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# RESEARCH MEMORANDUM

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FUSELAGE SIDE INLETS - A STUDY OF SOME FACTORS

AFFECTING THEIR PERFORMANCE AND A

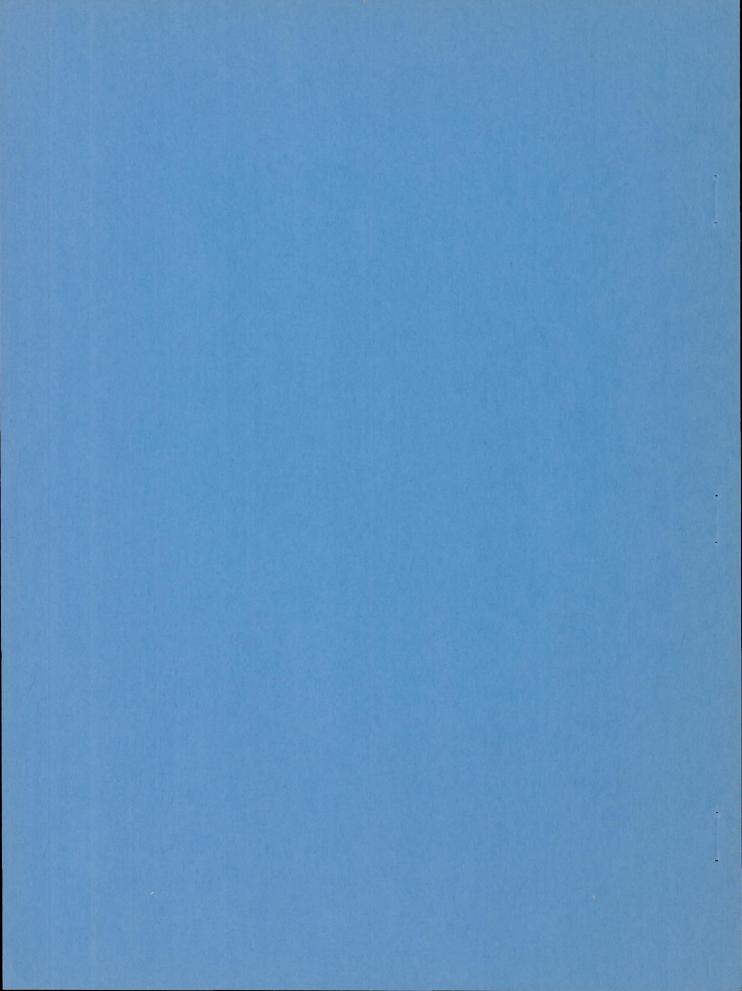
COMPARISON WITH NOSE INLETS

By Emmet A. Mossman, Frank A. Pfyl, and Frank A. Lazzeroni

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## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

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#### RESEARCH MEMORANDUM

#### FUSELAGE SIDE INLETS - A STUDY OF SOME FACTORS

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#### COMPARISON WITH NOSE INLETS1

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#### SUMMARY

This report first notes briefly certain basic principles affecting the performance of side-inlet air-induction systems. Following this discussion, the performance of several fuselage side inlets is examined, and comparison is made with nose inlets. Methods for improving the performance of both side inlets and nose inlets are reviewed, including boundary-layer control on the compression surfaces, revised geometry to provide a circular side inlet, and an internal-compression inlet having low external drag.

A procedure is outlined for analyzing inlet flow instability from a statistical point of view in which the flow is treated as a stationary random function of time. It is suggested that the root-mean-square amplitude of the pressure fluctuations be related to jet-engine performance and that the method can prove useful for correlating inlet instability obtained from wind-tunnel models with results from flight tests.

#### INTRODUCTION

In the design of an air-induction system to supply air efficiently to an engine placed in an airframe, consideration must be given to the somewhat diverse fields of aerodynamics and thermodynamics. Airplane range, and variously defined airplane efficiencies, can be shown to be functions of the lift-to-drag ratio and the propulsive efficiency. Generally speaking, the lift-to-drag ratio is considered to be in the province of the

<sup>1</sup>This report is substantially the same as a paper presented at an Institute of the Aeronautical Sciences Specialist Meeting, on March 21, 1955, in Los Angeles, California. aerodynamicist and the propulsive efficiency to be in the province of the thermodynamicist. The induction-system design involves both aerodynamics and thermodynamics; it can have a major influence on the drag of the airplane, and it affects the engine performance through deceleration of the induction air. It is the combination of these factors that makes induction-system design so vital to airplane performance.

As the aerodynamicist well knows, there is a divergence of opinion as to where the engine should be placed in any given design. This is especially true with a multiengine interceptor or fighter aircraft. It is beyond the scope of this paper to discuss relative merits of nacelles or pod installations as opposed to engine-fuselage arrangements. The aerodynamic and thermodynamic factors which should influence the design of an air-induction system are in the main known, but the information regarding them is diffused in the mass of literature dealing with subjects other than air-induction systems. In some cases the necessary research has not as yet been performed. It is the purpose of the present paper to discuss some of the aerodynamic factors which influence the performance of fuselage side inlets in the supersonic speed range up to a Mach number of about 2.0.

#### NOTATION

a	maximum	total	amplitude	of	the	pressure	pulsation,	10/	sq	ft
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- $C_{\rm D}$  drag coefficient,  $\frac{\rm D}{\rm qS}$
- d diameter of body, ft
- D net drag (measured drag minus the internal drag), lb
- f frequency, cps
- Fn net thrust, 1b
- G(f) spectral density,  $\frac{(lb/ft^2)^2}{sec}$
- h height of boundary-layer removal duct, ft
- l length of body, ft
- m mass flow through inlet, slugs/sec
- $\frac{m_1}{m_{\infty}}$  ratio of the mass flow through the inlet to the mass flow at freestream conditions passing through an area equal to the inlet entrance area

M Mach number

р	static pressure, lb/sq ft					
p	root-mean-square static pressure, lb/sq f					
Pt	total pressure, lb/sq ft					
q	dynamic pressure, lb/sq ft					
S	reference area, sq ft					
x	longitudinal distance, ft					
α	angle of attack, deg					
δ	boundary-layer thickness, ft					
θ	cone or wedge angle, deg					
λ	cowl lip angle, deg					

Subscripts

- ∞ free-stream condition
- 1 inlet station
- BL boundary-layer duct
- c compressor station
- isen isentropic
- s surface
- t total

#### DISCUSSION

#### Primary Principles

Performance improvements of air-induction systems can be expected to come from the application of certain fundamental aerodynamic principles related to the potential and viscous flow field of the body into which the inlet is located, supersonic wave drag concepts, and boundary-layer shockwave interaction effects. Before discussing the detailed results of recent research studies on side inlets, it would be well to review briefly these primary principles.

For nose inlets, the .ir flow up to the entrance is uniform. However, with side inlets the potential flow field of the fuselage at the inlet is nonuniform, there being both longitudinal and radial velocity gradients. The potential flow field of the fuselage, therefore, should influence to a great extent the choice of the inlet location. Figure 1, obtained from reference 1, shows a typical Mach number distribution along a fuselage nose. In the selection of a fuselage nose shape, the location of the inlet as well as the drag of the nose should be considered. If possible, advantage should be taken of the compression afforded by the nose. The inlet location should be selected so that the local Mach number is either below or near the free-stream value. For symmetrical fuselages, the known theoretical methods of computing the Mach number or pressure distribution give very good results; the first-order linearized theory (refs. 2 and 3) and the second-order theory (ref. 4) are adequate in this respect. For asymmetrical bodies a few cases have been treated in the literature (ref. 5).

Thus far only the potential flow field of the body at  $0^{\circ}$  angle of attack has been considered. Viscous crossflow effects become important as the angle of attack of the fuselage is changed. These effects are well known and have been pointed out in references 6 and 7. A sketch representing the physical process of viscous crossflow is also shown in figure 1. Here it is seen that as the angle of attack is increased, differences in the pressure field around the circumference of the body cause the boundary layer to flow into the top region, forming two lobes of low-energy air. As the angle of attack is increased further, these lobes form vortices. Extensive investigations of inlets at various circumferential locations on bodies of revolution have been made at both the Lewis and Langley laboratories (refs. 8 and 9). These tests show that inlets on the bottom and sides of the fuselage can have satisfactory characteristics; but difficulties have been experienced with the upper locations, especially with regard to the pressure recovery. However, some recent research has shown that with the inlet on the top, the effect of the vortices can be minimized by means of splitter plates and, consequently, the angle-of-attack effects need not be as adverse as those measured originally (ref. 10). When inlets are located on the sides of the fuselage, the local stream angle is greater than the angle of attack of the body. This effect decreases rapidly as the inlets are moved away from the fuselage.

In an examination of the basic concepts related to side inlets, mention should be made of applications of the "area" rule; that is, the estimation of wave drag from the longitudinal area distribution of a body (ref. 11). The literature indicates that, at the present time, it is not known how to apply the area rule to side-inlet air-induction systems. Tests on nose inlets, however, have shown that the area rule can be used for these designs. The wave drag of nose inlets operating at maximum mass flow has been predicted by the use of equivalent closed-body concepts (ref. 12). These nose inlet studies made at the Langley laboratory have indicated that the accuracy of the area-rule applications to nose inlets on slender bodies depends upon the ratio of the diameter of the inlet to the maximum diameter of the body. The accuracy appears to be good for ratios less than 0.3 to 0.4.

In a review of the factors which influence the performance of side inlets emphasis should be placed on shock-wave boundary-layer interaction. With side inlets the streamtube of induction air is contiguous to the fuselage surface, and the deceleration and compression of this air is accomplished by a shock-wave system which may impinge on the fuselage boundary layer. If the inlet is placed away from the fuselage, boundary-layer shock-wave interaction still occurs on the compression surfaces and may affect adversely the pressure recovery, air-flow stability, and drag of the inlet system. Schlieren studies of shock-wave boundary-layer interaction on probes in front of a blunt body (see, e.g., ref. 13) have indicated that for a shock wave of a given strength, the upstream disturbance is much less if the wave impinges on a turbulent boundary layer than if it interacts with a laminar or transitional boundary layer. It is believed that the photographic sequence shown on figure 2 illustrates these same effects for the case of air flow on the ramp of an inlet. At the top of the figure is shown an inlet operating at its maximum mass flow with the normal shock inside the inlet. As the mass flow is reduced, the normal shock moves in front of the inlet and interacts with the ramp boundary layer. The boundary layer is believed to be turbulent and the extent of the pressure disturbance which is transmitted upstream through the boundary layer is small, as indicated by the small wedge of separated air. With further reduction in the mass-flow ratio, the normal shock wave moves farther forward and finally interacts with a laminar or transitional portion of the boundary layer on the ramp. The upstream influence of the pressure disturbances is much greater, as can be seen in the region of separation extending to the very tip of the ramp. Accordingly, in the design of air-induction systems, interaction of the shock waves with laminar boundary layers should be avoided.

The influence of shock-wave boundary-layer interaction on airinduction performance appears to have been recognized by early investigators in the field of air induction. However, the importance of defining a satisfactory criterion for predicting the occurrence of shock-induced separation appears to have been overlooked. At the present time, the physical measurement of this interaction in which we are most interested is the pressure rise necessary to separate a boundary layer. Lange, in reference 14, reviewed in 1953 the known published information on the subject of the pressure rise which was then considered to be necessary to separate boundary layers. These and additional data are reviewed in figure 3. It is important to note that many diverse methods were used to

obtain the data, and that different criteria were used to determine the existence of separation. In the cases summarized by Lange, the pressure ratio for separation is obtained from the first peak pressure in the region of the wedge or the step. Schlieren observations of the bifurcation of a normal shock wave on the cone compression surfaces of nose-inlet models have been used by Nussdorfer as an indication of separation (ref. 15). Seddon used the surface pressures in the dead-air region behind a normal shock wave. At Mach numbers up to about 1.4, the pressure gradient was produced by a normal shock and subsonic diffusion between the shock system and the entry (ref. 16). Fage and Sargent made tests in which a normal shock wave produced the gradient necessary to separate the boundary layer, the separation being indicated from schlieren observations and pressure measurements (see ref. 17). The agreement between these methods is poor. The results are contrary to those reported by Bogdonoff and Kepler (ref. 17), who indicate no change in the separation pressure rise with Mach number. In the studies of boundary-layer shock-wave interaction previously cited, the pressure required to produce separation is taken to be that measured at the point of separation; however, recent unpublished information indicates that the required pressure rise is somewhat greater. In many practical installations it is not possible to design the ramp so that the pressure rise for separation will not be exceeded. If the separated flow can be made to reattach in these cases by use of boundary-layer control and other devices, the air-flow stability and pressure recovery can be improved. There would seem to be a need for new concepts relating to air-inlet design which take into account the separation criteria. It is clear, however, that the limits of these separation criteria are not well defined and that more research is indicated. The advancement of the inlet field depends to a large extent upon the research that will be done on this particular phase.

#### Performance of Side Inlets

The preceding primary principles provide a basis for anticipating improvements in side-inlet performance. It is not possible, however, always to take full advantage of the aerodynamic gains afforded by these concepts. In many cases structural or weight considerations may preclude certain inlet locations. In addition, many of the fundamental principles are still somewhat rudimentary, as is the case of the application of the area rule to air-induction design. Keeping in mind these and similar limitations to the application of the primary principles, let us consider next the performance of some actual side-inlet installations. Where possible, comparisons are made with nose-inlet installations. Figure 4 shows the pressure recovery of normal-shock side inlets as a function of free-stream Mach number. The pressure recovery at 95 percent of the maximum mass-flow ratio has been selected arbitrarily for comparison of the various inlets. The solid line curves present data on designs for various airplanes or missiles which were tested in wind tunnels as a part of developmental research programs (refs. 18 to 21). The dashed curves give

results of laboratory experiments on more idealized experimental models and also on pitot nose-inlet installations (refs. 22 to 25). Normalshock pressure recovery is shown also on the figure. Except for one case, there is an increment of about 0.04 between the side-inlet and nose-inlet induction systems at the higher Mach numbers. The exception is a circular side inlet (ref. 21) which exhibits considerably higher pressure recovery than the conventional type, its value approximating that for the nose inlets. Additional data will be given on this inlet later in the paper. Generally, it is realized that normal-shock inlets inflict severe performance penalties if they are used at Mach numbers above about 1.4.

The known recent pressure-recovery data on oblique-shock scoop inlets as applied to practical airplane models is summarized in figure 5 (refs. 21 and 26 to 28). There are little data on comparable nose inlets with ramps or wedges. From a review of the literature, it becomes evident that there are more side-inlet designs with wedges than with cones. However, with nose inlets or nacelles, the research on cone compression surfaces predominates. The pressure recovery of these practical side inlets is dependent on the design Mach number. The rapid dropoff in pressure recovery occurs at Mach numbers above that for which the oblique shock falls inside the inlet. Very good pressure recovery has been obtained with some of the designs at Mach numbers less than about 1.5. At the higher Mach numbers, difficulties have been encountered in reaching the values of the pressure recoveries obtained with the best nose inlets with external compression surfaces. A two-angle ramp has obtained the highest pressure recovery  $(p_{t_{\alpha}}/p_{t_{\infty}} = 0.87 \text{ at } M_{\infty} = 2.0)$ , although it should be noted that the stable mass-flow-ratio range was not large for this particular inlet.

Very little data exist from which a direct assessment can be made of the penalty in pressure recovery resulting from the placement of obliqueshock inlets on the side of a fuselage. Two comparisons have been derived from various published reports: One for an inlet design having a wedgecompression surface; the other for inlets having cone-compression surfaces. Figure 6 compares the pressure recovery of a nose inlet with a 14° wedge with that of the same inlet placed on the fuselage (refs. 29 and 30). The decrease in pressure recovery due to placing the inlet on the fuselage is 0 to 6 percent, depending on the Mach number. Comparison of various conical nose inlets with a half-cone inlet mounted on a flat plate (ref. 31) and a half-cone inlet on several fuselages is shown in figure 7. Since a conical nose inlet having a shape similar to the half-cone inlets was not tested, a pressure-recovery range obtained from several recent conical nose-inlet studies has been included on the figure (refs. 32 to 36). The data presented in figure 7 show progressive decreases in pressure recovery from the conical nose inlet to the half-cone inlet on the flat plate to the half-cone inlet on the various fuselages.

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The differences in the pressure recovery of nose inlets and the side inlets are due to the distortion of the potential flow field in the region of the inlet, to dissimilarities in the internal ducting, and to the viscous boundary layer of the fuselage on which the inlets are placed. The data on the two figures previously mentioned (figs. 6 and 7) are for boundary-layer control systems which were considered well designed. The magnitude of the decrease in pressure recovery of a side inlet as compared to a nose inlet can be much larger, depending to a great extent on the boundary-layer control system that is used.

Four boundary-layer control systems for side inlets which have been investigated are shown in figure 8. The suction or scoop type shown at the top of the figure takes the fuselage boundary layer into the fuselage. The diverter utilizes a wedge underneath the inlet to deflect the fuselage boundary layer as it passes underneath the compression surface and along the body. When a portion of the fuselage boundary layer can be put to some useful purpose, combinations of the suction and diverter systems are employed. A lesser amount of research, some at the Ames laboratory and some by the Royal Aircraft Establishment in Great Britain, has been done on the fourth type which removes only the low-energy portion of the fuselage boundary layer through a porous surface or through slots.

Before examining the characteristics of these boundary-layer control systems for supersonic inlets, let us consider first how they affect the flow into the inlet. That the boundary-layer control system can have a large influence on the flow field in front of the inlet is illustrated in the schlieren photographs of figures 9 and 10. These figures illustrate the effect of the boundary-layer diverter. Figure 9(a) shows the severe disturbances propagated upstream of a normal-shock inlet by a blunt  $130^{\circ}$ wedge. When the wedge angle was reduced to  $65^{\circ}$  (fig. 9(b)) and an indentation in front of the inlet was removed, the magnitude of the disturbances was greatly reduced, but not completely eliminated. Figure 10 shows how the oblique-shock system in front of a ramp-type inlet is altered by changes to the diverter angle of a combination of a diverter and suction system. In figure 10(a) the diverter wedge angle is about 40°. Although the schlieren photographs are not too clear, close examination shows that reducing the wedge angle to approximately 20° (fig. 10(b)) in the front portion of the diverter eliminated the disturbances. Piercy and Johnson in references 31, 37, and 38 have shown that wedge-type diverters yield inlet total-pressure recoveries comparable to the suction type, provided that small wedge angles are used and that the apex of the diverter wedge is downstream of the apex of the compression surface in front of the inlet. The penalty in pressure recovery incurred by placing the inlet in the fuselage boundary layer is shown in figure 11. Pressure recovery of several inlets is plotted as a function of  $h/\delta$ , where h is the height of the boundary-layer control inlet above the fuselage and  $\delta$  is the boundarylayer thickness. For the suction-type inlets, the mass flow through the boundary-layer removal system is the maximum used in the tests. It can be seen that diverter systems are more sensitive to placement in the

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fuselage boundary layer than are suction systems. Although the inlet pressure recovery is increased as the inlet is moved out of the boundary layer of the fuselage, the drag of the airplane or missile is also increased.

The drag contributed by various boundary-layer control systems applied to airplane, missile, and research models is summarized in figure 12 (refs. 9 and 39). Basing the drag coefficients on the capture area of the boundary-layer control system, which has been done in this figure, should put the dissimilar configurations on a comparable basis, to firstorder accuracy. The drag of the diverter is defined as the drag of the inlet-fuselage combination with diverter, minus the drag of the inletfuselage combination without the diverter (i.e., with the inlet placed contiguous to the fuselage and the inlet area increased by an amount equal to the area of the diverter system). For a ratio of capture area to wing area typical of four recent interceptors, these drag coefficients for the diverter systems represent from 3 to 10 percent of the total drag of an interceptor airplane. It can be seen that these forces are very large. The drag of the diverter system can be divided, roughly, into two components - the wedge pressure drag and the drag associated with viscous forces. An experimental breakdown of the drag is given in figure 13, which shows the magnitude of the two components (ref. 40). From this figure it is evident that large wedge angles should be avoided if the total diverter drag is to be kept small. The symbol in the figure is the total drag coefficient of a wedge-type diverter with a cusped shape; the data were obtained from model tests in the Ames 6- by 6-foot wind tunnel. If a straight wedge had been used, the diverter angle would have been 33°. The drag of this system was somewhat less than that for straight-sided wedges.

With one exception, the data shown in figure 12 were for inlets having diverter boundary-layer control systems. The drag was large for the one configuration which used a suction system. Subsonic tests at the Ames laboratory on an airplane in flight having a suction boundary-layer control system showed a drag-coefficient increment of 0.0015 even in the subsonic speed range (ref. 41). In both of these tests, the high drag seems to be associated with the design of the exit of the boundary-layer control duct. If there is no external disturbance due to exiting the air, the drag of the suction system can be computed as the loss of momentum of the boundary-layer air in passing through the ducting system. This momentum loss is inversely proportional to the pressure recovery in the boundary-layer scoop itself. A summary of the available information on the pressure recovery of the boundary-layer control duct is given in figure 14 (see refs. 31, 42, 43, 44, and 25). It can be seen from a comparison of the curves shown that in actual installations the recovery is much lower than the average pitot pressure through the boundary layer (ref. 45). The size of the internal boundary-layer duct necessary is also determined by the total-pressure recovery of the boundary-layer control system. This figure shows that in order to supply the same amount of air the ducting would have to be 1.5 to 2.0 times as large in these cases as

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it would if the theoretical recovery were attained. Included for comparison purposes are the pressure recoveries measured beneath a sintered ramp during model tests at the Ames laboratory. The amount of air removed was from 2 to 2-1/2 percent of the inlet mass flow, which corresponds to about 15 percent of the boundary-layer air.

#### Methods for Increasing Side-Inlet Performance

Having summarized the pressure recovery and drag penalties associated with many existing side-inlet installations, one may ask what methods are being considered to increase their performance. Boundary-layer control on the compression surfaces of the inlets has evidenced some promise. Figure 15 summarizes the results obtained on two separate models. These data are for two side-inlet installations in which the ramp is approximately one boundary-layer thickness away from the fuselage (ref. 27 and unpublished data). The increase in pressure recovery is sizable, an increment of 0.04 to 0.06 having been obtained with either porous-ramp surfaces or a slot inside the inlet.

In an effort to improve side-inlet performance, configurations somewhat less conventional have been investigated. A circular side inlet and a porous-ramp side inlet have been tested in the Ames 6- by 6-foot wind tunnel. One of these, the circular inlet, is shown with a more conventional ramp-type side inlet in figure 16. The porous-ramp side inlet, which is not shown, is similar in shape to the ramp inlet shown in this figure but has the porous compression surface contiguous with the fuselage, thus having no diverter. Pressure recovery and drag of these three inlets are compared in figure 17 at their matched operating condition, which corresponds to a range of mass-flow ratios from 0.77 to 0.95. The pressure recovery of the circular inlet is not significantly different from that of the ramp inlet with boundary-layer control when a diverter wedge is used. At Mach numbers above 1.5, a curve of pressure recovery versus mass-flow ratio shows the diverter inlet to have a higher pressure recovery at massflow ratios greater than 0.85. It should be noted, however, that installation of a compression surface in the circular inlet could increase its pressure recovery at the higher mass-flow ratios at Mach numbers above 1.5. The porous-ramp trapezoidal inlet without a diverter, that is, with the ramp next to the fuselage surface, has lower pressure recovery than the other two inlets. The drag of the circular inlet is considerably less than the drag of the conventional ramp inlet (see fig. 17). This drag decrease amounts to about 6 percent of the total airplane drag. It is believed that the drag reduction due to the circular inlet is associated with the type of boundary-layer control system which offers less restraint to the boundary-layer air as it flows rearward along the fuselage. The drag of the porous-ramp inlet is less than that for the conventional ramp inlet but greater than that for the circular inlet.

Schlieren observations of the flow field about the circular inlet and the ramp inlet, which has a trapezoidal entrance area, are shown in figures 18 and 19. These schlieren photographs were taken at a Mach number of 1.5 and show the shock pattern characteristics of these two inlets as the mass-flow ratio is reduced from a maximum. It is interesting to note the differences in the shock-wave boundary-layer interaction accompanying the normal shock wave in front of the inlets. There being no compression surface in front of the circular inlet, the normal shock is stronger than it is for the ramp inlet, and the upstream disturbances through the boundary layer give rise to an oblique shock wave. This oblique wave accounts for the high pressure recovery of the circular inlet at reduced mass-flow ratios.

A significant performance comparison of the three inlets tested involves a conversion of the drag force and pressure recovery into a single net propulsive force parameter (see fig. 20). The inlets and engine must also be compared at their actual operating points (at the operating or matched condition in which the air supplied by the inlet must be equal to the air required by the engine). For this analysis, a typical jet engine operating at sea level and 35,000 feet was assumed. The drag forces used in the computations are for the fuselage air-induction systems shown in the previous figure and do not include the drag of wing or tail surfaces. In the computations, the assumption is made that the drag is not affected by the small changes in the inlet area necessary to match the inlet-engine operation. The entrance area of the inlet simulated by the model during the tests was 4.2 square feet. In general, the circular inlet can be seen to have considerably better net propulsive force than either the conventional-ramp or porous-ramp inlets at supersonic speeds. Only small differences can be observed between the performance parameter for the conventional-ramp and porous-ramp inlets. It should be noted that at supersonic speeds the change in the net propulsive force parameter with inlet area (or with mass-flow ratio) is much less for the circular inlet than for either of the other two inlets, indicating a more favorable offdesign performance for the circular inlet. Figure 20 shows that an entrance area of about 4.0 square feet, full scale, appears to be a good compromise, when the performance in the speed range from 0 to 1.5 is considered. Somewhat higher performance at supersonic speeds can be attained with an inlet area of 3.5 square feet. However, severe performance losses are incurred during subsonic operation. It should be remembered that the inlets which have been analyzed were designed primarily for operation at Mach numbers up to 1.5. When the inlets are designed for operation at higher Mach numbers, which change the external shape of the inlets, the net propulsive force parameter would be changed considerably at all speeds. The porous-ramp inlet which eliminated the diverter system was not entirely successful on this particular installation. Because only 2 to 2-1/2 percent of the inlet air was removed, the pressure recovery was not increased sufficiently to take advantage of the reduction in drag. It is possible that increases of perhaps 50 to 100 percent in the amount of air taken through the porous surface could result in better pressure

recovery for this type of inlet. It should be mentioned, however, that the range of stable operation of the porous-ramp inlets without diverters is less than that of the conventional-ramp inlets with diverters or the circular inlet (which has the best stability characteristics).

An attempt is also being made to develop new types of inlets having high performance, which can be used as either side inlets or in conjunction with nacelles. An inlet configuration which has been evolved utilizes multishock compression, the compression occurring internally in the inlet. The inlet that has been tested is shown in figure 21. Multishock compression was selected so that the strength (or pressure rise) of the initial shock would be below that necessary for separation. Internal compression is used to eliminate the high drag, at Mach numbers greater than 1.9, associated with multishock cone or wedge inlets having compression external to the inlet lips. The inlet is axially symmetric, and the angles of the compression surfaces are low. A side-inlet installation with this design might be similar to the circular inlet shown in figure 16. To achieve high pressure recovery with an internal-compression inlet requires that the contraction ratio approach that necessary for isentropic recovery. Since a supersonic inlet will not start at these contraction ratios, provision was made to vary the contraction ratio by making the center cone movable. Starting in the supersonic speed range from M = 1.6 to M = 2.1 was accomplished by extending the cone. The inlets were designed for maximum efficiency in the Mach number range from 1.9 to 2.1 when the center cone is set so that the apex is almost in the entrance plane. The compression is as nearly as possible apportioned equally between the compression surfaces. The circular inlet shape was selected because it eliminated the corners and the two converging side walls of rectangular internal-compression inlets. The angularity of the annular compression surface was kept small to minimize the focusing of the oblique shock waves at the center of the passage. These inlets have been tested at Mach numbers of 1.9, 2.0, and 2.1. The pressure recovery measured is shown on figure 22 together with the values from several other cone inlet studies (refs. 23, 36, and 46 to 48). The pressure recovery of the internal-compression inlet compares quite favorably with the cone inlets (which have the highest pressure recovery obtained to date). The drag resulting from external surfaces having such small deflection angles  $(0^{\circ} \text{ to } 2^{\overline{\circ}})$  is low. The lip angles of the cone inlets are from  $10^{\circ}$  to  $25^{\circ}$ , which result in considerable drag penalties. Because of its low drag and high pressure recovery, the internal-contraction inlet appears to show considerable promise. The research is in a preliminary stage and more complete investigation is planned.

#### Air-Flow Instability

The preceding comments have been restricted to those aspects of sideinlet performance which pertain to pressure recovery, drag, and net propulsive force. Little has been said concerning another factor in the design of induction systems which is equally as important as drag or pressure recovery, that is, inlet instability. With external-shock inlets, the instability is indicated by rapid flow pulsations which are usually encountered as the mass-flow ratio is reduced below its maximum. The following discussion of this problem includes a brief examination of the current theoretical views concerning inlet instability, a short summary of the effect of inlet instability on jet-engine performance, and a suggested method for analyzing and correlating inlet instability.

Several theories have been proposed to describe the mechanism of air-flow instability, or "buzz," and to determine the triggering force necessary for its start. These are given in references 49 through 53. None of these theories have been able to explain a majority of the cases where instability has occurred, and at least two different triggering forces, boundary-layer separation and a velocity discontinuity arising at the intersection of an oblique and a normal shock, are now known to incite buzz. Reports on most model experiments simply point out the mass-flow ratio at which the instability occurs. Little information has been given of the oscillating nature of the air flow, that is, measurements of the frequency and amplitude of the pressure pulsations that occur in the internal ducting.

Before discussing the effect of instability on engine performance, it is necessary to distinguish clearly between air-flow pulsations at the compressor inlet and air-flow distortion at the compressor inlet. Flow distortion has been considered a steady-state condition. The distribution of total pressure at the compressor has been the parameter most widely used to correlate distortion patterns with decreases in jet-engine performance. Inlet instability produces air-flow pulsations, resulting in nonsteady flow processes. Very little qualitative research, and no quantative studies have been made to determine a parameter suitable for correlating air-flow pulsations with jet-engine performance. A few attempts have been made to use the distribution of total pressure at the compressor inlet, the basis apparently being that certain of the engine manufacturers have required that the total pressure should not vary over 5 percent. If the problem is one of flow distortion then such a parameter might be useful; however, it has no obvious connection with oscillating flows.<sup>2</sup>

It has been shown, experimentally, by several investigators that airflow distortion at the compressor inlet can impair the performance of jet engines, in some cases causing premature surging of the compressor. The tests reported in reference 54 were made in an NACA altitude test chamber at the Lewis laboratory on an axial-flow jet engine. The unequal flow distribution in these tests was such as to cause failure of the turbine under certain conditions. Before the failure, it also had the effect of reducing the efficiency of the compressor and the turbine, so that the thrust of the engine was reduced and the fuel consumption increased. Surging of jet-engine compressors also has been encountered during flight and, in most cases, has been attributed to air-flow distortion. However, many of these surges occurred under conditions where considerable flow unsteadiness existed, the surging difficulties being encountered during take-off and during high-speed climb and maneuvers, where separation from the inlet lips was present. One experimental study has been made on a jet-engine cone-inlet combination in the Lewis 8- by 6-foot wind tunnel which is reported in reference 33. Although buzz occurred, it appeared to be less severe with the engine installed and operating than it was with the engine removed. The data presented do not include measurements of the amplitude or frequency of the pressure fluctuations. It might be noted that buzz for this type of inlet is triggered by a velocity discontinuity due to the intersection of an oblique and a normal shock wave which comes in contact with the inner lip surface of the cowl. In another case, for an airplane in flight, the instability was started by separation induced by boundary-layer shock-wave interaction. The occurrence of the instability, which resulted in severe buffetting, agreed qualitatively with wind-tunnel results, but detailed measurements were not made.

The few, and sometimes conflicting, experimental observations of the effect of inlet instability on jet-engine performance direct attention to the need for a more unified approach to this problem. It was noted that records of the pulsating pressure in the induction system versus time, for several wind-tunnel models, were similar to records obtained in the study of velocity fluctuations in turbulent boundary layers. It was reasoned that inlet buzz could be analyzed in the same manner that turbulent boundary layers have been analyzed, that is, from a statistical point of view. Treating the unsteady flow as a stationary random function of time yields a method for constructing a more complete model of the flow

<sup>2</sup>It is impossible to obtain accurate and reliable data from a totalpressure tube mounted in such flows. It has been shown by Goldstein, in reference 55, that a total-pressure tube in an air stream with a fluctuating velocity will always indicate a pressure higher than the mean pressure. There is also the unknown effect of damping by the length of tube that connects the manometer with the total-pressure probe itself.

mechanism. By use of the concept of spectral density, it is possible to obtain the root-mean-square amplitude of the fluctuating pressure and to show the frequency range which contains the largest percentage of the turbulent energy (refs. 56 to 60). Figure 23 shows a typical pressuretime record that was obtained from one of the inlet models tested at the Ames laboratory. A schematic diagram of the method is outlined at the top of figure 24. The dynamic pressure cell which measures the oscillating pressures is mounted inside the inlet and the impulses from this cell are recorded onto a tape. The tape is then put through a wave analyzer which in turn plots the spectral density used in the analysis of the data. The spectral density derived from the magnetic tape as it is put through the wave analyzer is shown on the lower portion of the figure. These data are for a Mach number of 1.7 at a mass-flow ratio of 0.59. By integration of the total area beneath the curve of spectral density versus frequency, the root-mean-square amplitude of the pressure fluctuations can be obtained. This curve shows that the instability occurs between 10 and 450 cycles per second, with the energy being concentrated in two bands, one at 100 cycles and the other at 350 cycles. It was also determined from separate samples that the instability was a stationary random process.

The method employing the root-mean-square amplitude of the fluctuating pressure has been used in analyzing the data of two inlet models tested in the Ames 6- by 6-foot wind tunnel. Data for these two configurations are shown in figures 25 and 26. On the right of figures 25 and 26 are shown the maximum amplitude of the fluctuating pressure obtained from the pressure time records as a fraction of the free-stream total pressure. The curves on the left of figures 25 and 26 show the ratio of the root-meansquare fluctuating pressure (determined from spectral-density plots by the method just outlined) to the free-stream total pressure. For these two models, it can be seen that the ratio of the maximum amplitude may or may not be a smooth function of mass-flow ratio. However, in both cases the rms ratio of the fluctuating pressure is a smooth and continuous function of mass-flow ratio, its values increasing with increasing Mach number and with decreasing mass flow. It is interesting to note that the rms pressure amplitude does not increase suddenly, but increases smoothly as the massflow ratio is decreased. Schlieren observations of buzz, on the other hand, lead one to expect a sudden change of fluctuating pressure as the mass-flow ratio is decreased. It is believed that the rms amplitude, rather than the maximum amplitude of the pressure fluctuations are related to the jet-engine performance, and therefore the schlieren observations may be misleading. Use of this statistical approach should provide a

basis for analyzing the effects of pressure pulsations on jet engine performance and for correlating model and full-scale tests.

Ames Aeronautical Laboratory National Advisory Committee for Aeronautics Moffett Field, Calif., June 29, 1955

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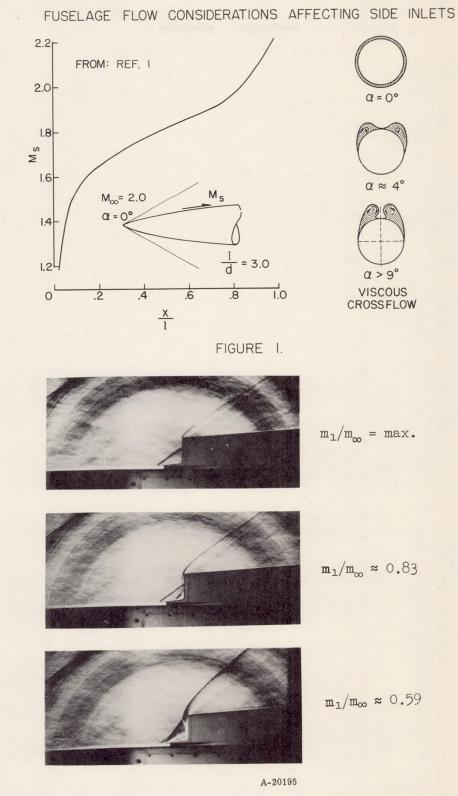
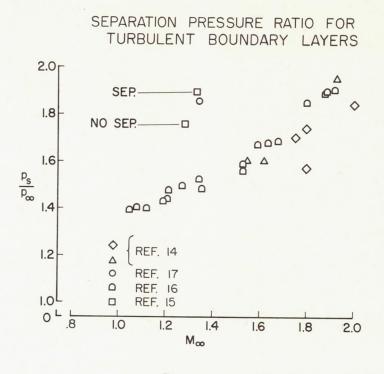


Figure 2.- Extent of flow separation on a ramp in front of an inlet.





PRESSURE RECOVERY OF NORMAL-SHOCK INLETS

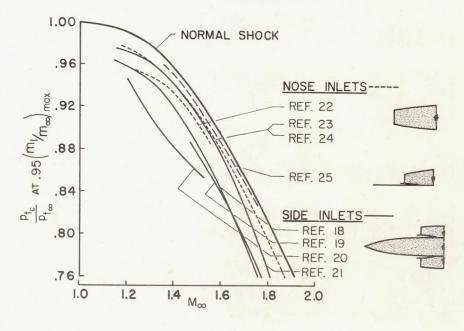


FIGURE 4.

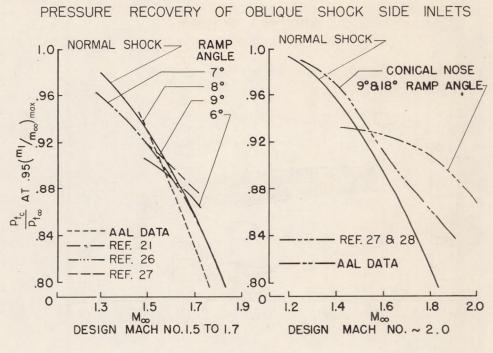
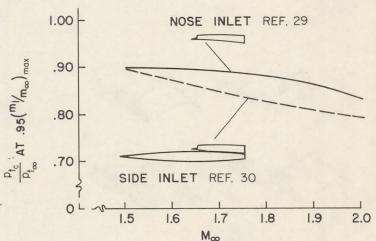


FIGURE 5.

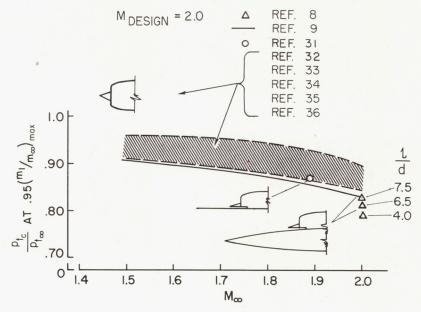
EFFECT OF A FUSELAGE ON THE PRESSURE RECOVERY OF A 14° RAMP INLET

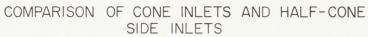
 $\frac{h}{\delta} = 1.0 \qquad \frac{l}{d} = 7.5$ 



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FIGURE 6.







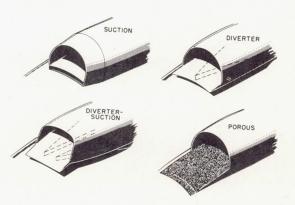
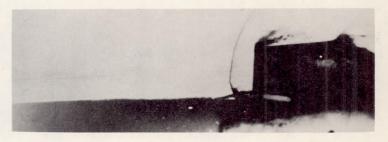


Figure 8.- Boundary-layer control systems for side inlets.



(a) Boundary-layer diverter angle =  $130^{\circ}$ .

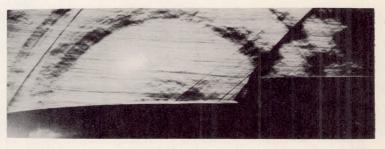


(b) Boundary-layer diverter angle =  $65^{\circ}$ .

Figure 9.- Effect of a diverter boundary-layer control system.



(a) Boundary-layer diverter angle =  $40^{\circ}$ .



A-20196

(b) Boundary-layer diverter angle =  $20^{\circ}$ .

Figure 10.- Effect of a diverter-suction boundary-layer control system.

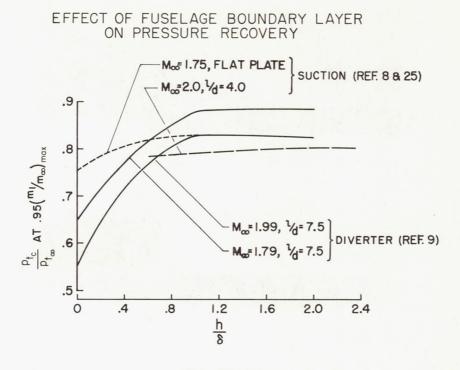


FIGURE II.

DRAG OF BOUNDARY-LAYER CONTROL SYSTEMS

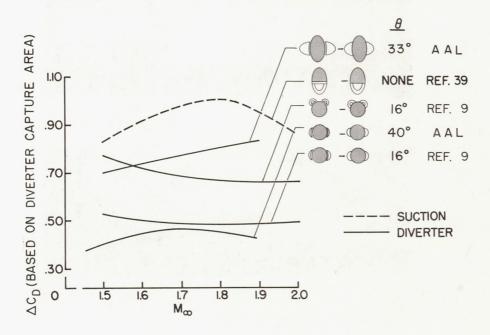
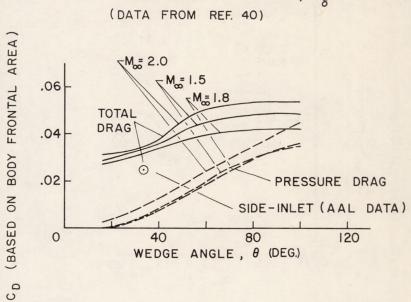


FIGURE 12.



DRAG OF WEDGE DIVERTERS,  $\frac{h}{8}$  = 1.0



PRESSURE RECOVERY OF BOUNDARY-LAYER CONTROL SYSTEMS

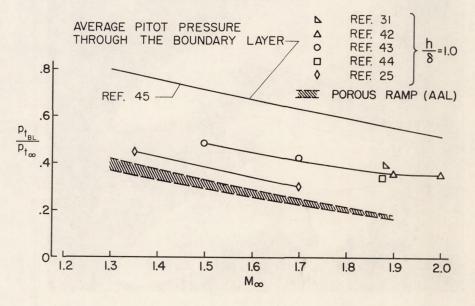


FIGURE 14.



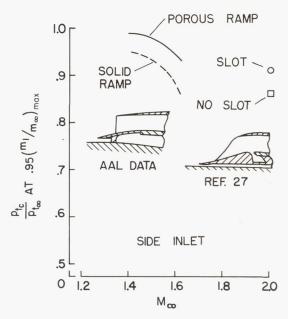
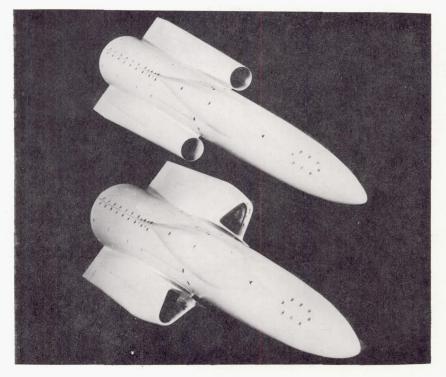


FIGURE 15.



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Figure 16.- Circular and trapezoidal side inlets.

COMPARISON OF THREE SIDE INLETS ("MATCHED" OPERATION ) 35,000 FT ALTITUDE

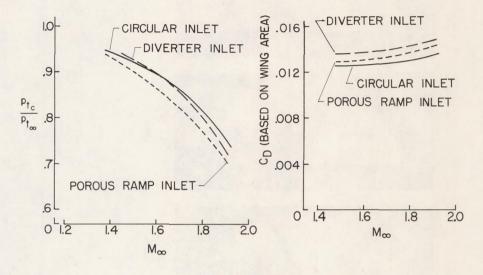
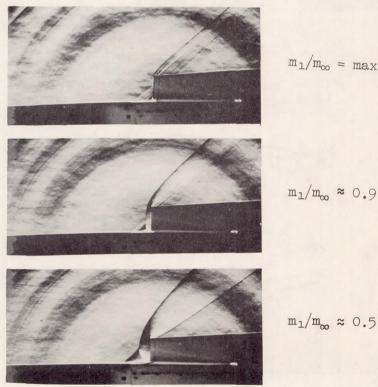


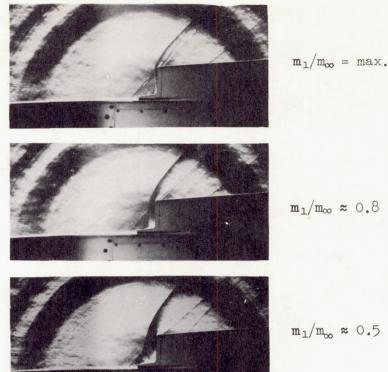
FIGURE 17.



 $m_1/m_{\infty} = max.$ 

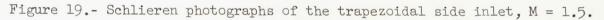
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Figure 18.- Schlieren photographs of the circular side inlet, M = 1.5.



 $m_1/m_{\infty} \approx 0.5$ 





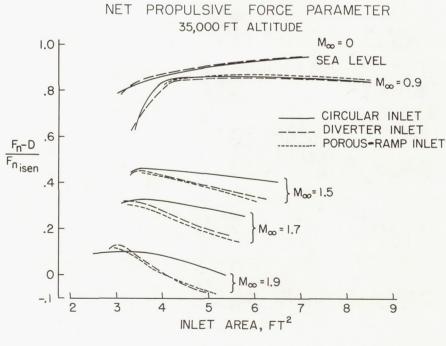


FIGURE 20.

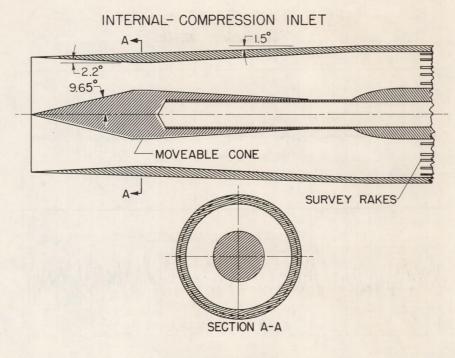


FIGURE 21.

COMPARISON OF CONE INLETS AND AN INTERNAL COMPRESSION INLET

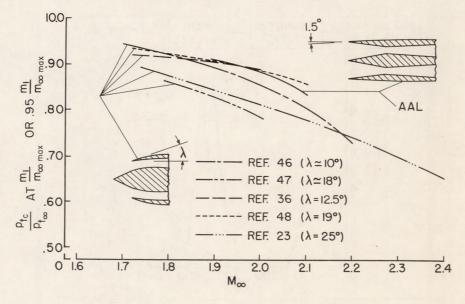


FIGURE 22.

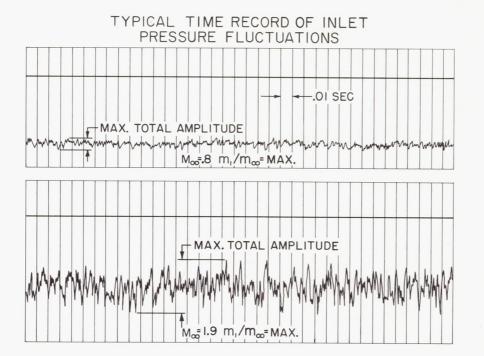


FIGURE 23.

TYPICAL SPECTRAL DISTRIBUTION FOR A TWIN SIDE INLET

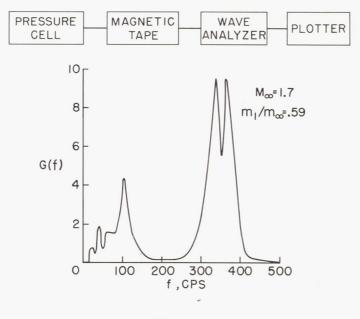
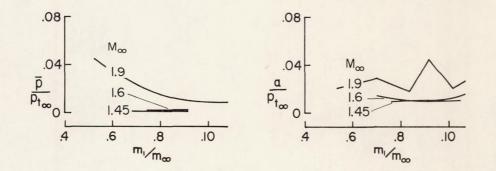


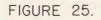
FIGURE 24.

### PARAMETERS FOR INLET INSTABILITY









PARAMETERS FOR INLET INSTABILITY

TWIN DUCT SIDE INLET

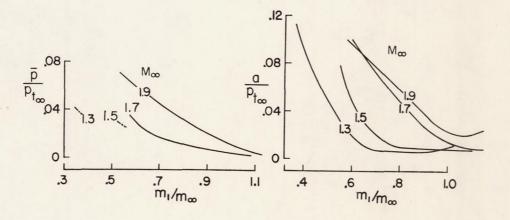


FIGURE 26.

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