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# Simulation of TunneLadder Traveling-Wave Tube Cold-Test Characteristics: <br> Implementation of the Three-Dimensional, Electromagnetic Circuit Analysis Code Micro-SOS 

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## Summary

The three-dimensional, electromagnetic circuit analysis code, Micro-SOS, can be used to reduce expensive and timeconsuming experimental "cold-testing" of traveling-wave tube (TWT) circuits. The frequency-phase dispersion characteristics and beam interaction impedance of a TunneLadder traveling-wave tube slow-wave structure were simulated using the code. When reasonable dimensional adjustments are made, computer results agree closely with experimental data. Modifications to the circuit geometry that would make the TunneLadder TWT easier to fabricate for higher frequency operation are explored.

## Introduction

Micro-SOS is a three-dimensional, finite-difference, electromagnetic plasma physics simulation code that was developed by Mission Research Corporation (MRC) in coopcration with Varian Associates, Inc. (refs. 1 to 3). Micro-SOS is a version of the MRC code SOS (Self Optimized Sector) but differs in that it does not have the capability to simulate charged particle trajectories. It can be operated in either a time-domain algorithm in which Maxwell's time-dependent equations are solved, or a frequency-domain algorithm (as in this report) in which the resonant mode frequencies and field patterns are obtained.

Micro-SOS was developed by MRC as part of a DOD- and NASA-sponsored effort to develop software for microwave tube design. This code can provide a fast, inexpensive circuit analysis capability that can be used to obtain "cold-test" information about the electromagnetic fields in a microwave tube circuit. The term "cold-test" refers to evaluation of a circuit without the presence of an electron beam. Cold-test measurements are typically performed in the laboratory on actual- or scaled-size circuit models. Using Micro-SOS can potentially eliminate the need for these time-consuming and cosily hardware cold-test measurements and greatly facilitate the design of novel microwave tube circuits.

In this report, Micro-SOS was used to determine the fre-quency-phase dispersion characteristics and beam interaction impedance of a TunneLadder traveling-wave tube (TWT) slow-wave circuit. We chose this circuit to simulate because it is capable of achieving high gain and power over a short distance and shows promise for a high-power, high-efficiency,
relatively low-cost TWT at millimeter-wave frequencies. Because of its rather complex geometry, this circuit has not been previously analyzed with a high degree of accuracy.

## Background

The TunneLadder is a millimeter-wave TWT with a fundamental forward-wave slow-wave circuit derived from the Karp circuit (refs. 4 and 5). The original Karp circuit (fig. 1) is a ridged waveguide with transverse slots in the top wall, with the slotted wall referred to as a "ladder." The radiofrequency (RF) field across the slots interacts with an electron beam that flows on either or both sides of the ladder. The passband of this circuit is above the cutoff frequency of the waveguide and below the frequency at which there is one-half wavelength between slots.

In the 1950 's and carly 1960 's, the original Karp circuit was primarily used in backward wave oscillators (BWO's) at frequencies up to 300 GHz (refs. 5 to 7). When operated as a BWO, the beam voltage is adjusted to a level of only a few kilovolts so that the interaction takes place with the first backward space harmonic (fig. 2) at the intercept with the beam voltage line $V_{1}$. By increasing the beam voltage to $V_{2}$, the interaction takes place with the fundamental forward wave and the Karp circuit operates as an amplifier. Fundamental forward-wave interaction implies a higher rate of gain than that in backward-wave interaction. Karp (ref. 7) showed that this advantage can be enhanced in the TunneLadder circuit by forming the ladder into a quasi-elliptical shape, creating a beam tunnel through which the beam passes (fig. 3). The tunnel is supported by dielectric chips in a double-ridge waveguide. The resulting TunneLadder circuit is a narrow bandwidth, high-efficiency, mechanically sturdy, and relatively inexpensive millimeter-wave amplifier.

Kosmahl and Palmer (ref. 8) performed an approximate field analysis study of an idealized TunneLadder circuit. When a two-dimensional geometry was used, the beam tunnel was approximated by a circle and the dielectric supports were ignored. By approximately matching the axial electric and magnetic fields at circuit boundaries, frequency-phase dispersion curves were obtained that were in fairly good agreement with the experimental results obtained by Karp (ref. 7).

Two 29-GHz TunneLadder TWT's, fabricated and tested by Varian Associates, Inc., under contract to NASA Lewis Research Center (NAS3-22466) (ref. 9) successfully demon-


Figure 1.-Karp circuit.


Figure 2.-Frequency-phase dispersion relationship for Karp circuit.
strated the bigh gain per length and interaction efficiency attainable with this narrow bandwidth circuit. The length of the slow-wave circuit was only 2.86 cm and the $10-\mathrm{kV}$, $215-\mathrm{mA}$ electron beam was focused with a single permanent magnet. The first TWT (S/N 101) achieved a peak saturated RF output power of 365 W , a very high interaction efficiency of 17.0 percent, and a $3-\mathrm{dB}$ bandwidth of 2.3 percent under pulsed operation. Because of an apparent vacuum leak, $\mathrm{S} / \mathrm{N}$ 101 could not be operated under continuous wave (CW) conditions. The second TWT (S/N 102) was operational at CW, with a peak saturated RF output power of 316 W , interaction efficiency of 13.8 percent, and bandwidth of 2.8 percent. The lower values of efficiency and power for $S / \mathrm{N} 102$ may have been due to a poor match in the output section. Despite these problems, the experimental results confirmed the high gain per length, high interaction efficiency, and narrow handwidth characteristics predicted for the TunneLadder circuit.

In order to accurately simulate the electrical characteristics of the Tunncladder using a coupled-cavity, RF-electron beam interaction computer model (e.g., ref. 10), input is

(a) Top view.

(b) End view.

Figure 3.-TunneLadder circuit.
required for both beam interaction impedance and RF phase shift per cavity period. The frequency dependence of the RF phase shift per cavity period is known as the dispersion relationship. In the past, this information has been obtained experimentally by cold-test measurements of resonant frequencies of a short-circuited length of the circuit (refs. 11 to 13).

Karp (ref. 7) determined the dispersion characteristics for a TunneLadder circuit with an 8-period, cold-test model built to a $16: 1$ scale. Figure 4 shows the dispersion curves for the three lowest-order modes. The lowest frequency curve represents the symmetric ladder mode which provides for the useful gain of the circuit. In this mode, each ridge and ladder has the same RF potential as its opposite member across the beam hole, and the axial electric field is finite on the axis. The intersect of this curve with the diagonal line, representing the electron beam axial velocity, corresponds to the operating frequency and phase shift per period. The next highest frequency curve represents the undesirable antisymmetric ladder mode. In this mode, the RF potential at each ridge or ladder is $180^{\circ}$ out-of-phase with its opposite member across the beam hole, and the axial electric field is zero on the axis. Interaction of the electron beam with this mode could produce undesired oscillation. However, because of the high frequency and weak axial electric field (except near the dielectric supports), circuit attenuation is higher than the gain, and the risk of oscillation is minimal (ref. 7). The circuit


Phase shift per period, rad
Figure 4.-Experimentally obtained dispersion curves for three lowest frequency modes of a TunneLadder circuit (from ref. 7).
attenuation is even higher for the third mode (fig. 4), called the cavity mode, which is essentially the transverse magnetic mode $\mathrm{TM}_{11}$ that propagates in a double-ridge waveguide.

As shown herein, Micro-SOS can be used instead of experimental cold-testing to obtain dispersion characteristics and beam interaction impedance for the symmetric ladder mode of a TunneLadder circuit.

## Simulation

Micro-SOS was used to simulate the frequency-phase dispersion characteristics of the symmetric ladder mode of the Varian $29-\mathrm{GHz}$ TunneLadder TWT (ref. 9) described in the previous section. The circuit is shown in figure 3 and the dimensions are given in table 1 . Figure 5 shows the $x_{1}-x_{2}$ cross-sectional Micro-SOS grid with a single cavity divided into 37 ( $\mathrm{x}_{1}$-direction) $\times 38$ ( $\mathrm{x}_{2}$-direction) $\times 8$ ( $\mathrm{x}_{3}$-direction) cells, totaling 11248 cells. The grid was nonuniform with the finest spacing in the beam hole region.

The procedure for calculating the dispersion characteristics is similar to that used by Kantrowitz and Tammaru (ref. 14) for a coupled-cavity circuit using the computer code ARGUS, a three-dimensional, electrodynamic circuit analysis code developed by Science Applications International Corporation (ref. 15). For a geometrically simpler coupledcavity circuit, Kantrowitz and Tammaru obtained an accurate dispersion curve using only resonant frequencies at three different values of RF phase shift per cavity period. These resonances were obtained with three separate computer runs, each with different boundary conditions on a single cavity. To determine an accurate dispersion curve for the highly dispersive Tunneladder circuit, in addition to the three frequencies obtained with single-cavity Micro-SOS computations, two more resonant frequencies were obtained from a single computer run on a string of two cavities with the appropriate boundary conditions (described next).

TABLE 1-DIMENSIONS OF 29-GHZ TUNNELADIDER CIRCUIT
[Sce fig. 3]

| Parameter | Dimensions, mm |
| :--- | :---: |
| Dielectric height, a | 0.2540 |
| bielectric width, $b$ | .3810 |
| Ridge height, $c$ | 1.0160 |
| Ridge width, $d$ | 1.9050 |
| Waveguide gap, $g$ | 1.2446 |
| Dielectric length, $k$ | .2032 |
| Ladder length, | .1524 |
| Gapplength, $m$ | .1651 |
| Period, $p$ | .3175 |
| Tunnel primary radius, $r_{1}$ | .4300 |
| Tunnel secondary radius, $r_{2}$ | .3048 |
| Side section height, $s$ | 3.2760 |
| Ladder thickness,, | .0035 |
| Side section width, $w$ | .8890 |



Figure 5.-Micro-SOS cross-sectional grid for TunneLadder
circuit.

In determining the resonance frequencies for both one- and two-cavity configurations, each axial boundary was truncated by either an "electric wall" or a "magnetic wall." An electric wall, $E$, is a boundary condition equivalent to a perfectly conducting plane at which the electric field is perpendicular and the magnetic ficld is parallel. With this boundary condition, the axial electric fields on each side of the boundary are in the same direction (fig. 6). It is simulated with Micro-SOS by using the STRUCTURE command. A magnetic wall, $M$, is a boundary condition that is a symmetry plane with parallel electric fields and perpendicular magnetic fields. With this boundary condition, the axial electric fields on the two sides of the boundary are in opposite directions (fig. 6). It is simulated with Micro-SOS by using the SYMMETRY command. Table II summarizes the boundary conditions used to obtain the various resonance points for the dispersion curve of the symmetric ladder mode. Table II also shows the run execution times consumed on Lewis' VAX minicomputer (model 9410). Additional resonance points could be obtained by modeling more than two cavitics, but would require an excessive amount of computer time.

The beam interaction impedance, known as the Pierce interaction impedance, is a measure of the strength of interaction between an RF-wave space harmonic and the electron beam. For the fundamental space harmonic, the beam interaction impedance on the axis is given by (ref. 16)

$$
\begin{equation*}
K_{0, \text { axis }}=\frac{E_{z 0}^{2}}{2 \beta_{0}^{2} P_{T O T}} \tag{1}
\end{equation*}
$$

where $E_{z}$ is the amplitude of the axial electric field of the fundamental space harmonic, $\beta_{(1)}$ is the axial phase constant


Figure 6.-Electric and magnetic wall boundary conditions
for Micro-SOs for Micro-SOS.

TABLE II. - MICRO-SOS RUNS WITH EXECUTION TIMES CONSUMED ON LEWIS' VAX minicomputer (MODEL 9410)

| Cavities <br> simulated | Boundary <br> conditions | Phase, <br> rad | Execution time, <br> min:sec |
| :---: | :---: | :---: | :---: |
| 1 | $E, E$ | $\pi$ | $4: 25$ |
| 1 | $E, M$ | $\frac{\pi}{2}$ | $15: 08$ |
| 1 | $M, M$ | 0 | $16: 41$ |
| 2 | $E, M$ | $\frac{\pi}{4}, \frac{3 \pi}{4}$ | $44: 29$ |

for the fundamental space harmonic, and $P_{T O T}$ is the total RF power flow given by

$$
\begin{equation*}
P_{T O T}=\frac{W_{T O T}}{N L} v_{g} \tag{2}
\end{equation*}
$$

where $L$ is the cavity period, $v_{g}$ is the group velocity, $N$ is the number of cavities modeled, and $W_{T O T}$ is the total electromagnetic energy stored in the cavities (obtained with MicroSOS by using the BALANCE and OBSERVE commands). The group velocity for equation (2) is obtained by taking the derivative of the best-fitting polynomial curve to the dispersion data and is defined as

$$
\begin{equation*}
v_{g}=\frac{\partial \omega}{\partial \beta_{0}}=2 \pi L \frac{\partial f}{\partial\left(\beta_{0} L\right)} \tag{3}
\end{equation*}
$$

where $\omega$ is angular frequency and $f$ is frequency.

To obtain $E_{z 0}$ in equation (1), the LINPRINT command is used to print out the values of the axial electric field at the center of each grid cell along the $z$-axis at the center of the beam hole. The axial electric field is then Fourier analyzed to determine $E_{z 0}$.

Note that the beam interaction impedance given in equation (1) is the value on the axis. In simulations with an RF-beam interaction coupled-cavity TWT model, such as in reference 10 , one must input the impedance integrated over the beam cross-section area. With the radial variation of the fundamental space harmonic of the electric field given by $I_{0}$ $\left(\gamma_{0} r\right)($ ref.17, p. 28), the finite beam interaction impedance is given by

$$
\begin{equation*}
K_{0, \text { beam }}=K_{0, \text { axis }}\left[I_{0}^{2}\left(\gamma_{0} b\right)-I_{1}^{2}\left(\gamma_{0} b\right)\right] \tag{4}
\end{equation*}
$$

where $K_{0, a x i s}$ is given by equation (1), $b$ is the beam radius, $I_{0}$ and $I_{1}$ are the modified Bessel functions, and $\gamma_{1}$ is the radial propagation constant for the fundamental space harmonic

$$
\begin{equation*}
\gamma_{0}=\sqrt{\beta_{0}^{2}-\frac{\omega^{2}}{c^{2}}} \tag{5}
\end{equation*}
$$

## Results

## Baseline TunneLadder Circuit

When first modeled with the exact dimensions from reference 9 , the symmetric ladder mode resonance at phase $\beta L=\pi$ occurred at 29.5 GHz , which is 6.35 percent under the experimental value of 31.5 GHz . By decreasing the thickness of the ladder between the beam hole and dielectric support by only 0.031 mm , with a simultaneous increase in the height of the dielectric chip from 0.254 to 0.285 mm (the shaded grid cells in figure 5 were replaced with dielectric), the calculated resonance frequency matched the experimental value. This change in ladder thickness can be justified because of the nature of the TunneLadder construction. When the Type IIA diamond chips are brazed onto the soft Amzirc ladder, they are very likely partially driven into the metal, decreasing the ladder thickness. To obtain a dispersion curve, resonant frequencies were obtained at phases of $0, \pi / 4, \pi / 2$, and $3 \pi / 4$ in addition to that at $\pi$ by using the cavity configurations and boundary conditions given in table II. The Micro-SOS input file used to obtain the resonant frequency at a phase of $\pi / 2$ is given in appendix $A$, and the input file used to obtain the resonant frequencies at phases $\pi / 4$ and $3 \pi / 4$ is given in appendix $B$.

In addition to calculating the resonant frequencies, MicroSOS can plot the electric field at any specified location using the VECTOR command. For example, the electric field pattern for the symmetric ladder mode at the $\pi / 4$ resonance point
is shown in figure 7(a) for an $x_{1}-x_{3}$ cross-section on the axis, and in figure 7 (b) for an $x_{1}-x_{2}$ cross-section through the center of a gap.

The dispersion curve for the symmetric ladder mode is obtained by plotting the calculated resonance points of table III (case 1) in figure 8. As shown, the agreement with the experimental results obtained from cold-test measurements (ref. 9) is very high, demonstrating the accuracy of the Micro-SOS simulation.

After the dispersion curve has been obtained, the beam interaction impedance can be calculated from equation (1). Table IV gives the parameters obtained from Micro-SOS that were used to calculate the impedance for three different values of phase. Figure 9 (case 1) shows that the impedance decreases with an increasing phase shift per cavity. There were no experimental data to compare the impedance values with, but the formulation for calculating the impedance has been verified with calculated results compared with data from a ferruleless coupled-cavity TWT circuit (ref. 18).

## Dielectric Rod Circuit

If the TunneLadder circuit is to be used at higher frequencies, the decrease in size would make accurate positioning of the dielectric chips extremely difficult. Fabrication would be much easier if the chips were replaced by two continuous dielectric rods. However, such an increase in the dielectric loading of a slow-wave circuit increases the capacitance, with expected deleterious consequences of decreased phase velocity (decreased frequency at a given phase) and impedance (ref. 12, pp. 43 to 45 ).

The Micro-SOS calculations shown in table III and figure 8 (case 2) confirm that the increased dielectric loading decreases the phase velocity, with the frequency decrease ranging from $1.02 \mathrm{GHz}(6.33$ percent) at a phase of zero to 3.07 GHz ( 9.75 percent) at a phase of $\pi$ rad. However, contrary to our expectations, the impedance calculated in table IV and shown in figure 9 (case 2) actually increased, rising 16.9 percent from 121.4 to $141.9 \Omega$ at a phase of $\pi / 2$ rad. The impedance increase can be explained by the added dielectric decreasing the frequency more at larger values of phase than at smaller values. This causes a flattening of the

TABLE III. - FREQUENCY-PHASE DISPERSION CALCULATIONS

| Casc | Dielectric | Side width, mm | Phase, rad |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 0 | $\frac{\pi}{4}$ | $\frac{\pi}{2}$ | $\frac{3 \pi}{4}$ | $\pi$ |
|  |  |  | Frequency, GHz |  |  |  |  |
| 1 | Chips | 0.8890 | 16.12 | 26.91 | 30.33 | 31.27 | . 31.50 |
| 2 | Rods | . 8890 | 15.10 | 24.73 | 27.54 | 28.26 | 28.4 .3 |
| 3 | Rods | . 6595 | 17.108 | 27.28 | 30.46 | 31.30 | 31.51 |



Figure 7.-Calculated electric field in symmetric ladder mode of TunneLadder circuit at a phase of $\pi / 4$.
dispersion curve (fig. 8) with resulting decreases in the group velocity and bandwidth. The group velocity, which is inversely proportional to the impedance, decreased 23.7 percent, whereas $E_{z 0}^{2} N L / W_{T O T}$, which is proportional to the impedance, decreased only 10.8 percent. Thus, there was a net increase in impedance.

To more accurately assess the effects of replacing the dielectric support chips with rods, circuits were compared at approximately equal operating frequencies by altering the


Figure 8.-Dispersion relationship for symmetric ladder mode of TunneLadder circuit.


Figure 9.-Calculated beam interaction impedances for TunneLadder circuits.
waveguide geometry of the TunneLadder circuit. As a guideline to altering the dimensions, an approximate relationship for the cutoff frequency of a double-ridge waveguide (ref. 19, p. 470),

TABLEIV. - BEAM INTERACTION IMPEDANCE

| Case | Parameter | Phase, rad |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\frac{\pi}{4}$ | $\frac{\pi}{2}$ | $\frac{3 \pi}{4}$ |
| 1 | Frequency, GHz $E_{z 1}^{2} N L / W_{T O 7}\left(10^{6} V^{2} / J m\right)$ Group velocity ( $10^{6} \mathrm{~m} / \mathrm{s}$ ) Impedance, $\Omega$ | $\begin{gathered} 27.10 \\ 3.522 \\ 15.56 \\ 184.8 \end{gathered}$ | $\begin{gathered} 30.59 \\ 2.418 \\ 4.066 \\ 121.4 \end{gathered}$ | $\begin{gathered} .31 .38 \\ .8477 \\ 1.282 \\ 60.01 \end{gathered}$ |
| 2 | Frequency, GHz $E_{2}^{2} N L / W_{T O T}\left(10^{\mathrm{n}} V^{2} / I m\right)$ <br> Group velocity ( $10^{6} \mathrm{~m} / \mathrm{s}$ ) <br> Impedance, $\Omega$ | $\begin{gathered} 24.82 \\ 3.193 \\ 1.3 .36 \\ 195.2 \end{gathered}$ | $\begin{gathered} 27.69 \\ 2.156 \\ 3.101 \\ 141.9 \end{gathered}$ | $\begin{gathered} 28.32 \\ .760 \\ .992 \\ 69.6 \end{gathered}$ |
| 3 | Frequency, GHz <br> $E_{z i 1}^{2} N L / W_{T m}\left(10^{n} V^{2} / I m\right)$ <br> Group velocity ( $\left.100^{\prime \prime} m / s\right)$ <br> Impedance, $\Omega$ a | $\begin{gathered} 27.41 \\ 3.294 \\ 14.59 \\ 184.4 \end{gathered}$ | $\begin{gathered} 30.64 \\ 2.259 \\ 3.699 \\ 124.7 \end{gathered}$ | $\begin{gathered} .31 .41 \\ .794 \\ 1.137 \\ 6.3 .4 \end{gathered}$ |

$$
\begin{equation*}
f_{c}=\frac{1}{2 \pi}\left(\frac{2 g}{\mu \varepsilon w s d}\right)^{1} \tag{6}
\end{equation*}
$$

was used, where $\mu$ is the permeability, $\varepsilon$ is the permittivity, and $g, w, s$, and $d$ are waveguide dimensions shown in figure 3. To increase the frequency, we chose to alter the side section width $w$. As shown in figure 8 and table III, a dielectric rod circuit with $w$ decreased by 25.8 percent (case 3) had a dispersion curve very similar to that of the original dielectric chip circuit (case 1). The calculated beam interaction impedance is also very similar as shown in figure 9 and table IV. Thus, a dielectric rod circuit with decreased side section width was shown to be very similar to a dielectric chip circuit with respect to dispersion and impedance.

## Conclusions

The usefulness of the electromagnetic circuit analysis computer code Micro-SOS in reducing the need for expensive and time-consuming experimental cold-testing in the design process for traveling-wave tube circuits was demonstrated. The code was used to calculate the frequency-phase dispersion characteristics and beam interaction impedance of a TunneLadder traveling-wave tube slow-wave structure. After making minor, justifiable adjustments in the dimensions of the ladder, computational results agreed very closely with experimental data.

While the TunneLadder TWT simulated in this study operated at a frequency of 29 GHz , this type of circuit is being considered for future use at higher frequencies. Because of the smaller circuit dimensions at higher frequencies, posi-
tioning of the dielectric chip ladder supports as used in the $29-\mathrm{GHz}$ circuit would be extremely difficult. Thus, simulations were made with the chips replaced by a pair of rods that are much easier to position accurately. Because of the increased dielectric loading of the rods, frequency, the ordinate of the dispersion curve, was decreased. However, one can compensate for this decrease in frequency by decreasing the side section widths. Thus, a modified TunneLadder circuit with decreased side section widths and a ladder supported by continuous dielectric rods could have approximately the same gain and efficiency but with a smaller bandwidth than the original circuit supported with dielectric chips.

## Lcwis Research Center

National Aeronautics and Space Administration
Cleveland, Ohio, September 28, 1992

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## Appendix A <br> Input File for $\pi / 2$ Phase

```
TITLE * TUNNELADER CIRCUIT, 1 CAV, 1 SYMMETRY * /
COMMENT * THE GRID SPACING IS IDENTIFIED THROUGH THE X1GRID, X2GRID, AND
    X3GRID COMMANDS. SINCE THE SPACING IS NOT UNIFORM, FUNCTION IS
    USED IN THE COMMAND. THE CELLS ARE LARGE IN THE AREAS OF LITTLE
    SIGNIFICANCE AND VERY FINE IN THE AREAS WHERE THE ELECTRIC FIELDS
    ARE STRONG. */
XIGRID FUNCTION 38 1 .00 5 .0001778 .000889
    3.000153 . 000459
    2.00003175 .0000635
    4.0000325 . 00013
    2.00005475 .0001095
    5.0000762 . 000381
    2.00005475 .0001095
    4.0000325 . }0001
    2.00003175 .0000635
    3.000153 .000459
    5 .0001778 .000889 /
X2GRID FUNCTION 40 1 0.00 5 .0002032 .001016
    2.0001143 .0002286
    1.0000254 . 0000254
    2.00003175 . 0000635
    8 .0000301625 .0002413
    3.00004233 . 000127
    8 .0000301625 . 0002413
    2.00003175 .0000635
    1.0000254 .0000254
    2.0001143 .0002286
    5 .0002032 .001016/
COMMENT * THE FULL LENGTH OF X3 IS .0003175 m * /
X3GRID FUNCTION 9 1 0.00 1 .0000762 .0000762
    1.0000254 .0000254
    4.00002857 .0001143
1.0000254 .0000254
1.0000762 .0000762 /
```

```
COMMENT * THE SYMMETRY COMMAND CREATES A "MAGNETIC" WALL AT THE BOUNDARY.
    BY EDITING THIS SECTION, THE PI, PI/2, AND 0 PHASE SHIFTS ARE
    OBTAINED. * /
SYMMETRY MIRROR +1 \(13814011 /\)
C SYMMETRY MIRROR -113814099/
```

```
COMMENT * THE ENTIRE GRID SPACE IS BLOCKED AS WELL AS ONE CELL LAYER
    ON EACH SURROUNDING WALL. THIS CREATES A PERFECT CONDUCTOR
    AT EACH BOUNDARY. * /
STRUCTURE CONFORMAL BLOCK +1 0 39 0 41 0 10/
```

```
COMMENT * HOLLOW OUT THE DOUBLE RIDGE * /
STRUCTURE CONFORMAL LEFTLEG -1 1 6 1 40 1 9/f
STRUCTURE CONFORMAL RIGHTLEG -1 33 38 1 40 1 9//
STRUCTURE CONFORMAL CENTER -1 6 33 6 35 1 9 /
```

COMMENT * ADD THE DIELECTRIC IN THE CENTER OF THE STRUCTURE BENEATH THE BEAMHOLE * /
DIELECTRIC NO NULL $5.50 .00 .0172261013 /$
DIELECTRIC NO NULL 5.50 .00 .01722313513 /
DIELECTRIC NO NULL 5.50 .00 .0172261079 /
DIELECTRIC NO NULL $5.50 .00 .01722313579 /$

```
COMMENT *FORM THE BEAMHOLE APPROXIMATING IT AS AN ELLIPSE. THE ENTIRE
    beam is formed as a solid first and then hollowed to achieve the
    PROPER THICKNESS OF THE BEAM TUNNEL.* /
STRUCTURE ELLIPTICAL BEAMFILL +1 CARTESIAN . 0018453.00163830 .0
    .0018453 .0016383 .0003174
    100.00046175 .00033655
    100.00046175 . 00033655
    03600360 /
```

STRUCTURE ELLIPTICAL BEAMHOLE -1 CARTESIAN .0018453 .0016383 0.0
.0018453 . 0016383.0003174
100.00043 . 0003048
100.00043 .0003048
$03600360 /$
STRUCTURE ELLIPTICAL SLOT1 -1 CARTESIAN . 0018453.0016383 .0000762
.0018453 .0016383 .0002413
100.00046175 .00033655
100.00046175 . 00033655
03600360 /
COMMENT * FORM THE LADDER * /
STRUCTURE CONFORMAL LADDERLEFT +1 $01010192219 /$
STRUCTURE CONFORMAL LADDERRIGHT +1 $29 \begin{array}{lllll}39 & 19 & 22 & 1 & 9\end{array}$
STRUCTURE CONFORMAL SLOT2 -1 $110192228 /$


COMMENT * ONE RESONANT FREQUENCY IS REQUESTED. THE MAXIMUM FREQUENCY, IN THIS COMMAND SET TO 35 GHZ , SHOULD BE APPROXIMATELY 10\% ABOVE THE EXPECTED MAXIMUM FREQUENCY. * /
FREQUENCY $135 \mathrm{E}+9.00550000 /$ DIAGNOSE FREQUENCY 101 /

COMMENT * THE BALANCE AND OBSERVE COMMANDS ARE USED TOGETHER TO CALCIULATE THE TOTAL ENERGY IN THE MODELED STRUCTURE. THIS VALUE OF ENERGY IS USED IN THE IMPEDANCE CALCULATIONS. *
BALANCE $113814019 /$
OBSERVE 1 YES ENERGY 10.00 .00 .00 .0 TOTAL $01 /$

COMMENT * THE LINPRINT COMMAND PRINTS OUT THE VALUES OF THE FIELD IN THE SPECIFIED REGION. THIS COMMAND WILL PRINT OUT THE AXIAL ELECTRIC field at the center of the beamhole. * /
LINPRINT 132119192020190010000001

COMMENT * THE RANGE COMMAND PLOTS THE FIELD VALUES THAT THE LINPRINT COMMAND PRINTS OUT. THE AXIAL ELECTRIC FIELD IS PLOTTED IN THIS COMMAND. THIS PLOT IS FOURIER ANALYZED TO OBTAIN THE EFFECTIVE FIELD SEEN BY THE BEAM AND USED TO CALCULATE THE PIERCE INTERACTION IMPEDANCE. * /
RANGE $1 \begin{array}{llllllllll}1 & 0 & 0 & 3 & 19 & 19 & 20 & 1 & 9 /\end{array}$

COMMENT * THE VECTOR COMMAND PLOTS THE RF FIELDS IN THE 2-DIMENSIONAL AREA SPECIFIED. * /
COMMENT * ELECTRIC FIELD IN THE X-Y PLANE THROUGH THE LADDER * / VECTOR 1111 E X1 X2 0.0 . 003683 0.0 .003277 . 0002413 .0002413 1515 /

COMMENT * X-Y PLANE THROUGH THE SLOT * /
VECTOR 11111 E X1 X2 0.0.003683 0.0.003277 . 0001587 . $00015871515 /$
COMmENT * $Y$-Z plane through the Ridge * /
VECTOR 1111 E X2 X3 .0005334 .0005334 0.0.003277 0.0.0003175 $1515 /$
COMMENT * TOP VIEW THROUGH THE CENTER * /
VECTOR 1111 EX X1 0.0 . 003683.001638 .0016380 .0 . $00031751515 /$
COMMENT * TOP VIEW THROUGH A DIELECTRIC * /
VECTOR 11111 EX X1 0.0.003683.0021461 . 0014610.0 . $00031751515 /$

START /
STOP /

## Appendix B

Input File for $\pi / 4$ and $3 \pi / 4$ Phases

```
TITLE *TUNNELADDER CIRCUIT, 2 CAV, 1 SYMMETRY * /
XIGRID FUNCTION 38 1 .00 5 .0001778 .000889
    3.000153.000459
    2.00003175 .0000635
    4.0000325 .00013
    2.00005475 .0001095
    5 .0000762 . 000381
    2.00005475 .0001095
    4.0000325 . 00013
    2.00003175 .0000635
    3.000153.000459
    5.0001778 .000889 /
XZGRID FUNCTION 40 1 0.00 5 .0002032 .001016
2.0001143 .0002286
1.0000254 . 0000254
2.00003175 .0000635
8.0000301625 .0002413
3.00004233 .000127
8.0000301625 .0002413
2.00003175 .0000635
1.0000254 .0000254
2.0001143.0002286
5.0002032 .001016 /
COMMENT * THE FULL LENGTH OF X3 IS . 000635 m * /
X3GRID FUNCTION 17 1 0.00 1 .0000762 .0000762
    1.0000254 .0000254
    4.000028575 .0001143
    1.0000254 .0000254
    2.0000762.0001524
    1.0000254 .0000254
    4.000028575 .0001143
    1.0000254 .0000254
    1.0000762 .0000762
STRUCTURE CONFORMAL BLOCK +1 0 39 0 41 0 18/
STRUCTURE CONFORMAL LEFTLEG -1 1 6 1 40 1 17/
STRUCTURE CONFORMAL RIGHTLEG -1 33 38 1 40 1 17/
STRUCTURE CONFORMAL CENTER -1 6 33 6 35 1 17/
CQMMENT * ADD THE DIELECTRIC IN THE CENTER OF THE STRUCTURE * /
COMMENT * BENEATH THE SLOT * /
DIELECTRIC NO NULL 5.5 0.0 0.0 17 22 6 10 1 3 /
```



```
DIELECTRIC NO NULL 5.5 0.0 0.0 17 22 6 10711/
DIELECTRIC NO NULL 5.5 0.0}0.
```

DIELECTRIC NO NULL $\begin{array}{llllllllll}5.5 & 0.0 & 0.0 & 17 & 22 & 6 & 10 & 15 & 17\end{array}$ DIELECTRIC NO NULL $5.50 .0 \quad 0.0 \quad 17 \quad 2231 \quad 351517 /$

COMMENT *FORM THE BEAMHOLE * /
STRUCTURE ELLIPTICAL BEAMFILL +1 CARTESIAN . 0018453 . 00163830.0 .0018453 . 0016383.000635 100.00046175 . 00033655 100.00046175 .00033655 03600360 /

STRUCTURE ELLIPTICAL BEAMHOLE -1 CARTESIAN . 0018453 . 00163830.0
.0018453 . 0016383.000635
100.00043 .0003048
100.00043 . 0003048

03600360 /
STRUCTURE ELLIPTICAL SLOT1 -1 CARTESIAN . 0018453 . 0016383 . 0000762
.0018453 .0016383 .0002413
100.00046175 .00033655
100.00046175 . 00033655

03600360 /
STRUCTURE ELLIPTICAL SLOT2 -1 CARTESIAN . 0018453 . 0016383 . 0003937
.0018453 .0016383 .0005588
100.00046175 .00033655
100.00046175 .00033655
$03600360 /$
COMMENT * FORM THE LADDER * /
STRUCTURE CONFORMAL LADDERLEFT +1 $0 \begin{array}{lllllll}10 & 19 & 22 & 1 & 17\end{array}$
STRUCTURE CONFORMAL LADDERRIGHT +1 $29 \begin{array}{llllll}39 & 19 & 22 & 1 & 17\end{array}$
STRUCTURE CONFORMAL SLOT3 -1 $110192228 /$
STRUCTURE CONFORMAL SLOT5 $-129381922 \quad 28 /$
STRUCTURE CONFORMAL SLOT7 -1 $111019221016 /$
STRUCTURE CONFORMAL SLOT9 $-1293819 \quad 221016$ /

SYMMETRY MIRROR +1 $138144011 /$

FREQUENCY 2 35E+9.005 50000 /
BALANCE 1138140117 /
OBSERVE 1 YES ENERGY 10.00 .00 .00 .0 TOTAL $01 /$
LINPRINT $13 \begin{array}{llllllllllllll}19 & 19 & 19 & 20 & 17 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0\end{array}$
RANGE $\begin{array}{lllllllllll}1 & 1 & 0 & 0 & 3 & 19 & 19 & 20 & 20 & 1 & 17\end{array}$
START /
STOP /


