# RESEARCH MEMORANDUM 

LARGE-SCALE WIND-TUNNEL TESTS OF AN AIRPLANE MODEL
WITH A $45^{\circ}$ SWEPTBACK WING OF ASPECT RATIO 2.8
EMPLOYING HIGH-VELOCITY BLOWING OVER THE
LEADING- AND TRAILING-EDGE FLAPS
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SUMMARY

An investigation was conducted to determine the longitudinal characteristics of an airplane model with a thin, highly swept and tapered wing of low aspect ratio equipped with plain leading-edge flaps in conjunction with blowing-type boundary-layer control applied to the flap radius. In these tests blowing-type boundary-layer control was also applied to a plain trailing-edge flap deflected $60^{\circ}$. Several leadingedge configurations and boundary-layer control system variables were investigated.

It was found that leading-edge-blowing boundary-layer control significantly increased maximum lift and improved stability near maximum lift. Lift and stability generally were sensitive to spanwise variations of leading-edge flap deflection and extent of blowing boundary-layer control.

Blowing momentum coefficient requirements for the leading-edge flaps were independent of nozzle height and free-stream airspeed. Increasing angle of attack increased critical momentum coefficient values.

Comparison of the results of this investigation with the results from another model configuration with the same wing and area-suction boundarylayer control showed blowing-type boundary-layer control produced larger lift increments with approximately the same boundary-layer control air flow.

Estimations of low-speed performance indicate leading-edge boundarylayer control reduced approach speed 20 percent and take-off ground roll and distance to 50 -foot altitude by about 40 percent.

## INIRODUCTION

The use of thin, low-aspect-ratio, sweptback wings on modern aircraft seriously limits the low-speed maximum lift and longitudinal stability. A number of studies have been made of the effectiveness of boundary-layer control on wing flaps as a means of improving the lowspeed characteristics of such airplanes. Some of the results obtained are presented in references 1 through 6. Results of tests of a $35^{\circ}$ swept wing with area suction and blowing applied to the trailing-edge flaps are reported in references 1 and 2, respectively. References 3 and 4 report results of blowing boundary-layer control applied to trailing-edge and leading-edge flaps on a $49^{\circ}$ swept wing. A study has also been made on a wing having $45^{\circ}$ of sweep, an aspect ratio of 2.8 , a taper ratio of 0.17 , and a thickness ratio of 0.05 . Results of tests with area-suction trailing-edge flaps are presented in reference 5. To control leading-edge air-flow separation, area suction was effectively applied at the radius of the leading-edge flap as reported in reference 6.

The present investigation was conducted to examine the effectiveness of blowing boundary-layer control applied to the hinge-line radius of the leading-edge flap on the latter wing plan form. For this investigation, the emphasis was placed on increasing maximum lift and retaining stability to maximum lift. Longitudinal characteristics were determined for two spanwise extents of trailing-edge flaps, three spanwise extents of leading-edge flap deflection, and various amounts of boundary-layer control. Corresponding leading-edge and trailing-edge boundary-layer control jet-momentum requirements were determined. An estimation of the effect of leading-edge flap boundary-layer control on low-speed performance is included. Results from a two-dimensional investigation conducted in a 2- by 5 -foot wind tunnel are included to supplement the three-dimensional leading-edge jet-momentum requirement data.

## NOTATION

b wing span, ft
BLC boundary-layer control
c chord, measured parallel to the plane of symmetry, ft
c' chord, measured normal to the wing leading edge, ft
$\overline{\mathrm{c}} \quad$ mean aerodynamic chord, $\frac{2}{\mathrm{~S}} \int_{0}^{\mathrm{b} / 2} \mathrm{c}^{2} d y$, ft
CD drag coefficient, $\frac{\text { drag }}{q_{\infty} S}$
CL lift coefficient, $\frac{\text { lift }}{q_{0 \infty} S}$
$\triangle C_{L} \quad$ increment in lift coefficient due to leading-edge boundarylayer control or trailing-edge flap deflection
$\triangle C_{\text {IS }} \quad$ increment in lift coefficient for tip stall
$\mathrm{C}_{\mathrm{m}} \quad$ pitching-moment coefficient computed about $0.25 \bar{c}$, pitching moment
$9_{\infty} S \bar{c}$
$C_{Q} \quad$ flow coefficient, $\frac{Q}{U_{\infty} S}$
$C_{\mu} \quad$ momentum coefficient, $\frac{W_{j} / g}{q_{\infty} S} V_{j}$
d. distance from the engine thrust line to the moment center, ft

D drag, lb
$F_{G} \quad$ gross thrust from engine, $\frac{W_{e} V_{T P}}{g}$, lb
$F_{n} \quad$ net thrust from engine, $\frac{W_{e} V_{T P}}{g}-\frac{W_{e} U_{\infty}}{g}, l b$
g acceleration of gravity, $32.2 \mathrm{ft} / \mathrm{sec}^{2}$
h nozzle height, inches, or altitude of the airplane, ft
L lift, Ib
L.E. leading edge

2 distance parallel to the plane of symmetry between the moment center and the effective turning point of the engine air at the inlet, ft
$\tau_{t}$ distance from the quarter-chord point of the wing mean aerodynamic chord to the quarter chord of the horizontal-tail mean aerodynamic chord, ft
p
$p_{t}$

V velocity, knots
jet velocity assuming isentropic expansion,

$$
\sqrt{\frac{2 \gamma}{\gamma-1} g R_{t_{d}}\left[1-\left(\frac{p_{\infty}}{p_{t}}\right)^{\frac{\gamma-1}{\gamma}}\right]}, \mathrm{ft} / \mathrm{sec}
$$

static pressure, lb/sq ft
total pressure, lb/sq ft
free-stream dynamic pressure, lb/sq ft
volume flow of boundary-layer-control air under standard conditions, cu ft/sec
Reynolds number, $\frac{U_{\infty} \bar{c}}{v}$, or gas constant for air, $53.3 \mathrm{ft}-1 \mathrm{~b} / \mathrm{lb}-{ }^{\circ} \mathrm{R}$ wing area without chord extension added, sq ft, or total takeoff distance, ft
take-off ground roll, ft
air distance over a 50-foot obstacle, ft
time, sec
total temperature, ${ }^{O_{R}}$
trailing edge
free-stream velocity, ft/sec
velocity at exit of engine tail pipe, ft/sec
gross weight, lb , or weight rate of $\mathrm{flow}, \mathrm{lb} / \mathrm{sec}$
streamwise distance along airfoil chord, ft
spanwise distance perpendicular to the plane of symmetry, ft
perpendicular distance above the extended wing chord plane, ft angle of attack of fuselage reference line, deg
dihedral, deg
$\delta$
Te leading edge
$\max$

maximum
te
tou
TP
radians

BP engine bleed port
critical
flap duct
engine
on the ground
flap jet
leading edge
tail
trailing edge
take-off
uncorrected
engine tail pipe
free stream
flap deflection measured normal to the flap hinge line, deg
kinematic viscosity of air, ftz/sec
pump efficiency, or wing semispan station, $\frac{2 y}{b}$
ratio of specific heats, 1.4 for air, and flight path angle,
angular distance between flap nozzle and the perpendicular from
the flap hinge line to the airfoil chord line (fig. 6), deg
rolling friction coefficient

## Subscripts

stall with power on, or point of initial separation

## MODEL AND APPARATUS

Figure 1 is a photograph of the model mounted in the Ames 40-by 80 -foot wind tunnel. A drawing of the model is shown in figure 2, and additional geometric data are given in table I.

## Wing

Plan form and airfoil section. - The basic wing had a quarter-chord sweep of $45^{\circ}$, aspect ratio of 2.8 , and a taper ratio of 0.17 . In addition, the basic wing had a lo-percent chord extension, measured parallel to the plane of symmetry, from $\eta=0.7$ to $l .0$. This configuration was used for the entire test program and is called the basic configuration. Airfoil sections parallel to the model plane of symmetry were modified NACA 0005-63 sections, coordinates of which are listed in table II.

Leading-edge flap. - The leading-edge flap was divided into three sections with flap breaks parallel to the plane of symmetry. The flap sections extended from $\eta=0.15$ to $0.4,0.4$ to 0.7 , and 0.7 to 1.0 and will be referred to hereinafter as root, intermediate, and tip leading-edge flap sections, respectively. Listing of the leading-edge flap deflections will follow the same order. For a typical case, $\delta_{\text {le }}=30,60,60$ indicates the root flap section was deflected $30^{\circ}$ and the intermediate and tip sections were deflected $60^{\circ}$.

Trailing-edge flap. - Small- and large-span trailing-edge flaps were used during the tests. The small-span flap extended from $\eta=0.21$ to 0.46 and had a constant 25 -percent wing chord, measured parallel to the plane of symmetry. The large-span flap was formed by combining the smallspan flap with one which extended from $\eta=0.46$ to 0.66 and also had a constant 25 -percent chord. Both flaps rotated about a hinge near the wing lower surface.

Blowing nozzles.- A typical cross section of the leading-edge flap nozzle is shown in figure 3(a). The nozzle was a slit located on the hinge-line radius of the flap and extended from $\eta=0.15$ to 1.0 . The chordwise nozzle position of $35.5^{\circ}$ as shown in figure 3 was maintained throughout the three-dimensional tests. During the investigation, two nozzle heights on the tip leading-edge flap were used. A nozzle height of 0.010 inch on both the intermediate and tip flap sections will be referred to hereinafter as leading-edge flap nozzle A, and a nozzle height of 0.050 inch on the tip section with 0.010 inch on the intermediate section will be referred to as nozzle $B$.

A trailing-edge flap nozzle cross section is shown in figure 3(b). The nozzle extended from $\eta=0.21$ to 0.66 . A chordwise nozzle position of $22.5^{\circ}$ with a nozzle height of 0.020 inch was maintained throughout the investigation.

Leading-edge modifications. - Changes in leading-edge contour as shown in figure 4 were made by increasing the leading-edge radius to approximately 0.9 -percent $c^{\prime}$ and adding a small amount of leadingedge camber. The coordinates for the L.E. modifications are listed in table III. Two spanwise extents of modified leading edge extending from $\eta=0.4$ to 1.0 and 0.7 to 1.0 were tested.

Tail

A swept horizontal tail (fig. 2) was used and was installed with its root at approximately 0.31 of the wing semispan above the extended wing chord plane. The tail was drooped at $20^{\circ}$ about a line parallel to the plane of symmetry and the extended wing chord plane. Except where specified, both horizontal and vertical tails were on the model throughout the tests.

## Fuselage and Engines

The wing was located approximately 0.13 of the wing semispan below the fuselage center line. The fuselage coordinates are listed in table IV. Compressor bleed from two J-34 turbojet engines, installed side by side inside the fuselage, supplied the blowing boundary-layer control air. The left engine supplied air to the leading-edge flaps; the right engine supplied the trailing-edge flaps. Engine bleed ports were enlarged to allow larger quantities of air to be bled from the compressor.

## Boundary-Layer-Control Air Ducting

Ducting to the leading- and trailing-edge flaps is shown in figure 5. The amount of bleed air delivered to the root, intermediate, and tip leading-edge flap sections, and the inboard and outboard portion of the trailing-edge flaps was controlled by butterfly valves in each duct. Total- and static-pressures and temperature measurements to obtain total weight rate of flow to the leading-edge flaps were taken at station 1 in figure 5. For the inboard and outboard portions of the trailing-edge flaps, measurements to obtain weight rate of flow were taken at stations 2
and 3, respectively. Total-pressure and temperature measurements used for calculating jet-momentum flow were taken at each of the entrances to the flap ducts (stations 4 through 13 in fig. 5).

## Two-Dimensional Airfoil

The airfoil, tested in a 2- by 5-foot wind tunnel, had a 2-foot chord section and a leading-edge flap hinged at 13.55 -percent chord as shown in figure 6. Coordinates of the airfoil are also given in figure 6. The flap had a blowing nozzle which could be rotated around the hinge-line radius of the flap. The airfoil extended across the 2 -foot width of the wind tunnel with pressure orifices located on the upper and lower surfaces of the airfoil center line.

TESTING AND PROCEDURE
Three-Dimensional Tests

Force and moment data were obtained for the three-dimensional model through an angle-of-attack range of $0^{\circ}$ to $33^{\circ}$. Model configurations for which force data were obtained are listed in table $V$ which may also be used as an index to the basic data. All tests, except for the brief tests at a higher free-stream velocity ( $U_{\infty}=159 \mathrm{ft} / \mathrm{sec}, \mathrm{R}=11.1 \times 10^{6}$ ) with variable $C_{\mu}$ and the two-dimensional tests, were made at $U_{\infty}=112 \mathrm{ft} / \mathrm{sec}$ corresponding to a Reynolds number of $8 \cdot 3 \times 10^{6}$. This Reynolds number corresponded to a free-stream dynamic pressure of 15 pounds per square foot.

Tests at variable angle of attack and constant $C_{\mu}$. - A major part of the data was obtained with the plain leading-edge flap with and without blowing and with the trailing-edge flap deflected $60^{\circ}$ with and without blowing. Various combinations of leading-edge flap deflections, as shown in table $V$, were tested. The modified leading edge was tested with the leading-edge flap deflected with blowing and with the small-span trailing-edge flap with blowing. Since this report is concerned primarily with the study of the wing leading edge, a constant Cute well above that required for flow attachment on the trailing-edge flap was maintained when blowing was utilized on the flap.

Tests with variable $C_{\mu}$ at constant angle of attack.- Momentum coefficient was varied on the intermediate and tip leading-edge flap sections either together or independently to determine its effect on the longitudinal characteristics of the model with the following variables: (1) free-stream velocity, and (2) nozzle heights of 0.010 and 0.050 inch
on the tip flap section. For the small- and large-span trailing-edge flaps, C $\mu$ te was varied at several angles of attack with the flap deflected $60^{\circ}$.

Two-Dimensional Tests

Two-dimensional tests in the 2- by 5-foot wind tunnel were used to investigate the effect of the chordwise location of an $h / c=0.00033$ leading-edge nozzle on flow requirements. The nozzle location was varied from 60 to 660 with respect to the reference line (fig. 6) and with the flap deflected $60^{\circ}$. Tests were conducted at $\alpha=36^{\circ}$ with a free-stream dynamic pressure of 20 pounds per square foot, corresponding to a Reynolds number of $1.6 \times 10^{6}$ based on a 2 -foot chord.

Measurement of Engine Thrust

The gross thrust of the engine (for a given configuration a function of $p_{t T P}\left(p_{\infty}\right)$ used for thrust corrections to the force data was obtained by calibration of the tail-pipe total-pressure measurement instrumentation with the wind-tunnel balance system. Engine weight rate of flow was obtained from the total-pressure and temperature measurements of the tail-pipe nozzles by means of the following equation:

$$
W_{e}=\frac{F_{G} g}{V_{T P}}
$$

CORRECTIONS TO DATA
Effects of Wind-Tunnel Walls

The following corrections for the effects of wind-tunnel-wall interference were made:

$$
\begin{aligned}
\alpha & =\alpha_{u}+0.75 C_{L} \\
C_{D} & =C_{D_{u}}+0.013 C_{L}{ }^{2} \\
C_{m} & =C_{m_{u}}+0.005 C_{L}
\end{aligned}
$$

## Effects of Engine Operation

Force data from the wind-tunnel balance system were corrected for the effects of engine thrust as follows:

$$
\begin{aligned}
& C_{L}=\frac{\text { total lift }}{q_{\infty} S}-\frac{F_{G} \sin \alpha}{q_{\infty} S} \\
& C_{D}=\frac{\text { total drag }}{q_{\infty} S}+\left(\frac{F_{G}}{q_{\infty} S} \cos \alpha-\frac{W_{e} U_{\infty}}{g q_{\infty} S}\right) \\
& C_{m}=\frac{\text { total moment }}{q_{\infty} S \bar{c}}+\left[\frac{F_{G}}{q_{\infty} S} \frac{\alpha}{c}-\frac{W_{e} U_{\infty}}{g q_{\infty \infty} S \bar{c}}(2 \sin \alpha+\alpha \cos \alpha)\right]
\end{aligned}
$$

These corrections include the force due to turning the engine air at the inlets when the airplane model is at an angle of attack.

RESULTS

Configurations for which the force data are presented herein are listed in table $V$. Three-component force data showing the longitudinal characteristics of the model with the small-span flap are presented in figures 7 through 10. Figure 7 presents a summary of the effect of leading-edge flap deflection and BLC on the longitudinal characteristics of the model. More detailed data are presented in figure 8. Figure 9 presents results showing the effects of spanwise extent of blowing boundary-layer control, and figure 10, the effects of the modified leading edge. Results for two spanwise extents of trailing-edge flap are shown in figure 11.

Data showing the influence of jet momentum on lift are presented in figures 12 through 17. Results included are the effects on leading-edge BLC requirements of nozzle height, free-stream velocity, angle of attack, and blowing nozzle position on the leading-edge flap radius. Trailingedge flap $C_{\mu}$ requirements are also shown.

Figures 18 and 19 compare results of this investigation (blowing BLC) and of reference 6 (area-suction BLC) to facilitate comparison of the two types of BLC with respect to longitudinal characteristics and $\triangle^{C} L_{S}$, the delay in tip stall, due to leading-edge flap deflections.

Results of calculations to show the effect of leading-edge blowing BLC on landing approach speed are shown in figure 20. Figures 21, 22,
and 23 present the calculations that show the effect of leading-edge BLC on take-off ground roll distance, air distance to 50 -foot altitude, and total distance to 50-foot altitude.

Results of design calculations to determine the leading-edge BLC system characteristics used in the performance analysis are presented in figures 24 through 26.

## DISCUSSION

This investigation was directed at increasing maximum lift while retaining longitudinal stability. The data in figure 7 show that, for the wing plan form considered here, trailing-edge flaps with BLC reduced the angle of attack for a given lift coefficient below maximum lift, but did not significantly increase maximum lift. In view of this, the major portion of the discussion will consider the effects on maximum lift and longitudinal stability of a plain leading-edge flap with blowing BLC applied on the flap radius.

The term "usable lift coefficient," as employed in the following discussion, is defined as the lift coefficient at which neutral longitudinal stability occurs; increasing lift above this value causes longitudinal instability.

> Summary of the Effect of the Leading-Edge Flap and Leading-Edge BLC on Longitudinal Characteristics

Data presented in figure 7 show the maximum gains realized in the tests. Deflection of only the trailing-edge flaps with BLC gave little increase in maximum lift coefficient or usable $C_{L}$. The deflection of the leading-edge flaps without leading-edge BLC increased $C_{I_{m a x}}$ from 0.99 to 1.25 , but usable $C_{L}$ was increased only from 0.83 to l.0. Appli cation of leading-edge BLC with larger leading-edge flap deflections increased $C_{\max }$ to $l .61$ and usable $C_{L}$ to 1.59 . The combination of leading-edge flap deflection and blowing leading-edge BLC increased usabl, $C_{\text {L }} 91$ percent. A large portion of this gain was the result of leadingedge BLC extending the range of longitudinal stability so that usable $C_{L}$ was near $C L_{\text {max }}$.

## Effect of Leading-Edge Configuration Variables on Longitudinal Characteristics

For this wing plan form, air-flow separation occurred first at the wing leading edge at the outboard wing sections and then progressed inboard with increased angle of attack. This stall progression resulted in longitudinal instability. In order to increase maximum lift and also retain longitudinal stability with BLC, it was necessary to have larger leading-edge flap deflections outboard than inboard and also to control the spanwise amount of BLC.

Effect of leading-edge flap deflection. - Data showing the effect of several combinations of leading-edge flap deflection on lift and stability are presented in figure 8. These data include results without leading-edge BLC, and with leading-edge BLC for the two leading-edge nozzles tested. The lift results are summarized as follows:

| Sie, deg | $\begin{gathered} \text { Leading-edge } \\ \text { nozzle } \end{gathered}$ | $\mathrm{C}_{\mu_{\text {Ie }}}$ | $\mathrm{C}_{\text {Lmax }}$ | $\Delta C_{\text {Imax }}$ | Usable CL | Usable $\triangle C_{L}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0,0,0 | - - | 0 | 0.99 | (a) | 0.83 | --- |
| 0,40,50 | - - | 0 | 1.25 | 0.26 | 1.00 | 0.17 |
| 0,50,60 | - - | 0 | 1.22 | . 23 | 1.00 | . 17 |
|  | - - | 0 | 1.20 | . 21 | 1.00 | .17 |
| 30,60,60 | - - | 0 | 1.06 | . 07 | . 98 | . 15 |
| 0,40,50 | A | . 027 | 1.32 | b. 07 | 1.26 | . 26 |
| 0,50,60 | A | . 027 | 1.40 | . 15 | 1.28 | . 28 |
| 0,60,60 | A | .027 | 1.44 | . 19 | 1.40 | . 40 |
| ${ }^{\text {c }} 30,60,60$ | B | . 030 | 1.51 | . 26 | 1.50 | . 52 |
| 0,40,50 | B | . 076 | 1.40 | b. 15 | 1.32 | . 32 |
| 0,50,60 | B | . 076 | 1.45 | . 20 | 1.44 | . 44 |
| 0,60,60 | B | . 076 | 1.48 | . 23 | 1.48 | . 48 |
| 30,60,60 | B | . 076 | 1.61 | . 36 | 1.59 | . 59 |

aIncrements from $\delta$ le $=0,0,0$ values
bIncrements from $\delta_{\gamma_{e}}=0,40,50$ values with $C_{\mu \imath e}=0$
cFrom figure 9(c)

The optimum leading-edge flap deflection without BLC ( $\delta_{\text {le }}=0,40,50$ ) increased CLmax by 26 percent and usable CL by 20 percent. With $C_{\mu_{\text {re }}}=0.027$ and the leading-edge flap deflection increased to $60^{\circ}$ at the intermediate and outboard sections, C $L_{\max }$ was increased by 45 percent and usable $C_{L}$ by 69 percent. With a larger $C_{\mu z e}(0.076)$, these values were 49 and 78 percent, respectively. Strong nose-down moments
beyond $C_{I_{\max }}$ and the relatively small increase in $C I_{\max }$ when $C_{\mu}$ e was increased indicated that the maximum lift of this configuration was limited by air-flow separation over the root section.

Protection against the root stall was provided by $30^{\circ}$ of leading-edge flap deflection without BLC. This amount of root protection in conjunction with the intermediate and tip sections deflected $60^{\circ}$ with BLC $\left(C_{\mu Z_{e}}=0.030\right)$ increased $C I_{\max }$ by 53 percent and usable $C_{L}$ by 81 percent. Corresponding increases with $C_{\mu}$ e $=0.076$ were 63 and 91 percent, respectively. Increasing root protection by increasing the root flap deflection to $50^{\circ}$ and applying BLC increased $C_{\text {max }}$ only an additional 3 percent (see fig. 8(d)). This small gain indicates that if a further gain in CLmax is to be realized, more effective flow control is required at the intermediate and tip sections. Increasing leading-edge flap deflection or $\mathrm{C}_{\mu \mathrm{l}}$ e can provide the additional control.

Effect of spanwise distribution of blowing BLC.- Limitations on the quantity of available bleed air or duct size may require some variations in the spanwise extent and quantity of blowing BLC. Figure 9 presents data showing the effects of such variations on the longitudinal characteristics of the model. The effect of blowing over the tip section alone compared with blowing over the tip and intermediate sections is shown in figure $9(a)$ and the pertinent data are tabulated below for $\delta_{e}=0,50,60$.

| $C_{\mu}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| $\eta=0.4$ <br> to 0.7 | $\eta=0.7$ <br> to 1.0 | CImax | Usable <br> $C_{L}$ |
| 0 | 0 | 1.22 | 1.00 |
| 0 | .011 | 1.24 | 1.12 |
| .013 | .014 | 1.40 | 1.30 |
| 0 | .057 | 1.30 | 1.22 |
| .014 | .060 | 1.45 | 1.45 |

The importance of blowing on the intermediate section in conjunction with blowing on the tip is apparent since increments of usable $C L$ of 0.18 and 0.23 were gained.

The effect of blowing increased amounts of BLC air over the tip section with a constant amount of blowing over the intermediate section is shown in figure $9(\mathrm{~b})$. No appreciable gain in usable $C_{L}$ was obtained. However, it is believed that with a $30^{\circ}$ root-flap deflection rather than the $0^{\circ}$ flap tested, an appreciable gain in $C_{L}$ would have been realized. This assertion is partially substantiated by data presented later
(fig. $14(\mathrm{~b})$ ) showing the variation of $C$ with $C_{\mu r e}$ at $\alpha=25.2^{\circ}$ and $\delta_{z_{e}}=30,60,60$. The same increase in tip section blowing as that for the data in figure $9(b)$ with $\delta_{\text {e }}=30,60,60$ increased $C_{L}$ by 0.12 .

The effect on $C_{\text {Lmax }}$ and usable $C_{L}$ of varying $C_{\mu z e}$ from 0.030 to 0.078 (see fig. $9(\mathrm{c})$ ) was small $\left(\Delta C_{\text {Lmax }}=0.1\right)$ when compared with the gain obtained by increasing $C_{\mu z e}$ from 0 (fig. 8(a)) to 0.030. These data had a tip to intermediate section blowing ratio of between 5 and 7 to $I$ and the root flap deflected $30^{\circ}$. Data in a later section of this report show that the lowest $C_{\mu l e}$ tested from $\eta=0.4$ to 1.0 ( 0.030 ) was adequate to provide BLC over the leading-edge flap radius as long as unseparated air flow existed in front of the leading-edge nozzle. Further reduction of $C_{\mu_{\text {le }}}$ (keeping the same spanwise flow distribution) would have allowed flow separation on the flap radius at the intermediate section and, perhaps, a resultant deterioration of longitudinal characteristics.

Effect of increased leading-edge radius and camber.- Research on increasing CLmax by enlarging the leading-edge radius and cambering the forward portion of the airfoil is reported in reference 7. Reference 5 presents results of tests on this modification in conjunction with a plain leading-edge flap, and reference 6 extends these data to the case with area suction applied to the radius of the flap. All three of these references report that the leading-edge modification improved longitudinal characteristics.

Details of this modification as applied in the present test are shown in figure 4. The effect on the longitudinal characteristics of applying this modification on two spanwise extents of the leading edge is shown in figure 10. No appreciable gain in $C_{\text {max }}$ or usable CL resulted from the application of the modification to the tip section. With the modification on both the intermediate and tip flap sections, $C_{L_{\max }}$ and usable $C_{L}$ were increased 0.05 , and the angle of attack for $C_{\max }$ was increased $\mathcal{I}^{\circ}$. This gain is smaller than would be anticipated from the data in references 5, 6, and 7 .

## Trailing-Edge Flaps

The data in figure 7 show that without leading-edge BLC, the small-span trailing-edge flap with area-suction BLC had little effect on CLmax or usable CL, but served mainly as a device to reduce the angle of attack for a given $C_{L}$ below $C_{I_{\max }}$.

Longitudinal characteristics.- Although trailing-edge flap blowing BLC did increase $C_{L_{\max }}$ and usable $C_{L}$ when accompanied by leadingedge BLC (fig. ll), the magnitude of the gains was small relative to the increases provided by leading-edge fiap BLC. With BLC applied to
the small-span trailing-edge flaps, usable $C_{L}$ and $C_{\text {Lmax }}$ were increased by values of 0.09 and 0.07 , respectively, whereas both increments of gain were 0.16 with BLC applied to the large-span flaps.

A reflex in the lift curve occurred when leading-edge BLC was applied without BLC on the trailing-edge flap. Static-pressure orifices near the trailing-edge flap radius showed that the minimum pressure on the flap approached the values obtained with trailing-edge BLC applied as the angle of attack was increased to about $8^{\circ}$. An apparent increase in lift-curve slope resulted which reduced the angle-of-attack changes due to trailingedge BLC for a given CL. In the a range consistent with the landing approach condition ( $\alpha=12^{\circ}$ to $16^{\circ}$ ), trailing-edge BLC reduced the angle of attack for a given $C_{L}$ by about $1-l / 2^{0}$ for the small-span flap and $4-1 / 2^{0}$ for the large-span flap.

Comparison with theory.- The theoretical lift increment obtainable from the deflected trailing-edge flaps used in this investigation was calculated by the method of reference 8. These increments for $\delta_{t e}=60^{\circ}$ are shown below.

| Flap span, $\eta$ | Experimental <br> (tail on)$\Delta C_{L}$ | Theoretical $\Delta C_{L}$ |
| :---: | :---: | :---: |
| $0.21-0.46$ | 0.43 | 0.53 |
| $.21-.66$ | .77 | .86 |

The experimental results listed above were obtained by extrapolation to $\alpha=0^{0}$ of the data in figure ll. The decrement of $\triangle C_{L}$ due to the tail is estimated to be 0.05 for the small-span trailing-edge flap and 0.08 for the large-span trailing-edge flap.

## Boundary-Layer-Control Flow Requirements

It was found in reference 2 that the $C_{\mu_{c}}$ required for a given trailing-edge configuration was dependent on flap deflection and nozzle location, and was independent of nozzle height, free-stream airspeed, and angle of attack. In the case of the leading-edge flap, the minimum pressure and pressure gradient on the leading-edge flap radius is dependent to some degree on angle of attack, so that leading-edge BLC flow requirements should also be dependent on angle of attack.

Figure 12 contains data showing the variation of $C_{L}$ with $C_{\mu \text { le }}$ for two blowing nozzle heights, two free-stream airspeeds, and two angles
of attack. These data indicate that, within the limits tested, lift obtained from $\mathrm{C}_{\mu_{2}}$ is independent of nozzle height and free-stream airspeed, and is dependent upon angle of attack.

Variation of leading-edge BLC flow requirements with angle of attack.- Figures 13 and 14 present data showing the variation of $C_{L}$ $\overline{\text { with }}_{\mu \text { re }}$ for several angles of attack. Figure 15 presents a cross plot of the data in figures 13 and 14, showing the variation of critical $\mathrm{C}_{\mu z}$ e with $\mathrm{C}_{\mathrm{L}}$. Critical $\mathrm{C}_{\mu z}$ e for the data in figure 15 was arbitrarily defined as the point where the slope of $C_{L}$ versus $C_{\mu z e}$ curve equals 8, and approximately corresponds to the point where BLC at the flap radius is realized without air-flow separation in front of the blowing nozzle.

These data show a rapid increase in total $C_{\mu c}$ with lift coefficient (or a). In general, the tip wing section had a larger value of $C_{\mu}$ than the intermediate section. This was due to the high section lift coefficients (when compared to the intermediate section) on the tip section of a wing with this plan form. Further, pressure distributions indicated that at $\alpha=25.2^{\circ}$, some flow separation existed in front of the BLC nozzle. The blowing BLC caused the flow to reattach, but at relatively high $C_{\mu r e}$ values. This could explain the rapid increase in $C_{\mu_{c}}$ above $C_{L}=1.35$ for intermediate and tip blowing shown in figure 15 .

Delaying the stall to a larger angle of attack would require prevention of the air-flow separation in front of the leading-edge blowing nozzle by larger flap deflections or BLC on the flap leading edge. The other alternative is provision for extremely large $C_{\mu}$ e values on the flap radius to induce flow reattachment.

Effect of leading-edge-blowing nozzle position.- Reference 2 reported that $\frac{C_{\mu}}{}$ requirements were independent of nozzle position on the trailing-edge flap radius as long as the nozzle was upstream from the minimum pressure point. A downstream position of the nozzle was found to increase the flow requirements.

The leading-edge nozzle was placed at $\theta=35.5^{\circ}$ during the threedimensional model investigation. The angle $\theta$ is shown in figure 6. This location was selected on the basis of results from an exploratory two-dimensional investigation. These data are presented in figure 16 . The trend exhibited by the two-dimensional results is similar to those observed in reference 2. Placement of the nozzle downstream of the minimum pressure $\left(\theta=36^{\circ}\right)$ greatly increased the BLC flow requirements; however, placement upstream caused no noticeable change. For all flap deflections tested during the three-dimensional model investigation, the leading-edge BLC nozzle was at or upstream from the point of minimum pressure on the flap radius.

Trailing-edge flap flow requirements.- Figure 17 presents data showing the variation of $\mathrm{C}_{\mathrm{L}}$ with $\mathrm{C}_{\mu \mathrm{te}}$. The data for the two trailingedge flaps were obtained with different leading-edge flap configurations. The data indicate that $C_{\mu_{c}}=0.0015$ and 0.006 with $\delta_{t e}=60^{\circ}$ for the small-span and large-span flaps, respectively. It is believed that at $\alpha=0^{\circ}$ these values were unaffected by the different leading-edge configurations.

Reference 2 gives a relationship for determining the equivalent two-dimensional $C_{\mu}$ from three-dimensional data. The data from the present investigation were used to obtain equivalent two-dimensional values of 0.0075 and 0.019 for the small- and large-span flaps, respectively. These are only 22 percent and 56 percent of the value ( 0.034 ) quoted in reference 2 for $\delta_{t e}=60^{\circ}$.

> Comparison of Blowing and Area-Suction BoundaryLayer Control

Since both area-suction (ref. 6) and blowing boundary-layer control investigations have been conducted on the same wing, some comparison of the effectiveness of the two types of BLC should be made. Although the wing and horizontal tail of the two models were actually the same for both investigations, the fuselages, wing height, and tail height were somewhat different. The over-all effect of these differences on the basic model without boundary-layer control was that the maximum lift coefficient and the lift-curve slope were less for the low-wing model than for the mid-wing model, as shown in figure 18. Also shown in the figure is the comparison with blowing and suction, indicating that blowing was more effective than suction in increasing maximum lift as well as retaining linear lift and pitching-moment characteristics to higher values of lift coefficient. In support of the foregoing, figure 19 has been prepared to show the relative effectiveness of the two types of BLC in preventing outboard stall as indicated by changes in drag and pitching moment and limited observations of pressure distributions. Identical spanwise configurations of leading-edge flap deflections were not tested; however, the results shown for the outboard flap should indicate the effectiveness of each system in preventing outboard stall. The value of $\triangle L_{S}$ shown in the figure corresponds to the increment of lift by which air-flow separation on the outboard sections is delayed from the value of lift coefficient at which separation occurred with no leading-edge flap deflections. Blowing provides significantly greater values of $\Delta C_{L_{S}}$ than area suction through the range of outboard flap deflections tested.

To illustrate the relative engine bleed-air requirements of the two boundary-layer-control systems a comparison has been made for conditions where each system achieved about the same lift coefficient ( $C_{L}$ of about 1.4) at an angle of attack of $21^{\circ}$ or $22^{\circ}$. For this
comparison suction BLC was given the added advantage of a modified leading edge. With area suction, reference 6 shows that a flow coefficient of about 0.001 is required, whereas for blowing the present investigation shows a momentum coefficient, $C_{\mu}$, of about 0.020 is required. The engine bleed-air requirements for each system were calculated by the method discussed in reference 2, assuming a flight speed of 130 knots and bleed air available from the engine at a pressure ratio of 5.0 and at a temperature of $900^{\circ} \mathrm{R}$. The engine bleed air was used directly for blowing BLC, whereas it was used to drive a pump for area-suction BLC. With a pump of 80 -percent efficiency the area-suction system would require about 30 percent of the bleed air required for blowing; with a pump of 15 -percent efficiency (an ejector pump), the area-suction system would require about 140 percent of that for blowing.

It can be concluded as was the case for trailing-edge flaps (ref. 2) that blowing systems will require the same order of bleed air from the engine as area suction unless the latter use reasonably efficient pumping systems.

## Evaluation of Blowing Boundary-Layer Control

Pertinent low-speed performance with and without blowing boundarylayer control is considered here. Results of computations of approach speed and take-off distance are presented. Details of the blowing nozzle size selection and performance calculations are contained in Appendixes A and B.

Approach speed.- Reference 9 shows $1.15 \mathrm{~V}_{\mathrm{S}}$ to be one criterion for landing-approach speed. This value will be used here. Figure 20(a) shows approach speed for the best configuration with leading-edge boundarylayer control ( $\delta_{z e}=30,60 ; 60$ ) and without leading-edge boundary-layer control $\left(\delta_{2 e}=0,40,50\right)$ with the small-span trailing-edge flap. The increase in usable CL obtained with leading-edge boundary-layer control reduced approach speed at $W / S=55$ pounds per square foot by 31 knots or about 21 percent. The effect of trailing-edge boundary-layer control with $\delta_{l e}=30,60,60$ and leading-edge BLC (fig. $20(\mathrm{~b})$ ) was a 4 -knot reduction of approach speed with the small-span flap. Approach speed was reduced an additional 5 knots with the large-span flap and BLC. Attitude of the aircraft during the landing approach was $15^{\circ}$ for the small-span trailing-edge flap with and without BLC, and $12^{\circ}$ for the large-span flap with BLC.

Take-off distance.- The method used and the assumption made in calculating take-off distance over a 50-foot obstacle are discussed in Appendix B. Two cases have been analyzed: (l) a minimum lift-off velocity of 1.05 V (angle of attack about $20^{\circ}$ ), and (2) the velocity corresponding to lift-off at an angle of attack of $15^{\circ}$.

The reduction in ground-roll distance for take-off with the application of leading-edge flap boundary-layer control is shown in figure 2l. For the case of 1.05 VS , the reduction in ground-roll distance is 37 percent over the entire wing loading range and for the case of a limiting angle of attack of $15^{\circ}$ the reduction varies from about 18 percent at a $\mathrm{W} / \mathrm{S}$ of $70 \mathrm{lb} / \mathrm{sq}$ ft to about 22 percent at a $\mathrm{W} / \mathrm{S}$ of $100 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$. For both cases, maximum thrust loss from full engine air bleed with the leading-ed.ge nozzle designed for $C_{\text {Imax }}$ near $\alpha=25^{\circ}$ was used in the calculations. Control of the engine air for the leadingedge BLC system during the take-off (discussed in Appendix A), and the resultant minimization of thrust loss due to BIC caused a further reduction of 150 to 300 feet in ground-roll distance throughout the wing loading range studied.

The reductions in air distance to obtain an altitude of 50 feet with the application of leading-edge BLC are shown in figure 22. Reductions of comparable percentages as in the ground roll are indicated for the low wing loading range of the airplane. However, at wing loadings greater than $80 \mathrm{lb} / \mathrm{sq} \mathrm{ft} ,\mathrm{the} \mathrm{F}_{\mathrm{n}} / \mathrm{W}$ ratio of the airplane without BLC is sufficiently low to leave little or no excess thrust for acceleration; under these conditions, larger reductions in transition distance resulted from the use of BLC, primarily as a consequence of the large reductions in drag. The control of bleed air also shows a more significant reduction in air distance to 50 feet at wing loadings greater than $80 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$.

The same trends in reduction in take-off distance with boundarylayer control are shown in figure 23 as the total distance to 50 feet of altitude. To summarize, it appears that the total take-off distance can be reduced by about 38 percent between $\mathrm{W} / \mathrm{S}$ of 65 to $85 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$ with reductions greater than 50 percent at $\mathrm{W} / \mathrm{S}$ about $90 \mathrm{lb} / \mathrm{sq}$ ft for takeoff based on $1.05 \mathrm{~V}_{\mathrm{S}}$. With the take-off speed limited to an angle of attack of $15^{\circ}$, the reduction in take-off distance varies from a value of about 20 percent at a $\mathrm{W} / \mathrm{S}$ of 65 to a value of about 30 percent at a $\mathrm{W} / \mathrm{S}$ of $85 \mathrm{lb} / \mathrm{sq}$ ft to greater than 40 percent at higher wing loadings. The use of controlled bleed indicates the largest improvements are to be made at the higher wing loadings corresponding to the lower thrust-to-weight ratios and can result in additional improvements of 1000 to 3000 feet. The thrust-to-weight ratio of the hypothetical airplane was 0.3 at a $\mathrm{W} / \mathrm{S}$ of $103 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$. It therefore appears that controlled bleed during the take-off may provide significant improvement in take-off performance, particularly for airplanes having thrust-to-weight ratios of less than about 0.3

## CONCLUSIONS

The following conclusions have been made from analysis of the test results:

1. Leading-edge-blowing boundary-layer control (BLC) significantly increased maximum lift and stability near maximum lift. Lift and stability were generally sensitive to spanwise variations in flap deflection and extent of blowing.
2. Variation of lift with momentum coefficient was independent of blowing nozzle height and free-stream airspeed. Increasing angle of attack increased critical leading-edge momentum coefficient values.
3. The trailing-edge flaps caused a relatively small gain in maximum and usable lift when compared to the leading-edge flaps.
4. Comparison of the results of this investigation with the results of NACA RM A57H21 (area-suction BLC) showed that the increments of maximum and usable lift due to leading-edge BLC were higher with the blowing BLC model. Leading-edge BLC air-flow requirements were of the same order of magnitude for the two types of BLC. Engine bleed-air requirements for the two types of BLC are, however, a function of the particular installation.
5. A limited two-dimensional investigation indicated that location of the blowing nozzle downstream from the point of minimum pressure on the leading-edge flap radius increased the critical momentum coefficient.
6. Estimation of the low-speed performance improvement obtainable with leading-edge BLC and small-span flap with BLC indicated a reduction in approach speed of 20 percent (based on 1.15 of the stalling speed) and a reduction of take-off distance over a 50-foot obstacle of as much as 40 percent at the higher wing loadings.

Ames Aeronautical Laboratory<br>National Advisory Committee for Aeronautics Moffett Field, Calif., Jan. 9, 1958

## APPENDIX A

## - DETERMINATION OF THE BOUNDARY-LAYER-CONTROL <br> SYSTEM CHARACTERISTICS

In evaluating the low-speed performance of an airplane with BLC the following elements in the design of the blowing BLC system were considered from the standpoint of their effects on performance.

## Aircraft Size and Power

The wing plan form considered was intended to represent one approach to the wing design of a high-performance fighter aircraft. Data for present-day aircraft indicate that a minimum $F_{n} / W$ ratio of 0.4 and operation at wing loadings from 50 to $100 \mathrm{lb} / \mathrm{sq}$ ft are representative. In accordance with these values, the linear model dimensions were increased 25 percent and two J-57 engines were assumed to be the power plants.

## Blowing Nozzle Height Selection

Reference 2 presents a method of matching the requirement of a trailing-edge flap blowing BLC system with the bleed capabilities of a turbojet engine. This method was used for the leading-edge BLC system. The value of $C_{\mu z e}=0.032$ was selected on the basis of the discussion in the present report regarding critical $C_{\mu}$.

The variation of $W_{B P}$ with duct pressure ratio for constant freestream velocities was calculated for this $C_{\mu}$ and is shown in figure 24. For the calculations, duct air pressure and temperature were assumed to be the same as at the engine bleed port. Air characteristics at the engine bleed port were obtained from reference lo. Flow conditions through the BLC nozzle were assumed to be isentropic. The variation of $W_{B P}$ with duct pressure ratio for several values of nozzle height were plotted as shown in figure 24.

Based on a design trim $C_{\max }$ of 1.47 , wing loadings were assigned to the constant velocity curves. The working area of the chart (fig. 24) is defined by the wing-loading range and pressure ratio available during take-off and landing approach. The large difference in duct pressure ratio available at take-off (10.5) and landing approach ( 6.2 for $10 \mathrm{ft} / \mathrm{sec}$ sinking speed) indicates that the selection of nozzle height is a compromise. The O.Ol0-inch nozzle height would limit landing approach speed.

The 0.015 -inch nozzle used in the calculations is the smallest size that would supply the stipulated $\mathrm{C}_{\mu}$ during landing approach; however, this nozzle would pass greater values of bleed air than necessary during takeoff if no bleed control is considered. The thrust loss due to air bleed will be discussed in the next section.

The trailing-edge flap nozzle heights selected by the same procedure * were very small From a practical construction standpoint, nozzle heights of 0.010 and 0.015 inch were selected for the small- and large-span flap, respectively.

Reduction of Thrust Losses Due to Boundary-LayerControl Air Bleed

Figure 25(a) shows the variation of $C_{\text {Lere }}$ with angle of attack obtained from figure $15(\mathrm{~b})$. As shown by the figure, $\mathrm{C}_{\mu_{c_{2}}}$ increases rapidly with increasing angle of attack. If the nozzle height selection is based on $C_{\mu_{c_{2}}}$ at a high angle of attack, which was the case for the performance estimation here, the engine bleed air for leading-edge BLC would be greatly in excess of that required through most of the take-off and landing-approach maneuver. Examination of the nozzle height chart (fig. 24) shows that at the take-off wing loadings of 90 to $100 \mathrm{lb} / \mathrm{sq} \mathrm{ft}$, the hypothetical airplane would have a stalling speed of approximately 140 knots. Figure $25(\mathrm{~b})$ shows the calculated BLC bleed air required at 140 knots with the 0.015 -inch leading-edge nozzle as a function of angle of attack. The bleed air supplied by the unrestricted ducting is also shown in the figure. Figure 25 (c) shows that, during the take-off ground run, as much as 11.5 percent of the thrust at takeoff can be lost due to unrestricted leading-edge BLC bleed air. Restricting the leading-edge BLC engine bleed air during the take-off to required values throughout the range of angles of attack resulted in no thrust loss during ground run to small values during transition. A throttle valve placed in the leading-edge ducting can be used to restrict the BLC engine bleed air flow. This valve could be controlled by a device which senses changes in angle of attack, dynamic pressure, etc.

It is also necessary to check the effect of the bleed air control during the landing approach. Figure 26 presents the variation of $C_{\mu}$ required and available with velocity for $10 \mathrm{ft} / \mathrm{sec}$ sinking speed. The thrust component of the lift was ignored for these calculations. For this hypothetical airplane, the bleed air control, designed for the takeoff conditions of figure 25 , would not supply the $C_{\mu z e}$ required during the landing approach. To do this the throttling of the valve must be reduced slightly.

## APPENDIX B

## PERFORMANCE COMPUTATIONS

The test results used for the low-speed-performance computation were modified as follows:

1. A drag coefficient increment of 0.06 was added to the test values to account for landing gear and airplane protuberances not found on the model.
2. The pitching moment used to obtain the trimmed $C_{L}$ was taken with the aircraft moment center at $0.33 \overline{\mathrm{c}}$ instead of $0.25 \overline{\mathrm{c}}$ as the data are presented.

In addition, the term $C_{I_{\max }}$ as used here is synonymous with the term "usable $C_{L}$ " in the body of the report.

## Approach Speed

An evaluation of approach speed for several present-day fighters was made in reference 9, which indicates that a value of $1.15 \mathrm{~V}_{\mathrm{S}}$ is one criterion for approach speed and is used herein. For flight at a constant wing loading and rate of sinking speed, the value of $\mathrm{V}_{\mathrm{S}}$ is dependent on $C_{\mu}$ available and the corresponding value of $C_{\text {max }}$ obtained. These variables can be obtained from the test results, the BLC system characteristics (as determined in Appendix A), and the engine characteristics during the landing approach. The stall speed was then determined by the following relation for dynamic pressure:

$$
q_{S}=\frac{W / S}{C_{L}+C_{D} \tan \alpha}
$$

where $C_{D} \tan \alpha$ is the $\Delta C_{L}$ due to the thrust component in the vertical direction.

Take-Off Distance

In the calculations the maneuver was considered in two parts: the ground roll, and the air distance required to clear a 50-foot obstacle. Ground distance is the distance required for the airplane to accelerate to a predetermined lift-off velocity at $\alpha=0^{\circ}$. The airplane is then
rotated to a suitable $\alpha$ for the lift-off with the landing gear down and held at this angle of attack until the 50 -foot height has been reached. The distance required for this climb is the air distance. A maximum performance take-off dictates that the lift-off should occur at $1.05 \mathrm{~V}_{\mathrm{S}}$ ( 0.907 C Lmax ) and the climb at the angle of attack required for flight at 1.05 VS . Since this angle is high (about $20^{\circ}$ ) with leading-edge BLC, and ground attitude on an actual aircraft may be limited, take-off distances with both $1.05 \mathrm{~V}_{S}$ and $\alpha=15^{\circ}$ as the criterion are presented.

Data available are insufficient to determine the optimum trailingedge configuration for take-off; accordingly, the effects of trailingedge configuration on take-off distance will not be considered here. All calculated take-off distance results are with the small-span flap deflected $60^{\circ}$ with BLC. An NACA standard day is assumed.

The ground roll distance was calculated by the following equation (from ref. ll):

$$
S_{g}=\frac{13.1 \frac{W}{S}}{C_{L_{G}}\left(\frac{D}{L}-\mu\right)} \ln \left[\frac{\frac{F_{n}}{W}-\mu}{\frac{F_{n}}{W}-\mu-\frac{C_{I_{G}}}{C_{L_{t o}}}\left(\frac{D}{L}-\mu\right)}\right]
$$

The air distance was obtained by a point-by-point solution of the equations for the forces on the airplane. These equations are as follows:

$$
\begin{aligned}
& \frac{d U}{d t}=g\left(\frac{F_{n}}{W} \cos \alpha-\frac{C_{D} q S}{W}-\sin \theta\right) \\
& \frac{d \gamma}{d t}=\frac{g}{U}\left(\frac{C_{L} q S}{W}+\frac{F_{n}}{W} \sin \alpha-\cos \theta\right)
\end{aligned}
$$

where $\gamma$ is the flight-path angle in radians. The finite increments of $U$ and $\gamma$ were calculated at l-second intervals, and the ground distance and altitude were then obtained by:

$$
\begin{aligned}
& S_{t}=\sum_{h=0}^{h=50}(U+\Delta U) \cos \gamma \\
& \left.h=\sum^{h} \gamma(U+\Delta U) \quad \text { (for small values of } \gamma\right)
\end{aligned}
$$

For the higher wing loadings, acceleration became zero prior to 50 feet and hence the transition reached completion before an altitude of 50 feet. In these cases, the distance to climb to 50 feet altitude at the steady rate of climb was added to the distance required to complete the transition.

For the purpose of the calculation, the following assumptions and simplifications were made: (l) average thrust was assumed through the speed range, (2) effects of ground proximity were neglected, and (3) the ground-resistance coefficient was $\mu=0.03$. The effect of thrust loss due to bleed air for BLC was evaluated and hence determined the value of $F_{n} / W$. With controlled bleed air, thrust loss due to engine bleed for leading-edge BLC was zero throughout the ground roll, and the minimum during transition, so that the gains realized from controlled bleed were a direct result of increased $F_{n} / W$.

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TABLE I.- GEOMETRIC DATA
WingArea, sq ft (without chord extension)334.8
Span, ft ..... 30.62
Mean aerodynamic chord, ft ..... 12.77
Root chord, ft ..... 18.69
Aspect ratio ..... 2.8
Taper ratio ..... 0.17
Sweep angle, degLeading edge51.7
Quarter-chord line ..... 45.4
Trailing edge ..... 14.2
Small-span trailing-edge flap
Area, sq ft ..... 25.81
Flap span, percent wing semispan ( 21 to 46 percent) ..... 25.0
Chord, percent wing chord ..... 25.0
Sweep angle of hinge line, deg ..... 26.8
Large-span trailing-edge flap41.14
Flap span, percent wing semispan ( 21 to 66 percent) ..... 45.0
Chord, percent wing chord ..... 25.0
Sweep angle of hinge line, deg ..... 26.8
Fuselage
Length, ft ..... 48.0
Maximum width, ft ..... 6.5
Fineness ratio in wing chord plane ..... 7.4
Horizontal tail (drooped 20 ${ }^{\circ}$ )St/S0.192
$\mathrm{b}_{\mathrm{t}} / \mathrm{b}$
0.53
0.53
$\imath_{t} / \bar{c}$ ..... 1.52
Aspect ratio ..... 4.0
Taper ratio ..... 0.30
Sweep angle of quarter-chord line, deg ..... 40.1

TABLE II.- COORDINATES OF BASIC WING

| NACA 0005 <br> Plane of <br> (Modified) <br> Symmetry |  |  |  |
| :---: | :---: | :---: | :---: |
| Station, <br> percent chord | Ordinate, <br> percent chord | Station, <br> percent chord | Ordinate, <br> percent chord |
| 0 | 0 | 30.00 | 2.501 |
| 1.25 | .789 | 40.00 | 2.419 |
| 2.50 | 1.089 | 50.00 | 2.206 |
| 5.00 | 1.481 | 60.00 | 1.902 |
| 7.50 | 1.750 | 67.00 | 1.650 |
| 10.00 | 1.951 | 70.00 | 1.500 |
| 15.00 | 2.228 | 80.00 | 1.000 |
| 20.00 | 2.391 | 90.00 | .500 |
| 25.00 | 2.476 | 100.00 | 0 |
| Leading-edge radius: 0.275 -percent c $c$ |  |  |  |


| Plain Chord Extension Perpen- <br> dicular to Leading Edge of <br> Plain Wing |  |
| :---: | :---: |
| Station, <br> percent chord | Ordinate, <br> percent chord |
| -4.83 | 0 |
| -4.75 | .23 |
| -4.60 | .39 |
| -4.40 | .53 |
| -4.20 | .64 |
| -3.90 | .78 |
| -3.00 | 1.03 |
| -2.00 | 1.15 |
| -1.00 | 1.23 |
| 1.00 | 1.35 |
| 3.99 | 1.50 |

TABLE III.- COORDINATES OF MODIFIED LEADING-EDGE SECTIONS PERPENDICULAR TO LEADING EDGE OF PLAIN WING

| Modified Leading Edge on Wing |  |  |
| :---: | :---: | :---: |
| Station, <br> percent chord | Ordinate, percent chord |  |
|  | Upper surface | Lower surface |
| 0 | -0.60 | -0.60 |
| .05 | -.29 | -.89 |
| .10 | -.18 | -1.01 |
| .25 | .07 | -1.22 |
| .50 | .35 | -1.42 |
| .75 | .53 | -1.54 |
| 1.25 | .80 | -1.65 |
| 2.00 | 1.06 | -1.71 |
| 2.50 | 1.21 | -1.71 |
| 3.00 | 1.38 | -1.70 |
| 3.50 | 1.42 | -1.68 |
| 4.00 | 1.49 | -1.67 |
| 4.50 | 1.57 | -1.66 |
| 5.00 | 1.64 | -1.64 |


| Modified Leading Edge on Plain Chord <br> Extension |  |  |
| :---: | :---: | :---: |
| Station, <br> percent chord | Ordinate, percent chord |  |
|  | Upper surface | Lower surface |
| -5.40 | -0.60 | -0.60 |
| -5.30 | -.17 | -.99 |
| -5.20 | -.02 | -1.16 |
| -5.00 | .21 | -1.35 |
| -4.60 | .49 | -1.55 |
| -4.20 | .67 | -1.64 |
| -3.60 | --1 | -1.65 |
| -3.20 | .97 | -1.62 |
| -3.00 | 1.02 | -1.61 |
| -2.00 | 1.15 | -1.46 |
| -1.00 | 1.23 | --- |
| -.92 | --- | -1.24 |

## TABLE IV.- FUSELAGE COORDINATES

| $\begin{array}{c}\text { Station, } \\ \text { ft }\end{array}$ | $\begin{array}{c}\text { Diameter, } \\ \text { ft }\end{array}$ | $\begin{array}{c}\text { Elliptical } \\$\end{array} | $\begin{array}{c}\text { Horizontal section } \\ \text { major axis, } \\ \text { ft }\end{array}$ |
| :---: | :---: | :---: | :---: | \(\left.\begin{array}{c}Vertical <br>

minor axis, <br>
ft\end{array}\right]\)

TABLE V.- MODEL CONFIGURATIONS FOR WHICH DATA ARE PRESENTED



A-22148
Figure 1.- Photograph of model in the Ames 40- by 80 -foot wind tunnel.


All dimensions in feet, unless otherwise noted


Figure 2. - Dimensional details of the model.
.010 inch from $\eta=0.15-.7$ .010 or .050 inch from $\eta=0.7-1.0$
(a) Typical leading-edge-flap cross section.

(b) Typical trailing-edge-flap cross section.

Figure 3.- Blowing nozzle arrangements of three-dimensional model.

(a) $\eta=0.4$ to 0.7

(b) $\eta=0.7$ to 1.0

Figure 4.- Leading-edge modification used in the investigation. All sections perpendicular to the wing leading edge. Dimensions in percent chord.


Figure 5.- Sketch of bleed-air ducting.


| $\left\lvert\, \begin{array}{\|c\|c\|} \hline \text { Station, } \\ \text { percent c } \end{array}\right.$ | Ordinate, percent |
| :---: | :---: |
| 0 | 0 |
| . 50 | . 80 |
| . 75 | . 97 |
| 1.25 | 1.22 |
| 2.50 | 1.69 |
| 5.00 | 2.33 |
| 7.50 | 2.81 |
| 10.00 | 3.19 |
| 15.00 | 3.81 |
| 20.00 | 4.27 |
| 25.00 | 4.60 |
| 30.00 | 4.83 |
| 35.00 | 4.96 |
| 40.00 | 5.00 |
| 45.00 | 4.89 |
| 50.00 | 4.69 |
| 55.10 | 4.38 |
| 60.00 | 4.02 |
| 65.00 | 3.60 |
| 70.00 | 3.13 |
| 80.00 | 2.10 |
| 90.00 | 1.06 |
| 100.00 | . 02 |
| L.E. radi | ius: 0.69 |



Figure 6. - Details of the two-dimensional blowing model.

|  | $\delta_{\text {le }}$, deg | $\delta_{\text {te }}$, deg | $C_{\mu l e}$ | $C_{\mu_{\text {te }}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\therefore 0,0,0$ | 0 | 0 | 0 |  |
| $\therefore 0,0,0$ | 60 | 0 | 0.006 |  |
| $\therefore 0,40,50$ | 60 | 0 | .006 |  |
| $\therefore 30,60,60$ | 60 | 0.076 | .006 |  |



(a) $C_{\text {MZe }}=0$

Figure 8. - Longitudinal characteristics for several leading-edge flap configurations with and without leading-edge BLC; small-span trailing-edge flap, $\delta_{t_{e}}=60^{\circ}, C_{\mu_{t e}}=0.006$.

(b) Leading-edge BLC with nozzle A; $C_{\mu z e}=0.027$.

Figure 8.- Continued.

(c) Leading-edge BLC with nozzle $B ; C_{\mu \imath e}=0.076$.

Figure 8. - Continued.

(d) Effect of root flap deflection with the modified leading edge from $\eta=0.4$ to 1.0.

Figure 8. - Concluded.


(a) Effect of blowing on the intermediate flap section; $\delta_{l e}=0,50,60$.

Figure 9.- Longitudinal characteristics with different amounts and spanwise extents of blowing

(c) Effect of changing total $C_{\mu}$, nozzle $B ; \delta$ e $=30,60,60$.

Figure 9.- Concluded.

(a) Effect of applying the modified leading edge from $\eta=0.7$ to 1.0 .

Figure 10. - Effect of the modified leading edge on longitudinal characteristics; $\delta_{2 e}=30,60,60$, leading-edge nozzle $B$, small-span trailing-edge flap, $\delta_{t e}=60^{\circ}$, $\mathrm{C}_{\mu}$ te $=0.006$.

(b) Effect of increasing the spanwise extent of modified leading edge.

Figure 10.- Concluded.

(a) Small-span trailing-edge flap.

Figure ll. - Effect of trailing-edge flap on the longitudinal characteristics of the model with and without leading-edge BLC; nozzle B with leading-edge BLC, $\delta$ te $=60^{\circ}$.

(b) Large-span trailing-edge flap.

Figure 1l. - Concluded.

(a) Effect of nozzle height.

(b) Effect of free-stream air velocity; leading-edge nozzle $B$.

Figure 12. - Variation of lift with leading-edge $C_{\mu} ; \delta_{e}=30,60,60$, small span flap, $\delta$ te $=60^{\circ}, C_{\mu t e}=0.006$.


Figure 13. - Effect of angle of attack on the variation of lift with $C_{\mu z e} ; \delta_{\text {re }}=30,60,60$, leading-edge nozzle A, small-span trailingedge flap, $\delta$ te $=60^{\circ}, C_{\mu t e}=0.006$.


Figure 14. - Effect of angle of attack on the variation of lift with $C_{\mu \text { le }}$, $\delta$ le $=30,60,60$, leading-edge nozzle $B$, small-span trailingedge flap, $\delta_{t e}=60^{\circ}, C_{\mu t e}=0.006$.

(a) Leading-edge nozzle A.

(b) Leading-edge nozzle B.

Figure 15. - Variation of $C_{\mu c l e}$ with $C_{L}, \delta_{l e}=30,60,60$; small-span trailing-edge flap, $\delta$ te $=60^{\circ}, C_{\mu t e}=0.006$.


Figure 16. - Effect of leading-edge nozzle location on $\mathrm{C} \mathrm{\mu}_{\mathrm{c}} \mathrm{c}_{\mathrm{e}}$; twodimensional data, $R=1.65 \times 10^{6}$, $\delta_{l e}=60^{\circ}, \alpha=36^{\circ}, h / c=0.00033$.

(a) Small-span flap, $\delta_{l e}=0,40,50$, without leading-edge BLC.

(b) Large-span flap.

Figure 17. - Variation of lift coefficient with $C_{\mu t e}, \delta_{t e}=60^{\circ}$.


Figure 18.- Comparison of the longitudinal characteristics of the area suction model and the blowing model; leading edge BLC applied from $\eta=0.4$ to l.0; small-span trailing-edge flap, $\delta_{t e}=60^{\circ}$.



Flagged symbols denote no BLC

Figure 19. - The effect of outboard leading-edge flap deflection with and without blowing or area suction on delaying tip stall.

(a) Effect of leading-edge blowing BLC with small-span trailing-edge flap; $\delta_{t e}=60^{\circ}, C_{\mu t e}=0.006$.

(b) Effect of trailing-edge flap span; $\delta_{t e}=600$ with leading-edge blowing BLC , $\delta \mathrm{\delta}_{\mathrm{e}}=30,60,60$.

Figure 20.- Effect of leading-edge and trailing-edge flap variables on approach speed with zero sinking speed.

(a) Based on $1.05 \mathrm{~V}_{\mathrm{S}}$.

(b) Based on $\alpha$ limitation.

Figure 21.- Variation of take-off ground roll with wing loading; smallspan trailing-edge flap with blowing BLC, $\delta_{t e}=60^{\circ}$.

(a) Based on 1.05 V .

(b) Based on a limitation.

Figure 22. - Effect of leading-edge BLC on take-off air distance over a 50 -foot obstacle; small-span trailing-edge flap with blowing BLC, $\delta_{t e}=60^{\circ}$.


Figure 23. - Effect of leading-edge BLC on total take-off air distance over a 50-foot obstacle; small-span trailing-edge flap with blowing $B L C, \delta_{t e}=60^{\circ}$.


Figure 24. - Leading-edge nozzle height selection chart; $\delta_{\text {le }}=30,60,60$, $C_{\mu \text { le }}=0.032$, trimmed $C_{L}=1.47$, small-span trailing-edge flap deflected $60^{\circ}$.

(a) Variation of $C_{\mu z e}$ required with $\alpha$; leading-edge nozzle $B$.

(b) Leading-edge air bleed flow required at 140 knots; $h=0.015$.

(c) Thrust loss caused by bleed air.

Figure 25.- sine bleed requirements and thrust loss due to unrestricted bleed at take-off.


Figure 26. - Effect on Cure available with the bleed air-flow control in the leading-edge ducting; $10 \mathrm{ft} / \mathrm{sec}$ sinking speed, $\mathrm{h}=0.015, \mathrm{~W} / \mathrm{S}=55 \mathrm{psf}$.

