

# 3 1176 01354 2007

NACA ACR No. 15631

NATIONAL ADVISORT COMMITTEE FOR AERONAUTICS

# ADVANCE CONFIDENTIAL REPORT

A SIMPLE METHOD FOR ESTIMATING TERMINAL VELOCITY

INCLUDING EFFECT OF COMPRESSIBILITY ON DRAG

By Ralph P. Bielat

#### SUMMARY

A generalized drag curve that provides an estimate for the drag rise due to compressibility has been obtained from an analysis of wind-tunnel data of several airfoils, fuselages, nacelles, and windshields at speeds up to and above the wing critical speed. The airfoils analyzed had little or no sweepback and effective aspect ratios above 6.5. A chart based on the generalized drag curve is presented. from which the terminal velocity of a conventional airplane that employs a wing of moderate aspect ratio and very little sweepback in a vertical dive may be rapidly estimated. In order to use the chart, the only data that need be known about the airplane are a low-speed drag coefficient, the wing critical speed, and the wing loading. The terminal velocities for three airplanes were computed in order to illustrate the use of the method and chart. Good agreement between the estimated terminal velocity and the measured flight terminal velocity was indicated for all three airplanes.

## INTRODUCTION

Several high-speed military airplanes in dives have encountered difficulties that could not be easily controlled by normal means. These difficulties, which may consist of diving moments, large changes in trim, large stick forces, tail buffeting, and the like, occur in highspeed dives when the speed of the airplane exceeds the critical speed by a large amount. For those airplanes for which maximum diving speeds are at or near the critical speed, little or no trouble occurs. The more recent fighter airplanes, however, have terminal Mach numbers well in excess of the critical Mach number and, as a result, often encounter difficulties in dives. Determination of the terminal velocity of the airplane is therefore important in order that the probability of encountering trouble in dives may be estimated.

The terminal velocity is also important because it forms the outer limits of the V-G diagram. Usually the outer limit of the V-G diagram is established by multiplying the maximum level-flight speed of an airplane by an arbitrary factor somewhat greater than 1.0. The terminal velocity of most recent airplanes, however, generally falls much below this arbitrary maximum speed, and these airplanes are therefore unnecessarily penalized by extra weight because they are designed for conditions that are not reached in actual flight.

The present report outlines a simple method for obtaining the terminal velocity of an airplane in a vertical dive and includes an estimate for the drag increase due to compressibility effects. The wind-tunnel test data were obtained from model tests conducted in the Langley 24-inch and 8-foot high-speed tunnels. All the data presented herein were obtained for zero lift.

The problem of determining the terminal velocity for airplanes for which the terminal velocity is near the critical speed is comparatively simple inasmuch as a constant value of drag coefficient can be assumed. The diving speeds of most present-day airplanes, however, occur beyond the critical speed and the problem is not so simple. The following two factors are involved: (1) the determination of the critical speed and (2) the rate of drag increase at speeds above the critical speed.

The critical speed used herein was arbitrarily taken as the critical speed of the wing-root section. Pressuredistribution data obtained from wind-tunnel tests were used to determine the critical speed, which is defined as the flight speed at which sonic velocity is reached locally. If experimental data are not available, however, the methods outlined in references 1 and 2 can be used for the determination of the critical speed. Selection, of the critical speed at the wing-root section for use in terminal-velocity estimation is justified on the grounds. that the root section usually has a lower critical speed than any other component part of the airplane. The wing root has the lowest critical speed because of its high thickness ratio and contributes a large part of the total airplane drag because of the large fraction of the wing. area concentrated at the inboard sections of tapered wings.

The rate of drag increase at speeds above the critical speed is more difficult to determine in the calculation

of the terminal velocity than the critical speed. A study of the drag of airfoils, fuselages, nacelles, and windshields has been made from wind-tunnel test data in order to determine the effects of compressibility on the drag. Because the rate of drag increase at speeds above the critical speed is so great, it was found that, within the accuracy required for terminal-velocity calculations, an average rate of drag increase may be used. A curve indicating the average rate of drag increase is presented herein. This curve was derived from an analysis of windtunnel data.

The method described herein for obtaining the terminal velocity of an airplane in a vertical dive has been in use at the NACA since 1941. Publication of the method, however, had been delayed pending the investigation of constriction corrections to be applied to the wind-tunnel data and the completion of high-speed dive tests made with several airplanes in order to compare terminal velocities obtained in flight with terminal velocities estimated by the simple method described herein. This method is not applicable to airplanes that utilize wing shapes of low aspect ratio and large sweepback but should be applied only to airplanes of conventional design that employ wing shapes of moderate aspect ratio and small amounts of sweepback due to wing taper ratio.

#### SYMBOLS

- V velocity
- a speed of sound in air
- M Mach number (V/a)
- C<sub>D</sub> drag coefficient
- CL lift coefficient

ρ mass density of air

S wing area

W weight of airplane

p atmospheric pressure at any altitude

2

 $\gamma$  ratio of specific heats (1.40 for air)

t/c ratio of thickness to chord of wing

Subscripts:

cr critical (when local sonic velocity has been reached on some point of body)

min minimum

T terminal

## DESCRIPTION OF MODELS

Airfoil models.- The airfoil models used herein represent two classes of airfoils - namely, the conventional NACA sections and the more recent low-drag highcritical-speed NACA sections. The conventional NACA airfoil sections are characterized by pressure distributions that have high peak pressures occurring near the leading edge. The low-drag NACA airfoil sections have comparatively flat pressure distributions with the peak pressures occurring at approximately 60 percent of the chord behind the leading edge.

Airfoils typical of the conventional airfoils are the NACA 0009-63, 0012-63, 23012, and 23014.7 sections; a current transport-model airfoil that has an NACA 2215 section at the root and tapers to an NACA 2212 section at the tip; and the Davis airfoil with a thickness ratio of 20.15 percent. The low-drag airfoils include the following NACA airfoil sections:

16-215	65-type modified, $\frac{1}{2}$ = 0.196	)
16-509	66.1-115	
16-515	67-114.5	
47 - 215	67,0-215	
0712101-220	· · · · · · · · · · · · · · · · · · ·	

The effective aspect ratio of the airfoil models tested varied from 6.5 to infinity.

Fuselage models.- The fuselage models are typical of fuselage shapes in use on current airplanes. The various fuselages represent bomber, fighter, and transport airplanes. Figure 1 shows the side-view drawing and the fineness ratio in side elevation of the different fuselage shapes. These fuselage models were tested in conjunction with wings (shown as dashed lines in fig. 1) and represent a wide variation in wing-fuserage interference. Nacelle and windshield models.- The data for the various nacelles and windshields were obtained from references 3 and 4, respectively. The nacelle and windshield designations used herein correspond to the designations used in references 3 and 4. All the nacelle models were tested with the same wing model, which consisted of the outboard panel of a wing section designed for use on a bomber airplane. The wing was a thick low-drag airfoil that had an NACA 65(218)-221 section at the root and tapered to an NACA 66(2x15)-416 section at the tip. The windshields were tested with a wing-fuselage combination. Drawings of the nacelle and windshield models are shown in figures 2 and 3, respectively.

#### RESULTS AND DISCUSSION

## Drag Characteristics

<u>Drag analysis.</u> In order to obtain a correlation of the rate of drag increase at speeds above the critical speed, the drag results for the various component parts of the airplane have been reduced to nondimensional parameters; that is,  $C_D/C_{D_{min}}$  is plotted against  $M/M_{CT}$ for each part tested. The use of these parameters represents a convenient method of making the data nondimensional in such a manner that the unknown quantities are expressed in terms of the known quantities.

The drag results at speeds up to and above the critical speed for the conventional NACA airfoils are presented in figures 4 and 5. Figures 6 to 9 show the variation of  $C_D/C_{D_{min}}$  with  $M/M_{cr}$  for the low-drag high-criticalspeed airfoils. It will be noted that all the airfoils presented in figures 4, 6, 7, and 8 exhibited approximately the same rate of drag increase at speeds above the critical speed; for this reason a curve of the average rate of drag increase at speeds above the critical speed maybe used. An average increase in drag of approximately 30 perćent above the minimum drag was indicated at  $\frac{M}{M_{cr}} = 1.0;$ 

at speeds of only 10 to 15 percent above the critical speed, however, the drag increased approximately 90 to 200 percent. This rapid increase in drag at speeds above the critical speed is associated with the formation

ŧ.

2

3

of compression shock waves and their effect on the boundary layer over the surface of the airfoils. The family of airfoils used in figure 5 showed less percentage of increase in drag at the critical speed than the NACA 0009, 0012, or the low-drag high-critical-speed airfoil sections. Both published (reference 5) and unpublished high-speed data show that the NACA 230-series airfoils differ from most of the other airfoils in that the critical speed can be exceeded by as much as 0.15 in Mach number before any serious changes in the aerodynamic characteristics of the airfoil occur. The critical speed of the NACA 230-series airfoils is therefore exceeded by approximately 7<sup>1</sup>/<sub>2</sub> percent

6

before the same percentage of increase in drag occurs as is shown for the other airfoils. The importance of this difference in the shape of the drag curve above the critical speed on the estimation of terminal velocity is discussed in the section entitled "Terminal-Velocity Calculation."

The rapid increase in drag before the critical speed is reached, which is shown for the NACA 67-114.5 airfoil in figure 9, is due to early separation of the flow over the after portion of the airfoil. This condition also affects the method for estimating the terminal velocity. An error in estimating the terminal velocity when the flow separates will occur only for those airplanes for which terminal velocities are at or near the critical speed; this separation of flow will not appreciably affect the determination of the terminal velocity for highperformance airplanes for which the terminal velocity occurs at speeds well above the critical speed.

Figure 10 shows the variation of  $C_D/C_{D_{min}}$  with  $M/M_{\rm Cr}$  for several fuselage shapes and fineness ratios. The drag increments for the nacelles and windshields are presented in figures 11 and 12, respectively. The critical speeds for these bodies were based on the wings with which the models were tested and were determined for the wing-root juncture. The effect of compressibility on the rate of drag increase at speeds above the wing critical speed for these bodies is similar to that for the air-foils.

In the correlation of the average drag increases of the various components of the airplane throughout the Mach number range, a generalized drag curve was derived

¥

1

and is presented in figure 13. The data presented in figures 4, 6, 7, 8, 10, 11, and 12 were used to obtain the generalized drag curve. The generalized drag curve is an average of the drag data for the airfoils, fuselages, nacelles, and windshields at speeds up to 10 percent above the critical speed. Only the average drag of the airfoils at speeds from 10 to 15 percent above the critical speed was used. The generalized drag curve was extrapolated by use of a straight-line extrapolation from 15 to 25 percent above the critical speed. The straightline extrapolation is believed to be sufficiently accurate for estimation of the terminal velocity in this region where the drag rises rapidly due to compressibility effects.

Constriction corrections. - Corrections for constriction effects have been applied to the data. The constriction corrections have been determined from pressure measurements obtained in the Langley 24-inch and 8-foot highspeed tunnels on NACA 0012 airfoil models of various The magnitude of the corrections applied to the sizes. drag coefficients amounted to less than one-half of 1 percent of the dynamic pressure q at low speeds and increased to approximately 2 percent of q at the critical speeds and to approximately 5 percent of q at a value of the Mach number below the choking speed of the tunnel. The corrections to the Mach numbers amounted to approximately one-half of these values. The constriction corrections were such that the coefficients were reduced and the Mach numbers were increased by the values stated. The greatest percentage of increase in correction, as would be expected, occurred for the models that had the largest ratio of model area to tunnel area.

Comparison with flight data.- Figure 14 shows the variation of over-all drag coefficient with Mach number for the XP-51 airplane as measured in flight and the variation with Mach number of the wing-profile drag at the mid-semispan station measured by the wake-survey method. These flight data are preliminary as corrections to the data have not been applied. The results obtained by use of the generalized drag curve in estimating the drag increases with Mach number are also shown in figure 14 for comparison with the flight measurements of over-all drag and wing-profile-drag data of the XP-51 airplane. The curves for the wing-profile drag and the overall airplane drag in flight begin to rise rather steeply

at about the same Mach number. This fact tends to justify the assumption that the wing-root critical speed is a suitable criterion to use in terminal-velocity calculations. The estimated drag derived from the generalized drag relation indicates higher drag coefficients at Mach numbers of approximately 0.55 to 0.75 than are shown for both the measured wing-profile drag and the over-all drag coefficients. Of more importance, however, is the good agreement that is shown for the values obtained by use of the generalized drag curve and the measured flight data at Mach numbers greater than 0.75, which is the region where the terminal Mach number usually occurs.

Figure 15 shows a comparison of measured flight drag and estimated drag for the XF2A-2 airplane of reference 6. An important difference in the drag curves occurs at Mach numbers around the critical Mach number. The estimated drag indicates lower drag coefficients than do the flight measurements. This difference is believed to be due to a combination of early shock formation on the cowling and airplane-wing roughness, which is believed to have caused some separation of the flow. Good agreement is indicated between the flight measurements and the estimated drag in the region where the drag coefficients rise steeply, which is the region that determines the terminal Mach number.

# Terminal-Velocity Calculation

The generalized drag curve (fig. 13) may be used as an approximation in determining the terminal velocity of an airplane in a vertical dive. The terminal velocity is reached when the drag of the airplane is equal to the weight of the airplane. The drag of the airplane in a dive combines both airplane and propeller characteristics. In the present analysis, however, zero propeller thrust is assumed and the propeller drag or thrust is therefore neglected. At supercritical speeds the drag or thrust caused by the propeller is considered to be negligible as compared with the drag of the airplane, particularly if the pilot throttles the engine and adjusts the propeller to a high blade-angle position.

The terminal velocity for zero-lift conditions is given by the relation

NACA ACR No. 15631

$$V_{\rm T} = \sqrt{\frac{W}{S} \frac{2}{\rho} \frac{1}{C_{\rm D}}} \tag{1}$$

or, in terms of the terminal Mach number  $M_T$  with the speed of sound equal to  $\sqrt{\frac{\gamma p}{\rho}}$ ,

$$M_{\rm T} = \frac{V_{\rm T}}{a} = \sqrt{\frac{W}{S} \frac{2}{\gamma} \frac{1}{p} \frac{1}{C_{\rm D}}}$$
(2)

Equation (2) can be rewritten in the form

$$M_{\rm T} = \sqrt{\frac{W}{S} \frac{2}{\gamma} \frac{1}{p} \frac{1}{C_{\rm D_{min}}} \frac{1}{C_{\rm D}/C_{\rm D_{min}}}}$$
$$= \sqrt{\frac{2}{\gamma} \frac{W}{pSC_{\rm D_{min}}} \frac{1}{C_{\rm D}/C_{\rm D_{min}}}}$$
(3)

where  $\frac{W}{pSC_{D_{min}}}$  is constant for each airplane at the

altitude for which  $M_{\rm T}$  is calculated and

$$\frac{C_{\rm D}}{C_{\rm D_{min}}} = f\left(\frac{M_{\rm T}}{M_{\rm cr}}\right)$$

which is obtainable from the generalized drag curve. Equation (3) can then be solved for the parameter  $\frac{W}{pSCD_{min}}$ . Figure 16 shows solutions of equation (3) for

various values of  $M_{cr}$  and  $\frac{W}{pSC_{D_{min}}}$ .

In computations of the terminal velocity, the only data that must be known about the airplane are the minimum

9

drag coefficient at zero (or approximately zero) lift coefficient or a low-speed drag coefficient whereby the minimum drag coefficient can be computed by use of the generalized drag curve, the wing critical speed, and the wing loading. Values of these quantities, all of which are used in calculations other than those for the terminal velocity, are easily obtained. With these values known for a particular airplane, the parameter  $\frac{W}{pSCD_{min}}$  can be calculated for different altitudes; then, for given values of  $M_{cr}$  and  $\frac{W}{pSCD_{min}}$ , the terminal Mach number can be obtained by use of figure 16.

In order to illustrate the method of obtaining the terminal velocity graphically, the terminal velocities have been calculated for the XF2A-2, P-39N-1, and P-47 airplanes. The pertinent data for these airplanes are given in the following table:

## TABLE I

#### AIRPLANE DATA

Airplane	Mcr	C <sub>D</sub> min	W S (lb/sq ft)
XF2A-2	0.61 (flight) .66 (corrected)	0.022 (flight)	26.1
P-39N-1	0.675 (estimated)	0.018 (estimated)	34.1
р-47	0.64 (wind tunnel) .69 (corrected)	0.020 (flight)	45.0

By use of these data the parameter  $\frac{1}{100}$ 

SC<sub>Dmin</sub> is

computed for each airplane. The use of figure 16 to estimate the terminal Mach number is illustrated for the P-47 airplane at 15,000 feet altitude. The variation of

terminal Mach number with altitude thus obtained for the three airplanes is presented in figure 17.

Also included in figure 17, for comparison with the estimated variation of terminal Mach number with altitude, are records of flight data for the XF2A-2, the P-47, the P-47C-1-RE, and the P-39N-1 airplanes. The flight record for the P-47C-1-RE airplane was obtained by the late Major Perry Ritchie in a terminal-velocity dive made at Wright Field in July 1943. The points represented by circles were obtained from a dive of a P-47 airplane made by a test pilot for the Republic Aviation Corporation. Unfortunately, a complete dive history is not available for this dive but it is believed that, had one been available, it would have followed a path similar to that obtained by the late Major Ritchie for the P-47C-1-RE airplane. It is further believed that the test points obtained at altitudes of 22,000 feet and 10,000 feet represent entry into and pull-out from the dive, respectively. Data for the XF2A-2 airplane were obtained from reference 6 and the data for the P-39N-1 were obtained from dive tests made at Ames Aeronautical Laboratory. The present method for estimating the terminal Mach number yields results that compare favorably with the flight measurements; the difference between the two is no greater than 0.02 in Mach number. This method for estimating the terminal Mach number is therefore believed to be sufficiently accurate for usual engineering purposes.

The section entitled "Drag Characteristics" indicates that the NACA 230-series airfoils and airfoils similar to the NACA 230-series could exceed the critical speed by approximately 0.05 to 0.15 in Mach number before any important changes in the aerodynamic characteristics

occurred. At  $\frac{M}{M_{cr}} = 1.0$ , therefore, the NACA 230-series

airfoils and similar airfoils did not show the same percentage increase in drag as was shown for almost all the other airfoils and for the generalized drag curve. Since in the calculation of the terminal velocity the critical speed of the airplane is based on the critical speed of the wing, it can be expected that for airplanes utilizing NACA 230-series airfoil sections or similar sections the estimation of the terminal velocity will be in error. If the generalized drag curve is used in the estimation of the terminal velocity, the indicated wing

critical speed must be increased approximately  $7\frac{1}{2}$  percent

for the NACA 230-series sections. This correction was applied to the critical speeds of the P- $\frac{1}{47}$  and XF2A-2 airplanes (see table I), since these airplanes have NACA 230series sections. The dashed curve on figure 17 for  $M_{\rm Cr} = 0.64$  is the result obtained if the indicated critical Mach number is used rather than the effective critical Mach number, which is about  $7\frac{1}{2}$  percent higher.

Langley Memorial Aeronautical Laboratory National Advisory Committee for Aeronautics Langley Field, Va.

## REFERENCES

- 1. Robinson, Russell G., and Wright, Ray H.: Estimation of Critical Speeds of Airfoils and Streamline Bodies. NACA ACR, March 1940.
- 2. Heaslet, Max. A.: Critical Mach Numbers of Various Airfoil Sections. NACA ACR No. 4618, 1944.
- Becker, John V.: High-Speed Tests of Radial-Engine Nacelles on a Thick Low-Drag Wing. NACA ACR, May 1942.
- 4. Delano, James B., and Wright, Ray H.: Investigation of Drag and Pressure Distribution of Windshields at High Speeds. NACA ARR, Jan. 1942.
- 5. Becker, John V.: High-Speed Wind-Tunnel Tests of the NACA 23012 and 23012-64 Airfoils. NACA ACR, Feb. 1941.
- Rhode, Richard V., and Pearson, H. A.: Observations of Compressibility Phenomena in Flight. NACA ACR No. 3D15, 1943.

- - - - - 🚒

12



Plan-view profile Circular cross section Nacelle 2 Nacelle | Circular cross section Elliptical cross section Nacelle 3 Nacelle 4 Circular cross section Nacelle 5 NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS Figure 2.- Nacelles tested. (Designations from reference 3.)

Fig. 3



4

÷



Figure 4. - Variation of ratio Co/Comin with M/Mcr for NACA 0009 and 0012 airfoils.

●「 」、「」など」などを受

Figs. 5,6



Figure 5. - Variation of ratio CD/CDMIN with M/Mcr for three conventional NACA airfoils.



Figure 6.- Variation of ratio Co/Comin with M/Mcr for NACA 16-509 and 16-515 airfoils. Transition fixed at 0.10 chord.





(b) Transition fixed at 0.40 chord, Figure 7 - Variation of ratio C<sub>D</sub>/C<sub>Dmin</sub> with M/M<sub>cr</sub> for several NACA airfoils.

Fig. 8





÷

Fig. 9

:





Fig. 10













L5G31 . NACA ACR No.



Figure 13. - Generalized drag curve.

Fig. 13

No. To Calendary



Figure 14.- Variation of measured flight drag and estimated drag with Mach number for XP-51 airplane.



Figure 15.- Variation of measured flight drag and estimated drag with Mach number for XF2A-2 airplane.







۲ig.