https://ntrs.nasa.gov/search.jsp?R=19930081835 2020-06-17T22:48:58+00:00Z



NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

	TECHNICAL	NOTE NO.	1158	- 		
FLUTTER AND	OSCILLATING	AIR-FORCE	CALCULATI	ONS FOR	AN	•
AIRFOIL	IN A TWO-DIM	ENSIONAL	SUPERSONIC	FLOW		·
В у	I. E. Garri	ck and S.	I. Rubinov	v		

SUMMARY

A connected account is given of the Possic theory of nonstationary flow for small disturbances in a twodimensional supersonic flow and of its application to the determination of the aerodynamic forces on an oscillating airfoil. Further application is made to the problem of wing fluttor in the degrees of freedom - torsion, bending, and aileron torsion. Numerical tables for flutter calculations are provided for various values of the Mach number greater than unity. Results for bendingtorsion wing flutter are shown in figures and discussed. The static instabilities of divergence and alleron reversal are examined as is a one-degree-of-freedom case of torsional oscillatory instability.

INTRODUCTION

The problem of flutter or aerodynamic instability for high-speed aircraft is of considerable importance and hence interest is directed to the aerodynamic problem of the oscillating airfoil moving forward at high speed. Although for conventional aircraft the subsonic and the near-sonic or transonic speed ranges are still of main interest, the purely supersonic speed range is becoming increasingly significant.

A theoretical treatment of the oscillating airfoil, of infinite aspect ratio, moving at supersonic speed has been given by Possio (reference 1). This treatment is based on the theory of small perturbations to the main stream, thus is essentially an acoustic theory, and leads to linearization of the equation satisfied by the velocity potential. The airfoil is therefore assumed to be very thin, at small angle of attack, and the flow is assumed nonviscous, unseparated, and free from strong shocks.

The small-disturbance linearized theory, being much less complicated than a more rigorous nonlinear theory, is to be regarded as an expedient which allows an initial theoretical solution. The theory permits the occurrence of weak (infinitesimally small) shocks and thus the basic trends and effects of the parameters of the simplified problem can be indicated. The theory reduces to that of Ackeret in the stationary (static) case and, like it, is not expected to be valid too near M = 1. In view of the restrictions and assumptions in the analysis important modifications may be required in certain cases for thick finite airfoils, but even here the simple theory for thin wing sections may serve as a basis.

In addition to Possio's brief work an equivalent extended treatment has been given by Borbely (reference 2) which utilizes contour integrations to carry out the solution of the partial differential equation for the velocity potential according to the Heaviside operator method or Laplace transform method. Recently, another equivalent treatment has been given in England by Temple and Jahn employing the method of characteristics. In reference 1 a few curves are given for the aerodynamic coefficients but no numerical values are tabulated. Reference 2 contains no numerical results. Temple and Jahn recognize the lack of numerical results and supply some initial calculations for the functions necessary for flutter calculations.

A paper has recently appeared by Schwarz (roference 3) devoted to computing and tabulating the key mathematical functions that arise in the theory. Tho present paper makes use of reference 3 to supply more extensive numerical tables for application of the theory. The formulas of the theory are recast in more familiar form for application to the flutter problem and a series of calculations on bonding torsion flutter are carried The performance of similar calculaout and discussed. tions for wing-aileron flutter is indicated. Brief discussions also are given of the static instabilities, divergence and alleron reversal, and of a one-degree-offreedom torsional oscillatory instability.

For completeness, a connected account of the Possio theory is presented since the original presentation in Italian is quite terse and also since it is believed that this treatment is the simplest and most suitable for general extensions. The extension of its application to include the aileron is given.

AIR FORCES AND MOMENTS ON AN OSCILLATING AIRFOIL MOVING

AT SUPERSONIC SPEED IN TWO-DIMENSIONAL FLOW

Differential Equation for the Velocity Potential

The differential equation satisfied by the velocity potential in fixed coordinates in the case of infinitesimal disturbances is the wave equation

$$\frac{1}{e^2} \frac{\partial^2 \not{a}}{\partial t^2} = \nabla^2 \not{a}$$
 (

where c is the velocity of sound in the undisturbed madium. (For the adiabatic equation of state $c^2 = \frac{dp}{d\rho} = \gamma \frac{p}{\rho}$.)

Referred to a system of rectangular coordinates moving forward at a constant supersonic speed v in the negative x-direction the wave equation satisfied by the velocity potential in two-dimensional flow becomes

 $\frac{1}{c^2}\frac{\partial^2 \alpha}{\partial t^2} + \frac{2v}{c^2}\frac{\partial^2 \alpha}{\partial x \partial t} + \left[\left(\frac{v}{c}\right)^2 - 1\right]\frac{\partial^2 \alpha}{\partial x^2} - \frac{\partial^2 \alpha}{\partial y^2} = 0 \qquad (2)$

It is proposed to treat the effect of a slightly cambered thin airfoil moving forward at a supersonic speed v at small (zero) angle of attack as that of a distribution of small disturbances placed along the x-axis and hence to utilize equation (2). The velocity components in the x- and y-directions relative to the moving airfoil are, respectively,

3

1)

and

which may be considered the additional components to the main stream due to the disturbance created by the presence of the airfoil. Relative to coordinates fixed in space the velocity components are $v + v_x$ and v_v .

 $v_x = \frac{\partial \emptyset}{\partial x}$

 $v_y = \frac{\partial y}{\partial y}$

Effect of a Source

Equation (2) is linear and solutions are therefore additive. An important particular solution of equation (2) having the property of a source pulse is

$$\phi_{0} = \frac{A(\xi, \eta, T)}{\sqrt{c^{2}(t - T)^{2} - [x - \xi - v(t - T)]^{2} - (y - \eta)^{2}}}$$
(3)

This solution may be considered to give the effect at a point (x, y) at time t of a disturbance of magnitude A originating at a point (ξ, η) at an earlier time T. The potential \emptyset_0 is thus a retarded potential and the elapsed time at (x, y) since the creation of the disturbance is $\tau = t - T$.

Unlike the situation for a subsonic flow, for a supersonic flow the effect of the disturbance is propagated only downstream, that is, the point being influenced (x, y) is always considered to be aft of the point of disturbance (ξ, η) . Equation (3) is thus valid in the angular region with vertex at (ξ, η) and bounded by two straight lines making the Mach angles $\pm \mu = \pm \sin^{-1}\frac{0}{v} = \pm \sin^{-1}\frac{1}{M}$ with respect to the x-axis. (See fig. 1.) Upstream from this angular region the value of \emptyset_0 is zero. It follows also that disturbances in the wake need not be considered and the solution to

11

the boundary problem may be attempted by a distribution of potentials of the type \emptyset_0 taken along the projection of the airfoil on the x-axis.

A disturbance at (ξ, η) created at time T is first felt at a point (x, y) after a certain time T_1 has elapsed. The point (x, y) penetrates the wave front of the disturbed region and because it is moving at a speed greater than that of the wave front it emerges from the disturbed region at a later time T_2 . Thus, the duration of this initial disturbance at (x, y) is $T_2 - T_1$. (See fig. 2.) The transition at (x, y) from a region of quiescence to a region of disturbance and vice versa is associated with the vanishing of the denominator in equation (3). The values of T_1 and T_2 for a disturbance created on the axis $\eta = 0$ are thus given by

$$\tau_{1,2} = \frac{M(x-\xi) \mp \sqrt{(x-\xi)^2 - y^2(M^2 - 1)}}{c(M^2 - 1)} \quad (1)$$

where the minus sign is associated with T_1 and the plus sign with T_2 and where $M = \frac{v}{c}$. It may also be observed that a negative quantity under the radical sign in equation (3) is to be interpreted as associated with an undisturbed region (that is, with $\emptyset = 0$).

Potential for a Distribution of Sources

The total effect at any point (x, y) is the sum of the effects of disturbances originating between the leading edge $\xi = 0$ and the intersection of the <u>Mach</u> line through (x, y) with the ξ -axis

$$\tilde{s} = \tilde{s}_1 = x - y\sqrt{M^2 - 1}$$

(since only disturbances created forward of the Mach angle region can affect (x, y); see fig. 3).

5.

-5-

I

The total potential at (x, y) at any time t is thus given by

$$\mathscr{J}(x, y, t) = \int_{0}^{1S_{1}} \int_{\tau_{1}}^{\tau_{2}} \frac{A(\xi, 0, t - \tau)}{\sqrt{c^{2}\tau^{2} - (x - \xi - v\tau)^{2} - y^{2}}} d\tau d\xi$$

$$= \frac{1}{\sqrt{v^2 - c^2}} \int_{0}^{\tilde{S}_{1}} \int_{\tau_{1}}^{\tau_{2}} \frac{A(\xi, 0, t - \tau)}{\sqrt{(\tau - \tau_{1})(\tau_{2} - \tau)}} d\tau d\xi$$
(5)

Boundary Condition and Strength of Distribution

The function $A(\xi, 0, t - \tau)$ giving the magnitude of the source distribution is now to be determined by the usual boundary condition of tangential flow along the airfoil. If the ordinate of any point of the mean line defining the airfoil is given as $y = y_m(x, t)$ the boundary condition may be written

$$\left(\frac{\partial p}{\partial y}\right)_{y=0} = w(x, t) = \frac{\partial y}{\partial t}$$
$$= v \frac{\partial y_m}{\partial x} + \frac{\partial y_m}{\partial t}$$
(6)

where w(x, t) thus represents the vertical velocity induced by the source distribution in order to realize tangential flow at the airfoil boundary. (In the stationary case - Ackeret treatment - the two surfaces of the airfoil may be considered as acting independently, which can also be done for the nonstationary case. However, for the purpose of obtaining the oscillating forces in the linear treatment it is sufficient to consider separately the upper and lower sides of only the mean line.)

6

The evaluation of $\frac{\partial \emptyset}{\partial y}$ as y approaches zero may be readily obtained by use of the variable θ instead of τ where $2\tau = (\tau_2 - \tau_1) \cos \theta + \tau_2 + \tau_1$. This substitution in equation (5) yields

$$\emptyset = \frac{1}{\sqrt{v^2 - c^2}} \int_{0}^{t} \int_{0}^{t} A(\xi, 0, t - \frac{\tau_2 + \tau_1}{2} - \frac{\tau_2 - \tau_1}{2} \cos \theta) d\theta d\xi$$

By differentiation with regard to y and with the aid of an integration by parts

$$\frac{\partial \emptyset}{\partial y} = \frac{1}{\sqrt{v^2 - c^2}} \frac{\partial \xi_1}{\partial y} \pi A \left(\xi_1, 0, t - \frac{My}{c\sqrt{M^2 - 1}} \right)$$
$$+ \frac{1}{\sqrt{v^2 - c^2}} \frac{y}{c\sqrt{M^2 - 1}} \int_0^{\sqrt{s}} \int_0^{\pi} \frac{\partial^2 A}{\partial t^2} \sin^2 \theta \ d\theta \ d\xi$$

Since $\xi_1 = x - y \sqrt{M^2 - 1}$, there results in the limit as y approaches zero on the positive side, the important relation

$$\left(\frac{\partial \emptyset}{\partial y}\right)_{y=+0} = -\frac{\pi}{c} A(x, 0, t)$$

or, briefly,

$$A(x, t) = -\frac{c}{\pi} w(x, t)$$
 (7)

For y approaching 0 on the negative side an equal and opposite result is obtained and hence the distribution of singularities to be utilized to replace the airfoil is of the source-sink type. Thus \emptyset is to be understood in the subsequent analysis to be prefixed

. . . .

1. **1**1

by a [±] sign, + for the upper side and - for the lower side.

The total potential for y = 0 may now be expressed by means of equations (5) and (7) as

where, from equation (4) with y = 0,

$$\tau_1 = \frac{x - \xi}{c} \frac{1}{M + 1}$$

and

$$r_2 = \frac{x - \xi}{c} \frac{1}{M - 1}$$

Application to Oscillating Airfoil

The general result given by equation (8) may now be applied for definiteness to the case of an airfoil performing small sinusoidal oscillations in several degrees of freedom. Let the wing undergo the following motions: a motion due to displacement h (velocity h) in a vertical direction; a torsional motion consisting of a turning about $x = x_0$ with instantaneous angle of attack α ; a rotation of an aileron about its hinge at $x = x_1$ with instantaneous aileron angle β measured with respect to α . (See fig. 1.)

In accordance with equation (6) the vertical velocity at any point x of the airfoil situated at $0 \le x \le 2b$ (of chord 2b and leading edge at x = 0) is easily recognized to be

$$w(x, t) = -[\dot{h} + v\alpha + (x - x_0)\dot{\alpha} + v\beta + (x - x_1)\dot{\beta}]$$
 (9)

where the β -terms are to be interpreted as zero for $x < x_1$ (and where the minus sign is introduced because

the vertical velocity w is positive upwards whereas the terms within the brackets are positive downwards).

It is convenient in treating sinusoidal motion to utilize the complex notation

$$\begin{array}{c} h = h_{D}e^{i\omega t} \\ \alpha = \alpha_{O}e^{i\omega t} \\ \beta = \beta_{O}e^{i\omega t} \end{array}$$
 (10)

where $h_0,\ \alpha_0,\ \text{and}\ \beta_0$ are complex amplitudes and hence include phase angles.

Since the further analysis is concerned only with exponential time variations of the type given in equation (10), the function $w(\xi, t - \tau)$ occurring in equation (8) is of the form $w(\xi)e^{i\omega(t-\tau)}$, which may also be written for convenience as $w(\xi, t)e^{-i\omega\tau}$. The potential \emptyset given by equation (8) may now be written as

$$\emptyset(x, t) = -\frac{1}{\sqrt{M^2 - 1}} \int_{0}^{\infty} w(\xi, t) I(\xi, x) d\xi \quad (11)$$

where

$$I(\xi, x) = \frac{1}{\pi} \int_{\tau_1}^{\tau_2} \frac{e^{-i\omega\tau}}{\sqrt{(\tau - \tau_1)(\tau_2 - \tau)}} d\tau$$

The integration with regard to τ may be readily performed by substitution of the variable θ where $2\tau = (\tau_2 - \tau_1) \cos \theta + \tau_2 + \tau_1$. Then

_

With τ_1 and τ_2 replaced by their values as given for equation (8) and with the aid of the Bessel function relation

$$\frac{1}{m} \int_{0}^{m} e^{-i\lambda\cos\theta} d\theta = J_{0}(\lambda)$$

it is recognized that

$$I(\xi, x) = e^{-i\omega \frac{x-\xi}{c}} \frac{M}{M^{2}-1} J_{0}\left(\frac{x-\xi}{c} \frac{\omega}{M^{2}-1}\right)$$
(12)

Throughout the subsequent analysis it is convenient to employ the variables x and ξ in a new sense to mean nondimensional quantities obtained by dividing the old variables by the chord 2b. The retaining of the symbols x and ξ for the nondimensional variables should lead to no confusion.

The potential \emptyset of equation (11) is then

where with the introduction of the important frequency parameters

$$k = \frac{\omega b}{v}$$
$$\overline{\omega} = \frac{2\pi N^2}{M^2 - 1}$$

the function I(E, x) becomes

$$I(\xi, x) = e^{-i\omega(x-\xi)} J_0\left[\frac{\omega}{M}(x-\xi)\right]$$
(12)

, , , ,

Thus, $I(\xi, x)$ is a function of the variable $x - \xi$ and of two parameters M and $\overline{\omega}$, or, alternatively, M and k.

It is desirable to express the potential \emptyset as the sum of the separate effects due to position and motion of the airfoil associated with the individual terms in equation (13). Thus

$$\emptyset(\mathbf{x}, \mathbf{t}) = \emptyset_{\alpha} + \emptyset_{\dot{\mathbf{h}}} + \emptyset_{\dot{\alpha}} + \emptyset_{\beta} + \emptyset_{\dot{\beta}}$$
(14)

where

$$\phi_{\alpha} = \frac{2b}{\sqrt{M^2 - 1}} v\alpha \int_{0}^{ix} I(\xi, x) d\xi$$

____11

- -----

_.....

: ___

....<u>.</u>

<u>ч</u>.

. ----

. =

. 🚠

· · · - ===

· -----

- FE

-2

-3

1.00

Forces and Moments

The basic pressure formula in the theory of small disturbances is

 $p = -\rho \frac{d\emptyset}{dt}$

which in the present case of the moving airfoil may be expressed as

$$p = -\rho \left(\frac{\partial \phi}{\partial t} + v \frac{\partial \phi}{\partial x} \right)$$

where ρ is the density in the unkisturbed medium. The local pressure difference on the airfoil surface between the upper and lower surfaces at any point x (nondimensional) is

$$p' = -2c \left(\frac{\partial \not a}{\partial t} + \frac{v}{2b} \frac{\partial \not a}{\partial x} \right)$$
(15)

The total force (positive downward) on the airfoil is

$$P = 2b \int_{0}^{1} p' dx$$
$$= -2\rho v \int_{0}^{1} \frac{\partial \emptyset}{\partial x} dx - 4\rho b \int_{0}^{1} \dot{\emptyset} dx \qquad (16)$$

The moment (positive clockwise; fig. 4) on the entire airfoil about any point x_0 is

$$M_{\alpha} = \mu b^{2} \int_{0}^{1} (x - x_{0}) p dx$$

= $-\mu \rho b v \int_{0}^{1} \frac{\partial \phi}{\partial x} (x - x_{0}) dx - 8\rho b^{2} \int_{0}^{1} \dot{\phi} (x - x_{0}) dx$ (17)

Similarly, the moment (positive clockwise; fig.), on the aileron about the hinge point x_1 is

$$M_{\beta} = l_{\mu} b^2 \int_{x_1}^{1} (x - x_1) p' dx$$

$$= -4\rho bv \int_{x_1}^{1} \frac{\partial \mathscr{D}}{\partial x} (x - x_1) dx - 8\rho b^2 \int_{x_1}^{1} \mathscr{D}(x - x_1) dx \quad (18)$$

· _

In the further reduction of equations (16) to (18), with the potential \emptyset replaced by its separated form given in equation (1/z), the following sets of integral evaluations are required:

$$\int_{0}^{11} \frac{\partial \mathscr{P}_{\alpha}}{\partial x} dx = \frac{2b}{\sqrt{h^{2} - 1}} \operatorname{var}_{1}(M, k)$$

$$\int_{0}^{11} \frac{\partial \dot{g}_{\dot{\alpha}}}{\partial x} dx = \frac{l_{\mu}b^2}{\sqrt{M^2 - 1}} \dot{\alpha} \left[r_2(M, k) - x_0 r_1(M, k) \right]$$

$$\int_{x_1}^{y_1} \frac{\partial \mathscr{G}_{\beta}}{\partial x} dx = \frac{2b}{\sqrt{M^2 - 1}} v\beta t_1(M, k, x_1)$$

$$\int_{x_1}^{1} \frac{\partial \not{\alpha}_{\beta}}{\partial x} dx = \frac{\mu b^2}{\sqrt{k^2 - 1}} \dot{\beta} t_2(x, k, x_1)$$

$$\int_{0}^{1} \phi_{\alpha} dx = \frac{2b}{\sqrt{M^{2} - 1}} var_{2}(M, k)$$

$$\int_{0}^{1} \phi_{\alpha} dx = \frac{\mu b^{2}}{\sqrt{M^{2} - 1}} \dot{a} \left[\frac{1}{2} r_{3}(M, k) - x_{0} r_{2}(M, k) \right]$$

.....

- _:

<u>. .</u>

. . . .

$$\int_{x_{1}}^{1} \phi_{\beta} dx = \frac{2b}{\sqrt{M^{2} - 1}} v\beta t_{2}(M, k, x_{1})$$
$$\int_{x_{1}}^{1} \phi_{\beta} dx = \frac{4b^{2}}{\sqrt{M^{2} - 1}} \dot{\beta} \frac{1}{2} t_{3}(M, k, x_{1})$$

$$\int_{0}^{1} \frac{\partial \alpha}{\partial x} x \, dx = \frac{2b}{\sqrt{M^{2} - 1}} \, v\alpha \, q_{1}(M, k)$$

$$\int_0^{\infty} \frac{\partial \mathscr{G}_{\dot{u}}}{\partial x} x \, dx = \frac{\mu b^2}{\sqrt{M^2 - 1}} \dot{\alpha} \left[\frac{1}{2} q_2(M, k) - x_0 q_1(M, k) \right]$$

$$\int_{x_{1}}^{1} \frac{\partial \mathscr{I}_{\beta}}{\partial x} x \, dx = \frac{2b}{\sqrt{M^{2}-1}} v \beta \left[s_{1}(M, k, x_{1}) + x_{1} t_{1}(M, k, x_{1}) \right]$$
$$\int_{x_{1}}^{1} \frac{\partial \mathscr{I}_{\beta}}{\partial x} x \, dx = \frac{4b^{2}}{\sqrt{M^{2}-1}} \beta \left[\frac{1}{2} s_{2}(M, k, x_{1}) + x_{1} t_{2}(M, k, x_{1}) \right]$$

$$\int_{0}^{1} \mathscr{A}_{\alpha} x \, dx = \frac{2b}{\sqrt{M^{2}-1}} \, v\alpha \, \frac{1}{2} \, q_{2}(M, k)$$

$$\int_{0}^{1} \mathscr{A}_{\alpha} x \, dx = \frac{4b^{2}}{\sqrt{L^{2}-1}} \, \dot{\alpha} \left[\frac{1}{6} \, q_{3}(M, k) - \frac{1}{2} \, x_{0} \, q_{2}(M, k) \right]$$

ļ

-

$$\int_{x_{1}}^{1} \beta_{\beta} x \, dx = \frac{2b}{\sqrt{M^{2} - 1}} \, v\beta \left[\frac{1}{2} \, s_{2} \left(M, \ k, \ x_{1} \right) + x_{1} \, t_{2} \left(M, \ k, \ x_{1} \right) \right]$$

$$\int_{x_{1}}^{1} \beta_{\beta} x \, dx = \frac{4b^{2}}{\sqrt{h^{2} - 1}} \, \beta \left[\frac{1}{6} \, s_{3} \left(M, \ k, \ x_{1} \right) + \frac{1}{2} \, x_{1} \, t_{3} \left(M, \ k, \ x_{1} \right) \right]$$

$$\int_{x_{1}}^{1} \frac{\delta \beta_{\alpha}}{\delta x} \left(x - x_{1} \right) \, dx = \frac{2b}{\sqrt{M^{2} - 1}} \, v\alpha \, p_{1} \left(M, \ k, \ x_{1} \right)$$

$$\int_{x_{1}}^{1} \frac{\delta \beta_{\alpha}}{\delta x} \left(x - x_{1} \right) \, dx = \frac{4b^{2}}{\sqrt{\mu^{2} - 1}} \, \alpha \, p_{1} \left(M, \ k, \ x_{1} \right) - x_{0} \, p_{1} \left(N, \ k, \ x_{1} \right)$$

$$\int_{x_{1}}^{1} \frac{\delta \beta_{\alpha}}{\delta x} \left(x - x_{1} \right) \, dx = \frac{4b^{2}}{\sqrt{\mu^{2} - 1}} \, \alpha \, \beta \, s_{1} \left(M, \ k, \ x_{1} \right)$$

$$\int_{x_{1}}^{1} \frac{\delta \beta_{\beta}}{\delta x} \left(x - x_{1} \right) \, dx = \frac{2b}{\sqrt{\mu^{2} - 1}} \, v\beta \, s_{1} \left(M, \ k, \ x_{1} \right)$$

15

-

Ċ

ŧ.

$$\int_{x_{1}}^{1} \mathscr{P}_{\alpha}(x - x_{1}) dx = \frac{2b}{\sqrt{M^{2} - 1}} v\alpha \frac{1}{2} p_{2}(M, k, x_{1})$$

$$\int_{x_{1}}^{1} \mathscr{P}_{\dot{\alpha}}(x - x_{1}) dx = \frac{hb^{2}}{\sqrt{M^{2} - 1}} \dot{\alpha} \left[\frac{1}{6} p_{3}(N, k, x_{1}) - \frac{1}{2}x_{0} p_{2}(N, k, x_{1})\right]$$

$$\int_{x_{1}}^{1} \mathscr{P}_{\beta}(x - x_{1}) dx = \frac{2b}{\sqrt{M^{2} - 1}} v\beta \frac{1}{2} s_{2}(M, k, x_{1})$$

$$\int_{x_{1}}^{1} \mathscr{P}_{\dot{\beta}}(x - x_{1}) dx = \frac{hb^{2}}{\sqrt{M^{2} - 1}} \dot{\beta} \frac{1}{6} s_{3}(M, k, x_{1})$$

;

The functions defined by the foregoing integral evaluations are further discussed in the following section; first, however, the force and moments (equations (16) to (18)) are given in their final forms as

$$P = -\frac{\mu_{0}b}{\sqrt{M^{2}-1}} \left[v \left(va + \dot{n} - 2bx_{0}\dot{a} \right) r_{1} + 2b \left(2v\dot{a} + \ddot{n} - 2bx_{0}\dot{a} \right) r_{2} + 4b^{2}\ddot{a} \frac{r_{3}}{2} + v^{2}\beta t_{1} + 4bv\dot{\beta} t_{2} + 4b^{2}\ddot{\beta} \frac{t_{3}}{2} \right]$$
(161)

$$M_{\alpha} = -\frac{\beta_{0}b^{2}}{\sqrt{M^{2}-1}} \left[v \left(va + \dot{n} - 2bx_{0}\dot{a} \right) q_{1} + 2b \left(2v\dot{a} + \ddot{n} - 2bx_{0}\ddot{a} \right) \frac{q_{2}}{2} + 4b^{2}\ddot{a} \frac{q_{3}}{6} + v^{2}\beta (s_{1} + z_{1}t_{1}) + 4bv\dot{\beta} \left(\frac{32}{2} + x_{1}t_{2} \right) \right]$$
+ $4b^{2}\ddot{a} \frac{q_{3}}{6} + x_{1} \frac{t_{3}}{2} \right] - 2bx_{0}P$ (171)

.

.

$$M_{p} = -\frac{6\rho b^{2}}{\sqrt{M^{2} - 1}} \left[v \left(v\alpha + \dot{h} - 2bx_{0}\dot{\alpha} \right) p_{1} + 2b \left(2v\dot{\alpha} + \ddot{h} - 2bx_{0}\ddot{\alpha} \right) \frac{p_{2}}{2} + 4b^{2}\ddot{\alpha} \frac{p_{3}}{6} + v^{2}\rho s_{1} + 4bv\dot{\beta} \frac{s_{2}}{2} + 4b^{2}\ddot{\beta} \frac{s_{3}}{6} \right]$$
(181)

Reduction and Evaluation of Foregoing Integrals

It is convenient to introduce the substitution $u = x - \xi$ and to express the function $I(\xi, x)$ (equation (12')) as

$$I(\xi, x) = I(u) = e^{-i\overline{\omega}u} J_0\left(\frac{\overline{\omega}}{M}u\right)$$
(19)

The various functions defined by the foregoing sets of integrals may now be expressed as follows:

$$r_{1}(M, k) = \int_{0}^{1} I(u) \, du$$

$$r_{2}(M, k) = \int_{0}^{1} \int_{0}^{x} I(u) \, du \, dx$$

$$r_{3}(M, k) = 2 \int_{0}^{1} \int_{0}^{x} (x - u) I(u) \, du \, dx$$

$$q_{1}(M, k) = \int_{0}^{1} u I(u) du$$

$$q_{2}(M, k) = 2\int_{0}^{1} \int_{0}^{1} x I(u) du dx$$

$$q_{3}(M, k) = 6\int_{0}^{1} \int_{0}^{1} x(x - u) I(u)$$

17

du dx

18
P_1(M, k, x_1) =
$$\int_{x_1}^{1} (u - x_1) I(u) du$$

P_2(M, k, x_1) = $2\int_{x_1}^{1} \int_{0}^{x} (x - x_1) I(u) du dx$
P_2(M, k, x_1) = $6\int_{x_1}^{1} \int_{0}^{x} (x - x_1)(x - u) I(u) du dx$
 $t_1(M, k, x_1) = \int_{0}^{1-x_1} I(u) du$
 $t_2(M, k, x_1) = \int_{0}^{1-x_1} \int_{0}^{x} I(u) du dx$
 $t_3(M, k, x_1) = 2\int_{0}^{1-x_1} \int_{0}^{x} (x - u) I(u) du dx$
 $s_1(M, k, x_1) = 2\int_{0}^{1-x_1} \int_{0}^{x} x I(u) du dx$
 $s_2(M, k, x_1) = 6\int_{0}^{1-x_1} \int_{0}^{x} x I(u) du dx$

.....

-**-**-

•

٠

······

. .___

Borbely (reference 2) has shown by means of reduction formulas that the six r- and q-functions may be obtained from a single integral. In a similar manner it may be indicated how the foregoing 15 functions may be obtained from the evaluation of the same integral. The reduction is accomplished in two stages. First, consider integrals of the following type:

$$f_{\lambda} = f_{\lambda}(M, \overline{\omega}) = \int_{0}^{1} I(u) u^{\lambda} du$$

$$g_{\lambda} = f_{\lambda}(M, \,\overline{\omega}x_{1}) = \frac{1}{x_{1}^{\lambda+1}} \int_{0}^{1} I(u) \, u^{\lambda} \, du \qquad \left\{ \begin{array}{c} (20) \\ \end{array} \right\}$$

$$h_{\lambda} = f_{\lambda} \left[M, \ \overline{\omega} \left(1 - x_{1} \right) \right] = \frac{1}{\left(1 - x_{1} \right)^{\lambda+1}} \int_{0}^{1-x_{1}} I(u) \ u^{\lambda} \ du$$

By integration by parts it can be readily verified that the following relations hold

$$r_{1} = f_{0}$$

$$r_{2} = f_{0} - f_{1}$$

$$r_{3} = f_{0} - 2f_{1} + f_{2}$$

$$q_{1} = f_{1}$$

$$q_{2} = f_{0} - f_{2}$$

$$q_{3} = 2f_{0} - 3f_{1} + f_{3}$$

.

•

....<u>ق</u>تيد. ا

÷

. ____ .

$$p_{1} = q_{1} - x_{1}r_{1} + x_{1}^{2}(g_{0} - g_{1})$$

$$p_{2} = q_{2} - 2x_{1}r_{2} + x_{1}^{3}(g_{0} - 2g_{1} + g_{2})$$

$$p_{3} = q_{3} - 3x_{1}r_{3} + x_{1}^{4}(g_{0} - 3g_{1} + 3g_{2} - g_{3})$$

$$t_{1} = (1 - x_{1})h_{0}$$

$$t_{2} = (1 - x_{1})^{2}(h_{0} - h_{1})$$

$$t_{3} = (1 - x_{1})^{3}(h_{0} - 2h_{1} + h_{2})$$

$$s_{1} = (1 - x_{1})^{2}h_{1}$$

$$s_{2} = (1 - x_{1})^{3}(h_{0} - h_{2})$$

$$s_{3} = (1 - x_{1})^{\frac{1}{2}}(2h_{0} - 3h_{1} + h_{3})$$

The final stage in the reduction of these functions is to utilize the following recursion formula (reference 2) obtained by integration by parts:

$$\frac{M^2 - 1}{M^2} \overline{\omega} f_{\lambda}(M, \overline{\omega}) = \left[1 + (1 - \lambda) \frac{1}{\overline{\omega}}\right] e^{-1\overline{\omega}} J_0\left(\frac{\overline{\omega}}{M}\right) - \frac{1}{M} e^{-1\overline{\omega}} J_1\left(\frac{\overline{\omega}}{M}\right) + 1(1 - 2\lambda) f_{\lambda-1}(M, \overline{\omega})$$

+
$$(1 - \lambda)^2 = \frac{1}{\omega} \mathbf{f}_{\lambda-2}(\mathbf{w}, \overline{\omega})$$
 (21)

.

where $\lambda \geq 1$ and f with a negative subscript is to be interpreted as zero.

The function $f_{\lambda}(M, \overline{\omega})$ may clearly refer also to the foregoing g- and h-functions, if $\overline{\omega}$ is replaced by the appropriate parameter; namely, $\overline{\omega}x_0$ for g_{λ} and $\overline{\omega}(1-x_0)$ for h_{λ} . (See equations (20).) The recursion relation (equation (21)) thus reduces the various functions to the single function

$$f_{0}(\mathbf{M}, \overline{\omega}) = \frac{1}{\omega} \int_{0}^{\overline{\omega}} e^{-i\mathbf{u}} J_{0}\left(\frac{\mathbf{u}}{\mathbf{M}}\right) d\mathbf{u}$$
(22)

which is therefore the only integral needed in the evaluation of the forces and moments.

The important integral in equation (22) has been recently made the subject of a mathematical investigation by Schwarz (reference i). Schwarz gives tables of the values of its real and imaginary parts to eight decimal places for $0 \le \overline{\omega} \le 5$ and for $1 \le M \le 10$ for conveniently small intervals. For values of $\overline{\omega} > 5$ not given in Schwarz' tables, the function f_0 may be evaluated by means of the following series development (reference 2):

$$f_{0}(M,\overline{\omega}) = e^{-i\overline{\omega}} \sum_{n=0}^{\infty} \left(\frac{M^{2}-1}{M^{2}} \overline{\omega} \right)^{n} \frac{1}{2^{n}n!(2n+1)} \left[\overline{J}_{n}(\overline{\omega}) + iJ_{n+1}(\overline{\omega}) \right] (23)$$

Table I gives values of the functions $f_{C}(M, \overline{\omega})$ based on the tables of Schwarz and on equation (23) for selected values of the Mach number $M = \frac{10}{9}, \frac{5}{4}, \frac{10}{7}, \frac{5}{3}, \frac{10}{2}, \frac{5}{7}, \frac{10}{7}, \frac{5}{3}, \frac{10}{2}, \frac{5}{2}, \frac{10}{3}, \frac{5}{3}, \frac{10}{5}, \frac{10}{5}, \frac{5}{3}, \frac{10}{5}, \frac{10$

EQUATIONS OF MOTION AND DETERMINANTAL EQUATION FOR

FLUTTER CONDITION

The equations of motion and the border-line condition of unstable equilibrium yielding the flutter speed and frequency may be obtained exactly as in the incompressible case treated, for example, in reference 4. The two-dimensional treatment (infinite aspect ratio) is retained herein. Modifications due to assumed vibration modes of the finite wing may of course be introduced as in current practice (for example, reference 5). The modification of the forces and moments due to the threedimensional nature of the flow is a more difficult problem which remains to be studied.

The equilibrium of the vertical forces, of the moments about the torsional axis $x = x_0$, and of the moments on the alleron about its hinge $x = x_1$ yields the three equations,

 $\ddot{\mathbf{n}}\mathbf{M} + \ddot{\alpha}\mathbf{S}_{\alpha} + \ddot{\beta}\mathbf{S}_{\beta} + \mathbf{n}\mathbf{C}_{\mathbf{h}} = \mathbf{P}$ $\ddot{\alpha}\mathbf{I}_{\alpha} + \ddot{\beta}\left[\mathbf{I}_{\beta} + 2\mathbf{b}(\mathbf{x}_{1} - \mathbf{x}_{0})\mathbf{S}_{\beta}\right] + \ddot{\mathbf{n}}\mathbf{S}_{\alpha} + \alpha\mathbf{C}_{\alpha} = \mathbf{M}_{\alpha}$ $\ddot{\beta}\mathbf{I}_{\beta} + \ddot{\alpha}\left[\mathbf{I}_{\beta} + 2\mathbf{b}(\mathbf{x}_{1} - \mathbf{x}_{0})\mathbf{S}_{\beta}\right] + \ddot{\mathbf{n}}\mathbf{S}_{\beta} + \beta\mathbf{C}_{\beta} = \mathbf{M}_{\beta}$ (24)

where the various parameters are defined in the list of notation. (See appendix.)

In order to define the border-line condition of unstable equilibrium separating damped and undamped oscillations, the variables h, α , and β are used in the sinusoidal exponential form given in equation (10). For the desired condition, it is necessary that the equations (24) have a (nontrivial) solution for the complex amplitudes h₀, α_0 , and β_0 , or that the following determinantal equation hold:

$$\begin{array}{c|cccc} \overline{A}_{ch} & A_{c\alpha} & A_{c\beta} \\ A_{ah} & \overline{A}_{a\alpha} & A_{a\beta} \\ A_{bh} & A_{b\alpha} & \overline{A}_{b\beta} \end{array} = 0 \qquad (25)$$

where the complex elements of the determinant in separated form are

$$\begin{split} \overline{A}_{ch} &= \Omega_{h} x - \mu + L_{1} + iL_{2} \\ A_{c\alpha} &= -\mu x_{\alpha} + L_{3} + iL_{4} \\ A_{c\beta} &= -\mu x_{\beta} + L_{5} + iL_{6} \\ A_{ah} &= -\mu x_{\alpha} + M_{1} + iM_{2} \\ \overline{A}_{a\alpha} &= \Omega_{\alpha} x - \mu r_{\alpha}^{2} + M_{3} + iM_{4} \\ A_{a\beta} &= -\mu \left[r_{\beta}^{2} + 2(x_{1} - x_{0})x_{\beta} \right] + M_{5} + iM_{6} \\ A_{bh} &= -\mu x_{\beta} + N_{1} + iN_{2} \\ A_{b\alpha} &= -\mu \left[r_{\beta}^{2} + 2(x_{1} - x_{0})x_{\beta} \right] + N_{3} + iN_{4} \\ \overline{A}_{b\beta} &= \Omega_{\beta} x - \mu r_{\beta}^{2} + N_{5} + iN_{6} \\ \end{split}$$

and where the L's, M's, and N's are defined by the force and moment equations (16'), (17'), and (18') expressed in the following forms:

23

24

$$P = -4\rho b v^{2} k^{2} e^{i\omega t} \left[\left(\frac{h_{0}}{b} \right) \left(L_{1} + iL_{2} \right) + \alpha_{0} \left(L_{3} + -iL_{4} \right) + \beta_{0} \left(L_{5} + iL_{6} \right) \right] \right]$$

$$M_{\alpha} = -4\rho b^{2} v^{2} k^{2} e^{i\omega t} \left[\left(\frac{h_{0}}{b} \right) \left(N_{1} + iM_{2} \right) + \alpha_{0} \left(N_{3} + iM_{4} \right) + \beta_{0} \left(N_{5} + iM_{6} \right) \right] \right] > (26)$$

$$M_{\beta} = -4\rho b^{2} v^{2} k^{2} e^{i\omega t} \left[\left(\frac{h_{0}}{b} \right) \left(N_{1} + iN_{2} \right) + \alpha_{0} \left(N_{3} + iN_{4} \right) + \beta_{0} \left(N_{5} + iN_{6} \right) \right] \right]$$

ŧ

. : : ::::

- 2

Hence,

$$L_{1} + iL_{2} = \frac{1}{\sqrt{M^{2} - 1}} \left(-2r_{2} + \frac{1}{k} r_{1} \right)$$

$$L_{3} + iL_{4} = \frac{1}{M^{2} - 1} \left[-2r_{3} + \frac{21}{k} r_{2} - \frac{1}{k} \left(-2r_{2} + \frac{1}{k} r_{1} \right) -2x_{0} \left(-2r_{2} + \frac{1}{k} r_{1} \right) \right]$$

$$L_{5} + iL_{6} = \frac{1}{\sqrt{M^{2} - 1}} \left[-2t_{3} + \frac{21}{k} t_{2} - \frac{1}{k} \left(-2t_{2} + \frac{1}{k} t_{1} \right) \right]$$

$$\begin{split} \mathbf{M}_{1} + \mathbf{i}\mathbf{M}_{2} &= \frac{1}{\sqrt{\mathbf{M}^{2} - 1}} \left[-2q_{2} + \frac{2\mathbf{i}}{\mathbf{k}} q_{1} - 2\mathbf{x}_{0} \left(-2\mathbf{r}_{2} + \frac{\mathbf{i}}{\mathbf{k}} r_{1} \right) \right] \\ \mathbf{M}_{3} + \mathbf{i}\mathbf{M}_{1} &= \frac{1}{\sqrt{\mathbf{M}^{2} - 1}} \left\{ -\frac{4}{3} q_{3} + \frac{2\mathbf{i}}{\mathbf{k}} q_{2} - \frac{4}{\mathbf{k}} \left(-2q_{2} + \frac{2\mathbf{i}}{\mathbf{k}} q_{1} \right) \right. \\ &\left. -2\mathbf{x}_{0} \left[-2\mathbf{r}_{3} + \frac{2\mathbf{i}}{\mathbf{k}}\mathbf{r}_{2} - \frac{4}{\mathbf{k}} \left(-2\mathbf{r}_{2} + \frac{4}{\mathbf{k}}\mathbf{r}_{1} \right) - 2q_{2} + \frac{2\mathbf{i}}{\mathbf{k}} q_{1} \right. \right. \\ &\left. -2\mathbf{x}_{0} \left(-2\mathbf{r}_{2} + \frac{4}{\mathbf{k}} \mathbf{r}_{1} \right) \right] \right\} \end{split}$$
$$\begin{split} \mathbf{M}_{5} + \mathbf{i}\mathbf{M}_{6} &= \frac{1}{\sqrt{\mathbf{M}^{2} - 1}} \left\{ -\frac{4}{3}\mathbf{s}_{3} + \frac{2\mathbf{i}}{\mathbf{k}}\mathbf{s}_{2} - \frac{4}{\mathbf{k}} \left(-2\mathbf{s}_{2} + \frac{2\mathbf{i}}{\mathbf{k}}\mathbf{s}_{1} \right) \right. \\ &\left. +2\left(\mathbf{x}_{1} - \mathbf{x}_{0}\right) \left| -2\mathbf{t}_{3} + \frac{2\mathbf{i}}{\mathbf{k}}\mathbf{t}_{2} - \frac{4}{\mathbf{k}} \left(-2\mathbf{t}_{2} + \frac{4}{\mathbf{k}}\mathbf{t}_{1} \right) \right| \right\} \end{split}$$

$$N_{1} + iN_{2} = \frac{1}{\sqrt{M^{2} - 1}} \left(-2p_{2} + \frac{2i}{k} p_{1} \right)$$

$$N_{3} + iN_{4} = \frac{1}{\sqrt{M^{2} - 1}} \left[\frac{h}{3} p_{3} + \frac{2i}{k} p_{2} - \frac{i}{k} \left(-2p_{2} + \frac{2i}{k} p_{1} \right) -2x_{0} \left(-2p_{2} + \frac{2i}{k} p_{1} \right) \right]$$

$$N_{5} + iN_{6} = \frac{1}{\sqrt{M^{2} - 1}} \left[-\frac{h}{3} s_{3} + \frac{2i}{k} s_{2} - \frac{i}{k} \left(-2s_{2} + \frac{2i}{k} s_{1} \right) \right]$$

The determinantal equation (25) with the foregoing complex elements is equivalent to two real simultaneous equations and hence may be solved for two unknowns. In a given case the usual unknowns are the flutter speed v_{-} and the flutter frequency ω or, more conveniently, the related nondimensional parameters X and 1/k. The parameter X appears linearly and only in the major diagonal elements (with bars), while the parameter 1/k appears transcendentally in every element of the determinant. Hence an obvious procedure though not the simplest for obtaining the simultaneous solutions of the two equations is to fix values of 1/k, to solve for the roots of the two polynomials in X, to plot graphically these roots against 1/k, and to note the points of intersection.

In a systematic numerical study of flutter any two parameters may be utilized as unknowns instead of X and 1/k, which is often more convenient. A discussion of such proceduro and the use of a method of elimination for simplifying the calculations is given in the appendix of reference 6.

The application to the two-degree-of-freedom subcase of bending-torsion flutter is treated more fully in the following section.

ì

=]

<u>.</u>

APPLICATION TO BENDING-TORSION FLUTTER

÷

The determinantal equation in the two degrees of freedom h and α is

 $\begin{vmatrix} \overline{A}_{ch} & A_{ca} \\ A_{ah} & \overline{A}_{aa} \end{vmatrix} = 0$

or

$$\begin{vmatrix} \Omega_{h} X - \mu + L_{1} + iL_{2} & -\mu x_{\alpha} + L_{3} + iL_{4} \\ -\mu x_{\alpha} + M_{1} + iM_{2} & \Omega_{\alpha} X - \mu r_{\alpha}^{2} + M_{3} + iM_{4} \end{vmatrix} = 0 (27)$$

The two equations in X obtained by equating the real and imaginary parts separately to zero are

$$\Omega_{n}\Omega_{\alpha}X^{2} + \left[\Omega_{\alpha}(L_{1} - \mu) + \Omega_{h}(M_{3} - \mu r_{\alpha}^{2})\right]X + C_{R} = 0$$
and
$$\left(\Omega_{\alpha}L_{2} + \Omega_{h}M_{\mu}X + C_{I} = 0\right)$$
(27)

where

$$C_{R} = \mu \left[x_{\alpha} (M_{1} + L_{3}) - (M_{3} - \mu r_{\alpha}^{2}) - L_{1} r_{\alpha}^{2} - \mu x_{\alpha}^{2} \right] + D_{R}$$

and

$$C_{I} = \mu \left[x_{\alpha} \left(M_{2} + L_{\mu} \right) - M_{\mu} - L_{2} r_{\alpha}^{2} \right] + D_{I}$$

where

$$D_{R} = L_{1}M_{3} - L_{3}M_{1} - L_{2}M_{1} + L_{1}M_{2}$$

and

$$D_{I} = L_{1}M_{4} - L_{4}M_{1} + L_{2}M_{3} - L_{3}M_{2}$$

For convenience in numerical tabulation, it is desirable to introduce primed quantities, independent of the parameter x_0 , defined by the following relations:

$$L_{3} = L_{3}' - 2x_{0}L_{1}$$

$$L_{4} = L_{4}' - 2x_{0}L_{2}$$

$$M_{1} = M_{1}' - 2x_{0}L_{1}$$

$$M_{2} = M_{2}' - 2x_{0}L_{2}$$

$$M_{3} = M_{3}' - 2x_{0}\left[(M_{1}' + L_{3}') - 2x_{0}L_{1}\right]$$

$$M_{4} = M_{4}' - 2x_{0}\left[(M_{2}' + L_{4}') - 2x_{0}L_{2}\right]$$
(28)

In table II convenient expressions for the quantities L_1 , L_2 , L_3 ', L_4 ', M_1 ', M_2 ', M_3 ', and M_4 ' are given and tabulated together with the combinations M_1 ' + L_3 ' and M_2 ' + L_4 '. Clearly these quantities depend on the function f_0 given in table I and hence the tabulation is made for the same values of M and 1/k (or $\overline{\omega}$). In addition, table II contains values for the quantities D_R and D_I which, in fact, are independent of x_0 and may be expressed as

$$D_{R} = L_{1}M_{3}' - L_{3}M_{1}' - L_{2}M_{4}' + L_{4}M_{2}'$$

and

$$D_{I} = L_{1}M_{4}' - L_{4}M_{1}' + L_{2}M_{3}' - L_{3}M_{2}'$$

The numerical application in the case of bendingtorsion flutter has been performed for various selected examples. In most of the calculations the numerical procedure was to fix values of 1/k, eliminate X, and

÷

ŧ

1 1

solve for the parameter x_{C} . Interpolation was also used to obtain additional points in order to improve the fairing of some of the curves. Values of 1/k less than 1 did not yield any flutter points in this procedure. Results are shown plotted in a number of figures (figs. 5 to 20); however, before these figures are discussed, it is desirable to explain the significance of the parameters and the numerical values assigned to them.

The parameter μ may be considered to signify the wing density and three selected values 3.927, 7.854, and 15.708 in the order of increasing wing density have been mainly used in the calculations. (These values correspond to values of $\frac{1}{\kappa} = 5$, 10, and 20 in the notation of reference 4.) Alternatively, an increase in μ may be interpreted as an increase in altitude for a fixed wing density. The parameter μ may be expected to range up to high values for actual supersonic wings at high altitude. Only a few calculations, however, have been made for high values of μ ($\mu = 73.54$, $\frac{1}{\kappa} = 100$; see fig. 18).

The parameter ω_h/ω_a is the ratio of the wing bending frequency to the wing torsional frequency and may be expected normally to be less than unity. The three values 0, 0.707, and 1 have been largely used in the calculations although other values up to 2 have also been studied.

The parameter x_0 represents the position of the elastic axis measured from the leading edge and the three values 0.4, 0.5, and 0.6 represent, respectively, positions at 40, 50, and 60 percent chord. (These values correspond to values of a = -0.2, 0, and 0.2 in the notation of reference 4.)

The parameter x_{α} represents the distance of the center of gravity from the elastic axis. For example, $x_{\alpha} = 0.2$ represents a position of the center of gravity 10 percent of the chord behind the elastic axis. In many of the calculations x_{α} has been regarded as variable.

23

The parameter r_{α}^2 represents the radius of gyration of the wing about the elastic axis and has been kept fixed at the value $r_{\alpha}^2 = 0.25$.

The ordinate in figures 5 to 20 is the nondimensional flutter coefficient $v/b\omega_{\alpha}$ where $b\omega_{\alpha}$ is a convenient reference speed. This coefficient is also a function of the Mach number $M = \frac{v}{c}$ and several values of M have been employed in the calculations.

In a plot of the flutter coefficient $v'b\omega_{\alpha}$ against M, straight lines drawn from the origin at angle δ and intersecting the curves may be given an interesting interpretation (fig. 17). The slope of the line is given by $\frac{v'b\omega_{\alpha}}{v'c} = \frac{c}{b\omega_{\alpha}}$ or $\cot \delta = \frac{b\omega_{\alpha}}{c}$. Thus,

cot δ is directly proportional to the product of the chord and the torsional frequency. The question of whether at a given value of M the value of $b\omega_{\alpha}$ which will just prevent flutter is also sufficient to prevent flutter at neighboring higher values of M is answered by the simple criterion of whether $\cot \delta$ increases or decreases. In figure 17 two typical flutter curves are shown. In curve B the value of bur just necessary to prevent flutter at a speed corresponding to the value of M at P_2 is insufficient to prevent flutter at any higher value of M for which the flutter curve is below the straight line OP2. For the type of curve A a maximum value of 6 occurs at the "design critical points" P. The values of $b\omega_{\alpha}$ just necessary to prevent flutter at a speed corresponding to the value of M at P_1 is also sufficient to prevent flutter at all higher speeds.

The following salient facts may be extracted by inspection of the figures. Flutter exists or is possible for various ranges of the parameters but, in general, compared with subsonic cases the ranges of the parameters yielding flutter are more restricted.

The chordwise position of the aerodynamic center, the center of the oscillating pressure, is an important factor in the consideration of flutter. In the simple theory the midchord is the aerodynamic center for M >> 1. For subsonic speeds, M << 1, the linearized theory indicates the quarter-chord position as the aerodynamic center. It should be expected that in the transonic region near M = 1 the aerodynamic center may shift considerably. From this point of view alone conclusions drawn from the simple theory for the range near M = 1 may require large modifications. The nature of the modifications may be roughly inferred by further experimental and theoretical study of the behavior of center-of-pressure locations.

For low values of the ratio of bending frequency to torsional frequency $\frac{\omega_h}{\omega_a} \approx 0$ the position of the center of gravity relative to the aerodynamic center is important. For center-of-gravity positions forward of the midchord no flutter exists, whereas for positions behind the midchord there is a sharp decrease in the flutter coefficient from infinity; the position of the elastic axis influences the value of the flutter coefficient in this region, forward positions being more favorable (figs. 5(a) to 16(a)).

For values of $\frac{\omega_h}{\omega_a} \approx 1$ the position of the center

of gravity relative to the elastic axis becomes of more importance. For center-of-gravity positions forward of the elastic axis no flutter exists, whereas for positions behind the elastic axis flutter does occur, and a relative minimum coefficient appears for center-of-gravity positions only slightly (a few percent of the chord) behind the elastic axis.

The intermediate case, for which $\frac{\omega_h}{\omega_a} = 0.707$,

shows a blending of the effects in which the centerof-gravity position relative both to the aerodynamic center and to the elastic axis is significant.

In figures 12 and 14 there are shown, for reference, some numerical values of ω/ω_{α} , the ratio of the flutter frequency to the torsional frequency.

The effect of the wing-density parameter μ is rather complicated but, in general, an increase in μ yields a corresponding increase in the flutter coefficient. For low values of ω_h/ω_a and for high wing densities this increase is expected to be proportional to $\sqrt{\mu}$. In the resonance-like region near $\frac{\omega_h}{\omega_a} = 1$ and for small values of x_a the flutter coefficient is relatively unaffected by the value of μ , and in this region the structural damping may be expected to be particularly effective in increasing the flutter coefficient.

For values of the Mach number near unity (for example $M = \frac{10}{9}$, a value for which the validity of the theory is in question), the flutter calculations become difficult to plot because of the appearance of other branches. In some cases (for instance, $x_0 = 0.6$) the flutter instability appears limited to a definite range of speed. Calculations to include damping were performed to verify the existance of the range. (The appearance of these other branches seems to involve values of 1/kfor which the quantity M_{\downarrow} is negative. The condition of negative M_{\downarrow} is significant for the one-degree-offreedom instability discussed in the next section.

A plot of the flutter coefficient against Mach number for two values of x_{α} is shown in figure 17. The significance of the straight lines drawn from the origin has already been discussed. The type of curve A is representative of the effect of forward location of the center of gravity and the type of curve B is representative of rearward locations of the center of gravity. Figure 18 gives a plot of the flutter coefficient against M for various values of the wing-density parameter u and for a rearward location of the center of gravity. The subsonic values for M = 0 and M = 0.7 shown on these curves and on some of the other figures have been either taken from reference 7 or calculated in the manner outlined therein. The subsonic and supersonic parts of the curves (figs. 17 and 18) have been arbitrarily joined by a dashed smooth curve in

31

the transonic range. In figure 19 there is given a cross plot of flutter coefficient against frequency ratio ω_h/ω_a , for various values of M, and in figure 20 is given a similar cross plot for three values of the elastic-axis parameter x_0 .

An indication of the effect of structural damping in increasing the flutter speed in a few examples may be obtained from the following table, where g_{α} and $g_{\rm h}$ are the torsional and flexural damping coefficients, respectively, and where $M = \frac{10}{7}$, $\mu = 7.854$, a = 0, and $x_{\alpha} = 0.2$:

ω _h /ω _α	Ξa	₿ <u>h</u>	ω/ω _α	v∕bw _a
0 0 0 •707 •707 •707 •707 •707 •707 •70	0 .05 .10 0 .05 .10 0 0 .05 .10	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0.673 643 628 777 771 766 788 797 762 784	2.438 2.551 2.6635 1.5569 1.5569 1.6623 1.6623 1.6623 1.6623 1.725

STATIC CASES - WING DIVERGENCE AND AILERON REVERSAL

It is of some interest to examine the expressions for the forces and moments in the limit case in which the frequency approaches zero. There follow then for the mean-line wing section the well-known static-case results which may of course be obtained directly without the use of a limiting process, as originally treated by Ackeret. Thus, with the use of the following relation easily verified from equations (20),

 $\lim_{k \to 0} f_{\lambda}(m, k) = \frac{1}{\lambda + 1}$

there are obtained from equations (16') to (18') for the lift and moments in the static case,

 $L = -\frac{\mu \rho b v^{2}}{\sqrt{h^{2} - 1}} \left[\alpha + (1 - x_{1}) \beta \right]$ $M_{\alpha} = -\frac{\mu \rho b^{2} v^{2}}{\sqrt{h^{2} - 1}} \left[(1 - 2x_{0}) \alpha + (1 - x_{1}) (1 + x_{1} - 2x_{0}) \beta \right]$ $M_{\beta} = -\frac{\mu \rho b^{2} v^{2}}{\sqrt{h^{2} - 1}} (1 - x_{1})^{2} (\alpha + \beta)$

These relations for the mean-line wing section are now used to obtain the critical speeds for the static instabilities -wing divergence and wing-alteron reversal (for wing of infinite span). At the wing divergence speed the effective torsional stiffness of the wing vanishes, hence the total moment about the elastic axis is zero. The sum of the structural restoring moment and the aerodynamic twisting moment is

$$xC_{\alpha} + \frac{\mu_{0}b^{2}v^{2}}{\sqrt{u^{2}-1}} \alpha(1 - 2x_{0})$$

which when equated to zero yields the divergence speed

$$v_{\rm D} = b\omega_{\alpha} (M^2 - 1)^{1/4} \sqrt{\mu r_{\alpha}^2} \frac{1}{\sqrt{2x_{\rm O} - 1}}$$

Thus, the divergence speed is real only for positions of the elastic axis behind the aerodynamic center (midchord, in the simple theory). This formula obviously should not be used for values of M too near unity.

For comparison it is of interest to note the corresponding result for the divergence speed in the subsonic case, where the aerodynamic center is (approximately) at the quarter-chord point. Thus,

$$v_{\rm D} = b\omega_{\alpha} (1 - M^2)^{1/4} \sqrt{\frac{r_{\alpha}^2}{\kappa}} \frac{1}{\sqrt{4x_0 - 1}}$$

where M < about 0.7.

The aileron reversal speed is determined by the condition that the change in angle of attack due to wing torsion nullifies the effect of movement of the aileron so as to yield no change in lift (in rolling moment, in the case of finite wing span). There are two equations to be satisfied for this condition; namely,

$$\alpha + (1 - \pi_1)\beta = 0$$

(that is, L = 0) and

$$\alpha C_{\alpha} + \frac{l_{\perp \rho b} 2_{v}^{2}}{\sqrt{4^{2} - 1}} \left[(1 - 2x_{0})\alpha + (1 - x_{1})(1 + x_{1} - 2x_{0})\mu \right] = 0$$

The alleron reversal speed, obtained by elimination of α and $\beta,$ is

$$v_{R} = b\omega_{\alpha} (M^{2} - 1)^{1/4} \sqrt{\mu r_{\alpha}^{2}} \frac{1}{\sqrt{x_{1}}}$$

For hinge positions aft of the midchord, the factor $1/\sqrt{x_1}$ in this expression varies from 1.4 to 1.0. The sileron reversal speed is thus relatively unaffected by the position of the hinge. In general v_R may be expected to be lower than v_D .

ONE-DEGREE-OF-FREEDOM OSCILLATORY INSTABILITY

As was pointed out by Possib, the theory indicates the existence of a torsional instability which may arise for a wing having only one degree of freedom. This instability is due to the wing being negatively damped in torsion and is associated with the vanishing (and change in sign) of the torsional damping coefficient M_{μ} (equation (26)).

Certain considerations for the case-of slow oscillations made by Possio (reference 1) and further discussed by Tomole and Jahn serve to bring out the main results. Thus from equation (20), for slow oscillations,

$$f_{\lambda}(M, k) \approx \frac{1}{\lambda + 1} - i \frac{2kM^2}{M^2 - 1} \frac{1}{\lambda + 2}$$

and

$$M_{4} \approx \frac{1}{\sqrt{M^{2} - 1}} \frac{1^{-2}}{k^{-3}} \left[4 - 9x_{0} + 6x_{0}^{2} - \frac{M^{2}}{M^{2} - 1} \left(2 - 3x_{0} \right) \right]$$

The condition $M_{i_{4}}(M, x_{0}) = 0$ is shown plotted in figure 21, where the shaded area is the region in which the instability is possible (negative $M_{i_{4}}$). The maximum ranges for the parameters x_{0} and M in this region are x_{0} less than 2/3 and M less than $\sqrt{2.5}$ (and greater than unity).

(It may be appropriate to mention that a similar torsional instability is theoretically indicated even in the subsonic (incompressible) case for positions of the axis of rotation between the leading edge and the quarter-chord point. However, the combination of parameters required for this indicated instability is practically unattainable.)

The torsional instability may be studied more fully in the general case. It is found that the range of instability for the parameters x_0 and M remains essentially as in the simple case (large 1/k) but more information may be obtained regarding the critical speed and frequency. The moment equation is equivalent to $\overline{A}_{ac} = 0$, or to the two equations

 $\Omega_{\alpha} X - \mu r_{\alpha}^{2} + M_{3}(N, x_{0}) = 0$ $M_{4}(N, x_{0}) + g_{\alpha} \Omega_{\alpha} X = 0$

- -

where the structural damping coefficient in torsion g_{α} has been introduced as in reference 6. The critical speed and frequency may be studied as functions of the parameters x_0 , M, g_{α} and the product combination μr_{α}^2 . Results of a few selected calculations are shown plotted in figure 22. Since instabilities are indicated for the range of near-sonic values ($1 \le M \le 1.58$) it would seem that a more comprehensive investigation of this problem is very desirable.

It may be remarked that a similar analysis for pure bending exhibits no instability while the case of the aileron alone does exhibit a range where such instability may occur. This range for an aileron hinged at its leading edge is $1 < M \leq \sqrt{2}$.

Langley Memorial Aeronautical Laboratory National Advisory Committee for Aeronautics Langley Field, Va., May 29, 1946

APPENDIX

SYMBOLS

ø	disturbance velocity potential		_
t	time at which disturbance influence is felt		
T	time at which disturbance is created		-
τ=t- 5	T		
p	pressure		
p†	pressure difference		-
ρ	density		ĩ
۲	adiabatic index (for air, $\gamma \approx 1.4$)		
v	velocity of main stream (supersonic)	<i>.</i> .	
C	velocity of sound in undisturbed medium		
М	Mach number (v/c)		
x	coordinate measured in direction of main stream		· _
У	ordinate		
×0	abscissa of axis of rotation of wing section (elastic axis)		
xl	abscissa of aileron hinge	-	
<u>č</u> , ŋ	abscissa and ordinate of point of disturbance	- 	
Ъ	one-half chord		-
Afte and کے ar to the ch	er equation (12) the quantities x , y , x_0 , x_1 , re employed nondimensionally and are referred nord 2b as reference length.	· _	~~

w(x, t) vertical velocity at position x on chord and at time t

.

37

- --- -

_,

-

...,

38

h vertical displacement of exis of rotation

a angular displacement about axis of rotation

β angular displacement of alleron; measured with respect to α

ω angular frequency of oscillation

k reduced frequency $(\omega b/v)^{\pm}$

ω

frequency parameter $\left(\frac{2kM^2}{M^2 - 1}\right)$

i

 $I(\xi, x)$ function given in equations (12) and (12)

 $J_n(\lambda)$ — Bessel function of order (n .

The following additional symbols, employed in the flutter equations, conform to the notation used in references 4 and 6, in which the half-chord b is the unit reference length.

M mass of wing per unit span

- Sa static moment of wing-aileron combination per unit span referred to the elastic axis
- S_{β} static moment of aileron per unit span referred to aileron hinge
- I_α moment of inertia of wing-aileron combination about elastic axis per unit span
- I moment of inertia of aileron about its hinge per unit span
- a coordinate of elastic axis measured from midchord $(2x_0 - 1)$
- c coordinate of aileron hinge axis measured from the midchord $(2x_1 1)$

 x_{α} location of center of gravity of wing-aileron system measured from elastic axis S_{α}/M_{b} ;

location of center of gravity in percent total chord measured from leading edge is 100 $\frac{1+a+x_{\alpha}}{2} = 100\left(x_{0} + \frac{x_{\alpha}}{2}\right)$

reduced location of center of gravity of alleron referred to c $\left(\hat{s}_{\beta}/M_{b}\right)$ ×β

ra radius of gyration of wing-aileron combination referred to a $\left(\sqrt{\frac{I_{\alpha}}{m^2}}\right)$

- reduced radius of gyration of aileron referred to c $\left(\sqrt{\frac{1_{\rm f}}{1_{\rm f}}}\right)$
- Cα torsional stiffness of wing around a per unit span
- Cβ torsional stiffness of aileron system around c per unit span
- $\mathtt{C}_{\mathtt{h}}$ stiffness of wing in deflection

natural angular frequency of torsional vibrations about elastic axis $\left(\sqrt{\frac{c_{\alpha}}{I_{\alpha}}}\right)$; $\left(\omega_{\alpha} = 2\pi f_{\alpha}\right)$, where f_{α}

is in cycles per second)

ω_Ŀ

ωα

rß

natural angular frequency of torsional vibrations $c \left(\sqrt{\frac{c_{\beta}}{I_{c}}} \right)$ of aileron around

ω_h

natural angular frequency of wing in deflection

 $\mu = \frac{\pi}{\underline{l}_{1}} \frac{\bot}{\kappa}$ wing density parameter, where $\kappa = \frac{\pi \rho b^{2}}{M}$

is the ratio of a mass of cylinder of air of a diameter equal to the chord of the wing to the mass of the wing, both taken for equal length along the span; this ratio may be expressed as $\kappa = 0.24(b^2/W)(\rho/\rho_0)$ where ₩ is the weight in pounds per foot span, b is in feet and $\rho/\rho_{\rm o}$ is the ratio of air density at altitude to that for normal standard air $\left(\mu = \frac{M}{\mu_{ob}^2} = \frac{\pi}{4} \frac{1}{\kappa}\right)$

_

 $g_{\alpha}, g_{\beta}, g_{h}$ structural damping coefficients (see reference 6) $L_{1}, L_{2}, L_{3}, L_{4}, M_{1}, M_{2}, M_{3}, M_{4}$ quantities defined in table II and by equations (26) and (28) v/ω_{α} flutter coefficient; that is, flutter speed divided by reference speed $b\omega_{\alpha}$ $\Omega_{\alpha}X = \mu r_{\alpha}^{2} \left(\frac{\omega_{\alpha}}{\omega}\right)^{2}$

 $\Omega_{\beta} X = \mu r_{\beta}^{2} \left(\frac{\omega_{\beta}}{\omega} \right)^{2}$ $\Omega_{h} X = \mu \left(\frac{\omega_{h}}{\omega} \right)^{2}$

where ω is the angular (flutter) frequency and

$$x = \mu r_{\alpha}^{2} \left(\frac{\omega_{\alpha}}{\omega} \right)^{2}$$

for case of bending-torsion (Note that in the incompressible case (references \hbar and 6) μ is replaced by $1/\kappa_*$)

REFERENCES

- 1. Possio, C.: L'azione aerodinamica sul profilo oscillante alle velocità ultrasonore. Acta, Pont. Acad. Sci., vol. I, no. 11, 1937, pp. 93-105.
- 2. V. Borbely, S.: Aerodynamic Forces on a Harmonically Oscillating Wing at Supersonic Velocity (2-Dimensional Case). R.T.P. Translation No. 2019, British Ministry of Aircraft Production. (From Z.f.a.M.M. Bd. 22, Heft 4, Aug. 1942, pp. 190-205.)
- Schwarz, L.: Untersuchung einiger mit den Zylinderfunktionen nullter Ordnung verwandter Funktionen. Luftfahrtforschung, Bd. 20, Lfg. 12, Feb. 8, 1944, pp. 341-372.
- 4. Theodorsen, Theodore: General Theory of Aerodynamic Instability and the Mechanism of Flutter. NACA Rep. No. 496, 1935.
- 5. Smilg, Benjamin, and Wasserman, Lee S.: Application of Three-Dimensional Flutter Theory to Aircraft Structures. ACTR No. 4798, Materiel Div., Air Corps, July 9, 1942.
- 6. Theodorsen, Theodore, and Garrick, I. E.: Flutter Calculations in Three Degrees of Freedom. NACA Rep. No. 741, 1942.
- 7. Garrick, I. E.: Bending-Torsion Flutter Calculations Modified by Subsonic Compressibility Corrections. NACA TN No. 1034, 1946.

TABLE I.- VALUES OF $\mathbf{f}_{0}(\mathbf{M}, \overline{\omega}) = (\mathbf{f}_{0})_{\mathrm{R}} + \mathbf{i}(\mathbf{f}_{0})_{\mathrm{I}}$ $(\mathbf{f}_{0})_{\mathrm{R}} = \frac{1}{\overline{\omega}} \int_{0}^{\overline{\omega}} \mathbf{J}_{0}(\frac{\mathbf{u}}{\overline{\mathbf{M}}}) \cos \mathbf{u} \, \mathrm{d}\mathbf{u}$

$(\mathbf{f}_0)_{\mathbf{I}} = -\frac{1}{\overline{\omega}}_{\mathbf{U}}$	$\int_{0}^{1\omega} J_{0}\left(\frac{u}{M}\right) \sin u$	u du
---------------------------------------------------------------------------	-----------------------------------------------------------	------

ធ	1 L	$(\mathbf{r}_0)_{R}$	$(r_0)_{I}$	ω	1 k	$(\mathbf{f}_0)_{\mathrm{R}}$	(r ₀) _I	
		$M = \frac{10}{9}$	$=\frac{10}{9} \qquad \qquad \mathbb{M}=\frac{10}{7}$					
20.00 10.00 8.00 5.00 4.20 3.20 2.50 2.10 1.68 1.40 1.10 .52 .10	0.526 1.053 1.316 1.755 2.105 2.508 4.211 5.289 4.211 5.269 9.569 20.243 40.486 105.263	0.02107622 .10786366 .15423397 .17593123 .23364109 .26927908 .27020078 .32453905 .40860905 .539882 .64370304 .75786234 .938879 .984312 .997660	-0.14998785 21774161 21646721 27930193 30623887 32995569 42367574 42767574 42767574 42895719 48895719 48895719 14031451 247350 128388 049910	20.00 10.000 5.990 3.1400 1.14 .540 .540 .04	$\begin{array}{c} 0.196\\ .392\\ .0065\\ 1.0065\\ 1.4965\\ 1.4965\\ 1.4965\\ 1.4965\\ .43272\\ 5.4128\\ .43272\\ 5.4128\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43272\\ .43$	0.01041793 02790057 .13530140 .15895143 .9688319 .32317741 .44414008 .59012790 .749343 .832504 .832504 .832504 .832504 .832504 .832504 .945429 .945429 .967340 .991735 .997930 .999675	-0.05473581 18976570 -33798972 -35747165 44343786 53918653 56786346 55477283 482889 413781 357217 293258 250038 195428 099425 049930 020000	
		$M = \frac{5}{4}$	•	$M = \frac{5}{3}$				
20.00 10.00 5.00 2.80 2.80 1.66 1.34 1.10 .88 .74 .28 .14 .06	0.278 .556 1.111 1.2684 1.984 1.984 2.525 3.3446 5.0513 7.508 7.508 19.8413 39.683 92.593	-0.02589034 .02529654 .19004335 .21539228 .22643569 .26380752 .38184436 .557683 .678777 .76855505 .844426 .886947 .933477 .982907 .995700 .999200	-0.08629977 -22399799 -33199853 -32383270 -36922184 -43392085 -51318210 -532604 -5500827 -45177830 -387852 -388397 -266032 -138218 -069779 -029983	· 000000000000000000000000000000000000	0.156 .312 .625 1.250 1.250 1.645 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.9502 1.95	0.00827247 -03440806 07303312 15700194 -28500372 -48400601 -59909796 -71425408 -839483 -892157 -926973 -951928 -965855 -980047 -994975 -998738 -999675	-0.07001922 -13439143 -32465775 -49133028 -57452410 -60117841 -57737682 -52373582 -419702 -352880 -295089 -242110 -205300 -157913 -079738 -039962 -020000	

42

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

Ø	$\frac{1}{k} (r_0)_R$		(r ₀) _I	ω	1 F	(f ₀) _R	(r ₀) _I
		M = 2		Ж = 5			
20.00 10.00 2.10 2.10 1.60 1.10 .64 .44 .44 .44 .44 .06 .02	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		-0.06337016 08613197 29541589 59458735 63550404 59698731 53566558 47882893 371721 305330 261128 128996 128996 029983 010000	20.00 10.00 5.00 1.70 1.00 1.00 1.00 1.00 1.00 1.00 1	0.104 .208 .496 .9925 1.22356 2.496 .92236 2.4860 .4.9667 .4.9667 .4.9667 .4.9667 .4.9667 .2.440 .10.417 .20.8322 .34.722 .104.167	-0.1854996 00207595 15446620 16645177 .41122567 .58072358 .77380710 .83908297 .884607 .936018 .958080 .970300 .980474 .986729 .986729 .993215 .998300 .999383 .999950	$\begin{array}{c} -0.06011798\\12707440\\17734818\\35826002\\70315051\\65532307\\52771202\\52771202\\45746891\\394511\\299626\\244532\\206750\\168271\\168271\\139032\\099645\\029983\\010000\\ \end{array}$
		$M = \frac{5}{2}$		$M = \frac{10}{3}$			
20.00 10.00 5.00 1.40 1.40 1.40 1.40 1.40 1.40 5.48 .758 .48 .728 .48 .728 .48 .728 .48 .728 .48 .728 .48 .728 .788 .788 .788 .788 .788 .788 .78	0.138 .4796 .992 1.708807 1.708807 1.798807 1.98807 4.400 7.98660 7.98660 7.98660 7.98660 19.6888 19.048	0.00671539 02216359 -05520172 -05938671 29706773 49182591 69153899 76519653 844299 909960 909960 909981 974266 981697 989675 997408 999350 999950	-0.04537548 -06784796 -2561405 -27691360 -65923330 -65290610 -57126881 -51684512 -436326 -341204 -280086 -234350 -187184 -158316 -119288 -059908 -029983 -010000	20.000 10.000 5.420 1.300 1.18866 5.456 .300 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .000 .0000 .000 .000 .000 .000	0.110 2200 59921 1.59921 1.69988 3.4990 1.69988 3.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.4990 2.1990 2.4990 2.4990 2.4900 2.9900 2.9900 2.9900 2.9900 2.9900 2.9900 2.99000 2.990000000000	0.00960890 02509080 -11086610 -12438944 .37034955 .53617331 .73436415 .80420000 .871331 .926118 .953675 .966677 .977606 .984410 .991595 .998260 .999367 .999950	-0.05304109 -08576219 -21422339 -31880518 -68956543 -65968944 -55334513 -49023486 -408825 -316656 -253427 -216005 -177806 -148727 -109495 -029983 -010000

TABLE I.- VALUES OF $\mathbf{f}_{0}(\mathbf{M}, \overline{\omega}) = (\mathbf{f}_{0})_{\mathrm{R}} + \mathbf{i}(\mathbf{f}_{0})_{\mathrm{I}}$ - Concluded

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

1

TABLE II .- VALUES OF FUNCTIONS USED IN THE FLUTTER CALCULATIONS

44

Þ, ۲ 0.0087

-0.0016

												-	
	The exp	messions e	mployed in	the calcul:	ation of thi	a table a	150 1						
	L	$=\frac{1}{\sqrt{t^2-1}}$	{-2(f ₀) _R +	+ ¹ / ₂ [10(<u>x</u>) = 1	$\frac{1}{2} = \frac{1}{2} J_1 \left(\frac{1}{2} \right)$	·) •••• •]			M l; = L ^l ·	• •1			
	¹ 2	$=\frac{1}{\sqrt{u^2-1}}$	{-2(\$0)1 +	· 프 [r () · · ·	$\overline{u} + \frac{1}{\underline{u}} J_1 \left(\frac{\overline{b}}{\underline{b}} \right)$	[) = 1 = v			#2' = L2 ·	• •2			•
	13'	= L ₁ + }	L ₂ + A ₁						¥3' = ∰(I1	$1 - B_1 + \frac{1}{k} (I$	(z + 4z)		•
	1 4	= t ₂ - 1	I + 42						#4' = ¹ /2	e - B2) - È(1	51 + *1)		
	where			~					۲				-
	* 1	■ √2 ² - 1		$(a)_{R} = \frac{1}{M} J_{0} \left(\frac{\overline{a}}{M} \right)$) cos . <u>∞</u> -1 ¹ (1) = 11 E	, ^B 1	$=\frac{1}{\sqrt{2}-1}\frac{1}{2}$	1 2x ² [- ² / ₀ J ₁ (+ 31(2) sin 5]
	A2	$\frac{1}{\sqrt{k^2-1}}$	$\frac{1}{2k^2} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} (r_0)$	$I + \frac{\pi}{7} 2^{0} \left(\frac{\pi}{\pi} \right)$	sin 🗉 - J ₁		Ba	$2 = \frac{1}{\sqrt{x^2 - 1}} \frac{1}{x}$	<u>1</u> 22 ² 5 5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\left(\sin \overline{\sigma} - \frac{1}{\pi} \right)$	(^w) sin W	+ $J_1\left(\frac{\overline{u}}{u}\right) \cos \overline{u}$	
	ł	Ŀı	L2	1.5'	т ц, '	K 1'	¥2'	¥3'	" 4'	¥1 + 13'	.¥2' + 44'	D _R	PI
	-						χ.	<u>10</u> 9				*	۲
ĺ	0.526	-0.02525	0.44559 .80255	0.25959	0.44106 .79116 .88074	-0.07557	0.46341 74716	0.24942	0.60938	0.18402	0.90447	-0.05382	0.00
	1.754	-39623 62771 -7/1997	1.32462 1.73618 2.15463	2.99585	68853 68882	11793 337722 20171	1.06558 1.46206 1.80417	2.65307	1 76531	3.11636 4.91053	1.95411 2.15067 2.5296	69014	-22 -91 1-41
	3.289	1.50005 2.52780 3.61621	2.69560	10.88273	- 62644 -5 21239	59212 2.13970 3.69590	1.72808 2.05115 3.10809	8.27851 12.62101 20.5530	2 12162	11.47515 20.80746	1.10161	-3.26198	7.03
	8.266 7.519	4 97649 5 92672 6 89867	7.84048	53.54517 85.65512	-21.13670	5 73565 7 19803 8 71601	5.65664	11.594.61 71.57563	-25.25245	59.07882 92.85315	-15.50006 -23.01591	-36.94,330	29 49 38 40
Į	20.245	8.35744 8.68383 8.784.60	39 58910 82 45879 216 90161	807.07986 5344.23646 22837.60050	-128.09476 -268.54746 -707.59822	10.99388	38.49893 81.89315 216.70691	787 81916 3324 26400 2831 80624	-168.60818 -357.96892 -942.10469	818.07374 3355.78019 22919.31720	-89-59583 -186-65431	-561.00925 -2286.54565	119.858
							¥ •	5 .	,				402.0794
	0.278	-0.00103	0.22815	0.06045	0.21882	0.00087	0.23777	0.05814 24339	0.29553	0.06132	0,45659	-0.01551	-0.001
Į	1.263	.09225 25179	.89629 1.11026	1.39479	.74500 .84102 .94772	07860	83508 84890	1.54400	1.30141 1.67536	1.31619 2.27270	1.67610	23051	.131 .226
ļ	2.525	89075	1.91297 3.05697	5.74578	-22823	86646 1-59007	1.34853	4.68307 9.82891	61189	2.21222 12.97368	1.57656	-2.25852	1.832
	5.051	1.87067	3.61041 7.46934	29.70974 48.52284	-3-30446	2.36703	2.00271 5.07717 7.01066	27.67224	-3.91126 -6.17197	32.07677 51.23178	1.77301 2.06989	-13-37591 -21-85719	3.855 4.901 6.317
	9.921 19.841	2.23050	12.58397	126 41442 519 94592	-9-22392	2.93717 3.10371	12.27385	124.01103 517.48047	-12 01794 -26 56078	129 35159 523 04965	3.04993	-56.54665 -231.76919	7.630
	92.595	2.36674	路鹅港	11426.15260	-95.90686	3.18859	123.35267	11423-45420	-125.00012	11429.34119	27.44381	-5761.50717	33.849 54.411
	0.133	-0.00008	0.06698	0.00885	0.06657	-0.00009	0.06739	0.00881	0.08885	0.00876	0.15396	-0.00146	-0.000
	-555 -555 -988	- 01646	26350 -44538	-49674	-45368	- 03647	27440	-47472	17812 35343 62041	.10762 .51172	53578 855528	- 01849 - 08471	- 000
	1.270	11850 14,082	60515 84295 1 07856	1.50219 2.31942	-55685 -69968 -83947	07924 15972 17466	78872 1.02878	.80838 1.45559 2.26740	75855 94750 1.13198	1.64190 2.49408	1.4886.0	- 150,60 - 280,07 - 14,506	039 056 072
	3.333 4.167	17153 17153 17886	1.85225	2-27821 6-29401 2-89987	1 31584 1 63041	22329 23489	1.81690	6 23471 9 83886	1.76306 2.18092	2.47416 6.51723 10.13476	3.13275	-1.210.2	.086 121 152
	4,920 6,349 7,407	18651	2 80009 3 62600 4 <u>21217</u>	12 97402 23 14814 31 55225	2.46157	21710	3.60626	23.08537 31.48909	3.28681	23 39524 31 80185	6.06783 7.09182	-4.45516 -6.07291	181 251 273
	19.018 19.018	.19178	10.98370 25.65424	209.34139 1140.31777	2 9207/ 7 33738 17 11024	25559	10.97698	209.27740	9.78561	209.59598 1140.57327	18.31436	-49.30930 -217.14303	-379 -7051 3-2522
	133.335	.19243	76,97811	10269.90887	91.94409		78.97625 ¥ =	- 2		10284.15512	120.29009	=1916.71291	6.522;
	0.119	0.00029	0.047	0.00567	0.04760	0.00059	0.04776	0.00567	0.06351	0.00626	0.09536	-0.00076	-0.0000
	476	- 01004 - 01083	196. 1967	09083 09847	18862 19634	- 02004 - 02254	19777 20253	08981	25367 26426	07079 07593	-38639 -39887 -72716	01018	.000
	1.253	0,114	49084 69385	65264 1 22505	16379 61784	01474	46633	63795 1.20742	62350 82810	-69738 1.29603	93012 1.25907	- 09271	013
ļ	2.180	07056	1.04583	2.64413	.88859 1.17780	09081	1.02807	2.62441 4.71024	1.18820	2.73494	1.91666	- 28385	029 039
۱	6.266	07286	2.14533	10.69564	1.75892	10561	2.15564	10.67140	2.54692 2.95974	10.80125 17.19652	2.444/2 3.69456 4.95001	-1.55561 -2.40598	1000
	9.921 19.811	.08230	2 51980 8 5546	12.91023	3.50826 7.01164	.10951	8.65195	12.89658	3 34996	171-58127	7.82311	-6.20185	1197
	39.683 119.048	.08308	51.95581	6185.28165	42.06234	.11068	51.95562	6185.22715	10.59929 54.78641	6185.38158	94.01796	-765.13832	-1.3065

NATIONAL ADVISORY COLLETTER FOR ARROWAUTICS

·<u>·</u>

.

-

.

÷

<u>1</u> k	Ľ1	L2	L3'	Ľ4'	* 1'	¥2'	¥3'	¥, '	u1, + r2,	¥2' + 14	D _R	DI	
¥ = 19 7													
0.1924 .3924 .2025 1.0253 1.0253 1.0253 1.0253 1.0253 2.1272 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.540 2.5400 2.540 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.5400 2.54000 2.54000 2.54000 2.54000 2.54000000000000000000000000000000000000	0.002911 -0009511 -0003586 -10629 -2861188 -721648 -721648 -72556 -875611 -915472 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -93592 -935	0 137530 137530 137530 147530 147530 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147535 147555 147555 147555 147555 147555 147555 1475555 1475555 1475555 1475555 1475555 1475555 1475555 1475555 1475555 1475555 1475555 1475555 14755555 14755555 14755555 147555555 147555555 147555555555 147555555555555555555555555555555555555	0.02700 .10722 .15630 .1141,04 .25630 .1141,04 .29507 .299507 .299507 .4978696 .15798696 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2550,0129 .2	0.13682 250919 250919 27631539 27631575 27631755 27631755 25517771 255541755 2556417 2556417 2556417 2557957	0.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1	0 120 120 120 120 120 120 120 12	0.02752 .10313 .45934 .69334 .1027742 .2.57142 .2.57142 .2.57642 .2.57642 .2.57642 .2.57642 .2.57642 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.57644 .2.576444 .2.576444 .2.576444 .2.576444	0.18373 .355932 .93121 1.10167 1.10651 1.10157 1.10157 1.10157 .75680 .77932 .77932 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .77952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .79952 .7	0.08997 .88710 .88710 .88710 .871057 .1138456 .2.22057 .5.45117 .0.653320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.53320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.5320 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.53200 .6.532000 .6.532000 .6.532000 .6.532000 .6.532000 .6.532000 .6.5320000 .6.532000000000000000000000000000000000000	0.27576 •55540 1.02349 1.820552 1.81552 2.27652 3.168166 4.07527 6.29977 6.29977 9.059671 9.059672 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.052567 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05257 19.05577 19.05577 19.05577 19.05577 19.05577 19.05577 19.057	-0.002111 -0.002111 -0.002111 -0.002111 -0.22311 -0.22311 -0.256025 -1.556025 -1.556025 -1.556025 -1.556025 -1.556025 -1.556025 -1.556025 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.7520 -1.75200 -1.75200 -1.75200 -1.75200 -1.75200 -1.7520	-0.00018 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -0.000120 -	
	<u> </u>												
0.1512 .620805 1.02550442 1.02550442 1.02550442 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.02506 1.0250	-0.00090 -00024 -003778 -11109 -25811 -30697 -35828 -37939 -37939 -40305 -41498 -41992 -42139 -42139	0.19313 .361751 .361751 .466617 1.577568 .267757 1.577568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277568 .277	0.011/71 0.5802 0.7781 0.7781 0.7781 0.7781 0.7808 0.57772 0.4008 0.57772 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.4008 0.	0.1805689 354689 554689 6456689 845668 845668 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 94510 945100 945100 945100 945100 945100 9451000000000000000000000000000000000000	-0 -0 -0 -0 -0 -0 -0 -0 -0 -0	0.258 9258 9258 9258 9455425 1.24559230 1.2455923019 1.2455923019 1.2455923019 1.2455923019 1.2455923019 1.2455923019 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 1.255219 10	0.011/h 253956 253956 253956 253956 1.65754 2.13510 3.28775 7.77701 18.5127 7.77401 18.5127 28.71605 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,5265 285,526555 285,526555555555555555555555555555555555	0.124911 .24911 .49212 .829199 1.629199 1.629199 1.629161 1.429654 1.635455 1.635455 1.635455 1.635455 1.635455 1.635455 1.635455 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.745555 1.7455555 1.7555555 1.7555555 1.7555555 1.7555555 1.7555555 1.7555555 1.7555555 1.75555555 1.75555555 1.7555555 1.7555555 1.7555555 1.7555555 1.7555555555 1.75555555555	0.01273 .05987 .59728 1.95728 1.95728 1.95755 2.87470 8.40535 12.81935 12.81935 12.81935 12.81935 12.81935 12.81935 12.81935 12.81935 28.2677 29.266.28472 29.286.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 28.28472 29.28572 28.28472 29.28572 28.28472 29.28572 29.2972 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29725 29.29755 29.29755 29.29755 29.29755 29.297555 29.297555 29.297555 29.2975555555555555555555555555555555555	0.186755 -794267 -996675 1-199151 1-99151 1-99050 2-4909168 -1-99051 2-4909168 -1-99051 2-4909168 -1-99051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-49051 2-490512 2-	-0,001945 -0,001945 -11145 -11145 -420961 -420961 -420961 -140964 -1508040 -1508040 -1508040 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17759545 -17		
						Ж =	<u>10</u> 3						
0 100009119880 1124093050459 1124093050459 124093050459 124093050459 1000091 124093050459 1000091 12405455 1000091 12405455 1000091 12405455 1000091 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 12405455 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 1240555 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 124055 1240555 124055 1240555 124055 1240555 12405555 124	-0.00012 -00010 -000468 -00527 00148 -00527 02511 -02717 02885 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05009 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -05000 -00000000	0.05287 15269 15269 15269 15269 1561299 1.561299 1.561299 1.561299 1.561299 1.561299 1.561299 1.561299 1.561299 1.561299 1.561299 1.55615 1.91245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.591245 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.5915 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125 1.59125	0.00363 0.01451 0.074792 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07452 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.07552 0.075520 0.075520 0.075520 0.075520 0.075520 0.075520 0.075520 0.07552000000000000000000000000000000000	0.03296 .06591 .13131 .1085 .20988 .5199 .51772 .71037 .91972 .71103 .91972 .71122 283185 .238261 10.38054 31.14219	-0.00026 -000399 -00138 010702 010702 02851 031520 037821 035985 0403782 035985 0403782 035985 040378 04156 04156 04156	0.0353760 1353760 1353760 1353760 1353760 1353760 10056129 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.5561690 1.55616900 1.55616900 1.5561690000000000000000000000000000000000	0,00363 0011533 0077860 229509 88311540 1,25509 88311540 1,25598556 1,25598556 11,7585567 11,5598556 11,7585567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5885567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,598567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,5985567 15,598557 15,598557 15,598557 15,598557 15,598557 15,5985757 15,5985757 15,5985757 15,59857577 15,59857577 15,598575777 15,59857577777777777777777777777777777777	0.0438004 1159603 1159603 1159603 1159603 1159603 159703 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 159803 1598003 1598000000000000000000000000000000000000	0,003372 0014901 005314 -53488 -47689 -92539 -226415 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54387 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -54587 -5459	0.05745000135 50742000135 5074205953246008 1.13677405953246008 1.149515787570595 1.1495157875705 1.14951577374008 1.149515787400 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508 1.149508	-0.00036 -00128 -00523 -00584 -00523 -00584 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -0055 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00525 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -00555 -	0 .00003 .00061 .00080 .00372 .00538 .00538 .00538 .01373 .01373 .01322 .01373 .01322 .02555 .07645 .25019 .25019 .13105	
					•	¥ =	5	· . ·	•				
0 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 1207 120	-0.00000000000000000000000000000000000	0.0499864158360546054605 0.13628158360546054605 0.1362815836054505 0.13628158360545054605 0.1415115860 0.151158060 11115115860 11115115860 11115115860 11115115860 11115115860 11115115860 11115115860 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580 1111511580	0.00217 .00868 .01905 .19349 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .00387 .00387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387 .30387	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	-0.000530 -0002751 -0002751 -0002751 -0002751 -0002751 -0002751 -0002750 -0002750 -0002750 -0002750 -01028 -01058 -011026 -011252 -011252 -011252 -01154	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0.00843 0.00843 0.00853 1977200 82570120 82570120 12,5575121 12,557512 12,557512 11,25853 12,557512 11,25853 12,557512 11,25853 12,557514 11,25853 12,557514 12,25853 12,557514 12,25853 12,557514 12,25853 12,557514 12,25853 12,557514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,255514 12,2555514 12,255514 12,2555514 12,2555514	2005 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015 2015	0.000 000 000 000 000 000 000 000 000 0	144 2020 2020 2020 2020 2020 2020 2020 2	-0.00011 -00059 -000591 -000516 -013506 -02568 -02568 -02560 -05601 -05601 -056131 -05615 -155675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.50675 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1.5075 -1	0 .00001 .00010 .00053 .00058 .00059 .00145 .00215 .00141 .00551 .00551 .00551 .00551 .00551 .00551 .00551 .005563 .000568	

TABLE II .- VALUES OF FUNCTIONS USED IN FLUTTER CALOULATIONS - Concluded

NATIONAL ADVISORY COMMITTEE FOR AEROWAUTICS





Figure 3.- Sketch showing that only disturbances created forward of the Mach angle region with vertex at ξ_{ℓ} , can affect (x,y).



Figure 4.- Sketch illustrating the three degrees of freedom h, α , and β of the oscillating airfoil.

. .

Ξ

To 0.4 10 Δ •5 •6 0 8 6 4 2 ¢ $\frac{\omega_h}{\omega_a} = 0.707$ (a) $\frac{\omega_h}{\omega_a} = 0$ $\frac{\omega_{h}}{\omega_{a}} = 1.0$ (c) (Ъ) 0 30 -10 Ŵ 50 90 300 -10 10 20 40 50 0 10 20 30 50 40 60 70 80 0 Center-of-gravity location, percent chord NATIONAL ADVISORY (a) Measured from leading edge.(b) and (c) Measured from elastic axis. COMMITTEE FOR AERONAUTICS.

₹/bwa



NACA TN No. 1158

Fig. 5a-c

x_o 0.4 4 10 .5 0 0 ġ 8 6 **≭∕b**wa . 2 $\frac{\omega_{\alpha}}{\omega_{\alpha}} = 1.0$ (a) $\frac{\omega_h}{\omega_a} = 0$ <u>생</u>=0.707 (•) (Ъ) 0 40 50 20 30 50 40 50 90 100 -10 10 20 30 -10 0 10 40 60 70 80 0 Center-of-gravity location, percent chord NATIONAL ADVISORY (a) Measured from leading edge. COMMITTEE FOR AERONAUTICS. (b) and (c) Measured from elastic axis.



Fig. 6a-c

NACA TN No. 1158



Figure 7.- The flutter coefficient against center-of-gravity location for several positions of elastic axis and for three values of the frequency ratio. $M = \frac{10}{9}$; $\mu = 15.708$. NACA TN No. 1158

Fig. 7a-c





• •

• •

•

Fig. 8a-c

NACA TN No. 1158





Fig. 9a-c



and for three values of the frequency ratio. $M = \frac{10}{7}$; $\mu = 15.708$.

· · · ·

•

NACA TN No. 1158

Fig. 10a-c





Fig. 11a-c

ł.





.....

Fig. 12a-c



NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS.



Fig. 13a-c

NACA TN No. 1158

x_o 1.00 作业 = 0.99 △ 0**.4** 10 •5 0 Ō 4 = 0.87 **85**中占 41**.01** 8 <u>₩</u> = 0.71 .67 ≙ 6 1.43 72 -87 ₹∕bwæ 1.03 'n .650 1.17 .I .81 ۴ n 4 n 0.82 .64 .65 .97 .79 1.10/ 1.99 | •59 .83 .65 , .53 2 78 1.01 1.0000 $(a) \quad \frac{\omega_h}{\omega_\alpha} = 0$ (b) $\frac{\omega_h}{\omega_\alpha} = 0.707$ (•) $\frac{\omega_h}{\omega_q} = 1.0$ 0 80 10 20 30 50 -10 10 20 30 40 50 40 50 60 70 90 100 -10 40 0 0 NATIONAL ADVISORY Center-of-gravity location, percent chord (a) Measured from leading edge.(b) and (c) Measured from elastic axis. COMMITTEE FOR ABRONAUTICS.



Т.

.

. 1

i . I . NACA TN No. 1158

Fig. 14a-c





i.

NACA TN No. 1158

Fig. 15a-c -





COMMITTEE FOR AERONAUTICS.

Fig, 16a-c

.

NACA TN No. 1158







Fig. 17





ŗ

Figure 18.- The flutter coefficient against Mach number for several values of μ . Other parameters are $\frac{\omega_h}{\omega_{\pi}} = 0$; $\mathbf{x}_{\alpha} = 0.2$; $\mathbf{s} = 0$.

,

.. . .-





Figure 19.- The flutter coefficient against frequency ratio for several values of M. Other parameters are a = 0; $x_{\alpha} = 0.2$; $\mu = 7.854$.

...

•





• •

<u>*</u> . . .





Fig. 21

ł

j

è ļi.





111

.

NACA TN No. 1158

Fig. 22a-c