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## RESEARCH MEMORANDUM

# VELOCITY DISTRIBUTIONS ON TWO-DIMENSIONAL 

WING-DUCT INLETS BY CONFORMAL MAPPING

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## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

## WASHINGTON

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# NATIONAL ADVISORY COMMITTTEE FOR ARRONAUTICS 

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## SUMMARY

The conformal mapping method of the Cartesian mapping function is applied to the determination of the velocity distribution on arbitrary two-dimensional duct-inlet shapes such as are used in wing installations. An idealized form of the actual wing-duct inlet is analyzed. The effects of leading-edge stagger, inlet-velocity ratio, and section lift coefficient on the velocity distribution are included in the analysis. Numerical examples are given and, in part, compared with experimental data.

## INIRODUCTION

Inlet contours for wing-duct installations, such as those used to conduct cooling air to engines, are generally designed on a more empirical basis than airfoil sections because the geometry of a wingduct inlet, hence the determination of its velocity distribution, is more complex than that of an airfoil section. By means of the conformal mapping method of reference 1 , however, the ideal incompressible velocity distribution over two-dimensional wing-duct inlets for arbitrary lift coefficients can be calculated with about the same labor as in the corresponding calculation for an isolated airfoil.

This method is herein applied to an arbitrary two-dimensional wing-duct inlet section. The theory is illustrated by numerical examples, which are, in part, compared with experimental data.

## ANALYSIS

Symbols
The more important symbols used in the paper are listed here. All velocities are expressed as fractions of the free-stream velocity; that is, the free-stream velocity is taken as unity.
$c_{2}$ section lift coefficient
c chord of duct-inlet section
d horizontal distance between leading edges of duct inlet
h vertical distance between leading edges of duct inlet
$r \quad$ stagger ratio in $\quad \zeta$-plane
$s \quad$ stagger ratio $d / h$ in $z$-plane
v velocity on surface of duct inlet
$V_{\text {Do }}$ velocity infinitely for inside duct
$v_{n}$ velocity at duct inlet
$z \quad$ plane of duct inlet section ( $x+i y$ )
$\zeta$ plane of chord lines $(\xi+i \eta)$
p plane of circle

The Conf ormal Transformation
The actual two-dimensional wing-duct configuration of figure $1(a)$ is replaced by the contour shown in figure $l(b)$. The two changes made in the original coniguration are: (a) removal of the internal flow resistance and (b) replacement of the streamlinos $A^{\prime} B^{\prime}$ and $C^{\prime} D$ ' by the parailel straight rigid boundaries $A B$ and $C D$. Change (a) results in a flow field of constant total pressure and change (b) in a simply connected flow field. The analysis is thereby considerably simplified. Both effects associated with the repiaced features, namely, variable inlct-velocity ratio and angle of attack, respectively, can be adequately represented in the flow function for the simplified configuration. For conventional wing-duct installations, the region of interest at the inlet, as regards velccity distribution,
is sufficiently far from the region in which changes (a) and (b) were mede that their influence on the required velocity distributions is negligible. (See ILLUSTRATIVE EXAMPLES.)

The simplified duct-inlet contour in the $z$-plane is now conformally mapped onto the staggerad semi-infinite parallel straight lines, $Q A B$ and $P C D$, in the $\zeta$-plane (fig. l(b)). This mapping is accomplished by the Cartesian mapping function (CMF), derined as the vector distance $z-\zeta$ between conformally corresponding points in the $z$ - and $\zeta$-planes (reference 1); thus

$$
\left.\begin{array}{rl}
z-\zeta & =(x-\xi)+i(y-\eta)  \tag{1}\\
& =\Delta x+i \Delta y
\end{array}\right\}
$$

The calculation of the CMF is carried out by considering it as a function of the central angle $\varphi$ of the p-plane circle into which the $\zeta$-plane contour can be conformally mapped by a known transformation. Inasmuch as $z-\zeta$ is regular on and outside of the $z$ - or $\zeta$-plane contours, by the conformal transformation from $\zeta$ to $p$ it is also regular on and outside of the p-plane circle. The real and imaginary parts of the CMF on the circle itself are therefore related by

$$
\begin{align*}
& \Delta x(\varphi)=-\frac{1}{2 \pi} \int_{0}^{2 \pi} \Delta y\left(\varphi^{\prime}\right) \cot \frac{\varphi^{2}-\varphi}{2} d \varphi^{\prime}  \tag{2}\\
& \Delta y(\varphi)=\frac{1}{2 \pi} \int_{0}^{2 \pi} \Delta x\left(\varphi^{\prime}\right) \cot \frac{\varphi^{\prime}-\varphi}{2} d \varphi^{\prime} \tag{3}
\end{align*}
$$

The conformal transformation of the $\zeta$-plane, staggered semiinfinite parallel lines, into the p-plane circle is carried out in two steps. In the first step a Schwarz-Christoffel transformation takes the $\zeta$-plane polygon into the real axis of a $t$-plane such that the upper-half $t$-plane corresponds to the $\zeta$-plane. With the correspondence of boundary points indicated in figure 2, this transformation is (reference 2):

$$
\begin{gather*}
\frac{d \zeta}{d t}=c_{1} \frac{\left(t-u_{2}\right)\left(t-u_{4}\right)}{t}  \tag{4}\\
\zeta=c_{1}\left[\frac{t^{2}}{2}-\left(u_{2}+u_{4}\right) t+u_{2} u_{4} \log _{e} t\right]+c_{2} \tag{5}
\end{gather*}
$$

The six constants given by $u_{2}, u_{4}$ (real), and $C l, C_{2}$ (complex) are detemined for the orientation and the scale indicated in figure 2 by the six conditions:
(a) $\mathrm{C}_{1}$ real (staggered lines horizontal)
(b) $a=l$, scale factor in $\zeta$-Flane
(c) $r$ equals desired stagger in $\zeta$-viane, $\zeta\left(u_{2}\right)=r+T-i$
(d) $u_{2}=-1$, scale factor in $t$-plane
(e) upper leading edge in $\zeta$-plane at point $(\tau, 0)$ or $\zeta\left(u_{4}\right)=\tau$ (two conditions)

The constant $T$ is inserted in condition (e) in order to locate the leading edge of the upper inlet section tangent to the $y$ axis. By use of the fcregoing conditions, equation (5) reduces to

$$
\begin{equation*}
\left.\zeta=\frac{1}{\pi}\left(\frac{t}{m}-1\right)\left[\frac{m}{2} \frac{t}{m}-1\right)+1\right]-\frac{1}{\pi} \log _{e} \frac{t}{m}+\tau \tag{6}
\end{equation*}
$$

The quantity $m \equiv u_{4}$ is the following function of the stagger ratio $r$ :

$$
\begin{equation*}
\pi r=\log _{e} m+\frac{1}{2}\left(m-\frac{1}{m}\right) \tag{7}
\end{equation*}
$$

Equation (7) is plotted in figure 3.
The second step of the desired transformation from $\zeta$ to $p$ consists in mapping the upper-helf t-plane onto the region outside of the p-plane unit circle by a bilinear transformation, here taken as

$$
\begin{equation*}
t=i\left(\frac{p+1}{p-1}\right) . \tag{8}
\end{equation*}
$$

The correspondence of points for equation (8) is indicated in figure 2, The use of other bilinear transformations wjill be discussed in ILLUSTRATIVE EXAMPIES.

Equations (1), (6), and. (3) constitute the conformal transformation from the region around the duct-inlet section in the physical $z-p l a n e$ to the region outside the unit circle p-plane. These equations, with $p=e^{i \varphi}$, give for conformally corresponding points on the boundaries

$$
\begin{equation*}
t=\cot \frac{Q}{2} \tag{9}
\end{equation*}
$$

$x=\xi+\Delta x$
$\left.x=\frac{1}{\pi}\left(\frac{1}{m} \cot \frac{\varphi}{2}-1\right)\left[\frac{m}{2}\left(\frac{1}{m} \cot \frac{\varphi}{2}-1\right)+1\right]-\frac{1}{\pi} \log _{e} \frac{1}{m}\left|\cot \frac{p}{2}\right|+\Delta x(\varphi)+T\right](1.0)$
$y=\eta+\Delta y$
$\left.\begin{array}{ll}y=\eta+\Delta y & \\ y=\Delta y(\varphi) & 0<\varphi<\pi \quad \text { upper-duct inlet section } \\ y=\Delta y(\varphi)-1 & \pi<\varphi<2 \pi\end{array}\right\}$
The leading-edge points of the upper-duct and lower-duct inlet sections may be defined as the upstream points of tangency of normals from the "chord" lines OA and RC with the duct-inlet contours (fig. I(b)). These points may be found as functions of $\varphi$ by minimizing $x$ with respect to $\varphi$ in equation (10). The resulting condition is

$$
\begin{equation*}
\frac{d \Delta x}{d \varphi}=\frac{\left(\cot \frac{\varphi}{2}-m\right)\left(\cot \frac{\varphi}{2}+l\right)}{\pi m \sin \varphi} \tag{12}
\end{equation*}
$$

## Velocity Distribution

The velocity distribution on the duct-inlet section is given by

$$
\begin{equation*}
v=\frac{\partial W}{\partial z} \tag{13}
\end{equation*}
$$

in which the complex potential $W$ is

$$
\begin{equation*}
W=\zeta+\frac{A}{\pi} t+\frac{B}{\pi} \log _{e} t \tag{14}
\end{equation*}
$$

The term $\zeta$ represents a uniform flow velocity to the right, of unit magnitude in the $\zeta$-plane, and gives a free-strean velocity of unity in the physical plane. The term $\frac{A}{\pi} t$ represents a uriform flow in the t-plane and corresponds to a circulatory flow around the duct inlet in the physical plane. This term gives the effect of angle of attack on the physical duct-inlet section, although the geometric angle of attack of the section analyzed must remain zero because of its semi-infinite extent. The term $\frac{B}{\pi} \log _{\theta} t$ represents the flow due to a source at the origin in the $t$-plane and gives the desired inlet velocity into the duct in the physical plene.

The quantitative effect of the parameters $A$ and $B$ in the physical plane is determined by evaluation of the complex velocity

$$
\begin{equation*}
\frac{d W}{d z}=\left(1+\frac{A}{\pi} \frac{\partial t}{d \zeta}+\frac{B}{\pi t} \frac{\partial t}{d \zeta}\right) \frac{d \zeta}{d z} \tag{15}
\end{equation*}
$$

where, by equation (6),

$$
\begin{equation*}
\frac{d t}{d \zeta}=\frac{\pi m t}{(t-m)(t+1)} \tag{16}
\end{equation*}
$$

and, because $z-\zeta$ is regular on and outside of the p-plane circle,

$$
\left.\begin{array}{c}
z-\zeta=\sum_{0}^{\frac{L_{n}}{p^{n}}} \\
\frac{d z}{d \zeta}=1-\frac{d p}{d \zeta} \sum_{0}^{\infty} \frac{n c_{n}}{n+1} \\
\frac{d z}{d \zeta}=1+\frac{2 i}{(t-i)^{2}} \frac{\pi m t}{(t-m)(t+1)} \frac{p^{n}}{0}, \frac{p^{n+1}}{p^{n+1}} \tag{18}
\end{array}\right\}
$$

Infinitely far inside the duct in the physical plane, the correspondence of points is: $z=\alpha, \quad \zeta=\infty$ by equation (17), $t=0$ by equation (6), and $p=-1$ by equation (8). Hence, at this point, $\frac{d z}{d \zeta}=1$ by equation (18), $\frac{d t}{d \zeta}=0$ and $\frac{1}{t} \frac{d t}{d \zeta}=-\pi$ by equation (16); and equation (15) gives for the velocity $\mathrm{v}_{\mathrm{D} 0}$ infinitely far inside the duct

$$
\begin{equation*}
{ }^{v} D \infty=I-B \tag{19}
\end{equation*}
$$

The velocity distribution on the inner wall of the duct-inlet section becomes almost constant a short distance behind the leading edge. (See ILIUSTRATIVE EXAMPLES.) The inlet volocity $V_{n}$ is defined as this asymptotic value. The inlet velocity $v_{n}$ will be different from $V_{D \infty}$ if the height at the inlet is different from the height (unity) infinitely far inside the duct. Infinitely f'ar upstream of the duct-inlet section the correspondence of points is: $z=-\infty$, $\zeta=-\infty, \quad t=i \infty$, and $p=1$, and consequently $\frac{d z}{d \zeta}=1, \quad \frac{d t}{d \zeta}=\frac{1}{t} \frac{d t}{d \zeta}=0$. This result holds infinitely far outside the duct in any direction. Hence, the free-stream velocity is, by equation (15), unity.

The quantity $A$ may be evaluated either as a function of the stagnation-point locations on the duct inlet or as a function of a suitably defined lift coefficient. In terms of the stagnation points, given by $\frac{d W}{d z}=0$ in equation (15), and with equations (16) and (9),

$$
\begin{gather*}
A=\frac{(m-1) \cot \frac{\varphi_{s t}}{2}-\cot ^{2} \frac{\varphi_{s t}}{2}+m(I-B)}{m \cot \frac{\varphi_{s t}}{2}}  \tag{20}\\
\cot \frac{\varphi_{s t}}{2}=\frac{-[1+m(A-1)] \pm \sqrt{[1+m(A-1)]^{2}+4 m(1-B)}}{2} \tag{21}
\end{gather*}
$$

For a given $A$ (and B) equation (21) is a quadratic equation for the two stagnation-point locations. When quantity $A$ is alternalively regarded as a function of lift coefficient $c_{l}$, the section lift coefficient is defined in terms of circulation and chord by the well-known isolated airfoil relation

$$
\begin{equation*}
c_{2}=\frac{2 \stackrel{\Gamma}{c}}{c} . \tag{22}
\end{equation*}
$$

The chord $c$ is defined as the overall length of the wing ductinlet section in the free-stream direction ( OE in fig. lb)), and the circulation $\Gamma$, as the line integral of the velocity over the circuit CFGHKMAEC around the wing-duct installation. This circulation can be evaluated as the sum of the potential difference over the lower surface $\Phi_{G}-\Phi_{C}$, and the potential difference over the upper surface $\Phi_{\mathrm{E}}-\Phi_{\mathrm{H}}$. The difference of potential over the paths GH and EC is neglected because the velocity is here approximately perpendicular to the path. Hence, by equation (14)

$$
\begin{aligned}
& \Phi_{E}-\Phi_{H}=\xi_{E}-\xi_{H}+\frac{A}{\pi}\left(t_{E}-t_{H}\right)+\frac{B}{\pi} \log _{e} \frac{t_{E}}{t_{H}} \\
& \Phi_{G}-\Phi_{C}=\xi_{G}-\xi_{C}+\frac{A}{\pi}\left(t_{G}-t_{C}\right)+\frac{B}{\pi} \operatorname{lcg} \frac{t_{G}}{t_{C}}
\end{aligned}
$$

and

$$
\left.\begin{array}{l}
F=\left(\Phi_{E}-\Phi_{H}\right)+\left(\Phi_{G}-\Phi_{C}\right) \\
\Gamma=\left(\xi_{E}-\check{\zeta}_{C}\right)-\left(\xi_{H}-\xi_{G}\right)+\frac{A}{\pi}\left[\left(t_{E}-t_{C}\right)-\left(t_{H}-t_{G}\right)\right]+\frac{B}{\pi} \log _{e}\left(\frac{t_{E} t_{G}}{t_{H} t_{C}}\right) \tag{23}
\end{array}\right\}
$$

Finally, solving for $A$ and expressing $\Gamma$ in terms of $c_{2}$ by equation (22) with $c=x_{E}$,

$$
\begin{equation*}
A=\frac{\pi\left[\frac{c_{l}}{2} x_{E}-\left(\xi_{E}-\xi_{C}\right)+\left(\xi_{H}-\xi_{G}\right)\right]-B \log _{e}\left(\frac{t_{E} t_{G}}{t_{H} t_{C}}\right)}{\left(t_{E}-t_{C}\right)-\left(t_{H}-t_{G}\right)} \tag{24}
\end{equation*}
$$

The quantities $x, \xi$, and $t$ at the various points indicated in equation (24) are given in terms of the corresponding central angle $\varphi$ by equations (9) and (10). The various $\varphi$ values are known when the conformal transformation of the duct inlet has been carried out.

For a $\operatorname{CMF} \Delta x(\varphi), \Delta y(\varphi)$, stagger constant $m$, and the constants $A$ and $B$ corresponding to the lift coefficient and the inlet-velocity ratio, the velocity distribution on the duct-inlet contour is given by the absolute magnitude of $\mathrm{dW} / \mathrm{dz}$ on the boundary. On the boundary, $p=e^{i \varphi}$,

$$
\left.\begin{array}{l}
\frac{d z}{d \xi}=1+\frac{d(z-\xi)}{d \xi}  \tag{25}\\
\frac{d z}{d \xi}=1+\frac{d(\Delta x+i \Delta y)}{d \varphi} \frac{d \varphi}{d t} \frac{d t}{d \xi}
\end{array}\right\}
$$

Substitution of equations (9), (16), and (25) into (15) yields for the velocity distribution on the duct-inlet section

$$
\begin{equation*}
v=\frac{\left(\cot \frac{\varphi}{2}-m\right)\left(\cot \frac{\varphi}{2}+1\right)+m A \cot \frac{\varphi}{2}+m B}{\pi m \sin \varphi \sqrt{\left[\frac{\left(\cot \frac{\varphi}{2}-m\right)\left(\cot \frac{\varphi}{2}+1\right)}{\pi m \sin \varphi}-\frac{d \Delta x}{d \varphi}\right]^{2}+\left(\frac{d \Delta y}{d \varphi}\right)^{2}}} \tag{26}
\end{equation*}
$$

Procedure for Calculation of CMF
The calculation of the CMF $\Delta x(\varphi), \Delta y(\varphi)$, and stagger constant $m$ for a given duct-inlet section may be carried out by a process of successive approximations similar to that of reference 1. The steps are outlined as follows:

1. The duct-inlet section is drawn in normal form (fig. l(b)). Point 0 is the origin and the scale is such that the normal distance between the chord lines $O A$ and $R C$ is unity. The stagger. $s=d / h$ of the duct inlet is, in general, different from the stagger $r$ of the chord lines.
2. A set of abscissas $x(\varphi)$ are calculated for a standard set of values of $\varphi$ by equation (10). The $\Delta x(\varphi)$ and. $T$ may be that of a previous example or, at worst, equal to zero. The value of $m$ may be taken from figure 3 for $r=s$.
3. The ordinates $y$ of the duct-inlet contour cormesponding to the abscissas $x$ of step 2 are measured. The function $\Delta y(p)$ is thereby determined (equation (11)).
4. The function $\Delta x(\varphi)$ is calculated from $\Delta y(\varphi)$ by equation (2).
5. The functions $\Delta x(\varphi)$ of step $4, \Delta y(\varphi)$ of step 3, and $m$ of step 2 constitute by equations (10) and (11) a duct-inlet section of which the difference in abscissas between the leading edges is, in general, other than that speciried. The constant $m$ is therefore adjusted to make this difference equal to the specified value. To this end equation (12) (corresponding to the values $\varphi_{1}$ and $\varphi_{2}$ for the two extremities) and the equation for the difference $d$ in the leading-edge abscissas

$$
\begin{equation*}
x\left(m, \varphi_{1}\right)-x\left(m, \varphi_{2}\right)=d \tag{27}
\end{equation*}
$$

obtained from equation (10), can be solved simultaneousiy for $\varphi_{1}$, $\varphi_{2}$, and $m$. A more convenient procedure is one of iteration. Initial values $\varphi_{1}$ and $\varphi_{2}$ for minimum $x$ are graphically obtained by plotting equation (10) in the necessary regions. A value of $m$ is then obtained from equation (27). With this value of $m$, values of $\varphi_{1}$ and $\varphi_{2}$ are again graphically found for minimum $x$ by equation (10). The process is continued until $\varphi_{1}, \varphi_{2}$, and $m$ do not change appreciably in successive calculations. Finaily, a constant $T$ is so chosen that $x\left(\varphi_{1}\right)=0$. The derived inlet section is now in normal form.
6. The values of $m$ and $T$ derived in step 5 and $\Delta x(p)$ and $\Delta y(\varphi)$ of steps 4 and 3 yield a shape by equations (10) and (11), which can be compared with the given one. If the agreement is not sufficiently close, steps 3 to 5 are repeated.
7. The velocity distribution is obtained by substitution of the final $m$ and the derivatives $\frac{d \Delta x}{d \varphi}$ and $\frac{d \Delta y}{d \varphi}$ of the final $C M F$ into equation (26). The value of $B$ is chosen to produce the desired inlet velocity (the velocity given by equation (26) on the inside walls of the duct-inlet section). The value of $A$ is chosen to locate the stagnation points in the desired manner (equation (21)) or for a desired nominal lift coeficicient (equation (24)).

The inverse problem, namely, the calculation of the duct-iniet section to produce a prescribed velocity distribution, may be treated by the methods given in referenses $l$ and 3.

## ILLUSTRATIVE EXAMPI.ES

As a first application of the theory, the symmetrical wing-duct installation ( $m=1.0$ ), on which pressure distributions were measured in reference 4 (shape 9), was analyzed. The installation is shown in figure 4 and the ordinates are listed in table l. The trailingedge portions were actually flaps by which the inlet velocity was varied. The scale used for the calculation was such that the iistance between trailing edges was unity, as assumed in the theory. An evenly spaced set of $48 \varphi$-vaiues was takon of which only 24 were actually used because of the symmetry. Off these 24 values, 21 were included in the front 8 percent of the chord. This portion of the duct inlet was theref ore the portion effectively analyzed. The leading-edge portion is plotted in figure 5 to a scale such that the vertical distance between the leading edges, the entrance height $h$, is unity.

The CMF obtained after four approximations (which produced coincidence of the specified shape and the derived shape) is listed in table 2 and plotted in figure 6. In the first two approximations the airfoil was drawn to an abscissa scale of 25 inches for the chord and had an ordinate scale four times the abscissa scale. The last two approximations were made for the airfoil drawn to a scale such that the chord length wess 100 inches; the ordinate scale was the same as the abscissa scale. The values of $\Delta x$ were computed, for the most part, by the method of numerical evaluation of conjugate functions developed in appendix $C$ of reference 5. Near $0^{\circ}$ and $180^{\circ}$, because of the rapid variation of $\Delta y(p)$ in these regions (fig. 6), $\Delta x$ was obtained by plotting the integrand of equation (2) and graphical integration. The values of the CMF graphically obtained are indicated in table 2. The velocity distributions, also listed in table 2, were calculated for injet-velocity ratios $v_{n}$ of $0,0.5$, and 1.0 and for nominal iift coefíicients of $0,0.3,0.6,0.9$, and are shown
in figure 7. The derivatives of the CMF used in calculating the velocity distribution were obtained by graphical measurement from the CMF.

The velocity distribution for $c_{2}=0$ and $v_{n}=0.5$ satisfactorily checked that experimentally obtained in reference 4 for $c_{l}=0$ and $v_{n}=0.473$ (fig. $7(c)$ ). The reason for the discrepancy between theoretical and experimental inlet-velocity ratios at which the velocity distributions agreed is not clear. Possible reasons are the changes in downstream shape required by the analysis and a difference in the method of specification of inlet-velocity ratio. The theoretical inlet velocity $v_{n}$ has been defined as the constant value approached by the velocity on the wall of the duct at a short distance behind the leading edge. The experimental determination of the inlet-velocity ratio in reference 4 was not made entirely clear.

The velocity distributions for the $c_{2}$ values 0.3 and 0.6 were also compared with the experimental data of reference 6 obtained for the same duct-inlet section at various angles of attack with Mach numbers of 0.20 . The comparison (given in figs. 7(c) and 7(d)) indicates the validity of the theoretical analysis, particularly of the derivation of the nominal section lift coefficient $c_{l}$.

The feature of the velocity distribution shown in figure 7 that should be particularly noted is the closeness to the leading edge (well within the 8 -percent of the chord length that was studied) at which the greatest changes in velocity distribution occur as a result of a change in operating conditions $v_{n}$ or $c_{2}$. This fact justifies and requires the analysis of a region very close to the inlet, that is, the concentration of the chosen set of the $\varphi$-points close to the inlet.

In order to fllustrate the use of the theory for the staggered case, $m \neq 1.0$, the $C M F \Delta x(\varphi)$ and $\Delta y(\varphi)$ for the symmetrical inlet was used with the m-values 1.5 and 2.0. These shapes and velocities are shown in figures 8 to 11 and are given in tables 3 and 4. In the graphs of the duct inlets, the ordinates have been so adjusted that the upper and lower leading edges are 0.5 and -0.5 , respectively. Although the derived shapes are different from the original unstaggered one, the effect of the stagger is to reduce the velocity peaks for positive lift coefficients.

When a more highly staggered inlet was derived for $m=3.0$ by the foregoing method, the upper contour of the resulting inlet was found to be excessively thick. The points in the physical plane
corresponding to $\Delta x(\varphi), \quad \Delta y(\varphi)$, and $m=-3.0$ were theref ore rearanged by using the same $\Delta x$ and $\Delta y$, regarded, however, as functions of $\theta$, with $\theta$ related to $\varphi$ by the bilinear transformation (see appendix $B$ of reference 5)

$$
\begin{equation*}
\underline{n}=\frac{p^{\prime}+\frac{n-1}{n+1}}{\frac{n-1}{n+1} p^{\prime}+1} \tag{28}
\end{equation*}
$$

where

$$
\begin{equation*}
p=e^{i \varphi}, p^{\prime}=e^{i \theta} \tag{29}
\end{equation*}
$$

and the two circles. The choice $n=1.5$ produced the shape shown in figure 1.2. The ordinates are listed in table 5. It should be noted that the use of an auxiliary bilinear transformation (equation (28), for example) provides a very flexible and convenjent method of distributing a given number of mapping points in the optimum manner. The auxiliary bilinear transformation may also be used to smooth out a sharply peaked function of ip to make its conjugate more easily calculable.

## CONFORMAL MAPPING OF LEADING-EDGE REGIONS

The requirement that the velocity distribution need be accurately known only near the leading edges permitted the great simplification in the mapping consisting of replacement of the doubly connected region by a simply connectea region. The modification of the contour shape far behind the leading edge did not appreciably alter the velocity distribution at the leading edges. Corresponding simplifications can be effected in other problems involving conformal mapping of aerodynamic shapes where only the leading-edge region is of interest.

Thus, for example, the leading-edge region of an isolated airfoil can be regarded as joining a semi-infinite shape as indicated in figure 13. The mapping of such a contour into a circle is quite simple. The leading-edge contour, $z$-plane, is mapped onto a semiinf inite chord line, $\zeta$-plane, by the CMF

$$
\begin{equation*}
z-\xi=\Delta x+i \Delta y=(x-\xi)+i(y-\eta) \tag{30}
\end{equation*}
$$

The semi-infinite chord line is mapped onto an infinite straight line, t-plane, by

$$
\begin{equation*}
\zeta=t^{2} \tag{31}
\end{equation*}
$$

and, in turn, the $t$-plane contour is mapped onto a unit circle by a bilinear transformation, such as

$$
\begin{equation*}
t=i\left(\frac{p+1}{p-1}\right) \tag{32}
\end{equation*}
$$

On the unit circle $p=e^{i \varphi}$, equations (30) to (32) give for the coordinates $x$ and $y$ of the leading edge contour in the physical plane

$$
\begin{align*}
& x=\cot ^{2} \frac{\varphi}{2}+\Delta x(\varphi)  \tag{33}\\
& y=\Delta y(\varphi) \tag{34}
\end{align*}
$$

The mapping of the leading-edge contour by equations (33) and (34) involves little more than the calculation of conjugates.

The velocity distribution is obtained from the ccmplex potential

$$
\begin{equation*}
W=\zeta+A t \tag{35}
\end{equation*}
$$

in which the term $\zeta$ represents the uniform free-stream flow and the term At a circulatory flow around the leading edge. On the leading-edge contour the velocity distribution |dW/dz| becomes

$$
\begin{equation*}
v=\frac{\left(1+\frac{A}{2} \tan \frac{\varphi}{2}\right) \cot \frac{\varphi}{2} \csc ^{2} \frac{\varphi}{2}}{\sqrt{\left(\cot \frac{\varphi}{2} \csc ^{2} \frac{\varphi}{2}-\frac{\partial \Delta x}{d \varphi}\right)^{2}+\left(\frac{\partial \Delta y}{\partial \varphi}\right)^{2}}} \tag{36}
\end{equation*}
$$

A similar development can be made for a cascade of leading-edge regions, which bears the same relation to a cascade of airfoils as the leading-edge region just treated bears to the isolated airfoil.

SAW-TOOIH FUNCTION AS INITIAL APPROXIMATION
In the mapping of semi-infinite contours, it may be required, or it may be simpler, to consider a contour for which the thickness at infinity is finite, as indicated in figure 13. The ordinate function $\Delta y(\varphi)$ will in this case be discontinuous at the value of $\varphi$ corresponding to the point at infinity on the physical-plane contour. The calculation of the CMF for such a contour will be simplified if the Cartesian mapping function $\Delta x+1 \Delta y$ is considered
as the sum of two component Cartesiam mapping functions $\Delta_{1} x+i \Delta_{1} y$ and $\Delta_{2} x+i \Delta_{2} y$, of which $\Delta_{1} x+i \Delta_{1} y$ is analytically known and represents a contour with the same thickness at infinity.

Thus, if the thickness at infinity of the contour in the physical piane is $T$, the "first harmonic" saw-tooth function (fig. 14)

$$
\begin{equation*}
\Delta_{I} y(\varphi)=\frac{T}{\pi}\left(\frac{\pi}{2}-\frac{\varphi}{2}\right) \tag{37}
\end{equation*}
$$

will yield a shape with this thickness. The function $\Delta_{I} x(\varphi)$ conjugate to $\Delta_{\underline{I}}(\varphi)$ may be simply obtained from the integral relation for the conjugate derivative (equation (C3) of reference 5)

$$
\frac{\partial \Delta x(\varphi)}{\partial \varphi}=-\frac{1}{4 \pi} \int_{0}^{2 \pi} \frac{\Delta y\left(\varphi^{\prime}\right)-\Delta y(\varphi)}{\sin ^{2} \frac{\varphi^{\prime}}{2} \frac{-\varphi}{2}} d \varphi^{\prime}
$$

Substitution of equation (37) into (38) and integration (using integration by parts) yielos

$$
\begin{equation*}
\frac{d \Delta_{1} x}{d \varphi}=\frac{T}{2 \pi} \cot \frac{p}{2} \tag{39}
\end{equation*}
$$

which by integration gives for $\Delta_{I} x$

$$
\begin{equation*}
\Delta_{1} x=\frac{T}{\pi} \log _{e} \sin \frac{\varphi}{2} \tag{40}
\end{equation*}
$$

The ordinate function derivative is evidently

$$
\begin{equation*}
\frac{d \Delta_{1} v}{d \varphi}=-\frac{T}{2 \pi} \tag{41}
\end{equation*}
$$

The CMF for a "second harmonic" saw-tooth (fig. 14) corresoonding to a duct-inlet section with thickness $T$ (of each component contour) at infinity may be obtained from that of the first harmonic saw-tocth function by replacing $p / 2$ in equations (37), (39), and (40) by $\varphi$ and by doubling the derivatives. Thus, for the second harmonic saw-tocth function

$$
\left.\begin{array}{ll}
\Delta_{1} y=\frac{T}{\pi}\left(\frac{\pi}{2}-\varphi\right) & 0<\varphi<\pi  \tag{42}\\
\Delta_{1} y=\frac{T}{\pi}\left(\frac{3 \pi}{2}-\varphi\right) & \pi<\varphi<2 \pi
\end{array}\right\}
$$

$$
\begin{gather*}
\frac{d \Delta_{1} y}{d \varphi}=-\frac{T}{\pi}  \tag{43}\\
\Delta_{1} x=\frac{T}{\pi} \log _{e} \sin \varphi  \tag{44}\\
\frac{d \Delta_{I} x}{d \varphi}=\frac{T}{\pi} \cot \varphi \tag{45}
\end{gather*}
$$

The duct-inlet shapes corresponaing to the second harmonic saw-tooth CMF have been calculated by equations (10) and (11) with $m=1.0$ (no stagger) and for $T=0.1,0.2$, and 0.3 . The contours are shown in figure 1.5 . For these shapes the velocity infinitely far inside the duct is, by equations (43), (45), and (26) with $p=\pi$

$$
\begin{equation*}
v_{D C}=\frac{1-B}{I-T} \tag{46}
\end{equation*}
$$

which, when compared with equation (19): shows the effect of narrowing the duct at infinity.

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TABLE 1 - ORDINATES OF SYMMETRICAL DUCT INLET [reference 4 , shape 9$]$

| Station (percent chord from leading edge) | Ordinate of cuter surỉace (measured from center line of channel) (percent chord) | Ordinate of inner surface (measured from center line of channel) (percent chord) |
| :---: | :---: | :---: |
| 0 | 3.343 | 3.34 |
| . 25 | 3.660 | 3.07 |
| . 5 | 3.835 | 3.05 |
| . 75 | 3.076 | 3.05 |
| 1.25 | 4.228 | 3.07 |
| 2.5 | 4.745 | 3.13 |
| 5 | 5.532 | 3.25 |
| 7.5 | 6.137 | 3.36 |
| 10 | 6.652 | 3.50 |
| 15 | 7.467 | 3.78 |
| 20 | 8.093 | 4.08 |
| 25 | 8.593 |  |
| 30 | 8.965 | 4.57 |
| 35 | 9.224 |  |
| 40 | 9.379 | 4.90 |
| 45 | 9.435 |  |
| 50 | 9.391 | 5.10 |
| 55 | 9.240 |  |
| 60 | 8.966 | 4.94 |
| 65 | 8.510 |  |
| 70 | 7.804 | 4.27 |
| 75 | 5.878 |  |
| 80 | 5.816 | 2.54 |
| 85 | 4.679 |  |
| 90 | 3.522 | 1.55 |
| 95 | 2.387 |  |
| 100 | 1.314 | 1.31 |

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TABLE 2.- ORDINATES AND VELOCITY DISTRIBUTIONS FOR SYMMETRICAI DUCT INLET WITH $s=0$ AND $m=1.0$
$\left[\tau=0 ; \varphi_{\mathrm{B}}=75.00^{\circ} ; \varphi_{\mathrm{G}}=285.00^{\circ} ; \varphi_{\mathrm{B}}=6.882^{\circ} ; \varphi_{\mathrm{C}}=353.12^{\circ} ; \mathrm{h}=2.4860\right]$

| $\stackrel{\oplus}{(d e g})$ | $x / h$ | $\begin{gathered} (y / h)+ \\ 0.2011 \\ \text { (ordinate } \end{gathered}$ | $\Delta \pi$ | $\Delta y$ | Velocity, $v$$\left(\nabla_{n}=0 ; B=1.00000\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | $\begin{aligned} & c_{2}=0 \\ & A=0 \end{aligned}$ | $\begin{aligned} & 0.3 \\ & 0.58494 \end{aligned}$ | $\begin{aligned} & 0.6 \\ & 1.16989 \end{aligned}$ | $\begin{aligned} & 0.9 \\ & 1.75483 \end{aligned}$ |
| Upper duct inlet section |  |  |  |  |  |  |  |  |
| $0 \times 7.5$ | $\infty$ | 0.2011 | a-2.8592 | 0 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1 | 12.3540 | . 8662 | a-5.1796 | 1.6534 | 1.0697 | 1.1107 | 1.1517 | 1.1927 |
| 2 | 2.8117 | 1.2098 | a-1.2595 | 2.5076 | 1.1719 | 1.2622 | 1.3524 | 1.4427 |
| 3 | 1.0887 | . 9259 | -. 5144 | 1.8018 | 1.1944 | 1.3334 | 1.4724 | 1.6113 |
| 4 | . 5162 | . 7713 | -. 2265 | 1.4174 | 1.2238 | 1.4157 | 1.6075 | 1.7993 |
| 5 | . 2490 | . 6695 | -. 2306 | 1.1644 | 1.2535 | 1.5025 | 1.7514 | 2.0003 |
| 6 | . 1225 | . 6121 | -. 0546 | 1.0217 | 1.3460 | 1.6721 | 1.9982 | 2.3243 |
| 7 | .0524 | . 5708 | -. 0115 | . 9190 | 1.4799 | 1.9068 | 2.3337 | 2.7606 |
| 8 | . 0221 | . 5410 | . 0400 | . 8448 | 1.6354 | 2.1877 | 2.7400 | 3.2923 |
| 9 | . 0041 | . 5165 | . 0699 | . 7839 | 1.8827 | 2.6185 | 3.3544 | 4.0902 |
| 10 | .0017 | . 4996 | .1060 | . 7420 | 2.0239 | 2.9324 | 3.8408 | 4.7493 |
| 11 | . 0033 | . 4858 | . 1307 | .7078 | 1.7745 | 2.6848 | 3.5951 | 4.5053 |
| 12 | . 0136 | . 4766 | . 1623 | . 6849 | 1.2056 | 1.9109 | 2.6161 | 3.3213 |
| 23 | . 0259 | . 4713 | . 1879 | . 6716 | . 7651 | 1.2754 | 1.7857 | 2.2960 |
| 14 | . 0471 | . 4690 | . 2268 | . 6659 | .4713 | . 8305 | 1.1898 | 1.5490 |
| 15 | . 0713 | . 4682 | . 2655 | . 6640 | . 2991 | . 5609 | . 8227 | 1.0845 |
| 16 | . 1034 | . 4675 | . 3168 | . 6621 | . 1961 | . 3947 | .5933 | . 7920 |
| 17 | .1385 | . 4690 | . 3685 | . 6659 | . 1305 | . 2853 | . 4401 | . 5948 |
| 18 | . 1842 | . 4705 | . 4379 | . 6697 | . 0858 | . 2069 | . 3280 | . .4491 |
| 19 | . 2363 | . 4736 | . 5131 | . 6773 | . 0543 | . 1480 | . 2416 | . 3353 |
| 20 | . 3067 | . 4766 | . 6195 | . 6849 | . 0324 | . 0319 | . 1740 | . 2447 |
| 21 | . 3912 | . 4789 | .7400 | . 6906 | . 0172 | . 0677 | .1182 | . 1687 |
| 22 | .5227 | . 4843 | . 9389 | . 7040 | . 0069 | . 0374 | . 0679 | . 0984 |
| 23 24 | .7401 | . 4950 | a1. 2595 | . 7306 | . 0017 | .0167 | .0318 | . 0468 |
| Lower duct inlet section |  |  |  |  |  |  |  |  |
| 24 | $\infty$ | -0.2011 | a3. 0449 | 0 | 0 | 0 | 0 | 0 |
| 25 | 0.7401 | -. 4950 | a1. 2585 | -. 7306 | . 0017 | . 0134 | . 0284 | . 0434 |
| 26 | . 5227 | -. 4843 | . 9389 | -. 7040 | . 0069 | . 0237 | . 0542 | . 0847 |
| 27 | .3812 | -. 4789 | .7400 | -. 6906 | . 0172 | . 0333 | . 0839 | .1344 |
| 28 | .3067 | -. 4766 | . 6195 | -. 6849 | . 0324 | . 0384 | .1091 | . 1799 |
| 28 | . 2363 | -. 4736 | . 5131 | -. 6773 | . 0543 | . 0393 | . 1329 | . 2266 |
| 30 | .1842 | -. 4705 | . 4379 | -. 6697 | . 0858 | . 0354 | . 1565 | .2776 |
| 31 | .1385 | -. 4690 | . 3685 | -. 6659 | .1305 | .0243 | . 1791 | . 3339 |
| 32 | . 1034 | -. 4675 | . 3168 | -. 6621 | . 1961 | . 0026 | . 2012 | . 3998 |
| 33 | . 0713 | -. 4682 | . 2655 | -. 6640 | .2991 | . 0373 | .2246 | . 4864 |
| 34 | .0471 | -. 4690 | . 2268 | . 66659 | .4713 | . 1120 | . 2472 | . 6065 |
| 35 | . 0259 | -. 4713 | . 1879 | -. 6716 | . 7651 | . 2548 | . 2555 | . 7659 |
| 36 | . 0136 | -. 4766 | . 1623 | -. 6849 | 1.2056 | . 5004 | . 2048 | . 8100 |
| 37 | . 0033 | -. 4858 | .1307 | -. 7078 | 1.7745 | . 8642 | . 0461 | . 9563 |
| 38 | . 0017 | -. 4996 | . 1060 | -. 7420 | 2.0239 | 1.1155 | . 2070 | .7014 |
| 39 | . 0041 | -. 5165 | . 0699 | -. 7839 | 1.8827 | 1.1468 | . 4109 | . 3248 |
| 40 | . 0221 | -. 5410 | . 0400 | -. 8448 | 1.6354 | 1.0831 | . 5308 | .0214 |
| 41 | . 0524 | -. 5708 | -. 0115 | -. 9190 | 1.4799 | 1.0531 | . 6261 | .1992 |
| 42 | . 1225 | -. 6121 | -. 0546 | -1.0217 | 1.3460 | 1.0198 | - 6937 | . 3676 |
| 43 | . 2490 | -. 6695 | -. 1306 | -1.1644 | 1.2535 | 1.0046 | . 7557 | .5068 |
| 44 | . 5162 | -. 7713 | -. 2265 | -1. 4174 | 1.2238 | 1.0320 | . 8402 | . 6484 |
| 45 | 1.0887 | -. 9259 | -. 5144 | -1.8018 | 1.1944 | 1.0554 | . 9165 | . 7775 |
| 46 | 8.8117 | -1.2098 | - -1.2695 | -2.5076 | 1.1719 | 1.0817 | . 8914 | . 9012 |
| 47 | 12.3540 | -. 8662 | a-5.1796 | -1.6534 | 1.0697 | 1.0287 | . 9877 | .9467 |

aobtained by graphical integration.
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TABLE 2. - Concluded
ORDIMATES AND VELOCITY DISTRIBUTIONS FOR SYMMETRICAL DUCT INLET - Conciuded

| (deg) | Veloolty, $V$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left(v_{n}=0.5 ; ~ B=-0.38907\right)$ |  |  |  | $\left(v_{n}=1.0 ; ~ B=-1.55000\right)$ |  |  |  |
|  | $\begin{aligned} & e_{l}=0 \\ & A^{2}=0 \end{aligned}$ | $\begin{array}{\|l\|} \hline 0.3 \\ 0.58494 \\ \hline \end{array}$ | $\begin{aligned} & 0.6 \\ & 1.16989 \\ & \hline \end{aligned}$ | $\begin{array}{\|l\|} \hline 0.9 \\ 1.75483 \end{array}$ | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0.3 \\ & 0.58494 \end{aligned}$ | $\begin{aligned} & 0.6 \\ & 1.16989 \end{aligned}$ | $\begin{aligned} & 0.9 \\ & 1.75483 \end{aligned}$ |
| Opper duct inlet section |  |  |  |  |  |  |  |  |
| $0 \times 7.5$ | 1.0000 | 1.0000 | 1,0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1 | 1.0633 | 1.1043 | 1.1454 | 1.1863 | 1.0580 | 1.0990 | 1.1400 | 1.1810 |
| 2 | 1.1437 | 1.2340 | 1.3242 | 1.4144 | 1.1201 | 1.2104 | 1.3006 | 1.3909 |
| 3 | 1.1288 | 1.2678 | 1.4067 | 1.5457 | 1.0739 | 1.2129 | 1.3518 | 1.4908 |
| 4 | 1.1018 | 1.2936 | 1.4854 | 1.6773 | . 9998 | 1.1916 | 1.3834 | 1.5752 |
| 5 | 1.0529 | 1.3018 | 1.5508 | 1.7997 | . 8852 | 1.1341. | 1.3830 | 1.6319 |
| 6 | 1.0252 | 1.3513 | 1.6774 | 2.0035 | . 7571 | 1.0832 | 1.4093 | 1.7354 |
| 7 | . 9800 | 1.4069 | 1.8338 | 2.2607 | . 5622 | . 9897 | 1. 4160 | 1.8429 |
| 8 | . 87882 | 1.4305 1.4509 | 1.9828 | 2. 2351 | . 2454 | .7977 | 1.3500 | 1.9023 |
| 10 | .3686 | 1.2770 | 2.1868 | 2.9226 3.0940 | .2607 1.0150 | . 4751 | 1.2110 | 1.9468 |
| 11 | . 1212 | . 7891 | 1.6993 | 2.6096 | 1.7055 | . 7952 | . 8121 | 1.7104 |
| 12 | . 4691 | . 2361 | . 9414 | 1.6467 | 1.8687 | 1.1635 | . 4583 | . 2470 |
| 13 | :.6167 | . 1064 | . 4039 | . 9142 | 1.7716 | 1.2613 | . 7510 | . 2407 |
| 14 | . 6405 | . 2813 | . 0780 | . 4372 | 1.5697 | 1.2105 | - 8512 | . 4920 |
| 15 | . 6314 | . 3696 | . 1078 | . 1540 | 1. 4090 | 1.1472 | . 8854 | . 6236 |
| 16 | . 6210 | . 4223 | . 2237 | . 0250 | 1.3038 | 1.1051 | . 8065 | . 7078 |
| 17 | . 6148 | . 4601 | . 3053 | . 1505 | 1.2378 | 1.0830 | . 9282 | . 7734 |
| 18. | . 6086 | . 4875 | . 3664 | . 2453 | 1. 1889 | 1.0678 | . 9467 | . 8256 |
| 19 | . 6008 | . 5071 | . 4135 | . 3198 | 1.1483 | 1.0546 | . 9610 | . 8673 |
| 20 | . 5948 | . 5240 | . 4532 | . 3825 | 1.1190 | 1.0482 | . 9774 | . 9067 |
| 21 | . 5859 | . 5354 | . 4849 | . 4344 | 1.0900 | 1.0395 | . 9890 | . 9395 |
| 22 | . 5435 | . 5130 | . 4825 | . 4519 | 1.0034 | . 9729 | . 9424 | . 9119 |
| 23 | . 5432 | . 5281 | . 5131 | . 4980 | . 9985 | . 9835 | . 9684 | . 9534 |
| 24 | 1.3891 | 1.3891 | 1.3891 | 1.3891 |  |  |  |  |
| Lower duct inlet section |  |  |  |  |  |  |  |  |
| 24 | 1.3891 | 1.3891 | 1.3891 | 1.3891 | 2.5500 | 2.5500 | 2.5500 | 2.5500 |
| 25 | . 5432 | . 5582 | . 5732 | . 5883 | . 9985 | 1.0135 | 1.0286 | 1.0436 |
| 26 | . 5435 | .5740 | . 6045 | . 6350 | 1.0034 | 1.0340 | 1.0645 | 1.0950 |
| 27 | . 5859 | . 6365 | . 6870 | . 7375 | 1.0900 | 1.1407 | 1.1910 | 1.2416 |
| 28 | . 5948 | . 6656 | . 7363 | . 8071 | 1.1190 | 1.1897 | 1.2605 | 1.3313 |
| 29 | . 6008 | . 6944 | . 7880 | . 8817 | 1.1483 | 1.2419 | 1.3355 | 1.4292 |
| 30 | . 6086 | . 7297 | . 8508 | . 9719 | 1.1889 | 1.3100 | 1.4311 | 1.5523 |
| 31 | . 6148 | . 7696 | . 9244 | 1.0792 | 1.2378 | 1.3926 | 1.5473 | 1.7021 |
| 32 | . 6210 | . 8196 | 1.0182 | 1.2169 | 1.3038 | 1.5024 | 1.7010 | 1.8987 |
| 33 | . 6314 | . 8932 | 1.1550 | 1.4168 | 1.4090 | 1.6708 | 1.9326 | 2.1944 |
| 34 | . 6405 | . 9998 | 1.3590 | 1.7183 | 1.5697 | 1.9289 | 2.2882 | 2.6474 |
| 35 | . 6167 | 1.1271 | 1.6374 | 2.1477 | 1.7717 | 2.2819 | 2.7923 | 3.3026 |
| 36 | . 4691 | 1.1743 | 1.8795 | 2.5848 | 1.8687 | 2.5739 | 3.2792 | 3.9844 |
| 37 | . 1212 | 1.0314 | 1.9417 | 2.8520 | 1.7055 | 2.6157 | 3.5261 | 4. 4364 |
| 38 | . 3686 | . 5399 | 1.4484 | 2.3568 | 1.0150 | 1.9234 | 2.8319 | 3.7403 |
| 39 | . 7151 | . 0208 | . 7567 | 1.4925 | . 2607 | . 9966 | 1.7325 | 2.4683 |
| 40 | . 8782 | . 3259 | . 2264 | . 7786 | . 2454 | . 3069 | . 8592 | 1.4114 |
| 41 | . 9800 | . 5531 | . 1262 | . 3007 | . 5622 | . 1353 | . 2916 | . 7185 |
| 42 | 1.0252 | . 6991 | . 3730 | . 0468 | . 7571 | . 4310 | . 1049 | . 2213 |
| 43 | 1.0529 | . 8040 | . 5551 | . 3062 | . 8852 | . 6363 | . 3874 | . 1385 |
| 44 | 1.1018 | . 9100 | . 7182 | . 5264 | . 9998 | . 8080 | . 6162 | . 4243 |
| 45 | 1.1288 | . 9898 | . 8509 | . 7119 | 1.0738 | . 9349 | . 7960 | . 6570 |
| 46 | 1.1437 <br> 1.0833 | 1.0535 1.0223 | .9632 .9813 | .8730 .9403 | 1.1201 1.0580 | 1.0299 1.0170 | .9396 .9780 | .8494 .9350 |
| 47 | 1.0833 | 2.0223 | . 9813 | . 9403 | 1.0580 | 1.0170 | . 9780 | . 9350 |

TABLE 3.- ORDINATES AND VELOCITY DISTRIBUTIONS FOR NONSYMETETCAL DUCT INLET WITH $s=0.132$ AND m $=1.5$
$\left[\tau=-0.0341 ; \varphi_{\mathrm{B}}=109^{\circ} ; \varphi_{G}=289.32^{\circ} ; \varphi_{\mathrm{E}}=6.51^{\circ} ; \varphi_{\mathrm{C}}=353.12^{\circ} ; \mathrm{h}=2.6667\right]$

| $\stackrel{\oplus}{(\operatorname{deg})}$ | $x / h$ | $\begin{gathered} (y / h)+ \\ 0.1650 \\ \text { (ordinate) } \end{gathered}$ | $\begin{gathered} \text { Velocity, } v \\ \left(v_{n}=0.5 ; B=-0.38907\right) \end{gathered}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & C_{l}=0 \\ & A^{2}=0.01518 \end{aligned}$ | $\begin{aligned} & 0.3 \\ & 0.38901 \end{aligned}$ | $\begin{aligned} & 0.6 \\ & 0.76285 \end{aligned}$ | $\begin{aligned} & 0.8 \\ & 1.13668 \end{aligned}$ |
| Upper duct inlet section |  |  |  |  |  |  |
| $0 \times 7.5$ | $\infty$ | 0.1650 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 1 | 6.3926 | . 7850 | 1.0751 | 1.1162 | 1.1571 | 1.1885 |
| 2 | 1.2849 | 1.1053 | 1.2487 | 1.3510 | 1.4533 | 1.5556 |
| 3 | . 4257 | . 8407 | 1.2072 | 1.3709 | 1.5346 | 1.6983 |
| 4 | . 1693 | . 6965 | 1.1023 | 1.3316 | 1.5608 | 1.7900 |
| 5 | . 0559 | . 6016 | . 9625 | 1.2689 | 1.5753 | 1.8817 |
| 6 | . 0159 | . 5481 | . 7539 | 1. 1475 | 1.5712 | 1.9349 |
| 7 |  | . 5096 | . 4219 | . 8743 | 1.3267 | 1.7790 |
| 8 | . 0057 | . 4818 | . 0418 | . 4934 | -. 9451 | 1.3968 |
| 9 | . 0134 | . 4590 | . 2796 | . 1409 | . 5614 | . 9820 |
| 10 | . 0295 | . 4433 | . 5018 | . 1377 | . 2264 | . 5905 |
| 11 | . 0455 | . 4304 | . 6440 | . 3338 | . 0236 | . 2866 |
| 12 | . 06667 | . 4219 | . 7169 | . 4593 | . 2018 | . 0558 |
| 13 | . 0876 | . 4169 | .7479 | . 5357 | . 3235 | .1112 |
| 14 | .1153 | . 4147 | .7295 | . 5609 | . 3922 | .2235 |
| 15 | .1446 | . 4140 | . 6994 | . 5654 | . 4315 | . 2975 |
| 16 | .1804 | . 4133 | . 6740 | . 5663 | . 4586 | . 3509 |
| 17 | . 2184 | . 4147 | . 6561 | . 5687 | . 4813 | . 3939 |
| 18 | . 2655 | . 4161 | . 6406 | . 5700 | . 4995 | . 4290 |
| 19 | . 3182 | . 4190 | . 6252 | . 5693 | . 5134 | . 4576 |
| 20 | . 3875 | . 4219 | . 6128 | . 5697 | . 5267 | . 4837 |
| $2 \lambda$ | - 4657 | - 4230 | . 5985 | . 5673 | . 5361 | .5049 |
| 22 | . 5953 | . 4290 | . 5515 | . 5324 | . 5133 | . 4942 |
| 23 | . 8010 | . 4390 | . 5469 | . 5374 | . 5279 | . 5183 |
| 24 | $\infty$ | . 1650 | 1.3891 | 1.3891 | 1.3891 | 1.3891 |
| Lower duct inlet section |  |  |  |  |  |  |
| 24 | $\infty$ | -0.2100 | 1.3891 | 1.3891 | 1.3891 | 1.3891 |
| 25 | 0.8062 | -. 4840 | .5398 | . 5495 | . 5592 | . 5689 |
| 26 | . 6058 | -. 4740 | . 5373 | . 5571 | . 5769 | . 5967 |
| 27 | . 4855 | -. 4690 | . 5775 | . 6105 | . 6436 | . 6766 |
| 28 | . 4088 | -. 4669 | . 5843 | . 6309 | . 6775 | .7241 |
| 29 | . 3452 | -. 4640 | . 5887 | . 6507 | . 7127 | .7748 |
| 30 | . 2985 | -. 4611 | . 5954 | . 6760 | . 7567 | .8374 |
| 31 32 | . 2576 | .4597 -.4583 | . 6010 | . 7046 | . 8081 | . 9116 |
| 32 33 | . 2264 | -. 4583 | . 6073 | . 7406 | . 8740 | 1.0073 |
| 34 | . 19764 | -. 4.4597 | . 6193 | .7954 | .9714 1.1143 | 1.1474 1.3554 |
| 35 | . 1574 | -. 4619 | . 6157 | . 9536 | 1.21 .2915 | 1.6294 |
| 36 | . $] 462$ | -. 4669 | .4874 | . 9380 | 1.3887 | 1.8394 |
| 37 | . 1362 | -. 4754 | .2085 | . 7658 | 1.3231 | 1.8804 |
| 38 | . 1334 | -. 4883 | .1844 | . 3848 | . .9540 | 1.5232 |
| 39 | . 1325 | -. 5040 | . 5214 | .0187 | . 4840 | . .9866 |
| 40 | . 1435 | -. 5268 | . 7311 | . 3237 | . 0837 | . 4912 |
| 41 | . 1614 | -. 5546 | . 8833 | .5481 | . 2128 | . 1224 |
| 42 | . 2081 | -. 5931 | . 9699 | . 7018 | . 4336 | . 1655 |
| 43 | . 2903 | -. 6466 | 1.0282 | . 8159 | . 6036 | .3913 |
| 44 | . 4663 | -. 7415 | 1.1043 | . 9347 | . 7651 | . 5955 |
| 45 | . 8257 | -. 8857 | 1.1660 | 1.0375 | . 9091 | . 7806 |
| 46 | 1.8893 | -1. 2.503 | 1.2070 | 1.1202 | 1.0334 | . 8466 |
| 47 | 7.6068 | -.8300 | 1.0715 | 1.0330 | 1.0334 | . 9560 |

TABLE 4.- ORDINATES AND VELOCITY DISTRIBUTIONS FOR NOMSYMMETRICAL DUCT INLET WITH $s=0.215$ AND $m=2.0$
$\left.T=0.0374 ; \Phi_{\mathrm{B}}=114.98^{\circ} ; \varphi_{G}=289.12^{\circ} ; \varphi_{\mathrm{E}}=6.19^{\circ} ; \varphi_{\mathrm{C}}=353.12^{\circ} ; \mathrm{h}=2.8525\right]$

|  | $\pi / h$ | $\begin{gathered} (y / h)+ \\ 0.1206 \\ \text { (ordinate) } \end{gathered}$ | $\left(v_{n}=0.5 ; B=-0.38907\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & c_{2}=0 \\ & A^{2}=0.03038 \end{aligned}$ | $\begin{aligned} & 0.3 \\ & 0.30445 \end{aligned}$ | $\begin{aligned} & 0.6 \\ & 0.57852 \end{aligned}$ | $\begin{aligned} & 0.9 \\ & 0.85259 \end{aligned}$ |
| Upper duct inlet section |  |  |  |  |  |  |
| $0 \times 7.5$ | $\infty$ | 0.1206 | 1.0000 | 2.0000 | 1.0000 | 1.0000 |
| 1 | 3.6137 | . 7002 | 1.0655 | 1.1068 | 1.1481 | 1.1895 |
| 2 | . 6084 | . 9997 | 1.3818 | 1.5022 | 1.6226 | 1.7430 |
| 3 | . 1545 | . 7522 | 1.2524 | 1.4466 | 1.6408 | 1.8350 |
| 4 | . 0444 | . 6175 | . 9326 | 1.1822 | 1.4317 | 1.6813 |
| 5 | . 0019 | . 5288 | . 6065 | .9191 | 1.2316 | 1.5442 |
| 6 | . 0009 | . 4738 | . 1917 | . 5156 | . 83396 | 1.1636 |
| 7 | .0091 | . 4427 | . 1527 | .1446 | . 4419 | . 7393 |
| 8 | . 0302 | . 4167 | .3887 | . 1260 | . 1366 | . 3993 |
| 9 | . 0489 | . 3954 | . 5511 | . 3185 | . 0860 | . 1466 |
| 10 | . 0727 | . 3807 | . 6559 | . 4525 | . 2491 | . 0458 |
| 11 | . 0943 | . 3687 | . 7284 | . 5498 | .3711 | . 1925 |
| 12 | .1194 | . 3607 | . 7656 | . 6112 | . 4567 | . 3023 |
| 13 | . 1435 | . 3560 | . 7797 | . 6474 | . 5151 | . 3827 |
| 14 | . 1731 | . 3540 | . 7553 | . 6461 | . 5370 | - 4278 |
| 15 | . 2037 | . 3534 | . 7217 | . 6324 | . 5430 | . 4537 |
| 16 | . 2399 | . 3527 | . 6929 | . 6194 | . 5461 | . 4726 |
| 17 | . 2778 | . 3540 | . 6717 | . 6111 | . 5506 | . 4900 |
| 18 | - 3240 | . 3554 | . 6531 | . 6036 | . 5541 | . 5046 |
| 19 | - 37.51 | . 3580 | . 6350 | . 5954 | . 5558 | . 5162 |
| 20 | . 4417 | . 3607 | . 6203 | . 5895 | . 5587 | . 5279 |
| 21 | . 5200 | . 3627 | . 6039 | . 5814 | . 5688 | . 5363 |
| 22 | . 6390 | . 3674 | . 5550 | . 5412 | . 5273 | . 5134 |
| 23 | . 8325 | . 3767 | . 5485 | . 5416 | . 5347 | . 5277 |
| 24 | $\infty$ | .1206 | 1.3891 | 1.3891 | 1.3891 | 1,3891 |
| Lower duct inlet section |  |  |  |  |  |  |
| 24 | $\infty$ | -0.2300 | 1.3891 | 1.3891 | 1.3891 | 1.3891 |
| 25 | 0.8399 | -. 4861 | . 5384 | . 5455 | . 5526 | . 5598 |
| 26 | . 6537 | -. 4768 | . 5345 | . 5491 | . 5638 | . 5784 |
| 27 | .5423 | -. 4721 | . 5738 | . 5983 | . 6228 | . 6474 |
| 28 | . 4716 | -. 4701 | . 5798 | . 6145 | . 6492 | . 6839 |
| 29 | . 4130 | -. 4675 | .5836 | . 6299 | . 6763 | . 7226 |
| 30 | . 3702 | -. 4648 | . 5900 | . 6504 | . 7108 | . 77.13 |
| 31 | . 3328 | -. 4635 | . 5957 | . 6735 | . 7512 | . 8289 |
| 32 | . 3043 | -. 4621 | . 6028 | .7030 | . 8033 | . 9036 |
| 33 | . 2782 | -. 4628 | . 6165 | . 7490 | . 8815 | 1.0140 |
| 34 | . 2587 | -. 4635 | - 6328 | . 8140 | . 09953 | 1.1765 |
| 35 | .2414 | -. 4655 | . 6221 | . 8744 | 1.1266 | 1.3789 |
| 36 | . 2311 | -. 4701 | . 5057 | . 8361 | 2.1665 | 1.4970 |
| 37 | . 2215 | -. 4781 | - 2602 | . 6600 | 1.0597 | 1.4595 |
| 38 | . 2182 | -. 4901 | . 0828 | . 3270 | . 7367 | 1.1464 |
| 39 | . 2160 | -. 5048 | . 3965 | . 0215 | - 3535 | . 7285 |
| 40 | . 2234 | -.5261 -.5522 | . 6176 | .3004 .5207 | . 0168 | . 3339 |
| 41 | - 2355 | -. 5522 -.5882 | . 7928 | . 5207 | - 2486 | . 0235 |
| 48 | .2702 .3306 | -.5882 -.6382 | .9072 | . 6814 | . 4557 | . 2299 |
| 43 44 | . 3306 | -. 6382 -.7869 | .9906 1.0874 | . 8060 | . 6216 | . 4369 |
| 45 | . 7152 | -. 8617 | 1.1876 | 1.0673 | . 9471 | . 8269 |
| 46 | 1.4561 | -1.1091 | 1.2634 | 1.1787 | 1.0939 | 1.0091 |
| 47 | 5.3157 | -. 8096 | 1.0653 | 1.0289 | . 9924 | . 9559 |

TABLE 5.- ORDINATES OF NONSYMMETRICAL DUCT INLET WITH $s=0.280$ AND $m=3.0$
$[n=1.5 ; \tau=0.0310 ; h=2.6613]$

| $\begin{gathered} \stackrel{\theta}{d^{e g}} \text { ) } \end{gathered}$ | $\left(\begin{array}{l} \Phi \\ ) \end{array}\right.$ | $\mathrm{x} / \mathrm{h}$ | $\begin{gathered} (y / h)+0.1306 \\ \text { (ordinate) } \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| Upper duct inlet section |  |  |  |
| $0 \times 7.5$ | 0 | $\infty$ | 0.1306 |
| 1 | 5.004 | 6.4980 | . 7519 |
| 2 | 10.032 | 1.1177 | 1.0729 |
| 3 | 15.108 | . 3003 | . 8077 |
| 4 | 20,256 | . 0902 | . 6632 |
| 5 | 25.503 | . 0130 | . 5682 |
| 6 | 30.874 | . 0011 | . 5145 |
| 7 | 36.398 | . 0074 | . 4759 |
| 8 | 42.103 | . 0312 | . 4481 |
| 9 | 48.021 | . 0539 | . 4252 |
| 10 | 54.184 | . 0829 | . 4094 |
| 11 | 60.625 | . 1097 | . 3966 |
| 12 | 67.380 | . 1407 | . 3880 |
| 13 | 74.483 | . 1704 | . 3830 |
| 14 | 81.969 | . 2059 | . 3809 |
| 15 | 89.870 | . 2425 | . 3801 |
| 16 | 98.213 | . 2851 | . 3794 |
| 17 | 107.018 | . 3293 | . 3809 |
| 18 | 116.293 | . 4063 | . 3823 |
| 19 | 126.031 | . 4410 | . 3851 |
| 20 | 136.207 | . 5159 | . 3880 |
| 21 | 146.773 | . 6037 | . 3901 |
| 22 | 157.658 | . 7349 | . 3952 |
| 23 | 168.770 | . 9460 | . 4052 |
| 24 | 180.000 | $\infty$ | . 1306 |
| Lower duct inlet section |  |  |  |
| 24 | 180.000 | $\infty$ | -0.2451 |
| 25 | 191.230 | 0.9617 | -. 5197 |
| 26 | 202.342 | . 7664 | -. 5097 |
| 27 | 213.227 | . 6513 | -. 5046 |
| 28 | 223.793 | . 5799 | -. 5025 |
| 29 | 233.969 | . 5222 | -. 4996 |
| 30 | 243.707 | . 4817 | -. 4968 |
| 31 | 252.982 | . 4473 | -. 4954 |
| 32 | 261.787 | . 4232 | -. 4939 |
| 33 | 270.130 | . 4024 | -. 4946 |
| 34 | 278.031 | . 3895 | -. 4954 |
| 35 | 285.517 | . 3802 | -. 4975 |
| 36 | 292.620 | . 3799 | -. 5025 |
| 37 | 299.375. | . 3825 | -. 5111 |
| 38 | 305.816 | . 3946 | -. 5239 |
| 39 | 311.979 | . 4119 | -. 5397 |
| 40 | 317.897 | . 4454 | -. 5626 |
| 41 | 323.602 | . 4926 | -. 5904 |
| 42 | 329.126 | . 5787 | -. 6290 |
| 43 | 334.497 | . 7176 | -. 6827 |
| 44 | 339.744 | . 9830 | -. 7777 |
| 45 | 344.892 | 1.5028 | -. 9222 |
| 46 | 349.968 | 2.9347 | -1.1874 |
| 47 | 354.996 | 10.1469 | -. 8664 |


(a) Actual.

(b) Ańalyzed.

Figure 1.- Wing-duct installation.

Fig. 2
NACA RM NO: E7C24


Figure 2.- Conformal relation of $\zeta$-, $t-$, and p-planes.

Fig. 4

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4, shape 9). $\mathrm{m}=1.0$.
Figure 4.- Symmetrical duct-inlet section (reference


Figure 5.- Leading edge of symmetrical duct-inlet section with $s=0$ and $m=1.0$.

Fig. 6


Figure 6.- Cartesian mapping function for duct-inlet sections.

(a) Tpper Leading edge: $V_{n}=0$.

Pigure 7.- Velocity distribution on upper and lower leading edges of symetrical ductinlet section vith $a 0$ and $m=1.0$.

(b) Lower leading edge; $\mathrm{v}_{\mathrm{n}}=0$.

Figure 7. - Continued. Velocity distribution on upper and lower leading edges of symmetrical duct-inlet section with $s=0$ and $m=1.0$.

(c) Upper leading edge; $v_{n}=0.5$.

Figure 7. - Continued. Velocity distribution on upper and lower leading edges of symmetrical duct-inlet section rith $s=0$ and $m=1.0$.

(d) Lower leading edge; $v_{n}=0.5$.

Figure 7. - Continued. Velocity distribution on upper and lower leading edges of symmetrical duct-inlet section with $s=0$ and $m=1.0$.
Velocity, v

(e) Upper leading edge; $\nabla_{n}=1.0$.

Figure 7. - Continued. Velocity distribution on upper and lower leading edges of symmetrical duct-inlet section with $s=0$ and $m=1.0$.

(f) Lower leading edge; $v_{n}=1.0$;

Figure 7. - Concluded. Velocity distribution on upper and lower leading edges of - symmetrical duct-inlet section with $s=0$ and $m=1.0$.


Figure 8.- Leading edge of nonsymmetrical duct-inlet section with $s=0.132$ and $m=1.5$.

Fig. 9 a
velocity, $v$

(a) Upper leading edge.

Figure 9. - Velocity distribution on upper and lower leading edges of nonsymetrical duct-inlet seetion $w i t h=0.18$ and $m=1.5 . V_{n}=0.5$.

(b) Lower leading edge.

Figure 9. - Concluded. Velocity distribution on upper and lower leading edges of nonsymmetrical duct-inlet'section with $s=0.132$ and $m=1.5 . \nabla_{n}=0.5$.

Fig. 10


Figure 10. - Leading edge of nonsymmetrical duct-inlet section with $s=0.215$ and $m=2.0$.

(a) Opper leading edge.

Plgure 11. - Velocity distribution on upper and lower leading edges of nonsymetrical duct-inlet section with $E=0.215$ and $m=2.0$. $v_{n}=0.5$.
Velocity, v

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|  |  |  |  |  |  |  |  |  |  |  |  |  | $\square$ |

(b) Lower leading edge.

Figure 11. - Concluded. Velocity distribution on upper and lower leading edges of nonsymmetrical duct-inlet section with $s=0.215$ and $w_{i}=2.0 . v_{n}=0.5$.


Pigure 12. - Leading edge of nonsymmetrical duct-inlet section with $s=0.280$ and $m=3.0 . n=1.5$.



Figure 13.- Mapping of leading-edge region for isolated airfoils.


Fig. 15


