TECHNICAL MEMORANDUMS

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

No. 562

EXPERIMENTAL INVESTIGATION OF AIRCRAFT PROPELLERS

EXPOSED TO OBLIQUE AIR CURRENTS

By O. Flachsbart and G. Kröber

From Zeitschrift für Flugtechnik und Motorluftschiffahrt
December 14, 1929

Washington
April, 1930

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EXPERIMENTAL INVESTIGATION OF AIRCRAFT PROPELLERS

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Summary

Two screw propellers, a normal airplane propeller with a
pitch/diameter ratio $H/D = 0.5$ and a helicopter propeller
$H/D = 0.2$, were tested in the large wind tunnel of the Göttin-
gen Aerodynamic Institute. With both propellers the angle be-
tween the propeller axis and the direction of the wind was var-
ied from 0 to 90°. In addition to the three force and the three
moment components in a wind-fast coordinate system, the corre-
sponding components in a propeller-fast coordinate system, a
total of six force and six moment components, together with the
propulsive efficiency, were measured or calculated from measure-
ments. The results are given in the form of diagrams and brief-
ly discussed. The propeller models and method of experimenta-
tion are described and the symbols are defined.

Introduction

Under normal operating conditions any propelled craft moves
so that the direction of the relative flow is exactly or very

nearly in the direction of the propeller axis. These conditions are the normal straightaway flight of an airplane, the vertical ascent and descent of a helicopter and the straightaway motion of a ship. Since these conditions predominate in practice, they have been made the principal objects of theoretical and experimental investigation.

All propelled craft sometimes come, however, into positions in which the direction of the relative flow deviates considerably from the direction of the propeller axis. The principal cases are:

1. Curving motion of all propelled craft. The angle between the propeller axis and the relative flow (hereinafter called the angle of flow and designated by α) is inversely proportional to the radius of the curve.

2. The horizontal flight of a helicopter, in which the horizontal motion is produced by inclining the propeller axis. On such a helicopter the propeller performs the dual function of vertical lift and horizontal propulsion. The resulting angle of flow (α) is large in comparison with case 1.

In 1914, Bramwell, Relf and Bryant, in wind-tunnel experiments with propellers exposed to oblique air currents, measured the thrust components parallel and perpendicular to the propeller axis at flow angles of $\alpha = 0$ to 25° * Similar measurements

*"Experiments to Determine the Lateral Force on a Propeller in a Side Wind." British A.C.A. Reports and Memoranda No. 123, Part II.

were recently made at the Junkers factory.* These experiments
cover the angles of flow in curving motion (case 1). Of course
they also cover the effect of the oblique flow in those cases
in which the relative flow is generally assumed with sufficient
accuracy to be axial. These cases include the straightaway
flight of an airplane whose propeller axis has a direction dif-
ferent from the direction of flight, inverted flight, the flow
relations in certain arrangements of the propeller above or be-
low the wings and similar cases.

In order to determine the behavior of propellers under the
operating conditions of case 2, Durand and Lesley investigated,
in 1921, a series of propellers of different H/D ratios (0.3,
0.5, 0.7) at angles of flow of $\alpha = 60$ to 90° in a wind tunnel
and determined the axial thrust and the torque.** Margoulis
has recnelty investigated helicopter-propeller models in a lat-
eral wind.***

Since the former of the above-mentioned cases (oblique flow
against airplane propellers) relates to small angles of flow and
the latter (oblique flow against helicopter propellers) relates
to large angles of flow and hence practically cover the range
from $\alpha = 0$ to 90°, and since, moreover, the quantities measured

*Bock, "Ueber die Einheit von Triebwerk und Flugwerk," Year-
book of the W.G.L., 1928, p.66.
**Durand and Lesley, "Tests on Air Propellers in Yaw." N.A.C.A.
Technical Report No. 113, 1921.
***Margoulis, "Les hélicoptères," Paris, 1922; "Nouvelles re-
cherches expérimentales sur les hélices d'hélicoptères," Comptes
Rendus 184, 1927, p.735.

by the earlier experimenters are limited in all cases to a por-
tion of the thrust components and moments, the authors general-
ized the problem according to the behavior of a propeller in a
side wind and undertook the task of investigating screw propel-
lers of different pitch in the wind tunnel at angles of flow of
0 to 90°. In addition to the propulsive efficiency, all forces
and moments in a wind-fast system and in a propeller-fast system
of coordinates were to be investigated.

The Propellers Tested

Two propeller models of the same diameter D, but of dif-
ferent pitch H, were tested.

1. An airplane propeller model of uniform pitch $H = 0.5 D$
throughout the whole radius (Fig. 1). The propeller was of the
type $S_1 F_2 A_1 P_1$ of the N.A.C.A. reports.*

2. A helicopter propeller with a uniform pitch of $H = 0.2$
D over the greater (outer) part of the radius (Fig. 2).

The diameter of both propellers was $D = 0.32$ m (12.6 in.).
They were made from a block of glued strips of wood, like full-
size propellers. In reporting the results, the propellers are
simply designated as I and II.

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*Durand and Lesley, "Experimental Research on Air Propellers-V."
N.A.C.A. Technical Report No. 141, 1925.

Suspension of Model

Both propeller models were tested in the large wind tunnel of the Göttingen Aerodynamic Institute. A small high-speed Göttingen electric motor of the type C was used to drive them.* The suspension in the wind tunnel is shown in Figures 3 and 4. The plane, in which the propeller axis can be adjusted, is the vertical plane of symmetry of the air stream. In only one case, in measuring the vertical moment, was it necessary, for technical reasons, to mount the propeller so it could be tilted in the middle horizontal plane of the air stream (Fig. 5). Before considering the experiments we must define the forces and moments.

Definitions and Notation

We will first express all the forces and moments as nondimensional and will use the following formulas.

Force or thrust coefficient

$$k_s = 100 \; \frac{\text{force}}{\frac{\rho}{2} \left(\frac{D}{2} \omega\right)^2 \; \frac{D^2 \pi}{4}}$$

Moment coefficient*

$$k = 100 \; \frac{\text{moment}}{\frac{\rho}{2} \left(\frac{D}{2} \omega\right)^2 \; \frac{D^2 \pi}{4} \; \frac{D}{2}}$$

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*"Ergebnisse der Aerodynamischen Versuchsanstalt zu Göttingen," Report III, 1927.
**These coefficients are 100 times those ordinarily used in propeller aerodynamics. It is customary to employ the propeller coefficients, like the wing coefficients, as 100 times the ordinary coefficients, on account of the smallness of the latter (e.g., 100 c_a and 100 k_d). In order not to be obliged to use this numerical factor 100 in the numerous diagrams in which the test re-
(For remainder of footnote, see bottom of page 6.)

ρ, density of surrounding medium $(kg \ s^2 \ m^{-4})$;

D, propeller diameter (m);

ω, angular velocity of propeller $\pi n/30$, when $n =$ its r.p.m. (s^{-1}).

In order to save trouble, it is allowable, instead of speaking of the force and moment coefficients k_s and k, simply to say the force (or thrust) k_s and the moment k.

All components are designated by a subindex. Since the thrust symbol already has the subindex s, we can easily distinguish the thrust forces and moments by using two subindices (e.g., k_{s_n} for the thrusts and only one for the moments (e.g., k_d).

Let us now imagine (Figs. 6-7) a wind-fast right-hand orthogonal system of axes XYZ so oriented that the X axis is in the direction of flow and the XZ plane is the vertical plane of symmetry in the air stream. With this system of axes we combine the propeller-fast system of axes $X'Y'Z'$ in such manner that the axis around which the propeller swings (the Y' axis) coincides with the Y axis. The adjustment plane of the propeller (the X'Z' plane) then lies in the XZ plane. Hence we can convert the wind-fast system of axes XYZ into the propeller-fast system of axes $X'Y'Z'$ by rotation about the Y axis by the angle of flow α.

According to this definition of the system of axes, the forces and moments, exerted on the propeller by the air, are as

sults are shown, the authors decided to use the above modified formula.

follows.

Wind-fast system of coordinates XYZ.

Forces:

k_{s_h}, horizontal thrust (thrust component in X direction);

k_{s_v}, vertical   "   ("   "   " Z   "   );

k_{s_s}, lateral   "   ("   "   " Y   "   ).

Moments (with reference to the axis point of the forward tangen-
tial plane of the propellers - Figures 1-2):

k_q,   lateral moment (moment about an axis in the direction
of flow = moment about the X axis);

k_k,   moment of yaw (moment about vertical axis = moment
about Z axis;

k_h,   vertical moment (moment about swing axis = moment
about Y axis).

Propeller-fast System of Coordinates X'Y'Z'

Forces:

k_{s_a}, axial thrust (thrust in the direction of the propel-
ler axis = thrust in X' direction;

k_{s_n}, normal thrust (thrust in Z' direction);

k_{s_s}, lateral   "   ("   " Y'   "   ).

Moments (with reference to the axis point of the forward tan-
gential plane of the propellers, Figs. 1-2):

k_r,   moment of roll (moment about the propeller axis =
moment about X' axis);

k_g,   moment of yaw (moment about Z' axis);

k_h,   vertical moment (moment about Y' axis).

The fact that the lateral thrust k_{s_s} and the vertical mo-
ment k_h coincide in both coordinate systems, is due to the
identity of the Y and Y' axis.

The rolling moment k_r exerted on the propeller by the
air forces, is obviously equal and opposite to the turning mo-
ment transmitted from the motor to the propeller. This turning
moment is expressed by k_d in the usual manner. Therefore, if
we define the positive k_d direction in opposition to the posi-
tive k_r direction, $k_r = k_d$ in every direction.

Moreover, if we define the efficiency of propulsion

$$\eta = \frac{k_{s_h}}{k_d} \lambda,$$

in which λ = velocity of flow v/peripheral velocity of blade
points u = pitch angle of propeller.

Experimental Method

The measured forces and moments are compared in the follow-
ing survey. The accompanying numbers refer to the wires leading

from the model to the balances in Figure 3.   They show how the quantities in question are measured.

   Measured thrust components:

   k_{s_v},   vertical thrust . . . . (3 + 4) + 5

   k_{s_h},   horizontal "   . . . .   1 + 2

   k_{s_s},   lateral   "   6

   Measured moments:

   $k_d(= k_r)$, turning moment (= rolling moment) . . .   7

   k_q,   lateral moment . . . . 3 - 4

   k_h,   vertical moment, measured with special suspension.

As shown in Figure 5, the plane of adjustment in the horizontal plane of the wind tunnel was such that the vertical moment could be measured by 1 - 2.

   The propeller speed, which averaged about 6500 r.p.m., was determined by the observation of a rotating mark actuated by the motor with a reduction of 1 : 400 and designated by 8 in Figure 3.

   In order to be able to eliminate the effect of the motor and of the suspension in the evaluation of the measurements, a comparative test had to be made without the propeller for all quantities excepting the turning moment and r.p.m. The desired quantity is then found from the difference between the main measurement (with propeller) and the comparative measurement (without propeller). This difference, which is unavoidable in

all force measurements in wind tunnels when the action of the
air forces on only a portion of the whole installation (on the
model alone) is to be studied, can, with the means now at our
disposal, be determined with satisfactory accuracy for models
at rest. There are unavoidable errors in the investigation of
independently running propellers, as always in the investigation
of moving models, since parts of the installation, whose resist-
ance is supposed to be eliminated by the comparative measure-
ment, lie in the accelerated slipstream of the propeller, while
exposed to a flow of less velocity in the comparative test.
The result is a greater or smaller deviation of the measured
quantities from the actual data of the isolated propeller.
Recent propeller-model testing stands render it possible to keep
this deviation very small in testing propellers exposed to ax-
ial currents. Since, in our investigations with a lateral wind,
the installations were necessarily more bulky, it was to be ex-
pected that the deviations would increase. A control test for
$\alpha = 0^{\circ}$ on the propeller-testing stand showed, however, that
they are generally small (Fig. 8). These deviations are negli-
gible in the comparison of the propeller curves obtained at dif-
ferent angles of flow.

During the first tests it was found necessary to measure
the three quantities separately:

1. The lateral thrust k_{s_s}, since the torque wire 7 in
Figure 3 disturbed the measurement. (It was removed for the

measurement of k_{s_s}.);

2. The lateral moment k_q, since the arrangement of the balances prevented the simultaneous measurement of k_q and k_{s_v};

3. The vertical moment k_h, which can be computed from k_{s_v} and k_{s_h}, but only inaccurately, since small discrepancies necessarily occur in measuring large quantities and the results are therefore considerably scattered. It was therefore preferred to determine k_h with the aid of a special experimental suspension (For this purpose the adjustment plane of the propeller axis had to be located in the middle horizontal plane of the wind tunnel).

The whole series of experiments was therefore divided as follows:

Simultaneous measurements of vertical thrust k_{s_v}, horizontal thrust k_{s_h}, and turning moment (torque) k_d;

Separate measurements of lateral thrust k_{s_s}, lateral moment k_q and vertical moment k_h.

In measuring the lateral thrust, there were strong disturbances of the flow about the motor and consequent strong lateral oscillations of the motor-propeller assembly. These ceased, however, when two vertical guide surfaces were installed on the upper side of the motor.

It was the intention of the authors to measure many components directly and to calculate only those (k_{s_a}, k_{s_n}, k_g)

which could not be measured due to the arrangement of the bal-
ances.

In general, the measurements proved feasible as planned,
although there were technical difficulties in individual cases
due to the smallness of the forces. All the vectors from the
X and X' directions disappear (on account of the symmetry) at
$\alpha = 0^\circ$. Hence they are very small at small angles of flow.
Only the measurement of the moment of yaw k_k failed on account
of these difficulties. This was determined graphically from
k_r and k_q. Figure 7 shows the vectorial relations of the three
quantities.

Evaluation of the Measurements and
Representation of the Results

In the evaluation of the test results it was found that
the measurements for small forces varied considerably. Most of the
the measured curves were therefore determined twice in the fol-
lowing manner:

1. The balance readings were made nondimensional without
regard to the comparative test, with α plotted as parameter
against λ and the scatterings averaged by eye.

2. From these curves the corrected test values were taken
for a given value of λ and plotted against α. After another
averaging of the now much smaller variations, the test values
were again plotted backward against λ.

With these mean values, further calculations were made, the comparative measurements and calibration were introduced, etc. This double plotting was found necessary for k_{s_h}, k_{s_v}, k_d, and k_q, while k_{s_s} and k_h could be measured directly.

Altogether there were measured:

Forces: k_{s_h}, k_{s_v}, and k_{s_s};

Moments: k_q, k_h, and $k_d = k_r$.

The thrust forces k_{s_a} and k_{s_n} were graphically determined from the measured forces k_{s_v} and k_{s_h}. The geometrical relation of the vectors is shown by Figure 6. Moreover, the moments k_k and k_g (Fig. 7) were obtained from the graphic combination of the measured moments k_r and k_q. Lastly, the efficiency

$$\eta = \frac{k_{s_h}}{k_d} \lambda,$$

was calculated, so that altogether the following quantities were determined mathematically:

Forces: k_{s_a} and k_{s_n};

Moments: k_k and k_g;

Efficiency: η :

Figures 9-30 represent all the force and moment components and the efficiency for propellers I and II, both as plotted against the pitch angle λ with the flow angle α as parameter and against α with λ as parameter. On account of the equality $k_d = k_r$, the latter was not plotted, but only the torque k_d.

exception of Figure 8, the introduction of the measuring points was omitted for the sake of clearness.

In the somewhat arbitrary elimination of the scattering by the above-described double averaging, controls were desired for the individual components. Hence the following connections derived from the geometric relations (Figs. 6-7) were investigated and confirmed.*

For the forces:

For $\lambda = 0$, k_{s_n} must disappear at all oblique angles of flow and k_{s_a} assume the value

$$k_{s_a} = \sqrt{k_{s_v}^2 + k_{s_h}^2} = \text{constant}$$

For $\alpha = 0°$, $k_{s_v} = 0$, $k_{s_n} = 0$, and $k_{s_s} = 0$ at all pitch angles;

For $\alpha = 90°$, $k_{s_n} = -k_{s_h}$ and $k_{s_a} = k_{s_v}$ at all pitch angles.

For the moments:

For $\lambda = 0$, k_g and k_h must disappear for all angles of flow and $k_r(= k_d)$ must assume the value

$$k_r = \sqrt{k_k^2 + k_q^2} = \text{constant}$$

For $\alpha = 0°$, k_h and k_g become zero at all pitch angles;

For $\alpha = 90°$, $k_k = k_r(= k_d)$ and $k_g = -k_q$ at all pitch angles.

*Moreover, we have compared our results, so far as possible, with the results of previous experimenters and found the agreement good. Perhaps there will be opportunity to compare our experimental results with the theoretical results of Pistolesi and Misztal.

Remarks on the Results

The most important points concerning the relations of the individual components were mentioned in the preceding section. It only remains to consider the results (Figs. 9-30). It must be assumed in advance that the effect of the obliqueness of the flow on the behavior of the propeller, in the region of $0° < \alpha <$ about $15°$, is negligible both for airplane propellers and for helicopter propellers. A comparison of the corresponding curves for airplane and helicopter propellers show an extensive agreement in their character. The diagrams must be examined for details. Attention is called to the following points.

Thrusts k_{s_a}, k_{s_v}, k_{s_h}, k_{s_n}, k_{s_s}

k_{s_a} - The constant axial thrust at $\lambda = 0$ decreases with the pitch angle at small angles of flow α and increases at larger angles α with the pitch angle. There is an intermediate region, at $\alpha =$ about 70 to $80°$, in which k_{s_a} (as also k_{s_s}) is almost independent of the pitch angle (Figs. 9-10).

k_{s_v} - Since the axial thrust k_{s_a} is negative at large λ, the vertical thrust k_{s_v} is also negative at small angles of flow α. The vertical thrust k_{s_v} becomes positive again at large angles of flow, since the axial velocity is smaller, and the axial thrust consequently becomes positive again (Figs. 11-12).

k_{s_h} – For similar reasons it follows, in agreement with the test results, that in the region of large λ, the horizontal thrust at small angles of flow is negative, while it is positive at large angles of flow. At $\alpha = 90^{\circ}$, there is only resistance (Figs. 13-14).

k_{s_n} – The normal thrust increases both with the pitch angle and with the angle of flow. Only at small λ the initial increase at large angles $(\alpha > 45^{\circ})$ recedes. The forces are much smaller than those previously mentioned, the maximum value being only $k_{s_n} = 0.8$. For the sake of clearness the curves were plotted so that the scale is five times as great as for k_{s_a}, k_{s_v}, and k_{s_h} (Figs. 15-16).

k_{s_s} – The lateral thrust is still smaller, its maximum value for the airplane propeller being only $k_{s_s} = 0.5$; and for the helicopter propeller only $k_{s_s} = 0.4$. There is a strong increase with the pitch angle, increasing at first with the angle α, then dropping to zero at about $\alpha = 85^{\circ}$ and then becoming negative. The scale of the diagram is likewise enlarged fivefold (Figs. 17-18).

Moments k_d, k_h, k_k, k_q, k_g

k_d – While for $\lambda = 0$ there is naturally no dependence of the rolling moment on the angle of flow, at large pitch angles the moment increases rapidly with increasing angle of flow, and

at $\alpha > 50^\circ$ the moment measured in the stand test does not recede again (Figs. 19-20).

k_h - The vertical moment shows a surprisingly uniform increase both with the angle of flow and with the pitch angle (Figs. 21-22).

k_k - The dependence of the moment of yaw on the pitch angle is only slight. More pronounced is the increase with the angle of attack (approximately as the sine) (Figs. 23-24).

k_q - The lateral moment at $\alpha = 0^\circ$ follows the course of the rolling moment. At $\alpha = 90^\circ$ it is identical with the negative moment of yaw, the transition being gradual (Figs. 25-26).

k_g - The moment of yaw shows quite a uniform dependence on the angle of pitch. With increasing angle of attack it becomes negative after an initial increase (Figs. 27-28).

Efficiency

η - For an airplane propeller the efficiency of propulsion attains a maximum of almost 75%. Since, as referred to like ordinates of the k_{s_h} and k_d curves, smaller pitch angles of helicopter propellers correspond to larger ones of airplane propellers, the propulsive efficiency, which is a function of the pitch angle, is smaller for the helicopter propeller, the maximum value of η being about 0.48 for the latter. For simple hel-

icopter propellers $-\alpha = 0^{\circ}$ and $\lambda = 0$ -, from which no work of transportation is required, the propulsive efficiency = 0 according to our definition (Figs. 29-30).

For estimations it is of advantage to know that, in plotting against λ in an angular range of $0^{\circ} < \alpha <$ about 45°,* the k_{s_a} curves have approximately equal ordinates for equal values $\lambda \cos \alpha$. The same statement holds true for k_d. In the above-mentioned angular range, we can therefore convert the k_{s_a} and k_d curves measured for $\alpha = 0^{\circ}$ into the corresponding curves for any angle of flow α_i, by multiplying their abscissas by $\frac{1}{\cos \alpha_i}$.** Since the normal and lateral components of the propeller thrust can be disregarded in the first approximation and it may therefore be assumed that the resulting propeller thrust is in the propeller axis even at $\alpha \neq 0^{\circ}$ and is therefore identical with k_{s_a}, this method of calculation enables the determination of the quantities k_{s_a}, k_{s_v}, k_{s_h}, k_d and η, for any values of α within the limits $0^{\circ} < \alpha <$ about 45°, from the measured axial thrust and torque for $\alpha = 0$, for propellers of not too great pitch.

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*The upper limit falls with increasing pitch of the propeller. For the helicopter propeller II, 60° might be allowed for the upper limit, but 45° is fully high enough for the airplane propeller I.

**Or, which amounts to the same thing, the k_{s_h} curve, since k_{s_a} and k_{s_h} are identical at $\alpha = 0$.

Translation by Dwight M. Miner,
National Advisory Committee
for Aeronautics.
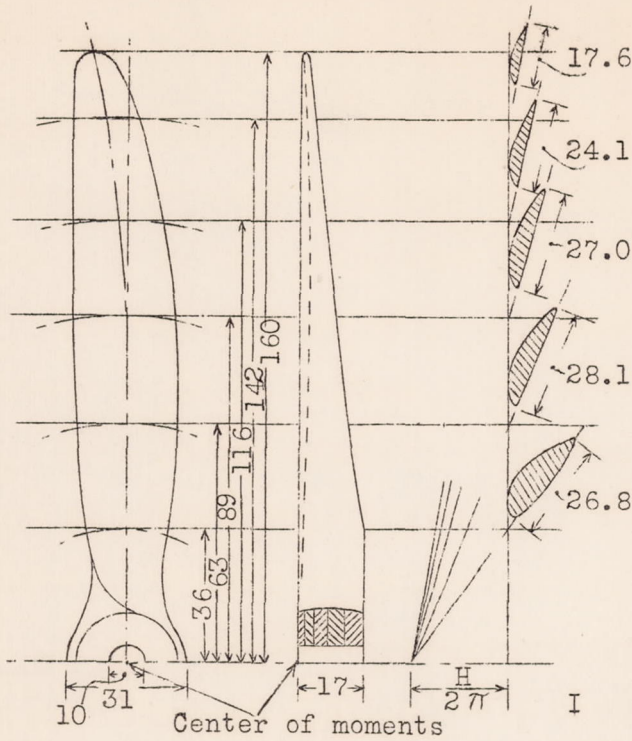
Fig.1 Airplane propeller
       (All measurements
in mm).

Center of moments

Fig.2 Helicopter propeller.
       (All measurements
        in mm).
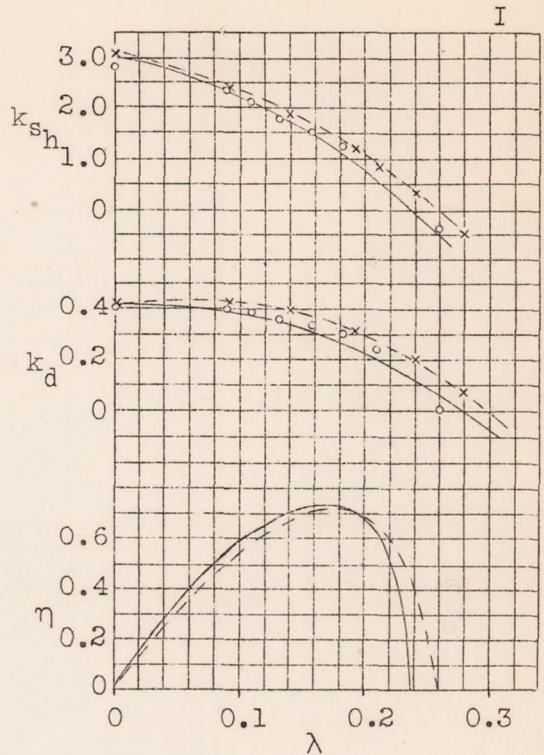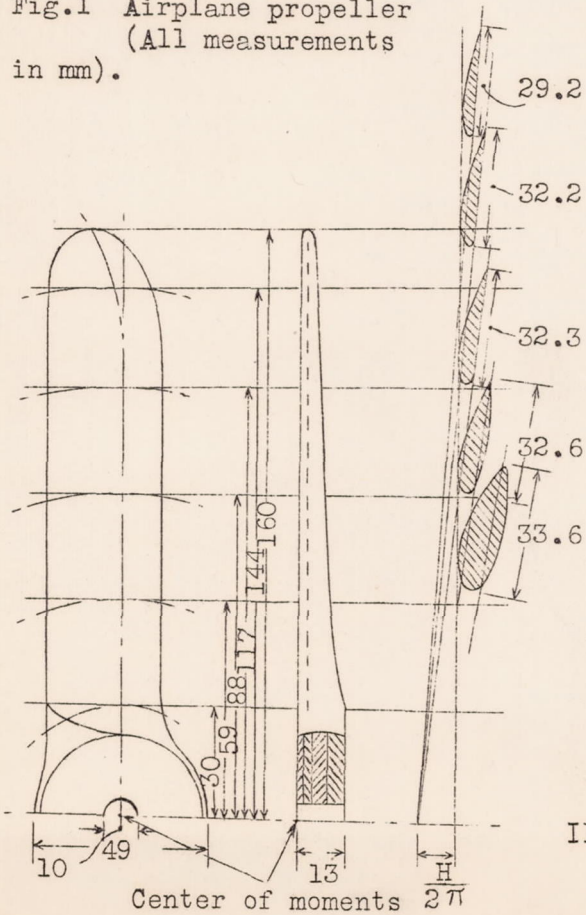
×-----× Propeller-test stand
          results.
o-------o Wind tunnel tests
          with oblique air
          currents.

Fig.8 Effect of support on test
       results. (Airplane prop. I
       at $\alpha = 0°$)
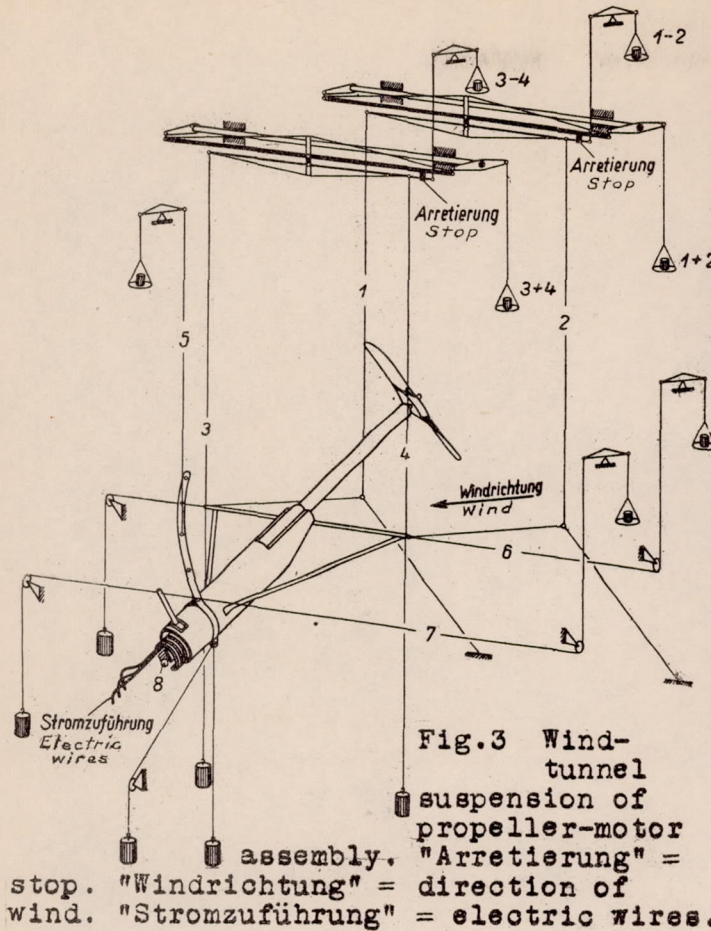
Fig.3 Wind-tunnel suspension of propeller-motor assembly. "Arretierung" = stop. "Windrichtung" = direction of wind. "Stromzuführung" = electric wires.
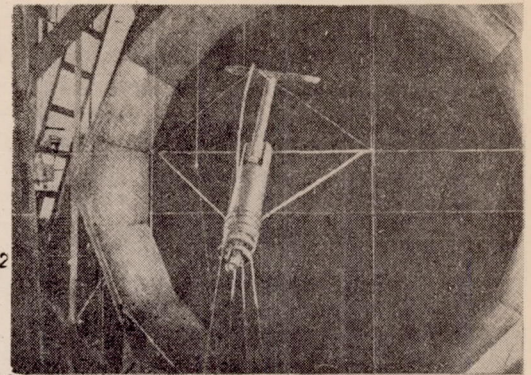
Fig.4 Wind-tunnel suspension of propeller-motor assembly.
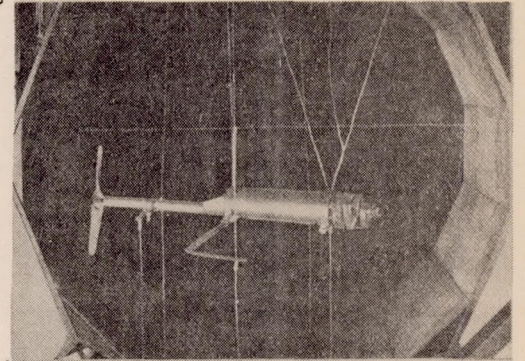
Fig.5 Special suspension for measuring vertical moment k_h.
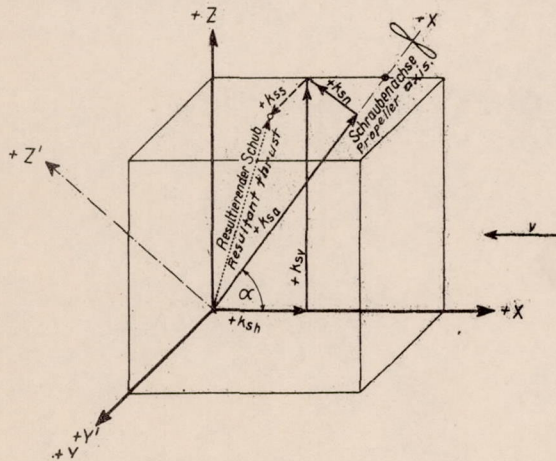
Fig.6 Thrust force.

The propeller axis lies in the XZ plane. The force vectors lie in the same plane. The dot and the dash vector fall out of the XZ plane. The cube is drawn in order to facilitate the spatial representation. Its edges were arbitrarily given a value of k_{s_v}.
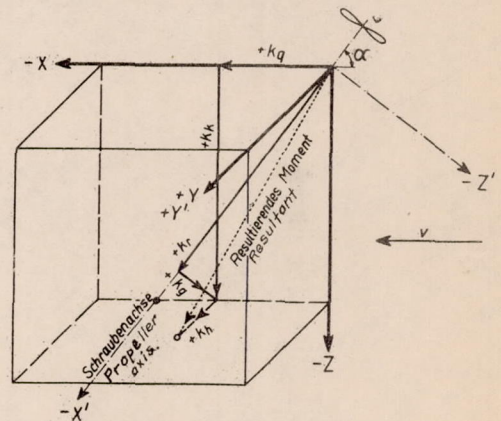
Fig.7 Moments.

The moment vectors are drawn in the usual way, so that the direction of motion indicated by the arrow, combined with the direction of rotation of the moment, produces a rotation to the right. The propeller axis lies in the XZ plane, as also the extended moment vectors. The dot and the dash vectors fall out of the XZ plane. The length of an edge of the cube is k_k.
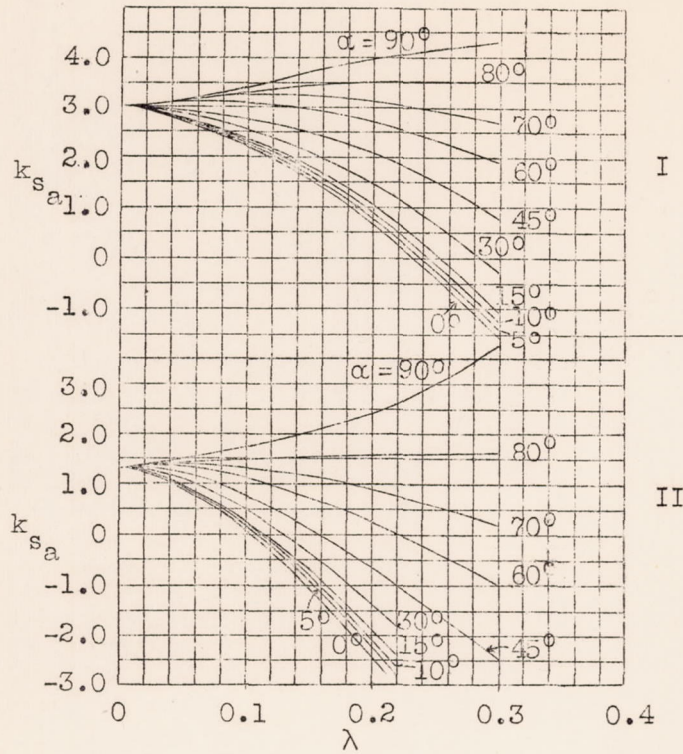
Fig.9

Axial thrust

plotted
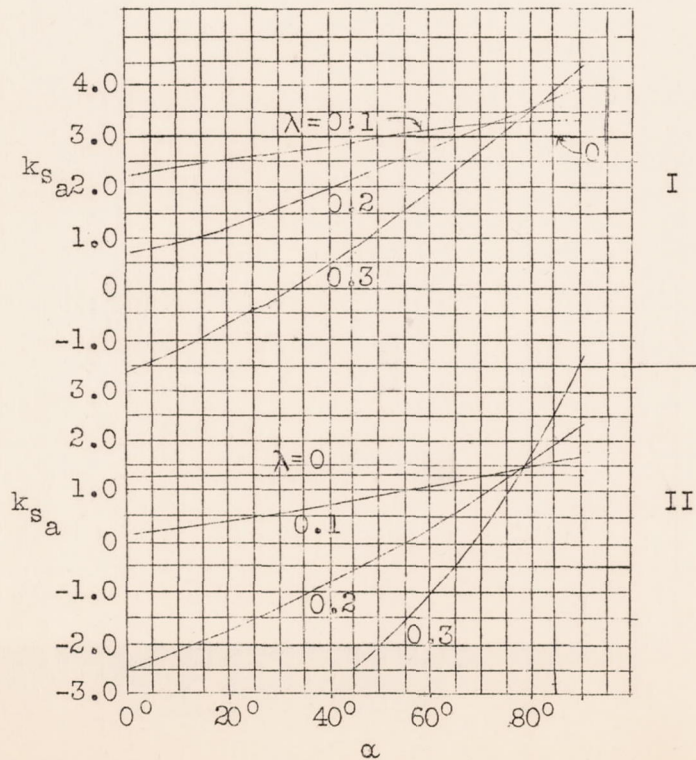
against λ

Fig.10

Axial thrust

plotted
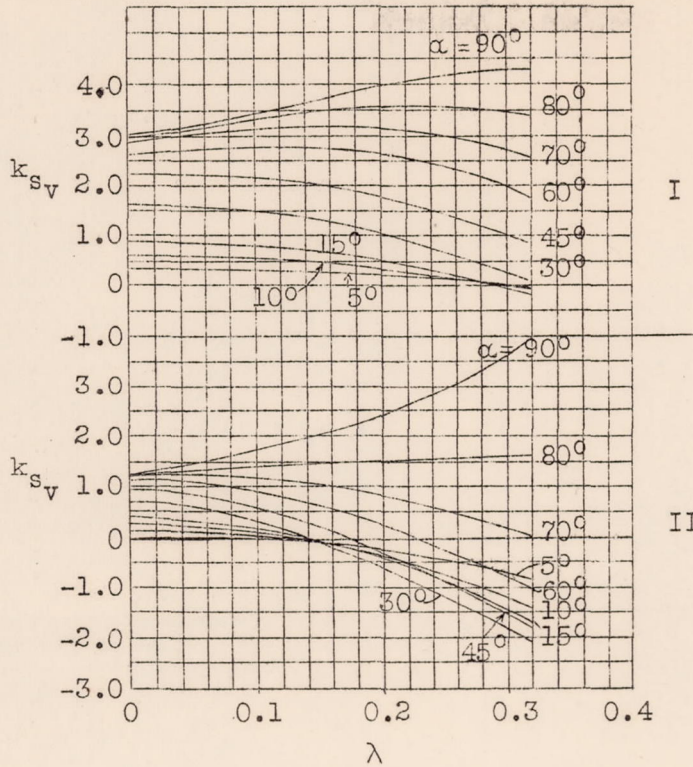
against α

Fig.11

Vertical thrust

plotted against

λ
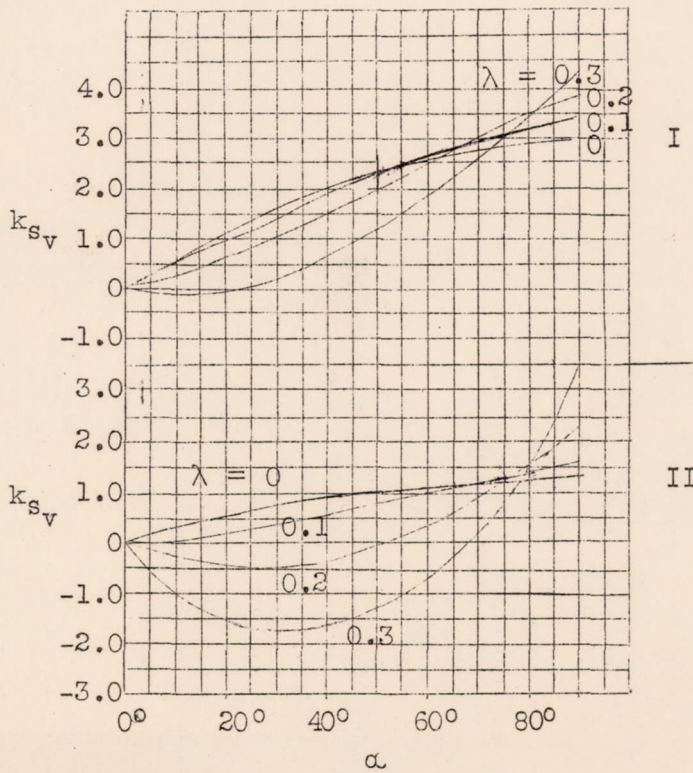
Fig.12

Vertical thrust

plotted against

α
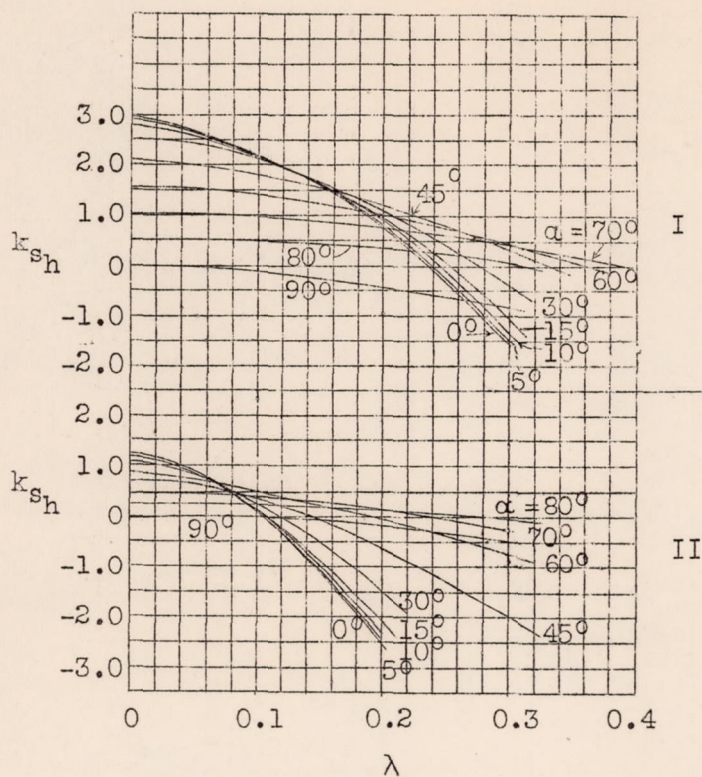
Fig.13

Horizontal thrust

plotted against

λ
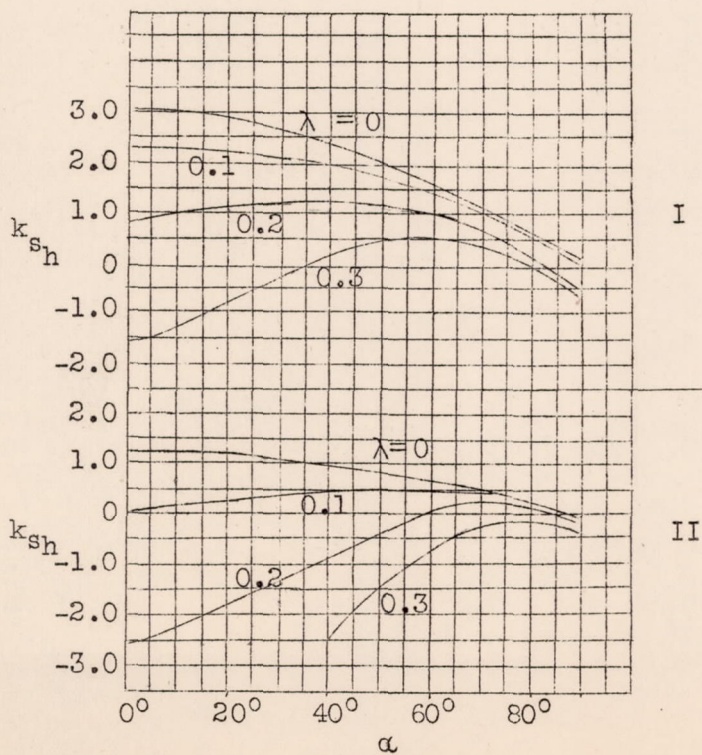
Fig.14

Horizontal thrust

plotted against

α
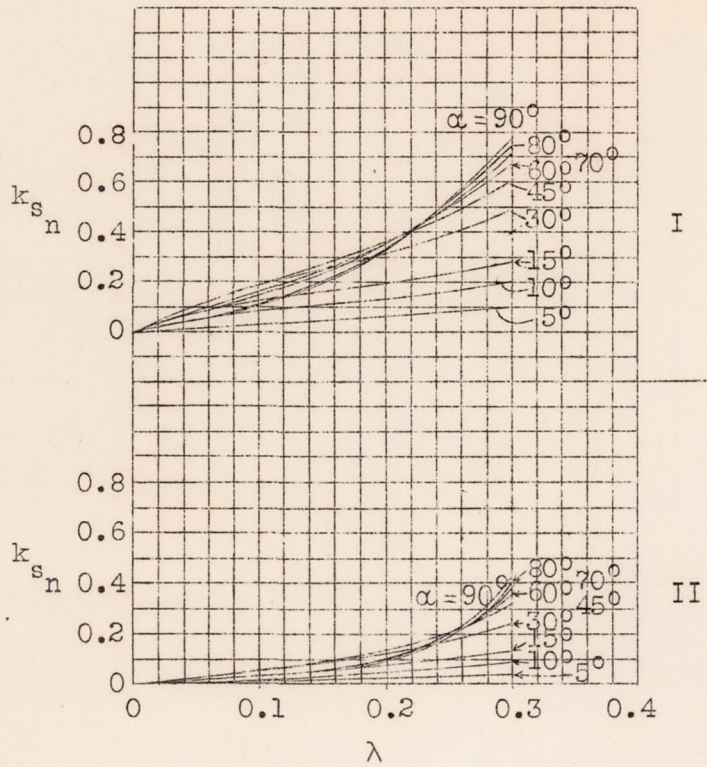
Fig.15

Normal thrust

plotted against

λ
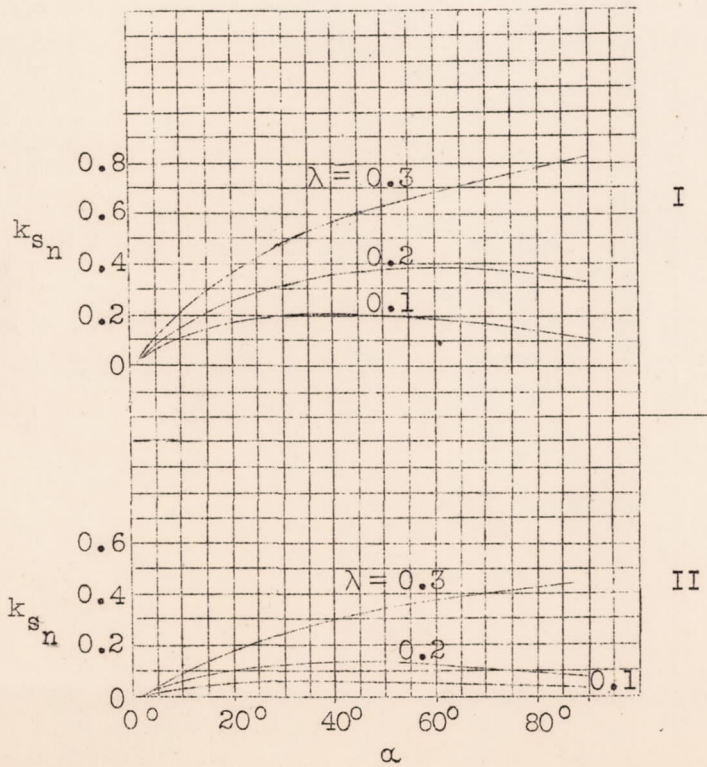
Fig.16

Normal thrust

plotted against

α
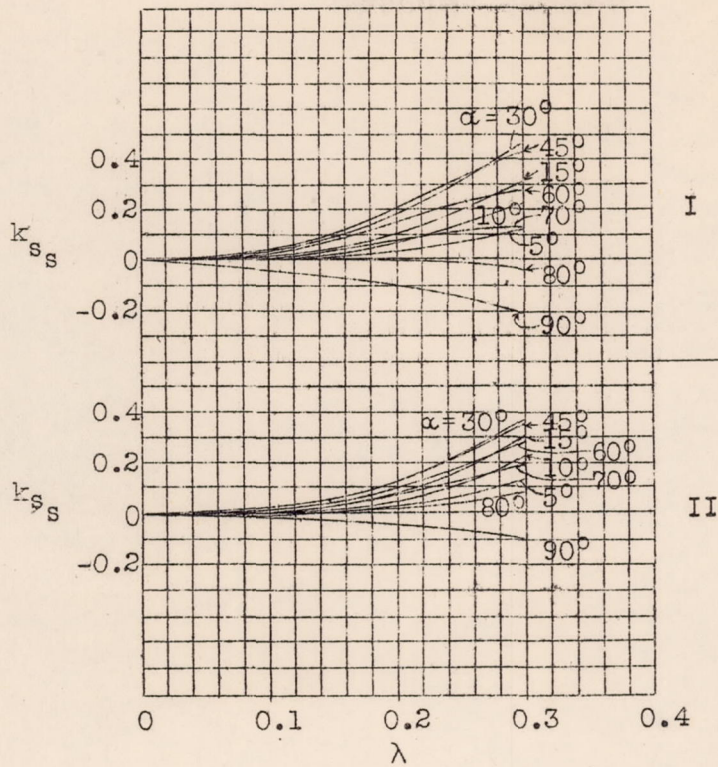
Fig.17

Lateral thrust

plotted against

λ
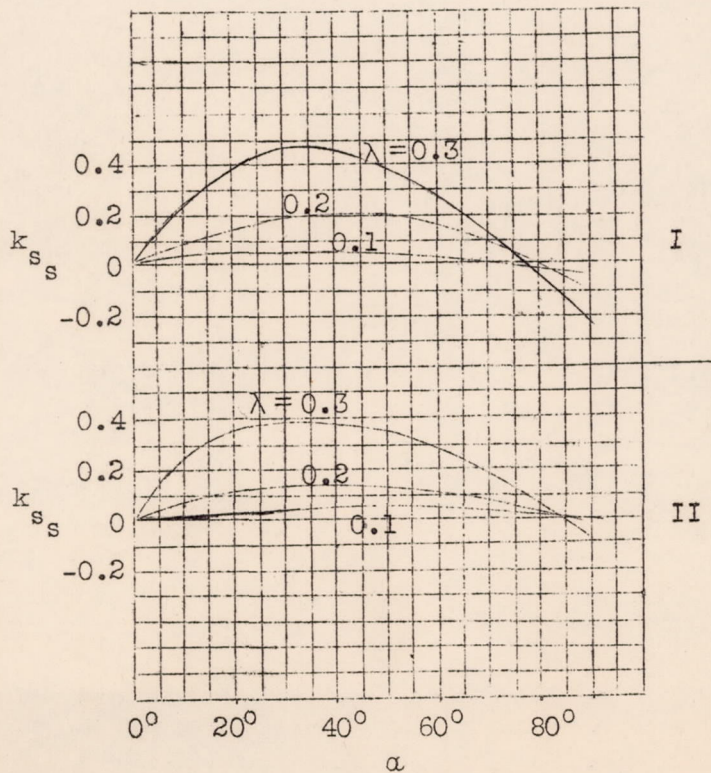
Fig.18

Lateral thrust

plotted against

α
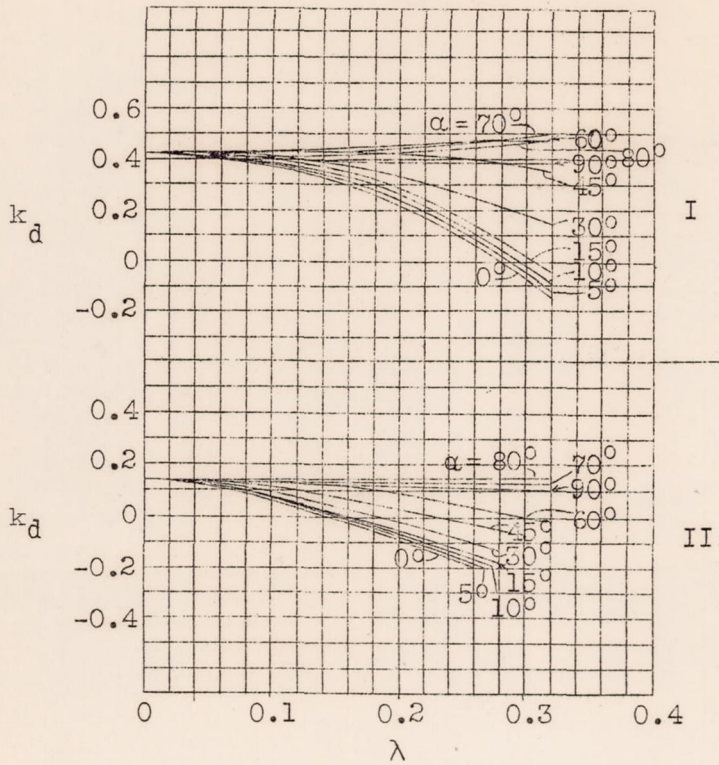
Fig.19

Torque moment

plotted against

λ
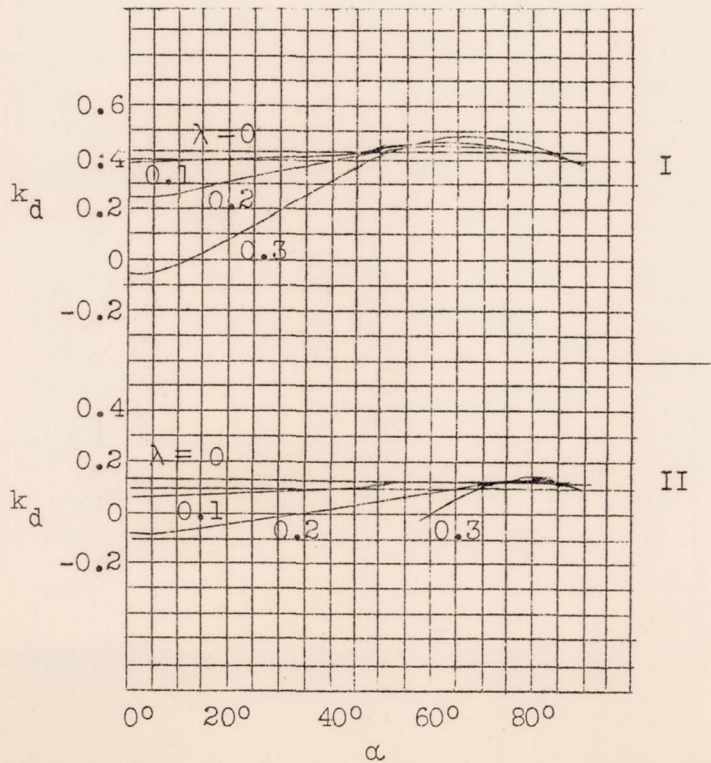
Fig.20

Torque moment

plotted against

α
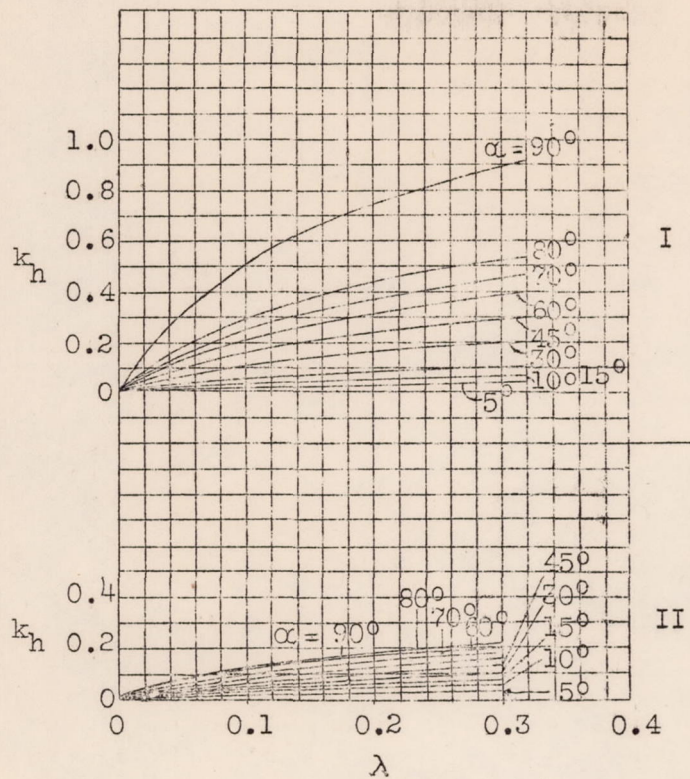
Fig.21

Vertical moment

plotted against

λ
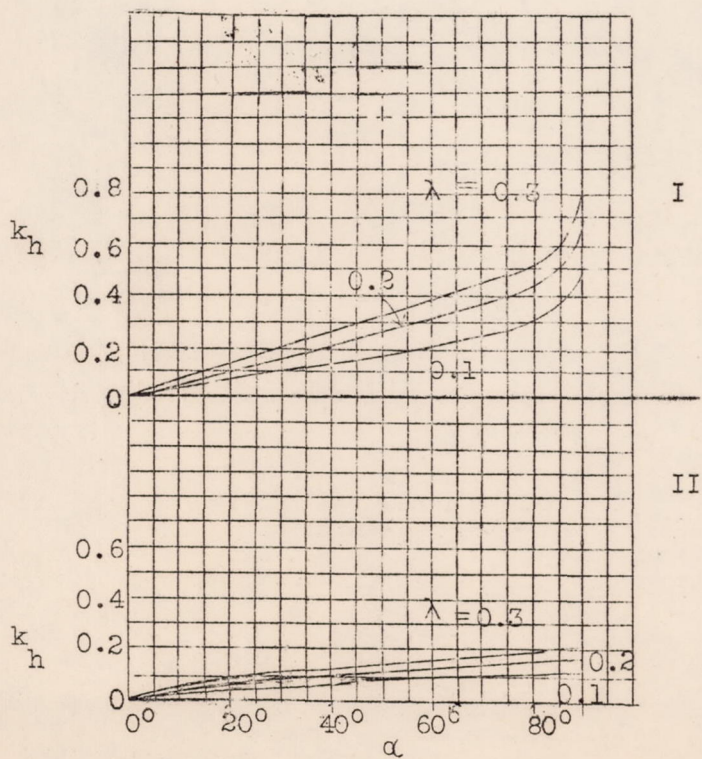
Fig.22

Vertical moment

plotted against

α
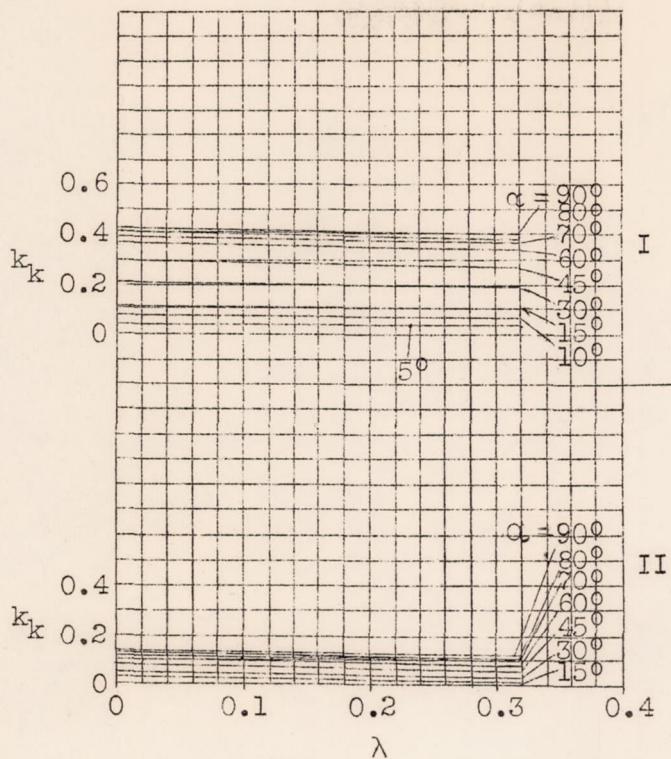
Fig.23

Moment of yaw

plotted against

λ
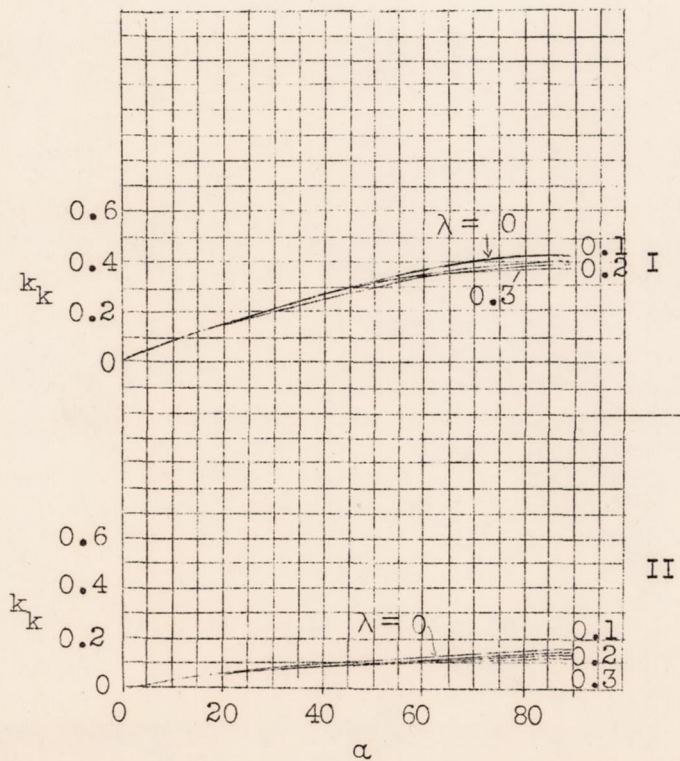
Fig.24

Moment of yaw

plotted against

α
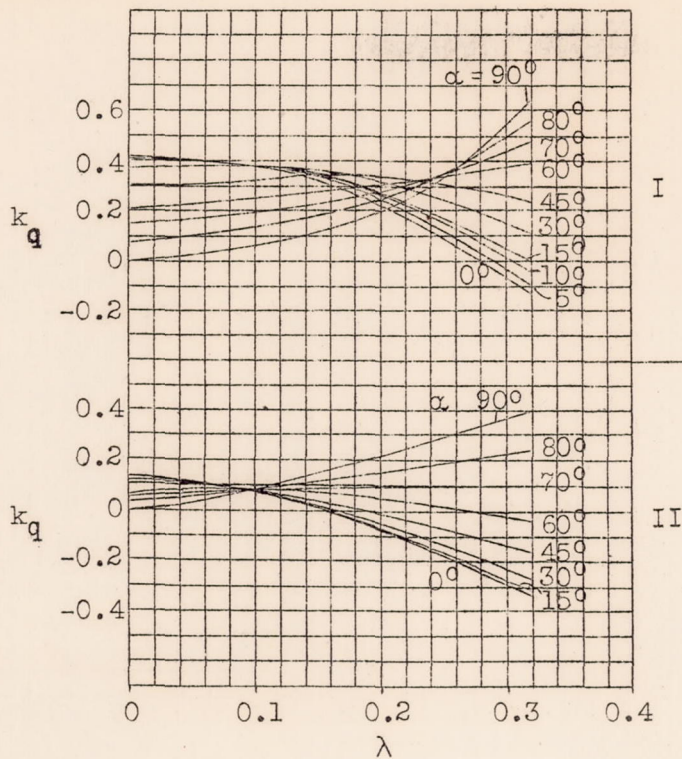
Fig.25

Lateral moment

plotted against

λ
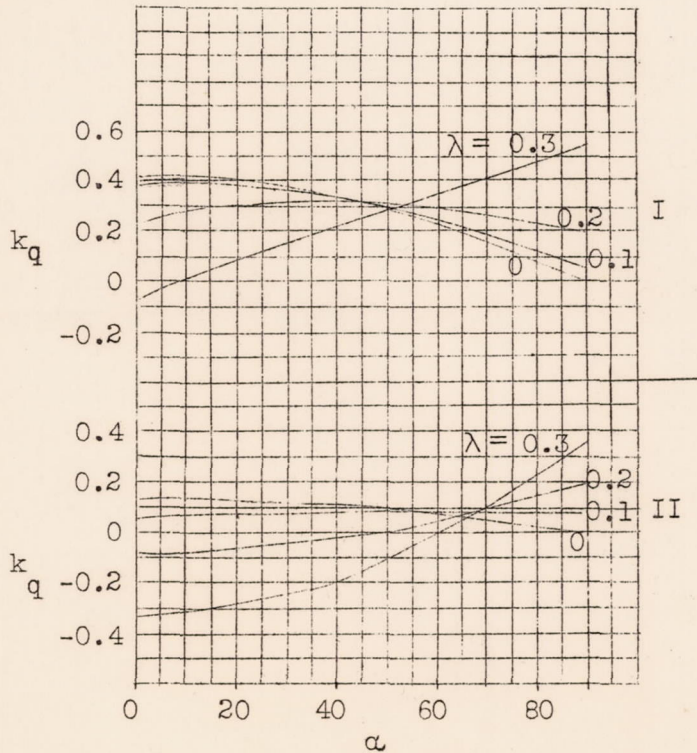
Fig.26

Lateral moment

plotted against

α
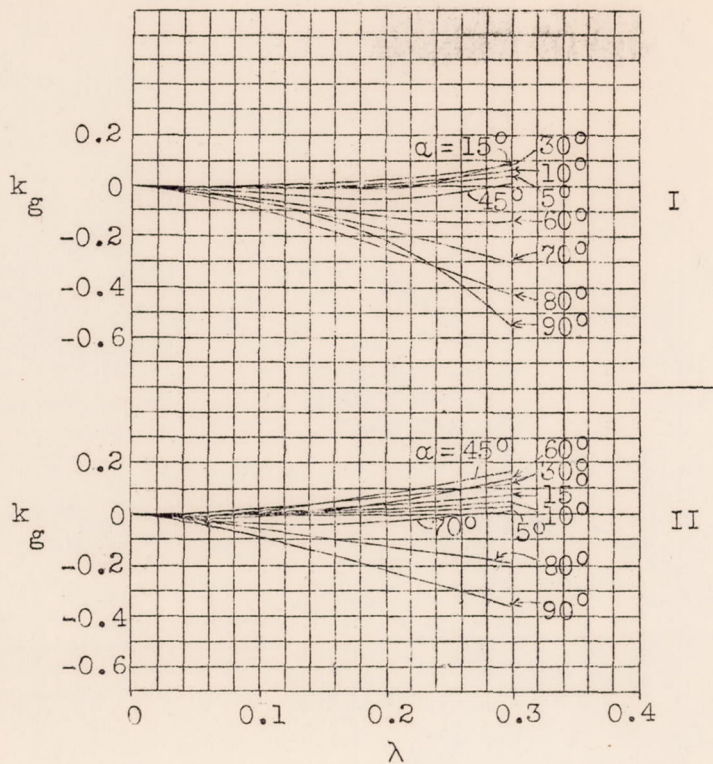
Fig.27

Moment of yaw

plotted against

λ
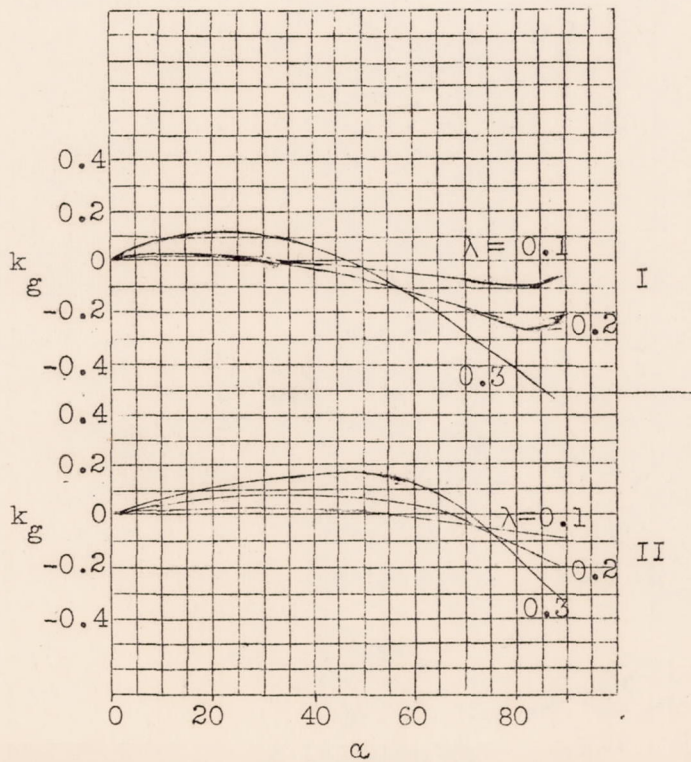
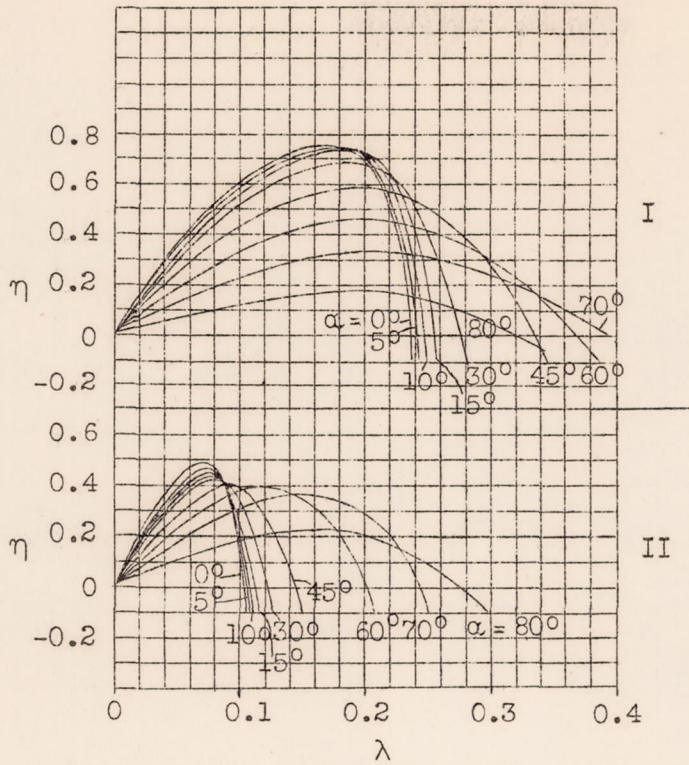Fig.28

Moment of yaw

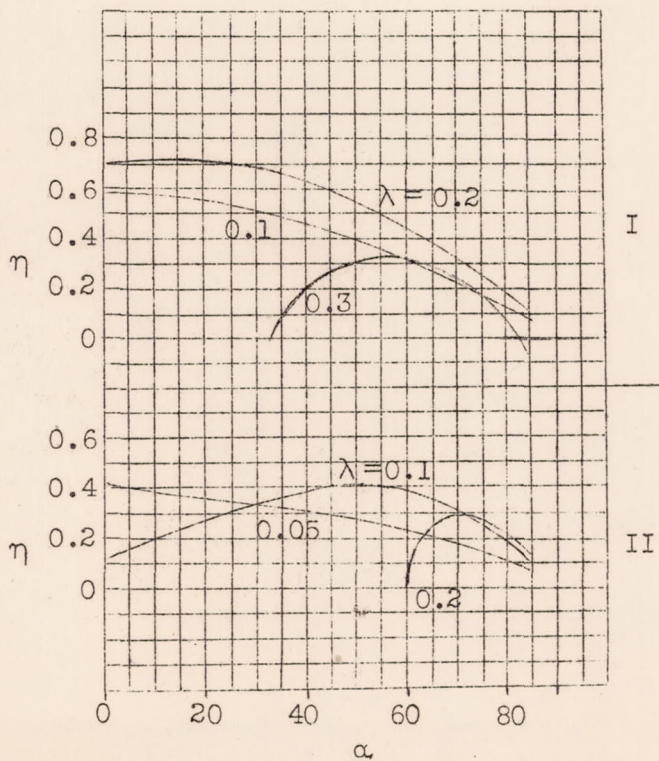plotted against

α

Fig.29

Propeller efficiency

plotted against

λ

Fig.30

Propeller efficiency

plotted against

α