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TECHNICAL NOTE 4109

LOW-SPEED YAWED-ROLLING CHARACTERISTICS AND

OTHER ELASTIC PROPERTIES OF A PAIR OF

40-INCH-DIAMETER, 14-PLY-RATING,

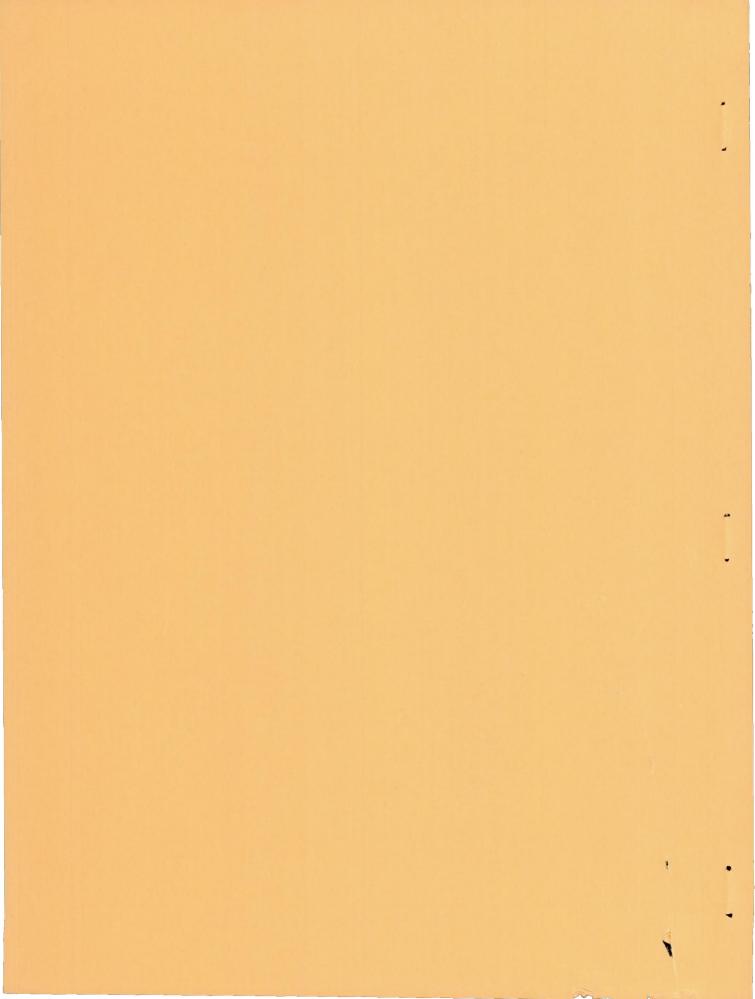
TYPE VII AIRCRAFT TIRES

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LOW-SPEED YAWED-ROLLING CHARACTERISTICS AND
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SUMMARY

The low-speed (up to 4 miles per hour) yawed-rolling characteristics of two 40 x 12, 14-ply-rating, type VII aircraft tires under straight-yawed rolling were determined over a range of inflation pressures and yaw angles for two vertical loadings. One load was approximately equal to the rated vertical load and the other load was approximately equal to twice the rated vertical load for these tires. Static tests were also performed to determine the vertical, lateral, torsional, and fore-and-aft elastic characteristics of the tires. The quantities measured or determined included lateral or cornering force, drag force, twisting moment or self-alining torque, pneumatic caster, vertical tire deflection, lateral tire distortion, wheel twist or yaw angle, rolling radius, and relaxation length. Some supplementary tests which included measurements of tire footprint area and the variation of unloaded tire radius and width with inflation pressure were made.

During straight-yawed rolling the normal force generally increased with increasing yaw angle within the test range. The pneumatic caster tended to decrease with increasing yaw angle. The sliding-drag coefficient of friction tended to decrease with increasing bearing pressure.

Measured lateral and torsional spring constants appeared to decrease with increasing amplitude of tire lateral distortion or twist, respectively.

INTRODUCTION

In order to cope with airplane landing and taxiing problems such as landings with yaw, wheel shimmy, and ground handling, designers of

landing gears must have reliable data on many elastic properties of airplane tires under such conditions. Until recently, the experimental data on such tire elastic properties, most of which are summarized and discussed in reference 1, were limited in both scope and quantity. Recently, a program was initiated by the National Advisory Committee for Aeronautics to alleviate this lack of experimental data by determining experimental values of some essential tire parameters for a range of tire sizes under static, kinematic (low-speed steady-state), and dynamic (transient and high-speed) conditions. Some static force-deflection tests of the program have been completed and the results were reported in reference 2. The low-speed yawed-rolling and some other elastic characteristics were reported in reference 3 for two 56-inch-diameter, 24-plyrating aircraft tires and in reference 4 for two 26-inch-diameter. 12-ply-rating aircraft tires. The present paper gives results from parts of the kinematic and static test programs for two 40-inch-diameter, 40 × 12, 14-ply-rating, type VII aircraft tires.

Most of the investigation consisted of towing the tire specimens along a straight path in a yawed condition. The angle-of-yaw range covered was from 0° to 24.5° and the inflation-pressure range was from about 74 pounds per square inch to 143 pounds per square inch. The two vertical-loading conditions investigated were 15,000 and 28,300 pounds per tire. The 15,000-pound vertical load represented approximately the rated load for this type of tire as specified by reference 5, whereas the 28,300-pound vertical load represented approximately twice the rated load. For each yawed-rolling run, the towing speed was held constant and did not exceed 4 miles per hour. The quantities measured or determined included vertical tire deflection, lateral force, drag force, self-alining torque, pneumatic caster, rolling radius, and relaxation length. Relaxation-length measurements were also obtained for the case of zero yaw for a standing and rolling tire.

Drag tests were conducted with the wheels locked to obtain measurements in the fore-and-aft direction of the maximum and sliding coefficients of friction and the stiffness of the tires for both wet- and dryconcrete conditions under a vertical load of approximately 9,100 pounds per tire.

Tests were performed on the standing tires to determine the static vertical-, lateral-, and torsional-elasticity characteristics. Some supplementary tests were also performed to measure tire footprint area and to determine the variation of the free-tire radius and width with tire inflation pressure.

SYMBOLS

Ag	gross footprint area, sq in.
An	net footprint area, sq in.
ъ	overall tire-ground contact width, in.
d	outside diameter of free tire, in.
F_R	resultant force, $\sqrt{F_x^2 + F_y^2}$, lb
F_{x}	instantaneous drag or fore-and-aft force (ground force parallel to direction of motion), lb
Fy	instantaneous cornering force (ground force perpendicular to direction of motion), lb
F_{Z}	vertical load on tire, lb
F_{ψ}	normal force (ground force perpendicular to wheel plane, F_{y} cos ψ + F_{x} sin $\psi),$ lb
2h	overall tire-ground contact length, in.
K _X	fore-and-aft spring constant, lb/in.
Ka	torsional spring constant, lb-in./deg
K_{λ}	lateral or side spring constant, lb/in.
L	relaxation length, in.
Lf	unyawed-rolling relaxation length, in.
Ls	static relaxation length, in.
Ly	yawed-rolling relaxation length, in.
$M_{ m Z}$	twisting moment or self-alining torque, lb-in.

N	cornering power (rate of change of cornering force with yaw angle for small yaw angles on a rolling tire, $dF_y,r,e/d\psi$
	or $dF_{\psi,r,e}/d\psi$ for ψ approaching 0), lb/deg
р	tire inflation pressure, lb/sq in.
Pb	minimum rated bursting pressure of tire, lb/sq in.
Po	tire inflation pressure at zero vertical load $(F_Z = 0)$, lb/sq in.
Pg	average gross footprint pressure, $F_{\rm Z}/A_{\rm g}$, lb/sq in.
p _n	average tire-ground bearing pressure, $F_{\rm Z}/A_{\rm n}$, lb/sq in.
q	pneumatic caster, $M_{z,r,e}/F_{\psi,r,e}$, in.
r	outside radius of free tire, $\frac{\text{Tire circumference}}{2\pi}$, in.
re	rolling radius, $\frac{\mathbf{v}}{\omega}$, in.
S	peripheral distance around tire, in.
v	rolling velocity, in./sec
W	maximum tire width, in.
x	displacement of wheel axle in direction of motion, in. or ft
δ	vertical tire deflection due to combined vertical and yaw loads, in.
δο	vertical tire deflection due to vertical load only, in.
η_{λ}	structural damping coefficient for lateral distortion
λ	lateral distortion of tire equator, in.
λο	lateral distortion of tire equator at center of contact, in.
μx,m	maximum drag coefficient of friction, $F_{X,n,m}/F_{Z}$

μx,s	sliding-drag coefficient of friction, $F_{\rm X}$,n,s/ $F_{\rm Z}$
μψ	yawed-rolling coefficient of friction, $F_{R,r,e,m}/F_{Z}$
Ψ	twist or yaw angle, deg
ω	wheel angular velocity, radians/sec
Subscripts:	
е	equilibrium or steady-state rolling condition
m	maximum
n	nonrolling condition
r	rolling condition
S	sliding condition

Bars over symbols denote the average values of the quantities involved for tires A and B.

APPARATUS

Test Vehicle

The basic test vehicle consisted of the fuselage and wing center section of a cargo airplane, which was towed tail-first by a tractor truck at such an attitude that the original airplane shock struts were nearly vertical. The original yokes and torque links of the landing-gear struts, along with the wheel assemblies, were replaced by steel wheel housings which held the tires and wheels tested. These steel wheel housings were connected together by means of an instrumented truss. Holes located in the wheel housing at angular intervals of 3.5° permitted the wheel frames to be rotated through a yaw-angle range of 0° to 24.5° toe out. A sketch of the basic test vehicle is shown in figure 1. A more detailed description of this test vehicle is given in reference 3 and applies in general to the present investigation.

For most of the tests the weight of the test vehicle was adjusted so that the vertical loading per tire was approximately 9,000 pounds, 15,000 pounds, or 28,000 pounds. The maximum towing force required was approximately 5,000 pounds per tire.

Instrumentation

The test vehicle was equipped with instruments for measuring lateral force, twisting moment (self-alining torque for the yawed-rolling case), drag, vertical tire deflection, horizontal translation, and wheel rotation. Measurements of these quantities were recorded simultaneously on a 14-channel recording oscillograph mounted in the test vehicle. This oscillograph was equipped with a 0.01-second timer. The instrumentation is discussed in detail in reference 3.

Tires

General description.— The tires used in this investigation were a pair of 40-inch-diameter, 40×12 , 14-ply-rating, type VII, rib-tread tires which were made by the same manufacturer. The specifications for these tires given in table I were obtained either from reference 5 or by direct measurements. Figure 2 shows inflated and deflated half cross sections of the two test tires. These cross sections were obtained from plaster casts taken at the end of the tests when the tires were in a worn condition. There is no appreciable difference between the profiles for the two tires.

Tire wear. - During the course of the present investigation, there was an appreciable progressive change in the cross-sectional shape of the tires due to skidding and working of the tires. Therefore, the chronological order in which the test data were collected may be of some importance in the interpretation of the data. This chronological order is indicated by a test series letter (A, B, C, D, E, or F) which is assigned to all data.

The change in tire-tread pattern due to tire wear during the tests is illustrated in figure 3. At the beginning of the tests the tread pattern of both tires had a rectangular cross section (fig. 3(a)). During test series B the sides of the treads in direct contact with the ground began to wear away, and this wearing away produced the tread shape shown in figure 3(b), which was taken at the end of test series B. During test series E this wear increased to the extent shown in figure 3(c).

Free-tire radius and width.— The hysteresis loops for free-tire radius and width plotted against inflation pressure are shown in figure 4 for tires A and B. The elapsed time from the start is shown for a few of the measurements presented. The variation in tire radius due to hysteresis for a given pressure is seen to be practically negligible (less than 0.2 inch) in the operating pressure range of these tires for this relatively slow rate of change of pressure. The corresponding change in width is about 0.1 inch. Also shown in this figure are several radius

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and width measurements which were made after the tires had been left unloaded at constant pressure for at least 24 hours in order to reach an equilibrium condition.

Test Surface

All yawed-rolling and drag tests were conducted by towing the test vehicle along the center of a 9-inch-thick reinforced-concrete taxi strip. This taxi strip had a slight crown so that the tires on the test vehicle were tilted (less than 1°) with respect to the surface. The taxi strip was a boarded concrete surface. Profiles of this concrete surface, indicating its roughness, are shown in both references 3 and 4. The test surface for the unyawed-rolling relaxation-length tests, the static lateral-elasticity tests, and most of the footprint-area measurements was a much smoother, level, reinforced-concrete hangar floor. The test surfaces for all other tests were steel plates.

TEST PROCEDURE AND EXPERIMENTAL RESULTS

The present investigation of tire characteristics is divided into the following parts: yawed-rolling tests, relaxation-length tests, locked-wheel drag tests, static vertical-elasticity tests, static lateral-elasticity tests, static torsional-elasticity tests, and supplementary measurements.

Yawed-Rolling Tests

For each of the yawed-rolling runs, the test vehicle was moved into towing position on the dry, clean, concrete taxi strip and the wheel housings were rotated and locked at the particular yaw angle desired. The tires were adjusted to the test inflation pressure and were then jacked clear of the ground to remove any residual stresses resulting from the previous runs or from the changing of the yaw angles of the wheels. The jacks were removed and the initial vertical tire deflections noted. The vehicle was then towed straight ahead, from this initial essentially unstressed condition, for a distance of approximately 40 feet. Although the speed remained approximately constant throughout any particular run, it varied from run to run within a speed range of approximately 0.7 to 4.0 miles per hour. Figure 5 shows tire B during a run at a yaw angle of 17.5°.

All runs at 0°, 3.5°, 7°, 10.5°, 14°, 17.5°, 21°, and 24.5° were made with both wheels symmetrically yawed with respect to the longitudinal axis of the test vehicle. Although these particular yaw angles

were the only angles easily attainable on the test vehicle, some test runs at 1.75° were made by yawing the wheels unsymmetrically with respect to the longitudinal axis of the test vehicle (that is, one wheel was set at an angle of 0° and the other at 3.5°). When towed ahead with these wheels unsymmetrically yawed, the test vehicle first veers off to the side because of the unsymmetrical forces. After a short distance, however, the vehicle runs smoothly with its longitudinal axis yawed with respect to the direction of motion so that both wheels have the same final intermediate yaw angle of 1.75° with respect to the direction of motion.

From the start of each run the measurements of lateral force, twisting moment or self-alining torque, drag force, vertical tire deflection, wheel rotation, and vehicle translation in the direction of motion were recorded continuously.

Tables II, III, and IV summarize all test data obtained during the final steady-state stage of the yawed-rolling runs and from a few supplementary runs to determine rolling radius at zero yaw. (The run numbers in the tables and figures do not indicate the chronological order in which the runs were made; they are listed only for convenience in referring to the test data.) In tables II, III, and IV, data are presented for three different test series (B, E, and F) which represent different vertical loadings. The variation of normal force $\overline{F}_{\psi,r,e}$, self-alining torque $\overline{M}_{z,r,e}$, and pneumatic caster \overline{q} with yaw angle is shown in figures 6 and 7 for all vertical loads and inflation pressures tested. The rolling radii are plotted in figure 8 as functions of tire inflation pressure and vertical tire deflection.

The buildup of cornering force with horizontal distance rolled during the initial stages of the yawed-rolling runs is illustrated in figure 9 for several inflation pressures and two vertical loadings. Inasmuch as for most runs there was a slight initial residual force or preload in the tires, the original test curves did not always pass exactly through the origin. The test curves shown in figure 9 have been horizontally shifted (if necessary) so that the extrapolation of each curve passes through the origin.

Relaxation-Length Tests

Three types of relaxation length were determined in this investigation, namely, static relaxation length $L_{\rm s}$, unyawed-rolling relaxation length $L_{\rm f}$, and yawed-rolling relaxation length $L_{\rm y}$. The definitions for these relaxation lengths are given in reference 3. The methods used to determine these relaxation lengths are as follows:

X

Static relaxation length $L_{\rm S}$.- The standing tires were given initial lateral deflections by pulling outward, by means of hydraulic rams, plates located underneath the tires. The lateral distortion of the center tire tread relative to the wheel center plane was then measured at several points around each tire circumference between the footprint edge and a point 180° from the center of contact.

Unyawed-rolling relaxation length $L_{\rm f}$. With the wheel housings positioned at 0° yaw, the tires were given initial lateral distortions by pulling outward on plates placed underneath the tires (as for the static relaxation length tests). The test vehicle was then rolled straight ahead for a distance of about 50 feet with the recording oscillograph making a continuous record of lateral force and horizontal translation.

Yawed-rolling relaxation length L_y . The basic data for the yawed-rolling relaxation lengths were obtained from the initial (force buildup) phase of the yawed-rolling tests. This relaxation length was evaluated for all runs except a few at large yaw angles for which tire skidding appeared to be too significant.

Relaxation-length data. Samples of the test data used to determine the three types of relaxation length for the tire specimens are shown in figure 10. This figure shows experimental data for three runs, plotted in both linear and semilogarithmic coordinates, together with empirical exponential curves which were obtained by fitting straight lines to these data on the semilogarithmic plots. The corresponding relaxation length for each set of data is, by definition, the denominator of the power of e in the equation of the exponential curve fitted to the data. (For example, the relaxation length for the data in figure 10(c) is 14.1 inches.) The values obtained in this manner from the test runs are listed in table V for the static-relaxation-length tests, in table VI for the unyawed-rolling relaxation-length tests, and in table II for the yawed-rolling relaxation-length tests.

Locked-Wheel Drag Tests

In order to determine tire stiffness and sliding drag in the fore-and-aft direction on dry concrete, the wheels were positioned at 0° yaw and locked to prevent rotation, and the test vehicle was pulled forward by hydraulic rams (see ref. 3) at a speed less than 10 inches per minute (0.009 mile per hour). A continuous record was taken of drag force and horizontal displacement during each run. In addition, several runs were made with the concrete surface wet. For these particular runs, the tires were jacked clear of the concrete surface immediately before a run and the concrete surface below each tire was wetted thoroughly with water by

means of a garden hose. The jacks were then removed and the run was conducted in the same manner as the dry-concrete runs. Throughout each wet-concrete run, a stream of water was directed onto the concrete surface in front of each tire so that the tires would always remain in contact with wet concrete.

During these tests, the weight of the test vehicle remained constant; however, the vertical load on the tires decreased slightly with increasing drag force as a consequence of the moment produced by the drag force. This change in vertical force was taken into account in the computation of friction coefficients. (It was not taken into account in the other tests, since the effect was small for those conditions.)

Most of the experimental data obtained from the locked-wheel drag tests are presented in table VII. Also, typical data are shown in figure 11 for the buildup of fore-and-aft force with horizontal distance pulled for several runs.

Static Vertical-Elasticity Tests

In the static vertical-elasticity tests the vertical loading on each tire was increased by increments from zero loading to a maximum value and was then reduced by increments to zero, the vertical tire deflection was noted for each value of vertical loading, and the unloaded-tire inflation pressure p_0 and loaded-tire inflation pressure p_0 were also measured. This procedure was followed for all test inflation pressures.

The static vertical-elasticity data obtained are presented in figure 12. This figure shows the variation of vertical loading with vertical tire deflection for the two tire specimens at the test inflation pressures.

Static Lateral-Elasticity Tests

In the static lateral-elasticity tests, the test vehicle was oscillated laterally through several cycles, at rates of 0.3 to 1.9 minutes per cycle, by means of double-acting hydraulic rams that were attached to the wheel axles and to the hangar floor. The amplitude of the lateral oscillation was kept approximately constant for successive cycles of each individual run, but was varied between 0.4 inch and 1.6 inches for different runs. The vertical tire deflection and tire inflation were measured prior to each run, and during the run the normal force and lateral tire distortion were recorded continuously on the oscillograph. This procedure was followed for several inflation pressures at both the 14,400-pound (series B) and the 28,300-pound (series E) vertical loadings.

The basic static lateral-elasticity test data are presented in figures 13 and 14 and table VIII. Figure 13 shows the variation of normal force with lateral tire distortion for several inflation pressures at an average vertical loading of 14,400 pounds for each tire (test series B). Figure 14 shows this variation at an average vertical loading of 28,300 pounds for each tire (test series E). Table VIII contains a list of all test conditions together with some tire lateral-stiffness and hysteresis parameters (to be discussed later) derived from the data in figures 13 and 14.

Static Torsional-Elasticity Tests

In the static torsional-elasticity test, steel turntables were placed beneath the wheels of the test vehicle. These turntables were rotated back and forth through several cycles, at rates of 0.5 to 1.9 cycles per minute, by means of double-acting hydraulic rams connected to each turntable. The amplitude of the torsional oscillation was kept approximately constant for successive cycles of each individual run, but was varied between 1.6° and 7.5° for different runs.

The vertical tire deflection and tire pressure were measured before each run. The twisting moment and turntable angular displacement were recorded continuously on the oscillograph during each run. This procedure was followed for several inflation pressures at both the 14,400-pound (series B) and the approximately 28,300-pound (series E) vertical loadings.

The basic static torsional-elasticity test data are shown in figures 15 and 16. Figure 15 shows the variation of twisting moment with twist angle for several inflation pressures at a vertical loading of 14,400 pounds for each tire (test series B). Figure 16 shows this variation at a vertical loading of approximately 28,300 pounds for each tire (test series E). Table IX contains a list of all test conditions, together with tire torsional-stiffness parameters obtained from figures 15 and 16.

Supplementary Measurements

In addition to the tests just described, some tire-contact or footprint-area measurements were made for the tire specimens at several inflation pressures and vertical tire deflections. For all runs except those of test series C these measurements were obtained from the imprint left on a piece of heavy paper placed between a chalked portion of the tires and a smooth concrete hangar floor. (For test series C a smooth steel plate was placed between tire and ground.) Several typical

imprints are shown in figure 17. The data obtained from the tire imprints are presented in table X.

PRECISION OF DATA

The instruments used in the tests and the methods of reducing the data are believed to yield results which are, on the average, accurate within the following limits:

Vertical load on tire, Fz, percent
Cornering force, Fy, percent ±
Force perpendicular to wheel plane (normal force) or lateral
force, F_{ψ} , percent
Drag force, F _x , 1b ±30
Self-alining torque or twisting moment, M_Z , lb-in $\pm 3,00$
Tire inflation pressure, po or p, lb/sq in ±
Outside radius of free tire, r, in ±0.0
Rolling radius, r_e , in
Horizontal translation in direction of motion, x, percent ±
Vertical tire deflection, δ_0 or δ , in
Lateral tire distortion, λ_0 or λ , in
Yaw angle or twist angle, ψ , deg

DISCUSSION OF PARAMETERS

Normal Force Fy,r,e

The variation of steady-state normal force with yaw angle, obtained from the test data in table II, is shown in figure 6 for approximately the rated vertical loading (\overline{F}_Z = 15,000 pounds, test series B), in figure 7 for approximately twice the rated vertical loading (\overline{F}_Z = 28,300 pounds, series E), and in figure 18 for both vertical loadings at two inflation pressures. These figures show that the normal force generally increased with increasing yaw angle within the test range. For the rated vertical loading (fig. 6), the normal force appeared to reach a maximum value at yaw angles between 17° and 25°; for approximately twice the rated loading (fig. 7), the normal force did not reach its maximum value within the tested yaw-angle range (up to 24.5°).

Cornering Force Fy,r,e

The steady-state cornering force follows substantially the trends that were described for the normal force, as is shown in figure 19 for two typical loading conditions.

Cornering Power N

The variation of cornering power with vertical tire deflection and inflation pressure for the two vertical loadings tested is shown in figures 20(a) and 20(b), respectively. These data, which were derived from the initial slope of the curves for the variation of normal force with yaw angle given in figures 6 and 7, indicate that, for constant vertical tire deflection, the cornering power increases with increasing inflation pressure and that, for constant inflation pressure, the cornering power decreases with increasing vertical tire deflection.

In order to compare the present test results for the 40-inch tires with the results of previous tests on other tires of the same general type (type VII; see ref. 5), cornering-power data from the present tests are compared in figure 21 with data for 56-inch-diameter tires from reference 3, for 26-inch-diameter tires from reference 4, and for 32- and 44-inch-diameter tires from reference 6. These data are presented in

the form of a plot of the dimensionless ratio $\frac{\overline{N}}{(\bar{p} + 0.11\bar{p}_b)\bar{w}^2}$ against

 $\frac{\delta_0}{\bar{r}}$, where \bar{p}_b is the minimum rated bursting pressure of the tire as taken from reference 5. (The form of these ratios is based on the results of a study of tire characteristics given in ref. 7.) From figure 21 it appears that the indicated cornering-power parameter is approximately the same for the different tires so that the cornering power for any tire of this type (type VII) can be estimated from the solid-line mean curve on the figure, with an error of less than ± 20 percent.

Self-Alining Torque $\overline{M}_{z,r,e}$

The variation of self-alining torque with yaw angle is shown in figures 6 and 7 for the two vertical loadings investigated. The self-alining torque generally increased with increasing yaw angle for small yaw angles and decreased with increasing yaw angle at large yaw angles. For constant vertical loading, the data indicate that increasing the inflation pressure tends to reduce the magnitude of the self-alining

torque at large yaw angles. In the case of constant inflation pressure, illustrated in figure 18, increasing the vertical loading increases the self-alining torque.

Maximum Self-Alining Torque $\overline{M}_{z,r,e,m}$

The variation of maximum self-alining torque with inflation pressure is shown in figure 22 for the two test conditions investigated. For constant vertical loading over the range of inflation pressures investigated, increasing the inflation pressure tends to decrease the maximum self-alining torque. For constant inflation pressure, the maximum self-alining torque increases with increasing vertical loading.

Pneumatic Caster
$$\bar{q} = \overline{M}_{z,r,e}/\overline{F}_{\psi,r,e}$$

The variation of pneumatic caster with yaw angle for all test conditions is shown in figures 6 and 7. These figures show that the pneumatic caster is at a maximum at small yaw angles and generally decreases with increasing yaw angle for the test range covered (up to 24.5° yaw). For constant inflation pressure, illustrated in figure 18, the pneumatic caster increases with increasing vertical load.

Drag Force Fx,r,e

The variation of steady-state (rolling condition) drag force with yaw angle for all conditions of the yawed-rolling test is shown in figure 23. These data show that the effect of inflation pressure on drag force for the two vertical loadings investigated is apparently small. In order to show trends more clearly, the ratio of drag force to cornering force $\overline{F}_{x,r,e}/\overline{F}_{y,r,e}$ is plotted against yaw angle for all test conditions in figure 24. If the total horizontal ground force during yawed rolling were normal to the wheel plane, the drag force $\overline{F}_{x,r,e}$ would be equal to the cornering force $\overline{F}_{y,r,e}$ multiplied by the tangent of the yaw angle, or $\overline{F}_{x,r,e}/\overline{F}_{y,r,e}=\tan\psi$. In figure 24, tan ψ is represented by the solid lines. Since the data do not usually fall along these lines, it appears that some force parallel to the wheel plane exists for most of the yaw-angle range investigated.

Yawed-Rolling Coefficient of Friction $\bar{\mu}_{\psi} = \bar{F}_{R,r,e,m}/\bar{F}_{z}$

The variation of yawed-rolling coefficient of friction with average bearing pressure or ground pressure is shown in figure 25 (square symbols), and the data are compared with corresponding data for 26-inch-diameter and 56-inch-diameter type VII tires (from refs. 3 and 4) in figure 26 (see unflagged symbols in fig. 26). From this comparison it appears that the data for the different tires are in fair agreement. (The fact that the coefficients are noticeably smaller for the 26-inch-diameter tires than for the other tires might be explained by consideration of possible experimental errors in the data for the 26-inch-diameter tires.)

Sliding-Drag (Fore-and-Aft) Coefficient of

Friction
$$\bar{\mu}_{X,S} = \overline{F}_{X,S}/\overline{F}_{Z}$$

The variation of sliding-drag coefficient of friction with average bearing pressure for both dry and wet concrete at the one vertical loading tested ($\overline{F}_{z}\approx 9,100~\text{pounds}$) is shown in figure 25. (See circle symbols.) These data are also listed in table VII. The sliding-drag coefficient of friction on dry concrete appears to decrease in magnitude with increasing bearing pressure. The friction coefficients found in the limited number of tests made on wet concrete tended to be slightly smaller than those found on dry concrete. Also shown in figure 25 for comparison purposes are the limited number of coefficient-of-friction values obtained from the yawed-rolling tests. (See square symbols.) A comparison of these data indicates that the sliding-drag coefficients of friction are in fair agreement with the corresponding yawed-rolling coefficients of friction.

Sliding-drag and yawed-rolling coefficients of friction obtained from tests on 56-inch and 26-inch tires (refs. 3 and 4) are compared with present test results in figure 26. The friction coefficients for the different tires are in fairly good agreement and show the same general trend. This general trend for all the data can be described by the empirical equation

$$\bar{\mu}_{\psi} = \bar{\mu}_{x,s} = 0.93 - 0.0011\bar{p}_{n}$$

where \bar{p}_n is in pounds per square inch. (See fig. 26.)

Maximum Drag Coefficient of Friction $\bar{\mu}_{x,m} = \bar{F}_{x,m}/\bar{F}_z$

The maximum drag force $\overline{F}_{x,m}$ at incipient slip is sometimes slightly larger than the drag force $\overline{F}_{x,s}$ required for steady sliding of the locked wheels and tires, as is shown in figure 11 for several typical runs. A comparison of maximum and sliding-drag coefficients of friction, presented in figure 27, indicates that the maximum drag coefficient of friction is rarely more than 3 percent greater than the sliding-drag coefficient of friction at the low speeds of these tests (less than 0.009 mile per hour).

Fore-and-Aft Spring Constant \overline{K}_{X}

The variation of fore-and-aft spring constant with tire inflation pressure, obtained from data in table VII for the one vertical loading investigated ($\overline{F}_{Z}\approx9,100$ pounds), is shown in figure 28. These data are derived from the initial slope of the curves for the variation of the fore-and-aft (drag) force \overline{F}_{X} with horizontal displacement \overline{x} . Samples of these curves for three test inflation pressures are presented in figure 11. For the one vertical loading tested, figure 28 indicates that the fore-and-aft spring constant increases slightly with increasing inflation pressure in the pressure range investigated.

Lateral Spring Constant \overline{K}_{λ}

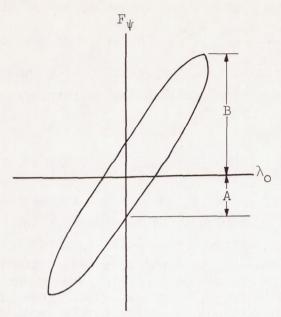
The variation of lateral spring constant with tire inflation pressure for the two vertical loadings tested is shown in figure 29(a). It may be seen from this figure that the lateral spring constant is approximately the same for both vertical loads tested and increases approximately linearly with increasing inflation pressure.

The effect of amplitude of lateral tire distortion on the spring constant may be seen from figures 14 and 29(b). The data in these figures indicate that the lateral spring constant, for any given inflation pressure and vertical load, decreases slightly with increasing lateral deformation.

Hysteresis Damping Coefficient for Lateral Deformation $\bar{\eta}_{\lambda}$

The experimental hysteresis damping data obtained from the static lateral-elasticity tests are presented in table VIII and figure 30 in terms of the conventional structural damping coefficient η_{λ} , which is

defined as the ratio of the maximum half-height of the corresponding force-deflection hysteresis loop to the maximum total force (that is, the ratio A/B in the sketch).



In figure 30 the hysteresis damping coefficient appears to decrease slightly with increasing inflation pressure for constant vertical load and to increase with increasing vertical load for constant inflation pressure.

Torsional Spring Constant K_{α}

The variation of static torsional spring constant $K_{\alpha,n}$ with tire inflation pressure for the two vertical loadings tested is shown in figure 31. The values of static spring constant shown in this figure (and in table IX) were obtained from the approximately straight-line portions of the curves in figures 15 and 16. From figure 31 it appears that the static torsional spring constants for the two tires are in fair agreement with each other. At constant pressure the static torsional spring constant increases with increasing vertical load.

The effect of amplitude of tire twist on the spring constant may be seen from figures 16 and 32. The data in these figures indicate that the static spring constant decreases appreciably with increasing amplitude of tire twist.

In figure 33 the static torsional spring constants $K_{\alpha,n}$ are compared with the corresponding spring constants $\overline{K}_{\alpha,r}$ obtained from the initial slopes of the self-alining-torque curves of figures 6 and 7 (that is, $\overline{K}_{\alpha,r} = \left(\frac{d\overline{M}_{Z,r,e}}{d\overline{\psi}}\right)_{\overline{\psi}\to 0}$). In figure 33 the torsional spring constants $K_{\alpha,r}$ obtained from the yawed-rolling tests appear to be about the same as or somewhat smaller than the corresponding static spring constants $K_{\alpha,n}$.

Footprint Area Ag or An

The variation of gross footprint area A_g , net footprint area A_n , and the ratio A_n/A_g with vertical tire deflection, obtained from data in table X, is shown in figure 34. Both A_g and A_n appear to increase nonlinearly with increasing vertical tire deflection for the deflection range covered. The ratio of net footprint area to gross footprint area appears to be approximately 75 percent of the gross footprint area. This ratio will, of course, change for tires having tread designs different from the ones tested.

Footprint Length 2h and Width b

The variation of footprint length 2h and width b with vertical tire deflection, obtained from data in table X, is shown in figure 35. Also shown in this figure as solid lines are the lengths of chords of circles having diameters equal to the free diameter d and maximum width w, respectively, of the tire at its rated inflation pressure and located at a distance $r-\delta_0$ from the center of the circles. A comparison of these quantities indicates that the experimental values of footprint width are approximately equal to the corresponding chord lengths, whereas experimental values of footprint length are usually smaller than the corresponding chord lengths for the vertical-tire-deflection range investigated.

Average Bearing Pressure $\bar{p}_n=\overline{F}_z/\overline{A}_n$ and Average Gross Footprint Pressure $\bar{p}_g=\overline{F}_z/\overline{A}_g$

The variation of average bearing pressure and average gross footprint pressure with tire inflation pressure is given in figure 36. The

data shown in this figure are derived from mean values of the curves given in figure 12 for the variation of vertical load with vertical tire deflection and from the faired curves given in figure 34 for the variation of footprint area with vertical tire deflection.

The solid line in figure 36 represents $\bar{p}_n = \bar{p}_g = \bar{p}$. Comparison of this line with the data for the average bearing pressure \bar{p}_n indicates that the average bearing pressure is appreciably greater than the inflation pressure and that it increases with increasing vertical deflection. The average gross footprint pressure p_g , however, is not greatly different from the inflation pressure for the inflation-pressure range covered.

Relaxation Length L

The variation of the three types of relaxation length with inflation pressure at two vertical loadings is shown in figure 37. For a given vertical loading the static relaxation length usually appears to be the largest of the three types of relaxation length and the yawed-rolling relaxation length appears to be the smallest. All three types of relaxation length appear to decrease with increasing vertical load and are relatively independent of inflation pressure.

Rolling Radius re

The variation of rolling radius with inflation pressure for the three vertical loadings investigated is shown in figure 8(a). The data presented in this figure were obtained from table III and are for essentially unyawed conditions. In order to show more clearly the trends of these data, the effect of inflation pressure has been isolated in figure 8(b), where rolling radius is plotted against vertical tire deflection for several constant inflation pressures. Figure 8(b) shows that, for constant inflation pressure, the rolling radius decreases with increasing vertical tire deflection and, for constant vertical tire deflection, the rolling radius increases slightly with increasing inflation pressure. Similar variations were observed in references 3 and 4 for 56-inch-diameter and 26-inch-diameter tires.

CONCLUSIONS

Tow tests were made primarily to determine the low-speed yawed-rolling characteristics of two 40×12 , 14-ply-rating, type VII aircraft tires at two vertical loadings which were approximately equal to the

rated vertical loading and twice the rated vertical loading for these tires. The results of these tests indicated the following primary conclusions:

- 1. The normal force generally increased with increasing angle of yaw within the test range $(0^{\circ} \text{ to } 24.5^{\circ})$.
- 2. The cornering power, under constant inflation pressure, decreased with increasing vertical tire deflection for the two vertical loadings investigated. For the case of constant vertical tire deflection, increasing the vertical loading increased the cornering power.
- 3. The self-alining torque generally increased with increasing angle of yaw for small angles of yaw and decreased with increasing angle of yaw at large angles of yaw.
- 4. The pneumatic caster generally decreased with increasing angle of yaw for the test range covered.
- 5. The sliding-drag coefficient of friction decreased with increasing bearing pressure; and at comparable bearing pressures, both the sliding-drag and yawed-rolling coefficients of friction followed approximately the same trends and magnitudes that were reported for 56-inch-diameter and 26-inch-diameter tires in NACA Technical Notes 3235 and 3604.
- 6. The static torsional spring constant, for a given vertical load and inflation pressure, decreased appreciably with increasing amplitude of tire twist.

Langley Aeronautical Laboratory,
National Advisory Committee for Aeronautics,
Langley Field, Va., July 24, 1957.

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TABLE I.- TIRE SPECIFICATIONS

Specifications	Military specification (ref. 5)	End of test, tires in worn condition		
	(ref.))	Tire A	Tire B	
Tire:	Part of Line 1			
Type ^a Ply rating Static load, 1b Inflation pressure, 1b/sq in. Burst pressure, 1b/sq in. Moment of static unbalance, oz-in. Diameter, deflated, in. Diameter, inflated, in. Maximum width, deflated, in. Maximum width, inflated, in. Bead width, in.	VII 14 14,500 95 380 (min.) 40 (max.) 40 (max.) 39.70 (min.) 39.70 (min.) 11.70 (min.) 12.35 (max.) 2.38 (max.)	38.00 39.16 11.80 }12.12 1.60	39.10 39.30 11.80 12.12 1.67	
Minimum wall thickness, in. Wall thickness at tread center line (including tread), in. Depth of tread (at tread center line), in. Casing weight, lb Tread pattern	0.29 (min.) 95 (max.) Rib	0.50 0.83 0.34 85 Rib	0.52 0.80 0.34 85 Rib	
Inner tube: Thickness, in		0.1	0.1	
Wheel: Rim diameter, in		21.00	21.00	

^aType VII is an extra-high-pressure tire.

TABLE II.- YAW TEST DATA

(a) Series B; \overline{F}_Z = 15,000 pounds

Run	po, lb sq in.	\bar{p} , $\frac{1b}{\text{sq in.}}$	$\bar{\delta}_{o}$, in.	$\bar{\delta}$, in.	Ψ, deg	F̄y,r,e,	F _{x,r,e} ,	$\overline{F}_{\psi,r,e}$,	$\overline{M}_{z,r,e}$, lb-in.	q, in.	L _y ,
1 2 3 4 5 6 7 8 9	74 74 74 74 74 74 74 74 74 75	79 77 78 78 78 78 77 78	3.4 3.4 3.5 3.5 3.5 5.5 5.5 5.5 5.5	3.5 3.6 3.7 3.7 3.9 4.6 4.6 4.8	1.75 3.5 7.0 7.0 10.5 14.0 17.5 21.0 24.5	1,240 2,440 4,590 4,520 6,410 8,110 9,370 9,900 10,400	200 300 1,000 900 1,600 2,300 3,200 3,800 4,100	1,240 2,450 4,670 4,590 6,590 8,440 9,900 10,600 11,160	12,100 20,100 21,300 23,700 25,600 23,700 21,600 12,600 14,000	9.72 8.20 4.57 5.17 3.88 2.81 2.18 1.19 1.25	(a) 11.5 12.8 14.1 (b) (b) (b) (b)
10 11 12 13 14 15 16 17 18	93 93 92 93 93 93 93 95 93 95	97 98 97 97 96 97 98 97 98	2.9 3.0 3.0 3.0 2.9 3.0 3.0 3.0 3.0	2.9 3.1 3.2 3.4 3.7 3.7 3.9	1.75 3.5 7.0 7.0 10.5 14.0 17.5 17.5 21.0 24.5	1,500 2,970 5,840 5,580 7,940 9,480 10,760 10,120 10,620 10,510	200 200 1,000 700 1,700 2,300 3,400 3,100 3,900 4,400	1,510 2,980 5,920 5,620 8,110 9,760 11,290 10,600 11,310 11,380	10,100 17,900 25,400 24,200 20,900 16,600 15,700 19,000 7,500	6.66 6.00 4.29 4.31 2.57 1.70 1.39 1.79 .67	(a) 12.7 12.2 12.4 (b) (b) (b) (b) (b) (b)
20 21 22 23 24 25 26 27	113 113 113 113 113 113 113 113	116 116 116 115 115 119 116 118	2.6 2.6 2.6 2.7 2.6 2.7 2.7	2.6 2.7 3.0 2.9 3.2 3.1 3.2 3.2	1.75 3.5 7.0 10.5 14.0 17.5 21.0	1,850 3,470 6,260 8,610 10,310 10,810 10,440 10,250	100 200 900 1,800 2,500 3,000 3,100 3,600	1,850 3,480 6,320 8,790 10,600 11,210 10,880 10,870	12,900 18,900 23,700 19,800 15,500 14,100 12,900 5,300	6.96 5.44 3.74 2.25 1.47 1.26 1.18	(a) 13.1 (a) (b) (b) (b) (b) (b)
28 29 30 31 32 33 34 35 36	133 133 133 133 132 132 130 133 132	134 135 135 134 135 134 132 134 134	2.3 2.4 2.4 2.4 2.4 2.4 2.4 2.4 2.4	2.4 2.6 2.6 2.7 2.6 2.7 2.6 2.7	1.75 3.5 7.0 7.0 10.5 14.0 17.5 17.5 21.0	2,020 4,070 7,100 7,150 9,550 10,540 (a) 11,090 10,470	100 200 1,100 1,100 1,900 2,400 3,100 3,300 3,600	2,020 4,080 7,180 7,230 9,730 10,810 (a) 11,560 11,080	10,000 19,200 21,700 15,700 17,600 11,800 (a) 13,800 5,800	4.95 4.70 3.02 2.17 1.81 1.09 (a) 1.19 .53	13.2 14.2 (a) 13.9 (b) (b) (b) (b) (b)

^aValue could not be accurately determined.

bValue not determined.

TABLE II. - YAW-TEST DATA - Concluded

(b) Series E; \overline{F}_Z = 28,300 pounds

Run	\bar{p}_{0} , 1b sq in.	p, lb sq in.	$\bar{\delta}_0$, in.	δ, in.	Ψ, deg	Fy,r,e,	F _{x,r,e} ,	Ψ̄ _{ψ,r,e} ,	$\overline{M}_{z,r,e}$, lb-in.	ā, in.	\overline{L}_y , in.
37 38 39 40 41 42 43 44 45 46	95 95 95 95 95 95 95 95 95	104 105 105 105 105 105 105 105 105	5.2 5.1 5.1 5.1 5.1 5.1 5.2 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5	5.3 5.5 5.5 5.5 5.5 5.5 5.5 5.5 6.5 6.5	1.75 1.75 3.5 7.0 7.0 10.5 10.5 14.0 17.5	1,100 1,020 1,860 1,860 3,200 3,400 5,020 4,960 6,880 8,590	700 300 800 700 1,100 1,400 2,500 2,200 3,600 4,700	1,120 1,030 1,910 1,900 3,310 3,550 5,390 5,280 7,550 9,610	11,600 12,900 22,700 19,800 43,300 41,600 55,000 58,100 52,200 54,200	10.36 15.52 11.88 10.42 13.08 11.72 10.20 11.00 6.91 5.64	(a) (a) 8.9 (a) 7.8 (a) 8.6 8.2 10.1 (b)
47 48 49 50 51 52 53 54 55	115 115 115 115 115 115 115 115	125 124 122 125 124 124 125 125 124	44444444	5.0 5.4	14.0 14.0 17.5	1,340 2,490 4,910 4,760 7,040 8,880 9,680 11,530 10,850	100 800 1,300 1,500 2,400 3,700 3,600 4,800 4,900	1,340 2,530 5,030 4,910 7,360 9,510 10,260 12,440 11,820	12,200 23,800 49,900 43,000 48,100 45,900 52,700 52,200 45,900	9.10 9.41 9.92 8.76 6.54 4.83 5.14 4.20 3.88	8.6 10.5 (a) (a) 10.1 (b)
56 57 58 59 60 61 62 63	135 135 135 135 135 135 135	142 143 142 143 141 143 143	4.0	4.0 4.1 4.1 4.2 4.4	1.75 3.5 7.0 7.0 10.5 14.0	1,470 1,430 2,910 5,790 5,730 8,770 11,530 13,900	100 100 400 1,400 1,500 2,300 3,700 5,000	1,470 1,430 2,930 5,920 5,870 9,040 12,080 14,760	12,100 9,400 24,700 49,500 44,000 45,500 42,100 35,900	8.23 6.57 8.43 8.36 7.50 5.03 3.49 2.43	7.5 11.6 13.1 9.5 12.1 12.4

aValue could not be accurately determined.

b_{Value} not determined.

X

TABLE III.- ROLLING-RADIUS DATA FOR SMALL YAW ANGLES

				Tire A					Tire B					
Run	Test	ψ, deg	p _o , lb sq in.	p, lb sq in.	F _z ,	δ_0 , in.	r _e ,	r,	p _o , <u>lb</u> sq in.	p, <u>lb</u> sq in.	F _z , lb	δ_0 , in.	r _e ,	r, in.
64 65 66 67	B B B	0 0 0	74 93 113 133	77 96 115 134	14,900 14,900 14,900 14,900	3.0	17.8 18.0 18.3 18.5	(a)	74 93 113 133	77 96 115 135	15,000 15,000 15,000 15,000	2.9	18.1	(a) (a) (a) (a)
68 69 70 71 72 73 74	E E E E E E	0 1.75 0 1.75 0 1.75	115 115 135 135	105 104 124 124 143 142 142	28,400 28,400 28,400 28,400 28,400 28,400 28,400	5.2 4.5 4.0 4.0	17.9 18.1 18.1	(a) (a) (a) (a) (a)	95 95 115 115 135 135	105 104 124 125 143 142 143	28,200 28,200 28,200 28,200 28,200 28,200 28,200	5.2 4.5 4.0 4.0	17.9 18.1 18.1	(a) (a) (a) (a) (a) (a) (a)
75 76 77	F F	0	75 95 125	77 97 126	(b) (b) (b)	2.1	18.5	19.61 19.65 19.70	95	78 97 114	(b) (b) (b)	2.1	18.5	19.60 19.64 19.66

avalue not measured.

TABLE IV.- PARAMETERS EVALUATED FROM YAW-TEST DATA

Runs	Test	\bar{p}_{0} , lb sq in.	p, lb sq in.	$\bar{\delta}_0$, in.	F _z ,	N̄, lb/deg	Ka,r, lb-in. deg	M _{z,r,e,m} , lb-in.	F _{ψ,r,e,m} ,	μψ
1 to 9 10 to 19 20 to 27 28 to 36	B B B	74 93 113 133	78 97 116 134	3.5 3.0 2.6 2.4	15,000 15,000 15,000 15,000	680 860 970 1,140	(b) (b) (b) (b)	25,000 24,000 23,000 22,000	(b) 11,400 11,100 11,300	(b) 0.76 .74 .75
37 to 46 47 to 55 56 to 63	E E E	95 115 135	105 124 142	5.2 4.5 4.0	28,300 28,300 28,300	515 715 850	6,100 6,700 7,000	56,000 51,000 49,000	(b) (b) (b)	(b) (b) (b)

aOnly approximate values of pressure and vertical deflection are listed in this table. All listed maximum values of force and moment were established with the aid of the faired curves in figures 6 and 7.

bBetween 9,000 and 10,000 pounds.

bValue could not be accurately determined.

TABLE V .- STATIC RELAXATION-LENGTH DATA

		F 100	tot all	Tire A			Tire B				
Run	Test series	p _o , lb sq in.	p, <u>lb</u> sq in.	F _Z ,	δ_0 , in.	L_s , in.	p _o , lb sq in.	p, 1b sq in.	F _z ,		L_{S} , in.
78 79 80 81 82	B B B B	74 93 93 113 133	78 97 100 116 (b)	14,400 14,400 14,400 14,400 14,400	3.2 3.3 2.5	15.5	74 93 93 113 133	78 97 95 119 (a)	14,400 14,400 14,400 14,400 14,400	3.5 3.3 2.6	(a) (a) 16.5 16.1 14.3
83 84 85 86	E E E	96 95 115 134	105 105 125 140	28,400 28,400 28,400 28,400	4.9	15.5	115	104 104 124 140	28,200 28,200 28,200 28,200	5.0	14.7

aValue could not be accurately determined.

TABLE VI.- UNYAWED-ROLLING RELAXATION-LENGTH DATA

Rur	Test series	$\frac{\bar{p}_{0}}{\text{sq in.}}$	p, lb sq in.	F _z ,	$\bar{\delta}_0$, in.	$\overline{L}_{f},$ in.
8° 88 89 90 92	B B B B B B B B B B B B B B B B B B B	(a) (a) (a) (a) (a) (a)	75 75 95 115 135 135	14,400 14,400 14,400 14,400 14,400 14,400	3.3 3.4 3.0 2.7 2.4 2.3	14.4 14.7 15.0 15.4 16.3 15.0
93	5 E	135	142	28,300	4.1	9.0

aValue not measured.

bValue not measured.

TABLE VII.- LOCKED-WHEEL DRAG-TEST DATA

Test series D: \overline{F}_z = 9,390 pounds for \overline{F}_x = 0; \overline{F}_z \approx 9,100 pounds for all values of \overline{F}_x in this table

Run	po, lb sq in.	p, lb sq in.	$\bar{\delta}_0$, in.	F _{x,n,m,}	F _{x,n,s,}	μ̃χ,m	ū̄ _{χ,s}	\overline{K}_{X} , $\frac{1b}{in}$.	Remarks
94	35	38	3.7	7,530	7,530	0.83	0.83	2,700	Dry concrete
95 96 97	45 45 45	47 48 48	3.2 3.3 3.1	7,680 6,880 7,190	7,680 (a) (a)	.84 .76 .79	.84 (a) (a)	2,800 2,800 2,700	}Dry concrete Wet concrete
98 99 100	60 63 60	63 64 62	2.7	7,000 7,400 7,160	(a) 7,370 (a)	.77 .81 .79	(a) .81 (a)	3,100 3,100 3,000	}Dry concrete Wet concrete
101	75 75	76 76	2.3	7,330 6,800	7,250 6,800	.81	.80	3,400 3,200	Dry concrete
103 104 105	82 81 81	84 82 83	2.3	6,770 6,630 6,840	6,700 6,550 6,810	.74 .73 .75	.74 .72 .75	3,400 3,400 3,800	Dry concrete Wet concrete
106	92	93	2.1	7,090	6,900	.78	.76	3,600	Dry concrete
107 108 109 110	97 97 97 101	98 98 98 102	2.1 2.0 2.0 2.0	6,670 6,320 6,710 7,100	6,670 6,290 6,620 6,920	.73 .69 .74 .78	.73 .69 .73	3,400 3,400 3,400 3,700	Dry concrete Wet concrete Dry concrete
111	110	111	1.9	6,740	6,550	.74	.72	3,500	Dry concrete
112	120 120	121 121	1.9	7,000 7,340	(a) (a)	.77 .81	(a) (a)	(a) 3,600	Dry concrete
114 115 116 117	124 124 124 127	125 124 124 128	1.8 1.8 1.8	6,530	6,550 6,390 6,220 6,310	.72 .72 .72 .73	.72 .70 .68 .69	3,600 4,100 3,600 3,600	}Dry concrete }Wet concrete
118	134	135	1.7	7,010	6,500	.77	.71	3,700	Dry concrete

aValue could not be accurately determined.

TABLE VIII.- STATIC LATERAL-ELASTICITY TEST DATA

Run	Test series	F _z ,	po, lb sq in.	p, lb sq in.	$\bar{\delta}_{o}$, in.	\overline{K}_{λ} , lb/in.	$\bar{\eta}_{\lambda}$	λ _{o,max} , in.	Minutes per cycle
119	ВВ	14,400	75 75	(a) (a)	3.3 3.3	1,850 1,820	0.10	1.5	0.7
121	В	14,400	95	(a)	2.8	2,360	.10	1.3	.4
122	В	14,400	115	(a)	2.6	2,640	.07	1.2	.4
123 124	B B	14,400	135 135	(a) (a)	2.3	2,840 3,280	.08 (b)	1.1	.4
125 126	E E	28,300 28,300	95 95	105 105	5.0	2,340 2,200	.14	.7 1.6	1.3
127 128	E E	28,300 28,300	115 115	124	4.3	2,750 2,500	.12	.7 1.4	1.3
129 130 131 132 133 134	E E E E E	28,300 28,300 28,300 28,300 28,300 28,300	135 135 135 135 135 135	142 142 142 142 142 142	3.8 3.8 3.8 3.8 3.8	3,530 3,530 3,670 3,160 3,170 2,970	.11 .07 .08 (b)	.4 .5 .7 .9 1.0	1.1 1.2 1.4 1.4 1.3

aValue not determined.

TABLE IX .- STATIC TORSIONAL-ELASTICITY TEST DATA

	_ rule		Tire A						Tire B						
Run	Test series	Minutes per cycle	F _Z ,	p _o , lb sq in.	p, lb sq in.	δ_0 , in.	Ψ _{max} , deg	Ka,n, lb-in. deg	F _z ,	p _o , lb sq in.	p, lb sq in.	δ_0 , in.	Ψ _{max} , deg	Ka,n, lb-in. deg	
135	В	0.7	14,400	(a)	b75	3.2	3.7	5,750	14,400	(a)	b75	3.3	4.1	4,850	
136	В	.6	14,400	(a)	b75	3.2	4.8	4,620	14,400	(a)	b75	3.3	4.6	4,970	
137	В	.5	14,400	(a)	b95	2.8	4.4	4,150	14,400	(a)	b95	2.8	4.1	4,310	
138	В	.6	14,400	(a)	b ₁₁₅	2.5	4.9	3,730	14,400	(a)	b ₁₁₅	2.5	4.2	4,030	
139	В	1.2	14,400	(a)	b134	2.2	4.2	3,550	14,400	(a)	b ₁₃₂	2.3	3.9	3,860	
140	В	.5	14,400	(a)	b ₁₃₅	2.3	4.4	3,600	14,400	(a)	b ₁₃₇	(a)	4.3	3,600	
141 142 143 144	E E E	.6 .7 1.2 1.2	28,400 28,400 28,400 28,400	95 95 95 95	105 104 105 105	5.1 5.1 4.9 5.0	1.8 3.2 5.1 7.4	9,520 7,740 6,950 6,450	28,200 28,200 28,200 28,200	95	105 104 105 105	5.1 5.1 4.9 4.9	1.8 3.2 5.2 7.0	9,350 7,810 7,400 6,860	
145 146 147 148 149	E E E E	.7 1.0 1.6 1.9	28,400 28,400 28,400 28,400 28,400	115 115 115 115 115	125 125 124 125 125	4.3 4.3 4.3	3.5 5.4 7.5	8,700 7,350 6,740 6,900 6,500	28,200 28,200 28,200 28,200 28,200	115 113 115 115 115	124 123 123 125 125	4.4 4.3 4.3 4.3 4.3	1.8 3.4 5.6 7.1 7.1	9,160 7,280 7,100 6,970 6,500	
150 151 152 153	E E	.8 1.1 1.1 1.5	28,400 28,400 28,400 28,400	135 135 135 135	142 142 142 142	3.9 3.9 3.9 3.8	3.6	9,000 7,240 6,450 6,080	28,200 28,200 28,200 28,200	135 135	142 142 141 140	3.9 4.0 3.9 3.8	3.6 5.1	9,330 7,240 6,500 6,160	

aValue not determined.

bValue could not be accurately determined.

 $^{^{\}mathrm{b}}\mathrm{May}$ be as much as 10 lb/sq in. too low.

TABLE X.- TIRE FOOTPRINT DATA

(a) Tire A

Run	Test	p _o , lb sq in.	p, lb sq in.	F _z ,	δ_0 , in.	Ag, in.2	A _n , in.2	b, in.	2h, in.	Remarks
154 155 156 157 158 159 160 161 162 163 164 165 166 167	A A A A A A A A A A A A A A A A A A A	37 37 57 77 97 (a) 34 54 59 74 83 93 98 108 129	(a) (a) (a) (a) (a) (a) 37 38 58 63 75 84 97 99 113	(b)	3.20 3.22 2.59 2.03 1.90 3.28 3.08 2.34 2.48 2.05 2.11 1.87 1.98 1.69	172 177 128 105 90 180 172 129 139 115 108 88 92 80 72	130 133 100 82 68 139 130 98 106 88 84 68 72 61	10.3 10.6 10.0 9.4 8.5 10.7 10.6 10.0 10.5 9.4 8.4 8.6 7.8	17.9 18.0 15.6 14.1 13.5 17.9 15.7 15.1 14.5 13.8 13.8	(c) (c) (c) (c) (d) (d) (d) (d) (d) (d) (d) (d) (d) (d
169 170 171 172	B B B	75 96 115 134	80 98 119 135	14,900 14,900 14,900 14,900	3.31 2.83 2.46 2.30	168 148 131 120	128 112 98 92	10.7 10.4 10.1 9.8	18.0 16.6 15.8 15.3	
173 174 175 176 177	0000	95 95 95 95 95	(a) (a) (a) (a) (a)	27,670 21,050 14,830 9,290 3,520	5.07 3.97 3.02 2.07 1.00	234 186 139 91 37	(e) (e) (e) (e)	12.0 11.3 10.4 8.5 5.0	21.6 18.9 16.1 13.3 8.9	r = 19.64 in.; w = 12.20 in.
178 179 180 181 182 183 184	D D D D D	35 45 60 83 98 124 132	(a) 48 63 85 99 125	9,390 9,390 9,390 9,390 9,390 9,390 9,390	3.72 3.08 2.48 2.06 1.97 1.79	(e) (e) (e) (e) (e) (e)	151 124 97 83 77 63 60	(e) (e) (e) (e) (e) (e)	(e) (e) (e) (e) (e) (e) (e)	(d) (d) (d) (d) (d) (d)
185 186 187 188	E E E	95 95 95 95	(a) (a) (a) (a)	28,320 21,550 15,540 9,170	5.12 4.02 3.03 2.00	244 197 154 99	180 147 (e) (e)	11.9 11.2 10.6 9.1	22.6 19.9 17.2 13.8	r = 19.61 in.; W = 12.21 in.

avalue not measured.

bBetween 9,000 and 10,000 pounds.

conly approximate values of pressures listed.

dFlat spot developed on tire for most of these runs.

e_{Value} not determined.

TABLE X.- TIRE FOOTPRINT DATA - Concluded

(b) Tire B

Run	Test series	p _o , lb sq in.	p, lb sq in.	F _z ,	δ ₀ , in.	Ag, in. ²	A _n , in. ²	b, in.	2h, in.	Remarks
189 190 191 192 193 194 195 196 197 198 199 200 201 202 203	A A A A A A A A A A A A	37 37 57 77 96 34 36 55 59 74 83 93 98 108 (a)	(a) (a) (a) (a) (a) (a) 38 37 58 63 76 85 97 100 113	(b)	3.12 3.23 2.56 (a) 1.88 3.12 3.43 2.34 2.51 2.21 2.08 1.81 1.93 1.66	176 134 109 94 173 182 134 139 109 108 91 92 81	136 134 101 83 71 131 138 100 106 83 83 69 71 61 55		15.9 14.3 13.6 18.0 15.9 16.1 14.6 14.5 13.6 13.8	(c) (c) (c) (c) (d) (d) (d) (d) (d) (d) (d) (d) (d) (d
204 205 206 207	B B B	75 94 115 135	81 96 119 138	15,000 15,000 15,000 15,000	3.23 2.96 2.54 2.25	151	130 114 98 90		17.0 15.9	
208 209 210 211 212 213 214	D D D	35 45 60 81 98 124 133	38 48 61 84 99 125 134	9,390 9,390 9,390 9,390 9,390 9,390	2.30 2.15 1.89	(e) (e) (e) (e)	151 129 103 85 77 64 62	(e) (e) (e) (e) (e) (e)	(e) (e) (e) (e) (e) (e)	(d) (d) (d) (d) (d) (d) (d)
215 216 217 218	E E	85 85 95 95	(a) (a) (a) (a)	28,190 21,100 14,720 8,780	4.37	144	186 152 (e) (e)	12.0 11.3 10.3 8.5	20.2	r = 19.62 in.; w = 12.17 in.

aValue not measured.

bBetween 9,000 and 10,000 pounds.

^cOnly approximate values of pressures listed.

dFlat spot developed on tire for most of these runs.

eValue not determined.

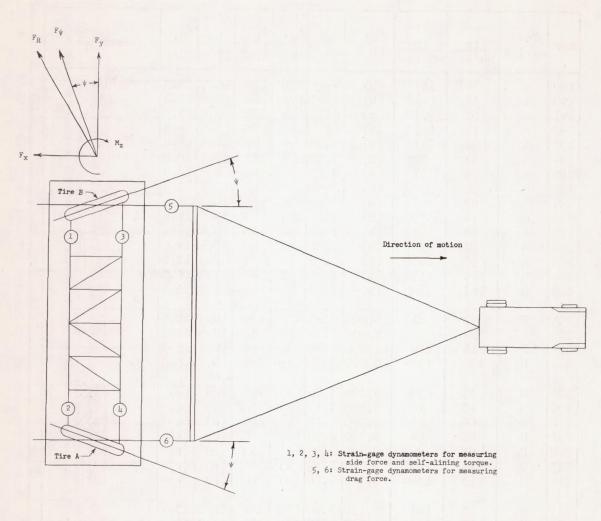


Figure 1.- Sketch of test vehicle.

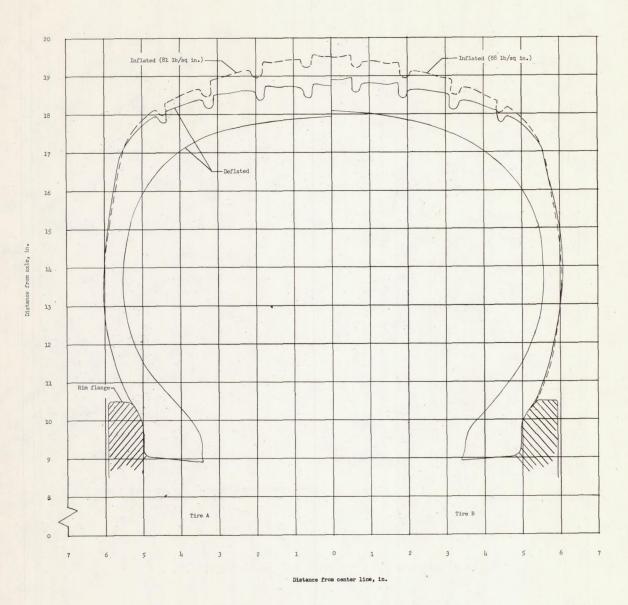
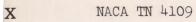
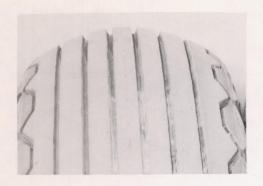


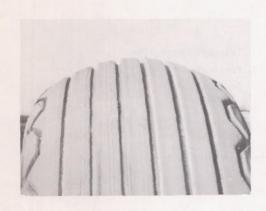
Figure 2. - Tire profiles.





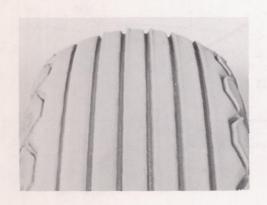


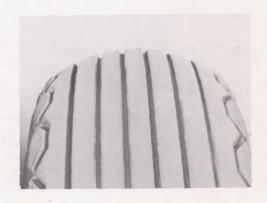
(a) At beginning of test.





(b) At conclusion of test series B.





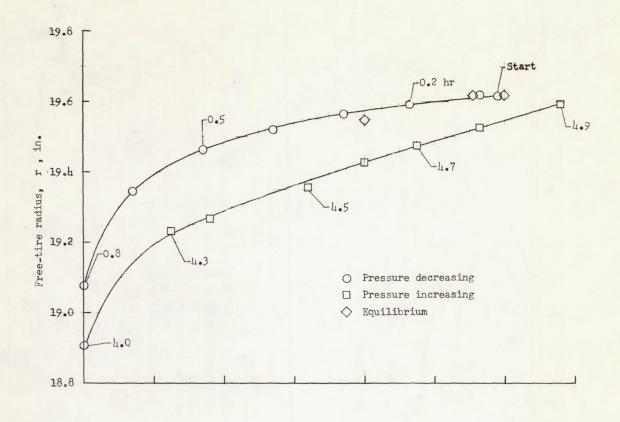
(c) At conclusion of test series E.

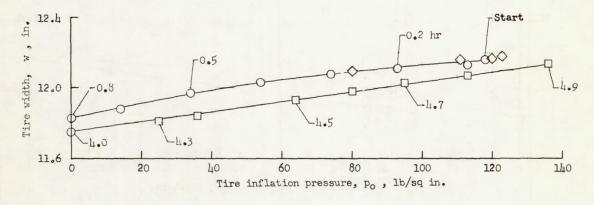
L-57-2726

Tire A

Tire B

Figure 3. - Tire wear.

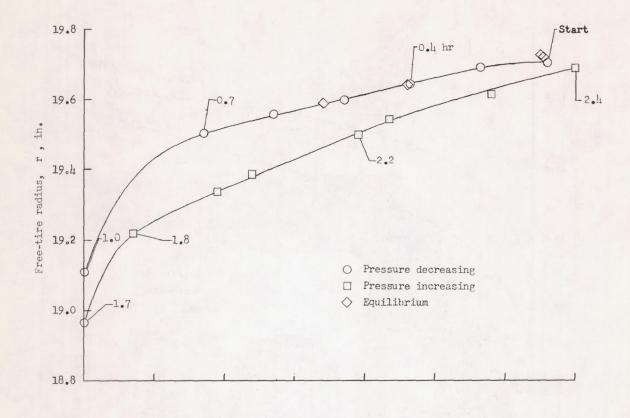


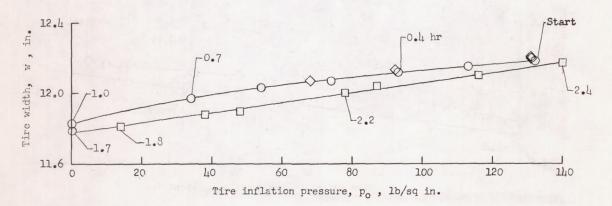


(a) Tire A.

Figure 4.- Free radius-pressure and width-pressure hysteresis loops.

Test series A and B.





(b) Tire B.

Figure 4.- Concluded.

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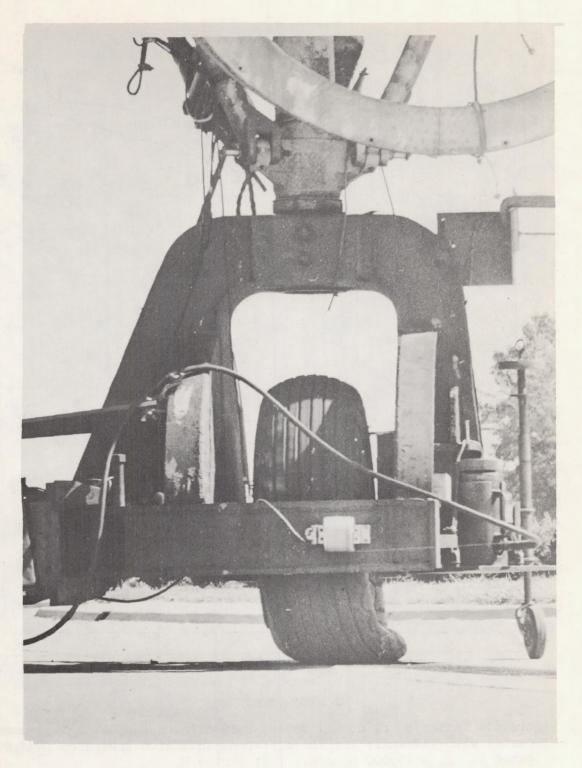


Figure 5.- Tire B under yawed rolling. $\psi = 17.5^{\circ}$; run 54.

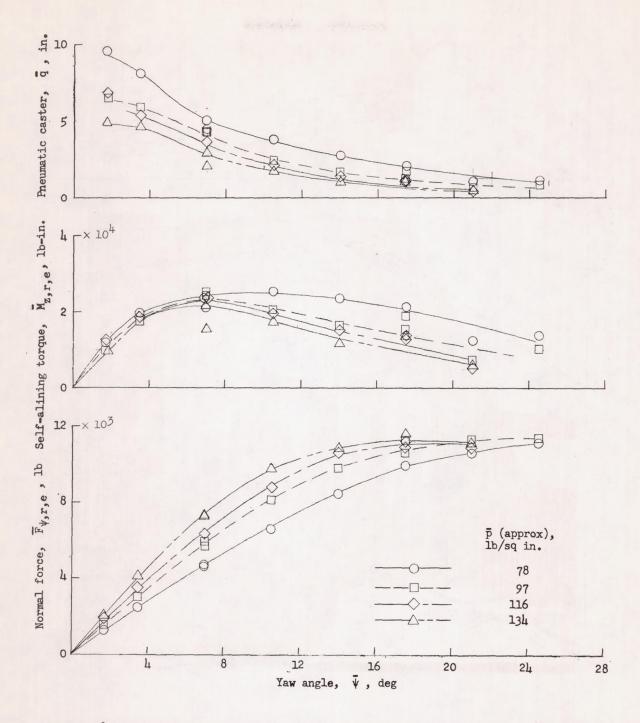


Figure 6.- Variation of normal force, self-alining torque, and pneumatic caster with yaw angle for the different inflation pressures investigated at $\overline{F}_{\rm Z}$ = 15,000 pounds. Test series B.

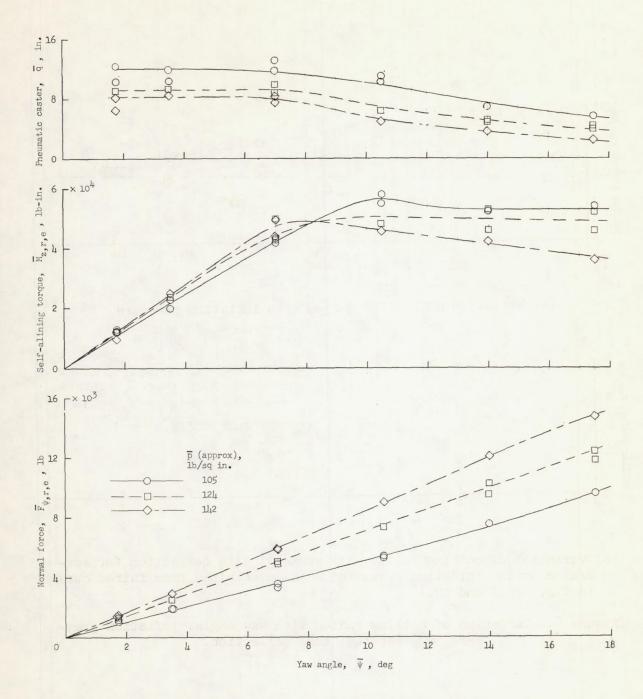
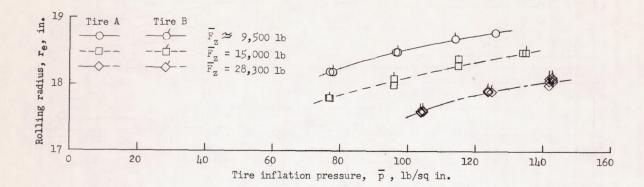
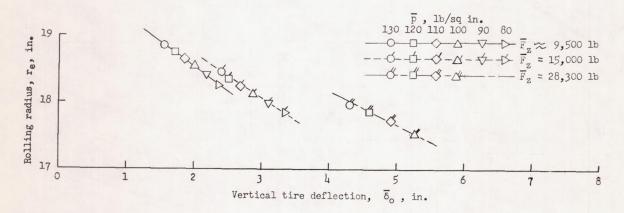


Figure 7.- Variation of normal force, self-alining torque, and pneumatic caster with yaw angle for the different inflation pressures investigated at \overline{F}_Z = 28,300 pounds. Test series E.

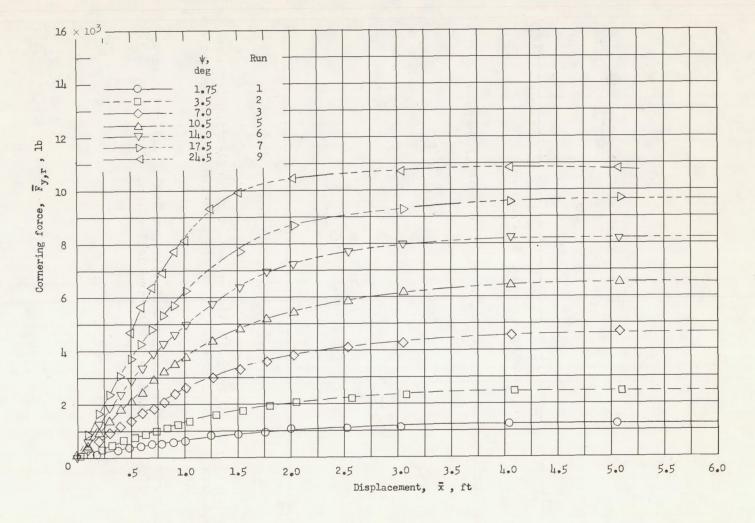


(a) Variation of rolling radius with inflation pressure.



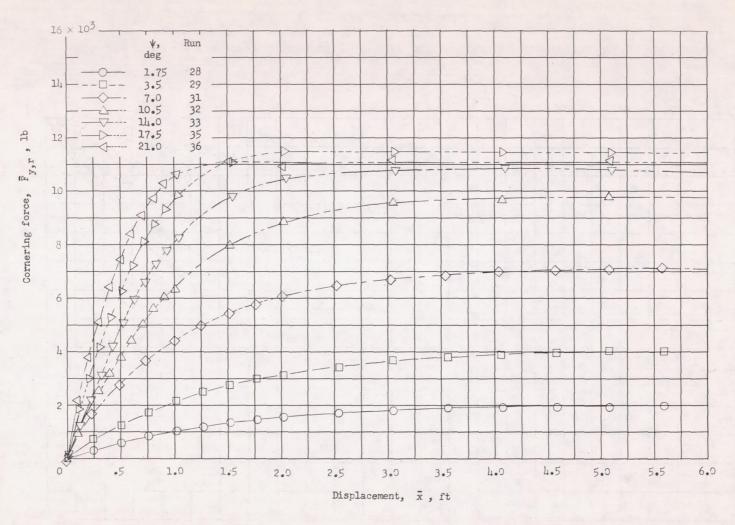
(b) Variation of rolling radius with vertical tire deflection for several constant inflation pressures. (Data obtained from faired curves in figs. 8(a) and 12.)

Figure 8.- Variation of rolling radius with yaw angle, inflation pressure, and vertical tire deflection.

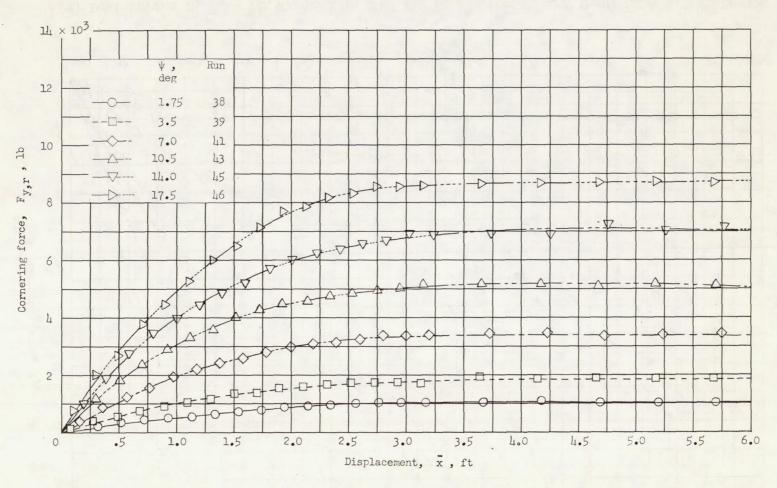


(a) Test series B; \overline{F}_Z = 15,000 pounds; $\overline{p}\approx 78$ pounds per square inch; $\overline{\delta}_O\approx 3.5$ inches.

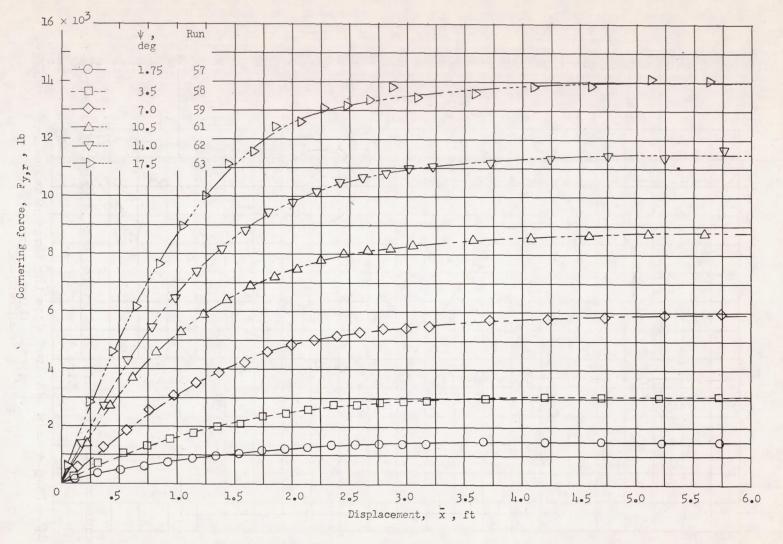
Figure 9.- Buildup of cornering force with distance rolled for some typical runs at several pressures.



(b) Test series B; \overline{F}_Z = 15,000 pounds; $\overline{p}\approx 134$ pounds per square inch; $\overline{\delta}_0\approx 2.4$ inches. Figure 9.- Continued.

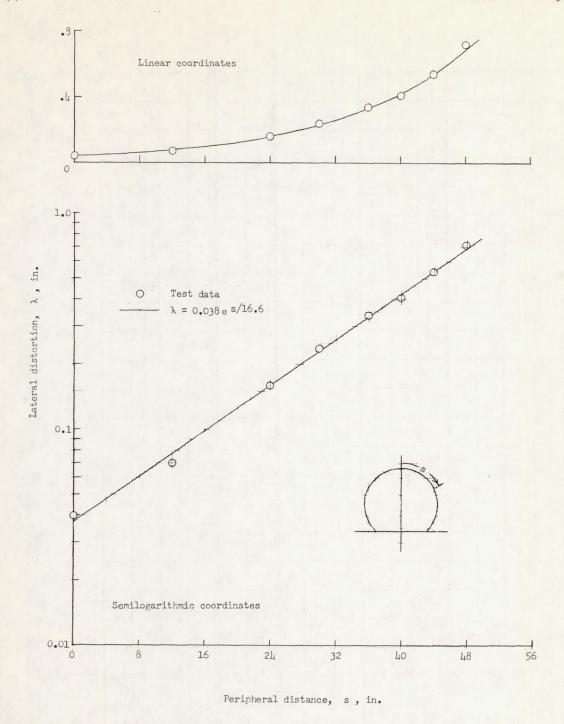


(c) Test series E; \overline{F}_Z = 28,300 pounds; $\overline{p}\approx$ 105 pounds per square inch; $\overline{\delta}_O\approx$ 5.2 inches. Figure 9.- Continued.



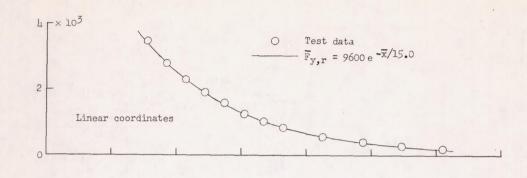
(d) Test series E; $\overline{F}_{\rm Z}$ = 28,300 pounds; $\overline{\rm p}$ \approx 142 pounds per square inch; $\overline{\delta}_{\rm O}$ \approx 4.0 inches.

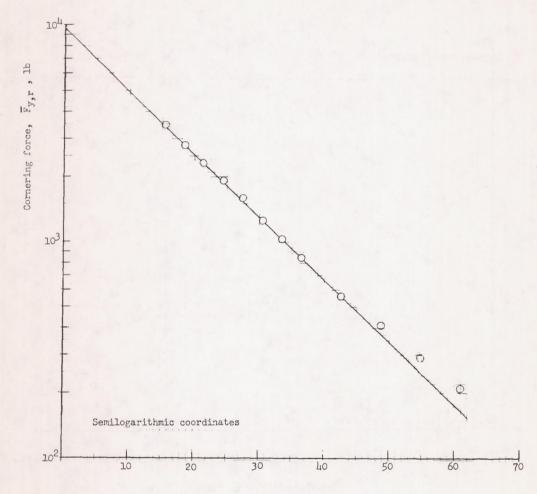
Figure 9. - Concluded.



(a) Experimental data used for determining static relaxation length for tire A for run 81.

Figure 10. - Sample data obtained from the three methods used to determine relaxation length.

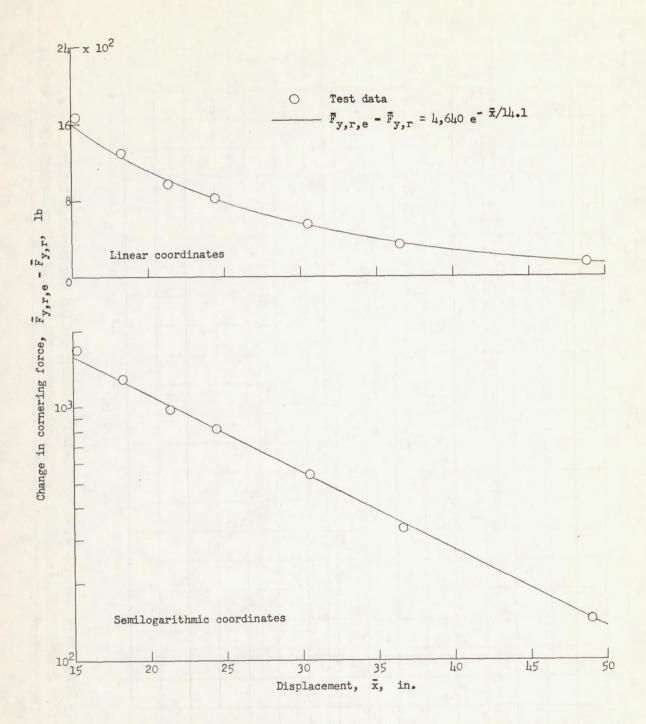




Displacement, \bar{x} , in.

(b) Experimental data used for determining unyawed-rolling relaxation length for run 92.

Figure 10. - Continued.



(c) Experimental data used for determining yawed-rolling relaxation length for run 4.

Figure 10. - Concluded.

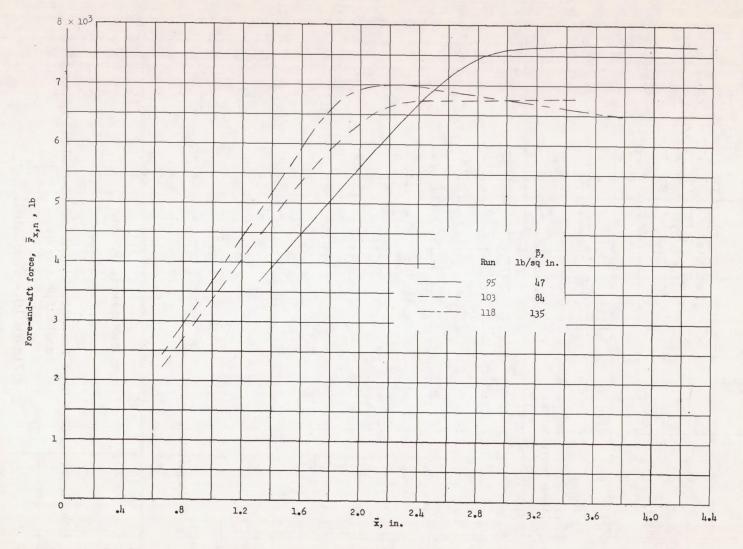


Figure 11.- Drag force buildup with horizontal distance pulled for several typical runs. \overline{F}_z = 9,390 pounds for $\overline{F}_{x,n}$ = 0; \overline{F}_x \approx 9,100 pounds at $F_{x,n,m}$ (from locked-wheel drag tests; test series D).

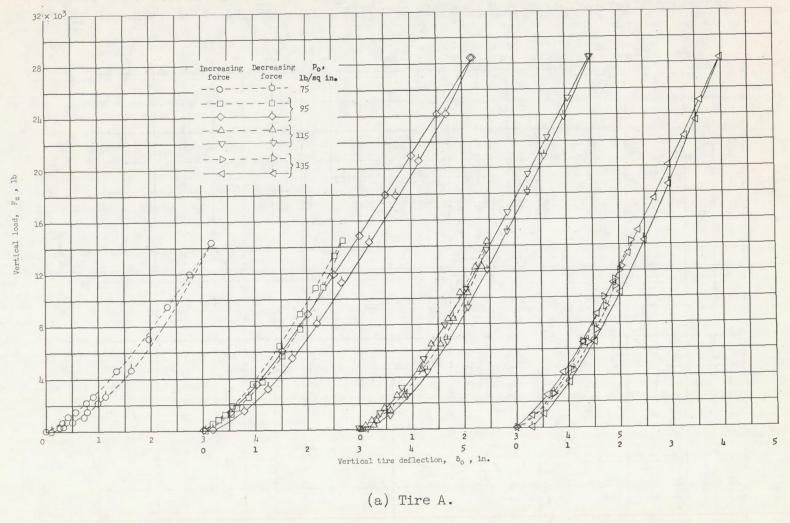
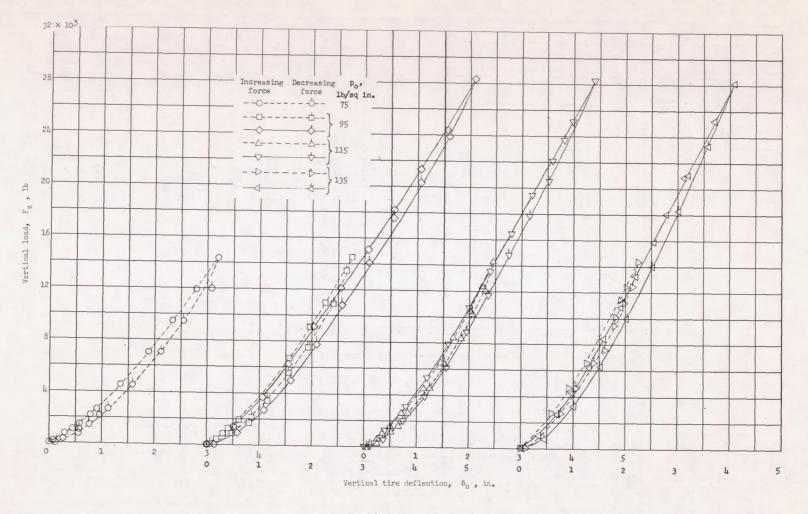


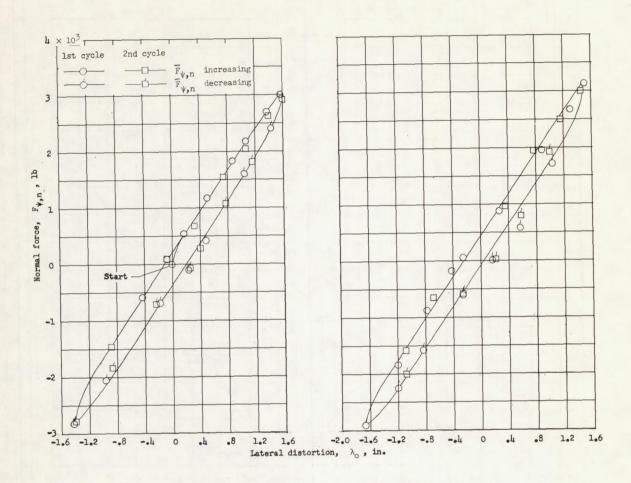
Figure 12.- Variation of vertical load with vertical tire deflection at various initial inflation pressures.



(b) Tire B.

Figure 12. - Concluded.

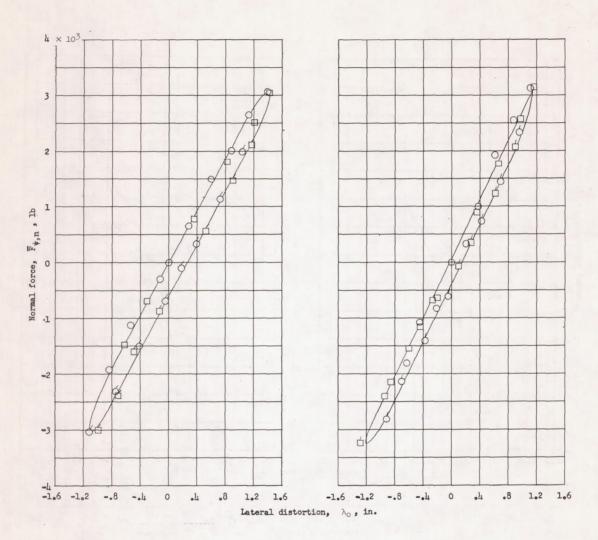
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(a) Run 119; $\bar{p}_0 = 75 \text{ lb/sq in.};$ $\bar{\delta}_0 = 3.3 \text{ in.};$ 43 sec/cycle.

(b) Run 120; $\bar{p}_0 = 75 \text{ lb/sq in.};$ $\bar{\delta}_0 = 3.3 \text{ in.};$ 27 sec/cycle.

Figure 13.- Variation of normal force with lateral tire distortion for an average vertical load per tire of 14,400 pounds. Test series B.



(c) Run 121;

$$\bar{p}_0 = 95 \text{ lb/sq in.};$$

 $\bar{\delta}_0 = 2.8 \text{ in.};$
26 sec/cycle.

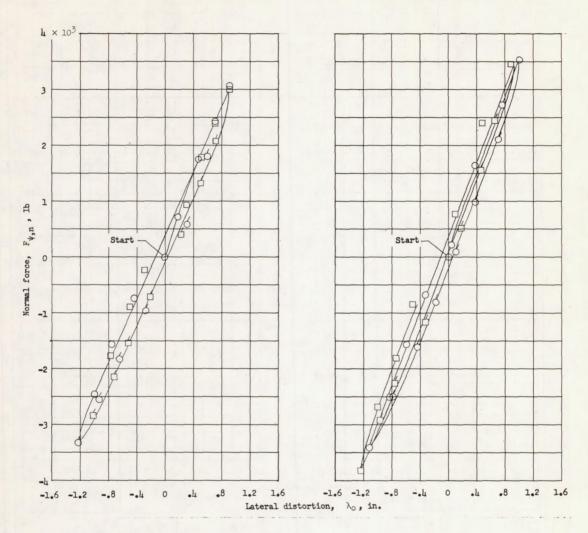
(d) Run 122;

$$\bar{p}_0 = 115 \text{ lb/sq in.};$$

 $\bar{\delta}_0 = 2.6 \text{ in.};$
26 sec/cycle.

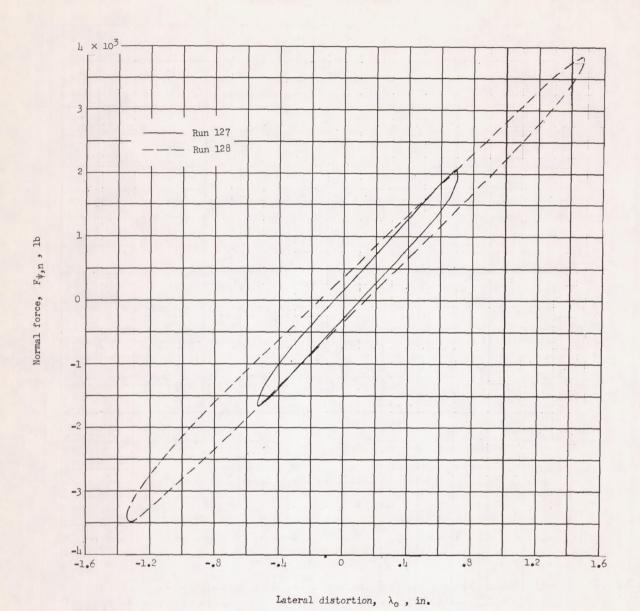
Figure 13. - Continued.

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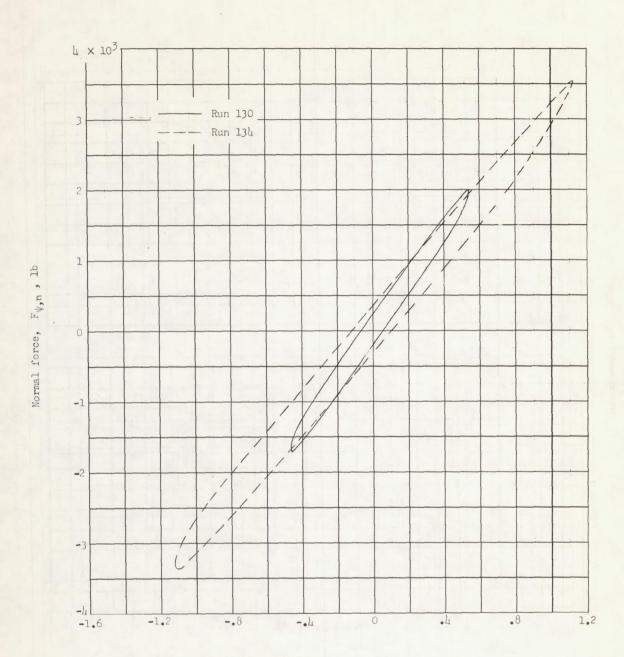
(e) Run 123; $\bar{p}_0 = 135 \text{ lb/sq in.};$ $\bar{\delta}_0 = 2.3 \text{ in.};$ 21 sec/cycle. (f) Run 124; $\bar{p}_0 = 135 \text{ lb/sq in.};$ $\bar{\delta}_0 = 2.3 \text{ in.};$ 21 sec/cycle.

Figure 13. - Concluded.



(a) $\bar{p}_0 = 115$ pounds per square inch; $\delta_0 \approx 4.3$ inches.

Figure 14. - Variation of normal force with lateral tire distortion for a vertical load per tire of 28,300 pounds. Test series E.



Lateral distortion, λ_0 , in.

(b) $\bar{p}_0 = 135$ pounds per square inch; $\bar{\delta}_0 = 3.8$ inches. Figure 14.- Concluded.

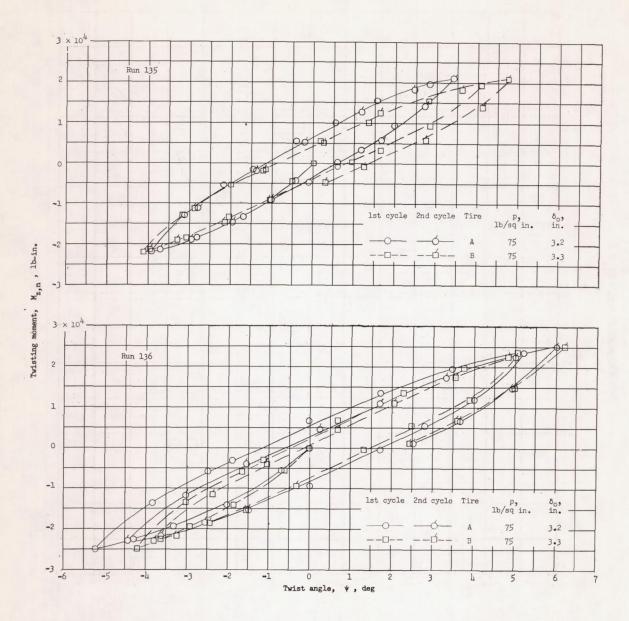


Figure 15. - Variation of twisting moment with twist angle for a vertical load of 14,400 pounds on each tire. Test series B.

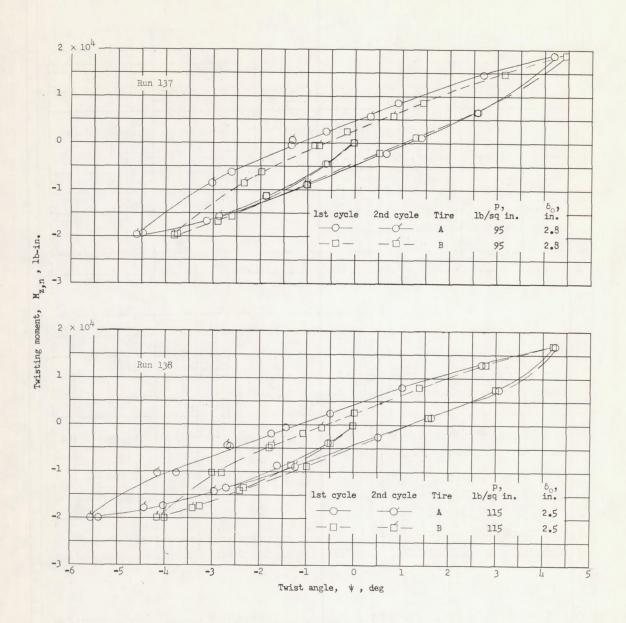
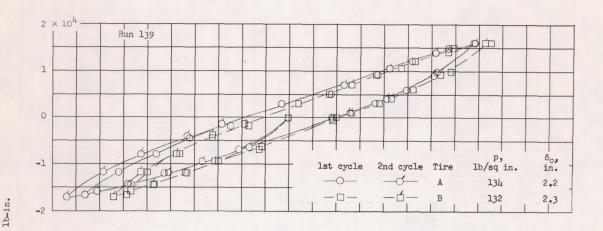


Figure 15. - Continued.



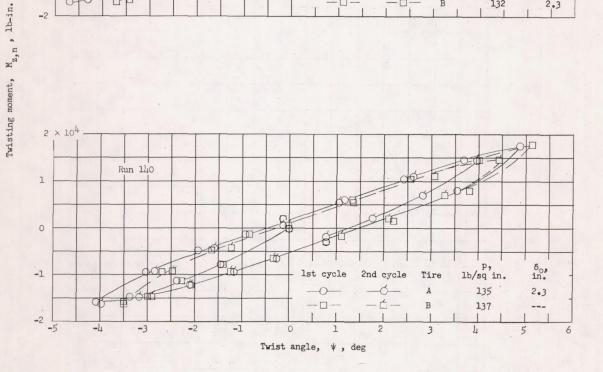
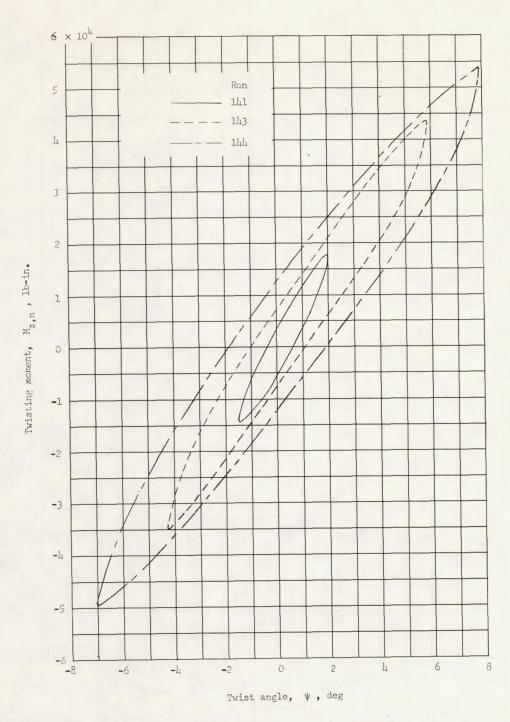
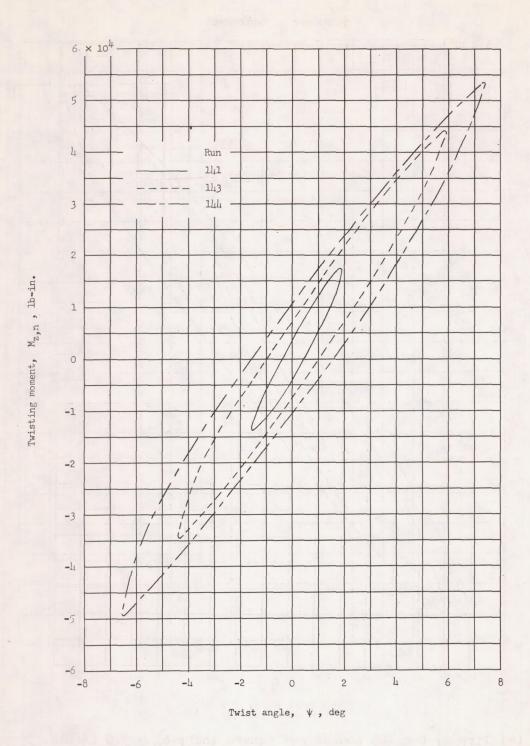


Figure 15. -. Concluded.

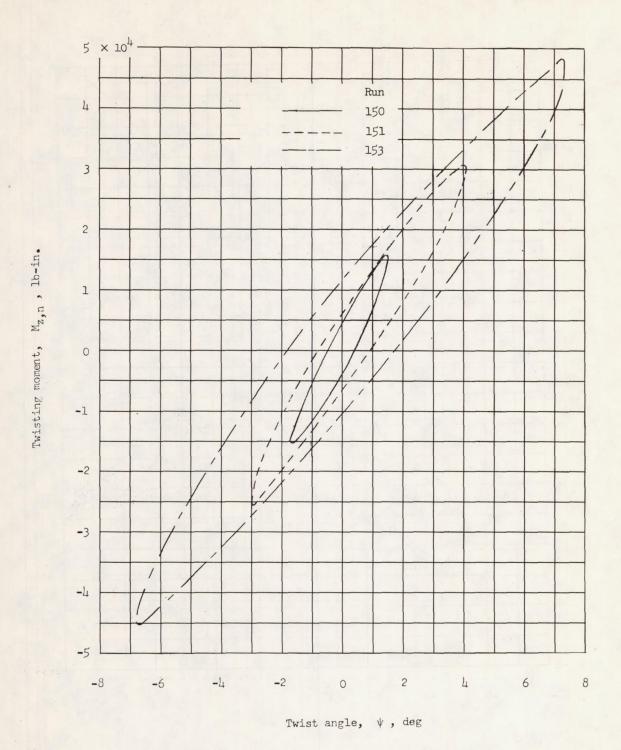


(a) Tire A; p \approx 105 pounds per square inch; $\delta_0 \approx$ 5.0 inches.

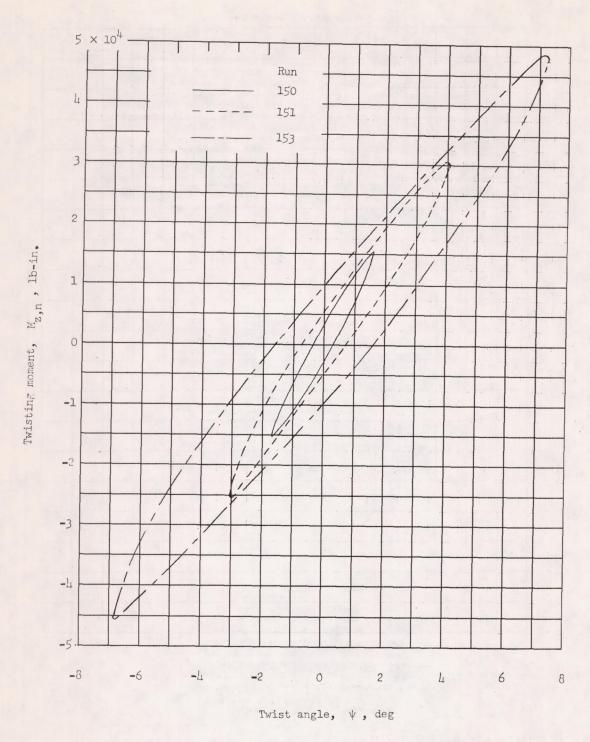
Figure 16. - Variation of twisting moment with twist angle for a vertical load of approximately 28,300 pounds on each tire. Test series E.



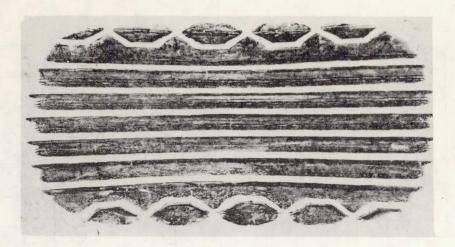
(b) Tire B; p \approx 105 pounds per square inch; $\delta_0 \approx 5.0$ inches. Figure 16.- Continued.



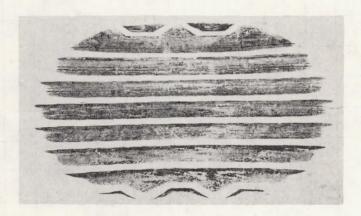
(c) Tire A; p = 142 pounds per square inch; $\delta_0 \approx 3.9$ inches. Figure 16.- Continued.



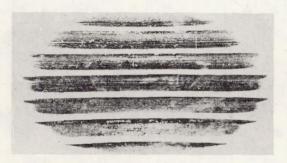
(d) Tire B; p \approx 141 pounds per square inch; $\delta_0 \approx 3.9$ inches. Figure 16.- Concluded.



(a) Run 215; $\delta_0 = 5.68$ inches; $p_0 = 85$ pounds per square inch; $F_Z = 28,190$ pounds.



(b) Run 217; δ_0 = 3.00 inches; p_0 = 95 pounds per square inch; F_Z = 14,720 pounds.



(c) Run 218; δ_0 = 2.04 inches; p_0 = 95 pounds per square inch; F_Z = 8,780 pounds.

Figure 17.- Typical tire footprints for tire B. L-97061

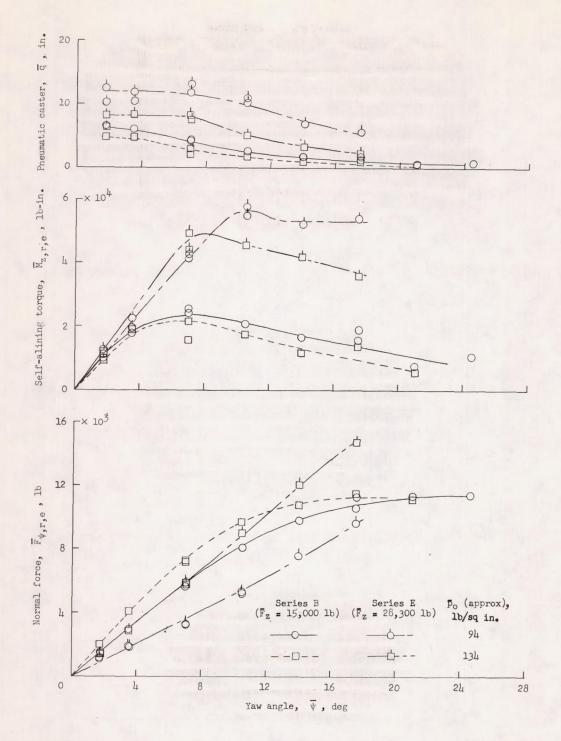


Figure 18.- Comparison of variation of normal force, self-alining torque, and pneumatic caster with yaw angle at two pressures for \overline{F}_z = 15,000 pounds (test series B) and \overline{F}_z = 28,300 pounds (test series E).

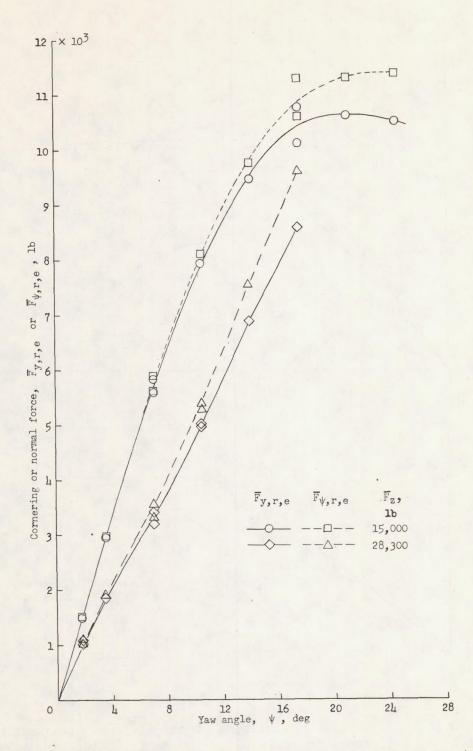
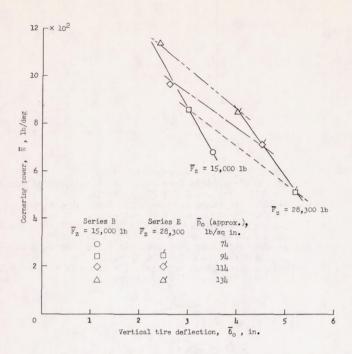
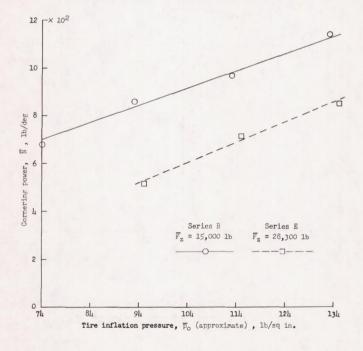


Figure 19.- Comparison of cornering-force and normal-force variations with yaw angle at $\bar{p}_0 \approx 94$ pounds per square inch for two vertical loadings.



(a) Variation of cornering power with vertical tire deflection.



(b) Variation of cornering power with inflation pressure.

Figure 20. - Variation of cornering power with vertical tire deflection and inflation pressure.

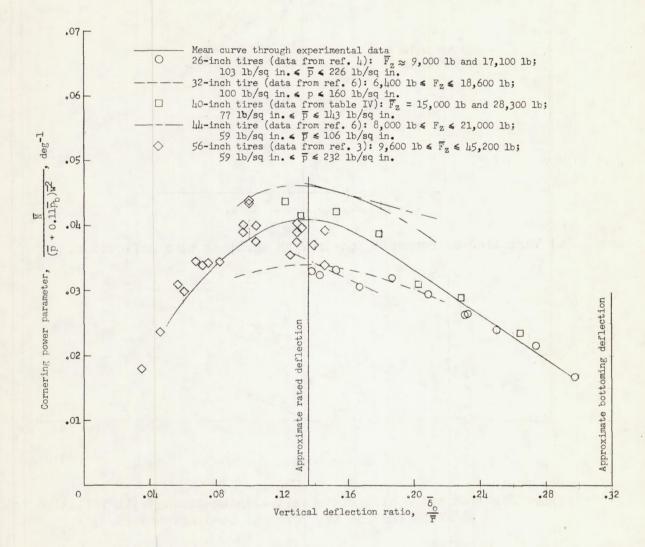


Figure 21.- Variation of cornering power with vertical deflection for five tires of different sizes.

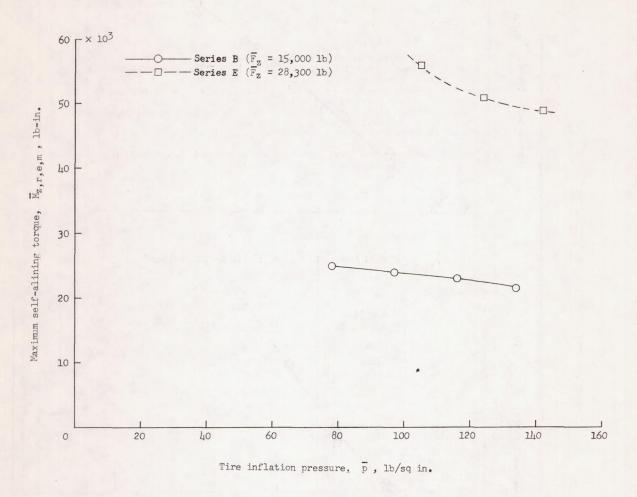
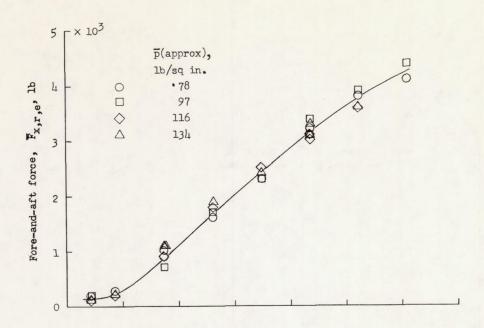
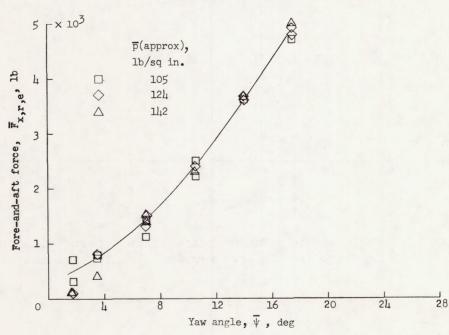


Figure 22. - Variation of maximum self-alining torque with inflation pressure for the two vertical loadings tested.

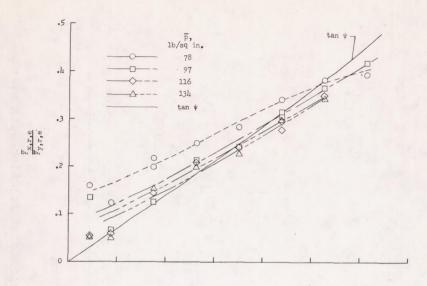


(a) Test series B; \overline{F}_{Z} = 15,000 pounds.

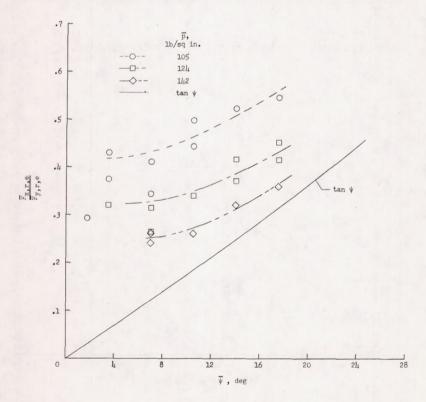


(b) Test series E; \overline{F}_{Z} = 28,300 pounds.

Figure 23.- Variation of drag force with yaw angle for the verticalload and pressure ranges tested.



(a) Test series B; $\overline{F}_{\rm Z}$ = 15,000 pounds.



(b) Test series E; \overline{F}_{Z} = 28,300 pounds.

Figure 24. - Variation of the ratio of drag force to cornering force with yaw angle.

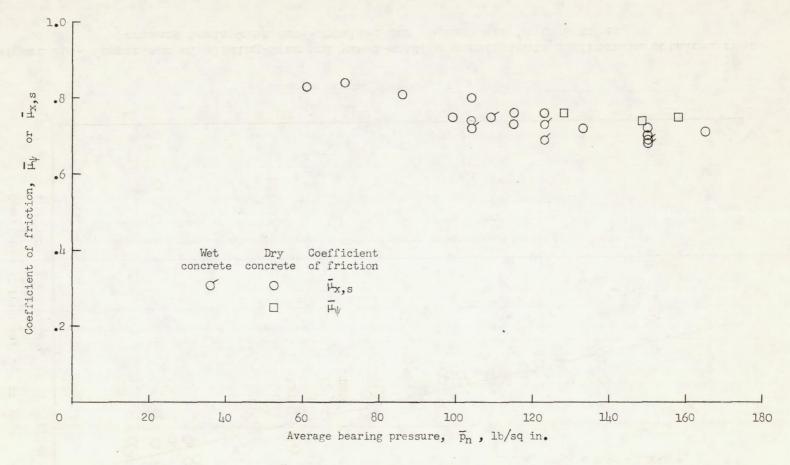


Figure 25.- Variation of sliding-drag and yawed-rolling coefficients of friction with average bearing pressure.

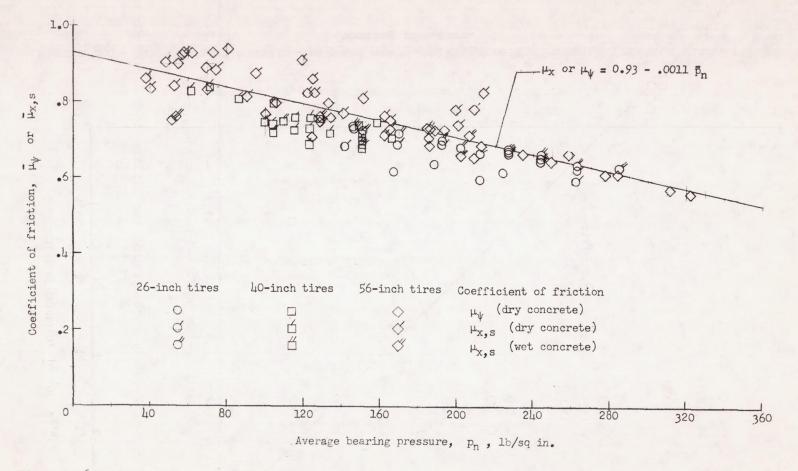


Figure 26.- Comparison of sliding-drag and yawed-rolling coefficients of friction obtained from present tests with data obtained for 26-inch and 56-inch tires.

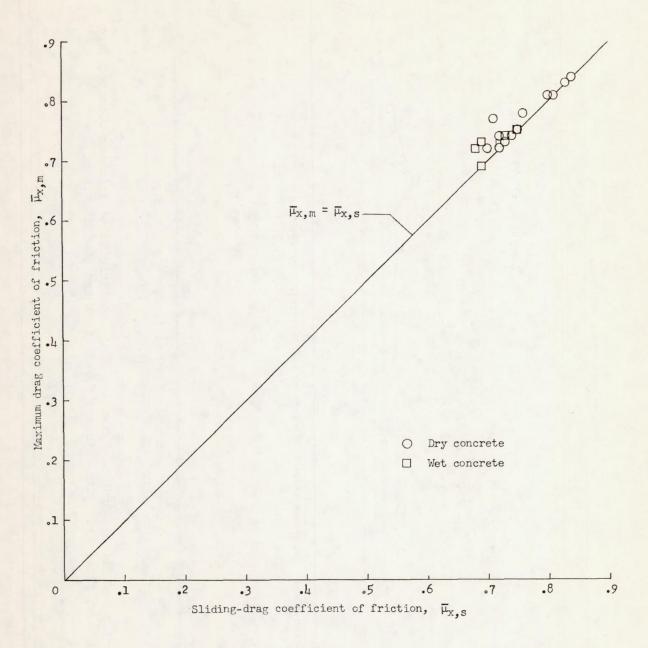


Figure 27.- Comparison of maximum drag and sliding-drag coefficients of friction.

0X

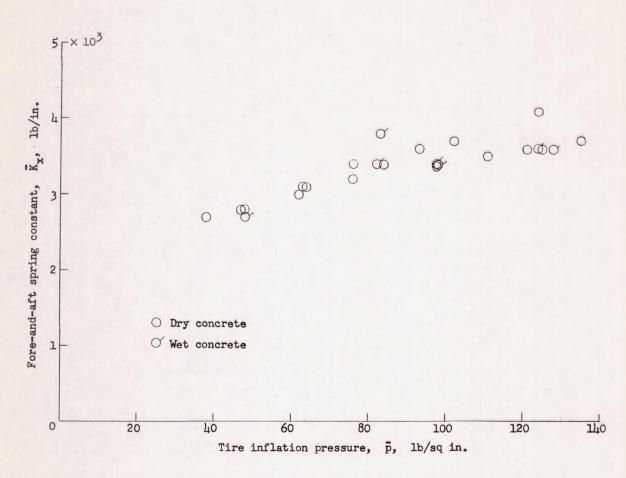
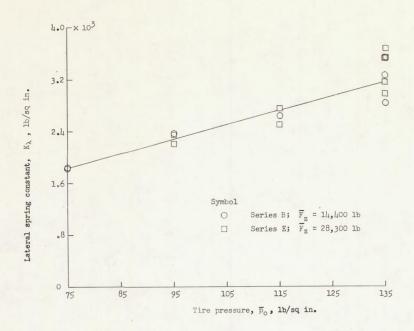
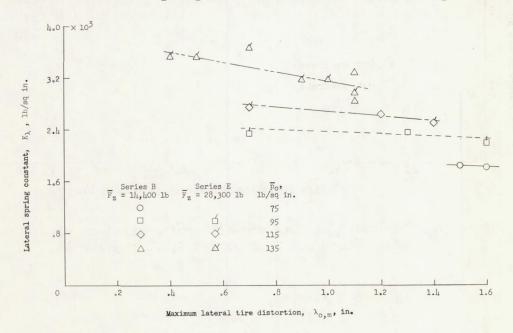


Figure 28.- Variation of fore-and-aft spring constant with tire inflation pressure. Test series D; $F_{\rm Z}\approx 9{,}100$ lb.



(a) Variation of lateral spring constant with tire inflation pressure.



(b) Variation of lateral spring constant with amplitude of lateral tire distortion.

Figure 29.- Variation of lateral spring constant with tire inflation pressure and amplitude of lateral tire distortion.

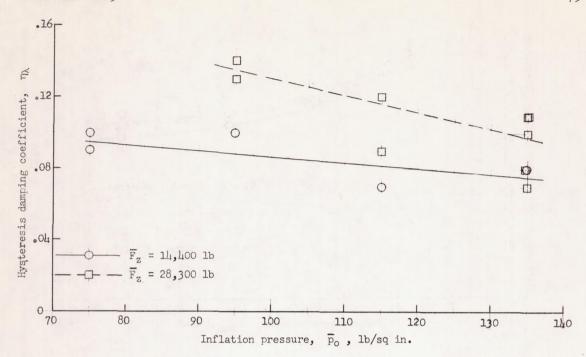


Figure 30. - Variation of hysteresis damping coefficient for lateral distortion with inflation pressure for two vertical loadings.

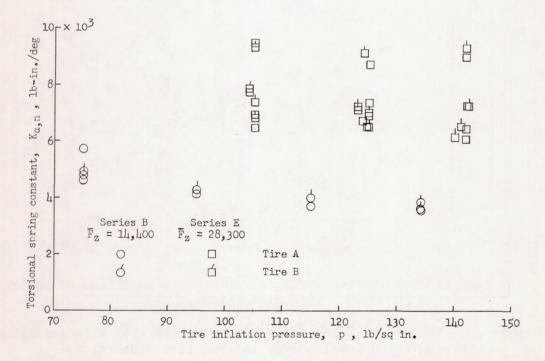


Figure 31. - Variation of torsional spring constant with tire inflation pressure for the two vertical loadings tested.

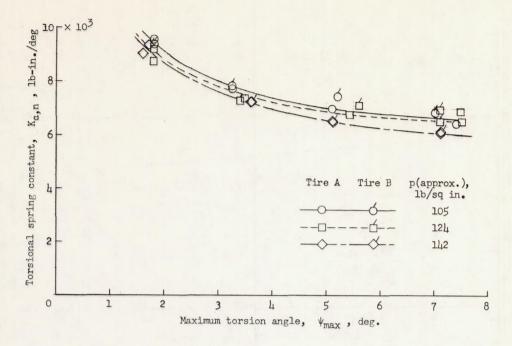


Figure 32.- Variation of static torsional spring constant with amplitude of hysteresis loop for several tire inflation pressures at the heavy vertical loading (\overline{F}_z = 28,300 lb).

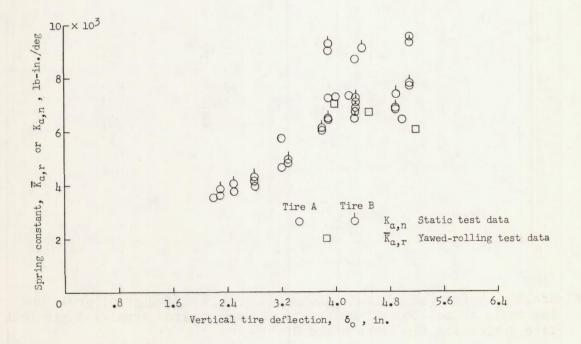


Figure 33. - Comparison of torsional spring constants from static and yawed-rolling tests. Test series B and E.

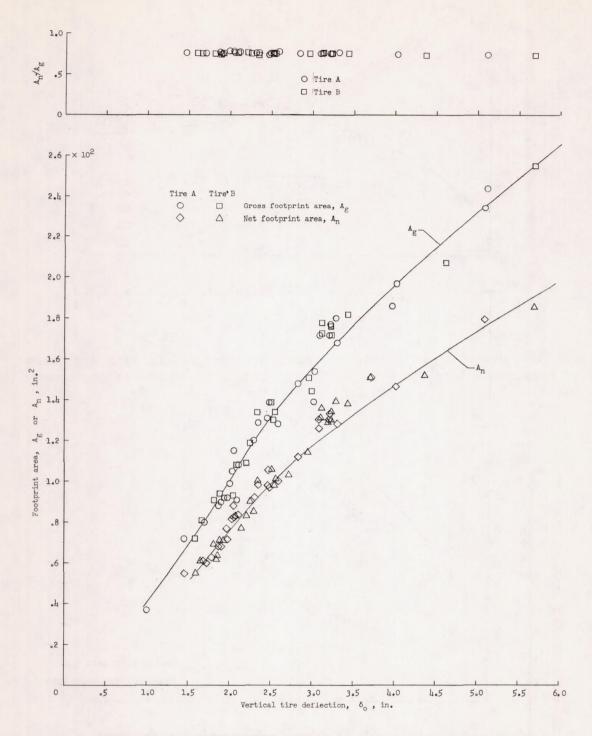


Figure 34.- Variation of gross footprint area, net footprint area, and the ratio of net footprint area to gross footprint area with vertical tire deflection for tires A and B.

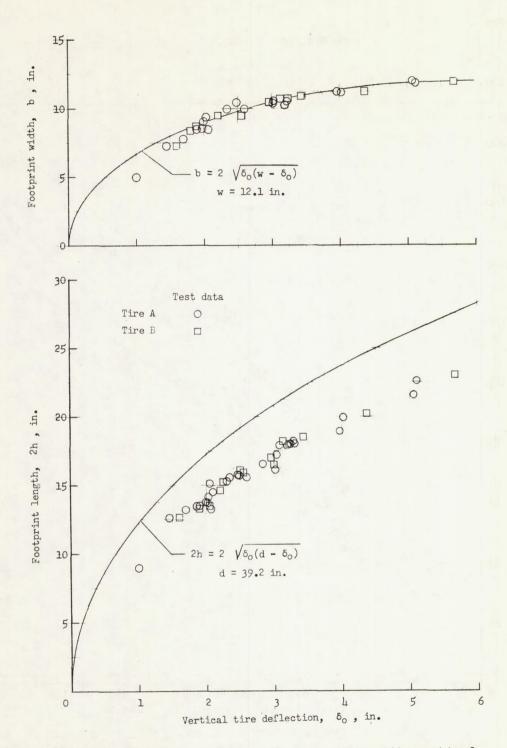


Figure 35. - Variation of footprint length and width with vertical deflection. Solid lines represent chord lengths of circles having diameters equal to the diameter and width at rated inflation pressure.

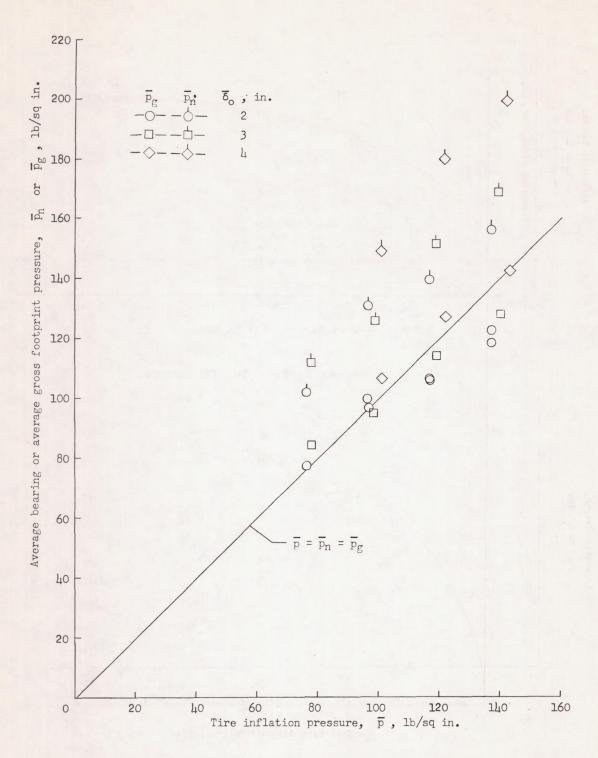
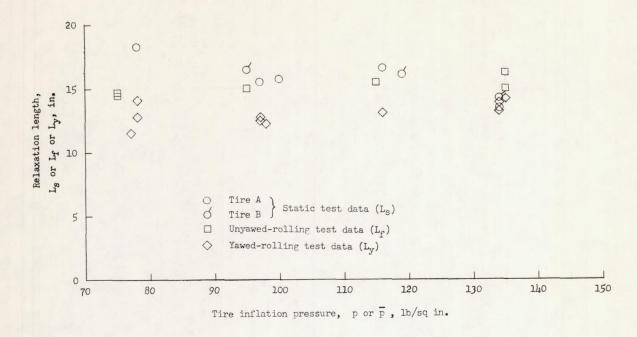
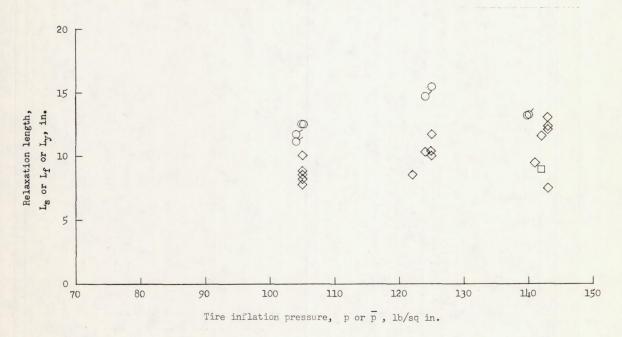


Figure 36.- Variation of average bearing pressure and average gross footprint pressure with tire inflation pressure for several constant vertical tire deflections.



(a) Test series B; $F_z \approx 14,700$ pounds.



(b) Test series E; $F_Z \approx 28,300$ pounds.

Figure 37. - Variation of relaxation lengths with tire inflation pressure for test series B and E.