(NASA-CR-190164) HEAT TRANSFER ANO PRESSURE

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CUBRC Report No. 6401
March, 1992

Prepared for:
NASA LEWIS RESEARCH CENTER
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CLEVELAND, OH 44135

ABSTRACT
Time averaged Stanton number and surface-pressure distributions are reported for the first-stage vane row, the first stage blade row, and the second stage vane row of the Rocketdyne Space Shuttle Main Engine two-stage fuel-side turbine. Unsteady pressure envelope measurements for the first blade are also reported. These measurements were made at $10 \%, 50 \%$, and $90 \%$ span on both the pressure and suction surfaces of the first stage components. Additional Stanton number measurements were made on the first stage blade platform, blade tip, and shroud, and at $50 \%$ span on the second vane. A shock tube was used as a short duration source of heated and pressurized air to which the turbine was subjected. Platinum thin-film heat flux gages were used to obtain the heatflux measurements, while miniature silicon-diaphragm flush-mounted pressure transducers were used to obtain the pressure measurements. The first stage vane Stanton number distributions are compared with predictions obtained using a version of STAN5 and a quasi-3D Navier-Stokes solution. This same quasi-3D N-S code was also used to obtain predictions for the first blade and the second vane.

## ACKNOWLEDGEMENTS

This research was performed by the Calspan UB Research Center under support of the NASA Lewis Research Center, Cleveland, OH, Grant No. NAG3-581. The authors gratefully acknowledge the contributions made to the success of this program by the contract monitors K.C. Civinskas and Dr. R. Gaugler of the NASA Lewis Research Center. Thanks are also extended to R. J. Boyle and K.C. Civinskas for performing the predictions to the data upon which we heavily depended. This work would have not been possible without the contributions of the many Calspan engineers and technicians, especially John R. Moselle, Robert M. Meyer, Shirley J. Sweet, Jeffrey L. Barton, and Robert M. Field.

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## SECTION 1

## INTRODUCTION

The results described in this document are a summary of the work performed under support of NASA Lewis Research Center Grant No. NAG3-581. This program was initiated in 1986 with the purpose of providing fundamental data that could be used to validate predictive codes that would be used to predict the heat transfer distributions and pressure loadings for the SSME fuel-side turbopump. Prior to the time that a full scale pump became available, the Garrett TFE 731-2HP turbine was used to develop techniques for obtaining the basic data of interest and for investigating the applicability of various predictive techniques. The results of this effort have been reported in Dunn, 1986, Dunn et al., 1986, Rae et al., 1988, Taulbee, Tran, and Dunn, 1988, Dunn, et al., 1989, Dunn, 1990, Tran and Taulbee, 1991, and George, Rae and Woodward, 1991. Once the SSME turbine stage became available, all attention focused on that machine with the purpose of: (a) providing experimental information for code validation to the turbopump consortium, and (b) to provide comparison data for a blowdown test rig at Marshall Space Flight Center which uses the same multi-stage turbine. The program was structured so that time-averaged, time-resolved, and phase-averaged data were to be obtained.

The results of several previous measurement programs that utilized many of the same diagnostic techniques as used here, but for different turbine stages, have been reported in Dunn and Stoddard, 1979 (Garrett TFE 731-2); Dunn and Hause, 1982 (Garrett TFE 731-2); Dunn, Rae, and Holt, 1984 (Garrett TFE 731-2); Dunn, Martin, and Stanek (Air Force LART), 1986; Dunn and Chupp, 1988 (Teledyne 702); Dunn and Chupp, 1989 (Teledyne 702); and Dunn, Bennett, Delaney, and Rao, 1990 (Allison Test Turbine). The short-duration facility used for the experiments reported here is the same one used to obtain the results reported in Dunn, Bennett, Delaney, and Rao, 1990.

The flow and heat transfer that occur in a turbine stage (or stages) represent one of the most complicated environments seen in any practical machine: the flow is unsteady (especially in the rotor), can be transonic, is generally three-dimensional, and is subjected to strong body forces. Despite these problems, satisfactory designs and expansions of operating envelopes have been achieved over the years due to the development of a sound analytical understanding of the flow and heat-transfer mechanics that define performance and to advances in materials and manufacturing processes. The analytical developments were made possible by a series of approximations, in which the level of detail retained in the modeling was sufficient to reveal important physical effects, while still allowing solutions to be found by available analytical/numerical methods.

The major milestones in the development of these methods have been the approximations that flow through each blade row is steady in coordinates fixed to the blades, that three-dimensionality can be handled by treating a series of two-dimensional flows in hub-to-shroud and blade-to-blade surfaces, and that the effects of viscosity can be estimated by non-interacting boundary-layer calculations and by loss models to account for secondary flow.

This technology base is surrounded by many analyses and numerical codes which can treat the flow on higher levels of approximation, and which are used from time to time to provide refined estimates of the flowfield and heat transfer, typically near a design point. Three-dimensional and unsteady flow effects are two areas where recently developed computational tools can provide useful information on the flow conditions, at least for the first stage of a multistage turbine. However, in the secc $\rightarrow+\rightarrow$ subsequent stages, these effects become more pronounced. The current state-of-the-art analyses can predict reasonably well the second stage vane pressure distribution but the predicted heatflux levels on the second vane are not as good as desired as illustrated by Blair, Dring, and Joslyn, 1988. These analyses are probably not adequate for the second rotor row, but experimental data have not been generally available for comparison with the prediction.

The results presented in this report contribute heat-flux data for the midspan region of the second stage vane.

Unsteadiness and three-dimensionality are direct consequences of the interaction of blades moving through vane wakes and the impact of multiple blade rows. The environment associated with the SSME fuel side turbine lends itself to a multistage analysis. Until very recently, such an analysis would have been envisioned as a complete, time-accurate, fully three-dimensional description of the flowfield. Some first steps toward the calculation of such flows can be seen in the work of Rai, 1987 and Rai and Madavan, 1988, but it is clear that the computational costs of this approach could very quickly become prohibitive. An alternative to the Rai approach is that described by Hah, 1984. Metzger, Dunn, and Hah, 1990(a), used a flowfield defined using the calculated technique described in Hah, 1984 to perform turbine tip and shroud heat-transfer predictions for a Garrett TFE 731 HP turbine stage. These predictions were shown to compare favorable with experimental results. Another approach to the problem is the one proposed by Giles, 1988, which has also been applied to turbine data obtained in a shortduration facility for a Rolls-Royce turbine by Abhari, Guenette, Epstein, and Giles, 1991.

Another approach to the problem is that described by Rao and Delaney, 1990, which until the present time, has only been applied to a single stage. The method proposed by these authors solves the quasi-three-dimensional Euler/Navier-Stokes equations using the explicit hopscotch scheme. The full stage computation is performed by coupling vane and blade solutions on overlapping O-type grids. In Dunn, Bennett, Delaney, and Rao, 1990, comparisons are given between the predictions of Rar and Delaney, 1990, and experimental data that were obtained for a full-stage turbine using the same experimental techniques described in this paper. Comparisons are presented for the time-averaged surface pressure, the unsteady envelope of the surface pressure, and the phase-resolved surface pressure near the trailing edge of the vane and on the blade. The agreement between the predictions and the measurements was found to be very good.

Detailed heat-flux data of the same type mentioned above were also obtained and will be presented in the open literature in the near future.

An alternate approach that is receiving current attention is based on a formulation of the passage-averaged equations of Adamczyk, 1985 and 1986, which until now have been used only as an analysis tool. It is apparent that this technique holds promise as the basis of a design method whose physical basis is considerably advanced beyond the current state of the art, and whose numerical implementation is simple enough to achieve without the need for excessive hours of supercomputer time. The formulation of closure models necessary to exploit Adamczyk's formulation relies on the availability of timeresolved flowfield data. Some of this information can be obtained from the work of Dring and Joslyn, 1986, who have probed the flow field within and around a one-and-one-half stage rotating turbine.

Civinskas, Boyle, and McConnaughey, 1988, have previously presented an analysis of the first stage blade of the turbine used here. The predictions presented here are a continuation of that work. The Navier-Stokes analysis of heat transfer was done using a modified version of the quasi-3D thin layer code developed by Chima, 1986. The modifications are explained in Boyle, 1991. An additional change for the purposes of this paper has been to incorporate the transition model of Mayle, 1991 for the first vane and the intermittency model of Mayle and Dullenkopf, 1989, 1990, for the first blade and the second vane. In addition to the quasi-3D Navier-Stokes analysis, the STAN5 (Crawford and Kays, 1976) boundary layer analysis, as modified by Gaugler, 1981 was used. Both the Navier-Stokes and boundary analyses used the MERIDL hub-to-shroud analysis of Katsanis and McNally, 1977 to determine the stream tube variation at appropriate spanwise locations. The edge conditions for the STAN5 boundary layer analysis were obtained using the TSONIC analysis of Katsanis, 1969.

The rotor blade tip of a gas turbine engine moves in close proximity to the outer stationary shroud. Typically, the gap between blade tip and shroud is kept as small as
possible in order to reduce losses. Active control of the gap is difficult and, even under the best of conditions, does not reduce the gap to zero. It would not be desirable to reduce this tip gap too much because during transient engine excursions a rotor rub might occur which may be more detrimental to the engine than the tip losses are to the performance. It is common practice for the turbine tip gap to be on the order of $1 \%$ to $1.5 \%$ of the blade height. The leakage flow is driven by the higher pressure on the blade pressure surface forcing fluid through the gap towards the suction surface and can result in relatively large heat transfer levels on the blade tip and on the blade suction surface in the vicinity of $90 \%$ to $100 \%$ span near the trailing edge. Heat transfer levels on the stationary shroud are also relatively large by comparison to blade midspan levels, but not as large as on the tip.

Many authors have studied the flow in the tip gap region: e.g., Allen and Kofskey, 1955; Booth, Dodge and Hepworth, 1982; Mayle and Metzger, 1982; Wadia and Booth, 1982; Bindon, 1986; Moore and Tilson, 1988; and Metzger and Rued, 1989. Heat-transfer measurements on the moving blades and the stationary shroud have been made by Dunn, Rae and Holt, 1984(a) and 1984(b), Dunn, Martin and Stanek, 1986, Dunn, 1989 and by Epstein, 1985 on the stationary shroud. Metzger, Dunn and Hah, 1990 applied the results of a three-dimensional Navier-Stokes solution (technique described in Hah, 1984) obtained for the actual experimental conditions and turbine (Garrett TFE 731-2-HP) to exercise a simple model of the tip flow and estimate the local heat flux levels for comparison with the experimental results.

In the remainder of this report, Section 2 provides a description of the experimental technique, the turbine flow path, and the instrumentation. Section 3 presents the experimental results and a comparison with predictions. Section 4 presents an estimate of the turbine efficiency based on the measured heat-flux distributions and the flowpath measurements. The appendicies provide information regarding the airfoil coordinates, the instrumentation locations, along with a tabular listing of the data.

## SECTION 2

## DESCRIPTION OF THE EXPERIMENTAL TECHNIQUE, THE TURBINE FLOW PATH, AND THE INSTRUMENTATION

### 2.1 The Experimental Technique

The measurements are performed utilizing a shock-tunnel to produce a shortduration source of heated and pressurized gas that passes through the turbine. Air has been selected as the test gas for these experiments. A schematic of the experimental apparatus illustrating the shock tube, an expansion nozzle, a large dump tank and a device that houses the turbine stage and provides the flow path geometry is shown in Figure 2.1.1. The shock tube has a $0.47-\mathrm{m}$ ( $18.5-\mathrm{inch}$ ) diameter by $12.2-\mathrm{m}$ ( $40-\mathrm{feet}$ ) long driver tube and $0.47-\mathrm{m}$ ( 18.5 -inch) diameter by $18.3-\mathrm{m}$ ( $60-\mathrm{feet}$ ) long driven tube. The driver tube was designed to be sufficiently long so that the wave system reflected from the endwall (at the left-hand end of the sketch) would not terminate the test time prematurely. At the flow conditions to be run for these measurements, the test time is very long for a shock tunnel facility being on the order of 40 milliseconds.

In order to initiate an experiment, the test section is evacuated while the driver, the double diaphragm section, and the driven tube are pressurized to predetermined values. Pressure values are selected to duplicate the design flow conditions. The flow function $\dot{w} \sqrt{\theta} / \delta$, wall-to-total temperature ratio $\left(T_{w} / T_{0}\right)$, stage pressure ratios, and corrected speed are duplicated. The shock-tunnel facility has the advantage that the value of $T_{o}$ can be set at almost any desired value in the range of $800^{\circ} \mathrm{R}$ to $3500^{\circ} \mathrm{R}$ (Shock tubes obviously can operate at higher $\mathrm{T}_{\mathrm{o}}$ values than $3500^{\circ} \mathrm{R}$, but at the expense of test time. Test time is a parameter that one does not sacrifice easily), and the test gas can be selected to duplicate the desired specific heat ratio. The pressure ratio across the turbine is established by the throat area of the flow control nozzle located at the exit end of the device housing the turbine. It is desirable to locate this throat as close to the turbine exit

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as is practical to reduce the time required to fill the cavity between the rotor exit and the choke. The model (shown later in Figure 2.3.1) is currently being redesigned to move the throat closer to the turbine exit. Simple one-dimensional calculations provide a good first estimate of the necessary exit area. Another characteristic of this facility is that the total pressure (or the Reynolds number) at the entrance to the vane row can be changed by moving the inlet to the device housing the turbine axially in the expanding nozzle flow so as to intercept the flow at a different freestream Mach number. If this doesn't provide sufficient range, then the reflected-shock pressure can be increased or the total temperature can be decreased in order to increase the Reynolds number, which was the approach taken in these tests.

Figure 2.1 .2 is a photograph of the facility illustrating many of the components described in the preceding paragraph. Figure 2.1 .3 is a wave diagram for the shock tube. The gas that subsequently passes through the turbine has been processed by both the incident and the reflected shock shown in Figure 2.1.3. The reflected-shock reservoir gas is expanded in the primary nozzle which has the effect of increasing the flow velocity, decreasing the total pressure and maintaining the total temperature at the reservoir value. The device housing the turbine will not pass all of the weight flow available in the primary nozzle, so the inlet must be carefully located in order to avoid a hammer shock. That is, there must be sufficient flow area for a normal shock to establish outside the inlet and for the remainder of the flow not passed through the turbine to pass between the lip of the inlet and the nozzle wall. If the inlet is placed too far into the nozzle, the nozzle flow will be blocked and very large short-duration forces will be exerted on the device with potentially disastrous effects. The flow downstream of the inlet normal shock is subsonic at a pressure determined by the shock strength at the particular pick-off location in the expansion.

### 2.2 The SSME Turbine




URIGINAL PAGE
WACK AND WHITE PHOTGGRAPH


Figure 2.1.3 SKETCH OF A TYPICAL SHOCK-TUBE WAVE DIAGRAM

Photographs of the first stage vane row (41 vanes), the first stage rotor row (63 blades), and the second stage vane row ( 39 vanes) are shown on Figures 2.2.1-2.2.5. The second stage rotor (not shown) has 59 blades. The tip/shroud clearance for the first stage rotor at the design speed condition is $\sim 0.015$ inches or $1.6 \%$ of blade height. Figures 2.2.1 and 2.2.2 show photographs of the front and rear view of the first-stage vane row illustrating a cut-back (which was accounted for in the analysis to be described later) of the vane near the hub endwall trailing edge. It can be seen that the surface finish of the vane row is much smoother than it is for the blades. An enlarged photograph of the blade surface qualitatively illustrating the surface roughness on the blade is shown on Figure 2.2.6. The surface roughness for this blade has been measured* and a typical profilometer scan of the blade surface is given in Figure 2.2.7. The results shown in this figure suggest an rms roughness of about $150,000 \AA$ which was used in the analysis of the heat-transfer data. Figures 2.2.4 and 2.2.5 are photographs of the second vane illustrating a surface finish comparable to the first vane and the absence of a cut-back at the trailing edge. The vane and blade coordinates are listed in the Appendix in section A.1.

### 2.3 The Turbine Flow Path

Figure 2.3 .1 is a drawing of the turbine stage illustrating the extent to which the flowpath of the SSME hardware has been reproduced. The preburner dome and bolt, the 13 struts upstream of the first-stage vane, the 12 flow straighteners, and 6 struts downstream of the second rotor have been included. At the exit of the model is a flow chok ..ninh is used to control both the mass flow through the turbine as well as the turbine exit pressure. The choke area computed using a one-dimensional approximation to the flow yielded exit areas very close to those required.

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Figure 2.2.1 PHOTOGRAPH OF SSME FUEL-SIDE TURBINE FIRST STAGE VANE, FRONT VIEW

CUT BACK OF VANE


Figure 2.2.2 PHOTOGRAPH OF SSME FUEL-SIDE TURBINE FIRST STAGE VANE, REAR VIEW


Figure 2.2.4 PHOTOGRAPH OF SSME FUEL-SIDE TURBINE SECOND STAGE VANE, FRONT VIEW


Figure 2.2.5 photograph of ssme fuel-side turbine second stage vane, rear view


Figure 2.2.6 ENLARGED PHOTOGRAPH OF FIRST BLADE SURFACE ROUGHNESS


Figure 2.2.7 PROFILOMETER SCAN OF BLADE SURFACE

Figure 2.3.1 SKETCH OF device housing ssme turbine stage

Mounted onto the forward end of the drive motor shaft is a 1000 pulse/revolution Hewlett Packard HEDS 5000 shaft encoder from which turbine speed and angular position is determined. This unit outputs a TTL pulse every $360^{\circ} \% 1000=0.36^{\circ}$ and a second TTL pulse once every revolution (the zero-crossing pulse). The shaft encoder was initially aligned such that the zero-crossing pulse occurred when the stagnation point of the first stage rotor blade containing the leading edge insert (heat-transfer) gage described in the next section was $12.2^{\circ} \mathrm{CCW}$ from TDC of the first stage vane. The pulses from the shaft encoder are used to trigger the data recording system. Since the turbine speed is not kept constant during the run, a 25 MHz timing pulse in the form of a ramp signal is fed into one channel of the high frequency data recorder to determine the arrival time of each encoder pulse. Mounted on the downstream end of the shaft is a 200 channel, freon/oil cooled, slip ring unit.

### 2.4 Heat-Flux Instrumentation

The heat-flux measurements were performed using thin-film resistance thermometers. These devices represent an old and very well established technology that was developed as part of the early hypersonics flow research work in the late 1950's for measurement of heat-flux distributions in short-duration facilities. The thin-film gages are made of platinum ( $\sim 100 \AA$ thick) and are hand painted on an insulating Pyrex (7740) substrate in the form of a strip that is approximately $1.02 \times 10^{-4}-\mathrm{m}(0.004-\mathrm{in})$ wide by about $5.08 \times 10^{-4}-\mathrm{m}(0.020-\mathrm{in})$ long. The response time of the elements is on the order of $10^{-8} \mathrm{~s}$. The substrates contrathe heat-flux gages are Epoxied within the base metal throughout the turbine stage. The substrate onto which the gage is painted can be made in many sizes and shapes.

Both button-type gages and the contoured leading-edge inserts were used for this work. The first stage vane and blade row were instrumented using both types of instrumentation along the $10 \%, 50 \%$, and $90 \%$ span locations. Some gages were installed
in the first stage blade shroud, blade platform, and blade tip. The second stage vane had button gages only along the $50 \%$ span. The locations of the heat transfer instrumentation are summarized in the Appendix in section A.2. Figure 2.4.1 is a photograph of a rotor blade that has been instrumented with button-types gages and Figure 2.4 .2 is a photograph of a blade containing a contoured leading-edge insert. Each of the gages has two lead wires. The wires from the gages on the rotor are routed through the hollow shaft to the slip-ring unit.

### 2.5 Pressure Instrumentation

Measurements were also obtained using miniature silicon diaphragm pressure transducers located on the first-stage vane and the first-stage blade. The particular gages being used are Kulite Model LQ-062-600A with an active pressure area of 0.64 mm by 0.64 mm , and a frequency response of about 100 kHz in the installed configuration. Twenty-eight pressure transducers were installed on the vanes and twenty-four were installed on the blades. The pressure transducers were placed at $10 \%, 50 \%$, and $90 \%$ span on the first vane and blade stages, and were distributed over several different vanes and blades so as to not disturb the integrity of the surface. No pressure transducers were installed in the second stage vane. The location of the surface mounted pressure transducers are summarized in the Appendix in section A.2. Figure 2.5.1 is a photograph of several of these transducers located at $10 \%$ span on the suction surface of the blade. Each of these transducers has four leads--two power leads and two output leads. The wires from the gages on the rotor are row the the hollow shaft to the slip-ring unit.

Flowpath static pressure was measured on the outer wall of the turbine model at the inlet and exit to the turbine stages and between each blade row. The upstream static pressure was nearly equal to the upstream total pressure because the inlet Mach number was low (on the order of 0.1 ). The inlet Mach number was calculated and the inlet total


Figure 2.4.2 PHOTOGRAPH OF LEADING-EDGE INSERT HEAT-FLUX GAGES ON FIRST-STAGE BLADE

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Figure 2.5.1 PHOTOGRAPH OF PRESSURE TRANSDUCERS AT $10 \%$ SPAN ON FIRST-STAGE BLADE SURFACE

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pressure was obtained from the isentropic flow relationship. Total pressure was also measured in the passage downstream of the second rotor using two rakes of transducers.

### 2.6 High Speed Data Acquisition

An attempt was made to obtain time resolved data for selected heat transfer and pressure gages on the first stage rotor using a bank of 24 programmable, high-speed data recording units (Datalab DL6010 and DL6020). These units were configured so that a sample was recorded whenever a pulse was output by the shaft encoder, i.e., once every $0.36^{\circ}$. A separate timer box was used to measure the recording time after trigger. The data obtained using this bank of high-speed recorders were, however, contaminated with noise that was inadvertently introduced into the system. The unsteady pressure and heat transfer envelopes therefore could not be obtained. This problem will be rectified by start of the second phase of this program.

## SECTION 3

## EXPERIMENTAL RESULTS AND COMPARISON WITH PREDICTIONS

A total of thirteen runs were made during which several model configurations were used. Of these thirteen runs and different model configurations, eight runs produced data that could be used for the intentions of this research program. Some of the runs that did not produce useable data were lost because of shock-tube diaphragm failures. The remainder were lost in experimenting with the configuration of the model inlet duct. Table 1 summarizes the reflected shock conditions, the flow conditions at the turbine inlet, and the turbine speed for the eight runs to be discussed herein. Two shock tube conditions were run for these experiments; the first at a reflected-shock pressure and temperature of approximately $6.2 \times 10^{3} \mathrm{kPa}(900 \mathrm{psia})$ and $544 \mathrm{~K}\left(980^{\circ} \mathrm{R}\right)$, respectively, and the second at a reflected-shock pressure and temperature of approximately $10 \times 10^{3}$ $\mathrm{kPa}(1445 \mathrm{psia})$ and $602 \mathrm{~K}\left(1084^{\circ} \mathrm{R}\right)$, respectively. For a given test condition, the range in reflected-shock pressure shown in Table 1 is the result of attempting to increase the test time by changing the relative amount of helium in the driver gas which also influences the incident shock Mach number and hence the reflected shock conditions. The two reflected-shock conditions result in first vane inlet Reynolds numbers (based on first vane chord) of approximately $1.4 \times 10^{5}$ and $2.5 \times 10^{5}$, respectively. Table $2(\mathrm{a})$ gives the measured upstream, interstage, and exit pressures, and Table 2(b) provides the pressure ratios for each of the vane and blade rows. The area of the downstream flow choke was changed so that data could be obtained at two values of stage presure ratio, for each test condition. Measurements were obtained with the turbine speed set at $100 \% \pm 1 \%$ of the design value or at approximately $103 \%$ of the design value. Limited data were obtained at off-design speed.

| Run | $\dot{W}$ <br> $[\mathrm{lbm} / \mathrm{s}]$ | $\mathrm{P}_{\mathrm{T}, \text { in }}$ <br> $\mathrm{P}_{\mathrm{s}, \text { out }}$ | $\mathrm{P}_{\mathrm{s}, \mathrm{in}}$ <br> $[\mathrm{psiag}]$ | Reflected <br> shock <br> pressure <br> $[\mathrm{psia]}]$ | Reflected <br> shock <br> temp. <br> $[\mathrm{R}]$ | Re $]_{\mathrm{vc}}$ <br> $\left(\mathrm{x} 10^{-5}\right)^{*}$ | Actual <br> speed <br> [rpm] | \% Design <br> speed $* *$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 9.52 | - | 90 | 865 | 949 | 2.39 | 6100 | 68 |
| 5 | 5.59 | 1.66 | 46.6 | 900 | 995 | 1.39 | 9075 | 99 |
| 6 | 5.81 | 1.65 | 48.3 | 929 | 990 | 1.44 | 9468 | 103 |
| 7 | 10.2 | 1.48 | 86 | 1519 | 1112 | 3.00 | 9612 | 99 |
| 8 | 9.74 | 1.38 | 89 | 1442 | 1084 | 2.69 | 9690 | 101 |
| 11 | 10.0 | 1.42 | 98 | 1369 | 1057 | 2.40 | 9585 | 101 |
| 12 | 5.83 | 1.54 | 48.3 | 925 | 981 | 1.45 | 9380 | 103 |
| 13 | 5.51 | 1.54 | 45.3 | 878 | 970 | 1.38 | 9365 | 103 |

*Reynolds number based on vane chord and vane inlet conditions.
${ }^{* *} \mathrm{~N}_{\text {corr }}=291.4 \mathrm{rpm} / \sqrt{{ }^{\circ} \mathrm{R}}$
Table 1--Summary of flow parameters.

| Run | $\begin{gathered} \mathrm{P}_{\mathrm{t}} \text { into } \\ 1 \text { st } \\ \text { vane } \\ \text { (psia) } \end{gathered}$ | $\mathrm{P}_{\mathrm{S}}$ exiting 1 $^{\text {St vane }}$ (psia) | $\mathrm{P}_{\mathbf{s}}$ exiting $1^{\text {St }}$ rotor (psia) | $\mathrm{P}_{\mathrm{S}}$ <br> exiting <br> $2^{\text {nd }}$vane <br> (psia) | $\mathrm{P}_{\mathbf{s}}$ <br> exiting <br> $2^{\text {nd }}$rotor <br> (psia) | $\mathrm{P}_{\mathrm{t}}$ exiting 2nd rotor (psia) | $\left.\frac{\mathrm{P}_{\mathrm{T}, \text { in }}}{\mathrm{P}_{\mathrm{s}, \text { out }}}\right\|_{\text {stage }}$ | $\left.\frac{\mathrm{P}_{\mathrm{T}, \text { in }}}{\mathrm{P}_{\mathrm{T}, \text { out }}}\right\|_{\text {stage }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 90.0 | 78.5 | 67.6 | - | - | - | - | - |
| 5 | 47.1 | 40.4 | 34.3 | 30.5 | 28.3 | 29.1 | 1.66 | 1.62 |
| 6 | 48.9 | 43.0 | 36.4 | 32.5 | 29.7 | 30.4 | 1.65 | 1.61 |
| 7 | 86 | 77 | 70 | 63 | 58.3 | 59.9 | 1.49 | 1.45 |
| 8 | 89 | 82 | 75 | 68 | 64.3 | 64.4 | 1.40 | 1.40 |
| 11 | 98 | 90 | 79 | 71.5 | 69.0 | 67.5 | 1.44 | 1.47 |
| 12 | 48.8 | 43.3 | 37.3 | 34.1 | 31.7 | 32.2 | 1.54 | 1.52 |
| 13 | 45.8 | 40.3 | 34.7 | 32.0 | 29.7 | 30.2 | 1.54 | 1.52 |

Table 2a--Measured interstage pressures. Static pressure were measured at the outer shroud.

| Run | $\begin{aligned} & \text { First vane } \\ & \mathrm{P}_{\mathrm{T}, \text { in }} \\ & \mathrm{P}_{\mathrm{s}, \text { out }} \end{aligned}$ | $\begin{aligned} & \text { First stage } \\ & \frac{\mathrm{P}_{\mathrm{T}, \text { in }}}{\mathrm{P}_{\mathrm{s}, \text { out }}} \end{aligned}$ | $\begin{gathered} \text { Second vane } \\ \mathrm{P}_{\mathrm{s}, \text { in }} \\ \mathrm{P}_{\mathrm{s}, \text { out }} \end{gathered}$ | $\begin{aligned} & \text { Second rolor } \\ & \frac{P_{s, \text { in }}}{\mathrm{P}_{\mathrm{s}, \text { out }}} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1.15 | 1.33 | - | - |
| 5 | 1.17 | 1.37 | 1.12 | 1.08 |
| 6 | 1.14 | 1.34 | 1.12 | 1.09 |
| 7 | 1.13 | 1.24 | 1.11 | 1.08 |
| 8 | 1.10 | 1.20 | 1.10 | 1.06 |
| 11 | 1.10 | 1.26 | 1.10 | 1.04 |
| 12 | 1.13 | 1.31 | 1.09 | 1.08 |
| 13 | 1.14 | 1.32 | 1.08 | 1.08 |

Table 2 b --Component pressure ratios. Static pressures were measured at the outer shroud.

The Stanton number results presented here for both of the vane rows and the first blade row are based on conditions at the first vane inlet. The relationship used to evaluate the Stanton number was

$$
\begin{equation*}
\mathrm{St}=\frac{\dot{q}(T)}{(\mathrm{W} / A)\left[H_{0}\left(T_{0}\right)-H_{w}(T)\right]} \tag{1}
\end{equation*}
$$

The value of $A$ used for this evaluation was $1.73 \times 10^{-2} \mathrm{~m}^{2}\left(0.186 \mathrm{ft}^{2}\right)$, and corresponds to the annular area upstream of the first stage vane. In this formulation, the heat flux and the wall enthalpy are both evaluated at the same temperature, $T$. If the cold-wall heat flux, $\dot{\mathbf{q}}\left(\mathrm{T}_{\mathbf{w}}\right)$, is desired, then it can be obtained by multiplying the given Stanton number by ( $\dot{\mathrm{W}} / \mathrm{A}$ ) $\left[\mathrm{H}_{0}\left(\mathrm{~T}_{0}\right)-\mathrm{H}_{\mathrm{w}}\left(\mathrm{T}_{\mathrm{w}}\right)\right]$. The greatest contributor to the uncertainty in Stanton number is the uncertainty in the weight flow, $\dot{W}$. For these experiments, the weight flow was found from an experimentally determined flow calibration curve supplied by NASA MSFC which plotted the flow function as a function of the total to static pressure ratio across the first stage nozzle. The uncertainty in the vane row pressure measurement translate into an uncertainty in the flow function and the weight flow. An uncertainty of approximately $10 \%$ in the weight flow was found. Assuming an uncertainty in the heat flux and temperature measurements to be $5 \%$, the expected error in the Stanton numbers can be calculated using the methodology of Kline and McClintock, 1953 to be $12 \%$.

### 3.1 First Vane and First Blade Surface Pressure Results

The measured surface pressure distributions on the first vane at $10 \%, 50 \%$, and $90 \%$ span along with the predicted pressure distributions are presented on Figures 3.1.13.1.3. These results are presented for two stage pressure ratios, approximately 1.54 and 1.65. The agreement between the data and the prediction at all three spanwise locations is not particularly good. The cause of the disagreement is in large part attributable to the uncertainty in the pressure measurement. Prior to the initial experiment, the pressure



Figure 3.1.4--Pressure distribution at $10 \%$ span on first blade.




### 3.2 First Vane Surface Stanton Number Results

Figures 3.2.1 and 3.2.2 present the measured Stanton number distributions for the vane at $50 \%$ span for Reynolds numbers of 140,000 and 250,000 , respectively. Figure 3.2.3 presents the Stanton number data for both Reynolds numbers at $10 \%$ span and Figure 3.2.4 presents data for both Reynolds numbers at $90 \%$ span. The low Reynolds number data were obtained at stage pressure ratios of 1.54 and 1.65 while the higher Reynolds number data were obtained at about 1.4 and 1.48. Inspection of the data suggests that the stage pressure ratio, in general, has little influence on the Stanton number distributions for the vane locations at which measurements were obtained.

The experimental results for the first vane presented in Figure 3.2.1 illustrate a rapid decrease in Stanton number on the suction surface from the stagnation point to about $15 \%$ wetted distance followed by a sharp increase near this location, then a peak at about $50 \%$ wetted distance. On the pressure surface, the data fall sharply from the stagnation point reaching a minimum at about $25 \%$ wetted distance, then increases steadily towards the trailing edge. This trend in the pressure surface data is consistent with that seen previously for the Garrett TFE731-2 HP turbine (Dunn, Rae and Holt, 1984), the Air Force LART (Dunn, Martin and Stanek, 1986) the Teledyne 702 turbine (Dunn and Chupp, 1988), as well as two other unpublished Calspan data sets. The peak Stanton number is shown to occur at the stagnation point and the maximum value reached on the suction and pressure surfaces are comparable with each other and equal to a little more than half of the stagnation value. Similar trends are seen at high Reynolds numbers (Figures 3.2.2) but with the $\because \therefore$ ms occurring closer to the stagnation point. Furthermore, the maximum in the suction surface data also occurs closer to the stagnation point.

Figure 3.2.1 also compares vane midspan experimental results with four predictions. Two of the predictions are for fully turbulent flow. The third and fourth predictions incorporate transition models. The two fully turbulent predictions were done


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using the quasi-3D Navier-Stokes analysis described by Boyle (1991) and Gaugler's modified version the STAN5 boundary layer analysis of Crawford and Kays (1976). The predictions including transition were obtained by incorporating the transition model of Mayle, 1991 and the transition model due to Dunham, 1972 into the just noted NavierStokes analysis. Of the two fully turbulent predictions, the STAN5 prediction illustrates better overall agreement with the data. On the suction surface, the STAN5 prediction doesn't fall as low as the data in the vicinity of $15 \%$ wetted distance, and it doesn't climb as high as the data beyond $50 \%$ wetted distance. On the pressure surface, both of the fully turbulent predictions agree with the data reasonably well from the stagnation point to about $40 \%$ wetted distance. The data points at $60 \%$ and $80 \%$ wetted distance are significantly greater than the prediction. It was noted earlier in this section that this trend has been seen previously for full-stage turbines. This same trend was noted by Nealy, et al., 1984 for a vane ring downstream of a combustor. However, the Navier-Stokes analysis used here was applied to those data (Boyle, 1991) and reasonably good agreement between data and prediction was obtained. It is felt that the relatively high upstream turbulence in itself is not sufficient to account for the high pressure surface heat transfer, since the local turbulence level decreases significantly as the flow accelerates through the vane passage. The good agreement between the STAN5 boundary layer prediction and the Navier-Stokes fully turbulent analyses suggests that the numerical solutions of the analyses are not the source of the disagreement with the experimental data.

For the calculation incorporating the Dunham, 1972 transition model, transition occurs midway along the suction surface. However, the prediction is not in good agreement with the experimental data from about $7 \%$ wetted distance to $50 \%$ wetted distance. This analysis predicts Stanton numbers along the pressure surface that are generally in agreement with STAN5 over the initial $50 \%$ of that surface. Beyond $50 \%$, the shape of the Dunham prediction deviates from the other two and falls below them and
well below the data. This is because the flow never becomes fully turbulent with this model. Also included on Figure 3.3.1 is the Navier-Stokes prediction with the Mayle, 1991 transition model incorporated. This prediction is in much better agreement with the data than is the other prediction incorporating transition. Overall, the Navier-Stokes prediction which includes the Mayle transition model appears to be in better agreement with the data than any of the other predictions.

Figure 3.2.2 presents a comparison between the high Reynolds number data and the same four predictions described above. There is very little difference among the predictions at this higher Reynolds number except in the vicinity of the stagnation point and in the region of $5 \%$ to $20 \%$ on the suction surface. Both the N-S and the STAN5 solutions predict the stagnation region data reasonably well. The N-S solution with the Mayle transition model predicts the $5 \%$ to $20 \%$ wetted distance region better than the N-S solution with the Dunham model. On the pressure surface, all of the predictions are in reasonably good agreement with each other and all fall below the data from the stagnation point to about $40 \%$ wetted distance. The experimental results at $60 \%$ and $80 \%$ wetted distance are underpredicted by a significant amount by all four solutions. In summary, the predictions shown in Figures 3.2.1 and 3.2.2 show best agreement with the data when a fully turbulent analysis is used, even for the low Reynolds number cases. The transition models of both Mayle and of Dunham are highly dependent on the freestream turbulence intensity. Previous measurements gave an intensity of about $6 \%$ at the turbine inlet. At the low Reynolds number, Dunham's model predicts the start of transition too far downstream on the suction surface. Mayle's model agrees better with the data. At the high Reynolds number, transition occurs close to the leading edge, and there is little difference among the predictions.

Figures 3.2.3 and 3.2.4 present the first vane Stanton number results at $10 \%$ and $90 \%$ span, respectively. Both sets of Reynolds number data are included on these figures. The N-S prediction with the Mayle transition model has been selected for comparison
with the experimental data. It would be anticipated that the high Reynolds number data set should be consistently lower than the low Reynolds number data by about $15 \%$ $\left((2)^{0.2}=1.15\right)$. There is sufficient uncertainty in the Stanton number results as described in Section 4 that generally, the data sets appear to overlap. The agreement between the suction surface prediction and the data is not as good as it was at midspan for either $10 \%$ or $90 \%$ span. In general, beyond $50 \%$ wetted distance, the prediction fell well above the data on the suction surface. The data point at $60 \%$ wetted distance is above the prediction, but no more so than the suction surface data points are below the prediction. The pressure surface data at $90 \%$ span are in as good agreement with the prediction as has been seen at any location on this vane.

### 3.3 First Blade Surface Stanton Number Results

### 3.3.1 Discussion of blade data

Figures 3.3.1 and 3.3.2 present the measured Stanton number distributions for the first blade at midspan for Reynolds numbers of 140,000 and 250,000 , respectively. The Reynolds number data sets are both given on the same figure for the $10 \%$ span (Figure 3.3.3) and the $90 \%$ span (Figure 3.3.4) locations. The heat-flux values in the vicinity of the leading-edge region are known to be sensitive to incidence angle. However, the rotor speed range over which data were taken in these experiments ( $99 \%$ to $103 \%$ of design) was sufficiently small that it is unlikely that incidence angle had a significant effect. Likewise, the local Stanton number is sensitive to stage pressure ratio because of the change in incidence angle associated with the higher axial velocity (increased weight flow) at the lower value of pressure ratio. From the weight flow data presented in Table 1 it was difficult to obtain an estimate of the incidence angle variation resulting from the difference in pressure ratio. The experimental data (runs 5, 6, 12, and 13) at the $10 \%$ and $90 \%$ spanwise locations are consistent with each other near the leading edge in that the Stanton numbers for runs 5 and 6 are consistently greater than those for runs 12 and 13.

$$
-
$$

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 point value. Included on Figure 3.3.1 are two fully turbulent Navier-Stokes predictions, one for a rough airfoil and the other for a smooth airfoil, and a N-S prediction, with the

Mayle and Dullenkopf, 1989, 1990 intermittency model included, for a smooth airfoil. The STAN5 boundary layer analysis showed separation for the midspan pressure surface using the predicted inviscid flow field for a boundary condition and, therefore, the STAN5 prediction could not be obtained for the blade. The Navier-Stokes analyses do not indicate a significant increase in heat transfer due to blade surface roughness. On the pressure surface both of the fully turbulent analyses are in good agreement with the experimental data. However, on the suction surface these same predictions fall consistently above the data. The third prediction included on Figure 3.3.1 is in essential agreement with the fully turbulent predictions on the pressure surface. On the suction surface, it also overpredicts the data, but is closer than the fully turbulent predictions. The predicted heat transfer at the leading edge is higher than the experimental data. The average augmentation of the heat transfer in the laminar region was calculated assuming a turbulence intensity of $10 \%$. The transition model used a background turbulence intensity of $2 \%$. The intermittency model overpredicted the heat transfer at the leading edge by about $33 \%$. This indicates that the augmentation due to freestream turbulence was excessive. The Froessling number at the stagnation region was calculated from the experimental results for this case, and using the cylinder in cross flow correlation of Traci and Wilcox, 1975 a freestream turbulence intensity of about $7 \%$ was estimated.

Along the entire pressure surface the fully turbulent predictions are nearly identical, and agree well with the experimental data. These predictions for the rotor are in contrast with those for the vane, where the pressure surface heat transfer exceeded the - lly turbulent prediction. The transitioning prediction, which includes the effect of freestream turbulence, overpredicts the pressure surface heat transfer. The largest source of uncertainty in the heat transfer predictions is due to the uncertainty in the freestream turbulence for the augmentation of the laminar viscosity due to this freestream turbulence.

### 3.3.2 Blade surface roughness considerations

The first stage blade of this turbine appeared to be rough and there was concern that the roughness may enhance the heat transfer. Blair and Anderson, 1992 have illustrated that this enhancement can be significant. The influence of surface roughness on the blade data presented herein was therefore investigated.

Boyle and Civinskas, 1991, investigated the influence of surface roughness on the predicted heat transfer to the surface. The effective roughness height was strongly dependent on both the roughness and the density. The roughness density can be found from the trace shown in Figure 2.2.7. In this figure, the horizontal axis is compressed by more than a factor of ten over the vertical axis. Even though the blade shown in Figure 2.4,1,2.4.2, and 2.5.1 are visibly rough, the peaks are not spaced closely together.

Comparing the two analyses shows that the effect of surface roughness is very small. This was not unexpected. The insensitivity to surface roughness is the result of both the low Reynolds number, and the effect of surface roughness density. In the Navier-Stokes analysis a reference $y^{+}$was used for an a priori determination of the grid spacing. This reference value is given by

$$
\mathrm{y}_{\mathrm{REF}}^{+}=0.17 \mathrm{y} \mathrm{Re}^{0.9} / \mathrm{s}^{0.1}
$$

where $y$ is the distance from the surface, Re is the exit Reynolds number per unit length, and $s$ is a characteristic distance.

An analogous reference roughness height is

$$
\mathbf{k}_{\mathrm{REF}}^{+}=0.17 \mathrm{kRe} \mathrm{Re}^{0.9} / \mathrm{s}^{0.1}
$$

For the low Reynolds number case the exit unit Reynolds number was 1.28 x $10^{7} / \mathrm{m}\left(3.9 \times 10^{6} / \mathrm{ft}\right)$.

The roughness height, $k$, in the above equations is not the actual roughness height, but rather the equivalent roughness height. The equivalent roughness height was estimated using the approach taken by Boyle and Civinskas, 1991 to be less than 0.3 of the actual roughness height. Even though the actual roughness height was $\sim 150,000 \AA$ ( 590 microinches), the value of $\mathbf{k}_{\text {REF }}^{+}$was calculated to be only 2.7 . This value of the reference roughness height is only approximate since it is based on a friction factor for a smooth flat plate. Nonetheless, the value of $k^{+}$is less than the value of 5 for a hydraulically smooth surface. Consequently, the rough and smooth heat transfer predictions are nearly identical. It should be noted that blades with this surface roughness, when operated in the SSME environment, are no longer hydraulically smooth due to the much higher Reynolds number of the actual engine. Calculations showed an increase in heat transfer of up to $25 \%$ due to surface roughness at the SSME operating conditions for $\mathrm{K}=0.3$. The parameter K represents the ratio of the equivalent roughness height $(\mathrm{k})$ to the actual roughness height.

Figure 3.3.2 presents the first blade midspan Stanton number data for the high Reynolds number case. Also included on this figure are three N-S predictions which were performed for different surface roughness heights. The N-S turbulent prediction with $\mathrm{K}=0$ is consistently above the $\mathrm{N}-\mathrm{S}$ prediction with the Mayle and Dullenkopf intermittency model. The value of Stanton number at the stagnation point is predicted reasonably well by the $\mathrm{N}-\mathrm{S}$ solution. On the suction surface, the $\mathrm{N}-\mathrm{S}$ turbulent prediction for a smooth surface $(\mathrm{K}=0)$ is consistently above the data. The prediction for $\mathrm{K}=0.3$ is about $12 \%$ high.: .. the initial $50 \%$ of the surface, then about the same over the remainder of the surface. The prediction for $\mathrm{K}=1.0$ represents a significant enhancement and is well above the data over the entire surface.

On the pressure surface of the blade, Figure 3.3.2 illustrates that the shape of the predictions is consistent with the data. The predictions for $\mathrm{K}=0$ and $\mathrm{K}=0.3$ both fall
below the data. The prediction for $\mathrm{K}=1.0$ is in reasonable good agreement with the data over the entire pressure surface.

Figures 3.3 .3 and 3.3 .4 present the experimental data and comparisons with predictions for the $10 \%$ span and the $90 \%$ span locations, respectively. Both sets of Reynolds number data are included on these figures. Figure 3.3.3 includes the fully turbulent N-S predictions for both Reynolds numbers and the N-S prediction with the Mayle and Dullenkopf intermittency model for the low Reynolds number. At the high Reynolds number, this prediction is essentially the same as the corresponding N-S fully turbulent prediction. For the suction surface, there is very little difference among the three predictions. The data between $5 \%$ and $15 \%$ wetted distance are substantially below the predictions, while the data between $50 \%$ and $80 \%$ are below, but in reasonable agreement with the predictions. For the pressure surface, the fully turbulent prediction is generally below the data while the intermittency model provides a reasonable representation of the data. The comparison presented in Figure 3.3.4 for the $90 \%$ span location demonstrates reasonably good agreement between the data and the intermittency model prediction for the suction surface and correspondingly good agreement on the pressure surface for the N - S fully turbulent prediction.

### 3.4 Second Vane Surface Stanton Number Results

The second vane Stanton number measurements are shown in Figures 3.4.1 for both Reynolds number cases and both stage pressure ratios. For the second vane, only midspan heat-flux data wet: . . . Figure 3.4.1 also includes the predicted midspan Stanton number distributions. A fully turbulent and an intermittency model prediction are shown. The high Reynolds number intermittency prediction provides a good prediction at the stagnation point. On the suction surface, the fully turbulent and the low Reynolds number intermittency model predictions are conservative over the entire surface. The high Reynolds number intermittency model prediction is a better representation of the

data. On the pressure surface, both the fully turbulent and the low Reynolds number intermittency models provide reasonable predictions of the data. The high Reynolds number intermittency model prediction on this surface is lower than the other two predictions by about $15 \%$ as would be anticipated.

### 3.5 Blade Platform, Blade Tip and Shroud Results for Design Speed Condition

Figures 3.5.1 and 3.5.2 present the blade platform Stanton number distribution for the low and high Reynolds number conditions, respectively, at three values of overall stage pressure ratio. At the higher Reynolds number, the data for the values of stage pressure ratio are in reasonable agreement. The low Reynolds number results presented in Figure 3.5 .1 also suggest that the influence of pressure ratio is small. Further, the influence of Reynolds number appears to be small. For both Reynolds number cases, the trend of the data is to show a relatively small Stanton number increase in the chordwise direction. However, with only two measurement locations, it is difficult to determine anything more than this trend. The platform Stanton number values are of the same order as the blade midspan values.

Figures 3.5 .3 and 3.5 .4 present the Stanton number results obtained from the gages located in the blade tip at the low and high Reynolds number condition, respectively. The high Reynolds number results of runs 7, 8 and run 11 (Figure 3.5.4) were obtained at values of pressure ratio ranging from 1.38 to 1.48. The results of run 11 are shown to consistently fall below those of run 8 . Run 7 , which was performed at the larger value of stage pressure ratio rac....sed results at the $75 \%$ chord location which are not consistent with a well defined influence of pressure ratio on the tip Stanton number. There also appears to be a rather wide range in Stanton number value at the $39 \%$ tipregion measuring station. The low Reynolds number experiments (which were run at stage pressure ratios of 1.54 and 1.65 ) illustrate even a more pronounced variation in results at the $18 \%$ measuring station (shown on Figure 3.5.3) than was shown at $39 \%$ tip




chord. There does not appear to be definitive influence of either Reynolds number or stage pressure ratio on the heat transfer results. For both Reynolds number cases, the tip region Stanton number values start out at small chord values with a rather wide variation, but converge near midchord. At chord values less than $40 \%$, the tip Stanton numbers are on the order of the blade midspan values, but at large chord values the tip Stanton numbers rapidly approach the blade stagnation point value.

Figures 3.5 .5 and 3.5 .6 present the Stanton number distributions on the stationary shroud. The high Reynolds number data presented on Figure 3.5.6 illustrate a relatively high value of Stanton number over the entire region for which data were obtained. Stage pressure ratio does not appear to influence the results. Figure 3.5 .5 presents corresponding results for the low Reynolds number test case. The results for both Reynolds numbers appear to be relatively independent of both Reynolds number and stage pressure ratio. For both Reynolds number cases, the shroud Stanton numbers are not as large as the blade stagnation point or tip values, but they are larger than the values measured at other blade locations.

Figures 3.5.7 and 3.5.8 are composite plots of the platform, tip and shroud Stanton number data as a function of blade chord. The root and tip locations are noted on the abscissa. For the data presented in both of these plots, the tip data are shown to be generally greater than either the platform or shroud data. The shroud data fall between the tip and the platform levels.

### 3.6 Vane and Blade Surface Results for Off-Design Speed (68\% Design Speed)

Figures 3.6.1-3.6.3 plot the Stanton number distributions for the $50 \%$, high Reynolds number runs on the first vane, first blade and second vane, respectively. These are included to complete the comparison between full speed and off-design speed data. As would be expected, speed has relatively little influence on the first vane for the vane pressure ratio of this turbine (Figure 3.6.1). Figure 3.6 .2 presents the first blade data and

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illustrates that in the vicinity of the leading edge, incidence angle has a noticeable influence on the magnitude of the Stanton number. Beyond $20 \%$ wetted distance on the pressure surface the influence of incidence angle is shown to be relatively small. For the suction surface at wetted distances less than $30 \%$, the trend is not consistent apparently because of the transition location. At $50 \%$ wetted distance and beyond, the off-speed data are generally above the design speed data. Figure 3.6 .3 presents the second vane Stanton number results. In the immediate region of the leading edge ( $5 \%$ to $10 \%$ ), the off-design turbine speed appears to have an influence on the second vane Stanton number distribution. If there was going to be an influence, it is in this region that one would expect it to occur. However, on the second vane, the influence dies out much more rapidly than it did for the first blade, being essentially gone by about $5 \%$ wetted distance on the pressure surface and by $20 \%$ wetted distance on the suction surface.

### 3.7 Blade Platform, Tip and Shroud Results for Off-Design Speed

Figures 3.7.1-3.7.3 present a comparison of the off speed ( $68 \%$ of design value) data with the design speed data for the blade platform, blade tip and the shroud, respectively. The data presented were obtained at the high Reynolds number at a stage pressure ratio of approximately 1.4 and 1.5. The results presented on Figure 3.7.1 for the platform illustrate that at each of the locations, the Stanton number results do not appear to be influenced by rotor speed. This is not surprising since both locations are sufficiently far from the stagnation point that incidence angle should not be important. Figure 3.7.2 compares the cre $d$ and design speed tip region data. For this region, Metzger and Rued, 1989 have shown that blade relative motion should not have a significant influence on the average tip region heat transfer. At two measuring stations, the off speed results fall above the design speed values. However, at the third station, this is not true and thus the results are inconclusive. Figure 3.7 .3 presents the time averaged shroud heat transfer results. The Stanton number is shown to have an increasing trend



towards the blade trailing edge as would be anticipated because of the increasing driver pressure on the flow through the tip in moving from the leading edge towards the trailing edge. For a reduced rotor speed, a particular gage in the shroud would be exposed to the tip gap flow for a longer period of time (per rotor revolution) but it is also clear of the rotor tip for a longer period of time. The fraction of time for which the shroud gage is covered by the tip is the same as it is for the higher speed. If the gap flow is the same, then one would not expect to see a significant influence on Stanton number. However, because the influence of rotor speed on the blade surface pressure distribution in the tip region was not measured it is not possible to be certain that the tip flow was the same for both speeds and thus it is difficult to close the discussion of this point.

## SECTION 4

## CONCLUSIONS

Surface pressure and Stanton number distributions have been measured at selected locations on the first vane, first blade and second vane of a full two-stage turbine. The first vane and first blade pressure measurements have been compared with the prediction, but the agreement was not particularly good because of difficulties with the measurement. The measured Stanton number distributions at midspan for the first vane and the first blade have been compared with predictions obtained using a quasi-3D N-S code and a modified STAN5 technique. For the first vane, comparisons were presented for the fully turbulent case and for the transition case using two transition models (Mayle, 1991 and Dunham, 1972). At the low Reynolds number, the Mayle transition model and the fully turbulent prediction provided good agreement with the suction surface data. The fully turbulent, the Mayle transition model, and the Dunham transition model all provided good agreement with the suction surface data for the high Reynolds number case. The first vane pressure surface data were consistently underpredicted by all of the predictions. The sensitivity of the predictions to flow parameters such as turbulence intensity, coupled with the lack of agreement for the vane pressure surface heat transfer illustrates the importance of correctly modeling the actual flow field in any heat transfer analysis.

The first blade data were compared to N-S turbulent and N-S with the Mayle and Dullenkopf, 1989, 1990 intermittency model predictions. There is very little difference between the results of these two predictions. For the blade suction surface, the predictions were consistently above the data. The agreement between data and prediction for the pressure surface was reasonably good.

The surface of the blade used in these experiments appeared to be very rough. However, when the roughness density was accounted for, the analysis showed only a small increase in blade heat transfer due to surface roughness. The relatively good
agreement between the measured and predicted rotor heat transfer supports this conclusion. In the analysis the effect of surface roughness is strongly dependent on Reynolds number. Consequently, for the actual SSME engine operating conditions the analysis predicts a significant increase in blade heat transfer due to surface roughness.

The second vane data were compared with N-S fully turbulent calculations and with a N-S solution including the Mayle and Dullenkopf intermittency model. For the suction surface, both calculations were generally conservative. However, for the pressure surface, the predicted Stanton number distributions were in good agreement with the experimental data.

The tip region was shown to exhibit high heat-transfer rates by comparison with the blade stagnation-point value. The shroud Stanton number values were less than the tip values, but higher than the platform values. Data were presented to illustrate the influence of off-design rotor speed on the vane and blade Stanton number distributions. The first vane Stanton number distribution was also not influenced by rotor speed. The tip and shroud distributions were not significantly influenced by rotor speed. However, both the first blade and the second vane were influenced by rotor speed in the vicinity of the leading edge. This influence persisted on the first blade over a greater portion of the surface than it did on the second vane.

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## APPENDIX

## A. 1 Vane and Blade Coordinates

## A.1.1 First Nozzle Coordinates

| First nozzle, hub |  |  |
| :--- | :---: | :---: |
|  | x [in] | y[in] |
|  | 0.00013213 | 0.85099 |
| 1 | 0.00052741 | 0.84738 |
| 2 | 0.0011839 | 0.84380 |
| 3 | 0.0020981 | 0.84027 |
| 4 | 0.0032653 | 0.83683 |
| 6 | 0.0046793 | 0.83347 |
| 7 | 0.0063326 | 0.83023 |
| 8 | 0.0082165 | 0.82712 |
| 9 | 0.010321 | 0.82415 |
| 10 | 0.012636 | 0.82134 |
| 11 | 0.015147 | 0.81870 |
| 12 | 0.017843 | 0.81626 |
| 13 | 0.020710 | 0.81402 |
| 14 | 0.023731 | 0.81199 |
| 15 | 0.026891 | 0.81018 |
| 16 | 0.030173 | 0.80861 |
| 17 | 0.033561 | 0.80728 |
| 18 | 0.037036 | 0.80620 |
| 19 | 0.040580 | 0.80538 |
| 20 | 0.057465 | 0.80198 |
| 21 | 0.074350 | 0.79836 |
| 22 | 0.091235 | 0.79453 |
| 23 | 0.10812 | 0.79048 |
| 24 | 0.12500 | 0.78620 |
| 25 | 0.14189 | 0.78169 |
| 26 | 0.15877 | 0.77696 |
| 27 | 0.17566 | 0.77199 |
| 28 | 0.19254 | 0.76678 |
| 29 | 0.20943 | 0.76133 |
| 30 | 0.22631 | 0.75564 |
| 31 | 0.24320 | 0.74969 |
| 32 | 0.26008 | 0.74349 |
| 33 | 0.27697 | 0.73703 |
| 34 | 0.29385 | 0.73031 |
| 35 | 0.31074 | 0.72331 |
| 36 | $0.3-10$ | 0.71603 |
| 37 | 0.34451 | 0.70847 |
| 38 | 0.36139 | 0.70062 |
| 39 | 0.37828 | 0.69246 |
| 40 | 0.39516 | 0.68401 |
| 41 | 0.4205 | 0.67523 |
| 42 | 0.42893 | 0.66613 |
| 43 | 0.44582 | 0.65670 |
| 44 | 0.46270 | 0.64692 |
| 45 | 0.47959 | 0.63678 |
|  |  |  |


| 46 | 0.49647 | 0.62627 |
| :--- | :--- | :--- |
| 47 | 0.51336 | 0.61539 |
| 48 | 0.53024 | 0.60410 |
| 49 | 0.54713 | 0.59240 |
| 50 | 0.56401 | 0.58027 |
| 51 | 0.58090 | 0.56769 |
| 52 | 0.59778 | 0.55464 |
| 53 | 0.61467 | 0.54110 |
| 54 | 0.63155 | 0.52705 |
| 55 | 0.64844 | 0.51244 |
| 56 | 0.66532 | 0.49727 |
| 57 | 0.68220 | 0.48148 |
| 58 | 0.69909 | 0.46504 |
| 59 | 0.71597 | 0.44791 |
| 60 | 0.73286 | 0.43004 |
| 61 | 0.74974 | 0.41137 |
| 62 | 0.76663 | 0.39184 |
| 63 | 0.78351 | 0.37136 |
| 64 | 0.80040 | 0.34986 |
| 65 | 0.81728 | 0.32721 |
| 66 | 0.83417 | 0.30331 |
| 67 | 0.85105 | 0.27798 |
| 68 | 0.86794 | 0.25103 |
| 69 | 0.88482 | 0.22221 |
| 70 | 0.90171 | 0.19120 |
| 71 | 0.91859 | 0.15755 |
| 72 | 0.93547 | 0.12064 |
| 73 | 0.95226 | 0.079845 |
| 74 | 0.95938 | 0.061524 |
| 75 | 0.96650 | 0.043204 |
| 76 | 0.97361 | 0.024844 |
| 77 | 0.98073 | 0.0065631 |
| 78 | 0.98230 | 0.0038427 |
| 79 | 0.98463 | 0.0017172 |
| 80 | 0.98750 | 0.00039538 |
| 81 | 0.99063 | $4.5100 e-06$ |
| 82 | 0.99374 | 0.00058252 |
| 83 | 0.99652 | 0.0020755 |
| 84 | 0.99872 | 0.0043429 |
| 85 | 1.0001 | 0.0071712 |
| 86 | 1.0006 | 0.010294 |
| 87 | 1.0006 | 0.011143 |
| 88 | 1.0005 | 0.011986 |
| 89 | 1.0003 | 0.012818 |
| 90 | 1.0001 | 0.013632 |
| 91 | 0.98945 | 0.044610 |
| 92 | 0.97884 | 0.075588 |
| 93 | 0.96823 | 0.10657 |
|  |  |  |


|  | 94 | 0.95762 | 0.13754 | 148 | 0.36250 | 0.98585 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | 95 | 0.94701 | 0.16852 | 149 | 0.35056 | 0.98708 |
|  | 96 | 0.93640 | 0.19950 | 150 | 0.33862 | 0.98796 |
|  | 97 | 0.92579 | 0.23047 | 151 | 0.32668 | 0.98848 |
|  | 98 | 0.91517 | 0.26145 | 152 | 0.31474 | 0.98865 |
| - | 99 | 0.90456 | 0.29243 | 153 | 0.30462 | 0.98856 |
|  | 100 | 0.89579 | 0.31792 | 154 | 0.29439 | 0.98827 |
|  | 101 | 0.88691 | 0.34341 | 155 | 0.28417 | 0.98779 |
| - | 102 | 0.87803 | 0.36860 | 156 | 0.27395 | 0.98712 |
|  | 103 | 0.86915 | 0.39346 | 157 | 0.26373 | 0.98626 |
|  | 104 | 0.86027 | 0.41799 | 158 | 0.25351 | 0.98521 |
| - | 105 | 0.85139 | 0.44216 | 159 | 0.24329 | 0.98396 |
|  | 106 | 0.84251 | 0.46596 | 160 | 0.23307 | 0.98252 |
|  | 107 | 0.83363 | 0.48935 | 161 | 0.22285 | 0.98088 |
|  | 108 | 0.82475 | 0.51232 | 162 | 0.21263 | 0.97903 |
| - | 109 | 0.81587 | 0.53485 | 163 | 0.20241 | 0.97698 |
|  | 110 | 0.80700 | 0.55689 | 164 | 0.19219 | 0.97472 |
|  | 111 | 0.79812 | 0.57842 | 165 | 0.18197 | 0.97224 |
| - | 112 | 0.78924 | 0.59939 | 166 | 0.17174 | 0.96954 |
|  | 113 | 0.78036 | 0.61975 | 167 | 0.16152 | 0.96661 |
|  | 114 | 0.76852 | 0.64546 | 168 | 0.15130 | 0.96344 |
| - | 115 | 0.75657 | 0.66951 | 169 | 0.14108 | 0.96003 |
|  | 116 | 0.74463 | 0.69194 | 170 | 0.13086 | 0.95635 |
|  | 117 | 0.73269 | 0.71293 | 171 | 0.12064 | 0.95241 |
|  | 118 | 0.72075 | 0.73262 | 172 | 0.11042 | 0.94819 |
| - | 119 | 0.70881 | 0.75107 | 173 | 0.10020 | 0.94367 |
|  | 120 | 0.69686 | 0.76840 | 174 | 0.089978 | 0.93883 |
|  | 121 | 0.68492 | 0.78470 | 175 | 0.079757 | 0.93365 |
| - | 122 | 0.67298 | 0.80004 | 176 | 0.069536 | 0.92810 |
|  | 123 | 0.66104 | 0.81450 | 177 | 0.059316 | 0.92215 |
|  | 124 | 0.64910 | 0.82813 | 178 | 0.049095 | 0.91577 |
|  | 125 | 0.63716 | 0.84099 | 179 | 0.038874 | 0.90891 |
| - | 126 | 0.62521 | 0.85311 | 180 | 0.028653 | 0.90151 |
|  | 127 | 0.61327 | 0.86455 | 181 | 0.018432 | 0.89349 |
|  | 128 | 0.60133 | 0.87533 | 182 | 0.016656 | 0.89197 |
| - | 129 | 0.58939 | 0.88549 | 183 | 0.014952 | 0.89037 |
|  | 130 | 0.57745 | 0.89505 | 184 | 0.013325 | 0.88869 |
|  | 131 | 0.56551 | 0.90404 | 185 | 0.011778 | 0.88693 |
| - | 132 | 0.55357 | 0.91249 | 186 | 0.010314 | 0.88511 |
|  | 133 | 0.54162 | 0.92041 | 187 | 0.0089374 | 0.88322 |
|  | 134 | 0.52968 | 0.92783 | 188 | 0.0076500 | 0.88126 |
| - | 135 | 0.51774 | 0.93476 | 189 | 0.0064551 | 0.87925 |
|  | 136 | 0.50580 | 0.94121 | 190 | 0.0053553 | 0.87719 |
|  | 137 | 0.49386 | 0.94720 | 191 | 0.0043528 | 0.87507 |
|  | 138 | 0.48192 | U.Sン2\% | 192 | 0.0034499 | 0.87292 |
| - | 139 | 0.46998 | 0.95787 | 193 | 0.0026486 | 0.87072 |
|  | 140 | 0.45803 | 0.96256 | 194 | 0.0019505 | 0.86849 |
|  | 141 | 0.44609 | 0.96683 | 195 | 0.0013573 | 0.86622 |
| - | 142 | 0.43415 | 0.97070 | 196 | 0.00087012 | 0.86393 |
|  | 143 | 0.42221 | 0.97418 | 197 | 0.00049012 | 0.86163 |
|  | 144 | 0.41027 | 0.97726 | 198 | 0.00021811 | 0.85930 |
| - | 145 | 0.39833 | 0.97997 | 199 | $5.4660 \mathrm{e}-05$ | 0.85697 |
|  | 146 | 0.38638 | 0.98230 | 200 | $1.4000 \mathrm{e}-07$ | 0.85463 |


| First nozzle, midspan |  |  | 52 | 0.62117 | 0.56245 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 53 | 0.63877 | 0.54814 |
|  | x [in] | y[in] | 54 | 0.65637 | 0.53329 |
| 1 | 0.00013143 | 0.87560 | 55 | 0.67397 | 0.51789 |
| 2 | 0.00052459 | 0.87200 | 56 | 0.69157 | 0.50191 |
| 3 | 0.0011775 | 0.86843 | 57 | 0.70917 | 0.48530 |
| 4 | 0.0020869 | 0.86491 | 58 | 0.72677 | 0.46804 |
| 5 | 0.0032478 | 0.86147 | 59 | 0.74437 | 0.45009 |
| 6 | 0.0046542 | 0.85813 | 60 | 0.76197 | 0.43139 |
| 7 | 0.0062986 | 0.85489 | 61 | 0.77957 | 0.41189 |
| 8 | 0.0081725 | 0.85179 | 62 | 0.79717 | 0.39153 |
| 9 | 0.010266 | 0.84882 | 63 | 0.81477 | 0.37025 |
| 10 | 0.012568 | 0.84602 | 64 | 0.83237 | 0.34795 |
| 11 | 0.015066 | 0.84339 | 65 | 0.84997 | 0.32454 |
| 12 | 0.017748 | 0.84094 | 66 | 0.86757 | 0.29991 |
| 13 | 0.020599 | 0.83870 | 67 | 0.88517 | 0.27391 |
| 14 | 0.023603 | 0.83667 | 68 | 0.90277 | 0.24636 |
| 15 | 0.026747 | 0.83486 | 69 | 0.92037 | 0.21706 |
| 16 | 0.030012 | 0.83329 | 70 | 0.93796 | 0.18573 |
| 17 | 0.033381 | 0.83195 | 71 | 0.95556 | 0.15198 |
| 18 | 0.036838 | 0.83086 | 72 | 0.97316 | 0.11533 |
| 19 | 0.040363 | 0.83003 | 73 | 0.99066 | 0.075653 |
| 20 | 0.057963 | 0.82639 | 74 | 0.99808 | 0.058299 |
| 21 | 0.075563 | 0.82253 | 75 | 1.0055 | 0.040945 |
| 22 | 0.093164 | 0.81843 | 76 | 1.0129 | 0.023591 |
| 23 | 0.11076 | 0.81408 | 77 | 1.0203 | 0.0062364 |
| 24 | 0.12836 | 0.80950 | 78 | 1.0219 | 0.0036896 |
| 25 | 0.14596 | 0.80467 | 79 | 1.0242 | 0.0016451 |
| 26 | 0.16356 | 0.79959 | 80 | 1.0271 | 0.00037010 |
| 27 | 0.18117 | 0.79426 | 81 | 1.0302 | $6.9900 \mathrm{e}-06$ |
| 28 | 0.19877 | 0.78868 | 82 | 1.0333 | 0.00059956 |
| 29 | 0.21637 | 0.78283 | 83 | 1.0360 | 0.0020971 |
| 30 | 0.23397 | 0.77673 | 84 | 1.0382 | 0.0043615 |
| 31 | 0.25157 | 0.77035 | 85 | 1.0396 | 0.0071818 |
| 32 | 0.26917 | 0.76370 | 86 | 1.0401 | 0.01029 .4 |
| 33 | 0.28677 | 0.75678 | 87 | 1.0400 | 0.011221 |
| 34 | 0.30437 | 0.74957 | 88 | 1.0399 | 0.012141 |
| 35 | 0.32197 | 0.74207 | 89 | 1.0397 | 0.013047 |
| 36 | 0.33957 | 0.73427 | 90 | 1.0394 | 0.013931 |
| 37 | 0.35717 | 0.72618 | 91 | 1.0284 | 0.043257 |
| 38 | 0.37477 | 0.71778 | 92 | 1.0173 | 0.072584 |
| 39 | 0.39237 | 0.70906 | 93 | 1.0063 | 0.10191 |
| 40 | 0.40997 | 0.70002 | 94 | 0.99527 | 0.13124 |
| 41 | 0.42757 | 0.69065 | 95 | 0.98424 | 0.16056 |
| 42 | 0.44517 | 0.68093 | 96 | 0.97320 | 0.18989 |
| 43 | 0.46277 | 0.67087 | 97 | 0.96217 | 0.21921 |
| 44 | 0.48037 | 0.66044 | 98 | 0.95113 | 0.24853 |
| 45 | 0.49797 | 0.64964 | 99 | 0.94010 | 0.27786 |
| 46 | 0.51557 | 0.63846 | 100 | 0.93097 | 0.30205 |
| 47 | 0.53317 | 0.62687 | 101 | 0.92174 | 0.32639 |
| 48 | 0.55077 | 0.61488 | 102 | 0.91250 | 0.35059 |
| 49 | 0.56837 | 0.60246 | 103 | 0.90327 | 0.37464 |
| 50 | 0.58597 | 0.58959 | 104 | 0.89403 | 0.39854 |
| 51 | 0.60357 | 0.57627 | 105 | 0.88480 | 0.42227 |


| 106 | 0.87557 | 0.44583 | 160 | 0.24168 | 1.0127 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 107 | 0.86633 | 0.46921 | 161 | 0.23105 | 1.0109 |
| 108 | 0.85710 | 0.49239 | 162 | 0.22042 | 1.0088 |
| 109 | 0.84786 | 0.51537 | 163 | 0.20979 | 1.0065 |
| 110 | 0.83863 | 0.53813 | 164 | 0.19916 | 1.0040 |
| 111 | 0.82940 | 0.56065 | 165 | 0.18853 | 1.0012 |
| 112 | 0.82016 | 0.58292 | 166 | 0.17789 | 0.99829 |
| 113 | 0.81092 | 0.60474 | 167 | 0.16726 | 0.99509 |
| 114 | 0.79861 | 0.63284 | 168 | 0.15663 | 0.99166 |
| 115 | 0.78619 | 0.65993 | 169 | 0.14600 | 0.98797 |
| 116 | 0.77377 | 0.68587 | 170 | 0.13537 | 0.98403 |
| 117 | 0.76134 | 0.71073 | 171 | 0.12474 | 0.97981 |
| 118 | 0.74892 | 0.73442 | 172 | 0.11411 | 0.97532 |
| 119 | 0.73650 | 0.75655 | 173 | 0.10348 | 0.97052 |
| 120 | 0.72408 | 0.77724 | 174 | 0.092848 | 0.96541 |
| 121 | 0.71166 | 0.79658 | 175 | 0.082217 | 0.95996 |
| 122 | 0.69924 | 0.81467 | 176 | 0.071586 | 0.95414 |
| 123 | 0.68681 | 0.83160 | 177 | 0.060955 | 0.94792 |
| 124 | 0.67439 | 0.84745 | 178 | 0.050325 | 0.94126 |
| 125 | 0.66197 | 0.86227 | 179 | 0.039694 | 0.93412 |
| 126 | 0.64955 | 0.87615 | 180 | 0.029063 | 0.92642 |
| 127 | 0.63713 | 0.88912 | 181 | 0.018432 | 0.91809 |
| 128 | 0.62471 | 0.90125 | 182 | 0.016656 | 0.91656 |
| 129 | 0.61229 | 0.91258 | 183 | 0.014952 | 0.91496 |
| 130 | 0.59987 | 0.92316 | 184 | 0.013325 | 0.91328 |
| 131 | 0.58745 | 0.93301 | 185 | 0.011778 | 0.91153 |
| 132 | 0.57503 | 0.94219 | 186 | 0.010314 | 0.90970 |
| 133 | 0.56261 | 0.95072 | 187 | 0.0089374 | 0.90781 |
| 134 | 0.55019 | 0.95863 | 188 | 0.0076500 | 0.90586 |
| 135 | 0.53777 | 0.96595 | 189 | 0.0064551 | 0.90385 |
| 136 | 0.52535 | 0.97271 | 190 | 0.0053553 | 0.90178 |
| 137 | 0.51293 | 0.97894 | 191 | 0.0043528 | 0.89967 |
| 138 | 0.50051 | 0.98465 | 192 | 0.0034499 | 0.89751 |
| 139 | 0.48809 | 0.98986 | 193 | 0.0026486 | 0.89532 |
| 140 | 0.47567 | 0.99460 | 194 | 0.0019505 | 0.89308 |
| 141 | 0.46325 | 0.99888 | 195 | 0.0013573 | 0.89082 |
| 142 | 0.45083 | 1.0027 | 196 | 0.00087012 | 0.88853 |
| 143 | 0.43840 | 1.0061 | 197 | 0.00049013 | 0.88623 |
| 144 | 0.42598 | 1.0091 | 198 | 0.00021811 | 0.88390 |
| 145 | 0.41356 | 1.0117 | 199 | $5.4660 \mathrm{e}-05$ | 0.88157 |
| 146 | 0.40114 | 1.0140 | 200 | $1.4000 \mathrm{e}-07$ | 0.87923 |
| 147 | 0.38872 | 1.0158 |  |  |  |
| 148 | 0.37630 | 1.0173 |  |  |  |
| 149 | 0.36388 | 1.0185 |  |  |  |
| 150 | 0.35146 | 1.0193 |  |  |  |
| 151 | 0.33904 | 1.0197 |  |  |  |
| 152 | 0.32662 | 1.0199 |  |  |  |
| 153 | 0.31609 | 1.0197 |  |  |  |
| 154 | 0.30546 | 1.0194 |  |  |  |
| 155 | 0.29483 | 1.0188 |  |  |  |
| 156 | 0.28420 | 1.0180 |  |  |  |
| 157 | 0.27357 | 1.0170 |  |  |  |
| 158 | 0.26294 | 1.0158 |  |  |  |
| 159 | 0.25231 | 1.0144 |  |  |  |


| First nozzle, tip |  |  | 52 | 0.64454 | 0.57030 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 53 | 0.66286 | 0.55520 |
|  | x [in] | $y$ [in] | 54 | 0.68117 | 0.53957 |
| 1 | 0.00013073 | 0.90027 | 55 | 0.69949 | 0.52337 |
| 2 | 0.00052177 | 0.89667 | 56 | 0.71780 | 0.50657 |
| 3 | 0.0011712 | 0.89311 | 57 | 0.73612 | 0.48915 |
| 4 | 0.0020757 | 0.88961 | 58 | 0.75443 | 0.47107 |
| 5 | 0.0032303 | 0.88618 | 59 | 0.77275 | 0.45229 |
| 6 | 0.0046291 | 0.88284 | 60 | 0.79106 | 0.43276 |
| 7 | 0.0062647 | 0.87961 | 61 | 0.80938 | 0.41243 |
| 8 | 0.0081285 | 0.87651 | 62 | 0.82769 | 0.39125 |
| 9 | 0.010211 | 0.87355 | 63 | 0.84601 | 0.36915 |
| 10 | 0.012500 | 0.87075 | 64 | 0.86432 | 0.34606 |
| 11 | 0.014985 | 0.86812 | 65 | 0.88264 | 0.32188 |
| 12 | 0.017652 | 0.86568 | 66 | 0.90095 | 0.29652 |
| 13 | 0.020488 | 0.86344 | 67 | 0.91927 | 0.26984 |
| 14 | 0.023476 | 0.86140 | 68 | 0.93759 | 0.24171 |
| 15 | 0.026603 | 0.85959 | 69 | 0.95590 | 0.21192 |
| 16 | 0.029850 | 0.85801 | 70 | 0.97422 | 0.18026 |
| 17 | 0.033202 | 0.85667 | 71 | 0.99253 | 0.14642 |
| 18 | 0.036639 | 0.85557 | 72 | 1.0108 | 0.11002 |
| 19 | 0.040145 | 0.85472 | 73 | 1.0291 | 0.071462 |
| 20 | 0.058460 | 0.85086 | 74 | 1.0368 | 0.055074 |
| 21 | 0.076775 | 0.84674 | 75 | 1.0445 | 0.038686 |
| 22 | 0.095090 | 0.84237 | 76 | 1.0522 | 0.022298 |
| 23 | 0.11341 | 0.83774 | 77 | 1.0599 | 0.0059098 |
| 24 | 0.13172 | 0.83285 | 78 | 1.0615 | 0.0035365 |
| 25 | 0.15004 | 0.82769 | 79 | 1.0638 | 0.0015731 |
| 26 | 0.16835 | 0.82227 | 80 | 1.0666 | 0.00034483 |
| 27 | 0.18667 | 0.81658 | 81 | 1.0697 | $9.4700 \mathrm{e}-06$ |
| 28 | 0.20498 | 0.81062 | 82 | 1.0728 | 0.00061660 |
| 29 | 0.22330 | 0.80438 | 83 | 1.0755 | 0.0021187 |
| 30 | 0.24161 | 0.79786 | 84 | 1.0777 | 0.0043802 |
| 31 | 0.25993 | 0.79105 | 85 | 1.0791 | 0.0071925 |
| 32 | 0.27824 | 0.78395 | 86 | 1.0795 | 0.010294 |
| 33 | 0.29656 | 0.77656 | 87 | 1.0795 | 0.011300 |
| 34 | 0.31487 | 0.76887 | 88 | 1.0794 | 0.012297 |
| 35 | 0.33319 | 0.76087 | 89 | 1.0791 | 0.013276 |
| 36 | 0.35150 | 0.75256 | 90 | 1.0788 | 0.014229 |
| 37 | 0.36982 | 0.74393 | 91 | 1.0673 | 0.041904 |
| 38 | 0.38813 | 0.73498 | 92 | 1.0558 | 0.069580 |
| 39 | 0.40645 | 0.72570 | 93 | 1.0444 | 0.097256 |
| 40 | 0.42476 | 0.71607 | 94 | 1.0329 | 0.12493 |
| 41 | 0.44308 | 0.70610 | 95 | 1.0215 | 0.15261 |
| 42 | 0.46139 | 0.69577 | 96 | 1.010 | 0.18028 |
| 43 | 0.47971 | 0.68507 | 97 | 0.99853 | 0.20796 |
| 44 | 0.49802 | 0.67400 | 98 | 0.98707 | 0.23564 |
| 45 | 0.51634 | 0.66254 | 99 | 0.97561 | 0.26331 |
| 46 | 0.53465 | 0.65068 | 100 | 0.96612 | 0.28622 |
| 47 | 0.55297 | 0.63840 | 101 | 0.95653 | 0.30942 |
| 48 | 0.57128 | 0.62570 | 102 | 0.94694 | 0.33264 |
| 49 | 0.58960 | 0.61255 | 103 | 0.93735 | 0.35589 |
| 50 | 0.60791 | 0.59895 | 104 | 0.92776 | 0.37916 |
| 51 | 0.62623 | 0.58487 | 105 | 0.91816 | 0.40247 |


|  | 106 | 0.90857 | 0.42580 | 154 | 0.31652 | 1.0506 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | 107 | 0.89898 | 0.44917 | 155 | 0.30548 | 1.0499 |
|  | 108 | 0.88939 | 0.47258 | 156 | 0.29444 | 1.0490 |
|  | 109 | 0.87980 | 0.49602 | 157 | 0.28340 | 1.0479 |
| - | 110 | 0.87020 | 0.51950 | 158 | 0.27236 | 1.0465 |
|  | 111 | 0.86061 | 0.54302 | 159 | 0.26132 | 1.0448 |
|  | 112 | 0.85102 | 0.56657 | 160 | 0.25028 | 1.0430 |
|  | 113 | 0.84143 | 0.58987 | 161 | 0.23924 | 1.0409 |
| - | 114 | 0.82864 | 0.62037 | 162 | 0.22820 | 1.0386 |
|  | 115 | 0.81574 | 0.65049 | 163 | 0.21716 | 1.0361 |
|  | 116 | 0.80284 | 0.67992 | 164 | 0.20612 | 1.0333 |
| - | 117 | 0.78994 | 0.70864 | 165 | 0.19507 | 1.0303 |
|  | 118 | 0.77705 | 0.73632 | 166 | 0.18403 | 1.0271 |
|  | 119 | 0.76415 | 0.76214 | 167 | 0.17299 | 1.0237 |
|  | 120 | 0.75125 | 0.78617 | 168 | 0.16195 | 1.0200 |
| - | 121 | 0.73835 | 0.80855 | 169 | 0.15091 | 1.0160 |
|  | 122 | 0.72545 | 0.82939 | 170 | 0.13987 | 1.0118 |
|  | 123 | 0.71255 | 0.84878 | 171 | 0.12883 | 1.0073 |
| - | 124 | 0.69966 | 0.86684 | 172 | 0.11779 | 1.0025 |
|  | 125 | 0.68676 | 0.88363 | 173 | 0.10675 | 0.99746 |
|  | 126 | 0.67386 | 0.89925 | 174 | 0.095713 | 0.99208 |
| - | 127 | 0.66096 | 0.91376 | 175 | 0.084673 | 0.98635 |
|  | 128 | 0.64806 | 0.92724 | 176 | 0.073633 | 0.98026 |
|  | 129 | 0.63516 | 0.93974 | 177 | 0.062593 | 0.97377 |
|  | 130 | 0.62226 | 0.95133 | 178 | 0.051553 | 0.96683 |
|  | 131 | 0.60936 | 0.96205 | 179 | 0.040513 | 0.95940 |
|  | 132 | 0.59647 | 0.97195 | 180 | 0.029472 | 0.95141 |
|  | 133 | 0.58357 | 0.98109 | 181 | 0.018432 | 0.94276 |
| - | 134 | 0.57067 | 0.98949 | 182 | 0.016656 | 0.94123 |
|  | 135 | 0.55777 | 0.99722 | 183 | 0.014952 | 0.93963 |
|  | 136 | 0.54487 | 1.0043 | 184 | 0.013325 | 0.93795 |
| - | 137 | 0.53197 | 1.0107 | 185 | 0.011778 | 0.93619 |
|  | 138 | 0.51907 | 1.0166 | 186 | 0.010314 | 0.93437 |
|  | 139 | 0.50617 | 1.0219 | 187 | 0.0089374 | 0.93248 |
|  | 140 | 0.49327 | 1.0267 | 188 | 0.0076500 | 0.93053 |
| - | 141 | 0.48038 | 1.0310 | 189 | 0.0064551 | 0.92851 |
|  | 142 | 0.46748 | 1.0348 | 190 | 0.0053553 | 0.92645 |
|  | 143 | 0.45458 | 1.0382 | 191 | 0.0043528 | 0.92434 |
| - | 144 | 0.44168 | 1.0411 | 192 | 0.0034499 | 0.92218 |
|  | 145 | 0.42878 | 1.0436 | 193 | 0.0026486 | 0.91998 |
|  | 146 | 0.41588 | 1.0457 | 194 | 0.0019505 | 0.91775 |
| - | 147 | 0.40298 | 1.0475 | 195 | 0.0013573 | 0.91548 |
|  | 148 | 0.39008 | 1.0489 | 196 | 0.00087013 | 0.91320 |
|  | 149 | 0.37718 | 1.0499 | 197 | 0.00049013 | 0.91089 |
|  | 150 | 0.36429 | 1.0506 | 198 | 0.00021811 | 0.90856 |
| - | 151 | 0.35139 | 1.0511 | 199 | $5.4670 \mathrm{e}-05$ | 0.90623 |
|  | 152 | 0.33849 | 1.0512 | 200 | $1.5000 \mathrm{e}-07$ | 0.90389 |
|  | 153 | 0.32756 | 1.0510 |  |  |  |



Figure A..1.1--First nozzle: tip, midspan, and hub

| - | A.1.2 First Rotor Coordinates |  |  | 49 | 0.62869 | 0.063833 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | First rotor, hub |  |  | 50 | 0.64159 | 0.072549 |
|  |  |  |  | 51 | 0.65449 | 0.081985 |
| - | x [in] |  | $y[i n]$ | 52 | 0.66739 | 0.092182 |
|  |  |  | 53 | 0.68029 | 0.10319 |
|  | 1 | 0.12085 |  | 0.22903 | 54 | 0.69319 | 0.11508 |
| - | 2 | 0.12139 | 0.22218 | 55 | 0.70609 | 0.12791 |
|  | 3 | 0.12192 | 0.21942 | 56 | 0.71899 | 0.14177 |
|  | 4 | 0.12246 | 0.21733 | 57 | 0.73189 | 0.15679 |
| - | 5 | 0.12299 | 0.21558 | 58 | 0.74479 | 0.17309 |
|  | 6 | 0.12352 | 0.21406 | 59 | 0.75759 | 0.19071 |
| - | 7 | 0.12406 | 0.21270 | 60 | 0.76711 | 0.20483 |
|  | 8 | 0.12459 | 0.21146 | 61 | 0.77662 | 0.21971 |
|  | 9 | 0.12513 | 0.21031 | 62 | 0.78613 | 0.23524 |
|  | 10 | 0.12556 | 0.20943 | 63 | 0.79565 | 0.25133 |
| - | 11 | 0.13846 | 0.18586 | 64 | 0.80516 | 0.26791 |
|  | 12 | 0.15136 | 0.16523 | 65 | 0.81468 | 0.28492 |
|  | 13 | 0.16426 | 0.14691 | 66 | 0.82419 | 0.30232 |
|  | 14 | 0.17716 | 0.13049 | 67 | 0.83371 | 0.32006 |
| - | 15 | 0.19007 | 0.11568 | 68 | 0.84322 | 0.33812 |
|  | 16 | 0.20297 | 0.10227 | 69 | 0.85273 | 0.35647 |
|  | 17 | 0.21587 | 0.090094 | 70 | 0.86225 | 0.37509 |
| - | 18 | 0.22877 | 0.079021 | 71 | 0.87176 | 0.39394 |
|  | 19 | 0.24167 | 0.068951 | 72 | 0.88128 | 0.41303 |
|  | 20 | 0.25457 | 0.059799 | 73 | 0.89079 | 0.43232 |
|  | 21 | 0.26747 | 0.051497 | 74 | 0.90030 | 0.45180 |
| - | 22 | 0.28037 | 0.043990 | 75 | 0.90982 | 0.47147 |
|  | 23 | 0.29327 | 0.037227 | 76 | 0.91933 | 0.49130 |
|  | 24 | 0.30617 | 0.031170 | 77 | 0.92885 | 0.51130 |
| - | 25 | 0.31907 | 0.025784 | 78 | 0.93826 | 0.53123 |
|  | 26 | 0.33197 | 0.021040 | 79 | 0.93867 | 0.53225 |
|  | 27 | 0.34487 | 0.016912 | 80 | 0.93897 | 0.53331 |
|  | 28 | 0.35777 | 0.013379 | 81 | 0.93915 | 0.53439 |
|  | 29 | 0.37067 | 0.010424 | 82 | 0.93921 | 0.53549 |
|  | 30 | 0.38357 | 0.0080306 | 83 | 0.93879 | 0.53836 |
|  | 31 | 0.39648 | 0.0061865 | 84 | 0.93756 | 0.54099 |
| - | 32 | 0.40938 | 0.0048812 | 85 | 0.93563 | 0.54316 |
|  | 33 | 0.42228 | 0.0041060 | 86 | 0.93316 | 0.54468 |
|  | 34 | 0.43518 | 0.0038545 | 87 | 0.93035 | 0.54543 |
|  | 35 | 0.44808 | 0.0041218 | 88 | 0.92745 | 0.54534 |
|  | 36 | 0.46098 | 0.0049050 | 89 | 0.92470 | 0.54442 |
|  | 37 | 0.47388 | 0.0062027 | 90 | 0.92233 | 0.54274 |
| - | 38 | 0.48678 | 0.0080152 | 91 | 0.92053 | 0.54046 |
|  | 39 | 0.49968 | $0 . \mathrm{vi} 0344$ | 92 | 0.90538 | 0.51508 |
|  | 40 | 0.51258 | 0.013194 | 93 | 0.89012 | 0.49148 |
|  | 41 | 0.52548 | 0.016569 | 94 | 0.87486 | 0.46955 |
| - | 42 | 0.53838 | 0.020478 | 95 | 0.85960 | 0.44909 |
|  | 43 | 0.55128 | 0.024929 | 96 | 0.84435 | 0.42991 |
|  | 44 | 0.56418 | 0.029933 | 97 | 0.82909 | 0.41190 |
|  | 45 | 0.57708 | 0.035504 | 98 | 0.81383 | 0.3949 |
|  | 46 | 0.58998 | 0.041659 | 99 | 0.79857 | 0.3789 |
|  | 47 | 0.60288 | 0.048416 | 100 | 0.78331 | 0.3638 |
|  | 48 | 0.61579 | 0.055799 | 101 | 0.76806 | 0.3496 |


|  | 102 | 0.75280 | 0.33613 | 156 | 0.14851 | 0.25838 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | 103 | 0.73754 | 0.32339 | 157 | 0.14698 | 0.25832 |
|  | 104 | 0.72228 | 0.31135 | 158 | 0.14544 | 0.25820 |
|  | 105 | 0.70703 | 0.29999 | 159 | 0.14390 | 0.25799 |
| - | 106 | 0.69177 | 0.28927 | 160 | 0.14237 | 0.25771 |
|  | 107 | 0.67651 | 0.27916 | 161 | 0.14083 | 0.25734 |
|  | 108 | 0.66125 | 0.26964 | 162 | 0.13929 | 0.25687 |
| - | 109 | 0.64599 | 0.26071 | 163 | 0.13776 | 0.25631 |
| - | 110 | 0.63074 | 0.25233 | 164 | 0.13622 | 0.25565 |
|  | 111 | 0.61548 | 0.24451 | 165 | 0.13468 | 0.25486 |
|  | 112 | 0.60022 | 0.23721 | 166 | 0.13315 | 0.25393 |
| - | 113 | 0.58496 | 0.23045 | 167 | 0.13161 | 0.25285 |
|  | 114 | 0.56971 | 0.22420 | 168 | 0.13007 | 0.25158 |
|  | 115 | 0.55445 | 0.21845 | 169 | 0.12854 | 0.25008 |
| - | 116 | 0.53919 | 0.21322 | 170 | 0.12700 | 0.24830 |
|  | 117 | 0.52393 | 0.20849 | 171 | 0.12546 | 0.24612 |
|  | 118 | 0.50867 | 0.20425 | 172 | 0.12393 | 0.24334 |
| - | 119 | 0.49342 | 0.20051 | 173 | 0.12239 | 0.23944 |
|  | 120 | 0.47816 | 0.19727 |  |  |  |
|  | 121 | 0.46290 | 0.19452 |  |  |  |
|  | 122 | 0.44764 | 0.19228 |  |  |  |
| - | 123 | 0.43238 | 0.19054 |  |  |  |
|  | 124 | 0.41713 | 0.18931 |  |  |  |
|  | 125 | 0.40187 | 0.18860 |  |  |  |
| - | 126 | 0.38661 | 0.18841 |  |  |  |
|  | 127 | 0.37135 | 0.18875 |  |  |  |
|  | 128 | 0.35610 | 0.18964 |  |  |  |
|  | 129 | 0.34084 | 0.19109 |  |  |  |
| - | 130 | 0.32558 | 0.19311 |  |  |  |
|  | 131 | 0.31032 | 0.19572 |  |  |  |
|  | 132 | 0.29506 | 0.19895 |  |  |  |
| - | 133 | 0.27981 | 0.20281 |  |  |  |
|  | 134 | 0.26455 | 0.20734 |  |  |  |
|  | 135 | 0.24929 | 0.21257 |  |  |  |
| - | 136 | 0.23403 | 0.21852 |  |  |  |
|  | 137 | 0.21878 | 0.22526 |  |  |  |
|  | 138 | 0.20352 | 0.23282 |  |  |  |
|  | 139 | 0.18826 | 0.24127 |  |  |  |
| - | 140 | 0.17300 | 0.25067 |  |  |  |
|  | 141 | 0.17157 | 0.25157 |  |  |  |
|  | 142 | 0.17003 | 0.25247 |  |  |  |
| - | 143 | 0.16849 | 0.25330 |  |  |  |
|  | 144 | 0.16696 | 0.25406 |  |  |  |
|  | 145 | 0.16542 | 0.25476 |  |  |  |
| - | 146 | 0.16388 | 0.25540 |  |  |  |
|  | 147 | 0.16234 | 0.25597 |  |  |  |
|  | 148 | 0.16081 | 0.25649 |  |  |  |
|  | 149 | 0.15927 | 0.25694 |  |  |  |
| - | 150 | 0.15773 | 0.25733 |  |  |  |
|  | 151 | 0.15620 | 0.25767 |  |  |  |
|  | 152 | 0.15466 | 0.25794 |  |  |  |
| $\sim$ | 153 | 0.15312 | 0.25814 |  |  |  |
|  | 154 | 0.15159 | 0.25829 |  |  |  |
|  | 155 | 0.15005 | 0.25837 |  |  |  |


| First rotor, midspan |  |  | 51 | 0.66155 | 0.074794 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 52 | 0.67315 | 0.085889 |
| x [in] |  | y[in] | 53 | 0.68476 | 0.097967 |
|  |  | 54 | 0.69636 | 0.11116 |
| 1 | 0.17979 |  | 0.15760 | 55 | 0.70796 | 0.12560 |
| 2 | 0.18048 | 0.15051 | 56 | 0.71956 | 0.14120 |
| 3 | 0.18117 | 0.14765 | 57 | 0.73117 | 0.15788 |
| 4 | 0.18186 | 0.14549 | 58 | 0.74277 | 0.17563 |
| 5 | 0.18255 | 0.14370 | 59 | 0.75428 | 0.19430 |
| 6 | 0.18325 | 0.14215 | 60 | 0.76284 | 0.20889 |
| 7 | 0.18394 | 0.14077 | 61 | 0.77140 | 0.22401 |
| 8 | 0.18463 | 0.13953 | 62 | 0.77996 | 0.23958 |
| 9 | 0.18532 | 0.13838 | 63 | 0.78851 | 0.25556 |
| 10 | 0.18588 | 0.13752 | 64 | 0.79707 | 0.27189 |
| 11 | 0.19747 | 0.11992 | 65 | 0.80563 | 0.28854 |
| 12 | 0.20907 | 0.10432 | 66 | 0.81418 | 0.30549 |
| 1.3 | 0.22066 | 0.090363 | 67 | 0.82274 | 0.32269 |
| 14 | 0.23226 | 0.077786 | 68 | 0.83130 | 0.34014 |
| 15 | 0.24386 | 0.066406 | 69 | 0.83986 | 0.35780 |
| 16 | 0.25546 | 0.056082 | 70 | 0.84841 | 0.37567 |
| 17 | 0.26706 | 0.046707 | 71 | 0.85697 | 0.39373 |
| 18 | 0.27866 | 0.038194 | 72 | 0.86553 | 0.41197 |
| 19 | 0.29026 | 0.030473 | 73 | 0.87408 | 0.43037 |
| 20 | 0.30186 | 0.023488 | 74 | 0.88264 | 0.44893 |
| 21 | 0.31346 | 0.017191 | 75 | 0.89120 | 0.46763 |
| 22 | 0.32506 | 0.011543 | 76 | 0.89975 | 0.48647 |
| 23 | 0.33667 | 0.0065094 | 77 | 0.90831 | 0.50544 |
| 24 | 0.34827 | 0.0020632 | 78 | 0.91677 | 0.52432 |
| 25 | 0.35987 | -0.0018200 | 79 | 0.91715 | 0.52530 |
| 26 | 0.37147 | -0.0051603 | 80 | 0.91742 | 0.52631 |
| 27 | 0.38308 | -0.0079749 | 81 | 0.91759 | 0.52735 |
| 28 | 0.39468 | -0.010278 | 82 | 0.91764 | 0.52839 |
| 29 | 0.40628 | -0.012082 | 83 | 0.91722 | 0.53127 |
| 30 | 0.41789 | -0.013396 | 84 | 0.91598 | 0.53391 |
| 31 | 0.42949 | -0.014227 | 85 | 0.91403 | 0.53608 |
| 32 | 0.44109 | -0.014583 | 86 | 0.91154 | 0.53760 |
| 33 | 0.45269 | -0.014466 | 87 | 0.90871 | 0.53833 |
| 34 | 0.46430 | -0.013880 | 88 | 0.90578 | 0.53822 |
| 35 | 0.4-590 | -0.012825 | 89 | 0.90301 | 0.53725 |
| 36 | 0.48750 | -0.011300 | 90 | 0.90061 | 0.53550 |
| 37 | 0.49911 | -0.0093034 | 91 | 0.89881 | 0.53307 |
| 38 | 0.51071 | -0.0068301 | 92 | 0.88521 | 0.50815 |
| 39 | 0.52231 | -0.0038744 | 93 | 0.87153 | 0.48428 |
| 40 | 0.53392 | -0.00042857 | 94 | 0.85784 | 0.46148 |
| 41 | 0.54552 | 0.0035173 | 95 | 0.84416 | 0.43968 |
| 42 | 0.55712 | 0.0079753 | 96 | 0.83047 | 0.41879 |
| 43 | 0.56873 | 0.012960 | 97 | 0.81679 | 0.39876 |
| 44 | 0.58033 | 0.018489 | 98 | 0.80310 | 0.37956 |
| 45 | 0.59193 | 0.024584 | 99 | 0.78942 | 0.36116 |
| 46 | 0.60353 | 0.031268 | 100 | 0.77573 | 0.34353 |
| 47 | 0.61514 | 0.038571 | 101 | 0.76205 | 0.32665 |
| 48 | 0.62674 | 0.046529 | 102 | 0.74836 | 0.31053 |
| 49 | 0.63834 | 0.055183 | 103 | 0.73468 | 0.29513 |
| 50 | 0.64995 | 0.064584 | 104 | 0.72099 | 0.28046 |


|  | 105 | 0.70731 | 0.26652 | 159 | 0.20126 | 0.18689 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | 106 | 0.69362 | 0.25330 | 160 | 0.19983 | 0.18645 |
|  | 107 | 0.67994 | 0.24079 | 161 | 0.19840 | 0.18594 |
|  | 108 | 0.66625 | 0.22899 | 162 | 0.19697 | 0.18535 |
| - | 109 | 0.65257 | 0.21790 | 163 | 0.19554 | 0.18466 |
|  | 110 | 0.63888 | 0.20751 | 164 | 0.19411 | 0.18387 |
|  | 111 | 0.62520 | 0.19783 | 165 | 0.19268 | 0.18297 |
|  | 112 | 0.61151 | 0.18884 | 166 | 0.19124 | 0.18194 |
| - | 113 | 0.59783 | 0.18053 | 167 | 0.18981 | 0.18077 |
|  | 114 | 0.58414 | 0.17291 | 168 | 0.18838 | 0.17943 |
|  | 115 | 0.57046 | 0.16596 | 169 | 0.18695 | 0.17787 |
| - | 116 | 0.55677 | 0.15967 | 170 | 0.18552 | 0.17605 |
|  | 117 | 0.54309 | 0.15404 | 171 | 0.18409 | 0.17386 |
|  | 118 | 0.52940 | 0.14905 | 172 | 0.18265 | 0.17113 |
| - | 119 | 0.51572 | 0.14468 | 173 | 0.18122 | 0.16736 |
|  | 120 | 0.50204 | 0.14094 |  |  |  |
|  | 121 | 0.48835 | 0.13781 |  |  |  |
|  | 122 | 0.47467 | 0.13527 |  |  |  |
| $\checkmark$ | 123 | 0.46098 | 0.13331 |  |  |  |
|  | 124 | 0.44730 | 0.13193 |  |  |  |
|  | 125 | 0.43361 | 0.13111 |  |  |  |
| $\cdots$ | 126 | 0.41993 | 0.13085 |  |  |  |
|  | 127 | 0.40624 | 0.13113 |  |  |  |
|  | 128 | 0.39256 | 0.13194 |  |  |  |
| - | 129 | 0.37887 | 0.13328 |  |  |  |
|  | 130 | 0.36519 | 0.13515 |  |  |  |
|  | 131 | 0.35151 | 0.13754 |  |  |  |
|  | 132 | 0.33782 | 0.14044 |  |  |  |
| - | 133 | 0.32414 | 0.14387 |  |  |  |
|  | 134 | 0.31045 | 0.14782 |  |  |  |
|  | 135 | 0.29677 | 0.15230 |  |  |  |
| - | 136 | 0.28309 | 0.15731 |  |  |  |
|  | 137 | 0.26941 | 0.16288 |  |  |  |
|  | 138 | 0.25572 | 0.16900 |  |  |  |
| - | 139 | 0.24204 | 0.17572 |  |  |  |
|  | 140 | 0.22836 | 0.18304 |  |  |  |
|  | 141 | 0.22703 | 0.18375 |  |  |  |
|  | 142 | 0.22559 | 0.18445 |  |  |  |
| - | 143 | 0.22416 | 0.18507 |  |  |  |
|  | 144 | 0.22273 | 0.18564 |  |  |  |
|  | 145 | 0.22130 | 0.18614 |  |  |  |
| - | 146 | 0.21987 | 0.18658 |  |  |  |
|  | 147 | 0.21844 | 0.18696 |  |  |  |
|  | 148 | 0.21701 | 0.18728 |  |  |  |
| $\leftarrow$ | 149 | 0.21558 | 0.18754 |  |  |  |
|  | 150 | 0.21415 | 0.18775 |  |  |  |
|  | 151 | 0.21271 | 0.18790 |  |  |  |
|  | 152 | 0.21128 | 0.18799 |  |  |  |
| $\because$ | 153 | 0.20985 | 0.18802 |  |  |  |
|  | 154 | 0.20842 | 0.18799 |  |  |  |
|  | 155 | 0.20699 | 0.18790 |  |  |  |
| - | 156 | 0.20556 | 0.18775 |  |  |  |
|  | 157 | 0.20413 | 0.18753 |  |  |  |
|  | 158 | 0.20270 | 0.18724 |  |  |  |


| First rotor, tip |  | y [in] | 51 | 0.66861 | 0.067602 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 52 | 0.67892 | 0.079595 |
| 1 | x [in] |  | 53 | 0.68922 | 0.092741 |
|  |  |  | 54 | 0.69953 | 0.10724 |
|  | 0.23860 |  | 0.086311 | 55 | 0.70983 | 0.12330 |
| 2 | 0.23945 | 0.078986 | 56 | 0.72014 | 0.14063 |
| 3 | 0.24030 | 0.076022 | 57 | 0.73044 | 0.15898 |
| 4 | 0.24115 | 0.073796 | 58 | 0.74075 | 0.17816 |
| 5 | 0.24200 | 0.071961 | 59 | 0.75098 | 0.19790 |
| 6 | 0.24285 | 0.070380 | 60 | 0.75858 | 0.21295 |
| 7 | 0.24370 | 0.068984 | 61 | 0.76618 | 0.22830 |
| 8 | 0.24455 | 0.067731 | 62 | 0.77378 | 0.24392 |
| 9 | 0.24540 | 0.066594 | 63 | 0.78138 | 0.25979 |
| 10 | 0.24609 | 0.065741 | 64 | 0.78898 | 0.27588 |
| 11 | 0.25639 | 0.054062 | 65 | 0.79658 | 0.29217 |
| 12 | 0.26670 | 0.043481 | 66 | 0.80418 | 0.30866 |
| 13 | 0.27700 | 0.033867 | 67 | 0.81178 | 0.32532 |
| 14 | 0.28731 | 0.025118 | 68 | 0.81938 | 0.34215 |
| 15 | 0.29762 | 0.017155 | 69 | 0.82698 | 0.35913 |
| 16 | 0.30792 | 0.0099103 | 70 | 0.83458 | 0.37626 |
| 17 | 0.31823 | 0.0033318 | 71 | 0.84218 | 0.39353 |
| 18 | 0.32853 | -0.0026254 | 72 | 0.84978 | 0.41092 |
| 19 | 0.33884 | -0.0079985 | 73 | 0.85738 | 0.42844 |
| 20 | 0.34914 | -0.012819 | 74 | 0.86498 | 0.44607 |
| 21 | 0.35945 | -0.017113 | 75 | 0.87258 | 0.46381 |
| 22 | 0.36975 | -0.020902 | 76 | 0.88018 | 0.48165 |
| 23 | 0.38006 | -0.024207 | 77 | 0.88778 | 0.49959 |
| 24 | 0.39036 | -0.027043 | 78 | 0.89530 | 0.51744 |
| 25 | 0.40067 | -0.029424 | 79 | 0.89564 | 0.51837 |
| 26 | 0.41098 | -0.031360 | 80 | 0.89588 | 0.51933 |
| 27 | 0.42128 | -0.032861 | 81 | 0.89603 | 0.52032 |
| 28 | 0.43159 | -0.033935 | 82 | 0.89608 | 0.52131 |
| 29 | 0.44189 | -0.034587 | 83 | 0.89565 | 0.52421 |
| 30 | 0.45220 | -0.034822 | 84 | 0.89440 | 0.52685 |
| 31 | 0.46250 | -0.034641 | 85 | 0.89244 | 0.52903 |
| 32 | 0.47281 | -0.034047 | 86 | 0.88993 | 0.53054 |
| 33 | 0.48311 | -0.033039 | 87 | 0.88708 | 0.53126 |
| 34 | 0.49342 | -0.031615 | 88 | 0.88413 | 0.53112 |
| 35 | 0.50372 | -0.029772 | 89 | 0.88133 | 0.53011 |
| 36 | 0.51403 | -0.027506 | 90 | 0.87892 | 0.52829 |
| 37 | 0.52434 | -0.024810 | 91 | 0.87709 | 0.52569 |
| 38 | 0.53464 | -0.021675 | 92 | 0.86506 | 0.50124 |
| 39 | 0.54495 | -0.018093 | 93 | 0.85295 | 0.47709 |
| 40 | 0.55525 | -0.014051 | 94 | 0.84083 | 0.45343 |
| 41 | 0.56556 | -0.0095350 | 95 | 0.82872 | 0.43028 |
| 42 | 0.57586 | -0.0045274 | 96 | 0.81661 | 0.40767 |
| 43 | 0.58617 | 0.00099160 | 97 | 0.80449 | 0.38564 |
| 44 | 0.59647 | 0.0070458 | 98 | 0.79238 | 0.36419 |
| 45 | 0.60678 | 0.013663 | 99 | 0.78027 | 0.34338 |
| 46 | 0.61708 | 0.020877 | 100 | 0.76815 | 0.32321 |
| 47 | 0.62739 | 0.028727 | 101 | 0.75604 | 0.30373 |
| 48 | 0.63770 | 0.037260 | 102 | 0.74393 | 0.28494 |
| 49 | 0.64800 | 0.046534 | 103 | 0.73181 | 0.26689 |
| 50 | 0.65831 | 0.056619 | 104 | 0.71970 | 0.24960 |


|  | 105 | 0.70759 | 0.23308 | 140 | 0.28362 | 0.11554 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | 106 | 0.69547 | 0.21736 | 141 | 0.28238 | 0.11607 |
|  | 107 | 0.68336 | 0.20245 | 142 | 0.28105 | 0.11656 |
|  | 108 | 0.67125 | 0.18837 | 143 | 0.27972 | 0.11698 |
|  | 109 | 0.65913 | 0.17513 | 144 | 0.27840 | 0.11735 |
| $\sim$ | 110 | 0.64702 | 0.16274 | 145 | 0.27707 | 0.11765 |
|  | 111 | 0.63490 | 0.15119 | 146 | 0.27574 | 0.11789 |
|  | 112 | 0.62279 | 0.14051 | 147 | 0.27442 | 0.11808 |
| $\because$ | 113 | 0.61068 | 0.13067 | 148 | 0.27309 | 0.11821 |
|  | 114 | 0.59856 | 0.12168 | 149 | 0.27176 | 0.11829 |
|  | 115 | 0.58645 | 0.11352 | 150 | 0.27044 | 0.11831 |
|  | 116 | 0.57434 | 0.10618 | 151 | 0.26911 | 0.11828 |
|  | 117 | 0.56222 | 0.099647 | 152 | 0.26778 | 0.11819 |
|  | 118 | 0.55011 | 0.093900 | 153 | 0.26646 | 0.11804 |
| $=$ | 119 | 0.53800 | 0.088917 | 154 | 0.26513 | 0.11784 |
|  | 120 | 0.52588 | 0.084676 | 155 | 0.26381 | 0.11758 |
|  | 121 | 0.51377 | 0.081152 | 156 | 0.26248 | 0.11726 |
|  | 122 | 0.50166 | 0.078319 | 157 | 0.26115 | 0.11688 |
| - | 123 | 0.48954 | 0.076149 | 158 | 0.25983 | 0.11644 |
|  | 124 | 0.47743 | 0.074617 | 159 | 0.25850 | 0.11593 |
|  | 125 | 0.46532 | 0.073693 | 160 | 0.25717 | 0.11536 |
| - | 126 | 0.45320 | 0.073351 | 161 | 0.25585 | 0.11471 |
|  | 127 | 0.44109 | 0.073563 | 162 | 0.25452 | 0.11398 |
|  | 128 | 0.42898 | 0.074301 | 163 | 0.25319 | 0.11316 |
|  | 129 | 0.41686 | 0.075540 | 164 | 0.25187 | 0.11225 |
| - | 130 | 0.40475 | 0.077254 | 165 | 0.25054 | 0.11124 |
|  | 131 | 0.39264 | 0.079418 | 166 | 0.24921 | 0.11011 |
|  | 132 | 0.38052 | 0.082008 | 167 | 0.24789 | 0.10885 |
| - | 133 | 0.36841 | 0.085002 | 168 | 0.24656 | 0.10743 |
|  | 134 | 0.35630 | 0.088377 | 169 | 0.24523 | 0.10582 |
|  | 135 | 0.34418 | 0.092112 | 170 | 0.24391 | 0.10396 |
|  | 136 | 0.33207 | 0.096189 | 171 | 0.24258 | 0.10177 |
|  | 137 | 0.31996 | 0.10059 | 172 | 0.24125 | 0.099068 |
|  | 138 | 0.30784 | 0.10529 | 173 | 0.23993 | 0.095429 |
|  | 139 | 0.29573 | 0.11028 |  |  |  |



Figure A.1.2--First rotor: tip, midspan, hub.

| A.1.3 Second Nozzle Coordinates |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Second Nozz | Coordnat | 49 | 0.48530 | 0.61780 |
| Second nozzle, hub |  |  | 50 | 0.50310 | 0.60810 |
|  |  |  | 51 | 0.52100 | 0.59770 |
| x [in] |  | $y[i n]$ | 52 | 0.53890 | 0.58670 |
|  |  | 53 | 0.55680 | 0.57510 |
| 1 | 0.067200 |  | 0.71990 | 54 | 0.57470 | 0.56290 |
| 2 | 0.067500 | 0.71690 | 55 | 0.59260 | 0.55000 |
| 3 | 0.068000 | 0.71390 | 56 | 0.61050 | 0.53650 |
| 4 | 0.068700 | 0.71100 | 57 | 0.62840 | 0.52230 |
| 5 | 0.069500 | 0.70800 | 58 | 0.64630 | 0.50740 |
| 6 | 0.070600 | 0.70520 | 59 | 0.66410 | 0.49180 |
| 7 | 0.071800 | 0.70240 | 60 | 0.68200 | 0.47560 |
| 8 | 0.073100 | 0.69970 | 61 | 0.69990 | 0.45860 |
| 9 | 0.074700 | 0.69710 | 62 | 0.71780 | 0.44080 |
| 10 | 0.076400 | 0.69460 | 63 | 0.73570 | 0.42220 |
| 11 | 0.078300 | 0.69220 | 64 | 0.75360 | 0.40290 |
| 12 | 0.080300 | 0.68990 | 65 | 0.77150 | 0.38260 |
| 13 | 0.082400 | 0.68780 | 66 | 0.78940 | 0.36150 |
| 14 | 0.084700 | 0.68580 | 67 | 0.80730 | 0.33940 |
| 15 | 0.087100 | 0.68390 | 68 | 0.82510 | 0.31630 |
| 16 | 0.089600 | 0.68220 | 69 | 0.84300 | 0.29210 |
| 17 | 0.092200 | 0.68070 | 70 | 0.86090 | 0.26680 |
| 18 | 0.094900 | 0.67930 | 71 | 0.87880 | 0.24020 |
| 19 | 0.097700 | 0.67810 | 72 | 0.89670 | 0.21230 |
| 20 | 0.10060 | 0.67710 | 73 | 0.91460 | 0.18290 |
| 21 | 0.10350 | 0.67630 | 74 | 0.93250 | 0.15180 |
| 22 | 0.10650 | 0.67560 | 75 | 0.95040 | 0.11890 |
| 23 | 0.10950 | 0.67520 | 76 | 0.96830 | 0.083800 |
| 24 | 0.11250 | 0.67490 | 77 | 0.98610 | 0.046300 |
| 25 | 0.11550 | 0.67480 | 78 | 1.0039 | 0.0060000 |
| 26 | 0.11850 | 0.67490 | 79 | 1.0046 | 0.0048000 |
| 27 | 0.12150 | 0.67520 | 80 | 1.0054 | 0.0036000 |
| 28 | 0.12450 | 0.67570 | 81 | 1.0064 | 0.0026000 |
| 29 | 0.12750 | 0.67640 | 82 | 1.0075 | 0.0017000 |
| 30 | 0.14540 | 0.68050 | 83 | 1.0087 | 0.0010000 |
| 31 | 0.16330 | 0.68380 | 84 | 1.0101 | 0.00050000 |
| 32 | 0.18120 | 0.68620 | 85 | 1.0115 | $1.0000 \mathrm{e}-04$ |
| 33 | 0.19900 | 0.68770 | 86 | 1.0129 | 0.0000 |
| 34 | 0.21690 | 0.68850 | 87 | 1.0143 | $1.0000 \mathrm{e}-04$ |
| 35 | 0.23480 | 0.68850 | 88 | 1.0157 | 0.00040000 |
| 36 | 0.25270 | 0.68780 | 89 | 1.0170 | 0.00080000 |
| 37 | 0.27060 | 0.68630 | 90 | 1.0183 | 0.0015000 |
| 38 | 0.28850 | 0.68410 | 91 | 1.0194 | 0.0024000 |
| 39 | 0.30640 | 0.68130 | 92 | 1.0205 | 0.0034000 |
| 40 | 0.32430 | 0.67780 | 93 | 1.0213 | 0.0045000 |
| 41 | 0.34220 | 0.67360 | 94 | 1.0220 | 0.0057000 |
| 42 | 0.36000 | 0.66880 | 95 | 1.0225 | 0.0071000 |
| 43 | 0.37790 | 0.66340 | 96 | 1.0228 | 0.0085000 |
| 44 | 0.39580 | 0.65730 | 97 | 1.0229 | 0.0099000 |
| 45 | 0.41370 | 0.65070 | 98 | 1.0229 | 0.010300 |
| 46 | 0.43160 | 0.64340 | 99 | 1.0229 | 0.010600 |
| 47 | 0.44950 | 0.63550 | 100 | 1.0229 | 0.011000 |
| 48 | 0.46740 | 0.62690 | 101 | 1.0228 | 0.011400 |


| 102 | 1.0227 | 0.011800 | 156 | 0.39660 | 0.91970 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 103 | 1.0227 | 0.012100 | 157 | 0.38200 | 0.92000 |
| 104 | 1.0226 | 0.012500 | 158 | 0.36740 | 0.91970 |
| 105 | 1.0225 | 0.012800 | 159 | 0.35270 | 0.91890 |
| 106 | 1.0223 | 0.013200 | 160 | 0.33810 | 0.91740 |
| 107 | 1.0047 | 0.062800 | 161 | 0.32350 | 0.91540 |
| 108 | 0.98700 | 0.11240 | 162 | 0.30890 | 0.91270 |
| 109 | 0.96930 | 0.16200 | 163 | 0.29430 | 0.90930 |
| 110 | 0.95160 | 0.21160 | 164 | 0.27960 | 0.90530 |
| 111 | 0.93400 | 0.26120 | 165 | 0.26500 | 0.90060 |
| 112 | 0.91630 | 0.31070 | 166 | 0.25040 | 0.89520 |
| 113 | 0.89860 | 0.36030 | 167 | 0.23580 | 0.88910 |
| 114 | 0.88090 | 0.40990 | 168 | 0.22110 | 0.88210 |
| 115 | 0.86320 | 0.45950 | 169 | 0.20650 | 0.87430 |
| 116 | 0.85820 | 0.47360 | 170 | 0.19190 | 0.86560 |
| 117 | 0.85300 | 0.48760 | 171 | 0.17730 | 0.85590 |
| 118 | 0.84790 | 0.50150 | 172 | 0.16270 | 0.84520 |
| 119 | 0.84280 | 0.51510 | 173 | 0.14800 | 0.83320 |
| 120 | 0.83760 | 0.52840 | 174 | 0.13340 | 0.82000 |
| 121 | 0.83250 | 0.54140 | 175 | 0.11880 | 0.80520 |
| 122 | 0.82730 | 0.55420 | 176 | 0.10420 | 0.78880 |
| 123 | 0.82220 | 0.56680 | 177 | 0.089600 | 0.77030 |
| 124 | 0.81700 | 0.57900 | 178 | 0.074900 | 0.74920 |
| 125 | 0.81190 | 0.59100 | 179 | 0.073300 | 0.74660 |
| 126 | 0.80670 | 0.60260 | 180 | 0.071900 | 0.74380 |
| 127 | 0.80160 | 0.61400 | 181 | 0.070700 | 0.74100 |
| 128 | 0.79640 | 0.62500 | 182 | 0.069600 | 0.73810 |
| 129 | 0.79130 | 0.63580 | 183 | 0.068700 | 0.73520 |
| 130 | 0.77680 | 0.66370 | 184 | 0.068000 | 0.73220 |
| 131 | 0.76210 | 0.68850 | 185 | 0.067500 | 0.72910 |
| 132 | 0.74750 | 0.71090 | 186 | 0.067200 | 0.72610 |
| 133 | 0.73290 | 0.73110 | 187 | 0.067100 | 0.72300 |
| 134 | 0.71830 | 0.74950 |  |  |  |
| 135 | 0.70360 | 0.76640 |  |  |  |
| 136 | 0.68900 | 0.78200 |  |  |  |
| 137 | 0.67440 | 0.79630 |  |  |  |
| 138 | 0.65980 | 0.80960 |  |  |  |
| 139 | 0.64520 | 0.82190 |  |  |  |
| 140 | 0.63050 | 0.83320 |  |  |  |
| 141 | 0.61590 | 0.84370 |  |  |  |
| 142 | 0.60130 | 0.85340 |  |  |  |
| 143 | 0.58670 | 0.86230 |  |  |  |
| 144 | 0.57210 | 0.87050 |  |  |  |
| 145 | 0.55740 | 0.87800 |  |  |  |
| 146 | 0.54280 | 0.88480 |  |  |  |
| 147 | 0.52820 | 0.89100 |  |  |  |
| 148 | 0.51360 | 0.89660 |  |  |  |
| 149 | 0.49900 | 0.90150 |  |  |  |
| 150 | 0.48430 | 0.90580 |  |  |  |
| 151 | 0.46970 | 0.90960 |  |  |  |
| 152 | 0.45510 | 0.91280 |  |  |  |
| 153 | 0.44050 | 0.91540 |  |  |  |
| 154 | 0.42580 | 0.91740 |  |  |  |
| 155 | 0.41120 | 0.91880 |  |  |  |


| Second nozzle, midspan |  |  | 51 | 0.51540 | 0.65420 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 52 | 0.53520 | 0.64120 |
| x [in] |  | $y[i n]$ | 53 | 0.55490 | 0.62760 |
|  |  | 54 | 0.57470 | 0.61330 |
| 1 | 0.022600 |  | 0.81050 | 55 | 0.59450 | 0.59830 |
| 2 | 0.022900 | 0.80750 | 56 | 0.61420 | 0.58270 |
| 3 | 0.023300 | 0.80450 | 57 | 0.63400 | 0.56640 |
| 4 | 0.024000 | 0.80160 | 58 | 0.65370 | 0.54950 |
| 5 | 0.024800 | 0.79880 | 59 | 0.67350 | 0.53180 |
| 6 | 0.025800 | 0.79600 | 60 | 0.69320 | 0.51340 |
| 7 | 0.026900 | 0.79320 | 61 | 0.71300 | 0.49430 |
| 8 | 0.028300 | 0.79050 | 62 | 0.73270 | 0.47440 |
| 9 | 0.029800 | 0.78800 | 63 | 0.75250 | 0.45370 |
| 10 | 0.031400 | 0.78550 | 64 | 0.77220 | 0.43220 |
| 11 | 0.033200 | 0.78310 | 65 | 0.79200 | 0.40980 |
| 12 | 0.035200 | 0.78090 | 66 | 0.81170 | 0.38650 |
| 13 | 0.037300 | 0.77870 | 67 | 0.83150 | 0.36230 |
| 14 | 0.039500 | 0.77670 | 68 | 0.85120 | 0.33710 |
| 15 | 0.041800 | 0.77490 | 69 | 0.87100 | 0.31080 |
| 16 | 0.044200 | 0.77320 | 70 | 0.89080 | 0.28330 |
| 17 | 0.046800 | 0.77160 | 71 | 0.91050 | 0.25460 |
| 18 | 0.049400 | 0.77020 | 72 | 0.93030 | 0.22460 |
| 19 | 0.052100 | 0.76900 | 73 | 0.95000 | 0.19310 |
| 20 | 0.054800 | 0.76800 | 74 | 0.96980 | 0.15990 |
| 21 | 0.057700 | 0.76710 | 75 | 0.98950 | 0.12490 |
| 22 | 0.060500 | 0.76640 | 76 | 1.0093 | 0.087800 |
| 23 | 0.063400 | 0.76580 | 77 | 1.0290 | 0.048200 |
| 24 | 0.066300 | 0.76550 | 78 | 1.0487 | 0.0059000 |
| 25 | 0.069300 | 0.76530 | 79 | 1.0493 | 0.0046000 |
| 26 | 0.072200 | 0.76530 | 80 | 1.0501 | 0.0035000 |
| 27 | 0.075100 | 0.76550 | 81 | 1.0511 | 0.0025000 |
| 28 | 0.078000 | 0.76590 | 82 | 1.0522 | 0.0017000 |
| 29 | 0.080900 | 0.76640 | 83 | 1.0535 | 0.0010000 |
| 30 | 0.10060 | 0.77000 | 84 | 1.0548 | 0.00040000 |
| 31 | 0.12040 | 0.77260 | 85 | 1.0562 | $1.0000 \mathrm{e}-04$ |
| 32 | 0.14010 | 0.77410 | 86 | 1.0576 | 0.0000 |
| 33 | 0.15990 | 0.77460 | 87 | 1.0590 | $1.0000 \mathrm{e}-04$ |
| 34 | 0.17960 | 0.77420 | 88 | 1.0604 | 0.00040000 |
| 35 | 0.19940 | 0.77300 | 89 | 1.0617 | 0.00090000 |
| 36 | 0.21910 | 0.77090 | 90 | 1.0630 | 0.0015000 |
| 37 | 0.23890 | 0.76800 | 91 | 1.0641 | 0.0024000 |
| 38 | 0.25860 | 0.76430 | 92 | 1.0651 | 0.0034000 |
| 39 | 0.27840 | 0.75990 | 93 | 1.0660 | 0.0045000 |
| 40 | 0.29820 | 0.75480 | 94 | 1.0667 | 0.0057000 |
| 41 | 0.31790 | 0.74900 | 95 | 1.0672 | 0.0071000 |
| 42 | 0.33770 | 0.74240 | 96 | 1.0675 | 0.0085000 |
| 43 | 0.35740 | 0.73520 | 97 | 1.0676 | 0.0099000 |
| 44 | 0.37720 | 0.72730 | 98 | 1.0676 | 0.010300 |
| 45 | 0.39690 | 0.71880 | 99 | 1.0675 | 0.010700 |
| 46 | 0.41670 | 0.70960 | 100 | 1.0675 | 0.011100 |
| 47 | 0.43640 | 0.69980 | 101 | 1.0674 | 0.011500 |
| 48 | 0.45620 | 0.68940 | 102 | 1.0674 | 0.011900 |
| 49 | 0.47590 | 0.67830 | 103 | 1.0673 | 0.012400 |
| 50 | 0.49570 | 0.66660 | 104 | 1.0672 | 0.012800 |


|  | 105 | 1.0670 | 0.013100 | 159 | 0.33530 | 1.0036 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | 106 | 1.0669 | 0.013500 | 160 | 0.31930 | 1.0032 |
|  | 107 | 1.0476 | 0.062100 | 161 | 0.30340 | 1.0021 |
|  | 108 | 1.0282 | 0.11070 | 162 | 0.28740 | 1.0002 |
| - | 109 | 1.0089 | 0.15930 | 163 | 0.27140 | 0.99770 |
|  | 110 | 0.98960 | 0.20780 | 164 | 0.25540 | 0.99440 |
|  | 111 | 0.97030 | 0.25640 | 165 | 0.23950 | 0.99030 |
|  | 112 | 0.95100 | 0.30500 | 166 | 0.22350 | 0.98540 |
| - | 113 | 0.93170 | 0.35350 | 167 | 0.20750 | 0.97970 |
|  | 114 | 0.91240 | 0.40210 | 168 | 0.19150 | 0.97310 |
|  | 115 | 0.89310 | 0.45070 | 169 | 0.17560 | 0.96560 |
| - | 116 | 0.88750 | 0.46450 | 170 | 0.15960 | 0.95710 |
|  | 117 | 0.88190 | 0.47850 | 171 | 0.14360 | 0.94750 |
|  | 118 | 0.87630 | 0.49230 | 172 | 0.12760 | 0.93690 |
| - | 119 | 0.87070 | 0.50610 | 173 | 0.11170 | 0.92500 |
|  | 120 | 0.86510 | 0.51970 | 174 | 0.095700 | 0.91180 |
|  | 121 | 0.85940 | 0.53320 | 175 | 0.079700 | 0.89710 |
|  | 122 | 0.85380 | 0.54660 | 176 | 0.063700 | 0.88070 |
| - | 123 | 0.84820 | 0.55980 | 177 | 0.047800 | 0.86240 |
|  | 124 | 0.84260 | 0.57290 | 178 | 0.031800 | 0.84180 |
|  | 125 | 0.83690 | 0.58570 | 179 | 0.029900 | 0.83900 |
| -- | 126 | 0.83130 | 0.59830 | 180 | 0.028200 | 0.83610 |
|  | 127 | 0.82570 | 0.61070 | 181 | 0.026700 | 0.83310 |
|  | 128 | 0.82010 | 0.62290 | 182 | 0.025400 | 0.82990 |
|  | 129 | 0.81440 | 0.63480 | 183 | 0.024400 | 0.82670 |
|  | 130 | 0.79860 | 0.66660 | 184 | 0.023500 | 0.82350 |
|  | 131 | 0.78260 | 0.69630 | 185 | 0.023000 | 0.82020 |
|  | 132 | 0.76660 | 0.72370 | 186 | 0.022600 | 0.81680 |
| - | 133 | 0.75060 | 0.74880 | 187 | 0.022500 | 0.81350 |
|  | 134 | 0.73470 | 0.77190 |  |  |  |
|  | 135 | 0.71870 | 0.79310 |  |  |  |
| - | 136 | 0.70270 | 0.81280 |  |  |  |
|  | 137 | 0.68670 | 0.83110 |  |  |  |
|  | 138 | 0.67080 | 0.84800 |  |  |  |
|  | 139 | 0.65480 | 0.86380 |  |  |  |
| - | 140 | 0.63880 | 0.87850 |  |  |  |
|  | 141 | 0.62280 | 0.89210 |  |  |  |
|  | 142 | 0.60690 | 0.90480 |  |  |  |
| - | 143 | 0.59090 | 0.91660 |  |  |  |
|  | 144 | 0.57490 | 0.92760 |  |  |  |
|  | 145 | 0.55890 | 0.93770 |  |  |  |
| - | 146 | 0.54300 | 0.94700 |  |  |  |
|  | 147 | 0.52700 | 0.95560 |  |  |  |
|  | 148 | 0.51100 | 0.96340 |  |  |  |
|  | 149 | 0.49510 | 0.97050 |  |  |  |
| - | 150 | 0.47910 | 0.97680 |  |  |  |
|  | 151 | 0.46310 | 0.98250 |  |  |  |
|  | 152 | 0.44710 | 0.98750 |  |  |  |
| - | 153 | 0.43120 | 0.99180 |  |  |  |
|  | 154 | 0.41520 | 0.99540 |  |  |  |
|  | 155 | 0.39920 | 0.99840 |  |  |  |
| - | 156 | 0.38320 | 1.0007 |  |  |  |
|  | 157 | 0.36730 | 1.0023 |  |  |  |
|  | 158 | 0.35130 | 1.0033 |  |  |  |


| Second nozzle, tip |  |  | 51 | 0.50980 | 0.71070 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 52 | 0.53150 | 0.69570 |
| $x$ [in] |  | y [in] | 53 | 0.55310 | 0.68000 |
|  |  | 54 | 0.57470 | 0.66370 |
| 1 | -0.022100 |  | 0.90100 | 55 | 0.59630 | 0.64660 |
| 2 | -0.021800 | 0.89810 | 56 | 0.61790 | 0.62900 |
| 3 | -0.021400 | 0.89520 | 57 | 0.63950 | 0.61060 |
| 4 | -0.020800 | 0.89230 | 58 | 0.66120 | 0.59150 |
| 5 | -0.020000 | 0.88950 | 59 | 0.68280 | 0.57170 |
| 6 | -0.019000 | 0.88670 | 60 | 0.70440 | 0.55120 |
| 7 | -0.017900 | 0.88400 | 61 | 0.72600 | 0.53000 |
| 8 | -0.016600 | 0.88140 | 62 | 0.74760 | 0.50790 |
| 9 | -0.015100 | 0.87880 | 63 | 0.76930 | 0.48510 |
| 10 | -0.013500 | 0.87640 | 64 | 0.79090 | 0.46150 |
| 11 | -0.011800 | 0.87400 | 65 | 0.81250 | 0.43700 |
| 12 | -0.0099000 | 0.87180 | 66 | 0.83410 | 0.41150 |
| 13 | -0.0079000 | 0.86970 | 67 | 0.85570 | 0.38250 |
| 14 | -0.0058000 | 0.86770 | 68 | 0.87730 | 0.35780 |
| 15 | -0.0035000 | 0.86580 | 69 | 0.89900 | 0.32940 |
| 16 | -0.0012000 | 0.86410 | 70 | 0.92060 | 0.29980 |
| 17 | 0.0013000 | 0.86260 | 71 | 0.94220 | 0.26900 |
| 18 | 0.0038000 | 0.86120 | 72 | 0.96380 | 0.23680 |
| 19 | 0.0064000 | 0.85990 | 73 | 0.98540 | 0.20320 |
| 20 | 0.0091000 | 0.85880 | 74 | 1.0071 | 0.16800 |
| 21 | 0.011800 | 0.85790 | 75 | 1.0287 | 0.13090 |
| 22 | 0.014600 | 0.85710 | 76 | 1.0503 | 0.091700 |
| 23 | 0.017400 | 0.85650 | 77 | 1.0719 | 0.050000 |
| 24 | 0.020200 | 0.85610 | 78 | 1.0934 | 0.0057000 |
| 25 | 0.023000 | 0.85580 | 79 | 1.0941 | 0.0045000 |
| 26 | 0.025900 | 0.85570 | 80 | 1.0949 | 0.0034000 |
| 27 | 0.028700 | 0.85580 | 81 | 1.0958 | 0.0025000 |
| 28 | 0.031500 | 0.85600 | 82 | 1.0970 | 0.0016000 |
| 29 | 0.034200 | 0.85640 | 83 | 1.0982 | 0.00090000 |
| 30 | 0.055900 | 0.85950 | 84 | 1.0995 | 0.00040000 |
| 31 | 0.077500 | 0.86130 | 85 | 1.1009 | $1.0000 \mathrm{e}-04$ |
| 32 | 0.099100 | 0.86190 | 86 | 1.1023 | 0.0000 |
| 33 | 0.12070 | 0.86140 | 87 | 1.1037 | 1.0000e-04 |
| 34 | 0.14230 | 0.85990 | 88 | 1.1051 | 0.00040000 |
| 35 | 0.16390 | 0.85740 | 89 | 1.1064 | 0.00090000 |
| 36 | 0.18560 | 0.85400 | 90 | 1.1077 | 0.0015000 |
| 37 | 0.20720 | 0.84970 | 91 | 1.1088 | 0.0024000 |
| 38 | 0.22880 | 0.84450 | 92 | 1.1098 | 0.0034000 |
| 39 | 0.25040 | 0.83850 | 93 | 1.1107 | 0.0045000 |
| 40 | 0.27200 | 0.83180 | 94 | 1.1113 | 0.0058000 |
| 41 | 0.29370 | 0.82430 | 95 | 1.1118 | 0.0071000 |
| 42 | 0.31530 | 0.81600 | 96 | 1.1121 | 0.0085000 |
| 43 | 0.33690 | 0.80700 | 97 | 1.1122 | 0.0099000 |
| 44 | 0.35850 | 0.79740 | 98 | 1.1122 | 0.010300 |
| 45 | 0.38010 | 0.78700 | 99 | 1.1122 | 0.010800 |
| 46 | 0.40170 | 0.77590 | 100 | 1.1122 | 0.011200 |
| 47 | 0.42340 | 0.76420 | 101 | 1.1121 | 0.011700 |
| 48 | 0.44500 | 0.75180 | 102 | 1.1120 | 0.012100 |
| 49 | 0.46660 | 0.73880 | 103 | 1.1119 | 0.012600 |
| 50 | 0.48820 | 0.72510 | 104 | 1.1117 | 0.013000 |


| - | 105 | 1.1116 | 0.013400 | 147 | 0.52580 | 1.0201 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 106 | 1.1114 | 0.013900 | 148 | 0.50850 | 1.0302 |
|  | 107 | 1.0905 | 0.061400 | 149 | 0.49120 | 1.0394 |
| - | 108 | 1.0695 | 0.10900 | 150 | 0.47380 | 1.0478 |
|  | 109 | 1.0486 | 0.15650 | 151 | 0.45650 | 1.0554 |
|  | 110 | 1.0276 | 0.20410 | 152 | 0.43920 | 1.0622 |
|  | 111 | 1.0067 | 0.25170 | 153 | 0.42180 | 1.0682 |
| - | 112 | 0.98570 | 0.29920 | 154 | 0.40450 | 1.0735 |
|  | 113 | 0.96480 | 0.34680 | 155 | 0.38720 | 1.0780 |
|  | 114 | 0.94380 | 0.39430 | 156 | 0.36990 | 1.0817 |
| - | 115 | 0.92290 | 0.44190 | 157 | 0.35250 | 1.0847 |
|  | 116 | 0.91690 | 0.45550 | 158 | 0.33520 | 1.0869 |
|  | 117 | 0.91080 | 0.46940 | 159 | 0.31790 | 1.0883 |
| - | 118 | 0.90470 | 0.48320 | 160 | 0.30060 | 1.0889 |
|  | 119 | 0.89860 | 0.49720 | 161 | 0.28320 | 1.0888 |
|  | 120 | 0.89250 | 0.51110 | 162 | 0.26590 | 1.0878 |
| - | 121 | 0.88640 | 0.52500 | 163 | 0.24860 | 1.0860 |
|  | 122 | 0.88030 | 0.53900 | 164 | 0.23120 | 1.0834 |
|  | 123 | 0.87420 | 0.55300 | 165 | 0.21390 | 1.0799 |
|  | 124 | 0.86810 | 0.56690 | 166 | 0.19660 | 1.0756 |
| - | 125 | 0.86200 | 0.58060 | 167 | 0.17930 | 1.0703 |
|  | 126 | 0.85590 | 0.59420 | 168 | 0.16190 | 1.0641 |
|  | 127 | 0.84980 | 0.60760 | 169 | 0.14460 | 1.0568 |
| - | 128 | 0.84370 | 0.62080 | 170 | 0.12730 | 1.0486 |
|  | 129 | 0.83760 | 0.63380 | 171 | 0.11000 | 1.0392 |
|  | 130 | 0.82040 | 0.66970 | 172 | 0.092600 | 1.0286 |
|  | 131 | 0.80300 | 0.70410 | 173 | 0.075300 | 1.0168 |
| - | 132 | 0.78570 | 0.73660 | 174 | 0.058000 | 1.0036 |
|  | 133 | 0.76840 | 0.76660 | 175 | 0.040600 | 0.98890 |
|  | 134 | 0.75110 | 0.79430 | 176 | 0.023300 | 0.97260 |
| - | 135 | 0.73370 | 0.81990 | 177 | 0.0060000 | 0.95450 |
|  | 136 | 0.71640 | 0.84370 | 178 | -0.011300 | 0.93440 |
|  | 137 | 0.69910 | 0.86580 | 179 | -0.013600 | 0.93150 |
| - | 138 | 0.68170 | 0.88650 | 180 | -0.015500 | 0.92830 |
|  | 139 | 0.66440 | 0.90570 | 181 | -0.017300 | 0.92510 |
|  | 140 | 0.64710 | 0.92380 | 182 | -0.018800 | 0.92180 |
| - | 141 | 0.62980 | 0.94060 | 183 | -0.020000 | 0.91830 |
|  | 142 | 0.61240 | 0.95630 | 184 | -0.020900 | 0.91480 |
|  | 143 | 0.59510 | 0.97100 | 185 | -0.021600 | 0.91120 |
|  | 144 | 0.57780 | 0.98470 | 186 | -0.022000 | 0.90760 |
| - | 145 | 0.56050 | 0.99740 | 187 | -0.022200 | 0.90390 |
|  | 146 | 0.54310 | 1.0092 |  |  |  |



Figure A.1.3--Second nozzle, tip, midspan, hub.

## A. 2 Listing of Instrumentation Locations

| Position No. | Location | VE/E | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| 44 | Pressure, $90 \%, \mathbf{S}_{\mathrm{T}}=1.426$ | 0.091 | 6.38 |
| 45 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.426$ | 0.173 | 12.13 |
| 46 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.426$ | 0.543 | 38.08 |
| 47 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.426$ | 0.872 | 61.15 |
| 48 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.426$ | 1.096 | 76.86 |
|  |  |  | 0 |
| 80 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0 | 0 |
| 81 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.0385 | 2.78 |
| 49 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.070 | 5.05 |
| 82 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.123 | 8.87 |
| 50 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.125 | 9.02 |
| 83 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.173 | 12.48 |
| 84 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.244 | 17.61 |
| 85 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.3235 | 23.34 |
| 51 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.477 | 34.42 |
| 52 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 0.821 | 59.24 |
| 53 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 1.048 | 75.61 |
| 54 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.386$ | 1.119 | 85.86 |
|  |  |  |  |
| 55 | Pressure, $23 \%, \mathrm{~S}_{\mathrm{T}}=1.374$ | 1.244 | 90.54 |
|  |  |  |  |
| 56 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.282$ | 0.084 | 6.55 |
| 57 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.282$ | 0.164 | 12.79 |
| 58 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.282$ | 0.496 | 38.69 |
| 59 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.282$ | 0.802 | 62.56 |
| 60 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.282$ | 1.047 | 81.67 |
| 61 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.282$ | 1.169 | 91.19 |

Table A.2.1--Heat flux instrumentation, first stage nozzle guide vane, pressure side.

| Position No. | Location | $\Sigma \mathrm{E} / \mathrm{E}$ | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| 62 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.726$ | 0.095 | 5.50 |
| 63 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.726$ | 0.376 | 21.78 |
| 64 | Suction, $90 \%$, $\mathrm{S}_{\mathrm{T}}=1.726$ | 0.809 | 46.87 |
| 65 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.726$ | 1.127 | 65.30 |
| 66 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.726$ | 1.435 | 83.20 |
|  |  |  |  |
| 80 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.000 | 0 |
| 86 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.0585 | 3.43 |
| 67 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.060 | 3.52 |
| 87 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.1385 | 8.12 |
| 88 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.215 | 12.60 |
| 89 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.285 | 16.71 |
| 90 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.363 | 21.28 |
| 68 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.381 | 22.33 |
| 69 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.603 | 35.35 |
| 70 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 0.857 | 50.23 |
| 71 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 1.090 | 63.89 |
| 72 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.706$ | 1.385 | 81.18 |
|  |  |  |  |
| 73 | Suction, $31 \%, \mathrm{~S}_{\mathrm{T}}=1.685$ | 1.579 | 93.71 |
|  |  |  |  |
| 74 | Suction, 19\%, $\mathrm{S}_{\mathrm{T}}=1.609$ | 1.489 | 92.54 |
| 75 | Suction, 10\%, $\mathrm{S}_{\text {T }}=1.580$ | 0.085 | 5.38 |
| 76 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.580$ | 0.367 | 23.23 |
| 77 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.580$ | 0.567 | 35.87 |
| 78 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.580$ | 1.177 | 74.49 |
| 79 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.580$ | 1.357 | 85.89 |

Table A.2.2--Heat flux instrumenatation, first stage nozzle guide vane, suction side.

| Position No. | Location | VE/E | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| 33 | Tip, $\mathrm{S}_{\mathrm{T}}=0.985$ | 0.1665 | 16.9 |
| 34 | Tip, $\mathrm{S}_{\mathrm{T}}=0.985$ | 0.379 | 38.48 |
| 35 | Tip, $\mathrm{S}_{\mathrm{T}}=0.985$ | 0.563 | 57.16 |
| 36 | Tip, $\mathrm{S}_{\mathrm{T}}=0.985$ | 0.702 | 71.27 |
|  |  |  |  |
| 12 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.101$ | 0.075 | 6.81 |
| 13 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.101$ | 0.509 | 46.23 |
| 37 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.101$ | 0.632 | 57.40 |
| 38 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.101$ | 0.767 | 69.66 |
| 14 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.101$ | 0.900 | 81.74 |
| 39 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.101$ | 0.991 | 90.01 |
|  |  |  |  |
| 1 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=0.898$ | 0.043 | 4.79 |
| 2 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=0.898$ | 0.406 | 45.21 |
| 3 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=0.898$ | 0.561 | 62.47 |
|  |  |  |  |
| 20 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.232$ | 0.090 | 7.31 |
| 21 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.232$ | 0.198 | 16.07 |
| 22 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.232$ | 0.636 | 51.62 |
| 23 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.232$ | 0.988 | 80.19 |
|  |  |  |  |
| 9 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=0.955$ | 0.052 | 5.45 |
| 10 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=0.955$ | 0.464 | 48.59 |
| 11 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=0.955$ | 0.622 | 65.13 |

Table A.2.3a--Heat flux instrumentation, first stage rotor.

| Position No. | Location | $\Sigma \mathrm{E} / \mathrm{E}$ | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| 24 | Platform | 0.222 | 22.05 |
| 25 | Platform | 0.595 | 59.09 |
|  |  |  |  |
| 26 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0 | 0 |
| 30 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.067 | 5.79 |
| 31 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.137 | 11.83 |
| 32 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.205 | 17.71 |
| 15 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.330 | 28.51 |
| 16 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.560 | 48.38 |
| 17 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.742 | 64.10 |
| 18 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 0.949 | 81.99 |
| 19 | Suction $50 \%, \mathrm{~S}_{\mathrm{T}}=1.158$ | 1.074 | 92.79 |
|  |  |  |  |
| 27 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.080 | 8.71 |
| 28 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.148 | 16.10 |
| 29 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.201 | 21.87 |
| 4 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.217 | 23.61 |
| 5 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.409 | 44.50 |
| 6 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.556 | 60.50 |
| 7 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.669 | 72.80 |
| 8 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.919$ | 0.806 | 87.70 |

Table A.2.3b--Heat flux instrumentation, first stage rotor (cont'd).

| Position No. | Location | $\sum \mathrm{E} / \mathrm{E}$ | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| 91 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 0.016 | 1.15 |
| 92 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 0.101 | 7.26 |
| 93 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 0.168 | 12.07 |
| 94 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 0.514 | 36.93 |
| 95 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 0.707 | 50.79 |
| 96 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 0.855 | 61.42 |
| 97 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.392$ | 1.071 | 76.94 |
|  |  |  |  |
| 98 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 0.00 | 0 |
| 99 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 0.137 | 7.92 |
| 100 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 0.375 | 21.69 |
| 101 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 0.545 | 31.52 |
| 102 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 0.893 | 51.65 |
| 103 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 0.975 | 56.39 |
| 104 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 1.155 | 66.80 |
| 105 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 1.302 | 75.30 |
| 106 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 1.369 | 79.18 |
| 107 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.729$ | 1.546 | 89.42 |

Table A.2.3c--Heat flux instrumentation, first stage rotor (cont'd).

| Position No. | Location | $\Sigma \mathrm{E} / \mathrm{E}$ | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| P1 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=0.891$ | 0.044 | 4.94 |
| P2 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=0.891$ | 0.403 | 45.23 |
| P3 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=0.891$ | 0.563 | 63.19 |
|  |  |  |  |
| P4 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.125$ | 0.068 | 6.00 |
| P5 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.125$ | 0.187 | 16.62 |
| P6 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.125$ | 0.875 | 77.78 |
|  |  |  |  |
| P7 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.921$ | 0.040 | 4.34 |
| P8 | Pressure, 50\%, $\mathrm{S}_{\mathrm{T}}=0.921$ | 0.125 | 13.57 |
| P9 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.921$ | 0.402 | 43.65 |
| P10 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=0.921$ | 0.670 | 72.75 |
|  |  |  |  |
| P11 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.065 | 5.54 |
| P12 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.141 | 12.06 |
| P13 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.214 | 18.37 |
| P14 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.296 | 25.41 |
| P15 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.534 | 45.84 |
| P16 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.702 | 60.26 |
| P17 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.165$ | 0.925 | 79.40 |
|  |  |  |  |

Table A.2.4a--Pressure Instrumentation, first stage rotor.

| P18 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=0.948$ | 0.047 | 4.96 |
| :---: | :--- | :---: | :---: |
| P19 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=0.948$ | 0.445 | 46.94 |
| P20 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=0.948$ | 0.593 | 62.55 |
|  |  |  |  |
| P21 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.215$ | 0.083 | 6.83 |
| P22 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.215$ | 0.231 | 19.01 |
| P23 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.215$ | 0.594 | 48.89 |
| P24 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.215$ | 0.896 | 73.74 |

Table A.2.4b--Pressure Instrumentation, first stage rotor (cont'd).

| Position No. | Location | $\sum \mathrm{E} / \mathrm{E}$ | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| P25 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.433$ | 0.068 | 4.75 |
| P26 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.433$ | 0.528 | 36.85 |
| P30 | Pressure, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.433$ | 1.064 | 74.25 |
|  |  |  |  |
| P33 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.425$ | 0.108 | 7.58 |
| P34 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.425$ | 0.218 | 15.30 |
| P35 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.425$ | 0.518 | 36.35 |
| P36 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.425$ | 0.860 | 60.35 |
| P37 | Pressure, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.425$ | 1.031 | 72.35 |
|  |  |  |  |
| P45 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.241$ | 0.061 | 4.92 |
| P46 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.241$ | 0.480 | 38.68 |
| P47 | Pressure, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.241$ | 1.023 | 82.43 |

Table A.2.5a--Pressure Instrumentation, first stage vane.

| Position No. | Location | $\Sigma \mathrm{E} / \mathrm{E}$ | \% Wetted Distance |
| :---: | :---: | :---: | :---: |
| P28 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.662$ | 0.100 | 6.02 |
| P29 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.662$ | 0.367 | 22.08 |
| P30 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.662$ | 0.775 | 46.63 |
| P31 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.662$ | 1.088 | 65.46 |
| P32 | Suction, $90 \%, \mathrm{~S}_{\mathrm{T}}=1.662$ | 1.359 | 81.77 |
|  |  |  |  |
| P38 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.728$ | 0.114 | 6.60 |
| P39 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.728$ | 0.252 | 14.58 |
| P40 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.728$ | 0.400 | 23.15 |
| P41 | Suction, 50\%, $\mathbf{S}_{\text {T }}=1.728$ | 0.592 | 34.26 |
| P42 | Suction, 50\%, $\mathbf{S}_{\mathbf{T}}=1.728$ | 0.847 | 49.02 |
| P43 | Suction, 50\%, $\mathrm{S}_{\mathrm{T}}=1.728$ | 1.108 | 64.12 |
| P44 | Suction, $50 \%, \mathrm{~S}_{\mathrm{T}}=1.728$ | 1.491 | 86.28 |
|  |  |  |  |
| P48 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.568$ | 0.091 | 5.80 |
| P49 | Suction, 10\%, $\mathrm{S}_{\mathrm{T}}=1.568$ | 0.354 | 22.58 |
| P50 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.568$ | 0.563 | 35.91 |
| P51 | Suction, 10\%, $\mathrm{S}_{\mathrm{T}}=1.568$ | 1.148 | 73.21 |
| P52 | Suction, $10 \%, \mathrm{~S}_{\mathrm{T}}=1.568$ | 1.333 | 85.01 |

Table A.2.5b--Pressure Instrumentation, first stage vane (cont'd).

| Position No. | Location |
| :---: | :--- |
| P53 | Hub wall, near midpassage, 0.062 aft of leading edge |
| P54 | Hub wall, 0.145 from suction surface, 0.062 aft of leading edge |
| P55 | Hub wall, 0.604 from leading edge, near pressure surface of vane <br> $\# 1$ |
| P56 | Hub wall, 0.575 from leading edge, near pressure surface of vane <br> $\# 7$ |
| P57 | Hub wall, 0.086 from trailing edge, near pressure surface of vane <br> $\# 7$ (in region where vane trailing edge has been removed |

Table A. 2.5 c --Pressure Instrumentation, first stage vane (cont'd).

## A. 3 Listing of Data: Pressure and Stanton numbers

| \% wetted <br> distance | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -82.4 | 0.88276 | 0.86732 | 0.90313 | 0.91504 | 0.90972 | 0.82652 | 0.79142 |
| -38.7 | 1.0000 | 1.0000 | 0.94244 | 0.96289 | 1.0049 | 1.0000 | 1.0000 |
| -4.9000 | 0.96158 | 0.92878 | 0.99996 | 1.0000 | 1.0000 | 0.95414 | 0.94347 |
| 5.8000 | 0.95961 | 0.93366 | 0.98175 | 0.99316 | 0.98234 | 0.93519 | 0.93470 |
| 22.600 | 0.91330 | 0.88780 | 0.93381 | 0.94922 | 0.93719 | 0.90828 | 0.89376 |
| 73.200 | 0.78621 | 0.77951 | 0.86190 | 0.87598 | 0.85672 | 0.74576 | 0.78070 |
| 85.000 | 0.77438 | 0.74829 | 0.77274 | 0.78320 | 0.79293 | 0.75972 | 0.77778 |

Table A.3.1--Pressure ratio distribution, first vane, $10 \%$ span. \% wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -72.400 | 0.86831 | 0.83445 | 0.89595 | 0.89234 | 0.88943 | 0.85020 | 0.84981 |
| -60.400 | 0.85767 | 0.83254 | 0.85645 | 0.87585 | 0.87378 | 0.83929 | 0.83624 |
| -36.400 | 0.99996 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| -15.300 | 0.99319 | 0.96172 | 0.98844 | 1.0000 | 0.99804 | 0.98611 | 0.99031 |
| -7.6000 | 0.95931 | 0.93971 | 0.94798 | 0.94277 | 0.94423 |  |  |
| 34.300 |  |  |  |  |  |  |  |
| 64.100 | 0.77442 | 0.76364 | 0.75723 | 0.76431 | 0.77397 | 0.75099 | 0.78488 |
| 74.700 | 0.81410 | 0.85742 | 0.79094 | 0.80213 | 0.83659 | 0.79663 | 0.85659 |

Table A.3.2--Pressure ratio distribution, first vane, $50 \%$ span. \% wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -36.800 | 1.0000 | 1.0000 | 0.99998 | 1.0000 | 1.0000 |  |  |
| -4.7000 | 0.89197 | 0.85129 | 0.93754 | 0.92958 | 0.91932 | 0.93100 | 0.83100 |
| 6.0000 | 0.86042 | 0.74738 |  | 0.88826 | 0.87242 | 0.68900 | 0.70700 |
| 22.100 | 0.72753 | 0.72164 | 0.74183 | 0.73709 | 0.72889 | 0.74900 | 0.76500 |
| 46.600 | 0.62141 | 0.62726 | 0.60763 | 0.61502 | 0.62101 | 0.64200 | 0.68600 |
| 65.500 | 0.78967 | 0.78646 | 0.76420 | 0.76526 | 0.77205 | 0.77000 |  |
| 81.800 | 0.97514 | 0.89609 | 0.99718 | 0.99624 | 0.98030 |  |  |

Table A.3.3--Pressure ratio distribution, first vane, $90 \%$ span. $\%$ wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -62.600 | 0.91500 | 0.89200 | 0.75936 | 0.82600 | 0.83500 | 0.79187 | 0.82190 |
| -46.900 | 0.91000 | 0.93600 |  | 0.97700 | 0.95800 | 0.92170 | 0.90000 |
| -5.0000 |  |  |  |  | 0.97900 | 0.99823 | 0.99978 |
| 6.8000 | 0.98300 | 0.95300 | 1.00103 | 0.97000 | 0.96500 | 0.87711 | 0.90190 |
| 19.000 | 0.81900 | 0.82500 | 0.72097 | 0.78800 | 0.80000 | 0.74628 | 0.77429 |
| 48.900 | 0.81100 | 0.81200 | 0.77809 | 0.83600 | 0.83000 | 0.78989 | 0.77714 |

Table A.3.4--Pressure ratio distribution, first blade, $10 \%$ span. \% wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -72.700 | 0.83400 | 0.88400 | 0.90100 | 0.89000 | 0.89900 | 0.86200 | 0.88500 |
| -13.600 | 0.83200 | 0.85100 |  | 0.73400 | 0.76500 | 0.87200 | 0.79600 |
| 5.6000 | 0.72000 | 0.74000 | 0.70000 | 0.70200 | 0.71300 |  |  |
| 12.100 | 0.81800 | 0.82500 | 0.89800 | 0.90700 | 0.91800 | 0.81900 | 0.84500 |
| 18.400 | 0.76000 | 0.78500 | 0.71100 | 0.68100 | 0.67400 | 0.75200 | 0.70900 |
| 25.400 | 0.79600 | 0.81800 | 0.79200 | 0.79100 | 0.76800 | 0.80700 | 0.76300 |
| 45.800 | 0.78300 | 0.77900 | 0.79200 | 0.79100 | 0.79700 | 0.76700 | 0.77800 |
| 60.300 | 0.67200 | 0.70300 | 0.63200 | 0.68600 | 0.71700 | 0.69000 | 0.72200 |
| 79.400 | 0.79000 | 0.80800 | 0.77400 | 0.82000 | 0.82500 | 0.77600 | 0.79500 |

Table A.3.5--Pressure ratio distribution, first blade, $50 \%$ span. \% wetted distances less than zero are on pressure surface, \% wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -45.200 | 0.91200 |  |  |  |  |  |  |
| -4.9000 | 0.89400 | 0.86700 | 0.90700 | 0.88200 | 0.88500 | 0.87600 | 0.88100 |
| 6.0000 | 0.91700 | 0.96700 | 0.85700 | 0.87600 | 0.91100 | 0.84100 | 0.87900 |
| 16.600 | 0.80500 | 0.82300 | 0.77400 | 0.77500 | 0.79900 | 0.75700 | 0.78600 |
| 77.800 | 0.80300 | 0.79400 | 0.75200 | 0.78900 | 0.85300 | 0.72700 | 0.75400 |

Table A.3.6--Pressure ratio distribution, first blade, $90 \%$ span. \% wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 1 | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -91.190 | 0.013191 | 0.015026 | 0.015452 | 0.013966 | 0.014661 | 0.016170 | 0.015130 | 0.014617 |
| -81.670 |  |  | 0.022809 | 0.025479 | 0.025560 | 0.027150 | 0.023096 | 0.021765 |
| -62.560 | 0.0079545 | 0.0082174 | 0.0083739 | 0.0084706 | 0.0087706 | 0.0092800 | 0.0086087 | 0.0079565 |
| -38.690 | 0.0055909 | 0.0040957 | 0.0040435 | 0.0063529 | 0.0064862 | 0.0068700 | 0.0039043 | 0.0035913 |
| -12.790 | 0.0070364 | 0.0058348 | 0.0057652 | 0.0069832 | 0.0073486 | 0.0073000 | 0.0057043 | 0.0053565 |
| -6.5500 | 0.0088909 | 0.0070870 | 0.0070870 | 0.0079160 | 0.0082569 | 0.0082500 | 0.0072000 | 0.0068783 |
| 5.3800 | 0.0075000 | 0.0067043 | 0.0066957 | 0.0077983 | 0.0076147 | 0.0079500 | 0.0058870 | 0.0056783 |
| 23.230 |  |  |  |  |  |  |  |  |
| 35.870 | 0.010964 | 0.011009 | 0.010870 | 0.010866 | 0.010798 | 0.011440 | 0.010800 | 0.0093739 |
| 74.490 | 0.0060455 | 0.0056522 | 0.0058435 | 0.0052941 | 0.0050550 | 0.0051300 | 0.0058000 | 0.0056609 |
| 85.890 | 0.0063000 | 0.0058870 | 0.0059913 | 0.0056050 | 0.0055229 | 0.0056800 | 0.0060609 | 0.0057565 |

Table A.3.7--Stanton number distribution, first vane, $10 \%$ span. \% wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 1 | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -75.610 | 0.010036 | 0.010365 | 0.010522 | 0.0096639 | 0.010037 | 0.010320 | 0.010200 | 0.010252 |
| -59.240 | 0.0095000 | 0.0088522 | 0.0091304 | 0.0093697 | 0.0096789 | 0.010020 | 0.0090087 | 0.0088348 |
| -34.420 | 0.0061182 | 0.0050174 | 0.0054000 | 0.0054622 | 0.0059725 | 0.0063300 | 0.0049304 | 0.0044348 |
| -23.020 |  | 0.0032087 | 0.0032696 | 0.0052941 | 0.0056239 | 0.0057500 | 0.0035304 | 0.0035826 |
| -17.360 |  | 0.0036522 | 0.0038609 | 0.0055210 | 0.0058073 | 0.0061600 | 0.0039478 | 0.0039304 |
| -12.300 | 0.0054545 | 0.0041652 | 0.0041565 | 0.0056555 | 0.0058624 | 0.0063000 | 0.0042957 | 0.0042696 |
| -9.0200 | 0.0081182 | 0.0078870 | 0.0076696 | 0.0076975 | 0.0080092 | 0.0081100 | 0.0068870 | 0.0063130 |
| -8.7500 | 0.0054636 | 0.0047478 | 0.0047991 | 0.0050420 | 0.0059174 | 0.0063300 | 0.0048174 | 0.0048348 |
| -5.0500 | 0.0099091 | 0.0067565 | 0.0068870 | 0.0086555 | 0.0085780 | 0.0089400 | 0.0068087 | 0.0064261 |
| -2.7400 | 0.0076636 | 0.0099739 | 0.0098783 | 0.0097647 | 0.010385 | 0.010960 | 0.010078 | 0.0100000 |
| 0.0000 |  | 0.014504 | 0.014522 |  |  |  |  |  |
| 3.4100 | 0.0086273 | 0.0097826 | 0.0097652 | 0.0092773 | 0.010780 | 0.0091400 | 0.010217 | 0.010191 |
| 3.5200 | 0.0092818 | 0.0091391 | 0.0092087 | 0.0090336 | 0.0092661 |  | 0.0093739 | 0.0087826 |
| 8.0700 | 0.0057818 | 0.0057913 | 0.0057043 | 0.0058235 | 0.0068440 | 0.0065700 | 0.0059217 | 0.0059217 |
| 12.520 | 0.0053909 | 0.0042870 | 0.0042435 | 0.0055462 | 0.0060826 | 0.0063300 | 0.0043913 | 0.0043652 |
| 16.600 |  | 0.0036522 | 0.0041130 | 0.0067143 | 0.0070917 | 0.0075300 | 0.0043130 | 0.0042696 |
| 22.330 | 0.010345 | 0.0070435 | 0.0068348 | 0.010151 | 0.010275 | 0.010620 | 0.0077913 |  |
| 35.350 | 0.0084727 | 0.0070435 | 0.0072348 | 0.0082941 | 0.0089633 | 0.0089500 | 0.0075304 | 0.0068174 |
| 50.230 | 0.0088273 | 0.0096000 | 0.0098174 | 0.0082017 | 0.0087156 | 0.0088200 | 0.0098435 | 0.0097217 |
| 63.890 | 0.0080727 | 0.0085217 | 0.0086696 | 0.0076134 | 0.0082018 | 0.0083600 | 0.0089565 | 0.0088696 |
| 81.180 | 0.0078091 | 0.0084609 | 0.0086957 | 0.0074538 | 0.0080459 | 0.0083100 | 0.0087826 | 0.0086609 |

Table A.3.8--Stanton number distribution, first vane, $50 \%$ span. $\%$ wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 1 | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -76.860 | 0.0081364 | 0.0082087 | 0.0084957 | 0.0093277 | 0.0088991 | 0.0080100 | 0.0085739 | 0.0085130 |
| -61.150 | 0.0092545 | 0.0086435 | 0.0088783 | 0.0094958 | 0.010303 | 0.0083200 | 0.0096435 | 0.0089652 |
| -38.080 | 0.0070545 | 0.0056087 | 0.0058696 | 0.0073445 | 0.0071101 | 0.0063900 | 0.0061913 | 0.0060435 |
| -12.130 | 0.0076909 | 0.0048870 | 0.0039304 | 0.0056723 | 0.0059083 | 0.0055500 | 0.0055304 | 0.0050435 |
| -6.3800 | 0.010009 | 0.0055565 | 0.0058174 | 0.0075882 | 0.0081284 | 0.0077900 | 0.0075391 | 0.0059217 |
| 5.5000 | 0.0090727 | 0.0075826 | 0.0081478 | 0.0091933 | 0.0098440 | 0.010710 | 0.0080783 | 0.0078783 |
| 21.780 |  | 0.0079565 | 0.0081217 | 0.0096975 | 0.010009 | 0.010340 | 0.0092261 | 0.0085043 |
| 46.870 | 0.0060000 | 0.0062087 | 0.0062696 | 0.0054706 | 0.0054954 | 0.0061600 | 0.0061565 | 0.0059391 |
| 65.300 | 0.0054545 | 0.0046522 | 0.0048696 | 0.0048487 | 0.0049817 | 0.0074000 | 0.0048609 | 0.0030174 |
| 83.200 | 0.0073909 | 0.0062522 | 0.0061739 | 0.0063361 | 0.0070367 | 0.0079000 | 0.0073739 | 0.0044522 |

Table A.3.9--Stanton number distribution, first vane, $90 \%$ span. $\%$ wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 1 | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -65.130 | 0.0071273 | 0.0068261 | 0.0071739 | 0.0091597 | 0.011275 | 0.0069300 | 0.0069652 | 0.0067391 |
| -48.590 | 0.0066455 | 0.0060522 | 0.0065913 | 0.0067815 | 0.0071376 | 0.0066600 | 0.0063304 | 0.0058870 |
| -5.4500 | 0.010309 | 0.0089739 | 0.0098870 | 0.010588 | 0.011028 | 0.0090900 | 0.0099913 | 0.0089826 |
| 7.3100 | 0.010482 | 0.0053304 | 0.0046870 | 0.0035882 | 0.0044128 | 0.0048500 | 0.0041304 | 0.0036696 |
| 16.070 | 0.0074091 | 0.0050870 | 0.0046000 | 0.0035714 | 0.0047431 | 0.0047400 | 0.0052783 | 0.0051739 |
| 51.620 |  | 0.0065652 | 0.0064348 | 0.0072353 | 0.0077064 | 0.0070000 | 0.0065913 | 0.0064261 |
| 80.170 | 0.0068727 | 0.0069391 | 0.0063130 | 0.0066387 | 0.0067982 | 0.0060300 | 0.0069478 | 0.0067043 |

Table A.3.10--Stanton number distribution, first blade, $10 \%$ span. $\%$ wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 1 | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -87.700 | 0.0076000 | 0.0077739 | 0.0079739 | 0.0081008 | 0.0087431 | 0.0078200 | 0.0080957 | 0.0079652 |
| -72.800 | 0.0075455 | 0.0068348 | 0.0070087 | 0.0071513 | 0.0076514 | 0.0067000 | 0.0070435 | 0.0067652 |
| -60.500 | 0.0070455 | 0.0066174 | 0.0066348 | 0.0071092 | 0.0076697 | 0.0068300 | 0.0067043 | 0.0065217 |
| -44.500 | 0.0056727 | 0.0052522 | 0.0051652 | 0.0056471 | 0.0058440 | 0.0051700 | 0.0052783 | 0.0051391 |
| -23.610 | 0.0059000 | 0.0055478 | 0.0058609 | 0.0059580 | 0.0058899 | 0.0053900 | 0.0058087 | 0.0055217 |
| -21.870 | 0.0060364 | 0.0053217 | 0.0055043 | 0.0059832 | 0.0062202 | 0.0057100 | 0.0054261 | 0.0054261 |
| -20.200 | 0.0064182 | 0.0056435 | 0.0057043 | 0.0057059 | 0.0061284 | 0.0054600 | 0.0057652 | 0.0058957 |
| -16.100 | 0.0062182 | 0.0051826 | 0.0059304 | 0.0061345 | 0.0064679 | 0.0062100 | 0.0053739 | 0.0055391 |
| -12.300 | 0.0087909 | 0.0048000 | 0.0052087 |  |  |  | 0.0080348 | 0.0045739 |
| -8.7100 | 0.0065909 | 0.0051217 | 0.0050522 | 0.0055378 | 0.0058349 | 0.0056100 | 0.0053043 | 0.0050609 |
| 0.0000 | 0.015782 | 0.016539 | 0.016365 | 0.014429 | 0.015321 | 0.013980 | 0.016800 | 0.016478 |
| 5.7000 | 0.0061545 | 0.0053565 | 0.0053739 | 0.0070420 | 0.0084954 | 0.0073300 | 0.0069217 | 0.0060957 |
| 11.830 | 0.010255 | 0.0037478 | 0.0028522 | 0.0040504 | 0.0049541 | 0.0055900 | 0.0060348 | 0.0059652 |
| 15.000 | 0.0080182 |  |  |  |  |  |  |  |
| 17.710 | 0.0080364 | 0.0065130 | 0.0057478 | 0.0065378 | 0.0072936 | 0.0072700 | 0.0088870 | 0.0088870 |
| 24.200 | 0.0065455 |  |  |  |  |  |  |  |
| 28.510 | 0.0054636 | 0.0078957 | 0.0080522 | 0.0073109 | 0.0074587 | 0.0071800 | 0.0078174 | 0.0076609 |
| 48.380 | 0.0087273 | 0.0072957 | 0.0072870 | 0.0066471 | 0.0071009 | 0.0066600 | 0.0072522 | 0.0070870 |
| 64.100 | 0.0062182 | 0.0056435 | 0.0056609 | 0.0052689 | 0.0056422 | 0.0052900 | 0.0058870 | 0.0057652 |
| 81.990 | 0.0054091 | 0.0049130 | 0.0050522 | 0.0045882 | 0.0048624 | 0.0044600 | 0.0052000 | 0.0049826 |
| 92.790 | 0.0053273 | 0.0047652 | 0.0048348 | 0.0045546 | 0.0047431 | 0.0044500 | 0.0050870 | 0.0048261 |

Table A.3.11--Stanton number distribution, first blade, $50 \%$ span. \% wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.

| \% wetted <br> distance | Run 1 | Run 5 | Run 6 | Run 7 | Run 8 | Run 11 | Run 12 | Run 13 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -62.470 | 0.0073455 | 0.0066696 | 0.0065217 | 0.0070084 | 0.0075413 | 0.0062500 | 0.0066348 | 0.0064087 |
| -40.420 |  | 0.0053913 | 0.0054174 | 0.0055294 | 0.0058165 | 0.0050300 | 0.0054522 | 0.0054087 |
| -4.7900 | 0.0099545 | 0.0086522 | 0.0085391 |  | 0.0085505 | 0.0074300 | 0.0086174 | 0.0084783 |
| 6.8100 | 0.0077818 | 0.0093478 | 0.0090609 | 0.0098151 | 0.010606 | 0.0085800 | 0.0083391 | 0.0079826 |
| 46.230 | 0.0084364 | 0.0080087 | 0.0077391 | 0.0082017 | 0.0086147 | 0.0070200 | 0.0080348 | 0.0076000 |
| 57.400 | 0.0074545 |  |  |  |  |  |  |  |
| 69.660 | 0.010464 |  |  |  |  |  |  |  |
| 81.740 | 0.0088545 | 0.0098783 | 0.0098783 | 0.0094118 | 0.0099358 | 0.0088400 | 0.010017 | 0.0098609 |
| 90.010 | 0.0079000 | 0.0080696 | 0.0081913 | 0.0076891 | 0.0081743 | 0.0071200 | 0.0085391 | 0.0081913 |

Table A.3.12--Stanton number distribution, first blade, $90 \%$ span. $\%$ wetted distances less than zero are on pressure surface, $\%$ wetted distances greater than zero are on suction surface.


[^0]:    * Roughness measurements were performed at the United Technologies Research Center and supplied to CUBRC courtesy of M. Blair. Figure 4(b) has been reproduced here with permission of M. Blair.

