NASA Technical Memorandum 103917

//4/_ 1177769
P. 26

Thermal Conductance of Augmented Pressed Metallic Contacts at Liquid Helium Temperatures

L. J. Salerno, P. Kittel, and A. L. Spivak

(NASA-TM-I03917) TNERMAL CONDUCTANCE OF AUGMENTEr **PRESSED** METALLIC **CONTACTS AT** LIOUIO HELIUM T_MPERATURES **(NASA)** 26 p N92-32474 Unclas

> G3/34 **0_I7769**

August 1992

 \bar{c}

 $\label{eq:2.1} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^{2} \left(\frac{1}{\sqrt{2}}\right)^{2} \left(\$

 \sim $\sim 10^{-1}$

Thermal Conductance of Augmented Pressed Metallic Contacts at Liquid Helium Temperatures

L. J. Salerno and **P.** Kittel, **Ames** Research Center, Moffett Field, California A. L. Spivak, Trans-Bay Electronics, Richmond, California

August 1992

 \sim $\sqrt{2}$

Ames Research Center Moffett Field, California 94035-1000

 $\label{eq:2.1} \frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2\pi}}\int_{\mathbb{R}^3}\frac{1$ $\label{eq:2.1} \begin{split} \mathcal{L}_{\text{max}}(\mathbf{r}) = \mathcal{L}_{\text{max}}(\mathbf{r}) \,, \end{split}$

 $\sigma_{\rm 2} = \omega$

 $\sim 10^{11}$

 $\mathcal{L}^{\text{max}}_{\text{max}}$ $\mathcal{L}^{\text{max}}_{\text{max}}$

griften g

 \hat{f} , and \hat{f} is a set of \hat{f} , and \hat{f} $\hat{\mathcal{L}}_{\text{max}}$ and $\hat{\mathcal{L}}_{\text{max}}$ are the set of $\hat{\mathcal{L}}_{\text{max}}$

Thermal conductance of augmented pressed metallic contacts at liquid helium temperatures

L. J. Salerno, P. Kittel, and A. L. Spivak*

NASA Ames Research Center, Moffett Field, **CA 94035-1000, USA *Trans-Bay Electronics, Richmond,** California **94084, USA**

The thermal **conductance of uncoated OFHC copper, 6061-T6** aluminum, **free-machining brass, and** 304 **stainless steel sample pairs which** have **been augmented with a gold coated 6061-T6** aluminum **washer** inserted **between** the contact **surfaces** has been measured **over** the **temperature range of** 1.6 **to** 6.0 K, with applied forces from 22 N to 670 N. The contact surfaces of the sample pairs were pre**pared** with **a 0.8** _ **lapped** finish, **while** the **finish of** the aluminum **washer was 0.2** gm **lapped.** The **contribution to** the **overall** thermal impedance **by** the **bulk conductance of** the aluminum **washer was negligible. It was found** that addition **of** the **washer offered no significant conductance** improvement **over** an uncoated single contact pair, any benefits from the gold plated washer being used to counter**act** the **addition of two more contact surfaces. Additionally,** the thermal **conductance** of **a** "combination" **aluminum sample pair having one gold coated and one uncoated surface was measured** and **compared to** the **washer pair.** The ratio **of** the **conductance of** the **washer pair to** half the **conductance of the** "combination" **pair** was **found to** be **constant and near unity over** the **temperature range of** the **data obtained,** within **experimental error.**

Keywords: pressed **contacts;** thermal **conductance; liquid** helium

 $\mathbf{1}$

The design of space flight missions employing cryogenically cooled instruments requires a knowledge of the thermal conductance of the bolted and pressed contacts between the instruments and their **respective refrigeration systems. Previous work** 1-5 **has shown** that the thermal conductance may be increased **significantly by gold coating both contact surfaces. In many** instances, **due** to the **size** and **configuration of** the **instrument, gold coating of** the insmunent **contact surface or of** an **entire cold plate may not be feasible. Hence, it has** been **suggested** that **gold plated washers placed at the** bolted joints between **the** instrument and its interface **may provide** a **simpler** and more cost **effective** method **of augmenting the** thermal **performance, despite the** addition **of two more** contact interfaces. *This* **paper** presents the results **of a** series **of measurements of** the thermal **conductance of uncoated** matched **sample pairs fabricated of OFHC copper, 6061-T6** aluminum, **free-machining brass,** and **304 stainless steel** having **a gold coated** aluminum **washer placed** between the **contact surfaces.**

Method- :.... ._-__ _

A detailed description of the apparatus and the experimental method has been presented previously, ¹ and **will** be summarized **here. The measurements** were **made with** the lower contact **linked** to **a liquid helium** bath held at approximately 1.3 K. The washer is placed in between the two contact surfaces. *The* conduction path **is through** an **uncoated surface,** a **gold** contact **surface,** the aluminum **washer,** another **gold contact surface,** and an uncoated **surface. A range** of **forces from 22 N** to **670 N was applied** to the contact pair/washer combination, **by** a **rocker ann** pulled by **a wire. An external** motor **drive Was U_** to apply the **force to** the **wire.** *The* **wire and** the **rocker arm-assembly are** thermally anchored to **the** cold plate, which **is** immersed **in** liquid **helium. In** between the lever and the **sample**

a sa kabiling ng pangalang taong taong pangalang na pangalang na pangalang na pangalang na pangalang na pangal
Pangalang na pangalang na pangal

 $\overline{2}$

pair/washer combination **is a stack** of **insulators.** A **heater** is placed between the insulators and the **upper** sample. Thermometers **are** placed in the **upper and** lower samples, in the upper insulator, and in the cold plate.

The aluminum washers measured 19.0 mm in diameter and **2.5** mm in height or 2.5 mm high. They were prepared by first lapping them to a 0.2 μ m surface finish. They were then cleaned ultrasonically **using** I,I,I Trichlorocthane followed by **a** reagent grade **surfactant** (Tergitol), rinsed in deionized water, cleaned **ultrasonically** in **acetone followed** by isopropyl alcohol, rinsed in de-ionized water, and blown dry in clean **nitrogen** gas. **Following** this procedure, all washers were inspected. In the coating process, **the** washers were first ion milled. Then **a** 100 **nm** layer of chromium was deposited, followed by 2 μ m of gold.

Overall **dimensions of** the **sample** pairs were 12.7 **mm** in diameter and **8.89 mm** in height for the **upper sample** and 10.2 **mm** in diameter and **15.2 mm** in **height for** the **lower sample. All** contact **sur**faces on the sample pairs were lapped to a 0.8μ m finish.

Results

For each sample pair, **data were taken at** 8 **forces** (22, **45,** 11,221,331,441,551, and 661 **N, although** the **forces were nominally listed at 22,** 44, **112, 224,** 336, 448, 560, and 670 **N),** 8 **heater** powers in the **range from O to 10** mW and **for a steady helium bath temperature** of **approximately** 1.3 **K. (For** the **stainless steel pair,** power **was** limited **to 2.5 mW due to** the **low** thermal conductivity of the material.) **For** each **force** the resulting **data** set of **upper (Th)** and **lower (Tc) sample** temperatures, and **heater** powers **(Q) was** fit **to** the **function**

 $\overline{\mathbf{3}}$

$$
Q + Q_0 = \int_{T_c}^{T_h} \alpha T^n dT
$$
 (1)

where Q_0 is the parasitic heat flux. The parameters to be fit are Q_0 , α , and n . Q_0 was -0.1 mW. The thermal **conductance is**

$$
k = \alpha T^{\prime\prime}
$$

(2)

The fitted thermal conductances are shown in Figures 1-4 for the aluminum, brass, copper, and stainless steel sample pairs. The fitted α and n are also listed in Table 1. The errors presented represent the scatter in the data. These errors do not reflect the estimated errors in individual readings which were ± 7.3 mK for temperature, ± 0.055 % for heat input, and, for force measurements, from ± 0.09 N to ± 1.4 N, depending upon sample and applied force.

Discussion

The **conductances** of **the** gold **coated** aluminum washer sandwich **are compared to the conductances** of both the previously measured uncoated contacts¹⁻⁴ and the previously measured gold coated contacts5 **in** Figures 5-8. All **comparisons** are **made at** the highest **applied contact force, 670 N.**

r

From the comparisons **in** Figures **5-8, it is** seen that **for** the aluminum contact pair, the conductance **is virtually** unchanged by addition **of** the **gold** coated aluminum washer. For the brass sample pair, addition of the washer results in both a degradation of conductance by approximately 1 mW/K **at** 1.6K, gradually le_ng to**a small** improvement in conductance **to a maximum** of **2.5 mW/K at 6.0** K, the **crossover** occurring **at approximately** 3.6 K. For the **copper** sample **pair, conductance** over **the entire** temperature **range is** degraded **by addition of** the **washer,** the degradation **reaching a maximum** of approximately **4.5 mW/K** at **6.0** K.

In **examining** the **stainless steel data, it can** be **seen** that the washer data **differ from** the uncoated data by no more than 0.4 **mW/K,** while the **gold** coated data **differs by** no **more** than 0.2 mW/K. At 6.0 K, the **experimental error** *gives* a **deviation of 0.1** mW/K **for** the uncoated **data,** 0.08 mW/K **for** the **gold** coated data, and **0.04 mW/K for** the washer data. **Therefore,** the **difference** between the **uncoated** and **gold coated** data **lies within twice** the **experimental error, while** the **difference** between the **uncoated** and **washer data** is **roughly four** times the **experimental error, suggesting** that **differences may** be **insignificant.** Another **uncertainty** in the comparison **between** the **augmented, coated,** and uncoated stainless steel samples **is** that the sample pairs were **made** several years apart, and hence, from different batches of material. Although the data reported here employ a temperature cor**rection to** account **for** the **low** thermal conductivity **of** the **material,5** the **reported bulk** conductivity **of 304** stainless steel is dependent **upon** the **particular batch,** and any temperature correction **made** to the **data** may **not** be **adequate** to **reflect** the true **bulk conductivity of** the subject batch. **A calculation was made comparing** the thermal conductance **obtained using** the **uncorrected** temperatures with **that obtained employing** the **correction.** The **result** indicated **a difference in magnitude of 0.02** roW/K, **or** half the **experimental error for** the **washer data,** again suggesting that any **differences** between the **stainless steel curves may be** insignificant.

The analysis performed **here treats** the conductance **path** as **a** single **impedance. This** approach **is valid, assuming** an insignificant contribution to the impedance **by** the **washer. In examining** the **bulk conductance of** the aluminum **washer, it was calculated to** be **over** two **orders of** magnitude **higher** than the **highest contact conductance reported;** therefore it **was** assumed to play a **negligible part in** the **overall contact conductance.**

A close look at the thermal path **shows** that **it** is **greatly constricted at the contacts because** the actual **contact** is **made only** at a **few** points, perhaps **as** low as **three.** Thus, **at** the **contacts,** the **heat**

flow **is constricted** to **a small region.** This **results** in an **increased** temperature **gradient** in the **contact region.** It **is** this **increase** which **is** here **referred** to as the contact conductance. Additionally, the con**ductance is** affected by the presence **of oxide layers on** the surfaces in contact. **Uncoated** aluminum, brass, and copper **develop** an **oxide layer** quickly after preparation. **This layer is** a poor thermal con**ductor. The** thermal path between the contacts includes two **oxide layers** in the region **of greatest** constriction **of** the heat **flow,** thus **enhancing** the temperature **gradient.** In the case **of** stainless steel, however, **oxidation occurs much more** slowly; therefore **its** contact conductance **is due** principally to the **constriction effect** in the bulk **material.**

Since the purpose **of gold** coating the contact surfaces **is** to prevent **oxidation,** coated contacts should have **only** the **constriction effect in** the base **metal,** unimpeded **by** a poorly conducting **oxide** layer. The dissimilar metals at the **interface** could affect the **local** conductivity, **however** these **layers** are so thin that their **effect** should be negligible. Gold, **being** soft, witl **deform more** readily than the **base** material. This will **increase** the actual contact area, **decreasing** the constriction and increasing the **conductance.** Again, this **layer is** so thin that this **effect** should be negligible. The relative **effect of** applying the **gold layer** to the different **materials is readily** apparent. The **gold** layer greatly improved the conductance **for materials** that readily **form oxide layers** (aluminum, **brass,** and copper), **but** did not improve **on** the **material** that **does** not **oxidize** readily (stainless **steel).** The **reduced conductance of** the **coated** stainless **steel over** the **uncoated** contacts may in part **be due** to the **addi**tional **layers of** material (the coatings) **in** the region **of greatest heat flow** constriction.

Introducing **a washer** between **the** contact **surfaces** adds **several** complications. One **is** the **effect of differential** thermal contractions. Such contractions could result in a shear stress at the contact, which **in** turn might affect the conductance. This problem was avoided **by cooling** the samples **from** room temperature with only a light applied force. Furthermore, the first data points were always

taken with **a** low **applied** force, **to allow** the different materials **to** independently contract, relieving most of any **shear stress.** A second complication is that the bulk conductance of the washer is not the **same (except for** the aluminum **sample)** as that **of** the contacts. This may **result** in thermal mismatch which increases the thermal impedance. A third complication **arises** from having twice the number of regions of constricted heat flow. *Since* two of these **regions** are coated and two **arc** uncoated, it would be **expected** that the conductance would depend on the **sum** of these impedances. When thermal impedances are in **series, as** they arc in this case, the impedances **simply** add. Therefore, the conductance is given by

$$
\mathbf{k=}\left\{ \sum \mathbf{k_{i}}^{-1}\right\} ^{-1}
$$

Ê

where the **ki arc** the individual *conductances.* Thus, the **total conductance** would be **less** than that of the **uncoated** conductance, the **effect** observed here.

To support **this** hypothesis, the thermal *conductance* of the "combination" **sample** pair was mea**sured. Earlier,** the washer conductance had been compared with the **sum** of the conductance of both **a** coated and an uncoated **sample** pair. **Figure 9** presents results of this comparison; however, this case is not representative of the actual conditions, thus the "combination" **sample** was **tested.** Results **arc shown** in **Figure** I0. A comparison of half the value of the "combination" *conductance* with the value of *conductance* obtained with the washer **should show identical** results. **Figure** I l compares the conductancc of half the "combination" case to that of the **uncoated, gold** coated, and washer *cases.* In **Figure** 12, it is demonstrated that the ratio of the thermal conductance for the washer case to half the thermal conductance of the "combination" case is constant, and essentially **unity,** over the temperature range **of** the **data obtained,** within **experimental error.** An **extensive error** analysis **was performed**

in which the **error in** the **ratio of** the thermal conductances was determined. First, **it** was necessary to determine the **error** in **k,** the thermal conductance. Since

 $k = \alpha T^n$

the error in **k**, as a function of the errors in α and n is given by

$$
\Delta \mathbf{k} = \left[\left\{ (\partial \mathbf{k}/\partial \alpha) \Delta \alpha \right\}^2 + \left\{ (\partial \mathbf{k}/\partial \mathbf{n}) \Delta \mathbf{n} \right\}^2 \right]^{1/2}
$$

Having obtained this **error,** the **root mean** square **error for** the **ratio was calculated at** both **1.6** K and 6.0 K. **The error** at 1.6 K was approximately **8%,** while at 6.0 K, **it** was 14.5%.This **demonstrates** that the thermal conductance **of** the sample pair having the washer **in between is** half the conductance **of** a single contact pair having **one gold** coated and **one uncoated** surface.

Conclusions

The thermal conductance **of** uncoated **OFHC copper,** 6061-T6 aluminum, **free-machining brass,** and **304** stainless steel **contacts having a** gold coated aluminum **washer** inserted between the contact **surfaces** has **been measured over** the temperature **range of** 1.6 to 6.0 **K,** with applied **forces from 22 N** to 670 **N.** The contribution to **the overall** thermal **impedance** by the bulk conductance **of** the aluminum washer was negligible. It was **found** that addition **of** the washer **offered** no significant conductance improvement **over** an uncoated single contact pair, since any benefit **from** the **use of** the **gold** plated washer was used to counteract the addition **of** two **more** contact surfaces. Additionally, the thermal conductance **of** a "combination" aluminum sample pair having **one** g01d coated and **one** uncoated surface **was measured** and compared to the **washer** pair. **The** ratio **of** the conductance **of** the washer pair to half the conductance **of** the "combination" pair was **found to be** constant, and near unity **over** the temperature **range of** the **data obtained,** within **experimental error.**

Acknowledgement

We would like to **thank Dave Paananen of Ball** Aerospace for his assistance in **cleaning and** coating the washers.

References

- **1 Salerno, L. J.,** Kittel, **P. and Spivak, A. L. Thermal Conductance of Pressed** Copper Contacts **at Liquid Helium Temperatures,** AIAA **J., Vol. 22 (1984), p. 1810.**
- **2 Salerno, L. J.,** Kittel, **P. and Spivak,** A. **L. Thermal** Conductance **of Pressed** OFHC **Copper** Con**tacts at Liquid Helium Temperatures, in:** Thermal Conductivity **18, Proceedings of** the **18th** International **Thermal Conductivity** Conference, **Plenum Press (1985),** p. **187.**
- **3 Salerno, L. J.,** Kittel, **P., Brooks, W.** F., **Spivak,** A. **C.** and Marks, **W.** G., **Jr.** Thermal Conductance of Pressed Brass Contacts at Liquid Helium Temperatures, Cryogenics, Vol. 26, (1986), **217.**
- 4 Salerno, **L. J., Kit'tel,** P., Scherkenbach, F. **E.** and Spivak, A. **L.** Thermal Conductance **of** Pressed Aluminum and Stainless Steel Contacts at **Liquid Helium** Temperatures, **in:** Thermal **Conductivity** 19, **Proceedings of** the **19th International** Thermal **Conductivity Conference, Plenum Press (1988), p.** 431.
- 5 **Kittel, P., Spivak, A. L. and Salerno, L. J.** Thermal Conductance **of Gold Plated Metallic Contacts at Liquid Helium Temperatures,** to **be published in Advances in Cryogenic Engineering,** 37 (1992)

Table 1 Results

 $\frac{1}{2\pi\epsilon}$

enna
Santa Carlos
Santa Carlos

 $\hat{\boldsymbol{\epsilon}}$

 $\displaystyle{ \raisebox{0.6ex}{\scriptsize{*}}} \alpha$ in units of mW/Kⁿ

Thermal conductance of augmented contacts at LHe temperatures

- Figure 1 0.8gm **Aluminum w/Au plated Aluminum** Washer
- Figure 2 **0.8 gm Brass w/Au plated** Aluminum Washer
- Figure **3 0.8 lain Copper w/Au plated** Aluminum **Washer**
- **Figure 4 0.8 gm Stainless Steel w/Au plated** Aluminum **Washer**
- Figure **5 0.8 lava** Aluminum/Au **coating/Washer Comparison**
- Figure 6 0.8 μ m Brass/Au coating/Washer Comparison
- **Figure** 7 **0.8** μ m Copper/Au coating/Washer Comparison
- Figure **8 0.8 gm Stainless Steel/Au coating/Washer Comparison**
- Figure **9 0.8 gm Aluminum/Washer/Sum** (Au **+ un)**
- Figure 10 0.8 gm Aluminum Combination **(1 Au** coated **surface +** 1 uncoated)
- Figure 11 **0.8 I.tm** Aluminum/Au **coating/Washer/Au-un** Comparison
- Figure 12 **Aluminum,** 0.8 **gra, Ratio of** k **Washer to** 1/2 k **Au-un combination**

Fig. 1

 β - β - β - β

 $\frac{1}{2}$

 \bar{z}

ر

 $\label{eq:2.1} \mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\mathcal{A})=\mathcal{A}(\$

Fig. 2

 \mathbf{r}

 $\frac{1}{2}$

Fig.

 $\overline{}$

 $\hat{\pmb{z}}$

Fig. 4

 $\overline{15}$

Fig. 5

 $\frac{1}{2}$

 \Box

 $\bar{\mathbb{C}}$

Fig.6

. . . .

 \cdot

Fig. 7

 $\ddot{}$

 $\vec{\tau}$

Fig. 8

Fig. 9

Ļ.

÷,

l,

 $\frac{1}{\epsilon}$ \bar{z}

 $\frac{1}{2}$

 \mathbf{A} and \mathbf{A} and \mathbf{A} are \mathbf{A}

J

Fig. 10

ż.

 $\tilde{\mathbf{V}}$

 $\frac{1}{2}$

Fig. 11

 $\overline{1}$

 $\label{eq:1} \begin{split} \textbf{L} & \textbf{L} = \textbf{L} \left(\textbf{L} \right) \textbf{L} \left(\textbf{L} \right) = \textbf{L} \left(\textbf{L} \right) \textbf{L} \left(\textbf{L} \right) = \textbf{L} \left(\textbf{L} \right) \textbf{L} \left(\textbf{L} \right) = \textbf{L} \left(\textbf{L} \right) \textbf{L} \left(\textbf{L} \right) = \textbf{L} \left(\textbf{L} \right) \textbf{L} \left(\textbf{L} \right) = \textbf{L} \left($

 \Rightarrow τ

ā

 $\sim 20\,$ km s $^{-1}$ e de la construcción de la constru
En 1970, en la construcción de la $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}$

 $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$ and $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$ and $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$ and $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$

 \mathcal{L}_{max} and \mathcal{L}_{max} . We can also also also

 $\bar{\gamma}$

 $\frac{1}{2}$

 $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})))$

 $\label{eq:2.1} \begin{split} \mathcal{L}_{\text{max}}(\mathbf{w}) & = \mathcal{L}_{\text{max}}(\mathbf{w}) \left[\mathcal{L}_{\text{max}}(\mathbf{w}) - \mathcal{L}_{\text{max}}(\mathbf{w}) \right] \times \mathcal{L}_{\text{max}}(\mathbf{w}) \\ & = \mathcal{L}_{\text{max}}(\mathbf{w}) \times \mathcal{L}_{\text{max}}(\mathbf{w}) \times \mathcal{L}_{\text{max}}(\mathbf{w}) \times \mathcal{L}_{\text{max}}(\mathbf{w}) \times \mathcal{L}_{\text{max}}(\mathbf{w}) \times \mathcal{L}_{\text{max}}(\$ \sim 100 masses (\sim 100 mass). The second contract \sim 100 mass $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$. The contribution of the set of $\mathcal{L}^{\mathcal{L}}$ $\label{eq:2} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{2}\left(\frac{1}{\sqrt{2}}\right)^{$ ~ 10

al<mark>ing and the straight</mark> and the second complete the second product of the second second second second second second المرادي المتفقية an an Salaman.
Ta san an san an an Alba

 $\label{eq:2.1} \mathcal{L}_{\text{max}}(\mathcal{L}_{\text{max}}) = \frac{1}{2} \sum_{i=1}^{2} \mathcal{L}_{\text{max}}(\mathcal{L}_{\text{max}})$ ~ 10 murti B.

 \sim \sim

 $\label{eq:2.1} \mathcal{F}^{(1)}_{\mathcal{A}}(x)=\left\{ \begin{array}{ll} \mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=\mathcal{F}^{(1)}_{\mathcal{A}}(x)=$ \sim and \sim $\label{eq:2.1} \mathcal{L}_{\text{max}} = \frac{1}{\sqrt{2\pi}}\left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2\pi}}\right)^{1/2} \left(\frac{1}{\sqrt{2$

 ω . In the case of ω Éstanistan en Grupo

ranta.
Alian di Afrika del Mandela $\sum_{i=1}^n \gamma_i \cdot \gamma_i$ $\hat{\mathcal{L}}$