load step number \\
\hline Max_CUTS & 3 & Maximum number of step cuts (halvings) \\
\hline BEG_LOAD & . 1 & Starting load factor \\
\hline Max_LOAD & 1.0 & Maximum load factor \\
\hline DBC & CC. DBC & Computational database name \\
\hline DBR & CC.DBR & Results database name \\
\hline PREP & <true> & Perform pre-processing (model generation) \\
\hline STABILITY & <true> & Perform linear stability (buckling) analysis \\
\hline IMPERFECTION & <true> & Superpose imperfections from (buckling) analysis before performing nonlinear(postbuckling) analysis \\
\hline NUM_IMP_MODES & 1 & Number of buckling modes used in creating imperfection \\
\hline IMP_MODES & 1 & Mode numbers used in creating imperfection \\
\hline IMP_AMPS & . 1 & Mode amplitudes \\
\hline NONLINEAR & <true> & Perform nonlinear (postbuckling) analysis \\
\hline POST & <false> & Perform post-processing (selected data archival) \\
\hline
\end{tabular}

\subsection*{4.2.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.2.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression fiag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{4.2.3.2 BC_PROCEDURE}

Boundary condition procedure name (default: CC_BC for specified forces; CCD_BC for specified displacements). The term "boundary conditions" refers both to displacement constraints and applied loading. Procedures CC_BC and CCD_BC both have the same zero displacement constraints. The only difference is that the former procedure applies axial forces to the simply supported edge, while the latter procedure prescribes non-zero axial displacements on that edge. The argument BC_PROCEDURE permits you to to supply your own boundary condition procedure, but keep in mind that this may drastically change the problem definition, and hence invalidate most of the discussion under Section 4.2.1.

\subsection*{4.2.3.3 BEG_LOAD}

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then BEG_LOAD \(=.1\) means that the first load step to be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is irrelevant for re-start runs. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.2.3.4 BEG_STEP}

Number of starting load step in nonlinear analysis (default=1). This is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1 . When re-starting (i.e., continuing in a subsequent run) a nonlinear analysis, BEG_STEP should be set to the number of the next step to be computed - not to the number of the last step computed. The solution procedure (NL_STATIC_1) will automatically use any previous step(s) required to continue the analysis - providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.2.3.5 DBC}

Name of computational database file (default=CC.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

\subsection*{4.2.3.6 DBR}

Name of results database file (default=CC.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups - indexed by load step number - for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

\subsection*{4.2.3.7 DRILLING_DOF}

Drilling degree of freedom flag (default: <false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AOTO_DOF_SUP is set.

\subsection*{4.2.3.8 ES_NAME}

Element name (default: EX97). This argument is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX97, is a 9-noded quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.2-1).

\subsection*{4.2.3.9 ES_PARS}

Element research parameters (default: \(0 ., \ldots\) ). This array is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.2.3.10 ES_PROC}

Element Processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{4.2.3.11 IMPERFECTION}

Imperfection superposition flag (default <true>). This flag should be turned on if you want geometric imperfections, corresponding to buckling modes, to be superimposed on the initial geometry. Pre-requisites for this option are pre-processing and stability analysis. If you are just starting or re-starting a nonlinear analysis in the current run, and imperfections have already been superposed in a previous run, then you should turn this flag off.

\subsection*{4.2.3.12 IMP_AMPS}

List of buckling mode amplitudes to be used in generating the imperfection (default=.1, \(10 \%\) of shell thickness). This option is relevant only if IMPERFECTION=<true>. The amplitudes in this list are interpreted as the maximum radial displacement to add to the initial nodal coordinates for a given buckling mode. Thus, the maximum coordinate perturbation due to a single buckling mode will occur wherever the mode shape has its maximum radial component.

\subsection*{4.2.3.13 IMP_MODES}

List of buckling mode numbers to be used in generating the imperfection (default=1). This option is relevant only if IMPERFECTION=<true>. The numbers in this list should be separated by commas, and there should be a total of NOM_IMP_MODES numbers.

\subsection*{4.2.3.14 MAX_CUTS}

Maximum number of load step cuts in nonlinear analysis (default=3). For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.2.3.15 MAX_LOAD}

Maximum load factor in nonlinear analysis (default=1.0). This sets an upper limit for the load level, which can be a convenient way of terminating the arc-length controlled solution algorithm employed within procedure WL_STATIC_1. Since the load factor is actually an unknown in this solution procedure, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. Thus, the analysis will be terminated when either MAX_LOAD is exceeded or NSTEPS is exceeded - whichever comes first. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.2.3.16 HNODES_A}

Number of axial nodes (default: 7). This is the number of nodes you wish to have along the axial direction of the cylindrical shell model, i.e., along one-tenth of the full cylinder's length. Note that this number should be consistent with the number of nodes per element. For example, NNODES \(\AA\) can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\section*{4．2．3．17 NNODES＿C}

Number of circumferential nodes（default：7）．This argument is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model，i．e．，along 15 degrees of circular arclength．Note that this number should be consistent with the number of nodes per element．For example，nNODES＿C can be any number greater than 1 for 4 －node quadrilateral elements，whereas it must be an odd number greater than 1 for 9 －node quadrilateral elements．

\section*{4．2．3．18 MONLINEAR}

Nonlinear（postbuckling）analysis flag（default＝＜true＞）．This flag should be turned on if you want to perform nonlinear analysis in the current run．The pre－requisites are pre－ processing，stability analysis and imperfection superposition，all of which may be performed either in a previous run or in the current run－by setting the appropriate arguments（i．e．， prep，Stability and Imperfection）．

\section*{4．2．3．19 NSTEPS}

Maximum number of load steps to be computed in the current nonlinear analysis run （default＝30）．For more details，refer to the same argument name under solution procedure wL＿STATIC＿1．

\section*{4．2．3．20 NOM＿IMP＿MODES}

Number of buckling modes used to represent geometric imperfections for nonlinear analysis （default＝1）．This option is relevant only if IMPERFECTION＝〈true〉．

\section*{4．2．3．21 POST}

Postprocessing flag（default＝〈false＞）．This flag should be turned on if you want selected response－history parameters to be added to the CC．DBR database．Note that it is not necessary to use this option in order to archive the basic load－displacement curve and solution parameters．It is only needed if you wish to archive special displacement and／or internal force component response histories post－facto．

\section*{4．2．3．22 PREP}

Preprocessing flag（default＝＜true＞）．This flag must be turned on the first time procedure COMPRESSED＿CYL is run，as it causes the model to be generated．If subsequent runs are used to perform other stages of the analysis（e．g．，nonlinear re－starts），then PREP must be set to＜false＞for those subsequent runs．

\section*{4．2．3．23 PRE＿STRESS}

Constant pre－stress flag（default：＜false＞）．By setting this flag to＜true＞，the procedure bypasses computing the linear solution to obtain the prebuckling stresses，and instead prescribes the prebuckling axial stress resultants to be uniform throughout the shell．This
amounts to procedure COMPRESSED_CYL invoking solution procedure L_STABIL_ 1 instead of procedure L_STABIL_2 to perform the buckling eigenvalue analysis. While the prescribed pre-stress used with this option is equal to the classical buckling value, the results can be somewhat different than those obtained using L_STABIL_2. The reason for this is that due to the simply supported boundary condition on the loaded edge, the prebuckling stress distribution (i.e., both the exact one and that obtained using a linear prebuckling analysis) is not really uniform. Note that even when the uniform PRE_STRESS option is selected, it is used only to obtain the buckling eigenvalues and mode shapes - which are in turn used as initial imperfections for the nonlinear analysis. The uniform pre-stress values are then ignored during the nonlinear analysis, which applies either forces or displacements to the simply-supported edge (depending on argument SPEC_DIS).

\subsection*{4.2.3.24 SPEC_DIS}

Specified displacement flag (default: 〈false〉). By setting this flag to <true>, uniform axial end-shortening is imposed instead of the uniform axial loading. This can make a significant difference in both the buckling and postbuckling response, and is not recommended for novice users of this procedure. This is because thin axially-compressed shells are not only imperfection sensitive, but also boundary condition sensitive, and uniform axial loading does not correspond (exactly) to uniform axial edge displacements. Note that the reference specified displacement (i.e., end-shortening) magnitude equals .01 inches, and corresponds to an axial load of about .467 times the classical buckling load.

\subsection*{4.2.3.25 STABILITY}

Stability (buckling) analysis flag (default: <true>). This flag should be turned on if you want the buckling eigenvalue analysis to be performed in the current run. Preprocessing is a pre-requisite for this option. If you are just performing a nonlinear analysis re-start run, then you should turn this flag off.

\subsection*{4.2.4 USAGE GUIDELINES AND EXAMPLES}

Procedure COMPRESS_CYL may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```

BEG_STEP = 1 ; --
HSTEPS = 10
BEG_LOAD = . }
MAX_LOAD = 3.0
DBc = CC.DBc ; DBr = CC.DBr )

```
(E1) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

Table 4.2-1 Typical CPU Times for Various Computer Systems
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
\hline VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CONVEX C220 \\
VERSION 7.0 & \\
\hline CRAY-2 & \\
\hline UNICOS 4.0 & \\
\hline
\end{tabular}
(E2) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call COMPRESSED_CYL
This will perform linear buckling eigenvalue analysis and 30 steps of nonlinear analysis with a \(7 \times 7\) grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.2-1.

\subsection*{4.2.5 LIMITATIONS}
(L1) Only 4-node and 9-node shell elements can be employed in the model. (Note: This can be easily modified.)
(L2) Not all of the solution parameters provided by procedure NL_STATIC_1 are accessible using this procedure. The main reason for this is the CLIP limitation of 25 arguments per procedure. Procedure COMPRESSED_CYL is exactly at this limit now.

\subsection*{4.2.6 ERROR MESSAGES AND WARNINGS}

If you have to repeat the preprocessing phase, you need to either delete the computational (.DBC) database, or delete the ES. SUMMARY dataset. Otherwise, the element processors will be run more than once for each element function (e.g., FORM STIFFNESS), and the effect will be cumulative. This is due to a lack of explicit initialization in the registration of element processors using procedure ES.

\subsection*{4.2.7 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
COMPRESSED_CYL & (main procedure) \\
GEN_SHELL & (generate shell model) \\
CC_BC & (generate boundary conditions/loads) \\
L_STABIL_2 & (perform stability analysis) \\
IMPERFECTION & (superpose buckling modes as imperfections) \\
HL_STATIC_1 & (perform nonlinear static analysis) \\
HISTORY & (archive selected displacement/force histories)
\end{tabular}

\subsection*{4.2.8 PROCEDURE LISTING}

\subsection*{4.2.9 REFERENCES}
4.2-1 Timoshenko, S. P.; and Gere, J. M.: Theory of Elastic Stability, McGraw-Hill, New York, 1961.
4.2-2 Stanley, G. M.: "Continuum-Based Shell Elements," PhD Dissertation, Stanford University, 1985.
4.2-3 Donnel, L. H.: Beams, Plates, and Shells, McGraw-Hill, New York, 1976.
4.2-4 CSM Testbed Applications Manual.

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\subsection*{4.3 Procedure COOK_MEM}

\subsection*{4.3.1 GENERAL DESCRIPTION}

This section describes a procedure that solves for the deflection of a trapezoidal panel subject to inplane shear and bending, also known as Cook's membrane (see ref. 4.31). The geometry of the membrane resembles a wing plan form (see figure 4.3-1) with an applied end shear load. The membrane has constant thickness, and the material is isotropic.


Figure 4.3-1 Cook's Membrane

\subsection*{4.3.1.1 Model Description}

\subsection*{4.3.1.2 Analysis Description}

\subsection*{4.3.1.3 Available Solutions}

\subsection*{4.3.2 PROCEDURE USAGE}

Procedure COOR_MEM may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and all have default values thus making them optional. The formal syntax is as follows:
```

*call COOK_MEM ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (-) may be used to continue the argument list on the next line.

The allowable arguments for procedure COOK_MEM are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{lccl} 
Argument & Default Value & & Meaning \\
& ES_ & & Element Processor \\
ES_PROC & EX97 & & Element name \\
ES_PARS & 0. & & Element research parameters \\
MDATA & 4 & & Number of grids to analyze \\
MNODES & \(3,5,7,9\) & & Number of nodes on each edge \\
AUTO_DOF_SUP & <true> & & Automatic d.o.f. suppression \\
DRILLING_DOF & <false> & & Drilling (normal rotational) freedoms \\
CM_DB & CM.DB & & Cook membrane database name
\end{tabular}

\subsection*{4.3.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.3.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{4.3.3.2 CH_DB}

Name of Cook membrane database file (default=CM.DB). This file will contain all model data and analysis results.

\subsection*{4.3.3.3 DRILLING_DOF}

Drilling degree of freedom flag (default: 〈false〉). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO_DOF_SOP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "fiat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{4.3.3.4 ES_NAME}

Element name (default: EX97). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES.PROC. The default shell-element type, EX97, is a 9-node quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.3-2).

\subsection*{4.3.3.5 ES_PARS}

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.3.3.6 ES_PROC}

Element processor (default: ESi) This is the name of the structural element (ES) Processor that contains the shell element type you wish to employ in the model. The default shellelement, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{4.3.3.7 NDATA}

Specifies the number of model/mesh refinements to analyze (default: 4). The degree of mesh refinement for each analysis is defined by the NNODES parameter.

\section*{4．3．3．8 HYODES}

A list of integers which represent the number of nodes on each edge of the surface for each analysis to be performed（default： \(3,5,9,17\) ）．The length of the list is defined by the NDATA parameter．The numbers in the list must be consistent with the element type selected． For example，NHODES can be any list of numbers greater than 1 for 4 －node quadrilateral elements，whereas it must be a list of odd numbers greater than 1 for 9 －node quadrilateral elements．

\section*{4．3．4 USAGE GUIDELINES AND EXAMPLES}

Procedure Procedure COOX＿MEM may be used by preceding the procedure name by the＊call directive．Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called．A space or blank is required between the end of the procedure name and the left parenthesis．If the default values of the procedure arguments are to be used，then only the procedure name is required．
＊call COOK＿MEM（ ES＿PROC＝ES1 ；－－
ES＿NAME＝EX97 ；－－ ES＿PARS \(=0\). ；－－
NDATA \(=4\) ；－－ NNODES \(=3,5,9,17\) ；－－ AUTO＿DOF＿SUP＝〈true＞；－－ DRILLING＿DOF＝〈false〉；－－ CM＿DB＝CM．DB－－ ）
（E1）To perform an entire analysis using the default options，simply invoke the procedure without any arguments，i．e．，
＊call COOK．MEM
This call will perform a linear static analysis for each of the element configurations specified by the default NNODES parameter．Also，a fine grid analysis is performed with approximately four times the nodes of the last analysis specified by parameter mHODES．The results of the fine grid analysis are used to normalize the results of each requested analysis．All analysis results are presented in table format by the procedure：
\begin{tabular}{|c|c|c|}
\hline \multicolumn{3}{|r|}{Cook＇s Membrane Analysis Data Element Name \(=\) EX97} \\
\hline MODES & DISPLACEMENT & NORMALIZED \\
\hline 3 & \(0.22677967 \mathrm{E}+02\) & 0.9440006730146 \\
\hline 5 & \(0.23594924 \mathrm{E}+02\) & 0.982170233148691 \\
\hline 9 & \(0.23889961 \mathrm{E}+02\) & 0.994451542428496 \\
\hline 17 & \(0.23989798 \mathrm{E}+02\) & 0.998607390930779 \\
\hline
\end{tabular}

A plot showing the deformed shape of the membrane is provided in figure 4.3-2. The analysis model used 9 -node quadrilateral elements with 17 nodes per edge.


Figure 4.3-2 Cooks Membrane Deflection Plot

The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.3-1.

Table 4.3-1 CPU TIMES Table
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
\hline VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline VENVEX C220 & \\
\hline URAY-2 7.0 & \\
\hline
\end{tabular}

\subsection*{4.3.5 LIMITATIONS}

None.

\subsection*{4.3.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.3.7 PROCEDURE FLOWCHART}
\begin{tabular}{rl} 
COOK_MEM & (main procedure) \\
GEN_PLATE & (generate model) \\
CM_BC & (generate boundary conditions/loads) \\
L_STATIC & (perform linear static analysis)
\end{tabular}

\subsection*{4.3.8 PROCEDURE LISTING}

\subsection*{4.3.8.1 UNIX Script}
```

cd $SCR/$OSER
cp $CSM_PAC/proclib.gal proclib.gal
chmod u+v proclib.gal
re CMEX97.*
time testbed <<\endinput
*get echo,off
*set plib=28
*opon 28 proclib.gal /old
*add '$CSH_APP/cook_mem/cook_men.clp'
*call COOK_MEM ( ES_PROC = ES1 ; -- . Element Processor
ES_NAME = EX97 ; -- . Element name
ES_PARS = 0. ; -- . Element paraneters
NDATA = 4 ; -- . Number of grids to analyze
NNODES = 3,5,0,17 ; -- . Number of nodes per side
AOTO_DOF_SUP=<true> ; --
DRILLING_DOF=<false> ; --
CM_DB = CMEX97.LO1 -- . Database
)
*stop
*close 28 /dolete
[xqt exit
londinput

```

\subsection*{4.3.8.2 CLAMP Procedure}
cook_mem.clp
```

*procedure COOK_MEM ( es_proc = es1 ; -- . element processor
es_name = ex97 ; -- . element name
es_pari = 0. ; -- . elenent paraneters
ndata = 4 ; -- . Number of grids to analyze
nnodes = 3,5,9,17 ; -- . Number of nodes per side
auto_dof_sup=<true> ; --
drilling_dof=\langlefalse\rangle ; --
cz_db = cR.db -- . database
)

```

```

- procedure for analysis of in-plane bending of trapezoidal menbrane

```

```

*dof/i ndata = [ndata]
*def/i nnodes[1:<ndate>] = [nnodes]
*def/i nnodes[<<ndata\rangle+1\rangle] = < (<nnodes[<ndata\rangle]>*2) + 1\rangle
*def/i 1ib = 1
*do \$j=1,<<ndata>+1>
*if < <\&j\rangle/1t <<ndata>+1\rangle>>/then
*open <lib>, [cm_db] /new

```
```

    *else
    *open <lib>, zezscr.lib/nev
    *endif
    *def/i nnt = << <nodes[<$j>]>*<nnodes[<$j\rangle]>>
    *def/e - = 1.0
    *det/e nu = . 33
    *def/e h = 1.0
    *call GEN_PLATE ( es_proc = [es_proc] ; --
        es_name = [es_name] ; --
        es_pars = [es_pars] ; --
        nodes_1 = <nnodes[<<j\rangle]\rangle ; --
        nodes_2 = <nnodes[<$j\rangle]> ; --
        xyz1 = 48.,44., 0.; --
        xyz2 = 48.,60., 0. ; --
        xyz3 = 0.,44., 0.; --
        xyz4 = 0., 0., 0.; --
        0 = \langleब\rangle ; nu = \langlenu\rangle ; thickness = \langleh\rangle ; --
        auto_dof_sup = [auto_dof_sup]; --
        drilling_dof = [drilling_dof]; --
        bc_procedure = TP_BC )
        parfora static analysis
    *def/e solver_nare == BAND
    *cal1 L_STATIC
        store the results for this run
    [xqt avs
        MACRO <lib> STAT DISP 1 1 semilocal 2 <6*<nnodes[<$j>]>> 6 'disps
        STOP
    #dof/e avgdisp = 0.
    *do \jj=1,\langlennode:[<< j\rangle]>
    *def/\bullet avgdisp = <<avgdisp\rangle + <disps[<<jj\rangle]\rangle \rangle
    * enddo
    |def/\bullet avgd[<< j\rangle] : < <avgdisp> / <nnodes[<<j\rangle]> >
    Hehow nacro:
    *enddo

- delete the normalizing analysis
*close <lib>/delete
. done
*remark
*romark
*renark
*remark

```

```

\#rezark Cook's Merbrane Analysis Data
*remark Element Name = [es_name]

```

```

*ronaxk NODES DISPLACEMENT NORMALIZED
*renark
*do \$j=1,<ndata>

```

```

*enddo

```

```

\#renark
*ronark
*romark
*renark
[xqt EXIT
*end
*procedure TP_BC ( nodes_1 ; nodes_2 ; es_nodes ; drilling_dof=<talse> )

```

```

- boundary condition procedure for trapezoidal plate analysis

```

```

    *def/i nn1 = [nodes_1]
    *def/i nn2 = [nodes_2]
    *det/i nen = [es_nodes]
    *def/i node_A = 1
    *def/i node_B = <nn1>
    |def/1 node_D = < <nn1\rangle*\langlenn2\rangle>>
    *det/i node_C = < <node_D\rangle - <mn1\rangle + 1\rangle
    boundary conditions
edge c-d gets clamped
constraint = 1
zero 123456 c clamp edge c-d
<node_C> <node_D> . of constant theta
*if < [drilling_dof] /eq <ialse>> /then
zero 4 - renove drilling dof
<node_A> <node_D> everywhere
*ondif
loading conditions
edge a-b receives uniform shear in positive global y direction
*
[xqt aus
alpha
case title
1 'in-plane shear (1.e., bending) of trapezoidal membrane"
sysvec : appl forc i 1
*def/e p=1.0 . total axial force on model boundary
*if <<nen>/eq 4>/then
*def/i nelts m < <nn1> - 1 >
*def/e12.4 Pelt = < <p> / \langlenelts\rangle >

```
```

    *dot/e12.4 Pend = < <Pelt>/2. >
    *do $jn = <node_1>, <node_B>
        *if<<<<jn> /eq <node_A>> /or <<$jn> /eq <node_B>> > /then
            i=2 : j=<$jn>: <Pend>
            *olse
            i=2 : j=<&jn> : <Pelt>
    *ondif
    *onddo
    *elsoif < <nen> /eq 9 > /then
*dof/i nolts = < (<nn1> - 1)/2 >
*dof/e12.4 Polt = < <p> / <nelts> >
*def/e12.4 Polt_1 = < 1.*<Polt>/6. \rangle
*dof/e12.4 Polt_2 = < 2.*<Pelt>/6. >
*dof/012.4 Polt_4 = < 4.*<Polt>/6. >
midside nodes
*do $j4 = <<node_A> + 1>, <<node_B>-1>, 2
        i=2 : j= <$j4> : <Pelt_4>
*enddo
shared nodes
*if < <nolts>/gt 1 >/then
*do $j2 = <<node_A>+2\rangle, <<node_B>-2\rangle, 2
        i=2 : j= <$j2\rangle : <Pelt_2\rangle
*enddo
*endif
corner nodes
i=2 : j= <node_A> : <Pelt_1>
i=2 : j= <nodo_B> : <P@lt_1>
*ondif
*ond

```

\subsection*{4.3.9 REFERENCES}
4.3-1 Stanley, G. M.: Continuum-Based Shell Elements. PhD Dissertation, Stanford University, Stanford, CA, 1985.
4.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.4 Procedure ELASTICA}

\subsection*{4.4.1 GENERAL DESCRIPTION}

\subsection*{4.4.1.1 Problem Description}

This section describes a procedure that solves the classical large deflection, large rotation problem of a cantilevered beam with an applied end moment as shown in Figure 4.4-1. The nonlinear response of the cantilevered beam bent into a circle by an applied end moment is determined.


Thickness \(=1 . \mathrm{in}\).
\[
\begin{aligned}
\mathrm{M} & =2 \pi \mathrm{in}_{\mathrm{n}} \mathrm{Ib} / \mathrm{in} . \\
\mathrm{E} & =120 . \mathrm{psi} \\
V & =0 .
\end{aligned}
\]

Figure 4.4-1 Elastic Problem.

\subsection*{4.4.1.2 Model Description}

Procedure ELASTICA models the entire strip using 2-D quadrilateral elements. The mesh is generated using procedure GEN_PLATE. Two sets of boundary conditions are available. The set in procedure ELASTICA_BC imposes a clamped condition at one end of the strip and a moment at the other end. Procedure EL_ECC_BC also imposes a clamped condition at one end and an eccentric axial load at the other.

\subsection*{4.4.1.3 Analysis Description}

Procedure ELASTICA performs either a linear static analysis using procedure L_STATIC or a nonlinear static analysis using procedure NL_STATIC_1.

\subsection*{4.4.1.4 Available Solutions}


Figure 4.4-2 Nonlinear Response of Elastica Problems.


Figure 4.4-3 Sequence of Deformed Shapes.

\subsection*{4.4.2 PROCEDURE USAGE}

Procedure ELASTICA may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call ELASTICA ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (-) may be used to continue the argument list on the next line.

The allowable arguments for procedure ELASTICA are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For the procedure ELASTICA, the following table lists each argument, its default value and meaning.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES_PROC & ES1 & Select element processor \\
\hline ES_NAME & EX97 & Select element within ES_PROC \\
\hline ES_PARS & 0. & Set element-research parameters \\
\hline NNODES_X & 11 & Number of nodes in x -direction \\
\hline nNODES_Y & 3 & Number of nodes in y-direction \\
\hline PREP & <true> & Preprocessing flag \\
\hline POST & <true> & Postprocessing flag \\
\hline linear & <true> & Perform Linear Analysis \\
\hline NONLINEAR & <true> & Perform Nonlinear Analysis \\
\hline AUTO_DOF_SUP & <false> & Automatic degree of freedom suppression \\
\hline DRILLING_DOF & <true> & \\
\hline BEG_STEP & 1 & Beginning Load Step Number \\
\hline BEG_LOAD & . 01 & Beginning Load Factor \\
\hline NSTEPS & 10 & Number of Load Steps \\
\hline DBC & ELASTICA.DBC & Computational Database \\
\hline DBR & ELASTICA.DBR & Results Database \\
\hline
\end{tabular}

\subsection*{4.4.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.4.3.1 AOTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness
associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{4.4.3.2 BC_PROCEDURE}

Boundary condition procedure name (default: ELASTICA_BC). Two sets of boundary conditions are available. The set in procedure ELASTICA BC imposes a clamped condition at one end of the strip and a moment at the other end. Procedure EL_ECC_BC also imposes a clamped condition at one end and an eccentric axial load at the other.

\subsection*{4.4.3.3 BEG_LOAD}

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then BEG_LOAD \(=.1\) means that the first load step to be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is irrelevant for re-start runs. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.4.3.4 BEG_STEP}

Number of starting load step in nonlinear analysis (default=1). This argument is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1 . When re-starting (i.e., continuing in a subsequent run) a nonlinear analysis, BEG_STEP should be set to the number of the next step to be computed - not to the number of the last step computed. The solution procedure (NL_STATIC_1) will automatically use any previous step(s) required to continue the analysis - providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.4.3.5 DBC}

Name of computational database file (default=ELASTICA.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

\subsection*{4.4.3.6 DBR}

Name of results database file (default=ELASTICA.DBR). This file will contain one dataset called RESPOMSE. HISTORY generated during nonlinear analysis. The dataset will contain record groups - indexed by load step number - for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

\subsection*{4.4.3.7 DRILLING_DOF}

Drilling degree of freedom flag (default: 〈false〉). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the 1UTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SOP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{4.4.3.8 ES_NAME}

Element name (default: EX97). This argument specifies the name of the specific shellelement type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX97, is a 9 -noded quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.4-1).

\subsection*{4.4.3.9 ES_PARS}

Element research parameters (default: 0., ...). This array allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.4.3.10 ES_PRDC}

Element processor (default: ES1) This argument specifies the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.4-1).

\subsection*{4.4.3.11 NNODES_X}

Number of nodes along beam length (default: 11). This argument is the number of nodes along the \(x\)-direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, NNODES_X can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{4.4.3.12 NNODES_Y \(^{\text {Y }}\)}

Number of nodes along beam depth (default: 3). This argument is the number of nodes along the \(y\)-direction of the beam shell model. Note that this number should be consistent with the number of nodes per element. For example, MNODES_Y can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{4.4.3.13 MONLINEAR}

Nonlinear (postbuckling) analysis flag (default=<true>). This flag should be turned on to perform nonlinear analysis in the current run.

\subsection*{4.4.3.14 MSTEPS}

Maximum number of load steps to be computed in the current nonlinear analysis run (default=30). For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.4.3.15 POST}

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the ELASTICA.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed to archive special displacement and/or internal force component response histories post-facto.

\subsection*{4.4.3.16 PREP}

Preprocessing flag (default=<true>). This flag must be turned on the first time procedure ELASTICA is run, as it causes the model to be generated. If subsequent runs are used to perform other stages of the analysis (e.g., nonlinear restarts), then PREP must be set to <false> for those subsequent runs.

\subsection*{4.4.4 USAGE GUIDELINES AND EXAMPLES}

Procedure ELASTICA may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```

POST =<false>; --
NONLINEAR =<false>; --
NSTEPS = 10 ; --
DBC = ELASTICA.DBc ; -- . Computational database
DBr = ELASTICA.DBr -- . Results database)

```
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call ELASTICA

This call will perform linear buckling eigenvalue analysis and 10 steps of nonlinear analysis with a \(11 \times 3\) grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.4-1.

Table 4.4-1 CPU TIMES Table
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
\hline VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN \\
SUNVIEW 4.0 & \\
\hline CONVEX C220 \\
VERSION 7.0 & \\
\hline CRAY-2 \\
UNICOS 4.0 & \\
\hline
\end{tabular}
(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

\subsection*{4.4.5 LIMITATIONS}
(L1) Only 4-node and 9-node shell elements can be employed in the model. (Note: This can be easily modified.)

\subsection*{4.4.6 ERROR MESSAGES AND WARNINGS}

If you have to repeat the preprocessing phase, you need to either delete the computational (.DBC) database, or delete the ES. SUMMARY dataset. Otherwise, the element processors will be run more than once for each element function (e.g., FORM STIFFNESS), and the effect will be cumulative. This is due to a lack of explicit initialization in the registration of element processors using procedure ES.

\subsection*{4.4.7 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
ELASTIC & (main procedure) \\
GEH_PLATE & (generate model) \\
ELASTICA_BC & (generate boundary conditions and end moment) \\
EL_ECC_BC & (generate boundary conditions and eccentric axial load) \\
L_STATIC & (perform linear static analysis) \\
IMPERFECTION & (superpose buckling modes as imperfections) \\
WL_STATIC_1 & (perform nonlinear static analysis) \\
HISTORY & (archive selected displacement/force histories)
\end{tabular}

\subsection*{4.4.8 PROCEDURE LISTING}

\subsection*{4.4.8.1 UNIX Script}

\author{
elastica.com
}
```

cd $SCM/$uSER
cp CSM_PRC/proclib.gal proclib.gal
chmod ut■ proclib.gal
rm ELASTICA.*
tine testbed << \endinput
*set echo,off
*set plib=28
*open/old 28 proclib.gal
*add '\&CSH_APP/olastica/olastica.clp'
*def/a solver_name xx ITV
*call ELASTICA ( ES_PROC = ES1 ; --
ES_RAME = EX97 ; --
ES_PARS = 0.0 ; --
MNODES_I = 11 ; --
MNODES_Y = 3 ; --
LINEAR=<false>; HOMLINEAR =<true>; --
NSTEPS = 36;drilling_dofz<false> ; --
DBc = ELISTICA.DBC ; -- . Computational database
DBr = ELASTICA.DBr -- . Results database
)

```
*stop
londinput

\subsection*{4.4.8.2 CLAMP Procedure}
elastica.clp
```

*procedure ELASTICA ( ES_PROC = ES1 ; -- .
ES_NIME = EX97 ; -- .
ES_PARS = 0. ; --
NNODES_X = 11 ; -- .
NNODES_Y = 3 ; -- .
PREP =<true>; -- .
POST =<true>; -- .
LINEAR =<true>; -- .
NONLINEAR =<true>; -- .
AOTO_DOF_SUP =\langlefalso\rangle; -- .
DRILLING_DOF z<true>; -- .
BEG_STEP = 1 ; -- .
BEG_LOAD = .01; -- .
NSTEPS = 10 ; -- . Number of load stops
DBC = ELASTICA.DBC ; -- . Computational database
DBr = ELASTICA.DBr -- . Results database
)
-
CSM Testbed Procedure for Analysis of ELASTICA Problen
*open 1, [DBC]
. Generate Plate Model of Cantilever Beam
*if < [PREP] > /then
*Call GEN_PLATE ( ES_PROC=[ES_PROC] ; ES_NAME=[ES_NAME] ;--
NODES_1 =[NNODES_X] ; NODES_2 =[NNODES_Y] ;--
E=120. ; NU = 0.; THICKNESS =1. ; --
xyz1=0.,0.,0.; xyz2=10.,0.,0.; --
xyz3=10.,1.,0.; xyz4=0.,1.,0.; --
AUTO_DOF_SUP =[auto_dof_sup] ; --
DRILLING_DOF =[drilling_dof] ; --
BC_PROCEDURE = ELASTICA_BC )
*toc
*ondif
. Parforn Solution
*if < [LINEAR] > /then
*call L_STATIC
*if < [POST] > /thon
*open 2, [DBr]
*dof/a ds_r = [ES_PROC].[ES_NIME].[NNODES_Y].[NNODES_Y]
*call HISTORY ( input_ldi =1 ; input_ds =STAT.DISP.1.1; --
output_ldi=2 ; output_ds=\langleds_r> ; --
output_rn =LATERAL_DISP; nodes=1; component=3 )
*call HISTORY ( input_ldi =1 ; input_ds =STAT.DISP.1.1; --
output_ldi=2 ; output_ds=\langleds_r> ; --

```
```

    output_rn =END_ROTATION; nodes=1; component=5 )
        *call HISTORY ( input_ldi =1 ; input_ds =STAT.DISP.1.1; --
                        output_ldi=2 ; output_ds=<ds_r> ; --
                        output_rn =1XIAL_DISP; nodes=1; conponent=1 )
        *remark
        *renark
        *renark
        ---------------------------------------------------------------
        *renark
        *renark ELASTICL Linear Results
        *renark
        *renark Exact:
        *renark LATERAL_DISP (compare with W at node 1) = 31.41
        *remark END_ROTATION (compare vith RV at node 1) = 6.28
        *remark AXIAL_DISP (compare vith O at node 1) m 0.0
        *renark
        *romark Conputed:
        *print rec 2, <de_r> LATERAL_DISP /1=drx
        *print rec 2, <ds_r> END_ROTATION /1=drx
        *print rec 2, <ds_r> AXIAL_DISP /1=drx
        *renark
        *renark
        *remark
    *endif
    *endif
*if < [NONLIMEAR] > /then
*dof ns_overwrite = <true>
*call HL_STATIC_1 ( beg_stop = [BEG_STEP] ; --
max_stop: = [MSTEPS] ; --
bog_load = [BEG_LOAD] ; --
max_load =1.00 ; --
NL_GEOM = 2 ; --
COROTATION = 1 ; --
Noninal_DB = [DBr] ; --
Honinal_DS = [ES_PROC].[ES_NAME].[NNODES_Y].[MNODES_Y] ;--
N_SELECT = 2 ; --
SEL_MODES = 1, 1;SEL_DOFS = 1,3)
*toc [DBR]
*ondif
[xqt exit
*end
*procedure EL_ECC_BC ( nodes_1; nodes_2; es_nodes; drilling_dof=<false> )
. Define Loads and Boundary Conditions for ELASTICI Model
*def/i nn_tot = < [nodes_1]*[nodes_2] >

```

```

- DEPINE BOUNDIRY CONDITIONS

```

```

•
[xqt TAB
CON 1
*if < [drilling_dof] /eq <false> > /then

```
```

        ZERO 6 . Suppres: MOMHAL hOtATIONS Everyvhere
        *do {n=1,<nn_tot>
        <$n>
        *enddo
    *endif
ZERO 2 . Suppress LATERAL MOTION Everywhere
*do $n=1,\langlenn_tot>
        <$n>
*onddo
ZERO 4 . Suppress TORSIONAL ROTATION Everywhere
*do $n=1,\langlenn_tot>
        <$n>
*enddo
ZERO 1,2,3,4,5,6 : CARTILEVER Right End of Bean
*do %n = [nodes_1], <nn_tot>, [nodes_1]
<\$n>
*enddo
. x\#\#\#\#E=x=m=n=

- Define Loads

```

```

•
[xqt \US
. Apply Uniform Eccentric Load Consistently (ovor unit uidth)
. Px results in Ronont about Y of 2*PI aince Eccentricity = .5
*dof/012.4 Px = <-4.*<PI\rangle >
*dof/o12.4 Px_1 = < <Px>/2. >
SISVEC : APPL FORC 1
*if < [ES_MODES]/eq 4 >/then
i=1 : j=1 : <Px_1>
i=1 : j=<[nodes_1]+1> : <Px_1>
*elseif < [ES_NODES] /eq }9\mathrm{ > /thon
*de1/012.4 Px_1 : < <Px>/6. >
*dof/012.4 Px_4 = < 4*<Px>/6. >
i=1 : j=1 : <Px_1>
i=1 : j=<[nodes_1]+1\rangle : <Px_4>
i=1 : f=<(2\#[nodes_1])+1\rangle : <Px_1>
*ondif
*ond
*procedure ELASTICA_BC ( nodes_1; nodes_2; es_nodes; drilling_dof=<false>)
Define Loads and Boundary Conditions for ELASTICA Model
*def/i nn_tot = < [nodes_1]*[nodes_2] >

```

```

- DEPINE BOUNDARY CONDITIONS

```

```

[xqt TAB
CON 1

```
```

*if < [drilling_dof] /oq <falso>) /thon
ZERO 6 . Supprese NORMAL ROTATIONS Everywhere
*do {n=1,<nn_tot>
<\$n>
*onddo
*endif
ZERO 2 . Suppress LATERAL MOTION Everywhere
*do $n=1,<nn_tot>
    <$n>
*enddo
ZERO 4 . SuppresE TORSIONAL ROTATION Everywhere
*do $n=1,<nn_tot>
    <$n>
*onddo
ZERO 1,2,3,4,5,6 . CAKTILEVER Right End of Beam
*do in = [nodes_1], <nn_tot>, [nodes_1]
<\$n>
*onddo

```

```

. Dofine Loads

- =xエ=3x=xIx==
[xqt AOS
. Apply Uniform M_y Consistently (over unit vidth)
*dof/012.4 My = < 2.*<PI>>
*dof/e12.4 My_1 = < <My>/2. >
STSVEC : APPL FORC 1
*if < [ES_MODES] /eq 4 >/then
i=5 : j=1 : <My_1>
i=5 : j=<[nodes_1]+1> : <My_1>
*elseif < [ES_NODES] /eq }9>/tho
*def/012.4 My_1 = < < My>/6. >
*def/012.4 Hy_4 = < 4*<My>/6. >
i=5 : j=1 : <ny_1>
i=5 : j=\langle[nodes_1]+1\rangle : <Hy_4\rangle
i=5 : j=<(2*[nodes_1])+1> : <My_1>
*endif
*ond

```

\subsection*{4.4.9 REFERENCES}
4.4-1 Timoshenko, S. P.; and Gere, J. M.: Theory of Elastic Stability, McGraw-Hill, New York, 1961.
4.4-2 Stanley, G. M.: "Continuum-Based Shell Elements," PhD Dissertation, Stanford University, 1985.
4.4-3 Donnel, L. H.: Beams, Plates, and Shells, McGraw-Hill, New York, 1976.
4.4-4 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.5 Procedure EULER_COLUMN}

\subsection*{4.5.1 GENERAL DESCRIPTION}

\subsection*{4.5.1.1 Problem Description}

This application problem involves a linear bifurcation buckling analysis of a thin isotropic strip subjected to uniform compression (see Figure 4.5-1). This problem is important in that plate and shell elements are frequently used to model stiffeners of stiffened panels. When these panels buckle in an "overall" Euler modeshape the stiffeners must also buckle in their plane (see Figure 4.5-2).


Figure 4.5-1 Euler Column Problem


Figure 4.5-2 Euler Buckling Modeshape

\subsection*{4.5.1.2 Model Description}

Procedure EOLER_COLUNN models the entire strip using 2-D quadrilateral elements. The mesh is generated using procedure GEN_PLATE and the boundary conditions are specified in procedure \(\bar{C} \bar{L} L \overline{U M N} \_\bar{B}\).

\subsection*{4.5.1.3 Analysis Description}

Procedure EULER_COLUMN performs a single linear buckling analysis with a specified prestress. The solution procedure L_STABIL_1 is used to perform the buckling analysis.

\subsection*{4.5.1.4 Available Solutions}

Analytical solution for the Euler buckling load is readily obtained from reference 4.5-1, page 22-28. The Euler buckling load is given by
\[
P_{E U L E R}=\frac{\pi^{2} E I}{L^{2}}
\]
where
\[
\begin{aligned}
E & =\text { Young's Modulus } \\
I & =\text { Moment of Inertia }=\frac{1}{12} t h^{3} \\
L & =\text { Column Length } \\
t & =\text { Column Thickness } \\
h & =\text { Column Width }
\end{aligned}
\]

For a specified uniform membrane stress resultant \(N_{x}^{o}\) of \(-1000 \mathrm{lb} / \mathrm{in}\)., the corresponding buckling load factor is
\[
\left(N_{x}\right)_{E U L E R}=P_{E U L E R} / h=\lambda_{E U L E R} N_{x}^{o}
\]

For the geometry and material properties used as default values of the procedure arguments, the exact solution for simple-support boundary conditions corresponds to a value of 0.456926 for \(\lambda_{E U L E R}\) (i.e., the smallest eigenvalue).

\subsection*{4.5.2 PROCEDURE USAGE}

Procedure EULER_COLUNR may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call EOLER_COLUNN ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure EULER_COLUMN are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline E & 10.E6 & Young's Modulus \\
\hline ES_PROC & ES1 & Element Processor \\
\hline ESIMAME & EX47 & Element name \\
\hline LX & 30.0 & Length in \(x\)-direction \\
\hline LY & 1.0 & Length in y -direction \\
\hline WODES_1 & 31 & Number of nodes along \(x\) \\
\hline HODES_2 & 3 & Number of nodes along y \\
\hline NO & 0.0 & Poisson's ratio \\
\hline PRINT & <false> & Print flag \\
\hline PS_1 & -1000.0 & Uniform axial compression prestress \\
\hline THICKNESS & 0.05 & Thickness \\
\hline
\end{tabular}

\subsection*{4.5.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.5.3.1 E}

Young's elastic modulus (default: \(10.0 \times 10^{6} \mathrm{psi}\) ).

\subsection*{4.5.3.2 ES_NAME}

Element name (default: EX47). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX47, is a 4 -noded quadrilateral element implemented in processor ES1, and described in the Computational Structural Mechanics Testbed User's Manual (see ref. 4.5-2).

\subsection*{4.5.3.3 ES_PROC}

Element Processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES1, is described in the Computational Structural Mechanics Testbed User's Manual (see refs. 4.5-2).

\subsection*{4.5.3.4 LX}

Length of the plate model in the \(\boldsymbol{x}\)-direction (default: 31.0 inches).

\subsection*{4.5.3.5 LY}

Length of the plate model in the \(y\)-direction (default: 1.0 inches).

\subsection*{4.5.3.6 \({ }^{\text {NODES_1 }}\)}

Number of nodes along x -direction (default: 31).

\subsection*{4.5.3.7 MODES -2}

Number of nodes along \(y\)-direction (default: 3 ).

\subsection*{4.5.3.8 NO}

Poisson's ratio (default: 0.0).

\subsection*{4.5.3.9 PRINT}

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, modeshapes, stresses) will be printed.

\subsection*{4.5.3.10 PS_1}

Uniform axial compression prestress (default: -1000 lb/in.).

\subsection*{4.5.3.11 THICKNESS}

Thickness of the plate (default: 0.05 inches).

\subsection*{4.5.3.12 WTDEN}

Weight density (default: \(0.1 \mathrm{lb} / \mathrm{in} .^{3}\) ). Processor LAU converts the weight density to mass density.

\subsection*{4.5.4 USAGE GUIDELINES AND EXAMPLES}

Procedure EULER_COLUNR may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call EOLER_COLUMN ( ES_PROC = ES1 ; ES_NAME = EX47 ; --
LX = 7.5 ; --
LY = 10.0 ; --
E = 30.E6 ; --
NU = 0.3 ; --
PRIMT = <false> ; --
THICRNESS = 0.1 ; --
UTDEN = 0.1 )

```
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,
```

*call EULER_COLUNN

```

Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.5-1.

Table 4.5-1 CPU TIMES Table
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 \\
VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CONVEX C220 \\
VERSION 7.0 & \\
\hline CRAY-2 \\
UNICOS 4.0 & \\
\hline
\end{tabular}

\subsection*{4.5.5 LIMITATIONS}

None

\subsection*{4.5.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.5.7 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
EULER_COLUNA & (main procedure) \\
GEN_PLATE & (define model) \\
COLUNN_BC & (define simple-support boundary conditions)
\end{tabular}

\subsection*{4.5.8 PROCEDURE LISTING}

\subsection*{4.5.8.1 UNIX Script}

```

*open 1 euler_colunn.101
*set echo off
*def/a eigensolver_name = EIG2
*def/a molver_name = INV
-
*sot plib=28
*open 28 proclib.gal /old
*add '\&CSM_APP/euler_column/euler_column.clp'

- Inplane Buckling of a Thin Strip
- 

*call EOLER_COLOMN ( es_name='ex97'; es_proc='es7')
-
[xqT EXIT
\endinput

```

\subsection*{4.5.8.2 CLAMP Procedure}
```

euler_column.clp

```
```

*procedure EOLER_COLUMN ( es_name = 'EX47'; --
\bullet__proc = 'ESI' ; --
- = 10.0e+6; --
nu = . 3 ; --
thicknesg= 0.05 ; --
ps_1 = -1000.0; --
1x =30.0 ; --
ly =1.0 ; --
nodes_1 = 31 ; --
nodes_2 = 3 )
•
*call GEN_PLATE ( es_proc=[es_proc];es_name=[es_name]; --
xyz1=0.0,0.0,0.0 ; --
xyz2=[lx],0.0,0.0 ; --
xyz3=[1x],[1y],0.0 ; --
xyz4=0.0,[1y],0.0 ; --
nodes_1=[nodes_1]; nodes_2=[nodes_2]; --
nsect=1; ex[e];nu=[nu];thickness=[thickness]; --
bc_procedure= 'COLOMN_BC' )
*toc 1
[xqT TAB
TITLE'EULER COLUMR BUCKLING PROBLEM
*call L_STABIL_1 ( pE_1=[ps_1]; print=<true>)
*toc 1
*ond
*procedure COLUNN_BC (nodes_1=31; nodes_2=3; --
es_nodes=<es_nen>; drilling_dof=\langletrue>)
*dof/i n1 = 1
*def/i n2 = [nodes_1]
*def/i n3 = < [nodes_1]*[nodes_2] >
*def/i n4 = < [nodes_1]*([nodes_2]-1) + 1 >
CON CASE 1

```
```

2ERO 3 4 5 : <n1>,<n3>
ZERO 2 : <n1>,\langlen4\rangle,[nodes_1]
ZERO 2 : <n2>,\langlen3>,[nodes_1]
*if < [drilling_dof] /eq 0 >/then
2ERO 6: <n1>,<n3>
*ondif
*ond

```

\subsection*{4.5.9 REFERENCES}
4.5-1 Brush, Don O. and Almroth, Bo O.: Buckling of Bars, Plates, and Shells, McGrawHill Book Company, New York, 1975.
4.5-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.6 Processor FOCUS_PANEL}

\section*{THIS SECTION UNDER PREPARATION}

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\subsection*{4.7 Processor FREE_EDGE}

THIS SECTION UNDER PREPARATION

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\subsection*{4.8 Processor GEN_STF_PANEL}

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\subsection*{4.9 Procedure HINGED_CYL}

\subsection*{4.9.1 GENERAL DESCRIPTION}

To verify the nonlinear aspects of the shell-element formulation, implementation, and adaptive (Crisfield/Riks) quasi-static solution algorithm, the snap-through of a hinged cylinder under a point force is considered. This problem, which involves only moderate geometric nonlinearities, is nevertheless interesting due to the limit-point characteristics of the loaddisplacements curve. Furthermore, due to the popularity of the problem, an abundance of numerical results are available for comparison.
This section describes a prcedure that solves the hinged cylinder problem (see figure 4.9-1) which exhibits snap-through behavior.

\(R=2540 \mathrm{~mm}\)
\(\mathrm{L}=254 \mathrm{~mm}\)
\(\mathrm{h}=12.7 \mathrm{~mm}\)
\(\theta=.1 \mathrm{rad}\)
\(E=3102.75 \mathrm{~N} / \mathrm{mm}^{2}\)
\(v=.3\)

Figure 4.9-1 Hinged Cylinder Problem.

\subsection*{4.9.1.1 Model Description}

\subsection*{4.9.1.2 Analysis Description}

\subsection*{4.9.1.3 Available Solutions}

\subsection*{4.9.2 PROCEDURE USAGE}

Procedure HINGED_CYL may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call HINGED_CYL ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure HINGED_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES_PROC & ES1 & Element Processor \\
\hline ES_NAME & EX97 & Element name \\
\hline ES_PARS & 0. & Element research parameters \\
\hline MMODES_A & 5 & Number of axial nodes \\
\hline nnodes_C & 5 & Number of circumferential nodes \\
\hline SPEC_DIS & <false> & Specified displacements \\
\hline 1OTO_DOF_SUP & <true> & Automatic d.o.f. suppression \\
\hline DRILLING_DOF & <false> & Drilling (normal rotational) freedoms \\
\hline HSTEPS & 10 & Number of nonlinear load steps \\
\hline BEG_STEP & 1 & Starting load step number \\
\hline Max_CUTS & 3 & Maximum number of step cuts (halvings) \\
\hline BEG_LOAD & . 1 & Starting load factor \\
\hline Max load & 1.0 & Maximum load factor \\
\hline DBC & CC. DBC & Computational database name \\
\hline DBR & CC.DBR & Results database name \\
\hline PREP & <true> & Perform pre-processing (model generation) \\
\hline LINEAR & <false> & Perform nonlinear (post-buckling) analysis \\
\hline TH_SCALE & 1.0 & \\
\hline TOL & . 001 & \\
\hline
\end{tabular}

\subsection*{4.9.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.9.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{4.9.3.2 BEG_LOAD}

Starting load factor in nonlinear analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then BEG_LOAD \(=.1\) means that the first load step to be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is irrelevant for re-start runs. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.9.3.3 BEG_STEP}

Number of starting load step in nonlinear analysis (default=1). This is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1 . When re-starting (i.e., continuing in a subsequent run) a nonlinear analysis, BEG_STEP should be set to the number of the next step to be computed - not to the number of the last step computed. The solution procedure (NL_STATIC_1) will automatically use any previous step(s) required to continue the analysis - providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.9.3.4 DBC}

Name of computational database file (default=HC.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

\subsection*{4.9.3.5 DBR}

Name of results database file (default \(=\mathrm{HC}\). DBR). This file will contain one dataset called RESPONSE. HISTORY generated during nonlinear analysis. The dataset will contain record groups -- indexed by load step number - for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

\subsection*{4.9.3.6 DRILLING_DOF}

Drilling degree of freedom flag (default: 〈false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AUTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) clements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SOP is set.

\subsection*{4.9.3.7 ES_NAME}

Element name (default: EX97). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shellelement type, EX97, is a 9 -noded quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.9-1).

\subsection*{4.9.3.8 ES_PARS}

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.9.3.9 ES_PROC}

Element processor (default: ES1) This is the name of the structural element (ES) Processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{4.9.3.10 MAX_CUTS}

Maximum number of load step cuts in nonlinear analysis (default=3). For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.9.3.11 MAXLOAD}

Maximum load factor in nonlinear analysis (default=1.0). This sets an upper limit for the load level, which can be a convenient way of terminating the arc-length controlled solution
algorithm employed within procedure NL_STATIC_1. Since the load factor is actually an unknown in this solution procedure, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. Thus, the analysis will be terminated when either MAX_LOAD is exceeded or NSTEPS is exceeded - whichever comes first. For more details, refer to the same argument name under solution procedure ML_STATIC_1.

\subsection*{4.9.3.12 NHODES_A}

Number of axial nodes (default: 7). This is the number of nodes you wish to have along the axial direction of the cylindrical shell model, i.e., along one-tenth of the full cylinder's length. Note that this number should be consistent with the number of nodes per element. For example, HNODES_A can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{4.9.3.13 NNODES_C}

Number of circumferential nodes (default: 7). This is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, i.e., along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, NNODES_C can be any number greater than 1 for 4node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{4.9.3.14 MONLINEAR}

Nonlinear (post-buckling) analysis flag (default=〈true>). This flag should be turned on if you want to perform nonlinear analysis in the current run. The pre-requisites are preprocessing, stability analysis and imperfection superposition, all of which may be performed either in a previous run or in the current run - by setting the appropriate arguments (i.e., PREP, STABILITY and IMPERFECTION).

\subsection*{4.9.3.15 HSTEPS}

Maximum number of load steps to be computed in the current nonlinear analysis run (default=30). For more details, refer to the same argument name under solution procedure ML_STATIC_1.

\subsection*{4.9.3.16 POST}

Postprocessing flag (default=<false〉). This flag should be turned on if you want selected response-history parameters to be added to the HC.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed if you wish to archive special displacement and/or internal force component response histories post-facto.

\subsection*{4.9.3.17 PREP}

Preprocessing flag (default=<true>). This flag must be turned on the first time procedure COMPRESSED_CYL is run, as it causes the model to be generated. If subsequent runs are used to perform other stages of the analysis (e.g., nonlinear re-starts), then PREP must be set to <false> for those subsequent runs.

\subsection*{4.9.3.18 SPEC.DIS}

Specified displacement flag (default: 〈false>). By setting this flag to <true>, uniform axial end-shortening is imposed instead of the uniform axial loading. This can make a significant difference in both the buckling and post-buckling response, and is not recommended for novice users of this procedure. This is because thin axially-compressed shells are not only imperfection sensitive, but also boundary condition sensitive, and uniform axial loading does not correspond (exactly) to uniform axial edge displacements. Note that the reference specified displacement (i.e., end-shortening) magnitude equals .01 inches, and corresponds to an axial load of about .467 times the classical buckling load.

\subsection*{4.9.4 USAGE GUIDELINES AND EXAMPLES}

Procedure HINGED_CYL may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
```

*call HINGED_CYL

```

This will perform linear buckling eigenvalue analysis and 30 steps of nonlinear analysis with a \(5 \times 5\) grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of systems is shown in Table 4.9-1.

Table 4. -1 CPU TIMES Table
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
\hline VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CONVEX C220 \\
VERSION 7.0 & \\
\hline URAY-2 & \\
\hline
\end{tabular}
(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

\subsection*{4.9.5 LIMITATIONS}

\subsection*{4.9.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.9.7 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
HINGED_CYL & (main procedure) \\
GEN_SHELL & (generate model) \\
HC_BC & (generate boundary conditions and applied loads) \\
HCD_BC & (generate boundary conditions and specified displacements) \\
L_STATIC_1 & (perform linear static analysis) \\
HL_STATIC_1 & (perform nonlinear static analysis) \\
HISTORY & (archive selected displacement/force histories)
\end{tabular}

\subsection*{4.9.8 PROCEDURE LISTING}

\subsection*{4.9.9 REFERENCES}

\section*{4.9-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.}

\subsection*{4.10 Procedure PEAR_CYL}

\subsection*{4.10.1 GENERAL DESCRIPTION}

The nonlinear shell response of cylindrical shells with a noncircular cross-section became the subject of intense research in the early 1970's. Early Space Shuttle fuselage configurations were noncircular, and the "pear-shaped" cross-section was a leading candidate. The pear-shaped cylinder shown in Figure 4.10-1 has been adopted by many researchers and the behavior of this shell subject to a uniform end-shortening investigated (e.g., refs. 4.101 and 4.10-2). The results in this section are compared with results reported by Hartung and Ball (ref. 4.10-1) and by Almroth and Brogan (ref. 4.10-2). In all cases, only one fourth of the cylinder is modeled. The shell is isotropic with a uniform thickness of 0.01 inches. The boundaries are simply supported.


Figure 4.10-1 Pear-shaped cylinder - geometry, properties, and loading.

\subsection*{4.10.1.1 Model Description}

The finite element model of the pear-shaped cylinder is generated in segments as shown in figure 4.10-2. Joint locations and element connectivity are defined using the mesh generating capabilities of Testbed processors TAB and ELD. The user must specify only the number of elements along the \(45^{\circ}\) arc of segment 1 (NEL_ARC), the number of elements along the flat edge of segment 2 (NEL_FLaT), and the number of elements and through the depth of the cylinder in the \(z\)-direction (NEL_DEPTH). The finite element mesh, loading, and constraints are then automatically generated. In order to facilitate both the model generation and the results interpretation, several alternate reference frames have been defined.

Reference frames 1,2 , and 3 are defined automatically in processor TAB as global reference frames, rotated \(-90^{\circ}\) about \(z\) axis, and rotated \(90^{\circ}\) about \(y\) axis, respectively. Reference frames 4,5 , and 6 are translations of the origin to points A, B, and C, respectively (see figure 4.10-2). Frames 7 and 8 involve rotations about the global \(z\)-axis and include no translations.

The results of interest in this analysis are the normal and tangential stresses and displacements. Each joint is therefore assigned a joint reference frame to which displacements, constraints, and loads are referred. The stress component directions are defined by the order of the element connectivity using the element network generators of processor ELD.

Segment 1 of the finite element model is generated using reference frame 4. The FORMAT \(=2\) statement of the TAB/JLOC subprocessor allows for the generation of a regular mesh of nodes on the cylindrical surface of segment 1 . The TAB/JLOC input is in cylindrical coordinates with point \(A\) as the origin of the cylindrical frame. The joints in this segment are each assigned joint reference frame -4 indicating a cylindrical frame with the joint 1 -axis concident with the outward normal at each joint, the joint 3 -axis coincident with the global \(z\)-axis, and the joint 2 -axis coincident with the tangent to each joint.

Segment 2 is also generated using frame 4 although in this case, frame 4 is employed as a rectangular frame. The TAB/JLOC subprocessor generates a regular mesh of nodes connecting the four corners of the rectangular surface of the segment. The TAB/JLOC input is in cartesian coordinates with point \(A\) at the origin of the rectangular frame. Each joint in this segment is assigned joint reference frame 7 indicating that the 1 - and 2 -axes of each joint are coincident with \(x\) and \(y\) axes rotated \(135^{\circ}\) about global \(z\). The joint 3 -axis and global \(z\)-axis are coincident.

Segment 3, a \(135^{\circ}\) section of arc, is generated using reference frame 5 , centered at point B. As with segment 1, the FORMAT \(=2\) statement of the TAB/JLOC subprocessor is used to generate a regular mesh of nodes on the cylindrical segment. The number of elements around the circumference of this segment is assumed to be three times the number of elements around the circumference of Segment 1. The joints in this segment are each assigned joint reference frame -5 indicating a cylindrical frame with the joint 1 -axis coincident with the outward normal at each joint, the joint 3 -axis coincident with the global \(z\)-axis, and the joint 2 -axis coincident with the tangent to each joint.

Segment 4 is generated using reference frame 6, centered at point C. Frame 6 is used as a rectangular frame to generate a regular mesh of nodes connecting the four corners of the rectangular surface of the segment. The number of elements along this segment is half that used in segment 2. Each joint in this segment is assigned joint reference frame 8 indicating that the 1- and 2 -axes of each joint are coincident with \(x\) - and \(y\) - axes rotated \(270^{\circ}\) about global \(z\)-axis. The joint 3 -axis and global \(z\)-axis are coincident.

Three finite element models were considered in this study as shown in Figure 4.10-3. Mesh 1 ( \(3 \times 26\) ) has three nodes through the cylinder depth and 26 nodes around the half-cylinder circumference (see Figure 4.10-3a). The mesh is composed of 504 -node quadrilateral shell elements (ES1/EX47 or ES5/E410) and a total of 78 nodes. Mesh \(2(5 \times 37)\) has five nodes through the cylinder depth and 37 nodes around the half-cylinder circumference (see Figure \(4.10-3\) b). This mesh accommodates both 4 - and 9 -node elements and will contain either 144 4-node (ES1/EX47 or ES5/E410) or 369 -node (ES1/ES97) quadrilateral shell elements and 185 nodes. Mesh \(3(7 \times 51)\) has seven nodes through the cylinder depth and 51 nodes around the half-cylinder circumference (see Figure 4.10-3c). Mesh 3 accommodates both 4- and 9-node elements and will contain either 300 4-node (ES1/EX47 or ES5/E410) or 759 -node (ES1/EX97) quadrilateral shell elements and 357 nodes.


Figure 4.10-2 Model Generation Strategy and Reference Frames

(a) Mesh 1.


4-node elements
(b) Mesh 2.


4-node elements


9-node elements


9 -node elements
(c) Mesh 3.

Figure 4.10-3 Finite element models of pear-shaped cylinder.

\subsection*{4.10.1.2 Analysis Description}

\subsection*{4.10.1.3 Available Solutions}

The pear-shaped cylinder is representative of a shell-type structure with a complex nonlinear collapse behavior. The shell response becomes nonlinear at a very low value of applied end-shortening, and the normal deflections of the flat portions of the shell increase rapidly. The nonlinear analysis of the cylinder is performed using the procedure NL_STATIC_1. The distribution of the normal displacement (normal to the shell surface) is shown in Figure 4.10-4 as a function of the applied load for the point of maximum normal displacement (at \(x=0, \theta=180^{\circ}\) ) and for all meshes and element types considered. These results indicate that a converged solution is provided by the ES1/EX97 elements as the curves for Mesh 2 and Mesh 3 in Figure 4.10-4c are nearly identical. These three solutions correspond to a discretization with 185 nodes with either 144 4-node flat classical (ES5/E410) elements, 144 4-node flat shear-flexible (ES1/EX47) elements, or 369 -node curved shear-flexible (ES1/EX97) elements.

A comparison of the three solutions obtained using Mesh 2 is provided in Figure 4.10-5. The effects of transverse shear flexibility, present in the ES1/EX97 and ES1/EX47 elements but not present in ES5/E410 elements, are apparent near collapse. The response curves begin to separate slightly at approximately half the elastic collapse load with the shear flexible elements exhibiting a consistent, yet slightly lower, stiffness than the response obtained using the ES5/E410 element. The elastic collapse loads obtained using the 4-node flat elements is nearly the same. However, results obtained using higher-order curved elements to model the shell and its response are approximately \(10 \%\) lower than the collapse loads obtained using the flat elements.

(a) Models using 4-node flat classical (ES5/E410) elements.

(b) Models using 4-node flat shear-flexible (ES1/EX47) elements.

(c) Models using 9 -node curved shear-flexible (ES1/EX97) elements.

Figure 4.10-4 Nonlinear response of pear-shaped cylinder.


Figure 4.10-5 Nonlinear response of pear-shaped cylinder - Mesh 2.

Hartung and Ball (ref. 4.10-1) reported an elastic collapse load of 2372 pounds using a finite difference version of STAGS. Several years later, Almroth and Brogan (ref. 4.10-2) performed a convergence study using the finite element version of STAGS and estimated that the elastic collapse load was between 2300 and 2400 pounds. These results, along with the Testbed results, and results from independent elastic collapse analyses using the STAGSC-1 computer code, are summarized in Table 4.10-1.

In Figure 4.10-6, the normal deflection at \(x=0\) is plotted as a function of the circumferential coordinate \(\theta\) for four different levels of applied load: 154, 300, 1689, and 2464 pounds (load steps \(10,20,30\) and 40 respectively). The final load step (step 40 at 2464 pounds) occurs just after collapse. The flat portions of the shell, from \(45^{\circ} \leq \theta \leq 90^{\circ}\) and \(157.5^{\circ} \leq\) \(\theta \leq 180^{\circ}\), show a rapid growth in normal deflections. Associated with this growth is a redistribution of the longitudinal stress indicating that the curved portions begin to take up a larger percentage of the total axial load. This type of behavior can be seen in Figure 4.10-7 which plots the longitudinal stress resultant as a function of the circumferential coordinate for load steps \(10,20,30\) and 40.
4.10-8

Table 4.10-1 Elástic collapse lóads for pear-shaped cylinder.
\begin{tabular}{|l|c|c|c|}
\hline Source & \begin{tabular}{c} 
Element \\
Name
\end{tabular} & Mesh \((1)\) & \begin{tabular}{c} 
Elastic Collapse Load, \\
pounds
\end{tabular} \\
\hline Hartung and Ball & \((2)\) & \(4 \times 40\) & 2372 \\
\hline Almroth and Brogan & 411 & \(3 \times 27\) & 3586 \\
& & \(5 \times 37\) & 2731 \\
& 440 & \(7 \times 47\) & 2586 \\
& & \(5 \times 37\) & 2657 \\
\hline STAGSC-1 & 410 & \(3 \times 47\) & 2530 \\
\hline CSM Testbed & ES5/E410 & \(3 \times 26\) & 3570 \\
& & \(5 \times 37\) & 2734 \\
& & \(7 \times 51\) & 3343 \\
& ES1/EX97 & \(5 \times 37\) & 2753 \\
& & \(7 \times 51\) & 2577 \\
& \multirow{3}{*}{} & 2475 \\
& ES1/EX47 & \(3 \times 26\) & 2466 \\
& & \(5 \times 37\) & 3945 \\
& & \(7 \times 51\) & 2696 \\
& & 2568 \\
\hline
\end{tabular}
(1) Mesh description is \(n \times m\) meaning \(n\) rows by \(m\) columns of nodes.
(2) Finite difference version of STAGS.


Figure 4.10-6 Normal deflection distribution at

Longitudinal inplane stress resultant, Ib/in.


Figure 4.10-7 Longitudinal inplane stress resultant \(N_{x}\) distribution at cylinder midlength for various load steps.

\subsection*{4.10.2 PROCEDURE USAGE}

Procedure PEAR_CYL may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call PEAR_CYL ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PEAR_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES.PROC & ES1 & Element Processor \\
\hline ES NAME & EX97 & Element name \\
\hline ES_PARS & 0. & Element research parameters \\
\hline NEL_ARC & & Number of elements along \(45^{\circ}\) arc segment \\
\hline NEL_DEPTH & & Number of elements along depth of shell \\
\hline NEL_FLAT & & Number of elements along largest flat segment \\
\hline LD_DIR & & Direction to total load \\
\hline LINEAR & & Perform linear analysis \\
\hline NSTEPS & 30 & Number of nonlinear load steps \\
\hline BEG_STEP & 1 & Starting load step number \\
\hline Max_CUTS & 3 & Maximum number of step cuts (halvings) \\
\hline BEG_LOAD & . 1 & Starting load factor \\
\hline Max load & 1.0 & Maximum load factor \\
\hline DBC & PEAR.DBC & Computational database name \\
\hline DBR & PEAR.DBR & Results database name \\
\hline STABILITY & <true> & Perform linear stability (buckling) analysis \\
\hline NONLINEAR & <true> & Perform nonlinear analysis \\
\hline POST & <false> & Perform postprocessing (selected data archival) \\
\hline
\end{tabular}

\subsection*{4.10.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.10.3.1 BEG_LOAD}

Starting load factor in nonlincar analysis (default=.1). This factor is multiplied times the reference load vector to obtain the starting load vector. For example, if specified forces are applied (which is the default option), then BEG_LOAD \(=.1\) means that the first load step to
be computed in the nonlinear analysis will be at one-tenth of the classical buckling load level. Note that this argument is irrelevant for re-start runs. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.10.3.2 BEG_STEP}

Number of starting load step in nonlinear analysis (default=1). This is the number of the first step to be computed during an analysis interval. When starting a nonlinear analysis, the first step is obviously 1 . When re-starting (i.e., continuing in a subsequent run) a nonlinear analysis, BEG_STEP should be set to the number of the next step to be computed - not to the number of the last step computed. The solution procedure (NL_STATIC_1) will automatically use any previous step(s) required to continue the analysis - providing the necessary steps are available in the database. Currently, the number of consecutive preceding steps required for a restart is three. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.10.3.3 DBC}

Name of computational database file (default=PEAR.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

\subsection*{4.10.3.4 DBR}

Name of results database file (default=PEAR.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups - indexed by load step number - for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

\subsection*{4.10.3.5 ES_NAME}

Element name (default: EX97). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX97, is a 9 -node quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.10-3).

\subsection*{4.10.3.6 ES_PARS}

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.10.3.7 ES_PROC}

Element processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shellelement, processor ES 1 , is described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.10-3).

\subsection*{4.10.3.8 LD_DIR}

Direction in which to total the load (default: 3). This argument specifies the direction in which the reaction forces will be summed in order to determine the total load applied.

\subsection*{4.10.3.9 LINEAR}

Linear analysis flag (default: <false>). This flag should be turned on to perform only a linear static analysis.

\subsection*{4.10.3.10 MAX_CUTS}

Maximum number of load step cuts in nonlinear analysis (default=3). For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.10.3.11 MAX_LOAD}

Maximum load factor in nonlinear analysis (default=1.0). This sets an upper limit for the load level, which can be a convenient way of terminating the arc-length controlled solution algorithm employed within procedure HL_STATIC_1. Since the load factor is actually an unknown in this solution procedure, there is no way of knowing a-priori how many load steps will be required to attain a particular load level. Thus, the analysis will be terminated when either MAX_LOAD is exceeded or NSTEPS is exceeded - whichever comes first. For more details, refer to the same argument name under solution procedure NL_STATIC_1.

\subsection*{4.10.3.12 MEL_ARC}

Number of elements along arc segment (default: 4). This argument specifies the number of elements along a \(45^{\circ}\) arc segment of the shell.

\subsection*{4.10.3.13 NEL_DEPTH}

Number of elements along depth of shell (default: 1). This argument specifies the number of elements along the length (or depth) of the shell.

\subsection*{4.10.3.14 NEL_FLAT}

Number of elements along flat segments (default: 4). This argument specifies the number of elements along the flat segments of the shell.

\subsection*{4.10.3.15 HONLINEAR}

Nonlinear analysis flag (default=<true>). This flag should be turned on to perform nonlinear analysis in the current run.

\section*{4．10．3．16 MSTEPS}

Maximum number of load steps to be computed in the current nonlinear analysis run （default＝30）．For more details，refer to the same argument name under solution procedure NL＿STATIC＿1．

\section*{4．10．3．17 POST}

Postprocessing flag（default＝＜false＞）．This flag should be turned on if you want selected response－history parameters to be added to the PEAR．DBR database．Note that it is not necessary to use this option in order to archive the basic load－displacement curve and solution parameters．It is only needed if you wish to archive special displacement and／or internal force component response histories post－facto．

\section*{4．10．3．18 STABILITY}

Stability（buckling）analysis flag（default＜true＞）．This flag should be turned on if you want the buckling eigenvalue analysis to be performed in the current run．Preprocessing is a pre－requisite for this option．If you are just performing a nonlinear analysis re－start run，then you should turn this flag off．

\section*{4．10．4 USAGE GUIDELINES AND EXAMPLES}

Procedure PEAR＿CYL may be used by preceding the procedure name by the＊call directive． Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called．A space or blank is required between the end of the procedure name and the left parenthesis．If the default values of the procedure arguments are to be used，then only the procedure name is required．
```

*call PEAR_CYL (ES_PROC = ES1 ; -- . Element Processor
ES_NAME = EX97 ; -- . Element name
MEL_ARC $=4$; -- Elements along 45 deg. arc
NEL_FLAT $=4$; -- . Elements along flat segment
NEL_DEPTH= 2 ; -- . Elements through depth ( $z$ )
LINEAR $=\langle t r u e\rangle ;-$.
PREP $=\langle t r u e\rangle ;--$.
STABILITY $=\langle$ false〉; -- .
NONLINEAR $=\langle$ false〉; -- .
POST $=\langle$ false〉; --.
DBC $\quad=$ PEAR.DBC; - .
DBR $\quad=$ PEAR.DBR ; --
NSTEPS $=30 ;--$
BEG_STEP $=1$; -- .
MAX_CUTS $=3$; -- .
BEG_LOAD $=.1 ;--$.
MAX_LDAD $=1$; --
LD_dir $=3$, ${ }^{--}$. Direction of total load calculation

```
(E1) To perform añ entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call PEAR_CYL
This will perform linear buckling eigenvalue analysis and 30 steps of nonlinear analysis with a \(7 \times 7\) grid of ES1/EX97 shell elements. The time required for this analysis is machine-dependent. Using the default values for the procedure arguments, the amount of CPU times required for a stability analysis and a nonlinear analysis on various computer systems are shown in Table 4.10-2.

Table 4.10-2 CPU TIMES Table
\begin{tabular}{|c|c|c|}
\hline \multirow{2}{*}{ Computer System } & \multicolumn{2}{|c|}{ Total CPU Time, sec. } \\
\cline { 2 - 3 } & Stability & Nonlinear \\
\hline VAX 11/785 & & \\
VMS 4.7 & & \\
\hline MicroVAX \\
ULTRIX 2.2 & & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & & \\
\hline CONVEX C220 & & \\
\hline VERSION 7.0 & & \\
\hline CRAY-2 & & \\
\hline
\end{tabular}
(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

\subsection*{4.10.5 LIMITATIONS}

None.

\subsection*{4.10.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.10.7 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
PEAR_CYL & (main procedure) \\
PEAR_MODEL & (define model) \\
ES & (define elements) \\
PEAR_CON & (define boundary conditions) \\
MATDAT & (define material properties) \\
DEF_ELTS4 & (define 4-node models) \\
DEF_ELTS9 & (define 9-node models) \\
PEAR_AD & (define applied displacements) \\
L_STATIC & (linear static analysis procedure) \\
TOTAL_LOAD & (sum reaction forces to get total load) \\
L_STABIL_2 & (linear stability analysis procedure) \\
TOTAL_LOAD & (sum reaction forces to get total load) \\
ML_STATIC_1 & (nonlinear static analysis procedure) \\
HISTORY & (archive historical data) \\
TOTAL_LOAD & (sum reaction forces to get total load)
\end{tabular}

\subsection*{4.10.8 PROCEDURE LISTING}

\subsection*{4.10.8.1 UNIX Script}

\author{
pear_cyl.com
}
```

cd $SCR/$OSER
cp $CSM_PRC/proclib.gal proclib.gal
chnod u+# proclib.gal
Tn PEAR.*
tine testbed <<\ondinput
    *sot echo off
    *get plib 28
    *open 28 proclib.gal /old
    #add '$CSH_APP/pear_cyl/pear_cyl.clp'
*def/i es_proj z 1
*def/i es_coro = 1
*def/i nl_geon = 2
*def/a solver_name =BAND
*def/a nl_solver mBAND
*call PEAR_CYL ( ES_PROC = ES1 ; -- . Elenent Processor
ES_NAME = EX97 ; -- . Element name

```
```

NEL_arc = 4 ; -- . Elements along 45 deg. arc
NEL_flat = 4 ; -- . Eloments along flat segment
NEL_depth= 3 ; -- . Elenents through depth (z)
NSTEPS =60 ; -- .
DBC = PEAE.DEC ; --
DBR = PEAR.DBR ; --
PREP = <true> ; --
LIMEAR = <false\rangle ; --
STABILITY= <false\rangle ; --
NONLINEAR= <true> ; --
HEHTON = <false> ; --
POST = <true> ; --
BEG_LOAD = . 2 ; -- .
MAX_LOAD = 120.0 )

```
[xqt EXIT
londinput

\subsection*{4.10.8.2 CLAMP Procedure}
pear_cyl.clp
```

*procedure PEAR_CYL ( ES_PROC = ES1 ; -- . Element Processor
ES_NAME = EX97 ; -- . Element name
NEL_arc = 4 ; --. Elements in 45 deg. arc
NEL_flat = 4 ; -- . Elements along flat segment
NEL_depth= 1 ; -- . Elements through depth
LD_dir = 3 ; -- . Direction of total load
NSTEPS = 30 ; --
BEG_STEP = 1 ; --
BEG_LOAD = . 01 ; --
MAX_LOAD = 1.0 ;--
MAX_CUTS = 3 ; --
DBC = PRAR.DBC; DBR = PEAR.DBR; --
PREP = <true>; --
LINEAR = <true>; --
STABILITY = \langlefalse\rangle; --
NONLINEAR = <false>; --
NEUTON = <falso\rangle; --
POST = <false> --
)

```

    CSM Testbed Procedure for Analysis of Pear-Shaped Cylinder
        written by S. McCleary (PRC Kentron) -- 2/88
*def/i MOH_ldi = 3
*open/ner 1 [DBC]
.
*if [PREP] /then
    *call PEAR_MODEL ( ES_proc = [ES_PROC]; --
                        ES_nane \(=[E S\) _NAME]; --
```

    nel_a = [NEL_arc] ; --
    nel_1 = [NEL_flet]; --
    nel_z = [HEL_depth] )
    *endif
•
-
*if < [LINEMR] >/then
•
*call L_STATIC
*call TOTAL_LOAD ( EqUIL_CK= 0 ; --
NSTEPS = 0 ; --
LOAD_SET = 1 ; --
CONS_SET = 1 ; --
MAME1 = 'STAT' ; --
NAME2 = 'REAC' ; --
FAC = 1.0 ; --
LD_DIR = [Ld_dir] --
)
*elseif < [STABILITY] > /then
.
*call L_STABIL_2 (function='all';n_modes=2;print=\langletrue\rangle;stress=<true\rangle ; --
cons_set=1; bcon_set=1 )
*call TOTAL_LOAD ( EQUIL_CK= 0 ; --
NSTEPS = 0 ; --
LOAD_SET = 1 ; --
CONS_SET = 1 ; --
HAME1 = 'STAT' ; --
NAME2 = 'REAC' ; --
FLC = 1.0 ; --
LD_DIR = [Ld_dir]
)
•
*endif
*open/ner 3, [DBr]
•
•
*if < [NOMLINEAR] > /then
*def/i ne_overwrite == <true>
*call ML_STATIC_1 ( NL_GEOM = <nl_geon> ; --
COROTATION=<es_coro> ; --
NEUTON = [NENTON] ; --
BEG_STEP = [BEG_STEP] ; --
MAX_STEPS = [NSTEPS] ; --
BEG_LOAD = [BEG_LOAD] ; --
MAX_LOAD = [MAX_LOAD] ; --
MAX_CUTS = [MAX_COTS] ; --
NOMINAL_DB = [DBr] ; --
NOMINAL_DS = [ES_PROC].[ES_NAME].1.1 ; --
N_SELECT = 2 ; --

```
```

    SEL_NODES = 1,\langle<nntotal>-<nnod_z\rangle+1\rangle ; --
    SEL_DOFS = 1,1
    )
*toc 1
*endif
*if < [POST] /gt 0 >/then
*opon 1, [DBC]
*open 3, [DBr]
*if < [POST] /eq 1 >/then
*call HISTORY ( input_ds = TOT.DISP; output_ldi = 1 ; --
output_ds= [ES_PROC].[ES_NAME].1.1 ; --
output_rn= RADILL_DISP ; LOCATION = NODES ; --
num_stops = [NSTEPS] ; --
stops = [BEG_STEP]:<[BEG_STEP]+[NSTEPS]-1>; --
num_nodes= 1 ; --
nodes = <<nntotal>-<nnod_z>+1> ; --
component = 1
)
*call TOTAL_LOAD ( EQOIL_CK= 0 ; --
NSTEPS = [NSTEPS] ; --
LOAD_SET = 0 ; --
CONS_SET = 0 ; --
NAME1 = 'REAC' ; --
NAME2 = 'FORC' ; --
FAC = 1.0 ; --
LD_DIR = [Ld_dir] --
)
*print 3 1 TOTAL*/out=0
*print 3 1 DISP_\mp@subsup{D}{_}{\prime<<nntotal>-<nnod_z>+1>* /out=0}
*endif
*ondif
*ond
*procedure PEAR_MODEL ( ES_proc = ES1 ; --
ES_name = EX97 ; --
nel_a = 4 ; --
nel_f = 4 ; --
nel_z = 2 )
. Initialize element macros
*call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [ES_PROC]; --
es_name = [ES_NAME] )
Set dimensions and number-of-nodes macros:

```
```

*def/g dz == 0.40 . Depth (in z direction) of cylinder
*def/g r x= 1.0
*de1/g sq2 = (2.0^0.6)
*def/g ra2 = < <r> * \langlesq2\rangle>
*def/g rd2 = < <r>/<|qq2\rangle\rangle
\#de1/g rr2 = < <r\rangle + \langlerd2\rangle \rangle
*def/g rn = < - <r\rangle\rangle
*def/g rr2n = < -<rr2>>
*def/g rd2n = < -<rd2\rangle>
*def/g re2m = < -<rs2\rangle>
*def/i nel_b = <[nel_f]*if < <es_nen>/eq 4>/then
*det/i mnod_z = = < [nel_z] + 1> . Through z
|det/i nnod_a =* < [nel_e] + 1 > . Along arc
*def/i nnod_i z= < [nel_f] + 1 > . Along llat segment
*def/i nnod_b m= <<nel_b\rangle + 1\rangle> . Along botton segment
*def/i nnod_c == <4*[nel_a]+[nel_1]+\langlenel_b\rangle + 1 > . Circunferentially
*olseif < <es_nen>/eq }9\mathrm{ >/then
*def/i nnod_z =z<2*[nel_z] + 1\rangle> . Through z
*def/i nnod_a =m<2*[nel_a] +1>> . Along arc
*def/i nnod_f == < 2*[nel_f] + 1 > . Llong flat segment
*def/i nnod_b == < 2*<nel_b\rangle + 1> . Llong botton segment
*def/i nnod_c == < 2*<4*[nel_a]+[nel_f]+\langlenel_b\rangle\rangle + 1 \rangle . Circumferentially
*endil
*det/i nnod_3a = < 3*< <nnod_a\rangle - 1 > + 1 > . Around 135 deg. arc
*del/i bsegi = 1 . Start segment 1
*def/i bseg2 = < <bseg1\rangle + \langle<nnod_a\rangle -1\rangle*\langlennod_z\rangle\rangle\rangle . Start segnent 2
*def/i bseg3 = < <bseg2\rangle + \langle<nnod_1\rangle -1\rangle*<nnod_z\rangle\rangle . Start megment 3
*def/1 bseg4 = < <bseg3\rangle + \langle\langlennod_3a\rangle-1\rangle*\langlennod_z\rangle\rangle\rangle . Start segment 4
*def/i nntotal == < <nnod_c>*<nnod_m>> . Total number of nodes
[xqt TAB
START <nntotal>

```

```

        4 1,0. 2,0. 3,0. 0.0 <ri>> 0.0
        6 1,0. 2,0. 3,0. <rd2m\rangle <rr2m\rangle 0.0
        6 1,0. 2,0. 3,0. 0.0 <rr2m> 0.0
        7 1,0. 2,0. 3,135.
        8 1,0. 2,0. 3,270.
    -------------------------
    Define joint locations:
    JOINT LOCATIONS
    | NREP $=4$ |  | 90 to 135 degree arc |  |  |  |  | <nnod_a> | <nnod_z> | <nnod_z> |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PORMAT = 2 |  |  |  |  |  |  |  |  |  |
| <bseg1> | 〈r> | 90.0 | 0.0 | <r> | 135.0 | 0.0 |  |  |  |
| 1 | 〈r> | 90.0 | 0.4 | <r> | 136.0 | 0.4 |  |  |  |

```

```

    Assign Joint Reference Frames:
    jOINT REFERENCE FRAHE ASSIGNMENTS
        NREP = -4: <bseg1>, <<bseg2> - 1>
        NREP = 7: \langlebseg2>, <<bseg3> - 1>
        NREF = -5: <bseg3>, <<bseg4> - 1>
        NREP = 8: <bseg4>, <untotal>
    -----------------------
    Constraint Definitions:
    *call PEAR_CON ( nnod_z = <nnod_2> ; nntotal = <nntotal> )
. ---------------------

- Matorial Proporties:
.
*call matdat
. ---------------------
- Element Definitions:
*if < <es_nen> /og 4 >/then
*call DEF_ELTS4 ( ES_name = [ES_name] ; --
nel_a = [nel_a] ; --
nel_1 = [nel_f] ; --
nel_z = [nel_x] ; --
nel_b = <nel_b> )
*else
*call DEF_ELTSO ( ES_name = [ES_name] ; --
nel_a = [nel_a] ; --
nel_f = [nel_1] ; --
nel_z = [nel_z] ; --
nel_b = <nel_b> )
*endif

```
```

- Applied Loading:
. ---------------
*call PEAR_AD ( nnod_z = <nnod_z> ; nntotal = <nntotal>)
.
*ond
•
*procedure PEAR_CON ( nnod_z ; nntotal )
CONSTRAINT DEFINITION 1 . Buckling; simply supported
syam plame=1 . Plane 2,3 plane of symetry
symin plane=3 . Plane 1,2 plane of symetry
nonzoro 3 : [nnod_z],[nntotal],[nnod_z] . Apply displacenent at z=dz
zero 1,2,6: [nnod_z],[nntotal],[nnod_z] . Edge z=dz simply supported
*if <ifeqs(<es_nane>;E410)> /then
*emark E410 drilling freedoms ON
*else
zoro 4 : 1, [nntotal], 1 . Constrain in-plane rotations
*endif
*ond
*procedure DEP_ELTS4 ( ES_mame ; --
nel_a ; --
nel_1 ; --
nol_z ; --
nel_b )
*def/i nel_circum = <4*[nel_a] + [nel_1] + [nel_b]>
*de1/i jinc = <[nel_z]+1>
*def/i j1 = 1
*def/i j2 =2
*def/i j3 = <<j2\rangle + <jinc>>
*def/i j4 = <<jl> + <jinc>>
- 

[xqt ELD
<es_expe_cmd>
<j1> <j2><j3> <j4> 1 [nel_z] <nel_circum>
stop
*ond
.
*procedure DEF_RLTSO ( ES_name ; --
nel_a ; --
nol_1 ; --
nel_z ; --
nel_b ;
*def/i nel_circui = <4*[nel_a] + [nel_f] + [nel_b]>
*def/i jinc = <2*[nel_z]+1>
*def/i j1 = 1
*def/i j2 = <<j1>+2>

```
```

*dof/i j3 = <<j2> + 2*<jinc>>
*dof/i j4 = <<j1> + 2*<jinc>>
*def/i jE = <<j1\rangle + 1\rangle
*de1/i j6 = <<j2> + <jinc>>
*def/i j7 = <<jb\rangle + 2*<jinc>>
*def/i j8 = <<j1> + <jinc>>
*def/i j0 = <<j5> + <jinc>>
-
[xqt ELD
<08_expe_cmd>
<j1\rangle <j2> <j3> <j4> <j5> <j6> <j7> <j8> <j9> 1 [nel_z] <nel_circum>
stop
*end
-
*procedure MATDAT
[xqt 10S
*def g = 3.84615e+6
*def/g t == 0.01
. E11 NU12 E22 G12 G13 G23 alPHA1 AlPHA2 UTDEN
TABLE(NI=16,NJ=1): OMB DATA 1 1
I=1,2,3,4,5,6,7,8,0
J=1: 10.0E+6 .30 10.0E+6 <g> <g> <g> 0.0 0.0 .1
TABLE (NI=3,NJ=1,ityPe=0): LAM OMB 1 1
J=1 : 1 \langlet> 0.00
[xqt lau
-
*and
.
\#procedure PEIR_AD (nnod_z ; nntotal )
[xqt avS
sysvoc : appl noti
i=3 : j=[nnod_z],[nntotal],[nnod_z] : -2.E-5
*ond

```

\subsection*{4.10.9 REFERENCES}
4.10-1 Hartung, R. F.; and Ball, R. E.: A Comparison of Several Computer Solutions to Three Structural Shell Analysis Problems. AFFDL TR-73-15, April 1973.
4.10-2 Almroth, B. O. and Brogan, F. A. (1981). "Computational Efficiency of Shell Elements," Nonlinear Finite Element Analysis of Plates and Shells, Hughes, T. J. R., Pifko, A., and Jay, A. (Editors), AMD Vol. 48, ASME, pp. 147-165.
4.10-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.11 Procedure PINCHED_CYL}

\subsection*{4.11.1 GENERAL DESCRIPTION}

The pinched cylinder - a circular cylindrical shell subjected to two equal and opposite radial forces at 0 and 180 degrees along its mid-span circumference - is a classical problem that has been used extensively to check the ability of shell elements to represent inextensional bending deformation. Two versions of the problem are considered here: (i) with open ends, and (ii) with a rigid membrane diaphragm on each end to prevent cross-sectional distortion. The open-ended version leads to pure inextensional deformation (i.e., zero membrane strains) in the limit as the shell thickness to shell radius ratio \(h / R\) approaches zero. An exact solution for this limiting case may be found in reference 4.11-1. The pinched cylinder with closed ends does not exhibit pure inextensional deformation, but rather a complex combination of bending and membrane effects with a bending boundary layer in the immediate vicinity of the concentrated loads. A series solution for this latter case may be found in reference 4.11-2.

This section describes a procedure that solves another classical problem which is one of the MacNeal-Harder test cases. Two versions of this circular cylindrical shell subjected to equal and opposite radial forces at its mid-span circumference are provided: (i) with open ends and (ii) with a rigid membrane diaphragm on each end. The L/2 by 90 -degree model used in each case is shown in figure 4.11-1.


Figure 4.11-1 Pinched Cylinder Problem.

\subsection*{4.11.1.1 Model Description}

\subsection*{4.11.1.2 Analysis Description}

\subsection*{4.11.1.3 Available Solutions}

\subsection*{4.11.2 PROCEDURE USAGE}

Procedure PINCHED_CYL may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call PINCHED_CYL ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PINCHED_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline ES_PROC & ES1 & Element processor \\
\hline ES. MAME & EX97 & Element name \\
\hline ES_PARS & 0. & Element research parameters \\
\hline NNODES_A & 5 & Number of axial nodes \\
\hline WNODES_C & 5 & Number of circumferential nodes \\
\hline AUTO_DOF_SUP & <true> & Automatic degrees of freedom suppression \\
\hline DRILLING_DOF & <false> & Drilling (normal rotational) freedoms \\
\hline DBC & PC.DBC & Computational database name \\
\hline DBR & PC.DBR & Results database name \\
\hline PREP & <true> & Perform preprocessing (model generation) \\
\hline LINEAR & <true> & Perform linear static analysis \\
\hline REACTION & <false> & Calculate internal forces or reactions \\
\hline POST & <true> & Perform postprocessing (selected data archival) \\
\hline
\end{tabular}

\subsection*{4.11.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.11.3.1 AUTO_DOF_SUP}

Automatic degree of freedom suppression flag (default: <true>). This option provides a convenient way of suppressing any freedoms that do not have any (or adequate) stiffness associated with them - for example, at nodes used to prescribe geometry only; or drilling freedoms in fine meshes composed of elements without normal rotational stiffnesses (see argument DRILLING_DOF).

\subsection*{4.11.3.2 DBC}

Name of computational database file (default=PC.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

\subsection*{4.11.3.3 DBR}

Name of results database file (default=PC.DBR). This file will contain one dataset called RESPONSE.HISTORY generated during nonlinear analysis. The dataset will contain record groups - indexed by load step number - for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

\subsection*{4.11.3.4 DRILLING_DOF}

Drilling degree of freedom flag (default: 〈false>). Drilling freedoms are defined as rotations normal to the surface of the shell. Leaving this flag off forces all drilling freedoms in the model to be suppressed. Turning it on forces all drilling freedoms to be active unless they are automatically suppressed using use of the AOTO_DOF_SUP argument. Note that while many shell elements do not have any rotational stiffness associated with their own surface-normal directions (at nodes), when shell elements are assembled as facets approximating an arbitrary shell surface, there is usually some misalignment between the element normal and the actual shell normal. This is especially true of "flat" (e.g., 4-node) elements. Hence, some rotational stiffness about the shell normal is usually present in the model. (A clear exception to this is a flat plate, where element and shell normals are identical.) For a cylindrical shell, the misalignment diminishes only as the number of elements is increased. Most shell elements in the Testbed have their own misalignment tolerance parameter, which determines when the AUTO_DOF_SUP argument will automatically suppress the drilling freedom. Note that for elements which have drilling stiffness, the DRILLING_DOF argument should be set to <true> regardless of how AUTO_DOF_SUP is set.

\subsection*{4.11.3.5 ESNAME}

Element name (default: EX97). This argument is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX97, is a 9 -noded quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 2.1-1).

\subsection*{4.11.3.6 ES_PARS}

Element research parameters (default: 0., ...). This argument allows is an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.11.3.7 ES_PROC}

Element processor (default: ES1) This argument is the name of the structural element (ES) processor that contains the shell element type you wish to employ in the model. The default shell-element, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{4.11.3.8 LINEAR}

Linear stress analysis flag (default: <true>).

\subsection*{4.11.3.9 \({ }^{\text {NNODES_A }}\)}

Number of axial nodes (default: 7). This argument is the number of nodes you wish to have along the axial direction of the cylindrical shell model, i.e., along one-tenth of the full cylinder's length. Note that this number should be consistent with the number of nodes per element. For example, NNODES_A can be any number greater than 1 for 4node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{4.11.3.10 NNODES_C}

Number of circumferential nodes (default: 7). This argument is the number of nodes you wish to have along the circumferential direction of the cylindrical shell model, i.e., along 15 degrees of circular arclength. Note that this number should be consistent with the number of nodes per element. For example, nNODES_C can be any number greater than 1 for 4 -node quadrilateral elements, whereas it must be an odd number greater than 1 for 9 -node quadrilateral elements.

\subsection*{4.11.3.11 POST}

Postprocessing flag (default=<false>). This flag should be turned on if you want selected response-history parameters to be added to the CC.DBR database. Note that it is not necessary to use this option in order to archive the basic load-displacement curve and solution parameters. It is only needed if you wish to archive special displacement and/or internal force component response histories post-facto.

\section*{4．11．3．12 PREP}

Pre－processing flag（default＝＜true＞）．This flag must be turned on the first time procedure PINCHED＿CIL is run，as it causes the model to be generated．If subsequent runs are used to perform other stages of the analysis（e．g．，nonlinear restarts），then PREP must be set to ＜false＞for those subsequent runs．

\section*{4．11．4 USAGE GUIDELINES AND EXAMPLES}

Procedure PINCHED＿CYL may be used by preceding the procedure name by the＊call directive．Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called．A space or blank is required between the end of the procedure name and the left parenthesis．
```

*call PINCHED_CYL ( ES_PROC = ES1 ; ES_HAME = EX97 ; --
NNODES_A = 7 ; NNODES_C = 7 ; --
SPEC_DIS = 〈false> ; --
DRILLING_DOF = 〈false> ; --
AOTO_DOF_SUP = <true> ; --
PREP = <true> ; --
STABILITY = <true> ; --
IMPERFECTION = 〈true> ; --
LINEAR = <true> ; --
POST = <true> ; --
BEG_STEP = 1 ; --
NSTEPS = 10 ; --
BEG_LOAD = .1 ; --
MAX_LOAD = 3.0 ; --
DBc = PC.DBc ; DBr = PC.DBr )

```
（E1）To perform an entire analysis using the default options，simply invoke the procedure without any arguments，i．e．，
＊call PINCHED＿CYL
This will perform linear buckling eigenvalue analysis and 10 steps of nonlinear anal－ ysis with a \(7 \times 7\) grid of ES1／EX97 shell elements．The time required for this analysis is machine－dependent．Using the default values for the procedure arguments，the amount of CPU time required for this analysis on various computer systems is shown in Table 4．11－1．

Table 4．11－1 CPU TIMES Table
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 \\
VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CONVEX C220 \\
VERSION 7.0 & \\
\hline CRAY-2 & \\
\hline UNICOS 4.0 & \\
\hline
\end{tabular}
(E2) Not suppressing the drilling rotational freedoms can cause strange behavior for some elements during nonlinear analysis. On the other hand, suppressing these freedoms explicitly using the DRILLING_DOF argument may cause some over-stiffening for coarse meshes with some elements. It is probably best to suppress the drilling freedoms explicitly unless the element actually has intrinsic drilling stiffness.

\subsection*{4.11.5 LIMITATIONS}

\subsection*{4.11.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.11.7 PROCEDURE FLOWCHART}
```

PINCHED_CYL (main procedure)
GEN_SHELL (generate model)
PC_BC (generate boundary conditions/loads)
PDC_BC
L_STATIC_1 (perform linear static analysis)
POST

```

\subsection*{4.11.8 PROCEDURE LISTING}

\subsection*{4.11.9 REFERENCES}
4.11-1 Timoshenko, S. and Woinowsky-Krieger, S., Theory of Plates and Shells, McGrawHill. New York, 1969.
4.11-2 Lindberg, G.M., Olson, M.D. and Cowper, G.R. "New Developments in the Finite Element Analysis of Shells", Q. Bull. Div. Mech. Eng. and the National Aeronautical Establishment, National Research Council of Canada, vol. 4, 1969, pp. nox.
4.11-3 Ashwell, D.G.: "Strain Elements, with Applications to Arches, Rings, and Cylindrical Shells," Finite Elements for Thin Shells and Curved Members, D.G. Ashwell and R.H. Gallagher (editors), John Wiley and Sons, New York, 1974, pp. 91-111.
4.11-4 Forsberg, Kevin: "An Evaluation of Finite Difference and Finite Element Techniques for Analysis of General Shells," In Proceedings of the Symposium on High Speed Computing of Elastic Structures, B. Fraeijs de Veubeke (editor), I.U.T.A.M., Liège, 1970, pp. 837-859.
4.11-5 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.12 Procedure PWHOLE}

\subsection*{4.12.1 GENERAL DESCRIPTION}

\subsection*{4.12.1.1 Problem Description}

This application problem involves a linear static stress analysis of a thin isotropic membrane with a central circular hole subjected to uniform compression (see Figure 4.12-1). This problem is important in that plate and shell elements are frequently used to model regions with a severe stress gradient.


Figure 4.12-1 Plate with Circular Hole

\subsection*{4.12.1.2 Model Description}

Procedure PWHOLE models an entire rectangular membrane using 2-D quadrilateral elements. The mesh is generated using processor CSM1. This processor generates a file named PANEL. PRC which is added to the procedure library. This file contains various procedures associated with model generation (PANEL_BC), and applied displacements (PANEL_AD).

\subsection*{4.12.1.3 Analysis Description}

Procedure PHHOLE performs a single linear static stress analysis. The solution procedure L_STATIC described in Chapter 3 is used to perform the static stress.

\subsection*{4.12.1.4 Available Solutions}

\subsection*{4.12.2 PROCEDURE USAGE}

Procedure PHHOLE may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call PWHOLE ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PWHOLE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{lccll} 
Argument & & Default Value & & Meaning \\
& ES_PROC & ES1 & & Element processor \\
ES_NAME & & EX47 & & Element name \\
ES_PAR & & 0.0 & & Element research parameters \\
NRINGS & & 4 & & Number of rings of elements \\
NSPOKES & & 16 & & Number of radial spokes of nodes \\
NELX & & 6 & & Number of elements along \(x\)-direction \\
NELE & 2 & & Number of elements across edge \\
NELBS & & 2 & & Number of elements between interior stiffeners \\
PRINT & & <false> & & Print flag \\
DIRECTION & 1 & & Direction of stress reference frame \\
LOCATION & & 'NODES' & Location for stress recovery
\end{tabular}

\subsection*{4.12.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.12.3.1 DIRECTION}

Direction for the element.stress (stress resultant) output (default: 1). The element stress coordinate system will be used if DIRECTION=0. The material axes ( \(x_{m}, y_{m}, z_{m}\) ) will be used if DIRECTION=1; the material axes ( \(y_{m}, z_{m}, x_{m}\) ) will be used for DIRECTION=2; and the material axes \(\left(z_{m}, x_{m}, y_{m}\right)\) will be used for DIRECTION=3. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 4.12-3).

\subsection*{4.12.3.2 ES_NAME}

Element name (default: EX47). This argument specifies the name of the specific shellelement type to select within the element processor defined by argument ES_PROC. The default shell-element type, EX47, is a 4 -node quadrilateral element implemented in processor ES1, and described in the Computational Structural Mechanics Testbed User's Manual (see ref. 4.12-2).

\subsection*{4.12.3.3 ES_PARS}

Element research parameters (default: 0.0, ...). This array allows an optional list of element-dependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

\subsection*{4.12.3.4 ES_PROC}

Element processor (default: ES1) This is the name of the structural element (ES) processor that contains the shell-element type you wish to employ in the model. The default shellelement, processor ES1, is described in the Computational Structural Mechanics Testbed User's Manual (see refs. 4.12-2).

\subsection*{4.12.3.5 LOCATION}

Location of the evaluation points for the element stresses or stress resultants (default: NODES). The element stresses or stress resultants are optionally computed by calling procedure STRESS (see Section 6.4). This argument may have four values. For LOCATION=IMTEG_PTS, the element stresses are computed at the element integration points. For LOCATIOM=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries.

\subsection*{4.12.3.6 NELBS}

Number of elements between interior stiffness (default: 2). Refer to processor CSM1 in reference 4.12-3 for a discussion of this argument.

\subsection*{4.12.3.7 NELE}

Number of elements across edge (default: 2). Refer to processor CSM1 in reference 4.12-3 for a discussion of this argument.

\subsection*{4.12.3.8 NELX}

Number of elements along \(x\)-direction (default: 6). Refer to processor CSM1 in reference 4.12-3 for a discussion of this argument.

\subsection*{4.12.3.9 RRINGS}

Number of rings of elements (default: 4). This argument specifies the number of rings of elements, either 4 -node or 9 -node quadrilateral elements, around the hole.

\subsection*{4.12.3.10 MSPORES}

Number of radial spokes of nodes (default: 16). This argument specifies the number of radial spokes of nodes which must be a multiple of 8 .

\subsection*{4.12.3.11 PRINT}

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, stresses) will be printed.

\subsection*{4.12.4 USAGE GUIDELINES AND EXAMPLES}

Procedure PWHOLE may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call PWHOLE ( ES_PROC = ES1 ; -- . ES_NAME = EX47 ; -- .
ES_PAR = 0.0 ; -- . Element research parameters
HRIMGS = 4 ; -- . Number of rings of elements
MSPOKES = 16 ; -- . Number of radial spokes of nodes
NELX = 6 ; -- . Number of elements along x-direction
NELE = 2 ; -- . Number of elements across edge
NELBS = 2 ; -- . Number of elements betreen interior stiffeners
DIRECTION = 1 ; -- . Direction of stress reference frame
LOCATION = 'NODES' -- . Location for stress recovery

```
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,
```

*call PWHOLE

```

Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.12-1.

Table 4.12-1 CPU TIMES Table
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
\hline VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CONVEX C220 & \\
\hline VRARSION 7.0 & \\
\hline UNICOS 4.0 & \\
\hline
\end{tabular}

\subsection*{4.12.5 LIMITATIONS}

None

\subsection*{4.12.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.12.7 PROCEDURE FLOWCHART}
\begin{tabular}{cl} 
PWHOLE & (main procedure) \\
ES & (define elements) \\
PANEL_START & (define start card) \\
PANEL_JLOC & (define joint locations) \\
PANEL_BC & (define boundary conditions) \\
MATDAT & (define material properties) \\
PANEL_CONN & (define element connectivity) \\
ES & (define freedoms) \\
PANEL_AD & (define applied displacements) \\
L_STATIC & (linear static solution procedure)
\end{tabular}

\subsection*{4.12.8 PROCEDURE LISTING}

\subsection*{4.12.9 REFERENCES}
4.12-1 Timoshenko, S. P. and Goodier, J. N.: Theory of Elasticity (Third Edition). McGraw-Hill Book Company. New York, 1970, pp. 90-97.
4.12-2 Peterson, R. E.: Stress Concentration Design Factors. John Wiley and SonsInternational, New York, 1953, pp. 77-88.
4.12-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.13 Procedure RECT-PLATE}

\subsection*{4.13.1 GENERAL DESCRIPTION}

This application problem involves linear static stress analysis, linear buckling analysis and linear vibration analysis of three thin isotropic rectangular plates simply supported along their edges (see Figure 4.13-1). Various loading cases are considered including uniaxial and biaxial compression, uniform inplane shear, and inplane bending (see Figure 4.13-2).

(a) Quarter Model of Plate 1.

(b) Haif Model of Plate 2.

(c) Full Model of Plate 3.

Figure 4.13-1 Rectangular Plate Problems.


Figure 4.13-2 Loading Conditions.

\subsection*{4.13.1.1 Model Description}

Procedure RECT_PLATE uses a quarter model, a half model, and a full model of a plate depending on the loading case. The mesh topology is rectangular and restricted to quadrilateral shell elements with 4-nodes. For the quarter model shown in Figure 4.13-1a, two edges are simply supported and two edges have symmetry conditions imposed. For the half model shown in Figure 4.13-1b, three edges are simply supported and symmetry conditions are imposed on the remaining edge. For the full model shown in Figure 4.13-1c, all four edges are simply supported.

\subsection*{4.13.1.2 Analysis Description}

Procedure RECT_PLATE performs six different analyses through successive procedure calls using the various solution procedures described in Chapter 3. The analyses performed are:
- Linear free vibration analysis about an unstressed state;
- Linear buckling analysis using a linearly-computed prestress state for uniform uniaxial compression;
- Linear buckling analysis using a prescribed prestress state for uniform biaxial compression;
- Linear free vibration analysis about a prescribed prestressed state for uniform biaxial tension;
- Linear buckling analysis using a linearly-computed prestress state for uniform inplane bending;
- Linear buckling analysis using a linearly-computed prestress state for uniform inplane shear.

\subsection*{4.13.1.3 Available Solution}

Analytical solutions for the vibration analyses are available in reference 4.13-1 and for the buckling analyses in reference 4.13-2.

\section*{Case 1: Free vibration}

For this analysis, the quarter model of plate 1 is used. From pages 492-494 of reference 4.13-1, the frequencies for vibration are given as
\[
\begin{equation*}
\omega_{m n}=\frac{\pi^{2}}{a^{2}} \sqrt{\frac{D}{\rho h}}\left(m^{2}+n^{2} \frac{a^{2}}{b^{2}}\right) \tag{4.13-1}
\end{equation*}
\]
where
\[
\begin{aligned}
\omega_{m n} & =\text { circular frequency (radians/second) } \\
\rho & =\text { mass density } \\
D & =\frac{E h^{3}}{12\left(1-\nu^{2}\right)} \\
h & =\text { plate thickness } \\
E & =\text { Young's modulus } \\
\nu & =\text { Poisson's ratio } \\
m, n & =\text { number of half-waves in the } x-, y-\text { directions, respectively }
\end{aligned}
\]
and
\[
f_{m n}=\frac{\omega_{m n}}{2 \pi} \quad \text { (hertz) }
\]

Using this formula, frequencies for this problem may be computed as follows:
\begin{tabular}{|c|c|l|c|}
\hline\(m\) & \(n\) & \(\omega_{m n}^{2}\) & \(f_{m n}\) \\
\hline 1 & 1 & \(4.9867 \times 10^{5}\) & 112.4 \\
1 & 3 & \(75.0712 \times 10^{5}\) & 436.1 \\
3 & 1 & \(186.7724 \times 10^{5}\) & 687.8 \\
\hline
\end{tabular}

\section*{Case 2: Uniform Uniaxial Compression}

For this analysis, the quarter model of plate 1 is used and the loading corresponds to \(N_{y}=-1.0 \mathrm{lb} / \mathrm{in}\). From pages \(351-356\) of reference \(4.13-2\), the buckling load is given as
\[
\begin{equation*}
\left(N_{y}\right)_{c r}=\frac{\pi^{2} D}{b^{2}}\left(n+\frac{1}{n} \frac{b^{2}}{a^{2}}\right)^{2} \tag{4.13-2}
\end{equation*}
\]

This expression implies that a plate buckles in such a way that there are \(n\) halfwaves in the direction of compression and only one halfwave in the perpendicular direction. The first term in equation (4.13-2) represents the Euler load for a strip of unit width and of length \(b\). The second term represents the change in buckling load for a continuous plate from an isolated strip. For this plate,
\begin{tabular}{|c|c|}
\hline\(n\) & \(\left(N_{y}\right)_{c r}, \mathrm{lb} /\) in. \\
\hline 1 & 523.04 \\
3 & 874.89 \\
5 & 1944.23 \\
\hline
\end{tabular}

\section*{Case 3: Uniform Biaxial Compression}

For this analysis, the quarter model of plate 1 is used and the loading corresponds to uniform biaxial compression
\[
N_{x}^{o}=N_{y}^{o}=-1.0 \mathrm{lb} / \mathrm{in}
\]

From pages \(356-360\) of reference \(4.13-2\), the buckling load may be derived from
\[
\begin{equation*}
N_{z} \frac{m^{2} \pi^{2}}{a^{2}}+N_{y} \frac{n^{2} \pi^{2}}{b^{2}}=D\left(\frac{m^{2} \pi^{2}}{a^{2}}+\frac{n^{2} \pi^{2}}{b^{2}}\right)^{2} \tag{4.13-3}
\end{equation*}
\]

If \(N_{x}\) and \(N_{y}\) are proportional, then
\[
N_{y}=R N_{x}
\]
where \(R\) is constant. Substituting this relation into equation (4.13-3) and solving for critical values of \(N_{x}\) gives
\[
\begin{equation*}
\left(N_{x}\right)_{c r}=\frac{\pi^{2} D}{a^{2}} \frac{\left(m^{2}+n^{2} \frac{a^{2}}{b^{2}}\right)^{2}}{\left(m^{2}+R n^{2} \frac{a^{2}}{b^{2}}\right)} \tag{4.13-4}
\end{equation*}
\]

The value of \(R\) is 1 for the loading case being considered. Thus
\[
\begin{equation*}
\left(N_{x}\right)_{c r}=\frac{\pi^{2} D}{a^{2}}\left(m^{2}+n^{2} \frac{a^{2}}{b^{2}}\right) \tag{4.13-5}
\end{equation*}
\]

The critical values are therefore
\begin{tabular}{|c|c|c|}
\hline\(m\) & \(n\) & \(\left(N_{x}\right)_{c r}, l b /\) in. \\
\hline 1 & 1 & 188.29 \\
1 & 3 & 730.58 \\
3 & 1 & 1152.36 \\
1 & 5 & 1815.15 \\
5 & 1 & 3080.48 \\
\hline
\end{tabular}

\section*{Case 4: Vibration with Prestress State}

For this analysis, the quarter model of plate 1 is used and the prestress state corresponds to uniform biaxial tension.
\[
N_{x}^{o}=N_{y}^{o}=S=1000 \mathrm{lb} / \mathrm{in}
\]

From pages 481-483 and 492-494 of reference 4.13-1, the vibration frequencies for a prestressed rectangular plate may be derived as
\[
\begin{equation*}
\omega_{m n}^{2}=\frac{\pi^{4} D}{a^{4} \rho h}\left(m^{2}+n^{2} \frac{a^{2}}{b^{2}}\right)^{2}+\frac{\pi^{2} S}{a^{2} \rho h}\left(m^{2}+n^{2} \frac{a^{2}}{b^{2}}\right) \tag{4.13-6}
\end{equation*}
\]

The first term of equation 4.13-6 represents the free vibration frequency. The second term represents the effect of uniform prestress on the vibration frequencies. Tensile prestress forces increases the vibration frequencies while compressive prestress forces decrease the vibration frequencies. For the plate considered herein, the vibration frequencies for a tensile prestress force S of \(1000 \mathrm{lb} / \mathrm{in}\). are as follows:
\begin{tabular}{|c|c|c|c|}
\hline\(m\) & \(n\) & \(\omega_{m n}^{2}\) & \(f_{m n}\) \\
\hline 1 & 1 & \(3.1470 \times 10^{6}\) & 292.34 \\
1 & 3 & \(17.7827 \times 10^{6}\) & 671.15 \\
3 & 1 & \(34.8851 \times 10^{6}\) & 940.03 \\
\hline
\end{tabular}

\section*{Case 5: Inplane Bending}

For this analysis, the half model of plate 2 is used and the loading across the edge \(A B\) varies linearly from \(N_{x}^{o}=1.0 \mathrm{lb} / \mathrm{in}\). at point A to \(N_{x}^{o}=-1.0 \mathrm{lb} / \mathrm{in}\). at point B. From pages 373-379 of reference 4.13-2, the buckling load is given as
\[
\begin{equation*}
\left(N_{x}\right)_{c r}=k \frac{\pi^{2} D}{b^{2}} \tag{4.13-7}
\end{equation*}
\]
where the value of \(k\) depends on the ratio \(\frac{a}{b}\) and on the linear distribution of the loading. Specific values of \(k\) are given in Table 9-6 on page 337 of reference 4.13-2. For the plate considered herein, the value of \(k\) is 24.1 which then gives a critical load of \(6534.54 \mathrm{lb} / \mathrm{in}\).

\section*{Uniform Inplane Shear}

For this analysis, the full model of plate 3 is used and the loading corresponds to
\[
N_{x y}^{o}=1.0 \mathrm{lb} / \mathrm{in} .
\]

From pages 379-385 of reference 4.13-2, the buckling load is given as
\[
\begin{equation*}
\left(N_{x y}\right)_{c r}=k \frac{\pi^{2} D}{a^{2}} \tag{4.13-8}
\end{equation*}
\]
where the value of \(k\) depends on the ratio of \(\frac{b}{a}\) and is given in Table 9-10 on page 382 of reference 4.13-2. For the plate considered herein, the value of \(k\) is 7.53 which then gives a critical load of \(3629.69 \mathrm{lb} / \mathrm{in}\).

\subsection*{4.13.2 PROCEDURE USAGE}

Procedure RECT PLATE may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call RECT_PLATE ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure RECT_PLATE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline CASE & 0 & Select analysis case \\
\hline E & 30.E6 & Young's Modulus \\
\hline ES.PROC & ES1 & Element Processor \\
\hline ES_NAME & EX47 & Element name \\
\hline LX & 7.5 & Length in x -direction \\
\hline LY & 10.0 & Length in y-direction \\
\hline NU & 0.3 & Poisson's ratio \\
\hline PRINT & <false> & Print flag \\
\hline THICKNESS & 0.1 & Thickness \\
\hline UTDEN & 0.1 & Weight density \\
\hline
\end{tabular}

\subsection*{4.13.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.13.3.1 CASE}

Select analysis case (default: 0). This argument is used to select a specified analysis case number from one to six. The procedure will then perform only that specfic analysis. If all six analysis cases are desired, then the argument CASE should be set to zero.

\subsection*{4.13.3.2 E}

Young's elastic modulus (default: \(30.0 \times 10^{6} \mathrm{psi}\) ).

\subsection*{4.13.3.3 ES. NAME}

Element name (default: EX47). This is the name of the specific shell-element type you wish to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX47, is a 4 -noded quadrilateral element implemented in Processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.13-3).

\subsection*{4.13.3.4 ES_PRDC}

Element Processor (default: ES1) This is the name of the structural element (ES) Processor that contains the shell element type you wish to employ in the model. The default shellelement, Processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{4.13.3.5 LX}

Length of the plate model in the \(x\)-direction (default: 7.5 inches).

\subsection*{4.13.3.6 LY}

Length of the plate model in the \(y\)-direction (default: 10.0 inches).

\subsection*{4.13.3.7 NO}

Poisson's ratio (default: 0.3).

\subsection*{4.13.3.8 PRINT}

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, modeshapes, stresses) will be printed.

\subsection*{4.13.3.9 THICKNESS}

Thickness of the plate (default: 0.1 inches).

\subsection*{4.13.3.10 UTDER}

Weight density (default: \(0.1 \mathrm{lb} / \mathrm{in} .^{3}\) ). Processor LAU converts the weight density to mass density.

\subsection*{4.13.4 USAGE GUIDELINES AND EXAMPLES}

Procedure RECT_PLATE may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
*call RECT_PLATE ( ES_PROC = ES1 \(;\) ES_NAME = EX47 ; --
CASE \(=0\); --
\(\mathrm{LX}=7.5\); --
\(L Y=10.0\); --
\(\mathrm{E}=30 . \mathrm{E} 6\); --
\(\mathrm{NO}=0.3\); --
PRINT = 〈false〉; --
THICKNESS \(=0.1\); --
WTDEN \(=0.1\) )
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,
*call RECT_PLATE
Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.13-1.

Table 4.13-1 Typical CPU Times for Various Computer Systems
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CONVEX C220 & \\
\hline VERSION 7.0 & \\
\hline URAY-2 & \\
\hline
\end{tabular}

\subsection*{4.13.5 LIMITATIONS}

The finite element model is restricted to models using 4 -node quadrilateral elements. The model has a total of 54 nodes and 40 elements ( 5 elements in the x -direction and 8 clements in the \(y\)-direction).

\subsection*{4.13.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.13.7 PROCEDURE FLOWCHART}
```

RECT_PLATE (main procedure)
ES (define elements)
L_VIBRAT_O (free vibration analysis; CASE=1)
L_STABIL_2 (buckling analysis with uniaxial compression; CASE=2)
L_STABIL_1 (buckling analysis with biaxial compression; CASE=3)
L_VIBRAT_1 (vibration with prestress; CASE=4)
L_STABIL_2 (buckling with inplane bending; CASE=5)
L_STABIL_1 (buckling with inplane shear; CASE=6)

```

\subsection*{4.13.8 PROCEDURE LISTING}

\subsection*{4.13.8.1 UNIX Script}
```

rect_plate.com

```
```

cd /scr/\$0SER
cp $CSM_PRC/proclib.gal proclib.gal
chnod u+m proclib.gal
rm rect_plate. }10
tine testbed << \endinput
*get echo off
*sot plib=28
*open 28 proclib.gal /old
*add '$CSM_APP/rect_plate/rect_plate.clp'
*open 1 rect_plate.101 /new
*def/a solver_neme = BLND
*def/a eigensolver_nane = LANZ

- Eigenvalue Problens (Buckling and Vibration)
for an Isotropic Rectangular Plate

```
```

*call RECT_PLATE ( case=2; es_name=ex47;es_proc=es7;print=<true>)
*stop
*close 28 /delete
\ondinput

```

\subsection*{4.13.8.2 CLAMP Procedure}
```

    rect_plate.clp
    ```
*PROCEDURE RECT_PLATE ( case=0; es_name='ex47';es_proc='es1'; --
        \(1 x=7.5 ; 1 y=10.0 ; e=30.0 e+6 ; n u=0.3 ;--\)
        thickness=0.1; wtden=0.1;print=<false>)
```

- Rectangular plate
*def/e g = < [@] / <2. * <1.+[nu]> > >
*dof/* alpha = .1-4
[XQT TAB
START 54,6
title'rectangolar plate problem
TEXT
'tHE POLLOWING PLATE PROBLEMS ARE SOLVED IN THIS mUN:
, 1 free vibration of ^ rectangular plate.
, 2 bockling of \ rectangular plate, compressed IN ONE direction.
, 3 BUCKLING OF \& RECTANGULAR PLATE, ONIFORM COMPRESSION.
, 4 free vibrltion Of \& PRE-STreSSEd rectangular plate.
, 5 buckling of a rectangular plate, bending load.
, b buckling of a mectangdlar plate, shear load.
,
joimt Locations
1000 [lx] 0 0 0 10
6 O [ly] O [lx] [ly] 0
CONSTAIINT CASE 1:
CON CASE 1
SYMMETRY PLANE=1
SYMMETRY PLANE=2
ZERO 3 4: 6,48,0
ZERO 3 5: 40,53
ZERO 3: 54
- CONSTRITNT CASE 2:
CON CASE 2
SYMMETRY PLANE=1
ZERO 2: 25
ZERO 3: 1,6: 12,54,6: 49,53
ZERO 4: 12,48,6
ZERO 5: 1,5: 49,53
- CONSTRIINT CASE 3:

```
```

CONSTRAINT CASE 3
ZERO 1: 1,6: 54
2RRO 2: 1,49,6
ZERO 3: 1,6: 12,54,6: 7,49,6: 50,53
ZERO 4: 12,48,6: 7,43,6
2ERO 5: 2,5: 50 53
[xqT AUS
TABLE(NI=16,NJ=1): DMB DATA 1 1
I=1,2,3,4,5,6,7,8,9
J=1: [0] [nu] [0] <g> <g> <g> <alpha\rangle <alpha> [vtden]
TABLE (NI=3,NJ=1,ITYPE=0): LAK OMB 1 1
J=1 : 1 [thickness] 0.
[XqT LAO
stop
-
*call ES ( function m 'DEFINE ELEMENTS' ; es_proc = [es_proc] ; --
es_name = [es_name] ; es_pars = 0.0 )
[XqT ELD
<ES_EXPE_CMD>
NSECT = 1
1287158

- LOAD CASE 1:
[xqT AOS
ALPHA: CASE TITLE 1
1'conpressive forces in y-direction applied at y=10.
SYSTEC: APPLIED FORCES 1
I=2
JOINTS=40: 54: -.75
JOINTS=50,53: -1.5
. LOAD CASE 2:
ALPEA: CASE TITLE 2
1'compressive forces in x- and y-directions applied at y=10., x=7.5
SISVEC: APPLIED FORCES 2
I=2
JOINTS=49: 54: -.75
JOIMTS =50,53: -1.50
I=1
JOINTS=6:54:-.625
JOINTS =12,48,6: -1.25
.
. LOAD CASE 3:
ALPHA: CASE TITLE 3
1'bending forces applied at x=7.5
SYSVEC: APPLIED FORCES 3
I=1
JOINTS=6: . 57292

```
```

JOINTS=12,24,6: .9375 .6250 . 3125
JOINTS=36,48,6: -. 3125 -.6250 -. .9375
JOINTS=54: -.57292
. LOAD CASE 4:
ALPHA: CASE TITLE 4
1'shear forces applied at x=7.5 and y=10.
SISVEC: APPLIED FORCES 4
I=2
JOINTS=6: 54: . 625
JOINTS=12,48,6: 1.250
I=1
JOINTS=49: 54: . }75
JOINTS=50,53: 1.500
. LOAD CASE 5:
ALPHA: CASE TITLE 5
1'tensile forces in x-direction applied at x=7.5
SYSVEC: APPLIED FORCES 6
I=1
JOINTS=6: 54: 1250.
JOINTS=12,48,6: 2500.
stop
. PROCESS
*if < [case] /eq 0 >/then
*call L_vibrat_0 ( function='all';N_modes=6;print=[print];vcon_set=1 ; --
mass_type='consistent')
*call L_STABIL_2 ( function='fact_solv';N_modes=2; --
cons_set=1; bcon_set=1; --
shift=0.0; stress=<true>; --
reaction=<true>;print=[print] )
*call L_STABIL_1 ( function='EIGEN'; bcon_set=1; --
M_modes=2; ps_1=-1.0;ps_2=-1.0;print=[print] )
*call L_VIBRAT_1 ( function='all';vcon_set=1; --
ps_1=1000.0;ps_2=1000.0;N_modes=6;print=[print] ; --
mass_type='consistent')
*call L_STABIL_2 ( function='fact_solv';N_modes=2; --
cons_set=2;bcon_set=2;load_set=3; --
shift=0.0; stress=\langletrue>; --
reaction=<true>;print=[print] )
*call L_STABIL_1 ( function='all';N_modes=2; --
ps_3=1.0;bcon_set=3; --
shift=0.0; --

```
```

    print=[print] )
    .
*else
*if < [cese] /eq 1 >/then
*call L_VIBRAT_0 ( function='all';N_modes=6;print=[print];vcon_set=1 ; --
mass_type='consistent')
•
*elseif < [case] /eq 2 >/then
*call L_STABIL_2 ( function='all';N_modes=2; --
location='all';direction=1; --
cons_set=1; bcon_set=1; --
shift=0.0; stress=<true>; --
reaction=<true>;print=[print] )
*elseif < [case] /eq 3 >/then
*call L_STABIL_1 ( function='all'; bcon_sot=1; --
N_modes=2; ps_1=-1.0;ps_2=-1.0;print=[print] )
*elsoif < [case] /eq 4 >/then
*call L_VIBl_T_1 ( function='all';vcon_set=1; --
ps_1=1000.0;ps_2=1000.0;N_modes=6;print=[print] ; --
mass_type='consistent')
•
*elseif < [case] /eq 5 >/then
*call L_STABIL_2 ( function='all';N_modes=2; --
cons_set=2;bcon_set=2;load_set=3; --
shift=0.0; stress=<true>; --
reaction=<true>;print=[print])
*elseif < [case] /eq 6 %/then
*call L_STABIL_1 ( function='all';N_modes=2; --
ps_3=1.0;bcon_set=3; --
shift=0.0; --
print=[print] )
*endif
*endif
-
[xqt dcu
toc 1
*end

```

\subsection*{4.13.9 REFERENCES}
4.13-1 Timoshenko, S., Young, D. H. and Weaver, W., Jr.: Vibration Problems in Engineering, Fourth Edition, John Wiley and Sons, Inc., New York, 1974.
4.13-2 Timoshenko, S. P.; and Gere, J. M.: Theory of Elastic Stability, Second Edition, McGraw-Hill, New York, 1961.
4.13-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

\subsection*{4.14 Processor RHOMBIC_PLATE}

\section*{THIS SECTION UNDER PREPARATION}

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\subsection*{4.15 Processor TRUNCATED_CONE}

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THIS SECTION UNDER PREPARATION
}

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\subsection*{4.16 Procedure VIB_2D}

\subsection*{4.16.1 GENERAL DESCRIPTION}

This application procedure involves linear free vibration analyses of a beam and a circular ring (see Figure 4.16-1). These one-dimensional structures are modeled using twodimensional shell elements. Various boundary conditions are imposed to obtain vibration modes about different coordinate axes.

(a) Cantilevered Beam
\(E=10 . \times 10^{6} \mathrm{psi}\)
\(\mathrm{V}=0\).
inner radius \(=6.366\) inches outer radius \(=7.366\) inches thickness \(=.1\) inches

(b) Circular Ring

Figure 4.16-1 Free Vibration Problems

\subsection*{4.16.1.1 Model Description}

Procedure VIB_2D uses a full model of the cantilevered beam and a quarter model of the circular ring. The mesh topology is rectangular and restricted to quadrilateral shell elements with 4 - or 9 -nodes. The mesh generation capability of processor ELD is used to generate the various meshes used in this application problem. The cantilevered beam shown in figure 4.16-1a is fixed at one end and free at the other. Only a quarter of the circular ring shown in figure \(4.16-1 \mathrm{~b}\) is modeled with symmetry conditions imposed at both ends.

\subsection*{4.16.1.2 Analysis Description}

Procedure VIB_2D performs three different linear free vibration analyses through successive procedure calls using the solution procedure L_VIBRAT_O described in Chapter 3.

\subsection*{4.16.1.3 Available Solution}

Analytical solutions for the vibration analyses are available in reference 4.16-1.

\section*{Case 1: Free Inplane Vibration}

For this analysis, all degrees of freedom in the \(z\)-direction have been constrained to zero so that only inplane vibration will occur. From page 369 of reference 4.16-1, the frequencies for longitudinal (axial) vibration are given as
\[
\begin{equation*}
\omega_{m}=\frac{m \pi}{2 L} \sqrt{\frac{E}{\rho}} \tag{4.16-1}
\end{equation*}
\]
and the frequencies for inplane flexural vibrations are given on page 426 of references 4.16-1 as
\[
\begin{equation*}
\omega_{m}=k_{m}^{2} \sqrt{\frac{E I_{z z}}{\rho A}} \tag{4.16-2}
\end{equation*}
\]
where
\[
\begin{aligned}
\omega_{m} & =\text { circular frequency (radians/second) } \\
\rho & =\text { mass density } \\
L & =\text { beam length } \\
E & =\text { Young's modulus } \\
I_{z z} & =\text { Moment of Inertia about } z \text {-axis, } \frac{1}{12} b^{3} h \\
\nu & =\text { Poisson's ratio } \\
m & =\text { number of half-waves in the } x \text {-directions, respectively }
\end{aligned}
\]
and
\[
f_{m}=\frac{\omega_{m}}{2 \pi} \quad \text { (hertz) }
\]

The constant \(k_{m}\) is obtained from the roots of the equation
\[
\begin{equation*}
\cos k_{m} L \cosh k_{m} L=-1 \tag{4.16-3}
\end{equation*}
\]

The consecutive roots of this equation are
\begin{tabular}{|c|c|}
\hline\(m\) & \(k_{m} L\) \\
\hline 1 & 1.875 \\
\hline 2 & 4.694 \\
\hline 3 & 7.855 \\
\hline 4 & 10.996 \\
\hline
\end{tabular}

Using these formula, frequencies for this problem may be computed as follows:
\begin{tabular}{|c|r|r|l|}
\hline\(m\) & \multicolumn{1}{|c|}{\(\omega_{m}^{2}\)} & \multicolumn{1}{|c|}{\(f_{m}\)} & Type \\
\hline 1 & \(4.776 \times 10^{5}\) & 109.990 & Flexural \\
2 & \(187.590 \times 10^{5}\) & 689.326 & Flexural \\
1 & \(1144.085 \times 10^{5}\) & 1702.351 & Axial \\
3 & \(1471.031 \times 10^{5}\) & 1930.328 & Flexural \\
2 & \(4576.338 \times 10^{5}\) & 3404.702 & Axial \\
4 & \(5649.057 \times 10^{5}\) & 3782.754 & Flexural \\
3 & \(10296.761 \times 10^{5}\) & 5107.054 & Axial \\
\hline
\end{tabular}

\section*{Case 2: Free Lateral Vibration}

For this analysis, only the degrees of freedom in the \(z\)-direction are unconstrained and hence lateral vibration mode shapes and frequencies will be obtained. From page 426 of reference 4.16-1, the frequencies are given as
\[
\begin{equation*}
\omega_{m}=k_{m}^{2} \sqrt{\frac{E I_{y v}}{\rho A}} \tag{4.16-4}
\end{equation*}
\]
where
\[
\begin{aligned}
& k_{m}=\text { roots of equation 4.16-3 } \\
& I_{y y}=\text { moment of inertia about } y \text {-axis, } \frac{1}{12} b h^{3}
\end{aligned}
\]

Using this formula, the vibration frequencies for this problem may be computed as follows:
\begin{tabular}{|c|r|r|}
\hline\(m\) & \multicolumn{1}{|c|}{\(\omega_{m}^{2}\)} & \(f_{m}\) \\
\hline 1 & \(4.776 \times 10^{3}\) & 10.999 \\
2 & \(187.590 \times 10^{3}\) & 68.933 \\
3 & \(1471.031 \times 10^{3}\) & 193.033 \\
4 & \(5649.057 \times 10^{3}\) & 378.275 \\
\hline
\end{tabular}

\section*{Case 3: Free Vibration of Ring}

For this analysis, a quarter model of the circular ring is used. The extensional vibration modes resemble the longitudinal vibration modes of prismatic beams. The simplest extensional mode of vibration corresponds to uniform radial motion of the ring (circles of periodically varying radius). From pages 476-477 of reference 4.16-1, the frequencies for the extensional vibration modes are given as
\[
\begin{equation*}
\omega_{m}=\sqrt{\frac{E\left(1+m^{2}\right)}{\rho R^{2}}} \tag{4.16-5}
\end{equation*}
\]
where \(R\) is the radius of centerline of ring.
Pure radial vibrations are obtained for the case of \(m=0\). Using this formula, the frequencies for extensional vibration may be computed as follows:
\begin{tabular}{|c|c|c|}
\hline\(m\) & \(\omega_{m}^{2}\) & \(f_{m}\) \\
\hline 0 & \(1.1441 \times 10^{8}\) & 1702.351 \\
1 & \(2.2882 \times 10^{8}\) & 2407.488 \\
2 & \(5.7204 \times 10^{8}\) & 3806.573 \\
3 & \(11.4408 \times 10^{8}\) & 5383.308 \\
\hline
\end{tabular}

The inplane flexural vibration of a circular ring corresponds to vibration modes in the plane of the ring. From pages 479-481 of reference 4.16-1, these frequencies are given as:
\[
\begin{equation*}
\omega_{m}=\sqrt{\frac{E I_{z z} m^{2}\left(1-m^{2}\right)^{2}}{\rho A R^{4}\left(1+m^{2}\right)}} \tag{4.16-6}
\end{equation*}
\]

For \(m=1\), the frequency is zero which implies that the ring moves as a rigid body. Using this formula, the frequencies for the inplane vibration modes may be computed as follows:
\begin{tabular}{|c|c|c|}
\hline\(m\) & \(\omega_{m}^{2}\) & \(f_{m}\) \\
\hline 1 & 0.0 & 0.0 \\
2 & 169.3749 & 2.071 \\
3 & 1354.9994 & 5.858 \\
4 & 4981.6155 & 11.233 \\
6 & 28038.4171 & 26.650 \\
8 & 91931.4991 & 48.256 \\
10 & 228278.8317 & 76.042 \\
\hline
\end{tabular}

\subsection*{4.16.2 PROCEDURE USAGE}

Procedure VIB_2D may be used by preceding the procedure name by the *call directive, and following it by a iist of arguments enclosed in parentheses. Procedure ā̄guments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
```

*call VIB_2D ( arg1 = val1 ; arg2 = val2 ; ...)

```
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure VIB_2D are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
\begin{tabular}{|c|c|c|}
\hline Argument & Default Value & Meaning \\
\hline case & bar & Select vibration case \\
\hline E & 10.E6 & Young's Modulus \\
\hline ES_PROC & ES1 & Element Processor \\
\hline ES MaME & EX97 & Element name \\
\hline GRIDS & 1 & Grid identification numbers \\
\hline NGRIDS & 1 & Number of grids \\
\hline HNX & 3 & Number of nodes for each grid \\
\hline L & 10.0 & Length in x -direction \\
\hline PRINT & <false> & Print flag \\
\hline THICRNESS & 0.1 & Thickness \\
\hline WTDEN & 5/6 & Weight density \\
\hline B & 1.0 & Beam or ring depth \\
\hline DBC & VIB_2D.DBC & Computational database name \\
\hline DBR & VIB_2D.DBR & Results database name \\
\hline SHIFT & 0.0 & Eigenvalue shift \\
\hline MASS_TYPE & CONSISTENT & Type of mass matrix \\
\hline N.MODES & 5 & Number of eigenvalues desired \\
\hline
\end{tabular}

\subsection*{4.16.3 ARGUMENT DESCRIPTIONS}

\subsection*{4.16.3.1 CASE}

Select vibration case (default: BAR). This argument selects the vibration analysis to perform. The options include BAR, BEAM, and RING. The CASE=BAR, the analysis corresponds to the axial vibration of a rod. For CASE=BEAM, the analysis corresponds to the lateral vibration of a beam. For CASE=RING, the analysis corresponds to extensional and flexural vibration of a circular ring.

\subsection*{4.16.3.2 DBC}

Name of computational database file (default=VIB_2D.DBC). This file will contain all model definition data, element computational data, one copy of the assembled and factored stiffness matrices, the buckling eigensolution, and displacement and internal force vectors for every load step computed during the analysis.

\subsection*{4.16.3.3 DBR}

Name of results database file (default=VIB_2D.DBR). This file will contain one dataset called RESPONSE. HISTORY generated during nonlinear analysis. The dataset will contain record groups - indexed by load step number - for a number of solution parameters, including the load factor and maximum axial displacement components. This database is valuable for obtaining load-displacement plots, and for evaluating the performance of the nonlinear solution strategy employed.

\subsection*{4.16.3.4 E}

Young's elastic modulus (default: \(10.0 \times 10^{6} \mathrm{psi}\) ).

\subsection*{4.16.3.5 ES.NAME}

Element name (default: EX97). This argument gives the name of the specific shell-element type to select, within the element processor defined by argument ES_PROC. The default shell-element type, EX97, is a 9-node quadrilateral element implemented in processor ES1, and described in The Computational Structural Mechanics Testbed User's Manual (see ref. 4.16-2).

\subsection*{4.16.3.6 ES_PROC}

Element processor (default: ES1) This argument gives the name of the structural element (ES) processor that contains the shell element type to employ in the model. The default shell-element, processor ES1, is described in The Computational Structural Mechanics Testbed User's Manual.

\subsection*{4.16.3.7 GRIDS}

Grid identification numbers (default: 1). This array specifies the identification number for each discretization.

\subsection*{4.16.3.8}

Length of the beam model in the \(x\)-direction (default: 10.0 inches). For the case of the circular ring, the radius is calculated as \(2 \mathrm{~L} / \pi\).

\subsection*{4.16.3.9 MASS_TYPE}

Type of mass matrix (default: CONSISTENT). If MASS_TYPE = CONSISTENT, the element processor will generate consistent element mass matrices that will be assembled by processor K to form the system mass matrix. If MASS_TYPE = DIAGONAL, the element processor will generate a diagonal or lumped mass matrix.

\subsection*{4.16.3.10 MGRIDS}

Number of grids (default: 1). This argument provides a mechanism to perform automatically a limited convergence study using several different discretizations.

\subsection*{4.16.3.11 H_MODES}

Number of converged eigenvalues desired (default: 5). This argument specifies the number of eigenvalues to calculate to a convergence criterion of .0001 .

\subsection*{4.16.3.12 NNX}

Array of number of nodes for WGRIDS models (default: 3). This array is of length NGRIDS and represents the number of nodes along the length of the beam or along the circumference of the ring.

\subsection*{4.16.3.13 PRINT}

Print flag (default: <false>). If the argument PRINT is defined to be <true>, then all computed results (displacements, modeshapes, stresses) will be printed.

\subsection*{4.16.3.14 SHIFT}

Eigenvalue shift (default: 0.0 ). Converged eigenvalues will only be obtained for eigenvalues greater than SHIFT. The shift parameter refers to the frequency squared ( \(\omega^{\mathbf{2}}\) ) for vibration problems.

\subsection*{4.16.3.15 THICKNESS}

Thickness of the beam (default: 0.1 inches). The ring thickness has a default value of one-tenth the beam thickness.

\subsection*{4.16.3.16 UTDEN}

Weight density (default: \(5 / 6 \mathrm{lb} / \mathrm{in} .^{3}\) ). Processor LAU converts the weight density to mass density.

\subsection*{4.16.4 USAGE GUIDELINES AND EXAMPLES}

Procedure VIB_2D may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
```

*call VIB_2D ( ES_PROC = ES1 ; ES_MAME = EX47 ; --
L = 10.0 ; --
E = 10.E6 ; --
B = 1.0 ; --
DBC = VIB_2D.DBC ; --

```
```

DBR = VIB_2D.DBR ; --
MASS_TYPE = CONSISTENT ; --
GRIDS = 1,2,3 ; --
NGRIDS = 3;-
MNX = 5,9,17; --
SHIFT = 0.0 ; --
N_MODES = 5 ; --
PRINT = <false\rangle ; --
THICKNESS = 0.1 ; --
UTDEN = 0.1

```
(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, that is,
*call VIB_2D
Using the default values for the procedure arguments, the amount of CPU time required for this analysis on various computer systems is shown in Table 4.16-1.

Table 4.16-1 Typical CPU Times for Various Computer Systems
\begin{tabular}{|c|c|}
\hline Computer System & \begin{tabular}{c} 
Total \\
CPU Time, \\
seconds.
\end{tabular} \\
\hline VAX 11/785 & \\
\hline VMS 4.7 & \\
\hline MicroVAX \\
ULTRIX 2.2 & \\
\hline SUN & \\
\hline SUNVIEW 4.0 & \\
\hline CRNVEX C220 \\
VERSION 7.0 & \\
\hline
\end{tabular}

\subsection*{4.16.5 LIMITATIONS}

None.

\subsection*{4.16.6 ERROR MESSAGES AND WARNINGS}

None.

\subsection*{4.16.7 PROCEDURE FLOWCHART}

VIB_2D
VIB_2D_CTL
VIB_2D_MOD
ES
VIB_2D_CON
VIB_2D_BCS
ES
L_VIBRAT_O
(main procedure)
(control procedure)
(define 2-D models of beam/ring)
(define elements)
(define connectivities)
(define boundary conditions)
(define freedoms)
(linear free vibration solution procedure)

\subsection*{4.16.8 PROCEDURE LISTING}

\subsection*{4.16.8.1 UNIX Script}
```

cd /scr/$OSE&
cp CSH_PRC/proclib.gal proclib.gal
chmod u+t proclib.gal
1m VIB*.*
tine testbed << \ondinput
*set echo off
*set plib=28
Hopen 28 proclib.gel /old
#add '$CSM_APP/vib_2d/vib_2d.clp'
\#def/a solver_name = INV
*def/a eigensolver_name = EIG2
. Axial Vibration of a Bar
*cal1 VIB_2D ( case = BAR; mass_type = CONSISTENT; --
ES_PROC=ES7 ; ES_NAME=EX97; --
L =10.0 ; thickness = . 1 ; b = 1.0 ; --
E = 1.07 ; utden = <5./6.> ; ---
M_modes = 5 ; print= <ialse\rangle ; --
shift=0.0 ; mnx=7,0,11; grids=1,2,3; ngrids=3; --
DBC=VIB_2D.DBC; DRR=VIB_2D.DBR )
. Lateral Vibration of a Beam
*call VIB_2D ( case = BEAM ; Ease_type = CONSISTENT; --
ES_PROC=ES7 ; ES_NAME=EX97; --
I. = 10.0 ; thicknesm = .1 ; b = 1.0 ; --
E = 1.e7 ; Etdon =<6./6.> ; ---
N_modes = 5 ; print= <ialse\rangle ; --
shift=0.0 ; nnx=5,0,17; grids=1,2,3; ngrids=3; --
DBC=\IB_2D.DBC; DBR=VIB_2D.DBR )
. Extensional and Flexural Vibrations of a Circular Ring
*call \nablaIB_2D ( case = RING ; mass_type = CONSISTENT; --
ES_PROC=ES7 ; ES_NAME=EX97; --
L = 10.0 ; thickness = .1 ; b = 1.0 ; --
E = 1.e7 ; wtden = <5./6.> ; ---
N_modes = 5 ; print=\langle{alse\rangle ; --
shift=0.0 ; mux=5,0,17; grids=1,2,3; ngrids=3; --
DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
*stop
*close 28 /delete
\ondinput

```

\subsection*{4.16.8.2 CLAMP Procedure}
vib_2d.clp
```

*procedure VIB_2D_CTL (case = BAR ; -- . BAR | BEAK | RING
mass_type = CONSISTENT ; - . CONSISTENT | DIAGONAL
ES_PROC=ES1 ; ES_NAME=EX97; --
L = 10.0 ; thickness = .1 ; b = 1.0 ; --
E = 1.e7 ; wtden = <5./6.\rangle ; ---
N_modes = 5 ; print= <false\rangle ; --
shift=0.0 ; nnx=5; grid=1; --
DBC=VIB_2D.DBC; DBR=VIB_2D.DBR )
*Open/ner 1, [DBC]
*call VIB_2D_HOD ( es_proc = [es_proc] ; es_name = [es_name]; --
nnx = [nnx] ; L = [L]; h=[thickness] ; --
E=[E]; b=[b]; rho=[wtden]; case=[case] )
. *shov macros
. Fset echo,on
*call L_VIBRAT_0 ( N_modes=[N_modes]; print = [print]; --
shift=[shift]; --
mass_type=[mass_type])
*end
*procedure VIB_2D_MOD ( es_proc=ES1; es_name=EX97; es_pars=0.; --
nnx = 11 ; --
L = 10.0; h = .1 ; --
E = 1.e7;b=1.0; --
rho = <5./6.\rangle ; case = BAR )
-----------------------------------------------------------
Vibrations of a Cantilevered Bean via Plate Elements
Define Model
*call ES ( function = 'DEFINE ELEMENTS' ; es_proc = [es_proc]; --
es_mame = [es_name] ; es_pars = [es_pars])
*def/i nny = < <ES_NEN>-.6 >
[XQT TAB
*def/i nnt = < [nnx]*<nny> >
START <nnt>
JLOC
DEPINE NODAL COORDINATES
*if < <IFELSE([case];RING;1;0)> >/then

- Define First Quadrant of a Cylinder of Unit Axial Length

```
```

*def/e theta = 90.

```
*def/e theta = 90.
*def/e radius = ([L]*2/\langlepi\rangle)
*def/e radius = ([L]*2/\langlepi\rangle)
FORMAT = 2
FORMAT = 2
1. <radius>, 0., 0., <radius>, <theta>, 0., [nnx], 1, <nny>
1. <radius>, 0., 0., <radius>, <theta>, 0., [nnx], 1, <nny>
[nnx], <radius>, 0., 1., <radius>, <theta>, 1.
```

[nnx], <radius>, 0., 1., <radius>, <theta>, 1.

```
```

        JREF
            NREF = -1
                1, <nnt>
    *else
    1, 0., 0., 0., [L], 0., 0., [nnx], 1, <nny>
        [nnx], 0., [b], 0., [L], [b], 0.
    *endif
    DEPINE MATERIAL/SECTION PROPERTIES
[xqT AUS

- Build Table of Material Data
TABLE(NI=16,NJ=1): OMB DATA 1 1
*def/e12.4 NO = 0.0
*def/g12.4 G = < [E] / (2.*(1.+\langleNU\rangle)) >
I=1,2,3,4, 5, 6,7,8,9
J=1: [E] <NU\rangle [E] <G\rangle\langleG\rangle \langleG\rangle 0. 0. [rho]
. Build Laminate Data Tables
TABLE(NI=3,NJ』1,ITYPE=0): LAY OMB 1 1
I=1,2,3 . (naterial_type, layer_thickness, angle(deg.)
J=1: 1 [h] 0.0
[XQT LAO
ONLINE=2
- GENERATE ELEMENTS
[xqt ELDD
<ES_EXPE_CMD>
ASECT = 1
Define elenent nodal connectivity
\#call VIB_2D_CONN ( nnx=[nnx]; nny=<nny>; nen=<es_nen> )
DEFINE BOUNDARY CONDITIONS
*call VIB_2D_BCS (nnx = [nnx] ; nny = <nny> ; --
nen = \langlees_nen> ; case = [case] )
ecall ES ( Iunction = 'DEFINE FREEDOHS' )
*end
*procedure VIB_2D_CONN ( nnx; nny; nen )

```

```

- Define Element Connectivity Hecord for ELD Processor

```

```

    *if < [nen] /eq 4>/then
        *do \iy = 1, <[nny]-1>
            *do $ix = 1, <[nnx]-1>
    ```
```

                *def/i n1 = < (<$iy>-1)*[nnx] + <$ix\rangle >
                *def/i n2 = < <n1> + 1 >
                *det/i n3 = < <n2\rangle + [nnx] >
                *def/i n4 = < <n3> - 1 >
                    «జエ===================
                    <n1> <n2> <n3> <n4>
    ```

```

                *onddo
        *onddo
    *elsoif < [non] /eq 9 > /thon
        *do $iy = 1, <[nny]-2>, 2
            *do $ix = 1, <[nnx]-2>, 2
                *def/i n1 = < (<$iy>-1)*[nnx] + <|ix>>
                *dof/i n2 = < <n1\rangle + 2 \rangle
                *dof/i n3 = < <n2\rangle + (2*[nnx]) >
                *def/i n4 = < <n3\rangle-2\rangle
                *def/i n5 = <\langlen1\rangle + 1 \rangle
                *dof/i n6 = < <n2\rangle + [nnx] \rangle
                *def/i n7 = < <n4\rangle + 1\rangle
                *def/i n8 = < <n6> - 2 \rangle
                *def/i n9 = < <n8> + 1 >
    ```



```

            *enddo
        *enddo
    *ondif
    *end
*procedure VIB_2D_BCS ( nnx=3; nny=3; nen=9; case = BAR )
. Define Boundary Conditions for Bean/Plate Vibrations
*def/i nnt = < [nnx]*[nny] >
[xqt TAB
CON 1
*if < <IFELSE([caso];BAR;1;0)> > /then
. DEFIRE CLAMPED BOONDARY CONDITIONS for LONGITODINAL vIBRATIONS
• ------------------------------------------------------------------------
ZERO 3, 4, 5 : 1, <nnt> . Suppress Out-of-Plane DOFS Everywhere
ZERO 1,2,3,4,5,6 . Clamp left boundary
*do %n=1,<<nnt>-[nnx]+1>, [nnx]
<\$n>
*enddo
*elseif < <IFELSE([case];BEAK;1;0)> > /thon
. DEFINE CLAMPED BOONDARY CONDITIONS for INPLANE VIBRATIONS

```
```

    ZERO 1, 2, 6: 1, <nnt> . Suppress In-Plane DOFS Everywhere
    ZERO 1,2,3,4,5,6 . Clamp left boundary
    *do %n=1,<<nnt>-[nnx]+1>, [nnx]
        <$n>
    *enddo
    *elseif < <IPELSE([cese];RING;1;0)> > /then
. dEFINE bOUNDARY CONDItIONS for EXTENSIDNAL and flEXURAL vibiationS

```
```

    ZERO 3, 4, 5: 1, <nnt> . Suppress Out-of-Plane DOFS Everywhere
    ```
    ZERO 3, 4, 5: 1, <nnt> . Suppress Out-of-Plane DOFS Everywhere
    SMMETRY PLANE = 1 . Symetry at theta = 90; 1/4 Model
    SMMETRY PLANE = 1 . Symetry at theta = 90; 1/4 Model
    STMMETRY PLINE = 2 . Syanetry at theta = 0
    STMMETRY PLINE = 2 . Syanetry at theta = 0
*endif
*end
*procodure VIB_2D ( case=BAR; nass_typexCONSISTENT;ngrids=1; grids=1; --
                L = 10.0 ; thickness = .1 ; b = 1.0 ; --
                E = 1.e7 ; wtden = <5./6.\rangle ; ---
                N_modes = 5 ; print= <false> ; nnx=3 ; --
                        shift=0.0 ; es_proc=ES1; es_name=EX97; --
                        DBC=\nablaIB_2D.DBC; DBR=\nablaIB_2D.DBR )
    *if < <IFELSE([CASE];BAR;1;0)> >/then
        *def/d thickness = [thickness]
    *elseif < <IFELSE([CASE];BEAM;1;0)> >/then
        *dof/d thickness = [thickness]
    *elseif < <IFELSE([CASE];RING;1;0)> > /then
        *de1/d thickness = < [thickness] / 10.0 >
    *endif
    *dof/i grids[1:[ngrids]] = [grids]
    *def/i mnx[1:[ngrids]] = [nnx]
    *do $g = 1,[ngrids]
        *def/i grid = <grids[<$g>]>
        *dof/i nnxs = <nnx[<&g>]>
        *call VIB_2D_CTL (case = [case]; mass_type = [aas_type] ; --
                        es_proc = [es_proc]; es_name = [es_name] ; --
                        nnx = <nnxs> ; thickness = <thickness> ; --
                L}\quad=[L] ; b= [b] ; --
                E = [E] ; wtden = [wtden] ; ---
                N_modes = [N_modes]; print= [print] ; --
                shift=[shift] ; --
                                DBC=[DBC]; DBR=[DBR] ; --
                                grid=<grid>)
    *enddo
*end
```


### 4.16.9 REFERENCES

4.16-1 Timoshenko, S., Young, D. H. and Weaver, W., Jr.: Vibration Problems in Engineering, Fourth Edition, John Wiley and Sons, Inc., New York, 1974.
4.16-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 5.0 Element Assessment Procedures

The procedures documented in this chapter are representative of the types of procedures that may be written to soive specific application (structural analysis) problems. Many of these high-level procedures invoke other (lower-level) procedures to perform preprocessing, solution, and postprocessing functions; which are described elsewhere in this manual. The use of procedures to perform structural analysis applications can provide users flexibility for parameterizing geometric data (e.g., stiffener spacing) as well as spatial discretization parameters (e.g., number of elements). The problems represented here are also intended to serve as part of a standard series of test problems to assess new structural elements installed in the CSM Testbed.

A summary of the procedures found in this chapter is provided by Table 5.0-1.

Table 5.0-1. Summary of Application Procedures
Procedure Name Problem Description

| DISTORTED_PC | Distorted-mesh version of the pinched_cyl problem; used <br> to study mesh distortion sensitivity of shell elements. |
| :--- | :--- |
| MH_BEAM | MacNeal-Harder Beam problems. |
| MH_CYL | MacNeal-Harder Thick-Walled Cylinder Problem. |
| MH_PLATE | MacNeal-Harder Plate Problems. |
| MH_SPHERE | Linear inextensional bending of a hemispherical shell <br> loaded by point forces. Model features "warped" quadri- <br> lateral shell-element (facet) discretization. |
| PATCH_TEST | Patch Test Problems. |
| SKEUED_GRID | Plate Buckling Problem with Skewed Grid. |

### 5.1 Processor DISTORTED.PC

## THIS SECTION UNDER PREPARATION

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### 5.2 Processor DISTORTED_PC_3D

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### 5.3 Procedure MH_BEAMS

### 5.3.1 GENERAL DESCRIPTION

### 5.3.1.1 Problem Description

This application problem solves the three MacNeal/Harder cantilever beam problems the twisted beam, the straight beam, and the curved beam. All three beams are solved with 4 - and 9 -node 2-D elements and 8 -, 20-, and 32-node $3-\mathrm{D}$ elements.

### 5.3.1.2 Model Description

The straight cantilever beam problem is solved using three element shapes - rectangular, trapezoidal, and parallelogram. This problem tests an element's ability to handle distorted meshes under various types of loading. It is clamped on one end and free at the other end where unit loads are applied in four directions - extension, torque, in-plane, and out-ofplane. The dimensions, mesh, and material properties of the beam are given in Figure 5.3-1.


Figure 5.3-1 MacNeal/Harder Straight Cantilever Beam
The twisted cantilever beam is modeled with 24 elements. The beam is clamped on one end and free at the other. It is twisted through $90^{\circ}$ root to tip. This problem tests an element's ability to handle warped elements (the four corners of the element do not lie in the same plane). Two different loading conditions are applied at the free end - in-plane unit load, and out-of-plane unit load. The dimensions, mesh, and material properties are shown in Figure 5.3-2.


Figure 5.3-2 MacNeal/Harder Twisted Cantilever Beam
The curved cantilever beam is modeled with six elements. It is clamped on one end and free at the other end, where unit loads are applied. The beam is curved, forming a $90^{\circ}$ arc. Two loading conditions are used - in-plane (vertical) and out-of-plane. This problem tests an element's ability to model in-plane curvature. The dimensions, mesh, and material properties are shown in Figure 5.3-3.

$$
\begin{aligned}
& E=1.0 \times 10^{7} \mathrm{psi} \\
& \mathrm{E}=0.25 \\
& \\
& \begin{array}{ll}
\text { inner radius } & =4.12 \text { inches } \\
\text { outer radius } & =4.32 \text { inches } \\
\text { arc } & =90^{\circ} \\
\text { thickness } & =0.1 \text { inches } \\
\text { mesh } & =6 \times 1
\end{array}
\end{aligned}
$$



Figure 5.3-3 MacNeal/Harder Curved Cantilever Beam

### 5.3.1.3 Analysis Description

A static, linear elastic analysis is performed, for any or all of the three problems. If the user chooses, displacements at the point of, and in the direction of the load are calculated and normalized with the theoretical results, for each loading condition.

### 5.3.1.4 Available Solutions

From reference 5.3-1, the theoretical solutions for the tip displacements for each problem and each loading condition are shown in Table 5.3-1.

| Load Condition | Tip displacement in direction of load (inches) |  |  |
| :--- | :---: | :---: | :---: |
|  | Straight | Curved | Twisted |
| Extension | $3.0 \times 10^{-5}$ | - | - |
| In-plane | .1081 | .08734 | .005424 |
| Out-of-plane | .4321 | .5022 | .001754 |
| Twist | .03208 | - | - |

Table 5.3-1 Theoretical tip displacements for each beam.

### 5.3.2 PROCEDURE USAGE

Procedure MH_BEAMS may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_BEAMS ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH_BEAMS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument | Default Value |
| :--- | :---: |
|  | 0. |
| ES_PARS | 0. |
| ES_PROC | ES1 |
| ES_IAME | EX47 |
| SPAR_DIM | none |
| DEL_IIB | <false> |
| REPORT | <true> |
| STRAIGHT | <true> |
| TWISTED | <true> |
| CURVED | <true> |

## Meaning

Element research parameters Element Processor
Element name 2-D or 3-D SPAR element Delete libraries Generate "report card" file
Solve straight beam
Solve twisted beam
Solve curved beam

### 5.3.3 ARGUMENT DESCRIPTIONS

### 5.3.3.1 ES_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

### 5.3.3.2 ES_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

### 5.3.3.3 ES_NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.3-2).

### 5.3.3.4 SPAR_DIM

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

### 5.3.3.5 DEL_LIB

Libraries are created for each model-stbm. 101 for the straight beam, cvbm. 101 for the curved beam, and twbm. 101 for the twisted beam. As the analysis proceeds, these libraries will automatically be deleted if DEL_LIB is <true>. This allows disk space to be conserved if the analyst does not need the libraries.

## 5．3．3．6 REPORT

Print report file（default＝＜true＞）．If REPORT is＜true＞an external file named BEAM＿＜es＿name＞．＜es＿proc＞will be generated．This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder．

## 5．3．3．7 STRAIGHT

Solve straight beam problem（default：＜true＞．This parameter simply indicates whether the straight cantilever beam problem is to be solved or not．

## 5．3．3．8 TUISTED

Solve twisted beam problem（default：＜true＞．This parameter simply indicates whether the twisted cantilever beam problem is to be solved or not．

## 5．3．3．9 CURVED

Solve curved beam problem（default：＜true＞．This parameter simply indicates whether the curved cantilever beam problem is to be solved or not．

## 5．3．4 USAGE GUIDELINES AND EXAMPLES

Procedure MH＿BEAMS may be used by preceding the procedure name by the $*$ call directive． Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called．A space or blank is required between the end of the procedure name and the left parenthesis．
＊procedure MH＿BEAMS（ES＿HAME＝EX47 ；－－
ES＿PROC＝ES1 ；－－
ES＿PARS $=0$ ；－－
SPAR＿DIM ；－－
DEL＿LIB＝〈false〉；－－
STRAIGHT＝＜true＞；－－
THISTED $=$＜true＞；－－
CURVED $=$＜true＞；－－
REPORT＝〈true〉 ）
（E1）To perform an analysis using the default options，simply invoke the procedure with－ out any arguments，i．e．，
＊call Mh＿beams
This will perform a static，linear elastic analysis of the MHBEAM problems．Since STRAIGHT，CURVED，and TWISTED are＜true＞and all three will be solved．Since REPORT is＜true＞and report card file named BEAM＿EX47．ES1 will be generated containing the normalized displacements of the corner nodes at the free end of the beams，Figure 5．3－4．

Figure 5．3－3 Report file generated using default arguments．
（E2）The following call statement will solve only the twisted beam problem for the ele－ ment EX08 in processor ES3．

```
*call MH_BEAMS ( ES_MAME = EXO8 ; --
    ES_PROC \(=\) ES3 ; --
    DEL_LIB \(=\) <true> ; --
    STRAIGHT = 〈false〉; --
    CURVED \(=\) 〈false〉; ;--
REPORT \(=\) 〈true〉
```

The library twbm． 101 will automatically be deleted．The report file BEAM＿EX08．ES3 is generated，Figure 5．3－5．


Figure 5.3-5 BEAM-EX08.ES3 resulting from the calling statement (E2).
(E3) The following call statement will solve the straight and twisted cantilever beam problems for the SPAR E43 element and generate the report file BEAM.E43.SPAR.

```
*call MH_BEAMS ( ES_HAME = E43 ; --
        ES_PROC = SPAR ; --
        SPAR_DIM = 2 ; --
        CURVED = <false> ; --
        REPORT = <true> )
```


### 5.3.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8- and 20-node solid elements.

### 5.3.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR_DIM is not set, the following error message will be printed and execution terminated.
The argument SPAR_DIM must be defined as 2 or 3 when
using SPAR elements.
Please set this argument and rerun.

### 5.3.7 PROCEDURE FLOWCHART

### 5.3.8 PROCEDURE LISTING

### 5.3.9 REFERENCES

5.3-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
5.3-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 5.4 Procedure MH_CYL

### 5.4.1 GENERAL DESCRIPTION

### 5.4.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The thick-walled cylinder problem is used to test an element's ability to handle a nearly incompressible material. As Poisson's ratio approaches 0.5 , singularities may arise in the stiffness matrix as a result of dividing by (1-2 $\nu$ ). Rubber, perhaps the most common nearly incompressible material, is sometimes used in structural components.

### 5.4.1.2 Model Description

A $10^{\circ}$ of the thick-walled cylinder, inner radius $=6$ inches, outer radius $=9$ inches, is modeled with only five elements as is shown in Figure 5.4-1. The thickness of this cross section is unity. Constraints are applied to all nodes so as to allow only radial displacements.

Either plate elements (2-D) or solid elements (3-D) may be used in this procedure. The 2 -D elements may be either the 4 - or 9 -node variety and the 3 -D elements may be either 8 - or 20 -node elements.

The cylinder is loaded with a unit pressure at the inner radius. This pressure is applied as a total force of .5236 lbs . distributed consistently on the nodes at the inner radius of the model, as is shown in Figure 5.4-2. Three sets of material properties are used in the analysis. Young's Modulus for all three is $1000.0 \mathrm{lb} / \mathrm{in}^{2}$, but Poisson's ratio is allowed to approach 0.5 by assuming the three values $.49, .499$, and .4999 .

a) 2-D

b) 3-D

Figure 5.4-1 MacNeal/Harder Thick-Walled Cylinder

a) 4-node 2 -D element

c) 8-node 3-D element

b) 9-node 2-D element

$P=-\frac{F}{12}$

$$
L=\frac{4 F}{12}
$$

d) 20-node 3-D element


ON CORNER NODES $=-5 / 8$ ON MIDEDGE NODES $=3 F / 16$
4) 32-node 3-D element

Figure 5.4-2 Consistent loading, 1.0 psi pressure at inner radius. $\mathbf{F}=.5236 \mathrm{lb}$.

### 5.4.1.3 Analysis Description

A static, linear elastic analysis is performed. The radial displacements of the nodes at the inner radius aré compared to theoretical displacements, and normalized results are printed.

### 5.4.1.4 Available Solutions

From reference 5.4-1, the exact solution for the radial displacement is:

$$
u(r)=\frac{(1+\nu) P R_{1}^{2}}{E\left(R_{2}^{2}-R_{1}^{2}\right)}\left[\frac{R_{2}^{2}}{r}+(1-2 \nu) r\right]
$$

where $R_{1}$ is the inner radius, $R_{2}$ is the outer radius, $P$ is the applied pressure, and $r$ is the variable radial position. Evaluating this expression at the inner radius ( $r=3.0$ ) for each value of $\nu$ yields the theoretical results in Table 5.4-1.

| Table 4.5-1 |  |
| :--- | :---: |
| Poisson's Ratio | Radial displacement at inner radius (inches) |
| 0.49 | $5.0399 \times 10^{-3}$ |
| 0.499 | $5.0602 \times 10^{-3}$ |
| 0.4999 | $5.0623 \times 10^{-3}$ |

### 5.4.2 PROCEDURE USAGE

Procedure MH_CYI may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_CYL ( arg1 = vall ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH_CYL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| ES_PROC | ES1 | Element Processor |
| ES_MAME | EX47 | Element name |
| ES_PARS | 0. | Element research parameters |
| SPAR_DIM | none | 2-D or 3-D SPAR element |
| REPORT | <true> | Generate "report card" file |

### 5.4.3 ARGUMENT DESCRIPTIONS

### 5.4.3.1 ES_NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.4-2).

### 5.4.3.2 ES_PROC

Element processor (default: ESI). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

### 5.4.3.3 ES_PARS

Element research parameters (default: $0 ., \ldots$ ). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

### 5.4.3.4 SPAR_DIM

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

### 5.4.3.5 REPORT

Print report file (default=<true>). If REPORT is <true> an external file named CYL_<es_name>.<es_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

### 5.4.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH_CYL may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*procedure MH_CYL ( ES_MAME = EX47 ; --
    ES_PROC = ES1 ; --
    ES_PARS = 0 ; --
    SPAR_DIM ; --
    REPORT = <true>)
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,

> *call MH_CYL

This will perform a static, linear elastic analysis of the MacNeal/Harder thickwalled cylinder problem using the EX47 element in processor ES1. Results will be given for all three values of Poisson's Ratio. The datasets will be written into a library called MH_CYL.LO1, and the "report card" file named CYL_EX47.ES1 will be generated, Figure 5.4-3.


MACZEAL-HARDER 2-D THICK-HALLED CYLIMDER
ELEMENT TAKE $=$ EX47
ELEMENT PROCESSOR = ES1




Figure 5.4-3 "Report Card" using default arguments.
(E2) To perform an entire analysis using an ES element, invoke the procedure with the appropriate arguments, i.e.

$$
\begin{array}{cc}
\text { *call MH_CYL }(\text { ES_NAME }=\text { BR2O } & \text {; }-- \\
\text { ES_PROC }=\text { ES10 } & \text {;- } \\
\text { ES_PARS }=3,3 \\
\text { REPORT }=\text { <true }) & ;-- \\
\end{array}
$$

This will perform a static linear elastic analysis using the BR20 element, a 20-node brick element located in processor ES10. A report file will be generated named CYL_BR20.ES10.
(E3) To perform the analysis using a SPAR element, invoke the procedure using the appropriate arguments as follows:

```
*call MH_CYL ( ES_NAME = E43 ; --
    ES_PROC = SPAR ; --
    SPAR_DIM = 2 ; --
    REPORT = <true> )
```

This will perform the analysis using the SPAR E43 element and generate the "report card" file named CYL_E43. SPAR. Note that the argument SPAR_DIM must be defined when using a SPAR element.

### 5.4.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8-, 20-, and 32 -node solid elements.

### 5.4.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR_DIM is not set, the following error message will be printed and execution terminated.
The argument SPAR_DIM must be defined as 2 or 3 when using SPAR elements.
please set this argument and rerun.

### 5.4.7 PROCEDURE FLOWCHART

### 5.4.8 PROCEDURE LISTING

### 5.4.9 REFERENCES

5.4-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
5.4-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 5.5 Procedure MH_PATCH

### 5.5.1 GENERAL DESCRIPTION

### 5.5.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The patch test is used to test an element's ability to handle a state of constant strain with a distorted grid. This is a necessary condition to guarantee convergence of the solution.

### 5.5.1.2 Model Description

The patch test is modeled for both 2-D and 3-D elements. The 2-D model consists of 5 distorted quadrilateral elements forming a .24 by .12 inch rectangular plate of thickness one inch, Figure 5.5-1. The 3-D model consists of seven distorted hexagonal elements forming a one inch cube, Figure 5.5-2. Element corner node locations for both the 2-D and 3-D model are shown in Table 5.5-1. For all higher order elements (2-D - 9-node and 3-D 20- and 32node) the midedge nodes are placed equidistant from the corner nodes. However, for the 2-D 9-node model, a parameter called TWEEK has been added to allow the elements to have curved sides. See section 5.5 .3 for details. The 2-D patch test is actually two separate tests, the membrane patch test, and the bending patch test. However, the bending patch test is not currently implemented.
In the membrane patch test, displacements are applied according to the following formulas:

$$
\begin{aligned}
& u=10^{-3}(x+y / 2) \text { in. } \\
& v=10^{-3}(y+x / 2) \text { in. }
\end{aligned}
$$

yielding a state of constant strain.
For the bending patch test:

$$
\begin{aligned}
w & =10^{-3}\left(x^{2}+x y+y^{2}\right) / 2 \mathrm{in} \\
\theta_{x} & =\frac{\partial w}{\partial y}=10^{-3}(y+x / 2) \\
\theta_{y} & =-\frac{\partial w}{\partial x}=10^{-3}(-x-y / 2)
\end{aligned}
$$

yielding a state of constant curvature.
A state of constant strain is applied to the 3-D model according to the formulas:

$$
\begin{aligned}
u & =10^{-3}(2 x+y+z) / 2 \mathrm{in} \\
v & =10^{-3}(x+2 y+z) / 2 \mathrm{in} . \\
w & =10^{-3}(x+y+2 z) / 2 \mathrm{in} .
\end{aligned}
$$


a) 2-D model

b) 3-D model

Figure 5.5-1 MacNeal/Harder Patch Test

| NODE | 3-D Model |  |  | 2-D Model |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | X | Y | Z | X | Y |
| 1 | 0.000 | 0.000 | 0.000 | 0.00 | 0.00 |
| 2 | 1.000 | 0.000 | 0.000 | 0.24 | 0.00 |
| 3 | 0.000 | 1.000 | 0.000 | 0.04 | 0.02 |
| 4 | 1.000 | 1.000 | 0.000 | 0.18 | 0.03 |
| 5 | 0.249 | 0.342 | 0.192 | 0.24 | 0.12 |
| 6 | 0.826 | 0.288 | 0.288 | 0.16 | 0.08 |
| 7 | 0.273 | 0.750 | 0.230 | 0.00 | 0.12 |
| 8 | 0.850 | 0.649 | 0.263 | 0.08 | 0.08 |
| 9 | 0.320 | 0.186 | 0.643 |  |  |
| 10 | 0.677 | 0.305 | 0.683 |  |  |
| 11 | 0.165 | 0.745 | 0.702 |  |  |
| 12 | 0.788 | 0.693 | 0.644 |  |  |
| 13 | 0.000 | 0.000 | 1.000 |  |  |
| 14 | 0.000 | 0.000 | 1.000 |  |  |
| 15 | 0.000 | 1.000 | 1.000 |  |  |
| 16 | 1.000 | 1.000 | 1.000 |  |  |

Table 5.5-1 Element Corner Node Locations

### 5.5.1.3 Analysis Description

A static, linear elastic analysis is performed. Stresses are calculated and printed, as is specified by the user, at the integration points, centroids, and/or nodes. See section 5.5.2 for details.

### 5.5.1.4 Available Solutions

From reference 5.5-1, the exact solutions are as follows:
2-D Membrane Patch Test

$$
\begin{aligned}
\varepsilon_{x} & =\varepsilon_{y}=\gamma_{x y}=10^{-3} \\
\sigma_{x} & =\sigma_{y}=1333 p s i \\
\tau_{x y} & =400 p s i
\end{aligned}
$$

2-D Bending Patch Test

$$
\begin{aligned}
M_{x} & =M_{y}=1.111 \times 10^{-7} \mathrm{in} . l \mathrm{lb} . \\
M_{x y} & =10^{-7} \mathrm{in.lb} . \\
\sigma_{x} & =\sigma_{y}= \pm .667 \mathrm{psi} \\
\tau_{x y} & = \pm .200 \mathrm{psi}
\end{aligned}
$$

3-D Solid Patch Test

$$
\begin{aligned}
\varepsilon_{x} & =\varepsilon_{y}=\varepsilon_{z}=\gamma_{x y}=\gamma_{y z}=\gamma_{x x}=10^{-3} \\
\sigma_{x} & =\sigma_{y}=\sigma_{z}=2000 p s i \\
\tau_{x y} & =\tau_{y z}=\tau_{x z}=400 p s i
\end{aligned}
$$

### 5.5.2 PROCEDURE USAGE

Procedure MH_PATCH may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_PATCH ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH_PATCH are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| ES_PROC | ES1 | Element Processor |
| ES.NAME | EX47 | Element name |
| ES_PARS | 0. | Element research parameters |
| SPAR_DIM | none | 2-D or 3-D SPAR element |
| REPORT | <true> | Generate "report card" file |
| STR_ALL | <true> | Compute stresses at nodes, integration points, and centroids |
| STR_NODES | <false> | Compute stress at nodes |
| STR_INTPTS | <false> | Compute stress at integration points |
| STR_CENTS | <false> | Compute stress at centroids |
| TWEEK | 0,0,0,0 | Move midside nodes print stresses |
| DISPLAY | 1 | Print stresses |
| nodes | 1 | Stresses at nodes and centroids |
| CROSS | 1 | Stresses at top, mid, and bottom surfaces |

### 5.5.3 ARGUMENT DESCRIPTIONS

### 5.5.3.1 ES_NAME

Element name (default=EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.5-2).

### 5.5.3.2 ES_PROC

Element processor (default=ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

### 5.5.3.3 ES.PARS

Element research parameters (default=0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

### 5.5.3.4 SPAR_DIM

Number of dimensions of SPAR element (default=none). If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

### 5.5.3.5 REPORT

Print report file (default=<true>). If REPORT is <true> an external file named CYL_<es_name>.<es_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

## 5．5．3．6 STRALL

（default＝＜true＞）．If＜true＞stresses will be calculated at the element nodes，centroids， and integration points．If REPORT is＜true＞，stress values at all three locations will be printed in the report file．

## 5．5．3．7 STR＿MODES

（default＝＜false＞）．By setting this argument to＜true＞，STR＿ALL will be automatically reset to 〈false＞，and stresses will be calculated only at the nodes．If REPORT is＜true＞， stress values at the nodes will be printed in the report file．

## 5．5．3．8 STR＿INTPTS

（default＝〈false＞）．By setting this argument to＜true＞，STR＿ALL will be automatically reset to＜false〉，and stresses will be calculated only at the integration points．If REPORT is＜true＞，stress values at the integration points will be printed in the report file．

## 5．5．3．9 STR＿CENTS

（default＝〈false〉）．By setting this argument to＜true＞，STR＿ALL will be automatically reset to 〈false＞，and stresses will be calculated only at the centroids．If REPORT is ＜true＞，stress values at the centroids will be printed in the report file．

## 5．5．3．10 TNEEK

（default $=0 ., 0 ., 0 ., 0$. ）．The TWEEK parameters are used to offset the midside nodes on 9－node 2－D elements．This allows the user to test an element＇s sensitivity to curved edges．There are four TWEEK parameters that one separated by commas，with the location and positive direction shown in Figure 5．5－3．$=$

## 5．5．3．11 DISPLAY

（default＝1）．For SPAR elements only．For the various values of DISPLAY，the following will be printed in the report file：

For two－dimensional elements，
If DISPLAY $\quad=1$ ，stresses
$=2$ ，membrane stress resultants
$=3$ ，bending stress resultants
For three－dimensional solids（ $\mathrm{S} 41, \mathrm{~S} 61, \mathrm{~S} 81$ ），
$=1, \mathrm{x}, \mathrm{y}, \mathrm{z}$ stress components
relative to the element reference frame
$=2$ ，principal stresses
$=3$ ，octahedral normal stress（ONS）， octahedral shear stress（OSS），
stress intensity（SI）， and yield stress ratio（YSR）
$=4$ ，display of $S_{x z} / Y_{x x}, S_{y y} / Y_{y y}, S_{z z} / Y_{x z}$

### 5.5.3.12 MODES

(default=1). For SPAR elements only. This parameter controls whether results will be printed for the element centroids or the nodes as follows:

If NODES $\quad=0$, restrict printout to element center
$=1$, printout for each node and element center

### 5.5.3.13 CROSS

(default=1). For SPAR elements only. This parameter controls whether results are printed for the element mid-surface of top, mid and bottom surfaces as follows:

If CROSS $\quad=0$, restrict printout to mid-surface stresses
$=1$, printout for top, mid, and bottom surface stresses
Note: The parameters DISPLAY, NODES and CROSS are actually resets to processor PSF. See section 12.2 in reference 5.5-2 for details.


Figure 5.5-2 Location and positive direction of TWEEK parameters

### 5.5.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH_PATCH may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*procedure MH_PATCH ( ES_NAME = EX47 ; --
    ES_PROC = ES1 ; --
    ES_PARS =0 ; --
    SPAR_DIM ; --
    STR_ALL = <true> ; --
    STR_NODES = <false\rangle ; --
    STR_INTPTS = <false> ; --
    STR_CENTS = <false> ; --
    DISPLAY = 1 ; --
    NODES = 1 ; --
    CROSS = 1 ; --
    TWEEK = 0., 0., 0., 0.;;-
```

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call MH_PATCH
This will perform a static, linear elastic analysis of the MacNeal/Harder patch test using the EX47 element in processor ES1. Stresses will be calculated at nodes, centroids, and integration points and the results will be printed to a file named PATCH_EX47.ES1. The datasets will be written to a library named patch. 101 .
(E2) To perform an analysis using the BRO8 element in processor ES10 and generating stresses only at the integration points:

```
*call MH_PATCH ( ES_NAME = EX43 ; --
    ES_PROC = ES4 ; --
    STR_NODES = <true> ; --
    REPORT = <true>
```

The report file named PATCH_BR08.ES10 will be generated containing the stresses at the element integration points only, Figure 5.5-3.
(E3) To perform an analysis using a SPAR element, invoke the procedure using the appropriate arguments as follows:

```
*call MH_PATCH ( ES_NAME = E43 ; --
    ES_PROC = SPAR ; --
    SPAR_DIM = 2 ; --
    DISPLAY = 1 ; --
    MODES = 0 ; --
    CROSS =0 ; --
    REPORT = <true>
    j
```

The report file PATCH_E43.SPAR will be generated containing stresses (display=1) at the element centroid midsurface (nodes $=0$, cross=0). See reference $5.5-2$, section 12.2 for further information about the parameters display, nodes, and cross (they are actually resets to processor PSF). Note that SPAR_DIM must be defined when using a SPAR element.

```
##############################################################
#################################################################
                    MACMEAL-HARDER 2-D PATCH TEST
                    ELEMENT NAME = EX43
ELEMENT PROCESSOR = ES4
ELEMENT PARAMATERS= 0
```



Figure 5.5-3 "Report Card" using EX43 in ES4.

### 5.5.5 LIMITATIONS

(L1) This procedure can only evaluate 4 - and 9 -node 2 -D elements, and 8 -, 20 -, and 32 -node solid elements.
(L2) Currently only the 2-D membrane patch test and the 3-D test are operational.

### 5.5.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR_DIM is not set, the following error message will be printed and execution terminated.
The argument SPAR_DIM must be defined as 2 or 3 when using SPAR elements.
Please set this argument and rerun.

### 5.5.7 PROCEDURE FLOWCHART

### 5.5.8 PROCEDURE LISTING

### 5.5.9 REFERENCES

5.5-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
5.5-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 5.6 Procedure MH_PLATE

### 5.6.1 GENERAL DESCRIPTION

### 5.6.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The plate problem tests an element's ability to handle aspect ratio, thinness, and various types of loading and boundary conditions. The problem can be solved with 4 - or 9-node 2-D elements or 8 -node 3-D elements.

### 5.6.1.2 Model Description

Due to the symmetry of the physical problem a quarter model is used. Symmetry boundary conditions are applied at $\mathbf{x}=0$ and $\mathrm{y}=0$. At $\mathrm{x}=a$ and $\mathrm{y}=b$ two different boundary conditions are used - simply supported and clamped. Two different types of loading are applied - a central point load of $\mathbf{P}=4.0 \times 10^{-4} \mathrm{lbs}$. and a uniform pressure of $\mathbf{q}=10^{-4} \mathrm{psi}$. The value of $a$ is 1.0 in ., but, in order to test an element's sensitivity to aspect ratio, $b$ has two values, 1.0 in . and 5.0 in . The quarter plate is modeled with $N \times N$ elements. A mesh convergence study is done, with $N$ taking the value in Table 5.6-1. The two values of $b$ gives element aspect ratios of 1 and 5 . A typical model with $N=4$, material properties, and dimensions are shown in Figure 5.6-1.


Figure 5.6-1 Typical plate model, $N=4$

|  | 2-D Model |  | 3-D Model |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 4-node | 9-node | 8-node | 20-node |
| $\mathrm{N}=$ | 2 | 2 | 2 | 2 |
|  | 4 | 4 | 4 | 4 |
|  | 6 | 6 | 6 | 6 |
|  | 8 |  | 8 |  |

Table 5.6-1 Values of $N$ for different element types

### 5.6.1.3 Analysis Description

A static, linear elastic analysis is performed for each of the eight possible combinations of aspect ratio, loading, and boundary condition. Libraries named pl<aspect>_<grid>. 101 are created, where <aspect> is aspect ratio and <grid> is $N$, the mesh size. As the analysis proceeds, these libraries may be deleted by setting the argument DEL.LIB is <true>. If the argument REPORT is <true>, the normalized midplate displacements will be printed in an external "report file" named PLATE_<es_name>.<es_proc>, where <es_name> is the element name and <es_proc> is the element processor.

### 5.6.1.4 Available Solutions

From reference 5.6-1, the exact solutions for the mid-plate displacement in the direction of the load for each boundary condition, load type, and aspect ratio are shown in Table 5.6-2.

| Boundary <br> Condition | Aspect <br> Ratio b/a | Mid-plate displacement (inches) |  |
| :---: | :---: | :---: | :---: |
|  | Uniform Pressure | Point Load |  |
| Simple | 1.0 | 4.062 | 11.60 |
|  | 5.0 | 12.97 | 16.96 |
| Clamped | 1.0 | 1.26 | 5.60 |
|  | 5.0 | 2.56 | 7.23 |

Table 5.6-2 Theoretical tip displacements for each beam.

### 5.6.2 PROCEDURE USAGE

Procedure MH_PLATE may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_PLATE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and ? double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH_PLATE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument |  | Default Value |  | Meaning |
| :--- | :---: | :---: | :--- | :--- |
|  | 0. |  | Element research parameters |  |
| ES_PARS |  |  |  | Element Processor |
| ES_PROC | ES1 |  |  | Element name |
| ES_NAME | EX47 |  | none |  |
| SPAR_DIM | 2-D or 3-D SPAR element |  |  |  |
| DEL_LIB | <false> |  | Delete libraries |  |
| REPORT | <true> |  | Generate "report card" file |  |

### 5.6.3 ARGUMENT DESCRIPTIONS

### 5.6.3.1 ES_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

### 5.6.3.2 ES_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

### 5.6.3.3 ES_NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in the The Computational Structural Mechanics Testbed User's Manual (reference 5.6-2).

### 5.6.3.4 SPAR_DIM

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

### 5.6.3.5 DEL_LIB

As the mesh convergence study proceeds, DEL_LIB determines whether or not the individual libraries for each $N$ will be deleted. This allows disk space to be conserved if the analyst does not need the libraries.

### 5.6.3.6 REPORT

Print report file (default=<true>). If REPORT is <true> an external file named PLATE_<es_name>.<es_proc> will be generated. This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder.

### 5.6.4 USAGE GUIDELINES AND EXAMPLES

Procedure MH_PLATE may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an analysis using the default options, simply invoke the procedure without any arguments, i.e.,
*call Mh_PLATE
This will perform a static, linear elastic, analysis of the MH_PLATE problem. The normalized mid-plate displacements for all combinations of loading, boundary conditions, and aspect ratio will be calculated and printed in the report file named PLATE_EX47.ES1, Figure 5.6-2. Eight libraries named pl1_2.101, pl1.4.101, pl1_6.101, pl1 8.101, pl5_2.101, pl5_4.101, pl5_6.101, and pl5_8.101 will be generated. In a library named pla_N.101, $A$ is the aspect ratio and $N$ is the mesh. These eight libraries will not be deleted as the analysis proceeds, because the default value of DEL_LIB is 〈false〉.



Figure 5.6-2 Report file generated using default arguments.
(E2) To solve the MacNeal/Harder Plate problem with element E410 in processor ES5, deleting the libraries as the analysis proceeds, use the following call statement.

(E3) To perform the analysis using a SPAR element, invoke the procedure with the appropriate element name and SPAR for the processor. The argument SPAR_DIM must be defined when using a SPAR element. The libraries will be deleted as the analysis proceeds.


```
REPORT = 〈true> )
```


### 5.6.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8 -node solid elements.

### 5.6.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR_DIM is not set, the following error message will be printed and execution terminated.
The argument SPAR_DIM must be defined as 2 or 3 when using SPAR elements.
Please set this argument and rerun.

### 5.6.7 PROCEDURE FLOWCHART

### 5.6.8 PROCEDURE LISTING

### 5.6.9 REFERENCES

5.6-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
5.6-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 5.7 Procedure MH_SPHERE

### 5.7.1 GENERAL DESCRIPTION

### 5.7.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The spherical shell problem tests an element's ability to handle double curvature.

### 5.7.1.2 Model Description

The spherical shell is modeled for both 2-D and 3-D elements. As is shown in figure 5.7-1, it is a one-eighth model of a spherical shell with a $12^{\circ}$ hole in the top. The hole in the top of the sphere allows triangular (2-D) and wedge-shaped (3-D) elements to be avoided. The sphere is loaded by two point loads ( 1 lb . each) applied at centric points as is shown in figure 5.7-1. The sphere is modeled with $N \times N$ elements. A mesh convergence study is done with $N$ taking the values in table 5.7-1.


An example of a 2-D and a 3-D model are shown in figure 5.7-2.

### 5.7.1.3 Analysis Description

A static, linear elastic analysis is performed. Displacements at the point of, and in the direction of the loads are calculated, normalized with theoretical results, and printed for each value of $N$ (table 5.7-1).

### 5.7.1.4 Available Solutions

From reference 5.7-1, the exact theoretical solution for the displacement at the point of, and in the direction of the load is .0940 inches.

### 5.7.2 PROCEDURE USAGE

Procedure MH_SPHERE may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_SPHERE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH_SPHERE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument |  | Default Value |  | Meaning |
| :--- | :---: | :---: | :--- | :--- |
|  |  | ES1 |  | Element Processor |
| ES_PROC |  |  | EX47 |  |
| ES_NAME |  |  | Element name |  |
| ES_PARS |  |  | Element research parameters |  |
| SPAR_DIM |  | none |  | 2-D or 3-D SPAR element |
| REPORT | <true> |  | Generate "report card" file |  |
| DEL_IB | <false> |  | Delete libraries |  |

### 5.7.3 ARGUMENT DESCRIPTIONS

### 5.7.3.1 ES_NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in The Computational Structural Mechanics Testbed User's Manual (reference 5.7-2).

### 5.7.3.2 ES_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES_PROC should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

### 5.7.3.3 ES_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

## 5．7．3．4 SPAR＿DIM

If a SPAR element is used，this parameter must be set to the number of dimensions of that element．If ES elements are used，this parameter need not be set at all．

## 5．7．3．5 REPORT

Print report file（default＝＜true＞）．If REPORT is＜true＞an external file named CYL＿＜es＿name＞．＜es＿proc＞will be generated．This file contains the normalized radial displacements of the nodes at the inner radius of the cylinder．

## 5．7．3．6 DEL＿LIB

Delete libraries（default＝〈false〉）．As the mesh convergence study progresses，libraries named SPLN．L01 are generated，where $N$ is the number of elements along each edge of model．If DEL＿LIB is set to＜true＞，these libraries will be deleted during the analysis． This allows disk space to be conserved if the analyst does not need the libraries．

|  | 2－D Model |  | 3－D Model |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 4－node | 9－node | 8－node | 20－node |
|  | 2 | 1 | 4 | 2 |
|  | 4 | 2 | 8 | 4 |
|  | 6 | 3 | 12 | 6 |
|  | 8 | 4 |  |  |
|  | 10 | 5 |  |  |
|  | 12 | 6 |  |  |

Table 5．7－1 $N=$ number of elements for convergence study． Model is $N \times N$ ．

## 5．7．4 USAGE GUIDELINES AND EXAMPLES

Procedure MH＿SPHERE may be used by preceding the procedure name by the＊call directive． Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called．A space or blank is required between the end of the procedure name and the left parenthesis．
＊procedure MH＿SPHERE（ ES＿MAME＝EX47

| ES＿MAME $=$ EX47 | $;--$ |
| :--- | :--- |
| ES＿PROC $=$ ES1 | $;--$ |
| ES＿PARS $=0$ | $;--$ |
| SPAR＿DIM | $;--$ |
| DEL＿LIB $=\langle$ false〉 $;--$ |  |
| REPORT $=\langle$ true〉 |  |

（E1）To perform an entire analysis using the default options，simply invoke the procedure without any arguments，i．e．，

## *call MH_SPHERE

This will perform a static, linear elastic analysis of the MacNeal/Harder spherical shell using the EX47 element in processor ES1. The one-eighth sphere, modeled by $N \times N$ elements, will be analyzed with $N=2,4,6,8,10$, and 12 . Six libraries will be created, SPHN.L01, one for each value of $N$. If the argument DEL_LIB is <true>, these libraries will be automatically deleted as the analysis proceeds. If the argument REPORT is <true>, the normalized displacements at the point of, and in the direction of, the load will be printed in a report file named CYL_EX47.ES1 for each value of $N$, figure 5.7-3.


Figure 5.7-3 Report file generated using default arguments.
(E2) The following call statement will solve the spherical shell problem for the solid element EX20 in processor ES3. The libraries for each value of $N$ will be deleted.

```
*call MH_SPHERE ( ES_MAME = EX2O ; --
    ES_PROC = ES3 ; ;--
    REPORT = <true> )
```

(E3) To perform the analysis using a SPAR element, invoke the procedure using the appropriate 4-node 2-D element or 8-node 3-D element and SPAR for ES_PROC. Note that the argument SPAR_DIM must be defined when using a SPAR element.

```
*call MH_SPHERE ( ES_MAME = S81 ; ; --
    ES_PROC = SPAR ; ;--
    REPORT = <true> )
```


### 5.7.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8-and 20-node solid elements.

### 5.7.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR_DIM is not set, the following error message will be printed and execution terminated.
The argument SPAR_DIM must be defined as 2 or 3 when
using SPAR elements.
Please set this argument and rerun.

### 5.7.7 PROCEDURE FLOWCHART

### 5.7.8 PROCEDURE LISTING

### 5.7.9 REFERENCES

5.7-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
5.7-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 5.8 Procedure MH_ROOF

### 5.8.1 GENERAL DESCRIPTION

### 5.8.1.1 Problem Description

This application problem is another of the MacNeal/Harder Standard Test Problems. The Scordelis-Lo Roof problem tests an element's ability to handle single curvature and distributed gravity loading.

### 5.8.1.2 Model Description

The Scordelis-Lo Roof is modeled for both 2-D and 3-D elements. Due to symmetry, only one-fourth of the roof is modeled. Loading is applied to the roof in the form of a distributed gravity load equal to 90.0 pounds per square foot of surface area. For higherorder elements the load is applied using consistent loading concepts. The roof is modeled with $N \times N$ elements on the quarter model. A mesh convergence study is done with $N$ taking the values in Table 5.8-1. An example of a 2-D model, $\mathrm{N}=4$, is shown in Figure 5.8-1. Material properties, boundary conditions, and dimensions are also shown in Figure 5.8-1.


Figure 5.8-1 Example Scordelis-Lo Roof Model, $N=4$.

### 5.8.1.3 Analysis Description

A static, linear elastic analysis is performed. The $x$-direction displacement at the midside of free edge, point $A$ in Figure 5.8-1, is calculated, normalized with the theoretical result, and printed for each value of $N$ (Table 5.8-1).

### 5.8.1.4 Available Solutions

From reference 5.8-1, the theoretical solution for the displacement in the direction of the load at the midside of the free edge is .3024 inches.

### 5.8.2 PROCEDURE USAGE

Procedure MH_ROOF may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MH_ROOF ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (-) may be used to continue the argument list on the next line.

The allowable arguments for procedure MH_ROOF are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| ES_PROC | ES1 | Element Processor |
| ES MAME | EX47 | Element name |
| ES.PARS | 0. | Element research parameters |
| SPAR_DIM | none | 2-D or 3-D SPAR element |
| REPORT | <true> | Generate "report card" file |
| DELLIB | <false> | Delete libraries |

### 5.8.3 ARGUMENT DESCRIPTIONS

### 5.8.3.1 ES.NAME

Element name (default: EX47). This is the name of the element type you wish to select, within the element processor defined by argument ES_PROC. SPAR or ES elements may be used. The elements are described in the appropriate section in The Computational Structural Mechanics Testbed User's Manual (reference 5.8-2).

### 5.8.3.2 ES_PROC

Element processor (default: ES1). This is the name of the element processor that contains the element you wish to evaluate in this procedure. If a SPAR element is used, ES_proc should be set to SPAR. The element processors are described in The Computational Structural Mechanics Testbed User's Manual.

### 5.8.3.3 ES_PARS

Element research parameters (default: 0., ...). This is an optional list of elementdependent parameters that some elements provide, primarily when the element is still undergoing research and refinement.

### 5.8.3.4 SPAR_DIM

If a SPAR element is used, this parameter must be set to the number of dimensions of that element. If ES elements are used, this parameter need not be set at all.

### 5.8.3.5 REPORT

Print report file (default=<true>). If REPORT is <true> an external file named ROOF_<es_name>. <es_proc> will be generated. This file contains the normalized vertical displacement of the node at the midside of the free edge, point A in Figure 5.8-1.

### 5.8.3.6 DEL_LIB

Delete libraries (default=<false>). As the mesh convergence study progresses, libraries named ROOFN.L01 are generated, where $N$ is the number of elements along each edge of model. If DEL_LIB is set to <true>, these libraries will be deleted during the analysis. This allows disk space to be conserved if the analyst does not need the libraries.

|  | 2-D Model |  | 3-D Model |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 4-node | 9-node | 8-node | 20-node |
|  | 2 | 1 | 4 | 2 |
|  | 4 | 2 | 8 | 4 |
|  | 6 | 3 | 12 | 6 |
|  | 8 | 4 |  |  |
|  | 10 | 5 |  |  |
|  | 12 | 6 |  |  |

Table 5.8-1 $N=$ number of elements for convergence study. Model is $N \times N$.

### 5.8.4 USAGE GUIDELINES AND EXAMPLES

Procedure KH_ROOF may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

(E1) To perform an entire analysis using the default options, simply invoke the procedure without any arguments, i.e.,

*call MH_ROOF

This will perform a static, linear elastic analysis of the MacNeal/Harder ScordelisLo roof using the EX47 element in processor ES1. The one-fourth roof, modeled by $N \times N$ elements, will be analyzed with $N=2,4,6,8,10$, and 12 . Six libraries will be created, ROOFN.L01, one for each value of $N$. If the argument DEL_LIB is <true>, these libraries will be automatically deleted as the analysis proceeds. If the argument REPORT is <true>, the normalized displacements at the point of, and in the direction of, the load will be printed in a report file named ROOF_EX47.ES1 for each value of $N$, Figure 5.8-3.

```
###########################################################
###########################################################
MACNEAL-HARDER 2-D SCORDELIS-LO ROOF PROBLEM
    ELEMENT NAME = EX47
    ELEMENT PROCESSOR = ES1
    ELEMENT PARAMATERS = 0.
------------------
\begin{tabular}{ll} 
GRID \(=2\) & 1.1225 \\
GRID \(=4\) & 0.9703 \\
GRID \(=6\) & 0.9884 \\
GRID \(=8\) & 0.9941 \\
GRID \(=10\) & 0.9971 \\
GRID \(=12\) & 1.0000
\end{tabular}
\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#\#
```

Figure 5.8-3 Report file generated using default arguments.
(E2) The following call statement will solve the Scordelis-Lo roof problem for the solid element EX08 in processor ES3. The libraries for each value of $N$ will be deleted.

$$
\begin{aligned}
\text { *call MH_ROOF ( ES_MAME } & =\text { EX08 } & ;-- \\
\text { ES_PRDC } & =\text { ES3 } & ;- \\
\text { DEL_LIB } & =\text { <true> } & ;--
\end{aligned}
$$

```
REPORT = <true> )
```

(E3) To perform the analysis using a SPAR element, invoke the procedure using the appropriate 4-node 2-D element or 8-node 3-D element and SPAR for ES_PROC. Note that the argument SPAR_DIM must be defined when using a SPAR element.

```
*call MH_ROOF ( ES_NAME = S81
    ; --
    ES_PROC = SPAR ; --
    SPAR_DIM = 3 ; ;-
```


### 5.8.5 LIMITATIONS

(L1) This procedure can only evaluate 4- and 9-node 2-D elements, and 8- and 20-node solid elements.

### 5.8.6 ERROR MESSAGES AND WARNINGS

If a SPAR element is used, and the argument SPAR_DIM is not set, the following error message will be printed and execution terminated.

The argument SPAR_DIM must be defined as 2 or 3 when using SPAR elements.
Please set this argument and rerun.

### 5.8.7 PROCEDURE FLOWCHART

### 5.8.8 PROCEDURE LISTING

### 5.8.9 REFERENCES

5.8-1 MacNeal, R. H.; and Harder, R. L.: "A Proposed Set of Problems to Test Finite Element Accuracy," Finite Elements in Analysis and Design, Vol. 1, 1985, pp. 3-20.
5.8-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 5.9 Processor SKEWED_GRID

THIS SECTION UNDER PREPARATION

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### 6.0 Postprocessing Procedures

The procedures documented in this chapter are for postprocessing the results of a given computation. These procedures provide exampies of stress recovery and internal force calculations as well as examples for extracting selected data from the computational database.

A summary of the procedures found in this chapter is provided in Table 6.0-1.

Table 6.0-1 Solution Procedures

| Procedure Name | Description |
| :--- | :--- |
| HISTORY | Tabulate Response History in Database |
| POST | Tabulate Selected Results in Database |
| STRESS | Compute Stresses and/or Strains from Displacements |
| TOTAL_LOAD | Compute Total Load for Applied Displacement Prob- <br> lems |

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### 6.1 Procedure HISTORY

### 6.1.1 GENERAL DESCRIPTION

Procedure HISTORY is typically used to consolidate the response history of one or more nodes or elements into a database other than the database used for the analysis. The procedure allows for the extraction of a single nodal degree of freedom from one or more nodes. It also provides the means for extracting a single stress component from one or more elements.

### 6.1.2 PROCEDURE USAGE

Procedure HISTORY may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
*call HISTORY ( arg1 = val1 ; arg2 = val2 ; ...)
where arg1 and arg 2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure HISTORY are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure BISTORY, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| COMPONENT | -- | nodal dof or element stress component |
| ELEMENT_DS | -- | name of element-list dataset |
| ELEMENT_RN | -- | name of element-list record |
| ELEMENTS | -- | element numbers |
| INPUT-DS | -- | root name of input dataset |
| OUTPUT_DS | -- | full name of output dataset |
| OUTPUT_RN | -- | root name of output record |
| NODE_DS | -- | name of node-list dataset |
| NODE_RN | -- | name of node-list record |
| NODES | -- | node numbers |
| NUM_ELEMENTS | -- | number of elements to process |
| AVERAGE | <false> | average flag |
| INPUT_LDI | 1 | logical device index of input database |
| LOCATION | NODES | post nodal quantities |
| NUM_NODES | 1 | number of nodes to process |
| NUM_STEPS | 1 | number of steps |
| OUTPUT_LDI | 2 | logical device index of output database |
| STEPS | 0:0 | step numbers |
| SUM | <false> | summation flag (over nodes) |

### 6.1.3 ARGUMENT DESCRIPTIONS

### 6.1.3.1 AVERAGE

Average flag (default: <false>). If <true>, an average value for specified nodes or elements will be computed and saved in the database; otherwise individual nodal or elemental values are computed and saved.

### 6.1.3.2 INPUT_LDI

Logical device index of input database (default: 1).

### 6.1.3.3 LOCATION

Identifies location of data to be processed; either NODES or ELEMENTS (default: NODES).

### 6.1.3.4 NUM_NODES

Number of nodes to process (default: 1). This argument is a required argument only if LOCATION=NODES.

### 6.1.3.5 NUM_STEPS

Number of steps for historical data recovery (default: 1).

### 6.1.3.6 OUTPUT_LDI

Logical device index of output database (default: 2).

### 6.1.3.7 STEPS

Step numbers for historical data recovery (default: 0). This argument is an array of length NOM_STEPS. If the argument STEPS $=0$, the linear solution is used.

### 6.1.3.8 SUM

Flag to perform summation (default: <false>). If <true> the quantity of interest wil be summed over either the elements or nodes as specified by LOCATIONS. It is the summed (resultant) value is then saved in the database.

### 6.1.3.9 COMPONENT

Column of data to be extracted. When LOCATION=NODES (e.g., COMPONENT=1 corresponds to $u$-direction displacement). When LOCATION=ELEMENT, COMPONENT is typically a stress resultant (e.g., COMPONENT $=1$ corresponds to $N_{x}$ ). This argument is always required.

### 6.1.3.10 ELEMENT_DS

Name of dataset containing list of elements to be processed. This argument is an active argument only if LOCATION=ELEMENTS.

### 6.1.3.11 ELEMENT_RN

Name of element-list record. This argument is an active argument only if LOCATION=ELEMENTS.

### 6.1.3.12 ELEMENTS

Element numbers to extract historical data. The argument ELEMENTS is an array of length NOM ELEMENTS that lists the element numbers for which historical data are extracted. This is an active argument only if LOCATION=ELEMENTS. Element numbers may be input either through the ELEMENTS argument or through a dataset containing the list (i.e., using the ELEMENTS_DS and ELEMENT_RN arguments.

### 6.1.3.13 INPUT.DS

Root name (i.e., first two words) of source dataset. This argument is always required.

### 6.1.3.14 OUTPUT_DS

Root name (i.e., first two words) of destination dataset. This argument is always required. The dataset is written one record per step per element for LOCATION=ELEMENTS or one record per step per node for LOCATION=NODES.

### 6.1.3.15 OUTPUT_RN

Root name (i.e., first word) of destination record. This argument is always required.

### 6.1.3.16 NODE_DS

Name of dataset containing list of nodes to be processed. This argument is an active argument only if LOCATION=NODES.

### 6.1.3.17 NODE_RN

Name of node-list record. This argument is an active argument only if LOCATION=NODES.

### 6.1.3.18 MODES

Node numbers to extract historical data. The argument NODES is an array of length NOM NODES that lists the node numbers for which historical data are extracted. This is an active argument only if LOCATION=NODES. Node numbers may be input either through the NODES argument or through a dataset containing the list (i.e., using the NODE_DS and NODE_RN arguments).

### 6.1.3.19 NOM_ELEMENTS

Number of elements to extract historical data. The argument NOM_ELEMENTS specifies the number of elements from which historical data are extracted. This is a required argument only if LOCATION=ELEMENTS.

### 6.1.4 USAGE GUIDELINES AND EXAMPLES

Procedure HISTORY may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*procedure HISTORY ( input_ldi = 1 ; -- . Idi of input database
    input_ds ; -- . root name of input dataset
    output_ldi = 2 ; -- . Idi of output database
    output_ds ; -- . full name of output dataset
    output_rn ; -- . root name of output record
    location = NODES ; -- . post nodal quantities
    num_steps = 1 ; -- . number of steps
    steps = 0:0; -- . step numbers
    num_nodes = 1;-- . number of nodes to process
    nodes ; -- . node numbers
    component ; -- . nodal dof or element stress
    sum = \langlefalse\rangle ; -- . summation flag (over nodes)
    average = \langlefalse\rangle ; -- . average flag
    node_ds ; -- . name of node-list dataset
```

```
node_rn ; -- . name of node-list record
element_ds ; -- . name of element-list dataset
element_rn ; -- . name of element-list record
num_elements ; -- : number of elements to process
elements -- . element numbers)
```


### 6.1.5 LIMITATIONS

Due to a restriction on the number of active macrosymbols, no more than 700 nodes or elements may be processed using NODE_DS or ELEMENT_DS.

Procedure HISTORY should be used only to process limited amounts of data due to the procedure's inherent inefficiency. Except for small problems, the SUM argument should not be used to perform summation over the nodes for multiple load steps. In most cases this operation should be performed using the TOTAL_LOAD procedure (see Section 6.5).

### 6.1.6 ERROR MESSAGES AND WARNINGS

None.

### 6.1.7 PROCEDURE FLOWCHART

### 6.1.8 PROCEDURE LISTING

```
*procedure 目STORY ( input_ldi = 1 ; -- . ldi of input database
    input_ds ; -- . root name of input dataset
    output_ldi = 2 ; -- . ldi of output database
    output_ds ; -- . full name of output dataset
    output_rn ; -- . root nane of output record
    location = NODES ; -- . post nodal quantities
    num_steps = 1 ; -- . number of steps
    steps =0:0; -- . step numbers
    num_nodes = 1 ; -- . number of nodes to process
    nodes ; -- . node numbers
    component ; -- . nodal dof or elenent stress
    sum = <false\rangle ; -- . summation flag (over nodes)
    average m <false> ; -- . average flag
    node_ds ; -- . name of node-list dataset
    node_rn ; -- . name of node-list record
    elerent_ds ; -- . name of elenent-list dataset
    element_rn ; -- . name of element-list record
    num_elements ; -- . number of elenents to process
    elements -- . element numbers
    )
```

- Procedure to Postprocess Response History from/to Database

```
*def/i steps[1:[num_steps]] = [steps]
*if < <IPELSE([LOCATION];NODES;1;0)> >/then
        *if < <IFELSE([node_ds]; ;1;0)> > /then
            *def/i num_nodes = [num_nodes]
            *def/i nodes[1:<num_nodes>] == [nodes]
        *else
            *find record [input_ldi], [node_ds], [node_rn] /nor=num_nodes
            *g2n /namex=nodes /typexi /maxn=<num_nodes> [input_ldi] [node_ds] --
                    [node_rn].1:<num_nodes>
        *endif
        [xgT VEC
        *find dataset [output_ldi] [output_ds] /seq=ids
        *if <<ide> /1e 0 > /thon
            *put dataset [output_ldi] [output_ds] /arat=2000 /seq=ids
        *endif
        *do &is x 1, [num_steps]
            *dof/i step_num = <steps[<$is>]>
            *ind dataset [input_ldi] [input_ds].<step_num>/seq=hist_ids
            *if < <hist_ids> /1. 0 >/thon
                *renark
                *ronark Dataset [input_ds].<step_num> not found by HISTORY
                    *renark
                    *roturn
            *ondif
            *if < [sum] /or [average] > /then
                *def/Q resultant = 0.0
            *endif
            *do &in = 1, <num_nodes>
                *def/i node_num = <nodes[<$in>]>
            COMPONENT <node_num> [component] [input_ds].<step_nun> -> val
                *if < [sum] /or [average] > /then
                    *def/e resultant = < <resultant\rangle + \langleval\rangle >
                    *else
                        *m2g/name=val /type=d [output_ldi] <ids> --
                            [output_rn].<step_num>
                *ondif
            *onddo
            *if < [sua] /or [average] > /then
                *if < [average] > /then
                    *dof/e resultant = < <resultant> / <num_nodos>>
                    *endif
                    *mgg/namerresultant /type=d [output_ldi] <ids> --
                    [output_rn].<step_num>
                *endif
        *enddo
    *elseif < <IFELSE([LOCATION];ELEMENTS;1;0)>> /then
        *if <<IFELSE([element_ds]; ;1;0)>> /then
            *dof/i num_elenents = [num_eloments]
            *def/i elements[1:<num_elexents>] == [elements]
        *else
            *find record [input_ldi], [element_ds], [element_rn] --
```

```
                                    /nor=num_eloments
        *g2m /name=elements /type=i /maxn=<num_elements> [input_ldi] --
            [element_ds] [element_rn].1:<num_elements>
        *endif
        [xqT vEC
        *do $is = 1, [num_steps]
            *def/i step_num = <steps[<$is>]>
            *find dataset [input_ldi] [input_ds].<step_num> /seq=hist_ids
            *if < <hist_ids> /le 0 > /then
                *ronark
                *ronark Datasot [input_ds].<stop_nus> not found by BISTORY
                *renark
                *retura
            *endif
            *if < [sum] /or [average] > /then
                *dof/* resultant = 0.0
            *endif
            *do $in = 1, <num_elenents>
                    *def/i element_num = <elements[<$in>]>
            COMPONENT <element_num> [conponent] [input_ds].<step_nus> -> val
                    *if < [sum] /or [average] > /then
                    *dei/Q resultant = < <resultant\rangle + \langleval\rangle >
                    *else
                    *n2g /naze=val /type=d [output_ldi] [output_ds] --
                    [output_rn].<stop_num>
                    *ondif
        *onddo
        *if < [sum] /or [average] > /then
            *if < [average] > /thon
                    *def/e resultant = < <resultant> / <num_elenents> >
            *ondif
            *n2g /namesresultant /type=d [output_ldi] [output_ds] --
                    [output_rn].<step_num>
        *ondif
        **nddo
    *ondif
*ond
```


### 6.1.9 REFERENCES

6.1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
6.1-2 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

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### 6.2 Procedure POST

### 6.2.1 GENERAL DESCRIPTION

Procedure POST is used to extract the response history of one or more nodes from one database and to consolidate it into another database. This procedure differs from procedure HISTORY in that POST cannot operate on element data (e.g., element stress resultants).

### 6.2.2 PROCEDURE USAGE

Procedure POST may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call POST ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure POST are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure POST, the following table lists each argument, its default value and meaning.

| Parameter | Default Value | Meaning |
| :---: | :---: | :---: |
| DOF | -- | Nodal degree of freedom index |
| INPUT.DS | -- | Root name of input dataset |
| NODES | -- | Node numbers |
| NODES_DS | -- | Name of node-list input dataset |
| NODES_RN | -- | Name of node-list input record |
| OUTPUT_DS | -- | Full name of output dataset |
| OUTPUT_RN | -- | Root name of output record |
| INPUT_LDI | 1 | Logical device index of input database |
| OUTPUT_LDI | 1 | Logical device index of output database |
| NSTEPS | 1 | Number of steps |
| STEPS | 0:0 | Step numbers |
| NNODES | 1 | Number of nodes to process |
| SUT | <false> | Summation flag (over node list) |

### 6.2.3 ARGUMENT DESCRIPTIONS

### 6.2.3.1 INPUT_LDI

Logical device index of input database (default: 1).

### 6.2.3.2 OUTPUT_LDI

Logical device index of output database (default: 1).

### 6.2.3.3 NSTEPS

Number of steps for historical data recovery (default: 1).

### 6.2.3.4 STEPS

Step numbers for historical data recovery (default: 0 ). This argument is an array of length NUM_STEPS. If the argument STEPS $=0$, the linear solution is used.

### 6.2.3.5 NNODES

Number of nodes to process (default: 1).

### 6.2.3.6 SUM

Flag to sum over nodes (default: <false>). If the argument SUM=<true>, the summation and not the nodal values will be saved in the database.

### 6.2.3.7 DOF

Nodal degree of freedom index (i.e., $1,2,3,4,5$, or 6 ).

### 6.2.3.8 INPUT.DS

Root name (first two words) of source dataset. This argument is mandatory.

### 6.2.3.9 NODES

Node numbers for which historical data are extracted. The argument NODES is an array of length NODES. Node numbers may be input either through the MODES argument or through a dataset containing the list (i.e., using the NODES_DS and YODES_RN arguments).

### 6.2.3.10 NODES_DS

Name of dataset containing list of nodes to be processed.

### 6.2.3.11 NODES_RN

Name of node-list record.

### 6.2.3.12 OUTPUT_DS

Root name (i.e., first two words) of destination dataset. This argument is mandatory. The dataset is written one record per step per node.

### 6.2.3.13 OUTPUT_RN

Root name (i.e., first word) of destination record. This argument is mandatory.

### 6.2.4 USAGE GUIDELINES AND EXAMPLES

Procedure POST may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call POST ( input_ldi = 1 ; -- . ldi of input database
        input_ds ; -- . root name of input dataset
        output_ldi = 1 ; -- . ldi of output database
        output_ds ; -- . full name of output dataset
        output_rn ; -- . root name of output record
        nsteps = 1 ; -- . number of steps
        steps =0:0; -- . step numbers
        nnodes = 1 ; -- . number of nodes to process
        nodes ; -- . node numbers
        dof ; -- . nodal degree of freedom index
        sum = \langlefalse\rangle ; -- . summation flag (over node list)
        nodes_ds ; -- . [name of node-1ist input dataset]
        nodes_rn -- . [name of node-list input record])
```


### 6.2.5 LIMITATIONS

Due to a restriction on the number of active macrosymbols, no more than 700 nodes should be processed using NODE_DS and NODE_RN.

### 6.2.6 ERROR MESSAGES AND WARNINGS

None.

### 6.2.7 PROCEDURE FLOWCHART

Procedure POST is self-contained and has no subprocedures.

### 6.2.8 PROCEDURE LISTING

```
*procedure POST ( input_ldi = 1 ; -- . ldi of input database
    input_ds ; -- . root name of input dataset
    output_ldi = 1 ; -- . ldi of output database
    output_ds ; -- . Iull name of output dateset
    output_rn ; -- . root neme of output record
    nsteps = 1 ; -- . number of steps
    steps= 0:0; -- . step numbers
    nnodes = 1 ; -- . number of nodes to process
    nodes ; -- . node numbers
    do1 ; -- . nodal degree of freedon index
    sun = <false\rangle ; -- . sumation flag (over node list)
    nodes_ds ; -- . [name of node-list input dataset]
    nodes_rn -- . [nane of node-list input record]
    )
- CLAMP Procedure to Post Hesponse History in a Databese
    *def/i steps[1:[nsteps]] = [steps]
    *if < <IFELSE([nodes_ds]; ;1;0)>>/then
        *def/i nnodes m [nnodes]
        *def/i nodes[1:<nnodes>] = [nodes]
    *else
        *ind record [input_ldi], [nodes_ds], [nodes_rn] /nor=nnodes
        *do $in = 1, <nnodes>
            *g2m /namesnodes[<&in>] /type=i [input_ldi] [nodes_ds] --
                [nodes_rn].<$in>
        *enddo
        *ondif
    [XQT VEC
    *ind dataset [output_ldi] [output_ds] /seqsids
    *il < <ids>/le 0 >/then
        *put dateset [output_ldi] [output_ds] /Erat=2000 /seqzids
    *endif
    *do $is = 1, [neteps]
        *def/i step_num = <Eteps[<$is>]>
        *i1 < [sun]>/then
            *def/e resultant = 0.0
        *endif
        *do &in = 1, <nnodes>
            *def/i node_num = <nodes[<<in\rangle]>
                COMPONENT <node_num> [dof] [input_ds].<step_nue> -> value
            *if < [sum]>/then
                *def/e resultant = <<resultant> + \langlevalue\rangle>
            *else
                *m2g/nanesvalue /type=d [output_ldi] [output_ds] --
                    [output_rn]_\langlenode_num>.\langlestep_num>
            *endif
        *enddo
        *if < [sum]>/then
```

*m2g /naneseresultant /type=d [output_ldi] [output_ds] -[output_rn].<step_num>
*ondif
*enddo
*ond

### 6.2.9 REFERENCES

6.2-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
6.2-2 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

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### 6.3 Procedure STRESS

### 6.3.1 GENERAL DESCRIPTION

Procedure STRESS drives the calculation of stress resultant and strain component datasets for either linear or nonlinear analyses. The user may select recovery of stress resultants or strain components at element centroids, element nodes, element integration points or at all three locations.

### 6.3.2 PROCEDURE USAGE

Procedure STRESS may be used by preceding the procedure name by the *call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

> *call STRESS ( arg1 = val1 ; arg2 = val2 ; ...)

For procedure STRESS, the following table lists each argument, its default value and meaning.

| Argument | Default Value |  | Meaning |
| :--- | :---: | :---: | :--- |
| CONS_SET | 1 |  | Constraint set number |
| COROTATION | 1 |  | Corotational flag (0=OFF, 1=ON) |
| DIM | 2 |  | Intrinsic element spatial dimension (2=2D, 3=3D) |
| DIRECTION | 1 |  | Direction for element stress and strain recovery |
| DISP_DS | STAT.DISP | First two words of displacement dataset name |  |
| LOAD_SET | 1 |  | Load set number |
| LOCATION | NODES | Location of the evaluation points for element stresses |  |
| NL_GEOM | 0 |  | Geometric nonlinearity flag |
| NOM_STEPS | 1 |  | Total number of steps requiring stress calculations |
| NVAL_METH | 3 |  | Method to be used for global smoothing |
| PRINT | <false> |  | Flag to print computed results |
| ROTN_DS | STAT.ROTM | First two words of rotation-vector dataset name |  |
| SMOOTH | <false> | Flag to compute smoothed global stresses |  |
| STEPS | 0 |  | Step numbers |
| STRAIN | <false> | Flag to compute element strains |  |
| STRESS | <true> | Flag to compute element stresses |  |

Tables 6.3-1, 6.3-2, and 6.3-3 list the datasets used or created by procedure STRESS, the procedures invoked by procedure STRESS, and the processors invoked by procedure STRESS, respectively.

| Dataset |  | Description | Lib | Input | Output |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ESSSUMMARY |  | ES Processor Status | 1 | $\checkmark$ | $\sqrt{ }$ |
| PROP.BTAB.* |  | Material/Section Properties | 1 | $\checkmark$ |  |
| STAT.DISP.i.j $\dagger$ |  | System Displacement Vector | 1 |  | $\sqrt{ }$ |
| STRS. $<E S$ NAM | $E>. i . j \dagger=$ | Element Stresses | 1 |  | $\sqrt{ }$ |
| $\dagger i=<$ load_set> and $j=$ <cons_set> |  |  |  |  |  |
| Table 6.3-2 Sub-Procedures Invoked by procedure STRESS |  |  |  |  |  |
| Procedure | Type | Function |  |  |  |
| ES | External | Element utility procedure |  |  |  |
| STRESS | Internal | Computes element stresses |  |  |  |


| Table 6.3-3 Processors Invoked by procedure STRESS |  |  |
| :--- | :--- | :--- |
| Procedure | Type | Function |
| ES $i$ | External | Element processors based on GEP |
| NVAL | Internal | Perform global smoothing |
| PESR | Internal | Print element stresses |
| PNSR | Internal | Print nodal stresses |

### 6.3.3 ARGUMENT DESCRIPTIONS

### 6.3.3.1 CONS_SET

Constraint set number (default: 1). This argument selects which constraint set to use in solving the linear system of equations.

### 6.3.3.2 COROTATION

Corotational update switch for large-rotation problems (default: <true>). This switch should be set to 〈true〉 when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element processor (ESi) section in the CSM Testbed User's Manual (see ref. 6.3-1) for specific guidelines.

### 6.3.3.3 DIM

Intrinsic element spatial dimension (default: 2). This argument selects the element spatial dimension: 2 for a two-dimensional element or 3 for a three-dimensional solid element.

### 6.3.3.4 DIRECTION

Direction for the element stress (stress resultant) output (default: 1). The element stress coordinate system will be used if DIRECTION $=0$. The material axes ( $x_{m}, y_{m}, z_{m}$ ) will be used if DIRECTION $=1$; the material axes ( $y_{m}, z_{m}, x_{m}$ ) will be used for DIRECTION $=2$; and the material axes ( $z_{m}, x_{m}, y_{m}$ ) will be used for DIRECTION $=3$. For isotropic materials, the first material axis is replaced by the corresponding global axis (see Section 4.3.3.9 of the CSM Testbed User's Manual, ref. 6.3-1).

### 6.3.3.5 DISP_DS

First two words of the dataset name for the displacement solution (default: STAT.DISP).

### 6.3.3.6 LOAD_SET

Load set number (default: 1). This argument selects which load set to use as a right-hand side vector.

### 6.3.3.7 LOCATION

Location of the evaluation points for the element stresses or stress resultants (default: NODES). The element stresses or stress resultants are optionally computed. This argument may have four values. For LOCATION=INTEG_PTS, the element stresses are computed at the element integration points. For LOCATION=CENTROIDS, the element stresses are computed at the element centroid. For LOCATION=NODES, the element stresses are extrapolated from the integration points to be element nodes. These element nodal stresses will be discontinuous across interelement boundaries. For LOCATION=ALL, the element stresses are computed at the element integration points, element centroid, and element nodes.

### 6.3.3.8 NL_GEOM

Geometric nonlinearity level: 0,1 , or 2 (default $=2$ ). A value of zero means that the problem is geometrically linear; a value of one means that the geometric nonlinearity will be handled globally (i.e., using corotational updates only); and a value of two means that
the nonlinear element strain-displacement relations will be used in addition to any global treatment of geometric nonlinearity. If COROTATION = <true>, options 1 and 2 refer to first-order and second-order corotation, respectively. The latter option can be significantly more accurate than the former for a given finite element model - depending on which element types are involved.

### 6.3.3.9 NOM_STEPS

Number of steps for stress recovery (default: 1).

### 6.3.3.10 NVAL_METH

Select method to be used for computing the smoothed global stresses (default: 3). Processor NVAL is used to compute the smoothed global stresses using the method defined by the argument NVAL_METH (see Section 12.5 of reference 6.3-1). If NVAL_METH=1, a topological interpolation of the element centroidal stresses is performed, and the element stresses must have been computed using LOCATION=CENTROIDS. If NVAL_METH=2, a projected least-squares interpolation of the element centroidal stresses is performed, and the stresses must have been computed using LOCATION=CENTROIDS. If NVAL_METH=3, the element nodal stresses (discontinuous across interelement boundaries) are averaged, and the element stresses must have been computed using LOCATION=NODES. Using LOCATION=ALL will generate element stresses at the element centroids, element nodes, and element gauss points. Acceptable values of location for specific values of NVAL_METH are as follows:

| NVAL_METH | Location |
| :---: | :---: |
| 1 | CENTROIDS, ALL |
| 2 | CENTROIDS, ALL |
| 3 | NODES, ALL |

### 6.3.3.11 PRINT

Flag to print computed results (default: <false>). If the argument PRINT=<true>, then the element stresses and/or nodal stresses will be printed.

### 6.3.3.12 ROTN_DS

First two words of the dataset name for the rotation solution (default: STAT.ROTN).

### 6.3.3.13 SMOOTH

Flag to compute smoothed global stresses (default: 〈false>). If the argument SMOOTH=<true>, then smoothed global stresses will be computed by processor NVAL using the method defined by the argument NVAL_METH.

### 6.3.3.14 STEPS

Step numbers for stress recovery (default: 0). This argument is an array of length NUM_STEPS. If the argument STEPS $=0$, the linear solution is used.

### 6.3.3.15 STRAIN

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRATN=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION.

### 6.3.3.16 STRESS

Flag to compute element stresses or stress resultants (default: <false>). If the argument STRESS=<true>, then the element stresses will be computed at the location and in the direction specified by the arguments LOCATION and DIRECTION.

### 6.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure STRESS may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call STRESS ( STRESS = <true\rangle ; --
    STRAIN = \langlefalse\rangle; ;--
    LOCATION = CENTROIDS ; --
    DIRECTION = 0 ; --
    NL_GEOM = 0 ; --
    CORO = 1 ; --
    LOAD_SET = 1 ; --
    CONS_SET = 1 ; --
    NUM_STEPS = 1 ; --
    PRINT = <false\rangle; --
    NVAL_METH = 3;--
    SMOOTH = <false\rangle; --
    DIM = 2 ; --
    STEPS = 0; --
    DISP_DS = STAT.DISP ; --
    ROTN_DS = STAT.RDTN )
```


### 6.3.5 LIMITATIONS

Applicable only to elements implemented using the generic element processor template. Procedure STRESS assumes that all datasets either required or generated reside on library one ( $\mathrm{LDI}=1$ ).

### 6.3.6 ERROR MESSAGES AND WARNINGS

An error message is printed and global stress smoothing will not be performed if the values of nVAL_METH and LOCATION are inconsistent. Processing of element data will continue. See Section 12.5 of reference 6.3-1 for usage of processor NVAL.

### 6.3.7 PROCEDURE FLOWCHART

| STRESS | (main procedure) |
| ---: | :--- |
| ES | (calculate element stresses and/or strains) |

### 6.3.8 PROCEDURE LISTING

```
*procedure STRESS ( STRESS = <true> ; --
    STRAIN = <false\rangle ; --
    LOCATION = CENTROIDS ; --
    DIRECTION = 0 ; --
    NL_GEOM = 0 ; --
    colo = 1 ;printx<false>; --
    LOAD_SET = 1 ; --
    CONS_SET = 1 ; --
    NOM_STEPS = 1 ; --
    SMOOTH = <false>; NVAL_METH = 3; --
    DIM = 2; --
    STEPS = 0 ; --
    DISP_DS = STAT.DISP ; --
    ROTN_DS = STAT.ROTN --
    )
```



```
*remark STRESS RECOVERY
```



```
--------------------------
- Loop on Solution Steps
    *def/i steps[1:[num_steps]] = [steps]
    *do $is = 1, [num_stops]
        *def/i istop = <steps[<$1s>]>
        *if <<istep>/ne 0>/then
            *det/a DS_SFX = <istep>
            *else
            *det/a DS_SFX = [load_set].[cons_set]
        *endif
*if < <[STRAIN] /ne <false>> /or <[STRESS] /ne <false>> > /then
. Define Elezent Stress/Strain Option and Dataset Names
```

```
*if < <[STRAIN] /eq <true>> /and <[STRESS] /eq <falso>> > /thon
    *def/p function = 'FORM STRAIN'
    *det/a STRAIN_DS = <DS_SFX>
    *def/a STRESS_DS = ',
*olseif < <[STRAIN] /eq <true>> /and <[STRESS] /eq <true>>> /then
    *def/p function = 'FORH STRESS'
    *dof/a STRATN_DS = <DS_SPX>
    *dof/a STRESS_DS = <DS_SPX>
*0lsoif < <[STRAIN] /eq <false>> /and <[STRESS] /eq <true>>> /then
    *def/p function = 'FORM STAESS'
    *dof/a STRAIN_DS = , ,
    *dof/a STRESS_DS = <DS_SFX>
*endif
- Invoke Element Processors to Form Stress/Strain
    *if < ifeqs( [location];ALL) > /then
C Calculate the stresses/strains at slement nodes, controids,
- and gauss points
*do $iloc = 1,3
    *if < ifeqs( <$iloc>;1) > /then
        *def/a location = CENTROIDS
        *elseif < ifeqs( <$iloc>;2) > /then
        *def/a location = NODES
        *elseif < ifeqs( <$iloc>;3) >/then
        *def/a location = INTEG_PTS
    *endif
        *call ES ( function = <function>
                03_nl_geon = [nl_geon] ; --
                es_coro = [coro] ; --
                \bullets_dis_ds = [DISP_DS].<DS_SFX> ; --
                es_rot_ds = [ROTN_DS].<DS_SFX> ; --
                es_str_dir = [DIRECTION] ; --
                es_str_loc = <location> ; --
                es_strain_ds = <strain_ds> ; --
                es_stress_ds = <stress_ds\rangle )
*enddo
        *olse
        Calculate the stresses/strains only at [LOCATIOK]
    *call ES ( function = <function> ; --
        0n_nl_geon = [nl_geon] ; --
        es_coro = [coro] ; --
        0s_dis_ds = [DISP_DS].<DS_SFX> ; --
        es_rot_d: = [ROTN_DS].<DS_SFX> ; --
        es_str_dir = [DIRECTION] ; --
        es_str_loc = [LOCATION] ; --
        es_strain_ds = <strain_ds> ; --
        es_stress_ds = <stress_ds> )
    *endif
```

```
- Print the Element Stresses
    *if < [print] >/then
    *if < ifeqs([location];ALL) > /then
            *def/i strese_loc = 0
    *elseif < ifeqs([location];CENTROIDS) > /then
            *dof/i stress_loc = 1
    *olseif < ifeqs([location];NODES) > /then
    *def/i stress_loc = 2
    *&lseif < ifeqs([location];INTEG_PTS) > /then
            *def/i stresz_loc = 3
    *endif
    [xqt pesr
        SELECT /global=[direction] /LOCATION=<stress_loc>
        *if <<istep> /eq 0>/then
        PRINT /LOAD_SET=[load_set] /CONSTRAINT=[cons_set]
        *else
        PRINT /LOAD_SET=<istep> /CONSTRAINT=0
        *endif
        STOP
    *endif
*ondif
- Calculate nodal stresses using processor NVAL
*if < [SMOOTH] > /thon
    *if < ifeqs( [LOCATION];ALL) >/then
    *elsoif /then < <[NVAL_HETH] /eq 3> /and --
                        <ifeq:([LOCATION];NODES)> >
    *elsoif /thon < <[NVAL_METH] /ne 3> /and --
                        <ifeqs([LOCATION];CEMTROIDS)> >
    *else
    *renark ************ERROR MESSAGE*******************
    *renark Stress evaluation point not consistent with
    *renark stress moothing method selected.
    *remark ********************************************
    *jump :EXIT
    *endif
    *def/a STRS = STRS.<es_nane>.<stress_ds>
    [xqt WVAL
        reset moth=[NVAL_METH], DIM=[DIM], DS=\langleSTRS>
        resot firsta1, last=<es_nstr>
        *if < [NVAL_METH] /oq 3 >/then
        *def/a REC = MODES_S[direction]
        *else
        *def/a REC = CENTROIDS_S[direction]
        *endif
        reset mECNAKE=<REC>
        STOP
    Print the Nodal Stresses
```

```
    *if < [print] > /thon
    [xqt pner
        *if < <istep>/*q 0 > /thon
        PRINT /loadx[load_set] /constraint=[cons_set] /nethod=[nval_meth]
        *0lse
        PRINT /load=<istep> /constraint=0 /method=[nval_meth]
        *andif
        STOP
        :EXIT
    *endif
*ondif
*onddo
* and
```


### 6.3.9 REFERENCES

6.3-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 6.4 Procedure TOTAL_LOAD

### 6.4.1 GENERAL DESCRIPTION

Procedure TOTAL_LOAD sums the reaction forces to determine the total applied load for problems with applied displacements for either linear or nonlinear analyses. The computed total load may be divided by a constant and scaled by a second constant.

### 6.4.2 PROCEDURE USAGE

Procedure TOTAL_Load may be used by preceding the procedure name by the *call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows (see example usage in Section 6.4.4):

```
*call TOTALLLOAD ( arg1 = val1 ; arg2 = val2 ; ...)
```

For procedure TOTAL_LOAD, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| INPUT_LDI | 1 | Input library number |
| OUTPUT_LDI | 1 | Output library number |
| NL_RESLDI | 3 | Library containing nonlinear results dataset |
| LOAD_SET | 1 | Load set number |
| CONS_SET | 1 | Constraint set number |
| NSTEPS | 0 | Total number of load steps to be processed |
| BEGIN_STEP | 1 | First load step to be processed |
| END_STEP | -1 | Last load step to be processed |
| LD_DIR | 1 | Load direction |
| EQUIL_CK | 0 | Flag enabling an equilibrium check |
| EA | 1.0 | Scaling constant |
| FAC | 2.0 | Scaling constant |
| NAME1 | 'STAT' | First word of input dataset name |
| NAME2 | 'REAC' | Second word of input dataset |
| INPUT.DS | , , | Full name of input dataset |
| OUTPUT_DS | , ' | Full name of output dataset |
| NL_RES_DS | , ' | Full name of dataset containing nonlinear results |
| INPUT_REC | 'data' | Input dataset record key |
| OUTPUT_REC | , , | Output record key |
| OUTPUT_FILE | , ' | Output file name |

Table 6.4-1 lists the datasets used by procedure TOTAL_LOAD.

| Table 6.4-1 |  |  |  | Datasets Input/Output by procedure TOTAL_LOAD |
| :--- | :--- | :---: | :---: | :---: |
| Dataset | Description | Lib | Input | Output |
| STAT.REAC.i.j $\dagger$ | Reaction Force Vector | INPUT_LDI | $\sqrt{ }$ |  |
| JDF1.BTAB.1.8 | Number of nodes and active d.o.f. | INPUT_LDI | $\sqrt{ }$ |  |

$\dagger i=$ <load_set> and $j=$ <cons_set> for linear analyses
$i=$ <step> and $\mathrm{j}=0$ for nonlinear analyses

### 6.4.3 ARGUMENT DESCRIPTIONS

### 6.4.3.1 INPUT_LDI

Input library number (default: 1 ).

### 6.4.3.2 OUTPUT_LDI

Output library number (default: 1). This argument sets the number of the output data library if an output dataset name (OUTPUT_DS) has been set. If an output dataset name has not been specified, this argument is ignored.

### 6.4.3.3 NL_RES LDI

Library containing nonlinear results dataset (default: 3). This argument is used only if the number of nonlinear load steps is to be calculated automatically (i.e., NSTEPS = ALL). In this case, the number of load steps is calculated based on the number of records found in the results dataset contained in the NL_RESLDI library.

### 6.4.3.4 LOAD_SET

Load set number (default: 1). This argument selects the load set to be used as a right-hand side vector. LOAD_SET is an active argument only if NSTEPS $=0$ and END_STEP $=-1$ (the default values).

### 6.4.3.5 CONS_SET

Load set number (default: 1). This argument selects the constraint set to be used in the solution of the linear system of equations. CONS_SET is an active argument only if NSTEPS $=0$ and END_STEP $=-1$ (the default values).

### 6.4.3.6 NSTEPS

Number of steps to be processed (default: 0). The number of load steps may be set to an integer or to the character string ALL. If NSTEPS = ALL, the number of load steps to be processed is calculated based on the information contained in the NL_RES_DS in library NL_RES_LDI. For use in linear static analyses, NSTEPS must be set to zero.

### 6.4.3.7 BEGIN_STEP

First load step to be processed (default: 1). This argument is active only if END_STEP is greater than zero in which case, load steps BEGIN_STEP through END_STEP will be processed.

### 6.4.3.8 END_STEP

Last load step to be processed (default: -1). This argument is active only if it is greater than zero in which case, load steps BEGIN_STEP through END_STEP will be processed.

### 6.4.3.9 LD_DIR

Load direction (default: 1). This argument defines the direction in which to perform the summation. The value of LD_DIR must be an active degree of freedom (i.e., $1,2,3,4,5$, or 6 and not specified as globally constrained in TAB/START).

### 6.4.3.10 EQUIL_CK

Flag enabling an equilibrium check (default: 0 ). The total load is calculated by summing the absolute value of the nodal contributions in the direction of LD_DIR. When EQUIL_CK is set to one (1), the absolute value is not used when performing the summation.

### 6.4.3.11 EA

Scaling factor (default: 1.0). Frequently the total load may be normalized by the extensional stiffness or critical buckling load. The total will be divided by the scaling factor EA before being saved or written out.

### 6.4.3.12 FAC

Scaling factor (default: 2.0). The default value of 2.0 will be used in most applications where the total load is being calculated. This is due to the use of the absolute value in the summation which essentially doubles the applied load. Frequently for finite element models with symmetry conditions imposed, the total load is only half the value of the summed reaction forces. The total load will be divided by the scaling factor FAC before being saved or written out.

### 6.4.3.13 NAME1

First word of reaction force dataset name (default: STAT). This is an active argument only if INPUT_DS $=$ ' ' (the default value).

### 6.4.3.14 NAME2

Second word of reaction force dataset name (default: REAC). This is an active argument only if INPUT_DS $=$ ' ' (the default value).

```
*call TOTAL_LOAD ( --
    nsteps = ALL ; -- . process all lozd steps
    1d_dir = 3 ; -- . direction of load is 3
    name1 = 'REAC' ; -- . first word of input dataset
    name2 = 'FORC' ; -- . second word of input dataset
    output_file = 'sum_load.dat' ) . output file name
```


### 6.4.5 LIMITATIONS

None.

### 6.4.6 ERROR MESSAGES AND WARNINGS

None.

### 6.4.7 PROCEDURE FLOWCHART

Procedure TOTAL_LOAD is self-contained and calls no other procedures.

### 6.4.8 PROCEDURE LISTING

```
*procedure TOTAL_LOAD ( --
    input_ldi = 1 ; -- . Input library
    output_ldi = 1 ; -- . Output library
    nl_res_ldi = 3 ; -- . Library containing nonlinear results ds
    load_set = 1 ;- . load set (linear only)
    cons_set = 1 ; -- . constraint set (linear only)
    nsteps = 0 ; -- . number of load steps to process
    begin_step = 1 ;- . first load step to process
    end_step = -1 ; -- . last load step to process
    ld_dir = 1 ; -- . direction of load
    equil_ck = 0 ; -- . if = 0, total load; i1 = 1, check equil.
    EA = 1.0 ; -- . EA (to get P/EA)
    fac =2.0 ; -- . divide final load
    mamel = 'STAT' ; -- . lirst word of input dataset
    nare2 = 'REAC' ; -- . second word of input dataset
    input_ds = "," ,";; -- . full nare of input dataset
    output_ds = ',' '",; -- . output dataset
    nl_res_ds = 'ES*' ; -- . nonlinear results dataset name
    input_rec = 'DATA' ; -- . input dataset record key
    output_rec = 'TOTAL_LOAD'; -- . output record
    output_file = ',',',) . output file name
    [xqt LOAD
    resot inlib=[input_ldi], outlib=[output_ldi], reslib=[nl_res_ldi]
    reset iset=[cons_set], ncon=[cons_set]
    reset nsteps=[nsteps], strt=[begin_step]
    reset idir=[ld_dir], eqck=[equil_ck]
                                    &
```

```
    reset ea=[EA],
    reset n1=[name1],
    reset dsin=[input_ds], dsout=[output_ds]
    1fac=[fac]
    n2=[name2]
    rnout=[output_rec]
    reset outfil=[output_file]
    stop
*end
```


### 6.4.9 REFERENCES

None.

### 7.0 Utility Procedures

The procedures documented in this chapter are convenient utility procedures that are ū̄eful in mañy analysis tasks.

A summary of the procedures found in this chapter is provided in Table 7.0-1.

Table 7.0-1 Utility Procedures

| Procedure Name | Utility Description |
| :--- | :--- |
| COMSTRAIN | Impose Scaled Applied Displacements |
| COPY_DS | Copy a Dataset and Rename |
| EIGEN | Perform Eigenvalue Analysis |
| ES | Generic Element Processor Control |
| FACTOR | Factor (Decompose) System Stiffness Matrix |
| FORCE | Form Force Vectors |
| IMPERFECTION | Superpose Initial Geometric Imperfection |
| INITIALIZE | Model initialization |
| MASS | Form Mass Matrix |
| MODEL_SURMARY | Model Summary Information |
| PRINT_EFIL | Print Selected Segments of EFIL Dataset |
| RESEQUENCE | Resequence Nodal Equations |
| SOLVE | Solve System of Equations |
| STIFFNESS | Form Stiffness Matrix |
| SWITCH_DS | Switch the Names of Two Datasets |

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### 7.1 Procedure CONSTRAIN

### 7.1.1 GENERAL DESCRIPTION

Procedure CONSTRAIN scales the applied motion vector. This procedure is generally used for nonlinear analyses with applied displacements.

### 7.1.2 PROCEDURE USAGE

Procedure CONSTRAIN is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call CONSTRAIN ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure CONSTRAIN are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure CONSTRAIN, the following table lists each argument, its default value and meaning.

| Argument | Default Value |  | Meaning |
| :--- | :---: | :---: | :--- |
| APPLIED_MOTION |  |  | Name of applied motion dataset |
| CONSTRAINT_SET | 1 |  | Constraint set number |
| DISPLACEMENT |  |  | Name of scaled applied motion dataset |
| LDI | 1 |  | Logical device index |
| LOAD_FACTOR | 1.0 |  | Load factor |

### 7.1.3 ARGUMENT DESCRIPTIONS

### 7.1.3.1 APPLIED_MOTION

Full dataset name of the basic applied displacements (e.g., APPL.MOTI.1.1).

### 7.1.3.2 CONSTRAINT_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.1.3.3 DISPLACEMENT

Full dataset name of the scaled applied displacements (e.g., TOT.DISP.1).

### 7.1.3.4 LDI

Logical device index (default: 1).

### 7.1.3.5 LOAD_FACTOR

Load factor (default: 1.0). This argument defines the load factor or scaling constant to be used to scale the basic applied motions.

### 7.1.4 USAGE GUIDELINES AND EXAMPLES

Procedure CONSTRAIN is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call CONSTRAIN ( LDI = 1 ; CONSTRAINT_SET = 1 ;
    LOAD_FACTOR = 1.0 ;
    APPLIED_MOTION = APPL.MOTI.1.1;
    DISPLACEMENT = TOT.DISP.1 )
```


### 7.1.5 LIMITATIONS

Procedure CONSTRAIN assumes that processor VEC is executing.

### 7.1.6 ERROR MESSAGES AND WARNINGS

None.

### 7.1.7 PROCEDURE FLOWCHART

Procedure CONSTRAIN is self-contained with no subprocedures.

### 7.1.8 PROCEDURE LISTING

```
*procedure CONSTRAIN ( ldi = 1 ; --
    constraint_set = 1 ; --
    load_factor = 1.0 ; --
    applied_motion ; --
    displacement )
. Impose Specified Displacenent Constraints (Single Point)
    *if < <spec_disp_flag> > /then
        SPECIFY [load_factor] [applied_motion] -> [displacenent]
    *ondif
*end
```


### 7.1.9 REFERENCES

7.1-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 7.2 Procedure COPY_DS

### 7.2.1 GENERAL DESCRIPTION

Procedure COPY_DS copies a dataset in a given library to another dataset in possibly a different library. This procedure only uses directives from the command language (see reference 7.1-1).

### 7.2.2 PROCEDURE USAGE

Procedure COPY DS may be used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call COPY_DS ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg 2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure COPY.DS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure COPY_DS, the following table lists each argument, its default value and meaning.

| Parameter | Default Value |  | Meaning |
| :--- | :---: | :--- | :--- |
| FROM_DS | - |  | Source dataset name |
| TO_DS | - |  | Target dataset name |
| FROM_LDI | 1 | Source logical device index |  |
| TO_LDI | 1 | Target logical device index |  |

### 7.2.3 ARGUMENT DESCRIPTIONS

### 7.2.3.1 FROM_LDI

Source logical device index (default: 1).

### 7.2.3.2 FROM_DS

Source dataset to be copied.

### 7.2.3.3 TOLDI

Target logical device index (default: 1).

### 7.2.3.4 TO.DS

Target dataset for copying source dataset into.

### 7.2.4 USAGE GUIDELINES AND EXAMPLES

Procedure COPY_DS may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*procedure COPY_DS ( from_ldi=1; from_ds; to_ldi=1; to_ds )
```


### 7.2.5 LIMITATIONS

None.

### 7.2.6 ERROR MESSAGES AND WARNINGS

None.

### 7.2.7 PROCEDURE FLOWCHART

Procedure COPY_DS is self contained with no subprocedures.

### 7.2.8 PROCEDURE LISTING

```
*procedure COPY_DS ( from_ldi=1; from_ds; to_ldi=1; to_ds )
---------
CLAMP Procedure to copy dataset and rename
    *if < [from_ldi] /eq [to_ldi] > /then
        *def/i 1dix = 30
        *opon/scratch <ldix>
        *copy <ldix> s [from_1di], [from_ds]
        *rename <ldix>, [from_ds] = [to_ds]
        *copy [to_ldi] = <ldix> , [to_ds]
        *clos, <ldix>
    *el=0
        *copy [to_ldi] = [fron_ldi], [from_ds]
        *rename [to_ldi], [fron_ds] = [to_ds]
```


## *ondif

*ond

### 7.2.9 REFERENCES

7.1-1 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.

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### 7.3 Procedure EIGEN

### 7.3.1 GENERAL DESCRIPTION

Procedure EIGEN solves a linear eigenvalue problem using an eigensolver defined by the global macrosymbol eigensolver_name. If eigensolver_name is EIG or EIG2, a matrix iteration procedure with subspace iteration is used as implemented in processors EIG and EIG2, respectively (see Section 9.1 of reference 7.3-1). If eigensolver_name is defined to be LAN, a Lanczos algorithm implemented in processor LAN will be used (see Section 9.2 of reference 7.3-1). If eigensolver_name is defined to be LANZ, the alternate Lanczos method implemented in processor LANZ will be used (see Section 9.3 of reference 7.3-1).

### 7.3.2 PROCEDURE USAGE

Procedure EIGEN is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call EIGEN ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure EIGEN are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure EIGEN, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| Constraint_SET | 1 | Constraint set number |
| LDI | 1 | Logical device index |
| LOAD_SET | 1 | Load set number |
| KNAME | K | First word of the name of the dataset containing the assembled stiffness matrix. |
| PROBLEM_TYPE | 'buck' | Define problem type for either buckling or vibration. |
| MASS_TYPE | 'CONSISTENT, | Form of mass matrix (consistent or diagonal) |
| ERROR_TOL | 1.0E-4 | Error tolerance for eigenvalue convergence |
| \#_MODES | 1 | Number of converged eigenmodes desired |
| INIT_VECTORS | 0 | Number of iteration vectors |
| SHIFT | 0.0 | Eigenvalue shift |
| MAX_ITERS | 20 | Maximum number of iterations |

Tables 7.3-1 and 7.3-2 list the datasets used or created by procedure EIGEN and the processors invoked by procedure EIGEN, respectively.

| Dataset | Description | Input | Output |
| :---: | :---: | :---: | :---: |
| AMAP..ic2.isize | Factorization Map for INV | $\checkmark$ |  |
| CON..j | Constraints | $\checkmark$ |  |
| INV.<KNAME>.j | Factored Stiffness Matrix | $\checkmark$ |  |
| JDF1.BTAB.1.8 | Model Summary | $\checkmark$ |  |
| JSEQ.BTAB.2.17 | Nodal Elimination Sequence | $\checkmark$ |  |
| KMAP..nsubs.ksize | Model Connectivity Map | $\checkmark$ |  |
| <KNAME>.SPAR.jdf\% | Assembled Stiffness Matrix | $\checkmark$ |  |
| <KGNAME>.SPAR.jdf2 | Assembled Geometric Stiffness Matrix | $\checkmark$ |  |
| <MNAME>.SPAR.jdf2 | Assembled Consistent Mass Matrix | $\checkmark$ |  |
| VIBR.MODE.i.j $\dagger$ | Vibration eigenmodes |  | $\checkmark$ |
| VIBR.EVAL. $\mathrm{i} . \mathrm{j} \dagger$ | Vibration eigenvalues |  | $\checkmark$ |
| BUCK.MODE. $\mathrm{i} . \dagger$ ¢ | Buckling eigenmodes |  | $\checkmark$ |
| BUCK.EVAL.i.j $\dagger$ | Buckling eigenvalues |  | $\checkmark$ |


| Table 7.3-2 Processors Invoked by procedure EIGEN |  |  |
| :--- | :--- | :--- |
| Procedure | Type | Function |
| EIG/EIG2 | Internal | Solves eigenproblem using subspace iteration |
| LAN | External | Solves eigenproblem uing Lanczos method |
| LANZ | External | Solves eigenproblem using Lanczos method |
| GETK | Internal | Converts nodal block matrix format to compact sparse for- <br> mat |

### 7.3.3 ARGUMENT DESCRIPTIONS

### 7.3.3.1 PROBLEM_TYPE

Defines problem type (default: 'BUCK'). This argument selects the type of eigenproblem to solve either buckling (BUCK) or vibration (VIBR).

### 7.3.3.2 ECON_SET

Constraint set number for eigenproblem (default: 1). This argument selects which constraint set to be used in solving the eigenproblem which may be different from that used for determining the prestress state.

### 7.3.3.3 LDI

Logical device index (default: 1).

### 7.3.3.4 LOAD_SET

Load set number (default: 1). This argument selects which load set to be used as a right-hand side vector.

### 7.3.3.5 KNAME

First word of the dataset name containing the assembled stiffness matrix (default: K).

### 7.3.3.6 KGNAME

First word of the dataset name containing the assembled geometric stiffness matrix (default: KG).

### 7.3.3.7 MNAME

First word of the dataset name containing the assembled mass matrix (default: CEM).

### 7.3.3.8 MASS_TYPE

Form of mass matrix (default: 'CONSISTENT'. This argument defines the form of the mass matrix to be either consistent or diagonal.

### 7.3.3.9 ERROR_TOL

Error tolerance for convergence of eigenvalues (default: 1.OE-4).

### 7.3.3.10 N.MODES

Number of converged eigenmodes desired (default: 1).

### 7.3.3.11 INIT_VECTORS

Number of initial iteration vectors (default: 0). If the default value is used, then the number of initial iteration vectors will be the minimum of <2* <N_MODES>> and $\ll$ N_MODES $>+8>$.

### 7.3.3.12 SHIFT

Eigenvalue shift (default: 0.0 ).

### 7.3.3.13 MAX_ITER

Maximum number of iterations in solving the eigenproblem (default: 20).

### 7.3.4 USAGE GUIDELINES AND EXAMPLES

Procedure EIGEN is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call EIGEN ( KNAME = K ; ECON_SET = 1 ;
    LOAD_SET = 1 ; KGNAME = KG )
```

Before procedure EIGEN is called the global macrosymbol eigensolver_name should be defined as described in Section 7.3.1 and should be consistent with the value used when procedure FACTOR was called. If it is not specified, then the default value EIG2 will be used.

### 7.3.5 LIMITATIONS

None.

### 7.3.6 ERROR MESSAGES AND WARNINGS

None.

### 7.3.7 PROCEDURE FLOWCHART

Procedure EIGEN is self-contained with no subprocedures.

### 7.3.8 PROCEDURE LISTING

```
*procedure EIGEN ( PROBLEM_TYPE = 'BOCK' ; -- . Problen type: BUCK or VIBR
    ldi = 1 ; -- . library number
    kname = 'K' ; -- . First name of material stiffness matrix
    kgname = 'KG' ; -- . First name of geonetric stiffness matrix
    mame = 'CEM' ; -- . First name of mass matrix
    error_tol = 1.0e-4 ; -- . Error tolerance on eigenevalues
    load_set = 1 ; -- . Load set number
    mask_type = 'CONSISTENT' ; -- . Form of mass matrix
    N_modes = 1; -- . Number of modes desired
    IMIT_vectors = 0 ; -- . Nunber of initial vectors
    SEIPT =0.0 ; -- . Eigenvalue shift
    max_iters = 20 ; -- . Maximum numbor of iterations
    econ_set = 1 ). Constraint set for eigenproblem
. Procedure to solve the eigenvalue problen using different
. eigensolvers. The eigensolver is selected using the
. global macrosymbol "oigensolver_name".
Perforn Eigenvalue Analysis (with [kname].SPAR and [kgname].SPAR)
    *if < [IMIT_vectors] /eq 0 >/then
        *def/i H_vectors = < MIN( 2*[N_modes]; [N_modes]+8) >
        *else
        *def/i H_vectors = [INIT_vectors]
    * ondif
.
Select eigensolvar
--------------------
. Use processor EIG
*if < ifeqs(<eigensolver_name>;EIG) > /then
    *def NS_OVERWRITE = <false>
    [XqT EIG
    RESET PROB=[PROBLEM_TYPE]
    RESET INIT=<N_vectors>, SHIFT=[shift], NREQ=[N_modes]
    RESET CONY=[error_tol], NDYN=[max_iters], con=[econ_set],NEUSET=[load_set]
    RESET K=[kname]
    RESET KG=[kgname]
    RESET Ma[mane]
    RESET KLIB=[LDI], KILIB=[LDI], KGLIB=[LDI], KLIB=[LDI] ,OUTLIB= [LDI]
    RESET INLIB=[LDI],OLDSET=[LDI]
    STOP
    Use processor EIG2
```

```
*elseif < ifeqs(<eigensolver_name>;EIG2) > /then
    *def NS_OVERURITE = <falso>
    [xQT EIG2
    RESET PROB=[PROBLEM_TYPE]
    EESET INITz<N_vectors>, SHIFT=[shift], NREQ=[N_modes]
    RESET CONV=[orror_tol], NDYN=[nax_iters], con=[econ_set],NEUSET=[load_set]
    RESET K=[kname]
    RESET XG=[xgname]
    RESET Mm[mane]
    RESET KLIB=[LDI],KILIB=[LDI],KGLIB=[LDI],MLIB=[LDI] ,0UTLIB=[LDI]
    RESET INLIB=[LDI],OLDSET=[LDI]
    STOP
*elseif < ifeqs(<eigensolver_name>;LAN) > /then
- Ose processor LAN
    *def NS_OVERURITE = <false>
    [xqt LAN
        HESET PROB=[PROBLEM_TYPE],LDI=[LDI]
        EESET KNAM=[kname], KGNA=[kgname], MNAM=[nname]
        RESET NK=[max_iters], shiftx[shift], ncon=[econ_set]
        STOP
*elseif < ifeqs(<eigensolver_name>;LANZ) > /then
    *def HS_OVRQURITE = <false\rangle
*if < ifeqs([PROBLEH_TYPE];BUCK) > /then
        [xqt GETK
            reset sipr=0, form=2, save=1
            reset k=k, redo=0, kred=k, reac=0
        [xqt GETK
            reset sipr=0, form=2, save=1
            Fuset k=kg, redo=1, kred=k, reac=0
        [xqt LANZ
        RESET PROB=2, plvl=3,check=1, conx[econ_set]
        MESET nreq=[N_modes], conv=[error_tol]
    EESET kg=[kgname]
*elseif < ifeqs([PROBLEM_TYPE];VIBR) > /then
    [xqt GETK
        reset sipra0, form=2, save=1
        reset k=k, redo=0, kred=k, reac=0
    *if < ifegs([nasm_type];CONSISTENT) > /then
    *def/i ncase=1
    [xqt GETK
        reset sipr=0, form=2, save=1
        reset k=[mname], redo=1, kred=k, reac=0
    *else
    *def/i ncase=0
    *endif
    [xqt LANZ
    RESET mcase=<ncase>, plvl=3,check=1,con=[econ_set]
    MESET nreq=[N_modes], conv=[error_tol]
    RESET E=[nname]
*endif
```


## *endif <br> *end

### 7.3.9 REFERENCES

7.3-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.4 Procedure ES

### 7.4.1 GENERAL DESCRIPTION

Procedure ES is a high-level procedure that controls the structural element processors (ESi). The Generic Element Processor (GEP) provides a template with which many individual finite-element processors may be developed and coexist as independent modules in the CSM Testbed (see ref. 7.4-1). The GEP template for structural elements is referred to as ES, and all element processors built with this template have names that begin with ES (e.g., ES1, ES2, ...). Each of these ESi processors performs all operations for all of the elements implemented within the processor - including element definition, stiffness, force, mass (etc.) generation, and various pre/post-processing functions.*

Since ESi processors are typically built by different developers, you might expect a wide variety of User-interface characteristics. However, because of the generic template employed, all ESi processors share the same command language and global datasets. This means that once the user has learned to invoke one ESi processor, the user has learned them all.

The main difference between ESi processors will be in the specific elements implemented within them. Some ESi processors may have only one element type inside. Others may have a family of elements of a certain class (e.g., 4-, 9 - and 16 -node shell elements). Still others may embed an entire library of structural elements, containing various members of each class (e.g., beam, shell, solid). Each of these specific element types is given a corresponding name within each ESi processor; so that the combination of ESi processor name and element type is unique. Thus, to employ a particular ESi processor correctly, the user will have to consult specific documentation on the individual elements contained within that processor. Such documentation is provided in the CSM Testbed User's Manual (see ref. 7.4-2).

In the following sections, the generic features of ESi processors are described in detail.

[^0]The description includes ESi processor commands and macrosymbols, and the datasets required or produced by these commands (Section 2.2), the high-level procedure interface, which makes it possible to write analysis procedures that invoke a single, generic procedure (called ES) to generate element arrays automatically for all ESi processors required in a given problem; a glossary of ES macrosymbols, which gives more detailed definitions for the macrosymbols and procedure arguments; and some explicit examples of how to use ESi processors, interactively, or using the procedure ES interface.

### 7.4.2 PROCEDURE USAGE

Procedure ES may be invoked by the *call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are orderindependent, and most have default values thus making them optional. The formal syntax is as follows:

> *call ES ( arg1 = val1; arg2 = val2; ...)
where argi are argument names and vali are the corresponding values. The following are valid arguments for procedure ES; note that those arguments without default values are mandatory, while the others are optional.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| ES NAME | -- | Element-type name |
| ES_ML_GEOM | -- | Geometric nonlinearity |
| ES_ML_MATL | -* | Material nonlinearity |
| ES_NLLIOAD | -- | Load nonlinearity |
| ES_PARS | -- | Research parameters |
| ES_PROC | -- | Processor name |
| FUNCTION | -- | Processor command |
| ES_CORO | 1 | Corotational option |
| ES_COUNT | 0 | Create or accumulate ES.SUMMARY |
| ES_DIS_DS | STAT.DISP.1.1 | Displacement dataset |
| ES_DOF_DS | ES.DOFS | Active-freedom dataset |
| ES_ECC_DS | WALL.PROP | Eccentricity dataset |
| ES_FRC_DS | INT.FORC.1.1 | Force vector dataset |
| ES_ROT_DS | Stat_ROTA.1.1 | Rotation vector dataset |
| ES_STR_LOC | CENTROIDS | Stress locations |
| ES_STR_DIR | 0 | Stress directions |
| ES_STRAIN_DS | ' | Element strain dataset |
| ES_STRESS_DS | , | Element stress dataset |
| ES_SOM.DS | ES. SUMMARY | ES summmary dataset |
| LDI | 1 | Logical device index |
| NUM_CON_DS | 1 | Number of constraint datasets |

Table 7.4-1 Datasets Input/Output by Procedure ES

| Dataset | Description | Lib | Input | Output |
| :--- | :--- | :--- | :--- | :--- |
| ES.SUMMARY | ES Processor Status | 1 |  | $\sqrt{ }$ |
| ES.DOFS | 1 |  |  | $\sqrt{ }$ |
| <ES_NAME>.EFIL.0.nnod | Element Computational Data | 1 |  | $\sqrt{ }$ |
| DIR.<ES_NAME>.0.nnod | Element EFIL Directory | 1 | $\sqrt{ }$ |  |
| DEF.<ES_NAME>.0.nnod | Element Definition (Connectivity) | 1 | $\sqrt{ }$ |  |
| PROP.BTAB.2.* | Material/Section Properties | 1 | $\sqrt{ }$ |  |
| STAT.DISP.i.j | System Displacement Vector | 1 | $\sqrt{ }$ |  |
| STAT.ROTA.i.j | System Rotation Vector | 1 | $\sqrt{ }$ |  |
| QJJT.BTAB. | Nodal Transformations | 1 | $\sqrt{ }$ |  |
| INT.FORC.i.j | System Internal Force Vector | 1 |  | $\sqrt{ }$ |
| DEM.DIAG | Diagonal (Lumped) Mass Matrix | 1 |  | $\sqrt{ }$ |
| CEM.SPAR.jdfz | Assembled Consistent Mass Matrix | 1 |  | $\sqrt{ }$ |
| STRN.<ES_NAME>. | Element Strains | 1 |  | $\sqrt{ }$ |
| <ES_STRAINDS> |  |  |  |  |
| STRS.<ES_NAME>. | Element Stresses | 1 |  | $\sqrt{ }$ |
| <ES_STRESS_DS> |  | Assembled material stiffness matrix | 1 |  |
| K.SPAR.jdf2 | Assembled geometric stiffness matrix | 1 |  | $\sqrt{ }$ |
| KG.SPAR.jdf2 |  |  |  |  |

$\dagger i=$ <load_set $>$ and $j=<$ cons_set $>$

Table 7.4-2 Sub-Procedures Invoked by Procedure ES

| Procedure | Type | Function |
| :--- | :--- | :--- |
| ES | Internal | Main procedure |
| ES_DOFS | Internal | Automatic DOF Suppression for ESi |

Table 7.4-3 Sub-Procedures Invoked by Procedure ES

| Processor | Type | Function |
| :--- | :--- | :--- |
| ESi | External | Various element processors |
| VEC | Internal | Vector functions |

## Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY

| Macrosymbol | Type | Definition |
| :---: | :---: | :---: |
| ES_C | I | Continuity of interelement "displacement" field, e.g., $0 \Rightarrow C^{0}$ (displacement continuity only) <br> $1 \Rightarrow C^{1}$ (displacement and slope continuity) |
| ES_CLAS | A | Element class. Currently valid classes: BEAM, SHELL, SOLID, WILD (See Section 3.4 for examples.) |
| ES_CNS | I | Constitutive interface option (see Chapter 5). <br> $0 \Rightarrow$ elements use the standard constitutive interface for stress and tangent-modulus calculations; <br> $1 \Rightarrow$ elements compute their own stresses, but use standard constitutive interface for tangent-modulus calculations; $\geq 2 \Rightarrow$ elements compute their own stresses and tangentmoduli; standard constitutive interface is not used. |
| ES_CORO | I | Corotation switch; employed by ES processor for automatic treatment of geometric nonlinearity due to large rotations. Relevant only if problem is geometrically nonlinear. (See Chapter 4 for an explanation of these options.) <br> $0 \Rightarrow$ Off: corotational operations will be skipped; <br> $1 \Rightarrow$ Low-Order Option: basic corotational transformations will be employed to enable large rotations; $2 \Rightarrow$ High-Order Option: a more accurate (and expensive) treatment of large rotations and consistent linearization than option 1 will be employed. |
| ES_COUNT | I | Element processor count. Relevant only for DEFINE ELEMENTS command. <br> $0 \Rightarrow$ First element processor to be defined; create ES.SUMMARY dataset. <br> $>0 \Rightarrow$ Not first element processor to be defined; use existing ES.SUMMARY dataset and Increment element processor number by one. |
| ES_DIM | I | Number of intrinsic element spatial dimensions, e.g., <br> 1 if ES_CLAS = BEAM <br> 2 if ES_CLAS = SHELL <br> 2 or 3 if ES_CLAS = SOLID |

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (continued)
$\left.\begin{array}{lll}\hline \text { Macrosymbol } & \text { Type } & \text { Definition } \\ \hline \text { ES_DIS_DS } & \text { A } & \begin{array}{l}\text { Name of system displacement-vector dataset (SYSVEC } \\ \text { format). Relevant for most FORM commands and some } \\ \text { POST commands. (Default: STAT.DISP.1.1) }\end{array} \\ \hline \text { ES_DOF_DS } & \text { A } & \begin{array}{l}\text { Name of element freedom-table dataset (SYSVEC for- } \\ \text { mat). Relevant only for DEFINE FREEDOMS com- } \\ \text { mand. When using procedure ES, this dataset will au- } \\ \text { tomatically be created, initialized, and updated cumu- } \\ \text { latively with contributions from all pertinent ES pro- } \\ \text { cessors. (Default: ES.DOFS) }\end{array} \\ \hline \text { ES_ECC_DS } & \text { A } & \begin{array}{l}\text { First two words of dataset name that contains section } \\ \text { property data including reference surface eccentricities. } \\ \text { (Default: WALL.PROP). }\end{array} \\ \hline \text { ES_EXPE_CMD } & \text { A } & \begin{array}{l}\text { Complete EXPE command line appropriate for defin- } \\ \text { ing elements with processor ELD. This macrosymbol is } \\ \text { constructed only in response to a call to procedure ES } \\ \text { with FUNCTION=DEFINE ELEMENTS'. }\end{array} \\ \hline \text { A } & \begin{array}{l}\text { Name of system force-vector dataset (SYSVEC format), } \\ \text { where element distributed forces (internal and/or ex- } \\ \text { ternal) are to be assembled. Relevant only for FORM }\end{array} \\ \hline \text { FORCE command, in which case this vector must be } \\ \text { created and initialized before issuing the command (or } \\ \text { calling procedure ES). Contributions from all pertinent }\end{array}\right\}$

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (continued)
Macrosymbol Type Definition

ES_MASS_DIAG 4 First word of the dataset name for a diagonal mass matrix. (Default: DEM).

| ES_MASS_DS | A | First two words of the dataset name for a diagonal mass matrix. <br> (Default: <ES_MASS_DIAG>.DIAG). |
| :---: | :---: | :---: |
| ES_NAME | A | Name of element type, within current ES processor, to be processed by subsequent commands. (For example EX97 would be a valid element-type name within processor ES1.) |
| ES_NDOF | I | Number of freedoms per element node. Currently valid options (2, 3 or 6 ), e.g., |
|  |  | 2 for 2-D solid elements ( $u, v$ ) |
|  |  | 3 for 3-D solid elements ( $u, v, w$ ) |
|  |  | 6 for beam, plate or shell elements ( $u, v, w, \theta_{x}, \theta_{y}, \theta_{z}$ ) |
| ES.NEE | I | Number of element equations; $=\text { ES_NEN } \times \text { ES_NDOF }$ |
| ES_NEN | I | Number of element nodes. |
| ES_NIP | I | Number of element integration points; i.e., points at which stresses (continuum or resultants, depending on element type) are stored. |
| ES_NL_GEOM | I | Geometric nonlinearity switch; $0 \Rightarrow$ Off: problem is geometrically linear (small displacements/rotations); |
|  |  | $1 \Rightarrow$ Low-Order Option: problem is geometrically nonlinear, but elements should use linear strain-displacement relations. Meaningful only if ES_CORO $>0$, so that large rotations can be handled automatically by the corotational algorithm; |

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (continued)

| Macrosymbol | Type | Definition |
| :---: | :---: | :---: |
|  |  | $2 \Rightarrow$ High-Order Option: problem is geometrically nonlinear and elements should use nonlinear element straindisplacement relations. May be used in conjunction with ES_CORO $>0$ to obtain higher-order accuracy for beam and shell elements that employ moderate-rotation straindisplacement relations; |
|  |  | $3 \Rightarrow$ same as 2 plus finite strains are expected. |
| ES_NL_LOAD | I | Load nonlinearity switch; <br> $1 \Rightarrow$ process displacement-dependent element loads only; <br> $0 \Rightarrow$ process displacement-independent element loads only. |
| ES_NL_MATL | I | Material nonlinearity switch; <br> $1 \Rightarrow$ element is materially nonlinear; <br> $0 \Rightarrow$ element materially linear. |
| ES_NORO | I | Element normal-rotation parameter. Relevant only for automatic freedom suppression of plate/shell elements. Indicates minimum angle (in degrees) between shell element normal vector and any computational basis vector - at each element node - below which the corresponding rotational freedom should be suppressed if no other elements are attached; |
|  |  | $=0 \Rightarrow$ Element has normal-rotation ("drilling") stiffness; normal rotational freedoms will automatically be suppressed. |
|  |  | $>0 \Rightarrow$ Element does not have normal-rotation ("drilling") stiffness; it is assumed that rotational stiffness exists about any computational axis that makes an angle of at least <ES_NORO> degrees with the element normal vector at an element node. |

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (continued)
Macrosymbol Type Definition
ES_NPAR I Number of element research parameters in array ES_PARS.

| ES_NSTR | I | Number of stress components per integration point. Currently valid options compatible with standard constitutive interface: |
| :---: | :---: | :---: |
|  |  | 8 for ES_CLAS $=$ SHELL and ES_C $=0$; |
|  |  | 6 for ES_CLAS $=$ SOLID and ES_DIM $=3$; |
|  |  | 6 for ES_CLAS $=$ SHELL and ES_C $=1$; |
|  |  | 6 for ES_CLAS $=$ BEAM and ES_C $=0$; |
|  |  | 4 for ES_CLAS $=$ BEAM and ES_C $=1$; |
|  |  | 3 for ES_CLAS $=$ SOLID and ES_DIM $=2$. |
| ES_OPT | I | Element-type option number. Meaningful only to the element developer; it is the developer's numerical equivalent of ES_NAME. |
| ES.PARS | D | Array of element research parameters. Meaning depends on specific element type. (Consult appropriate section in CSM Testbed User's Manual, ref. 4). |
| ES.PROC | A | Name of element (ES) processor to be executed (e.g., ES1, ES2, ...); currently relevant only as an argument for procedure ES, and only when argument FUNCTION = 'DEFINE ELEMENTS'. |

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (continued)

| Macrosymbol | Type | Definition |
| :--- | :---: | :--- |
| ES_PROJ | I | Rigid-body projection option. Used to automatically re- <br> move (most of) the spurious energy generated by some <br> elements during infinitesimal rigid-body motion. This is |
| performed by operating on the element stiffness and force <br> arrays with a projection matrix (or projector). The pro- <br> jector, and its derivative, can have a beneficial effect on <br> element accuracy in both linear and geometrically nonlin- <br> ear regimes. |  |  |

$0 \Rightarrow$ Off: projection will be omitted;
$1 \Rightarrow$ Low-order Option: basic projection will be included;
$2 \Rightarrow$ High-order Option: basic projection plus a differential correction to the geometric stiffness will be included.

ES_ROT_DS A Name of system rotation pseudo-vector dataset (SYSVEC format). Relevant for most FORM commands during geometrically nonlinear analysis, but only if elements with rotational freedoms are involved. (Default: STAT.ROTA.1.1)

ES_SHAP A Shape of element surface used to define coordinate triad; currently recognized options: LINE, TRIA or QUAD.

ES_STOR I Number of "private" variables to be stored/retrieved for the element developer in dataset EFIL.<ES_NAME>.

ES_STR_DIR I Element stress/strain direction option. Indicates in which coordinate system element stresses or strains in datasets defined by <ES_STRESS_DS> or <ES_STRAIN_DS> (respectively) will be computed. Relevant only for command $=$ 'FORM STRAIN' or 'FORM STRESS'. Valid options:
$0 \Rightarrow$ element stress coordinate system
$1 \Rightarrow$ material axes $\left\{x_{m}, y_{m}, z_{m}\right\}=\left\{x_{g}, y_{g}, z_{g}\right\}$
$2 \Rightarrow$ material axes $\left\{y_{m}, z_{m}, x_{m}\right\}=\left\{y_{g}, z_{g}, x_{g}\right\}$
$3 \Rightarrow$ material axes $\left\{z_{m}, x_{m}, y_{m}\right\}=\left\{z_{g}, x_{g}, y_{g}\right\}$
(Note: For isotropic materials, the first material axis is replaced by the corresponding global axis; see the SREF command under processor ELD in the Testbed User's Manual (ref. 4) for details. Default: 0)

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (continued)
Macrosymbol Type Definition

ES_STR_LOC A Element stress/strain evaluation point option. Indicates where stresses or strains in datasets defined by <ES_STRESS_DS> or <ES_STRAIN_DS> (respectively) will be computed. Relevant only for command = 'FORM STRAIN' or 'FORM STRESS'. Currently valid options: CENTROIDS $\Rightarrow$ element centroids; creates record group: CENTROIDS_<ES_STR_DIR>.1:nel
NODES $\Rightarrow$ element nodes; creates record group:
NODES_<ES_STR_DIR>.1:nel
INTEG_POINTS $\Rightarrow$ element integration points; creates: INTEG_PTS_<ES_STR_DIR $>.1:$ nel
where "nel" is the number of elements in the dataset, and where macrosymbol ES_STR_DIR designates the directions of the stress/strain components, and is defined elsewhere in this Glossary.
(Default: 'CENTROIDS')
ES_STRAIN_DS A Third part of element strain dataset name. The first name is always STRN; the second name is always the element-type name, i.e., <ES_NAME>; and the third name, <ESSSTRAIN_DS> must be a string of integers separated by periods.
For example, if <ES_STRAIN_DS> = <step>.<iter>
where <step> $=20$ and <iter> $=3$, and if the elementtype name were EX97, then the full dataset name would be: STRN.EX97.20.3
Relevant only for command = 'FORM STRAIN'.
(No default; absence means that strains will be stored (embedded) within dataset EFIL.<ES_NAME $>$ only currently not implemented.)

Table 7.4-4 ES PROCESSOR MACROSYMBOL GLOSSARY (concluded)

| Macrosymbol | Type | Definition |
| :---: | :---: | :---: |
| ES_STRESS_DS | A | Third part of element stress dataset name. The first name is always STRS; the second name is always the element-type name, i.e., <ES_NAME>; and the third name, <ES_STRESS_DS> must be a string of integers separated by periods. For example, if <ES_STRESS_DS> $=\langle$ step $\rangle$.<iter>, <br> where <step> $=20$ and <iter> $=3$, and if the elementtype name were EX97, then the full dataset name would be: STRS.EX97.20.3 <br> Relevant only for command = 'FORM STRESS'. <br> (No default; absence means that stresses will be stored (embedded) within dataset EFIL.<ES_NAME> only.) |
| ES_SUM_DS | $\wedge$ | Name of ES summary dataset, which contains nominal records corresponding to most of the macrosymbol parameters appearing in this Glossary - for each ES processor/element defined in the model. Relevant for all ES commands. (Default: ES.SUMMARY) |
| ES_TWIS | I | Sign of twisting curvature for shell elements. |
|  |  | $+1 \Rightarrow$ twist based on continuum definition of shear strain; |
|  |  | -1 $\Rightarrow$ twist based on negative of continuum definition. |
|  |  | (Note: The default convention for constitutive matrices output from processor LAU corresponds to the -1 option. Hence processor ES compensates for this reversal if ES_TWIS $=+1$.) |
| ES_TGC_DS | I | Name of nodal transformation dataset (QJJT.BTAB.*.*) |
| ES.XYZ_DS | I | Name of nodal coordinate dataset (JLOC.BTAB.*.*) |
| LDI | I | Logical device index or library number for archiving and retrieving data. (Default: 1) |

### 7.4.3 ARGUMENT DESCRIPTION

### 7.4.3.1 ES_CORO

Corotation switch; employed by ESi processors for automatic treatment of geometric nonlinearity due to large rotations. Relevant only if problem is geometrically nonlinear. (See Chapter 4 of reference 7.4-1 for an explanation of these options.) If ES_CORO equals zero, then the corotational operations will be skipped. If ES_CORO equals one (low-order option), then the basic corotational transformations will be employed to enable large rotations. If ES_CORO equals two (high-order option), then a more accurate (and expensive) treatment of large rotations and consistent linearization than option 1 will be employed.

### 7.4.3.2 ES_CDUNT

Element processor count (default: 0). This argument is used to create and/or accumulate data in the ES.SUMMARY dataset for finite element models using multiple element processors.

### 7.4.3.3 ES_DIS_DS

Name of system displacement-vector dataset in SYSVEC format (default: STAT.DISP.1.1). Relevant for most FORM commands.

### 7.4.3.4 ES_DOF_DS

Name of element freedom-table dataset (SYSVEC format). Relevant only for DEFINE FREEDOMS command. When using procedure ES, this dataset will automatically be created, initialized, and updated cumulatively with contributions from all pertinent ESi processors. (Default: ES.DOFS)

### 7.4.3.5 ES_ECC_DS

Name of element section property eccentricity dataset (default: WALL. PROP). Relevant for all FORM commands.

### 7.4.3.6 ES_PRC_DS

Name of system force-vector dataset in SYSVEC format, where element distributed forces (internal and/or external) are to be assembled (default: STAT.REAC.1.1). Relevant only for FORM FORCE command, in which case this vector must be created and initialized before issuing the command (or calling procedure ES). Contributions from all pertinent ESi processors will be assembled into this vector if procedure ES is called with argument FUNCTION = 'FORM FORCE.

### 7.4.3.7 ES_NAME

Name of element type, within current ESi processor, to be processed by subsequent commands. (For example, EX97 would be a valid element-type name within processor ES1.)

### 7.4.3.8 ES_NL_GEOM

Geometric nonlinearity switch. If ES_NL_GEOM equals zero (no corotational frames), then the problem is geometrically linear (small displacements/rotations). If ES_NL_GEOM equals one (low-order option), then the problem is geometrically nonlinear, but elements should use linear strain-displacement relations. Meaningful only if ES_CORO $>0$, so that large rotations can be handled automatically by the corotational algorithm. If ES_ML_GEOM equals two (high-order option), then the problem is geometrically nonlinear and elements should use nonlinear element strain-displacement relations. May be used in conjunction with ES_CORO $>0$ to obtain higher-order accuracy for beam and shell elements that employ moderate-rotation strain-displacement relations.

### 7.4.3.9 ES_NL_MATL

Material nonlinearity switch. If ES_NL_MATL is greater than zero, then the element is materially nonlinear. If ES_NL_MATL is zero, then the element is materially linear.

### 7.4.3.10 ES_NL_LOAD

Load nonlinearity switch. If ES_NL_LOAD is greater than zero, then the element loads are displacement dependent. If ES_NL_LOAD equals zero, then the element loads are not displacement dependent.

### 7.4.3.11 ES.PARS

Array of element research parameters. Meaning depends on specific element type. Consult appropriate section in CSM Testbed User's Manual, ref. 7.4-2.

### 7.4.3.12 ES_PROC

Name of element (ES) i processor to be executed (e.g., ES1, ES2, ...); currently relevant only as an argument for procedure ES, and only when argument FONCTION = 'DEFINE ELEMENTS'.

### 7.4.3.13 ES_ROT_DS

Name of system rotation pseudo-vector dataset in SYSVEC format (default: STAT.ROTA.1.1). Relevant for most FORM commands during geometrically nonlinear analysis; but only if elements with rotational freedoms are involved.

### 7.4.3.14 ES_STR_LDC

Element stress/strain location option (default: 'CENTROIDS'). Indicates where stresses or strains in datasets defined by <ES_STRESS_DS> or <ES_STRAIN_DS> (respectively) will be computed. Relevant only for FUNCTION $=$ 'FORM STRAIN' or 'FORM STRESS'. Currently valid options:

- CENTROIDS $\Rightarrow$ element centroids; creates record group:

CENTROIDS_<ES_STR_DIR>.1:nel

- NODES $\Rightarrow$ element nodes; creates record group: NODES_<ES_STR_DIR>. $1:$ noel
- INTEG_POINTS $\Rightarrow$ element integration points; creates: IMTEG_PTS_<ES_STR_DIR>.1:nel
where "noel" is the number of elements in the dataset, and where macrosymbol ES_STR_DIR designates the directions of the stress/strain components, and is defined elsewhere in this glossary.


## 7．4．3．15 ES＿STR＿DIR

Element stress／strain direction option（default：E）．Indicates in which coordinate system element stresses or strains in datasets defined by＜ES＿STRESS＿DS＞or＜ES＿STRAIN＿DS＞（re－ spectively）will be computed．Relevant only for FUNCTION＝＇FORM STRAIN＇or＇FORM STRESS＇．Currently valid options include E for the element stress coordinate system，M for the material coordinate system，and $G i$ for the coordinate system whose $x$ axis corresponds to global coordinate axis $\boldsymbol{x}_{\boldsymbol{i}}$ ．

## 7．4．3．16 ES＿STRAIN＿DS

Third part of element strain dataset name．The first name is always STRN；the second name is always the element－type name，i．e．，＜ES＿MAME＞；and the third name， ＜ES＿STRAIN＿DS＞must be a string of integers separated by periods（see CSM Testbed Data Library Description，reference 7．4－3）．For example，if 〈ES＿STRAIN＿DS＞＝＜step〉．＜iter＞ where＜step＞$=20$ and＜iter＞$=3$ ，and if the element－type name were EX97，then the full dataset name would be：STRN．EX97．20．3．Relevant only for FUNCTION＝＇FORM STRAIM＇．No default；absence means that strains will be stored（embedded）within dataset EFIL．＜ES＿NAME＞only－currently not implemented．

## 7．4．3．17 ES＿STRESS＿DS

Third part of element stress dataset name．The first name is always STRS；the second name is always the element－type name，i．e．，＜ES＿NAME＞；and the third name，＜ES＿STRESS＿DS＞ must be a string of integers separated by periods same as previously stated．For example， if 〈ES＿STRESS＿DS＞$=$＜step＞．＜iter＞，where＜step＞$=20$ and＜iter＞$=3$ ，and if the element－type name were EX97，then the full dataset name would be：STRS．EX97．20．3． Relevant only for FUNCTION＝＇FORM STRESS＇．No default；absence means that stresses will be stored（embedded）within dataset EFIL．〈ES＿NAME＞only．

## 7．4．3．18 ES＿SOM＿DS

Name of ES summary dataset，which contains nominal records corresponding to most of the macrosymbol parameters appearing in this glossary－for each ESi processor／element defined in the model（default：ES．SUMMARY）．Relevant for all ES commands．

### 7.4.3.19 PUNCTION

All structural element (ESi) processors based on the generic element processor template, share the same processor commands. This makes it easier for the User, and enables the construction of a generic command procedure to handle any combination of ESi processors. The commands recognized by ESi processors fall into three categories: INITIALIZE, DEFINE, and FORM, which roughly correspond to preprocessing and computation phases of analysis. The IMITIALIZE command initializes the element data. The DEFINE commands are used to prepare or re-format model definition datasets, such as element connectivity, freedom activity, loads, etc.* The FORM commands are used to form element computational data, such as stiffness matrices, force vectors, etc. Table 7.4-5 provides a summary of ES processor commands and their respective functions.

[^1]| Table 7.4-5 Summary of Generic ES Processor Commands |  |  |
| :---: | :---: | :---: |
|  | Command | Description |
| INITIAL |  | Initialize element data |
| DEFINE | ELEMENTS FREEDOMS | Define element parameters Perform automatic DOF suppression |
| FORM | ```STIFFNESS [/MATL/GEOM/LOAD/TANG] FORCE [/INT/EXT/RES/DYN] MASS [/CONS/DIAG] STRAIN STRESS``` | Form element stiffness <br> Form element force <br> Form element mass <br> Form element strains <br> Form element stress |

In addition to these commands, ESi processors can be controlled with a number of built-in macrosymbols, all of which begin with ES_. The macrosymbols typically set logical switches and/or control parameters, and allow re-assignment of database names from their default values.

| Table 7.4-6 ANALYSIS/COMMAND CORRESPONDENCE <br> ES Processor Commands vs Analysis Type |  |
| :---: | :---: |
| Analysis Type | Processor Commands |
| All Preprocessing | INITIALIZE <br> DEFINE ELEMENTS <br> DEFINE FREEDOMS |
| Linear Statics | FORM STIFFNESS/MATL FORM FORCE/EXT |
| Linear Dynamics | FORM STIFFNESS/MATL FORM MASS/CONS FORM FORCE/EXT |
| Buckling Eigenvalue | FORM STIFFNESS/MATL FORM STIFFNESS/GEOM FORM FORCE/EXT |
| Vibration Eigenvalue | $\begin{aligned} & \text { FORM STIFFNESS/MATL } \\ & \text { FORM MASS } /\{\text { CONS \\| DIAG }\} \end{aligned}$ |
| Nonlinear Statics | FORM STIFFNESS/TANG FORM FORCE/INT FORM FORCE/EXT FORM FORCE/RES |
| Nonlinear Dynamics | FORM STIFFNESS/TANG FORM MASS/\{CONS \| DIAG\} FORM FORCE/INT FORM FORCE/EXT FORM FORCE/DYN |

### 7.4.4 PROCEDURE FLOWCHART

| ES | (main procedure) |
| :--- | :--- |
| ES_DOFS | (automatic DOF suppression for ESi) |

### 7.4.5 LIMITATIONS

Procedure ES assumes that all datasets either required or generated will reside on library one ( $\mathrm{LDI}=1$ ).

### 7.4.6 ERROR MESSAGES AND WARNINGS

None.

### 7.4.7 USAGE GUIDELINES AND EXAMPLES

Procedure ES may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.


| ES_DOF_DS = | ES.DOFS | ; -- . Active-freedom dataset |
| :---: | :---: | :---: |
| ES_ECC_DS = | ES. ECCEN | ; -- . Eccentricity dataset |
| ES_FRC_DS * | STAT.REAC | ; -- . Force-vector dataset |
| ES_ROT_DS = | STAT.ROTA | ; -- . Rotation-vector dataset |
| ES_SUM_DS | ES SUMMARY | ; -- . ES sumary dataset |
| ES_STRAIN_DS | $=\langle f a l s e\rangle$ | ; -- . Element strain dataset |
| ES_STRESS_DS | $=\langle f a l s \theta\rangle$ | ; -- . Element stress dataset |
| ES_STR_LOC | * 'CENTROIDS' | ; -- . Stress locations |
| ES_STR_DIR | $={ }^{\prime} E$ ' | ; -- . Stress directions |
| NOM_CON_DS | $=1$ | ; -- . No. of constraint datasets |
| LDI | $=1$ | -- . Logical device index |

The following examples illustrate how element processors based on the generic structuralelement (ES) processor template can be used to perform structural analysis with the CSM Testbed. For simplicity, we consider preprocessing (i.e., model generation), linear analysis, nonlinear analysis, and postprocessing (i.e., stress recovery, etc.) examples separately. The differences between employing individual ESi processors directly versus accessing them using the generic ES procedure interface will be stressed, with an intended bias towards the latter.

### 7.4.7.1 Preprocessing Examples

For clarity, a very simple problem will be considered, and the use of the generic structuralelement processor illustrated by showing all of the steps involved in generating a finite element (FE) model for this problem. Both the physical problem and the discrete model to be used is given in Figure 7.4-1. The problem is a rectangular plate ( 10 in . by 5 in .), cantilevered on one edge, and loaded on the other by a concentrated lateral force. For the model, a 3 by 3 grid is used which corresponds to a 2 by 2 mesh of 4 -node plate/shell elements. The Testbed procedure for this model is given in Figure 7.4-2. The interpretation of each line of the procedure will now be described.

The *procedure statement in Figure 7.4-3 shows the arguments (parameters) for the procedure and sets default values for each of them ( $x$-length, $y$-length, thickness, elastic modulus, Poisson's ratio, and precision). Thus the dimensions and properties of the plate model are parameterized, but the finite element discretization is fixed. $\dagger$ The next two lines ([xqt TAB and START 9) run the processor TAB and reserve space for a total of 9 nodes. Then, the JLOC command and subsequent data define the global coordinates for these 9 nodes in a rectangular 3 by 3 grid.

Material and section properties are then defined by first executing processor AUS to tabulate the raw data, and then executing processor LAU to generate an integrated constitutive matrix for shell elements (see the CSM Testbed User's Manual for details on processor LAU).

The key portion of the example begins with the *call to procedure ES with FUNCTION = 'DEFINE ELEMENTS', in which element type EX42 of processor ES1 is registered for participation in the model. This call also causes a number of element type-oriented macrosymbols, all beginning with ES_, to be defined - for example, ES_NEN (number of element nodes), ES_NIP (nuber of element integration points), etc. These macrosymbol values are automatically built into the character string macrosymbol ES_EXPE_CMD (by procedure ES), which serves as the EXPE command for processor ELD. Note that in the PLATE_MODEL example, <ES_EXPE_CMD> appears immediately after [XQT ELD (execute processor ELD). This sequence causes the ES_EXPE_CMD macrosymbol to expand internally into the following commmand line:

which would eventually decode into:

| EXPE | EX42 | 4 | 2 | 4 | 6 | 0 | 1 | 102 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

The execution of processor ELD with the above EXPE command is necessary for generation of various element datasets such as DEF.EX42.* and DIR.EX42.* (see the CSM Testbed

[^2]User's and Dataset Manuals, references 7.4.2 and 7.4-3, respectively). Note that the ES_ macrosymbols referenced in this example are all described in the Macrosymbol Glossary in Table 7.4-4.

Next, the NSECT command is used as a section property pointer. HSECT=1 means that the integrated constitutive matrix stored in the first column of dataset PROP.BTAB.2.101 will be employed by all elements whose nodal connectivity is defined on the following lines. The element nodal connectivity is then defined for four 4 -node elements. Note that the numbering convention is counter-clockwise within each element (see Fig. 2.2-1). Boundary conditions and loads are then defined using the CON command of processor TAB, and the SYSVEC command of processor AUS, respectively (see Figure 7.4-2). The CON command suppresses all freedoms along $x=0$ (the built-in edge), and the SYSVEC command distributes transverse nodal forces along the other edge, which add up to a unit load. Note that both boundary conditions and loads have been defined with respect to nodes rather than elements. Automatic consistent element nodal load generation will be available once the DEFINE LOADS command has been implemented within the ES processor shell.

Finally, procedure ES is called again to perform automatic degree of freedom suppression, using the DEFINE FREEDOMS command. In this case, the effect will be for processor ES1 to suppress drilling rotational freedoms (i.e., the 6 th degree of freedom) at all nodes, since element type EX42 has no stiffness associated with these freedoms. (Note: If the plate had blade stiffeners which were also modeled with EX42 elements, all 6 degrees of freedoms at nodes along the plate/stiffener intersection lines would be retained, since at least one of the intersecting elements at those nodes would possess the necessary stiffness.)

```
*Procedure PLATE_MODEL ( Lx=10.; Ly=5.; h=.1; E=1.e7; PR=.3; prec=2 )
    [xqt TAB
    START 9
GENERATE NODES ( rectangular grid, 3 x 3 nodes)
        JLOC
            1 0., 0., 0. [Lx], 0., 0. 3, 1, 3
            3 0., [Ly], 0. [Lx], [Ly], 0.
. tabulate material and section Properties
    [xqt AUS.
        TABLE(NI=16,NJ=1): OMB DATA 1 1..
        I=1,2,3,4,5,6 : J=1 : [E] [PR] [E] <G> <G> <G>
        TABLE(NI=3,NJ=1,ITYPE=0): LAM OMB 1 1
        I=1,2,3 . : J=1: 1 [h] 0.0.
RUN CONSTITUTIVE PRE-PROCESSOR
    [xqt LAU
GENERATE ELEMENTS
    *call ES ( function='DEFINE ELEMENTS'; ES_PROC=ES1; ES_MAME=EX42 )
    [xqt ELD
        <ES_EXPE_CKD>
        HSECT = 1
            elt 1, l
```

Figure 7.4-1 Sample Preprocessing Procedure.

- IMPOSE BOUNDARY CONDITIONS
[rqt TAB
CON
ZERO 1:6 : 1 : 4 : 9
. APPLY LOADS
- [xqt AUS

SYSVEC : APPL FORC 1 $\mathrm{i}=3$ : $\mathrm{j}=3$ : . 25 : $\mathrm{i}=3$ : $\mathrm{j}=6$ : . 50 : $\mathrm{i}=3$ : $\mathrm{j}=9$ : . 25

## *call ES (function = 'DEFINE FREEDOMS' )

*end

Figure 7.4-2 Sample Preprocessing Procedure.

### 7.4.8 Linear Analysis Examples

A sample linear static analysis procedure, which employs the procedure ES to invoke the appropriate ESi processors is shown in Figure 7.4-4. For purposes of illustration, the problem has been kept simple (notice that there are no procedure arguments), but keep in mind that many analysis procedures may involve more sophisticated features. The procedure in Figure 7.4-4 can be read as follows. The [xqt E directive causes processor E to construct *.EFIL.* datasets for all participating element types. Note that, while space for these datasets is reserved in the database, meaningful data has not yet been deposited there.

The first call to procedure ES then causes INITIALIZE to be stored in the EFIL datasets by all participating ESi processors - as prescribed by previous calls to procedure ES with function = 'DEFINE ELEMENTS'. For example, if the preprocessing example given in Figure 7.4-3 had preceded the call to L_STATIC, then only processor ES1, element type EX42, would be invoked to INITIALIZE. More information on the effect of the INITIALIZE command may be found in Section 2.2. The second call to procedure ES is to form the element material (linear) stiffness matrices for all elements in the model using *call ES (function='FORM STIFFNESS/MATL'). The element matrices are deposited in Segment 5 of the EFIL dataset. Since no other arguments are employed in this call to the procedure ES, the default values are implied. Thus, for example, the problem is assumed to be linear (ES_NL_GEOM $=0$ ), and there is no need for a displacement dataset (whose name is given by argument ES_DIS_DS) to be input by the ES Processors.

Next, assembly of the element stiffness matrices into a system matrix is performed by processor K. Note that the element matrices have already been transformed to the computational (nodal degrees of freedom) bases, so that the function of processor $K$ is merely to add appropriate submatrices.

Finally, processors INV and SSOL are executed in order to factor and solve the assembled system of equations, respectively. The displacement solution will be stored, as indicated by the RESET command for processor SSOL, in dataset STAT.DISP.1.1.

```
*procedure L_STATIC
**
- Initialize Element Datasets
    [xqt E
O-
. Initialize Element Computational Data
*call ES ( function = 'INITIALIZE' )
Form Element Material Stiffness Matrices
*call ES (function = 'FORM STIFFNESS/MATL' )
•
Assemble Material Stiffness Matrix
    [xqt K
•
. Factor Stiffness Matrix
- -------------------------
    [xqt INV
Solve for Displacements
    [XQT SSOL
    RESET SET=1, CON=1
*end
```

Figure 7.4-3 Sample Linear Static Analysis Procedure

### 7.4.9 Nonlinear Analysis Examples

A brief example of how to employ ESi processors in nonlinear analysis procedures, by including selected excerpts from an actual nonlinear static analysis procedure that will
hopefuliy convey the essential aspects. Typically, engineering-oriented users wiil invoke an existing nonlinear analysis procedure rather than writing their own, so this example is intended more for researchers involved in algorithm development.

The "skeleton" of a nonlinear static analysis procedure is shown in Figure 7.4-5, with only those aspects involving ESi processors shown. There is very little difference in the use of the procedure ES to invoke ES processors from what was employed in the linear static analysis procedure compare with Figure 7.4-4, except that some additional arguments must be explicitly defined.

First, the usual call to INITIALIZE for all ESi processors is present. This call enables the participating element processors to generate, and store, any data that will be used repeatedly during the analysis - rather than having to recompute it at each iteration of every analysis load step.

Next, the nested load-step and iteration loops, typical of most incremental/iterative nonlinear solution algorithms for structural analysis are encountered. Within these loops, it is necessary to compute residual force vectors (right-hand sides) at each iteration and tangent stiffness matrices at selected load steps/iterations.

The assembled residual force vector is computed by first initializing a system internal force vector (using processor VEC), calling the procedure ES to form/assemble all element contributions to the internal force vector, and finally subtracting the assembled internal force vector from a load-step scaled external force vector, which is assumed to have been generated elsewhere.

Notice that in the FORM FORCE/INT call to procedure ES, arguments ES_NL_GEOM, ES_CORO, ES_DIS_DS, ES_ROT_DS and ES_FRC_DS are each explicitly defined. The reader is urged to look up these arguments in the Macrosymbol/Argument Glossary, Table 7.4-4. These arguments let the ESi processors know that the problem is geometrically nonlinear (both globally and at the element level). The corotational algorithm is to be employed to make the rotational motion "appear" small at the element level, but allow it to be arbitrarily large globally. The current displacement dataset is called TOT.DISP.<\$step>, where <\$stop> is the load-step number; the current rotation (pseudo-vector) dataset is called

TOT.ROTA.〈\$step〉; and the current system internal force vector into which the element contributions are to be assembled is called INT.FORC.<\$step>.

Finally, the formation/factorization of the tangent stiffness matrix is shown in Figure 7.4-5 which involves first the formation/transformation of the element tangent stiffness matrices by ESi processors, which are deposited in the *.EFIL.* datasets; then the assembly of the element matrices into the system tangent stiffness matrix by processor K ; and finally the factorization of the assembled (system) tangent stiffness matrix by processor INV. Note that both material and geometric stiffness contributions have been superimposed at the element level.

```
*procedure NL_STATIC ( NUM_STEPS = 1; NOM_ITERS = 10 )
Initialize Element Computational Data
    #call ES (function = 'INITIALIZE' )
    :
    *do $step = 1, [NUM_STEPS]
    *do $iter = 1, [NOM_ITERS]
        FORM RESIDOAL FORCE VECTOR
        [xqt VEC
            INT.FORC <- O.
            *call ES (function = 'FORM FORCE/INT'; --
                        es_nl_geom = 2; es_coro = 1; --
                                es_dis_ds = TOT.DISP.<$step>; --
                                es_rot_ds = TOT.ROTA.<$step>; --
                                es_frc_ds = INT.FORC.<$step>)
        [xqt vEC
        RES.FORC <- <load_factor> * EXT.FORC - INT.FORC.<$step>
. :
            FORM/FACTOR TANGENT STIFFNESS MATRIX
        *call ES (function = 'FORM STIFFNESS/TANG' ; --
                        es_nl_geom = 2; es_coro = 1; --
                        es_dis_ds = TOT.DISP.<$step>; --
                                es_rot_ds = TOT.ROTA.<$step>; --
                                es_frc_ds = INT.FORC.<$step>)
        [xqt K
        [xqt INV
    :
    *enddo
    *enddo
```

Figure 7.4-4 Sample Nonlinear Static Analysis Procedure Excerpts

### 7.4.10 Postprocessing Examples

By postprocessing refers to functions which can be performed after the displacement solution has been obtained for a linear or nonlinear structural analysis. For example, in a nonlinear static (or transient) analysis, the user may choose not to archive the stresses and strains which were used as intermediate variables during the process of obtaining a displacement solution history. The user may then compute stresses and/or strains at selected load (or time) steps and save these in the database for perusal. The end-user phase of postprocessing is of course the actual printing or display of the results (displacements, stresses, strains, etc.); however, the main interest here is in the prerequisite functions that are performed by ESi processors.

An example of a postprocessing procedure that employs ESi processors to form, and archive in the database, both stresses and strains after the mainstream analysis has already been performed. Procedure STRESS_STRAIN contains arguments to select the stress/strain locations (the default is at element centroids), component directions (the default is in the element local stress/strain coordinate system), existing displacement and rotation (for nonlinear analysis) datasets to be employed for strain computation.

Note that there is a step loop in the procedure, and that both stresses and strains for all participating elements are formed by just a single call to procedure ES per step. This is because the FORM STRESS command automatically causes strains to be formed as well as stresses, and when both ES_STRAIN_DS and ES_STRESS_DS are explicitly defined, then both of these quantities are also output to the database.

```
*procedure STRESS_STRAIN ( LOCATION = CENTROIDS ; DIRECTION = 0 ; --
    NL_GEOM = 0 ; CORO =0 ; --
    NOM_STEPS = 1 ; STEPS = 1:1 ; --
    DIS_DS = TOT.DISP ; ROT_DS = TOT.ROTA )
```

- Loop on Solution Steps
*def/i steps[1:[num_steps]] = [steps]
*do $\backslash \$ i s=1$, [num_steps]
*def/i step $=$ <steps [<<br>\$is>]>
Invoke Element Processors to Form Stress/Strain
*call ES ( function $=$ 'FORM STRESS'
es_nl_geom $=[$ nl_geom $] \quad ;-$ -
es_coro $=$ [coro] ; --
es_dis_ds $=\left[D I S \_D S\right] .\langle s t e p\rangle ;--$
es_rot_ds $=$ [ROT_DS].<step> ; --
os_str_dir $=$ [DIRECTION] ; --
es_str_loc $=$ [LOCATION] ; --
es_strain_ds $=$ 〈step> ; --
es_stress_ds $=$ 〈step> )
*onddo
*end

Figure 7.4-5 Sample Postprocessing Procedure

### 7.4.11 PROCEDURE LISTING

```
*procedure ES ( function ; --
\begin{tabular}{ll} 
es_proc & ; -- \\
es_name & ; -- \\
es_pars & ; --
\end{tabular}
```

```
beg_update 06_MAY_1089 [GMS] ES_COUNT
    es_count = 0 ; -- . 0/1=>create/accur ES.SUMMARY
- ond_update
\begin{tabular}{|c|c|}
\hline \multicolumn{2}{|l|}{en_nl_geon \(=0\); --} \\
\hline \multicolumn{2}{|l|}{es_nl_matl \(=0\); --} \\
\hline \multicolumn{2}{|l|}{es_nl_load \(=0\); --} \\
\hline es_dis_ds = STAT.DISP.1.1 & ; -- \\
\hline es_dof_ds \(=\) ES \({ }^{\text {d }}\) DOFS & ; -- \\
\hline es_ecc_ds = WILL.PROP & ; -- \\
\hline es_frc_ds \(=\) INT.PORC.1.1 & ; -- \\
\hline -8_rot_ds = STAT.ROTA.1.1 & ; -- \\
\hline es_sum_ds = ES.SUMMARY & ; -- \\
\hline es_mass_diag = DEM & ; -- \\
\hline es_strain_ds = , & ; -- \\
\hline es_stress_ds \(=\), , & ; -- \\
\hline es_str_loc \(=\) CENTROIDS & ; -- \\
\hline es_str_dir \(=0\) & ; -- \\
\hline num_con_ds \(=1\) & \\
\hline
\end{tabular}
- beg_update 26_APR_1989 [GMS] CONSISTENT LOADS
```

```
    es_load_factor \(=1.0 \quad\);-
```

    es_load_factor \(=1.0 \quad\);-
    es_load_set \(=1 \quad\); -
    ```
    es_load_set \(=1 \quad\); -
```

- end_update 26_APR_1989 [GMS] CONSISTENT LOADS
ldi
= 1 )
- Generic Procedure for Structural Elenent (ES) Processors
$\qquad$

```
*if < <IFELSE([function];DEFINE ELEMENTS;1;0)> >/thon
    *dof/a es_proc = [es_proc]
    *dof/a es_name = [es_name]
    *def/d es_pars[1:10] = [es_pars]
    *def/a es_sum_ds = [es_sur_ds]
        Initialize ES SOMMary Dataset
        *find dataset [1di] <es_sum_ds> /seq=es_ids
. beg_update 06_MAY_1989 [GMS] ES_CDUNT
        *if <<<es_ids> /1e 0 \rangle /or < [es_count] /eq 0 > >/thon
            *put dataset [ldi] <es_sum_ds> /|rat=2000 /seq=es_ids
            *def/i es_num = 1
        *else
            *find record [1di], <es_sum_ds>, ES_PROC /nor=es_num
            *dof/i es_nur = < <es_nun> + 1 >
        *endif
- ond_update
        *n2g /name=mes_proc /type=a [ldi] <es_ids> ES_PROC.<0E_num>
        *=2g/nare==0s_name /type=a [ldi] <es_ids> ES_MAME.<es_num>
        *m2g/name==es_pars /type=d /maxn=10 [ldi] <es_ids> ES_PARS.<es_num>
```

. -----------------

- Run ES Processor
. ------------------
[1qT 〈es_proc>
[function]

```
- Define macrosyabol for ELD/EIPE command
    *if <<es_stor>/gt 0 >/then
        #def/i es_net = < (<<es_stor>-1)/\langlees_nen>) + 1 >
        *-18*
            *def/i es_nst = 1
        *endil
. BEG_OPDATE MAY_5_1989 [SNO] EXPE CHANGE
    *def/a ES_EXPE_CMD=m'EXPE '[es_name]' '<es_nen>' '--
    &def/a ES_EIPE_CMD=F'EXPE '[@s_name]' '4' '--
. END_OPDATE
<es_opt\rangle' '\langlees_nen\rangle' '\langleबs_ndof\rangle' ,\langlees_nst\rangle' 1 10'<es_din>' '<csm_precision>
*01:*
    *find dataset [ldi] [es_sum_ds] /seqzes_ids
    *def/a es_mass_diag =x [es_mass_diag]
    *del/a es_mase_ds zx [es_mass_diag].DIAG
•
. ----------------------------------------------------
. Find Number of Element Processors from Database
    *ind record [ldi], <es_ids>, ES_PROC /nor=num_es_proc
    *if < <num_es_proc>/1e 0 >/then
        *remark Cannot find any ES Processor names in dataset [es_sur_ds]
```

e
＊endif

＊call ES＿DOFS（ function＝IMITIALIZE；es＿dof＿ds＝［es＿dof＿ds］）
＊endif

Process all Elemont Processors Found
＊do \＄ies $=1$ ，＜num＿es＿proc＞
＊g2n／name＝＝ES＿PROC／type＝a［ldi］＜es＿ids＞ES＿PROC．＜\＄ies＞
＊g2n／name＝＝ES＿NAME／type＝a［ldi］〈es＿ids＞ES＿NAME．〈\＄ies＞
＊g2n／namex＝ES＿PARS／type＝d［1di］＜es＿ids＞ES＿PARS．〈\＄ies＞
＊g2n／namex＝ES＿NSTR／type＝d［1di］＜es＿ids＞ES＿NSTR．＜\＄ies＞
＊def／i ES＿CORO＝［es＿coro］
＊dof／e ES＿DIS＿DS＝［es＿dis＿ds］
＊def／a ES＿DOP＿DS＝［es＿dot＿ds］
＊def／a ES＿ECC＿DS＝［es＿ecc＿ds］
＊def／i ES＿FIKI＝［es＿fikx］
＊def／a ES＿FRC＿DS＝［es＿frc＿ds］
＊def／i ES＿ML＿GEOM＝［es＿nl＿geon］
＊def／i ES＿ML＿LOAD $=$［es＿nl＿load］
＊def／i ES＿NL＿MATL＝［es＿nl＿matl］
＊def／a ES＿ROT＿DS＝［es＿rot＿ds］
－beg＿update 26＿APR＿1989［GMS］CONSISTENT LOADS
＊def／g ES＿LOAD＿FACTOR＝［es＿load＿factor］
＊def／i ES＿LOAD＿SET＝［es＿load＿set］
．end＿update 26＿APR＿1989［GMS］CONSISTENT LOADS

```
    *def/a ES_STR_DIR = [en_str_dir]
    *def/a ES_STR_LOC = [0s_str_loc]
    *if < <IPELSE([es_strain_ds]; ;0;1)> > /then . (if not blank)
        *det/a ES_STRAIN_DS = [0s_strain_ds]
    *endif
    *if <<IFELSE([0s_strons_ds]; ;0;1)>> /thon . (if not blank)
        *dof/a ES_STRESS_ds = [es_strese_ds]
        *endif
        [XQT <es_proc>
        [function] . DEFINE FREEDOMS | FORM FORCE | STIFPNESS | ...
    * enddo
    *if < <IPELSE([function];DEFINE FREEDOMS;1;0)> > /then
    *call ES_DOPS ( function=PINALIZE; ez_dof_ds=[es_dof_ds]; --
        nu__con_ds=[num_con_ds] )
    *ondif
*endif
STOP
*and
. =DECK ES_DOFS
*procedure ES_DOFS ( {unction=INITIALIZE; es_dof_ds=ES.DOFS; --
                        num_con_ds=1; ldi=1 )
        *if < <IFELSE([function];INITIALIZE;1;0)> > /then
    *renark
    *remark ES_DOFS: Performing Autonatic DOF Suppression for ES Elts
    *def/i ns_overurite m= <true>
    Initialize Eloment DOF Dataset
```

```
    ------------------------------
    *g2m /namexparaneters /typexi /maxn=18 [Idi] JDF1.BTAB.1.8 DATA.1
    *def/i num_nodes = <parameters[1]>
    *dof/i num_dols = <parameters[2]>
    [xq] vec
    IMIT_TAB [es_dof_ds] <num_dofs> BY <num_nodes>
*olsoif < <IPELSE([function];FINALIZE;1;0)> >/thon
    Morge Element DOF Dataset vith Constraint Datasets
    *def/i num_cds = 0
    *do $cds = 1, [num_con_ds]
        *def/a con_ds = com..<$cds>
        *ind dataset [ldi], <con_ds>/seqzid_cds
        *if <<$cds>/oq 1 >/then
        [xqT vEC
        *endif
        *if <<id_cds>/gt 0 >/then
            *ronark ES_DOFS Processing Constraint Dataset: <con_ds>
            MERGE_DOF [es_dof_ds] -> <con_ds>
            *def/i num_cds = < <num_cds> + 1 >
        *endif
    *enddo
    *remark
    *renark ES_DOPS Processed <num_cds> Constraint Datasets
    *r*nark
    *def/i ns_overwrite ={ <false>
```


## *endif

## * ond

### 7.4.12 REFERENCES

7.4-1 Stanley, G. M.; and Nour-Omid, S.: The Computational Structural Mechanics Testbed Generic Structural-Element Processor Manual. NASA CR-181728, March 1990.
7.4-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Users Manual. NASA TM-100644, October 1989.
7.4-3 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

### 7.5 Procedure FACTOR

### 7.5.1 GENERAL DESCRIPTION

Procedure FACTOR decomposes or factors a system matrix using a solver defined by the global macrosymbol solver_name. If solver_name is defined to be INV, the original nodalblock sparse solver implemented in processor INV will be used (see Section 6.7 of reference 7.5-1). If solver_name is defined to be BAND, a variable-bandwidth direct solver implemented in processor BAND will be used (see Section 8.5 of reference 7.5-1).

### 7.5.2 PROCEDURE USAGE

Procedure FACTOR is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are orderindependent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call FACTOR ( arg1 = val1 ; arg2 = val2 ; ...)
```

where argi and arg 2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure FACTOR are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure FACTOR, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning <br> CONSTRAINT_SET |
| :--- | :---: | :--- |
| INPUT_MATRIX | 1 | Konstraint set number <br> First word of the name of the dataset containing <br> the assembled stiffness matrix |
| OUTPUT_MATRIX | $K$ | Second word of the name of the dataset containing <br> the factored system stiffness matrix |
| INPUT_LDI | 1 | Logical device index for input_matrix |
| OUTPUT_LDI | 1 | Logical device index for output_matrix |

Tables 7.5-1 and 7.5-2 list the datasets used or created by procedure FACTOR and the processors invoked by procedure FACTOR, respectively.

| Table 7.5-1 Datasets Input/Output by procedure FACTOR |  |  |  |
| :--- | :--- | :---: | :---: |
| Dataset | Description | Input | Output |
| AMAP..ic2.isize | Factorization Map for INV | $\sqrt{ }$ |  |
| CON.. $\boldsymbol{j}^{\dagger}$ | Constraints | $\sqrt{ }$ |  |
| INV.O_M. ${ }^{\dagger *}$ | Factored Stiffness Matrix |  | $\checkmark$ |
| JDF1.BTAB.1.8 | Model Summary | $\sqrt{ }$ |  |
| JSEQ.BTAB.2.17 | Nodal Elimination Sequence | $\sqrt{ }$ |  |
| KMAP..nsubs.ksize | Model Connectivity Map | $\sqrt{ }$ |  |
| I_M.SPAR.jdf2** | Assembled Stiffness Matrix | $\sqrt{ }$ |  |


| Table 7.5-2 |  |  |
| :--- | :--- | :--- | Processors Invoked by procedure FACTOR

### 7.5.3 ARGUMENT DESCRIPTIONS

### 7.5.3.1 CONSTRAINT_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.5.3.2 INPOT MATRIX

First word of the dataset name containing the assembled stiffness matrix (default: $\mathbb{K}$ ).

### 7.5.3.3 OUTPUT.MATRIX

Second word of the dataset name containing the factored system stiffness matrix (default: K ). This notation is only valid if the macrosymbol solver_name is set to INV.

### 7.5.3.4 INPUTLDI

Input logical device index containing the input matrix (default: 1).

### 7.5.3.5 OUTPUT_LDI

Output logical device index containing the output matrix (default: 1).

### 7.5.4 USAGE GUIDELINES AND EXAMPLES

Procedure FACTOR may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call FACTOR ( INPUT_MATRIX = K ; CONSTRAINT_SET = 1 )
```

Before procedure FACTOR is called, the global macrosymbol solver_name should be defined as described in Section 7.5.1; otherwise, the default value of INV will be used.

### 7.5.5 LIMITATIONS

None.

### 7.5.6 ERROR MESSAGES AND WARNINGS

None.

### 7.5.7 PROCEDURE FLOWCHART

Procedure FACTOR is self-contained with no subprocedures.

### 7.5.8 PROCEDURE LISTING

```
*procedure fICTOR ( input_matrix = K ; output_matrix = K ; --
    input_ldi = 1 ; output_ldi = 1; --
    constraint_set = 1)
. Procedure to factor a systen matrix using different solvers.
. The solver is selected using the global macrosymbol "solver_name".
*if < ifeqs( <solver_name>; ) > /then
*def/a solver_name == INV
*endif
```

```
*if < ifeq:( <solver_name>;INV) > /then
. Dse original nodal block sparse solver originally in SPAR
[XQT INV
    reset X = [input_matrix]
    reset KLIB = [input_ldi]
    reset KILIB = [output_ldi]
    reset CON = [constraint_set]
    reset LLL =40000
    reset DZERO = 1.E-20
    reset spdp = <csm_precision>
*elseif < ifeqs( <solver_name>;BAND) > /then
. Use Banded solvor
[XqT BAND
        reset neth=28, ldl=1, klib=[input_ldi]
        reset ncon=[constraint_set], dzero=1.0e-20, k=[input_matrix]
        reset opt=1, res=-1
*endif
STOP
. Define factored-matrix parameters as global nacrosymbols
-
*if < ifeqs( <solver_name>;ITER) > /then
    *def/e coef_det == 1.0E+01
    *def/i exp10_det == 1
    *def/i num_neg == 0
    *def/i sign_det =x 1
*0lse
    *romark Determinant of [input_matrix] = <coef_det> * 10 ** <exp10_det>
    *renark Number of negative roots = <num_neg>
    *def/i sign_det == <SIGN(1.;<coof_det>)>
*endif
*end
```


### 7.5.9 REFERENCES

7.5-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.6 Procedure FORCE

### 7.6.1 GENERAL DESCRIPTION

Procedure FORCE drives the calculation of force vectors for either linear or nonlinear analyses.

### 7.6.2 PROCEDURE USAGE

Procedure FORCE may be used by preceding the procedure name by the *call directive, and following it by a list of arguments separated by semicolons (;) and enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call FORCE ( arg1 = val1 ; arg2 = val2 ; ...)
```

For procedure FORCE, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| corotation | 1 | Corotational flag (0, 1, 2) |
| DISPLACEMENT |  | First two words of displacement dataset name |
| LDI | 1 | Logical device index |
| LOAD_SET | 1 | Load set number |
| LOAD_FACTOR | 1.0 | Load factor |
| NL_GEOM | 0 | Geometric nonlinearity flag |
| NL_LOAD | 0 | Nonlinear load terms (live terms) |
| NL_MATL | 0 | Material nonlnearity flag |
| ROTATION |  | First two words of rotation-vector dataset name |
| TYPE | RESIDUAL | Type of force vector (residual, external, internal) |
| INPUT_FORCE |  | Input force vector dataset name |
| OUTPUT_FORCE | SYS. FORCE | Output force vector dataset name |

Tables 7.6-1, 7.6-2, and 7.6-3 list the datasets used or created by procedure FORCE, the procedures invoked by procedure FORCE, and the processors invoked by procedure FORCE, respectively.

Table 7.6-1 Datasets Input/Output by procedure FORCE

| Dataset | Description | Input | Output |
| :--- | :--- | :---: | :---: |
| ES.SUMMARY | ES Processor Status | $\sqrt{ }$ | $\sqrt{ }$ |
| INT.FORC.i. $j^{\dagger}$ | System Internal Force Vector |  | $\sqrt{ }$ |
| STAT.DISP.i.j ${ }^{\dagger}$ | System Displacement Vector |  | $\sqrt{ }$ |
| STAT.REAC.i.j$\dagger$ | System Reaction Force Vector |  | $\sqrt{ }$ |

$\dagger i=$ <load_set $>$ and $j=$ <cons_set $>$

Table 7.6-2 Sub-procedures Invoked by procedure FORCE

| Procedure | Type | Function |
| :--- | :--- | :--- |
| ES | External | Element utility procedure |
| FORCE |  | Main Procedure |


| Table 7.6-3 Processors Invoked by procedure FORCE |  |  |
| :--- | :--- | :--- |
| Procedure | Type | Function |
| ES $\boldsymbol{i}$ | External | Element processors based on GEP |
| VPRT | Internal | Print SYSVEC-format vectors |

### 7.6.3 ARGUMENT DESCRIPTIONS

### 7.6.3.1 COROTATION

Corotational update switch for large-rotation problems (default: 1). This switch should be set to 1 when the model involves finite elements that require corotation for geometric nonlinearity. This is true of most beam and shell elements, and may be true for some solid (3D) elements used to model shell structures. Consult the appropriate element processor (ESi) section in the CSM Testbed User's Manual (see ref. 7.6-1) for specific guidelines.

### 7.6.3.2 DISPLACEMENT

First two words of the dataset name for the displacement solution.

### 7.6.3.3 INPUT_FORCE

Full dataset name for the input or basic force vector.

### 7.6.3.4 OUTPUT_FORCE

Full dataset name for the output force vector (default: SYS . FORCE).

### 7.6.3.5 LDI

Logical device index (default: 1).

### 7.6.3.6 LOAD_FACTOR

Load factor used to scale the basic applied loads or displacements (default: 1.0).

### 7.6.3.7 NL_GEOM

Geometric nonlinearity level: 0,1 , or 2 (default: 2). A value of zero means that the problem is geometrically linear; a value of one means that the geometric nonlinearity will be handled globally (i.e., using corotational updates only); and a value of two means that the nonlinear element strain-displacement relations will be used in addition to any global treatment of geometric nonlinearity.

### 7.6.3.8 ES_NL_MATL

Material nonlinearity switch. If ES_NL_MATL is greater than zero, then the element is materially nonlinear. If ES_NL_MATL is zero, then the element is materially linear.

### 7.6.3.9 MLLIOAD

Nonlinear loading index for live loads (default: 0 ).

### 7.6.3.10 ROTATION

First two words of the dataset name for the rotation solution.

### 7.6.3.11 TYPE

Type of force vector to form (default: RESIDOAL. This argument selects the type of force vector to form (RESIDUAL, IMTERNAL, or EXTERNAL).

## 7．6．4 USAGE GUIDELINES AND EXAMPLES

Procedure FORCE may be used by preceding the procedure name by the＊call directive． Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called．A space or blank is required between the end of the procedure name and the left parenthesis．If the default values of the procedure arguments are to be used，then only the procedure name is required．

```
*call FORCE ( LOAD_SET = 1 ; INPOT_FORCE = APPL.FORC.[load_set].1;
    OUTPUT_FORCE = EXT.FORC; TYPE = EXTERNAL;
    LOAD_FACTOR = 2.5; LDI = 1 )
```


## 7．6．5 LIMITATIONS

Applicable only to elements implemented using the generic element processor template．

## 7．6．6 ERROR MESSAGES AND WARNINGS

None．

## 7．6．7 PROCEDURE FLOWCHART

| FORCE | （main procedure） |
| ---: | :--- |
| ES | （internal force calculation） |

## 7．6．8 PROCEDURE LISTING

```
*procedure porce ( type \(=\) RESIDUAL ; -- . RESIDUAL | EXTERNAL \(\mid\) INTRRNAL
                                    input_force ; --
    output_force = SYS.FORCE ; --
    load_set \(=1\); --
    load_factor = 1.0 ; --
    nl_geom \(=0 \quad\); --
    nl_matl \(=0 \quad\); --
    nl_load \(=0 \quad\); --
    displacenent ; --
    rotation ; --
    corotation \(=0\); --
    ldi = 1 )
    [xqt VEC
- Initialize Output Force Vector
    *find [ldi] [output_force] /seq=ids_oforce
    *if 〈〈ids_oforce〉/le 0 〉/then
```

```
        *g2n /namexnum_nodes /type=i [ldi] MODEL.SUMMARY NOM_NODES
        *g2m /name=nun_dofs /type=i [ldi] MODEL.SUMHARY NOM_DOPS
        INIT_VEC [output_force] <num_dofs> BY <num_nodes>
    *else
        [output_force] <- 0.
    *endif
    Add Scaled Input Force Vector
    *if <<IPELSE([input_force]; ;0;1)>> /then
        *find [ldi] [input_force] /seq=ids_iforce
        *if <<ids_iforce>/gt 0 >/then
        [putput_force] <- [load_factor] [input_force]
        *ondif
    *endif
    Add Element Forces
- 
    *call ES ( function = 'PORM FORCE/[type]'; --
                ldi = [ldi] ; --
                es_nl_geon = [nl_geon] ; --
                es_nl_load = [nl_load] ; --
                es_coro = [corotation] ; --
                es_dis_ds = [displacenent] ; --
                es_rot_ds = [rotation] ; --
                es_load_factor = [load_factor]; --
                es_load_set = [load_set] ; --
                es_frc_ds = [output_force] )
*end
```


### 7.6.9 REFERENCES

7.6-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 7.7 Procedure IMPERFECTION

### 7.7.1 GENERAI DESCRIPTION

Procedure IMPERFECTION to superpose a set of normalized buckling modes to form an initial geometric imperfection shape. This imperfection shape is then added to the nodal coordinates of the structure. The original nodal coordinates are first copied into another dataset and saved for subsequent use if desired.

### 7.7.2 PROCEDURE USAGE

Procedure IMPERFECTION is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call IMPERFECTION ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg 2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure IMPERFECTION are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure IMPERFECTION, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| AMPS | 1.0 | Amplitude of each buckling mode |
| MODE | 1 | Mode numbers |
| N.MODES | 1 | Number of buckling modes used in computing imperfection shape |
| LDI | 1 | Logical device index |

Processor IMP is used to perform the modal superposition (see reference 7.7-1).

### 7.7.3 ARGUMENT DESCRIPTIONS

### 7.7.3.1 AMPS

Amplitudes of buckling mode shapes (default: 1.0). This argument gives an array of amplitudes for the buckling mode shapes. The array amps has N_MODES entries.

### 7.7.3.2 LDI

Logical device index (default: 1).

### 7.7.3.3 MODE

Buckling mode shape numbers (default: 1). This argument gives an array of mode numbers to be used in generating the initial geometric imperfection shape. The array MODE has N MODES entries.

### 7.7.3.4 NMODES

Number of buckling mode shapes to use (default: 1). This argument gives the total number of buckling mode shapes to be superposed to form the initial geometric imperfection shape.

### 7.7.4 USAGE GUIDELINES AND EXAMPLES

Procedure IMPERFECTION may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call IMPERFECTION ( n_modes=1; modes=1; amps=1.0 )
```


### 7.7.5 LIMITATIONS

Procedure IMPERFECTION only considers normalized buckling modeshapes in forming the initial geometric imperfection shape.

### 7.7.6 ERROR MESSAGES AND WARNINGS

None.

### 7.7.7 PROCEDURE FLOWCHART

| IMPERFECTION | (main procedure) |
| :---: | :--- |
| COPY_DS | (copy datasets) |
| SWITCH_DS | (switch datasets) |

### 7.7.8 PROCEDURE LISTING

```
*procedure IMPERFECTION ( n_modes=1; modes=1; amps=1.0; ldi=1 )
-
- CLAMP Procedure to Superpose Buckling Modes as Initial Imperfections
    *renark
    #remark Inposing Geonetric Imperfections
    #renark
    *remark - - - Saving old nodal coordinates in JLOC.OLD.2.5
        #call COPY_DS ( Iron_ldi=[ldi]; fron_ds = JLOC.BTAB.2.5 ; --
            to_ldi = [1di]; to_ds = JLOC.OLD.2.5 )
            *call SHITCH_DS ( ldix[1di]; --
            ds_1 = JLOC.BTAB.2.5; ds_2 = JLOC.OLD.2.5 )
    *remark
    #remark - - - Adding linear combination of buckling modes to coords
    #renark
        [IQT IMP
            *det/i modes[1:[n_modes]] = [modes]
            *def/e12.4 amps[1:[n_modes]] = [amps]
            #do %in = 1, [n_modes]
            SUPERPOSE <amps[<$im>]> BUCK.MODE.1.1 /mode=<modes[<$im>]> /NORM
            *remark - - - Mode m <modes[<&im>]> , Amplitude = <anps[<$im>]>
            *enddo
*end
```


### 7.7.9 REFERENCES

7.7-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 7.8 Procedure INITIALIZE

### 7.8.1 GENERAL DESCRIPTION

Procedure INITIALIZE performs standard initialization functions and resequencing of the joint.

### 7.8.2 PROCEDURE USAGE

Procedure INITIALIZE is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call INITIALIZE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure INITIALIZE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure INITIALIZE, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| CONSTRAINT_SET | 1 | Constraint set number |
| LDI | 1 | Logical device index |
| Maxcon | 35 | Maximum number of joints connected to any one joint |
| RENUMBER | <false> | Flag to resequence the joints internally |
| RSEQ_METHOD | -1 | Resequencing method |

### 7.8.3 ARGUMENT DESCRIPTIONS

## T.8.3.1 CONSTRAINT_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.8.3.2 MAXCON

Maximum number of joints connected to any one joint (default: 35).

### 7.8.3.3 RENOMBER

Flag to resequence the joints internally (default: <false>).

### 7.8.3.4 RSEQ_METHOD

Resequence method (default: -1). This argument selects which resequencing method to use. The procedure RESEQUENCE is called for this task (see Section 7.12).

### 7.8.3.5 LDI

Logical device index (default: 1).

### 7.8.4 USAGE GUIDELINES AND EXAMPLES

Procedure IMITIALIZE is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
*call INITIALIZE ( LDI = 1 ; CONSTRAINT_SET = 1 ; RENOMBER = 〈true>)

### 7.8.5 LIMITATIONS

None.

### 7.8.6 ERROR MESSAGES AND WARNINGS

None.

### 7.8.7 PROCEDURE FLOWCHART

| INITIALIZE | (main procedure) |
| :---: | :--- |
| ES | (initialize element processor) |
| RESEQUENCE | (resequence the joints) |
| MODEL_SURMARY | (create MODEL_SUMMARY dataset) |

### 7.8.8 PROCEDURE LISTING

```
*procedure INITIALIZE ( renumber=<false>; constraint_set = 1; ldi=1; --
    rseq_method = -1; maxcon = 35 )
- Perform Standard Initialization Functions
. -----------------------------------------
. ---------------------------------
- initialize element configuration
    [XqT E
    *call ES ( function = 'INITIMLIZE'; ldi=[ldi] )
    *lenark Element configuration initialized.
    RESEqUENCE NODES FOR SOLVER EFFICIENCY
    *if < [renumber] > /thon
        *Call RESEQOENCE ( rseq_mothodz[rseq_method]; --
                ldi=[ldi]; maxcon=[aaxcon] )
    *ondif
    CONSTROCT MATRIX TOPOLOGY MAPS
        [xQT TOPO
            reset maxsub = 100000, lram=40000, lrkn=100000
    RESET BLIB=[ldi]
    RESET HLIB=[1di]
    RESET ILIB=[ldi]
    *if < ifeqs( <solver_nane>;INV ) > /then
*olse
reset AMAP=0
*ondif
    ----------------------
    CONSTRUCT DOF TABLE
    [xqT vEC
        INIT_DOF CON..[constraint_set] -> DOF.TABL
```

*Remark DOF TABLE initialized.

- CREATE MODEL SUMMARY DATASET

```
    *call MODEL_SUMMAY ( ldi=[1di] )
STOP
*end
```


### 7.8.9 REFERENCES

7.8-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.9 Procedure MASS

### 7.9.1 GENERAL DESCRIPTION

Procedure MASS forms the assembled unconstrained mass matrix.

### 7.9.2 PROCEDURE USAGE

Procedure mass is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call MASS ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MASS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure MASS, the following table lists each argument, its default value and meaning.

| Argument |  | Default Value |  |
| :--- | :---: | :--- | :--- |
| TYPE | CONSISTEAT |  | Type of mass matrix |
| MASS | CEM |  | Output dataset name |
| LDI | 1 | Logical device index |  |

Tables 7.9-1 and 7.9-2 list the datasets used or created by procedure MASS and the processors invoked by procedure MASS, respectively.

Table 7.9-1 Datasets Input/Output by procedure MASS

| Dataset | Description | Input | Output |
| :--- | :--- | :---: | :---: |
| JDF1.BTAB.1.8 | Model Summary | $\sqrt{ }$ |  |
| JSEQ.BTAB.2.17 | Nodal Elimination Sequence | $\sqrt{ }$ |  |
| KMAP..nsubs.ksize | Model Connectivity Map | $\sqrt{ }$ |  |
| <MASS>.SPAR.jdfz | Assembled Mass Matrix |  | $\sqrt{ }$ |
| DEM.DIAG | Diagonal Mass Matrix |  | $\sqrt{ }$ |


| Table 7.9-2 Processors Invoked by procedure MASS |  |  |
| :--- | :--- | :--- |
| Procedure | Type | Function |
| VEC | Internal | Vector algebra utilities |
| K | Internal | Assembles unconstrained system matrices |
| ESu | External | Various element processors based on the GEP |

### 7.9.3 ARGUMENT DESCRIPTIONS

### 7.9.3.1 LDI

Logical device index (default: 1).

### 7.9.3.2 MASS

Name of the mass matrix dataset (default: CEM). For a consistent mass matrix, the dataset name is [MASS].SPAR.jdf2. For a diagonal mass matrix, the dataset name will be <es_mass_diag> or DEM.DIAG.

### 7.9.3.3 TYPE

Type of mass matrix (default: CONSISTENT). This argument defines the form of the mass matrix to be either consistent or diagonal.

### 7.9.4 USAGE GUIDELINES AND EXAMPLES

Procedure MASS is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call MASS ( TYPE = DIAGONAL; MASS = <es_mass_diag>; ldi = 1)
```


### 7.9.5 LIMITATIONS

None.

### 7.9.6 ERROR MESSAGES AND WARNINGS

None.

### 7.9.7 PROCEDURE FLOWCHART

MASS (main procedure)
ES (form element mass matrices)

### 7.9.8 PROCEDURE LISTING

```
*Procedure MASS ( type = CONSISTENT ; -- . CONSISTENT | DIAGONAL
            1di=1; mass = CEM ) . Output dataset
    *renark
    *Renark Forming [type] Mass Matrix
    *renark
    *if < <IPELSE([TYPE];DIAGONAL;1;0)> > /then
        Initialize Diagonal (Lumped) Mass Matrix
    *g2n /name=num_dois /type=i [ldi] MODEL.SUMMARY NOH_DOFS
    *g2m /name=num_nodes /type=i [ldi] MODEL.SUMPARY NOM_NODES
        [xqT VEC
        IMIT_VEC <OS_masE_ds> <NOM_DOFS> BY <NOH_NODES>
    *endif
- Form Element Mass Matrices (in EFIL Dataset)
```

```
    *call ES ( function = 'PORM MASS/[type]'; ldi=[ldi] )
. Assenble Element Consistent Mass Matrix into Systen Matrix
-------------------------------------------------------------
    *if < <IFELSE([TYPE];CONSISTENT;1;0)> > /then
        [xqT K
        reset name = [mass]
        RESET BLIB=[1di]
        RESET ELIBx[1di]
        RESET HLIB=[1di]
        RESET OOTLIB=[ldi]
        RESET SPDP=<csm_precision>
        *endif
*end
```


### 7.9.9 REFERENCES

7.9-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.10 Procedure MODEL_SUMMARY

### 7.10.1 GENERAL DESCRIPTION

Procedure MODEL_SUMMARY generates a summary dataset which contains parameters about the finite element model. These parameters include the number of element processors used (<num_es_types>), the total number of nodes (<num_nodes>), the number of unconstrained degrees of freedom (<num_dofs>), and the number of equations (<num_eqns>). These parameters are written to the MODEL.SUMMARY dataset.

### 7.10.2 PROCEDURE USAGE

Procedure MODEL_SUMMARY is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

> *call MODEL_SUMMARY ( arg1 = val1 ; arg2 = val2 ; ...)
where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure MODEL_SUMMARY are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure MODEL_SUMMARY, the following table lists each argument, its default value and meaning.

| Argument | Default Value |  | Meaning |
| :--- | :---: | :--- | :--- |
|  | 1 |  | Constraint set number |
| LDI | 1 |  | Logical device index |

Table 7.10-1 lists the datasets used or created by procedure MODEL_SUMMARY.

| Table 7.10-1 Datasets Input/Output by procedure MODEL_SUMMARY |  |  |  |  |
| :--- | :--- | :--- | :--- | :---: |
| Dataset | Description | Lib | Input | Output |
| JDF1.BTAB.1.8 | Model Summary | $\sqrt{ }$ |  |  |
| MODEL.SUMMARY | Model Summary Parameters |  | $\sqrt{ }$ |  |

### 7.10.3 ARGUMENT DESCRIPTIONS

### 7.10.3.1 CONSTRAINT_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.10.3.2 LDI

Logical device index (default: 1).

### 7.10.4 USAGE GUIDELINES AND EXAMPLES

Procedure MODEL_SUMMARY is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call MODEL_SUMMARY ( LDI = 1 ; CONSTRAINT_SET = 1)
```


### 7.10.5 LIMITATIONS

None.

### 7.10.6 ERROR MESSAGES AND WARNINGS

None.

### 7.10.7 PROCEDURE FLOWCHART

Procedure MODEL_SUMMARY is self-contained with no subprocedures.

### 7.10.8 PROCEDURE LISTING

```
*Procedure MODEL_SUMMARY ( ldi=1 ; constraint_set=1 )
- ------------------------------------------------
. Got model parametors from various datasets
*find record [ldi] ES.SUMMLRY, ES_PROC /nor=num_es_types
*g2m /name=parameter: /type=i /naxn=18 [ldi] JDP1.BTAB.1.8 DATA.1
*def/i num_nodes = <paraneters[1]>
*def/i num_dofs = <paraneters[2]>
----------------------------------------------------
- Install the MODEL.SDMMARY dataset, if necessary
*find dataset [ldi] MODEL.SDMARY /seq=ids_MS
*if < <ids_HS> /le 0 > /then
        *put dataset [1di] MODEL.SUMMARY /arat=64 /seq=ids_MS
*ondif
. ------------------------------------------------
- Store paramotors in the MODEL.SOMMARY dataset
*e2g/nameznum_es_types /typezi [ldi] MODEL.SUMMRY NOM_ES_TYPES
*E2g/rane=num_nodes /type=i [ldi] MODEL.SUMMARY %UM_MODES
*n2g /name=nur_dofs /type=i [ldi] MODEL.SDMMARY wOH_DOFS
*m2g /name=nun_eqns /type=i [ldi] MODEL.SUMMRY NOM_EqNS
*end
```


### 7.10.9 REFERENCES

7.10-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

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### 7.11 Procedure PRINT_EFIL

### 7.11.1 GENERAL DESCRIPTION

Procedure PRINT_EFIL prints one or all segments of the es_name.EFIL.itype.nnod dataset where es_name is the element name (e.g., EX97). The procedure processes all elements of the specified element type.

### 7.11.2 PROCEDURE USAGE

Procedure PRINT_EFIL is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call PRINT_EFIL ( arg1 = val1 ; arg2 = val2 )
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure PRINT_EFIL are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure PRINT_EFIL, the following table lists each argument, its default value and meaning.

| Argument | Default Value |  | Meaning |
| :--- | :---: | :---: | :--- |
|  | ELEMENT |  |  |
| SEGMENT | ALL |  | Element name |
|  |  |  |  |

The segments of the EFIL are printed using processor PRTE (see reference 7.11-1).

### 7.11.3 ARGUMENT DESCRIPTIONS

### 7.11.3.1 ELEMENT

Element name (default: EX97). The argument specifies the element name for which the EFIL segments are to be printed.

### 7.11.3.2 SEGMENT

EFIL segment to be printed (default: ALL). The EFIL (see reference 7.11-2) contains nine segments. Any one or all of the segments may be selected for printing using the argument SEGMENT. The EFIL segments are as follows:

| Segment | Item | Length | Type | Description |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | Definition |  |  | Integ | Same as dataset DEF.<ES_NAME>. |
| 2 | Material |  |  | Real | (currently unused) |
| 3 | Geometry |  |  | Real | Element geometric parameters. |
|  |  | XE0 | $(3, n e n)$ |  | Initial element nodal coordinates in <br> element basis. |
|  |  | TEG | $(3,3)$ |  | Transf. from global to current element <br> basis. |
|  |  | TEC | $(3,3, n e n)$ |  | Transf. from computational to element <br> basis at element nodes. |
|  |  | TEG0 | $(3,3)$ |  | Tritial elt. nodal coords <br> in global basis. |
|  |  | DE | $(n, n e n)$ |  | Deformational displacements (drom global to initial element $).$ |
| 4 | Property |  |  | Real | (currently unused) |
| 5 | Matrix | KM | $n m t$ | Real* | Element matrix (stiffness/mass); <br> only upper triangle of nodal blocks. |
| 6 | Aux. Storage |  |  | Real | Auxiliary storage for element developer. |
| 7 | Stress |  |  | Real | (currently unused) |
| 8 | Therm. Force |  |  | Real | (currently unused) |
| 9 | Therm. Stress |  |  | Real | (currently unused) |

*The element stiffness/mass matrix, item KM in Segment 5, may be stored in either single or double precision, as specified in dataset DIR.es_name.itype.nnod (entry 15). However, all of the other REAL data in the es_name.EFIL.itype.nnod dataset are stored exclusively in single precision.

### 7.11.4 USAGE GUIDELINES AND EXAMPLES

Procedure PRINT_EFIL may be used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any
or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call PRINT_EFIL ( element = EX97; segment = ALL )
```


### 7.11.5 LIMITATIONS

None.

### 7.11.6 ERROR MESSAGES AND WARNINGS

None.

### 7.11.7 PROCEDURE FLOWCHART

Procedure PRINT_EFIL is self-contained with no subprocessors.

### 7.11.8 PROCEDURE LISTING

```
*procedure PRINT_EPIL ( elenent = EX97; segment = ALL )
Print Segnont(s) of EFIL Dataset
*if < <ifelse([segment];ALL;i;0)> > /then
    *def/i seg1 = 1
    *def/i seg2 = 0
*olse
    *if <<ifelse([segaent];DEFINITION;1;0)> > /then
        *def/i seg1 = 1
    *elseif < <ifelse([segment];MATERIAL;1;0)> > /then
        *def/i seg1 = 2
    *elseif < <ifelse([segment];GEDMETRY;1;0)> >/then
        *def/i seg1 = 3
    *elsoif < <ifelse([segnent];PROPERTY;1;0)> > /then
        *def/i seg1 = 4
    *elseif <<ifelse([segment];STIFFNESS;1;0)> >/then
        *def/i seg1 = 5
    *elseif <<ifelse([segment];STRESS_recovERY;1;0)> > /then
        *def/i seg1 = 6
    *elseif < <ifelse([segment];STORE;1;0)> > /then
        *def/i segi = 6
    *elsoif < <ifelse([segnent];STRESS;1;0)> > /then
        *def/i sog1 = 7
    *elseif < <ifelse([segment];THERMAL_FORCE;1;0)> > /then
        *def/i seg1 = 8
```

```
    *elseif < <ifelse([segment];THERMAL_mECOVERY;1;0)> > /then
    *def/i seg1 = 0
    *endif
    *def/i sog2 = <seg1>
*endif
[XQT PRTE
    RESET SEG1 = <seg1>
RESET SEG2 = <seg2>
[element]
STOP
*end
```


### 7.11.9 REFERENCES

7.11-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.
7.11-2 Stewart, Caroline B.: The Computational Structural Mechanics Testbed Data Library Description. NASA TM-100645, October 1988.

### 7.12 Procedure RESEQUENCE

### 7.12.1 GENERAL DESCRIPTION

Procedure RESEQUENCE resequences the node numbers internally for a solver defined by the global macrosymbol solver_name. If rseq_method is -1 , then a resequencing method implemented in processor RSEQ (see Section 6.1 of reference 7.12-1) is selected which is appropriate for the equation solver defined by the global macrosymbol solver_name. That is,

| solver_name | rseq_method |
| :--- | :---: |
| INV | 1 |
| BAND | 2 |
| ITER | 1 |
| SPK | none |

If rseq-method is 10 , then the profile-front minimization resequencing method implemented in processor PFM (see Section 6.2 of reference 7.12-1). If the global macrosymbol solver_name is SPK, no resequencing is performed since processor SPK performs its own resequencing (see Section 8.6 of reference $7.12-1$ ). Other values of rseq_method will select a specific resequencing method requested by a user.

### 7.12.2 PROCEDURE USAGE

Procedure RESEQUENCE is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call RESEQUENCE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure RESEQOENCE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.
For procedure RESEQUENCE, the following table lists each argument, its default value and meaning.

| Argument | Default Value |  | Meaning |
| :--- | :---: | :---: | :--- |
|  |  | 1 |  |
| LDI |  | Logical device index |  |
| MAXCON | 35 |  | Maximum number of joints connected to any one joint |
| RSEQ_METHOD | -1 |  | Resequencing method |

Tables 7.12-1 and 7.12-2 list the datasets used or created by procedure RESEQUENCE and the processors invoked by procedure RESEQUENCE, respectively.

| Table 7.12-1 | Datasets Input/Output by procedure RESEQUENCE |  |  |
| :--- | :--- | :---: | :---: |
| Dataset | Description | Input | Output |
| JSEQ.BTAB.2.17 | Nodal Elimination Sequence |  | $\sqrt{ }$ |
| KMAP..nsubs.ksize | Model Connectivity Map | $\sqrt{ }$ |  |


| Table $\mathbf{7 . 1 2 - 2}$ |  | Processors Invoked by procedure RESEQUENCE |
| :--- | :--- | :--- |
| Procedure | Type | Function |
| RSEQ | Internal | Joint resequencing |
| PFM | Internal | Joint resequencing using profile-front minimization |

### 7.12.3 ARGUMENT DESCRIPTIONS

### 7.12.3.1 LDI

Logical device index (default: 1).

### 7.12.3.2 MAXCON

Maximum number of joints connected to any one joint (default: 35).

### 7.12.3.3 RSEQ_METHOD

Resequencing method (default: -1 ). If rseq_method is -1 , then a resequencing method implemented in processor RSEQ (see Section 6.1 of reference 7.12-1) is selected which is appropriate for the equation solver defined by the global macrosymbol solver_name.

| solver_name | rseq_method |
| :--- | :---: |
| INV | 1 |
| BAND | 2 |
| ITER | 1 |
| SPK | none |

If rseq_method is 10 , then the profile-front minimization resequencing method implemented in processor PFM (see Section 6.2 of reference 7.12-1). If the global macrosymbol
solvor_name is SPK, no resequencing is performed since processor SPK performs its own resequencing (see Section 8.6 of refercnce $7.12-1$ ). ()ther values of reoq_mothod will select a specific resequencing method requested by a user.

### 7.12.4 USAGE GUIDELINES AND EXAMPLES

Procedure RESEQUENCE is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call RESEQUENCE ( RSEQ_METHOD = 2 )
```


### 7.12.5 LIMITATIONS

None.

### 7.12.6 ERROR MESSAGES AND WARNINGS

None.

### 7.12.7 PROCEDURE FLOWCHART

Procedure RESEQUENCE is self-contained with no subprocedures.

### 7.12.8 PROCEDURE LISTING

```
*procedure RESEqUENCE ( rseq_method=-1 ; maxcon=35; ldi=1 )
*if < ifeqs( <solvor_name>;SPK) > /then
    *remark ********************************************
    *renark Processor SPK does it! oun resequencing *
    *renark *********************************************
    *else
            *if < [rseq_nethod] /eq 10>/thon
                    [xqt PFM
                        HESET BLIB=[1di]
                        reset naxcon = [naxcon]
        **lseif < [rseq_method] /ne -1 > /then
            [xqT msEq
                aESET BLIB=[ldi]
                reset nethod=[rseq_method], maxcon=[maxcon]
        *0le*
            *if < ifeqs( <solver_name>;INV) > /then
                *def/i rseq_method = 1
```

```
        *elsaif < ifeqs( <solver_nane>;BAND) > /then
            *def/i rseq_method = 2
        *else
            *def/i rseq_method = 1
            *endif
            [xqT RSEQ
            IESET BLIB=[1di]
            reset methods<resq_method>, maxcon=[maxcon]
        *ondif
*ondif
*and
```


### 7.12.9 REFERENCES

7.12-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.13 Procedure SOLVE

### 7.13.1 GENERAL DESCRIPTION

Procedure SOLVE solves a lincar system of equations using a solver defined by the global macrosymbol solver_name. If solver_name is INV, the forward-reduction-backsubstitution phase of the original nodal-block sparse solver implemented in processor SSOL will be used (see Section 8.3 of reference 7.13-1). If solver_name is defined to be BAND, a variable-bandwidth direct solver implemented in processor BAND will be used (see Section 8.5 of reference 7.13-1). If solver_name is defined to be ITER, an iterative method implemented in processor ITER will be used (see Section 8.4 of reference 7.13-1). If solver_name is defined to be SPK, the SPARSPAK-A direct solver will be used to factor and solve the system of equations (see Section 8.6 of reference 7.13-1).

### 7.13.2 PROCEDURE USAGE

Procedure SOLVE is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call SOLVE ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure SOLVE are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure SOLVE, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning |
| :---: | :---: | :---: |
| APPLIED.MOTION | 1 | Flag for applied displacements |
| Constraint_set | 1 | Constraint set number |
| LDI | 1 | Logical device index |
| LOAD_SET | 1 | Load set number |
| Matrix | K | First word of the name of the dataset containing the assembled stiffness matrix. |
| RHS | APPL.FORC | First two words of the dataset name for the right-hand side system vector. |
| SOL\% | STAT.DISP | First two words of the dataset name for the displacement solution |

Tables 7.13-1 and 7.13-2 list the datasets used or created by procedure SOLVE and the processors invoked by procedure SOLVE, respectively.

| Table 7.13-1 |  |  | Datasets Input/Output by procedure SOLVE |  |
| :--- | :--- | :--- | :--- | :--- |
| Dataset | Description | Lib | Input | Output |
| AMAP..ic2.isize | Factorization Map for INV | 1 | $\sqrt{ }$ |  |
| APPL.FORC.i.1 $\dagger$ | Applied force vector | 1 | $\sqrt{ }$ |  |
| APPL.MOTI.i.1 $\dagger$ | Specified displacement vector | 1 | $\sqrt{ }$ |  |
| CON..j | Constraints | 1 | $\sqrt{ }$ |  |
| EQNF.FORC.iset.1 | Fquivalent nodal forces | 1 | $\sqrt{ }$ |  |
| INV.<KNAME>.j | Factored Stiffness Matrix | 1 | $\sqrt{ }$ |  |
| JDF1.BTAB.1.8 | Model Summary | 1 | $\sqrt{ }$ |  |
| JSEQ.BTAB.2.17 | Nodal Elimination Sequence | 1 | $\sqrt{ }$ |  |
| KMAP..nsubs.ksize | Model Connectivity Map | 1 | $\sqrt{ }$ |  |
| <KNAME>.SPAR.jdf2 | Assembled Stiffness Matrix | 1 | $\sqrt{ }$ |  |
| STAT.DISP.i. $\dagger$ | System Displacement Vector | 1 |  | $\sqrt{ }$ |
| STAT.REAC.i. $\boldsymbol{j}^{\dagger}$ | System Reaction Force Vector | 1 |  | $\sqrt{ }$ |


| Table 7.13-2 Processors Invoked by procedure SOLVE |  |  |
| :--- | :--- | :--- |
| Procedure | Type | runction |
| BAND | External | Solves system of equations using stiffness matrix in variable- <br> bandwidth solver |
| ITER | External | Solves system of equations using iterative method |
| SPK | External | Solves system of equations using SPARSPAK-A solve |
| SSOL | Internal | Solves system of equations using nodal-block-sparse solver |
| VEC | Internal | Vector algebra utilities |

### 7.13.3 ARGUMENT DESCRIPTIONS

### 7.13.3.1 APPLIED_MOTION

Flag indicating that applied displacements are involved in the loading (default: 0 or FALSE).

### 7.13.3.2 COHSTRAINT_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.13.3.3 LDI

Logical device index (default: 1).

### 7.13.3.4 LOAD_SET

Load set number (default: 1). This argument selects which load set to be used as a right-hand side vector.

### 7.13.3.5 MATRIX

First word of the datasel name containing the assembled stiffness matrix (default: $K$ ).

### 7.13.3.6 BHS

First two words of the dataset name for the right-hand side system vector (default: APPL. FORC).

### 7.13.3.7 SOLH

First two words of the dataset name for the displacement solution (default: STAT.DISP).

### 7.13.4 USAGE GUIDELINES AND EXAMPLES

Procedure SOLVE is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.

```
*call SOLVE ( MATRIX = K ; CONSTRAINT_SET = 1 ;
    LOAD_SET = 'APPL.FORC' ; SOLN = 'STAT.DISP' )
```

Before procedure SOLVE is called the global macrosymbol solver_name should be defined as described in Section 7.12.1 and should be consistent with the value used when procedure FACTOR was called. If it is not specified, then the default value INV will be used.

### 7.13.5 LIMITATIONS

None.

### 7.13.6 ERROR MESSAGES AND WARNINGS

None.

### 7.13.7 PROCEDURE FLOWCHART

Procedure SOLVE is self-contained with no subprocedures.

### 7.13.8 PROCEDURE LISTING

```
*procodure SOLVE ( rhs='appl.forc'; soln='stat.disp' ; matrix = K ; --
    load_set=1; constraint_set=1; applied_motion; --
    ldi=1 )
. Procedure to solve a linear syatem of equations using different solvers.
. The solver is selected using the global nacrosymbol "solver_name".
-1f < ifeqs( <solver_name>; ) > /thon
*def/a solver_name E= INT
*ondif
-
- Define Unique Pseudo Load Set Number for SSOL Vector Datasets
. --------------------------------------------------------------------
    *def/i iunique = 9989
. Copy Light-Hand-Side Vector to SSOL Force Dataset
    [xqt vEC
```

```
    APPL:POAC.<iunique>.i <- [rin] /aingle_precision
- Copy Applied Motions to SSOL Applied Motion Dataset
    #iIId [1di] APPL.nOTI.<iunique>.1 /seqzids_AMO
    *if < <ids_AMO\rangle/gt 0 >/then
        APPL.MOTI.<iunique>.1 <- 0.
    *else
        *g2n /nere=num_nodes /type=i [ldi] MODEL.SUMMRY NOM_NODES
        *g2n /rame=num_dofs /type=i [ldi] MODEL.SUMMARY NOM_DOFS
        INIT_\nablaEC APPL.MOTI.<iunique>.1 <num_dofs> BY <num_nodes>
    *ondif
    *if < <IFELSE([applied_notion]; ;0;1)> >/then
        *find [ldi] [applied_motion] /sequids_AM
        *if < <ids_AM>/gt 0 >/then
            APPL.MOTI.<iuniqua>.1 <- [applied_motion]
        *ondif
    *endif
*if < ifeqs( <solver_name>;INV) > /thon
- Use original nodal block sparse solver originally in SPAR
[xgT SSOL
    RESET K = [natrix]
    RESET KLIB = [ldi]
    RESET XILIB = [ldi]
    RESET QLIB = [ldi]
    LESET SET = <iunique>
    RESET COM = [constraint_set]
*elseif < ifeqa( <solvor_name>;BAND) > /then
. Vie Banded solver
[XQT BAND
    reset moth=28, ldl=1
    reset ncon=[constraint_set], dxero=1.0e-20, k=[natrix]
    reset opt=2, res=1, isot=<iunique>
*elseif < ifequ( <colver_name>;ITER) > /then
. Use Iterative solver
-
[xqT ITER
    reset ep=1,init=11,xnit=-.1,meth=1,time=1,itol=15
    reset ncon=[constraint_set], iset=<iunique>; k=[natrix]
    reset amax=0.5
*elseif < ifeqs( <solver_name>;SPK) > /then
. Use SPARSPAK solver
[XQT SPK
    select /const=[constraint_set] /kname=[natrix]
        solect /asglva=2 /ngglvl=2 /load=<iunique>
*ondif
```

```
    [xqt VEC
- Copy Solution Vector to Required Output Dataset
. ---------------------------------------------------
    *def/a std_name = STAT.DISP.[load_set].[constrmint_set]
    *if < <IFELSE([soln];<std_name>;1;0)> > /thon
        *ronace [ldi] STAT.DISP.<iunique>.[constraint_sot] = --
                        STAT.DISP.[load_sot]. [constraint_set]
        *ronare [ldi] STAT.REAC.<iunique>.[constraint_set] = --
        STAT.REAC.[load_set].[constraint_set]
    *else
        [soln] <- STIT.DISP.<iunique>.[constraint_set]
    *ondif
*end
```


### 7.13.9 REFERENCES

7.13-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.14 Procedure STIFFNESS

### 7.14.1 GENERAL DESCRIPTION

Procedure STIFFNESS forms the assembled unconstrained stiffness matrix.

### 7.14.2 PROCEDURE USAGE

Procedure STIFFNESS is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:

```
*call STIFFNESS ( arg1 = val1 ; arg2 = val2 ; ...)
```

where arg1 and arg 2 represent argument names, and vall and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure STIFFHESS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure STIFPNESS, the following table lists each argument, its default value and meaning.

| Argument | Default Value | Meaning <br> TYPE |
| :--- | :---: | :--- |
| TANG | Type of stiffness matrix to form (default: TANG). <br> This argument defines the type of stiffness to form linear <br> material stiffness matrix (MATL), geometric stiffness <br> matrix (GEOM), or the tangent stiffness matrix (TANG). <br> Constraint set number (default: tt 1). This argument <br> selects which constraint set to be used in solving the <br> linear system of equations. <br> Corotation flag |  |
| COROTATION | 1 | 1 |

Tables 7.14-1 and 7.14-2 list the datasets used or created by procedure STIFFNESS and the processors invoked by procedure STIFFNESS, respectively.

| Table 7.14-1 Datasets Input/Output by procedure STIFFNESS |  |  |  |
| :--- | :--- | :--- | :--- |
| Dataset | Description | Input | Output |
| JDF1.BTAB.1.8 | Model Summary | $\sqrt{ }$ |  |
| JSEQ.BTAB.2.17 | Nodal Elimination Sequence | $\sqrt{ }$ |  |
| KMAP..nsubs.ksize | Model Connectivity Map | $\sqrt{ }$ |  |
| <STIFFNESS>.SPAR.jdf2 | Assembled Stiffness Matrix |  | $\sqrt{ }$ |


| Table 7.14-2 |  |  |
| :--- | :--- | :--- |
| Processors Invoked by procedure STIFFNESS |  |  |
| Procedure | Type | Function |
| VEC | Internal | Vector algebra utilities |
| ESi | External | Various element processors based on the GEP |
| K | Internal | Assembles unconstrained stiffness matrix |

### 7.14.3 ARGUMENT DESCRIPTIONS

### 7.14.3.1 TYPE

Type of stiffness matrix to form (default: TANG). This argument defines the type of stiffness to form linear material stiffness matrix (MATL), geometric stiffness matrix (GEOM), or the tangent stiffness matrix (TANG).

### 7.14.3.2 CONSTRAINT_SET

Constraint set number (default: 1). This argument selects which constraint set to be used in solving the linear system of equations.

### 7.14.3.3 INPUT_LDI

Logical device index with the element stiffness matrices (default: 1).

### 7.14.3.4 OUTPUT_LDI

Logical device index for the assembled unconstrained stiffness matrix (default: 1).

### 7.14.3.5 LOAD_SET

Load set number (default: 1). This argument selects which load set to be used as a right-hand side vector.

### 7.14.3.6 LOAD_FACTOR

Load factor for the basic load system (default: 1.0).

### 7.14.3.7 STIFFNESS

First word of the dataset name containing the assembled unconstrained stiffness matrix (default: K).

### 7.14.3.8 DISPLACEMENT

Full dataset name for the displacement vector.

### 7.14.3.9 ROTATION

Full dataset name for the rotation vector.

### 7.14.3.10 COROTATION

Corotation switch; employed by ESi processors for automatic treatment of geometric nonlinearity due to large rotations (default: 1). Relevant only if problem is geometrically nonlinear. (See Chapter 4 of reference $7.2-1$ for an explanation of these options.) If COROTATION equals zero, then the corotational operations will be skipped. If COROTATION equals one (low-order option), then the basic corotational transformations will be employed to enable large rotations. If COROTATION equals two (high-order option), then a more accurate (and expensive) treatment of large rotations and consistent linearization than option 1 will be employed.

### 7.14.3.11 ES_NL_GEOM

Geometric nonlinearity switch (default: 0). If ES_NL_GEOM equals zero (no corotational frames), then the problem is geometrically linear (small displacements/rotations). If NL_GEOM equals one (low-order option), then the problem is geometrically nonlinear, but elements should use linear strain-displacement relations. Meaningful only if COROTATION $>0$, so that large rotations can be handled automatically by the corotational algorithm. If UL_GEOM equals two (high-order option), then the problem is geometrically nonlinear and elements should use nonlinear element strain-displacement relations. May be used in conjunction with COROTATION $>0$ to obtain higher-order accuracy for beam and shell elements that employ moderate-rotation strain-displacement relations.

### 7.14.3.12 ML_MATL

Material nonlinearity switch (default: 0). If NL_MATL is greater than zero, then the element is materially nonlinear. If L_MATL is zero, then the element is materially linear.

### 7.14.3.13 NLLOAD

Load nonlinearity switch (default: 0). If ML LOAD is greater than zero, then the element loads are displacement dependent. If ML_LOAD equals zero, then the element loads are not displacement dependent.

### 7.14.4 USAGE GUIDELINES AND EXAMPLES

Procedure STIFFNESS is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis.
*call STIFFHESS ( TYPE = MATL ; CONSTRAINT_SET = 1 ; STIFFNESS $=\mathrm{K}$ )

### 7.14.5 LIMITATIONS

None.

### 7.14.6 ERROR MESSAGES AND WARNINGS

None.

### 7.14.7 PROCEDURE FLOWCHART

| STIFFNESS | (main procedure) |
| :---: | :---: |
| ES | (form element stiffness matrices) |

### 7.14.8 PROCEDURE LISTING

```
*procedure STIFFHESS ( type = TANG ; -- . MATL I GEOM | TANG
                nl_geon = 0 ; --
    nl_matl = 0 ; --
    nl_load = 0 ; --
    displacement ; -- . Input dataset
    rotation ; --. Input dataset
    corotation = 1 ; --
    load_factor = 1.0 ; --
    load_set = 1 ; --
    stiffnes: = K ; -- . Output dateset
    input_ldi =1 ; --
    output_ldi = 1 ; --
    constraint_set = 1 )
    *ronark
    *Remark Forming [type] Stiffness Matrix
    *remark
- Porm Element Stiffness Matrices (in EFIL Datasot)
    *call ES ( function = 'FORM STIFFNESS/[type]' ; --
    ldi = [input_ldi] ; --
        es_nl_geom = [nl_geom] ; --
```

| -n_nl_matl | = [nl_matl] | ; -- |
| :---: | :---: | :---: |
| es_nl_load | = [nl_load] | - |
| es_dis_ds | = [displacenent] | -- |
| -s_rot_ds | = [rotation] | ; -- |
| es_coro | = [corotation] | ; -- |
| es_load_factor | = [load_factor] | ; -- |
| -s_load_set | = [load_set] |  |

- Assonble Elenont Stiffness Matrix into Systen Matrix

[XIT K
RESET MAME $=$ [stifiness]
RESET BLIB $=$ [input_1di]
RESET ELIB : [1nput_1di]
reset hlib - [input_ldi]
aESET OUTLIB $=[$ [output_ldi]
RESET SPDP = 〈can_preciaion>
- and


### 7.14.9 REFERENCES

7.14-1 Stewart, Caroline B.: The Computational Structural Mechanics Testbed User's Manual. NASA TM-100644, October 1989.

### 7.15 Procedure SWITCH_DS

### 7.15.1 GENERAL DESCRIPTION

Procedure SWITCH_DS switches two datasets within the same data library. This procedure only uses directives from the command language (see reference 7.7-1).

### 7.15.2 PROCEDURE USAGE

Procedure SWITCH_DS is used by preceding the procedure name by the *call directive, and following it by a list of arguments enclosed in parentheses. Procedure arguments are order-independent, and most have default values thus making them optional. The formal syntax is as follows:
*call SWITCH_DS ( arg1 = val1 ; arg2 = val2 ; ...)
where $\arg 1$ and arg2 represent argument names, and val1 and val2 represent their corresponding values. Note that semi-colons are required between arguments, and a double dash (--) may be used to continue the argument list on the next line.

The allowable arguments for procedure SWITCH_DS are summarized in the following table, along with their default values (if they exist). Note that arguments without defaults are generally mandatory, while those with defaults are generally optional. Exceptions to this rule are noted in the following section under detailed argument descriptions.

For procedure SUITCH_DS, the following table lists each argument, its default value and meaning.

| Argument | Default Value |  |
| :--- | :---: | :--- |
| DS_1 | - | Meaning |
| DS_2 | - | Source dataset name <br> Target dataset name |
| LDI | 1 | Logical device index |

### 7.15.3 ARGUMENT DESCRIPTIONS

### 7.15.3.1 LDI

Source logical device index (default: 1). Data library number containing the two datasets DS_1 and DS_2.

### 7.15.3.2 DS_1

Source dataset to be copied from within the data library with a logical device index of LDI to the target dataset named DS_2.

### 7.15.3.3 DS_2

Target dataset for copying the source dataset named DS_1 from within the data library with a logical device index of I, I)I.

### 7.15.4 USAGE GUIDELINES AND EXAMPLES

Procedure SWITCH_DS is used by preceding the procedure name by the *call directive. Procedure arguments may be changed from their default values by including any or all of the arguments and their new values when the procedure is called. A space or blank is required between the end of the procedure name and the left parenthesis. If the default values of the procedure arguments are to be used, then only the procedure name is required.

```
*call SWITCH_DS ( ldi=1; ds_1; ds_2)
```


### 7.15.5 LIMITATIONS

None.

### 7.15.6 ERROR MESSAGES AND WARNINGS

None.

### 7.15.7 PROCEDURE FLOWCHART

Procedure SUITCH_DS is self contained with no subprocedures.

### 7.15.8 PROCEDURE LISTING

```
*procedure SWITCH_DS ( ldi=1; ds_1; ds_2 )
. Clamp Procedure to ewitch two datasote within a data library
    *dof/a tmp_ds = xxxx.xxxx.9990.9090.9909
    *roname [ldi], [ds_1] = <t#p_ds>
    *rename [ldi], [ds_2] = [ds_1]
    *renare [1di], \langletmp_ds\rangle=[ds_2]
*end
```


### 7.15.9 REFERENCES

7.7-1 Felippa, Carlos A.: The Computational Structural Mechanics Testbed Architecture: Volume II - Directives. NASA CR 178385, February 1989.



[^0]:    * Exception: Element connectivity for all element processors is currently performed by Testbed processor ELD.

[^1]:    * Again, element connectivity is currently performed using Testbed processor ELD.

[^2]:    $\dagger$ In practice, it is often the other way around: The model properties and dimensions are fixed, while the discretization is varied. We have fixed the discretization here merely to simplify the example.

