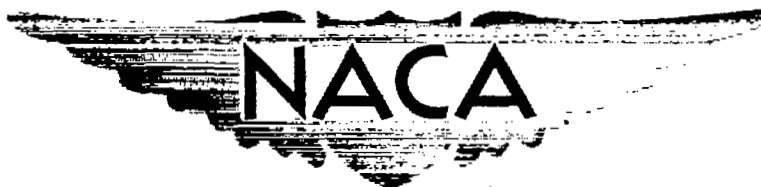


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RESEARCH MEMORANDUM

CORRELATION OF ANALOG SOLUTIONS WITH EXPERIMENTAL
SEA-LEVEL TRANSIENT DATA FOR CONTROLLED
TURBINE-PROPELLER ENGINE, INCLUDING
ANALOG RESULTS AT ALTITUDES

By James Lazar and Wilfred L. DeRocher, Jr.

Lewis Flight Propulsion Laboratory
Cleveland, Ohio

FOR REFERENCE

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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

WASHINGTON
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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

RESEARCH MEMORANDUM

CORRELATION OF ANALOG SOLUTIONS WITH EXPERIMENTAL SEA-LEVEL

TRANSIENT DATA FOR CONTROLLED TURBINE-PROPELLER ENGINE

INCLUDING ANALOG RESULTS AT ALTITUDES

By James Lazar and Wilfred L. DeRocher, Jr.

SUMMARY

A satisfactory correlation was obtained between experimental sea-level transient data at constant flight speed and solutions from the analog representation. The analog representation is accomplished by transfer functions that were formed from a frequency-response analysis of the experimental transient data as obtained from the controlled engine. This analog representation was then used to compute system response at altitude.

The engine-control system with an underdamped sea-level turbine-speed response and fixed-control constants resulted in an oscillatory system at 35,000 feet. Variation of control constants to maintain sea-level turbine-speed response at all altitudes resulted in large blade-angle initial overshoot at 35,000 feet. This large blade-angle overshoot may result in over torque at 35,000 feet if the sea-level overshoot approaches maximum allowable torque. Variation of control constants to maintain system loop gain and ratio of engine time constant to control time constant at sea-level values resulted in a similar initial turbine speed and blade-angle overshoots at 35,000 feet, but in an increase in the time required for turbine speed to first reach its final value.

INTRODUCTION

Early flight tests of controlled turbine-propeller engines indicated that a controlled engine system that is stable at low altitudes and low flight speeds is not necessarily stable at high altitudes and high flight speeds (reference 1). In collaboration with the Air Materiel Command, U. S. Air Force, an investigation was initiated at the NACA Lewis laboratory to study reasons for the trend toward instability with increase in altitude and flight speed, to provide a means for predicting the altitude behavior on a controlled turbine-propeller engine, and to indicate means for avoiding instability at altitude or high flight speed.

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In order to accomplish the objectives of this program, the Air Materiel Command provided the NACA with turbine-propeller engines and several types of control system. The first phase of this engine investigation showed that the dynamic relation of turbine speed to fuel flow or blade angle is approximately a first-order lag and that linear differential equations are applicable over the sea-level static operating range of the T31-1 turbine-propeller engine (reference 2).

This report presents the correlation of analog solutions with experimental sea-level transient data for the Aeroproducts AT-1 (modified) control on the T31-1 engine and analog results for altitude conditions at zero ram. The control varies blade angle to obtain a desired turbine speed while the power output of the engine is varied by adjusting the engine fuel flow. The control is essentially integral plus proportional in action and was modified by the manufacturer at the request of the NACA so that the amount of integral and the amount of proportional action could be varied.

Transient-response data for the engine and the control were obtained from operation of the controlled engine system in a sea-level static test stand. A transfer-function representation of each of the loop components was determined from analysis of the transient data. These component transfer functions were used to represent the system on an analog and because the comparison of analog solutions and experimental data was satisfactory, the transfer functions were used to study the altitude response of the system. The analog representation was first used to investigate the effect of altitude on the controlled engine system with fixed control constants. In addition, two methods of varying the control constants to compensate for the effect of altitude on the system were studied.

APPARATUS AND INSTRUMENTATION

Engine

Type	Turbine propeller, T31-1
Compressor	Axial flow
Burner section	Nine reverse-flow combustion chambers
Turbine	Single stage, mixed flow
Exhaust nozzle	Fixed area
Speed range	11,000 to 13,000 rpm
Maximum turbine-outlet temperature	1265° F

Propeller

Type	Aeroproducts A542F-17
Diameter	12 feet, 1 inch
Beta arm	Input lever for propeller-pitch-change mechanism
Action	Proportional relation between beta arm and blade angle
Pitch-change mechanism	Hydraulic, self contained

Control

Type	Aeroproducts AT-1 (modified)
Action	Proportional plus integral
Control mechanism	Hydraulic, self contained
Modifications	Proportional and integral constants were provided with range of adjustments by Aeroproducts Division of General Motors Corporation

Steady-State Instruments

Turbine speed	a-c. tachometer generator coupled to drag-type tachometer indicator; maximum error $\pm 1/3$ of 1 percent for full scale
Engine fuel flow	Calibrated A.S.M.E. sharp-edged orifice with bellows-type differential pressure gage; maximum error ± 1 percent of full scale
Propeller-blade angle	Position circuit (fig. 1); maximum error $\pm 1/2^\circ$
Speed-setting-lever position	Position circuit (fig. 1); maximum error ± 1 percent of full scale
Load torque	Oil pressure of self-balancing hydraulic system, which acts on ring gear in reduction unit; maximum error ± 1 percent of full scale
Turbine-outlet temperature	Chromel-alumel thermocouple; maximum error $\pm 20^\circ$ F

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Transient Instruments

Turbine speed	d-c. tachometer generator with filter circuit to oscillograph galvanometer; break frequency of filter circuit, 0.53 cycle per second
Engine fuel flow	Position circuit (fig. 1); potentiometer connected to pointer of differential pressure gage connected to A.S.M.E. sharp-edged orifice; natural frequency, 10 to 15 cycles per second
Propeller-blade angle	Position circuit (fig. 1); potentiometer connected to blade shank; slip-ring device used for electrical connection; natural frequency of oscillograph element, 40 cycles per second
Speed-setting-lever position	Position circuit (fig. 1); natural frequency of oscillograph element, 40 cycles per second
Propeller-input-lever (beta arm) position	Position circuit (fig. 1); natural frequency of oscillograph element, 40-cycles-per-second
Turbine-outlet temperature	Chromel-alumel thermocouple; break frequency, 0.1 cycle per second
Transient-data recorder	Photorecording oscillograph with critically damped 40-cycles-per-second galvanometer elements (changes recorded from initial operating point). Each oscillogram was calibrated by photographs of steady-state instruments taken before and after each run.
Time scale	10 cycles per second; voltage from audio-oscillator. Checked by 60 cycles-per-second line frequency.

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DETERMINATION OF TRANSFER FUNCTIONS

For purposes of analysis, the engine and the control system are represented by the block diagram of figure 2. All symbols are defined in the appendix. Each of the system components, control, propeller-pitch-change mechanism, engine, and speed-measuring instrument, are indicated by a block. In each of the blocks, the transfer

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function $KG(i\omega)$ relates the output to the input of that particular block (reference 3). Speed error is formed by a comparison of required speed and measured speed. The power output of the engine is varied by the engine fuel flow.

The determination of the transfer function for each component of the control system was necessary for the analog studies. Three steps were used to determine the transfer functions: obtaining controlled engine experimental transient-response data, harmonic analysis and frequency-response calculations, and fitting the transfer functions to the frequency-response data.

Transient response of controlled system to disturbances in speed setting. - It was desired to determine the transfer functions of speed to blade angle, blade angle to beta arm, and beta arm to speed error. Transient changes in turbine speed, blade angle, beta arm, and speed setting were recorded on a photorecording oscillograph for ramp-type disturbances in speed setting. The engine fuel flow was maintained constant throughout these runs. These transient data were obtained for various values of the integral and proportional control constants, which could be varied independently by two screw-type adjustments. An example of a transient run is shown in figure 3, which includes the 10-cycle-per-second timing marks. Contact with successive turns on the winding of the potentiometers created the multitude of small steps in the traces of speed setting, blade angle, and beta arm. The temperature trace is not sufficiently accurate to be useful because of the low sensitivity.

Harmonic analysis and frequency response. - In order to determine the transfer function of each system component (fig. 2), the frequency characteristic of each component was formed. The transformation from the time domain to the frequency domain was accomplished by harmonic analysis. Methods of harmonic analysis that are used in this report and that apply to gas-turbine engines are discussed in reference 4. For this particular work, the integrals of the harmonic analysis were evaluated using Bickley's approximation formula for six differences with an IBM digital computer.

Results of the harmonic analysis of the input and output to each component are combined to compute the frequency characteristic. The frequency characteristic may be represented by the amplitude ratio and the phase angle of the output with respect to the input of the component as a function of frequency. The phase angle and the logarithm of the amplitude ratio were plotted against the logarithm of the frequency for each of the components, as is shown in figure 4.

Frequency-response data for the engine and the speed-measuring instrument are shown in figures 4(a) and 4(b), for the propeller-pitch-change mechanism in figures 4(c) and 4(d), and for the control in figures 4(e) and 4(f). Figure 4 is discussed in greater detail in the next section.

Transfer functions of system components. - A transfer function may be considered as a function of frequency and thus a frequency characteristic can be prepared for each transfer function. Conversely, each frequency characteristic may be represented by a transfer function.

For the engine and the speed-measuring instrument, the frequency characteristic as defined by the data points in figures 4(a) and 4(b) indicates that the transfer function may be two lags in series. The form of the transfer function is

$$[KG(i\omega)]_e [KG(i\omega)]_r = \left(\frac{-K_e}{1+i\tau_e\omega} \right) \left(\frac{K_r}{1+i\tau_r\omega} \right) \quad (1)$$

From equation (1), the amplitude ratio A and the phase angle ϕ written as functions of frequency ω are

$$A = K_e K_r \sqrt{\left(\frac{1}{1+\tau_e^2\omega^2} \right) \left(\frac{1}{1+\tau_r^2\omega^2} \right)} \quad (2)$$

and

$$\phi = \tan^{-1} \frac{-\omega(\tau_e + \tau_r)}{1 - \tau_e \tau_r \omega^2} \quad (3)$$

Equation (3) may be written for values of ω at -45° and at -90° from figure 4(b) and the two simultaneous equations solved for engine and speed-measuring time constants, τ_e and τ_r , respectively. The value of speed-measuring-instrument gain K_r is 1 so that the steady-state value of the measured turbine speed N_m is the actual turbine speed N_e . The engine gain K_e is the ratio of the steady-state change in turbine speed to the steady-state change in blade angle β . The negative sign before K_e in equation (1) is the result of an increase in speed due to a decrease in blade angle. Equations (2) and (3) with appropriate values of the constants have been plotted as the dashed lines in figures 4(a) and 4(b), respectively. For frequencies less than 2 radians per second, the variation between the experimental frequency characteristic and the transfer-function

approximation is in the order of 2 percent in the amplitude ratio against frequency plot (fig. 4(a)) and in the order of 4° in the phase angle against frequency plot (fig. 4(b)). Reference 2 and more recent data indicate that the transfer function of turbine speed to blade angle is a first-order lag, thus the second lag is attributed to the speed-measuring instrument.

The action of the propeller-pitch-change mechanism is such that a position of the input (beta arm) results in a corresponding position of the output (blade angle). An examination of transient data indicated that the propeller-pitch-change mechanism had a dead band and also a lag due to the hydraulic amplifier. The dead-band effect can be observed in figure 3 where the blade angle does not move until the beta arm has arrived at some value. As these nonlinearities are not easily represented, a first-order lag

$[KG(i\omega)]_{\beta} = \frac{K_{\beta}}{1+i\tau_{\beta}\omega}$ was assumed to represent the transfer function

for the propeller-pitch-change mechanism. The variation in time constant for a series of runs was determined using the 22.5° point on the plot of phase angle against frequency. The time constant fell in the range of 0.2 to 0.45 second with 0.3 second as an average. The propeller-pitch-change-mechanism gain K_{β} was made unity so that the units could all be combined in the proportional and integral constants of the control. The frequency characteristic of the propeller-pitch-change-mechanism transfer function approximation $[KG(i\omega)]_{\beta} = \frac{1}{1+i0.3\omega}$ is plotted as the dashed lines of

figures 4(c) and 4(d). For frequencies less than 2 radians per second, the variation between the transfer-function approximation and the frequency characteristic is of the order of 20 percent for the amplitude ratio against frequency plot in figure 4(c) and of the order of 6° for the phase angle against frequency plot of figure 4(d).

The data points in figures 4(e) and 4(f) define the frequency characteristic of the control and indicate that the form of the control transfer function should be integral plus proportional, that is,

$$[KG(i\omega)]_c = -\left(K_p + \frac{K_i}{i\omega}\right) = -K_p \left(1 + \frac{1}{i\tau_c\omega}\right) \quad (4)$$

where the control time constant τ_c is equal to control proportional constant K_p divided by control integral constant K_i . From equation (4), the amplitude ratio and phase angle are

$$A = \frac{1}{\sqrt{K_p^2 + \frac{K_i^2}{\omega^2}}} \quad (5)$$

and

$$\phi = \tan^{-1} \frac{K_i}{K_p \omega} \quad (6)$$

The amplitude ratio approaches K_p as ω approaches infinity. The value of K_p is taken as the value of the amplitude ratio at the higher frequencies of figure 4(e). Scale factors for the amplitude ratio are determined from the calibration of the experimental transient runs. Also from equation (5), the amplitude ratio is approximately equal to K_i/ω for low values of frequency. For a value of K_p determined from the high frequencies in figure 4(e) and a value of K_i determined from the low frequencies in figure 4(e), the resulting frequency characteristic of the transfer function did not agree too well with the experimental frequency characteristic as defined by the data points in figures 4(e) and 4(f). An examination of the accuracy of the method used to compute the experimental frequency characteristic of figures 4(e) and 4(f) indicated that inaccuracies were more probable in the low-frequency range. These inaccuracies are due to the fact that a small error in either speed setting or turbine speed, when these quantities are approximately equal, means a large error in their difference. Because of this inaccuracy, the dotted lines of figures 4(e) and 4(f) were obtained by substituting other values of K_i into equations (5) and (6) until a reasonable approximation was found. For frequencies less than 2 radians per second, the variation between the transfer-function approximation and the experimental frequency characteristic is of the order of 20 percent for the amplitude ratio against frequency plot in figure 4(e) and of the order of 14° for the phase angle against frequency plot in figure 4(f).

Range of control constants. - It is possible to adjust independently the values of the integral and proportional constants for the control by two screw-type adjustments. The proportional setting is defined as the number of turns of the adjusting screw from its full-out position and the integral setting is defined as the number

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of turns of the adjusting screw from its full-in position. Several runs were made at each setting of the control adjusting screws. The results of these runs are presented in the control calibration curves (figs. 5(a) and 5(b)). The proportional constant may be varied from approximately 0.004° to 0.0085° per rpm and the integral constant from approximately 0.0025° to 0.0061° per second per rpm. For any position of the control adjusting screws, the values of the proportional and integral constants may vary as much as 15 percent from the values as given by curves in figure 5. This error is due in part to a steady-state instrumentation error of ± 10 percent of the transient change and in part to an inability to measure the actual input (speed error) to the control.

COMPARISON OF ANALOG SOLUTIONS WITH EXPERIMENTAL DATA

The transfer functions were used as a basis to form an analog of the system. Analog solutions were obtained for comparison with experimental transient data to determine the validity of the representation.

An electronic-type analog was used in this study. The analog block diagram is similar to the control-system block diagram presented in figure 2. Scale factors were determined from the criterion that loop gains for the real and analog systems be identical. The maximum time for the analog to complete a solution determined the time scale factor. Analog solutions are displayed in the form of traces on a cathode-ray oscilloscope with time as the abscissa and a system parameter as the ordinate.

A comparison of computed and experimental transient response data is shown in figure 6. For the experimental transient data (figs. 6(a) and 6(b)), the control constants were set close to their maximum values and for the experimental transient data (figs. 6(c) and 6(d)), the setting was close to minimum values. The transfer functions and their constants for the analog solutions of figure 6 were determined by the preceding method from the experimental transient data. In all cases, the number of oscillations and the percentage overshoot of the analog solutions and the experimental transient data were similar. The deviation of the analog solutions from the experimental data is partly due to the nonlinearities of the propeller-pitch-change mechanism. One of these nonlinearities is indicated in the photorecording oscillograph trace of figure 3 as the time elapsed from the initial beta-arm movement to the initial blade-angle movement. If the analog

solutions are translated to the right by the amount of this elapsed time, about 0.3 second, a much better agreement between the analog solutions and the experimental transient data will be obtained.

As the agreement between the analog solutions and experimental transient data is considered to be satisfactory, an analog investigation of response at altitude could be made.

ALTITUDE RESPONSE OF CONTROLLED SYSTEM

For the engine, there are two factors that vary with altitude under conditions of constant flight speed: (1) the engine gain factor, and (2) the engine time constant. The engine time constant has been shown analytically to vary with altitude pressure and temperature (reference 5) in accordance with the following relation:

$$\tau_e = \tau_{e, \text{corr}} \frac{\sqrt{\theta}}{\delta}$$

where τ_e is the engine time constant for any altitude, $\tau_{e, \text{corr}}$ is the time constant for NACA standard sea-level conditions, θ is the temperature ratio, and δ is the pressure correction factor. This relation has also been experimentally verified at this laboratory. Correction factors are also applied to the engine gain as follows

$$K_{e, \text{corr}} = \frac{\Delta N_{\text{corr}}}{\Delta \beta_{\text{corr}}} = \frac{\Delta N}{\sqrt{\theta}} \cdot \frac{1}{\Delta \beta} = \frac{K_e}{\sqrt{\theta}}$$

or

$$K_e = K_{e, \text{corr}} \sqrt{\theta}$$

where K_e is the engine gain at any altitude and $K_{e, \text{corr}}$ is the engine gain at NACA standard sea-level conditions. Based on NACA standard altitude tables, the variation in engine time constant from sea level to 35,000 feet is 371 percent of its sea-level value, whereas the variation in engine gain factor from sea level to 35,000 feet is only 13 percent.

For analog studies, a single sea-level value of engine time constant was considered. This requires an examination of the values of the engine time constant throughout the sea-level operating range of the engine. Sea-level equilibrium characteristics

of the T31-1 engine with the Aeroproducts A542F-17 propeller are shown in figure 7 where load torque, referred to the turbine, is plotted against turbine speed for lines of constant blade angle and for lines of constant fuel flow. The acute angle between the intersection of a line of constant fuel flow and a line of constant blade angle has been shown to be indicative of the engine time constant (reference 2). It can be seen that variation of this angle is less than two to one; thus the variation of the engine time constant will also be in the order of two to one. As the variation in engine time constant is not large, a representative value of 2.9 seconds was chosen and a single study performed for this operating point. Another factor is that fuel-flow disturbances are not considered in the analog studies because the stability of a linear system may be studied by means of either fuel flow or speed-setting disturbances. In this report, only speed-setting disturbances were investigated.

Altitude pressure and temperature were not sensed by the original control component, thus the control constants do not vary with altitude. In order to investigate the condition of control constants invariant with altitude, analog solutions for turbine-speed and blade-angle response were obtained for sea level, 25,000 feet, and 35,000 feet.

The system response was also investigated for two methods of control compensation at 35,000 feet. These two methods of control compensation are: (1) control constants varied to maintain the sea-level turbine-speed response at all altitudes, and (2) control constants varied to maintain the sea-level loop gain and the ratio of engine time constant to control time constant at all altitudes.

Control constants invariant with altitude. - The control constants were not designed to vary with altitude or flight speed, thus the system response was investigated for the condition of fixed control constants assuming constant flight speed. For this condition, only the engine gain factor and engine time constant vary with altitude. The values of the component constants and the response of turbine speed and blade angle to a sudden change in speed setting for the three altitudes are shown in figures 8(a) and 8(b). The system becomes more oscillatory as the altitude is increased as shown in figure 8(a), and the initial turbine-speed overshoot at 35,000 feet is twice the initial overshoot at sea level. In addition, as the altitude increases from sea level to 35,000 feet, the time for turbine speed to initially reach its final value increases from 1 second to 3.5 seconds and the time for turbine speed to settle out at its final value increases from 12 seconds to 65 seconds. The blade-angle response curves of figure 8(b) show the same forms of oscillation as the

speed response curves; also, the initial overshoot at 35,000 feet is approximately twice the initial overshoot at sea level. Variation in the final value of blade angle is due to the change in the engine gain factor with altitude. It should be noted that the effect of variation in flight speed is not considered in this report.

An engine and control system, if operated as shown by the turbine-speed and blade-angle responses of figures 8(a) and 8(b) for 35,000 feet, could be seriously damaged, particularly when operated near the speed limit. Thus, this system with an underdamped sea-level turbine-speed response and fixed control constants may result in an unsafe system at 35,000 feet. If the control constants had been chosen to give a slightly under-damped system at 35,000 feet and were invariant with altitude, then an overdamped system with a very long time to reach its final value would result at sea level.

Control constants varied to maintain sea-level turbine-speed response at all altitudes. - One of the primary difficulties with the system when the control constants were fixed was the widely varying speed response with altitude under conditions of constant flight velocity. Because of this variation in speed response with fixed control constants, an investigation was conducted to determine the values of control constants that would result in sea-level turbine-speed response at 35,000 feet. The values of loop constants and the turbine-speed and blade-angle responses for 35,000 feet are shown in figures 9(a) and 9(b) as curve 2. Turbine-speed response as shown by curve 2 (fig. 9(a)) is identical to the sea-level turbine-speed response, curve 1. However, the blade-angle response as shown by curve 2 is very different from the sea-level blade-angle response, curve 1 (fig. 9(b)). The blade-angle initial overshoot is 650 percent of final blade-angle change and the blade-angle initial undershoot is 100 percent of final blade-angle change at 35,000 feet. These high values of blade-angle overshoot and undershoot could result in excessive torques and possible damage to the reduction gearing. At increased altitudes, however, an increase in blade-angle overshoot over that at sea level can be tolerated because of altitude density reductions.

The advantage of this system is the identical speed response at all altitudes. The disadvantages are the excessive blade-angle initial overshoot and initial undershoot at high altitude and the complication of additional sensing and computing equipment in the control to attain the altitude compensation.

Control constant varied to maintain sea-level loop gain and ratio of engine time constant to control time constant at all altitudes. - Another method of altitude compensation investigated was the condition of fixed loop gain and fixed ratio of engine time constant to control

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time constant. In general, if the loop gain and the time constant ratio are fixed, then the response will be similar at all altitudes. However, at an altitude of 35,000 feet, the propeller-pitch-change-mechanism lag and the turbine-speed-recording lag become insignificant with respect to the increased engine and control time constants, and the response is less oscillatory at 35,000 feet than at sea level. The values of the loop constants and the turbine-speed and blade-angle responses for 35,000 feet are shown in figures 9(a) and 9(b) as curve 3.

The initial overshoot of the speed response at 35,000 feet as shown by curve 3 is less than the initial overshoot of the speed response at sea level, as shown by curve 1 (fig. 9(a)). However, the time for turbine speed to initially reach its final value at 35,000 feet is about 3 seconds as compared to only about 1 second at sea level. The initial blade-angle overshoot at 35,000 feet is 110 percent of the final blade-angle change as shown by curve 3 and 140 percent at sea level, curve 1 (fig. 9(b)). The disadvantages are the increasing rise time from sea level to 35,000 feet and the need for altitude sensing and computing equipment. A faster rise time may be achieved at 35,000 feet if a more oscillatory system can be tolerated at sea level.

SUMMARY OF RESULTS

An analog representation of a turbine-propeller engine and control system was formulated from sea-level static experimental transient data. A satisfactory correlation was obtained between analog solutions and the experimental transient data. The analog representation was used to compute system response at altitude from which the following conclusions may be drawn:

1. The actual engine-control system with an underdamped turbine-speed response at sea level and fixed control constants resulted in twice the initial turbine-speed overshoot at 35,000 feet as at sea-level and the time for turbine speed to settle out at its final value increased from approximately 12 seconds at sea level to about 65 seconds at 35,000 feet.

2. Variation of control constants to maintain sea-level turbine-speed response at all altitudes resulted in the initial blade-angle overshoot increasing from 140 percent of final blade-angle change at sea level to 650 percent at 35,000 feet.

3. Variation of control constants to maintain system loop gain and ratio of engine time constant to control time constant at sea-level

values resulted in similar initial turbine-speed and blade-angle overshoots at all altitudes, but an increase in the time required for turbine speed to first reach its final value from 1 second at sea level to 3 seconds at 35,000 feet. However, if a more oscillatory system may be tolerated at 35,000 feet, this method may be modified to provide a faster rise time at 35,000 feet.

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APPENDIX - SYMBOLS

A	amplitude ratio, $ KG(i\omega) $
$[KG(i\omega)]_c$	control transfer function
$[KG(i\omega)]_e$	engine transfer function
$[KG(i\omega)]_r$	speed-measuring-instrument transfer function
$[KG(i\omega)]_\beta$	propeller-pitch-change-mechanism transfer function
$G(i\omega)$	function of $i\omega$ representing time dependent part of transfer function
K	constant or frequency invariant portion of transfer function
K_e	engine gain, rpm/deg β
K_i	control integral constant, $\frac{\text{deg } \beta/\text{sec}}{\text{rpm}}$
K_p	control proportional constant, deg β /rpm
K_r	speed-measuring-instrument gain, rpm/rpm
K_β	propeller-pitch-change-mechanism gain, deg β /deg β
N_e	actual turbine speed, rpm
N_m	measured turbine speed, rpm
N_s	turbine-speed setting, rpm
Q	load torque referred to turbine, ft-lb
W_f	fuel flow, lb/hr
i	imaginary number, $i^2 = -1$
β	propeller-blade angle, deg
β_a	propeller beta arm, deg

θ	temperature correction factor, $\frac{\text{ambient static temperature}}{\text{NACA standard sea-level temperature}}$
δ	pressure correction factor, $\frac{\text{ambient static pressure}}{\text{NACA standard sea-level pressure}}$
Φ	phase angle, $\tan^{-1} \frac{\text{imaginary part of } KG(i\omega)}{\text{real part of } KG(i\omega)}$
τ_c	control time constant, sec
τ_e	engine time constant, sec
τ_r	speed-measuring time constant, sec
τ_β	propeller-pitch-change-mechanism time constant, sec
ω	frequency, radians/sec

Subscripts:

corr altitude corrected value

REFERENCES

1. Davis, Frank W.: Problems of Gas-Turbine-Propeller Combinations. Aero. Eng. Rev., vol. 7, no. 4, April 1948, pp. 30-36.
2. Taylor, Burt L., III, and Oppenheimer, Frank L.: Investigation of Frequency-Response Characteristics of Engine Speed for a Typical Turbine-Propeller Engine. NACA TN 2184, 1950.
3. Brown, Gordon S., and Campbell, Donald P.: Principles of Servomechanisms. John Wiley & Sons, Inc., 1948.
4. LaVerne, Melvin E., and Boksenbom, Aaron S.: Frequency Response of Linear Systems from Transient Data. NACA Rep. 977, 1950. (Formerly NACA TN 1935.)
5. Otto, Edward W., and Taylor, Burt L., III: Dynamics of a Turbojet Engine Considered as a Quasi-Static System. NACA TN 2091, 1950.

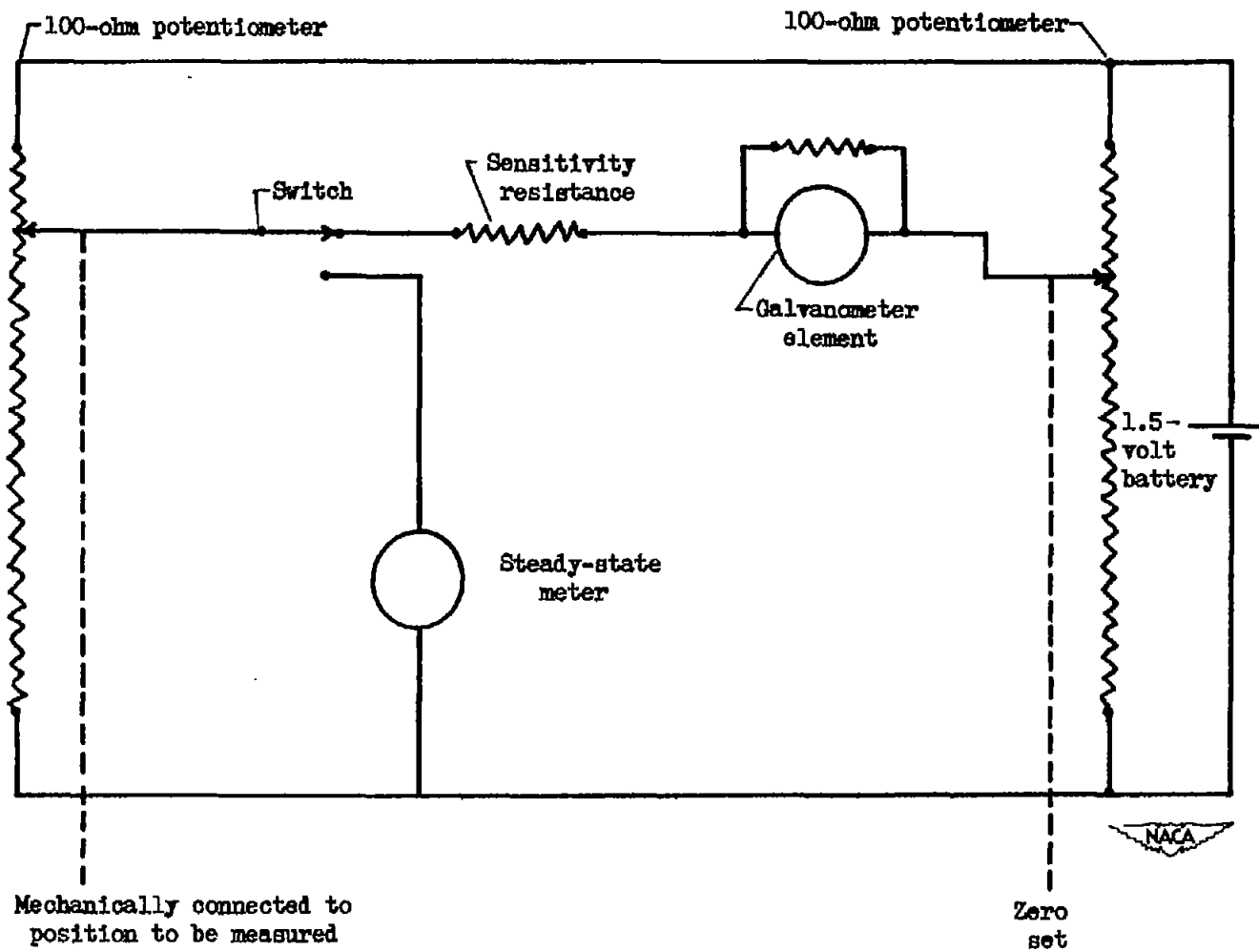


Figure 1. - Schematic diagram of typical steady-state and transient position measuring circuit.

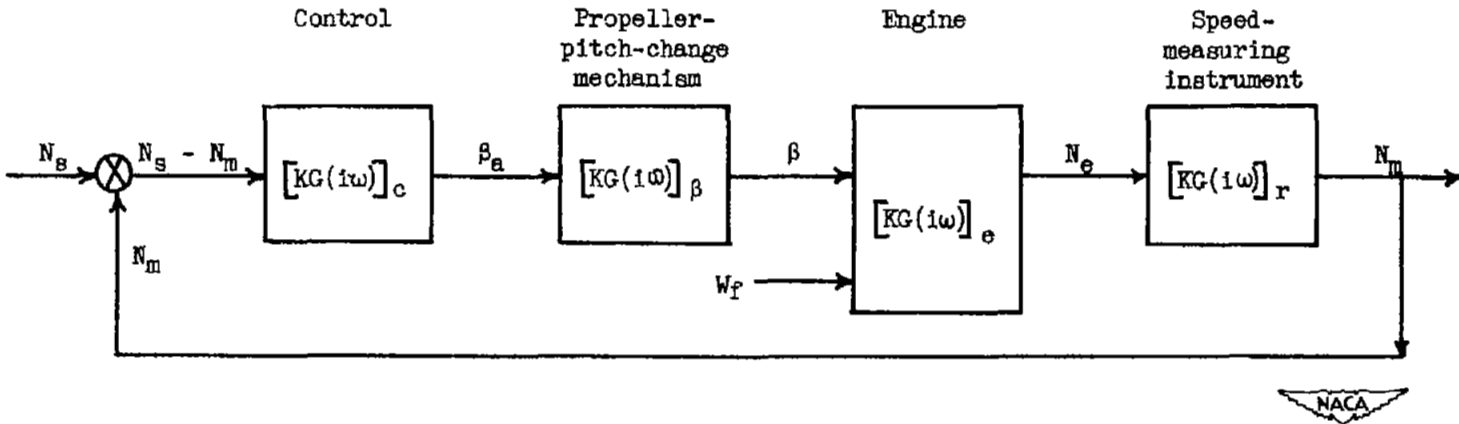


Figure 2. - Block diagram of turbine-speed - blade-angle control on turbine-propeller engine for analysis and analog studies.

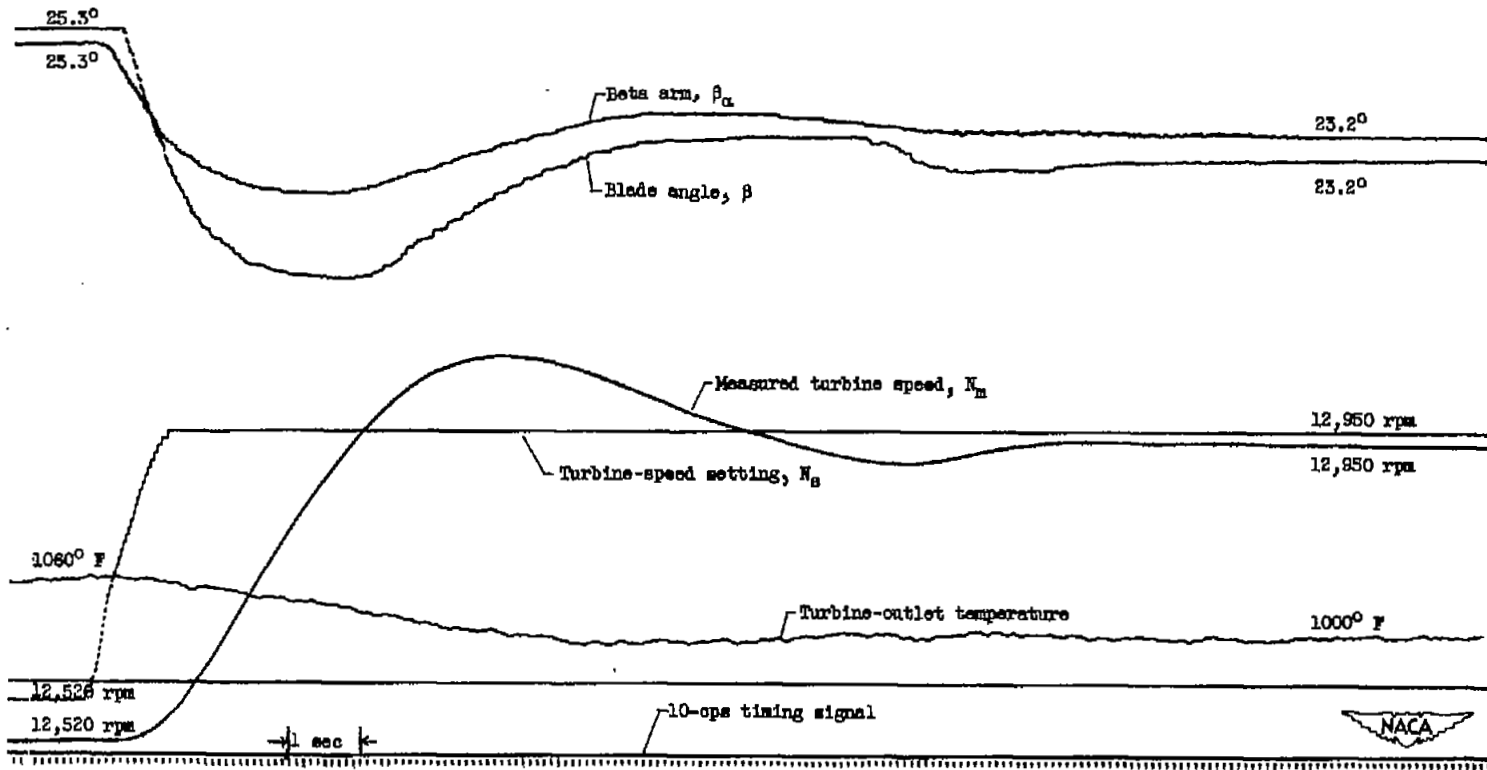
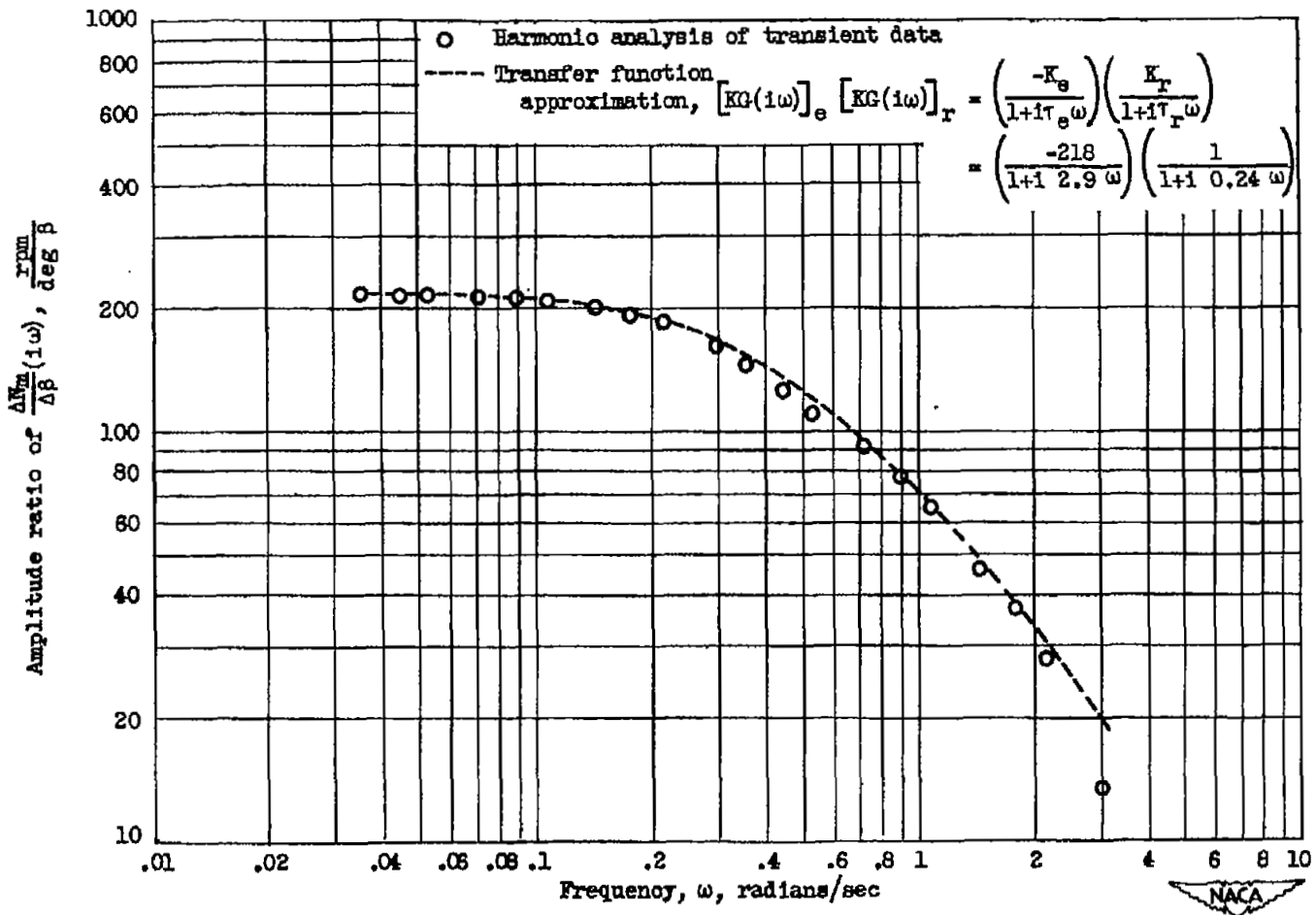
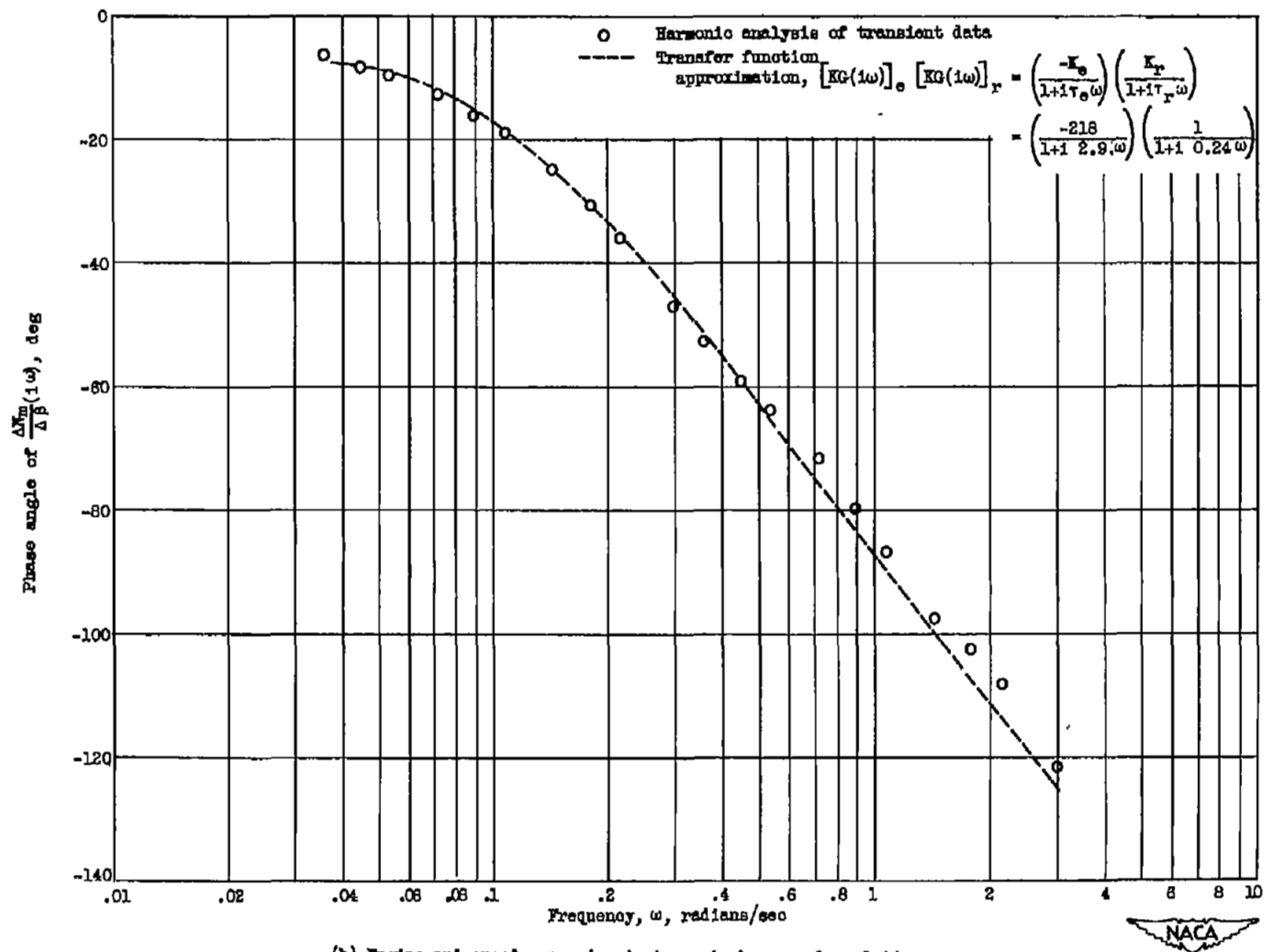


Figure 5. - Typical transient recording showing system responses to ramp-type disturbance in speed setting with constant fuel flow for turbine-propeller engines and turbine-speed - blade-angle control system.



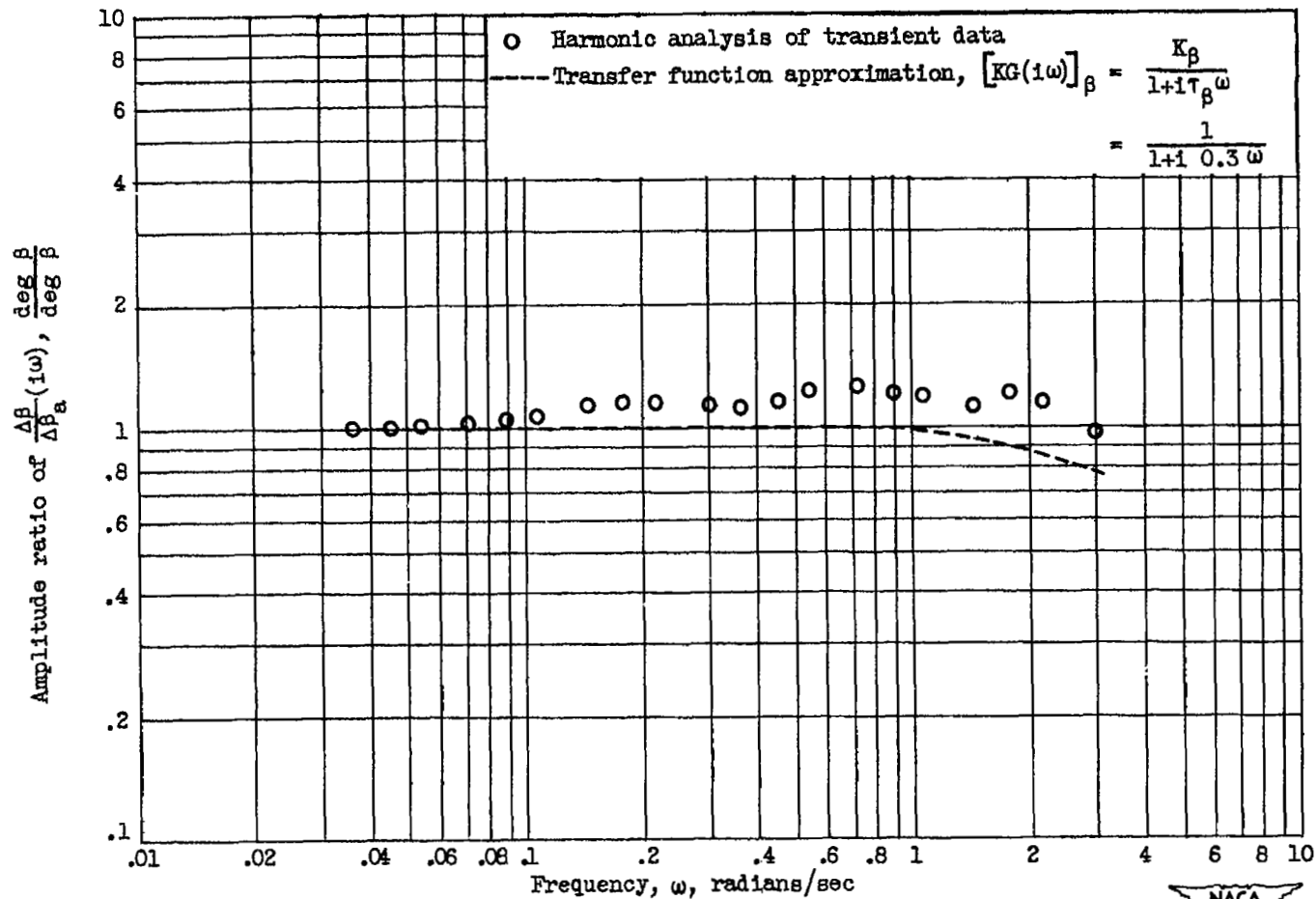
(a) Engine and speed-measuring instrument amplitude ratio relation.

Figure 4. - Frequency characteristic of system components as determined from harmonic analysis of experimental transient response to ramp-type disturbances in speed setting with constant fuel flow and as approximated by transfer functions for turbine-propeller engine and turbine-speed - blade-angle control system.



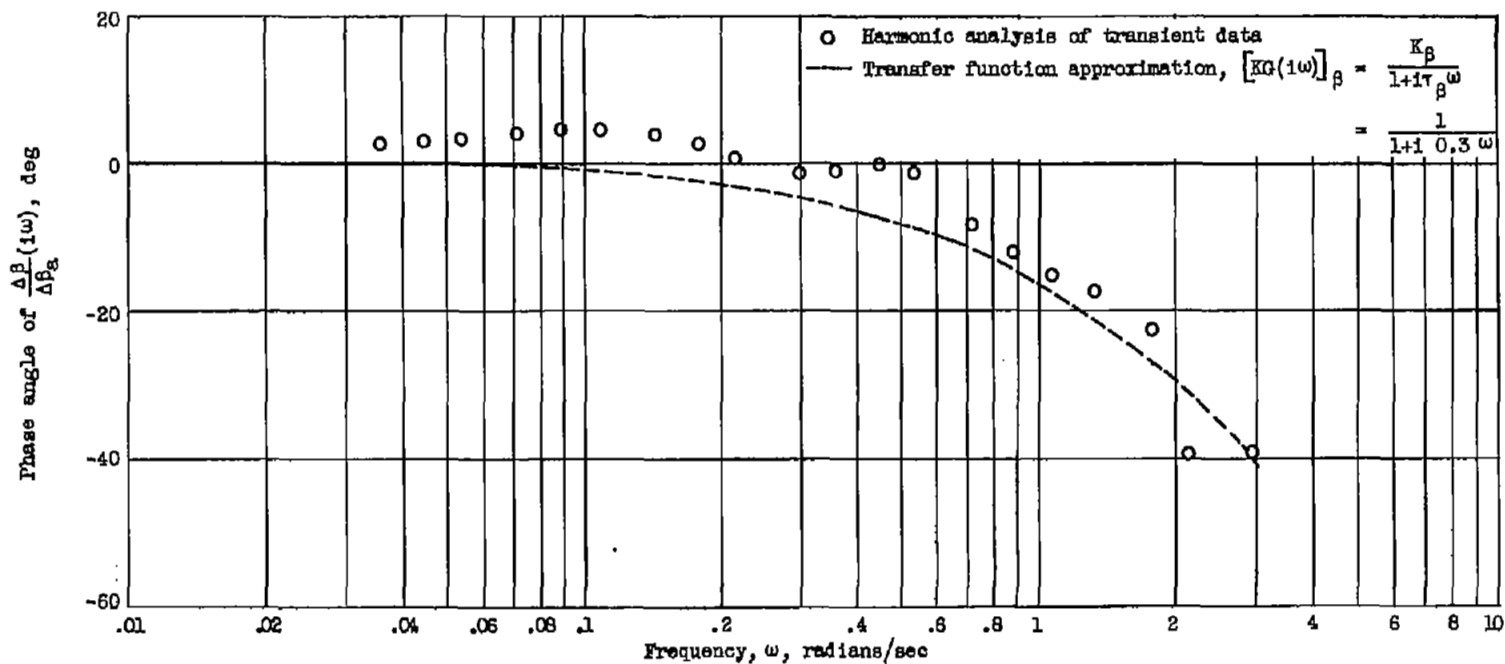
(b) Engine and speed-measuring instrument phase angle relation.

Figure 4. - Continued. Frequency characteristic of system components as determined from harmonic analysis of experimental transient response to ramp-type disturbances in speed setting with constant fuel flow and as approximated by transfer functions for turbine-propeller engine and turbine-speed - blade-angle control system.



(c) Propeller-pitch-change mechanism amplitude ratio relation.

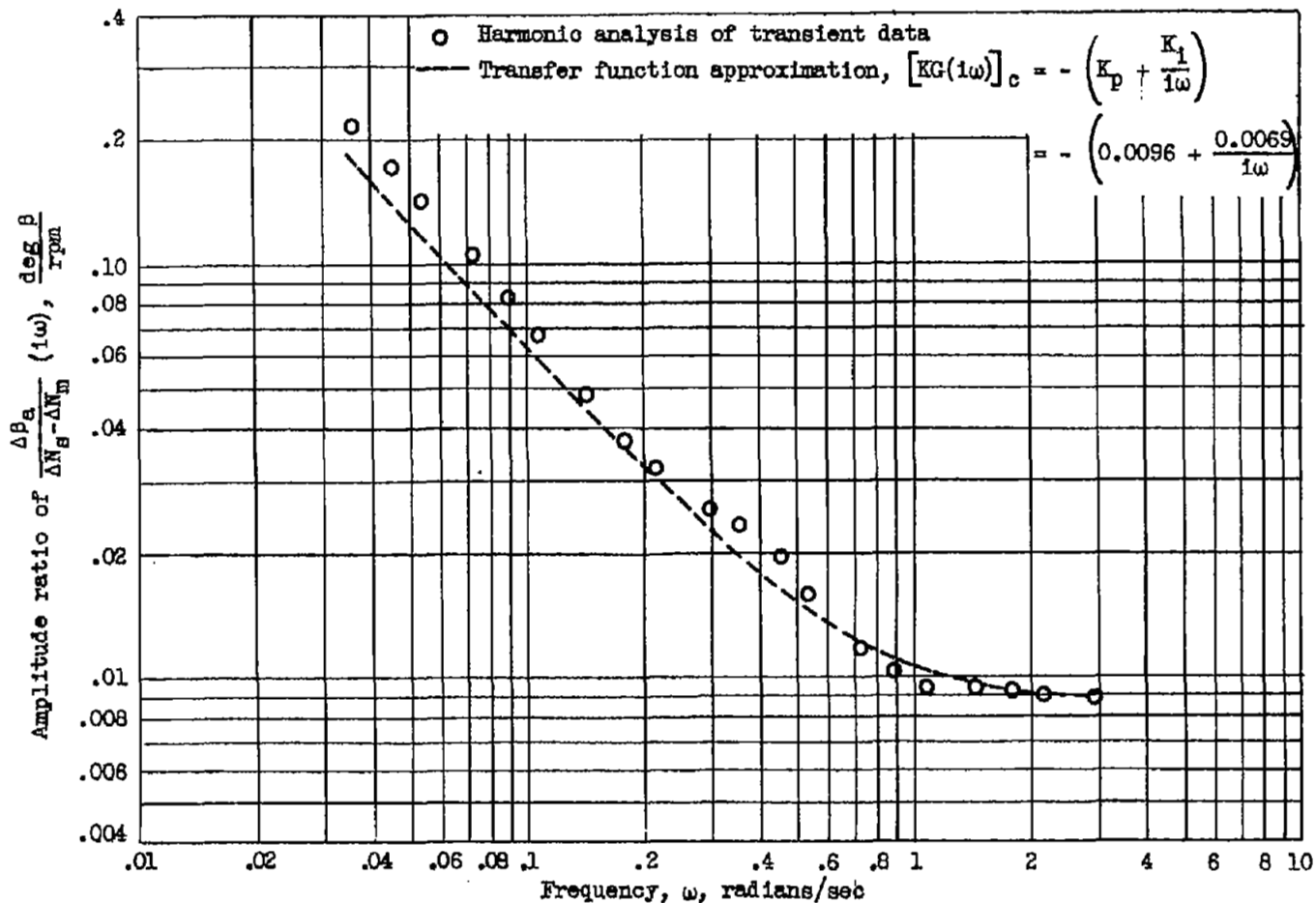
Figure 4. - Continued. Frequency characteristic of system components as determined from harmonic analysis of experimental transient response to ramp-type disturbances in speed setting with constant fuel flow and as approximated by transfer functions for turbine-propeller engine and turbine-speed - blade-angle control system.



(d) Propeller-pitch-change mechanism phase angle relation.



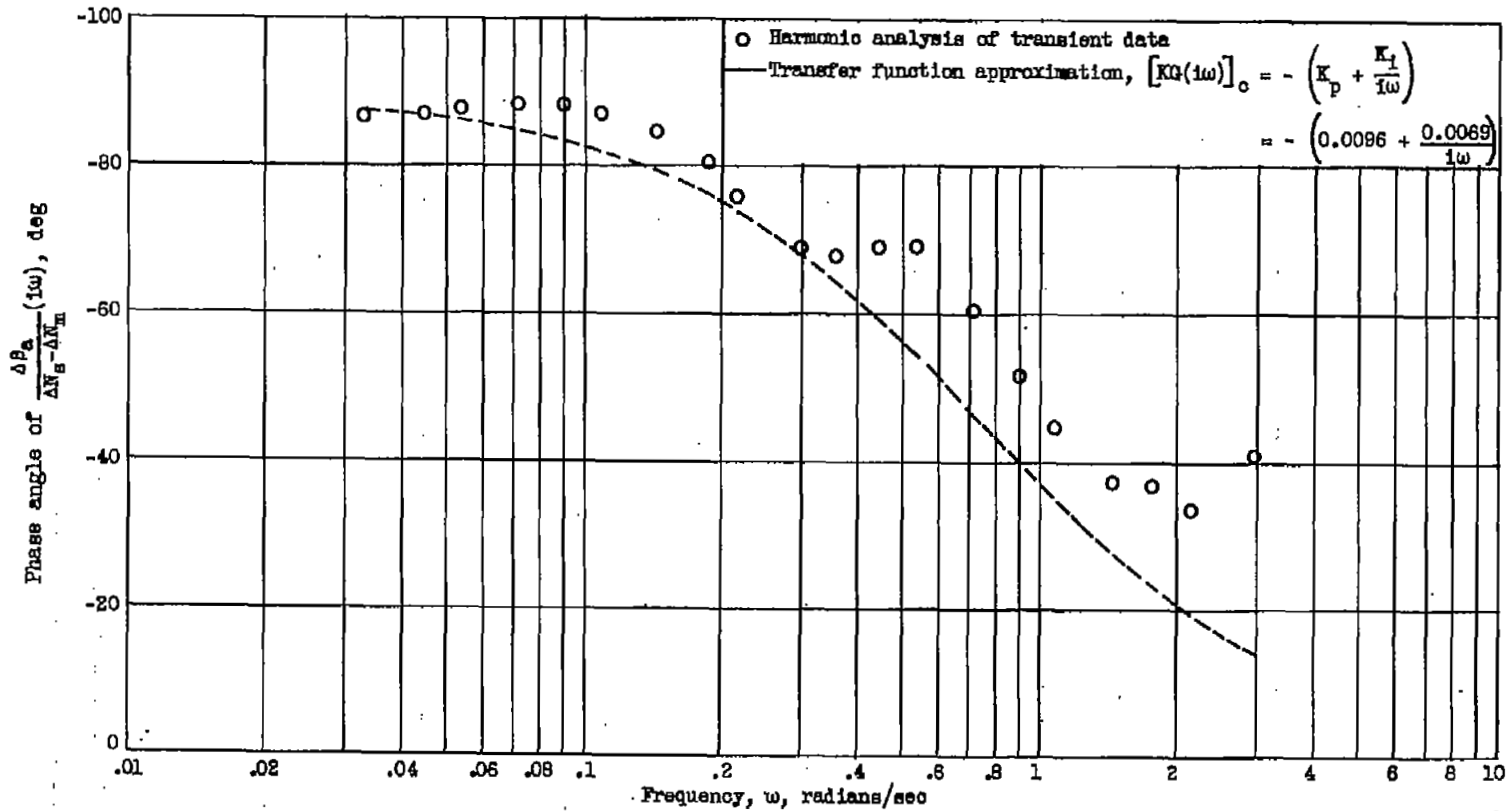
Figure 4. - Continued. Frequency characteristic of system components as determined from harmonic analysis of experimental transient response to ramp-type disturbances in speed setting with constant fuel flow and as approximated by transfer functions for turbine-propeller engine and turbine-speed - blade-angle control system.



(e) Control amplitude ratio relation.



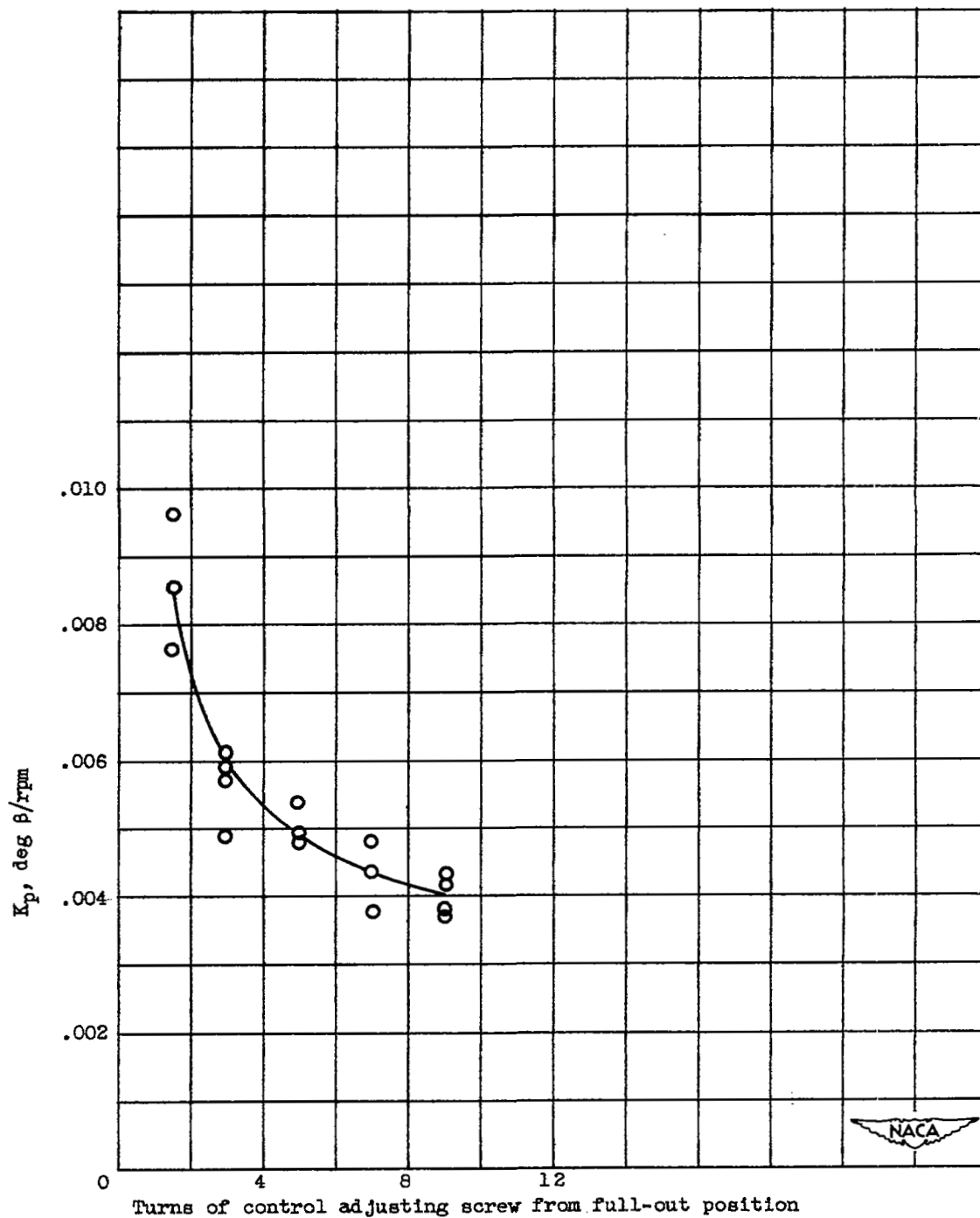
Figure 4. - Continued. Frequency characteristic of system components as determined from harmonic analysis of experimental transient response to ramp-type disturbances in speed setting with constant fuel flow and as approximated by transfer functions for turbine-propeller engine and turbine-speed - blade-angle control system.



(f) Control phase angle relation.



Figure 4. - Concluded. Frequency characteristic of system components as determined from harmonic analysis of experimental transient response to ramp-type disturbances in speed setting with constant fuel flow and as approximated by transfer functions for turbine-propeller engine and turbine-speed - blade-angle control system.



(a) Proportional constant K_p .

Figure 5. - Calibration of turbine-speed - blade-angle control.

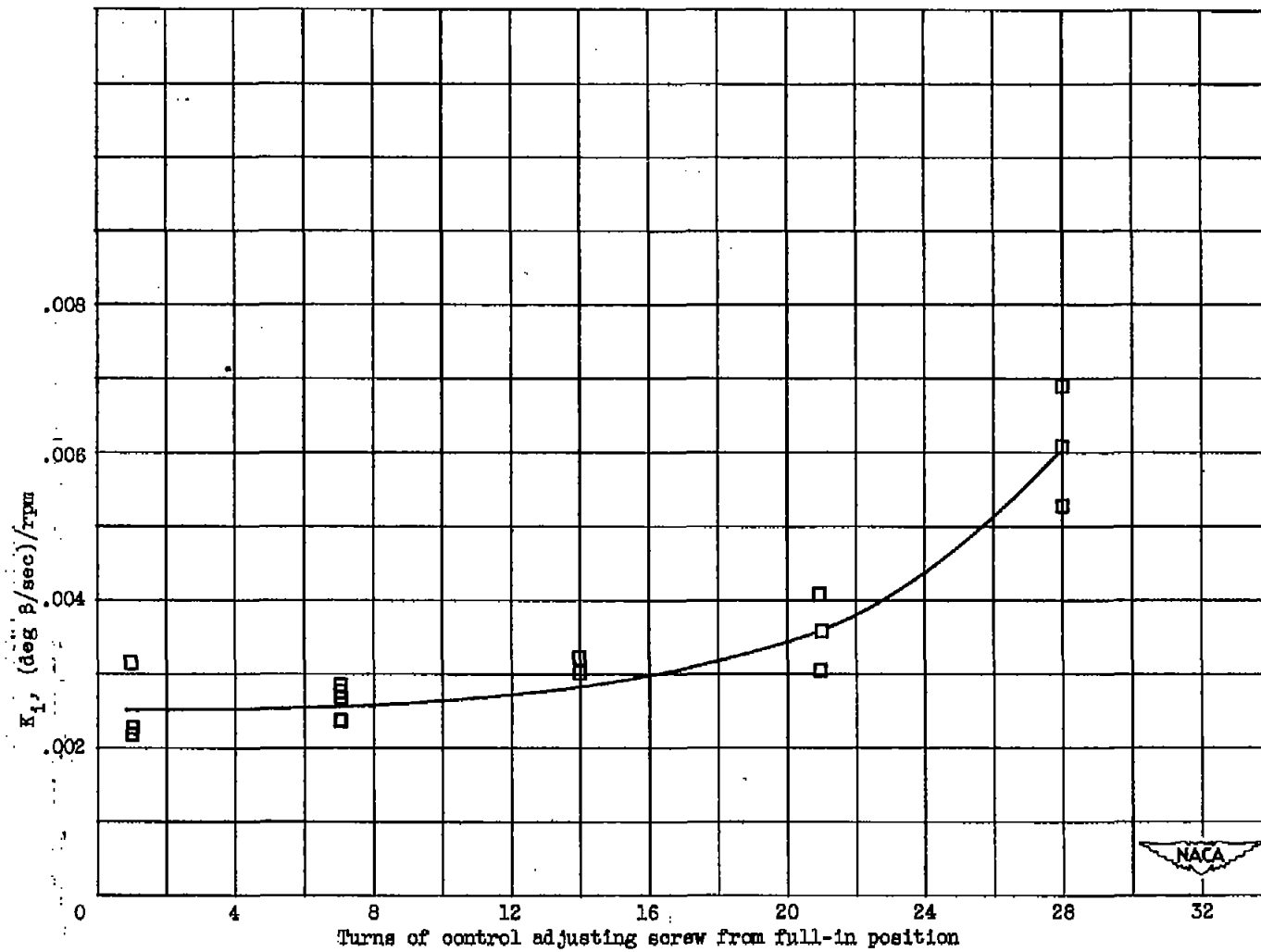
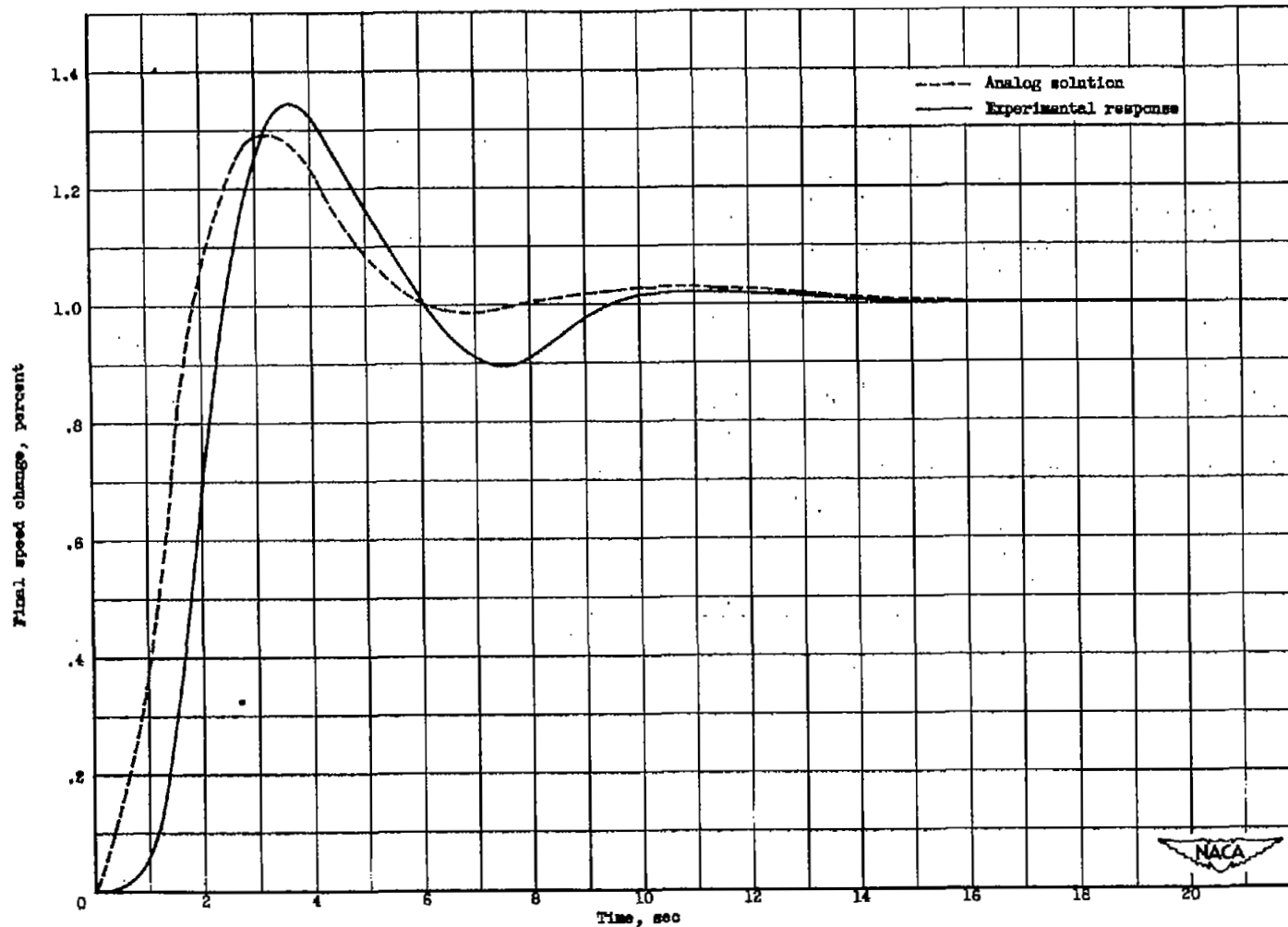
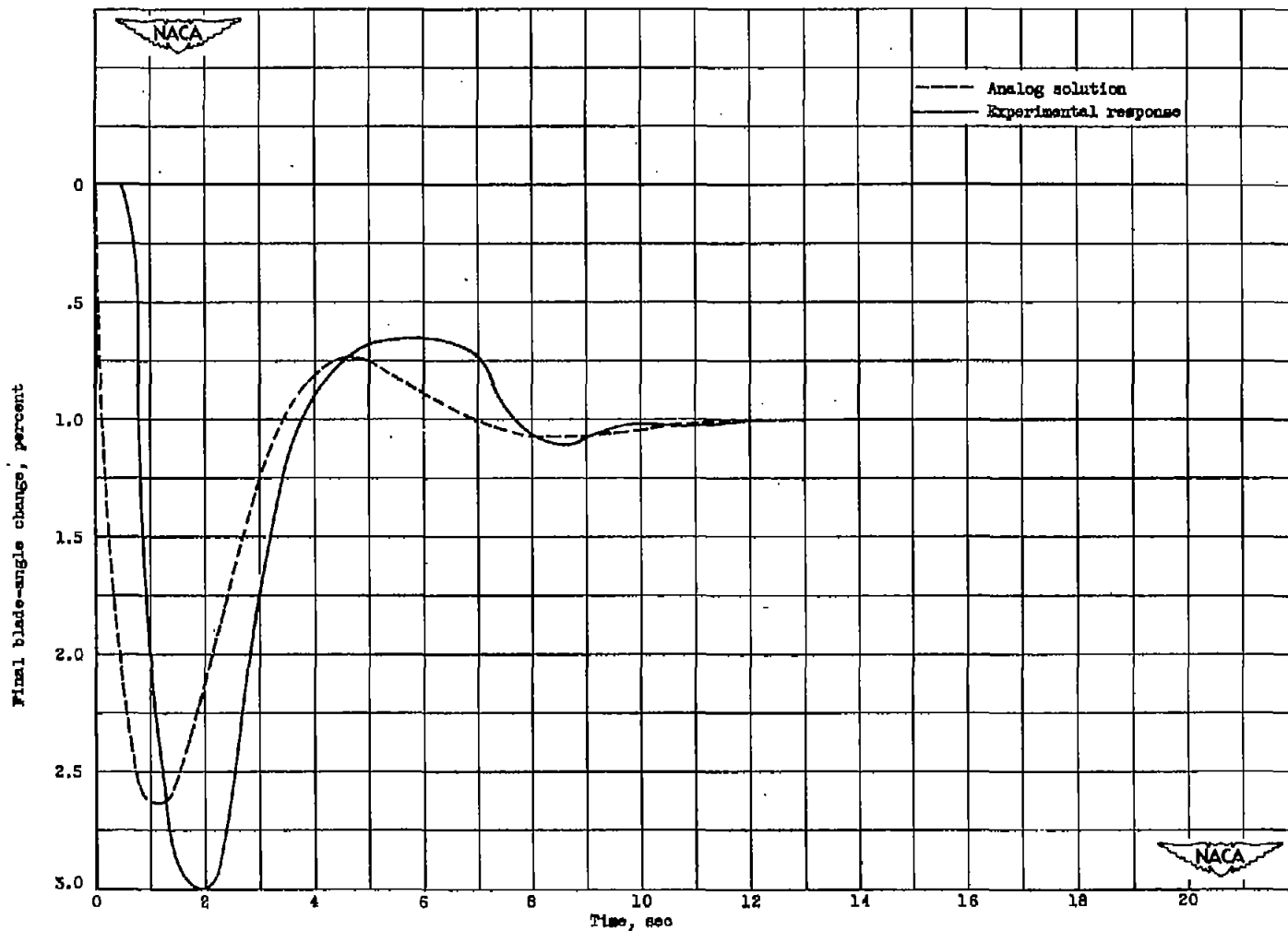
(b) Integral constant K_I .

Figure 5. - Concluded. Calibration of turbine-speed - blade-angle control.



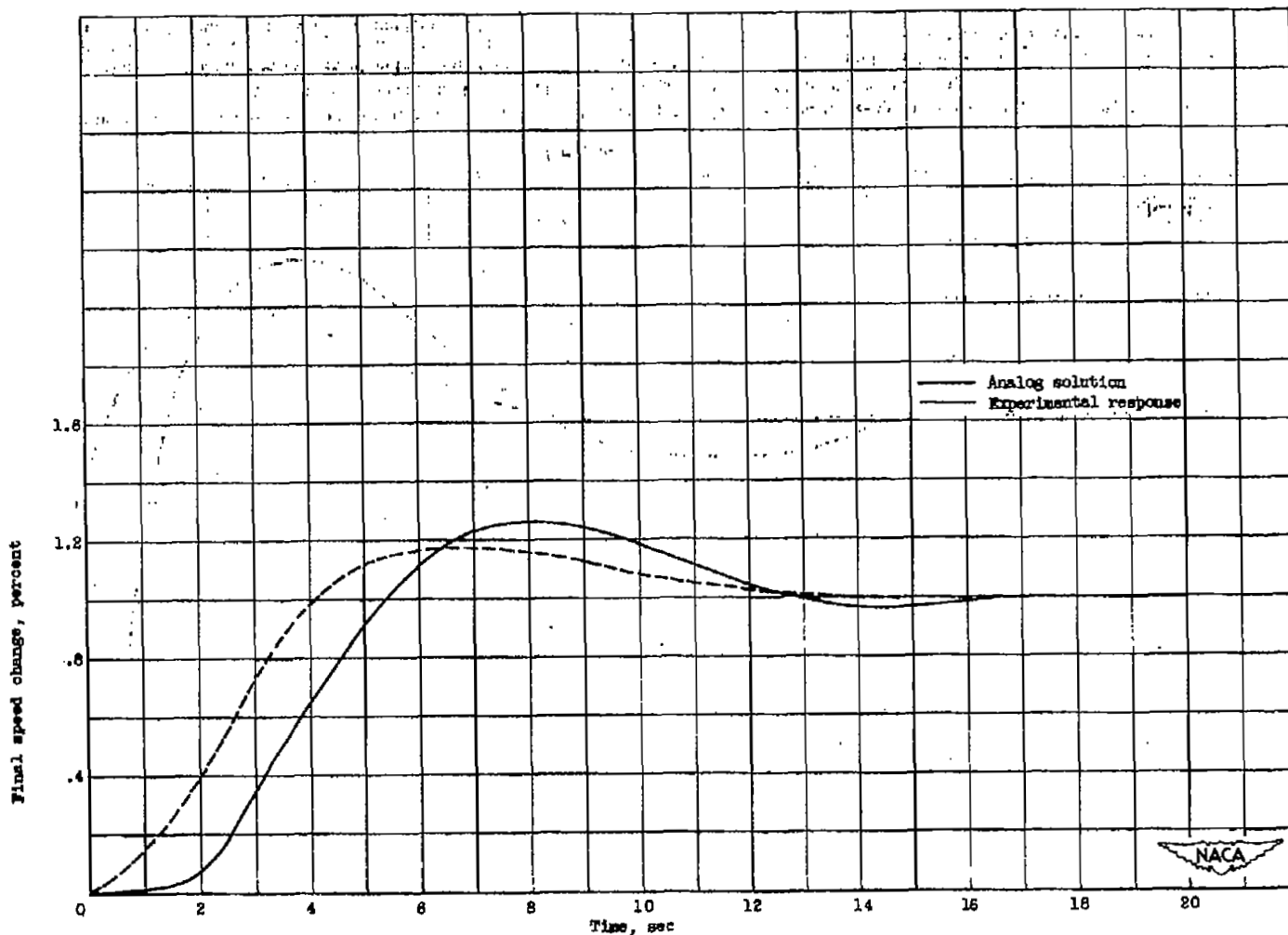
(a) Turbine speed. K_p , 0.0084 deg β /rpm; K_I , 0.0068 (deg β /sec)/rpm; τ_0 , 1.23 sec; turbine-speed change, 11,940 to 12,410 rpm; blade-angle change, 30.5° to 28.1°; load-torque change, 504 to 465 foot-pounds.

Figure 6. - Comparison of experimental transient response and analog solutions to ramp-type disturbances in speed setting with constant fuel flow for turbine-propeller engine and turbine-speed - blade-angle control system. (Analog solution determined from harmonic analysis and transfer function approximation.)



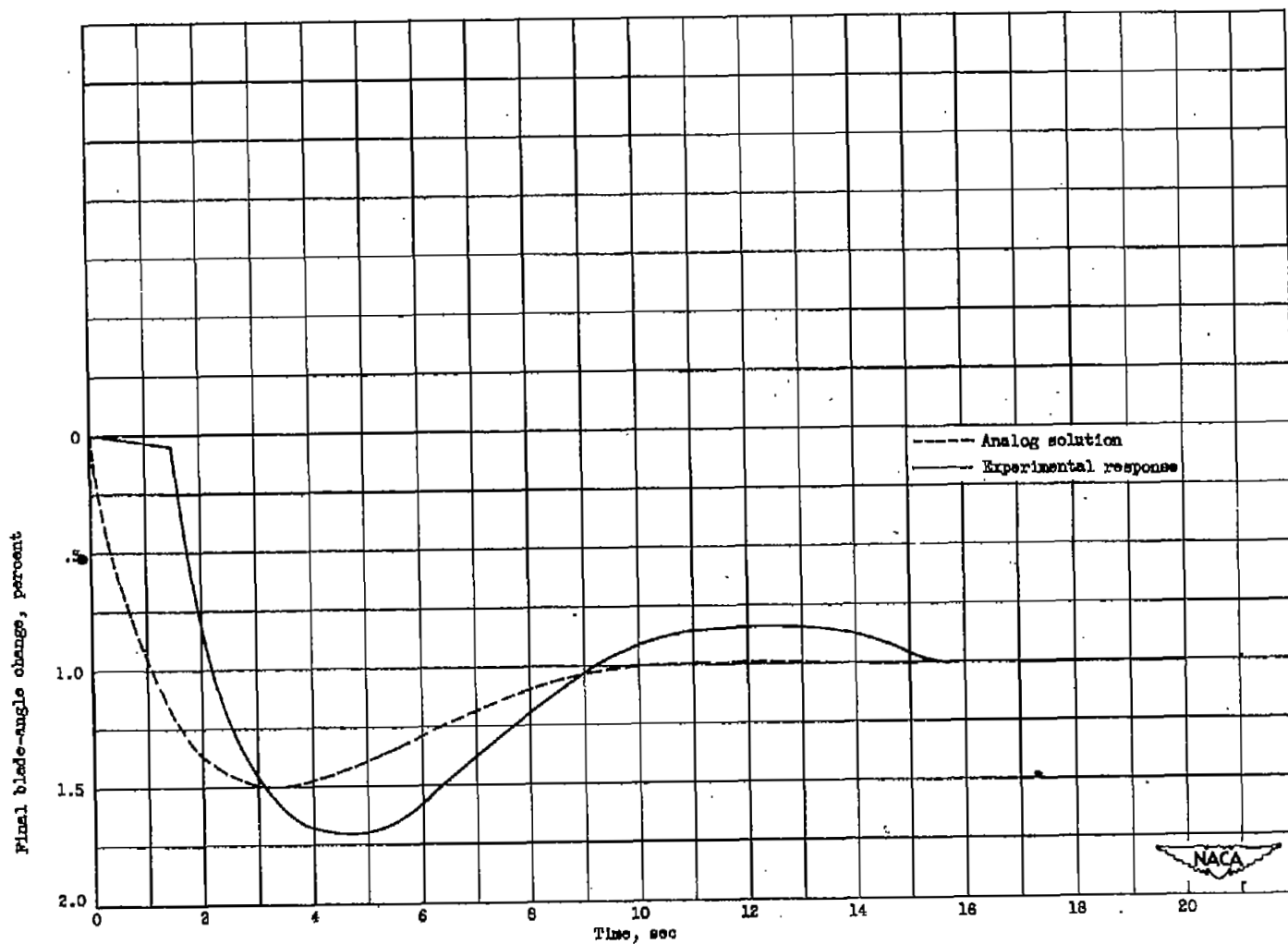
(b) Blade angle. K_p , 0.0084 deg β /rpm; K_f , 0.0068 (deg β /sec)/rpm; τ_o , 1.25 sec; turbine-speed change, 11,940 to 12,410 rpm; blade-angle change, 30.3° to 28.1° ; load-torque change, 504 to 485 foot-pounds.

Figure 6. - Continued. Comparison of experimental transient response and analog solutions to ramp-type disturbances in speed setting with constant fuel flow for turbine-propeller engine and turbine-speed - blade-angle control system. (Analog solution determined from harmonic analysis and transfer function approximation.)



(c) Turbine speed. K_p , 0.0040 deg β /rpm; K_1 , 0.0032 (deg β /sec)/rpm; τ_0 , 1.25 sec; turbine-speed change, 11,440 to 12,080 rpm; blade-angle change, 26.4° to 25.4°; load-torque change, 353 to 279 foot-pounds.

Figure 8. - Continued. Comparison of experimental transient response and analog solutions to ramp-type disturbances in speed setting with constant fuel flow for turbine-propeller engine and turbine-speed - blade-angle control system. (Analog solution determined from harmonic analysis and transfer function approximation.)



(d) Blade angle. K_p , 0.0040 deg β /rpm; K_I , 0.0032 (deg β /sec)/rpm; τ_0 , 1.25 sec; turbine-speed change, 11,440 to 12,080 rpm; blade-angle change, 28.4° to 23.4° ; load-torque change, 333 to 279 foot-pounds.

Figure 6. - Concluded. Comparison of experimental transient response and analog solutions to ramp-type disturbances in speed setting with constant fuel flow for turbine-propeller engine and turbine-speed - blade-angle control system. (Analog solution determined from harmonic analysis and transfer function approximation.)

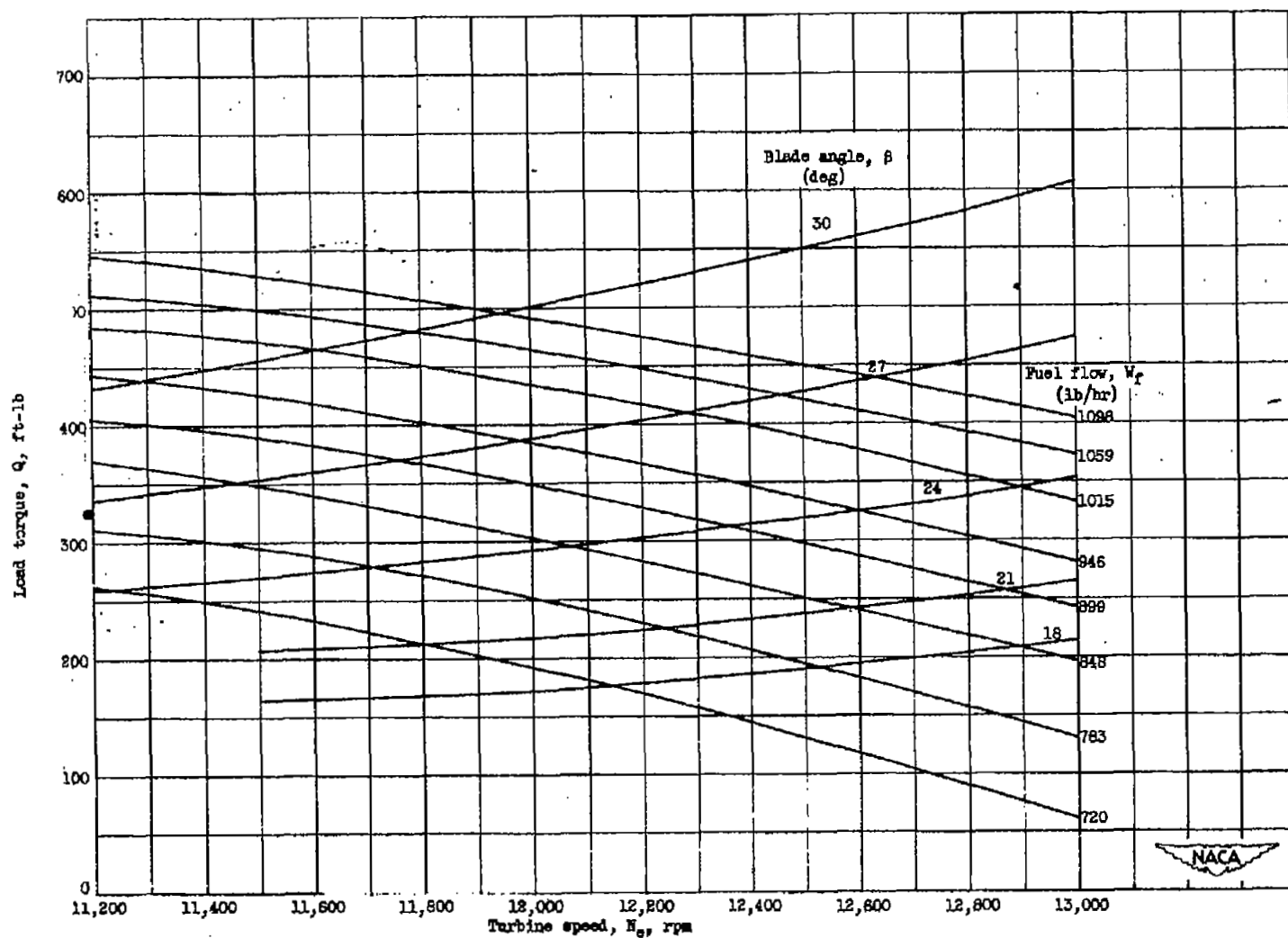
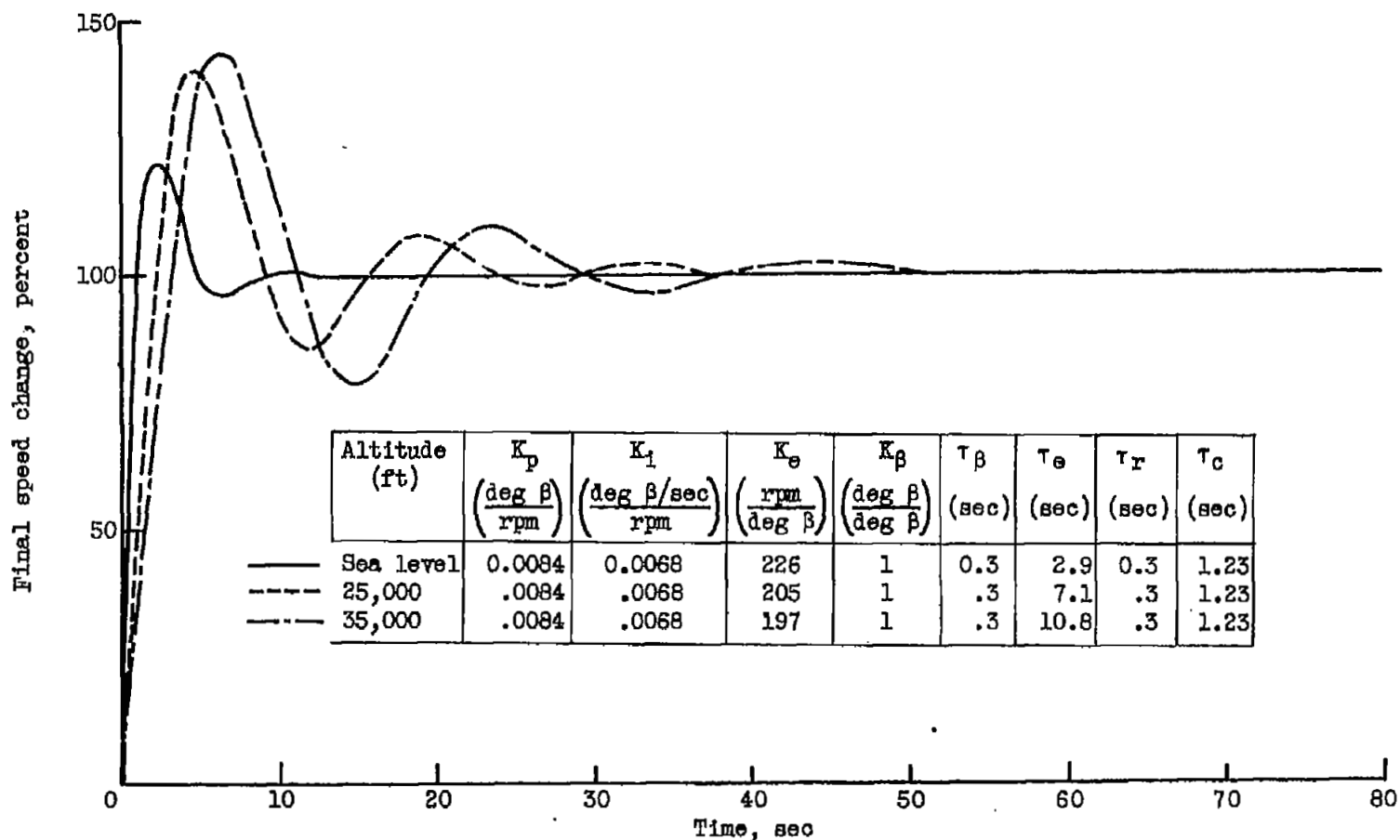


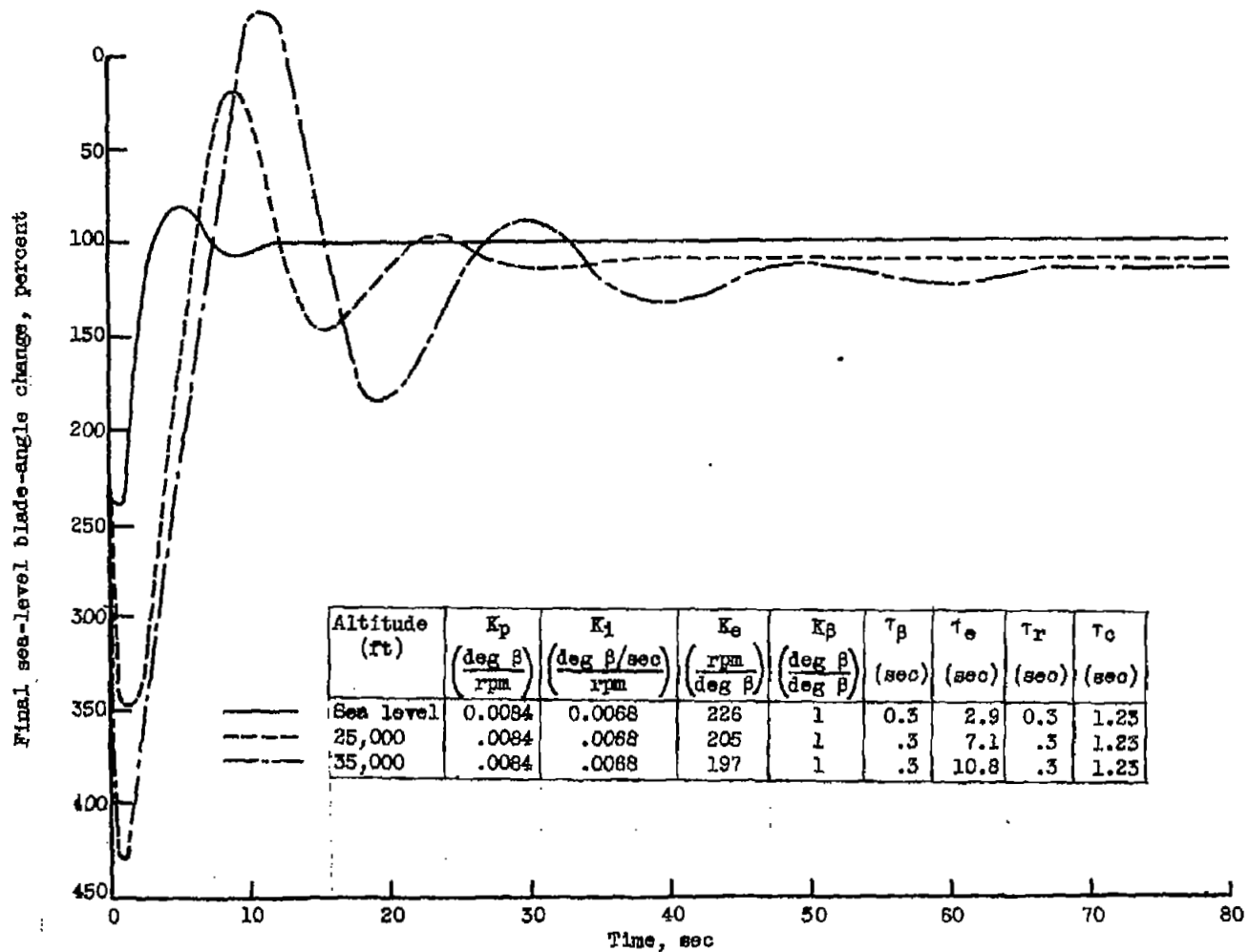
Figure 7. - Relation between engine load torque and turbine speed for constant blade angle and fuel flow as obtained from sea-level zero-rpm experimental data for turbine-propeller engine with AeroProducts AS4ZF-17 propeller.



(a) Turbine speed.



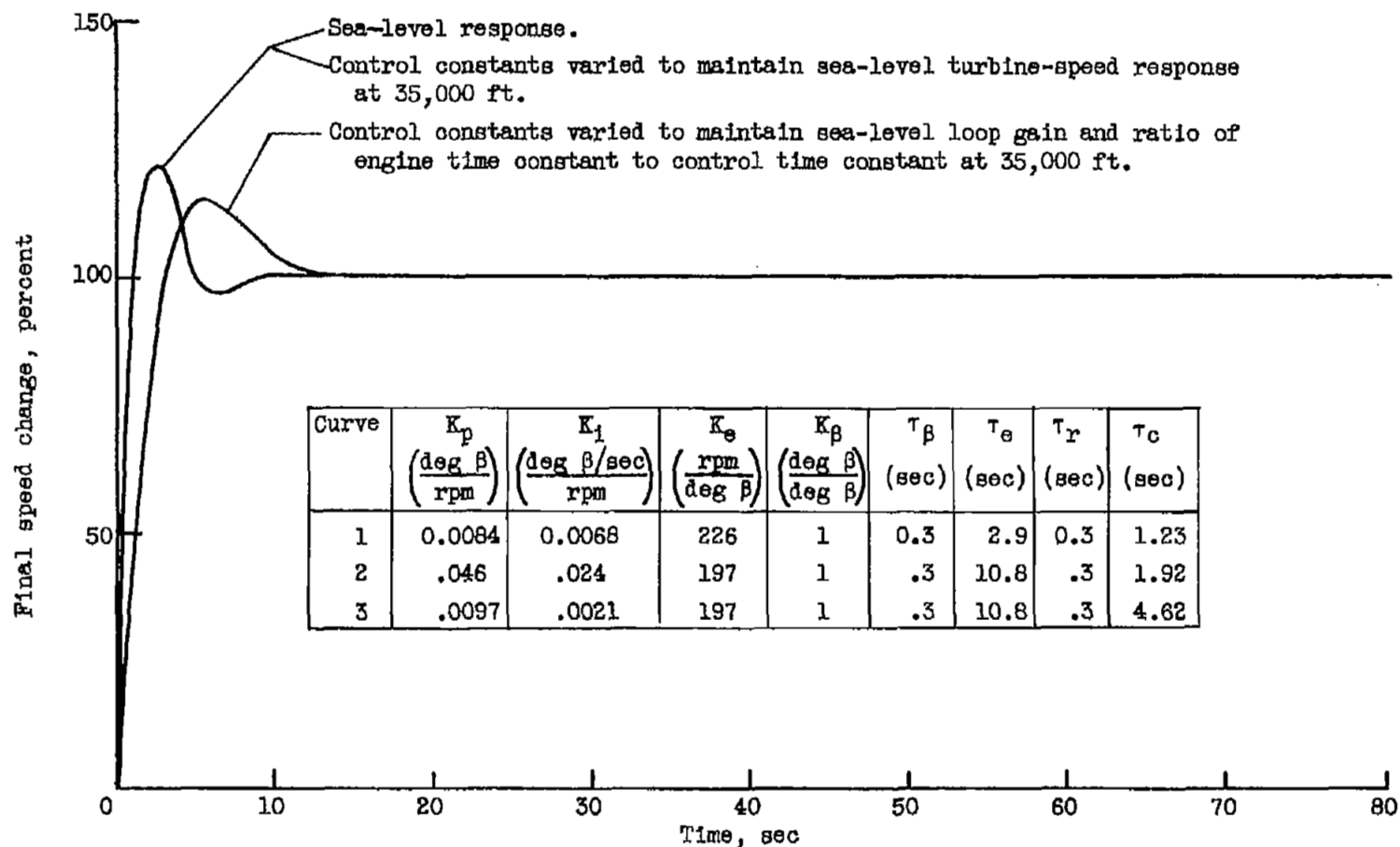
Figure 8. - Computed altitude transient response of turbine speed and blade angle for turbine-propeller engine and turbine-speed - blade-angle control system with fixed-control constants.



(b) Blade angle.



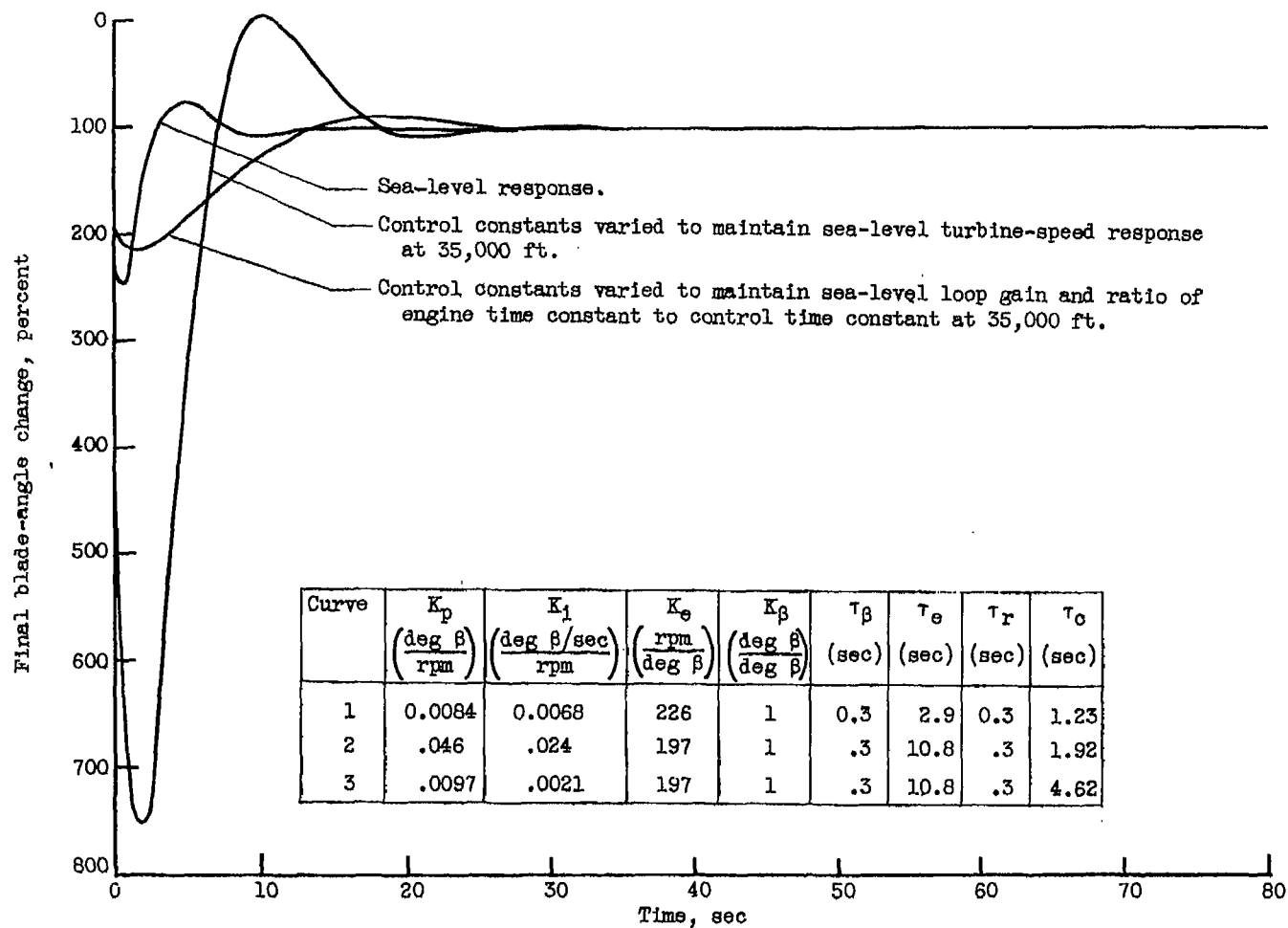
Figure 8. - Concluded. Computed altitude transient response of turbine speed and blade angle for turbine-propeller engine and turbine-speed - blade-angle control system with fixed-control constants.



(a) Turbine speed.



Figure 9. - Computed turbine speed and blade angle transient response at sea level and 35,000 feet of turbine-propeller engine with turbine-speed - blade-angle control system for various values of control constants.



(b) Blade angle.



Figure 9. - Concluded. Computed turbine speed and blade angle transient response at sea level and 35,000 feet of turbine-propeller engine with turbine-speed - blade-angle control system for various values of control constants.

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