

# RESEARCH MEMORANDUM

#### ANALYSIS OF RAM-JET ENGINE PERFORMANCE INCLUDING

#### EFFECTS OF COMPONENT CHANGES

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## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

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#### SUMMARY

Ram-jet engine performance data are presented over a range of engine design variables to aid in the selection and evaluation of a ramjet engine configuration with particular emphasis on one suitable for a long-range supersonic missile. Calculated design-point performance of engines using JP-4 fuel is presented for a wide range of engine totaltemperature ratios and combustion-chamber-inlet Mach numbers for flight Mach numbers from 1.5 to 4.0. The results include engine thrust, drag, fuel consumption, and area ratios, and are presented both with and without nacelle drag included. Maximum engine fuel specific impulse (including nacelle drag) is 1600 to 1700 pound-seconds per pound and occurs at a flight Mach number of 2.5 to 3.0. Over-all engine efficiency, however, continues to increase to a flight Mach number of 4.0, where it is 35 to 40 percent.

Important gains in both thrust coefficient and specific impulse may be achieved by improving the diffuser pressure recovery. Changes in flameholder pressure loss and combustor length have only small effects on engine performance. That these factors, however, influence combustion efficiency is significant, because the specific impulse varies directly with the efficiency, although the thrust coefficient is practically unaffected. Engine performance is very sensitive to changes in nozzle performance, a l-percent variation in velocity coefficient often producing a 3-percent variation in engine thrust and specific impulse. Some underexpansion of the exhaust gases is desirable to reduce nacelle drag whenever the nozzle-exit diameter exceeds that of the combustion chamber.

With a fixed-geometry configuration, a ram-jet engine does not operate satisfactorily at off-design conditions. Somewhat better thrust can be obtained with the added complication of a translating-spike diffuser, although the specific impulse is poorer. Use of a movable plug to vary the throat area of the exhaust nozzle yields both thrust and specific impulse approaching those of a continuously variable geometry engine.

#### INTRODUCTION

The suitability of the ram-jet engine for the propulsion of highspeed aircraft has been generally recognized and accepted. The selection of the proper engine for such applications must be based on many factors relating to the airframe-engine combination. The purpose of this report is to present calculated ram-jet engine performance data over a range of engine design parameters in order to aid in the selection and evaluation of an engine design. General emphasis is placed on designs suitable for a long-range supersonic missile. A second purpose is to illustrate the relative importance of the different engine parameters that influence the design of the ram-jet engine. Many other thermodynamic cycle studies of ram-jet engines are presented in the literature (e.g., refs. 1 and 2). This report presents a wider range of operating conditions, uses somewhat more advanced, but realistic, component characteristics, and demonstrates the effect of changes in these component characteristics.

The engine performance data are presented such that they may be used either with or without nacelle drag included and are therefore suitable for aircraft configurations with either internal or external engine installations.

The report has three major sections:

(1) General design-point engine performance is presented for a wide range of engine total-temperature ratios and combustion-chamber-inlet Mach numbers for flight Mach numbers from 1.5 to 4.0. The fuel used is JP-4, and nominal assumptions are used for the component characteristics.

(2) The sensitivity of these design-point results to changes in the nominal assumptions is indicated by showing the effect of varying the different component parameters, one at a time, on the performance of selected engines. The parameters investigated are diffuser pressure recovery, flameholder pressure loss, combustion efficiency, nozzle velocity coefficient, nozzle expansion ratio, nozzle jet-deflection angle, and altitude. Calculations were also made comparing a high-energy fuel (pentaborane) with JP-4.

(3) Off-design performance is presented for an engine designed for efficient cruising at a flight Mach number of 3.5. Configurations having fixed geometry, continuously variable geometry, and two types of practically variable geometry are compared. Off-design performance is not emphasized, because results obtained in missile studies indicate that self-boosting capabilities are not important for ram-jet-powered long-range missiles using rocket boosters.

#### ANALYSIS

The symbols used in this report are defined in appendix A.

A schematic diagram of a ram-jet engine is shown in figure 1. Highspeed air enters the engine at station 1 and is decelerated to a low velocity at 2. Fuel is added, ignition takes place, and combustion is stabilized at the flameholders, between stations 2 and 3. Combustion occurs in a constant-area duct from stations 3 to 4, and the hot gases are expanded and discharged through a convergent-divergent nozzle (stations 4 to 6).

The performance calculations were made on the basis of onedimensional flow, using the equations of state, continuity, and conservation of momentum and energy. Reference 2 presents equations similar to those used in the present analysis, in which the values of  $\gamma$  are based on the gas static temperature and composition at each station. The problem of specifying the gas properties is discussed more fully in appendix B, and the assumed engine geometry and methods used in calculating the engine drags are detailed in appendix C. Engine performance data, which are generally presented for an altitude of 70,000 feet, may be used for any altitude in the isothermal region of the atmosphere with negligible error.

Engine performance is presented in this report in terms of the following:

(1) Propulsive thrust coefficient  $C_{\rm T}$ , defined as engine thrust minus nacelle drag per unit cross-sectional area, divided by free-stream incompressible dynamic pressure. The cross-sectional area used is the diffuser capture area or the combustion-chamber frontal area, whichever is larger. This coefficient is a measure of the engine size required to produce a given amount of propulsive thrust.

(2) Specific impulse I, defined as engine thrust minus nacelle drag divided by engine fuel-flow rate. At any given flight speed, this parameter is a measure of the efficiency with which thrust is produced.

Similarly, the net-thrust coefficient and specific impulse  $C_F$ and  $I_F$  are defined as above except that nacelle drag is not included.

Most of the various engine parameters fall into two groups: (A) those of major importance that cannot be finally specified without a complete flight analysis, and (B) those that can be realistically chosen from an engine study alone, or that are limited by what can practically be achieved. These major variables (group A) were taken as flight Mach number, combustion-chamber-inlet Mach number, and engine total-temperature ratio. A complete set of design-point performance calculations was obtained for different values of these variables, based on nominal assumptions made for the component parameters of group B. The range of calculations for these major variables included flight Mach numbers from 1.5 to 4.0, combustion-chamber-inlet Mach numbers from 0.125 to 0.225, and engine total-temperature ratios corresponding to fuel-air ratios of approximately 0.01 to stoichiometric, except where limited by thermal choking.

The following assumptions were used for the variables of group B in the design-point calculations:

(1) Engines were considered with both single- and double-cone diffusers. The design-point engines operated critically (i.e., with the normal shock located at the inlet lip). For the single-cone diffuser, cone angle was varied with design flight speed to achieve maximum pressure recovery. For the two-cone diffuser, the cone angles were not selected for maximum pressure recovery but chosen to permit use of a lowdrag cowl (low lip angle). Figure 2 shows the assumed variation of pressure recovery with flight Mach number for the two diffuser types. The illustrated single-cone values are in good agreement with the experimental data for similar inlets reported in reference 3. Reference 4 shows that, in the present state of inlet development, the engine performance obtained with the single-cone inlet with low drag cowl is as good as that afforded by more elaborate diffusers such as the isentropic spike.

(2) Flameholder total-pressure loss was taken as twice the incompressible dynamic pressure at station 2. Combustion of the fuel (JP-4 with a lower heating value H of 18,640 Btu/lb) took place from stations 3 to 4 with an assumed efficiency of 0.90. The resulting relation between  $\tau$  (engine total-temperature ratio) and fuel-air ratio f/a for different flight Mach numbers is shown in figure 3. Reference 5 reports the achievement of about 0.95 efficiency with the same amount of flameholder loss in tests of a 16-inch combustor at a combustor pressure of about 1 atmosphere.

(3) The nozzle velocity coefficient was taken as 0.975. Values of this magnitude have been obtained experimentally for convergent-divergent nozzles at nozzle pressure ratios  $P_4/p_6$  of about 15 (ref. 6). At flight Mach numbers of 2.5 and higher, the nozzle-exit diameter is generally the largest diameter of the engine. To reduce nacelle drag in these cases, the nozzle expansion ratio was made less than that required for complete expansion of the gases to ambient pressure. From unpublished

data obtained in long-range missile studies showing the effect of expansion ratio on missile range, the optimum expansion ratio is roughly generalized by the empirical formula

$$\frac{A_6}{A_3} = 1 + 0.55 \left[ \left( \frac{A_6}{A_3} \right)_{p_6 = p_0}^{p_6 = p_0} - 1 \right]$$
(1)

where  $\left(\frac{A_6}{A_3}\right)_{p_6=p_0}$  is the ratio of nozzle-exit to combustion-chamber area

for complete expansion. This expression was used for the design-point engine calculations whenever the nozzle-exit diameter exceeded that of the combustion chamber. In all other cases the nozzle was made completely expanding.

The sensitivity of the design-point results to changes in these assumed values of the various component parameters was indicated by calculating the effect of varying these parameters, one at a time, at flight Mach numbers of 2.5 and 3.5. At each speed, two values of  $\tau$  were considered, a low value for good cruising performance and a higher value to give increased thrust for acceleration.

The off-design performance of engines designed for cruising at a flight Mach number of 3.5 was also evaluated. Engines equipped with the following features were considered:

- (1) Continuously variable diffuser and nozzle
- (2) Variable-throat-area nozzle with fixed diffuser
- (3) Translating-spike diffuser with fixed nozzle
- (4) Fixed diffuser and nozzle

#### RESULTS AND DISCUSSION

#### Design-Point Performance

The calculated design-point values of propulsive thrust coefficient and specific impulse are shown in figure 4 for the single-cone diffuser as functions of flight Mach number  $M_0$ , ratio of combustion-chamber-exit to -inlet total temperature  $\tau$ , and combustion-chamber-inlet Mach number  $M_2$ . These data, as well as engine area ratios and drag coefficients, are listed in table I. Similar data are listed in table II for the two-cone diffuser. The values of  $C_{\rm T}$  and I include nacelle drag. The corresponding values without nacelle drag may be obtained by the relations

$$C_{\mathbf{F}} = C_{\mathbf{T}} + C_{\mathbf{D}}$$
(2)

$$I_{\rm F} = I \frac{C_{\rm F}}{C_{\rm T}}$$
(3)

Performance of engines having velocity coefficients other than 0.975 may be calculated from the following formula:

$$C_{\rm T} = \frac{C_{\rm V}}{0.975} \left[ (C_{\rm T})_{0.975} + C_{\rm D} + 2 \left( \frac{A_{\rm l}}{A_{\rm S}} \right) \right] - C_{\rm D} - 2 \left( \frac{A_{\rm l}}{A_{\rm S}} \right)$$
(4)

which is based on the assumption that the jet thrust is directly proportional to the velocity coefficient and that the nacelle drag does not change. The change in I is directly proportional to the change in  $C_m$ .

Performance can also be computed for values of combustion efficiency other than 0.90. At any constant value of  $\tau$ , the thrust coefficient remains essentially constant with changes in combustion efficiency, and specific impulse and fuel-air ratio are given by

$$I = \frac{\eta_c}{0.90} I_{0.90}$$
(5)

$$\frac{f}{a} = \frac{\eta_c}{0.90} \left(\frac{f}{a}\right)_{0.90}$$
(6)

The effect of changes in diffuser pressure recovery may be approximated by the following expressions:

$$C_{\rm T} = \frac{F - D}{q_{\rm O}A_{\rm S}} = \left(C_{\rm T}' + \frac{A_{\rm 6}/A_{\rm 3}}{\frac{\gamma}{2} M_{\rm O}^2} + C_{\rm D}\right) \frac{P_{\rm 2}/P_{\rm O}}{(P_{\rm 2}/P_{\rm O})'} + \frac{A_{\rm 6}/A_{\rm 3}}{\frac{\gamma}{2} M_{\rm O}^2} \left(\frac{P_{\rm 6}}{P_{\rm O}} - 1\right) - C_{\rm D}$$

$$(7)$$

$$I = I' \frac{C_{T}}{C_{T}'} \frac{(P_{2}/P_{0})'}{P_{2}/P_{0}}$$
(8)

$$A_{1}/A_{3} = \frac{(A_{1}/A_{3})'(P_{2}/P_{0})}{(P_{2}/P_{0})'}$$
(9)

in which  $(P_2/P_0)'$  denotes the single-cone pressure recoveries given in figure 2, and  $C_T$ , I', and  $(A_1/A_3)'$  are the values listed in table I. Equations (7) to (9) are based on the assumptions that the inlet capture area is varied with pressure recovery and nacelle drag and nozzle exit area are constant. The data of table I and equations (7) to (9) were used to compute the performance presented in table II for the low-cowldrag two-cone diffuser. (Note that eqs. (7) and (8) require that  $C_T$  be based on  $A_3$ .)

The remaining discussion, except where noted, is based on the lowcowl-drag single-cone diffuser. Although the actual level of performance may be somewhat different with other diffuser types, all the trends are expected to be the same.

Figure 4 shows that high thrusts are obtained at the high values of  $\tau$  and maximum specific impulses at intermediate values of  $\tau$ . Raising  $\tau$  (at a constant  $M_0$  and  $M_2$ ) increases the exit momentum of the gases, mainly because of the higher jet velocity and, to a lesser degree, because of the increased fuel mass flow. However, as  $\tau$  is raised, the fuel flow increases at a greater rate than the jet thrust, so that, after the constant loss of the inlet momentum drag is sufficiently overcome, the specific impulse reaches a maximum and then decreases. When nacelle drag is included, the value of  $\tau$  for maximum specific impulse is raised.

The effect of flight Mach number on over-all engine efficiency and specific impulse is shown in figure 5, in which the value of  $\tau$  is varied to provide maximum I and E at each flight speed. Combustionchamber-inlet Mach number is generally 0.200, except for  $M_{O}$  above 3.5, where it was necessary to reduce  $M_2$  to prevent the diffuser-inlet diameter from exceeding that of the combustion chamber. Maximum I (1600 lb-sec/lb including nacelle drag) occurs at  $M_0$  of 2.5. This flight Mach number, however, may not be optimum for a missile, because missile range is more nearly related to the over-all engine efficiency, which in turn is proportional to the product of specific impulse and flight velocity rather than to specific impulse alone. Maximum E of the order of 0.35 is realized at  $M_0$  near 4, while the highest efficiency obtainable at MO of 2.5 is only 27 percent. For engines with a two-cone diffuser, the maximum values of I and E are 1700 and 40; respectively. (Still higher values of E would be expected for  $M_{\Omega}$  greater than 4.) t\_\_\_\_

The effect of combustion-chamber-inlet Mach number  $M_2$  is indicated in figure 4 but is more readily apparent in a cross plot of some of these data (fig. 6). The thrust coefficient increases with  $M_2$  because of the essentially linear increase in air flow to the point where the inlet capture area becomes equal to the combustion-chamber area. The value of  $M_2$  at which these areas are equal is higher than the

region of interest shown in figure 6, but is a function of the flight speed and the diffuser pressure recovery. Raising  $M_2$  also increases both the flameholder pressure loss and the momentum pressure loss due to heat addition. If nacelle drag is not included, the specific impulse decreases with increasing values of  $M_2$ . However, higher values of  $M_2$  reduce the diameter of the combustor and nozzle relative to the diffuser capture area and so result in lower nacelle drag per pound of air (provided the capture area remains smaller than the combustion-chamber area). Because of these two opposing effects, the specific impulse including drag is fairly insensitive to variations in  $M_2$  for the conditions of figure 6.

#### Effect of Variations in Design-Point Assumptions

Diffuser pressure recovery. - Diffuser total-pressure ratio is used in this report as a measure of the efficiency with which the diffuser converts the kinetic energy of the captured airstream to pressure. Lines of constant kinetic-energy efficiency superimposed on the curve of pressure recovery against flight Mach number (fig. 2) show that the lower numerical values of total-pressure ratio at high flight Mach numbers do not necessarily mean lower diffuser efficiency.

The nominal diffuser assumed for the design-point calculations is an oblique-shock inlet with a single-cone spike centerbody. Figure 7 shows the effect on engine performance of changes in the assumed values of pressure recovery. (This performance is based on the drag of a lowangle cowl at all pressure recoveries.) The engine air flow per unit combustion-chamber area increases linearly with pressure recovery, so that the propulsive thrust coefficient (based on combustion-chamber area) also increases nearly linearly. As pressure recovery is increased, the diffuser capture area enlarges relative to the combustion chamber in order to handle these larger air flows at constant M2. At high flight Mach numbers and high pressure recoveries, the resulting capture area often becomes greater than the combustion-chamber area. The size of the engine required to produce a given thrust is then indicated by basing the thrust coefficient on diffuser capture area. At a flight Mach number of 2.5, the combustion chamber is always the larger for the range of pressure recoveries considered. At a flight Mach number of 3.5 and  $M_2$ of 0.20, the capture area becomes the larger at pressure recoveries greater than 0.43, which causes the sharp break in thrust coefficient observed at this point in figure 7. The engine specific impulse increases with increasing pressure recovery because of the higher pressure ratio across the exhaust nozzle. The higher air flow also improves the specific impulse because of the lower nacelle drag per pound of air.

In general, however, diffuser designs that result in improved pressure recoveries have associated with them high engine-cowl pressure drags. Consequently, the gain in engine performance resulting from improved pressure recovery may be largely offset by the resulting engine drag increase. Figure 8 shows engine performance at a flight Mach number of 3.5 as a function of both pressure recovery and engine nacelle drag coefficient. The dotted line repeats the low-angle-cowl drag values from figure 7 and represents the best performance attainable at any value of pressure recovery. Figure 8 indicates the penalties in drag rise that are acceptable to obtain better engine performance as a result of improved pressure recovery. Calculations based on the experimentally measured pressure recovery and cowl drags reported in reference 3 confirm the conclusion that currently available high-recovery inlets do not yield better over-all engine performance than does the single-cone type. Although the single-cone inlet was used to give performance representative of that available with other current inlet types, the advanced inlets have greater potentialities for improvement, as indicated in figure 8. Other factors must also be considered, of course, in comparing different diffuser designs. For example, a single-cone inlet may be easier to design and manufacture and is less sensitive to angle of attack than are more elaborate types. On the other hand, the higher pressure provided by an advanced inlet may increase combustion efficiency and prevent blowout.

The effects of variations discussed in the following sections are based on the use of a single-cone diffuser.

Combustion efficiency. - If  $\tau$  is held constant in an engine, variations in combustion efficiency have only a negligible effect on engine thrust. However, fuel flow and hence specific impulse are directly proportional to the combustion efficiency. The great importance of this effect lies in the fact that the range of a ram-jet missile varies directly with the specific impulse, if all other factors do not change.

Flameholder pressure loss. - The purpose of the flameholder is to ensure the ignition and efficient burning of a fuel-air mixture moving at several hundred feet per second when the laminar flame speed of the mixture may be in the order of only 5 feet per second. Increased flow blockage and turbulence often improve the combustion efficiency but introduce pressure losses detrimental to the thrust output of the engine. A compromise is often necessary between these opposing factors. The change in propulsive thrust and specific impulse with the flameholder, cold-flow pressure-drop coefficient is indicated in figure 9 for a constant combustion efficiency.

<u>Fuel type</u>. - Another combustor variable that may be changed to improve performance is the fuel used. High-energy fuels permit raising both thrust and specific impulse, but they are generally more expensive

than hydrocarbon fuels, or they may have other undesirable characteristics such as pumping or storage problems. Calculations were made for pentaborane  $(B_5H_9)$  as a typical high-energy fuel frequently mentioned for ram-jet applications. Figure 10 shows the propulsive thrust coefficient and specific impulse of an engine designed for flight Mach number of 3.5 for pentaborane and JP-4. These calculations for  $B_5H_9$  were made with the assumption of equilibrium composition of the exhaust gases and with expansion to the same area assumed with JP-4. Data for these calculations were taken from reference 7. These curves are for a combustion efficiency of 0.95 for the pentaborane and 0.90 for the JP-4 fuel.

For the same thrust coefficient, a specific impulse with pentaborane of more than 150 percent of that with JP-4 is indicated at low fuel-air ratios up to those that give maximum specific impulse. The improvement is less at high fuel-air ratios that give near maximum thrust coefficient.<sup>a</sup>

Nozzle area ratio. - The effect of nozzle area ratio is presented in figure 11. Very little loss in propulsive thrust coefficient and specific impulse is suffered by cutting back the nozzle area as much as 30 percent from that required for complete expansion. In fact, for smaller amounts of underexpansion, gains of 1 or 2 percent may be realized, because reducing these areas reduces the external nacelle drag sufficiently to compensate for the lower internal thrust. In addition, since the nozzle was assumed to have a velocity coefficient less than 1.0, a small amount of underexpansion results in a very small increase in internal thrust. It is sometimes proposed that the nozzle-exit area not be permitted to exceed the combustion-chamber area. This condition  $(A_6 = A_3)$  is marked on the curves of figure 11. It is apparent that this amount of underexpansion results in appreciable losses, particularly • at the higher flight speed. The performance of a convergent nozzle  $(A_6 = A_5)$  is seen to be very poor at both speeds.

Nozzle velocity coefficient. - The velocity coefficient (defined as the actual velocity at the nozzle exit divided by the ideal isentropic velocity at the nozzle exit for the same pressure ratio) is used to indicate the amount of the nozzle internal flow losses. These losses, which reduce the total pressure, are due to shocks, turbulence, and viscous effects within the gas stream and to wall friction at the gas boundaries. The effect on engine performance of a variation in the nozzle

<sup>a</sup>Since the calculations for figure 10 were completed, revised data have become available for the combustion products of  $B_5H_9$ . The curve presented, therefore, is only indicative of the general improvement possible with  $B_5H_9$ ; the absolute magnitudes may be somewhat in error. (Ref. 8 presents charts and tables which incorporate these revised combustion data and which may be used for cycle calculations with pentaborane fuel.)

velocity coefficient from the assumed value of 0.975 is indicated in figure 12. A 1-percent change in velocity coefficient changes the thrust and specific impulse from 2 to 3 percent for the indicated values of Mach number and  $\tau$ .

There are other sources of thrust losses through the nozzle that do not affect total-pressure loss. In addition to the flow losses treated through the application of a nozzle velocity coefficient, the assumption of one-dimensional flow implies that all exhaust gases are discharged axially and that there are no radial gradients in velocity. Neither of these implications is necessarily true. A nonuniform temperature distribution at the combustor exit would result in radial velocity gradients. Calculations indicate that all reasonable temperature distributions, such as a parabolic profile, result in thrust losses of less than 2 percent. Losses due to nonaxial discharge from a conical nozzle with a half-angle of 15° would be of the order of 1.5 percent. Use of a smaller angle or changes in nozzle contour would reduce this loss, although possibly at the expense of increased manufacturing cost and nozzle length.

<u>Nozzle jet-deflection angle</u>. - An interesting possibility for improving the performance of a ram-jet missile lies in turning the jet thrust of the engine downward. This slightly decreases the forward thrust and specific impulse but provides some lift, thereby permitting the use of a smaller wing and lowering the missile weight and drag. Figure 13 presents the effect of jet-deflection angle on engine performance, in which  $C_{T,v}$  represents the component of vertical thrust divided by the free-stream dynamic pressure  $q_0$  and the engine cross-sectional area  $A_m$ . These data are based on the assumption that nacelle drag does not change with deflection angle.

Altitude. - In the stratosphere (between 35,332 and 105,000 ft), changing flight altitude has only a small effect on propulsive thrust coefficient and specific impulse through the Reynolds number effect on nacelle skin-friction drag coefficient. Below the tropopause, in addition to this Reynolds number effect, the changing ambient temperature significantly affects ram-jet performance. In this region more fuel is required to maintain a design au as the altitude is reduced. This extra mass addition, although it raises the thrust coefficient slightly, lowers the specific impulse considerably. This same increase in fuel consumption is felt by the over-all engine efficiency; however, the increased flight velocity (at constant flight Mach number) reduces the magnitude of the effect. These considerations combine to produce the variations in propulsive thrust coefficient, specific impulse, and overall efficiency shown in figure 14. Also important is the effect of flight altitude (not shown) on combustion efficiency through changes in ambient pressure and temperature, which in turn establish the temperature, pressure, and velocity at the combustor inlet.

#### Off-Design Performance

All the previous discussion has been concerned with a continuously variable-geometry engine or a series of fixed-geometry design-point engines. Thus, it is implied that the inlet capture area is sized to avoid subcritical spillage, the diffuser cone angle is selected for optimum pressure recovery, the diffuser spike can be translated for correct positioning of the oblique shock upon the cowl lip, and the nozzle-throat area and area ratio are optimum. A practical engine incorporating such variable components is not yet available.

This invariance of geometry is of no concern if the engine can always be operated at its design or cruise point. Design-point engine operation is possible for a ram-jet missile that cruises along a Breguet flight path, provided the missile is fully boosted to its cruising Mach number and altitude by some other means. Even after starting cruise flight, however, some corrective action may be required and off-design engine operation may be necessary. Moreover, ram-jet thrust may be desired during the boost phase of the flight. In order to include engine performance for these flight conditions, some off-design engine calculations were also made. Because it was desired to indicate trends rather than absolute magnitudes, a constant value of  $\gamma$  of 1.30 for the exhaust gas was used for ease of computation of the off-design performance.

Figure 15 shows the propulsive thrust coefficient and specific impulse of a fixed-geometry engine designed to operate at  $M_0$  of 3.5,  $M_2$ of 0.200, and  $\tau$  of 2.25. Because the combustor must now operate over a wide range of flight conditions, the combustion efficiency (0.87) was assumed to be slightly lower than that for the design-point case (0.90). Along each line of constant  $M_{\Omega}$ , the parameter  $\tau$  is raised to increase the thrust coefficient. For any given  $\tau$  there is a single unique value of  $M_2$  due to the choked fixed-nozzle throat area. At  $M_0$  of 3.5 and values of  $\tau$  below 2.25, M<sub>2</sub> is greater than 0.2 and the diffuser operates supercritically, with a severe loss in pressure recovery and a consequent adverse effect on thrust and specific impulse. As  $\tau$  is raised by burning more fuel, M2 is reduced to its design value, and the diffuser then operates critically, with the normal shock positioned at the diffuser lip. This condition corresponds to the sharp break in the curve. Further increase of  $\tau$  causes subcritical diffuser operation. Although the external shock or "bow wave" so generated does not necessarily reduce the diffuser pressure recovery severely, it spills air that would normally enter the engine and causes large additive-drag losses. With subcritical operation and no loss in pressure recovery, a small gain in thrust is obtainable over critical operation, but the specific impulse drops markedly. In addition to inefficient operation,

subcritical operation often results in instability of flow or "buzzing," which can, in severe cases, even blow out the combustor flame or damage the diffuser structure. In general, then, subcritical operation is undesirable.

For speeds less than design, best engine performance is also generally obtained with the value of  $\tau$  chosen to give critical diffuser operation. However, as flight speed is reduced, the value of M<sub>2</sub> for critical operation is raised.

The off-design performance of several engines designed for efficient cruising at a flight Mach number of 3.5 and incorporating various types of geometry variation is shown in figure 16 as a function of flight Mach number. Performance is shown for the engines operating at their maximum thrust condition. Also included are data for critical operation of a fixed-geometry engine obtained by cross-plotting the peaks of the curves from figure 15. The performance of an engine with both continuously variable inlet diffuser and exit nozzle is obtained with a wide-open exhaust nozzle and a stoichiometric fuel-air ratio. Extremely large penalties in thrust are suffered with the fixed-geometry engine, with a thrust at flight Mach number 2.5 of only 15 percent of that available from an engine equipped with a continuously variable inlet and outlet. These large thrust losses are mainly due to the necessity of reducing  $\tau$  to prevent subcritical operation. The ability to burn more fuel without being forced into the subcritical region explains why the continuously variable engine can produce more thrust than the fixed-geometry engine even at the design Mach number of 3.5.

Equipping an engine with either a movable-spike inlet or a variablearea exit nozzle, both of which are currently feasible, results in considerable gain over fixed-geometry engine performance. With a movablespike inlet, the spike is translated axially so that all air spillage occurs behind an oblique shock. The flow behind the oblique shock remains supersonic, and the additive drag is not as severe as in the case of a bow wave. This spillage permits  $\tau$  to be increased without causing subcritical operation. Thrust increases over the fixed configuration of 50 to 100 percent are possible, but the specific impulse is very low.

Thrust levels approaching the continuously variable case with about the same specific impulse can be achieved with an engine having a fixed inlet and a movable-plug nozzle. Although the nozzle throat area is variable, the nozzle-exit diameter is fixed and the nozzle expansion ratio cannot be independently chosen. At a flight Mach number of 2.5, the thrust is 74 percent that of the continuously variable engine.

#### CONCLUDING REMARKS

The calculated design-point performance of ram-jet engines using JP-4 fuel is presented for a wide range of engine total-temperature ratios and combustor-inlet Mach numbers for flight Mach numbers of 1.5 to 4.0. The results, which include engine thrust, drag, fuel consumption, and area ratios, are given in both graphical and tabular form. Maximum engine specific impulse (including nacelle drag) is approximately 1600 to 1700 pound-seconds per pound and occurs at a flight Mach number of about 2.5 to 3.0. Over-all engine efficiency, however, continues to increase to a flight Mach number of 4.0.

Calculations are also presented which indicate the sensitivity of the design-point results to changes in diffuser pressure recovery, flameholder pressure loss, combustion efficiency, fuel type, nozzle expansion ratio, nozzle velocity coefficient, nozzle jet-deflection angle, and altitude. Significant gains in both thrust coefficient and specific impulse may be achieved by improving the diffuser pressure recovery. However, presently available inlet designs that provide high recovery also have high cowl pressure drags which largely offset this potential gain. Changes in flameholder pressure loss have only small effects on engine performance. This factor may, however, influence combustor efficiency and the resulting range. Engine performance is very sensitive to changes in nozzle performance, a 1-percent variation in velocity coefficient often producing a 3-percent variation in engine thrust and specific impulse. Some underexpansion of the exhaust gases is desirable to reduce nacelle drag whenever the nozzle-exit diameter exceeds that of the combustion chamber.

Satisfactory off-design operation of a ram-jet engine is not possible with a fixed-geometry configuration. Somewhat better thrust can be obtained with the added complication of a translating-spike diffuser, although the specific impulse is poorer. Use of a movable plug to vary the throat area of the nozzle yields both thrust and specific impulse approaching those of a continuously variable-geometry engine. In considering engines designed for good cruise performance at flight Mach number 3.5 but operating at flight Mach number 2.5, the maximum thrusts are 15, 37, and 74 percent of that available with continuously variable geometry for engines with fixed-geometry, translating-spike diffuser, and movable-plug nozzle, respectively.

Lewis Flight Propulsion Laboratory National Advisory Committee for Aeronautics Cleveland, Ohio, April 25, 1956

#### APPENDIX A

#### SYMBOLS

The following symbols are used in this report:

A area, sq ft

- $A_{m}$  diffuser capture area  $A_{1}$  or combustion-chamber area  $A_{3}$ , whichever is larger, sq ft
- $C_{D}$  nacelle drag coefficient,  $D/q_{\Omega}A_{m}$
- $C_{F}$  net-thrust coefficient,  $F/q_{O}A_{m}$
- $c_{\rm T}$   $\,$  propulsive thrust coefficient,  $c_{\rm F}$   $c_{\rm D}$

 $C_{vr}$  nozzle velocity coefficient

D drag, lb

E over-all engine efficiency,  $(F - D)V_{0}/JHw_{r}$ 

F net thrust,  $m_6 V_6 - m_0 V_0 + A_6 (p_6 - p_0)$ , lb

f/a fuel-air ratio

H lower heating value of fuel, Btu/lb

I fuel specific impulse, (F - D)/w<sub>f</sub>, lb-sec/lb

 $I_F$  fuel specific impulse not including drag,  $F/w_f$ , lb-sec/lb

J mechanical equivalent of heat, 778 ft-lb/Btu

M Mach number

m mass-flow rate, slugs/sec

P total pressure, lb/sq ft

p static pressure, lb/sq ft q incompressible dynamic pressure,  $\rho V^2/2$ , lb/sq ft

R gas constant, 53.4 ft-lb/(lb)( $^{O}$ R)

T total temperature, <sup>O</sup>R

```
t static temperature, <sup>O</sup>R
```

```
V velocity, ft/sec
```

```
w<sub>f</sub> fuel-flow rate, lb/sec
```

 $\gamma$   $% \gamma$  ratio of specific heat at constant pressure to specific heat at constant volume

```
\eta_c combustion efficiency, w_{f,id}/w_{f,ac}
```

- $\lambda$  jet-deflection angle, deg
- ρ density, lb/cu ft
- $\tau$  engine total-temperature ratio,  $T_{4}/T_{3}$

Subscripts:

- ac actual
- ef effective
- fr friction
- id ideal
- nom nominal
- v vertical
- 0 free stream
- 1 diffuser inlet
- -2 combustion-chamber inlet (upstream of flameholder)
- 3 combustion-chamber inlet (downstream of flameholder)
- 4 combustion-chamber exit

5 nozzle throat

6 . nozzle exit

#### APPENDIX B

#### THERMODYNAMIC ASSUMPTIONS

Assigning correct gas properties and maintaining high computational accuracy are very important in any ram-jet engine analysis, because small changes in the calculated jet thrust may be magnified 3 or 4 times in the net propulsive thrust. Specification of the gas properties involves realistic choice of  $\gamma$ , R, and  $\tau$  as functions of temperature, fuel-air ratio, and pressure (if there is appreciable dissociation).

Data for octane (ref. 2), which include dissociation effects, were converted to JP-4 and used in constructing figure 3, which gives  $\tau$  as a function of  $M_0$  and f/a for an ambient temperature of  $392^{\circ}$  R. Similar curves were constructed for altitudes under the tropopause where the ambient temperature is different from 392° R. The very high temperatures plus the changes of composition due to burning cause the  $\gamma$  of the combustion gases to vary appreciably from 1.40 if equilibrium is reached. These equilibrium values, as a function of temperature and f/a and for a pressure of 1 atmosphere, were obtained from reference 9, which includes a very appreciable effect of dissociation. Molecular equilibrium is not necessarily maintained during the expansion of the gas through the nozzle. However, considerations of heat-capacity lag and chemical-reaction rates indicated that the process is probably closer to equilibrium than to "frozen" conditions. After trying several different methods, it was found that specifying an effective  $\gamma$  for the nozzle by

 $\gamma_{\rm ef}=\frac{1}{2}~(\gamma_4~+\gamma_6)$ 

gave best results as checked by equilibrium calculations using references 10 and 11. The deviations in net thrust were generally found to be less than 3 percent. According to reference 9, this means of specifying  $\gamma_{\rm ef}$  is also best for use in the isentropic equation

$$\frac{t}{T} = \left(\frac{p}{P}\right)^{\frac{\gamma-1}{\gamma}}$$

The value of R for the airstream was taken as  $53.4 \text{ ft-lb/(lb)}(^{O}\text{R})$ . The same value was used for the exhaust gas with small error (ref. 12).

#### APPENDIX C

#### ENGINE DRAG

The engine thrust is defined in terms of the total-momentum changes occurring between the free-stream tube ahead of the engine and the exhaust at the end of the engine. The drag must, therefore, include all the external forces acting on the stream tube and engine between the same two points. These forces are composed of pressure forces acting perpendicular to the stream tube and engine, and a friction force acting parallel to the engine nacelle due to the viscosity of the air. The pressure (or wave) drag may be further broken down into the part acting directly on the nacelle and the additional, imaginary part acting on the stream tube because of the way the thrust was defined. The latter force is termed additive drag, and was calculated by the method of reference 13.

The nacelle friction drag was calculated from the following equation, which is based on the flat-plate formula of reference 14:

$$C_{D,fr} = \frac{A_{W}}{A_{3}} \frac{0.0306 \text{ K}}{\text{Re}^{1/7} \left(1 + \frac{\gamma - 1}{4} \text{ M}_{0}^{2}\right)^{5/7}}$$

where  $A_W$  is nacelle skin area, K is a shape factor taken as 1.05 for a cylindrical nacelle, and the Reynolds number Re is based on free-stream conditions with a nominal length of 30 feet and a nominal altitude of 70,000 feet.

The nacelle pressure drag was obtained from the linearized theory from reference 15. For the low-speed cases when the exit area was smaller than combustion-chamber area, data for boattail drag for a 7.04<sup>o</sup> cone were used from the same source. The diffuser cowl was assumed conical, with no added pressure drag incurred from a curved lip.

The engine was assumed to have a fineness ratio (length divided by combustion-chamber diam.) of 9, the diffuser being nominally 4, combustion chamber 3, and nozzle 2. The appearance of the engine as a

function of flight speed is as shown in the following sketch (not to scale):



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#### TABLE I. - DESIGN-POINT RAM-JET ENGINE PERFORMANCE

#### WITH SINGLE-CONE DIFFUSER

Flight Mach number, M <sub>O</sub>											
	· · · · · · · · · · · · · · · · · · ·		1.5			2.0					
	(	Combu	stion-	chamber	r-inlet	Mach number, M <sub>2</sub> = 0.150					
$A_1/A_3 = 0.287$						$A_1/A_3 = 0.382$					,
τ	c <sub>T</sub>	I	° <sub>D</sub>	<sup>A</sup> <sub>6</sub> ∕A <sub>3</sub>	$A_5/A_3$	τ	C <sub>T</sub>	Ϊ.	C <sub>D</sub>	A <sub>6</sub> /A <sub>3</sub>	A <sub>5</sub> /A <sub>3</sub>
2.0 3.0 4.0 5.0 6.0 7.0 7.32	0.023 .210 .383 .533 .698 .882 .945	152 907 1054 1080 1056 998 975	0.186 .175 .161 .143 .122 .109 .109	0.468 .585 .699 .812 .931 1.060 1.106	0.395 .499 .590 .690 .794 .909 .945	2.5 3.0 3.5 4.0 4.5 5.0 5.5 5.96	0.291 .428 .551 .670 .780 .880 .990 1.096	1274 1372 1400 1393 1360 1307 1227 1139	0.118 .009 .098 .086 .087 .088 .090 .092	0.750 .840 .925 1.005 1.085 1.174 1.275 1.380	0.450 .499 .548 .595 .643 .696 .751 .807
	(	Combus	stion-0	hamber	r-inlet	Mach n	number	, M <sub>2</sub> =	= 0.175	5	
	1	A1/A3	= 0.33	54				A <sub>1</sub> /A <sub>3</sub>	= 0.44	14	
2.0 3.0 4.0 5.0 a 6.0	0.055 .282 .471 .635 .780	418 1043 1139 1106 984	0.175 .158 .138 .113 .109	0.550 .694 .825 .970 1.124	0.465 .590 .713 .843 1.000	2.5 3.0 3.5 4.0 4.5 5.0 5.5 a_5.5 5.85	0.365 .524 .660 .780 .895 1.007 1.122 1.206	1426 1508 1488 1438 1369 1288 1197 1130	0.104 .086 .084 .085 .087 .089 .092 .094	0.874 .985 1.086 1.180 1.287 1.400 1.527 1.618	0.530 .593 .654 .720 .790 .863 .940 1.000
	(	Combu	stion-	ehambe:	r-inlet	Mach r	number	, M <sub>2</sub> =	= 0.200	)	
	I	A <sub>1</sub> /A <sub>3</sub>	= 0.3	79		$A_1/A_3 = 0.505$					
2.5 3.0 3.5 4.0 4.5 <b>a</b> 4.77	0.225 .344 .454 .550 .625 .625	996 1131 1177 1178 1136 1065	0.150 .137 .121 .103 .100 .101	0.726 .808 .896 .986 1.080 1.132	0.620 .697 .779 .865 .952 1.000	2.25 2.50 2.75 3.00 3.25 3.75 4.25 a <sup>4</sup> .60	0.347 .440 .520 .598 .672 .804 .927 1.006	1433 1498 1527 1519 1502 1448 1371 1312	0.091 .081 .082 .083 .084 .087 .090 .093	0.941 1.009 1.072 1.139 1.194 1.324 1.460 1.560	0.581 .620 .660 .700 .743 .832 .929 1.000
Combustion-chamber-inlet Mach number, M <sub>2</sub> = 0.225											
$A_1/A_3 = 0.424$							1	A <sub>1</sub> /A <sub>3</sub>	= 0.56	54	
2.50 2.75 3.00 3.25 3.50 <b>a</b> 3.80	0.266 .348 ·.400 .452 .499 .540	1079 1151 1180 1177 1144 1047	0.130 .122 .111 .099 .097 .099	0.835 .876 .931 .988 1.040 1.110	0.719 .766 .819 .870 .928 1.000	2.25 2.50 2.75 3.00 3.25 a.50 a.50 a.72	0.399 .488 .574 .657 .733 .801 .863	1469 1492 1497 1481 1457 1423 1377	0.081 .083 .084 .086 .087 .089 .091	1.078 1.152 1.226 1.302 1.378 1.456 1.530	0.675 .721 .770 .822 .879 .940 1.000

a Thermal choking

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#### TABLE I. - Continued. DESIGN-POINT RAM-JET ENGINE PERFORMANCE

Flight Mach number, M <sub>O</sub>											
2.5							3.0				
	(	Combus	stion-o	chamber	-inlet	Mach number, M <sub>2</sub> = 0.150					
	$A_1/A_3 = 0.505$						$A_1/A_3 = 0.626$				
τ	C <sub>T</sub>	I	CD	A <sub>6</sub> /A <sub>3</sub>	A <sub>5</sub> /A <sub>3</sub>	τ	с <sub>т</sub>	I	CD	A <sub>6</sub> ∕A <sub>3</sub>	A <sub>5</sub> /A <sub>3</sub>
2.0 2.5 3.0 3.5 4.0 4.5 4.80	0.284 .469 .638 .795 .960 1.132 1.250	1441 1555 1546 1510 1432 1329 1249	0.076 .072 .073 .074 .075 .077 .078	0.960 1.052 1.125 1.193 1.275 1.371 1.436	0.397 .453 .501 .552 .606 .661 .697	2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.96	0.390 .507 .620 .730 .834 .951 1.079 1.349	1522 1565 1566 1550 1516 1474 1419 1300	0.061 .062 .063 .064 .065 .066 .069 .073	1.1771.2351.2901.3441.4021.4661.5401.701	0.398 .429 .456 .481 .506 .537 .559 .619
	(	Combus	stion-	chambei	-inlet	Mach	number	, M <sub>2</sub> =	= 0.175	5	•
	1	A <sub>1</sub> /A <sub>3</sub>	= 0.58	36			1	A <sub>1</sub> /A <sub>3</sub>	= 0.72	27	
2.0 2.5 3.0 3.5 4.0 4.5 4.80	0.348 .554 .749 .934 1.125 1.302 1.420	1512 1594 1565 1508 1406 1299 1212	0.070 .071 .073 .075 .077 .079 .081	1.062 1.138 1.246 1.338 1.432 1.535 1.600	0.468 .534 .598 .665 .734 .810 .860	2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.96	0.458 .591 .722 .851 .972 1.105 1.249 1.546	$1537 \\ 1576 \\ 1574 \\ 1551 \\ 1515 \\ 1462 \\ 1402 \\ 1266$	0.058 .061 .063 .066 .067 .069 .072 .078	$1.305 \\ 1.370 \\ 1.430 \\ 1.499 \\ 1.567 \\ 1.644 \\ 1.732 \\ 1.942$	0.472 .507 .538 .571 .606 .641 .674 .747
	(	Combus	stion-	chambei	r-inlet	Mach	number	, M <sub>2</sub> =	= 0.200	)	
		A <sub>1</sub> /A <sub>3</sub>	= 0.6	56		$A_1/A_3 = 0.826$					
2.0 2.5 3.0 3.5 4.0 a 4.45	0.400 .630 .850 1.052 1.250 1.420	1537 1597 1566 1501 1396 1287	0.071 .072 .074 .076 .079 .082	1.158 1.262 1.363 1.470 1.589 1.710	0.545 .625 .706 .793 .888 1.000	2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.96	0.520 .657 .801 .953 1.091 1.239 1.390 1.692	1531 1561 1555 1533 1496 1444 1375 1220	0.065 .067 .068 .070 .072 .074 .076 .084	1.425 1.502 1.578 1.652 1.727 1.822 1.908 2.162	0.545 .590 .633 .673 .714 .763 .811 .918
	(	Combus	stion-	chambei	r-inlet	Mach	number	, M <sub>2</sub> =	= 0.225	5	
$A_1/A_3 = 0.745$							1	A <sub>1</sub> /A <sub>3</sub>	= 0.92	23	
2.00 2.25 2.50 2.75 3.00 <b>a</b> 3.25 <b>a</b> 3.66	0.439 .565 .689 .810 .920 1.028 1.201	1519 1556 1565 1555 1527 1487 1400	0.071 .073 .074 .075 .076 .077 .080	1.240 1.301 1.360 1.421 1.486 1.551 1.669	0.625 .675 .722 .775 .829 .897 1.000	2.00 2.25 2.50 2.75 3.00 3.25 <b>a</b> 3.58	0.589 .748 .900 1.052 1.197 1.351 1.584	1551 1556 1544 1513 1465 1410 1314	0.053 .055 .072 .074 .076 .078 .083	1.553 1.628 1.714 1.817 1.901 2.022 2.168	0.629 .680 .730 .787 .840 .901 1.000

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#### WITH SINGLE-CONE DIFFUSER

a Thermal choking

### TABLE I. - Concluded. DESIGN-POINT RAM-JET ENGINE PERFORMANCE

WITH	SINGLE-CONE	DIFFUSER
	OTHOTO-COULD	DILLOUM

Flight Mach number, M <sub>O</sub>											
		3.5			4.0						
	(	stion-	chambe:	r-inle	t Mach number, M <sub>2</sub> = 0.125						
$A_1/A_3 = 0.618$						$A_1/A_3 = 0.743$					
τ	C <sub>T</sub>	I	C <sub>D</sub>	A <sub>6</sub> /A <sub>3</sub>	A <sub>5</sub> /A <sub>3</sub>	τ	$^{C}\mathrm{T}$	I	c <sub>D</sub>	A <sub>6</sub> /A <sub>3</sub>	A <sub>5</sub> /A <sub>3</sub>
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.271 .388 .505 .628 .759 .900 1.059	1349 1411 1428 1422 1398 1353 1276	0.055 .056 .057 .058 .059 .062 .064	1.209 1.275 1.341 1.406 1.488 1.615 1.744	0.303 .329 .355 .376 .400 .426 .451	1.50 1.75 2.00 2.25 2.50 2.75	0.162 .334 .493 .654 .838 1.047	954 1255 1324 1334 1310 1218	0.047 .050 .052 .054 .058 .064	1.362 1.457 1.543 1.627 1.804 2.048	0.281 .308 .334 .356 .383 .412
· .	(	Combus	stion-	chamber	r-inlet	Mach	$\frac{\pi^{1}}{r_{3}} = 0.743$ $\frac{\tau}{r_{T}} \begin{bmatrix} I \\ C_{T} \end{bmatrix} \begin{bmatrix} C_{D} \\ A_{6}/A_{3} \end{bmatrix} \begin{bmatrix} A_{5}/A_{3} \\ A_{5}/A_{3} \end{bmatrix}$ $\frac{1.50}{0.162} \begin{bmatrix} 954 \\ 0.047 \\ 1.362 \\ 0.281 \\ 0.334 \end{bmatrix} \begin{bmatrix} 255 \\ 0.50 \\ 1.457 \\ 0.334 \\ 1255 \end{bmatrix} \begin{bmatrix} 0.021 \\ 0.281 \\ 0.383 \\ 0.52 \\ 1.543 \\ 0.58 \\ 1.804 \\ 0.64 \end{bmatrix} \begin{bmatrix} 0.281 \\ 0.383 \\ 0.64 \\ 2.048 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.64 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.64 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.64 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.64 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.64 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.64 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.383 \\ 0.412 \\ 0.58 \\ 0.48 \end{bmatrix} \begin{bmatrix} 0.383 \\ 0.399 \\ 0.57 \\ 0.213 \\ 0.592 \\ 0.55 \\ 0.243 \\ 0.592 \\ 0.55 \\ 0.591 \\ 0.592 \\ 0.55 \\ 0.591 \\ 0.244 \\ 0.75 \end{bmatrix} \begin{bmatrix} 0.213 \\ 0.403 \\ 0.63 \\ 0.63 \\ 0.63 \\ 0.63 \\ 0.65 \\ 0.71 \\ 0.2356 \\ 0.501 \\ 0.401 \end{bmatrix} \begin{bmatrix} 0.43 \\ 0.63 \\ 0.63 \\ 0.63 \\ 0.65 \\ 0.71 \\ 0.2356 \\ 0.501 \\ 0.401 \end{bmatrix} \begin{bmatrix} 0.43 \\ 0.43 \\ 0.63 \\ 0.63 \\ 0.63 \\ 0.65 \\ 0.75 \\ 0.244 \\ 0.75 \\ 0.244 \\ 0.35 \\ 0.055 \\ 0.750 \\ 0.401 \end{bmatrix} \begin{bmatrix} 0.43 \\ 0.43 \\ 0.43 \\ 0.63 \\ 0.63 \\ 0.63 \\ 0.65 \\ 0.75 \\ 0.401 \\ 0$				
		A <sub>1</sub> /A <sub>3</sub>	= 0.74	40	·		1	A <sub>1</sub> /A <sub>3</sub>	= 0.89	90	
1.75 2.00 2:25 2.50 2.75 3.00 3.25	0.341 .470 .617 .755 .908 1.076 1.255	1375 1441 1450 1442 1412 1360 1266	0.054 .056 .058 .060 .062 .066 .070	1.358 1.437 1.515 1.606 1.695 1.856 2.015	0.370 .401 .430 .459 .487 .519 .549	1.50 1.75 2.00 2.25 2.50 2.75	0.213 .403 .592 .784 1.001 1.254	1045 1263 1329 1329 1314 1217	0.049 .052 .055 .058 .063 .071	1.536 1.653 1.762 1.880 2.086 2.356	0.399 .373 .403 .435 .466 .501
	(	Combus	stion-o	chamber	-inlet	Mach :	number,	, M <sub>2</sub> =	0.175	5	
		A <sub>1</sub> /A <sub>3</sub>	= 0.85	58		$A_1/A_3 = 1.032$					
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.389 .553 .720 .887 1.060 1.240 1.440	1410 1452 1462 1450 1415 1353 1250	0.058 .060 .062 .064 .067 .072 .077	1.524 1.609 1.691 1.805 1.912 2.104 2:284	0.438 .474 .507 .544 .578 .620 .662	1.50 1.75 2.00 2.25 2.50 2.75	0.244 .467 .687 .906 1.158 1.449	1035 1263 1329 1335 1310 1213	0.055 .057 .061 .064 .069 .078	1.730 1.844 1.986 2.125 2.352 2.680	0.401 .438 .477 .513 .551 .598
Combustion-chamber-inlet Mach number, M <sub>2</sub> = 0.200								-			
$A_1/A_3 = 0.976$											
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.428 .610 .995 1.195 1.400 1.634	1375 1420 1436 1426 1394 1340 1240	0.063 .065 .067 .069 .072 .077 .084	1.665 1.768 1.871 1.991 2.118 2.311 2.560	0.506 .551 .594 .638 .683 .732 .790			· · ·	· · · · · · · · · · · · · · · · · · ·		

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#### TWO-CONE DIFFUSER

[Note: Values of  $C_D,\,A_6/A_3,\,\text{and}\,\,A_5/A_3$  are assumed to be the same as those in table I.]

Flight Mach number, M <sub>O</sub>										
	2.0			2.5			3.0			
Combustion-chamber-inlet Mach number, $M_2 = 0.150$										
Al/A	3 = 0.3	92	A <sub>l</sub> /A	3 = 0.5	57	A <sub>l</sub> /A	3 = 0.7	58		
τ	$c_{\mathrm{T}}$	I	τ	τ C <sub>T</sub> I			C <sub>T</sub>	I		
2.5 3.0 3.5 4.0 4.5 5.0 5.5 5.96	0.309 .451 .577 .700 .814 .918 1.032 1.141	1319 1406 1429 1417 1382 1327 1245 1155	2.0 2.5 3.0 3.5 4.0 4.5 4.80	0.344 .344 .550 .738 .913 1.097 1.289	1581 1652 1621 1571 1483 1372 1287	2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.96	0.525 .668 .810 .943 1.071 1.215 1.373 1.706	1690 1704 1684 1652 1607 1555 1491 1358		
C	ombusti	on-chai	nber-in	let Mac	h numb	er, M <sub>2</sub>	= 0.175			
A <sub>l</sub> /A	$A_1/A_3 = 0.456$ $A_1/A_3 = 0$					A <sub>l</sub> /A	3 = 0.8	80		
2.5 3.0 3.5 4.0 4.5 5.0 5.5 <b>a</b> 5.85	0.386 .550 .691 .815 .934 1.050 1.170 1.257	1469 1541 1516 1462 1391 1308 1215 1146	2.0 2.5 3.0 3.5 4.0 4.5 4.80	0.416 .645 .863 1.069 1.283 1.480 1.612	1639 1683 1635 1565 1453 1339 1248	2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.96	0.611 .774 .736 1.095 1.244 1.408 1.586 1.954	1692 1705 1684 1648 1601 1545 1470 1321		
C	ombusti	on-chai	nber-in	let Mac	h numb	er, M <sub>2</sub>	= 0.200			
A <sub>1</sub> /A	3 = 0.5	19	A <sub>l</sub> /A	3 = 0.7	35	A <sub>1</sub> /A	3 = 1.1	00		
2.25 2.50 2.75 3.00 3.25 3.75 4.25 <b>a</b> 4.60	0.368 .464 .547 .627 .704 .841 .969 1.051	1479 1538 1563 1552 1532 1474 1395 1334	2.0 2.5 3.0 3.5 4.0 a4.45	0.476 .761 .977 1.203 1.424 1.615	1658 1678 1632 1556 1442 1327	2.00 2.25 2.50 2.75 3.00 3.25 3.50 3.96	0.691 .860 1.037 1.224 1.394 1.577 1.763 2.139	1680 1687 1663 1626 1579 1518 1440 1274		
C	Combustion-chamber-inlet Mach number, M <sub>2</sub> = 0.225									
A <sub>1</sub> /A	3 = 0.5	79	A <sub>l</sub> /A	3 = 0.8	22	A <sub>1</sub> /A	3 = 1.1	18		
2.25 2.50 2.75 3.00 3.25 3.50 <sup>a</sup> 3.72	0.422 .515 .604 .690 .768 .839 .893	1514 1532 1533 1514 1487 1452 1388	2.00 2.25 2.50 2.75 3.00 3.25 a3.66	0.521 .661 .800 .935 1.058 1.178 1.372	1633 1651 1647 1627 1542 1545 1450	2.00 2.25 2.50 2.75 3.00 3.25 <sup>a</sup> 3.58	0.695 .870 1.040 1:208 1.368 1.539 1.796	1688 1670 1644 1604 1546 1482 1376		

<sup>a</sup>Thermal choking.

TABLE II. - Concluded. DESIGN-POINT RAM-JET

ENGINE PERFORMANCE WITH TWO-CONE DIFFUSER

<sup>[</sup>Note: Values of  $C_D$ ,  $A_6/A_3$ , and  $A_5/A_3$ are assumed to be the same as those in table I.]

Flight Mach number, M <sub>O</sub>									
	3.5		4.0						
Combust	ion-chamb	er-inlet	Mach number, $M_2 = 0.125$						
Al	$/A_3 = 0.8$	34	$A_1/A_3 = 1.048$						
τ	CT	I	τ	C <sub>T</sub>	I				
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.435 .595 .756 .926 1.106 1.303 1.523	1602 1604 1584 1552 1509 1451 1359	1.50 1.75 2.00 2.25 2.50 2.75	0.284 .520 .738 .959 1.214 1.507	1243 1452 1472 1452 1452 1410 1302				
Combust	ion-chamb	er-inlet	Mach nu	mber, M <sub>2</sub>	= 0.150				
Al	$/A_3 = 0.9$	99	Al	/A <sub>3</sub> = 1.2	56				
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.535 .713 .915 1.106 1.317 1.551 1.801	1597 1619 1593 1564 1517 1452 1346	1.50 1.75 2.00 2.25 2.50 2.75	0.300 .518 .735 .955 1.206 1.501	1311 1445 1468 1441 1409 1296				
Combust	ion-chamb	er-inlet	Mach nu	mber, M <sub>2</sub>	= 0.175				
A <sub>l</sub>	/A <sub>3</sub> = 1.1	58	$A_1/A_3 = 1.456$						
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.525 .720 .918 1.117 1.323 1.542 1.783	1631 1621 1598 1566 1515 1443 1327	1.50 1.75 2.00 2.25 2.50 2.75	0.304 .530 .754 .978 1.237 1.538	1287 1432 1459 1440 1399 1288				
Combus inlet M	tion-cham Mach num 2 = 0.200	ber,		,					
Al	/A <sub>3</sub> = 1.3	18							
1.75 2.00 2.25 2.50 2.75 3.00 3.25	0.507 .697 .895 1.099 1.309 1.526 1.775	1589 1584 1567 1538 1490 1426 1315	- - -						



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Figure 2. - Effect of flight Mach number on critical diffuser pressure recovery.





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Combustion-chamber total-temperature ratio,  $\tau$ 





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(b) Flight Mach number, 2.0.

Figure 4. - Continued. Design-point performance of ram-jet engine with single-cone diffuser.



(c) Flight Mach number, 2.5.







Figure 4. - Continued. Design-point performance of ram-jet engine with single-cone diffuser.

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Figure 5. - Effect of flight Mach number on design-point performance of ram-jet engine. Engine total-temperature ratio chosen for maximum efficiency. . • ÷

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Figure 6. - Effect of combustion-chamber-inlet Mach number on ram-jet engine performance.



(b) Flight Mach number, 3.5.



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Figure 8. - Effect of diffuser pressure recovery and engine drag coefficient on ram-jet engine performance. Flight Mach number, 3.5; combustion-chamber-inlet Mach number, 0.200; engine total-temperature ratio, 2.50.



Figure 9. - Effect of flameholder pressure loss on ram-jet engine performance. Combustion-chamber-inlet Mach number, 0.200; combustion efficiency, 0.90. (Specific impulse is affected in same proportion as thrust.)



Figure 10. - Comparison between performance of engines using pentaborane and JP-4 fuel. Flight Mach number, 3.5; combustion-chamber-inlet Mach number, 0.200.





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Figure 15. - Off-design performance of fixed-geometry ram-jet engine designed for flight Mach number of 3.5, combustion-chamber-inlet Mach number of 0.200, and engine total-temperature ratio of 2.25. Combustion efficiency, 0.87; ratio of specific heats for exhaust gases, 1.30.



Figure 16. - Off-design performance of various fixed- and variable-geometry ram-jet engines operating at maximum thrust. Engines designed for flight Mach number of 3.5, combustion-chamber-inlet Mach number of 0.200, and engine total-temperature ratio of 2.50. Combustion efficiency, 0.87; ratio of specific heats for exhaust gases, 1.30.